

UNIVEFF:TY OF CALIFORNIM, DEPARTMEI. OF CIVILENGINEERINO BERIS:゙っEY, CAUFORNIA

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## National Tube Company

# BOOK OF STANDARDS <br> AND 

USEFUL INFORMATION

CONTAINING

TABLES OF SIZES AND
OTHER USEFUL INFORMATION PERTAINING TO TUBULAR GOODS

THE ENGINEERING DATA FOR THIS BOOK EDITED BY

PROF. REID T. STEWART

1872

Price, $\$ 1.00$
1902

# National Tube Company 

## BLACK AND GALVANIZED WROUGHT MERCHANT PIPE

 Of All Kinds in Sizes from $1 / 8$ to 30 inches.
## BOILER TUBES

Of Mild Steel and Charcoal Iron For Stationary, Locomotive and Marine Work.

CASING, TUBING and DRIVE PIPE FOR WELL PURPOSES.

## GAS AND OIL LINE PIPE.

## CYLINDERS,

Lapwelded and Seamless, tested 100 lbs . to $3,700 \mathrm{lbs}$., for Compressed Air, Carbonic Acid Gas, Anhydrous Ammonia, Etc., Etc., Etc.

## WATER AND GAS MAINS.

CONVERSE AND MATHESON LEAD JOINT PIPE FOR MAINS.

Seamless Tubes, Shrapnel, Projectiles and Miscellaneous Forgings.
$8003 \div 5$

## National Tube Company

## WORKS AT

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Pennsylvania PITTSBURGH
*
MIDDLETOWN
PHILADELPHIA CHESTER OIL CITY
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YOUNGSTOWN . . . . . OHIO
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GENERAL OFFICE
FRICK BUILDING, PIT'TSBURGH, PA.

## LOCAL SALES OFFICES

Havemeyer Building 420 California Street
${ }_{267}$ South Fourth Street
Western Union Building
The Frick Building
National Tube Works

NEW YORK CITY, N. Y. SAN FRANCISCO, CAL. PHILADELPHIA, PA. CHICAGO, ILL. PITTSBURGH, PA. ST. LOUIS, MO.

## FOREIGN OFFICE

Dock House, Billiter Street, LONDON, E. C., ENG.


## PREFACE

In the following tables of Standard dimensions of Tubular Goods, it has been our aim to group together in one book all of the dimensions and data pertaining to standards as manufactured by National Tube Co. at this date, swith the object of making this book a practical and valuable aid to all users of Pipes, Tubes, etc. The use of Tubular Goods has become so extensive that a great variety of articles necessary for different purposes has to be manufactured, and a large amount of data has accumulated on the subject, and we trust that our effort to put this before the public in a compact form will prove of balue.

We have also taken up certain subjects closely related to the use of pipes, tubes, etc., and furnished such general information and engineering data pertaining to same, as, we think, woill be useful and appropriate in a book of this kind, woith the idea of popularizing such information that would lead to the intelligent application of tubular goods for purposes where engineering skill and judgment should be exercised. This data was prepared for publication by Prof. Reid T. Sterwart and is largely compiled from modern waell-known engineering authorities on the subjects.

## Tables

## OF

## STANDARD DIMENSIONS

OF

## Tubular Goods

AS MANUFACTURED BY THE

National Tube Co.

NATIONAL TUBE COMPANY.
NATIONAL TUBE CO.-Black or Galvanized Standard Weight Pipe.

| Diameter. |  |  | $\begin{aligned} & \text { Thick- } \\ & \text { ness. } \end{aligned}$ | Circumference. |  | Transverse Areas. |  |  | Nom.Wgt. per ft. lbs. | Threads per In. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Nom | External. | Internal. |  | External. | Internal. | External. | Internal. | Metal. |  |  |
| 1/8 | . 405 | . 269 | . 068 | 1.272 | . 845 | . 1288 | . 0568 | . 0720 | . 241 | 27 |
| $1 / 4$ | . 540 | . 364 | . 088 | 1.696 | 1.144 | . 2290 | . 1041 | . 1249 | . 42 | 18 |
| $3 / 8$ | . 675 | . 493 | . 091 | 2.121 | 1.549 | . 3578 | . 1909 | . 1669 | . 559 | 18 |
| 1/2 | . 840 | . 622 | . 109 | 2.639 | 1.954 | . 5542 | . 3039 | . 2503 | . 837 | 14 |
| 3/4 | 1.050 | . 824 | . 113 | 3.299 | 2.589 | . 8659 | . 5333 | . 3326 | 1.115 | 14 |
| $1{ }^{14}$ | 1.315 | 1.047 | . 134 | 4.131 | 3.289 | 1.3581 | . 8609 | . 4972 | 1.668 | $111 / 2$ |
| 11/4 | 1.660 | 1.380 | . 140 | 5.215 | 4.335 | 2.1642 | 1.4957 | . 6685 | 2.244 | $111 / 2$ |
| $11 / 2$ | 1.900 | 1.610 | . 145 | 5.969 | 5.058 | 2.8353 | 2.0358 | . 7995 | 2.678 | $111 / 2$ |
| 2 | 2.375 | 2.067 | . 154 | 7.461 | 6.494 | 4.4301 | 3.3556 | 1.074 | 3.609 | $111 / 2$ |
| 21/2 | 2.875 | 2.467 | . 204 | 9.032 | 7.750 | 6.4918 | 4.7800 | 1.712 | 5.739 | 8 |
| 3 | 3.500 | 3.066 | . 217 | 10.996 | 9.632 | 9.6211 | 7.3827 | 2.238 | 7.536 | ، |
| $31 / 2$ | 4.000 | 3.548 | . 226 | 12.566 | 11.146 | 12.566 | 9.886 | 2.680 | 9.001 | " |
| 4 | 4.500 | 4.026 | . 237 | 14.137 | 12.648 | 15.904 | 12.730 | 3.174 | 10.665 | " |
| $41 / 2$ | 5.000 | 4.508 | . 246 | 15.708 | 14.162 | 19.635 | 15.960 | 3.675 | 12.34 | '6 |
| 5 | 5.563 | 5.045 | . 259 | 17.477 | 15.849 | 24.306 | 19.985 | 4.321 | 14.502 | " |
| 6 | 6.625 | 6.065 | . 280 | 20.813 | 19.054 | 34.472 | 28.886 | 5.586 | 18.762 | , |
| 7 | 7.625 | 7.023 | . 301 | 23.955 | 22.063 | 45.664 | 38.743 | 6.921 | 23.271 | " |
| 8 | 8.625 | 7.981 | . 322 | 27.096 | 25.073 | 58.426 | 50.021 | 8.405 | 28.177 | ' |
| 9 | 9.625 | 8.937 | . 344 | 30.238 | 28.076 | 72.760 | 62.722 | 10.04 | 33.701 | . |
| 10 | 10.750 | 10.018 | . 366 | 33.772 | 31.472 | 90.763 | 78.822 | 11.94 | 40.065 | / |
| 11 | 11.750 | 11.000 | . 375 | 36.913 | 34.558 | 108.43 | 95.034 | 13.40 | 45.95 | * |
| 12 | 12.750 | 12.000 | . 375 | 40.055 | 37.699 | 127.68 | 113.09 | 14.59 | 48.985 | " |

[^0]| DiAMETER. |  |  | Thickness. | Circumperence. |  | TRANSVERSE AREAS. |  |  | Nom. Wgt. per ft. lbs. | Threads per In. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Nom. | External. | Internal. |  | External. | Internal. | External. | Internal. | Metal. |  |  |
| 1/8 | .405 | . 205 | .100 | 1.272 | .644 | 129 | . 033 | .096 | 29 | 27 |
| $1 / 4$ | .540 | . 294 | . 123 | 1.696 | . 924 | 229 | . 068 | 161 | 54 | 18 |
| $3 / 8$ | .675 | . 421 | . 127 | 2.121 | 1.323 | . 358 | 139 | . 219 | 74 | 18 |
| 1/2 | 840 | . 542 | . 149 | 2.639 | 1.703 | . 554 | 231 | . 323 | 1.09 | 14 |
| $3 / 4$ | 1.050 | .736 | .157 | 3.299 | 2.312 | . 866 | .425 | . 441 | 1.39 | 14 |
| 1 | 1.315 | .951 | . 182 | 4.131 | 2.988 | 1.358 | .710 | . 648 | 2.17 | 111/2 |
| $11 / 4$ | 1.660 | 1.272 | . 194 | 5.215 | 3.996 | 2.164 | 1.271 | . 893 | 3.00 | $111 / 2$ |
| $11 / 2$ | 1.900 | 1.494 | . 203 | 5.969 | 4.694 | 2.835 | 1.753 | 1.082 | 3.63 | $111 / 2$ |
| 2 | 2.375 | 1.933 | . 221 | 7.461 | 6.073 | 4.430 | 2.935 | 1.495 | 5.02 | $111 / 2$ |
| $21 / 2$ | 2.875 | 2.315 | . 280 | 9.032 | 7. 273 | 6.492 | 4.209 | 2.283 | 7.67 | 8 |
| 3 | 3.500 | 2.892 | . 304 | 10.996 | 9.086 | 9.621 | 6.569 | 3.052 | 10.25 | 66 |
| $31 / 2$ | 4.000 | 3.358 | . 321 | 12.566 | 10.549 | 12.566 | 8.856 | 3.710 | 12.47 | 66 |
| 4 | 4.500 | 3.818 | .341 | 14.137 | 11.995 | 15.904 | 11.449 | 4.455 | 14.97 |  |
| $41 / 2$ | 5.000 | 4.280 | .360 | 15.708 | 13.446 | 19.635 | 14.387 | 5.248 | 18.22 | 68 |
| 5 | 5.563 | 4.813 | .375 | 17.4777 | 15.120 | 24.306 | 18.193 | 6.113 | 20.54 | 6 |
| 6 | 6.625 | 5.751 | . 437 | 20.813 | 18.067 | 34.472 | 25.976 | 8.496 | 28.58 | 6 |
| 7 | 7.625 | 6.625 | .500 | 23.955 | 20.813 | 45.664 | 34.472 | 11.192 | 37.67 | 66 |
| 8 | 8.625 | 7.625 | . 500 | 27.096 | 23.955 | 58.426 | 45.664 | 12.762 | 43.00 | 6 |
| 9 | 9.625 | 8.625 | . 500 | 30.238 | 27.096 | 72. 760 | 58.426 | 14.334 | 48.25 | 6 |
| 10 | 10.750 | 9.750 | .500 | 33.772 | 30.631 | 90.763 | 74.662 | 16.101 | 54.25 | 66 |
| 12 | 12.750 | 11.750 | . 500 | 40.055 | 36.914 | 127.68 | 108.43 | 19.25 | 65.00 | 66 |

NATIONAL TUBE CO.-Standard Double Extra Strong Pipe.

| DiAmeter. |  |  | Thickness. | Circumference. |  | Transverse Areas. |  |  | Nom. Wgt. per ft. lbs. | Threads per In. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Nom. | External. | Internal. |  | External. | Internal. | External. | Internal. | Metal Area. |  |  |
| 1/2 | . 840 | . 244 | . 298 | 2.639 | . 767 | . 554 | . 047 | .507 | 1.7 | 14 |
| 3/4 | 1.050 | . 422 | . 314 | 3.299 | 1.326 | . 866 | . 140 | . 726 | 2.44 | 14 |
| 1 | 1.315 | . 587 | . 364 | 4.131 | 1.844 | 1.358 | . 271 | 1.087 | 3.65 | $111 / 2$ |
| $11 / 4$ | 1.660 | . 885 | . 388 | 5.215 | 2.780 | 2.164 | . 615 | 1.549 | 5.2 | $111 / 2$ |
| $11 / 2$ | 1.900 | 1.088 | . 406 | 5.969 | 3.418 | 2.835 | . 930 | 1.905 | 6.4 | $111 / 2$ |
| 2 | 2.375 | 1.491 | . 442 | 7.461 | 4.684 | 4.430 | 1.744 | 2.686 | 9.02 | $111 / 2$ |
| $21 / 2$ | 2.875 | 1.755 | . 560 | 9.032 | 5.514 | 6.492 | 2.419 | 4.073 | 13.68 | 8 |
| 3 | 3.500 | 2.284 | . 608 | 10.996 | 7.176 | 9.621 | 4.097 | 5.524 | 18.56 | " |
| $31 / 2$ | 4.000 | 2.716 | . 642 | 12.566 | 8.533 | 12.566 | 5.794 | 6.772 | 22.75 | " |
| 4 | 4.500 | 3.136 | . 682 | 14.137 | 9.852 | 15.904 | 7.724 | 8.180 | 27.48 | " |
| $41 / 2$ | 5.000 | 3.564 | . 718 | 15.708 | 11.197 | 19.635 | 9.976 | 9.659 | 32.53 | ${ }^{6} 6$ |
| 5 | 5.568 | 4.063 | . 750 | 17.477 | 12.764 | 24.306 | 12.965 | 11.341 | 38.12 | 6 |
| 6 | 6.625 | 4.875 | . 875 | 20.813 | 15.315 | 34.472 | 18.665 | 15.807 | 53.11 | " 6 |
| 7 | 7.625 | 5.875 | . 875 | 23.955 | 18.457 | 45.664 | 27.109 | 18.555 | 62.38 | " |
| 8 | 8.625 | 6.875 | . 875 | 27.096 | 21.598 | 58.426 | 37.122 | 21.304 | 71.62 | * |

[^1]HEATING SURFACE.

| STANDARD WEIGHT PIPE. Length of Pipe in Ft. per Sq. Ft. of |  |  | EXTRA STRONG PIPE. |  |  | DBLE. EX. STRONG PIPE. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Size. | External | Internal SURFACE. | Size. | EXTERNAL | Internal | Size. | External | Internal Surface. |
|  | 9.44 | 14.2 | 1/8 | 9.44 | 18.63 | 1/2 | 4.55 | 15.67 |
| $1 / 4$ | 7.07 | 10.5 | $1 / 4$ | 7.07 | 12.99 | $3 / 4$ | 3.64 | 9.05 |
| $3 / 8$ | 5.66 | 7.76 | $3 / 8$ | 5.66 | 9.07 |  | 2.90 | 6.51 |
| 1/2 | 4.55 | 6.15 | 1/2 | 4.55 | 7.05 | 11/4 | 2.30 | 4.32 |
| $3 / 4$ | 3.64 | 4.64 | 3, | 3.64 | 5.11 | $11 / 2$ | 2.01 | 3.51 |
|  | 2.90 | 3.66 | $1{ }^{1 / 4}$ | 2.90 | 4.02 | , | 1.61 | 2.56 |
| 11/4 | 2.30 | 2.77 | $11 / 4$ | 2.30 | 3.00 | $21 / 2$ | 1.33 | 2.18 |
| $13 / 2$ | 2.01 | 2.38 | $11 / 2$ | 2.01 | 2.56 | $31 / 2$ | 1.09 | 1.67 |
| 2 | 1.61 | 1.85 | 2 | 1.61 | 1.97 | $31 / 2$ | . 955 | 1.41 |
| $23 / 2$ | 1.33 | 1.55 | 21/2 | 1.33 | 1.65 | 4 | . 849 | 1.22 |
| 3 | 1.09 | 1.25 | 3 | 1.09 | 1.33 | $41 / 2$ | . 764 | 1.07 |
| $31 / 2$ | . 955 | 1.08 | $31 / 2$ | . 955 | 1.14 | 5 | . 687 | . 94 |
| 4 | . 849 | . 949 | 4 | . 849 | 1.00 | 6 | . 577 | . 78 |
| $41 / 2$ | . 764 | . 848 | $41 / 2$ | . 764 | . 893 | 8 | . 501 | . 65 |
| 5 | . 687 | . 757 | 5 | . 687 | . 793 | 8 | . 443 | . 55 |
| 6 | . 577 | . 630 | 6 | . 577 | . 664 | $\ldots$ | $\ldots$ | .... |
| 7 | . 501 | . 544 | 7 | . 501 | . 598 |  | .... |  |
| 8 | . 443 | . 478 | 8 | . 443 | . 502 | $\ldots$ |  |  |
| 9 | . 397 | . 427 | 9 | . 397 | . 443 |  | $\ldots$ |  |
| 10 | . 355 | . 381 | 10 | . 355 | . 399 | $\ldots$ | $\ldots$ |  |
| 11 | . 325 | . 348 |  |  |  |  |  |  |
| 12 | . 299 | . 319 | 12 | 299 | . 325 | .... | $\ldots$ | $\ldots$ | outside of other joint can be secured thereln. The weights are practically the same.

DIAMETER.

| DIAMETER. |  |  | THICKNESS. |  | CIRCUMFERENCE. |  | Transverse Areas. |  |  | Nom. Wgt. per ft. lbs. | Threads per inch. | Nom. Diam. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Nom. | Exter'l\| | Inter'l. | Ins. | S.W.G. | Exter'1 | Inter'l. | Exter'l. | Inter'l. | Metal. |  |  |  |
| 2 | 2.25 | 2.06 | . 095 | 13 | 7.069 | 6.4717 | 3.976 | 3.33 | .643 | 2.22 | 14 | 2 |
| 21/4 | 2.50 | 2.282 | . 109 | 12 | 7.854 | 7. 1691 | 4.909 | 4.090 | 819 | 2.82 | 14 | 21/4 |
| 21/2 | 2.75 | 2.532 | .109 | 12 | 8.639 | 7.9545 | 5.939 | 5.035 | 904 | 3.13 | 14 | 21/2 |
| 23/4 | 3. | 2.782 | . 109 | 12 | 9.425 | 8.7399 | 7.069 | 6.078 | .991 | 3.45 | 14 | 23/4 |
| 3 | 3.25 | 3.01 | . 120 | 11 | 10.210 | 9.4562 | 8.296 | 7.116 | 1.180 | 4.10 | 14 | 3 |
| $31 / 4$ | 3.50 | 3.26 | . 120 | 11 | 10.996 | 10.2416 | 9.621 | 8.347 | 1.274 | 4.45 | 14 | $31 / 4$ |
| 31/2 | 3.75 | 3.51 | .120 | 11 | 11.781 | 11.0270 | 11.045 | 9.676 | 1.369 | 4.78 | 14 | $31 / 2$ |
| 33 | 4. | 3.732 | . 134 | 10 | 12.566 | 11.7244 | 12.566 | 10.940 | 1.626 | 5.56 | 14 | $33 / 4$ |
| 4 | 4.25 | 3.982 | . 134 | 10 | 13.352 | 12.5098 | 14.186 | 12.454 | 1.732 | 6.00 | 14 | 4 |
| 41/4 | 4.50 | 4.218 | . 141 |  | 14.137 | 13.2513 | 15.904 | 13.973 | 1.931 | 6.36 | 14 | 41/4 |
| $41 / 4$ | 4.50 | 4.094 | . 203 | 6 | 14.137 | 12.8617 | 15.904 | 13.163 | 2.741 | 9.38 | 14 |  |
| 41/2 | 4.75 | 4.468 | . 141 |  | 14.923 | 14.0367 | 17.728 | 15.676 | 2.052 | 6.73 | 14 | 41/2 |
| 41/2 | 4.75 | 4.344 | . 203 | 6 | 14.923 | 13.6471 | 17.728 | 14.820 | 2.908 | 9.39 | 14 | 41/2, |
| $43 / 4$ | 5. | 4.704 | . 148 | 9 | 15.708 | 14.7781 | 19.635 | 17.380 | 2.255 | 7. 7.80 | 14 | $43 / 4$ |
| 5 | 5.25 | 4.954 | . 148 | 9 | 16.493 | 15.5634 | 21.648 | 19.275 | 2.373 | 8.20 | 14 | 5 |
| 5 | 5.25 | 4.867 | . 191 |  | 16.493 | 15.2902 | 21.648 | 18.604 | 3.044 | 9.86 | 14 | 5 |
| 5 | 5.25 | 4.753 | . 248 | $31 / 2$ | 16.493 | 14.9320 | 21.648 | 17.743 | 3.905 | 12.80 | 111/2 | 5 |
| 5 | 5.25 | 4.65 | . 300 | 1 | 16.493 | 14.6084 | 21.648 | 16.982 | 4.666 | 15.88 | 111/2 | 5 |
| $5 \frac{3}{16}$ | 5.50 | 5187 | . 156 |  | 17.279 | 16.2955 | 23.758 | 21.131 | 2.627 | 8.62 | 14 | $5 \frac{8}{16}$ |
| 5 | 5.50 | 5.042 | . 229 | 41/2 | 17.279 | 15.8399 | 23.758 | 19.965 | 3.793 | 12.49 | 111/2 | $5 \frac{3}{16}$ |
| $55 / 8$ | 6. | 5.688 | . 156 | , | 18.850 | 17.8694 | 28.274 | $25.40 \%$ | 2.867 | 10.46 | 14 | $55 / 8$ |



National Tube Co. Standard Line Pipe.

|  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 2.375 | . 154 | 3.609 | 111 | 8 | 8.625 | . 281 | 25.00 | 8 |
| 21/2 | 2.875 | . 204 | 5.739 | 8 | 8 | 8.625 | . 322 | 28.177 | 8 |
| 3 | 3.5 | . 217 | 7.536 | 8 | 9 | 9.625 | . 344 | 33.701 | 8 |
| 31/2 | 4. | . 2226 | 9.001 | 8 | 10 | 10.75 | . 2865 | 32.00 | 8 |
| 4 | 4.5 | . 237 | 10.665 | 8 | 10 | 10.75 | . 3145 | 35.00 | 8 |
| 41/2 | 5. | . 246 | 12.49 | 8 | 10 | 10.75 | . 366 | 40.065 | 8 |
| 5 | 5.563 | . 259 | 14.502 | 8 | 12 | 12.75 | . 340 | 45.00 | 8 |
| 6 | 6.625 | . 28 | 18.762 | 8 | 12 | 12.75 | . 375 | 48.985 | 8 |
| 7 | 7.625 | . 301 | 23.271 | 8 |  |  |  |  |  |

National Tube Co. Standard Oil Well Tubing.

|  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 2.375 | . 1725 | 4. | 11 | 41/2 |  | . 246 | 12.49 | 8 |
| 2 | 2.375 | . 1935 | 4.50 | $111 /$ | 5 | 5.563 | . 259 | 14.502 | 8 |
| $21 / 6$ | 2.875 | . 204 | 5.739 | 111\% | 6 | 6.625 | . 28 | 18.76 | 8 |
| $21 / 2$ | 2.875 | . 221 | 6.25 | $111 \%$ | 7 | 7.625 | . 301 | 23.271 | 8 |
| 3 | 3.5 | . 217 | 7.536 | 111/2 | 8 | 8.625 | . 322 | 28.177 | 8 |
| 3 | 3.5 | . 2445 | 8.50 | 1113 | 8 | 8.625 | . 363 | 32.00 | 8 |
| 3 | 3.5 | . 2925 | 10.00 | 111/2 | 9 | 9.625 | . 344 | 33.701 | 8 |
| 31/2 | 4. | . 226 | 9.001 | 8 | 10 | 10.75 | . 366 | 40.065 | 8 |
| 4 | 4.5 | . 237 | 10.665 | 8 | 12 | 12.75 | . 375 | 49.98 | 8 |
| 4 | 4.5 | . 2595 | 11.75 | 8 |  |  |  |  |  |

National Tube Co. Standard Drive Pipe.

|  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 2.375 | . 154 | 3.609 | 111/2 | 6 | 6.625 | . 28 | 18.76 | 8 |
| 21/2 | 2.875 | . 204 | 5.789 | 8 | 7 | 7.625 | . 301 | 23.271 | 8 |
| 3 | 3.5 | . 217 | 7.536 | 8 | 8 | 8.625 | . 322 | 28.177 | 8 |
| 31/2 | 4. | . 226 | 9.001 | 8 | 9 | 9.625 | . 344 | 33.701 | 8 |
| 4 | 4.5 | . 237 | 10.665 | 8 | 10 | 10.75 | . 366 | 40.065 | 8 |
| 4112 |  | . 246 | 12.49 | 8 | 12 | 12.75 | . 375 | 49.98 | 8 |
| 5 | 5.563 | . 259 | 14.502 | 8 |  |  |  |  |  |

NATIONAL TUBE COMPANY.
Thickness of Metal Required for Flush Joint Pipe and Tubing.

| SIZE. | 5 Inch Pipe. | $\left\|\begin{array}{c}5 \text { Inch } \\ \text { Extern'l } \\ \text { Diame- } \\ \text { ter. }\end{array}\right\|$ | 6 Inch Pipe. | $\left\|\begin{array}{c}6 \text { Inch } \\ \text { Extern'l } \\ \text { Diame- } \\ \text { ter. }\end{array}\right\|$ | $\begin{aligned} & 7 \text { Inch } \\ & \text { Pipe. } \end{aligned}$ | $\left\|\begin{array}{c}7 \text { Inch } \\ \text { Extern'l } \\ \text { Diame- } \\ \text { ter. }\end{array}\right\|$ | 8 Inch Pipe. | 8 Inch Extern'l Diameter. | 9 Inch Pipe. | 9 Inch <br> Extern'l <br> Diame- <br> ter. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Thickness of Metal, inches | 1/4 | $1 / 4$ | $\frac{9}{32}$ | $\frac{9}{32}$ | ${ }_{1}^{5} 6$ | ${ }_{1}^{5}$ | $\frac{1}{3} \frac{1}{2}$ | $\frac{1}{3} \frac{1}{2}$ | $\frac{1}{3} \frac{1}{2}$ | $\frac{1}{3} \frac{1}{2}$ |
| SIZE. | 10 Inch | $\left\|\begin{array}{c}10 \text { Inch } \\ \text { Extern'l } \\ \text { Diame- } \\ \text { ter. }\end{array}\right\|$ | 11 Inch | $\left\|\begin{array}{c}11 \text { Inch } \\ \text { Fxtern'l } \\ \text { Diame- } \\ \text { ter. }\end{array}\right\|$ | 12 Inch Pipe. | $\left\|\begin{array}{c}12 \text { Inch } \\ \text { Extern'l } \\ \text { Diame- } \\ \text { ter. }\end{array}\right\|$ | 13 Inch Extern'l Diameter. | 14 Inch Extern'l Diame- ter. | 15 Inch Extern'l Diame- ter. |  |
| Thickness of Metal, inches | 9/8 | 3/8. | 3/8 | 9/8 | 9/8 | 9/8 | $\frac{13}{2}$ | $\frac{1}{3} \frac{3}{2}$ | $\frac{13}{3}$ |  |

Nominal Weight in Pounds per Foot of Standard Thicknesses of Large Sizes O. D. Pipe.

| O. D. | 1/4 in. thick | $\frac{5}{58}$ in. thick | 38 in . thick | Is in. thick | 12 in. thick | $\frac{16}{16}$ in. thick | 5/8 in. thick | \% in. thick | $3 / 4$ in. thick |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 14 inches | 36.75 | 45.72 | 54.61 | 63.42 | 72.16 | 80.80 | 89.36 | 97.84 | 106.2 |
| 15 * | 39.42 | 49.06 | 58.62 | 68.10 | 77.50 | 86.81 | 96.03 | 105.2 | 114.2 |
| 16 6 | 42.09 | 52.40 | 62.63 | 72.78 | 82,85 | 92.83 | 102.7 | 112.5 | 122.2 |
| 17 " | 44.76 | 55.74 | 66.64 | 77.46 | 88.19 | 98.84 | 109.4 | 119.9 | 130.3 |
| 18 6 | 47.44 | 59.08 | 70.65 | 82.14 | 93.54 | 104.8 | 116.1 | 127.2 | 138.3 |
| 20 | 52.78 | 65.76 | 78.67 | 91.49 | 104.2 | 116.9 | 129.4 | 141.9 | 154.3 |
| 21 6 | 55.45 | 69.10 | 82.68 | 96.17 | 109.6 | 122.9 | 136.1 | 149.3 | 162.3 |
| 22 " |  | 7244 | 86.68 | 100.8 | 114.9 | 128.9 | 142.8 | 156.6 | 170.3 |
| 24.4 |  | 79.13 | 94.70 | 110.2 | 125.6 | 140.9 | 156.2 | 171.3 | 186.3 |
| 26 : |  |  | 102.7 | 119.5 | 136.3 | 152.9 | 169.5 | 186.0 | 202.4 |
| 28 4 |  |  | 110.7 | 128.9 | 147.0 | 165.0 | 182.9 | 200.7 | 218.4 |
| 30 4 | -..... | **** | -.... | 138.2 | 157.7 | 177.0 | 196.3 | 215.4 | 234.4 |

NATIONAL TUBE CO,-Standard Boiler Tubes.

| Diameter. |  | Thickness. |  | Circumference. |  | Transverse Areas. |  |  | Length of Tube Per Square Ft. |  | Nom. Wgt. per ft. lbs. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| O. D. | I. D. | Ins. | Nearest B.W.G. | External. | Internal. | External. | Internal. | Metal. | Ex. Surf. | In. Surf. |  |
| 1 | . 810 | . 095 | 13 | 3.142 | 2.545 | . 7854 | .5153 | . 2701 | 3.819 | 4.715 | . 90 |
| $11 / 4$ | 1.060 | . 095 | 13 | 3.927 | 3.330 | 1.2272 | . 8825 | . 3447 | 3.056 | 3.603 | 1.15 |
| 11/2 | 1.310 | . 095 | 13 | 4.712 | 4.115 | 1.7671 | 1.3478 | . 4193 | 2.547 | 2.916 | 1.40 |
| 13/4 | 1.560 | . 095 | 13 | 5.498 | 4.901 | 2.4053 | 1.9113 | . 4940 | 2.183 | 2.448 | 1.66 |
| 2 | 1.810 | . 095 | 13 | 6.283 | 5.686 | 3.1416 | 2.5730 | . 5686 | 1.909 | 2.110 | 1.91 |
| 21/4 | 2.060 | . 095 | 13 | 7.069 | 6.472 | 3.9761 | 3.3329 | . 6432 | 1.698 | 1.854 | 2.16 |
| $21 / 2$ | 2.282 | . 109 | 12 | 7.854 | 7.169 | 4.9087 | 4.0899 | . 8188 | 1.528 | 1.674 | 2.75 |
| 23/4 | 2.532 | . 109 | 12 | 8.639 | 7.954 | 5.9396 | 5.0349 | . 9047 | 1.389 | 1.508 | 3.04 |
| 3 | 2.782 | . 109 | 12 | 9.425 | 8.740 | 7.0686 | 6.0787 | . 9899 | 1.273 | 1.373 | 3.33 |
| $31 / 4$ | 3.010 | . 120 | 11 | 10.210 | 9.456 | 8.2958 | 7.1157 | 1.1801 | 1.175 | 1.269 | 3.96 |
| $31 / 2$ | 3.260 | . 120 | 11 | 10.996 | 10.242 | 9.6211 | 8.3469 | 1.274 | 1.091 | 1.171 | 4.28 |
| $33 / 4$ | 3.510 | . 120 | 11 | 11.781 | 11.027 | 11.045 | 9.6762 | 1.369 | 1.018 | 1.088 | 4.6 |
| 4 | 3.732 | . 134 | 10 | 12.566 | 11.724 | 12.566 | 10.939 | 1.627 | . 955 | 1.024 | 5.47 |
| 41/2 | 4.232 | . 134 | 10 | 14.137 | 13.295 | 15.904 | 14.066 | 1.838 | . 849 | . 902 | 6.17 |
| 5 | 4.704 | . 148 | 9 | 15.708 | 14.778 | 19.635 | 17.379 | 2.256 | . 764 | . 812 | 7.58 |
| 6 | 5.670 | . 165 | 8 | 18.850 | 17.813 | 28.274 | 25.249 | 3.025 | . 637 | 673 | 10.16 |
| 7 | 6.670 | . 165 | 8 | 21.991 | 20.954 | 38.485 | 34.941 | 3.544 | . 546 | .573 | 11.9 |

NATIONAL TUBE CO.-Standard Boiler Tubes.

| DIAMETER. |  | Thickness. |  | Circumperence. |  | Transverse Areas. |  |  | Length of Tube Per Square Ft. |  | Nom. Wgt. per ft. lbs. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| O. D. | I. D. | Ins. | Nearest <br> B. W.G. | External. | Internal. | External. | Internal. | Metal. | Ex. Surf. | In. Surf. |  |
| 8 | 7.670 | . 165 | 8 | 25.133 | 24.096 | 50.265 | 46.204 | 4.061 | . 477 | . 498 | 13.65 |
| 9 | 8.640 | . 180 | 7 | 28.274 | 27.143 | 63.617 | 58.629 | 4.988 | . 424 | . 442 | 16.76 |
| 10 | 9.594 | . 203 | 6 | 31.416 | 30.140 | 78.540 | 72.291 | 6.249 | . 382 | . 398 | 21.00 |
| 11 | 10.560 | . 220 | 5 | 34.558 | 33.175 | 95.033 | 87.582 | 7.451 | .347 | . 362 | 25.00 |
| 12 | 11.542 | . 229 | 41/2 | 37.699 | 36.260 | 113.10 | 104.63 | 8.47 | .319 | . 330 | 28.50 |
| 13 | 12.524 | . 238 | 4 | 40.841 | 39.345 | 132.73 | 123.19 | 9.54 | .294 | .305 | 32.06 |
| 14 | 13.594 | . 248 | $31 / 2$ | 43.982 | 42.424 | 153.94 | 143.22 | 10.72 | . 273 | . 283 | 36.00 |
| 15 | 14.482 | . 259 | 3 | 47.124 | 45.496 | 176.71 | 164.72 | 11.99 | . 254 | . 264 | 40.60 |
| 16 | 15.460 | . 270 | 21/2 | 50.265 | 48.569 | 201.06 | 187.71 | 13.35 | . 239 | . 247 | 45.20 53.00 |
| 18 | 17.432 | . 284 | 2 | 56.549 | 54.764 | 254.47 | 238.66 | 15.81 | . 212 | . 219 | 53.00 |
| 20 | 19.376 | . 312 | 1 | 62.832 | 60.872 | 314.16 | 294.86 | 19.30 | . 190 | .197 | 65.00 |
| 22 | 21.314 | . 343 | 0 | 69.115 | 66.960 | 380.13 | 356.80 | 23.33 | . 173 | .179 | 78.00 |
| 24 | 23.25 | . 375 | 00 | 75.398 | 73.042 | 452.39 | 424.56 | 27.83 | . 159 | .164 | 93.00 |
| 26 | 25.25 | . 375 | 00 | 81.681 | 79.325 | 530.93 | 500.74 | 30.19 | . 147 | . 151 | 101.00 |
| 28 | 27.25 | . 375 | 00 | 87.965 | 85.608 | 615.75 | 583.21 | 32.54 | . 136 | . 140 | 109.00 |
| 30 | 29.25 | . 375 | 00 | 94.248 | 91.892 | 706.86 | 671.96 | 34.90 | . 127 | . 130 | 117.00 |

[^2]Cannot cut to length closer than $\frac{1}{18}$ inch.


| DIAMETER. |  | Thickness. |  | Circumference. |  | Transverse Areas. |  |  | LengTh of TUBE Per Square Ft. |  | Nom. Wgt. per ft. lbs. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ext. | Internal | Dec. | B. W.G. | External. | Internal. | External. | Internal. | Metal. | Ex. Surf. | In. Surf. |  |
| 11/8 | . 935 | . 095 | 13 | 3.534 | 2.937 | . 9940 | . 6866 | . 3074 | 3.395 | 4.085 | 1.04 |
| $1{ }^{1} 8$ | 1.122 | . 095 | 13 | 4.123 | 3.526 | 1.3530 | . 9896 | . 3634 | 2.910 | 3.403 | 1.22 |
| $13 / 8$ | 1.185 | . 095 | 13 | 4.320 | 3.723 | 1.4849 | 1.1029 | . 3820 | 2.778 | 3.223 | 1.29 |
| 158 | 1.435 | . 095 | 13 | 5.105 | 4.508 | 2.0739 | 1.6173 | . 4566 | 2.351 | 2.662 | 1.53 |
| 17/8 | 1.685 | . 095 | 13 | 5.890 | 5.294 | 2.7612 | 2.2299 | . 5313 | 2.037 | 2.266 | 1.78 |
| 21/8 | 1.935 | . 095 | 13 | 6.676 | 6.079 | 3.5466 | $2.940{ }^{7}$ | . 6059 | 1.797 | 1.974 | 2.04 |
| 23/8 | 2.185 | . 095 | 13 | 7.461 | 6.864 | 4.4301 | 3.7497 | . 6804 | 1.608 | 1.748 | 2.30 |
| 27/8 | 2.657 | . 109 | 12 | 9.032 | 8.347 | 6.4918 | 5.5446 | . 94772 | 1.328 | 1.439 | 3.18 |
| $41 / 4$ | 3.982 | . 134 | 10 | 13.352 | 12.51 | 14.186 | 12.453 | 1.733 | .899 | . 959 | 5.82 |
| $43 / 4$ | 4.482 | . 134 | 10 | 14.923 | 14.081 | 17.728 | 15.777 | 1.951 | . 804 | . 852 | 6.53 7 7.97 |
| $51 / 4$ | 4.954 | . 148 | 9 | 16.493 | 15.563 | 21.648 | 19.275 | 2.373 2.488 | .728 .694 | .771 .734 | 7.97 8.36 |
| $51 / 2$ | 5.204 | . 148 | 9 | 17.279 | 16.349 | 23.758 | 21.270 | 2.488 | . 694 | . 734 | 8.36 |

[^3]NATIONAL TUBE COMPANY.
NATIONAL TUBE CO.-Bedstead Tubing.


## STANDARD DIMENSIONS OF COUPLINGS

FOR

## STEAM, GAS AND WATER PIPE,

BLACK AND GALVANIZED.

| Size of Pipe. Nominal Inside Diameter | Inside Diameter of Coupling | Outside Diameter of Coupling | $\begin{aligned} & \text { Length } \\ & \text { of } \\ & \text { Coupling } \end{aligned}$ | Thread per Inch of Screw. | Average Weight of Coupling in Pounds. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Inches. | Inches. | Inches. | Inches. |  |  |
| 1/8 | $\frac{11}{32}$ | $\frac{1}{3} \frac{9}{2}$ | $\frac{1}{1} \frac{3}{6}$ | 27 | . 031 |
| $1 / 4$ | $\frac{1}{8} \frac{5}{2}$ | $\frac{23}{3}$ | $\frac{1}{1} \frac{5}{6}$ | 18 | . 046 |
| $3 / 8$ | $\frac{87}{64}$ | $\frac{27}{32}$ | $1 \frac{1}{16}$ | 18 | . 078 |
| 1/2 | $\frac{23}{32}$ | 1 | $1 \frac{5}{16}$ | 14 | . 124 |
| $3 / 4$ | $\frac{63}{6}$ | $1 \frac{21}{64}$ | 116 | 14 | . 250 |
| 1 | $1 \frac{11}{4}$ | $1 \frac{9}{16}$ | $1 \frac{18}{16}$ | $111 / 2$ | . 455 |
| 11/4 | $11 / 2$ | $16 \frac{1}{4}$ | $21 / 8$ | $111 / 2$ | . 562 |
| $11 / 2$ | 13/4 | $2 \frac{7}{38}$ | 23/8 | $111 / 2$ | . 800 |
| 2 | $2 \frac{7}{82}$ | 23/4 | 25/8 | $111 / 2$ | 1.250 |
| $21 / 2$ | $2 \frac{21}{2}$ | $3{ }^{9} 2$ | 27/8 | 8 | 1.757 |
| 3 | $31 / 4$ | $3 \frac{1}{1} \frac{5}{6}$ | $31 / 8$ | 8 | 2.625 |
| $31 / 2$ | $3 \frac{25}{32}$ | $4{ }_{16}^{7}$ | $35 / 8$ | 8 | 4.000 |
| 4 | $4 \frac{1}{6} \frac{7}{4}$ | 5 | $35 / 8$ | 8 | 4.125 |
| $41 / 2$ | $43 / 4$ | $51 / 2$ | $35 / 8$ | 8 | 4.875 |
| 5 | $5 \frac{9}{32}$ | $6 \frac{7}{82}$ | 41/8 | 8 | 8.437 |
| 6 | $6 \frac{11}{32}$ | $7{ }^{7} 6$ | $41 / 8$ | 8 | 10.625 |
| 7 | $73 / 8$ | $8{ }_{16}{ }^{\frac{5}{6}}$ | $41 / 8$ | 8 | 11.270 |
| 8 | $83 / 8$ | $9{ }_{1}^{56}$ | $45 / 8$ | 8 | 15.150 |
| 9 | $9{ }_{1}^{7}{ }^{7}$ | 103/8 | $51 / 8$ | 8 | 17.820 |
| 10 | $10 \frac{7}{16}$ | $11 \frac{21}{82}$ | $61 / 8$ | 8 | 27.700 |
| 11 | $11 \frac{15}{3}$ | $12 \frac{2}{8} \frac{1}{2}$ | $61 / 8$ | 8 | 33.250 |
| 12 | $12^{7}{ }^{7}$ | $137 / 8$ | $61 / 8$ | 8 | 43.187 |
| 13 | $13 \frac{1}{1} \frac{1}{6}$ | $15^{\frac{1}{16}}$ | $61 / 8$ | 8 | 49.280 |
| 14 | $14 \frac{28}{32}$ | $163 / 8$ | $61 / 8$ | 8 | 63.270 |
| 15 | $15 \frac{11}{16}$ | 173/8 | $61 / 8$ | 8 | 66.000 |

# STANDARD DIMENSIONS OF COUPLINGS 

FOR

## REGULAR CASING.

| Size of Casing. Nominal Inside Diameter | Inside Diameter of Coupling | Outside Diameter of Coupling | $\begin{gathered} \text { Length } \\ \text { of } \\ \text { Coupling } \end{gathered}$ | Thread per Inch of Screw. | Average Weight Coupling in Lbs. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Inches. | Inches. | Inches. | Inches. |  |  |
| $13 / 4$ | $17 / 8$ | $2{ }^{\frac{5}{6}}$ | $23 / 8$ | 14 | . 90 |
| 2 | $2{ }^{74}$ | $2{ }^{\frac{2}{3} \frac{5}{8}}$ | 25/8 | 14 | 1.31 |
| $21 / 4$ | $2{ }^{\frac{11}{82}}$ | $2 \frac{2}{32}$ | 25/8 | 14 | 1.50 |
| $21 / 2$ | $2 \frac{19}{3}$ | $3{ }^{\frac{5}{3}}$ | 25/8 | 14 | 1.62 |
| 23/4 | $2{ }^{2 \frac{27}{8}}$ | $318{ }^{\frac{1}{2}}$ | 25/8 | 14 | 1.75 |
| 3 | $3{ }^{\frac{3}{8}}$ | $33 / 4$ | $31 / 8$ | 14 | 2.62 |
| $31 / 4$ | $3 \frac{11}{33^{2}}$ | 4 | $31 / 8$ | 14 | 2.87 |
| $31 / 2$ | $3{ }^{\frac{10}{10}{ }^{\frac{2}{2}} \text { ( }}$ | $41 / 4$ | $31 / 8$ | 14 | 3.06 |
| $33 / 4$ | $3 \frac{3}{3 \frac{3}{2}}$ | $41 / 2$ | $31 / 8$ | 14 | 2.25 |
| 4 | $4{ }_{1}^{16}$ | $4{ }^{\frac{2}{8}}$ | $35 / 8$ | 14 | 3.62 |
| 41/4 | $43 / 8$ | $5{ }^{\text {a }}$ | 35\% | 14 | 3.93 |
| $41 / 2$ | $4 \frac{1}{3}$ 星 | $5 \frac{7}{8 \frac{7}{2}}$ | 358 | 14 | 4.06 |
| 43/4 | $4 \frac{15}{18}$ | $5 \frac{15}{8 \frac{5}{8}}$ | 358 | 14 | 4.93 |
| 5 | $5^{\frac{186}{64}}$ | $5 \frac{18}{18}$ | $41 / 8$ | 14 \& 111/2 | 5.68 |
| $5 \frac{3}{16}$ | $5^{\frac{6}{18}}$ | $61 \frac{1}{12}$ | $41 / 8$ | 14 \& $1111 / 2$ | 5.93 |
| 55\% | $5 \frac{15}{65}$ | 65\% | $41 / 8$ | 14 \& 111/2 | 6.37 |
| 61/4 | $6 \frac{18}{6}$ | $7 \frac{6}{82}$ | $41 / 8$ | 14 \& 111/2 | 7.93 |
| 65/8 | ${ }_{65}^{65}$ | 758 | 458 | 14 \& 111/2 | 9.68 |
| $71 / 4$ | ${ }^{7} \frac{1}{65}$ | $81 / 4$ | 45/8 | 14 \& $111 / 2$ | 9.93 |
| 75/8 | $7{ }^{\frac{8}{85}{ }^{\frac{8}{2}} 8}$ | $8 \frac{83}{38}$ | $51 / 8$ | $111 / 2$ | 14.00 |
| 81/4 | $8 \frac{8}{8 \frac{8}{2}}$ | $93 / 8$ | $51 / 8$ | $111 / 2$ | 15.37 |
| 85/8 |  | $93 / 4$ | $51 / 8$ | $111 / 2$ | 15.93 |
| $95 / 8$ | $93 / 4$ | $10 \frac{25}{82}$ | $61 / 8$ | $111 / 2$ | 24.60 |
| $101 / 4$ | $101 / 2$ | $111 / 2$ | $61 / 8$ | $111 / 2$ | 26.00 |
| $105 / 8$ | $10 \frac{2}{85}$ | $117 / 8$ | $61 / 8$ | $111 / 2$ | 27.83 |
| 115/8 | $11{ }^{\frac{8}{3} \frac{8}{8} \text { 5 }}$ | 127/8 | $61 / 8$ | $111 / 2$ | 29.75 |
| $121 / 2$ | $12{ }^{\frac{5}{8} \frac{5}{8}}$ | 14 | $61 / 8$ | $111 / 2$ | 35.00 |
| $131 / 2$ | $13{ }^{\frac{8}{8} \text { \% }}$ | 15 | $61 / 8$ | $111 / 2$ | 42.50 |
| $141 / 2$ | $14{ }^{3} / 4$ | $161 / 8$ | $61 / 8$ | $111 / 2$ | 50.00 |
| 151/2 | $153 / 4$ | 171/8 | $61 / 8$ | $111 / 2$ | 52.50 |

## STANDARD DIMENSIONS OF COUPLINGS

FOR
LINE PIPE.

| Size of Pipe, Nominal Inside Diameter | $\left\lvert\, \begin{gathered} \text { Inside } \\ \text { Diameter } \\ \text { of } \\ \text { Coupling } \end{gathered}\right.$ | Outside Diameter of Coupling | $\left\lvert\, \begin{gathered} \text { Length } \\ \text { of } \\ \text { of } \end{gathered}\right.$ | Thread per Inch of Screw. | Average Weight of Coupling in Pounds. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Inches. | Inches. | Inches. | Inches. |  |  |
| $1 / 4$ | $\frac{15}{82}$ | $\frac{51}{64}$ | $1{ }_{18}{ }^{\frac{5}{6}}$ | 18 | . 06 |
| 3/8 | $\frac{37}{64}$ | $\frac{31}{32}$ | 15/8 | 18 | . 17 |
| 1/2 | $\frac{23}{32}$ | $1 \frac{5}{38}$ | $1 \frac{1}{1} \frac{8}{6}$ | 14 | . 29 |
| 3/4 | $\frac{15}{16}$ | $13 / 8$ | $2 \frac{1}{16}$ | 14 | . 41 |
| 1 | $1 \frac{11}{64}$ | 15/8 | $2{ }^{\frac{5}{16}}$ | $111 / 2$ | . 64 |
| 11/4 | $11 / 2$ | $21 / 8$ | $2 \frac{18}{3}$ | $111 / 2$ | 1.10 |
| $11 / 2$ | $1 \frac{23}{32}$ | $2 \frac{9}{32}$ | $2 \frac{13}{16}$ | $111 / 2$ | 1.18 |
| 2 | $2{ }^{\frac{5}{82}}$ | 27/8 | 33/4 | $111 / 2$ | 2.50 |
| $21 / 2$ | $2 \frac{19}{88}$ | $3{ }_{1}^{76}$ | 33/4 | 8 | 3.12 |
| 3 | $3 \frac{7}{88}$ | $4 \frac{1}{16}$ | $33 / 4$ | 8 | 3.85 |
| $31 / 2$ | 33/4 | $4 \frac{23}{32}$ | $4 \frac{8}{16}$ | 8 | 5.00 |
| 4 | $4{ }^{\frac{7}{8}}$ | $5 \frac{8}{16}$ | $4 \frac{3}{16}$ | 8 | 6.50 |
| $41 / 2$ | $4 \frac{23}{3}$ | 55/8 | $4 \frac{8}{16}$ | 8 | 7.70 |
| 5 | 51/4 | $6{ }_{16}^{5}$ | 51/8 | 8 | 11.21 |
| 6 | $6 \frac{5}{16}$ | $7 \frac{18}{8 \frac{1}{2}}$ | $51 / 8$ | 8 | 12.00 |
| 7 | $7 \frac{11}{8 \frac{1}{2}}$ | $8 \frac{15}{3}$ | $61 / 8$ | 8 | 14.75 |
| 8 | $8 \frac{11}{8 \frac{1}{2}}$ | 99 | $51 / 8$ | 8 | 23.25 |
| 9 | 911 ${ }^{18}$ | $10 \frac{9}{16}$ | $61 / 8$ | 8 | 26.48 |
| 10 | 103/8 | 11111 | $61 / 8$ | 8 | 29.50 |
| 11 | 113/8 | $12 \frac{11}{16}$ | $61 / 8$ | 8 | 34.75 |
| 12 | $12{ }^{7} 7$ | 137/8 | $61 / 8$ | 8 | 39.50 |
| 13 | $13 \frac{11}{16}$ | $15 \frac{1}{16}$ | $61 / 8$ | 8 | 46.00 |
| 14 | $14 \frac{2}{8} \frac{3}{8}$ | $16 \frac{5}{16}$ | $61 / 8$ | 8 | 59.75 |
| 15 | $15 \frac{11}{16}$ | $171 / 4$ | $61 / 8$ | 8 | 62.25 |

## STANDARD DIMENSIONS OF COUPLINGS

FOR DRIVE PIPE.

| Size of <br> Pipe <br> Nominal <br> Inside | Inside <br> Diameter <br> Diameter <br> of <br> Ooupling | Outside <br> Diameter <br> of <br> oupling | Length <br> of <br> of <br> Coupling | Thread <br> per Inch of <br> Screw. | Average <br> Weight of <br> Coupling |
| :---: | :---: | :---: | :---: | :---: | :---: |
| in Pounds. |  |  |  |  |  |

STANDARD DIMENSIONS OF COUPLINGS
FOR
TUBING.

| Size of Tube Nominal Inside Diameter | Inside Diameter of Coupling | Outside <br> Diameter of <br> Coupling | Length of Coupling | Thread per Inch of Screw. | Average Weight of Coupling in Pounds. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Inches. | Inches. | Inches. | Inches. |  |  |
| $11 / 4$ | $11 / 1{ }^{2}$ | $21 / 8$ |  |  |  |
| $2_{2}^{112}$ | 123 238 285 |  | 2013 | $111 / 9$ | 1.18 2.50 |
| $21 / 2$ | 23 23 23 23 | 2188 | 334 | $111 /$ | 3.12 |
| 3 | - $3 \frac{3}{7}$ | $4{ }^{18}$ | 334 | 111/2 | 3.85 |
| 31/2 | $3{ }^{8}$ | $4{ }^{13}$ | $4{ }^{16}$ | 8 | 5.09 |
| 4 | $4{ }^{\frac{7}{37}}$ | $5{ }^{\frac{3}{3}}$ | $4{ }^{16}$ | 8 | 6.50 |
| 41/83 | $4{ }^{\frac{3}{23}}$ | $55 \%$ | $4{ }^{\frac{185}{15}}$ | 8 | 7.70 |
| 5 | $51 / 4$ | ${ }^{6}{ }^{\frac{8}{6}}$ | $51 / 8$ | 8 | 1121 |
| 6 | $6_{16}^{5}$ | $7 \frac{1}{3} \frac{3}{2}$ | 51/8 | 8 | 12.00 |




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LAP-WELDED PIPE FIT'TED WITH CAST IRON COLLAR FLANGES.

Complete.
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SPECIAL LIGET LAP-WELDED PIPE Fitted with Cast Iron Lugged Flanges.

LAP-WELDED PIPE
Fitted with Cast Iron Collar Flanges.


LAP-WELDED PIPE
Fitted with Cast Iron Double Riveted Flanges.


LAP-WELDED PUMP COLUMNS
Fitted with Cast Iron Lugged Pump Column Flange.


LAP-WELDED PIPE
Fitted with Cast Iron Single Riveted Flanges.


Fitted with Solid Welded Flanges.



| Pipe Size. | Outside <br> Diameter <br> of Flange | Thickness of Face. | $\begin{gathered} \text { Number } \\ \text { of } \\ \text { ofts. } \end{gathered}$ | Size of Bolts. | Bolt Hole Circle. | Weight per Pair in Lbs. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Inches. <br> 2 | Inches. 6 | Inches. 5/8 | 4 | Inches. | Inches. 43/4 | 8 |
| $21 / 2$ | 7 | $\frac{11}{1} 8$ | 4 | 1/2 | $51 / 2$ | 12 |
| 3 | $71 / 2$ | 3/4 | 4 | 1/2 | 6 | 14 |
| $31 / 2$ | $81 / 2$ | $\frac{1}{18}$ | 4 | 1/2 | 7 | 20 |
| 4 | 9 | $\frac{1}{15}$ | 4 | 5/8 | $71 / 2$ | 24 |
| $41 / 2$ | 91/4 | $\frac{15}{15}$ | 8 | 5/8 | 73/4 | 25 |
| 5 | 10 | $\frac{1}{15}$ | -8 | 5/8 | $81 / 2$ | 30 |
| 6 | 11 | 1 | 8 | 5/8 | $91 / 2$ | 34 |
| 7 | 121/2 | $1 \frac{1}{16}$ | 8 | 5/8 | 103/4 | 46 |
| 8 | $131 / 2$ | $11 / 8$ | 8 | 5/8 | 113/4 | 54 |
| 9 | 15 | $11 / 8$ | 12 | 5/8 | 131/4 | 66 |
| 10 | 16 | $1{ }_{1}{ }^{\frac{8}{6}}$ | 12 | $3 / 4$ | 141/4 | 74 |
| 12 | 19 | 11/4 | 12 | $3 / 4$ | 17 | 112 |
| 14 o.d. | 21 | $13 / 8$ | 12 | 7/8 | 183/4 | 147 |
| 15 " | 221/4 | $13 / 8$ | 16 | 7/8 | 20 | 162 |

## SPECIAL

## Steel Lap-Welded Pipe,

FITTED WITH
CONVERSE PATENT LOCK JOINT. (Cast Iron Hub.)


SILVERTIN.

Size.
APPROXIMATE, WEIGHT.

| O. D. <br> Inches. | Nearest B'g'm Wire Gauge. | Plain Ends, per foot. lbs. | Hub. lbs. | Lead, one side. lbs. | Complete, per foot. lbs. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 13 | 1.91 | 5 | 1 | 2.00 |
| 3 | 12 | 3.33 | 9 | 2 | 3.94 |
| 4 | 11 | 4.89 | 14 | $21 / 2$ | 5.81 |
| 5 | 10 | 6.85 | 19 | 3 | 8.02 |
| 6 | 10 | 8.26 | 21 | 4 | 9.65 |
| 7 | 9 | 10.65 | 32 | $51 / 2$ | 12.74 |
| 8 | 9 | 12.21 | 35 | 7 | 14.54 |
| 9 | $81 / 2$ | 14.58 | $371 / 2$ | $71 / 2$ | 17.08 |
| 10 | 81/2 | 16.18 | 41 | 8 | 18.90 |
| 12 | 7 | 22.35 | 58 | 10 | 26.13 |
| 14 | 7 | 25.25 | 73 | 12 | 30.00 |
| 15 | $61 / 2$ | 30.00 | 85 | 15 | 36.40 |
| 16 | 5 | 39.60 | 132 | $171 / 2$ | 46.25 |
| 18 | 1/4" | 47.00 | 149 | 30 | 56.25 |
| 20 | 5 ${ }^{16}$ | 65.15 | 217 | 38 | 78.50 |
| 22 | $\frac{11}{82}{ }^{\prime \prime}$ | 78.50 | 280 | 50 | 96.00 |
| 24 | $3{ }^{\prime \prime}$ | 93.50 | 342 | $581 / 2$ | 114.50 |
| 26 | $3 / 8{ }^{\prime \prime}$ | 102.00 | 380 | 70 | 138.00 |
| 28 | $3 / 8$ " | 110.00 | 430 | 85 | 151.00 |
| 30 | $7^{7 \prime \prime}$ | 136.60 | 475 | 100 | 168.60 |

## WEIGHTS OF FITTINGS.

## Converse Joint.

As a matter of convenience and to give an idea of the average weight of Converse Patent Lock Joint Fittings, we submit the following list of a few standard patterns.

All ends are Converse Lock Bells, except where otherwise stated. Bell connections for cast iron pipe are indicated by an asterisk (*) ; bell connections for threaded pipe, by a single dagger ( $\dagger$ ).

REDUCING TEES.

| Size. | $\left\|\begin{array}{c} \text { Weight } \\ \text { lbs. } \end{array}\right\|$ | Size. | $\begin{gathered} \text { Weight } \\ \text { 1bs. } \end{gathered}$ | Size. | $\begin{gathered} \text { Weight } \\ \text { lbs. } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3×2x2 | 34 | 6x5x5 | 81 | $14 \times 14 \times 10$ |  |
| $3 \times 2 \mathrm{x} 3$ | 30 | $6 \times 6 \times 5$ | 97 | $14 \times 14 \times 12$ |  |
| $3 \times 3 \times 2$ | 36 | $7 \times 4 \times 7$ |  | 16x16x 4 | 330 |
| 3x4x3 | 35 | $7 \times 7 \times 4$ | 81 | 16x16x 6 | 355 |
| $4 \times 2 \times 4$ | 43 | $7 \times 5 \times 7$ |  | 16x16x 8 |  |
| $4 \times 3 \times 2$ | 39 | $7 \times 7 \times 5$ | $\ldots$ | 16x16x10 |  |
| $4 \times 4 \times 2$ | 35 | $7 \times 6 \times 7$ | ... | 16x16x12 |  |
| $4 \times 3 \times 4$ | 36 | 7x7x6 | ... | 16x16x14 |  |
| $4 \times 4 \times 3$ | 37 | 7x6x6 |  | 18x18x 6 |  |
| $4 \times 3 \times 3$ | 40 | $8 \times 4 \times 8$ | 107 | 18x18x10 |  |
| $4 \times 4 \times 6$ | 55 | $8 \times 8 \times 4$ | 91 | 18x18x12 |  |
| $5 \times 3 \times 5$ |  | $8 \mathrm{x} 5 \times 8$ | 117 | 18x $18 \times 16$ |  |
| 5x5x3 | 57 | 8 x 8 x 5 | 118 | 20x20x 6 |  |
| $5 \times 4 \times 5$ |  | $8 \times 6 \times 5$ | 100 | $20 \times 20 \times 8$ | 640 |
| 5x5x4 | 60 | $8 \times 6 \times 8$ | 103 | $20 \times 20 \times 10$ |  |
| 5x5x6 | 70 | $8 \times 8 \times 6$ | 97 | $20 \times 20 \times 12$ |  |
| 6x3x3 | 60 | $8 \times 6 \times 6$ | 87 | 20x20x14 |  |
| 6x3x6 | 60 | 10x10x4 | 118 | 20x20x16 |  |
| 6x4x5 | 76 | 10x10x5 |  | $24 \times 24 \mathrm{x} 6$ |  |
| 6x4x6 | 68 | 10x6x 10 |  | $24 \times 24 \mathrm{x} 8$ |  |
| 6x6x3 | 59 | 10x10x6 | 141 | $24 \times 24 \times 10$ |  |
| 6x6x4 | 70 | 10x10x8 | 136 | $24 \times 24 \times 12$ |  |
| 6x5x4 | 79 | 12x12x4 | 161 | $24 \times 24 \times 14$ |  |
| 6x4x4 | 58 | 12x12x6 | 156 | $24 \times 24 \times 16$ |  |
| $6 \times 5 \times 6$ |  | 12x12x8 | 160 |  |  |

## CONVERSE JOINT FIT'TINGS.

CROSSES.

| Size. | $\begin{gathered} \text { Weight } \\ \text { lbs. } \end{gathered}$ | Size. | $\begin{gathered} \text { Weight } \\ \text { lbs. } \end{gathered}$ | Size. | $\begin{gathered} \text { Weight } \\ \text { lbs. } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2x2x2x2 | 21 | $8 \mathrm{x} \mathrm{8x} 8 \mathrm{x} 8$ | 156 | 18x18x18x18 |  |
| $3 \mathrm{x} 3 \times 3 \times 3$ | 39 | $10 \times 10 \times 10 \times 10$ | 205 | 20x20x20x20 |  |
| $4 \times 4 \times 4 \times 4$ | 57 | $12 \times 12 \times 12 \times 12$ | 306 | 22x22x22x22 |  |
| 5x5x5x5 | 71 | 14x14x14x14 | ... | $24 \times 24 \times 24 \times 24$ |  |
| 6x6x6x6 | 104 | 16x16x16x16 |  |  |  |

REDUCING CROSSES.

| Size. | $\left.\begin{gathered} \text { Weight } \\ \text { lbs. } \end{gathered} \right\rvert\,$ | Size. | $\begin{array}{\|c\|} \hline \text { Weight } \\ \text { lbs. } \end{array}$ | Size. | $\begin{gathered} \text { Weight } \\ \text { lbs. } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $3 \times 3 \times 2 \times 2$ |  | 6x $4 \times 6 \times 4$ | 78 | 10x $8 \times 10 \times 8$ | 218 |
| $3 \times 2 \times 3 \times 2$ |  | 6 x 6 x 6 x 3 | 103 | 12x12x 6x 6 | 166 |
| $4 \times 4 \times 2 \times 2$ | 39 | 8 x 8 x 4 x 4 | 98 | 12 x 6 x 12 x 6 |  |
| $4 \times 4 \times 3 \times 3$ | 46 | 8 x 4 x 8 x 8 | 131 | 12 x 12 x 8 x 8 |  |
| 4x3x4x3 | 60 | 8 x 6 x 8 x 6 | 129 | 12x $8 \times 12 \mathrm{x} 8$ |  |
| 5x5x3x3 | 50 | 8 x 6 x 4 4 4 | 132 | $12 \times 10 \times 12 \times 10$ | 261 |
| $5 \mathrm{x} 3 \times 5 \mathrm{x} 3$ |  | 8 x 8 x 6 x 6 | 118 | $14 \times 14 \times 12 \times 12$ |  |
| $5 \times 5 \times 4 \times 4$ | 71 | 8 x 8 xx 5 x | 127 | $16 \times 16 \times 10 \times 10$ |  |
| $5 \times 4 \times 5 \times 4$ |  | 10x10x 4x 4 | 125 | $16 \times 16 \times 12 \times 12$ |  |
| $5 \times 5 \times 5 \times 4$ | 71 | 10x 4x10x 4 | 123 | $18 \times 18 \mathrm{x}$ 6x 6 |  |
| 6x6x4x4 | 77 | $10 \times 10 x 5 \times 5$ | 162 | $18 \times 18 \times 10 \times 10$ |  |
| $6 \times 6 \times 3 \times 3$ | 67 | 10x 5x10x 5 |  | 18x18x12x12 | 646 |
| 6x3x6x3 |  | $10 \times 10 x 686$ | 166 | 20x20x 6x 6 |  |
| $6 \times 6 \times 5 \times 5$ | 120 | 10x 6x10x 6 |  | $20 \times 20 \times 10 \times 10$ |  |
| 6x5x6x5 | 102 | 10x10x 8x $8 \mid$ | 198 | 20x20x16x16 |  |

MISCELLANEOUS CROSSES.

| Size. | Weight lbs. | Size. | $\begin{gathered} \text { Weight } \\ \text { lbs. } \end{gathered}$ | Size. | $\begin{gathered} \text { Weight } \\ \text { lbs. } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $4 \times 4 \times 6 \times 4$ | 92 | 6x6x6x4 | 105 | $8 \times 6 \times 8 \times 4$ |  |
| $6 \mathrm{x} 5 \times 6 \mathrm{x} 4$ | 110 | $6 \times 6 \times 6 \times 3$ | 103 | $8 \mathrm{x} 4 \times 6 \times 6$ | 136 |
| $6 \mathrm{x} 4 \times 4 \times 4$ | 90 | $8 \times 6 \times 8 \times 5$ | 126 |  |  |
| 6x4x6x3 | 93 | $8 \mathrm{x} 4 \times 8 \times 8$ | 131 | ... | ... |

Some of the weights in these tables of Converse Joint Fittings are not given ; the reason being that there are not Standard patterns for the sizes where weights are omitted, and the patterns of some other sizes are made adaptable for same. This would cause a variation in weights, and for this reason it is thought best to give no fixed weights for fittings so manufactured.

TEES.

| Size. | Weight, lbs. | Size. | Weight, lbs. | Size. | $\begin{aligned} & \text { Weight, } \\ & \text { lbs. } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $2 \times 2 \times 2$ | 17 | 8 x 8 x 8 | 127 | $15 \times 15 \times 15$ | $\ldots$ |
| $3 \times 3 \times 3$ | 29 | 9 x 9 x 9 |  | 16x16x16 | $\ldots$ |
| $4 \times 4 \times 4$ | 45 | $10 \times 10 \times 10$ | 178 | $18 \times 18 \times 18$ |  |
| $5 \times 5 \times 5$ | 56 | $12 \times 12 \times 12$ | 192 | 20x20x20 | $95 \%$ |
| 6x6x6 | 70 | $13 \times 13 \times 13$ |  | $22 \times 22 \times 22$ |  |
| $7 \times 7 \times 7$ | 84 | $14 \times 14 \times 14$ | 359 | $24 \times 24 \times 24$ |  |

MISCELLANEOUS TEES.

| SIzE. | Weight, lbs. | Size. | Weight, lbs. | Size. | Weight, lbs. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $6 \times 5 \times 4$ | 79 | 10x $8 \times 10$ | 135 | 12 x 8 x 12 | 282 |
| 10x $4 \times 10$ |  | $10 \times 10 \times 12$ | 182 | $12 \times 8 \mathrm{x} 8$ |  |
| 10x $5 \times 10$ |  | 10x $8 \times 8$ |  | $14 \times 12 \times 14$ |  |
| 10x 6x 6 | 110 | $12 \times 6 \times 12$ |  | 16x 8x16 | 600 |

REDUCERS.

| Size. | Weight, lbs. | Size. | Weight, lbs. | Size. | Weight, lbs. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3 to 2 | 27 | 8 to 5 | 70 | 16 to 6 | 295 |
| 4 to 2 | 22 | 8 to 6 | 63 | 16 to 8 |  |
| 4 to 3 | 27 | 10 to 4 | 90 | 16 to 10 | 256 |
| 5 to 3 | 39 | 10 to 5 | 94 | 16 to 12 | 256 |
| 5 to 4 | 36 | 10 to 6 | 94 | 18 to 16 | 442 |
| 6 to 2 | 55 | 10 to 8 | 107 | 20 to 12 | 395 |
| 6 to 3 | 36 | 12 to 5 | 154 | 20 to 18 | 505 |
| 6 to 4 | 40 | 12 to 6 | 154 | 20 to 16 | 608 |
| 6 to 5 | 46 | 12 to 8 | 138 | 24 to 12 |  |
| 7 to 5 | 52 | 12 to 10 |  | 24 to 18 |  |
| 8 to 3 | 60 | 13 to 12 | 90 | 24 to 20 |  |
| 8 to 4 | 53 | 14 to 13 | 88 |  |  |

## ELLS.

| Size. | Wt. lbs. | Size. | Wt. 1bs. | SIzE. | wt. lbs. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $2 \times 2 \times 90^{\circ}$ | 12 | $7 \times 7 \times 45^{\circ}$ | . | $14 \times 14 \times 22 \frac{1}{2}^{\circ}$ |  |
| $2 \times 2 \times 60^{\circ}$ |  | $7 \times 7 \times 30^{\circ}$ |  | $14 \times 14 \times 10^{\circ}$ |  |
| $2 \times 2 \times 45^{\circ}$ | 9 | $7 \times 7 \times 22 \frac{1}{2}^{\circ}$ | 39 | $15 \times 15 \times 90^{\circ}$ |  |
| $2 \times 2 \times 30^{\circ}$ | 8 | $7 \times 7 \times 10^{\circ}$ |  | $15 \times 15 \times 60^{\circ}$ |  |
| $2 \times 2 \times 22 \frac{1}{2}^{\circ}$ |  | $8 \times 8 \times 90^{\circ}$ | 95 | $15 \times 15 \times 45^{\circ}$ |  |
| $2 \times 2 \times 10^{\circ}$ |  | $8 \mathrm{x} 8 \times 60^{\circ}$ | 71 | $15 \times 15 \times 30^{\circ}$ |  |
| $3 \times 3 \times 90^{\circ}$ | 25 | $8 \mathrm{x} 8 \times 45^{\circ}$ | 69 | $15 \times 15 \times 22 \frac{1}{2}^{\circ}$ |  |
| $3 \times 3 \times 60^{\circ}$ |  | $8 \mathrm{x} 8 \times 30^{\circ}$ |  | $15 \times 15 \times 10^{\circ}$ |  |
| $3 \times 3 \times 45^{\circ}$ | 12 | $8 \mathrm{x} 8 \times 22 \frac{1}{2}^{\circ}$ | 64 | $16 \times 16 \times 90^{\circ}$ | 420 |
| $3 \times 3 \times 30^{\circ}$ |  | $8 \mathrm{x} 8 \times 10^{\circ}$ | 50 | $16 \times 16 \times 60^{\circ}$ |  |
| $3 \times 3 \times 22 \frac{1}{2}^{\circ}$ | 13 | $10 \times 10 \times 90^{\circ}$ | 148 | $16 \times 16 \times 45^{\circ}$ | 265 |
| $3 \times 3 \times 10^{\text {- }}$ |  | $10 \times 10 \times 60^{\circ}$ |  | $16 \times 16 \times 30^{\circ}$ |  |
| $4 \times 4 \times 90^{\circ}$ | 32 | $10 \times 10 \times 45^{\circ}$ | 93 | $16 \times 16 \times 22 \frac{1}{2}^{\circ}$ |  |
| $4 \times 4 \times 60^{\circ}$ | 25 | $10 \times 10 \times 30^{\circ}$ |  | $16 \times 16 \times 10^{\circ}$ |  |
| $4 \times 4 \times 4{ }^{\circ}$ | 23 | $10 \times 10 \times 22 \frac{1}{2}^{\circ}$ |  | $18 \times 18 \times 90^{\circ}$ |  |
| $4 \times 4 \times 30^{\circ}$ | 17 | $10 \times 10 \times 10^{-}$ |  | $18 \times 18 \times 60^{\circ}$ |  |
| $4 \times 4 \times 22 \frac{1}{2}^{\circ}$ | . | $12 \times 12 \times 90^{\circ}$ | 205 | $18 \times 18 \times 45^{\circ}$ |  |
| $4 \times 4 \times 10^{\circ}$ |  | $12 \times 12 \times 60^{\circ}$ |  | $18 \times 18 \times 30^{\circ}$ |  |
| $5 \times 5 \times 90^{\circ}$ | 41 | $12 \times 12 \times 45^{\circ}$ | 132 | $18 \times 18 \times 22 \frac{1}{2}^{\circ}$ |  |
| $5 \times 5 \times 60^{\circ}$ |  | $12 \times 12 \times 30^{\circ}$ | 108 | $18 \times 18 \times 10^{\circ}$ |  |
| $5 \mathrm{x} 5 \times 45^{\circ}$ | 32 | $12 \times 12 \times 22 \frac{1}{2}^{\circ}$ | 112 | $20 \times 20 \times 90^{\circ}$ | 840 |
| $5 \times 5 \times 30{ }^{\circ}$ |  | $12 \times 12 \times 10^{\circ}$ | 95 | $20 \times 20 \times 60^{\circ}$ |  |
| $5 \times 5 \times 22{\frac{1}{}{ }^{\circ}}$ | . | $13 \times 13 \times 90^{\circ}$ | 230 | $20 \times 20 \times 45^{\circ}$ |  |
| $5 \times 5 \times 10^{\circ}$ |  | $13 \times 13 \times 60^{\circ}$ | . | $20 \times 20 \times 30^{\circ}$ | 620 |
| $6 \times 6 \times 90^{\circ}$ | $5 \%$ | $13 \times 13 \times 45^{\circ}$ |  | $20 \times 20 \times 22 \frac{1}{2}^{\circ}$ | 365 |
| $6 \times 6 \times 60^{\circ}$ | 48 | $13 \times 13 \times 30^{\circ}$ |  | $20 \times 20 \times 10^{\circ}$ |  |
| $6 \times 6 \times 45^{\circ}$ | 41 | $13 \times 13 \times 22^{\frac{1}{2}}{ }^{\circ}$ |  | $24 \times 24 \times 90^{\circ}$ | 1143 |
| $6 \times 6 \times 30^{\circ}$ | 39 | $13 \times 13 \times 10^{\circ}$ |  | $24 \times 24 \times 60^{\circ}$ |  |
| $6 \times 6 \times 22 \frac{1}{2}^{\circ}$ | 30 | $14 \times 14 \times 90^{\circ}$ | 247 | $24 \times 24 \times 45^{\circ}$ |  |
| $6 \times 6 \times 10^{\circ}$ | 30 | $14 \times 14 \times 60^{\circ}$ |  | $24 \times 24 \times 30^{\circ}$ |  |
| $7 \times 7 \times 90^{\circ}$ | 72 | $14 \times 14 \times 45^{\circ}$ | 163 | $24 \times 24 \times 22 \frac{1}{2}^{\circ}$ | 550 |
| $7 \times 7 \times 60^{\circ}$ |  | $14 \times 14 \times 30^{\circ}$ |  | $24 \times 24 \times 10^{\circ}$ |  |

Y'S.

| Size. | Wt. 1bs. | Size. | Wt. 1bs. | Size. | Wt. 1bs. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3x3x 3 | 33 | $6 \times 6 \times 6$ | 123 | $12 \times 12 \times 12$ | 350 |
| $4 \times 4 \times 4$ | 70 | $8 \times 8 \times 8$ | 180 | $18 \times 18 \times 18$ | 1145 |
| $5 \times 5 \times 5$ | 95 | $10 \times 10 \times 10$ | 262 | 20x20x20 | 2400 |

## PLUGS.

| SIZE. | Wt. <br> lbs. | SIZE. | Wt. <br> lbs. | SIZE. | Wt. <br> lbs. |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
|  |  | 1 | 6 | 10 | 10 |
| 3 | 3 | 7 | 14 | 12 | 25 |
| 4 | 5 | 8 | 19 | 14 | 40 |
| 5 | 9 | 9 | 22 | 16 | 54 |

## MISCELLANEOUS.

| CROSSES. |  | TEES. |  | ELLS. |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Size. | Wt. lbs. | Size. | Wt. lbs. | Size. | Wt. lbs. |
| $\begin{aligned} & 3 \times 3 \times 1+\times 1 \dagger \\ & 4 \times 4 \times 2+\times 2 \dagger \\ & 4 \times 4 \times 6^{*} \times 6^{*} \\ & 4 \times 4 \times 4 \times 2 \dagger \\ & 6 \times 6 \times 8^{*} \times 8^{*} \\ & 6 \times 6 \times 4 \times 2 \dagger \end{aligned}$ | 22 | $2 \mathrm{x} 2 \times \mathrm{l}+$ | 11 | $6 \mathrm{x} 4+\mathrm{x} 90^{\circ}$ | 70 |
|  | 56 | $2 \mathrm{x} 2 \mathrm{x} 1 \frac{1}{2}+$ | 11 | $6 \mathrm{x} 5+\times 90^{\circ}$ | 65 |
|  | 124 | $3 \mathrm{x} 3 \mathrm{x} 1{ }^{+}$ | 22 | $12 \times 12+$ x $60{ }^{\circ}$ | 180 |
|  | 75 | $3 \mathrm{x} 2 \dagger \mathrm{x} 3$ | 43 | REDUCE | RS. |
|  | 184 | 4x $4 \times 2$ | 44 | Size. | Wt. 1bs |
|  | 83 | $\begin{array}{llll}5 \times 1 & 3 & \mathrm{x} 2 \\ 6 \mathrm{x} & 6 & \mathrm{x} 2\end{array}$ | 97 | 4 to $2 \downarrow$ | 17 |
|  |  | $10 \times 10 \times 4 \frac{1}{2}+$ | 163 | 12 to $12^{*}$ | 247 |
|  |  | $10 \times 10 \times 7{ }^{7}$ | 165 | 16 to $16^{*}$ | 450 |
|  |  | 4x $4 \times 4$ | 49 | 8 to $8 *$ | 61 |
|  |  | $2 \mathrm{x} 2 \mathrm{x} 2+$ | 16 | 8* to 6 | 62 |
|  |  | $6 \times 6 \times 6$ * | 115 | $6^{*}$ to 6 | 46 |

Fittings on the above Miscellaneous List may vary in weight 15 per cent. All combinations of Converse and threaded pipe, and Converse and cast-iron pipe connections will be uncertain weights, as patterns are changed for each requirement.

## SPECIAL

## Steel Lap-Welded Pipe

## FITTED WITH <br> MATHESON PATENT JOINT.



| O. D. | Thick- <br> ness <br> nearest <br> B. W. G. | Approximate Weights. |  | Per Foot <br> Complete. | Pounds of <br> Lead <br> in Joint. |
| :---: | :---: | :---: | :---: | :---: | :---: | | Lead |
| :---: |
| Space. |$\quad$| Size of |
| :---: |
| Rings. |

## WEIGHT OF FITTINGS.

 Matheson Joint.Heavy-faced figures indicate openings tapped for Standard Pipe.

TEES.

| Size. | Wgt. 1bs.\|| | Size. | Wgt. 1bs. |
| :---: | :---: | :---: | :---: |
| $2 \times 2 \times 2$ | 11 | $6 \mathrm{x} 5 \times 4$ | 96 |
| $3 \times 3 \times 3$ | 19 | 6 x ¢ 63 | 93 |
| $3 \mathrm{x} 3 \times 4$ | 35 | 6 x 4 x | 100 |
| $4 \times 4 \times 4$ | 35 | $6 \mathrm{x} 3 \times 16$ | 90 |
| $4 \times 4 \times 4$ | 39 | $7 \times 7 \times 7$ |  |
| $4 \times 4 \times 3$ | 35 | $7 \times 7 \times 6$ | 115 |
| $4 \times 4 \times 3$ | 35 | 8 x ¢ 8 x 8 | 159 |
| $4 \times 4 \times 2$ | 37 | $8 \times 8 \times 6$ | 173 |
| $4 \times 4 \times 2$ | 36 | $8 \times 8 \times 4$ | 172 |
| $4 \times 4 \times 1$ | 34 | $8 \times 6 \times 8$ | 176 |
| $4 \times 4 \times 6$ | 98 | $9 \times 9 \times 10$ |  |
| $4 \times 3 \times 4$ | 35 | $10 \times 10 \times 10$ | 256 |
| $5 \times 5 \times 5$ | 41 | $10 \times 10 \times 8$ | 270 |
| $5 \times 5 \times 4$ | 58 | $10 \times 10 \times 6$ | 268 |
| $5 \times 5 \times 4$ | 58 | $10 \times 10 \times 4$ | 285 |
| $5 \times 3 \times 5$ | 56 | $11 \times 11 \times 11$ | 353 |
| $6 \times 6 \times 6$ | 91 | $12 \times 12 \times 12$ | . . |

ELBOWS.

| Size. | Degree. | Wgt lbs. | Size. | Degree. | Wgt.1bs. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $2 \times 2$ | 90 | 9 | $8 \times 8$ | 30 | 60 |
| $3 \times 3$ | 45 | 11 | $8 \times 8$ | 45 | 77 |
| $3 \times 3$ | 90 | 18 | $8 \times 8$ | 90 | 137 |
| $4 \times 4$ | 45 | 22 | $9 \times 9$ | 45 | .. |
| $4 \times 4$ | 90 | 33 | $9 \times 9$ | 90 |  |
| $4 \times 3$ | 90 | 32 | $10 \times 10$ | 13 | 66 |
| $5 \times 5$ | 45 | 36 | $10 \times 10$ | 16 | 78 |
| $5 \times 5$ | 90 | 45 | $10 \times 10$ | 18 | 79 |
| $6 \times 6$ | 30 | 29 | $10 \times 10$ | 25 | 90 |
| $6 \times 6$ | 45 | 45 | $10 \times 10$ | 28 | 98 |
| $6 \times 6$ | 45 | 45 | $10 \times 10$ | 30 | 98 |
| $6 \times 6$ | 90 | 79 | $10 \times 10$ | 36 | 110 |
| $7 \times 7$ | 45 | 57 | $10 \times 10$ | 45 | 126 |
| $7 \times 7$ | 90 | 100 | $10 \times 10$ | 90 | 235 |

## ELBOWS.

| Size. | Degree. | Weight lbs. | SIzE. | Degree. | Weight lbs. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $11 \times 11$ | 45 | 160 | $12 \times 12$ | 45 | $\ldots$ |
| $11 \times 11$ | 60 | 192 | $12 \times 12$ | 90 | 372 |
| $11 \times 11$ | 90 | 255 |  |  |  |

CROSSES.

| Size. | Weight. lbs. | SIze. | Weight. lbs. |
| :---: | :---: | :---: | :---: |
| $2 \times 2 \times 2 \times 2$ | 13 | $6 \times 4 \times 3 \times 3$ | 125 |
| $3 \times 3 \times 3 \times 3$ | 28 | $7 \times 7 \times 7 \times 7$ | 135 |
| $4 \times 4 \times 4 \times 4$ | 42 | $7 \times 7 \times 6 \times 6$ | 153 |
| $4 \times 4 \times 4 \times 3$ | 43 | $8 \times 8$ x 8 x 8 | 200 |
| $4 \times 4 \times 3 \times 3$ | 46 | $8 \times 8 \times 8 \mathrm{x} 4$ | 229 |
| $4 \times 4 \times 2 \times 2$ | 45 | $8 \times 8 \times 8 \times 6$ | 230 |
| $4 \times 4 \times 2 \times 2$ | 43 | $8 \times 8 \times 4 \times 4$ | 209 |
| $4 \times 3 \times 3 \times 3$ | 45 | $8 \times 8 \times 14 \times 16$ | 1190 |
| $5 \times 5 \times 5 \times 5$ | 66 | $8 \times 6 \times 8 \times 6$ | 220 |
| $5 \times 5 \times 5 \times 4$ | 69 | $8 \times 6 \times 8 \times 4$ | 235 |
| $5 \times 5 \times 4 \times 4$ | 74 | $8 \times 6 \times 3 \times 3$ | 238 |
| $5 \times 4 \times 5 \times 5$ | 72 | $8 \times 4 \times 4 \times 4$ | 218 |
| $6 \times 6 \times 6 \times 6$ | 108 | $9 \times 9 \times 9 \times 9$ |  |
| $6 \times 6 \times 4 \times 4$ | 117 | $10 \times 10 \times 10 \times 10$ | 337 |
| $6 \times 6 \times 4 \times 3$ | 120 | $10 \times 10 \times 10 \times 8$ | 339 |
| $6 \times 4 \times 4 \times 4$ | 127 | $12 \times 12 \times 12 \times 12$ |  |

Heavy faced figures indicate openings tapped for Standard Pipe.

REDUCERS.

| Size. | Weight | Size. | Weight Lbs. | Size. | $\begin{aligned} & \text { Weight } \\ & \text { Lbs. } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $3 \times 2$ | . | $6 \times 4$ | 21 | $9 \times 8$ | . |
| $4 \times 3$ | 11 | $6 \times 3$ | . | $9 \times 7$ | - |
| $4 \times 3$ | 14 | $6 \times 3$ | 25 | $9 \times 6$ | . |
| $4 \times 2$ | 12 | $7 \times 6$ | . | $10 \times 9$ | . |
| $5 \times 5$ | 19 | $7 \times 5$ | - | $10 \times 8$ | 50 |
| $5 \times 4$ | 17 | $8 \times 7$ |  | $10 \times 6$ | 46 |
| $5 \times 3$ | . | $8 \times 6$ | 39 | $10 \times 4$ | 52 |
| $6 \times 5$ | . | $8 \times 4$ | 43 | $12 \times 10$ | 75 |
| $6 \times 4$ | 22 |  |  |  |  |

PLUGS.

| Size. | Weight <br> Lbs. | Size. | Weight <br> Lbs. | Size. | Weight <br> Lbs. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 1 | 6 | 7 | 10 | 23 |
| 3 | 2 | 7 | 13 | 12 | $\ldots$ |
| 4 | 3 | 8 | 15 | 14 | 58 |
| 5 | 5 | 9 | $\ldots$ | 16 | 88 |
|  |  |  | 14 |  |  |

Heavy-faced figures indicate openings tapped for Standard Pipe.
Some of the weights in these tables of Matheson Joint Fittings are not given; the reason being that there are not Standard patterns for sizes where weights are omitted and the patterns of some other size are made adaptable for same. This would cause a variation in weights, and for this reason it is thought best to give no fixed weights for fittings so manufactured.


PLAIN UPSET.

UPSET TUBES are becoming very generally used for Marine Boiler work ; in many cases the ordinary, as well as the Stay Tubes, are thickened or upset on ends, greater durability and strength being claimed for same.

The difficulties encountered in upsetting ends of tubes are not generally appreciated, and upsets are often asked for that are either very difficult or practically impossible to make. As a guide for ordering such tubes a set of tables has been prepared showing the practicable limits that should be observed in tubes of this kind. If a greater diameter is required for upset end than that shown on table giving maximum upset-this can be accomplished by expanding the end after upsetting as is shown in the cut below. The tables are all based on an upset $21 / 2$ inches long which is the usual length for Boiler Stay Tubes. If shorter length will answer a heavier upset than those shown on maximum table can be secured.


