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## Engineer's Office, Chesapeake and Ohio Railroad, \} Richmond, March 29, 1872.

Major Howard has given in this book a simple, yet perfectly accurate method of ascertaining the solid contents of any prismoid. The calculation from end areas is corrected by tables well arranged and few in number, and he has all the accuracy of the prismoidal formula with scarcely more trouble than in averaging end areas.
H. D. WHITCOMB, Chief Engineer Chesapeake and Ohio Railroad.
E. T. D. MYERS,

Chief Engineer Richmond, Fredericksburg, and Potomac Railroad.

## EARTHWORK MENSURATION,

## ON THE BASIS OF THE

## PRISMOIDAL FORMULA.

Containing a Simple and Labor-saving Method of OBTAINING PRISMOIDAL CONTEXTS DIRECTLY FROM END AREAS.

ILLUSTRATED BY EXAMPLES, AND ACCOMPANIED BY PLAIN RULES FOR PRACTICAL USE.

BY
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## 49995

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## PREFACE.

This work claims to present a new and systematized method of finding the prismoidal contents of Earthwork by means of Tables accompanied by Rules so plain and simple of application as to fit it for the common uses of Engineers.

When the ratios of the side slopes are constant between end sections of which the transverse surface lines are sensibly similar, all ordinary cases of thorough cut and fill, terminal pyramids, side-hill work, and borrow pits are covered by Formulæ (17), (18), and (19), and the prismoidal contents for all side slopes and bases are taken from Tables 4 and 5 by Rules (1), (2), and (3).

In the method used, the heights of equivalent level sections are not involved, nor is any calculation needed for 100 -feet lengths beyond ascertaining the half-sum and the difference of two quantities. For the most part Tables do the work of the calculator, and any one who can approximate cubic contents by the rough method of "Average Areas" is competent to obtain the prismoidal contents by the Rules given.

The tables of level cuttings are not needed when areas are given, and are included chiefly for use in preliminary estimates when the only data are the centre heights and the angles of the transverse surface slopes. With these, the heights of equivalent level sections are readily found by Mr. Trautwine's well-known and very ingenious diagrams, than which for the purpose intended probably no better means can be devised. When these heights have been ascertained, the use of the special Correction Tables in connection with those of level cuttings will reduce to a minimum the labor of computing the prismoidal contents. If further tables of level cuttings are considered necessary, the reader is referred to Mr. Trautwine's "Excavation and Embankment," or to the example given at the end of this work, by careful attention to which any required table may be written out with entire accuracy in a few hours. Special corrections for any side slopes may be obtained by Rule 12.

Not an inconsiderable advantage of the present method is that, by
giving accurate corrections for the familiar approximations in general use, the calculator has the element of error constantly before him, and must speedily learn by practice, if not by theory, the cases in which such corrections become important. But while enough is given, both by rule and example, in Part II. to guide the least theoretical in the use of the tables, in Part I. a strictly mathematical investigation of principles and derivation of formulæ is submitted to the careful reader.

The article on Correction of Contents for Curvature was suggested by that on the same subject in "Henck's Field-Book," but, by the formulæ and table of factors given, in ordinary cases the corrections are much more readily obtained in practice.

All of the tables in this work have been calculated by the writer, and, as the system used was that of continued additions with special tests at intervals, it is believed that they will be found absolutely correct within the purposed limits, whether the last figure of any amount given be intended to express the nearest whole number or the nearest decimal.

## NOTATION AND SIGNS USED.

$\qquad$

A and $\mathrm{A}^{\prime}=$ end areas of earthwork.
$\mathrm{M}=$ middle area.
$a$ and $a^{\prime}=$ areas of triangle between road-bed and intersection of side slopes produced.
$b$ and $b^{\prime}=$ road-bed widths.
$c$ and $c^{\prime}=$ centre heights of profile.
$\hbar$ and $h^{\prime}=$ heights of equivalent level sections.
$s$ and $s^{\prime}=$ ratios of opposite side slopes to 1.
$d$ and $d^{\prime}=$ side distances.
$h_{1}$ and $h_{2}=$ side heights.
$\mathrm{N}, \mathrm{N}^{\prime}, n$ and $n^{\prime}=$ correction numbers.
$\mathrm{C}=$ contents for 100 feet.
Q $=$ correction for curvature.
$\mathbb{X}=$ " greater or less than."
$\sim=$ "the difference between."
"Grade triangle " = triangle between the base and the intersection of the side slopes produced.

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## PART I.

AREAS.-GROUND SLOPING TRANSVERSELY. THOROUGH-CUT.
Fig. 1.


Let area $\mathrm{ABCFD}=\mathrm{A}$, area $\mathrm{DFG}=a$, centre height $\mathrm{BE}=c$, side heights AK and $\mathrm{CL}=h_{1}$ and $h_{2}$, side distances AM and NC $=d$ and $d^{\prime}$, base $\mathrm{DF}=b$, and ratios of side slopes to $1=s$ and $s^{\prime}$.

Case 1.—Side slopes the same. $s^{\prime}=s$. Produce the side slopes until they meet in G.

$$
\begin{aligned}
& \mathrm{EG} \times s=\frac{b}{2} \text {, hence } \mathrm{EG}=\frac{b}{2 s} \\
& \text { and area } a=\frac{b \times \frac{b}{2 s}}{2}=\frac{b^{2}}{4 s}
\end{aligned}
$$

$$
\text { But } \mathrm{BG}=c+\frac{b}{2 s} \text {, hence }
$$

$$
\begin{align*}
& \text { area } \mathrm{ACG}=\mathrm{A}+a=\left(c+\frac{b}{2 s}\right)\left(\frac{d+c}{2}\right) \\
& \text { and } \mathrm{A}=\frac{\left(\frac{\left.c+\frac{b}{2 s}\right)\left(d+l^{\prime}\right)}{2}-\frac{b^{2}}{4 s} \ldots \ldots\right.}{} \tag{1}
\end{align*}
$$

Example.-Given $s^{\prime}=s=\frac{3}{4} ; b=18 \mathrm{ft} . ; d=30.9 ; d^{\prime}=21.6 ;$ $c=22.0$.

$$
\begin{aligned}
& \left.\frac{b}{2 s}(\text { tab. } 1)=12, \text { and } a \text { (tab. } 2\right)=108 . \\
& A+a=\frac{(22.0+12.0)(30.9+21.6)}{2}=892.5 \\
& \text { and } A=892.5-108=784.5 .
\end{aligned}
$$

Case 2.—Opposite side slopes unequal. $s^{\prime} \ggg s$.
The areas of the triangles DAE, $\mathrm{EAB}, \mathrm{BCE}$, and ECF are respectively

$$
\begin{array}{r}
\frac{\frac{b}{2} \times h_{1}}{2}, \frac{c \times d,}{2}, \frac{c \times d^{\prime}}{2}, \text { and } \frac{\frac{b}{2} \times h_{2}}{2} \\
\text { and, } \mathrm{A}=\frac{\frac{b}{2}\left(h_{1}+h_{2}\right)+c\left(d+l^{\prime}\right)}{2} \ldots . \tag{2}
\end{array}
$$

Example.-s $=\frac{1}{4} ; s^{\prime}=1 ; b=16 ; c=12.6 ; d \& l^{\prime}=10.1 太$ $29.8 ; h_{1} \& h_{2}=8.4 \& 21.8$.

$$
A=\frac{8(8.4+21.8)+12.6(10.1+29.8)}{2}=370.6
$$

Case 3.-DE greater or less than EF.

$$
\text { Let } \mathrm{DE}=\frac{b}{2}, \text { and } \mathrm{EF}=\frac{b^{\prime}}{2}
$$

The triangles DAE, EAB and BCE have the same expressions for their areas as in casc 2 , and area $\operatorname{ECF}=\frac{\frac{b^{\prime}}{2} \times h_{2}}{2}$
hence, $\quad \mathrm{A}=\frac{\frac{b h_{1}}{2}+\frac{b^{\prime} h_{2}}{2}+c\left(d+l^{\prime}\right)}{2} \ldots \ldots \ldots$.
Example.-Double width track. $s=\frac{1}{2} ; s^{\prime}=\frac{3}{4} ; \frac{b}{2}=9 ; \frac{b^{\prime}}{2}=21$

$$
\begin{aligned}
& c=32.8 ; h_{1} \& h_{2}=24.4 \& 40.4 ; d \& d^{\prime}=21.2 \& 51.3 \\
& \mathrm{~A}=\frac{9.0 \times 24.4+21.0 \times 40.4+32.8(21.2+51.3)}{2}=1 \% 23
\end{aligned}
$$

Formula (1) applies only to case 1 ; formula (2) to cases 1 and 2 ; and formula (3) is gencral for all cases where the whole road-bed width is either in cutting or embankment, and the surface slopes are sensibly regular between the centre and side stakes.

## AREAS.-SIDE HILL CUTTING.

Let $q=$ the horizontal distance from centre line to grade point opposite, and $\mathrm{A}=$ the area of excavation.

Case 1.-Both centre and side height in excavation.
The areas of triangles DAE and EAB are as before, and that of the triangle running out to grade $=\frac{c q}{2}$
hence,

$$
\begin{equation*}
\mathrm{A}=\frac{\frac{b h_{1}}{2}+c(d+q)}{2} \tag{4}
\end{equation*}
$$

Example. $-s=1, b=20, c=4.3, h_{1}=10.6, d=20.6$, and $q=6.2$.

$$
\Lambda=\frac{10 \times 10.6+4.3(20.6+6.2)}{2}=110.6
$$

Case 2.-Centre height in emlankment.

$$
\begin{equation*}
\mathrm{A}=\frac{\left(\frac{b}{2}-q\right)}{2}^{2} \tag{5}
\end{equation*}
$$

Example. $-b=18, h=10, q=5 . \quad \mathrm{A}=\frac{(9-5) 10}{2}=20$
AREAS.-GROUND LEVEL TRANSVERSELY. Fig. 2.


Case 1.—Side slopes the same, or $s^{\prime}=s$. $\mathrm{AE}=\mathrm{FB}=k s$, and $\mathrm{EF}=\mathrm{CD}=b$
Area $\mathrm{ABCD}=\left(\frac{\mathrm{AB}+\mathrm{CD}}{2}\right) h=\left(\frac{h s+b+h s+b}{2}\right) h$

$$
\begin{equation*}
\text { or } \mathrm{A}=(b+h s) h \tag{6}
\end{equation*}
$$

Example.— $\quad s^{\prime}=s=\frac{1}{2} ; ~ b=16 ; h=20$

$$
A=\left(16+20 \times \frac{1}{2}\right) 20=26 \times 20=520
$$

When the field notes are given, this example can, of course, be worked by any one of formulæ (1), (2), or (3).

Case 2.—Opposite side slopes unequal, or $s^{\prime}><s$.

$$
\mathrm{AE}=h s ; \mathrm{FB}^{\prime}=h s^{\prime} ; \text { and } \mathrm{EF}=\mathrm{CD} .
$$

area $\mathrm{AB}^{1} \mathrm{CD}=\left(\frac{\mathrm{AB}^{\prime}+\mathrm{CD}}{2}\right) h=\left(\frac{h s+b+h s^{\prime}+b}{2}\right) h$
or $\mathrm{A}=\left(b+h\left(\frac{s+s^{\prime}}{2}\right)\right) h$

$$
\begin{aligned}
& \text { Example.-s }=\frac{1}{2} ; s^{\prime}=1 ; b=16 ; \pi=20 . \\
& \qquad \mathrm{A}=\left(16+20 \times \frac{3}{4}\right) 20=31 \times 20=620 .
\end{aligned}
$$

AREAS.-GROUND BROKEN TRANSVERSELY.
Fig. 3.


To calculate the area abclefy $b^{\prime} c^{\prime} d^{\prime} e^{\prime} f^{\prime} g$.
The elevations and horizontal distances apart of the points $a, b, c, c, e, f, g$, must be determined in the usial manner before the surface is disturbed, and of $b^{\prime}, c^{\prime}, l^{\prime}, e^{\prime}, f^{\prime}, g^{\prime}$, after the excavation is made.

Calculate the area $\mathrm{A} a b \operatorname{cld} \operatorname{cfg} \mathrm{~B}$ between the surface line and the assumed datum plane AB ; also

The area $\mathrm{A} a b^{\prime} c^{\prime} l^{\prime} e^{\prime} f^{\prime} g^{\prime} g \mathrm{~B}$ between the bottom of the pit as excavated and the same datum plane AB .

The difference between the results so obtained, gives the area required.

When the cross sections of the line have the surface broken transversely, if the slope stakes are supposed to be at $a$ and $g$ (fig. 3 ), and AB is the plane of the road-bed, calculate

1st : the area $\mathrm{A} a b c d e f g \mathrm{~B}$
$2 d$ : the triangles of excess $=\frac{h_{1}^{2} s+h_{2}^{2} s^{\prime}}{2}$
The difference between the above two results will give the area of earthwork required.

For side hill work the process is similar, except that only one triangle of excess $=\frac{\pi_{1}^{2} s}{2}$, is to be deducted.

This of course applies to embankment as well as excavation.
None of the preceding cases require that the cross section shall be drawn before calculating its area.
CONTENTS.-FRUSTUM FORMULA.


If ABCD and $\mathrm{A}^{\prime} \mathrm{B}^{\prime} \mathrm{C}^{\prime} \mathrm{D}^{\prime}$ be two consecutive cross sections with like surface lines and side slopes but unequal bottom widths, by producing the side slopes until they meet at E and $\mathrm{E}^{\prime}$, the whole figures ABE and $\mathrm{A}^{\prime} \mathrm{B}^{\prime} \mathrm{E}^{\prime}$ are similar as well as the triangles CDE and $\mathrm{C}^{\prime} \mathrm{D}^{\prime} \mathrm{E}^{\prime}$. But the solid $\mathrm{ABCDA} \mathrm{A}^{\prime} \mathrm{B}^{\prime} \mathrm{C}^{\prime} \mathrm{D}^{\prime}$ being the difference between the frustums $A B E A^{\prime} \mathrm{B}^{\prime} \mathrm{E}^{\prime}$ and $\mathrm{CDEC}^{\prime} \mathrm{D}^{\prime} \mathrm{E}^{\prime}$ its cubic contents are
$\left(\mathrm{ABE}+\mathrm{A}^{\prime} \mathrm{B}^{\prime} \mathrm{E}^{\prime}+\sqrt{\mathrm{ABE} \times \mathrm{A}^{\prime} \mathrm{B}^{\prime} \mathrm{E}^{\prime}}\right)_{\overline{3}}^{l}$

$$
-\left(\mathrm{CDE}+\mathrm{C}^{\prime} \mathrm{D}^{\prime} \mathrm{E}^{\prime}+\sqrt{\mathrm{CDE} \times \mathrm{C}^{\prime} \mathrm{D}^{\prime} \mathrm{E}^{\prime}}\right)_{\overline{3}}^{l}
$$

in which $l$ represents the distance between the cross sections.

If areas $\mathrm{ABCD}, \mathrm{A}^{\prime} \mathrm{B}^{\prime} \mathrm{C}^{\prime} \mathrm{D}^{\prime}, \mathrm{CDE}$ and $\mathrm{C}^{\prime} \mathrm{D}^{\prime} \mathrm{E}^{\prime}$ be represented by $\mathrm{A}, \mathrm{A}^{\prime}, a$ and $a^{\prime}$ respectively, then taking $l$ as 100 feet, and representing the contents in cubic yards by $\mathbf{C}$, we have:
$\mathrm{C}=\frac{\left.(\mathrm{A}+a)+\left(\mathrm{A}^{\prime}+a^{\prime}\right)+\sqrt{(\mathrm{A}+a)\left(\mathrm{A}^{\prime}+a^{\prime}\right.}\right)-\left(a+a^{\prime}+\sqrt{\left.a a^{\prime}\right)}\right.}{3} \times \frac{100}{2 \gamma}$.
If $\mathrm{CD}=\mathrm{C}^{\prime} \mathrm{D}^{\prime}$ then $a^{\prime}=a$, and the formula becomes:
$\mathrm{C}=\left(\frac{(\mathrm{A}+a)+\left(\mathrm{A}^{\prime}+a\right)+\sqrt{(\mathrm{A}+a)\left(\mathrm{A}^{\prime}+a\right)}}{3}-a\right) \frac{100}{27}$.
When $\mathrm{CD}=\mathrm{C}^{\prime} \mathrm{D}^{\prime}=0, a$ vanishes, and

$$
\begin{equation*}
\mathrm{C}=\left(\frac{\mathrm{A}+\mathrm{A}^{\prime}+\sqrt{\mathrm{AA}^{\prime}}}{3}\right) \frac{100}{27} . \tag{10}
\end{equation*}
$$

which is the formula for the frustum of a pyramid.
By formulæ (8), (9), and (10) the whole of the formulæ for cubic contents hereafter given may be conveniently tested.

As the solid resulting from connecting the homologous sides of two similar and parallel sections of unequal areas is the frustum of a pyramid, formula (10) is applicable to any plane solid with such end sections.

## CONTENTS.-PRISMOIDAL FORMULA.

Fig. 5.


Let ABCDF be a given cross section, with a base $\mathrm{FD}=b$, and $s$
and $s^{\prime}$ the ratios of its side slopes to 1 ; also let IKDF be an equiralent cross section with level surface, height MN $=h$, and with same base and side slopes. Produce the side slopes to their intersection at E , and from E let fall the perpendicular EL on IK, intersecting the base in G. Let area $\mathrm{ABCDF}=\mathrm{IKDF}=\mathrm{A}$, and $\mathrm{FDE}=a$.

In the triangle $\mathrm{FDE}, \mathrm{FG}=\mathrm{EG} \times s$, and $\mathrm{GD}=\mathrm{EG} \times s^{\prime}$, or $\mathrm{FD}=\mathrm{EG}\left(s+s^{\prime}\right)$, whence $\mathrm{EG}=\frac{\mathrm{FD}}{s+s^{\prime}}=\frac{b}{s+s^{\prime}}$ and area FDE $=\frac{\mathrm{FD} \times \mathrm{EG}}{2}=\frac{b}{2} \times \frac{b}{s+s^{\prime}}=\frac{b^{2}}{2\left(s+s^{\prime}\right)}=a$.

Similarly in triangle IKE, $\mathrm{EL}=h+\frac{b}{s+s^{\prime}}$
$\operatorname{IK}=\left(h+\frac{b}{s+s^{\prime}}\right)\left(s+s^{\prime}\right)$, and area IKE $=\left(h+\frac{b}{s+s^{\prime}}\right)^{2}\left(\frac{s+s^{\prime}}{2}\right)=\mathrm{A}+a$; consequently,
$\mathrm{A}=\overline{\mathrm{EL}}^{2}\left(\frac{s+s^{\prime}}{2}\right)-a=\left(h+\frac{b}{s+s^{\prime}}\right)^{2}\left(\frac{s+s^{\prime}}{2}\right)-\frac{b^{2}}{2\left(s+s^{\prime}\right)}$
from which,

$$
\mathrm{EL}=h+\frac{b}{s+s^{\prime}}=\sqrt{\left(\mathrm{A}+\frac{b^{2}}{2\left(s+s^{\prime}\right)}\right) \frac{2}{s+s^{\prime}}}=\sqrt{(\mathrm{A}+a) \frac{2}{s+s^{\prime}}}
$$

For convenience of calculation, let $\mathrm{GE}=\frac{b}{s+s^{\prime}}$ be represented by $g$, and EL by H; then as $\frac{b^{2}}{2\left(s+s^{\prime}\right)}=\left(\frac{b}{s+s^{\prime}}\right)^{2} \frac{s+s^{\prime}}{2}=y^{2}\left(\frac{s+s^{\prime}}{2}\right)$ we have, by substitution in (11),

$$
\mathrm{A}=\left(\mathrm{H}^{2}-g^{2}\right) \frac{s+s^{\prime}}{2}
$$

For a second section with corresponding parts $b^{\prime}, \mathrm{H}^{\prime}, s$ and $s^{\prime}$, and areas $\mathrm{A}^{\prime}$ and $a^{\prime}$

$$
\mathrm{A}^{\prime}=\left(\mathrm{H}^{\prime 2}-g^{\prime 2}\right) \frac{s+s^{\prime}}{2}
$$

and for the area $M$ of a cross section midway between $A$ and $A^{\prime}$,

$$
\begin{equation*}
\mathrm{M}=\left(\left(\frac{\mathrm{H}+\mathrm{H}^{\prime}}{2}\right)^{2}-\left(\frac{g+g^{\prime}}{2}\right)^{2}\right) \frac{s+s^{\prime}}{2} \ldots \ldots \ldots \ldots \tag{12}
\end{equation*}
$$

The prismoidal formula for the contents C between two end areas A and $\mathrm{A}^{\prime}$ at a distance apart $=l$, with an area M midway between them is :

$$
\begin{equation*}
\mathrm{C}=\left(\frac{\mathrm{A}+\mathrm{A}^{\prime}+4 \mathrm{M}}{6}\right) l \tag{13}
\end{equation*}
$$

$$
\text { But } \frac{A+A^{\prime}}{6}=\frac{A+A^{\prime}}{2}-\frac{A+A^{\prime}}{3}
$$

and by substitution in (13)

$$
\begin{equation*}
\mathrm{C}=\left(\frac{\mathrm{A}+\mathrm{A}^{\prime}}{2}-\frac{\mathrm{A}+\mathrm{A}^{\prime}-2 \mathrm{M}}{3}\right)^{l} \tag{14}
\end{equation*}
$$

also $\frac{4 M}{6}=M-\frac{2 M}{6}$; and substituting this in (13)

$$
\begin{equation*}
\mathrm{C}=\left(\mathrm{M}+\frac{\mathrm{A}+\mathrm{A}^{\prime}-2 \mathrm{M}}{6}\right)^{l} \tag{15}
\end{equation*}
$$

The two last expressions for the value of C show that the calculation of contents by averaging the end areas requires a minus correction ; and by the middle area (or, what is equivalent, taking the amount corresponding to the average of the end heights from a special table) a plus correction of exactly half as much. The actual minus correction will now be found. By substituting the values of $A, A^{\prime}$ and $M$ in the second term of (14) we have :
$\mathrm{C}=\left(\frac{\mathrm{A}+\mathrm{A}^{\prime}}{2}-\frac{\left.\left(\mathrm{H}^{2}-g^{2}\right)^{\frac{s}{2}+s^{\prime}} \frac{-}{2}+\left(\mathrm{H}^{\prime 2}-g^{\prime 2}\right)^{\frac{s}{2}+s^{\prime}} \frac{-2}{2}\left(\left(\frac{\mathrm{H}+\mathrm{H}^{\prime}}{2}\right)^{2}-\left(\frac{g+g^{\prime}}{2}\right)^{2}\right) \frac{s+s^{\prime}}{2}\right)}{3}\right)$
and reducing**

$$
\begin{equation*}
\mathrm{C}=\left(\frac{\mathrm{A}+\mathrm{A}^{\prime}}{2}-\left(\frac{\left(\mathrm{H}-\mathrm{H}^{\prime}\right)^{2}-\left(g-g^{\prime}\right)^{2}}{6}\right) \frac{s+s^{\prime}}{2}\right)^{l} . \tag{16}
\end{equation*}
$$

$\mathrm{But} \mathrm{H}=\sqrt{\left(\mathrm{A}+\frac{b^{2}}{2\left(s+s^{\prime}\right)}\right) \frac{2}{s+s^{\prime}}} ; \quad \mathrm{H}^{\prime}=\sqrt{\left(\mathrm{A}^{\prime}+\frac{b^{\prime 2}}{2\left(s+s^{\prime}\right)}\right) \frac{2}{s+s^{\prime}}} ;$ $g=\frac{b}{s+s^{\prime}}$; and $g^{\prime}=\frac{b^{\prime}}{s+s^{\prime}}$, and by substitution in (16)

$$
\mathrm{C}=\left\{\frac{\mathrm{A}+\mathrm{A}^{\prime}}{2}-\left(\frac{\left.\left(\sqrt{\left(\mathrm{A}+\frac{b^{2}}{2\left(s+s^{\prime}\right)}\right) \frac{2}{s+\delta^{\prime}}}-\sqrt{\left(\mathrm{A}^{\prime}+\frac{b^{\prime 2}}{2\left(s+s^{\prime}\right)}\right) \frac{2}{s+s^{\prime}}}\right)^{2}-\left(\frac{b-b^{\prime}}{s+s^{\prime}}\right)^{2}\right)}{6}\right)^{\frac{s+s^{\prime}}{2}}\right\}^{2}
$$

* Neglecting the common factors $\frac{s+s^{\prime}}{2}$ and $l$, and the denominator, the second term becomes,

$$
\begin{array}{r}
\left(\mathrm{H}^{2}-g^{2}\right)+\left(\mathrm{H}^{\prime 2}-g^{\prime 2}\right)-2\left(\frac{\left(\mathrm{H}+\mathrm{H}^{\prime}\right)^{2}}{4}-\frac{\left(g+g^{\prime}\right)^{2}}{4}\right)=\mathrm{H}^{2}-g^{2}+\mathrm{H}^{\prime 2}-g^{\prime 2} \\
-\frac{\mathrm{H}^{2}+2 \mathrm{HH}^{\prime}+\mathrm{H}^{\prime 2}}{2}+\frac{g^{2}+2 g g^{\prime}+g^{\prime 2}}{2} \\
=\frac{2 \mathrm{H}^{2}-2 g^{2}-2 \mathrm{H}^{\prime 2}-2 g^{\prime 2}-\mathrm{H}^{2}-2 \mathrm{HH}^{\prime}-\mathrm{H}^{\prime 2}+g^{2}+2 g g^{\prime}+g^{\prime 2}}{2} \\
=\frac{\mathrm{H}^{2}-2 \mathrm{HH}^{\prime}+\mathrm{H}^{\prime 2}-g^{2}+2 g g^{\prime}-g^{\prime 2}}{2}=\frac{\left.\mathrm{H}-\mathrm{H}^{\prime}\right)^{2}-\left(g-g^{\prime}\right)^{2}}{2}
\end{array}
$$

and restoring the factors $\frac{s+s^{\prime}}{2}$ and $l$, and the denominator, we obtain formula (16).

Reducing :*

$$
\mathrm{C}=\left(\frac{\mathrm{A}+\mathrm{A}}{2}-\left(\frac{\left(\sqrt{\mathrm{A}+\frac{b^{2}}{2\left(s+s^{\prime}\right)}}-\sqrt{\mathrm{A}^{\prime}+\frac{b^{\prime 2}}{2\left(s+s^{\prime}\right)}}\right)^{2}-\left(\frac{b-b^{\prime}}{s+s^{\prime}}\right)^{2} \frac{s+s^{\prime}}{2}}{6}\right) l\right.
$$

making $l=100$, dividing by 27 , observing that $(x-y)^{2}=(y-x)^{2}=$ $(y \sim x)^{2}$, and that $\frac{b^{2}}{2\left(s+s^{\prime}\right)}=a$, we obtain :

$$
\begin{equation*}
\mathrm{C}=\left(\frac{\mathrm{A}+\mathrm{A}^{\prime}}{2}-\frac{\left(\sqrt{\mathrm{A}+a} \sim \sqrt{\mathrm{~A}^{\prime}+a^{\prime}}\right)^{2}}{6}+\frac{\left(b \sim b^{\prime}\right)^{2}}{2\left(s+s^{\prime}\right)}-\frac{100}{6} .\right. \tag{17}
\end{equation*}
$$

This is the general formula when the opposite side slopes and end road-bed widths are both different.

When the road-bed widths are the same, or $b \sim b^{\prime}=0$, the last term vanishes, and the formula becomes :

$$
\begin{equation*}
\mathrm{C}=\left(\frac{\mathrm{A}+\mathrm{A}^{\prime}}{2}-\frac{\left(\sqrt{\mathrm{A}+a} \sim \sqrt{\mathrm{~A}^{\prime}+a}\right)^{2}}{6}\right) \frac{100}{27} . \tag{18}
\end{equation*}
$$

This is the general formula for all slopes and bases where the base is constant between the two end sections.

When $b=\dot{b}^{\prime}=o, a=0$, and

$$
\begin{equation*}
C=\left(\frac{A+A^{\prime}}{2}-\frac{\left(\sqrt{A} \sim \sqrt{A^{\prime}}\right)^{2}}{6}\right) \frac{100}{27} \tag{19}
\end{equation*}
$$

This is the general formula for the frustum of a pyramid, $\dagger$ such as may be the solid between two sections of side hill excaration.

The correction in terms of equivalent level heights $\hbar_{\text {and }} \hbar^{\prime}$ may be found directly from (16) as follows:

When $b^{\prime}=b$, the expression $\left(g-g^{\prime}\right)^{2}$ vanishes and (16) becomes:

* In squaring the binomial of radicals the factor $\sqrt{\frac{\bar{z}}{s+y^{\prime}}}$ becomes $\left(\sqrt{\frac{\bar{z}}{s+s^{\prime}}}\right)^{2}$ in the first term, $\sqrt{\frac{2}{s+\delta^{\prime}}} \sqrt{\frac{2}{s+\delta^{\prime}}}$ in the second, and $\left(\sqrt{\frac{\frac{2}{s+s^{\prime}}}{}}\right)^{2}$ in the third, or in each $\frac{2}{s+s^{\prime}}$, thus cancelling the factor $\frac{8+8^{\prime}}{2}$, except in the last term of the numerator.
$\dagger$ Formula (10) before given for the frustum of a pyramid may be transformed into formula (19); for $\frac{A+A+\sqrt{\mathrm{AA}^{\prime}}}{3}=\frac{2 A+2 A^{\prime}+2 \sqrt{\mathrm{AA}^{\prime}}}{6}=$ $\frac{3 A+3 A^{\prime}-A-A^{\prime}+2 \sqrt{A A^{\prime}}}{6}=\frac{3\left(A+A^{\prime}\right)}{6}-\frac{A-2 \sqrt{A A^{\prime}}+A^{\prime}}{6}=\frac{A+A^{\prime}}{2}-$ $\frac{\left(\sqrt{A} \sim \sqrt{A^{\prime}}\right)^{2}}{6}$. When $A^{\prime}=0$ in formula (19) it becomes $C=\left(\frac{A}{2}-\frac{(\sqrt{A})^{2}}{6}\right) \frac{100}{2 \overline{7}}$ $=\left(\frac{A}{2}-\frac{A}{6}\right) \frac{100}{27}=\frac{A}{3} \times \frac{100}{27}$, which is the formula for the solidity of a pyramid, as it should le.

$$
\mathrm{C}=\left(\frac{\mathrm{A}+\mathrm{A}^{\prime}}{2}-\frac{\left(\mathrm{H}-\mathrm{H}^{\prime}\right)^{2}}{6}\left(\frac{s+s^{\prime}}{2}\right)\right) l
$$

but $\left(\mathrm{H}-\mathrm{H}^{\prime}\right)^{2}=\left(\left(h+\frac{b}{s+s^{\prime}}\right)-\left(h^{\prime}+\frac{b}{s+s^{\prime}}\right)\right)^{2}=\left(h-h^{\prime}\right)^{2}=\left(h \sim h^{\prime}\right)^{2}$
and substituting, making $l=100$, and dividing by 27 ,

$$
\begin{equation*}
\mathrm{C}=\left(\frac{A+\mathrm{A}}{2}-\frac{\left(h \sim h^{\prime}\right)^{2}}{6}\left(\frac{s+s^{\prime}}{2}\right)\right) \frac{100}{2 \gamma} \ldots \ldots \ldots \ldots \ldots \ldots \tag{20}
\end{equation*}
$$

As the plus correction for calculation by middle area was found to be one half of the minus correction for averaging end areas, by making the requisite changes in (20) :

$$
\mathrm{C}=\left(\mathrm{M}+\frac{\left(h \sim h^{\prime}\right)^{2}}{12}\left(\frac{s+s^{\prime}}{2}\right)\right) \frac{100}{27}
$$

but when $b^{\prime}=b$, from formula (12), we obtain*

$$
\mathrm{M}=b\left(\frac{h+h^{\prime}}{2}\right)+\left(\frac{h+h^{\prime}}{2}\right)^{2} \frac{s+s^{\prime}}{2}
$$

and by substitution :

$$
\begin{equation*}
\mathrm{C}=\left\{b\left(\frac{h+h^{\prime}}{2}\right)+\left(\left(\frac{h+h^{\prime}}{2}\right)^{2}+\left(\frac{h \sim h^{\prime}}{12}\right)^{2}\right) \frac{s+s^{\prime}}{2}\right\} \frac{100}{27} \ldots \tag{21}
\end{equation*}
$$

This formula is for use when the equivalent level heights have been obtained.

## APPLICATION OF THE PRISMOIDAL FORMULA.

The prismoidal formula in its ordinary form is applicable to a variety of solids, regular and irregular, but requires that the actual middle section shall be previously determined and its area known.

In a modified form it can be applied practically by means of tables; such applications, however, always involving a value of the

* By substituting the values of $\mathrm{H}, \mathrm{H}^{\prime}, g$ and $g^{\prime}$ in formula (12) it becomes :

$$
\left.\mathrm{M}=\left(\frac{\left(h+\frac{b}{s+s^{\prime}}\right)+\left(h^{\prime}+\frac{b^{\prime}}{s+s^{\prime}}\right.}{}\right)\right)^{2}-\left(\frac{\frac{b}{s+s}+\frac{b^{\prime}}{s+s^{\prime}}}{2}\right)^{2}
$$

making $b^{\prime}=b$, and squaring :

$$
\begin{aligned}
& \mathrm{M}=\frac{\left(h+\frac{b}{s+s^{\prime}}\right)^{2}+2\left(h+\frac{b}{s+s^{\prime}}\right)\left(\pi^{\prime}+\frac{b}{s+s^{\prime}}\right)+\left(h^{\prime}+\frac{b}{s+s^{\prime}}\right)^{2}-4\left(\frac{b}{s+s^{\prime}}\right)^{2}}{4} \\
& =\frac{h^{2}+\frac{2 b h}{8+s^{\prime}}+\left(\frac{b}{s+s^{\prime}}\right)^{2}+2 h h^{\prime}+\frac{2 b h^{\prime}}{8+s^{\prime}}+\frac{2 b h}{s+s^{\prime}}+2\left(\frac{b}{s+s^{\prime}}\right)^{2}+h^{2}+\frac{2 b h^{\prime}}{8+s^{\prime}}+\left(\frac{b}{8+s^{\prime}}\right)^{2}-4\left(\frac{b}{s+s^{\prime}}\right)^{2}}{4}\left(\frac{s+s^{\prime}}{2}\right) \\
& =\frac{2 b h\left(\frac{2}{s+s^{\prime}}\right)+2 b h^{\prime}\left(\frac{2}{s+s^{\prime}}\right)+h^{2}+2 h h^{\prime}+h^{\prime 2}}{4}\left(\frac{s+s^{\prime}}{2}\right)=b\left(\frac{h+h^{\prime}}{2}\right)+\left(\frac{h+h^{\prime}}{2}\right)^{2} \frac{s+s^{\prime}}{2} .
\end{aligned}
$$

This also results directly from formula (7) by taking the area of a second section for a height of $h^{\prime}$, and averaging like parts for $M$.
middle area which can be deduced directly from the end areas without necessitating a previous knowledge of the parts of either the middle or the end sections.

But in all of its modifications, as well as in its ordinary form, the prismoidal formula invariably involves the area of the actual middle section of the solid to which it is applied, and, as in "Roots and Squares" and "Equivalent level heights," both methods involve a value of the area of this middle section (carried to intersection of side slopes when in thorough-cut) which can be proved identical with that of the frustum of a pyramid, the theoretical application of these methods is limited to solids with end sections sensibly similar, or which can be rendered so by being carried to the intersection of the side slopes.

As the above has been ignored by other writers on this subject, its mathematical proof will be given.

The contents of a frustum may be expressed either by the prismoidal or the frustum formula, therefore in the case of a frustum :

$$
\frac{\mathrm{A}+\mathrm{A}^{\prime}+4 \mathrm{M}}{6} \times l=\frac{\mathrm{A}+\mathrm{A}+\sqrt{\mathrm{AA}^{\prime}}}{3} \times l
$$

whence $\mathrm{A}+\mathrm{A}^{\prime}+4 \mathrm{M}=2 \mathrm{~A}+2 \mathrm{~A}^{\prime}+2 \sqrt{\mathrm{AA}^{\prime}}$, and $\mathrm{M}=\frac{\mathrm{A}+\mathrm{A}^{\prime}+2 \sqrt{\mathrm{AA}^{\prime}}}{4}$ $=\left(\frac{\sqrt{\mathrm{A}^{\prime}}+\sqrt{\mathrm{A}^{\prime}}}{2}\right)^{2}$

The formula of Roots and Squares where A and $\mathrm{A}^{\prime}$ represent the end sections* is (Formula 19) :

$$
C=\left(\frac{A+A^{\prime}}{2}-\frac{\left(\sqrt{\mathrm{A}}-\sqrt{\mathrm{A}^{\prime}}\right)^{2}}{6}\right) \frac{100}{27}
$$

and the prismoidal formula for the same solid is:

$$
\mathrm{C}=\left(\frac{\mathrm{A}+\mathrm{A}^{\prime}+4 \mathrm{M}}{6}\right)^{\frac{100}{27}}
$$

hence $\frac{A+A^{\prime}+4 M}{6}=\frac{A+A^{\prime}}{2}-\frac{\left(\sqrt{A}-\sqrt{A^{\prime}}\right)^{2}}{6}$
clearing fractions, $\mathrm{A}+\mathrm{A}^{\prime}+4 \mathrm{M}=3 \mathrm{~A}+3 \mathrm{~A}^{\prime}-\left(\sqrt{\mathrm{A}}-\sqrt{\mathrm{A}^{\prime}}\right)^{2}$
and $\mathrm{M}=\frac{2 \mathrm{~A}+2 \mathrm{~A}^{\prime}-\mathrm{A}+2 \sqrt{\mathrm{AA}^{\prime}}-\mathrm{A}^{\prime}}{4}=\left(\frac{\sqrt{\mathrm{A}}+\sqrt{\mathrm{A}^{\prime}}}{2}\right)^{2}$
In two end sections with surface level transversely and side slopes constant, if H and $\mathrm{H}^{\prime}$ reprèsent the heights from intersection of side slopes to surface and $s$ the ratio of the side slopes to 1 , the areas of

[^0]the end sections to intersection are $\mathrm{H}^{2} s=\mathrm{A}$, and $\mathrm{H}^{\prime 2} s=\mathrm{A}^{\prime}$, and for the area of the middle section, by averaging like parts :
\[

$$
\begin{aligned}
& \mathrm{M}=\left(\frac{\mathrm{H}+\mathrm{H}^{\prime}}{2}\right)^{2} s=\left(\frac{\mathrm{H} \sqrt{s}+\mathrm{H}^{\prime} \sqrt{s}}{2}\right)^{2}=\left(\frac{\sqrt{\mathrm{H}^{2} s}+\sqrt{\mathrm{H}^{\prime 2} s}}{2}\right)^{2} \\
&=\left(\frac{\sqrt{\mathrm{A}}+\sqrt{\mathrm{A}^{\prime}}}{2}\right)^{2}
\end{aligned}
$$
\]

which is the same value of M as that before obtained. Substituting this in the prismoidal formula :

$$
\begin{aligned}
& C=\frac{A+A^{\prime}+4\left(\frac{\left.\sqrt{\mathrm{~A}}+\sqrt{\mathrm{A}^{\prime}}\right)^{2}}{2} \times \frac{100}{27},\right. \text { and reducing, }}{6}+\frac{A+A^{\prime}+A+2 \sqrt{\mathrm{AA}^{\prime}}+\mathrm{A}^{\prime}}{6} \times \frac{100}{27}=\frac{A+A^{\prime}+\sqrt{\mathrm{AA}^{\prime}}}{3} \times \frac{100}{27}
\end{aligned}
$$

which is the formula for the frustum of a pyramid, and shows that this value of M introduced into the prismoidal formula limits its application to such solids only as are frustums of pyramids. This will be illustrated further from Example 5, page 36, in which when carried to the intersection of the side slopes produced, the end sections are similar.

