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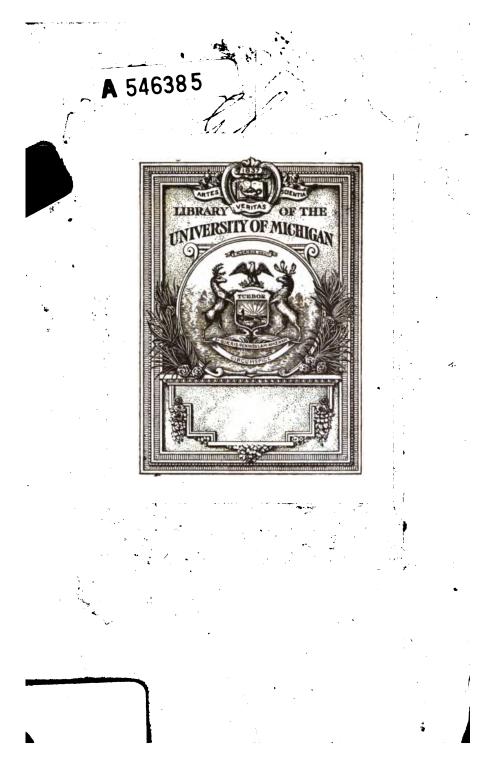
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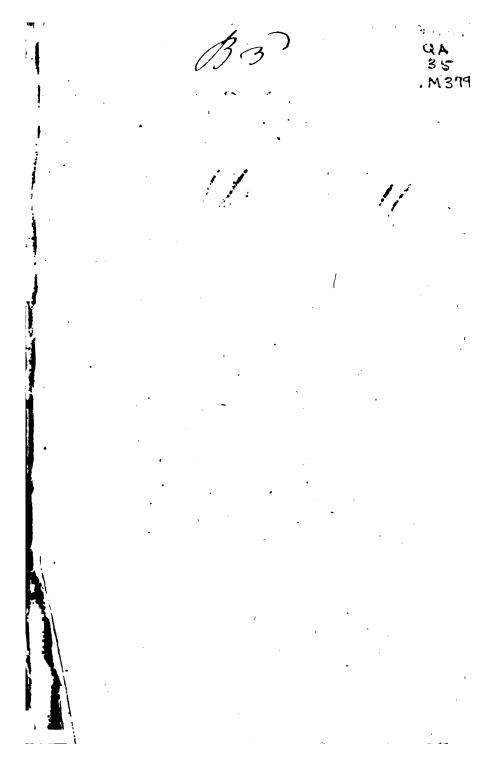
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ANEW

COMPLEAT and UNIVERSAL SYSTEM or BODY

OF

DECIMAL ARITHMETICK,

CONTAINING,

- I. The Whole Doctrine of Decimal Numbers, not only the Plain and Terminate, but also such as Repeat or Circulate ad Infinitum; and a Plain but Perfect Management of both, laid down and explained in all the Fundamental Rules of Plain Arithmetick, and by Logarithms.
- II. The Application and Use of Decimal Arithmetick in all the Parts or Branches of Arithmetical Science; viz. Vulgar Arithmetick, Vulgar Fractions, Duodecimal, and Sexagessimal Arithmetick; also in Algebra and Logarithms. In all which its Excellency and absolute Necessity is fully evinced.
- III. Its Application and Use in all such Parts of the Mathematicks as absolutely require its Affiftance; viz. Plain Trigonometry, and the Arts depending thereon; as, Navigation, Fortification, Altimetry, and Longimetry; Also the Mensuration of all Kinds of Superficies and Solid Bodies; and the Arts resulting therefrom; as, Gauging, Surveying, &c.
- IV. A New and Compleat Sett of Decimal Tables never before published, shewing by Inspection the Value of all Kinds of Decimals (without the tedious Methods of Reductions hitherto used) to four or fix Places of Figures; Also all the Common Tables very much inlarged, corrected, and improved; wherein all the Circulating Numbers are marked. With all other Tables of Interest, Annuities, Exchange, &c. necessary to render the Work compleat.
- V. An exact and accurate Canon of Logarithms for natural Numbers. And thro' the Whole, feveral Things new and useful, not here express'd.

By Benjamin Martin.

LONDON:

Printed for J. Noon, at the White Hart, near Mercers Chappel, in Cheapfide. M.DCC.XXXV. · · · · ·

The PREFACE.

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4-16-18.

I Prefume 'tis entirely needle's to write a Panegyric on the fuperlative Excellency of the noble Science of Decimal Arithmetick, fince the World has already been sufficiently apprized thereof in the extream Benefit and Service it has afforded the World of Mathematical Literature, even the' in its Embryo State; much less doth it need Encomiums to fet forth its Nature, Worth, and valuable Properties, which have been difcovered and illustrated by late Improvements; of which the enjuing Work is but (as it were) an Inflance.

The Book I here prefent the World withol is a regular System of this valuable Art, according to all the latest Improvements of others, and many (in the several Parts thereof) of my own; the two greatest of which are, The Dostrine of infinite circulating Decimals by the learned Mr. Samuel Cum; the other, A New Sett of Tables shewing the Value of any Decimal Part of any Integer, whether Money, Weight, Measure, Motion, Time, Sc. by Inspetiion only, to a sufficient Exactings, without the tedious Reductions bitherto necessarily used; which soft me not a little Time and Pains to calculate, but was necessarily to render this Art compleat.

The Foundation on which I have built this Superfructure is the abovementioned Gentleman's small, but learned, Treatife of the Doctrine of Decimal circulating Numbers: But that great Master having laid the Foundation deep, and in a great Measure out of the Vulgar Ken; I thought it might be of Service to young Students, a little to disclose and lay it more open to their View, and this was ull I at first intended to do; but having done that. Materials came in so fast, that I went on and erected the System of Decimal Science thereupon, as you here fee it; of which take the following Account.

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In

In the Fundamental Rules of the Art, viz. Addition, Subfraction, Multiplication, and Division, I have been as plain as possibly I could without Prolixity, and shewn the compleat and perfet Management of both Plain and Circulating Decimal Numbers in each of the Rules, in so easy and obvious a Method as the meanest Capacity, with proper Attention, may comprehend; and have taken care, in its proper Place, to give the true Reason, or Rationale, of each particular and different Process, especially of those relating to Circulating or Repeating Numbers of all Kinds, as I went on, omitting nothing that I could communicate towards the perfetting this fundamental and important Part.

In Reduction I have perfetted this Art beyond what it hath ever been; as I have not only largely exemplified all the common and oulgar Methods of Reducing to, and from Decimals, in all kinds of Vulgar, Fractional, Duodecimal, and Sexagefimal Numbers, by Arithmetical Operations; but bave compleated the Tabular Part, which has been bitberto very deficient, both in the Tables already extant. and in the Want of others. The first of these Defects I have endeavoured to supply by correcting, inlarging, and compleating the common Tables for reducing the various Deneminations of all Kinds of Quantities to Decimal Numbers; wherein I have taken care to mark all the Circulating or Repeating Numbers, Single or Compound, fo far forlb as they came within the Verge or Limits of the (aid Tables; which hath not till now been done by any. The other Defett, and that which renders this excellent Art most lame and imperfect, viz. The Want of proper Tables to express again the Value of a Decimal in the Vulgar Denominations, or known Parts of its Integer, without tedious and operofe Arithmetical Reductions, I have also supplied by the Addition of a compleat Sert of fuch Tables, and shewn their Use in Examples of all Varieties. The Reader may have a farther Account of thefe Tables in the Place where they are inferted ; of which I thall fay no more, but that these are the first Tables of this Kind that were ever published.

What I have bither to faid, relates purely to the Nature and

The PREFACE.

and Substance of the Art it felf; what follows concerns its Application to Arithmetical and Mathematical Sciences.

In Vulgar Arithmetick, I have applied the Dostrine of Decimal Numbers, both Plain and Circulating, in every Part; and shewn its admirable Use, Service, and Expediency thro' the Whole. Particularly I have facilitated the Business of Practice by a new Table and Method of Working by Decimals; whereby the Difficulty and the Intricacy of this Rule by common Arithmetick is avoided.

In Inchange I have been very particular and explicit, baving made this Affair (the Basis of Merchandise) more intelligible to meaner Capacities than I have met with it; explained the Nature and Meaning of the Par and Courfe. of Exchange, and have exhibited large and compleat Tables of both; fuch as are very rare to be found in Books of this Nature, they they are an indispensable Part of Decimal Arithmetick. The Rules of Interest, Simple and Compound, being of so great and general Concernment and Importance, and yet so little truly understood, I have taken abundance of Pains and Care to let young Students fee the Theory, or true Reason and Nature thereof. by a perspicuous Method of Resolving the most excellent Theorems of the late Mr. Ward, in Decimal Numbers : which in this Part of Arithmetick are absolutely necessary. And to facilitate and expedite Calculations of Interest, I bave procured a compleat Sett of Decimal Tables of Interest, and shewn their Construction and Use. In the other Parts of common Arithmetick, I have been large and clear, and omitted Nothing that I could contribute to perfest them. In fine, in every Part I have shewn the Neceffity and Expediency, and in the Whole, the Preference and superior Utility of Decimal Computations.

In Vulgar Fractions, I bave shewn how all Questions are most easily and commodiously resolved by Decimals; and for that End have calculated a Table shewing by Inspection the Decimal equal to any Vulgar Fraction whose Denominator exceeds not Twenty, I have extended the Table no farther, because those small Fractions are most frequent and useful in Busines.

In

In Deodecimal and Sexagelimal Arithmetick, I bave forcen the Nature and Rules of the Arts; and, by many Examples, how Questions are most advantagiously wrought by Decimal Numbers, especially in Duodecimals, so much as fed in Mensuration, I have also inserted compleat Tables for turning Duodecimal and Sexagesimal Numbers into Decimal ones, and such as are not to be found every where; wherein (as in all my other Tables) I have noted the Circulating Decimals, which no one besides bath done.

In the excellent Art of Logarithms, I have not only explain'd the Principles and Rules of the Art it felf, but largely shewn bow all Kinds of Decimals are managed and ordered thereby; others have tanght the World the Management of plain or terminate Decimals by Logarithms ; But that of circulating or repeating Decimals of all Kinds, hath fallen to my Province only, fince no one before has attempted I have here explain'd the Method of finding the Logađ. rithms of any Repetend, whether fingle or compound, pure or mixed with absolute Numbers, with more Ease and Certainty than can be found for any terminate Decimal exceeding the Numbers in the Canon. I have flewn how to work all Sorts of Decimals in all the Rules of this noble Art; and to make this Part of the Work compleat, I have inferted a Canon of Logarithms for Natural Numbers; where by Rules you are taught to find the Logarithms of any Number not exceeding 10000000, and the contrary.

In Algebra, the Use and Necessity of Decimals in raising and resolving Equations, I have demonstrated in a Select Number of the most curious and useful Questions relating to the Theory of Arithmetick, to the Philosophy of Motion, & c. and shewn how lame and imperfect, even this most perfect and perfecting Art would be without the Subservence of Decimal Numbers.

Hitherto of the Use and Application of Decimals in the several Parts of Arithmetical Science; in the next Place take what concerns its Application to the Principal Parts of Mathematical Knowledge.

In Plain Trigonometry, I have convinced the Reader how absolutely necessary Decimals are in order to express the the Quantity of the Sides of all Right-lined Triangles, in the Solution of all the Cales of Right and Oblique-angled Trigonometry. And as this Art is the Foundation and Effence of feveral others, as Fortification, Navigation, Menfuration of Altitudes and Diffances, &c. I have likewife fhewn the Nature and Rudiments of those Arts and Sciences, and the Manner of performing Conclusions by them in Decimal Numbers. So that any Perfon may here both learn the Art of Trigonometrical Calculation, and its Application to the aforefaid Arts, after the best Method, with the fame Ease and to as good Parpose, as from many Books wrote purposely on the Subject.

In the Menfuration of Superficies and Solids, no one will pretend to diffute the Superlative Use of Decimal Arithmetick; whereof the small Trass I have bere published is a fufficient Instance. I have not only taught how the measure more Superficies and Bodies than any other one Book that I know of, but show'd how this Art is the very Basis and Substance of Gauging, Surveying, and all other Kinds of Measurements used by Artificers, none of which can be obtain'd to any good Purpose without it; nor any Operations therein so well gerform'd as by Decimal Arithmetick; and here I have provided the Gauger with a Table of Multipliers or Divisors for finding the Content of any Superficies, or the Capacity of any Vessel in Wine Gallons, Ale Gallons, Corn Gallons or Corn Bushels, whether the Dimensions be taken in Inches, Feet, or Yards.

Thus I have given a general Account of the Substance of the Book; it would be endlefs to defeend to Particulars: Many Things of Importance in various Parts of the Book will offer themfelves to the View of the Reader unexpectedly, and appear in the whole, with the Face of Novelty. I have fpared no Pains in Confulting the best modern Authors on each particular Head as I went on, and extracted from them feverally whatever I found of value and Worth and would contribute to perfect my Defign; fo that nothing of Confequence can be found in any other Piece of Decimal Fractions (as this noble Art has been diminutively called) led) but what may be here met with amidst a great Variety of other novel, but useful and curious Matters.

So that upon the Whole I hope this Book doth truly merit the Title it hears, viz. A New Compleat and Universal System or Body of Decimal Arithmetick.

If then any Person be defirous of a Good and thorough Knowledge of Decimal Numbers of every Kind, and of their Compleat and perfect Management by the Rules of Art, they may be here fatisfied. If they would learn its Application, or bow to use it to the best Advantage in the various Arts, Trades, and Business of Life, they will here meet with plentiful Instructions, and Examples in every Sort, adapted to particular Cafes. Would they learn the true Grounds, or Rationale, of all Arithmetick whether Vulgar, Fractional, Duodecimal, Sexagefimal; and of the Mathematical Arts, Menfuration, Gauging, Surveying, Navigation, Fortification, Altimetry, Longimetry, &c. let them please to spend a few of their spare Hours bere. Are they disposed to learn the Use of Logarithms, or the Method of Trigonometrical Calculations, they are here with Eafe informed. In short, they may bere find in one fmall Volume, what I have been obliged to turn over many both fmall and great to procure ; and therefore if Variety, Utility, Novelty and Brevity can please, I hope the Publick will candidly accept my Labours. I am not apprifed of any Faults therein, and am very fure there are but few material Ones, baving taken all the Care and Pains I was able, to prevent them.

But if the well difpos'd and inquisitive Reader, after baving perused it throughly, *shall then judge it* deficient; I should be very glad if any thing better of the Kind should offer, that may afford him greater Satisfaction; and till then only, I entreat his kind Acceptation and candid Perusal of This.

VALE.

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INTRODUCTION,

CONCERNING

The Nature, Kinds, and Notation, of DECIMAL NUMBERS.

I. THE excellent Art of Decimal Arithmetick derives its Name from a LatinWorl (viz Decem, Ten) which denotes the Nature of its Numbers, which repréfent the Parts of any Integral

Quantity divided in a Decuple, Decimal, or tenfold Prc. portion.

2. Any Integer, or whole Quantity, being divided into 10, 100, 1000, 10000, Sc. Parts, because those Numbers are in a Decimal or tenfold Proportion; therefore such Numbers as represent any of those Parts, are call'd Decimal Numbers, or Decimals.

3. Thus, suppose I divide any whole Quantity into 10 Parts, and take 7 of them; those are called 7 decimal or tenth Parts of that Integer; and are thus vulgarly wrote $7\frac{7}{7}$; suppose it divided into 100, 1000, Sc. Parts; then 7 of them would be express'd thus $7\frac{7}{7-5}$, Sc. and read as before.

4. Also many Integers and Parts of another, would be expressed thus, $8_7\frac{7}{7}$, $19\frac{47}{1766}$, $475\frac{164}{17666}$, $2\frac{194}{16666}$, 56, and read thus; 8, and 7 tenths; 19, and 67 Hundreths, or Parts of a 100; 475, and 154 Thousandths, or Parts of a Thousand; 2, and 2946 Parts of ten Thousand. Thus the *Denominator* of Decimal Parts or Numbers, is always an Unite with Cyphers annexed.

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5. Therefore if the Places of Figures in the Numerator be equal in Number to the Places of Cyphers in the Denominator, (or be made equal thereto, by prefixing Cyphers;) the Denominator in fuch a Cafe will be known, though it be not written; and therefore in the Notation of Decimal Numbers, is always omitted; and the Numerator (ordered as aforefaid) alone is join'd to the integral Quantity, with a Comma, or Point, to diffinguish it therefrom.

6. Hence $\frac{34}{2 \circ 4}$; $\frac{47}{7 \circ 5^{2}}$; $\frac{277}{7 \circ 5^{2}}$; $\frac{277}{7 \circ 5^{2}}$; $\frac{4}{7 \circ 5^{2}}$; \mathcal{E}_{c} . are thus written, .34; .045; .C0271; .004. Alfo $27\frac{3}{1 \circ 5}$; $58\frac{4}{7 \circ 5}$; $129\frac{133}{7 \circ 5 \circ 5}$; $1\frac{7}{7 \circ 5 \circ 5}$; are wrote 27.3; 98,04; 129.0132; 1,0017. And on the contrary, by .12; 1.76; .006; 2,003); .001; we understand $\frac{12}{7 \circ 5}$; $1\frac{76}{7 \circ 5}$; $\frac{7}{7 \circ 5}$; $2\frac{37}{1 \circ 5}$; $\frac{7}{7 \circ 5}$;

7. Cyphers prefixed to decimal Numbers, decreafe their Value in a decuple or tenfold Proportion; as affixed to Integers, they increafe their Value in the fame Proportion: thus.5; .05; .005; .0005; Ec. are, as they proceed, each one ten times lefs then the preceding Decimal; as is eafy to conceive.

8. When the *Denominator* is an Aliquot Part of the Numerator increased by Affixing Cyphers thereto, the Decimal equivalent to such a Fraction, will be compleat and terminate; as, $\frac{1}{12} = .5$; $\frac{1}{12} = .25$; $\frac{1}{25} = .75$; $\frac{1}{25} = .05$; $\frac{1}{25} = .025$; $\frac{1}{25} = .1375$; $\frac{3}{25} = .003125$; $\frac{1}{25} = .6875$.

9. But if the Denominator be no aliquot Part of the Numerator thus increased; the Decimal equivalent to such Fraction will be interminate or endless; that is, it will constantly repeat one Digit only; as $\frac{1}{3} = .3333333$, Sc. ad infinitum; or $\frac{4}{5} = .666666$, Sc. or $\frac{7}{12} = .5833333$, Sc. or $\frac{1}{3} = .138888$, Sc. or $\frac{3}{3} = .032291666666$, Sc. fine fine.

10. Or elfe a certain Number of Figures perpetually Circulate, or repeat in the Quotient. Thus $\frac{2}{17} = .18$ 18 18 18, Sc. ad infinitum; also $\frac{1}{12} = .185$ 185 185 185, Sc. And $\frac{2}{12} = .952380952380$, Sc. And $\frac{1}{12} = .01$ 36 36 36, Sc. without End. And those Numbers which thus infimittely circulate or repeat, are most firly termed Reperends. Those which circulate a Digit only, are called a fingle Re*fetend*;

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Nature, Kinds, and Notation of Decimals. 2

petend ; and those in which several Figures circulate, are call'd a Compound Repetend, in the following Tract.

11. For the greater Elegance and Perfpicuity, in all the Operations of Circulating Numbers, I have dashed the first and last Figure of the Repetend; thereby making one Place of the Repetend sufficient. Thus the Examples above are thus wrote or expressed; 3; .8; .583; 128: .0322916. And the Compound Repctends thus; .18; .18; .52380; and .0138; herein following the Ingenious Mr. Cunn, the first Improver of this Part of Decimal Arithmetick.

12. In a Compound Repetend, any one of the circulating Figures may be made the first of the Repetend; for Instance, in the Repetend 8.6825 325 325, &c. it may be made 8.63252; pr 8.632932. And by this Means any two or more Repetends may be made to begin and end in the fame Place; and then they are faid to be conterminous.

13. Several other Things relating to the Nature and Propersies of circulating Numbers, I have interspersed in the following Treatife in their proper Places, where they may be undergood, and which are pot to be found in any other Book of Decimal Arithmetick.

14. In all Decimal Numbers, if the Point of Distinction be removed one Place towards the Right Hand, every Figure, and confequently the Whole Expression, will be increated in a tenfold Proportion; as in those Decimal Expressions 3.756, 37.56, 375.6, 3756. which are each. one 10 times greater than the preceding one. In which Proportion alfo, 'tis manifest, they decrease in Value, by removing the Decimal Point a Place to the Left. Hand.

15. The Nature and Properties of Decimal Numbers, are the fame with those of Integers or Whole Numbers, and the Method of Working both the fame (excepting Repetends). Hence ariferh the Excellency and fuperior Usefulnels of Decimal Arithmetick, above all other kinds of Computation.

16. To make the preceding Proposition evident, suppole 'twere required to express the Time fince our Saviour's Incarnation to the Year prefent, in Centuries and Decimal Parts of a Century ; it would be thus 17.33; where you observe one half of the Number confilt of Jutgers, and the other half of Decimals. But suppose the Time ex-B 2

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a constant

The Introduction, concerning the

Prefs'd in Years, the Number confiils of the fame Figures, 1733; and is whole or integral.

17. Hence 'tis plain the fame Number may be either Integral or Decimal, and that either in Whole or in Parr, according to what is made the Integer; for in the foregoing Cafe, if a Myriad be the Integer, the Time will be expressed by a pure Decimal 0.1733; if a Century be the Integer, by a mix'd Decimal 17.33; if a Year be the Integer, by the integral Number 1733; as before.

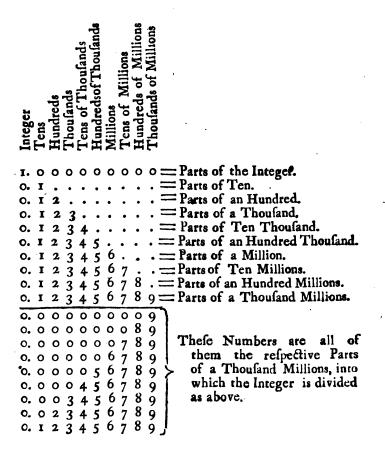
18. All the different Species, or Parts of different Kinds and Deneminations, of Money, Weights, and Measures, and all other Quantities, are to be reduced to Decimals, or may be expressed in Decimal Parts of their respective Integers, by proper Tables calculated for that Purpole; also any Decimal may very nearly by Inspection only (without the tedious Reductions hitherto used) be read in the vulgar Parts of Denominations of its respective Integer, by a Set of new Tables, which I have composed for the Ease of those who are conversant in this excellent Science.

19. Since then it has been fhewn that Decimals are the fame with whole Numbers, as to their Nature and the Manner of Operation; and that all mix'd Numbers, or fuch as confift of divers and different Demominations, are reducible thereto, and vice verfa; it follows that all the Arithmetick of mix'd and heterogeneous Numbers is to be perform'd by Decimals, with the fame Eafe, Expedition, and Pleafure as that of whole Numbers.

20. And by Confequence, That Vulgar Arithmetick, Vulgar Fractions, Ducdecimal and Sexagefimal Arithmetick, (those Paris of the Science of Computation hitherto deem'd fo hard and incricate, and therefore but little fludied or known) are all by this noble Art of Decimal Arithmetick perform'd with the utmost Fase and Pleasure, that any Arithmetick is capable of, and which I have abundantly evinced in the Sequel of the ensuing Work.

21. The Figures of a *Decimal Number* are to be numerated as those of whole Numbers, viz. from the Right Hand to the Left; but they must be denominated of the Number of Parts the Integer is divided into. The following Table will make the Numeration and Denomination of Decimals very eafy.

A TABLE of the Numeration and Denomination of DECIMALS.



An

An Explanation of the Characters and Abbreviatures used in the following Book.

It has been of late an Expedient to avoid Prolixity in Writing, to make use of some convenient and fignificant Characters to express those Words which most often occur, and occasion Tediousness and Tautology in the Work, the most irksome Vices that can attend it; and accordingly I have here used them; which, with their Significations, are thus to be understood.

Figure. Names.	Significations.
+ Plus, or mor	
- Minus, or 1	els. As a - b, is a lefe b; in Subraction,
× Multiplied	
- Divided by	
= Equal to.	Ass=b, is a equal to b; in Equat.
:? ls to.	As a: b .: c.: d; as a is to b, fo is
So is.	2 c to d; in Proportions.
G- Involved.	As 2. O, is the 2d involved.
w Evelved.	As 2 au, is the 2d evolved, or extracted.
✓ Surd Root.	Au y ab, y ab, y ab, y ab, Sc. is the Root 6quare, cub'd, biquadrate, Sc. of α a burd.

CHAP. I.

Addition of DECIMALS.

A Ddition of Decimal Parts admits of various Cales, according to their different Kinds; either as they are terminate and compleat, or interminate, and continually repeat either one or more Figures. I shall illustrate all the several Varieties by suitable Examples of Money, Weight, Measure, &c. Cafe I. If your Decimals be terminate, place Units under Units, Tens under Tens, $\mathcal{E}c.$ in whole Numbers, and annex the Decimals in order towards the Right Hand; then add them, and cut off from the Sum to the Right Hand fo many Places for Decimals as are equal to the greateft Number of Decimal Places in any of the given added Numbers:

EXAMPL Add togeth		gr. 2,4 1,0
The S	Sum 132,3125 = 132 - 6 - 3 -	Ø
Example II. Add together	$\begin{array}{c} l. Troy. \\ 457,825 \\ 570,065625 \\ 24,5375 \\ 806,253125 \\ 0,003125 \\ 695,05 \end{array} \begin{array}{c} l. 02. purt. \\ 43 \equiv 1 - 0, \\ 73 \equiv 8 - 15 - 4, \end{array}$	
The Sum	2553,73.43.75 = 2553 - 8 - 16 - 6	
		-

Cafe 2. If you have a great many feveral Sams to add, and their Decimals run to a great Number of Places, it will not be neceffary to add them all, but only fo many Places, as are fufficient to give the Value in the aggregated Sum, which will require but 4 or 5 Places, or 6 at most; for fo far only the largest Tables go.

Observe to make that Figure (at which you break off) more by a Unit, if the next rejected Figure be more than 5; but if the next Figure be less than 5, reject the Figures only.

Then add the feveral Sums, and the certain Places of the Decimal are generally fewer by one than the Decimal Places retained in any of the given Sums. I shall subjoin an Example at large, and the same thus contracted.

EXAMPLE

EXAMPLE.

4 7.9 ⁸ 2774354	ניין	47.98277
175.6732956	1 2	175.6733
2.43752432	contra	2.43752
97.702006764 276.92301762		97.70201 276.92302
30.00420999		30.00421
630.722828648		630.72283

In this Example there are 4 Places of Decimals certain, or the fame, in both Operations; and the Rule will fearce ever err *above an Unit* in the laft Place. Now whatever you fuppole the Integral Quantities to be, the *Tables* will fnew you the Value of the Decimal Parts.

Cafe 3. Suppose the Numbers you are to add have repeating Decimals; if they are fingle Repetends, make them all conterminous, that is, end together; and then add as before, only to the last, or Right Hand Place of Decimals, add as many Units as there are Nines in it; and that last Digit shall be one of the Repetends.

N. B. It may be proper to give the first and last Places of all Repetends a Dall with the Pen, for Distinction.

> E X A M P L E I. *l.* 124.273 64.516 0.733 59.800 *l. s. d. qr.* 3.873 5,30 = 1, -2,8845.016 5,73 = 14 - 7 - 8Sum = 297.773 = 297 - 14 - 7 - 3,68

> > EXAMPLE

EXAMPLE II.

Feet.
5 ,91 <i>8</i> 66
0.0208%
2.56250
4.83333 F. In. qrs.
6.041665,16=17
2.866663,04 = 1.92
Sum = 22,04186=22- C-2

EXAMPLE III.

Oz. Troy Wt	• ,		
4,727083			
2.583333			
0.002083			
9.0291\$6			
4.031250			
7.035418	oz.	pwt.	gr.
10.758333	5,33		- 1,58
6.91\$666	1,08	= 1 -	- 14,4
45.083333:	= 45	-1-	- 16

EXAMPLE IV.

۱

Days.	•		
275.252 777	Υ.		
47 87.111			
436.027083			
10.627777			
101.255555	D.	H.	•
127.769444 5	,20 =		• 2,8
243.958333 2	,81 :	= 19 -	- 26,4
Sum = 1242.81208z ==	1242 -	- 10 -	- 20.2

С

Cafe

9

- --

Cafe 4. If your Decimal be a compound Repetend, that is, confifts of feveral Places of Figures which continually repeat or return; the Sum or Aggregate of any given Number of fuch Decimals will also repeat; and the Number of Places, or of the Figures, in each repetend, will be equal to the leaft common Multiple of those feveral Numbers which reprefent the Places of Figures in the Repretends added. Hence (tho' it be fearce ever neceffary to have above five or fix Places of Decimals, yet) if any one be minded to fee the Repetend compleat, he must observe this Rule;

From the Place where all the Repetends begin together, continue each Decimal to a Number of Places equal to the *Multiple aforefaid*; then add, and to the last Place add as many Units as there are 10's in the Place where the Repetends all begin together, and the Figures in those two Places are the *first* and the *last* of the *Repetend*. The Examples following will make all plain.

EXAM.	$I. \begin{cases} 13 \cdot 046x & l. s. d. qr. \\ 2 \cdot 004y \\ 5 \cdot 723x \end{cases} \begin{cases} .50 =1 - 1.78 \\ .37 = 7 - 4 - 3.2 \end{cases}$
•	Sum $21 \cdot 3760 = 21 - 7 - 6 - 1$

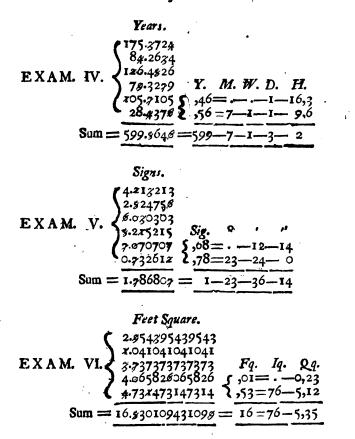
	• ·	C. i	Wt. /	ร์ข.					
EXAM.	c ¹	4 ·	472	958	С.	Q.	<i>lb</i> .	oz.	d r.
EXAM	п У	2 .	307	243	(,38=	=			1,09
	••• \$	9 •	a20	763 .	\$, 33=	=	••••	• <u>5</u> —:	14,61
	(Ι.	9 I2	37\$	(,71 =	- 2	23-	- 8	5,12
Su	m = 4	17 ·	713	338 =	= 47-	-2-	-23-	14-	4,82

Rods.

ЕХАМ	. 111.	121 · 47237 80 · 27\$55 64 · 90\$3# 89 · 07#44	$\begin{array}{c} R. Yd. \ F. \\ \mathbf{x}_{3,87=,2} \\ \mathbf{x}_{3,72=3,-2} \\ \mathbf{x}_{3,72=3,-2} \end{array}$	In. 1,73 0,56
	Som 🗯	355 . 72872	=355-4-0-	0,3

EXA M-

10



These Six Examples, I imagine, are sufficient to illustrate this last Case of compound Repetends ; but if it chances to happen that a compleat or terminate Decimal be to be added with them, you must attix Cyphers thereto, to esteem and deal with them as a Repetend.

C 2 C H A P.

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CHAP, II.

SUBSTRACTION.

Cafe I. T F your Decimals be terminate and compleat, place as directed in this Cafe of Addition, and Substract as in Whole Numbers; imagining all the vacant Places fill'd with Cyphers.

EXAMPLE I.

	L.					
From	729.4726 634.927	5	,56=	=	- 1-	-1,38
Substract	634.927	ι	<u>,54</u> =	=10-	- 9-	-2,4
Remains	94.5456	=	94:	10	: 10	: 3,78

EXAMPLE IL

	С.	Ç.	Q.	<i>lb</i> .	oz.	dr.
From	472,07 392,4354	,46=	=		-8-	-3,88
Subitract	<u>392,4354</u>	L <u>,</u> 03=	=2-	-14-		5,39
Remains	79,6346 =					

EXAMPLE III.

	<i>lb</i> .	lb. oz. pwt. gr.
From Subtract	147,	$\begin{cases} ,52 = -1 - 5,95 \\ ,27 = 3 - 4 - 19,2 \end{cases}$
Şubtract	94,7248	1,27 = 3 - 4 - 19,2
Remains	52,2752	= 52 - 3 - 6 - 1,15

Cafe 2. If your Decimals run to many Places of Figures, do as directed in the Cafe of Addition; and fut firact as in the Laft Cafe; and the laft place of the Decimal Remainder will never Err more than an Unit.

Substraction of Decimals.

EXAMPLE I.

From 2,752804624 take 1,476937679.

	Miles,	М.	F.	P.	Y.	F.	In.
		5,67=					1,23
Thus, ${$	2,752805 1,476938	3,58=	=	·1	4-	-2	1,14
			-			The state of the s	
Remains	1,275867	= 1-	-2-	-8	-0	-I	6,57

In this Example the last Figure 7 is a Unit too much, but that is not to be regarded; for in this Cafe the Value of a Unit in that Place is but ,063 of an Inch.

Cafe 3. If your Decimal repeat Single Figures, proceed (as in this Cafe of Addition) to place them, and fubfrace as ufual; except that when the Subtrahend is the greater Number, you must increase the upper Figure by 9 only, and in every fich Cafe carry one to the next Place.

EXAMPLE L

	L .	1.	s.	d.	gr.
From Subftract	54,73333 { 17,2541\$,91 = ,77=	= • - =15 -	-2 -4	0,73 ·3,2
Remains	36,77916=				

EXAMPLE II.

	L.	1.	. 5 .	d.	qr.
From	57,5289 49,5833	5,56=	•	- I	-1,38
Substract	49,5883	2,94=	-18	- 9-	-2,4
Remains	7,945	=	-18-	-10-	-3,78

EXAMPLE III.

From Subfiract	Hogsbeads. 1672,4518 879,3000				
Remains	793.1518=	7	193-	-9	4,4

EXAMPLE IV.

	Loads.	L.	Q.	B.	G.
From Substract	472,222 § 346,178	,60= ,04=	=		1,92 4 ,8
Remains	126,048 =	-	-		and successive states

EXAMPLE V.

	Years.	Y .	М.	W.	D.	H .
From		5 ,8 8:				
Substract	,00831\$	2,94	=12-	-I-	.o	2,4
Remains	47,948883	= 47	-12-	-1-	-3-	-7,48

Cafe 4. If the Decimals be compound Repetends, order them as directed in the Cafe of Addition; then fubfiract; and look if you must berrow one in the Place where both Repetends begin together; if fo, you must add one to the Right-Hand place of the Subtrahend; and the Remainder either Whole or in Part, will thew the Repetend.

EXAMPLE L

	L.	ι.	s.	d,	qr.
From	47,4 <i>*</i> 78178 15, <i>58</i> 56565	\$,21=	×	هيمرو مي	-2,01
Substract	15,5\$56565	2,85=	=17-	-0-	-0
Remaius	31,8\$21612 :		-17-	-0	-2,01

EXAMLE II.

From Subfiract	Ounces. 153.ø2749 142,8935 3	Oz. pw. gr. \$,49=- 2,35 \$,07=1-9,6
Remains	11,07498 :	= 11-1-11,95

EXAMPLE III.

,	Rods Sq.	Rq. Yq.	Fq.
From	75.5333	{,35= ,77=23-	- • 94
Substract	42.7597	1,77=23-	-2,44
Remains	32.7738 =	= 3223	-3,38

EXAMPLE IV.

From Substract	47.8\$40260	Y. F. In. Q. $\begin{cases} ,81 = 1, 16 \\ ,92 = 2 - 9 - 0, 48 \end{cases}$
Remains	6,9#8100#	= 6-2-9-1,64

EXAMPLE V.

Days. D. H. M.

From Substract	75.2758000 {,94=
Remains	27,919443 = 27 - 22 - 3,93

EXAMPLE VI.

	Degrees.	Ď. / ″
From	49,5285285	\$,49=17,64
Subfiract	38,4736000	7,05=3-0
Remains	11,0549285	= <u>11-3-17,64</u>

CHAP.

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CHAP. III.

MULTIPLICATION.

Cafe I. T F your Decimals be compleat and terminate. whether they be pure or join'd with Integers. Multiply them as if they were all whole Numbers; and cut off (to the Right-Hand) fo many Places for Decimal Parts in the Product as there were in both the Multiplier and Multiplicand counted together. But if it fo happen that there are not fo many Places in the Product, fupply the Defect by prefixing Cyphers.

EXAMPLE I.

12	9636 848 }	Fq. Inq. , $60 =$, $51 = 73 - 780 - 74$	Qr. 13,8
Product 780	0,516 =	780-74-	- 4,84

EXAMPLE II.

Multir	b y 42,5 1	Yards.
	425 17004 8502	
Preduct	10,2499	1 = 10 - 2 - 35,88

EXAM-

۰.

Multiplication of Decimals.

EXAMPLE III.

Multiply 78,546 by 436	Miles,
471276 235638 314184	M. Fq. R. Y. F. In. $\begin{cases} ,60 \Rightarrow -1 - 5 - 0 - 1,8 \\ ,05 = -16 - 0 - 0 - 0 \end{cases}$
Product 34246,056	= 34246 - 0 - 17 - 5 - 0 - 1,8

`.. .

EXAMPLE IV.

Mult	ipl y by	,02365 ,0435	} of a Mile.
		11825 7095 9460	$Mq. Aq. Rq. Pq. \begin{cases} ,28 = 2,85 \\ ,10 = 0 - 2 - 22,4 \end{cases}$
Product	,00	1028775	= 0 - 0 - 2 - 25,25

Cafe 2. When it happens that the Places of Decimals run far in both Factors, and confequently would make a very large Decimal in the Product, you may contract your Work, in fuch a Cafe, to as few Places of Decimals in the Product as you pleafe, or is fuitable to your Defign, by the following *Rule*, viz. fet the Units Place of the *Multiplier* directly under that Figure of the Decimal Part of the *Multiplicand* whose Place you would preferve in the Product.

Then invert, or place all the other Figures of the Multiplier in a contrary order to the common way.

Laftly, in Multiplying always begin at the Figure of the Multiplicand which flands over the Figure wherewith you are then a Multiplying, fetting down the first Figure of each particular Product directly under one another. But withal take care to fee what Increase would arise from the Multiplying of the two next Right-Hand Figures of the Multiplicand, which you must constantly add to the first Figure in every Product.

EXAM-

17

D

EXAMPLEI

Suppose I would multiply 92.412031 Yards by 47,29195 Yards, and to have only four Places of Decimals in the Product.

Place them as before directed, and they will fland

Thus { 92,412031 59192,74	The Multiplicand as usual. The Multiplier inversed.
36964812,	
6468842	·
184824	
83171	
<u>9</u> 24	
832	N.
4370,3451	•••

The Reason of, and how great a part of the Work is faved by, this Contraction, will appear from the Operation at large.

Thus $\begin{cases} 92,412031\\59192,74 \\ 46 \\ 2050155 \\ 831 \\ 708279 \\ 924 \\ 12031 \\ 83170 \\ 8279 \\ 184824 \\ 062 \\ 6468842 \\ 17 \\ 36964812 \\ 4 \\ 4370,3451 \\ 4935045 \\ \end{cases}$

Hence it appears, that balf the Work is uselefs, viz. all those Figures included in the Square, whose Sum make indeed 7 places of Decimals, but are of no value, and therefore superfluous.

EXAMPLE II.

Multiply 14,794, by 12,123; and to have thereby referv'd **two** Places of Decimals in the Product, place them

Thus {14,794	The common way { 14,794		
321,21	at large. { 12,123		
14794 2959 148 30 <u>4</u> 179,35		4 4382 29 588 147 94 2958 8 14794 179,34 7662	

" EXAMPLE III.

Multiply 257,356 with 76,48, and for an Intire Product of Integers, place them as by the Kule

Thus {257,350 84,67		The fame \$ 257,356 at large. \$ 7648
18015		20 58848 102 9424
	-	102 9424
103		1544 136
20		18014 92
19682		19682, 58688

From these Examples, tis manifest how advantagous these compendious Contractions are to facilitate and shorten the Work of those long and operous Calculations and Computations, which the experienced Practitioner finds occur but too often in Arithmetick, Algebra, and Geometry.

Cafe 2. If the Multiplicand be a Repetend only, and the Multiplier a fingle Digit, Multiply as usual; only observe to add in the last place of the Product as many Units as it contains Nines, and that place is a Repetend.

D 2

EXAM-

20

EXAMPLE L

	Signs of the Zodiack.
Multiply by	10,701# {,83=15-0 5 {,50=15-0-0
	5,5083 = 5 -15-15-0

EXAMPLE II,

Multiply by	9,30#Z ,7S	Yards. {	Fq. In. q. ,80=,-10,33 1,13=1-24,48
Product	65,138	m	65-1-34,81

EXAMPLE III.

Multiply by	476,05 } ,08 }	Poles.	$\begin{array}{c} Yq. \ Fq. \\ 44 =1,18 \\ .08 = 2 - 3,76 \end{array}$
Product	38,08 <u>4</u> 4	=	38-2-4,94

But if the Multiplier confift of feveral Digits or Figures, then make each particular Product conterminous, by continue ing the fingle Repetend of each towards the Right-Hand.

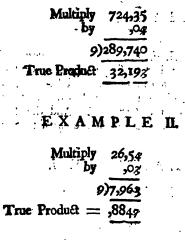
EXAMPLE L

Muki	内内	748,6 4 ,634
	4	299457 2245983 4918#66
Product	47	4,63057

E

If the Multiplier be a Repetend, multiply as ufual; but in the Product, cut off one place lefs for Decimals than ufual (which is all one as multiplying by Ten) and divide by Nine; continue the Quotient till it becomes a Single or Compound Repetend; and this thall be the true Refuls or Anfwer.

EXAMPLE L



EXAMPLE III,

Multi	ply by	251,43 8,7 4
	9)	100,473
		111638 76001 91144
Product	21	98,604\$

EXAM

Ĩ.

EXAMPLE IV.

:

Multiply 48,7 2,1,3 9)146263 1625.148 1 487544 9750888 Product 104,0094

Cafe 4: If the Multiplicand be a Compound Repetend, and the Multiplier but a fingle Digit, Multiply as in Cafe the First; but observe to add to the Right-Hand Place of the Product fo many Units as there are Tens in the Product of the Left-Hand Place of the Repetend. And the Product shall contain a Repetend whole Places are equal to those in the Multiplicand.

EAAMPLE I. Multinite \$82.247

by	8	• 7	31 · TA
Produce	4658,778		

EXAMPLE H

Multiply -	- 592 ,6378
by	,03
Product	177,78135

EXAMPLE III,

Multiply	37 <i>#9,23</i>
by	,007
Product	26,24164

l£

If the Multiplier confifts of Places more than one, make all the feveral Products conterminous towards the Right-Hand, as taught in the last Cafe.

EXAMPLE L

Multipl	y 7 3,2\$8ø
Ъ	
	5128200
	21977597
	293134534
Product	3202,40538
	and the state of t

EXAMPLE II.

Mul	tiply by	4027,301 <i>2</i> 43 7 0,2
		805#6025 819x108911
		0829038190 0920509205
Product	1760	0112,02332

But if not only the Multiplicand, but the Multiplier also be a Compound Repetend, Multiply (as has been before taught,) each Figure of the Repetend, and add the feveral Products together; Then add the Refult to it felf in this Manner, fet the first Left-Hand Figure fo many Places forward as exceeds the Number of Places in the Repetend by one; and the Reft of the Figures in order after it; and thus proceed till the Refult last added be carried beyond the first; Lastly, add these feveral Refults together, beginning under the Right-Hand Place of the first, and from thence dash as many Figures for a Repetend, as the Repetend of the Multiplier does confist of.

EXAM.

ÉXAMPLE L Makiply 235,01 3,20 by 151006 67002 70503 First Product 7871326 7871326 7871326 True Product 787,9205 EXAMPLE II. Mukiply 432067 ,02436 by 2592402 1296201 1728268 884134 First Product 1052515212 1052515 84. 105 80. True Product 10526,2047# EXAMPLE III. Multiply 42710,36 ,20403 Dy 12813108 17084144 8542072 First Product 8714,1957508 87141957 Sc. 871 Sr. True Product 8714,2828936

F

If the Multiplier has any terminate Places join'd with the Repetend, and if the Repetend be fmall and these many, the best way will be to multiply and add the Products of the Repetend first; then after multiply by the terminate Figures, and add their Products to the Sum of the Product of the Repetend; and to this last Refult add the faid Sum of the Repetend Products, as in the last Examples.

EXAMPLE.

Multiply 432,43 by 23,414 172972 43243 The Sum 605402 of the Product of the Repetends. 172972 129729 86486 FOI2491602 605402 6054 Sc. 60 Sr.

But if the terminate Figures are few, and the Places of the Repetend are many; the flortest way will be to fubfiract the terminate Figures from those of the Repetend, and multiply by the Remainder as a Repetend.

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EXAM-

CHAP. IV.

DIVISION of DECIMALS.

DIVISION of Decimals is perform'd in the fame manner as Division of Integers, both in regard of placing the Numbers, and the Work it felf.

The *ibiefeft Difficulty*, in general, is to different the true Value of the Quotient Figures, that is, how to feparate juffly the Integers and Decimals it contains. However the Business of Valuing the Quotient is render'd very plain and obvious, by a due Observation of either of the following Rules, viz.

Rule I. The Quotient Figure is always of the fame Value with that Figure of the Dividend, under which the Units Place of its Product stands. Or thus,

Rule II. The Decimal Parts in the Divisor and Quotient must be always equal in Number to those of the Dividend.

Some Authors give one of these Rules, and fome the other; but I have supplied you with both, that nothing may be wanting to render this necessfary and frequent Part of the Art as easy and ready as possible.

From the fecond general Rule may be deduced these four particular and very useful Directions, viz.

1 Direct. When the Decimal Places in the Divisor and Dividend are equal, the Quotient will be whole Numbers.

2 Direct. When the Places of Decimals in the Dividend exceed those of the Divisor, the Decimal Parts in the Quotient must be equal to that Excess.

3 Direct. If the Divisor exceed the Dividend in Decimal Places, annex Cyphers to make them equal, then will the Quotient be Integers, by Direct 1.

4 Direct: If after you have finished Division and find not fo many Figures in the Quotient as there ought to be places of Decimal Parts by the general Rule, supply that Defect by prefixing Cyphers to the Quotient.

The Learner being thus fraught with general Rules and particular Directions; canner, I think, without Impeachment of his Ingenuity, require any thing farther to be faid or done to

, 28

to make Division of Decimals evident and easy, except the Operations themselves in all the various Cales; to which I now proceed.

Cafe 1. When your Decimals are compleat and foon terminate, place them and work as in Whole Numbers, having a first regard to the Rules and Directions before given for Valuing the Quotient.

In Division of Decimals there may happen Nine Varieties, with respect to the Nature of the Numbers, which may be of three Sorts; viz.

First, Integers; or Whole Numbers.

Secondly, Mixt; confifting of Integers and Decimals.

Thirdly, Pure Decimals; without any Whole Numbers. Now the Dividend being it felf of three Kinds, and capable of a Divifor of three kinds, there follows of confequence, these nine Diverstites, viz.

Any Whole Number may be divided by a *Whole Number* may be divided by a *Mixt Number*. Decimal.

A Mixt Number may be divided by a 2 Mixt Number. L Decimal.

A Pure Decimal may be divided by a Mixt Number. Decimal.

I shall explain and exemplify this by one Example, viz. by 1722 divided by 12 thus, at large.

12) 1722.0 (12	[143.5
• 52 48	••••
• 42 36	
· 60	•
••	

Here

Here you fee the Divisor and Dividend are both whole Numbers; and because there was a Remainder of 6, 1 borrow a Cypher in order to divide it off clean, which gives (by Direct 2.) one Place, to wir, 5 in the Quotient for a Decimal. I shall subjoin this one Example varied according to all the Varieties aforefaid.

Variety	I I2)1722.0 (143,5	by Direct. 2.
	2-12)172,20 (14,5	by Direct. 2.
	3 12),17220 (,01435	by Direct. 4.
	4	1435	by Direct. 1.
	5-1,2)172,20 (143,5	by Direct. 2.
	6— — I,2),17220 (,1435	by Direct. 2.
•	7	14350	by Direct. 3.
	8,12)17,220 (by Direct. 2.
	9,I2),17220 (1,435	by Direct. 2.

But notwithftanding I have given a Specimen of all the Varieties in the last Example, and pointed to the Direction, by which each Quotient was form'd; yet 'twill be neceffary to illustrate the general Rule by Examples wrought at large, wherein the immediate Ufe of the particular Directions will more obviously appear.

Example 1. Wherein the Places of Decimal Parts in the Divisor and Dividend are equal.

8,45) 295,75 (35	,0074) ,4884 (66
2535	444
• 4225	444
4225	444
• • • •	•••

Here because the Decimals in Divisor and Dividend are equal in Number, therefore the Quotients in both Instances are whole Numbers, by Direct. 1.

Example

Example 2. When the Decimal Parts of the Dividend exceed these of the Division.

24,3) 78 0,516 (32,12	,0067) ,3953 (,59
729	335
515	· 603
486	603
- 291 243	•••
486 486	

In this Case the *Excess* is cut off in both the Quotients for Decimal Parts; by *Direct.* 2.

Example 3. When there are not fo many Places of Parts in the Dividend as in the Dividor.

7,68 4) 192,100 (25 • 15368	·	,7875)441,0000 (560		
• 15300			39375	
· 38 420		•	47250	
38420		•	47250	
		•		

Here Cyphers are annexed to the Dividend, to answer the Decimal Places of the Divisor, that the Quote might be whole Numbers; as in Direct 1. by Direct. 3.

Example 4. When, after Division is finished, there are not so many Figures in the Quotient as there should be Decimal Parts by the General Rule.

957) 7, 25406 (,00758	,575),0007475(, 0013
6699	575
5550	1725
4785	1725
7658 7656	
• • • •	· 1

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In both these Inflances, by Direction 4. I prefix Cyphers to the Quotients, that together with those in the Divisors they anight be equal to the Decimal Places of the Dividend.

If any Whole, Mixt, or Decimal Number is given to be divided by 10, 100, 1000, Sc. you only remove the feparating Point towards the Left-hand fo many Places as there are Cyphers in the Divisor; as on the contrary in Multiplication, the feparating Point is moved to the Right-hand fo many Places as there are Cyphers in the Multiplier.

Division. Multiplication. 10)1523(152,3 1,523 X 10=15,23 $1,523 \times 100 = 152,3$ 100)1523(15,23 $1,523 \times 1000 = 1523$ 1000)1523(1,523 ,0072 X 10= ,072 10)72 (7,2 $,0072 \times 100 = ,72$ 100)72 (,72 ,0072 × 1000 = 7,2 1000)72 (,072 $,0072 \times 10000 = 72$ 10000)72 (,0072

EXAMPLES in

I shall next give a Method whereby you may work any Cafe of Division by Multiplication, and vice versa, any Cafe of Multiplication by Division; and this, in many Instances, will be found very excellent and useful.

PROBLEM I.

Suppose I have any Number, 7315, to multiply by any other Number 125; but yet have a mind to divide the faid Number, and to have a Quotient equal to the Product of those two Numbers; Quere the Divisor?

Rule. Divide a Unit with Cyphers annexed by the given Multiplier, and the Quotient is the Divisor fought.

EXAMPLE.

1000

Given Multiplier 125) 1.000 (,008 = the Divisor fought.

Then

Division of	Decimals. 33
Then { Multiply 7315 by 125	,008) 7315,000 (914375 72
36575 14630	II 8
<u>7315</u> 914375	35 32
-	30 24
	60 56
	40 40
	40

Thus I have obtain'd a Quotient the fame as the Product. Q. E. I.

PROBLEM IL

Suppose I have any Number 7315 to be divided by any other Number ,008; but would multiply the faid Number, and have a Product equal to the Quotient of the fame Number divided by ,008; Quere the Multiplier ?

Rule. Divide an Unit, with Cyphers annexed, by the given Divisor, and the Quotient will be the Multiplier fought.

,008) 1000 (125 = the Multiplier fought. $\frac{8}{20}$ 16 40 40 ...

Thus you fee this, and the Remainder of the Work, is only the Reverse of the former; and therefore need not be repeated.

Cafe

Cafe 2. If your Divisor confift of many Places of Decimal Parts, the Work may be very much contracted, and yet a just Quotient obtained by the following Rule. Having determin'd the Value of the Quotient Figures, proceed in multiplying the Divisor with the first Quotient Figure as usual; but for every Figure after, in multiplying, omit or prick off one in the Divisor; still having a due regard to the Increase, which would arise from the Figure and Figures so omitted.

EXAMPLES.

Contracted.

At large.

7,9863) 70,2300 (8,7938 ···· 638904	7,9863) 70,2300 (8,7938 638904	
• 63396	63396 0	
55904	55904 I	
•7492	7491 90	
7187	7187 67	
• 305	304 230	
239	239 589	
• 66 63	64 6410 62 8904	
-31	0 7506	

Tho' much Labour be this way faved, yet it is not proper to use it unlefs the Decimals in the Quotient be fure to four or fix Places; fince 'tis obvious, the next Place, or all the Remainder of the Quotient in the contrasted Work would be three times more or greater than the fame in the Work at large.

If the Dividend contain many Places of Decimals, there's no occasion for using but a very few of the first, as appears by this second Example.

2

EXA M-

-)

` E X	K A M I	PLE N.
3,141592)	165,6995 1570796	001296 (52,7438
	86199 62831	
	23368 21 <i>9</i> 91	• • •
•	1377 1256	• • • •
· · ·	121 94	• • • • •
•	27 25	
	2	· · · · · · · · · · · · · · · · · · ·

Here you may observe, that of Ten Decimal Places in the Dividend, I have used only Four; and yet have a Quotient to four Places of Decimals true : Hence all the Figures which would have fill'd the dotted Space, had it been work'd at large, are *superflueus*; and those, tis evident, make balf the Work.

Cafe 3. If your Dividend contain a fingle Repetend, and your Divisor be a fingle terminate Digit, divide as usual; and when you take down your Repetend, the Quotient will begin to repeat.

EXAM.L	EXAM. II.
4) 195,02 (48,75	,6) 3176,0 (5293
16	30
35 32	17 12
	56
30 28	<u>54</u>
22 20 } Ad Infinitum	$\begin{array}{c} 2 \vartheta \\ 18 \end{array} \} A d Infinitum.$
2	F 2 If

 i_i 3.1

36

If the Divisor be any Number of terminate Digits, the Quotient will repeat a fingle Digit; but not always begin, when the Repetend is taken down.

EXAM. III.	EXAM. IV.
	,65)106036,78 <i>3</i> (217,#
48	97530
312	85067
288	48765
248	363028
240	341355
66	216733 ad infinitum.
48	1950605
186	21673
144	
4267 at infinite	
420 384 ad infinitum.	
• 42	

If your Divisor be only a fingle Repetend, and the Divisdend a terminate Number, multiply the Dividend by 9, onoting off one more Right-hand Figure in the Product, which is now your new Dividend; then divide as usual, and the Quotient will be juft.

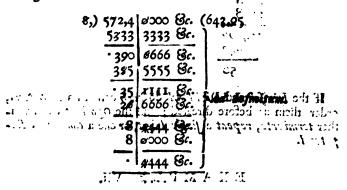
E X A M P L E The Dividend == 57 Multiply by	72,4 9	Divide 51		
Divisor $= .8 \times 51$	5,16	= the new	Dividend.	
Divisor = $, \frac{51}{48}$	<u> </u>	643,95 =	the true Q	uotient.
• 3'	5		. .	•
3:	ź		•	
	I		-	
2	4			
	76			
	72			
-	40	·		
	40			
	• •	•		Other-

Otherwise thus; place the Dividend under it felf, but one Place forward to the Right-hand; And then substract, the Remainder will be the new Dividend, the same as before.

		The Dividend The fame placed	572,40 5724	as before. 31.2 one Figure forwards.
<u>,</u>	• ,			Dividend as before.

From hence also appears the Reafor of cutting off one more Figure in the new Dividend for Decimal.

That either of these Ways will give the fame Quotient you have seen, and that the Quotient this way produced is the only true one will appear from the Work of the last Example at large.



In this Operation, tis manifed though the Reptiends in every particular Step would proceed to Infinity, yet in the last Place you see there is an infinite Product equal to an infinite Remainder; and confequently the Work must there cease, and the Quotient nevertheless be true.

If the Divisor confifts of terminate Numbers join'd to the Repetend, and the Dividend be complete ; proceed thus: Subfract the terminate Numbers of the Divisor from the Divisor it felf, and the Remainder shall be a new Divisor; and deal with the Dividend as in the last Example, for a new Dividend.

EXAM-

EXAMPLE VI.

1. .

Suppole it requised to divide 8569,88 by 4,80; Work as follows;

486) 8569,88 (1760,9 the Quotient if work'd at large. 48 856988

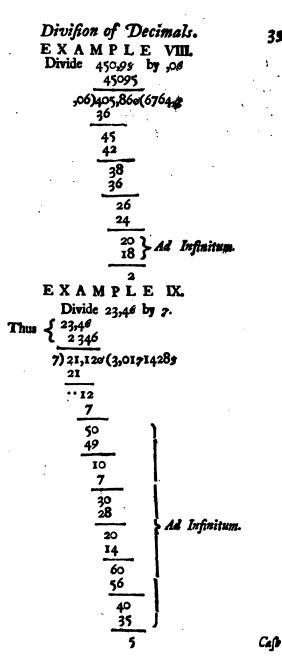
4,38) 7712,892 (1760,9 the	fime.	, r
438	ef e state in the state of the	• •
3332	· · · · · · · ·	•
2668	•	
2628	· · · ·	
**4092 3942	• • •	
50		

If the Divisor and Dividend do each contain a Repetend, order them as before directed; and the Quotient will be either terminate, repeat a fingle Digit, or elle a compound Repetend.

EXAMPLE VIL

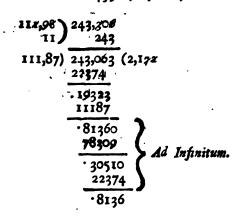
EXAM-

.



Cafe. 4. If Compound Repetends are found in your Divifor, or Dividend, or both; then observe to fet the Divifor and Dividend under themfelces so many Places forwards to the Right-hand, at there are Places in the Repetend of the Divisor exclusively; next, subfruct them, and the Remainders will be respectively a new Divisor and Dividend.

EXAMPLE L



Divide 243308, by 11198.

The Truth of the Work will appear as well by the common Rule of multiplying the Divisor and Quotient, as by the Work at large.

If there be no terminate Part of the Divisor, you substract nothing from it.

EXAM-

S 1

EXA	MPLE	· II.
Divide Then	395,273 &14 395273	by ,317
-217)	394,878341	11245.672
/]-//	317	(
:	621	
•		
	• 1447 1268	
A.	ومحمد والمشاركة	
	• 1798	
	1585	
. ·	• 2133	
i c	1902	
· ·	1 22TA	
	2219	
	- man Man	
	951	

EXAMPLE m.

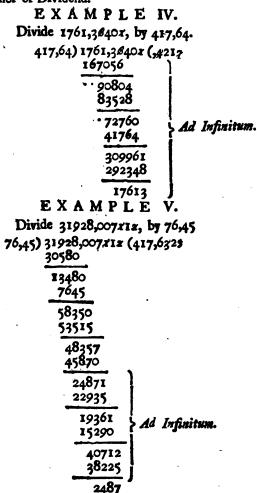
·.••

G

. . .

. If

If there be no *Repetend* in the *Divisor*, whatever the Dividend may be, there's no Subfiraction to be made et either Divisor or Dividend.



In Division it may often happen that the Quotient may not repeat to foon as is defined; in fuch Cafe the Value of the Quotient may be expressed compleatly by a Vulgar Fraction. But

But in order to underfland this, twill be necellary to premife the following Lemma's.

Lemma 1.

A Series of Nines infinitely continued, is equal to Unity, or One, in the next Left-hand Place; thus 0,999, Sc. is equal to 1; and ,0999 Sc. =,1; and ,00999 Sc. =,01; and 549,99 Sc. = 55.

and 549,99 &c. = 55. Demonstration. Tis evident that ,9 = 7? wants, only .' of Unity; and ,99 wants ...'; ,999 wants ...' of Unity; fo that if the Series were continued to Infinity, the Difference between that Series of Nines and an Unit, would be equal to Unity divided by Infinity, that is, Nothing at all. Q. E. D.

Lemma 2.

Any fingle Repetend multiplied by 10, and then fubfiraBed from that Product; the Remainder will be the fame Number compleat or terminate, in the next superior Lefthand Place.

Demonstration. Let the given Repetend be ,6666, Bc, this multiplied by 10 is 6,666 Bc.

From which Substract ,666 Sc.

There will remain 6, ... a whole Number.

Thus 47,77 &c. will become 430. and ,0333 &c. will be 23. Q. E. D.

Corollary 1.

Hence it follows that if any Compound Repetend be multiplied by an Unit with fo many Cyphers annexed as are equal to the Places of the Repetend, and then fubfiracted from the Product, there will be left to the Left-hand the fame Numbers terminate and compleat, that conflicted the Repetend; thus, 325 multiplied by 1000, will be 32\$,325 from which if you fubfiract, 32\$ there will remain the terminate Number 325; Thus 12,743 will be 12731; and,000243 will be ,743, and 5225,3 will become 5270,1.

Corollary. 2.

Hence also if any *Repstend* be multiplied by so many Nines as it contains Places, the Refult will be the same as be-G 2 fore;

fore; that is, the Repetend terminate and complete. For any thing multiplied by Ten, and once subfinated, is the fame as multiplied by Nine;

Thus; ,666 Sc. × 9 = 5,999 Sc. = 6. by Lemma 1. And \$27 × 999 = 526,999 = 527. per idem. Corollary 3.

Hence it must follow that, vice ver/a, any Number divided by as many Nines as it contains Figures is equal to the fame Number perpetually circulating; Thus $\frac{6}{2}$ = ,666 Gc.

And $\frac{527}{999} = .527$. And $12 \frac{743}{999} = 12.743$. Corollary 4.

44

Hence, lastly, appears the Reason of all the different Methods and peculiar Processes used in the Arithmetick of Circulating Numbers, call'd Repetends.

The preceeding Lemma's and Corollaries being well underftood, it will then be very eafy to value any kind of Decimals in the manner of Vulgar Frations. For the Quotient in Division, take this Example from Mr, Cunn.

EXAMPLE VI.

Divide 213476, by 4176.

	2x3,478134 (2x3478	26586
4	Construction of the local data and the locae data a	5-4 00000
417,2) 213282658 (51117	
• • • •	20860	417,2
	· ·	, .
	•• 4662	
	4172	
	4905	
	4172	
	•7345	
• •	4172	
-	Construction of the local division of the lo	
•	31738	
	29204	
	and the second s	
	: 25346	
	25032	
(,		
. 1	• • • 314 •	

The

The Reafon why the Quotient is thus expressed will be evident if we confider.

First, That 314 is not the entire Remainder because the Dividend is a *Repetend*, perpetually supplying a circulating Remainder, which expressed in its proper Terms would be, where we leave off, wrote thus 31426586. But this infinite

Series of Figures is usely expected thus, 314 2000 by Carol. 2.

Secondly, It being plain that 31409999 is the time Remainder, and 417,2 the Divisor, 'ris' necessary they should be expressed in the Quotient as here you see them by the Rules of common Division.

If infleted of $314\frac{26586}{99999}$ you write its Equivalent 31486584, and from it fubfiract the terminate part 314, there will remain 31426272 a new Numerator. And if to 417,2 you add as many Cyphers as the Repetend confifts of Places, thus 417,200000; and again fubfiract it, as a terminate part, there will remain 417195828 for a new Denominator; and

then this new and more fimple Fraction 31426272 will be

equal to that in the Quotient.

The Reafon of reducing the Fractions of the Quotient in this Manner is obvious from Corol. 1. of Lem. 2.

For $31436586 \times 100000 = 3142658626586$ Sr. From which substract it self 31426586 Sr.

And there will remain the new Numerator 31426271 as before;

Then $417,2 \times 100000 = 417,200000$ From which fubftrast it felt 4172

There remains the Denominator 417195828 as before.

Thus I have fupplied you with Rules for managing the whole Doctrine of Circulating Numbers; and given the Theory and Reafons for the fame; which you may fearch for in vain in any other Book (that I know of) fo fully as here laid down.

CHAP.

CHAP. V.

REDUCTION of DECIMALS.

T being inficiently experienced that all Arithmetical Operations are with the greateft Facility and Expedition work'd in whole Numbers; that Valgar Fractions, and Numbers of diverfe Denominations in their Management require great Art, and are attended with much Perplexity; and that the noble Art of Decimal Arithmetick alone is fusceptible of all the various kinds of Numbers, and at the fame time hath all its Operations perform'd by the fame eafy and common Rule, and in the very fame manner of Integral Quantities, or whole Numbers; This, I fay, being well known to all veried in the Science of Numbers, hath juftly rendered Decimal Arithmetick in the greateft Efteem among those who underfland it; and is most generally used by them in almost all kinds of Numerical Calculations.

The Part we now treat of is abfolutely neceffary to the grue Understanding and Use of this excellent Art; and teaches,

First, To reduce or express any Vulgar Fraction in Decimal Parts of the Integral Quantity.

Secondly, To reduce fuch Numbers as confift of various Parts and Denominations, as those of Money, Weight, Meafure, Sc. into Decimals for more eafy Operation.

Thirdly, To reduce Decimal Parts, into the common and known Parts of Money, Measure, &cc.

Cafe 1. To reduce Vulgar Fractions into Decimals, the common Rule is, to divide the Numerator by the Denominator, and the Quotient will be the Decimal required; that is, equivalent to the Vulgar Fraction given.

EXAMPLE I.

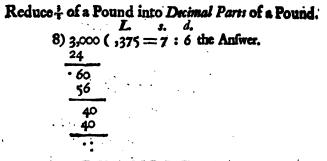
What is the Decimal equivalent to the Fraction $\frac{3}{4}$? 4) 3,00 (,75 'I be Decimal required.

′ -	2	8		
	٠	2	5	
		20	3	
1				

۰,

EX.

EXAMPLE IL



EXAMPLE III.

Reduce - of a Pound Troy into Decimal Parts, oz. pwt.

16) 3,0000 (,1875 = 2 : 5 the Animer.

10
140 12 8
120 112
••

EXAMPLE IV.

Reduce $\frac{4}{17}$ of a Rod into Decimals. Rod. F. In. Qr. 27) 4,000 (,x48 = 2 : 5 : 1 Answer. $\frac{27}{130}$ $\frac{108}{220}$ $\frac{216}{104}$ Ad Infinitum.

EXAM

Reduction, Sec. into Decimal, Sec.

EXAMPLE V

Roduce of free a Hayband into Decimals

Gal. Pts.

Hence the Anfwer is 5,407 = 5:25:5

Reduction of Vulger Fractions into Decimals is also commodiously performed by Logarithms, especially when the Fraction is large; thus, full the Logarithm of the Denominator from the Logarithm of the Numerator, the Remainder is the Logarithm of the Basimod Parts.

EXAMPLE I. By Logistichus.

Reduce the Fraction $\frac{127}{4123}$ into Decimal Parts.

Thus, the Logarithm of 127 is ______ 2.1038037 the Logarithm of 4123 fubftract, ______ 3.6152133 Remains the Logarithm or the Decim_______0308 = 8.4885904

EXAMPLE IL.

What is the Blankak of the mix'd Fullicus

From the Lagarithm of the Numerator 91 1.9590414 Substract the Logarithm of the Denominator 3.5414544 There Remains the Log. of the Dec., 026557 - 8.4175870 To which prefix the integral Quantity 5, and the Answer will be compleat, thus 5.026157.

The fame thing might as well have been done by reducing the mixt Fraction into an improper one, oix. $\frac{17486}{3479}$ Then,

Reduction, &c. by Logarithms.

Then, as in the first Example.

From the Log. of the Numerator 17486 - 4.2426904 Subfract the Log. of the Denominator 3479 - 3.5414544

Remains the Log. of the Anfwer 5,026157 — 0.7012360 Note, In the first and fecond Examples, and in all fuch Cafes where you fubstract a greater Index from a lefs, you borrow Tens and as many Digits as the remaining Index want; of Nine, fo many Cypbers prefix to the Decimal.

Cafe 2. To reduce Numbers which express Quantities of various Kinds and Denominations, as Money, Measure, &c. into Decimals, there are three Ways or Methods, which are as follows.

Method 1. Reduce the different Species to one; that is, to the lowest Denomination they confiss of: then reduce the Integer to the fame Denomination; the first will be the Numerator, the latter the Denominator of a Vulgar Fraction; which Fraction reduced to a Decimal (by Case 1.) will be that required.

EXAMPLE I.

What Decimal Part of a Pound is 5s. 7d. 3?

	5.		Ĭ.	
Multiply	5	Then teduc	e 1. the Int	eger.
By 12 d.	12	•	20	
	60		20	
Add the 7d.	7		12	
	67	Pence.	240	
Mul. by 49	4	· .	4	
	268	•••	960 Farthin	gs in a Pound.
Add the 3q	3	· :	-	
-	27I ·	Fartbings.		2
	•	. 0		<u> ን</u>

That is $\left\{\frac{271}{960}$ the Numerator $\left\{\right\}$ of the Vulgar Fraction.

Then 960) 271,0000 (,28229 Sc. The Answer. H

So

30 Reduction of different Denominations,

So that ,28229 is the Decimal Part of a Pound in one Denomination, equal to 5 s. 7d. 4, the Part of a Pound in diverse Denominations.

EXAMPLE II.

What Decimal Part of a Hundreid Weight is 2 9. 21 lb.

Q. 7%. oz. Reduce 2: 21: 12 to Ounces. 28 77 16 454 78 1244 Ounces 1792 Ounces in C. W.

Then $\left\{\frac{1244}{1792}\right\}$ is the Vulgar Fraction.

And 1792) 1244,0 (=,694196 the Decimal Part of an Flundred Weight (answering to 29.: 21 lb. : 12-ez. required.

EXAMPLE III.

What Definal Part of a Red or Pole, is 4 Y. : 2F. : 8In ?

Y. F. In.	
4:2:8	1 Pole.
3	5.5
14	5,5
12	. 3
176 Inches.	16,5
·	12
	1980 In bes in a Pole.

But $\frac{176}{198} = \frac{188}{99} = .8$ the (repeating) Dethnizh of a Pole,

equal to the 4 Yards, 2 Feet, and 8 Inches.

In the fame Manner proceed with any other given Species. Method

into Decimal Rasts of the Integer.

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Method 2. Find what Detimol, Bars the least Danomic. nation of the given Species, is of the next Superior, to which, prefix the given Part of the next superior Denomination; then fee what Decimal Part this wint Number is of the next Inperior Denomination, to which again prefix what is given ofit; and thus proceed till you afcend to the Integ m, it felf, and find what Decimal Part of it, the last mixed Number is, which will be that lought.

EXAMPLE I

What Decimal Part of a Round is 12 s. 6 d 4? 4) 2,0 (,5 the Decimalios one Penny for 1. Finit Secondly 12). 6,5 (,5416 the Dec. Part of a Shill, for 6d. 4: Thirdly 20) 12,5416 (,627083 the Decimal Part of a Pound, as was required, for 125. 6d. ...

EXAMPLE IL

What Decimat of a Pound Troy is 202. 18 pwt. 20 gr. A 24) 20,000 (.875 the Decimal for 20 gr. Firft Secondly 20) 18;875 (.94375 the Decimal for 18 pwt. 2097. Thirdly, 12) 2,94375 (.2453125 the Decimal Part of a Pound Froy for 202. 18 pwt. 20 gr. as was required.

EXAMPLE III.

What Decimal Part of a War is 6m. 2w. 5d. 6b. 40' 50"?

60) 50,00 (,8% Decimals for 50" of 1'. Firft

Secondry 65) 40,83 (,680% Dec. for 40': 50" of an Hour. Thirdly, 24) 6,680s (12783148 = 6H. 40': 50" of a Day. Fourthly, 7) 5,2783 x48 (,75404 Sc. Decimals of a Week. 4) 3,75404 Br. (193851 Decimals of a Month. Fifthhy Sixthly, 13) 6,93851 (,53373 Decimals of a Year.

So that we fee the fix different Parts of Time above fpecified are reduced to this finall Decimal ,53373; which exprefieth the fame Part of a Year as they do; which, by the way, may be an Instance of the great Simplicity, Eafe, and Excellency of this admirable Art.

In these three Examples I have omitted the Work at large, fetting down only the Divisors, Dividends, and Quotients as ſuffi-

Reduction to Decimals by Tables.

52

fufficient to give the *Learner* as good a Notion of the Method as the Operations at length, which he may make his *Exercife at pleafure* to good advantage.

Method 3. The third Method for finding the Decimal of any given Part of Quantity confifting of diverse Denominations, is by Tables ready calculated for that purpose.

This is not only the most easy, but the most expeditious Manner of working the Processes of all Kind of Computations in general; and is of particular service in this Case of preparing Numbers for Decimal Operations.

For that reason I have here inferted a Set of Tables, which, tho' fome are common of this kind, are the most compleat and universal of any I have seen extant; and in order to render them so, I have not only very much enlarged and new vamped the old ones, but also added other very useful ones; as those who are read in these Matters, will soon perceive.

By the following Tables, all the Species of Money, Weight, Meafure, &cc. confifting of what ever Denomination, and be the Integer what you pleafe, are immediately turn'd into Decimal Parts; and are then work'd with the known Facility and Pleafure of Whole Numbers.

As to the manner of using those Tables, that is so obvious and natural, even by a bare Inspection, that I prefume tis needless to fay any thing to a Person of Genius, though a Learner, about that. The Scheme of Examples following being sufficient to testify the great Use and Excellency of such Tables, and are both Precedents and Precepts themselves.

EXAMPLE L

What is the Decimal Part of a Pound for 13 s. 7 d. 2?

In Table I. you find answering to 3 Farthings - - ,65 - ,0322916

,6822916

The Anfwer is _____

EXAMPLE II.

What Decimal Part of a Mark is 11 s. 2 d. $\frac{1}{2}$ In Table I. under a Mark, against $\begin{cases} 11 \text{ Shillings} & - & -, 65 \\ 2 \text{ Pence} & - & -, 0125 \\ 2 \text{ Farthings} & - & -, 003125 \\ - & -, 840625 \\ E \text{ X A M} \end{cases}$

Reduction to Decimals by Tables. 53

EXAMPLEIM

What Decimal Part of	a Moidore is 9	s. 3 d.	¥?
In Table I. under Moi-	$\begin{cases} 9 \text{ Shillings} \\ 3 \text{ Pence}_i \end{cases}$	<u> </u>	,00ø2\$9
dore you find against	Li Farthing		,000771

The Answer is this compound Repetend ,343363992

EXAMPLE, IV.

What Decimal of a Pound Troy answers to 5 oz. 17 profs. 22 gr. ?

In Table II. you find against	S Ounces	;	,41 <i>8666</i> ,0708 <i>3</i> 3
•	C 22 Grains		,003819
The Sum of wh	ich is the Anfwer —	-	,491319

EXAMPLE V.

What Decimal Part of an Hundred Weight is 21 lb. 14 oz.?

In Table III. you	∫2I Pounds	 	,1875
find against	X14 Ounces	 	,007812
The Answer is			,195312

EXAMPLE VI.

What Decimal 1	Part of a Tun	is 3 qr.	6 bush.	7 gall?
In Table V. Dry. Measure, against	3 Quarters	•		,6
Measure, against	7 Gallons		_	,021875
The Answer is	-			- ,771875

EXAMPLE VII.

What Decimal Part of a Hogshead of Wine, is 2 ; Rund. 14 Gall. ?

In Table VI. Liquid Mea-	,71425	
fure, you find against 314 Gallons	,22222 Sc.	
The Answer (repeating a fingle Figure is	,936472 8c. EXAM	

54: Body How to Desimals by Tables.

EXAMPLE VIIL

How is 27 Miles, 7 Eurlargs, 25, Rod, and 4 Yards expressed in Derimals?

In Table VIII. Long 5 7 Eurlongs	,875 ,109375
Integer) you find against C 4 Yards	,002272
The 27 Miles prefixed, the Anfwer will be	27,986647

EXAMPLE IX.

What Decimal Part of a Year is 7 Months, 3 Weeks, and, 2: Days?

In Table IX. you \$7. W olifere against 30	mthe	 ,538461
olderve against 33 V	eeka	 ,097630
	iys —	 x005494
The Answer is		,601585

EXAMPLE X.

What Devined' P	art of a Sign of th	e Zodia is	25 ⁹ 46 ⁸ 8" ?
In Table X. you	S 25 Degrees	-	28833333
find against	46 Minutes		235555
- _	C 8 Seconds		,000073
The Answer is a	fingle Repetend		8589618

EXAMPLE XI.

What Decimal Pa	art of a Degree,	is 49	574?	
In the fame Table you fee against	549 Minutes			, 81\$66 6
you lee againff	7 57 Seconds			,015833
The Answer is				8325

Having thus fo largely exemplified the Use of the Tables, the Tables themselves follow; wherein observe, 1. I have dash'd the first Figure of all first Repeareds, and the first and last of the compound Repetends that come within the Table. 2. I have nevertheles continued each to fix Places for their sukes who would be exact, but more not well how to manage Repetends.

Common

Common Tables of Money, Weights, Meafures, and Time.

Tables I. Monry.

Eath.

4 = 1 Penny. 48 = 12 = 1 Shilling. 500 = 240 = 20 = 1 Pound.

Table III. Apothosaries Meight. Grains. 20 = 1 Scruple. 60 = 3 = 1. Beam. 480 = 24 = 18 = 1 Ounce. 5760 = 288 = 96 = 12 = 11b. Table III. Troy Weight. Grains. 24 = 1 Penny Weight. 480 = 20 = 1 Ounce. 7560 = 240 = 12 = 3. b.

Tuble IV. Moneyers Weight.

Blanks.

24 = 1 Periot. 480 = 20 = 1 Droite. 11520 = 1480 = 124 = 124 ite. 230400 = 9000 = 480 = 20 = 1 Grain.

Table V. Averdupois Weight.

Drams.

16.= 1'Ounte. 256 = 16 = 1 Pound. 28672 = 1792 = 112 = 1 Hundred. '573440 = 35840 = 2040 = 20 = 1 Pun.

`Table

्ः

......

. Table VI. Wine Meafare. Cubic In. 231 = 1 Gallon. 9702 = 42 = 1 Terte. 14553 = 63 = 1' = 1 Hogshead. $\begin{array}{rrrr} 19404 = 84 = 2 = 1; = 1 \ Punch.\\ 29106 = 126 = 3 = 2 = 1; = 1 \ Butt.\\ 58212 = 252 = 6 = 4 = 3 = 2 = 1 \ Tun. \end{array}$. Table VII, Ale Measure. Cubic In. 282 = 1 Gallon. 2256 = 8 = 1 Firkin. 4512 = 16 = 2 = 1 Kilderkin. 9024 = 32 = 4 = 2 = 1 Barrel. 13536 = 48 = 6 = 3 = 11 = 1 Hogshead. Table VIII. Beer Measure. • . • • 1 Cubic In. ·) ፣ 282 = I Gallon. 2583 = 9 = 1 Firkin. 5076 = 18 = 2 = 1 Kilderkin. 10152 = 36 = 4 = 2 = 1 Barrel. 15228 = 54 = 6 = 3 = 1; = 1 Hogsbead. A. A. Table IX. Dry Measure. Cubic In. 268.8=] Gallon. 537.6= 2= 1 Peck. 2150.4= 8= 4= 1 Bufbel. 8601.6 = 32 = 16 = 4 = 1 = Coomb.17203.2= 64= 32= 8= 2= 1 Quarter. 68812,8=256=128=32= 8= 4=1 Chalder. 86016.0=350=160=40=10= 5=1 Wey, or Load. 172032.0=640=320=80=20=10=2=1 Laft.

Weights, Meafures, and Time.

Table X. Of Time.

Seconds. 60 == 1 Minute. 60= 1 Elmar. 3600= 86400= 1440= 24=: 1 Day. 604800= 10080= 168= 7= 1 Week. 2419200 = 40320 = 672 = 28 = 4 = 1 Month. 31556937=525949=8765=365=52=13+1 Day, + 5 Hours, +48' +57" = Year.

Table XI. Long Measure.

Barly Corns. 3 Inch. 36 12 I Foot. 108 36 36 3 1 Yard. 594 198 161 51 1 Pole. 23760 7920 660 220 40 1 Farlong. 190080 63360 5280 1760 320 8 1 Mile.

Table XII. Square Measure.

Square In.

144 I Feet fq. 1296 9= 1 Yards fq. 3600 25 2.7 1 Paces fq. 39204 3724 304 10.8 1 Poles fq. 1568160 10890 1210 435.6 401 Rood fq. 6272640 43560 4840 1742 160 41 Arres fq.

Tuble XIII. Scripture Meafure.

1.

Table IV. Eastern Measure.

Cubits. 400 = 1 Stadium. 2000 = 5 = 1 Sabbath Days Journey. 4000 = 10 = 2 = 1 Eaftern Miles. 12000 = 30 = 6 = 3 = 1 Parafang. 96000 = 240 = 48 = 24 = 8 = 1 Days Journey.

Table XV. Hebrew Measure.

Table XVI. Hebrew Measure.

Eapb.

$$1\frac{1}{2} = 1 Log.$$

 $5\frac{1}{3} = 4 = 1 Cab.$
 $16 = 12 = 3 = 1 Hin.$
 $32 = 24 = 6 = 2 = 1 Seab.$
 $96 = 72 = 18 = 6 = 3 = 1 Bath Epba.$
 $960 = 720 = 180 = 60 = 30 = 10 = 1 Coron Chomer.$

Table XVII. Hebrew Money.

Gerabs.		_	101	1.					
10	=			ab.		-			
				1					
I 200	_	I 20	=	60	—	ł	Ma	neb.	
60000	=	6000	=	3000	-	50	=	1 Tales	zf.
	. '								

Decimal

			D' all Day
TABL		P. q. Dec. Par	. P. q. D. Par.
Money ; the Intege	one Pound r.	8,0033333 8 4 ,034375	4,0,5333333
the Integer 5. Dec. Par. 1,05 2,1 3,15 4,92 5,25 6,3 7,35 8,4 9,45 10,5 11,55 12,6 13,65 14,7 15,75 16,8 17,85 2	r. P.q Dec. Par. p.q Dec. Par. p.q $p.q$ $p.$	$8 \frac{1}{2} 034375$ $8 \frac{1}{2} 035416$ $8 \frac{1}{2} 035416$ $8 \frac{1}{2} 0364583$ $9 \frac{1}{2} 0365416$ $9 \frac{1}{2} 039583$ $9 \frac{1}{2} 040625$ $10 \frac{1}{2} 040625$ $11 \frac{1}{2} 040625$ $10 \frac{1}{2} 04065$	$\begin{array}{c} 4 & 4,3541 \text{ #} \\ 4 & 2,375 \\ 4 & 395833 \\ 5,0,41 \text{ #} 666 \\ 5 & 4,4375 \\ 5 & 2,458333 \\ 5 & 4,4791 \text{ #} 6 \\ 6,0,5 \\ 6 & 4,520833 \\ 6 & 3,541 \text{ #} 6 \\ 6 & 3,542 \\ 7 & 583333 \\ 7 & 4,6041 \text{ #} 6 \\ 7 & 2,625 \\ 7 & 3,645833 \\ 8 & 5,9 \text{ #} 666666 \\ 8 & 1,6875 \\ 8 & 3,708333 \\ 8 & 3,7291 \text{ #} 6 \\ 9 & 5,75 \\ 9 & 3,77882 \\ \end{array}$
18,99 19,95 2	$ \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c}$	$0_{4},0208,3$ $0_{2},041,666$ $0_{4},0625$ 1,0,08,333 $1_{4},1041,66$ $1_{4},125$ $1_{3},1458,33$ 2,0,16666 $2_{4},1875$ $2_{1},208,333$ $2_{3},2291,666$ $3_{2},25$ $3_{4},2708,233$ $3_{2},291,666$ $3_{4},3125$ $1_{2},208,333$ $3_{2},291,666$ $3_{4},3125$	9 1,791866 9 1,791866 9 1,8125 10,0,8,3333 10 1,854186 10 2,875 10 4,895833 11 3,918666 11 1,9375 11 2,958333 11 4,979185

Decimal Tables of Money, Weight, &c.

1 Crown	P.D. Part.	P.D. Parts.	P. Dec. Parts.
the In- teger.	1,0125	6,0375	1,00396825
SID.Par.	2,025	7,04375	2,007936
S.D.P.W.	3,0375	9'05625	3,01,1904 4,015873
1,2	5,0625	10'0625	5,01,0841
2.4	6,075	11,06875	6,023809
4,8	7,0875 8,1	gr. D. Parts.	7,027777 8,03,1746
P. D.Par.	9,1125	1,0015625	9:03\$714
1,01866	10,125	2,003125	10,039682
2,03333	11 ,1375 gr D. Part.	3,0046875	11,043650
3,05	1,003125		gr.De. Parts.
4,08666	2,00625	A Guinea	1,000992
6,I	3,009375	the Integer.	2,001984 3,002976
7,11666	111-1	S.D. Parts.	55002970
8,13333	A Mark the Integer.	1,047619	1
9,15 10 18666	S. D. Part.	2,095238	A Corol the
11,18333	1,075	3,\$42857	Integer.
gr D.Par.	2,15	4,190476	S. 043478
1 20416	3 ,225	6 285714	12043478
2 20883	4 3	7.333333	2086957
3,0125	6 ,45	8,380952 9,42857x	3°130436 4°173914
	7,525	10,476190	5217393
A Noble	9,675	11,523089	67260872
the In-	10,75	12,571428	7'304350 8'347829
teger.	11,825 12,9	14,866666	97391308
S.D.Par.	13,975	15,714285	102434786
1,15	P. D. Part.	16,761904	112478265
2,3	1,00625	18,857142	122565222
3,45	2,0125	19,904761	14/008701
4,6	3,01875	20,952380	15252180
5.75	5,03125		170739137

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Magnare, Time; and Motion. 61

	an agran cy start	the and the Tation	
SID. Part.	5. D. Part.	A Moleore	S. B. Parts.
18,782616	9 ,36	the Inte-	21 777777
19 826095	10 4	ger.	22 5814814
20,869573	11,44	G.O. Dant	23 ,45,2851
21,913052	12 48	S.D. Parts.	24 ,888888
22,256531	13 ,52 14 ,56	10032037	25 525925
P.D. Part.	15,6	2po74074	26 ,962962
1,003623	16,64	3 11111	P. D. Parts,
2,007246	17 ,68	4,248148 5,209185	1,003086
3,010989	18,72.	227222	2,004172
4.0145.02	19,76	7 358259	3,00#2\$9
5,018225	20 ,8 21 ,84	8,298290	4 ,012345
6,021938	21,84 22,86	9 333333	5 ,014432
7,025561	23,92	19,370370	6 ,0185185
8 0 191 84 9,032707	24,96	11,407407	7,021604
10,036232	P. D. Part.	12,#4444	\$,024691 9,027777
11,039855	r. D. Pari.	13,48x481 14,518918	10,030864
	1,003333	15 \$55555	11,033950
gr.D. Part.	2,008666	10,892392	
1,000905	3,01	17 8 28629	gr. D. Parts.
2,001811	4,013333	18,866666	1,000771
3,002717	5,016606	19,703707	2,001543
I	7.022222	20,740740	31,002314
l E	7,0223333 8,020000	1	
A Jacobus	9,03		
the Inte-	10,033333 11,038666	TABI	
ger.	11,038666	Troy Weigh	nt; one Pound
S.D. Part.	gr. D. Part,	the In	tener
		auro 4/1	
1604	1,0008/3	Qr. D. Par.	0z. D. Par.
2,08	3,0025		
2,12		I ,08333 2 ,1 6 666	7,58333 8,66666
4,16 5,2		3,25	9 ,75
6 ,24		4 33333	10 ,83333
7,28		5 ,41\$66	11 ,91466
7,28 8,32		6,5	
	all stations		

Pwt.

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63		mal'	Tables o	f Ma	oney, W	eight	?
Pa.	D.P.art.	Pw	D. Part.	Gr.	D. Part.	Gr.	D. Part.
	,004166	19	,003298	8	,01#6666	16	000000
2	,008833	20	,003472	9	,01875	17	,0333333 ,03541 <i>6</i>
3	,0125	21	,003646	10	,020833	18	,0375
4	,014666	22	,00381 <i>9</i>		,022910	19	,039583
	,020883	23	,003993	12	,025	20	,041,866
56	,025			13	,027083	21	,04375
7	,0291.16			14	,029166	22	,045833
8	,033333	On	Ounce	15	,03125	23	,047916
9	^{,0} 375	the	Integer.				
10	,941 <i>8</i> 66	Per	D. Part.		÷-		
II	,°45833				ΓΑΒ	7	III.
12	,05	1	,05				+41.
13 14	,0541 <i>86</i> ,058333	2	,1	Av	erdupois	Wei	ght, one
15	,0625	3	,15		Hundred V	AToin h	+ the In-
16	,0#6666	4	,2 ,7			r ugu	6 5136 <u>21</u> 8-
17	,070833	5	,25	1 "	eger,		
18	,075		13 .	-			
19	,0791#6	78	,3 % ,4	gr.	D. Part.	16:	D. Part.
Gr.	D. Part.	9	,45	I	.25	16	,142857
-		10	, 5 ·	2	5.	17	,151785
1	,000173	II	55 -	3	,75	18	,160714
2	,000347	12	,6	16.	D. Part.	19	,169643
3	,000521	13	,65		l	20	,178571
4	,000694	14	·7	1.	,008928	21	,1875
5	,000868 ,001042	15	,75 ,8 ···	'2	,017857	22	,196428
	,001042	17	,85	3	,026786	23 24	,205357 ,214286
78	,001389	18	,9 ·	4	,035714 ,044643	25	,223214
9	,001562	19	,95 ·	5	,0535 7 I	26	,232143
10	,001736		1		,0625	27	,241071
11	,00191	Gr	. D. Part.	78	,071428	Oz.	
12	,002083	1	,002082	9	,080357	Uz.	D. Part.
13	,002257	2	,004160		,089286	1	,000558
14	,602431	3	,00625	11	,098214	2	,001116
15	,002604	4	,008,333	12	,107143	3	,001674
16	,002778	5	,01041\$,116071	4	,002232
17	,002951		,0125	14	,125	5	,00279
118	,003125	17	<u>',014583</u>	15	,133928	<u>' 6</u>	,003 34 8

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Measure, Time, and Mation.

. 1	Aeasure, Tim	e, and Motion.	63
Oz. D. Part. 7 ,003906 8 ,004464 9 ,005022 10 ,00558 11 ,006138 12 ,006696 13 ,007254 14 ,007812 15 ,00837 One Pound the Integer. Oz. 'D. Part. Oz. 'D. Part.	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	D. Part. ,041866 ,083333 D. Part. ,002083 ,004186 ,00625 ,008333 ,010418 ,0125 ,014583 ,014583 ,014583 ,01875 ,020833 ,022916
I ,0625 2 ,125 3 ,1875 4 ,25 5 ,3125 6 ,375 7 ,4375 8 ,5 9 ,5625 T A B 1	7 ,027343 8 ,03125 9 ,035156 10 ,039062 11 ,042968 12 ,046875 13 ,050781 14 ,054687 15 ,058593	II One Ounce 13 the Integer. 14 Dr. D. Part. 16 1,125 1 ,125 2 ,25 3 ,375 4 ,5 5 ,625 6 ,75 7 ,875	,022916 ,025 ,027083 ,029166 ,03125 ,033333 ,03541# ,375 ,039583
Apothecary one Pound	<i>Oz.</i> D. Part. <i>Oz.</i> D. Part. <i>6</i> <i>7</i> <i>58233</i> <i>8</i> <i>66666</i> <i>9</i> <i>75</i> <i>10</i> <i>82333</i>		V. Tun or er. <u>D. Part.</u> ,6 .8

Б.