UPSET AND SWELLED.
NATIONAL TUBE COMPANY.
TABLE SHOWING ORDINARY UPSET FOR TUBES.


|  |  | Outside Diameter in Inches. |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $11 / 2$ | $13 / 4$ | 2 | 21/4 | 21/2 | $23 / 4$ |  | $31 / 4$ | $31 / 2$ | $33 / 4$ | 4 | 41/4 | 41/2 | $43 / 4$ | 5 |  |  |
| 10 | . 134 | 1.70 | 1.95 | 2.20 | 2.45 | 2.70 | 2.95 | 3.20 | 3.45 | 3.70 | 3.95 | 4.20 | 4.45 | 4.70 | 4.95 | 5.20 | Outsid of | Diameter Upset. |
| 9 | . 148 | 1.72 | 1.97 | 2.22 | 2.47 | 2.72 | 2.97 | 3.22 | 3.47 | 3.72 | 3.97 | 4.22 | 4.47 | 4.72 | 4.97 | 5.22 | * | , |
| 8 | . 165 | 1.75 | 2.00 | 2.25 | 2.50 | 2.75 | 3.00 | 3.25 | 3.50 | 3.75 | 4.00 | 4.25 | 4.50 | 4.75 | 5.00 | 5.25 | c | " |
| 7 | . 188 | 1.78 | 2.03 | 2.28 | 2.53 | 2.78 | 3.03 | 3.28 | 3.53 | 3.78 | 4.03 | 4.28 | 4.53 | 4.78 | 5.03 | 5.28 | 6 | 6 |
| 6 | . 203 | 1.80 | 2.05 | 2.30 | 2.55 | 2.80 | 3.05 | 3.30 | 3.55 | 3.80 | 4.05 | 4.30 | 4.55 | 4.80 | 5.05 | 5.30 | 6 | 6 |
| 5 | . 219 | 1.83 | 2.08 | 2.33 | 2.58 | 2.83 | 3.08 | 3.33 | 3.58 | 3.83 | 4.08 | 4.33 | 4.58 | 4.83 | 5.08 | 5.33 | ، | * |
| 4 | . 238 | 1.86 | 2.11 | 2.36 | 2.61 | 2.86 | 3.11 | 3.36 | 3.61 | 3.86 | 4.11 | 4.36 | 4.61 | 4.86 | 5.11 | 5.36 | 66 | " |
| $1 / 4$ | . 250 | 1.88 | $2.13$ | 2.38 | 2.63 | 2.88 | 3.13 | 3.38 | 3.63 | 3.88 | 4.13 | 4.38 | 4.63 | 4.88 | 5.13 | 5.38 | 6 | 6 |
| -989 | . 281 | 1.92 | 2.17 | 2.42 | 2.67 | 2.92 | 3.17 | 3.42 | $3.67$ | 3.92 | 4.17 | 4.42 | 4.67 | 4.92 | 5.17 | 5.42 | . | * |
| 88 <br> 16 <br> 16 | . 313 | 1.97 | 2.22 | 2.47 | 2.72 | 2.97 | 3.22 | 3.47 | 3.72 | 3.97 | 4.22 | 4.47 | 4.72 | 4.97 | 5.22 | 5.47 | , | 6 |
| 16 <br> $\frac{11}{82}$ | . 344 | 2.02 | 2.27 | 2.52 | 2.77 | 3.02 | 3.27 | 3.52 | 3.77 | 4.02 | 4.27 | 4.52 | 4.77 | 5.02 | 5.27 |  | ، | 6 |
| 82 $3 / 8$ | . 375 | 2.06 | 2.31 | 2.56 | 2.81 | 3.06 | 3.31 | 3.56 | 3.81 | 4.06 | 4.31 | 4.56 | 4.81 | 5.06 |  |  |  | ، |
| $\frac{1}{8} \frac{8}{3}$ | . 406 | 2.11 | 2.36 | 2.61 | 2.86 | 3.11 | 3.36 | 3.61 | 3.86 | 4.11 | 4.36 | 4.61 | 4.86 |  |  |  | , | /f |
| $\frac{1}{7}{ }^{7}$ 16 | . 438 | 2.16 | 2.41 | 2.66 | 2.91 | 3.16 | 3.41 | 3.66 | 3.91 | 4.16 | 4.41 | 4.66 |  |  |  |  |  | f |


| 山. 『『 |  | Outside Diameter in Inches |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 烒烒药 | 11／2 | $13 / 4$ | 2 | 214 | 21／2 | 23／4 | 3 | 31／4 | 31／2 | 33／4 | 4 | $41 / 4$ | $41 / 2$ | $43 / 4$ | 5 |  |  |
| 10 | ． 134 | 1.77 | 2.02 | 2.27 | 2.52 | 2.77 | 3.02 | 3.27 | 3.52 | 3.77 |  |  |  |  |  |  | Outsi | de Diameter f Upset． |
| 9 | ． 148 | 1.80 | 2.05 | 2.30 | 2.55 | 2.80 | 3.05 | 3.30 | 3.55 | 3.80 | 4.05 | 4.30 |  |  |  |  |  | ، |
| 8 | ． 165 | 1.83 | 2.08 | 2.33 | 2.58 | 2.83 | 3.08 | 3.33 | 3.58 | 3.83 | 4.08 | 4.33 | 4.58 | 4.83 |  |  |  | ＂ |
| 7 | ． 188 | 1.88 | 2.13 | 2.38 | 2.63 | 2.88 | 3.13 | 3.38 | 3.63 | 3.88 | 4.13 | 4.38 | 4.63 | 4.88 | 5.13 | 5.38 |  | ＊ |
| 6 | ． 203 | 1.91 | 2.16 | 2.41 | 2.66 | 2.91 | 3.16 | 3.41 | 3.66 | 3.91 | 4.16 | 4.41 | 4.66 | 4.91 | 5.16 | 5.41 |  | ＊ |
| 5 | ． 219 | 1.94 | 2.19 | 2.44 | 2.69 | 2.94 | 3.19 | 3.44 | 3.69 | 3.94 | 4.19 | 4.44 | 4.69 | 4.94 | 5.19 | 5.44 |  | 6 |
| 4 | ． 238 | 1.98 | 2.23 | 2.48 | 2.73 | 2.98 | 3.23 | 3.48 | 3.73 | 3．98 | 4.23 | 4.48 | 4.73 | 4．94 | 5.23 | 5．48 |  | －6 |
| 1／4 | ． 250 | 2.00 | 2.25 | 2.50 | 2.75 | 3.00 | 3.25 | 3.50 | 3.75 | 4.00 | 4.25 | 4.50 | 4.75 | 5.00 | 5.25 | 5.50 | ， | ${ }^{6}$ |
| －${ }^{2}$ | ． 281 | 2.06 | 2.31 | 2.56 | 2.81 | 3.06 | 3.31 | 3.56 | 3.81 | 4.06 | 4.31 | 4.56 | 4.81 | 5.06 | 5.31 | 5.56 |  | 6 |
| $\frac{5}{16}$ | ． 313 | 2.13 | 2.38 | 2.63 | 2.88 | 3.13 | 3.38 | 3.63 | 3.88 | 4.13 | 4.38 | 4.63 | 4.88 | 5.13 | 5.38 | 5.63 | ， | ＊ |
| $\frac{11}{81}$ | .344 | 2.19 | 2.44 | 2.69 | 2.94 | 3.19 | 3.44 | 3.69 | 3.94 | 4.19 | 4.44 | 4.69 | 4.94 | 5.19 | 5.44 |  |  | ＊ |
| 3／8 | ． 375 | 2.25 | 2.50 | 2.75 | 3.00 | 3.25 | 3.50 | 3.75 | 4.00 | 4.25 | 4.50 | 4.75 | 5.00 | 5.25 |  |  |  | ＂ |
| $\frac{18}{8} \frac{8}{2}$ | ． 406 | 2.31 | 2.56 | 2.81 | 3.06 | 3.31 | 3.56 | 3.81 | 4.06 | 4.31 | 4.56 |  | 5.06 |  |  |  |  | 6 6 |
| $\frac{7}{16}$ | ． 438 | 12.38 | 2.63 | 2.88 | 3.13 | 3.38 | 3.63 | 3.88 | 4.13 | 4.38 | 4.63 | 4.88 | ｜ |  |  |  | 6 | ، |

## PIPE BENDS.

The attached table gives the advisable radius and the greatest and least radii to which standard thickness pipe may be bent.

If the radius must be reduced from the minimum given in the table, the thickness of the pipe must be increased. For such bends it is best to submit sketch.

When the radius is greater than the maximum given in the list, the bend is apt to look like a series of kinks, owing to the Bender having to take short heats, unless the radius is so great that the pipe may be bent cold.

With offset bends try to make according to Drawing F.-261, rather than Drawings F. -257 or 262 . The straight length between the bends is of advantage to the pipe Bender.

With the welded flanges there must be a short straight length of pipe adjacent to each flange. On sizes under 4 inches this should equal, at least, one and a half diameters. On sizes over 4 inches it should equal, at least, one diameter of the pipe. In all cases it is better if equal to two diameters of straight pipe.

## BENT TUBES.

These are more difficult to bend than standard weight pipe. Try not to vary from the advisable radius given in the table. With tubes it is frequently necessary to increase the thickness over that of standard boiler tubes in order to bend them.

## TABLE OF RADII

FOR

## PIPE BENDS.

| Pipe Size. | Minimum Radius. | Maximum Radius. | Advisable Radius. |
| :---: | :---: | :---: | :---: |
| Inches. | Inches. | Inches. | Inches. |
| 21/2 | 10 | 25 | 15 |
| 3 | 12 | 30 | 18 |
| $31 / 2$ | 14 | 35 | 21 |
| 4 | 16 | 40 | 24 |
| 41/2 | 18 | 45 | 27 |
| 5 | 20 | 50 | 30 |
| 6 | 24 | 60 | 36 |
| 7 | 28 | 70 | 42 |
| 8 | 32 | 80 | 48 |
| 9 | 36 | 90 | 54 |
| 10 | 40 | 100 | 60 |
| 11 | 44 | 110 | 66 |
| 12 | 48 | 120 | 72 |
| 14 o. d. | 60 | 140 | 84 |
| 15 " | $68^{\circ}$ | 145 | 90 |
| 16 " | 76 | 150 | 100 |
| 18 " | 90 | 165 | 125 |
| 20 " | 120 | 180 | 150 |
| 22 " | 132 | 198 | 165 |
| 24 " | 144 | 216 | 180 |

## STOCK PIPE BENDS

## AMERICAN OR ENGLISH STANDARD

 THREADS AND COUPLINGS.

| Pipe Size. | Radius <br> "R." | Centre To <br> Face" A." |
| :---: | :---: | :---: |
| Inches. | Inches. | Inches. |
| $1 / 8$ | $11 / 4$ | 2 |
| $1 / 4$ | $1 \frac{5}{16}$ | $21 / 4$ |
| $3 / 8$ | $1 \frac{7}{16}$ | $2 \frac{9}{16}$ |
| $1 / 2$ | $13 / 4$ | $31 / 8$ |
| $3 / 4$ | $2 \frac{3}{16}$ | $3 \frac{15}{16}$ |
| 1 | $2 \frac{9}{16}$ | $4 \frac{9}{16}$ |
| $11 / 4$ | 3 | $51 / 8$ |
| $11 / 2$ | $3 \frac{5}{16}$ | $5 \frac{11}{16}$ |
| 2 | $4 \frac{7}{16}$ | $6 \frac{1}{16}$ |
| $21 / 2$ | $6 \frac{11}{16}$ | $9 \frac{7}{16}$ |
| 3 | 8 | 10 |



OFFSET BEND, No. F. 257.


ANGLE BEND, No. F. 260.


OFFSET BEND, No. F, 26 r.


OFFSET BEND, No. F. 262.

$180^{\circ}$ BEND, No. F. 258.
$90^{\circ}$ BEND, No. F. 259.

## DIMENSIONS

of
National Trolley Poles

AND

DEFLEC'TIONS
UNDER STATED LOADS
Length of Pole, 34 feet.

Length of Pole, 34 feet.

Length of Pole, 33 feet.

Length of Pole, 33 feet.

Length of Pole， 32 feet．

|  | $\begin{aligned} & \stackrel{+}{0} \\ & \text { B } \\ & 0.0 \\ & B \end{aligned}$ | BUTT． |  | MIDDLE． |  | END．${ }^{\text {a }}$ |  | Table |  | OF | Deflections |  |  | Measured |  |  | Fref |  | End． |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 勉 |  | $16^{\prime}-10^{\prime \prime}$ |  | $10^{\prime}-2^{\prime \prime}$ |  | $8^{\prime}-0^{\prime \prime}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 号 |  | － | \％ | $\dot{0}$ | 0 | － |  | Top Line Gives Loads |  |  |  |  | in Pounds |  | Applied |  | 18＂From |  | End． |
|  |  | $\bigcirc$ | 震 | $\bigcirc$ | $\underset{H}{H}$ | $\bigcirc$ | 豆 | 400 | 600 | 800 | 1000 | 1200 | 1400 | 1600 | 1800 | 2000 | 2200 | 2400 | 2600 |
| 53 | 1552 | 9.625 | 0.625 | 8.00 | 0.437 | 7.00 | 0.312 | 1.14 | 1.71 | 2.29 | 2.86 | 3.42 | 4.00 | 4.58 | 5.15 | 5.72 | 6.29 | 6.84 | 7.44 |
| 54 | 1416 | ＂ | 0.562 | ＂ | 0.406 | ＂ | 0.281 | 1.22 | 1.83 | 2.43 | 3.04 | 3.65 | 4.26 | 4.86 | 5.47 | 6.08 | 6.69 | 7.30 | 7.90 |
| 55 | 1319 | ＂ | 0.500 | ＂ | ＂ | ＂ | ، | 1.29 | 1.94 | 2.59 | 3.24 | 3.88 | 4.54 | 5.18 | 5.83 | 6.48 | 7.13 | 7.76 |  |
| 6 | 1144 | ＂ | 0.437 | 8.625 | 0.312 | 7.625 | 0.220 | 1.39 | 2.09 | 2.80 | 3.49 | 4.19 | 4.89 | 5.60 | 6.28 | 6.98 |  |  | 2800 |
| 57 | 1068 | ＂ | 0.406 | ＂ | 0.281 | ＂ | ＂ | 1.50 | 2.26 | 3.00 | 3.76 | 4.52 | 5.26 | 6.00 | 6.77 |  |  |  | 8.00 |
| 58 | 1013 | ＂ | 0.375 | 8.00 | 0.312 | 7.00 | 0.218 | 1.65 | 2.47 | 3.30 | 4.12 | 4.94 | 5.77 | 6.60 |  |  |  |  |  |
| 59 | 918 | ， | 0.312 | 8.625 | 0.281 | 7.625 | 0.220 | 1.77 | 2.65 | 3.53 | 4.42 | 5.30 | 6.19 |  |  |  |  |  |  |
| 60 | 971 | 9.00 | 0.375 | 8.00 | 0.300 | 7.00 | 0.220 | 1.92 | 2.89 | 3.85 | 4.81 | 5.77 | 6.73 |  |  |  |  |  |  |
| 61 | 848 | ＂ | 0.312 | ＂ | 0.281 | ＂ | 0.220 | 2.20 | 3.29 | 4.39 | ． 49 |  | 7.69 |  |  |  |  |  |  |


Length of Pole, 31 feet.



Length of Pole, 30 feet.



Length of Pole, 29 feet.


NATIONAL TUBE COMPANY.
Length of Pole, 29 feet.

| $\begin{aligned} & \dot{\Phi} \\ & \text { 品 } \\ & \text { z } \\ & \text { z } \end{aligned}$ | $\begin{aligned} & \stackrel{3}{3} \\ & \stackrel{0}{0} \\ & 0 \\ & 3 \end{aligned}$ | BUTT. |  | MIDDLE. |  | END. |  | TABLE OF |  | DEFLECTION |  |  | S Measured |  |  | AT | FREE END. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | $9^{\prime}-2^{\prime \prime}$ |  | $7^{\prime}-3^{\prime \prime}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | $\begin{array}{l\|l\|l\|l\|l\|l\|l\|l\|l\|l\|} \hline \dot{\sim} \\ \hline 0 & \dot{\sim} \\ \hline \end{array}$ |  | $\begin{array}{l\|l} \hline \dot{A} & \dot{u} \\ \dot{0} & \dot{y} \\ \hline \end{array}$ |  | $\begin{array}{l\|l\|l} \hline \dot{a} & \underset{\sim}{u} \\ \dot{u} \\ \dot{u} \end{array}$ |  | top Line Gives Loads in Pounds Applied 18* From End. |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  | 100 | 200 |  |  | 300 | 400 | 500 | 600 | 700 | 800 | 900 | 1000 | 1200 | 1400 |
| 140 | 867 | 8.625 | 0.406 |  |  | 7.625 | 0.281 | 6.625 | 0.220 | 0.366 | 0.732 | 1.101 | 1.461 | 1.83 | 2.20 | 2.56 | 2.92 | 3.29 | 3.66 | 4.40 | 5.12 |
| 141 | 786 | 6 | 0.343 | 6 | 6 | " | " | 0.400 | 0.800 | 1.201 | 1.60 | 2.00 | 2.40 | 2.80 | 3.20 | 3.60 | 4.00 | 4.80 | 5.60 |
| 142 | 702 | " | 0.281 | " | ${ }^{6}$ | ${ }^{\prime \prime}$ | " | 0.459 | 0.918 | 1.381 | 1.84 | 2.30 | 2.76 | 3.21 | 3.68 | 4.13 | 4.59 | 5.52 |  |
| 143 | 772 | 8.00 | 0.375 | 6.625 | 0.343 | 5.562 | 0.203 | 0.494 | 0.988 | 1.481 | 1.98 | 2.47 | 2.96 | 3.46 | 3.96 | 4.45 |  |  |  |
| 144 | 695 | 6 | 0.343 | ${ }^{6}$ | 0.281 | 6 | , | 0.547 | 1.09 | 1.64 | 2.18 | 2.74 | 3.28 | 3.83 | 4.36 | 4.92 |  |  |  |
| 145 | 646 | " | 0.281 | 7.00 | , | 6.00 | 0.220 | 0.582 | 1.16 | 1.742 | 2.33 | 2.91 | 3.49 | 4.07 | 4.66 | 5.24 |  |  | 1600 |
| 146 | 653 | 7.625 | 0.343 | 6.625 | 0.259 | 5.00 | 0.203 | 0.622 | 1.24 | 1.87 | 2.49 | 3.11 | 3.73 | 4.35 | 4.98 | 5.60 |  |  |  |
| 147 | 587 | 6 | 0.281 | " | * | 5.562 | 6 | 0.694 | 1.39 | 2.08 | 2.78 | 3.47 | 4.16 | 4.86 | 5.56 | 6.25 |  |  | 84 |
| 148 | 564 | ${ }^{6}$ | 4 | 6.00 | ' | 5.00 | 16 | 0.763 | 1.53 | 2.29 | 3.05 | 3.82 | 4.58 | 5.34 | 6.10 | 6.87 |  |  | 0 |
| 149 | 609 | 7.00 | 0.343 | 5.562 | 0.312 | 4.50 | 6 | 0.856 | 1.71 | 2.57 | 3.42 | 4.28 | 5.14 | 5.99 | 6.84 | 7.70 |  |  |  |
| 150 | 537 | \% | 0.281 | 6.00 | 0.259 | 5.00 | 16 | 0.919 | 1.84 | 2.76 | 3.68 | 4.60 | 5.51 | b. 43 | 7.36 | 8.27 |  |  |  |
| 151 | 516 | " | " | 5.562 | 6 | 4.50 | 6 | 1.00 | 2.00 | 3.00 | 4.00 | 5.00 | 6.00 | 7.00 | 8.00 |  |  |  |  |
| 152 | 503 | 6.625 | 0.30 | . | 0.238 | , | 6 | 1.10 | 2.20 | 3.30 | 4.40 | 5.50 | 6.60 | 7.70 |  |  |  |  |  |
| 153 | 464 | " | 0.259 | " | 6 | " | * | 1.20 | 2.40 | 3.60 | 4.80 | 6.00 | 7.20 | 8.40 |  |  |  |  |  |
| 154 | 514 | 6.00 | 0.343 | 5.00 | 0.281 | 4.00 | \% | 1.36 | 2.72 | 4.08 | 5.446 | 6.80 | 8.16 |  |  |  |  |  |  |
| 155 | 467 | 6 | 0.312 | " | 0.238 | " | " | 1.49 | 2.98 | 4.47 | 5.96 | 7.45 | 8.94 |  |  |  |  |  |  |
| 156 | 418 | * | 0.259 | ${ }^{6}$ | , | ، | 6 | 1.65 | 3.30 | 4.95 | 6.60 | 8.25 | 9.90 |  |  |  |  |  |  |



Length of Pole, 28 feet.

Length of Pole, 27 feet.

Length of Pole, 27 feet.



|  | $\begin{aligned} & \stackrel{1}{8} \\ & \dot{80} \\ & \dot{0} \\ & \stackrel{B}{3} \end{aligned}$ | $\begin{gathered} \text { BUTT. } \\ 14^{\prime}-4^{\prime \prime} \end{gathered}$ |  | $\frac{\text { MIDDLE. }}{8^{\prime}-2^{\prime \prime}}$ |  | END．$6^{\prime}-6^{\prime \prime}$ |  |  | ABLE | OF | Deflections |  |  | Measured |  | D AT | Free |  | END． |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  | $\begin{array}{r} \text { 苞 } \\ \text { H } \\ \hline \end{array}$ | $\stackrel{\dot{\circ}}{\dot{\circ}}$ | $\begin{array}{r} \dot{U} \\ \text { U } \\ \text { 畨 } \\ \hline \end{array}$ | $\dot{0}$ | $\square$ | Top Line Gives Loads in Po |  |  |  |  |  | ounds APplied |  |  | 18＊From |  | End． |
|  |  |  |  |  |  |  |  | 1000 | 1200 | 1400 | 1600 | 1800 | 2000 | 2200 | 2400 | ＇2600 | 2800 | 3000 | 3300 |
| 209 | 1297 | 9.625 | 0.625 | 8.00 | 0.437 | 7.00 | 0.312 | 1.23 | 1.48 | 1.72 | 1.97 | 2.21 | 2.46 | 2.71 | 2.96 | 3.20 | 3.44 | 3.69 | 4.06 |
| 210 | 1183 | 6 | 0.562 | ＂ | 0.406 | ＂ | 0.281 | 133 | 1.60 | 1.86 | 2.13 | 2.39 | 2.66 | 2.93 | 3.20 | 3.46 | 3.72 | 3.99 | 4.39 |
| 211 | 1100 | ＇ | 0.500 | ＂ | ＂ | ＂ | ＂ | 1.42 | 1.70 | 1.99 | 2.27 | 2.56 | 2.84 | 3.12 | 3.40 | 3.69 | 3.98 | 4.26 |  |
| 212 | 954 | ＂ | 0.437 | 8.625 | 0.312 | 7.625 | 0.220 | 1.53 | 1.84 | 2.14 | 2.45 | 2.75 | 3.06 | 3.37 | 3.68 | 3.98 |  |  | 3600 |
| 3 | 891 | ＂ | 0.406 | ＂ | 0.281 | ＂ | ＂ | 1.64 | 1.97 | 2.30 | 2.62 | 2.95 | 3.28 | 3.61 | 3.94 |  |  |  | 4.44 |
| 214 | 845 | ＂ | 0.375 | 8.00 | 0.312 | 7.00 | 0.218 | 1.80 | 2.16 | 2.52 | 2.88 | 3.24 | 3.60 | 3.96 |  |  |  |  |  |
| 215 | 764 | ＂ | 0.312 | 8.625 | 0.281 | 7.625 | 0.220 | 1.94 | 2.23 | 2.72 | 3.10 | 3.49 | 3.88 |  |  |  |  |  |  |
| 216 | 810 | 9.00 | 0.375 | 8.00 | 0.300 | 7.00 | ＂ | 2.10 | 2.52 | 2.94 | 3.36 | 3.78 | 4.20 |  |  |  |  |  |  |
| 217 | 705 | ＂ | 0.312 | ， | 0.281 |  | ＂ | 2.39 | 2.87 | 3.35 |  |  |  |  |  |  |  |  |  |

NATIONAL TUBE COMPANY.
Length of Pole, 26 feet.



|  | $\begin{aligned} & \stackrel{3}{3} \\ & \text { B } \\ & 0 \\ & B \\ & 3 \end{aligned}$ | BUTT. |  | MIDDLE. |  | END. |  |  | ABLE | OF | DEFLECTIONS |  |  | Measured |  | AT | Free |  | End. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $13^{\prime}-11^{\prime \prime}$ |  | $7^{\prime}-10^{\prime \prime}$ |  | 6'-3' |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | $\dot{A}$ | $\begin{aligned} & \text { M } \\ & \text { U } \\ & \text { H } \\ & \hline \end{aligned}$ | $\stackrel{A}{0}$ | 蜜 | $\begin{aligned} & \dot{\theta} \\ & \dot{0} \end{aligned}$ | 总 | Top Line Gives Loads in P |  |  |  |  |  | Ounds | Applied |  | $18^{*}$ From |  | End. |
|  |  |  |  |  |  |  |  | 1000 | 1200 | 1400 | 1600 | 1800 | 2000 | 2200 | 2400 | 2600 | 2800 | 3000 | 3400 |
| 235 | 1255 | 9.625 | 0.625 | 8.00 | $0.437{ }^{7}$ | 7.00 | 0.312 | 1.05 | 1.26 | 1.47 | 1.68 | 1.89 | 2.10 | 2.31 | 2.5 | 2.73 | 2.94 |  | 3.67 |
| 236 | 1144 | . | 0.562 | " | 0.406 | " | 0.281 | 1.13 | 1.36 | 1.58 | 1.8 | 2.03 | 2.26 | 2. |  |  | 3.16 | 39 | 3.84 |
| 7 | 1063 | - | 0.500 | " | ، | ، | " | 1.18 | 1.42 | 1.67 | 1.90 | 2.14 | 2.38 | 2.62 | 2.84 | 3.09 | 3.34 | 3. |  |
| 8 | 923 | '، | 0.437 | 8.625 | 0.312 | 7.625 | 0.220 | 1.30 | 1.56 |  | 2.08 | 2.34 | 2.60 | 2.86 | 3.12 | 3.38 | 3.64 |  | 3800 |
| 239 | 862 | " | 0.406 | " | 0.281 | - ${ }^{\prime}$ | " | 1.41 | 1.69 | 1.97 | 2.26 | 2.54 | 2.82 | 3.10 | 3.38 | 3.67 |  |  | 3.99 |
| 240 | 817 | " | 0.375 | 8.00 | 0.312 | 7.00 | 0.218 | 1.53 | 1.84 |  | 2.45 | 2.75 | 3.06 | 3.37 | 3.68 |  |  |  |  |
| 2 | 738 | " | 0.312 | 8.625 | 0.281 | 7.625 | 0.220 | 1.63 | 1.95 | 2.28 | 2.61 | 2.93 | 3.26 | 3.59 |  |  |  |  |  |
| 242 | 783 | 9.00 | 0.375 | 8.00 | 0.300 | 7.00 | " | 1.78 | 2.14 | 2.49 | 2.85 | 3.20 | 3.56 | 3.92 |  |  |  |  |  |
| 243 | 682 | " | 0.312 | " | \|0.281 | " | ' ${ }^{\prime}$ | 2.02 | 2.4 | 2.83 | 3.23 |  |  |  |  |  |  |  |  |


Length of Pole, 24 feet.


| Length of Pole， 24 feet． |  |  |  |  |  |  |  | End |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 药 | $\frac{\text { BUTt. }}{13^{\prime}-6^{\prime}}$ |  | $\left.\frac{\text { MIDDLE. }}{7^{\prime}-6^{\prime \prime}} \right\rvert\,$ |  | $\frac{\text { END. }}{6^{\prime}-0^{\prime \prime}}$ |  | Table of Deflections Measured at Free End． |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  | Top | Line | Gives | Loa |  | Pounds | PpLI | ED $18{ }^{\circ}$ | ${ }^{\circ}$ From | m En |
|  |  | $\bigcirc$ | 总 | $\bigcirc$ | 云 | 0 | 总 | 100 | 200 | 300 | 400 | 600 | 80010 |  | 1400 | 1600 | 18002000 |
| $270$ |  | 8.625 | 50 | 7.625 | 50.281 | 6.625 | 50.220 |  | 0.336 | 0.5 | 0672 | 1.01 | 1，34 1.68 |  | 2.35 | 2.69 | 3.02336 |
|  |  | ＂ | 0.343 |  |  |  | ＂ | 0.185 | 0.370 | 0.555 | （0．740 |  | 1481.85 | 2.22 | 2.59 | 2.96 | 3.333 .70 |
|  |  |  | 0.281 |  |  | 5. | 30 | 0212 |  |  | 0.848 |  | 1.802 .12 |  |  |  |  |
|  | 3655 | 8.00 | ${ }^{0.375}$ | 6.625 | 50.343 | 5． 563 | 0.203 | 0．227 | 0.454 | $\begin{aligned} & 40.681 \\ & 40756 \end{aligned}$ | $10.908$ | 1.36 | 1828.27 |  |  |  |  |
|  |  | ＂، | $\begin{gathered} 0.343 \\ 0.281 \end{gathered}$ |  | $0.281$ | 6.00 | 0.220 | ${ }_{0}^{0.252}$ |  | $\begin{aligned} & 40.756 \\ & 0.813 \end{aligned}$ | $\begin{aligned} & 81.01 \\ & 81.08 \end{aligned}$ | 1.51 | 2．1622．52 |  |  |  |  |
| 276 | 555 | 7.625 | 50.842 | 6.625 | 0．259 | 5.00 | 0.203 | 0.288 | 0.576 | 0.864 | 1.15 | 1.73 | 2.302 .88 | 3．46 |  |  |  |
|  | 497 |  | 0.281 |  |  | 5.563 |  | 0.322 | 0644 | 0.966 | 1.29 |  | 2.58322 | 3.86 |  |  | 04 |
|  | 479 | ＂ | ， | 6.00 | ． | 5.00 | ＂ | 0.358 | 0716 | 1.07 | 1.43 | 2.14 | 2.86 3．58 |  |  |  |  |
|  | 517 | 7.00 | 0.343 | 5.562 | 20.312 | 4.50 | ＂ | 0.391 | 0.782 | 1.17 | 1.56 |  | 3．12 3.91 |  |  |  |  |
|  | 454 |  | 0.281 | 6.00 | 0.259 | 5.00 | ＂ | 0.426 | 0852 | 1.28 | 1.70 | 2.56 | 3.404 .26 |  |  |  |  |
|  | 1438 | ＂ |  | 5.562 | 2 ＂ | 4.50 |  | 0.460 | 0.920 | 1.38 | 1.84 | 2.76 | 3.68 |  |  |  |  |
|  | 428 | 6.625 | 50.300 |  | ${ }^{0.238}$ |  | ＂، | 0.508 | 1.02 | 1.52 | 2.03 | ${ }_{3}^{3.04}$ | ${ }^{4.06}$ |  |  |  |  |
|  | 3395 |  | 0.259 |  | ＂ | ＂ |  | 0553 |  | 1.66 | 2，22 | 3.32 | 4.44 |  |  |  |  |
|  | 437 | 6.00 | 0.343 | 5.00 | 0.281 | 1.00 | ＂＂ | 0.622 | 1.24 | 1.87 | 2.48 | 3.74 4 10 | 496 |  |  |  |  |
|  | 5397 | ＂ | ［ $\begin{aligned} & 0.312 \\ & 0.259\end{aligned}$ | 0 | 0.238 | ＂ | ＂، | ${ }_{0}^{0.682}$ |  | 2．28 | ${ }_{3}^{2.72}$ | $\left\|\begin{array}{l} 4.10 \\ 4.53 \end{array}\right\|$ |  |  |  |  |  |



## Seamless

## Tubular Goods

## SEAMLESS DRAWN TUBING.

In submitting the following information on the subject of Seamless Tubing, together with the accompanying tables, etc., we call attention to the rapid strides made in the demand and in process of manufacture of this grade of Tubes in the last few years. These Tubes are becoming generally used for high grade Boiler work, where high steam pressures are required, especially for Marine Boilers, the Navy Department of all first-class Naval powers having extensively adopted the same. In both Locomotive and Stationary Boilers the use of this Tubing is becoming recognized as a high grade quality. The extending use of compressed air and other gases under high pressures has developed a good demand for these tubes for storage tanks, high pressure bottles, transmission lines, etc. The absence of all laps or seams, together with uniformity of size, gauge and quality, recommends this grade of material as very superior where unquestioned uniformity and strength are required, in connection with the lightest weight available for the purpose.

Seamless Tubes with varying thicknesses of walls are also being used quite extensively for Mechanical and Engineering purposes; for bushings, collars, hollow shafts, spindles, axles, etc., in the construction of different classes of machinery.

Different grades of steel can be used, giving a wide range of ductility and tensile strength, which allows a selection of material suited and adaptable to the requirements demanded. The methcd of manufacture of Seamless Tubes is such that the possibilities of physical defects in material are reduced to a minimum.

# Extract from Proceedings of Niagara Falls Society of American Mechanical Engineers. December, 1898. 

## What Constitutes a Seamless Tube?

"Henry Souther said, in the discussion of this question, that the scientific and technical designation of a tube, whether seamed or seamless, depended solely upon the tube itself, and not upon the process followed in its manufacture. Referring to the dictionary you will find that the word "seamless" means without seam, which conveys no light upon the subject. Turning to the word "seam" it is found that it is defined as a joint, suture, or line of union, and here in the last term we find the key. A tube jointed in any way cannot be seamless. If, in the primary stages of its manufacture, it be lap, butt or lock-jointed, it cannot by any subsequent operation be deprived of the seam, and therefore cannot be considered, when completed, as being seamless A strictly seamless tube may be made by any one of three operations. First, a billet may be, by successive steps, punched into the form of a tube with extremely thick sides; and these may then, by the ordinary drawing processes, be reduced to a tube with thin walls. Next, the billet may be bored, or the blank may be cast with a hole in it, and in either case then drawn to the required dimensions. Thirdly, the tube may be made by the cupping process, which consists in taking a disk of the metal, forming it into a cup shape, gradually elongating the cup and reducing it in diameter, and finally by this means producing a tube. Each and all of these processes yield a tube which is absolutely seamless and about which there is and can be no dispute. In all tubes formed with a seam the edges have first been separated, then united, either by lap or butt weld, or by some lock-joint system, and in these the joint cannot be eliminated by any after processes. The Custom House of the United States recognizes the difference between a seam and a seamless tube. A seamless tube is one in which the walls have never been separated from the time the metal was in a molten condition to the time of the completion of the tube."

## COLD DRAWN TUBES.

The Weight Sheet for Seamless Cold Drawn Tubes, as given on following page, is applicable for Tubes intended for many different purposes. The sizes from $3 / 8$ inch to $11 / 2$ inch diameter and from 16 to 23 gauge inclusive are generally classified as Bicycle Tubing, on account of their very general use in Bicycle construction. They are used, however, for many other different purposes. These Tubes are manufactured from Open Hearth Steel of analysis best suited for the purpose. They have a fine finish and are drawn accurate to size and gauge. These tubes are admirably adapted for all construction requiring a maximum strength and minimum weight. They have great rigidity and are suited for high transverse strains.

Tubes for boiler purposes, from 1 inch to 4 inches, and and from 13 to 6 gauge inclusive, are made of mild Open Hearth Steel, of analysis best suited to give toughness and ductility. The process of manufacture is such that only material free from laps, seams, cracks and all physical imperfections can be used. This insures a high uniformity of quality and reduces the possibility of accident, due to imperfections of material, laps and welds, to a minimum.

Tubes of thicknesses other than those given above are generally termed " Mechanical Tubes," and are used in the construction of many classes of machinery for bushings, hollow shafts and spindles, axles, collars, rings, ferrules, pump barrels, etc., etc. Often a considerable saving in machine work is effected by the use of these tubes in place of parts heretofore made by boring and turning round bars, the tubes admitting of a lighter and stronger construction than by using the former material.
Tubing for Locomotive, Marine and Stationary
Purposes. Engineering Foot of Seamless Cold Drawn
$\|$ | 4 -


## Table showing Weight per Foot in Pounds of Various Diameters and Thicknesses of HOT FINISHED TUBES.



Table showing Weight per Foot in Pounds of Various Diameters and Thicknesses of HOT FINISHED TUBES.
(CONTINUED.)

| © | THICKNESS OF WALL. |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0 \cdot \frac{\pi}{a}$ | 1/4 | ${ }^{5}$ | 3/8 | ${ }^{\frac{7}{16}}$ | 1/8 | ${ }^{18}$ | 58 | $3 / 4$ | 7/8 | 1 |
| 7 | 17.83 | 22.08 | 26.25 | 30.33 | 34.33 | 38.25 | 42.09 | 49.51 | 56.60 | 63.36 |
| 1/8 | 18.17 | 22.50 | 26.75 | 30.92 | 35.00 | 3899 | 42.92 | 50.51 | 57.79 | 64.69 |
|  | 18.50 | 22.92 | 27.25 | 81.49 | 35.67 | 39.74 | 43.75 | 51.51 | 58.95 | 66.02 |
|  | 18.83 | 23.33 | 27.75 | 32.07 | 36.33 | 40.49 | 44.58 | 52.50 | 60.11 | 67.35 |
|  | 19.16 | 23.74 | 28.24 | 32.66 | 36.99 | 41.23 | 45.41 | 53.49 | 61.27 | 68.67 |
|  | 19.49 | 24.16 | 28.74 | 33.24 | 37.66 | 41.98 | 46.24 | 54.49 | 62.43 | 70.00 |
|  | 19.82 | 24.57 | 29.24 | 33.82 | 38.32 | 42.73 | 47.07 | 55.49 | 63.57 | 71.33 |
| $7 / 8$ | 20.15 | 24.98 | 29.73 | 34.40 | 38.98 | 43.47 | 47.90 | 56.48 | 64.73 | 72.65 |
| 8 | 20.48 | 25.39 | 30.22 | 34.97 | 39.64 | 44.21 | 48.72 | 57.47 | 65.89 | 73.97 |
| $1 / 8$ | 20.80 | 25.80 | 30.71 | 35.54 | 40.29 | 44.95 | 49.54 | 58.46 | 67.04 | 75.29 |
| 14 | 21.12 | 26.20 | 31.20 | 36.11 - | 40.94 | 45.68 | 50.36 | 59.44 | 68.19 | 76.61 |
| 8 | 21.44 | 26.61 | 31.68 | 36.68 | 41.59 | 46.41 | 51.17 | 60.42 | 69.34 | 77.92 |
| $1 / 9$ | 21.77 | 27.02 | 32.17 | 37.25 | 42.25 | 47.15 | 51.99 | 61.41 | 70.49 | 79.24 |
| 5 | 22.10 | 27.44 | 32.66 | 37.82 | 42.90 | 47.89 | 52.81 | 62.39 | 71.64 | 80.56 |
|  | 22.43 | 27.85 | 33.15 | 38.39 | 43.55 | 48.62 | 53.63 | 63.37 | 72.79 | 81.87 |
| 7/8 | 22.76 | 28.26 | 33.64 | 38.96 | 44.20 | 49.36 | 54.44 | 64.35 | 73.93 | 83.18 |
| 9 | 23.08 | 28.67 | 34.13 | 39.53 | 44.85 | 50.09 | 55.25 | 65.33 | 75.07 | 84.49 |
| $1 / 8$ | 23.41 | 29.08 | 34.63 | 40.11 | 45.51 | 50.83 | 56.07 | 66.31 | 7622 | 85.80 |
|  | 23.74 | 29.48 | 35.12 | 40.69 | 46.17 | 51.57 | 56.89 | 67.29 | 77.37 | 87.11 |
| 3 | 24.07 | 29.88 | 35.61 | 41.26 | 46.83 | 52.31 | 57.71 | 68.27 | 78.51 | 88.42 |
|  | 24.40 | 30.29 | 36.10 | 41.83 | 47.48 | 53.05 | 58.53 | 69.25 | 79.65 | 89.73 |
|  | ${ }^{24}{ }^{\prime} 73$ | 30.71 | 36.60 | 42.41 | 48.14 | 53.79 | 59.36 | 70.24 | 80.80 | 91.04 |
| 3 | 25.06 | 31.12 | 37.10 | 42.99 | 48.80 | 54.53 | 60.18 | 71.23 | 81.95 | 92.35 |
| 7/8 | 25.39 | 31.53 | 37.59 | 43.57 | 49.46 | 55.27 | 61.00 | 72.22 | 83.10 | 93.66 |
| 10 | 25.72 | 31.94 | 38.08 | 44.14 | 50.12 | 56.01 | 61.82 | 73.20 | 84.25 | 94.97 |
| $1 / 8$ | 26.04 | 32.35 | 38.57 | 44.71 | 50.77 | 56.75 | 62.64 | 74.18 | 85.40 | 96.28 |
|  | 26.36 | 32.75 | 39.06 | 45.28 | 51.42 | 57.48 | 63.46 | 75.16 | 86.54 | 97.59 |
|  | 26.68 | 33.15 | 39.54 | 45.85 | 5207 | 58.21 | 64.27 | 76.14 | 87.68 | 98.90 |
|  | 27.01 | 33.56 | 40.03 | 46.42 | 52.73 | 58.95 | 65.09 | 77.13 | 88.83 | 100.21 |
|  | 27.34 | 33.97 | 40.52 | 46.99 | 53.37 | 59.69 | 65.91 | 78.11 | 89.98 | 101.52 |
|  | 27.67 | 34.38 | 41.01 | 47.56 | 54.02 | 60.42 | 66.73 | 79.09 | 91.13 | 102.83 |
| 78 | 28.00 | 34.79 | 41.50 | 48.13 | 54.68 | 61.15 | 67.54 | 80.07 | 92.27 | 104.14 |
| 11 | 28.32 | 35.20 | 41.99 | 48.70 | 55.33 | 61.88 | 68.35 | 81.05 | 93.41 | 105.45 |
|  | 28.65 | 35.61 | 42.49 | 49.28 | 55.99 | 62.62 | 69.17 | 8203 | 94.56 | 106.76 |
|  | 28.98 | 36.02 | 42.98 | 49.8 : | 56.65 | 63.36 | 69.99 | 83.01 | 95.71 | 108.07 |
|  | 29.31 | 36.43 | 43.47 | 50.44 | 57.31 | 64.10 | 70.81 | 83.99 | 96.85 | 109.38 |
|  | 29.64 | 36.84 | 43.96 | 51.01 | 57.96 | 64.84 | 71.63 | 84.97 | 97.99 | 110.69 |
|  | 29.97 | 37.26 | 44.46 | 51.59 | 58.60 | 65.58 | 72.46 | 85.96 | 99.14 | 112.00 |
|  | 30.30 | 37.67 | 44.96 | 52.17 | 59.26 | 66.32 | 73.28 | 86.95 | 100.29 | 113.81 |
| 78 | 30.63 | 38.08 | 45.45 | 52.74 | 59.92 | 67.06 | 74.10 | 87.94 | 101.44 | 114.62 |

## Table showing Weight per Foot in Pounds of Various

 Diameters and Thicknesses of HOT FINISHED TUBES.(CONTINUED.)

| 这 | THICKNESS OF WALL. |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0 \stackrel{\pi}{\square}$ | $1 / 4$ | ${ }^{5} 8$ | 3/8 | 16 | 1/2 | 16 | 5/8 | $3 / 4$ | 7/8 | 1 |
|  | 30.96 | 38.49 | 45.94 | 53.31 | 60.58 | 67.80 | 74.92 | 88.92 | 102.59 | 115.93 |
|  | 31.28 | 38.90 | 46.43 | 53.88 | 61.23 | 68.54 | 75.74 | 89.90 | 103.73 | 117.24 |
|  | 31.60 | 39.30 | 46.92 | 54.45 | 61.88 | 69.27 | 76.56 | 90.88 | 104.87 | 118.55 |
|  | 31.92 | 39.70 | 47.40 | 55.02 | 62.53 | 70.00 | 77.37 | 91.86 | 106.01 | 119.86 |
|  | 32.25 | 40.11 | 47.89 | 55.59 | 63.19 | 70.74 | 78.19 | 92.85 | 107.16 | 121.17 |
|  | 32.58 | 40.52 | 4838 | 5616 | 63.84 | 71.48 | 79.01 | 93.83 | 108.31 | 122.48 |
|  | 32.92 | 40.94 | 48.88 | 56.74 | 64.50 | 72.22 | 79.84 | 94.82 | 109.47 | 123.80 |
|  | 33.26 | 41.36 | 49.38 | 57.32 | 65.16 | 72.96 | 80.66 | 95.81 | 110.62 | 125.12 |
| 13.818 | 33.60 | 41.79 | 49.89 | 57.91 | 65.83 | 78.71 | 81.49 | 96.81 | 111.78 | 126.45 |
|  | $33.94$ | 42.21 | 50.40 | 58.50 | 66.50 | 74.46 | 82.32 | 97.80 | 112. | 127.77 |
|  | 34.28 | 42.64 | 50.91 | 59.10 | 67.18 | 75.22 | 88.16 | 98.80 | 114.11 | $129.10$ |
|  | 34.62 34.96 | 43.06 | 51.42 | 59.69 | 67.86 | 75.98 | 84.00 | 99.80 | 115.28 | 130.43 |
|  | 34.96 | 43.49 | 51.93 | 60.29 | 68.54 | 76.75 | 84.85 | 100.81 | 116. | 131.77 |
|  | 35.28 35.59 | 43.89 44.29 | 52.42 52.90 | 60.86 61.43 | 69.20 69.85 | 77.49 | 85.68 | 101.80 | 117.60 | $\begin{aligned} & 133.08 \\ & 134.39 \end{aligned}$ |
|  | 35.90 | 44.68 | 53.38 | 61.99 | 70.50 | 78.96 | 87.32 | 103.78 | 119.90 | 135.70 |
| 1 | 36. | 45. | 53.85 | 62.55 | 71.14 | 79.69 | 88.13 | 104.76 | 121.05 | 137.01 |
|  | 36.52 | 45.45 | 54.32 | 63.10 | 71.78 | 80.41 | 88.94 | 105.74 | 122.20 | 138.32 |
|  | 36.85 | 45.86 | 54.79 | 63.66 | 72.42 | 81.14 | 89.75 | 106.72 | 123.35 | 139.64 |
|  | 37.19 | 46.28 | 55.29 | 64.22 | 73.07 | 81.87 | 90.57 | 107.71 | 124.51 | 140.97 |
|  | 37.54 | 46.71 | 55.80 | 64.81 | 78.72 | 8.2.61 | 91.39 | 108.70 | 125.67 | 142.30 |
|  | ${ }_{38}^{37.90}$ | 47.15 | 56.32 | 65.41 | 74.40 | 83.35 | 92.22 | 109.70 | 126.84 | 143.64 |
|  | 38.25 | 47.59 | 56.84 | 66.01 | 75.08 | 84.11 | 93.04 | 110.69 | 128 | 144.97 |
|  | 38.60 | 48.03 | 57.37 | 66.62 | 75.77 | 84.88 | 93.89 |  |  |  |
| 15$1 / 8$18388818587488 | 38.94 | 48.46 | 57.89 | 67.23 | 76.46 | 85.65 | 94.74 | 112.68 | 130.33 | 147.64 |
|  | 3927 | 48.88 | 58.40 | 67.83 | 77.15 | 86.42 | 95.59 | 113.69 | 131.49 | 148.97 |
|  | 39.60 | 49.79 | 58.90 | 68.42 | 77.83 | 87.19 | 96.44 | 114.70 | 132.64 | 150.29 |
|  | 39.92 | 49.70 | 59.39 | 69.00 | 78.50 | 87.95 | 97.29 | 115.71 | 133.81 | 151.61 |
|  | 40.24 | 50.10 | 59.88 | 69.57 | 79.16 | 88.70 | 98.13 | 116.72 | 134.98 | 152.92 |
|  | 40.56 | 50.50 | 60.36 | 70.14 | 79.81 | 89.41 | 98.96 | 117.73 | 136.15 | 154.25 |
|  | 40.88 | 50.90 | 60.84 | 70.70 | 80.46 | 9017 | 99.78 | 118.73 | 137.32 | 155.58 |
|  | 41.20 | 51.30 | 61.32 | 71.26 | 81.12 | 90.90 | 100.59 | 119.72 |  | 156.91 |
| 16 | 41.52 | 51.70 | 61.80 | 71.82 | 81.76 | 91.62 | 101.40 | 120.70 | 139.65 | 158.24 |
|  | 41.84 | 52.10 | 62.28 | 72.38 | 82.40 | 92.34 | 102.20 | 121.67 | 140 | 159.57 |
|  | 42.14 | 52.48 | 62.74 | 72.92 | 83.02 | 93.04 | 102.98 | 122.62 | 141.92 | 160.87 |
|  | 42.45 | 52.87 | 63.21 | 73.47 | 83.65 | 93.75 | 103.77 | 123.57 | 143.04 | 162.17 |
|  | 4276 | 53.26 | 63.68 | 74.02 | 84.28 | 94.45 | 104.56 | 124.52 | 144.16 | 163.46 |
|  | 43.13 | 53.71 | 64.21 | 74.63 | 84.97 | 95.23 | 105.41 | 125.53 | 145.33 | 164.80 |
|  | 43.47 | 54.11 | 64.69 | 75.19 | 85.61 | 95.95 | 106.21 | 126.49 | 146.45 | 166.09 |
| 78 | 43.82 | 54.55 | 65.19 | 75.77 | 86.27 | 96.69 | 107.03 | 127.47 | 147.59 | 167.39 |
| 17 | 44.19 | 55.00 | 65.73 | 76.37 | 86.95 | 97.45 | 107.87 | 128.47 | 148.75 | 168.71 |

Table Showing Weight Per Foot in Lbs. of Various Diameters and Gauges of

| B. W. G. | 0 | 1 | 2 | 8 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Decimal of 1 Inch. | . 34 | . 3 | . 284 | . 259 | . 238 | . 220 | . 203 | . 180 | . 165 | . 148 | . 131 | . 120 | . 109 | . 095 | . 083 | .072 | . 065 | . 058 | . 049 |
| Nearest Fraction of 1 Inch. | ${ }^{\frac{11}{3}}$ | 192 | $\frac{9}{32}$ | $\frac{17}{6}$ | $\frac{1}{6} \frac{5}{4}$ | ${ }^{\frac{7}{32}}$ | $\frac{1}{64}$ | $\frac{3}{16}$ | $\frac{11}{6}$ | $\frac{9}{84}$ | ${ }^{17}$ | 1/8 | ${ }^{7} 8$ | $3^{32}$ | ${ }_{12}^{12}$ | ${ }^{86}$ | $\frac{1}{18}$ | 1788 | $\frac{3}{64}$ |
| Outside Diam. |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $1 / 8$ | 2.82 | 2.61 | 2.51 | 2.34 | 2.23 | 2.10 | 1.97 | 1.79 | 1.68 | 1.53 | 1.41 | 1.27 | 1.17 | 1.03 | 0.91 | 0.80 | 0.72 | 0.64 | 0.55 |
|  | 3.27 | 3.01 | 2.88 | 2.68 | 2.54 | 2.38 | 2.23 | 2.02 | 1.87 | 1.72 | 1.58 | 1.42 | 1.31 | 1.15 | 1.02 | 0.90 | 081 | 0.72 | 0.61 |
|  | 8.72 | 3.40 | 3.26 | 3.02 | 2.85 | 266 | 2.49 | 2.25 | 2.08 | 1.91 | 1.75 | 157 | 1.45 | 1.27 | 1.18 | 0.99 | 0.89 | 0.79 | 0.68 |
|  | 4.17 | 3.80 | 3.63 | 3.36 | 3.16 | 2.96 | 2.76 | 2.49 | 2.30 | 2.10 | 1.93 | 1.73 | 1.59 | 1.40 | 1.24 | 1.09 | 0.98 | 0.87 | 074 |
|  | 4.62 | 4.19 | 4.00 | 3.70 | 3.48 | 3.25 | 3.03 | 2.72 | 2.51 | ${ }_{2}^{2} 30$ | 2.10 | 1.89 | 178 | 1.52 | 1.35 | 1.18 | 1.06 | 0.95 | 0.81 |
|  | 5.07 | 4.59 | 4.38 | 4.04 | 3.79 | 3.54 | 329 | 2.96 | 2.73 | 2.49 | 2.28 | 2.05 | 1.88 | 1.65 | 1.46 | 1.28 | 1.15 | 1.02 | 0.87 |
| 378 | 5.52 | 4.98 | 4.75 | 4.38 | 4.11 | 3.84 | 3.56 | 3.20 | 2.95 | . 2.69 | 2.46 | 2.21 | 2.02 | 1.77 | 1.57 | 1.37 | 1.24 | 1.10 | 0.94 |
| 2 | 5.97 | 5.38 | 5.12 | 4.72 | 4.42 | 3.13 | 3.88 | 3.43 | 3.16 | 2.88 | 2.63 | 2.36 | 2.16 | 1.90 | 1.68 | 1.47 | 1.32 | 1.18 | 1.00 |
| $1 / 8$ | 6.42 | 5.77 | 5.50 | 5.06 | 4.74 | 4.41 | 4.09 | 3.67 | 3.38 | 3.08 | 2.81 | 2.52 | 2.31 | 2.02 | 1.79 | 1.56 | 1.41 | 1.25 | 1.07 |
|  | 6.87 | 6.17 | 5.87 | 5.40 | 5.05 | 4.70 | 4.36 | 3.91 | 3.60 | 3.27 | 2.98 | 2.68 | 2.45 | 2.15 | 1.90 | 1.66 | 1.49 | 1.33 | 1.13 |
|  | 7.31 | 6.56 | 6.24 | 5.74 | 5.36 | 4.99 | 4.63 | 4.14 | 3.81 | 3.46 | 3.16 | 2.84 | 2.59 | 2.27 | 2.01 | 1.75 | 1.58 | 1.40 | 1.20 |
|  | 7.76 | 6.96 | 6.62 | 6.08 | 5.69 | 5.28 | 489 | 4.38 | 4.03 | 3.66 | 3.34 | 3.00 | 2.74 | 2.40 | 2.12 | 1.85 | 1.66 | 1.48 | 1.26 |
|  | 8.21 | 7.35 | 6.99 | 6.42 | 6.00 | 5.57 | 5.16 | 4.62 | 4.25 | 3.85 | 3.51 | 3.15 | 2.88 | 2.52 | 2.23 | 1.94 | 1.75 | 1.56 | 1.33 |
|  | 8.66 | 7.74 | 7.36 | ${ }^{6} .76$ | 6.32 | 5.80 | 5.43 | 4.85 | 4.46 | 4.05 | 3.69 | 3.31 | 3.02 | 265 | 2.34 | 2.04 | 1.84 | 1.63 | 1.39 |
|  | 9.11 | 8.23 | 7.74 | 7.10 | ${ }^{6.63}$ | 6.14 | 5.69 | 5.03 | 4.68 | 4.24 | 386 | 3.47 | 3.16 | 2.77 | 2.45 | 2.13 | 1.92 | 1.71 | 1.46 |
|  | 9.56 | 8.63 | 8.11 | 7.44 | ${ }^{6.95}$ | 6.43 | 5.96 | 5.32 | 4.90 | 4.44 | 4.04 | 363 | 3.31 | 2.90 | 2.56 | 2.23 | 2.01 | 1.79 | 1.52 |
| 1/8 | 10.03 | 9.02 | 8.48 | 7.78 | 7.26 | 6.72 | 6.23 | 5.56 | 5.11 | 4.63 | 4.22 | 3.79 | 3.45 | 3.02 | 2.67 | 2.32 | 2.09 | 1.86 | 1.58 |


T＇able Showing Weight Per Foot in Lbs．of Various Diameters and Gauges of

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| $\stackrel{20}{7}$ | \％ | 0 |  <br>  |
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| $\infty$ | $\underset{\sim}{4}$ | 筬 | ふ ふ0 0iosoco |
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| $\begin{aligned} & \dot{0} \\ & \dot{B} \end{aligned}$ |  |  |  |

NATIONAL TUBE COMPANY.


NATIONAL TUBE COMPANY．
Table Showing Weight Per Foot in Lbs．of Various Diameters and Gauges of

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| 4 | 处 | $\sim_{*}^{*}$ |  <br>  |
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| 0 | \％ | － |  <br>  |
| $\begin{gathered} \text { 4. } \\ \text { M } \end{gathered}$ |  |  |  |

## TABLE OF LENGTHS AND WEIGHTS OF WORKING BARRELS.



| Length in Feet. | 2 Inch Barrel Weight in lbs. |  |  | 21/2 Inch Barrel Weight in lbs. |  |  | 3 Inch Barrel Weight in lbs. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5 |  | to |  |  | to |  | 47 | to | 55 |
| 6 |  | " |  | 43 | " |  | 54 | " |  |
| 7 | 38 | '، |  |  | ، |  | 61 | " | 69 |
| 8 | 41 | " |  |  | " |  | 68 | " | 76 |
| 9 | 44 | " |  |  | " |  | 75 | ' | 83 |

## ILLUSTRATIONS

OF

## Standard and Special Seamless Cylinders.


${ }_{2}^{x} 5$ inch Standard Seamless Cylinder.
(See Table, page 84.)


8 inch Standard Seamless Cylinder.
(See Table, page 85.)


## 8 inch Special Seamless Cylinder.

(See Table, page 86.)

## Table of Weights and Capacities of 5 inch Standard Seamless Cylinders.

Outside Diameter, $5_{18}{ }^{\circ}$ inches. Thickness of Wall, $\frac{13}{8}$ inch. (See illustration, page 83.)
Tested to 3700 lbs . per square inch Hydrostatic Pressure.

| Length over all in inches. | Average Weight in lbs. | Capacity in Cubic inches. | Capacity in Cubic feet. | Capacity in U.S. Gallons. | Capacity in lbs. Liquid Carbonic Acid Gas. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 36 | 39.00 | 653 | 0.8779 | 2.88 | 15. |
| 361/2 | 39.47 | 663 | 0.3839 | 2.87 | 15.2 |
| 37 | 39.94 | 673 | 0.3900 | 2.92 | 15.4 |
| 371/2 | 40.41 | 683 | 0.8961 | 2.96 | 15.6 |
| 38 | 40.88 | 694 | 0.4022 | 3.01 | 15.8 |
| 381/8 | 41.35 | 704 | 0.4083 | 3.05 | 16. |
| 39 | 41.82 | 714 | 0.4143 | 3.10 | 16.4 |
| 391/2 | 42.29 | 725 | 0.4204 | 3.14 | 16.4 |
| 40 | 42.76 | 735 | 0.4265 | 3.19 | 16.6 |
| 401/2 | 43.23 | 745 | 0.4326 | 3.23 | 16.8 |
| 41 | 43.71 | 756 | 0.4387 | 3.28 | 17. |
| 411/3 | 44.18 | 766 | 0.4447 | 3.32 | 17.2 |
| 42 | 44.65 | 776 | 0.4508 | 3.37 | 17.4 |
| 421/2 | 45.12 | 786 | 0.4569 | 3.41 | 17.6 |
| 43 | 45.59 | 797 | 0.4630 | 3.46 | 17.8 |
| 431/2 | 46.06 | 807 | 0.4691 | 3.50 | 18. |
| 44 | 46.53 | 817 | 0.4751 | 3.55 | 18.2 . |
| 441/2 | 47.00 | 828 | 0.4812 | 3.59 | 18.4 |
| 45 | 47.47 | 838 | 0.4873 | 3.64 | 18.6 |
| 451/3 | 47.94 | 848 | 0.4934 | 3.68 | 18.8 |
| 46 | 48.42 | 859 | 0.4995 | 3.73 | 19. |
| 461/2 | 48.89 | 869 | 0.5055 | 3.77 | 19.2 |
| 47 | 49.36 | 879 | 0.5116 | 3.81 | 19.4 |
| 471/3 | 49.83 | 889 | 0.5177 | 3.85 | 19.6 |
| 48 | 50.30 | 900 | 0.5238 | 3.90 | 19.8 |
| 481/2 | 50.77 | 910 | 0.5299 | 3.94 |  |
| 49 | 51.24 | 920 | 0.5359 | 3.99 | 20.2 |
| 491/2 | 51.71 | 981 | 0.5420 | 4.03 | 20.4 |
| 50. | 52.18 | 941 | 0.5481 | 4.08 | 20.6 |
| 501/2 | 52.65 | 951 | 0.5542 | 4.12 | 20.8 |
| 51. | 53.13 | 962 | 0.5603 | 4.17 | 21. |
| 511/3 | 53.60 | 972 | 0.5663 | 4.21 | 21.2 |
| 52 | 54.07 | 982 | 0.5724 | 4.26 | 21.4 |
| 521/2 | 54.54 | 992 | 0.5785 | 4.30 | 21.6 |
| 53 | 55.01 | 1003 | 0.5846 | 4.35 | 21.8 |
| 531/2 | 55.48 | 1013 | 0.5907 | 4.39 |  |
| 54 | 55.95 | 1023 | 0.5967 | 4.44 | 22.2 |
| 5416 | 56.42 | 1034 | 0.6028 | 4.48 | 22.4 |
| 55 | 56.89 | 1044 | 0.6089 | 4.53 | 22.6 |
| 551/3 | 57.36 | 1054 | 0.6150 | 4.57 | 22.8 |
| 56 | 57.84 | 1065 | 0.6211 | 4.62 | 23. |
| 561/2 | 58.81 | 1075 | 0.6271 | 4.66 | 23.2 |
| 57 | 58.78 | 1085 | 0.6332 | 4.71 | 23.4 |
| 571/2 | 59.25 | 1095 | 0.6393 | 475 | 23.6 |
| 58 | 59.72 | 1106 | 0.6454 | 4.80 | 23.8 |
| 581/2 | 60.19 | 1116 | 0.6515 | 4.84 | 24. |
| 59 | 60.66 | 1126 | 0.6575 | 4.89 | 24.2 |
| ${ }_{60}^{591 / 2}$ | 61.18 | 1137 | 0.6636 0.6697 | 4.93 4.97 | 24.4 24.6 |
| 60 | 61.60 | 1147 | 0.6697 | 4.97 | 24.6 |

## Table of Weights and Capacities of 8 inch Standard

## Seamless Cylinders.

Outside Diameter, $8_{{ }^{9} 8}$ inches. Thickness of Wall, ${ }_{37}^{3}$ inch.
(See illustration, page 83.)
Tested to 3700 lbs . per square inch Hydrostatic Pressure.

| Length over all in inches. | Average Weight in lbs. | Capacity in Cubic inches. | Capacity in Cubic feet. | Capacity in U. S. Gallons. | Capacity in lbs. Liquid Carbonic Acid Gas. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 36 | 69.4 | 1781 | 1.0307 | 7.71 | 37. |
| 361/2 | 70.25 | 1806 | 1.0454 | 7.82 | 37.5 |
| 37 | 71.1 | 1832 | 1.0601 | 7.94 | 38. |
| 371/2 | 71.95 | 1857 | 1.0783 | 8.05 | 88.5 |
| 38 | 72.8 | 1883 | 1.0895 | 8.16 | 39. |
| 381/2 | 73.65 | 1908 | 1.1042 | 8.27 | 99.5 |
| 39 | 74.5 | 1934 | 1.1189 | 8.38 | 40. |
| 391/2 | 75.35 | 1952 | 1.1336 | 8.49 | 40.5 |
| 40 | 76.2 | 1985 | 1.1483 | 8.60 | 41. |
| 401/2 | 77.05 | 2010 | 1.1630 | 8.71 | 41.5 |
| 41 | 77.9 | 2036 | 1.1778 | 8.82 | 42. |
| 411/2 | 78.75 | 2061 | 1.1925 | 8.93 | 42.5 |
| 42 | 79.7 | 2087 | 1.2072 | 9.04 | 43. |
| 4216 | 80.55 | 2112 | 1.2219 | 9.15 | 43.5 |
| 43 | 81.4 | 2138 | 1.2368 | 9.26 | 44. |
| 431/8 | 82.25 | 2163 | 1.2515 | 9.37 | 44.5 |
| 44 | 83.1 | 2189 | 1.2662 | 9.48 | 45. |
| 441/2 | 83.95 | 2214 | 1.2809 | 9.59 | 45.5 |
| 45 | 84.8 | 2240 | 1.2956 | 9.70 | 46. |
| 451/3 | 85.65 | 2265 | 1.3103 | 9.81 | 46.5 |
| 46 | 86.5 | 2291 | 1.3251 | 9.92 | 47. |
| 461/2 | 87.35 | 2316 | 1.3398 | 10.03 | 47.5 |
| 47 | 88.2 | 2342 | 1.3545 | 10.14 | 48. |
| 4719 | 89.05 | 2367 | 13692 | 10.25 | 48.5 |
| 48 | 89.9 | 2393 | 1.3839 | 10.36 | 49. |
| 481/2 | 90.75 | 2418 | 1.8966 | 10.47 | 49.5 |
| 49 | 91.6 | 2444 | 1.4113 | 10.58 | 50. |
| 491/2 | 92.45 | 2469 | 1.4260 | 10.69 | 50.5 |
| 50 | 93.3 | 2495 | 1.4407 | 10.80 | 51. |
| 501/2 | 94.1 | 2520 | 1.4554 | 10.91 | 51.5 |
| 51 | 95. | 2546 | 1.4702 | 11.02 | 52. |
| $511 / 2$ | 95.85 | 2571 | 1.4849 | 11.13 | 52.5 |
| 52 | 96.7 | 2597 | 1.4996 | 11.24 | 53. |
| 521/2 | 97.55 | 2622 | 1.5143 | 11.35 | 53.5 |
| 53 | 98.4 | 2648 | 1.5290 | 11.46 | 54. |
| $531 / 2$ | 99.25 | 2673 | 1.5437 | 11.57 | 54.5 |
| 54 | 100.1 | 2699 | 1.5585 | 11.68 | 55. |
| 541/2 | 100.95 | 2724 | 1.5732 | 11.79 | 55.5 |
| 55 | 101.8 | 2750 | 1.5879 | 11.90 | 56. |
| $551 / 8$ | 102.65 | 2775 | -1.6026 | 12.01 | 56.5 |
| 56 | 103.5 | 2801 | 1.6174 | 12.12 | 57. |
| 561/3 | 104.35 | 2826 | 1.6321 | 12.23 | 57.5 |
| 57 571 | 105.2 106.05 | 2852 | 1.6468 | 12.34 12.45 | 58. |
| 5712 58 | 106.05 106.9 | 2877 | 1.6615 1.6762 | 12.45 | 58.5 59. |
| 581/2 | 107.75 | 2928 | -1.6909 | 12.67 | 59.5 |
| 59 | 108.6 | 2954 | [1.7056 | 12.78 | 60. |
| $591 / 8$ | 109.45 | 2979 | 1.7203 | 12.89 | 60.5 |
| 60 | 110.5 | 3005 | 1.7303 | 13.00 | 61. |

## Table of Weights and Capacities of 8 inch Special Seamless

## Cylinders for Holding Carbonic Gas.

Outside Diameter, 8 inches. Thickness of Wall, ${ }_{3 \pi}^{75}$ inch.
(See illustration, page 83.)
Tested to 3000 lbs . per square inch Hydrostatic Pressure.

| Length over all in inches. | Average Weight in lbs. | Capacity in Cubic inches. | Capacity in Cubic feet. | Capacity in U. S. Gallons. | Capacity in lbs. Liquid Carbonic Acid Gas. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 36 | 74.2 | 1459 | . 8448 | 6.31 | 30. |
| 361/3 | 75.0 | 1482 | .8573 | 6.41 | 30.4 |
| 37 | 75.8 | 1504 | . 8703 | 6.51 | 30.9 |
| 371/2 | 76.6 | 1526 | . 8833 | 6.60 | 31.3 |
| 38 | 77.4 | 1549 | . 8963 | 6.70 | 31.8 |
| 381/2 | 78.2 | 1571 | . 9093 | 6.80 | 32.2 |
| 39 | 79.0 | 1594 | . 9223 | 6.89 | 32.7 |
| 391/2 | 79.8 | 1616 | . 9353 | 6.99 | 33.1 |
| 40 | 80.6 | 1639 | . 9483 | 7.09 | 33.6 |
| 401/2 | 81.4 | 1661 | . 9613 | 7.19 | 34. |
| 41 | 82.2 | 1684 | . 9744 | 7.28 | 34.5 |
| 411/2 | 83.0 | 1706 | . 9874 | 7.38 | 34.9 |
| 42 | 83.8 | 1729 | 1.0004 | 7.48 | 35.4 |
| 421/2 | 84.6 | 1751 | 1.0134 | 7.58 | 35.8 |
| 43 | 85.4 | 1773 | 1.0264 | 7.68 | 36.3 |
| 431/2 | 86.2 | 1796 | 1.0394 | 7.77 | 36.7 |
| 44 | 87.0 | 1818 | 1.0524 | 7.87 | 37.2 |
| 441/2 | 87.8 | 1841 | 1.0654 | 7.96 | 37.6 |
| 45 | 88.6 | 1863 | 1.0784 | 8.06 | 38.1 |
| 451/2 | 89.4 | 1886 | 1.0914 | 8.16 | 38.5 |
| 46 | 90.2 | 1908 | 1.1045 | 8.26 | 39. |
| 461/2 | 91.0 | 1931 | 1.1175 | 8.35 | 89.4 |
| 47 | 91.8 | 1953 | 1.1305 | 8.45 | 39.9 |
| 4716 | 92.6 | 1976 | 1.1435 | 8.55 | 40.3 |
|  | 93.4 | 1998 | 1.1565 | 8.65 | 40.8 |
| 481/2 | 94.2 | 2020 | 1.1695 | 8.74 | 41.2 |
| 49 | 95.0 | 2043 | 1.1825 | 8.84 | 41.7 |
| 491/2 | 95.8 | 2067 | 1.1955 | 8.94 | 42.1 |
| 50 | 96.6 | 2090 | 1.2085 | 9.04 | 42.6 |
| 501/2 | 97.4 | 2112 | 1.2215 | 9.13 | 43.0 |
| 51 | 98.2 | 2135 | 1.2346 | 9.23 | 43.5 |
| $511 / 2$ | 99.0 99.8 | 2157 | 1.2476 1.2606 | 9.33 9.42 | 43.9 44.3 |
| 52 | 99.8 100.6 | 2180 | 1.2606 1.2736 | 9.42 9.52 | 44.3 44.8 |
| 521/8 | 100.6 101.4 | 2202 | 1.2736 1.2866 | 9.52 9.62 | 44.8 45.2 |
| 531/2 | 102.2 | 2247 | 1.2996 | 9.72 | 45.7 |
| 54 | 103.0 | 2269 | 1.8126 | 9.81 | 46.1 |
| 541/2 | 103.8 | 2292 | 1.3256 | 9.91 | 46.6 |
| 55 | 104.6 | 2314 | 1.3386 | 10.01 | 47.0 |
| 551/2 | 105.4 | 2337 | 1.3516 | 10.11 | 47.5 |
| 56 | 106.2 | 2359 | 1.3647 | 10.20 | 479 |
| 561/8 | $10^{\prime \prime} .0$ | 2381 | 1.3777 | 10.30 | 48.4 |
| 57 | 107.8 | 2403 | 1.3907 | 10.40 | 48.8 |
| $571 / 2$ | 108.6 | 2426 | 1.4037 | 10.49 | 49.3 |
| 58 | 109.4 | 2449 | 1.4167 | 10.59 | 49.7 |
| $581 / 2$ 59 | 110.2 | 2471 | 1.4297 | 10.69 | 502 |
| $59.1 / 2$ | 111.0 111.8 | 2493 2516 | 1.4427 | 10.79 10.88 | 50.6 |
| 60 | 112.6 | 2538 | 1.4687 | 10.98 | 51.5 |

## Table of Weights and Capacities of Seamless Cylinders

 of various diameters.

Tested 3700 lbs. per square inch Hydrostatic Pressure.


## Table of Weights and Capacities of Seamless Cylinders

of various diameters.
(COntinued.)


## Table of Weights and Capacities of 5 inch Standard Lap-Welded Cylinders (Class B).

Outside Diameter, $5_{16}^{9}$ inches. Thickness of Wall, $1 / 4 \mathrm{inch}$.


Tested to 3700 lbs. per square inch Hydrostatic Pressure.

| Length over all in inches. | Average Weight in lbs. | Capacity in Cubic inches. | Capacity in Cubic fect. | Capacity in U.S. Gallons. | Capacity in lbs. Liquid Carbonic Acid Gas. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 36 | 49.14 | 618. | 0.3576 | 2.68 | 14. |
| 361/2 | 49.67 | 628. | 0.3636 | 2.72 | 14.2 |
| 37 | 50.20 | 638. | 0.3696 | 2.77 | 14.4 |
| 371/2 | 50.73 | 648. | 0.3756 | 2.81 | 14.6 |
| 38 | 51.26 | 658. | 0.3816 | 2.86 | 14.8 |
| $381 / 2$ | 51.79 | 668. | 0.3876 | 2.90 | 15. |
| 39 | 52.32 | 679. | 0.3930 | 2.95 | 15.2 |
| 391/2 | 52.85 | 689. | 0.3996 | 2.99 | 15.4 |
| 40 | 53.38 | 699. | 0.4056 | 3.04 | 15.6 |
| 401/2 | 53.91 | 709. | 0.4116 | 3.08 | 15.8 |
| 41 | 54.44 | 719. | 0.4176 | 3.13 | 16. |
| 411/2 | 54.97 | 730. | 0.4236 | 3.17 | 16.2 |
| 42 | 55.50 | 740. | 0.4296 | 3.22 | 16.4 |
| 421/2 | 56.03 | 750. | 0.4356 | 3.26 | 16.6 |
| 43. | 56.56 | 760. | 0.4416 | 3.31 | 16.8 |
| 431/2 | 57.09 | 770. | 0.4476 | 3.35 | 17. |
| 44 | 57.62 | 781. | 0.4536 | 3.40 | 17.2 |
| 441/2 | 58.15 | 791. | 0.4596 | 3.44 | 17.4 |
| 45 | 58.68 | 801. | 0.4656 | 3.49 | 17.6 |
| 451/8 | 59.21 | 811. | 0.4716 | 3.53 | 17.8 |
| 46 | 59.74 | 821. | 0.4776 | 3.58 | 18. |
| 461/2 | 60.27 | 831. | 0.4836 | 3.62 | 18.2 |
| $4{ }^{3}$ | 60.80 | 842. | 04896 | 8.67 | 18.4 |
| 471/2 | 61.33 | 852. | 0.4956 | 3.71 | 18.6 |
| 48 | 61.86 | 862. | 0.5016 | 3.76 | 18.8 |
| 481/3 | 62.39 | 872. | 0.5076 | 3.80 | 19. |
| 49 | 62.92 | 882. | 0.5136 | 3.85 | 19.2 |
| 491/2 | 63.45 | 892. | 0.5196 | 3.89 | 19.4 |
| 50 | 63.98 | 903. | 0.5256 | 3.94 | 19.6 |
| 501/2 | 64.51 | 913. | 0.5316 | 3.98 | 19.8 |
| 51. | 6504 | 923. | 0.5376 | 4.03 | 20. |
| 511/2 | 65.57 | 933. | 0.5436 | 4.07 | 20.2 |
| 52 | 66.10 | 943. | 0.5496 | 4.12 | 20.4 |
| 521/2 | 66.63 | 954. | 0.5556 | 4.16 | 20.6 |
| 53 | 67.16 | 964. | 0.5616 | 4.21 | 20.8 |
| $531 / 2$ | 67.69 | 974. | C. 5676 0.5736 | 4.26 | 21. |
| 54. | 68.22 | 984. | 0.5736 | 4.31 | 21.2 |
| 5416 | 68.75 | 994. | 0.5796 | 4.35 | 21.4 |
| ${ }_{5516}$ | 69.28 69.81 | 1005. | 0.5856 0.5916 | 4.40 4.44 | 21.6 21.8 |
| 56 | 70.84 | 1025. | 0.5916 0.5976 | 4.48 | 21.8 |
| 561/2 | 70.87 | 1035. | 0.6036 | 4.52 | 22.2 |
| 57 | 71.40 | 1045. | 0.6096 | 457 | 22.4 |
| 571/2 | 71.93 | 1055. | 0.6156 | 4.61 | 22.6 |
| 58 | 72.46 | 1066. | 0.6216 | 4.66 | 22.8 |
| 581/2 | 72.99 | 1076. | 0.6276 | 4.70 | 23. |
| 59 | 78.52 | 1086. | 0.6336 | 4.73 | 23.2 |
| 591/8 | 74.05 | 1096. | 0.6396 | 4.76 | 23.4 |
| 60 | 74.58 | 1106. | 0.6456 | 4.80 | 23.6 |

## Illustrations of Various Hydraulic Forgings. <br> Various Styles of Valve Protecting Caps used on Carbonic Acid Gas Cylinders.



These Caps are made of light material in various sizes, suitable for the Valves of Cylinders.

## Boiler Shells.



These Shells are made in various sizes from $6^{\prime \prime}$ Diameter, by ${ }^{1}$ foot long, to $24^{*}$ Diameter, $x$ 3 feet long. They are made from Steel of 55,000 to 60,000 Tensile Strength.

Seamless Floats For Feed Water Regulators.


These Floats are made from Steel of High Tensile Strength, so as to make them as light as possible. They are subjected to a Hydrostatic Collapsing Test of sco lbs. per square inch.

## Shrapnel Forging.



These iShrapnels are made of $a_{a}^{*}$ Special Grade of Steel, and Forged from a Solid Billet.

Shrapnel Forging.


These Shrapnels are made of a Special Grade of Steel, and Forged from a Solid Billet.

Shrapnel Forging.


These Shrapnels are made of a Special Grade of Steel, and Forged from a Solid Billet.

## Illustrations of Various Hydraulic Forgings.

 Projectile Forging.

Made from Special Grade of Steel, and Forged from a Solid Billet.

Bushing Forging for Axle Bearings.


These are made from High Grade Steel, and forged from a Solid Billet.

Separator T'ubular Forging.

## Separator Bowl Forging.



These Bowls are made from High Grade Steel of 85,000 to 90,000 Tensile Strength.
Separator Bowl Forging.
Separator Bowl Forging.


These Bowls are made from High Grade Steel of 85,000 to 90,000 Tensile Strength.


These Bowls are made from High Grade Steel of 85,000 to 90,000 Tensile Strength.


# USEFUL INFORMATION 

RELATING CHIEFLY TO

## Tubular Construction <br> COMPILED BY <br> NATIONAL TUBE CO.

## WATER.

Water is composed of two gases, hydrogen and oxygen, in the ratio of two volumes of former to one of the latter. It is never found pure in nature, owing to the readiness with which it absorbs impurities from the air and soil. Water boils under atmospheric pressure ( 14.7 lb .) at $212^{\circ}$, passing off as steam. Its greatest density is at $39.1^{\circ} \mathrm{F}$., when it weighs 62.425 lbs . per cubic ft .

## Weight of Water per Cubic Foot at Different Temperatures.

|  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $32^{\circ}$ | 62.42 | $140^{\circ}$ | 61.37 | $240^{\circ}$ | 59.10 | $350^{\circ}$ | 55.52 | $460^{\circ}$ | 51.26 |
| 40 | 62.42 | 150 | 61.18 | 250 | 58.81 | 360 | 55.16 | 470 | 50.85 |
| 50 | 62.41 | 160 | 60.98 | 260 | 58.52 | 370 | 54.79 | 480 | 50.44 |
| 60 | 62.37 | 170 | 60.77 | 270 | 58.21 | 380 | 54.41 | 490 | 50.05 |
| 70 | 62.31 | 180 | 60.55 | 280 | 57.90 | 390 | 54.03 | 500 | 49.61 |
| 80 | 62.23 | 190 | 60.32 | 290 | 57.59 | 400 | 53.64 | 510 | 49.20 |
| 90 | 62.13 | 200 | 60.07 | 300 | 57.26 | 410 | 53.26 | 520 | 4878 |
| 100 | 62.02 | 210 | 59.82 | 310 | 56.93 | 420 | 52.86 | 530 | 48.36 |
| 110 | 61.89 | 212 | 59.71 | 320 | 56.58 | 430 | 52.47 | 540 | 47.94 |
| 120 | 61.74 | 220 | 59.64 | 330 | 56.24 | 440 | 52.07 | 550 | 47.52 |
| 130 | 61.56 | 230 | 59.37 | 340 | 55.88 | 450 | 51.66 | 560 | 47.10 |

One ft . of water column at $39^{\circ} .1 \mathrm{~F}=62.425 \mathrm{lbs}$. on the square ft .

| " | " | " | " | " | -0.4335 " " " " |
| :--- | :--- | :--- | :--- | :--- | :--- |
| " | " | " | " | " | -0.0295 atmospheric pressure |
| " | " | " | " | -0.8826 in. mercury column at |  |
| $32^{\circ} . \mathrm{F}$. |  |  |  |  |  |

" $\quad=773.3 \mathrm{ft}$. of air column at $32^{\circ} . \mathrm{F}$. and atmospheric pressure.
One lb. pressure on sq. $\mathrm{ft} .=0.01602 \mathrm{ft}$. water column at $39.1^{\circ} \mathrm{F}$. " " " " " in $=2.307$ " " " " $39.1^{\circ} \mathrm{F}$.
One atmospheric pressure $=29.92 \mathrm{in}$. mercury column -33.9 ft . water column.
One inch of mercury column at $32^{\circ} \mathrm{F}$. -1.133 ft water column. One foot of air column at $32^{\circ} \mathrm{F}$. and 1 atmospheric pressure 0.001293 ft . water column.

## BOILER INCRUSTATION AND CORROSION.

Water, from natural sources, as a rule contains more or less carbon dioxide, which holds in solution carbonates of lime and magnesia. On boiling the water, the carbon dioxide is driven out and the lime and magnesium in solution are thrown down in the form of a white or grayish mud, that may be easily removed from the boiler by thorough washing. The presence of other impurities, such as organic matter or sulphate of lime, is likely to make the deposit hard and adhering.

Sulphate of lime is more soluble in cold than in hot water, and is entirely thrown down at a temperature of $280^{\circ}$ Fahrenheit. It forms a hard and adhering scale and has a bad effect upon scales and deposits, composed chiefly of carbonates.

The evident treatment of water containing sulphate of lime is to heat the feed water, before entering the boiler, to a temperature of at least $280^{\circ}$ Fahrenheit. This should be done in such a manner as to give time for the deposition of the sulphate of lime when thrown out of solution.

A deposition may arise from the settling of clay and other matter held in suspension in the water. In water otherwise free from impurities this matter commonly deposits in the form of a soft mud that may be easily removed from the boiler. In conjunction, however, with other impurities, as, for example, sulphate of lime, it may form an adhesive scale, in which case it is usually best to free the feed water from suspended matter by filtration.

In some cases chemical treatment, either internally or externally, should be resorted to. This is especially the case with feed waters containing much free acid, in which case the free acid should be neutralized by chemical treatment, preferably before entering the boiler.

If more than 100 parts per 100,000 of total solid residue be present in the water, it will ordinarily cause trouble from scale, and should be condemned for use in the boiler unless a better supply be unattainable. Scale reduces the efficiency of the heating surface by detracting from the conducting quality of the metal and is apt to cause overheating or burning of the metal, or even bulging of the plates that are subjected to the intense heat of the furnace. Grease, owing to its adhesive nature, may, by collecting impurities contained in the water, become sufficiently heavy to sink. In this condition it is apt to attach itself to a plate or pipe near the furnace and may, owing to its non-conducting qualities, cause serious overheating, resulting in burning, bulging or even blowing out.

If water contains more than 5 parts per 100,000 of free sulphuric or nitric acid, serious corrosion will ensue not only in boiler plates, but also in tubes, pipes, cylinders and other parts with which the steam comes in contact.

Animal and vegetable oils and greases decompose into fatty acids when subjected to the temperature of high pressure steam. Because of this their presence in a high pressure steam engine or boiler will cause serious corrosion.

Experiments have shown that pure water, into which air has been forced, on boiling causes corrosion.

Highly heated surfaces in contact with water containing common salt corrode and pit rapidly. The sides of the furnace, the tube plates and the hottest tubes suffer most.

It is clear then that feed-water, free from solids, combined or in suspension, organic matter, acids of all kinds, and air, would be best for the life of boilers.

## TABULAR VIEW.

Troublesome Trouble.
Substance.
Remedy or
Paliliation.

Sediment, mud, clay, Incrustation. Filtration ; blowing etc.

Readily soluble salts.

Bicarbonates of lime, magnesia, iron.

Sulphate of lime.
" Blowing off.
(Heating feed. Addition of causticsoda, lime, or magnesia, etc.
$\left\{\begin{array}{c}\text { Addition of carbon- } \\ \text { ate soda, barium } \\ \text { chloride, etc. }\end{array}\right.$

Chloride and sulphate of magne- $\}$ Corrosion. $\left\{\begin{array}{l}\text { Addition of carbon- } \\ \text { ate of soda, etc }\end{array}\right.$ sium.
$\left.\begin{array}{c}\text { Carbonate of soda in } \\ \text { large amounts. }\end{array}\right\}$ Priming. $\left\{\begin{array}{c}\text { Addition of barium } \\ \text { chloride, etc. }\end{array}\right.$ Acid(inminewaters). Corrosion. Alkali.
$\left.\begin{array}{c}\text { Dissolved carbonic } \\ \text { acid and oxygen. }\end{array}\right\}$


Organic matter (sew-
age).
Organic matter. Corrosion, Ditto.

Analyses in Parts per 100,000 of Water giving Bad Results in Steam-boilers. (A. E. Hunt.)

|  |  |  |  |  |  | $$ | 号 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Coal-mine | 110 | 25 | 119 | 39 | 890 | 590 | 780 | 30 | 640 |  |
| Salt-well. | 151 | 38 | 1.90 | 48 | 360 | 990 | 38 | 21 | 30 | 13.10 |
| Spring............. | 75 | 89 | 95 | 120 | 310 | 21 | 75 | 10 | 80 | 36 |
| Monongahela River.. | 130 | 21 | 161 | 33 | 210 | 38 | 70 |  |  |  |
| "6 "6 | 80 | 70 |  |  |  |  | 90 |  |  |  |
| Allegheny River near | 32 | 82 | 61 | 1.04 |  | 1.90 | 38 |  |  |  |
| Allegheny River near Oil-works...... | 30 | 50 | 41 | 68 | 890 | 42 | 23 |  |  |  |

In cases where water containing large amounts of total solid residue is necessarily used, a heavy petroleum oil, free from tar or wax, which is not acted upon by acids or alkalies, not having sufficient wax in it to cause saponification, and which has a vaporizing-point at nearly $600^{\circ}$ F., will give the best results in preventing boiler-scale. Its action is to form a thin greasy film over the boiler linings, protecting them largely from the action of acids in the water and greasing the sediment which is formed, thus preventing the formation of scale and keeping the solid residue from the evaporation of the water in such a plastic suspended condition that it can be easily ejected from the boiler by the process of "blowing off." If the water is not blown off sufficiently often, this sediment forms into a "putty" that will necessitate cleaning the boilers.

Oxidation of pipes may be prevented by coating the pipe with some protecting material. Galvanizing is coating the pipe with zinc, which, being practically unacted upon by water from most natural sources, preserves it. A coating of hot coal tar is very effective as a preventive of corrosion by fresh or salt water.