Thus carried to intersection, the end areas and the actual middle area are respectively 349,2951 , and 1333 , as given page 36 .

By Roots and Squares

$$
\mathrm{M}=\left(\frac{\sqrt{349}+\sqrt{2951}}{2}\right)^{2}=1332
$$

By equivalent level heights

$$
\begin{aligned}
& \mathrm{H}=\sqrt{\frac{\mathrm{A}}{s}}=\sqrt{349 \times \frac{2}{3}}=15.25 \\
& \mathrm{H}^{\prime}=\sqrt{\frac{\mathrm{A}^{\prime}}{s}}=\sqrt{2951 \times \frac{2}{3}}=44.35 \\
& \mathrm{M}=\left(\frac{\mathrm{H}+\mathrm{H}^{\prime}}{2}\right)^{2} s=\left(\frac{15.25+44.35}{2}\right)^{2} \times \frac{3}{2}=1332
\end{aligned}
$$

By substituting this value of $M$ in the prismoidal formula :

$$
\mathrm{C}=\frac{349+2951+4 \times 1332}{6} \times \frac{100}{27}=1438 \text { tab. } 4=5326 \text { cyds. }
$$

For calculation by equivalent level heights as table 15 has a base of 14 feet, and the above heights are taken to intersection of side slopes, $\left(\frac{\mathrm{H}+\mathrm{H}^{\prime}}{2}\right) \times 14 \times \frac{109}{27}$ must be deducted from contents taken from tables.

By Rule 4,

$$
\begin{aligned}
\frac{15.25+44.35}{2} & =29.8 \text { table } 15 \ldots 6,475 \\
15.25 \sim 44.35 & =29.1 \text { table } 17 . \frac{+392}{6,8 \% 1}
\end{aligned}
$$

Deduct $29.8 \times 14 \times \frac{100}{27}=417.2$ table $4 \ldots-1,545$

$$
\overline{5,326} \text { cyds. }
$$

By mean proportional or frustum formula :
$\mathrm{C}=\frac{349+2951+\sqrt{349 \times 2951}}{3} \times \frac{100}{27}=1438.3$ table $4 \ldots 5,327 \mathrm{cyds}$.
By deducting the grade prism $32.7 \times \frac{100}{27}=121$ cyds., practically the same result as that given on page 36 is obtained.
^nother case in which the area of the actual middle section can be deduced from the end areas directly, is when each of the latter can be expressed by two surface dimensions, one of which is the same for both end sections, as in solids whose end sections are parallelograms or triangles with the same base and different heights, or vice versa. Thus if $b \hbar=\mathrm{A}$ and $b h^{\prime}=\mathrm{A}^{\prime}$ represent the end areas of a solid of which the end sections are triangles with the same base and different heights, as may be the case in side hill cutting where the transverse surface slope increases regularly between the end sections, by averaging like parts the middle area is

$$
\mathrm{M}=b\left(\frac{h+h^{\prime}}{2}\right)=\frac{b h+b h^{\prime}}{2}=\frac{\mathrm{A}+\mathrm{A}^{\prime}}{2}
$$

And as the prismoidal formula is applicable here, by substituting this value of M :

$$
\mathrm{C}=\frac{\mathrm{A}+\mathrm{A}^{\prime}+\left(\frac{\mathrm{A}+\mathrm{A}^{\prime}}{2}\right)^{4}}{6} \times \frac{100}{2 \gamma}=\frac{\mathrm{A}+\mathrm{A}^{\prime}}{2} \times \frac{100}{27}
$$

which is the average area formula, in this case giving the prismoidal contents. As an example, suppose the triangular end sections of the solid to have a base of 20 feet and heights of 10 and 40 feet respectively. Then $\mathrm{A}=10 \times 10=100 ; \mathrm{A}^{\prime}=10 \times 40=400$; and $\mathrm{M}=10 \times \frac{10+40}{2}=250=\frac{\mathrm{A}+\mathrm{A}^{\prime}}{2}$.
By the prismoidal formula :

$$
\mathrm{C}=\frac{100+400+4 \times 250}{6} \times \frac{100}{27}=250 \text { table } 4 \ldots 926 \mathrm{cyds}
$$

Calculated by Roots and Squares $\mathrm{M}=\left(\frac{\sqrt{100}+\sqrt{400}}{2}\right)^{2}=225$,
and this substituted in the prismoidal formula gives

$$
\mathrm{C}=\frac{100+400+4 \times 225}{6} \times \frac{100}{27}=233.3 \text { table } 4=864 \mathrm{cyds} .
$$

Here the average area formula gives the prismoidal contents, and the prismoidal formula applied by its modification of Roots and Squares gives a very rough approximation. The same inaccuracy is of course involved in the method by equivalent level heights, whatever may be the shape of the equivalent and similar end sections of which the level heights are obtained. For instance, if the side hill work is excavated at rock slope, the level heights, if carried to vertex, may be taken for sections with any other side slopes, as 1 to 1 , or $1 \frac{1}{2}$ to 1 .

At 1 to 1 carried to vertex $\mathrm{H}=\sqrt{\frac{100}{1}}=10 ; \mathrm{H}^{\prime}=\sqrt{\frac{400}{1}}=$ 20 , and to calculate by table 12 , with side slopes $1 \times 1$ and base 18 feet :

$$
\begin{aligned}
\frac{10+20}{2} & =15 \text { table } 12 \ldots \ldots \ldots \ldots . .1833 \\
10 \sim 20 & =10 \text { table } 14 \ldots \ldots \ldots \ldots \ldots+31 \\
\text { Deduct } 15 \times 18 \times \frac{100}{27} & =2 \% 0 \text { table } 4 \ldots \ldots \ldots \ldots-1000
\end{aligned}
$$ 864 cyds.

at $1 \frac{1}{2}$ to 1 carried to vertex $\mathrm{H}=\sqrt{100 \times \frac{2}{3}}=8.16 ; \mathrm{H}^{\prime}=\sqrt{400 \times \frac{2}{3}}$ $=16.33$, and to calculate by table 15, with side slopes $1 \frac{1}{2}$ to 1 , and base 14 feet.

$$
\begin{aligned}
& \frac{8.16+16.33}{2}=12.245 \text { table } 15 \ldots \ldots . .1468 \\
& 8.16 \sim 16.33=8.1 \% \text { table } 17 \ldots \ldots .+31
\end{aligned}
$$

Deduct $12.245 \times 14 \times \frac{100}{27}=1 \% 1.4$ table $4 \ldots \ldots .-635$
864 cyds.
The two last examples show the same error of 62 cyds. obtained by Equivalent level heights, as before by Roots and Squares.

By mean proportionals or frustum formula :

$$
\frac{100+400+\sqrt{100 \times 400}}{3} \times \frac{100}{27}=233.3 \text { table } 4 \ldots . .864 \mathrm{cyds} .
$$

By Rule 2,

$$
\begin{aligned}
\frac{100+400}{2} & =250 \text { table } 4 \ldots \ldots \ldots \ldots . .926 \\
10 \sim 20 & =18 \text { table } 5 \ldots \ldots \ldots \ldots \ldots 62
\end{aligned}
$$

864 cyds.
If the above sections were similar, as for instance with dimensions $10 \times 10$ and $20 \times 20$, the first method by average areas would give too much by 62 cyds, whilst by the others the true prismoidal contents would be obtained.

If both the heights and bases are different and the sections are not similar, the middle area will be less than $\frac{A+A^{\prime}}{2}$ and greater than $\left(\frac{\sqrt{A}+\sqrt{A^{\prime}}}{2}\right)^{2}$, and cannot be obtained directly from the end areas. In such cases, the exact contents can be determined by the prismoidal formula only by first obtaining the dimensions of the actual middle section and calculating its area.

Practically in railroad earthwork it is only when the transverse surface lines of the end sections are very dissimilar and the areas differ greatly in size that the resulting errors become important, and as at such points the cross sections are usually taken nearer together, it is very rarely the case that the methods of Roots and Squares and Equivalent level heights fail of practical correctness. In cases of doubt, however, especially when the surface is warped between the end sections, it is safer and better to obtain the area of the actual middle section before calculating the contents.

## CORRECTION OF CONTENTS FOR CURVATURE.

The following article was suggested by that given in Henck's "Field Book," page 110.

In excaration on curves, although the cross sections are actually staked out in the direction of the radii at the extremities of the chords, the calculation of contents is made as if these cross sections were perpendicular to the chords. In some cases, especially where the transyerse surface slope is considerable, this is the occasion of a sensible error requiring a corresponding correction, the amount of which is determined as follows:

Fig. 6.


Suppose A, B, and C to be three consecutive 100 feet stations on a curve of radius OB ; and BF and BH the side distances at station B.

The calculation of contents between A and B , and B and C made as if the cross sections at these points were on the lines $\mathrm{K}_{1} \mathrm{~L}_{1}$. and $K L$, and $K^{\prime} L^{\prime}$ and $K_{2} L_{2}$, or perpendicular to the chords $A B$ and $B C$, requires at each station a correction similar to that at $B$, which will now be considered. It is evident that the correction is the difference between the masses $\mathrm{KBK}^{\prime}$ and $\mathrm{L}^{\prime} \mathrm{BL}$, on opposite sides of the centre line, and between the two vertical planes KL and $K^{\prime} L^{\prime}$; these masses having for their cross sections respectively the half-breadths BF and BH . The angle $\mathrm{KBK}^{\prime}$ being very small, the arcs $\mathrm{KFK}^{\prime}$ and $\mathrm{L}^{\prime} \mathrm{HL}$ will be considered as straight lines; and, as the angle $\mathrm{KBF}=\mathrm{L}^{\prime} \mathrm{BH}=\frac{1}{2} \mathrm{KBK}^{\prime}=\mathrm{TBA}=\mathrm{D}$, the deflection angle of the curve, the distance $\mathrm{KF}=\mathrm{BF} \times \sin \mathrm{D}$; or, generally for small angles, any horizontal line as $\mathrm{KK}^{\prime}$ or $\mathrm{L}^{\prime} \mathrm{L}$ measured perpendicularly to the radius OB , and terminated by the planes KL and $\mathrm{K}^{\prime} \mathrm{L}^{\prime}$, is practically equal to BF or BH (the corresponding horizontal distance from the centre line) multiplied by $2 \sin \mathrm{D}$. Consequently, the masses $\mathrm{KBK}^{\prime}$ and $\mathrm{L}^{\prime} \mathrm{BL}$ being considered as truncated prisms with the areas of the half-breadths BF and BH as bases, their heights at any given points are equal to the horizontal distances of these points from the centre line, multiplied into twice the sine of the deflection angle.


Let FBHT represent the cross section at B (Fig. 6).
To simplify calculations, the equal prisms MP' and PTN are added.

The area $\mathrm{FBT}=(\mathrm{BP}+\mathrm{PT}) \frac{\mathrm{FB}^{\prime}}{2}=\left(c+\frac{b}{2 s}\right) \frac{d}{2}$, and the heights of the prism corresponding are $=d \times 2 \sin \mathrm{D}$ at F , and $=0$ at B and T. Its contents therefore $=\left(c+\frac{b}{2 s}\right) \frac{d}{2} \times\left(\frac{d \times 2 \sin \mathrm{D}}{3}\right)$. Similarly the contents of prism IIBT $=\left(c+\frac{b}{2 s}\right) \frac{d^{\prime}}{2} \times\left(\frac{d^{\prime} \times 2 \sin \mathrm{D}}{3}\right)$ and the correction required, which is the difference of their volumes,

$$
\begin{aligned}
& =\left(c+\frac{b}{2 s}\right) \frac{d^{2}}{2} \times \frac{2 \sin \mathrm{D}}{3} \sim\left(c+\frac{b}{2 s}\right) \frac{d^{\prime 2}}{2} \times \frac{2 \sin \mathrm{D}}{3} \\
& =\left(c+\frac{b}{2 s}\right)\left(\frac{d^{2} \sim d^{\prime 2}}{2}\right)\left(\frac{2 \sin \mathrm{D}}{3}\right)
\end{aligned}
$$

and if Q represents the required correction in cubic yards,

$$
\begin{equation*}
\mathrm{Q}=\left(c+\frac{b}{2 s}\right)\binom{d+d^{\prime}}{2^{-}}\left(d \sim d^{\prime}\right)\left(\frac{2 \sin \mathrm{D}}{3 \times 27}\right) . \tag{22}
\end{equation*}
$$

But, from formula (1), $\left(c+\frac{b}{2 s}\right)\left(\frac{d+l^{\prime}}{2}\right)=\mathrm{A}+a$, the area carried to intersection of side slopes; also $\sin \mathrm{D}=\frac{50}{\mathrm{R}}$, and as $\mathrm{R}=\frac{5730}{\mathrm{C}^{\circ}}$, in
which $\mathrm{C}^{\circ}$ represents the degree of curve, $2 \sin \mathrm{D}=50 \times 2 \times \frac{\mathrm{C}^{\circ}}{5730}$ $=\frac{\mathrm{C}^{\circ}}{57.3}$

Therefore,

$$
\begin{equation*}
\mathrm{Q}=(\mathrm{A}+a) \mathrm{C}^{\circ} \times \frac{\left(d \sim d^{\prime}\right)}{5 \% .3 \times 3 \times 27} \cdots \tag{23}
\end{equation*}
$$

In side hill work, as shown by Mr. Henck, the general formula for the correction in cubic feet is $\mathrm{Q}=\frac{w h}{2}(a+b-w) \frac{100}{3 \mathrm{~K}}$, in which $w$ represents the width of excavation at the road-bed. But as $\frac{w h}{2}$ $=\mathrm{A}$, the area of earthwork, in this case the correction in cubic yards is

$$
\mathrm{Q}=\mathrm{A} \times \mathrm{C}^{\circ} \times \frac{(d+b-w)}{57.3 \times 3 \times 2 \gamma} \cdots \ldots \ldots \ldots \ldots \ldots \ldots(24)
$$

Values of the last factor in formulæ (23) and (24) are given in Table 18.

In excavation the correction for curvature as obtained by formulæ (23) and (24) is to be added when the curve is convex, and subtracted when it is concave toward the higher ground, and in embankment these conditions are reversed. It is supposed to be applied at the middle one of three cross sections at intervals of 100 feet, and all on the same curve.

If the distance to either of the cross sections next the one under consideration differs from 100 feet, the correction found as above is to be multiplied by the half sum of the two distances and divided by 100.

At points of curre or tangent one of these distances of course becomes nothing.

Whether the side slopes, or the widths from the centre line to the edge of the road-bed, are different or not, if the transverse surface lines are broken, the cross sections should be drawn to scale, the two half-breadths divided into triangles, and the horizontal distances from the centre line to the corners of each subdividing triangle measured on the drawing. The sum of the three distances for each triangle multiplied by its area and by $\frac{2 \sin D}{3}$ will give the contents in cabic feet of the prism corresponding. It is not material how the sides of the subdividing triangles are drawn, provided that the whole of each triangle is on the same side of the centre line. The difference of the masses whose cross sections are the half-
breadths FB and BH (Fig. 6), and which lie on opposite sides of the centre line between the vertical planes $K L$ and $K^{\prime} \mathrm{L}^{\prime}$, the base plane and the planes of the side slopes, is in all cases the correction required.

With double-width track or opposite side slopes different, if the surface is regular from the centre to the slope stakes, from formula (3), the areas of the triangles of one half-breadth are $\frac{b}{4} \times h_{1}$ and $\frac{c d}{2}$, and of the other $\frac{b}{4} \times h_{\mathrm{a}}$ and $\frac{c d^{\prime}}{2}$

The heights of the prisms corresponding to these areas are $\left(a+\frac{b}{2}+0\right) \frac{2}{3} \sin \mathrm{D} ;(a+0+0) \frac{2}{3} \sin \mathrm{D} ;\left(d^{\prime}+\frac{b^{\prime}}{2}+0\right) \frac{2}{3} \sin \mathrm{D} ;$ and $\left(a^{\prime}+0+0\right) \frac{2}{3} \sin \mathrm{D}$, and their contents
$\left(\frac{b}{4} \times h_{1}\right)\left(d+\frac{b}{2}\right)^{\frac{2}{3}} \sin \mathrm{D} ;\left(\frac{c d^{2}}{2}\right) \frac{2}{3} \sin \mathrm{D} ;\left(\frac{b^{\prime}}{\frac{1}{4}} \times h_{2}\right)\left(d^{\prime}+\frac{b^{\prime}}{2}\right) \frac{2}{3} \sin \mathrm{D}$; and $\left(\frac{c d^{\prime 2}}{2}\right) \frac{2}{3} \sin \mathrm{D}$; but as $\frac{2}{3} \frac{\sin \mathrm{D}}{27}=\mathrm{C}^{\circ} \times 0.000215$, the correction
in cubic yards becomes

$$
\begin{array}{r}
\mathrm{Q}=\left\{\left(\frac{b}{4} \times \pi_{1}\right)\left(d+\frac{b}{2}\right) \sim\left(\frac{b^{\prime}}{4} \times h_{2}\right)\left(d^{\prime}+\frac{b^{\prime}}{2}\right)+c\left(\frac{d+d^{\prime}}{2}\right)\right. \\
\left.\times\left(d \sim d^{\prime}\right)\right\} \mathbf{C}^{\circ} \times 0.000215 \ldots \tag{25}
\end{array}
$$

## PART II.

## PLAIN INSTRUCTIONS

FOR OBTAINING THE PRISMOIDAL CONTENTS OF EARTHWORK, WITH practical rules and examples showing the uses of the ACCOMPANYING TABLES IN SIMPLIFYING COMPUtations by the formule of part i.

The following Rules for computation of Cubic Contents are based on the condition that the transverse surface lines of the end sections shall be sensibly similar ; but it will be observed that 1,2 , and 3 together cover all cases to which the method of "Roots and Squares," or of " Equivalent level heights," can be correctly applied, and that the practical limit of their application may be indefinitely extended by increasing the proximity of the cross sections in rough ground.

To find the prismoidal contents of thorough-cut or fill when road-bed width and side slopes are constant between end sections.
Given : areas, side slopes, and base ( A and $\mathrm{A}^{\prime}, s$ and $s^{\prime}$, and $b$ ).
Rule 1.-(Formula 18).

Enter table 2 with the given road-bed width (b), and the half sum of the ratios of the side slopes $\left(\frac{s+s^{\prime}}{2}\right)$, and take out the corresponding area $=a . \quad$ Add this to each of the given end areas and the square roots of the resulting quantities ( $\sqrt{\mathrm{A}+a}$ and $\sqrt{\mathrm{A}^{\prime}+a}$ ) from table 3 are N and $\mathrm{N}^{\prime}$, the correction numbers.

Enter table 4 with the average of the end areas $\left(\frac{A+A^{\prime}}{2}\right)$, and table 5 with the difference of the correction numbers ( $\mathrm{N} \sim \mathrm{N}^{\prime}$ ), and take out the corresponding quantities. The difference of the quantities taken from tables 4 and 5 is the contents in cubic yards for a length of 100 feet.

For a different length multiply by the length in feet and divide by 100 .

Example.—Given $\Lambda=974 ; \mathrm{A}^{\prime}=87 ; s=\frac{1}{2} ; s^{\prime}=\frac{3}{4} ; b=20$.

From table 2 when $b=20$ and $\frac{s+s^{\prime}}{2}=\frac{5}{8}$, the area of the grade triangle ( $a$ ) $=160$

$$
\begin{aligned}
& \sqrt{\mathrm{A}+a}= \sqrt{974+160}=1134 \text { table } 3 \ldots \ldots \ldots 3.7=\mathrm{N} \\
& \sqrt{\mathrm{~A}^{\prime}+a}=\sqrt{87+160}=247 \text { table } 3 \ldots \ldots \ldots .15 .7=\mathrm{N}^{\prime} \\
& \frac{\mathrm{A}+\mathrm{A}^{\prime}}{2}= \frac{974+87}{2}=530.5 \text { table } 4 \ldots \ldots \ldots .1965 \\
& \mathrm{~N} \sim \mathrm{~N}^{\prime}= 33.7 \sim 15.7=18.0 \text { table } 5 \ldots \ldots \cdot-200 \\
& \quad \text { Contents for } 100 \text { feet......... } \overline{1765} \text { eyds. }
\end{aligned}
$$

For a different length as 80 feet, $1765 \times 0.8=1412$ cyds.
Note.-If the square roots of the areas to the intersection of the side slopes are obtained and recorded when the areas are calculated, as will ordinarily be found more convenient, the data are A and $\mathrm{A}^{\prime}$ and N and $\mathrm{N}^{\prime}$, and only the two last steps of Rule 1 are necessary.

To find the prismoidal contents of side hill work, pyramids, and any solid with similar end sections.
Given : end areas ( A and $\mathrm{A}^{\prime}$ ).
Rule 2 (Formula 19).
Take the square roots of the end areas $\left(\sqrt{\mathrm{A}}\right.$ and $\left.\sqrt{\mathrm{A}^{\prime}}\right)$ from table $3=n$ and $n^{\prime}$.

Enter table 4 with the arerage of the end areas $\left(\frac{A+A^{\prime}}{2}\right)$, and table 5 with the difference of the correction numbers ( $n \sim n^{\prime}$ ), and take out the corresponding quantities. The difference between the quantities taken from tables 4 and 5 is the contents in eubic yards for 100 feet.

For a different length multiply by the length in feet and divide by 100 .

Example.-Given end areas $\mathrm{A}=41$ and $\mathrm{A}^{\prime}=185$.
$\sqrt{\mathrm{A}}=41$ table $3=6.4=n ; \sqrt{\mathrm{A}^{\prime}}=185$ table $3=13.6=n^{\prime}$.
$\frac{\mathrm{A}+\mathrm{A}^{\prime}}{2}=\frac{41+185}{2}=113$ table $4 \ldots \ldots .418 .5$
$и \sim n^{\prime}=6.4 \sim 13.6=7.2$ table $5 \ldots \ldots . .32 .0$
Contents for 100 feet. . . . . . . . . . 386.5 cyds.
For a different length, as 25 feet, $\frac{386.5}{4}=96.6$ cyds.
Example.-Pyramid. Given end areas $\mathrm{A}=104$ and $\mathrm{A}^{\prime}=0$. $\sqrt{\mathrm{A}}=10 \pm$ table $3=10.2=n ; \sqrt{\mathrm{A}^{\prime}}=0=n^{\prime}$.

$$
\begin{aligned}
& \frac{\mathrm{A}+\mathrm{A}^{\prime}}{2}=\frac{104+0}{2}=52 \text { table } 4 \ldots \ldots \ldots .192 .6 \\
& n \sim n^{\prime}=10.2 \sim 0=10.2 \text { table } 5 \ldots \ldots-64.2 \\
& \quad \text { Contents for } 100 \text { feet.............. } 128.4 \text { cyds. }
\end{aligned}
$$

For a different length, as 60 feet, $128.4 \times 0,6=7 \%$ cyds.
Note.-Examples under Rule 1 can be readily tested by Rule 2 , the difference in the working being that the grade prism is first included and then deducted. For instance, in the example given under Rule 1; the end areas to intersection of side slopes are 1134 and 247 , and the square roots corresponding $33 . \%$ and $16 . \%$-then :
$\frac{1134+247}{2}=695.5$ table $4 \ldots \ldots \ldots \ldots .2558$
$33 . \% \sim 15.7=18.0$ table $5 \ldots \ldots \ldots \ldots-200$
Contents to intersection of side slopes. . $\overline{2358}$
Less grade prism 160 table $4 \ldots \ldots \ldots .-593$

Contents of earthwork for 100 feet. $\overline{1765}$ cyds.
To find the prismoidal contents of thorough-cut or fill when the end road-bed widths are different.
Given : end areas, side slopes, and end road-bed widths ( A and $\mathrm{A}^{\prime}$; $s$ and $s^{\prime} ; b$ and $b^{\prime}$ ).

## Rule 3 (Formula 17).

Enter table 2 with $\frac{s+s^{\prime}}{2}$ and $b, b^{\prime}$ and $b \sim b^{\prime}$ respectively, and take out the corresponding areas $a, a^{\prime}$ and $a^{\prime \prime}$. From table 3 take out the square roots of the end areas to intersection $\sqrt{\overline{A+a}}=\mathrm{N}$, and $\sqrt{\mathrm{A}^{\prime}+a^{\prime}}=\mathrm{N}^{\prime}$.

Enter table 4 with $\frac{\mathrm{A}+\mathrm{A}^{\prime}}{2}+\frac{a^{\prime \prime}}{6}$, and table 5 with $\mathrm{N} \sim \mathrm{N}^{\prime}$, and the difference between the corresponding quantities taken from tables 4 and 5 is the contents in cubic yards for 100 feet. For a different length multiply by the length in feet and divide by 100 .

Example.-Given $b=16 ; b^{\prime}=40 ; s=\frac{1}{4} ; s^{\prime}=\frac{3}{4} ; \mathrm{A}=1565$; $\mathrm{A}^{\prime}=253$.

Here $\dot{a}=128 ; a^{\prime}=800 ; a^{\prime \prime}=288 ; \mathrm{N}=41.1$ and $\mathrm{N}^{\prime}=32.4$.

$$
\frac{\mathrm{A}+\mathrm{A}}{2}+\frac{a^{\prime \prime}}{6}=\frac{1565+253}{2}+\frac{288}{6}=95 \% \text { table } 4 \ldots \ldots 3544.4
$$

$$
\mathrm{N} \sim \mathrm{~N}^{\prime}=41.1 \sim 32.4=8.7 \text { table } 5 \ldots \ldots \ldots \ldots-46 .{ }^{7}
$$

Contents for 100 feet. . . . . . . . . . . . . . . . . 3497.8
For a different length, as 50 feet $\ldots . \frac{3497.7}{2}=1749 \mathrm{cyds}$.

The example under Rule 3 is of a case where averaging the end areas gives less than the prismoidal contents. It may be tested by Formula 8, page 12, as also Rules 1 and 2 by Formulæ 9 and 10.
To find the prismoidal contents when the ground is level transversely, ar where the heights of equivalent level sections have been obtained.
Given : level heights, base and half-sum of ratios of side slopes ( $h$ and $h^{\prime} ; b$ and $\frac{s+s^{\prime}}{2}$ ).

## Rule 4 (Formula 21).

Enter the table of level cuttings for the proper base and side slopes with the half-sum of the end heights $\left(\frac{h+h^{\prime}}{2}\right)$, and the table of special plus corrections for the same side slopes with the difference of the end heights ( $h \sim h^{\prime}$ ), and take out the corresponding quantities. The sum of these quantities is the contents for 100 feet.

For a different length, multiply by the length in feet and divide by 100 .

$$
\begin{gathered}
\text { Example.—Given } b=14 ; h=8.6 ; h^{\prime}=36.8 ; \frac{s+s^{\prime}}{2}=1 \frac{1}{2} . \\
\frac{h+h^{\prime}}{2}=\frac{8.6+36.8}{2}=22.7 \text { table } 15 \ldots \ldots \ldots \ldots .4040 \\
h \sim h^{\prime}=8.6 \sim 36.8=28.2 \text { table } 17 \ldots \ldots \ldots \ldots+368 \\
\quad \text { Contents for } 100 \text { feet................................ }
\end{gathered}
$$

To find the Correction for Curvature in single width thorough-cut when the transverse surface slope is regular.
Given : area to intersection of side slopes, degree of curve, and difference of side distances ( $\mathrm{A}+a, \mathrm{C}^{\circ}$, and $d \sim d^{\prime}$ ).

## Rule 5 (Formula 23).

Enter table 18 with $d \sim d^{\prime}$ and take out the corresponding factor : multiply this into the product of $\mathrm{A}+a$ by $\mathrm{C}^{\circ}$, and the result is Q the correction in cubic yards, to be applied at the middle one of three stations, all on the same curve and 100 feet apart. If the distance to either of the other two stations from the middle one differs from 100 feet, multiply by the half-sum of the two distances and divide by 100 .

This correction is to be added or subtracted accordingly as the curve is convex or concave toward the higher ground.

Example.—Given $c=28 ; h_{1}=40 ; h_{2}=16 ; d=74 ; d^{\prime}=38 ;$ $b=28 ; \mathrm{R}=1400$; or $\mathrm{A}+a=2090 ; \mathrm{C}^{\circ}=4^{\circ} .09 ; ~ d \sim d^{\prime}=36$. 36 table $18=0.00 \% \% 6$,
and $2090 \times 4.09 \times 0.00 \% 76=66.3$ cyds.
If the distances to the two adjacent stations are 50 and 40 feet respectively, the correction required is $\frac{50+40}{200} \times 66.3=66.3 \times 0.45$ $=29.8 \mathrm{cyds}$.

To find the correction for curvature in side-hill work when the trensverse surface slope is regular.
Given : area; degree of curve; side distance ; road-bed width ; and width of excavation at road-bed $\left(\mathrm{A} ; \mathrm{C}^{\circ} ; d ; b ; w\right)$.

## Rule 6 (Formula 24).

Enter table 18 with $d+b-w$ and take out the corresponding factor : multiply this by the product of A by $\mathrm{C}^{\circ}$, and the result is Q the correction in cubic yards, to be applied in all respects as in Rule 5.

Example. -Given $w=17 ; \quad b=30 ; ~ d=51 ; ~ h_{1}=\mathfrak{d t} ; \mathrm{l}=$ 1600 ; or $\mathrm{A}=204 ; \mathrm{C}^{\circ}=3^{\circ} .58 ; ~ a+b-w=64$.

64 table $18=0.01379$,
and $204 \times 3.58 \times 0.013 \%=10.1$ cyds.
If both intervals are 50 feet, the correction required is $\frac{50+50}{200}$ $\times 10.1=10.1 \times 0.5=5$ cyds.

For correction for curvature when the transverse surface slope is broken, or for double-width thorough-cut, see page 24.

Rules 5 and 6 apply to excavation only. For embankment the correction is to be addecd or subtracted accordingly as the curve is concave or convex toward the higher ground.

## MISCELLANEOUS EXAMPLES.

Eximple 1.


Example 1, as above, is of the railroad cut given in Morris's "Earthworks,"* pp. 47-54, with contents computed by Rules 1 , 2, and 4, and the auxiliary tables of the present work. As here used, the areas are supposed to belong to sections which, when carried to the intersection of the side slopes in thorough-cut, are rendered sensibly similar, and the examples as here given are intended

[^1]to show only the comparative facility of arriving at the prismoidal contents by Mr. Morris's methods and those of the preceding rules when the above condition of similarity is fulfilled, and not to endorse the application of the method of "Roots and Squares" (or of the rules of this work) in cases where the hypothetical middle area materially differs from the actual one.*

Except by trial with the actual middle section and the prismoidal formula, it seems almost impossible in cases of dissimilar end sections to know when the application of the method of Roots and Squares, or of the preceding rules, begins to fail of practical correctness, but it may safely be assumed that if the ground is properly and sufficiently cross-sectioned, the results obtained by them will be practically the prismoidal contents.

The above tabulated example shows all the steps necessary in finding the prismoidal contents in cubic yards when the areas are given. Columns (1), (2), and (3) being written out, (4) is derived directly from (3) by areraging ; (5) from (3) by adding area of grade triangle in thorough-cut ; (6) from (5) by table 3 ; (7) from (6) by subtraction ; (8) from (4) by table 4 ; (9) from (\%) by table 5 ; and (10) from (8) and (9) by subtraction.

Column (4) gives the average end areas throughout the cut, including the terminal pyramids, and the only break in the routine of adding the area of the grade triangle in column (5) is at the point where the cutting runs out on the lower side. At such points two areas have to be used, the one of earthwork plus the grade triangle, for computation of thorough-cut by Rule 1, and the other of earthwork alone, for the calculation of the pyramid or side-hill work into which the thorough-cut changes, and of which the computation of contents falls under Rule 2.

Column (8) gives the contents between each two stations roughed out by the common method of " average areas," column (9) the corresponding error, and column (10) the prismoidal contents, all in cubic yards.

It is not strictly necessary to write out all of the columns given above, but errors are so much more readily detected when all of the steps are shown, that ordinarily time and labor will be saved by adopting some system of tabulating similar to the above, both as regards the number of columns and the arrangement by which the figures referring to each two stations may be recorded on a line between them.

[^2]The prismoidal contents in cubic yards between stations 1 and 17 are given by Mr. Morris as 15,721, and by the above computation as 15,723 , whilst the contents of the whole cut given by him as 16,664 appear above as $16,24 \%$. The discrepancy is in the truncated portions of the cut outside of stations 1 and 17 , which by some oversight he gives as 943 , instead of 524 cubic yards.

The preceding example will now be computed by equivalent level heights and Rule 4. The data of level heights are supposed to be obtained from Trautwine's diagrams, as when such accuracy is required as renders the calculation of areas necessary, Rule 1,2 , or 3 should be used for the computation of contents.

Example 2.


With equivalent level heights given, the above tabulated example shows all the steps required in finding the approximate prismoidal conteats in cubic yards. Columns (1), (2), and (3) being written out, (4) is derived directly from (3) by averaging, and (5) from (3) by subtracting. The table of level cuttings for a base of 20 feet and slopes 1 to 1 , from which column (6) should be taken, is not published in this volume, but its place may readily be supplied by adding 1. to each of the herghts of column (3), and taking 70 from each of the corresponding quantities in table 12. Such remainders are the amounts in column (6). Column (7) is derived from (5) by table 14 , and (8) from (6) and (7) by addition.

In ordinary ground sloping transversely, the area of earthwork of the terminal pyramid at the point where the centre height is nothing, is about one-fourth of the area of the section where the pyramid begins ; and practically, as only small quantities are concomed, the equivalent level height corresponding may be taken as one-fourth of that corresponding to the area of the base of the pyramid.

The calculation of contents by equivalent level heights and tables is well suited for preliminary or approximate estimates, especially if, as in the present case, when the sum of the tenths of the end heights is uneven, the average is always taken as the tenth next greater than the actual half-sum.

The variation between the contents of the thorough-cut from 1 to 17, as given in Examples 1 and $\Omega$, is due to the fact that the equivalent level hieights are carried out to tenths only. In the present case, at a height of 20 feet the increment is over two cubic yards for each 0.01 of a foot, and in embankment at the same height it is still greater. As in practice neither equivalent level heights nor those of the tables of level cuttings are carried out to hundredths, one cause of the greater accuracy of the previous method by Rules 1 and 2 is evident. It may be replied that crrors as important are involved in the field work, the cross section stakes being set only approximately; but that an element of error should voluntarily be introduced into the calculations because another such already exists in the data, is a position that will not be contended for scriously.

Example 3.-In a cutting with road-bed width 16 feet, and opposite side slopes $\frac{1}{2}$ and $\frac{3}{4}$ to 1 , the given areas of two consecutive cross sections with similar transverse surface lines and at a distance apart of 100 feet, are 100 and 1000 square feet respectively: required the prismoidal contents. Here the area of the grade triangle (table 2)
is 102 , and consequently the whole areas to intersection are 202 and 110 ?.

> To find the correction numbers $N$ and $N^{\prime \prime}$.
> 202 table 3
> $14.2=N$
> 1102 table 3............................ $33.2=N^{\prime}$

To find the contents in cubic yards.

$$
\frac{100+1000}{2}=550 \text { table } 4 \ldots \ldots \ldots \ldots \ldots . . . . . . .
$$

$14.2 \sim 33.2=19.0$ table 5...............-223
Contents for 100 feet. . ........... $\overline{1814}$ cyds.
Test by Formula 9.
$\sqrt{202 \times 1102}=47 \%=$ mean area to intersection.
$\left(\frac{202+1102+472}{3}-102\right) \frac{100}{27}=(592-102) \frac{100}{27}$

Example 4.-Given 100 and 1000 square feet respectively as the areas of two similar cross sections 100 feet apart, irrespective of shape or number of sides in perimeter : required the prismoidal contents.