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64 Decimal Tubles	of Money, Weight,
B. D. Part. G. D. Part. $i_{,025}$ $j_{,05}$ $j_{,075}$ $j_{,015625}$ $j_{,075}$ $j_{,015625}$ $j_{,015625}$ $j_{,0155}$ $j_{,0155}$ $j_{,02125}$ $j_{,009375}$ $j_{,009375}$ $j_{,009375}$ $j_{,015625}$ $j_{,009375}$ $j_{,0125}$ $j_{,015625}$ $j_{,0125}$ $j_{,015625}$ $j_{,0125}$ $j_{,015625}$ $j_{,0125}$ $j_{,015625}$ $j_{,0125}$ $j_{,0125}$ $j_{,0125}$ $j_{,012625}$ $j_{,012625}$ $j_{,012625}$ $j_{,012625}$ $j_{,012625}$ $j_{,012625}$ $j_{,012625}$ $j_{,012625}$ $j_{,012625}$ $j_{,012625}$ $j_{,012625}$ $j_{,012625}$ $j_{,012625}$ $j_{,0125}$ $j_{,012625}$ $j_{,0125}$ $j_{,012625}$ $j_{,021875}$ $j_{,012625}$ $j_{,021875}$ $j_{,012625}$ $j_{,021875}$ $j_{,012625}$ $j_{,02125}$ $j_{,02375}$ $j_{,02375}$ $j_{,02375}$ $j_{,02375}$ $j_{,02375}$ $j_{,009375}$	T A B L E VI. Liquid Meafure. For Wine, $Oc. One Tun$ the Integer. H. D. Part. One Hogh 1,25 R. D. Part. 2,55 R. D. Part. 1,035714 2,57142 1,035714 2,57142 1,035714 2,57142 1,071428 21,71425 1,107143 3,85713 2,142857 G. D. Part. 1,003968 1,015872 2,031746 5,027936 3,011904 6,025235 4,01872 7,31744 1,003968 3,047619 1,003968 3,047619 1,003968 3,047619 1,003968 3,047619 1,003968 3,047619 1,003968 3,047619 1,019841 8,126984 6,023808 9,142857 7,027776 9,035714 10,039682 13,226984 11,04355 14,2573 12,047618 14,2573 13,05774 10,15673 14,055555 13,226984 1

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One

Measure	e, Time	; 4	nd Moti	an.	65
One Rundler P. 11	D. Part.	G.	D. Part.	G.	D. Part
G. D. Part. 2,0	006941	1 2	,0,18518	50	,0\$2892 ,11111
2, TIIII 4, C 2, IIIII 4, C 2, I6 5666 5, C	20833 29777 34722	34	,0\$5555 ,07#074	8	,129,829 ,148148
1 1 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	41 <i>656</i> 48511	Т	ABL	E.	VIII.
7 ,388888 8 ,414414 9 ,5 One (the in	teger.	Lor	ng Mcafu the In		
	. Part 25	F.	D. Part.	\overrightarrow{P}	D. Part
12 \$\$66666 2 ,2 13 ,7\$22222 3 ;3 14 ,777777 4 ;5 15 ,8\$33333 5 ,6 16 ,688888 6 ,7	5 75 25	I 2 3 4 5 6	,125 ,25 ,375 ,5 ,625	17 18 19 20 21	,053125 ,05625 ,059375 ,0625 ,065625
17 ,9 #4444 7 ,8	75) 6 7 <u>P</u> .	\$75 \$875	22 23 24	,009023 ,06875 ,071875
•	711.	ī	D. Part.	25 26 27	,078125 ,08125 ,084375
Of Ale and Beer fure ; one Hoge the Integer.	Mea Ihcad	2 3 4 5 6	,00625 ,009375 ,0125 ,015625 ,01875	28 29 30 31	,090625 ,090675 ,096875
Fr. D. Part. G. D. I ,18066 2		7 8	,021875 ,025	32 33 34	,I ,103125 ,10625
2 x3333 3 ,00 3 x5 4 ,00	41,85t 625 83333	9 10 11	,028125 ,03125 ,034375	35 36	,109375 ,1125 ,115625
5,8333 6,1	25 45833	12 13 14	,0375 ,040625 ,04375	37 38 39	,115025 ,11875 ,121875
1,020833		15 16	,046875 ,05	¢	

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Decimal Tables of Money, Weight,

$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	0. Part.
1,009568 29,725 2,010101 2, 2,001136 30,75 3,01915 3,	
I ,009568 29 ,725 2 ,010101 2 , 2 ,001136 30 ,75 3 ,01915 3 ,	2555
2,001136 30 575 3 ,01515 3 ,	
3,001704 31,775 4,020202 4,	2823
	TIT
4 ,002272 32 ,8 5 ,02525 5 ,	1388
5 ,002841 33 ,825 6 ,080303 6 ,	1856
	1944
34 1.85 7 1085353 7 35 1.875 8 1042404 8	2222
26 0 0 000051 0	25
WITE CUTEDING FOR AND TITO CONSERVED ITO	2777
	3055
P. D. Part. 39 1975	1.201
	1
1 ,025 Y: D. Part One Yard	
2 ,05 I ,004\$45 the Integer.	1
	1
4 pl 3 y017836 F. D. Part.	1
2	C 1
7 175 F. D. Part.	
TARTE	IX.
11 ,275 2 ,003030 1 A D L E	
	lear the
	Car Hue
15 375 Integer.	
16 14 Y. D. Part. M. D. Part. M.	D. Part
	,846153
10 475 2 763636 2 753040 12	,9230 76
2 545454 3 230769 11	D. Part.
21 525 4 3727272 4 307692	
120 1 c 1 5 600000 5 1304015 1 I	,01923
	,03846
	,05763
125 Sec 1 2 1 201010 9 10923071	
20 ,65 2 ,121212 9 ,092307 27 ,675 2 ,121212 10 ,76923	

D.

M	asure, Time		_
D. D. Part	D.D. Part.	TAB	LEX.
I ,002747 2 ,005494 3 ,008241 4 ,010988 5 ,013735	2 ,285714 3 ,428571 4 ,571428 5 ,714285 6 ,857142	Of Motion, Zodiac the D ^o ,D. Part.	A Sign of the Integer.
6 ,016482 One Month the Integer. W. D. Part. I ,25 2 ,5 3 ,75 D. P. Art I ,035714 2 ,071428 3 ,107142 4 ,142856 5 ,17857 6 ,214284 One Week the Integer.	0 ,057142 H. D. Part. 1 ,005952 2 ,011904 3 ,017856 4 ,023808 5 ,02976 6 ,035712 7 ,041664 8 ,047616 9 ,053568 10 ,05952 11 ,005472 12 ,071424 13 ,077376 14 ,083328 15 ,68928 16 ,095232 17 ,101184 18 ,107136 19 ,113088 20 ,11904 21 ,124992 22 ,130944	Do. D. Part. 1,033333 2,060000 3,1 4,133333 5,185000 6,2 7,233333 8,285000 9,3 10,325000 12,4 13,483333 14,4853333 14,486000 15,5 16,533333 17,580000 18,6 19,633333 20,80000 21,7 22,733333 23,780000	$\begin{array}{c cccccc} \hline & & & & & \\ \hline & & & & & & \\ 0 & & & & & \\ 0 & & & & &$
D. Part. 1 ,142857	23 ,136896	24 ,8 25 ,833333 26 ,86006 27 ,9 28 ,933333 29 ,985696 <u>M' D. Part.</u> 1 ,000555 2 ,00111	26,014144 27,015 28,014555 29,016411 30,014666 31,017222 32,017777 33,018<33 34,018888 35,019444 36,02

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Decimal Tables of Money, Weight,

-			-		-	0 '	_
M	D. Part.	15%.	D. Part.	S".	D. Part.	M'.D. I	Part.
37	,020\$55	15	,000137	54	,000496	28 ,48	5666
38	,02.1111	16	,000146	55	,000506	29 148,	\$335
39	,021666	17	,000155	50	,000515	30 35	
40	,C22222	18	,000164	57	,000524	31 51	8666
41	,022777	19	,000173	58	,000533	32 ,5%	3333
42	,028333	20	,000184	59	,000542	33 555	
43	,023388	21	,000193	1.000		34 ,50	6666
44	,024444	22	,000202	1.0	1.000	35 ,58	3333
45	,025	23	,000211	AL	egree the	36 ,6	
46	,025555	24	,00022		nteger.		8666
47	,026111	25	,000229	-		38 ,67	333
48	,026666	26	,000238	M	D. Part.	39 ,65	981
49	,027222	27	,000247	I	,016666		6666
50	,027777	28	,000256	2	,083333	41 ,68	333
51	,028733	29	,000265	3	,05	42 07	
52	,028888	30	,000276	4	,086666		\$666
53	,029444	31	,000285	5	,08,333	44 ,73	3333
54	,03	32	,000294	6	I	45 ,75	
55	,030,955	33	,000303	7	,116666		6666
56	,031111	34	,000312	8	,1 .3333	47 ,78	8333
57	,031656	35	,000322	9	,15	48 ,8	
58	,032222	36	,000331	10	,186666		6666
59	,032777	37	,00034	II	,183333	50 ,83	333
S".	D. Part.	38	,000349	12	,2	51 ,85	
0.	D. Fart.	39	,000358	13	,218666		6566
I	,0000009	40	,000368	14	,233333	53 ,88	833
2	,000018	41	,000377	15	,25	54 ,9	
3	,00027	42	,000386	16	,286666	1 - 6	\$660
4	,000036	43	,000395	17	,283333		3333
15	,000046	44	,000404	18	1.3	57 .95	
6	,000055	45	,000414	19	,318666		6666
17	,0000064	+0	,000423	20	\$33333		333
8	,000073	+7	,000432	21	1,35	S". D.	Part
19	,000083	48	,000441	22	,386666		
10	,000092	49	,00045	23	,38,333		027
11	,000101	50	,00046	24	,4		035
12	,00011	51	,000469	25	,418566		083
13	,000119	52	,000478	26	433333	4 ,00	rll
II.	,000128	53	,000487	27	,45	5,00	138

s.

Measure, Time; and Motion.

S'':	D. Part.	5".	D. Part.	15".	D. Part.	<i>S.</i> "	D. Part.
6	,001866	20	,00\$555	34	,009444	48	,013333
7	,001944	21	,005833	35	,009722	49	,013671
8	,002222	22	,006711	36	,01	50	,013888
9	,0025	23	,00638 8	37	,010277	51	,014166
10	,002777	24	,00#666	38	,010555	52	,014444
II	,003055	25	,006941	39	,010833	53	,014722
12	,003333	26	,007222	40	,01111	54	,015
13	,003621	- 27	,0075	41	,011388	55	,015277
14	,0038888	28	,00 <i>7</i> 777	42	,011,666	56	,018555
15	,004186	22`	,008055	43	,011944	57	,015822
16	,004141	30	,008,333	44	,012222	58	,016711
17	,004722	31	,0086x1	45	,0125	59	,016388
18	,005	32	,008888	46	,012777		
19	,005277	133	,0091 <i>6</i> 6	47	,013055		1

1

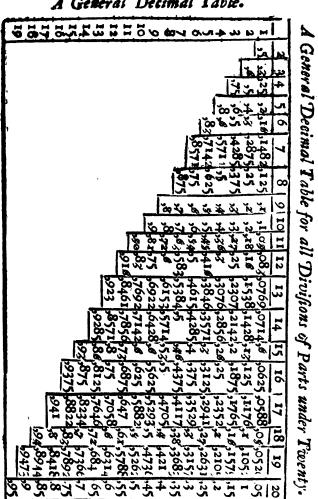
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A General Decimal Table.

The Explanation and Use of the foregoing general Decimal Table.

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r. The Figures at Top, which run to 20, flew the Number of Parts any Quantity or Integer is divided into; and the Figures in the fide Column are those Parts themselves; The Figures forming the triangular Space, and disposed into proper Columns, are the Decimal Parts of the Integral Quantity answering thereto. Hence any Quantity divided into any Number of Parts under 20, the Decimals answering to each of those Parts are seen in one view in their proper Column.

Example. Suppose a Quantity divided into Eight equal Parts, and you would know the Decimal Part equivalent to each: Look at top for 8, under which are disposed the Decimals, viz., 125, 25, 375 Sc. antiwering in order to the Parts in the fide Goluma.

2. The Figures in the fide Column may be taken for the Numerator, and those at top, for the Danominator of a Vulgar Fraction.

gar Fraction. Then the Decimal corresponding to thole two Numbers refpectively, is equal to the forefaid Fraction: Thus the Decimal 5714 answering to 4 in the file, and 7 at top, is equal

to the Fraction $\frac{4}{7}$. So $\frac{9}{13} = ,6922$. $\frac{5}{6} = ,83$. $\frac{6}{11} = ,84$. $\frac{13}{16} = ,8125$. $\frac{16}{19} = ,8418$. $\frac{19}{20} = ,85$ Gc.

Also any larger Fraction whole Parts are an Equimultiple of any of these tabular Fractions, or may be reduced to them, are equally answer'd in Decimals by this Table; see this Example $\frac{588}{1512} = \frac{84}{210} = \frac{21}{54} = \frac{7}{100} = 338$ Decimals in the Table.

Cafe 3. To reduce any Decimal into the equivalent known Parts of Coin, Weights, Measure, Motion, &c. observe this

Rule. Multiply the given Decimal by the Number of Units contain'd in the next lower Denomination of that Species of Quantity, which your Decimal is of; and thus proceed, till Reduction of Decimals, &c.

till you have converted your Decimals, or come to the lounest Part; and the *feveral Products* will be the *feveral Parts* of the Quantity required. See the following Examples.

EXAMPLE I.

What common Parts of a Pound (viz. Shillings, Pence, Sc.) are contain'd in 0,73825 Decimal Parts of a Pound? First, Multiply by 20 Shillings, the next lower Dem.

14,76500 Shillings.

Then Multiply by 12 the next lower De. to the last. 9,18000 Pence.

Laftly, Multiply by 4 the lowest Denomin. of all. 0,72000 Farthings.

Hence the Answer is 14 Shillings, 9 Pence, and 7 Tenths, or 72 Hundredths of a Farthing.

EXAMPLE II.

Reduce	0,72083	to	the	known	Parts	of a	Crown

	5	
	3,60416	
	12	
	7,24999	
		Infwer 3 s. 7 d. 4.
•	0,99999	
•		MPLE III.
Reduce		into known Parts of a Mark.
9) 2,671875	
	,2968750	-
	2671875	
	890625	Thus the Answer is exact with-
	11,8750000	out any Remainder, viz.
	12	Marks s. d.
	10,5000000	5 : 11 : 10 : ¹ / ₂ .
	4	· · ·
		•
	2,00000000	EXAM-

EXAMPLE IV.

Reduce ,727564 into the known Parts of a Pound Troy. 12 8,730768 20 14,615360 24 2461440 1230720 14,768640

The Answer is 8 oz. 14 penny wt. 14 gr. 3.

EXAMPLE V.

,49723 into the known Parts of an C. Weight. Reduce 4 1,98892 ·28 791136 197784 27,68976 16 413856 68976 11,03616 16 21696 3616 0,57856

٢

The Answer will stand thus, 1 gr. 27 lb. 11 oz. 01 dr.

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EXAMPLE VI.

Reduce ,578	r of a	Roð	into	irs	known Farts.
5,5	5				
289	r				
2892	3				
3,182,	- t				
_	3				
0,5#5	~ \$				
1					
6,558	5				

The Answer is 3 yds. 0 Ft. 6; In.; and this repeating Decimal ,058; over.

These fix Examples I imagine sufficient to shew the common Method of reducing Decimal Parts into the common and known Parts of any Species of Quantity.

But as those Operations of Reduction are for the most part very laborious, tedious, and require abundance of Figures, I have sometimes wondred that a Set of Tables have not been composed to facilitate this Part of Decimal Arithmetick, as well as for the contrary Operations of reducing different Species into Decimals; especially fince one is as necessary as the other. Tables for that purpose have long fince been contrived, but none for the reverse; to turn into, but not to turn out of Decimals.

Tis true, fome Decimals (as those of Money) have the first and fometimes the second Figure pretty easily valued by a finall Application of thought; but even this is for the Skilful to do, not for any that are but Tyro's, or rude in the Art. Yet how much Tables for Reduction of Decimals to vulgar Parts are wanting, may appear from the great Industry many have used to lay down Rules for that purpose. which being fo prolix, verbose, obscure, and consequently impertiment, that a Person wou'd sooner and with more ease and pleasure work out his Answer by the ordinary Method than by those unintelligible and infignificant Rules; and according to the old Saw, wou'd find the farthest way about, the nearest way home.

Description and Use of New Tables. 75

But having for Reafons already render'd determined to write a compleat Treatife of Decimal Arithmetick, I thought it could by no means be worthy of, or answer that Title, unlefs with many other Improvements, I could make one more to render this Part of the Art most easy and expeditious; and having imploy'd my Thoughts a little on this Topic, I foon perceived an Expedient that wou'd do the business, which was this.

Viz. To divide the Figures of Decimals into Pairs, from the left Hand to the right; then to tabulate the Digits of every Pair from Units to an Hundred, in proper Columns; and laftly, to affix the true Value of every Place of Figures in the Column appointely answering thereto.

So that by this means the Value of any two Places of Figures (fo far as they are valuable) in any Decimal, is feen by Infpettion only; and the Value of four or fix Places are as it were placed in one view, and with the greatest eafe and readinefs are obtain'd in any common Species of Coins, Measures, and Weight. But it being a Contrivance of my own, I thall not on that Account fay any thing as to their Merit; but only give a flort Description of the Tables and the Manner of using them by an Example of each.

A Description of the following new Decimal Tables.

For every different Kind of Decimals in common Ufe, I have composed a proper Set of Tables, and according as the Decimal is more or lefs valuable, it is divided into two or three Pairs; and to each of these Pairs is a Table exhibiting the true value of the Figures in each Pair from Unit to 100. The Tables of every fort are feen at the top of the Page; thus reprefented Table 1. Table 2. &c. Each Table confifts of feveral Columns; the first Column has at Top N°. to fignifie the Numbers of the Decimal Pairs. The other Columns (all but the laft) reprefent the Value of the Numbers in the first Column in the various Denominations of the Parts the Integer are vulgarly known by. The last Column contains the Decimal Parts of the last Denomination, and in every Table is marked with P.ts.

Having given a brief Explanation of the Tables in general, I fhall now fhew their Use in different the Value of L_2 any

76 Description and Use of New Tables, &c.

0Z.

any Decimal given, which is thus. Suppose you would know the Value of the Decimal ,689459 of a Tun Averdupois Weight, proceed thus; first divide those Numbers into Pairs as here, 68,94,57; then take the first right Hand Pair, viz. 57, and feek in Table 1. Averdupois Weight, and you will

find against $\begin{cases} 7 - 0 - 325 \\ 50 - 1 - 379 \end{cases}$ that is, 2,04; then for the fecond Pair, 94, look in Table 2. and against 94 you lee 21 16. Ooz. 52 posts.; and for the third Pair; 68, feek in Theble 3. and against 68 you observe 13 C. 2 gr. 11 th. 3,2 oz. So that these several Numbers added in a proper manner will ftand thus,

		С.	qr.	16.	02.
SPirft Pair ,57		00	:0:	00:	02,04
Against the Second Pair ,94		00	; 0 :	21:	00,52
Against the Second Pair ,94 Third Pair ,68		13	: 2 :	11:	03,2
Hence the value of ,689457	is .	13	: 3 :	04 :	05;76

Now that the Reader may fee at once both the Advantage and Exacinefs of the Tables; I shall shew the Work of finding the value of the faid Derimal, at large in the common way of Reduction, which is as follows.

$$,689457 \text{ of a Tur.}$$

 20
 $13,789140 = Handred.$
 4
 $3,156560 = Quarter of C.$
 28
 1252480
 313120
 $4,383680 = Pounds.$
 16
 2302080
 $383680 = Ounces.$
The

For Valuing of Decimals.

	C .	qr.	Ш.	0Z.
The Value this way is The Value by the Table is	13	: 3 :	04:	06,13 88 Sc.
The Value by the Table is	13	:3:	04:	05,76
The Difference only	00	:0:	•••	00,3788

Hence it appears how exact, and yet how eafy and expeditions these Tables are in the business of Reducing Decimals to their proper Value in the common and vulgar Parts of their proper Integer. I shall next give Examples of all kinds of Decimal Parts, in order to render the Use and Emoluments of these new invented Tables, as plain and obvious as may be; tho' they are of themselves as eafy to be understood as any Arithmetical Tables whatfoever.

EXAMPLE L

What is the Value of ,4725 of a	Pound Ste	rling ?
		s. d.
$ In \left\{\begin{array}{l} Table \ I, \\ Table \ 2. \end{array}\right\} \text{ againft } \left\{\begin{array}{l} ,25 \text{ is} \\ ,47 \text{ is} \end{array}\right. $	لمحمدو	$00:0:\frac{1}{2},4$ 9:4: $\frac{1}{4},2$
Table 2.5 "Burnin 2,47 is		9:4:4,2
	Anfwer	$9:5:\frac{1}{4},6$

EXAMPLE II.

Υ.

What is the Value of ,147 of a Shilling or 1	Foot A
	d. gr.
In $\left\{ \begin{array}{c} Table \ 1 \end{array} \right\}$ against $\left\{ \begin{array}{c} 70 \text{ is} \\ 14 \text{ is} \end{array} \right\}$	00 : 0,336
Table 2. 5 - 5 - 3, 14 is -	01:2,72
The Answer in d , and f , or In . and qr . is	01:3,056

EXAMPLE III.

What is the Value of ${}_{,7347}$ of a Pound Troy? In $\{ \begin{array}{c} Table 1. \\ Table 2. \end{array} \}$ against $\{ \begin{array}{c} {}_{,477} \text{ is } \\ {}_{,773} \text{ is } \end{array} = \begin{array}{c} 00: 01: 3,07 \\ 08: 15: 4,8 \\ 08: 16: 7,87 \end{array} \}$

EXAM.

The Use of the New Tables for

EXAMPLE IV.

What is the Value of ,91249 of a C. Weight Averdupois? Qr. lb. oz. dr.In $\begin{cases} Table 1. \\ Table 2. \\ Table 3. \end{cases}$ against $\begin{cases} ,92 \text{ is } - 0:00:00:02,58 \\ ,24 \text{ is } - 0:00:04:04,8 \\ ,91 \text{ is } - 3:17:14:11,52 \end{cases}$ Anfwer 3: 18:03:02,9

EXAMPLE V.

What is the Value of ,7777 of a Pound Apothecaries Weight?

In { Table 1. } against {	,77 is — ,77 is —	· 5 00 09	::	3 0 1	:	9 2 2	::	gr. 04,88 15,2
	Antwer	<u> 99</u>	:	.2	;	2	:	00,08

EXAMPLE VI.

What is the Value of ,8754 of a Tun, Wine Measure. P. Hg. T. G. In $\{ \begin{array}{c} Table \ 1. \\ Table \ 2. \end{array} \}$ against $\{ \begin{array}{c} ,54 \ is \\ ,87 \ is \end{array} - \begin{array}{c} 0:0:0:0:0:01,36 \\ 1:1:0:30,24 \end{array}$ Ansiver $\begin{array}{c} 1:1:0:30,24 \\ 1:1:0:316 \end{array}$

EXAMPLE VII.

What is the Value of ,7509 of a Load of Corn ? In $\{ \begin{array}{c} Table 1. \\ Table 2. \end{array} \}$ against $\{ \begin{array}{c} ,09 \text{ is} \\ ,75 \text{ is} \end{array} = \begin{array}{c} 2 & B. & G. \\ 0:0:0:0,28 \\ 3:6:0 \\ 3:6:0,28 \end{array} \}$

EXAM-

EXAMPLE VIII.

What is the Value of ,8495 of a Year . In $\{ Table 1. \}$ against $\{ ,95 \text{ is } -07:0:3:11,22 \ ,84 \text{ is } -10:3:5:14,4 \ Answer 11:0:2:01,62 \$

EXAMPLE IX.

What is the Value of ,889 of an Hour or Degree ?

$\ln \left\{ \begin{array}{c} Table & 1. \\ Table & 2. \end{array} \right\} \text{ againft} \left\{ \begin{array}{c} ,90 \\ ,88 \\ ,88 \end{array} \right\}$			00 52	: 32 ,4 : 48,
N	An	lwer	53	: 20,4

EXAMPLE X.

What is the Value of ,0596 of a Sign of t	the Zodiac A
	0 <i>1 1</i> /
In $\left\{ \begin{array}{cc} Table & I. \\ Table & 2. \end{array} \right\}$ against $\left\{ \begin{array}{cc} ,96 & is \\ ,05 & is \end{array} \right\}$	00:17:16
In Z Table 2. 5 against 2,05 is -	01:30:00
Anfwer	01:47:16

EXAMPLE XI.

What is the Value of ,976305 of a Mile?

					•		1	Fr	,	R.		Yd	•	Fi	•	In.
_	5	Table	1.7	againft	2	,05	is	0	;	00	:	0	:	0	:	00,91
In	3	Table	2.	🖌 againft	3	,63	is	0	:	02	:	0	:	σ	:	02,79
	L	Table	3.		L	۶97	is	7	:	30	:	2	:	0	:	07,2
					A	nfwe	r	7	:	32	:	2	:	0	:	10,3

EXAM-

The Use of the new Tables, &c.

EXAMPLE XIL

What is the Value of ,278 of a Yand fquare ? F.q. In.q. In { Table 1. } against { ,80 is. 0-: 10,33 2:61,92 Anfwer 2: 72,25

EXAMPLE XIIL

What is the Value of ,795007 of a Mile fquare? R. P. In Stable 1. Table 2. Table 3. Answer 508 : 3 : 08,71

EXAMPLE XIV.

What is the Value of ,974 of an Acre? Y. 0:00:19,36 3:35:06,05 $In \left\{\begin{array}{c}
Table I. \\
Table 2.
\end{array}\right\} again \left\{\begin{array}{c}
,40 \\
.97
\end{array}\right\}$ Anfwer 3: 35: 25,41

EXAMPLE XV.

What is the Value of ,629 of a Yard folid? In. In { Table 1. } against { ,90 is ,62 is 00: 419,94 16:1278,72 Anfwer 16: 1698.66

TABLE

A Set of NEW DECIMAL TABLES expressing the Value of any Decimal in the Known or Vulgar Denominations of the Integral Quantity, whether Money, Weight, Time, Motion, or Measure of every Kind.

Table I.	Of Money,	0ne	Pound the	Integer.
----------	-----------	-----	-----------	----------

NIC	211		The state		NIe	14		TD.	1.	NIC	<u>.</u>	· · ·	1 De	-1
IN'	?.ld.	f.	Pr.	1	N°	.j d.	J f.		-	Nº	'd.	f .	Pr.	I
1			,09		29	1		7.78	21-	1 57	Ī	1	1.18	L
		-	10					l'as	1	1.26	· 1	li	28	
		1	20	i	30	1		2,78 ,88 ,98	3	120	1:	1	122	L
2 3 4 5 6	1		,19 ,28 ,38 ,48 ,57 ,67	1.	31		1 :		31	57 58 59 60 61			,48 ,58 ,68 ,78 ,87 ,97 ,06	Ľ
4	-	-	,30	1	134	· —		,98	21	100	I	Ĭ	12	I.
	-	1-	,40	1	32 33 34 35 36 37 38 39		10 10 10 10 10 10 10 10 10 10 10 10 10 1	,17	1.	101	I		,07	ľ
0	-		»57		34		3	,27 ,37	1	02	I I	11	,97	ŀ
.7 8		-	107		35		3	1.37	1	03		2	,00	L
N N	1-	-	,76 ,86		36		3	1,40	1	64	I	2	,16 ,26	i
9	-	-	,86		37		3	1,56	1	65	I	2	,26	
9 10 11			,96 ,05		38	-	3	,46 ,56 ,65 ,75 ,84]	62 63 64 65 66 67 68	I	2	,35	[.
II		I	,05		39		3	1.75	}	67	1	· 2	,45	
12	-		,15		40	-	3	,84		68.	I	2	,54	
13 14 15 16	-	Т	,24 ,34		41		3	,94	1	69	1	2	,35 ,45 ,54 ,64 ,74 ,83 ,93 ,02	
14	1-1	I	,34	·	42	11	ō	,03	1.	70 71	I	2	574	
15		I	.11	· i	43	I	0	,12	Ł.	y i	I	2	,83	
16		1	52		44	1	0	,22	ŧ.	72	T	2	,93	
17		I	,44 ,53 ,53		.45	I	0	,32			I	2	.02	1.
17 18		1	70		46	I	ō	.11		73 74 75 76 77 78	1	2	,12	
1 10			,7 2 ,82	. 1	17		ō	,41 ,51 ,6		175	ſ	2	,22	
19 20		7 T	,92		47 48	I I	0	·/·		-6	i	21.	,31	
21	-		⁹	Í	40	I		, o			ī	3	20 1 T	
		2 2	, 51	.	49		0	%		40	i	31	24.	
22	i− 1		,11	- G	<u>5</u> 0	I I	0	,7 ,8 ,89 ,99 ,09	·			2	,41 , 9 ,6	
23 '24	-	2	2 ²⁰		51		0	,09		79 85	I I	21	, ,	·
24	-	2	,3 1		52	I	0	,99		00	I	-3	,7	
25 26		2 2	14 .		53	. I	1	,09		81	I	31	,79 ,89	
25		2	,49	j	54	. 1	1	,19		ŏ2	Ŧ	<u>`3</u>]	,09	
27 28	-	2 2	,3 ,4 ,49 ,59 ,68		54 55 56	7	I	,291		82 83	. 1		,98 ,06	••
28		2	,68 ^L		56	1	1	,381		.84	2	0	,06	

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Nº.

82 A Set of New Decimal Tables, &c.

N°.	<u>d.</u>	f.	Pt.	N°.	d.	f.	Pt.		N8.	d.	f .	Pt.
85	2	0	,16	90	2	0	,64		95	2	 I	,12
86	2	0	,25	91	2		,73		.96	2	I	,2I
87	2	0	,35	92	2	0	,83		97	2	I	,31
88	2	0	,44	93	2	0	,92	1	98	2	1	,4
89	2	0	,54	94	2	I	,02		99	2	1	,5

Table II. Of Money, one Pound the Integer.

INº	. f.	[d.	f .	Pr.		N°	f .	d.	f .	Pt.	ī	Nº.	1.	d.	f.	Pt.
		⊢-		I								-	- 1		-	
1 2 3 4 5 6		2	1	,6		29	5	9	2	› 4		57 58	11	4 7	0 10 0	,2
2	-	4	3	,2		30 31	6	0	0	,		58	11	7	0	,8
3		7		,8		31	6	2	I	,6		59 60	II	9	2	,4
4	,	9	2	> 4		32	6	47	.3 0 2 0 1	,2 ,8		60	12	0		,-
5	1	0	0	,		33	6		0			61 62 63 64 65 66 67 68 69 70 71	12	2	H MONOH MO	,6
6	1	2	I	,6		34 35 36	6777778888888999	9	2	, 4		62	T 2	4	3	,2,8
78	1	4	3	,2 ,8		35	7	0	0	,- ,6		63	I 2	7	0	,8
	I	7	0	,8		36	7	2	I	,6	Ċ	64	12	9	2	,4
9	I	9	2	,4		37 38	7	4 7	3	,2 ,8		65	13	0	0	2
10	2	0	0			38	7	7	0			66	τ3	2	1	,6
11	2	2	I	,6 ,2 ,8		39	7	9 0	2	, 4		67	13	4	3	,2
12	2	4	3	,2		40 j	8		0			68	13	7	0	,8
13	2	7	3 0 2	,8		39 40 41 42	8	2	2 0 1 3 0 2 0	,6		69	13	9	2	4
14	2	9	2	14		42	8	4 7 9 0	3	,2		70	14	0		1.1
15 16	3	0	0			43	8	7	0	,8		71	14	2	1	,6
16	3	2	I	,— ,6		43 44	8	9	2	,4		72	14	4	1 000	8
17 18 19	**************************************	4	30	,2 ,8		45 46	9			,-!		73	۲4	7		8
18	3	7		,8		46	.9	2 4 7	1	,6		74 75 76	14	9	20	4
19	3	9	2 C	,4		47	9	4	3	,2		75	15	0	0	2.1.8
20	4	0 2	C			47 48	9	7	Ċ	,8		76	15	2	11	0
21	4	2	I	, 6.		49	9	· 9	1 3 0 2	,4		77	15	4	3	28
22	4	4	2	12		50	10	0	0	,—		78	15)	7	200	8
23	4	4	3	,8,		5I	10	2		,6		79	15	9		4
24	4	9	2	,4	. 1	52	10	4	3	.2			16	0	0 13	
25	5	0				53	10	7	Ó	,8	Í	81	16	2	1,	6
25 26	5	2	1	, -		54	10	9	2	4		82	16	4	21	2 1
27	5	4	2	,2	·]	55	11	0	Ø	,		83	16	7	1,30	8
27 28	5	7	ó	,8 I	Ļ	55 56	11	2	II.	,6	ļ	83 84	16	9	2	41

Nº

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Nº.	ſ.	d.	f.	Pr.	Nº.	<u>] ſ.</u>	d.	f .	Pt.	ſ	Nº.	ſ. 1	d.	f ,∙	Pr.
85	17				90	18	0				95	19		-	,
85	17	2	I	,6	91	'18	2	I	,6		96	19	2	I	,6
87	17	4	3	,2	92	18	4	3	,2		97	19	4	3	,2
88	17	7	0	,8	93	18	7	0	,ð		<i>9</i> 8	19	7	0	,8
89	17	9	21	<u>,4 '</u>	94	18	9	21	,4		99	191	9	2	<u>,4</u>

Table I. Troy Weight, one Pound the Integer.

No	Pwt.	gr.	Pt.	INº.	Pwt	gr.	Pt.	I INº.	Pwt.	gr.	Pt.
1	1000	1-		-				1	-	-	0
I	-	-	,57	29	-	16	17	57	I	8	,84
2	1	I	1 1 1	30	-	17	,28	58	I	9	,4I
3	10	1		31	-	17	,85	59	I	9	,99
4	-	2	,388	32	-	18	143	60	I	10	,57
15	-			33	$\overline{}$	19	,-	6I	I	II	,14
345678	1111	34	:45	34	-	19	,58	62	I	11	,72
7	-	4	,03	35	-	20	,16	63	I	12	,29
	-	45	,6	36	-	20	,73	64	I	12	,87
9	-	5	,19	37	-	21	,31 ,88	05	I	13	,45
10	-	56	,76	38	-	21	,88	66	I	14	,02
II	-	6	,34	39	-	22	,46	67	I	14	,6
12	111	6	.91	40	-	23	,04	68	I	15	,17
13	- 1	7	,48	41	-	23	,61	69	I	15	,75
14	-	78	,001	42	I	Ó	,19	70	I	16	,33
15		8	,64	43	I	0	.76	71	I	16	0
16	-	9	,21	44	I	I	,34	72	I	17	,48
17	-	9	,79	45	I	I	,92	73	I	101	,05
17 18	F	10	,36	46	I	2	,49	74	I	18	,63
19	-	IC	,94	47	1	3	,07	75	I	19	,2
20		11	,52	47 48	I	3	,64	76	I	19	\$77
21	-	12	,09	49	I	4	,22	77	I		35
22		12	,67	50	1	4	,8	78	I		,92
23	-	13	,24	51	I	5	,37	79	I		,5
24	-	13	,82	52	I	5	,95	80	1	22	,08
24 25	-	14	,4	53	I	6	,52	81	I	22	,65
26	-	14	,97	54	I	7	,I	82	I		,23
	-	15	,55	55	i	7	,69	83	il	23	,8
27 28	-	16	,12	56	I	8	,26	84	2	pi	.28

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Nº.	Port.	gr.	Pt_{\cdot}	Nº.	Put	.gr.	Pt.	Nº.	Pwt.	gr.	Pt.
85	2	c	,96	90	2	13	,84	25	2	6	,72
86	2	11	,53	91	2	4	,4I	96	2	7	,29
87	2	2	,11	92.	2	4	,99	97	2	7	,87
88	2	2	8ک,	93	2	5	,56	98	2	8	,44
89	2	13	,26	94	2	16	,14	99	2	9	,02

Table II. Troy Weight, one Pound the Integer.

Nº.	02	psp	gr.	20.		02.	10	gr.	pt.	1	V°.	oz.	pw.	gr.	pt.
1	-	2	9	,6	29	3	9	14	74		7	6	16	19	2
2	-	4	19	,2	30	3		0		4	8.	6	19		-8
3	-	7	4	,8	31	3		9	,6		9	17	I	14	24
4	-	9	14		32	3		19	,2	1	50	17	4	0	
5	14	12	0	,-	33	3	19	4	,8	1	51	17	6	2	6
6	1	14	9	,6	34	4	I	14	.4		52	7	8	19	,2
7	-+	16	19	,2	35.	4		0	,-	1	53	17	11	4	,8
8	4	19	4	,8	36	4	6	9	,5		54	7	13	12.11	14
2	1	1	14	14	37	4		19	,2		55	17	16	0	,
IO	1	4	C	,-	38.	4	11	4	,8		56	17	18	2	,6
11	1	6	9	,6	39	4	13	1.1	1,4		57	8	0	19	,2
12	1	8	19		40	4	10	0	,-		58	8	3	4	,8
13	1	11	4	,8	41	4	18	9	,6		59	8	15	14	,4
14	1	13	14	.4	42	5	0	19	,2		70	8	8	0	-
15	11		C	-	43	1 5		4	,8	1 1:	71	8	10	9	,6
16	1	18	2	,6	44	5	5	14	1.4	18	72	8	12		,2
17	12	0	19	,2	45	5	8	0	,-		3	8	15	4	,8
18	2	3	4	,8	46	5	10	9	,6		4	18	17	12.0	54
19	2	5	14	14	47	5		19	,2		5	19	0	Ó	,-
20	2	8	0	1-	48	5		4	,8		16	9	2	9	,6
21	2	10	9	,6	49	5		14	1,4	1 7	7	9	4	19	,2
22	2	12	19	,2	50	6		Ó	1,-	5	8	9	7	4	,8
23	2	15	4	,8	51	6	2	9	,6		19	9	0	14	,4
24	2	17	14	.4	152	6	4	19	,2		30	9	12	0	-
25	3	a	Ċ	-	53	6		4	,8		11	19	14	9	,6
26	3	2	9	,6	54	6	9	14	24	1 8	32	19	16	19	,2
27	3	4	19	,2	55	6	12	ò	-		33	19	19	4	,8
28	13	7	4	,8	56	6	14	2	,6	18	1	IO	I	14	4

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Nº.

A Set of New Decimal Tables, &c.

N°.	0z.]	pw.	gr.	pt.	N٩.	3 Z -	pw.gr pt.	N°.	oz.	pw.	gr.	P5 .
85	10	4	0	,	90	10	16 C,	95	11	8	0	-
86	10	6	9	,6	91	ıς	18 9,6	96	II	10	9	.6
87	10	ð	19	,2	92	II	019,2	97	11	12	19	.2
88 89	10	11	4	,0	93		3 4,8 5 14,4	9 8 99	11	15	4	,8

Table I.

Table II. { Troy Weight, one Ounce the Integer.

1-Nº	Pwt.	gr.	Pts.	1	Nº.	Pwt.	gr.	Pt.		Nº.	Pwt.	gr.	Pt.
· · · · · ·								- ,8					
I			,048		I		4	,ð		29	5 6	19	,2
2 3 4 5 6			,096		2		9	,6		30 312 334 356 78 90 41	6	0	,
1 2			,1 44		3		14	,4		31	6	4 9	, 8
4			,192		4		19	,2		32	6	9	,6
2		<u> </u>	,24 ,288		3 4 5 6	I	0	<u>ا، ج</u>		33	6	14	, 4
		۱ <u> </u>	,200			I	4	,8		34	6	19	,2
7			,336 ,384		7 8	I	9	,6		35	7	0	,—
0		Γ.	,304		ð	I	14	,4		30	7	4 9 14 19	,9 ,8 ,6
9 10		F -	,432 ,48 ,96		9	I	19	,2		37	7	9	,6
15			,40		10	2 2	0	,_		38	7	14	,4
20		Ϊ.	,96		11		4	,8		39	7	19	,2
30		1 1	,44		J 2	2	ģ	,6		4 ⁰	8	0	,—
30 40 50 60 70 80 90			,92		13 14 15 16	2	14	,4		4 ^I	666677777888888999999 10	4 9	,
50		2 2	,4 ,88		14	2	19	,2		42	8	9	,6
00			,00	Ι.	15	3	0	,8		43	8	14 19	, 4
70		3 3	,36 ,84			3	4 9	, °		44	8	19	,2
00		3	,04		17 18	3	29	,6		44 45 46	9	0	,
195		4	, <u>5</u> 2	1		3	14 19	,4		40	9	4 9	,— ,8
					19	3	19	,2		47 48	9	9	,6
					20	4	0	,° ,8		48	9	14	,4
				1	21	4	49	,0		49	9	19	,2
1	1		1		22	4	9			50	10	0	,
	1				23 24 25 26	3333444445555	14 19	1,4		50 51 52 53	10	4	,8
			1		24	4		,2		52	10	9	.,6
			1		25	5	0	, 8		53	10	14	174
1	1			1		5	4	,ð		54	10	19	,2
1		1		1	27 28	15	9	,6		54 55 56	II	0	,
L	1)	1	1	28	5	14	1,4	1	156	11	14	;8

Nº.

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A Set of New Decimal Tables, &c.

Nº.	Pwt.	8r.	Pt.	Nº.	Fwt.	gr.	Pt.	N°.	Pwt.	87.	P1.
57	II	9	,6	72	11	9	,6	87	17	9	,6
58	II	14	5 4	73		14	, 4	88	17	14	> +
59	11	19	,2	74	14	19	,2	89	17	19	,2
60	12	0	,	75	15	0	,—	9 0	18	0	,-
16	12	4	,8	76	15	4	,8	91	18	4	,8
62	12	ġ	,6	77	15	9	,6	92	18	9	,6
63	12	14	5 4	78	15	14	,4	93	18	14	7 4
64	12	19	,ż	79	15	19	,2	94	18	19	,2
65	13	0	·,	8 5	16	0	,—	95	19	0	,—
66	13	4	,8	81	16	4	,8	96	19	4	,8
67	13	9	,6	82	16	9	,6	97	19	9	,6
68	13	14	,4	83	16	14	,+	98	19	14	,4
69	13	19	,2	84	16	19	, ²	<i>9</i> 9	19	19	,2
70	14	0	,-	85	17	0	,—				
71	14	14	,8	86	17	4	,8				

Table I.

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Table II. { Averdupois Weight, one Pound the Integer.

Nº.	dr.	Pts.	-	Nº.	oz.	dr.	Pt.		N°.	oz.	dr.	Pt.
												7
II		,025		I		2	,56		19	3	0	,64
2		,051		2		5	,12		20	3	· 3	,2
3		,076		3		7	,68		2₽	3	5 8	,76
		,102		4		10	,24		22	3	8	,32
1 2		,128		5		12	,8		23	3	10	,68
456		,153		4 5 6		15	,36		24	かででか 4	13	,44
		,179			1	Í	,92		25	4	Ō	,
78		,204	1	7 8	ī	4	,48		26	4	2	,56
			1	9	Ī	7	,04	1	27	4	5	. I2
9		,23		10	l i	9	,6	1	28	4	7	,68
10		,256		11	Î	12	,16		29	4	10	,24
20		,512					(·	ł			12	,8
30		,768		12	I	14	,72		30	4		26
40	I	,024		13	2	I	,28		31	4	15	,36
50	I	,28		14	2	3	,84	1	32	5	I	.92
60	I	,536		15	2	6	,4	1	33	555	4	,48
70	1	,792		16	2	8	,96		34	5	7	,04
80	2	,048		17	2	11	,52		35	5	9	.6
90	2	,304		18	1 2	14	,08	1	36	15	12	,16

Nº.

A Set of New Decimal Tables, &c.

		1			510		1.	1. 13.4		110	-	. 7	1.0.4
Nº.	02.	dr.	Pt.	ł	Nº.	oz.	dr.	<i>Pt</i> .		N°.	, oz.	dr.	Pt.
1		1.7	1		58	1		1.0		-	100	1.2	
37 38	5	14	,72	}	20	9	4	,48	1	79 80	12	10	,24
30	6	I	,28		5 9 6 0	9	7	,04	Ł		12	12	,8
39	6	36	,84	1		9	9	,6		81	12	15	;36
40	6	6	14	ł	61	9	12	,16	ł	82	13	L I	.92
41	6	8	,96		62	9	14	,72	1.	83	13.	4	,48
42 .	6	111	,52		63	IÇ	i	,28	t	84	13	4	,04
43	6	14	,08		64	10	2	,84	ŀ	85	13	9	,6
44		6	,64		65	10	3 6	5 4		85 86	13	12	,16
44 45 46	7 7 7 7 7	1	,2 ,2		66	10	8	,96		87	13	14	,72
172	4	3 5 8	12		67	10	11	50		88		-+	28
40	<u></u>	6	,76		68	10		,52 ,08		89	14	I	,28 ,84
47 48	7		,32 ,88		60		14	,00			14	3	
40		10			69	II	0	,64		90	14	368	, 4
49	7	13	, 44		7 0	п	3	,2		9 1	14		,96
50	8	0	,—		71	11	5	,76		92	14	11	,52
49 50 51	8	2	,56		72	11	8	,32		93	14	14	,08
52	8	5	,12	- 1	73	11	10	,32 ,88	- 1	94	15	0	,68 ,64
53	78888888	7	,68		74	11	13	,44		95	15		,2
54	8.	10	,24		75	12	ő	,		96	15	- KI	,76
	8.	12	,8		76	12	2	,56		97	15	358	.22
55 56	8		26		77	12	5	,12		<u>98</u>	15	10	,32 ,88
22		15	,36		78			,68				- 1	"
57	91	11	,92		10 1	12	7	,00		<u>99</u>	151	13	<u>974</u>

Table I.

Table II. { Averdupois Weight, one C. or 112 lb. the Int.

Nº.	dr.	Pt.	Nº Nº	. oz.	dr.	Pt.	Ī	Nº.	joz.	dr.	Pt.
I		,02	II		2	,86	I	12	2	2	,4
2		,05	2		5	,73		13	2	5 8	,27
3		,08	3		8	,6		14	2	8	,13
4		,11	4		11	,46		15	2	11	,ວ່
5		,1 4	5		14	,33		IÓ	2	13	,87
6		,17	6	1	1	,2		17	3	Ō	,73
7		,2	7		4	,06		18	3	3	,6
8		,22	8	1	6	,93		19	3	6	,47
9		,25	9	1	9	,80		20	3	9	,34
10	- •]	,28	10		12	,67	:	21	3	12	,2
20	1	<u>,57</u>	111	. 11	15 1	,53		22	3'	15	,7

Nº.

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 Table I.
 Table II.
 Averdupois
 Weight,

 one C. or 112 lb. the Int.

Table

A Set of New Decimal Tables, &c. 89

Table I.

Table II. SAverdupois Weighte

						:				·			
Nº.	16.	0Ż.	dr.	Pt.	19	. 0	. 1	2	3	16.	りえ.	dr.	Pt.
-				100	-	Nº		T	1 m - 1		0	•••	· · ·
76	-	13	9	i89			25	50 51	75 76	C 1	I	0 4	57 2
77 78	-	13 13	12 15	275 162		12	27	52	77	-2,	3	13	,44
79		14 14	1) 2	,49		3	28	53	78	3	5	12	,16
80	_	14	.5	,36		4	29	54	79	.4	7	10	,88
81		14	8	,22		15	3 Þ	55	85	5	9	9	,6
82	_	14	11	,09		5	31	56	81	·6	II	8	,3Z
83		14	13	,96		8	32	57	82	78	13	7	,04
197		15	0	,82			33	58	83		15	5	,76
85 86		15	3	,69		.9	34	59	84	IO	I	4	,48
86	-	15	6	,56		10	35	60	85 86	11	3	3	,2
87	-	15	9	,4I		11	36	61 62	87	12	15	I	,92 ,64
88	-	15	12	,28		12	37 38	63	88	13 14	78	d	,36
89 90		15	15 2	,15 ,03		13 14	39	64	89	15	10	5: 14	,°8
91	li	0	4	,89		15	40	65	90	16	12	12	,8
92	l i	0	7	,76		16	41	66	91	17	14	11	,52
93	Ī	0	10	,63		17	42	ŏ7	92	19	σ	10	,24
94	II	0	13	,49	•	18	43	ŏ8	93	20	2	8	,96
95	I	1	ó	,36		19	44	89	94	21	4	7	,ó8
96	I	I	3	,23		20	45	70	95	2 2		6	,4
97	ļΓ	I	6	,09		2 I	46	71	96	23	8	5	,12
98	I	I	8	\$96		22	47	72	97	24	10	3	,84
99	I	I	11	,83		23	48	73	98	25	12	2	,56
	<u> </u>			<u>.</u>	<u>'</u>	124	42	74	199	26	14	1	,28
											:		
			1	നം	ble	TT	{ A on:	vèrl	lap.	015	I	Nei	ght,
Т	able	: I.		: 1 a	DIE	11.	l on:	; T	un	or L	oat	th	e Int.
							- -				}		
INP.	16.	P		Na	116.	,0Z. 1	Pt.		Nº	. 16	. 10	z.	Pt.
T	1.	ā.	2	T	10	3	,58		5	1 1		T	,9
2	- •	. ,0		2	0	7	,16		56	1		5	,48
3		· ,1		3	0	10	574	t	7.8	1		9	,06
4	• •	. I, _I	4	4		114	,32	<u> </u>	8	1	ť	2	,64

N

Nº.

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90 A Set of New Decimal Tables, &c.

$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	<i>P</i>
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	42 ,58 ,16 ,77 ,9 ,46 ,40 ,64
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	42 ,58 ,16 ,77 ,9 ,46 ,40 ,64
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$,58 ,16 ,74 ,52 ,40 ,40 ,64
0 ,28 12 2 10 ,96 51 11 6 9 ,32 13 2 14 ,54 52 11 10 10 ,35 14 3 2 ,12 53 11 13 20 ,41 15 3 5 ,7 54 12 1 30 1 ,07 16 3 9 ,28 55 12 4 40 1 ,43 17 3 12 ,86 56 12 8	,58 ,16 ,74 ,72 ,9 ,48 ,06
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$,16 ,74 ,32 ,9 ,48 ,06
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$,74 ,32 ,9 ,48 ,06
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$,32 ,9 ,48 ,06
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$,48 ,06 ,64
40 1 ,43 17 3 12 ,86 56 12 8 50 1 ,79 18 4 0 ,44 57 12 12	,06 ,64
	.64
	,04 ,22
	,22
70 2 ,5 20 4 7 ,6 59 13 3 80 2 ,86 21 4 11 ,18 60 13 6	
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$,0 _0
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$, <u>5</u> 0
$\begin{array}{cccccccccccccccccccccccccccccccccccc$,96 154
$\begin{array}{cccccccccccccccccccccccccccccccccccc$,12
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$,7 ,7
$\begin{array}{cccccccccccccccccccccccccccccccccccc$.28
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$,28 ,86
29 6 7 82 68 15 3	,44
30 6 II ,4 69 IS 7	.02
31 6 14 ,98 70 15 10	.6
32 7 2 ,56 71 15 14	,18 ,76
33 7 6 :14 72 16 1	,76
34 7 9 ,72 73 16 5 35 7 13 ,3 74 16 8	,34
35 7 13 33 74 16 8 36 8 0 ,88 75 16 12	,92
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$,34 ,92 ,5 ,0 8 ,66
37 8 4 ,46 76 17 0 - 38 8 8 ,04 77 17 3	,°ð
	,00
39 8 11 ,62 78 17 7 40 8 15 ,2 79 17 10	,34 ,82
40 8 15 ,2 79 17 10 41 9 2 ,78 80 17 14	,02
41 9 2 ,78 80 17 14 42 9 7 ,36 81 18 1	,4 ,98
	,90 ,56
	,14
44 9 13 ,52 83 18 9 45 10 1 ,1 84 18 12	,72
45 10 1 ,1 84 18 12 46 10 4 ,68 85 19 0	.2
46 10 4 ,68 85 19 0 47 10 8 ,26 86 19 3	,3 ,88
	1

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Nº.

A Set of New Decimal Tables, &c.

Nº.	16.	oz.	Pt.		Nº.	16.	oz.	Pt.	Nº.	16.	oz.	Pt.	1
87	19		,46		92	20	9	,36	97	21	11	,26	[
88 89	19 19		,04 ,62		93 94	20 21		» <u>9</u> 4	98	21	14	,84	ľ
90	20		,2	, ,	94 95	21		,52 ,I	99	22	2	,42	ŀ
91	20	5	,78		96	21		,68.					

Table III. Averdupois Weight, one Tun the Integer.

N°	. C.	Q.	116.	oz.	Pt	1	N	C.	<u>q.</u>	116.	oz.	Pt	-
					1				124			4	ł
I	.0	0	22	6	,4		29	5	3	5	9	.6	I
2	0	I	16	12	,4 ,8		30	56	. 3	5	0	-	ł
3	0	2	22 16 11 .5 0	3	,2 ,6	1	31	6	0	22	6	1.4	ł
4	0	3	5	ģ	,6	ŀ	32	•6	01	16	12	1.3	ł
5	J	Ó	Ó	0		F	33	.6	2	II	3	.2	I
6	0 L I I	0	22 16 11	3 9 0 6 12	.4	Ľ	34	6	2 3 0		9	6	ł
7	I	I	16	12	.8		25	7.	6	5	1.0	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	ł
8	1 1	2	11	2	.2	ľ	36	7	ō	22	6	1.4	ł
I 2 3 4 5 6 7 8 9 10	1	3	5	9	, 48, 7 , 49, 7 , 6		37	1 4	0 1	16	12	12	l
10	2	ó	ó	ō			28	1 4	2	11		,0	l
-11	2	.0	22	3 9 0 6	A.		20	4	2	Ē	2	P: 16 , 48, 26 , 48, 26	ŀ
12	2	.0 I	5 0 22 16 11 5 0	12	, 400 20		331 2 3 3 4 5 6 7 8 9 0 1 2 4 3	6 6 7 7 7 7 7 8 8 8 8 8 9 9 9 9 9 9 10	30 0 1 2 30	5	3 9 0	,5	l
13	2	2	11	12 .3 9 0	.2		11	Ř	.0	22	6	1	
14	2	2	5		.6	•	12	l ă	·U	22 16	12	な	
15		3	ó	6	,		12	ă	2	11	12	,0	
16		0	22	6	,		17) 11	Ř	2		39 06	,4	
.17		0 I	22 16 11	12	,4 ,8 ,2 ,6		44		3	5	9	,0	l
18	2	2	TT		,0		+)	2	~	0	4	,-	l
19	2	2	ैंद	3	7		40		÷	-4	0	な !	l
20		0	· 5 0	: 0			4/	2	0 I 2'	22 16 11	12	,0	į
21	3 3 3 3 3 4 4 4	230012	22	6	,4 ,4 ,4 ,2 ,6		40	2	2	11	12 3 9 0 6	tor vor ' tor vo	
22	4	7	22 16		なし		47	2	3 0	` 5 0	9		
22	4	2	11	12	"		20		0	0	0	,—	
24		2		2	" <u>~</u>		21	10	0 I	22 16		·4	
-11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28	4	3. 0 0	.5 ∶0	3 9 0 6 12	,0		445678905535556	10	I	16	12	,4 ,8 ,2 ,6	
26				2	2		53	10 10	2	11	3906	,2	
27	5	I	22 16	0	,4 ,8 ,2		54		3	- 5 - 0	9	,6	
28	21		1	12	,0		55	11	0	· 0	0		
20	<u>. 51</u>	2	II	3	,21	1	56	11	0	22	61	,	

N 2

N?:

92. A Set of New Decimal Tables, &c.

1 110	C.	Δ	72 .		Pt.		Nº.	<i>C</i>	0	16.	07	Pt.	i -
INº.	0.	Q.	16-1	et.	1.40	·			8		oz.	E+.	
57	11	I	10	12	,8		70	15	3	5	9	,6	
58	11	2	11	3	,2		79 80	16	ó	á	ó	,0	
59	11	3	3	ó	,6	ζ	81	16	· 0	22	6		
60	12	õ	Ó	9. 0			82	16	Ĩ	16	12	,4 ,8	ľ
61	12	õ	22	6'	,		82	1 6	2	'II		,2	ł
62	12	1	16	12.	,4 ,8		83 84	¥6			390	,6	Ļ
							8-		30	5	2		
63 64 65 66	12	2	11	39	,2		85	17	•	0		\$	
04	12	3. Q	5	9	,6		86	17	0	22	6	14	
95	13 13			a 6	· • • •	F·	87	17	I	16	12	,8	
60		0	22		,4		88	17	2	11	39	,2	L
67 68 69	13	ľ	16	ξ 2	12 16	ľ	89	17.	1 3	5	9	,6	
68	13	2	11	3	12		90	18	0	. 0	0	,0	l
69	13	3	5	- 3 9 0	6		9. I	18	0	22	6	.4	
70	14	O O	Ó.	0			92	18	II	16	12	,4 ,8	ł
71	14	0	22	6	,4	1	93	F 8	2	II	3	,2	
72	14	ł r	16	42	,4 ,8		94	18	13	5	19	,6	l
73	14	2	111	3	.2	1	195	19	3	Ó	0	,	ł
74	114	3	5	39	,2 ,6	ŀ.	96	119	0	1,22	6	14	ļ
75	15	10	Ιô	10	1-	1.	97	19	T	16	12	,4 ,8	I
75 76	15	0	22	6			98	19		111	3	,2	I
77.	15	Ĩ	16	1,2	,4 ,8	1	99	19		5	9	,6	ł
78	IR	2	11	3	,2		175	1 29	3	10	1 9) "	
14		1 4	P . I .		1.94			!					1

Table I.

Table II. { Apothecarics Weight, one the Integer.

Nº.	Э	gr.	Pi.	D	10.	3	31	Э	gr.	Pt.	Ī	Nº.	3	3	Ð	gr.	Pi
I			,56	ìΠ	1			2	17	,6		11	I	2	1	13	,6
2		1	,15	£ 1	2		I	2	15	,2		12	1	3	1	11	,2
3		1	,72	1	3	17	2	2	12	,8	1	13	1	4	1	8	,8
4		2	3		4		3	2	10	14	ΕP	14	I	5	1	6	•4
5		2	,60		5	17	4	2	8	200	Ы	15	1	6	I	4	1-
0	77	3	,45	1	0	17	12	2	5	,0	EI.	10	1	7	1	1	,0
8	50	4	,03	-	8	1.	7	2	0	.8	П	17	2	1	0	19	$^{2}_{.8}$
9		5	,19		9	I	0	I	18	,4	И	19	2	2	C	14	14
10	17 2	5	,76		0	1 1) I	1	16	,-	15	20	2	3	C	112	

Nº,

A Set of New Decimal Tables, Sec. <u>Ì</u> Nº G. P. Nº.G. P Pt. N٩ G. Pt. Ρ. Pr. **,8**4 ,88 ,64 ,68 5 81 Şτ 71 44 ,24 57 0 **91** 2 82 ,28 72 5 57 58 45 2 51 92 7 7 ;72 ,76 83 84 85 86 73 45 ,92 52 2 ,32 93 4 ,96 46 4 52 7 ,36 <u>5</u>9 74 94 95 96 6 75 76 59 60 8 47 2 53 4 ,4 ,04 ,08 30 ,84 ,88 47 48 7 54 ,44 ,48 87 88 ·6 61 4 54 55 56 97 98 7**7** 78 ,12 3 0 ,50 61 5 49 ,92 ,16 79 80 6 89 62 49 ,50 2 ,96 99 3 90 56 5 в 50 ,2 Beer Méafure. Table I. Table II. 071 Nog bead the Integer. Ne No P. Pt. Nº. G. Pt, G., P. **,3**2 ,64 ,04 4 3 ,36 0 23 12 I I ,08 2 2 I σ I2 7 .68 24 ,96 345678 ,12 3 I 4 1 25 13 4 2 ,28 26 14 ,17 4 Ç 32 23 516 ,6 5 ,64 14 ,21 27 4 <u>,</u>25 ,92 28 15 à **.9**6 ,34 ,38 ,24 ,50 ,88 7 8 IŚ 5 ,28 3445567788 29 2 6 ,6 16 30 1 9 9 i 31 5262 16 ,92 **,**2 , 10 ,43 ,86 10 3730 32 17 ,24 į : ,56 ,88 ,52 ,84 ,16 ,48 ,8 17 20 <u>3</u>3 11 18 34 30 ,29 I 12 ,72 ,16 18 40 I 13 35 ,2 7 3 7 į ,52 ,84 50 36 2 14 40515 19 4 60 37 2.3333 **,**59 19 15 38 70 ,02 16 ,I2 20 4 ,16 80 ,48 ,8 ,45 ,88 9 39 17 ,44 21 **9**0 18 9 ,76 40 2I 4 ,08 10 2 ,12 19 Ò 4I 22 IQ 6 ,44 ,76 20 ,4 :5 1 6 42 22 21 II 2 ,72 43 23 23 .08 22 II 7 .04 44

Nº,

T	able	I.	 	Ta	ble	п.{	Win bead	le]	Meaf e Inte	ure, ger.	one	Høgs-
TNY	Ρ,	Pt.		Nº.	G. 1	P.	Pt.	Ń	Nº.	G.	<i>P</i> .	Pt. f
120000000000000000000000000000000000000	1.1.1.1.223344	Qu 1 2 2 3 3 5 4 4 5 L 5 L 5 Q 5 Q 5 Q 5		1 2 3 4 5 6 7 8 9 10 11 2 13 4 5 6 7 8 9 00 11 2 13 4 5 6 7 8 9 00 11 2 3 4 5 6 7 8 9 00 11 2 3 4 5 6 7 8 9 00 11 2 3 4 5 6 7 8 9 00 11 2 3 3 4 5 6 7 8 9 00 11 2 3 3 4 5 6 7 8 9 00 11 2 3 4 5 6 7 8 9 00 11 2 3 4 5 6 7 8 9 00 11 2 3 4 5 6 7 8 9 00 11 2 3 4 5 6 7 8 9 00 11 2 3 4 5 6 7 8 9 00 11 2 3 4 5 6 7 8 9 00 11 2 3 4 5 6 7 8 9 00 11 2 3 4 5 6 7 8 9 00 11 2 3 4 5 6 7 8 9 00 11 2 3 4 5 6 7 8 9 00 11 2 3 4 5 6 7 8 9 00 11 2 3 4 5 6 7 8 9 00 11 2 3 4 5 6 7 8 9 00 11 2 3 4 5 6 7 8 9 00 11 2 3 4 5 6 7 8 9 00 11 2 3 4 5 6 7 8 9 00 11 2 3 4 5 6 7 8 9 00 11 2 3 4 5 6 7 8 9 00 11 2 3 3 4 5 6 7 8 9 00 11 2 3 4 5 6 7 8 9 00 11 2 3 3 4 5 6 7 8 9 00 11 2 3 3 4 5 6 7 8 9 00 11 2 3 3 4 5 6 7 8 9 00 11 2 3 3 4 5 6 7 8 9 00 11 2 3 3 4 5 6 7 8 9 00 11 2 3 3 4 5 6 7 8 9 00 11 2 3 3 4 5 6 7 8 9 00 11 2 3 3 4 5 6 7 8 9 00 11 2 3 3 4 5 6 7 8 9 00 11 2 3 3 4 5 6 7 8 9 00 11 2 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	111233455667889000111233345567788900212	57 7416 30 52 7416 30 52 7416 306 30 52 7416 30	48 26 26 26 26 26 26 26 26 26 26 26 26 26		678901234567890123456789012345666666666897	2233425562778889001223344555677789990011223344	527416 30 527416 416 30 527416 30 527416 30	48 26 48 26 48 29 1 0 0 1 1 2 2 8 26 44 4 5 5 6 6 8 2 6 2 6 7 7 8 8 8 9 9 1 0 0 1 1 2 2 8 26 4 4 4 5 5 6 6 4 8 2 6 7 7 8

75 76 77 78 79 80	G. 44 44 45 45 46 47 47 47 48 49 49 50	P. P. 5 . 8 2 . 7 . 9 7 . 9 7 . 9 7 . 0 . 1 1 . 1 6 . 1 . 2 . 2 7 . 9 9 9 9 . 0 . 0 . 1 1 . 1 6 . 1 . 1 6 . 1 . 1 . 2 . 2 . 2 . 2 . 9 . 9 . 9 . 9 . 9 . 9 . 9 . 9 . 9 . 9	- 48 26 - 48 26	81 82 83 84 85 85 85 85 85 85 85 85 85 85 85 85 90	515555555555555555555555555555555555555			48 2 6 48 2 6	N 91 92 93 94 95 96 97 98 99	- 1 57 57 58 59 60 61 61	274163052	P:. 44, 58 776 8, 88 92 96 1
N°. I 2 3 4 5 6 7 8 9 10 20 30 40 50 60 70 80 90	P. I	I. Pt. ,04 ,08 ,12 ,21 ,25 ,34 ,38 ,38 ,38 ,38 ,38 ,38 ,38 ,38		N ⁹ 1 2 3 4 5 6 7 8 9 10 11 12 3 4 5 6 7 8 9 10 11 12 3 4 5 6 7 8 9 10 11 12 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 16 17 17 17 17 17 17 17 17	able G-0 I I 2 2 3 3 4 4 5 5 6 7 7 8 8 9 9 10 11 11	P. 40 41 51 6 26 37 30 40 51 5 26 2 7	P 1 3 4 9 2 6 2 4 5 8 2 5 8 4 6 8 1 4 7 8 4 7 0			G. 12 12 13 14 15 16 17 18 18 19 20 21 21 22 23 23		

Nº,

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A Set of New Decimal Tables, &c.

TNº	G.	P .	Pt.		Nº.	G.	<i>P</i> .	Pt.	T	Nº.	G.	P .	Pt.
1	24	2	*		64	34	4	-48		83	44	6	
45 46	24	6	,72		65	35	0	,48 ,8		84	45	2	,56 ,88
47	25	3	,04		66	35	5	,12		85	45	7	,2
47 48	25	7	,36 ,68		67	36		,44		86	46	3	,52 ,84
49 50	26	3			68	36	5	,76		87	46	7	,84
50	·27	0	,		69	37	26	,68		88 89	47 48	4	,16
51	27 28	4 0	,32 ,64		70	37 38	0 2	,4 ,72		.90 .90	40 48	0	,48 ,8
52	28	4	,96		71 72	38	7	,04		91	49	4 0	,0 ,12
53	29	ī	,28		73	39	3	.26		92	49	5	,44
54 55 56	29	3	,6	· ·	74	39	· 7	,36 ,68		93	50	í	,76
56	30	1	,92		75	40	4	,		94	50	6	,76 ,08
57	30	6	,24		76	4I	0	,32		95	51	2	
58	31	2	,56 ,88		72	41	·4	,64		96	51	•6	,4 ,72
59	31	•6			78	42	0	,96		97	52	3	,04
60 61	32	3	,2	- 7	79 80	42	5	,28 ,7		9 8 99	52	7	,36 ,68
62	32 33	7 3	,52 ,64	1	8t	4 3 43	. 5	,92-		77 1	53	. 3	. 100
63	22 34). 0	,16	1	82	49 44	2	,24					

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Table I. Com Measure, one Buschel the Integer.

Nº.	G.	P.	Pt.,	INº	.G.	Ρ.	1Pt.	INº.	G.	P.	Pt.
-	-			1		115		17	122		ō
I	-	-	,64	16	I	2	1,24	31	2	3	,84
2		I	,28	17	1	2	,88	32	2	4	,48
3	-	1	,92	18	I	3	,52	33	2	5	,12
4	-	2	,56	19	1	4	,16	34	2	5	,76
5	-	3	,2	20	I	4	,8 1	35	2	6	14
6	-	5000	,84	21	I	5	,44	36	2	7	,04
7	-	4	,48	22	I	6	,08	37	2	17	,68
8	1	5	,12	23	I	6	,72	38	3	0	,32
9	-		,76	24	I	7	,36	39	3	0	,96
IO	1	56	,4	25	2	ò		40	3	I	,6
11	2	7	,04	26	2	0	,64	41	3	2	,24
12	-	7	,68	27	2	I	,28	42	3	2	,88
13	I	Ó	,32	28	2	I	92	43	3	3	,52
14	1	0	,96	29	2	2	,56	44	3	4	,16
15	I	I	.6	30	2	2	2	45	3	4	,8

N° 4: 3 3 3 3 4 4 4 4 4 4 4 4 4 4 4 4 4 4	P. Pr. -5,74 6,98 6,72 7,36 6,72 7,36 0,98 1,9	64 65 66 67 68 69 70 71 72 73 74 75		0 1 2 2 3 4 4 5 6 6 7 0	N 8 2 8 3 8 4 8 5 8 6 87 88 89 90 91 92 93 93	6 6 6 6 6 7 7 0 0 1 2 2 2 3 3 4 5 5 6 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	,04 ,68 ,32 ,96 ,6 ,24 ,88 ,52
58 4 59 4 60 4 61 4 62 4 63 5 Table	5,12 5,76 6,4 7,68 0,52 2. I.	77 78 79 80 81 81	6 6 6 6 6 6 6 7		Autorter	7 4 7 4 7 5 7 6 7 6 7 7 8 8 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9	,8 ,44 ,08 ,72 ,36
I I I I I I I I <td>,05 ,1 ,15 ,2 ,25 ,3 ,35 ,4 ,45 ,51 ,02 ,53</td> <td>I 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0</td> <td>01 1 1 1 1 1 1 0 m 0 v</td> <td>,12 ,24 ,36 ,48</td> <td>I4 I I7 I I7 I I70 I I70 I I I70 I I I70 I I I70 I I I70 I I I70 I I I 20 I I I 22 I I 22 I I 22 I I 22 I I 22 I I 22 I I 22 I I 22 I I 20 I I 2 2 1 I 2 2 2 1 I 2 2 1 I 2 2 1 I 2 2 1 I 2 2 1 I 2 2 1 I 2 2 2 1 I 2 2 1 I 2 2 1 1 2 2 1 2 1 2 2 1 2 2 1 2 2 1 2 2 1 2 2 1 2 2 2 1 2</td> <td>0 I 4 I 7 4 I 6 30 5 2 0 5 7 0 0 5</td> <td>,68 ,92 ,94 ,16 ,28 ,4 ,52 ,64 ,76 ,88 ,-</td>	,05 ,1 ,15 ,2 ,25 ,3 ,35 ,4 ,45 ,51 ,02 ,53	I 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	01 1 1 1 1 1 1 0 m 0 v	,12 ,24 ,36 ,48	I4 I I7 I I7 I I70 I I70 I I I70 I I I70 I I I70 I I I70 I I I70 I I I 20 I I I 22 I I 22 I I 22 I I 22 I I 22 I I 22 I I 22 I I 22 I I 20 I I 2 2 1 I 2 2 2 1 I 2 2 1 I 2 2 1 I 2 2 1 I 2 2 1 I 2 2 1 I 2 2 2 1 I 2 2 1 I 2 2 1 1 2 2 1 2 1 2 2 1 2 2 1 2 2 1 2 2 1 2 2 1 2 2 2 1 2	0 I 4 I 7 4 I 6 30 5 2 0 5 7 0 0 5	,68 ,92 ,94 ,16 ,28 ,4 ,52 ,64 ,76 ,88 ,-

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38 A Set of New Decimal Tables, &c.

3-	•			,									
N 10.8 28 8	P. 2 3 4 4	P1.		N9. 27, 28, 29, 30, 31, 22,	B. 2 2 2 2 2 2 2	G. 1 1 2 3 3 4	27	Pt. -24 -36 -48 -,72 -40 -72 -40 -72	NR. 64 65 66 67 68 69	B. 55555	G. 0 1 2 2 3 4	741741	Pt. ,68 ,8 ,92 ,04 ,16 ,28
•			• ··	32 334 356 378 39 40	1 2 2 2 2 A 2 3 mmm	33455677001	4163053052741	,6 2 4 90 ,72 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	70 71 72 73 74 75 76	555550666666666	45667001	410 30520527410 30530527417	14 1,52 1,64 1,76 1,88
			•	41 42 43 44	`~~~~~ ~ ~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	2234456670	174163052	,92 ,04 ,16 ,28 ,52 ,64 ,76 ,88	77 78 79 80 81 83 83 84 83 84 85	6 6 6 6 6 6 6 6 6 6 6 6 6	12334556	74103053	,36 ,48 ,0 ,72 ,84 ,96 ,08 ,2
	2 - 4 - 2			44 48 20 1 2 3 4 5 6	344444444	0 1 1 2	05274	,	87 88 89 90 91 91 92	6 6 7 7 7 7 7 7 7 7 7 7	7 7 0 1 2 2	0 5 2 7 4 J 7 4	12 46 8 0 2 4 6 8 2 4 6 8 9 0 4 1 8 4 5 6 7 8 9 0 0 2 3 4 5 6 8 9 0 4 1 8 4 5 6 7 8 8 9 0 4 6 8 7 8 7 8 7 8 8 7 8 8 7 8 8 7 8 8 7 8 8 7 8 8 7 8 8 7 8 8 7 8 8 7 8 8 7 8 8 7 8 8 7 8 8 7 8 8 7 8 8 7 8 8 7 8 8 7 8 8 7 8 7 8 7 8 8 7 8 8 7 8 7 8 7 8 7 8 8 7
				578 59 61 62 63	444445	774556770	16 70 5 70 5 7	84 96 2 32 32 34 34 36	94 95 96, 97 98 99	777777	3445667	4163052	,28 ,4 ,52 ,64 ,76 ,88
Ļ								<u> </u>	<u> </u>				Nº

N°.

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Table I. | Table II. { Wine Measure, one Time the Integer.

Nº]	G.	Pts.		Na	IP	Ĥ	T.	G.	Pt.		NQ.	P.	H	T	IG.	Fr
				-	1	1		1.	[]			<u> </u>	[1	
I		,025		I			-	2	,52		6	<u>-</u> +	1	0	27	672
2		,05		2		_		5	.04		27	ի -	I	0		,24
3		,075		2	I		_	7	,54		8		I	. 0		,76
1		,1		Á	-	-		10	,68		9	+ -	1	0	25	,28
13		,126		5	-			12			jo j	┝.;	ī	. 0	37	,8
45	. . '	,15İ	łł	3450					,12		T		1		40	,32
		,176		7				17			2		1	ъ П	0	.8 ₄I
78	_	,201		7	-				,16		3	L -	ī	Ī	2	26
9		,226		0				22	-68		2	L -	1		2	,36 ,88
10		,252	İ.	9 10		7		25	2		4		r	I	Ś	,36 ,88 ,4
20				10			-		,2 ,72	14	5		I	I	10	,92
		,504		12	-	-	-	20	,24	14			- 1	ī	13	74
30 20 20 20 20 20 20 20 20 20 20 20 20 20		,756			-		Ň	54		11	7 8		• I	1	12	24
	I	,008.	·	13		-	•	24	,76	14	0		I	I	15 18	20
20	I	,26		14	-	-		35	,28 ,8	14	9.		0	0	10	49
	I	,512		15 16	-		-	37	,0	12	0 '	I			9	
73 83	I	,764		10	-			12	,32	5	I :		.0	0	2	52
05	2	,015		17 18		-	I		84	55	2	I	0.	0	2	,04 ,56
90	2	,268	1		-	-1	Ì	3	,76	12	3	T I	0	0	_7	22
	(-)		1	19	-	-	I	٦	,88 -1	15	4	Ţ	9	0	10	,00
1 1			1	20	-	-1	1	9	+	15	<u>5</u> .]	Ì	0	0	12	
1 1			- 1	21	-	-		10,	92	555		I	0	0	15	12
1 1				22			1	[3],	44	12,	7 I	ч	٥		17	64
1 1				23	-1	-	1	۲Ş),	96	5	5	I	0	• 0	20	16
1 1		2		24	-	-	1	ι8 ,	96 48	59	2	1	0		22	
1 1			1	25		P	0	0,		6		I	0		25	2
1 1		2		26	-	ŕ	0	2,	52	6		1	0		27	72
		8		27	_	1	0000	55	04	6	2	I	0	0		24
				28	_	Ĥ	0	75	56	6	3	I	o	0	32	76
				29		1	c	10,	80	{6	1	Ι	0	0	356	28
				30	_	1	c	12,	6	16	5	I	0	0	37	8
1	1. I			31	_	1	CH	15,	12	16	5	1	0	0	40	32
				32	-	-1	ch	ネ	64	6	71	I	0	I	d,	32 84
				33	_	1	C	20,	16	68	3	1	0	1		
				34	_	r	c	22,	68	69		1	000000	I	3,	36 88
		1	1	33 34 35		r	d	s,	21	170		1	0	I	8 ĺ,	41

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N%.

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Table I.

-1

A Set of New Decimal Tables, &c.

Nº.	P.1	H.	T.	G.	Pt.	Nº	P	H.	T.	G.	Pt.	Nº.	<i>P</i> .	H.	T.	G.	Pt.
71	1	0	I	10	92	81	1	I	p	15	,12	91	1	1	c	40	,32
72	I	0	I	13	,44	82	T	I	0	17	,64	92	1	I	1	C	,84
73	I	0	I	15	,96	83	1 1	1	0	20	,16	93	1	I	1	3	,36
74	1	0	I	18	,48	84	1	I	C	22	,68	94	I	1	1	5	,88
75	I	1	0	0	-	85	1	I	C	25	,2	195	1	1	I	8	,4
76	1	I	0	2	,52	86	1	1	- 0	27	,72	96	1	1	1	1C	,92
77	1	I	0	5	,04	87	1	I	C	30	,24	97	1	1	1	13	,44
78	I	I	0	7	,56	88	1	1	C	32	,76	98	1	I	1	15	,90
79	I	I	0	10	,c8	89	1	1	C	35	,28	99	1	I	1 1	18	,48
80	1	I	0	12	,6	190	1	I	C	37	,8		1		1.1	H	17

Table II. { One Foot, or one Shilling the Integer.

·1			1		In.		;			In.	1	
<u>N°.</u> 1	Q .	Pts.		Nº.'	P.	Q.	Pt.		N°.	P .	Q.	Pt.
		,004	•	ī	-	_	,48		22	2	2	,56
2		,009		2		_	,96		23	2	3	,04
	'	,014		3		I	,44		24	2	3 3 0	,52
I Á		,019:		4	-	I	,92	ŀ	25 26	3	0	
3 4 5 6		,024	ļ .	3456 78	-	2	,4 ,88		26	3 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	0	,48 ,96
	• •:	,024 ,028		. 6	-	2	,88	ļ	27 28	3	0	,96
7		,033 ,038		7	-	3 3 0	,36 ,84		28	3	I	, 44
8		,038		8		3	,84	ł	29	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	I	,92
·9 10		,043 ,948		9	I	0	,32 ,8		30	3	2	,4 ,88
10	!	,348		10	1	0 1	,0		31	3	2	,00
20		,096		11	1 1	1	,28	1	32 33	3	Ś	20
30	• •	,144	1	12	I	2	,76		22	2	2330	204
40		,192	· ·	13 14	1 i	2	,24 ,72	Í.	25	4 4	0	,36 ,84 ,32 ,8
20 30 40 50 60		,24 ,288	1	14	I		1.2		26	4	I	,28
70	122	226	l.	15	i	2	,2 ,68		37	4	Ī	,76
70 80		,336 ,384		17	2	6	,16	1	28	4	2	,24
90		,432	1	17 18	2	3300	,64		34 35 36 37 38 39	4		,72
		175-		19	2	1	,12		40	4		,2
	Ι.		1	20	2	1	,6	1	41	4	330	,68
}			, I	21	2	2	,08	1	42	15	Ó	,16

				-					. —				· · · · ·
1	In		-		210	In.				1.70	In.		
Nº.	Ρ.	Q.	Pt.		Nº.	<i>P</i> .	<i>Q</i> .	Pt.		Nº.	₽.	Q.	Pt.
43	5	0	64		62	7	I	,76		81	9	2	,88
	5	ĩ	,12	1	63	14				82		r -	,00
44		Ī	,6	Ì	22	7		,24		82	9	3	,36 ,84
45 46	5	1	,08		64	7	2	,72		83	9		,04
40	2	2		ł÷	65	7	3	,2	1:	84 85	10	0	,32 ,8
47	5	2	,56		66	17	3	,68		85	10	0	,8
48	5	3	,04	Ι.	67	8		,16		86	10	I	,28
47 48 49	5	3	,52		68	8	0	,64		87	10	Ĩ	,76
50	555566	0			69	,8	I	,12	ł	87 88	10	2	,24
50 51	6	0	,48	1	70	8	I	,6	ł	89	10	2	,72
52	6	0	,96	1	71	8	2	,08		90	10	3	,2
53	6	I	,44	ł	72	8	2	,56	{	91	10	3	,68
54	6	I.	,92		73	788888888888888	3	,04		92	II	30	,16
55	6	2			74	8	3	,52		93	11	0	,64
56	6	2	,4 ,88		75	10	l ó			94	II	I	,12
57	6		.26		76	6	0	,48		05	11	I	,6
58	6	3	,36 ,84		77	9 9 9	0	,96]	95 96	11	2	,08
53 54 55 56 57 58 59 60	7	6	22		78	9	1	,44		97	II	2	,56
60	7	l õ	,32 ,8				l i	,92		98	II		,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,
61	17		,28		79 83	9	- 1					3	,04
	• /	1	,20	1	.00	19	2	,4		99	II	3	,52

Table I.

Table II. { Liquid common Meaf. a Hogfb. of 51 Gall. Ist.

N° I 2 3 4 5 6 7 8 9 10 2 3 2	P.	Pt. ,03 ,07 ,11 ,15 ,19 ,22 ,26 ,3 ,34 ,38 ,76 ,15	N°. 1 2 3 4 5 6 7 8 9 10 11 12	G 1 1 2 2 3 3 4 4 5 5 6	P. 37 37 37 26 26 26	Pt. ,848 ,68 2 ,36 ,2,048 ,756 ,428 ,754 ,428 ,020	N°. 14 15 16 17 18 19 20 21 22 23 24 25 26	6 7 7 8 8 9 9 10 10 11 11 12	P. 515150404040	Pt. ,76, 448, 12, 98, 648, 22, 10, 10, 10, 10, 10, 10, 10, 10, 10, 10
30 40	1	,15 ,53	12 13	5	6 1	,98 ,92	25 26	12 12	3	, 8 4

Nº.

IOI

101		I 30			~W		CI THE			E J, C		
N°.	P .	Pt.		Nº.	G.	P .	Pt.			rG.	<i>P</i> .	Pt.
50	1	,92		27	12	7	,68		64	30	5	120 42 120 44 12 1 45 28 1 2 4 2 2 2 4 2 2 2 4 2 2 2 4 2 2 2 4 2 2 2 4 2
50 60 70 80 90	2	,3		27 28	13	3	,52		65	30 31 32 32 32 33 33	í	.6
70	2	,3 ,68		29	13	7	.26		65 66 67 68 69	31	5	.44
80	3	,07		30	14	7 3 7 2 6 2 6	,2 ,2 ,04 ,88		67	32	Í	,28
90	3	,07 ,45		21	14	7	,04		68	32		,12
				31 32	15	2	,88		69	33	5 0	,96
				33	15	6	,72		70	33	4	,8
				33 34 35 36	15 15 16	2	,56		70 71 72	34	0	,64
				35	16	6	1,4		72	34	0 4 0	,48
				36	17	2	,24		73	35	0	,32
				37 38	17	6	,08		74	35	4	,16
				38	17 18 18	I	,92 ,76		75	36	0	,-
				39 40	18	5	,76		76	36	3	,84
				40	19	Í	,6		77	30	7	,68
				-4I	19	5	, 1 4 ,28		70	37	3	۶ <u>۶</u> 2
				42	20	I	,28		79	37	7	,30
1				43	20	5	,12		73 74 75 76 77 78 79 80 81 81 82	34 35 36 36 37 37 38 38 38	403737372	,2
1				44	21	0	,96		82	30	7	,01
				45 46	21 22	4	,8 ,64		83	39 3 9 40	6	,00
				40	22	4	104			3 7		3/4
				47 48	23	0	,48 ,32 ,16		84 85 86	40	2 6	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,
1				40	23	4	.16		86	41	2	21
1.1				50	24	5			87	41	2 6	.08
				49 50 51 52	24		1.84	[87 88 89 90 91	42	I	.92
				52	24	37	.68		89	42	5	.76
				52	25	3	.52		95	43	í	.6
				54	25	1 ź	,36		91	43	5	.44
				55	25 26	3	,2		92	44	í	,28
			1	53 54 55 56	26	7 3 7 2	,04		93	44	1 5 0 4	,12
				57	27	2	,88		93 94	45	ó	,96
1				57 58	27	6	,72		95	45	4	,8
				59	27 28	2	,		95 96	45 46	0	,64
1	I ·			59 60	28	6	54		97 98	46 47	4 0	,12 ,96 ,8 ,64 ,48 ,32 ,16
1				61	29	2 6	,24 ,08		<i>9</i> 8	47	Ó	,32
				62	29		,08		99	47	4	,16
1.	1			63	30	I	,92	:				
E		1.1										
1)	-			1				1	

Table I.Table II.Corn Meafure, a Tun
or Load the Integer.

Nº.	~	Pt.	-	NIO	~	D.	~	-		110		-		
	G.	F		N°.	2:	<i>B</i> .	G.	Pt.		Nº.	Q.	<i>B</i> .	G.	Pt.
II		.02		I				,2		25				
12		,03 ,06		2			36			35 36 37 38 39 40 41 42 43 44	I	6	0	,
	_	,09				• -		, ,4		30	I	6	3	,2
17	-	7 09		3	•	I	1	,4 ,6 ,8		37	I	6		, 4
17		,12 ,16		4	••	I	4 0	,ð		38	1	• 7	1	,6
12		,10		3 4 56		2	0	,		39	I	7	4	,8
0		,19		6	'	2	3	,2		40	2	Ó	o	,—
34567 8	-	,22		7 8		2	36	,4		41	2	0	4 0 36	,2
ō		,25 ,28		8		3 3 4	I	,4 ,6 ,8		42		0	6	1
9 10		,28		9 10		2	Ā	.8		12	2	I	1	,4 ,6
10		,32		lío.		4	4 0	,		42	2			~
20		64	ł	11	1	4		,2		44	2	I 2.	4 0	,8
30	<u> </u>	,64 ,96 ,28	1	12	1	17	36	,*		42		2.	0	
40		28	1	1.2		12	0	14		40	2	2	36	,2
so		,6		13 14 1 ⁵ 16	1	4 5 5 6 6 6	Т	,4 ,6 ,8		45 46 47 48	2	2	¢	;4 ,6
60	li	100		14]	2	4	, o :	Ľ	48 I	2	33	· 1	,6
70		,91		15		0	σ	,		49	2	3	4	,8
80	2	,24				0	3	,		50	2	4	Ó	,]
30 40 50 60 70 80 90	2	,56 ,88		17 18			T 40 36	40,8, , , , , , , 8		51	2	4	4 0 36 1	,2
~	2	,88		18		7	1	,6		52	2	4	6	,4
1			Į	19	- •	7	4	,8		52	2	5	I	,6
1		•		20	I	Ó	l d			54	2	5	4	,8
1		•	l: ·	21	II	0	2	.2	1		5	1 6	- 7	
		·	Ϊ.		1	0	2	. 1		26	2 2	6 16	0 00 H	;;
				22	1	1		17.		2	2	6	. 2	,2
1			[24	1	Ī		, 0		127			D	,4 ,6
1			ļ.	24	1.1	2	4	,0	ļ,	50	2	7		,0
	į			22 23 24 25 26	1	2	0	,	Ι.	159	2	7	4 0	,8
. .	1		Ι.				3	,2	l	501 515 555 556 578 500 612 634 656 66	3	.0	0	,
1				27 28	I	12	6	<i>></i> 4		61	3	0	36	,2
1 (•	ľ			23344	l r	,4 ,6 ,8		62	3	1;0		,4
		.	;	29	I I I	13	4	,8		63	13	T	II	,4 ,6 ,8
1 1	1			30		4		,—	·	64	2	1		8
	- 1		· ·	31	1	4	1	,2		65	2	2	- 1 0	,
1 1	- 1			32	1	4	12		ŀ	66	2	2		2
1 [·	22	11.	1 3	0	17		177	2	2	12	,2.
{				30 31 32 33 34	1	455	1 40 36 1 40 36 1 40 36 1 4	,4 ,6 ,8		67 68	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~		.3 :6 .1	,4 ,0.'
1			•- •	77		1 2-	4	- ⁹		60	13.	3	I .I	,0,

Nº.	Q.	<i>B</i> .	G.	Pt.		Nº.	Q.	B .	G.	Pt.	Γ	Nº.	Q	B.	G .	Pt.
69	 3	2		- ,8		80	4	0	0	,		91	4	4	3	- ,2
70	3	4	c	,—		81	4	G	3	,2		92	4	1 · ·	6	•4
71	3	4		,2		82	4	0	6	,4		93	4	5	1	,6
72	3	4	6	,4		83. 84	.4	.I	I	,5 ,8		94 95	4	$\frac{5}{6}$.4	, °
73	3	15		,6 .8		24 85	4	2	+ c	30		96	4	6	3	,7
75	13			,		36	4	2	3	,2	,	97	4	6	5 6	,1
76	3	6	3	,2	18	87	4	2	6	54		98	4	7	I	,6
77	3	6	6	,4		38	4	3	1	,6		99	4	7	4	,8
78	3	7	1	,6		39	4	3		,8		·	· I			
79	3	7	4	,8		90	4	4	0.	,-		1				

Table I. | Table II. { Long Measure, one Pole or Rod the Integer.

Nº.	In.	Pts. 1	1	N٩	Yd.	Ft	In.	Pt.		Nº.	Yd	Ft.	In,	Pt.
	•						- ·				-;			
I	-	,019		'I	-		I.	,98	ŀ	23	Ì I	0	9	,54
2	-	,039		2.	-	-	• 3	,96		24	\mathbf{I}_{i}	0	II	,52
3	-	,059		3.	-	-	5	,94	ŀŀ	25	1 I	I	I	,5
3 4 5 6	-	,079		3 · 4 ·	-	—	7	,92		26	I	I	3	,48
5	—	,099		5.	-	-	9	.9		27	٠I	1	5	,46
6	-	1,118		6	-	_	11	,88		27 28	· L	ľ	7	,44
7	-	.128		7	-	II	I	,86	[]	29	I	1	9	, 42
7 8	-	,158		7 8	_	1	3	,84	11	30	۱	I	hi	,4
.9	-	,178		9	_	1 1	5	,82	11	31	I	2	I	,38
10.	_	,198		10	-	ļ	1 7	,8		32	Ĩ	2	3	,36
20	<u></u>	,396		11	-	1 i	9	,78		33	ī	2	5	,34
30	-	,594		12	-	1 ;	hí	,76	11	55 34	l i		17	,32
40	_	,792				2				24	l i		9	:3
50				13			4	574		35			11	;5 ,28
60	ΙΞ,	,99		14		2		,72	11	36		2		,20
	1	,188		15	-	2		1.7	11	37	2	0	I	,26
70 80	1 1	,386		16	-	2		,68	11	38	2	0	3	,24
	Ļ	,584		17	-	2		,66	11	39	2	0	5	,22
90	1	,782		18	1-	2		,64		40	2	0	7	,2
		1		19	I	C	1	,62		4I	2	0	9	,18
10.1		2 N		20	1.1			,6		42	2	0	11	,16
1.				21	1	0	5	,58		43	2	1	1	,14
P	1	1.	•	22	1	1 0		1,56		44	2		13	,12

Nº	Yd	Ft	In	Pt.	INP.	Yd	Ft	In	Pt.	INº.	Yd	Ft	In	Pt.
17		177			17		1.	16		0.			1	
45	2	I	5	,I	64	3	I	6	572	83	4	I	8	,34
46	2	I	7	,08	65	3	I	8	17	84	4	I	10	,32
47	2	I	9	,06	66	3	I	10	,68	85	4	2	0	
48	2	I	11	,04	67	3	2	0	,66	86	4	2	2	,26
49	2	2	I	,02	68	3	2	2	,64	87	4	2		,26
50	2	2	3		69	3	2	4	,62	88	4	2	6	,24
51	2	2	4	,98	70	3	2	6	,6	89	4	2	8	,22
52	2	2	6	,96	71	3	2	8	,58	90		2	10	r 1
53	2	2	8	,94	72	3	2	10	,56	91	4	ő		,2 ,18
	2	2	10				0	0	20	1.	5	1. 1. 1. 1. 1.		
54		1.50		,92	73	4	1.000		,54	92	5	0		,16
55	3	0	0	,9	74	4	0	2	,52	93	5	0	4	,14
56	3	0	2	,88	75	4	0	4	,5	94	5	0	6	,12
57	3	0	, 4	,86	76	4	0	6	,48	95	5	0	8	,I
58	3	0	6	,84	77	4	0	8	,46	96	5	0	IO	,08
59	3	0	8	,82	78	4	0	10	,44	97	5	I		,06
60	3	0	10	,8	79	4	I	0	,42	98	5	I		,04
61	3	I	0	,78	80		Ĩ	2		99	5	Î		
62	2	i			81	4	I	1	,4	79	2	-	4	,02
	3	4	2	,76		4	-	4	,38	1	100			
63	3	11	4	,74	182	4	1	6	,36					- 1

Table I.