## WATER PRESSURE．

The pressure of still water in pounds per square inch against the sides of any pipe or vessel of any shape what－ ever，is due alone to the head，or height of the surface of the water above the point considered pressed upon， and is equal to 0.434 pounds per square inch for every foot of head．The fluid pressure per square inch is equal in all directions．

To find the total pressure of quiet water against and perpendicular to any surface，whether vertical，horizontal or inclined at any angle，whether it be flat or curved； multiply together the area in square feet of the surface pressed，the vertical depth of its center of gravity below the surface of the water，and the constant 62.5 ．The product will be the required pressure in pounds．This may be expressed by formula as follows ：

$$
\mathrm{P}=62.5 \mathrm{~A} \mathrm{D}
$$

In which $P=$ the pressure in pounds of quiescent water on the surface considered．
$A=$ the area pressed upon in square feet，and
$\mathrm{D}=$ the vertical depth in feet of center of gravity of surface considered．
Pressures in Pounds per Square Inch in Pipes，Etc．，under different Heads of Water．

|  |  |  |  |  |  |  |  |  | 亗品 ๗．． <br> 运岢 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.43 | 15 | 6.49 | 29 | 12.55 | 43 | 18.62 | 57 | 24.69 |
| 2 | $0 . \diamond 6$ | 16 | 6.93 | 30 | 12.99 | 44 | 19.05 | 58 | 25.12 |
| 3 | 1.30 | 17 | 7.36 | 31 | 13.42 | 45 | 19.49 | 59 | 25.55 |
| 4 | 1.73 | 18 | 7.79 | 32 | 13.86 | 46 | 19.92 | 60 | 25.99 |
| 5 | 2.16 | 19 | 8.22 | 33 | 14.29 | 47 | 20.35 | 61 | 26.42 |
| 6 | 2.59 | 20 | 8.66 | 34 | $14 . \% 2$ | 48 | 20.79 | 63 | 26.85 |
| 7 | 3.03 | 21 | 9.09 | 35 | 15.16 | 49 | 21.22 | 63 | 27.29 |
| 8 | 3.46 | 22 | 9.53 | 36 | 15.59 | 50 | 21.65 | 64 | 27.72 |
| 9 | 3.89 | 23 | 9.96 | 37 | 16.02 | 51 | 22.09 | 65 | 28.15 |
| 10 | 4.33 | 24 | 10.39 | 38 | 16.45 | 52 | 22.52 | 66 | 28.58 |
| 11 | 4.76 | 25 | 10.82 | 39 | 16.89 | 53 | 22.95 | 67 | 29.02 |
| 12 | 5.20 | 26 | 11.26 | 40 | 17.32 | 54 | 23.39 | 68 | 29.45 |
| 13 | 5.63 | 27 | 11.69 | 41 | 17.75 | 55 | 23.82 | 69 | 29.88 |
| 14 | 6.06 | 28 | 12.12 | 42 | 18.19 | 56 | 24.26 | 70 | 30.32 |

Pressures in Pounds per Square Inch in Pipes, Etc., under different Heads of Water.
(CONTINUED.)

|  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 71 | 30.75 | 121 | 52.41 | 171 | 74.07 | 221 | 95.73 | 271 | 117.39 |
| 72 | 31.18 | 122 | 52.84 | 172 | 74.50 | 222 | 96.16 | 272 | 117.82 |
| 73 | 31.62 | 123 | 53.28 | 173 | 74.94 | 223 | 96.60 | 273 | 118.26 |
| 74 | 32.05 | 124 | 53.71 | 174 | 75.37 | 224 | 97.03 | 274 | 118.69 |
| 75 | 32.48 | 125 | 54.15 | 175 | 75.80 | 225 | 97.46 | 275 | 119.12 |
| 76 | 32.92 | 126 | 54.58 | 176 | 76.23 | 226 | 97.90 | 276 | 119.56 |
| 77 | 33.35 | 127 | 55.01 | 177 | 76.67 | 227 | 98.33 | 277 | 119.99 |
| 78 | 33.78 | 128 | 55.44 | 178 | 77.10 | 228 | 98.76 | 278 | 120.42 |
| 79 | 34.21 | 129 | 55.88 | 179 | 77.53 | 229 | 99.20 | 279 | 120.85 |
| 80 | 34.65 | 130 | 56.31 | 180 | 77.97 | 230 | 99.63 | 280 | 121.29 |
| 81 | 35.08 | 181 | 56.74 | 181 | 78.40 | 231 | 100.06 | 281 | 121.72 |
| 82 | 35.52 | 132 | 57.18 | 182 | 78.84 | 232 | 100.49 | 282 | 122.15 |
| 83 | 35.95 | 133 | 57.61 | 183 | 79.27 | 233 | 100.93 | 283 | 122.59 |
| 84 | 36.39 | 134 | 58.04 | 184 | 79.70 | 234 | 101.36 | 284 | 123.02 |
| 85 | 36.82 | 135 | 58.48 | 185 | 80.14 | 235 | 101.79 | 285 | 123.45 |
| 86 | 37.25 | 136 | 58.91 | 186 | 80.57 | 236 | 102.23 | 286 | 123.89 |
| 87 | 37.68 | 137 | 59.34 | 187 | 81.00 | 237 | 102.66 | 287 | 124.82 |
| 88 | 38.12 | 138 | 59.77 | 188 | 81.43 | 238 | 103.09 | 288 | 124.75 |
| 89 | 38.55 | 139 | 60.21 | 189 | 81.87 | 239 | 103.53 | 289 | 125.18 |
| 90 | 38.98 | 140 | 60.64 | 190 | 8230 | 240 | 103.96 | 290 | 125.62 |
| 91 | 39.42 | 141 | 61.07 | 191 | 82.73 | 241 | 104.39 | 291 | 126.05 |
| 92 | 39.85 | 142 | 61.51 | 192 | 83.17 | 242 | 104.83 | 292 | 126.48 |
| 93 | 40.28 | 143 | 61.94 | 193 | 83.60 | 243 | 105.26 | 293 | 126.92 |
| 94 | 40.72 | 144 | 62.37 | 194 | 84.03 | 244 | 105.69 | 294 | 127.35 |
| 95 | 41.15 | 145 | 62.81 | 195 | 84.47 | 245 | 106.13 | 295 | 127.78 |
| 96 | 41.58 | 146 | 63.24 | 196 | 84.90 | 246 | 106.56 | 296 | 128.22 |
| 97 | 42.01 | 147 | 63.67 | 197 | 85.33 | 247 | 106.99 | 297 | 128.65 |
| 98 | 42.45 | 148 | 64.10 | 198 | 85.76 | 248 | 107.43 | 298 | 129.08 |
| 99 | 42.88 | 149 | 64.54 | 199 | 86.20 | 249 | 107.86 | 299 | 129.51 |
| 100 | 43.31 | 150 | 64.97 | 200 | 86.63 | 250 | 108.29 | 300 | 129.95 |
| 101 | 43.75 | 151 | 65.40 | 201 | 87.07 | 251 | 108.73 | 310 | 134.28 |
| 102 | 44.18 | 152 | 65.84 | 202 | 87.50 | 252 | 109.16 | 320 | 138.62 |
| 103 | 44.61 | 153 | 66.27 | 203 | 87.93 | 253 | 109.59 | 330 | 142.95 |
| 104 | 45.05 | 154 | 66.70 | 204 | 88.36 | 254 | 110.03 | 340 | 147.28 |
| 105 | 45.48 | 155 | 67.14 | 205 | 88.80 | 255 | 110.46 | 350 | 151.61 |
| 106 | 45.91 | 156 | 67.57 | 206 | 89.23 | 256 | 110.89 | 360 | 155.94 |
| 107 | 46.34 | 157 | 68.00 | 207 | 89.66 | 257 | 111.32 | 370 | 160.2 \% |
| 108 | 46.78 | 158 | 68.43 | 208 | 90.10 | 258 | 111.76 | 380 | 164.61 |
| 109 | 47.21 | 159 | 68.87 | 209 | 90.53 | 259 | 112.19 | 390 | 168.94 |
| 110 | 47.64 | 160 | 69.31 | 210 | 90.96 | 260 | 112.62 | 400 | 173.27 |
| 111 | 48.08 | 161 | 69.74 | 211 | 91.39 | 261 | 113.06 | 500 | 216.58 |
| 112 | 48.51 | 162 | 70.17 | 212 | 91.83 | 262 | 113.49 | 600 | 259.90 |
| 113 | 48.94 | 163 | 70.61 | 213 | 92.26 | 263 | 118.92 | 700 | 303.22 |
| 114 | 49.38 | 164 | 71.04 | 214 | 92.69 | 264 | 114.36 | 800 | 346.54 |
| 115 | 49.81 | 165 | 71.47 | 215 | 93.13 | 265 | 114.79 | 900 | 389.86 |
| 116 | 50.24 | 166 | 71.91 | 216 | 9356 | 266 | 115.22 | 1000 | 433.18 |
| 117 | 50.68 | 167 | 72.34 | 217 | 93.99 | $26 \%$ | 115.66 |  |  |
| 118 | 51.11 | 168 | 72.77 | 218 | 94.43 | 268 | 116.09 |  |  |
| 119 | 51.54 | 169 | 73.20 | 218 | 94.86 | 269 | 116.52 |  |  |
| 120 | 51.98 | 170 | 73.64 | 220 | 95.30 | 270 | 116.96 |  |  |

## FLOW OF WATER IN PIPES.

The vertical height of the source of water above the outlet is called the head. The greater the head the greater will be the velocity of efflux if the length and diameter of the pipe remain constant.

To find the velocity of water discharged from a pipe line longer than 4 times its diameter, knowing the head, length and inside diameter, use the following formula:

$$
\mathrm{v}=\mathrm{m} \sqrt{\frac{\mathrm{hd}}{\mathrm{~L}+54 \mathrm{~d}}},
$$

In which $\mathrm{v}=$ approximate mean velocity in feet per second,
$\mathrm{m}=$ coefficient from table below,
$\mathrm{d}=$ diameter of pipe in feet,
$\mathrm{h}=$ total head in feet,
$\mathrm{L}=$ total length of line in feet.

## VALUES OF COEFFICIENT M.

| h | Diameter of Pipe in Feer. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| L+54d | 0.05 | 0.10 | 0.50 | 1 | 1.5 | 2 | 3 | 4 |
|  | M | M | M | M | M | M | M | M |
| 0.005 | 29 | 31 | 33 | 35 | 37 | 40 | 44 | 47 |
| 0.01 | 34 | 35 | 37 | 39 | 42 | 45 | 49 | 53 |
| 0.02 | 39 | 40 | 42 | 45 | 49 | 52 | 56 | 59 |
| 0.03 | 41 | 43 | 47 | 50 | 54 | 57 | 60 | 63 |
| 0.05 | 44 | 47 | 52 | 54 | 56 | 60 | 64 | 67 |
| 0.10 | 47 | 50 | 54 | 56 | 58 | 62 | 66 | 70 |
| 0.20 | 48 | 51 | 55 | 58 | 60 | 64 | 67 | 70 |

The above coefficients are averages deduced from a large number of experiments.' In most cases of pipes carefully laid and in fair condition, they should give results within 5 to 10 per cent. of the truth.

Example.-Given the head, $h=50 \mathrm{ft}$; the length, $L=5280 \mathrm{ft}$.; and the diameter, $d=2 \mathrm{ft}$.; to find the velocity and quantity of discharge.

Substituting these values in above formula, we get:

$$
\sqrt{\frac{\mathrm{d} \mathrm{\times h}}{\mathrm{~L}+54 \mathrm{~d}}}=\sqrt{\frac{2 \times 50}{2580+108}}=\sqrt{\frac{100}{5388}}=0.136
$$

In column headed $\sqrt{\frac{h d}{L+54 d}}$ find 0.10 , which is the value nearest to 0.136 , and look along this line until column headed " 2 " is reached, then read 62 as the value of coefficient $m$.

Then $v=62 \times 0.136=8.432 \mathrm{ft}$. per sec., the required velocity.

To find the discharge in $\mathrm{cu} . \mathrm{ft}$. per sec., multiply this velocity by area of cross section of pipe in sq. ft .

Thus, $3.1416 \times(1)^{2} \times 8.432=26.49 \mathrm{cu} . \mathrm{ft}$. per sec.
Since there are 7.48 gal . in a $\mathrm{cu} . \mathrm{ft}$., the discharge in gal. per sec. $=26.49 \times 7.48=198.2$.

The above formula is only an approximation, since the flow is modified by bends, joints, incrustations, etc. Wrought Iron and Steel Pipes are smoother than cast iron ones, thereby presenting less friction and less encouragement for deposits ; and, being in longer lengths, the number of joints is reduced, thus lessening the undesirable effects of eddy currents.

To find the head in feet necessary to give a stated discharge in cu. ft., use the formula.*

$$
\mathrm{h}=\frac{0.000704 \mathrm{Q}^{2}(\mathrm{~L}+54 \mathrm{~d})}{\mathrm{d}^{5}}
$$

In which $h$ - total head in feet,
$\mathrm{L}=$ total length of line in feet,
$d$ - diameter of pipe in feet,
Q - quantity of water in $\mathrm{cu} . \mathrm{ft}$. per second.
Example.-Given the diameter of pipe, $d=0.5 \mathrm{ft}$.; the length of pipe, $L=20 \mathrm{ft}$.; and the quantity of water to be discharged, $q=3.07 \mathrm{cu} . \mathrm{ft}$. per sec.; to find the necessary head.

Substituting these values in the above formula,* we get:

$$
\mathrm{h}=\frac{0.000704 \times 9.4 \times(20+27)}{(0.5)^{5}}
$$

$$
=\frac{0.000704 \times 9.4 \times 47}{0.03125}=9.95 \mathrm{ft} ., \text { the required head. }
$$

The following formula* is simpler and can be used when $54 d$ in relation to $L$ is so small as to be negligible.

$$
h=\frac{0.000704 Q^{2} \times L}{d^{5}}
$$

If the pipe, instead of being straight, has easy curves (say with radius not less than 5 diameters of the pipe) either horizontal or vertical, the discharge will not be materially diminished, so long as the total heads, and total actual lengths of pipe remain the same, but it is advisable to make the radius as much more than 5 diameters as can conveniently be done.

To find the diameter of a pipe of given length to deliver a given quantity of water under a given head, use the following :

$$
\mathrm{d}=0.234 \sqrt[s]{\frac{\mathrm{Q}^{2} \mathrm{~L}}{\mathrm{~h}}}
$$

In which $d$ - diameter of pipe in feet,
$\mathrm{Q}=\mathrm{cu} . \mathrm{ft}$. per second delivered,
L - length of line in feet,
h - head in feet.
Example.-Given the head, $\mathrm{h}=700$ feet ; the length of pipe, $L=3000$ feet; the quantity to be delivered, $Q=4$ $\mathrm{cu} . \mathrm{ft}$. per. sec.; required the diameter of pipe necesssary.

Substituting these values in the above formula,* we get :

$$
\mathrm{d}=0.234 \sqrt[5]{\frac{16 \times 3000}{700}}=0.234 \sqrt[5]{68.57}=0.545 \mathrm{ft} .=6.54 \mathrm{in}
$$

The diameter of a pipe may also be found by using the following formula : *

$$
\mathrm{D}=125 \sqrt[5]{\frac{q^{2} \times \mathrm{L}}{\mathrm{~h}}}
$$

In which $\mathrm{D}=$ diameter of pipe in inches, $\mathrm{q}=$ gallons per second,
${ }^{\circ} \mathrm{L}=$ length of line in feet, $\mathrm{h}=$ head in feet.

If, in formula $v=m \sqrt{\frac{d \times h}{L+54 d}}$ we substitute 48 as an average value for $m$, we get :

$$
v=48 \sqrt{\frac{\mathrm{~d} \times \mathrm{h}}{\mathrm{~L}+54 \mathrm{~d}}}
$$

The following table, calculated by the above formula shows the velocities and discharges through a pipe one mile long and one foot in diameter, under different heads. But they will be very nearly the same for any greater lengths; and also quite approximate for shorter ones not less than 1000 or even 500 diameters long, provided that in all cases they have the same RATE OF HEAD ; that is, if the given pipe of one foot diameter is 2 or 3 miles long, it must have 2 or 3 times as much head as the pipe in the table in order to have very nearly the same velocity and discharge.

[^4]The velocities and discharges through a straight, smooth pipe one foot in diameter, and one mile or 5280 diameters in length.

| Head in <br> feet per <br> 100 feet. | Head in <br> feet mile. | Velocity in <br> feet per <br> second. | Discharge <br> in cubic feet <br> per second. | Discharge <br> in cubic feet <br> per 24 hours. |
| :---: | :---: | :---: | :---: | :---: |
| .0019 | .1 | .208 | .1633 | 14,114 |
| .0038 | .2 | .293 | .2301 | 19,880 |
| .0057 | .3 | .359 | .2819 | 24,360 |
| .0076 | .4 | .415 | .3267 | 28,229 |
| .0095 | .5 | .464 | .3638 | 31,435 |
| .0114 | .6 | .508 | .3989 | 34,464 |
| .0132 | .7 | .549 | .4311 | 37,247 |
| .0151 | .8 | .585 | .4602 | 39,760 |
| .0170 | .9 | .623 | .4901 | 42,343 |
| .0189 | 1. | .656 | .5144 | 44,431 |
| .0237 | .25 | .735 | .5753 | 49,701 |
| .0284 | .5 | .805 | .6322 | 54,604 |
| .0331 | .75 | .871 | .6832 | 59,011 |
| .0379 | 2. | .928 | .7276 | 62,870 |
| .0426 | .25 | .984 | .7696 | 66,484 |
| .0473 | .5 | 1.04 | .8168 | 70,572 |
| .0521 | .75 | 1.08 | .8482 | 73,284 |
| .0568 | 3. | 1.13 | .8914 | 76,982 |
| .0758 | 4. | 1.31 | 1.028 | 88,862 |
| .0947 | 5. | 1.47 | 1.150 | 99,403 |
| .1136 | 6. | 1.61 | 1.264 | 109,209 |
| .1325 | 7. | 1.74 | 1.366 | 118,022 |
| .1514 | 8. | 1.86 | 1.455 | 125,740 |
| .1703 | 9. | 1.96 | 1.539 | 132,969 |
| .1894 | 10. | 2.08 | 1.633 | 141,145 |
| .2273 | 12. | 2.27 | 1.782 | 153,964 |
| .2652 | 14. | 2.45 | 1.924 | 166,233 |
| .3030 | 16. | 2.62 | 2.057 | 177,724 |
| .3409 | 18. | 2.78 | 2.183 | 188,611 |
| .388 | 20. | 2.93 | 2.301 | 198,806 |
| .4735 | 25. | 3.28 | 2.572 | 222,156 |
| .5682 | 30. | 3.59 | 2.819 | 243,604 |
| .6629 | 35. | 3.88 | 3.047 | 263,260 |
| .7576 | 40. | 4.15 | 3.267 | 282,288 |
| .8523 | 45. | 4.40 | 3.451 | 298,209 |
| .9470 | 50. | 4.64 | 3.638 | 314,352 |
| 1.136 | 60. | 5.08 | 3.989 | 344,649 |
| 1.326 | 70. | 5.49 | 4.311 | 372,470 |
| 1.515 | 80. | 5.85 | 4.602 | 397,613 |
|  |  |  |  |  |

The velocities and discharges through a straight, smooth pipe one foot in diameter, and one mile or 5280 diameters in length.

| Head in feet per 100 feet. | Head in feet per mile. | Velocity in feet per second. | Discharge in cubic feet per second. | Discharge in cubic feet per 24 hours. |
| :---: | :---: | :---: | :---: | :---: |
| 1.704 | 90. | 6.23 | 4.900 | 423,435 |
| 1.894 | 100. | 6.56 | 5.144 | 444,312 |
| 2.083 | 110. | 6.87 | 5.395 | 466,128 |
| 2.272 | 120. | 7.18 | 5.639 | 487,209 |
| 2.462 | 130. | 7.47 | 5.866 | 506,822 |
| 2.652 | 140. | 7.76 | 6.094 | 526,521 |
| 2.841 | 150. | 8.05 | 6.322 | 546,048 |
| 3.030 | 160. | 8.30 | 6.534 | 564,576 |
| 3.219 | 170. | 8.55 | 6.715 | 580,176 |
| 3.408 | 180. | 8.80 | 6.903 | 596,418 |
| 3.596 | 190. | 9.04 | 7.100 | 613,440 |
| 3.788 | 200. | 9.28 | 7.276 | 628,704 |
| 4.261 | 225. | 9.84 | \%.696 | 664,848 |
| 4.735 | 250. | 10.4 | 8.168 | 1705,728 |
| 5.208 | 275. | 10.8 | 8.482 | 1732,844 |
| 5.682 | 300. | 11.3 | 8.914 | '769,824 |
| 6.629 | 350. | 12.3 | 9.621 | 831,168 |
| 7.576 | 400. | 13.1 | 10.28 | 888,624 |
| 8.532 | 450. | 13.9 | 10.91 | 943,056 |
| 9.47 | 500. | 14.7 | 11.50 | 994,032 |
| 10.41 | 550. | 15.4 | 12.09 | 1,044,576 |
| 11.36 | 600. | 16.1 | 12.64 | 1,092,096 |
| 12.30 | 650. | 16.7 | 13.11 | 1,132,704 |
| 13.25 | 700. | 17.4 | 13.66 | 1,180,224 |
| 14.20 | 750. | 18.0 | 14.13 | 1,220,832 |
| 15.15 | 800. | 18.6 | 14.55 | 1,257,408 |
| 16.09 | 850. | 19.1 | 15.00 | 1,296,000 |
| 17.04 | 900. | 19.6 | 15.39 | 1,329,696 |
| 17.99 | 950. | 20.3 | 15.94 | 1,377,216 |
| 18.94 | 1000. | 20.8 | 16.33 | 1,411,456 |
| 22.73 | 1200. | 22.7 | 17.82 | 1,539,648 |
| 26.52 | 1400. | 24.5 | 19.24 | 1,662,336 |
| 30.30 | 1600. | 26.2 | 20.57 | 1,777,248 |
| 34.08 | 1800. | 27.8 | 21.83 | 1,886,112 |
| 37.87 | 2000. | 29.3 | 23.01 | 1,988,064 |
| 47.35 | 2500. | 32.8 | 25.72 | 2,221,560 |
| 56.81 | 3000. | 35.9 | 28.19 | 2,436,040 |

Head is the vertical distance from the surface of the water in the reservoir to the center of gravity of the lower end of the pipe when the discharge is into the air ; or to the level surface of the lower reservoir when the discharge is under water.

To reduce cubic feet to U. S. Gallons, multiply by 7.48.

To find either the area of pipe, the mean velocity, or the quantity discharged, when the other two are given, use the following:


Mean velocity in _Discharge in cubic feet per second, feet per second. Area in square feet.

Discharge in cubic feet $=$ Area in $\times$ Mean velocity in per second. $=$ square feet $\times$ feet per second.
[The terms may be in inches instead of feet; and in minutes or hours instead of seconds.]

For the diameter of a long pipe required to deliver either more or less water than that of a 1 foot diameter, and under the same rate of inclination, or of head in feet per mile, see table on next page.

The use of this table is not sufficiently correct for pipes less than about 1,000 (or at furthest 500 ) diameters long.

|  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | . 0833 | . 0020 | $12 \mathrm{x} / 2$ | 1.042 | 1.106 |
| $11 / 2$ | . 1250 | . 0055 | 13 | 1.083 | 1.221 |
| 2 | . 1667 | . 0113 | 14 | 1.167 | 1.470 |
| $21 / 2$ | . 2083 | . 0198 | 15 | 1.250 | 1.746 |
| 3 | . 2500 | . 0310 | 16 | 1.333 | 2.053 |
| $31 / 2$ | . 2917 | . 0458 | 17 | 1.417 | 2.388 |
| 4 | . 3333 | . 0643 | 18 | 1.5 | 2.754 |
| $41 / 2$ | . 3750 | . 0857 | 19 | 1.583 | 3.153 |
| 5 | . 4167 | . 1119 | 20 | 1.667 | 3.585 |
| $51 / 2$ | . 4583 | . 1422 | 21 | 1.75 | 4.051 |
| 6 | . 5 | . 1767 | 22 | 1.833 | 4.551 |
| $61 / 2$ | . 5417 | . 2159 | 23 | 1.917 | 5.084 |
| 7 | . 5833 | . 2600 | 24 |  | 5.649 |
| $71 / 2$ | . 6250 | . 3090 | 245/8 | 2.052 | 6.000 |
| 8 | . 6667 | . 3631 | 26 | 2.167 | 6.912 |
| $81 / 2$ | . 7083 | . 4220 | 28 | 2.333 | 8.319 |
| 9 | . 75 | . 4871 | 30 | 2.5 | 9.822 |
| $91 / 2$ | . 7917 | . 5575 | 301/4 | 2.521 | 10. |
| $10^{1 / 2}$ | . 8333 | . 6337 | 32 | 2.667 | 11.6 |
| $101 / 2$ | . 8750 | . 7157 | 34 | 2.833 | 13.5 |
| 11 | . 9167 | . 8044 . | 36 | 3. | 15.5 |
| $111 / 2$ | . 9583 | . 8987 | 38 | 3.167 | 17.8 |
| 12 | 1. | 1. | 40 | 3.333 | 20.2 |

To find the discharge from a pipe (not less than 1,000 , or at least 500 times its own diameter in length) when the head is given, take from the first table the discharge through a pipe one ft . in diameter for the given head, and divide the required discharge by this tabular one; then look for the quotient in the column of the second table, headed "Ratio of Discharge," and opposite it, in columns 1 and 2 , will be found the required diameter.

From this table we see that a 14 inch pipe will deliver nearly $11 / 2$ times as much as a 12 inch pipe, and a 16 inch one fully twice as much as a 12 inch, all having the same length and head.

EXAMPLE.-Having given the head from a reservoir to a certain point of delivery, as 20 ft . in a distance of $1,860 \mathrm{ft}$., what must be the diameter of a pipe to deliver 6 cubic feet of water per second ?

We find that a fall of 20 ft . in 1,860 , is equal to a fall of 1.075 ft . in 100 ; or $1,860: 20=100: 1.075$. Then we see by the first table that with a fall of 1.075 ft . in 100 , a long pipe of 1 ft . diameter discharges about 3.8 cubic feet per second. But we want $\frac{{ }_{3}}{}{ }^{6} \frac{8}{8}=1.58$ times as much as the 1 ft . pipe can deliver; then by the second table, we see that the pipe to do this, under the same rate of head, must be about $141 / 2 \mathrm{in}$. in diameter. In practice we should adopt at least 15 in .



EXAMPLE.-Given 120 feet head and 600 feet length of 18 inch pipe, discharging 3500 gallons per minute : To find effective head: Look in column headed " 18 inch Pipe," and opposite 3500 in . first column read " 4.7 ft ." (which is the loss of head by friction for an 18 in . pipe 1000 ft . long), and multiplying this by $600 / 1000$, or 0.6 , we get 2.82 ft , the loss of head. The effective head required then equals 120 ft . less 2.8 ft . or 117.2 ft .

Flow of Water in Pipes for a Velocity of 100 Ft. per Minute.

| $\underset{\text { in }}{\text { Diameter }}$ Inches. | Area in Square Feet. | Flow in Cubic Feet per Minute. | Flow in U.S. Minute. | $\underbrace{\substack{\text { Gallons } \\ \hline}}_{\substack{\text { Ullow in } \\ \text { per Hour. }}}$ |
| :---: | :---: | :---: | :---: | :---: |
| 3/8 | . 00077 | 0.077 | . 57 | 34 |
| 3/2 | . 00136 | 0.136 | 1.02 | 61 |
| 13/4 | . 00307 | 0.307 | 2.30 | 138 |
| 1. | . 00545 | 0.545 | 4.08 | 245 |
| 11/4 | . 00852 | 0.852 | 6.38 | 383 |
| $11 / 2$ | . 01227 | 1.227 | 9.18 | 551 |
| 13/4 | . 01670 | 1.670 | 12.50 | 750 |
| , | . 02182 | 2.182 | 16.32 | 979 |
| 21/2 | . 0341 | 3.41 | 25.50 | 1,530 |
| 3 | . 0491 | 4.91 | ${ }^{36.72}$ | 2,203 |
| 4 | . 0873 | 8.73 | 65.28 | 3,917 |
| 5 | . 136 | 13.6 | 102.00 | 6,120 |
| 6 | . 196 | 19.6 | 146.88 | 8,813 |
| 7 | . 267 | 26.7 | 199.92 | 11,995 |
| 8 | . 349 | 34.9 | 261.12 | 15,667 |
| 9 | . 442 | 44.2 | 330.48 | 19,829 |
| 10 | . 545 | 54.5 | 408.00 | 24,480 |
| 11 | . 660 | 66.0 | 493.68 | 29,621 |
| 12 | . 785 | 78.5 | 587.52 | 35,251 |

To find the quantity in gallons a pipe will deliver, the velocity of flow being 100 ft . per minute: Square the diameter in inches and multiply by 4.08 .

## Flow of Water in House-service Pipes.

(Thomson Meter Co.)

| $\begin{aligned} & \text { Condition } \\ & \text { of } \\ & \text { Discharge. } \end{aligned}$ |  | Discharge in Cubic Feet per Minute from the Pipe. |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Nominal Diameters of Iron or Lead Ser-vice-pipe in Inches. |  |  |  |  |  |  |  |  |
|  |  | 1/2 | 5/8 | $3 /$ | 1 | 11/2 | 2 | 3 |  | 6 |
| Through 35 feet of servicepipe, no back pressure. | 301 | 1.10 | 1.923 | 3.01 | 6.13 | 16.58 | 33.34 | 88.16 | 173.85 | 444.63 |
|  | 40 | 1.27 | 2.223 | 3.48 | 7.08 | 19.14 | 38.50 | 101.80 | 200.75 | 513.42 |
|  | 50 | 1.42 | 2.483 | 389 | 7.92 | 21.40 | 43.04 | 113.82 | 224.14 | 574.02 |
|  | 60 | 1.56 | 2.71 | 4.26 | 8.67 | 23.44 | 47.15 | 124.68 | 245.87 | 628.81 |
|  |  | 1.74 | 3.03 | 4.77 | 9.70 | 26.21 | 52.71 | 139.39 | 274.89 | 703.03 |
|  | 100 | 2.013 | 3.505 | 5.50 | 11.20 | 30.27 | 60.87 | 160.96 | 317.41 | 811.79 |
|  | 130 | 2.29 | 3.99 | 6.28 | 12.77 | 34.51 | 69.40 | 183.52 | 361.91 | 925.58 |
| Through 100 feet of servicepipe, no back pressure. | 80 | 0.66 | 1.161 | 1.8 | 3.78 | 10 | 21.30 | 58.19 | 118.13 | 317.23 |
|  | 40 | 0.77 | 1.34 | 2.12 | 4.36 | 12.01 | 24.59 | 67.19 | 136.41 | 366.30 |
|  | 50 | 0.86 | 1.50 | 2.37 | 4.88 | 13.43 | 27.50 | 75.13 | 152.51 | 409.54 |
|  | 60 | 0.94 | 1.65 | 2.60 | 5.34 | 14.71 | 30.12 | 82.30 | 167.06 | 448.63 |
|  | 75 | 1.05 | 1.84 | 2.91 | 5.97 | 16.45 | 33.68 | 92.01 | 186.78 | 501.58 |
|  | 10 | 1.22 | 2. | 3. | 6.90 | 18.99 | 38.89 | 106.24 | 215.68 | 579.18 |
|  | 130 | 1.39 | 2.423 | 3.83 | 7.86 | 21.66 | 44.34 | 121.14 | 245.91 | 660.36 |
| Through 100 feet of servicepipe, and 15 feet vertical rise. | 30 | 0.55 | 0.961 | 1. | 3.11 | 57 | 17.55 | 47 | 17 | 260 |
|  | 0, | 0.66 | 1.151 | 1.81 | 3.72 | 10.24 | 20.95 | 57.20 | 116.01 | 311.09 |
|  | 50 | 0.75 | 1.312 | 2.06 | 4.24 | 11.67 | 23.87 | 65.18 | 132.20 | 354.49 |
|  | 60 | 0.83 | 1.45 | 2.29 | 4.70 | 12.94 | 26.48 | 72.28 | 146.61 | 393.13 |
|  | 75 | 0. | 1.64 | 2.59 | 5.32 | 14.64 | 29.96 | 81.79 | 165.90 | 444.85 |
|  | 100 | 1.10 | 1.923 | 3.02 | 6.21 | 17.10 | 35.00 | 95.55 | 193.82 | 519.72 |
|  | 130 | 1.26 | 2.203 | 3.48 | 7.14 | 19.66 | 40.23 | 109.82 | 222.75 | 597.31 |
| Through 100 feet of servicepipe, and 30 feet vertical rise. | 30 | 0.44 | 0.77 | 1.22 | 2.5 | 8.80 | 14 | 38 | 78.54 | 211 |
|  | 40 | 0.55 | 0.97 | 1.53 | 3.15 | 8.68 | 17.79 | 48.68 | 98.98 | 266.59 |
|  | f 50 | 0.65 | 1.14 | 1.79 | 3.69 | 10.16 | 20.82 | 56.98 | 115.87 | 312.08 |
|  | 60 | 0.73 | 1.28 | 2.02 | 4.15 | 11.45 | 23.47 | 64.22 | 130.59 | 351.73 |
|  | 75 | 0.84 | 1. | 232 | 4.77 | 13.15 | 28.95 | 73.76 | 149.99 | 403.98 |
|  | 100 | 1.00 | 1.74 | 2.75 | 5.65 | 15.58 | 31.93 | 87.38 | 177.67 | 478.55 |
|  | 130 |  |  | 3.19 | 6.55 | 18.07 | 37.02 | 101 | 206.04 | 554.96 |

RELATIVE DISCHARGING CAPACITIES OF FULL SMOOTH PIPES．

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[^5]SAFE PRESSURES AND EQUIVALENT HEADS OF WATER FOR CAST IRON PIPE OF
（Calculated by F．H．Lewis，from Fanning＇s Formula．）
SIZE OF PIPE．

| दे | $\begin{gathered} \text { тәәg } \\ \text { u! peวн } \end{gathered}$ |  |
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Safe Pressures and Equivalent Heads of Water for Cast Iron Pioe of Different Sizes and＇Thicknesses．（Cont＇d）

| 0．E気E | SIZE OF PIPE． |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $22^{*}$ |  | $24^{\prime \prime}$ |  | 27 |  | $30^{\circ}$ |  |  |  | $36^{*}$ |  | $42^{\prime \prime}$ |  | $48^{\circ}$ |  | $60^{\circ}$ |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | $\begin{aligned} & \text { 志 } \\ & \text { تِّ } \\ & \text { 芯 } \\ & \text { 出 } \end{aligned}$ |  | $\begin{aligned} & \text { 思 } \\ & \text { ت̈ } \\ & \text { 芯 } \\ & \text { 出 } \end{aligned}$ |
|  | 40 | 92 | 30 | 69 | 19 | 64 |  |  |  |  |  |  |  |  |  |  |  |  |
|  | 60 | 138 | 49 | 113 | 36 | 83 | 24 | 55 |  |  |  |  |  |  |  |  |  |  |
| $1{ }^{1}$ | 80 | 184 | 68 | $15{ }^{\prime \prime}$ | 52 | 120 | 39 | 90 |  |  |  |  |  |  |  |  |  |  |
|  | 101 | 233 | 86 | 198 | 69 | 159 | 54 | 124 | 42 | 97 | 32 | 74 |  |  |  |  |  |  |
|  | 121 | 279 | 105 | 242 | 85 | 196 | 69 | 159 | 55 | 127 | 44 | 101 |  |  |  |  |  |  |
| 1 | 142 | 327 | 124 | 286 | 102 | 235 | 84 | 194 | 69 | 159 | 57 | 181 | 38 | 88 |  | 55 |  |  |
|  | 182 | 419 | 161 | 371 | 135 | 311 | 114 | 263 | 96 | 221 | 8 | 189 | 59 | 136 | 43 | 99 |  |  |
| 114 | 224 | 516 | 199 | 458 | 169 | 389 | 144 | 332 | 124 | 286 | 107 | $\stackrel{247}{ }$ | 81 | 187 | 62 | 143 | 34 | 78 |
| 138 | ．．．．． | ．．．． | 237 | 546 | 202 | 465 | 174 | 401 | 151 | 348 | 132 | 304 | 103 | 237 | 81 | 187 | 49 | 118 |
| $11 \%$ | …… | ．．．．． | 2s | ， | 236 | 544 | 204 | 470 538 | 178 | 410 | 157 | 362 | 124 | 286 | 99 9 | 228 | 64 | 147 |
| 108 |  |  |  |  | ..... | ．．．．．． | 234 | 538 | 205 | 472 537 | 182 | 419 | 145 | 334 385 | 118 | 272 313 | 79 | 182 |
| 138 | ．．．．．．．． |  |  |  |  |  |  | ．．．．．．．． | 233 | 537 | 207 | 477 | 167 | 385 433 | 136 155 15 | 313 357 | 94 109 | 217 |
| ${ }_{2}^{178}$ | ．．．．．．．． |  |  |  |  |  |  |  |  |  | ．．．．．． |  | 188 | 433 | 155 174 | 357 401 | 109 124 | 251 286 |
|  |  |  |  |  |  |  |  |  |  |  |  | ．．．．．． | 210 | 484 | 174 | 401 | 124 139 | 286 320 |
| 218 | ．$\cdot$ |  |  |  |  |  |  |  |  |  |  |  | ．．．．． |  | 193 212 | 488 | 139 | 320 355 |
| － 217 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 184 | 424 |
| 234 |  |  |  |  |  |  |  |  |  | ． | ．．． |  | ．．．． | ． | ． | ．．．． | 214 | 482 |

[^6]
# WEIGH'TS OF CAST' IRON PIPE TO LAY 12 FEE'T LENGTHS. 

 Weights are in Pounds and include Hub. (Calculated by F. H. Lewis.)

Contents in Cubic Feet and U. S. Gallons of Pipes and Cylinders of Various Diameters and One Foot in Length.

1 gallon=231 cubic inches. 1 cubic foot-7.4805 gallons.

|  | For 1 Foot in Length. |  |  | For 1 Foot in Length. |  |  | For 1 Foot in Length. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Cubic ft. also Area in Sq. ft | $\left\lvert\, \begin{gathered} \text { U.S. } \\ \text { Gals. } \\ 231 \\ \text { Cu. In. } \end{gathered}\right.$ |  | Cubic Ft. also Area in Sq. Ft. | U. S. <br> Gals. <br> 231 <br> Cu. In. |  | Cubic Ft. also Area in Sq. Ft. | $\begin{gathered} \text { U.S. } \\ \text { Gals. } \\ 231 \\ \mathrm{Cu} . \mathrm{In} . \end{gathered}$ |
|  | . 0003 | . 0025 |  | . 2485 | 1.859 | 19 | 1.969 | 14.73 |
|  | . 0005 | . 004 |  | . 2673 | 1.999 | 191/2 | 2.074 | 15.51 |
| \%/8 | . 0008 | . 0057 | $71 / 4$ | . 2867 | 2.145 | 20 | 2.182 | 16.32 |
| $7^{76}$ | . 001 | . 0078 | 71.2 | . 3068 | 2.295 | 201/2 | 2.292 | 1715 |
|  | . 0014 | . 0102 | $73 / 4$ | . 3276 | 2.45 | 21 | 2.405 | 17.99 |
|  | . 0017 | . 0129 | 8 | . 3491 | 2.611 | 213/2 | 2.521 | 18.86 |
|  | . 0021 | . 0159 | $81 / 4$ | . 3712 | 2.777 | 22 | 2.640 | 19.75 |
|  | . 0026 | . 0193 | 81.2 | . 3941 | 2.948 | 2212 | 2.761 | 20.66 |
|  | . 0031 | . 0233 | $83 / 4$ | .4176 | 3.125 | 23 | 2.885 | 21.58 |
|  | . 0036 | . 0269 | 9 | . 4418 | 3.305 | 231/2 | 3.012 | 22.53 |
|  | . 0042 | .0312 | $91 / 4$ | . 4667 | 3.491 | 24 | 3.142 | 23.50 |
|  | . 0048 | . 0359 | $91 \%$ | . 4922 | 3.682 | 25 | 3.409 | 25.50 |
|  | . 0055 | . 0408 | $93 / 4$ | . 5185 | 3.879 | 26 | 3.687 | 27.58 |
| $11 / 4$ | . 0085 | . 0638 | 10 | . 5454 | 4.08 | 27 | 3.976 | 29.74 |
| 112 | . 0123 | . 0918 | 1014 | . 5730 | 4.286 | 28 | 4.276 | 31.99 |
| 134 | . 0167 | . 1249 | 101/2 | . 6013 | 4.498 | 29 | 4.587 | 34.31 |
| , | . 0218 | . 1632 | 1034 | . 6303 | 4.715 | 30 | 4.909 | 36.72 |
| $21 / 4$ | . 0276 | . 2066 | 11. | . 66 | 4.937 | 31 | 5.241 | 39.21 |
| $21 / 2$ | . 0341 | . 2550 | 1114 | . 6903 | 5.164 | 32 | 5.585 | 41.78 |
| 23 | . 0412 | . 3085 | 1112 | . 7213 | 5.396 | 33 | 5.940 | 44.43 |
| 3 | . 0491 | . 3672 | 1134 | . 7530 | 5.633 | 34 | 6.305 | 47.16 |
| $31 / 4$ | . 0576 | . 4309 | 12 | . 7854 | 5.875 | 35 | 6.681 | 49.98 |
| 317 | . 0668 | . 4998 | 121/2 | . 8522 | 6.375 | 36 | 7.069 | 52.88 |
| 334 | . 0767 | . 5738 | 13 | . 9218 | 6.895 | 37 | 7.467 | 55.86 |
| 4 | . 0873 | . 6528 | 131/2 | . 994 | 7.436 | 38 | 7.876 | 58.92 |
| 414 | . 0985 | . 7369 | 14 | 1.069 | 7.997 | 39 | 8.296 | 62.06 |
| 412 | . 1134 | .8263 | 141/2 | 1.147 | 8.578 | 40 | 8.727 | 65.28 |
| $43 / 4$ | . 1231 | . 9206 | 15 | 1.227 | 9.180 | 41 | 9.168 | 68.58 |
| 5 | . 1364 | 1.020 | 151/2 | 1.310 | 9.801 | 42 | 9.621 | 71.97 |
| $51 / 4$ | . 1503 | 1.125 | 16 | 1.396 | 10.44 | 43 | 10.085 | 75.44 |
| 51.3 | . 1650 | 1.234 | 161/2 | 1.485 | 11.11 | 44 | 10.559 | 78.99 |
| 534 | . 1803 | 1.349 | 17 | 1.576 | 11.79 | 45 | 11.045 | 82.62 |
| 6 | . 1963 | 1.469 | 171/2 | 1.670 | 12.49 | 46 | 11.541 | 86.33 |
| $61 / 4$ | . 2131 | 1.594 | 18 | 1.768 | 13.22 | 47 | 12.048 | 90.13 |
| 61/2 | . 2304 | 1.724 | 181/2 | 1.867 | 18.96 | 48 | 12.566 | 94.00 |

To find the capacity of pipes greater than those given, look in the table for a pipe of one half the given size, and multiply its capacity by 4 ; or one of one third its size, and multiply its capacity by 9 , etc.
To find the weight of water in any of the given sizes multiply the capacity in cubic feet by the weight of a cubic foot of water at the temperature of the water in the pipe.
To find the capacity of a cylinder in U. S. gallons, multiply the length by the square of the diameter and by 0.0034 .

CYLINDRICAL VESSELS, TANKS, CISTERNS, ETC.
Diameter in Feet and Inches, Area in Square Feet, and U. S. Gallons Capacity for One Foot in Depth.

1 gallon $=231$ cubic inches $=0.1337$ cubic foot.

| Diam. | Area. | Gals. | Diam. | Area. | Gals. | Diam. | Area. | Gals. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ft. In. | Sq. ft. | One foot depth. | Ft. In. | Sq. ft. | Onefoot depth. | Ft. In. | Sq. ft. | One foot depth. |
| 1 | 785 | 5.87 |  | 8.727 | 65.28 |  | 25.22 | 188.66 |
| 11 | . 922 | 6.89 | 35 | 9.168 | 68.58 | 5 9 | 25.97 | 194.25 |
| 12 | 1.069 | 8.00 |  | 9.621 | 71.97 | 510 | 26.73 | 199.92 |
| 13 | 1.227 | 9.18 |  | 10.085 | 75.44 | 511 | 27.49 | 205.67 |
| 1 | 1.396 | 10.44 |  | 10.559 | 7899 | 6 | 28.27 | 211.51 |
| 15 | 1.576 | 11.79 |  | 11.045 | 82.62 | $6 \quad 3$ | 30.68 | 229.50 |
| 16 | 1.767 | 13.22 | $3 \quad 10$ | 11.541 | 86.33 |  | 33.18 | 248.23 |
| 17 | 1.969 | 14.73 | 311 | 12.048 | 90.13 | 6 9 | 35.78 | 267.69 |
| 18 | 2.182 | 13.32 | 4 | 12.566 | 94.00 | 7 | 38.48 | 287.88 |
| 19 | 2.405 | 17.99 |  | 13.095 | 97.96 |  | 41.28 | 308.81 |
| 110 | 2.640 | 19.75 |  | 13.635 | 102.00 |  | 44.18 | 330.48 |
| 111 | 2.885 | 21.58 |  | 14.186 | 106.12 | $7 \quad 9$ | 47.17 | 352.88 |
| 2 | 3.142 | 23.50 |  | 14.748 | 110.32 | 8 | 50.27 | 376.01 |
| 21 | 3.409 | 25.50 |  | 15.321 | 114.61 | $8 \quad 3$ | 53.46 | 399.88 |
| 22 | 3.687 | 27.58 |  | 15.90 | 118.97 |  | 56.75 | 424.48 |
| 23 | 3.976 | 29.74 |  | 16.50 | 123.42 |  | 60.13 | 449.82 |
| 2 | 4.276 | 31.99 |  | 17.10 | 127.95 | 9 | 63.62 | 475.89 |
| 25 | 4.587 | 34.31 | $4 \quad 9$ | 17.72 | 132.56 |  | 67.20 | 502.70 |
| 26 | 4.909 | 36.72 | $4 \quad 10$ | 18.35 | 137.25 |  | 70.88 | 530.24 |
| 27 | 5.241 | 39.21 | 411 | 18.99 | 142.02 |  | 74.66 | 558.51 |
| 28 | 5.585 | 41.78 | 5 | 19.63 | 146.88 | 10 | 78.54 | 587.52 |
| 29 | 5.940 | 44.43 | 5 | 20.29 | 151.82 | $10 \quad 3$ | 82.52 | 617.26 |
| 210 | 6.305 | 47.16 | 5 2 | 20.97 | 156.83 | 106 | 86.59 | 647.74 |
| 211 | 6.681 | 49.98 | 5 | 21.65 | 161.93 | 109 | 90.76 | 678.95 |
| 3 | 7.069 | 52.88 | 54 | 22.34 | 167.12 | 11 | 95.03 | 710.90 |
| $3 \begin{array}{ll}3 & 1\end{array}$ | 7.467 | 55.86 | 5 5 | 23.04 | 172.38 | $11 \quad 3$ | 99.40 | 743.58 |
| $3 \quad 2$ | 7.876 | 58.92 | 56 | 23.76 | 177.72 | 11 | 103.87 | 776.99 |
| $3 \quad 3$ | 8.296 | 62.06 | 57 | 24.48 | 183.15 | 11.9 | 108.43 | 811.14 |

CYLINDRICAL VESSELS, TANKS, CISTERNS, ETC.
Diameter in Feet and Inches, Area in Square Feet, and U. S. Gallons Capacity for One Foot in Depth. 1 gallon $=231$ cubic inches $=0.1337$ cubic foot.
(CONTINUED.)

| Diam. | Area. | Gals. | Diam. | Area. | Gals. | Diam. | Area. | Gals. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ft. In. | Sq. ft. | One foot depth. | Ft. In. | Sq. ft. | One foot depth. | Ft. In. | Sq. ft. | One foot depth. |
| 12 | 113.10 | 846.03 | 19 | 283.53 | 2120.9 | 26 | 530.93 | 3971.6 |
| 12 | 117.86 | 881.65 | $19 \quad 3$ | 291.04 | 2177.1 | $26 \quad 3$ | 541.19 | 4048.4 |
| 12 | 122.72 | 918.00 |  | 298.65 | 2234.0 | $26 \quad 6$ | 551.55 | 4125.9 |
| 129 | 127.68 | 955.09 | $19 \quad 9$ | 306.35 | 2291.7 | 269 | 562.00 | 4204.1 |
| 13 | 132.73 | 992.91 | 20 | 314.16 | 2350.1 | 27 | 572.56 | 4283.0 |
| 13 | 137.89 | 1031.5 | $20 \quad 3$ | 322.06 | 2409.2 | $27 \quad 3$ | 583.21 | 4362.7 |
| 13 | 143.14 | 1070.8 | $20 \quad 6$ | 330.06 | 2469.1 | 276 | 593.96 | 4443.1 |
| 139 | 148.49 | 1110.8 | $20 \quad 9$ | 338.16 | 2529.6 | $27 \quad 9$ | 604.81 | 4524.3 |
| 14 | 153.94 | 1151.5 | 21 | 346.36 | 2591.0 | 28 | 615.75 | 4606.2 |
| 14 | 159.48 | 1193.0 | $21 \quad 3$ | 354.66 | 2653.0 | $28 \quad 3$ | 626.80 | 4688.8 |
| 14 | 165.13 | 1235.3 | $21 \quad 6$ | 363.05 | 2715.8 | 286 | 637.94 | 4772.1 |
| 14 | 170.87 | 1278.2 | $21 \quad 9$ | 371.54 | 2779.3 | 289 | 649.18 | 4856.2 |
| 15 | 176.71 | 1321.9 | 22 | 380.13 | 2843.6 | 29 | 660.52 | 4941.0 |
| 15 | 182.65 | 1366.4 | 223 | 388.82 | 2908.6 | 293 | 671.96 | 5026.6 |
| 15 | 6188.69 | 1411.5 | 226 | 397.61 | 2974.3 | 296 | 683.49 | 5112.9 |
| 15.9 | 194.83 | 1457.4 | 229 | 406.49 | 3040.8 | $29 \quad 9$ | 695.13 | 5199.9 |
| 16 | 201.06 | 1504.1 | 23 | 415.48 | 3108.0 | 30 | 706.86 | 5287.7 |
| 16 | 207.39 | 1551.4 | $23 \quad 3$ | 424.56 | 3175.9 | $30 \quad 3$ | 718.69 | 5376.2 |
| 16 | 613.82 | 1599.5 | 236 | 433.74 | 3244.6 | 306 | 730.62 | 5465.4 |
| 169 | 920.35 | 1648.4 | $23 \quad 9$ | 443.01 | 3314.0 | 309 | 742.64 | 5555.4 |
| 17 | 226.98 | 1697.9 | 24 | 452.39 | 3384.1 | 31 | 754.77 | 5646.1 |
| 17.3 | 3233.71 | 1748.2 | $24 \quad 3$ | 461.86 | 3455.0 | $31 \quad 3$ | 766.99 | 5737.5 |
| 17 | 6240.53 | 1799.3 | 246 | 471.44 | 3526.6 | 316 | 779.31 | 5829.7 |
| $17 \quad 9$ | 9247.45 | 1851.1 | $24 \quad 9$ | 481.11 | 3598.9 | 319 | 791.73 | 5922.6 |
| 18 | 254.47 | 1903.6 | 25 | 490.87 | 3672.0 | 32 | 804.25 | 6016.2 |
| 18 3 | 261.59 | 1956.8 | 253 | 500.74 | 3745.8 | 323 | 816.86 | 6110.6 |
| 18 | 6268.80 | 2010.8 | 256 | 510.71 | 3820.3 | 326 | 829.58 | 6205.7 |
| 189 | 276.12 | 2065.5 | 250 | 520.77 | 3895.6 | 329 | 842.39 | 6301.5 |

## Weight of Water in Foot Lengths of Pipe of Different Bores.

(62.425 Lbs. Per Cubic Foot.)

| Bore In. | Water Lbs. | Bore In. | Water Lbs. | Bore In. | Water Lbs. | Bore In. | Water Lbs. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1/8 | 0.0053 | 3 | 3.0643 | $73 / 4$ | 20.450 | 17 | 98.397 |
| $1 / 4$ | 0.0213 | 31/8 | 3.3250 | 8 | 21.790 | 171/2 | 104.27 |
| $3 / 8$ | 0.0479 | 31/4 | 3.5963 | 81/4 | 23.174 | 18 | 110.31 |
| 1/2 | 0.0851 | 33/8 | 3.8782 | $81 / 2$ | 24.599 | 181/2 | 116.53 |
| $5 / 8$ | 0.1330 | 31/2 | 4.1708 | $83 / 4$ | 26.068 | 19 | 122.91 |
| $3 / 4$ | 0.1915 | 35/8 | 4.4741 | 9 | 27.579 | 191/2 | 129.47 |
| 7/8 | 0.2607 | $33 / 4$ | 4.7879 | $91 / 4$ | 29.132 | 20 | 136.19 |
|  | 0.3405 | 37/8 | 5.1125 | $91 / 2$ | 30.728 | 21 | 150.15 |
| $11 / 8$ | 0.4309 |  | 5.4476 | 93/4 | 32.366 | 22 | 164.79 |
| 11/4 | 0.5320 | $41 / 4$ | 6.1498 | 10 | 34.048 | 23 | 180.11 |
| 13/8 | 0.6437 | 41/2 | 6.8946 | 101/2 | 37.537 | 24 | 196.11 |
| 11/2 | 0.7661 | 43/4 | 7.6820 | 11 | 41.198 | 25 | 212.80 |
| 15/8 | 0.8997 | 5 | 8.5119 | 111/2 | 45.028 | 26 | 230.16 |
| $13 / 4$ | 1.0427 | 51/4 | 9.3844 | 12 | 49.028 | 27 | 248.21 |
| 17/8 | 1.1970 | 51/2 | 10.299 | 121/2 | 53.199 | 28 | 266.93 |
| 2 | 1.3619 | 53/4 | 11.257 | 13 | 57.540 | 29 | 286.34 |
| 21/8 | 1.5375 | 6 | 12.257 | 131/2 | 62.052 | 30 | 306.43 |
| 21.4 | 1.7237 | 61/4 | 13.300 | 14 | 66.733 | 31 | 327.20 |
| 23/8 | 1.9205 | $61 / 2$ | 14.385 | 141/2 | 71.585 | 32 | 348.65 |
| $21 / 2$ | 2.1280 | 63/4 | 15.513 | 15 | ${ }^{76.607}$ | 33 | 370.78 |
| 25/8 | 2.3461 | 7 | 16.683 | $151 / 2$ | 81.799 | 34 | 393.59 |
| $23 / 4$ | 2.5748 | 71/4 | 17.896 | 16 | 87.162 | 35 | 417.08 |
| 27/8 | 2.8142 | 71/2 | 19.152 | 161/2 | 92.694 | 36 | 441.26 |

Weights of water in cylinders of the same length are proportional to the squares of the diameters. Therefore, to get weight of cylinder of water one foot long and 60 inches diameter, take from above table weight of water of 30 inch pipe and multiply it by the square of $60 \div 30$, or the square of two; thus, $306.43 \times 4=1225.72=$ the weight of water in one foot length of a 60 inch pipe.


## Number of U. S. Gallons in Rectangular Tanks.

For One Foot in Depth.


EXAMPLE.-To find number of gallons in a rectangular tank that is 7.5 ft . by 10 ft ., the water being 4 ft . deep: Look in extreme left hand column for 7.5 and opposite to this in column headed " 10 " read 561.04 , which being multiplied by 4 , the depth of water in the tank, gives 2244.2 the number of gallons required.
Theo Note．－The actual discharge will be less than the theoretical one given below，varying with the form of nozzle or tube through which the water flows．For a ring nozzle 64 per cent．，and for a good form of tapering smooth nozzle about 82 per cent．，can be assumed as the actual discharge．

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|  | 号 |  |

## WATER-POWER.

(Kent's Pocket Book.)

Power of a Fall of Water-Efficiency.-The gross power of a fall of water is the product of the weight of water discharged in a unit of time into the total head, i. e., the difference of vertical elevation of the upper surface of the water at the points where the fall in question begins and ends. The term " head" used in connection with waterwheels is the difference in height from the surface of the water in the wheel-pit to the surface in the pen-stock when the wheel is running.

If $Q=$ cubic feet of water discharged per second, $D=$ weight of a cubic foot of water $=62.36 \mathrm{lbs}$. at $60^{\circ} \mathrm{F} ., H$ $=$ total head in feet; then
$D Q H=$ gross power in foot-pounds per second, and $D Q H \div 550=0.1134 Q H=$ gross horse power.

If $Q^{\prime}$ is taken in cubic feet per minute,

$$
\text { H. P. }=\frac{Q^{\prime} H \times 62.36}{33,000}=0.00189 Q^{\prime} H
$$

A water-wheel or motor of any kind cannot utilize the whole of the head $H$, since there are losses of head at both the entrance to and the exit from the wheel. There are also losses of energy due to friction of the water in its passage through the wheel. The ratio of the power developed by the wheel to the gross power of the fall is the efficiency of the wheel. For $75 \%$ efficiency, net horsepower $=0.00142 Q^{\prime} H=\frac{Q^{\prime} H}{706}$

Horse-power of Water Flowing in a Tube.-The head due to the velocity is $\frac{v^{2}}{2 g}$; the head due to the pressure is $\frac{f}{w}$; the head due to actual height above the datum plane is $h$ feet. The total head is the sum of these $=\frac{v^{2}}{2 g}+h+\frac{f}{w^{3}}$ in feet, in which $v=$ velocity in feet per second, $f=$ pressure in lbs. per sq. ft., $w=$ weight of $1 \mathrm{cu} . \mathrm{ft}$. of water $=62.4 \mathrm{lbs}$. If $p=$ pressure in lbs. per sq. in., $\frac{f}{w}=2.309 p$. In hydraulic transmission the velocity and the height above datum are usually small compared with the pressure-head. The work or energy of a given quantity of water under pressure $=$ its volume in cubic feet $\times$ its pressure in lbs. per sq. ft .; or if $Q=$ quantity in cubic feet per second, and $p=$ pressure in lbs. per square inch, $W=144 p Q$, and the H. P. $=\frac{144 p Q}{550}=0.2618 p Q$.
Formula for Computing Power of Jet Water-Wheels of the Pelton Type. (F, K. Blue).
Let $H P=$ horse-power delivered by the water-wheel ; $d=$ diameter of nozzle ; $w=$ weight of one $\mathrm{cu} . \mathrm{ft}$. of water, or 62.5 lbs ; $E=$ efficiency of the water-wheel ; $q=$ quantity of water in cubic feet per minute ; $c=$ coefficient of discharge from the nozzle, which may be ordinarily taken as $0.9 ; h=$ effective head (actual head less friction head) in feet ; then

$$
\begin{gathered}
\mathrm{HP}=\frac{\mathrm{wE} \mathrm{q} \mathrm{~h}}{33,000}=0.00189 \mathrm{Eq} \mathrm{~h}=0.00436 \mathrm{Eq} \mathrm{p} .= \\
0.00496 \mathrm{Ec} \mathrm{~d} \\
\mathrm{q}=529 \frac{\mathrm{HP}}{\mathrm{Eh}}=2.62 \mathrm{c}^{\mathrm{h}^{3}}=0.0174 \mathrm{Ec} \mathrm{~d} \sqrt{\mathrm{~h}}=4 \mathrm{c} \mathrm{~d}^{2} \sqrt{\mathrm{p}^{3}} . \\
\mathrm{d}=14.2 \sqrt{\frac{\mathrm{HP}}{\mathrm{Ec} \sqrt{\mathrm{~h}^{3}}}}=7.58 \sqrt{\frac{\mathrm{HP}}{\mathrm{Ec} \sqrt{\mathrm{p}^{3}}}}= \\
0.62 \sqrt{\frac{\mathrm{q}}{\mathrm{c} \sqrt{\mathrm{~h}}}}=1 / 2 \sqrt{\frac{\mathrm{q}}{\mathrm{c} \sqrt{\mathrm{p}}}} .
\end{gathered}
$$

The Pelton Water-wheel.-Mr. Ross E. Browne (Eng'g News, Feb. 20 , 1892) thus outlines the principles upon which this water-wheel is constructed :

The function of a water-wheel, operated by a jet of water escaping from a nozzle, is to convert the energy of the jet, due to its velocity, into useful work. In order to utilize this energy fully the wheel-bucket, after catching the jet, must bring it to rest before discharging it, without inducing turbulence or agitation of the particles.

This cannot be fully effected, and unavoidable difficulties necessitate the loss of a portion of the energy. The principal losses occur as follows : First, in sharp or angular diversion of the jet in entering, or in its course through the bucket, causing impact, or the conversion of a portion of the energy into heat instead of useful work. Second, in the so-called frictional resistance offered to the motion of the water by the wetted surfaces of the buckets, causing also the conversion of a portion of the energy into heat instead of useful work. Third, in the velocity of the water, as it leaves the bucket, representing energy which has not been converted into work

Hence, in seeking a high efficiency: 1. The bucketsurface at the entrance should be approximately parallel to the relative course of the jet, and the bucket should be curved in such a manner as to avoid sharp angular deflection of the stream. If, for example, a jet strikes a surface at an angle and is sharply deflected, a portion of the water is backed, the smoothness of the stream is disturbed, and there results considerable loss by impact and otherwise. The entrance and deflection in the Pelton bucket are such as to avoid these losses in the main.


Fig. 134.


Fig. 135.
2. The number of buckets should be small, and the path of the jet in the bucket short; in other words, the total wetted surface should be small, as the loss by friction will be proportional to this.
3. The discharge end of the bucket should be as nearly tangential to the wheel periphery as compatible with the clearance of the bucket which follows; and great differences of velocity in the parts of the escaping water should be avoided. In order to bring the water to rest at the discharge end of the bucket, it is shown, mathematically, that the velocity of the bucket should be one half the velocity of the jet.

A bucket, such as shown in Fig. 135, will cause the heaping of more or less dead or turbulent water at the point indicated by dark shading. This dead water is subsequently thrown from the wheel with considerable velocity, and represents a large loss of energy. The introduction of the wedge in the Pelton bucket (see Fig. 134) is an efficient means of avoiding this loss.

A wheel of the form of the Pelton conforms closely in construction to each of these requirements.

In a test made by the proprietors of the Idaho mine, near Grass Valley, Cal., the dimensions and results were as follows: Main supply-pipe, 22 in . diameter, 6900 ft . long, with the head of $3861 / 2$ feet above centre of nozzle. The loss by friction in the pipe was 1.8 ft ., reducing the effective head to 384.7 ft . The Pelton wheel used in the test was 6 ft . in diameter and the nozzle was 1.89 in . diameter. The work done was measured by a Prony brake, and the mean of 13 tests showed a useful effect of $87.3 \%$.


Fig. 136.

## Miners' Inch Measurements. (Pelton Water Wheel Co.)

The cut, Fig. 136, shows the form of measuring-box ordinarily used, and the following table gives the discharge in cubic feet per minute of a miner's inch of water, as measured under the various heads and different lengths and heights of apertures used in California.

| Length of Opening in inches. | Openings 2 Inches High. |  |  | Openings 4 Inches High. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Head to | Head to | Head to | Head to | Head to | Head to |
|  | Centre 5 inches. | Centre 6 inches. | Centre 7 inches. | Centre, <br> 5 inches. | Centre, 6 inches. | Centre, 7 inches. |
|  | Cu ft . | Cu ft . | $\mathrm{Cu} . \mathrm{ft}$. | Cu. ft. | Cu. ft. | Cu. ft. |
| 4 | 1.348 | 1.473 | 1.589 | 1.320 | 1.450 | 1.570 |
| 6 | 1.355 | 1.480 | 1.596 | 1.336 | 1.470 | 1.595 |
| 8 | 1.359 | 1.484 | 1.600 | 1.344 | 1.481 | 1.608 |
| 10 | 1.361 | 1.485 | 1.602 | 1.349 | 1.487 | 1.615 |
| 12 | 1.363 | 1.487 | 1.604 | 1.352 | 1.491 | 1.620 |
| 14 | 1.364 | 1.488 | 1.604 | 1.354 | 1.494 | 1.623 |
| 16 | 1.365 | 1.489 | 1.605 | 1.356 | 1.496 | 1.626 |
| 18 | 1.365 | 1.489 | 1.606 | 1.357 | 1.498 | 1.628 |
| 20 | 1.365 | 1.490 | 1.606 | 1.359 | 1.499 | 1.630 |
| 22 | 1.366 | 1.490 | 1.607 | 1.359 | 1.500 | 1.631 |
| 24 | 1.366 | 1.490 | 1.607 | 1.360 | 1.501 | 1.632 |
| 26 | 1.366 | 1.490 | 1.607 | 1.361 | 1.502 | 1.633 |
| 28 | 1.367 | 1.491 | 1.607 | 1.361 | 1.503 | 1.634 |
| 30 | 1.367 | 1.491 | 1.608 | 1.362 | 1.503 | 1.635 |
| 40 | 1.367 | 1.492 | 1.608 | 1.363 | 1.505 | 1.637 |
| 50 | 1.368 | 1.493 | 1.609 | 1.364 | 1.507 | 1.639 |
| 60 | 1.368 | 1.493 | 1.609 | 1.365 | 1.508 | 1.640 |
| 70 | 1.368 | 1.493 | 1.609 | 1.365 | 1.508 | 1.641 |
| 80 | 1.368 | 1.493 | 1.609 | 1.366 | 1.509 | 1.641 |
| 90 | 1.369 | 1.493 | 1.610 | 1.366 | 1.509 | 1.641 |
| 100 | 1.369 | 1.494 | 1.610 | 1.366 | 1.509 | 1.642 |

## PUMPS AND PUMPING ENGINES.

## (Kent's Pocket Book.)

Theoretical Capacity of a Pump.-Let $Q^{\prime}=\mathrm{cu} . \mathrm{ft}$. per min. $; G^{\prime}=$ Amer. gals. per min. $=7.4805 Q^{\prime} ; d=$ dianı. of pump in inches ; $l=$ stroke in inches; $N=$ number of single strokes per min.

Capacity in $\mathrm{cu} . \mathrm{ft}$. per min.

$$
Q^{\prime}=\frac{\pi}{4} \cdot \frac{d^{2}}{144} \cdot \frac{l N}{12}=0.0004545 N d^{2} l
$$

Capacity in gals. per min.

$$
G^{\prime}=\frac{\pi}{4} \cdot \frac{N d^{2} l}{231}=0.0034 N d^{2} l
$$

Diameter required for a given capacity per min.

$$
d=46.9 \sqrt{\frac{Q^{\prime}}{N l}}=17.15 \sqrt{\frac{G^{\prime}}{N l}}
$$

If $v=$ piston speed in feet per min.,

$$
d=13.54 \sqrt{\frac{Q^{\prime}}{v}}=4.95 \sqrt{\frac{\bar{G}^{\prime}}{v}}
$$

If the piston speed is 100 feet per min.:

$$
\begin{gathered}
N l=1200, \text { and } d=1.354 \sqrt{Q^{\prime}}=0.495 \sqrt{G^{\prime}} ; \\
G^{\prime}=4.08 d^{2} \text { per min. }
\end{gathered}
$$

The actual capacity will be from $60 \%$ to $95 \%$ of the theoretical, according to the tightness of the piston, valves, suction-pipe, etc.

Theoretical Horse-power required to raise Water to a given Height.

Let $Q^{\prime}=\mathrm{cu} . \mathrm{ft}$. per $\min . ; G^{\prime}=$ gals. per $\min . ; W=\mathrm{wt}$. in lbs.; $P=$ pressure in lbs. per sq. ft.; $p=$ pressure in lbs. per sq. in.; $H=$ height of lift in ft .; $W=62.36 Q^{\prime}, P$ $=144 p, p=0.433 H, H=2.309 p, \mathrm{G}^{\prime}=7.4805 Q^{\prime}$.

$$
\begin{aligned}
& \mathrm{HP}=\frac{Q^{\prime} P}{33,000}=\frac{Q^{\prime} H \times 144 \times .433}{33,000}=\frac{Q^{\prime} H}{529.2}=\frac{G^{\prime} H}{3958.7} \\
& \mathrm{HP}=\frac{W H}{33,000}=\frac{Q^{\prime} \times 62.36 \times 2.309 p}{33,000}=\frac{Q^{\prime} p}{229.2}=\frac{G^{\prime} p}{1714.5}
\end{aligned}
$$

For the actual horse-power required an allowance must be made for the friction, slips, etc., of engine, pump, valves, and passages.

Depth of Suction,-Theoretically a perfect pump will lift water from a depth of nearly 34 feet, corresponding to a perfect vacuum ( $14.7 \mathrm{lbs} . \times 2.309=33.95$ feet); but since a perfect vacuum cannot be obtained, on account of valve-leakage, air contained in the water, and the vapor of the water itself, the actual height is generally less than 30 feet. In pumping hot water, the water must flow into the pump by gravity. The following table shows the theoretical maximum depth of suction for different temperatures, leakage not considered :

| $\begin{gathered} \dot{x} \\ \dot{Z} \\ \underset{\sim}{0} \\ H \end{gathered}$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 101.4 | 1 | 27.88 | 31.6 | 183.0 | 8 | 13.63 | 15.5 |
| 126.2 | 2 | 25.85 | 29.3 | 188.4 | 9 | 11.59 | 13.2 |
| 144.7 | 3 | 23.81 | 27.0 | 193.2 | 10 | 9.55 | 10.9 |
| 153.3 | 4 | 21.77 | 24.7 | 197.6 | 11 | 7.51 | 8.5 |
| 162.5 | 5 | 19.74 | 22.4 | 201.9 | 12 | 5.48 | 6.2 |
| 170.3 | 6 | 17.70 | 20.1 | 205.8 | 13 | 3.44 | 3.9 |
| 177.0 | 7 | 15.66 | 17.8 | 209.6 | 14 | 1.40 | 1.6 |



## STEAM

AND
STEAM APPARATUS.

## STEAM.

Under the ordinary atmospheric pressure of 14.7 pounds per square inch, water boils at $212^{\circ}$ Fahr., passing off as steam, the temperature at which it boils varying with a variation in the pressure.

Dry steam is steam not containing any free moisture. It may be either saturated or superheated.

Wet steam is steam containing free moisture in the form of spray or mist, and has the same temperature as dry saturated steam of the same pressure.

Saturated steam is steam in its normal state, that is, steam whose temperature is that due its pressure; by which is meant steam at the same temperature as that of the water from which it was generated and upon which it rests.

Superheated steam is steam at a temperature above that due to its pressure.

A British thermal unit is the quantity of heat required to raise one pound of water at $39^{\circ} .1$ Fahr. through one degree of temperature.

The total heat of the water is the number of British thermal units needed to raise one pound of water from $32^{\circ} \mathrm{F}$. to the boiling point, under the given pressure.

The latent heat of steam is the number of British thermal units required to convert one pound of water, at the boiling point, into steam of the same temperature.

The total heat of saturated steam is the number of heat units required to raise a pound of water from $32^{\circ} \mathrm{F}$. to the boiling point, at the given pressure, plus the number required to evaporate the water at that temperature.

The specific heat of steam is the quantity of heat required to raise the temperature of one pound of steam through one degree of temperature. In British units and near the saturation temperature it equals, at constant pressure, 0.48 .

The specific gravity of steam at any temperature and pressure, as compared with air of same temperature and pressure, is approximately 0.623 . One cubic inch of water evaporated into steam at $212^{\circ} \mathrm{F}$. becomes 1646 cubic in., that is, nearly one cu. ft.

Water in contact with saturated steam has the same temperature as the steam itself. Water introduced into superheated steam will be vaporized until the steam becomes saturated, and its temperature becomes that due its pressure. Cold water, or water at a lower temperature than that of the steam, introduced into saturated steam, will condense some of it, thus lowering both the temperature and pressure of the rest until the temperature again equals that due its pressure.

## PROPERTIES OF SATURATED STEAM．

|  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 101.99 | 70.0 | 1043.0 | 1113.1 | 0.00299 | 334.5 |
| 2 | 126.27 | 94.4 | 1026.1 | 1120.5 | 0.00576 | 173.6 |
| 3 | 141.62 | 109.8 | 1015.3 | 1125.1 | 0.00844 | 118.5 |
| 4 | 153.09 | 121.4 | 1007.2 | 1128.6 | 0.01107 | 90.33 |
| 5 | 162.34 | 130.7 | 1000.8 | 1131.5 | 0.01366 | 73.21 |
| 6 | 170.14 | 138.6 | 995.2 | 11338 | 0.01622 | 61.65 |
| 7 | 176.90 | 145.4 | 990.5 | 1135.9 | 0.01874 | 53.39 |
| 8 | 182.92 | 151.5 | 986.2 | 1137.7 | 0.02125 | 47.06 |
| 9 | 188.33 | 156.9 | 982.5 | 1139.4 | 0.02374 | 42.12 |
| 10 | 193.25 | 161.9 | 979.0 | 1140.9 | 0.02621 | 38.15 |
| 15 | 213.03 | 181.8 | 965.1 | 1146.9 | 0.03826 | 26.14 |
| 20 | 227.95 | 196.9 | 954.6 | 1151.5 | 0.05023 | 19.91 |
| 25 | 240.04 | 209.1 | 946.0 | 1155.1 | 0.06199 | 16.13 |
| 30 | 250.27 | 219.4 | 938.9 | 1158.3 | 0.07360 | 13.59 |
| 35 | 259.19 | 228.4 | 932.6 | 1161.0 | 0.08508 | 11.75 |
| 40 | 267.13 | 236.4 | 927.0 | 1163.4 | 0.09644 | 10.37 |
| 45 | 274.29 | 243.6 | 922.0 | 1165.6 | 0.1077 | 9.285 |
| 50 | 280.85 | 250.2 | 917.4 | 1167.6 | 0.1188 | 8.418 |
| 55 | 286.89 | 256.3 | 913.1 | 1169.4 | 0.1299 | 7.698 |
| 60 | 292.51 | 261.9 | 909.3 | 1171.2 | 0.1409 | 7.097 |
| 65 | 297.77 | 267.2 | 905.5 | 1172.7 | 0.1519 | 6.583 |
| 70 | 302.71 | 272.2 | 902.1 | 1174.8 | 0.1628 | 6.143 |
| 75 | 307.38 | 276.9 | 898.8 | 1175.7 | 0.1736 | 5.760 |
| 80 | 311.80 | 281.4 | 895.6 | 1177.0 | 0.1843 | 5.426 |
| 85 | 316.02 | 285.8 | 892.5 | 1178.3 | 0.1951 | 5.126 |
| 90 | 320.04 | 290.0 | 889.6 | 1179.6 | 0.2058 | 4.859 |
| 95 | 323.89 | 294.0 | 886.7 | 1180.7 | 0.2165 | 4.619 |
| 100 | 327.58 | 297.9 | 884.0 | 1181.9 | 0.2271 | 4.403 |
| 105 | 331.13 | 301.6 | 881.3 | 1182.9 | 0.2378 | 4.205 |
| 110 | 334.56 | 305.2 | 878.8 | 1184.0 | 0.2484 | 4.026 |
| 115 | 337.86 | 308.7 | 876.3 | 1185.0 | 0.2589 | 3.862 |
| 120 | 341.05 | 312.0 | 874.0 | 1186.0 | 0.2695 | 3.711 |
| 125 | 344.13 | 315.2 | 871.7 | 1186.9 | 0.2800 | 3.571 |
| 130 | 347.12 | 318.4 | 869.4 | 1187.8 | 0.2904 | 3.444 |
| 140 | 352．85 | 324.4 | 865.1 | 1189.5 | 0.3118 | 3.212 |
| 150 | 358.26 | 330.0 | 861.2 | 1191.2 | 0.3321 | 3.011 |
| 160 | 363.40 | 335.4 | 857.4 | 1192.8 | 0.3530 | 2.833 |
| 170 | 368.29 | 340.5 | 853.8 | 1194.3 | 0.8737 | 2.676 |
| 180 | 372.97 | 345.4 | 850.3 | 1195.7 | 0.3945 | 2.535 |
| 190 | 377.44 | 350.1 | 847.0 | 1197.1 | 0.4153 | 2.408 |
| 200 | 381.73 | 354.6 | 843.8 | 1198.4 | 0.4359 | 2.294 |
| 225 | 391.79 | 365.1 | 836.3 | 1201.4 | 0.4876 | 2.051 |
| 250 | 400.99 | 374.7 | 829.5 | 1204.2 | 0.5393 | 1.854 |
| 275 | 409.50 | 383.6 | 823.2 | 1206.8 | 0.5913 | 1． 691 |
| 300 | 417.42 | 391.9 | 817.4 | 1209.3 | 0.644 | 1.553 |
| 325 | 424.82 | 399.6 | 811.9 | 1211.5 | 0.696 | 1.437 |
| 350 | 431.90 | 406.9 | 806.8 | 1213.7 | 0.748 | 1.337 |
| 375 | 438.40 | 414.2 | 801.5 | 1215.7 | 0.800 | 1.250 |
| 400 | 445.15 | 421.4 | 796.8 | 1217.7 | 0.853 | 1.172 |
| 500 | 466.57 | 444.8 | 779.9 | 1224.2 | 1.065 | 0.939 |

The absolute pressures given in column one may be converted into gauge pressures by subtracting the constant 14．7：Thus， 115 lbs．，absolute $=115-14.7=100.3$ lbs．gauge．

## FACTORS OF EVAPORATION.

|  | STEAM PRESSURE IN POUNDS PER SQUARE INCH, GAUGE. |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0. | 5. | 15 | 25. | 35. | 45. | 55. | 65. | 75. | 85. |
| Dgrs. |  |  |  |  |  |  |  |  |  |  |
| 32 | $1.18{ }^{\text {\% }}$ | 1.192 | 1.199 | 1.204 | 1.209 | 1.212 | 1.216 | 1.218 | 1.221 | 1.223 |
| 35 | 1.184 | 1.189 | 1.196 | 1.201 | 1.206 | 1.209 | 1.213 | 1.215 | 1.218 | 1.220 |
| 40 | 1.179 | 1.184 | 1.191 | 1.196 | 1.201 | 1.204 | 1.208 | 1.219 | 1.213 | 1.215 |
| 45 | 1.173 | 1.178 | 1.185 | 1.190 | 1.195 | 1.198 | 1.202 | 1.204 | 1.207 | 1.209 |
| 50 | 1.168 | 1.173 | 1.180 | 1.185 | 1.190 | 1.193 | 1.197 | 1.199 | 1.202 | 1.204 |
| 55 | 1.163 | 1.168 | 1.175 | 1.180 | 1.185 | 1.188 | 1.192 | 1.194 | 1.197 | 1.199 |
| 60 | 1.158 | 1.163 | 1.170 | 1.175 | 1.180 | 1.183 | 1.187 | 1.189 | 1.192 | 1.194 |
| 65 | 1.153 | 1.158 | 1.165 | 1.170 | 1.175 | 1.178 | 1.182 | 1.184 | 1.187 | 1.189 |
| 70 | 1.148 | 1.153 | 1.160 | 1.165 | 1.170 | 1.173 | 1.177 | 1.179 | 1.182 | 1.184 |
| 75 | 1.143 | 1.148 | 1.155 | 1.160 | 1.165 | 1.168 | 1.172 | 1.174 | 1.177 | 1.179 |
| 80 | 1.137 | 1.142 | 1.149 | 1.154 | 1.159 | 1.162 | 1.166 | 1.168 | 1.171 | 1.173 |
| 85 | 1.132 | 1.137 | 1.144 | 1.149 | 1.154 | 1.157 | 1.161 | 1.163 | 1.166 | 1.168 |
| 90 | 1.127 | 1.132 | 1.139 | 1.144 | 1.149 | 1.152 | 1.156 | 1.158 | 1.161 | 1.163 |
| 95 | 1.122 | 1.127 | 1.134 | 1.139 | 1.144 | 1.147 | 1.151 | 1.153 | 1.156 | 1.158 |
| 100 | 1.117 | 1.122 | 1.129 | 1.134 | 1.139 | 1.142 | 1.146 | 1.148 | 1.151 | 1.153 |
| 105 | 1.111 | 1.116 | 1.123 | 1.128 | 1.133 | 1.136 | 1.140 | 1.142 | 1.145 | 1.147 |
| 110 | 1.106 | 1.111 | 1.118 | 1.123 | 1.128 | 1.131 | 1.135 | 1.137 | 1.140 | 1.142 |
| 115 | 1.101 | 1.106 | 1.113 | 1.118 | 1.123 | 1.126 | 1.130 | 1.132 | 1.135 | 1.187 |
| 120 | 1.096 | 1.101 | 1.108 | 1.113 | 1.118 | 1.121 | 1.125 | 1.127 | 1.130 | 1.132 |
| 125 | 1.091 | 1.096 | 1.103 | 1.108 | 1.113 | 1.116 | 1.120 | 1.122 | 1.125 | 1.127 |
| 130 | 1.085 | 1.090 | 1.097 | 1.102 | 1.107 | 1.110 | 1.114 | 1.116 | 1.119 | 1.121 |
| 135 | 1.080 | 1.085 | 1.092 | 1.097 | 1.102 | 1.105 | 1.109 | 1.111 | 1.114 | 1.116 |
| 140 | 1.075 | 1.080 | 1.087 | 1.092 | 1.097 | 1.100 | 1.104 | 1.106 | 1.109 | 1.111 |
| 145 | 1.070 | 1.075 | 1.082 | 1.087 | 1.092 | 1.095 | 1.099 | 1.101 | 1.104 | 1.106 |
| 150 | 1.065 | 1.070 | $1.0 \mathrm{C}^{7}$ | 1.082 | 1.087 | 1.090 | 1.094 | 1.096 | 1.099 | 1.101 |
| 155 | 1.059 | 1.064 | 1.071 | 1.076 | 1.081 | 1.084 | 1.088 | 1.090 | 1.094 | 1.095 |
| 160 | 1.054 | 1.059 | 1.066 | 1.071 | 1.076 | 1.079 | 1.083 | 1.085 | 1.088 | 1.090 |
| 165 | 1.049 | 1.054 | 1.061 | 1.066 | 1.071 | 1.074 | 1.078 | 1.080 | 1.083 | 1.085 |
| 170 | 1.044 | 1.049 | 1.056 | 1.061 | 1.066 | 1.069 | 1.073 | 1.075 | 1.078 | 1.080 |
| 175 | 1.039 | 1.044 | 1.051 | 1.056 | 1.061 | 1.064 | 1.068 | 1.070 | 1.073 | 1.075 |
| 180 | 1.033 | 1.038 | 1.045 | 1.050 | 1.055 | 1.058 | 1.062 | 1.064 | 1.067 | 1.069 |
| 185 | 1.028 | 1.033 | 1.040 | 1.045 | 1.050 | 1.053 | 1.057 | 1.059 | 1.062 | 1.064 |
| 190 | 1.023 | 1.028 | 1.035 | 1.040 | 1.045 | 1.048 | 1.052 | 1.054 | 1.057 | 1.059 |
| 195 200 | 1.018 | 1.023 | 1.030 | 1.035 | 1.040 | 1.043 | 1.047 | 1.049 | 1.052 | 1.054 |
| 200 | 1.013 | 1.018 | 1.025 | 1.030 | 1.035 | 1.038 | 1.042 | 1.044 | 1.047 | 1.049 |
| 205 | 1.007 | 1.012 | 1.019 | 1.024 | 1.029 | 1.032 | 1.036 | 1.038 | 1.041 | 1.043 |
| 210 | 1.002 | 1.007 | 1.014 | 1.019 | 1.024 | 1.027 | 1.031 | 1.033 | 1.036 | 1.038 |
| 212 | 1.000 | 1.005 | 1.012 | 1.017 | 1.022 | 1.025 | 1.029 | 1.081 | 1.084 | 1.036 |

## FACTORS OF EVAPORATION.

| Tivid | STEAM PRESSURE IN POUNDS PER SQUARE INCH, GAUGE. |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 95. | 105. | 115. | 125. | 135. | 145. | 155. | 165. | 175. | 185. |
| Dgrs. |  |  |  |  |  |  |  |  |  |  |
| 32 | 1.226 | 1.228 | 1.230 | 1.231 | 1.233 | 1.235 | 1.236 | 1.238 | 1.239 | 1.240 |
| 35 | 1.223 | 1.225 | 1.227 | 1.228 | 1.230 | 1.232 | 1.233 | 1.235 | 1.236 | 1.237 |
| 40 | 1.218 | 1.220 | 1.222 | 1.223 | 1.225 | 1.227 | 1.228 | 1.230 | 1.231 | 1.232 |
| 45 | 1.212 | 1.214 | 1.216 | 1.217 | 1.219 | 1.221 | 1.222 | 1.224 | 1.225 | 226 |
| 50 | 1.207 | 1.209 | 1.211 | 1.212 | 1.214 | 1.216 | 1.217 | 1.219 | 1.220 | 1.221 |
| 55 | 1.202 | 1.204 | 1.206 | 1.207 | 1.209 | 1.211 | 1.212 | 1.214 | 1.215 | 1.216 |
| 60 | 1.197 | 1.199 | 1.201 | 1.202 | 1.204 | 1.206 | 1.207 | 1.209 | 1.210 | 1.211 |
| 65 | 1.192 | 1.194 | 1.196 | 1.197 | 1.199 | 1.201 | 1.202 | 1.204 | 1.205 | 1.206 |
| 70 | 1.187 | 1.189 | 1.191 | 1.192 | 1.194 | 1.196 | 1.197 | 1.199 | 1.200 | 1.201 |
| 75 | 1.182 | 1.184 | 1.186 | 1.187 | 1.189 | 1.191 | 1.192 | 1.194 | 1.195 | 1.196 |
| 80 | 1.176 | 1.178 | 1.180 | 1.181 | 1.183 | 1.185 | 1.186 | 1.188 | 1.189 | 1.190 |
| 85 | 1.171 | 1.173 | 1.175 | 1.176 | 1.178 | 1.180 | 1.181 | 1.183 | 1.184 | 1.185 |
| 90 | 1.166 | 1.168 | 1.170 | 1.171 | 1.173 | 1.175 | 1.176 | 1.178 | 1.179 | 1.180 |
| 95 | 1.161 | 1.163 | 1.165 | 1.166 | 1.168 | 1.170 | 1.171 | 1.173 | 1.174 | 1.175 |
| 100 | 1.156 | 1.158 | 1.160 | 1.161 | 1.163 | 1.165 | 1.166 | 1.168 | 1.169 | 1.170 |
| 105 | 1.150 | 1.152 | 1.154 | 1.155 | 1.157 | 1.159 | 1.160 | 1.162 | 1.163 | 1.164 |
| 110 | 1.145 | 1.147 | 1.149 | 1.150 | 1.152 | 1.154 | 1.155 | 1.157 |  | 1.159 |
| 115 | 1.140 | 1.142 | 1.144 | 1.145 | 1.147 | 1.149 | 1.150 |  | 1.153 | 1.154 |
| 120 | 1.135 | 1.137 | 1.139 | 1.140 | 1.142 | 1.144 | 1.145 | 1.147 | 1.148 | 1.149 |
| 125 | 1.130 | 1.132 | 1.134 | 1.135 | 1.137 | 1.139 | 1.140 | 1.142 | 1.143 |  |
| 130 | 1.124 | 1.126 | 1.128 | 1.129 | 1.131 | 1.133 | 1.134 | 1.136 | 1.137 | 1.138 |
| 135 | 1.119 | 1.121 | 1.123 | 1.124 | 1.186 | 1.128 | 1.129 | 1.131 | 1.132 | 1.133 |
| 140 | 1.114 | 1.116 | 1.118 | 1.119 | 1.121 | 1.123 | 1.124 | 1.126 | 1.127 | 1.128 |
| 145 | 1.109 | 1.111 | 1.113 | 1.114 | 1.116 | 1.118 | 1.119 | 1.121 | 1.122 | 1.123 |
| 150 | 1.104 | 1.106 | 1.108 | 1.109 | 1.111 | 1.118 | 1.114 | 1.116 | 1.117 | 1.118 |
| 155 | 1.098 | 1.100 | 1.102 | 1.103 | 1.105 | 1.107 | 1.108 | 1.110 | 1.111 | 1.112 |
| 160 | 1.093 | 1.095 | 1.097 | 1.098 | 1.100 | 1.102 | 1.103 | 1.105 | 1.106 | 1.107 |
| 165 | 1.088 | 1.090 | 1.092 | 1.093 | 1.095 | 1.097 | 1.098 | 1.100 | 1.101 | 1.102 |
| 170 | 1.083 | 1.085 | 1.087 | 1.088 | 1.090 | 1.092 | 1.093 | 1.095 | 1.096 | 1.097 |
| 175 | 1.078 | 1.080 | 1.082 | 1.083 | 1.085 | 1.087 | 1.088 | 1.090 | 1.091 | 1.092 |
| 180 | 1.072 | 1.074 | 1.076 | 1.077 | 1.079 | 1.081 | 1.082 | 1.084 | 1.085 | 1.086 |
| 185 | 1.067 | 1.069 | 1.071 | 1.078 | 1.074 | 1.076 | 1.077 | 1.079 | 1.080 | 1.081 |
| 190 | 1.062 | 1.064 | 1.066 | 1.067 | 1.069 | 1.071 | 1.072 | 1.074 | 1.075 | 1.076 |
| 195 | 1.057 | 1.059 | 1.061 | 1.062 | 1.064 | 1.066 | 1.066 | 1.069 | 1.070 | 1.071 |
| 200 | 1.052 | 1.05 | 1.056 | 1.057 | 1.05 | 1.061 | 1.062 | 1.064 | 1.0 | 1. |
| 205 | 1.046 | 1.048 | 1.050 | 1.051 | 1.053 | 1.055 | 1.056 | 1.058 | 1.059 | 1.060 |
| 210 | 1.041 | 1.043 | 1.045 | 1.046 | 1.048 | 1.050 | 1.051 | 1.053 | 1.054 | 1.055 |
| 212 | 1.039 | 1.041 | 1.043 | 1.044 | 1.046 | 1.048 | 1.049 | 1.051 | 1.052 | 1.053 |

## Explanation of Table of Properties of Saturated Steam:

 The first column shows the absolute pressure of steam as it rises freely from water of the same temperature, and is equal to 14.7 lbs . + the pressure shown by the steam gauge.The second column shows the temperatures in degrees Fahrenheit at which water vaporizes under the pressures opposite in column one.