To find the correction numbers $n$ and $n$.

$$
\begin{aligned}
& 100 \text { table } 3 \\
& 10.0=n \\
& 1000 \text { table } 3 \text {. } \\
& .31 .6=n^{\prime}
\end{aligned}
$$

To find the contents in culic yards.

$$
\begin{aligned}
& \frac{100+1000}{2}=550 \text { table } 4 \ldots \ldots . . . . . . . . . . . . . . .203 \% \\
& 10.0 \sim 31.6=21.6 \text { table } 5 \\
& -288 \\
& \text { Contents for } 100 \text { feet. . . . . . . . . . . } \overline{1749} \text { cyds. } \\
& \text { Test by Formula } 10 . \\
& \sqrt{100 \times 1000}=316=\text { mean aréa. } \\
& \left(\frac{100+1000+316}{3}\right) \frac{100}{27}=472\left(\frac{100}{27}\right) \\
& =4 \% 2 \text { table } 4 \\
& 1748 \text { cyds. }
\end{aligned}
$$

Example 5.-At two stations 100 feet apart with base $b=14$ feet, and side slopes $s=1 \frac{1}{2}$ to 1 , given the notes of the cross section at the first station, centre height $\mathrm{C}=10.2$, side heights $h_{1}$ and $h_{\mathrm{a}}=$
6.8 and 15.2, and side distances $d$ and $d^{\prime}=17.2$ and 29.8 ; and at second station, centre height 38.6 , side heights 28.6 and 53.0 , and side distances 49.9 and 86.5.

Calculation of areas $A$ and $A^{\prime}$, and correction numbers $N$ and $N^{\prime}$.
For the grade triangle corresponding to $b=14$ and $\frac{s+s^{\prime}}{2}=1 \frac{1}{2}$, the height table $1=4.67$, and the area table $2=33=a$.

$$
\text { By Formula (1) and Rule } 1 .
$$

Area $(\mathrm{A}+a)=\frac{\left(10.2+4.6^{7}\right)(17.2+29.8)}{2}=349$ table $3=18.4=$ correction number $N$; and $349-33=316=\mathrm{A}$.

Area $\left(\mathrm{A}^{\prime}+a^{\prime}\right)=\frac{(38.6+4.67)(49.9+86.5)}{2}=2951$ table $3=54.3$ $=$ correction number $N^{\prime}$; and $2951-33=2918=\mathrm{A}^{\prime}$.

Calculation of Contents.-Formula (18), Rule 1.

$$
\begin{aligned}
\frac{316+2918}{2} & =1617 \text { table } 4 \ldots \ldots \ldots \ldots \ldots \ldots . . . \ldots 5989 \text { cyds. } \\
18.7 \sim 54.3 & =35.6 \text { table } 5 \ldots \ldots \ldots \ldots \ldots . \ldots 88
\end{aligned}
$$

Contents for 100 feet. . . . . . . . . . . . . $520 \%$ cyds.
Test by Formula 13.
From the preceding data the notes of the middle area would give centre height 24.4 , and side distances 33.55 and 58.15 ; and by Formula (1)

$$
\frac{(24.4+4.67)(33.55+58.15)}{2}-33=1333-33=1300=\mathrm{M} .
$$

by Formula (13) $\frac{317+2918+1300 \times 4}{6} \times \frac{100}{2 y}=1406$ tab. $4=5207 \mathrm{cyds}$.

> To find the equivalent level heights.-(Rule \%.) 316 table 4.... $11 \% 0$ table 10. . . 10.6 equiv. lev. ht. 2918 table 4....10,807 table 10...39.7 " "،
> Test by Trautwine's method, with level heights. 10.6 table 10............. . . . . . . . . . . . . . . . . . 1174
> 39.7 table 10. . . . . . . . . . . . . . . . . . . . . . . . . . 10,815
> ( 25.15 table $10 \ldots . . . .4818 .5$ ) $\times 4 \ldots . . .$. . $19,2 \% 4$
> Contents for 100 feet. . ......... $6[\overline{5,210,5} \overline{31,263}$ cyds.

By Formula (21), Rule (4), with level heights.

$$
\begin{align*}
& \frac{10.6+39.7}{2}=25.15 \text { table } 10 \ldots \ldots \ldots \ldots . \ldots 4818.5 \\
& 10.6 \sim 39.7=29.1 \text { table } 15 \ldots \ldots \ldots \ldots+392.0 \\
& \text { Contents for } 100 \text { feet } \ldots \ldots \ldots \ldots .5,210.5 \\
& \text { cyds. }
\end{align*}
$$

By Fornula (20), with end areas and level heights.

$$
\frac{316+2918}{2}=1617 \text { table } 4 \ldots \ldots \ldots \ldots \ldots \ldots . . \ldots 989
$$

Approximation ly Formula (20), with centre leights of profile sabstituted for level heights.

$$
\begin{aligned}
\frac{316+2918}{2} & =1617 \text { table } 4 \ldots \ldots \ldots \ldots \ldots . . \ldots 5989 \\
10.2 \sim 38.6 & =28.4 \text { table } 17 \ldots \ldots \ldots \ldots .-\% 47 \\
\text { Approximate contents for } 100 \text { feet.5, } 242 & \text { cyds. }
\end{aligned}
$$

This approximation is for an extreme case, as in practice the difference between two consecutive centre heights is rarely as much as one-half of the difference above taken. In ordınary cases this approximation gives results very nearly correct.

It will be obserred that by Trautwine's method, as given above, three quantities are taken from the tables, and that it involves an addition of three quantities, a multiplication, and a division ; whilst by Rule 4 , which with the same data gives the same result, the sum of two quantities taken from the tables is the required contents.

Example 6.-Correction of Contents for Curvature.-If the second cross section of Example 5 is at the middle one of three stations 100 feet apart, and all of them on a $6^{\circ}$ curve which is concave toward the higher ground, the correction for curvature to be deducted at the station under consideration is obtained as follows by Rule 5 :

From the above $\mathrm{C}^{\circ}=6$, and from the notes of Example 5, $\mathrm{A}+a=2951$, and $d \sim d^{\prime}=36.6$. But 36.6 table $18=0.007885$; and $\mathrm{Q}=2951 \times 6 \times 0.007885=139.6 \mathrm{cyds}$.

## Test by Henck's Formula.

$\mathrm{C}=\left\{\frac{1}{2} c(d-d)+\frac{1}{4} b\left(h-h^{\prime}\right)\right\} \times \frac{2}{3}\left(d+d^{\prime}\right) \sin \mathrm{D}$, in which $d$ and $d^{\prime}$ are side distances, $h$ and $l^{\prime}$ side heights, $c$ the centre height, and D
the deflection angle; hence from the above and the notes of Example 5,
$\mathrm{C}=\left(\frac{38.6}{2} \times 36.6+\frac{14 \times 24.4}{4}\right) \times \frac{2 \times 136.4}{3} \times 0.05234=376 \dot{8} .5 \mathrm{cu}$. feet
$=139.6$ cyds. In practice $d \sim d^{\prime}$ is required to the nearest foot only.

## REMARKS ON ESTIMATING CONTENTS.

## profile eartiwork.

In addition to the cross sections at the regular stations, others are necessary where changes begin in the character of the transverse surface slope, as well as at all points where the surface line of the profile changes its direction ; and all of the formulæ and rules heretofore given for finding the contents suppose the solid to be between two consecutive cross sections taken at such points.

In passing from cutting into embankment, cross sections should always be taken at the two points on opposite sides of the road-bed where the cutting "runs out." This will obviate the necessity for staking out the "P.P." except with a zero point on the centre line, $a s$, in addition to accurate data for calculation of the pyramids of cut and bank which lie between the two cross sections thus taken, two more zero points, one on each side of the road-bed, will be given. For like reasons, in passing from thorough into side hill cutting, the point on the lower side where the excaration runs out should be cross-sectioned.

Where the original quantities of excavation and embankment have been calculated, and the work is being done aecording to the slope-stakes and field-notes, probably the simplest method of obtaining the quantities moved in an unfinished cutting or embankment is to take the average heights above or below the road-bed at each of the several stations of that portion which has been worked upon, and then, with Formula (21), Rule 4, and tables, to calculate by these heights the quantities remaining to be done. The latter subtracted from the original quantities between the same stations will, of course, give the desired amount.

When the material lies in strata, a similar means may be used for determining the respective quantities of the different kinds of
excaration. For example, a cutting may be composed of earth at top, loose rock below the earth, and solid rock at bottom : the amounts then calculated by the loose rock heights, and deducted from the original quantities giving the earth, and the solid rock similarly calculated and deducted from the amounts obtained by the loose rock heights giving the loose rock. When the necessary arerage heights have been obtained, the quantities corresponding may be found very rapidly by Rule 4 and the proper tables.

For approximate estimates, when the centre heights and transverse surface slopes only are given, the shortest method is to find the equivalent level heights by Trautwine's diagrams, and then take out the contents by Rule 4 .

When the work is carried on irregularly, no general rules for ascertaining the true contents can be given. When the cross sections are very irregular and dissimilar, the best practical rule is to take them at very short intervals. This in all cases reduces the error in the calculation of contents to a minimum.

A very careful and thorough investigation of the mathematical methods of calculating irregular earthwork is given in the article on "Earthwork" in Henck's "Field-Book," and to that the theoretical reader is referred.

## BORROW PITS.

For obtaining the contents of extensive borrow pits, the following will be found to be about as simple a method as is consistent with correctness. Before the excavation is commenced, lay off the surface in squares, rectangles, or triangles, small enough to be considered as plane surfaces, and take elevations with the Level at all of the corners. These elevations must be referred to a base which will be below the bottom of the borrow pit when the work is finished.

A plan of the ground as laid off should then be made, and the elevations above the base recorded on it at the corners. When en estimate of the quantities excarated is to be made during the progress of the work, the horizontal limits of the pit as then excavated should be taken, and inside of these limits the whole of the ground again divided into rectangles and triangles without reference to the former surface divisions, the elevations above the base plane again leing taken at all corners, including those on the surface at the edges of the pit.

The original quantity inside of the pit limits and down to the base plane, taken as a series of truncated prisms, should then be calculated, and next the quantity remaining inside of the pit limits
and above the base plane. The difference between these amounts gives the quantity excavated.

The advantage of using an independent method of dividing up the ground after the original surface has been removed is that it rarely happens that the best arrangement of these subdivisions for reducing to plane surfaces will agree accurately, either in size or position, with those originally taken on the ground surface. If, however, the same divisions can be taken in the bottom of the pit as originally on the surface, the differences of the elevations at each corner taken before and after the excavation is made will give the heights of the prisms, of which the contents may be obtained by a single calculation.

In order to prevent the necessity for recalculating the finished portions at each estimate, when any portion of the pit will not again be disturbed, its limits should be referenced on the ground and indicated on the plan, and its contents recorded separately.

## RULES FOR VARIOUS USES OF TABLES.

## To find the height of an equivalent level section.

*Given : areas, side slopes, and base.

$$
\text { Rule } \% .
$$

Enter table 4 with the given area, and take out the corresponding quantity: find the quantity nearest to this in the body of table of level cuttings with the given side slopes and base, and the index number corresponding is the equivalent level height to the nearest tenth.

[^3]Example.-Given $a=800 ; \frac{s+s^{\prime}}{2}=1 \frac{1}{2} ; b=14$
800 table 4. . . . 2963 table 15 . . . 18.9 equiv. lev. ht.
To find the area corresponding to a level height, reverse the process of Rule $\%$.

## To find the muddle area of Rule 1.

Given : $\mathbf{N}, \mathbf{N}^{\prime}$, and $a$.
Rule 8.
Enter table 3 with $\frac{N+N^{i}}{z}$, and take out the quantity corresponding ; from this deduct $a$, and the remainder is the middle area.

From example 5, page 36, $\mathrm{N}=18.7$; $\mathrm{N}^{\prime}=54.3$; and $a=33$.

$$
\frac{18 . \%+54.3}{2}=36.5 \text { table } 3 \ldots \ldots \ldots \ldots . .1332
$$

$$
1332-33=1299=\mathrm{M}
$$

To find the middle area of Rule 2.
Given : $n$ and $n^{\prime}$.
Rule 9.
Enter table 3 with $\frac{n+n^{\prime}}{\sim}$, and the quantity corresponding is the middle area.

Example. -With similar end areas $4 \times 25=100$, and $8 \times 50=$ 400 , the middle area is $6 \times 3 \% .5=225$. Here $n=10$ and $n^{\prime}=20$, and $\frac{n+n}{2}=\frac{10+20}{2}=15$ table $3=225=\mathrm{M}$.

To find the middle area of Rule 4.
Given : $h$ and $h^{\prime} ; \frac{s+s^{\prime}}{\sim}$; and $b$.

## Rule 10.

Enter the table of level cuttings for the given side slopes and base with $\frac{h+h^{\prime}}{2}$, and take out the corresponding quantity : find the quantity nearest to this in the body of table 4, and the index number corresponding is the middle area.

Example.-From example 5, page 36, $h=10.6$ and $h^{\prime}=39 . \%$.

$$
\frac{10.6+39.7}{2}=25.15 \text { table } 15 \ldots .4818 \text { table } 4 \ldots . \ldots 1301
$$



## To extend the Correction Tables, general or special.

Rule 11.
When the difference of the correction numbers, or of the level heights, is too large to enter the table with, take one-half of it, and with this enter and take out the corresponding quantity, which multiplied by 4 gives the correction required for a length of 100 feet.

Examples.-In table 5 the correction corresponding to 32 is 632.1, which multiplied by 4 gives 2528.4 , the correction corresponding to 64 .

In table 17 , the correction corresponding to 12.2 1s 68.9 , which multiplied by 4 gives 275.6 , the correction corresponding to 24.4.

> To find the special corrections for any given side slopes from the general correction table.

## Rutle 12.

Enter table 5 with $h \sim h^{\prime}$, and take out the corresponding quantity ; for the special plus corrections multiply this by the quartersum of the ratios of the side slopes $\left(\frac{s+s^{\prime}}{4}\right)$; for the special minus. correction multiply by the half-sum $\left(\frac{s+s^{\prime}}{2}\right)$. The corrections so obtained are for $=$ lengths of 100 feet.

Examples.-From table 5 the general minus correction corresponding to 39.4 is 958.2 , and the plus correction for $\frac{s+s^{\prime}}{2}=1 \frac{1}{2}$ is $958.2 \times \frac{3}{4}=\% 18 . \%$ corresponding to 39.4 table $1 \%$. The minus correction for $\frac{s+s^{\prime}}{2}=\frac{1}{2}$ is $958.2 \times \frac{1}{2}=479.1$ corresponding to 39.4 table 14. In like manner with $\frac{s+s^{\prime}}{2}=\frac{1}{5}$ the plus correction for 39.4 $=958.2 \times 0.1=95.8$, table 8 ; and with $\frac{s+s^{\prime}}{2}=1$, the minus corrections, general and special, are the same, as are $\mathrm{N} \sim \mathrm{N}^{\prime}$ and $\hbar \sim \hbar^{\prime}$. (See table 5, and examples 1 and 2, pages 31 and 33.)

## EXPLANATIONS OF TABLES.

Table 1 is for obtaining the height of the grade triangle. To use it, find the half-sum of the ratios of the given side slopes at the top, and the number vertically below, and on the same line with the given road-bed width in the left column, is the height required. Thus with $b=16$ and $\frac{s+s^{\prime}}{2}=\frac{5}{8}$ the height corresponding is 12.8 .

Table 2 contains the area of the same triangle. It is used with the same data and entered in the same way. Thus with $b=18$ and $\frac{s+s^{\prime}}{2}=\frac{1}{2}$ the area corresponding $=a=162$.

Table 3 gives square roots to tenths, or correction numbers of areas. To use it, find in the body of the table the number nearest to that which expresses the area under consideration, and the figures on the same horizontal line in the left column are the whole numbers, and that immediately above it, at the top of the table, the tenths of the correction number required. Thus if the area to intersection of side slopes is 2,000 , the correction number N is 44.7 ; if one of similar end areas is 230 , the correction number $n$ is 15.2 .

Table 4 is for finding the contents for 100 feet corresponding to a given area. The left column contains the tens, and the top the units, of the area. In the body of the table are the corresponding contents in cubic yards for lengths of 100 feet. In the short table of two lines prefixed, the contents corresponding to the tenths of the area are given, and these when required are to be added to the contents taken from the main table. Thus the contents corresponding to the area $1872 . \%$ are $6933.3+2.6=6935.9$ cubic yards.

Table 5 is for obtaining the corrections for computations by average areas. The arithmetical difference between the correction numbers is to be found in whole numbers and tenths respectively, in the left column and at the top of the table, and the number corresponding in the body of the table is the correction in cubic yards for a length of 100 feet. Thus if the difference of the correction numbers is 28.3 , the correction corresponding is 494.4 cyds. This correction is always to be subtracted.

The Tables of Level Cuttings for special side slopes and road-bed widths give the cubic yards for lengths of 100 feet corresponding to the different heights, of which the whole numbers are in the left column and the tenths at top.

The special tables of plus corrections give the correction for computation by averaging equivalent level heights. The differences of the end heights in feet and tenths respectively are in the left column and at top, and the corresponding corrections for lengths of 100 feet in the body of the table. Care must be taken to use the correction table with the half sum of the side slopes the same as that of the table of level cuttings of which the contents are to be corrected.

The special tables of minus corrections give the corrections for average areas when entered with the heights of equivalent level sections. The side slopes of the table must be the same as those of the end sections, between which the contents are to be corrected.

When the tables of minus corrections for special slopes are entered with the differences of the centre heights of the profile instead of those of the equivalent level heights, in ordinary ground a close approximation to the true correction is obtained.

For the special plus correction tables the half-sum of the side slopes is indicated at the top. For the special minus corrections the slopes are indicated at the bottom of the same tables.

Table 18 contains factors for calculation of the corrections for curvature. Its use is explained in Rules 5 and 6.

## TABLE No. 1.

Roadbed Width in Left Column; half-sum of ratios of Side Slopes at Top; Height of Grade Triangle in body of Table.

| 岂 | $\frac{1}{5}$ | $\frac{1}{4}$ | $\frac{3}{8}$ | $\frac{1}{2}$ | $\frac{5}{8}$ | 3 | 7 | 1 | 11/8 | $1 \frac{1}{4}$ | 13 | $1 \frac{1}{2}$ | 2 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | 25 | 20 | 13.3 | 10 | 8.0 | 6.7 | $5 \cdot 7$ | 5 | 4.4 | 4.0 | 3.6 | 3.3 | 2.5 |
| 12 | 30 | 24 | 16.0 | 12 | 9.6 | 8.0 | 6.9 | 6 | $5 \cdot 3$ | 4.8 | $4 \cdot 4$ | 4.0 | 30 |
| 14 | 35 | 28 | 18.7 | 14 | 11.2 | 9.3 | 8.0 | 7 | 6.2 | 5.6 | 5.1 | 4.7 | 3.5 |
| 16 | 40 | 32 | 21.3 | 16 | 12.8 | 10.7 | 9.1 | 8 | 7.1 | 6.4 | 5.8 | $5 \cdot 3$ | 4.0 |
| 18 | 45 | 36 | 24.0 | 18 | 14.4 | 12.0 | 10.3 | 9 | 8.0 | 7.2 | 6.5 | 6.0 | 4.5 |
| 20 | 50 | 40 | 26.7 | 20 | 16.0 | 13.3 | 11.4 | 10 | 8.9 | 8.0 | 7.3 | 6.7 | 5.0 |
| 22 | 55 | 44 | 29.3 | 22 | 17.6 | 14.7 | 12.6 | II | 9.8 | 8.8 | 8.0 | 7.3 | 5.5 |
| 24 | 60 | 43 | 32.0 | 24 | 19.2 | 16.0 | 13.7 | 12 | 10.7 | 9.6 | 87 | 8.0 | 6.0 |
| 26 | 65 | 52 | 34.7 | 26 | 20.8 | 17.3 | 14.9 | 13 | 11.6 | 10.4 | 9.5 | 8.7 | 6.5 |
| 28 | 70 | 56 | 37.3 | 28 | 22.4 | 18.7 | 16.0 | 14 | 12.4 | 11.2 | 10.2 | 9.3 | 7.0 |
| 30 | 75 | 60 | 40.0 | 30 | 24.0 | 20.0 | 17.1 | 15 | 13.3 | 12.0 | 10.9 | 10.0 | 7.5 |
|  | $\frac{1}{5}$ | $\frac{1}{4}$ | $\frac{3}{8}$ | $\frac{1}{2}$ | $\frac{5}{8}$ | $\frac{3}{4}$ | $\frac{7}{8}$ | 1 | $1 \frac{1}{8}$ | $\frac{1}{4}$ | $1 \frac{3}{8}$ | $1 \frac{1}{2}$ | 2 |

TABLE No. 2.
Roadbed Width in Left Column; half-sum of ratios of Side Slopes at Top; Area of Grade Triangle in body of Table.

| 过 | $\frac{1}{5}$ | $\frac{1}{4}$ | 3 | $\frac{1}{2}$ | $\frac{5}{8}$ | $\frac{3}{4}$ | $\frac{7}{8}$ | 1 | $1 \frac{1}{8}$ | $1 \frac{1}{4}$ | 13 $\frac{3}{8}$ | $1 \frac{1}{2}$ | 2 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | 125 | 100 | 66.7 | 50 | 40.0 | 33.3 | 28.6 | 25 | 22.2 | 20.0 | 18.2 | 16.7 | 12.5 |
| 12 | 180 | 144 | 96.0 | 72 | 57.6 | 48.0 | 41.1 | 36 | 32.0 | 28.8 | 26.2 | 24.0 | 18.0 |
| 14 | 245 | 196 | 130.7 | 98 | 78.4 | 65.3 | 56.0 | 49 | 43.5 | 38.2 | 35.6 | 32.7 | 24.5 |
| 16 | 320 | 256 | 170.7 | 128 | 102.4 | 85.3 | 73.1 | 64 | 56.9 | 51.2 | 46.6 | 42.7 | 32.0 |
| 18 | 405 | 324 | 216.0 | 162 | 129.6 | 108.0 | 92.6 | 81 | 72.0 | 64.8 | 58.9 | 54.0 | 40.5 |
| 20 | 500 | 400 | 266.7 | 200 | 160.0 | 133.3 | 114.3 | 100 | 88.9 | 80.0 | 72.7 | 66.7 | 50.0 |
| 22 | 605 | 484 | 322.7 | 242 | 193.6 | 161.3 | 138.3 | 121 | 107.5 | 96.8 | 88.0 | 80.7 | 60.5 |
| 24 | 720 | 576 | 384.0 | 288 | 230.4 | 192.0 | 164.6 | 144 | 128.0 | II 5.2 | 104.7 | 96.0 | 72.0 |
| 26 | 845 | 676 | 450.7 | 338 | 270.4 | 225.3 | 193.1 | 169 | 150.2 | 135.2 | 122.9 | 112.7 | 84.5 |
| 28 | 980 | 784 | 522.7 | 392 | 313.6 | 261.3 | 224.0 | 196 | 174.2 | 156.8 | 142.6 | 130.7 | 98.0 |
| 30 | 1125 | 900 | 600.0 | 450 | 360.0 | 300.0 | 257.1 | 225 | 200.0 | 180.0 | 163.6 | 150.0 | 112.5 |
|  | $\frac{1}{5}$ | $\frac{1}{4}$ | $\frac{3}{8}$ | $\frac{1}{2}$ | $\frac{5}{8}$ | $\frac{3}{4}$ | $\frac{7}{8}$ | 1 | $1 \frac{1}{8}$ | $1 \frac{1}{4}$ | $1 \frac{3}{8}$ | $1 \frac{1}{2}$ | 2 |

TABLE No. 3.
Arcas in body of Table; Correction Nos., in feet and tenths, in left column and at top.

| $\stackrel{\stackrel{\rightharpoonup}{0}}{\stackrel{y}{\omega}}$ | $\bigcirc$ | . 1 | . 2 | . 3 | . 4 | . 5 | . 6 | . 7 | . 8 | 9 | $\begin{array}{\|c\|} \hline \text { Diff.tor } \\ 0.05 \end{array}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | o | 0.0 | 0.0 | 0.1 | 0.2 | 0.3 | 0.4 | 0.5 | 0.6 | 0.8 | 0.05 |
| 1 | I | 1. 2 | 1.4 | 1. 7 | 2. | 2.3 | 2.6 | 2.9 | 3.2 | 3.6 | 0.2 |
| 2 | 4 | 4.4 | 4.8 | $5 \cdot 3$ | 5.8 | 6.3 | 6.8 | 7.3 | 7.8 | 8.4 | 0.3 |
| 3 | 9 | 9.6 | 10.2 | 10.9 | Ir. 6 | 12.3 | 13. | 13.7 | 14.4 | 15.2 | 0.4 |
| 4 | 16 | 16.8 | 17.6 | 18.5 | 19.4 | 20.3 | 21.2 | 22.1 | 23. | 24. | 0.5 |
| 5 | 25 | 26. | 27. | 28.1 | 29.2 | 30.3 | 31.4 | 32.5 | 33.6 | 34.8 | 0.6 |
| 6 | 36 | 37.2 | 38.4 | 39.7 | 4 t . | 42.3 | 43.6 | 44.9 | 46.2 | 47.6 | . 7 |
| 8 | 49 | 50.4 | 51.8 | 53.3 | 54.8 | 56.3 | 57.8 | 59.3 | 60.8 | 62.4 | 0.8 |
| 8 | 64 | 65.6 | 67.2 | 68.9 | 70.6 | 72.3 | 74. | 75.7 | 77.4 | 79.2 | 0.9 |
| 9 | 81 | 82.8 | 84.6 | 86.5 | 88.4 | 90.3 | 92.2 | 94.1 | 96. | 98. | I. |
| 10 | 100 | 102. | 10. | 106.I | 108.2 | 110.3 | 112.4 | 114.5 | 116.6 | 118.8 | I.I |
| 11 | 121 | 123.2 | 125.4 | 127.7 | 130. | 132.3 | 134.6 | 136.9 | 139.2 | 141.6 | 1.2 |
| 12 | 144 | 146.4 | 148.8 | 151.3 | 153.8 | 156.3 | 158.8 | 161.3 | 163.8 | 166.4 | 1.3 |
| 13 | 169 | 171.6 | 174.2 | 176.9 | 179.6 | 182.3 | 185. | 187.7 | 190.4 | 193.2 | I. 4 |
| 14 | 196 | 198.8 | 201.6 | 204.5 | 207.4 | 210.3 | 213.2 | 216.1 | 219. | 222. | 1. 5 |
| 15 | 225 | 228. | 231. | 234.1 | 237.2 | 240.3 | 243.4 | 246.5 | 249.6 | 252.8 | I. 6 |
| 16 | 256 | 259.2 | 262.4 | 265.7 | 269. | 272.3 | 275.6 | 278.9 | 282.2 | 285.6 | 1.7 |
| 17 | 289 | 292.4 | 295.8 | 299.3 | 302.8 | 306.3 | 309.8 | 313.3 | 316.8 | 320.4 | 1. 8 |
| 18 | 324 | 327.6 | 331.2 | 334.9 | 338.6 | 342.3 | 346. | 349.7 | 353.4 | 357.2 | 1.9 |
| 19 | 361 | 364.8 | 368.6 | 372.5 | 376.4 | 380.3 | 384.2 | 388.1 | 392. | 396. | 2. |
| 20 | 400 | 404. | 408. | 412.1 | 416.2 | 420.3 | 42.4 | 428.5 | 432.6 | 436.8 | 2.1 |
| 21 | 441 | 445.2 | 449.4 | 453.7 | 458. | 462.3 | 466.6 | 470.9 | 475.2 | 479.6 | 2.2 |
| 22 | 48 | 488.4 | 492.8 | 497.3 | 501.8 | 506.3 | 510.8 | 515.3 | 519.8 | 524.4 | 2.3 |
| 23 | 529 | 533.6 | 538.2 | 542.9 | 547.6 | 552.3 | 557. | 561.7 | 566.4 | 571.2 | 2.4 |
| 24 | 576 | 580.8 | 585.6 | 590.5 | 595.4 | 600.3 | 605.2 | 610.1 | 615. | 620. | 2.5 |
| 25 | 625 | 630. | 635. | 640.1 | 645.2 | 650.3 | 655.4 | 660.5 | 665.6 | 670.8 | 2.6 |
| 26 | 676 | 681.2 | 686.4 | 691.7 | 697. | 702.3 | 707.6 | 712.9 | 718.2 | 723.6 | 2.7 |
| 27 | 729 | 734.4 | 739.8 | 745.3 | 750.8 | 756.3 | 761.8 | 767.3 | 772.8 | 778.4 | 2.8 |
| 28 | 784 | 789.6 | 795.2 | 800.9 | 806.6 | 812.3 | 818. | 823.7 | 829.4 | 835.2 | 2.9 |
| 29 | 841 | 846.8 | 852.6 | 858.5 | 864.4 | 870.3 | 876.2 | 882.1 | 888. | 894. | 3.0 |
| 30 | 900 | 906. | 912. | 918.1 | 924.2 | 930.3 | 936.4 | 942.5 | 948.6 | 954.8 | 3.1 |
| 31 | 961 | 967.2 | 973.4 | 979.7 | 986 | 992.3 | 998.6 | 1005 | 1011 | 1018 | 3.2 |
| 32 | 1024 | 1030 | 1037 | 1043 | 1050 | 1056 | 1063 | 1069 | 1076 | 1082 | 3.3 |
| 33 | 1089 | 1096 | 1102 | 1109 | III6 | 1122 | 1129 | 1136 | 1142 | 1149 | 3.5 |
| 34 | 1156 | 1163 | 1170 | 1176 | II83 | 1190 | 1197 | 1204 | 1211 | 1218 | 3.6 |
| 35 | 1225 | 1232 | I239 | 1246 | 1253 | 1260 | 1267 | 1274 | 1282 | 1289 | 3.6 |
| 36 | 1296 | 1303 | 1310 | 1318 | 1325 | 1332 | 1340 | 1347 | 1354 | 1362 | 3.7 |
| 37 | I369 | 1376 | 1384 | 1391 | 1399 | 1406 | 1414 | 1421 | 1429 | 1436 | 3.8 |
| 38 | I 444 | 1452 | 1459 | 1467 | 1475 | 1482 | 1490 | 1498 | 1505 | 1513 | 3.9 |
| 39 | 1521 | 1529 | 1537 | 1544 | 1552 | 1560 | 1568 | 1576 | 158. | 1592 | 4.0 |
| 40 | 1600 | 1608 | I616 | 1624 | 1632 | 1640 | 1648 | 1656 | 1665 | 1673 | 4.1 |
| 41 | 1681 | 1689 | 1697 | 1706 | 1714 | 1722 | 1731 | 1739 | 1747 | 1756 | 4.2 |
| 42 | 1764 | 1772 | 1781 | 1789 | 1798 | 1806 | 1815 | 1823 | 1832 | 1840 | 4.2 |
| 43 | 1849 | 1858 | 1866 | 1875 | 1884 | 1892 | 1901 | I910 | 1918 | 1927 | $4 \cdot 3$ |
| 44 | 1936 | 1945 | 1954 | 1962 | 1971 | 1980 | 1989 | 1998 | 2007 | 2016 | 4.4 |
| 45 | 2025 | 2034 | 2043 | 2052 | 2061 | 2070 | 2079 | 2088 | 2098 | 2107 | 4.5 |
| 46 | 2116 | 2125 | 2134 | 2144 | 2153 | 2162 | 2172 | 2181 | 2190 | 2200 | 4.7 |
| 47 | 2209 | 2218 | 2228 | 2237 | 2247 | 2256 | 2266 | 2275 | 2285 | 2294 | 4.8 |
| 48 | 2304 | 2314 | 2323 | 2333 | 2343 | 2352 | 2362 | 2372 | 2381 | 2391 | 4.8 |
| 49 | 2491 | 2411 | 2421 | 2430 | 2440 | 2450 | 2460 | 2470 | 2480 | 2490 | 5.0 |
| 50 | 2500 | 2510 | 2520 | 2530 | 2540 | 2550 | 2560 | 2570 | 2581 | 2591 | 5.0 |
|  | - | . 1 | 2 | 3 | . 4 | . 5 | . 6 | . 7 | . 8 | . 9 |  |

TABLE No. 3-Concluded.
Areas in bodly of Table; Correction Nos., in fect and tenths, in left column and at top.

|  | 0 | . 1 | . 2 | $\cdot 3$ | . 4 | . 5 | . 6 | . 7 | . 8 | . 9 | $\begin{gathered} \text { Diff.for } \\ 0.05 \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 51 | 2601 | 2611 | 2621 | 2632 | 2642 | 2652 | 2663 | 2673 | 2683 | 2694 | 5.2 |
| 52 | 2704 | 2714 | 2725 | 2735 | 2746 | 2756 | 2767 | 2777 | 2788 | 2798 | 5.2 |
| 53 | 2809 | 2820 | 2830 | 2541 | 2852 | 2862 | 2873 | 2884 | 2894 | 2905 | 5.3 |
| 54 | 2916 | 2927 | 2938 | 2948 | 2959 | 2970 | 2981 | 2992 | 3003 | 3014 | 5.4 |
| 55 | 3025 | 3036 | 3047 | 3053 | 3069 | 3080 | 3091 | 3102 | 3114 | 3125 | 5.5 |
| 56 | 3136 | 3147 | 3158 | 3170 | 3181 | 3192 | 3204 | 3215 | 3226 | 3238 | 5.7 |
| 57 | 3249 | 3260 | 3272 | 3283 | 3295 | 3306 | 3318 | 3329 | 3341 | 3352 | 5.7 |
| 58 | 3364 | 3376 | 3387 | 3399 | $3+11$ | 3422 | $343+$ | 3446 | 3457 | 3469 | 5.8 |
| 59 | 3481 | 3493 | 3505 | 3516 | 3528 | 3540 | 3552 | 3564 | 3576 | 3583 | 5.9 |
| 60 | 3600 | 3612 | 3624 | 3636 | 3648 | 3660 | 3672 | 3684 | 3697 | 3709 | 6.0 |
| 61 | 3721 | 3733 | 3745 | 3753 | 3770 | 3752 | 3795 | 3507 | $3 \mathrm{SI9}$ | 3832 | 6.2 |
| 62 | $384+$ | 3856 | 3869 | 3851 | 3 S 94 | 3906 | 3919 | 3931 | 3944 | 3956 | 6.2 |
| 63 | 3969 | 3982 | 3994 | 4007 | 4020 | 4032 | 4045 | 4058 | 4070 | 4083 | 6.3 |
| 64 | 4096 | 4109 | 4122 | 4134 | 4147 | 4160 | 4173 | 4186 | 4199 | 4212 | 6.4 |
| 65 | 4225 | 4238 | 4251 | 4264 | 4277 | 4290 | 4303 | 4316 | 4330 | 4343 | 6.5 |
| 66 | 4356 | 4369 | 4382 | 4396 | 4409 | 4122 | 4436 | $4+49$ | 4462 | 4476 | 6.7 |
| 67 | 4489 | 4502 | 4516 | 4529 | 4543 | 4556 | 4570 | 4583 | 4597 | 4610 | 6.7 |
| 68 | 4624 | 4638 | 4651 | 4665 | 4679 | 4692 | 4706 | 4720 | 4733 | 4747 | 6.8 |
| 69 | 4761 | 4775 | 4789 | 4802 | 4316 | 4830 | $484+$ | 4858 | 4872 | 4886 | 6.9 |
| 70 | 4900 | 4914 | 4928 | 4942 | 4956 | 4970 | 4984 | 4998 | 5013 | 5027 | 7.0 |
| 7 I | 50+1 | 5055 | 5069 | 5084 | 5098 | 5112 | 5127 | 5141 | 5155 | 5170 | 7.2 |
| 72 | 5184 | 5198 | 5213 | 5227 | 5242 | 5256 | 5271 | 5285 | 5300 | 5314 | 7.2 |
| 73 | 5329 | 5344 | 5358 | 5373 | 5385 | 5402 | 5417 | 5432 | 5446 | 5461 | 7.3 |
| 74 | 5476 | 5491 | 5506 | 5520 | 5535 | 5550 | 5565 | 5580 | 5595 | 5610 | 7.4 |
| 75 | 5625 | 5640 | 5655 | 5670 | 5685 | 5700 | 5715 | 5730 | 5746 | 5761 | 7.5 |
| 76 | 5776 | 5791 | 5806 | 5822 | 5837 | 5852 | 5868 | 5883 | 5 S 93 | 5914 | 7.7 |
| 77 | 5929 | $59+4$ | 5960 | 5975 | 5991 | 6006 | 6022 | 6037 | 6053 | 6068 | 7.7 |
| 78 | 60S 4 | 6100 | 6115 | 6131 | $6{ }_{6} 47$ | 6162 | 6178 | 6194 | 6209 | 6225 | 7.8 |
| 79 | 624 I 6400 | 6257 6156 | 6273 | 6288 | 6304 | 6320 | 6336 | 6352 | 6368 | 6384 | 7.9 |
| 80 | 6400 6561 | $6+16$ 6577 | $6+32$ 6593 | $6+43$ 6510 | 6464 6626 | 6480 6642 | 6496 6659 | 6512 6675 | 6529 6691 | 6545 6708 | 8.0 |
| 82 | $672+$ | 6740 | 6757 | 6773 | 6790 | 6806 | 6823 | 6839 | 6856 | 6872 | 8.2 |
| 83 | 6889 | 6906 | 6922 | 6939 | 6956 | 6972 | 6989 | 7006 | 7022 | 7039 | 8.3 |
| 84 | 7056 | 7073 | 7090 | 7106 | 7123 | 7140 | 7157 | 7174 | 7191 | 7208 | 8.4 |
| 85 | 7225 | 7242 | 7259 | 7276 | 7293 | 7310 | 7327 | 7344 | 7362 | 7379 | 8.5 |
| 86 | 7396 | 7413 | $7+30$ | $7+48$ | $7+65$ | 7482 | 7500 | 7517 | 7534 | 7552 | 8.6 |
| 87 | 7569 | 7586 | $750+$ | 7621 | 7639 | 7656 | 7674 | 7691 | 7709 | 7726 | 8.7 |
| 88 | 77+4 | 7762 | 7779 | 7797 | 7815 | 7832 | 7850 | 7868 | 7885 | 7903 | 8.8 |
| 89 | 7921 | 7939 | 7957 | 7974 | 7992 | 8010 | So28 | $80+6$ | 8064 | 8082 | 8.9 |
| 90 | SIOO | 8113 | 8 L 36 | 8154 | 8172 | 8190 | 8208 | 8226 | 8245 | 8263 | 9.0 |
| 91 | 8231 | 8299 | 8317 | 8336 | 8354 | 8372 | 8391 | 8409 | 8427 | 8446 | 9.2 |
| 92 | $8+6$ | 8452 | 8501 | 8519 | 8538 | 8556 | 8575 | 8593 | 8612 | 8630 | 9.2 |
| ¢3 | 8649 | 8568 | 8686 | 8705 | 8724 | 8742 | 8761 | 8780 | 8798 | 8317 | 9.3 |
| 94 | 8836 | 8555 | 8874 | 8892 | 8911 | 8930 | 8949 | 8968 | 8987 | 9006 | 9.4 |
| 95 | 9025 | $90+4$ | 9063 | 9082 | 9101 | 9120 | 9139 | 9158 | 9178 | 9197 | 9.5 |
| 96 | 9216 | 9235 | 9254 | 9274 | 9293 | 9312 | 9332 | 9351 | 9370 | $939{ }^{\circ}$ | 9.6 |
| 97 | 9409 | 9428 | 9445 | 9467 | 9487 | 9506 | 9526 | 9545 | 9565 | 9584 | 9.7 |
| 98 | 9604 | 9624 | 9643 | 9663 | 9683 | 9702 | 9722 | 9742 | 9761 | 9781 | 9.8 |
| 99 | ${ }^{\text {9301 }}$ | 9821 | ${ }^{9} 4 \times 1$ | 9860 | 9880 | 9900 | 9920 | 9940 | 9960 | 9980 | 9.9 |
| 100 | 000 | 10020 | 10040 | 10060 | 10030 | 10100 | 10120 | IOI40 | 10161 | 10181 | 10.0 |
|  | - | . 1 | . 2 | . 3 | . 4 | . 5 | . 6 | . 7 | . 8 | . 9 |  |