Table II. { Long Measure, one Yard the Integer.

Nº.	Q.	P t.	Nº.	Ft	In	Q.	Pt.	1	Nº.	Ft	In	2.	Pt.
I	1	,014	IT	-	1	1	.44	11	14	-	5	0	.16
2	-	,028	2	-	-	2	,88	84	15	-	5	I	,6
3	-	,042	3		I	0	,32		16	-	5	3	,04
4	-	,057	4	-	1	I	,76	14	17	-	6	0	,48
5	-	,072	15	-	1	3	,2		18	-	6	I	,92
6	-	,086	6	-	2	0	,64		19	-	6	3	,36
7	1-	,I	7	-	2	2	,081	1	20	-	7	0	,8
8	-	,115	8	-	2	3	,52	1	21	-	7	2	,24
9	-	,129	9	-	3	0	,96		22	-	7	3	,68
10	-	,144	10	-	3	2	,4	1	23	-	8	1	,I 2
20	-	,288	II	-	3	3	,84	1	24	-	8	2	,56
30	-	,432	12	-	4	1	,28	1	25	-	9	0	,-
40	-	,576	13	-	4	2	72	1	26	-	9	I	,44

P

N٩

N	Q.	Pt.	Nº	Ft	ln.	R.	Pt.	Nº.	Ft	In	Q.	Pt.
2 300 700 00		P1. ,72 ,864 ,908 ,152 ,296	N 278 9 3 1 2 3 3 4 5 6 78 9 0 1 2 3 4 4 5 6 78 9 0 1 2 3 4 5 6 78 9 0 1 2 3 5 5 5 5 5 5 5 5 5 5 6 6 6 6 5 5 5 5 5		9 10 10 10 11 11 11 0 0 0	201 30 2 30 2 31 201 30 1 30 2 31 201 201 30 2 30 2	Pt. 88 376 48 32 6 48	N 645667897777777777777778988888888888990123345667899999999999999999999999999999999999	F I I I 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	111100011122333344455556667788889999000111	Q 0 1 30 1 30 2 31 2 0 1 2 0 1 30 2 30 2	2 16 0 48 26 15 1 488 37 2 6 5 9 488 2 7 1 6 0 48 2 6 2 8 2 8 2 8 2 8 2 8 2 8 2 8 2 8 2

Table I. Table II. { Long Measure, one Mile the Integer.

Nº.	In.1	Pts.	IN	°.[R.	Yd	Ft	In	Pt.	Γ.	Nº,	R.	Yd	Ft	In	Pri
1	;		-		-	F_				-					'
I		,063		I	-		6	,33 ,66	11	36 37 38 39	T	0	2	5	, 88 ,
2		,126 ,189		2 -	-	1	9	,66	11	37	ĩ	1	0	Ó	,21
3		,189		3 -		ł	6	,99	H	38 -	I	1	0	6	,54
4		,252		4 ├─		2	I	,32	}	39	I	1	Ι	С	,54 ,87
15		,252 ,315 ,378		3		2	7	,65	11	40.	I.	れ	I	7	2
0		,378		6	I	0	I	,98		4 I	I	1	2	1	,53
7		,44I			I I I	٥	8	,31		42	I	1	. 2	7	,86
34507890		,441 ,504 ,633 ,266 ,899 ,532 ,165 ,789		8	I	1 2 2 2 3 4 4 2 2 3 5 4 4 4 5 5 5 4 4 5 5 5 4 4 5 5 5 5 4 4 5	2	36 9 9 9 9 9 9 9 9 9 9 9 9 9		40 41 42 43 44 45 46 47 48	I	2	200112200112201122011220101001	2	8,21,47,36,9258,147,36,9258,147,36,9258,147,36,9258
9		,567	I	9 -	I I	ľ	8	,97		44	1	2	0	8	,52 ,85 ,18
10		,633	I	> −	I	2	3	, 3		45	I	2	I	2	,85
20	I	,266	1 5	ı (—	I	2	9	,63		46,	1	2	ł	9	,18
30	I	,899	1	2 -	2	Q	3	,96	1	47 '	I I I	2	2	3	5I
40	2	,532	L	3 -	2	0	10	,29	1	48	I	4	2	2	,84
50	3	,165	I.	4 -	2	I	4	,62	1	49		3	d	4	,17
30 40 50 60	3	,789	1	5 –	2	I	10	,95		50	I	3	0	10	5
70 80	33455	,431 ,064		5 –	2	2	5	,28	1	5012 512 512 512 512 512 512 512 512 512 5	I	3	1	4	,83
8 0	5	,064	1	7 -	2	2	11	,61	ľ	52	I	3	1	11	,16
00	5	,697	1	3	3	0	5	94	1	53	1	3	2	ź5	,49
1.1		1.00	19	> -	3	Ŀ	C	,27		54	I	3	2	IH	,82
					3	Ľ	6	,6		55	1	4	9	6	,15
			2		3	2	0	93	1	56	I	4	I	9	,48
1		0.111	2:		3	2	7	,26	ľ	57	I	4	I	6	,81
		100	2	3 -	4	0	1	,5 <i>9</i>	ľ	58	I	4	2	· I	,14
			24	+ -	4	C	7	59 92	ľ	59	I	4	2	7	47
			2 22 20 20		4	I	7 2 8	,25 ,58 ,91	1	60	I	5	C	1	,8
		1 A. 1	20	5 - 7 -	4	1	8	,58		61	I	5	С	8	,13
			27	7 -	4	2	2	91		62	I	5	1	2	,46
			28		4	2	9	,24	1	63	2	ଁ	c	2	79
			29	> ト	5	С	3	57	-10	64	2	O,	С	9	12
	1.1	0.0	30) -	5	C	9	9	-	65	2	o	1	3	45
		1.0	3	ι O	5	1	4	23	10	56	2	o	1	9	,78
			3	2 1	<u>2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 </u>	c c	2 9 3 9 7 9 7 9 7 9 7 9 7 9 7 9 7 9 7 9 7	56 89	10	63 64 65 66 67 68 69	2	4 1 1 N N N N N N N N N N N N N N N N N	2	-4	, I I
			33	3 1	0	С	10,	89	1	58	2		2	۱C	44
			30		0	1	5	22	10	\$9	2	I	2 2 2 0 0	4	77
	1.4		139	;] [0	1	11,	55	; ;	70	2	I	С	Ш ,	I

· P 2

N٩

Nº.	R.p	rd	Ft	In	Pt.	1Nº	.IR.	Yd	Ft,	In	Pt.	N?	R.	Yd	Ft	1	Pt.
71	2	I	1	5	,43	81	2	3	0	8	73	91	2	5	0	C	,03
72	2	I	1	11	,70	82	2	3	1	3	06	92	2	5	0	6	,36
73	2	I	2	E	,09	83	2	3	1	2	39	23	2	5	I	C	,69
74	2	2	0	C	,42	84	2	3	2	3	72	24	3	0	0	1	,02
75	2	2	0	6	,75	85	2	3	2	10	,05	95	3	0	0	7	35
76	2	2	1	1	,08	86	2	4	0	4	,38	96	3	0	I	1	,68
77	2	2	I	7	,41	87	2	4	0	10	7I	97	3	0	I	8	,01
78	2	2	2	1	74	88	2	4	1	5	,04	28	3	0	2	2	34
79	2	2	2	8	,07	89	2	4	1	11	,37	99	3	0	2	8	,67
85	2	3	0	2	.4 1	20	2	4	2	5	7		1		1		

Table III. Long Measure, one Mile the Integer.

Nº.	Fg	R.	Yd	Ft	In.	Pt.	INº.	Fg	R.	Yd	Ft	In.	Pt
-												-	
I	0	3	I	0	3	,6	23	1	33	3	0	10	,8
2		6	2	0	7	,2	24	I	36	4	I	2	,4
3		9	3	0	10	,8	25	2	0	0	0	0	
34		12	4	I	2	,4	26	2	3	I	0	3	,6
5		16	0	0	0	,-	27	2	6	2	0	7	,2
56		19	I	0	3	,6	28	2	9	3	0	IO	,8
		22	2	0	7	,2	29	2	12	4	I	2	,4
78		25	3	0	10	,8	30	2	16	Ó	0	0	1
9		28	4	1	2	,4	31	2	19	I	0	3	,6
10		32	i o	0	0		32	2	22	2	0	7	,2
11		35	I	0	3	,6	33	2	25	3	0	10	,8
12		38	2	0	7	,2	34	2	28	4	I	2	,4
13	I	I	3	D	IC	,8	35	2	32	40	0	0	,-
14	I	4	4	1	2	,4	36	2	35	I	10	3	,6
15	I	48	ó	0	0	,-	37	2	38	2	10	17	,2
16	I	11	I	0	3	,6	38	3	I	3	0	10	,8
17	1	14	2	0	7	,2	39	3	4	4	I	2	1,4
18	1	17	3	0	10	,8	40	50.00	48	Ó	0	0	,-
19	I	20	4	I	2	,4	41	3	II	I	0	3	,6
20	I	24	0	0	0	1.1	42	3	14	2	0	7	,2
21	I	27	I	0	3	,6	43	5	17	3	0	10	,8
22	I	130	2	0	1 7	,2	44	3	20	4	1	2	1,4

Nº.

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Nº.	Fg	R.	Yd	Ft	In.	Pt.		Nº.	Fg	R.	Yd	Ft	In.	Pt.
								1.		_				
45	3	24	0	0	0	,-		73	5	33	5	0	10	,8
46	3	27	1	0	3	,6	1	74	56	36	4	I	2	.4
17		30	2	0	7	,2		75		0	0	0	0	
48	3	33	3	D	10	,8		76	6	3	I	0	3	,6
49	3	36	4	I	2	,4		77	6	36	2	0	7	,2
49 50	4	0	0	0	0			77 78	6	9		0	3 7 10	,8
51	4	36	I	0	3	,6			6	12	34	1	2	,4
52	4	6	2	0	7	,2		79 80	6	16	o	0	0	
53	4	9	3	0	IO	,8		81	6	19	I	0		,6
54	4	12	4	I	2	,4		82	6	22	2	0	37	,2
55	4	16	o	0	0	-		82	6	25	3	0	10	,8
56	4	19	I	0	3	,6		84	6	28	4	I	2	
57	4	22	2	0	7	,2		85 86	6		0	0	0	•4
57 58	4	25	3	0	10	,8		86	6	52 35 30	1	0		,6
59	4	28	4	I	2	,4		87	6	28	2	0	37	,2
59 60	4	32	40	0	0			88	7	20 I	3	0	10	,8
61	4	35	I	0	3	,6		89	7		2	I	2	
62	4	38	2	0	7	.2		90	7	48	4	0	ő	•4
62	5	I	1.10	0	10	,2 ,8		91	7	II	I	0		,-
64	15		34	I	2	.4	2.3	92	7		2	0	3	,6
63 64 65 66	5	8	0	0	0		1		7	14		0	7	,2 ,8
66	5	II	I	0	3	,6		93		17	3	I	10	
67	5	1.000	2	0	2	,0		94	7		4		2	,4
67 68	5	14		0	7 10	,2 ,8		95 96	7	24	0	0	0	1-
69	2	17	3	I				07	7	27	I	0	3	,6
70	5		40	1.00	2	,4		97 98	7	30	2	0	7	,2
70	5	24	10 C 10	0	0	;6		90	7	33	3	0	10	,8
71	5	27	I	0	3	,0		99	7	36	4	I	2	,4
72	5	30	2	0	7	,2					1.1			1.1

 Table I.
 Square Meafure, one

 Mile Square the Integer.

Nº.	Pq	Pts.	Nº.	Aq	Rq	Pq	Pt.	Nº.	Aq	Rq	Pq	Pt.
1												
		,102	Ι				,24	6			2 I	•44
		,204	2		-	20	,48	7		I.	31	,68
3		,307	3	-		30	,72	8	-	2	I	,92
4	-	,4°9		-			,96	9				
5		,512	5	! —	I	11	,2	10	-	2	22	,4

Vº.	\underline{Pq}	Pts.	Nº.	Aq	RI	Pq	Pt.	Nº.	Aq	Rq	Pq	Pt.
6		,614	11		2	32	,64	51	3	I	2	,2.
7		,716	12		3	2	,88	52	3	I	12	,48
8		,819	13		3	13	,12	53	3	I	22	,7:
9		,921	14		3	23	,36	54	3	I	32	,90
0	I	,02	15		3	33	,6	55	3	2	3	,2
20	2	,04	16	1	0	3	,84	56	3	2	13	.4
30	3	,07	17	I	0	14	,08	57	3	2	23	,6
to	4	,09	18	1	0	24	,32	58	3	2	33	,9
50	5	,12	19	I	0	34	,56	59	3	3	4	,1
50	6	,14	20	1	1	4	,8	60	3	5000	14	,4
70	78	,16	21	I	1	15	,04	61	3	3	24	,6 ,8
80		,19	22	I	1.1	25	,28	62	3	3	34	,8
70	9	,21	23	1	I	35	,52	63	4		5	,1
			24	1	2	5	,76	64	4		15	13
		1 1	25	1	• ~	16	,-	65	4		25	,6
			26	1	. ~	26	,24	66	4		35	,8
		1 1	27	I	2	36	,48	67	4		6	,0
			28	I		6	,72	68	4		16	,3
	1	1 1	29	I	3	16	,96	69	4		26	,5
		1 1	30	I	3	27	,2	70	4		36	,8
	1	1 1	31	I	3	37	,44	71	4		7	,0
		1 1	32	2		7	,68	72	4		17	,2
			33	2		17	,92	73	4		27	,5
	1	1 1	34	2		28	,16	74	4	2	37	,7
	1	1 1	35	2		38	,4	75	4	3	8	,-
	L	1 1	30	2	1.5	8	,64	76	4	3	18	,2
		1 1	37	2	1	19	,88	77	4		28	1.4
		1 1	38	2		29	,12	78	4		38	1,7
			39	2		39	,36	79 80	5	0		,9
		1 1	40	2	2	9	,6	81	5			,2
	1.1	1 1	41	2	2	19	,84	82	5		100	1,4
	1	1 1	42	2		29	,08	02	5		39	,6
		1 1	43	2		39	132	83	15		1 .	,9
			44	2		10	,56	84	5			,1
		1 1	45	2	50	20	,8	85 86	15		10	,4
		1 1	46	2		31	,04	87	5		C 1 1 1 1 1	,6,8
	1		+7	3		I	,28	88	5			
		1 1	48	3	C	11	,52	100	15	2		,1
	1	1 1	49	30	00	32	,70	89 90	5	2		,3 ,6

N٥

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Nº. Ag Rg Pg I	1 Nº.	AqRq Pq	Pt. Nº	Ag Rg Pg Pt.
01 5 211	84 94	6 0 2	56 97	6 022 28
91 5 311, 92 5 322, 93 5 332,	08 95	6 0 2 6 0 12 6 0 23	8 98	6 0 33,28 6 1 3,52 6 1 13,76
93 5 3325	321 96	6 0 23	,04 99	6 113,76

Table III. Square Measure, one Mile Square the Integ.

Nº.	Aq.	Rq	Pq		Nº.	Aq.	Rg	Pq	N9.	Aq.	Rq	Pq
I	6					217	2	16	67	429		8
2	12	1	24 8		34 35	224	0	10	68	429	3	32
	19	3	32		30 36	230	ĭ	-, 24	69	43) 441	2	16
3	25	2	10		37	236		24 8	7 0	448	ō	
4	32	ō	,		38	243	3	32	7I	454	I	, 24
4 5 6	38	I	21		39	249	2	16	72	460	3	24 8
	44	2	24 8		40	256	ō	•-,	73	467	0	32
78	44 51	30	32		41	262		24	74	473	2	16
o	57	2	16		42	268	2	24 8	75	485	0	-,
9 10	57 64	0	,		43	275	ó		76	485 486	I	24
11	70	I	24		44	281 288	1 3 0 2 0	32 16	77	492	3	²⁴ 8
12	70 76 83 89	3	24 8		45	288	0	,	77 78	499	ó	32
13	83	ó	32		46	294	I	24 8	79 80	505	2	32 16
14	89	2	16		47	300	3	8	80	512	0	,
15	96	0	-,		47 48	307	3 0 2	32	81	518	I	24 8
15 16	102	I	24 8		49	313	2	16	82	524	3	8
17	108	3	8		50	320	0	,	83	153I	0,	32
17 18	115	Ō	32		51	326	I	24	84 85	537	2.	16
19	121	2	16		52	332 339 345	1 3 0 2	8	85	537 544	0	۰-,
20-	128	0	,		53	339	0	32	86	550	1	24 8
21	I34	Ι	24 8		54	345	2	16	87 88	556	3	8
22	140	3	8		55	1352	0	-,	88	563	0	32
23	147	0	32 16	I	56	358 364	I	24 8	89	569	2	16
24	147 153 160	2	16	1	55 56 57 58	364	3 0 2 0 1		90	550 556 563 569 576 582 582 588	0	,
25	160	0	,	l	58	371	0	32	91	582	I	24 8
26	166	I	24		59 60	377 384	2	16	92		3	
27 28	172	3	8		60	384	l °	,	93	595	0	32 16
	179	0	32	l	61	390	II	24 8	94	601	2	
29	185	2	16		62	396	3	o	95	60	0	,
30	192	0		l	63	403		32	96 07	614	I	24
31	298	I	24 8	1	64	409	2	16	<i>9</i> 7	620	3	8
32 33	204	3	l o		65 66	416 422	0	7	98 99	627 633	0 2	32 16
33	211	10	132	1	00	1422		24	99	044	2	No

Nº.

E.

Table I.	Table II	∫ Square	Measure, are the Integer	oke
I abic I.		Rod Squ	are the Integer	r.

NS.	Fq	Pt.	1	Nº.	Yq.	Fa	Pt		Nº.	Ya	Fq	Pt
_				_	1.	Fq 2 58	-•			Y q	- 4	
I	-	,02		I	-	2	,72		36	10	.7	,92
2	-	,05		2	-	5	244		27	II	I	,64
3	-	,05 ,08		3	-	8	,16		38	II	4	,36
4	-	,1		4	I	I	,88		39	11	7	,08
2 3 4 5 6 7 8 9 10	-	,1 ,13 ,16 ,18 ,21 ,24		3 4 5 6 7 8	I	4	,16 ,88 ,6 ,32 ,04 ,76		40	12	Ó	,92 ,64 ,36 ,98 ,52 ,96 ,68
6		,16		6	I	4 7 1	,32		4 I	12	3	,52
7	-	,18		7	2	I	,04		42	12	36	,24
8		,21		8	2	3	,76		43	12	8	,96
. 9	-	,24		9	2	36	,48		44	13	2	,68
10	-	,27		10		0	,2		45	13	5	,4
20		,54		9 10 11	3	2	,92		46	13 13 13	58	,12
30		,8i		12	3	0.2 58	,64		47	14	I	,4 ,12 ,84
40	I	,08	077		3	8	,36		48	14	4	,56
50	1	,35	£	14	4	2	,08		49	14	7	,56 ,28
30 40 50 60	1	,62		15		4	,8		50	15	Í	, —
70 80 90	1	,08 ,08 ,35 ,62 ,89 ,16		13 14 15 16 17 18	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	471360358	,48 ,2 ,92 ,64 ,36 ,08 ,52 ,24		Ś1	15 15 15 16		,72
80	2	,16		17	5	Ī	,24		52	15	36	.44
90	2	,43		18	Ś	3	,96 ,68		53	16	0	,16
1				19	Ś	6	,68		54	16	2	,88
	1	1		20	6	0	,4		ŚŚ	16		,6
	1.1	8.1		21	6	3	,12		56	16	58	,32
				22	6	5	,84		57	17	2	,04
1			6	23	6	8	,56	ł	58	17	4	,76
			К —	24	7	2	,12 ,84 ,56 ,28	I	59	17	7	,48
				25	7	5	,		60	18	1	,2
				24 25 26	7778888	2 5 7 1			61	17 17 17 18 18 18	3	,92
				27	8	I	,44		62	18	6	,64
			D.,	28	8	4 6	,16		63	19	0	,36
	1 1			29	8	6	,88	i	64	19		,08
				30	9	0	,72 ,44 ,16 ,88 ,6		65	19 19	3 5 8	,8
				31	9 9 9 9 9	0 36 8	.22		66	19	8	,52
				32	9	6	,04		67	20	2	,24
				33	9	8	,76		68	20		,96
1			0	34	10	2	,48		69	20	4 7 1	,724,188 2468 ,74,188 2468 ,2468 ,2468 ,2468 ,2468 ,2468 ,2468 ,2468 ,2468
			1	27 28 29 30 31 32 33 54 35	10	5	,04 ,76 ,48 ,2		41 2 3 4 4 5 6 7 8 9 0 1 2 3 3 4 5 6 7 8 9 0 6 6 6 6 6 6 6 6 8 9 70	21	li	1,4

Nº.	Yq	Fq	Pt.		N°.	Yq	Fq	Pt.	1	Nº.	Yq	Fq	Pt.
71	21	4	,12		81	24	4	,32		91	27	4	,52
72	21	6	.84		82	24	7	,04		92	27	7	,24
73	22	0	,56		83	25	0	,76		93	28	0	,96
74	22	3	,28		84	25	3	,48		94	28	3	,68
.75	22	6	,—1		85	25	6	,2	ŀ	95	28	6	5 4
.76	22	8	,72	_	86	25	8	,92		96	29	0	,12
77	23	2	,4 4		87	26	2	,64		97	29	2	;84
.78	23	5	,16		88	26	5	,36		<i>9</i> 8	29	5	,56
79	23	7	,88	1	89	26	8	,08		99	29	8	,28
8 0	23	I	,6		90	27	I	,8					

Table I.

] Table II. { Square Measure, one Yard Square the Integer.

1 10	1.	1 01	-	NIO	17.	1 1 .		_				
Nº.	<u>Iq.</u>	Pt.	i	Nº.	Fg	Iq. '	Pt.		Nº.	Fq	1q.	Pt]
Ī		,12		I		12	,96		-			أم
									23	2	10	,08
2		,25		2	- .	25	,92		24	2	23	,04
3		,38		3		38	,88		25	2	36	,
456		,5I		3 4 5 6		51 64	,84		· 26	2	48 .61	,96
5	'	,64		5		.64	,8		27	2	.61	92
]	,77				77	,76		28	2	74	,88
7		,9		7		90	,72		29	2	87	,84
7 8	I	,03		7 8		103	,68		30	2	100	,8 -
9	II	,16		9		116	,64		31	2	113	,76
10	I	,29		10		129	,6		32	2	126	,72
20	2	,5 <i>9</i> ,88		11		142	,56.		33	2	139	,68
30	3	,88	3	12	I	11	.52		34	3	8	,64
40	3 5 6	,17		13	đ	24	,48		34 35 36 37 38	3	21	,6
50	6	,46		14	I	37	,44		36 :	3	34	,56
60	7	,75		15	I	50	,4		37	3	47	.52
70	9	,04		15 16	1	50 63	,4 ,36		38	ź	47 60	,48
80	10	,33		17	I	76	,32		39	2	72	,44
90	II	,62		18	1	89	,28.		40	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	73 86	,4
		-		19	I	102	,24		41		99	,36
		1		20	I	115	,2		42	2	112	,32
		I.		21	I	128	,16		43	2	125	,28
	· •			22	I	141	,12		44	3 3 3 3 3	138	,24

Q

INº1	Fq	Iq.	Pt.	1	Nº.	Fq	Iq.	Pt.		Nº.	Fq	1q.	Fr.
-											- 1	-	
45	4	7	,2		64	5	109	,44		83	7	67	,68
46	4	20	,16		65	5	I 22	,4		84	7	80	,64
47	4	33	,12		66	5	135	,36		85	7	93	,6
- 1 8	4	46	,08		67	56	4	,32		86	7	106	,96
49	4	59	,04		68	6	17	,28		87	7	119	.52
50	4	72	,		69	6	30	,24		88	1 7	132	,48
ξī	4	84	,96		70	6	43	,2		89	78	Ĩ	,44
52	4	97	,92		71	6	56	,16		90	8	14	,4
63	4	110	,88	Į	72	6	69	,12		91	8	27	,36
54	4	123	,84		73	6	8z	,08	ľ	92	8	40	,32
lit i	4	136	,8			6	95	, ō4	łł	93	8	53	,28
55 56	5	<u>م</u> ريد	,76		74	6	108	1 04		94	8	66	,24
	2	5 18			75	6	120	,96	ł	24	8	•	
57 58	5		372	1	76	6				95	8	79	,2 ,4
120	5	31	,68	1	77		133	,92		96		92	,16
59	9	44	,64	١.	78	1	2	,88		97	8	105	,12
50	5	57	1,6		79	7	1 15	,84		98	8	118	, 08
ÓI	5	1 <u>7</u> 0	,56		80	7	28	,8	1	99	8	131	,04
62	5	83	1.52		81	1 7	41	,76	t	I			
63	5	96	1,4 8		82	7		,72		<u> </u>	1		

Table I.

I

Table II. { Square Measure, one Foot Square the Integer.

$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	-	<u> </u>		-		-			-	-		-		TKIN
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	<i>P1</i> .	9.9	19.	Nº.		<i>Pt</i> .	9.9	1q.	Nº.		<i>F</i> t .	9.1	19.	IN"
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	-44						÷-		·			-	4 -	-
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$,96	.2	20	14			7	1	Ţ	31	,23			
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$,6	9	21	15		82,	14	2	'2	6	146	·		2
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$,64	0	23	16		,12	5	4	3	9	,69		-	3
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$,6 8 .	7	24			,16	12	5	4.	2	,92	-		4.
$\begin{array}{cccccccccccccccccccccccccccccccccccc$,72	14	25	18	•	,2	3	7	5	2 B		Ì	-	5
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$,76	5		:19			10	8	6	8	;,38	1		6
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$,8	12	28	20	r = 1	,2B	1	10	7			I		7.
10 - 2,3 10 14 6,4 23 33 1 20 - 4,6 11 15 13,44 24 34 8	,84	3	30	2I	• •	1,32	8	II	8	4	,8⊥	Ì	-	8
20 - 4,6 11 15 13,44 24 34 8	,88,	10	31	. 22		,36	15	12	9	7.	,07,	2		9
- 1	,92		33	23	÷.	,4	6	14	ro		,3	2		10
	,96	8	34	24				15	ĮI.		,6		1-	20
30 - 0,9 12 17 4,48 25 30 0	,	0	36	25		,48	4	17	12		,9	6		30
40 - 92, 13 18 11,52 26 37 7	,84	7	37	26			II	18	13/		2,	9	<u> </u>	142

Iq.	0.0	Det	N10	To .	0.0	$P_{t.}$		NIO	7.1		
19.	9.9	1-1-	1-		99			3	1q.	9.9	Pt.
-	11	1,5	27	38	14	,08		64	92	2	,56
-	13	,8	28	42		,12		65	93	9	,6
I	0	,I	29	41	12	,16		66	95	0	,64
1.1.1.1.1.1.1.1	1.		30		3			67	96	7	,68
I	4	17				,24		68	97	14	,72
			32	46		,28	10	69	99	5	,76,84,88
			33	47		,32		70	100		,8
			34	40	15	,30			102	3	,84
	11		35	50				72	103	10.000	,88
			30	21	13	244		73	105		,92
			37	25	4	52		74			,96
			30	24		.56	12	12			5
			10			.6			109		,04
			40			,64	1	78	110	14	,00
			12	60		,68		70	112	12	,12
		1 t	42	61	TA			80	115		,2
			44	63	5	,76		81	116	10	,24
	1.1		45	64	12	,8	1.10	82	118		,28
			46	66		,84		82		8	,32
			47	67	10	,88		84		15	,30
			48	69	I	,92	1.15	85		6	14
11			49	70	8	,96		86			,44
			50		0	,	- AL	87	125	4	,48
			51	73		,04	1.16	88	126	II	,51
			52	74	14	,08			128	2	.50
			53		5	,12			129		.6
			54	77	12			91	131		,64
			55	79	3	,2			132	7	,68
			56	80		,24			133	14	,71
			57	82	I			94	135	5	.76
			158	83	8	,32		95	126	12	.8
	1.1		59	84	15	,36		96	138		.84
	1.1		60	86		,4		97	139	10	,88
			61	87		.44		98	141	I	,92
			62	89		,48	X	99	142	8	,90
	:		63	190	ni	,52					1
		1 1	1.	1	1	12.00			4	A	
	111	- 11 - 13 1 0 1 2	- 11,5 - 13,8 1 0,1 1 2,4	- II,5 27 - 13,8 28 I 0,I 29 I 2,4 30	1 1 38 1 27 38 40 1 1 15 27 127 27 28 40 1 1 15 28 29 41 1 15 30 14 46 1 15 30 14 46 1 13 0 14 47 33 44 50 51 33 34 50 51 33 56 37 38 39 41 42 44 45 66 67 90 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 <	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$

Q 2

INº.	F.c.	Pc.		Nº.	Fc	1.c.	P1.	1	Nº.	Fc	l.c.	Pt.
ī		,66		1		466	,56		36	9	1244	,16
2	9	,32		2		933	,12		37	9	1710	,72
	12	,98		3	_	1399	,68		37 38	Í	449	,28
1 4	13 18	,65	·	4	I	138	,24		39	10	915	,84
3 4 5 6	23	,31		4 5 6	I	604	,8		40	10	1382	,4
6	27	,98		6	1	1071	,36	Í	41	11	I 20	,96
7	32	,64		7	r	1537	,92		42	11	587	,52
7 8	37	,31		7 8	2	276	,48		43	11	1054	,081
9	4 I	,97		9 10	2	743	,04		44	II	1520	,64
ro	46	,65		IO	2	1209	,6 ,16		45	12	259	,2
20	.93	,3		11	2	1676	,16		46	12	725	,76
30	139	,98		12	3 3 3	414	,72		17	12	1192	,32 ,88
40	186	,6		13	3	881	,28 ,84		48	12	1658	,88
50 60	233	,25		14	3	1347	,84		49	13	397	,44
60	279	,9		15 16	4	86	› 4		50 51	13	864	,
70 8 0	326	,62		16	4	552	,96		51	13	1330	,56
80	373	, 2		17 18	4	1019	,52		52	34	69	,12
90	419	,94		18	4	1486	,08		53	14	535	,68
	1000	1.0	ŝ.	19	5	224	,64		54	14	1002	,24
1.1				20	5	691	,2		55	14	1468	,8
			1.11	21	5	1157	,76		56	15	207	,36
			N 11	22	5 6	1624	,32 ,88		57	15	673	,92
				23	6	362	,60	ľ.	58	15	1140	,48
	-			24	6	8 29	, 44		59 60	15	1607	,04
				25	6	1296	,		60	16	345 812	,6
	-		103	26	7	34	,56		61 62	16 16	012	,16
			1.5	27 28	7	501	,12 ,68		62		1278	,72
			610		7	967	,00		63	17	17	,28 ,84
			67	29	7 8	1434	,24		64		483	,04
			1.5	30	8	172	,8 ,36		65 66	17	950	,4
	2			31	8	639	20		67	17 18	1416	,96
				32	8	1105	,92		67 68	10	155	,52
			1	33		1572	,48		60	18	622 1088	,08
		1		34 35	9	311	,04		69 70	18		,64
1		1		135	19	777	,6		70	10	1555	,2

Table I. | Table II. { Cubic or Solid Measure, one Solid Yard the Integer.

N.

A Set of New Decimal Tables, &c. 117

Nº.	Fc	1. c.	Pt	Nº.	Fc.	I.c.	Pt.	INº.	Fc	I. c.	Pt.
1			-6	81	21	1502		91		984	- 1
71	19	293	,76 ;	1		1503	,36	11	24		90
72	19	760	,32	82	22		,92	92	24		,52
73	19	1226		83	22	708	,48	93	25	190	
74	19	1693	,44	84	22	1175		194	25	656	,64
75	20	432	,—	85	22	1641		95	25	1123	,2
76	20	898	,56	86	23	380	,16	96	25	1589	,76
77	20	1365		87	23	846	,72	97	26	328	,32
78	21	103	,68	88	23	1313	,28	98	26	794	88
79	21	570	,24	89	24	51	,84	99	26	1261	,44
8 0	21	1036	,8	90	24	518	,4				

Table I. | Table II. { Cubic or Solid Meafure, one Solid Foot the Integer.

INS.	I.C	20	Pt.	 Nº.	I. c.	25	Pt.	1	Nº.	. I. c.	Qc	Pt.
		\sim				\simeq					- 10 · .	1
I		11	,05	I	17	17	,92		23	397	28	,16
2	-	22	,11	- 2	34	35	,84		24	414	46	,08
3 4 5 6	-	33	,17	3	51 69	53	,76	81	25	432	00	,
4	-	44	,23	4	69	7	.68		26	449	17	,92
5		55	,29	4 5 6	86	25	,6	1.1	27	466	35	,84
6	I	2	,35	6	103	43	,52		28	483	53	,7 6
7	I	13	,41	7 8	120	61	,44		29	501	7	,68
7 8	I	24	, 47	8	138	15	,36		30	518	25	,6
9	I	35	,53	9	155	33	,28		31	535	43	,52
10	I	46	,59	10	172	51	,2		32	552	61	,44
20	3	29	,18	II	190	5	,12		33	570 587	15	,26
30	3 56 8	11	,77	12	207	23	,04		34	587	33	,28
40	6	58	,36	13	224	40	,96		35	604	51	,2
50	8	40	,95	14	241	58	,96 ,88	2.	36	622	5	,12
5 0 63	10	23	,54	15	259	12	,8		37	639	23	,04
70 80	12	Ó	,13	16	276	30	,72	1	38	656	40	,96
80	13	52	,7 2	17	293	48	,64		39	673	58	,88
90	15	35	,31	18	311	2	,56		40	691	12	,8
			-	19	328	20	,48		41	708	30	,72
				20	345	38	14		42	725	48	,64
·				21	362	56	,32		43	743	2	1,5ó.
<u> </u> '				22	380	10	,24	Ļ.	44	760	20	1,48

Nº.	I.c.	Re	kt.	Nº.	1. 6.	40	Pt.	N	1.6	40	Ft.
45	777	38	,4	64	1105	58	,88	83	1434	115	,36
46	794	56	,32	65	1123	Í2	,8	84	1451		
47	812	10	,24	66	1140		,72	85	1468	51	
48	829	28	,16	67	1157	48	,64	86	1486	5	,12
49	846	46	,08	68	1175		,56	87	1503	23	,04
50	864	Ó		69	1192		,48	88	1520		
51	88 i	17	.92	70	I 209	38	,4	89	1537		,88
52	898	35	,84	71	1226	56	,32	90	1555	12	,8
53	915	53	76	72	1244		,24	91	1572		,72
54	933		,68	73	1261		,16	92	1589	48	,64
55	<i>9</i> 50	25	,6	74	1 278	46	,08	193	1607	2	,56
56	967	43	52	75	1296	0	,	94	1624	20	,48
57	<i>9</i> 84	61	,44	76	1313'		,92	95	1641	38	<i>•</i> 4
58	1002	15	36	77	1330		,84	96	1658	56	,32
59	1019	33	28	78	I347,		,76	97	1676	10	,24
60	1036	51	2	79	1365		,68	98	1693.		
61	1054	5	12	80	1382		,6	197	1710	46	,08
62	1071	23	04	81	1399	43	,52				
63	1088	40	,96'	82	1416	61	,44'	•]		

Table I.

1

Table IL { Land Measure, one Acre she Integer.

1

I

NO	Pa	Yal	Pt .	-	Rods	0.	T	2	21	Pal	Ya	Pr
	14					[2	- 2	14	
II			,48		Nº.	0	25	50	75	0	Ō	,0
2	_		,96			I	26	51	76	I	18	,15
3		1	44			2	27	52	77	3	6	,05
	1	·I	,92			3	28	53	78	4	24	,2
456		2	4			4	29	54	79	6	12	, I .
6		2	,88			56	130	55	80	8	0	,—
7		3	,36			6	31	56	81	9	18	,15
78		3	,84			7 8	32	57	82	11	6	,05
9	-	4	,32			8	33	58	83	12	24	,2
10	-	4	,84		1	9	34	59	84	14	12	,I
20	-	9	,68		1	10	35	60	85	16	0	. ·
30		14	,52			II	36	61	86	17	18	,15.
40		19	,36]	12	37	62	87	19	6	,05

A Set of New Decimal Tables, &c. 119

Nº.	Pq	Yq.	Pt.	Rods	0	1	2	3	Pq	Yq	Pt.
50		24	,2	Nº.	13	38	63	88	20	24	,2
60		29	,94	i .	14	39	64	89	22	12	μI
70	I	30	,88	Į .	15	40	65	90	24	Q	,
80	I	8	,72		16	4I	66	91	25	18	,15
190	I	13	,56	1	17	42	67	92	27	6	,05
				1	18	43	68	93	28	.24	,2
1 1				}	19	44	69	94	30	-12	, I
				i	20	45	70	95	32	0	,
		· ·		ł	21	46	7L	96	33	.18	,15
				l	22	47	72	97	35	6	,05
				ł	23	48	73	98	36	24	,2
1				 1	24	'49	74	1 <i>9</i> 9.	38	12	',1

Table I. | Table II. { Time. One Year the In-

-4	Nº.	17	Ħ	P.	+	NO	М	17	ih.	Ħ	PA	No	M	W	D.	H	P+
	14.	<i>D</i> .	1.1.	4 81					.	120	4 10				μ.		- 1
	T			B 7		1			5	75	,6	19	2	1	6	8	
		·							1.3	1 - 1	94		-	_			
	2		I	174		2	-	:1	ŀO		,2	20	2	2	3	Q	
	3		2	163		3	-	I	3	22	,8 I	21	2	2	6	ΙŞ	,6
1	4		3	15	•	4	-	2	Ö,			22	2	3	3	7	,2
	5	-	4	138		5	\vdash	2	4	6	,	23	2	3	6	22	,8
ł	6	-	5	125		6	-	.3	Ó	21	,6	24	3	0	3	14	,4
1	7	-	6	112		7	\vdash	.3	4	13	,2	25	3	1	Ō	Ö	, (
1	8		7	1-		8	11	ó		4	,8	26	3	I	3	21	,6
	9		7	,88		9	1	'o	4	20	,4	27	3	2		13	1
	10		8	,76	:	10	1	1	I	12	,—	28	3	2	4	4	0
	20		17	,52	•	11	1	I	5	3	6	29	3	3	c	20	4
	30	1	2	,28		12	1	:2	Í	19	,2	30	3	3	4	12	, _]
	40	1	11	,04	•	13	I	2	5	10	,8	31	4	ó	I	3	,6
ŀ	50	I	19	,8		14	I	3	2	2	,4	32	4	0	4	19	,2
ŀ	60	2	4	,56		15	1	3	6	18	,	33	4	I	i	IC	8
ŀ	73	2	13	,32		16	2	ć	2	9	,6	34	4	I	5		,4
	8 ว	2	22	,08		17	2	С	6	1	,2	35	4	2	í	_	,6
	90 [.]	3	6	,84		18	2	1	3	16',	8	36	4	2	-51	9	.6

120 A set of New Decimal Tables, &c.

i	N°.	М.	W.	D .	H.	Pt.		Nº.	M	W.	D.	H.	Pt.
								69	 8				
	37 38 39 40	4	3 3 3 0 3 0	2	I 16	,2 ,8 ,4		70		3		20 12	,4
	20	4	S S	5 2	8	,00 		70 71 72	9 9	I	3	3	,— ,6
	37	2	0	6	ġ	24		72	9	I	3	2 19	,0
	41	5	I	2	15	.6		72	9	2	3	10	.8
	42	ź	I	6	7	.2		74	9	2	4	2	.4
	41 42 43 44 45 46 47 48	4555555556	2	2	16 8 0 15 7 22	, 6, 2, 8, 4, 6	l i	75	9		ŏ	2 18	1,8,4,1,6,1,8,4
	44	Ś		6	14	,4		76	9	300	4	9	,6
	45	Ś	3		6	·		77	9 10	ó	i	I	,2
	46	5	2 2 2 2 3	3 6	14 6 21	,6		78	IC	0	4	1 16 8	,8
	47	6		3	13 4 20	,2 ,8		<u>7</u> 9	10	I	1	8	7 4
	48	.6	I	0	4	,8		80	10.	I	5.	0	,—
	49 551 52 53 55 57 58 59 61 61 62	6	I	3	20	¥ , 0, 1, 8, 0, 0, 1, 8, 0, 1, 9, 1, 8, 0, 0, 1, 8, 0, 0, 1, 8, 0, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,		81	IO	2	I	15 7 22	, o v o 4
	50	6	2		12	17		82 0	I0	2 3 3 0 0	52	7	,2
	ŞI	6	2	4 0	3 19 10	,0		ō3	10:	• 3	2	22	,ð
	52	6 6	3 3 0		19	,2	•	04 01	10	3	5	14 6 21	7 4
	23		3	4	10	,0		0) 94	11	0	2 6	0	,— ,6
	24	7	0	1	2 18	-74		8-	11 11	I	2	21	,0
)) \$6	4	Ţ	4 1	10 9	,-		88	11	I	6	12	,2 Q
	57	14				,0		80	11	2	2	4 20	,2 ,8 ,4
	58	7777777 77778	12	5 1	1 16 8	.8		90	11		6	12	74
	59	1 7			8	.4		91	11	2 3 3 0	1	2	,- ,6
	60	7	2330	5.2.5 2.6	0			92	11	1.2	36	3 19	,2
	61	7	3	Ś	15 7 22	,6		93	12	ó		10	, 8
	62			2	7	,2		94	12	I.	3	2	,4
	63	8 8	0 I	6	22	,8		95	12	I	30	18	
	64		I	2	14 6	› 4]	73 74 75 77 77 78 79 81 2 34 56 78 89 99 99 99 99 99 99 99 99 99 99 99 99	112	2		9	,6 ,2 ,8
	65	8 8	I	6	6	,-		97	12	2	4	1 16	,2
	66		2	2	21	,- ,6		98	12	3	0	16	
	63 64 65 66 67 68	8 8	2	6	13	,2 ,8		99	12	3	4	8	, 4
	68	8	3	3	4	<u>,</u> ŏ	·		ł	1	ł	1	

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Nº.

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22			
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-		•	.

I. | Table II. { Time. Integer.

One Month the

105	<i>IVIONID</i>	

Nº.			-				-				
14	H.	Pf.		W.	0	I I	2	1_3	Ų.	H,	. Pt.
I I	•		1	Nº.			1 ==				
		,06		14-	0	25	50	75	0	0	l,
2		,13			I	26	51	76	0	6	,72
3		,2			2	27	52	77	0	13	+44
345678		,26			3	28	53	77 78	0	20	,16
Ś		,33			4	29	54	70	I		,88
6		,4	4				55	79 80	1	2	,000
7	_	76		· ·	5	30	22			9	,6
ģ		,46				31	56	81 82	1	16	132
0	-	,53			78	32	57 58	Ø 2	1	23	,04
9		,6			8	33	58	83	2	5	.46
10		,67			9	34	59 60	01 I	2	12	,48
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A Set of New Decimal Tables, &c. 123

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CHAP.

CHAP VI. The Use of DECIMIALS in all the Rules. of Proportion, VIZ. The Rule of Three direct and Inverse; and the double Rule of Five Numbers. I. I.R ECT Proportion is when of four Numbers, the first is in the fame Proportion bigger or less than the second, as the third is bigger or less than the faurth Number. Phu as 4 is to 12 for 18 to 0.18; confequently the secon middle Numbers multiplied together, are qual to the Product of the two extreme ones; as 12% 6 == 18 × 4 == 72. Hence is deduced the general Rule for working all Queltions in the Rule of Ubree direct, viz. Multiply the feond Numbers whe third, and divide by the

first; and the Qubtient will be the fourth Number fought, or Answer.

Now as these Rules of Proportion have some certain Numbers given to find others in the same Proportion, and their Subject being generally *Trade* and *Merchandise*, those given Numbers often consist of *diverse Parts* and *Denominations*, which therefore are to be reduced to *Decimals*, in order for the Question to be wrought in the simplest Manner, and with the greatest easte and expedition; which ought to be the *Aim* of every *Artist*.

But as the Manner of Reducing the Parts of Coins, Measures, Weights, &c. hath been fully taught already; I shall only here express the Question vulgarly, but state and work it decimally.

Queficion 1. If $7\frac{1}{2}$ Yards of Cloth coft 2l. 12 s. 9d. What will 140 $\frac{1}{2}$ Yards coft at that Rate?

Thus

	fe of Decimals	827
Vulgarly Deçimally	7 2 2 12 9 1 140 2 7,75 2,6379 : 140,5 -	**************************************
· · · · ·	131875 105500 11 26375	L. s. d.
···- 7;7	75) 979, 56875 (47,8153 = 3100	
~ • •	• 6056 .5425 • 6318	
	<u> 6200</u> 1187	
	4125 3875	

2325

2500

Queftion 2. At the Rate of 51.8 s. 4 d. per C. Weight, What will 19C. 2 gr. 14 lb. coft?

. C. l. ۰. C. Q. 13. **J**. d Stated thus Vulgarly 1: 5-8-4:: 19:2:14 Decimally 1: 5,416 :: 19,625 5**,**41*6* 1.2. 4 9) 117750 **a**. . ٤ 130833. ١. 11 19625 1 78500 98125 wer, 106 /. 106,302082

4 1 6

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Question

Queftion 3. Suppose four Hogbeads, three Firkins, and five Gallons of Bess cold 61. 143. 8 d. How much is that per Hogbead, and per Gallon 3

Hds. Fr. G. l. s. d. Stated thus { Vulgarly 4-3-5:6-14-8:: I. Decimally 4,5929: 6,73: :: I

OPERATION.

4,5829) 6,73333 (45 ⁶⁷³
4,588) 6,7266 (1,4661 (,0271 4588 (108
21386 · 386 18352 378
* 30340 **81 27528 54
28120 27 27528
**5920
45 88 1332

7. 1. s. d. The Answer $\begin{cases} 1,4661 \neq 1 : 9 : 3 + per Hog bead. \\ 0,0271 \neq 0 : 0 : 6 + per Gallon. \end{cases}$

Queffion 4. The mean Motion of the Sun being known to be 59' 8" each Day, 'tis required to know in what time He performs one intire Revolution through the whole Circle of the Ecliptic, or 360 Degrees.

This Queffion 5 Vulgarly 0-59-8: 1:: 360-00-00 is thus flated. Decimally ,983 : 1:: 360

QPL

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OPERATION

,983) 360 (98, 360 ,887) 324,000 (365,2762=365:6:37:43 2661
• 5790
5322
.4680
4435
• 2450
<u>1774</u> 6760
6700
5510
5322
- 1881
¥774
106

These are the various Cases which may happen in the Rule of Three Direct; by which any one may observe the Advantage of Decimals, and the absolute Necessity of understanding the Management of circulating or repeating Decimals.

The Rule of Three Inverse.

Inverse Proportion is, when of four Numbers, the third bears the fame Ratio or Analogy to the first, as the second does to the fourth:

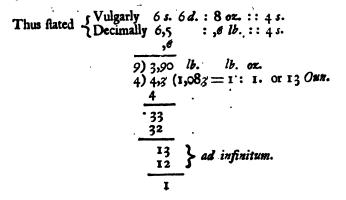
Whence the *Rule* is; to multiply the first and fecond of the given Numbers, and divide that **Product** by the third; the Quotient will be the fourth Number, or Answer.

To know when the Terms of a proposed Question are in this reciprocal or inverse Proportion, observe this Rule; viz. When the third { Bigger } than the first, { Lefs, } Number is { Leffer } and requires { More, } Terms

130 in the Golden Rule direct.

Terms are in the inverse Ratio; and are to be worked by the Rule above; as in the following Inflances.

Queftion 1. If when Wheat is fold for 5s. 6d. per Bushel, the Penny White Loaf ought to weigh eight Ounces Troy; What must it weigh when it is at 4s. per Bushel?

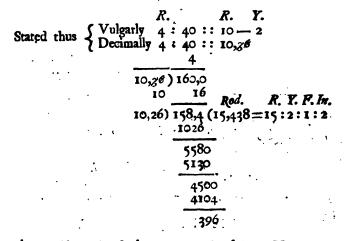


Queficon 2. Two Equal Parallelograms A, B given, the Length of A is 8 Feet 8 Inches, and its Breadth 4 Feet and 3 Inches; the Breadth of B is 2 Feet 10 Inches, Quere its Length?

F. In. F. In. F. In. SVulgarly 4-3:8-8:: 2-10 Thus stated Decimally 4,25 : 8,6 :: 2,83 8,8 8.6 2,85 4,25 9) 2550 2823 13 3400 36,82 **2.8**2 13 Inches the Answer. 368 2,55) 3315 255 765 Question

The Use of Decimals

Quefiion 3. A Piece of Land 4 Rod broad and 40 long; being a Statute-Acre; tis required to know what Length, with 10 Rod and 2 Yards Breadth, will make an Acre?



The Double Rule of Three ; or Rule of Five Numbers.

In this Rule of Proportion there are *Five* Numbers given to find a Sixth in Proportion; which is either Direct or Inverfe, according to the Nature of the Question.

Quefiions in this Rule are performed at two Operations, that is, by a *double flating* the Quefiion, most generally.

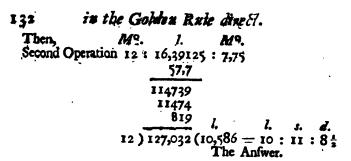
Question 1. What is the Interest of 364 l. 5 s. for seven Months, three Weeks, at the Rate of 4 l. 10 s. per Cent. per Annum?

 $\begin{array}{c} l. & M. l. s. l. s. M. W. \\ Thus {Vulgarly 100: 12: 4 - 10::364 - 5: 7 - 3 \\ flated {Decimally 100: 12: 4,5 :: 364,25 : 7,75 \\ l. l. l. \\ First Operation, 100: 4,5:: 364,25 \\ Hence the Interest of 364,25 l. { 182125 \\ for one Year, is 16,39125 l. { 145700 \\ 100 \\ 1639,125 \\ (16,39125 \\ \end{array}$

S 2

Then

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Question 2. Suppose it were required to know what Prineigal would gain 151. 14 s. 8 d. in nine Months and three Days, at the Rate of 41. 10s. per Cent, per Annum, Quere. the Answer?

l s. M° . *l*. *l*. s. *d*. M° D. Thus Vulgarly 4:10-12-100-15:14:8-9:3flated Decimally 4,5 -12-100-15,73 -9,107

The First Operation Direct.

ı	$ \begin{array}{c} :: 15,72 \\ 100 \\ 4,5 \\ 135 \\ 223 \\ 180 \\ \hline 433 \\ 4^{05} \\ 283 \\ 270 \\ 133 \\ 90 \\ \end{array} $	u Ad infinitum.

The Second Operation therefore must be wrought in-

. . .

Thus,

The Use of Decimals

M?. Thus, 12 :	M°. 349,62 :: 9,107 12	
	69,82\$ 34,9699 Y. I. s. d.	
9, 10 7)	4193,5 (460,6956 = 460 : 13 : 11 36428	:
	55275 54642	
	•• 63355 54642	
·	- 87135 81949	

But any Queffion in this Rule may be answered at one Operration, by the following Rule :

Make the $\begin{cases} 1 & \text{ff} \\ 2 & \text{five, the fame} \\ 3 & \text{five, the fame} \\ \end{cases}$

Then, Multiply the *Three* Numbers to the Right-hand together, and the *two firft* to the Left-hand; and divide the *firft Product* by this *laft*, and the *Quotient* will be the firth Number, or *Anfwor*, if the Proportion be *Direg*.

Queficen 3. If a 1000 Men can dig a Trench 500 Feet Long in 24 Hours, what Length of fuch a Trench can 9800 Men dig in 10 Hours?

Thus .

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Men Hours Feet Men Hours Thus flated, 1000. 24: 500 :: 9800. 10 24 IO 24000 98000 500 24 000)49000 000 (2041,6 48... 100 96 • 40 24 The Answer is Feet Feet In. 160 2041 = 2041 : 8144 Infinitum. The Length required.

in the Golden Rule direct.

If any Part of the Question be in reciprocal or inverse Proportion; place the Three first Numbers as in the last Question; and of the other two, place *That* the fourth, which is of the fame kind as the fecond; and confequently the other must be the fifth Number.

Question 4. If 1000 Men can dig a Trench in 24 Hours 500 Feet Long, How many Men will dig 2041, & Feetin 10 Hours?

Stated thus,		H. Feet. 4 : 500 : :	<i>H. Feet.</i> 10 [°] : 2041, ^g
		10	1000
		5000	2041866,6
Rule. Multi	ply the.	•	
1st, 2d, and 5th bers, and the 3	inum-	L	81#5666,6
4th; then divi	de the S		40833333,3
first Product by t		5 00	0,490001000(9800
the Quotient is t	he An.	• ,	45 .
fwer; viz. 9800 Men.	0 Men. J	•	40
-	-		40
			•• 00

But for the greater readiness and ease of the ingenious Arithmetician, I thall transcribe that famous general Theorem in The Use of Decimals.

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in Mr. Ward's Young Mathematician's Guide, which thews at once how to answer any Question of Fioe Numbers at one Operation, without regard to the Proportion of the Terms; be that Direct or Indirect as it will.

The Theorem is this, TgP = Gpt. In this Theorem you observe three Capital Letters, viz. T, P, G, and the fame three Letters in *fmall* Characters, g, p, t. The three Capitals fignity the Three first conditional Terms of the Question,

Thus, SP, Is the Principal Caufe of Gain, Lofs, Action, &c. T, Is the Time, Space, Diftance, &c. G, Is the Gain, Lofs, Action, &c.

Of the *Three fmall Letters*, (which correspond to, and fignify the fame with the *Capitals*) two always move the Quefison, the other fhews the *Anfwer*; which, as the Letters are three, is *threefold*; and anfwered by the fame *Theorem* difposed in these three proper *Terms*.

Viz. If $\begin{cases} P \\ g \\ \end{cases}$ be fought, the Theorem is $\begin{cases} \frac{T_g P}{iG} = P.\\ \frac{T_g P}{Gp} = t.\\ \frac{Gt P}{T_w} = g. \end{cases}$

Or thus, $T_gP \div Gt = p$. $T_gP \div Gp = t$. $Gpt \div TP = g$.

If any Arithmetician should complain he does not underfland such Algebraic Forms and Characters, all that I have to answer is, That 'tis a very necessary Part of his Business and Profession, and highly concerns him to learn it.

Come Contraction and

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CHAP.

CHAP. VII.

A New Decimal Practice; or a short Way of computing all kind of Merchandise by DECIMALS.

HO' there is force any Part of Arithmetick in which Decimals are of greater (or indeed to great) Service, as Prefile; yet fins of all others has been the leaft improved by it; hardly an Author can be met with on this Head; and thole who have undertaken it, have prefunded as with but imperfect Sketches, and left the Matter unfinited. I hope what follows in this Chapter will give Satis-Metion in this Point.

The Tables of aliquot Parts commonly used, are these

s. d. Parts. 40 - 0 - 2 6 - 8 - 3 5 - 0 - 4 4 - 0 - 5 3 - 4 - 6 2 - 0 - 10 4 - 12	The even or aliquot Parts of a Pound Sterling. By which di- viding, gives an Answer in Pounds.
d. Parts. .6 - 2 Y	
$\begin{array}{c} 4 - 3 \\ 3 - 4 \\ 2 - 6 \\ 1 \\ 1 \\ 1 - 12 \end{array}$	The even or aliquot Parts of a Shilling Sterling. By which di- viding, gives an Answer in Shil- lings.

But the Table following is far more general, expeditions and useful; and has not yet been applied to Decimal Practice.

A

• • • •			· · · · ·	
Price Divisors.	Price.	Divisors.	Price	Divisors.
d. q . o: 1 3,4,80 o: 2 6,80 o: 3 4,80 1: 0 4,60 1: 1 4,6,8 1: 2 2,80 1: 3 3,49,-8 2: 0 3,40 2: 1 3,40,+8 2: 2 3,40,+4 2: 3 80,-12 3: 1 80,+12	<i>d</i> . <i>q</i> . <i>6</i> : 1 <i>6</i> : 2 <i>6</i> : 3 <i>7</i> : 1 <i>7</i> : 2 <i>8</i> : 0 <i>7</i> : 1 <i>7</i> : 3 <i>8</i> : 2 <i>8</i> : 3 <i>9</i> : 1 <i>9</i> : 1	$80, \times 2, +12$ 40, +12 40, +6 40, +6 40, +6 40, +6 40, +4 40, +4 $80, \times 3, -4$ $80, \times 3, -4$ $80, \times 3, +12$	s. 1 2 3 4 5 6 6 7 7 8 9 10 10 11 13	20 10, $+2$ 10, $+2$ 10, $\times 2$ 4 10, $\times 3$ 10, $\times 3$, $+2$ 10, $\times 3$, $+2$ 10, $\times 4$, $+2$ 3, $+10$ 2, $+10$ 10, $\times 6$ 10, $\times 7$ 10, $\times 7$
$3 : 2 : 80, +6$ $3 : 3 : 80, +4$ $4 : 0 : 60.$ $4 : 1 : 3, 40, \times 2, +8$ $4 : 2 : 60, +8, 2$ $5 : 0 : 6, 8$ $5 : 1 : 40, -8$ $5 : 2 : 40, -12$ $5 : 3 : 80, \times 2, -12$ $5 : 3 : 80, \times 2, -12$ $5 : 0 : 40.$	9:2 9:3 10:0 10:1 19:3 10:3 11:0 11:2	80, ×3, +4 80, ×3, +4 30, +4,8 20, +8 20, +8 20, +2,2,6 20, +2,2,6 20, +2,2,6 40, ×2, -12 30, +2, -16		40, X7 40, X7 10, X8 10, X8, +2 10, X8

A General Table for Decimal Practice.

An Explanation of the preceeding Table."

The first Column shews the Price of the Commodity, either in Pence and Farthings, or in Shillings, for one of a fort; as one Pound, Yard, Piece, &cc,

Against the Piece, you observe in the fecond Column, feveral Numbers, of which those which fiand first, and have nothing prefixt to them, are Divisors; by which any given Quantity or Number of Yards, Ells, Pounds, are to be divided.

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If any Number follow these with any Character prefixt to them as $2,40,\times2,+8$. $80,\times3,-12$, Sc. They are to be understood, and read, as in the following Examples.

3,4,-8 From a 4th of a 3d, take one 8th of that 4th To a 4th of a 3d add an 8th of that 4th. 3,4,+8 To a 40th of a 3d, multiplied by 2, add 3,40,X2,+8 an 8th of that 40th. To a 60th add an 8th of that 60th, and 60,+8,2 'half of that 8th. To a 3d add an half of that 3d, then fub-3,+2,-16 { fract a 16th of that 2d. From the given Number take one 20th 1.---20 Part.

These being well understood, 'twill not be difficult to use the Table on all occasions with ease; especially after perusing the Examples ensuing, which are chosen for the more difficult Parts thereof.

Note, When the Price confits of Shillings only, the Number may be multiplied by the Decimal, that is, half the Namder of Shillings, and the Answer will be the fame.

Ex. 1. At 19. per Yard, What coft 144 Yards? One 3d = 48One 4th of that = 12One soth of that = 0,15=3s. Answer. . . Ex. 2. At 39. per Yard, What coft 172,5 Yards? One 4th = 43,125One 80th of that $= 0.53907 = 103.9d \frac{1}{4}$. Ex. 3. At 1 d. 1 q. What coft 1792,25 One 4th = 448,0625A 6th of that = 74,67708 An 8th of that $= 9,33463 = 91.6s.8\frac{1}{2}d$. Ex. 4. At 1 d. 3 q. What coft 9742,6 One 3d = 3247,5 A 40th of that = 81,18888 From which take an 8th = 10,1436rl. s. d. Remains the Anfwer = 71,04527=71:00:104 Ex.

A New Decimal Practice.

Ex. 5. At 2 d. 1 q. What coft 3696,24 One 3d = 1232,08A 40th of that = 30,8020\$ To which add one 8th =3,85025 L £ đ. The Sum the Anfwer == 34,6523 = 34 : 13:05 Ex. 6. At 2 d. 3 q. What coft 4130,22? One 8oth =51,827 From which take a 12th == 4,302 L _ d. Remains the Answer = = 47 : 6:6 47,328 = Ex. 7. At 4 d. 1 q. What coft 1932,49 ? One 3d = 644,16A 40th of that 🚃 16.104 Ditto = 16,104 Of which add an 8th == 2,017 L The Sum is the Answer == 34,22x = 34:4:5Ex. 8. At 4 d. 3 q. What coft 948,48? One 60th =15,802 One 8th of that == 1,978 One half of that == 0,987 L đ. s. The Sum is the Anfwer = 18,272 = 18:15:5 Ex. 9. At 5 d. 3 q. What coft 1012,2 ? One 80th =12,6 2 One 80th, $\chi_2 =$ 25,33 Substract a 12th of an 80th == 1,05 d. L Remains the Answer == 24,27 = 24 : 5 : 6

T 2

Ex.

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Ex. 10. At 8 d. 1 g. What coft 2640? One 80th = 33' 3
That multiplied by $3 = 99$ Subfract a 4th of an 80th = $8,25$ l. s. d.
Remains the Anfwer $= 90,75 = 90:15:0$
Ex. 11. At 9 d. 1 q. What coft 96x,9z? One 80th = 12,024 3
An 8oth $\times 3 = 36,072$ To which add 1 2th of an 8oth = 1,002 <i>l. s. d.</i>
The Sum is the Anfwer = $37,074 = 37$: 1 : 5 ⁴ / ₄
Ex. 12. At 10 d. 3 q. What coff 1600 One 40th = 40 Add an half = 20 Add halt that = 10 Add a fixth of that = $1, \emptyset$ <i>l. s. d.</i> The Sum is the Anfwer = $71, \emptyset = 71: 13: 4$
Ex. 13. At 11 d. 3 q. What coff $908,18$? One 30th = $30,208$ To which add an half = $15,103$
From the Sum = $45,30\%$ Subfract a 16th = $0,943$ 1. s. d.
Remains the Answer $= 44,369 = 44$: 7:3
<i>Ex.</i> 14. At 7 s. What coft $365,25$? One 10th = $36,525$ 3
One 10th $\times 3 = 109,575$. To which add half that 10th = 18,2625 The Sum is the Anfwer = 127,8375 = 127:16:9
Ex.

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A New Decimal Practice.

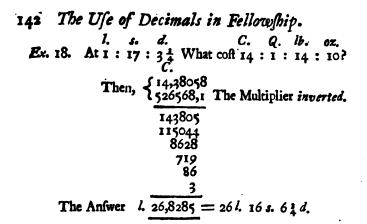
Ex. 15. At 19 s. What coft 257, ?? Substract a 20th = 12,882 L đ. Remains the Anfwer = 244,783 = 244 : 15 : 8Ex. 16. At 13 s. 9 1 d. What coft 96x,92? 96x,9z 8 oth = 12, o2410th = 96, 1923 For the 80th $X_3 = 36,97z$ $9\frac{1}{4}d$. For 13 12 of 80 = 1,002 $10th \times 6 = 577, x_{53}$ Shil. s. d. 1 of 10th = 48,096 Add { 37,074 for 0:94 625,249 for 13:00 The Sum = 625The Anfwer = 662, 323 for 13:94

In this Example (and any other) the Anfwer for the Sbillings is found with least trouble, and Figures, by Multiplying the given Number by the Decimal of the Shillings,

If the Price or Value confift of Pounds, Shillings, Pence, Sec. the most ready and practical way, is to turn the whole into Decimals, then multiply the given Number (turn'd into Decimals also, if express'd in diverse Parts;) and the Product will be the Answer.

Ex. 17.	At 51. 16s. 8d. What coft 270? 1. s. d.
	$5,8_3 = 5:16:8$
	9)810
<i>;</i>	900
	2160
	1 350
	The Answer $= 1575,00$
	Fy.

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These Examples are fufficient to the ingenious Practical Student of *Decimal Arithmetick*; who with those Instructions will easily (proprio Marte) apply this noble Art to all Cases of Common Trade and Merchandise.

CHAP. VIII.

The Use of DECIMALS in the Rules of Fellowship, Tare and Trett, Barter, Gain and Loss, Exchange, Alligation, Rule of False Position, Extraction of Roots,

Single Fellowship; or That without Time.

t.

HE Rules of Fellowship are proper to Merchants and those who Trade in Company, or Partnership; where they have a common Joint-Stock to traffick withal; for to every one of the Company is distributed his due share of Gain or Loss acquired by Trading, in proportion to his Stock laid out, by this following

Rule

The Use of Decimals in Fellowship. 143

Rule.

As the total Sum of the Stocks, is to the total Gain or Loss; so is each Man's particular Stock, to his particular Gain or Loss.

Example. Suppose Four Merchants, A, B, C, D, make a Joint Stock of 421 l. 8 s. 6 d.

	C	А	puts in	154	:	13	:4	==	154, <i>8666</i> 110,9250
Thue	ر	B	-	110	:	18	:6	=	110,9250
I musy	7	С		95	:	00	: 8	=	110,9250 95,0333
	L	D		60	:	16	: 0	=	60,8
The	who	ble	Stock =	421	:	08	: 6	=	421.425

The Trade and Gain 88 l. 17 s. 10 d. = 88,8918 l. Tis required to find each Man's Part or Share of that Gain.

l. l. Then as 421,425 : 88,8918		154,5 110,925 95,03 60,8	: 32,6192 : 23,394 : 20,0425 : 12,8227
The Sum of the feveral Shar	es		- 88,8784

Which being the fame with, or equal to, the total Gains always proves the Trath of the Work.

But all Cafes in the Rules of Fellowship are foonest and easieft answer'd by finding the Proportional Part of the Gain or Loss due to one Pound; and then by that to multiply each Man's particular Part of the Stock; for the feveral Products in fuch Cafes, are the feveral Answers; viz. each Man's Part of the Gain or Loss.

l. l. l. l. Thus, As 421,425 : 88,8918 :: 1 : ,2109 the common Multiplier.

7. A's Part of Stock = 154,6 Multiply by ,2109	<i>B</i> 's Part of Stock = 110,925 Multiply by ,2109
1391ø 154866 3093333	998325 1109250 221850
As Part of Gain $=$ 32,6192	B 's P . of Gain = $23,394$, $3c$.

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C's Part of Stock = 95,02 Multiply by ,2105	<i>L's</i> Part of Srock = 60,8 Mukiply by ,2109
85524 95033 1900#566	6080
Cs Part of Gain $= 20,04253$	D's Part of Gain=12,82272

Here every Man's Share is the fame as before.

Double Fellowship, or That with Time.

Fellowship with Time confiders the Share of the Gain or Lofs with regard to the Money, and the Time it was imployed, and proportionates it to both by the following

Rule.

Multiply each Man's Stock by the Time it was employed; then fay, As the fum of those Products, is to the whole Gain or Loss; fo is every one of the Products, to its proportional Part of the Gain or Loss.

Example. Three Merchants A, B, and C, enter into Partnership, thus;

A puts in 65,5 for 8 Months, 2 Weeks, and 3 Days. B - 78, 0 - 12 Months, 3 Weeks, and 1 Day, C - 84 - 6 Months, and 6 Days.

They traffick and gain 140,016 l. 'Tis required to find each Man's Share proportional to his Stock, and Time 'twas in.

 $\begin{cases} l. Months. Products. \\ Stock 65,5 \times 8,607 = 563,7585 \\ B's Stock 78,6 \times 12,3357 = 970,4084 \\ C's Stock 84, \times 6,214 = 521,976 \\ The Sum of the Products = 2056,1429 \end{cases}$

Then

Then, As 2056,1429 : 140,016 $\begin{cases}
:: 563,7585 : 38,3918 = A \\
:: 970,4084 : 66,0846 = B \\
:: 521,976 : 35,5465 = C \\
The whole Gain very near = 140,0229 l.
\end{cases}$

Questions in this Rule also are much better answerd by finding the Proportional Part to one Pound, for a common Multiplier, as before.

Thus, as 2056,1429 : 140,018 :: 1 : ,0681 Comm on Multiplier.

L

For $B = 970,408$: 563,7585.	The Operation for $A_{,=}$
1860,	1860,0	The Multiplier inverted
58224	338255	:
7763	45100	· · · · · · · · · · · · · · · · · · ·
97	563	-
66,080	38,3918	
		. -

For
$$C = 521,9760$$

1860,0
313185
41758
522
35,5465 {Their feveral Parts of the
Gain, as before.

Thus appears the excellent Use of Decimals in the Rules of Fellowship.

Tare and Trett.

Tare is the Weight of the Hogshead, Cheft, Bag, Cast, &c. which contain the Goods bought or fold.

Trett is an Allowance of 4 lb. in 100, or 104 lb. for Goods wherein is Loss by refuse, &c.

Cloff is an Allowance of 2 Pound upon every Draught which exceedeth 300 Grofs Weight.

Sub-

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Subtile is the Weight when the Tare is deducted, but not the Trett.

Neat Weight is the Remainder when Tare, Trett, and Cloff, if all are allowed, are taken away.

For refolving Questions in this Rule there are *feveral* Methods; but those by Decimals are much the shortest and best, and are as follow.

Question 1. What is the Neat Weight of 9 C. 2 gr. 7 lb. Tare at 14 lb. per Cent. to be deducted.

First, This may be answered by the Golden Rule in Decimals.

1b. C. If i C. allow 14, What will 9,5625 allow for Tare? 14 382500 95625Total Tare 1b. = 133,875 = 1,1953 C. C. The Grofs Weight = 9,5625 The Whole Tare = 1,1953 to be fulfinacted. The Difference is = 8,3672 = 8C. 1 qr. 13 lb. the Neat Weight.

A Second Way, is to Multiply the Gross Weight by the Decimal of C. Weight, equal to the Tare allow'd.

> The Grofs Weight $\neq 9,5625$ The Decimal of 14lb. = ,12547812519125095625

The Tare (as before) = 1,1953125 to be fubilitated.

A Third Way, is to multiply the Gross Weight by the Decimal of the Neat Part of a Hundred Weight.

Thus,

The Use of Decimals in Tare and Trett. 147

C. Thus, from 1,000 SubAract ,125	C. Then 9,5625 578,0	Multiplier inverted.
The Neat of C. ,875	76500 6697	
	478	

The Neat Weight total = 8,3671 as above.

A Fourth Way, is to work by Aliquet Parts as in Practice. Thus 14 being the Sth Part of 112; if you take an 8th of 9,5625, that will be the Tare of the Whole.

C. Thus, $\begin{cases} 2,5625 \text{ the Grofs Weight.} \\ \frac{1}{3} = 1,1953 \text{ the Tare, as before.} \end{cases}$

For the more expeditions finding the Fare by Aliquot Parts, know inferted the following Table of Tare and proper Divisors.

Tare.	Divifors.	E	Tare.	Divifors.	Tare.	Divifors.
<i>lb.</i> I	2,7,8		8	2,7	15	2,8,×2,+7
2	7,8 7,8,+2		9	2,7,+8	16	7 2,7,X2,+8
3	457		11	2,7,+4 2,7,+4,2	17 18	7,+8
56	4,7,+4	11	12	2,7,+2	19	7,+4,-20
7	2,8		14	8	21	8,+2

The Confirtuction and Use of this Table of Tare is the fame with the Table of Prices or Values in Practice, which see there taught.

Having flewn how to find the Tare, the next Business is to find the Trett, or the Neat Weight when the Trett is deducted from the Subtile;

Thus Multiply 5,0384 the Product is the Weight. the Subtile by 5,0384 the Product is the Neat Weight.

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Question

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Question 2. In 72C. 3 qr. 12lb. Gross, Tare at 12lb. per C. Trett 4lb. per 104. How many C. neat 3

C. The Grofs = 72,8571Multiply by the Decimal of 12lb. inverted =1701,0 72857 5100 72 The Tare (fubtile) = 7,8029 The Subtile = 65,0542Multiplier inverted = 4830,0 19516 5204 260 The Trett to be fubtile = 2,4980 The Neat Wr. = 62,5562 A Shorter Way, thus; C. The Gross = 72,8571Mult. by the Neat Dec. of 112 lb. inverted = 8298,0 582856 65571 I457 582 The Subtile = 65,0466The Multiplier inverted = 6169,0 585419 39027 650 390. The Neat Weight = 62,5486

These are the *best Methods* for finding *Tare* and *Trett*; and *that* I have here given for finding the *Trett* is *new* to me, not having feen it in any Author I have met with.

5

Barter.

Barter.

By the Rule of Barter, Merchants and Traders exchange Goods of different Values, Kinds, and Quantities, fo as to fustain no Lofs or Difadvantage by such a Barter or Change.

Question 1. Two Merchants, A and B barter; A would exchange 5C. 2 gr. 14 lb. of Pepper, worth 3 l. 10 s. per C. with B for Cotton worth 10 d. per lb. How much Cotton must B give A for his Pepper?

Proceed thus by Decimals to find the Value of the Pepper.

C. l. C.
Say, As
$$I : 3,5 :: 5,875$$

3,5
29375
17625
The Value of the Pepper 20,5625 = 20: 11: 2

Then to find the Quantity of *Cotton* equal to the Value of the Pepper;

•••	1.	С.	Ι.	
Say, As,	0418	: .00802		25
		,000/2	29800	~)
			1645	
			185	
			Á	
	-		T	
		,0416	,1834	
		041	1834	<i>l</i> .
			- (dal	
		,º375)	16506	(4,4016
Thus Pour inc 1			1500	
Thus B must give A C. C. ar. 1b.) ·		1506	ı
	(1500	
$4,4016 = 4 : 1 : 17^{1}$	5		and the second s	_ `
of Cotton for his Pep-			:•• 60	0
per.	1	-	37	15
	•		and the second	· · · ·
	•			:50
_			22	250
			-	Oustion
	•			Question

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Queficer 2. A has 52 Dozen of Hats, worth in ready Money 2s. 6 J. but barters at 2s. 9 d. per Hat. B has Cotton at 10 d. per Pound, ready Money. Quere at what **pass per Pennel** B mult barter his Cotton, and how much he mult give for the Plats ?

s. First; fay, As 2,4 : ,25 :: ,87 : 087 == One Penny. So that B's Conton is to be advanted a Penny a Found in Darten. Secondly, to find the Value of the (624) Harts in barter; Hat 1. Hat I. Say, As 1 : ,1375 :: 624 : 85,8 624 5500 2750 8250 1. S. $8_{5,8000} = 8_{5}$: 16 the Price of all the Hats. Thirdly to know what Cotton at 11 d. per Pound can be had for that Money ; 1. С. 1. С. Suy, As ,04582 : ,00892 .: 55,8 : 10,6982 85,8 71.36 4460 7136 ,04583),765336 C458 765336 ,04125),6888024 (16,6982 C. 4125 27630 Hence it appears that 24750 B muft give in-Exchange 286g2* C. Q. С. *lb*. 24750 16,6982 = 16:2:24of Cotton at 11.d. per lb. ÷ 40524 for 52 Dozen of Hats at 37125 2 s. 9 d. per Hat. 33990 33000 9900 8250 1650 Thefe

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The Use of Decimals in Gain and Loss. 151

These two Questions well understood, are sufficient for all other Cales in this Rule.

Gain and Lofs.

By this Rule Men of Trade and Bufferefs know what they get by Retailing Goods; and in cafe of Damage, what they lofe, by felling is at any given Rate; and whether they gain or lofe, to know at what Rate per Cent.

Question 1. If I buy Cambricks at 5 s. 6 d. per Yard, and fell them at 8 s. 9 d. What is the Gain per Cent?

s. d. e. d. l. l. s. d. Say {Vulg. 5-6:8-9::100:159-1-9!Dec. ,275:4375::100:159,09

s. d. s. d. l. l. s. d. Or, thus, $Vulg. 5-6:3-3::100:59-1-9^{1}_{4}$ The Gain Dec. 275:1625::100:59.09 Sper Cent.

By the very fame Manner of Working you find the Lofs. Quefice 2. If I buy Cambrick at 5 s. 6 d. per Yard, How must I fell it to Gain 59 l. 1 s. 9 ¹/₂ d. per Cent.³ The Converse of the last Method folves this Question.

1. l. s. d. s. d. s. d. Thus Vulg. 100: 159-1-9¹/₄::5-6:8-9 The Price fay, Dec. 100: 159,09 :: ,275: ,4375 Per Tord.

Quefilon 3. If I buy a C. Weight of Tobacco for 41. 13 s. 4 d. and fell it at 11 d. per Pound; What do I Gain or Lofe, and at what per Cent?

First find what a C. Weight will amount to at 11 d. per Pound.

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	l. s. d.	<i>l.</i>
Then from		And from 110
Take	4-13-4	take 100

Remains 0- 9-4 the Gain, at the Rate of 101. per C.

The Converse of this needs no Example.

ľ

Queficer 4. If I buy 5¹ Loads of Wheat for 451. 16 s. 8 d. For how much must I fell it per Quarter, to gain 61. 10 s. by the Bargain?

First {To the given Price = 45–16–8 Add the defigned Gains = 6–10–0 The Sum is = 52–6–8

for which the faid Wheat must be fold. $5\frac{1}{2}$ Load = 27,5 Quarters.

Qrs. l. Q. l. l. s. d. Therefore fay 27,5: 52,3:: I: $1,903 = 1-18-0^{T}$ the Anfwer.

These being the *principal Cases* of this Rule, are sufficient if well understood; and the Operations at large are omitted for the Exercise of the Ingenious.

Exchange.

Both the Name and Eufinefs of Exchange is analogous to that of Barter; only that relates to Goods and Commodities; whereas this is concern'd in Foreign Coins, Weights, and Measures.

Exchange then confifts in finding the true Sum or Value of one Country Coin, &c. equivalent to any given Sum or Value of that of any other Country.

The Par of Exchange is the fixt and Standard Value of Foreign Coins, &c. express'd in Sterling Money of our own; and is that in the Tables. Tis fo called because in Exchange, Par pro Pari, i. e. One equal Value for another, is given.

The Courfe of Exchange is the current Price of E_{λ} change, always unfettled, being fometimes above and fometimes below the Par; according to the various Circumflances and Accidents of Trade and Nations.

The

Decimal Tables of Foreign Coins. 153

The Course of Exchange is published in the Weekly Papers and Pamphlets, which compar'd with the Par in the Tables, it appears whether it be above or below it at any Time.

EXAMPLE.

Courfe of Es	ccha	nge.	The Par	. Differe	me.
Amfterdam Rotterdam Hamburgh Antwerp Madrid	s. 35 35 35 34 35	q . : • • • • • • • • • • • • • • • • • •	s. {33: 33: 33: 33:	$ \begin{array}{c} \mathbf{d}, & \mathbf{s}, \\ 4 \\ 4 \\ 4 \\ \mathbf{-1} \\ \mathbf{-1} \\ \mathbf{-1} \\ \mathbf{-1} \\ 4 \\ \mathbf{-2} \\ \mathbf{-2} \\ \mathbf{-2} \end{array} $	<i>d</i> . 7 7 7 9 0 0 7
E Legborn Genoa Venice	53 48	Pence	$\begin{cases} -54 \\ -54 \\ -52 \end{cases}$		

It is to be observed, that when the Course of Exchange is above the Par, tis a general Indication that our Trade is prosperous, and the Nation on the Gainful Side; as on the contrary, if tis below the Par, the Trade is bad, and the Nation looser.

The Par of Exchange in Coins, Measures, Weights, &c. between Us and Foreigners, are expressed in the following Tables, and which I have reduced to Decimals for more convenient and ready refolving of Queftions in this Rule.

Low Country Coins.

	1. s. d.	Į.
A Stiver — —	0:0:15	10,005
▲ Flemish Shilling (= 6 Stivers)	0:0:75	0,03
A Gilder ($= 20$ Stivers) -	0:2:0	0,1
A Flem. Pound (=33 s. 4 d. Flemish)	1:0:0	1,0
	0:2:3	0,115
A Campen Doller -	0:7:7;	0,13
A Zeland Doller	0:3:0	0,15,
A Lyons Doller	0:4.0	0,2
A Specie Doller	0:5:0	0,25
A Duccatoon	0:6:3?	0,315

X

Ger-

German Coins.

A Rix Doller of the Empire A Gilder of Noremberg				<i>d</i> . 3 ‡ 1	1. 0,2 156 0,354		
French Coins.							
A Denier A Soulz (= 12 Denien) A Livre (= 20 Soulz) A Crown (= 3 Livres)	111	.0 0 0 0	0 0 1 4	0 1 0 1° 6 6	0,0003 1 0,00374 0,075 0,225		

Spanish Coins.

Malvadies 13.7 make		σ	0 0	0,00104
A Rial (=372 Malvadies)	-	0	0-6	0,02812
A Piece of 8 (Rials) Pillar		0	4 6	0,22812
A Piece of 8 Mexico		0	4 6	0,225
A Piece of 8 Peru -		0	4 5	0,22003
A Piece of 8 Seville -				0,225

Portugal Coins.

Rees, 12, 4 of which make Mill Res (= 1000 Rees).	-	σ	σ	I.	0,004 16 0,3354 1 0,062 5
Mill Res (= 1000 Recs).	 `	0	6	8 ‡	0,33541
A Teftoon —		0	ľ	3	0,0625

Italian Coins.

The Livre at Leghorn		0	Ő	9	0,0375
Crown ourrant at Florence		0	5	3	0,2625
Ducat de Banco, at Venice		Q	4	4	0,21
The Courrant Du at -	•	0	3	4	0,29
		ο	5	0	0,25
A St. Mark -		0	2	Ŋ	0,1416
A Palermo Florio -	, and the second second second second second second second second second second second second second second se	٥.	2	6	10,125

Deci

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Decimal Tables of Foreign Long Measures.

London	Foot	1,000	Lyons	- Ell 3,97	16
Paris		1,068	Bologn	- 2,05	56
Amsterdam	-	0,942	Amsterdam	- 2,20	59
Brill		1,103	Antwerp	—· 2,2	73
Antwerp		0,946	Leyden	2,2	60
Dort	-	1,184	Frankford.	- 1,8	
Leyden	-	1,033	Hamburgh	- · 1,9	05
Lorrain		0,958	Leipfick	- 2,2	ðo
Mechlin		0,919	Lubeck	1,9	
Middleburgh		0,991	Noremburg		
Strasburgh	·	0,920	Bavaria	- 0,9	
Brenten		0,964	Vienna	— ` 1 ,0	54
Cologn		0,954	Bononia	⊶ 2,İ	
Frankford ad	Mæn	0,948	Dantzick	- 1,9	•3
Španifh		100,1	Florence	- Brace 1,9	43
Toledo		0,900	Spanifh	- Palm 0,7	'5I
Ròman		0,967	Spanifh	— Vare 3,0	
Bononia	-	1,204	Lisbon	2,7	zo
Mantua		1,569	Gibraltar	- 2,7	160
Venice		1,162	Toledo	- 2,6	85
Dantzick	-	0,944	Naples	- Canna 6,8	86
Copenhagen.		0,965	Genoa	- Palm o,8	BBO
Prague		1,026	Milan	- Calamus 6,	j4 4
Riga		1,831	Parma	- Cubit 1,8	366
Turin		1,062	China	- 1,0	216
Greek		1,007	Cairo		324
			Turkifh		200
			Perfian	- Arala 3,1	197
		lb.		i	īb.
London, The	Pounds	•	London.	The Deneda	
Averdupt		1,00	Averdi		,00
Paris		0,93	Middlebur	•	,98
Lyons -		1,09	Strasburgh		193
Bologn		0,89	Bremen		94
Amfterdam	-	- 0,93	Cologn		39 7
Antwerp		0,98	Frankford		193 193
Leyden		c,96	4 -	ah — o	25
Lorain	-	0,98			,15
Mechlin		0,98	Norembur	eh - c	,-, ,94
ATA9433355		~,70	X 2	. Co	pen
					A

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156 Decimal Tables of the Course of Exchange.

		l. 1		<i>l</i> .
London, the Averdupo	is Pound }	1,00	London, the Pound { Averdupois	1,00
Copenhagen		0 94	Genoa —	1,42
Vienna			Mantua —	1,43
Caffile		0,99	Milan -	1,40
Lisbon		1,06	Parma	1,43
Gibraltar	· ·	1,03	Venice —	1,53
Toledo		1,00	Dantzick -	1,19
Rome		1,23	Prague —	1,06
Bononia		1,27	Cairo —	1,61
Florence		1,23	Constantinople -	0,86
Naples	- ,	1,43		•

Having prefented the Reader with large Tables of the Par of Exchange: I shall next exhibit a Table of the Course of Exchange in Pence, and Shillings and Pence, (into which Foseign Coins are reduced) in Decimal Parts of a Pound Sterling.

Decimal Tables of the Course of Exchange.

P.	7.	P.		P.	1.	<i>P</i> .	
	,001	16	,08	37	,15418	58	,2418
	,002	17	·,07083	38	,1583 -	- 59	,2458 3
3	,0031	18	j075	39	,1625	60	,25
1	,0016	19	,0791\$,16	61	,25416
1	,0026	20	,08,7	41	,17083	62	,2583
4	,0036	21	,0875	42	,175	63	,2625
	,00416	22	,0916	43	,179TØ	64	,26
2	,cc8 <i>7</i>	23 -	,0 95 8;;	44	,183	65	,27083
3	,0125	24	•,τ° •	45	,1875	66	,275
4	,016	25	,10416		,1918	67	,27916
4 5 6	,02084	26	,108 <u>3</u> .	47	,19583	68	,283
	,025	27	,1125	48	,2	69	;2875
17	,02916		,116	49	,20418	70	,2916
8	,03	. 29	,12083		,2083	71	,2958;
9	,0375	30	,125	51	,2125	72	,3
10	,0418	31	,12916		,21\$	73	,3041
11	,0458%		,17	53	,22083	74	,3087
12	,05	33	,1375	54	,225	75	,3125
13	,05418		,1418	55	,22916	76	,310
114	,0583	35	,1458,	56	,23	77	,3208
115	,0625	36	1,15	1 97	1,2375	78	,325

Decimal Tables of the Course of Exchange. 157

IP.		7. 1	P., 7.		P	<i>l, I</i>	1.
Г.	Ŀ	<u></u>	·	1	<u></u>		
79		2918	35,35418		91,37	918	7 ,40418
83			36 ,358,		92,38		28 ,4083
81		375	37,3625		93 ,38		9 ,4125
82			38,38		94,39		
83	122		39,37083		241,32		,418
84	123		20,275		95 ,39	583	1
1 03	•,3	2	20 375	_	961.4		
			1 × .		• •	•	
			· ·		•		
S.1	P.	Flem. P.	Eng. P.		S. P.	Flem. P.	Eng. P.
1-	-		~~~~~				
32	٥	1,6	,625		\ 8	1,73	,576923
ľ	I	1,60416	,623376		· 9	1,7375	,575 5 39
·	2	1,608%	,621761		10	1,7418	,574162
	3	1,6125	,620155		11	1,74587	,972792
	3 4	1,616	,618556	ŀ.	35.0	1,75	,571428
	56	1,62083	,616966		Ĩ	1,75418	,570071
1	6	1,525	,615384		2	1,7583	,568720
4	7	1,62918	,613810		3	1,7625	,567375
	7 8	1,6%	,612244		4	1,78	,566037
	9	1,6375	,610687			1,77083	,564705
Ι,	0	1,641.	:,609137		56	1,775	,563380
	r	1,64583	,007591			1;77918	,562060
		1,65	,600000		78	1,78,	,5607+7
33	71	1,6541,6	,604534		1 g	1,7875	,)05/4/
	I	1,0583	602015		10	1,/0/)	,559440
	2	1,6625	,603015			1,7916	,558139
	3	1,002)	,601503 ,6		II	1,79583	,556844
	4	1,6	,0		36.0	1,8	,5
	5	1,6708,	,5 <i>9</i> 8503		· 1	1,80416	,554272
		1,675	,597014		2	1,808%	,552995
]	7 8	1,67916	·595533		• 3	1,8125	,551724
		1,683	,594059		4	1,818	,550458
ł	9	1,6875	,592592		56	1,82087	,549199
1	0	1,691\$,591133		6	1,825	,547945
	I	1,69583	,589685	l.	78	1,82918	,546697
34	.o	1,7	,588235	i		1.8/	,54
·11	I	1,70418	586797		9	1,8375	,544217
·	2	1,708%	.585365		10	1,8410	,5+2986
	3	1,7125	583941		11	1,84582	,541760
	4	1,718	,582524		37.0	1.85	,540
1.	Ś	1,7208%	,581113		<i>"</i> 1	1,85416	.539325
	4 5 6	1,725	,579710		2	1,858,	.528116
	7	1,72918	,578313		3	1,8525	,536912
Į	<u>/ '</u>	-,/ -,/ -,	,,,,,,,,			-,	1170926

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S. P.	Flem P.	Eng. P.	S . <i>P</i> .	Flem. P.	Eng. P.
45678	1,8# 1,8708 <i>;</i> 1,875 1,8791# 1,88 <i>;</i>	,535714 ,534521 ,53 ,532150 ,530973	9 10 11 38.0	1,8875 1,891ø 1,89583 1,9	,529801 ,528634 ,527472 ,526315

From these Sets of Tables of the Par and Course of Exchanges, (which are more compleat than any I have yet seem in the Common Rooks of Arithmetick.) the ingenious Accomptant will readily call up any Bill of Exchange; or convert the Coins, Weights and Measures of any other Country into the fame of our own. And by comparing the Course with the Pas, may see whether our Nation Gains or Lafes by trading to any Foreign Parts, and in what Proportion.

Queftion 1. Suppose at Venice I would exchange 1751. 121. 6 d. for their Ducats de Banco at 4 s. 4 d per Piece, How many must I have?

2. L L 8. ₹. First, 175-12-6 = 175,625; and 4-4 = ,218. Then ,21\$) 175,625 Ductts 21 175625 The Answer. (759,3 ,195) 158,0625 fere, S 1365 1156 975 1812 1755 1 575

Queficon 2. The Courfe of Exchange at Madrid being now 41² d. per Piece of 8 Mexico, what Number of thole Pieces may I have in exchange for 532,766 l. ?

Per Table the First, of the Course of Exchange 41 3 d. =,174431.

Then ,17442) 533,766 (=3060 Pieces, the Answer.

Queft-

' The Use of Decimals in Exchange.

Question 3. A Bill of Exchange was accepted at Lordon for the Payment of 933,931. for the fame value delivered as Lisbon in Milrees ; Exchange at 5 s. 4 d. per Piece. How many of those Milrees was paid at Liston?

First 64 d. (= 5 s. 4 d.) = ,281.

Then ,26) 933,93 (=3502,25 Milrees, the Anfwer.

Now had these 3502,25 Milress been exchanged at Far (viz. 6 s. 8 1 d.) they would have amounted to 1174,6895 h which is above 240 % more; and confequently there was fo much lofs.

Question 4. In 1421 Pieces of 8 Peru, How many English Pounds Sterling, Exchange at Par?