The third column shows the number of British thermal units required to raise one pound of water from $32^{\circ} \mathrm{F}$. to the boiling temperatures opposite in column two.

The fourth column shows the number of heat units that are absorbed, or changed from sensible to latent heat, when one pound of water at the boiling point changes to steam of the same temperature.

The fifth column shows the number of heat units absorbed when one pound of water at $32^{\circ} \mathrm{F}$. has its temperature raised to the boiling point and is then changed to steamat constant pressure and temperature. This column gives the total heat of formation of steam from water at $32^{\circ} \mathrm{F}$.

The sixth column shows the weights in pounds per cubic ft . of saturated steam at the corresponding pressures and temperatures given in columns one and two.

The seventh column shows volumes in cubic ft. of one pound of steam.

Explanation of Table of Factors of Evaporation: The factors in this table were obtained, for the various feedwater temperatures and steam pressures given, by subtracting the heat above $32^{\circ} \mathrm{F}$. in one pound of feed-water from the total heat above $32^{\circ}$ in one pound of steam, and then dividing the remainder thus obtained by 965.7 , the latent heat of steam at atmospheric pressure.

Example:-Given the boiler pressure $=105 \mathrm{lbs}$. per square in. guage, and the feed-water temperature $=55^{\circ} \mathrm{F}$.; to find the factor of evaporation. Look in the column or steam pressures headed 105 and opposite to 55 degrees in the first column, read 1.204, the factor required. It will therefore require 1.204 times as many heat units to evaporate a certain weight of water from a feed-water temperature of $55^{\circ} \mathrm{F}$. into steam under 105 pounds guage as would be required to evaporate the same weight of water from a temperature of $212^{\circ} \mathrm{F}$. into steam under one atmospheric pressure. that is, from and at $212^{\circ} \mathrm{F}$.
This table is useful in rating boilers and in preparing reports of tests.

## FLOW OF STEAM FROM ORIFICES.

The flow of steam from a vessel of one pressure into that of another pressure becomes greater the greater the difference in pressure between the two vessels, until the lower is 0.58 the absolute pressure of the higher. Any further reduction of the pressure in the second vessel, even down to a vacuum, fails to enhance the flow of the steam between the two. In flowing through the best shaped nozzle the steam expands to the external pressure and also to the volume corresponding to this pressure, so long as it is not less than 58 per cent. of the internal pressure. For an external pressure of 58 per cent. or less, the ratio of expansion becomes constant and is 1.624.

## OUTFLOW OF STEAM INTO THE ATMOSPHERE.

(D. K. CLARK.)

| Initial <br> Pressure. | External Pressure. | Expansion in nozzle. | Velocity of outflow at constant density. | Actual velocity of outflow expanded. | Discharge |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Lbs. per sq. in. absolute. | Lbs. per sq. in. absolute. | Ratio. | Ft. per sec. | $\begin{aligned} & \text { Ft. per } \\ & \text { sec. } \end{aligned}$ | Lbs. per sq. in. per minute. |
| 25.37 | 14.7 | 1.624 | 863 | 1401 | 22.81 |
| 30 | 14.7 | 1.624 | 867 | 1408 | 26.84 |
| 40 | 14.7 | 1.624 | 874 | 1419 | 35.18 |
| 45 | 14.7 | 1.624 | 877 | 1424 | 39.78 |
| 50 | 14.7 | 1.624 | 880 | 1429 | 44.06 |
| 60 | 14.7 | 1.624 | 885 | 1437 | 52.59 |
| 70 | 14.7 | 1.624 | 889 | 1444 | 61.07 |
| 75 | 14.7 | 1.624 | 891 | 1447 | 65.30 |
| 90 | 14.7 | 1.624 | 895 | 1454 | 77.94 |
| 100 | 14.7 | 1.624 | 898 | 1459 | 86.34 |
| 115 | 14.7 | 1.624 | 902 | 1466 | 98.76 |
| 135 | 14.7 | 1.624 | 906 | 1472 | 115.61 |
| 155 | 14.7 | 1.624 | 910 | 1478 | 132.21 |
| 165 | 14.7 | 1.624 | 912 | 1481 | 140.46 |
| 215 | 14.7 | 1.624 | 919 | 1493 | 181.58 |

The weight of steam discharged from a cylindrical nozzle or a short pipe may be approximately found, when the pressure of the atmosphere receiving the steam is less than 58 per cent. of the initial pressure, by the following formula (Napier's Rule): $W=a p \div 70$; in which $W=$ flow in pounds per second, $a=$ area of orifice in square inches; and $p=$ absolute initial pressure per square inch of the steam.

For a circular opening in a thin plate multiply the discharge as obtained from the above formula by 0.65 .

## FLOW OF STEAM IN PIPES.

(KENT'S POCKET BOOK).
A formula commonly used for velocity of flow of steam in pipes is the same as Downing's for the flow of water in smooth cast iron pipes, viz.:

$$
\mathrm{V}=50 \sqrt{\frac{\mathrm{H}}{\mathrm{~L}} \mathrm{D}}
$$

in which $V=$ velocity in feet per second, $L=$ length, and $D=$ diameter of pipe in feet, $H=$ height in feet of a column of steam, of the pressure of the steam at the entrance, which would produce a pressure equal to the difference of pressures at the two ends of the pipe. (For derivation of the coefficient 50 , see Briggs on "Warming Buildings by Steam," Proc. Inst. C. E., 1882.)

If $Q=$ quantity in cubic ft. per minute, $d=$ diameter in inches, $L$ and $H$ being in feet, the formula reduces to

$$
Q=4.723 \sqrt{\frac{\mathrm{H}}{\mathrm{~L}} \mathrm{~d}^{\mathrm{s}}} \quad \mathrm{H}=0.448 \frac{\mathrm{Q}^{2} \mathrm{~L}}{\mathrm{~d}^{5}}, \quad \mathrm{~d}=0.537 \sqrt[5]{\frac{\mathrm{Q}^{2} \mathrm{~L}}{\mathrm{H}}} .
$$

If $p_{1}=$ pressure in pounds per sq. in. of the steam at the entrance to the pipe, $p^{2}=$ the pressure at the exit, then $144\left(p_{1}-p_{2}\right)=$ difference in pressure per sq. ft. Let $w=$ density or weight per cu. ft . of steam at the pressure $p_{1}$, then the height of column equivalent to the difference in pressures is

$$
H=\frac{144\left(p_{1}-p_{2}\right)}{w} \text { and } Q=60 \times 0.7854 \times 50 D^{2} \sqrt{\frac{144\left(p_{1}-p_{2}\right) D}{w L}}
$$

If $W=$ weight of steam flowing in pounds per minute $=Q w$ and $d$ is taken in inches, $L$ being in feet:

$$
\begin{aligned}
& W=56.68 \sqrt{\frac{w\left(p_{1}-p_{2}\right) d^{5}}{L}} ; Q=56.68 \sqrt{\frac{\left(p_{1}-p_{2}\right) d^{s}}{L W}} ; \\
& \quad d=0.199 \sqrt[5]{\frac{W^{2} L}{w\left(p_{1}-p_{2}\right)}}=0.199 \sqrt[5]{\frac{Q^{2} w L}{p_{1}-p_{2}}} . \\
& \text { Velocity } \frac{\text { in feet per minute }=V=Q \div 0.7854 \frac{d^{2}}{144}}{=10390 \sqrt{\frac{\left.p_{1}-p_{2}\right) d}{w L}}}
\end{aligned}
$$

For a velocity of 6000 feet per minute, $d=\frac{w L}{3\left(p_{1}-p_{2}\right)}$; $\mathrm{p}_{1}-\mathrm{p}_{2}=\frac{\mathrm{w} \text { L }}{3 \mathrm{~d}}$.

For a velocity of 6000 feet per minute, a steam pressure of 100 pounds gauge, or $W=0.264$, and a length of 100 feet.

$$
\mathrm{d}=\frac{8.8}{\mathrm{p}_{1}-\mathrm{p}_{2}} ; \quad \mathrm{p}_{1}-\mathrm{p}_{2}=\frac{8.8}{\mathrm{~d}}
$$

That is, a pipe 1 inch diameter, 100 feet long, carrying steam of 100 pounds gauge pressure at 6000 feet velocity per minute, would have a loss of pressure of 8.8 pounds per sq. inch, while steam traveling at the same velocity in a pipe 8.8 inches diameter would lose only 1 pound pressure.
G. H. Babcock in "Steam," gives the formula

$$
W=87 \sqrt{\frac{w\left(p_{1}-p_{2}\right) d^{\delta}}{L\left(1+\frac{3.6}{d}\right)}}
$$

One of the most widely accepted formulae for flow of water is D'Arcy's, which is

$$
V=c \sqrt{\frac{H D}{L 4}}
$$

Using D'Arcy's coefficients, and modifying his formula to make it apply to steam, to the form

$$
Q=c \sqrt{\frac{\left(p_{1}-p_{2}\right) d^{5}}{w L}} ; \text { or } W=c \sqrt{\frac{w\left(p_{1}-p_{2}\right) d^{5}}{L}}
$$

we obtain for,
Diam. in. $\begin{array}{lllllllll}1 & 2 & 3 & 4 & 5 & 6 & 7 & 8\end{array}$ $\begin{array}{lllllllll}\text { Value of } c, & 45.3 & 52.7 & 56.1 & 57.8 & 58.4 & 59.5 & 60.1 & 60.7\end{array}$
$\begin{array}{lllllllll}\text { Diam. in. } & 9 & 10 & 12 & 14 & 16 & 18 & 20 & 24\end{array}$ $\begin{array}{lllllllll}\text { Value of } \mathrm{c}, & 61.2 & 61.8 & 62.1 & 62.3 & 62.6 & 62.7 & 62.9 & 63.2\end{array}$

In the absence of direct experiments these coefficients are probably as accurate as any that may be derived from formulae for flow of water.

Loss of pressure in lbs. per sq. in. $=p_{1}-p_{8}=\frac{Q^{2} w L}{c^{2} d^{5}}$.

## RESISTANCE TO FLOW BY BENDS,

## VALVES, ETC.

Mr. Briggs states that in "Warming Buildings by Steam," that the resistance at the entrance to a pipe consists of two parts, namely: the head $\frac{v^{2}}{2 g}$, which is necessary to create the velocity of flow, and the head $0.505 \frac{v^{2}}{2 g}$, which overcomes the resistance to entrance offered by the mouth of the pipe. The total loss of head at entrance then equals the sum of these, or $1.505 \frac{v^{2}}{2 g}$, in which $V=$ velocity of flow of steam in the pipe, in feet per second, and $g=$ acceleration due to gravity, or 32.2 .

The Babcock \& Wilcox Co. state in "Steam" that the resistance at the opening, and that at a globe valve, are each about the same as that caused by an additional length of straight pipe, as computed by the formula,

Additional length of pipe $=\frac{114 \times \text { diameter of pipe }}{1+(3.6 \div \text { diameter })}$, from which has been computed the following table:

| Diameter in inches | 2 | $2 \frac{1}{2}$ | 3 | $3 \frac{1}{2}$ | 4 | 5 | 6 | 7 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Additional length, feet | 7 | 10 | 13 | 16 | 20 | 28 | 36 | 44 |
| Diameter in inches | 8 | 10 | 12 | 15 | 18 | 20 | 22 | 24 |
| Additional length, feet | 53 | 70 | 88 | 115 | 143 | 162 | 181 | 200 |

The resistance to flow at a right-angled elbow is about equal to $2 / 3$ that of a globe valve.

The above values are to be considered as being only approximations to the truth.

Example.-Find the discharge from a steam pipe when the given length $=120$ feet and the diameter $=8$ inches; the pipe containing 6 right-angled elbows and two globe valves, the pressure at the two ends being respectively 105 and 103 lbs. per sq. in. gauge.

The resistance to entrance, from the above table, for 8 inch pipe $=53$ feet; the resistance of 6 elbows $=6 \times 53 \times 2 / 3$ $=212$ feet; the resistance of two globe valves $=2 \times 53=$ 106 feet; making a total resistance $=53+212+106=371$ feet of additional length of pipe. Therefore, the steam would encounter the same resistance flowing through a straight 8 -inch pipe, whose length equals $120+371$, or 491 feet, as it would in flowing through the given pipe with its various resistances.

Then in the formula $W=c \sqrt{\frac{w\left(p_{1}-p_{2}\right) d^{5}}{L}}$,
$L=491$ feet; $p_{1}=105 \mathrm{lbs}$. per sq. in.; $p_{2}=103 \mathrm{lbs}$. per sq. in.; $d=8$ inches; $c$, for an 8 -inch pipe $=60.7$; and $w$, from table of Properties of Saturated Steam, $=0.27$

Substituting in formula we get

$$
\mathrm{W}=60.7 \sqrt{\frac{0.27(105-103) 8^{5}}{491}}=364 .
$$

The pipe, then, under the stated conditions, would discharge approximately 364 pounds of steam per minute, or $21,800 \mathrm{lbs}$. per hour; which, on the basis of 30 lbs . per horse-power hour, would have a capacity of 728 boiler horse-power. Since one pound of steam at 104 lbs . gauge has a volume of $3.7 \mathrm{cu} . \mathrm{ft}$., the pipe would discharge $1,350 \mathrm{cu} . \mathrm{ft}$. per minute, or $81,000 \mathrm{cu} . \mathrm{ft}$. per hour.

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The above table was calculated by the formula $W \propto$ (varies as) $\frac{d^{3}}{d+3.6}$, in which $W=$ weight of fluid delivered in a given time, and $d=$ diameter (internal) in inches. In the upper right hand triangle of the table the figures refer to nominal diameters, while in the lower triangle they refer to actual diameters.

Example.-To find number of standard 2 inch pipes to deliver as much fluid as one standard 7 inch pipe: In the upper triangle look in column headed 7 and opposite 2 in the extreme right hand column, read 29. Twentynine 2-inch pipes will then deliver as much as one 7-inch pipe.

## NON-CONDUCTING COVERINGS FOR S'TEAM PIPES.

A bare pipe carrying steam, and made of iron, steel or other conducting material, loses heat by convection to the surrounding air and by radiation to the surrounding objects, both of which cause a loss of steam by condensation.

This loss is lessened in practice by covering the outer surface of the steam pipe with a material that will offer a greater resistance to the flow of heat than that offered by the material of the pipe.

A good material for this purpose should not suffer serious deterioration from the heat or vibration to which it would be subjected in practice; and in all cases where damage from fire might result, it should never consist of combustible matter. Under the conditions of practice, especially in places where it may become damp, a good pipe covering should consist of materials that will not rapidly deteriorate, and should contain nothing that will seriously corrode the pipe.

Since air does not take up heat by radiation, but receives heat by contact with a hot body only, it would appear that the greater the porosity of a material, that is, the greater the percentage of volume of finely divided
air it contains, the greater will be its non-conducting qualities. This is noticeably the case in the commercial pipe coverings that consist substantially of the same materials, when these materials contain different percentages of still air. In every case the more porous the material, other things being equal, the greater will be its non-conducting properties.

The following table contains averages made up from results obtained by a number of carefully conducted tests, and represent approximately what may be expected when these materials are properly applied as steam-pipe coverings in practice. The table gives the quantity of heat transmitted through covered steampipes, when that transmitted through a naked pipe is taken as 100 , the covering, except where otherwise indicated, being one inch thick.
Kind of Covering.
Relative Amount of Heat Transmitted.
Naked pipe ..... 100
Hair felt, asbestos lined and canvas covered.... 16 to 18Wool felt, " " " "
Two layers of asbestos paper ..... 70 to 80
Four ..... 45 to 55
Asbestos mixed with some plaster of paris. ..... 28 to 34
Magnesia mixed with a little asbestos fiber, can-vas covered18 to 20
Best mineral wool, lined and canvas covered ..... 18 to 20
Pipe painted with black asphaltum. ..... about 105
Pipe painted with white glossy paint ..... 95

For coverings having values less than 25 in the above table, the values for thicknesses of covering of $11 / 2$ and 2 inches (those in the table being for one inch, as noted) may be approximately obtained by multiplying respectively by 0.78 and 0.58 . Thus, a pipe covered with magnesia and canvas covered would transmit an amount, if $11 / 2$ inches thick $=(18$ to 20$) \times 0.78=14$ to 15.5 ; and if 2 inches thick an amount $=(18$ to 20$) \times 0.58=10.5$ to 11.5 , that transmitted by a similar bare pipe being 100 in the same length of time.

## LOSS OF HEAT FROM BARE IRON STEAM PIPES.

Steam pressure $=100 \mathrm{lbs}$. gauge, surrounding air at $62^{\circ} \mathrm{F}$. Steam temperature $=338^{\circ}$ Fahr.

|  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11/2 | 423 | 6 | 1221 | 12 | 2290 | 22 | 3949 |
| 2 | 494 | 7 | 1420 | 14 | 2645 | 24 | 4264 |
| 3 | 692 | 8 | 1580 | 16 | 2961 | 26 | 4617 |
| 4 | 869 | 9 | 1738 | 18 | 3315 | 28 | 4932 |
| 5 | 1067 | 10 | 1935 | 20 | $3632^{\circ}$ | 30 | 5288 |

CONDENSATION OF STEAM IN BARE IRON PIPES.

Steam pressure $=100 \mathrm{lbs}$. gauge, surrounding air at $62^{\circ} \mathrm{F}$. Steam temperature $=338^{\circ}$ Fahr.

|  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 0.48 | 6 | 1.39 | 12 | 2.61 | 22 | 4.51 |
|  | 0.56 | 7 | 1.62 | 14 | 3.02 | 24 | 4.87 |
| 3 | 0.79 | 8 | 1.80 | 16 | 3.38 | 26 | 5.27 |
| 4 | 0.99 | 9 | 1.98 | 18 | 3.78 | 28 | 5.63 |
| 5 | 1.22 | 10 | 2.21 | 20 | 4.15 | 30 | 6.04 |

## CONDENSA'TION OF STEAM IN COVERED <br> IRON PIPES.

Corresponding to a percentage of that in a bare pipe varying from 15 per cent. for a 30 -inch pipe to 19 for a $11 / 2$ inch pipe, which approximates to what may be expected in practice from the application of the best commercial pipe coverings.

Steam pressure $=100 \mathrm{lbs}$. gauge, surrounding air at $62^{\circ} \mathrm{F}$.
Steam temperature $=338^{\circ}$ Fahr.

|  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11/2 | 0.09 | 6 | 0.22 | 12 | 0.40 | 22 | 0.68 |
| 2 | 0.10 | 7 | 0.25 | 14 | 0.46 | 24 | 0.73 |
| 3 | 0.13 | 8 | 0.28 | 16 | 0.51 | 26 | 0.79 |
| 4 | 0.16 | 9 | 0.30 | 18 | 0.57 | 28 | 0.84 |
| 5 | 0.19 | 10 | 0.34 | 20 | 0.63 | 30 | 0.90 |

Example.-Find the saving resulting from covering an 8 -inch steam pipe that is 120 feet long.
Condensation in bare pipe $=1.80 \times 120=216.0 \mathrm{lbs}$. per hr.

$$
\text { " "covered" }=0.28 \times 120=33.6 \text { " " " }
$$

Saving of steam effected by covering $=182.4$ " " " Which on a 10 -hour basis would amount to an annual saving of about 550,000 pounds of steam. Assuming that one lb . of coal evaporates, under actual conditions, 9 lbs . of water, the saving of fuel in this case resulting from the application of a good commercial pipe covering, would amount to about $60,000 \mathrm{lbs}$. of coal, or 30 short tons per annum. At two, three and four dollars per ton for fuel this would amount to an annual saving of $\$ 60.00$, $\$ 90.00$ and $\$ 120.00$ respectively.

Since the steam carrying capacity of a pipe of this size, as ordinarily installed for power purposes, would be about $24,000 \mathrm{lbs}$. of steam per hour, the above saving would represent about $1 / 2$ of one per cent. of its carrying capacity.

Where fuel is inexpensive and the steam pipes are short, the net saving due to covering the pipes is, of course, insignificant; but even in this case, especially in confined situations, the pipes should be ordinarily covered in order to make the temperature of the space near them less unendurable to workmen and others, in warm weather.

## POWER OF ENGINES AND BOILERS.

Work, in the mechanical sense, is the overcoming of resistance through space, and is measured by the amount of the resistance multiplied by the distance through which it is overcome.

The unit of work, in Great Britain and the United States, is the foot-pound, which is an amount of energy equivalent to the lifting of one pound through a height of one foot.

The unit of rate of doing work is a quantity of work equivalent to the doing of 33,000 foot-pounds in one minute, and is called a horse-power. This is a mechanical horse-power, and should not be confused with the boiler horse-power, which is based upon the evaporation of a stated quantity of water under certain stated conditions.

The indicated horse-power of a steam engine is the horse-power developed by the steam in the cylinder and delivered to the piston. In a double acting single cylinder engine, the indicated horse-power $=\frac{\text { plan }}{33,000,}$, in which $p=$ the mean effective pressure in lbs. per sq. in., as obtained from the indicator card, $l=$ length of stroke in feet, $a=$ area of piston in sq. inches and $n=$ number of working strokes per minute. If the engine has more than one cylinder compute the power of each and take
the sum. If great accuracy is desired the area of crosssection of piston rod should be deducted from the piston area for the crank end, and the powers of the two ends computed separately, since the mean effective pressures of the two ends will not ordinarily be found to be exactly the same. For single acting engines substitute for $n$ the number of working strokes only.

Net or brake horse-power of an engine is the horsepower delivered by the engine from its shaft, by belt or otherwise. It may be obtained from the indicated horsepower by multiplying by the mechanical efficiency: For example, an engine indicating 300 H.P., with a mechanical efficiency of 88 per cent., would have a net or brake horse-power $=300 \times 0.88=264$.

The unit of evaporation is the number of B.T.U. necessary to convert one pound of water at $212^{\circ} \mathrm{F}$. into steam of the same temperature, and is therefore equal to 965.7 B.T.U., the latent heat of one pound of steam at atmospheric pressure.

Boiler Horse-power. A Committee of the American Society of Mechanical Engineers recommended the unit of boiler power known as the "Centennial Standard," and this is now generally accepted. They advised that the commercial horse-power be taken as an evaporation of 30 pounds of water per hour from a feed water temperature of $100^{\circ} \mathrm{Fahr}$. into steam at 70 pounds per square inch gauge pressure. This is equivalent to $341 / 2$ units of evaporation, that is, to $341 / 2$ pounds of water evaporated from a feed water temperature of $212^{\circ}$ Fahr. into steam at the same temperature. This "Centennial Standard" unit is equivalent to 33,305 British thermal units per hour.

It was the opinion of this Committee that a boiler rated at any stated power should be capable of developing that power with easy firing, moderate draught, and ordinary fuel, while exhibiting good economy; and, at times, when maximum economy is not the most important object to be attained, at least one-third more than its rated power to meet emergencies.

Example.-A battery of boilers evaporate $20,000 \mathrm{lbs}$. of feed-water per hour, the temperature of feed-water being $40^{\circ} \mathrm{F}$., and the gauge pressure 100 lbs . per sq. in. Find the equivalent evaporation from and at $212^{\circ} \mathrm{F}$.; also the commercial horse-power.

The factor of evaporation, from $40^{\circ} \mathrm{F}$. and at 100 lbs . gauge, is (see table of factors of evaporation) 1.219. Therefore the equivalent evaporation from and at $212^{\circ}=$ $20,000 \times 1.219=24,380 \mathrm{lbs}$. per hr.

Since one commercial horse-power is equivalent to the evaporation of 34.5 lbs . of water per hour, from and at $212^{\circ}$, the commercial horse-power $=24,380 \div 34.5=707$.

In the above example the steam is assumed to be dry and saturated. In case it is not a correction must be made.

1. Assume that the steam contains 2 per cent. of moisture. Of the $20,000 \mathrm{lbs}$. of feed-water, then, 98 per cent. or $19,600 \mathrm{lbs}$. will be evaporater and the remaining 400 lbs. will pass from the boiler as water at the temperature of the steam. Each pound of this water will carry away from the boiler an amount of heat necessary to raise its temperature from $40^{\circ} \mathrm{F}$., the temperature of the feedwater, to $337^{\circ}$, the temperature of the steam, or 296 B.T.U. per 1 lb . of entrained water. Had the entrained water been evaporated each pound would have carried away an additional amount equal to its latent heat at boiler pressure, or 876 B.T.U. per 1b., or $876 \times 400=350,400$ B.T.U. per hour, for the total amount of entrained water. Under the assumed conditions, then, the boiler imparts 350,400 heat units less to the feed-water per hour than would have been the case had there been no entrained water; that is, its capacity is less by $350,400 \div 33,305$ (the heat equivalent of a boiler H.P.) $=10.5$ horse-power. The actual commercial horse power of the boiler then $=707-$ $10.5=696.5$.
2. Assume that the steam is superheated 20 degrees; that is, to a temperature of $337^{\circ}+20^{\circ}=357^{\circ} \mathrm{F}$. Then the additional heat imparted to each pound of feed-water over that necessary to generate dry saturated steam is $20^{\circ} \times 0.48$ (the specific heat of steam) $=9.6$ heat units per 1 lb ., or $9.6 \times 20,000=192,000$ per hr., or $192.000 \div 33,305=$ 5.8 horse-power. The actual horse-power of boiler then $=707+5.8=712.8$.

## Horse-power per Pound Mean Effective Pressure.

Formula, $\frac{\text { Area in sq. in. } \times \text { piston-speed }}{33,000}$.


The indicated horse-power of an engine equals $\frac{\text { plan }}{33,000}=$ $\underline{a \times l n \times p}=\underline{\text { area of piston } \times \text { piston speed }} \times p$, in which $p=$ 33,000 33,000
mean effective pressure in lbs. per sq. in.; $l=$ length of stroke in ft .; $a=$ effective area of piston in sq. in.; and $n=$ number of impulse strokes per minute.

The piston speed for a single acting, double acting or a multiple cylinder engine $=$ the length of stroke in $\mathrm{ft} . \times$ number of impulse strokes per minute.

## FEED-WATER HEA'TERS.-(kent).

Percentage of Saving for Each Degree of Increase in Temperature of Feed-water Heated by Waste Steam.

| Initial <br> Temp. | Pressure of Steam in Boiler, lbs. per sq. in. above Atmosphere. |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0 | 20 | 40 | 60 | 80 | 100 | 120 | 140 | 160 | 180 | 200 |
| $32^{\circ}$ | . 0872 | . 0861 | . 0855 | 0851 | 0847 | . 0844 | 0841 | . 0839 | . 0837 | 0835 | 0833 |
| 40 | . 0878 | . 0867 | . 0861 | . 0856 | 0853 | . 0850 | . 0847 | . 0845 | . 0843 | 0841 | . 0839 |
| 50 | . 0886 | . 0875 | . 0868 | . 0864 | . 0860 | . 0857 | . 0854 | . 0852 | . 0850 | . 0848 | . 0816 |
| 60 | . 0894 | . 0883 | . 0876 | . 0872 | 0867 | . 0864 | . 0862 | . 0859 | . 0856 | 0855 | . 0853 |
| 70 | . 0902 | . 0890 | . 0884 | . 0879 | . 0875 | . 0872 | . 0869 | . 0867 | . 0864 | 0862 | . 0860 |
| 80 | . 0910 | . 0898 | . 0891 | . 0887 | . 0883 | . 0879 | . 0877 | . 0874 | . 0872 | . 0870 | . 0868 |
| 90 | . 0919 | . 0907 | . 0900 | . 0895 | . 0888 | . 0887 | . 0884 | . 0883 | 0879 | 0877 | 0875 |
| 100 | .0927 | . 0915 | . 0908 | . 0903 | . 0899 | . 0895 | . 0892 | . 0890 | . 0887 | 0885 | . 0883 |
| 110 | . 0936 | . 0923 | . 0916 | . 0911 | . 0907 | . 0903 | . 0900 | . 0898 | . 0895 | 0893 | . 0891 |
| 120 | . 0945 | . 0932 | 0925 | . 0919 | . 0915 | . 0911 | . 0908 | . 0906 | 0903 | . 0901 | . 0899 |
| 130 | . 0954 | . 0941 | . 0934 | . 0928 | 0924 | 0920 | . 0917 | . 0914 | . 0912 | . 0909 | . 0907 |
| 140 | . 0963 | . 0950 | . 0943 | . 0937 | . 0932 | . 0929 | .0925 | . 0923 | . 0920 | 0918 | . 0916 |
| 150 | . 0973 | . 0959 | . 0951 | . 0946 | . 0941 | . 0937 | . 0934 | . 0931 | . 0929 | . 0926 | . 0924 |
| 160 | . 0982 | . 0968 | . 0961 | . 0955 | . 0950 | 0946 | . 0943 | . 0940 | . 0937 | . 0935 | 0933 |
| 170 | . 0992 | . 0978 | . 0970 | . 0964 | . 0959 | . 0955 | . 0952 | . 0949 | . 0946 | . 0944 | . 0941 |
| 180 | . 1002 | . 0988 | . 0981 | . 0973 | . 0969 | . 0965 | . 0961 | . 0958 | . 0955 | . 0953 | . 0951 |
| 190 | . 1012 | . 0998 | . 0989 | . 0983 | . 0978 | . 0974 | . 0971 | . 0968 | . 0964 | . 0962 | . 0960 |
| 200 | . 1022 | . 1008 | . 0999 | . 0993 | . 0988 | . 0984 | . 0980 | . 0977 | . 0974 | . 0972 | . 0969 |
| 210 | . 1033 | . 1018 | . 1009 | . 1003 | . 0998 | . 0994 | . 0990 | . 0987 | . 0984 | . 0981 | . 0979 |
| 220 |  | . 1029 | . 1019 | . 1013 | . 1008 | . 1004 | . 1000 | . 0997 | . 0994 | 0991 | . 0989 |
| 230 |  | . 1039 | . 1031 | 1024 | . 1018 | . 1012 | . 1010 | . 1007 | . 1003 | 1001 | . 0999 |
| 240 |  | . 1050 | 1041 | 1034 | . 1029 | . 1024 | . 1020 | . 1017 | . 1014 | 1011 | . 1009 |
| 25 |  | . 106 | 10 | 10 | 1040 | . 1035 | 10 | 102 | 10 | 10 | . 1019 |

An approximate rule for the conditions of ordinary practice is: A saving of $1 \%$ is made by each increase of $11^{\circ}$ in the temperature of the feed-water. This corresponds to 0.0909 per cent. for each degree.

The calculation of saving is made as follows: Let total heat of 1 lb . of steam at the boiler-pressure $=H$; tơtal heat of 1 lb . of feed-water before entering the heater $=h_{1}$, and after passing through the heater $=h_{2}$; then the saving made by the heater is $\frac{h_{2}-h_{1}}{H-h_{1}}$.

Example.-Given boiler pressure $=100 \mathrm{lbs}$. gauge; feed water temperature, original $=60^{\circ} \mathrm{F}$. and final $=209^{\circ} \mathrm{F}$.; to find the percentage of saving resulting from heating the feed-water. From the table of properties of saturated steam we find $H=1185$ B.T.U.; $h_{1}=60-32=28$ B.T.U.; $h_{2}=209-32=177$ В.Т.U.
Then the saving by heater $=\frac{h_{2}-h_{1}}{H-h .}=\frac{177-28}{1185-28}=12.9$ per cent.

To solve by table look in column of steam pressures headed " 100 " and opposite to $60^{\circ}$ in first column read 0.0864 , which multiplied by $(209-60=149)$ the increase of temperature of feed-water, gives 12.9 per cent., as before.

Safe Working Pressures in Cylindrical Shells of Boilers, Tanks, Pipes, etc., in Pounds per Square Inch.
(KENTS POCKET BOOK).
Longitudinal seams double-riveted.
(Calculated from formula $P=14000 \times$ thickness $\div$ diameter.)

|  | DIAMETER IN INCHES. |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 24 | 30 | 36 | 38 | 40 | 42 | 44 | 46 | 48 | 50 | 52 |
| 1 | 36.5 | 29.2 | 24.3 | 23.0 | 21.9 | 20.8 | $\overline{19.9}$ | 19.0 | 18.2 | 17.5 | 16.8 |
| 2 | 72.9 | 58.3 | 48.6 | 46.1 | 43.8 | 41.7 | 39.8 | 38.0 | 36.5 | 35.0 | 33.7 |
| 3 | 109.4 | 87.5 | 72.9 | 69.1 | 65.6 | 62.5 | 59.7 | 57.1 | 54.7 | 52.5 | 50.5 |
| 4 | 145.8 | 116.7 | 97.2 | 92.1 | 87.5 | 83.3 | 79.5 | 76.1 | 72.9 | 70.0 | 67.3 |
| 5 | 182.3 | 145.8 | 121.5 | 115.1 | 109.4 | 104.2 | 99.4 | 95.1 | 91.1 | 87.5 | 84.1 |
| 6 | 218.7 | 175.0 | 145.8 | 138.2 | 131.3 | 125.01 | 119.3 | 114.1 | 109.41 | 105.0 | 101.0 |
| 7 | 255.2 | 204.1 | 170.1 | 161.2 | 153.1 | 145.91 | 139.2 | 133.2 | 127.6 | 122.5 | 117.8 |
| 8 | 291.7 | 233.3 | 194.4 | 184.2 | 175.0 | 166.71 | 159.1 | 152.2 | 145.81 | 140.0 | 134.6 |
| 0 | 328.1 | 262.5 | 218.8 | 207.2 | 196.9 | 187.5 | 179.0 | 171.2 | 164.1 | 157.5 | 151.4 |
| 10 | 364.6 | 291.7 | 243.1 | 230.3 | 218.8 | 208.3 | 198.9 | 190.2 | 182.3 | 175.0 | 168.3 |
| 11 | 401.0 | 320.8 | 267.4 | 253.3 | 240.6 | 229.2 | 218.7 | 209.2 | 200.5 | 192.5 | 185.1 |
| 12 | 437.5 | 350.0 | 291.7 | 276.3 | 262.5 | 250.0 | 238.6 | 228.3 | 218.7 | 210.0 | 201.9 |
| 13 | 473.9 | 379.2 | 316.0 | 299.3 | 284.4 | 270.9 | 258.5 | 247.3 | 237.0 | 227.5 | 218.8 |
| 14 | 410.4 | 408.3 | 340.3 | 322.4 | 306.3 | 291.7 | 278.4 | 266.3 | 255.2 | 245.0 | 235.6 |
| 15 | 546.9 | 437.5 | 364.6 | 345.4 | 328.1 | 312.5 | 298.3 | 285.3 | 273.4 | 266.5 | 252.4 |
| 16 | 583. |  |  |  | 350 |  | 318.2 | 304.4 |  | 280.0 | 269 |
|  | DIAMETER IN INCHES. |  |  |  |  |  |  |  |  |  |  |
|  | 54 | 60 | 66 | 72 | 78 | 84 | 90 | 96 | 102 | 108 | 120 |
| 1 | 16.2 | 14.6 | 13.3 | 12.2 | 11.2 | 10.4 | 9.7 | 9.1 | 8.6 | 8.1 | 7.3 |
| ${ }_{3}$ | 32.4 | 29.2 | 26.5 | 24.3 | 22.4 | 20.8 | 19.4 | 18.2 | 17. 2 | 16.2 | 14.6 |
| 3 | 48.6 | 43.7 | 39.8 | 36.5 | 33.7 | 31.3 | 29.2 | 27.8 | 25.7 | 24.3 | 21.9 |
| 4 | 64.8 | 58.3 | 53.0 | 48.6 | 44.9 | 41.7 | 38.9 | 36.5 | 34.3 | 32.4 | 29.2 |
| 5 | 81.0 | 72.9 | 66.3 | 60.8 | 56.1 | 52.15 | 48.6 | 45.6 | 42.9 | 40.5 | 36.5 |
| 6 | 97.2 | 87.5 | 79.5 | 72.9 | 67.3 | 62.5 | 58.3 | 54.7 | 51.5 | 48.6 | 43.8 |
| 8 | 113.4 | 102.1 | 92,8 | 85.1 | 78.5 | 72.9 | 68.1 | 63.8 | 60.0 | 56.7 | 51.0 58.3 |
| 8 | 129.6 | 116.7 | 106.1 | 97.2 109.4 | 89.7 | 83.3 93.8 | 77.8 | 72.9 | 68.6 77.2 | 64.8 72.9 | 58.3 65.6 |
| 10 | 162.0 | 145.8 | 132.6 | 121.5 | 112.2 | 104.2 | 87.2 | 81.1 | 85.8 | 81.0 | 72.9 |
| 11 | 178.2 | 160.4 | 145.8 | 133.7 | 123.4 | 114.6 | 106.9 | 100.3 | 94.4 | 89.1 | 80.2 |
| 12 | 194.4 | 175.0 | 159.1 | 145.8 | 134.6 | 125.0 | 116.7 | 109.4 | 4102.9 | 97.2 | 87.5 |
| 13 | 210.7 | 189.6 | 172.4 | 158.0 | 145.8 | 135.4 | 126.4 | 118.5 | 111.5 | 105.3 | 94.8 |
| 14 | 228.9 | 204.2 | 185.6 | 170.1 | 157.1 | 1145.8 | 136.1 | 127.6 | 120.1 | 113.4 | 102.1 |
| 15 | 243.1 | 218.7 | 198.9 | 182.3 | 168.3 | 3156.3 | 145.8 | 136.7 | 7128.7 | 121.5 | 109.4 |
| 16 | 1259.3 | 233.3 | 3212.1 | 194.4 | 1179.5 | 5166.7 | 155.6 | 145.8 | 8137.3 | 3129.6 | 6116.7 |

The preceding table has been computed for externallyfired boilers, with longitudinal seams double-riveted and having an efficiency of 0.7 . A factor of safety of 5.5 has been assumed for steel of $55,000 \mathrm{lbs}$. tensile strength.

## SIZES OF CHIMNEYS FOR STEAM BOILERS.

by william kent, m. e.

The accompanying tabe of sizes of chimneys for various horse powers of boilers is based on the following data:

1. The draught power of the chimney varies as the square root of the height.
2. The retarding of the ascending gases by friction may be considered as equivalent to a diminution of the area of the chimney, or to a lining of the chimney by a layer of gas which has no velocity. The thickness of this lining is assumed to be two inches for all chimneys, or the diminution of area equal to the perimeter $\times$ two inches (neglecting the overlapping of the corners of the lining). Expressed algebraically, let $D=$ diameter, $A=$ area, $E=$ effective area.

For square chimneys, $E=D^{2}-\frac{8 D}{12}=A-\frac{2 \sqrt{A}}{3}$. For round chimneys, $E=\pi\left(D^{2}-\frac{8 D}{12}\right)=A-0.592 \sqrt{ } \bar{A}$.

For simplifying calculations, the coefficient of $\sqrt{A}$ may be taken as 0.6 for both square and round chimneys, and the formula becomes

$$
E=A-0.6 \sqrt{A}
$$

3. The power varies directly as this effective area $E$.
4. A chimney 80 feet high, 42 inches diameter, has been found to be sufficient to cause a rate of combustion
of 120 pounds of coal per hour per square foot of area of chimney, or if the grate area is to the chimney area as 8 to 1 , a combustion of 15 pounds of coal per square foot of grate per hour. This is fair practice for a boiler of modern type, in which flues, or tubes are of moderate diameter, gas passages circuitous, and heating surface extensive in proportion to rate of combustion, so as to cool the chimney gases to $400^{\circ}$ or $500^{\circ} \mathrm{Fahr}$. and produce high economy.
5. A chimney should be proportioned so as to be capable of giving sufficient draught to cause the boiler to develop much more than its rated power, in case of emergencies, or to cause the combustion of 5 pounds of fuel per rated horse-power of boiler per hour.

Conditions 4 and 5 being assumed, the 80 feet $\times 42$ inches chimney, 9.62 square feet area, will cause the combustion of $9.62 \times 120=1154.4$ pounds of coal per hour, or at 5 pounds of coal per horse-power per hour, is rightly proportioned for 231 horse-power of boilers.
The power of the chimney varying directly as the effective area, $E$, and as the square root of the height, $h$, the formula for horse-power of boiler for a given size of chimney will take the form,-

HP. $=C E \sqrt{h}$, in which $C$ is a constant.
For the $80^{\prime} \times 42^{\prime \prime}$ chimney,

$$
\begin{aligned}
E=A-0.6 \sqrt{A} & =7.76 \text { square feet. } \\
\sqrt{h} & =8.944 \text { feet. }
\end{aligned}
$$

Substituting these values in the formula it becomes -

$$
\begin{aligned}
& 231=C \times 7.76 \times 8.944 \text {, } \\
& \text { whence } C=3.33 \text {, }
\end{aligned}
$$

and the formula for horse-power is
HP. $=3.33 E \sqrt{h}$, or, HP. $=3.33(A-0.6 \sqrt{A}) \sqrt{h .}$
If the horse-power of boiler is given, to find the size of chimney, the height being assumed,

$$
E=\frac{0.3 \mathrm{HP}}{\sqrt{h}} .
$$

For round chimneys, diameter of chimney $=$ Diam. of $E+4^{\prime \prime}$.
For square chimneys, side of chimney $=\sqrt{E+4^{\prime \prime}}$.
In the formulae and table no account has been taken of the difference which is believed by some authorities to exist in the efficiencies of round and square chimneys of equal area, nor of the differences of friction and of rate of cooling of the gases in iron and in brick chimneys. Should experimental data of these differences, or of the effect of infiltration of air into brick chimneys, be obtained in future, the formulae and table may be corrected accordingly.



AIR.

## AIR.

Air consists of a mechanical mixture of the two gases oxygen and nitrogen in the ratio of 20.7 parts of the former to 79.3 of the latter by volume, and 23 of the former to 77 of the latter by weight. In its natural state it contains small quantities of various substances, such as moisture, carbon dioxide, $\mathrm{CO}_{2}$, the lately discovered element argon, etc.

The weight of dry air at $32^{\circ} \mathrm{F}$. and atmospheric pressure ( 14.7 lbs . per sq. in.) is 0.0807 lbs . per cu. ft.; from which the volume of one pound $=12.4 \mathrm{cu} . \mathrm{ft}$. At other temperatures and pressures its weight in lbs. per cu. ft . is $W=\frac{1.325 \times B}{459 . 亡+\mathrm{t}}$, in which $B=$ reading of barometer in inches and $t=$ temperature F .

The absolute zero of temperature, on the Fahr. scale is $492^{\circ}$ below $32^{\circ}$, or $-460^{\circ} \mathrm{F}$.

The absolute temperature then is obtained by adding $460^{\circ}$ to the temperature as read from the Fahr. scale. Thus $60^{\circ} \mathrm{F} .=60^{\circ}+460^{\circ}=520^{\circ}$ absolute; and $-20^{\circ} \mathrm{F} .=$ $-20^{\circ}+460^{\circ}=440^{\circ}$ absolute.
Mechanical equivalent of heat.-Heat energy and mechanical energy are mutually convertible, that is, a unit of heat requires for its production, and produces by its disappearance, a definite amount of mechanical energy, namely, 778 foot-pounds of work for each British thermal unit.

Boyle's law states that the product of the pressure and volume of a portion of gas is constant so long as the temperature is constant, that is, $p v=c$, in which $p=$ pressure in lbs. per sq. ft. and $v=$ volume in $\mathrm{cu} . \mathrm{ft}$. For air at $32^{\circ} \mathrm{F}$, , this constant quantity is 26,200 foot-pounds, or $p v=26,200 \mathrm{ft} .1 \mathrm{bs}$.

Charles' and Gay Lussac's law states that when the pressure is constant all gases expand alike for the same increase of temperature. The amount of this expansion
between $32^{\circ}$ and $212^{\circ} \mathrm{F}$, is 0.365 of the original volume: and for each degree it equals $0.365 \div 180=0.00203$. Similiarly, when the volume remains constant the pressure varies in the above ratio.

Combining Boyle's and Charles' laws we see that the product of the pressure and volume of a portion of gas is proportional to the absolute temperature. Thus, $\frac{p v}{p_{1} v_{1}}=$ $\frac{T}{T_{1}}$, in which $p$ and $p_{1}=$ absolute pressures (that is pressures above a vacuum) in 1 bs . per sq. ft .; $v$ and $v_{1}=$ volumes in cu. ft.; $T$ and $T_{1}=$ absolute temperatures.

Transforming the above equation and substituting 32 for $T_{1}$ and 26,200 for $p_{1} v_{1}$, we get

$$
p v=\frac{p_{1} v_{1}}{T_{1} \cdot} T=53.2 T
$$

The specific heat of a gas is the quantity of heat, in heat units, necessary to raise the temperature of one pound of the gas through one degree of temperature.

The specific heat of air at constant pressure is $c_{p}=0.238$ and at constant volume is $\dot{c}_{\mathrm{v}}=0.169$ British thermal unit.

Adiabatic expansion or compression of a gas means that the gas is expanded or compressed without transmission of heat to or from the gas. This would be the case were the expansion or compression to take place in an absolutely non-conducting cylinder, in which case the temperature, pressure and volume would vary as indicated by the following formulae.

$$
\begin{array}{lll}
\frac{\mathrm{v}_{2}}{\mathrm{v}_{1}}=\left(\frac{\mathrm{p}_{1}}{\mathrm{p}_{2}}\right)^{0.71}: & \frac{\mathrm{p}_{2}}{\mathrm{p}_{1}}=\left(\frac{\mathrm{v}_{2}}{\mathrm{v}_{2}}\right)^{1.41}: & \frac{\mathrm{T}_{2}}{\mathrm{~T}_{1}}=\left(\frac{\mathrm{v}_{1}}{\mathrm{v}_{2}}\right)^{0.41}: \\
\frac{\mathrm{v}_{2}}{\mathrm{v}_{1}}=\left(\frac{\mathrm{T}_{1}}{\mathrm{~T}_{2}}\right)^{2.46}: & \frac{\mathrm{p}_{2}}{\mathrm{p}_{1}}=\left(\frac{\mathrm{T}_{2}}{\mathrm{~T}_{1}}\right)^{3.46}: & \frac{\mathrm{T}_{2}}{\mathrm{~T}_{1}}=\left(\frac{\mathrm{p}_{2}}{\mathrm{p}_{1}}\right)^{0.29}:
\end{array}
$$

in which $p_{1}, v_{1}$ and $T_{1}=$ initial absolute pressure, volume and absolute temperature and $\mathrm{p}_{2}, \mathrm{v}_{2}$ and $\mathrm{T}_{2}=$ final absolute pressure, volume and absolute temperature of the gas.

Table for Adiabitic Compression or Expansion of Air. (Proc., Inst. M. E., Jan. 1881, p. 123.)

| Absolute Pressure. |  | Absolute Temperature. |  | Volume. |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\frac{\mathrm{P}_{2}}{\mathrm{P}_{1}}$ | $\frac{\mathrm{P}_{1}}{\mathrm{P}_{\mathrm{a}}}$ | $\frac{\mathrm{T}_{2}}{\mathrm{~T}_{1}}$ | $\frac{T_{1}}{T_{2}}$ | $\frac{V_{1}}{V_{2}}$ | $\frac{\mathrm{V}_{2}}{\mathrm{~V}_{1}}$ |
| 1.2 | 8.33 | 1.054 | . 948 | 1.138 | 8.79 |
| 1.4 | 7.14 | 1.102 | . 907 | 1.270 | . 788 |
| 1.6 | . 625 | 1.146 | . 873 | 1.396 | . 716 |
| 1.8 | . 556 | 1.186 | . 843 | 1.518 | . 659 |
| 2.0 | . 500 | 1.222 | . 818 | 1.636 | . 611 |
| 2.2 | . 454 | 1.257 | . 796 | 1.750 | . 571 |
| 2.4 | . 417 | 1.289 | . 776 | 1.862 | . 537 |
| 2.6 | . 385 | 1.319 | . 758 | 1.971 | . 507 |
| 2.8 | . 357 | 1.348 | . 742 | 2.077 | . 481 |
| 3.0 | . 333 | 1.375 | . 727 | 2.182 | . 458 |
| 3.2 | . 312 | 1.401 | . 714 | 2.284 | . 438 |
| 3.4 | . 294 | 1.426 | . 701 | 2.384 | . 419 |
| 3.6 | . 278 | 1.450 | . 690 | 2.483 | . 403 |
| 3.8 | . 263 | 1.473 | . 679 | 2.580 | . 388 |
| 4.0 | . 250 | 1.495 | . 669 | 2.676 | . 374 |
| 4.2 | . 238 | 1.516 | . 660 | 2.770 | . 361 |
| 4.4 | . 227 | 1.537 | . 651 | 2.863 | . 349 |
| 4.6 | . 217 | 1.557 | . 642 | 2.955 | . 338 |
| 4.8 | . 208 | 1.576 | . 635 | 3.046 | . 328 |
| 5.0 | . 200 | 1.595 | . $62 \%$ | 3.135 | . 319 |
| 6.0 | . 167 | 1.681 | . 595 | 3.569 | . 280 |
| 7.0 | . 143 | 1.758 | . 569 | 3.981 | . 251 |
| 8.0 | . 125 | 1.828 | . 547 | 4.377 | . 228 |
| 9.0 | . 111 | 1.891 | . 529 | 4.759 | . 210 |
| 10.0 | . 100 | 1.950 | . 513 | 5.129 | . 195 |

Work of adiabatic compression of air.-If air is compressed from a volume $v_{1}$ and pressure $p_{1}$ to a volume $v_{2}$ and pressure $p_{2}$, in a non-conducting cylinder without clearance, the work involved in delivering one pound is as follows:

Work of compression $=2.46 \mathrm{p}_{1} \mathrm{v}_{1}\left[\left(\frac{\mathrm{v}_{\mathrm{i}}}{\mathrm{v}_{\mathbf{2}}}\right)^{0.41}-1\right]=$ $2.46 p_{1} v_{1}\left[\left(\frac{p_{2}}{p_{2}}\right)^{0.29}-1\right]$.

Work of expulsion $=p_{2} v_{3}=p_{1} v_{1}\left(\frac{p_{2}}{p_{2}}\right)^{0.29}$
Total work is the sum of the work of compression and expulsion less the work, $p_{1} v_{1}$, of the atmosphere done on the piston during admission, or

Total work $=3.46 \mathrm{p}_{1} \mathrm{v}_{1}\left[\left(\frac{\mathrm{p}_{2}}{\mathrm{p}_{1}}\right)^{0.29}-1\right]$.
The mean effective pressure equals the total work $\div$ the initial volume, $\mathrm{v}_{1}$, or

$$
3.46 \mathrm{p}_{1}\left[\left(\frac{\mathrm{p}_{3}}{\mathrm{p}_{1}}\right)^{0.29}-1\right]
$$

Isothermal expansion or compression of a gas means that the gas is expanded or compressed with the addition or rejection of sufficient heat to maintain the temperature constant. In this case, the temperature being constant, the pressure and volume will vary according to Boyle's law, namely

$$
p v=C
$$

in which $p=$ absolute pressure in lbs. per sq. ft., $v=$ volume in cu. ft., and $C=a$ constant depending upon the temperature. For a temperature of $32^{\circ} \mathrm{F}$. this constant is $26,200 \mathrm{ft} .1 \mathrm{bs}$., and for isothermals corresponding to other temperatures it may be found from the formula $C=53.2 T$, in which $T=$ the absolute temperature of the isothermal.

Work of isothermal compression of air.-If air is compressed from a volume $v_{1}$ and pressure $p_{1}$ to a volume $v_{2}$ and pressure $p_{2}$, in a cylinder without clearance, in such manner as to keep the temperature constant, the work involved in delivering one pound is as follows:

Work of compression $=p_{1} v_{1} \log _{e} \frac{\mathrm{v}_{1}}{\mathrm{v}_{2}}$.
Work of expulsion $=p_{2} \mathrm{v}_{2}=\mathrm{p}_{1} \mathrm{v}_{\mathrm{i}}$.
The total work then is the sum of the work of compression and expulsion less the work, $\mathrm{p}_{1} \mathrm{v}_{1}$, of the atmosphere done on the piston during admission, or

Total work $=p_{1} v_{1} \log _{e} \frac{v_{1}}{v_{3}}+p_{1} v_{1}-p_{1} v_{1}=p_{1} v_{1}$ $\log e \frac{V_{2}}{V_{2}}$.

In this formula Naperian, or hyperbolic, logarithms must be used. These may be obtained from the common logarithms by multiplying by the constant 2.303 .

The mean effective pressure equals the total work $\div$ the initial volume, $v_{1}$, or $p_{1} \log _{e} \frac{v_{1}}{v_{2}}$.

Volumes Mean Pressures per Stroke, 'Temperatures, etc., in the Operation of Air-compression from from 1 Atmosphere and $60^{\circ}$ Fahr. (F. Richards, Am. Mach., March 30, 1893.)

|  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| 0 | 1 | 1 | 1 | 0 | 0 | $60^{\circ}$ |
| 1 | 1.068 | . 9363 | . 950 | . 96 | . 97 | 71 |
| 2 | 1.136 | . 8803 | . 910 | 1.87 | 1.91 | 80 |
| 3 | 1.204 | . 8305 | . 876 | 2.72 | 2.80 | 89 |
| 4 | 1.272 | . 7861 | . 840 | 3.53 | 3.67 | 98 |
| 5 | 1.340 | . 7462 | . 810 | 4.30 | 4.50 | 106 |
| 10 | 1.680 | . 5952 | . 690 | 7.62 | 8.27 | 145 |
| 15 | 2.020 | . 4950 | . 606 | 10.33 | 11.51 | 178 |
| 20 | 2.360 | . 4237 | . 543 | 12.62 | 14.40 | 207 |
| 25 | 2.700 | . 3703 | . 494 | 14.59 | 17.01 | 234 |
| 30 | 3.040 | . 3289 | . 453 | 16.34 | 19.40 | 252 |
| 35 | 3.381 | . 2957 | . 420 | 17.92 | 21.60 | 281 |
| 40 | 3.721 | . 2687 | . 393 | 19.32 | 23.66 | 302 |
| 45 | 4.061 | . 2462 | . 370 | 20.57 | 25.59 | 321 |
| 50 | 4.401 | . 2272 | . 350 | 21.69 | 27.39 | 339 |
| 55 | 4.741 | . 2109 | . 331 | 22.76 | 29.11 | 357 |
| 60 | 5.081 | . 1968 | . 314 | 23.78 | 30.75 | 375 |
| 65 | 5.423 | . 1844 | . 301 | 24.75 | 32.32 | 389 |
| 70 | 5.762 | . 1735 | . 288 | 25.67 | 33.83 | 405 |
| 75 | 6.102 | . 1639 | . 276 | 26.55 | 35.27 | 420 |

Volumes, Mean Pressures per Stroke, Temperatures, etc. (CONTINUED.)

|  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| 80 | 6.412 | . 1552 | . 2670 | 27.38 | 36.64 | $432^{\circ}$ |
| 85 | 6.782 | . 1474 | . 2566 | 28.16 | 37.94 | 447 |
| 90 | 7.122 | . 1404 | . 2480 | 28.89 | 39.18 | 459 |
| 95 | 7.462 | . 1340 | . 2400 | 29.57 | 40.40 | 472 |
| 100 | 7.802 | . 1281 | . 2324 | 30.21 | 41.60 | 485 |
| 105 | 8.142 | . 1228 | . 2254 | 30.81 | 42.78 | 496 |
| 110 | 8.483 | . 1178 | . 2189 | 31.39 | 43.91 | 507 |
| 115 | 8.823 | . 1133 | . 2129 | 31.98 | 44.98 | 518 |
| 120 | 9.163 | . 1091 | . 2073 | 32.54 | 46.04 | 529 |
| 125 | 9.503 | . 1052 | . 2020 | 33.07 | 47.06 | 540 |
| 130 | 9.843 | . 1015 | . 1969 | 33.57 | 48.10 | 550 |
| 135 | 10.183 | . 0981 | . 1922 | 34.05 | 49.10 | 560 |
| 140 | 10.523 | . 0950 | . 1878 | 34.57 | 50.02 | 570 |
| 145 | 10.864 | . 0921 | . 1837 | 35.09 | 51.00 | 580 |
| 150 | 11.204 | . 0892 | . 1796 | 35.48 | 51.89 | 589 |
| 160 | 11.880 | . 0841 | . 1722 | 36.29 | 53.65 | 607 |
| 170 | 12.560 | . 0796 | .165'\% | 37.20 | 55.39 | 624 |
| 180 | 13.240 | . 0755 | . 1595 | 37.96 | 57.01 | 640 |
| 190 | 13.920 | . 0718 | . 1540 | 38.68 | 58.57 | 657 |
| 200 | 14.600 | . 0685 | . 1490 | 39.42 | 60.14 | 672 |

Combined compression of air, is compression under conditions that permit of some withdrawal of heat during compression, but not sufficient to keep the temperature of the air constant. In this case the compression curve lies between the isothermal and adiabatic curves, and the relation of pressure to volume may be expressed by the formula

$$
p v^{n}=C
$$

in which $p=$ absolute pressure in lbs, per sq. ft.; $v=$ volume in cu . ft.; $C=$ a constant; and $n=$ an exponent whose value may vary from 1 , that for isothermal, to 1.41, that for adiabatic compression or expansion.

Work of combined compression.-If air is compressed from a volume $v_{1}$ and pressure $p_{1}$ to a volume $v_{2}$ and pressure $p_{2}$, in a cylinder without clearance, the work involved in delivering one pound is as follows:

$$
\begin{aligned}
& \text { Work of compression }=\left(p_{2} v_{2}-p_{1} v_{1}\right) \frac{v_{2}}{v_{1}-v_{2}}= \\
& 53.2\left(T_{2}-T_{1}\right) \frac{v_{2}}{v_{1}-v_{3}}
\end{aligned}
$$

Work of expulsion $=\mathrm{p}_{2} \mathrm{v}_{\mathbf{2}}$.
The total work is the sum of the work of compression and expulsion less the work, $\mathrm{p}_{1} \mathrm{v}_{1}$, done by the atmosphere on the piston during admission, or

$$
\begin{aligned}
\text { Total work } & =\left(p_{2} v_{2}-p_{1} v_{1}\right) \frac{v_{2}}{v_{1}-v_{2}}+p_{2} v_{2}-p_{1} v_{1} \\
& =\left(p_{2} v_{2}-p_{1} v_{1}\right) \frac{v_{1}}{v_{1}-v_{2}}
\end{aligned}
$$



The results of air compression and expansion are shown by the above diagram.

## Useful information on Volume and Pressure Curves of Air.

## (FROM COMPRESSED AIR MAGAZINE.)

In the diagram on the preceding page, the figures at the left indicate pressures in atmospheres above a vacuum ; the corresponding figures at the right denote pressures in pounds per square inch, by the gauge. At the top are volumes from one-tenth to one. At the bottom, degrees of temperatures from zero to 1,000 degrees Fahrenheit. The two curves which begin at the lower left hand corner and extend to the upper right are the lines of compression, or expansion. The upper one being the "Adiabatic" curve, or that which represents the pressure at any point on the stroke, with the heat developed by compression remaining in the air; the lower is the "Isothermal," or the pressure curve, when the heat of compression is withdrawn so as to keep the temperature constant. The three curves which begin at the lower right hand corner and rise to the left are heat curves, and represent the increase of temperature corresponding to different pressures and volumes, assuming in one case that the temperature of the air before admission to the compressor is zero, in another sixty degrees, and in another one hundred degrees.

Beginning with the adiabatic curve, we find that for one volume of air, when compressed without cooling, the curve intersects the first horizontal line at a point between 0.6 and 0.7 volume, the gauge pressure being 14.7 pounds. If we assume that this air was admitted to the compressor at a temperature of zero, it will reach about $100^{\circ}$ when the gauge pressure is 14.7 pounds. If the air had been admitted to the compressor at $60^{\circ}$, it would register about $176^{\circ}$ at 14.7 pounds gauge pressure. If the air were $100^{\circ}$ before compression, it would go up to about $230^{\circ}$ at this pressure. Following this adiabatic curve until it intersects line No. 5, representing a pressure of five atmospheres above a vacuum ( 58.8 pounds
gauge pressure), we see that the total increase of temperature on the zero heat curve is about $270^{\circ}$; for the $60^{\circ}$ curve it is about $370^{\circ}$, and for the $100^{\circ}$ curve it is $435^{\circ}$. The diagram shows that when a volume of air is compressed adiabatically to 21 atmospheres ( 294 pounds gauge pressure), it will occupy a volume a little more than one-tenth; the total increase of temperature with an initial temperature of zero, is about $650^{\circ}$; with $60^{\circ}$ initial temperature it is $800^{\circ}$ and with $100^{\circ}$ initial it is $900^{\circ}$. It will be observed that the zero heat curve is flatter than the others, indicating that when free air is admitted to a compressor cold, the relative increase of temperature is less than when the air is hot. This points to the importance of low initial temperature. It is plain that a high initial temperature means a higher temperature throughout the stroke of a compressor. The diagram gives the loss of temperature during compression from initial temperatures of $0^{\circ}, 60^{\circ}, 100^{\circ}$. If we compare the compression line from zero with the compression line from $100^{\circ}$, we observe that in compressing the air from, say 1 atmosphere to 10 atmospheres, the original difference, which at the start was only $100^{\circ}$, has now been about doubled; that is, it has reached $200^{\circ}$, and in carrying the compression to 20 atmospheres, the difference now becomes about $250^{\circ}$. Each horizontal division represented by the figures at the bottom is equal to $100^{\circ}$, and the space between any two adjacent horizontal lines may be sub-divided into 100 equal parts representing $1^{\circ}$ each.

Where there is a system of cooling the air during compression, the lines on the indicator cards can be traced between the adiabatic and isothermal curves on the diagram.

For all practical purposes in using this diagram, it is best to follow the adiabatic curve in all determinations, except where the exact pressure line is known. This diagram will be found convenient to those who are called upon to figure the pressure at different points in the
stroke of an air compressor, and it points out the common error of neglecting to take into consideration in one's figures the fact that, at the beginning of the stroke, one atmosphere in volume already exists. Beginning at the lower left hand corner, the adiabatic pressure curve intersects the first horizontal line at that point in the stroke when the pressure on the gauge will register 14.7 pounds.

The next horizontal line shows where the gauge reaches 29.4 pounds, and it is evident here that the piston of an air compressor travels much farther in reaching 14.7 pounds than in doubling that pressure or in reaching 29.4 pounds; thus an air compressor is an engine of unevenly distributed resistance. During the early stages of the stroke it has a slowly accumulating load to carry, while later on this load is multiplied very rapidly. This is one of the reasons for heavy flywheels in air compressors.

## Compressed Air.

EFFFECT OF COMPOUNDING, COOLING, INTER-COOLING, AFTER-COOLING AND REHEATING.
(From Compressed Air Magazine.)
Builders of air compressors and those who use compressed air will agree that the problem of heating or cooling air is a difficult one. Hot air in the cylinder of an air compressor means a reduction in the efficiency of the machine. The trouble is, that there is not sufficient time during the stroke to cool thoroughly by any available means. Water-jacketing is the generally accepted practice, but it does not by any means effect through cooling. The air in the cylinder is so large in volume that but a fraction of its surface is brought in contact with the jacketed parts. Air is a bad conductor of heat and takes time to change its temperature. The piston while pushing the air towards the head rapidly drives it away from the jacketed surfaces; so that little or no cooling takes place. This is especially true of large cylinders where the economy effected by water-jackets is considerably less than in small cylinders. Engineers who are shown indicator cards from large air compressors with pressure lines running away from the adiabatic, naturally regard them with suspicion and look for leaks past the piston or through the valves. Such leaks will explain many isothermal cards, and until something better than a water-jacket is devised, it is well to seek economy in air compression through compounding.

The great advantage of compounding is in the fact that the inter-cooler, which should always be used with compound machines, effects a larger saving by cooling and thereby causing the air to shrink in volume between the stages. A properly designed inter-cooler should reduce the temperature of the air back to the orginal
point, that is, to the temperature of the intake air. It can even do more than this, especially in winter, when the water used in the inter-color is of low temperature. A simple coil of pipe submerged in water is not an effective inter-cooler, because the air passes through the coil too rapidly to be cooled to the core, and such intercoolers do not sufficiently split up the air to enable it to be cooled rapidly. This splitting up of air is an important point. A nest of tubes carrying water and arranged so that the air is forced between and around the tubes is an efficient form of inter-cooler.

Receiver inter-coolers are more efficient than those of the common type because the air is given more time to pass through the cooling stages and because of the freedom from wire drawing which may take place in intercoolers of small volumetric capacity.

After-coolers are in some installations as important as inter-coolers. An after-cooler serves to reduce the temperature of the air after the final compression. In doing this it serves as a drier, reducing the temperature of air to the dew point, thus abstracting moisture before the air is started on its journey. In cold weather with air pipes laid over the ground an after-cooler may prevent accumulation of frost in the interior walls of the pipes, for where the hot compressed air is allowed to cool gradually the walls of the pipe in cold weather act like a surface condenser and moisture may be deposited on the inside, for the same reason that we have frost on the inner side of a window pane. Another advantage of the aftercooler is that it keeps the temperature of the line pipe uniform, otherwise this pipe will be hottest near the compressor, gradually cooling down and being thus subject to irregularities of expansion and contraction.
The following table will serve to illustrate the large saving that it is possible to effect by compounding. This table gives the percentage of work lost by the heat of compression, taking isothermal compression, or compression without heat, as a base.

|  | One Stage. |  | Two Stage. |  | Four Stage. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\begin{aligned} & \text { \% of work lost in } \\ & \text { terms of Isothermal } \\ & \text { Compression. } \end{aligned}$ |  |  |  |
| 60 | 30. \% | 23. \% | 13.38\% | $11.8 \%$ | 4.65\% | 4.45\% |
| 80 | 34. | 25.26 | 15.12 | 13.12 | 5.04 | 4.80 |
| 100 | 38. | 27.58 | 17.10 | 14.62 | 8.00 | 7.41 |
| 200 | 52.35 | 34.40 | 23.20 | 18.88 | 9.01 | 8.27 |
| 400 | 68.60 | 40.75 | 29.70 | 22.90 | 12.40 | 11.04 |
| 600 | 83.75 | 44.60 | 32.65 | 24.60 | 15.06 | 13.10 |
| 800 | 90. | 47.40 | 35.80 | 26.33 | 16.74 | 14.32 |
| 1000 | 96.80 | 49.20 | 39.00 | 28.10 | 16.90 | 14.45 |
| 1200 | 106.15 | 51.60 | 40.00 | 28.60 | 17.45 | 14.85 |
| 1400 | 108. | 52. | 41.60 | 29.4 | 17.70 | 15.00 |
| 1600 | 110. | 53.3 | 42.90 | 30.0 | 18.40 | 15.54 |
| 1800 | 116.80 | 54. | 44.40 | 30.6 | 19.12 | 16.05 |
| 2000 | 121.70 | 54.8 | 44.60 | 30.8 | 20.00 | 16.65 |

In the above table no account is taken of jacket cooling, it being a well known fact among pneumatic engineers that water jackets, especially cylinder jackets, though useful and perhaps indispensable, are not efficient in cooling, especially so in large compressors. The volume of air is so great in proportion to the surface exposed and at the time of compression so short, that little or no cooling takes place. Jacketed heads are useful auxiliaries in cooling, but it has become an accepted theory among engineers that compounding or stage compression is more fertile as a means of economy than any other system that has yet been devised. The two and four stage figures in this table (columns 3 and 4), are based on reduction to atmospheric temperature, or $60^{\circ}$ Fahrenheit, between stages. A rule which might be
observed to advantage among engineers is to specify that the manufacturers should supply a compressor with coolers provided with one square foot of tube cooling surface for every ten cubic feet of free air furnished by the compressor when running at its normal speed.

Referring again to the table, we learn that when air is compressed to 100 pounds pressure per square inch in a single stage compressor without cooling, the heat loss may be thirty-eight (38) per cent. This condition, of course, does not exist in practice, except perhaps, at exceedingly high speeds, as there will be some absorption of heat by the exposed parts of the machine. It is safe, however, to say that in large air compressors that compress in a single stage up to 100 pounds gauge pressure, the heat loss reaches thirty (30) per cent. This, as shown by the table, may be cut down more than onehalf by compressing in two-stages, and with three-stages this loss is brought down to eight (8) per cent. theoretically, and perhaps to three or five (3 or 5) per cent. in practice. As higher pressures are used, the gain by compounding is greater.

## Efficiency of Air Compressors at

## Different Altitudes.

The altitude, where the compressor is to operate, is an important factor because it affects its capacity to a greater or lesser extent, according to the elevation. As the density of the atmosphere decreases with the altitude, a compressor located at a high altitude takes in less weight of air at each revolution, that is to say, the air being taken in at a lower pressure, the early part of each stroke is occupied in compressing the air up to the normal pressure of 14.7 pounds, and the capacity of the air cylinder is correspondingly diminished. The power
required to drive the same compressor is also less than at sea level, but the decrease in power required is not in as great a ratio as the reduction in capacity. Therefore, compressors to be used at high altitudes should have the steam and air cylinders properly proportioned to meet the varying conditions at different places.

The following table shows the efficiency and loss in capacity of compressors working at different altitudes, also the approximate decrease in power required as compared with the same compressor working at sea level, and delivering air at 70 pounds pressure per square inch.

## TABLE OF EFFICIENCIES A'T DIFFEREN'T AL'TITUDES.

 the efficiency at sea level being 100 per cent.|  | Barometric Pressure. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Inches, Mercury. | Pounds per Square Inch. |  |  |  |
| 1000 | 28.88 | 14.20 | 97. | 3. | 1.8 |
| 2000 | 27.80 | 13.67 | 93. | 7. | 3.5 |
| 3000 | 26.76 | 13.16 | 90. | 10. | 5.2 |
| 4000 | 25.76 | 12.67 | 87. | 13. | 6.9 |
| 5000 | 24.79 | 12.20 | 84. | 16. | 8.5 |
| 6000 | 23.86 | 11.73 | 81. | 19. | 10.1 |
| 7000 | 22.97 | 11.30 | 78. | 22. | 11.6 |
| 8000 | 2211 | 10.87 | 76. | 24. | 13.1 |
| 9000 | 21.29 | 10.46 | 73. | 271 | 14.6 |
| 10000 | 20.49 | 10.07 | 70. | 30. | 16.1 |
| 11000 | 19.72 | 9.70 | 68. | 32. | 17.6 |
| 12000 | 18.98 | 9.34 | 65. | 35. | 19.1 |
| 13000 | 18.27 | 8.98 | 63. | 37. | 20.6 |
| 14000 | 17.59 | 8.65 | 60. | 40. | 22.1 |
| 15000 | 16.93 | 8.32 | 58. | 42. | 23.5 |

Horse-power Required to Compress 100 Cubic Feet Free Air, from Atmospheric to Various Pressures.

| Gauge <br> Pressure, <br> Pounds. | One-Stage <br> Compression, <br> D. H. P. | Gauge <br> Pressure, <br> Pounds. | Two-Stage <br> Compression, <br> D. H. P. | Four-Stage <br> Compression, <br> D H. P. |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |
| 10 | 3.60 | 60 | 11.70 |  |
| 15 | 5.03 | 80 | 13.70 | 10.80 |
| 20 | 6.28 | 100 | 15.40 | 14.50 |
| 25 | 7.42 | 200 | 21.20 | 18.75 |
| 30 | 8.47 | 300 | 24.50 | 21.80 |
| 35 | 9.42 | 400 | 27.70 | 24.00 |
| 40 | 10.30 | 500 | 29.75 | 25.90 |
| 45 | 11.14 | 600 | 31.70 | 27.50 |
| 50 | 11.90 | 700 | 33.50 | 28.90 |
| 55 | 12.67 | 800 | 34.90 | 30.00 |
| 60 | 13.41 | 900 | 36.30 | 31.00 |
| 70 | 14.72 | 1000 | 37.80 | 31.80 |
| 80 | 15.94 | 1200 | 39.70 | 33.30 |
| 90 | 17.06 | 1600 | 43.00 | 35.65 |
| 100 | 18.15 | 2000 | 45.50 | 37.80 |
|  |  | 2500 |  | 39.06 |
|  |  | 3000 |  | 40.15 |

D. H. P., delivered horse-power at compressor cylinder.

## Capacity of Air Compressors.

To ascertain the capacity of an air compressor in cubic feet of free air per minute, the common practice is to multiply the area of the intake cylinder by the feet of piston travel per minute. The free air capacity of the compressor divided by the number of atmospheres will give the volume of compressed air per minute. To ascertain the number of atmospheres at any given pressure, add 14.7 lbs . to the gauge pressure, divide this sum by 14.7 and the result will be the number of atmospheres.

The above method of calculation, however, is only theoretical and these results are never obtained in actual practice even with compressors of the very best design.

Allowances should be made for losses of various kinds, the principal loss being due to clearance spaces, but in machines of poor design and construction other considerable losses occur through imperfect cooling, leakages past the piston and through the discharge valves, insufficient area and improper working of inlet valves, etc. We have seen compressors where the total loss was fully 25 to 30 per cent., whereas, 3 to 10 per cent. should be the maximum-according to the size-in compressors of proper design and construction.

Weights of Air, Vapor of Water, and Saturated Mixtures of Air and Vapor at Different 'Temperatures, under the Ordinary Atmospheric Pressure of 29.92 inches of Mercury.

|  |  | $\begin{aligned} & \text { Elastic Force of Vapor, } \\ & \text { Inches of Mercury. } \end{aligned}$ | Mixtures of AIr Saturated with Vapor |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Weight of Cubic Foot of the Mixture of Air and Vapor. |  |  | $\begin{aligned} & \text { Weight of Vapor } \\ & \text { mixed with } 116 \text { of } \\ & \text { Air, } 1 \mathrm{bs} \text {. } \end{aligned}$ |
|  |  |  |  |  |  |  |  |
| 0 | . 0864 | . 044 |  | . 0863 | . 000079 | . 086379 | 2 |
| 12 | . 0842 | . 074 | 29.849 | . 0840 | . 000130 | . 084130 | . 00155 |
| 2 | . 0824 | . 118 | 29.803 | . 0821 | . 000202 | . 082302 | . 00245 |
| 32 | . 0807 | . 181 | 29.740 | . 0802 | . 000304 | . 080504 | . 00379 |
| 42 | . 0791 | . 267 | 29.654 | . 0784 | . 000440 | . 078840 | . 00561 |
| 52 | . 0776 | . 388 | 29.533 | . 0766 | . 000627 | . 077227 | . 00819 |
| 62 | . 0761 | . 556 | 29.365 | . 0747 | . 000881 | . 075581 | . 01179 |
| 72 | . 0747 | . 785 | 29.136 | . 0727 | . 001221 | . 073921 | . 01680 |
| 82 | . 0733 | 1.092 | 28,829 | . 0706 | . 001667 | .072267 | . 02361 |
| 92 | . 0720 | 1.501 | 28.420 | . 0684 | . 002250 | . 070717 | . 03289 |
| 102 | . 0707 | 2.036 | 27.885 | . 0659 | . 002997 | . 068897 | . 04547 |
| 112 | . 0694 | 2.731 | 27.190 | . 0631 | . 003946 | . 067046 | . 06253 |
| 122 | . 0682 | 3.621 | 26.300 | . 0599 | . 005142 | . 065042 | . 08584 |
| 132 | . 0671 | 4.752 | 25.169 | . 0564 | . 0006639 | . 063039 | . 11771 |
| 142 | . 0660 | 6.165 | 23.756 | . 0524 | . 008473 | . 060873 | . 16170 |
| 152 | . 0649 | 7.930 | 21.991 | . 0477 | . 010716 | . 058416 | . 22465 |
| 162 | . 0638 | 10.099 | 19.822 | . 0423 | . 013415 | . 055715 | . 31713 |
| 172 | . 0628 | 12.758 | 17.163 | . 0360 | . 016682 | . 052682 | . 46338 |
| 182 | . 0618 | 15.960 | 13.961 | . 0288 | . 020536 | . 0493336 | . 71300 |
| 192 | . 0609 | 19.828 | 10.093 | . 0205 | . 025142 | .045642 | 1.22643 |
| 202 | . 0600 | 24.450 | 5.471 | . 0109 | . 030545 | . 041445 | 2.80230 |
| 212 | . 0591 | 29.92 | 0.000 | . 0000 | 036820 | .036820 | Infinite |

## FLOW OF AIR THROUGH AN ORIFICE FROM A RESERVOIR INTO 'T'HE ATMOSPHERE,

In Cubic Feet of Free Air per Minute for Varying Diameters of Orifice and Gauge Pressures.


|  | 45 | 50 | ${ }_{60}^{60}$ lbs. | 70 lbs. | 80 lbs. | 90 lbs. | 100 lbs. | 125 lbs. | 150 lbs. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\frac{7}{64}$ | 0.208 | 0.225 | 0.26 | 0.295 | 0.33 | 0.364 | 0.40 | 0.486 | 0.57 |
| $\frac{1}{31}$ | 0.843 | 0.914 | 1.05 | 1.19 | 1.33 | 1.47 | 1.61 | 1.97 | 2.33 |
| ${ }^{32}$ | 3.36 | 3.64 | 4.2 | 4.76 | 5.32 | 5.87 | 6.45 | 7.85 | 9.25 |
|  | 13.4 | 14.50 | 16.8 | 19.0 | 21.2 | 23.50 | 25.8 | 31.4 | 37.2 |
| 14 | 53.8 | 58.2 | 67. | 76. | 85. | 94. | 103. | 125. | 148. |
| 3 | 121. | 130. | 151. | 171. | 191. | 211. | 231. | 282. | 334. |
| 1 | 215. | 232. | 268. | 304. | 340. | 376. | 412. | 502. | 596. |
| 5/8 | 336. | 364. | 420. | 476. | 532. | 587. | 645. | 785. | 925. |
| 3 | 482. | 522. | 604. | 685. | 765. | 843. | 925. |  |  |
| 178 | 658. | 710. | 622. | 930. | 1004. |  |  |  |  |
| 1 | 860. | 930. |  |  |  |  |  |  |  |

The above table was computed with the aid of Fliegner's equations and have given results that approximate very closely to the conditions of actual practice. These equations are :

$\begin{aligned} & \text { For } p_{1}>2 p a, G=0.530 F \frac{p_{1}}{\sqrt{T_{1}}} \\ &$$$
p_{1}>2 p a, G=1.060 F \sqrt{\frac{p a\left(p_{1}-p a\right)}{T_{1}}} ; \text { in which }
$$$\end{aligned}$

$G=$ flow of air through the orifice in lbs. per sec.,$F=$ area of orifice - in square inches, $p_{2}=$ pressure in reservoir in lbs. per sq. in., $p a=$ pressure of atmosphere, $T_{1}=$ absolute temperature, Fahrenheit, of air in reservoir.

## FLOW OF AIR THROUGH PIPES.*

The following new and original tables are based upon D'Arcy's formula adapted to the flow of elastic fluids, namely:
$\left.\begin{array}{c}\text { Discharge in cubic } \\ \text { feet per minute }\end{array}\right\}=c \sqrt{\frac{d^{5} \times\left(p_{1}-p_{g}\right)}{l \times w_{1}} .}$
As it is most convenient in the case of compressed air installations to deal with its equivalent volume of free air, $i . e .$, air at atmospheric pressure, these tables have been specially calculated with this end in view.

Table I. Gives the theoretical volume of equivalent free air in cubic feet that will flow per minute at various pressures through straight pipes of various diameters, each roo feet long, no reduction of the final pressure being allowed for.

The formula by which it is calculated is:
$\left.\begin{array}{c}\text { Theoretical discharge } \\ \text { of free air }\end{array}\right\}=F_{\mathrm{t}}=\frac{c \sqrt{d^{\mathrm{s}}}}{10} \times \frac{f_{1}}{\sqrt{w_{1}}}$.
Table II. Is a table of multipliers to be used in connection with $F_{\mathrm{t}}$, as found by Table I., by which may be obtained the theoretical discharge of equivalent free air from pipes of various lengths up to 60,000 feet. It is calculated from

$$
\left.\begin{array}{l}
\text { Multiplier for } \\
\text { length of pipe }
\end{array}\right\}=M_{1}=\sqrt{\frac{100}{l}} .
$$

[^7]Table III. Is a table of Multipliers to be used in connection with $F_{\mathrm{t}}$ and $M_{1}$ as found by Tables I. and II., to obtain the real volume of discharge of equivalent free air, for reductions of the terminal pressure varying from 1 to 50 pounds. It is calculated from

$$
\left.\begin{array}{l}
\text { Multiplier for } \\
\text { real discharge }
\end{array}\right\}=M_{\mathrm{r}}=\frac{f_{2}}{f_{1}} \times \sqrt{p_{1}-p_{2}}
$$

The notation used in above formulas is
$d=$ actual diameter of pipe in inches.
$l=$ length of pipe in feet.
$c=$ a co-efficient, (D'Arcy's) varying with the diameter of the pipe.
$w_{1}=$ density of the air at initial gauge pressure.
$p_{1}$ and $p_{2}=$ initial and terminal gauge pressures.
$f_{1}$ and $f_{2}=$ factors to reduce compressed air at initial and terminal pressures $p_{1}$ and $p_{2}$ to their corresponding volumes of free air.

Tables are also added showing the increase in the length of pipe to be allowed for on account of the friction caused by globe valves, elbows and tees.

Several examples are worked out to show the method of using the tables for the solution of problems likely to be met with by the Engineer.
TABLE I. TABLE I. Giving the Theoretical Volume of Equivalent Free Air, in Cubic Feet, that will flow per minute at
various pressures throughstraight pipes of different diameters, each 100 feet long, not allowing for reduction of pressure.

| 12 | 15 | 18 | 20 | 22 | 24 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 14530 | 22530 | 36280 | 48180 | 61870 | 77880 |


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TABLE II. MULTIPLIERS FOR LENGTH OF PIPE.

| Length, <br> feet. | Multipler <br> $\mathrm{M}_{1}$. | Length, <br> feet. | Multipler <br> $\mathrm{M}_{1}$. |
| :--- | :--- | :--- | :--- |
| 100 | 1.0 | 6000 | 0.129 |
| 200 | 0.707 | 7000 | 0.119 |
| 300 | 0.577 | 8000 | 0.112 |
| 400 | 0.500 | 9000 | 0.105 |
| 500 | 0.447 | 10000 | 0.100 |
| 600 | 0.408 | 12000 | 0.0912 |
| 7750 | 0.365 | 15000 | 0.0817 |
| 1000 | 0.316 | 20000 | 0.0707 |
| 1250 | 0.283 | 25000 | 0.0632 |
| 1500 | 0.258 | 30000 | 0.0577 |
| 2000 | 0.224 | 35000 | 0.0534 |
| 2500 | 0.200 | 40000 | 0.0500 |
| 3000 | 0.183 | 45000 | 0.0471 |
| 3500 | 0.169 | 50000 | 0.0447 |
| 4000 | 0.158 | 55000 | 0.0426 |
| 5000 | 0.141 | 60000 | 0.0408 |



The formulas by which these tables have been calculated show that the following factors enter into their composition :

$$
\text { The diameter of the pipe. . . . . . . }=d \text {. }
$$

The length of the pipe........... $=l$. $\left.\begin{array}{l}\text { The initial and final pressures, } \\ \text { or the reduction of pressure }\end{array}\right\}=p_{1}-p_{2}$. The equivalent free air discharged .$=F$.
It being often required to find any one of these factors when the others are known, the following examples are given to show the method of procedure in each case.

The simple statement of the formula, adapted to the tables becomes

Free air discharged $=F=F_{\mathrm{t}} \times M_{1} \times M_{\mathrm{r}}$
and by this all problems involving any of the above factors may be solved, as shown in the examples.

Example 1.-To find the volume of free air discharged.
Example 2.-To find the reduction of pressure.
" 3.-To find a suitable diameter of pipe.
" 4.-To find the length of pipe which may be used.
Example I.-Given a 3 -inch pipe, 10,000 feet long, initial pressure $1,100 \mathrm{lbs}$., terminal pressure $1,050 \mathrm{lbs}$.; to find the volume of equivalent free air discharged.

By Table I.-Under $3^{\prime \prime}$ pipe and opposite 1,100 lbs. we find $F_{\mathrm{t}}=2,906$.
By Table II.-For 10,000 feet of pipe, $M_{1}=0.1$. "، "، III.-Under 50 1bs. reduction and opposite $1,100 \mathrm{lbs} ., M_{\mathrm{r}}=6.75$.
Then as shown
$F=F_{\mathrm{t}} \times M_{1} \times M_{\mathrm{r}}=2,906 \times 0.1 \times 6.75=1,961$ cubic feet free air.

Example 2.-Given a 4 -inch pipe, 600 feet long, initial pressure 60 lbs ., required to discharge 1,200 cubic feet free air. What will be the reduction of pressure and the terminal pressure?

By Table I.-Under 4" pipe and opposite 60 lbs., we find $F_{t}=1,535$.
By Table II.-For 600 feet, $M_{1}=0.408$. Given $F=1,200$.
By transposing the formula

$$
M_{\mathrm{r}}=\frac{\mathrm{F}}{F_{\mathrm{t}} \times M_{1}}=\frac{1,200}{1,535 \times 0.408}=1.9
$$

Now by Table III., opposite 60 lbs . pressure, and under 4 lbs . reduction, we find $M_{\mathrm{r}}=1.89$, so that the terminal pressure will be slightly less than $60-4=56$ pounds.

Example 3.-It is required to discharge 1000 cubic feet of free air from a pipe 2,500 feet long. The initial pressure is 100 lbs . and the terminal pressure must not be less than 90 lbs . What diameter of pipe should be used ?