TABLE No. 4.

| Areas... | 0.1 | 0.2 | 0.2 | 0.3 | 0.4 | 0.5 | 0.6 | 0.7 | 0.75 | 0.8 | 0.9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Contents............. | 0.4 | 0.7 | 0.9 | I.I | 15 | 1.9 | 22 | 2.6 | 2.8 | 30 | 3.3 | Areas: Tens in left Column and Units at top, Contents for 100 feet in cubic yards in body of Table.


| $\stackrel{\text { ® }}{ \pm}$ | 0.0 | 1.0 | 2.0 | 3.0 | 4.0 | 5.0 | 6.0 | 7.0 | 8.0 | 9.0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0.0 | 3.7 | 7.4 | 11.1 | 14.8 | 18.5 | 22.2 | 25.9 | 29.6 | 33.3 |
| 1 | 37. | 40.7 | 44.4 | 48.1 | 51.9 | 55.6 | 59.3 | 63. | 66.7 | 70.4 |
| 2 | 74.1 | 77.8 | 81.5 | 85.2 | 88.9 | 92.6 | 96.3 | 100. | 103.7 | 107.4 |
| 3 | 11.1 | 114.8 | 118.5 | 122.2 | 125.9 | 129.6 | 133.3 | 137. | 140.7 | 144.4 |
| 4 | 148.1 | 151.9 | 155.6 | 159.3 | 163. | 166.7 | 170.4 | 174.1 | 177.8 | 181.5 |
| 5 | 185.2 | 188.9 | 192.6 | 196.3 | 200. | 203.7 | 207.4 | 211.1 | 214.8 | 218.5 |
| 6 | 222.2 | 225.9 | 229.6 | 233.3 | 237. | 240.7 | 244.4 | 248.1 | 251.9 | 25.6 |
| 7 | 259.3 | 263. | 266.7 | 270.4 | 274.1 | 277.8 | 281.5 | 285.2 | 288.9 | 292.6 |
| 3 | 296.3 | 300. | 303.7 | 307.4 | I.I | 314 | 318.5 | 322 | 325.9 | 329.6 |
| 9 | 333.3 | 337. | 340.7 | 344.4 | 348.1 | 351.9 | 355.6 | 359.3 | 363. | 366.7 |
| 10 | 370.4 | 374. I | 377.8 | 381.5 | 385.2 | 388.9 | 392.6 | 396.3 | 400. | 403.7 |
| 11 | 407.4 | 411.1 | 414 | 418.5 | 422.2 | 425.9 | 429.6 | 433.3 | 437. | 440.7 |
| 12 | 444.4 | 448.1 | 451.9 | 455.6 | 459.3 | 463. | 466.7 | 470.4 | 474.1 | 477.8 |
| ${ }^{1}$ | 48 I .5 | 485.2 | 488.9 | 492.6 | 496.3 | 500. | 503.7 | 507.4 | 51 II .1 | 514.8 |
| 14 | 518.5 | 522.2 | 525.9 | 529.6 | 533.3 | 537 | 540.7 | 544.4 | 548.1 | 551.9 |
| 15 | 555.6 | 559.3 | 563. | 566.7 | 570.4 | 574.1 | 577.8 | 58 I .5 | 585.2 | 588.9 |
| 16 | 592.6 | 596.3 | 600. | 603.7 | 607.4 | 61 I .1 | 614.8 | 618.5 | 622.2 | 625.9 |
| 17 | 629.6 | 633.3 | 637. | 640.7 | 644.4 | 648.1 | 651.9 | 655.6 | 659.3 | 663. |
| 18 | 666:7 | 670.4 | 674.1 | 677.8 | 681.5 | 685.2 | 688.9 | 692.6 | 696.3 | 700. |
| 19 | 703.7 | 707.4 | 711.1 | 714.8 | 718.5 | 722.2 | 725.9 | 729.6 | 733.3 | 737. |
| - | 740.7 | 744.4 | 748.1 | 751.9 | 755.6 | 759.3 | 763. | 766.7 | 770.4 | 774.I |
| 21 | 777.8 | 781.5 | 785.2 | 788.9 | 792.6 | 796.3 | 800. | 803.7 | 807.4 | 8 II .1 |
| 22 | 814.8 | 818.5 | 822.2 | 825.9 | 829.6 | 833.3 | 837. | 840.7 | 844.4 | 848.1 |
| 23 | 851.9 | 855.6 | 859.3 | 863. | 866.7 | 870.4 | 874.I | 877.8 | 881.5 | 885.2 |
| 24 | 888.9 | 892.6 | 896.3 | 900. | 903.7 | 907.4 | 9 II.I | 914.8 | 918.5 | 922.2 |
| 25 | 925.9 | 929.6 | 933.3 | 937. | 940.7 | 944.4 | 948.1 | 951.9 | 955.6 | 959.3 |
| 26 | 963. | 966.7 | 970.4 | 974.1 | 977.8 | 981.5 | 985.2 | 988.9 | 992.6 | 996.3 |
| 27 | 1000. | 1003.7 | 1007.4 | IOII. 1 | 1014.8 | Ior8.5 | 1022.2 | 1025.9 | 1029.6 | 1033.3 |
| 28 | 1037. | 1040.7 | $1044 \cdot 4$ | 1048.I | 1051.9 | 1055.6 | 1059.3 | 1063. | 1066.7 | 1070.4 |
| 29 | 1074. 1 | 1077.8 | 108I. 5 | 1085.2 | 1088.9 | 1092.6 | 1096.3 | 1100 | 1103.7 | 1107.4 |
| 30 | 1111.1 | III4.8 | 1118.5 | I122.2 | 1125.9 | 1129.6 | 1133.3 | 1137. | 1140.7 | 1144.4 |
| 31 | 1148.1 | 1151.9 | 1155.6 | 1159.3 | 1163. | 1166.7 | 1170.4 | 1174.1 | 1177.8 | 1181.5 |
| 32 | 1185.2 | 1188.9 | 1192.6 | 1196.3 | 1200. | 1203.7 | 1207.4 | 1211.1 | 1214.8 | 1218.5 |
| 33 | 1222. | 1225.9 | 1229.6 | 1233.3 | 1237. | 1240.7 | 1244.4 | 1248.1 | 1251.9 | 1255.6 |
| 34 | 1259.3 | 1263. | 1266.7 | 1270.4 | 1274.1 | 1277.8 | 1281.5 | 1285.2 | 1288.9 | 1292.6 |
| 35 | 1296.3 | 1300. | 1303.7 | 1307.4 | I3II.1 | 1314.8 | 1318.5 | 1322.2 | 1325.9 | 1329.6 |
| 36 | 1333.3 | 1337. | 1340.7 | 13 | 1348.1 | 1351.9 | I 355.6 | 1359.3 | 1363. | 1366.7 |
| 37 | 1370.4 | 1374.I | 1377.8 | 1381.5 | 1385.2 | 1388.9 | 1392.6 | I 396.3 | 1400. | 1403.7 |
| 38 | 1407.4 | 1411.1 | 1414.8 | 1418.5 | 1422.2 | 1425.9 | 1429.6 | $1433 \cdot 3$ | 1437. | 1440.7 |
| 39 | 1444.4 | 1448.1 | 1451.9 | 1455.6 | 1459.3 | 1463. | 1466.7 | 1470.4 | 1474.I | 1477.8 |
| 40 | 1481.5 | 1485.2 | 1488.9 | 1492.6 | 1496.3 | 1500. | 1503.7 | 1507.4 | 1511 | 1514.8 |
| 41 | 1518.5 | 1522.2 | 1525.9 | 1529.6 | 1533.3 | 1537. | 1540.7 | 1544.4 | 1548.1 | 1551.9 |
| 42 | 1555.6 | 1559.3 | 1563. | 1566.7 | 1570.4 | 1574.1 | 1577.8 | 1581.5 | 1585.2 | 1588.9 |
| 43 | 1592.6 | 1596.3 | 1600. | 1603.7 | 1607.4 | 1611.1 | 1614.8 | 1618.5 | 1622.2 | 1625.9 |
| 44 | 1629.6 | 1633.3 | 1637. | 1640.7 | 1644.4 | 1648.I | 1651.9 | 1655.6 | 1659.3 | 1663. |
| 45 | 1666.7 | 1670.4 | 1674.1 | 1677.8 | 1681. 5 | 1685.2 | 1688.9 | 1692.6 | 1696.3 | 1700. |
| 46 | 1703.7 | 1707.4 | 1711.1 | 1714.8 | 1718.5 | 1722.2 | 1725.9 | 1729.6 | 1733.3 | 1737. |
| 47 | 1740.7 | 1744.4 | 1748.1 | 1751.9 | 1755.6 | 1759.3 | 1763. | 1766.7 | ${ }^{1} 770.4$ | 1774.1 |
| 48 | 1777.8 | 1781.5 | 1785.2 | 1788.9 | 1792.6 | 1796.3 | 1800. | 18037 | 1807.4 | 1811.1 |
| 49 | 1814.8 | 1818.5 | 1822.2 | 1825.9 | 1829.6 | 1833.3 | 1837. | 1840.7 | 1844.4 | 1848.1 |
| 50 | 1851.9 | 1855.6 | 1859.3 | 1863. | 1866.7 | 1870.4 | 1874. 1 | 1877.8 | 1881. 5 | 1885.2 |
|  | 0. | 1. | 2. | 3. | 4. | 5. | 6. | 7. | 8. | 9. |

TABLE Ňo. 4-Continued.

| Areas. ....................... | 0.1 | 0.2 | 0.25 | 0.3 | 0.4 | 0.5 | 0.6 | 0.7 | 0.75 | 0.8 | 0.9 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Contents................ | 0.4 | 0.7 | 0.9 | 1.1 | 1.5 | 1.9 | 2.2 | 2.6 | 2.8 | 3.0 | 3.3 |

Areas: Tens in left Column and Units at top. Contents for 100 feet in cubic yards in body of Table.

|  | 0. | 1. | 2. | 3. | 4. | 5. | 6. | 7. | 8. | 9. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 51 | 1888.9 | 1892.6 | 1896.3 | 1900. | 1903.7 | 1907.4 |  | 1914.8 | 1918.5 | 1922.2 |
| 52 | 1925.9 | 1929.6 | 1933.3 | 1937. | 1940.7 | 1944.4 | 1948.1 | 1951.9 | 1955.6 | 1959.3 |
| 53 | 1963. | 1966.7 | 1970.4 | 1974.1 | 1977.8 | 1981.5 | 1985.2 | 1988.9 | 1992.6 | 1996.3 |
| 54 | 2000. | 2003.7 | 2007.4 | 201 I. | 2014.8 | 2018.5 | 2022.2 | 2025.9 | 2029.6 | 2033.3 |
| 55 | 2037. | 2040.7 | 2044.4 | 2048.1 | 2051.9 | 2055.6 | 2059.3 | 2063. | 2066.7 | 2070.4 |
| 56 | 2074.I | 2077.8 | 2081.5 | 2085.2 | 2088.9 | 2092.6 | 2096.3 | 2100. | 2103.7 | 2107.4 |
| 57 | 2111.1 | 2114.8 | 2118 | 2122.2 | 2125.9 | 2129.6 | 2133.3 | 2137. | 2140.7 | 2144.4 |
| 58 | 2148.1 | 2151.9 | 2155.6 | 2159.3 | 2163. | 2166.7 | 2170.4 | 2174.1 | 2177.8 | 2181.5 |
| 59 | 2185.2 | 2188.9 | 2192.6 | 2196.3 | 2200. | 2203.7 | 2207.4 | 22II. | 2214.8 | 2218.5 |
| 60 | 22 | 2225.9 | 2229.6 | 2233.3 | 2237. | 2240.7 | 2244.4 | 2248.1 | 2251.9 | 2255.6 |
| 61 | 2259.3 | 2263. | 2266.7 | 2270.4 | 2274.r. | 2277.8 | 2281.5 | 2285.2 |  | 2292.6 |
| 62 | 2296.3 | 2300. | 2303.7 | 2307.4 | 2311.1 | 2314.8 | 2318.5 | 2322.2 | 2325.9 | 2329.6 |
| 63 | 2333.3 | 2337. | 2340.7 | 2344.4 | 2348.1 | 2351.9 | 2355.6 | 2359.3 | 2363. | . 7 |
| 64 | 2370.4 | 2374.1 | 2377.8 | 2381.5 | 2385.2 | 2388.9 | 2392.6 | 2396.3 | 2400 | 2403.7 |
| 65 | 2407.4 | 2411.1 | 2414.8 | 2418.5 | 2422.2 | 2425. | 2429.6 | 2433.3 | 2437. | 2440.7 |
| 66 | 2444.4 | $2+48.1$ | 2451.9 | 2455.6 | 2459 | 2463. | 2466.7 | 2470.4 | 2474 | 2477.8 |
| 67 | 2481.5 | 2485.2 | 2483.9 | 2492.6 | 2496.3 | 2500. | 2503.7 | 2507.4 | 2511 | 2514.8 |
| 68 | 2518.5 | 2522.2 | 2525.9 | 2529.6 | 2533.3 | 2537. | 2540.7 | 2544.4 | 2548.1 | 2551.9 |
| 69 | 2555 | 2559.3 | 2563. | 2566.7 | 2570.4 | 2574. I | 2577.8 | 25 SI. 5 | 2585.2 | 2588.9 |
| 70 | 2592.6 | 2596.3 | 2600. | 2603.7 | 2607.4 | 2611.I | 2614.8 | 2618.5 | 2622.2 | 2625.9 |
| 71 | 2629.6 | 2633.3 | 2637. | 2640.7 | 2644.4 | 2648.1 | 2651.9 | 2655.6 | 2659.3 | 2663. |
| 72 | 2666.7 | 2670.4 | $2674 . \mathrm{I}$ | 2677.8 | 2681.5 | 2685.2 | 2688.9 | 2692.6 | 2696.3 | 2700. |
| 73 | 2703.7 | 2707.4 | 2711.1 | 2714.8 | 2718.5 | 2722.2 | 2725.9 | 2729.6 | 2733.3 | 2737. |
| 74 | 2740.7 | 2744.4 | 2748.1 | 2751.9 | 2755.6 | 2759.3 | 2763. | 2766.7 | 2770.4 | 2774.I |
| 75 | 2777.8 | 2781.5 | 2785.2 | 2788.9 | 2792.6 | 2796.3 | 2800. | 2803.7 | 2807.4 | 28 II.I |
| 76 | 2814.8 | 2818.5 | 2822.2 | 2825.9 | 2829.6 | 2833.3 | 2837. | 2840.7 | $284+4$ | 2848.1 |
| 77 | 2851.9 | 2855.6 | 2859.3 | 2863. | 2866.7 | 2870.4 | 2874.1 | 2877.8 | 2881.5 | 2885.2 |
| 78 | 2588.9 | 2892.6 | 2896.3 | 2900. | 2903.7 | 2907.4 | 2911.1 | 2914.8 | 2918.5 | 2922.2 |
| 79 | 2925.9 | 2929.6 | 2933.3 | 2937. | 2940.7 | 2944.4 | 2948.1 | 2951.9 | 2955.6 | 2959.3 |
| 80 | 2963. | 2966.7 | 2970.4 | 2974. 1 | 2977.8 | 2981.5 | 2985.2 | 2988.9 | 2992.6 | 2996.3 |
| 8 I | 3000. | 3003.7 | 3007.4 | 3011. | 3014.8 | 3018.5 | 3022.2 | 3025.9 | 3029.6 | $3033 \cdot 3$ |
| 82 | 3037. | 3040.7 | 3044.4 | 3048.1 | 3051.9 | 3055.6 | 3059.3 | 3063. | 3066.7 | 3070.4 |
| 83 | 3074.1 | 3077.8 | 3081. 5 | 3085.2 | 3088.9 | 3092.6 | 3096.3 | 3100. | 3103.7 | 3107.4 |
| 84 | 3111. | 3114.8 | 3118.5 | 31 | 3125.9 | 3129.6 | 3133.3 | 3137 | 3140.7 | 3144.4 |
| 85 | 3I48.I | 31519 | 3155.6 | 3159.3 | 3163. | 3166.7 | 3170.4 | 3174.1 | 3177 | 3181.5 |
| 86 | 3185.2 | 3188.9 | 3192.6 | 3196.3 | 3200 | 3203.7 | 3207.4 | 3211 | 3214 | 3218.5 |
| 87 | 32 | 3225.9 | 3229.6 | 3233.3 | 3237. | 3240.7 | 3244.4 | 3248 | 3251.9 | 3255.6 |
| 88 | 3259.3 | 3263. | 3266.7 | 3270.4 | 3274.I | 3277 | 3281.5 | 3285 | 3288.9 | 3292.6 |
| 89 | 3296.3 | 330 | 3303.7 | $3307 \cdot 4$ | 3311 | 3314 | 3318 | 3322 | 3325.9 | 3329.6 |
| 90 | 3333.3 | 3337. | 3340.7 | $33+4.4$ | 3348. | 3351.9 | 3355.6 | 3359.3 | 3363. | 3366.7 |
| 91 | 3370.4 | 3374.I | 3377.8 | 3381.5 | 3385 | 3388.9 | 3392.6 | 3396.3 | 3400. | 3403.7 |
| 92 | 3407.4 | 341 I . | 3414.8 | 34 | 34 | 3425. | 3429.6 | 3433.3 | 3437 | 3440.7 |
| 93 | 3444 | 3448. | 3+51.9 | 345 | 3459.3 | 3463. | 34667 | 3470. | 3474. | 3477.8 |
| 94 | 3481.5 | 3485 | 3488.9 | 349 | 3496.3 | 3500. | 3503.7 | 3507.4 | 351 I. 1 | 3514.8 |
| 95 | 3518.5 | 35 | 3525.9 | 3529.6 | 3533.3 | 3537. | 3540.7 | 3514.4 | 3548.1 | 3551.9 |
| 96 | 3355.6 | 35 | 3563. | 3566.7 | 3570.4 | 3574.I | 3577.8 | 3581.5 | 3585.2 | 3588.9 |
| 97 | 3592.6 | 3596.3 | 3600. | 3603.7 | 3607.4 | 3611.1 | 3614.8 | 3618.5 3655 | 3622.2 3659.3 | 63.9 |
| 98 | 3629.6 | 3633.3 | 3637. | 3640.7 | 3644.4 | 3648.1 | 3651.9 | 3655.6 36926 |  |  |
| 99 | 3666.7 3703.7 | 3670.4 3707.4 | 3674.1 3711.1 | 3677.8 37 T .8 | 3681.5 3718.5 | 3635.2 3722.2 | 3685.9 3725.9 | 3692.6 3729.6 | 3696.3 $3733 \cdot 3$ | 3700. 3737. |
|  | o. | 1. | 2. | 3. | 4. | 5. | 6. | 7. | 8. | 9. |

TABLE No. 4-Continued.

| A | 0.1 | 0.2 | 0.25 | 0.3 | 0.4 | 0.5 | 0.6 | 0.7 | 0.75 | 0.8 | 0.9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Contents | 0.4 | 0.7 | 0.9 | 1.1 | 1.5 | 1.9 | 22 | 2.6 | 2.8 | 3.0 | 3.3 | Areas: Tens in left Column and Units at top. Contents for 100 feet in cubic yards in body of Table.


| 岕 | 0. | 1. | 2. | 3. | 4. | 5. | 6. | 7. | 8. | 9. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 374 |  | 3755.6 | 3759.3 | 3763. | 3766.7 | 3770.4 |  |
| 102 | 3777 | 3781.5 | 3785.2 | 3788.9 | 3792.6 | 3796.3 | 3800. | 3803.7 | 3807.4 | 38II.I |
| 103 | 38 t 4 | 3818 | 3822.2 | 3825.9 | 3829.6 | $3833 \cdot 3$ | 3837. | 3840.7 | 3844.4 | 3848.1 |
| 104 | 3851.9 | 3855.6 | 3859.3 | 3863. | 3866.7 | 3870.4 | 3874.I | 3877.8 | 3881.5 | 3885.2 |
| 105 | 3888.9 | 3892.6 | 3896.3 | 3900. | 3903.7 | 3907.4 | 39 II .1 | 3914.8 | 3918.5 | 3922.2 |
| 106 | 3925.9 | 3929.6 | 3933.3 | 3937. | 3940.7 | 3944.4 | 3948.1 | 3951.9 | 3955.6 | 3959.3 |
| 107 | 3963. | 3966.7 | 3970.4 | 3974.I | 3977.8 | 3981.5 | 3985.2 | 3988.9 | 3992.6 | 3996.3 |
| 108 | 4000. | 4003.7 | 4007.4 | 4011.1 | 4014.8 | 4018.5 | 4022.2 | 4025.9 | 4029.6 | 4033.3 |
| 109 | 4037. | 4040.7 | 4044.4 | 4048.1 | 4051.9 | 4055.6 | 4059.3 | 4063. | 4066.7 | 4070.4 |
| I 10 | 4074.I | 4077.8 | 408 I .5 | 4085.2 | 4088.9 | 4092.6 | 4096.3 | 4100. | 4103.7 | $4107 \cdot 4$ |
| III | 4111.1 | 4114.8 | 4118.5 | 4122.2 | 4125.9 | 4129.6 | 4133.3 | 4137. | 4140.7 | 4144.4 |
| 112 | 4148.1 | 4151.9 | 4155.6 | 4159.3 | 4163. | 4166.7 | 4170.4 | 4174.1 | 4177.8 | 4181.5 |
| 113 | 4185.2 | 4188.9 | 4192.6 | 4196.3 | 4200. | 4203.7 | 4207.4 | 4211.1 | 4214.8 | 4218.5 |
| 114 | 4222.2 | 4225.9 | 4229.6 | 4233.3 | 4237. | 4240.7 | 4244.4 | 4248.1 | 4251.9 | 4255.6 |
| 115 | 4259.3 | 4263. | 4266.7 | 4270.4 | $4274 . \mathrm{I}$ | 4277.8 | 4281.5 | 4285.2 | 4288.9 | 4292.6 |
|  | 4296.3 | 4300. | 4303.7 | 4307.4 | 43 II. 1 | 4314.8 | 4318 | 4322.2 | 4325.9 | 4329.6 |
| 117 | $4333 \cdot 3$ | 4337. | 4340.7 | 4344.4 | 4348.1 | 4351.9 | 4355 | 4359.3 | 4363. | 4366.7 |
| 118 | 4370.4 | $4374 . \mathrm{I}$ | 4377.8 | 4381.5 | 4385.2 | 4388.9 | 4392 | 4396.3 | 4400. | 4403.7 |
| 119 | 4407.4 | 44 II. I | 4414.8 | 4418 | 4422.2 | 4425.9 | 4429 | $4433 \cdot 3$ | 4437. | 4440.7 |
| 120 | 4444.4 | 4448.1 | 4451.9 | 4455 | 44 | 4463. | 4466.7 | 4470.4 | 4474.1 | 4477.8 |
| 121 | 448 I .5 | 4485.2 | 4488.9 | 44 | 4496.3 | 4500. | 4503.7 | $4507 \cdot 4$ | 45 II. 1 | 4514.8 |
| 122 | 4518.5 | 4522.2 | 4525.9 | 45 | $4533 \cdot 3$ | 4537. | 4540 | 45 | 4548.1 | 4551.9 |
| 123 | 4555.6 | 4559 | 4563. |  | 4570.4 | 4574 | 4577.8 | 4581.5 | 4585.2 |  |
| 124 | 459 | 4596.3 | 4600. | 4603.7 | 4607.4 | 4611.1 | 4614.8 | 4618.5 | 4622.2 | 4625.9 |
| 125 | 4629. | 4633.3 | 4637. | 4640.7 | 4644.4 | 4648.I | 4651.9 | 4655.6 | 4659.3 | 4663. |
| 125 | 4666.7 | 4670.4 |  | 4677 | 4681.5 | 5. | 4688.9 | 4692.6 |  | 4700. |
| 127 | 4703.7 | 4707.4 | 4711.1 | 4714 | 4718.5 | 4722.2 | 4725.9 | 4729.6 | 4733.3 | 47 |
| 128 | 4740.7 | 4744.4 | 4748 | 4751 | 4755 | 4759.3 | 4763. | 4766.7 | 4770.4 | 4774.1 |
| 129 | 4777.8 | 4781.5 | 4785.2 | 4788.9 | 4792.6 | 4796.3 | 4800. | 4803.7 | 4807.4 | 4811.1 |
| 130 | 48 I4.8 | 4818.5 | 4822.2 | 4825.9 | 4829.6 | 4833.3 | 4837. | 4840.7 | 4844.4 | 4848.1 |
| 131 | 4851. | 4855.6 | 4859.3 | 4863. | 4866.7 | 4870.4 | 4874.I | 4877.8 | 488 I .5 | 4885.2 |
| 132 | 4888.9 | 4892.6 | 4896.3 | 4900. | 4903.7 | $4907 \cdot 4$ | 49II.I | 4914.8 | 4918.5 | 4922.2 |
| 133 | 4925.9 | 4929.6 | $4933 \cdot 3$ | 4937. | 4940.7 | 4944.4 | 4948.1 | 4951.9 | 4955.6 | 4959.3 |
| 134 | 4963. | 4966.7 | 4970.4 | 4974 | 4977.8 | 4981.5 | 4985.2 | 4988.9 | 4992.6 | 4996.3 |
| 135 | 5000. | 5003.7 | 5007.4 | 5011. | 5014.8 | 5018.5 | 5022.2 | 5025.9 | 5029.6 | 5033.3 |
| 136 | 5037. | 5040.7 | 5044.4 | 5048.1 | 5051.9 | 5055.6 | 5059.3 | 5063. | 5066.7 | 5070.4 |
| 137 | 5074. | 5077.8 | 508 I .5 | 5085.2 | 5088.9 | 5092.6 | 5096.3 | 5100. | 5103.7 | 5107.4 |
| 138 | 5111.1 | 5114.8 | 5118.5 | 5122.2 | 5125.9 | 5129.6 | 5133.3 | 5137. | 5140.7 | 5144.4 |
| 13 | 5148.1 | 5151.9 | 5155.6 | 5159.3 | 5163. | 5166.7 | 5170.4 | 5174.1 | 5177.8 | 5181.5 |
| 14 | 5185.2 | 5188.9 | 5192.6 | 5196.3 | 5200. | 5203.7 | 5207.4 | 5211.1 | 5214.8 | 5218.5 |
| 14 | 5222.2 | 5225.9 | 5229.6 | 5233.3 | 5237. | 5240.7 | 5244.4 | 5248.1 | 5251.9 | 5255.6 |
| 14 | 5259.3 | 5263. | 5266.7 | 5270.4 | 5274.1 | 5277.8 | 5281.5 | 5285.2 | 5288.9 | 5292.6 |
| 143 | 5296.3 | 5300. | 5303.7 | 5307.4 | 5311.1 | 5314.8 | 5318.5 | 5322.2 | 5325.9 | 5329.6 |
| 144 | 5333.3 | 5337. | 5340.7 | 5344.4 | 5348.1 | 5351.9 | 5355.6 | $5359 \cdot 3$ | 5363. | 5366.7 |
| 145 | 5370.4 | 5374.1 | 5377.8 | 538 I .5 | 5385.2 | 5388.9 | 5392.6 | 5396.3 | 5400. | 5403.7 |
| 146 | 5407.4 | $54 \mathrm{II.I}$ | 5414.8 | 5418.5 | 5422.2 | 5425.9 | 5429.6 | 5433.3 | 5437. | 5440.7 |
| 147 | 5444.4 | 5448.1 | 5451.9 | 5455.6 | 5459.3 | 5463. | 5466.7 | 5470.4 | 5474.I | 5477.8 |
| 148 | 5481.5 | 5485.2 | 5488.9 | 549 | 5496.3 | 5500. | 5503.7 | 5507.4 | 5511 | 5514.8 |
| 149 | 5518.5 | 5522.2 | 5525.9 | 5529.6 | 5533.3 | 5537. | 5540.7 | 5544.4 | 5548.1 | 5551.9 |
| 150 | 5555.6 | 5559.3 | 5563. | 5566.7 | 5570.4 | 5574 | 5577.8 | 5581.5 | 5585.2 | 5588 |
|  | 0. | 1. | 2. | 3. | 4. | 5. | $\sigma$. | 7. | 8. | 9. |

TABLE No. 4-Continted.

| Area | 0.1 | 0.2 | 0.25 | $\bigcirc 3$ | 0.4 | 0.5 | 0.6 | 0.7 | 0.75 | 0.8 | 0.9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Contents. | 0.4 | 7 | 0.9 | 1.1 | 15 | 1.9 | 22 | 2.6 | 2.8 | 30 | 3.3 |

Areas: Tens in left Column and Units at top. Contents for 100 fect in cubic yards in body of Table.

| $\stackrel{\dot{0}}{\text { ¢ }}$ | 0. | 1. | 2. | 3. | 4. | 5. | 6. | 7. | 8. | 9. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 5596.3 | 5600. | 5603.7 | 5607.4 | 5611.1 | 5614.8. | 5618.5 | 5622.2 |  |
| 152 | 5629. | 5633.3 | 5637. | 56 | 56 | 5648.1 | 5651.9 | 5655.6 | 5659.3 |  |
| 153 | 5666.7 | 5670.4 | 5674.I | 5677.8 | 5681.5 | 5685.2 | 5688.9 | 5692.6 | 5696.3 | 5700. |
| 154 | 5703.7 | 5707.4 | 5711.1 | 5714.8 | 5718.5 | 5722.2 | 5725.9 | 5729.6 | 5733.3 | 5737. |
| 155 | 5740.7 | 5744.4 | 5748.1 | 5751.9 | 5755.6 | 5759.3 | 5763. | 5766.7 | 5770.4 | 5774. |
| 156 | 5777.8 | 5781.5 | 5785.2 | 5788.9 | 5792.6 |  | 5800. | 5803.7 | 5807.4 | 5811.1 |
| 157 | 5814.8 | 5818.5 | 5822.2 | 5825.9 | 5829.6 | 5833.3 | 5837. | 5840.7 | 5844.4 | 5848.1 |
| 158 | 5851.9 | 5855.6 | 5859.3 | 5863. | 5866.7 | 5870.4 | 5874.1 | 5877.8 | 5881.5 | 5885.2 |
| 159 | 5888.9 | 5892.6 | 5896.3 | 5900. | 5903.7 | 5907.4 | 5911.1 | 5914.8 | 5918.5 | 5922.2 |
|  | 5925.9 | 5929.6 | 5933.3 | 5937. | 5940.7 | 5944.4 | 5948.1 | 5951.9 | 5955.6 | 5959.3 |
| 161 | 5963. | 5966.7 | 5970.4 | 5974. 1 | 5977.8 | 5981.5 | 5985.2 | 5988.9 | 5992.6 |  |
| 162 | 6000. | 6003.7 | 6007.4 | 6011.1 | 6014.8 | 6018.5 | 60 | to25.9 |  | 6033.3 |
| 163 | 6037. | 6040.7 | 604 | 6048. | 6051.9 | 6055.6 | 6059 | Cc63. | tct6. 7 | 6070.4 |
| 164 | 6074.1 | 6077.8 | 6oSr. 5 | 6055.2 | 6088.9 | 6092.6 | tog6 | 6100. | 6103.7 | 6107.4 |
|  | 6III.I | 6114.8 |  | 61 | 6125.9 | 6129.6 | 6133.3 | 6137. | 6140.7 | 6144.4 |
|  | 6148 | 6151.9 | 6155.6 | 615 | 6163. | 6166.7 | 6170.4 | 6174.1 | 6177.8 | 6181.5 |
| 167 | 6185 | 6r88 | 6192.6 | 6196 | o. | 6203.7 | 6207.4 | 6211.1 | $\mathrm{C}_{214} \mathrm{C}^{8}$ | 6218.5 |
| 168 | 622 | 6225 | 6229.6 | 6233.3 | 6237. | 6240.7 | 624 | 6248.1 | 6251.9 | 6355.6 |
| 169 | 6259 | 6263. | 6266.7 | 6270.4 | 6274. | 6277.8 | 6281.5 | 285.2 | 6288.9 | 6292.6 |
| 170 | 6296 | 630 | 6303.7 | 6307 | 6311.1 | 6314.8 | 6318.5 | 6322.2 | 6325.9 | 6329.6 |
| 171 | 6333 | 6337. | 6340 | 63 | 6348.1 | 6351.9 | 6355.6 | 6359.3 | 6363. | $6_{366.7}$ |
| 172 | 6370. | 6374 | 6377.8 | 6381 | 6385.2 | 6388.9 | 6392.6 | 6396.3 | 6400 | 3.7 |
| 173 | 6407 | $6+11$ | $6+14$ | $6+18.5$ | $6+22.2$ | 6425.9 | 6429.6 | 6433.3 | 6437. | . 7 |
| 174 | $64+$ | $6+48$ | $6+51.9$ | 6455.6 | 6459.3 | 6463. | 6466.7 | 6470.4 | 6474.1 | 6477.8 |
| 175 | 6481 | 6485.2 | $6+88.9$ | 6492.6 | 6496.3 | 6500. | 6503.7 | 6507.4 | 6511.1 | ${ }_{6} 514.8$ |
| 176 | 6518. | 6522.2 | 6525.9 | 6529.6 | 6533.3 | 6537. | 6540.7 | 6544.4 | 6548.1 |  |
| 177 | 6555.6 | 6559.3 | 6563. | 6566.7 | 6570.4 | 6574.1 | 6571 |  | 6585.2 |  |
| 178 | 6592.6 | 6596.3 | 6600. | 6603.7 | 6607.4 | 6611.1 | 661 |  | 6622.2 |  |
| 179 | 6629.6 | $6633 \cdot 3$ | 6637. | 66.40 .7 | 6644 | $66+8.1$ | 6651.9 | 6655.6 | C659.3 | 6663. |
| 18 | 6666.7 | 6670.4 | 667+. 1 | 6677.8 | 6681.5 | 6685.2 | 6688.9 | 6692.6 | 6696.3 | 67co. |
| 18 | 6703. | 6707.4 | 6711.1 | 6714.8 | 6718 | 6722.2 | 6725. | 6729.6 | 6733.3 | 6737. |
| 182 | $67+0.7$ | $67+4.4$ | 6748.1 | 6751.9 | 6755 | 6759.3 | 6763. | 6766.7 | 6770.4 | 6774.1 |
| 183 | 6777.8 | 6781.5 | 6785.2 | 6788.9 | 679 | 6796.3 | 6800. | 6803.7 | 6807.4 | 6811.1 |
| 184 | 681. 8 | 6818. | 6822 | 6825. | 6829 | 6833.3 | 6837. | 68.40 .7 | 684 | 6848.1 |
| 185 | 6851.9 | 6S55.6 | 6859 | 6863. | 6366 | 6870.4 | 6874.1 | 6877 | 6881 | 6885.2 |
| 185 | 6888.9 | 6892.6 | 6896.3 | 6900. | 690 | 6907.4 | 69 | 6914.8 | 6918.5 | 6922.2 |
|  | 6925.9 | 69 | 6933.3 | 6937. | $69+1$ | $69+4.4$ |  |  | 6955.6 | 3 |
| 188 | 6963. | 6966.7 | 6970.4 | 6974. | 697 | 69 |  |  | 69 | 6996.3 |
| 189 | 7000. | 7003.7 | 7007 | 7011 | 701 | 701 | 70 |  | 7029 | 7033.3 |
| 190 | 7037. | 7040.7 | 704 | 7048 | 705 | 7055 |  | 7063. | 7066 | 7070.4 |
| 191 | 7074.1 | 7077 | 7031 | 7085 | 7058 | 7092 | 7096.3 | 7100 | 7103 | 7107.4 |
| 192 | 7111 | 7114 | 7118 | 71 |  | 7129 | 7133 | 7137 | 714 | 7144.4 |
| 193 | 7143 | 7151 | 7155 |  | 7163 | 7166.7 | 770 | 7174 | 7178 | 7181.5 |
| 194 | 71 | 7188. | 7192 | 7196.3 | 7200. | 7203.7 | 7207 | 7211 | 721 | 7218.5 |
| 195 | 7222.2 | 7225.9 | 7229.6 | 7233.3 | 7237 | 7240.7 | 724 | 7248 | 7251 | 7255.6 |
| 19 | 7259 | 7263. | 7266.7 | 7270.4 | 72 | 727 | 7281 | 728 | 7288 |  |
| 197 | 7296.3 | 730 | 7303 | 7307 | 7311 | 7314.8 | 7318 | 732 | 7325 | 7329.6 |
| 19 | 7333.3 | 73 | 7340 | 73 | $73+8$ | 7351 | 7355 | 739 | 7363. | 7366.7 |
| 199 | 7370. | 7374 | 7377.8 | 7381.5 | 7385.2 | 7388.9 | 7392.6 | 7396.3 | 7400 | 74037 |
| 200 | $7+07$. | 41 | 7414 | 7418.5 | 7422.2 | 7425.9 | 7429.6 | 7433.3 | 7437. | 7440 |
|  |  |  | 2. | 3. | 4. | 5. | 6. | 7. | 8. | 9. |