Multiply -1421 By the Par $= 22083$ 9) 4263		ť	
		Another Way.	
	473 # 11368	(For $1 = 0,22057$	
	2 8 420	20 = 4,41,466 400 = 88,2333	
	2842	1000 = 220,83333	
Answer	<i>1.</i> 313,8041 <i>8</i>	(1421 == 313,80416	

Queftion 5. When the Exchange from Antwerp to Lon. don is at 11. 4 s. 7 d. (= 34 s. 7 d.) Flemish; How many Pounds English at London will ballance 236 l. Flemish at Antwerp ?

Multiply the Tabular Num-ber for English Pounds },57831, Sa-By the given Number - 236 The Product is the Asswer 1.136,4819, Sa. Proceed thus,

Queffior 6. What Number of Flemis Pounds will be equivalent to 400 L Starling, Exchange at 11. 12 s. 6 d. (=333.6d.)

Multiply the Pound Flemish 1,675 By the Number of Pounds Sterling 400 The Product is the Answer = 670,000 Pounds Storl.

Question 7. A Dutch Man fella 2350 Flemish Ells of Holland to an English Man, a Spaniard, a Venetian, an Italian, and

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and a Portuguese; who are to have each a like Quantity; Quere how much in their own Country Measure?

First 2050 Flemish Ells are equal to 1230 Ells English, equal to 4612,5 Feet, which divided by 5 quotes 922,5 Feet each.

Then by the Table of Measure 922,5 Feet are e- qual to	(307,5 793,89 1228,36 482,2 225,4*	Yards for the Briton. Feet for the Venetian. Palms for the Spaniard. Braces for the Italian. Vares for the Portuguele.	} } An£ }
qual to	1 335,45	Vares for the Portuguese.	j

Quefiion 8. What Number of Pounds Averdupois at Vienna will Equiponderate 270 Pounds Averdupois Weight at London?

Divide 270 by ,83. the Quotient 325,3 l. is the Answer.

But if twas required to know what Number of Pounds Averdupois Weight at London would equal any given Number at any other place, then you must multiply by the Tabular Number.

Alligation, or Rule of Composition.

Alligation (fo called of the Latin Word Alligo, to bind or tie tegether; because the vulgar Way is to tie or connest tegether the Numbers concern'd in the Work,) is a Rule for Compounding or Mixing several Ingredients of different Sorts together, in any Manner or Proportion. And is divided into Alligation, Medial and Alternate.

Aligation Medial is that by which the Mean Rate or Price of any Mixture is found when the particular Quantities, and their Prices, are given; and it is perform'd by this

Rule,

Multiply each Quantity by its Price; then fag, As the Sum of all the Quantities, is to the Sum of the faid Products, fo is any Part of the Mixture, to the Mean Price of of that Part.

Question 1. A Tobacconist would mix 20 lb. of Tobacco at 9 d. the Pound with 60 lb. at 14 d. per lb. with 40 lb. at 18 d. per lb. and with 12 1 lb. at 2 s. per lb. Quere what a Pound of such a Mixture is worth?

Firft

ł

~	lb. Rate.	P	roducts.	
. 20	X .0275 pro	duceth	0,75	•
Firft, 260	×,0583 pro	duceth —	3,5	•
	×,0583 pro ×,075 pro	duceth —	3,0	•
C12	2,75 X,1 pro	duceth	1,275	•
The Sum 132	2,75 of the Quan.	The Sum	8,525 the H	rod.
	16. 1.			. :
Then fay,	As 132,75 : 8,52	25::1:0642	1	· .
. 132,7	75) 8,5250 (,064:	$2 = 1 s. 3 \frac{1}{4}a.$	per 16. An	iwer.
	79650			···· .
•	• 56000 - 11 -	$(\mathcal{O}_{\mathcal{O}}) = \mathcal{O}_{\mathcal{O}}$		·•
•	53100	1 1 1 LA	ttia – s	13.12
	• 29000		· • • •	· · ·
• •	20550		· .	1 L
• • • • • •	2450			- • ,••
per oz. 8.1 9 oz. at 4 ¹ . gether, Quer	. A Gold (mith oz. at 4.1, 5 s.; 1-3 s. 4.4. Supp e what an Gunc oz. 1.	3 on at 41. of these all m e of that Mix I.	6 s. 8 d.	and to-
per oz. 8 1 9 oz. at 4 l.	oz. at 4.1, 5.4, 13.5. 4.4. Supp what an Game oz. 1. 12 X 4, pro 83 X 4,25 pro 3 X 4,3 pro	3 oz. at 41. of thefe all m e of that Mix l.	6 s. 8 d. elted down ture would	and to- d be
per oz. 8,3 9 oz. at 4 ¹ , gether, Guer worth?	oz. at 41, 5 5.; 13 5. 44. Supp what an Guna oz. 1. 12 X 4; pro 3 X 4,25 pro 3 X 4,3 pro 9 X 4,4 pro	3 95% at 41. of the all m e of that Min cluceth 348 oduceth 35,27 duceth 13	6 s. 8 d. elted down ture would	a to- d be
per oz. 8, 1 9 oz. at 4 ¹ , gether, <i>Guer</i> worth? First, <i>S</i> The Sam 3	oz. at 41, 5 s.; 13 s. 44. Supple what an Guna oz. 1. 12 X 4. pro 83 X 4,25 pro 3 X 4,3 pro 9 X 4,4 pro 12,3 Th	3 per et 4/. ofe there all m e of that Mix duceth 48 oduceth 35,27 oduceth 42 e Sum F38,27	6 s. 8 d. elted down ture would 5	and a to- d be
per oz. 8, 1 9 oz. at 4 ¹ , gether, Guer worth? First, S The Sam 3 Then fay,	oz. at 41, 54.; 13.5.44. Supple what an Gurac oz. 1. 12 X 4; pro 3 X 4,25 pro 3 X 4,3 pro 9 X 4,4 pro 233 The As 32,30z.:	3 pe_{c} at $4!$. of the the fe all m e of that Mix duceth 48 duceth 35,27 duceth 42 e Sum 538,27 8,275 7 :: : 1 o	6 s. 8 d. elted down ture would 5 5 of the l	and a to- d be
per oz. 8, 1 9 oz. at 4 l, gether, Guer worth ? First, S The Sam 3 Then fay,	oz. at 41, 5 s.; 13 s. 44. Supple what an Guna oz. 1. 12 X 4. pro 83 X 4,25 pro 3 X 4,3 pro 9 X 4,4 pro 12,3 Th	3 pe_{c} at $4!$. of the the fe all m e of that Mix duceth 48 duceth 35,27 duceth 42 e Sum 538,27 8,275 7 :: : 1 o	6 s. 8 d. elted down ture would 5 5 of the l	and a to- d be
per oz. 8, 1 9 oz. at 4 l, gether, Guer worth ? First, S The Sam 3 Then fay,	oz. at 41, 5 6.; 13 5. 44. Supple what an Guna oz. 1. 12 X 4. pro 3 X 4.3 pro 9 X 4.3 pro 9 X 4.4 pro 1233 The As 32,3 oz. : 13 138,275 (4,2805) 1292	3 pe_{c} at $4!$. of the the fe all m e of that Mix duceth 48 duceth 35,27 duceth 42 e Sum 538,27 8,275 7 :: : 1 o	6 s. 8 d. elted down ture would 5 5 of the l	and a to- d be
per oz. 8, 1 9 oz. at 4 l, gether, Guer worth ? First, S The Sam 3 Then fay,	oz. at 41, 54.; 13 5. 44. Supple what an Guna oz. 1. 12 X 4. pro 83 X 4,25 pro 3 X 4,3 pro 9 X 4,4 pro 9 X 4,4 pro 12,3 Th As 32,3 oz. : 13 138,275 (4,2805)	3 pe_{c} at $4!$. of the the fe all m e of that Mix duceth 48 duceth 35,27 duceth 42 e Sum 538,27 8,275 7 :: : 1 o	6 s. 8 d. elted down ture would 5 5 of the l	and a to- d be
per oz. 8, 1 9 oz. at 4 l, gether, Guer worth ? First, S The Sam 3 Then fay,	oz. at at $5.5.4$ $i3.5.4$ at Supple $what$ an $Guman oz. l. 12 X.4.5 processor 3.5.4.5 at processor 3.5.4.5 processor at 3.5.4.5 processor processor 3.5.4.5 processor processor 3.5.4.5 processor processor 3.5.4.5 processor processor 3.5.4.5.5 processor processor 3.5.7.5 (4.280.5) 1292 2.90.7 646 646 $	3 pe_{c} at $4!$. of the the fe all m e of that Mix duceth 48 duceth 35,27 duceth 42 e Sum 538,27 8,275 7 :: : 1 o	6 s. 8 d. elted down ture would 5 5 of the l	and a to- d be
per oz. 8, 1 9 oz. at 4 l, gether, Guer worth ? First, S The Sam 3 Then fay,	oz. at $41, 54.;$ 13 s. $44.$ Supper what an Gauge oz. 1. 12 X 4. proper what an Gauge 03 X 4.3 proper what an Gauge 3 X 4.3 proper what an Gauge 9 X 4.4 proper what an Gauge 12,3 The As 32,3 oz. : 12 138,275 (4.2805) 1292 907 646 2615	3 pe_{c} at $4!$. of the the fe all m e of that Mix duceth 48 duceth 35,27 duceth 42 e Sum 538,27 8,275 7 :: : 1 o	6 s. 8 d. elted down ture would 5 5 of the l	and a to- d be
per oz. 8, 1 9 oz. at 4 l, gether, Guer worth ? First, S The Sam 3 Then fay,	oz. at $4l, 54.;$ 13 s. $44.$ Supper what an Gauge oz. l. 12 X 4; proper what an Gauge oz. l. 12 X 4; proper what an Gauge 3 X 4,32 proper state 9 X 4,4 proper state 9 X 4,4 proper state 138,275 (4,2805) 1292 907 646 2615 2584	3 pe_{c} at $4!$. of the the fe all m e of that Mix duceth 48 duceth 35,27 duceth 42 e Sum 538,27 8,275 7 :: : 1 o	6 s. 8 d. elted down ture would 5 5 of the l	and a to- d be
per oz. 8, 1 9 oz. at 4 ¹ , gether, Guer worth? First, S The Sam 3 Then fay,	oz. at $41, 54.;$ 13 s. $44.$ Supp what an Guna oz. 1. 12 X 4. pro 3 X 4,32 pro 9 X 4,4 pro 9 X 4,4 pro 12,3 Th As 32,3 oz. : 13 138,275 (4,2805) 1292 : 907 646 2615 2584 : 3100	3 pe_{c} at $4!$. of the the fe all m e of that Mix duceth 48 duceth 35,27 duceth 42 e Sum 538,27 8,275 7 :: : 1 o	6 s. 8 d. elted down ture would 5 5 of the l	and a to- d be
per oz. 8, 1 9 oz. at 4 ¹ , gether, Guer worth? First, S The Sam 3 Then fay,	oz. at $4l, 54.;$ 13 s. 44. Supp what an Gum oz. l. 12 X 4; pro 83 X 4,25 pro 3 X 4,3 pro 9 X 4,4 pro 2,3 Th As 32,3 oz. : 13 138,275 (4,2805 1292	3 0 41 41. of the the call m constraints of that Mix but the constraints of that Mix but the constraints of the constraints but the constraints of the constraints of the constraints but the constraints of the constraints of the constraints but the constraints of t	6 s. 8 d. elted down ture would 5 5 of the l	and be A be A be A be A be A be A be A be A

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Alligation Alternate is that by which the particular Quantities of every Ingredient in any Mixture are found; when the particular Rates of every one of the Ingredients; and the Mean Rates are given.

This is (as it were) the Converse of the former, and admits of three Cales.

The particular Rates and the Mean Rate be-Cafe 1, ing given, to find the Quantity of each Ingredient for the Mixture proposed.

Queftion 1. A Vintuer would make a Mixture of Malaga at 7 s. 6 d. per Gallon ; with Canary at 6 s. 9 d. per Gallon ; Sherry at 5 s. per Gallon, and White Wine at 4s. 3 d. per Gallon: What Quantity of each Sort must be take, that the Whole Measure may be fold for 5 s. 10 d. per Gallon?

Note, In all Questions of this Nature, where two or four Things are mixt together, when one balf of the Prices are Greater, and the other balf leffer than the Mean Rate, you must fet a greater and lesser Price above, and the fame below the mean Price; then take the Difference between the mean Rate and the particular Rates, and place them alternately, and they will be the Quantities requir'd.

> Rates ' Differences'.

(7,5 Malaga 1,583 Gal. of Malaga. 4,25 White \$ 1,8 Gal. of White. 5 Sherry 20,918 Gal. of Sherry. 6,75 Canary 50,8% Gal. of Canary. Mean Rate = 5,83

The Sum of those Differences is = 5,0Gallons the whole Mixture.

Note, The-Differences are not only the Quantities, which answer'the Question, but any other Numbers, in the fame Proportion as they are, will answer the Question as well.

ForAll multiplied by	1,583 1,6 0,918 0,83
Produce the Proportionals These multiplied by	4,75 5 2,75 2,5
Produce these whole Num- bers in the fame Ratio, and fo on In infinitum. In Case one of the Given be {Greater} and all the re Rate-	19. 20. 11. 10. Rates (when more than two) $\{ Letter \}$ than the mean
Rate-	TGreater 5 min the mouse

The Use of Decimals in Alligation. 163 Then the mean Rate, particular Rates, and Differences mult fland as in the following Examples.

P. Mean Rate 20 {2 2	R. Differe 18 4+2 22 2 24 2	SMean Ro		$\left.\begin{array}{c} R. Differ. \\ 4 \\ 4 \\ 4 \\ 4 \\ 6+2 \end{array}\right\}$
$\sum_{n=1}^{2}$	Difference 1+5+1 2 2 2	$\begin{cases} s. \\ 3 \\ 0r_{4^{\circ}} \end{cases}$	$ \begin{array}{c} R. Di \\ 10 \\ 8 \\ 25 \\ 36 \\ 48 \\ 36 \\ 48 \\ 30 \end{array} $	fferences. } 0+15+49

The Method is the fame for any other given Rates, or Prices.

Cafe 2. When the Particular Rates, the Mean Rate, and the Quantity of one Ingredient is given; to find the Quantity of all the reft of the Ingredients.

This is call'd *Aligntion Partial*, because a *Part* of the Mix'd Ingredients only are known.

In this Cafe you must fet down the mean Rate, the particular Rates, and their Differences just as before; then fay, Rule.

As the Difference opposite to the known Quantity, is to the known given Quantity; so is any other Difference, to the Quantity of its opposite Name.

Queftion 2. How much Malaga at 7 s. 6 d.; Sherry at 5 s.; White Wine at 4 s. 3 d. the Gallon, must be mixt with eighteen Gallons of Canary at 9 s. 9 d. per Gallon, that the Whole may be fold for 5 s. 10 d. per Gallon?

Rates. Mean Rate 5,83 Mean Rate 5,83 Mean Rate 5,83 Rates. 7,5 Sherry 5 1,8 6,75 Canary 1,583 4,25 White 5 0,918

Then, As 1,587:18:: 0,87 to the Gallons of Malaga. 1,8 to the Gallons of Sherry. 0,918 to the Gallons of W. Wine.

I leave the Work to exercise the Learner.

Y 2

Cafe

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Cafe 3. The particular Rates, the mean Rate, and the Sum of all the Quantities of the Ingredients given; hence to find the particular Quantities of the Mixture.

This is call'd *Alligation Total*; because, the whole Quantity of the Mixture is given.

¹ It is thus perform'd; fet down the mean Rate, the partienlar Rates; and find their Differences as before. Then fay,

Rule. As the Sum of all the Differences, is to the Sum of all the Quantities; fo is each particular Difference, to its particular Quantity.

Queflion 3. Suppose it required to mix Malaga at 7 s. 6 d. with Canary at 6 s. 9 d. Sherry at 5 s, and White Wine at 4 s. 3 d. per Gallon; and the whole Quantity to be $84\frac{1}{3}$ Gallons, and to be fold at 5 s. 10 d. per Gallon; Quere the Quantity of each Sort for the Mixture?

Mean Rate	5,83 2	7,5 5 6,75 4 ,25	Malaga Sberry Canary White	$ \begin{cases} 0.83 \\ 1.6 \\ 1.583 \\ 0.916 \end{cases} $ Differences.
			•	5 = The Sum.
	••••	•		34 7
•	C .11		V 0,83	7 to the Quan-) Malaga.

Gallons. Then, As 5: 84,625:: 1,583 for of Sherry. 1,583 for of Sherry. 1,583 for of Sherry. 1,583 for of Sherry. 1,683 for othe Quan-Sherry. 1,693 for oth

Note, The Work of these, and such like Proportions, may be very much thornened, and easierly perform'd by a common Multiplicator as in Fellowship.

Now because Alligation alternate answers not Questions compleatly, that is, does not give all the Answers such Questions are capable of; and so perhaps not always those which best fuit the occasion; I thall shew (from Mr. Ward) how this Imperfection of common Arithmetick is supplied by Algebra, and all the possible Answers to any Questions may be clearly and easily discovered.

Question 4. A Tobacconist hath three Sorts of Tobacco, viz. one of 2 s. 8 d. per Pound; another of 20 d. per Pound; a third fort of 16 d. per Pound; of these he would make a Mixture to contain 55 Pound that may be fold for 22 d. per Pound; How much of each Sort may he take?

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Té:

$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	4e=336-16a e= 84- 4a	nified by a must be lefs than 21, and (by the 8th) Step greater than g_{1}^{*} . That is a
3-71 8.	y = 3a - 28	may be any Number between 21 and $9\frac{1}{5}$.

If there be more than three Quantities concerned in the Queficion, the Work will be more large; becaufe the Limits of all the Quantities above two, must be found.

Quefition 5. Suppose it were required to mix four Sorts of Wine together; viz. one worth 7 s. 4 d. per Gallon; a fea cond worth 4 s. 7 d. a third worth 3 s. 8 d. and a fourth worth 2 s. 9 d. per Gallon. How much of each Sort must be taken to make a Mixture of 63 Gallons, to be fold for 5 s. 6 d. per Gallon, without Lofs?

s. d. d.	•
c = that Quantity worth 7 4 = 88	;
e = that worth - 4 7 = 55	
First let $\leq y =$ that worth -3 $8 = 44$	
u = that worth $-29 = 33$	
First let $\begin{cases} a = \text{that Quantity worth 7} 4 = 88\\ e = \text{that worth} - 4 7 = 55\\ y = \text{that worth} - 3 8 = 44\\ u = \text{that worth} - 2 9 = 33\\ \text{the mean Rate} - 5 6 = 66 \end{cases}$	
Then 1.1 $a + e + y + u = 63$	
And $a 88a + 55a + 44a + 22a - 4358$	
And 2. $88a + 55e + 44y + 33u = 4158$. 1-a 3. $e + y + u = 63 - a$	
1-a = 3. $a + y + u = 03 - a$	
2-88a 4.155e + 44y $33u = 4158 - 68a$	
3×33 5. $33^{\mu} + 33^{\mu} + 33^{\mu} = 2079 - 33^{\mu}$	
$\begin{array}{c} 2-88a \\ 3\times 33 \\ 4-5 \end{array} \begin{array}{c} 4 \\ 5 \\ 3^{2} \\ 4-5 \end{array} \begin{array}{c} 5 \\ 3^{2} \\ 4-5 \end{array} \begin{array}{c} +31y \\ 3^{2} \\ 4-5 \end{array} \begin{array}{c} +31y \\ 3^{2} \\ 4-5 \end{array} \begin{array}{c} +31y \\ 3^{2} \\ 4-5 \end{array} \begin{array}{c} +31y \\ 3^{2} \\ 4-5 \end{array} \begin{array}{c} -2079 \\ 55a \end{array}$	
6 - 11 7. 2e + g = 189 - 5a	
3×55 8. 550 + 55 9 + 552 == 3465 - 554	
8-4 9. 119 + 22 ⁴ = 33 ⁴ - 93	
9-11 10. $y + 2u = 3a - 63$ Suppose 11. $a = 22$. Then 5a 11c, and 3a =	
Suppose 11. $a = 22$. I nen 5a · 11C, and $3a =$:0)
Fer 7th 12. $2e + y = 189 - 54 = 79$	_
a a second a second a second a second a second a second a second a second a second a second a second a second a	12-20
	, "Here -

166 The Use of Decimals in Position. 12-2e 13 y = 79 - 2ePer 3d. 14 e + y + u = 63 - a = 4114-e 15 y + u = 41 - e15-13 16 u = e - 38

From the feventh and tenth Steps it appears, that the Quantity denoted by a, must be lefs than 37⁴, and greater than 21 Gallons; whence 16 answer flow from the Limits of a only. Then if a be put = 22, by the thirteenth and fixteenth Steps it appears e = 39. y = 1, and u = 1. And thus proceeding with each fingle value of a, above 120 Answers may be found to this Question in whole Numbers; in Fractions, infinite.

Polition, or Rule of Falle.

This Rule of Position, or rather Supposition, is to call'd, because we suppose or make a Position of some uncertain Numbers, in order that by reasoning from them we may gain the true Number sought; and because those Positions are altogether at random or adventure, the Rule is also call'd False.

The Use of this Rule, before the common Knowledge of Agebra, was much more confiderable than fince; because that Art supplies Theorems for resolving all kind of Questions in this Rule in a better and more curious a manner than here; Yea fome of the best Pieces of Arithmetick have intirely discarded it, and others post-pone it, as obsolve and of little use, fince Algebra.

Quefiions in this are mostly perform'd by one or two Suppositions; if by one, the Rule is faid to be of Single Position; if two Suppositions are necessary, 'tis called Double Position.

Single Polition.

Queficion 1. Three Merchants A, B, C trade in Company, and gain 100 l. of which A had a certain Part, B had twice as much, and C had thrice as much as B; How much had each Man?

Suppose A had 4l, then B must have 8l, and C would have 24l, which together make 36l, but shou'd have been an 100l.

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There-

The Use of Decimals in Position.

Therefore Reafon by Proportion 1. 1. 1. Thus, As $\frac{1}{26}$: $\frac{1}{100}$:: $\begin{cases} 4 : 11, x = A \\ 8 : 22, x = B \\ 24 : 66, 8 = C \end{cases}$

Their several Parts added make - 100 for Proof.

Queftion 2, A Schoolmafter being asked how many Scholars he had; answer'd, if I had as many, and $\frac{1}{4}$ as many, and $\frac{1}{4}$ as many, I should have 99. How many had he?

Suppose he had 40; Then 40 + 40 + 20 + 50 = 150, but it should have been but 99. Therefore fay

As 110 : 40 :: 99 : 36 Scholars, the Answer.

Queftion 3. Three Men A, B, C buy a Ship for 310 l. 15 s. of which A paid an unknown Sum; B paid 2¹/₂ as much: and C 3¹/₂ as much : How much did each Man pay?

Suppose A paid 48l, then B paid $48 \times 2,5 = 120l$, and C must pay $48 \times 3,3 = 160l$. But 48 + 120 + 160= 328 infread of 310,75l. Say therefore, As 328 : 48 :: 310,75 : 45,4756, Sc.

Then A B C	paid	45,4756 113,689 151,5853
Proo	f is the Sum	 310,75

Double Polition.

In the Double Rule, two Suppositions are used, because here the Numbers cannot be parted to find the Answer by Proportion as before.

Therefore when we make two Suppofitions, and mils in both, observe the Nature of the Errours, whether they be Greater or Leffer than the Number proposed; and accordingly mark them with the Signs More or Lefs, viz. +, -; and place them precisely against their proper Suppositions; then observe the general

Rule,

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Rule,

Viz. As the Difference of the Errours if alike, (or their Sum if unlike) is to the Difference of the Suppositions; fo is either of the Errours, to a fourth Number.

The family Number add to, or fubfinatt from, the Suppofrien opposite tait; and you have the Number fought.

Queficer 1. Admit three Merchants build a Ship which coft 1360 Pounds. A pays a certain Part unknown; B paid $2\frac{1}{2}$ as much, wanting 15,5 Å and C paid as much as both \mathcal{A} ; and B, and 75,25 l. over; How much did each Man pay?

First, Suppose April 200 *l*. then *B* must have paid 484,5 l. and *C* paid 759,75 *l*. But those three Sums, viz. 200 + 484,5 + 759,75 = 1444,251 which is more than 1360 by 84,25l. Wherefore the first Errour is -+ 84,25l.

Secondly, Suppose A paid 180 l. then B paid 434,5 l. and C paid 689,75 l. But 180 + 434,5 + 689,75 = 1304,25 l. which is too little by 35,75 l. therefore the Suppositions and their Errours will fand thus,

The First Supposition 200, + 84,25 Errour. The Second Supposition 180, -55,75 Errour. The Difference of Supposition 200 140=Sum of Errours. Then by the General Rule, fay, As, $\begin{cases} 140 : 20 :: 55,75 : 7,964 & & \\ 140 : 20 :: 84,25 : 12,035 & & \\ \end{cases}$

Then, $\begin{cases} 200 - 12,035 = \\ 180 + 7,964 = \end{cases}$ 187,964 = A's Part. Then B muft have paid - 454,410 = B's Part. And C muft have paid - 717,624 = C's Part. The Sum of which is = 1360 for Proof.

Note, When the Errours are equal and have unlike Signs; balf the Sum of the Suppositions, is the Number fought.

Ex-

Extraction of Roots.

The extream Use of Decimals in all kinds of Extractions is fufficiently known to all verfed in Arithmetical Know. ledge; and its abfolute Necessity in some Parts; of Arithme-tick, and its Excellency beyond even Logarithms themselves in others, is also as well known.

I would know what is the Square Root of 161,29?

Thus 161,29 (12,7 = the Anfwer. 22) 4. <u>44</u> 247) 1729 1729 22) 61

What is the Square Root of 3477? In fuch Cafes as this, you must add twice as many Cyphers to the given Number, as you defign to have Decimal Places in the Root of the above Number to three Places of Decimals.

Then	3477,000000 (58,881 the Root req	pir'd.
′ ; 108)	977 864	••	
116 8)	10300 9344		,
J1768)	•• 95600 94144		
117761) · 145600 J17761		:

Z

Regul-

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Required the Square Rost of 2; to 6 Places of Decimals.

2,00000	2000000 (1.44 4213 the Root required.
84) 100 196	
281) · · 400	
2824) 11900 11298	
2828) ··· 604 565 · 38 28	Having here got 3 Places of the 6, I work by the contrasted way of Division, and gain the other 3 as truly as if prought at large.
10 8 (2)	
What is the Squar	e Root of 4489 ?
,4489	(,67 the Root requir'd.

What is the Square Root of ,00576?

What

The Ufe of Decimals in Extractions. 171

What is the Square Rebt of codoyday 2:

,00005625 (,0075 = the Root fought. 49 145) 725 725

To Extract the Roots of Single Repetends.

What is the Square Root of , x or that y infinitely repeated ?

٦ر	, , , , 1111111 9 (Br. (13333	Sr.	the Square	Root
63)			, <i>'</i>		
663)	• 22 } 1 1989		•	, <u>-</u> •	
6663)	22211 199 89	Ş	9 4	downward	
•	2222	<u>1</u> 2	nd	İnfinitum.	

What is the Square Root of 344,4 &c.? 41,4444 &c. (8,66 &c. the Root. 36 1326) 844 7956 1326) 8844 7956 88844 Ad Infinitum.

If the Root does not repeat in the first Figure, 'twill be very uncertain when it will repeat.

Note, Only these two Digits 1 and 4 (of all the Nine) when infinitely repeated; have their Roots, pure fingle Repetends.

Z 2

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To Extract the Square Root of Compound Repetends.

What is the Square Root of 198,85?

Thus, 198,88 (14,030568658 the Root.

24)	•96

2

	568 409
2806 05) ·	1595685 1403025
280611	168366
	· 24294 22448
i.	• 1846 1683
	; 162 140

In this Manner the skilful Artift may proceed and gain the Root of any Repetend to what Number of Places he pleafeth. I omit the Extradion of the Cube Root here; becaufe I shall have occasion to shew the Method and Rationale of that, and of the Square Root. both, when I come to shew the Use of Decimals in Algebra. **1** N 1 2 1 1 2 1 2 1 2 1 2 **1 7 2**

CHAP. IX.

The Use of DECIMALS in the Business of Interest both Single and Compound; Of Annuities, Pensions, Cr. their Value in Present Worth, and in Arrears; Of Rebate or Discount; Of Free-hold or Real Estates.

I NTEREST is a *fmall Sum of Money* paid for the Use of any greater Sum, according to any Rate agreed on; as 5 l. per 100 l. Scc. for a Year; and it is either Simple or Compound.

Simple Interest is that which arises only from the Principal or Sum of Money lent; and both Interest, and Principal are always the fame as at first.

Compound Interest is that which ariseth from the Principal and its Simple Interest (when due and forborn) reckoned together as a New Sum, to that both Principal and Interest here are always increasing.

Annuities, Pensions; Salaries, &c. are Rents, Profits, and Payments made Yearly, or Half Yearly, &c. and they are faid to be in Arrears, when they are due and unpaid for any Number of Payments.

Rebate or Discount is an Abatement of Part of a Sum of Money due fometime hence, in Confideration of prompt or present Payment of the Remainder; and this is done at any Rate of Interest.

In exemplifying the wonderful Use of Decimals in the Affair of Interest, Sec. I need only thew the Reader the Solutions of those admirable Theorems in Numbers at large, which Mr. Ward (in his Mathematician's Guide) has with great Invention contrivid from the following Data, and Method of Reasoning from thence.

In

In Single Intereft. $S \stackrel{P}{=} Any + incipal or Sam put to Interest.$ R = The Ratio of the Rate per Cent. per Annum.2. T = The Time of the Principal & Intereft. In Annatives, at Shuple Interest U = The Annuity, Penfion] or Kindly Ront, ac. T = Time of Forbearante, or being Unpaid. R = The Raise of Interest, as before A = The Amount of the Aumuity and its Interest, - 1 = * By way of Substitution, in Arrears. Ŕ 1..... I. i... $\frac{2}{R} - \frac{2P}{U} + 1 = \kappa$ By Subfitution also, in pref. worth. P = The Present Worth of Annuisian dec.

In Compound Interest thele Characters fignify the fame Things as here; only T here, is there wrote in a fmall Letter (1) and denotes the Power of R; or is the Index of the Power to which R is to be involved; and R = Amount of 11, and its Intereft one Year. From the above Data, he makes the following Proportions. 11. . . is

Simple Interest,

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The Ratio of the Rate of Interest fignified by R is thus found (for us only the Interest of 1% for 7 Year.)

1. Raib. t. **h.** r - 200-2-41 - 2-212 2 2 ,041 🕮 R 20 41 per Cent. 100:4,5 :: 1:,045 = R at 4 : per Cent. 100:5 :: 1:,05 = R at 5 for Gent. 100: 5,5 :: 1 : ,055 = R at 5 : per Gent. 100: 0 :: 1 : 5 : ,06 = R at 6 per Cent.

And & I. 2. 3. 4. 5. 6. 8. = Hars. { R. 2R. 2R. 4. 5. 6. 6. 2 Interef. Honce 'tis evident the Simple Interest of Th is a Scries' of Terms in Arithmested Progreffion increating. (R = The first Term, and also the Common Differ.

Wherein $\begin{cases} T = 1 \text{ ne symmetry} \\ TR = The last Term of the Series. \end{cases}$ T =The Number of all the Terms.

Then

1. Int ... Then, As 1 : TR :: P : TRP - Interest of P. But the Principal and its Interest sched is equal to the Amount. Whence this General Theorem,

TRP=P=4

Annuities, Simple Intereft.

Here U = the Yearly Rent, and R = the Ratio of interest. Then 2U = the Rent, and RU = the Interest for the second Year; and thus the following Progressions for five Years.

Hence 'tis plain, that RU+2RU+3RU+4RU+SU=4. The Sum of all the Rents and their Interests being forborn five Years. From whence it follows

That RU+2RU+3RU+4RU=A-TU. For here T=5. Divide all by U. Then R+2 R+3 R+4R= 4-TU Then by Subflitution, put R+2R+3R+4R=Z. Then $1+e+3+4\pm\frac{2}{R}$ Now the first and last Terms

of the Prograffion are 144=3=T. Therefore T-1 × T = Sum of all the Terms.

Now $\frac{TT-T}{2} = \frac{Z}{K}$ Hence $\frac{TTR-TR}{2} = Z$. Confequently $\frac{TTR - TR}{2} = \frac{A - TU}{U}$ The General Theorem

for Annuities in Arcears.

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But because P = the Prefent Worth, is not in the left General Theorem. That will answer no Questions relating thereto; Wherefore a New one must be contravid : Now because A denotes the fame Thing, viz. the Amount, in both the laft General Theorems; and because any two Quantities, equal to one and the fame thing, are equal to one another. And PTR + P = A in the first General Theorem; And $\frac{TTRU - TRV + 2TU}{2} = 4 \text{ in the latter General Theor.}$

Tacre-

The UTe of Decimals is Interell. 176

Therefore $PTR + P = \frac{TTRU - TRU + 2TU}{T}$ is the General Theorem for Questions about the prefent Worth or Purchafing of Annuities.

Compound Interest.

The Proportion for finding R the Ratio of the Rate of Compound Interest, (which is only the Amount of 1 1. and its Interest for one Year,) is This

L: As $\begin{cases} 100 : 105 :: 1 : 1,05 = R at 5 per Cent. \\ 100 : 106 :: 1 : 1,06 = R at 6 per Cent, &cc. \end{cases}$

But as one Pound, is to the Amount of one Pound, at one Year's End; fo is that Amount, to the Amount of one Pound at two Year's End; and fo on continually.

1 That is, 1 : R : : R : RR : : RR : RR : : R3 : R4 :: R4 :: R4 :: R1:: &c.

. . . .

Then $\begin{cases} 1 \cdot 2 \cdot 3 \cdot 4 \cdot 5 \cdot = Y \text{ ears.} \\ R. R^3 \cdot R^3 \cdot R^4 \cdot R^3 \cdot = T \text{ the Amount of } 1 \ 1 \ at \end{cases}$ any Rate.

Hence 'tis evident the Amount proceeds in a Geometrical Proportion, wherein the Time (= t), or Number of Years. is always equal to, or the fame with, the Index of the Power of the last and bigbest Term of the Series; viz. Rs, or Rt.

But, as one Pound : is to the Amount of one Pound for any given Time :: to is any proposed Principal or Sum : to its Amount for the fame Time.

That is, As 1 : Rt :: P : PRt.

But PR: = A The General Theorem.

Annuities. Compound Interest.

 $rac{R}{rac{R}} = One Pound and its Intereft for one Year, as before.$ U = The first Year's Rent without Interest.

Then RU = The Amount of the first Year's Rent, and its Intereft.

And hence is form'd the following Progression of Amounts in continued Geometrical Proportion.

Thus $\begin{cases} 1. 2. 3. 4. 5. & cc. The Years. \\ U+UR+UR^3+UR^3+UR^4, & cc. The Amounts. \end{cases}$ Hence

The Use of Decimals in Interest. _ 177 .

Hence $U + UR + UR^2 + UR^3 + UR^4 = A$ The Amount of any Yearly Rent or Annuity forborn five Years.

Now the last Term in the above Series is $UR^4 = UR^{1-1}$. Therefore $A - UR^{1-1} =$ The Sum of all the Antecedents. And A - U = The Sum of all the Confequents in the Series.

So that it will be, $U: RU: : A - UR^{i-1} : A - U$. Therefore $AU - UU = RUA - UUR^{i}$. Divide all by U. Then $A - U = RA - UR^{i}$. The General Theorem.

For the prefent Worth, we must proceed as in Simple Intereft in this Cafe, to gain an Equation or general Theorem, wherein shall be P.

The Theorem for Intereft is $PR^{t} = A$. And in the laft Theorem $\frac{UR^{t} - U}{R - 1} = A$. Confequently, $PR^{t} = \frac{UR^{t} - U}{R - 1}$ The General Theorem.

Free-hold Estates, Compound - Interest

Free-bold or Real Estates are supposed to be purchased for ever. And the Computation of the Value of such Estates is grounded on a Series of Geometrical Proportionals decreasing ad Infinitum.

Let P, U, R, denote the fame as before; then the Series will be $\frac{U}{R} \cdot \frac{U}{R^2} \cdot \frac{U}{R^3} \cdot \frac{U}{R^4} \cdot \frac{U}{R_5} (=P)$ &c. till the laft Term be = 0. Then will P = 0 = Sum of all the Antecedents; and $P = -\frac{U}{R} = Sum$ of all the Confequents.

Therefore, as $\frac{U}{R}: \frac{U}{K^*}:: P: P - \frac{U}{R}$ which gives P R- U = P. The general Theorem.

Theorems Refolving all Questions concerning Simple : Interest,

Given P, R, T; To find A? Theorem 1. TRP + P = A. Given T, R, A; To find P? Theorem 2. $\left\{\frac{A}{TR+1} = P\right\}$.

Given

178 The Use of Decimals in Interest. Given A, P, T; To find R? Theorem 3. $\left\{\frac{A-P}{TP}=R\right\}$. Given P, R, A; To find T? Theorem 4. $\left\{\frac{A-P}{RP}=T\right\}$.

Queffion 1. What will 256L 105. Amount to in three Years, one Quarter, two Months, and eighteen Days, at 64. per Cent. per Ann.

Here is given $\begin{cases} P = 256,5 \\ R = 0,06 \\ T = 3,46598 \end{cases}$ To find *A*, per The. 1.

Multiply - 3,46598 = TBy - 0,06 = RProduct - 0,2079588 = TRMult. by Invertion 5,652 = P. 4159176 1039794 124775 10397 The Product - 53,34142 = TRPAdd - +250,5 = PAnfwer - $l_{309,84142} = A = 309l_{10}l_{10}s_{10}d_{10}$

Question 2. What Principal or Sum of Money put to Interest, will raise a Stock of (or be worth) 405 l. 6 s. in five Years, and eight Months, at the Rate of 51. per Cent. per Ann.?

Here is given $\begin{cases} A = 405,30016 \\ R = 0.05 \\ T = 5,613698 \end{cases}$ To find P, per The. 2.

Multi-

Multiply 5,61369 By - 0,0	
Product 0,2806849 Add Unity 1,	=TR
TR + 1 = 1,2806845	$\begin{array}{c} \hline p) 405,30016(316,471441) \implies P. \\ 38420547 \\\hline 2109469 \\\hline 1280684 \end{array}$
Hence the Principal	· 828785 768410
is 316,47144 l. which, in common Coin, is 316 l. 9 i. 5 d. for the Anfwer.	• 60375 51227 • 9+48
- •	8264 • 184 128
	- 56 51 5
	5

Note, By this Theorem 'tis you find what prefent Money, or prompt Payment, will fatisfy a Debt due any Time herealter, Abating or Discounting at any Rate per Cent.

Quefition 3. At what Rate of Interest per Cent. will 36 l. amount to 36 l. 18 s. 11 $d \pm d$. in fix Months, three Weeks, and three Days.

Here is given
$$\begin{cases} P = 36\\ T = 526\\ A = 36,9468 \end{cases}$$
 To find R, per The. 3.

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A 1 2

Multi-

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Multiply ,528 = T By - 36 = P 3156 1578 Fred. 18,936 = T s Then As 1:005:	Sut 1	$\begin{array}{rcl} & 36,9468 = A \\ & & P$
	<i>Time</i> will 2	00 l. 1 s. 8 d. amount to
Here is given $\begin{cases} P = \\ R = \\ A = \end{cases}$	200,083 0,045 250,	Fo find T, per T b20. 4.
Molt. 200,083 $\doteq P$ By - 0,045 $= R$	From Subft.	250,000 = A 200,08z = P
100041 6 8003333	9,00375)	49,91866(5,54399= T 4501875
Prod. 9,00375 = PR		489791 450187
The Time then is Years		39604 36012
5,54399 = 5 Years, 7 Months, and 3 Days.		3592 2701
·····		891 810
	•	81 .81
<pre>< ' + + + + + + + + + + + + + + + +</pre>	11.1	•

Given U, T, R; to find A? Theorem 1. $\int \frac{TTU - TU}{2} R + TU = A$.

Given

The Use of Decimals in Intereft. 181 Given A, T, R; To find U: Theorem 2. $\left\{ \frac{2A}{TTR - TR + 2T} = U \right\}$ Given A, T, U; To find R: Theorem 3. $\left\{ \frac{2A - 2TU}{TTU - TU} = R \right\}$ Given U, R, A; To find T? Theorem 4. $\left\{ \sqrt{\frac{2A}{RU} + \frac{xx}{4}} - \frac{1}{3} x = T \right\}$

Queftion 1. If 2501. Yearly Rent (or Annuity, &c.) be forborn or unpaid 7 Years; what will it amount to in that Time, at the Rate of 61. per Cent. per Annum?

Here is given $\begin{cases} U = 250 \\ T = 7 \\ R = 0,06 \end{cases}$ To find A, per Theorem 1.

Mukiply By	,	= U = T	••	•	1
Product - By		= TL = T.	Γ.	•	
Substract	12250	= TT = TU			
Remains Halve Multiply by	5250	= TI $= TI$ $= R$		TU. TU÷	2
Adđ	315,00 1750,	=TL	J		•
Sum	2065 1.	$= \Lambda$	The	Anfwer.	,

If the Payment of the aforefaid Annuity had been made balf Yearly, then would $U = 125 = \frac{250}{2}$, and T = 14 =Number of Payments; and $R = 0.03 = \frac{0.06}{2}$, and working as per Theorem; A will be found = 2091 l. 5 s. which is

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is more than the Yearl's Payment by 261. 5s. Hence the oftner the Payment, the more advantagious.

Queflion 2. What Annuity, or Yearly Payment, being unpaid 8 1 Years, will raife a Stack of 572 l. 12 s. 8 d. at 5 per Cent, per Annun.

Here is given $\begin{cases} A = \\ T = \\ R = \end{cases}$	572,63 8,5 6,05 To find U, per Theor. 2.
Mukiply — By —	8,5 = T $,05 = R$
Again by 🦾	$4^{25} = TR$ 8,5 = T 2125
Product — Subftract —	$\frac{3400}{3,6125} = TTR \\ 0,4250 = TR$
Remains $-$ Add 8,5 \times 2 $=$ 1	3,1875 = TTR - TR
TTR_TR+2T=20,187	5) 1145,2666 &c. = 2A (56,73148 1009375
	• 1358916 1211250 • 147666
The Annuity there-	141312 **6354
fore is $56,73148 = 56$. 14 s. 7 d. The An- fwer.	6056 298 201
	* 97 80
	· 17 16 · 1

Que ft.

Question 3. At what Rate of Interest, per Cent. per Ann. will 401. 13 s. 4 d. Yearly Rent, amount to 4501. 13 s. 4 d. in 9 Years?

Here is given
$$\begin{cases} A \neq 450, \\ T = 9 \\ U = 40, \\ \end{bmatrix}$$
 To find R, per Theorem 3.

40,**#** = U Multiply By g = T366 = TU Product. Multiply again by 9 = T From that Prod. 8294 = TTU Substract = TU366 = TTU - TU The Divisor. Remains 2928 Then from 901,3 = 2ASubstract 732 = 2TU $169,3 \pm 2A - 2TU$ The Dividend. Remains Then 2928) 169,33 (0,05784 = R 14640 2293 2049 244

1. 1. 1. 1. 1. 1. s. d. Therefore as $1:0,05784::100:5,784 = 5:15:8\frac{1}{4}$ the Rate per Cent. required.

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Queftion 4. In what Time will 250 l. Yearly Rent, raife a Stock of 2065 l. allowing 6 per Cent. &c. for the Forbearance of the Payments as they become due ?

Here is given $\begin{cases} U = 250 \ 7 \\ A = 2065 \\ R = 0,06 \end{cases}$ To find T, per Theorem 4.

Firft

First Then stultip By	y - 250	= 2A $= U$ $= R$	م - بر ز
Product is	- 15	•	·
Then	- 33,3	$x = \frac{2}{R}$	• . i
And 33,3 -	I = 32,3	$=\frac{2}{K}-1=K$	
And 32,3 -	- 2 = 16,14	$\theta = \frac{1}{2}x$	
The Square	of it is 261,3	$6x = \frac{1}{4} xx = \frac{xx}{4}$	
To which ad	ld 275,3	$=\frac{2A}{RU}$	<i>.</i> .
The Sum is	.536,6	$\frac{1}{24} = \frac{2A}{RI} + \frac{xx}{4}$	
The Square of which is	Root } 23,1	$\beta = \sqrt{\frac{2A}{RU} + \frac{xx}{4}}$	
From which	take 16,1		
There remains viz.	ins 7 7 Years.	= T The Time	required,

The Divisions and Extractions at large I have omitted for the Learner's Exercise; but I have represented all the Numbers in One; which Mr. Ward's Method could not do as being der ficient in the Doctrine of Calculating Numbers, as may be observed in his Work of this and other Questions of Interest,

N. B. In all Queficons about Yearly, or flated Rents and Payments, the Intereft is reckoned for every Payment after it becomes due, thro' the whole Time of Forbearance.

Theorems refulving all Questions concerning the Present Worth of Annuities, Pensions, Gc. at Simple Interest.

> Given U, R, T; To find P? Theorem 1. $\left\{ \frac{TTR - TR + 2T}{2TK + 2} U = P \right\}$

> > Given

The Use of Decimals in Interest. 185 Given P, R, T; To find U. Theorem 2. $\begin{cases} TR + 1 \\ TTR - TR + 2T \end{cases}$ $2^P = U$ Given P, U, T; To find R. Theorem 3. $\begin{cases} 2P - 2TU \\ TTU - TU - 2PT \end{cases} = R$ Given U, P, R; To find T. Theorem 4. $\sqrt{\frac{2P}{RU} + \frac{xx}{4}} \pm \frac{1}{4}x = T$

Question 1. What is 75! Yearly Rent, to continue 9 Years, worth in ready Money, at 6 per Cent. &c.

Here is given
$$\begin{cases} U = 75 \\ R = 0,06 \\ T = 9 \end{cases}$$
 To find P, per Theorem 1
Multiply $-$ 0,06 \equiv R
By $-$ 9 \equiv T
The Product $54 \equiv TR$
Again by $9 \equiv T$
From which $4,86 \equiv TTR$
Take $54 \equiv TR$
Remains $4,32 \equiv TTR - TR$
To which add $18,00 \equiv 2T$
Dividend $\equiv 22,32 \equiv TTR - TR + 2T$
Dividend $\equiv 3,08 \equiv 2TR + 2$

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Then

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Then 3,0	8) 22,32 (7,24675
-	2156. $75 = U$
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	616 5072725
	143 (543,50625 = P
	$\begin{array}{c} 1_{440} \\ 1_{232} \\ \hline \\ 1_{232} \\ 1_{232} \\ \hline \\ 1_{$
	- Anfwer.
	2000
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	Constantine and
	• 2320
•	2156
	/ • 1640
	1540
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Question 2. What Annuity, to continue 21 Years, will 1921. 1 s. 5 1 d. parchase, at 5 per Cent.?

Here is given $\begin{cases} P = 192,0731 \\ T = 21 \\ R = 0,05 \end{cases}$ To find U, per The. 2. Multiply 21 = TBy ,05 = RThat Product 1,05 = TRAgain by 21 = T105 =210 The Product is 22,05 = TTRFrom which take 1,05 = TRThere remains 21,00 = TTR - TRTo which add 42,00 = 2TThe Divifor 63,00 = TTR - TR + 2T-Then to 1,05 = TRAdd Unity 1,00 == 1 The Dividend = 2,05 = TR + I

Then

Then 63) 205 (,03254 189
160
126
• 340
315
250
252
But $-384,1462 = 2P$ Multiply by 45230,8 invert
115244
7683
1920
- 153
Product and The
Product $-12,5 = U$

The Annuity then is 12,5l = 12l. 10 s. the Answer.

Note, This is a very frequent and useful Question; and ought to be worked with great Exactness; and therefore if a Person be not very ready at, nor rightly understands the Manner of Contracted Multi. plication and Division, 'twill be best to work the common Way. Which also is to be observed in all Questions of Moment.

Question 3. At what Rate of Simple Interest, will 250,3? or 250 l. 6 s. 8 d. purchase an Annuity of 30 l. 10 s. per Annum, to continue 10 Years.⁹

Here is given $\begin{cases} P = 250,3\\ U = 32,5\\ T = 10 \end{cases}$ To find R, per Theorem 3.

l

B b 2 Multiply

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Multiply 30,5 = UAnd $500, \theta = 2P$ By 10 = TAlfo 610,0=2TU 305 = TUThe Product is Differ. 109,z=2PWhich again mult, by 10 **= T** -2TU the Divi-Produceth 3050 = TTULdend From which take 305 = TUThere remains 2745 = TTU - TU.Then 5006, s = 2PT $2261, \theta = TTU - TU - 2PT$ The Difference the Divisor.

2261,6)109,3 Then See Division of Repetends. 2261 109 2035,5) 8840 (,04343 = R8142 698 610 • 88 81 6 1 l. l. 1. 1.

Then fay, As 1 : 0,04343 : : 100 : 4,343 = 4 l. 6 s.10 d. the Rate per Cent. fought.

Question 4. In what Time will 71. per Annum pay a Debt of 1201. 8 s. at 61. per Cent. Or, For how long a Time may an Annuity of 71. per Annum be purchas'd or enjoy'd for 1201. 8 s. at the aforesaid Rate?

Here is given
$$\begin{cases} U = 7 \\ R = 0.06 \\ P = 120.4 \end{cases}$$
 To find T, per Theorem 4.

Fiifi

 $\begin{bmatrix}
1,03 = \frac{1}{2} \\
103 = \frac{1}{2} \\
9)309 = \frac{344}{10333} \\
1,067 = \frac{1}{2} \\
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1007 = \frac{1}$ 240,8 = 2P34,4 = $\frac{2P}{U}$ Firft And From which take $33x^2 = \frac{2}{R}$. To the Remaind. $1,0\% = \frac{2}{R} - \frac{2P}{U}$ Add Unity =+1I $2,0\% = \frac{2}{R} - \frac{2P}{T} + 1 = x$ by Subflitut. The Sum is Then $1,03 = \frac{1}{2}x$ 1,067 = ±** And 0,42 = RUAgain $-573,3 = \frac{2P}{RU}$ And Then - 574.4 = $\frac{2P}{RU} + \frac{xx}{4}$ Sq. Boot of that 23,96 = $\sqrt{\frac{2P}{RU} + \frac{xx}{4}}$ Then To which add $1,03 = \frac{1}{2}x$ 24.9 = 25 = T the Time fought. The Sum is

Having thus, in a most performance Manner, show'd the great and invaluable Service of Decimals in working Questions of Simple Interest, &c. I shall proceed to treat of the fame things, in the like Manner, in Compound Interest.

Theorems refolving all Questions of Compound Interest.

> Given P, R, t; To find $A^{?}$ Theorem 1. $PR^{t} = A^{?}$ Given A, R, t; To find P? Theorem 2. $\left\{\frac{A}{Rt} = P\right\}$ Given $\left\{\frac{P, A, R}{P, A, t}\right\}$ to find $\left\{\frac{t^{?}}{R^{?}}\right\}$ Theorem 3. $\left\{\frac{A}{P} = R^{t}\right\}$

Rates.

Rates.	Logarithms.	Rates.	Logarithms.
1,10 =	= 0,041392	1,055	= 0,023252
1,58 =	= 0,033423	1,045	= 0,019116
	= 0,025305	1,04	= 0,017033
1,05 =	= 0,021189	₹,03	= 0,012837

Queftion 1. What will 256 l. 10 s. amount to in 7 Vears, at 6.1. per Cent. Scc. Compound Intereft?

Here is given
$$\begin{cases} P = 256,5 \\ R = 1,06 \\ t = 7 \end{cases}$$
 To find A, per Theorem 1.

Multiply the Logarithm of the Rate 1,06 = 0,025305By the Index of its Power (viz. t =) 7 The Product the Logarit. of $R^7 = 1,50363 = 0,177135$ Multiply that by P — = 256,5 = 2,409087The Product is the Amount A = 385,6811 = 2,586222That is, $3551.135.7\frac{1}{4}d$, the Answer required.

Question 2. What Principal, or Sum of Money, will raife a Stock of 20,6 in 5 Years, at 51. per Cent. per Annum Compound Interest?

Here is given $\begin{cases} A = 20,5 \\ t = 5 \\ R = 1,05 \end{cases}$ To find P, per Theorem 2:

Multiply the Logarithm of the Rate 1,05 = 0,021189By the Index of its Power t = -5The Product is the Logar. of $R^c = 1,27628 = 0,105945$ By which divide the Amount A = 20,6 = 1,313867The Quotient is the Principal P = 16,1407 = 1,207922That is 151.75. the Sum required.

Question 3. In what Jime will 37 l. 175 s. amount to 76,05 l. (or 76 l. 13 s.) at 4 l. 10 s. per Cent?

Here is given $\begin{cases} A = 76,65 \\ P = 37,75 \\ R = 1,745 \end{cases}$ To find t, per Theorem 3. Divide

Divide the Amount -A = 76,65 = 1,884512By the Principal (or Sum) P = 37,75 = 1,574216The Quotient is $-\frac{A}{r} = R^{t} = 2,02046 = 0,307595$ Then 2,03046 divided by (R =) 1,045; and that Quo-

tient again by 1,043; and thus continually dividing the Quotients by 1,045, 'till nothing remains, the Number of fuch Divisions will be equal to (t =) the Time fought. But this is fooner, and eafier done by much, by Logarithms.

Thus, Divide the Logarithm of 2,03046 ($= R^{1}$) by the Logarithm of 1,045 (= R) and the Quotient is the Time.

0,019116) 0,307596 (16,091 = t the Time fought. 19116

116436 114696 . 1740 1720	Viz. 16 Years, 1 Month, and 5 Days, the Anf.
. 20	
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Concessor of the local division of the local	
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Question 4. At what Rate of Compound Interest, will 511. 15 s. amount to 701. 18 s. in 5 Years?

Here is given
$$\begin{cases} P = 51,75 \\ A = 70,9 \\ t = 5 \end{cases}$$
 To find R, per T becorem 3.

Divide the Amount By the Principal or Sum A = 70.9 - 1.850646By the Principal or Sum P = 51.75 = 1.713910The Quotient will be $R^t = Rs = 1.370048 = 0.136736$ The Surfolid Root of which is R = 1.065 = 0.027347 *l. l. l. s.* Then fay, As 1 : 1.265 :: 100 : 106.5 = 106-10=R the Rate per Cent. per Annum fought.

Note; R^s being equal to 1,370048, of Confequence $R = s_{-1,370048}$, which may be extracted by an A'gebraick converging Series; the Manner of doing it, fee in Chap. 11. of the Use of Decimals in A'gebra.

Theo-

Theorems refolving all Questions relating to Annuitics, Oc. in Arrear, calculated at Compound Interest.

Given U, R, t; To find
$$A \stackrel{*}{\stackrel{*}{\scriptstyle \rightarrow}}$$

Theorem 1. $\left\{ \frac{UR^t - U}{R - 1} = A \right\}$

Given A, R, t; To find U? Theorem 2. $\begin{cases} \frac{RA-A}{R^{2}-1} = U \end{cases}$

Given U, A, R; To find t? Theorem 3. $\begin{cases} \frac{RA+U-A}{U} = R^{t} \end{cases}$

Given A, U, t; To find R? Theorem 4. $\begin{cases} A \\ U \end{cases} R - R^{t} = \frac{A - U}{U}$

Question 1. If 30 l. Yearly Rent be forborn or unpaid 9 Years; What will it amount to at the Rate of 6 l. per Cent. &cc. Compound Interest?

Here is given $\begin{cases} U = 30 \\ t = 9 \\ R = 1,06 \end{cases}$ To find A, per Theorem 1.

In the first Place, let R = -1,06 = 0,025305Be involved to the 9 Power (viz. R^{t}) -9That will be $-R^{9} = 1,689451 = 0,227745$ Multiply by U = 30 = 1,477121The Product is $-UR^{t} = 50,683530 = 1,704866$ From that Subfract U = 30The Remainder is the Divid. $= 20,68353 = UR^{t} - U$. Divide therefore $UR^{t} - U = 20,68353 = 1,315626$ By -R - 1 = 0,06 = 8,778151The Quotient is -A = l.344,7267 = 2,537475That is the Amount = 344l. 14 s. $6\frac{1}{4}d$. the Anfwer.

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Question 2. What Annuity 31. 10 s. per Cent. Compound Interest, will raise a Stock of 344 l. 5 s. being forborn 8 Years?

Here is given
$$\begin{cases} A = 344,25 \\ R = 1,035 \\ t = 8 \end{cases}$$
 To find U , per Theor. 2.

A = 344,25 = 2,536874Multiply the Amount نسو . R = 1,035 = 0,014940By the Rate From that Product -RA = 356,29875 = 2,551814Substract the Amount -A = 344,25The Remainder is RA - A = 12,04875, the Divid. Then involve R = 1,035 = 0,014940 To the 8th Power - viz. Re $R^8 = 1,316803 = 0,119520$ That Power will be The fame lefs Unity is $R^2 - 1 = 0,316803$, the Divisor. Therefore divide RA - A = 12,04875 = 1,080908 $R^{t} - 1 = 0,316803 = 9,500785$ By - U= 38,0297 = 1,580123 The Quotient is

The Annuity therefore which was fought, is found to be 38,0297 l. = 38 l. 0 s. 7 d. per Annum, Answer.

Question 3. In what Time will 38 l. 0 s. 7 d. raise a Stock of 344 l. 5 s. at 3 l. 10 s, per Cent. per Annum, Compound Interest?

Here is given
$$\begin{cases} U = 38,0297 \\ A = 344,25 \\ R = 1,035 \end{cases}$$
 To find *t*, per Theor. 3.

First multiply the AmountA = 344,25 = 2,536874By the given RateR = 1,035 = 0,014940To that ProductRA = 356,29875 = 2,551814Add the AnnuityU = 38,0297From the SumRA + U = 394,32845Take the AmountA = 314,25The Remain-
der is the RA + U = 38,0297 = 1,699651Divi. whichU = 38,0297 = 1,580123The Quotient will beR t = 1,316803 = 0,119528Then Divide 1,316803 continually by the Rate 1,035 un-

till nothing retains, and the Number of those Divisions will be 8 = r = Time required.

But thich better by Logarithms thus; Divide the Logarithm of the Power by the Logarithms of the Rate, the Quotient is $\pm t$ the Time fought.

> Thus C. 314941) 0/119528 (8=1 the Time, shr.) 0,119528 8 Years; Answer. J

Queflion 4. At what Rate per Cent. Compound Interest, will 391. Yearly Rent, being forborne or unpaid 9 Years, amount to 3441. 14 s. 6 4 d.

Here is given
$$\begin{cases} U = 30\\ A = 344,7267 \end{cases}$$
 To find R, per The. 4.

First divide the Amount A = 344,7267 = 2,537475By the Annuity -U = 30 = 1,477121The Quotient is -U = 714,7909 = 1,000354Again the Amount A - U = 314,7267 = 2,497933Which divide by -U = 30 = 1,477121The Quotient is $-\frac{A - U}{U} = 10,49014 = 1,020812$ Now $R_1 = R_2$. Therefore the Theorem affords this Equation, viz. 11,4909R - R⁹ = 10,49014 This

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This Equation is easily refolved by a Converging Series (which fee in the Use of Decimals in Algebra.)

Note, This Question may be very eafily and expeditiously answer'd, by the Rule of False Position; thus

Make two Suppositions. of the Rate, which may include between them the Rate you feek.

Then find what the Amounts of the given Annuity would be at the two suprefed Rates of Interest, per Theorem 1.

Lastly; Observe the Errors of those Amount from the Amount here given, then by those Suppositions and their Errors, find the true Rate, (viz. 1,06) as is there taught.

Theorems refalsing all Queflions concerning the Prefent Worth of Annuities, Penfions, or Leafes in Revertion, at Compound Interest.

> Given U, R, t; To find P? Theorem 1. $\begin{cases} U - \frac{U}{R} \\ R - 1 \end{cases} \xrightarrow{P}$

Given P, R, t; To find U? Theorem 2. $\left\{ \frac{\overline{PR\iota} \times \overline{R} - PR\iota}{R\iota - 1} = U. \right\}$

Given U, R, P; To find t?

Theorem 3.
$$\left\{ \frac{U}{P+U-PR} = R^{t} \right\}$$

Given U, P, *; To find R? Theorem 4. $\left\{ \frac{U}{P} = \frac{U}{P} R^{t} + R^{t} - R^{t+t} \right\}$

Question 3. What is 30 l. Yearly Rent, Worth in ready Money, for its Continuance 7 Years, allowing 61. per Cent. Compound Interest to the Purchases?

Here is given $\begin{cases} U = 30 \\ R = 1,06 \\ t = 7 \end{cases}$ To find P, per Thyprem 1. C c 2 First

First, involve R = 1,06 = 0.025305To the 7th Power, (viz. R7) 17 That will be $R^7 = 1.50061 = 0.177135$ Then divide U = 30 = 1,477121By R', there will remain 19,9520 = 1,299986U Then from the Annuity -20 Substract 19,952 10,048 = 1,002079**Remains the Dividend** U, Which divide by the Rate lefs 0,06 = 8,778151Unity $= \mathbf{R} - \mathbf{I}$ The Quotient is the prefent = 167,4716 = 2,223928 Worth -PThe Present Worth, In ready Money is 1671. 9s. 5d. the

Anfwer.

N. B. Suppose this were an Annuity in Reversion, or not to be entered on till after 7 Years are past, and thenceto continue 7 Years; and you would know the present Worth; find by the second Theorem of Compound Interest, what ready Money will amount to 1671.9s.5d. in 7 Years, at the same Rate of Interest; and that will be its present Worth; and so for any other Annuity in Reversion.

Question 2. What Annuity, to continue 7 Years, may be purchased for 1201.5s. at 6 per Cent. Compound Interest?

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 $P = \frac{120,25}{P} \sum_{i=1,06}^{20,25} \zeta \text{ To find } U, per Theor. 2,$ Here is given R = 1,06r = 7t = 7Involve the Rate R = 1,06 = 0,025305To the Index of its Power (viz. = ij : The Power of R will be $R_{7} = 1,50361 = 0,177135$ Which mult. by the prefent Worth P=120,25 = 2,080081 PR' = 180,8c87 = 2,257219The Product is "-" R = 1,06 = 0,025305Multiply that by the Rate That Product is $P_{R} \times R = 191,65722 = 2,282524$ From which fubftract PR' = 182,8c87There Remains the Dividend $10,84852 = PR' \times R$ - PR'. Divide

Divide therefore $PR \times R - PR = 10,84852 = 1,035359$ By the Power of R lefs $I = R^{1} - I = 2,5036I = 9,702113$ The Quotient is the Annity U = 21,54057 = 1,333256The Annuity fought therefore is 21,54057 l. = 21 l. 10 s 9 3 d. Queftion 3. For what Time will 16y l. 9 s. 5 d. purchase an Annuity of 301. per Annum, at 6 per Cent. Compound Interest ? Here is given $\begin{cases} P = 167,4716 \\ U = 30 \\ R = 1.06 \end{cases}$ To find *t*, per Theor. 3. To the prefent Worth P = 167,4716Add the Annuity U = 3012 P + U = 197,4716The Sum is Then mult. the prefent Worth P = 167,4716 = 2,283928 By the Rate R = 1,06 = 0,025305- PR = 177,5199 = 2,249233The Product is Which fubil. from Sum of P+U = 197,4716The Remainder is P+U-PR = 19,9517 the Divisor. Then Divide the Annuity - U = 30 = 1,47712IBy the Divisor P + U - PR = 19,9517 = 1,299986 $R^{t} = 1,50361 = 0,177135$ The Quotient is Lafily, Divide the Logarithm of Rt, by the Logarithm of the Rate; the Quotient will be the Time = t fought.

Thus, 0,025305) 0,177135 (7 = t the Time fought, 0,177135 piz. 7 Years. Aniwer,

Queficor 4. Suppose I purchase an Annuity of 21 l. 10 s. 9, d. to continue 7 Years, for 120.1. 5 s. zeedy Maney; at what Rate per Cent. Compound Interest, was the Purchase made?

Here is given $\begin{cases} P = 120,25\\ U = 21,54057\\ t = 7 \end{cases}$ To find R, per Th: 4. First,

First, divide the Annuity	U = 21,54057 = 1,333256
By the prefent Worth	- $P = 120,25 = 2,080084$
The Quotient is	$\frac{U}{P} = 0,17915 = 9,253172$

Then multiply it into the given Power of the Rate, to which add the Power, &c. as per Theorem; and you have this Equation, viz. $0.17915R^7 + R^7 - R^8 = 0.17915$; whence a Perfon ready at Agebraick Extractions, may foon different R = 1.06. Then fay, as 1 l. : 0.06 l. :: 100 l. : 6 l. the Rate per Cent. required.

Note; This (and all Questions of this Nature) may be answered by the Rule of Postien, in the same manuer as was directed in the south Question of Annuities in Arrears.

Theorems refolving all Questions relating to the Purchafing of Free-hold or Real Estates, at Compound Interest.

> Given PR; To find U? Theorem 1. PR - P = U. Given UR; To find P?

Theorem 2.
$$\frac{U}{R-\tau} = P$$
.

Given P, U; To find R?

Theorem 3.
$$\frac{P+U}{P} = R$$
.

Question 1. Suppose a Free-bold Estate of 25 l. per Anrum were to be fold; What is the Worth, allowing 5 l. 10 s. per Cent. &c. Compound Interest to the Buyer?

Here is given $\left\{ \begin{matrix} U = 25 \\ R = 1,055 \end{matrix} \right\}$ To find P, per Theor. 2.

Divide the Annual Rent - U = 25 = 1,397940By the Rate has Unity R - 1 = 0,055 = 8,740362The Quotient is the Worth P = 4\$4,5 = 2,657578The Value of that Effate therefore is 454 h 10 s. $10\frac{4}{4}$ d. Q. E. I.

Queftion

.

Queffion 2. Suppose a Perfon would be out 416L 13.5. 4 d. on a Free-bold Effate, and to as to be allowed 61. per Cent. for his Money, Compound Interest; What must be the Annual Rent of fuch an Estate?

Here is given $\begin{cases} P = 418,6 \\ R = 1,06 \end{cases}$ To find U, per Theor. I. Multiply the prefeat Worth P = 418,6 = 2,619789By the Rate R = 1,06 = 0,025305The Product is PR = 441.6 = 2,645094From which fubfract the Worth P = 418,6There remains the Annual Rent U = 251. per Annum. Question 3. Suppose one give 4161. 13 t. 4 d. for a Freebold Effate of 251. per Annum; What Rate per Cent. Compound Intereft, has the Purchafer for his Money?

Here is given $\begin{cases} P = 41656 \\ U = 25 \end{cases}$ To find R, per Theor. 3. To the prefent Worth P = 41856Add the Annual Rent U = 2550Divide their Sum P + U = 441.6 = 25645094By the prefent Worth P = 41856 = 25645094By the prefent Worth P = 41856 = 25019789The Quotient is the Rate fought R = 1.06 = 0.025305Then fay, As 1 l. : .06 l. : : 100 l. : 6l. per Gent. the Anfiver.

Rebate or Discount.

What this is I have already defined in the Beginning of this Chapter; The Intereft, and Diflount, of the fame Parcel of Money, is very different, the vulgarly underflood (and accordingly is reckoned) the fame thing.

In order therefore to have a right Notion of Difcount, and how it differs from Intereft; we must consider, that Intereft is the Increase of any Principal, or Sum of Money, according to any Rate, or Proportion, agree'd on; and in computing it, we have Regard only to the bare Principal; But what is properly call'd Discount, is the Difference between a Sum of Money due any Time hence, and such another Sum as, being put to Interest, would, with its Increase by Interest, become equal to the faid Sum hereaster due.

Thus,

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Thus, for Example, If I have 105 l. due to me 12Months hence; the Difcount for prompt Payment thereof at 5 l. per Cent. Simple Interest must be 5 l. and the present Money, or Worth of that 105 l. is 100 l.; Because if I put 100 l. out at the aforefaid Rate, it would in that Time be equal or amount to 105 l. Wherefore the Interest of 105 l difcounted (as is the common way) I should receive but 99 l. 15 s.; the Interest of the 105 l. being 5 s. more than the true Difcount; and confequently the reckoning litterest for Difcount is very difadvantagious to those who make fuch Difcounts.

The Proportion for Rebate or Discount then is,

As 100 l. and the Rate : is to the Rate :: to is any other Sum : to its true Diffount for the fame Time.

The *Theorem* for finding at once both the *Difcount* and *prefent Worth* of any Sum of Money, due any time hereafter, is the fecond *Theorem* of *Simple* and *Compound Intereft*, as I there observed.

By the fecond Theorem of Simple Interest, it was found that the present Worth of 4051. 6 s. 0 d. due 5 Years and 8 Months hence at 5 per Cent.

- · · · •		l. s. d.
Muft be		316-9-5
Which fubfiracted from the Debt, leaves the true Discount	ر نستیم	88-16-7
But the latereft of that Sum is for that Time		113-15-2
Which exceeds the true Difcount by	_	24-18-7

Above a fourth Part loss to the Difcounter of Interest for fuch a Sum.

Note. This Theorem of Mr. Ward's, is far more easy, concile, and elegant, than any other extant, for finding the prefent Worth, or Discount for prompt Pagment of any Debt.

A TA-

A Table of Days for any given Time.

Detember		335	336	337	338	339		341		343		345	346	347	348	349	350	351	352	353	354	355	356	357	358	359	360		361	361	361 362	361
November	-	305	306	307	308	309	310	311	312	313	314	315	316	317	318	319	320	321	322	323	324	325	326	327	328	329	330	11	331	331	332	332 333
October	-	274	275	276	277	278	279	280	281	282	283	284	285	286	287	288	289	290	291	292	293	294	295	296	297	298			500		301	301
September	-	244	245	246	247	248	249	250	251	292	253	254	255	256	257		259	260			263	264	265	266	267	2681	269		2/01:		271	271
ynany	100	213	214	215	216	217	218	219	220	221			224	225	226			229				233	234	235		237 :	238 :		637 3		240 :	240 2
Finf	-0.	182	183	184	185	186	187	188	189	193	191	192	193	194	195	196	197	198	199	200	201	202	203			206	207	208		1.20	209	209 210
June	1.1.1	152	153	154	155	156	157	158	199	160	161	162	163	164	165	166	167	168	169	170	171	172	173					178		179	179	179
May	-	121	122	123	124	125	126	127	128	129	130	131	132	133	134	135				139				143			146	147	121	148	148	148
April	-	91	92	93	94	95	96	97	98	99	100	101	102	103				107	108		110							117		118	118	118
March	17-	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75		77	78		0 1	0		83			86	0		88	88
February	-	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58		59	59	59
Farmary		1	2	3	4 5	5	6	78		9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27		28	29	
Days		1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	0	28	29	29 30
			ģ	Į	1	1				1		1	ł	ł	I	ł	ł	I	Į	۱	ł	I	ļ	l	Į	ł	l	۱	а.	ł		

The Ufe of the Table.

First ; To know the Number of Days from the Beginning of the Year, to any given Day of any Month. Dd This

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203 The Use of the preceeding Table.

This is obtain'd by Infpection only; Thus from January the 1A, to September the 7th, is 250 Days; To November the 27th are 331, Sc.

Secondly, To know what is the Number of Days from any given Day of any Month, to the End of the Year.

Suppose September the seventh, then from - 365

Substract the Number answering to Sept. 7 - 250

There remains the Number of Days fought, viz. 115 Days.

Ibirdly, To find the Number of Days between the given Day of any one Month, and any given Day of any other Month, in the fame Year.

For Inflance, To know how many Days there are between April the 17th, and October 23.

Thus, From the Number answering to October 23 - 296 Subfract that answering to April 17 - 107

The Remainder is the Number of Days fought - 189

Fourthly, To find the Number of Days, from any given Day of any Month in one Year, to any given Day of any Month in the next Year.

How many Days is it from September the 7th, 1733, to April the 19th, 1734?

From the Days of a Whole Year	365 250
Remains the Number to the End of the Year To which add the Number to April 19	115
The Sum is the Number of Days required -	224

And thus is the Number of Days readily found for any Interval of Time given, in the fame Year compleatly; or which is part of one, or part of another Year.

How very neceffary and useful a Table this is in all Parts of Arithmetical Science relating to Time is sufficiently evident to the Skilful therein; but because it is more particularly so in the whole Affair of Interest, I have therefore prefixed it to the other Tables.

Having then the Number of Days, 'tis eafy to find what Decimal Part of the Year, they make ; and having found that, you have the T, t, in the foregoing Theorems representing any Part of a Year. An The Nature, Conftruction, and Ule, &c. 203

An Example in Simple and Compound Intereft, will make the whole Matter eafy and confpicuous.

Example 1, What will 651. amount to, being lent from March the 7th to November the 3d, at 51. per Cent. per Annum Simple Intereft?

From March the 7th to November the 3d are 241 Days; those make 8 Months, 2 Weeks, and 3 Days, = 660273 Decimals of a Year. Then by Theorem 1.

Multiply the Time T = 0.665273By the Ratio of the Rate R = 0.05And that Product TR = 0.03301365Multiply by the Principal P = 65The Product is TR P = 2.14588725To which add the Principal P = 65

The Sum is the Amount fought = 67,1458 &cc. l. Example 2. What is the Amount thereof at Compound Intereft, the Rate and Time, being the fame ?

The Logarithm of the Rate $R \equiv 1,05 \equiv 0,0211893$ Multiply by the Time $f \equiv ...,6603$ The Product is the Logar. of $R^c = R_{0,5603} \equiv 0,0139912$ To which add the Log. of the Prin. $P \equiv 63 \equiv 1,8129133$

The Sum is the Log. of Amount A =67,1281= 1,8269045

And thus the *Theorems* ferve to answer Questions, when the *Time* is only part of a Year, as well as when complet Years,

Proem to the Tables of Simple Interest, concerning their Nature, Construction, and Use.

The great Defign of Tables of Interest (both Simple and Compound) is Ease and Expedition in practical Calculations. For, befides that the Rules expressed in Words for answering Questions of Interest are tedious and intricate, and the Reason no ways to be understood; the Operations themselves are, for the most part, very laborious; and consequently Tables which expedite and facilitate the Fractice are indispensibly necessary.

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so4 The Nature, Confiruction, and Use

This being underliably evident, the Queffion occurs, Whether these Tables are to be made in Decimal or mixed Numbers (i. e. such as express the Money in its common Demominations of Pounds, Shillings, and Pence)? The Answer to this can admit of no Demurr amongst those who understand the Doctrine of Decimal Numbers; they all know the Exsellency and superiour Use of the first Sort, viz. Decimal Tatles. But Interest Tables expressed in common Money are indulged to those who understand not Decimals, as Crutches to the Lame, and Spectacles to the Weak-fighted.

The Numbers in the first of these Tables of Simple Interest for Days, and in the Second for Years, being in Arithmetical Proportion, makes them capable of that Perfection, which no other Tables can pretend to.

Thefe Tables are fo contrived, That the Interest of any Principal Sum is easily found for any Number of Days or Years at any Rate from one Pound to Ten, with the Halves and Quarters. Having followed herein the Rev. Mr. Brown in his Arithmetica Infinita.

The Construction of these Tables is easy from the Theorems themselves, (and indeed the Reason of their Construction on can be no otherways fo eafily conceiv'd.) Thus by Theo. rem the first of Simple Interest, viz. tRP + P = A is the first and second Table constructed. For funce the Amount lefs the Principal, is equal to the Interest, therefore the Theorem will be tRP = Intereft. Now if P = 1 l.t = ,002739 Bc. (the Decimal of a Year for one Day), and R = any Ra. tio of Interest, suppose 5 per Cent.; then the Simple Interest of one Pound for one Day, at 5 per Cent. is ,002739 Sc. \times .05 \times 1 = 00013698 Sc. which being multiplied by the nine Digits feverally conffiture that part of the Table of Intereft at 5 per Cent. and thus the whole first Table is made. The ferond Table for Years is only the various Ratio's of Interest multiplied by the faid Nine Digits; for fince t = 1Year, and P = 1 it will be tRP = R the Interest for the firft Year, &cc.

The third Table flews the Rebate or Different to be made for one Pound, at the feveral Rates per Cent. for Days. The Manner, Truth, and Reafon of its Confiruction is derived from Theorem 2. of Simple Interest, viz. $\frac{A}{tR-1} = P$. For fince the Principal or present Worth subducted from the Amount gives the Rebate or Different of that Amount; therefore

of Decimal Tables of Simple Interefi-205 fore the Diffeount of any Amount for any Time at any Rate (without Regard of the prefent Value or principal Money) may be found by this Theorem $\frac{AtR}{tR + r} = D = Difcount$, Hence if we put A = 1 l. t = ,302739 &. and R = anyRatio of Interest, suppose 5 per Cent. then by this last Theorem we have the Discount of one Pound for one Day at the Rate of 5 per Cent. per Annum ; For AtR = 1 × ,002729 \mathcal{B}_{c} , $\chi_{05} = 00012698 \, \mathcal{B}_{c}$. And tR + 1 = 100012698Bc. then by Division; 1,00012698 Bc.),00012698 Bc. (=,00013697 &c. the Difcount. If t = 1 Year; then the Annual Discount of one Pound at 5 per Cent. will be found, by the above Theorem, thus; AtR = .05 and tR + 1 = 1.05. Therefore by Division, 1,05) ,05 (== ,04761904 &. the Discount. And thus is the Discount of any Sum at any Rate for any Time above one Year found at once by the above Theorem ; and for any Time under a Year by the Table of Difcount for Days, of which I have now taught the Comfiruction in a new and more rational Method than any I have yet feen.

The Use of Table I, and II.

In order to understand how to make those two Tables universally usefull, the Reader is to observe, that if a Number consists of only one Digit with Cyphers affixed, as 10, 50, 700, 0000, 800000, &: 'tis called a *pure Number*; but those Numbers which consist of more than one, or wholly of Digits, As 370, 568, 7569, &: may be called *Mixed Numbers*. Now every *mixed* Number may be resolved into those *pure Numbers*, of which they are compassed; thus the *mixed* Number 507, may be resolved into the Pure Numbers 500, 60, and 7; fo also 15890 is resolved into 10000, 5000, 800, and 90.

Now then as to the Ufe of the Tables, observe these Rules;

I. If the Number of Days, Years, &c. proposed, be a mixed Number, let it be refulved into pure Numbers.

II. With the *pure Numbers* feverally enter the Tables, and take those *Decimal Numbers* which shand against the first Figure of each *pure Number*, in the Column marked Numbers.

III. Remove the Decimal Point in each fuch Decimal Num-

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Number, fo many Places to the Right-band, as there are Cyphers in the respective pure Numbers.

IV. Lafily, Add together all the Decimal Numbers, and find the Value thereof by the Tables for that purpose.

These things premised, the U/e of the Tables will be obvious from the *Examples* of the following *Problems*.

Problem 1.

To find the Interest of any Sum of Money for a Day, or a Vear, at any Rate per Cent. per Annum,

Example 1.

What is the Interest of 2746 *l*, at 5 *l*. 15 *s. per Cent.* for a Day?

			Decimals.
In Table 1, under	7	2000	 ,31506
the Rate 5 [‡] . You	ς.	700	,11027
find against the pure	5	40	 ,00630
Numbers	2	. 6	 ,00094
The Answer is	•		 $73257 = 8 s. 7 \frac{3}{4} d.$

Example 2.

What is the Interest of the fame Sum, at the fame Rate for a Year ?

			Decimals.	
ſ	2000		150,00000)
In Table 2. 🤰	700		40,25000	\int Under $5^{\frac{1}{2}} d$.
You find against)	40		2,30000	(per Cent.
- (6		0,34500	Under 5 ¹ d. Sper Cent.
The Anfwer in Which is in	Decima Money	$ls \overline{l} \\ y = 1$	and the second s	

Problem 2.

To find the Interest of any Sum of Money for any Num. ber cf Days.

Example.

What is the Interest of 2651. for 149 Days, at the Rate of 31. 15 s. per Cent. &c.

Multi-

of Decimal Tables of Simple Interest. 207

Multiply the Principal Sum - 265 l. By the given Number of Days - 149

The Product is the mixed Number 39485, with which refolved, enter the Table as before :

Decimals. 3,08200) 30000 Thus in Table 1. 9000 0,92466 You find against Under 31. 0,04109 400 the pure Numper Cent. 0,00822 80 bers 0,00051 5

The Answer in Decimals - 1. 4,05648

In Money 41. 1 s. 1 1 d.

The Method is the fame for any greater Number of Days.

Problem. 3.

To find the Interest of any Sum forborne any Number of Years at any of the given Rates per Cent.

Example.

What is the Interest of 1751. 15 s. forborne 13 Years at the Rate of 6 per Cent. &c.?

Multiply the Principal Sum By the Number of Years given	175,75
By the Number of Years given	 13
The Product is the mixed Number	 2284,75

Which refolved, as before, will fland thus,

	2000,		120,000	
	200,		12,000	
In Table 2.	80,		4,800	Under 6 per
You find against	4,		0,240	Cent.
	- ,7	-	0,042	
	l ,05		0,003]	
		· · ·		

The Answer in Decimals 1, 137,085

The fame in Money 137 l. 1 s. 8 d ...

N.B. The

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N. B. The Reader. must observe, in refolving a mixed Number wherein are Decimals, to remove the Point one Place more to the left than are the Namber of Cypbers in the Decimal pure Number, as in the last Example.

The Use of Table III. Of Discount.

In feeking the Discount for any Sum due at the End of any Number of Days, if the Number of Days be a mixed one, refolve them into pure Numbers as before taught; and even with them in the Table take the Discount of 1 l. which add and multiply by the Principal Sum, the Product will be the Discount thereof.

Problem 4.

To find the Discount of any Sum, for any Number of Days, at any given Rate in the Table.

ERample.

What is the Discount of 83 Pounds, 10 Shillings, for 235 Days at 4 per Cent. per Annim?

You find $\begin{cases} 200 \\ -30 \\$	Decimals. ,0214478 Under ,0032769 4 per Ce	#1 .
Which multiplied by the Sum	$\frac{30252723}{835}$ $\frac{835}{2,110237}$ $\frac{1}{36} = 2-2$	d.

Problem 5.

To find the Discount of any Sum for a Year.

Example.

What is the Difcount of 100 l. for one Year, at 5 per Cent?

In

In the Table under 5 per ,047619 &c. Cent. and againft 365 Days is ,047619 &c. Which mul. by the Principal Sum 100 1

The Product is the Anfwer $\overline{1.4,7619 & c.} = 4-15-2\frac{1}{4}$ Now the Interest of 100 l. for one Year, at 5 5-0-0The Differ. therefore of Diffcount and Interest, is $0-4-9\frac{1}{4}$

Whence 'tis evident, he who allows Interest for Discount wrongs himself confiderably, which yet is very common among Traders; for fo much Money ought to be paid, as, at Interest, would amount to the Sum due, in the Time proposed.

Example 2.

What is the Difcount of 9342 l. at $4\frac{1}{2}$ per Cent. for a Year?

The Difcount of 1 l for 365 Days, at $4\frac{1}{2}$ per Cent. in the Table, is _____}, c43062, &c. Which multiplied by the Principal Sum 9342 The Product is the Answer ______l. 402,2852 &c.

In Money 402 l. 5 s. $8\frac{1}{2}$. And thus proceed for other annual Difcounts.

I must acknowledge this Table of *Difcount* gives not the precife Truth, and yet differs but little from it; being fufficiently exact for any Ufc. None but a Table of the *Difcount* for every Day, can be perfect; because every Day's Difcount differs, being still less as the Number of Days increase.

This Table is *perfectly true* for all the Days express'd therein, and, as I faid, may be used without much Errour for any other.

Example in Prob. 4. The true Difcount is The Difcount by this Table The Int. for the Time and Rate	$\begin{array}{c} l. s. d. \\ 2 - 1 - 11 \\ 2 - 2 - 2 \\ \hline 2 - 3 - 0 \end{array}$
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TABLES

TABLES of Simple Interest.

 Table I. The Interest of one Pound for Days.

 Table II. The Interest of one Pound for Years.

 Data and Data and Control of the Second for Years.

Both at any Rate per Cent. from one to ten Pounds with Halves and Quarters.

Table I. The Interest of one Pound per Diem.

Numb.	I per Cen.	1 1 per C.	1 ½ per C.	1 + per C.
T	,00002740	,00003425	,00004110	,00004794
2	,00005480	,00006850	200008220	,00009589
3	,00008220	,00010274	:00012329	,00014383
4	,00010959	,0 0013699	<i>x</i> 00016438	
5	,00013698	,00017123	200020548	,00023972
6	,00016438	,00020548	,00024657	,00028767
7	,00019178	,00023973	200028767	,00033562
8	,00021918	,000273 <i>9</i> 8	200032877	,00038356
9 Month.	,00024657	,00030822 ,001041 <i>66</i>	x00036986	,0004315L
1130/11/2.		,00104100	,00125000	,00145833

Table II. The Interest of one Pound per Annum.

Numb.	1 per Cent.	1 4 per C.	1 ; per C.	1 1 per C.
1 2 3 4 5 6 7 8	0,01000000 0,02000000 0,03000000 0,04000000 0,05000000 0,05000000 0,07000000	0,01250000 0,02500000 0,03750000 0,05000000 0,06250000 0,06250000 0,08750000	0,01 500000 0,0300000 0,04 500000 0,0600000 0,07 500000 0,09000000 0,10500000	0,01750000 0,0350000 0,05250000 0,0700000 0,08750000 0,10500000
<u>_</u> <u>9</u>	0,09000000	0,11290000	0,12000000	0,1400000 0,15750000

Table

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Table I. The Interest of one Pound per Diem.

Numb.	2 per C.	2 + per C.	2 1 per C.	2 + per C.
	,00005480	,00006164	,00006849	,00007534
2	,00010959	,00012329	,00013699	,00015068
3	,00016438	,00018493	,00020547	,00022602
4	,00021918	,00024657	,00027397	,00030337
5	,00027397	,00030822	,00034246	,0003767I
6	,00032876	,00036986	,00041095	,00045205
7	,00038356	,00043151	,00047945	,00052739
8	,00043835	,00049315	,00054794	,00060274
9	,00049315	,00055479	,00061644	,00067808
Month	,001 <i>8</i> 66666	,00187500	,00208733	,0022,71.66

Table II.	The	Interest of	one Pound	per	Annum.
		and the spectral spec		F	

Numb.	2 per Cent.	2 ' per C.	2 ; per C.	2 à per l'.
I	0,02000000	0,02250000	0,02500000	3,02750000
2		0,0450000		0,05500000
3		0,06750000		0,08250000
4	0,0800000	0,09000000	0,1000000	00000011,0
5	0,10000000	0,11250000	0,12500000	0,13750000
6		0,13500000		0,10500000
7		0,15750000		0,19250000
8	0,16000000	0,1800000	0,2000000	
9	0,18000000	0,20250000	0,22500000	0,24750000

Table I. The Interest of one Pound per Diem.

Numb.	3per Cent.	1 3 4 per C.	3 2 per C.	3 + per C.
I	,00008220	,00008904	,00009589	,00010274
2	300016438	,00017808	,00019178	,00020548
3	,00024657	,00026712	,00028767	,00030822
4	300 032877	,00035616	,00038356	,00041096
5	,00041096	,00041520	,00047945	,00051363
6	,00049315	,00053421	,00057534	,00061644
7	,00057534	,00062328	,00067123	,00071917
8	,00065753	,00071232	,00076712	,00082192
. 9	,000 <u>739</u> 72	,00080137	,00086301	,0 009246 5
Morth.	,00250000	,002708%3	,00291\$65	,00312500

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Table

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Table II. The Interest of one Pound per Annum.

Numb.	3 per Gent.	3 + per C.	3 2 per C.	3 4 per C.
I	0,03000000	0,03250000	0,03500000	0,03750000
2			0,0700000	
3	0,0900000	0,09750000	0,10500000	0,11250000
4	C,I 2000000	0,13000000	0,14000000	0,1500000
5	0,15000000	CI,6250000	0,17500000	0,18750000
6	0,18000000	0,19500000	0,2100000	0,22500000
7	0,21000000	C,22750000	0,24500000	0,26250000
8	C,2400000	0,2600000	0,28000000	0,3000000
9	C,27000000	0,2900000	0,31500000	10,33750000

Table I.	The	Intereft	of	ore	Pound	per	Diem.
----------	-----	----------	----	-----	-------	-----	-------

Lays.	4 per Cent.	4 + per C.	4 * per C.	4 ³ / ₄ per C.
I	,00010959	,00011644	,00012329	,00013014
2	,00021918	,00023288	,00024657	,00026027
3	,00032877	,00034931	,00036986	,00039041
4	,00043836	,00046575	,00049315	,00052055
5.	,00054794	,0005821 <i>9</i>	,00061643	,00065068
6	,00065753	,00069853	,00073973	,00078c82
7	,00075712	,00081507	,00086301	,00091096
8	,00087671	,00093151	,00098630	,00104109
9	,00098630	,00104794	,0011C959	,00117123
Month.	,00%333333	,00354186	,0037500	,0039587

Table II. The Interest of one Pound per Annum.

Ycars.	+ per Cent.	4 4 per C.	$4\frac{1}{2}per C.$	4 + per C.
I	0,04000000	0,04250000	0,04500000	0,04750000
2	0,7800000	0,0850000	0 ,090000 0	0,09500000
3	0,12000000	0,12750000	0,13500000	0,14250000
4	0,16000000	c,1700000	0,1800000	0,1900000
5	0,20000000	0,21250000	0,22500000	0,23750000
Ğ	0,24000000	0,25500000	0,27000000	3,28500000
7	0,2800000	0,29750000	0,31500000	0,33250000
8		0,3400000		
9	0,36000000	0,38250000	0,40500000	0,42750000



Table	I. Th	e Interest	of	one	Pound	per Diem.
-------	-------	------------	----	-----	-------	-----------

Days.	5 per Cent.	5 4 per C.	5 2 per C.	5 4 per C.
I	,00013698	,00014383	,00015068	,00015753
2	,00027397	,00028767	,00030137	,00031507
3	,00041096	,00043151	,00045205	,00047260
4	,00054794	,00057534	,00060274	,00063014
5	,00068493	,00071918	,00075342	,00078767
6	,00082192	,00086301	,00090411	,00094520
7	,00095890	,00100685	,00105479	,00110274
8	,00109589	,00115068	,00120548	,00126027
9	,00123288	,001 29452	,00135616	,00141781
Month.	,0041#6666	,00437500	,00458733	,00479186

Table II.	The	Intereft	of o	ne Pound	per	Annum.
	A 176	Ture (1 c) .	- y - t		F	

Years.	5 per Cent.	5 4 per C.	5 2 per C.	5 ± per C.
1	0,05000000	0,05250000	0,05500000	0,05750000
2			0,11000000	
3	0,15000000	0,15750000	0,16500000	0,17250000
4			0,22000000	
5				0,28750000
6	0,3000000	0,31500000	0,3300000	0,3450000
7	0,35000000	0,36750000	0,38500000	0,40250000
8			0,4400000	
9	0,45000000	0,47250000	0,49500000	0,51750000

Table I. The Interest of one Pound per Diem.

Days.	6 per Cent.	6 ¹ / ₄ per C.	$6\frac{1}{2}$ per C.	6 ³ / ₄ per G.
I	,00016438	,00017123	00017808	,00018493
2	,00032876	,00034246	00035616	,00036986
3	,00049315	,00051370	00053424	,00055479
4	,00065753	,00068493	00071232	,00073972
5	,00082192	,00085616	.00089041	,00092466
6	,00098630	,00102740	00106849	,00110959
7	,00115008	,00119863	00124657	,00129452
8	,00131507	,00136986	00142465	,00147945
9	,00147945	,00154109	00160274	,00166438
Month.	,00500000	,00520833	00541856	,00562500

Table

Table II. The Interest of one Pound per Annum.