Here we have given $F=1000$.
By Table II . . . . . . $M_{1}=0.200$ for 2,500 feet.
" " III. ....... $M_{\mathrm{r}}=2.88$ for $p_{1}=100 \mathrm{lbs}$., and $p_{2}=90 \mathrm{lbs}$.
By transposing the formula we get

$$
\mathrm{F}_{\mathrm{t}}=\frac{F}{M_{1} \times M_{\mathrm{r}}}=\frac{1,000}{0.200 \times 2.88}=1,736
$$

By Table I. looking along the line of 100 lbs . pressure we see that the value of $F_{\mathrm{t}}$ for a $31 / 2$-inch pipe is 1,370 , and for a 4 -inch pipe 1,904 , so that this latter size of pipe would have to be used.

Example 4.-It is required to transmit 4,000 cubic feet of free air through a 6 -inch pipe, the initial pressure being 200 lbs . How far can it be carried with a reduction of pressure of 10 lbs .?

Here we have given $F=4,000$.
By Table I..... $F_{\mathrm{t}}=7,489$ for 200 lbs . pressure and $6^{\prime \prime}$ pipe.
By Table III..... $M_{\mathrm{r}}=3.01$ for 200 lbs . pressure and io lbs. reduction.
Then by transposing the formula:

$$
M_{1}=\frac{F}{F_{\mathrm{t}} \times M_{\mathrm{r}}}=\frac{4,000}{7,489 \times 3.01}=0.177
$$

Now by Table II. we see that this is an intermediate value of $M_{1}$ between 3000 and 3500 feet, so that the distance sought is approximately 3250 feet.

## GLOBE VALVES, TEES AND ELBOWS.

The reduction of pressure produced by globe valves is the same as that caused by the following additional lengths of straight pipe, as calculated by the formula :

$$
\text { Additional length of pipe }=\frac{114 \times \text { diameter of pipe }}{1+(3.6 \div \text { diameter })}
$$

$\left.\begin{array}{l}\text { Diameter of pipe. } \\ \hline \text { Addition'llength. }\end{array}\right\} \begin{array}{cccccccccccc}1 & 1 \frac{1}{2} & 2 & 2 \frac{1}{2} & 3 & 3 \frac{1}{2} & 4 & 5 & 6 & \text { inches. } \\ 2 & 4 & 7 & 10 & 13 & 16 & 20 & 28 & 36 & \text { feet. }\end{array}$

$$
\begin{array}{cccccccccc}
7 & 8 & 10 & 12 & 15 & 18 & 20 & 22 & 24 & \mathrm{ins} . \\
\hline 44 & 53 & 70 & 88 & 115 & 143 & 162 & 181 & 200 & \mathrm{ft} .
\end{array}
$$

The reduction of pressure produced by elbows and tees is equal to $\frac{2}{8}$ of that caused by globe valves.

These additional lengths of pipe for globe valves, elbows and tees must be added in each case to the actual lengths of straight pipe. Thus, a 6 -inch pipe, 500 feet long, with one globe valve, 2 elbows and three tees, would be equivalent to a straight pipe $500+36+(2 \times 24)$ $+(3 \times 24)=656$ feet long, and' this is the length which must be used in the tables as the value of $M_{1}$.

## GENERAL EXAMPLE.

How much free air will a 6 -inch pipe, 8,000 feet long, discharge under the following conditions, namely: Initial pressure 150 lbs ., terminal pressure 135 lbs ., with 2 globe valves, 3 elbows and 1 tee?

The equivalent length of straight pipe must first be found as follows :

$$
8,000+(2 \times 36)+(3 \times 24)+24=8,168 \text { feet. }
$$

Now we have
By Table I., $F_{\mathrm{t}}=6,558$ for 6 inch pipe and 150 lbs . pressure.
By Table II., $M_{1}=0.112$ for 8000 feet, making by interpolation say 0.110 for 8,168 feet.
By Table III., $M_{\mathrm{r}}=3.42$ for 150 lbs . pressure and 14 lbs . reduction, and 3.61 for 150 lbs . pressure and 16 lbs . reduction, so that by interpolation $M_{\mathrm{r}}$ would be 3.51 for 15 lbs . reduction of pressure.
Then by the formula :
Free air discharged $=F=F_{\mathrm{t}} \times M_{1} \times M_{\mathrm{r}}$.

$$
=6,558 \times 0.11 \times 3.51
$$

$=2,532$ cubic feet equivalent free air per minute.

## FORMULA FOR FLOW OF AIR IN PIPES.

Mr. Richards, in Am. Mach., Dec. 27, 1894, published a new formula, viz.:

$$
\begin{gathered}
p=\frac{V^{2} L}{10,000 d^{5} a} ; \quad V=\sqrt{\frac{10,000 d^{5} a p}{L} ; \quad L=\frac{10,000 d^{5} a p}{V^{2}}} ; \\
d^{5} a p=\frac{V^{2} L}{10,000 p} ;
\end{gathered}
$$

in which $V=$ actual volume of compressed air delivered, in cubic feet per minute (not the volume of free air, as
in the other formula), $L=$ length of pipe in feet, $d=$ internal diameter of pipe in inches, $p=$ head or additional pressure in pounds per square inch required to maintain the flow, and $a$ is a coefficient varying with the diameter of the pipe. Its value for different nominal diameters of wrought-iron pipe is given by Mr. Richards as follows :

| Diam., <br> Inches. | Value <br> of $a$. | Diam., <br> Inches. | Value <br> of $a$. | Diam., <br> Inches. | Value <br> of $a$. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | .35 | $31 / 2$ | .79 | 12 | 1.26 |
| 114 | .44 | 4 | .84 | 16 | 1.34 |
| $11 / 2$ | .50 | 5 | .93 | 20 | 1.4 |
| 2 | .56 | 6 | 1. | 24 | 1.45 |
| $21 / 2$ | .65 | 8 | 1.125 |  |  |
| 3 | .73 | 10 | 1.2 |  |  |

The following values of the fifth power of $d$ and of $d^{5} a$ are given by Mr. Richards to facilitate calculations:

| Fifth Powers of $d$. |  | Value of $d^{5} a$. |  |
| :---: | :---: | :---: | :---: |
| 1 1........ 1 | $5^{\prime \prime} \ldots$ 3,125 | $1^{\prime} \ldots \ldots .$. | 5"... 2,918.75 |
| $114, \ldots \ldots .3 .05$ | $6^{\prime \prime} \ldots \quad 7,776$ | $114 . . . . . .1 .34$ | $6^{*} \ldots$... 7,776 |
| 112"....... 7.59 | $8^{\prime \prime} \ldots \quad 32,768$ | 112"..... 3.80 | $8^{*} \cdot \cdots 636,864$ |
| 2'......... 32 | $10^{*} \ldots .100,000$ | $2^{\prime \prime} \ldots . . .{ }^{18.08}$ | $10^{\prime \prime} \ldots \quad 120,000$ |
| 2119.…... 97.65 | $12^{*} \ldots$... 248,832 | 21/8'..... 63.47 | $12^{*} \ldots \quad 313,528$ |
| $3^{*} \ldots \ldots \ldots . .243$ | $16^{\prime \prime} \ldots . .1,048,576$ | $3^{\prime \prime} \ldots . . . .1{ }^{177.4}$ | $16^{*} \ldots .1,405,091$ |
| 31/2'...... 525 | 20..... 3,200,000 | 31/6... . 413.2 | $20^{\circ} \cdots .4,480,000$ |
| 4*........ 1024 | 24".... 7,962,624 | $4^{*} \ldots . . . . .860 .2$ | $24^{\prime \prime} \ldots . .11,545,805$ |

GAS.

## FLOW OF GAS IN PIPES.

If $d=$ diameter of pipe in inches ; $Q=$ quantity of gas delivered in cu. ft. per hour ; $l=$ length of pipe in yards ; $h=$ pressure in inches of water column; $s=$ specific gravity of the gas, air being one; then

$$
\begin{gathered}
Q=1000 \sqrt{\frac{d^{5} h}{s l}}, \quad \text { (Molesworth). } \\
Q=1350 d^{2} \sqrt{\frac{d h}{s l}}, \quad \text { (King's Treatise on Coal Gas.) }
\end{gathered}
$$

$$
Q=1290 \sqrt{\frac{d^{5} h}{d(s+l)}} \text {,(J. P. Gill, Am. Gas-light Jour., 1894). }
$$

Mr. Gill's formula is said to be based on experimental data, and to make allowance for obstructions by tar, etc., that tend to check the flow of gas through the pipe.

An experiment made by Mr. Klegg, in London, on a 4 inch pipe, 6 miles long, gave a discharge that corresponds very closely with that computed by the use of Molesworth's formula.

Maximum Supply of Gas through Pipes in cu. ft. per Hour, Specific Gravity being 0.45. Formula $Q=1000 \sqrt{d^{5} h \div s l}$.
(Molesworth.)
Length of Pipe $=10$ Yards.

|  | Pressure by the Water-gauge in Inches. |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0.1 | 0.2 | 0.3 | 0.4 | 0.5 | 0.6 | 0.7 | 0.8 | 0.9 | 1.0 |
| $3 / 8$ | 13 | 18 | 22 | 26 | 29 | 31 | 34 | 36 | 38 | 41 |
| $1 / 8$ | 26 | 37 | 46 | 53 | 59 | 64 | 70 | 74 | 79 | 83 |
| 34 | 73 | 103 | 126 | 145 | 162 | 187 | 192 | 205 | 218 | 230 |
|  | 149 | 211 | 258 | 298 | 333 | 365 | 394 | 422 | 447 | 471 |
| $11 / 4$ | 260 | 368 | 451 | 521 | 582 | 638 | 689 | 737 | 781 | 823 |
| 11/3 | 411 | 581 | 711 | 821 | 918 | 1006 | 1082 | 1162 | 1232 | 1299 |
|  | 843 | 1192 | 1460 | 1686 | 1886 | 2066 | 2231 | 2385 | 2530 | 2667 |

Maximum Supply of Gas through Pipes, etc.-(Continued.)
Length of Pipe $=100$ Yards.

| U. | Pressure by the Water-gauge in Inches. |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\stackrel{\square}{\square}$ | 0.1 | 0.2 | 0.3 | 0.4 | 0.5 | 0.75 | 1.0 | 1.25 | 1.5 | 2.0 | 2.5 |
| $1 / 3$ | 8 | 12 | 14 | 17 | 19 | 23 | 26 | 29 | 32 | 36 | 42 |
| $3 / 4$ | 23 | 32 | 42 | 46 | 51 | 63 | 73 | 81 | 89 | 103 | 115 |
| 1 | 47 | 67 | 82 | 94 | 105 | 129 | 149 | 167 | 183 | 211 | 236 |
| 11/4 | 82 | 116 | 143 | 165 | 184 | 225 | 260 | 291 | 319 | 368 | 412 |
| $11 / 3$ | 130 | 184 | 225 | 260 | 290 | 356 | 411 | 459 | 503 | 581 | 649 |
| 2 | 267 | 377 | 462 | 533 | 596 | 730 | 843 | 943 | 1033 | 1193 | 1333 |
| 2116 | 466 | 659 | 807 | 932 | 1042 | 1276 | 1473 | 1647 | 1804 | 2083 | 2329 |
| ) | 735 | 1039 | 1270 | 1470 | 1643 | 2012 | 2323 | 2598 | 2846 | 3286 | 3674 |
| 31/2 | 1080 | 1528 | 1871 | 2161 | 2416 | 2958 | 3416 | 3820 | 4184 | 4831 | 5402 |
|  | 1508 | 2133 | 2613 | 3017 | 3373 | 4131. | 4770 | 5333 | 5842 | 6746 | 7542 |

Length of PIPE $=1000$ Yards.

|  | Pressure by the Water-gauge in Inches. |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0.5 | 0.75 | 1.0 | 1.5 | 2.0 | 2.5 | 3.0 |
| 1 | 33 | 41 | 47 | 58 | 67 | 75 | 82 |
| 11/2 | 92 | 113 | 130 | 159 | 184 | 205 | 226 |
| 2 | 189 | 231 | 267 | 327 | 377 | 422 | 462 |
| 216 | 329 | 403 | 466 | 571 | 659 | 737 | 807 |
| 3 | 520 | 636 | 735 | 900 | 1039 | 1162 | 1273 |
| 4 | 1067 | 1306 | 1508 | 1847 | 2133 | 2385 | 2613 |
| 5 | 1863 | 2282 | 2635 | 3227 | 3727 | 4167 | 4564 |
| 6 | 2939 | 3600 | 4157 | 5091 | 5879 | 6573 | 7200 |

Length of Pipe $=5000$ Yards.

| "\% | Pressure by the Water-gauge in Inches. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 同 | 1.0 | 1.5 | 2.0 | 2.5 | 3.0 |
| 2 | 119 | 146 402 | 169 465 | 189 520 | 207 |
| 3 | 329 | 402 | 465 | 520 | 569 |
| 4 | 675 | 826 | 955 | 1067 | 1168 |
| 5 | 1179 | 1443 | 1667 | 1863 | 2041 |
| 6 | 1859 | 2277 | 2629 | 2939 | 3220 |
| 7 | 2733 | 3347 | 3865 | 4321 | 4734 |
| 8 | 3816 | 4674 | 5397 | 6034 | 6610 |
| 9 | 5123 | 6274 | 7245 | 8100 | 8873 |
| 10 | 6667 | 8165 | 9428 | 10541 | 11547 |
| 12 | 10516 | 12880 | 14872 | 166\%8 | 18215 |

Where there is apt to be trouble from frost no pipe less than $3 / 4$ inch should be used, and in extremely cold climates the smallest size should not be less than one inch.

To provide for the resistance due to bends, one rule is to allow a pressure of 0.204 inch of water column for each right angled elbow.

## Services for Burners.

The following table is the standard of the principal gas works. It governs the size of pipe used by gas fitters for consumers, and will be found of value. Every service should have a T so placed as to permit of easily clearing the service pipe should any obstruction occur in it.

| Size <br> of Pipe. | Threads <br> per Inch. | Weight <br> per Foot. | Length <br> allowed. | Number of <br> Burners. |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  | Feet. |  |
|  | 27 | .243 | 2 | 1 |
| $1 / 4$ | 18 | .422 | 6 | 1 |
| $3 / 8$ | 14 | .561 | 20 | 3 |
| $1 / 2$ | 14 | .845 | 30 | 6 |
| $1 / 4$ | $111 / 2$ | 1.126 | 50 | 20 |
| 11 | $111 / 2$ | 1.670 | 70 | 35 |
| $11 / 4$ | $111 / 2$ | 2.258 | 100 | 60 |
| $11 / 2$ | $111 / 2$ | 2.694 | 150 | 100 |
| 2 | 8 | 3.367 | 200 | 200 |
| $21 / 2$ | 8 | 5.773 | 300 | 300 |
| 3 | 8 | 7.547 | 450 | 450 |
| 4 | 8 | 10.728 | 600 | 750 |

## TABLE OF AQUEOUS VAPOR

Contained in 1000 Cubic Feet of Gas at Indicated Temperature.

| Temp. <br> Degres | Volume, <br> Aqueous <br> Vapor. | Temp <br> Degrees | Volume, <br> Aqueous <br> Vapor. | Temp. <br> Degrees | Volume, <br> Aqueous <br> Vapor. |
| :---: | ---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
| 40 | 9.33 | 54 | 15.33 | 68 | 24.06 |
| 41 | 9.73 | 55 | 15.86 | 69 | 24.83 |
| 42 | 10.13 | 56 | 16.40 | 70 | 25.66 |
| 43 | 10.53 | 57 | 16.93 | 71 | 26.53 |
| 44 | 10.93 | 58 | 17.53 | 72 | 27.40 |
| 45 | 11.33 | 59 | 18.10 | 73 | 28.30 |
| 46 | 11.73 | 60 | 18.66 | 74 | 29.23 |
| 47 | 12.13 | 61 | 19.23 | 75 | 30.20 |
| 48 | 12.53 | 62 | 19.80 | 76 | 31.20 |
| 49 | 12.93 | 63 | 20.50 | 77 | 32.20 |
| 50 | 13.33 | 64 | 21.20 | 78 | 33.23 |
| 51 | 13.80 | 65 | 21.90 | 79 | 34.23 |
| 52 | 14.26 | 66 | 22.60 | 80 | 35.33 |
| 53 | 14.80 | 67 | 23.30 | 81 | 36.43 |

## TABLE OF THE WEIGHTS OF GAS－HOLDERS．

In Pounds for every One－tenth of an Inch maximum
Pressure，and for Diameter from 20 to 200 Feet．

|  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 20 | 164 | 53 | 1149 | 86 | 3026 | 119 | 5793 |
| 21 | 181 | 54 | 1193 | 87 | 3097 | 120 | 5891 |
| 22 | 198 | 55 | 1238 | 88 | 3168 | 121 | 5990 |
| 23 | 217 | 56 | 1283 | 89 | 3241 | 122 | 6089 |
| 24 | 236 | 57 | 1329 | 90 | 3314 | 123 | 6189 |
| 25 | 256 | 58 | 1376 | 91 | 3388 | 124 | 6290 |
| 26 | 277 | 59 | 1424 | 92 | 3463 | 125 | 6392 |
| 27 | 298 | 60 | 1473 | 93 | 3538 | 126 | 6495 |
| 28 | 321 | 61 | 1522 | 94 | 3615 | 127 | 6598 |
| 29 | 344 | 62 | 1573 | 95 | 3692 | 128 | 6703 |
| 30 | 368 | 63 | 1624 | 96 | 3770 | 129 | 6808 |
| 31 | 393 | 64 | 1676 | 97 | 3849 | 130 | 6914 |
| 32 | 419 | 65 | 1729 | 98 | 3929 | 131 | 7021 |
| 33 | 446 | 66 | 1782 | 99 | 4010 | 132 | 7128 |
| 34 | 473 | 67 | 1837 | 100 | 4091 | 133 | 7237 |
| 35 | 501 | 68 | 1892 | 101 | 4173 | 134 | 7346 |
| 36 | 530 | 69 | 1948 | 102 | 4256 | 135 | 7456 |
| 37 | 560 | 70 | 2005 | 103 | 4340 | 136 | 7567 |
| 38 | 591 | 71 | 2062 | 104 | 4425 | 137 | 7678 |
| 39 | 622 | 72 | 2121 | 105 | 4510 | 138 | 7791 |
| 40 | 655 | 73 | 2180 | 106 | 4597 | 139 | 7904 |
| 41 | 688 | 74 | 2240 | 107 | 4684 | 140 | 8018 |
| 42 | 723 | 75 | 2301 | 108 | 4772 | 141 | 8133 |
| 43 | 757 | 76 | 2363 | 109 | 4861 | 142 | 8249 |
| 44 | 792 | 77 | 2426 | 110 | 4950 | 143 | 8366 |
| 45 | 828 | 78 | 2489 | 111 | 5041. | 144 | 8483 |
| 46 | 866 | 79 | 2553 | 112 | 5132 | 145 | 8601 |
| 47 | 904 | 80 | 2618 | 113 | 5224 | 146 | 8720 |
| 48 | 943 | 81 | 2684 | 114 | 5317 | 147 | 8840 |
| 49 | 982 | 82 | 2751 | 115 | 5410 | 148 | 8961 |
| 50 | 1023 | 83 | 2818 | 116 | 5505 | 149 | 9083 |
| 51 | 1064 | 84 | 2887 | 117 | 5600 | 150 | 9205 |
| 52 | 1106 | 85 | 2956 | 118 | 5696 | 200 | 16364 |

Example.-Find the weight of a gas-holder 80 feet in diameter, the maximum pressure being 3.2 inches water column, or $32 / 10$ ths.

In preceding table, opposite 80 in column of diameters read 2618 , the weight for $1 / 10$ th inch pressure. Therefore the weight required $=2618 \times 32=83,7761 \mathrm{bs}$.

IRON AND STEEL.

## IRON AND ST'EEL.

Wrought Iron is the product of the puddling process. It is made in a reverberatory furnace by melting pig iron on a hearth of iron oxide, over which passes a reducing flame which causes the carbon to unite with the oxide during the mixing which the puddler gives it, and further causes a large portion of the impurities to enter the surrounding slag. As the impurities-carbon, manganese, phosphorus, sulphur, silicon-leave the molten iron, the melting point rises so that the iron becomes first viscous, then pasty. When it has been worked into a ball the puddler carries it, still at a welding heat, to the hammer or squeezer where the greater part of the slag which permeated it is expelled from the mass. The roughly shapen slab is then rolled into muck bar, which, when piled, rolled and re-rolled becomes the wrought iron of commerce.

Steel is the malleable product of either the cementation process, the crucible, the converter or the open hearth furnace.

Cementation is the earliest process that we know of for making steel, and was founded upon the fact that wrought iron if packed in charcoal and heated to a high temperature, while excluded from air, absorbs carbon. The process consisted in packing bars of wrought iron, of about $3 / 4$ inch thickness, in charcoal, and then sealing up the vessel and keeping it at a yellow heat until the carbon had penetrated to the centres of the bars and converted them into steel. The carbon penetrates the bar at the rate of about $1 / 8$ inch in 24 hours, and while the point of saturation of iron by carbon is about $1.50 \%$, yet the average content of carbon by this process in the finished bars, is about $1 \%$ or lower.

The use of steel made by this process was always limited because of the fact that it contained the old seams and slag imarks which everywhere crossed and
recrossed the iron, causing great trouble in the manufacture of cutting tools. But by melting this steel (called also blister steel, because its surface was covered with blisters) in a covered crucible, the seams and fibres of slag all disappeared, and a homogeneous ingot was the result. But this was a long way to a steel ingot, and the pursuit of cheapness gave rise to the direct method of melting iron in a crucible, made for the purpose, together with the requisite carbon and other ingredients necessary for imparting hardness, toughness, etc. The molten iron absorbs the carbon very quickly and gives a product which approaches closely the merit of that produced by the older method.

Up to the middle of the nineteenth century these two processes were the principal ones, yet they were too expensive for a product of general use, except for tools.

About 1856, Sir Henry Bessemer completed his experiments and gave to the world his famous process. In this process the pig iron is melted and poured into a bottle shaped vessel. Air is then blown into it from the bottom, burning out, first the silicon, then the manganese and carbon, (the first two elements entering the slag, the last one going out of the mouth of the converter as gas) but not reducing either the phosphorus or sulphur. When the carbon is burned out-a fact recognized by the color of the flame-the vessel contains practically pure wrought iron, which becomes steel on the addition of sufficient carbon and manganese to give the requisite hardness and toughness to the cast.

When the iron is melted in a Converter which has a silicon lining the process is called the Acid Bessemer, and the principal fuel to keep the bath liquid is silicon. If the iron is high in phosphorus and melted in a vessel lined with dolomite or magnesite the process is called the Basic Bessemer and phosphorus is the principal element of fuel.

Following the introduction of Sir Henry Bessemer's process, William Siemans invented the regenerative
furnace, a furnace in which the heat of the waste gases passes through chambers checkered off with fire brick, which so obstruct the passage of the gases to the chimney as to make them give up their heat. The air and fuel gas entering the furnace is then passed through this hot checker work and highly heated, thus returning to the furnace a large part of the heat carried out before by the gases passing to the stack. In a furnace of similar construction Open Hearth Steel is made. Pig iron, steel scrap, wrought iron, and iron ore charged together, or separately, (all, one or any two of them) are rendered steel by burning out their impurities with an oxidizing flame. If the metal is melted on a hearth lined with sand, the carbon, manganese and silicon are burned out and the sulphur and phosphorus remain as before. This is the Acid Open Hearth Process. But if, on the other hand, the bottom is made of dolomite or magnesite, and lime is added to hold the phosphorus in the slag formed (as in the case of Basic Bessemer) the phosphorus, silicon, carbon and manganese are burned out, and sulphur remains as before. This is the Basic Open Hearth process.

We have, then, steel made by the following processes:
1st. Cementation.
2d. Crucible.
3rd. Bessemer, $\left\{\begin{array}{l}\text { Acid } \\ \text { Basic }\end{array}\right\}$ Converter.
4th. Open Hearth, $\left\{\begin{array}{c}\text { Acid } \\ \text { Basic }\end{array}\right\}$ Furnace.

Standard Specifications for Special Open-Hearth Plate and Rivet Steel, as adopted by the Association of American Steel Manufacturers.

Testing and Inspection (1). All tests and inspections shall be made at place of manufacture prior to shipment.

Test Pieces (2). The tensile strength, limit of elasticity and ductility, shall be determined from a standard test
piece cut from the finished material. The standard shape of the test piece for sheared plates shall be as shown by the following sketch :


Piece to be of same thickness as the plate.

On tests cut from other material the test piece may be either the same as for plates, or it may be planed or turned parallel throughout its entire length. The elongation shall be measured on an original length of 8 inches, except when the thickness of the finished material is $5-16$ inch or less, in which case the elongation shall be measured in a length equal to sixteen times the thickness; and except in rounds of $5 / 8$ inch or less in diameter, in which case the elongation shall be measured in a length equal to eight times the diameter of section tested. Four test pieces shall be taken from each melt of finished material ; two for tension and two for bending.

Annealed Test Pieces (3). Material which is to be used without annealing or further treatment is to be tested in the condition in which it comes from the rolls. When material is to be annealed or otherwise treated before use, the specimen representing such material is to be similarly treated before testing.

Marking (4). Every finished piece of steel shall be stamped with the melt number. Rivet steel may be shipped in bundles securely wired together, with the melt number on a metal tag attached.

Finish (5). All plates shall be free from surface defects and have a workmanlike finish.

Chemical Properties (6).
\(\left.\left.$$
\begin{array}{llll}\text { Extra soft and } \\
\text { Fire Box Steel. }\end{array}
$$\right\} \begin{array}{lll}Maximum \& Phosphorous, \& .04 \% <br>

Flange or boiler\end{array}\right\} \quad\)| Sulphur. |
| :--- | :--- |, $.04 \%$

Physical Properties (7). Steel shall be of four gradesExtra Soft, Fire Box, Flange or Boiler, and Boiler Rivet Steel.

Extra Soft Steel (8). Ultimate strength, 45,000 to 55,000 pounds per square inch.

Elastic limit, not less than one-half the ultimate strength. Elongation, 28 per cent.

Cold and Quench bends, 180 degrees flat on itself, without fracture on outside of bent portion.

Fire Box Steel (9). Ultimate strength, 52,000 to 62,000 pounds per square inch.

Elastic limit, not less than one-half the ultimate strength. Elongation 26 per cent.

Cold and Quench bends, 180 degrees, flat on itself, without fracture on outside of bent portion.

Flange or Boiler Steel (10). Ultimate strength, 52,000 to 62,000 pounds per square inch.

Elastic Wimit, not less than one-half the ultimate strength. Elongation, 25 per cent.

Cold and Quench bends, 180 degrees flat on itself, without fracture on outside of bent portion.

Boiler Rivet Steel (11). Steel for boiler rivets shall be made of the extra soft quality specified in paragraph No. 8.

Variation When Ordered to Gauge (12). For all plates ordered to gauge, there will be permitted an average excess of weight over that corresponding to the dimensions on the order equal in amount to that specified in the following table, provided no plate shall be rejected for light gauge measuring $.01^{\prime \prime}$ or less, below the ordered thickness.

## Table of Allowances for Overweight for Rectangular Plates 1/4 Inch Thick and Heavier.

Note.-The weight of 1 cubic inch of rolled steel is taken at 0.2833 pounds.

| Thickness of Plate. | Width of Plate. |  |  |
| :---: | :---: | :---: | :---: |
|  | Up to 75 in . | 75 in . to 100 in . | Over 100 in. |
| $1_{6} / 1.10$. | ${ }_{8} 10$ per cent. | 14 per cent. | 18 per cent. |
|  |  | $\begin{array}{ll} 12 & " ، \\ 10 & " 4 \end{array}$ | $\begin{array}{ll} 16^{\circ} \\ 13 & " ، \end{array}$ |
|  | 6 ، | 8 " | 10 " |
| 1/2 | 5 | $7{ }^{7}$ | 9 " |
|  | 41/2 " | 61/2 " | $81 / 2$ " |
|  |  | $6^{6}$ " |  |
| Over 5/8"... | $31 / 2$ | 5 " | $61 / 2$ " |

Table of Allowances for Overweight for Rectangular Plates less than 1/4 Inch in Thickness.

| Thickness of Plate. | Width of Plate. |  |
| :---: | :---: | :---: |
|  | Up to 50 in . | 50 in . and above. |
| $1 / 8 \mathrm{in}$. up to $\frac{5}{82}$ in. <br> $\begin{array}{llll}\frac{8}{82} & \text { " } & \frac{8}{16} & " \\ \frac{3}{16} & \text { " } & 1 / 4 & "\end{array}$ | $\begin{array}{cc} 10 & \text { per cent. } \\ 81 / 2 & " \\ 7 & " \\ \hline \end{array}$ | $\begin{aligned} & 15 \text { per cent. } \\ & 12 \text { " } \\ & 10 \end{aligned}$ |

Variation When Ordered to Weight (13). Plates $121 / 2 \mathrm{lbs}$. or heavier when ordered to weight, shall not average more variation than $21 / 2$ per cent., either above or below the theoretical weight.

Plates from 10 to $121 / 2$ lbs., when ordered to weight, shall not average a greater variation than the following:

Up to 75 inches wide, $21 / 2$ per cent., either above or below the theoretical weight.

75 inches and over, 5 per cent., either above or below the theoretical weight.

Plates under 10 lbs . down to 5 lbs . when ordered to weight shall not average more variation than 3 per cent. above or 5 per cent. below the theoretical weight.

Plates under 5 lbs . when ordered to weight shall not average more variation than 5 per cent. either above or below the theoretical weight.
TABLE OF STRENGTH OF MATERIALS IN POUNDS PER SQUARE INCH.

| Tensile Strength. |  | Compressive Strength. |  | Shearing Strength. | Modulus of Elasticity. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Elastic Limit. | Ultimate. | Elastic Limit. | Ulitimate. | Ultimate. | Tension. | Shear. |
| 36,000 | 56,000 | 34,000 | . | 43,000 | 30,000,000 | 9,000,000 |
| 42,000 | 68,000 | 39,000 | ....... | 48.000 | " | , ${ }^{6}$ |
| 47,000 | 68,000 | 43,000 | . . . . . | 53,000 | 4 | 4 |
| 48,000 | 80,000 | 46,000 | . . . . . . | 57,000 | 6 | 46 |
| 53,000 | 89,000 | 53,000 | ....... | 60,000 | 4 | " |
| 63,000 | 103,000 | 63,000 | . | 68,000 | " | ${ }^{4}$ |
| 80,000 | 120,000 | 80,000 |  | , | 30,000,000 | 12,000.000 |
| 190,000 | 80,000 | . |  | ...... | 36,000,000 | 14,000,000 |
| . | 80,000 | ...... | . . . . . | . | . .......... | ........... |
| ...... | 250,000 60,000 | . ..... | ....... | ...... | . . . ....... | . |
| ....... | 60,000 80,000 | . . . . . . . | ....... | ......... | . . . . . . . . . . | -.......... |
| 28,000 | 56,000 | . | . . . . . | 40,000 | 28,000,000 | $9,000,000$ |
| 24,000 | 45,000 |  |  | 32,000 |  |  |
| ...... | 15,000 | . | 70,000 | 13,000 | 15,000,000 | 5,000,000 |
| 0 | 25,000 | -. ... | 110,000 | 20,000 | 20,000,000 | 8,000,000 |
| 15,000 | 25,000 | ..... | . . . . . . | -...... | . .......... | . . . . . . . . |
| 22,000 | 35,000 | ....... | . . . . . . |  | ....... | . |
| ...... | 18,000 | ..... | . . . . . ${ }^{\text {a }}$ | ....... | . . . . . . . . | . . . . . . . . |
|  | 48,000 | .... | . . . . . . | ..... |  | . . . ....... |
| 17,000 | 36,000 | . . . | . ....... | . . . . . | 12,000,000 | .......... |
| 51,000 | 74,000 | ,000 | . . . . . . | . . . . . | 13,000,000 | , |
| 5,500 | 20.000 | 4,000 | . . . . . . | ...... | 15,000,000 | 5,000,000 |
| ...... | 30,000 | ...... |  |  | 16,000,000 | - |
|  | 58000 | ...... |  |  | 17,000,000 |  |
| 20,000 | 58,000 | . . . . . |  | 43,000 | 14,000,000 | 5,000,000 |
| ...... | 82,000 65,000 | ...... | ....... | . . . . . | . . . . . . . . | . . . . . . . . |
| 30,000 | 65,000 60,000 | ...... | 125,000 | ...... | . | . |
| 80,000 | 100.000 | .. . . . | 120,000 | . . . . . | . . . . . . . . |  |

MATER1AL.

Steel, Bessemer and open


|  $0^{\circ} 0^{\circ} 0^{\circ}$ |
| :---: |
| uoqrej јо 'ұиәง 1әd |

Steel, crucible.................. tempered
Steel, 8 to 5\% nickel..................... $\left\{\begin{array}{l}\text { from } \\ \text { to }\end{array}\right.$
Steel castings. .......................... $\left\{\begin{array}{l}\text { from } \\ \text { to }\end{array}\right.$
Wrought iron.................. $\{$ high grade
Cast iron............................... $\left\{\begin{array}{l}\text { from } \\ \text { to }\end{array}\right.$
Malleable cast iron.................. $\left\{\begin{array}{l}\text { from } \\ \text { to }\end{array}\right.$ on
$\underbrace{\text { an }}$ Delta metal.......................... $\left\{\begin{array}{l}\text { castings } \\ \text { rolled }\end{array}\right.$ (castings Copper........................ $\left\{\begin{array}{l}\text { called plates } \\ \text { roll drawn } \\ \text { hard }\end{array}\right.$
 Aluminum bronze....... $\left\{\begin{array}{lll}0.1 & \text { al., } & 0.9 \\ 0.07 & \text { c. } & 0.93\end{array}\right.$ Manganese bronze.

## TENACITY OF METALS AT VARIOUS

## TEMPERATURES.

Tensile Strength of Iron and Steel at High Temperatures.James E. Howard's tests (Iron Age, April 10, 1890), shows that the tensile strength of steel diminishes as the temperature increases from $0^{\circ}$ until a minimum is reached between $200^{\circ}$ and $300^{\circ} \mathrm{F}$., the total decrease being about $4,000 \mathrm{lbs}$. per square inch in the softer steels and from 6,000 to $8,000 \mathrm{lbs}$. in steels of over $80,000 \mathrm{lbs}$. tensile strength. From this minimum point the strength increases up to a temperature of $400^{\circ}$ to $650^{\circ} \mathrm{F}$., the maximum being reached earlier in the harder steels, the increase amounting to from 10,000 to $20,000 \mathrm{lbs}$. per square inch above the minimum strength at from $200^{\circ}$ to $300^{\circ}$. From this maximum, the strength of all the steels decreases steadily at a rate approximating $10,000 \mathrm{lbs}$. decrease per $100^{\circ}$ increase of temperature. A strength of $20,000 \mathrm{lbs}$. per square inch is still shown by 0.10 C . steel at about 1000 F ., and by 0.60 to 1.00 C . steel at about $1600^{\circ} \mathrm{F}$.

The strength of wrought iron increases with temperature from $0^{\circ}$ up to a maximum at from 400 to $600^{\circ} \mathrm{F}$., the increase being from 8,000 to $10,000 \mathrm{lbs}$. per square inch, and then decreases steadily till a strength of only 6,000 lbs. per square inch is shown at $1,500^{\circ} \mathrm{F}$.

Cast iron appears to maintain its strength, with a tendency to increase, until $900^{\circ}$ is reached, beyond which temperature the strength gradually diminishes. Under the highest temperatures, $1,500^{\circ}$ to $1,600^{\circ} \mathrm{F}$., numerous cracks on the cylindrical surface of the specimen were developed prior to rupture. It is remarkable that cast iron, so much inferior in strength to the steels at atmospheric temperature, under the highest temperatures has nearly the same strength the high-temper steels then have.

Strength of Iron and Steel Boiler-plate at High Temperatures. (Chas. Huston, Jour. F. I., 1877.)

Average of Three Tests of Each.

| Temperature F ........................ |  | ${ }_{5750}{ }^{5750}$ | ${ }^{925} 5^{\circ}$ |
| :---: | :---: | :---: | :---: |
| Charcoal iron plate, ${ }_{\text {/4 }}$ tensile strength, libs.. | $\underset{26}{55,366}$ | $\begin{gathered} 63,080 \\ 23 \end{gathered}$ | 65,343 21 |
| Soft open-hearth steel, tensile strength, ib . ${ }^{\text {a }}$. | 54,600 | 66,083 | 64,350 |
| "\% "\% ${ }^{\text {a }}$ " contr. \%........... | 47 |  | 33 |
| " Crucible steel, tensile strength, ibs... | 64,000 36 | 69,266 30 | 68,600 |

## Strength of Wrought Iron and Steel at High Temperatures.

 -(Jour. F. I., cxii., 1881, p. 241.) Kollmann's experiments at Oberhausen included tests of the tensile strength of iron and steel at temperatures ranging between $70^{\circ}$ and $2000^{\circ} \mathrm{F}$. Three kinds of metal were tested, viz., fibrous iron having an ultimate tensile strength of $52,464 \mathrm{lbs}$., an elastic strength of $38,280 \mathrm{lbs}$., and an elongation of $17.5 \%$; fine-grained iron having for the same elements values of $56,892 \mathrm{lbs}$., $39,113 \mathrm{lbs}$, and $20 \%$; and Bessemer steel having values of $84,826 \mathrm{lbs} ., 55,029 \mathrm{lbs}$., and $14.5 \%$. The mean ultimate tensile strength of each material expressed in per cent. of that at ordinary atmospheric temperature is given in the following table, the fifth column of which exhibits, for purposes of comparison, the results of experiments carried on by a committee of the Franklin Institute in the years 1832-36.| Temperature Degrees F. | Fibrous Wrought Iron, p. c. | Fine-grained Iron, per cent. | Bessemer Steel, per cent. | Franklin Institute, per cent. |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 100.0 | 100.0 | 100.0 | 96.0 |
| 100 | 100.0 | 100.0 | 100.0 | 102.0 |
| 200 | 100.0 | 100.0 | 100.0 | 105.0 |
| 300 | 97.0 | 100.0 | 100.0 | 106.0 |
| 400 | 95.5 | 100.0 | 100.0 | 106.0 |
| 500 | 92.5 | 98.5 | 98.5 | 104.0 |
| 600 | 88.5 | 95.5 | 92.0 | 99.5 |
| 700 | 81.5 | 90.0 | 68.0 | 92.5 |
| 800 | 67.5 | 77.5 | 44.0 | 75.5 |
| 900 | 44.5 | 51.5 | 36.5 | 53.5 |
| 1000 | 26.0 | 36.0 | 31.0 | 36.0 |
| 1100 | 20.0 | 30.5 | 26.5 | ..... |
| 1200 | 18.0 | 28.0 | 22.0 | ..... |
| 1300 | 16.5 | 23.0 | 18.0 | . .... |
| 1400 | 13.5 | 19.0 | 15.0 | ..... |
| 1500 | 10.0 | 15.5 | 12.0 | ..... |
| 1600 | 7.0 | 12.5 | 10.0 | . . |
| 1700 | 5.5 | 10.5 | 8.5 | ..... |
| 1800 | 4.5 | 8.5 | 7.5 | .... |
| 1900 | 3.5 | 7.0 | 6.5 | .... |
| 2000 | 3.5 | 5.0 | 5.0 | ..... |

## MECHANICS OF MATERIALS RELATING TO

## TUBULAR CONSTRUCTION.

## STRENGTH OF MATERIALS.

A tensile stress is produced in the walls of a cylindrical vessel, such as a pipe, tank, boiler, etc. when it contains a fluid such as water, steam or air, under pressure.

The ultimate or breaking strength of a material is reached when the tensile stress equals its cohesive force, in which case the material is on the point of being ruptured.

The working strength of a material is that fraction, or portion, of the ultimate or breaking strength that experience has shown it is best to use in practice, in order to guard against failure due to unforeseen causes, such as defects and the possible action of unknown forces.

The unit working strength of a material is the working strength of one square inch of cross section of that material.

The factor of safety is the factor or number by which the ultimate strength is divided in order to obtain the working strength. The proper factor to use in any given case would depend upon the characteristics of the material and the nature of the forces, whether quiescent or impulsive.

In tubular construction, reasonably free from vibration and shock, a factor of safety of from 5 to 6 should be ordinarily used for wrought iron and steel, and from 8 to 10 for cast iron. Where there is uncertainty as to the magnitude and nature of the forces acting, or where there is much vibration or shock, such as water hammer in steam pipes or the sudden stoppage of flow in a water pipe, these factors should be increased to from one and one-half to three or more times the values given, depending upon the severity of the vibration or shock.

It is best, when possible, to compute the straining actions of shocks, as for example the increase in fluid pressure in a long water pipe when the flow is more or less quickly checked, in which case they should be added to the normal straining action. Having provided for these abnormal forces, the ordinary factors of safety should then be used.

Stress and Strain.-Should the fluid pressure in a cylindrical vessel be gradually increased from zero, it will be
observed that the walls of the vessel will stretch, thus increasing its volume. The stretch of the material constituting the walls is termed the strain due to the force tending to tear the material asunder.

The molecular actions within the material which oppose the external forces, and which resist deformation, are termed stresses.

An elastic material when deformed by a straining action recovers its original form when the straining action is removed; as, for example, spring steel, ivory, etc.

A plastic material when deformed does not recover its original form when the straining action is removed; as, for example, lead, putty, etc.

Elastic limit.-Materials such as wrought iron and low carbon steel are elastic under some conditions and plastic under others. At ordinary atmospheric temperatures, these materials may be strained up to a point, termed the elastic limit, without suffering any permanent deformation when the straining action is removed.

Should, however, the elastic limit be exceeded, the material will but partially recover its original form when the straining action is removed, in which case it is said to have received a permanent deformation or set.

Up to the elastic limit the strain is proportional to the stress, that is, strain $\div$ stress $=$ a constant. Beyond the elastic limit this constant becomes ordinarily an increasing varible.

The modulus of elasticity of a material is obtained by dividing the unit stress by the strain, for unit length.

Shearing strength of a material.-When a cylindrical vessel, made up from plates, connected together in the usual manner by riveted joints, is subjected to a fluid pressure, the adjoining plates will tend to separate by sliding one upon the other, thus subjecting the material of the rivets to a shearing action. The ability of a rivet to resist this action is known as its shearing strength, and the stress created by snch action is called the shearing stress.

Unit shearing strength of a material is the shearing strength of one square inch of cross-section of that material.

VALUES OF I (Moment of Inertia), AND S. (Section Modulus), FOR USUAL SECTIONS.

| sections. | I |
| :---: | :---: |

$\mathrm{x} \times$ Denotes position of neutral axis.

## Bending Moments and Defiections of Beams under Various Systems of Loading.

$W=$ total load.
$l=$ length of beam.
(1) Beam fixed at one end and loaded at the other.


Maximum bending moment at point of support $=W l$.
Maximum shear at point of support $=W$.
Deflection $=\frac{W l^{3}}{3 E I}$
(3) Beam supported at both ends, single load in the middle


Maximum bending moment at middle of beam $=\frac{W l}{4}$
Maximum shear at points of support $=1 / 2 / W$.
Deflection $=\frac{W l^{3}}{48 E I}$
(5) Beams supported at both ends, single unsymmetrical load.


Maximum bending moment under load $=\frac{W a b}{l}$
Maximum shear : at support near $a=\frac{W b}{l}$; at other support $=\frac{W a}{l}$
Maximum deflection

$$
=\frac{W a b(2 l-a)}{9 E I l} \sqrt{1 / 3 a(2 l-a)}
$$

$I=$ moment of inertia $E=$ modulus of elasticity.
(2) Beam fixed at one end, and uniformly loaded.


Maximum bending moment at point of support $=\frac{W l}{2}$
Maximum shear at point of support $=W$.
Deflection $=\frac{W l^{3}}{8 E I}$
(4) Beam supported at both ends and uniformly loaded.


Maximum bending moment at middle of beam $=\frac{W l}{8}$
Maximum shear at points of support $=1 / 2 W_{W l^{3}}$
Deflection $=\frac{W}{76.8 E I}$
(6) Beam fixed at both ends and uniformly loaded.


Maximum bending moment at point of support $=\frac{W l}{12}$

Maximum shear at points of support $=1 / 2 W$.
Deflection $=\frac{W l^{3}}{384 E I}$

## DEFLECTION AND STRENGTH OF PIPES TO RESIST BENDING ACTION.



The bending moment of a force is obtained by multiplying the force, $P$, in pounds, by the lever arm, $l$, in inches, with which it acts. Thus in the case of a trolley pole the bending moment at the ground, G , is

$$
\mathrm{M}=\mathrm{P} 1, \text { and at } \mathrm{G}_{1} \text { is } \mathrm{M}_{1}=\mathrm{Pl}_{1}
$$

The deflection of a pipe or tube when loaded transversely, that is, so as to subject it to a bending moment, is the deformation in inches produced by the given loading, and is due, of course, to the elasticity of the materials constituting it. In case of a trolley pole the greatest deformation will be at the extreme top of the pole.

For a horizontal pipe supported at equidistant points the greatest deflection will be midway between supports.

The moment of inertia of a section is the sum of the products of each elementary area of the section by the square of its distance from an assumed axis of rotation. It is a necessary factor in formulæ for the determination of deflection of structures considered as beams.

The moment of resistance of cross-section of a beam is the moment that resists a bending action at that crosssection.

The section modulus is the factor that when multiplied by the unit working strength of the material will give the moment of resistance of cross-section of a structure considered as a beam.

In every case when a beam, as for example a trolley pole or a horizontal pipe supported at points, is subjected to a bending action the following condition must exist at every cross-section, namely: Bending moment $=$ moment
of resistance of cross-section=unit working strength of material $\times$ section modulus.


Example 1.-A 4 inch steel pipe has one end firmly fixed in a wall so as to project horizontally a distance of 8 feet. Find the greatest safe load it will carry at the free end, also the deflection with this load.
Solution: From the table of Standard Steam and Gas Pipe, we see that the outside and inside diameters are $\mathrm{d}=4.500$ and $\mathrm{d}_{1}=4.026$ inch. Assuming an ultimate strength of material $=60,000 \mathrm{lbs}$. per sq. inch, and a factor of safety of 6 , we get as a working unit strength $60,000 \div 6=10,000 \mathrm{lbs}$. From the table of Section Moduli we get

$$
\text { Section modulus }=0.098\left(\mathrm{~d}^{3}-\frac{\mathrm{d}_{1}^{4}}{\mathrm{~d}}\right)
$$

which multiplied by the unit working strength gives

$$
\text { Moment of resistance }=980\left(d^{3}-\frac{d_{1}^{4}}{d}\right)
$$

$$
\mathrm{d}^{3}=(4.5)^{3}=91.125 \text { (see table of cubes). }
$$

$\log \cdot \frac{d_{1}{ }^{4}}{d}=\log \cdot \frac{(4.026)^{4}}{4.5}=4 \log \cdot 4.026-\log .4 .5=4 \times 0.60$
$-0.6532=1.7664$, or $\frac{d_{1}^{4}}{d}=58.4$, the number whose log. is 1.7664
Then moment of resistance $=980(91.1-58.4)=32,046$ inch 1bs.

The bending moment at support $=\mathrm{WL}=\mathrm{W} 8 \times 12=$ 96 W inch lbs. Since the bending moment equals the moment of resistance, then

$$
\begin{aligned}
96 \mathrm{~W} & =32,046, \text { or } \\
\mathrm{W} & =333 \mathrm{lbs} . \text {, the required load. }
\end{aligned}
$$

For this style of loading (see table) the

$$
\text { Deflection }=\frac{W 1^{3}}{3 \mathrm{EI}}
$$

In which $W=333$, the safe load as computed;

$$
\begin{aligned}
& L_{1}=96, \text { the length of beam in inches; } \\
& E=26,000,000 . \text { the modulus of elasticity; } \\
& I=0.049\left(d^{4}-d_{1}^{4}\right)=0.049\left[\left(4.5^{4}-(4.026)^{4}\right]=\right.
\end{aligned}
$$

7.21, the moment of inerta of cross-section.

Substituting these values in above formula we get

$$
\text { Deflection }=\frac{333 \times(96)^{3}}{3 \times 26,000,00 \times 7.21}=0.53 \text { inch }
$$

Example 2.-A 10 inch standard lap welded steel pipe, carrying water, is suspended from the top of a tunnel, as shown in the figure, the points of support being spaced at a distance of 20 feet apart.

Find the deflection, D, due to the weight of the pipe and its contained water, on the supposition that the pipe bears equally on all of its supports.

Solution: From the table of Standard Steel Welded Pipe we get weight of pipe per $\mathrm{ft} .=40.06 \mathrm{lbs}$., and weight of contained water per $\mathrm{ft} .=34.13 \mathrm{lbs}$., making a gross weight per foot of 74.2 lbs ., or for 20 feet a total weight of approximately 1500 pounds.

Since the pipe is assumed to run continuously from one support to another, the deflection will be greatest midway between supports, and will be the same as that for a beam
fixed at both ends and uniformly loaded. For this style of loading (see page 212) the

$$
\text { Deflection }=\frac{\mathrm{W} 1^{3}}{384 \mathrm{EI}}
$$

In which $W=1500$ pounds;

$$
L_{1}=20 \times 12=240 \text { inches; }
$$

$E=26,000,000$, the modulus of elasticity;
$\mathrm{I}=0.049\left(\mathrm{~d}^{4}-\mathrm{d}_{1}{ }^{4}\right)=0.049\left[(10.75)^{4}-(10.02)^{4}\right]$
$=160$, the moment of inertia of cross-section.
Substituting these values in above formula we get

$$
\text { Deflection }=\frac{1500 \times(240)^{3}}{384 \times 26,000,000 \times 160}=0.014 \text { inch. }
$$

In practice, where the usual rigid joints are used, it is often the case that a pipe does not bear equally upon all the hangers, and in cases of careless erecting or of shifting of hangers, the pipe may not receive any support from one or more of the hangers.

Should each alternate hanger, in the above example, become inactive, owing to any cause, the maximum deflection then would be that due to an unsupported length of 40 feet of pipe. An inspection of the formula will show that the deflection of a beam increases directly as the weight $\times(\text { length })^{3}$, or, for uniformly loaded beams, since the weight increases directly as the length, as the (length) ${ }^{4}$.

Since in this case the length is doubled, the deflection will be increased 16 fold (that is $2^{4}$ ), or to an amount $=$ $0.014 \times 16=0.22$ inch.

In the same manner it can be shown that an unsupported portion of 60 feet in length will deflect or sag an amount $=0.014 \times 3^{4}=1.13 \mathrm{inch}$.


Should the pipe be merely supported at the ends, and not straight and continuous from one support to another, then the conditions would be those of a simple beam uniformly loaded and supported at the ends.

By comparing the deflection formulæ for the case just considered and this case, it will appear that the deflection for this case will be five times as great; or, for the three cases considered above, $0.07,1.10$ and 5.65 inches respectively.

The maximum deflection, or sag, that should be permitted in practice will depend ordinarily upon the effective thickness of wall of pipe and the unit working strength of the material composing it.

The effective thickness of pipe in any particular case will be the thickness remaining after deducting the depth of screw-thread (for wrought pipe with threaded ends for coupling or flange connections) plus a reasonable amount for the deterioration due to corrosion, or other causes; which amount will depend upon the nature of the service and the expected life of pipe.

In every practical example the effective thickness of pipe should be used in applying all formulæ relating to strength of pipe to resist either bending or bursting.

## STRESS DUE TO INTERNAL BURSTING PRESSURE.

Owing to the difference in the nature of the stress occuring in thin and thick walls of cylinders, pipes, etc., when subjected to a fluid pressure, it will be necessary to divide them into two classes, namely, those having thin walls and those having thick walls. In the following discussion only those having thin walls will be considered.

Let $d=$ internal diameter in inches ;
$\mathrm{t}=$ thickness of cylinder wall in inches ;
$\mathrm{p}=$ internal fluid pressure, 1 bs . per sq. inch ;
$\pi=3.1416$;
$\mathrm{f}_{\mathrm{t}}=$ unit working strength in tension ;
$\mathrm{f}_{\mathrm{c}}=$ " " " " compression ;
$\mathrm{f}_{\mathrm{s}}=$ " " " "shear;
$e=$ efficiency of joint, or $\frac{\text { strength of joint }}{\text { strength of plate }} ;$
$\mathrm{c}=$ thickness of metal, in inches, allowed for wasting away due to corrosion, or other causes.

## STRENGTH OF THIN CYLINDERS TO RESIST' BURSTING.



The force tending to tear the plate along a line lying circumferentially around the cylinder, as, for example, along the section lying in the plane A B, will equal the fluid pressure exerted on one end of the cylinder, which equals the area of a cross-section of cylinder in square inches $\times$ internal pressure per square inch, or
$\left.\begin{array}{l}\text { Longitudinal bursting pressure } \\ \text { tending to rupture circumferentially }\end{array}\right\}=\frac{\pi \mathrm{d}^{2}}{4} \mathrm{p}$.
This bursting pressure will be resisted by the tenacity of the metal whose cross-section lies in the plane AB, which equals the circumference, or distance around the cylinder, multiplied by the thickness of the metal. Hence
$\left.\begin{array}{l}\text { Resistance to bursting pressure } \\ \text { tending to rupture circumferentially }\end{array}\right\}=\pi \mathrm{dt} \mathrm{f}_{\mathrm{t}}$.
Since the resistance to the bursting pressure must equal the pressure itself, we have

$$
\pi d \mathrm{tf}_{\mathrm{t}} .=\frac{\pi \mathrm{d}^{2}}{4} \mathrm{p}, \text { or } \mathrm{t}=\frac{\mathrm{dp}}{4 \mathrm{f}_{\mathrm{t}}} ; \mathrm{p}=\frac{4 \mathrm{f}_{\mathrm{t}} \mathrm{t}}{\mathrm{~d}}
$$



The force tending to tear the plate along a line extending longitudinally, as, for example, along the section lying in the plane $C D$, will equal the sum of the normal components of the fluid pressures on the inner surface of the cylinder, which it can be shown is the same as the fluid pressure on a surface equal to the length of the cylinder multiplied by its diameter, or $d$. We then have
$\left.\begin{array}{l}\text { Transverse bursting pressure } \\ \text { Tending to rupture longitudinally }\end{array}\right\}=\mathrm{d} 1 \mathrm{p}$.
This bursting pressure will be resisted by the tenacity of the metal whose cross-section lies in the plane CD, which latter equals twice the length of cylinder multiplied by the thickness of the metal. Hence

$$
\left.\begin{array}{l}
\text { Resistance to bursting pressure } \\
\text { Tending to rupture longitudinally }
\end{array}\right\}=21 \mathrm{t} \mathrm{f}_{\mathrm{t}} \text {. }
$$

Since the resistance to the bursting pressure must equal the pressure itself, we have

$$
21 \mathrm{t} \mathrm{f}_{\mathrm{t}}=\mathrm{d} 1 \mathrm{p}, \text { or } \mathrm{t}=\frac{\mathrm{d} p}{2 \mathrm{f}_{\mathrm{t}}} ; \mathrm{p}=\frac{2 \mathrm{f}_{\mathrm{t}} \mathrm{t}}{\mathrm{~d}}
$$

From a comparison of the above formulæ, it will be seen that the force due to a fluid pressure within a pipe, boiler, or other cylindrical vessel, that tends to cause rupture longitudinally is twice that which tends to cause rupture transversely, that is circumferentially or around the pipe.

From the above relations, then, it will appear that a pipe, or other cylindrical vessel having walls of uniform thickness, when subjected to a fluid pressure only, will always tend to rupture longitudinally. The strength at the joints, resisting rupture transversely, may be reduced by the cutting of threads or riveting to flanges, or otherwise, to an amount equal to one-half the strength of the
metal of pipe in cross-section, without altering the tendency of the pipe to rupture longitudinally.

Example 1.-Find the safe working pressure and also the bursting pressure of a standard 10 -inch lap-welded steel pipe, having plain ends, or welded heads.

Solution: Assuming that the pipe is not subjected to shock or vibration, we will assume a unit working strength of material $=10,000 \mathrm{lbs}$., which allows a factor of safety of 6 on the assumption that the ultimate tensile strength is $60,000 \mathrm{lbs}$. per sq. inch.

Then in the formula for the internal fluid pressure.

$$
\mathrm{p}=\frac{2 \mathrm{f}_{\mathrm{t}} \mathrm{t}}{\mathrm{~d}}
$$

$f_{t}=10,000 \mathrm{lbs} .$, the unit working strength of material;
$\mathrm{t}=0.366 \mathrm{inch}$, the thickness of wall of pipe;
$d=10.385$, the diameter of pipe.
Substituting these values we get

$$
\mathrm{p}=\frac{2 \times 10,000 \times 0.366}{10.385}=705 \mathrm{lbs} . \text { per sq. in. }
$$

The bursting pressure, on the above assumption, would be six times the working pressure, or

Bursting pressure $=705 \times 6=4,230 \mathrm{lbs}$. per sq. in.
Example 2.-Find the working pressure for the pipe given in example 1, when provision is made for wasting away of the metal by corrosion, or otherwise, so as to reduce the thickness of the walls by $1 / 8$ inch.

Then $\mathrm{t}=0.366-0.125=0.241$ inch, the thickness of wall after corrosion of $1 / 8$ inch has occurred, the other values remaining the same as before. Substituting in the formula for pressure we get

$$
p=\frac{2 \times 10,000 \times 0.241}{10.385}=465 \text { lbs. per sq. in. }
$$

In practice it is often necessary to provide, especially in steam and water pipes, for stresses due to vibration, shock, temperature changes and various other causes, in which case the factor of safety of six assumed in the above examples should be increased to from 8 to 15 for
wrought pipe, depending upon the severity of these actions.

Assuming a factor of safety of 12 , the safe working pressure in the above examples would be for Example 1, 350 lbs. per sq. in., and for example 2, 230 lbs . per sq. inch.

Example 3.-Find the thickness of a mild steel seamless cylindrical receiver, 20 inches in diameter, to contain air at $2,000 \mathrm{lbs}$. per sq. in. gauge pressure.

Solution: Assuming a unit working strength of material of $12,000 \mathrm{lbs}$. then in the formula for thickness,

$$
\mathrm{t}=\frac{\mathrm{d} \mathrm{p}}{2 \mathrm{f}_{\mathrm{t}}}
$$

$\mathrm{d}=20$, the diameter of receiver in inches;
$p=2,000$, the internal pressure in lbs. per sq. inch;
$f_{t}=12,000$, the working strength per sq. in. of material;
Substituting these values in the formula we get

$$
\mathrm{t}=\frac{20 \times 2,000}{2 \times 12,000}=1.67 \text { inches }
$$

In tubular construction, having longitudinal riveted joints intended to resist internal fluid pressure, the formulæ for thickness of wall and for safe working pressure will become

$$
t=\frac{d p}{2 e f_{t}} ; \quad p=\frac{2 e f_{t} t}{d}
$$

In which $\mathrm{d}=$ diameter of vessel in inches;
$t=$ thickness of wall in inches;
$\mathrm{p}=$ internal fluid pressure, 1 bs . per sq. inch;
$f_{t}=u n i t$ working strength of material in tension;
$\mathrm{e}=$ efficiency of riveted joint, from 0.6 to 0.8 .
To provide in practice for wasting away of the metal, due to corrosion, or other causes, the above formulæ will become

$$
t=\frac{d p}{2 e f_{t}}+c ; \quad p=\frac{2 e f_{t}(t-c)}{d}
$$

Where $c=$ reduction in the thickness, in inches, of the metal constituting the wall of the vessel, because of the wasting away of the metal in practice due to corrosion and other causes.

Example 4.-Find the thickness of plate for a 60 -inch steam boiler, to carry 100 lbs . gauge pressure, the longitudinal riveted joints having an efficiency of 0.7 , the ultimate tensile strength of the material being $60,000 \mathrm{lbs}$. per sq. inch.

Solution: Assuming an actual factor of safety of five and allowing $1 / 8$ inch for wasting away of plates during the life of the boiler, we have in the above formula for thickness of plate:
$d=60$, the diameter of boiler in inches;
$p=100$, the gauge pressure per sq. inch;
$f_{t}=12,000$, the unit working strength of material;
$e=0.7$, the efficiency of longitudinal joint;
$c=0.125$, the allowance for corrosion, etc.
Substituting these values in the formula we get

$$
\mathrm{t}=\frac{60 \times 100}{2 \times 0.7 \times 12,000}+0.125=0.48 \text { inch }
$$

Example 5.-Find the greatest steam pressure that could be carried by the boiler, in Example 4, when new, that is, before any wasting away of metal has occurred, all other conditions being the same.

Solution: Making $\mathbf{c}=0$ in the above equation, we get

$$
t=\frac{d p}{2 e f_{t}} ; \text { and } p=\frac{2 e f t}{d}
$$

Which are the general equations for the thickness, $t$, in inches and safe fluid pressure, $p$, in 1 bs , per sq. inch, for pipes or other cylindrical vessels having longitudinal riveted joints.

Substituting the values, given in Example 4, in the above formula for pressure, we get

$$
\mathrm{p}=\frac{2 \times 0.7 \times 12,000 \times 0.48}{60}=135 \text { lbs. gauge. }
$$

In Examples 4 and 5 an actual factor of safety at the longitudinal joints is assumed, which makes the apparent factor of safety, that is, the factor of safety on the plate itself, for the assumed conditions, $=5 \div 0.7=7.1$.

In practice an apparent factor of safety of 5 is often used, for double riveted longitudinal lap joints, resulting in an actual factor of safety of $5 \times(0.68$ to 0.72$)=$ from 3.4 to 3.6. Very often no allowance is made for the wasting away of the metal, which fact in conjunction with the use of too small a factor of safety will account for a large number of the boiler explosions that have occurred in practice.

## STRENGTH OF CYLINDER ENDS OR HEADS.



The ends or heads of a cylindrical vessel intended to contain a fluid under pressure, should be designed so as to be as strong as the cylindrical part of the vessel. This can ordinarily be best accomplished by giving the end the form of a portion of a hollow sphere, as shown in the figure, whose radius equals the diameter of the cylindrical part, in which case to be equally strong throughout the thickness should be the same as that of the cylindrical part. This is because of the fact that for a given internal fluid pressure, the stress created in the walls of a thin hollow cylinder will be the same as that created, for the same pressure, in the walls of a thin hollow sphere of double the diameter.

The use of flat ends should be avoided, except for constructions such as tube plates, where they are desirable because of constructional reasons and can be easily stayed.
HOLLOW, CYLINDRICAL, WROUGHT IRON PILLARS.-BREAKING LOADS IN TONS.
Calculated by Gordon's Formula (Trautwine.) Thickness 1/8 Inch.


Thickness $1 / 4$ Inch.

WROUGHT IRON PILLARS, ETc.-(CONTINUED)
OUter Diameters in Inches.











Thickness 1 Inch.

SHEARING AND BEARING VALUE OF RIVETS.

SHEARING AND BEARING VALUE OF RIVETS.

| Diam. of Rivet in Inches. |  | Area. of Rivet. | $\begin{array}{\|c\|} \text { Single } \\ \text { Shear at } \\ 7,500 \mathrm{lbs} . \\ \text { per } \\ \text { sq. in. } \\ \hline \end{array}$ | Bearing Value for different Thicknesses of Plate at $15,000 \mathrm{lbs}$. per square inch ( $=$ Diameter of Rivet $\times$ Thickness of Plate $\times 15,000 \mathrm{lbs}$.) |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Fraction | Decimal |  |  | $1 / 4{ }^{\prime \prime}$ | $\frac{5}{18}^{\prime \prime}$ | $3 / 8{ }^{\prime \prime}$ | $\frac{7}{16}{ }^{\prime \prime}$ | $1 / 2^{\prime \prime}$ | $\frac{9}{18}^{\prime \prime}$ | 5/8" | $\frac{1}{1 \frac{1}{6}}{ }^{n}$ | 3/4" | $\frac{1}{1} \frac{3}{6}{ }^{\prime \prime}$ | 7/8" |
| $\begin{aligned} & 3 / 8 \\ & \frac{7}{16} \end{aligned}$ | .375 .4375 | .1104 .1503 | 828 1130 | 1410 1640 | 2050 |  |  |  |  |  |  |  |  |  |
| $1 / 2$ 16 | .5 .5625 | .1963 .2485 | 1470 1860 | 1880 2110 | 2340 2640 | 2810 3160 | 3690 |  |  |  |  |  |  |  |
| 5/8 | . 625 | . 3068 | 2300 | 2340 | 2930 | 3520 | 4100 |  |  |  |  |  |  |  |
| $\frac{11}{1} 6$ | . 6875 | . 3712 | 2780 |  | 3220 | 3870 | 4510 | 5160 |  |  |  |  |  |  |
| $3 / 4$ | . 75 | . 4418 | 3310 |  | 3520 | 4220 | 4920 | 5630 | 6330 |  |  |  |  |  |
| $\frac{1}{18}$ | . 8125 | .5185 | 3890 |  |  | 4570 | 5330 | 6090 | 6860 | 7620 |  |  |  |  |
| $7 / 8$ 15 | . 875 | . 6013 | 4510 5180 |  |  | 4920 5270 | 5740 6150 | 6560 77030 | 7380 7910 | 8200 8790 |  |  |  |  |
| $\frac{1}{1} \frac{5}{6}$ | . 9875 | . 6903 | 5180 |  |  | 5270 | 6150 | 7030 | 7910 | 8790 | 9670 |  |  |  |
|  | 1. | . 7854 | 5890 |  |  |  | 6560 | 7500 | 8440 | 9380 | $10310$ | 11250 |  |  |
| $1 \frac{1}{16}$ | 1.0625 | . 8866 | 6650 |  |  |  | 6970 | 7970 | 8960 | 9960 | 10960 | 11950 | 12950 |  |
| 11/8 | 1.125 | . 9940 | 7460 |  |  |  |  | 8440 | 9490 | $10550$ | $11600$ | $12660$ | $13710$ | $14770$ |
| $1 \frac{8}{16}$ | 1.1875 | 1.1075 | 8310 |  |  |  |  | 8910 | 10020 | 11130 | 12250 | $13360$ | $14470$ | $15590$ |

## WEIGHT OF RIVETS IN POUNDS PER 100.

 Length from under head. One cubic ft. weighing 480 lbs .| Length <br> Inches. | 3/8" | 1/2" | 5/8' Diam. | $3 / 4 \text { " }$ <br> Diam. | $7 / 8^{\prime \prime}$ <br> Diam. | $1 \prime$ Diam. | $\begin{aligned} & 11 / 8^{\prime \prime} \\ & \text { Diam. } \end{aligned}$ | $\begin{aligned} & 11 / 4^{\prime \prime} \\ & \text { Diam. } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 114 | 5.4 | 12.6 | 21.5 | 28.7 | 43.1 | 65.3 | 91.5 | 123. |
| 11/2 | 6.2 | 13.9 | 23.7 | 31.8 | 47.3 | 70.7 | 98.4 | 133. |
| 13/4 | 6.9 | 15.3 | 25.8 | 34.9 | 51.4 | 76.2 | 105. | 142. |
| 2 | 7.7 | 16.6 | 27.9 | 37.9 | 55.6 | 81.6 | 112. | 150. |
| $21 / 4$ | 8.5 | 18.0 | 30.0 | 41.0 | 59.8 | 87.1 | 119. | 159. |
| $21 / 2$ | 9.2 | 19.4 | 32.2 | 44.1 | 63.0 | 92.5 | 126. | 167. |
| $23 / 4$ | 10.0 | 20.7 | 34.3 | 47.1 | 68.1 | 98.0 | 133. | 176. |
| 3 | 10.8 | 22.1 | 36.4 | 50.2 | 72.3 | 103. | 140. | 184. |
| $31 / 4$ | 11.5 | 23.5 | 38.6 | 53.3 | 76.5 | 109. | 147. | 193. |
| 31/2 | 12.3 | 24.8 | 40.7 | 56.4 | 80.7 | 114. | 154. | 201. |
| 33/4 | 13.1 | 26.2 | 42.8 | 59.4 | 84.8 | 120. | 161. | 210. |
| 4 | 13.8 | 27.5 | 45.0 | 62.5 | 89.0 | 125. | 167. | 218. |
| $41 / 4$ | 14.6 | 28.9 | 47.1 | 65.6 | 93.2 | 131. | 174. | 227. |
| 41/2 | 15.4 | 30.3 | 49.2 | 68.6 | 97.4 | 136. | 181. | 236. |
| $43 / 4$ | 16.2 | 31.6 | 51.4 | 71.7 | 102. | 142. | 188. | 244. |
| 5 | 16.9 | 33.0 | 53.5 | 74.8 | 106. | 147. | 195. | 253. |
| 514 | 17.7 | 34.4 | 55.6 | 77.8 | 110. | 153. | 202. | 261. |
| $51 / 2$ | 18.4 | 35.7 | 57.7 | 80.9 | 114. | 158. | 209. | 270. |
| $53 / 4$ | 19.2 | 37.1 | 59.9 | 84.0 | 118. | 163. | 216. | 278. |
| 6 | 20.0 | 38.5 | 62.0 | 87.0 | 122. | 169. | 223. | 287. |
| 61/2 | 21.5 | 41.2 | 66.3 | 93.2 | 131. | 180. | 236. | 304. |
| 7 | 23.0 | 43.9 | 70.5 | 99.3 | 139. | 191. | 250. | 321. |
| $71 / 2$ | 24.6 | 46.6 | 74.8 | 106. | 147. | 202. | 264. | 338. |
| 8 | 26.1 | 49.4 | 79.0 | 112. | 156. | 213. | 278. | 355. |
| 81/2 | 27.6 | 52.1 | 83.3 | 118. | 164. | 223. | 292. | 372. |
| 9 | 29.2 | 54.8 | 87.6 | 124. | 173. | 234. | 306. | 389. |
| $91 / 2$ | 30.7 | 57.6 | 91.8 | 130. | 181. | 245. | 319. | 406. |
| 10 | 32.2 | 60.3 | 96.1 | 136. | 189. | 256. | 333. | 423. |
| 101/2 | 33.8 | 63.0 | 101. | 142. | 198. | $26 \%$. | 347. | 440. |
| 11 | 35.3 | 65.7 | 105. | 148. | 206. | 278. | 361. | 457. |
| 111/2 | 36.8 | 68.5 | 109. | 155. | 214. | 289. | 375. | 474. |
| 12 | 38.4 | 71.2 | 113. | 161. | 223. | 300. | 388. | 491. |
| Heads | 1.8 | 5.7 | 10.9 | 13.4 | 22.2 | 38.0 | 57.0 | 82.0 |

## WEIGHT IN POUNDS OF 100 BOLTS WITH SQUARE HEADS AND NUTS.

One cubic foot weighing 480 lbs .

| 品 | Diameter of Bolt, Inches. |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\cdots$ | $1 / 4$ | $\frac{5}{18}$ | 9/8 | ${ }^{7} 18$ | 1/2 | 5/8 | $3 / 4$ | 7/8 | 1 |
| 11/6 | 4.0 | 6.8 | $\underline{10.6}$ | 15.0 | 23.9 | 40.5 | 70.0 |  |  |
| $13 / 4$ | 4.4 | 7.3 | 11.3 | 16.1 | 25.1 | 42.7 | 73.1 |  |  |
| 2 | 4.7 | 7.8 | 12.0 | 17.2 | 26.3 | 44.8 | 76.2 |  |  |
| 214 | 5.1 | 8.4 | 12.6 | 18.2 | 27.7 | 47.0 | 79.3 |  |  |
| 21 | 5.4 | 8.9 | 13.3 | 19.2 | 29.0 | 49.2 | 82.4 | 120.5 |  |
| 234 | 5.8 | 9.5 | 14.0 | 20.2 | 30.4 | 51.4 | 85.5 | 124.7 |  |
| 3 | 6.1 | 10.0 | 14.7 | 21.2 | 31.8 | 53.5 | 88.7 | 128.9 | 185.0 |
| 3112 | 6.8 | 11.1 | 16.0 | 23.2 | 34.7 | 57.9 | 95.0 | 137.4 | 196.0 |
| 4 | 7.5 | 12.2 | 17.4 | 25.2 | 37.5 | 62.3 | 101.2 | 145.8 | 207.0 |
| 41 | 8.2 | 13.2 | 18.7 | 27.2 | 40.2 | 66.7 | 107.5 | 159.2 | 218.0 |
|  | 8.9 | 14.3 | 20.0 | 29.1 | 43.0 | 71.0 | 113.7 | 167.7 | 229.0 |
|  | 9.6 | 15.4 | 21.4 | 31.2 | 45.7 | 75.4 | 120.0 | 176.1 | 240.0 |
|  | 10.3 | 16.5 | 22.8 | 33.1 | 48.4 | 79.8 | 126.2 | 184.6 | 251.0 |
|  | 11.0 | 17.6 | 24.1 | 35.1 | 51.2 | 84.1 | 132.5 | 193.0 | 262.0 |
|  | 11.7 | 18.6 | 25.9 | 37.1 | 54.0 | 88.5 | 138.7 | 201.4 | 273.0 |
| 71/2 | 12.4 | 19.7 | 27.7 | 39.1 | 56.7 | 92.9 | 145.0 | 209.9 | 284.0 |
| 8 | 13.1 | 20.8 | 29.5 | 41.0 | 59.4 | 97.2 | 151.2 | 218.3 | 295.0 |
| 9 |  |  | 33.1 | 45.0 | 64.8 | 106.0 | 163.7 | 240.2 | 317.0 |
| 10 | .... |  | 36.7 | 49.0 | 70.3 | 114.7 | 176.2 | 257.1 | 339.0 |
| 11 | .... |  | 40.4 | 53.0 | 75.8 | 123.5 | 188.7 | 273.9 | 360.0 |
| 12 |  | ..... | 44.0 | 57.0 | 81.3 | 132.2 | 201.0 | 290.0 | 382.0 |
| 13 |  |  |  |  | 86.7 | 140.7 | 213.4 | 307.7 | 404.0 |
| 14 |  |  |  |  | 92.2 | 149.2 | 225.9 | 324.5 | 426.0 |
| 15 |  |  |  |  | 97.7 | 157.6 | 238.3 | 341.4 | 448.0 |
| 16 |  |  |  |  | 103.1 | 166.1 | 250.8 | 358.3 | 470.0 |
| 17 |  |  |  |  | 108.6 | 174.6 | 263.2 | 375.2 | 492.0 |
| 18 | $\ldots$ | . |  | ... | 114.1 | 183.1 | 275.6 | 392.0 | 514.0 |
| 19 20 |  |  |  |  | 119.5 | 191.5 | 288.1 | 408.9 | 536.0 |
| 20 | $\ldots$ | ... | .... |  | 125.0 | 200.0 | 300.5 | 425.8 | 558.0 |
| Per in. additional. | 1.4 | 2.2 | 3.6 | 4.0 | 5.5 | 8.5 | 12.4 | 16.9 | 22.0 |

APPROXIMATE WEIGHT OF NUT'S AND BOLT HEADS IN POUNDS.

| Diam. of Bolt in Inches | $1 / 4$ | ${ }^{5}$ | 3/8 | ${ }^{7}$ | -1/2 | 5/8 | $3 / 4$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Weight of Hexagon <br> Nut and Head..... | . 017 | . 042 | . 057 | . 109 | . 128 | . 267 | . 43 |
| Weight of Square Nut and Head..... | . 021 | . 049 | . 069 | . 120 | . 164 | . 320 | . 55 |
| Diam. of Bolt in Inches | 7/8 | 1 | 11/4 | 11/2 | 1344 | 2 | 21/2 |
| Weight of Hexagon <br> Nut and Head..... | $:^{73}$ | 1.10 | 2.14 | 3.78 | 5.6 | 8.75 | 17.0 |
| Weight of Square <br> Nut and Head .... | . 88 | 1.31 | 2.56 | 4.42 | 7.0 | 10.5 | 21.0 |

## Sizes and Weights of Hot Pressed Hexagon Nuts.

The sizes are the usual manufacturers', not the Franklin Institute Standard. Both weights and sizes are for unfinished Nuts. One cubic foot weighing 480 lbs .

| Size of Bolt. | $\begin{aligned} & \text { Weight } \\ & \text { of } 100 \\ & \text { Nuts. } \end{aligned}$ | Rough Hole. | Thickness of Nut. | Short Diameter. | $\begin{aligned} & \text { Long } \\ & \text { Dia- } \\ & \text { meter. } \end{aligned}$ | No. of Nuts in 100 lbs. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1/4 | 1.3 | $\frac{7}{32}$ | 1/4 | 1/2 | . 58 | 8000. |
| $\frac{5}{16}$ | 2.4 | 88 | 16 | 5/8 | . 72 | 4170. |
| 3/8 | 4.1 | $\frac{11}{3}$ | 3/8 | 3/4 | . 87 | 2410. |
| $\frac{7}{16}$ | 6.8 | $\frac{18}{8 \frac{8}{8}}$ | $\frac{7}{16}$ | 7/8 | 1.01 | 1460. |
| 1/2 | 7.1 | $\frac{7}{16}$ | 1/2 | 7/8 | 1.01 | 1410. |
| 1/2 | 9.8 | 7 | 1/2 | 1 | 1.15 | 1020. |
| $\frac{9}{16}$ | 14.0 | 1/2 | $\frac{9}{16}$ | 11/8 | 1.30 | 710. |
| 5/8 | 14.7 | $\frac{9}{16}$ | 5/8 | 11/8 | 1.30 | 680. |
| 5/8 | 19.1 | $\frac{9}{16}$ | 5/8 | 11/4 | 1.44 | 520. |
| 5/8 | 22.9 | $\frac{9}{16}$ | $3 / 4$ | 11/4 | 1.44 | 440. |
| 3/4 | 27.2 | $\frac{21}{8 \frac{1}{8}}$ | 3/4 | 13/8 | 1.59 | 370. |
| 3/4 | 39. | $\frac{31}{3}$ | 7/8 | 15/8 | 1.73 | 256. |
| 7/8 | 44. | $\frac{35}{82}$ | 7/8 | 11/2 | 1.88 | 226. |
| 7/8 | 50. | $\frac{25}{3}$ | 1 | $15 / 8$ | 1.88 | 198. |
| 1 | 57. | 7/8 | 1 | 13/4 | 2.02 | 176. |
| 1 | 64. | 7/8 | $11 / 8$ | $13 / 4$ | 2.02 | 156. |
| 11/8 | 96. | $\frac{1}{15}$ | 11/4 | 2 | 2.31 | 104. |
| 11/4 | 134. | $1 \frac{1}{16}$ | 13/8 | 21/4 | 2.60 | 75. |
| $13 / 8$ | 180. | $1 \frac{8}{16}$ | 11/2 | $21 / 2$ | 2.89 | 56. |
| 11/2 | 235. | $1 \frac{5}{16}$ | 15/8 | 23/4 | 3.18 | 42. |
| 15/8 | 300. | $1 \frac{7}{16}$ | 13/4 | 3 | 3.46 | 33.4 |
| $13 / 4$ | 370. | $1 \frac{9}{16}$ | 17/8 | 31/4 | 3.75 | 26.7 |
| 17/8 | 460. | $1 \frac{11}{16}$ | 2 | 31/2 | 4.04 | 21.5 |
| 2 | 450. | $1 \frac{18}{18}$ | 2 | $31 / 2$ | 4.04 | 22.4 |
| 21/8 | 560. | 178 | 21/8 | $33 / 4$ | 4.33 | 18.0 |
| 21/4 | 560. | $2{ }^{\circ}$ | 21/4 | $33 / 4$ | 4.33 | 17.7 |
| 23/8 | 680. | 21/8 | 23/8 | 4 | 4.62 | 14.7 |
| $21 / 2$ | 810. | $21 / 4$ | 21/2 | 41/4 | 4.91 | 12.3 |
| 23/4 | 980. | $2 \frac{7}{16}$ | $23 / 4$ | 41/2 | 5.20 | 10.2 |
| 3 | 1150. | $2 \frac{11}{1}$ | 3 | $43 / 4$ | 5.48 | 8.7 |
| 31/4 | 1340. | $2 \frac{1}{1} \frac{5}{6}$ | 31/4 | 5 | 5.77 | 7.5 |
| $31 / 2$ | 1580. | 31/8 | 31/2 | $51 / 4$ | 6.06 | 6.3 |

Sizes and Weights of Hot Pressed Square Nuts.
The sizes are the usual manufacturers', not the Franklin Institute Standard. Both weights and sizes are for unfinished Nuts. One cubic foot weighing 480 lbs.

| Size of Bolt. | $\begin{gathered} \text { Weight } \\ \text { of } 100 \\ \text { Nuts. } \\ \hline \end{gathered}$ | Rough Hole. | Thickness of Nut. | Side of Square | Diagonal | $\begin{aligned} & \text { No. of } \\ & \text { Nuts in } \\ & 100 \mathrm{lbs} \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1/4 | 1.5 | $\frac{7}{82}$ | 1/4 | 1/2 | . 71 | 6800. |
| - ${ }^{16}$ | 2.9 | $\frac{9}{82}$ | - 16 | 5\% | . 88 | 3480. |
| 3/8 | 4.9 | $\frac{11}{82}$ | $3 / 8$ | $3 / 4$ | 1.06 | 2050. |
| $\frac{7}{16}$ | 7.7 | $\frac{1}{8} \frac{3}{2}$ | $\frac{7}{16}$ | 7/8 | 1.24 | 1290. |
| 1/2 | 8.6 | $\frac{7}{16}$ | 1/2 | 7/8 | 1.24 | 1170. |
| 1/2 | 11.8 | $\frac{7}{16}$ | 1/2 | 18 | 1.41 | 850. |
| ${ }^{2}{ }^{2}$ | 16.7 | 1/2 | $\frac{9}{16}$ | 11/8 | 1.59 | 600. |
| 5/8 | 17.7 | $\frac{9}{16}$ | 5/8 | 11/8 | 1.59 | 570. |
| 5\% | 22.8 | 16 | 5/8 | 11/4 | 1.77 | 440. |
| $3 / 4$ | 32.3 | $\frac{21}{8} \frac{1}{2}$ | $3 / 4$ | 13/8 | 1.94 | 310. |
| 3/4 | 39.8 | $\frac{8}{8} \frac{1}{2}$ | 3/4 | 11/2 | 2.12 | 251. |
| 7/8 | 53. | $\frac{2}{8} \frac{5}{2}$ | 7/8 | 15/8 | 2.30 | 190. |
| 7/8 | 63. | $\frac{2}{8} \frac{8}{5}$ | $7 / 8$ | $13 / 4$ | 2.47 | 159. |
| 1 | 68. | 7/8 | 1 | 13/4 | 2.47 | 146. |
| 1 | 94. | 7/8 | 1 | 2 | 2.83 | 106. |
| 11/8 | 103. | $\frac{1}{1} \frac{15}{6}$ | 11/8 | 2 | 2.83 | 97. |
| 11/8 | 137. | $\frac{1}{16}$ | 11/8 | 21/4 | 3.18 | 73. |
| 11/4 | 145. | $1 \frac{1}{16}$ | 11/4 | 21/4 | 3.18 | 69. |
| 11/4 | 186. | 11. | 11/4 | 21/2 | 3.54 | 54. |
| 13/8 | 247. | $1 \frac{3}{16}$ | 13/8 | 23/4 | 3.89 | 41. |
| 11/2 | 319. | $1 \frac{5}{16}$ | 11/2 | 3 | 4.24 | 31.3 |
| 15\% | 400 | $1{ }^{7} 6$ | $15 / 8$ | 31/4 | 4.60 | 24.8 |
| $13 / 4$ | 500. | 196 | $13 / 4$ | 31/2 | 4.95 | 19.9 |
| 17/8 | 620. | $1 \frac{11}{16}$ | 17/8 | $33 / 4$ | 5.30 | 16.2 |
| 2 | 750. | $1 \frac{1}{1} \frac{8}{8}$ | 2 | 4 | 5.66 | 13.4 |
| 21/8 | 780. | $17 / 8$ | 21/8 | 4 | 5.66 | 12.8 |
| 21/4 | 930. | 2 | $21 / 4$ | 41/4 | 6.01 | 10.7 |
| 23/8 | 960. | 21/8 | 23/8 | 41/4 | 6.01 | 10.4 |
| $21 / 2$ | 1130. | $21 / 4$ | $21 / 2$ | 41/2 | 6.36 | 8.9 |
| 23/4 | 1370. | $2{ }_{16}$ | $23 / 4$ | $43 / 4$ | 6.72 | 7.3 |
| 3 | 1610. | $21 \frac{1}{8}$ | 3 | 5 | 7.07 | 6.2 |
| $31 / 4$ | 2110. | $2 \frac{1}{6}$ | 31/4 | 51/2 | 7.78 | 4.7 |
| 31/2 | 2750. | 31/8 | 31/2 | $6^{1}$ | 8.49 | 3.6 |

## STANDARD GAUGES.

| 8 | Thickness in Decimals of an Inch. |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { y } \\ & 4 \\ & 0 \\ & 0 \\ & z \end{aligned}$ | Birmingham Stubb's Iron Wire | Browne \& Sharpe | United States | British Imperial | Washburn \& Moen Co. | Trenton Iron Co. | Stubs Steel Wire |
| $7{ }^{\circ}$ | .... |  | . 50000 | . 500 | ..... | . $\cdot$. |  |
| $6^{\circ}$ |  |  | . 46875 | . 464 | ..... |  |  |
| $5^{\circ}$ |  |  | . 43750 | . 432 |  | . 45 | .... |
| $4^{\circ}$ | . 454 | . 46000 | . 40625 | . 400 | . 3938 | . 40 | .... |
| $3{ }^{\circ}$ | . 425 | . 40964 | . 37500 | . 372 | . 3625 | . 36 | ... |
| $2{ }^{\circ}$ | . 380 | . 36480 | . 34375 | . 348 | . 3310 | . 33 | .... |
| 0 | . 340 | . 32486 | . 31250 | . 324 | . 3065 | . 305 | $\ldots$ |
| 1 | . 300 | . 28930 | . 28125 | . 300 | . 2830 | . 285 | . 227 |
| 2 | . 284 | . 25763 | . 26562 | . 276 | . 2625 | . 265 | . 219 |
| 3 | . 259 | .22942 | . 25000 | . 252 | . 2437 | . 245 | . 212 |
| 4 | . 238 | . 20431 | . 23437 | . 232 | . 2253 | . 225 | . 207 |
| 5 | . 220 | . 18194 | . 21875 | . 212 | . 2070 | . 205 | . 204 |
| 6 | . 203 | . 16202 | . 20312 | . 192 | . 1920 | . 190 | . 201 |
| 7 | . 180 | . 14428 | . 18750 | . 176 | . 1770 | . 175 | . 199 |
| 8 | . 165 | . 12849 | . 17187 | . 160 | . 1620 | . 160 | . 197 |
| 9 | . 148 | . 11443 | . 15625 | . 144 | . 1483 | . 145 | . 194 |
| 10 | . 134 | . 10189 | . 14062 | . 128 | . 1350 | . 130 | . 191. |
| 11 | . 120 | . 09074 | . 12500 | . 116 | . 1205 | . 1175 | . 188 |
| 12 | . 109 | . 08081 | . 10937 | . 104 | . 1055 | . 1050 | . 185 |
| 13 | . 095 | . 07196 | . 09375 | . 092 | . 0915 | . 0925 | . 182 |
| 14 | . 083 | . 06408 | . 07812 | . 080 | . 0800 | . 0800 | . 180 |
| 15 | . 072 | . 05707 | . 07031 | . 072 | .0720 | . 0700 | . 178 |
| 16 | . 065 | . 05082 | . 06250 | . 064 | .0625 | . 0610 | . 175 |
| 17 | . 058 | . 04526 | . 05625 | . 056 | . 0540 | . 0525 | . 172 |
| 18 | . 049 | . 04030 | . 05000 | . 048 | . 0475 | . 0450 | . 168 |
| 19 | . 042 | . 03589 | . 04375 | . 040 | . 0410 | . 0400 | . 164 |
| 20 | . 035 | . 03196 | . 03750 | . 036 | . 0348 | . 0350 | . 161 |
| 21 | . 032 | . 02846 | . 03437 | . 032 | . 0317 | . 0310 | . 157 |
| 22 | . 028 | . 02535 | . 03125 | . 028 | . 0286 | . 0288 | . 155 |
| 23 | . 025 | . 02257 | . 02812 | . 024 | . 0258 | . 0250 | . 153 |
| 24 | . 022 | . 02010 | . 02500 | . 022 | . 0230 | .0225 | . 151 |
| 25 | . 020 | . 01790 | . 02187 | . 020 | . 0204 | . 0200 | . 148 |
| 26 | . 018 | . 01594 | . 01875 | . 018 | . 0181 | . 0180 | . 146 |
| 27 | . 016 | . 01419 | . 01719 | . 0164 | . 0173 | . 0170 | . 143 |
| 28 | . 014 | . 01264 | . 01562 | . 0148 | . 0162 | . 0160 | . 139 |
| 29 | . 013 | . 01126 | . 01406 | . 0136 | . 0150 | . 0150 | . 134 |
| 30 | . 012 | . 01002 | . 01250 | . 0124 | . 0140 | . 0140 | . 127 |
| 31 | . 010 | . 00893 | . 01094 | . 0116 | . 0132 | . 0130 | . 120 |
| 32 | . 009 | . 00795 | . 01016 | . 0108 | . 0128 | . 0120 | . 115 |
| 33 | . 008 | . 00708 | . 00938 | . 0100 | . 0118 | . 0110 | . 112 |
| 34 | . 007 | . 00630 | . 00859 | . 0092 | . 0104 | . 0100 | . 110 |
| 35 | . 005 | . 00561 | . 00781 | . 0084 | . 0095 | . 0095 | . 108 |
| 36 | . 004 | . 00500 | . 00703 | . 0076 | . 0090 | . 0090 | . 106 |
| 37 | .... | . 00445 | . 00664 | . 0068 | ..... | . 0085 | . 103 |
| 38 | . | . 00398 | . 00625 | . 0060 | ..... | . 0080 | . 101 |
| 39 40 |  | . 00353 |  | ..... | ..... | . 0075 | . 099 |
| 40 | .. | . 00314 | ...... | .. | ...... | . 0070 | . 097 |

## DECIMALS OF AN INCH AND FOOT FOR

EACH $\frac{1}{6}$.