TABLE No. 4-Continued.

| Areas....................... | 0.1 | 0.2 | 0.25 | 0.3 | 0.4 | 0.5 | 0.6 | 0.7 | 0.75 | 0.8 | 0.9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Contents.................. | 0.4 | 0.7 | 0.9 | 1.1 | .1 .5 | 1.9 | 2.2 | 2.6 | 2.8 | 3.0 | 3.3 |

$\therefore$ reas: Tens in left Column and Units at top. Contents for 100 fect in cubic yards in body of Table.

| 岕 | 0. | 1. | 2. | 3. | 4. | 5. | 6. | 7. | 8. | 9. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 231 | 7444 | 744 | 7451.9 | 7455.6 | 7459.3 | 7463. | 7466.7 | 7470.4 | 7474.I | . 8 |
| 202 | 7481 | 7485.2 | 7488.9 | 7492.6 | 7496.3 | 7500. | 7503.7 | 7507.4 | 75 II.I | 7514.8 |
| 233 | 7518 | 7522.2 | 7525.9 | 752 | 7533.3 | 7537. | 7540.7 | $7544 \cdot 4$ | 7548.I | 7551.9 |
| 204 | 7555.6 | 7559.3 | 7563. | 7566.7 | 7570.4 | 7574.I | 7577.8 | 7581.5 | 7585.2 | 7588.9 |
| 205 | 7592 | 7596.3 | 7600. | 7603.7 | 7607.4 | 7611.1 | 7614. | 7618.5 | 7622.2 | 7625.9 |
| 206 | 7629.6 | 7633.3 | 7637. | 7640.7 | $7644 \cdot 4$ | 7648.1 | 7651.9 | 7655.6 | 7659.3 | 7663. |
| 207 | 7666.7 | 7670.4 | 7674.1 | 7677.8 | 7681.5 | 7685.2 | 7688.9 | 7692.6 | 7696.3 | 7700. |
| 8 | 7703.7 | 7707.4 | 7711.1 | 7714.8 | 7718.5 | 7722.2 | 7725.9 | 7729.6 | $7733 \cdot 3$ | 7737. |
| 209 | 7740.7 | 7744.4 | 7748.1 | 7751.9 | 7755.6 | 7759.3 | 7763. | 7766.7 | 7770.4 | 7774.I |
| 210 | 7777.8 | 7781.5 | 7785.2 | 7788.9 | 7792.6 | 7796.3 | 7800. | 7803.7 | 7807.4 | 7811.1 |
| 211 | 7814.8 | 7818.5 | 7822.2 | 7825.9 | 7829.6 | 7833.3 | 7837. | 7840.7 | 7844.4 | 7848.I |
| 212 | 7851.9 | 7855.6 | 7859.3 | 7863. | 7866.7 | 7870.4 | 7874.1 | 7877.8 | 7881.5 | 7885.2 |
| 213 | 7888.9 | 7892.6 | 7896.3 | 7900. | 7903.7 | 7907.4 | 7911.I | 7914.8 | 7918.5 | 7922.2 |
| 214 | 7925.9 | 7929.6 | 7933.3 | 7937. | 7940.7 | 7944.4 | 7948.1 | 7951.9 | 7955.6 | . 3 |
| 5 | 7963. | 7966.7 | 7970.4 | 7974.I | 7977.8 | 798 I .5 | 7985.2 | 7988.9 | 7992.6 | 7996.3 |
| 216 | 8000. | 8003.7 | 8007.4 | 801 I.I | 8014.8 | Sor 8.5 | 8022.2 | 8025.9 | 8029.6 | 8033.3 |
| 217 | 8037. | 80.0 .7 | $80+4.4$ | 8048.1 | 805 I .9 | 8055.6 | 8059.3 | 8063. | 8066.7 | 8070.4 |
| 218 | 8074.1 | 8077.8 | 808 r .5 | 8085.2 | 8088.9 | 8092. 5 | 3096.3 | 8100. | 8103.7 | 8107.4 |
| 219 | 8111.1 | 8154.8 | 8118.5 | 8122 | 8125.9 | $812 c .6$ | 3133.3 | 8137. | 8140.7 | 8144.4 |
| 220 | 8148.1 | 8151.9 | 8155.6 | 8159.3 | 8163. | 8166.7 | 8170.4 | 8174.1 | 8177.8 | 8181.5 |
| 221 | 8185.2 | 8188.9 | 8192.6 | 8196.3 | . | 8203.7 | 8207.4 | 82II.I | 8214.8 | 8218.5 |
| 222 | 8222.2 | 8225.9 | 8229.6 | 8233.3 | 8237. | 8240.7 | 8244.4 | 8248.1 | 825 I.9 | 8255.6 |
| 223 | 8259.3 | 8263. | 8266.7 | 8270.4 | 8274.1 | 8277.8 | 8281.5 | 8285.2 | 8288.9 | 8292.6 |
| 224 | 8296.3 | 8300. | 8303.7 | 8307.4 | 8311.1 | 8314.8 | 8318.5 | 8322.2 | 8325.9 | 8329.6 |
| 22 | 8333.3 | 8337. | 8340.7 | 8344.4 | 8348.1 | 835 I. 9 | 8355.6 | 8359.3 | 8363. | 8366.7 |
| 225 | 8370.4 | 8374.1 | 8377.8 | 838 I. 5 | 8385.2 | 8388.9 | 8392.6 | 8396.3 | 8400. | 8403.7 |
| ${ }^{2} 22$ | 8407.4 | 8 811. 1 | 8414.8 | 8418.5 | 8422.2 | 8425.9 | 8429.6 | 8433.3 | 8437. | 8440.7 |
| 228 | $8+44.4$ | 8448.1 | 8451.9 | 8455.6 | 8459.3 | 8463. | 8466.7 | 8470.4 | 8474.1 | 8477.8 |
| 229 | 848 I .5 | 8485.2 | 8488.9 | 8492.6 | 8496.3 | 8500. | 8503.7 | 8507.4 | 85 II.I | 85 I 4.8 |
| 230 | 8518.5 | 8522.2 | 8525.9 | 8529.6 | 8533.3 | 8537. | 8540.7 | $8544 \cdot 4$ | 8548.1 | 8551.9 |
| 23 r | 8555.6 | 8559.3. | 8563. | 8566.7 | 8570.4 | 8574.1 | 8577.8 | 8581.5 | 8585.2 | 8588.9 |
| 232 | 8592.6 | 8596.3 | 8600. | 8603.7 | 8607.4 | 8611.I | 8614.8 | 8618.5 | 8622.2 | 8625.9 |
| 233 | 8629.6 | 8633.3 | 8637. | 8640.7 | 8644.4 | 8648.1 | 8651.9 | 8655.6 | 8659.3 | 8663. |
| 234 | 8666.7 | 8670.4 | 8674.1 | 8677.8 | 8681.5 | 8685.2 | 8683.9 | 8692.6 | 8696.3 | 8700. |
| 235 | 8703.7 | 8707.4 | 871 I.I | 8714.8 | 8718.5 | 8722.2 | 8725.9 | 8729.6 | 8733.3 | 8737. |
| 235 | 8740.7 | 8744.4 | 8748.1 | 8751.9 | 8755.6 | 8759.3 | 8763. | 8766.7 | 8770.4 | 8774.1 |
| 237 | 8777.8 | 8781.5 | 8785.2 | 8788.9 | 8792.6 | 8796.3 | 8800. | 8803.7 | 8807.4 | 8811.I |
| 238 | 8814.8 | 8818.5 | 8822.2 | 8825.9 | 8829.6 | 8833.3 | 8837. | 8840.7 | 8844.4 | 8848.I |
| 239 | 885 I. 9 | 8855.6 | 8859.3 | 8863. | 8866.7 | 8870.4 | 8874.1 | 8877.8 | 8881.5 | 8885.2 |
| 240 | 88889 | 8892.6 | 8896.3 | 8900. | 8903.7 | 8907.4 | 8911.1 | 8914.8 | 8918.5 | 8922.2 |
| 241 | 8925.9 | 8929.6 | 8933.3 | 8937. | 8940.7 | 8944.4 | 8948.1 | 8951.9 | 8955.6 | 8959.3 |
| 242 | 8963. | 8966.7 | 8970.4 | 8974.1 | 8977.8 | 8981.5 | 8985.2 | 8988.9 | 8992.6 | 8996.3 |
| 243 | 9000. | 9003.7 | 9007.4 | 9011.1 | 9014.8 | 9018.5 | 9022.2 | 9025.9 | 9029.6 | 9033.3 |
| 244 | 9037. | 9040.7 | 9044.4 | 9048.1 | 9051.9 | 9055.6 | 9059.3 | 9063. | 9066.7 | 9070.4 |
| 245 | 9074.I | 9077.8 | 9081.5 | 9085.2 | 9088.9 | 9092.6 | 9096.3 | 9100. | 9103.7 | 9107.4 |
| 246 | 9III.I | 9114.8 | $9^{118.5}$ | 9122.2 | 9125.9 | 9129.6 | 9133.3 | 9137. | 9140.7 | 9144.4 |
| 247 | 9148.1 | 91519 | 9155.6 | 9159.3 | 9163. | 9166.7 | 9170.4 | 9174.I | 9177.8 | 9181.5 |
| 248 | 9185.2 | 9188.9 | 9192.6 | 9196.3 | 9200. | 9203.7 | 9207.4 | 92 II. 1 | 9214.8 | 9218.5 |
| 249 | 9222.2 | 9225.9 | 9229.6 | 9233.3 | 9237. | 9240.7 | 9244.4 | 9248.1 | 9251.9 | 9255.6 |
| 250 | 9259.3 | 9263. | 9266.7 | 9270.4 | 9274.I | 9277.8 | 9281.5 | 9285.2 | 9288.9 | 9292.6 |
|  | o. | 1. | 2. | 3. | 4. | 5. | 6. | 7. | 8. | 9. |

## 53

TABLE Ňo. 4-Continued.

| Areas........................ | 0.2 | 0.2 | 0.25 | 0.3 | 0.4 | 0.5 | 0.6 | 0.7 | 0.75 | 0.8 | 0.9 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Contents. . . . . . . . . . | 0.4 | 0.7 | 0.9 | 1.1 | 1.5 | 1.9 | 2.2 | 2.6 | 2.8 | 3.0 | 3.3 |

Areas: Tens in left Column and Units at top. Contents for 100 feet in cubic yards in body of Table.

| ذ | 0. | 1. | 2. | 3. | 4. | 5. | 6. | 7. | 8. | 9. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 251 | 9296.3 | 9300. | 9303.7 | 9307.4 | 9311.1 | 9314.8 | 9318.5 | 9322.2 | 9325.9 | 9329.6 |
| 252 | 9333.3 | 9337. | 9340.7 | 93+4.4 | 934 | 0351.9 | 9355.6 | $9359 \cdot 3$ | 9363. | 9366.7 |
| 253 | 9370.4 | 9374. I | 9377.8 | 9381.5 | 9385.2 | 9388.9 | 9392.6 | 9396.3 | 9400. | 9403.7 |
| 254 | 9407.4 | 9411.1 | 9414.8 | 9418.5 | 9422.2 | 9425.9 | 9429.6 | 9433.3 | 9437. | 9440.7 |
| 255 | 9+44.4 | 9448.r | 9451.9 | 9455.6 | 9459.3 | 9463. | 94667 | 9470.4 | 9474. I | 9477.8 |
| 256 | 948 r .5 | 9485.2 | 9488.9 | 9492.6 | 9496.3 | 9500. | 9503.7 | 9507.4 | 9511.1 | 9514.8 |
| 257 | 9518.5 | 9522.2 | 9525.9 | 9529.6 | 9533.3 | 9537. | 9540.7 | 9544.4 | 9548.1 | 9551.9 |
| 258 | 9555.6 | 9559.3 | 9563. | 9566.7 | 9570.4 | 9574.1 | 9577.8 | 9581.5 | 9585.2 | 9588.9 |
| 259 | 9592.6 | 9596.3 |  | 9603.7 | 9607.4 | 9611.1 | 9614.8 |  | 9622.2 |  |
| 260 | 9629.6 | 9633.3 | 9637. | 9640.7 |  | 9648.1 |  | 9655.6 |  | 9663. |
| 261 | 9666.7 | 9670.4 | 9674. 1 | 9677.8 | 9681.5 | 9685.2 | 9688.9 | 9692.6 | 9696.3 | 9700. |
| 262 | 9703.7 | 9707.4 | 9711.1 | 9714.8 | 9718.5 | 9722.2 | 9725.9 | 9729.6 | 9733.3 |  |
| 263 | 9740.7 | 9744.4 | 9748.1 | 975 I .9 | 9755.6 | 97593 | 9763. | 9766.7 | 9770.4 | 9774.1 |
| 264 | 9777.8 | 9781.5 | 9785.2 | 9788.9 | 9792.6 | 9796.3 | 9800. | 9803.7 | 9807.4 | 9811.1 |
| 265 | 98 ¢4.8 | 9818.5 | 9822.2 | 9825.9 | 9829.6 | 9833.3 | 9837. | 9840.7 |  | 9848.1 |
| 266 | 9851.9 | 9855.6 | 9859.3 | 9863. | 9866.7 | 9870.4 | 9874.1 | 9877.8 | 988 I .5 | 9885.2 |
| 267 | 9888.9 | 9892.6 | 9896.3 | 9900. | 9903.7 | 9907.4 | 9911.1 | 9914.8 | 9918.5 | 9922.2 |
| 268 | 9925.9 | 9929.6 | $9933 \cdot 3$ | 9937. | 9940.7 | 9944.4 | 9948.1 |  | 9955.6 | 9959.3 |
| 269 | 9963. | 9966.7 | 9970.4 | 9974.I | 9977.8 | 9981.5 | 9985.2 | 9988.9 | 9992.6 | 9996.3 |
| 270 | 10000. | 10003.7 | 10007.4 | 10011.1 | 10014.8 | 10018.5 | 10022.2 | 10025.9 | 10029.6 | 10033.3 |
| 271 | 10037. | 10040.7 | 10044.4 | 10048.1 | 10051.9 | 10055.6 | 10059.3 | 10063. | 10066.7 | 10070.4 |
| 272 | 10074.1 | 10077.8 | 10081. 5 | 10085.2 | 10088.9 | 10092.6 | 10096.3 | OI | 10103.7 | 10107.4 |
| 273 | IOIII. 1 | IOII4. 8 | IOI 18.5 | 1O122.2 | 10125.9 | 10129.6 | IOI33.3 | 10137. | IOI40.7 | 10144.4 |
| 274 | IOI48.1 | 10151.9 | 10155.6 | IOI 59.3 | 10163. | 10166.7 | 10170.4 | IOI74.I | 10177.8 | 10181.5 |
| 275 | IOI 85.2 | 10188.9 | 10192.6 | IoI96.3 | 0200. | 10203.7 | 10207.4 | IO2II.1 | 10214.8 | 10218.5 |
| 276 | 10222.2 | 10225.9 | 10229.6 | $10233 \cdot 3$ | 10237. | 10240.7 | 10244.4 | 10248.1 | 10251.9 | 10255.6 |
| 277 | 10259.3 | 10263. | 10266.7 | 10270.4 | 10274.1 | 10277.8 | 10281.5 | 10285.2 | 10288.9 | 10292.6 |
| 278 | 10296.3 | 10300. | 10303.7 | 10307.4 | 10311.1 | 10314.8 | 10318.5 | 10322.2 | 10325.9 | 10329.6 |
| 279 | 10333.3 | 10337. | 10340.7 | 10344.4 | 10348.1 | 10351.9 | 10355.6 | 10359.3 | 10363. | 10366.7 |
| 280 | 10370.4 | 10374.1 | 10377.8 | 10381.5 | 10385.2 | 10388.9 | 10392.6 | 10396.3 | 10400. | 10403.7 |
| 281 | 10407.4 | 10411.1 | 10414.8 | 10418.5 | 10422.2 | 10425.9 | 10429.6 | 10433.3 | 10437. | 10440.7 |
| 282 | 10444. | 10448.1 | 10451.9 | 10455.6 | 10459.3 | 10463. | 10466.7 | 10470.4 | 10474.1 | 10477.8 |
| 283 | 10481.5 | 10485.2 | 10488.9 | 10492.6 | 10496.3 | 10500. | 10503.7 | 10507.4 | 10511.1 | 10514.8 |
| 284 | 10518.5 | 10522.2 | 10525.9 | 10529.6 | 10533.3 | 10537. | 10540.7 | 10544.4 | 10548.1 | 10551.9 |
| 285 | IO555.6 | 10559.3 | 10563. | 10566.7 | 10570.4 | 10574.1 | 10577.8 | 10581.5 | 10585.2 | 10588.9 |
| 286 | 10592.6 | 10596.3 | 10600. | 10603.7 | 10607.4 | 106II.I | 10614.8 | 10618.5 | 10622.2 | 10625.9 |
| 287 | 10629.6 | 10633.3 | 10637. | 10640.7 | 10644.4 | 10648.1 | 10651.9 | 10655.6 | 10659.3 | 10663. |
| 288 | 10666.7 | 10670.4 | 10674.1 | 10677.8 | 10681.5 | 10685.2 | 10688.9 | 10692.6 | 10696.3 | 10700. |
| 289 | 10703.7 | 10707.4 | 10711.1 | 10714.8 | 10718.5 | 10722.2 | 10725.9 | 10729.6 | 10733.3 | 10737. |
| 290 | 10740.7 | 10744.4 | 10748.1 | 10751.9 | 10755.6 | 10759.3 | 10763. | 10766.7 | 10770.4 | 10774.1 |
| 291 | 10777.8 | 10781.5 | 10 '785.2 | 10788.9 | 10792.6 | 10796.3 | 10800. | 10803.7 | 10807.4 | 108II.I |
| 292 | 10814.8 | 10818.5 | 10822.2 | 10825.9 | 10829.6 | 10833.3 | 10837. | 10840.7 | 10844.4 | 10848.1 |
| 293 | 10851. | 0855.6 | 10859.3 | 10863. | 10866.7 | 10870.4 | 10874.1 | 10377.8 | 1088I. 5 | 10885.2 |
| 294 | 10888.9 | 10892.6 | 10896.3 | 10900. | 10903.7 | 10907.4 | 10911.1 | 10914.8 | 10918.5 | 10922.2 |
| 295 | 10925.9 | 10929.6 | 10933.3 | 10937. | 10940.7 | 10944.4 | 10948.1 | 10951.9 | 10955.6 | 10959.3 |
| 296 | 10963. | 10966.7 | 10970.4 | 10974.1 | 10977.8 | 10981.5 | 10985.2 | 10988.9 | 10992.6 | 10996.3 |
| 297 | 11000. | 11003.7 | 11007.4 | 11011.1 | 11014.8 | 11018.5 | 11022.2 | 11025.9 | 11029.6 | 11033.3 |
| 1298 | 11037. | 11040.7 | 11044.4 | 11048.1 | 11051.9 | IIO55.6 | 11059.3 | 11063. | 11066.7 | 11070.4 |
| 299 | 11074.1 | 11077.8 | 11081.5 | 11085.2 | 11088.9 | 11092.6 | 11096.3 | 11100 | 11103.7 | 11107.4 |
| 300 | IIIII.I | 11114.8 | IIII8.5 | III22.2 | III25.9 | II 129.6 | I I I 33.3 | 11137. | III 40.7 | 1144.4 |
|  | 0. | 1. | 2. | 3. | 4. | 5. | 6. | 7. | 8. | 9. |

TABLE No. 4-Continued.

| A | 0.I | 0.2 | 0.25 | - 3 | 0.4 | 0.5 | 0.6 | 0.7 | 0.75 | 0.8 | 0.9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| on | 0.4 | 0.7 | 0.9 | I.I | 1.5 | 1.9 | 22 | 2.6 | 2.8 | 3.0 | 3.3 |

## Areas: Tens in left Column and Units at top. Contents for 100 feet in cubic yards in body of Table.

| 宸 | 0. | I. | 2. | 3. | 4. | 5. | 6. | 7. | 8. | 9. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 301 |  |  |  |  |  | 11166.7 |  |  |  |  |
| ) | 11185.2 | III88.9 | 11192.6 | 11196.3 | 1200. | 11203.7 | 11207.4 | 11211.1 | 11214.8 | 11218.5 |
| 303 | 11222. | 11225.9 | 11229 | 11233.3 | I1237. | 11240.7 | 11244.4 | 11248.1 | 11 |  |
| 304 | 11259. | 11263. | 11266 | 11270.4 | 41274.1 | 11277.8 | 11281.5 | 11285.2 |  |  |
| 305 | II2 | 11300. | 113 |  |  | 11314 | 81318.5 | 1132 |  |  |
| 305 | 11333.3 | 11337. | I1340.7 | 11344.4 | 11348 | 11351 | 11355 | 1135 | 11363. |  |
| 307 | 11370. | 11374.1 | 11377.8 | 11381.5 | 511385.2 | 11388.9 | ${ }^{11} 392.6$ | 11396.3 | 11400. | 11403.7 |
| 308 | 11407. | II4II.I | 11414 | 11418 | 511422.2 | 1142 |  | $11433 \cdot 3$ | 1143 |  |
| 309 |  | 11448.1 | 11451 | 11455.6 | 611459.3 | 11463. | 11466.7 | 11470.4 | 11474 |  |
| 310 | 11481 | 485 |  |  | 11496 | 11500. | 11503.7 |  |  |  |
| 311 | 11518.5 | 11522. | 11525. | 11529 | 611533.3 | 1537. | 11540.7 | 1154.4 | 1154 | 15 |
| 312 | 11555. | 11550 | 11563. | 11566.7 | 11570.4 | 11574.1 | 11577.8 | 11581.5 | 11585.2 |  |
| 313 | 11592.6 | 11596 | 1600. |  |  |  |  |  |  |  |
| 314 | 11629.6 | 11633.3 | 11637. | 11640.7 | 11644 | 11648 | 11651.9 | ${ }^{116555}$ |  |  |
| 315 | 116 |  | 11674.I | 11677.8 | 11681.5 | 11685.2 |  | ${ }^{11692.6}$ | 116 |  |
| 316 | 11703. | 11707 | 11711 | 11714.8 | 11718.5 | 11722 | 11725 | 1172 | 1173 |  |
| 317 | 11740. | 11744 | 11748.1 | 11751.9 | 11755.6 | 11759 | 11763. | 11766.7 | 1177 | 11 |
| 318 | 1177 | 11781 | 117 | 1178 | 11792 | 11796 |  | 11803.7 | 118 |  |
| 319 | 11814 | 11818.5 | 182 | 11825 | 1822 | 11833 | 11837. | 11840.7 |  |  |
|  | 11851 | 退 | 1185 | 11863. | I1866 | 11870 | 11874 | 11877.8 |  | 11 |
| 321 | II888 | 11892. | II896 | 11900 | 11903 | 11907 | 11911 | 11914.8 | 119 |  |
|  | II925 |  | 11933.3 | 11937. | 11940.7 | 11944.4 | 41948.1 | 11951.9 | 1195 |  |
| 323 | 11963. | 11966.7 | 11970.4 | 11974.1 | 11977.8 | 11981.5 | 11985.2 | I1988.9 | 1199 |  |
|  | 12000. | 12003.7 | 1200 | 12011 | 12014.8 | 12018 | 12022 | 12025 | 120 | ${ }^{12033.3}$ |
| 325 | 12037. | 12040 | 1204 | 12048.1 | 12051.9 | 1205 | 61205 | 12063. | 1206 | 12070.4 |
| 326 | 12074 | 12077 |  |  | 120 |  |  | 121 | 1210 |  |
|  | 12111.1 | 12114.8 | 12118.5 | 12122 | 12125 | 12129.6 | 612133.3 | 12137.0 | 1214 | 121 |
| 328 | 12148. | 1215 | 12155.6 | 12159 | ${ }^{12163}$. | ${ }^{12166.7}$ | 12170 |  |  |  |
| 329 | 12185.2 | 12188.9 | ${ }^{12192.6}$ | 12196.3 | 12200 | 12203.7 | 12207. | 12211.1 |  |  |
| 330 | 12222.2 | 12225.9 | 12229.6 | $12233 \cdot 3$ | 12237. | 12240.7 | 12244.4 | 12248.1 | 1225 |  |
| 33 r | 12250 | 12263. | 12266.7 | 12270.4 | 12274.1 | 12277.8 | 12281. | 12285.2 | 122 |  |
|  | I2296 | 12300. | 12303.7 | 12307.4 | 12311.1 | 12314.8 | 12318.5 | 12322.2 | 12325. |  |
| 333 | 12333. | 12337. | 12340 | 12344 | 12348 | 1235 | ${ }^{12355.6}$ | 12359.3 | 12363. |  |
|  | 12370. | 12374.1 | 12377.8 | 12381. | 12385.2 | 12388. | ${ }^{12392.6}$ | ${ }^{12396}$ | 12400. | 12403.7 |
|  | 12407. | 12411.1 | 12414.8 | 12418. | ${ }^{12422.2}$ | 12425.9 | 12429.6 | $12433 \cdot 3$ | 12437. | 12440.7 |
| 336 | 12444 | 12448.1 | 12451.9 | 12455.6 | 12459.3 | 12463. | 12466.7 | $12470 \cdot 4$ | 12474.1 | 124 |
| 337 | 12481. | 12485.2 |  | 12492.6 | 12496.3 | 12500. | 12503.7 | 12507.4 | 1251 | 12514.8 |
| $33^{8}$ | 12518. | 12522. | 12525 | 12529.6 | ${ }^{12533} 3$ | 12537. | 12540 | 12544.4 |  |  |
| 339 | 12555.6 | 12550 | 12563. | 12566.7 | 12570.4 | 12574.1 | 12577 | 12581.5 | 1258 |  |
|  | 12592.6 | 12596.3 |  | 12603.7 | 12607.4 | 12611.1 | 12614.8 | 12618.5 | 1262 | 2625.9 |
| 34 r | 12629.6 | 12633.3 | 12637. | 12640.7 | 12644. | 12648.1 | 12651 | 12655.6 |  | 12663. |
| 342 | 12666.7 | 12670. | 12674.1 | 12677.8 | 12681 | 12685.2 | 12688 | 12692.6 | 126 |  |
| 343 | 12703.7 | 12707.4 | 12711.1 | 12714.8 | 12718 | 12722.2 | 12725 | 12729.6 | 12733 |  |
| 345 | 12740. | 12744 | 12748.1 | 1275 | 12755 | 1275 | 12763 | 12766.7 | 1280 | ${ }^{\text {127 }}$ |
|  | 12777 | 12781.5 | 12785.2 |  | ${ }^{12792.6}$ | 12796. | ${ }^{12800}$ | 12803.7 | 1280 | $12811 . \mathrm{I}$ |
| 346 | 12814. | 12818. | 12822.2 | 12825. | 12829.6 | 12833. | 12837. | 12840 | 1284 | 12848.1 |
| 347 | 12851. | ${ }^{12855}$ |  | 12863. | 12866.7 | 12870 | 12874. | 12877 | 1288 |  |
| 348 | 128 | ${ }^{12892}$ | 12896.3 | 12900. | 12903.7 | 12907.4 | 12911.1 | 12914.8 | 12918 | 12922.2 |
|  | 12925. | 12929 | 12933.3 | 12937. | 12940.7 | I2944.4 | 12948.1 | 12951.9 | 12955 |  |
| 350 | 12963. | 12966. | 12970.4 | 12974. | 12977 | 12981. | 12985 | 12988. | 12992 | 12996 |
|  | 0. | I. | 2. | 3. | 4. | 5. | б. |  | 8. | و. |

TABLE Ko. 4-Concluded.

| Areas. | 0.1 | 0.2 | 0.25 | 0.3 | 0.4 | 0.5 | 0.6 | 0.7 | 0.75 | 0.8 | . 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Contents... | 0.4 | 0.7 | 09 | I.I | 1.5 | 1.9 | 2.2 | 2.6 | 2.8 | 3.0 | 3.3 |

Areas: Tens in left Column and Units at top. Contents for 100 feet in cubic yards in body of Table.

| 守 | 0. | 1. | 2. | 3. | 4. | 5. | 6. | 7. | 8. | 9. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |

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13000.



















































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1.
2.
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5. 6.
7.
8.
9.

## TABLE No. 5.

Minus Corrections corresponding to $N \sim N^{\prime}$, or $n \sim n^{\prime}$, and general for all side slopes. For computation by average Areas.
Difference of Correction numbers in feet and tenths in left column and at top; Correction in cubic yards for 100 ft. in body of Table.

| 辿 | 0. | 1. | 2. | 3. | 4. | 5. | 6. | 7. | 8. | 9. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0.0 | 0.0 | 0.0 | 0.1 | O.T | 0.2 | 0.2 | 0.3 | 0.4 | 0.5 |
| 1 | 0.6 | 0.7 | 0.9 | 1.0 | . 2 | 1.4 | 1. 6 | 1.8 | 2.0 | 2.2 |
| 2 | 2.5 | 2.7 | 3.0 | $3 \cdot 3$ | 3.6 | 3.9 | 4.2 | 4.5 | 4.8 | 5.2 |
| 3 | 5.6 | 5.9 | 6.3 | 6.7 | 7.1 | 7.6 | 8.0 | 8.5 | 8.9 | 9.4 |
| 4 | 9.9 | . 4 | 10.9 | 1.4 | 2.0 | 12.5 | 3.1 | 13.6 | 4.2 | 14.8 |
| 5 | 15.4 | 16.1 | 16.7 | 17.3 | 18.0 | 18.7 | T9.4 | 20.1 | 20.8 | 1.5 |
| 6 | 22.2 | 23.0 | 23.7 | 245 | 25.3 | 26.1 | 26.9 | 27.7 | 28.5 | 9.4 |
| 7 | 30.2 | 31.1 | 32.0 | 32.9 | 33.8 | 34.7 | 35.7 | 36.6 | 37. | 38.5 |
| 8 | 39.5 | 40.5 | 41.5 | 42.5 | 43.6 | 44.6 | 45.7 | 46.7 | 47.8 | 48.9 |
| 9 | 50.0 | 51.1 | 52.2 | 53.4 | $5+5$ | 55.7 | 56.9 | 58.1 | 59.3 | 60.5 |
| 10 | 61.7 | 63.0 | 64.2 | 65.5 | 66.8 | 68.1 | 69.4 | 70.7 | 72.0 | 73.3 |
| II | 74.7 | 76.1 | 77.4 | 78.8 | 80.2 | 8 I .6 | 83.1 | 84.5 | 86.0 | 87.4 |
| 12 | 88.9 | 90.4 | 91.9 | 93.4 | 94.9 | 96.5 | 98.0 | 99.6 | 101 | 102.7 |
| 13 | 104.3 | 105.9 | 107.6 | 109.2 | 110.8 | 112.5 | 114.2 | 115.9 | 117.6 | 119.3 |
| 14 | 121.0 | 122.7 | 124.5 | 126.2 | 128.0 | 129.8 | 131.6 | 133.4 | 135.2 | 137.0 |
| 15 | 138.9 | 140.7 | 142.6 | 144.5 | 146.4 | 148.3 | 150.2 | 152.2 | 154.1 | 156.1 |
| 16 | 158.0 | 160.0 | 162.0 | 164.0 | 166.0 | 168.1 | 170.1 | 172.2 | 174.2 | 176.3 |
| 17 | 178.4 | 180.5 | 182.6 | 184.7 | 186.9 | 189.0 | 191.2 | 193.4 | 195.6 | 197.3 |
| 18 | 200.0 | 202.2 | 204.5 | 206.7 | 209.0 | 211.3 | 213.6 | 215.9 | 218.2 | 220.5 |
| 19 | 222.8 | 225.2 | 227.6 | 229.9 | 232.3 | 234.7 | 237.1 | 239.6 | 242.0 | 2445 |
| 20 | 246.9 | 249.4 | 251.9 | 254.4 | 256.9 | 259.4 | 262.0 | 264.5 | 267.1 | 269.6 |
| 21 | 272.2 | 274.8 | 277.4 | 280.1 | 282.7 | 285.3 | 288 | 290.7 | 293.4 | 296.1 |
| 22 | 298.8 | 301.5 | 304.2 | 307.0 | 309.7 | 312.5 | 315.3 | 318.1 | 320.9 | 323.7 |
| 23 | 326.5 | 329.4 | 332.2 | 335.1 | 338.0 | 340.9 | 343.8 | 346.7 | 349.7 | 352.6 |
| 24 | 355.6 | 358.5 | 361.5 | 364.5 | 367.5 | 370.5 | 373.6 | 376.6 | 379.7 | 382.7 |
| 25 | 385.8 | 388.9 | 392.0 | 395.1 | 398.2 | 401.4 | 404.5 | 407.7 | 410.9 | 414.1 |
| 26 | 417.3 | 420.5 | 423.7 | 427.0 | 430.2 | 433.5 | 436.8 | 440.1 | 443.4 | 446.7 |
| 27 | 450.0 | 453.3 | 456.7 | 460.1 | 463.4 | 466.8 | 470.2 | 473.6 | 477.1 | 480.5 |
| 28 | $44^{4} .0$ | 487.4 | 490.9 | 494.4 | 497.9 | 501.4 | 504.9 | 508.5 | 51 | 515.6 |
| 29 | 519.1 | 522.7 | 526.3 | 529.9 | 533.6 | 537.2 | 540.8 | 544.5 | 54 | 551.9 |
| 30 | 555.6 | 559.3 | 563.0 | 566.7 | 570.5 | 574.2 | 578.0 | 58 I .8 | 585.6 | 589.4 |
| 31 | 593.2 | 597.0 | 600.9 | 604.7 | 608.6 | 612.5 | 616.4 | 620.3 | 624.2 | 628.2 |
| 32 | 632.1 | 636.1 | 6 ¢0.0 | 644.0 | 648.0 | 652.0 | 656.0 | 660.1 | 664.1 | 668.2 |
| 33 | 672.2 | 676.3 | 680.4 | 684.5 | 688.6 | 692.7 | 696.9 | 701 | 705.2 | 709.4 |
| 34 | 713.6 | 717.8 | 722.0 | 726.2 | 730.5 | 734.7 | 739.0 | 743.3 | 747.6 | 751.9 |
| 35 | 756.2 | 760.5 | 764.8 | 769.2 | 773.6 | 777.9 | 782.3 | 786.7 | 791.1 | 795.6 |
| 36 | 800. | 804.5 | 808.9 | 813.4 | 817.9 | 822.4 | 826.9 | 831.4 | 836.0 | 840.5 |
| 37 | 845. | 849.6 | 854.2 | 858.8 | 863.4 | 88.I | 872.7 | 877.3 | 882.0 | 886.7 |
| 38 | 891.4 | 896.I | 900.8 | 905.5 | 910.2 | 915.0 | 919.7 | 924.5 | 929.3 | 934.1 |
| 39 | 938.9 | 943.7 | 948.5 | 953.4 | 958.2 | 963.1 | 968.0 | 972.9 | 977.8 | ${ }^{982.7}$ |
| 40 | 987.7 | 992.6 | 997.6 | 1002.5 | 1007.5 | 1012.5 | 1017.5 | 1022.5 | 1027.6 | 1032.6 |
| 41 | 1037.7 | 1042.7 | 1047.8 | 1052.9 | 1058.0 | 1063.1 | 1068.2 | 1073.4 | 1078.5 | 1083.7 |
| 42 | 1088.9 | 1094.1 | 1099.3 | 1104. 5 | 1109.7 | 1115.0 | 1120.2 | 1125.5 | 1130.8 | 1136.1 |
| 43 | 1141.4 | 1146.7 | 1152.0 | II57.3 | 1162.7 | 1168. | 1173.4 | 1178.8 | 1184.2 | 1189.6 |
| 44 | 11.95 .1 | 1200.5 | 1206.0 | 1211.4 | 1216.9 | 1222.4 | 1227.9 | 1233.4 | 1238.9 | 1244.5 |
| 45 | 1250.0 | 1255.6 | 1261.1 | 1266.7 | 1272.3 | 1277.9 | 1283.6 | 1289.2 | 1294.8 | 1300.5 |
| 46 | 1306.2 | 1311.9 | 1317.6 | I323.3 | 1329.0 | 1334.7 | 1340.5 | 1346.2 | 1352.0 | 1357.8 |
| 47 | 1363.6 | 1369.4 | 1375.2 | 1381.0 | 1386.9 | 1392.7 | 1398.6 | 1404.5 | 1410.4 | 1416.3 |
| 48 | 1422.2 | 1428.2 | 1434.1 | 1440.I | 1446.0 | 1452.0 | 1458.0 | 1464.0 | 1470.0 | 1476.I |
| 49 | 1482.1 | 1488.2 | 1494.2 | 1500.3 | 1506.4 | 1512.5 | 1518.6 | 1524.7 | 1530.9 | 1537.0 |
| 50 | 1543.2 | 1549.4 | 1555.6 | 1561.8 | 1568.0 | 1574.2 | 1580.5 | 1586.7 | 1593.0 | 1599.3 |
|  |  | 1. | 2. | 3. |  |  |  |  | 8. | 9. |

## TABLE No. 5-Concluded.

Minus Corrections corresponding to $N \sim N^{\prime}$, or $n \sim n^{\prime}$, and general for all side slopes. For computation by average Areas.
Difference of Correction numbers in feet and tenths in left column and at top; Correction in cubic yards for 100 ft. in body of Table.