Years.	6 per Cent.	6 4 per C.	6 2 per C.	6 1 per C.
· 1	0,06000000	0,06250000	0,06500000	0,06750000
2		0,1250000		
3	0,18000000	0,18750000	0,19500000	0,20250000
4	0,24000000	0,2500000	0,2600000	0,2700000
5	0,3000000	0,31250000	0,32500000	0,33750000
6	0,36000000	0,37500000	0,3900000	0,40500000
l 7	0,12000000	0,43750000	0,45500000	0,47250000
8		0,5000000		
9	0,54000000	0,56250000	0,58500000	0,60750000

Table I. Th	Interest	of one	Pound	per Diem.
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Days.	7 per Cent.	7 4 per C.	7 1 per C.	7 4 per C.
I	,00019178	,00019863	,00020548	,00021233
2	,00038356	,00039726	,00041096	,00042466
3	,00057534	,00059589	,00061644	,00063699
4	,00076712	,00079452	,00082192	,00084932
5	,00095890	,00099315	,00102739	,00106164
6	,00115068	,00119178	,00123288	,00127397
7	,00134246	,00139041	,00143836	,00148630
8	,00153425	,00158904	,00164384	,00169863
9	,00172603	,00178767	,00184932	,00191096
Mouth.	,0058,333	,00604186	,00525000	,00645833

Table II. The Interest of one Pound per Annum.

Years.	7 per Cent.	7 4 per C.	7 2 per C.	7 + per C.
1	c,97000000	0,07250000	0,07500000	0,07750000
2	5,14000000	C,14500000		0,15500000
3	0,21000000	0,21750000	0,22500000	0,23250000
4	0,28000000	0,2900000	0,3000000	0,3100000
5	0,35000000	0,36250000	0,37500000	0,38750000
6	0,42000000	0,43500000	0,4500000	0,4650000
7	3, 4 <i>9</i> 00000	0,50750000	0,52500000	0,5425000
8	<i>ว</i>,56000000	0,58000000	0,6000000	0,6200000
9	5,6300000	0,65250000	0,67500000	0,69750000

Table

Decimal Tables of Simple Interest. 215

Table I. The Interest of one Pound per Diem.

Days.	8 per C.	8 + per C.	8 ÷ per C.	8 ³ / ₄ per C.
1	,00021918	,00022603	,00023287	.00023973
2	,00043835	,00045205	,00046575	,00047945
3	,00065753	,00067808	,00069863	,00071918
4	,00087671	,00090411	,00093150	,00095890
5	,00109589	,00113014	,00116438	,00119863
6	,00131507	,00135616	,00139726	,00143835
7 '	,00153425	,00158219	,00163013	,00167808
8	,00175342	,00180822	,00186301	,00191781
9	,00197260	,00203424	,00209589	,00215753
Month!	,00666666	,00687500	1,00708,33	,00729166

	Table I	I. The	Intereft	of	one	Pound	per	Annum.
--	---------	--------	----------	----	-----	-------	-----	--------

Years.	8 per Gent.	8 4 per C.	8 ; per C.	8 ; per C.
I /	0,08000000	0,08250000	0,08500000	0,08750000
2	0,16000000	0,16500000	0,1700000	0,17500000
3	0,24000000	0,24750000	0,25500000	0,25250000
4	0,32000000	0,3300000	0,3400000	0,3500000
5	0,4000000	0,41250000	0,12500000	0,43750000
6	0,1800000	0,49500000	0,5100000	0,52500000
7				0,61250000
8				0,7000000
9	0,72000000	0,74250000	0,76500000	0.73750000

Table I. The Interest of one Pound per Diem.

Days.	9 per Cent.	9 + per C.	9 + per C.	9 ; per C.
I	,00024657	,00025342	,00026028	00026712
2	,00049315	,00050084	,00052055	00052424
3	,00073972	,00076027	,00078082	00080137
4	,00098630	,001013 7 0	,00104109	00106849
5	,00123287	,00126712	,00130137	00133561
• 6	,00147915	,do152055	,00156164	00160274
7	,00172602	,00177397	,00182192	00186986
8	,001 <i>9</i> 7260	,00202739	,00208219	00213699
9	,00221918	,00228082	,00234246	00240410
Month.	,00750000	,00770833	,00791\$66	00812500

Table

Table II.	The 1	Interest of	one Pound	per 1	Annum.
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Years.	9 per Cent.	9 4 per C.	9 ½ per C.	9 ³ per C.
I	0,09000000	0,09250000	0,09500000	0,09750000
2	0,1800000			0,19500000
3	0,27000000	0,27750000	0,28500000	0,29250000
4	0,36000000			0,3900000
5	0,45000000	0,46250000	0,47500000	0,48750000
6	0,54000000	0,55500000	0,57000000	0,5850000
7	0,63000000			0,68250000
8	0,72000000	0,7400000	0,7600000	0,7800000
9	0,81000000	0,83250000	0,85500000	0,87750000



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TABLE M.

· 6

Of SIMPLE INTEREST.

The Rebate or Difcount of one Pound for Days, at the Rates of 2; 2¹/₂; 3; 3¹/₂; 4; 4¹/₃; 5; 6; per Cent. per Annum.

Days.	2 per Cent.	2 ½ per C.	3 per Cent.	3 ' per C.
I	,0000548	,0000685	,0000822	,0000959
2	,0001096	,0001370	,0001644	,0001917
3	,0001644	,0002054	,0002465	,0002876
•4	,0002191	,0002739	,0003287	,0003834
5	,0002739	,0003424	,0004108	,0004792
6	,0003287	,0004108	,0004929	,0005750
7	,0003834	,0004792	,0005750	,0006 7 08
8	,0004382	,0005477	,0006571	,0007666
9	,0004929	,0006161	,0007392	,0008623
10	,0005477	,0006845	,0008212	,0009580
20	,0010947	,0013680	,0016411	,0019141
30	,0016411	,0020506	,0024597	,0028685
40	,0021870	,0027322	,0032769	,0038210
50	,0027322	,0034139	,0040928	,0047716
60	,0032769	,0040928	,c049073	,0057205
70	,0038210	,0047716	,0057205	,0066676
80	,0043644	,0054496	,0065324	,0076128
. 9 5	,0049073	,0061266	,0073429	,0085563
; I 00	,0054496	,0068027	,0081522	,0094985
110	,0059913	,0074779	,0089601	,0104379
120	,0065324	,0081522	,0097667	,0113760
130	,0070729	,0088255	,0105720	,0123123
140	,0076128	,0094980	,0113760	,0132468
150	,0081522	,0101695	,0121786	,0141796
160	,0086909	,0108401	,0129785	,0151106

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TABLE

118 Decimal Talles of Rebate or Discount.

TABLE III.

The Discount of one Pound for Days.

Days.	4 per Cent.	4 : per C.	5 per Cent.	6 per Gent.
I	,0001096	,0001233	,0001370	,0001644
2	,0002191	,0002465	,0002739	,0003287
3	,0003287	,0003697	,0004108	,0004929
4	,0004382	,0004929	,00054.77	,000657.1
5	,0005477	,0006161	,0006845	,0008212
6	,0006571	,0007392	,0008212	,0039853
	,0007665	,0008623	,00095,80	,0011494
7 8	,0008759	,0009853	,0010947	,0013133
9	,0009853	,0011084	,0012314	,0014773
10	,0010947	,0012314	,0013680	,0016411
				,
20	,0021870	,0024597	,0027322	,0032769
30	,0032769	,0036850	,0040928	,0049073
40	,0043644	,0049073	,0054496	,0065324
50	,0054496	,0061266	,0068027	,0081522
60	,0065234	,0073429	,0081522	,0097667
70	,0076128	,0085563	,0094980	,0113760
8 0	,0086909	,0097667	,0108401	,01 29780
90	,0097667	,0109741	0121786	,0145788
100	,0108401	,0121786	,0135135	,0161725
110	,0119112	,0133802	,0148448	,0177610
120	,01 29800	,0145788	,0161725	,0193444
130	,0140465	,01577,46	,0174 9 <u>6</u> 6	,0209228
140	,0151006	,0169674	,0188172	,0224960
150	,0161725	,0181574	,0201342	,0240642
160	,0172321	,0193444	,0214477	,0256272
	1 301/2321	1,0173444	1 204144//	·

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Decimal Tables of Relate or Discount. 219

TABLE MI.

The Discount of one Pound for Days.

1 N				
Days.	2 per cent.	2 - per C.	3 per Cent.	3 2 per C.
170	,0092291	,0115098	,0137801	,0160399
180	,0097667	,0121786	,0145788	,0169674
190	,0103037	,0128465	,0153763	,0178932
200	,0108401	,0135135	,0161725	,0188172
210	,0113759	,0141796	,0169674	,01 <i>9739</i> 5
	F			
220	,0119112	,0148 448	,0177610	,0206601
230	,0124459	,0195091	,0185534	,0215789
240	,0129800	,0161725	,0193444	,0224959
250	,0135135	,0168350	,0201342	,0234114
260	,0140465	,0174966	,0209227	,0243251
		T	1	·····
270	,0145788	,0181574	,02171,00	0252270
280	,0191106	,0188172	,0224960	,0252370 ,0261473
29 0	,0156418	,0194762	,0232807	,0270558
300	,0161725	,0201342	,0240642	,0279627
310	,0167026	,0207914	,0248464	,0288679
			1 - 1 - E-H	
320	,0172321	,0214477	,0256273	020772
330	,0177610	,0221031	,0264070	,0297714
340	,0182894	,0227577	,0271855	,0306732
350	,0188172	,0234114	,0279627	,0315734
360	,0193444	,0240642	,0287387	,0324718
		,	,	,0333686
361	,0193971	0241204	,0288162	
362	,0193971	,0241294	0000002	0,334582
363	,0194490	,0241946	,0288937	° , 335478
364	0105550	,0242598	,0289712	0,336374
. <u>365</u> .	,01 <i>9</i> 5552 ,01 <i>9</i> 6078	,0243251	,0290487	0,337269
	- mininter		,0291262	033816#

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TABLE

220 Decimal Tables of Simple Interest.

TABLE III.

The Discount of one Pound for Days.

Days.	4 per Cent.	4 2 per C.	5 per Cent.	6 per Cent.
170	,0182894	,0205286	,0227577	,0271855
1 8 5	,0193444	,0217100	,0240642	,0287387
1 <i>9</i> 0	,0203972	,0228885	,0253672	,0302 8 69
200	,0214477	,0240642	,0 26 6667	,0318302
210	,02 24960	,0252370	, 0279627	,0333686
220	,0235420	,0264070	,0292553	,0349022
230	,0245858	^{,0275743}	,0305445	,0364309
240	,0256273	,0287387	,0318302	, 0379547
250	,0266667	,0299003	,0331126	,0394737
260	,0277038	,0310592	,0343915	,0409879
270	,0287387	,0322153	,0356671	,0424974
280	,0297714	,0333686	,0369393	,0440021
290	,0308019	,0345192	,0382082	,0455021
300	,0318302	,0356671	,0394737	,0469974
310	,0328564	,0368122	,0407352	,0484880
320	,0338804	, ⁰ 37 <i>9</i> 547	,0419948	,0499740
330	,0349022	,0390444	,0432503	,0514553
340	,035,7218	,0402314	,0445026	,0529320
350	,0369393	,0413657	,0457516	,0544041
360	,0379547	,0424974	,0469974	,0558717
				0560180
361	,0380561	,0426104	,0471218	,0560182
362	,0381575	,0427234	,0472462	,0561647
363	,0382588	,0428364	,0473705	,0563111
364	,0383602	,0429493	,0474948	,0564575
365	,0384615	,0430622	,0476191	.0566038

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The

The Nature, Construction, and Use of the Decimal Tables of Compound Interest.

What Compound Intereft is, I have already fhewn in the Theoretical Part of this Doctrine; and from the faid Theory it also appears that Tables of Compound Interest are absolutely neceffary for those who understand not Logarithms or Algebrs; and therefore (though I have taught the Use of Logarithms after the best Manner in this Book) yet I have supplied the Reader with a Set of Six Tables for the Purposes of Compound Interest; I have tramed them from the most compleat and approved Calculations of Mr. John Smart; his Book (which is wholly on Tables of Interest) having the best Character for Exactness, and the Errata's of the Press, no more than four.

As I intend nothing shall be wanting in any Part of this System, to make it compleat; so I have contrived these Tables to answer any Question of Compound Interest, for the Rates contained therein: For though they are not so large as the Largest, yet are they larger and more universal than any others, in any mixed Pieces of Arithmetick I have yet seen; I have chosen all the most usual and necessary Rates of Interest; and continued each Annual Table to 50 Years which is farther than is generally needful; and shall shew how they may be used for any indefinite Number of Years required; but first of their Construction, which is thus in the most demonstrative Manner deduced from the Theorems aforegoing, whence not only the Manner, but the Reason of their Construction (a Thing very necessary, though I know not where else to be met with) will be exceeding apparent.

The Confiruction of the First Table which shews the Amount of one Pound for Days, as also of the Second Table, which shews the same for Years, is made from Theorem 1. of Compound Interest, which is $PR^t = A$. Now if we put P 1 l. then is the Theorem reduced to $R^t = A$. Confequently, if R = 1,05 l. per Cent. (or any other Ratia) and R = 1, 2, 3, 4, Sc. Years;

Amount

Amonuts.

Then it will be R = A = 1.05 the first Year. Which mult, by R = 1.05The Product is $R^3 = A = 1.1025$ the second Year. And again by R = 1.05The Product is $R^3 = A = 1.157625$ the third Year. And again by R = 1.05The Product is $R^4 = A = 1.21550625$ the fourth Year.

And thus for the other Years fublequent in the Table.

Thus also if R = 1,00013368 the Ratio for 1 Day. Mult. as before R = 1,00013368

The Prod. is $R^2 = A = 1,00026738$ the Amount for 2D. And again by R = 1,00013368

The Prod. is $R^3 = A = 1,00040110$ the Amount for 3 D.

Thus is found the Amounts for all the subsequent Days in the Table.

Here it may be proper to observe, that the Amanet or Interest of any Sum, at the same Rate, is more at Compound Interest than at Simple, for any time above a Year; equal for one Year; but lefs for any time lefs than a Year. Though this forms strange in the left Allertion; yet the Reason is evident to any who understands and confiders that Simple Interest is grounded on Arithmetical, but Compound Interest on Geometrical Progression.

The Confiruction of Table 3. is by Theorem 2. viz. $\frac{A}{R_t}$ = P the prefent Worth or Value of one Pound, which is here to be confidered as the Amount; therefore if A = 1, R = 1,05 and t = 1, 2, 3, 4, 5, and Years, as before; 'tis evielent that Unity, or 1, being divided by the Numbers in the fecond Table (defigned by R) will give the Numbers in this third Table, or the prefent Values of 1h for the Tabular Years, and 5 per Cent. and fo for any other Rate of Intereft.

Example

of the foregoing Decimal Tables.

Henample at 5 per Cons.

The Confirultion of Table 4. is from Theorem 1. of Annuities, &cc. in Arrears, viz. $\frac{UR^{t}-U}{R-1} = A$. Now as it is U = 1. and R = 1,05 as before, then the Theorem will be brought to $\frac{R^{t}-1}{0,05} = A$, the Annuars of 1.1. Annuary for the Numbers of Years defign'd by t: That is, from (R^{t}) the Numbers in the ferond Table; fubfiract Unity, or 1. The Remainder divided by .05 (or R - 1) gives the Numbersin the fourth Table.

Example at 5 per Cent.

) :	ounts Innu-		อ้
2 99 99 1,1025 99 11 98 1,157625 1 11 19 10,21550625 10 11 1,27628156	4,31525 4,31012		3 }	CUL
道日 音 、2762815 6	18 €0 (5,52563	VE y D		

And thus you proceed for any other Rate of Intereft.

The Confiruction of Table 5. is contained in Theorem 1., of the prefent Worth or Value of Annuties, which fee; Now therein U = 1 l. and putting R = 1,05, and t = 1, 2,31, 4, 5; Sc. Years; that Theorem immediately becomes $R_{i} - I = P$, the prefent Worth fought. But in Confinction 0. of Table 4. 'twas them that $\frac{R_{i} - I}{\sqrt{5}}$ configured that Numbers of that Table. Therefore 'tis manifed, if the Num-t bers in Table 4. be divided by R^{t} (that is, by $1,05^{t}$, 1

Divide

212

224 The Nature, Confiraction, and U/e Divide the Numbers of the fourth Table, by the Numbers of the first Table, the Quotients make the fifth Table.

Table 1.Table 4.Table 5.1,05)1,00000 (=0,95238, Gc. for the 1ft Year.1,1025)2,05000 (=1,85941, Gc. for the 2d Year.1,157625)3,15250 (=2,72324, Gc. for the 3d Year.1,21550625)4,310125 (=3,54595, Gc. for the 4th Year.1,27628150)5,525631 (=4,32947, Gc. for the 5th Year, Gc.And thus for any other Rate of Interest.

The Confiruation of Table 6, is to be deduced from Theorem 2. of the prefent Worth of Annuities, Sc. which fee. Now fince in this Cafe P is = 1 l. therefore that Theorem will be reduced to this form, $RR^t - R = UR^t - U$; whence (at 5 per Cent.) 'twill be $0.5 R^t = UR^t - U$; confequently $\frac{0.5R^t}{R^t - 1} = U$ the Annuity required; but this being just the Reverse of $\frac{R^t - 1}{0.5 R^t}$, which make the Numbers of Table 5. 'tis plain, these two Theorems which conflitute the Numbers of Table 5. and 6. multiplied together can make but 1. that is $\frac{0.5 R^t}{R^t - 1} \times \frac{R^t - 1}{0.5 R^t} = 1$. Hence then if the Numbers of Table 5. be made Divi-

Hence then if the Numbers of Table 5. be made Divifors, and Unity or 1. the conflant Dividend, the Quotients thall be the Numbers which conflitute the fixth Table, at 5 per Cent. and after the fame Manuer for any other Rate of Interest.

Example at 5 per Cent.

à su	(,9523809)法产量 (1,05)-====(1):
ZEZ	1,8594103 (-5 E.B. ,5378	049 و 1 2 3
t sf		
- 5 a g	(1,05 1,8594103) 2,7232480 3,5459505 4,3294767) 3,5459505 4,3294767 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	

In like manner, when necessary, may other Tables be confuructed from the Theorems; Here are as many Tables as any Book (that I have feen) contains, and more than are in moft. My Aim in the Confiruction of these Tables is more to flew the

<u>r</u>___

of the Dec. Tables of Comp. Interest. 225

the young Artist the Rationale or Reason thereof, than the Manner how only; fince the latter has been often done, the former not at all that I know of; at least, not in the natural Method by Deduction from the Theory it felf, as I have here done it.

Quomedo failum eft ? Is a Question proper to Mechanicks ; Cur ita fit faciendum ? Beseems an Artist to enquire.

The Use of the following Tables.

The U_{fe} of all these Tables depends on this one obvious and eafy General Rule,

Multiply the Tabular Number, which flands against the given Number of Days or Years, and under the given Rate of Interest, by the given Principal Sum; and the Product will fatisfy the Question.

Example of 2461. at 5 per Cent. for 30 Days, or Years. In Table I. against 30 Days under 5 per C. stands 1,0040182 Which multiplied by the Principal Sum. 246 The Product is the Amount required ; viz. 1. 247,0684772 In Table II. Against 30 Years, at 5 per Cent. is 4,3219424 Which multiplied by 246 The Product is the Amount required ; viz. 1. 1063,1978 Bc. In Table III. Against the fame Time and Rate, is 0,2313775 Which multiplied by 246 The Product is the prefent Worth required ; 1. 56,9189 Bc. In Table IV. For the given Time and Rate, is 66,4388475 Which multiplied by 246 The Prod. is the A. of fuch an Annuity; 1, 16343,9565. Bc. In Table V. For the given Time and Rate, is 15,372451 Which multiplied by 240 The Prod. is the present W. of that Ann. 1. 3781,6229 Be.

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In Table VI. For the given Time and Rate, is ,c650514, Which multiplied by - 246 The Product is the purchased Annuily: 1. 16,5026 BC

Therefore by the Tables we immediately know, that 246 L forborne 30 Days, at 5 per Cent. per Annum Compound Intereft will amount to 247 l. 1 s. $4^{\frac{1}{4}}$ d.

That 2461. forborne 30 Years, at 5 per Cont. See. will A. mount to 10631. 3 s. 11 4 d.

That the present Worth of 246 l. due 30 Years hence, at the Rate of 5 per Cent. &c. is 56 l. 18 s. 3 4 d.

That the Amount of an Annuity of 2461. per Annum. forhome or unpaid 30 Years, at 5 per Cent. &c. is 163431. 19 s. 1 2 d.

That the present Worth of an Annuity of 2461. to continue 30 Years, at 5 per Cent, per Aunum, is 37811. 12 s. 5 ± d.

That the Annualty which 246 l. will purchase, to continue 30 Years, reckoning 5 per Cent. Istereft, is 16 l. per Annum.

If the Amount of any Sum be fought, for a Number of Days which are not in the first Table, and Years which are not in the facoud, observe this

Rule; Divide the given Number of Days, or Years, into two fuch Numbers as are in the Table, then multiply the Amounts pertaining to each, into each other; then thall the Produst be the Amount for the Time required.

Example 1.

What will 523L construct to, in 194 Hays, at 5 per Cent. per Annum? The two Parts of this Number in the Table, are 190, and 4; therefore,

In Table I. Against 190 Days, under 5 per C. is 1,0257228And against 4 Days, at the fame *Rate*, is 1,0005348The Prod. is the Am. of 1 l. for 194 Days, viz. 1,0262714Which multiply by the Principal Sum, viz. 523This Product is the Answer 1.5367399840In Maney, 536 l. 14 s. 9 J. d.

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of the Dec. Tables of Comp. Interest. 229

Example 2.

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What is the Amount of 1507. in 91 Fears, at 5 per Cent ?

In Table II. Against 50 Years, under 5 per C. is 11,4674000 And against 41 Years, at 5 per C. is 7,3919881

The Prod. is the Am. of 1 l. for 91 Years, viz. 84,7668833 Which multiply by the Principal Son, viz. 159 The Product is the Anliver _____ l. 12715,032495In Money 12715 l. 0 s. 7 $\frac{1}{3}$ d.

Example 3.

What will 923 l. amount to in 5 Years and 194 Days; # 5 per Gent?

In Table II. against 5 Years, at 5 per Cent. is 1,2762816And the Apr. of t l. in 194 Days, as above, is 1,0262914The Pr. is the Apr. of 1 l. in 5 Years, and 194 D. 1,3098113Which multiplied by the Principal Sum ______523 The Product is the Answer, viz. _____ l. 685,0313413 In Money 685 l. 0 s. 7 1 d.

N. B. The other Tables of Compound Interest, as they cannot in this Manner be extended, so they feldom require it.

I shall now present the Reader with a few Questions of a more complex Nature, and which frequently happen, in order to thew the more extensive Use of the Tables.

Question 1.

Suppose I have 7901. to be paki me within 7 Years, in this Manner; at the End of the first Year 901. of two Years, 1001. of four Years 2004 and of feven Years 9001. Quere what the prefent Worth of those several Payment's is in ready Money, allowing 4 3 per Cent. Compound Interest?

In

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In Table III. the present Worth of 1 l. at $4\frac{1}{2}$ per Cent. Due at the End of I Year, is C,9569378 Which multiply by the Principal 90 The Product is the present Worth of 90 l. = 86,124403 Thus the prefent Worth of 100 l. due at] 91,57299 the End of two Years, is found Alfo, if 2001. at the End of 4 Years **= 167,71**226 And of 400 l. at the End of 7 Years 293,93140 The Sum of all these is 1. 639,341052 Which answers the Question, viz. 6391. 6s. 91 d.

Question 2.

A owes to B 455% to be paid in 14 Years, viz. at the End of every 2 Years 65%. But he would agree to pay him in 7 Years, by equal Payments each Year; which B agrees to, and at the Rate of o per Cent. Compound Interest. Quere what the Annual Payment must be?

- I. Find the prefent Worth (by Table III.) of the 7 Payments which were at first to be made, as per Quest. I. which you will find to be 293 l. 3 s. 2 d.
- 2. Then find (by *Table VI.*) what Annuity, to continue 7 Years at the given Rate, 293 l. 5 s. 2 d. will purchafe; which you will find to be 52 l. 10 s. 8 d. and is the Answer to the Question.

Question 3.

A has a Term of 7 Years in an Estate of 351. per Annum. B has a Term of 14 Years in the same Estate in Reversion after the 7 Years; and C has a farther Term of 20 Years in Reversion after the 21 Years. Quere the present Values of the several Terms, at the Rate of 5 per Cent. per Annum?

By 7	Sable V. the prefent Valu			
found,	for 41 Years, to be for 21 Years, to be for 7 Years, to be	 •••	605 448	$ \begin{array}{c} s & a \\ 6 & & 0^{\frac{1}{2}} \\ 14 & & 9^{\frac{1}{2}} \\ 10 & & 5^{\frac{1}{2}} \end{array} $

Which

of the Dec. Tables of Comp. Interest. 229

Which substract from each other, it will appear,

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That the present Value of A's Term of B's Term of C's Term	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
For these Values answer the Question	1. 605 - 6 - 03

Question 4.

Which is most advantagious a Term of 15 Years in an Estate of 100 l. per Annum, or the Reversion of such an Eflate for ever after the Expiration of the faid 15 Years; computing at the Rate of 5 per Cent. per Annum Compound Intereft ?

An Eftate of 100 l. per Annum, in Fee } 1. 2000

Simple at 5 per Cent. is Worth ______ . 2000 In Table V. the prefent Value of the fame } 1. 1037,9658

The Difference is 1. 952,0342

Now this Difference being the Value of the Reversion, it appears that the first Term of 15 Years is better than the Reversion for ever afterwards by 75,9316 1. = 75 1. 18 s. $7\frac{1}{2}d$. Answer.

Question 5.

A Perfon having 12 Years to come, in a Leafe of an Eflate of 601. per Annum for 40 Years, would know what present Money he must pay in order to renew or compleat the Leafe by adding 28 Years thereto, computing at 6 per Cent. Compound Interest?

By Table V. the prefent Value of 1 l. per } 1. 15,046297

Annum, at 6 per Cent. for 40 Years, is By the fame Table the Value of 11. per An. at that Rate, for 12 Years to come, is 1. 8,383844

	The Difference is	1.	6,662453
	Which multiplied	by	63
The Product is In Money,	the Answer, viz	Ι.	399,747180

Queftion

Queftion 6.

A gives 1550 l. for an Annuity of 100 l. per Annum for 50 Years. B puts 1550 l. out at Intereft. It is required to know which will amount to the greateft Sum at the End of the 50 Years, at the Rate of 6 l. per Cent. &c. Compound Intereft?

By Table IV. the Amount of 100 l. Annuity, in 50 Years, at 6 per Cent. 29033,59046 may be found to be _____

By Table II. it may be found, that the Amount of 1550 l. for that Time and l. 28551,23883 Rate will be _____

Hence A's Annuity is more than B's 1550 l. by l. 452,35161 at the End of 50 Years. The preferit Value of which Difference is found, by Table NI. to be 201. 3 s. $8\frac{1}{3}$ d. and fo much was A's Cafe better than B's,

Question 7.

What Annuity to continue 14 Years, may be purchased with 1000 l. due at the end of 5 Years; the Annuity to comthence prefently, at 5 l. per Cent ?

By Table III. the prefent Worth of loog l, due 5 Years hence at 5 per Cent. l = 1.783,5262may be found -

By Table VI. it may be found, that the 3 = 1.79,1518 for 14 Years, at the Rate of 5 per Cent. is

In Money, 791. 3 s. 0 4 d. per Annum, the Aufwer.

Question 8.

For a Leale of certain Profits for 7 Years, A, makes two Offers, either to pay 150 l. as a Fine, and 300 l. per Annum; or 1700 l. Fine, without any Rent. B, bids 650 l. Fine, and 200 l. per Annum. And C, offers 200 l. Fine, and 405 l. per Annum. Quere which is the best Offer, and what the Difference, computing at 5.1. per Cent. &cc. Compound Intervise

1. By

of the Dec. Tables of Comp. Interest. 231
1. By Table II. the Amount of 1501 in 2 211,0659 7 Years, at 5 per Cent. may be found to be 2 211,0659 By Table IV. the Amount of 300 l. per Annum in 7 Years at the given Rate may 2 242,6025 be found
Therefore A's Offer, at the End of 7 Years } 1. 2453,6684
2. By Table II. the Amount of 17001. in 7 Years (A's fecond Offer) at the faid Rate, is found to be l. 2392,0802
3. By Table II. the Amount of 6501. in 7 Years, at the given Rate, will be found \$ 1. 914,6189 to be By Table IV. the Amount of 5.
By Table IV. the Amount of 2001. per Annum in 7 Years, at that Rate, will be 1. 1628,4016 found to be
Therefore B's Offer will, in 7 Years, a- } 1. 2543,0205 4. By Table II. the Amount of 200 l. in 7 Years, at the given Rate, will be found { l. 281,4212 By Table IV. the Amount of 405 l. per Annum for the given Time and Rate, will { l. 3297,5132 be found to be
So that C's Offer, in 7 Years, will amount to 1. 3578,9344
The Amounts therefore of the faid Offers, at the End of the faid Term, being thus known; the Prefent Worth of the feveral Amounts may be found by Table III. which are as follow.
L. s. d. The prefent Worth of A's first Offer will be 1885-18-03 A's fequed, Offer - 1700-00-00 B's Offer - 1807-05-06
C's Offer 254308 Therefore the prefent Worth of what C offers is more
than $-$ A's fitth Offer, by $657-14-5$ A's fecond Offer, by $843-9$
B's Offer, by - 786- 4-2 Which fully answers the Question.
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N. B. This

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N. B. This Queflion might be more readily answered by finding the prefent Worths of the several offer'd Annuities (as per Table V.) and adding to them the feveral Fines; as the Reader may try at his Leifure.

Question 9.

What Annuity is fufficient to pay off a Debt of 50 Milii. ons in 30 Years at 4 l. per Cent. Compound Intereft?

per Annum.

So that fuppoling the National Debt to be 50 Millions, and the Interest paid to be 2 Millions per Annum, or 4 l. per Cent. then will a Sinking Fund of 891505 l, per Annum, clear the whole Debt in 30 Years.

N. B. By this Example appears the Necessfity of continuing the Tabular Numbers to fo mary Places of Decimals.

Question 10.

Suppose one Farthing had been lent at Compound Interest at 5 per Cent. in the first Year of the Christian Æra, or Birth of Christ, and so continued to this present Year thereof 1734; Quere the Amount thereof?

N. B. Though this Quefilion might be answered by Table II. as I have before thewn, yet I thall here use Logarithms, as most expeditious in this Case. For having faid enough about the Use of the Tables, I here intend only to give the Reader a hint of the furprising Nature of Numbers in Geometrical Proportion.

Therefore, The Logarithm of the Rate 1,05=0,0211893 Multiplied by the Time ______ 1734 The Product is _______ 36,7422462 To which add the Logarithm of 1 Farthing, or the ,0010418 Part of a Pound, = 7,0177288piz. ______ The Sum is the Log. of the Amount fought = 33,7599750

Now

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Now the Index of this Logarithm being 33, flows the Number of Figures, of which the Amount of one Farthing in the given Time doth confift; to be 34, of which let it be fufficient to express the 4 first in Figures; the Reft in Cyphers; then will the faid Amount be

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Now the Value of a folid Body, perfectly Spherical, whole Diameter is 8000 Englifh Miles, (which is formewhat bigger than the Diameter of the Globe of our Earth.) I fay fuch a folid Body of fine Gold would be in Value about

Now if from each of these great Numbers, be cut off 23 Cyphers, the remaining Figures will be 57540000000 in the Amount of the Farthing; and 23866 in the Value of the Globe of Gold. But 23866) 57540000000 (=2400000nearly.

Hence it appears, That one fingle Farthing put out to Usury in the Manner aforesaid would amount to more in Value than two Millions and four bundred Thousand Glokes of fine folid Gold, each bigger than the Globe of the Earth! A firange and surprising, but no less certain Truth! And this immense Amount would be greatly increased by inlarging the Rate of Interest.

I shall now conclude this Part, by prefenting the Reader with a *small Table* concerning the prefent Worth or Value of *Effates* upon *Lives*, with its Ufe; This Table was at first composed by the Great and Learned Dr. Halley, for every Fifth Year of Age to the 70th, as follows.

ASC.	Year's Purchasé	Age	Year's Purchafe	Age	Year's Purchase
I	10,28	25	12,27	50	9,21
5	13,40	30	11,72	55	8,51
10	13;44	35	11,12	60	7,60
15	13,33	40	10,57	65	6,54
20	12,78	45	9,91	70	5,32

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The Use of the TABLE.

Suppose a Perfon of 50 Years of the offers to fell his Life in an Estate of 461. per Annum, what is the Value thereof in Really Money.

The Age of 50, is Years Purchate 9,21 Which multiply by the Annuity 46 The Product in the Answer 423. 23 r. 2 1 d. = 423.66

If it happen that a Life and a Reversion For for many Years after, be offered; 'twill be necessary to reduce the Year's Purchast into Years corosin, or Years of a Lease, by the Fifth Table; thus, Suppose I would find what Number of certain Years conversionds to 20,57 Years Furchase, and 5 per Cent. Look in Fishe V. under the given Rate, and I find the next neareft Value of Annuity of 11. per Annum to 10,57, to be 20,4772537, opposite to which is 17 Years, which afe to be added to the Years in Reversion, and then the Cafe is thus easily folved. Ranningle.

What is the preferit Worth of an Estate of 781. per annum clear Rout for 20 Years after the Death of a Perfor 40 Years of Age, at 6 per Cent?

The Age of 40 Years is 10,57 Years purchale, which in Mable V. gives 17 Years certain to come at 6 per Cent. Then 20 + 17 = 37 Years.

Years. 1.

Therefore the prefent Worth of 1 1. for 37-14,7367804 per Annum for the given have J for 17=20,4792597 The prefent Worth of 1 l. per Annum for 20= 4,2595207 Which multiply by the Annuity 78 The Prod. is the Aufwer 2321. 4 s. 11 d. = 1. 232,2426 146

TABLES

TABLES of COMPOUND INTEREST.

TABLE I.

The Amount of one Pound for Days; at the Rates of 2; 2; 3; 3; 4; 4; 4; 5, and 6 per Cent. per Annum.

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	Days.	2 per C.	2 + per C.	3 per C.	3 ‡ per C.
111	· · · · · · · · · · · · · · · · · · ·	1,0000542	1,0000676	1,0000809	1,0000012
		1,0001085	1,0001353	1,0001619	1,0001885
1	2	1,0091637	1,0002029	1,0002429	1,0002827
	7	1,0002170	1,0002706	1,0003240	1,0003770
	- Z	1,0002713	1,0003383	1,0004050	1,0004713
					-10004/-5
÷	4	TOODBOEE	T 000 4050		7 00026-6
-	6	1,0003255	1,0004059	1,0004860	1,0005656
1	. 7:	1,0003798	1,0004736	1,0005670	1,0006600
1		1,0004341	1,0005412	1,0096480	1,0007542
1	e .	1,0004884	1,0006090	1,0007291	1,0008486
	15	I,0005426	1,0006767	1,0008101	1,0009429
			THINNY		
1	· 20	1.0010856	1,0013439	1,0016209	1,0018867
1	go	1,0016289	1,0020315	1,0024324	1,0028315
1	40	1,0031735	1,0027007	1,0033445	1,0037771
	so .	1,0027163	1,0033882	1-0010572	1,0047236
	60	1,0032605	1,0040673	1,0048708	1,0056710
			TRYNAM		
Į	70	1,0038049	3,0047468	1,0056849	1,0066193
ł	80	1,0013497	1,9054267	1,0064996	1,0075685
1		1,0040947	1,0061071	1,0073151	1,0085186
ł	100	1,0054401	1,0067880	1,0081311	1,0094696
1	- 110 -	1,0059857	1,0074693	1,9089179	1,0104214
ł			-1-1-1-12	-14.66	-1
1					
	120	1,0055316	1,0081511	1,9997653	1,0113742
I	130	1,0070779	1,0988334	1,0105834	1,0123279
I	149	1,0976244	1,9995161	1,9114931	1,0132825
1	150	1,0081712	1,0101003	1,0122215	1,9142379
Į	160	1,0087183	1,0108829	1,0130415	1,0151943
4					

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TABLE

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TABLE I.

The Amount of one Pound, Compound Interest.

Days.	4 per C.	4 + per C.	5 per C.	6 per C.
I	1,0001074	1,0001206	1,0001336	1,0001596
2	1,0002149	1,0002412	1,0002673	1,0003193
3	1,0003224	1,0003618	1,0004011	1,0004790
4	1,0004299	1,0004824	1,0005348	1,0006387
5	1,0005374	1,0006031	1,0006685	1,0007985
6	1,0006449	1,0007238	1,0008023	1,0009583
7	1,0007524	1,0008445	1,0009361	1,0011181
8	1,0008600	1,0009652	1,0010699	1,0012779
2	1,0009675	1,0010859	1,0012037	1,0014378
. 10	1,0010751	1,0012066	1,0013376	1,001 5976
-		·		
20	1,0021513	1,0024148	1,0026770	1,0031979
30	1,0032288	1,0036243	1,0040182	1,0048007
40	1,0043074	1,0048354	1,0053611	1,0064060
• /	1,0053871	1,0060479	1,0067059	1,0080139
ୁ <u></u> ତ୍ର ତେ	1,0064680	1,0072618	1,0080525	1,0096244
70	1,0075501	1,0084773	1,0094009	1,0112375
80	1,0086333	1,0096942	1,0107511	1,0128531
	1,0097177	1,0109125	1,0121031	1,0144713
90 100	1,0108033	1,0121324	1,0134569	1,0160921
110	1,0118900	1,0133537	1,0148125	1,0177155
				-30+//+33
120	1,0129779	1,0145765	1,0161699	1,0193415
130	1,0140670	1,0158007	1,0175291	1,0209701
140	1,0151572	1,0170265	1,0188902	1,0226013
150	1,0102487	1,0182537	1,0202531	1,0242351
160 ·	1.0173412	1,0194824	1,0216178	1,0258715
	يبغ والمشارك والمساد			
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TABLE I.

The Amount of one Pound, Compound Interess.

ſ	Days.	2 per-C.	2 3 per 6.	3 per C.	3 1. per C.
	170	1,0092658	1,0115670	1,0138623	1,0161416
1	IBO ·	1,0098135	1,0122516	1,0146837	1,0171098
ł	190	1,0103615	1,0129366	1,0155057	1,0180689
1	200	1,0109098	1,0136221	1,0163284	1,0190288
	. 210	1,0114584	1,01,43081	1,0171518	1,0199897
	220	1,0120073	1,0149945	1,0179759	1,0209515
Ł	230	1,0125565	1,0156814	1,0188006	1,0219142
1	240	1,0131060	1,0163687	1,0196260	1,0228778
ł	250	1,0136558	1,0170565	1,0204520	1,0238424
4	260	1,0142059	1,0177448	1,0212788	£ ,0248078
	· 270	1,0147563	1,0184336-	1,0221062	1,0257741
L	280	1,0153070	1,0191228	1,0229342	1,0267414
	290	1,0158580	1,0198125	1,0237630	1,0277096
ł	- 300 -	1,0164093	1,0205026	1,0245924	1,0286786
	310	1,0169609	1,0211932	1,0254225	1, 0296486
1	320	1,0175127	1,0218843	1,0262532	1,0306195
	330	1,0180649	1,0225758	1,0270847	1,0315914
	340	1,0186174	1,0232679	1,0279168	1,0325641
ł	350	1,0191702	1,0239603	1,0287495	1,0335378
-	360	1,0197233	1,0246533	1,0295830	1,0345123
1	361	1,0E97786	1,0247226	1,0296664	1,0346098
	362	1,0198340	1,0247919	1,0297497	1,0347073
I	363	1,0198893	1,0248613	1,0298331	1,0348049
ł	364	1,0199446	1,0249306	1,0299165	1,0349024
	365	1,0200000	1,0250000	1,0300000	1,0350000

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TABLE I.

The Amount of one Pound, Compound Interest.

Dayı.	4 per C.	4 1 per G.	5: por C:	6 per C
170	1,0184350	1,0207226	1,0229843	1,0275105
180	1,0195299	1,0219448	1,0243527	10191522
190	1,0206261	1,0231774	1,0257228	I 0307964
200	1,0217233	1,0244120	1,0270949	10324433
210	T 0228218	1,0256481	1,0284687	1,0340928
230	1,0239215	1,0268858	1,0298444	1,03577450
230	1,0250233	1,0281249	1,031 2219	1 0373998
240	1,0261243	1,0293655	1,0326013	1,0390572
250	1,0272275	1,0306076	1,0339825	1,0407173
260	T,0283319	1,0318512	1,0353656	₹,0423800
				571 S 10 2 3
270	1,0294375	1,0330963	1,0367505	1,0440454
- 250	1,0305443	1,0343429	1,0381375	1,0457135
290	1,0316522	1,0355910	1,0395259	1,0473842
300	1,0327614	1,0368406	1,0409164	1,0490576
310	1,0338717	1,0383917	1,0423087	4,0509336
320	1,0349832	1,0393444	10437029	1,0524124
330	1,0360960	1.0405985	1,0450990	1,0540938
340	1,0372099	1,0418542	¥ 0464969	1,0557779
350	1,0383250	1,0431114	1 047 8 967	1,0574647
90 0	1,0394413	1,0443700	₹ ,04 <i>9</i> 29 8 4	1,0591542
361	1,0395530	1,0444960	1,0494387	1,0593233
362	1,0396648	1,0446220	1,0495790	1,0994924
363	1,0397765	1,0447479	1,0497193	1,0596616
364	1,0398882	1,0448739	1,0498596	1,0598308
365	1,0400000	1,0450000	1,0500000	1,0600000
4 50	<u> </u>			

TABLE

TABLE II.

Of COMPOUND INTEREST. The Amount of one Pound for Years, at the Rates of 2; 2; 3; 3; 3; 4; 4; 5; and 5; per Cent. per Annum.

i1,0200001,02500001,0300001,035000021,04040001,05062501,06090001,071225031,06120801,07689061,09272701,208717841,08243211,10381281,12550881,147523051,10408081,13140821,15927401,187686361,12616241,15969341,19485231,229255371,14868561,18868571,22987331,229255371,14868561,21840291,26677001,316809891,9509251,24886291,30477311,3628973101,21899441,28008451,38423381,4405987111,44337431,31208661,38423381,44599697121,46824171,34486881,42576081,5110686131,92360661,37651101,46853371,5639560141,81947871,41297381,51258971,6186945151,44586831,42576081,77339860171,40024141,52161821,65284761,7946755181,42924621,55965871,70243301,3574892191,45081111,59865011,75350601,9225013201,485994741,63861641,80011121,9897888211,51566631,67958181,86029452,0594314221,54597961,72157141,91610342,1315115231,57589921,76461061,97358652,2061144241,60843721,8	Years.	2 per C.	2 1 per C.	3 per C.	3 + per C.
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		1.020000	1 0280000		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$					
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	_	1.0612080	1.0768006	1,0009000	1,0712250
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	4	1.0824201	T. TO78178	1,092/2/0	1,1007178
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	र	1.1040808	1.1214082	·,1 2))000	1,175230
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		-,		1,1,92/40	1,1070003
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	*		1.1506004		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		1,1201024	* - 8868	1,1948523	
9 I,1950925 I,2485029 I,3047731 I,3628973 10 I,2189944 I,280845 I,3439163 I,4105987 11 I,2433743 I,3120866 I,3842338 I,4259697 12 I,2682417 I,3448888 I,4257608 I,5110686 13 I,2936066 I,3765110 I,4685337 I,5639560 14 I,8194787 I,4129738 I,5125897 I,6186945 15 I,8458683 I,4482981 I,5579674 I,6753488 16 I,5727857 I,4845056 I,6047064 I,7339860 17 I,4002414 I,5216182 I,6528476 I,7946755 18 I,4282462 I,5596587 I,7024330 I,8574892 19 I,4568111 I,5986501 I,7535060 19 I,4558111 I,5986501 I,7535060 19 I,4568111 I,5986501 I,7535060 19 I,4568111 I,5986501 I,7535060 19 I,4568111 I,5986501 I,7535060 19 I,5156663 I,6795818 I,8602945 2,0594314 22 I,5459796 I,7215714 I,9161034 2,1315115 23 I,5758992 I,7646106 I,9735865 2,2061144 24 I,5084372 I,8087259 2,0327941 2,2833284		1,1400050	1,10000)/	1,2298733	1,2722792
$\begin{array}{c c c c c c c c c c c c c c c c c c c $		1,1710593	1,2104029	1,2007700	1,3168098
III,2433743I,3120866I,3842328I,4599697I2I,2682417I,3448888I,4257608I,5110686I3I,2936066I,3785110I,4685337I,5629560I4I,8194787I,4129738I,5125897I,6186945I5I,8458683I,4482981I,5579674I,6753488I6I,3727857I,4845056I,6047064I,7339860I7I,4002414I,5216182I,6528476I,7946755I8I,4282462I,5596587I,7024330I,8574892I9I,4568111I,5986501I,7535060I,922501320I,4859474I,6386164I,8001112I,989788821I,5156663I,6795818I,86029452,059431422I,5459796I,7215714I,91610342,131511523I,5768992I,7646106I,97358652,206114424I,6084372I,80872592,03279412,2833284		1,1950925	1,2400029	1 ,3047731	1,3628973
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	10	1,2109944	4,2000047	1,3439163	I,4I05 987
$\begin{array}{cccccccccccccccccccccccccccccccccccc$					
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		I, 2 433743	1,31 20866	1,3842338	1,4599697
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		1,2682417	1,3448888	1,4257608	1,5110686
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	-		1,3785110	1,4685337	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	14	1,8194787	1,4129738	1,5125897	1,6186945
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	15	1,145868 3	1,4482981	1,5579074	1,6752488
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$					
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	16	1,3727857	1.4845056	1.6017061	1 7220860
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$. 17	1,4002114	1.\$216182	1.6528476	1.7046755
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	18	1,4282462		1.7024220	1.857/802
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	19	1,4568111	1.5986501	1.7525060	1.0225012
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	20	1,4859471	1.6286164	1.8061112	1.080-1888
22 1,5459796 1,7215714 1,9161034 2,1319115 23 1,5758992 1,7646106 1,9735865 2,2061144 24 1,5084372 1,8087259 2,0327941 2,2833284					-,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,
22 1,5459796 1,7215714 1,9161034 2,1319115 23 1,5758992 1,7646106 1,9735865 2,2061144 24 1,5084372 1,8087259 2,0327941 2,2833284	21	1.8146667	1.69058.9	T Shacast	
23 1,5768992 1,7646106 1,9735865 2,2061144 24 1,6084372 1,8087259 2,0327941 2,2833284		1.5450706	-10,00,00	1,0002945	20594314
24 1,5084372 1,8087259 2,0327941 2,2833284		1.5758000	7 76451061		2,1319115
		1.5084253		1,9735005	2,2001144
	•	1.6406050	r.8ca04-	2,0327941	2,2033284
-, -, -, -, -, -, -, -, -, -, -, -, -, -	-7 (1,8539441	2,0937779	2,3632449

TABLE

TABLE II.

The Amount of one Pound, Compound Interest.

I I, 2 J, 3 J, 4 J, 5 J, 6 I, 7 I, 8 I, 9 I, 10 I, 11 I, 12 J, 13 J, 14 J, 15 I, 16 J, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1	per C. 0400000 0816000 1248640 1698586 2166529 2653190 3159318 3685691 4233118 4802443 5394541 60010322 6650735 77316764	4 1 per C. 1,0450000 1,0920250 1,1411661 1,1925186 1,2461819 1,3022601 1,3608618 1,4221006 1,4860951 1,5529694 1,6228530 1,6958814 1,7721961	5 per C. 1,0500000 1,1025000 1,1576250 1,2155063 1,2762816 1,3400956 1,4071064 1,4774554 1,5513282 1,6288946 1,7103393 1,7958563 1,8156491	6 per C. 1,0600000 1,1236000 1,1210160 1,2624769 1,3382256 1,4185191 1,5036303 1,5938481 1,6894790 1,7908477 1,8982980 2,0121965 2,1329283
2 - J, 3 I, 4 I, 5 I, 6 I, 7 I, 8 I, 9 I, 10 I, 11 I, 12 I, 13 I, 14 I, 15 I, 16 I,	0816000 1248640 1698586 2166529 2653190 3159318 3685691 4233118 4802443 5394541 6010322 6650735	1,0920250 1,1411661 1,1925186 1,2461819 	1,1025000 1,1576250 1,2155063 1,2762816 1,340 3956 1,4071064 1,4774554 1,5513282 1,6288946 1,7103393 1,7958563	1,1236000 1,1910160 1,2624769 1,3382256 1,4185191 1,5036303 1,5938481 1,6894790 1,7908477 1,8982980 2,0121965
3 1, 4 1, 5 1, 6 1, 7 1, 8 1, 9 1, 10 1, 11 1, 12 1, 13 1, 14 1, 15 1, 16 1,	1248640 1698586 2166529 2653190 3159318 3685691 4233118 4802443 5394541 5394541 56010322 56650735	1,1411661 1,1925186 1,2461819 1,3022601 1,3608618 1,4221006 1,4860951 1,5529694 1,6228530 1,6958814 1,7721961	1,1576250 1,2155063 1,2762816 1,340 3956 1,4071064 1,4774554 1,5513282 1,6288946 1,7103393 1,7958563	1,1910160 1,2624769 1,3382256 1,4185191 1,5036303 1,5938481 1,6894790 1,7908477 1,8982980 2,0121965
4 1, 5 1, 6 1, 7 1, 8 1, 9 1, 10 1, 11 1, 12 1, 13 1, 14 1, 15 1.6	1698586 2166529 2653190 3159318 3685691 4233118 4802443 5394541 5394541 60010322 6650735	1,1925186 1,2461819 1,3022601 1,3608618 1,4221006 1,4860951 1,5529694 1,6228530 1,6958814 1,7721961	1,2155063 1,2762816 	1,2624769 1,3382256 1,4185191 1,5036303 1,5938481 1,6894790 1,7908477 1,8982980 2,0121965
4 1, 5 1, 6 1, 7 1, 8 1, 9 1, 10 1, 11 1, 12 1, 13 1, 14 1, 15 1.6	1698586 2166529 2653190 3159318 3685691 4233118 4802443 5394541 5394541 60010322 6650735	1,1925186 1,2461819 1,3022601 1,3608618 1,4221006 1,4860951 1,5529694 1,6228530 1,6958814 1,7721961	1,2762816 1,340 3956 1,4071064 1,4774554 1,5513282 1,6288946 1,7103393 1,7958563	1,3382256 1,4185191 1,5036303 1,5938481 1,6894790 1,7908477 1,8982980 2,0121965
5 1, 6 1, 7 1, 8 1, 9 1, 10 1, 11 1, 12 1, 13 1, 14 1, 15 1. 16 1,	2653190 3159318 3685691 4233118 4802443 5394541 6010322 6650735	I,2461819 I,3022601 I,3608618 I,4221006 I,4860951 I,5529694 I,6228530 I,6958814 I,7721961	I,340 3956 I,407 1064 I,4774554 I,55 13 282 I,6288946 I,7103 393 I,7958563	1,4185191 1,5036303 1,5938481 1,6894790 1,7908477 1,8982980 2,0121965
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	3159318 3685691 4233118 4802443 5394541 56010322 56650735	1,3608618 1,4221006 1,4860951 1,5529694 	1,4071064 1,4774554 1,5513282 1,6288946 	1,5036303 1,5938481 1,6894790 1,7908477 1,8982980 2,0121965
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	3159318 3685691 4233118 4802443 5394541 56010322 56650735	1,3608618 1,4221006 1,4860951 1,5529694 	1,4071064 1,4774554 1,5513282 1,6288946 	1,5036303 1,5938481 1,6894790 1,7908477 1,8982980 2,0121965
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	3685691 4233118 4802443 5394541 6010322 6650735	1,4221006 1,4860951 1,5529694 	1,4774554 1,5513282 1,6288946 	1,5938481 1,6894790 1,7908477 1,8982980 2,0121965
9 1, 10 1, 11 1, 12 1, 13 1, 14 1, 15 1. 16 1,	4233118 4802443 5394541 6010322 6650735	1,4860951 1,5529694 1,6228530 1,6958814 1,7721961	1,5513282 1,6288946 	1,6894790 1,7908477 1,8982980 2,0121965
10 I, 11 I, 12 I, 13 I, 14 I, 15 I. 16 I,	4802443 5394541 6010322 6650735	1,5529694 1,6228530 1,6958814 1,7721961	1,6288946 1,7103393 1,7958563	1,7908477 1,8982980 2,0121965
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	6010322	1,6958814 1,7721961	1,7958563	2,0121965
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	6010322	1,6958814 1,7721961	1,7958563	2,0121965
13 1, 14 1, 15 1. 16 1,	6650735	1,77 21961	1,7958563 1,8156491	2,0121965
14 1, 15 1. 16 1,	6650735 7216764		1,8156491	2,1329283
15 I. 	7216761			
<u> </u>	", J~~/ "T	1,8519449	1,9799316	2,2609039
	8009435	1,9352824	2,0789282	2,3965582
	8729812	2,0223701	2,1828746	2,5402517
17 1	9479005	2,1133768	2,2920183	2,6927728
	0258165	2,2084787	2,4066192	2,8543392
19 2	,1068492	2,3078603	2,5269502	3,0255995
	,1911231	2,4117140	2,6532977	3,2071355
21 2	,2787681	2,5202111	2,7859626	3,3995636
22 2	,3699188	2,0336520	2,9252607	3,6035374
23 2	,4647155	2,7521663	3,0715238	3,8197497
24 2	,5633042	2,8760138	3,2251000	4,0489346
25 2	6658363	3,0054344	3,3863549	4,2918707

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Dec. Tables of Comp. Inter. for 50 Years. 244

TABLE H.

The Amount of one Pound, Compound Interest.

				1
Years.	z per Cont.	2 - per C.	g per Gent.	3 7 per C.
26	1,6734189	1,9002927	2,1565912	2,4439585
- 117 -	1,7058864	1,9478000	2,2212890	2,5315871
28	117410242	1,9964950	2,2879276	2,6201719
29				2,7118999
-30	4,8113615	2,0975675	2,4272624	2,8067937
34	3. 8× 7258858		2. 5000804	2,9050314
32	7.88 A ENTO	2,2037509	0. 8425 199	2,300 576 4
33		2,2588308		
34		2,3153221		
35				3,3335904
		1		
:36				3,4502661
37				3,5710254
38				3,6960113
39	2,1047447	2,0195744	3,1070209	3,8253717
4•	2,2080390	2,0850038	3,2020377	3,9592597
41	2,2522004	2,7521904	3,3598989	4.0978338
42 ·	2,2979444	2,8209952	3,4606958	8,4,2412579
43	2,3431893	2,8915500	3,564516	4,3897020
44	2,3900531	2,9638080	3,671452	4,5433416
45	2.4378542	3,0379032	3,781595	84,7023585
46	2.4866112	2.1128208	1.805042	4,86694#1
47	2.5363425	2.1016071	LOI18040	5,03728+0
#8	2,5870702	2.271480	1,132251	15,2135889
49	2,6388117	12,2522768	1,256210	5,3960645
50	12,6915880	3,457108	1-3839060	5,5849208
·		,		

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TABLE II.

The Amount of one Pound, Compound Interest.

Years.	A per	Cent.	$4\frac{1}{2}$ per	<u>C. 5</u>	per C.	6 per Cent.
26			3,1406		5556727	4,5493829
27			3,28200		7334563	4,8223459
28			3,42969		9201291	5,1116866
29			3,5840		1161356	5,4183878
30	3,243	3975	3,7453	181 4,	3219424	5,7434911
31	3,373	1334	3,9138	574 4,	5380395	6,0881006
32	3,508	0587	4.08998	310 4,	7649415	6,4533866
33	3,648	3811	4,2740	301 5,	0031885	6,8405898
34	3,794	3163	4,46630	515 5,	2533480	7,2510252
35	3,946	0 8 89	4,66734	478 5,	5160154	7,6860867
36	4,103	9325	4,8773	784 5,	7918161	8,1472519
37	4,268	0 8 98	5,09680	504 6,	0814069	
38	4,438	8134	5,32621	192 6,	3854773	9,1542523
39	4,616	3659	5,56585	90 6,	7047511	
40	4,801	0206	5,81630	545 7,	0399887	10,2857178
41	4,993	0614	6,07810	09 7,	3919881	10,9028609
42	5,192	7839	6,35161	54 7,	7615875	11,5570326
43	5,400	4952	6,63743			12,2504545
44	5,616	5150	6,93612	129 8,	5 5 7 1 5 0 3	12,9854818
45	5,841	1756	7,24824	84 8,	9850078	13,7646107
46	6,074	8227	7,57441	96 9,	4342582	14,5904873
47	6,3178		7,91526		9059711	15,4659166
48	6, 70	5282	8,27145	55 10,	4012696	16,3938716
49	6 , 8 <u>3</u> 33	493	8,64367	1010	9213331	17,3775039
501	7,1066	8331	9,03263	62'11,4	4674000	18,4201541

TABLE

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TABLE III.

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i.

Of COMPOUND INTEREST.

The Prefent Worth of one Pound for Years, at the Rates of 2; 2; 3; 3; 3; 4; 4; 4; 5, and 6; per Cent. per Annum.

Years.	2 per C.	$2\frac{1}{2}per C.$	3 per C.	3 = per C.
. 1	,9803921	,9756097	,9708738	,9661836
2	,9611687	,9518144	,9 +25959	,9335107
3	,9423223	.,9285994	,9151417	,9019427
4	,9238454	,9059506	,888 48 7 ວ	,8714422
5	,9057308	,8838542	,8 626088-	,8419732
. 6	,8879713	,8622968	,8374843	,8135006
	,8705601	,8412654	,8130915	,7859910
7 8	,8534903	,8207465	,7894092	,7594116
ġ	,8357552	,8007283	,7664167	,7337710
10	,8203483	,7811984	,7440939	,7089188
11	,8042630	,7621447	,7224213	,6849457
12	,7884931	J7435558	,7013799	,6617833
13	J7730325	,7254203	,6839513	.6291041
14	,757875°	,7 077272	,6611178	,6177818
15	,7430147	,6904655	,6418619	,5968906
16	,7 28 <u>4</u> 458	,6736249	,6231669	,5767059
17	,7141625	,6571950	,6050164	,5572038
18	,7001593	,6411659	,5873946	,5383611
19	,6864307	,6255277	,5702860	,5201557
20	,6729713	,6102739	,5536758	35025659
21	,6597758	,5953862	\$ 5375493	,4855709
22	,6468390	,5858646	,5218925	,4691506
23	,6341559	,5666972	,5066917	,4532856
24	,6217214	,5528753	,4919337	,4379571
25	,6095308	,5393905	,4776056	,4231470

li 2

TABLE

244 Dec. Tables of Comp. Int. for 50 Years.

TABLE III.

The Prefent Worth of one Pound, Comp. Interest.

Years.	A DEM C.	4 - per C.	s per G.	te per C.
I	,9615385	,9542378	\$\$23810	,9433962
2	,9245562	,9157299	,0070295	,8899964
3	,8889964	,8762966	,8638376	,8396193
4	,8548042	,8385613	8227025	7920937
5	,8219271	,8024511	7835262	,7472582
6	,7903145	,7618957	,7462154	,7049605
1 (,7599178	,7348285	7106813	,0650571
- 7	,7306902	,7031851	,6768394	,6274124
9	,7025867	,6729044	,6446589	\$918985
10	,6755642	* , 6439277	,6139133	\$583948
		•		
11	°6495809	,6161987	,5846793	,5267875
12	°6245971	,5896639	5568374	,4969694
13	26005741	,5642716	,5303214	4688390
14	'577475I	\$5399729	1,5050679	,4423010
15	1. 15552645	\$,5 167204	4810171	,4172051
		*		
16	,5339082	,4944693	,4581115	3936463
17	,5133733	4731764	4362967	,3713644
18	,4936281	,4528004	,4155207	,3503438
19	,4745424	,4333018	\$8957340	3309130
20	4963870	,4146429	3768895	1,3118047
21	4388336	3967874	,3589424	,2941554
22	,4219554	,3797009	3418499	·,2775051
23	,4057263	,3633501	,3255713	,2617973
24	,3901215	3477035	,3100079	.2469786
25	,3751168	,3327306	,2953028	-,2329986

TABLE

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Dec. Tables of Comp. Int. for 55 Tones 243

TABLE IM.

The Prefent Worth of one Peund, Comp. Invergit

Yoors.	2 perC.	2 : pm 6.	apenG.	3- 13-
26	15975799	,526 2300	463694	4088978
27	,5858620	5138997	45 020 P	, 3050T23
28	5743746	5009770	,4370768	,3816443
29.	,5632123	,4886613	4P4344	,7687482
30.	,5520709	4767427	: ,4# 1986	,7 562 98 4
31	,5412460	1,469.2008	,329987E	, <u>3</u> 442 39 4
32	, 53063,73	1,4530006	3887370	·3325
35	1,5202207	-44 27930	\$,3770263	,3213417
34	,5100282.	1,48 090.93	3060449	-,3104 76 1
35,	5000276	1,42137EL	*,3597034	,19999769
				,47999.09
36.	,4002222	1,41 10237	· ,34 90924.	,2898927
1 77	1,4806109	1,401067E	1,384982g	,2800326
38	4711872	1,3912849	1,3252262:	,1705 81 9
38	1,4019482	- ,38174DA	1,7197936	,2614125
40	,4528934	1,3724306	1,3065968	,\$ 525 7 25
4	4449 1032	1,3033470	1.2996785	,24403M
42	-,43520#R	1,3544818	1,2889592	,4357 79 1
43	,1267688.	1,3458389	1,28014291	,2278099
44	,4184008	1,3374038	,27237E8	,4201023
45	,1101968	i ,32917 44	1,2644386	,1126594
46	,4031537	1 ,3211458:	1,2567365	,2054679
47	,3942684	, 3133129	,2492588	, 1 985197
48	,3865376	,7096782	,24 99988	,1918 065
49	,3789584	,2982458	,4457,00°	
50	1.337+5279	20004290	,234 9503	, 1853202
^{, ,y}	[] 37/ 4748.80	,2909422:	,2281071	K ,1790954

246 Dec. Tables of Comp. Int. for 50 Years.

TABLE III.

The Present Worth of one Pound, Comp. Interest.

Years.	<u>4 per C.</u>	4 * per C.	5 per C.	6 per C.
26	,3606892	3184025	,2812497	,2198100
27	,3468166	,3046914	,2678483	,2073680
28	3334775	,2915707	,2550936	,1 <i>9</i> 56301
29	,3206514	,27,0150	,2429463	,1845567
30	,3083187	,2670000	,2313775	,1741101
31	,2964603	,2555024	,2203595	,1642548
32	,2850579	,2444999	,2098662	,1549574
33	,2740942	,2339712	,1998762	,1461862
34	,2635521	,2238959	,1903548	,1379115
35	,2534155	,2142544	,1812903	,1301052
-72		,=:+=)++	<u></u>	
36	,2436687	,2050282	,1726574	,1227408
37	,2342969	,1961992	,1644356	,1157932
38	,2252854	,1877504	,1566054	,1092389
39	,2166206	,1796655	,1491479	,1030555
40	,2082890	,1719287	,1420457	,0972222
41	,2002779	,1645251	,1352816	,0917191
42	,1925749	,1574403	,1288396	,0865274
43	,1851682	,1506605	,1227044	,0816296
44	,1180464	,1441728	,1168613	,0770091
45	,1711984	,1379644	,1112965	,0726501
.46	,1646139	,1320233	,1059967	,0685378
47	,1582826	,1263381	,1009492	,0646583
48	,1521948	,1208977	,0961421	,0609984
49	,1463411	,1156916	,0915639	,0575457
50	,1407126	,1107097	,0872037	,0542884

TABLE IV.

Of COMPOUND INTEREST.

The Amount of one Pound per Annum, or Annuity, for Years; at the Rates of 2; 2; 3; 3; 4; 4; 4; 5, and 6 per Cent. per Annum.

Years.	2 per Cent.	2 1 per-C.	3 per Cent.	3 2 per C.
Ĩ	1,0000000	1,0000000	, 1,0000000	1,0000000
2	2,0200000	2,0250000	2,0300000	2,0350000
3	3,0604000	3,0756230	3,0909000	3,1062250
4	4,1216080	4,1525156	4,1836270	4,2149429
5	5,2040402	5,2563285	5,3091358	5,3024059
6	6,3081210	6,3877367	6,4684099	6,5501522
. 7	7,4342834	7,5474302	7,6624622	7,7794075
8	8,5829691	8,7361159	8,8923360	9,0516866
9	9,7546284	9,9545188	10,1591061	10,3684958
IÒ	10,9497210	11,2033818	11,4638793	11,7313931
11	12,1687154	12,4834663	12,8077957	13,1419919
I2	13,4120897	13,7955530	14,1920296	14,6019516
13	14,6803315	15,1404418	15,6177904	16,1130303
14	15,9739381	16,5189528	17,0863242	17,6769864
15	17,2934169	17,9319267	18,5989139	19,2956809
16	18,6392853	19,3802248	20,1568813	20,9710297
17	20,0120719	20,8647304	21,7615877	22,7050158
18	21,4123124	22,3863487	23,4144354	24,4996913
19	22,8405580	23,9460074	25,1168684	26,3971805
22	24,2973698	25,5446576	26,8703745	28,2796818
21	25,7833172	27,1832740	28,6764857	30,2694707
22	27,2989835	28,8628559	30,5367803	32,3289022
23	28,8449632	30,58,1273	32,4528837	34,460,4137
24	30,4218625	32,3490379	34,4264702	36,6665 282
25	32,0302997	34,1577639	36,4592643	38,9498567

TABLE

And Des. Tables of Comp. Int. for 50 Tears.

TABLE IV.

. 1

The Amount of I L. Annuity, Compound Interest.

	- han ban		<u> </u>	
Boars.	2 per .G.	2 per C.	3 per C.	3ª per C.
T	8,0000000	1,0000000	1,0000000	1,000000
	2,0400000	2;\$450000	2,950000	2,000000
:81 (3,1236000	3,1370250	3,1525000	3,1835000
4	4,2464640	4,1781911	4,2101250	4,8740016
-5	5,4263226	5,4709099	3, \$250 812	5,\$370930
4	·0,6320455	5,768891y	5,8019128	6,9753187
	7,8982945	8,0191518	6,1420084	6,8938378
\$	9,219.2002	9,8800136	9,5491089	9,8974681
9	10,5827953	10,8021142	11,0265643	11,4913162
a a	12,0061070	12,2682094	12,5776929	±3,1807958
RT.	12.486 1914	T2.8117988	TA. 9067871	14.9718435
12 -	15,0258045	15.4610218	15.0171265	16,0099420
43:	16,6268377	171500123	17.1120808	48,8 821385
14	110,2919112	18.0221004	140.0000200	41,0150667
ЪŠ	20,0235876	20,7840543	a1,5785536	03,2750707
16	121.8215011	07 91 09 96	23,6374918	The Kant AR
17 -	22.6075127	177 4 4 7 7 7 6	25,8403664	25,6725289 28,2128806
18	25.6454120	24,74,7009	28,1323847	30,0056534
19	27.6712201	20.0635625	30,5390039	33, 7 599925
20	29.7780780	31,3714220	33,0059541	36,7855920
21	31,9692017	33,7831368	75 +7	
22	34,2479698	125,103=300	35,7192518	
23	136,6178886	36,3033779	38,5052144	
24 24	39,0826041	41,6891963		46,995828
25	41.6150082	44,5652101		
~)	17-3-7.38003	144) 1	47,727098	3 54,8645128

Dec. Tables of Comp. Int. for 50 Years. 249

TABLE IV.

The Amount of 1 l. Annuity, Compound Intereft.

Years.	2` per Cent.	2 ÷ per C.	3 per Cent.	3 ½ per C.
26		36,0117080	38,5530422	41,3131017
27	35,3443238	37,9120007	40,7096335	43,7590602
28	37,0512103	39,8598008	42,9309225	46,2906273
29	38,7922345	41,8562958	45,2188502	48,9107993
30	40,5680792	4 3,9 02 7 032	47,5754157	51,6226773
31	42,3794408	46,0002707	50,0026782	54,4294719
32		48,1502775	52,5027585	57,3345025
33	46,1115702	50,3540345	55,0778413	60,3412101
34	48,0338016	52,6128653	57,7301765	63,4531524
35	49,9944776	54,9282074	60,4620818	66,6740127
36	3T,9943672	57,3014126	63,2759443	70,0076032
37	54,0342545	59,7339479	66,1742226	73,4578693
38	56,1149396	62,2272966	69,1594493	77,0288947
39	58,2372384	64,7829791	72,2342327	80,7249060
40	60,4019832	67,4025535	75,4012597	
41	62,6100228	70,0876174	78,6632975	88,5095375
42	64,6822233	72,8398078		
43	67.1594678	75.6608020	85,4838923	96,8486293
44	69,5026511	78,5523231	89,0484191	101,2383313
45	71,8927103	81,5161312	92,7198614	
46	74.2205645	84,5540344	96.5014172	110,4840315
47	76.8171758	87.65788<2	100,3965005	
48 48	79.2525102	90.8595824	104,1083960	120.2882566
49	81.0405607	04.1210729	108.5106179	125.6018156
50	84,5794015	97,4843488	108,5406479 112,7968673	130,9979102

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\$50 Dec. Tables of Comp. Int. for 50 Years.

TABLE IV.

The Amount of 1 l. Annuity, Compound Interest.

Years	4 per	Cent.	4 : per Cent.	5 per Cent.	6 per Cent.
26 27 28 29 30	47,08 49,96 52,96	17446 42144 75830 62863 49377	47,5706446 50,7113236 53,9933332 57,4230332 61,0070698	54,6691265 58,4025828 62,3227119	63,7057657 68,5281176 73,6397983
31 32 33 34 35	62,70 66,20 69,85	83352 14687 95274 79045 22248	68,6662452 72,7562263 77,0302565	75,2988294 80,0637708 85,0669594	84,8016774 90,8897780 97,3431647 104,1837546 111,4347799
36 37 38 39 40	81,70 85,97 <i>9</i> 0,40	03362 91497	91,0413443 96,1382048 101,4644249	101,6281388 107,7095458 114,0950231	119,1208667 127,2681187 135,9042058 145,0584581 154,7619656
41 42 43 44 45	104,81 110,01 115,41	95978 23817 28169	118,9247885 125,2764040 131,9138422	135,2317511 142,99333386 151,1420056	165,0476836 175,9505446 187,5075772 199,7580319 212,7435138
46 47 48 49 50	132,94 139,26 145,83	53 <i>9</i> 04 82060 37342	153,6726331 161,5879016 169,8593572	178,1194218 188,0253925 198.1266626	226,5081246 241,0986121 [256,5645288 272,9584006 290,3359046

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TABLE V.

Of COMPOUND INTEREST.

The Prefent Worth of one Pound per Annum, or Annuity for Years, at the Rates of 2; 2; 3; 3; 4; 4; 4; 5, and 6; per Cent. per Annum.

Years.	2 per Cent,	$2\frac{1}{2}perC.$	3 per Cent.	3 ½ per C.
1	0,9803922	0,9756098	0,9708738	0,9661836
2	1,9415609	1,9274242	1,9134697	1,8996943
3	2,8838833	2,8560236	2,8286114	2,8016379
4	3,8077287	3,7619742	3,7170984	3,6730792
5	4,7134595	4,6458285	4,5797072	4,5150524
6	5 602 1000	5.5081054	5 (1777.07.0	
_	5,6014309	5,5081254	5,4171914 6,2302829	5,3285530
78	6,471 <i>99</i> 11 7,3254814	6,3493906 7,17 01372	7,0196922	6,1145439 6,8739555
9	8,1622367	7,9708655	7,7861089	7,6076865
10	8,9825850	8,7520639	8,5302028	8,3166053
11 I	9,7868480	9,5142087	9,525624 I	9,0015510
12	10,5753412	10,2577646	9,9540040	9,6633343
13	11,3483737	10,9831839	10,6349553	10,3027385
74	12,1062487	11,6909122	11,2960731	10,9205203
15	12,8492635	12,3813777	11,9379351	11,5174109
16		13,0550027	12,5611020	12,0941168
17	13,5777093 14,2918719	13,7121977	13,1661185	12,6513206
18	14,9920313	14,3533636	13,7535131	13,1896812
19	15,6784620	14,9788913	14,32,37991	13,7098374
20	16,3514333	15,5891623	14,8774748	I4,2124033
21	17,0112092	16,1845486	15,4150241	14,6979742
22	17,6580482	16,7654132	15,9369166	15,1671248
23	18,2922041	17,3321105	16,4436084	15,6204105
24	18,9139256	17,8849858	16,9355421	16,0583676
1 25	119,5234565	18,4243764	17,4131477	16,4815146
		Kk		CARI

Kk 2

ABLI

252 Dec. Tables of Comp. Int. for 50 Years.

TABLE V.

The Present Worth of 1l. Annuity, Comp. Interes ?.

Years.	4 per Cent.	4 ½ per C.	5 per Cent.	6 · per Cent.
I	0,9615385	0,9569378	0,9523809	0,9433962
2	1,8860947	1,8726678	1,8594103	1,8333926
3	2,7750910	2,7489644		2,6730119
4	3,6298952	3,5875257	3,5459505	3,4651056
5	4,4518223	4,3899767	4,3294767	4,2123638
6	5,2421369	5,1578725	5,0756921	4,9173244
7	6,6020547	5,8927009	5,7 8 63734	5,5823815
7 8	6,7327448	6,5958851	6,4632128	6,2097939
9	7,4353314	7,2687905	7,1078217	6,8016923
10	8,1108955	7,9127182		7,3600871
. 11	8,7604763	8,5289169	8,3064142	7,8868747
12	9,3850733	9,1185808	8,8632516	8,3838440
13	9,9856473	9,6828524	9,3925730	8,8526831
14	10,5631223	10,2228253	9,8986409	9,2949840
15	11,1183868	10,7395457	10,3796500	9,7122491
16	11,6522949	11,2340151	10,8377695	10,1058953
17	12,1656680	11,7071914	11,2740662	10,4 77 2597
18	12,6592961	12,1599918	11,6895869	10,8276035
19	13,1339385	12,5932936	12,0853208	11,1581165
20	13,5903253	13,0079365	12,4622103	11,4699213
21	14,0291589	13,40,17239	12,8211527	11,7640767
22	14,4511142	13,7844248	13,1630026	12,0415818
23	14,8558405	14,1477749	13,4885739	12,3033790
24	15,2469619	14,4954784	13,7986418	12,5503576
25	15,6220787	14,8282089	14,0939445	12,7833562

Dec. Tables of Comp. Int, for 50 Yeasr. 353

TABLE Y,

The Present Worth of 11. Annuity, Comp. Intereft.

Yearş.	2 per C.	2 1 per C.	3 per Cent.	3 ± per C.
26	20,1210358	18,9506111	17,8768420	16,8903523
27	20,7068978	19,4640109	18,3270315	17,2853645
28	21,2812724	19,9648887	18,7641082	17,6670188
29	21,8443847	20,4535499	19,1884546	18,0357670
30	22,3964556	20,9302926	19,6004413	18,3920454
31	22,9377015	21,3954074	20,0004285	18,7362758
32	23,4683348	21,8491780	20,3887655	19,0688656
33	23,9885636	22,2918809	20,7657918	19,3902082
34	24,4985917	22,7237863	21,1318367	19,7006842
35	24,9986193	23,1451573	21,4872200	20,0006612
36	25,4888425	23,5562511	21,8322525	20,2904938
37	25,9694534	23,9573181	22,1672354	20,5705254
38	26,4406406	24,3485030	22,4924016	20,8410874
- 39	26,9025888	24,7303444	22,8082151	21,1024999
40	27,3554792	25,1027751	23,1147719	21,3550723
41	27,7994895	25,4661220	23,4123999	21,5991037
42	28,2347936	25,8206068	23,7013592	21,8348828
43	28,6615623	26,1664457	23,9819021	22,0626887
44	29,0799631	26,5038495	24,2542739	22,2827910
⁴⁵	29,4901599	26,8330239	24,5187125	32,4954503
46	29,8923136	27,1541696	24,7754490	22,7009181
47	30,2865820	27,4674826	25,0247078	22,8994378
48	30,6731196	27,7731537	25,2667066	23,0912443
49	31,0520780	28,0713695	25,5016569	23,2765645
50	31,4236059		25,7297640	23,4556179

TABLE

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TABLE V.

The Present Worth of z l. Annuity, Comp. Inter.

Years.	4 per Cent.	4 \$ per C.	5 per Cent.	6 per Cent.
26	15,9827678	15,1466115	14,3751853	13,0031663
27 28	16,3295844 16,6630618	15,4513028 15,7428735	14,6430336 14,8981272	13,2105342
20	16,9837132	16,0218885	15,1410735	J 3,406 1644 13,5907211
39	17,2920318	16,2888885	15,3724510	13,7648312
31 32	17,5884921 17,8735500	16,5443909 16,7888909	15,5928104 15,8026766	13,9290861 14,0840435
33	18,1476441	17,0228621	16,0025491	14,2302297
34 35	18,4111962 18,6646116	17,2467580 17,4610124	16,1 <i>929</i> 039 16,3741942	14,3681412 14,4982465
36 37	18,9082803	17,6660406	16,5468516	14,6209 8 72 14,7367 8 04
38	19,3678625	18,0499902	16,8678926	14,8460192
39 40	19,5844831 19,7927721	18,2296557 18,4015844	17,0170406 17,1590 8 62	14,9490747 15,0462969
41	19,9930500	18,5661095	17,2943678	15,1380160
42 43	20,1856250 20,3707931	18,7235498 18,8742103	17,4232074	I 5,3061730
45	20,5488395	19,0183831	17,5459118 17,6627732	
- 45	20,7200378	19,1563474	17,7740697	15,4558321
46	20,8846517		17,8800663	
47	21,0429342	19,4147088	17,9610155	15,5890282
48	21,1951289			
49 50	21,,414/00			

TABLE VI.

Of COMPOUND INTEREST.

The Annuity which one Pound will purchase for any Number of Years; at the Rates of 2; 2;;3;3;;4;4;5, and 6 per Cent. per Annum.

Years	o ver Cent	2 + per C.	a per Cent	2 1 per C
	2 per Gent.	2 T pt/ 9.	3 per cent.	<u>3 T per C.</u>
I	1,0200000	1,0250000	1,0300000	1,0350000
2	,5150495	,5188272	,5226108	,5264005
3	,3467547	,3501372	,3535304	,3569342
4	,2626238	,2658179	,2690271	,2722511
_ 5	,2121584	,2152469	,2183546	,2214814
6	,1785258	,1815499	,1845975	,1876682
7 8	,1545120	,1 574954	,1605064	,1635445
8	,1365098	,1394674	,1424564	,1454767
9	,1225154	,1254569	,1284339	,1314460
10	,1113265	,1142588	,1172305	,1202414
11	,1021779	,1051060	,1080775	,II1092C
12	,0945596	,0974871	,1004621	,1034840
13	,0881183	,0910483	,0940295	,0970616
14	,0826020	,0855365	,0885263	,0915707
15	,0778255	,0807665	,0837666	,0868251
16	,0736501	,0765990	,0796109	,0826848
17	,0699698	,0729278	,0759525	,0790431
18	,0667021	,0696701	,0727087	,0758168
19	,0637818	,0667606	,0698139	,0729403
20	,0611557	,0641471	,0672157	,0703610
21	,0587847	,0617873	,0648718	,0680366
22	,0566314	,0596466	,0627474	,0659321
23	,0546681	,0576964	,0608139	,0640188
24	,0528511	,0559128	,0590474	,0622728
25	,0512204	,0542759	,0574279	,0606740

TABLE

256 Dec. Tables of Comp. Inter. for 50 Tears.

TABLE VI.

The Annuity which one Pound will purchase, Compound Interest.

			•		
	Tears.	4 per Cent.	$4\frac{1}{3}$ per C.	5 per C.	6 per Cent.
	I	1,040000	1,0450000	1,0500000	1,0600000
	2	,5301961	\$339976	,5378049	5454369
	3	,3603485	,3637734	,3672086	,3741098
	4	,2754901	,2787437	,2820118	,2885915
	5	,2246271	,2277916	,230 9 748	,2 373964
•	6	,1907619	,1938784	,1970157	,2033626
	7	,1666096	,1097015	,1728198	,1791350
	8	,1485279	,1516097	,1547218	,1610359
	9	,1344930	sI375745	,1406901	,1470222
	IO	,1232909	,1263788	,1295046	,1358680
	11	,1141490	,1172482	,1203890	,1267929
	12	,1065522	,1096662	,1128254	,1192770
	13	,1001437	\$1032754	,1064558	,1129601
	14	,0946690	,0978203	,1010340	,1275849
	15	,0899411	,0931138	,0963423	,1029628
	16	,0858200	0,890154	,0922699	,0989521
	17	,0821985	0,854170	,0886991	,0954448
	18	so789933	0,822369	,0855462	,0923565
	19	,0761386	0,794073	,0827450	,0896209
	20	<u>50735818</u>	0,768761	,0802426	,0871846
	21	,0712801	,0746006	,0779961	,0850046
	21	,0691988	→ 725457	,0759705	,0830456
	23	,0673091	,0706825	,0741368	,0812785
	24	,0655868	,0689870	,0724709	,0796790
Į	25	,0640121	,0674390	,0709545	,0782267
	•				
					`A B L E

TABLE

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Dec. Tables of Comp. Int. for 50 Tears. 257

ŤABLE VI.

The Annuity, which one Pound will purchase, Compound Interest.

Tears.	2 Per Cent.	2 <u>+</u> per C.	3 per Cent.	13 ÷ per C.
26	,0496992	,0527688	,0559383	,0592054
27	,0482931	,0513769	,0545642	,0 <u>57</u> 8524
- 28	,0459897	,0500879	,0532932	,0566027
29	,0457784	,0488913	,0521147	,0554454
30	,0446499	,0477776	,0510193	,0543713
31	,0435964	,0467390	,0499989	,0533724
32	,0426106	,0457683	,0490466	,0524415
· 33	,0416865	,0448594	,0481561	;05 15724
34	,0408187	,0440068	,0473220	,0507597
34 35	,0400022	,0432056	,0465393	,0499984
36	,0392329	,0424516	,0458038	,0492842
37	,0385068	,0417409	,0451116	,0486133
38	,0378206	,0410701	,0444593	,0479821
39.	,0371711	,0404362	,0438439	•Q473878
40	,0363558	,0398362	,0432624	,0468273
41	,0359719	,0392679	,0427124	,0462982
42	,0354173	,0387288	,0421917	,0457983
43	,0348899	,0382169	,0416981	,0453254
44	,0343879	<i>,</i> 9377304	,0412299	,0448777
: 45	,0839096	£0372675	.30407852	,0444534
46	,0334534		,0403625	,0440511
47	,0330179	,03640671	,0399605	,0436692
~48` `	,0326018	,0360060	,0395778	,0433065
49	-0322040	-, 1 35 52 35	,0392131	,0429617
50	.0318035	.0352581	,0388655	,0426337

11 1 1

238 Dec. Tables of Comp. Inter. for 50 Teurs.

TABLE VL

The Annuity which one Pound will purchase, Compound Interest.

Years.	A per Cent.	4 - per C.	5 per Cent.	6 per Cent.
26	,0625674	,0060214	,0095643	,0769044
27	,0612385	,0647195	-,0681919	,0756972
28	,0000130	,0035208	,0071225	,0745926
29	,0588799	30024140	,0,000455	,0735796
30	,05,78301	,0013915	,0550514	,0726489
31 8	,0568;54	,0004435	,0641321	,0717522
32	,0559486	,0595632	50632804	,0710023
33 :	,0551036	,0587445	,0624900	,0702729
34 0	,0543148	,0579819	,0617554	,0695984
35	,0535773	,0572705	,0610717	3068 <u>9739</u>
36	,0528869	,0566058	,0004345	,0683948
37	,0522396	,°5'59840	,05 <i>9</i> 8398	,0678574;
38	,0516319	,0554017	j0 <u>5</u> 92842	, 0673581
39	,05 10608	,0548557	10587640	,0668938
40	,0505235	<u>,0543431</u>	sa582782	,0664915
41	;0500174	0,538616	,05 78223	,0660589
42	,0495402	0,534087	59578947	,0656834
43	,04 90 899	0,529824	505 6 99 33	5065333 I
4 4	,0486645	°C,525807		005006 I
45	,0482625	0,522020	,0562617	,0047005
46	,0478821	,0518447	ja559282	,0644149
47	,0475219	,05:15073	ja5156+42	
48	-0471807	,0511886	£553184	SO638977
*49	- 60468571	,050\$872	,0550397	30686636
-19-1	.,84611021	,0505023	,25 47767.	,0684443

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IJ

CHAP.

CHAP.X.

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The Use of DECIMALS in Vulgar, Duodecimal, and Sexagefimal Fractions.

Kulgar Fractions in Decimals.

HAVE already shewn the Method of finding the Decimal equivalent to any Vulgar Praction, in Reduction; What I propose here, is to thew with how much greater Ease and Pleasure any of the Operations of Vulgar Fractions are wrought by Decimal Numbers. I shall exemplify the Matter in the common Rules as follows.

Additioz.

Example 1. What is the Sum of $\frac{7}{9}$ and $\frac{2}{7}$ of a Pound? Add $\begin{cases} The Desimal of \frac{7}{9} = .3777 \\ The Desimal of \frac{3}{7} = .4285 \end{cases}$ By the general Decimal Table, P. The Sum of both is = $l. 1,2062 = 1l. 4s. 1\frac{1}{2}d.$ Anf.

Example 2. What is the Value of $\frac{1}{16}$ and $\frac{5}{6}$ of a Shilling ?

Add The Decimal of $\frac{1}{16} = ,0625$ By the faid Ta-To the Dec. of $\frac{5}{6} \pm ,8333$ bie. Their Sum is ______ 0,89583 == 10 4 d. Anf. Example L12

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260 The Use of Decimals in the
Example 3. What is $\frac{2}{13}$, $\frac{3}{13}$ and $\frac{7}{13}$ of a Yard?
(The Decimal of $\frac{2}{13} = ,1538$)
Add \leq And the Dec. of $\frac{3}{13} = ,3307$ \geq By the Tab.
(And the Dec. of $\frac{7}{13} = .5384$)
The Sum, of Course, is $\frac{12}{13} = 0.9239 = 2 F. 9 In.$ An.
<i>Example</i> 4. What is the Value of $\frac{2}{3}$, $\frac{4}{5}$, $\frac{2}{9}$, and $\frac{3}{4}$
of $\frac{5}{0}$ of a Hundred Weight Averdupois?
The Decimal of $-\frac{2}{3} = .6666$
Add The Decimal of $-\frac{4}{5} = ,8000$ By the Table. The Decimal of $-\frac{2}{9} = ,2222$
Add { The Designed of 2 Table.
$1 = Detimar of \frac{1}{9} = \frac{1}{9} + \frac{1}{222}$
The Dec. of $\frac{3}{4}$ of $\frac{5}{6} = \frac{5}{8} =, 6250$
The Sum of all is $-C.2,3138=2:1:7:2$
Example 5. What Number of Years, do $476\frac{7}{11}$, $36\frac{9}{16}$,
$21\frac{10}{11}$, $7\frac{13}{14}$, $1\frac{14}{17}$ and $\frac{17}{19}$ of a Year, make?
$476\frac{7}{11} = 476,8363$
$36\frac{9}{10} = 36,5625$
These mixed Fractions $21\frac{10}{11} = 21,5090$
being fet down in order, $7\frac{13}{14} = 7,9285$ and the Decimals of the
and the Decimals of the 14 Fractional Parts being 14 = 1,8234
found in the General Table 1 17.
and fet down opposite there- to : add them, and their $\frac{17}{19} = \frac{0,8944}{-19}$
sum will be 19 545,7541 Years.
That is EAS Years a Months, 2 Weeks, and 2 Days nearly.
Substraction.

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Arithmetick of Vulgar Fractions. 261

Substraction.

Example 1. What is $\frac{5}{6}$ lefs $\frac{2}{8}$ of a Pound Sterling ? $-\frac{5}{6} = ,8_{333}$ By the gevent $-\frac{3}{8} = ,375$ By the gevent neral Deci-mal Table. From Substract - 0,4583 = 9s. 2d. Anf. There remains *Example* 2. What is the Value of $\frac{2}{3}$ of $\frac{7}{8}$ lefs $\frac{3}{4}$ of 2 of a Rod? From $-\frac{2}{3}$ of $-\frac{7}{8} = \frac{7}{12} = .583$ Subfract $\frac{3}{4}$ of $\frac{5}{9} = \frac{5}{12} = .418$ By the Table. There remains - 0,167 = 0Y. 2 F. 9 In. Example 3. What is $14\frac{2}{9}$, lefs $\frac{5}{7}$ of a Pound Troy 3 m - $14\frac{2}{9} = 14,222$ By the Table. i.e - $\frac{5}{7} = 0,7142$ by the Table. There remains - 13,5080 = 13:6:2From Take Example 4. What is $170\frac{17}{19}$, less $159\frac{9}{19}$ C. Weight, Averdupois ? From - $17c\frac{17}{19} = 170,8947$ By the Take - $159\frac{9}{19} = 159,4736$ By the Table. Table, There remains the Answer 11,4211 C. Multi_ 261

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Multiplication.

Bumple 1. What is $\frac{4}{7}$ of a Yang multiplied by $\frac{3}{9}$ of a Tand multiplied by $\frac{3}{9}$ of a

Multiply. - $\frac{4}{7} = ,5714$ By - $\frac{2}{9} = ,2$ (9),11428

The Product is 1 Fq. 20,3 Inq. == ,12697

Example 2. Suppose a Piece of Timber 14³/₇ Feet in Length, $\frac{8}{11}$ of a Foot Wide, and $\frac{1}{2}$ of $\frac{5}{8}$ of a Foot thick, What is the Solid Content of that Piece? Multiply the Length $-14\frac{4}{7} = 14,4285$ By the Width $-\frac{8}{11} = 92$ The Product will be found to be -10,49343That multiplied by the Thicknefs, which is $\frac{1}{2}$ of $\frac{5}{8} = \frac{5}{16}$ = 3125The Product is the Content fought = 3,27618, St.

That is, 3 Fest, 483 Inches, 46; Quarters, folid Content the Answer.

Example 3. There is a Ciflern $10\frac{1}{6}$ Feet in Length, $4\frac{5}{9}$ Deep, and $5\frac{4}{11}$ Wide; Quese how many Corn Gallons it will hold?

Multi-

Arithmetick of Vulgar Fractions.

- Multiply the Length $-10\frac{1}{6} = 10,10^{\circ}$ By the Width $-5\frac{4}{11} = 5,30^{\circ}$ That Product will be $-54,52630^{\circ}$ Multiply that by the Depth $-4\frac{5}{9} = 4,3^{\circ}$ The Product is the Solid Content $} = 248,3976$ Sec. Multiply that by the Gallons in a Solid Foot; viz. $\frac{13}{32}$ = 6,40625The Product is the Number of = 1591,2969 Sec.
 - Note; When there is given any Number of pure Fractions to be multiplied into one sneather; You may multiply the Numerators and Denominators into one another, and the Products will be a Fraction, whole Value in Decimals you may find as before taught,

Thus, $\begin{cases} Multiply <math>\frac{1}{9}, \frac{2}{7}, \frac{5}{11}, \frac{9}{17} \text{ all into torrestrictiver.} \\ \text{Then } 1 \times 2 = 2, 2 \times 5 = 10, 10 \times 9 = 90.7 \text{ to} \\ \text{And } 9 \times 7 = 63, \times 11 = 893, \times 17 = 993.7 \text{ to} \\ \text{But } \frac{30}{1309} = 0,00764 \text{ The Anference} \end{cases}$

Divifion.

