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Calculation of Wave Attenuation Due to Friction and Shoaling : An Evaluation

by William G. Grosskopf

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PREFACE

This report presents an evaluation of the Bretschneider and Reid (1954) technique for calculating wave attenuation due to friction and shoaling using data collected at the Coastal Engineering Research Center's (CERC) Field Research Facility (FRF), Duck, North Carolina. The work was carried out under CERC's coastal engineering research program.

The report was prepared by William G. Grosskopf, Hydraulic Engineer, under the general supervision of Dr. C.L. Vincent, Chief, Coastal Oceanography Branch, Research Division.

Comments on this publication are invited.

Approved for publication in accordance with Public Law 166, 79th Congress, approved 31 July 1945, as supplemented by Public Law 172, 88th Congress, approved 7 November 1963.

TED E. BISI

Colonel, Corps of Engineers Commander and Director

CONTENTS

| | CONVERSION FACTORS, U.S. CUSTOMARY TO METRIC (SI) | Page 5 |
|----|--|-----------|
| | SYMBOLS AND DEFINITIONS | 6 |
| | I INTRODUCTION | 7 |
| I | I CALCULATING CHANGES IN WAVE HEIGHT DUE TO BOTTOM FRICTION AND SHOALING | 7 |
| II | I COMPARISON WITH FIELD DATA | 10 |
| I | V EXAMPLE PROBLEM | 10 |
| , | V SUMMARY AND CONCLUSIONS | 14 |
| | LITERATURE CITED | 15 |
| | TABLES | |
| 1 | Comparison of predicted and observed wave heights | 11 |
| 2 | Average deviation of Bretschneider and Reid's theory from observed wave heights | 12 |
| 3 | Illustration of the inapplicability of Bretschneider and Reid's theory in areas of irregular bottom topography | 12 |
| | FIGURES | |
| 1 | Graph used in determining the integral of the bottom dissination | |

| 1 | function, ϕ_f , for waves passing over a constantly sloping bottom | 8 |
|---|---|----|
| 2 | Friction factor diagrams | 9 |
| 3 | Comparison of observed and predicted wave heights at the nearshore gage, Duck, North Carolina | 12 |

| U.S. | customary | units | of measurement | used in | this | report | can | be | converted | to |
|-------|------------|-------|----------------|---------|------|--------|-----|----|-----------|----|
| metri | c (SI) uni | ts as | follows: | | | | | | | |

| Multiply | by | To obtain |
|--------------------|-------------------------|---|
| inches | 25.4 | millimeters |
| | 2.54 | centimeters |
| square inches | 6.452 | square centimeters |
| cubic inches | 16.30 | cubic centimeters |
| feet | 30.48 | centimeters |
| | 0.3048 | meters |
| square feet | 0.0929 | square meters |
| cubic feet | 0.0283 | cubic meters |
| yards | 0.9144 | meters |
| square yards | 0.236 | square meters |
| cubic yards | 0.7646 | cubic meters |
| miles | 1.6093 | kilometers |
| square miles | 259.0 | hectares |
| knots | 1.852 | kilometers per hour |
| acres | 0.4047 | hectares |
| foot-pounds | 1.3558 | newton meters |
| millibars | 1.0197×10^{-3} | kilograms per square centimeter |
| ounces | 28.35 | grams |
| pounds | 453.6 | grams |
| | 0.4536 | kilograms |
| ton, long | 1.0160 | metric tons |
| ton, short | 0.9072 | metric tons |
| degrees (angle) | 0.01745 | radians |
| Fahrenheit degrees | 5/9 | Celsius degrees or Kelvins ¹ |

¹To obtain Celsius (C) temperature readings from Fahrenheit (F) readings, use formula: C = (5/9) (F -32).

To obtain Kelvin (K) readings, use formula: K = (5/9) (F - 32) + 273.15.