| 辰 | . 0 | . 1 | 2 | . 3 | . 4 | . 5 | . 6 | . 7 | . 8 | . 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 51 | 1605.6 |  | 1618.2 |  | 1630.8 | 1637.2 | 1643.6 | 1649.9 | 1656.3 | 1 |
| 52 | 1669. 1 | 1675.6 | 1682.0 | 1688.5 |  | 1701.4 | 1707.9 | 1714.4 | 1720.9 | 172 |
| 53 | 1734.0 | 1740.5 | 1747.1 | 1753.6 |  | 1766.8 | 1773.4 | 1780.1 | 1786.7 | 179 |
| 54 | 1800.0 | 1806.7 | 1813.4 | 1820.1 | 1826.8 | 1833.5 | 1840.2 | 1847.0 | 1853.7 | 1860.5 |
| 55 | 1867.3 | 1874.1 | 1880.9 | 1887.7 | I894.5 | 1901. 4 | 1908.2 | 1915.1 | 1922.0 | 1928.9 |
| 56 | 1935.8 | 1942.7 | 1949.7 | 1956.6 | 1963.6 | 1970.5 | 1977.5 | 1984.5 | 1991.5 | 1998.5 |
| 57 | 2005.6 | 2012.6 | 2019.7 | 2026.7 | 2033.8 | 2040.9 | 2048.0 | 2055.1 | 2062.2 | 2069.4 |
| 58 | 2076.5 | 2033.7 | 2090.9 | 2098.1 | 2105.3 | 2112.5 | 2119.7 | 2127.0 | $213+2$ | 2141.5 |
| 59 | 2148.8 | 2156.1 | 21063.4 | 2170.7 | 2178.0 | 2185.3 | 2192.7 | . | 2207.4 | 2214.8 |
| 60 | 2222.2 | 2229.6 | 2237.1 | 2244.5 | 2252.0 | 2259.4 | 2266.9 | 2274.4 | 2281.9 | 2289.4 |
| 6r | 2296.9 | 2304.5 | 2312.0 | 2319.6 | 2327.1 | 2334.7 | 2342.3 | 2349.9 | 2357.6 | 2365.2 |
| 62 | 2372.8 | 2380.5 | 2388.2 | 2395.9 | 2403.6 | 2411.3 | 2419.0 | 2426.7 | 2434.5 | 2442.2 |
| 63 | 2450.0 | 2457.8 | 2465.6 | $2473 \cdot 4$ | 2481.2 | 2.489 .0 | 2496.9 | 2504.7 | 2512.6 | 2520.5 |
| 64 | 2523.4 | 2536.3 | 2544.2 | 2552.2 | 2560.1 | 2568.1 | 2576.0 | 2584.0 | 2592.0 | 2600.0 |
| 65 | 2608.0 | 2615.1 | 2624.1 | 2632.2 | 2640.2 | 2648.3 | 2656.4 | 2664.5 | 2672.6 | 2680.7 |
| 66 | 2688.9 | 2697.0 | 2705.2 | 2713.4 | 2721.6 | 2729.8 | 2738.0 | 2746.2 | 2754.5 | 2762.7 |
| 67 | 2771.0 | 2779.3 | 2787.6 | 2795.9 | 2804.2 | 2812.5 | 2820.8 | 2829.2 | 2837.6 | 2845.9 |
| 68 | 2854.3 | 2862.7 | 2871.1 | 2879.6 | 2888.0 | 2896.5 | 2904.9 | 2913.4 | 2921.9 | 2930.4 |
| 69 | 2938.9 | $2947 \cdot 4$ | 2956.0 | 2964.5 | 2973.1 | 2981.6 | 2990.2 | 2998.8 | 3007.4 | 3016.I |
| 70 | $302+7$ | 3033.3 | 30.42 .0 | 3050.7 | 3059.4 | 3068.1 | 3076.8 | 3085.5 | 3094.2 | 3103.0 |
| 71 | 3111.7 | 3120.5 | 3129.3 | 3138.1 | 3146.9 | 3155.7 | 3164.5 | 3173.4 | 3182.2 | 3191.1 |
| 72 | 3200.0 | 3208.9 | 3217.8 | 3226.7 | 3235.7 | 3244.6 | 3253.6 | 3262.5 | 3271.5 | 3280.5 |
| 73 | 3239.5 | 3298.5 | 3307.6 | 3316.6 | 3325.7 | 3334.7 | 3343.8 | 3352.9 | 3362.0 | 3371.1 |
| 74 | 3380.2 | 3339.4 | 3398.5 | 3407.7 | 3416.9 | 3426.1 | 3435.3 | 3444.5 | 3453.7 | 3463.0 |
| 75 | $3+72.2$ | $34^{81} .5$ | 3490.8 | 3500.1 | 3509.4 | 3518.7 | 3528.0 | 3537.3 | 3546.7 | 3556.I |
| 76 | 3565.4 | 3574.8 | 3584.2 | 359 | 3603.I | 3612.5 | 362 | 3631.4 | 3640.9 | 3650.4 |
| 77 | 3659.9 | 3669.4 |  |  |  | 3707.6 | 37 | 3726.7 | 3736.3 | $37+5.9$ |
| 78 | 3755.6 | 3765.2 | 3774.8 | 3784.5 | 3794.2 | 3803.9 | ${ }^{3813.6}$ | 3823.3 | 33.0 |  |
| 79 | 3352.5 | 3862.2 | 3872.0 | 3881 | 3891.6 | 3901.4 | 3911.2 | 3921.0 | 3930.9 | 3940.7 |
| 80 | 3950.6 | 3960.5 | 3970.4 | 3980.3 | 3990.2 | 4000.2 | 4010 | 4020.1 | 4030.0 | 4040.0 |
| 81 | 4050.0 | 4060.0 | 4070.0 | 4080.1 | 4090.1 | 4100.2 | 4 |  | 4130.4 | 4140.5 |
| 82 | 4150.6 | 4160.7 | 4170.9 | 4 ISI .0 | 4191.2 | 4201.4 | 42 | 422 I | 4232 | 4242 |
| 83 | 4252.5 | 4262.7 | 4273.0 | 4283.3 | 4293.6 | 4303.9 | 4314.2 | 4324.5 | 4334.8 | 4345.2 |
| 84 | 4355.6 | 4365.9 | 4376.3 | 4386.7 | 4397.1 | 4407.6 | 4 | 4428.5 | 4438.9 | 4449.4 |
| 85 | $4+59.9$ | 4470.4 | $44^{80.9}$ | 4491.4 | 4502.0 | 4512.5 | 4523.1 | 4533.6 | 454 | 4554.8 |
| 86 | 4565.4 | 4576.1 | 4586.7 | 4597.3 | 4 | 4618.7 | 4629.4 | 4640.1 | 465 | 4661.5 |
| 87 | 4672.2 | 4633.0 | 4693.7 | 4704.5 | 4715.3 | 4726.1 | 4736.9 | 4747.7 | 4758.5 | 47694 |
| 88 | 4780.2 | 4791.1 | 4802.0 | 4812.9 | 4823.8 | 4834.7 | 4845.7 |  | 4867 | . 5 |
| 89 | 4889.5 | 4900.5 | 4911.5 | 4922.5 | 4933.6 | 4944.6 | 4955.7 | 4966.7 | 4977.8 | 4988.9 |
| 90 | 5000.0 | 5011.1 | 50 | 5033.4 | 50 | 5055.7 | 5066.9 | 5078.1 | 5089.3 | 5100.5 |
| 91 | 5111.7 | 5123.0 | 5134. | 5145.5 | 5156.8 | 51 | 5179.4 | 5190.7 | 5202 | 5213.3 |
| 92 | 5224.7 | 5236.1 | 5247.4 | 5258.8 | 5270.2 | 5281.6 | 5293.1 | 5304.5 | 5316.0 | 5327.4 |
| 93 | 5338.9 | 5350.4 | 5361.9 | 5373.4 | 5384.9 | 5396.5 | 5408.0 | 5419.6 | 5431.1 | 5442.7 |
| 94 | 5454.3 | 5465.9 | 5477.6 | 5489.2 | 5500.8 | 55 J2.5 | 5524.2 | 5535.9 | 5547.6 | 5559.3 |
| 95 | 5571.0 | 5582.7 | 5594.5 | 5606.2 | 5618.0 | 5629.8 | 5641.6 | $5653 \cdot 4$ | 5665.2 | 5677.0 |
| 96 | 5683.9 | 5700.7 | 5712.6 | 5724.5 | 5736.4 | 5748.3 | 5760.2 | 5772.2 | 5784.1 | 5796.1 |
| 97 | 5808.0 | 5820.0 | 5832.0 | 5844.0 | 5856.0 | 5868.1 | 5880.1 | 5892.2 | 5904.2 | 5916.3 |
| 98 | 5928.4 | 5940.5 | 5952.6 | 5964.7 | 5976.9 | 5989.0 | 6001.2 | 6013.4 | 6025.6 | 6037.8 |
| 99 | 6050.0 | 6062.2 | 6074.5 | 6086.7 | 6099.0 | 6111.3 | 6123.6 | 6135.9 | 6148.2 | 6160.5 |
| 100 | 6172.8 | 6185.2 | 6197.6 | 6209.9 | 6222.3 | 6234.7 | 6247.1 | 6259.6 | 6272.0 | 6284 |
|  | 0 | I | . 2 | -3 | . 4 | . 5 | . 6 | . 7 | . 8 | 9 |

TABLE No. 6.-Level Cuttings. $\frac{s+8^{\prime}}{2}=\frac{1}{5} ; b=16$ feet.

| 菭 | . 0 | . 1 | . 2 | . 3 | . 4 | . 5 | . 6 | . 7 | . 8 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0.0 | 5.9 | 11.9 | 17.8 | 23.8 | 29.8 | 35.8 | 41 | 47.9 | 53.9 |
| 1 | 60.0 | 66.1 | 2 | 78.3 | 84.4 | 90.6 | 96.7 | 102.9 | 109.1 | 1 I 5.3 |
| 2 | 121.5 | 127.7 | 134.0 | 140.2 | 146.5 | 152.8 | 159.1 | 165.4 | 171.7 | 178.1 |
| 3 | 184.4 | 190.8 | 197.2 | 203.6 | 210.0 | 216.5 | 222.9 | 229.4 | 235.9 | 242.4 |
| 4 | 248.9 | 255.4 | 262.0 | 268.5 | 275.1 | 281.7 | 288.3 | 294.9 | 301.5 | 308.2 |
| 5 | 314.8 | 321.5 | 328.2 | 334.9 | 341.6 | 348.3 | 355.1 | 361.8 | 368.6 | 375.4 |
| 6 | 382.2 | 389.0 | 395.9 | 402.7 | 409.6 | 416.5 | 423.4 | 430.3 | 437.2 | $4+4.2$ |
| 7 | 451.1 | 458.1 | 465.I | 472.1 | 479.1 | 486.1 | 493.2 | 500.2 | 507.3 | 514.4 |
| 8 | 521.5 | 528.6 | 535.7 | 542.9 | 550.0 | 557.2 | 564.4 | 571.6 | 578.8 | 586.1 |
| 9 | - 593.3 | 600.6 | 607.9 | 615.2 | 622.5 | 629.8 | 637.2 | 644.5 | 651.9 | 659.3 |
| 10 | 666.7 | 674.1 | 681.5 | 689.0 | 696.4 | 703.9 | 711.4 | 718.9 | 726.4 | 733.9 |
| 11 | 741.5 | 749.0 | 756.6 | 764.2 | 771.8 | 779.4 | 787.1 | 794.7 | 802.4 | 8 IO .1 |
| 12 | 817.8 | 825.5 | 833.2 | 841.0 | 848.7 | 856.5 | 864.3 | 872.1 | 879.9 | 887.7 |
| 13 | 895.6 | 903.4 | 911.3 | 919.2 | 927.1 | 935.0 | 942.9 | 950.9 | 958.8 | 966.8 |
| 14 | 974.8 | 982.8 | 990.8 | 998.9 | 1007 | 1015 | 1023 | 103I | 1039 | 1047 |
| 15 | 1056 | 1064 | 1072 | 1080 | 1088 | 1096 | 1105 | III3 | 1121 | 1129 |
| 16 | II38 | 1146 | II54 | 1163 | 171 | 1179 | 1188 | 1196 | 1205 | 1213 |
| 17 | 1221 | 1230 | 1238 | 1247 | 1255 | 1264 | 1272 | 1281 | 1290 | 1298 |
| 18 | 1307 | 1355 | 1324 | 1333 | 1341 | 1350 | 1358 | 1367 | 1376 | 1385 |
| 19 | 1393 | 1402 | $1{ }_{4} 11$ | 1420 | 1428 | 1437 | 1446 | 1455 | 1464 | 1473 |
| 20 | 1482 | 1490 | 1499 | 1508 | 1517 | 1526 | 1535 | 1544 | ${ }_{1} 5$ | 1562 |
| 21 | 1571 | 1580 | 1589 | 1598 | 1607 | 1616 | 1626 | 1635 | I644 | r653 |
| 22 | 1662 | 1671 | 1681 | 1690 | 1699 | 1708 | 1718 | 1727 | 1736 | 1745 |
| 23 | 1755 | ${ }_{1764}$ | 1774 | 1783 | 1792 | 1802 | 1815 | 1821 | 1830 | 1839 |
| 24 | 1849 | 1858 | 1868 | 1877 | 1887 | 1896 | 1906 | 1916 | 1925 | 1935 |
| 25 | 1944 | 1954 | 1964 | 1973 | 1983 | 1993 | 2002 | 2012 | 2022 | 2032 |
| 25 | 2041 | 2051 | 2061 | 2071 | 2081 | 2091 | 2100 | 2110 | 2120 | 2130 |
| 27 | 2140 | 2150 | 2160 | 2170 | 2180 | 2190 | 2200 | Io | 22 | 2230 |
| 28 | 2240 | 2250 | 2260 | 2270 | 2280 | 2291 | 2301 | 2311 | 2321 | 2331 |
| 29 | 2341 | 2352 | 2362 | 2372 | 2382 | 2393 | 2403 | 2413 | 2424 | 2434 |
| 30 | 2444 | 2455 | 2465 | 2476 | 2486 | 2496 | 2507 | 2517 | 2528 | 2538 |
| 31 | 2549 | 2559 | 2570 | 2581 | 2591 | 2602 | 2612 | 2623 | 2634 | 2644 |
| 32 | 2655 | 2665 | 2676 | 2687 | 2698 | 2708 | 2719 | 2730 | 2741 | 2751 |
| 33 | 2762 | 2773 | 2784 | 2795 | 2806 | 2816 | 2827 | 2838 | 2849 | 2860 |
| 34 | 2871 | 2882 | 2893 | 2904 | 2915 | 2926 | 2937 | 2948 | 2959 | 2970 |
| 35 | 2981 | 2993 | 3004 | 3015 | 3025 | 3037 | 3048 | 3060 | 3071 | 3082 |
| 35 | 3093 | 3105 | 3116 | 3127 | 3138 | 3150 | 3161 | 3173 | 3184 | 3195 |
| 37 | 3207 | 3218 | 3230 | 3241 | 3252 | 3264 | 3275 | 3287 | 3298 | 3310 |
| 38 | 3321 | 3333 | 3345 | 3356 | 3368 | 3379 | 3391 | 3403 | 3414 | 3426 |
| 39 | 3438 | 3449 | 3461 | 3473 | 3485 | 3496 | 3508 | 3520 | 3532 | 3544 |
| 40 | 3556 | 3567 | 3579 | 3581 | 3593 | 3605 | 3617 | 3629 | 3641 | 3653 |
| 41 | 3675 | 3687 | 3699 | 3711 | 3723 | 3735 | 3747 | 3759 | 3771 | 3783 |
| 42 | 3796 | 3808 | 3820 | 3832 | 3844 | 3856 | 3869 | 388 I | 3893 | 3905 |
| 43 | 3918 | 3930 | 3942 | 3955 | 3967 | 3979 | 3992 | 4004 | 4017 | 4029 |
| 44 | 4041 | 4054 | 4066 | 4079 | 4091 | 4104 | 4116 | 4129 | 4142 | 4154 |
| 45 | 4167 | 4179 | 4192 | 4205 | 4217 | 4230 | 4242 | 4255 | 4268 | 428 I |
| 46 | 4293 | 4306 | 4319 | 4332 | 4344 | 4357 | 4370 | 4383 | 4396 | 4409 |
| 47 | 442 I | 4434 | 4447 | 4460 | 4473 | 4486 | 4499 | 4512 | 4525 | 4538 |
| 48 | 4551 | 4564 | 4577 | 4590 | 4603 | 4616 | 4630 | 4643 | 4656 | 4669 |
| 49 | 4682 | 4695 | 4709 | 4722 | 4735 | 4748 | 4762 | 4775 | 4788 | 4801 |
| 50 | 4815 | 4828 | 4842 | 4855 | 4868 | 4882 | 4895 | 4909 | 4922 | 4935 |
| 51 | 4949 | 4962 | 4976 | 4989 | 5003 | 5016 | 5030 | 5044 | 5057 | 5071 |
| 52 | 5084 | 5098 | 5112 | 5125 | 5139 | 5153 | 5166 | 5180 | 5194 | 5208 |
| 53 | 5221 | 5235 | 5249 | 5263 | 5277 | 5291 | 5304 | 5318 | 5332 | 5346 |
| 54 | 5360 | 5374 | 5388 | 5402 | 5416 | 5430 | 5444 | 5458 | 5472 | 5486 |
| 55 | 5500 | 5514 | 5528 | 5542 | 5556 | 5571 | 5585 | 5599 | 5613 | 5627 |
| 56 | 5641 | 5656 | 5670 | 5684 | 5698 | 5713 | 5727 | 5741 | 5756 | 5770 |
| 57 | 5784 | 5799 | 5813 | 5828 | 5842 | 5856 | 5871 | 5885 | 5900 | 5914 |
| 58 | 5929 | 5943 | 5958 | 5973 | 5987 | 6002 | 6016 | 603 I | 6046 | 6060 |
| 59 | 6075 | 6089 | 6104 | 6119 | 6134 | 6148 | 6163 | 6178 | 6193 | 6207 |
| 60 | 6222 | 6237 | 6252 | 6267 | 6282 | 6296 | 63 II | 6326 | 634 I | 6356 |
|  | . 0 | . 1 | . 2 | $\cdot 3$ | . 4 | . 5 | . 6 | . 7 | . 8 | . 9 |

TABLE No. 7.-Level Cuttings. $\frac{8+8^{\prime}}{2}=\frac{1}{5} ; b=28$ feet.

| 江 | . 0 | . 1 | . 2 | . 3 | . 4 | . 5 | . 6 | . 7 | . 8 | . 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | . | 10.4 | 20.8 | 31.2 | 41.6 | 52.0 | 62.5 | 73.0 | 83.4 | 93.9 |
| 1 | 104.4 | 115.0 | 125.5 | 136.1 | 146.6 | 157.2 | 167.8 | 178.4 | 189.1 | 199.7 |
| 2 | 210.4 | 221.0 | 231.7 | 242.4 | 253.2 | 263.9 | 274.6 | 285.4 | 296.2 | 307.0 |
| 3 | 317.8 | 328.6 | 339.4 | 350.3 | 361.2 | 372.0 | 382.9 | 393.8 | 404.8 | 415.7 |
| 4 | 426.7 | 437.6 | 448.6 | 459.6 | 470.6 | 481.7 | 492.7 | 503.8 | 514.8 | 525.9 |
| 5 | 537.0 | 548.2 | 559.3 | 570.4 | 581.6 | 592.8 | 604.0 | 615.2 | 626.4 | 637.6 |
| 6 | 648.9 | 660.2 | 671.4 | 682.7 | 694.0 | 705.4 | 716.7 | 728.1 | 739.4 | 750.8 |
| 7 | 762.2 | 773.6 | 785.1 | 796.5 | 808.0 | 819.4 | 830.9 | 842.4 | 854.0 | 865.5 |
| 8 | 877.0 | 888.6 | 900.2 | 911.8 | 923.4 | 935.0 | $9+6.6$ | 958.3 | 970.0 | 981.6 |
| 9 | 993.3 | 1005 | 1017 | 1029 | 1040 | 1052 | 1064 | 1076 | 1087 | 1099 |
| 10 | IIII | 1123 | 1135 | 1147 | 1159 | 1171 | 1182 | 1194 | 1206 | 1218 |
| 11 | 1230 | 1242 | 1254 | 1266 | 1278 | 1291 | 1303 | 1315 | 1327 | 1339 |
| 12 | 1351 | 1363 | 1375 | 1388 | 1400 | 1412 | 1424 | 1437 | 1449 | 1461 |
| 13 | 1473 | 1486 | 1498 | 1510 | 1523 | 1535 | 1547 | 1560 | 1572 | 1585 |
| 14 | 1597 | 1609 | 1622 | 1634 | 1647 | 1659 | 1672 | 1685 | 1697 | 1710 |
| 15 | 1722 | 1735 | 1747 | 1760 | 1773 | 1785 | 1798 | 1811 | 1823 | 1836 |
| 16 | 1849 | 1862 | 1874 | 1887 | 1900 | 1913 | 1926 | 1938 | 1951 | 1964 |
| 17 | 1977 | 1990 | 2003 | 2016 | 2029 | 2042 | 2055 | 2068 | 2081 | 2094 |
| 18 | 2107 | 2120 | 2133 | 2146 | 2159 | 2172 | 2185 | 2198 | 2211 | 2225 |
| 19 | 2238 | 2251 | 2264 | 2277 | 2291 | 2304 | 2317 | 2330 | 2344 | 2357 |
| 20 | 2370 | 2384 | 2397 | 2410 | 2424 | 2437 | 2451 | 2464 | 2478 | 2491 |
| 21 | 2504 | 2518 | 2531 | 2545 | 2558 | 2572 | 2586 | 2599 | 2613 | 2626 |
| 22 | 2640 | 2654 | 2667 | 2681 | 2695 | 2708 | 2722 | 2736 | 2750 | 2763 |
| 23 | 2777 | 2791 | 2805 | 2818 | 2832 | 2846 | 2860 | 2874 | 2888 | 2902 |
| 24 | 2916 | 2929 | 2943 | 2957 | 2971 | 2985 | 2999 | 3013 | 3027 | 3041 |
| 25 | 3056 | 3070 | 3084 | 3098 | 3112 | 3126 | 3140 | 3154 | 3169 | 3183 |
| 26 | 3197 | 3211 | 3226 | 3240 | 3254 | 3268 | 3283 | 3297 | 3311 | 3326 |
| 27 | 3340 | 3354 | 3369 | 3383 | 3398 | $3+12$ | 3426 | 344 I | 3455 | 3470 |
| 28 | $34^{8+}$ | 3499 | 3514 | 3528 | 3543 | 3557 | 3572 | 3586 | 3601 | 3616 |
| 29 | 3630 | 3645 | 3660 | 3674 | 3689 | 3704 | 3719 | 3733 | $374{ }^{8}$ | 3763 |
| 30 | 3778 | 3793 | 3807 | 3822 | 3537 | 3852 | 3867 | 3882 | 3897 | 3912 |
| 31 | 3927 | 3942 | 3957 | 3972 | 3987 | 4002 | 4017 | 4032 | 4047 | 4062 |
| 32 | 4077 | 4092 | 4107 | 4122 | 4138 | 4153 | 4168 | 4183 | 4193 | 4214 |
| 33 | 4229 | 4244 | 4259 | 4275 | 4290 | 4305 | 4321 | 4336 | 4351 | 4367 |
| 34 | 4332 | 4393 | $4{ }^{1} 3$ | 4429 | 4444 | 4459 | 4475 | 4490 | 4506 | 4521 |
| 35 | 4537 | 4553 | 4568 | $45^{8} 4$ | 4599 | 4615 | 4631 | 4646 | 4662 | 4678 |
| 36 | 4693 | 4709 | 4725 | 4741 | 4756 | 4772 | 4788 | 4804 | 4819 | 4835 |
| 37 | 4851 | 4867 | 4883 | 4899 | 4915 | 493 I | 4946 | 4962 | 4978 | 4994 |
| 38 | 5010 | 5026 | 5042 | 5058 | 5074 | 5091 | 5107 | 5123 | 5139 | 5155 |
| 39 | 5171 | 5187 | 5203 | 5220 | 5236 | 5252 | 5268 | 5285 | 5301 | 5317 |
| 40 | 5333 | 5350 | 5366 | 5382 | 5399 | 5415 | 5431 | 5448 | $546+$ | 5481 |
| 41 | 5497 | 5513 | 5530 | 5546 | 5563 | 5579 | 5596 | 5613 | 5629 | 5646 |
| 42 | 5662 | 5679 | 5695 | 5712 | 5729 | 5745 | 5762 | 5779 | 5795 | 5812 |
| 43 | 5829 | $5{ }^{5} 46$ | 5862 | 5879 |  | 5913 | 5930 | 5946 | 5963 | 5980 |
| 44 | 5997 | 6014 | 6031 | 6048 | 6065 | 6082 | 6099 | 6116 | 6133 | 6150 |
| 45 | 6167 | $618+$ | 6201 | 6218 | 6235 | 6252 | 6269 | 6286 | 6303 | 6321 |
| 46 | 6338 | 6355 | 6372 | 6389 | 6407 | 6424 | 644 I | 6458 | 6476 | 6493 |
| 47 | 6510 | 6528 | 6545 | 6562 | 6580 | 6597 | 6615 | 6632 | 6650 | 6667 |
| 48 | $66{ }_{4}$ | 6702 | 6719 | 6737 | $675+$ | 6772 | 6790 | 6807 | 6825 | 6842 |
| 49 | 6860 | 6878 | 6895 | 6913 | 6931 | 6948 | 6966 | 6984 | 7002 | 7019 |
| 50 | 7037 | 7055 | 7073 | 7090 | 7108 | 7126 | 7144 | 7162 | 7180 | 7198 |
| 51 | 7216 | 7233 | 7251 | 7269 | 7287 | 7305 | 7323 | 7341 | 7359 | 7377 |
| 52 | 7396 | 7414 | 7432 | 7450 | 7468 | 7486 | 7504 | 7522 | 7541 | 7559 |
| 53 | 7577 | 7595 | 7614 | 7632 | 7650 | 7668 | 7687 | 7705 | 7723 | 7742 |
| 54 | 7760 | 7778 | 7797 | 7815 | 7834 | 7852 | 7870 | 7889 | 7907 | 7926 |
| 55 | 7944 | 7963 | 7982 | 8000 | 8019 | 8037 | 8056 | 8074 | 8093 | 8 II 2 |
| 56 | 8130 | 8 r 49 | 8168 | 8186 | 8205 | 8224 | 82.43 | 8261 | 8280 | 8299 |
| 57 | 8318 | 8337 | 8355 | 8374 | 8393 | 8412 | 843I | 8450 | 8469 | 8488 |
| 58 | 8507 | 8526 | S545 | 8564 | 8583 | 8602 | 8621 | 8640 | 8659 | 8678 |
| 59 | 8697 | 8716 | 8735 | 8754 | 8774 | 8793 | 8812 | 8831 | 8850 | 8870 |
| 60 | 8889 | 8908 | 8927 | 8947 | 8966 | 8985 | 9005 | 9024 | 9043 | 9063 |
|  | . 0 | . 1 | . 2 | .3 | . 4 | . 5 | . 6 | . 7 | . 8 | . 9 |

TABLE No. 8.

## Plus Corrections for $\frac{s+s^{\prime}}{2}=\frac{1}{5}$.

| $\left[\begin{array}{c}  \pm \\ \hline \\ \text { H } \end{array}\right.$ | 0. | 1. | 2. | 3. | 4. | 5. | 6. | 7. | 8. | 9. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.1 |
| 1 | 0.1 | O.I | 0.1 | 0.1 | 0.1 | 0.1 | 0.2 | 0.2 | 0.2 | 0.2 |
| 2 | 0.3 | 0.3 | 0.3 | 0.3 | 0.4 | 0.4 | 0.4 | 0.5 | 0.5 | 0.5 |
| 3 | 0.6 | 0.6 | 0.6 | 0.7 | 0.7 | 0.8 | 0.8 | 0.9 | 0.9 | 0.9 |
| 4 | 1.0 | 1.0 | I.I | I.I | 1.2 | 1.3 | 1.3 | 1.4 | 1.4 | 1.5 |
| 5 | 1.5 | 1.6 | 1.7 | 1.7 | I. 8 | 1.9 | 1.9 | 2.0 | 2.1 | 2.2 |
| 6 | 2.2 | 2.3 | 2.4 | 2.5 | 2.5 | 2.6 | 2.7 | 2.8 | 2.9 | 2.9 |
| 7 | 3.0 | 3.1 | 3.2 | $3 \cdot 3$ | $3 \cdot 4$ | 3.5 | 3.6 | 3.7 | 3.8 | 3.9 |
| 8 | 4.0 | 4.1 | 4.2 | $4 \cdot 3$ | 4.4 | 4.5 | 4.6 | 4.7 | 4.8 | 4.9 |
| 9 | 5.0 | 5.1 | 5.2 | $5 \cdot 3$ | 5.5 | 5.6 | $5 \cdot 7$ | 5.8 | 5.9 | 6.1 |
| 10 | 6.2 | 6.3 | 6.4 | 6.6 | 6.7 | 6.8 | 6.9 | 7.1 | 7.2 | 7.3 |
| 11 | $7 \cdot 5$ | 7.6 | $7 \cdot 7$ | 7.9 | 8.0 | 8.2 | 8.3 | 8.5 | 8.6 | 8.7 |
| 12 | 8.9 | 9.0 | 9.2 | 9.3 | 9.5 | 9.7 | 9.8 | 10.0 | 10.1 | 10.3 |
| 13 | 10.4 | 10.6 | 10.8 | 10.9 | II. 1 | 11.3 | 11.4 | 11.6 | 11.8 | 11.9 |
| 14 | I2.I | 12.3 | 12.5 | 12.6 | 12.8 | 13.0 | 13.2 | 13.3 | 13.5 | 13.7 |
| 15 | I3.9 | 14.1 | 14.3 | 14.5 | I 4.6 | 14.8 | 15.0 | 15.2 | 15.4 | 15.6 |
| 16 | 15.8 | 16.0 | 16.2 | 16.4 | 16.6 | 16.8 | 17.0 | 17.2 | 17.4 | 17.6 |
| 17 | 17.8 | 18.1 | 18.3 | 18.5 | 18.7 | 18.9 | I9.I | 19.3 | 19.6 | 19.8 |
| 18 | 20.0 | 20.2 | 20.5 | 20.7 | 20.9 | 21.1 | 2 I .4 | 21.6 | 21.8 | 22.1 |
| 19 | 22.3 | 22.5 | 22.8 | 23.0 | 23.2 | 23.5 | 23.7 | 24.0 | 24.2 | 24.5 |
| 20 | - 24.7 | 24.9 | 25.2 | 25.4 | 25.7 | 25.9 | 26.2 | 26.5 | 26.7 | 27.0 |
| 21 | 27.2 | 27.5 | 27.7 | 28.0 | 28.3 | 28.5 | 28.8 | 29.1 | 29.3 | 29.6 |
| 22 | 29.9 | 30.2 | 30.4 | 30.7 | 31.0 | 3 I .3 | 31.5 | 31.8 | 32.1 | 32.4 |
| 23 | 32.7 | 32.9 | 33.2 | 33.5 | 33.8 | 34. 1 | 34.4 | 34.7 | 35.0 | 35.3 |
| 24 | 35.6 | 35.9 | 36.2 | 36.5 | 36.8 | 37.1 | 37.4 | 37.7 | 38.0 | 38.3 |
| 25 | 38.6 | 38.9 | 39.2 | 39.5 | 39.8 | 40.1 | 40.5 | 40.8 | 41.1 | 41.4 |
| 26 | 41.7 | 42.1 | 42.4 | 42.7 | 43.0 | 43.4 | 43.7 | 44.0 | 44.3 | 44.7 |
| 27 | 45.0 | 45.3 | 45.7 | 46.0 | 46.3 | 46.7 | 47.0 | 47.4 | 47.7 | 48.1 |
| 28 | 48.4 | 48.7 | 49.1 | 49.4 | 49.8 | 50.1 | 50.5 | 50.9 | 5 I .2 | 51.6 |
| 29 | 51.9 | 52.3 | 52.6 | 53.0 | 53.4 | 53.7 | 54.1 | 54.5 | 54.8 | 55.2 |
| 30 | 55.6 | 55.9 | 56.3 | 56.7 | 57.1 | 57.4 | 57.8 | 58.2 | 58.6 | 58.9 |
| 31 | 59.3 | 59.7 | 60.1 | 60.5 | 60.9 | 61.3 | 61.6 | 62.0 | 62.4 | 62.8 |
| 32 | 63.2 | 63.6 | 64.0 | 6.4 .4 | 64.8 | 65.2 | 65.6 | 66.0 | 66.4 | 66.8 |
| 33 | 67.2 | 67.6 | 68.0 | 68.5 | 68.9 | 69.3 | 69.7 | 70.1 | 70.5 | 70.9 |
| 34 | 71.4 | 71.8 | 72.2 | 72.6 | 73.1 | 73.5 | 73.9 | 74.3 | 74.8 | 75.2 |
| 35 | 75.6 | 76.1 | 76.5 | 76.9 | 77.4 | 77.8 | 78.2 | 78.7 | 79.1 | 79.6 |
| 36 | 80.0 | 80.5 | 80.9 | 8 I .3 | 8 I .8 | 82.2 | 82.7 | 83.1 | 83.6 | 84.1 |
| 37 | 84.5 | 85.0 | 85.4 | 85.9 | 86.3 | 86.8 | 87.3 | 87.7 | 88.2 | 88.7 |
| 38 | 89.1 | 89.6 | 90.1 | 90.6 | 91.0 | 9 I .5 | 92.0 | 92.5 | 92.9 | 93.4 |
| 39 | 93.9 | 94.4 | 94.9 | 95.3 | 95.8 | 96.3 | 96.8 | 97.3 | 97.8 | 98.3 |
| 40 | 98.8 | 99.3 | 99.8 | 100.3 | 100.8 | 101.3 | 101. 8 | 102.3 | 102.8 | 103.3 |
|  | 0. | I. | 2. | 3. | 4. | 5. | 6. | 7. | 8. | 9. |

Note.-The quantities in the above table multiplied by 2 give the minus corrections for $\frac{8+8^{\circ}}{2}=\frac{1}{5}$.