Example 1. Divide $\frac{5}{7}$ by $\frac{3}{17}$

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264 The Use of Decimals in the	
Thus $\frac{1}{17} = 0,0588$, $71428s = \frac{5}{7}$ (12,14754 = The	
17 -00 7 (Anfwer.	
588 (ALLIWC.	
1262	
1176	
868	
588	
2805	
2352	
• 4437	
• 4437 4116	
· · · · · · · · · · · · · · · · · · ·	
. 3211 2940	
- 2714	
2352	
• 362	
The second and the second seco	
Example 2. What is $\frac{16}{19}$ divided by $\frac{2}{5}$ of $\frac{8}{15}$?	
Thus $\frac{2}{5}$ of $\frac{8}{15} = \frac{16}{75} = ,213$,842105263 $= \frac{16}{19}$	
5 15 75 3213/304210/203 19	
21 842105263	
,192 ,7578947368 (3,947368	
There is formewhat re- 576	
markable and uncommon in	
5th, 8c. Remainders, with	
the Numbers taken down, 768 confift of 2 Pair of the fame	
Figures; Secondly, That the 1414	
2d, 4th, Sc. Remainders, 1344	
with the Figures taken down,	
are just half the others; 576	
Thirdly, That where the Re-	
mainders of Pairs are prime 1313	
Numbers, the next is a Re- 1152	
mainder is a Pair of even 1616	
Numbers, and then goes on as before, as at the 5th and 1536	
sth. ··· 808 Ex-	

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Arithmetick of Vulgar Fractions. 265

Example 3. What is $2\frac{7}{18}$ of a Pound, divided by $\frac{10}{11}$?

Thus
$$\frac{10}{11} = ,50$$
 2,388 $= 2\frac{.7}{18}$
 $\frac{.56}{.54}$
 $\frac{.56}{.54}$
 $\frac{.70}{.56}$
 $\frac{.54}{.70}$
 $\frac{.70}{.53}$

Example 4. What is it per C. Weight, when $2I\frac{7}{11}C$. costs 67-7 Pounds? Thus $21\frac{7}{11} = 21, 6_3$ 67,4375 = $67\frac{7}{16}$ 674375 21 21,42) 66,763125 (3,11685 ?. 6426 1. 34 2502 2142 That is 3,116851. = 31. 2s. 4d. per C. the · 3611 2142 1511 Ánfwer. 14692 12852 18405 (17136 12690 10710 1980

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Extraction

The Use of Decimals in the

Extraction of Roots. Example 1. What is the Square Root of $\frac{25}{26}$?

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The Decimal of $\frac{25}{30} = ,694(,833 = \frac{5}{6} = \text{the Root}$ $\frac{64}{489}$ $1663) \cdot 544$ $\frac{489}{555}$

Example 2. Required the Square Root of the Surd Fraction $\frac{13}{17}$?

The Decimal of $\frac{13}{17} = .7647058$ Sc. the Root of which extracted will be .8744726 Sc. the Aniwer.

Example 3. Extract the Square Root of $58\frac{7}{9}$ The Decimal of the mixed Fraction $58\frac{7}{9} = 58,7$

Then extract thus; 58,7 (7,86 = $7\frac{2}{3}$ = the Root (foughr. 146) $\cdot 977$ 876 1526) 19177 9156 1023

Exam-

The Use of Decimals in, &c. 267

Example 4. Extract the Cube Root of $\frac{3}{16}$

This is beft (as being vafily fooneft and cafieft) done by Logarithms, thus,

From the Logarithm of the Numerator 3 = 0,4771212Subfiract the Logar. of the Denominator 16 = 1,2041200

There remains the Lagar. of the Dec. ,1875 = 9,2730012Add to the Index of that Logarithm 20 - ,29,2730012One Third of which Logarithm is ,29,2730012

One Third of which Logorithm is : the Logarithm of the Root fought \$.572358 = .9,7576670

The Cube Root then of $\frac{3}{16}$ is ,572358 which was to be found.

Example 5. What is the Cube Root of $512\frac{13}{15}$?

First, From the Logarithm. of the 2 - 13 = 1,113943Numerator of the Fractional Part 3 - 13 = 1,113943Substract the Logarith. of the Denominator 15 = 1,176091

There remains the Logarithm of the Dec. $,8\% = ,9,93785^2$ To which add the *integral* Part 512

The Cube Root therefore of 51213 is 8,0045

Note. The Use of Decimals is not only very obvious in all Parts of the Doctrine of Vulgar Fractions, but absolutely necessary in Extraction of Roots; which sometimes else cannot be done.

The Use of DECIMALS in Duodecimal Arithmetick.

Duodecimals are a Sort of Fractions made use of in Menfuration; Where one Foot is the Integer; The Foot is divided into twelve Parts or Inches; one of these, into twelve others, and so on dividing by twelve. Whence as ten is the Common Denominator in Decimals, so twelve is the Common Denominator in Duodecimal Fractions.

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The Notation and Reading of Duodecimals is

Thus *Feet, Primes, Seconds, Thirds, Fourths, &c.* 15 : *c*9 : *i*0 : *c*6 : *i*1 &*c.*

Now becaufe this kind of Arithmetic is useful to Performs concern'd in Building, Measuring, &c. and the most useful Parts, viz. Multiplication, Division, and Extraction, being by far the most difficult; I thought it very proper (and hope it will be very acceptable) to shew how those Operations may be most easily and speedily perform'd by Decimal Arithmetick.

To that End I have made the following Table for the ready converting any *Duodecimals* into *Decimals*, and the contrary. The Use of which, to those who understand any Decimal Tables at all, is very obvious and eafy.

Duode-	The Decimal Parts.						
cimals.	Primes. '	Seconds"	Thirds."	Fourths.""			
	,088333	,006944	,000578	,000048			
2.	,1\$6666	,013888	,001157	,000096			
3	,25	,020833	,001736	,000144			
4	333333	,027777	,002314	,000192			
5	,118566	,034722	,002893	,000241			
6	5	,041.666	,003472	,000289			
.7	,587333	,0486.11	,004051	,000337			
- 78 .	,656666	,C\$ 9555	,004629	,000386			
9	,75	,0625	,005208	,000435			
i	,833333	,069444	,005787	,000482			
11	,918666	,076388	,006365	,000530			

The Duodecimal Table.

This Table, as I faid, being fo easy, needs no Infiructions for its Use; nor thall I pretend to say *Decimals* are of any Service in the *Rules* of *Addition* and *Substraction* of *Duo decimals*.

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But

Duodecimal Arithmetick.

But their extream Utility in the aforefaid Operations of Multiplication, Division, and Extraction of Roots, of Duodecimals, will be underiably evident by the enfuing Examples.

Multiplication.

Example 1. What is 9 F, 10' multiplied by 8 F. 08'?

Multiply the Decimal of 9:10 = 9.83By the Decimal of 8:08 = 8.6

9) 5900

The Product is the Feet 78#66

Answer, viz. 5 85:2:8 = 85,222 Feet.

Example 2. What is the Product of 40 F. 09': 10"; by 11': 09"?

	Feet	•	,	••	.,,		r
Multiply the Decimal By the Decimal of	of 4 0	:	69	:	10	-	40,8194
By the Decimal of			11	:	09	===	,9791

In fuch Cafes where the Desimals run far, and terminate in Repetends, 'tis best to multiply by the contracted, or inperted Way, heretofore taught, thus;

•	`		40,81944 <i>1979</i> ,0
		. ,	36 7375¢ 285736 36737 468 272
			The second second second second second second second second second second second second second second second s

Answer. 39 F. 11': 07": 06" ; 06 = 39,96903 Feet.

Example

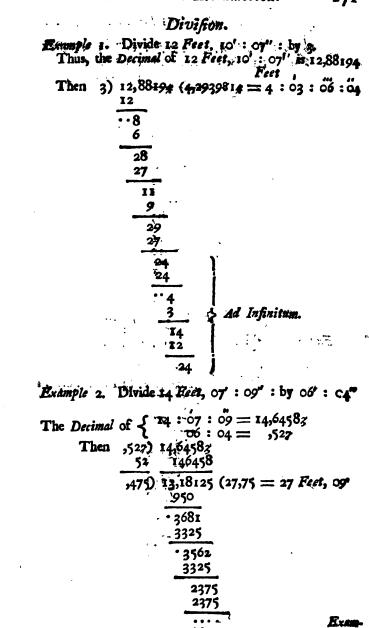
The Use of Decimals in

Example 3. What is 175 Feet, 00' : 04" : by 08"? Feet 1 11 **)** 11 Multiply the Decimal of 175:00 04:00:00 = 175,022 By the Decimal of **08 == ,000386** 1050166 14002222 52508333 The Profluict is 2 P The Product to Str. 1 N N N N N - 007560721 Makiply 17:09:02:06 == 17,76736 Example 4. By .6 == The Product is the Answer 106 F. 07' : 03" = 106,60416 Example 5. What is the Square of 12 Feet, 09':07"; TOM ? Thus S 12; 09: 07: 10 12: 09: 07: 10 Inverted 12,804399 93408,21 12804390 2560878 1024351 5121 384 115 Answer 163 Feet, 11' 05" 01" 09" = 163,95239

Division.

Duodecimal Arithmetick.

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The Use of Decimals in

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Example 3. Divide 5 Feet, by 1 Foot, 02': 03" : 11"
The Decimal of 1 Foot, 02' : 03" : 11" = 1,193865
Then $x = x \cos (86x) + \cos (2000) = (4.188079) = (4.18807$
4 775460 (4 F. 02': 03": 01""
4//)400 (41.02.00) 001
• 224540
119386
105154
95509
* •9645
9550
••94
83
II
10
•
Feet , all,
Example 4 {Divide 32: 10: 11: 06 = 32,913194 By 8: 01: 10: 11 = 8,159142
8:01:10:11=8,159142
Thus $8,159142$) $32,913194$ ($4,033904 =$
132636568 (4.F. 00 : 04": 10"
:• 276626
244774
* 31852

2447

7375 . 7343

> 32 32

> > Extraction

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The Use of Decimals, &c.

Extraction of Roots.

The Decimal of those Duodecimals is 163,95239, the Square Root of which extracted either by Logarithms or in the com-

F. , , , , , , , , , , , , mon way, gives the Side 12:09:07:10 for Anfwer.

By Logarithms

As in Vulgar, fo in *Duodecimal Fractions*, the *Extraction* of Roots, can be performed, no way fo well as by Decimal Parts; and the other Laborious Operations are hereby rendered eafy and concife.

The Use of Decimals in Sexagefimal Arithmetick.

Sexog: finals are those Fractions which have 60 for their common Denominator; and are chiefly used in Computations of Motion and Time.

Hence this Kind of Arithmetick is proper to Aftronomy, which, as it is a Science of Motion, and Time, makes use thereof in all its Calculations: Hereby it is the Aftronomer calculates the Motion, Place, Magnitude, Diftance, Time, Afpects, and other Phænomena of the Heavenly Bodies; the Sun, Moon, Planets, Comets, and Stars.

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The Notation and Reading of Sexagefimals is in this Manner following;

Viz. Viz. Sigrs, Degrees, Minutes, Seconds, Thirds, &c. Viz. C 05 : 26 : 57 : 53 : 47 &cc.

And as 60 is one Degree of Motion, fo it is one Hour of Time; hence Sexage fimals properly to called; begin only at Minutes, and go to Seconds, Thirds, &c. forwards, inboth Motion, and Time; though in common, it comprehends any Division of either.

But as all Aftronomical Calculations are made from Sexagefinal Numbers, already computed and disposed into **Tables** of various Sorts; if I would shew or demonstrate the Use of Decimals, and their Preference to Sexagefinal Numbers in these Kind of Computations; I must first suppose those Sexagefinal Tables, made into Decimal ones; and if such a thing were once done, I believe 'twould be no very hard Task to make good the Proposition afferted.

The Reader need only judge of this by the following Example of Addition in both Species.

	•	S	exag	e fin	ially.				Decimally.
	3		ð		1		11		5
	03		21	:	57	:	49	\equiv	3,73211
	11	:	29	:	47	:	58	=	11,9933 f
	10	:	18	:	59	:	37	=	10,63311
	09	:	25	:	17	:	43	=	9,84317
	c8	:	29	:	59	:	57		8,99996
	11	:	18	:	43	:	49	=	11,62433
Sum	c8	:	24	:	46	:	53		8,82601

In this Specimen I think 'tis eafy to observe how concile, fimple, natural and eafy the Operation by *Decimals* is if compared with the Sexagefimal Process; which therefore I think much needs prove the Freference and Excellency of those Tables in Decimals.

But fince none as yet have faid any thing about this Affair, nor have we any Aftronomical Tables in Decimals, I that give a Specimen thereof in the Mean Motions of all the Planets for one whole Year, Day, Hour, and Minúte, in the Table fubjoin'd.

Planets

Planets.	A Year.	A Day.	An Hour.	A Minute.
	<u>S.</u>	<u>s.</u>	<i>S</i> .	S.
Sun	11,99025 .	0,03285	0,001367	0,000018
Moon	4,31271	0,43921	0,018292	0,000294.
Saturn .	0,40709	0,00TLI	0,000046	0,000 000
Jupiter	1,01096	0,00276	0,000110	o,000000
Mars	6,37574	0,01749	0,000728	0,000009
Venus	7,49255	0,055340 -	10,00222 1	0,000036
Moresery.	1,70005 :	0,13639	0,005683	0,000092
L				

Such then is the Form, and fuch would be the Difference of Decimal and Sexage fimal Tables; The Numbers here are bomogeneous, all of one Sort; in them, they are beterogeneous, or confift of diverfe Sorts; here they are Uniform and to be wrote as integral Numbers, there they are ranged in a different Form and in diverfe Claffes, as all mixed Numbers are; befides the great Eafe and Facility of Working Decimal in Comparison of Sexage fimal 'Numbers, as I before observed. Upon all these Accompts, and several others I might mention, A Set of Astronomical Tables in Decimal Numbers must certainly be much more Useful, and every way preferable to the prefent Sexage fimal Tables.

After having turn'd your Sexage fimal Numbers into Decimals, they are to be worked in the fame Manner as Duodecimals through all the Rules, as is there taught; and therefore needs not be here again repeated. Only, I would here obferve, that the Rules of Multiplication and Division, which are here often neceffary, cannot be perform'd without a great deal of Difficulty, or a long and tedious Process, whereas by Decimals 'tis done with the utmost Facility and Expedition.

To this End, I have taken Care that the Reader should not want large and sufficient Tables for the expeditious turning of his Sexage fimals into Decimals, and the contrary; the like of which are not to be found elsewhere, that I know of.

CHAP. XI.

The Use and Management of DECIMALS (after a new Manner) by Logarithms.

HERE may chance to happen to the Reader a double Advantage in this Chapter; for first, he may here perceive, not only the common, but an entire nero Management of Decimals by Logarithms; and fecondly, he may here as well as any where learn the whole noble and excellent Art of Logarithmical Arithmetick, if he has not learnt it already; for Decimals and Integers having the fame effential Properties, the Logarithms of both are the fame, and differ only in their Indexes.

But that the young Student may the better understand how to vary and adjust the Index of the Logarithm, I have in the following Table given all Variety of Cafes that can happen to a Number, its Logarithm, and Index, under the various Conditions, and Denominations of Whole Number, Mixed Number, Pure Decimal, Repeating Decimals, Decimals with Cyphers prefixed, Sc. as follow.

			Index Logar.
Whole Numbers	*****		= 3,7195799
Mixed Numbers		52,43	$= 2,7195799 \\= 1,7195799 \\= 0,7195799$
A Perfe& Decimal		,5243	= 9,7195799
Decimals with Cyphers	prefixed §	,005243	= 8,7195799 = 7,7195799
A Single Repetend		3,	= 6,7195799 = 0,5228787
Mixed Single Re-	243	3 or 243	$= 1,6368221 \\= 2,3862016$
Compound Repetends	. 5243, <i>3</i>	S 4:3 2,43	$= 3,7196075 \\= 0,6378333 \\= 0,3860408$
• • •		(<i>\$</i> ,243	= 0,7196234

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			Ind	e x	Logar.
	7	,00003	-	5,52	28787
Compound Repetends with	2	,0004%	=	6,63	378332
Cyphers — —	7	,00243	_	7.38	362408
÷ .	L	,05243	=	8,7	196234
Mix'd Compound Repetends	کے ا	243	=	2,38	363 818
Mix a Compound Repetition	୍କ୍	52,43		1,71	196000
The fame with Cyphers	ہ کے	,000243		6,38	363818
and much with Cyplicis	ι	,005243	=	7,7	96000

From this general Scheme, the following Observations may be made relating to the Logarithm, and determining its Index for any Kind of Number.

Observation 1. That the Index of the Logarithm of any whole Number, is always one lefs than the Number of Places of Figures in the whole Number.

Observation 2. That the Logarithm of any Number, whether Integral, Mix'd, or wholly Decimal, is the very fame; only the Index differs and must be adjusted folely in regard of the integral Part of the Number; as per Observ. 1.

Observation 3. That if there be no integral Part but the Number is entirely *Decimal*, and the first left-hand Figure be one of the *nine Digits*, the *Index* is (\circ) .

Observation 4. That if the Number be entirely Decimal, and have any Number of Cyphers prefixed, the Index (being in this Case dotted on both lides) must be such as, when subfiracted from 9, the Remainder may express the Number of Cyphers prefixed.

Observation 5. That any Repetend, or Set of Circulating Numbers, whether Whole, or Decimal, observe all the Rules of terminate Numbers aforementioned, relating to the Index; but the Logarithm is different.

Observation 6. That the Logarithm varies, according as the same Figures are either terminate or repetends; and again as those Repetends make either a Part, or the Whole Number; or thus, the Logarithm is bigger or less as the first Figure of the Repetend is so.

As to what concerns the *Adding* and *Subfracting* of *Indexes*, that may be throughly understood by the following **Table of all the** *Varieties* that can happen in that Affair.

Addi_

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Addition.	Subfiraction.
1. To – 2,5132176	1. From - 4,3193976
Add – 1,8061800	Substract 1,8061800
Sum = 4,3193976	Rem. = $2,5132176$
2. To $-$,3,3916407	2. From - ,18,5957607
Add $-$,5,2041200	Take - ,3,3916407
Sum $=$,18,5957607	Rem. = ,5,2041200
3. To $-$ 2,2671717	3. From $-$ 0,4086215
Add $-$,8,1414498	Take $-$,8,1414498
Sum $=$ 0,4086215	Sum $=$ 2,2671717
4. To $-$,8,5132176	4. From $-$ 0,4086215
Add $-$ 3,8061800	Take $-$ 2,2671717
Sum $=$ 2,3193976	Sum $=$,8,1414498
5. Add 5,5,5132176 ,8,8061800	5. From
Sum = ,3,5865693	Sum = ,8,1414498

To understand the better what concerns the Ordering and Adjusting the *Indices*, in the foregoing Examples, I have subjoin'd the following *Scheme* of the Number of Cyphers, and their corresponding *Indices*.

Numb. of Cy. 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, Sc. Their Indic. 9, 8, 7, 6, 5, 4, 3, 2, 1, 0, 19, 18, 17, 16, 15, Sc.

Hence observe, In adding Indices, 1. If both be Affirmative, their Sum is Affirmative. 2. If both be Negative, and the Sum be under 10, add 10 thereto; but if above 10, or just 10, cast away 10; the Remainder is negative. 3. If one Index be affirmative, and the other negative; the Sum if under 10 is negative : it just 10, or above 10, cast 10 away; the Remainder is affirmative. after a new Manner by Logarithms. 279

In Subfracting Indices, observe, 1. If they are both Affirmative, and the Higher be the Greater, the Remainder is Affirmative; if the Lower be the Greater, the Remainder is Negative, (10 being added to the bigber.) 2. If one or both be Negative, and the bigber fmaller than the lower, add 10 to it; than if the bigber be of greater Value, the Remains are Affirmative; if not, they are Negative.

In order to understand the Art of Logarithms, and the dexterous Management of Numbers (more particularly *circulating* Decimal Numbers) thereby, 'twill be absolutely necessary to understand, and that perfectly well, the following Legarithmetical Problems.

- Rule. Begin at the Left-hand to fubfiract (mentally) each Figure from 9, and the last of all from 10.
 - Enam. What is the Arithm. Compl. of the Log. 3,8649262 Answer (per Rule) is = 6,1350738
- Problem 2. To find the Logarithm of any terminate Number under 10000000.
- Rule. Take the Logarithm out of the Tables to the four firft Figures of any given Number of above four Places, and also the next greater Logarithm; then take the Difference of thefe two Logarithms, and multiply it by the remaining Figures of the given Number; from the Product cut off to many Places of Figures to the Right-hand, as were the remaining Figures above four; then add the other Part of the Product to the Logarithm of the four Figures first taken out of the Canon; that Sum is the Logarithm fought.

Example. Required the Logarishm of 1012659?

The Logarithm of	$- \begin{cases} 1012 = \\ 1013 = \end{cases}$	3,0056094	• .
Their Difference Multiply by the remain	ning Figures	- 4289 6 59	•
The Product (with 3 Which add to the Log	Places cut off) partition of 1012=	2826,4 ====================================	51
The Sum is the Loga	richus	60054631 1	ought.
			Problem

Problem 1. To find the Arithmetical Complement of any given Logarithm.

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- **Problem 3.** A Logarithm being given, to find the Number belonging to the fame.
- **Rule.** Seek the next lefs Logarithm to the given one, in the Tables, and its four Figures are the first four of the Number required. Then take the Differences of the given Logarithm and the next lefs, and also the next greater and next lefs; Add to the first Difference, fo many Cyphers as you feek Figures more than four. Divide That by the second Difference, and the Quotient annexed to the four Figures first found compleats the Number required.

Example. Required the Number of the given Logarithms 6,0054631?

The Logarithm next lefs is -1012 = 3,0051805The Logarithm next greater is -1013 = 3,0056094The Diff. of the given Log. and next lefs is = 2826The Dift. of the next lefs, and next greater is = 4289

Then fay, As 4289 : 2826 ; : 1000 : 659, which annex to the first four Figures 1012, they compleat 1012659 the Number fought for the given Logarithm.

- Problem 4. To find the Logarithm of any terminate Decimal Number.
- Rule. Seek the Logarithm for it as though it were a whole Number, and then adapt the Index as before taught.

Thus the Logarithm of 1012,659 is 3,0054631, and of 1012659 = ,9,0054631, $\mathcal{C}c$.

- Problem 5. To find the Logarithm of a fingle Repetend, or circulating Digit.
- Rule. To the tabular Logarithm of the Digit, add the Arithmetical Complement of the Logarithm of 9, the Sum is the Logarithm fought.

Example. Required the Logarithm of 6?

To the Tabular Logarithm of 6 = 0.9781512Add the Arith. Complement of the Log. 9 = 0.0457575The Sum is the Logarithm fought of 8 = 0.8239087

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In this Manner I have calculated the Logarithms of all the Nine Digits perpetually circulating, and disposed them ready for Use in the annexed Table. Rep. Digits. Logarithms. x = 0.0457575 z = 0.3467875 3 = 0.5228787 4 = 0.6478175 5 = 0.7447275 6 = 0.8239087 7 = 0.8908555 8 = 0.9488475g = 1.000000

Problem 6. To find the Logarithm of any pure Compound Repetend.

Rule. To the Tabular Logarithm of the Number (as terminate,) add the Arithmetical Complement of the Logarithms of fo many 9's, as are Places of the Repetend; the Sum is the Logarithm of the given Repetend.

Example 1. Required the Logarithm of the Compound Repetend 24?

To the Tabular Logarithm of -24 = 1,3802112Add the Arithmetical Complement of 99 = 0,0043648The Sum is the Logarithm of -24 = 1,3845760

Example 2. Required the Logarithm of 36,3?To the Tabular Logarithm of -36,5 = 1,5622929Add the Arithmetical Complement of 999 = 0,0004345The Sum is the Logarithm of -36,3 = 1,5627274

Example 3. Required the Logarithm of 374%? To the Tabular Logarithm of -3746 = 3,5735678Add the Arithmetical Complement of 9999 = 0,0000434The Sum is the Logarithm of -374% = 3,5736112

Example 4. Required the Log with m of 200,60? To the Tabular Logarithm of -200,60 = 2,3023309Add the Arith. Comp. of the Log. of 99999 = 0,0000043The Sum is the Logarithm of 200,60 = 2,3023352

O o

Note.

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Note. In all the foregoing Examples (and in those which follow) the Indexes of the Arithmetical Complements are omitted; and this must be observed by the Learner in all Operations of this kind.

Problem 7. To find the Logarithm of any mixed Repetend, either Sirg'e or Compound.

Rule. From the given mix'd Repetend, substract its terminate Part; Then to the Legarithm of the Remainder add the Arithmetical Complement of the Logarithm of so many Nines, as there are Figures in the Repetend, the Sum will be the Legarithm sought.

Example 1. Requir'd the Logarithm of 2,6?

From the given Repetend Substract the terminate Part		2,8	
Substract the terminate Part		2	
Then to the Logarithm of Add the Arithm. Comp. of the	Logar. of	^{2,4} = 9 =	0,3802112 0,0457575
The Sum is the Logarithm	of 🛶	2,6 =	0,4259687

Example 2. Required the Legarithm of 57,27?

From the given Repetend			
Then to the Logarithm of	51,51 9		1,7118 915 0,0457575
The Sum is the Legarithm of	57,2 <i>3</i>	Ė	1,7576490

Example 3. Requir'd the Logarithm of 2,753?

From the given Repetend - 2,793 Subduct the terminate Part - 27

Then to the Logarithm of -2,726 = 0,4355258Add the Arith. Compl. of the Log. of 99 = 0,0043648The Sum is the Logarithm of -2,753 = 0,4398906

Example

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Example 4. Requir'd the Logarithm of 725,8?

From - - $7^{25,6}$ Subdust - - $7^{25,6}$ To the Logarithm of - $7^{24,9} = 2,8602781$ Add the Arit. Compl. of the Log. of 999 = 0,0004345The Sum is the Logarithm of - 725,6 = 2,8607126

Example 5. Requir'd the Legarithm of 268927?

From ______ 26892,7Subfract ______ 26To the Logarithm of ______ 26890,1 = 4,4295924Add the Arit. Comp. of the Log. of 9999 = 0,0000434The Sum is the Logarithm of ______ 26892,7 = 4,4296358

In the like Manner may the Logarithm of any other Mix'd Repetend be found, fo far as the Canon of Logarithms (you use) will permit.

Problem 8. Between two Numbers given, to find any Number of mean Proportionals required.

Rule. Substract the Logarithm of the leffer Number from the Logarithm of the greater; divide the Remainder by a Number greater by one than the Number of Means fought; this Quotient add to the Logarithm of the leffer Number; the Sum is the Logarithm of the first Mean; to which the faid Quotient is to be added again for the Logarithm of the fecond Mean; and thus proceed for as many Means as you please.

Oo2 Example

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Example. Between 8 and 56 to find four Mean Propertional Numbers.

The Logarithm of 56 is	1,748188 0 0, <i>9</i> 030 <i>9</i> 00
The Remainder or Difference is -	- 0,8450980
One fifth Part (for four Means) is -	- 0,1690196
To which add the Logarithm of 8 -	- 0,9030900
The Sum is the Log. of the first Mean 11,	B 09=1,0721096
To which add again	- 0,1690196
The Logarithm of the fecond Mean 27	,42=1,2411292
Add again -	0,1690196
The Logarithm of the third Mean is 25	,71=1,4101488
Add again -	0,1690196
Logarithm of the fourth and last Mean 37	94=1,5791684

This Problem I have chiefly inferted for their Sakes who would hereby learn to calculate Tables of Compound Intereft; The Numbers in the Table of Amounts of 1/. being only Mean Proportionals between the Logarithm of Rate and the laft Year's Amount in the Table.

Multiplication of all Kinds of Decimals by Logarithms.

Rule. Rule. To the Logarithm of the Multiplicand, Add the Logarithm of the Multiplier; The Sum is the Logarithm of the Product.

Example 1.	Multiply By		12,4 = 1,093421 3,6 = 0,556302	17 25
The	Product	` ~~ ~	44,64 = 1,649724	12
Example 2.	Multipl y By		36,5 = 1,562292 ,00019 = ,6,278753	:9 ;6
	Product		,006935 = ,7,841046	5

Example

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Example 3.	By $ 570 = 2,7558748$ Product $ 434,34 = 2,6378298$
Example 4.	Multiply - ,0097 = ,7,9867777 By - ,00021 :6,3222193 Product - ,000002037 :4,3089910
Example 5	Multiply $ 26,4 = 1,4216039$ By $ -$ By $ -$ Product $ -$
Example 6	Multiply $ 2,73 = 0,4361626$ By $ 2,8 = 0,4259687$ Product $ 7,28 = 0,8621313$
Example 7.	Multiply $,473 = ,9,6748611'$ By $ 83 = 1,8037053$ Product $ 30,1 = 1,4785664$
Example 8	
E xam p le 9	Multiply $ \delta, = 0.8239087$ By $, s =, 9.7447275$
Example 1	o. Multiply $-\frac{36,3}{2,4} = 1,5627274$ By $-\frac{2,4}{2,4} = 0.3845760$
Example 1	Product $88,5734218$ Sc. = 1,9473034 1. Multiply - $2x,23$ = 1,3265407 By - $4x,0$ = 1,6234581 Product - $300,718$ = $2,9499988$

Example

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Ecomple	I2.			,00420	-	,7,623458I
		By		,00008	=	,5,9488475
		Product	,000003;	735 Br.	=	,3,5723056

Division of all Kinds of Decimals by Loga-rithms.

Rule From the Logarithm of the Dividend, Substrast the Logarithm of the Divisor; The Remainder is the Logarithm of the Quotient.

Example 1.	Divide $-$ 44,64 = 1,6497242 By $-$ 12,4 = 1,0934217
·	The Quotient - 36 = 0,5563025
Example 2.	Divide $-310 = 2,4913617$ By $-4,275 = 0,6309361$
	Quotient $-72,51457 = 1,8604256$
Example 3.	Divide $-$ 434,34 = 2,6378298 By $,762 = ,9,8819550$
	Quotient - 570 = 2,7558748
Example 4.	Divide $-$,006935 $=$,7,8410465 By $-$ 36,5 $=$ 1,5622929
	Quotient $-$,00019 $=$,6,2787536
Example 5.	Divide $-$,000002073 $=$,4,3089910 By $-$,00021 $=$,6,3222193
	Quotient,0C97 = ,7,,3867717
Example 6.	Divide $-$ 176 = 2,2455126 By $ \ell_{0}$ = 0,8239087
	Quotient $-$ 26,4 $=$ 1,4216039
Example 7.	Divide $ 7,28 = 0,8621314$ By $ 2,\emptyset = 0,4259687$
	Quotient - 2,73 = 0,436162 Examp7

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Example 8.	Divide By Quotient		\$3,	= 1,4785 = 1,8037 = 3,9,6748	053
Example 9.	Divide By Quotient		(Contraction of Contraction of Contr	= 2,1979 $= 0,4398$ $= 1,7576$	- Contraction of the local division of the l
Example 10.	Divide By		~ 3,70	= 0,5680 = <u>,2,744</u> 7	6362
	Quotient	۰.		= 0,8239	-
Example 11.	Divide By	9 	00,718 4 2 ,0	= 2,9499 = 1,6234	9 88 581
• • • •	Quotient		21,28	= 1,3265	407
Example 12.	Divide By	,000000, 10, '	24330 8 002172	= ,3,3861 = ,6,3370	1506
	Quotient	,00	11,7,98 =	= ,7,0491	454

The Golden Rule in Decimals ly Logarithms.

 Example 1. Direct Propertion.

 If 2C, 3qr. 21 lb. of Sugar
 $-2_{39}^{375} = 0.4679778$

 Coft 61, 1s. 8d.
 $-6_{5} \circ 8_{3} = 0.7841316$

 What cofts 12C. 2qrs.
 $-12_{55} = 1.0969100$

 1.8810416

Answer, $251.17 s. 8\frac{1}{4}d. - 25,8864583 = 1,4130638$ Example 2. Inverse Proportion.

If Wheat be 6 s. 4 d. per Buschel, -6,3 = 0,8016325And the Pen. white Loaf weigh $7\frac{1}{4}$ oz. 7,75 = 0,8893017What musch it weigh, when Wheat is 3 s. 10 d. per Buschel? -3,83 = 0,5835766Auswer, 12 oz. 16 pwt. 2 gr. = 12,8043 & = 1,1073576 Note.

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Mote, Either of those Queffions sony (and that most conveniently) be wrought at once, viz. by One Addition of the two Logarithms now added, and the Avithmetical Complement of that Logarithm that is fubficated; for to fubficate a Logarithm, or add its Arithmetical Complement, produces the fame Effect, or is the fame Thing.

Example 3. Direct Propertion at one Operation.

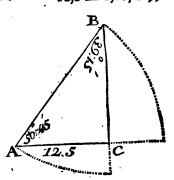
 If $\frac{1}{2}$ C. of Tobarro

Exemple 4. Inverse Proportion, at one Operation.

If 8 Rods in Width, - 8 = 0,9030900 Require 20 in Length, to make an Acre; 20 = 1,3010300 What Length does 12,5 Rods in 20 = 1,3010300Width require for an Acre? 12,5 = 8,9030899

Anfwer, 12,8 Rods

This Method with working at once with Arithmetical Complement is to be adviled to the expert Geometrician in his Trigonometrical Calculations, as much the best.



Example 5.

As the Sine of the Angle ABCIs to the Side given AC - 39: 15 = 0.1987985 12.5 = 1.0969100So is the Sine of the Angle BAC 50: 45 = 9.8889612To the Side fought BC - 15.3 = 1.1846697Extraction

12,8 = 1,1072099

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Extraction of Roots in Decimals by Logarithms.

To extract the Root of any Number, do thus;

If it be the	Square Root Cube Root Biquadrate Root Surfolid Root	Z Divide the Lo garithm of the given Number	ŧ)	2345
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Then the fecond, third. fourth, Sc. Past of the Logarithm thus divided, thall be the Logarithm of the Root longitt.

Example 1. What is the Square Root of the Number 2830,24?

The Logarithm thereof is - 3,4518232 Half of which, is the Logarithm of 53,2 = 1,7259116 The Root fought.

Example 2. Requir'd the Square Root of 13.2?

The Logatithm of the given Number 13,2 = 1,7205,735Half, is the Logar. of the Root 3,6331 Ge. = 0,5602869

Example 3. Required the Square Root of 14,0?

The Logarithm of ______ 14,8 = 1,1663314 Half, is the Logar. of the Root 3,8297 Sc. = 0,5831657

Example 4. What is the Cabe Root of 1,728?

The Logarithm of ______ 1,728 = 0,2379437 One Third, is the Log. of the Cabe Root 1,2 = 0,0791812

Example 4. What is the Biquadrate Root of 179,62 }

Example 6. Quere the Surfolid Root of 31,39?

The Logarithm of ______ 31,25 = 1,4948500 One Fifth, is the Log. of the Root 1,990 Ge. = 0,2989700

P p

Note;

Note; When the Index is Negative, add to it 10 for the Square Root, 20 for the Cube; 30 for the Biquadrate; 40 for the Surfolid Root, Sc. and then divide as before; as in the following general Example.

Example 7. What are the feveral Roots of ,27589?

The Logarithm of -,2758g =,9,4407132 An Half, is the Square Root,52523 &c. =,9,7203566 A Third, is the Cube Root,6509 &c. =,9,8135710 A Fourth, is the Biquadrate Root,7247 &c. =,9,8601783 A Fifth, is the Surfolid Root,7729 &c. =,9,8881426

CHAP. XII.

1 .

The Use of DECIMALS in Algebra; exemplified in the Resolution of thirty four Select, Pleasant, and Useful Algebraick Questions.

N OTWITHSTANDING Algebra has the Glory and Reputation of being one of the Topmoft Branches of the Tree of human Arts and Sciences; yet must it be acknowledged that (as fublime and useful a Science as it is) it would answer no great Purpose of practical Knowledge, were not the Art of Decimal Arithmetick, on every Occasion, called in to its Affistance. Vulgar Fractions and Algebra together, may be view'd as the Blind leading the Blind; And Whole Numbers miserably help the lame Dog over the Stile.

,'Tis Decimals therefore which in all Cafes (not fudied and fiated on purpose, but) which contingently or occasionally happen, can only speak out plainly and intelligibly the recluse Meaning of an Algebraick Equation or Theorem.

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This

This I shall make appear by the Resolution of the most curious pleasant and useful Questions, which I have science from the best Algebraick Authors extant?

Queficion 1. The Sum (= s = 67) of any two Numbers, and their Difference (= d = 30) being given to find those Numbers.

Let	I	a = the Greater, and $e =$ the Lesser Number.	•
Then	2	a+e=s=67	
And	3	a - e = d = 30	
2+3	4	a + e = s = 67 a - e = d = 30 2a = s + d = 97	
$4 \div 2$	5	$a = \frac{s+a}{2} = 48,5$ the greater Numb.	
2-3	6	2e = s - d - 37 fought,	,
$6 \div 2$	7	$e = \frac{s-d}{2} = 18,5 \text{ the leffer Number}$	

Question 2. The Sum (= s = 15) and Product (= p = 15) of any two Numbers given, to find those Numbers?

Then
$$\begin{cases} 1 & a+e = s = 15 \\ 2 & ae = p = 15 \\ ae = p = 15 \\ aa + 2ae + ee = ss = 225 \\ 2 \times 4 & 4 \\ 3 - 4 & 5 & aa - 2ae + ee = ss = 4p = 165 \\ 5 & a & 2ae + ee = ss - 4p = 165 \\ 5 & a & 2ae + ee = ss - 4p = 12,845 & 3c. \\ 1 + 6 & 7 & 2a = s + \sqrt{ss - 4p} = 12,845 & 3c. \\ 7 - 2 & 8 & a = \frac{e + \sqrt{ss - 4p}}{2} = 13,921 & 3c. & 3c. \\ 1 - 6 - 2 & 9 & e - \frac{s - \sqrt{ss - 4p}}{2} = 1,038 & 3c. & 1c. \\ 1 - 6 - 2 & 9 & e - \frac{s - \sqrt{ss - 4p}}{2} = 1,038 & 3c. & 1c. \\ 1 - 6 - 2 & 9 & e - \frac{s - \sqrt{ss - 4p}}{2} = 1,038 & 3c. & 1c. \\ 1 - 6 - 2 & 9 & e - \frac{s - \sqrt{ss - 4p}}{2} = 1,038 & 3c. & 1c. \\ 1 - 6 - 2 & 9 & e - \frac{s - \sqrt{ss - 4p}}{2} = 1,038 & 3c. & 1c. \\ 1 - 6 - 2 & 9 & e - \frac{s - \sqrt{ss - 4p}}{2} = 1,038 & 3c. & 1c. \\ 1 - 6 - 2 & 9 & e - \frac{s - \sqrt{ss - 4p}}{2} = 1,038 & 3c. & 1c. \\ 1 - 6 - 2 & 9 & e - \frac{s - \sqrt{ss - 4p}}{2} = 1,038 & 3c. & 1c. \\ 1 - 6 - 2 & 9 & e - \frac{s - \sqrt{ss - 4p}}{2} = 1,038 & 3c. & 1c. \\ 1 - 6 - 2 & 9 & e - \frac{s - \sqrt{ss - 4p}}{2} = 1,038 & 3c. & 1c. \\ 1 - 6 - 2 & 9 & e - \frac{s - \sqrt{ss - 4p}}{2} = 1,038 & 3c. & 1c. \\ 1 - 6 - 2 & 9 & e - \frac{s - \sqrt{ss - 4p}}{2} = 1,038 & 3c. & 1c. \\ 1 - 6 - 2 & 9 & e - \frac{s - \sqrt{ss - 4p}}{2} = 1,038 & 3c. & 1c. \\ 1 - 6 - 2 & 9 & e - \frac{s - \sqrt{ss - 4p}}{2} = 1,038 & 3c. & 1c. \\ 1 - 6 - 2 & 9 & e - \frac{s - \sqrt{ss - 4p}}{2} = 1,038 & 3c. & 1c. \\ 1 - 6 - 2 & 9 & e - \frac{s - \sqrt{ss - 4p}}{2} = 1,038 & 3c. & 1c. \\ 1 - 6 - 2 & 9 & e - \frac{s - \sqrt{ss - 4p}}{2} = 1,038 & 3c. & 1c. \\ 1 - 6 - 2 & 9 & e - \frac{s - \sqrt{ss - 4p}}{2} = 1,038 & 3c. & 1c. \\ 1 - 6 - 2 & 9 & e - \frac{s - \sqrt{ss - 4p}}{2} = 1,038 & 3c. & 1c. \\ 1 - 6 - 2 & 9 & e - \frac{s - \sqrt{ss - 4p}}{2} = 1,038 & 3c. & 1c. \\ 1 - 6 - 2 & 9 & 1c. & 1c. \\ 1 - 6 - 2 & 9 & 1c. & 1c. \\ 1 - 6 - 2 & 1c. & 1c. \\ 1 - 6 - 2 & 1c. & 1c. \\ 1 - 6 - 2 & 1c. & 1c. \\ 1 - 6 - 2 & 1c. & 1c. \\ 1 - 6 - 2 & 1c. & 1c. \\ 1 - 6 - 2 & 1c. & 1c. \\ 1 - 6 - 2 & 1c. & 1c. \\ 1 - 6 - 2 & 1c. & 1c. \\ 1 - 6 - 2 & 1c. & 1c. \\ 1 - 6 - 2 & 1c. & 1c. \\ 1 - 6 - 2 & 1c. & 1c. \\ 1 - 6 - 2 & 1c. & 1c. \\ 1 - 6 - 2 & 1c. & 1c. \\ 1 - 6 - 2 & 1c. & 1c. \\ 1 - 6 - 2 & 1c. & 1c. \\ 1 - 6 - 2 & 1c. \\ 1 - 6 - 2 & 1c. & 1c.$$

Qu flion 3. What two Numbers are those whole Sum is = 40 = s, and the Greater divided by the Leffer shall quote $50 = q^2$

Here
$$\begin{cases} 1 & a + e = s = 40 \\ 2 & a = q = 50 \\ 2 & a = q = 50 \\ 4 + q = 5 \\ 4 + q = 5 \\ 5 + q + 1 \\ 1 - 6 \\ 7 \\ 4 = \frac{qs}{q + 1} = \frac{4}{q + 1} = \frac{40}{393156}$$
 Quere *a*, and *e*?
Quere *a*, and *e*?
Quere *a*, and *e*?
Quere *a*, and *e*?
Quere *a*, and *e*?
Quere *a*, and *e*?
Quere *a*, and *e*?
Quere *a*, and *e*?
Quere *a*, and *e*?
A = q = 50
Quere *a*, and *e*?
Quere *a*, and *e*?
A = q = 50
Quere *a*, and *e*?
Quere *a*, and *e*?
Quere *a*, and *e*?
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Quere *a*, and *e*?
A = q = 50
Quere *a*, and *e*?
Quere *a*, and *e*?
Quere *a*, and *e*?
Quere *a*, and *e*?
Quere *a*, and *e*?
Quere *a*, and *e*?
A = q = 50
Quere *a*, and *e*?
Quere *a*, and *e*?
Quere *a*, and *e*?
Quere *a*, and *e*?
Quere *a*, and *e*?
A = q = 50
Quere *a*, and *e*?
Quere *a*, and *e*?
Quere *a*, and *e*?
Quere *a*, and *e*?
Quere *a*, and *e*?
Quere *a*, and *e*?
A = q = 50
Quere *a*, and *e*?
Quere *a*, and *e*?
Quere *a*, and *e*?
Quere *a*, and *e*?
Quere *a*, and *e*?
Quere *a*, and *e*?
A = q = 30, 31, 56. Sc. Quere *a*?
Quere *a*, and *e*?
Quere *a*?
Quere *a*?

Gueffien 4 What two Numbers are those, whose Sum is = 8 = s, and the Sum of their Squares $37\frac{5}{6} = z^3$

Here
$$\begin{cases} 1 & 1 + e \ \text{sm} s \equiv 8 \\ 2 & aa + ee = z = 37, s \end{cases}$$
 Quere a, and e?
1 Q 2 3 $aa + 2ae + ee = ss = 64$
3 - 2 4 $2ae = ss - z = 26, 4$
2 - 4 5 $aa - 2ae + ee \equiv 2z - ss \equiv 11, z$
5 w 2 0 $a - e = \sqrt{122 - ss} = 3, s$
1 + 6 7 $2a \equiv s + \sqrt{122 - ss} = 3, s$
7 $\div 2$ 8 $a \equiv \frac{s + \sqrt{122 - ss}}{2} = 5, s$ Greater
1 - 6 $\div 2$ 9 $e = \frac{4 - \sqrt{22 - ss}}{2} = 2, s$ Leffer fought,

Queflion 5. If the Sum of any two Numbers be 50 = s, and the Difference of their Squares be 273 = s, What are the faid Numbers?

the faid Numbers ? Here $\begin{cases} 2 & a_1 + e \equiv s \equiv 50 \\ 2 & a_2 - ee \equiv x \equiv 213 \end{cases}$ Quere a, e? $2 \div 1 & 3 & a - e \equiv \frac{x}{5!} \equiv 5:46$ $1 \div 3 & 4 & 2a \equiv \frac{5s \pm x}{25} \equiv 5:46$ $4 \div 2 & 5 & a \equiv \frac{5s \pm x}{25} \equiv 27,73$ the Greater $1 - 3 \div 2 & 6 & e \equiv \frac{5s \pm x}{25} \equiv 22,27$ the Leffer South. Queficent

Queftion 6. Suppole the Difference of two Numbers be 30 = d, and the Product 512 = p. Quere the Numbers?

More {	I X	$a - e = d = 305$ Quere $a_1 a_2^{2}$ $a_2 = p = 512$ $f = dd = 900$
102	3	$aa - 2ae + ee \doteq dd = 900$
2 X 4	4	$4^{ae} = 4p = 9048$
3+4	" 9 1 76	A + 200: + A = A + 40 + 2548
6+1-2	7	4 <i>ae</i> = 4 <i>p</i> = 9048 4 <i>a</i> + 2 <i>a</i> + <i>ae</i> = 4 <i>a</i> + 4 <i>p</i> = 2948 4 <i>a</i> + <i>e</i> = $\frac{\sqrt{da} + \sqrt{da}}{\sqrt{da} + 4p}$ = 42,18 Greater 1 Numb.
62	8.	12,18 Leffer
	r : 1	lt #as i ∫

Question 7. Suppose the Différence of two Numbers be the fame with the Questions of the Greater divided by the Leffer, viz. = 18. Quere those Numbers?

Here
$$\begin{cases} 1 & a - e = d = 18 \\ 2 & \frac{4}{e} = q = 18 \\ 2 & \frac{4}{e} = q = 18 \\ 4 & a = q = 18 \\ 1 + e & 4 & a = d + e = 18 + e \\ 3i & 4 & 9 & = d + e = 18 + e \\ 3i & 4 & 9 & = d + e = 18 + e \\ 5 & -e & 6 & q = -i = d = 19 + e \\ 5 & -e & 6 & q = -i = d = 19 \\ 6 - q - I & 7 & e = \frac{d}{q - I} = 1,058 \text{ the Leffer} \\ I - 7 & 8 & e = \frac{qd}{q - I} = 1,058 \text{ the Leffer} \end{cases}$$
 Number fought.

Question 8. The Difference of two Numbers = 5'= d, and the Sum of their Spears, = 52 = 2, being given ; tained those Numbers,

Here
$$\begin{cases} 1 & 4 - e = d = 5 \\ 2 & aa + ee = x = 55 \\ 2 & aa - 2ae + ee = dd = 25 \\ 2 & -3 & 4 \\ 2 & +4 & 5 & aa + 2ae + ee = 2x - dd = 30 \\ 2 & +4 & 5 & aa + 2ae + ee = 2x - dd = 85 \end{cases}$$

5 🗰 2

I

5 av 2 6
$$|a + e \equiv \sqrt{2z - dd} = 9,219$$

 $|a + 6 \div 2|$ 7 $|a = \frac{d + 2z - dd}{2} = 7,109$ Greater Number
 $6 - 1 \div 2|$ 8 $|e = \frac{\sqrt{2z - dd}}{2} = 2,109$ Leffer from the

Queflion 9. The Difference of any two Numbers = 12 = d, and the Difference of their Squares = 279 = x, being given; to find those Numbers?

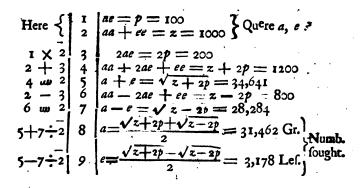
Here
$$\begin{cases} 1 \\ 2 \\ aa = ee = x = 279 \end{cases}$$
 Quere *a*, *e*?
 $2 \div 1 \\ 3 \\ a + e = \frac{x}{d} = 23,25$
 $1 + \frac{7}{3} \\ 4 \\ 2a = \frac{dd + x}{d} = 35,25$
 $a = \frac{dd + x}{2d} = 17,625$ Greater
 $3 - \frac{7}{5} \\ 6 \\ e = \frac{x - dd}{2d} = 5,625$ Leffer $\begin{cases} \text{Number} \\ \text{fought}, \end{cases}$

Queficen 10. The Product of any two Numbers being = 573 - p, and the Quotient of the Greater divided by the Leffer = 75; Quere those Numbers?

Here
$$\begin{cases} 1 & ae = p = 573 \\ 2 & \frac{a}{e} = q = 75 \end{cases}$$
 Quere a, e ?
 $1 \times 2 & 3 & aa = qp = 42975$
 $3 \text{ us } 2 & 4 & a = \sqrt{qp} = 207,304 \text{ Sc. Greater} \\ 1 \div 2 & 5 & ee = -p = 7,64 \\ 5 \text{ us } 2 & 6 & e = \sqrt{\frac{p}{2}} = 2,764 \text{ Sc. Leffer I} \end{cases}$ Number
 $gueftion$

1 1 2

Queftion 11. The Product of any two Numbers =100=P, and the Sum of their Squares =1000=z; Quere those Numbers?



Queftion 12. The Product of any two Numbers =10=p, and the Difference of their Squares = 20 = x, being given; thence to find those Numbers?

Here
$$\begin{cases} \begin{vmatrix} 1 \\ 2 \\ aa = p = 10 \\ aa - ee = x = 20 \end{cases}$$
 Quere *a*, *e*?

$$aaee = pp = 100 \\ aaaa - 2aaee + eeee = xx = 400 \\ aaaa - 2aaee + eeee = xx = 400 \\ aaaa + 2aaee + eeee = xx + 4pp = 800 \\ 6 uu = 2 \\ 7 \\ 2 + 7 \\ 8 \\ 2 + 7 \\ 8 \\ 2 = x + \sqrt{xx + 4pp} = 28,284 \\ 8 \div 2 \\ 9 \\ uu = 2 \\ 10 \\ a = \sqrt{x + \sqrt{xx + 4pp}} = 24,142 \\ a = \sqrt{x + \sqrt{xx + 4pp}} = 24,142 \\ a = \sqrt{x + \sqrt{xx + 4pp}} = 4,917 \ \text{Sc. G.} \\ au = \sqrt{x + \sqrt{xx + 4pp}} = 4,917 \ \text{Sc. G.} \\ au = \sqrt{x + \sqrt{xx + 4pp}} = 2,035 \ \text{Sc. L.} \\ au = \sqrt{x + 4pp - x} = 2,035 \ \text{Sc. L.} \end{cases}$$

Queflior 13. The Quotient of any two Numbers =10-q, and the Same of their Squares = 57 = 2, being given; to find that Numbers?

Queficion 14. Suppose the Quotient of two Numbers
$$= 20 = q$$
, and the Difference of their Squares $= 100 = x$;
Thence to find the Numbers.

Here
$$\begin{cases} 1 & | \frac{a}{e} = q = 20 \\ 2 & | a - ee = \pi = 100 \end{cases}$$
 Quere a, e^{a}

$$a = qe = 20e \\ aa = qe = 20e \\ aa = qe = 400ee \\ aa = x + ee = 100 + ee \\ aa = x + ee = 100 + ee \\ qee = x + ee = x = 100 \\ f = ee \\ 7 & | qee = ee = \pi = 100 \\ 7 \div qq = 1 \\ 8 & | ee = \frac{x}{qq} = 1 \\ 2 + 8 & | ee = \frac{qqx}{qq} = 1 \\ 2 + 8 & | ee = \frac{qqx}{qq} = 1 \\ 9 & | aa = \frac{qqx}{qq} = 1 \\ 9 & | aa = \frac{qqx}{qq} = 1 \\ 9 & | aa = \frac{qqx}{qq} = 1 \\ 9 & | aa = \frac{qqx}{qq} = 1 \\ 9 & | aa = \frac{qqx}{qq} = 1 \\ 9 & | aa = \sqrt{\frac{qqx}{qq}} = 10,012 \ Se. \ Greater \\ 8 & | w = 2 \\ 11 & | e = \sqrt{\frac{x}{qq} = 1} = 0,5006 \ Se. \ Lefter \\ \end{cases}$$
 Numb.
Queftion

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Queflion 15. Suppose the Sum of the Squares of any two Numbers = 300 = z, and the Difference of the faid Squares = 250 = x, to find the Numbers?

H	ére {	I 2	$aa + ee = z = 300 aa - ee = x = 250 2na = z + x = 550aa = \frac{z + x}{2} = 275$	a, e .*	
Ì.	+ 2	3	2na = z + x = 550		
3	÷ 2	4	$aa = \frac{z + x}{2} = 275$		
4	EN 2	5	$a = \sqrt{\frac{2}{2}} = 16,583 \text{ Gr. Gre}$ $e = \sqrt{\frac{2-x}{2}} = 5 \qquad \text{Gr. Leff}$	ater .Numb	ćť
•	And	6	$e = \sqrt{\frac{2-x}{2}} = s$ Sc. Left	Ter J	•

Thus any two of thole Six Things (viz. Sum, Difference, Product, Quotient, Sum of the Squares, and Difference of the Squares, of any two Numbers) being given ; twill be eafy to find the Numbers themselves and all the other Particulars:

I have chose to give the Analytical Process of the Work of each Question at large, that the Young Student may see the Manner of Investigating Theorems; and by viewing the frequent Divisions and Extractions, may the more clearly perceive the great Use, or rather; the absolute Necessity of Decimals, in order to express the Equations in Numbers.

But in those Questions which follow, I have only exhibited the *Theorem* or Equation which answers them, and given the Solution of each in *Decimal* Numbers.

Queftion 16. There are two Numbers a, e. The Sum of their Squares is as +ee = z = 27 The Greater is to the Lefs as 12 = b is to 7 = d That is a : e :: b : dQuere a, e^{-2}

Theorem.
$$e = \sqrt{\frac{zdd}{dd + bb}}$$
 to be related.

First Multiply the Sum of the Squares z = 97By the Square of d = - dd = 49The Product is - zdd 4763 Dividend. Then to the Square of d = - dd = 49Add the Square of b = - + bb = 144The Sum of both is - dd + bb = 193 Divisor. Q q By

By which Divide zdd, $\frac{zdd}{dd + bb} = 24,6792$ Se. The Quotient will be $\frac{dd}{dd + bb} = e = 4,966$ The Square Root of which is $\sqrt{\frac{zdd}{dd + bb}} = e = 4,966$ Then as $\begin{cases} d: e :: b : a \\ 7: 4,966: : 12:8,513 \end{cases}$ Thus $\begin{cases} a=8,513 \\ e=4,966 \end{cases}$

Queficen 17. There are three Numbers in continued Proportion, viz. - - a. m. e.The Sum of the Extremes - $a + e = 37\frac{2}{5} = s$ And the Mean - m = 13. Quere a, e.s

Theorem. $a = \frac{s + \sqrt{ss - 4mm}}{2}$ to be folved.

Firft, The Square of the Sum is -35 = 1398,70And the Square of $m \times 4$ is -4mm = 676Which subfracted, there remains, ss - 4mm = 722,76The Square Root whereof is $\sqrt{ss - 4mm} = 26,885$ To which add the Sum of the Extreams s = 37,4That Sum is $-s + \sqrt{ss - 4mm} = 64,285$ The half of that is the Firft Number a = 32,142Then as $\begin{cases} a : m :: m : \\ 32,142 : 13 :: 13 : \end{cases}$ e = 5,257The Sum of which is the Proof a + e = 37,4

Quefilion 18. There are three Numbers in continued Proportion, viz. Their Sum is $-a+m+e=s=31\frac{2}{7}$ Quere And the Sum of their Sq. aa+mm+ee=z=763

Theorem. $m = \frac{ss - z}{-2s}$ to be folved.

Pinft, Pinft,

First, from the Square of their Sum ss = 978,7955 St. Substract the Sum of their Squares z = 763

The *Remainder* is ss - z = 215,7955 Which divided by twice the Sum 2s = 62,871428Gives the Quotient m = 3,446 Br. Then 31,285714 - 3,446 = 27,839 = a + eWhich may be found as in the Theorem of the last Question.

Quefiion 19, Suppose three Numbers a, b, c in Mulfical Proportion, viz. As a: c:: a-b: b-c, and any Two of them being given, to find the Third.

Theorem 1. $a = \frac{cb}{2c-b}$ Finds a, if b, c, be given. Theorem 2. $b = \frac{2at}{c + a}$ Finds b, if a, c, be given. Theorem 3. $c = \frac{ba}{2a-b}$ Finds c, if a, b, be given,

Suppose b = 13, and c = 10 To find a? $\begin{array}{c} b = 13 \\ c = 10 \end{array}$ Multiply By The Product · cb == 130

Divide by twice c, lefs b, 2c-b=7) 130=cb (1,8,57142. The Quotient is a = 18,57142 the Number fought. And

to for either of the other.

Question 20. Suppose four Numbers, a, b, c, d, in Mufical Proportion, viz. a: d:: a - b: c - d; and any Three of these given, to find the fourth.

Theorem 1. $a = \frac{db}{2d - c}$ Finds a, if b, c, d, be given. Theorem 2. $b = \frac{2aa - ca}{A}$, Finds b, if a, d, c, be given. Theorem 3. $c = \frac{2da - db}{a}$, Finds c, if a, b, d, be given. Theorem 4. $d = \frac{ca}{2a-b}$, Finds d, if a, b, c, be given. Qq 2 Queflion

1.

Queflion 21. Suppose it was required to divide any Number (20 = i) into Extream and Mean Proportion; That is, into two such Parts, a, and e, that aq = qe + ee = se. Quere q, $e \neq$

Square the given Number - ss = 400Add thereto $\frac{1}{4}$ of the faid Square - $\frac{1}{4}ss = 100$

The Sum is $- \frac{ss + \frac{1}{5}ss = 500}{\text{The fquare Root thereof is } - \sqrt{ss + \frac{1}{4}ss} = 22,3606 \ \text{Bg.}$ From which fubfract $\frac{1}{5}$ the given Numb. $\frac{1}{5}s = 10$

There Remains the Greater Part -a = 12,3606 Sc. Which substracted from the given Numb. There remains the Leffer Part e = 7,6393 Sc.

Note, Tis impossible to answer this Question in Whole Numbers.

Question 22. What is the Canon or Theorem for Extracting the square Root?

Suppose a + e = Root; Then the Canon is this, yiz. aa + 24e + ee = Square.

Extract the Sq. Root of 655,36 = aa + 2ae + eeFrom the Numb fubil: 400 = aa (a = 20)There Remains $-\frac{255,36}{225} = 2ae + ee$ $\begin{cases} a = 20\\ e = 5 \end{cases}$ Divide that by 2a=40 255,36(5 = e)Then fubfract $-\frac{225}{225} = 2ae + ee$ $\begin{cases} a + e = 25\\ = a, auew. \end{cases}$ There Remains $-\frac{30,36}{30,36} = 24e + ee$ anew. Which divid by. 2a=50 30,36(,6 = e) anew (25=a)

Which divid by. 2a=50, 30, 36, 6=e anew Then again substract 30, 36=2ae+ee $\begin{cases} 25=a\\ ,6=e\\ 25,6=a+e \end{cases}$

Question 23. What is the Canon or Theorem for extracting the Case Root?

Suppose a + e = Root, Then aaa + 3aae + 3aee + eeeis the Canor or Rule for Extracting any Cube Root. Required

Requir'd the C. Root of 1953,125 = aas + 3aae + 3aee + eee Subfract the Cube 1000 = aaa (a=10. If. There remains 953,125 = 3aae + 3aee + eee Div. by 344+34=330)953,125(2=e Then 600 = 2000 And 120 <u>= 3aee</u> Lafily 8 S 3aae + 3aee + see fubit. The Sum of all is 728 from the Remainder. There remains 225,125 = 3aae + 3aee + eee, anew. Div. by 344+34 = 468)225,125(,5 = e Then a = 10Then 216,000 = 3aae= 2 And 9,000 = 34ee 4 + e = 12Lafily 0,125 = eee= a, anew. The Sum of all is 225,125 = 3aae + 3aee + eee to be (fubit. from the last Rem.

Hence the Root is 10 + 2 + ,5 = 12,5

Quefice 24. What is the Manner of Extraction by Conperging Series, or Theorems raifed thereby?

There are feveral Kinds of Converging Series for this Purpole, but Mr. Ward's I take to be the beft, which is thus.

Let
$$aa = G$$
. Quere $a \ge 3$

Let I
$$|r + e = a$$
 The Root fought,
 $|r - r| = 2$ $|r + 2re + ee = aa = G.$
 $|r - r| = 3$ $|2re + ee = G - rr = D$ The Dividend.
Then $|4| \frac{D}{2r + e} = e$, or, $\frac{D}{r + \frac{1}{2}e} = e$ {Theorems for the Sq. Roor,
Let

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Note, From hence appears the Rationale of the Method of extracting the Cube Root; for the Precepts there are only the Words expressing the order and combination of the Symbols of this Cazor.

		Let $aaa = G$. Quere a .
Put	I	r + e a The Root fought
· I G 3	2	rrr + gree + gree + eee = aaa = G
2 - 111	3	3578 -1. 3ree + eve = G TTT
3 ÷ 37	4	$r + e = a \text{The Root fought}$ $rrr + 3rre + 3ree + eee = aaa = G$ $3rre - 3ree + eee = G rrr$ $re + ee + \frac{eee}{3r} = D, \text{ the Dividend.}$
Reject 2r	5	$re + ee = D \frac{de}{3r}$ being of fmall or no Value.
5÷	6	$\frac{D}{r+e} = e.$ The <i>Theorem</i> for the <i>Cube</i> .

If aaaa = G Then $\frac{G}{2rr} \stackrel{r^*}{=} D$ and $\frac{D}{2r + 3e} = e$. The Theorem for the Biquadrate Root.

- If aaaaa = G. Then $\frac{G r!}{5r^3} = D$. And $\frac{D}{r + 2c}$ The *Theorem* for the Surfolid Root. And in the fame Manner proceed for any other Root.
 - Note; To work by these Theorems, r must be taken less than the Root; otherwise, if r be taken greater than the true Root, it will be rr - G instead of G - rr, and $\frac{D}{2r - e} = e$ and the same in other Theorems for the other Roots.

After the fame Manner you raife Theorems for all kind of adfested Equations.

Suppose aaa + 24a = 587914 Quere a?

Put I r+e=a Put r=80I $\bigcirc 3$ 2 rrr + 3rre + 3ree = aaaI $\bigcirc 3$ 2 rrr + 3rre + 3ree = aaaI X 24 3 24r + 24e = 2442 in Numb. 4 512000 + 19200e + 240ee = aaa3 in Numb. 5 1920 + 24e = 24a 4 + 5 6 513920 + 19224e + 240ee = 587914 5 - 513920 7 19224e + 240ee = 739947 $\div 240$ 8 80, 1e + ee = 308, 31 = D the Dividend 8 \div 9 $e = \frac{D}{80, 1 + e}$ See the Operation. 80_{11}

•

The Use of Decimals in Algebra: 303 80,1) 308,31 = D (3,7 = e +e = 3 2493 1 Divifor 83,1) 59,01 +e = .7 5866 2 Divifor 83,8) ...35 r = 80 e = 3.7r + e = 83,7 = a

Here $8_{3,7}$ is a new r for a *ferond Operation*; but being involved will be found too big, or *greater* than the *true Root*; Therefore it must be made r - e = a the Root.

h

Thus $ \mathbf{I} \mathbf{r} - \mathbf{e} = \mathbf{a}$	the Root fo	ought.
I G 3 2 rrr - 3rre	+ 3788 =	aa a '
		244
I X 24 3 24r - 24e 2 in Numb. 4 586376,253		7e+251,1ee=ana
$3 \text{ in Numb.} 5 2008,8 \\ 4 + 5 6 588385,053 \\ $	- 248	=24a
4 + 5 6 588385,053		7e + 251,1ee=587
		= 471,053 (914
7 - 251,1 8 183,7955e -	• ee = 1,8	7595778 = D
$8 \div 9 = \frac{D}{2}$		• •
03,795		,
Operat		81 annonesta
•3,7955) - e = 02,	1,6759577	8(,022392736
and an and a second second second second second second second second second second second second second second		
1 Divisor 83,7755)	,2001477	
$-e \Rightarrow ,002$	1675470	
2 Divifor 83,7735)	,0329007	3
$-e \equiv ,0003$,0251319	6.
3 Divisor 83,7732	,0077688	2 From hence
	75395	8 'tis sufficient to
	-	work by Con-
the second second second second second second second second second second second second second second second s	2292 1675	
	Para and a second second second second second second second second second second second second second second s	
	616	
	5 8 5	4 Roor.
Niama a Galar	30	4 .
Now = 83,7	05	• •
And $* = 0,0223927$		
Then $r - e = 83,67760726$	54=a 52	
The Root of 587914 requ		
	•	4 Br. And

And if this Root be not exact enough, it may be made at New r, to work as before, in a third Operation.

And thus may the Root of any Adfected Equation be

Questión 25.

1	Any Body -	-	Å
	Pals over a given Space		С,
1	In a given Time		f
	And any other Body	-	B
6	País over a Space	م ن بو	d
Suppole	In the Time		g
	Alfo their Diftance of	Place —	C
	And the <i>Interval</i> of <i>T</i> which they begin to m	ime, in y	Б
	There as a second		

•

[Thence to determine — * The Diffance they pais, 'ere the hindmoft Body overtakes the foremoft, if they both tend the fame way; or before they meet, if their Motions be opposite.

First, If they both tend the fame Way, and A begin to move first, and is nearest the Place they tend to ;

The Theorem is
$$x = \frac{bdc + fed}{fd - ge}$$
 1.

But if B begin to move $x = \frac{hdc - fed}{fd - gc} 2$.

If they both begin to move in the fame Moment; the *Theorem* will be thus $\begin{cases}
x = \frac{fed}{fd - g^{t}} & 3
\end{cases}$

For if b = o, then the Member of the Equation that has it, vanisheth.

Secondly. If the Moveable Bodies meet, and x, as before, be the Diffance of the fartheft Body, from the Place of Rencounter, or Meeting; then e - x will be the Diffance of the other Body. Call the Body at fartheft Diffance A, and the other B.

Then,

Then, if A moves first, the Theorem is - $x = \frac{cdb + cgs}{fd + gc}$ 4.

But if B moves first, $x = \frac{cdb + ige}{fd + ge}$ 5.

If they both move at the fame time, the Theorem $\begin{cases} x = \frac{g^2}{fd + g^2} & 6. \end{cases}$

These Six Theorems answer most of the curious (and forme of them very useful) Questions that are usually proposed conconcerning the *Motion* of two Bodies.

Question 26. Suppose the Sun (A) in the Beginning of Virgo, and eight Days after the Moon (B) is in the Beginning of Gemini; Quere the Place of the next New Moon?

Here are given $\begin{cases}
c = 0,03285 = 00:59:08 \\
f = 1, \\
d = 0,4892 = 13:10:35 \\
g = 1, \\
e = 3, \\
b = 8,
\end{cases}$ By Theorem 1, work as follows;

Multiply -d = 0,4892)'s given Motion. By -c = 0,03285 ©'s given Motion. The Product is dc = 0,01607Which mult. by b = 8 Difference of Time. That Prod. is dcb = 0,12856Again multiply d = 0,4892By -fc = 3The Prod. is fcd = 1,4676To which add dcb = 0,12856Sum is bdc + fcd = 1,59616 The Dividend. Then from -fd = 0,4892Subfract -gc = 0,03285Remains fd-gc = 0,45635 The Divifor.

Rr

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By which divide, The Quotient is x = 3,49769 = 3: 14: 55: c5To which add the Moor's pref. $\Gamma L = 2: c0: c0: c0$ The Sum is the Place of the 1

The Sum is the Place of the Next New Moor fought Vir. In W } 14:55:05

Queficion 27. If a Ship B fail from the Equator percifely North, at the Rate of $7\frac{1}{2}$ Degrees in 3 Days, and another Ship A, 8 Days after fet fail on the fame Meridian the fame Way, in

Latitude 30 : 30, and runs 8 : 45 in five Days; 'tis required to tell in what Degree of North Latitude B will overtake A?

By Theorem 2. Thus;

Multiply the given Motion of A — $c = 8,75$ By the given Motion of B — $d = 7,5$
The Product is $dc = 65,625$ Multiply that by the Interval of Time $b = 8$
The Product is the Substrahend $-bdc = 525,000$
Then multiply the given Interval of Places $e = \frac{36,5}{7,5}$ By the given Motion of $B - d = \frac{7,5}{7,5}$
The Product is $ -$
The Product is $-$ fed = 1368,75 From which substrate the Substrate of $-$ bdc = 525,00
Remains the Lividend $-$ fed - bdc = $8_{+3,75}$ Then from 7.5 × 5 $ fd =$ 37.5 Subftraæt 8,75 × 3 $ gc =$ $26,25$
There remains the Divifor $- fd_{-gc} = 11,25$ By which Divide ; the Quotient is $= x$, $= 75$ th Deg. the Latitude fought, viz.

Queficion 28. A challenges B to run a Race with him, provided he will give him 30 Rod in a 100; now the Velocity of B's Running to that of A, is as $7\frac{1}{4}$ to $5\frac{1}{2}$, Quere which of the two beat?

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By

By Theorem 3, work thus; Multiply the Velocity of B - d = 7,75By the given Interval of Diftance - e = 30The Product (because f = 1) is the Dividend fed = 232,5

Then from - - fd = 7.75Subfract - gc = 5.5There Remains the Divifor fd-gr = 2.25Then - 2.25) 232.5 (103 = x = 103.3 Rods.

Hence A beat B, fince above the 100 Rods were país'd 'ere B came up with, or could overtake him.

Question 29. Suppose the Hour and Minute Hand of a Horologium, or Clock, be now both in Conjunction at 12, Quere the Place of their next Conjunction?

If you proceed by the fame Theorem 3, you will flud it to b. h. h. h. h. h. h. h. h. h. h. be at 1 : or Hours = 1 : 5 : 27 : 16 : 21 : 49, St. the last five Places repeating ad infinitum. Hence we may observe, that though there really is a certain Moment of Time in which the Minute-Hand is precisely in Conjunction with the Hour-Hand, yet 'tis impossible to determine or reprefent that Moment of Time either in whole Nambers, or Decimal Fractions; But by Vulgar Fractions we know it is 1. Hours, that is just one Eleventh Part of an Hour after one a Clock.

Quefition 30. From Landon to Chichefter is 60 Miles; A Post-Boy (A) fets out from London, and goes $8\frac{1}{4}$ Miles in $2\frac{1}{2}$ Hours; Another Post-Boy (B) $1\frac{1}{2}$ Hour after fets out from Chichefter, and rides 9 Miles in $3\frac{1}{4}$ Hours. I demand how far A will have gone before he meets B?

This Question is answer Multiply As given Space By the Interval of the	ed by Fimes	Theorem	4. thus; -c = b = b	8,75
Then multiply that Prod By the given Space of E	uct ·		ch = d =	13,125
The Product is	- I	 Rr 2	cdb =	118,125 Again

Again multiply $ c =$ By the given Time of B $ g =$	8,75
And that Product $- cg =$	28,4395
Mult. by the Interv. of Diffance $-e =$	63
To that Product $- cg^2 =$	1706,25
Add that above, viz. $- cdh =$	118,125
The Sum is the Dividend cdb + cge ==	1824,375
Then to the Product above, $-cg =$	28,4375
Add the Prod. of $(f \times d = 2, 5 \times 9)$ fd =	22,5
The Sum is the Divisor $-fd+cg$, = By which dividing; the Quoti- ent is the Diff. of A's Journey $x =$ Then the Diffance B will have $y =$ pass'd is	50,9375 36,208 23,791 Anf.

And thus proceed for answering Questions by Theorems the fifth and fixth. By these Theorems several other pretty Problems proposed, may be resolved by any one versed in those Matters.

Queftion 31. This prefent Year of our Lord, the Cycle of the Sun is 6 = e, and the Cycle of the Moon (call'd the Prime or Golden Number) is 5 = d; Quere the Year of the Dionyfian Æra or Period?

	C	e	=	6				•	7	Let x be the Year of the Pe-
Here is given	3	ď	=	5					2	Year of the Pe- riod fought.
	C	ć		d	=	#	Ξ	I	2	ried lought.

The Theorem is 59, x = 2, x = 3, x = 2, x = x.

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For, multiply the Diffe By the Number	rence of	the Cycles	z = 1 59,1	
Then that Product is To which add $\not \propto 3, r$			= 59,r = 15,9	
From that Sum Subfiract $e \times 2, r$	<u>ل</u> لہ ن		= 74,0 = 12,6	·
There remains the Yea	r of the	Period	62	fought. This

The Use of Decimals in Algebra. 309

This Theorem I contrived my felf; and inferted it here as being a Decimal one.

Question 32. Let A, and B, be two fpherical Bodies perfectly elastick, and let (a) denote the Volocity of A, and (b) = the Velocity of B; then the Motion of A = aA, and the Motion of B = b B; laftly let x = the Increase of Motion communicated by the Impact or Stroke, to one Body; and the Decrease or Loss of Motion in the percutient or striking Body.

Let A follow B, and let it be required to determine the Celerity of each Body after the Stroke or Impulfe.

If A and B tend both the fame Way, the Theorem for $\begin{cases} A \ s \ Celerity \ is \ x = \frac{aA - aB + 2bB}{A + B} \\ B \ s \ Celerity \ is \ x = \frac{2aA - bA + bB}{A + B} \end{cases}$

But if they meet, the *The*orems will be altered thus, for $\begin{cases} A, & x = \frac{aA - aB - 2bB}{A + B}\\ B, & x = \frac{2aA + bA - bB}{A + B} \end{cases}$

Example. Suppose two Bodies of the fame fort, A of 5; Pounds, and 9 Degrees of Velocity; and B of 6; Pounds, and 4 Degrees of Velocity; tend the fame Way; Quere their Celerities after the Impulse?

Here A = 5,3. a = 9. B = 6,5. b = 4. Then,

From the Motion of A = -aA = 48Subfract the Velocity of A into B = aB = 58,5There remains negative, -aA-aB = -10,5To which add twice the Motion of B - 2bB = +52There Remains the Dividend - = +41,5Then A + B = 11,8 + 41,5 (3,49 = A's Celerity. In like Manner may be found 8,46 = B's Celerity.

Note; If either Celerity come out Negative, it fignifies the Motion of that Body, after the Impulse, to be contrary to what it was before.

I have

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I have inferted this Queftion and Theorem, for the Sake of any fuch Perfons as would wifh to have always a Theorem by them for the ready determining the Celerity of Bodies in Motion by Calculation, and the rather becaufe this Doctrine of Motion is the principal Bafis of a good Part of the modern unchanical Philosophy.

Quefice 33. Says A, I've an Acre of Land to inclose; fays B, I've ten Thousand such Acres as those, which lie in a Square; but the Form you defign must have the same Fercing as goes round all mine. Quere the Length and Breadth of A's Acre of Land?

Let $\begin{cases} a = 1 = \text{The Area of A's Plot of Land.} \\ d = 100 = \text{The Side of B's fquare Plot.} \\ \mathbf{x} = \text{The Side of A's Plot to be found.} \end{cases}$

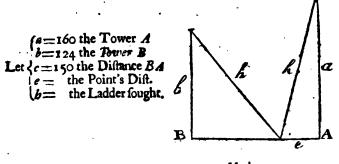
The Theorem is $\kappa = \sqrt{dd + a} : + d$.

From the Square of d dd = 10000Subfract the given Area -a = 1There remains -dd - a = 9999The Sq. Root thereof is $\sqrt{dd-a} = 99,995$ To which add -d = 100The Sum is one Side of the Area x=199,995= the Length. And the other Side is $-\frac{a}{x}=0,005=$ the Breadth. Thus traice their Sum is =4b=400 the Perimeter of Both.

Quefition 34. Suppose the Tower A 165 Feet high, and another Tower B 124 Feet high, at the Diffamee AB = 150Feet; 'tis required to set a Ladder in some Point (e) in the 1 ine A, of such a length, as from thence it may reach the Tops of both the Towers: Quere the Point e, and the length of such a Ladder ?

Let

The Use of Decimals in Algebra. 3



The Theorem for the Diffance (e) $\frac{bb+cc-ae}{2^6} = e^{-ab}$

Then for the Length of the Ladder (b) $\sqrt{aa + ce} = b$

Thus, to the Square of B's beight -bb = 15376Add the Square of the Diffance -cc = 22500Then from that Sum -bb + cc = 37876Subfract the Square of A's beight -aa = 25600There remains the Dividend bb + cc - aa = 12276Which divided by 2c = 300, the e = 40.92Quotient is the Diffance (e) - e = 40.92Then the Length of the Ladder is $\sqrt{aa + ee} = b = 165,149$ BC.

CHAP.

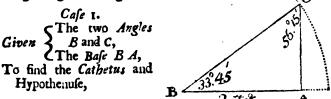
CHAP. XIII.

The Use of DECIMALS in Plain Trigonometry, and other Mathematical Sciences depending thereon.

HE excellent Use and indispensable Necessity of this noble Art in all Trigonometrical Calculations, is evident enough to those who are versed therein. Nothing with any Exactines, Ease, or Expedition can be done therein without it; and as Trigonometry is the Foundation (yea the very Essence) of Navigation, Fortification, Altimetry, Longimetry, and is of Use also in divers Cases of Astronomy, Surveying, Dialling, &c. 'tis manifest the Use and Knowledge of Decimal Arithmetick is so requisite in all those Arts and Sciences, that without its Afsistance a Person can make but a gloomy and fruitless Progress in the Study of them.

I shall therefore illustrate the Use of Decimals in the Refolution of all the Cases of Right-lined Trigonometry (for that only is to be understood in this Chapter) both in the Doctrine of Right-angled, and Oblique-angled Triangles, as follows.

Right-angled Triangles.



The Analogy to find the Catbetus.

As the Sine of the Angle C 56:15 Com. Arith. c, 2801536Is to the Bafe B A 24,3 — = 1,3863818 So is the Sine of the Angle 33,45 — = 9,7447390 To the Cathetus or Perpendicular 16,26 = 1,2112744 Cafe

The Ule of Decimals, &c.

Cafe 2. The Analogy to find the Hypothenuse.

As the Sine of the Angle C_{56} : 15 Com. Arith. 0,0801536 Is to the Bafe BA 24,3 — I,3863818 So is Radius 90 — I0,0000000 To the Hypothenufe BC 29:27 — I,4665354

Cafe 3. Cafe 3. Given Stand C, And the Hypothemufe B C; To find the Bafe and Cathetus. B 33.45 A

The Analogy for finding the Bafe.

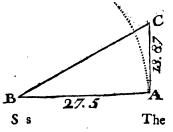
As Radius 90 — 10,0000000 Is to the Hypothenule BC 27:53 — 10,0000000 So is the Sign of the Angle C_{50} : '15 — 9,9198464 To the Bale BA, 22:89 — 1,3597370

Cafe 4. The Analogy to find the Cathetus.

As the Radius 90 — 10,0000000 Is to the Hypothenule BC 27:33 = 10,0000000 So is the Sine of the Angle B 33: 45 = 9,7447390 To the Cathetus, or AC 15:29 — 1,1846296

Cafe 5.

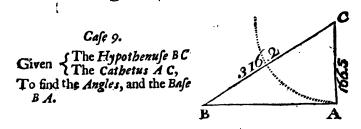
Given $\begin{cases} The Bafe B A, \\ The Cathetus AC; \end{cases}$ To find the Argles, and the Hypothenufe.



The Use of Decimals

The Analogy to find the Angle B. 1,4393327 As the Bafe B A 27:5 Is to the Radius 90 10,0000000 1,1420765 So is the Perpendicular 13:87 To the Tangent of the Angle B 26 : 46 9,7027438 -Then the Angle C is 63 : 14. Cafe 6. The Analogy to find the Hypothenule. As the Tangent of the Angle B 16 : 46 C. A. 0,2972562 Is to the Cathetus AC 13:87 1,1420765 So is the Secart of the fame Angle B 10,0492225 1,4885552 To the Hypothenuse 30:8 The Secant of any Angle is the Arithmetical Com-Note. plement of the Co fine of the faid Angle, added to Radius 10,0000000. $oldsymbol{C}$ Cafe 7. S The Bafe B A, Given The Hypothenule BC; To find the Angles, and the Catbetus A C, The Analogy for the Angle C. Α 2.8 As the Hypothenuse BC 26 1,4259687 10,0000000 Is to Radius 90 So is the Base B A 22:8 1,3579348 To the Sine of the Angle C 58:45 9,9319661 Wherefore the Angle B 31:15. Cafe 8. The Analogy to find the Cathetus. As Radius 90 10,0000000 Is to the Hypothenuse 26 1,4259687 So is the Sine of the Angle B 31:15 9,7149776 1,1409463 To the Cathetus AC 13:83 Caje

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in Trigonometrical Calculations.

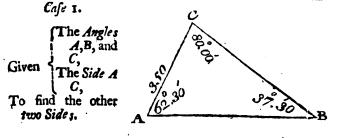
The Analogy to find the Angle C.

As the Cathetus A C 166:5 — Arith. Com. 7,7788467 Is to the Radius 90 — 10,000000 So is the Hypothenufe B C, 316:2 = 2,500369 To the Secant of the Angle C, 58:15 = 10,2788836 Then the other Angle B will be 31:45

Cafe 10. The Analogy for finding the Bafe.

As the Radius 90 Is to the Cathetus 166:5		- =	10,0000000 2,2211533
So is the Tangent of the A	ungle C 58:1	5 ==	10,2084365
To the Base B A 268:92	7 —	- =	2,4295898

Oblique-angled Triangles,

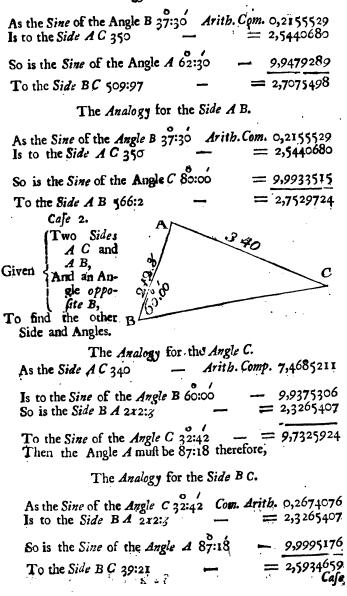


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The Use of Decimals

The Analogy for the Side B C.

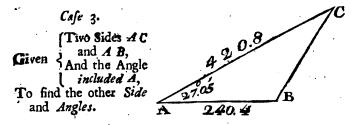


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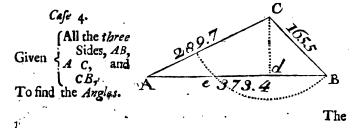


The Analogy for the Angles.

As the Sum of the two Sides 661:2 Com. A. = 7,1796672 Is to the Difference of the Sides 180:4 = 2,2562365 So is Tangent of $\frac{1}{2}$ Sum of the unknown Angles B and C 76:27 = 10,6179795 To the Tangent of $\frac{1}{2}$ their Difference 48:32 = 10,0538832Then, To half the Sum - 76:27 of two Ang. B, C. Add half the Difference 48:32The Sum is - 124:59 = Greater Ang. B. Subfract the $\frac{1}{2}$ Differ. Remains 27:55 = Leffer Angl. C.

The Analogy for the Side BC.

As the Sine of the Angle C	27:55	Arith Com.	0,3295808
Is to the Sine of the Angle So is the Side A B 240,4		»5 =	9,6582842 2,3809345
To the Side BC 23,37		- =	2,3687995



The Analogy for the Segments Ad, and dB.

As the Greater Side or Bafe AB 373:4 Ar. Com. 7,4278258 Is to the Sum of the other two Sides AC + CB = 455.2 _____} = 2,6582023 So is the Difference of the two Sides AC - CB = 124:2 _____} = 2,0941216 To the Difference of the Segments of the Bafe Ae = 151:4 _____} = 2,1801497 Then from the Grea. Side or Bafe = 373:4 Subit. the Diff. of the Segments Ae = 151:4 There will remain eB ______ = 2222 The helf of which is Bd ______ = 222

The half of which is Bd = ed = 111 the Leffer Segm. Also to Ae add ed, the Sum is Ad = 262:4 the Greater Seg.

The whole Oblique Triangle ACB being thus refolved into the two Right-angled Triangles ACd, and BCd, the Angles A, B, and C are found by the feventh Cafe of Right-angled Triangles foregoing.

Having thus pais'd through all the Cafes of Right and Oblique-angled Plain Triangles, in each of which the abfolute Necellity of Decimal Numbers to express the Length of the Sides fought, is sufficiently evident; I shall next shew, in brief, the Application of the foregoing Dectrine of Plain Trigonometry to several Arts Mathematical; intending thereby to convince those who purpose to learn them, of the Necessity of their first learning Decimal Arithmetick.

The Use of Decimals in Navigation exemplified in all Kinds of Sailing.

1. Plain Sailing.

In Plain Sailing, or That by the Plain Chart, the Parts of a Triangle receive new Denominations.

Thus, The Bafe is the Difference of Longitude or Departure;

The Perpendicular is the Difference of Latitude; The Hypothenufe is the Diffance the Ship has run; The Angle at Perpend. is the Courfe of the Ship; And the Angle at Base the Complement of the Course. Admit in the Art of Navigation.

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Admit a С Ship fails from the Lat. North ð Nby 51:30 oni the Rumb. 5*9*8 **A** C Nautic Miles whofe Course is 33 SW bW; Quere her Depar ture В Departure and Difference of Latitude ?

The Analogy for finding the Departure.

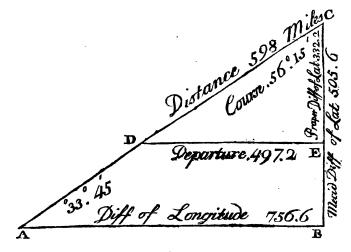
As Radius 90 - Is to the Diffance run AC 598		10,0000000 = 2,7767012
So is the Sine of the Courfe C 56 :	15 -	- 9,9198464
To the Departure Westward from her former Meridian	} 497:2	= 2,6965476

The Analogy for the Difference of Latitude.

As the Radius 90 Is to the Diftance run AC 598	==	10,0000000 2,7767012
So is the Co-fine of the Courfe 33:45		9,7447390
To the Difference of Latitude 332:2	=	2,5214402
But 332,2 Miles are equal to 5:32,2, and being South-wefterly.	the S	Ship`s Courfe
Therefore from the Latitude failed from Subfract the Difference of Latitude		51:30' N. 5:32,2
Remains the Latitude come to -	=	45:57,8 N.
The fame Cafe follows in		Mercator's

Mercator's Sailing.

Mercator's Sailing, or That calculated by his Chart, is much more correct and exact than Plain Sailing: For in this Chart the Degrees of Latitude increase according as the Degrees of Longitude decrease; and these Increments of the Degrees of Latitude are called the Meridional Parts; of which a Table is composed, by Means of which Mercator's Chart is constructed, on which a Ship's Distance, Course, proper and increased Difference of Latitude, the Departure and Difference of Longitude, are truly laid down or delineated, as in the Scheme subjoin'd.



The Analogy for the Difference of Longitude.

As Radius 90° - 10,000000 Is to the Increased Differ. of Lat. 505:6 = 2,7038071 So is the Tangent of the Course 56:15 - 10,1751074 To the Difference of Longitude 756:6 = 2,8789145 The fame Cafe and Data follow in

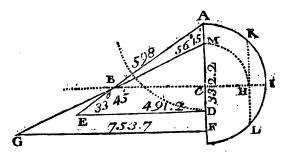
Middle

Middle Latitude Sailing.,

This kind of Sailing is computed from the middle Parallel of Latitude, which is half the Sum of the two Latitudes of the Places, fail'd from, and come to; and depends altogether on the following general Theorem or Analogy.

As the Co-fine of Middle Latitude Is to the Tangent of the Courfe, So is the Difference of Latitude in Miles, &c. To the Difference of Longitude in Miles, &c.

The Reason of this general Analogy is evident in the following Scheme and is deduced therefrom.



Explanation of the Scheme.

$\dot{I}\dot{K} = IL$	Is the Middle Latitude 48.44.
CM = CH	The Co-fine of the Middle Latitude.
AD = MF	The Difference of Latitude.
DE	The Departure Westward.
FG	The Difference of Longitude.
ЯE	The Diftance failed.
ÉлD	The Rhumb or Course SW by W.
BC	The Tangent of the Courfe.

Now 'tis manifeft As CM : CB :: MF : FG, which is the fame as the *Analogy* above in Words at length,

The

The Analogy for the Difference of Longitude.

As the Co. fine of Middle Lat. 48.44 A		
Is to the Tangent of the Courle 56.15 So is the Difference of Latitude 332.2		10,1758074 2,5213990
To the Difference of Longit. 753.7	=	2,8772497

Note 1. The Proportions for finding the Difference of Latitude and Departure in Mecator's and Middle Latitude Sailing, are the fame as in Plain Sailing, and therefore not repenced.

2. That Mecator's Sailing gives the correct Difference of Latitude and Longitude both; Middle Latitude Sailing, only the correct Difference of Longitude; Plain Sailing gives neither correctly; and therefore their Merits are in Proportion.

3. That Middle Latitude Sailing agrees with Plain Sailing in fome Refpects; and with Mercator's in others, very nearly; and therefore is to be used accordingly.

4. That from the foregoing Inflance it is evident no exact Calculations in Navigation can be made without Decimal Numbers; and though I have express'd but one Place of Decimals, yet three Places more may be easily found by Problem 3. of Logarithms.

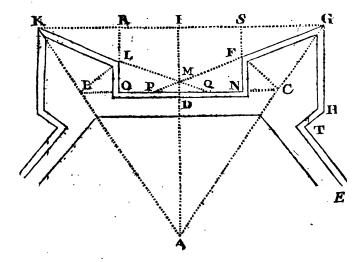
The Use of Decimals in Fortification.

A Fort is a Piece of Ground in Form of a Po'ygon regular or irregular, environ'd with a Rampier, or Wall, and a Ditch to impede the Aflaults of an Enemy.

A Scheme of a regular Pentagmal Fort, with its Explanation, is here after fubjoin'd.

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The



The Explanation, or Names of the feveral Parts.

I.	The	Cartaine				-	ON
2.	The	B4lwark	or Baft	ion	· 🖛	N	FGHT
3.	The	Front of	the Bul	wark			FG
		Flank			-		NF
5.	The	Gorge of	a Bulw	ark		-	NT
6.	The	Gorge L	ine			-	NĈ
		Head Li	ne		-	-	CG
		Shoulder				-	+ F
9.	The	Flanked	Angle		-	(market)	G
10.	The	Inmard]	Manking	Angle			SGF
II.	The	Ontward	Flankin	e Angle	+		KMG
12.	The	Long ft L	ine of <u>I</u>	Defence			PG
13.	The	Sborteft 1	ine of i	Defense			PF
14.	The	Falfe Br	a y		•	******	БC

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A Table

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A Table of the Dimensions of the Angles offerved in Fortifying the regular Polygons following.

Number of the Sides of the Polygons.	· · ·	VI.	VII.	VIII.	IX.	x.
	D M	M Q	D M	D M	D M	D M
Angle at the Centre $-BAC$	72,		51,26	45,00	40,00	36,00
١	_	120,00	128,34	135,00	140,00	144,00
L'Half thereof BCA	\$4,00	60,00	64,17	67,30	70, 0	72,00
1		15,00	15,00	15,00	15,00	15,00
I		75,00	79,17	82,30	85,20	87,00
The Half there'F - FGC		37,30	39,38		42,30	43,30
ngle	19,30	22,30	24,39	26,15	27,30	28,37
eht Angle		00'06	90,00	90,00	90,00	00'06
5 	109, 0	112, 0	114,39	116,15	117,30	118,30
opposite to the Head Li		62,30	64,39	66,15	67,30	68,30
opposite to the Front	86,00	80,00	75,43	72,30	70,00	68,00
Complement of SGF, viz. SFG	00°04	62,30	65,41	63,45	62,30	61,30
je j	1,1,0	135, 0	131,22	127,30	125, 0	123, 0
		42,00	40,001	40,00	40,001	10,02

Tho?