5

SYMBOLS AND DEFINITIONS

| А | horizontal displacement amplitude of water particles |
|-------------------|---|
| c_{f} | friction coefficient |
| d | water depth |
| d ₉₀ | sand grain size of 90th percentile of sediment samples |
| $^{\rm H}{\rm s}$ | significant wave height |
| H _{sn} | significant wave height at location n |
| Ks | shoaling coefficient |
| K _{sn} | shoaling coefficient at location n |
| k | wave height |
| k _s | roughness height |
| L | wavelength |
| L _n | wavelength at location n |
| L _o | deepwater wavelength |
| m | bottom slope |
| R _e | Reynolds number |
| Т | wave period |
| u _b | maximum horizontal water particle velocity |
| ν | kinematic viscosity |
| φ | integral of the dimensionless shoaling factor, φ_{f} |
| φf | dimensionless shoaling factor |

CALCULATION OF WAVE ATTENUATION DUE TO FRICTION AND SHOALING: AN EVALUATION

by William G. Grosskopf

I. INTRODUCTION

Many processes are responsible for variations in the energy of nearshore waves including breaking, friction, shoaling, refraction, percolation, and nonrigid bottom effects. However, in an area where nearshore bottom contours are straight and parallel, and bottom conditions indicate a nonpermeable and nonelastic sea floor, wave breaking, shoaling, refraction, and friction remain dominant. The area seaward of the pier end at U.S. Army Coastal Engineering Research Centers's (CERC) Field Research Facility (FRF), Duck, North Carolina, meets these conditions. Data from FRF can be used to evaluate different formulations of these processes.

This report evaluates the Bretschneider and Reid (1954) theory recommended in the Shore Protection Manual (SPM) (U.S. Army, Corps of Engineers, Coastal Engineering Research Center, 1977) for calculating the effect of bottom friction and shoaling on incoming waves, using data gathered from two offshore Waverider buoy gages (manufactured by Datawell, Haarlem, The Netherlands) located off the pier end at FRF. The two Waveriders operate in depths of approximately 18 and 10 meters, at 2,880 and 680 meters from shore, respectively. These instruments are located far enough offshore to avoid the possibility of wave breaking, other than whitecapping, as a dissipative mechanism between Waveriders for the data set used. Simultaneously observed wave spectra from these two gages during 1978 and 1979 were compared to calculated wave characteristics, using Bretschneider and Reid's (1954) prediction for waves traveling over an impermeable bottom of constant slope. It is found that Bretschneider and Reid's method provides a close correlation with observed data, especially in cases where the wave spectrum is narrow and single-peaked.

II. CALCULATING CHANGES IN WAVE HEIGHT DUE TO BOTTOM FRICTION AND SHOALING

Attenuation of wave height due to bottom friction and shoaling can be calculated using equation (1), for waves with significant wave height, $H_{\rm g}$, wave period, T, traveling over a bottom of slope, m, and depth, d, at the outer gage 1. Shoaling effects are calculated using linear theory. The relation is

$$H_{s2} = K_{s} H_{s1} \left(\frac{C_{f} H_{s1}}{mT^{2}} \phi + 1 \right)^{-1}$$
(1)

where

C_f = friction coefficient

K_s = shoaling coefficient

m = bottom slope

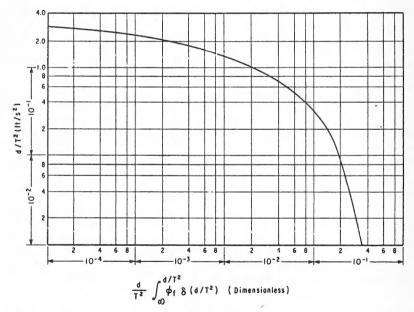
 H_{s2} = significant wave height at nearshore gage 2 (Waverider gage 610) H_{s1} = significant wave height at outer gage 1 (Waverider gage 620) The shoaling coefficient can be calculated from

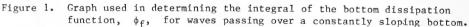
$$K_{s} = \left[\left(\tanh \frac{2\pi d}{L} \right) \left(1 + \frac{\frac{4\pi d}{L}}{\sinh \frac{4\pi d}{L}} \right) \right]^{-1/2}$$
(2)

and

$$\phi = \int_{\infty}^{d/T^2} \phi_f \,\delta\left(\frac{d}{T^2}\right) \tag{3}$$

The term ϕ can be evaluated from Figure 1.