DECIMALS OF A FOOT FOR EACH INCH.

| In | Ft. | In. | Ft. | In. | Ft. | In. | Ft. | In. | Ft. | In. | Ft. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | .0833 | 3 | .2500 | 5 | .4167 | ry | .5833 | 9 | .7500 | 11 | .9167 |
| 2 | .1667 | 4 | .3333 | 6 | .500 | 8 | .6667 | 10 | .8333 | 12 | 1.0000 |

WEIGHTS OF SHEETS AND PLATES OF STEEL, WROUGH'T IRON, COPPER AND BRASS.

Birmingham Gauge.

| No. of Gauge. | Thickness in Inches. | Weight per Square Foot. |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Steel. | Iron. | Copper. | Brass. |
| 0000 | . 454 | 18.5232 | 18.16 | 20.5662 | 19.4312 |
| 000 | . 425 | 17.3400 | 17.00 | 19.2525 | 18.1900 |
| 00 | . 380 | 15.5040 | 15.20 | 17.2140 | 16.2640 |
| 0 | . 340 | 13.8720 | 13.60 | 15.4020 | 14.5520 |
| 1 | . 300 | 12.2400 | 12.00 | 13.5900 | 12.8400 |
| 2 | . 284 | $11.58 i 2$ | 11.36 | 12.8652 | 12.1552 |
| 3 | . 259 | 10.5672 | 10.36 | 11.7327 | 11.0852 |
| 4 | . 238 | 9.7104 | 9.52 | 10.7814 | 10.1864 |
| 5 | . 220 | 8.9760 | 8.80 | 9.966 | 9.4160 |
| 6 | . 203 | 8.2824 | 8.12 | 9.1959 | 8.6884 |
| 7 | . 180 | 7.3440 | 7.20 | 8.1540 | 7.7040 |
| 8 | . 165 | 6.7320 | 6.60 | 7.4745 | 7.0620 |
| 9 | . 148 | 6.0384 | 5.92 | 6.7044 | 6.3344 |
| 10 | . 134 | 5.4672 | 5.36 | 6.0702 | 5.7352 |
| 11 | . 120 | 4.8960 | 4.80 | 5.4360 | 5.1360 |
| 12 | . 109 | 4.4472 | 4.36 | 4.9377 | 4.6655 |
| 13 | . 095 | 3.8760 | 3.80 | 4.3035 | 4.0660 |
| 14 | . 083 | 3.3864 | 3.32 | 3.7599 | 8.5524 |
| 15 | . 072 | 2.9376 | 2.88 | 3.2616 | 3.0816 |
| 16 | . 065 | 2.6520 | 2.60 | 2.9445 | 2.7820 |
| 17 | . 058 | 2.3664 | 2.32 | 2.6274 | 2.4824 |
| 18 | . 049 | 1.9992 | 1.96 | 2.2197 | 2.0977 |
| 19 | . 042 | 1.7136 | 1.68 | 1.9026 | 1.7976 |
| 20 | . 035 | 1.4280 | 1.40 | 1.5855 | 1.4980 |
| 21 | . 032 | 1.3056 | 1.28 | 1.4496 | 1.3696 |
| 22 | . 028 | 1.1424 | 1.12 | 1.2684 | 1.1984 |
| 23 | . 025 | 1.0200 | 1.00 | 1.1325 | 1.0700 |
| 24 | .022 | . 8976 | . 88 | . 9966 | . 9416 |
| 25 | . 020 | . 8160 | . 80 | . 9060 | . 8560 |
| 26 | . 018 | . 7344 | . 72 | . 8154 | . 7704 |
| 27 | . 016 | . 6528 | . 64 | . 7248 | . 6848 |
| 28 | . 014 | . 5712 | . 56 | . 6342 | . 5992 |
| 29 | . 013 | . 5304 | . 52 | . 5889 | . 5564 |
| 30 | . 012 | .4896 | . 48 | . 5436 | . 5136 |
| 31 | . 010 | . 4080 | . 40 | . 4530 | . 4280 |
| 32 | . 009 | . 3672 | . 36 | . 4077 | . 3852 |
| 33 | . 008 | . 3264 | . 32 | . 3624 | . 3424 |
| 34 | . 007 | . 2856 | . 28 | . 3171 | . 2996 |
| 35 | . 005 | . 2040 | . 20 | . 2265 | $.2140$ |
| 36 | . 004 | . 1632 | .16 | . 1812 | $.1712$ |
| Specific Gravities. Weight of a Cubic Ft. |  | 7.85 | 7.70 | 8.72 | 8.24 |
|  |  | $489.6$ | $480.0$ | $543.6$ | $513.6$ |
|  |  | 0.2833 | 0.2778 | 0.3146 | 0.2972 |

## WEIGHTS OF SHEETS AND PLATES OF STEEL, WROUGH'T IRON, COPPER AND BRASS.

American or Browne \& Sharpe Gauge.

| No. of Gauge. | Thickness in Inches. | Weight per Square Foot. |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Steel. | Iron. | Copper. | Brass. |
| 0000 | .460000 | 18.7680 | 18.4000 | 20.8380 | 19.6880 |
| 000 | .409642 | 16.7134 | 16.3857 | 18.5556 | 17.5327 |
| 00 | . 364796 | 14.8837 | 14.5918 | 16.5253 | 15.6133 |
| 0 | . 324861 | 18.2543 | 12.9944 | 14.7162 | 13.9041 |
| 1 | . 289297 | 11.8033 | 11.5719 | 13.1052 | 12.3819 |
| 2 | . 257627 | 10.5112 | 10.3051 | 11.6705 | 11.0264 |
| 3 | . 229423 | 9.3605 | 9.1769 | 10.3929 | 9.8193 |
| 4 | . 204307 | 8.3357 | 8.1723 | 9.2551 | 8.7443 |
| 5 | .181940 | 7.4232 | 7.2776 | 8.2419 | 7.7870 |
| 6 | . 162023 | 6.6105 | 6.4809 | 7.3396 | 6.9346 |
| 7 | . 144285 | 5.8868 | 5.7714 | 6.5361 | 6.1754 |
| 8 | .128490 | 5.2424 | 5.1396 | 5.8206 | 5.4994 |
| 9 | . 114423 | 4.6685 | 4.5769 | 5.1834 | 4.8973 |
| 10 | . 101897 | 4.1574 | 4.0759 | 4.6159 | 4.3612 |
| 11 | . 090742 | 3.7023 | 3.6297 | 4.1106 | 3.8838 |
| 12 | . 080808 | 3.2970 | 3.2323 | 3.6606 | 3.4586 |
| 13 | . 071962 | 2.9360 | 2.8785 | 3.2599 | 3.0800 |
| 14 | . 064084 | 2.6146 | 2.5634 | 2.9030 | 2.7428 |
| 15 | . 057068 | 2.3284 | 2.2827 | 2.5852 | 2.4425 |
| 16 | . 050821 | 2.0735 | 2.0328 | 2.3022 | 2.1751 |
| 17 | .04525\% | 1.8465 | 1.8103 | 2.0501 | 1.9370 |
| 18 | . 040303 | 1.6444 | 1.6121 | 1.8257 | 1.7250 |
| 19 | . 035890 | 1.4643 | 1.4356 | 1.6258 | 1.5361 |
| 20 | . 031961 | 1.3040 | 1.2784 | 1.4478 | 1.3679 |
| 21 | . 028462 | 1.1612 | 1.1385 | 1.2893 | 1.2182 |
| 22 | . 0235346 | 1.0341 | 1.0138 | 1.1482 | 1.0348 |
| ${ }_{24}^{23}$ | .022572 | . 922094 | . 902888 | 1.0225 .91058 | .96608 .86032 |
| 25 | . 017900 | . 73032 | . 71600 | . 81087 | .76612 |
| 26 | . 015941 | . 65039 | . 63764 | . 72213 | . 68227 |
| 27 | . 014195 | . 57916 | . 56780 | . 64303 | . 60755 |
| 28 | . 012641 | . 51575 | . 50564 | . 577264 | . 54103 |
| 29 | . 011257 | . 45929 | . 45028 | . 50994 | . 48180 |
| 30 | . 010025 | . 40902 | . 40100 | . 45413 | . 42907 |
| 31 | . 008928 | . 36426 | . 35712 | . 40444 | . 38212 |
| 32 | . 007950 | . 32436 | . 31800 | . 36014 | . 34026 |
| 33 | . 007080 | . 28886 | . 28320 | . 32072 | . 30302 |
| 84 | . 006305 | . 25724 | . 25220 | . 28562 | . 26985 |
| 35 | . 005615 | . 22909 | . 22460 | . 25436 | . 24032 |
| 36 | . 005000 | . 20400 | . 20000 | . 22650 | . 21400 |

WEIGHT OF PLATE IRON IN POUNDS PER LINEAL FOOT.
(Based on 480 lbs . per Cubic Foot. For Steel add 2 per cent.)

|  | Thickness in Inches. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | ${ }_{18}^{18}$ | 1/8 | $\frac{3}{16}$ | 1/4 | ${ }_{18}^{18}$ | 3/8 | ${ }^{\frac{7}{818}}$ | 1/2 |
| 12 | 2.50 | 5.00 | 7.50 | 10.00 | 12.50 | 15.00 | 17.50 | 20.00 |
| 13 | 2.71 | 5.42 | 8.13 | 10.83 | 13.54 | 16.25 | 18.96 | 21.67 |
| 14 | 2.92 | 5.83 | 8.75 | 11.67 | 14.58 | 17.50 | 20.42 | 23.33 |
| 15 | 313 | 6.25 | 9.38 | 12.50 | 15.63 | 18.75 | 21.88 | 25.00 |
| 16 | 3.33 | 6.67 | 10.00 | 13.33 | 16.67 | 20.00 | 23.33 | 26.67 |
| 17 | 3.54 | 7.08 | 10.63 | 14.17 | 17.71 | 21.25 | 24.79 | 28.33 |
| 18 | 3.75 | 7.50 | 11.25 | 15.00 | 18.75 | 22.50 | 26.25 | 30.00 |
| 19 | 3.96 | 7.92 | 11.87 | 15.83 | 19.79 | 23.75 | 27.71 | 31.67 |
| 20 | 4.17 | 8.33 | 12.50 | 16.67 | 20.83 | 25.00 | 29.17 | 33.33 |
| 21 | 4.38 | 8.75 | 13.13 | 17.50 | 21.88 | 26.25 | 30.63 | 35.00 |
| 22 | 4.58 | 9.17 | 13.75 | 18.33 | 22.92 | 27.50 | 32.08 | 36.67 |
| 23 | 4.79 | 9.58 | 14.38 | 19.17 | 23.96 | 28.75 | 33.54 | 38.33 |
| 24 | 5.001 | 10.00 | 15.00 | 20.00 | 25.00 | 30.00 | 35.00 | 40.00 |
| 25 | 5.21 | 10.42 | 15.62 | 20.83 | 26.04 | 31.25 | 36.46 | 41.67 |
| 26 | 5.421 | 10.83 | 16.25 | 21.67 | 27.08 | 32.50 | 37.92 | 43.33 |
| 27 | 5.63 | 11.25 | 16.88 | 22.50 | 28.13 | 33.75 | 39.38 | 45.00 |
|  | 5.831 | 11.67 | 17.50 | 23.33 | 29.17 | 35.00 | 40.83 | 46.67 |
| 29 | 6.041 | 12.08 | 18.13 | 24.17 | 30.21 | 36.25 | 42.29 | 48.33 |
| 30 | 6.25 | 12.50 | 18.75 | 25.00 | 31.25 | 37.50 | 43.75 | 50.00 |
| 32 | 6.67 | 13.33 | 20.00 | 26.67 | 33.33 | 40.00 | 46.67 | 53.33 |
| 34 | 7.081 | 14.17 | 21.25 | 28.33 | 35.42 | 42.50 | 49.58 | 56.67 |
| 36 | 7.501 | 15.00 | 22.50 | 30.00 | 37.50 | 45.00 | 52.50 | 60.00 |
| 38 | 7.921 | 15.83 | 23.75 | 31.67 | 39.59 | 47.50 | 55.42 | 63.33 |
|  |  | 16.67 | 25.00 | 33.33 | 41.67 | 50.00 | 58.33 | 66.67 |
| 42 | 8.75 | 17.50 | 26.25 | 35.00 | 43.75 | 52.50 | 61.25 | 70.00 |
| 44 | 9.171 | 18.33 | 27.50 | 36.67 | 45.84 | 55.00 | 64.17 | 73.33 |
| 46 | 9.58 | 19.17 | 28.75 | 38.33 | 47.92 | 57.50 | 67.08 | 76.67 |
| 48 | 10.00 | 20.00 | 30.00 | 40.00 | 50.00 | 60.00 | 70.00 | 80.00 |
|  | 10.42 | 20.83 | 31.25 | 41.67 | 52.08 | 62.50 | 72.91 | 83.33 |
| 52 | 10.83 | 21.67 | 32.50 | 43.33 | 54.17 | 65.00 | 75.83 | 86.67 |
|  | 11.25 | 22.50 | 33.75 | 45.00 | 56.25 | 67.50 | 78.75 | 90.00 |
|  | 11.67 | 23.33 | 35.00 | 46.67 | 58.33 | 70.00 | 81.66 | 93.33 |
| 58 | 12.08 | 24.17 | 36.25 | 48.33 | 60.42 | 72.50 | 84.58 | 96.67 |
| 60 | 12 | 25.00 | 37.50 | 50.00 | 62.50 | 75.00 | 87.50 | 100.00 |

WEIGHT OF PLATE IRON IN POUNDS PER LINEAL FOOT
(CONTINUED.)

|  | THICKNESS |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | ${ }_{16}$ | 5/8 | $\frac{11}{16}$ | $3 / 4$ | $\frac{18}{18}$ | 7/8 | $\frac{1}{1} \frac{5}{6}$ | 1 |
| 12 | 22.50 | 25.00 | 27.50 | 30.00 | 32.50 | 35.00 | 37.50 | 40.00 |
| 13 | 24.38 | 27.08 | 29.79 | 32.50 | 35.21 | 37.92 | 40.63 | 43.33 |
| 14 | 26.25 | 29.17 | 32.08 | 35.00 | 37.92 | 40.83 | 43.75 | 46.67 |
| 15 | 28.13 | 31.25 | 34.38 | 37.50 | 40.63 | 43.75 | 46.88 | 50.00 |
| 16 | 30.00 | 33.33 | 36.67 | 40.00 | 43.33 . | 46.67 | 50.00 | 53.33 |
| 17 | 31.88 | 35.42 | 38.96 | 42.50 | 46.05 | 49.59 | 53.13 | 56.67 |
| 18 | 33.75 | 37.50 | 41.25 | 45.00 | 48.75 | 52.50 | 56.25 | 60.00 |
| 19 | 35.67 | 39.58 | 43.54 | 47.50 | 51.45 | 55.41 | 59.37 | 63.33 |
| 20 | 37.50 | 41.67 | 45.83 | 50.00 | 54.17 | 58.33 | 62.50 | 66.67 |
| 21 | 39.38 | 43.75 | 48.13 | 52.50 | 56.88 | 61.25 | 65.63 | 70.00 |
| 22 | 41.25 | 45.83 | 50.42 | 55.00 | 59.58 | 64.17 | 68.75 | 73.33 |
| 23 | 43.13 | 47.92 | 52.71 | 57.50 | 62.30 | 67.09 | 71.88 | 76.67 |
| 24 | 45.00 | 50.00 | 55.00 | 60.00 | 65.00 | 70.00 | 75.00 | 80.00 |
| 25 | 46.88 | 52.08 | 57.29 | 62.50 | 67.70 | 72.91 | 78.13 | 83.33 |
| 26 | 48.75 | 54.17 | 59.58 | 65.00 | 70.42 | 75.83 | 81.25 | 86.67 |
| 27 | 50.63 | 56.25 | 61.88 | 67.50 | 73.13 | 78.75 | 84.38 | 90.00 |
| 28 | 52.50 | 58.33 | 64.17 | 70.00 | 75.84 | 81.67 | 87.50 | 93.33 |
| 29 | 54.38 | 60.42 | 66.46 | 72.50 | 78.55 | 84.59 | 90.63 | 96.67 |
| 30 | 56.25 | 62.50 | 68.75 | 75.00 | 81.25 | 87.50 | 93.75 | 100.0 |
| 32 | 60.00 | 66.67 | 73.33 | 80.00 | 86.67 | 93.33 | 100.0 | 106.7 |
| 34 | 63.75 | 70.83 | 77.91 | 85.00 | 92.08 | 99.17 | 106.3 | 113.3 |
| 36 | 67.50 | 75.00 | 82.50 | 90.00 | 97.50 | 105.0 | 112.5 | 120.0 |
| 38 | 71.25 | 79.17 | 87.09 | 95.00 | 102.9 | 110.8 | 118.8 | 126.7 |
| 40 | 75.00 | 83.33 | 91.67 | 100.0 | 108.3 | 116.7 | 125.0 | 133.3 |
| 42 | 78.75 | 87.50 | 96.25 | 105.0 | 113.7 | 122.5 | 131.3 | 140.0 |
| 44 | 82.50 | 91.67 | 100.8 | 110.0 | 119.2 | 128.3 | 137.5 | 146.7 |
| 46 | 86.25 | 95.83 | 105.4 | 115.0 | 124.6 | 134.2 | 143.8 | 153.3 |
| 48 | 90.00 | 100.0 | 110.0 | 120.0 | 130.0 | 140.0 | 150.0 | 160.0 |
| 50 | 93.75 | 104.2 | 114.6 | 125.0 | 135.4 | 145.8 | 156.3 | 166.7 |
| 52 | 97.50 | 108.3 | 119.2 | 130.0 | 140.8 | 151.7 | 162.5 | 173.3 |
| 54 | 101.3 | 112.5 | 123.8 | 135.0 | 146.3 | 157.5 | 168.8 | 180.0 |
| 56 | 105.0 | 116.7 | 128.3 | 140.0 | 151.7 | 163.3 | 175.0 | 186.7 |
| 58 | 108.8 | 120.8 | 132.9 | 145.0 | 157.1 | 169.2 | 181.3 | 193.3 |
| 60 | 112.5 | 125.0 | 137.5 | 150.0 | 162.5 | 175.0 | 187.5 | 200.0 |

Angle of thread $=60^{\circ}$.

UNITED STATES, OR SELLERS SYSTEM OF SCREW-HEADS.-(continued.)

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| :---: | :---: |
| -səyวuI -bS U! кроя 7 log jo еә. V |  <br>  |
| ? <br> јо ЧІР! $M$ | an wnon |
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| - YouI دәđ speәiч, | - 00 ค |
|  |  |

## STANDARD SIZES OF SCREW-THREADS FOR BOLTS AND TAPS.

(CHAS. A BAUER.)

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | $n$ | $D$ | d | $h$ |  | $D^{\prime}-D$ | $D^{\prime}$ | $d^{\prime \prime}$ | $H$ |
| $\begin{aligned} & 1 / 4 \\ & 5 \\ & \frac{16}{6} \\ & 78 \\ & 76 \\ & 58 \\ & \hline 8 \\ & 0 / 4 \\ & 7 / 8 \end{aligned}$ |  | Inches | Inches | Inches | Inches | Inches | Inches | Inches | Inches |
|  | 20 | . 2608 | . 1855 | . 0379 | . 0062 | 006 | 2668 | 1915 | 2024 |
|  | 18 | . 3245 | . 2403 | 421 | . 0070 | . 006 | . 3305 | 2 | 2589 |
|  | 16 | . 3885 | . 2938 | 0474 | . 0078 | . 006 | 3945 | 2998 | 3139 |
|  | 14 | . 5166 | .34000 | . 0548 | . 00096 | . 0006 | . 4590 | 4060 | 3670 |
|  | 12 | . 5805 | .4543 | . 0631 | . 0104 | . 007 | . 5875 | . 4613 | . 4802 |
|  | 11 | . 6447 | . 5069 | . 0689 | . 0114 | . 007 | . 6517 | . 5139 | . 5346 |
|  | 10 | . 7717 | . 6201 | . 0758 | . 0125 | . 007 | . 7787 | . 6271 | . 6499 |
|  | 9 | . 8991 | . 7307 | . 0842 | . 0139 | . 007 | . 9061 | . 7377 | . 7630 |
|  | 8 | 1.0271 | . 8376 | . 0947 | . 0156 | . 007 | 1.0311 | . 8446 | . 8731 |
| $11 / 8$ | 7 | 1.1559 | . 9394 | . 1083 | . 0179 | . 007 | 1.1629 | . 9464 | . 9789 |
| 11/4 | 7 | 1.2809 | 1.0644 | . 1083 | . 0179 | . 007 | 1.2879 | 1.0714 | 1.1039 |

$A=$ nominal diameter of bolt.
$D=$ actual diameter of bolt.
$d=$ diameter of bolt at bottom of thread.
$n=$ number of threads per inch.
$f=$ flat of bottom of thread.
$h=$ depth of thread.
$D^{\prime}$ and $d^{\prime}=$ diameters of tap.
$H=$ diameter of hole in nut before tapping.

$$
\begin{aligned}
& D=A+\frac{.2165}{n} \\
& d=A-\frac{1.29904}{n} \\
& h=\frac{.7577}{n}=\frac{D-d}{2} \\
& f=\frac{.125}{n} \\
& H=D^{\prime}-\frac{1 \cdot 288}{n}=D^{\prime}-.85(2 h)
\end{aligned}
$$

Efficiency of Screw-bolts.-Mr. Lewis gives the following approximate formula for ordinary screw-bolts (V threads, with collars): $p=$ pitch of screw, $d=$ outside diameter of
screw，$F=$ force applied at circumference to lift a unit of weight， $\mathrm{E}=$＝efficiency of screw．For an average case，in which the coefficient of friction may be assumed at 0.15 ，

$$
F=\frac{p+d}{3 d}, \quad E=\frac{p}{p+d}
$$

For bolts of the dimensions given above， $1 / 2$－inch pitch， and outside diameters $11 / 2,21 / 2,31 / 2$ ，and $41 / 2$ in．，the efficiencies according to this formula would be，respec－ tively， $0.25,0.167,0.125$ ，and 0.10 ．

James McBride（Trans．A．S．M．E．，xii．781）describes an experiment with an ordinary 2 －in．screw－bolt，with a V thread， $41 / 2$ threads per inch，raising a weight of 7500 lbs ．， the force being applied by turning the nut．Of the power applied $89.8 \%$ was absorbed by friction of the nut on its supporting washer and of the threads of the bolt in the nut．The nut was not faced，and had the flat side to the washer．

STRENGTH OF WROUGHT IRON BOLTS．
（COMPUTED BY A．F．NAGLE．）

|  | Number of Threads． |  |  | Stress upon Bolt upon Basis of working strength of |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  | 苟 | 岗 | 殸 | بِّ | 茳 |  |
|  |  |  |  |  | ． | ． | फ่ | － |  |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  | \& |  | ర్రి 耳్ర |  |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  | s． | lbs． | lbs． | lbs． | lbs． | lbs． |
| 1／3 | 13 | ． 38 | ． 12 | 350 | 460 | 580 | 810 | 1160 | 5800 |
| ${ }^{16}$ | 12 | ． 44 | ． 15 | 450 | 600 | 750 | 1050 | 1500 | 7500 |
|  | 11 | ． 49 | ． 19 | 560 | 750 | 930 | 1310 | 1870 | 9000 |
|  | 10 | ． 60 | ． 28 | 750 | 1130 | 1410 | 1980 | 2830 | 14000 |
|  | 9 8 | ． 81 | ． 39 | 1180 | 1570 | 1970 | 2760 | 3940 | 19000 |
|  | 8 | ． 91 | ． 62 | 1550 | 2070 | 2600 | 3630 | 5180 | 25000 |
| 11 | 7 | 1.04 | ． 65 | 1950 | 2600 | 3250 | 4560 | 6510 | 30000 |
| $13 / 8$ | 6 | 1.12 | 1.00 | 3000 | 4000 | 5000 | 7000 | 10000 | 6000 |
| 11.2 | 6 | 1.25 | 1.23 | 3680 | 4910 | 6140 | 8600 | 12280 | 6000 |
| 18 | 51／2 | 1.35 | 1.44 | 4300 | 5740 | 7180 | 10000 | 14360 | 65000 |
| 134 | 5 | 1.45 | 1.65 | 4950 | 6600 | 8250 | 11560 | 16510 | 74000 |
| 17／8 | 5 | 1.57 | 1.95 | 5840 | 7800 | 9800 | 13640 | 19500 | 85000 |
| ${ }_{21}$ | 41／3 | 1.66 | 2.18 | 6540 | 8720 | 10900 | 15æ60 | 21800 | 95000 |
| $21 / 4$ | $41 / 2$ | 1.92 | 2.88 | 8650 | 11530 | 14400 | 20180 | 28800 | 125000 |
| 219 | 4 | ${ }_{2}^{2.12}$ | 3.55 | 10640 | 14200 | 17730 | 24830 | 35500 | 150000 |
| $23 / 4$ | 316 | $\stackrel{2.37}{2.57}$ | 4.43 | 13290 | 17770 | 22150 | 31000 | 44300 | 186000 |
| 31／2 | $31 / 4$ $31 / 4$ | 3.57 | 5.20 7.25 | 15580 | 20770 | 26000 | 36360 | 52000 | 213000 |
|  | 8 | 3.50 | 9.62 | 28860 | 38500 | 48100 | 67350 | 96200 | 290000 385000 |

When the greatest load that has to be sustained by a bolt is known, and the working strength per sq. in. of the material constituting it is determined, look in the proper column for the given load. Should the load sought be not found, then take the load next larger as found in the column, and opposite to it in the first column read the required size of bolt.

Effect of Initial Strain in Bolts.-Suppose that bolts are used to connect two parts of a machine and that they are screwed up tightly before the effective load comes on the connected parts. Let $P_{1}=$ the initial tension on a bolt due to screwing up, and $P_{2}=$ the load afterwards added. The greatest load may vary but little from $P_{1}$ or $P_{2}$, according as the former or the latter is greater, or it may approach the value $P_{1}+P_{2}$, depending upon the relative rigidity of the bolts and of the parts connected. Where rigid flanges are bolted together, metal to metal, it is probable that the extension of the bolts with any additional tension relieves the initial tension, and that the total tension is $P_{1}$ or $P_{2}$, but in cases where elastic packing, as india rubber, is interposed, the extension of the bolts may very little affect the initial tension, and the total strain may be nearly $P_{1}+P_{2}$. Since the latter assumption is more unfavorable to the resistance of the bolt, this contingency should usually be provided for. (See Unwin, "Elements of Machine Design" for demonstration.)

WEIGHTS
AND
MEASURES.

## WEIGHTS AND MEASURES.

## AVOIRDUPOIS OR COMMERCIAL WEIGHT.

UNITED STATES AND BRITISH.

| Grains. | Ounces. | Pounds. | Hundredweight. | Gross Tons. |
| :---: | :---: | :---: | :---: | :---: |
| ${ }_{437.5}^{1 .}$ | 1.002286 | 0.000143 0.0625 | 0.00000128 0.0005588 | 0.0000000176 0.0002790 |
| 7000. | 16. |  | ${ }_{0}^{0.00059884}$ | ${ }_{0}^{0.00004464}$ |
| 784000. | 1792. | 112. | 1. | 0.05 |
| 5680000. | 35840 . | 2240. | 20. | 1. |

1 pound avoirdupois $=1.215278$ pounds troy.
1 net ton $=2000$ pounds $=0.892857$ gross tons.
1 pound troy $=0.82286$ pounds avoirdupois.

## LINEAR MEASURE.

UNITED STATES AND BRITISH.

| Inches. | Feet. | Yards. | Rods. | Miles. |
| :---: | :---: | :---: | :---: | :---: |
| 12. | 1.08333 | 0.02778 0.33333 | 0.0050505 0.0606061 | 0.00001578 0.00018939 |
| 36. |  |  | 0.1818182 | 0.00056818 |
| 198. 63360. | 16.5 5280. | ${ }_{1760.5}$ | 1. 320. | 0.003125 1. |

## GUNTER'S CHAIN MEASURE.

## USED IN SURVEYING.

1 link $=7.92$ inches $=0.01$ chain $=0.000125 \mathrm{mile}$.
1 chain $=100$ links $=66$ feet $=4$ rods $=0.0125$ mile
1 mile $=80$ chains $=8000$ links.

## SQUARE OR SURFACE MEASURE.

UNITED STATES AND BRITISH.

| Square <br> Inches. | Square Feet. | Square Yards | Square Rods. | Acres. | Square Miles. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.006944 | 0.0007716 |  |  |  |
| 144 1296 |  | ${ }^{0.111111}$ |  | 0.0002066 |  |
| 39204 | ${ }_{272.25}^{9}$ | 30.25 |  | 0.00625 | 0.000009\% ${ }^{\text {a }}$ |
| 6272640 | $425360 .$ | $\begin{gathered} 4840 . \\ 309760 \end{gathered}$ | $\begin{array}{r} 160 . \\ 102400 \end{array}$ | 1. 640 | 0.0015625 |

1 acre $=10$ square chains.

## CUBIC MEASURE.

1728 cubic inches $=1$ cubic foot,
27 cubic feet $=1$ cubic yard $=46656$ cubic inches, 1 cord wood $=4 \mathrm{ft} . \times 4 \mathrm{ft} . \times 8 \mathrm{ft} .=128$ cubic feet, 1 perch of masonry $=16.5 \mathrm{ft} . \times 1.5 \mathrm{ft} . \times 1 \mathrm{ft} .=24.75$ cubic feet, but is generally assumed to be 25 cubic feet.

## DRY MEASURE.

UNITED STATES ONLY.

| Struck Bush. | Pecks. | Quarts. | Pints. | Gallons. | Cubic Inch. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 4 | 32. | 64 | 8. | 2150.4 |
|  | 1 | 8. | 16 | 2. | 537.6 |
|  |  | 1. | 2 | 0.25 | 67.2 |
|  |  | 0.5 | 1 | 0.125 | 33.6 |
|  |  | 4. | 8 | 1. | 268.8 |

The United States standard unit for dry measure is the old English Winchester bushel, which contains 2,150.42 cubic inches, or 1.2445 cubic feet.

The heaped bushel, the cone of which is 6 inches above the brim of the measure, contains $2,747.7$ cubic inches.

In New York a bushel contains 2,218.2 cubic inches, or 1.2837 cubic feet, which is the same as the Imperial bushel of England. 33 English or Imperial bushels are equal to 34.04 Winchester or United States bushels.

## LIQUID MEASURE.

UNITED STATES ONLY.

| Cubic Inch. | Pints. | Quarts. | Gallons. | Barrels. | Hogshead. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 28.875 | 1. | 0.5 | 0.125 | 0.003968 |  |
| 57.75 | 2. | 1. | 0.25 | 0.007937 |  |
| 231. | 8. | 4. | 1. | 0.031746 |  |
| 7276.5 | 252. | 126. | 31.5 |  | 0.5 |
| 14553.0 | 504. | 252. | 63. | 2. | 1. |

The British Imperial gallon $=1.20032$ U. S. gallons.
The United States standard unit for liquid measure is the gallon $=231 \mathrm{cu}$. in. $=8.33888$ pounds, avoirdupois, of distilled water at $62^{\circ}$ Fahr.

The English standard is the Imperial gallon $=277.2738$ cu . in. $=10$ pounds, avoirdupois, of distilled water at $62^{\circ}$ Fahr.

## NAUTICAL MEASURE.

A knot or nautical mile $=1.1527$ statute miles $=6086$. feet $=$ length of a minute of longitude of the earth at the equator, at the level of sea, as determined by U.S. Coast Survey.

3 knots = 1 league.

## SHIPPING MEASURE.

1 Register ton $=100$ cubic feet.
1 U . S. Shipping ton $=40$ cubic feet.
1 British Shipping ton $=42$ cubic feet.

## MEASURE OF WORK AND POWER.

A unit of work = one foot pound, or a pressure of one pound exerted through a space of one foot.

A British Thermal unit $=778$ foot pounds.

> 33,000 foot pounds per minute, 550 foot pounds per second, 42.42 heat units per minute, 0.707 heat units per second, 746 watts,
> 0.746 kilowatt.

## 'THE METRIC SYSTEM OF WEIGH'TS AND MEASURES.

In the Metric System, the Meter is the base of all the weights and measures which it employs.

The Meter is the primary unit of length and was intended to be one-ten millionth part of the distance, measured on a meridian of the earth, from the equator to the pole, and equals about 39.37 inches.

Upon the Meter are based the following primary units; the Square Meter the Are, the Cubic Meter or Stere the Liter, and the Gram.

The Square Meter or Centare is the unit of measure for small surfaces.

The Are is the unit of land measure ; this is a square whose side is ten meters in length, and which contains one hundred square meters or centares.

The Cubic Meter, or Stere, is the unit of volume; this is a cube whose edge is one meter in length.

The Liter is the unit of capacity; this is the capacity of a cube whose edge is one tenth of a meter, that is, one decimeter in length.

The Gram is the unit of weight ; this is the weight of distilled water at $4^{\circ}$ centigrade, contained in a cube whose edge is the one hundredth part of a meter.

From these primary units the higher and lower orders of units are derived decimally as follows:

Scheme of the Weights and Measures of the Metric System.

| Ratios | Lengths | Surfaces | Volumes | Weights |
| :---: | :---: | :---: | :---: | :---: |
| 1,000,000. |  |  |  | Millier, or Tonneau |
| $100,000$. 10,000 |  |  |  |  |
| 10,000. | Myr'iameter |  | Kii'oliter | Myr'iagram ${ }^{\text {Kil'ogram, or Kilo }}$ |
| 100. | Hec'tometer | Hect'are | Hec'toliter | Hec'togram |
| 10. | Dek'ameter |  | Dek'aliter | Dek'agram |
| 1.1 | Meter | Are | Li'ter | Gram |
| ${ }_{0.01}^{0.1}$ | Cen'timeter | Cen'tare | Dec' ${ }^{\text {ditiliter }}$ | Dec'igram |
| 0.001 | Mil'limeter |  | Mil'liliter | Mill'ligram |

It will be seen, from this table, that ten millimeters equal one centimeter, ten centimeters equal one decimeter, and so on.

Multiples and sub-multiples of the units, meter, liter and gram are expressed by the prefixes :

$$
\begin{array}{l|l}
\text { Deka }=10 & \text { Deci }=0.1 \\
\text { Hecto }=100 & \text { Centi }=0.01 \\
\text { Kilo }=1000 & \text { Milli }=0.001
\end{array}
$$

## ABBREVIATIONS COMMONLY IN USE.

mm, millimeter,
cm , centimeter,
dm, decimeter,
m , meter,
km, kilometer, $\mathrm{mm}^{2}$, square millimeter, $\mathrm{cm}^{2}$, " centimeter, dm ${ }^{2}$, " decimeter,
$\mathrm{m}^{2}$, square meter, $\mathrm{km}^{2}$ " kilometer, $\mathrm{mm}^{8}$, cubic millimeter, $\left.\mathrm{cm}^{8}\right\}$ " centimeter, $\mathrm{dm}^{3}$, " decimeter, $\mathrm{m}^{3}$, " meter,
a , are ; ha, hectare ; cl, centiliter; 1 , liter ; hl , hectoliter ; s, stere ; mg, milligram ; cg, centigram; g, gram; kg , kilo, or kilogram ; t , tonneau, or metric ton.

## MET'RIC AND U. S. CONVERSION TABLE.

$$
\begin{aligned}
& \text { MEASURES OF LENGTH. } \\
& \text { METRIC Tо U. S. } \\
& 1 \text { millimeter }=0.03937 \text { inch. } \\
& 1 \text { centimeter }=0.3937 \\
& 1 \text { meter }=39.37 \text { inches. } \\
& 1 \text { " }=3.2808 \text { feet. } \\
& 1 \text { kilometer }=0.6214 \text { mile. } \\
& \text { U. S. то METRIC. } \\
& 1 \text { inch }=25.4 \text { millimeters. } \\
& 1 \text { " }=2.54 \text { centimeters. } \\
& 1 \text { " }=0.254 \text { meter. } \\
& 1 \text { foot }=0.3048 \text { " } \\
& 1 \text { mile }=1.609 \text { kilometers. }
\end{aligned}
$$

## MEASURES OF SURFACE.

Metric to U.S.
1 sq. millimeter $=0.00155$ sq. inch.
1 " centimeter $=0.155$ " "
1 " meter $=10.764$ " feet.
1 " " $=1.196$ " yards.

1 hectare $=2.471$ acres.
1 " $=0.00386$ sq. mile.
1 sq. kilometer $=0.3861$ " '
U. S. to Metric.

1 sq. inch $=645.14$ sq. millimeters.
1 " " $=6.452$ " centimeters.

1 "foot $=0.0929$ " meter.
1 " yard = 0.8361 " "
$1 \quad$ acre $=0.4047$ hectares.
1 sq. mile $=259.00 \quad$ "
$1 " "=2.59$ sq. kilometers.

## MEASURES OF VOLUME AND CAPACITY.

Metric to U. S.

| 1 cu. centimeter | $=0.061 \mathrm{cu}$ inch. |  |
| :--- | :--- | :--- | :--- |
| 1 | " meter | $=35.316$ "، feet. |
| 1 | " | $=1.308$ " yards. | 1 liter $=1 \mathrm{cu}$. decimeter $=61.023 \mathrm{cu}$. inch.

LIQUID MEASURE.

| 1 liter | $=1.0567$ | quart. |
| :--- | :--- | :--- |
| 1 | " | 0.2642 |
| 1 gallon. |  |  |

DRY MEASURE.
1 liter $=0.908$ quart.
1 hectoliter $=2.8375$ bushels
U. S. to Metric.

1 cu. inch $=16.39 \mathrm{cu}$. centimeters.
1 " foot $=0.0283$ " meter.
1 " yard = 0.7645 " "
1 " foot $=28.32 \quad$ liters.
LIQUID MEASURE.
1 quart $=0.9463$ liter.
1 gallon $=3.7854$ liters.
1 " $=0.0038 \mathrm{cu}$. meter.

## DRY MEASURE.

1 quart $=1.1013$ litres.
1 bushel $=0.3524$ hectoliter.

## WEIGHTS.

Metric to U. S.
1 milligram $=0.0154$ grain.
1 gram $=15.432$ grains.
1 kilogram = 2.2046 lbs . (avoir.)
metric ton $=1.1023$ net tons.
1 " " $=0.9842$ gross ton.
U. S. to Metric.

| 1 grain | $=64.80$ milligrams. |  |
| :--- | :--- | :--- |
| 1 "" | $=0.0648$ gram. |  |
| 1 lb. (avoir.) | $=0.4536$ | kilogram. |
| 1 net ton | $=0.9076$ metric ton. |  |
| 1 gross ton | $=1.0161 \quad "$ tons. |  |

## COMPOUND UNITS.

## Metric to United States.

1 kilogram per meter $\quad=0.6720 \mathrm{lbs}$. per foot.
1 kilogram per sq. centimeter $=14.223 \mathrm{lbs}$. per sq. inch.
1 kilogram per sq. meter $\quad=0.2048 \mathrm{lbs}$. per sq. foot.
1 kilogram per cubic meter $=0.0624 \mathrm{lbs}$. per cubic ft .
1 kilogram-meter $\quad=7.233$ foot pounds.
1 chevel vapeur (metric H. P.) $=0.986$ horse-power.
1 kilo. watt
$=1.340$
1 kilo. per chevel
$=2.235 \mathrm{lbs}$. per H. P.

## United States to Metric.

1 lb . per foot $\quad=1.4882$ kilograms per meter.
1 lb . per sq. inch $=0.0703$ kilo. per sq. centimeter.
1 lb . per sq. foot $=4.8825$ kilograms per sq. meter.
1 lb . per cubic foot $=16.0192$ kilo. per cubic meter.
1 foot pound $\quad=0.1383$ kilogram-meter,
1 horse-power $=1.014$ chevel vapeur (metric H. P.)
1 " " $=0.746$ kilo watt.
1 lb . per horse-power $=0.447$ kilos per chevel.

## HEAT INTENSITY.

Temp. Centigrade $=\left(\right.$ temp. Fahr. $\left.-32^{\circ}\right) \frac{5}{9}$. Temp. Fahrenheit $=\left(\right.$ temp. C. $\left.\times \frac{9}{5}\right)+32^{\circ}$.

## HEAT QUANTITY.

A kilogram calorie $\quad=3.968$ British thermal units.
A pound calorie $=1.8$ " " "
A British thernal unit $=0.252$ kilogram calorie
A British thermal unit $=0.555$ pound calorie.

MECHANICAL, ELECTRICAL AND HEAT EQUIVALENTS.
(H. W. LEONARD.)

| Unit. | Equivalent Value in Other Units. |
| :---: | :---: |
| $\underset{\text { K. }}{\stackrel{1}{\mathrm{~W}} \mathrm{~W} .}$ | 1,000 watt hours. <br> 1.34 horse-power hours. <br> $2,654,200 \mathrm{ft}$.-lbs. <br> $3,600,000$ joules. <br> 3,412 heat units. <br> 367,000 kilogram metres. <br> 0.235 lb . carbon oxidized with perfect efficiency. <br> 3.53 lbs . water evaporated from and at $212^{\circ} \mathrm{F}$. <br> 22.75 lbs . of water raised from $62^{\circ}$ to $212^{\circ} \mathrm{F}$. |
| $\stackrel{1}{\text { H. P. }}=$ | 0.746 K. W. hours. <br> $1,980,000 \mathrm{ft}$.-lbs. <br> 2,545 heat-units. <br> $273,740 \mathrm{k} . \mathrm{g} . \mathrm{m}$. <br> 0.175 lb . carbon oxidized with perfect efficiency. <br> 2.64 lbs . water evaporated from and at $212^{\circ} \mathrm{F}$. <br> 17.0 1bs. water raised from $62^{\circ} \mathrm{F}$. to $212^{\circ} \mathrm{F}$. |
| $\stackrel{1}{\text { Kilowatt }}=$ | 1,000 watts. <br> 1.34 horse-power. <br> $2,654,200 \mathrm{ft}$.-lbs. per hour. <br> $44,240 \mathrm{ft}$.-1bs. per minute. <br> 737.3 ft .-1bs. per second. <br> 3,412 heat-units per hour. <br> 56.9 heat-units per minute. <br> 0.948 heat-unit per second. <br> 0.2275 lb . carbon oxidized per hour. <br> 3.53 lbs . water evaporated per hour from and at $212^{\circ} \mathrm{F}$. |

MECHANICAL, ELECTRICAL AND HEAT EQUIVALENTS.-(CONTINUED).

| Unit. | Equivalent Value in Other Units |
| :---: | :---: |
| H. $\stackrel{1}{\mathrm{P}} .=$ | 746 watts. <br> 0.746 K . W. <br> $33,000 \mathrm{ft}$. 1 lbs . per minute. <br> 550 ft .-1bs. per second. <br> 2,545 heat-units per hour. <br> 42.4 heat-units per minute. <br> 0.707 heat units per second. <br> 0.175 lbs . carbon oxidized per hour. <br> 2.64 lbs. water evaporated per hour from and at $212^{\circ} \mathrm{F}$. |
| $\stackrel{1}{\text { Joule }}=$ | $\begin{aligned} & 1 \text { watt second. } \\ & 0.000000278 \mathrm{~K} . \mathrm{W} . \text { hour. } \\ & 0.102 \mathrm{k} . \mathrm{g} . \mathrm{m} . \\ & 0.0009477 \text { heat-units. } \\ & 0.7373 \mathrm{ft} .-\mathrm{lb} \text {. } \end{aligned}$ |
| $\begin{gathered} 1 \\ \mathrm{Ft.-1b} . \end{gathered}$ | 1.356 joules. <br> 0.1383 k . g. m. <br> 0.000000377 K . W. hours. <br> 0.001285 heat-units. <br> 0.0000005 H . P. hour. |
| $\stackrel{1}{\text { Watt }}=$ | 1 joule per second. <br> 0.00134 H. P. <br> 3.412 heat-units per hour. <br> 0.7373 ft .-lb. per second. <br> 0.0035 lb . water evaporated per hour. <br> 44.24 ft .-lbs. per minute. |
| 1 Watt per sq. in. $=$ | 8.19 heat-units per square foot per minute. 6371 ft .-lbs. per square foot per minute. 0.193 H. P. per square foot. |

## MECHANICAL, ELECTRICAL AND HEAT EQUIVALENTS.-(CONTINUED).

| Unit. | Equivalent Value in Other Units. |
| :---: | :---: |
| 1 <br> Heat <br> unit. <br> $=$ | 1,055 watt seconds. <br> $778 \mathrm{ft} .-1 \mathrm{bs}$. <br> 107.6 kilogram metres. <br> 0.000293 K . W. hour. <br> 0.000393 H. P. hour. <br> 0.0000688 lb . carbon oxidized. <br> 0.001036 lb . water evaporated from and at $212^{\circ} \mathrm{F}$. |
| 1 Heatunit. per Sq.ft. per $\min .=$ | 0.122 watt per square inch. 0.0176 K . W. per square foot. 0.0236 H . P. per square foot. |
| 1 Kiloggram Metre $=$ | $7.233 \mathrm{ft} .-\mathrm{lbs}$. <br> 0.00000365 H. P. hour. <br> $0.00000272 \mathrm{~K} . \mathrm{W}$. hour. <br> 0.0093 heat-units. |
| 1 lb. Carbon Oxidized with perfect Efficiency | 14,544 heat-units. <br> 1.11 lb . Anthracite coal oxidized. <br> 2.5 lbs . dry wood oxidized. <br> 21 cubic feet illuminating-gas. <br> $4.26 \mathrm{~K} . \mathrm{W}$. hours. <br> 5.71 H. P. hours. <br> $11,315,000 \mathrm{ft} .-1 \mathrm{bs}$. <br> 15 lbs . of water evaporated from and at $212^{\circ} \mathrm{F}$. |
| 1 lb . Water Evaported from and at $212^{\circ} \mathrm{F}$. $=$ | 0.283 K. W. hour. 0.379 H. P. hour. 965.7 heat-units. $103,900 \mathrm{k} . \mathrm{g} . \mathrm{m}$. $1,019,000$ joules. 751,300 ft. -1 bs. 0.0664 lb. of carbon oxidized. |

## MENSURATION,

## TRIGONOMETRY

AND
MATHEMATICAL TABLES.

## MENSURATION, TRIGONOMETRY AND MATHEMATICAL TABLES.

## MENSURATION.

## Mensuration of Surfaces.

Area of any parallelogram $=$ base $\times$ perpendicular height.
" " " triangle $\ldots$. . $=$ base $\times 1 / 2$ perpendicular height.
" ، " circle $\ldots .$. . $=(\text { diameter })^{2} \times(0.7854$, or approx. 11/14.)
" " sector of circle.... $=\operatorname{arc} \times 1 / 2$ radius.
" " segment of circle $=$ area of sector of equal radius and arc less area of triangle.
" " parabola.......... $=$ base $\times 2 / 3$ height.
" " ellipse...... ..... $=$ longest diameter $\times$ shortest diameter $\times 0.7854$.
" " cycloid.......... $=$ area of generating circle $\times 3$.
" " any regular polygon $=$ sum of its sides $X$ perpendicular from its center to one of its sides $\div 2$.
Surface of cylinder........ $=$ area of both ends + (length $\times$ circumference.) " " cone.......... $=$ area of base + (circumference of base $\times 1 / 2$ slant height.)
" " sphere. ......... $=(\text { diameter })^{2} \times(3.1416$, or approx. 22/7.)
" " frustum........ $=$ (sum of girt at both ends $\times 1 / 2$ slant height) + area of both ends.

Surface of cylindrical ring $=$ thickness of ring added to the inner diameter $X$ by the thickness $\times 9.8698$. " " segment . . . . . . $=$ height of segment $\times$ by whole circumference of sphere of which it is a part.

## AREA OF AN IRREGULAR PLANE SURFACE.



Divide the surface into any number of parallel strips of equal widths, "d." Take the sum of the middle ordinates $h_{1}$, $h_{2}$, etc., to $h_{n}$, inclusive ; then the sum of these middle ordinates, multiplied by " $d$ " will give the area required.

The result, of course, is only approximate, the closeness of the approximation depending upon the number of strips into which the surface is divided.

Any degree of accuracy desired may be attained by making the number of strips sufficiently numerous. In practice it is usually best to determine the area of an irregular figure by the use of a planimeter, an instrument especially designed for measuring areas of plane figures.

## REGULAR POLYGONS.

1. To find the area of any regular polygon. Square one of its sides, and multiply this square by the corresponding number in the third column of the following table.
2. Having a side of a regular polygon, to find the radius of a circumscribing circle. Multiply the side by the corresponding number in the fourth column.
3. Having the radius of a circumscribing circle, to find the side of the inscribed regular polygon. Multiply the radius by the corresponding number in the fifth column.

## TABLE OF REGULAR POLYGONS.

| $\begin{aligned} & \dot{\ddot{0}} \\ & \dot{0} \\ & \dot{i n} \\ & \dot{0} \\ & \dot{8} \\ & \ddot{z} \end{aligned}$ | Name of Polygon. | $\underset{S^{2} X}{\text { Area }}=$ | $\begin{aligned} & \text { Radius } \\ & =S \times \end{aligned}$ | $\begin{aligned} & \text { Side }= \\ & \mathrm{R} \times \end{aligned}$ | Angle contained between two sides |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3 | $\left\{\begin{array}{c}\text { Equilateral } \\ \text { triangle }\end{array}\right\}$ | . 433 | . 5774 | 1.732 | $60^{\circ}$ |
| 4 | Square | 1. | . 7071 | 1.4142 | $90^{\circ}$ |
| 5 | Pentagon | 1.7205 | . 8507 | 1.1756 | $108^{\circ}$ |
| 6 | Hexagon | 2.5891 |  |  | $120^{\circ}$ |
| 7 | Heptagon | 3.6339 | 1.1524 | . 8678 | $128.57^{\circ}$ |
| 8 | Octagon | 4.8284 | 1.3066 | . 7654 | $135^{\circ}$ |
| 9 | Nonagon | 6.1818 | 1.4619 | . 684 | $140^{\circ}$ |
| 10 | Decagon | 7.6942 | 1.618 | . 618 | $144^{\circ}$ |
| 11 | Undecagon | 9.3656 | 1.7747 | . 5635 | $147.27^{\circ}$ |
| 12 | Dodecagon | 11.1962 | 1.9319 | . 5176 | $150^{\circ}$ |

In the above table $S=$ side of polygon and $R=$ radius of circumscribing circle.

## PROPERTIES OF THE CIRCLE.

Diameter $\times 3.1416=$ circumference.
" $\times 0.8862=$ side of an equivalent square.
" $\quad \times 0.7071=$ side of an inscribed square.
$(\text { Diameter })^{2} \times 0.7854=$ area of circle.
Radius $\quad \times 6.2832=$ circumference.
Circumference $\div 3.1416=$ diameter.
The circle contains a greater area than any plane figure, bounded by an equal perimeter, or outline.

The areas of circles are to each other as the squares of their diameter, radii or circumferences. Thus, a circle whose diameter is double that of another has four times the area of the other.

## VOLUMES OF SOLIDS.

Vol. of Cylinder . . . . . . . . . . $=$ area of one end $\times$ length.
" " Sphere. . . . . . . . . . $=$ cube of diameter $\times 0.5236$.
" " Segment of sphere $=$ (cube of the height + three times the square of radius of base $\times$ height) $\times$ 0.5236 .
" " Cone or pyramid... $=$ area of base $\times 1 / 3$ perpendicular height.
" " Frustum of cone... $=$ (product of diameter of both ends + sum of their squares) $\times$ perpendicular height $\times 0.2618$.
" " Frustum of pyramid $=$ (sum of the areas of the two ends + square root of their product) $\times$ by $1 / 3$ of the perpendicular height.
" "Wedge........... $=$ area of base $\times 1 / 2$ perpendicular height.
" "Frustum of wedge. . $=1 / 2$ perpendicular height $\times$ sum of the areas of the two ends.
" "Ring .............. $=$ (thickness + inner diameter) $\times$ square of the thickness $\times 2.4674$.

TRIGONOMETRICAL FORMULAE.


TRIGONOMETRICAL EQUIVALENTS.


## FUNCTIONS OF SUM AND DIFFERENCE OF TWO ANGLES.

$\operatorname{Sin}(x+y)=\sin x \cos y+\cos x \sin y$
$\operatorname{Sin}(x-y)=\sin x \cos y-\cos x \sin y$
$\operatorname{Cos}(x+y)=\cos x \cos y-\sin x \sin y$
$\operatorname{Cos}(x-y)=\cos x \cos y+\sin x \sin y$
$\operatorname{Tan}(x+y)=\frac{\tan x+\tan y}{1-\tan x \tan y}$
$\operatorname{Tan}(x-y)=\frac{\tan x-\tan y}{1+\tan x \tan y}$
$\operatorname{Cot}(x+y)=\frac{\cot x \cot y-1}{\cot x+\cot y}$
$\operatorname{Cot}(x-y)=\frac{\cot x \cot y+1}{\cot y-\cot x}$

## FUNCTIONS OF HALF AN ANGLE.

$$
\begin{aligned}
& \operatorname{Sin} 1 / 2 z= \pm \sqrt{\frac{1-\cos z}{2}} \\
& \operatorname{Tan} 1 / 2 z= \pm \sqrt{\frac{1-\cos z}{1+\cos z}} \\
& \operatorname{Cos} 1 / 2 z= \pm \sqrt{\frac{1-\cos z}{2}} \\
& \operatorname{Cot} 1 / 2 z= \pm \sqrt{\frac{1+\cos z}{1-\cos z}}
\end{aligned}
$$

## SUMS AND DIFFERENCES OF FUNCTIONS.

$\operatorname{Sin}(x+y)+\sin (x-y)=2 \sin x \cos y$
$\operatorname{Sin}(x+y)-\sin (x-y)=2 \cos x \sin y$
$\operatorname{Cos}(x+y)+\cos (x-y)=2 \cos x \cos y$
$\operatorname{Cos}(x-y)-\cos (x+y)=2 \sin x \sin y$

Then by making $(x+y)=A$ and $(x-y)=B$, we have $x=1 / 2(A+B)$ and $y=1 / 2(A-B)$, whence-
$\sin A+\sin B=2 \sin 1 / 2(A+B) \cos 1 / 2(A-B)$
$\sin A-\sin B=2 \cos 1 / 2(A+B) \sin 1 / 2(A-B)$
$\operatorname{Cos} A+\cos B=2 \cos 1 / 2(A+B) \cos 1 / 2(A-B)$
$\cos A-\cos B=2 \sin 1 / 2(A+B) \sin 1 / 2(A-B)$

$$
\begin{aligned}
& \frac{\operatorname{Sin} A+\sin B}{\operatorname{Sin} A-\sin B}=\frac{\tan 1 / 2(A+B)}{\tan 1 / 2(A-B)} \\
& \frac{\operatorname{Cos} A+\cos B}{\operatorname{Cos} A-\cos B}=\frac{\cot 1 / 2(A+B)}{\tan 1 / 2(A-B)}
\end{aligned}
$$

## SOLUTION OF RIGHT TRIANGLE.



Given $A$ and $c$, to find $B, a$ and $b$. $B=90^{\circ}-A ; A=c \sin A ; b=c \cos A$.

Given A and a , to find $\mathrm{B}, \mathrm{b}$ and c .

$$
B=90^{\circ}-A ; b=a \cot A ; c=\frac{a}{\sin A}
$$

Given $A$ and $b$, to find $B, a$ and $c$.
$B=90^{\circ}-A ; a=b \tan A ; c=\frac{b}{\cos A}$.
Given c and a , to find $\mathrm{A}, \mathrm{B}$ and b .
$\operatorname{Sin} A=\frac{a}{c} ; B=90^{\circ}-A ; b=a \cot A$.
Given a and b , to find $\mathrm{A}, \mathrm{B}$ and c .
$\operatorname{Tan} A=\frac{a}{b} ; \quad B=90^{\circ}-A ; c=\frac{a}{\sin A}$.

## SOLUTION OF OBLIQUE TRIANGLE.



LAW OF'SINES.

$$
\frac{a}{b}=\frac{\sin A}{\sin B} ; \quad \frac{b}{c}=\frac{\sin B}{\sin C} ; \quad \frac{a}{c}=\frac{\sin A}{\sin C}
$$

## LAW OF COSINES.

$$
\begin{aligned}
& a^{3}=b^{2}+c^{2}-2 b c \cos A \\
& b^{2}=a^{2}+c^{2}-2 a c \cos B \\
& c^{2}=a^{2}+b^{2}-2 a b \cos C
\end{aligned}
$$

## LAW OF TANGENTS.

$$
\begin{aligned}
& \frac{a-b}{a+b}=\frac{\tan 1 / 2(A-B)}{\tan 1 / 2(A+B)} \\
& \frac{a-c}{a+c}=\frac{\tan 1 / 2(A-C)}{\tan 1 / 2(A+C)} \\
& \frac{b-c}{b+c}=\frac{\tan 1 / 2(B-C)}{\tan 1 / 2(B+C)}
\end{aligned}
$$

Given $\mathrm{a}, \mathrm{A}$ and B , to find $\mathrm{C}, \mathrm{b}$ and c .

$$
C=180^{\circ}-(A+B) ; b=\frac{a \sin B}{\sin A} ; c=\frac{a \sin C}{\sin A}
$$

Given $\mathrm{a}, \mathrm{b}$ and A , to find $\mathrm{B}, \mathrm{C}$ and c .
$\sin \mathrm{B}=\frac{\mathrm{b} \sin \mathrm{A}}{\mathrm{a}} ; \mathrm{C}=180^{\circ}-(\mathrm{A}+\mathrm{B}) ; \mathrm{c}=\frac{\mathrm{a} \sin \mathrm{C}}{\sin \mathrm{A}}$

Given $\mathrm{a}, \mathrm{b}$ and C , to find $\mathrm{A}, \mathrm{B}$ and c .

$$
\begin{aligned}
& A=1 / 2(A+B)+1 / 2(A-B) \\
& B=1 / 2(A+B)-1 / 2(A-B)
\end{aligned}
$$

$c=\frac{b \sin C}{\sin B}$, or $=\frac{a \sin C}{\sin A}$, or $=\sqrt{a^{3}+b^{2}-2 a b \cos C}$.
Given $\mathrm{a}, \mathrm{b}$ and c , to find A, B and C.
$\operatorname{Sin} 1 / 2 A=\sqrt{\frac{(S-b)(S-c)}{b c}} ;$ in which $S=1 / 2(a+b+c)$;
$\operatorname{Cos} 1 / 2 \mathrm{~A}=\sqrt{\frac{\mathrm{S(S-a)}}{\mathrm{bc}}} ; \operatorname{Tan} 1 / 2 \mathrm{~A}=\sqrt{\frac{(\mathrm{S}-\mathrm{b})(\mathrm{S}-\mathrm{c})}{\mathrm{S}(\mathrm{S}-\mathrm{a})}} ;$

$$
\begin{aligned}
& \operatorname{Sin} 1 / 2 B=\sqrt{\frac{(S-a)(S-c)}{a c}} ; \\
& \operatorname{Sin} 1 / 2 C=\sqrt{\frac{(S-a)(S-b)}{a b}}
\end{aligned}
$$

$$
\operatorname{Cos} 1 / 2 \mathrm{~B}=\sqrt{\frac{\mathrm{S(S-b)}}{\mathrm{ac}}} ; \quad \operatorname{Cos} 1 / 2 \mathrm{C}=\sqrt{\frac{\mathrm{S(S-c}}{a b}} ;
$$

$\operatorname{Tan} 1 / 2 \mathrm{~B}=\sqrt{\frac{(\mathrm{S}-\mathrm{a})(\mathrm{S}-\mathrm{c})}{\mathrm{S}(\mathrm{S}-\mathrm{b})}} ;$
$\operatorname{Tan} 1 / 2 C=\sqrt{\frac{(S-a)(S-b)}{S(S-c)}}$.

## AREA OF A TRIANGLE.

Area $=1 / 2$ a $c \sin B$, that is, the area of a triangle equals $1 / 2$ the product of two sides multiplied by the sine of the included angle.

$$
\begin{gathered}
\text { Also area }=\sqrt{S(S-a)(S-b)(S-c)} \\
\text { Where } S=1 / 2(a+b+c)
\end{gathered}
$$

## MATHEMATICAL TABLES.

|  | SINE. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ¢ | $0^{\prime}$ | $10^{\prime}$ | $20^{\prime}$ | $30^{\prime}$ | $40^{\prime}$ | $50^{\prime}$ | $60^{\prime}$ |  |
| 0 | 0.00000 | 0.00291 | 0.00582 | 0.00873 | 0.01164 | 0.01454 | 0.01745 | 89 |
| 1 | 0.01745 | 0.02036 | 002327 | 0.02618 | 0.02908 | 0.03199 | 0.03490 | 88 |
| 2 | 0.03490 | 0.03781 | 0.04071 | 0.04362 | 0.04653 | 0.04943 | 0.05234 | 87 |
| 3 | 0.05234 | 0.05524 | 0.05814 | 0.06105 | 0.06395 | 0.06685 | 0.06976 | 86 |
| 4 | 0.06976 | 0.07266 | 0.07556 | 0.07846 | 0.08136 | 0.08426 | 0.08716 | 85 |
| 5 | 0.08716 | 0.09005 | 0.09295 | 0.09585 | 0.09874 | 0.10164 | 0.10453 | 84 |
| 6 | 0.10453 | 0.10742 | 0.11031 | 0.11320 | 0.11609 | 0.11898 | 0.12187 | 3 |
| 7 | 0.12187 | 0.12476 | 0.12764 | 0.13053 | 0.13341 | 0.13629 | 0.13917 | 2 |
| 8 | 0.13917 | 0.14205 | 0.14493 | 0.14781 | 0.15069 | 0.15356 | 0.15643 | 81 |
| 9 | 0.15643 | 0.15931 | 0.16218 | 0.16505 | 0.16792 | 0.17078 | 0.17365 | 80 |
| 10 | 0.17365 | 0.17651 | 0.17937 | 0.18224 | 0.18509 | 0.18795 | 0.19081 | 79 |
| 11 | 0.19081 | 0.19366 | 0.19652 | 0.19937 | 0.20222 | 0.20507 | 0.20791 | 78 |
| 12 | 0.20791 | 0.21076 | 0.21360 | 0.21644 | 0.21928 | 0.22212 | 0.22495 | 77 |
| 13 | 0.22495 | 0.22778 | 0.23062 | 0.23345 | 0.23627 | 0.23910 | 0.24192 | 76 |
| 14 | 0.24192 | 0.24474 | 0.24756 | 0.25038 | 0.25320 | 0.25601 | 0.25882 | 75 |
| 15 | 0.25882 | 0.26163 | 0.26443 | 0.26724 | 0.27004 | 0.27284 | 0.27564 | 74 |
| 16 | 0.27564 | 0.27843 | 0.28123 | 0.28402 | 0.28680 | 0.28959 | 0.29237 | 73 |
| 17 | 0.29237 | 0.29515 | 0.29798 | 0.30071 | 0.30348 | 0.30625 | 0.30902 | 72 |
| 18 | 0.30902 | 0.31178 | 0.31454 | 0.31730 | 0.32006 | 0.32282 | 0.32557 | 71 |
| 19 | 0.32557 | 0.32832 | 0.33106 | 0.33381 | 0.33655 | 0.33929 | 0.34202 | 70 |
| 20 | 0.34202 | 0.34475 | 0.34748 | 0.35021 | 0.35293 | 0.35565 | 0.35837 | 69 |
| 21 | 0.35837 | 0.36108 | 0.36379 | 0.36650 | 0.36921 | 0.37191 | 0.37461 | 68 |
| 2\% | 0.37461 | 0.37730 | 0.37999 | 0.38268 | 0.38537 | 0.38805 | 0.39073 | 67. |
| 23 | 0.39073 | 0.39341 | 0.39608 | 0.39875 | 0.40142 | 0.40408 | 0.40674 | 66 |
| 24 | 0.40674 | 0.40939 | 0.41204 | 0.41469 | 0.41734 | 0.41998 | 0.42262 | 65 |
| 25 | 0.42262 | 0.42525 | 0.42788 | 0.43051 | 0.43313 | 0.43575 | 0.43837 | 64 |
| $\stackrel{26}{ }$ | 0.43837 | 0.44098 | 0.44359 | 0.44620 | 0.44880 | 0.45140 | 0.45399 | 63 |
| 27 | 0.45399 | 0.45658 | 0.45917 | 0.46175 | 0.46433 | 0.46690 | 0.46947 | 62 |
| 28 | 0.46947 | 0.47204 | 0.47460 | 0.47716 | 0.47971 | 0.48226 | 0.48481 | 61 |
| 29 | 0.48481 | 0.48735 | 0.48989 | 0.49242 | 0.49495 | 0.49748 | 0.50000 | 60 |
| 30 | -0.50000 | 0.50252 | 0.50503 | 0.50754 | 0.51004 | 0.51254 | 0.51504 | 59 |
| 31 | 0.51504 | 0.51753 | 0.52002 | 0.52250 | 0.52498 | 0.52745 | 0.52992 | 58 |
| 32 | 0.52992 | 0.53238 | 0.53484 | 0.53730 | 0.53975 | 0.54220 | 0.54464 | 57 |
| 33 | 0.54464 | 0.54708 | 0.54951 | 0.55194 | 0.55436 | 0.55678 | 0.55919 | 56 |
| 34 | 0.55919 | 0.56160 | 0.56401 | 0.56641 | 0.56880 | 0.57119 | 0.57358 | 55 |
| 35 | 0.57358 | 0.57596 | 0.57833 | 0.58070 | 0.58307 | 0.58543 | 0.58779 | 54 |
| 36 | 0.58779 | 0.59014 | 0.59248 | 0.59482 | 0.59716 | 0.59949 | 0.60182 | 53 |
| 37 | 0.60182 | 0.60414 | 0.60645 | 0.60876 | 0.61107 | 0.61337 | 0.61566 | 52 |
| 38 | 0.61566 | 0.61795 | 0.62024 | 0.62251 | 0.62479 | 0.62706 | 0.62932 | 51 |
| 39 | 0.62932 | 0.63158 | 0.63383 | 0.63608 | 0.63832 | 0.64056 | 0.64279 | 50 |
| 40 | 0.64279 | 064501 | 0.64723 | 0.64945 | 0.65166 | 0.65386 | 0.65606 | 49 |
| 41 | 0.65606 | 0.65825 | 0.66044 | 0.66262 | 0.66480 | 0.66697 | 0.66913 | 48 |
| 42 | 0.66913 | 0.67129 | 0.67344 | 0.67559 | 0.67773 | 0.67987 | 0.68200 | 47 |
| 43 | 0.68200 | 0.68412 | 0.68624 | 0.68835 | 0.69046 | 0.69256 | 0.69466 | 46 |
| 44 | 0.69466 | 0.69675 | 0.69883 | 0.70091 | 0.70298 | 0.70505 | 0.70711 | 45 |
|  | $60^{\prime}$ | $50^{\prime}$ | $40^{\circ}$ | $30^{\prime}$ | $20^{\prime}$ | $10^{\prime}$ | $0^{\prime}$ | * |
|  |  |  |  | COSINE |  |  |  | $\stackrel{\circ}{\circ}$ |

MATHEMATICAL TABLES. (Continued.)

|  | COSINE. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| - | $0^{\prime}$ | $10^{\prime}$ | $20^{\prime}$ | $30^{\prime}$ | 40' | $50^{\prime}$ | $60^{\prime}$ |  |
| 0 | 1.00000 | 1.00000 | 0.99998 | 0.99996 | 0.99993 | 0.99989 | 0.99985 | 89 |
| 1 | 0.99985 | 0.99979 | 0.99973 | 0.99966 | 0.99958 | 0.99949 | 0.99939 | 88 |
| 2 | 0.99939 | 0.99929 | 0.99917 | 0.99905 | 0.99892 | 0.99878 | 0.99863 | 87 |
| 3 | 0.99863 | 0.99847 | 0.99831 | 0.99813 | 0.99795 | 0.99776 | 0.99756 | 86 |
| 4 | 0.99756 | 0.99736 | 0.99714 | 0.99692 | 0.99668 | 0.99644 | 0.99619 | 85 |
| 5 | 0.99619 | 0.99594 | 0.99567 | 0.99540 | 0.99511 | 0.99482 | 0.99452 | 84 |
| 6 | 0.99452 | 0.99421 | 0.99390 | 0.99357 | 0.99324 | 0.99290 | 0.99255 | 83 |
| 7 | 0.99255 | 0.99219 | 0.99182 | 0.99144 | 0.99106 | 0.99067 | 0.99027 | 82 |
| 8 | 0.99027 | 0.98986 | 0.98944 | 0.98902 | 0.98858 | 0.98814 | 0.98769 | 81 |
| 9 | 0.98769 | 0.98723 | 0.98676 | 0.98629 | 0.98580 | 0.98531 | 0.98481 | 80 |
| 10 | 0.98481 | 0.98430 | 0.98378 | 0.98325 | 0.98272 | 0.98218 | 0.98163 | 79 |
| 11 | 0.98163 | 0.98107 | 0.98050 | 0.97992 | 0.97934 | 0.97875 | 0.97815 | 78 |
| 12 | 0.97815 | 0.97754 | 0.97692 | 0.97630 | 0.97566 | 0.97502 | 0.97437 | 77 |
| 13 | 0.97437 | 0.97371 | 0.97304 | 0.97237 | 0.97169 | 0.97100 | 0.97030 | 76 |
| 14 | 0.97030 | 0.96959 | 0.96887 | 0.96815 | 0.96742 | 0.96667 | 0.96593 | 75 |
| 15 | 0.96593 | 0.96517 | 0.96440 | 0.96363 | 0.96285 | 0.96206 | 0.96126 | 74 |
| 16 | 0.96126 | 0.96046 | 0.95964 | 0.95882 | 0.95799 | 0.95715 | 0.95630 | 73 |
| 17 | 0.95630 | 0.95545 | 0.95459 | 0.95372 | 0.95284 | 0.95195 | 0.95106 | 72 |
| 18 | 0.95106 | 0.95015 | 0.94924 | 0.94832 | 0.94740 | 0.94646 | 0.94552 | 71 |
| 19 | 0.94552 | 0.94457 | 0.94361 | 0.94264 | 0.94167 | 0.94068 | 0.93969 | 70 |
| 20 | 0.93969 | 0.93869 | 0.93769 | 0.93667 | 0.93565 | 0.93462 | 0.93358 | 69 |
| 21 | 0.93358 | 0.93253 | 0.93148 | 0.93042 | 0.92935 | 0.92827 | 0.92718 | 68 |
| 22 | 0.92718 | 0.92609 | 0.92499 | 0.92388 | 0.92276 | 0.92164 | 0.92050 | 67 |
| 23 | 0.92050 | 0.91936 | 0.91822 | 0.91706 | 0.91590 | 0.91472 | 0.91355 | 66 |
| 24 | 0.91355 | 0.91236 | 0.91116 | 0.90996 | 0.90875 | 0.90753 | 0.90631 | 65 |
| 25 | 0.90631 | 0.90507 | 0.90383 | 0.90259 | 0.90133 | 0.90007 | 0.89879 | 64 |
| 26 | 0.89879 | 0.89752 | 0.89623 | 0.89493 | 0.89363 | 0.89232 | 0.89101 | 63 |
| 27 | 0.89101 | 0.88968 | 0.88835 | 0.88701 | 0.88566 | 0.88431 | 0.88295 | 62 |
| 28 | 0.88295 | 0.88158 | 0.88020 | 0.87882 | 0.87743 | 0.87603 | 0.87462 | 61 |
| 29 | 0.87462 | 0.87321 | 0.87178 | 0.87036 | 0.86892 | 0.86748 | 0.86603 | 60 |
| 30 | 0.86603 | 0.86457 | 0.86310 | 0.86163 | 0.86015 | 0.85866 | 0.85717 | 59 |
| 31 | 0.85717 | 0.85567 | 0.85416 | 0.85264 | 0.85112 | 0.84959 | 0.84805 | 58 |
| 32 | 0.84805 | 0.84650 | 0.84495 | 0.84339 | 0.84182 | 0.84025 | 0.83867 | 57 |
| 33 | 0.83867 | 0.83708 | 0.83549 | 0.83389 | 0.83228 | 0.83066 | 0.82904 | 56 |
| 34 | 0.82904 | 0.82741 | 0.82577 | 0.82413 | 0.82248 | 0.82082 | 0.81915 | 55 |
| 35 | 0.81915 | 0.81748 | 0.81580 | 0.81412 | 0.81242 | 0.81072 | 0.80902 | 54 |
| 36 | 0.80902 | 0.80730 | 0.80558 | 0.80386 | 0.80212 | 0.80038 | 0.79864 | 53 |
| 37 | 0.79864 | 0.79688 | 0.79512 | 0.79335 | 0.79158 | 0.78980 | 0.78801 | 52 |
| 38 | 0.78801 | 0.78622 | 0.78442 | 0.78261 | 0.78079 | 0.77897 | 0.77715 | 51 |
| 39 | 0.77715 | 0.77531 | 0.77347 | 0.77162 | 0.76977 | 0.76791 | 0.76604 | 50 |
| 40 | 0.76604 | 0.76417 | 0.76229 | 0.76041 | $0.75851$ | 0.75661 | 0.75471 | 49 |
| 41 | 0.75471 | 0.75280 | $0.75088$ | 0.74896 | $0.74703$ | $0.74509$ | $0.74314$ | 48 |
| 42 | 0.74314 | 0.74120 | $0.73924$ | $0.73728$ | $0.73531$ | $0.73333$ | $0.73135$ | 47 |
| 43 | 0.73135 | 0.72937 | 0.72737 | $0.72537$ | $0.72337$ | $0.72136$ | 0.71934 | 46 |
| 44 | 0.71934 | 0.71732 | 0.71529 | 0.71325 | 0.71121 | 0.70916 | 0.70711 | 45 |
|  | $60^{\prime}$ | $50^{\prime}$ | $40^{\prime}$ | $30^{\prime}$ | $20^{\prime}$ | $10^{\prime}$ | $0^{\prime}$ | ${ }_{8}$ |
|  |  |  |  | SINE. |  |  |  | ロٌ |

MATHEMATICAL TABLES. (continued.)

|  | TANGENT. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $0^{\prime}$ | $10^{\prime}$ | $20^{\prime}$ | $30^{\prime}$ | $40^{\prime}$ | $50^{\prime}$ | $60^{\prime}$ |  |
| 0 | 0.00000 | 0.00291 | 0.00582 | 0.00873 | 0.01164 | 0.01455 | 0.01746 | 89 |
| 1 | 0.01746 | 0.02036 | 0.02328 | 0.02619 | 0.02910 | 0.03201 | 0.03492 | 88 |
| 2 | 0.03492 | 0.03783 | 0.04075 | 0.04366 | 0.04658 | 0.04949 | 0.05241 | 87 |
| 3 | 0.05241 | 0.05533 | 0.05824 | 0.06116 | 0.06408 | 0.06700 | 0.06993 | 86 |
| 4 | 0.06993 | 0.07285 | 0.08578 | 0.07870 | 0.08163 | 0.08456 | 0.08749 | 85 |
| 5 | 0.08749 | 0.09042 | 0.09335 | 0.09629 | 0.09923 | 0.10216 | 0.10510 | 84 |
| 6 | 0.10510 | 0.10805 | 0.11099 | 0.11394 | 0.11688 | 0.11983 | 0.12278 | 83 |
| 7 | 0.12278 | 0.12574 | 0.12869 | 0.13165 | 0.13461 | 0.13758 | 0.14054 | 82 |
| 8 | 0.14054 | 0.14351 | 0.14648 | 0.14945 | 0.15243 | 0.15540 | 0.15838 | 81 |
| 9 | 0.15838 | 0.16137 | 0.16435 | 0.16734 | 0.17033 | 0.17333 | 0.17633 | 80 |
| 10 | 0.17633 | 0.17933 | 0.18233 | 0.18534 | 0.18835 | 0.19136 | 0.19438 | 79 |
| 11 | 0.19438 | 0.19740 | 0.20042 | 0.20345 | 0.20648 | 0.20952 | 0.21256 | 78 |
| 12 | 0.21256 | 0.21560 | 0.21864 | 0.22169 | 0.22475 | 0.22781 | 0.23087 | 77 |
| 13 | 0.23087 | 0.23393 | 0.23700 | 0.24008 | 0.24316 | 0.24624 | 0.24933 | 76 |
| 14 | 0.24933 | 0.25242 | 0.25552 | 0.25862 | 0.26172 | 0.26483 | 0.26795 | 75 |
| 15 | 0.26795 | 0.27107 | 0.27419 | 0.27732 | 0.28046 | 0.28360 | 0.28675 | 74 |
| 16 | 0.28675 | 0.28990 | 0.29305 | 0.29621 | 0.29938 | 0.30255 | 0.30573 | 73 |
| 17 | 0.30573 | 0.30891 | 0.31210 | 0.31530 | 0.31850 | 0.32171 | 0.32492 | 72 |
| 18 | 0.32492 | 0.32814 | 0.33136 | 0.33460 | 0.33783 | 0.34108 | 0.34433 | 71 |
| 19 | 0.34433 | 0.34758 | 0.35085 | 0.35412 | 0.35740 | 0.36068 | 0.36397 | 70 |
| 20 | 0.36397 | 0.36727 | 0.37057 | 0.37388 | 0.37720 | 0.38053 | 0.38386 | 69 |
| 21 | 0.38386 | 0.38721 | 0.39055 | 0.39391 | 0.39727 | 0.40065 | 0.40403 | 68 |
| 22 | 0.40403 | 0.40741 | 0.41081 | 0.41421 | 0.41763 | 0.42105 | 0.42447 | 67 |
| 23 | 0.42447 | 0.42791 | 0.43136 | 0.43481 | 0.43828 | 0.44175 | 0.44523 | 66 |
| 24 | 0.44523 | 0.44872 | 0.45222 | 0.45573 | 0.45924 | 0.46277 | 0.46631 | 65 |
| 25 | 0.46631 | 0.46985 | 0.47341 | 0.47698 | 0.48055 | 0.48414 | 0.48773 | 64 |
| 26 | 0.48773 | 0.49134 | 0.49495 | 0.49858 | 0.50222 | 0.50587 | 0.50953 | 63 |
| 27 | 0.50953 | 0.51320 | 0.51688 | 0.52057 | 0.52427 | 0.52798 | 0.53171 | 62 |
| 28 | 0.53171 | 0.53545 | 0.53920 | 0.54296 | 0.54673 | 0.55051 | 0.55431 | 61 |
| 29 | 0.55431 | 0.55812 | 0.56194 | 0.56577 | 0.56962 | 0.57348 | 0.57735 | 60 |
| 30 | 0.57735 | 0.58124 | 0.58513 | 0.58905 | 0.59297 | 0.59691 | 0.60086 | 59 |
| 31 | 0.60086 | 0.60483 | 0.60881 | 0.61280 | 0.61681 | 0.62083 | 0.62487 | 58 |
| 32 | 0.62487 | 0.62892 | 0.63299 | 0.63707 | 0.64117 | 0.64528 | 0.64941 | 57 |
| 33 | 0.64941 | 0.65355 | 0.65771 | 0.66189 | 0.66608 | 0.67028 | 0.67451 | 56 |
| 34 | 0.67451 | 0.67875 | 0.68301 | 0.68728 | 0.69157 | 0.69588 | 0.70021 | 55 |
| 35 | 0.70021 | 0.70455 | 0.70891 | 0.71329 | 0.71769 | 0.72211 | 0.72654 | 4 |
| 36 | 0.72654 | 0.73100 | 0.73547 | 0.73996 | 0.74447 | 0.74900 | 0.75355 | 53 |
| 37 | 0.75355 | 0.75812 | 0.76272 | 0.76733 | 0.77196 | 0.77661 | 0.78129 | 52 |
| 38 | 0.78129 | 0.78598 | 0.79079 | 0.79544 | 0.80020 | 0.80498 | 0.80978 | 51 |
| 39 | 0.80978 | 0.81461 | 0.81946 | 0.82434 | 0.82923 | 0.83415 | 0.83910 | 50 |
| 40 | 0.83910 | 0.84407 | 0.84906 | 0.85408 | 0.85912 | 0.86419 | 0.86929 | 49 |
| 41 | 0.86929 | 0.87441 | 0.87955 | 0.88473 | 0.88992 | 0.89515 | 0.90040 | 48 |
| 42 | 0.90040 | 0.90569 | 0.91099 | 0.91633 | 0.92170 | 0.92709 | 0.93252 | 47 |
| 43 | 0.93252 | 0.93797 | 0.94345 | 0.94896 | 0.95451 | 0.96008 | 0.96569 | 46 |
| 44 | 0.96569 | 0.97133 | 0.97700 | 0.98270 | 0.98843 | 0.99420 | 1.00000 | 45 |
|  | $60^{\prime}$ | $50^{\prime}$ | 40 | $30^{\prime}$ | $20^{\prime}$ | $10^{\prime}$ | $0^{\prime}$ |  |
|  | COTANGENT. |  |  |  |  |  |  | - |

## MA'THEMATICAL TABLES. (continued.)

|  | COTANGENT. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Q | $0 \times$ | $10^{\prime}$ | $20^{\prime}$ | $30^{\prime}$ | $40^{\prime}$ | $50^{\prime}$ | $60^{\prime}$ |  |
| 0 | $\infty$ | $\overline{343.77371}$ | $\overline{171.88540}$ | 114.58865 | 85.93979 | 68.75009 | $\overline{57.28996}$ | 89 |
| 1 | 57.28996 | 49.10388 | 42.96408 | 38.18846 | 34.36777 | 31.24158 | 28.63625 | 88 |
| 2 | 28.63625 | 26.43160 | 24.54176 | 22.90377 | 21.47040 | 20.20555 | 19.08114 | 87 |
| 3 | 19.08114 | 18.07498 | 17.16934 | 16.34986 | 15.60478 | 14.92442 | 14.30067 | 86 |
| 4 | 14.30067 | 13.72674 | 13.19688 | 12.70621 | 12.25051 | 11.82617 | 11.43005 | 85 |
| 6 | 11.43005 | 11.05943 | 10.71191 | 10.38540 | 10.07803 | 9.78817 | 9.51436 | 84 |
| 6 | 9.51436 | 9.25530 | 9.00983 | 8.77689 | 8.55555 | 8.34496 | 8.14435 | 83 |
| 7 | 8.14435 | 7.95302 | 7.77035 | 7.59575 | 7:42871 | 7.26873 | 7.11537 | 82 |
| 8 | 7.11537 | 6.96823 | 6.82694 | 6.69116 | 6.56055 | 6.43484 | 6.31375 | 81 |
| 9 | 6.313\% | 6.19703 | 6.08444 | 5.97576 | 5.87080 | 5.76937 | 5.67128 | 80 |
| 10 | 5.67128 | 5.57638 | 5.48451 | 5.39552 | 5.30928 | 5.22566 | 5.14455 | 79 |
| 11 | 5.14455 | 5.06584 | 4.98940 | 4.91516 | 4.84300 | 4.77286 | 4.70463 | 78 |
| 12 | 4.70463 | 4.63825 | 4.57363 | 4.51071 | 4.44942 | 4.38969 | 4.33148 | 77 |
| 13 | 4.33148 | 4.27471 | 4.21933 | 4.16530 | 4.11256 | 4.06107 | 4.01078 | 76 |
| 14 | 4.01078 | 3.96165 | 3.91364 | 3.86671 | 3.82083 | 3.77595 | 3.73205 | 75 |
| 15 | 3.73205 | 3.68909 | 3.64705 | 3.60588 | 3.56557 | 3.52609 | 3.48741 | 74 |
| 16 | 3.48741 | 3.44951 | 3.41236 | 3.37594 | 3.34023 | 3.30521 | 3.27085 | 73 |
| 17 | 3.27085 | 3.23714 | 3.20406 | 3.17159 | 3.13972 | 3.10842 | 3.07768 | 72 |
| 18 | 3.077 ${ }^{\circ} 8$ | 3.04749 | 3.01783 | 2.98869 | 2.96004 | 2.93189 | 2.90421 | 71 |
| 19 | 2.90421 | 2.87700 | 2.85023 | 2.82391 | 2.79802 | 2.77254 | 2.74748 | 70 |
| 20 | 2.74748 | 2.72281 | 2.69853 | 2.67462 | 2.65109 | 2.62791 | 2.60509 | 69 |
| 21 | 2.60509 | 2.58261 | 2.56046 | 2.53865 | 2.51715 | 2.49597 | 2.47509 | 68 |
| 22 | 2.47509 | 2.45451 | 2.43422 | 2.41421 | 2.39449 | 2.37504 | 2.35585 | 67 |
| 23 | 2.35585 | 2.33693 | 2.31826 | 2.29984 | 2.28167 | 2.26374 | 2.24604 | 66 |
| 24 | 2.24604 | 2.22857 | 2.21132 | 2.19430 | 2.17749 | 2.16090 | 2.14451 | 65 |
| 25 | 2.14451 | 2.12832 | 2.11233 | 2.09654 | 2.08094 | 2.06553 | 2.05030 | 64 |
| 26 | 2.05030 | 2.03526 | 2.02039 | 2.00569 | 1.99116 | 1.97680 | 1.96261 | 63 |
| 27 | 1.96261 | 1.94858 | 1.93470 | 1.92098 | 1.90741 | 1.89400 | 1.88073 | 62 |
| 28 | 1.88073 | 1.86760 | 1.85462 | 1.84177 | 1.82906 | 1.81649 | 1.80405 | 61 |
| 29 | 1.80405 | 1.79174 | 1.77955 | 1.76749 | 1.75556 | 1.74375 | 1.73205 | 60 |
| 30 | 1.73205 | 1.72047 | 1.70901 | 1.69766 | 1.68643 | 1.67530 | 1.66428 | 59 |
| 31 | 1.66428 | 1.65337 | 1.64256 | 1.63185 | 1.62125 | 1.61074 | 1.60033 | 58 |
| 32 | 1.60033 | 1.59002 | 1.57981 | 1.56969 | 1.55966 | 1.54972 | 1.53987 | 57 |
| 33 | 1.53987 | 1.53010 | 1.52013 | 1.51084 | 1.50133 | 1.49190 | 1.48256 | 56 |
| 34 | 1.48256 | 1.47330 | 1.46411 | 1.45501 | 1.44598 | 1.43703 | 1.42815 | 55 |
| 35 | 1.42815 | 1.41934 | 1.41061 | 1.40195 | 1.39336 | 1.38484 | 1.37638 | 54 |
| 36 | 1.37638 | 1.36800 | 1.35968 | 1.35142 | 1.34323 | 1.33511 | 1.32704 | 5 |
| 37 | 1.32704 | 1.31904 | 1.31110 | 1.30323 | 1.29541 | 1.28764 | 1.27994 | 5 |
| 38 | 1.27994 | 1.2'230 | 1.26471 | 1.25717 | 1.24969 | 1.24227 | 1.23490 | 51 |
| 39 | 1.23490 | 1.22758 | 1.22031 | 1.21310 | 1.20593 | 1.19882 | 1.19175 | 50 |
| 40 | 1.19175 | 1.18474 | 1.17777 | 1.17085 | 1.16398 | 1.15715 | 1.15037 | 49 |
| 41 | 1.15037 | 1.14363 | 1.13694 | 1.13029 | 1.12369 | 1.11713 | 1.11061 | 48 |
| 42 | 1.11061 | 1.10414 | 1.09770 | 1.09131 | 1.08496 | 1.07864 | 1.07237 | 47 |
| 43 | 1.07237 | 1.06613 | 1.05994 | 1.05378 | 1.04766 | 1.04158 | 1.03553 | 46 |
| 44 | 1.03553 | 1.02952 | 1.02355 | 1.01761 | 1.01170 | 1.00583 | 1.00060 | 45 |
|  | $60^{\prime}$ | $50^{\prime}$ | $40^{\prime}$ | $30^{\prime}$ | $20^{\prime}$ | $10^{\prime}$ | $0^{\prime}$ | ¢ |

CIRCUMFERENCES AND AREAS OF CIRCLES. Diameter from $\frac{1}{84}$ to 100 , advancing chiefly by Eighths.

| Diam. | Circum. | Area. | Diam. | Circum. | Area. | Diam. | Circum. | Area. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \frac{1}{64} \\ & \frac{1}{3 / 2} \\ & \frac{1}{3} \\ & 64 \\ & \frac{1}{18} \\ & \frac{18}{38} \\ & 1 / 8 \\ & 1 / 8 \\ & \frac{6}{32} \\ & 18 \\ & 17 \\ & 32 \end{aligned}$ | . 04909 | . 00019 |  | 6.6759 | 3.5466 | 5. ${ }^{7}$ | 17.08217.279 | 23.221 |
|  | . 09818 | . 00077 |  | 6.8722 | 3.7583 |  |  | 23.758 |
|  | .147\%6 | . 00173 |  | 7.0686 | 3.9761 | 9 | 17.475 | 24.301 |
|  | . 19635 | . 00307 |  | 7.2649 | 4.2000 |  | 17.671 | 24.850 |
|  | . $2945 \%$ | . 00690 |  | 7.4613 | 4.4301 |  | 17.868 | 25.406 |
|  | . 39270 | .01227 |  | 7.6576 | 4.6664 |  | 18.064 | 25.967 |
|  | . 49087 | . 01917 |  | 7.8540 | 4.9087 |  | 18.261 | 26.535 |
|  | . 58905 | . 02761 |  | 8.0503 | 5.1572 |  | 18.457 | 27.109 |
|  | . 68722 | . 03758 |  | 8.2467 | 5.4119 | $\frac{16}{16}$ | 18.653 | 27.688 |
| $\begin{aligned} & 1 / 4 \\ & \frac{1}{4} \\ & \frac{9}{3} \\ & \frac{1}{6} \\ & \frac{1}{3} \frac{1}{2} \\ & 3, \\ & \frac{18}{3} \\ & \frac{7}{7} \\ & \frac{1}{3} \frac{5}{2} \end{aligned}$ | . 78 | . 04909 |  |  | 5.6727 |  | 18.850 | 28.274 |
|  | . 888357 | . 06213 |  | ${ }_{8.8357}$ | 6.2126 | 1 | 19.242 |  |
|  | . 98175 | . 07670 |  | $\begin{aligned} & 9.0321 \\ & 9.22 \times 4 \end{aligned}$ | $\begin{aligned} & 6.4918 \\ & 6.7771 \end{aligned}$ | $1 / 4$ | 19.635 | 30.680 |
|  | 1.0799 | . 09281 |  |  |  | 3/8 | 20.028 | 31.919 |
|  | 1.1781 | . 11045 |  |  |  |  | 20.813 | 33.183 |
|  | 1.2763 | . 12962 | 3. | 9.4248 | 7.0686 | 58 |  | 34.4\%2 |
|  | 1.3744 | . 15033 | ${ }^{\frac{1}{16}}$ | 9.6211 | 7.3662 | $3 / 4$ | 21.206 | 35.785 |
|  | 1.4726 | . 17257 | $1 / 8$1818 | 9.8175 | 7.6699 | 278 | 21.598 | 37.122 |
|  |  |  |  | 10.014 | 7.97988.2958 |  |  |  |
|  | 1.5708 | . 19635 | 14 | 10.210 |  | 7. | 21.991 | 38.485 |
|  | 1.6690 | . 22166 | 5 | 10.407 |  |  | 22.384 | 39.871 |
|  | 1.7671 | . 24850 | 988 | 10.603 | 8.6179 8.9462 | $\begin{aligned} & 18 \\ & 34 \\ & 38 \end{aligned}$ | 22.776 | 41.28242.718 |
|  | 1.8653 | . 27688 |  | 10.799 | 9.2806 |  | 23.169 |  |
|  | 1.9635 | . 30680 | 12 | 10.996 | 9.6211 | $\begin{aligned} & 3 / 8 \\ & 1 / 2 \\ & \hline \end{aligned}$ | 23.562 | 42.718 44.179 |
|  | 2.0617 | . 33824 |  | 11.192 | 9.9678 | $\begin{aligned} & 1 / 2 \\ & 5 \\ & 3 / 8 \end{aligned}$ | 23.955 | 45.664 |
|  | 2.1598 | . 37122 | 58 | 11.388 | 10.321 |  | 24.347 | $\begin{aligned} & 47.173 \\ & 48.707 \end{aligned}$ |
|  | 2.2580 | . 40574 |  | $11.585$ | 10.680 | 748 | 24.740 |  |
|  | 2.3562 | . 44179 |  | $\begin{aligned} & 11.781 \\ & 11.977 \end{aligned}$ | 11.045 | 8. | 25.133 |  |
|  | 2.4541 | . 479378 |  | 12.174 | 11.793 | $\begin{aligned} & 1 / 8 \\ & 1 / 4 \\ & 3 \end{aligned}$ | 25.525 | 50.265 51.849 |
|  | 2.5525 |  |  | 12.370 | 12.177 |  | 25.918 | 53.45655.088 |
|  | 2.6507 | $\begin{array}{r} .51849 \\ .55914 \end{array}$ | ${ }^{18}$ |  |  |  |  |  |
|  | 2.7489 | . 60132 | 4. | 12.566 | 12.56612.962 | $\begin{aligned} & 34 \\ & 38 \\ & 16 \end{aligned}$ | 26.704 | 56.745 |
|  | 2.8471 | .64504.69029 |  | $\begin{aligned} & 12.763 \\ & 12.959 \end{aligned}$ |  | $18$ | 27.09627.489 | $58.426$ |
|  | 2.9452 |  |  |  | 13.364 | $\begin{aligned} & 5 \% \\ & 5 \\ & 3 \end{aligned}$ |  | $\begin{array}{r} 60.132 \end{array}$ |
|  | 3.0434 | . 73708 |  | $\begin{aligned} & 13.155 \\ & 13.352 \end{aligned}$ | $\begin{aligned} & 13.772 \\ & 14.186 \end{aligned}$ | 78 | 27.882 | $61.862$ |
| 1. |  | . 7854 |  |  |  |  |  |  |
|  |  |  | \% 8 | 13.548 | 14.607 |  | ${ }_{28} 8.267$ | 63.617 |
|  | 3.5343 | .8866 .9940 |  | 13.744 | 15.033 |  | 28.667 | $\begin{aligned} & 65.397 \\ & 67.201 \end{aligned}$ |
|  | 3.7306 | $\begin{aligned} & 1.1075 \\ & 1.2272 \end{aligned}$ | $\begin{aligned} & 98 \\ & 78 \\ & 1 / 2 \\ & 18 \end{aligned}$ | 14.13714.334 | 15.904 | 148888 | 29.452 |  |
|  | 3.9270 |  | $\begin{aligned} & 2, \\ & \hline 18 \\ & \hline 18 \end{aligned}$ |  | 16.349 | $\begin{aligned} & 1 / 5_{8} \\ & \hline \end{aligned}$ | 29.845 | 70.882 |
|  | 4.1233 | $\begin{aligned} & 1.2272 \\ & 1.3530 \end{aligned}$ | 5\% | 14.53014.726 | 16.800 |  | 30.238 | .760 |
|  | 4.3197 | 1.4849 |  |  | 17.257 | 3 | 30.631 |  |
|  | 4.5160 | 1.6230 |  | 14.923 | 17.728 | 78 | 31.023 | 76.589 |
|  | 4.7124 | 1.7671 |  | 15.119 | 18.190 |  |  |  |
|  | 4.9087 | 1.9175 |  | 15.315 | 18.665 | 10 | 31.416 | 78.540 |
|  | 5.1051 | 2.0739 | 8 | 15.512 | 19.147 | $1 /$ | 31.809 | 80.516 |
|  | 5.3014 | 2.2365 |  |  |  |  | 32.201 | 82.516 |
|  | 5.4978 | 2.4053 |  | 15.708 | 19.635 |  | 32.594 | 84.541 |
|  | 5.6941 | 2.5802 |  | 15.904 | 20.129 |  | 32.987 | 86.590 |
|  | 58905 | 2.7612 |  | 16.101 | 20.629 |  | 33.379 | 88.664 |
|  | 6.0868 | 2.9483 |  | 16.297 | 21.135 |  | 33.772 | 90.763 |
|  |  |  |  | 16.493 | 21.648 | 0 | 34.165 | 92.886 |
| 2. | 6.2832 | 3.1416 |  | 16.690 | 22.166 |  |  |  |
| ${ }_{18}^{18}$ | 6.4795 | 33410 | 3/8 | 16.886 | 22.691 | 11. | 34.558 | 95.038 |

CIRCUMFERENCES AND AREAS OF CIRCLES. (CONTINUED.)