The Use of Decimals in Fortification. 325

Tho' 'tis not neceflary the Angles in Forts fhould be precifely fuch as are before affign'd; yet fuppoling them to be fuch, I fhall fhew how to determine the Quantity of the Sides and Lines of the Pentagonal Fort above in Decimal Numbers by Trigonometrical Calculations, having the Length of the Curtaine and Front of the Bulwark given.

Admit the Curtaine be -ON = 140And the Front of the Bulwark FG = 93 } Yards.

Then the Analogy for the Sine SF, is

As the Radius 90 10,0000000 Is to the Front of the Bulwark FG = 92 == 1,9700368 So is the Sine of the Angle SFG 19.30 - 9,5235000 To the Sine -SF = 31.15 = 1,4935368Again; As Radius 90 10,0000000 Is to the Front of the Bulwark FG = 93 = 1,9700268So is the Co-fine of Angle SFG 70.30 9,9743466 SG = 87.98 = 1,9443834To the Line Then SG = 87.98, and SI = 73. Therefore the whole Sine K = 315.96. Again; as the Sine of the Angle IAG 30.00 A C. 0, 2307813 Is to KG = IG = 157.98**2,1986500** So is Radius 90 10,0000000 To the Semidiameter A G = 268.8 2,4294313 Again; as the Sine of the IAG 30.00 A.C. 0,2307813 Is to $\frac{1}{4}$ the Side of the Pe IG =157.98=2,1986500 So is the Sine of the Angle AGI 54.00 - 9,9079576 To the Perpendicular $A I \stackrel{e}{=} 217.4$ = 2,3373889

Again;

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Again, as the Sine of the Angle FCG 86.00 A.C. 0,0010592 Is to the Front FG = 93= 1,9700368 So is the Sine of the Angle FGC 34.30 9,7531280 To the Line FC = 52.99🕶 1,7 242240 Alfo, as the Sine of F C G 80,00 Arith. C. 0,0010592 Is to the Front Fa = 98**I,970036** So is the Sine of the Angle GFC 59.40 9,9353204 To the Head Line & E = 80.61 = 1,9004104Then AG - CG = AG = 188.19 the Semidiameter of the inner Pantogon. Again, as Radius 95 10,0000000 Is to the Line FC = 52.991,7242240 So is the Sine of the Angle FCN 40.00 9,8080675 To the Flank FN = 24.061,5322915 Then FN + 8F = ID = 65.21. And AI - ID =AD == 152.19 Again, as Radius 90 10,0000000 Is to the Line F C = 52.991,7242240 So is the Sine of the Angle NFC 50.00. 2,8842540 To the Gorge Line NC = 40.59= 1,6084780 Then NC+ND=DC=119,59 And 2DC=BC=221.18 Again, as the Sine of FP 1 19.30 Arith. C. 0,4765047 = 1,5322915Is to the Flank FN = 34So is the Sine of the Augle #FN 70-30 9,9743466 To the Line P N = 96.19 = 1,9831428 Then O N - P N = O P = 42.81 the fecond Flank. And ON + SG = RG = 227.98. Then in the Triangle ROG As

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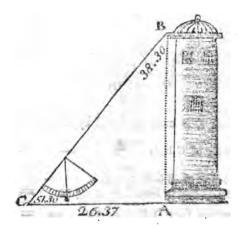
The Use of Decimals in Altimetry, &c. 327 As the Line RO(=ID) = 65.21A. C. 8,1856858 Is to the Line R G = 227.982,3578967 So is Radius 90 10,0000000 To the Tangent of the Angle ROG 74.02 10,5435825 Then, as the Sine of ROG 74.02 Arith. C. 0,0170850 Is to the Sine RG = 227.28= 2,3578967 So is Radius 50 10,0000000 To the Line of Defence OG = 237.13 2,3749817 Thus having the Angles as in the Table, you are here

taught the Manner of finding the Sides and Sines of any regular Fort, in any Measure, and Decimal Parts thereof.

The Use of Decimals in Measuring Heighths, Depths, and Distances; both accessible and inaccessible.

1. Altimetry, or the Menfuration of Altitudes and Depths, is thus performed.

Let A B reprefent a Tower whole Height is required. Suppose { The Diftance AC = 26.37 Yards. The Angle ACB (found by a Quadrant) 51.30.

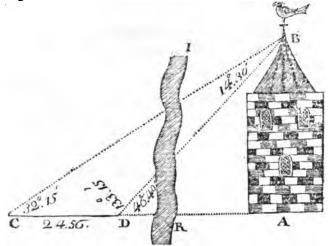


The Analogy for finding the Height A E.

As Radius 90 Is to the Diffance AC = 26.37 - = 10,0000000 Is to the Diffance AC = 26.37 - = 1,4211101 So is the Tangent of ACB = 51.30 - 10,0993948 To the Height of the Tower AB = 33.15 = 1,5205049

And thus the *Height* or *Altitude* of any other *acceffible* Object may be found.

Suppose the Steeple A B be *inacceffible* for the River R I; Then with a Quadrant at C take the Angle A C B, and meafure a Diffance to D, where take again the Angle A D B; and let those Angles, and the Diffance be as in the adjoin'd Figure.

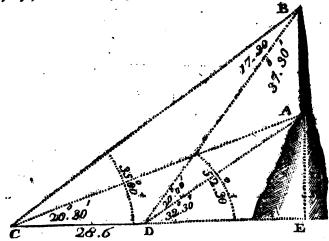


Then **DB** must be found by this Analogy.

As the Sine of C B D 14.30 — C. A. 0,6014004 Is to the Sine of B C D 32.15 — 9,7272276 So is the Diftance or Side C D = 24.56 = 1,3902284 To the Vifual Line D B = 52.34 — = 1,7188564Having Altimetry, or Measuring Altitudes. 319 Having found D B, you may find AB, thus;

As Radius 90 — 10,0000000 Is to the Line DB = 52.34 — 10,0000000 Is to the Line DB = 52.34 — 10,0000000 I,7188564 So is the Sine of ADB 46.45 = 9,8623526 To the Height required AB = 38.12 = 1,5812090 Thus you find the Height of any inacceffible Objects.

If the Object whole Height you would measure flaudeth shoft, as on a Hill, Sec. as the Tower AB; then take the Angles BCH 35.00, ACH 20.30; then from C measure the Difference CD = 28.6 Yards, and at D, take the Angles BDH 52.30, and ADH 32.30, as below.



Then the Analogy for finding the Side D B, is

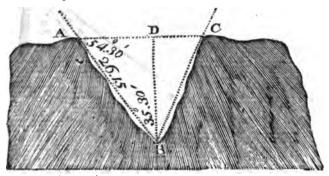
As the Sine of CBD 17.30 — Arith. Com. 0,5218582 Is to the Sine of BCD 35.00 — 9,7585913 So is the Side of Diftance CD = 28.6 = 1,4563660To the Vifual Line DB = 54.55 = 1,7368155U u Then Then fay, as the Sine of Complement of BAD >

(to 180) 57.30 A. C. _ 50,0739708Is to the Sine of B D A 20.00 _ 9,5340517

So is the Side DB = 54.55 - = 1,7368155 To the Height of the Object AB = 22.12 = 1,3448383

Depths, if Perpendicular, are most conveniently measured with a Line and Plumet; but if the Depth be flarting, such as Valleys, &c. and the perpendicular Profoundity be required; do as follows.

Let A BC be a Valley, whole oblique Defcents or Sides are AB, and BC; and its perpendicular Depth BD required. Then measure the Side AB, or BC, and take with a Guadrant the Angle ABD, or DBC, whereby the others will be known; then (fuppofing them as below) use the following Analogy.



The Analogy for finding the Depth D B.

As Radius 90 — 10,0000000 Is to the flast Defcent AB = 26.15 = 1,4174717So is the Sine of BAD 50.30 — 9,9106860 To the Perpendicular Depth DB = 21.28 = 1,3281577The fame might have been equally found by the other Right-angled Trilangle CDB, by the fame Method. 2. Lon giv. Longimetry, or measuring Distances. 331

2. Longimetry, or the Menfuration of the Diftances of Oljeors, either from Us, or from one another, is thus performed.

Let A, B, be two Trees; and let it be required to find the **Diffance** of A from C or D; as also of B from the fame two **Points**; and the Diffance of A from B.

Having (by a Theodolite or Semicircle) at D, found the Angles BDC, and ADB; and at C the Angles ACD and ACB; and measured the Distance of the two Stations CD, as below: Use the following Analogies.



The Analogy for finding AC.

As the Sine of the Angle CAD 10.15 A. C. 0,5531072 Is to the Diffance of Stations CD = 25.05 = 1,3988077So is the Sine of the Angle ADC 76.45 — 9,9882821 To the Diffance AC = 87.33 • — = 1,9411972

The Analogy for the Distance AD.

As the Sine of the Angle C AD 16.15 A.C. 0,5531072 Is to the Diffance of Stations C D = 25.05 = 1,3988277 So is the Sine of A C D 87.00 - = 9,9994044To the Diffance AD = 89.39 - = 1,9513193

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The Analogy for the Diftance BC.

As the Sine of the Angle C B D 18.15 A. C. 0,5042284 Is to the Diffance of Stations CD 25.05 = 1,3900077So is the Sine Comp. of the Angle BDC 9,99979 (to 180.) 88.15 To the Differer B C # 7995 ₩ 1,902833' The Analogy for the Distance BD. As the Sine of the Angle C BD 18:15 A.C. 0,5042284 Is to the Diffence of Stations CD = 25,05 = 1,398807 So in the Sine of the Angle BCD 70.30 9,9743460 To the Diffance BD = 144 The Analogy for the Diffance of the Pensifrom each other, viz. A B. But firft fty As the Sum of the two Sides, AC+CB = 7,7765050 167.28 Arith. Comp. Is to their Difference A.C - CB = 7.38 = 0,8680564 So is the Tang. of half the Angles ABC+BAC 9,9<u>9</u>54822 81:45 To the Tangent of half their Difference ABC-BAC 2.30 Then the Angle CBA 84.15; and the Angle BAC 79.15. Wherefore the Analogy for the Diftance A B, is, £ ••• As the Sine of the Angle ABG 84.15 1.6. 0.0021917 Is to the Diftance of A C = 87.33= 1,9411972 Bo is the Sine of the Angle A C B 16.30 - 9,4533418 To the Dift. of the two Trees AB = 24,93 = 1,3967307Thu[§]

The Use of Decimals in Mensuration, &c. 333

Thus I have endeavoured to make it appear how abfolutely neceffary the Use and Knowledge of the noble Art of Decimal Arithmetick is in those Parts of Mathematical Science, which require Triggnometrical Calculations, by Examples in the most common and useful Arts; I might have gone farther, and shewn its Use in several Parts of Astronomy, Sc. but I intend only an infructive Specimen of its excellent Use in this Kind of Learning, and such I prefume this Chapter will be found to be.

CHAP. XIV.

3

The great life of DECIMALS in the Menfuration of all Kinds of Superficies and Solids.

N this Track (wherein the Use of Decimal Arithmetick in most obvious, necessary, and excellent) I have only this to adversife the Reader, That the Numbers are abfolutely taken; and may represent any Dimensions, is Dickes, Feet, Yards, Rods, Miles, Acres, &cc. in the Area's, and Solid Content of Bodies. And that after the Area, or Content is found, I thall thew the Manner of Reducing it to any of the Dimensions used in Surveying, Guaging, &cc. by means of Decimals.

E Proposition 1. To measure a Square.

Rule. Multiply a Side into it felf, the Product is the Area or Sware Content.

Avanple, Suppose the Side AB = 12,6 Multiply by in felf, _ 12,6



The Square Content or Area is = 150,4

Propo_

The Use of Decimals in the

Proposition 2. To Measure a Paralellogram.

Rule. Multiply the Length by the Breadth, the Product is the Area, or Content.

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Example. Mult. the Length AB=16,5 By the Breadth BD= 8,6



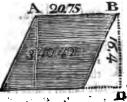
The Product is the Content = 141,9

Proposition 3. To Measure a Rhombus.

Rule. Multiply one Side into the perpendicular Height, the Product is the Area or Content required.

> - 8303 124545 207575

Exam. Mult. the Side AB = 20,78By the Height BD = 16,4

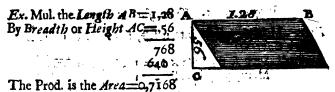


Ex.

The Product is the Area = 340,474

Proposition 4. To Measure a Rhomboides.

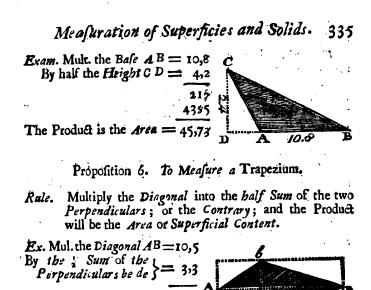
Rule. Multiply the Length by the perpendicular Height, or Breadth, the Product is the Content.



Proposition 5. To Measure a Plain Triangle.

Rule. Multiply the Base into half the Perpendicular Height; or the Whale perpendicular Height into half the Base; the Product will give the Atea.

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The Prod. is the Content =34,65

Proposition 7. To Measure a Parallelopleuron.

315 315

Rule. Multiply the Diagonal by the half Sum of the two Perpendiculars, the Product is the Area.

Exam. Mult the Diagonal AB=14.3By $\frac{1}{4}$ Sum of cd and cb = 6.3

. 1

The Product is the Content = 90,3

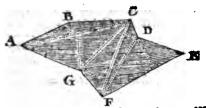
Proposition 8. To Measure an irregular Polygon, or Polygram.

Rule. Divide all fuch multa galar and irregular Figures into Trapeziums and Triargles, then measure them by Prop. 5 and 6. Example.

The Use of Decimals in the

Example. Divide the irregular Polygon ABCDEFG into the Trapezium ABCG, then into the Triangles GCF, CFD, and FDE which are to be meafured as taught in Pro-

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position 5, and 6, and the Sum of all added together, will give the Superficial Content or Area of the given Polygram.

Propolition 9. To Measure any regular Polygon, as a Pentzgon, Hexagon, Heptagon, Octagon, Nonagon, Sc.

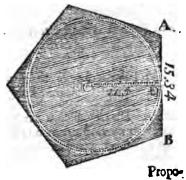
Rule. Multiply half the Sum of its Sides into the Radius of the Circle inforibed in the Figure ; or balf that Radius into the Sum of the Sides, the Product will be the area theorem.

Engender Suppose the Side of the } A E	3=15,34
Multiply by the Number of Sides -	2,5
	7670 306 8
The Product is the ½ Sum of the Sides — Multiply that by the Radius CD —	= 38,35 = 10,5
	19175
the build in the Area	102,675

The Product is fac Area

A Tubic of the Siles of Polygons to the Radius of a Circle inferibed.

Trigon, as 1:0,288675 &c. Pentagon, as 1:0,08819 &c. Odfagon, as 1:0,08819 &c. Decagon, as 1:1,538841 &c. Dedcagon, as 1:1,866320 &c.

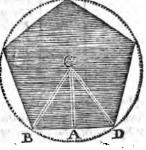


Mensuration of Superficies and Solids. 337

Proposition 10. To find fuch constant Multipliers for any of the Regular Polygons, That multiplying the Square of any Side thereby, the Product shall be the Area of the Polygon.

Example. In a Pentagon.

Div, the whole Circle, viz. 360 Deg. By the Number of Sides ; here 5. The Quotient is the $< BCD = 72^{\circ}$ The $\frac{1}{2}$ thereof is the $< A^{C}B \equiv 36^{\circ}$ Whole Comp. is the $< ABC \equiv 54^{\circ}$



Then make this Proportion ;

As the Sine of the Angle A C B = 36 = 0,2307813Is to half the Side (= 1, always) = ,5 = ,9,6989700 So is the Sine of the Angle A B C = 54 = 9,9079576

To the Perpendicular, or Radius of the inferibed Circle - AC = ,68819 = ,9,8377089.

Then (by the laft Proposition) Arith. Comp. = 0,68819 Multiplied into $\frac{1}{2}$ Sum of the Sides - = 2,5 344095 137638The Product is the Area - = 1,720475

And thus may the Area for any other Polygons be found whole Side is 1. And this Area will be the conflant Multiplier for that kind of Polygon. A Table of fuch Multipliers, or Area's, for the legeral Regular Polygons follow.



Sides

Sides.	Name s.	Multipliers.
3	Trigon	0,433013
4	Tetragon	1,000000
Ś	Pentagon	1,720475
6 ·	Hexagon	2,598076
7	Heptagon	3,633959
. 8	Octagon	4,828427
9	Ennengon	6,181827
10	Decagon	7,69+209
11	Endecagon	8,514250
12	Dodecagon	9,330125

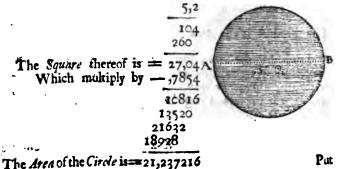
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Now as thefe are the Area's of each Polygon respectively, whole Side is 1; and as the Area's of Like Figures, are as the Square of their bomologous, or like Sides; therefore the Square of a Side of any of those Polygons multiplied into its respective Area in the Table, will produce the true Area thereof.

Example. Suppose the Side of a Heptagon be 10; the Square of which is 100; but $100 \times 3,633959 = 363,3959 =$ Area of such a Heptagon, and the like for any other.

Proposition 11. To Measure a Circle.

- Rade. Mukiply the Square of the Diameter (if that be given) by 0,7854; the Product is the Area. Or, (if the Periphery be given) Multiply the Square of the Periphery by 0,07957; the Product is the Area, as before.
- **Exa.** Suppose the Diameter of a Circle be AB = 5,2



M-nsuration of Superficies and Solids. 339

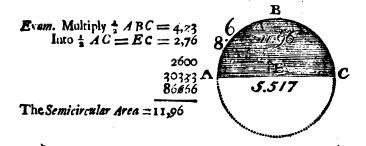
Put D = Diameter; P = Periphery; and A = Area, of any Circle.

Then it will be $\begin{cases} 3,1416D = P. & \text{And } 0,7854DD = A. \\ 0,3183P = D. & \text{And } 0,07957PP = A. \\ \sqrt{1},2732 = D. & \text{And } \sqrt{12,5664A} = P. \end{cases}$

Thus by those fix Theorems may all the Varieties relating to the Diameter, Periphery, and Area's of Circles be folved.

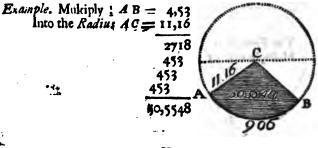
Proposition 12. To Measure a Semicircle.

Rule. Multiply half the Semicircular Arch, into half the Diameter; the Product is the Area.



Proposition 13. To Measure the Sector of a Circle.

Rule. Multiply half the Arch into the Radius, the Product is the Area of the Sector.



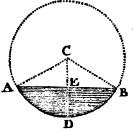
X x 2

Propor

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Proposition 14. To Measure the Segment of a Circle.

Rule. Compleat the Sector ACBD, and measure it by the last Proposition; and then find the Area of the Triangle ABC by Proposition <. Then subduct the Area of the Triangle from the Area of the Sector, the Remainder is the Area of the Segment.



Or thus, (by the Curious Theorems of Mr. Ward.)

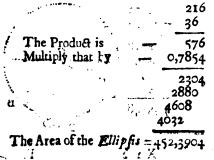
R = The Radius, or Semidiameter AC. Let A = The Diff between the verfed Sine and Radius. C = Half the Chord or Bafe of the Scg. AE (viz. EC.)

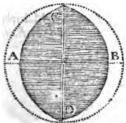
Theorem $\begin{cases} \frac{2}{3} \frac{RR}{R} - \frac{1}{3} \frac{Rd}{d} - \frac{dd}{d} \times C = S, & \text{The Area} \\ \text{of the Segment.} \end{cases}$

Proposition 15. To Measure an Ellipsi.

Rule. Multiply the Transverse and Conjugate Diameters into each other; then multiply that Product by the Number 0,7854, the Product is the Area required.

Exam. Mult. the Transverse CD = 36By the Conjugate AB = 16



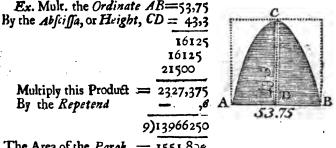


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Mensuration of Superficies and Solids. . 341

Proposition 16. To Measure the Parabola.

Rule. Multiply the Greatest Ordinate, or Base, into the perpendicular Height, and that Product by the fingle Repetend , 8, the Product is the Area.



The Area of the Parab. = 1551,80%

Note, an eafier way is to multiply the first Product by 24 and then divide by 3 for the Area; fince $\frac{2}{2} = \mathcal{B}$

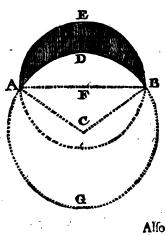
Proposition 17. To Measure the Circular Space, called. Lune; (being like the falcated Moon.)

Rule. In order to find the Area of the Lune A E B D, feek first the Area of the Semicircle AEB, by Prop. 12. Then find the Area of the Segment ADBF of the Circle ADBG, by Prop. 14.

Laftly; Substract the Area of the Segment from the Area of the Semicirle ; there remains the Area of the Lune required.

i. •1

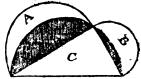
4.1.2



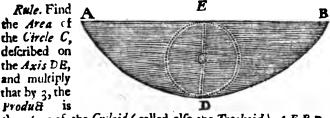
- |

Alfo the two Lunes A, B, are together equal to the Triangle C.

Note, This is call d the Quadrature, or Squaring the Lunes of Hippocrates.



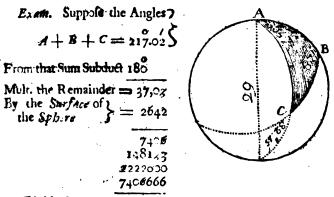
Propention 18. To Measure the Cycloid.



the Area of the Cycloid (called also the Trochoid) A E B D.

Proposition 19. To Measure a Spherical Triangle.

Rule. From the Sum of the three Angles, fubduct 180 Degrees, multiply the Superficies of the whole Sphere or Globe by the Remainder; this Froduct divide by 720, the Quotient is the Content or Area of the Triargle.



Divide by 720) $\overline{978}_{\pm 2}$, \mathcal{C} (135,891 = Area of the Triarg e.

Note,

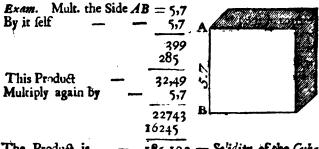
Mensuration of Superficies and Solids. 343

Note, This is a very uncommon, curious, and useful Propolition.

Mensuration of Solids.

Proposition 20. To Measure a Cube,

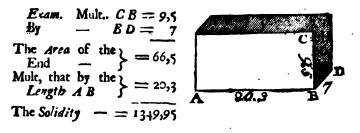
Rule. Multiply the Side of the Cube into it felf, and that Product again by the Side; this last Product will be the Solid Cortent, or Solidity of the Cube.



The Product is - 185,193 = Solidity of the Cube.

Proposition 21. To Measure 4 Parallelopipedon.

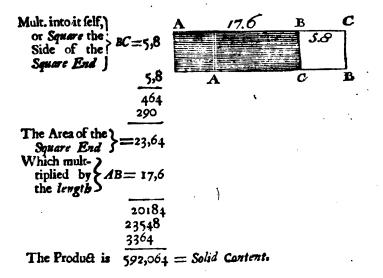
Rule. Find the Area of the End or Bafe, and Multiply that by the Length of the Piece, the Product is the Solid Content thereof.



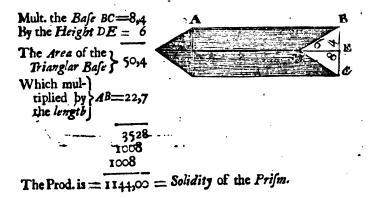
Exam-

i.

Example 2. Of a Square Prism, or Parallelopipedon.



Example 3. Of a Triangular Prism.



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Memsuration of Superficies and Solids. 345,

Example 4. Of a Cylinder.



the Cylinder S= 1022,2 Proposition. 22. To Measure the Convex Superficies of \$

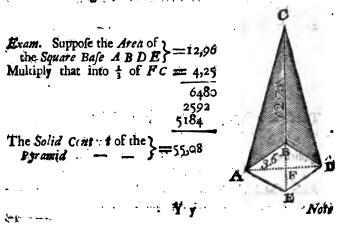
Cylinder.

Rule. Multiply the Periphery of the Base into the Length of the Cylinder; the Broduct is the Content.

Example. Suppose the Circumference of the Bafe 20,944 (in the last Figure) BECD to be _____ 23,944 Then multiply that by the Length AB _____ 23 62832 41888 The Superficial Content of the Cylinder _____ 481,712

Proposition 23. To Measure a Pyramid.

Rule. Multiply the Area of the Bafe into one Third of its Altitude or Height; the Product is the Solid Content.

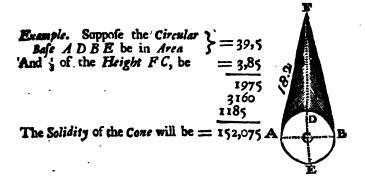


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Note, The Rule is general for any kind of *Pyramid* whole Base is any regular Polygon.

Proposition 24. To Measure a Cone.

The Rule is the very fame as for the *Pyramid* in the laft Propentition.



Propolition 25. To Measure the Curve Superficies of a Cone.

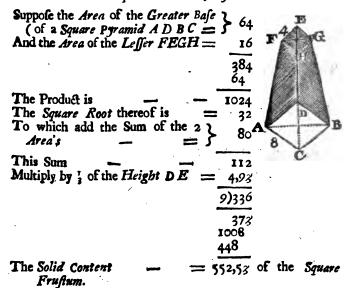
Rule. Multiply the Periphery of the Base into the Length of the Side; Half that Product is the Content or Area of the Curve Surface.

Example. Suppose the Periphery ADBE (of } 23,6 the Cone above) be That the Length of its Side AF = 18,2 472 1888 236 429,52 The Convex Superficies of the Cone will be found } 214,76

Bropolition 26. To Measure the Frushum of a Pyramid or Cone, cut parallel to its Base.

Rule. Multiply the Area of the Greater Base, by the Area of the Leffer, and extract the Square Root of the Product; To Mensuration of Superficies and Solids. 347 To that Root, add the Sum of the two Area's of the End; then multiply this last Sum by ; of the Frustum's Height, the Product is the Solid Content.

Example 1. Of any Pyramid.



And thus the Frustum of any other kind of Pyramid is to be found.

Example 2. Of a Cone,

Suppose the Area of the Greater Base 122,6 (of the Cone adjoin'd) ADBC = 11,2And the Area of the Leffer FEGH = 11,2 2452 1226 1226 1226 1373,12

Yy 2

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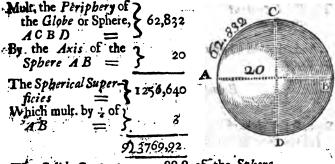
E

The Square To which a	Root the	ereof is n of the two	Area's	s ==	= 37,055 133,8	£i.
This <i>laft St</i> Multiply by	m z of the	Height K E			170,855 6,75	
	• •			1	854275 1195985 225130	
The Solid	Content		••••		53,27 125	I

Proposition 27. To Measure a Sphere, or Body perfectly Round.

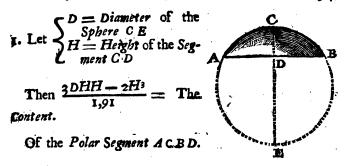
Rule. Multiply the Diameter into the Circumference, the Product is the Superficial Content; then multiply that by $\frac{1}{2}$ of the Diameter, the Product will be the Solid Content of the Sphere.

Example. Of the Superficial and Solid Content.



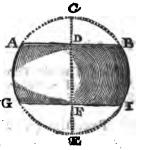
The Solid Content = 4188,8 of the Sphere.

Proposition 28. To Measure any Frustum or Segment of a Sphere or Globe. 1. Let Mensuration of Superficies and Solids. 349



2. Let $\begin{cases} D = Diameter \ C \ E, \ as \\ before, \\ x = the \ Bafe \ AB = GI. \\ FI = the \ Thickness \ DF. \end{cases}$

Then $\frac{2DD + xx}{33^{2}} \times H =$ the Middle Segment ABIG, called the Zone. By these two Theorems, may the Solidity of any Segment of a Globe or Sphere be found.



To find the Superficial Content of any Segment, as

Thus So is the Height of any Segment, To the Area of its Curve Superficies.

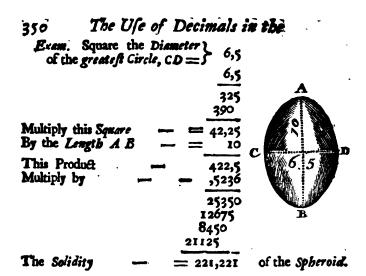
Proposition 29. To find the Content of a Spheroid.

Rule. Multiply the Square of the Diameter of the Greates Circle; by the Length; then multiply that Product by 0,5236; this last Product will be the Solidity of the Spheroid.

Eran.

- I

and and a



Note, The two Theorems, which find the Content of the Segments of a Sphere, find those like Segments of the Spheroid, if in them D be made = CD, in this Spheroid.

Proposition 30. To Measure a Parabolic Conoid.

Rule. Multiply the Square of the Diameter of the Bafe by the Height; and that Product by 0,3927; this last Product is the folid Content.

Exam. Mult. into it felf, or 9,2 fquare the Diameter AB=5 9,2 D 184 828 This Source 84,64 Multiply by the Height CD = 10 And the Product 846,4 Multiply by ,3927 5*9*248 16928 76176 25392 The folid Content = 332,38128 of the Parabolic Conoid.

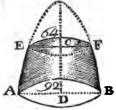
Propo-

Mensuration of Superficies and Solids. 351

Proposition 31. To Measure the Frustum of a Parabolic Conoid.

Rule. Add the Square of the Diameter of the Leffer Bafe to the Square of the Diameter of the Greater Bafe, Divide that Sum by 2,5464; then multiply the Quotient by the Height; the Product is the Solid Content.

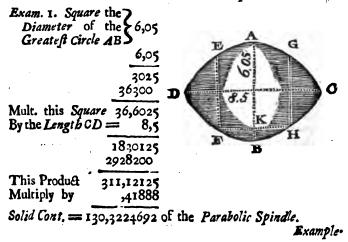
Exam. The Square of AB = 84,64And the Square of EF = 40,96Sum of the Squares - = 125,6



Then 2,5464) 125,600 (49,3244 $\frac{101856}{237440} \underbrace{5 = CD}_{246,622} \text{ the Height.} \\
\underline{229176}_{8264} \underbrace{5 = CD}_{8264} \text{ the Solidity of the}_{(Fruftum A B F E.} \\$

Proposition 32. To Measure a Parabolic Spindle, or Pyramidoid.

Rule. Multiply the Square of the Diameter of the Greatest Circle, by the Length; and that Product by 0,41888; this last Product is the Solid Content of the Spindle.



352 . The Use of Decimals in the

Example 2. To Measure the Middle Segment of the spindle, EGHF.

Let $\begin{cases} D = \text{the Diameter of the greateft Circle A B.} \\ C = \text{the Diameter of either Bale or End EF or GH}, \\ x = 2BK = \text{the Ruces of AB above EF, or GH}, \\ L = \text{the Length of the Frastum F H.} \end{cases}$

Theorem
$$\left\{\frac{2DD+CC-0,4\times\pi}{3,82}\times L=\right\}$$
 solidity of the middle Frustum.

Proposition 33. To Measure any of the Five Regular (or Platonic) Bodies.

Those Bodies being only an Aggregate of fo many Pyramids as they confiss of Sides, each Side being the Base of a Pyramid, may, with due Confideration, be measured by Proposition 22. However for the more ready and expeditious Practice, I shall here subjoin a Table of the Solidity and Superficies of each Body whose Side is 1. or Unity.

Sides,	Names.	Superficies.	Solidity.
4 Tri,	Tetrabedron	1,732051	0,1178511
6 Sq.	Hexabedron	,6,000000	1,0000000
8 Tri.	Octabedron	3,464102	0,4714045
12 Pent.	Dodecabedron	20,645729	7,663119
20 Tri,	Icofabedron	8,660254	2,181695

* To use the preceeding Table for finding the Superficies of any of those five Bodies, do thus;

Square the Given Side of the Body, and by that multiply the Tabular Superficial Number; the Product is the Superficies of the Body, which was fought.

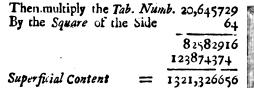


Exam-

Example. Suppose the Side of the Dodecabedron be ϑ , the square of which is δ_{\downarrow} .

Tetrahedron.





Dodetabedron.

To find the Solid Content; Multiply the Tabular Number of the Solidity, by the Cube of the Side given, the Product is the Solid Content.

Example. Of the aforefaid Dodecabedron.



Icosahedron.

Multiply the Tabular Numb. 7,663119 By the Cube of the Side 512(=8,) viz. 51215320238 7663119 38315595 Solid Content = 3923,516928

20238 3119 525 16928

And thus proceed for the Supe ficies and Solidity of the other Bodies.

Proposition 34. To Measure any folil or hollow Body bow irregular soever.

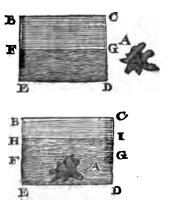
Rule. Take any $V \in \iint i$ in Form of a Para'lelopipedor, and fill it with Water to a certain Height, and then immerfe Z z the

The Use of Decimals in the

the irregular Body therein, and observe how much the Water is raised by the Side of the Veffel; for that Water is equal in Quantity, or Solid Content, to the irregular Body; and may be found by Proposition 20.

Example. Suppose the Veffel BCDE, in Form of a Parallelopipedon, whole Length is two Feet, eight Inches; and Breadth one Foot, ten Inches; and it be fill'd with Water to FG, twelves Inches Deep = EF. And it is reguired to measure the Log A, of a most irregular Form. In order to do this, I take and immerge the Log in the Veffel of Water (as in the lower Figure) and obferve the Water rife from FG to HI, the Height of which (viz. FH,

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or GI) I measure, and find to be 5,5 Inches.

Then by Proposition 20, I find a Body of Water, 2 Feet, 8 Inches in Length; I Foot, ten Inches in Width, and 5,5 Inches Deep, to contain 3520 Solid Inches, or 2,037 Solid Feet; which therefore is the Solid Content of the Log A?

Proposition 35. To affign the Dimersions by which the feveral Artificers measure their Work.

· (r Superfi.ial	As Pavements, Chimneys, Pieces,
Mafons measure & Feet and their Work by Inches) Solid	Cornifhes, &c. Columns, and o- ther folid Parts of Buildings.

Bricklayers meafure by the Yard; Pavements, Pieces, &c. Rod; All manner of Walls, and Chimneys. Square; All manner of Tyling, and Slating.

Ga: Bankers mea- S Equare of Roofing, Partitioning, Floorruce by the 100 Feet Sing, Gc.

Jqin-

Mensuration of Superficies and Solids. 355

Joiners, Painters, Plaiste- Square Yard for the most part; rers measure by the feldom, by the Foot Square.

Glafiers measure their { Decimal Foot Square ; very rarely by Work by the { Inches and Quarters.

Solid Inches.

- Gaugers measure the Area's 231, For Wine Gallons. and Content, of Superficies and Solids, by 268,8. For Corn Gallons.
- Surveyers measure ; Rod or Pole ; but mostly by the Chain's Land by the for an 100 Links = 4 Rod.
- Proposition 36. To affige Multipliers, and Divisors, whereby the Gauger may readily find any Area or Content in Gallons or Buthels, whether the Dimensions be taken in Inches, Feet, or Yards.

This I shall do by disposing the Numbers in their proper Order in the Table subjoin'd.

Dimensions.	Multipliers.	Divisors.
Inches.	0.004329 W. G 0.003546 A. G 0.003722 C. G 0.000465 C. E	. 282 A.G. 268.8 C.G.
Feet	7.48052 W.G 6.12765 A.G 6.42448 C.G 0.80356 C.E	. 0.16352 A.G. 0.15565 C.G.
Yards	67.32468 W.G 55.14885 A.G 57.82032 C.G 7.23204 C.B	. 0.018168 A.G. . 0.017294 C.G.
Note,	W.G. 7 A. G. 7 C. G. 6 C. B. 6	Wine Gallons. Ale Gallons. Com Gallons. Com Buschels.

ZZA

The

The Use of the preceeding Table.

If by the foregoing Propositions the. Area or Content of any Superficies or Solid be found; and you would know how many Wine, Ale, or Corn Gallons, or Bushels it contains; Mukiply, or Divide, the given Area or Solidity, by the Tabular Number corresponding to the respective Measure, and Dimension, the Product is the Area or Content sought in Gallons, or Bushels.

Example. Suppose the Parallelopipedon in Example 1. of **Proposition 20.** represent a Ciflern, and the Dimensions there used be Feet; then the folid Content of the Ciflern is there found to be 1349,95 Solid or Cubick Feet.

Then $\begin{cases} 1349,95\times7,48052 = \text{Content in Wine Gallons.} \\ 1349,95\times6,12765 = \text{Content in Ale Gallons.} \\ 1349,95\times6,42448 = \text{Content in Corn Gallons.} \\ 1349,95\times6,80356 = \text{Content in Corn Bufbels.} \end{cases}$

Or by Division.

Thus $\begin{cases} ,13368 \} 1349,95 (= \text{Content in Wine Gallons.} \\ ,16352 \} 1349,95 (= \text{Content in Ale Gallons.} \\ ,15565 \} 1349,95 (= \text{Content in Corn Gallons.} \\ 1,24446 \} 1349,95 (= \text{Content in Corn Bulbels.} \end{cases}$

And were Dimensions taken by a Decimal Yard or Foot (which are by far the best Instruments for Mensuration;) The Business of Gauging would be easy, and greatly expedited by a Table not before extant, that I know of.

Note; If you would find the Content of Circular Area's at one Operation (without reducing them by the common Multiplier 0,785398) do thus,

Divide the Square of	S	359,05 for Ale Gallons. 294,12 for Wine Gallons.
the Diameter by	7	342,24 for Corn Gallons. 2738, for Corn Bushels.

But

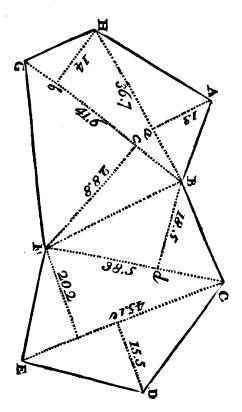
Mensuration of Superficies and Solids. 357

But in this Cafe the *Dimensions* must be understood of Inches only.

By what I have fuid in this Froposition, I suppose the dexterous young Artist will be easily apprised of the Nature, Manner, and Reason of Gauging; and how to apply the foregoing Propositions to that purpose.

Proposition 37. To apply the foregoing Propositions of Superficial Mensuration to Surveying.

Suppose a Field in Form of an Irregular Polygon; as ABCDEFGH, below.





The Use of Decimals in the 258 The Field being measured, Plotted, and the Plot refolved into Trapezia, and Triangles, as per Proposition 8. Proceed to find the Contents of the Triangles by Propofition 5. and of the Trapezia by Proposition 6. Thus for the Area of the Triangle H A B. Multiply half the Base HB = 18,35By the Perpendicular A a = 12 5505 1835 238,55 = the Area. For the Area of the Triangle FBC, $\frac{1}{1}FC = 19,25$ Multiply By the Perpendicular Bd = 18,59625 15400 1925 356,125 == the Area. For the Area of the Trapezium BHGFB, Multiply half the Diogonal GB = 20.8By the Sum of the Perpend. Hb+Fc=42.81664 416 832 890,24 = the Area. For the Area of the other Trapezium CDEFC, Multiply half the Diagonal CE = 27,55By the Sum of the Perpend. De + Ff = 35,719285 13775 8265 To this laft 983,535 = the Area. 890,24 Add the other Area's 356,125 238,55 2468,45 = the Field. The Sum of all is the Content -Now

Mensuration of Superficies and Solids. 359

Now if the Numbers are supposed to be Poles or Rods, Divide the Whole Superficial Content or Area of the Field, by 160, the Quotient will be the Number of Statute Acres the Field contains. See the Work.

160) 2468,45 (15, 16	4278 Acres; Acres	; Rood Rods	Yards
86	Or, 15 :	1:28	: 13
80 68			
64			
• 44		·	
125 112			
• 130 128		•	
••• 2		x	

But if the Field was measured with a Chain of an 100 Links (=4 Rods.) Then, because an Acre contains 10 Square Chains, and every Square Chain containing 10000 Square Links, therefore a Square Acre will contain 10000 Square Links; and hence the Reason of firiking off 5 Figures to the Right-hand from a Given Area in Links, and taking the Rest for Acres. In this Case, the Area of the Plot above would be but, 0246845 of an Acre; i.e. about 3 Poles and 7 Yards, Square Measure.

But suppose the Figure above represent the Plot of a large Common whole Dimensions are taken in Chains and Decimal Parts of a Chain: Then the Area thereof would be 2468,45 Square Chains, which is 246,845 Acres; Or, 246 Acres, 3 Roods, 14 Poles.

And thus may any Area, or Superficial Content of any Field or Plot of Ground (found by fome one of the first 19 Propositions of this Chapter) be turned or resolved into Acres by this Proposition.

Note, By the nineteenth Proposition you may find, with ease, the Number of Miles or Acres contained in the Whole, or any Part, of the Superficies of the terrestrial Globe; and of any Province, Kingdom, Empire, or Nation of the World; and 360

and it ought therefore to be well underftood by all who would fludy *Folitical Arithmetick*, this being the most certain, curious, and principal Branch of that Art; Tho' it be not inevery Tract on that Subject, nor in any Book of Mensuration that I know of.

I hus I have finithed a Tract of *Planometry*, and *Stereometry*, or of the *Menfuration* of *Superficies* and *Solids*; containing a *Greater* Variety than I know to be in many Books, wrote wholly on the Subject, of two, three, or four Shillings *Price*; having endeavoured here, as in all other Parts of this *Syftem*, to oblige the *Reader* with all that could be *ufeful* for him to know, in the most plain but *Compendious Manner*, at the eafleft Rate.

Vive, Vale; Si quid novisti rectius istis, Candidus imperti; si non, bis utere mecum.

FINIS.



TABLE

OF THE

LOGARITHMS

TO ALL

NUMBERS,

Not exceeding 10000, or 4 Places, whether they be Intire, Broken, or Mixt Numbers.

Particularly useful in Extracting the Square Cube, &c. Roots, and folving Questions in Compound Interest, &c.

Ass

Artificial Numbers : Or,

Natural	• •	, I	2	3	4
Ni mbers.	0000000	0413927	0791812	1139433	1461280
2	3010300	3222103	3424227	3517278	3802112
. 3	4771212	4913617	5051500	5185139	5 : 14789
	6020600	61278 8	6232.93	4334684	6474527
5	6989700	7075702	7160033	7=4=759	7323937
1.5	7781918	7853200	79:3917	.7903405	8051800
7	8450980	8512583	8573325	8033229	
8	9030900	9084850	9138138	9190;81	9242793
9	9542425	9190414	9617878	9584829	9731278
100	6000000	0004341	0008677	0013009	
101	0013214	0047511	0051805	0056094	0060379
. 402	0.8408-	0000 157	0094509	0098756	
10,3	0128372	0132587	0136794		0145205
104	0170353	Gt71507	0178697	0482843	0187005
105	0211893	0216027	0220157	0224284	0228400
106	0253059	0257154	0261245	0265333	0269416
107	0293838	0297895	0301948	0305997	0310043
108	0334237	0338297	0342293	0346284	0350293
109	0374265	0378247	0382226	0386202	0390173
110	0413927	0417873	0421816	0125755	0429591
111	0453230	0457140	0461048	0464952	0468852
, 112	0491180	04950161	0499328	0503797	0507663
113	0530784	0534620	0538464	0542899	0540790
114	0569048	0572856	0976661	0580462	0584260
115	0606978	0610753	0514525	0618293	0622058
116	0644580	C648322	0652001	0655797	0659530
117	0081899	068 rc 69	0689276	052983 0729847	Q696681
	0718820	9722499	0720179		0733517 0770043
119	0759470 0791812	0759118		0802656	0806261
120	0791812	0795430 0831441	0799045 c835026	0838698	0842187
121	0863598	08671441	0870712	0874264	0877814
122	0809011	0002580	00000107	0909631	0913151
125	0934217	0937718	0941210	0944711	0948204
125	0934217	0972473	0976043	0979511	0989975
126	1033705		1010193	1014033	1017471
127	1038037	1041455	1044871	1048284	1051094
128	1072100	1075491	1075880	1082250	1085650
129	1105897	1109262	1112625	1115985	1119343
130	1139433	1142773	1146110	1149444	1152776
131	1172713	1176027	1179338	1182647	1185954
132	1205739	120002		1215598	1218880
133	1238516	1241780	1245042	1248301	1251558
				1280760	
134	1271048	1274288	1277525	1280760	1283993

362

Logarithms (to 1349:-)

:363

	•	120%	aivi inns.	10 1.30	もいう	303
	bers.	-5	6	¹ 7	18	9 9
	1	1760912	2041200	2304489	2352725	27875361
	2	3979400	4149733	4313637.	4471.580	4023980
		5440680	5563015	5682017	3797836	5910046
	3	6532125	6627578	6720978	6812412	
1	5.	7403627	7481580	7.58748	7634280	
	6	8120812	8195439	8260744	8325089	8388491
	7	8129133 8750613	8808136	8854907	8920946	
· · ·	8.	9204189	9344984	9395191	9444827	9493900
	9	9777236	9822712	9807717	9912261	9996352
	100	9777230	0025980	0030295	0014905	0038912
:		0021601	0068937		0034303	0081743
1	101	0064660		0073209		0124154
	105	0107239	0111473	0115704	0119931	0166155
11	103	6149403	0133597	0117787	0101973	
	104.	.0191103	0195317	0199467	0203513	0207755
	105	0232524	0236639	0240750	0244897	0248960
	100	0273496	0277572	0281644	0285712	0289777
1	107	0314085	0318123	0322197	0320198	0330214
ľ	108.	0354297	0358298	0362295	0365289	
1	109	0394141	0398105	0402056	0406023	04a 9 977
1	'11 0'	0433073	0437551	0441476	0445398	0449315
1.	111	0472749	0476642	0480532	0484418	0488301
ľ.	112	0511525	0515384	0519239	0523091	0520939
	113.	0549958	0553783	0557605	0561433	0564237
	114	0588055	0591846	.0595634	0999419	
	115	0625820	0619578	0633334	0037085	064d834
	116	0663259	0666985	0070768	0674428	0678145
	117	0700379	0704073	0707765	0711453	0715138
	118	0737183	0740847	0744507	0748164	0751818
	119	0773679	0777312	0780941	0784568	0788192
1	120	0809870	0813473	0817073	0820669	0824263
	121	0845753	0849336	0852906	0856473	0850037
	122	0881301	0884905	0888446	0891984	0891519
	I23	0916669	0920185	0913696	0927206	0930714
1	124	0951693	0955180	0958664	0962146	0969625
1	125	0985437	0989896	0993353	0996806	1000257
	126	1020905	1024337	1027766	1031192	1034619
	127	1055101	1058506	1061909	1065308	1068704
	128	1089031	1092410	1095785	1099159	1102529
1	129	1122698	1126050	1129400	1132746.	1130091
1	1;0	1156105	1159432	1162750		1169394
1	131	1189257	1192559	1195858	1199 54	120:44
1 .	132	1222159	1225435	1228709	1231981	1235250
	133	1254813	1258004	1261314	1264561	12678.
· I	1;4	1287223	1290450	1293676	1 1 296 890	1300110

A a a 3

Artificial Numbers : Or,

I 30I 335389I 338581I 341771I 344958I 37I 307200I 370374I 373541I 376705I 38I 398791I 401937I 405080I 408222I 39I 430148I 433271I 435392I 439511I 40I 401280I 404381I 407480I 470577I 41I 492191I 495270I 498347I 501422I 42I 522883I 525941I 528996I 532049I 43I 553360I 556306I 59430I 562462I 44I 583612I 586640I 58063I 652650I 45I 613680I 61674I 619606I 622656I 45I 613680I 616572I 649474I 652443I 45I 673173I 676127I 679078I 682027I 48I 702617I 705550I 708482I 711411I 49I 731803I 734776I 737688I 709580I 50I 760913I 763807I 766699I 798389I 51I 789769I 792645I 795518I 798389I 52I 818456I 849752I 82583I 855421I 54I 875207I 878026I 830844I 883659I 55I 993317I 906118I 908917I 911714I 56I 931446I 934049I 536810I 939590I 57I 958966I 961762I 964525I 967287I 58I 986571I 993319I 992065I 994809I 5920139712067022019431 </th <th colspan="7">Artificial Numbers : Or,</th>	Artificial Numbers : Or,						
135 130338 130553 130767 1312978 136 133589 1338581 1341771 13449582 137 1367206 1370374 1373541 1376705 138 1398791 1401937 1405080 1408222 139 1430148 1433271 1453921 1439511 140 1401380 1404381 1407480 1470577 141 1492191 1495270 1498347 1501422 142 152883 1525941 158996 1532049 143 155360 156536 155462 168640 144 1583625 1566463 159463 159463 143 155360 156650 159463 1592663 144 1583625 156650 159463 1592663 145 1613680 151674 1652443 16820561 146 164352 1646502 1649474 1652443 147 1673173 1076127 1679078 1082027 148 1702617 1705550 1708482 1711411 155 149 1731803 1734776 1737688 1740598 17983894 150 1760913 1763807 1766699 17983894 1556990 153 1846941 1849752 1852483 185621 1557 157 193297 1906118 1909917 191711 175681727 157 19869671 1934049 1536810 </th <th>4</th>	4						
13713 $\overline{0}7200$ 13 $\overline{0}7374$ 13 $\overline{1}373141$ 13 $\overline{0}705$ 1313813987911401937140508014082221413914 $\overline{3}0148$ 1433271143 $\overline{0}392$ 14395111414014 $\overline{0}1480$ 14 $\overline{0}3271$ 14 $\overline{0}5920$ 14 $\overline{3}9511$ 1414014 $\overline{0}1280$ 14 $\overline{0}4381$ 14 $\overline{0}7480$ 14 $\overline{7}0577$ 141411492191149527014 $\overline{9}8347$ 1501422151421528831525941152896015 $\overline{3}2462$ 1514315533601556306155943015624621614315536015166741519606162265616145161368016166741519606162265616146164352816465021649474165244316145163363153672717084821711411151481702617170555017084821711411141491731803173477617376881740598151501760913176380717666901769590151511789769179264517955181798389141521818456182129218241461826999151531846941184975218528831855421151551903171906181934059153681019395901515719389671193404015368101939590151571985	316187						
137136720613703741373541137670515138139879114019371405080140822214139143014814332711456392143951114140140138014043811407480147057714141149219114952701498347150142215142152883152594115889615320491514315536015630615594301562463161431583625158640168965315926631614415836251586401689651159263316145161368015166741619606168265611614616435281646502164947416524431614817026171705550170848217114111514917318031734776173768817405981150176091317638071766699176959015151178976917926451795518179838911152181845618129218241461826990151531846941184975218528831855421151551903171906118190917191714161571938961934049153681019395901515819869711933191992065199480915159201307120167022019431202215816	348144						
139143014814332711436392143911114014612801464381146748014705771411492191149527014983471501422142152288315259411528996153204914315533601556390155943015624621441583615158664018896531592663145161368016166741619606162265614616435281646502164947416524431471673173167612716790781632027148170261717055501708482171141114917318031734776173768817405981501760913176380717666901769490151178976917926451795518179838915218184361821292182414618269991531846941184975218528318561211541932171906118199391719117141561931461934040153681019395015719859619617621964525190728715819869711933191992065199480915920139712017622013941	379867						
140146128014643811467480147057714141149219114952701498347150142219142152288315259411589961532049191431553360155639615594301562462191441583615158664015899531592663191451613680161667416196061622656161461643528164650216494741652443161471673173167612716790781632027161481702617170550170848217114111414917318631734776173768817405981150176091317638071766699176959017151178976917926451795518179838911152181843618212921824146182699911153184694118497521852831855421141541875207187618199391719117141915519323171906118193691719117141915719389619517621964525190728719959019157198596195176219645251907287191581986971193319199206519948091915920139712017622019431202215820	411361						
141 1492191 1495270 1498347 1501422 151422 142 1522883 1525941 1588996 8532049 1532049 143 1553360 1556196 1559430 1562462 159430 144 1583055 1586640 1589653 1592663 145 1613680 1016674 1619606 1622656 146 1643528 1046502 1649474 1652443 147 167373 1676127 1679078 1652027 148 1702617 170550 1708482 1711411 149 1731863 1734776 1737688 1740598 150 1760913 1763807 1766590 1769590 151 1789769 1792645 1795518 1798389 152 1818456 1821292 1824146 1826999 153 1846941 1849752 185283 1855421 154 1875207 1878026 1830844 1883659 157 193146 1934049 1536810 199590 191714 156 193146 1934039 1596515 1997287 1997287 157 1985996 1961762 1964515 1907287 1907287 159 2013971 2016702 2019431 2022158 1922158	42628						
14215228831525941152899615320491143155336015563961559430156246219144158362515866401589653159266319145161368016166741619606162265616146164352816465021649474165244316147167317316761271679078163202716148170261717055501708482171141117149173180317347761737688174059811501760913176380717665901769590171511780769179164517951817983891152181843618212921824146182699915153184694118497521855884418855911515418752071878026185084418836591515519931719061181908917191171415156193146193404915368101939590151581985961961762196452519672871515819869711933191992065199480915159201397120167012019431202215816	73671						
143 1553360 1556396 1559430 1562462 159463 144 1583615 1586640 1589653 1592663 169665 145 1613680 1616674 1619606 1622656 146 1643528 1646502 1649474 1652443 147 1673173 1676127 1679078 1632027 148 1702617 1705550 1708482 1711411 149 1731803 1734776 1737688 1740598 150 1760913 1763807 1766590 1769590 151 1789769 179518 1798389 152 1818436 1821292 1824146 153 1846941 1849752 1855421 153 1903317 1906118 1908917 156 1931446 1934049 1536810 157 193896 1934049 1536810 158 1986571 1993219 1992065 158 1986571 1993219 1992065 159 2013971 2016702 2019431	504494						
I_{44} $I_58_361_5$ I_58664_0 I_5866_3 $I_59^266_3$ $I_59^266_3$ $I45$ $I61_368_0$ I^61667_4 $I619666$ $I6226_56$ $I6226_56$ $I46$ $I6_43_528$ $I646_502$ $I64947_4$ $I6524_43$ $I6524_43$ $I47$ $I67317_3$ $I676127$ $I679078$ $I632027$ $I48$ $I702617$ $I705550$ $I708482$ $I711411$ $I49$ $I73186_3$ $I734776$ $I737688$ $I740598$ $I50$ $I760913$ $I763807$ $I766590$ $I769590$ $I51$ $I789769$ $I792645$ $I795518$ $I79838914$ $I52$ $I8184_36$ $I821292$ $I824146$ $I82699914$ $I53$ $I86941$ $I849752$ $I82583$ 18554214 $I55$ $I903317$ $I906118$ $I908917$ $I911714$ $I56$ $I93146$ $I934049$ $I536810$ $I939590$ $I57$ $I95896$ $I961762$ $I964515$ $I907287$ $I58$ $I986571$ $I939319$ $I992065$ $I94809$ $I59$ 2013971 2016702 2019431	535100						
145 1613680 1516674 1619606 16226_36 161674 146 $1643_{3}28$ $1646_{5}02$ 1649474 $16524_{3}2$ $16674_{3}26_{3}$ 147 1673173 1676127 1679078 1632027 148 1702617 1705550 1708482 1711411 149 1731863 1734776 1737688 1740598 150 1760913 1763807 1766999 1795988 150 1760913 1763807 1766999 179938914 151 1789769 1792645 1795718 179838914 152 1818456 181292 181446 182699914 153 1846941 1849752 1855421 1655421 153 1903177 1906118 190917 191714 156 193146 1934049 1536810 1939590 1577 157 19859671 199319 1992065 1994809 159 158 198671 1939319 1992065 1994809 159 159 2013971 2016701 2019431 2022158 2012587	503491						
146 1643528 1646502 1649474 1652433 1652433 147 1673173 1676127 1679078 1632027 1632027 148 1702617 1705550 1708482 1711411 17140598 149 1731803 1734776 1737688 1740598 150 1760913 1763807 1766999 1769590 151 1789769 1792645 1795518 179838914 152 1818436 1821292 1844146 182699914 153 1846941 1849752 1855421 1655914 154 1875207 1878026 1830844 1883659 1557 157 1933177 1906118 1908917 191714 1935996 157 1935996 1934049 1536810 1939596 1972874 158 198671 1939319 1992065 1994809 193207257 159 2013971 2016702 2019431 202215872	\$9\$672						
147 1673173 1676127 1679078 1632027 1632027 148 1702617 1705550 1708482 1711411 171411 149 1731863 1734776 1737688 1740598 150 1760913 1763807 176699 1769590 151 1789769 1792645 1795518 1798389 152 1818456 181292 1814146 182699916 153 1846941 1849752 1852583 1855421 154 1875207 1878026 1830844 1883659 155 1903177 1906118 1909917 191714 156 193146 1934049 1536810 1939590 157 19859671 1939319 1992065 194809 158 1986771 1939319 1992065 194809 159 2013971 2016702 2019431	525644						
14817026171705550170848217114111714917318031734776173768817405981715017609131763807176669917695901715117897691792645179551817983891152181843618212921824146182699911531846941184975218528318554211154187520718702618308441883659115519031771906118190891719117141156193146193404915368101939590115719589651901762196452519072871158198677119331919920651994809115920130712016701201943120221582	555413						
149 173186_3 $L73476$ 1737688 1740598 1 150 1760913 1763807 1766699 1769590 1769590 151 1789769 1792645 1795518 1798389 152 1818436 1811292 1814466 1826999 153 1846941 1849752 1852583 1855421 154 1875207 1878026 1890844 1883659 155 1903317 1906118 1909917 1911714 156 1931246 1934019 1536810 1939590 157 1986971 1989319 1992065 1994809 158 1986571 1989319 1992065 1994809 159 2013971 2016701 2019431 202215872	684975						
150 176913 176307 176699 179950 151 1789769 1792645 179518 1798389 152 1818436 1811292 1814466 1826999 153 1846941 1849752 1852583 1855421 154 1875207 1878026 1890844 1883659 155 1903317 1906118 1909917 1911714 156 1931246 1934019 1536810 1939590 157 1958996 1907762 1964525 1907287 158 1986571 199319 1992065 1994809 159 2013971 2016702 2019431	714339						
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	743400						
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	772478						
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155 1903317 1906118 1903017 1911714 19 156 1931146 1934019 1536810 1939590 19 157 1958996 1961762 1964515 1967287 19 158 1986571 1989319 1992065 1994809 19 159 2013971 2016702 2019431 2022158 20	858153						
I56 1931446 1934049 I536810 1939590 1 I57 1958996 1961762 1964525 1967287 1 I58 1986571 1989319 1992065 1994809 1 I59 2013971 2016702 2019431 2022155 2	886473						
157 1958996 1961762 1964525 1967287 1 158 1986571 1989319 1992065 1994809 1 159 2013971 2016701 2019431 2022155 2	914510						
158 1986571 1989319 1992065 1994809 1 159 2013971 2016701 2019431 2022158 2	942307						
IS9 2013971 2016702 2019431 2022158 20	970047						
	097552 024883						
	052044						
	079035						
	105860						
	132521						
	159018						
165 2174839 2177471 2180100 2182727 2	185355						
	211533						
	237554						
	203421						
169 227886; 2281436 2284003 2286570 2	289134						
	314696						
	340108						
	365373						
173 2380461 2382971 2385479 2387986 2	390491						
174 2405492 8+07988 2410481 2412974 2	415465						
175 1430380 2432861 2435341 2437819 24	440296						
176 2455127 2457593 2460059 2462523 2	464986						
177 2479733 2482186 2484637 2487085 24	489536						
126 2504200 2506639 2509077 2511513 2	513948						

	Logarithms (to 1789.)					365
,	Natural Number:	5	6	7.	8	y · 9
	135	1319393	1322597	1325798	1328998.	1332194
	136	1351320	1354507	1357685	1360861	1364034
	137	1383027	1386184	1389339	1392492	1395643
	138	1414498	1417632	1420765	1423895	1427022
	139	1445742	1448854	1451964	1455072	1458177
	\$40	1476763	1479853	1482941	1486026	1489110
	141	1507564	1510632	1513698	1516762	1519824
	142	1538149	1541195	1544240	1547282	1550322
	143	1 5685 19	1571544	1 574568	1577589	1580608
	£44	1598678	1601683	1604685	1607686	1610684
	145	1628630	1031614	1634595	1637575	1640553
	346	1658376	1661340	1664301	1667200	1670218
	147	1687920	1690863	1693805	1696744	1699682
:	JĄS	1717264	1720188	1723110	1726029	1728947
	149	1746412	1749316	1752218	1755118	1758016
	150	1875365	1778250	1781132	1784013	1786892
	151	1804126	1806992	1809856	1812718	1815578
	152	1832698	1835545	1838.90	1841233	1844075
	- 153	1861084	1853912	1866739	1869563	1872386
	154.)	1889285	1892095	1894903	1897709	1907514
	155	1917304	1920096	1922886	1925674 1953460	19284 ⁶ 1 1956229
	156	1945143	1947917	1950690	1981070	1983821
	157	1972806	1975562 2003032	1978317 2005769	2008505	2011239
	1 58 159	2000293 2027607	2030329		2035768	2038485
	160	2054750	2057455	2033049 2050159	2062869	2065560
	101	2034/30	2084413	2087100	2089785	2092468
1	162	2108534	21 01205	2113876	21 10544	2119211
	163	2135178	2137833	2140487	2143130	2145789
	164	2161659	2164298	2166935	2109572	2172206
	165	2187980	2190603	2193225	2195845	2198464
1	166	2214142	2216750	2219356	2221960	2224563
	167	2240148	2242740	2245331	2247920	2250507
	168	2265999	2208576	2271151	2273724	2276296
	169	2291697	2294258	2296818	2299377	2301934
	170	1317244	2319790	2322335	2324879	2327421
	171	2342641	2345173	2347703	2350232	2352759
	172	2367891	2370408	2372923	2375437	2377950
	173	2 392995	2395497	2397998	2400498	2402996
	174	2417954	2420442	24229-9	2425414	2427898
	175	2442771	2445245	2447718	2450189.	2452658
	176	2467447	2469907	2472365	2 +7 +823	2477278
	177	2491984	2494430	2496874	2 499317	2501759
	178	2516382	2518814	2521245	2523075	2526103

Artificial Numbers : Or,

	300	##F * 1		willours Or,		
1	Natural Numbers.	' °		ž	3	4
	179	2528530	2530956	2533380	2535803	2538224
	180	2552725	2555137	2557548	2559957	2502305
	181	2576786	= 5791 34	2581582	2583278	2580373
	182	2000714	2003099	2605484	2607867	2610248
	183	2624511	2625883		2031025	2010240
	184	2548178	2050538	2629255	1635253	2033993
	185	2071717	2674064	2652896	267874	2057009
	185			2676410		2681077
	187	2695129	2697464	2699797	2702128	2704459
		2718416	2720738	2723058	2725373	2727696
	188	2741578	2743888	2746196	2748503	2750809
	189	2764618	2766915	2769211	2771 500	2773800
	190	2787536	2789821	2792105	2794389	2796669
	191	2810334	2812607	2814879	2817150	2819419
	192	2433012	2835274	2837534	2839793	2842051
	193	2855573	2857823	2800071	2902318	2864565
	¹ 94	2878017	2880255	2982492	2884728	2856963
	195	2900346	2902573	29 04798	2907022	2902:45
	1,6	2922561	2924776	2 92699 0	2929203	2231415
	197	2944662	2 9458 66	2949069	2951271	2053475
	1,8	2956652	2,68845	2971036	2373227	2975417
	193	2988531	2990713	2992893	2,95073	2997151
	200	3010300	3012471	3014641	1010839	3018977
	201	3031961	3034121	3030:80	3038438	3040595
	2c2	3053514	3055663	3057811	30599;9	3062105
	203	3074960	3077099	3079237	3051374	3083.09
	2 04	3020302	30984:0	3100557	3102084	3104800
	205	3117539	3119657	3121774	3123883	3126004
	206	3138672	3140760	3142887	3144992	31 47097
	207	5159703	3161801	3163897	310599;	3168087
	208	31806:3	3182721	3184807	3186893	3188977
	209	3201163	3203540	3205617	3207692	3209767
	210	3222193	3224260	3220327	3228393	3230457
	211	3242825	3244882	3246939	3248995	3251050
	212	3263359	3255407	3267454	3269500	3271545
	213	328:796	3285834	3-87872	3289909	3291944
1	214	33041 18	33e6167	3303 95	3310222	3312248
	215	3324 285	3326:04	3328423	3330440	3332457
	215	3344537	3346548	3348557	3305565	3352572
	217	3364597	3366598	3368;98	3370597	3372595
	218	23 4:65	3326557	3388547	3392537	3392526
	219	3404441	3406424	3408405	3410,86	3412365
	220	3424227	3426100	3428173	3430145	3432116
	221	3443923	3445887	3447851	3449814	
	222	3463530	3465486			3451776
<u> </u>	* * 4	. 34. 33 30	2447440	3407441	3459395	<u>347134</u> 8

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Logarithms (to 2229.)

.180 .181 182 .183	52 2549045 2564772 2588766 2635361 2659964 2683439 2706788	6: 2543063 2567177 2591158 3615008 2638727 2662317 2662317	· 7 2545481 2569581 2593549 2617385 2641092	8 2547897 2571984 359 1939 2619762	9 2550312 2574386 2598327 2622137
179 180 181 181 182 183	2 56 47 72 2 5 8 87 66 2 6 3 16 19 2 6 3 6 3 5 1 2 6 5 99 6 4 2 6 8 3 4 3 9	2507177 2591158 3015008 2038727 20602317	2569581 2593549 2617385 2641092	2571984 359 1939 2619762	2574386 2598327
.180 .181 .182 .183	2 56 47 72 2 5 8 87 66 2 6 3 16 19 2 6 3 6 3 5 1 2 6 5 99 6 4 2 6 8 3 4 3 9	2507177 2591158 3015008 2038727 20602317	2569581 2593549 2617385 2641092	2571984 359 1939 2619762	2574386 2598327
.181 182 -183	2588766 26312629 2636361 2659964 2683439	2591158 3015008 2038727 2062317	2593549 2617385 2641092	359 1939 2619762	2598327
182	263 2639 2636361 2659964 2683439	3615008 2638727 2662317	2617385 2641092	2619762	
183	2636361 269 <i>996</i> 4 2683439	2638727 2662317	2641092	//	40221371
	26499 6 4 2643439	2662317		2643455	2645817
	2683439	6 49 4 94	2664669	2667020	2669369
185	2706788	~003700	2689119	2790457	2692794
		2709116	2711443	2713769	2716093
187	2730013	2732328	2734643	2736956	2739268
.188 .	2753113	2755417	2757719	2760020	2762320
189 1	2770092	2778383	2780673	2782962	2785250
190	2798950	2801229	2803507	2805784	2108059
191	2321688	2823955	2826221	2828486	2830750
	2844307	2846563	2848317	2851070	2853322
193	2806810	2869054	2871296	2873938	2875778
	2889190	2891428	2893659	2855889	2898118
195	29 51 468	2913688	291 5908	2918127	2920344
196	2933628	2935835	2938044	2940251	2942457
197	2959671	2257869	2960067	2962263	2961458
198	2977605	2979792	2981979	3984164	2986348
199	2999420	3001605	3003781	3005955	3008128
203	30+1144	3023300	3025474	3027637	3029799
	3042751	3044905	3047059	3049212	3011363
202	3064290	,3066394	3068537	3070679	3072820
	3085644	3087778	3089910	3091041	3094172
	3106933	3109095	3111173	3113299	3115420
	3128118	3130231	3132343	3134454	3136563
	3149:00	3151303	3153405	3155505	3157605
207	3170181	3172273	3174365	3176455	3178545
208	3191061	3193143	3195284	3197305	3199384
	3111840	3213913	3219984	3818255	3220124
	3932525	3234584	2336615	3238706	3240766
	3293104.	3255157	32 \$ 7 209	3-59260	3261310
	3273589	3275633	3277675	3279716	3281757
	3293979	32,70012	3295045	3300077	3302108
	3314273	3316297	3318322	3320343	3322364
	3331471	3330488	3338401	3340514	3342526
	3334979	3356585	3318589	3360593	3362196
	3374593.	3376589	3378584	3380579	3382572
	3394514	3395901	3398488	3400473	3402458
219	3414345	3415343	3418301	3420277	3422252
	3434086	3436055	3439023	3439991	3441957
221	3453737	3455698	3457657	3459515	3461573
2.2	347 3200	3475252	3477202	3479152	3481101