The friction coefficient, $C_{\rm f}$, has been given considerable attention in laboratory and theoretical studies in recent years. Bretschneider and Reid (1954) recommend using a constant value of 0.01. More recent laboratory work has indicated a dependence of friction factor on the Reynolds number and dimensionless bottom roughness height. Jonsson (1966) and Kamphuis (1975) produced and refined a friction factor diagram, as shown in Figure 2, where the friction factor, $C_{\rm f}$, can be found if the Reynolds number at the sea

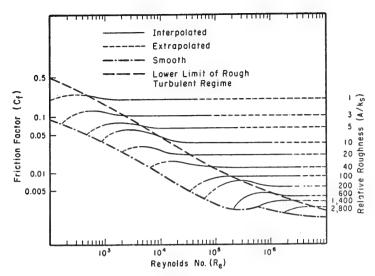


Figure 2. Friction factor diagrams (after Kamphuis, 1975).

floor, R_e, and the relative roughness height, A/k_s, are known. The Reynolds number is related to the bottom velocity under the wave by

$$R_{e} = \frac{u_{b} A}{v}$$
(4)

where

maximum horizontal water particle bottom velocity is uЪ

$$\frac{\pi H_{sl}}{T \sinh \frac{2\pi d}{L}}$$

L wavelength

kinematic viscosity of seawater equals 6.25×10^{-7} meters per ν second

А

$$\frac{H_{s1}}{2 \sinh \frac{2\pi d}{L}}$$

wave number $(2\pi/L)$ k -

This technique, which is explained and illustrated in CERC Field Guidance Letter 79-4 (Esteva, 1979), is used to determine C_{f} in the present study.

III. COMPARISON WITH FIELD DATA

Simultaneous observations of a variety of significant wave heights, periods, and energy spectrum shapes were chosen from available field data to illustrate possible weaknesses or strengths of Bretschneider and Reid's (1954) theory in all types of wave climate. The wave data selected were obtained from two Waverider buoy gages located in an area outside the breaker zone where sediment characteristics indicate that bottom friction is the predominant dissipation mechanism. Using conditions at the outer gage (Waverider gage 620) as input for Bretschneider and Reid's predictive equations, resulting calculated wave characteristics at the nearshore gage (Waverider gage 610) are compared to observed wave height values. Results are shown in Table 1 and Figure 3. Negative deviations from observed wave heights indicate the predicted value is lower than actually observed; i.e., the theory predicts more frictional energy loss than is observed. The range of friction coefficients used is 0.004 to 0.07. Most of the large underpredictions occur when no change or an actual increase in wave height is observed from offshore to inshore, possibly due to strong wind-wave generation. Overprediction indicates that other dissipation processes are occurring. Table 2 summarizes the results of this study. Figure 3 indicates that negative deviations are more pronounced for broad or multipeaked spectra, while narrow or single-peaked spectra correspond to slightly overpredicted wave heights. General trends show that the theory corresponds closely to observed wave conditions with maximum deviations of 60 percent but most conditions are within 15 percent. Examining only the data points for the narrow, single-peaked spectra, overprediction occurs for lower wave heights; underprediction occurs for larger waves which tend to be more nonlinear at the same shallow depth.

Table 3, which presents the results of Bretschneider and Reid's theory using Baylor staff gages (manufactured by Baylor Company, Houston, Texas) along the pier at FRF, provides an example of the theory's inapplicability where bottom contours are not straight and parallel. The irregular pierinduced topography causes the theory to overpredict wave height at Baylor gage 665 (located 350 meters from shore), inshore of Baylor gage 625 (located 630 meters from shore), indicating that other processes (e.g., refraction, bottom scattering) are affecting wave heights. As shown in the table, preliminary runs of a more advanced, nonlinear model indicate that the additional observed losses are likely due to refraction. This example shows that caution must be taken in applying the Bretschneider and Reid theory near manmade structures or in areas of irregular bathymetry.