CIRCUMFERENCES AND AREAS OF CIRCLES.
(CONTINUED.)


CIRCUMFERENCES AND AREAS OF CIRCLES.
(CONTINUED.)


## CIRCUMFERENCES AND AREAS OF CIRCLES.

(CONTINUED.)

| Diam. | Circum. | Area. | Diam. | Circum. | Area. | Diam. | Circum. | Area. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 67.14 $3 / 8$18883878 | 211.272 | 3552.0 |  | 230.907 | 4242.9 | $\begin{array}{r} 79.34 \\ 78 \end{array}$ | 250.542 | 4995.2 |
|  | 211.665 | 3565.2 |  | 231.300 | 4257.4 |  | 250.935 | 5010.9 |
|  | 212.058 | 3578.5 |  | 231.692 | 4271.8 |  |  |  |
|  | 212.450 | 3591.7 |  | 232.085 | 4286.3 |  | 251.327 | 5026.5 |
|  | 212.843 | 3605.0 |  |  |  |  | 251.720 | 5042.3 |
|  | 213.236 | 1/8 | $\begin{gathered} 1 / 8 \\ 14 \\ 38 \\ 18 \\ 19 \\ 58 \\ 3 \\ 74 \\ 78 \end{gathered}$ | 232.871 | 4300.8 | 14 | 252.113 | 5058.0 |
|  |  |  |  |  | 4315.4 |  | 252.506 | 5073.8 |
|  | 213.62 | 3631.7 |  | 233.263 | 4329.9 |  | 252.898 | 5089.6 |
|  | 214.021 | 3645.0 |  | 233.656 | 4344.5 |  | 253.291 | 5105.4 |
|  | 214.414 | 3658.4 |  | 234.049 | 4359.2 |  | 253.684 | 5121.2 |
|  | 214.806 | 3671.8 |  | 234.441 | 4373.8 | 8 | 254.076 | 5137.1 |
|  | 215.199 | 8685.3 |  | 234.834 | 4388.5 |  |  |  |
|  | 215.592 | 3698.7 |  | 235.227 | 4403.1 | 81. | 254.469 | 5153.0 |
|  | 215.984 | 3712.2 | 75. |  |  |  | 254.862 | 5168.9 |
|  | 216.377 | 3725.7 |  | 235.619 | 4417 |  | 255.254 | 5184.9 |
| 69. |  |  | $1 / 4$ | 236.012 236.405 | 4432.6 | 2 | 255.647 | 5200.8 |
|  | 217.16 | 3752.8 | $\begin{aligned} & 348 \\ & 3 \\ & 18 \end{aligned}$ | 236.798 | 4462.2 | 58 | 256.433 | 5216.8 |
|  | 217.555 | 3766.4 |  | 237.190 | 4477.0 |  | 256.825 | 5248.95264.9 |
|  | 217.948 | 3780.0 |  | 237.583 | 4491.8 | 78 | 257.218 |  |
|  | 218.34 | 3793.7 | 78 | 237.976 | 4506.7 | 82 |  | $5264.9$ |
|  | 218.733 | 3807.8 |  | 238.368 | 4521.5 |  | 1 | 5281.0 |
|  | 219.126 | 3821.0 |  |  |  |  |  | 5297 |
|  | 219.519 |  | 76. | 238 | 45 |  | 258.396 | 5313.35329.4 |
|  |  |  | $\begin{aligned} & 1 / 8 \\ & 1 / 4 \\ & 8 / 8 \\ & 1 / \\ & 5 / 8 \\ & 3 / 4 \\ & 78 \end{aligned}$ | 239.154 | 4551.4 | \% 18 | 258.789 |  |
|  | 219.911 | 3848. |  | 239.546 | 4566.4 |  | 259.181 | 5345.6 |
|  | 220.304 | 38622 |  | 239.939 | 4581.3 |  | 259.574 | 5361.8 |
|  | 220.697 | 3876.0 |  | 240.332 | 4596.3 | 38 | 259.967 | 5378.1 |
|  | 221.090 | 3889.8 |  | 240.725 | 4611.4 |  | 260.359 | 5394.3 |
|  | 221.482 | 3903.6 |  | 241.117 | 4626.4 |  |  |  |
|  | 221.875 | 3917.5 |  | 241.510 | 4641.5 |  | 260.752 | 5410.6 |
|  | 222.268 | 3931.4 |  |  |  |  | 261.145 | 5426.9 |
|  | 222.660 |  | 77 | 241.903 | 465 | 14 | 261.538 |  |
| 71. |  |  | $11 / 4$ | 242.295 | 4671.8 |  | 261.930262.323 | 5459.6 |
|  |  | 3959.2 |  | 242.68 | 4686.9 | \% |  | 5476.0 |
|  | 223.44 | 3973.1 | 1 | 243.081 | 4702.1 |  | 262.716 | 5492.4 |
|  | 223.838 | 3987.1 |  | 243.473 | 4717.3 |  | 263.108 | 5508.8 |
|  | 224.231 | 4001.1 | 5\% | 243.866 | 4732.5 | 78 | 263.501 | 5525.3 |
|  | 224.624 | 4015.2 |  | 244.259 | 4747.8 |  |  |  |
|  | $\stackrel{225.017}{225}$ | 4029.2 4043.3 | 78 | 244.65 | 4763.1 |  | 264.286 | 5541.8 |
| 8 | 225.802 | 4057.4 |  | 245.0 | 4778 |  | $\begin{aligned} & 264.679 \\ & 265.072 \end{aligned}$ | $\begin{aligned} & 5558.3 \\ & 5574.8 \end{aligned}$ |
|  |  |  | $\begin{aligned} & 1 / 8 \\ & 1 / 4 \end{aligned}$ | 245.437 | 4793.7 |  |  | 5591.45607.9 |
|  | 226.19 | 4071 |  | 245.830 | 4809.0 | 8 | 265.465 |  |
|  | 226.58 | 4085.7 |  | 246.222 | 4824.4 |  | 265.857 | 5607.9 5624.5 |
|  | 226.980 | 4099.8 |  | 246.615 | 4839.8 | 88 | 266.250 | $\begin{aligned} & 5641.2 \\ & 5657.8 \end{aligned}$ |
|  | 227.373 | 4114.0 |  | 247.008 | 4855.2 |  | 266.643 |  |
|  | 227.765 | 4128.2 |  | 247.400 | 4870.7 |  |  |  |
|  | 228.158 | 4142.5 | 78 | 247.793 | 4886 |  | 267.035 | 5674.55691.2 |
|  | 228.551 | 4156.8 |  |  |  |  | 267.428 |  |
| 73. $1 / 8$$1 / 4$$3 / 8$ | 228.94 | 4171 | 79. |  | $4901.7$ |  | 267.821 | 5707.9 5724.7 |
|  | 229.33 |  |  | 248.971 | 4932.7 |  |  | 5741.5 5758.3 <br> 5775.1 5791.9 |
|  | 229.729 |  |  | 249.364 | 4948.3 |  |  |  |
|  | 230.122 |  |  | 249.757 | 4963.9 |  |  |  |
|  | 230.51 |  |  | 250.149 | 4979.5 |  |  |  |

CIRCUMFERENCES AND AREAS OF CIRCLES.
(CONTINUED.)

| am | Circum | Area. | Diam. | Circu | Area. | Diam. | Circum. | Area. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 86. $1 / 8$18$3 / 8$18$5 / 8$3343 | 270.17 | 5808.8 | 90.7/8 | 285.492 | 6486.0 | $\begin{array}{r} 95.5 / 8 \\ 34 \\ 7 / 8 \end{array}$ | 300.415 | 7181.8 |
|  | 270.570 | 5825.7 |  |  |  |  | 300.807 | 7200.6 |
|  | 270.962 | 5842.6 |  | 285.885 | 6503.9 |  | 301.200 | 7219.4 |
|  | 271.35 | 5859.6 |  | 286.278 | 6521.8 |  |  |  |
|  | 271.74 | 5876.5 |  | 286.670 | 6539.7 |  | 301.5 | 23 |
|  | 272.140 | 5893.5 |  | 287.06 | 6557.6 |  | 301.98 | 7257.1 |
|  | 272.533 | 5910.6 |  | 287.456 | 6575.5 |  | 302.378 | 7276.0 |
|  | 272.92 | 5927.6 |  | 287.848 | 6593.5 |  | 302.771 | 7294.9 |
|  |  | 5944.7 | 78 | 28 | 6629.6 | 588 | 303.556 | 73332.8 |
|  | 273.711 | 5961.8 |  |  |  |  | 303.949 | 7351.8 |
|  | 274.104 | 5978.9 | 92. |  | 6647.6 | $8 / 8$ | 304.342 | 7370.8 |
|  | $274.49 \hat{1}$ | 5996.0 |  | 289.419 | 6665.7 | . |  |  |
|  | 274.88 | 6013.2 |  | 289.812 | 6683.8 |  |  | 7389.8 |
|  | 275 | 6030.4 |  | 290.20 | 6701.9 |  | 30 | 7408.97428.0 |
|  | 275 | 6047.6 |  | 290.597 | 6720.1 |  | 305.520 |  |
| 78 |  | 6064.9 | $\begin{aligned} & 73 \\ & 58 \\ & 38 \\ & 78 \end{aligned}$ | $\begin{aligned} & 290.990 \\ & 291.383 \end{aligned}$ | 6738.2 |  | 305.913 | 7447.1 7466. |
|  |  | 60 |  |  | 6774.7 | 2 | 306.698 | 7485.3 |
|  | 276853 | 6099.46116.7 | 93. | 291.775 |  |  | 307.091 | 7504.5 |
|  | 277.246 |  |  | 292.168 | 6792.9 | 78 | 307.483 | 7523.7 |
|  | 277.63 | 6134.1 |  | 292.561 | 6811.2 | 98. | 307.87 |  |
|  | 278.03 | 6151.4 | 14 | 292.954 | 6829.5 <br> 6847.8 |  | 307.876 | 7543.0 |
|  | 278.424 | 6168.8 | $\begin{aligned} & 17 \\ & 58 \\ & 3 / 4 \\ & 3 / 8 \end{aligned}$ |  |  | 98. | 308.269 | 7543.0 7562.2 |
|  | 278.816 | $\begin{aligned} & 6186.2 \\ & 6203.7 \end{aligned}$ |  | 293.739 | 6866.1 |  | 308.661 | 7581.5 |
|  |  |  |  | $\begin{aligned} & 294.132 \\ & 294.524 \end{aligned}$ | $\begin{aligned} & 6884.5 \\ & 6902.9 \end{aligned}$ | 888 | 309.054 | 7600.87620.1 |
|  |  | $\begin{aligned} & 6221.1 \\ & 6238.6 \end{aligned}$ |  |  |  | 5 | $\begin{aligned} & 309.447 \\ & 309 \\ & \hline 840 \end{aligned}$ |  |
|  |  |  |  | 294.917 | 69213 |  | $\begin{aligned} & 310.232 \\ & 310.625 \end{aligned}$ | 7658.9 |
|  | 280.38 | 6256.1 |  | 295.310 | 6939.8 | 78 |  | 7678.3 |
|  | 280.78 | 6273.7 | 94. | 295.702 | $\begin{aligned} & 6958.2 \\ & 6976.7 \end{aligned}$ |  | 810.6~ |  |
|  | 281.17 | $\begin{aligned} & 6291.2 \\ & 6308.8 \end{aligned}$ | $\begin{aligned} & 1 / 4 \\ & 3 / 8 \\ & 18 \end{aligned}$ | $\begin{aligned} & 296.095 \\ & 296.488 \end{aligned}$ |  |  | 311.018 | 7697.77717.1 |
|  | 281.56 |  |  |  | 6976.7 <br> 6995.3 | 99. | 311.410 |  |
|  | 281.95 | 63264 | 19 | 296.881 | 7013.8 |  | 311.803 | $7736.6$ |
| /8 | 28 | 6344.1 | $\begin{aligned} & 5 \% \\ & 58 \\ & 3 / 4 \\ & 7 / 8 \end{aligned}$ | $\underset{297.666}{297.273}$ | $\begin{aligned} & 7032.4 \\ & 7051.0 \end{aligned}$ | 1/4 | 312.196312.588 | 7756.17775.6 |
|  |  |  |  |  |  |  |  |  |
|  |  | 6361.76379.46397.1 |  | 298.059 | $\begin{aligned} & 7051.0 \\ & 7069.6 \end{aligned}$ | 588 | $\begin{aligned} & 312.981 \\ & 313.374 \end{aligned}$ | 7795.27814.8 |
|  | 283.136 |  | 95. |  |  |  |  |  |
|  | 283.529 |  |  | $\begin{aligned} & 298.451 \\ & 298.844 \\ & 299.237 \\ & 299.629 \\ & 300.022 \end{aligned}$$300.022$ | $\begin{aligned} & 7088.2 \\ & 7106.9 \\ & 7125.6 \\ & 7144.3 \\ & 7163.0 \end{aligned}$ |  | $\begin{aligned} & 313.767 \\ & 314.159 \end{aligned}$ | 7834.47854.0 |
|  | 283.921 | $\begin{aligned} & 6397.1 \\ & 6414.9 \\ & 6432.6 \end{aligned}$ | 95. $1 / 8$183818 |  |  | 100. |  |  |
|  | 284.314 |  |  |  |  |  |  |  |
|  | 284.707 | $\begin{aligned} & 6432.6 \\ & 6450.4 \\ & 6468.2 \end{aligned}$ |  |  |  |  |  |  |
| $3 / 4$ | 285.100 |  |  |  |  |  | 314.159 |  |

FIF'TH ROOTS AND FIF'TH POWERS.

| Power. | No. or Root. | Power. | No. or Root. | Power. | No. or Root. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| .0000100 | . 1 | . 000796 | . 240 | . 034503 | . 51 |
| . 0000110 | . 102 | . 000883 | . 245 | . 038020 | . 52 |
| . 0000122 | . 104 | . 000977 | . 250 | . 041820 | . 53 |
| . 0000134 | . 106 | . 001078 | . 255 | . 045917 | . 54 |
| . 0000147 | . 108 | . 001188 | . 260 | . 050328 | . 55 |
| . 0000161 | . 110 | . 001307 | . 265 | . 055073 | . 56 |
| . 0000176 | . 112 | . 001435 | . 270 | . 060169 | . 57 |
| . 0000193 | . 114 | .001573 | . 275 | . 065636 | . 58 |
| . 0000210 | . 116 | .001721 | . 280 | .071492 | . 59 |
| 0000229 | . 118 | .001880 | . 285 | .077760 | . 60 |
| . 0000249 | . 120 | . 002051 | . 290 | . 084460 | . 61 |
| .0000270 | .122 | . 002234 | . 295 | . 091613 | . 62 |
| .0000293 | . 124 | . 002430 | . 300 | . 099244 | . 63 |
| . 0000318 | . 126 | . 002639 | . 305 | . 107374 | . 64 |
| . 0000344 | . 128 | . 002863 | . 310 | . 116029 | . 65 |
| . 0000371 | . 130 | . 003101 | . 315 | . 125233 | . 66 |
| . 0000401 | . 132 | . 003355 | . 320 | . 135012 | . 67 |
| . 0000432 | . 134 | . 003626 | . 325 | . 145393 | . 68 |
| . 0000465 | . 136 | . 003914 | . 330 | . 156403 | . 69 |
| . 0000500 | . 138 | . 004219 | . 335 | . 168070 | . 70 |
| . 0000538 | . 140 | . 004544 | . 340 | . 180423 | . 71 |
| . 0000577 | . 142 | . 004888 | . 345 | . 193492 | . 72 |
| . 0000619 | . 144 | . 005252 | . 350 | . 207307 | . 73 |
| . 0000663 | . 146 | . 005638 | . 355 | . 221901 | . 74 |
| . 0000710 | . 148 | . 006047 | . 360 | . 237305 | . 75 |
| . 0000754 | .150 | . 006478 | . 365 | . 253553 | . 76 |
| . 0000895 | .155 | . 006934 | . 370 | . 270678 | . 77 |
| . 000105 | . 160 | . 007416 | . 375 | . 288717 | . 78 |
| . 000122 | . 165 | . 007924 | . 380 | . 307706 | . 79 |
| . 000142 | . 170 | . 008459 | . 385 | . 327680 | . 80 |
| . 000164 | . 175 | . 009022 | . 390 | . 348678 | . 81 |
| . 000189 | . 180 | . 009616 | . 395 | . 370740 | . 82 |
| . 000217 | . 185 | . 010240 | . 400 | . 393904 | . 83 |
| . 000248 | . 190 | . 011586 | . 41 | . 418212 | . 84 |
| .000282 | -195 | . 013069 | . 42 | . 443705 | . 85 |
| . 000320 | . 200 | . 014701 | . 43 | . 470427 | . 86 |
| . 000362 | . 205 | . 016492 | . 44 | . 498421 | . 87 |
| . 000408 | . 210 | . 018453 | . 45 | . 527732 | . 88 |
| . 000459 | . 215 | . 020596 | . 46 | . 558406 | . 89 |
| . 000515 | . 220 | . 022935 | . 47 | . 590490 | . 90 |
| . 000577 | . 225 | . 025480 | . 48 | . 624032 | . 91 |
| . 000944 | . 230 | . 028248 | . 49 | . 659082 | . 92 |
| . 000717 | . 235 | . 031250 | . 50 | . 695688 | . 93 |

Fifth Roots and Fifth Powers. (CONTINUED.)

| Power. | No. or Root. | Power. | No. or Root. | Power. | No. or Root. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| . 733904 | . 94 | 15.9495 | 1.74 | 525.219 | 3.50 |
| . 773781 | . 95 | 16.8874 | 1.76 | 563.822 | 3.55 |
| . 815373 | . 96 | 17.8690 | 1.78 | 604.662 | 3.60 |
| . 858734 | .97 | 18.8957 | 1.80 | 647.835 | 3.65 |
| . 903921 | . 98 | 19.9690 | 1.82 | 693.440 | 3.70 |
| . 950990 | . 99 | 21.0906 | 1.84 | 741.577 | 3.75 |
| 1. | 1 | 22.2620 | 1.86 | 792.352 | 3.80 |
| 1.10408 | 1.02 | 23.4849 | 1.88 | 845.870 | 3.85 |
| 1.21665 | 1.04 | 24.7610 | 1.90 | 902.242 | 3.90 |
| 1.33823 | 1.06 | 26.0919 | 1.92 | 961.58 | 3.95 |
| 1.46933 | 1.08 | 27.4795 | 1.94 | 1024.00 | 4.00 |
| 1.61051 | 1.10 | 28.9255 | 1.96 | 1089.62 | 4.05 |
| 1.76234 | 1.12 | 30.4317 | 1.98 | 1158.56 | 4.10 |
| 1.92541 | 1.14 | 32.0000 | 2.00 | 1230.95 | 4.15 |
| 2.10034 | 1.16 | 36.2051 | 2.05 | 1306.91 | 4.20 |
| 2.28775 | 1.18 | 40.8410 | 2.10 | 1386.58 | 4.25 |
| 2.48832 | 1.20 | 45.9401 | 2.15 | 1470.08 | 4.30 |
| 2.70271 | 1.22 | 51.5363 | 2.20 | 1557.57 | 4.35 |
| 2.93163 | 1.24 | 57.6650 | 2.25 | 1649.16 | 4.40 |
| 3.17580 | 1.26 | 64.3634 | 2.30 | 1745.02 | 4.45 |
| 3.43597 | 1.28 | 71.6703 | 2.35 | 1845.28 | 4.50 |
| 3.71293 | 1.30 | 79.6262 | 2.40 | 1950.10 | 4.55 |
| 4.00746 | 1.32 | 88.2735 | 2.45 | 2059.63 | 4.60 |
| 4.32040 | 1.34 | 97.6562 | 2.50 | 2174.03 | 4.65 |
| 4.65259 | 1.36 | 107.820 | 2.55 | 2293.45 | 4.70 |
| 5.00490 | 1.38 | 118.814 | 2.60 | 2418.07 | 4.75 |
| 5.37824 | 1.40 | 130.686 | 2.65 | 2548.04 | 4.80 |
| 5.77353 | 1.42 | 143.489 | 2.70 | 2683.54 | 4.85 |
| 6.19174 | 1.44 | 157.276 | 2.75 | 2824. 75 | 4.90 |
| 6.63383 | 1.46 | 172.104 | 2.80 | 2971.84 | 4.95 |
| 7.10082 | 1.48 | 188.029 | 2.85 | 3125.00 | 5.00 |
| 7.59375 | 1.50 | 205.111 | 2.90 | 3450.25 | 5.10 |
| 8.11368 | 1.52 | 223.414 | 2.95 | 3802.04 | 5.20 |
| 8.66171 | 1.54 | 243.000 | 3.00 | 4181.95 | 5.30 |
| 9.23896 | 1.56 | 263.936 | 3.05 | 4591.65 | 5.40 |
| 9.84658 | 1.58 | 286.292 | 3.10 | 5032.84 | 5.50 |
| 10.4858 | 1.60 | 310.136 | 3.15 | 5507.32 | 5.60 |
| 11.1577 | 1.62 | 335.544 | 3.20 | 6016.92 | 5.70 |
| 11.8637 | 1.64 | 362.591 | 3.25 | 6563.57 | 5.80 |
| 12.6049 | 1.66 | 391.354 | 3.30 | 7149.24 | 5.90 |
| 13.3828 | 1.68 | 421.419 | 3.35 | 7776.00 | 6.00 |
| 14.1986 | 1.70 | 454.354 | 3.40 | 8445.96 | 6.10 |
| 15.0537 | 1.72 | 488.760 | 3.45 | 9161.33 | 6.20 |

Fifth Roots and Fifth Powers. (CONTINUED.)

| Power. | No. or Root. | Power. | No. or Root. | Power. | No. or Root. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 9924.37 | 6.30 | 176234. | 11.2 | 3043168. | 19.8 |
| 10737. | 6.40 | 192541. | 11.4 | 3200000. | 20.0 |
| 11603. | 6.50 | 210034. | 11.6 | 3363232. | 20.2 |
| 12523. | 6.60 | $2287 \% 6$. | 11.8 | 3533059 . | 20.4 |
| 13501. | 6.70 | 248832. | 12.0 | 3709677 . | 20.6 |
| 14539. | 6.80 | 270271. | 12.2 | 3893289 . | 20.8 |
| 15640. | 6.90 | 293163. | 12.4 | 4084101. | 21.0 |
| 16807. | 7.00 | 317580. | 12.6 | 4282322. | 21.2 |
| 18042. | 7.10 | 343597. | 12.8 | 4488166. | 21.4 |
| 19349. | 7.20 | 371293. | 13.0 | 4701850. | 21.6 |
| 20731. | 7.30 | 400746. | 13.2 | 4923597. | 21.8 |
| 22190. | 7.40 | 432040. | 13.4 | 5153632. | 22.0 |
| 23730. | 7.50 | 465259. | 13.6 | 5392186. | 22.2 |
| 25355. | 7.60 | 500490. | 13.8 | 5639493. | 22.4 |
| 27068. | 7.70 | 537824. | 14.0 | 5895793. | 22.6 |
| 28872. | 7.80 | 577353. | 14.2 | 6161327. | 22.8 |
| 30771. | 7.90 | 619174. | 14.4 | 6436343. | 23.0 |
| 32768. | 8.00 | 663383. | 14.6 | 6721093. | 23.2 |
| 34868. | 8.10 | 710082. | 14.8 | 7015834. | 23.4 |
| 37074. | 8.20 | 759375. | 15.0 | 7320825. | 23.6 |
| 39390. | 8.30 | 811368. | 15.2 | 7636332. | 23.8 |
| 41821. | 8.40 | 866171. | 15.4 | 7962624. | 24.0 |
| 44371. | 8.50 | 923896. | 15.6 | 8299976. | 24.2 |
| 47043. | 8.60 | 984658. | 15.8 | 8648666. | 24.4 |
| 49842. | 8.70 | 1048576. | 16.0 | 9008978. | 24.6 |
| 52773. | 8.80 | 1115771. | 16.2 | 9381200. | 24.8 |
| 55841. | 8.90 | 1186367. | 16.4 | 9765625. | 25.0 |
| 59049 | 9.00 | 1260493. | 16.6 | 10162550. | 25.2 |
| 62403. | 9.10 | 1338278. | 16.8 | 10572278. | 25.4 |
| 65908. | 9.20 | 1419857. | 17.0 | 10995116. | 25.6 |
| 69569. | 9.30 | 1505366. | 17.2 | 11431377. | 25.8 |
| 73390. | 9.40 | 1594947. | 17.4 | 11881376. | 26.0 |
| 77378. | 9.50 | 1688742. | 17.6 | 12345437. | 26.2 |
| 81537. | 9.60 | 1786899. | 17.8 | 12823886. | 26.4 |
| 85873. | 9.70 | 1889568. | 18.0 | 13317055. | 26.6 |
| 90392. | 9.80 | 1996903. | 18.2 | 13825281. | 26.8 |
| 95099 , | 9.90 | 2109061. | 18.4 | 14348907. | 27.0 |
| 100000. | 10.0 | 2226203. | 18.6 | 14888280. | 27.2 |
| 110408. | 10.2 | 2348493. | 18.8 | 15443752. | 27.4 |
| 121665. | 10.4 | 2476099. | 19.0 | 16015681. | 27.6 |
| 133823. | 10.6 | 2609193. | 19.2 | 16604430. | 27.8 |
| 146933. | 10.8 | 2747949. | 19.4 | 17210368. | 28.0 |
| 161051. | 11.0 | 2892547. | 19.6 | 17833868. | 28.2 |

Fifth Roots and Fifth Powers. (continued.)

| Power. | No. or Root. | Power. | No. or Root. | Power. | No. or Root. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 18475309. | 28.4 | 28629151. | 31.0 | 60466176. | 36.0 |
| 19135075. | 28.6 | 31013642. | 31.5 | 64783487. | 36.5 |
| 19813557. | 28.8 | 33554432. | 32.0 | 69343957. | 37.0 |
| 20511149. | 29.0 | 36259082. | 32.5 | 74157715. | 37.5 |
| 21228253. | 29.2 | 39135393. | 33.0 | 79235168. | 38.0 |
| 21965275. | 29.4 | 42191410. | 33.5 | 84587005. | 38.5 |
| 22722628. | 29.6 | 45435424. | 34.0 | 90224199. | 39.0 |
| 23500728. | 29.8 | 48875980. | 34.5 | 96158012. | 39.5 |
| 24300000. | 30.0 | 52521875. | 35.0 | 102400000. | 40.0 |
| 26393634. | 30.5 | 56382167. | 35.5 |  |  |



Squares, Cubes, Square Roots, Cube Roots, Logarithms, Reciprocals, Circumferences and Circular Areas of Nos. from 1 to 1000.
(FROM CARNEGIE HAND BOOK.)

| No. | Sq. | Cube. | Square Root. | Cube <br> Root. | Log. | $\begin{gathered} 1000 \\ X \\ \text { Recip. } \end{gathered}$ | No. = Dia. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Circ'm | Area. |
| 1 | 1 | 1 | 1.0000 | 1.0000 | 0.00000 | 1000.000 | 3.142 | 0.7854 |
| 2 | 4 | 8 | 1.4142 | 1.2599 | 0.30103 | 500.000 | 6.283 | 3.1416 |
| 3 | 9 | 27 | 1.7321 | 1.4422 | 0.47712 | 333.333 | 9.425 | 7.0686 |
| 4 | 16 | 64 | 2.0000 | 1.5874 | 0.60206 | 250.000 | 12.566 | 12.5664 |
| 5 | 25 | 125 | 2.2361 | 1.7100 | 0.69897 | 200.000 | 15.708 | 19.6350 |
| 6 | 36 | 216 | 2.4495 | 1.8171 | 0.77815 | 166.667 | 18.850 | 28.2743 |
| 7 | 49 | 343 | 2.6458 | 1.9129 | 0.84510 | 142.857 | 21.991 | 38.4845 |
| 8 | 64 | 512 | 2.8284 | 2.0000 | 0.90309 | 125.000 | 25.133 | 50.2655 |
| 9 | 81 | 729 | 3.0000 | 2.0801 | 0.95424 | 111.111 | 28.274 | 63.6173 |
| 10 | 100 | 1000 | 3.1623 | 2.1544 | 1.00000 | 100.000 | 31.416 | 78.5398 |
| 11 | 121 | 1331 | 3.3166 | 2.2240 | 1.04139 | 90.9091 | 34.558 | 5.0332 |
| 12 | 144 | 1728 | 3.4641 | 2.2894 | 1.07918 | 83.3333 | 37.699 | 113.097 |
| 13 | 169 | 2197 | 3.6056 | 2.3513 | 1.11394 | 76.9231 | 40.841 | 132.732 |
| 14 | 196 | 2744 | 3.7417 | 2.4101 | 1.14613 | 71.4286 | 43.982 | 153.938 |
| 15 | 225 | 3375 | 3.8730 | 2.4662 | 1.17609 | 66.6667 | 47.124 | 176.715 |
| 16 | 256 | 4096 | 4.0000 | 2.5198 | 1.20412 | 62.5000 | 50.265 | 201.062 |
| 17 | 289 | 4913 | 4.1231 | 2.5713 | 1.23045 | 58.8235 | 53.407 | 226.980 |
| 18 | 324 | 5832 | 4.2426 | 2.6207 | 1.25527 | 55.5556 | 56.549 | 254.469 |
| 19 | 361 | 6859 | 4.3589 | 2.6684 | 1.27875 | 52.6316 | 59.690 | 283.529 |
| 20 | 400 | 8000 | 4.4721 | 2.7144 | 1.30103 | 50.0000 | 62.832 | 314.159 |
| 21 | 441 | 9261 | 4.5826 | 2.7589 | 1.32222 | 47.6190 | 65.973 | 346.361 |
| 22 | 484 | 10648 | 4.6904 | 2.8020 | $1.3424 \%$ | 45.4545 | 69.115 | 380.133 |
| 23 | 529 | 12167 | 4.7958 | 2.8439 | 1.36173 | 43.4783 | 72.257 | 415.476 |
| 24 | 576 | 13824 | 4.8990 | 2.8845 | 1.38021 | 41.6667 | 75.398 | 452.389 |
| 25 | 625 | 15625 | 5.0000 | 2.9240 | 1.39794 | 40.0000 | 78.540 | 490.874 |
| 26 | 676 | 17576 | 5.0990 | 2.9625 | 1.41497 | 38.4615 | 81.681 | 530.929 |
| 27 | 729 | 19683 | 5.1962 | 3.0000 | 1.43136 | 37.0370 | 84.823 | 572.555 |
| 28 | 784 | 21952 | 5.2915 | 3.0366 | 1.44716 | 35.7143 | 87.965 | 615.752 |
| 29 | 841 | 24389 | 5.3852 | 3.0723 | 1.46240 | 34.4828 | 91.106 | 660.520 |
| 30 | 900 | 27000 | 5.4772 | 3.1072 | 1.47712 | 33.3333 | 94.248 | 706.858 |
| 31 | 961 | 29791 | 5.5678 | 3.1414 | 1.49136 | 32.2581 | 97.389 | 754.768 |
| 32 | 1024 | 32768 | 5.6569 | 3.1748 | 1.50515 | 31.2500 | 100.531 | 804.248 |
| 33 | 1089 | 35937 | 5.7446 | 3.2075 | 1.51851 | 30.3030 | 103.673 | 855.299 |
| 34 | 1156 | 39304 | 5.8310 | 3.2396 | 1.53148 | 29.4118 | 106.814 | 907.920 |
| 35 | 1225 | 42875 | 5.9161 | 3.2711 | 1.54407 | 28.5714 | 109.956 | 962.113 |
| 36 | 1296 | 46656 | 6.0000 | 3.3019 | 1.55630 | 27.7778 | 113.097 | 1017.88 |
| 37 | 1369 | 50653 | 6.0828 | 3.3322 | 1.56820 | 27.0270 | 116.239 | 1075.21 |
| 38 | 1444 | 54872 | 6.1644 | 3.3620 | 1.57978 | 26.3158 | 119.381 | 1134.11 |
| 39 | 1521 | 59319 | 6.2450 | 3.3912 | 1.59106 | 25.6410 | 122.522 | 1194.59 |
| 40 | 1600 | 64000 | 6.3246 | 3.4200 | 1.60206 | 25.0000 | 125.66 | 1256.64 |
| 41 | 1681 | 68921 | 6.4031 | 3.4482 | 1.61278 | 24.3902 | 128.81 | 1320.25 |
| 42 | 1764 | 74088 | 6.4807 | 3.4760 | 1.62325 | 23.8095 | 131.95 | 1385.44 |
| 43 | 1849 | 79507 | 6.5574 | 3.5034 | 1.63347 | 23.2558 | 135.09 | 1452.20 |
| 44 | 1936 | 85184 | 6.6332 | 3.5303 | 1.64345 | $22.72 \% 3$ | 138.23 | 1520.53 |
| 45 | 2025 | 91125 | 6.7082 | 3.5569 | 1.65321 | 22.2222 | 141.37 | 1590.43 |

Squares, Cubes, Square Roots, Cube Roots, Logarithms, Etc.
(CONTINUED.)

| No | Sq. | Cube. | Square Root. | Cube <br> Root. | Log. | $\begin{gathered} 1000 \\ X \\ \text { Recip. } \end{gathered}$ | No $=$ Dia. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Circ'm | Area. |
| 46 | 2116 | 97336 | 6.7823 | 3.5830 | 1.66276 | 21.7391 | 144.51 | 1661.90 |
| 47 | 2209 | 103823 | 6.8557 | 3.6088 | 1.67210 | 21.2466 | 147.65 | 1734.94 |
| 48 | 23304 | 110592 | 6.9282 | 3.6342 | 1.68124 | 20.8333 | 150.80 | 1809.56 |
| 49 | 2401 | 117649 | 7.0000 | 3.6593 | 1.69020 | 20.4082 | 153.94 | 1885.74 |
| 50 | 2500 | 125000 | 7.0711 | 3.6840 | 1.69897 | 20.0000 | 157.08 | 1963.50 |
| 51 | 2601 | 132651 | 7.1414 | 3.6084 | 1.70757 | 19.6078 | 160.22 | 2042.82 |
| 52 | 2704 | 140608 | 7.2111 | 3.7325 | 1.71600 | 19.2308 | 163.36 | 2123.72 |
| 53 | 2809 | 148877 | 7.2801 | 3.7563 | 1.72428 | 18.8679 | 166.50 | 2206.18 |
| 54 | 2916 | 157464 | 7.3485 | 3.7798 | 1.73239 | 18.5185 | 169.65 | 2290.22 |
| 55 | 3025 | 166375 | 7.4162 | 3.8030 | 1.74036 | 18.1818 | 172.79 | 2375.83 |
| 56 | 3136 | 175616 | 7.4833 | 3.8259 | 1.74819 | 17.8571 | 175.98 | 2463.01 |
| 57 | 3249 | 185193 | 7.5498 | 3.8485 | 1.75587 | 17.5439 | 179.07 | 2551.76 |
| 58 | 3364 | 195112 | 7.6158 | 3.8709 | 1.76343 | 17.2414 | 182.21 | 2642.08 |
| 59 | 3481 | 205379 | 7.6811 | 3.8930 | 1.77085 | 16.9492 | 185.35 | 2733.97 |
| 60 | 3600 | 216000 | 7.7460 | 3.9149 | 1.77815 | 16.6667 | 188.50 | 2827.43 |
| 61 | 3721 | 226981 | 7.8102 | 3.9365 | 1.78533 | 16.3934 | 191.64 | 2922.47 |
| 62 | 3844 | 238328 | 7.8740 | 3.9579 | 1.79239 | 16.1290 | 194.78 | 3019.07 |
| 63 | 3969 | 250047 | 7.9373 | 3.9791 | 1.79934 | 15.8730 | 197.92 | 3117.25 |
| 64 | 4096 | 262144 | 8.0000 | 4.0000 | 1.80618 | 15.6250 | 201.06 | 3216.99 |
| 65 | 4225 | 274625 | 8.0623 | 4.0207 | 1.81291 | 15.3846 | 204.20 | 3318.31 |
| 66 | 4356 | 287496 | 8.1240 | 4.0412 | 1.81954 | 15.1515 | 207.35 | 3421.19 |
| 67 | 4489 | 300763 | 8.1854 | 4.0615 | 1.82607 | 14.9254 | 210.49 | 3525.65 |
| 68 | 4624 | 314432 | 8.2462 | 4.0817 | 1.83251 | 14.7059 | 213.63 | 3631.68 |
| 69 | 4761 | 328509 | 8.3066 | 4.1016 | 1.83885 | 14.4928 | 216.77 | 3739.28 |
| 70 | 4900 | 343000 | 8.3666 | 4.1213 | 1.84510 | 14.2857 | 219.91 | 3848.45 |
| 71 | 5041 | 357911 | 8.4261 | 4.1408 | 1.85126 | 14.0845 | 223.05 | 3959.19 |
| 72 | 5184 | 373248 | 8.4853 | 4.1602 | 1.85733 | 13.8889 | 226.19 | 4071.50 |
| 73 | 5329 | 389017 | 8.5440 | 4.1793 | 1.86332 | 13.6986 | 229.34 | 4185.39 |
| 74 | 5476 | 405224 | 8.6023 | 4.1983 | 1.86923 | 13.5135 | 23248 | 4300.84 |
| 75 | 5625 | 421875 | 8.6603 | 4.2172 | 1.87506 | 13.3333 | 235.62 | 4417.86 |
| 76 | 5776 | 438976 | 8.7178 | 4.2358 | 1.88081 | 13.1579 | 238.76 | 4536.46 |
| 77 | 5929 | 456533 | 8.7750 | 4.2543 | 1.88649 | 12.9870 | 241.90 | 4656.63 |
| 78 | 6084 | 474552 | 8.8318 | 4.2727 | 1.89209 | 12.8205 | 245.04 | 4778.36 |
| 79 | 6241 | 493039 | 8.8882 | 4.2908 | 1.89763 | 12.6582 | 243.19 | 4901.67 |
| 80 | 6400 | 512000 | 8.9443 | 4.3089 | 1.90309 | 12.5000 | 251.33 | 5026.55 |
| 81 | 6561 | 531441 | 9.0000 | 4.3267 | 1.90849 | 12.3457 | 254.47 | 5153.00 |
| 82 | 6724 | 551368 | 9.0554 | 4.3445 | 1.91381 | 12.1951 | 257.61 | 5281.02 |
| 83 | 6889 | 571787 | 9.1104 | 4.3621 | 1.91908 | 12.0482 | 260.75 | 5410.61 |
| 84 | 7056 | 592704 | 9.1652 | 4.3795 | 1.92428 | 11.9048 | 263.89 | 5541.77 |
| 85 | 7225 | 614125 | 9.2195 | 4.3968 | 1.92942 | 11.7647 | 267.04 | 5674.50 |
| 86 | 7396 | 636056 | 9.2736 | 4.4140 | 1.93450 | 11.6279 | 270.18 | 5808.80 |
| 87 | 7569 | 658503 | 9.3274 | 4.4310 | 1.93952 | 11.4943 | 273.32 | 5944.68 |
| 88 | 7744 | 681472 | 9.3808 | 4.4480 | 1.94448 | 11.3636 | 276.46 | 6082.12 |
| 89 | 7921 | 704969 | 9.4340 | 4.4647 | 1.94939 | 11.2360 | 279.60 | 6221.14 |

Squares, Cubes, Square Roots, Cube Roots, Logarithms, Etc.
(CONTINUED.)

| No. | Sq. | Cube. | Square Root. | Cube <br> Root. | Log. | $\begin{gathered} 1000 \\ X \\ \text { Recip. } \end{gathered}$ | No. = Dia. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Ci | . |
|  |  |  |  | 4.4814 | 1.95424 | 11.1111 |  | 6361.73 |
|  |  | 753571 | 9.5394 | 4.4979 | 1.95904 | 10.9890 |  |  |
| 92 | 8464 | 778688 | 9.5917 | 4.5144 | 1.96379 | 10.8696 |  | 6647.61 |
| 93 | 8649 | 804357 | 9.6437 | 4.5307 | 1.96848 | 10.7527 | 292.17 | 6792.91 |
| 94 | 8836 | 830584 | 9.6954 | 4.5468 | 1.97313 | 10.6388 | 295.31 | 6939.78 |
|  | 9025 | 857375 |  | 4.56 |  | 10.5263 |  |  |
|  | 9216 | 884736 | 9.798 | 4.5789 | 1.98227 | 10.4167 |  |  |
|  | 9409 | 912673 | 9.8489 | 4.5947 | 198677 | 10.3093 | 304.73 | 7389.81 |
|  | 9604 | 941192 | 9.8995 | 4.6104 | 1.99123 | 10. 2041 | 307.88 | 7542.96 |
| 99 | 980 | 970299 | 9.9499 | 4.6261 | 1.99564 | 10.1010 |  | 69 |
|  | 100 | 1000 | 10.0 | 4.641 | 2.00000 | 10.0000 | 314.16 | 98 |
| 101 | 1020 | 1030301 | 10.0499 | 4.6570 | 2.00432 | 9.90099 | 317.30 | 8011.85 |
| 102 | 10404 | 1061208 | 10.0995 | 4.6723 | 2.00860 | 9.80392 | 320.44 | 171.28 |
| 103 | 10609 | 1092727 | 10.1489 | 4.6875 | 2.01284 | 9.70874 | 323.58 | 8332.29 |
| 104 | 10816 | 1124864 | 10.1980 | 4.7027 | 2.01703 | 9.61538 | 326.73 | 8494.87 |
| 105 | 11025 | 1157625 | 10.2470 | 4.717 | 2.02119 | 9.52381 |  | . 01 |
| 106 | 11236 | 1191016 | 10.2956 | 4.7326 | 2.02531 | 9.43396 | 333.01 | . 73 |
| 107 | 11449 | 1225043 | 10.3441 | 4.7475 | 2.02938 | 9.34579 | 336.15 | 02 |
| 108 | 11664 | 1259712 | 10.3923 | 4.7622 | 2.03342 | 9.25926 | 339.29 | 88 |
| 109 | 11881 | 1295029 | 10.4403 | 4.7769 | 2.03743 | 9.174 |  |  |
|  | 12 | 13 | 10 | 4.7 |  | 9.0 |  | 32 |
|  | 12 | 13676 | 10.535 | 4.805 | 2.04 | 9.009 | 348.72 | 89 |
|  | 12 | 140492 | 10.583 | 4.820 | 2.04 | 8.928 | 351.86 | 52.03 |
| 13 | 12 | 1442897 | 10.6301 | 4.8346 | 2.05308 | 8.84956 | 355.00 | 10028.7 |
| 114 | 129 | 1481544 | 10.6771 | 4.8488 | 2.05690 | 8.74193 |  | 10907. |
| 115 | 1322 | 152087 | 10.723 | 4.8629 | 2.060 | 8.69 |  |  |
| 116 | 13456 | 1560896 | 10.7703 | 4.8770 | 2.06446 | 8.62069 | 364.42 | 10568.3 |
| 117 | 13689 | 1601613 | 10.8167 | 3.8910 | 2.06819 | 8.54701 | 367.57 | 10751.3 |
| 118 | 13924 | 1643032 | 10.8628 | 4.9049 | 2.07188 | 8.47458 | 370.71 | 10935.9 |
| 119 | 14161 | 168515 | 10.908 | 4.9187 | 2.07555 | 8.4033 |  | 11122.0 |
|  | 11 | 1728 | 10 | 4.9 | 2.07918 | 8.333 |  |  |
|  | 1464 | 177156 | 11.000 | 4.946 | 2.082 | 8.264 | 380. | 11499.0 |
|  | 1488 | 18158 | 11.045 | 4.959 | 2. | 8.19672 | 383. | 11689.9 |
| 123 | 15129 | 186086 | 11.0905 | 4.9782 | 2.08991 | 8.13008 | 386.42 | 11882.3 |
| 124 | 1537 | 190662 | 11.1355 | 4.98 | 2.09342 | 8.06152 |  |  |
| 125 | 15625 | 1953125 | 11.1803 | 5.0000 | 2.09691 | 8.00000 | 392.70 | 12271.8 |
| 126 | 15876 | 2000376 | 11.2250 | 5.0133 | 2.10037 | 7.93651 | 395.84 | 12469.0 |
| 127 | 16129 | 204838 | 11.2694 | 5.0265 | 2.10380 | 7.87402 | 398.98 | 12667.7 |
| 128 | 16384 | 209715 | 11.3137 | 5.0397 | 2.10721 | 7.81250 | 402.12 | 12868.0 |
| 129 | 1664 | 214 | 11.357 | 5.0 | 2.1105 | 7.75194 | 405.2 | 13069.8 |
| 130 | 1690 | 219700 | 11.4018 | 5.0658 | 2.1139 | 7.692 | 408 | 13273.2 |
| 131 | 1716 | 224809 | 11.4455 | 5.0788 | 2.1172 | 7.633 | 411.5 | 13478.2 |
| 2 | 17424 | 2299968 | 11.4891 | 5. 0916 | 2.1205 | 7.57576 | 414.69 | 13684.8 |
| 133 | 17689 | 2352637 | 11.5326 | 5.1045 | 2.12385 | 7.51880 | 417.8 | 13892.9 |
| 134 | 1795 | 2406104 | 11.575 | 5.1172 | 2.1271 | 7.46269 | 420. | 14102.6 |

Squares, Cubes, Square Roots, Cube Roots, Logarithms, Etc.
(CONTINUED.)

|  |  |  | Square | Cube |  |  | No. | $=\mathrm{Dia}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | Recip. | Circ'm | Area. |
| 135 | 18225 | 2460375 | 11.6190 | 5.1299 | 2.13033 | 7.40741 | 424.12 | 14313.9 |
| 136 | 18496 | 2515456 | 11.6619 | 5.1426 | 2.13354 | 7.35294 | 427. 26 | 14526.7 |
| 137 | 18769 | 2571353 | 11.7047 | 5.1551 | 2.13678 | 7.29927 | 430.40 | 14741.1 |
| 138 | 19044 | 2628072 | 11.7473 | 5.1676 | 2.13988 | 7.24638 | 433.54 | 14957.1 |
| 139 | 19321 | 2685619 | 11.7898 | 5.1801 | 2.14301 | 7.19424 | 436.68 | 15174.7 |
| 140 | 19600 | 2744000 | 11.8322 | 5.1925 | 2.14613 | 7.14286 | 439.82 | 15393.8 |
| 141 | 19881 | 2803221 | 11.8743 | 5.2048 | 2.14922 | 7.09220 | 442.96 | 15614.5 |
| 142 | 20164 | 2863288 | 11.9164 | 5.2171 | 2.15229 | 7.04225 | 446.11 | 15836.8 |
| 143 | 20149 | 2924207 | 11.9533 | 5.2293 | 2.15534 | 6.99301 | 449.25 | 16060.6 |
| 144 | 20736 | 2985984 | 12.0000 | 5.2415 | 2.15836 | 6.94444 | 452.39 | 16286.0 |
| 145 | 21025 | 3048625 | 12.0416 | 5.2536 | 2.16137 | 6.89655 | 455.53 | 16513.0 |
| 146 | 21316 | 3112136 | 12.0830 | 5.2656 | 2.16435 | 6.84932 | 458.67 | 16741.5 |
| 147 | 21609 | 3176523 | 12.1244 | 5.2776 | 2.16732 | 6.80272 | 461.81 | 16971.7 |
| 148 | 21904 | 3241792 | 12.1655 | 5.2896 | 2.17026 | 6.75676 | 464.96 | 17203.4 |
| 149 | 22201 | 3307949 | 12.2066 | 5.3015 | 2.17319 | 6.71141 | 468.10 | 17436.6 |
| 150 | 22500 | 3375000 | 12.2474 | 5.3133 | 2.17609 | 6.66667 | 471.24 | 17671.5 |
| 151 | 22801 | 3442951 | 12.2882 | 5.3251 | 2.17898 | 6.62252 | 474.38 | 17907.9 |
| 152 | 23104 | 3511808 | 12.3288 | 5.3368 | 2.18184 | 6.57895 | 477.52 | 18145.8 |
| 153 | 23409 | 3581577 | 12.3693 | 5.3485 | 2.18469 | 6.53595 | 480.66 | 18385.4 |
| 154 | 23716 | 3652264 | 12.4097 | 5.3601 | 2.18752 | 6.49851 | 483.81 | 18626.5 |
| 155 | 24025 | 37288\% | 12.4499 | 5.3717 | 2.19033 | 6.45161 | 486.95 | 18869.2 |
| 156 | 24336 | 3796416 | 12.4900 | 5.3832 | 2.19312 | 6.41026 | 490.09 | 19113.4 |
| 157 | 24649 | 3869893 | 12.5300 | 5.3947 | 2.19590 | 6.36943 | 493.23 | 19359.3 |
| 158 | 24964 | 3944312 | 12.5698 | 5.4061 | 2. 19866 | 6.32911 | 496.37 | 19606.7 |
| 159 | 25281 | 4019679 | 12.6095 | 5.4175 | 2.20140 | 6.28931 | 499.51 | 19855.7 |
| 160 | 25600 | 4096000 | 12.6491 | 5.4288 | 2.20412 | 6.25000 | 502.65 | 20106.2 |
| 161 | 25921 | 4173281 | 12.6886 | 5.4401 | 2.20683 | 6.21118 | 505.80 | 20358.3 |
| 162 | 26*44 | 4251528 | 12.7279 | 5.4514 | 2.20952 | 6.17284 | 508.94 | 20612.0 |
| 163 | 26569 | 4330747 | 12.7671 | 5.4626 | 2.21219 | 6.13497 | 512.08 | 20867.2 |
| 164 | 26896 | 4410944 | 12.8062 | 5.4737 | 2.21484 | 6.09756 | 515.22 | 21124.1 |
| 165 | 27225 | 4492125 | 12.8452 | 5.4848 | 2.21748 | 6.06061 | 518.36 | 21382.5 |
| 166 | 27556 | 4574296 | 12.8841 | 5.4959 | 2.22011 | 6.02410 | 521.50 | 21642.4 |
| 167 | 27889 | 4657463 | 12.9228 | 5.5069 | 2.22272 | 5.98802 | 524.65 | 21904.0 |
| 168 | 28224 | 4741632 | 12.9615 | 5.5178 | 2.22531 | 5.95238 | 527.79 | 22167.1 |
| 169 | 28561 | 4826809 | 13.0000 | 5.5288 | 2.22789 | 5.91716 | 530.93 | 22431.8 |
| 170 | 28900 | 4913000 | 13.0384 | 5.5397 | 2.23045 | 5.88235 | 534.07 | 22698.0 |
| 171 | 29241 | 5000211 | 13.0767 | 5.5505 | 2.23300 | 5.84795 | 537.21 | 22965.8 |
| 178 | 29584 | 5088448 | 13.1149 | 5.5613 | 2.23553 | 5.81395 | 540.35 | 23235.2 |
| 173 | 29929 | 5177717 | 13.1599 | 5.5721 | 2.23805 | 5.78035 | 543.50 | 28506.2 |
| 174 | 30276 | 5268024 | 13.1909 | 5.5828 | 2.24055 | 5.74713 | 546.64 | 23778.7 |
| 175 | 30625 | 5359375 | 13.2288 | 5.5934 | 2.24304 | 5.71429 | 549.78 | 24052.8 |
| 176 | 30976 | 5451776 | 13.2665 | 5.6041 | 2.24551 | 5.68182 | 552.92 | 24328.5 |
| 177 | 81329 | 5545233 | 13.3041 | 5.6147 | 2.24797 | 5.64972 | 556.06 | 24605.7 |
| 178 | 31684 | 5639752 | 13.3417 | 5.6252 | 2.25042 | 5.61798 | 559.20 | 24884.6 |
| 179 | 32041 | 5735339 | 13.3791 | 5.6357 | 2.25285 | 5.58659 | 562.35 | 25164.9 |

Squares, Cubes, Square Roots, Cube Roots, Logarithms, Etc.
(CONTINUED.)

| No. | Sq. | Cube. | Square Root. | Cube Root. | Log. | $\begin{gathered} 1000 \\ \text { X } \\ \text { Recip. } \end{gathered}$ | No. $=$ Dia. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Circ'm | Area. |
| 180 | 32100 | 5832000 | 13.4164 | 5.6462 | 2.25527 | 5.55556 | 565.49 | 25446.9 |
| 181 | 32761 | 5929741 | 13.4536 | 5.6567 | 2.25768 | 5.52486 | 568.63 | 25730.4 |
| 182 | 33124 | 6028568 | 13.4907 | 5.6671 | 2.26007 | 5.49451 | 571.77 | 26015.5 |
| 183 | 33489 | 6128487 | 13.5277 | 5.6774 | 2.26245 | 5.46448 | 574.91 | 26302.2 |
| 184 | 33856 | 6229504 | 13.5647 | 5.6877 | 2.26482 | 5.43478 | 578.05 | 26590.4 |
| 185 | 34225 | 6331625 | 13.6015 | 5.6980 | 2.26717 | 5.40541 | 581.19 | 26880.3 |
| 186 | 34596 | 6434856 | 13.6382 | 57083 | 2.26951 | 5.37634 | 584.34 | 27171.6 |
| 187 | 34969 | 6539203 | 13.6748 | 5.7185 | 2.27184 | 5.34759 | 587.48 | 27464.6 |
| 188 | 35344 | 6644672 | 13.7113 | 5.7287 | 2.27416 | 5.31915 | 590.62 | 27759.1 |
| 189 | 35721 | 6751269 | 13.7477 | 5.7388 | 2.27646 | 5.29101 | 593.76 | 28055.2 |
| 190 | 36100 | 6859000 | 13.7840 | 5.7489 | 2.27875 | 5.26816 | 596.90 | 28352.9 |
| 191 | 36481 | 6967871 | 13.8203 | 5.7590 | 2.28103 | 5.23560 | 600.04 | 28652. 1 |
| 192 | 36864 | 7077888 | 13.8564 | 5.7690 | 2.28330 | 5.20833 | 603.19 | 28952.9 |
| 193 | 37249 | 7189057 | 13.8924 | 5.7790 | 2.28556 | 5.18135 | 606.33 | 29255.3 |
| 194 | 37636 | 7301384 | 13.9284 | 5.7890 | 2.28780 | 5.15464 | 609.47 | 29559.2 |
| 195 | 38025 | 7414875 | 13.9642 | 5.7989 | 2.29003 | 5.12821 | 612.61 | 29864.8 |
| 196 | 38416 | 7529536 | 14.0000 | 5.8088 | 2.29226 | 5.10204 | 615.75 | 30171.9 |
| 197 | 38809 | 7645373 | 14.0357 | 5.8186 | 2.29447 | 5.07614 | 618.89 | 30480.5 |
| 198 | 39204 | 7762392 | 14.0712 | 5.8285 | 2.29667 | 5.05051 | 622.04 | 30790.7 |
| 199 | 39601 | 7880599 | 14.1067 | 5.8383 | 2.29885 | 5.02513 | 625.18 | 31102.6 |
| 200 | 40000 | 8000000 | 14.1421 | 5.8480 | 2.30103 | 5.00000 | 628.32 | 31415.9 |
| 201 | 40401 | 8120601 | 14.1774 | 5.8578 | 2.30320 | 4.97512 | 631.46 | 31730.9 |
| 202 | 40804 | 8242408 | 14.2127 | 5.8675 | 2.30535 | 4.95050 | 634.60 | 32047.4 |
| 203 | 41209 | 8365427 | 14.2478 | 5.8771 | 2.30750 | 4.92611 | 637.74 | 32365.5 |
| 204 | 41616 | 8489664 | 14.2829 | 5.8868 | 2.30963 | 4.90196 | 640.89 | 32685.1 |
| 205 | 42025 | 8615125 | 14.3178 | 5.8964 | $2.311^{175}$ | 4.87805 | 644.08 | 33006.4 |
| 206 | 42436 | 8741816 | 14.3527 | 5.9059 | 2.31387 | 4.85437 | 647.17 | 33329.2 |
| 207 | 42819 | 8869743 | 14.3875 | 5.9155 | 2.31597 | 4.83092 | 650.31 | 33653.5 |
| 208 | 43264 | 8998912 | 14.4222 | 5.9250 | 2.31806 | 4.80769 | 653.45 | 33979.5 |
| 209 | 43681 | 9129329 | 14.4568 | 5.9345 | 2.32015 | 4.78469 | 656.59 | 34307.0 |
| 210 | 44100 | 9261000 | 14.4914 | 5.9439 | 2.32222 | 4.76190 | 659.73 | 34636.1 |
| 211 | 44521 | 9393931 | 14.5258 | 5.9533 | 2.32428 | 4.73934 | 662.88 | 34966.7 |
| 212 | 44944 | 9528128 | 14.5602 | 5.9627 | 2.32634 | 4.71698 | 666.02 | 35298.9 |
| 213 | 45369 | 9663597 | 14.5945 | 5.9721 | 2.32838 | 4.69484 | 669.16 | 35632.7 |
| 214 | 45796 | 9800344 | 14.6287 | 5.9814 | 2.33041 | 4.67290 | $67 \% .30$ | 35968.1 |
| 215 | 46225 | 9938375 | 14.6629 | 5.9907 | 2.33244 | 4.65116 | 675.44 | 36305.0 |
| 216 | 46656 | 10077696 | 14.6969 | 6.0000 | 2.33445 | 4.62963 | 678.58 | 36643.5 |
| 217 | 47089 | 10218313 | 14.7309 | 6.0092 | 2.33646 | 4.60829 | 681.73 | 36983.6 |
| 218 | 47524 | 10360232 | 14.7648 | 6.0185 | 2.33846 | 4.58716 | 684.87 | 37925.3 |
| 219 | 47961 | 10503459 | 14.7986 | 6.0277 | 234044 | 4.56621 | 688.01 | 37668.5 |
| 220 | 48400 | 10648000 | 14.8324 | 6.0368 | 2.34242 | 4.54545 | 691.15 | 38013.3 |
| 221 | 48841 | 10793861 | 14.8661 | 60459 | 2.34439 | 4.52489 | 694.29 | 38359.6 |
| 222 | 49284 | 10941048 | 14.8997 | 6.0550 | 2.34635 | 4.50450 | 697.43 | 38707.6 |
| 223 | 49729 | 11089567 | 14.9332 | 6.0641 | 2.34830 | 4.48431 | 700.58 | 39057.1 |
| 224 | 50176 | 11239424 | 14.9666 | 6.0732 | 2.35025 | 4.46429 | 703.72 | 39408.1 |

Squares, Cubes, Square Roots, Cube Roots, Logarithms, Etc.
(CONTINUED.)

| No. | Sq. | Cube. | Square <br> Root. | Cube <br> Root. | Log. | $\begin{gathered} 1000 \\ X \\ \text { Recip. } \\ \hline \end{gathered}$ | No. = Dia. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Circ'm | Area. |
|  | 5062 | 11390625 | 15.0000 | 6.0822 | 2.35218 | 4.44444 |  |  |
| 226 | 5107 | 11543176 | 15.0333 | 6.0912 | 2.35411 | 4.42478 | 710.00 | 40115.0 |
| 227 | 51529 | 11697083 | 15.0665 | 6.1002 | 2.35603 | 4.40529 | 713.14 | 40470.8 |
| 228 | 51984 | 11852352 | 15.099 | 6.1091 | 2.85793 | 4.38596 | 716.28 | 40828.1 |
| 229 | 52441 | 12008989 | 15.1327 | 6.1180 | 2.35984 | 4.36681 | 719.42 | 41187.1 |
| 230 | 52900 | 12167000 | 15.1658 | 6.1269 | 2.36173 | 4.34783 | 722.57 | 41547.6 |
| 231 | 53361 | 12326391 | 15.1987 | 6.1358 | 2.36361 | 4.32900 | 725.71 | 41909.6 |
| 232 | 53884 | 12487168 | 15.2315 | 6.1446 | 2.36549 | 4.31034 | 728.85 | 42273.3 |
| 233 | 54289 | 12649337 | 15.2643 | 6.1534 | 2.36736 | 4.29185 | 731.99 | 42638.5 |
| 234 | 54756 | 12812904 | 15.2971 | 6.1622 | 2.36922 | 4.27350 | 735.13 | 43005.3 |
| 235 | 5522 | 129778 | 15.32 | 6.17 | 2.371 | 4.25532 | 738. |  |
| 236 | 55696 | 13144256 | 15.3623 | 6.179 | 2.37291 | 4.23729 | 741.42 | 43743.5 |
| 238 | 56169 | 13312053 | 15.3948 | 6.188 | 2.37475 | 4.21941 | 744.56 | 44115.0 |
| 238 | 56644 | 13481272 | 15.4272 | 6.1972 | 2.37658 | 4.20168 | 747.70 | 44488.1 |
| 239 | 57121 | 13651919 | 15.4596 | 6.2058 | 2.37840 | 4.18410 | 750.84 | 44862.7 |
| 240 | 57600 | 13824000 | 15.4919 | 6.2145 | 2.38021 | 4.16667 | 753.98 | 45238.9 |
| 241 | 58081 | 13997521 | 15.5242 | 6.2231 | 2.38202 | 4.14938 | 757.12 | 45616.7 |
| 242 | 58564 | 14172488 | 15.5563 | 6.2317 | 2.38382 | 4.13223 | 760.27 | 45996.1 |
| 243 | 59049 | 14348907 | 15.5885 | 6.2403 | 2.38561 | 4.11523 | 763.41 | 46377.0 |
| 244 | 59536 | 14526784 | 15.6205 | 6.2488 | 2.38739 | 4.09836 | 766.55 | 46759.5 |
| 245 | 6002 | 1470612 | 15.65 | 6.257 | 2.3891 | 4.081 | 769.69 | 47143.5 |
| 246 | 60516 | 14886936 | 15.6844 | 6.265 | 2.39094 | 4.06504 | 772. | 47529.2 |
| 247 | 61009 | 15069223 | 15.7162 | 6.2743 | 2.392\%0 | 4.04858 | 775.97 | 47916.4 |
| 248 | 61504 | 15252992 | 15.7480 | 6.2828 | 2.39445 | 403226 | 779.12 | 48305.1 |
| 249 | 62001 | 15438249 | 15.7797 | 6.2912 | 2.39620 | 4.01606 | 782.26 | 48695.5 |
| 250 | 62500 | 15625000 | 15.8114 | 6.299 | 2.39794 | 4.00000 | 785.40 | 49087.4 |
| 251 | 63001 | 15813251 | 15.8430 | 6.3080 | 2.39967 | 3.98406 | 788.54 | 49480.9 |
| 252 | 63504 | 16003008 | 15.8745 | 6.3164 | 2.40140 | 3.96825 | 791 | 49875.9 |
| 253 | 64009 | 16194277 | 15.9060 | 6.3247 | 2.40312 | 3.95257 | 794.82 | 50272.6 |
| 254 | 645 | 16 |  |  | 2. | 3.98701 |  |  |
|  | 65025 | 1658137 | 15.9687 | 6.3413 | 2.40654 | 3.92157 | 801.11 | 51070.5 |
| 256 | 65536 | 16777216 | 16.0000 | 6.3496 | 2.40824 | 3.90625 | 804.25 | 51471.9 |
| 257 | 66049 | 16974593 | 16.0312 | 6.3579 | 2.40993 | 3.89105 | 807.39 | 51874.8 |
| 258 | 66564 | 17173512 | 16.0624 | 6.3661 | 2.41162 | 3.87597 | 810.53 | 52279.2 |
| 259 | 67081 | 17373979 | 16.0935 | 6.3743 | 2.41330 | 3.86100 | 813.67 | 52685.3 |
| 260 | 6.600 | 17576000 | 16.1245 | 6.3825 | 2.414 | 3.84615 | 816.81 | 53092.9 |
| 26 | 68121 | 17779581 | 16.1555 | 6.390 | 2.41664 | 3.83142 | 819.96 | 53502.1 |
| 262 | 68644 | 17984728 | 16.1864 | 6.3988 | 241830 | 3.81679 | 823.10 | 53912.9 |
| 263 | 69169 | 18191447 | 16.2173 | 6.4070 | 2.41996 | 3.80228 | 826.24 | 54325.2 |
| 264 | 69696 | 18399744 | 16.2481 | 6.4151 | 2.42160 | 3.78788 | 829.38 | 54739.1 |
| 265 | 70225 | 18609625 | 16.2788 | 6.4232 | 2.42325 | 3.77358 | 832.52 | 55154.6 |
| 266 | 70756 | 18821096 | 16.3095 | 6.4312 | 2.42488 | 3.75940 | 835.66 | 55571.6 |
| 267 | 71289 | 19034163 | 16.3401 | 6.4393 | 2.42651 | 3. ${ }^{1} 4532$ | 838.81 | 55990.3 |
| 268 | 71824 | 19248832 | 16.3707 | 6.4473 | 2.42813 | 3.73134 | 841.95 | 56410.4 |
| 269 | 72361 | 19465 | 16 | 6.4 | 2.42 | 3.717 | 845 | 2.2 |

## Squares, Cubes, Square Roots, Cube Roots, Logarithms, Etc.

(CONTINUED.)

| o. | Sq. | Cube. | Square Root. | Cube <br> Root. | Log. | $\begin{gathered} 1000 \\ X \\ \text { Recip. } \end{gathered}$ | No. = Dla. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Circ'm | Ar |
| 270 | 72900 | 19683000 | 164317 | 6.4 | 2.43136 | 3.70370 |  |  |
| 271 | 73441 | $199(12511$ | 16.4621 | 6.4713 | 2.43297 | 3.69004 | 851.37 | 57680.4 |
| 272 | 73984 | 20123648 | 16.4924 | 6.4792 | 2.43457 | 3.67647 | 854.51 | 58106.9 |
| 273 | 74529 | 20346417 | 16.5227 | 6.4872 | 2.43616 | 3.66300 | 857.66 | 58534.9 |
| 274 | 75076 | 20570824 | 16.5529 | 6.4951 | 2.43775 | 3.64964 | 860.80 |  |
| 275 | 75 | 2079687 | 16.5 | 6.5 | 2.438 | 3. | 863.94 |  |
| 276 | 7617 | 21024576 | 16.61 | 6.51 | 2.44091 | 3.62319 | 867.08 |  |
| 277 | 76729 | 21253933 | 16.64 | 6.518 | 2.44248 | 3.61011 | 870.22 | 60262.8 |
| 278 | 77784 | 21484952 | 16.673 | 6.5265 | 2.44404 | 3,59712 | 873.36 | 60698.7 |
| 279 |  | 21717639 | 16.703 | 6.5343 | 2.44560 | 3.58423 | 876.50 | 61136.2 |
| 280 | 78400 | 21952000 | 16.7332 | 6.5421 | 2.44716 | 3.57143 | 879.65 |  |
| 281 | 78961 | 2:2188041 | 16.7631 | 6.5499 | 2.44871 | 3.55872 | 882.79 |  |
| 282 | 79524 | 22425768 | 16.7929 | 6.55 | 2.45025 | 3.54610 | 885.93 | . 0 |
| 283 | 80089 | $2: 665187$ | 16.8226 | 6.5654 | 2.45179 | 3.5335 | 889.07 | 8 |
| 284 | 80656 | 22906304 | 16.8523 | 6.5731 | 2.45332 | 3.5211 | 892 |  |
| 285 | 81 | 231 | 16 | 6. | 2.4 | 3.50877 | 89 |  |
| 28 | 81 | 2339365 | 16.911 | 6.6 | 2.456 | 3.49650 | 898.50 | 4 |
| 287 | 82 | 2363990 | 16.941 | 6.59 | 2.457 | 3.484 | 901.64 | 2.5 |
| 288 | 82944 | 238878 ¢ | 16.970 | 6.603 | 2.45939 | 3.4722 | 904.78 |  |
| 89 | 83521 | 2413756 |  | 6.611 | 2.46090 | 3.46021 |  |  |
| 290 | 84100 | 24389000 | 17.029 | 6.6191 | 2.46240 | 3.44828 | 911.06 |  |
| 291 | 84681 | 24642171 | 17.0587 | 6.6267 | 2.46389 | 3.43643 | 914.20 | 66508.3 |
| 292 | 85264 | 24897088 | 17.0880 | 6.6343 | 2.46538 | 3.42466 | 917.35 |  |
| 293 | 85849 | 25153757 | 17.1172 | 6.6419 | 2.46687 | 3.41297 | 920.49 |  |
| 294 | 86436 | 25412184 | 17.1464 | 6.6494 | 2.46835 | 8.40136 | 923.63 |  |
| 295 | 87025 | 25672375 | 17.1756 | 6.656 | 2.46982 | 3.38983 | 926.77 |  |
| 296 | 87616 | 25934336 | 17.204 | 6.6644 | 2.4712 | 3.37838 | 929.91 |  |
| 297 | 88209 | 26198078 | 17.233 | 6.6719 | 2.4727 | 3.36700 | 933.05 | 69279.2 |
| 298 |  | 28463592 | 17.2627 | 6.67 | 2.4742 | 8.35570 | 936.19 | 69746.5 |
| 299 |  | 26730899 |  |  | 2.475 | 3.34448 | 939.34 |  |
| 100 | 90000 | 27000000 | 17.3205 | 6.69 | 2.4712 | 3.333 | 942.48 |  |
| 301 | 90601 | 27270901 | 17.3494 | 6.7018 | 2.47857 | 3.32226 | 945.62 | 71157.9 |
| 302 | 91204 | 27543608 | 17.3781 | 6.7092 | 2.48001 | 3.31126 | 948.76 | 71631.5 |
| 303 | 91809 | 27818127 | 17.4069 | 6.7166 | 2.48144 | 3.30033 | 951.90 | 72106.6 |
| 304 | 92416 | 28094464 | 17.4356 | 6.7240 | 2.48287 | 3.28947 |  |  |
| 305 | 93025 | 283726 | 17.46 | 6.73 | 2.484 | 3.278 | 958.19 |  |
| 306 | 9363 | 28652616 | 17.492 | 6.738 | 2.4857 | 3.2679 | 961. | 73541.5 |
| 307 | 94249 | 28934443 | 17.5214 | 6.74 | 2.4871 | 3.2573 | 964. | 74023.0 |
| 308 | 94864 | 29218112 | 17.5499 | 6.753 | 2.48855 | 3.24675 | 967.61 | 74506.0 |
| 309 | 95481 | 29503629 | 17.578 | 6.760 | 2.4899 | 3.23625 | 970. |  |
| 310 | 96100 | 29791000 | 17.6068 | 6.7679 | 2.49136 | 3.22581 | 973.89 | 75476.8 |
| 311 | 96721 | 30080231 | 17.6352 | 6.7752 | 2.49276 | 3.21543 | 977.04 | 75964.5 |
| 312 | 97344 | 30371328 | 17.6635 | 6.7824 | 2.49415 | 3.20513 | 980.18 | 764 |
| 313 | 97969 | 30664297 | 17.6918 | 6.7897 | 2.49554 | 3.19489 | 983.32 | 76944.7 |
| 314 | 98596 | 30959144 | 17.7200 | 6.796 | 2.4969 | 3.1847 | 986.4 | 77437.1 |

Squares, Cubes, Square Roots, Cube Roots, Logarithms, Etc.
(CONTINUED.)

| o. | Sq. | Cube. | Square Root. | Cube <br> Root. | Log. | $\begin{gathered} 1000 \\ \times \\ \text { Recip } \end{gathered}$ | No $=$ Dia. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Circ'm | Ar |
|  |  |  |  |  |  |  |  |  |
|  | 998 | 31554 | 17.7 | 6.8113 | 2.49969 | 3.16456 | 992.74 |  |
|  | 100489 | 31855013 | 17.8045 | 6.8185 | 2.50106 | 3.15457 |  |  |
|  | 101124 | 32157432 | 17.8326 | 6.8256 | 2.50243 | 3.14465 | 999.03 | 79422.6 |
| 319 | 101761 | 32461759 | 17.8606 | 6.8328 | 2.50379 | 3.13480 | 1002.2 | 79922.9 |
|  |  |  |  |  |  | 3.1 |  |  |
| 321 |  | 330 |  | 6.8470 | 2.506 | 3.11 |  |  |
| 322 | 103684 | 33388248 |  | 6.8 | 2.507 | 3.105 |  | 81433.2 |
| 323 | 104329 | 33698267 | 17.9722 |  |  | 3.09598 | 1014.7 | 81939.8 |
| 324 | 104978 | 34012224 | 18.0000 | 6.8683 | 2.51055 | 3.08642 |  | 82448.0 |
|  |  |  |  |  |  | 3.07692 |  |  |
|  | 106276 | 34645 | 18.05 | 6.8824 | 2.51322 | 3.06749 | 1024.2 | 83469.0 |
|  | 106929 | 34965 | 18.08 | 6.8894 | 2.514 | 3.05810 | 1027.3 | 83981.8 |
| 328 | 107584 | 3528 | 18.110 | 6.896 | 2.51587 | 3.04878 | 1030.4 | 84496.3 |
| 29 |  |  |  |  | 2.51720 |  |  |  |
|  |  |  |  |  |  |  |  |  |
| 331 | 109561 | 36264691 | 18.193 | 6.917 |  | 3. | 1039.9 | 0 |
| 332 | 110224 | 36594368 | 18.220 | 6.9244 | 2.52114 |  |  | 86569.7 |
| 333 | 110889 | 36926037 | 18.2483 | 6.9313 | 2.52244 | 3.00300 | 1046.2 | 87032.0 |
| 334 |  |  |  | 6.9382 | 2.52375 | 2.99401 | 1049.3 | 87615.9 |
|  |  |  |  |  |  |  |  | 88141.3 |
|  | 112 | 379 | 18 | 6.9 | 2.52 | 2.9 |  |  |
|  | 113569 | 38272 | 18 | 6.958 | 2.527 |  |  | 89196.9 |
| 2 | 114244 | 38614472 | 18.38 | 6.965 | 2.52 |  |  |  |
| 339 |  |  |  |  |  |  |  |  |
| 311 | 115600 | 39304000 |  |  |  |  |  |  |
| 341 | 116281 | 39651821 | 18.4662 | 69864 | 2.53275 | 2.932 | 1071.3 |  |
| 34. | 116964 | 40001688 | 18.4932 | 6.9932 | 2.53403 | 2.9239 | 1074.4 | 91863.3 |
| 343 | 117649 | 40353607 | 18.5203 | 7.0000 | 2.53529 | 2.91545 | 1077.6 | 92401.3 |
| 34 |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |
|  | 119716 | 4142173 | 18.6011 | 7.0203 | 2.539 | 2.890 | 1087.0 | 94024.7 |
| 347 | 120409 | 41781923 | 18.6278 | 7.0271 | 2.540 | 2.8 | 1090.1 | . |
| 348 | 121104 | 42144192 | 18.6548 | 7.0338 | 2.5415 |  | 1093.3 |  |
| 349 | 121801 | 42508549 | 18.6815 | 7.0106 | 2.51283 | 2.86 |  |  |
| 350 | 122500 | 42875000 | 18.7083 | 7.0473 | 2.54407 | 2.85744 | 1109.6 | 3011.3 |
| 351 | 123201 | 43243551 | 18.7350 | 7.0540 | 2.54531 | 2.84900 | 1102.7 | 96761.8 |
|  | 123904 | 43614208 | 18.7617 | 7.0607 | 2.54654 | 2.8409 | 1105.8 | 97314.0 |
| 35 | 1246 | 4398 | 18.7883 | ¢ 7.0674 | 2.54777 | 2.83286 | 1109.0 | 97867.7 |
| 35 |  |  | 18.8149 | 7.0740 | 2.549 | 2.82486 | 1112.1 |  |
| 355 | 126025 | 44738875 | 18.8414 | 7.0807 | 2.55023 | 2.81690 | 1115.3 | 98979.8 |
| 356 | 126736 | 45118016 | 18.8680 | 7.0873 | 255145 | 2.80899 | 1118.4 | 99538. 2 |
| 357 | 127449 | 45499293 | 18.8944 | 7.0940 | 2.55267 | 2.80112 | 1121.5 | 100098 |
| 358 | 128164 | 45882712 | 18.9209 | 7.1006 | 2.55388 | 2.79330 | 1124.7 | 100660 |
| 359 | 12888 | 4626 | 18.947 | 7.107 | 2.555 | 2.7855 | 1127 | 1012 |