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Artificial Numbers: Or,

300	2				
Natoral.	0	I	2 .	3	. 4
Numbers 223	3483049	3484996	3486942	3488887	3490832
224	3502480	3504419	3506356	3508253	3510228
225	3521825	3523755	3525684	3527612	3529539
220	3541084	3543000	3544920	3546845	3548764
227	3560259	3562171	3564083	3565994	3567905
228	3579348	3581253	3583150	3585059	3586961
229	5598355	3000251	3602146	3004040	3005034
230	3617278	3619166	3621053	3622939	3624825
231	3636120	3638000	3639878	3641796	3643633
232	3654880	3656751	3658622	3660492	3002301
233	3673559	3075423	3677285	3679147	3681008
234	3692159	3694014	3695869	3697723	3699576
235	3710679	3712520	3714373	3716219	3718005
236	3729120	3730960	3732799	3734637	3736475
237	3747483	3749316	3751147	3752977	3754807
238	3765769	3767594	3769418	3771240	3773062
239	37 83979	3785796	3787612	3789427	3791241
240	3802112	3803922	3805730	3807538	3809345
241	3820170	3821972	3823773	3825573	3827373
242	3838154	3839948	3841741	3843534	3845320
243	3856063	3857850	3859636	3861421	2862200
244	3873898	3875678	3877457	3879235	3881012
245	3891661	3893433	2895205	3896975	3898746
246	3909351	3911116	3912880	3914644	3916407
247	3926969	3928727	3930485	3932241	3933997
248	3944517	3946268	3948018	3949767	3951510
249	396 1993	3963734	3965480	3967823	3968964
250	3979400	3981137	3982873	3984608	3986343
251	3996737	3998467	4000196	4001923	4003653
252	4014005	4015728	4017451	4019172	4020893
253	4031205	4032921	4034637	4036352	4938066
254	4048337	4050047	4051755	4053464	4055171
255	4065402	4007105	4068807	4070508	4072209
256	4082400	4084096	4085791	4087486	4989180
	4099331	4101021	4102710	4104398	4106085
257 258	4116197	41 17880	4119562	4121244	4122925
259	4132998	4124674	4136350	4138085	4139700
260	4149733	4151404	4153073	4154742	4156410
261	4106405	4168069	4169732	4171394	4172066
262	4183013	4184670	4180327	4187983	4189638
263	4199557	4201208	4202859	4204509	4206158
264	4216039	4217684	4219328	4220972	4222614
265	4232459	4234097	4225735	4237372	4239009
266	4248816	4250449	4252080	4253712	4255342
~~~~	7.00000	1-1-11	J.		

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368

Logu		arithms	(to 26	<b>69.)</b>	369	
	Natural Numbers.	5	8	7 :	8	2
	223	3492775	3494718	3496660	3408501	3500541
	224	3512163	3514098	3516031	3517963	3519895
	225	3531465	3533391	3535310	3537239	3539162
	226	3550682	3552599	3554515	3556430	3558345
	227	3569813	3571723	3573030	3575537	3577448
	228	3588862	3590762	3592662	3594560	3596458
	229	3607827	3609719	3611610	3513500	3615390
	<b>2</b> 30	3626709	3628593	3630476	3632358	3634239
	231	3645510	3047380	3649260	3651134	3653007
	232	3664230	3666097	3667964	3669830	3671695
	233	3682869	3084728	3686587	3688445	3690301
	234	3701428	3703280	3705131	3706981	3708330
	235	3719909	3721753	3723996	3725438	3727279
	236	3738311	3740147	3741983	3743817	3745651
	237	3756636	3758464	3760292	3762118	3763944
	238	37 <b>7</b> 4884	3776704	3778524	3780343	3782161
1	239	3793055	3794868	3796680	3798492	3800302
	<b>*\$</b> 40	3811151	38 <b>12956</b>	3814761	3816565	3818368
	241	3829171	3830969	3832766	3834563	3836359
	242	3847117	3848908	3850698	3852487	3854275
	243	3864990	3866773	3868555	3870337	3872118
1	244	3892789	3884565	3886340	3888114	3889888
	245	3900515	3902284	3904092	3905819	3907585
1	245	3918169	391993:1	3921691	3923452	3925211
	247	3935752	3937505		3941013	3942765
1	248	3953264	3955011	3956758	3958504	3960249
	249	3970705	397244 <b>6</b>	3974185	39759 ² 4	3977662
]	250	3988077	398981.1	3991543	3993275	3995007
1	251	4005380	4007106	4008832	4010557	4012282
1	252	4022614	4024333	4020052	4027771	4029488
	253	4039780	4041492	4043205	4044916	4046627
	254	4056878	4058584	4000289	4001994	4063698
1	215	4073909	4075608	4077307	4379005	4080703
	250	4090874	4092567	4094259	4099950	4097641
Ĵ	257	4107772	4109459	4111144	4112829	4114513
	258	4124605	4126285	4127964	4129643	4131 320
	25.9	4141374	4143047	4144719	4146391	4148063
	260	4158077	4196744	4161410	4163976	4164741
3	<b>2</b> 61	4174717	4176377	4178937	4179696	4181355
Ĵ	261	4191193	4192947	4194001	4196254	4197906
Ś	263	4207806	4209454	411101	4212748	4214394
	264	4124257	4225898	4227539	4229180	4230820
•	205	4240545	4242281	4243915	4245550	
. /	.265	4250972.	4258601	4260130	4261858	4263486

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## Artificial Numbers: Or,

Natoral. Numbers	•	I	2	3	4
267	4265113	4266739	4268365	4269990	4271614
268	4281348	4282968	4284588	4285207	4287825
269	4297523	4299137	4300751	4302364	4303976
270	4313058	4315246	4316853	4318460	4320067
271	4329693	4331295	4312897	4334498	4336098
272	4345689	4347285	4348881	4350476	4352071
273	43.61626	4363217	4364807	4366396	4367985
274	4377506	4379090	4380674	4382258	4383841
275	4393327	4394906	4396484	4398062	4399639
276	4409091	4410664	4412237	4413809	4415380
277	4424798	4426365	4427932	4429499	4431065
278	4442448	4442010	4443571	4445 132	4446692
279	4456042	4457598	4459154	4460709	4462264
380	4471580	4473131	4474681	4476231	4477780
281	4487063	4488608	4490153	4491697	4493241
282	4502491	450403I	4505570	4507109	4508647
283	4517864	4119399	4520933	4522465	4523998
284	4533183	4534712	4536241	4537769	4539296
285	4548449	4549972	4551495	4553018	4554540
286	4963660	4565179	4566696	4568213	4569731
237	4578819	4580332	4581844	4583350	4584868
258	4593925	<b>459543</b> 3	4596940	4598446	4599953
289	4008978	4610481	4611983	4613484	4614985
290	4623980	4625477	4626974	4628470	4629966
291	4638930	4640422	4641914	4643405	4644895
292	4653828	4655316	4656802	4658288	4659774
293	4668676	4670158	4671640	4673120	4674601
294	4683473	4684950	4686427	4087903	4689378
295 296	4698220	4699692	4701163	4702034	4704105
297	4712917	4714384	4715850	4717317	471 8782
298	4727564	47 <b>2</b> 9027 4743620	4730488	4731949 474 ⁶ 533	4733410
	4742163	4743020	4745076 4759 <b>6</b> 16	4761067	4747988
299 300	475 ⁶⁷¹² 4771212	4758164 47 <b>7</b> 2660		4775553	47.62518
301	4785065	4792000	4774107	4789991	4776999
302	4800069	4787108		4804381	4791432
303 :	4814426	4801507 4815859	4802945. 4817292	4818724	4805818 4820156
304	4818736	4830104	4831592	4833019	4040150
305	4842998	4844422	4845845	4847268	4834446 4848650
306	4857214	4858633	4860052	4861470	4862888
307	4871384	4850033	4874212	4875626	4877020
308	4885507	4886917	4888326	4889735	4877039
309	4899585	4900990	4902395	4903799	4891144 4905203
310	4913617	491 5018	4916418	4917818	4919217
			+7	-17-/510	

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Logarithms (to 3109.)

	Log	WI + DIJII24	. <b>(</b> , , , , , , , , , , , , , , , , , , ,		J/~	
Natoral	5	6	7	8	9	
Numbers. 267	4273238	4274861	4276484	4278106	4279727	
269	4289443	4291060	4292677	4294293	4295908	ľ
269	4305588	4307:99	4308809	4310419	4312029	
	4321673		4324883	4326487		
270	4337698	4323278	4340896	4342494	4344092	
271		4339198	4356851	4358444	4300035	
272	4353065 4369573	4355258	4372748	4374334	4375920	
273	4385423	4371161	43885.87	4390167		
274	4401210	4387005 4402792	4404368	4405943	4407517	
: 275	4416951	4418522	4420092	4421661		ł
270	4432630	4410522	4435759	4437322	4438885	
277	4448252	4+34 97	4451370	4452928	4454485	
278	4463818	4149811	4466925	4468477	4470029	
279 280		4465372	4452424	4483971	4485517	
281	4479329	4490877 4496326	4497868	4499410	4500951	
282	4494784		4513258	4514794	4516329	
	4510184	4511721			4531654	
283	4525531	4527062	4528593	4530124		
284	4540823 455 ⁶⁰⁶¹	4542349	4543875 4559102	4545400 4500522	45.62142	
285 286		4557582		4575791	4577305	
	4571246	4572762	4574277	4590908	4592417	
287	4586378	4587889	<b>4</b> 589399 46044 <b>68</b>	4605972	4607475	
288	4601458 4616486	4602963	4619485	4620381	4622482	
289	4010400	4617986	4029403	4625044	4637437	
290	4631461 46463 <b>8</b> 6	4632956	463 <b>4450</b> 4645364	4635944 4650853	4652341	
291	4040300	4647875	4045304	4665711	4667194	
292	4661259 46760 <b>8</b> 1	4662743	4664227	4680518	468 1996	
293		4677560	4679039 4693801	4695275	4696748	ľ
294	4690853	4692327	4093001	4709982	4711450	
295	4705575	4707044		4724639	4726102	
296	4720247	4721711	4723175 4737788			
297.	4734870	4736329		4739247 4753806		
298	4749443	4750898	4752352 4766867	4768316	4769765	
299	4763968	4765118	4781334	4782778	4784222	
300	4778445	4779890		4797191	4798631	
301	4792873	4794313	4795754	4811559	4812993	
302	4807254	4808689	4810124	4825878	4827307	
303	4821587	4823018	4824448	4840150	4841574	
304	4835873 4850112	4837299	483 <b>8725</b> 4852954	4854375	4855795	ł
305	4864200	4851533	4867138	4868554	4869969	۷
306	4864305	4865721	4881275	4882686	4884097	
307	4878451	4879863		4896773	4898179	
308	4892552	4893959	4895366	4919814	4912216	ľ
309.	4906607	4908009	4909412 4923413	4924810		
310	4920010	4922014	4943423	47.4010		

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Artificial Numbers : Or,

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21-				,	
Natorial Mumbers.	0		1 ¹	3	4
311	4927604	4929000	3930390	4931791	4933180
312	4941546	4942938	4944329	4945720	49471:0
313	4955443	49568;1	4958218	4959604	4900990
314	4969296	4970679	4972062	4973444	4974825
315	4983106	4984484	4985862	4987240	4988617
310	4996871	4998245	4999619	5000992	5002305
317	5010593	5011962	5013332	5014701	5016069
318	5024271	\$025637	5027002	5028366	5029731
319	5037907	9039268	5040529	5041989	5043349
	5051500	\$032857		5053560	000000
320		5066403	5054213		9096929
321	5005050		5067795	5069107	507c459
322	5078559	5°799°7	5081259	5082603	5083950
323	5092025	\$C93370	5094712	5090057	5097400
324	\$105450	\$106790	5108130	5109469	5110808
325	5118834	5120170	5121909	5122841	5124175
326	5132176	\$133508	5134840	5136171	5837508
327	5145478	5140805	5148133	5149460	5150787
. 328	5158738	5160062	5151386	5162709	5164031
329	5171959	5173279	5174598	\$175917	5177236
330	5185139	5186455	5187771	5189085	5190400
331	5198280	5199592	5200903	5202214	5203525
332	521(381	5212689	5213996	\$215303	5216610
333	5224442	\$225740	5227050	5228353	5229656
334	5237465	5238765	5240004	5241 364	5242663
335	5250448	\$251744	5253040	5254335	5255631
330	5263393	5264685	5265977	5267269	5268560
337	5276299	1277588	5278876	5280163	5281451
337 338	5289167	\$290452	5291736	5293020	5294303
319	\$301997	1303278	5304558	5305839	5307118
340	5314789	\$316066	5317343	5318619	5319895
34t	5327544	\$328817	5330090	\$331363	5332635
342	5340261	\$341531	5342800	5344069	5345338
343	5352941	\$354207	5355473	5356738	5358003
344	5365584	5366847	5368100	9369370	5370631
345	5178191	5379450	5380708	5381966	5383223
346	5300761	5392010	\$393271	5394525	5395779
347	5403295	5404546	\$405797	\$407048	5408298
348	5415792	\$417040	5418288	\$419535	5420781
349	5428254	5429498	5430742	5431986	543 3229
350	5440680	5441921	5443161	\$444401	5449641
351	5453071	5454308	5455545	\$456781	5458017
352	\$405427	5466660	\$467894	5469126	5470359
353	5477747	5478977	5480207	5481436	5482665
1- 144	5490022	5491.259	5492486		5404937
- Aller			1+2-4-4	water a free the	

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Logarithms (to 3549.)

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Numbers.	5.	6 -	7	8	1 <b>9</b> 1
311	4934580	4935974	4997368	4938761	4940194
382	4949500	4949890	4991279	4952667	4954056
313	4962779	4963761	4905145	4966529	4967913
314	4976306	4977987	4978947	4980347	4981727
315	4989994	4,91370	4992740	4994121	4995496
310	9923737	1001100	5006483	5007852	5009222
317	5017437	5018805	5929174	5021539	5022905
318	5031094	\$032458	5033833	5035183	5036545
-319	5044705	1046068	5047426	5048785	5050142
310	5058280	1099635	5060990	5962344	5063697
321	5071810	5073260	5074512	5075860	5077210
322	9089997	1086644	5987999	5089335	5090680
323	1098743	\$100085	5101427	5102768	5104109
324	9119147	5113485	5134823	5119190	5117497
325	9125510	5126844	5128178	512 <u>95</u> 31	5130844
326	j138832	5 140 162	5141491	5142820	5144149
327	9292123	5153439	5154764	5156089	5157414
328	5165354	5100076	5 167997	5169318	5170039
325	9178554	5179872	5181189	5182506	5183823
330	\$191715	5 193028	5194342	5195855	5196 <b>96</b> 8
331	9204835	5206145	5207455	5298764	\$210073
332	\$217916	5219232	5220528	5221833	5223138
333	9230958	5232260	5233562	5234863	5326164
334	5243961	5249299	5246357	5247854	5249151
335	\$256925	5258219	5259513	5260807	5262100
330	\$269851	5271141	5272431	\$ 273721	5275010
337	5182738	5284024	5285311	5286596	5287882
338	5291587	5296869	5298152	5299434	5300716
339	5308398	5309677	5310955	5312234	5313512
340	5321171	5322446	5323921	5324996	5326270
341	5333907	5335179	5336450	5337721	5338991
342	5346606	5347874	5349141	5350408	\$3\$1075
343	5359267	5360532	5361795	\$303059	5364322
344	5371892	5373153	5374413	5375672 5388250	\$376932
341	5384481	5385737	5386994		5389506
240	5397032	5398186	5399538	5400791	5402043
347	5409548	5410798	5412047	5413296	5414144
348	5422028	541 3274	5424519	5425765	5427010
349	5434472	5435714	5436956	5438198 5450596	5439439 5451834
350	5446880	5448119	5449358	3450790	
351	5459*53	5460489	5461724	5462958	5464193 5476517
352	5471591	5472823 5485123	54.74055 5486351	5475286 5487578	5498806
393	5483894	5705143	5498612	5499836	5501060
354	5400162	\$497387	7470016	1499010	3301000

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Artificial Numbers : Or,

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<b>7/4</b>				,	
Natoral Numbers,	0	Ι.	2	3	4
355	5502283	5503507	\$ 504730	5505952	5507174
356	5514500	5515720	5516939	5518158	5519377
357	5526682	5527898	\$529114	5530330	5531545
358	5538830	<b>554</b> 0043	5541250	5542468	
359	5550944	5552154	5553362	5554572	5555781
360	5563025	5564231	\$565437	\$566643	5567848
361	5575072	5570275	5577477	5578680	5579881
362	5587086	5588285	5589484	5590683	5591882
363	5599066	5600262	\$601458	5602654	5603849
364	5611014	5612207	5613399	5614592	5615784
365	5622929	5624118	5625308	5626497	5627685
366	5634811	5635997	5637183	5538369	5639555
367	5646661	5647844	5649027	5650209	5651392
368	\$658478	5659658	<b>5660</b> 838	5662017	\$663196
369	5670264	5671440	5672617	5673793	5674969
370	5682017	5683191	5684364	5685537	5686710
371	5693739	5694910	5696080	5697249	5698419
372	5705429	5706597	\$707764	5708930	5710097
373	5717088	5718252	\$719416	5720580	5721743
374	5728716	5729877	5731038	5732198	5733358
375	\$740313	5741471	5742628	5743786	\$744943
376	5751878	5753033	5754188	5755342	5756496
377	5763413	5764565	5765717	5766868	\$768019
378	5774917	5776057	5777215	5778363	5779511
279	5786392	5787538	5788683	5789828	5790973
380	5797836	5798979	5800121	5801263	5802405
281	5809250	5810389	5811529	5812668	5813807
382	\$820634	5821770	5822907	5824043	5825179
383	5831988	5833122	5834255	5835388	5836521
384	5843312	5844443	5845574	5846704	5847834
385	5854617	5855735	5856863	5857990	5859117
386	5865873	5866998	5868123	5869247	\$870371
387	5877110	5878232	5879353	5880475	5881596
388	5888317	\$889436	5890555	5891674	5892792
389	5899496	5900612	5901728	5902844	5903959
390	5910646	5911759	5912873	\$913985	5915098
391	5921768	5922878	5923988	\$925098	5926208
392	5932861	99339 <b>6</b> 8	5935076	5936183	\$937290
393	5943925	5945030	5946135	5947239	5948344
394	5954962	5956064	5957166	5958268	5959369
395	5965971	\$967070	5968169	5969268	5970357
396	5976952	5978048	5979145	5980241	5981336
397	5987905	5988999	5990092	5991186	5997279
398	15998831	5999922	6001013	6002103	6003193

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		Log	g <i>arithms</i>	( to 39	980.)	375	•
1	Natural Numbers,	5	6	7	8	9	
ľ	355.	5508396	5509618	5510839	5512059	5513280	
ł	350	5520595	5521813	5523031	\$524248	5525465	
1	357	5532760	5533975	5535189	5536403	5537617	
	358	5544892	5546103	\$547314	5548524	5549735	
	359	5556989	5558197	5559404	5500612	5561818	
	360	5569053	5570257	5571461	\$572665	\$573869	
	361	5581083	5582284	5583485	5584686	5585886	
	362	5593080	5594278	5595476	5596673	5597870	
I	363	5605044	5006239	5607433	5608627	5009820	
	364	5616975	5618167	5619358	5620;48	5621739	
	365	5628875	5630062	5631250	5632437	5633624	
	366	5640740	5641925	5643109	5644293	9045477	
	367	5652573	5653755	5654936	5656117	5657298	
	368	5664375	5665553	566673I	5667909	5669087	
ł	369	5676144	5677320	5678494	5679689	5680843	
	370	5637882	5689054	5690226	5691397	5592568	
	371	5699588	\$700757	5701920	5703094	5704262	
	372	5711263	5712428	5713594	5714759	5715924	۴
	373	6722906	5724069	5725231	5726393	5727555	
	37.4	5734518	5735678	5736837	5737996	5739154	
	375	5746099	5747256	5748412	5749568	5750723	
	376	5757650	5758803	\$759956	5761109	5762261	
	377	5769169	5770320	5771470	577 26 20	5773709	
	378	5780659	5781806	5782953	5784100	57.85240	ľ
	379	5792118	5793262	5794406	5795550	5796693	
	380	5803547	5804688	5805829	5806969	5808110	
	381	5814945	5816084	5817222	5818359	5819497	
	382	5826314	5827450	5828585	5829719	5830854	
	383	5837654	5838786	5839918	5841050	5842181	
	384	5848963	5850093	5851222	5852351	5853479	
	385	5860244	586137.0	5862496	5863622	5864748	
ł	386	\$871495	5872618	5873742	5874865	5875987	
	387	5882717	5883838	<b>588</b> 4958	5886078	5887198	
4	388	5893910	5895028	5896145	5897262	5898379	
	389	5905075	5906189	5907304	5908418	5909532	
	390	5916210	5917322	5918434	5919546	5920657	
	391	5927318	5928427	5929536	5930644	5931753	i i
	392	5938397	<b>5</b> 939503	5940609	5941715	5942820	
	393	5949447	5950551	5951654	5952757	5953860	
	394	5960470 5971465	5961571 5972563	5962671 5973660	5963771 5974758	5964871	
	395	5982432	5983527	5984622	59/4/5° 5985717	5975855 5986811	
	396		5993527 5994464	5995556	5996648		
	397	5993371	600 <b>5</b> 373	6006462	6007551	5997739 1008640	
	398	6074283		0.000402	000/11	074047	

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### Artificial Numbers : Or,

Namal Nombers	0	1 I -	1 2	3	4
399	0000729	6010817	6011905	6012993	601 4081
400	6020600	6021685	6022771	6023856	602494
401	6031444	6032527	6033609	6034692	603577
402	6042261	004334I	6044421	6045500	604658
403	0053050	6054128	6055205	5055282	6057355
404	6963814	6064888	6065963	6067037	606811
405	6074550	607 5622	6076694	6077766	607883
406	6085260	6086330	6087390	6088468	608953
407	6095944	6097011	6098078	6099144	6100210
408	6106092	6107666	6108730	6109794	611085
409	6117233	6118295	6119356	0120417	612147
410	6127839	6128898	6129957	6131015	613207
411	6138418	6139475	6140531	6141587	614264
412	õi48972	6150026	6151080	6152133	615318;
413	8159501	6160552	6161603	6162654	616370
414 415	6170003	6171052	6172101	6173149	6174197
415	6180481	6181527	6182573	6183619	618456
417	6190933	6191977	6193021	6194064	619510
419 418	9201360	6202402	6203443	6204484	620552
41.9	6211763 6222140	<b>6212802</b>	6213840	6214879	621591
420	6232423	6227177	6224213	6225149	622628
421	6242821	6233527 6243852	6234560 6244884	6235594	6236627
422	6223154	6254153	6255182	6245915 6250211	624694
423	6263404	<b>6264430</b>	6265457	6266483	6257239
424	6273659	6274683	6275707	62767.30	626750
425	628;889	82 84011	6285933	6286954	6277754 628797
426	6294096	6295115	6296134	6297153	6298171
427	6304279	6205206	5306312	6307329	630834
428	4314438	0315452	6316467	6317481	631849
429	6314573	6325585	6326597	6327600	632862
:430	6334685	6335694	63367.04	6337713	633872
431 ÷	6344773	6345780	6346788	6347795	634880
.432	6314837		6356848	6357852	6358851
-433	6364879	6365882	6366884	6367887	636888
-434	6374897	6375898		6377898!	637889
-435 1	6384893	6284801	6386889	6387887	638888
·436 ;	6394865	6395861	6396857	.6397852	639884
·×43 <u>7</u>	6474814		6496802	6407795	640878
-438	-6414741	6415733	6416724	6417715	641870
-499	-6424645	-6429634	0426013	.6427612	642860
440	:6434517	6435514	6436500	6437487	643847
441	6444386	6445371	.6446399	6447339	644832
-412	0214223	6411005	-6416+87	6497169	-6458151

376

	Log	arithms	(to 44	.29.)	377
Natural N. mbers.	5	6	7	8	9
399	6015168	6016255	6017341	6018428	6019514
400	6026525	6027109	6028193	6029277	6030361
401	6036855	6037937	0039718	6040099	6041180
402	6047659	6048738	6049815	6050895	6051973
403	6058435	6059512	6060587	6061663	6062738
404	6069185	6070259	6071332	6072405	6073478
405	6079909	6080979	6082050	6083120	6084190
406	609000 <b>5</b>	6091674	6092742	609;879	6094877
407	6101275	6102342	6103407	6104472	5105537
408	6111921	6112948	6114046	6115109	6116171
409	6122539	6123599	6124660	6125720	6126779
410	6133132	6134189	6135247	6136304	6137361
411	6143698	6144754	6145809	51468 <b>63</b>	6147918
412	6154240	6155292	6156345	6157397	0158449
413	6164755	6165805	6166855	6167905	6158954
414	6175245	6176293	6177340	61.78387	6179434
415	6185710	6186755	6187800	6188845	6189889
416	6196150	6197193	6198235	6199277	6200319
417	6206565	6207605	6208645	6209684	6210721
418	6216955	6217992	6219330	6220067	6221104
419	6227320	6228355	6229300	6230424	6231459
420	6237660	6238693	6239725	6240757	6241789
421	6247976	6249006	6250036	6251066	6252095
422	5258267	6259295	6260322	6261350	6262377
423	6268534	6269559	6270585	6271610	6272634
424	6278777	6279800	6280823	6281845	6282867
425	628×995	6290016	6291036	6292057	6293076
426	6299,190	6300208	6301226	6302244	63 3 262
427	6309361	6310377	6311392	6312408	6313423
428	6313508	6320522	6321535	6322548	6323560
429	6329632	6330643	6331653	6332664	6333674
430	6339732	6340740	6341749	6342757	6343765
431	6349808	0350814	6351820	6352826	6353832
432	6359861	6360865	6361869	6362872	6363876
433	6369891	6370893	6371894	6372895	6373896
434	6379898	6380897	6381896	6382895	6383894
435	6389882	6390879	6391876	6392872	6393869
436	6399842	6400837	6401832	6402826	6403820
437	6409781	6410773	6411765	6412758	6413749
438	6419696	6420686	6421676	6422666	6423656
439	6429589	6430577	6431565	64;2552	6433540
, 440	6439459	6410445	6411430	6442416	6443401
441	6449307	6450291	6451274	6452257	6453240
442	6459133	6460114	6461095	6462076	6453057

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Artificial Numbers : Or,

3/0	AINIJOUR IVANIOUS . UIg						
Natural Numbers.	0	II	2	3	4		
443	6464037	6465017	6465997	6466977	6467957		
444	6473830	6474808	6475785	6476763	6477740		
445	0483600	6484576	6485552	6486527	6487502		
446	6493349	6494322	6495296	6496259	6497242		
447	6503075	6504047	6505018	6505989	6506960		
448	5512780	6513749	6514719	6515687	6516656		
449	6522463		6524397	6525364	6416030		
450	6522.24	6523430	6534055	6535019	6526331		
	6532125	6533090	6543691	6544653	6535984		
451	6541765	6542728	6561206	6554266	6545016		
452	6551384	6552345	<b>655</b> 3306 6562899	6563857	6555226		
453	6560982	6561941	6302099	667.407	6564815		
454	6570559	6571515	6572471	6573427	6574383		
455	6580114	6581068	6582023	6582976	6583930		
456	6589648	6590601	6591553	6592505	659;456		
457	6599102	6600112	6601002	6602012	6602962		
458	6608655	6609603	6610551	6611499	6612446		
459	6618127	6619073	6620019	6620954	6621910		
460	6627578	6628522	6629466	6630410	0631353		
461	6637009	6637951	6638893	6639835	0640776		
462	0646420	6647360	6648299	6649239	6650178		
463	6655810	6556748	6657685	6658623	6650560		
464	6665180	6666116	6667051	6667987	6668922		
465	6674530	6675463	6676397	6677331	0678264		
466	0683855	6684791	6685723	6686654	6687585		
467	6693169	6694099	6695028	6695958	0696887		
468	6702459	6703386	6704314	6705242	6706169		
469	6711728	6712654	6713580	6714506	6715431		
470	6720979	6721903	6722826	6723750	6724673		
471	6730209	6731131	6732053	6732974	67:3896		
472	6739420	6740340	6741260	6742179	6743059		
473	6748611	6749529	6750447	6751.65	6752283		
474	6757783	6758700	6759615	6760531	6761447		
475	0766936	6767850	6768764	6769678	6770592		
476	6776069	6776982	6777894	6778806	67.79718		
477	6785184	6786094	6787004	6787914	6788824		
478	6794279	6795187	6796096	6797004	6797912		
479	6803355	6804262	6805168	6806074	6806980		
480	6812412	6813317	.6814222	6815126	6816030		
481	6821451	6822354	6823256	6824159	6825061		
482	6830470	6831371	6832272	6833173	6834073		
483	6839471	6840370	6841269	6842168	6843066		
484	6848454	6849351	6850248	6851145	6852041		
485	6857417	6858313	6859208	6860103	6860998		
486	6865363	6867256	6868149	6869043	6859936		
					0009950		

Logarithms ( to 4869.) 379

Natural, Numbers56789Numbers $6468936$ $6469915$ $6470894$ $6471873$ $64728511$ $443$ $6478718$ $6479695$ $6480671$ $6481648$ $6482624$ $445$ $6488477$ $6499187$ $6590426$ $6491401$ $6492375$ $446$ $6498215$ $6499187$ $6500160$ $6501132$ $6502104$ $447$ $6507024$ $6518502$ $6510561$ $6520228$ $6521496$ $449$ $6527297$ $6528253$ $6529229$ $6531876$ $65311610$ $450$ $653686$ $6557732$ $6546739$ $6548576$ $6549462$ $452$ $656773$ $6567730$ $6567886$ $658644$ $650023$ $452$ $6556186$ $6557145$ $6556180$ $6577250$ $678205$ $453$ $6565773$ $656730$ $6567886$ $6506776$ $6598212$ $453$ $6555732$ $658739$ $658739$ $658743$ $6598212$ $454$ $6575339$ $677250$ $657743$ $6598212$ $457$ $6538337$ $6586790$ $658743$ $6607766$ $456$ $6532393$ $6614340$ $6615237$ $6607768$ $459$ $6612393$ $6614340$ $6615237$ $66265367$ $450$ $6632296$ $6632371$ $6636371$ $663867$ $450$ $6613297$ $6631393$ $66143379$ $66445339$ $451$ $6613297$ $669874$ $6590766$ $673933$ $462$ $6651117$ $6613246$		Lugi		(10 4	- / /	5/7
443       6468936       6469915       6470894       6471873       6472851         444       6478718       6479695       6480671       6481648       6482624         445       6488477       6489412       6499187       650010       6501132       6592104         446       6498115       6499187       650010       6510841       6511811         447       650790       6508901       8510961       6510841       6511811         448       6517624       6518593       65192029       6533195       6537145       65398.90       6540802         451       6546578       6537145       6538105       65590423       453       6566723       6570423       6556022         453       6565773       656730       657688       6586454       6566022         454       651539       6597545       657743       65780423       6578165       6579159         454       658484       6585837       658630       6597364       6598216       6598216       6598217       6598216       6598217       6598216       6598217       6598216       6598217       6598216       6598217       6596706       65360776       659673       6607706       6596217       6579226		5	6.	1 7	8	9
444 $6478718$ $6479695$ $6480671$ $6481648$ $6482624$ $445$ $6488477$ $6489415$ $6490420$ $6490140$ $6492375$ $446$ $6498215$ $6499187$ $6500165$ $6501132$ $6502104$ $447$ $6507906$ $650901$ $8509871$ $6510841$ $6511811$ $443$ $6517624$ $6518503$ $6529229$ $6537195$ $6514513160$ $450$ $6536948$ $65379122$ $65383676$ $6540452$ $6550423$ $452$ $6556773$ $656730$ $6567688$ $658643$ $656022$ $453$ $655773$ $656730$ $6576888$ $658643$ $6569622$ $454$ $6575339$ $6775206$ $657743$ $65866762$ $454$ $6575339$ $6775206$ $657743$ $658667688$ $4566788$ $658743$ $65867688$ $658743$ $6598212$ $457$ $6594088$ $6595396$ $6567736$ $65772506$ $458$ $6515319$ $65962106$ $659774616598212$ $459$ $6603911$ $6604806$ $6638096$ $6607786$ $450$ $6613239$ $6514340$ $6615287$ $6626796$ $451$ $66171717667266652995$ $6623295$ $6633297$ $465$ $6642537$ $66643379$ $6644539$ $6609857$ $6661434$ $6662327166632927$ $66658927$ $465$ $6689476$ $65993786679987666738326792876465668947666791976679987666799876667982266779185766799876679987667982766798276$		6468026	6460010	6470804	6471872	6472851
445 $6488477$ $6489425$ $6490426$ $6491401$ $6492375$ 446 $6498215$ $6499187$ $6500150$ $6501132$ $6502104$ 447 $6507910$ $6598901$ $8509871$ $6510841$ $6511811$ 448 $6517634$ $65189305$ $6510541$ $6510841$ $6511811$ 449 $6527297$ $6528263$ $6529220$ $6530942$ $6521456$ 450 $6536948$ $6537912$ $653876$ $65398.90$ $6540802$ 451 $6546578$ $6547530$ $6567730$ $656788$ $658645$ $6550423$ 452 $6557733$ $6567700$ $6577850$ $6578160$ $65792150$ $65792150$ 453 $6565773$ $6567730$ $6567800$ $6578160$ $65792150$ $6578160$ 454 $658484$ $6585837$ $6586790$ $6587743$ $6588696$ $65023$ 456 $6594408$ $6595359$ $6596100$ $6597250$ $6577660$ 457 $6603911$ $6604800$ $66058000$ $6607760$ $6607760$ 458 $6613393$ $6614340$ $6612347$ $66232650$ $6624745$ 450 $6632296$ $6632321$ $6653307$ $66445430$ $6644539$ 451 $6611717$ $6642658$ $6643319$ $6644539$ $66445480$ 452 $6679197$ $6601434$ $6662371$ $66732051$ $66732561$ 453 $66079197$ $668130$ $669378$ $6591308$ $6592239$ 465 $6688516$ $6898745$ $6590578$		6478718	6170604		6481648	6482624
$4_{46}$ $6498215$ $6499187$ $6500165$ $6501132$ $6502104$ $447$ $650790$ $6908901$ $8509871$ $6510841$ $6511811$ $449$ $6517624$ $6918593$ $6510541$ $6520928$ $6520928$ $6520928$ $449$ $6527297$ $612823$ $6520228$ $6539160$ $450$ $6536948$ $6537912$ $6538767$ $65408023$ $451$ $6546578$ $6547539$ $6547539$ $6549462$ $451$ $6546578$ $65771456$ $6558105$ $659023$ $453$ $656773$ $6567730$ $65678806790$ $6587443$ $451$ $65548484$ $6585837$ $6586790$ $6587743$ $456$ $6594408$ $6595359$ $6596310$ $6597761$ $457$ $6503911$ $6604860$ $6605809$ $6607786$ $450$ $652255$ $6623829$ $6632690$ $6624745$ $450$ $6622555$ $66238295$ $6632937$ $6617181$ $450$ $6622555$ $66238295$ $6632937$ $6632937$ $462$ $6651117$ $664268667$ $66279395$ $6673935$ $463$ $6669877$ $6699378$ $6591308$ $6692239$ $465$ $668516$ $6689477$ $6692748$ $6592267$ $465$ $668516$ $6689247$ $6692766$ $6732957$ $465$ $6679197$ $6611334$ $6623971$ $6632927$ $465$ $6687476$ $6592478$ $6591308$ $6592239$ $467$ $66987616$ $6898745$ <t< th=""><th></th><th>6488477</th><th>6480469</th><th></th><th>6401101</th><th>6402275</th></t<>		6488477	6480469		6401101	6402275
447 $6107930$ $690801$ $890871$ $610841$ $6511811$ $443$ $6517624$ $6918593$ $6519561$ $6120528$ $6521496$ $449$ $6527297$ $6128263$ $6529229$ $613016$ $6521496$ $450$ $6536948$ $6537912$ $653876$ $6539839$ $6540802$ $451$ $654778$ $6547739$ $6548501$ $6549462$ $6550423$ $452$ $6556186$ $657745$ $657730$ $6567888$ $6586456$ $656023$ $453$ $656773$ $656770$ $6567688$ $6586456$ $6579159$ $454$ $677339$ $6576396$ $6597250$ $6577236$ $65781205$ $457$ $6594884$ $6585379$ $6596310$ $65972461$ $6598212$ $456$ $6593159$ $6596310$ $65972461$ $6598212$ $457$ $6603911$ $6604800$ $66287957$ $6607706$ $458$ $66132296$ $6623739$ $6647459$ $6607706$ $459$ $6612246$ $6632296$ $662371$ $6633339$ $6614717$ $6642658$ $6643379$ $6644530$ $460$ $6698766$ $6670792$ $6671727$ $66726161$ $679197$ $6661434$ $6662371$ $66633037$ $66424745$ $463$ $6697816$ $6898746$ $6799676$ $670923$ $465$ $6697816$ $6698746$ $6799676$ $6709526$ $466$ $668516$ $6698746$ $6799676$ $6706022$ $467$ $6697816$ $6698746$ $6799676$ <th></th> <th>6409215</th> <th>6400197</th> <th></th> <th>6 501 92</th> <th>6:02.04</th>		6409215	6400197		6 501 92	6:02.04
443 $6517624$ $6918593$ $6519561$ $652928$ $6529195$ $6531160$ $450$ $6536948$ $6537912$ $653876$ $6539195$ $6531160$ $450$ $6536948$ $6537912$ $653876$ $6539195$ $657453$ $451$ $6546578$ $654739$ $6548507$ $6549462$ $6550423$ $453$ $656773$ $6567730$ $6567688$ $6549462$ $6550423$ $453$ $656773$ $6567730$ $6577250$ $6578205$ $6579159$ $454$ $6577339$ $6577230$ $6577230$ $657743$ $6586962$ $454$ $6577339$ $657623$ $6596310$ $6.97261$ $6598212$ $457$ $6503911$ $6604860$ $6605909$ $6605758$ $6607788$ $6613393$ $6614340$ $6615287$ $6616234$ $6617181$ $459$ $6622755$ $66236307$ $6636497$ $6636497$ $6632296$ $6633239$ $66341379$ $6644539$ $6645480$ $462$ $6651117$ $6670392$ $671727$ $6673955$ $463$ $669876$ $670926$ $670792$ $673773$ $6592239$ $465$ $6697816$ $6698745$ $6599378$ $6591308$ $6592239$ $467$ $6697816$ $6698745$ $6599378$ $6591308$ $6592239$ $466$ $6688516$ $6689475$ $6599574$ $6709626$ $6716326$ $470$ $6725596$ $672578$ $673595$ $67292487$ $471$ $6734936$ $67259574$ $6720556$ $67$		6107020	6408001			6411911
449 $6527297$ $6328263$ $6529229$ $633194$ $6531160$ 450 $653688$ $6537912$ $6538876$ $65398.99$ $6540502$ 451 $654678$ $6547739$ $6548501$ $6549622$ $657023$ 452 $655713$ $6567730$ $6567886$ $6590623$ 453 $6567730$ $6567730$ $6577856$ $6578250$ 454 $6575339$ $6577250$ $6578257$ $6579261$ 454 $6575339$ $6577250$ $6577250$ $6577250$ 454 $6592212$ $6592261$ $65982122$ 457 $6503911$ $6604360$ $6605809$ 456 $6192468$ $6795359$ $6596310$ $6597261$ 458 $6613393$ $6614340$ $6615287$ $6610234$ $66122565$ $6623800$ $6624745$ $6625690$ 451 $6611717$ $6642658$ $66437399$ $6644539$ 462 $6651117$ $6652056$ $6652995$ $6633933$ 463 $6669857$ $667092$ $670792$ $6671727$ 463 $6669857$ $667092$ $6708023$ $6709876$ 465 $6697816$ $6698745$ $6599378$ $6591308$ 469 $6716356$ $671281$ $6718206$ $673574$ 470 $6725596$ $672578$ $673574$ $672052487$ 471 $6734817$ $6735738$ $6736574$ $672052487$ 473 $6716226$ $673177$ $678629$ $6720512$ 474 $6762362$ $6763277$ $6765107$ $676602248$		6517594	6418602	6610661		6621406
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465 $0079197$ $6680130$ $66811062$ $6581995$ $6632927$ $466$ $6688516$ $6689447$ $6690378$ $6591308$ $6592239$ $467$ $6697816$ $6698745$ $6599674$ $6700602$ $6701530$ $463$ $6707096$ $6708023$ $6708950$ $6709876$ $6710802$ $469$ $6716356$ $6717281$ $6718206$ $6719130$ $6720544$ $470$ $6725596$ $672519$ $6727412$ $5728365$ $6729287$ $471$ $6734817$ $6735738$ $6736559$ $6737574$ $6738500$ $472$ $6744018$ $6744937$ $6745856$ $6746775$ $6747693$ $473$ $6752362$ $6763277$ $6764192$ $6765107$ $6766022$ $475$ $677505$ $6772418$ $6773332$ $6774244$ $6775157$ $476$ $6780629$ $6781540$ $6782452$ $6783322$ $6784273$ $477$ $6789734$ $6790643$ $6791552$ $6792461$ $6793370$ $478$ $6798819$ $6799727$ $680634$ $680541$ $6825464$ $682546$ $481$ $6825963$ $6826865$ $681773$ $6837673$ $6838673$ $683572$ $6837673$ $6838673$ $683572$ $483$ $6843965$ $6844863$ $684775$ $6843659$ $6847556$ $682566$ $682566$ $682566$ $482$ $6833973$ $6835773$ $6837673$ $6835672$ $6835672$ $6835672$ $6835672$ $6847556$ $474$ $6752565$ $6$	403	0006497	0001434	0002371	0003307	0004244
466 $6688516$ $6689447$ $6690378$ $6591308$ $66922339$ 467 $6697816$ $6698745$ $6599674$ $6700602$ $6701530$ 468 $6707096$ $6708023$ $6708950$ $8709876$ $6710802$ 469 $6716356$ $6717281$ $6718206$ $6720547$ 470 $6725596$ $6725196$ $6725196$ $6725196$ 471 $6734917$ $6735738$ $6736596$ $674757574$ 472 $6744018$ $674937$ $6745504$ $6745755$ 473 $6752362$ $6763177$ $6765107$ $6747693$ 474 $6762362$ $6763177$ $6765107$ $6766022$ 475 $6775556$ $6772418$ $6773332$ $6774244$ $67780629$ $6781540$ $6782452$ $67834273$ 476 $6788629$ $6781540$ $6782452$ $67834273$ 477 $6789734$ $6790643$ $6791552$ $6792461$ $6798819$ $6799727$ $6800634$ $6801541$ $6802448$ 479 $6807886$ $6808792$ $6809597$ $6810602$ $6811507$ 480 $6816934$ $6817838$ $6818741$ $682566$ $682564$ 481 $6825963$ $6823857$ $6836773$ $6837673$ $6838572$ 483 $6843965$ $6844863$ $684773$ $6835672$ $6847575$ 484 $6852938$ $68338734$ $685773$ $6836673$ $6847575$ 485 $6861892$ $6862787$ $6863681$ $6864575$ $6867522$ 485 <td< th=""><th>404</th><th>0009857</th><th>0070792</th><th>0071727</th><th>0072001</th><th>0073595</th></td<>	404	0009857	0070792	0071727	0072001	0073595
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	405	0079197	0680130	0081002	0081995	6602927
468 $6707096$ $6708023$ $6708950$ $8709876$ $6710802$ 469 $6716356$ $6717281$ $6718106$ $6719130$ $672054$ 470 $6725596$ $6726519$ $6727412$ $6728365$ $6729287$ 471 $6734817$ $6735738$ $6736599$ $6737574$ $6738500$ 472 $6744018$ $6744937$ $6745856$ $6746775$ $6747693$ 473 $6753200$ $6754117$ $6755034$ $6755951$ $6716867$ 474 $6762362$ $6763277$ $6764192$ $6765107$ $6760222$ 475 $677505$ $6772418$ $6773332$ $6774244$ $6775157$ 476 $6780629$ $6781540$ $6782452$ $6783362$ $6784273$ 477 $6789734$ $6790643$ $6791552$ $6792461$ $6793370$ 478 $6798819$ $6799727$ $6800634$ $6801541$ $6802448$ 479 $6807894$ $6817838$ $6818741$ $6819645$ $6829569$ 480 $6816934$ $6817838$ $6817736$ $6836573$ $6837573$ 481 $6825963$ $5826865$ $6827766$ $6888668$ $6829569$ 482 $6834973$ $6834873$ $68475761$ $6846559$ $6847576$ 484 $6852938$ $6843863$ $68475761$ $6846559$ $6847576$ 484 $6852938$ $68258776766$ $685457671$ $68545756$ $68656222$ 485 $6861892$ $686378776663681168545751686545756686545756$			6689447	6690378	0091308	0092239
$\begin{array}{cccccccccccccccccccccccccccccccccccc$			6098745	0599674		0701530
470 $6725596$ $6726519$ $6727412$ $5728365$ $6729287$ 471 $6734917$ $6735738$ $673659$ $6737574$ $6738500$ 472 $6744018$ $6744937$ $6745856$ $6746775$ $6747693$ 473 $6753200$ $6754117$ $6755034$ $6755951$ $6716867$ 474 $6762362$ $6763277$ $6764192$ $6765107$ $67660222$ 475 $677505$ $6772418$ $6773332$ $6774244$ $6775157$ 476 $6780629$ $6781540$ $6782452$ $6783362$ $6783734$ 477 $6789734$ $6790643$ $6791552$ $6792461$ $6793370$ 478 $6798819$ $6799727$ $6800634$ $6801541$ $6802448$ 479 $6807896$ $6808792$ $680997$ $6816924$ $6815054$ 481 $6825963$ $5825865$ $6817736$ $683565$ $6829569$ 482 $6833973$ $6838773$ $6836773$ $6838572$ 483 $6843965$ $684365$ $6847561$ $684659$ $6847556$ 484 $6852938$ $6833834$ $68545761$ $685659$ $68565266$ 484 $6852938$ $6823834$ $68545761$ $6856576$ $68664575$ 485 $6861892$ $68638384$ $6855626$ $6856526$ $6856526$ 485 $6861892$ $686383834$ $6855761$ $68545756$ $6865626$ 485 $6861892$ $6863681657666865766845756668457566684565968475756865457566684659$		0707090				
$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$		6716350	6717281			6720054
$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$		0725596	0726519			6729287
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$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$			⁰ 744937	0745850		6747693
475         677         505         6772418         6773332         6774244         6775157           476         6780629         6781540         6782452         6783362         6784273           477         6789734         6790643         6791552         6792461         6793370           478         6798819         6799727         6800634         6801541         6802448           479         6807886         6808792         6800697         6310602         6811507           480         6816934         6817838         6818741         6810445         682548           481         6825963         0826865         6817766         6828668         682569           482         6834973         6831873         683773         683773         683867           483         6843965         6844863         6845761         684659         6847556           483         6843965         6843834         6854770         6855026         6855026         68475556           484         6852938         6863834         6853737         6835672         6864552         684755         6864552           485         6861892         68628363         6845761         6865526		0713200	0754117	6755034	6755951	
476         6780629         6781540         6782452         678362         6784273           477         6789734         6790643         6791552         6792461         6793370           478         6798819         6799727         6800634         6801541         6802448           479         6807836         6808792         6809697         6910602         6811507           480         6816934         6817838         6818741         681945         6829548           481         6825963         082865         6817766         6828668         6829569           482         6834973         6831873         6836773         6838673         6838572           483         6845963         082865         6817766         6828668         6829569           482         6834973         6831873         6835773         6838673         6838572           483         6843965         6844863         6845761         6846559         6847556           484         6852938         6835834         685761         6864659         684755           485         6861892         68628787         6863681         6865526         685622           485         6861892         686			6763277	6764192	6765107	
$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$			6772418	6773332	6774244	6775157
478         6798819         6799727         6800634         6801541         6802448           479         6807896         6808792         680697         6910602         6811507           480         6816934         6817838         6818741         681945         6820548           481         6825963         6826865         6827766         6828668         6829569           482         6834973         6835873         6836773         6837673         6838572           483         6843965         6844863         6845761         6840659         6847556           484         6852938         6833834         6854730         6855626         685522           485         6861892         5862787         6863681         6864575         6865467	476	6780629	6781540		6783362	6784273
479         6807896         6808792         680697         6910602         6811507           480         6816934         6817838         6818741         681945         6820548           481         6825963         6826865         6827766         6828668         6829569           482         6834973         6835873         6836773         6837073         6838572           483         6843965         6844863         6845761         6840659         6847556           484         6852938         68353834         6854730         6855626         6815522           485         6861892         5862787         6863681         6864575         68654652		6789734	6790643	6791552	6792461	6793370
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485 6861892 6862787 6863681 6864575 6865469	484	6852938	6853834	6854730	6855620	6856522
486 6870828 6871727 68-9619 16879506 6894008	485	6861892	6862787	6863681	6864575	6865469
	486	6870828	6871721	6872613	6873506	6874398

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Artificial Numbers: Or,

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Numbers,	Ŭ		2	3	4
487	6875290	6876181	687 <b>7</b> 073	6877564	6878855
488	6884198	6885088	6885978	6886867	6887757
489	0893019	6893977	6894864	6895752	6896640
490	6901961	6902847	6903733	6904616	6505505
491	6910815	6911699	6912584	6913468	6914352
492	6919651	6920534	6921416	6922298	6923180
493	6928469	6929350	6930231	6931111	6931991
494	6937269	6938148	6939027	693 <b>99</b> 06	6940785
495	6946052	0946929	6947806	6948683	694956U
496	6494817	6955692	6956568	6957443	6958318
497	6963564	6964438	6965311	6 <b>9661</b> 85	6967058
<b>4</b> 9 <b>8</b>	6972293	6973165	6974037	6974909	6975780
499	6981005	6981876	6982746	6983616	6984485
500	698 <b>9</b> 700	6990569	6991437	6992305	0993173
SOI	°998377	6999244	7000111	7000977	7001843
502	7007C37	7007902	7008767	7009622	7010496
503	7015650	7016543	7017400	7018269	7019132
504	702430 <b>5</b>	7025167	7026:28	7026890	7027751
505	7032914	7033774	7034633	7035493	7036352
500	7041505	7042363	7043 <b>22</b> 1	7044079	7044937
507	7090080	7050936	7051792	7052649	7053505
508	70586;7	7059492	7060347	7061201	7062055
509	7067178	7068031	7068884	7069737	7070589
510	7075702	7076553	7077405	7078250	7079107
311	7084206	7085059	7085908	7086758	708 <b>76</b> 07
512	7092700	7093548	7094396	7095244	7096091
513	7101174	7102020	7102866	7103713	7104559
514	7109631	7110476	7111321	7112165	711:010
515	7118072	7118915	7119759	7120601	7 21444
516	7126497	7127339	7128180	7129021	7129862
517	7134905	7135745	7136585	7137425	7138264
518	7143298	7144136	7 44974	7145812	7146650
519	71<1674	7152510	7153347	7154183	7155019
<b>5</b> 20	7160033	7160869	7161703	7162538	7163373
521	7168377	7169211	7170044	7170877	7171710
522	7176705	7177537	7178369	71 79200	7180032
523	7185017	7185847	7,186677	7187507	7188337
524	7193313	7194142	7194970	7195799	7196627
525	7201593	7202420	7203247	7204074	72049°I
526	7200817	7210683	7211508	7212334	7213159
527	7218106	7218930	7219754	7220578	7221401
528	7226339	7227162	7227984	7228806	7229628
529	7234557	7235378	7236198	7237019	7237839
430	72-3759	7243578	7244397	3245216	7246035

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Logarithms (to 5309.) 381

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Natural Numbers.	5	6	7.	8	s,
487	6879746	6880637	6881528	6882418	6883308
488	6988646	6889535	6890423	6691312	6892200
489	6897527	6898414	6899301	8810006	6901074
490	6906390	6907275	6905161	6909046	6909930
491	6915235	6916119	6917002	6917885	6918768
492	6924062	6924944	6925826	6926707	6927588
493	6932872	6933752	6934611	6935511	6936390
494	6941663	6942541	6943419	6944297	6945174
495	6950437	6951313	6952189	6953065	6953941
496	6959193	6960067	6960942	6961816	6962690
497	6967931	6968804	6969676	6970549	69 <b>714</b> 21
498	6976652	6977523	6978394	6979264	6980135
499	6985355	6986224	6987093	6987963	6988831
500		6994908	6995776	6996643	6997510
501	6994041	7003575	7004441	7005307	7006172
502	7002709	7012225	7013089	7013953	7014816
-	7011361	7020857	7021719	7022582	7023444
503	7019995 7028612	7029472	7070333	7031193	7032054
504 505	-	7038071	7038929	7039788	7040647
506	7037212	7046652	7047509	7048366	7049223
	7045793	7055216	7056072	7056927	
507 508	7054360	7063764	7064617	7005471	7057782 7066324
500	7062910 7071442	7072294	7073146	7073998	7074850
		7080808	7081659	7082505	7083359
510 511	70 <b>79957</b> 7088456	7089305	7090154	7091003	7091,851
512	7096939	7097786	7098633	7099480	7100327
513		7106250	7107096	7107941	7108786
514	7105404 7113854	7114698	7115542	7116385	7117229
515	7122287	7123129	7123971	7124813	7125655
516	7130703	7131544	7133385	7133225	7134065
517		7139943	7140782	7141620	7142459
518	7139104 71474 ⁸ 8	7148325	7149162	7150000	7150837
	7155856	7156691	7157527	7158363	7159198
519 520	7164207	7165042	7165876	7166710	7167544
521	7172543	7173376	7174208	7175041	7175873
522	7180863	7.181694	7182525	7183356	7184186
	7189167	7189996	7190826	7191055	7192484
523 524		7198283	71991,11	7199938	7200766
524 525	7197455 7205727	7206554	7207380	7208206	7209032
526		7214809	7215633	7216458	7217282
	7213984	7223048	6223871	7224694	7225517
527 528	7222225		7232093	7232914	
	7230450 72386 <b>6</b> 0	7231272 7239480	7232093	7232914 7241120	7233736
529	7246854	7239400	7248491	7249309	7241939 7250127
53 <del>6</del> 7	/2400)4	7247672	140491	1-49309	141014/1

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vambers, 53 l	7250945	7251763	7252581	7293398	7254215
532	7219110	7259933	7200749	7201509	7262380
533	7267272	7268087	7268901	7269716	
\$34	7275413	7176226	7277039	7277832	7278664
535	7283538	7284349	7285161	7285972	1286784
536	7291648	7292458	7293268	7894078	1294888
\$37	7299743	7300551	7301360	7302168	
138	7307823	7308630	7809437	7310244	
539	7315888	7316693	7317499	7318304	
940	7323938	7 <b>3247</b> 49	7325946	7326390	
941	3331973	7332775	7333578	7334380	
542	7339993	7340794	7341595	7.34= 396	1343197
\$43	7347998	7348798	7349598	7350397	7391196
544	7355989	7356787	7357585	7398383	7399181
549	7363965	7364762	7365598	7366355	7367151
946	7371926	7372792	7373517 7381461	7374312	
347	7379673	7380667		7382254	
548	7387806	7388598	7389390	7390182	7390974
549	7395723	7396514	7397305 7405206	7398390	
550	7403027	7404416	7413092	7405999	
552	7411510	7412304 7420177	7420964	7413880 7421750	
552	7419391 7487251	7428037	7428822	7429607	
\$ 53	7439098	7435881	7436669	7437449	
554 555	7442930	7443712	7444495	7445277	7446059
550	7440748	7451529	7452310	7453091	7453871
517	7458552	7459332	7460111	7460890	
558	7466342	7407120	7467898	7468676	
559	7474118	7474895	7475672	7476448	
560	7481880	7482650	7483431	7484206	7484981
561	7489629	7490403	7491177	7491950	
562	7497363	7498130	7498908	7499681	7500453
563	7505087	7505855	750626	7907398	7508168
564	7512791	7513561	7514331	7515100	
565	7520484	7521253	7522022	7522790	
566	7528164	7528932	7529699	7530466	
567	<b>7</b> 93 <b>9</b> 831	7536596	7537362	7938128	7538893
508	7541483	7544248	7545012	7545777	7546541
569	7451123	7951880	75-2649	7553412	
570	7558749	7559510	756:279	7\$61034	7561795
571	7500361	7567122	7567882	7568642	7569402
572	7573960	7574719	7575479	7576237	7576996
573	7581546	7582304	7583062 7590632	7583819	7584577
574	7589119	7589875	7390032	7591388	7552144

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Logarithms (to 5749.)

	LO	garrious	· (*0 )7	49.)	30	3
Natural Numbers.	5	<b>6</b>	. 7	8	9	ł
531	7255033	7255850	7256667	7257483	7258300	
532	7263196	7264012	7264827	7495642	726,6457	ľ
.533	7271344	7272158	7272972	7273786	7274509	ł
534	7279477	72 0290	7281101	7281914	7282726	l
535	7287595	7288406	7289216	7290027	7290828	
536	7295697	7295506	7297316	7298125	7298934	l
537	7303785	7394593	7305400	7306208	7307015	
538	7311857	7312663	7313470	7314276	7315082	ŀ
539	7319914	7320719	7331524	7323329	7323133	
\$40	7327957	7328760	7329564	7330367	7331170	
541	7335985	7336787	7337588	7338390	7339191	
542	7343997	7344798	7 \$45598	7346398	7347198	:
543	7351995	7352794	7353593	7354593	7355191	Ľ
\$44	7359979	7360776	7361574	7302371	7363168	
545	7367918	7368744	7369540	7 3 7 9 3 3 5	7371131	ŀ
546	7375902	7376690	7377491	7378285	7379076	
547	7383841	7384634	7385427	7386220	7387013	
548	7391766	7392558	7323350	7394141	739,4932	ł
549	7399677	7400467	7401257	7402047	7402837	
550	7407573	7408362	7409151	7409939	7410728	
.551.	7415455	7416283	7417030.	7417817	7418604	Ŀ.
552	7423323	7424109	7424895	7425680	7426466	ć
553	7431176	7431961	7432745	7433530		
554	7439015	7439799	7440582	7441365	7442147	ŀ
555.	7446841	7447622	7448404	7449187	7449967	l.
550	7454552	7435432	7456212	7456992	7457772	
557	7462449	7403228	7464006.	7494785	7465,564	Ł
558	7470232	747 1009	747 1787	7472564	7473341	Į
5.9	7478001	7478777	7479553	7489329	7481105	l
500	7485756	7486531	7487306	7488080	7488854	ł
561	7493498	7494271	7495044	7495817	7496590	ł
562	7501225	7501997	7592769	7503541	7504312	l
553	7508939	7509710	7510480	7511251	7512021	ł
564	7516639	7517409.	7518178	7518947	7519716	l
565	7524326	7525094	75.25862	7526620	7547397	I
506	7531999.	7532766	7533538	7534298	7535005	ł
\$67	7539659	7540424	7541189	7541954.	7542719	
168	7547305	7548069	7548832	7549596		
569	7554937	7555700	7556462	7557224		
\$70	7562596	7563318	7564079	7564840		I
571	7570162	7570922	7571682	7572441	7573201	
572	7577755	7578513	7579472	7580030.		
\$73	7,585334	7586591	7586848	7587605	7 , 88362	
574	7592900	7593656	7594412	7 . 95 . 68	7 494022	ļ
						ŧ.

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Numbers.	о 1	. • 1	2	3 H	• • f
575	7596678	7597434	7598189	7598944	7599699
576	7604225	7604979	7605733	7609486	7607240
\$77	7611758	7612511	761 3263	7014016	7614768
578	7619278	7620030	7620781	7621532	7622283
\$79	7626786	7027536	7628286	7629035	7629785
580	7634280	7635029	7635777	7636526	7637274
<b>5</b> 81	7641761	7642509	7643256	7644003	7644750
582	7649230	7649976	7650722	7651468	7652214
583	76566*6	7657430	7658175	7658920	7659664
584	7664128	7664872	7665616	7666359	7667102
585	7671559	7672301	7673043	7673785	7674527
586	7678976	7679717	7680458	7681199	7681940
587	7686381	7687121	7687860	7688600	7689339
588	7693773	7694512	7695250	7695988	7696727
583	7701153	7701890	7702627	7703364	7704101
590	7708520	7709256	7709992	7710728	77 1 1 4 6 3
591	7715875	771 6610	7717344	771 ⁸⁰ 79	7718813
592	7723217	77-395 ^I	7724684	7725417	7726150
593	7730547	7731279	7732011	7732743	7733475
594	7737864	7738596	7739326	7740057	7740788
595	7745170	7745899	7746629	7747359	7748088
596	7752463	7753191	7753920	7754648	7755376
597	7759743	7760471	7751 198	7761925	7762652
598	1767012	77677;8	7768464	7769190	7769916
599	7774268	7774993	7775718	7776443	7777167
600	7781513	7782236	7782960	7783983	7784407
601	7788745	7789467	7790190	7790912	7791634
602	7795965	7796686	7797408	7798129	7798850
603	7803173	7803893	7804613	7805333	7806053
604	7810369	7811088	7811807	7812526	7813245
605	7817554	7818272	7818989	7819707	7820424
606	7824726	7825443	7826159	7826876	7827592
607 608	7831887	7832602	7833318	7834033	783474
	7839036	7839750	7840464	7841178	7841892
609	7846173	7854010	7847599	7855434	7849024 7856145
610	7853298	7861123		7862544	7863254
611	7860412		7868933	7869643	7903254
612 613	7867514	7875313	7876021	7876730	7870352 7877438
	7874605	7882391		7883805	7884512
614 615	7881004	7889457		7890869	7891575
616	780590		7897217	7897922	7898626
617	7895807 7901852				7905666
618	7904852	7910587	7911290		
1 010	+ / yuyaag	· /yIU]0/	1 / 711-90	• / 7 11 996	/y== 0y1

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Natural 5 6 7 Numbers. 575 7600453 7601208 7601952 7	8 602717	9
	602717	
575 7000453 7001208 7001952 7		7603471
	610253	7611005
	617775	7618527
	625285	7626035
579 7630534 7631284 7632033 7	632782	763353I
	640266	7641014
581 7615497 7646244 7646991 7	647737	7648484
582 7652959 7053705 7654450 7	655195	7655941
	662641	7662385
	670074	7670816
	677494	7678235
	684901	7685641
	692296	7693035
	699678	7700416
	707048	7707784
	714405	7715140
	721750	77224 ⁸ 3
	729082	7729814
	736402	7737133
	743710	7744440
	751005	7751734
	758288	7759016
	765559	7766286
	772818	7773543
	780065	7780789
	787299	7788022
	794522	7795243
	801732	7802453
	808931	7809650
	810118	7816836
	823293	7824010 7831171
607 7835463 7836178 7836892 7	837607	7838321
	844746	7845460
	851874	7852586
	858990	7859701
	866095	7866809
	873188	7873896
	880269	7880976
	887339	7888045
615 7892281 7892986 7893691 7	894397	7895102
	901444	7902148
	908479	7909182
	915503	7916204

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Natural Numbers.	. •		2	3	4
619	7916906	7917608	7918309	7919011	7919712
620	7923917	7924617	7915318	7926018	7920713
621	7930916	7931615	7932314	7933014	7933712
622	7937204	7938602	7939300	7939998	7940696
623	7944880	7945578	7946274	7946971	7947668
624	7951 146	7912542	7953238	7953933	7954629
625	7958800	7959495	79:0190	7950884	7061578
626	7965743	7966437	7917131	7967824	7968517
627	7972075	7973368	7974060	7974753	7975445
628	7979596	7980288	7980979	7981671	7982362
629	7986506	7987197	7987887	7988577	7982267
630	7993405	7994097	7994781	7995473	7996162
631	8000194	8000982	8001670	8002358	8003040
632	8007171	8007858	800 8545	8009232	8009919
633	\$014037	8014723	8015409	8015095	8016781
634	8020893	8021578	8022262	8022947	8023031
635	8027737	8028421	8029105	8029789	8030472
636	8034571	8035254	8031937	8036619	8037302
627	8041394	8042076	8042758	8043439	8044121
637 638	8048207	8048887	8049568	8050248	8050920
629	8055009	8055688	8056368	8057047	8057720
640	8061800	8062478	8063157	8063835	806451
641	8068580	8069258	8069935	8070612	8071290
642	8075350	8070027	8076703	8077379	807805
643	8082110	8082785	8083460	8084136	808481
644	8088859	8089533	8000207	8090881	8091559
645	8095597	8096270	8096944	8097617	8098290
646	8102325	8102997	8103670	8104342	810501
647	8 109043	8109714	8110385	8111056	8111727
648	8115750	8110420	8117090	8117760	8118430
649	8122447	8123116	8123785	8124454	812512
650	8129134	8129802	8130470	8131138	8131809
. 651	8135810	81;6477	8137144	8137811	8138478
652	8142476	8143142	8143808	8144474	8145140
653	8149132	\$140707	8150462	8151127	\$15179
654	8155777	8156441	8157105	8157769	815843
655	8162413	8163076	\$163739	8104402	8165062
656	8169038.	8169700	\$170302	\$171024	8171680
657 .	8175654	8176215	8176975	8177636	8178297
658	8182259	8182019	8183579	8184239	8184898
659	8188854.	8189513	8190172	\$19:831	8191489
660	8195439	81,96097	8196755	8197413	8198071
66,I	8202015	8202672	8203328	203987	820464
662	8208580	8200230	8209892	821054	

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Logarithms (to 6629.)

	Log	<i>ariums</i>	(10 00	49· J	2°?
Natural Numbers.	5	6	7	8	1.0
619	7920413	7921114	7921815	7922516	7923216
620	7927418	7928118	7928817	7929517	7930217
621	7934411	7935110	7935809	7936507	7937206
622	7941394	7942091	7942789	7943486	7944183
623	7948305	7949061	7949757	7950454	7951150
624	7955324	7956020	7956715	7957410	7958105
625	7962273	7962967	7963662	796435 <b>6</b>	7965050
620	7969211	7969904	7979597	7971290	7971983
627	7976137	7976829	7977521	7978213	7978905
628	7983053	7983744	7984435	7985125	7985816
. 629	7989957	7990647	7991337	7992027	7992716
630	7996851	7997540	7998228	7998917	7999605
631	8003734	8004421	8005109	8005796	8006484
632	8010605	8011292	8011978	8012665	8013351
633	8017466	8018152	8018837	8019522	8020208
634	8024316	8025001	8025685	8026369	8027053
635	8031156	8031839	8032522	80;3205	8033888
636	8037984	8038666	8039348	8040031	8040712
637	8044802	8015483	\$046164	8046845	8047526
°638	8051600	8052289	8052969	8053649	8054329
639	8058405	8059085	8019763	8060442	8061121
640	8065191	8065869	8066547	8067225	8067003
641	8071967	8072643	8073320	8073997	8074874
642	8073731	8079407	8080083	8080759	8081434
643	8085A85	8086160	8086835	8087910	8088184
644	8092229	8092903	8043177	8094250	8094924
645	8098962	8099635	8100308	8100980	8101653 8108371
646	8105685	8106317	8107029	8107700	8115080
647	8112398	8113068	8113739	8114409 8121108	8121778
648	8114100	8119769	8120439.	8127797	8128465
649	8125792	8125460	8127129	8134475	8135143
650	8132473	133141	8133808	8141144	8141810
651	8139144	8139811	8140477 8147135	8147801	8148467
652	8145805	8146471	8153785	8154449	8155113
653	8152456 8159096	8153120	\$100423	\$161087	8161750
654	8155727	8159760	8167052	\$167714	8168376
655 6 <b>56</b>	8172347	8166389 8173009	8173670	8174331	8174993
657	8178958	8179618	8180278	8180939	8181500
658	8185558	8186217	8186877	8187536	8188195
659	8192145	3192826	8193455	8194123	8194781
660	8198728	8199386	8200043	8200700	8201358
661	820,298	8205955	8205011	\$207268	8207924
662	8211859	82125,14	8212170	8213825	8214480
				1.0.3.14.1310	

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					. 0,9	- 1	•
	TOTA	0		1 *	3	4	
Ē	61.7	15155-	-917:00	7919209	7919011	7919712	
	(25	-,2;01	79:4617	7915313		7920712	
•	ć21	1,051		79323 4			
:	£12	-9:-2	1 75:550	70,9300			ł
	٤1;	2:4.5	754-57			7947668	ł
I	t 2.4	1.41.4				7954629	
	£2ș	-,< <b>5</b> 500	7959495	79:019		7-01578	ł
	¢:5	1;45743	7966437	1 79 17131	7967824	79:8517	ł
	(2-	757=274	797336	7974260	7974753	7975445	
	623	13-95,6	755028	7980979	7581671	7982362	
	627	7;565:5			7988577	7982267	
	630	\$>5,405	7994-397	7994781		7596162	
	é31	30:0294		8001573		5003046	
	6:2	1.2.1			\$009232	8209919	
	633	\$014037			8015095	8016781	
	6;4	lc: 19;	SC21578		8022947	8023632	
	6;5	\$027737	\$328421	8029105	8029789	8030472	
	¢;5	2034571	8035254		8036619	8037302	
1	6;7	\$241394	\$042076	8042758	8043429	8044121	
	6;\$	8041207	8048357	8049568	8050249	8250929	
	6:9	8055000	8055588	8056;68	8057047	8057726	ĺ
	Cto	3061800	\$062478	8003157	8063935	8064513 8071290	
	641 642	5068580	8009258		8070(13	8078055	
	643	8075350 808=110	\$070027 \$0827\$5	1076703	8077379 8084136	8084811	
	544 544	5055559	8059533	8:83460	8c90381	8091555	
	*2	\$~>5597	80,5170	8090207 8096911	8097617	8098:90	
1.7	46	8102325	8102997	8103670	8104342	8105013	
1.2	47	8 to 9043	8109714	8110:85	8111050	\$111727	
	548	\$115750	8110420	8117090	8117760	8118430	
1.6	49	8122347	812;116	8123785	8124454	8125123	
	50	\$129134	8120805	8130470	8131138	8131805	
	\$1	\$135810	81;6477	8137144	8137811	8138478	
	52	814:475	8143142	\$143808	\$14474	\$145140	
6	53	8149132	\$149797	8150462	8151127	81517	
6		8155777	8156441	8157105	\$157769	815	
6	56	8162413	\$163076	\$163739	8104402	8	
	56	81690;8	8169700	\$170;02	\$171024		
	57	8175654	8176315	8176976	8177		
D-	1 62	8181459	\$181919	8183579	1		
6		\$188854	8189513	8192175			
6	ia - 1	8195438	81,6097	to fee			
¢(		202014	8202072	16.			
60	52 5	\$208580	5100230				
-	-	-					

	Natural Numbers.	5	6	1 7	8	109	i
	619	7920413	7921114	7921815	7922516	7921216	l
	620	7927418		7928817			I
	621	7934411	7935110				I
	622	7941394		and the second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second second se			I
	623	7948305					I
	624	7955324		7956715			l
	625	7962273	7962967	7953662			l
1	626	7969211	7969904	7970197		7971983	l
1	627	7976137	7976829	7977521	7978213	7978905	ŀ
ł	628	7983053	7983744	7984435	7985125		l
I	629	7989957	7990647	7991337	7992027	7992716	l
I	6,0	7996851	7997540	7998228	7998917	7999605	l
I	631	8003734	8004421	8005109	8005796	8006484	
I	632	8010605	8011292	8011978	8012665	8013351	ŀ
I	633	8017466	8013152	8018837	8019522	8020208	
ł	634	8024316	8025001	8025685	8026369	8027053	
I	635	8031156	8031839	8032522	80;3205	8033888	
ŀ	636	8037984	8038666	8039348	8040031	8040712	
Į	637	8044802	8045483	8046164	8046845	8047526	
l	638	8051609	8052289	8052969	8053649	8054329	
ŀ	639	8058405	8059085	8059763	8060442	8061121	
l	640	8065191	8065869	8066547	8067225	8067903	
L	641	8071967	8072643	8073320	8073997	8074874	
l	642	8078731	8079407	8080083	8080759	8081434	
L	643	8085485	8086100	8086835	8087510	8088184	
l.	644	8092229	8092903	8093577	8094250	8094924	
ľ	645	8098962	8099635	8100308	8100980	8101653	
1		8105685	8106357	8107029	8107700	8108371	
ł.		8112398	8113068	8113739	8114409	8115080	
		0010118	8119769	8120439.	\$121108	8121778	
8		8125792	8125460	8127129	8127797	8128455	
b		8132473	8133141	8133808	8134475	8135143	
b	651	8139144	8139811	8140477	8141144	8141810	
	652	8145805	8146471	8147135	8147801	814845	
		8152456	8153120	8153785	8154449	SISSAN	
		815909	760	8160423	8161087	Batter	
	2.45	1547	89	8167052	8167714	A State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of State of S	
			29	8173670	817433	DIP-	
	4	12	18	8180178	8180531	and i	
			-17	8186877	818752		
			900	8193455	8114	100 C	
			Sector 1	0043		100	

•	388	Arti	ficial N	umbers :	Or,	
ł	Natural Numbers.	0	1	2	. 3	4 1
	663	8215135	8215790	8216445	8217100	8217755
	664	8221681	8222335	8122389	8223643	8224296
	665	8228210	8228869	8229522	8230175	8230828
	666	8234742	8235394	8236045	8236698	8237350
	667	8241258	8241909	8242560	8243211	8243862
	658	8247765	8248415	8249065	8249715	8290364
	669	8254261	8254910	8255559	8256208	8255857
	670	8260748	8261396	8262044	8262692	8263340
	671	8267225	8257872	8268519	8269160	8269813
	672	8273693	8274339	8274985	8275631	8276277
	673	8280151	8280796	8281441	8282086	8282731
	674	8286599	8287243	8257887	8288532	8289176
	675	8293038	8293681	8294324	8294967	\$295611
	676	8299467	8300109	8300752	8301394	8302036
	677	8305887	8306528	8307169	8307811	8308152
	678	8312297	8312937	8313578	8314218	5314858
	679	8318698	8319337	8319977	8320016	8321255
	680	8325089	8325728	8326366	8327005	0327643
	681	8331471	8332109	8332746	8333384	8334021
	682	8337844	8338480	8339117	83;9754	8340390
1	683	8344207	8344843	8345479	8346114	8346750
	684	8350561	8351196	8351831	8352465	\$352100
	685 686	8356906	8357540	8358174	8358807	8359441
	<b>6</b> 8 ₇	8363241	8363874	8364507	\$365140	0305772
	688	8369567	8;70199	8370832	8371463	×372095
	689	8375884	8376516	8377147	8377778	837840g
	<b>6</b> 50	8382192	8382822	8383453	8384083	8384713
	691	8388491	8189120	8389750	8390379	8391008
	692	8394780 8401061	8395409	8396037	8396666	8397294
	693		8401638	8402316	8402943	8403571
	694	8407332	8407959	\$408585	8409212	8409838
		8413595	8414220	8414846	8415472	8416097
•	695 696	8419848	8420473	8421098	8421722	8422347
•	697	8426092	8426716	8427340	8427964	8428588
	698	8432328 8438554	8432951	8433574	8434197	8434819
	659	8444772	8439176	8439798	8440420	
	700	8450980	8445393	8446014	8446635	8447256
	701	8457180	8451601 8457800	8452291 8458419	8452841	8453461
	702	8463371	8463990	8464608	8459038	8459658
	703	8469553	8470171	8470789	8465227	8465845
÷	704 .	8479727	8476343	8476960	8471406	847 2024
	705	8481891	8482507	8483123	8477577 8483739	8478193 8484355
	706	8488047	8488662	8489277	8489892	8490507
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Logárithms ( to 7069.)

			<b>`</b> /		
Natural Numbers.	5	<b>6</b> :	7	8	9.
663	8218409	8219064	8219718	8220372	8221027
664	8224950	8225603	8226257	8226910	8227563
665	8231481	8232133	8232786	8233438	8234090
666	82350.2	823 613	8239305	8239956	8240607
667	8-44513	8245103	8245814	8246464	8247114
668	8251014	8251664	8252313	8252963	8253612
669	8:57506	8258154	8258803	8259451	8260100
670	8263988	8264635	8205283	8265931	8266578
671	8270460	8271107	8271752	8272400	8273046
672	8276913	8277969	8278214	8278860	B279505
673	8233376	8284021	8284665	8285310	8285955
674	8289820	8 <b>290</b> 463	8291107	8291751	8292394
675	82962 14	8296896	8297539	8298182	8298824
676	8302678	8303320	8303962	8304603	8305245
677	8309093	8309734	8310375	831.010	8311656
678	8315499	8316139	8316778	8317418	8318058
679	8321895	8322534	8323173	8323812	8324450
680	8328281	8328919	8329558	8330195	8330833
681	8334659	8335296	833 5933	8336570	8337207
. 682	8341027	8341663	8312299	8342937	8343571
683	8347385	8348021	8348656	8349291	8349926
684	8353735	8354369	8355003	8315638	8396272
685	8300075	8360708	8391341	8361975	8362608
686	8366405	8367038	8367670	8368303	8368935
687 688	8372727	8373359	8373990	8374622	8 375253
600	8379039	8379670	8380301	8380931	8381562
689	8385343	8385973	8386602	8387232	8387861
690	8391637	83 <b>9226</b> 5 839 <b>855</b> 0	8392895	8393523	8;94152
691	8397922		8399178	8399806	8400433
692	8404 98	401825	8405452	8406079	8406706
693	8410465 8416722	8411091	841 1717	8412343	8412969
694	8410722	8417348	8417973	8413598	8419223
695 696	8429211	8423596 8429735	8424220	8421844	8415468
697	8435442	8436065	8430458	8431081	8431705
698	S44# 664	8442286	8436687	8437310	8437932
699	8447877	8148498	8442907	8143529	8444150
700	8454081	8454701	8449119	8449739	8450360
701	8460277	8460896	8455321 8461515	8455941	8456561
702	8460463	8467081	8467700	8462134 8468318	8462752 8468935
703	8472641	8473258	8473876	8474493	8475110
704	8478810	8479426	8480043	8480659	8481275
705	8484970	8485586	8486201	8486817	8487432
- 706	8491122	8491736	8492 <u>35 i</u>	8492955	8493580
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	390	277	144101 17	warnoers: Or,		
1	Natoral Numbers.	0	T	2	3.	1 * 1
	707	8494194	8494808	8494423	8496037	8496651
	708	8500333	8,00946	8501559	8502172	8502786
	709	8506462	8507075	8507687	8508300	8508912
	710	8512583	8513195	8513807	8514418	8515030
	711	8518696	8519307	8519917	8520528	8521139
	712	8514800	8525410	8526020	8516629	8527239
		8530895	8531504	8538113	8532722	8533331
	713	8536982	8537590	8538198	8538806	8539414
	714 715	8543000	8543668	8544275	8544882	8545489
			8549737	8550343	8550949	8551556
	716	8549130	8555797	8556403	85\$7008	8557014
	717	8555192	8561849	8562454	8563059	8563663
	718	8561241	8607893	8568497	8569101	8569701
	719	8567289		8574535	8575134	8575737
	720	8573325	8473928	8580557	8-8-1-0	
	721	8579353	8579955	8586575	8581159	8581761
	722	8585372	8585973		8587176	85 <b>877</b> 77
	723	8591383	8591984	8592584	8593185	8503785
	724	8597386	8597985	8598585	8599185	8599784
	725	8603380	8603979	8604578	8605177	8605776
	726	8609366	8609964	8610462	8611160	8611758
	717	8615344	8615941	8616539	8617136	8617733
	. 728	8621314	8621910	8632507	8623103	8623699
	729	8627275	8627871	8628467	8629062	8629658
	730	8633229	863,823	8634418	8635013	8635608
	731	801917∡ 1	8639768	8640362	8640956	8641550
	732	8645111	8645704	8646297	8646890	8647483
	733	8051040	8651632	8652225	8652817	8653409
	734	8656961	8657562	8658144	8658735	8659827
	735	8662873	8663464	8664055	8664646	8665236
	736	8668778	8669368	866994\$	8670648	8671138
	737	8674675	8675264	8675858	8676442	8677931
	738	8680564	8681162	8681740	8682329	8682917
	739	8686444	8687032	8687620	8688207	8688794
	740	8992317	8692904	8693491	8694077	8694664
	741	8698182	8698768	8699354	8699949	8700526
	742	8704039	8704624	8705109	8795795	8706380
	743	8709888	8710473	8711057	8711641	8712926
	744	8715729	8716313	8716897	8717480	8718064
	745	8721563	8722146	8722728	8723311	8723894
	746	8727388	8727970	8728552	8729134	8799710
	747	8733206	8 4 3 3 7 8 8	8734369	8734960	8735531
	748	8739016	8739597	8749177	8740757	874133
	749	8744818	8745398	8745978	8746557	8747-37
	750	8750613	8751192	8751771	8752349	8752928

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Logarithms (to 7509.)

		2	s (to 7		391	
Natural Numbers.	. 5	6	7 :	8	· 9	1
707	8497264	8497878	8498492	8499106	8499719	
708	8503399	8504011	8504624	8505237	\$ 505850	
709	8509524	8510136	8510748	8511360	8511972	
710	8515641	8516252	8516863	8517474	8518085	
711	8521749	8522359	8522970	8523580	8524190	
712	8527849	8528458	8529068	8529677	8530286	
713	8533940	8534548	8535157	8535765	8536374	
714	8540022	8540030	8541238	3541845	\$542453	
715	8546096	8546703	8547310	\$547917	8548524	
716	8552162	8552768	8553374	8553980	8554586	
717 718	8558219	8558824	8569429	8500035	8560640	ł
719	8 <b>564268</b> 8570308	8504872 8570912	8555476 8571515	8506081	8500085	ł
720	8576340	8576943	8577545	8572118 8578148	\$572722	
721	8582303	8582965	8583567	8584169	8578750	Į
722	8588379	8588980	8589581	8590181	8584770 8590782	
723	8594385	8591986	8595586	8596186	8596786	
724	8600384	8600983	8601583	8602182	8602781	
725	8606374	8606973	8607571	8608170	8608768	
726	8612356	8612954	8613552	8614149	8614747	
727	8618330	8618927	8619524	8620120	8620717	
728	8624296	8624892	8625488	8626084	8626679	
729	8630253	8630848	8631443	8632039	8622624	
730	8636202	8636797	8637391	8637985	8638580	
731	8642143	8642737	8643331.	8643924	8044517	
732	8648076	8648669	8649262	8649855	8650447	
733	8654001	8654593	8655185	8655777	8656369	ł
734	8659918	8660 <b>509</b>	8661100	8661691	8662282	
735	8665827	8666417	8667008	8667598	8668188	
736	8671728	8672317	8672907	8673496	8674086	
737	8677620	8678209	8678798	8679387	8679975	
738 739	8683505 8689382	8684093	8684681	8685269	\$685857	
740	8695251	8689969	8690556	8691143	8691730	
741	8701112	8695 <b>837</b> 870169 <b>7</b>	8696423	8697010	8697596	-
742	8706965	8707549	8702283 8708134	8720868 8708719	8703454	
743	8712810	8713394	8-12079	87 14562	8709304	
744	8718647	8719230	8713978 8719814	8720397	8715140 8720980	l.
745	8724476	8725059	8725641	8726224	8726806	
746	8730298	8730880	8731461	8732043	8732625	
747	8736112	8736693	8737274	8737855	8738435	
748	8741918	8742498	8743078	8743658	8744238	
749	8747716	8748296	8748875	8749454	8750034	
750	8753507	8754086	8754664	8755243	8755821	

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Natural Numbers,	4 O "	T ·	2'	3	4
751	8756399	8756978	8757556	8759124	8758712
752	8762178	8762750	8763333	8763911	8764488
753	8767950	8768526	8769133	0769680	8770256
754	8773713	8774289	8774865	8775441	8776017
755	8779469	8780045	8780620	8781195	8781770
750	3785218	8785792	8786367	8786941	8787515
757	8790959	8791532	8792106	8792680	8793253
758	0796692	8797265	8797838	8798411	8798983
759	8802418	8802000	8803562	8804134	8804706
760	8808136	8808707	8809279	8809850	8810421
761	8813847	8814417	0814088	8815558	8816120
762	8819550	8820120	8820680	8821250	8821829
763	8825245	8825815	8826384	8826953	8827;22
764	8830934	8831502	8832070	8832620	883;207
765	0030014	8837182	8837750	8838317	8838885
766	8842288	8842855	8843421	8843988	8844555
767	8847954	8848520	8849086	8846652	8850218
768	8853612	8854178	8854743	8855308	8855874
769	8850262	8859828	8860303	0000c7	8861522
770	8864007	8865471	8866033	8866590	8867163
771	887044	8871107	8871670	8872233	8872706
772	8876173	8876726	8877298	8877860	8878422
773	8841795	8082287	0882018	S883480	8884042
774	8887410	8887971	8884532	8880003	8889653
775	8803017	8893577	8894138	8894698	8095258
776	8898617	8899177	00,09730	89002 <u>0</u> 0	8900844
777	8904210	8904765	8905328	800<887	8906445
778	8909796	8910354	8910912	8911470	8912028
779	8915375	8915932	8916489	<b>091</b> 7047	8917604
780	8920945	8921503	8922059	8922016	8923173
781	8926510	8927066	8937622	8928178	8928734
782	8932068	8932623	8933178	8933733	8934288
783	8937618	8938172	8938727	8939281	8939836
784	8943161	8943715	8944263	8944822	8945376
785	8948697	8919250	8949803	8950356	8950909
786	8954225	8954778	8951330	8955883	8956435
787	8959747	8960299	8960851	8961403	8961954
788	8965262	8965813	8966364	8966915	8967466
789	8978770	8971 120	8971871	8972421	8972971
790	8976271	8976821	8977370	8977920	8978469
791	8981755	8982314	8982863	8983412	8983960
79 ²	8987252	8987800	8988348	8988897	8989445
793	8992732	8993279	8993827	8994375	8994922
794	8998205	8998752	8999299	8,99846	90303921

Logarithms (to 7949.) 393

Natural56789Numbers.751 $8759290$ $8759868$ $8760445$ $8761023$ $876160$ 752 $8755065$ $8765642$ $8766219$ $8765796$ $876737$ 753 $8770823$ $8771409$ $8771985$ $8772501$ $8773137$ 754 $8776592$ $877168$ $8777743$ $8778319$ $8778899$ 755 $8782345$ $8782919$ $8783494$ $8784069$ $8784643$ 756 $8783089$ $8788663$ $8789237$ $8789811$ $8790556$ 757 $8793826$ $8794400$ $8794973$ $8795546$ $8796113$ 758 $8799556$ $8800128$ $88c0701$ $8801273$ $88018464$ 759 $8805278$ $8805850$ $88c6421$ $8806993$ $8307562$ 760 $8810992$ $8811563$ $8812134$ $8818400$ $8818960$ 761 $886699$ $8812968$ $8823737$ $88240797$ $8830647$ 763 $8828090$ $828659$ $8829228$ $8829797$ $8830647$ 764 $8833775$ $8834343$ $8834911$ $8835479$ $8850693$ 765 $8550784$ $8851350$ $8851915$ $8857948$ $8866324$ 768 $8850726$ $8863854$ $886571$ $88698671$ 769 $866086$ $8362651$ $8863854$ $8869417$ 768 $8850726$ $8863854$ $8860571$ $888123$ 773 $884603$ $885105$ $8891336$ $897498$ 774 $890214$
751 $8759290$ $8759868$ $8760445$ $8761023$ $8761602$ $752$ $8755065$ $8765642$ $8766219$ $8765796$ $876737$ $753$ $8770833$ $8771409$ $8771985$ $8772501$ $8773137$ $754$ $8776592$ $877168$ $8777733$ $8778309$ $8784069$ $8784069$ $755$ $8782345$ $8782019$ $8783494$ $8784069$ $8784663$ $756$ $8783689$ $8783653$ $8789237$ $8789811$ $8703867$ $756$ $8793826$ $879400$ $8794973$ $8705546$ $8706112$ $757$ $8793826$ $879400$ $8794973$ $8705546$ $8706184$ $759$ $8855278$ $8802850$ $88c6421$ $8806993$ $8307566$ $760$ $881092$ $8811563$ $8812134$ $8812705$ $8313276$ $761$ $881699$ $8817269$ $8817840$ $8818410$ $8818960$ $762$ $8822398$ $8822968$ $8823537$ $8824076$ $763$ $8828090$ $8818659$ $8829228$ $8829797$ $88303647$ $764$ $8833775$ $8834343$ $8634911$ $88354783$ $885699$ $767$ $8850784$ $8857509$ $8851348$ $885699$ $767$ $8850784$ $88579547$ $8863779$ $885334$ $767$ $8857726$ $88579547$ $8863779$ $8856334$ $768$ $8856439$ $88579547$ $8863795$ $8863779$ $8856334$ $769$ $8866363$ $8879547$ $88$
752         8755065         8765642         8766219         8765796         876737           753         8770833         8771409         8771985         8772501         877313           754         8776592         877168         877743         878309         8784669         8784669           755         878235         8782919         8783494         8784069         8784664           756         878369         8783653         8789237         8789811         870338           757         8793826         8794400         8794973         8705546         8706113           758         8799556         8805278         8805278         8801273         8801273         8801840           759         885278         880580         8812134         8812705         8313276         8313276           761         8810992         8817269         8817840         8818410         881896           762         8822398         8822908         8823537         8824107         8824076           763         8828000         8828659         8829228         8829797         783036           764         8833775         8834911         835479         883604           765
753 $8770833$ $8771409$ $8771985$ $8772501$ $877315$ $754$ $8776592$ $8777168$ $8777743$ $8778319$ $8778369$ $755$ $8782345$ $8782919$ $8783494$ $8784069$ $8784643$ $756$ $8783089$ $8788663$ $8789237$ $8789811$ $8790364$ $757$ $8793826$ $8794400$ $8794973$ $8795546$ $8796163$ $757$ $8793826$ $8794400$ $8794973$ $8795546$ $8796163$ $758$ $8799556$ $8800128$ $88c0701$ $8806923$ $807566$ $760$ $8810992$ $8811563$ $8812134$ $8812705$ $8313276$ $761$ $8816992$ $8817269$ $8817840$ $8818410$ $8818969$ $762$ $8822398$ $8822968$ $8823777$ $8824077$ $8820767$ $763$ $8828090$ $8818659$ $88249797$ $8820767$ $8830643$ $764$ $883775$ $8834333$ $8834911$ $8835479$ $8830452$ $764$ $883775$ $8834538$ $8846255$ $8846821$ $8847336$ $764$ $8837758$ $8857004$ $8857569$ $8858134$ $885304$ $766$ $885726$ $8863354$ $8863279$ $8863344$ $768$ $8850726$ $8863254$ $8863354$ $8869417$ $769$ $886726$ $8863257$ $88860571$ $8858123$ $774$ $890214$ $890775$ $89633891896$ $8897498$ $8976565$ $777$ $895818$ $89637$ $8969$
754 $8776592$ $8777168$ $8777743$ $8778319$ $8778319$ $8778309$ $755$ $8782345$ $8782919$ $8783494$ $8784069$ $8784643$ $756$ $8788089$ $8788663$ $8789237$ $8789811$ $8799364$ $757$ $8793826$ $8794400$ $8794973$ $8795546$ $8796115$ $757$ $8793826$ $8794400$ $8794973$ $8795546$ $8796115$ $757$ $8793826$ $8794400$ $8794973$ $8795546$ $8796115$ $759$ $885278$ $8805850$ $88c6421$ $8806993$ $807564$ $760$ $8810992$ $8811563$ $8812134$ $8812705$ $8313276$ $761$ $8816992$ $8817269$ $8817840$ $8818410$ $8818966$ $763$ $8828090$ $8822398$ $8829797$ $8826076$ $8823077$ $763$ $8828090$ $8828659$ $8824977$ $883075$ $764$ $883775$ $8834333$ $8834911$ $8835479$ $8830547$ $765$ $8859452$ $8840019$ $8840255$ $8846821$ $884733$ $766$ $8857044$ $8851350$ $885134$ $885304$ $768$ $8856439$ $8857044$ $885354$ $8857048$ $8857048$ $768$ $8850726$ $8863354$ $8869817$ $886988$ $769$ $886086$ $8862651$ $8863257$ $886698$ $771$ $89726$ $8879537$ $889635$ $8897498$ $887561$ $772$ $8878985$ $8879576$ $8896353$
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Еее

3 <b>94</b>	Art	ificial A	lumbers .	: Or,	
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805	9057960	<b>9</b> 058498	9059038	9059577	9060116
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817	9122220	9122752	9123234	9123815	9124346
818	9127533	9128064	9128595	9129126	9129656
819	S132839	9133369	9133899	9134430	9134960
820	9138139	9138668	9139198	9139727	9140257
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825	9164539	9165066	9165592	9166118	9166645
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829	9185545	9186069	9186593	9187117	9187640
830	9190781	9191304	9191827	9192350	9192873
831	9196010	9196533	9197055	9197578	9198100
832	9201233	9201755	9202217	9202799	9203321
833	9206450	9206971	9207493	9208014	9208535
834	921 1661	9212181	9212702	9213222	9213743
83<	,921686 <u>5</u>	9217385	9217905	9218425	9218945
830	9222063	9222582	9223102	9223621	9224140
837	9227255	9227773	9228292	9228811	9229330
838	0232440	92;2958	9233477	9233995	92345134

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	Log	garithms	r (to 83	89.)	395
Natural Numbers.	5	6	7	8	9
795	9006402	9006948	9007494	9008039	9008585
796	9011858	9012403	9012984	9013448	9014038
797	9017307	9017851	2018.96	9018910	501948c
798	9022749	902 3293	9023837	9024381	9024924
799	9028185	9028728	9029271	9029814	9030357
800	90,3613	9034156	9034698	9935241	9035783
801	9033035	9739577	9040119	9040661	9041302
802	9044150	9044992	9045533	9046073	9046615
803	9049859	9050399	9050940	9051480	9052020
804	9055261	9055800	9056340	<b>9</b> 056880	9057419
805	9060655	9061195	9061734	9062274	9062812
806	9066044	9066582	9067121	9067659	9068197
807	9071425	9071963	9072501	9073038	9073576
808	9076800	9077337	<b>9</b> 07 <b>7874</b>	9078411.	<b>2078</b> 948
809	9082169	9082705	9083241	9083778	9084314
810	9087530	9088066	9088602	9089137	9089673
811	9092885	9093420	9093955	<b>90944</b> 50	9095025
812	9098234	9098768	9099303	<b>9</b> 099837	9100371
813	9103570	9104109	9104643	9105177	9105710
814	9108911	9109444	9109977	9110510	9111043
815	9114240	9114772	9115305	9115837	9116369
-816	9119562	9120094	9120626	9121157	9121689
817	9124878	9125409	9125940	9126471	9127002
818	9130187	9130717	9131248	9131778	9132309
819 800	9135490	9136019	9136549	9137079	9137609
820	9140786	9141315	9141844	9142373	914:90;
821	9146076	9146604	9147133	9147661	9148190
822 823	9151359	9151887	9152415	9152943	9153471
824	9150636	9157163	9147691	9158218	9158745
825	9161907	9162433	9162960	9163487	9164013
826	9167171 917 <b>2</b> 429	9167697	9168223	9168749	9161275
827	9177680	9172954 9178205	9173479	9174005	9174530
828	9182925		9178730	9179214	9179779
829	9188164	9183449 9188687	9183273	9184497 9189734	9185021
830	9193396	9193919	9189211 9191442	9191965	9190258 9195488
831	9198622	9199145	91 <i>9</i> 9667	9200189	9200711
832	9203842	920436 <b>4</b>	9199087	9205407	9205929
833	9209056	9209577	9210098	9210619	9211140
834	9214263	9214784	9215304	9215824	9216345
835	9219465	9219984	9220504	9221024	9221543
836	9224659	9225179	9225698	9226217	9226736
837	9229848	9230367	9230885	9231404	9231922
838	9235031	9235549	9236066	9236584	0237102
<u> </u>		2-21747	- <u>x-</u> )-(-0	97707-4	x-3/104

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396	Art	tificial N	Numbers.	: Or,		
Natural Numbers.	}	I	2	3	4	
839	9237620	9238137	9238655	9239172	9239690	
840	9242793	921310	9243827	9244344	9244860	
841	9247900	9248476	9248993	9249509	9250025	
842	9253121	9253637	9254152	9254668	9255184	ł
843	92:8276	9258791	9259306	9259821	9260336	
844	926;424	9253939	9264453	9264968	9265482	
845	9268567	9269081	9269595	9270109	9270622	
816	9273704	9274217	9274730	9275243	9275757	Ł
847 848	9278834	9279347 9284471	9279859 9284983	9280372 9 <b>2</b> 85495	9280885 9286007	
849	9289077	9289588	9290100	<b>92</b> 90611	9291123	
850	9204189	9294700	9295211	9295722	9296233	ł
851	9299296	9299806	9300316	9300826	9301336	
852	9304396	9304906	9305415	9305925	9306434	
853	9309490	9309999	9310508	9311017	9311526	
854	9314:74	9315087	9315596	9316104	9316612	
855	9319661	9320169	9320677	9321185	6321692	
850	9324738	9325245	9325752	9326259	9326767	
857	9129808	9330315	9330822	9331328	9331835	ŀ
858	9334873	9335379	9335885	9336391	9336897	ł
859	9339932	9340437	9340943	9341448	9341953	
860	9344984	9345489	9345994	93464 <b>9</b> 9	9347004	Ŀ
861	435 <u>0</u> 032	9350536	9351040	9351544	9352049	
102	9355073	9355576	9356080	9356584	9357087	
\$ 853	9360108	9360511	9361114	9361617	9362120	Ľ
ð <b>6</b> 4	9305137	9365640	9366143	9366645	9367148	
865	9370161	9370563	9371165	9371667	9372169	
866	9375 79:	9375680	9376182	9376683	9377184	1
867	9380191	9380692	9381193	9381693	9382194	١.
868 869	9385197	9385697 9390597	9386198 9391197	9386698 9391697	9397198 9392196	ł
870	9390198 9395193	9395692	9396191	9396690	9397189	
871	9400182	<b>9</b> 4co68o	9401179	9401677	9402176	ł
872	9425165	9405663	9406161	9406659	9407157	1
873	9410142	9410640	9411137	9111635	9412132	5
874	9419114	9415611	9415108	9416605	9417101	
875	9420081	9420577	9421073	9421569	9422065	÷
876	5425041	9425537	9426032	9426528	9427024	
877	9429996	9430491	9430986	9431481	9431976	ł
878	9434945	9435440	9435934	9436429	9436923	ŀ
879	2439882	9440353	9440877	S441371	9441865	ŀ
880	9444827	9445320	9445814	9446307	9446800	L
881	9449759	9450252	9450745	9451238	9451730	
1 882	9454686	9455178	9455671	9456163	9456655	

Logarithms (to 8829.)

	, <b></b> -2	<b>?</b>			_ >>/
Natural Numbers-	• 5	<b>, б</b> ,	7 1	· •	9
839	9240208	9240724	9241246	9241759	9242276
: 840	9245377	9245894	9246410	9246927	9247444
841	9250541	9251057	9251573	9252689	9252605
842	9255699	9256215	9256730	9257245	9257761
843	9260851	9261366	9261880	9262395	9262910
844	9265995	9266511	9267025	9267539	9268053
845	9271136	9271650	9272163	9272677	9273190
846	9276270	9276783	9277296	9277808	9278321
847	9281397	9281909	9882422	9282934	9283446
848	9286518	9287030	9287542	9288054	9288565
849	9291634	9292145	9292656	9293167	9293678
049	9991037		9297764	9298275	9298785
850	9296743	9297254	9302866	9490475	9303886
851	9101847	9302357		9303376	9303000
852	9306944	9307453	9307963	9308472	9308981
853	9312035	9312544	9313053	9313561	9314070
854	9317121	9317629	9318137	9318645	9319153
855	9322200	9322703	9323215	9323723	9324230
856	9327274	9327781	9328288	9328795	9329301
857	9332341	9332848	9333354	9333860	9334367
8,8	9337403	9337909	9338415	9338920	9339426
859	9342459	934-964	9343469	9343974	9344479
1 860	9347509	9348013	9348518	9349022	9349527
861	9352553	9353057	9353561	9354065	9354569
862	6357591	9358095	9358598	9359101	9359605
: 863	9352623	9363126	9363629	9364132	9364635
864	9367650	9368152	9368655	9369157	9369659
865	9372671	9373172	9373674	9374176	9374 ⁶ 77
866	9377686	9378187	9378688	9379189	9379690
867	9382695	9383195	9383696	9384196	9384697
. 868	9387698	9388198	9388698	9389198	9389698
869	9392696	9393195	9393695	9394191	9 94693
870	9397688	9398187	9398685	9399184	9399683
871	9402674	9403172	9403670	9404169	9404667
872	9497654	9408152	9408650	9409147	9409645
· 873.	9412629	9413126	9413023	9414120	9414617
874	9417598	9418095	9418591°	9419088	9419584
875	9422561	9423058	9423554	9424049	9424545
876	9427519	9428015	9428510	9429005	9429501
. 877	9432471	9432966	9433461	9433956	<b>943</b> 4450
878	9437418	9437912	9438406	9438900	9439395
879	9442358	9442852	9443346	9443840	9444333
. 880	94172 <b>9</b> 4	9447787	9448280	9448773	9419206
881	9452223	9452716	9453208	9453701	9454193
882	9457147	9457639	9458131	9458623	9459115

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Natural	0	Ī	2	. 3	4 1
Numbers. 883	9459607	9460099	9160591	9461082	9461574
884	9464523	9465014	9465505	9465996	9466487
885	9469433	9469923	9470414	9470905	9471395
886	9474337	9474827	9475317	9475 807	9476297
887	9479230	9479726	9480215	9480705	9481194
888	9484130	9484619	9485108	9485597	9486085
889	9489018	9489506	9489994	9490483	9490971
990	9493900	9494388	9494876	9495364	9495.852
891	9498777	9499264	9499872	9500235	9100726
892	9503049	9104135	9504622	9504109	9505596
893	9508515	9909001	9509487	9409973	9510459
894	9513375	9513861	9514347	9514832	9515318
895	9518230	9718716	9519201	95 19686	9520171
896	9523080	9923565	9524049	9524534	9525018
97	9527924	9528409	<b>9528</b> 893	9529377	9529861
898	9532763	9533247	9533730	9534214	9134697
899	<b>953</b> 7597	9538080	9538563	9539046	9539529
900	9542425	9542908	9543390	9543872	9544355
901	9547248	9\$47730	9548212	9548694	9549176
902	9552065	9152547	9553028	9953510	9553991
903	9556877	9557358	9557839	9558320	9558801
904	9561684	9562165	9562645	9563125	9563605
905	9566486	9966966	9567445	956-925	9568405
906	9571282	9571761	9572241	9572720	9573199
907	9576073	9576552	9577030 9581815	9577509	9577988
908	9580858	9581337 9586117	9586594	9582293	9582771
909	9585639	9590891	9501368	9587072	9587549
910 911	9590414	9995660	9596137	9591845 9596614	9592322
912	9595184 9599948	0000425	9600901	9601377	9597090 9601853
913	9604708	9605183	9605659	9696135	9606610
914	9609462	9609937	9610412	9610887	9611362
915	9614211	9614686	9615160	9615635	96.0 09
916	9618955	9619429	9619903	9620377	9620851
917	9623693	9624167	9624640	9625114	9625587
918	9628427	96289:0	962973	9629846	9630319
.919	9633155	9633628	9634100	\$63:573	9635045
920	9637878	9638350	9638822	9639294	9639766
921	9642596	9643068	9643539	9644011	9644482
922	9647309	9647780	9648251	9648722	9547193
923	9652017	9652488	9652958	9653428	9653899
924	9656720	9657190	9657660	9658130	9658599
925	9661417	9661887	9662336	9662826	9663295
926	9666110	<b>.96</b> 67579	9667048	9667517	9667985

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	Logarithms (to 9269.) 399							
Natural Numbers.	5	. 6	7	8	9 1			
883	9462066	9462557	9463048	9463540	9464031			
884	9466978	9467469	9467960	9468451	9468942			
885	947 886	9472376	947 2866	9473357	9473847			
886	9476787	9477277	9477767	9478257	9748747			
887	9481684	9482173	9482662	9483151	9483641			
888	9486574	9487063	9487552	9488040	9488529			
889	9491450	9491948	94924 36	9492924	9493412			
890	9495330	9496827	9497314	9497802	9498290			
891	9501213	9501701	9502188	9502675	9503162			
892	9506082	0506560	9507055	9507542	9508028			
893	9510946	9511432	9511918	9512404	9512889			
894	9515803	9516289	9516774	9517260	9517745			
895	9520656	9521141	9521626	9522111	9522595			
896	9525503	9525987	9526472	9526956	9527440			
897	9530345	9530828	9531312	9531790	9532280			
898	9535 181	9535664	9536147	9536631	9537114			
899	9540012	9540494	9540977	9541460	9541943			
900	9544837	9545319	9545802	9546284	9546766			
901	9549657	9550139	9550621	9551102	9551584			
902	9554472	9554953	9555434	9555915	9556397			
903	9559282	9559762	9560243	9560723	9561204			
904	9564086	9564566	9565046	9565526	9566006			
905	9568885	9569364	9569844	9570323	9570803			
906	9573678	9574157	9374636	9575115	9575594			
907	9578466	9578945	9579423	9579902	9580380			
908	9983249	9583727	9584205	9584683	9585161			
909	9588027	9588505	9588982	9589459	9589937			
910	9592799	9593276	9593754	9594230	9594707			
911	9597507	9598043	9598520	9598996	9599472			
912	9602329 9607086	9 <b>602</b> 805	9503280	9603756	9604232			
913	9611837	9607561 9612312	9608036	9608511	9608987			
914 915	9616583	9617058	9612787	9613261	9613736			
916	9621325	9621799	9617 <b>5</b> 32 96 <b>22</b> 272	<b>961</b> 8006 9622746	9618481			
917	0626061	9626534	9627007	9627481	9623220 9627954			
918	9630792	9631264	9631737	9632210	0632683			
919	9635517	9635990	9636462	9636934	9637406			
920	9640238	9640710	9641181	9641653	9642125			
921	9644953	9645425	9645896	9646367	9646838			
922	9649664	9650134	9650605	9651076	9651546			
923	9654369	9614839	9655309	9655780	9656250			
924	9659069	9559539.	9660009	9660478	9563948			
925	9663764	9664233	9664703	9665172	9665641			
926	9668454	9668923	9669392	9669860	9670329			

	Nacoral	0		2		
	Numbers,				3	4
ľ	927	9670797	9671266	9671734	9672203	<b>96</b> 726 <b>7</b> 1
ł	928	9675480	9675948	9676416	9676883	9677351
I	929	9680157	9680625	9581092	9681559	9682027
I	930	9684829	9685296	9685763	9686230	9686697
ł	931	9689497	9689963	9690430	9690896	9691362
I	932	9694159	9694625	9695091	9695557	9696023
	933	9698816	9699282	9699747	9700213	9700678
-{	934	9703459	9703934	9704399	9704863	9705328
1	935	9708116	9708581	9709045	9709509	9709974
1	936	9712758	9713222	9713686	9714150	9714614
	937	<b>9</b> 717396	9717859	9718323	9718786	9719249
4	938	9722028	9722491	9722954	9723417	972;880
	939	9726656	9727118	9727581	9728043	9728506
1	940	9731278	9731741	9732202	9732664	9733126
	941	9735896	9736358	9736819	9737281	9737742
	942	9740509	<b>97409</b> 70	9741431	9741892	9742353
	943	9745117	9745577	9745038	<b>9746</b> 498	9746959
	944	9749720	9750180	9750640	9751100	9751560
	945	9754318	9754778	9755237	9755695	9756150
1	946	9758911	9759370	9759829	9760288	9760747
ł	947	9763500	9763958	9764417	9764875	9765334
	948	9768083	9768541	9768999	9759457	9769915
1	949	9772662	9773120	9773577	9774035	9774492
ł	950	9777236	9777693	9778150	9778607	9779064
ł	951	9781805	9782262	9782718	9783175	9783631
	952	9 <b>7</b> 86369	9786826	9787282	97 ⁸ 7738	9788194
	953	9790929	9791385	9791840	9792296	9792751
I	954	9795484	9795939	9796394	9796849	9797304
1	955	9800034 9804579	9800488	9800943	980i398	9801852
	956 957	9809119	9805033	9805487	9805942	9806396
1	958 958	9813655	9809573 9814108	9810027	9810481	9810934
	9 <b>59</b>	9818186	9818639	9814562	9815015	9815468
1	919 960	9822712	9823165	9819092 9823617	9819544 9824069	9819997
1	961	9827234	9827686	9828138	<b>9828</b> \$89	9824522
	962	9831751	9832202	9832654	9833105	9829041 9833556
ł	963	9836263	9836714	9837165	9837616	9538066
ł	964	9840770	9841221	9841671	9842122	9842572
	965	9845273	9845723	9846173	0845623	9847.073
1	966	9849771	9850221	9850670	9851120	9851569
	967	9854265	9854714	9855163	9855612	9856061
	968	9858754	9819202	9859651	9860099	9860548
ł	<b>9</b> 69	9863238	9863686	9864134	9864582	9865030
1	970	9867717	9868165	9868513	9869065	9869508

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Logarithms (to 9709.) 401

	Lug			-4-1	• .
Natural Numbers.	5	6	7	: 8	9
927	9673139	9673607	9674076	9674544	9675012
928	9677819	9678287	9678754	9679222	9679690
	<b>968249</b> 4	9682961	9683428	9683895	9684362
929		9687630	9688097	9588564	9689030
930	9687164	9692295	9692761	9693227	9693693
931	9691829	9696954	9697420	9697885	9698351
932	9696488	9701608		9702539	9703004
933	9701143	9701000	9702074 9706722	9707187	9707652
934	9705793	9706258	9700722	9711830	9712294
935	9710438	9710902	9711366	9716469	9716932
936	9715078	9715542	9716005		9721565
937	<b>9</b> 719 <b>7</b> 13	9720175	9720639	9721102	9726193
938	9724343	9724805	9725268	9725731	9730816
939 .	9728968	972943 ⁰	9729892	9730354	
940	9733588	9734050	9734511	9734973	9735435
941	9738203	9738664	9739126	9739587	9740048
942	9742814	9743274	9743735	9744195	9744656
943	9747419	9747879	9748340	9748800	9749260
944	9752020	97 <u>5</u> 2479	9752939	9753399	9753858
945	9756615	9757075	9757534	9757993	9758452
946	9761206	9761665	9762124	9762582	9763041
947	9765792	9766251	9766709	9767167	9767625
948	9770373	9770831	9771289	9771747	9772204
949	9774950	9775407	9775864	9776322	9776779
950	9779521	97799 <b>7</b> 8	9780435	9780852	9781348
951	9784088	9784544	9785001	9785457	9785913
952	9788650	9789100	9789562	9790017	9790473
953	9793207	9793662	9794,118	9794573	9795028
954	9797759	9798214	0798669	9799124	9799579
955	0802307	9802761	9803216	9803670	9804125
950	9806850	9807304	9807758	9808212	9808666
957	9811388	9811841	9812295	9812748	9813202
958	9815921	9816374	9815827	9817280	9817733
959	9820450	9820902	9821355	9821807	9822260
960	9821974	9825426	9825878	\$826330	9826782
961	9829493	9839945	9830396	9830848	9831299
962	9834007	9834459	9834910	9835361	9835812
963	9838517	9838958	9839419	9839869	9840;20
964	9843022	9843473	9843923	9844373	9844823
965	9847523	9817973	9848422	9848872	9949322
906	9852019	9852468	9852917	9813316	9853816
967	9856510	9856959	9857407	9857856	9858305
968	9860056	9861445	9861893	9862341	9862790
969	9865478	9865926	9866374	9866822	9867270
970	9869955	9870403	9870850	9871298	6871745
7/5	1				

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Natoral	0 1	1	2	3	4
Numbers.	9872192	9972640	9873087	9873534	9871981
.971	9176663	9877109	9877550	9878003	9878 149
972	9881128	9881575	9882021	9882107	9882913
. 973	9885590	9886035	9886481	9866927	9897373
974	9890016	9390493	9893937	9891382	9891 128
975	9894498	9894943	9895388	9895833	9896278
976	9893946	0899190	9899435	9900279	9900723
977 978	9903389	9903833	9904277	9904721	9905164
	9957827	9908270		9909158	9909601
979 980	9912261	9912701	0913147	9913590	9914033
981	9916697	9917133	9917575	9918018	9918401
982	9921115	99:1557	9921999	9922441	5922884
983	9925535	9925977	9926419		9927302
984	9929951	9930392	\$930834		9931716
985	9934362	9934803	9935244		9930126
986	9938769	9939210	9939650		9940531
987	991;172	9943612			9944931
988	9947569	9948009		1 0 00	
989	9951963	9952402			9953719
	9956352	9956791		9957668	9958100
990 991	9960737		9951613	9962051	
	9965117			9901430	
992 993	9969492			9970804	997124:
994	9973864	9974301			
995	9978231	9978667			
996	9982593			99839 I	998433
997	9986952			9388258	998869
998	9991 301				
999	9995655	9996090		9996955	999739

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402

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Logarithms (to 10000.)

403

Natura'	5	6	7	8	9
.971	9874428	9874875	9875322	9875769	9876216
972	9878896	\$879343	9879789	9880230	9880682
973	9881365	9×838-6	98 4252	9884698	9*85144
074	9887818	988 264	9188710	9889135	988,60L
975	9892273	9892718	9893163	9 93508	9894050
975	9896722	9897157	9897 12	9898055	9898501
977	9901168	9901612	9902056	9902500	9902 <b>9</b> 44
978	9905608	9906052	9906496	9906940	9907383
979	9910044	9917438	9910931	9911374	9911818
980	5914476	9914919	9915362	9915805	9916247
984-	9918903	9919345	9919788	9920230	9920673
982	9923726	9923758	y924210	9924651	9925093
933	9927714	9928185	9928627	9929068	9929510
984	9932157	9932598	9933039	9933480	9933921
985	9935566	9937007	9937448	9937888	9938329
986	9940971	9941411	9941851	9942291	9742731
987	<b>99</b> 45371	9945811	9916251	99466,0	9947130
988	9949767	99 <b>592</b> 06	9950645	9951085	9951524
- 989-	9954158	9954597	9955036	9955474	9955913
990	9958545	9954983	9959422	9959860	9960298
991	9962927	9,63365	9953803	9904241	9964679
992	9967305	9967743	\$968180	9968518	9969055
<b>9</b> 93	9971679	9972116	9972553	9972990	9973427
994	9976048	9976485	9976921	9977358	<b>977794</b>
995	9980413	9980849	9981285	9981721	9982157
926	9984773	9985209	9985645	9986080	9986516
99Z	9989129	9989964	9990000	9990435	9990870
998	9993481	9993916	9994350	9994785	9995220
999	9997828	9998292	9998697	9999131	9993566

## 10000 it's Log. == 4.0000000

# The End of the Table of the Logarithms.

### Fff2

R = 1 ...

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