GIVEN: A wave with the following wave height and period at gage 620 at an 18meter depth:

> $H_{s620} = 2.0$ meters T = 10 seconds

FIND: The wave height 2,200 meters closer to shore in a depth of 10 meters. Assume a d_{00} of the sediment to be 0.3 millimeter.

| Data file No. | Date | | Time | Observed significant wave conditions (vace 620) | erved significant wave conditions (vace 620) | Wave heigh | Wave height | Shoaling | Friction | Deviation from observed | Wave |
|---------------------|----------|------|------|---|--|-----------------|---------------|----------|----------------|----------------------------|-------------|
| | | | | Height (m) | Period (s) | Observed (m) | Predicted (m) | Ks Ks | C _f | (pet) | oheccro |
| - | 13 Sept. | 1978 | 1920 | 2.,7 | 08 | 2.5 | 2.4 | 0.93 | 0.004 | -4.0 | Narrow |
| 2 | 13 Sept. | 1978 | 2020 | 2.4 | 08 | 2.4 | 2.2 | 0.93 | 0.004 | -8.3 | Broad |
| e | 13 Sept. | 1978 | 2120 | 2.5 | 07 | 2.3 | 2.2 | 0.92 | 0.004 | -4.3 | Narrow |
| 4 | 10 Sept. | 1978 | 1020 | 1.2 | 60 | 1.3 | 1.1 | 96*0 | 0.004 | -15.4 | Broad |
| 20 | 13 Sept. | 1978 | 1120 | 1.5 | 04 | 1.3 | 0.6 | 0.98 | 0*070 | -53.8 | Multipeaked |
| 9 | 13 Sept. | 1978 | 1220 | 1.6 | 04 | 1.5 | 0.6 | 0.98 | 0.070 | -60.0 | Broad |
| 2 | 25 Sept. | 1978 | 1020 | 6*0 | 60 | 0.8 | 6*0 | 0.96 | 0.004 | +12.5 | Narrow |
| 80 | 03 Sept. | 1978 | 2020 | 6*0 | 60 | 0.8 | 6*0 | 0.96 | 0*004 | +12.5 | Narrow |
| 6 | 03 Sept. | 1978 | 2120 | 0.8 | 10 | 0.8 | 0.8 | 0.98 | 0.004 | 0*0 | Multipeaked |
| 10 | 03 Sept. | 1978 | 2220 | 0.8 | 08 | 0.7 | 0.7 | 0.93 | 0.004 | 0*0 | Multipeaked |
| 11 | 09 Sept. | 1978 | 1820 | 1.2 | 10 | .1.3 | 1.2 | 0.98 | 0.004 | -7.7 | Multipeaked |
| 12 | 10 Sept. | 1978 | 0920 | 1.4 | 10 | 1.2 | 1.4. | 0.98 | 0.004 | +16.7 | Narrow |
| 13 | 12 Sept. | 1978 | 0920 | 1.3 | 10 | 1.3 | 1.3 | 0.98 | 0.004 | 0*0 | Narrow |
| 14 | 12 Sept. | 1978 | 1920 | 1.2 | 14 | 1.0 | 1.3 | 1.10 | 0.004 | +13.0 | Narrow |
| 15 | 14 Sept. | 1978 | 0720 | 2.3 | 90 | 2.1 | 1.9 | 0.91 | 0.004 | -9.5 | Multipeaked |
| 16 | 01 Aug. | 1978 | 1920 | 0.6 | 07 | 0•6 | 0.5 | 0.92 | 0.008 | -16.7 | Broad |
| 17 | 01 Aug. | 1978 | 2020 | 0.6 | 08 | 0*6 | 0.6 | 0.93 | 0.006 | 0*0 | Broad |
| 18 | 13 Nov. | 1978 | 1520 | I.8 | 08 | 1.9 | 1.6 | 0.93 | 0.004 | -15.7 | Broad |
| 19 | 27 June | 1979 | 0820 | 1.6 | 90 | 1.8 | 1.4 | 0.91 | 0.005 | -22.2 | Broad |
| 20 | 12 Nov. | 1979 | 2120 | 1.9 | 05 | 1.7 | 1.5 | 0.93 | 0.010 | -]1.8 | Broad |
| 21 | 20 June | 1979 | 1420 | 1.7 | 08 | 1.8 | 1.5 | 0.93 | 0.004 | -16.7 | Multipeaked |
| 22 | 25 Sept. | 1979 | 0519 | 1.8 | 60 | 1.8 | 1.7 | 0.96 | 0,004 | -5.6 | Broad |
| 23 | 25 Sept. | 1979 | 0319 | 1.8 | 60 | 1.8 | 1.7 | 96*0 | 0.004 | -5.6 | Multipeaked |
| 24 | 18 Oct. | 1979 | 1320 | 2.1 | 10 | 2.1 | 2.0 | 0.98 | 0*004 | -4.7 | Narrow |
| 25 | 18 Oct. | 1979 | 1120 | 2.2 | 12 | 2.3 | 2.3 | 1.04 | 0.004 | 0*0 | Narrow |
| 26 | 18 Oct. | 1979 | 0720 | 2.2 | 12 | 2.4 | 2.3 | 1.04 | 0.004 | -4.2 | Narrow |
| 27 | 17 Oct. | 1979 | 1420 | 2.9 | 90 | 2.7 | 2.5 | 0.91 | 0.004 | -7.4 | Narrow |
| 28 | 25 Sept. | 1979 | 0419 | 2 . 0 | 08 | 1.8 | 1.8 | 0.93 | 0.004 | 0*0 | Narrow |
| 29 | 12 Nov. | 1979 | 0840 | 2.1 | 90 | 1.7 | 1.8 | 0.91 | 0.005 | +5.8 | Narrow |
| 30 | 12 Nov. | 1979 | 2140 | 1.9 | 08 | 1.6 | 1.7 | 0.93 | 0.004 | +6.3 | Narrow |
| 31 | 25 Sept. | 1979 | 0339 | 1.8 | 07 | 1.8 | 1.6 | 0.92 | 0.004 | -11.1 | Broad |