Squares, Cubes, Square Roots, Cube Roots, Logarithms, Etc.
(CONTINUED.)

| No. | Sq. | Cube. | Square Root. | Cube <br> Root. | Log. | $\begin{gathered} 1000 \\ X \\ \text { Recip. } \end{gathered}$ | No. $=$ Dia. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Circ'm | Area. |
| 360 | 129600 | 46656 | 18.9 | 7.1138 | 2.55630 | 2. |  | 101788 |
| 361 | 130321 | 47045881 | 19.000 | 7.1204 | 2.55751 | 2.77 |  |  |
| 362 | 131044 | 47437928 | 19.0263 | 7.1269 | 2.55871 | 2.76 | 1137.3 | 102922 |
| 363 | 131769 | 47832147 | 19.0526 | 7.1335 | 2.55991 | 2.75482 | 1140.4 | 103491 |
| 364 | 132496 | 48228544 | 19.0788 | 7.1400 | 2.56110 | $2.747 \times 5$ | 1143.5 | 104062 |
| 365 | 1332 | 48627 | 19.1 | 7.1466 | 2.56 | 2.73 |  | 104635 |
| 366 | 13395 | 49027 | 19.131 | 7.1531 | 2.563 | 2.73 | 1149.8 | 105209 |
| 367 | 13468 | 494308 | 19.1572 | 7.159 | 2.56 | 2.724 | 1153.0 | 105785 |
| 808 | 135424 | 49836032 | 19.1833 | 7.1661 | 2.56585 | 2.71739 | 1156.1 | 106362 |
| 369 | 136161 | 50243409 | 19.2094 | 7.1726 | 2.56703 | 2.71003 | 1159.2 | 106941 |
| 310 | 136900 | 50653000 | 19.2354 | 7.1791 | 2.56820 | 2.70270 | 1162.4 | 107521 |
| 371 | 137641 | 51064811 | 19.2614 | 7.1855 | 2.56937 | 2.69542 | 1165.5 | 108103 |
| 372 | 138334 | 51478818 | 19.2873 | 7.1920 | 2.57054 | 2.68817 | 1168.7 | 108687 |
| $3 \% 3$ | 139129 | 51895117 | 19.3132 | 7.1984 | 2.57171 | 2.68097 | 1171.8 | 109272 |
| 374 | 139876 | 52313624 | 19.339 | 7.2048 | 2.57287 | 2.6738 | 1175.0 | 109858 |
| 375 | 140 | 5273 | 19.3 | 7.2 | 2.5 | 2.6 |  | 110447 |
| 376 | 1413 | 5315737 | 19.390 | 7.217 | 2.575 | 2.659 | 1181.2 | 111036 |
| 377 | 14212 | 5358263 | 19.41 | 7.22 | 2.5763 | 2.652 | 1181.4 | 111628 |
| 8 | 142884 | 54010152 | 19.4422 | 7.2304 | 2.57749 | 2.6155 | 1187.5 | 112221 |
| 9 | 143641 | 54439939 | 19.4679 | 7.2368 | 2.57864 | 2.638 |  | 112815 |
| 380 | 144400 | 54872000 | 19.493 | 7.2432 | 2.57978 | 2.631 | 1193.8 |  |
| 381 | 145161 | 55306341 | 19.5192 | 7.2495 | 2.58093 | 2.62467 | 1196.9 | 114009 |
| 382 | 145924 | 55742968 | 19.5448 | 7.2558 | 2.58206 | 2.61780 | 1200.1 | 114608 |
| 383 | 146689 | 56181887 | 19.5704 | 7.2622 | 2.58320 | 2.61097 | 1203.2 | 115209 |
| 384 | 147456 | 56623104 | 19.5959 | 7.2685 | 2.58433 | 2.60417 | 1206.4 | 115812 |
| 385 | 14822 | 57066625 | 19.621 | 7.274 | 2.5 | 2.597 | 1209.5 | 116416 |
| 386 | 148996 | 57512456 | 19.646 | 7.2811 | 2.586 | 2.59 | 1212.7 | 117021 |
| 387 | 149769 | 57960603 | 19.672 | 7.2874 | 2.5877 | 2.583 | 1215.8 | 117628 |
| 388 | 150544 | 58411072 | 19.6977 | 7.2936 | 2.5888 | 2.57732 | 1218.9 | 118237 |
| 389 | 151321 | 58863869 | 19.723 | 7.2999 | 2.58995 | 2.570 |  |  |
| 390 | 152100 | 59319000 | 19.7484 | 7.3061 | 2.59106 | 2.56410 | 1225.2 | 119459 |
| 391 | 152881 | 59776471 | 19.7737 | 7.3124 | 2.59218 | 2.55755 | 1228.4 | 120072 |
| 392 | 153664 | 60236288 | 19.7990 | 7.3186 | 2.59329 | 2.55102 | 1231.5 | 120687 |
| 393 | 154449 | 60698457 | 19.8242 | 7.3248 | 2.59439 | 2.54453 | 1234.6 | 121304 |
| 394 | 155236 | 61162984 | 19.8494 | 7.3310 | 2.59550 | 2.53807 | 1237.8 | 121922 |
| 395 | 1560 | 6162987 | 19.874 | 7.3372 | 2.59660 | 2.581 | 1240.9 | 122542 |
| 396 | 15681 | 6209913 | 19.8997 | 7.343 | 2.597 | 2.525 | 1244 | 123163 |
| 397 | 157609 | 62570773 | 19.9249 | 7.349 | 2.598 | 2.5188 | 1247 | 123786 |
| 398 | 158404 | 63044792 | 19.9499 | 7.3558 | 2.59988 | 2.51256 | 1250.4 | 124410 |
| 399 | 159201 | 63521199 | 19.9750 | 7.3619 | 2.6009 | 2.50627 | 1253 | 125036 |
| 400 | 160000 | 64000000 | 20.0000 | 7.3681 | 2.60206 | 2.50000 | 1256.6 | 125664 |
| 401 | 160801 | 64481201 | 20.0250 | 7.3742 | 2.60314 | 2.49377 | 1259.8 | 126293 |
| 402 | 161604 | 64964808 | 20.0499 | 7.3808 | 2.60423 | 2.48756 | 1262.9 | 126923 |
| 403 | 162409 | 65450827 | 20.0749 | 7.3864 | 2.60531 | 2.48139 | 1266.1 | 127556 |
| 404 | 163216 | 6593926 | 20.099 | 7.392 | 2.6063 | 2.4752 | 1269.2 | 128190 |

Squares, Cubes, Square Roots, Cube Roots, Logarithms, Etc.
(CONTINUED.)

| No. | Sq. | Cube. | Square Root. | Cube <br> Root. | Log. | $\begin{gathered} 1000 \\ X \\ \text { Recip. } \end{gathered}$ | No. = Dia. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Circ'm | Area. |
| 405 | 164025 | 66430125 | 20.1246 | 7.3986 | 2.60746 | 2.46914 | 1272.3 | 128825 |
| 406 | 164836 | 66923416 | 20.1494 | 7.4047 | 2.60853 | 2.46305 | 1275.5 | 129462 |
| 407 | 165649 | 67419143 | 20.1742 | 7.4108 | 2.60959 | 2.45700 | 1278.6 | 130100 |
| 408 | 166464 | 67917312 | 20.1990 | 7.4169 | 2.61066 | 2.45098 | 1281.8 | 130741 |
| 409 | 167281 | 68417929 | 20.2237 | 7.4229 | 2.61172 | 2.44499 | 12849 | 131382 |
| 410 | 168100 | 68921000 | 20.24 | 7.4290 | 2.612 | 2.43902 | 1288.1 | 132025 |
| 11 | 168921 | 69426531 | 20.2731 | 7.4350 | 2.61384 | 2.43309 | 1291.2 | 132670 |
| 412 | 169744 | 69934528 | 20.2978 | 7.4410 | 2.61490 | 2.42718 | 1291.3 | 133317 |
| 413 | 170569 | 70444997 | 20.3224 | 7.4470 | 2.61595 | 2.42131 | 1297.5 | 133965 |
| 414 | 171396 | 70957944 | 20.3470 | 7.4530 | 2.61700 | 2.41546 | 1300.6 | 134614 |
| 415 | 172225 | 71473375 | 20.3715 | 7.4590 | 2.61805 | 2.40964 | 1303.8 | 135265 |
| 416 | 173056 | 71991296 | 20.3961 | 7.4650 | 2.61909 | 2.40385 | 1306.9 | 135918 |
| 417 | 173889 | 78511713 | 20.4206 | 7.4710 | 2.62014 | 2.398 | 1310.0 | 186572 |
| 418 | 174724 | 73034632 | 20.4450 | 7.4770 | 2.62118 | 2.39234 | 1313.2 | 137228 |
| 419 | 175561 | 73560059 | 20.4695 | 7.4829 | 2.62221 | 2.38664 | 1316.8 | 137885 |
| 0 | 176400 | 74088000 | 20.4939 | 7.4889 | 2.62325 | 2.38095 | 1319.5 | 138544 |
| 421 | 177241 | 74618161 | 20.5183 | 7.4948 | 262428 | 2.37530 | 1322.6 | 139205 |
| 422 | 178084 | 75151448 | 20.5426 | 7.5007 | 2.62531 | 2.36967 | 1325.8 | 139867 |
| 423 | :789\%9 | 75686967 | 20.5670 | 7.5067 | 2.62634 | $2.3640 \sim$ | 1328.9 | 140531 |
| 424 | 179776 | 76225024 | 20.5913 | 7.5126 | 2.62737 | 2.35849 | 1332.0 | 141196 |
| 425 | 180625 | 76765625 | 20.6155 | 7.5185 | 2.62839 | 2.35294 | 1335.2 | 141863 |
| 426 | 181476 | 77308776 | 20.6398 | 7.5244 | 2.62941 | 2.34742 | 1338 | 142531 |
| 427 | 182329 | 77854483 | 20.6640 | 7.5302 | 2.63043 | 2.34192 | 1341.5 | 143201 |
| 428 | 183184 | 78402752 | 20.6882 | 7.5361 | 2.63144 | 2.33645 | 1344.6 | 143872 |
| 429 | 184041 | 78953589 | 20.7123 | 7.5420 | 2.63246 | 2.38100 | 1347.7 | 141545 |
| 430 | 184900 | 79507000 | 20.7364 | 7.5478 | 2.63347 | 2.32558 | 1350.9 | 145220 |
| 431 | 185761 | 80062991 | 20.7605 | 7.5537 | 2.63448 | 2.32019 | 1354.0 | 145896 |
| 432 | 186624 | 80621568 | 20.7846 | 7.5595 | 2.63548 | 2.31482 | 1357.2 | 146574 |
| 433 | 187489 | 81182737 | 20.8087 | 7.5654 | 2.63649 | 2.30947 | 1360.3 | 147254 |
| 434 | 188356 | 81746504 | 208327 | 7.5712 | 2.63749 | 2.30415 | 1363.5 | 147934 |
| 435 | 189225 | 82312875 | 20.856 | 7.5770 | 2.63849 | 2.29885 | 1366.6 | 148617 |
| 436 | 190096 | 82881856 | 20.8806 | 7.5828 | 2.63949 | 2.29358 | 1369.7 | 149301 |
| 437 | 190969 | 83453453 | 20.9045 | 7.5886 | 2.64048 | 228833 | 1372.9 | 149987 |
| 438 | 191844 | 84027672 | 20.9281 | 7.5944 | 2.64147 | 2.28311 | 1376.0 | 150674 |
| 439 | 192721 | 84604519 | 20.9523 | 7.6001 | 2.64246 | 2.27790 | 1379.2 | 151363 |
| 440 | 193600 | 85184000 | 20.9762 | 7.6059 | 2.64345 | 2.27273 | 1382.3 | 152053 |
| 441 | 194481 | 85766121 | 21.0000 | 7.6117 | 2.64444 | $2.26 \pi 57$ | 1385.4 | 152745 |
| 442 | 195364 | 86350888 | 21.0238 | 7.6174 | 2.64542 | 226244 | 1388.6 | 153439 |
| 443 | 196249 | 86938307 | 21.0476 | 7.6232 | 2.64640 | 2.25734 | 1391.7 | 154134 |
| 444 | 197136 | 87528384 | 21.0713 | 7.6289 | 2.64738 | 2.25225 | 1394.9 | 154830 |
| 445 | 198025 | 88121125 | 21.0950 | 7.6346 | 2.64836 | 2.24719 | 1398.0 | 155528 |
| 446 | 198916 | 88716536 | 21.1187 | 7.6403 | 2.64933 | 2.24215 | 1401.2 | 156228 |
| 447 | 199809 | 89314623 | 21.1424 | 7.6460 | 2.65031 | 2.23714 | 1404.3 | 156930 |
| 448 | 200704 | 89915392 | 21.1660 | 7.6517 | 2.65128 | 2.23214 | 1407.4 | 157633 |
| 449 | 201601 | 90518848 | 21.1896 | 7.6574 | 2.6522 | 2.2271 | 1410. | 158337 |

Squares, Cubes, Square Roots, Cube Roots, Logarithms, Etc.
(CONTINUED.)

| No. | Sq. | Cube. | Square <br> Root. | Cube <br> Root. | Log. | $\begin{gathered} 1000 \\ \times \\ \text { Recip. } \end{gathered}$ | No. = Dia. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Circ'm | Area. |
| 450 | 202500 | 9112500 | 21.2132 | 7.6631 | 2.65321 | 2.22222 |  |  |
| 451 | 203401 | 91733851 | 21.2368 | 7.6688 | 2.65418 | 2.21730 |  | 159751 |
| 452 | 204304 | 92345408 | 21.2603 | 7.6744 | 2.65514 | 2.21239 | 142 | 160460 |
| 453 | 205209 | 92959677 | 21.2838 | 7.6801 | 2.65610 | 2.20751 | 1423.1 | 161171 |
| 454 | 206116 | 93576664 | 21.3073 | 7.6857 | 2.65706 | 2.20264 | 1426.3 | 161883 |
|  | 207025 | 94196375 | 21.3307 | 7.6914 | 2.65801 | 2.19780 | 1429.4 | 162597 |
| 456 | 207936 | 94818816 | 21.3542 | 7.6970 | 2.65896 | 2.19298 | 1432.6 | 163313 |
| 457 | 208849 | 95443993 | 21.3776 | 7.7026 | 2.65992 | 2.18818 | 1435 | 164030 |
| 458 | 209764 | 96071912 | 21.4009 | 7.7082 | 266087 | 2.18341 | 1438.9 | 164748 |
| 459 | 210681 | 96702579 | 21.4243 | 7.7138 | 2.66181 | 2.17865 | 1442.0 | 165468 |
| 460 | 21160 | 9733600 | 21.4476 | 7.7194 | 2.66 | 2.17 |  | 166190 |
| 461 | 212521 | 97972181 | 21.4709 | 7.7250 | 2.663 | 2.16920 | 1448.3 | 166914 |
| 462 | 213444 | 98611128 | 21.4942 | 7.730 | 2.66464 | 2.1645 | 1451 | 167639 |
| 463 | 214369 | 99252847 | 21.5174 | 7.7362 | 2.66558 | 2.1598 | 1454 | 168365 |
|  |  |  | 21.5407 | 7.7418 | 2.66652 | 2.1551 | 1457. |  |
| 465 | 216225 | 100544625 | 21.5639 | 7.7473 | 2.66745 | 2.15054 | 1460.8 | 169823 |
| 466 | 217156 | 101194696 | 21.5870 | 7.7529 | 2.66839 | 2.14592 | 1464.0 | 170554 |
| 467 | 218089 | 101847563 | 21.6102 | 7.7584 | 2.66932 | 2.14133 | 1467. | 171287 |
| 468 | 219024 | 102503232 | 21.6333 | 7.7639 | 2.67025 | 2.13675 | 1470.3 | 172021 |
| 469 | 219961 | 108161709 | 21.6564 | 7.7695 | 2.67117 | 2.13220 | 1473.4 | 172757 |
| 470 | 220900 | 10382300 | 21.679 | 7.7750 | 2.67210 | 2.127 | 1476.5 | 173494 |
| 471 | 221841 | 104487111 | 21.7025 | 7.7805 | 2.673 | 2.12314 | 1479 | 174234 |
| 472 | 222784 | 105154048 | 21.725 | 7.7860 | 2.67394 | 2.118 | 148 | 174974 |
| 73 | 223729 | 105823817 | 21.7486 | 7.7915 | 2.67486 | 2.1141 | 1486 | 175716 |
| 74 | 224676 | 106496424 | 21.7715 | 7.7970 | 2.67578 | 2.10971 | 1489.1 |  |
| 475 | 225625 | 107171875 | 21.7945 | 7.8025 | 2.67669 | 2.10526 | 1492.3 | 177205 |
| 476 | 226576 | 107850176 | 21.8174 | 7.8079 | 2.67761 | 2.10084 | 1495 | 177952 |
| 477 | 227529 | 108531333 | 21.8403 | 7.8134 | 2.67852 | 2.09644 | 1498.5 | 178701 |
| 478 | 228484 | 109215352 | 21,8632 | 7.8188 | 2.67943 | 2.09205 | 1501.7 | 179451 |
| 479 | 229441 | 109902239 | 21.8861 | 7.8243 | 2.68034 | 2.08768 | 1504.8 | 180203 |
|  | 230400 | 110592000 | 21.9089 | 7.829 | 2.68124 | 2.08333 | 1508.0 | 180956 |
|  | 231361 | 111284641 | 21.9317 | 7.8352 | 2.682 | 2.07900 |  | 181711 |
| 482 | 232324 | 111980168 | 21.9545 | 7.8406 | 2.68305 | 2.07469 | 1514.3 | 182467 |
| 483 | 233289 | 112678587 | 21.9773 | 7.8160 | 2.68395 | 2.07039 | 1517.4 | 183225 |
| 484 | 234256 | 113379904 | 22.0000 | 7.8514 | 2.68485 | 2.06612 | 1520.5 | 183984 |
| 485 | 235225 | 114084125 | 22.0237 | 7.8568 | 2.68574 | 2.06186 | 1523.7 | 184745 |
| 486 | 236196 | 114791256 | 22.0454 | 7.8622 | 2.68664 | 2,05761 | 1526.8 | 185508 |
| 487 | 237169 | 115501303 | 22.0681 | 7.8676 | 268753 | 2.05339 | 1530.0 | 1862\%2 |
| 488 | 238144 | 116214272 | 22.0907 | 78730 | 2.68842 | 2.04918 | 1533.1 | 187038 |
| 489 | 239121 | 116930169 | 22.1133 | 7.8784 | 2.68931 | 2.04499 | 1536.2 | 187805 |
| 490 | 240100 | 117649000 | 22.1359 | 7.8837 | 2.69020 | 2.04082 | 1539.4 | 188574 |
| 491 | 241081 | 118370771 | 22.1585 | 7.8891 | 2.69108 | 2.03666 | 1542.5 | 189345 |
| 492 | 242064 | 119095488 | 22.1811 | 7.8944 | 2.69197 | 2.03252 | 1545.7 | 190117 |
| 493 | 243049 | 119823157 | 22.2036 | 7.8998 | 2.69285 | 2.02840 | 1548.8 | 190890 |
| 494 | 244036 | 12055378 | 22.2261 | 7.905 | 2.69373 | 2.02429 | 1551. | 191665 |

Squares, Cubes, Square Roots, Cube Roots, Logarithms, Etc.
(CONTINUED.)

| No. | Sq. | Cube. | Square Root. | Cube <br> Root. | Log. | $\begin{gathered} 1000 \\ \text { X } \\ \text { Recip. } \\ \hline \end{gathered}$ | No. = Dia. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Circ'm | Area. |
| 48 | 245025 | 121287375 | 22.2486 | 7.9105 | 2.69461 | 2.02020 |  | 192442 |
| 496 | 246016 | 122023936 | 22.2711 | 7.9158 | 2.69548 | 2.01613 | 1558.2 | 193221 |
| 497 | 247009 | 122763473 | 22.2935 | 7.9211 | 2.69636 | 2.01207 | 1561.4 | 194000 |
| 498 | 248004 | 123505992 | 22.3159 | 7.9264 | 2.69723 | 2.00803 | 1564.5 | 194782 |
| 499 | 249001 | 124251499 | 22.3383 | 7.9817 | 2.69810 | 2.00401 | 1567.7 | 195565 |
| 500 | 250000 | 1250000 | 22.360 | 7.93 | 2.698 | 2.000 | 1570.8 | 196350 |
| 501 | 251001 | 125751501 | 22.3830 | 7.942 | 2.69984 | 1.996 | 1573.9 | 197136 |
| 502 | 252004 | 12650600 | 22.4054 | 7.947 | 2.70070 | 1.992 | 1577.1 | 197923 |
| 503 | 253009 | 127263527 | 22.4277 | 7.9528 | 2.70157 | 1.98807 | 1580.2 | 198713 |
| 504 | 254016 | 128024064 | 22.4499 | 7.9581 | 2.70243 | 1.98413 | 1583.4 | 199504 |
| 505 | 255025 | 128787625 | 22.4722 | 7.9634 | 2.70329 | 1.98020 | 1586.5 | 200296 |
| 506 | 256036 | 129554216 | 22.4944 | 7.9686 | 2.70415 | 1.97629 | 1589.7 | 201090 |
| 507 | 257049 | 130323843 | 22.5167 | 7.9739 | 2.70501 | 1.9723 | 1592.8 | 201886 |
| 508 | 258064 | 131096512 | 22.5389 | 7.9791 | 2.70586 | 1.9685 | 1595.9 | 202683 |
| 509 | 259081 | 131872229 | 22.5610 | 7.9843 | 2.70672 |  | 1599.1 | 203482 |
| 510 | 260 | 13 | 22 | 7.9 | 2.70757 | 1.96 | 1602.2 | 204282 |
| 511 | 261121 | 133432831 | 22.6053 | 7.994 | 2.70842 | 1.9560 | 1605.4 | 205084 |
| 512 | 262144 | 134217728 | 22.6274 | 8.000 | 2.70927 | 1.95312 | 1608.5 | 205887 |
| 513 | 263169 | 135005697 | 22.6495 | 8.0052 | 2.71012 | 1.94932 | 1611.6 | 206692 |
| 514 | 264196 | 135796744 | 22.6716 | 8.0104 | 2.71096 | 1.94553 | 1614.8 | 207499 |
| 515 | 265225 | 135590875 | 22.6936 | 8.015 | 2.71181 | 1.941 | 1617.9 | 208307 |
| 516 | 266256 | 137388096 | 22.7156 | 8.0208 | 2.712 | 1.987 | 1621 | 209117 |
| 517 | 267289 | 138188413 | 22.7376 | 8.0260 | 2.71349 | 1.934 | 1624.2 | 209928 |
| 518 | 268324 | 138991832 | 22.7596 | 8.0311 | 2.71433 | 1.93050 | 1627.3 | 210741 |
| 519 | 269361 | 139798359 | 22.7816 | 8.036 | 2. | 1. |  |  |
|  | 270400 |  |  | 8.0415 | 2.71600 | 192308 | 1633.6 | 212372 |
| 521 | 271441 | 141420761 | 22.8254 | 8.0466 | 2.71684 | 1.91939 | 1636.8 | 213189 |
|  | $2 \pi 2484$ | 142236648 | 22.8473 | 80517 | 2.71767 | 191571 | 1639.9 | 214008 |
| 523 | 273529 | 143055667 | 22.8692 | 8.0569 | 2.71850 | 1.91205 | 1643.1 | 214829 |
| 524 | 274576 | 143877824 | 22.8910 | 8.0620 | 2.71933 | 1.90840 |  | 215651 |
| 525 | 275625 | 14470312 | 22.912 | 8.067 | 2.720 | 1.90476 | 1649.3 | 216475 |
| 526 | 276676 | 145531576 | 22.934 | 8.07 | 2.7209 | 1.901 | 1652.5 | 217301 |
| 5 | 277729 | 146363183 | 22.9565 | 8.077 | 2.72181 | 1.89753 | 1655.6 | 218128 |
| 528 | 278784 | 147197952 | 22.978 | 8.08 | 2.72263 | 1.89394 | 1658.8 | 218956 |
| 529 | 27981 | 14 | 23.000 | 8.087 | 2.7234 | 1.89036 | 1661.9 | 219787 |
|  | 280900 | 148877000 | 23.0217 | 8.0927 | 2.72428 | 1.88679 | 1665.0 | 220618 |
| 531 | 281961 | 149721291 | 23.0434 | 8.0978 | 2.72509 | 1.88324 | 1668.2 | 221452 |
| 532 | 283024 | 150568768 | 23.0651 | 8.1028 | 2.72591 | 1.87970 | 1671 | 222287 |
| 533 | 284089 | 151419427 | 23.0868 | 8.1079 | 2.72673 | 1.87617 | 1674.5 | 223123 |
| 534 | 28515 | 152273304 | 23.1084 | 8.1130 | 2.7275 | 1.872 | 1677.6 | 223961 |
|  | 28622 | 153130375 | 23.1301 | 8.1180 | 2.72835 | 1.86916 | 1680.8 | 224801 |
| 536 | 287296 | 153990656 | 23.1517 | 8.1231 | 2.72916 | 1.86567 | 1683.9 | 225642 |
| 537 | 288369 | 154854153 | 23.1733 | 8.1281 | 2.72997 | 1.86220 | 1687.0 | 226484 |
| 538 | 289444 | 155720872 | 23.1948 | 8.1332 | 2.73078 | 1.85874 | 1690.2 | 227329 |
| 539 | 290521 | 156590819 | 23.2164 | 8.1382 | 2.7315 | 1.85529 | 1693.3 | 228175 |

Squares, Cubes, Square Roots, Cube Roots, Logarithms, Etc.
(CONTINUED.)

| No. | Sq. | Cube. | Square Root. | Cube <br> Root. | Log. | $\begin{gathered} 1000 \\ \text { X } \\ \text { Recip. } \end{gathered}$ | No. = Dia. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Circ'm | Area. |
|  | 291600 | 157464000 | 23.2379 | 8.1433 | 273239 | 1.85185 | 1696.5 | 229022 |
| 1 | 292681 | 158340421 | 23.2594 | 8.1483 | 2.73320 | 1.84843 |  | 229871 |
| 542 | 293764 | 159220088 | 23.2809 | 8.1533 | 2.73400 | 1.84502 | 170 | 230722 |
| 543 | 294849 | 160103007 | 23.3024 | 8.1583 | 2.73480 | 1.84162 | 1705.9 | 231574 |
| 544 | 295936 | 160989184 | 23.3238 | 8.1633 | 2.73560 | 1.8382 | 1709.0 | 232428 |
| 545 | 2970 | 16187 | 23.3 | 8.1 | 2.73640 | 1.83 | 1712.2 | 233283 |
| 546 | 298116 | 1627713 | 23.366 | 8.17 | 2.73719 | 1.83150 | 1715.3 | 234140 |
|  | 299209 | 1636673 | 23.388 | 8.1783 | 2.73799 | 1.82815 | 1718.5 | 234998 |
| 548 | 300304 | 16456659 | 23.4094 | 8.1833 | 1-73878 | 1.82482 | 1721.6 | 235858 |
| 549 | 301401 | 165469149 | 23.4307 | 8.1882 | 2.73957 | 1.82149 | 1724.7 | 236720 |
| 550 | 302500 | 166375000 | 23.4521 | 8.1932 | 2.74036 | 1.818 | 1727.9 | 237583 |
| 551 | 303601 | 167284151 | 23.4734 | 8.1982 | 2.74115 | 1.81 |  | 238448 |
| 552 | 304704 | 168196608 | 23.4947 | 8.2031 | 2.74194 | 1.81159 | 1734.2 | 239314 |
| 553 | 305809 | 169112377 | 23.5160 | 8.2081 | 2.74273 | 1.80832 |  | 240182 |
| 554 | 306916 | 170031464 | 23.5372 | 8.2130 | 2.74351 | 1.80505 |  | 241051 |
|  | 30 | 1709 | 23 | 8.2 | 2. | 1.8 |  | 241922 |
| 556 | 30913 | 17187961 | 23.5797 | 8.2229 | 2.74507 | 1.798 |  | 242795 |
|  | 31024 | 17280869 | 23.6008 | 8.2278 | 2.74586 | 1.7953 | 1749.9 | 243669 |
| 558 | 311364 | 173741112 | 23.6220 | 8.2327 | 274663 | 1.79211 | 1753.0 | 244545 |
| 559 | 312481 | 174676879 | 23.6432 | 8.2377 | 2.74741 | 1.78891 | 1756.2 | 245422 |
| 560 | 313600 | 175616000 | 236643 | 8.2426 | 2.74819 | 1.78571 | 1759.3 | 246301 |
| 561 | 314721 | 176558481 | 23.6854 | 8.2475 | 2.74896 | 1.78253 | 1762.4 | 247181 |
| 562 | 315844 | 177504328 | 23.7065 | 8.2524 | 2.74974 | 1.77936 | 1765.6 | 248063 |
| 563 | 316969 | 178453547 | 23.7276 | 8.2573 | 2.75051 | 1.77620 | 1768.7 | 248947 |
| 564 | 318096 | 179406144 | 23.7487 | 8.2621 | 2.751 | 1.77305 |  |  |
|  | 3192 | 18636212 | 23.769 | 8.267 | 2.752 | 1.769 | 1775.0 | 250719 |
|  | 320356 | 18132149 | 23.790 | 8.2719 | 2.752 | 1.766 | 1778.1 | 251607 |
|  | 321489 | 18288426 | 23.8118 | 8.2768 | 2.75358 | 1.76367 | 1781.3 | 252497 |
| 808 | 322624 | 183250432 | 23.8328 | 8.2816 | 2.75435 | 1.76056 | 1784.4 | 253388 |
| 569 | 323761 | 184220009 | 23.8537 | 8.2865 | 2.75511 | 1.75747 | 1787.6 |  |
| 570 | 324900 | 185193000 | 23.8747 | 8.2913 | 2.755 | 1.75439 | 1790.7 | 255176 |
| 571 | 328041 | 186169411 | 23.8956 | 8.2962 | 2.75664 | 1.75131 | 1793.9 | 256072 |
| 572 | 327184 | 187149248 | 23.9165 | 8.3010 | 2.75740 | 1.74825 | 1797.0 | 256970 |
| 573 | 328329 | 188132517 | 23.937 | 8.3059 | 2.75815 | 1.74520 | 1800.1 | 257869 |
| 574 | 329476 | 189 |  | 8.31 | 2.758 | 1.742 |  |  |
|  | 330625 | 190109375 | 23.9792 | 8.8155 | 2.75967 | 1.73913 | 1806.4 | 259672 |
| 576 | 331776 | 191102976 | 24.0000 | 8.3203 | 2.76042 | 1.73611 | 1809.6 | 260576 |
| 518 | 332929 | 192100033 | 24.0208 | 8.3251 | 2.76118 | 1.73310 | 1812.7 | 261482 |
| 578 | 334084 | 193100552 | 24.0416 | 8.3300 | 2.76193 | 1.73010 | 1815.8 | 262389 |
| 579 | 335241 | 194104539 | 24.0624 | 8.33 | 2.76268 | 1.78712 | 1819.0 | 263298 |
| 580 | 336400 | 195112000 | 24.0832 | 8.3396 | 2.76343 | 1.72414 | 1822.1 | 264208 |
| 581 | 337561 | 196122941 | 24.1039 | 8.3443 | 2.76418 | 1.72117 | 1825.3 | 265120 |
| 582 | 338724 | 197137368 | 24.1247 | 8.3491 | 2.76492 | 1.71821 | 1828.4 | 266033 |
| 583 | 3398 | 198155287 | 24.1454 | 8.3539 | 2.76567 | 1.71527 | 1831.6 | 266948 |
| 584 | 3410 | 19917670 | 24.1 | 8.35 | 2.76641 | 1.71233 | 1834 | 267 |

# Squares, Cubes, Square Roots, Cube Roots, Logarithms, Etc. 

(CONTINUED.)

| No. | Sq. | Cube. | Square <br> Root. | Cube <br> Root. | Log. | $\begin{gathered} 1000 \\ \times \\ \text { Recip. } \end{gathered}$ | No. $=$ Dia, |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Circ'm | Area. |
| 58 | 3422 | 20020 |  | 8.3634 | 2.76716 | 1.70940 |  | 268783 |
| 58 | 34339 | 201230056 | 24.2074 | 8.3682 | 2.76790 | 1.70649 | 1841.0 | 269701 |
| 58 | 344569 | 212262003 | 24.2281 | 8.3730 | 2. 76864 | 1.70358 | 1844.1 | 270624 |
| 588 | 34574 | 203297472 | 24.2487 | 8.3777 | 2.76938 | 1.70068 | 1847.3 | 271547 |
| 589 | 346921 | 204336469 | 24.2693 | 8.3825 | 2.77012 | 1.69779 | 1850.4 |  |
| 590 | 348100 | 205379000 | 24.2899 | 8.38 | 2.77085 | 1.69492 |  |  |
| 591 | 349281 | 206425071 | 24.3105 | 8.3919 | 2.77159 | 1.69205 | 1856.7 | 274325 |
| 592 | 350464 | 207474688 | 24.3311 | 8.3967 | 2.77232 | 1.68919 | 1859.8 | 275254 |
| 593 | 351649 | 208527857 | 24.3516 | 8.4014 | 2.77305 | 1.68634 | 1863.0 | 276184 |
| 594 | 352836 | 209584584 | 24.3721 | 8.4061 | 2.77379 | 1.68350 | 1866.1 | 277117 |
|  | 35 | 210 | 24. | 8. | 2.77 | 1.680 | 1869.3 | 278051 |
| 596 | 35521 | 21170873 | 24.418 | 8.415 | 2.77525 | 1.677 | 1872.4 | 278986 |
| 597 | 356409 | 212776173 | 24.433 | 8.420 | 2.7759 | 1.675 | 1875.5 | 279923 |
| - | 357604 | 213847192 | 24.4540 | 8.4249 | 2.77670 | 1.67224 | 1878.7 | 280862 |
| 99 | 358801 | 214921799 | 24.4745 | 8.4296 | 2.77743 | 1.66945 |  |  |
| 600 | 360000 | 216000000 | 24.4949 | 8.4343 | 2.77815 | 1.666 | 1885.0 | 282743 |
| 601 | 361201 | 217081801 | 24.5153 | 8.4390 | 2.77887 | 1.66389 | 1888.1 | 283687 |
| 602 | 362404 | 218167208 | 24.5357 | 8.4437 | 2.77960 | 1.66113 | 1891.2 | 284631 |
| 603 | 363609 | 219256227 | 24.5561 | 8.4484 | 2.78032 | 1.65837 | 1894.4 | 285578 |
| 604 | 364816 | 220348864 | 24.5764 | 8.4530 | 2.78104 | 1.65563 | 1897.5 | 286526 |
|  | 366 |  | 24.5 | 8.4 | 2.78176 |  | 1900.7 |  |
|  | 367236 | 222545016 | 24.6171 | 8.4623 | 2.78247 | 1.650 | 1903.8 | 288426 |
| 607 | 368449 | 223648543 | 246374 | 8.4670 | 2.78319 | 1.647 | 1907 | 289879 |
| 608 | 369664 | 224755712 | 24.6577 | 8.4716 | 2.78890 | 1.64474 | 1910.1 | 290333 |
| 609 | 370881 | 225866529 | 24.6779 | -8.4763 | 2.78462 | 1.64204 | 1913.2 |  |
| 610 | 372100 | 226981000 | 24.698 | 8.48 | 2.7 | 1.6 | 1916.4 | 292347 |
| 611 | 373321 | 228099131 | 24.718 | 8.4856 | 2.78604 | 1.63666 | 1919 | 293206 |
| 61 | 374544 | 229220928 | 24.73 | 8.4902 | 2.78675 | 1.633 | 1922. | 294166 |
| 613 | 37576 | 23034639 | 24.758 | 8.4948 | 2.78746 | 1.63132 | 1925.8 | 295128 |
| 61 |  | 2314755 | 2 |  | 2. |  | 19 |  |
|  |  |  | 24.7992 | 8.5040 | 2.78888 | 1.6260 | 1932.1 | 29021 |
| 616 | 379456 | 233744896 | 24.8193 | 8.5086 | 2.78958 | 1.62338 | 1935.2 | 298024 |
| 617 | 380689 | 234885113 | 24.8395 | 85132 | 2.79029 | 1.62075 | 1938.4 | 298992 |
| 618 | 381924 | 236029032 | 24.8596 | 8.5178 | 2.79099 | 1.61812 | 1941.5 | 299962 |
| 619 | 383161 | 237176 | 24.8797 | 8.52 | 2.79169 | 1.61551 | 1944.7 |  |
| 620 | 384 | 238328000 | 24.899 | 8.527 | 2.792 | 1.612 | 1947.8 | 301907 |
| 621 | 38564 | 239483061 | 24.9199 | 8.531 | 2.79309 | 1.6103 | 1950.9 | 302882 |
| 62 | 386884 | 240641848 | 24.9399 | 8.536 | 2.79379 | 1.60772 | 1954.1 | 303858 |
| 623 | 388129 | 241804367 | 24.9600 | 8.5408 | 2.79449 | 1.60514 | 1957.2 | 304836 |
| 624 | 389376 | 242970624 | 24.9800 | 8.5453 | 2.79518 | 1.60256 | 1960.4 | 305815 |
| 625 | 390625 | 244140625 | 25.0000 | 8.5499 | 2.79588 | 1.60000 | 1963.5 | 306796 |
| 626 | 391876 | 245314376 | 25.0200 | 8.5544 | 2.79657 | 1.59744 | 1966.6 | 307779 |
| 62 | 393129 | 246491883 | 25.0400 | 8.5590 | 2.7972' | 1.59490 | 1969.8 | 308763 |
| 628 | 394384 | 247673152 | 25.0599 | 8.56 | 2.797 | 1.59236 | 1972.9 | 309748 |
| 29 | 3956 | 48858 | 25.0 | 8.56 | 2.798 | 1.589 | 197 | 310 |

Squares, Cubes, Square Roots, Cube Roots, Logarithms, Etc.
(CONTINUED.)

| No. | Sq. | Cube. | Square <br> Root. | Cube <br> Root. | Log. | $\begin{gathered} 1000 \\ X \\ \text { Recip. } \end{gathered}$ | No. = Dia. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Circ'm | Area. |
|  | 396900 | 250047000 | 25.0998 | 8.5 | 2.79934 | 1. |  | 31172 |
| 631 | 398161 | 251239591 | 25.1197 | 8.5772 | 2.80003 | 1.5847 | 1982.4 | 312715 |
| 632 | 399424 | 252435968 | 25.1396 | 8.5817 | 2.80072 | 1.58 | 1985. | 313707 |
| 633 | 400689 | $25363613 \%$ | 25.1595 | 8.5862 | $2.8 \cup 140$ | 1.57978 | 1988. | 314700 |
| 634 | 401956 | 254840104 | 25.1794 | 8.5907 | 2.80209 | 1.577 | 1991.8 | 315696 |
| 63 | 4032 | 2560 | 25.1 | 85 | 2.80 | 1.57 | 19949 | 316692 |
| 63 | 404496 | 257259456 | 25.219 | 8.5997 | 2.803 | 1.5 | 1998.1 | 317690 |
| 63 | 405769 | 258474853 | 25.2389 | 8.60 | 2.8041 | 1.569 | 2001.2 | 318690 |
| 638 | 407044 | 259694072 | 25.258 | 8.608 | 2.80482 | 1.56740 | 2004.3 | 2 |
| 639 | 408321 | 260917119 | 25.278 | 8.6132 | 2.80550 | 1.56495 | 2007.5 | 5 |
| 640 | 409 | 262144000 | 25.2982 | 8.6177 | 2.80618 | 1.562 | 2010.6 | 321699 |
| 641 | 410881 | 263374721 | 25.3180 | 8.6222 | 280686 | 1.5600 |  | 322705 |
| 642 | 412164 | 264609288 | 25.3377 | 8.6267 | 2.80754 | 1.5576 | 2016.9 | 323713 |
| 643 | 413449 | 265847707 | 25.3574 | 8.6312 | 2.80821 | 1.55521 | 2020.0 | 324722 |
| 644 | 414736 | 267089984 | 25.3772 | 8.6357 | 2.808 | 1.552 | 2023.2 |  |
| 645 | 41602 |  | 25. |  |  | 1. |  | 45 |
| 646 | 417816 | 269586136 | 25.4165 | 8.64 | 2.8102 | 1.54 | 2029 | 327759 |
| 647 | 418609 | 270840023 | 25.4362 | 8.6490 | 2.81090 | 1.545 | 2032.6 | 75 |
| 648 | 419904 | 272097792 | 25.4558 | 8.653 | 2.81158 | 1.54321 | 2035.8 | 329792 |
| 649 | 421201 | 273359 |  | 8.657 | 2.81224 | 154083 | 2038.9 |  |
|  |  | 27462500 | 25.4951 | 8.6624 | 2.81291 | 1.53846 | 2042.0 | 331831 |
|  | 423801 | 275894451 | 25.5147 | 8.6668 | 2.81358 | 1.53610 | 2045 | 332853 |
|  | 425104 | 277167808 | 25.5313 | 8.6713 | 2.81425 | 1.53374 |  | 333876 |
| 653 | 426409 | 278445077 | 25.5539 | 8.6757 | 2.81491 | 1.53139 | 2051.5 | 334901 |
| 654 | 427716 | 27972626 | 25.5734 | 8.6801 | 2.81558 | 1.52905 |  |  |
| 655 | 42902 | 28101137 | 25.593 |  | 2.816 | 1.52672 | 205 |  |
| 656 | 430336 | 282300416 | 25.6125 | 8.689 | 2.8169 | 1.524 | 20 | 337985 |
| 757 | 431649 | 283593393 | 256320 | 8.693 | 2.8175 | 1.5220 | 206 | 339016 |
| 758 | 432964 | 284890312 | 25.6515 | . | 2.81823 | 1.51976 | 2067.2 | 340044 |
| 65 | 43 |  |  |  |  | 1.51745 |  |  |
|  |  | 28749600 | 25.6905 | 8.7066 | 2.81954 | 1.51515 | 2073.5 | 342119 |
|  | 436921 | 288804781 | 25.7099 | 8.7110 | 2.82020 | 1.51286 | 2076. | 343157 |
| 662 | 438244 | 290117528 | 257294 | 8.7154 | 2.82086 | 1.51057 | 2079.7 | 344196 |
| 663 | 439569 | 291434:247 | 25.7488 | 8.7198 | 2.82151 | 1.50830 | 2082.9 | 345237 |
| 664 | 440896 | 292754944 | 25.7682 | 8.7241 | 2.82217 |  | 2086.0 | T |
| 66 | 14222 | 294079 | 25.7 | 8.7 | 2.822 | 1.503 |  |  |
|  | 443 | 29540829 | 25.807 | 8.732 | 2.823 | 1.501 | 2092 | 348368 |
|  | 444889 | 29674096 | 25.8263 | 8.737 | 2.8.4 | 1.49925 | 2095 | 349415 |
| 668 | 446224 | 298077632 | 25.8457 | 8.7416 | 2.82478 | 1.49701 | 2098.6 | 350464 |
| 669 |  | 29941830 | 25.865 | 8.746 | 2.825 | 1.49477 | 2101.7 |  |
| 670 | 448900 | 300763000 | 25.8844 | 8.7503 | 2.82607 | 1.49254 | 2104.9 | 352565 |
| 671 | 450241 | 302111711 | 25.9037 | 8.7547 | 2.89672 | 1.49031 | 2108.0 | 353618 |
| 672 | 451584 | 303464448 | 25.9230 | 8.7590 | 2.82737 | 1.48810 | 2111.2 | 354673 |
| 673 | 452929 | 304821217 | 25.9422 | 8.7634 | 2.82802 | 1.48588 | 2114.3 | 355730 |
| 674 | 454276 | 30618202 | 25.961 | 8.7677 | 2.8286 | 1.4836 | 2117 | 356788 |

Squares, Cubes, Square Roots, Cube Roots, Logarithms, Etc.
(CONTINUED.)

| No. | Sq. | Cube. | Square Root. | Cube Root. | Log. | $\begin{gathered} 1000 \\ \times \\ \text { Recip } \end{gathered}$ | No. $=$ Dia. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Circ'm | Area. |
|  |  | 3075 | 25.9868 | 8.7721 | 2.82930 | 1.48148 |  | 77 |
| 676 | 456976 | 308915776 | 26.0000 | 8.7764 | 2.82995 | 1.47929 |  | 358908 |
| 677 | 458329 | 310288783 | 26.0192 | 8.7807 | 2.83059 | 1.47711 | 2126.9 | 359971 |
| 678 | 459684 | 311665752 | $26 . C 384$ | 8.7850 | 2.83123 | 1.47493 | 2130.0 | 361035 |
| 679 | 461041 | 313046839 | 26.0576 | 8.7893 | 2.83187 | 1.47875 | 2133.1 | 362101 |
| 680 | 462400 | 314432000 | 26.0768 | 8.7937 | 2.83251 | 1.47059 | 2136.3 | 363168 |
| 68 | 463761 | 315821241 | 26.0960 | 8.798 | 2.83315 | 1.46843 | 2139.4 | 364237 |
| 682 | 465124 | 317214568 | 26.1151 | 8.8023 | 2.83378 | 1.46628 | 2142.6 | 365308 |
| 683 | 466489 | 318611987 | 26.1343 | 8.8066 | 2.83442 | 1.46413 |  | 366380 |
| 68 | 467856 | 320013504 | 26.1534 | 8.8109 | 2.83506 | 1.46199 | 2148.9 |  |
|  | 469225 | 32141912 | 26.1725 | 8.8152 | 2.83569 | 1.459 | 2152.0 | 368528 |
| 68 | 470596 | 322828856 | 26.1916 | 8.8194 | 2.83632 | 1.45773 | 2155.1 | 369605 |
| 687 | 471969 | 324242703 | 26.2107 | 8.8237 | 2.83696 | 1.45560 | 2158.3 | 370684 |
| 688 | 473344 | 325660672 | 26.2298 | 8.8280 | 2.83759 | 1.45349 | 2161.4 | 371764 |
| 689 | 474721 | 327082769 | 26.2488 | 8.8323 | 2.83822 | 1.45138 | 2164.6 | 372845 |
| 690 | 476 | 328509000 | 26.2679 | 8.836 | 2.83885 | 1.449 | 2167.7 | 373928 |
| 69 | 477481 | 329939371 | 26.2869 | 8.8408 | 2.83948 | 1.44718 | 2170.8 | 375013 |
| 692 | 478864 | 331373888 | 26.3059 | 8.8451 | 284011 | 1.44509 | 2174.0 | 376099 |
| 693 | 480249 | 332812557 | 26.3249 | 8.8493 | 2.84073 | 1.44300 | 2177.1 | 377187 |
| 694 | 481636 | 334255384 | 26.3439 | 8.8536 | 2.84136 | 1.44092 |  |  |
| 695 | 483025 | 335702375 | 26.3629 | 8.8578 | 2.84198 | 1.43885 | 2183.4 | 379367 |
| 696 | 484416 | 337153536 | 26.3818 | 8.8621 | 2.84261 | 1.43678 | 2186.6 | 380459 |
| 697 | 485809 | 338608873 | 26.4008 | 8.8663 | 2.84323 | 1.43472 | 2189.7 | 381554 |
| 698 | 487204 | 340068392 | 26.4197 | 8.8706 | 2.84386 | 1.43267 | 2192.8 | 382649 |
| 699 |  | 341532099 | 26.4386 |  | 2.84448 | 1.43062 |  |  |
| 700 | 49000 | 34300000 | 26.4 | 8.8790 | 2.84510 | 1.42857 |  | 385845 |
| 701 | 491401 | 344472101 | 26.4764 | 8.8833 | 2.84572 | 1.42653 | 2202.3 | 385945 |
| 70:3 | 492804 | 345948408 | 26.4953 | 8.8875 | 2.84634 | 1.42450 | 2205.4 | 387047 |
| 703 | 494209 | 347428927 | 26.5141 | 88917 | 2.81696 | 1.42248 | 2208.5 | 388151 |
| 704 | 495616 | 348913664 | 26.5330 | 8.8959 | 2.84757 | 1.42046 | 2211.7 | 389256 |
| 705 | 497025 | 35040262 | 26.5518 | 8.9001 | 284819 | 1.41844 | 2214.8 | 390363 |
| 706 | 498436 | 351895816 | 26.5707 | 8.904 | 2.84880 | 1.416 | 2218 | 391471 |
| 707 | 499849 | 353393243 | 26.5895 | 89085 | 2.81942 | 1.4143 |  | 392580 |
| 708 | 501264 | 354894912 | 26.6083 | 8.9127 | 2.85003 | 1.41243 | $2 \% 24.3$ | 393692 |
| 709 | 502681 | 356400829 | 26.6271 | 8.9169 | 2.85065 | 1.41044 | 2227.4 | 394805 |
| 710 | 504100 | 357911000 | 266458 | 8.9211 | 2.85126 | 1.40845 | 2230.5 | 395919 |
| 711 | 505521 | 359425431 | 26.6646 | 8.9253 | 2.85187 | 1.40647 | 2233.7 | 397035 |
| 712 | 506944 | 360944128 | 26.6833 | 8.9295 | 2.85248 | 1.40449 | 2236.8 | 398153 |
| 713 | 508369 | 362467097 | 26.7021 | 8.9337 | 2.85309 | 1.40253 | 2240.0 | 399272 |
| 714 | 509796 | 363994344 | 26.7208 | 8.9378 | 2.85370 | 1.40056 | 2243.1 | 400393 |
| 715 | 511225 | 365525875 | 26.7395 | 8.9420 | 2.85431 | 1.39860 | 2246.2 | 401515 |
| 716 | 512656 | 367061696 | 26.7582 | 8.9462 | 2.85491 | 1.39665 | 2249.4 | 402639 |
| 717 | 514089 | 368601813 | 26.7769 | 8.9503 | 2.85552 | 1.39470 | 2252.5 | 403765 |
| 718 | 515524 | 370146232 | 26.7955 | 8.9545 | 2.85612 | 1.39276 | 2255.7 | 404892 |
| 719 | 516961 | 371694959 | 26.8142 | 8.9587 | 2.85673 | 1.39082 | 2258.8 | 406020 |

## Squares, Cubes, Square Roots, Cube Roots, Logarithms, Etc.

(CONTINUED.)

| No. | Sq | Cube. | Square Root. | Cube <br> Root. | Log. | $\begin{gathered} 1000 \\ \times \\ \text { Recip. } \end{gathered}$ | No. = Dia. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Circ'm | Ar |
| 72 |  |  |  | 8.96 | 2.855 | 1.3 |  |  |
| \% | 519811 | 374805361 | 26.8514 | 8.9670 | 2.85 |  |  |  |
| 722 | 521284 | 376367048 | 26.8701 | 8.9711 | 2.85854 | 1.38504 | 2268.2 | 409416 |
| 723 | $522<29$ | 377933067 | 26.8887 | 8.9752 | 2.85914 | 1.38313 | 2271.4 | 410550 |
| 724 | 524176 | 379503424 | 25.9072 | 8.9794 | 2.85974 | 1.38122 | 2274.5 | 7 |
| \% | 525 | 3810 | 26. | 8.98 | 2.86034 | 1.37931 | 2277 |  |
| 72 | 527076 | 382657 | 26.9144 | 8.98 | 2.86094 | 1.37 | 2380.8 | 413965 |
| 72 | 528529 | 384240583 | 28.9629 | 8.9918 | 2.86153 | 1.375 | 2283.9 | 6 |
| 728 | 5209884 | 385828352 | 26.9815 | 8.9959 | 2.86213 |  | 2387.1 |  |
| 29 |  | 38\% 420489 | 27.0000 | 9.0000 | $2.862 \% 3$ | 1. | 2290.2 | 3 |
| 730 | 532900 | 389017000 | 27.0185 | 9.0041 | 2.86332 | 1.36986 |  |  |
| 731 | 534361 | 390617891 | 27.0370 | 9.0082 | 2.86392 | 1.36799 | 22 | 6 |
| 732 | 535824 | 3922233168 | 27.0555 | 9.0123 | 2.86451 | 1.3661 | 2299.7 | 420835 |
| 733 | 537289 | 39383283 ' | 27.0740 | 9.0164 | 2.86510 | 1.36426 | 2302 | 421986 |
| 734 | $5: 38756$ | 395446904 | 27.0924 | 9.0205 | 2.865\%0 | 1.362 | 2305 |  |
| 735 | 540 | 397 | 2 | 9.0 | 2.866 | 1.36054 | 2309.1 | 424293 |
| 736 | 54169 | 398689 | 27.1293 | 9.028 | 2.8668 | 1.35870 | 2312.2 | 425448 |
| 737 | 543169 | 40031555 | 27.1477 | 9.0328 | 2.86747 | 1.35685 | 2315.4 | 604 |
| 738 | 544644 | 401947272 | 27.1662 | 9.0369 | 2.86806 | 1.35501 | 2318.5 |  |
| 739 | 546121 | 403583419 | 27.1846 | 9.0410 | 2.86864 | 1.35318 | 2321.6 |  |
| 740 | 547600 | 405224000 | 27.2029 | 9.0450 | 2.869 | 1.35135 | 2324.8 | 430084 |
| 11 | 549081 | 406869021 | 27.2213 | 9.0491 | 2.868 | 1.34953 | 2327.9 | 431247 |
| 742 | 550564 | 408518488 | 27.2397 | 9.0532 | 2.87040 | 1.34771 | 2331 | 432412 |
| 743 | 552049 | 410172404 | 27.2580 | 9.0572 | 2.87099 | 1.34590 |  | 433578 |
| 744 | 55353 | 411830784 | 27.2764 | 9.0 | 2. | 1.34409 |  |  |
| 745 | 555025 | 41349362 | 27.2 | 9.065 | 2.87216 | 1.34228 | 2340.5 | 435916 |
| \% | 556516 | 415160936 | 27.3130 | 9.0694 | 2.87274 | 1.34048 | 2343.6 | 487087 |
| $74 \%$ | 558009 | 416832723 | 27.3313 | 9.0735 | 2.87332 | 1.33869 | 2346.8 | 438259 |
| 748 | 559504 | 418508992 | 27.3496 | 9.0775 | 2.87390 | 1.33690 | 2349.9 | 439433 |
| 749 | 561001 | 420189749 | 27.3679 | 9.08 | 2.87448 | 133511 |  |  |
| 350 | 562500 | 42187500 | 27.3861 | 9.0856 | 2.8750 | 1.33333 | 2356.2 | 441786 |
| 751 | 564001 | 423564751 | 27.4044 | 9.0896 | 2.87564 | 1.33156 | 2353 | 442965 |
| 752 | 565504 | 425259008 | 21.4236 | 9.0937 | 2.87622 | 1.329 | 2362 | 44146 |
| 753 | 567009 | 42695717 | 27.4408 | 9.0977 | 2.87680 | 1.3283 | 2365 | 445028 |
| 754 | 56851 | 42 | 27 | 9.1 | 2.8 |  |  |  |
| 755 | 570 | 43036 | 27.47 | 9.1057 | 2.87795 | 1.32450 | 2371.9 | 447697 |
| 756 | 57153 | 4322081216 | 27.4955 | 9.1098 | 2.87852 | 1.32275 | 2375.0 | 448883 |
| 757 | 5730 | 433198093 | 27.5136 | 9.1138 | 2.87910 | 1.32100 | 2378.2 | 4500\% 2 |
| 758 | 574564 | 435519512 | 27.5318 | 9.1178 | 2.87967 | 1.31926 | 2381.3 | 451262 |
| 759 | 576081 | 437245479 | 27.5500 | 9.1218 | 2.8802 | 1.31752 | 2384 | 452453 |
| 760 | 577600 | 438976000 | 27.5681 | 9.1258 | 2.88081 | 1.31579 | 2387.6 | 453646 |
| 761 | 579121 | 440711081 | 27.5862 | 9.1298 | 2.88138 | 1.81406 | 2390.8 | 454841 |
| 762 | 580644 | 442450728 | 27.6043 | 9.1338 | 2.88196 | 1.3123 | 2393.9 | 45603\% |
| 3 | 582169 | 414194947 | 27.6225 | 9.1378 | 2.88252 | 1.3106 | 2397.0 | 457234 |
| 764 | 583696 | 44594374 | 27.64 | 9.14 | 2.883 | 1.308 | 2400 | 458434 |

Squares, Cubes, Square Roots, Cube Roots, Logarithms, Etc*
(CONTINUED.)

| No. | Sq. | Cube. | Square Root. | Cube <br> Root. | Log | $\begin{gathered} 1000 \\ \text { X } \\ \text { Recip. } \\ \hline \end{gathered}$ | No. $=$ Dia. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Circ'm | Area |
|  | 58 | 4476 |  |  | 2.88366 |  |  |  |
| 766 | 58675 | 449455096 | 27.6767 | 9.1498 | 2.88423 | 1.30548 |  |  |
| 767 | 588289 | 451217663 | 27.6948 | 9.1537 | 2.88480 | 1.30378 | 2409.6 |  |
| 768 | 589824 | 452984838 | 27.7128 | 9.1577 | 2.88536 | 1.30208 | 2412.7 |  |
| 769 | 591361 | 454756609 | 27.7308 | 9.1617 | 2.88593 | 1.30039 | 2415.9 |  |
| 770 | 592900 | 456533000 | 27.7 | 9.1657 | 2.88649 | 1.29870 | 2419.0 |  |
| 771 | 594441 | 458314011 | 27.7669 | 9.1696 | 2.88705 | 1.29702 | 2422.2 |  |
| 772 | 595984 | 460699648 | 27.7849 | 9.1736 | 2.88762 | 1.29534 | 2425.8 | 468085 |
| 773 | 597529 | 461889917 | 27.8029 | 9.1775 | 2.88818 | 1.29366 | 2428.5 | 469298 |
| 774 | 599076 | 463684824 | 27.8209 | 9.1815 | 2.88874 | 1.29199 | 2431.6 |  |
| 7 | 600625 | 465484375 | 27.838 | 9.1855 | 2.88930 | 1.29032 | 2434.7 | 471730 |
| 776 | 602176 | 467288576 | 27.8568 | 9.1894 | 2.88986 | 1.28866 | 2437.9 | 472948 |
| 777 | 603729 | 469097433 | 27.8747 | 9.1933 | 2.89042 | 1.28700 | 2441.0 | 474168 |
| 778 | 605284 | 470910952 | 27.8927 | 9.1973 | 2.89098 | 1.28535 | 2444.2 | 475389 |
| 779 | 606841 | 472729139 | 27.9106 | 9.2012 | 2.89154 | 1.28370 | 2447.3 | 476612 |
| 88 | 608 | 474 |  | 9. |  | 1.28205 |  | 477836 |
| 781 | 609961 | 47637954 | 27.946 | 9.2091 | 2.8926 | 1.28041 | 2453.6 | 479062 |
| 78 | 611524 | 47821176 | 27.9643 | 92130 | 2.893 | 1.27877 | 2456.7 | 480290 |
| 783 | 613089 | 48004868 | 27.9821 | 9.2170 | 2.8937 | 1.27714 | 2459.9 | 481519 |
| 784 | 614656 | 481890304 | 28 | 9.2209 |  | 1.27551 |  |  |
| 8 | 616235 | 483736625 | 28.0179 | 9.224 |  | 1.27389 | 2466.2 |  |
| 786 | 617796 | 485587656 | 28.0357 | 9.2487 | 2.89542 | 1.27226 | 2469.3 | 16 |
| 787 | 619369 | 487443403 | 28.0535 | 9.2326 | 2.89597 | 1.27065 | 2472.4 | 486451 |
| 788 | 620914 | 489303872 | 28.0713 | 9.2365 | 2.89653 | 1.26904 | 2475.6 | 487688 |
| 789 | 6.22521 | 491169069 | 28.0891 | 9.2404 | 2.89708 | 1.26743 | 2478.7 | 488927 |
| 60 | 62 | 49303900 | 28.1069 | 9.2 | 2.8 | 1.2 | 2481.9 | 490167 |
| 791 | 625681 | 494913671 | 28.124 | 9.2482 | 2.89818 | 1.26422 | 2485.0 | 491409 |
| 79 | 627264 | 49679308 | 28.1425 | 9.2521 | 2.89873 | 1.2626 | 2488 | 492652 |
| 79 | 628849 | 498677257 | 28.1603 | 9.2560 | 2.89927 | 1.26103 | 2491.3 | 493897 |
| 794 | 630436 | 500566184 | 28.1780 | 9.2599 | 2.89982 | 1.25945 |  |  |
| 79 | 632025 | 50245 | 28.1957 | 9.2638 | 2.90037 | 1.25786 | 2497.6 | 496391 |
| 796 | 633616 | 504358336 | 28.2135 | 9.2677 | 2.90091 | 1.25628 | 2500.7 | 497641 |
| \%97 | 635209 | 506261573 | 28.2312 | 9.2716 | 2.90146 | 1.25471 | 2503.8 | 498892 |
| 798 | 636801 | 508169592 | 28.2489 | 9.2754 | 2.90200 | 1.25313 | 2507.0 | 500145 |
| 799 |  | 510082399 | 28.2666 | 9.2793 | 2.90255 | 1.25156 | 25 | 501399 |
|  | 640000 | 512000000 | 28.2843 | 9.283 | 2.9030 | 1.2500 | 2513.3 | 502655 |
| 80 | 641601 | 513922401 | 28.3019 | 9.287 | 2.9036 | 1.248 | 2516 | 503912 |
| 802 | 643204 | 515849608 | 28.3196 | 9.2909 | 2.90417 | 1.2468 | 2519 | 505171 |
| 803 | 644809 | 517781627 | 28.3373 | 9.2948 | 2.90472 | 1.24533 | 2522.7 | 506432 |
| 804 | 646416 | 51971846 | 28.3549 | 9.2986 | 2.90526 | 1.24378 | 2525.8 | 7694 |
| 80 | 648025 | 521660125 | 28.3725 | 9.3025 | 2.90580 | 1.24224 | 2529.0 | 508958 |
| 80 | 649636 | 523606616 | 28.3901 | 9.3063 | 2.90634 | 1.24069 | 2532.1 | 510223 |
| 80 | 051249 | 525557943 | 28.4077 | 9.3102 | 2.90687 | 1.23916 | 2535.3 | 511490 |
| 80 | 652864 | 527514112 | 28.4253 | 9.3140 | 2.90741 | 1.23762 | 2538.4 | 512758 |
| 809 | 65 | 5294751 | 28.4 | 9.3179 | 2.90795 | 1.2360 | 2541. | 51 |

## Squares，Cabes，Squar Roots，Cube Roots，Lagurithen，Eit．



| a． | \＄0 | Cuibe | Spuaver Finit | Cuite空mat． | Life． |  | $\mathrm{Na}=\mathrm{Dr}$ m |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Cunctm | ${ }^{\text {a }}$ |
|  |  |  |  |  | P1 |  |  |  |
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|  | （1）350 | 34\％me | mis | 9． | ［ | $11.30{ }^{\text {a }}$ | 패제 $\pm$ | \％） |
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|  | 709\％ | Surmuper | 758 | 9，其 | \＃gintir | 12 |  | 5 |
|  |  | 54loli | 935014 | 1 3 |  | 1． | 25019 | 201 |
|  |  |  | 5 | T． |  |  | 2 |  |
|  | trix | 33 | 运碞 | 9．7m | ？${ }^{\text {a }}$ | 1. | ㅍำ29 | 淢 |
| 4 ys | $6{ }^{6}$ | 35xutrincts |  | 1．${ }^{\text {anc }}$ | $\pm .0$ |  | pepe 4 | 뇌ํ |
| 438 |  | Sixiultam | 25 men |  | $\pm 9 \mathrm{y}$ | 1.30 | \＃int 5 | करत4 |
| ＋4．4 | 478 | \＃5uctumy | 720．754 |  | 2． 3 ¢5 |  |  |  |
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| 420 | Weas |  | 23 74.0 | 9．tar | 2．Mirus | 1.3019 | 29xitil | 3 |
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|  |  | 5 | 7385 | T 4 UE |  | 1.3 | \＃has 3 | Sug |
| 23 | 639 | \％ | 밴N | 2．4部 |  | 1.30 Cl | wiontis | 3wars |
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| 6 | $6{ }^{6}$ | SEH2 | $3{ }^{3}$ | T 4 －431 | 2 |  |  | Sukhre |
| S 2 | TWM | कौ045 | 능 | 9．－484 | 2 2 | II． |  | 3nta |
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| S等 |  | Wपाए | ast | 9．45 | 2 2 Th |  |  | \％ |
|  |  |  | 25.4 | 9．498 | $\pm 3$ | － | 2mins 9 |  |
|  |  | 5 S 4 | 3 | 9.451 |  | L LRAM | Hita | 3andic |
|  |  | 354 | 푠 | T－449 | 2.30 ers | 1．15\％ | \＃tixts． 2 |  |
| － 4 | TII | 는 | 렝 |  |  | 11.1802 | mathe | 8 |
|  |  |  |  | 9. | 2 | 1.1 | ］atal |  |
|  | 7144035 | H02351135 | maman | 9．454 | \％ 9 | ， | 9\％ |  |
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| 546 |  | （andevinge | 229 1314 | 9．4183 | P 38 | 1． $11^{3}$ | mant | Hecrs |
| S |  | 51 |  | 9.4 | 2 |  | 2ammen |  |
|  |  | $45^{4}$ | 균） 13445 | 9.4 | 23．99942 | 1．109 | 4 | ¢ล์ |
|  |  | cunarsisi | 2n－174 | 9．060 | ＋${ }^{2}$ gramus | 1．103n | 3Ttu 5 | 30696 |
|  | Tissin4 | firsforne | 캔 11896 | 9． 1810 | T．Smbut | 1.17 mb | 3950 |  |
|  | TET619 | neal |  | 9．4538 | P． | 1．1m93is | 3imp ${ }^{\text {a }}$ |  |
| 534 | \％mo | 8 | ， | 9－ 125 | 2． 5 \＄04 | 1．1103 | 7020 |  |

Squares, Cubes, Square Roots, Cube Roots, Logarithms, Etc.
(CONTINUED.)

| No. | Sq. | Cube. | Square Root. | Cube Root. | Log. | $\begin{gathered} 1000 \\ \text { X } \\ \text { Recip. } \end{gathered}$ | No. = Dia |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Circ'm | Area. |
|  | 731025 | 625026375 | 29.2404 | 9.4912 | 2.98197 | 1.16959 |  |  |
| 856 | 732736 | 627222016 | 29.2575 | 9.4949 | 2.93247 | 1.16822 | 2689.2 |  |
| 857 | 734449 | 629422793 | 29.2746 | 9.4986 | 2.93298 | 1.16686 | 2692.3 | 576835 |
| 858 | 736164 | 631628712 | 29.2916 | 9.5023 | 2.93349 | 1.16550 | 2695.5 | 578182 |
| 859 | 737881 | 633839779 | 29.3087 | 9.5060 | 2.93399 | 1.16414 | 2698.6 | 579530 |
| 860 | 739600 | 636056000 | 29.325 | 9.5097 | 2.93450 | 1.16279 | 2701.8 | 580880 |
| 861 | 741321 | 638277381 | 29.3428 | 9.5134 | 2.93500 | 1.16144 | 2704.9 |  |
| 862 | 743044 | 640503928 | 29.3598 | 9.5171 | 2.93551 | 1.16009 | 2708.1 | 583585 |
| 864 | 744769 | ${ }^{642735647}$ | 29.3769 | 9.5207 | 2.93601 | 1.15875 | 2711.2 | 584940 |
| 864 | 746496 | 644972544 | 29.3939 | 9.5244 | 2.93651 | 1.15741 | 2714.3 | 586297 |
| 865 | 748225 | 647214625 | 29.4109 | 9.5281 | 2.93702 | 1.15607 | 2717.5 | 587655 |
| 866 | 749956 | 649461896 | 29.4279 | 9.5317 | 2.93752 | 1.15473 | 2720.6 | 589014 |
| 867 | 751689 | 651714363 | 29.4449 | 9.5354 | 2.93802 | 1.15340 | 2723.8 | 590375 |
| 868 | 753424 | 653972032 | 29.4618 | 9.5391 | 2.93852 | 1.15207 | 2726.9 | 591738 |
| 869 | 755161 | 656234909 | 29.4788 | 9.5427 | 2.98902 | 1.15075 | 2730.0 | 593102 |
| 870 | 756 | 658503000 | 29 | 9.5 | 2.9 | 11 | 2733.2 | 594468 |
| 871 | 758641 | $660{ }^{\prime \prime} 76311$ | 29.512i | 9.5501 | 2.9400 | 1.148 | 2736.3 | 595835 |
| 872 | 760384 | 663054848 | 29.5296 | 9.5537 | 2.94052 | 1.14679 | 2739.5 | 597204 |
| 873 | 762129 | 665338617 | 29.5466 | 9.5574 | 2.94101 | 1.14548 | 2742.6 | 598575 |
| 874 | 763876 | 667627624 | 29.5635 | 9.5610 | 2.94151 | 1.14416 | 2745.8 | 599947 |
| 875 | 765625 | 669921875 | 29.5804 | 95647 | 2.94201 | 1.14286 | 2748.9 | 601320 |
| 876 | 767376 | 672221376 | 29.5973 | 9.5683 | 2.94250 | 1.14155 | 2752.0 | 602696 |
| 877 | 769129 | 674526133 | 29.6142 | 9.5719 | 2.94300 | 1.14025 | 2755.2 | 604073 |
| 878 | 770884 | 676836152 | 29.6311 | 9.5756 | 2.94349 | 1.13895 | 2758.3 | 605451 |
| 879 | 772641 | 679151439 | 29.6479 | 9.5792 | 2.9 | 1.137 | 27 | 60 |
| 880 | 774400 | 681472000 |  | 9.5828 | 2.9444 | 1.13636 | 2764.6 | 608212 |
| 881 | 776161 | 683797841 | 29.6816 | 9.5865 | 2.9449 | 1.13507 | 2767.7 | 609595 |
| 882 | 777924 | 686128968 | 29.6985 | 9.5901 | 2.94547 | 1.13379 | 2770.9 | 610980 |
| 883 | 779689 | 688465387 | 29.7153 | 9.5937 | 2.94596 | 1.13250 | 2774.0 | 612366 |
| 884 | 781456 | 690807104 | 29.7321 | 9.5973 | 2.94645 | 1.13122 | 2777.2 | 613754 |
| 885 | 783225 | 693154125 | 29.7489 | 9.6010 | 2.94694 | 1.12994 | 2780.3 | 615143 |
| 886 | 784996 | 695506456 | 29.7658 | 9.6046 | 2.9474 | 1.128 | 2783. | 616534 |
|  | 786769 | 697864103 | 29.7825 | 9.6082 | 2.94792 | 1.12740 | 2786.6 | 617927 |
| 888 | 788544 | 700227072 | 297993 | 9.6118 | 294841 | 1.12613 | 2789.7 | 619321 |
| 889 | 790321 | 702595369 | 29.8161 | 9.6154 | 2.94890 | 1.12486 | 2792.9 | 620717 |
| 890 | 792100 | 704969000 | 29.8329 | 9.6190 | 2.94939 | 1.12360 | 2796.0 | 622114 |
| 891 | 793881 | 707347971 | 29.8496 | 9.6226 | 2.94988 | 1.12233 | 2799.2 | 623513 |
| 892 | 795664 | 709732288 | 29.8664 | 96262 | 2.95036 | 1.12108 | 2802.3 | 624913 |
| 893 | 797449 | 712121957 | 29.8831 | 9.6298 | 2.95085 | 1.11982 | 2805.4 | 626315 |
| 894 | 799236 | 714516984 | 29.8998 | 9.6334 | 2.95134 | 1.11857 | 2808.6 | 627 |
| 895 | 801025 | 716917375 | 29.9166 | 9.6370 | 2.95182 | 1.11732 | 2811.7 | 629124 |
| 896 | 802816 | 719323136 | 29.9333 | 9.6406 | 2.95231 | 1.11607 | 2814.9 | 630530 |
| 897 | 804609 | 721734273 | 29.9500 | 9.6442 | 2.95279 | 1.11483 | 2818.0 | 631938 |
| 898 | 806404 | 724150792 | 29.9666 | 9.6477 | 2.95328 | 1.11359 | 2821.2 | 633348 |
| 899 | 808201 | 726572699 | 29.9833 | 9.6513 | 2.95376 | 1.11235 | 2824.3 | 634760 |

# Squares, Cubes, Square Roots, Cube Roots, Logarithms, Etc. 

(CONTINUED.)

| No. | Sq. | Cube. | Square Root. | Cube <br> Root. | Log. | $\begin{gathered} 1000 \\ \times \\ \text { Recip. } \\ \hline \end{gathered}$ | No. $=$ Dia |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Circ'm | Area. |
|  | 810 | 72 |  |  | 2. |  |  | 636173 |
| 901 | 811801 | 731432701 | 30.0167 | 9.6585 | 2.95472 | 1.10988 | 2830 |  |
| 902 | 813604 | 733870808 | 30.0333 | 9.6620 | 2.95521 | 1.10865 | 2833.7 | 639003 |
| 903 | 815409 | 736314327 | 30.0500 | 9.6656 | 2.95569 | 1.10742 | 2836.9 | 640421 |
| 904 | 817216 | 738763264 | 30.0666 | 9.6692 | 2.95617 | 1.10619 | 2840.0 | 641840 |
|  | 8190 | 741 |  | 9. | 2.9 |  |  |  |
| 906 | 82083 | 7436774 | 30. | 9.6 | 2.95 | 1.10375 | 28 | 644683 |
| 907 | 82264 | 7461426 | 30.11 | 9.6 | 2.957 | 1.102 | 28 | 646107 |
| 908 | 8:446 | 748613312 | 30.13 | 9.6 | 2.9580 | 1.10131 | 2852 | 647533 |
| 909 | 826 | 751089429 | 30.149 | 9.68 | 2.958 | 1.10011 | 2855.7 | 648960 |
|  | 828100 |  |  | 9.690 | 2.95904 | 1.09890 |  |  |
| 11 | 829921 | 756058031 | 30.1828 | 9.6941 | 2.95952 | 1.09769 | 2862 |  |
| 912 | 831744 | 758550528 | 30.1993 | 9.6976 | 2.95999 | 1.09649 | 2865 | 53250 |
| 913 | 833569 | 761048497 | 30.2159 | 9.7012 | 2.96047 | 1.09529 | 2868 | 654684 |
| 914 | 835396 | 763551944 | 30.2324 | 9.7047 | 2.96095 | 1.09409 |  | 656118 |
|  |  | \%660 | 30.24 | 9.7 | 2.9 |  |  |  |
| 916 | 83905 | 7685752 | 30.265 | 9.7 | 2.9619 | 1.09170 | 287 |  |
| 917 | 84088 | 7710952 | 30.28 | 9.7 | 2.962 | 1. | 28 | 660433 |
| 918 | 84 | 7736206 |  | 9.7 | 2.9 |  | 28 | 661874 |
| 918 |  | 776 |  |  |  |  |  |  |
|  |  |  |  |  |  |  | 2890.3 | 664761 |
| 921 | 848241 | 781229961 | 30.348 | 9.7294 | 2.96426 | 1.0857 | 28 |  |
| 922 | 850084 | 783777448 | 30.3645 | 9.7329 | 2.96473 | 1.08460 | 2896 | 54 |
| 923 | 851929 | 786330467 | 30.3809 | 9.7364 | 2.96520 | 1.08342 | 2899.7 | 69103 |
| 924 | 853776 | 788889024 | 30.3974 | 9.7400 | 2.96567 | 1.08225 | 2902.8 |  |
|  | 8556 | 79145312 | 30.41 | 9.74 | 2.966 | 1.081 |  | 672006 |
|  | $85 \pi 47$ | 79402277 | 30.4302 | 9.747 | 2.966 | 1.0799 | 2909 | 673460 |
|  | 85932 | 79659798 | 30.4467 | 9.750 | 2.967 | 1.078 | 2912 | 674915 |
|  | 86118 | 79917875 | 30.4631 | 9.7540 | 2.96 |  | 29 | 676372 |
| 099 |  |  | 30.479 |  |  |  |  |  |
|  |  | 8033 | 30.49 | 9. | 2.98 | 1.0 |  |  |
| 931 | 86676 | 80695449 | 30.5123 | 9.764 | 2.96895 | 1.074 | 2924.8 | 0752 |
| 932 | 868624 | 80955756 | 30.5287 | 9.768 | 2.96942 | 1.072 | 2928.0 |  |
| 933 | 870489 | 812166237 | 30.5450 | 9.7715 | 2.96988 | 1.07181 | 2931.1 | 683680 |
| 934 |  | 814780 | 30.5614 | 9.775 | 2.9 | 1.070 | 2934.2 | 685147 |
| 35 | 8742 | 81740037 | 30.5 | 9.7785 | 2.970 | 1.069 | 2937. | 88615 |
| 936 | 876096 | 82002585 | 30.5941 | 9.7819 | 2.971 | 1.068 | 2940 | 688084 |
|  | 877969 | 822656953 | 30.610 | 9.78 | 2.97174 | 1.067 | 2943.7 | 689555 |
|  | 879844 | 825193672 | 30.626 | 9.7 | 2972 | 1.066 | 2946.8 | 691028 |
| 939 |  | 827936 | 30 | 9.7 | 2.9 |  |  |  |
| 11 | 883600 | 830584000 | 30.6594 | 9.7959 | 2.97313 | 1.06383 | 2953.1 | 693978 |
| 941 | 885481 | 833237621 | 30.6757 | 9.7993 | 2.97359 | 1.06270 | 2956.2 |  |
| 942 | 887364 | 835896888 | 30.6920 | 9.8028 | 2.97405 | 1.06157 | 2959.4 | 96934 |
| 943 | 889249 | 838561807 | 30.7083 | 9.8063 | 2.97451 | 1.06045 | 2962.5 | 698415 |
| 944 | 891136 | 84123238 | 30.724 | 9.809 | 2.97497 | 1.05932 | 2965. | 699897 |

Squares, Cubes, Square Roots, Cube Roots, Logarithms, Etc.
(CONTINUED.)

| No. | Sq. | Cube. | Square <br> Root. | Cube <br> Root. | Log. | $\begin{gathered} 1000 \\ X \\ \text { Recip } \end{gathered}$ | No. = Dia. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Circ'm | Area. |
| 9 | 893025 | 8439086 | 30.7409 | 9.8132 | 2.97543 | 1.05820 | 2968.8 | 701380 |
| 9 | 894916 | 846590536 | 30.7571 | 9.8167 | 2.97589 | 1.05708 | 2971.9 | 702865 |
| 9 | 896809 | 849278123 | 30.7734 | 9.8201 | 2.97635 | 1.05597 | 2975.1 | 704352 |
| 948 | 898704 | 851971392 | 30.7896 | 9.8236 | 2.97681 | 1.05485 | 2978.2 | 705840 |
| 949 | 900601 | 854670349 | 30.8058 | 9.8270 | 2.97727 | 1.05374 | 29814 | 707330 |
| 950 | 902500 | 857375000 | 30.8221 | 9.8305 | 2.97772 | 1.05263 | 2984.5 |  |
| 951 | 904401 | 860085351 | 30.8383 | 9.8339 | 2.97818 | 1.05152 | 2987.7 | 710315 |
| 952 | 906304 | 862801408 | 30.8545 | 9.8374 | 2.97864 | 1.05042 | 2990.8 | 711809 |
| 953 | 908209 | 865523177 | 30.8707 | 9.8408 | 2.97909 | 1.04932 | 2993.9 | 713306 |
| 954 | 910116 | 868250664 | 30.8869 | 9.8443 | 2.97955 | 1.04822 | 29971 | \%14803 |
|  | 912025 | 870983 | 30.9031 | 9.8 | 2.98000 | 1.0 | 3000.2 | 716303 |
| 95 | 913936 | 873722816 | 30.9192 | 9.8511 | 2.98046 | 1.0460 | 3003.4 | 717804 |
| 957 | 915849 | 876467493 | 30.9354 | 9.8546 | 2.98091 | 1.0449 | 3006.5 | 719306 |
| 958 | 917764 | 879217912 | 30.9516 | 9.8580 | 2.98137 | 1.04384 | 3009.6 | 720810 |
| 959 | 919681 | 8819\%4079 | 30.9677 | 9.8614 | 2.98182 | 1.04275 | 3012.8 | 722316 |
| 96 | 921600 | 884736000 | 30.9839 | 9.8648 | 2.98227 | 1.04167 | 3015.9 | 723823 |
| 961 | 923521 | 887503681 | 31.0000 | 9.8683 | 2.98272 | 1.04058 | 3019.1 | 725332 |
| 96 | 925444 | 890277128 | 31.0161 | 9.8717 | 2.98318 | 1.03950 | 3022.2 | 726842 |
| 96 | 927369 | 893056347 | 31.0322 | 9.8751 | 2.98363 | 1.03842 | 3025.4 | 728354 |
| 964 | 929296 | 8958 | 31.0483 | 9.8785 | 2.98408 | 1.03734 | 3028.5 |  |
| 96 | 981225 | 898632125 | 31.0644 | 9.8819 | 2.98 | 1.03627 | 3031.6 | 731382 |
| 966 | 933156 | 901428696 | 31.0805 | 9.8854 | 2.98498 | 1.03520 | 3034.8 | 732899 |
| 967 | 935089 | 904231063 | 31.0966 | 9.8888 | 2.98543 | 1.03413 | 3037.9 | 734417 |
| 968 | 937024 | 907039232 | 31.1127 | 9.8922 | 2.98588 | 1.03306 | 3041.1 | 735937 |
| 969 | 938961 | 909853209 | 31.1288 | 9.8956 | 2.98632 | 1.08199 | 3044.2 | 737458 |
| 970 | 940900 | 912673000 | 31.1448 | 9.8990 | 2.98677 | 1.03093 | 3047.3 | 738981 |
| 971 | 942841 | 915498611 | 31.1609 | 9.9024 | 2.98722 | 1.02987 | 3050.5 | 740506 |
| 972 | 944784 | 918330048 | 31.1769 | 9.9058 | 2.98767 | 1.02881 | 3053.6 | 742032 |
| 973 | 946729 | 921167317 | 31.1929 | 9.9092 | 2.98811 | 1.02775 | 3056.8 | 743559 |
| 974 | 948676 | 924010424 | 31.2090 | 9.9126 | 2.9885 |  |  | 745088 |
| 975 | 950625 | 926859375 | 31.2250 | 9.9160 | 298900 | 1.02564 | 3063.1 | 746619 |
| 976 | 952576 | 929714176 | 31.2410 | 9.9194 | 2.98945 | 1.02459 | 3066.2 | 748151 |
| 977 | 954529 | 932574833 | 31.2570 | 9.9227 | 2.98989 | 1.02354 | 3069.3 | 749685 |
| 978 | 956484 | 935441352 | 31.2730 | 9.9261 | 2.99034 | 1.02249 | 3072.5 | 751221 |
| 979 | 958 | 938313739 | 31.2890 | 9.9295 | 2.99078 | 1.02145 | 3075.6 | 752758 |
| 980 | 960400 | 941192000 | 31.3050 | 9.9329 | 2.99123 | 1.02041 | 3078.8 | 754296 |
| 981 | 962361 | 944076141 | 31.3209 | 9.9363 | 2.99167 | 1.01937 | 3081.9 | 755837 |
| 982 | 964324 | 946966168 | 31.3369 | 9.9396 | 2.99211 | 1.01833 | 3085.0 | 757378 |
| 983 | 966289 | 949862087 | 31.3528 | 9.9430 | 2.99255 | 1.01729 | 3088.2 | 758922 |
| 984 | 968256 | 952763904 | 31.3688 | 9.9464 | 2.99300 | 1.01626 | 3091.3 | 760466 |
| 98 | 970225 | 955671625 | 31.3847 | 9.9497 | 2.99344 | 1.01523 | 3094.5 | 762013 |
| 98 | 972196 | 958585256 | 31.4006 | 9.9531 | 2.99388 | 1.01420 | 3097.6 | 763561 |
| 987 | 974169 | 961504803 | 31.4166 | 9.9565 | 2.99432 | 1.01317 | 3100.8 | 765111 |
| 988 | 976144 | 964430272 | 31.4325 | 9.9598 | 2.99476 | 1.01215 | 3103.9 | 766662 |
| 989 | 978121 | 967361669 | 31.4484 | 9.9632 | 2.9952 | 1.0111 | 3107 | 768 |

Squares, Cubes, Square Roots, Cube Roots, Logarithms, Etc.
(CONTINUED.)

| No. | Sq. | Cuhe. | Square <br> Root. | Cube <br> Root. | Log | $\begin{gathered} 1000 \\ X \\ \text { Recip. } \end{gathered}$ | No $=$ Dia. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Circ'm | Area. |
| 990 | 980100 | 970299000 | 31.4643 | 9.9666 | 2.99564 | 1.01010 | 3110.2 | 769760 |
| 991 | 982081 | 973242271 | 31.4802 | 9.9699 | 2.99607 | 1.00908 | 3118.3 | 771325 |
| 2 | 984064 | 976191488 | 31.4960 | 9.9733 | 2.99651 | 1.00806 | 3116.5 | 772882 |
| 993 | 986049 | 979146657 | 31.5119 | 9.9766 | 2.99695 | 1.00705 | 3119.6 | 774441 |
| 994 | 988036 | 982107784 | 31.5278 | 9.9800 | 2.99739 | 1.00604 | 3122.7 | 776002 |
| 995 | 990025 | 985074875 | 31.5436 | 9.9833 | 2.99782 | 1.00503 | 3125.9 | 777564 |
| 996 | 992016 | 988047936 | 31.5595 | 9.9866 | 2.99826 | 1.00402 | 3129.0 | 779128 |
| 997 | 994009 | 991026973 | 31.5753 | 9.9900 | 2.99870 | 1.00301 | 3132.2 | 780693 |
| 88 | 996004 | 994011992 | 31.5911 | 9.9933 | 2.99913 | 1.00200 | 3135.3 | 782260 |
| 99 | 99800 | 9970029 | 31.607 | 9.996 | 2.9995 | 1.0010 | 3138. | 783828 |



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[^0]:    Allow variation in weight per foot of 5 per cent. above and 5 per cent. below. Cannot cut closer to length than
    riginch. Shipped threads and couplings unless otherwise ordered.

[^1]:    Allow variation of 5 per cent. above and 5 per cent. below standard in weight per foot.
    Cannot cut to length closer than $\frac{1}{15}$ inch. Shipped plain ends unless otherwise ordered.

[^2]:    Allow variation of 5 per cent. above and 5 per cent. below standard in weight per foot.

[^3]:    Allow variation of $5 \%$ above and $5 \%$ below standard in weight per foot
    Cannot cut to length closer than $\frac{1}{16}$ inch.

[^4]:    * When solving examples by the use of these formulas use the table of Fifth Powers and Fifth Roots. Solutions may also be easily effected by the use of logarithms.

[^5]:    쁜 6 is 12 inch pipe the last column ：Read 15.6 ；therefore in © 4 in column headed＂ 4 ＂and opposite to number required．

[^6]:    FORMULA FOR THICKNESS OF CAST IRON WATER PIPE．
    

[^7]:    *Copyright 1899, by the Ingersoll-Sergeant Drill Co., New York, and is reprinted, by permission, from their catalogue of air compressors.