TABLE No. 9.-Level Cutimgs. $\frac{8+8^{\prime}}{2}=\frac{1}{2} ; b=16$ feet.

| 易 | 0. | 1. | 2. | 3. | 4. | 5. | 6. | 7. | 8. | 9. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0.0 | 5.9 | 11.9 | 17.9 | 24.0 | 30.1 | 36.2 | 42.4 | 48.6 | 54.8 |
| 1 | 61.1 | 67.4 | 73.8 | 80.2 | 86.6 | 93.1 | 99.6 | 106.1 | 112.7 | I 19.3 |
| 2 | 125.9 | 132.6 | 139.3 | 146.1 | - 1529 | 159.7 | 166.6 | 173.5 | 180.4 | 187.4 |
| 3 | 194.4 | 201.5 | 208.6 | 215.7 | 222.9 | 230.1 | 237.3 | 244.6 | 251.9 | 259.3 |
| 4 | 266.7 | 274.1 | 281.6 | 289.1 | 296.6 | 304.2 | 311.8 | 319.4 | 327.1 | 334.8 |
| 5 | 342.6 | 350.4 | 358.2 | 366.1 | 374.0 | 381.9 | 389.9 | 397.9 | 406.0 | 414.1 |
| 6 | 422.2 | 430.4 | 438.6 | 446.8 | 455.I | 463.4 | 471.8 | 480.2 | 488.6 | 497.1 |
| 7 | 505.6 | 514.1 | 522.7 | 531.3 | 539.9 | 548.6 | 557.3 | 566.1 | 574.9 | 583.7 |
| 8 | 592.6 | 601.5 | 610.4 | 6 I 9.4 | 628.4 | 637.5 | 646.6 | 655.7 | 664.9 | 674.1 |
| 9 | 683.3 | 692.6 | 701.9 | 711.3 | 720.7 | 730.1 | 739.6 | 749.1 | 758.6 | 768.2 |
| 10 | 777.8 | 787.4 | 797.1 | 806.8 | 816.6 | 826.4 | 836.2 | 846.I | 856.0 | 865.9 |
| II | 875.9 | 885.9 | 896.0 | 906.1 | 916.2 | 926.4 | 936.6 | 946.8 | 957.1 | 967.4 |
| 12 | 977.8 | 988.2 | 998.6 | 1009 | 1020 | 1030 | 1041 | 1051 | 1062 | 1073 |
| 13 | IOS3 | 1094 | 1105 | 1116 | 1127 | 1138 | 1148 | II59 | 1170 | 1182 |
| 14 | 1193 | 1204 | 1215 | 1226 | 1237 | 1249 | 1260 | 1271 | 1283 | 1294 |
| 15 | 1306 | 1317 | 1329 | 1340 | 1352 | 1363 | 1375 | 1387 | 1399 | 1410 |
| 16 | 1422 | 1434 | 1446 | 1458 | 1470 | 1482 | 1494 | 1506 | 1518 | 1530 |
| 17 | 1543 | I 555 | 1567 | 1579 | 1592 | 1604 | 1617 | 1629 | 1642 | 1654 |
| 18 | 1667 | 1679 | 1692 | 1705 | 1717 | 1730 | 1743 | 1756 | 1769 | 1782 |
| 19 | 1794 | 1807 | 1820 | 1834 | 1847 | 1860 | 1873 | 1886 | 1899 | 1913 |
| 20 | 1926 | 1939 | 1953 | 1966 | 1980 | 1993 | 2007 | 2020 | 2034 | 2047 |
| 21 | 2061 | 2075 | 2089 | 2102 | 2116 | 2130 | 2144 | 2158 | 2172 | 2186 |
| 22 | 2200 | 2214 | 2228 | 2242 | 2257 | 2271 | 2285 | 2299 | 2314 | 2328 |
| 23 | 2343 | 2357 | 2372 | 2386 | 2401 | 2415 | 2430 | 2445 | 2459 | 2474 |
| 24 | 2489 | 2504 | 2519 | 2534 | 2548 | 2563 | 2578 | 2594 | 2609 | 2624 |
| 25 | 2639 | 2654 | 2669 | 2685 | 2700 | 2715 | 2731 | 2746 | 2762 | 2777 |
| 26 | 2793 | 2808 | 2824 | 2839 | 2855 | 2371 | 2887 | 2902 | 2918 | 2934 |
| 27 | 2950 | 2966 | 2982 | 2998 | 3014 | 3030 | 3046 | 3062 | 3079 | 3095 |
| 28 | 3111 | 3127 | 3144 | 3160 | 3177 | 3193 | 3210 | 3226 | 3243 | 3259 |
| 29 | 3276 | 3293 | 3309 | 3326 | 3343 | 3360 | 3377 | 3394 | 3410 | 3427 |
| 30 | 3444 | 3462 | 3479 | 3496 | 3513 | 3530 | 3547 | 3565 | 3582 | 3599 |
| 31 | 3617 | 3634 | 3652 | 3669 | 3687 | 3704 | 3722 | 3739 | 3757 | 3775 |
| 32 | 3793 | 3810 | 3828 | 3846 | 3864 | 3882 | 3900 | 3918 | 3936 | 3954 |
| 33 | 3972 | 3990 | 4009 | 4027 | 4045 | 4063 | 4082 | 4100 | 4119 | 4137 |
| 34 | 4156 | 4174 | 4193 | 4211 | 4230 | 4249 | 4267 | 4286 | 4305 | 4324 |
| 35 | 4343 | 4362 | 4380 | 4399 | 4418 | 4438 | 4457 | 4476 | 4495 | 4514 |
| 36 | 4533 | 4553 | 4572 | 4591 | 4611 | 4630 | 4650 | 4669 | 4689 | 4708 |
| 37 | 4728 | 4747 | 4767 | 4787 | 4807 | 4826 | 4846 | 4866 | 4886 | 4906 |
| 38 | 4926 | 4946 | 4966 | 4986 | 5006 | 5026 | 5047 | 5067 | 5087 | 5107 |
| 39 | 5128 | 5148 | 5169 | 5 I 89 | 5210 | 5230 | 5251 | 5271 | 5292 | 5313 |
| 40 | 5333 | 5354 | 5375 | 5396 | 5417 | 5438 | 5458 | 5479 | 5500 | 5522 |
| 41 | 5543 | 5564 | 5585 | 5606 | 5627 | 5649 | 5670 | 5691 | 5713 | 5734 |
| 42 | 5756 | 5777 | 5799 | 5820 | 5842 | 5863 | 5885 | 5907 | 5929 | 5950 |
| 43 | 5972 | 5994 | 6016 | 6038 | 6060 | 6082 | 6104 | 6126 | 6148 | 6170 |
| 44 | 6193 | 6215 | 6237 | 6259 | 6282 | 6304 | 6327 | 6349 | 6372 | 6394 |
| 45 | 6417 | 6439 | 6462 | 6485 | 6507 | 6530 | 6553 | 6576 | 6599 | 6622 |
| 46 | 6644 | 6667 | 6690 | 6714 | 6737 | 6760 | 6783 | 6806 | 6829 | 6853 |
| 47 | 6876 | 6899 | 6923 | 6946 | 6970 | 6993 | 7017 | 70.40 | 7064 | 7087 |
| 48 | 7111 | 7135 | 7159 | 7182 | 7206 | 7230 | 7254 | 7278 | 7302 | 7326 |
| 49 | 7350 | 7374 | 7398 | 7422 | 7447 | 7471 | 7495 | 7519 | 75.4 | 7568 |
| 50 | 7593 | 7617 | 7642 | 7666 | 7691 | 7715 | 7740 | 7765 | 7789 | 7814 |
| 51 | 7839 | 7864 | 7889 | 7914 | 7938 | 7963 | 7988 | 8014 | 8039 | 8064 |
| 52 | 8089 | 8114 | 8139 | 8 I 65 | 8 I 90 | 8215 | 8241 | 8266 | 8292 | 8317 |
| 53 | 8343 | 8368 | 8394 | 8419 | 8445 | 8471 | 8497 | 8522 | 8548 | 8574 |
| 54 | 8600 | 8626 | 8652 | 8678 | 8704 | 8730 | 8756 | 8782 | 8809 | 8835 |
| 55 | 8861 | 8887 | 8914 | 8940 | 8967 | 8993 | 9020 | 9046 | 9073 | 9099 |
| 56 | 9126 | 9153 | 9179 | 9206 | 9233 | 9260 | 9287 | 9314 | 9340 | 9367 |
| 57 | 9394 | 9422 | 9449 | 9476 | 9503 | 9530 | 9557 | 9585 | 9612 | 9639 |
| 58 | 9667 | 9694 | 9722 | 9749 | 9777 | 9804 | 9832 | 9859 | 9887 | 9915 |
| 59 | 9943 | 9970 | 9998 | 10026 | 10054 | 10082 | IOIIO | IOI 38 | 10166 | 10194 |
| 60 | 10222 | 10250 | 10279 | 10307 | 10335 | 10363 | 10392 | 10420 | 10449 | 10477 |
|  | . 0 | . 1 | . 2 | . 3 | . 4 | . 5 | . 6 | . 7 | . 8 | . 9 |

TABLE No. 10.-Level Cuttivgs. $\frac{s+s^{\prime}}{2}=\frac{1}{2} ; b=28$ fcet.

| 2 | . 0 | I | . 2 | . 3 | . 4 | . 5 | . 6 | . 7 | . 8 | . 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| - | O. |  | . 8 | 31.3 | 41.8 | 52.3 | 62.9 | 73.5 | 84.1 | 94.8 |
| 1 | 105.6 | 116.3 | 127.1 | 137.9 | 148.8 | 159.7 | 170.7 | 18 I .6 | 192.7 | 203.7 |
| 2 | 214.8 | 225.9 | 37.1 | 248.3 | 259.6 | 270.8 | 282.1 | 293.5 | 304.9 | 316.3 |
| 3 | 327.8 | 339.3 | 350.8 | 362.4 | 374.0 | 385.6 | 397.3 | 409.1 | 420.8 | 432.6 |
| 4 | 444.4 | 456.3 | 468 | 480.2 | 492.1 | 504.2 | 516.2 | 528.3 | 540.4 | 552.6 |
| 5 | 56 | 577.I | 589.3 | 601. 6 | 614.0 | 626.4 | 638.8 | 651.3 | 663.8 | 676.3 |
| 6 | 688.9 | 701.5 | 714.1 | 7268 | 739.6 | 752.3 | 765.r | 777.9 | 790.8 | 803.7 |
|  | 816.7 | 829.6 | 842.7 | 855.7 | 868.8 | 881.9 | 895.1 | 908.3 | 921.6 | 934.8 |
| 8 | 948.I | 96 I .5 | 974.9 | 988.3 | 1002 | 1015 | 1029 | 1042 | 1056 | 1070 |
| 9 | 1083 | 1097 | 111 | 1125 | I138 | 1152 | 1166 | 1180 | 1194 | 1208 |
| 10 | 1222 | 1236 | 1250 | 1265 | 279 | 1393 | 1307 | 322 | 1336 | 350 |
| 11 | 1365 | 1379 | 1394 | 1408 | ${ }_{1}^{1} 423$ | + 438 | 1452 | 1467 | I482 | 1496 |
| 12 | 1511 | 1526 | 1541 | 1556 | Í571 | 1586 | ( | 1616 | 1631 | 1646 |
| 13 | 1661 | 1676 | 1692 | 1707 | 1722 | 1738 | 1753 | 1768 | 1784 | 1799 |
| 14 | 1815 | 1830 | 1846 | 1862 | 1877 | I893 | 1909 | 1925 | 1940 | 956 |
| 15 | 1972 | 1988 | 2004 | 2020 | 2036 | 2052 | 2068 | 2085 | 2101 | 117 |
| 16 | 2133 | 2150 | 2166 | 2182 | 2199 | 2215 | 2232 | 2246 | 2265 | 2282 |
| 17 | 2298 | 2315 | 2332 | 2348 | 2365 | 2382 | 2399 | 2416 | $2+33$ | 2450 |
| 18 | 2467 | 2484 | 2501 | 2518 | 2535 | 2552 | 2570 | 2587 | 2604 | 2622 |
| 19 | 2639 | 2656 | 2674 | 2691 | 2709 | 2726 | 2744 | 2762 | 2779 | 2797 |
| 20 | 2815 | 2833 | 2850 | 2868 | 2886 | 2904 | 2922 | 2940 | 2958 | 2976 |
| 2 I | 2994 | 3013 | 3031 | 3049 | 3067 | 3086 | 3104 | 3122 | 314 I | 3159 |
| 22 | 3178 | 3196 | 3215 | 3234 | 3252 | 3271 | 3290 | 3308 | 3327 | 3346 |
| 23 | 3365 | 3384 | 3403 | 3422 | 3441 | $3+60$ | 3479 | 3498 | 3517 | 3536 |
| 24 | 3556 | 3575 | 3594 | 3614 | 3633 | 3652 | 3672 | 3691 | 3711 | 3730 |
| 25 | 3750 | 3770 | 3789 | 3809 | 3829 | 3849 | 3868 | 3888 | 3908 | 3928 |
| 25 | 3946 | 3968 | 3988 | 4008 | 4028 | 4049 | 4069 | 4089 | 4109 | 4130 |
| 27 | 4150 | 4170 | 4191 | 4211 | 4232 | 4252 | 4273 | 4294 | 4314 | 4335 |
| 28 | 4356 | 4376 | 4397 | 4418 | 4439 | 4460 | 448 I | 4502 | 4523 | 4544 |
| 29 | 4565 | 4586 | 4607 | 4628 | 4650 | 4671 | 4692 | 4714 | 4735 | 4756 |
| 30 | 4778 | 4799 | 4821 | 4842 | 4864 | 4886 | 4907 | 4929 | 4951 | 4973 |
| 31 | 4994 | 5016 | 5038 | 5060 | 5082 | $5 \mathrm{IO}_{4}$ | 5126 | 5148 | 5170 | 5193 |
| 32 | 5215 | 5237 | 5259 | 5282 | 5304 | 5326 | 5349 | 5371 | 5394 | 5416 |
| 33 | 5439 | 5462 | 5484 | 5507 | 5530 | 5552 | 5575 | 5598 | 5621 | 5644 |
| 34 | 5667 | 5690 | 5713 | 5736 | 5759 | 5782 | 5805 | 5828 | 5852 | 5875 |
| 35 | 5898 | 5922 | 5945 | 5968 | 5992 | 6015 | 6039 | 6062 | 6086 | 6110 |
| 36 | 6133 | 6157 | 6181 | 6205 | 6228 | 6252 | 6276 | 6300 | 6324 | 6348 |
| 37 | 6372 | 6396 | 6420 | 6445 | $6+69$ | 6493 | 6517 | 6542 | 6566 | 6590 |
| 38 | 6615 | 6639 | 6664 | 6688 | 6713 | 6738 | 6762 | 6787 | 6812 | 6836 |
| 39 | 6861 | 6886 | 6911 | 6936 | 6961 | 6986 | 7011 | 7036 | 7061 | 7086 |
| 40 | 7111 | 7136 | 7162 | 7187 | 7212 | 7238 | 7263 | 7288 | 7314 | 7339 |
| 41 | 7365 | 7390 | 7416 | 7442 | 7467 | 7493 | 7519 | 7545 | 7570 | 7596 |
| 42 | 7622 | 7648 | 7674 | 7700 | 7726 | 7752 | 7778 | 7805 | 7831 | 7857 |
| 43 | 7883 | 7910 | 7936 | 7962 | 7989 | 8015 | 8042 | 8068 | 8095 | 8122 |
| 44 | 8148 | 8175 | 8202 | 8228 | 8255 | 8282 | 8309 | 8336 | 8363 | 8390 |
| 45 | 8417 | 8444 | 8471 | 8498 | 8525 | 8552 | 8580 | 8607 | 8634 | 8662 |
| 46 | 8689 | 8716 | 8744 | 8771 | 8799 | 8826 | 8854 | 8882 | 8909 | 8937 |
| 47 | 8965 | 8993 | 902 | 9048 | 9076 | 9104 | 9132 | 9160 | 9188 | 9216 |
| 48 | 924 | 9273 | 9301 | 9329 | 9357 | 9386 | 9414 | 9442 | 9471 | 9499 |
| 49 | 9523 | 9556 | 9585 | 9614 | 9642 | 9671 | 9700 | 9728 | 9757 | 9786 |
| 5 | 9815 | 9844 | 9873 | 9902 | 9931 | 9960 | 9989 | 10018 | 10047 | 10076 |
| 5 | 10106 | IOJ 35 | 10164 | 10194 | 10223 | 10252 | 10282 | 103II | 10341 | 10370 |
| 52 | 10400 | 10430 | 10459 | 10489 | 10519 | IO549 | 10578 | 10608 | 10638 | 10668 |
| 53 | 10698 | 10728 | 10758 | 10788 | 10818 | 10849 | 10879 | 10909 | 10939 | 10970 |
| 54 | IIOOO | 11030 | 1106I | riogi | 11122 | III 15 | 11183 | I1214 | II244 | 11275 |
| 55 | 11306 | 11336 | 11367 | 11398 | 11429 | 11460 | II491 | 11522 | I1553 | 11584 |
| 56 | 11615 | 11646 | 11677 | 11708 | 11740 | 11771 | 11802 | 11834 | 11865 | 11896 |
| 57 | I1928 | I 1959 | II991 | 12022 | I2054 | 12086 | 12117 | 12149 | 1218I | 12213 |
| 58 | I2244 | 12276 | 12308 | 12340 | 12372 | 12404 | 12436 | 12468 | I2500 | 12533 |
| 59 | 12565 | 12597 | I2629 | I2662 | I2694 | 12726 | 12759 | 12791 | 12824 | I2856 |
| 60 | 12889 | 12922 | I2954 | 12987 | 13020 | 13052 | 13085 | 13118 | 13151 | 13184 |
|  | 0 | . 1 | . 2 | . 3 | . 4 | . 5 | . 6 | . 7 | . 8 | . 9 |

## TABLE No. 11.

Plus Corrections for $\frac{8+8^{8}}{2}=\frac{1}{2}$.

|  | . 0 | . 1 | . 2 | -3 | . 4 | . 5 | . 6 | . 7 | . 8 | . 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0. | 0. | 0. | 0. | 0. | o. | 0.1 | 0.1 | 0.1 | 0.1 |
| 1 | 0.2 | 0.2 | 0.2 | 0.3 | 0.3 | 0.3 | 0.4 | 0.4 | 0.5 | 0.6 |
| 2 | 0.6 | 0.7 | 0.7 | 0.3 | 0.9 | 1.0 | 1.0 | I.I | 1.2 | 1.3 |
| 3 | 1.4 | 1.5 | 1.6 | 1.7 | 1.8 | 1.9 | 2.0 | 2.1 | 2.2 | 2.3 |
| 4 | 2.5 | 2.6 | 2.7 | 2.9 | 3.0 | 3.1 | 3.3 | 3.4 | 3.6 | 3.7 |
| 5 | 3.9 | 4.0 | 4.2 | 4.3 | 4.5 | 4.7 | 4.8 | 5.0 | 5.2 | 5.4 |
| 6 | 5.6 | 5.7 | 5.9 | 6.1 | 6.3 | 6.5 | 6.7 | 6.9 | 7.1 | 7.3 |
| 7 | 7.6 | 7.8 | 8.0 | 8.2 | 8.5 | 8.7 | 8.9 | 9.1 | 9.4 | 9.6 |
| 8 | 9.9 | 10.1 | 10.4 | 10.6 | 10.9 | II.I | I 1.4 | 11.7 | 12.0 | 12.2 |
| 9 | 12.5 | 12.8 | 13.1 | 13.3 | 13.6 | 13.9 | 14.2 | 14.5 | 14.8 | 15.1 |
| 10 | 15.4 | 15.7 | 16.1 | 16.4 | 16.7 | 17.0 | 17.3 | 17.7 | 18.0 | 18.3 |
| II | 18.7 | 19.0 | 19.4 | 19.7 | 20.1 | 20.4 | 20.8 | 21.1 | 21.5 | 21.9 |
| 12 | 22.2 | 22.6 | 23.0 | 23.3 | 23.7 | 24.1 | 24.5 | 24.9 | 25.3 | 25.7 |
| 13 | 26.1 | 26.5 | 26.9 | 27.3 | 27.7 | 28.1 | 23.5 | 29.0 | 29.4 | 29.8 |
| 14 | 30.2 | 30.7 | 31.1 | 31.6 | 32.0 | 32.4 | 32.9 | 33.3 | 33.8 | 34.3 |
| 15 | 34.7 | 35.2 | 35.7 | 36.1 | 36.6 | 37.1 | 37.6 | 38.0 | 38.5 | 39.0 |
| 16 | 39.5 | 40.0 | 40.5 | 41.0 | 41.5 | 42.0 | 42.5 | 43.0 | 43.6 | 44.1. |
| 17 | 44.6 | 45.1 | 45.7 | 46.2 | 46.7 | 47.3 | 47.3 | 48.3 | 48.9 | 49.4 |
| 18 | 50.0 | 50.6 | 5 I .1 | 51.7 | 52.2 | 52.8 | 53.4 | 54.0 | 54.5 | 55.1 |
| 19 | 55.7 | 56.3 | 56.9 | 57.5 | 58.1 | 58.7 | 59.3 | 59.9 | 60.5 | 61.1 |
| 20 | 61.7 | 62.3 | 63.0 | 63.6 | 64.2 | 64.9 | 65.5 | 66.1 | 66.8 | 67.4 |
| 21 | 68.1 | 68.7 | 89.4 | 70.0 | 70.7 | 71.3 | 72.0 | 72.7 | 73.3 | 74.0 |
| 22 | 74.7 | 75.4 | 76.1 | 76.7 | 77.4 | 78.1 | 78.8 | 79.5 | 80.2 | 80.9 |
| 23 | 81.6 | 82.3 | 83.1 | 83.8 | 84.5 | 85.2 | 86.0 | 86.7 | 87.4 | 88.1 |
| 24 | 88.9 | 89.6 | 90.4 | 9 9 .1 | 91.9 | 92.6 | 93.4 | 94.1 | $9+9$ | 95.7 |
| 25 | 96.5 | 97.2 | 98.0 | 98.8 | 99.6 | 100.3 | ror.r | 101. 9 | 102.7 | 103.5 |
| 26 | $10+3$ | 105.1 | 105.9 | 106.7 | 107.6 | 108.4 | 109.2 | 110.0 | 110.8 | 111.7 |
| 27 | 112.5 | 113.3 | II4.2 | I15.0 | 115.9 | 116.7 | 117.6 | I18.4 | 119.3 | 120.1 |
| 28 | 121.0 | . 121.9 | 122.7 . | 123.6 | 124.5 | 125.3 | 126.2 | 127.1 | 128.0 | 128.9 |
| 29 | 129.8 | 130.7 | 131.6 | 132.5 | 133.4 | I34.3 | 135.2 | 136.1 | 137.0 | 138.0 |
| 30 | 138.9 | 139.8 | 140.7 | 141.7 | 142.6 | 143.6 | 144.5 | 145.4 | 146.4 | 147.3 |
| 31 | 148.3 | 149.3 | 150.2 | 151.2 | 152.2 | 153.1 | 154.1 | 155.1 | 156.1 | 157.0 |
| 32 | 158.0 | 159.0 | 160.0 | 161.0 | 162.0 | 163.0 | 164.0 | 165.0 | 166.0 | 167.0 |
| 33 | 168.1 | 169.1 | 170.1 | 171.1 | 172.2 | 173.2 | 174.2 | 175.3 | 176.3 | 177.3 |
| 34 | $17^{8.4}$ | 179.4 | 180.5 | 181.6 | 182.6 | 183.7 | 184.7 | 185.8 | 186.9 | 188.0 |
| 35 | 189.0 | 190.1 | 191.2 | 192.3 | 193.4 | 194.5 | 195.6 | 196.7 | 197.8 | 198.9 |
| 36 | 200.0 | 201.1 | 202.2 | 203.3 | 104. 5 | 205.6 | 206.7 | 207.9 | 209.0 | 210.1 |
| 37 | 211.3 | 212.4 | 213.6 | 214.7 | 215.9 | 217.0 | 218.2 | 219.3 | 220.5 | 221.7 |
| 38 | 222.8 | 224.0 | 225.2 | 226.4 | 227.6 | 228.7 | 229.9 | 231.1 | 232.3 | 233.5 |
| 39 | 234.7 | 235.9 | 237.1 | 238.3 | 239.6 | 240.8 | 242.0 | 243.2 | 244.5 | 245.7 |
| 40 | 246.9 | 248.1 | 249.4 | 250.6 | 251.9 | 253.1 | 254.4 | 255.6 | 256.9 | 258.1 |
|  | . 0 | . 1 | . 2 | $\cdot 3$ | . 4 | . 5 | . 6 | . 7 | . 8 | . 9 |

Minus Corrections for $\frac{8+8^{\prime}}{2}=\frac{1}{4}$.
Note.-The quantities from the above table divided by two give the plus corrections for $\frac{8+8^{\prime}}{2}=\frac{1}{4}$.

TABLE No. 12.-Level Cuttings. $\frac{s+s^{\prime}}{2}=1 ; b=18$ feet.

| 峎 | . 0 | . 1 | . 2 | . 3 | . 4 | . 5 | . 6 | . 7 | . 8 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\bigcirc$ |  | 6.7 | 13.5 | 3 | 27.3 | 34.3 | 4 I .3 | 48.5 | 55.7 | 63.0 |
| I | 70.4 | 77.8 | 85.3 | 92.9 | 100.6 | 108.3 | 116.1 | 24.0 | 132.0 | 40.0 |
| 2 | 148.1 | 156.3 | 164.6 | 72.9 | 181.3 | 189.8 | 198.4 | 207.0 | 215.7 | 224.5 |
| 3 | 233.3 | 242.3 | 251.3 | 260.3 | 269.5 | 278.7 | 288.0 | 297.4 | 306.8 | 316.3 |
| 4 | 325.9 | 335.6 | 345.3 | 355.1 | 365.0 | 375.0 | 385.0 | 395.I | 405.3 | 415.6 |
| 5 | 425.9 | 436.3 | 446.8 | 457.4 | 468.0 | 478.7 | 489.5 | 500.3 | 511.3 | 522.3 |
| 6 | 533.3 | 544.5 | 555.7 | 567.0 | 578.4 | 589.8 | 601.3 | 612.9 | 624.6 | 636.3 |
| 7 | 648.1 | 660.0 | 672.0 | 684.0 | 696.1 | 708.3 | 720.6 | 732.9 | 745.3 | 757.8 |
| 8 | 770.4 | 783.0 | 795.7 | 808.5 | 821.3 | 834.3 | 847.3 | 860.3 | 873.5 | 886.7 |
| 9 | 900.0 | 913.4 | 926.8 | 940.3 | 953.9 | 967.6 | 981.3 | 995.I | 1009 | 1023 |
| 10 | 1037 | 1051 | 1065 | roso | 1094 | 1108 | 1123 | 1137 | 1152 | 1167 |
| II | 1181 | 1196 | 1211 | 1226 | 1241 | 1256 | 1272 | 1287 | 1302 | 1318 |
| 12 | 1333 | 1349 | 1365 | 1380 | 1396 | 1412 | 1428 | 1444 | 1460 | 1476 |
| 13 | 1493 | 1509 | 1525 | 1542 | 1558 | 1575 | 1592 | 1608 | 1625 | 1642 |
| 14 | 1659 | 1676 | 1693 | 1711 | 1728 | I 745 | 1763 | 1780 | 1798 | 1816 |
| 15 | 1833 | 1851 | 1869 | 1887 | 1905 | 1923 | 1941 | I960 | 1978 | 1996 |
| 16 | 2015 | 2033 | 2052 | 2071 | 2089 | 2108 | 2127 | 2146 | 2165 | 2184 |
| 17 | 2204 | 2223 | 2242 | 2262 | 2281 | 2301 | 2321 | 2340 | 2360 | 2380 |
| 18 | 2400 | 2420 | 2440. | 2460 | 2481 | 2501 | 2521 | 2542 | 2562 | 2583 |
| 19 | 2604 | 2624 | 2645 | 2666 | 2687 | 2708 | 2729 | 2751 | 2772 | 2793 |
| 20 | 2815 | 2836 | 2858 | 2880 | 2901 | 2923 | 2945 | 2967 | 2989 | 3011 |
| 21 | 3033 | 3056 | 3078 | 3100 | 3123 | 3145 | 3168 | 3191 | 3213 | 36 |
| 22 | 3259 | 3282 | 3305 | 3328 | 3352 | 375 | 3398 | 3422 | 3445 | 3469 |
| 23 | 3493 | 35 | 3540 | 3564 | 35 | 3612 | 3636 | 3660 | 3685 | 3709 |
| 24 | 3733 | 3758 | 3782 | 3807 | 3832 | 3856 | 881 | 3906 | 3931 | 3956 |
| 25 | 3981 | 4007 | 4032 | 4057 | 4083 | 4108 | 4134 | 4160 | 4185 | 4211 |
| 26 | 4237 | 4263 | 4289 | 4315 | 4341 | 4368 | 4394 | 4420 | 4447 | 4473 |
| 27 | 4500 | 4527 | 4553 | 4580 | $\because 507$ | 4634 | 4661 | 4688 | 4716 | 4743 |
| 28 | 4770 | 4798 | 4825 | 4853 | 4881 | 4908 | 4936 | 4964 | 4992 | 5020 |
| 29 | $50+8$ | 5076 | 5105 | 5133 | 5161 | 5190 | 5218 | 5247 | 5276 | 5304 |
| 30 | 5333 | 5362 | 5391 | 54 | 5449 | 5479 | 5508 | 5537 | 5567 | 5596 |
| 31 | 5626 | 5656 | 5685 | 5715 | 5745 | 5775 | 5805 | 5835 | 5865 | 5896 |
| 32 | 5926 | 5956 | 5987 | 6017 | 6048 | 6079 | 6109 | 6140 | 6171 | 6202 |
| 33 | 6233 | 6264 | 6296 | 6327 | 6358 | 6390 | 642 I | 6453 | 6485 | 6516 |
| 34 | 6548 | 6580 | 6612 | 6644 | 6676 | 6708 | 6741 | 6773 | 6805 | 6838 |
| 35 | 6870 | 6903 | 6936 | 6968 | 7001 | 7034 | 7067 | 7100 | 7133 | 7167 |
| 36 | 7200 | 7233 | 7267 | 7300 | 7334 | 7368 | 7401 | 7435 | 7469 | 7503 |
| 37 | 7537 | 7571 | 7605 | 7640 | 7674 | 7708 | 7743 | 7777 | 7812 | 7847 |
| 38 | 7881 | 7916 | 7951 | 7986 | 8021 | 8056 | 8092 | 8127 | 162 | 8198 |
| 39 | 8233 | 8269 | 8305 | 8340 | 8376 | 8412 | 8448 | 8484 | 8520 | 8556 |
| 40 | 8593 | 8629 | 8665 | 8702 | 8738 | 8775 | 8812 | 8848 | 8885 | 8922 |
| 41 | 8959 | 8996 | 9033 | 9071 | 9108 | 9145 | 9183 | 9220 | 9258 | 9296 |
| 42 | 9333 | 9371 | 9409 | $9+47$ | 9485 | 9523 | 9561 | 9600 | 9638 | 9676 |
| 43 | 9715 | 9753 | 9792 | 9831 | 9869 | 9908 | 9947 | 9986 | 10025 | 10064 |
| 44 | 10104 | IOI43 | 10182 | 0222 | 10261 | 10301 | 1034I | 10380 | 10420 | 10460 |
| 45 | 10500 | 10540 | 10580 | 10620 | 10661 | 10701 | 1074I | 10782 | 10822 | 10863 |
| 46 | IO904 | 10944 | 10985 | 11026 | 11067 | IIIO8 | III49 | III9I | 11232 | I1273 |
| 47 | 11315 | II356 | 11398 | 11440 | 11481 | I 1523 | II565 | 11607 | II649 | 11691 |
| 48 | II733 | 11776 | 11818 | 11860 | 11903 | 11945 | 11988 | 12031 | 12073 | 12116 |
| 49 | 12159 | 12202 | 12245 | 12288 | 12332 | 12375 | 12418 | 12462 | 12505 | 12549 |
| 50 | 12593 | 12636 | 12680 | 12724 | 12768 | 12812 | 12856 | 12900 | 12945 | 12989 |
| 51 | I3033 | 13078 | 13122 | 13167 | 13212 | 13256 | I 3301 | ${ }^{1} 3346$ | ${ }^{1} 3391$ | 13436 |
| 52 | I3481 | 13527 | 13572 | 13617 | 13663 | 13708 | 13754 | 13800 | 13845 | 1389 x |
| 53 | I 3937 | 13983 | 14029 | 14075 | 14121 | 14168 | 14214 | 14260 | 14307 | 14353 |
| 54 | I4400 | 14447 | 14493 | 14540 | 14587 | 14634 | 14681 | 14728 | 14776 | 14823 |
| 55 | 14870 | 14918 | 14965 | 15013 | 15061 | 15108 | 15156 | 15204 | 15252 | 15300 |
| 56 | 15348 | 15396 | 15445 | 15493 | 15541 | I5590 | 15638 | 15637 | 15736 | ${ }^{15784}$ |
| 57 | 15833 | 15882 | 15931 | 15980 | 16029 | 16079 | 16128 | 16177 | 16227 | 16276 |
| 58 | I6326 | 16376 | 16425 | 16475 | 16525 | 16575 | 16625 | 16675 | 16725 | 16776 |
| 59 | 16826 | 16876 | 16927 | 16977 | 17028 | 17079 | 17129 | 17180 | 17231 | 17282 |
| 60 | 17333 | 17384 | 17436 | 17487 | 17538 | 17590 | 17641 | I7693 | 17745 | 17796 |
|  | . 0 | . 1 | . 2 | . 3 | . 4 | . 5 | . 6 | . 7 | . 8 | . 9 |

TABLE No. 13.-Level Cutings. $\frac{8+8^{8}}{2}=1 ; b=30$ feet.

| 江 | . 0 | I | . 2 | . 3 | . 4 | . 5 | . 6 | . 7 | . 8 | . 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 |  | 11.1 | 2 | 33.7 | 45.0 | 56.5 | 68.0 | 79.6 | 1.3 | 103.0 |
| 1 | 114.8 | 126.7. | 138.7 | 150.7 | 162.8 | 175.0 | 187.3 | 199.6 | 212.0 | 224.5 |
| 2 | 237.0 | 249.7 | 262.4 | 275.I | 288.0 | 300.9 | 313.9 | 327.0 | 340.1 | 353.4 |
| 3 | 366.7 | 380.0 | 393.5 | 407.0 | 420.6 | 434.3 | 448.0 | 46 r .8 | 475.7 | 489.7 |
| 4 | 503.7 | 517.8 | 532.0 | 546.3 | 560.6 | 575.0 | 589.5 | 604.0 | 618.7 | 633.4 |
| 5 | 643.1 | 663.0 | 677.9 | 692.9 | 708.0 | 723.1 | 738.4 | 753.7 | $769 . c$ | 784.5 |
| 6 | 800.0 | 815.6 | 831.3 | 847.0 | 862.8 | 878.7 | 894.7 | 910.7 | 926.8 | $9+3.0$ |
| 7 | 959.3 | 975.6 | 992.0 | 1008 | 1025 | 1042 | 1058 | 1075 | 1092 | 1109 |
| 8 | 1126 | 1143 | 1160 | 1177 | 1195 | 12 | 1229 | 1247 | 1265 | 1282 |
| 9 | 1300 | 1318 | 1336 | 1354 | 372 | 1390 | 1408 | 1426 | 1445 | 463 |
| 0 | 1481 | 1500 | 519 | 537 | 556 | 1575 | 1594 | 1613 | 1632 | 1651 |
| 11 | 1670 | 1690 | 1709 | 728 | 1748 | $\pm 768$ | 1787 | 1807 | 1827 | 1847 |
| 12 | 1867 | 1887 | 7 | 927 | 1947 | 1968 | 1988 | 2008 | 2029 | 2050 |
| 3 | 2070 | 2091 | 2112 | 2133 | 2154 | 2175 | 2196 | 2217 | 2239 | 2260 |
| 14 | 2281 | 2303 | 2325 | 2346 | 2368 | 2390 | 2412 | 2434 | 2456 | 2478 |
| 15 | 2500 | 2522 | 2545 | 2567 | 2589. | 2612 | 2635 | 2657 | 2680 | 2703 |
| 16 | 2726 | 2749 | 2772 | 2795 | 2818 | 2842 | 2865 | 2888 | 912 | 2936 |
| 17 | 2959 | 2993 | 3007 | 3031 | 3055 | 3079 | 3103 | 3127 | 3151 | 3176 |
| 18 | 3200 | 3224 | 3249 | 3274 | 3298 | 3323 | 3348 | 3373 | 3398 | 3423 |
| 19 | $3+48$ | 3473 | 3499 | 3524 | 3549 | 3575 | 3601 | 3626 | 3652 | 3678 |
| 20 | 3704 | 3730 | 3756 | 3782 | 3808 | 3834 | 3861 | 3887 | 3913 | 3940 |
| 21 | 3967 | 3993 | 4020 | 4047 | 4074 | 4101 | 4128 | 4155 | 4182 | 4210 |
| 22 | 4237 | 4264 | 4292 | 4320 | 4347 | 4375 | 4403 | 4431 | 4459 | 4487 |
| 23 | 4515 | 4543 | 4571 | 4600 | 4628 | 4656 | 4685 | 4714 | 47.42 | 4771 |
| 24 | 4800 | 4829 | 4858 | 4887 | 4916 | 4945 | 4975 | 5004 | 5033 | 5063 |
| 25 | 5093 | 5122 | 5152 | 5182 | 5212 | 5242 | 5272 | 5302 | 5332 | 5362 |
| 26 | 5393 | 5423 | $5+53$ | 5484 | 5515 | 5545 | 5576 | 5607 | 5638 | 69 |
| 27 | 5700 | 5731 | 5762 | 5794 | 5825 | 5856 | 5888 | 5920 | 5951 | 5983 |
| 28 | 6015 | 60 | 6079 | 6111 | 6143 | 6175 | 6207 | 6240 | 6272 | 6304 |
| 29 | 6337 | 6370 | $6+02$ | $6+35$ | 64 | 6501 | 653 | 6567 | 6600 | 6633 |
| 30 | 6667 | 6700 | 6733 | 6767 | 6801 | 6834 | 6868 | 6902 | 6936 | 6970 |
| 31 | 7004 | 7038 | 7072 | 7106 | 7141 | 7175 | 7209 | 7244 | 7279 | 7313 |
| 32 | $734{ }^{3}$ | 7383 | 7418 | $7+53$ | 74 | 7523 | 7558 | 7594 | 7629 | 7664 |
| 33 | 7700 | 7736 | 7771 | 7807 | 7843 | 7879 | 7915 | 7951 | 7987 | 8023 |
| 34 | 8059 | 8096 | 8132 | 8163 | 8205 | 8242 | 8278 | 8315 | 8352 | 8389 |
| 35 | $8{ }_{426}$ | $8+63$ | 8500 | 8537 | 8575 | 8612 | 8649 | 8687 | 8725 | 8762 |
| 36 | 8300 | 8338 | 8876 | 8914 | 8952 | 8990 | 9028 | 9066 | 9105 | 143 |
| 37 | 9181 | 9220 | 9259 | 9297 | 9336 |  | 9414 | 9453 | 9492 | 9531 |
| 38 | 9570 | 9610 | 9649 | 9688 | 9728 | 976 | 9807 | 9847 | 9887 | 9927 |
| 39 | 9967 | 10007 | 10047 | 10087 | 10127 | 10 | 10208 | 10248 | 10289 | 10330 |
| 40 | 10370 | 10411 | 10452 | 10493 | $1053+$ | 10575 | 10 | 10657 | 10699 | 10740 |
| 4 T | 10781 | 10823 | 10865 | 10906 | 10948 | 10990 | 11032 | 11074 | 11116 | 11158 |
| 42 | I120 | 11242 | 11285 | 11327 | 11369 | 11412 | I 1455 | 11497 | 11540 | 11583 |
| 43 | 11626 | 11669 | 11712 | 11755 | 11793 | 11842 | I1885 | 11928 | 11972 | 12016 |
| 44 | 12059 | 12103 | 12147 | 12191 | 12235 | 12279 | 12323 | 12367 | 12411 | 12456 |
| 45 | 12500 | 12544 | 12589 | 12634 | 12678 | 12723 | 12768 | 12813 | 12858 | 12903 |
| 46 | 12948 | 12993 | 13039 | 1308. | 13129 | 13175 | 13221 | 13266 | 13312 | 13358 |
| 47 | $13+0+$ | $13+50$ | 13496 | 13542 | 13588 | 13634 | 13681 | 13727 | 13773 | 13820 |
| 48 | r3867 | 13913 | 13960 | 14007 | 14054 | Itici | 14148 | 14195 | 14242 | 14290 |
| 49 | 14337 | 14384 | 14432 | I 4480 | 14527 | 14575 | 14623 | 14671 | 14719 | 14767 |
| 50 | I4815 | 14863 | 14911 | 14960 | 15008 | 15056 | 15105 | 15154 | 15202 | 15251 |
| 51 | 15300 | 15349 | 15398 | 15447 | 15496 | 15545 | 15595 | ${ }_{15644}$ | 15693 | 15743 |
| 52 | 15793 | $158+2$ | 15892 | 15942 | 15992 | 16042 | 16092 | 16142 | 16192 | 16242 |
| 53 | 16293 | $163+3$ | 16393 | 16444 | 16495 | 16545 | 16596 | 16647 | 16698 | 16749 |
| 54 | 16800 | 16851 | 16902 | 16954 | 17005 | 17056 | 17108 | 17160 | 17211 | 17263 |
| 55 | 17315 | 17367 | 17419 | 17471 | 17523 | 17575 | 17627 | 17680 | 17732 | 17784 |
| 56 | 17837 | 17890 | 17942 | 17995 | 18048 | 18101 | 18154 | 18207 | 18260 | 18313 |
| 57 | 18367 | 18420 | 18473 | 18527 | 18581 | 18634 | 18688 | 18742 | 18796 | 18850 |
| 58 | 18904 | 18958 | 19012 | 19066 | 19121 | 19175 | 19229 | 19284 | 19339 | 19393 |
| 59 | 19448 | 19503 | 19558 | $1{ }^{19613}$ | 19668 | 19723 | 19778 | 19834 | 19889 | 19944 |
| 60 | 20000 | 20056 | 20111 | 20167 | 20223 | 20279 | 20335 | 20391 | 20447 | 20503 |
|  | . 0 | . 1 | . 2 | . 3 | . 4 | . 5 | . 6 | . 7 | . 8 | . 9 |