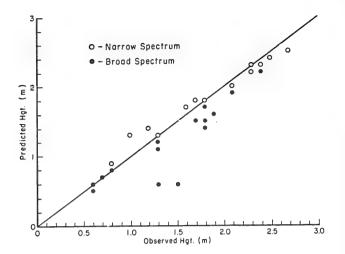


Figure 3. Comparison of observed and predicted wave heights at the nearshore gage (Waverider gage 610), Duck, North Carolina.

| Table | 2. | Average | deviation | of | Bretschneider | and | |
|-------|----|---------|-----------|----|---------------|-----|--|
| | | | | | | | |

Reid's theory from observed wave heights.1

| Wave spectra | Deviation (pct) | Regression line |
|------------------------------|--------------------|------------------|
| Narrow | +4.2 | y = 0.83x + 0.33 |
| Broad | -15.3 | y = 0.87x - 0.05 |
| All spectra (multipeaked) | -6.5 | y = 0.91x + 0.03 |

 $^{\rm l}{\rm Correlation}$ coefficient for all spectra equals 0.926.

Table 3. Illustration of the inapplicability of Bretschneider and Reid's theory in areas of irregular bottom topography.

| | | | | · · · · · · · · · · · · · · · · · · · | -gaiar boccom | |
|---------------|------|-------------------|---------|---------------------------------------|---------------|-----------------------------|
| | | Wa | ve heig | ght (m) | 1 | Estimated H _{s665} |
| Date | Time | Obse | rved | Predicted | Deviation | by including |
| | | H _{s625} | Hs665 | ^H s665 | from observed | refraction |
| | | | | | (pct) | (m) - |
| 13 Sept. 1978 | 0300 | 0.9 | 0.5 | 0.96 | 91.2 | 0.50 |
| 13 Sept. 1978 | 2100 | 2.5 | 1.6 | 2.33 | 45.8 | 1.50 |
| 13 Sept. 1978 | 2300 | 2.4 | 1.4 | 2.24 | 60.3 | 1.44 |
| 14 Sept. 1978 | 1100 | 2.1 | 1.3 | 1.97 | 51.2 | 1.26 |
| 15 Sept. 1978 | 1600 | 1.3 | 0.7 | 1.29 | 85.1 | 0.78 |
| 18 Oct. 1978 | 0700 | 2.2 | 1.6 | 25 | 55.1 | 1.32 |
| 18 Oct. 1978 | 1100 | 2.1 | 1.4 | 2.2 | 59.1 | 1.26 |

SOLUTION:

(1) Determine friction coefficient. From SPM Table C-1 (U.S. Army, Corps of Engineers, Coastal Engineering Research Center, 1977) for $(d/L_0)_{620} = 0.115,$

$$\left(\frac{d}{L}\right)_{620} = 0.154$$
 and $L_{620} = 116.9$ meters

Using linear theory,

$$A = \frac{H_{s620}}{2 \sinh kd} = \frac{2.0}{2(1.126)} = 0.89 \text{ meter}$$
$$u_{b} = \frac{\pi H_{s620}}{T \sinh kd} = \frac{\pi (2.0)}{10(1.126)} = 0.56 \text{ meter per second}$$

From equation (4),

$$R_{e} = \frac{u_{b} A}{v} = \frac{(0.56)(0.89)}{(6.25 \times 10^{-7})} \approx 8.3 \times 10^{5}$$
$$\frac{A}{m} = \frac{A}{m} = \frac{0.89}{m} = 1,483$$

$$\frac{1}{k_s} = \frac{1}{2d_{90}} = 0.0006$$

Figure 2 then yields the friction coefficient at gage 620 to be

$$C_{f} = 0.004$$

(2) Determine predicted wave height. The average depth in the traverse is 14 meters:

$$\frac{d}{T^2} = \frac{14}{(10)^2} = \frac{14}{100} = 0.14$$

From Figure 1,

$$\frac{d}{T^2} \phi = 0.180 \text{ or } \phi = 1.29$$

The bottom slope, m, is (8.0/2,200) = 0.0036, and the shoaling coefficient is determined at gage 610 where the wave height is unknown:

$$K_{s} = \left[\left(\tanh \frac{2\pi d}{L} \right) \left(1 + \frac{4\pi d}{L} \right) \right]^{-1/2}$$
$$K_{s610} = \left[\left(0.591 \right) \left(1 + \frac{1.360}{1.819} \right) \right]^{-1/2} = 0.984$$

The predicted wave height at gage 610 is then found by equation (1) to be

V. SUMMARY AND CONCLUSIONS

The combined effect of shoaling and bottom friction is underpredicted an average deviation of 6 percent by Bretschneider and Reid's (1954) theory, based on 31 observations. This study indicates that care must be taken in applying the predictive theory when wave spectra are broad or multipeaked, or when the bathymetry is irregular and the bottom contours are not straight and parallel.

For parallel bottom contour cases, the largest deviations from observed wave conditions arise when the wave spectrum which corresponds to the significant wave characteristics is broad or multipeaked. These large deviations, due to the presence of large amounts of energy relative to the total energy of the spectrum in many wave components, indicate that the significant wave height may not be a representative number to use for calculations in the equations when the spectrum is not narrow and single-peaked.

The calculations in Table 3 show that caution must be taken when using the equations in areas of irregular bathymetry or near coastal structures where the bathymetry may not be uniform. Other types of wave attenuation processes become important in these cases, with refraction being particularly dominant when the contours are not parallel and other bottom irregularities such as holes and shoals are present.

The choice of the friction coefficient will also play a role in compounding the predicted wave height deviation from actual observations. The coefficients used here are a result of controlled laboratory studies and, therefore, may not be a true representation of field coefficients. The presence of bottom ripples is not considered in this analysis, but has been shown to be a variable in determining the friction coefficient. Also, linear theory is used to calculate bottom velocity and horizontal water particle displacement; higher order calculations may lower present deviations.

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