## TABLE No. 14.

Plus Corrections for $\frac{s+s^{\prime}}{2}=1$.

| $\begin{gathered} \hline \stackrel{\text { U }}{0} \\ H \end{gathered}$ | . 0 | . 1 | . 2 | . 3 | . 4 | . 5 | . 6 | . 7 | . 8 | . 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.1 | 0.1 | 0.2 | 0.2 | 0.3 |
| 1 | 0.3 | 0.4 | 0.4 | 0.5 | 0.6 | 0.7 | 0.8 | 0.9 | I. 0 | I.I |
| 2 | 1.2 | 1.4 | 1.5 | 1. 6 | 1.8 | 1.9 | 2.1 | 2.2 | 2.4 | 2.6 |
| 3 | 2.8 | 3.0 | 3.2 | 3.4 | 3.6 | 3.8 | 4.0 | 4.2 | 4.5 | 4.7 |
| 4 | $4 \cdot 9$ | 5.2 | $5 \cdot 4$ | 5.7 | 6.0 | 6.3 | 6.5 | 6.8 | 7.1 | $7 \cdot 4$ |
| 5 | 7.7 | 8.0 | 8.3 | 8.7 | 9.0 | 9.3 | 9.7 | 10.0 | 10.4 | 10.7 |
| - 6 | II.I | - 11.5 | 11.9 | 12.3 | 12.6 | 13.0 | 13.4 | 13.9 | 14.3 | 14.7 |
| 7 | 15.1 | 15.6 | 16.0 | 16.4 | 16.9 | 17.4 | 17.8 | 18.3 | 18.8 | 19.3 |
| 8 | I9.8 | 20.3 | 20.8 | 2 I .3 | 21.8 | 22.3 | 22.8 | 23.4 | 23.9 | 24.4 |
| 9 | 25.0 | 25.6 | 26.1 | 26.7 | 27.3 | 27.9 | 28.4 | 29.0 | 29.6 | 30.3 |
| 10 | 30.9 | 31.5 | 32.1 | 32.7 | 33.4 | 34.0 | 34.7 | 35.3 | 36.0 | 36.7 |
| II | 37.3 | 38.0 | 38.7 | 39.4 | 40.1 | 40.8 | 41.5 | 42.3 | 43.0 | 43.7 |
| 12 | 44.4 | 45.2 | 45.9 | 46.7 | 47.5 | 48.2 | 49.0 | 49.8 | 50.6 | 51.4 |
| 13 | 52.2 | 53.0 | 53.8 | 54.6 | 55.4 | 56.2 | 57.1 | 57.9 | 58.8 | 59.6 |
| 14 | 60.5 | 6 I .4 | 62.2 | 63.1 | 64.0 | 64.9 | 65.8 | 66.7 | 67.6 | 68.5 |
| 15 | 69.4 | 70.4 | 71.3 | 72.3 | 73.2 | 74.2 | 75.1 | 76.1 | 77.0 | 78.0 |
| 19 | 79.0 | 80.0 | 81.0 | 82.0 | 83.0 | 84.0 | 85.0 | 86.1 | 87.1 | 88.2 |
| 17 | 89.2 | 90.3 | 9 I 3. | 92.4 | 93.4 | 94.5 | 95.6 | 96.7 | 97.8 | 98.9 |
| 13 | 100.0 | IOI. 1 | 102.2 | 103.4 | 104.5 | 105.6 | 106.8 | 107.9 | 109. $\mathrm{I}^{\circ}$ | 110.2 |
| 19 | III. 4 | I 12.6 | 113.8 | II 5.0 | 116.2 | II7.4 | II8.6 | II9.8 | 121.0 | 122.2 |
| 20 | 123.5 | 124.7 | 125.9 | 127.2 | 128.4 | 129.7 | 131.0 | 132.3 | 133.5 | 134.8 |
| 21 | I36.1 | 137.4 | 138.7 | 140.0 | 141.3 | 142.7 | I44.0 | 145.3 | 146.7 | 148.0 |
| 22 | 149.4 | 150.7 | 152.1 | I53.5 | . 154.9 | 156.3 | 157.6 | 159.0 | 160.4 | 161. 9 |
| 23 | 163.3 | 164.7 | 166.1 | 167.6 | 169.0 | 170.4 | 171.9 | I73.4 | 174.8 | I76.3 |
| 24 | 177.8 | 179.3 | ISo. 8 | 182.3 | 183.8 | 185.3 | 186.8 | 188.3 | 189.8 | I9I. 4 |
| 25 | I92.9 | 19.4 | I96.0 | 197.6 | 199.I | 200.7 | 202.3 | 203.9 | 205.4 | 207.0 |
| 26 | 208.6 | 210.3 | 211.9 | 213.5 | 215.1 | 216.7 | 218.4 | 220.0 | 221.7 | 223.3 |
| 27 | 225.0 | 226.7 | 228.3 | 230.0 | 231.7 | 233.4 | 235.1 | 236.8 | 238.5 | 240.3 |
| 23 | 242.0 | 243.7 | 245.4 | 247.2 | 248.9 | 250.7 | 252.5 | 254.2 | 256.0 | 257.8 |
| 29 | 259.6 | 261.4 | 263.2 | 265.0 | 266.8 | 268.6 | 270.4 | 272.2 | 274.1 | 275.9 |
| 30 | 277.8 | 279.6 | 281.5 | 283.4 | 285.2 | 287.1 | 289.0 | 290.9 | 292.8 | 294.7 |
| 31 | 296.6 | 298.5 | 300.4 | 302.4 | 304.3 | 306.3 | 308.2 | 310.2 | 312.1 | 314.1 |
| 32 | 316.0 | 318.0 | 320.0 | 322.0 | 324.0 | 326.0 | 328.0 | 330.0 | 332.0 | 334.1 |
| 33 | 336.I | 338.2 | 340.2 | 342.3 | 344.3 | 346.4 | 348.4 | 350.5 | 352.6 | 354.7 |
| 34 | 356.8 | 358.9 | 361.0 | 363.1 | 365.2 | 367.4 | 369.5 | 371.6 | 373.8 | 375.9 |
| 35 | 378.1 | 380.2 | 382.4 | 384.6 | 386.8 | 389.0 | 391.2 | 393.4 | 395.6 | 397.8 |
| 36 | 400.0 | 402.2 | 404.5 | 406.7 | 408.9 | 411.2 | 413.4 | 415.7 | 418.0 | 420.3 |
| 37 | 422.5 | 424.8 | 427.1 | 429.4 | 431.7 | 434.0 | 436.3 | 438.7 | 441.0 | 443.3 |
| 38 | 445.7 | 448.0 | 450.4 | 452.7 | $455 . \mathrm{I}$ | 457.5 | 459.9 | 462.3 | 464.6 | 467.0 |
| 39 | 469.4 | 471.9 | 474.3 | 476.7 | 479.1 | 481.6 | 484.0 | 486.4 | 488.9 | 491.4 |
| 40 | 493.8 | 496.3 | 498.8 | 501.3 | 503.8 | 506.2 | 508.8 | 511.3 | 513.8 | 516.3 |
|  | . 0 | . 1 | . 2 | $\cdot 3$ | . 4 | .5 | . 6 | .7 | . 8 | . 9 |

Minus Corrections for $\frac{s+s^{\prime}}{2}=\frac{1}{2}$.
Note.-For minus corrections for $\frac{s+s^{\prime}}{2}=1$, see Table 5.

TABLE No. 15.-Levèl Cuttings. $\frac{8+8^{\prime}}{2}=1 \frac{1}{2} ; b=14$ feet.

| A | . 0 | . 1 | . 2 | . 3 | . 4 | . 5 | . 6 | . 7 | . 8 | . 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0.0 | 5.2 | 10.6 | 16.1 | 21.6 | 27.3 | 33.1 | 39.0 | 45.0 | 5 I .2 |
| 1 | . | 63.8 | . 2 | 76.8 | 83.5 | 90.3 | 97.2 | 104.2 | 111.3 | 18.6 |
| 2 | 125.9 | 133.4 | 14.0 | 148.6 | 156.4 | 164.4 | 172.4 | 180.5 | 188.7 | 197.1 |
| 3 | 205.6 | 214.1 | 222.8 | 231.6 | 240.5 | 249.5 | 258.7 | 267.9 | 277.3 | 286.7 |
| 4 | 296.3 | 306.0 | 315.8 | 325.7 | 335.7 | 345.8 | 356.1 | 366.4 | 376.9 | 387.5 |
| 5 | 393.1 | 408.9 | 419.9 | 430.9 | 442.0 | 453.2 | 46.6 | 476.1 | 487.6 | 499.3 |
| 6 | 511.1 | 523.0 | 535.0 | 547.2 | 559.4 | 571.8 | 584.2 | 596.8 | 609.5 | 622.3 |
| 7 | 635.2 | 648.2 | 661.3 | 674.6 | 687.9 | 701.4 | 7.15 .0 | 728.6 | 742.4 | 756.4 |
| 8 | 770.4 | 784.5 | 798.7 | 813.1 | 827.6 | 842.1 | 856.8 | 871.6 | 886.5 | 901.5 |
| 9 | 916.7 | 931.9 | 947.3 | 962.7 | 978.3 | 994.0 | roro | 1026 | 1042 | 1058 |
| 10 | 1074 | 1090 | 1107 | 1123 | 1140 | 1157 | 1174 | 1191 | 1203 | 1225 |
| -11 | 1243 | 1260 | 1278 | 1295 | 1313 | 1331 | 1349 | 1367 | I385 | 1404 |
| 12 | 1422 | 1441 | 1459 | 1478 | 1497 | 1516 | 1535 | 1555 | 1574 | 1593 |
| 13 | 1613 | 1633 | 1652 | 1672 | 1692 | 1713 | 1733 | 1753 | 1774 | 1794 |
| 14 | 1815 | 1836 | 1857 | 1878 | 1899 | 1920 | 941 | 1963 | I984 | 2006 |
| 15 | 2028 | 2050 | 2072 | $209+$ | 2116 | 2138 | 61 | 2183 | 2206 | 2229 |
| 16 | 2252 | 2275 | 2298 | 2321 | 2345 | 2368 | 2392 | 2415 | 2439 | $2+63$ |
| 17 | 2487 | 2511 | 2535 | 2560 | $258+$ | 2609 | 2633 | 2658 | 2683 | 2703 |
| 18 | 2733 | 2759 | 2784 | 2809 | 2835 | 2861 | 2886 | 2912 | 2938 | 2965 |
| 19 | 2991 | 3017 | 3044 | 3070 | 3097 | 3124 | 3151 | 3178 | 3205 | 3232 |
| 20 | 3259 | 3287 | 3314 | 3342 | 3370 | 3398 | 3426 | $3+54$ | 3482 | 3510 |
| 21 | 3539 | 3567 | 3596 | 3625 | 3654 | 3683 | 3712 | 3741 | 3771 | Soo |
| 22 | 3830 | 3859 | 3889 | 3919 | 3949 | 3979 | 4009 | 4040 | 4070 | 4101 |
| 23 | 4131 | 4162 | 4193 | $422+$ | 4255 | 4287 | 4318 | 4349 | 4381 | 4413 |
| 24 | 4444 | 4476 | 4508 | 4541 | 4573 | 4605 | 4638 | 4670 | 4703 | 4736 |
| 25 | 4769 | 4802 | 4835 | 4563 | 4901 | 4935 | 4963 | 5002 | 5036 | 5070 |
| 26 | 5104 | 5139 | 5172 | 5206 | 52.1 | 5275 | 5310 | 5345 | 5380 | 5415 |
| 27 | 5450 | $5+85$ | 5521 | 5556 | 5592 | 5627 | 5663 | 5699 | 5735 | 5771 |
| 28 | 5807 | $584+$ | 5880 | 5917 | 5953 | 5990 | 6027 | 6064 | 6101 | 6139 |
| 29 | 6176 | 6213 | 6251 | 6289 | 6326 | 6364 | 6!02 | 6441 | 6479 | 6517 |
| 30 | 6556 | 6594 | 6633 | 6672 | 6711 | 6750 | 6789 | 6828 | 6867 | 6907 |
| 31 | $69+6$ | 6986 | 7026 | 7066 | 7106 | 7146 | 7186 | 7226 | 7267 | 7307 |
| 32 | 7348 | 7389 | 7430 | 7471 | 7512 | 7553 | 7595 | 7636 | 7678 | 7719 |
| 33 | 7761 | 7803 | 7845 | 7887 | 7929 | 7972 | 8 OI 4 | 8057 | 8099 | 8142 |
| 34 | 8185 | 8228 | 8271 | 8315 | 8358 | 8401 | 8445 | 8489 | 8532 | 8576 |
| 35 | 8620 | 8665 | 8709 | 8753 | 8798 | 8842 | 8857 | 8932 | 8977 | 9022 |
| 36 | 9067 | 9112 | 9157 | 9203 | 9248 | 9294 | 9340 | 9386 | 9432 | 9478 |
| 37 | 9524 | 9570 | 9617 | 9663 | 9710 | 9757 | 9804 | 9851 | 9893 | $99+5$ |
| 38 | 9993 | 10040 | 10088 | 10135 | 10183 | 10231 | 10279 | 10327 | 10375 | 10424 |
| 39 | 10472 | 10521 | 10569 | 106IS | 10667 | 10716 | 10765 | 10815 | 10864 | IO913 |
| 40 | Iog63 | IIOI3 | 11062 | 11112 | 11162 | 11213 | 11263 | 11313 | 11364 | II414 |
| 41 | II 465 | 11516 | 1156 | 11618 | 11669 | 11720 | 11775 | I 1823 | 11874 | 11926 |
| 42 | 11978 | 12030 | 12082 | 12134 | 12186 | 12238 | 12291 | 12343 | 12396 | 12449 |
| 43 | 12502 | 12555 | 2608 | 12661 | 12715 | 12768 | 12822 | 12875 | 12929 | 12983 |
| 44 | 13037 | 13091 | 13145 | 13200 | 13254 | 13309 | 13363 | 13418 | 13473 | 13523 |
| 45 | I3583 | 13639 | $1369+$ | 13749 | 13805 | 13861 | 13916 | 13972 | 14028 | 14085 |
| 46 | 14141 | I 4197 | 14254 | 14310 | I 4367 | 14424 | 14481 | 14538 | 14595 | 14652 |
| 47 | I4709 | ${ }^{1}+767$ | 14824 | 14852 | $\underline{1}+9+0$ | 14998 | 15056 | 15114 | 15172 | 15230 |
| 48 | 15289 | 15347 | 15406 | 15465 | 15524 | 15583 | 15642 | 15701 | 15761 | 15820 |
| 49 | 15880 | 15939 | 15999 | 16059 | 16119 | 16179 | 16239 | 16300 | 16360 | 1642I |
| 50 | I6481 | 16542 | 16603 | 1666 | 16725 | 16787 | 16848 | 16909 | 16971 | 17033 |
| 5 5 | 17094 | 17156 | 17218 | 17281 | 17343 | 17405 | 17468 | 17530 | 17593 | 17656 |
| 52 | 17719 | 17782 | 17845 | 17908 | 17971 | 18035 | 18093 | 18162 | 18226 | 18290 |
| 53 | I8354 | 18418 | 18482 | I8546 | 18611 | 18675 | 18740 | 18805 | 18870 | 18935 |
| 54 | 19000 | 19065 | 19131 | 19196 | 19262 | 19327 | 19393 | 19459 | 19525 | I9591 |
| 55 | 19657 | 19724 | 19790 | I9857 | 19923 | 19990 | 20057 | 20124 | 20191 | 20259 |
| 56 | 20326 | 20393 | 20461 | 20529 | 20596 | 20664 | 20732 | 208or | 20869 | 20937 |
| 57 | 21006 | 21074 | 21143 | 21212 | 21281 | 21350 | 21419 | 21488 | 21557 | 21627 |
| 58 | 21696 | 21766 | 21836 | 21906 | 21976 | 22046 | 22116 | 22186 | 22257 | 22327 |
| 59 | 22398 | $22+69$ | 22540 | 22611 | 22682 | 22753 | 22825 | 22896 | 22968 | 23039 |
| 60 | 23111 | 23183 | 23255 | 23327 | 23399 | 23472 | 23544 | 23617 | 23689 | 23762 |
|  | 0 | . 1 | . 2 | $\cdot 3$ | . 4 | . 5 | 6 | .7 | . 8 | . 9 |

TABLE No. 10.-Level Cuttings. $\frac{s+8}{2}=1 \frac{1}{2} ; b=26$ feet.

| 家 | . 0 | . 1 | . 2 | . 3 | . 4 | . 5 | . 6 | . 7 | . 8 | . 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0.0 | 9.7 | 19.5 | 29.4 | 39.4 | 49.5 | 59.8 | 70.1 | 80.6 | 1.2 |
| 1 | ror. 9 | 112.6 | 123.6 | 134.6 | 145.7 | 156.9 | 168.3 | 179.8 | 191.3 | 203.0 |
| 2 | 214.8 | 226.7 | 238.7 | 250.9 | 263.1 | 275.5 | 287.9 | 300.5 | 313.2 | 326.0 |
| 3 | 338.9 | 351.9 | 365.0 | 378.3 | 391.6 | 405.1 | 418.7 | 432.4 | 446.r | 460.1 |
| 4 | 474.I | 488.2 | 502.4 | 516.8 | 531.3 | 545.8 | 560.5 | 575.3 | 590.2 | 605.2 |
| 5 | 620.4 | 635.6 | 651.0 | 666.4 | 682.0 | 697.7 | 713.5 | 729.4 | 745.4 | 761.5 |
| 6 | 777.8 | 794.1 | 810.6 | 827.2 | 843.9 | 860.6 | 877.6 | 894.6 | 911.7 | 928.9 |
| 7 | 946.3 | 963.8 | 981.3 | 999.0 | IOI 7 | 1035 | 1053 | 1071 | 1089 | 1107 |
| 8 | II26 | II45 | I163 | I 182 | 1201 | 1220 | 1239 | 1258 | 1278 | 1297 |
| 9 | 13I7 | 1336 | 1356 | 1376 | 1396 | 1416 | 1436 | 1457 | 1477 | 1498 |
| 10 | -519 | I539 | 1560 | 1581 | 1602 | 1624 | 1645 | 1666 | 1688 | I710 |
| 11 | I 732 | 1753 | 1775 | 1798 | 1820 | 1842 | 1865 | 1887 | I910 | 1933 |
| 12 | 1956 | 1979 | 2002 | 2025 | 2048 | 2072 | 2095 | 2119 | 2143 | 2167 |
| 13 | 2191 | 2215 | 2239 | 2264 | 2288 | 2312 | 2337 | 2362 | 2387 | 2412 |
| 14 | 2437 | 2462 | 2488 | 2513 | 2539 | 2564 | 2590 | 2616 | 2642 | 2668 |
| 15 | 2694 | 2721 | 2747 | 2774 | 2801 | 2827 | 2854 | 2881 | 2908 | 2936 |
| 15 | 2963 | 2990 | 3018 | 3046 | 3074 | 3101 | 3129 | 3158 | 3186 | 3214 |
| 17 | 3243 | 3271 | 3300 | 3329 | 3358 | 3387 | 3416 | 3445 | 3474 | 3504 |
| 18 | 3533 | 3563 | 3593 | 3623 | 3653 | 3683 | 3713 | 3744 | 3774 | 3804 |
| 19 | 3835 | 3866 | 3897 | 3928 | 3959 | 3990 | 4022 | 4053 | 4085 | 4116 |
| 20 | 4148 | 4180 | 4212 | 4244 | 4276 | 4309 | 4341 | 4374 | 4407 | 4439 |
| 2 I | 4472 | 4505 | 4538 | 4572 | 4605 | 4638 | 4672 | 4706 | 4740 | 4773 |
| 22 | 4807 | 4842 | 4876 | 4910 | 4945 | 4979 | 5014 | 5049 | 5084 | 5119 |
| 23 | 5154 | 5189 | 5224 | 5260 | 5295 | 5331 | 5367 | 5403 | 5439 | 5475 |
| 24 | 5511 | 5548 | 5584 | 5620 | 5657 | 5694 | 5731 | 5768 | 5805 | 5842 |
| 25 | 5880 | 5917 | 5955 | 5992 | 6030 | 6068 | 6106 | 6144 | 6182 | 6221 |
| 26 | 6259 | 6298 | 6337 | 6375 | 6414 | 6453 | 6492 | 6532 | 6571 | 6610 |
| 27 | 6650 | 6690 | 6730 | 6769 | 6809 | 6850 | 6890 | 6930 | 6971 | 7011 |
| 28 | 7052 | 7093 | 7134 | 7175 | 7216 | 7257 | 7298 | 7340 | 7381 | 7423 |
| 29 | 7465 | 7507 | 7549 | 7591 | 7633 | 7676 | 7718 | 7760 | 7803 | 7846 |
| 30 | 7889 | 7932 | 7975 | 8018 | So62 | 8105 | 8149 | 8192 | 8236 | 8280 |
| 31 | 8324 | 8368 | 8412 | 8457 | 8501 | 8546 | 8591 | 8635 | 8680 | 8725 |
| 32 | 8770 | 8816 | 886I | 8906 | 8952 | 8998 | 9044 | 9089 | 9135 | 9182 |
| 33 | 9228 | 9274 | 9321 | 9367 | 9414 | 9461 | 9508 | 9555 | 9602 | 9649 |
| 34 | 9696 | 9744 | 9791 | 9839 | 9887 | 9935 | 9983 | 10031 | 10079 | 10128 |
| 35 | 10176 | 10224 | 10273 | 10322 | 10371 | 10420 | 10469 | r05I8 | 10568 | 10617 |
| 36 | 10667 | 10716 | 10766 | 10816 | 10866 | 10916 | Iog66 | IIOI7 | 11067 | IIIIS |
| 37 | III69 | II2I9 | 11270 | II32I | II372 | II 424 | II475 | II 526 | 11578 | II630 |
| 38 | II682 | 11733 | 11785 | 11838 | 11890 | 11942 | 11995 | 12047 | 12100 | 12153 |
| 39 | 12206 | 12259 | 12312 | 12365 | 12418 | 12472 | 12525 | 12579 | I2633 | 12687 |
| 40 | 12741 | 12795 | 12849 | 12904 | 12958 | 13012 | 13067 | 13122 | 13177 | 13232 |
| 4 I | 13287 | I 3342 | 13398 | 13453 | 13509 | 13564 | 13620 | 13676 | 13732 | 13788 |
| 42 | 13844 | I3901 | 13957 | I4OI4 | 14071 | 14127 | 14184 | 14241 | 14298 | 14356 |
| 43 | 14413 | 14470 | 14528 | 14586 | 14644 | 14701 | 14759 | 14818 | 14876 | 14934 |
| 44 | 14993 | $\mathrm{I}_{5} \mathrm{O}_{5} \mathrm{I}$ | 15110 | 15169 | 15228 | 15287 | 15346 | 15405 | 15464 | 15524 |
| 45 | 15583 | ${ }_{1} 5643$ | 15703 | 15763 | 15823 | 15883 | 15943 | 16004 | 16064 | 16124 |
| 46 | 16185 | 16246 | 16307 | 16368 | 16429 | 16490 | 16552 | 16613 | 16675 | 16736 |
| 47 | 16798 | 16860 | 16922 | I6984 | 17046 | 17109 | 17171 | 17234 | 17297 | 17359 |
| 48 | 17422 | I7485 | 17548 | 17612 | 17675 | 17738 | 17802 | 17866 | 17930 | I 7993 |
| 49 | 18057 | 18122 | 18186 | 18250 | 18315 | 18379 | 18444 | 18509 | 18574 | 18639 |
| 50 | 18704 | 18769 | 18834 | 18900 | 18965 | 19031 | 19097 | 19163 | 19229 | 19295 |
| 51 | 19361 | 19428 | 19494 | 19560 | I9627 | 19694 | 19761 | 19828 | 19895 | 19962 |
| 52 | 20030 | 20097 | 20165 | 20232 | 20300 | 20368 | 20436 | 20504 | 20572 | 20641 |
| 53 | 20709 | 20778 | 20847 | 20915 | 20984 | 21053 | 21122 | 2 1192 | 21261 | 21330 |
| 54 | 21400 | 21470 | 21540 | 21609 | 21679 | 21750 | 21820 | 21890 | 21961 | 22031 |
| 55 | 22102 | 22173 | 22244 | 22315 | 22386 | 22457 | 22528 | 22600 | 22671 | 22743 |
| 56 | 22815 | 22887 | 22959 | 23031 | 23103 | 23176 | 23248 | 23320 | 23393 | 23466 |
| 57 | 23539 | 23612 | 23685 | 23758 | 23832 | 23905 | 23979 | 24052 | 24126 | 24200 |
| 58 | 24274 | 24348 | 24422 | 24497 | 24571 | 24646 | 24721 | 24795 | 24870 | 24945 |
| 59 | 25020 | 25096 | 25171 | 25246 | 25322 | 25398 | 25474 | 25549 | 25625 | 25702 |
| 60 | 25778 | 25854 | 25931 | 26007 | 26084 | 26161 | 26238 | 26315 | 26392 | 26469 |
|  | . 0 | . 1 | . 2 | . 3 | . 4 | . 5 | . 6 | . 7 | . 8 | . 9 |

## TABLE No. 17.

$\dot{\text { Plus Corrections for } \frac{8+8^{\prime}}{2}}=1 \frac{1}{2}$.

| 这 | . 0 | . 1 | . 2 | . 3 | . 4 | . 5 | . 6 | . 7 | . 8 | . 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.1 | 0.1 | 0.2 | 0.2 | 0.3 | 0.4 |
| 1 | 0.5 | 0.6 | 0.7 | 0.8 | 0.9 | 1.0 | 1.2 | 1.3 | 1.5 | 1.7 |
| 2 | 1.9 | 2.9 | 2.2 | 2.4 | 2.7 | 2.9 | 3.1 | $3 \cdot 4$ | 3.6 | 3.9 |
| 3 | 4.2 | 4.4 | 4.7 | 5.0 | $5 \cdot 4$ | 5.7 | 6.0 | 6.3 | 6.7 | 7.0 |
| 4 | $7 \cdot 4$ | 7.8 | 8.2 | 8.6 | 9.0 | 9.4 | 9.8 | 10.2 | 10.7 | II.I |
| 5 | 11.6 | 12.0 | 12.5 | 13.0 | 13.5 | 14.0 | 14.5 | 15.0 | - 15.6 | 16.1 |
| 6 | 16.7 | 17.2 | 17.8 | 18.4 | 19.0 | 19.6 | 20.2 | 20.3 | 21.4 | 220 |
| 7 | 22.7 | 23.3 | 24.0 | 24.7 | 25.4 | 26.6 | 26.7 | $27 \cdot 4$ | 28.2 | 23.9 |
| 8 | 29.6 | 30.4 | 3 I .1 | 31.9 | 32.7 | 33.4 | $3+.2$ | 35.0 | 35.9 | 36.7 |
| 9 | 37.5 | 33.3 | 39.2 | 40.0 | 40.9 | 41.8 | 42.7 | 43.6 | 44.5 | $45 \cdot 4$ |
| 10 | 46.3 | 47.2 | 48.2 | 49.1 | 50.1 | 51.0 | 52. | 53. | 54. | 55. |
| 11 | 56. | 57. | 58.1 | 59.1 | 60.2 | 61.2 | 62.3 | 63.4 | 64.5 | 65.6 |
| 12 | 66.7 | 67.8 | 68.9 | 70. | 71.2 | 72.3 | 73.5 | $7+7$ | 75.9 | 77. |
| 13 | 78.2 | 79.4 | 80.7 | 81.9 | 83.1 | 84.4 | 85.6 | 86.9 | 88.2 | 89.4 |
| 14 | 90.7 | 92.0 | 93.4 | 94.7 | 96.0 | 97.3 | 93.7 | 100. | 101.4 | 102.8 |
| 15 | 104.2 | 105.6 | 107.0 | 108.4 | 109.3 | III. 2 | 112.7 | 114.1 | II5.6 | 117. |
| 16 | 118.5 | 120. | 121.5 | 123. | 124.5 | 126. | 127.6 | 129.1 | 130.7 | 132.2 |
| 17 | 133.8 | 135.4 | 137.0 | 138.6 | 140.2 | 14 I .8 | 143.4 | 145. | 146.7 | 148.3 |
| 18 | 150. | 151.7 | I 53.4 | 155. | 156.7 | 158.4 | 160.2 | 161.9 | 163.6 | 165.4 |
| 19 | 167.1 | 168.9 | 170.7 | 172.4 | 174.2 | 176:0 | 177.9 | 179.7 | 181.5 | 183.3 |
| 20 | 185.2 | 187. | 188.9 | 190.3 | 192.7 | 194.6 | 196.5 | 198.4 | 200.3 | 202.2 |
| 21 | 204.2 | 206.1 | 20S. 1 | 210. | 212. | 214. | 216. | 218. | 220. | 222. |
| 22 | 224. 1 | 226.1 | 228.2 | 230.2 | 232.3 | 234.4 | 236.5 | 238.6 | 240.7 | 242.8 |
| 23 | 244.9 | 247. | 249.2 | 251.3 | 253.5 | 255.7 | 257.9 | 260.0 | 262.2 | 264.4 |
| 27 | 266.7 | 268.9 | 271.1 | 273.4 | 275.6 | 277.9 | 280.2 | 282.4 | 28.7 | 287.0 |
| 25 | 289.4 | 291.7 | 294. | 296.3 | 298.7 | 301.0 | 303.4 | 305.8 | 308.2 | 310.6 |
| 25 | 313. | 315.4 | 317.8 | 320.2 | 322.7 | 325.1 | 327.6 | 330.0 | 332.5 | 335. . |
| 27 | 337.5 | 340.0 | 342.5 | 345.0 | $3+7.6$ | 350.1 | 352.7 | 355.2 | 357.8 | 360.4 |
| 28 | 363.0 | 365.6 | 368.2 | 370.8 | 373.4 | 376.0 | 378.7 | 381.3 | 384.0 | 386.7 |
| 20 | 389.4 | 392.0 | 394.7 | 397.4 | 400.2 | 402.9 | 405.6 | 408.4 | 411.1 | 413.9 |
| 30 | 416.7 | 419.4 | 422.2 | 425.0 | 427.9 | 430.7 | 433.5 | 436.3 | 439.2 | $44^{2.0}$ |
| 31 | $4+4.9$ | 447.3 | 450.7 | 453.6 | 456.5 | 459.4 | 462.3 | 465.2 | 463.2 | 471.1 |
| 32 | 474.1 | 477.0 | 450.0 | 483.0 | 486.0 | 489.0 | 492.0 | 495.0 | 493.1 | 501. 1 |
| 33 | 504.2 | 507.2 | 510.3 | 513.4 | 516.5 | 519.6 | 522.7 | 525.8 | 528.9 | 532.0 |
| 34 | 535.2 | 538.3 | 541.5 | 544.7 | 547.9 | 551.0 | 554.2 | 557.4 | 560.7 | 563.9 |
| 35 | 567.1 | 570.4 | 573.6 | 576.9 | 580.2 | 533.4 | 586.7 | 590.0 | 593.4 | 596.7 |
| 36 | 600.0 | 603.3 | 606.7 | 610.0 | 613.4 | 616.8 | 620.2 | 623.6 | 627.0 | 630.4 |
| 37 | 633.8 | 637.2 | 640.7 | 644.1 | 647.6 | 651.0 | 654.5 | 658.0 | 661.5 | 665.0 |
| 38 | 668.5 | 672.0 | 675.6 | 679.1 | 682.7 | 686.2 | 689.8 | 693.4 | 697.0 | 700.6 |
| 39 | 704.2 | 707.8 | 711.4 | 715.0 | 718.7 | 722.3 | 726.0 | 729.7 | 733.4 | 737.0 |
| 40 | 740.7 | 744.4 | 748.2 | 751.9 | 755.6 | 759.4 | 763.1 | 766.9 | 770.7 | 774.4 |
|  | . 0 | . 1 | . 2 | -3 | . 4 | . 5 | . 6 | . 7 | . 8 | . 9 |

Minus Corrections for $\frac{s+s^{\prime}}{2}=\frac{3}{4}$.
Nore.-The quantities from above table divided by two give the plus correc.
tions for $\frac{8+8^{\prime}}{2}=\frac{3}{4}$.

TABLE No. 18.
Factors for Correction of Contents on Curves.

| $\begin{aligned} & d_{s} d^{\prime} \\ & \text { in } \\ & \text { feet. } \end{aligned}$ | Factor. | $\left\lvert\, \begin{gathered} d s d^{\prime} \\ \text { in } \\ \text { feet. } \end{gathered}\right.$ | Factor. | $\left\|\begin{array}{c} d \rho d^{\prime} \\ \text { in } \\ \text { feet. } \end{array}\right\|$ | Factor. | $\left\lvert\, \begin{gathered} d_{s} d^{\prime} \\ \text { in } \\ \text { feet. } \end{gathered}\right.$ | Factor. | $\begin{gathered} d_{s} d^{\prime} \\ \text { in } \\ \text { feet. } \end{gathered}$ | Factor. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | . 00022 | 21 | . 00452 | 4 I | . 00883 | 61 | .OI314 | 81 | .OI745 |
| 2 | . 00043 | 22 | . 00474 | 42 | . 00905 | 62 | . 01336 | 82 | . 01767 |
| 3 | . 00065 | 23 | . 00496 | 43 | . 00926 | 63 | . 01357 | 83 | .or 788 |
| 4 | . 00086 | 24 | .005I7 | 44 | . 00948 | 6.4 | .OI379 | 84 | . 01810 |
| 5 | .00108 | 25 | . 00539 | 45 | . 00970 | 65 | . 01400 | 85 | . 01831 |
| 6 | .00129 | 26 | . 00560 | 46 | .00991 | 66 | .OI422 | 86 | .OI853 |
| 7 | .00151 | 27 | . 00582 | 47 | .OIOI3 | 67 | .OI444 | 87 | .OI875 |
| 8 | .00172 | 28 | . 00603 | 48 | . 01034 | 68 | .01465 | 88 | .or896 |
| 9 | .00194 | 29 | . 00625 | 49 | . 01056 | 69 | . 01487 | 89 | .orgr |
| Io | . 00215 | 30 | . 00646 | 50 | . 01077 | 70 | .OI 508 | 90 | .OI939 |
| II | . 00237 | 31 | . 00668 | 51 | .orog9 | 71 | .OI530 | 91 | .01961 |
| 12 | . 00259 | 32 | .00689 | 52 | .OII20 | 72 | .OI551 | 92 | .org82 |
| 13 | . 00280 | 33 | .00711 | 53 | .OII42 | 73 | .OI573 | 93 | . 02004 |
| 14 | . 00302 | 34 | . 00733 | 54 | .O1163 | 74 | .OI594 | 94 | . 02025 |
| 15 | . 00323 | 35 | . 00754 | 55 | .OII85 | 75 | .01616 | 95 | . 02047 |
| 16 | . 00345 | 36 | .00776 | 56 | . 01207 | 76 | .01637 | 96 | . 02068 |
| 17 | . 00366 | 37 | . 00797 | 57 | . 01228 | 77 | .OI659 | 97 | .02090 |
| 18 | . 00388 | 38 | .00819 | 58 | .OI250 | 78 | .01681 | 98 | .02III |
| 19 | . 00409 | 39 | . 00840 | 59 | .01271 | 79 | . 01702 | 99 | .02133 |
| 20 | .0043I | 40 | . 00862 | 60 | . 01293 | 80 | .OI724 | 100 | .02155 |

## The Construction of Tables of Contents of Level Cuttings.

Base $=b$; half sum of side slopes $=s$.
For each 0.1 of height, the second difference $=(0.074074+) s$.
Between heights 0.0 and 0.1 first difference $=\frac{10 b+s}{27}$

$$
\begin{aligned}
& \begin{array}{lll}
" & " & 2.7=10 b+27 \times s \\
" & " & 5.4=20 b+27 \times 4 s
\end{array}
\end{aligned}
$$

To write out a table of level cuttings progressing in height by tenths, rule five columns carried to heights of 2.7 when $s=1$ or one of its multiples, and to heights of 5.4 when $s=\frac{1}{4}$ or one of its odd multiples.

Example.-(See portion of table given below) $b=28 ; s=1$. Here the second difference $=0.074074+$; first difference between heights 0.0 and $0.1=10.407407+$; between 2.7 and $2.8=12.407407+$.

Place the heights from 0.0 to 2.8 in the first column ; then put first difference $10.40 \% 40 \%+$ in third column opposite 0.0 in first, and second difference $0.0 \% 40 \%+$ immediately above the first difference.

As a test for the continued addition of the second difference, put the first difference $12.40740 \%$ in its place in third column, opposite 2.7 in first. Now add $0.0740 \% 4+$ for each 0.1 of height up to 2.7, taking care to record the repeating fractions correctly, and see that the last addition gives $12.40 \% 40 \%$ + opposite 2.\%. Then add each amount in third column to the amount on its left in second, recording each sum in the next line below, and keeping the repeating fractions correct. The contents in second column opposite 2.7 should be $=$ $106+27 s=307.0$.

Now repeat the amounts in the second column to the nearest tenth, placing them in the fourth column, and as before with regard to the heights in the first. From the fourth column, by subtraction, write the first differences anew, to the nearest tenth, in the fifth column, and opposite their respective positions in the third.

For the remainder of the table, rule columns in sets of threes; the first of each set to contain respectively the heights from 2.8 to $5.4,5.5$ to $8.1,8.2$ to 10.8 , etc. Then increase each of the first differences in the 5th column by $2 s=2.0$, and the first differences from 2.8 to 5.4 are obtaned for the eighth column. These again increased by 2.0 give
the first differences from 5.5 to 8.1 for the eleventh column, etc. In this way the first differences for the whole table may be written to one place of decimals. Each first difference is to be added to the contents opposite in the next column on the left, and the sum recorded in the first line below. With contents calculated by Formula $\mathbf{C}=(b+h s)$ $h \times \frac{100}{27}$ at intervals for tests, mistakes are almost impossible.

To carry out the table to whole numbers only, repeat the second column to the nearest whole number, get the first differences to whole numbers by subtraction, and proceed in all respects as above directed.*

| (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (II) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Contents. | $\begin{array}{r} 0.074074 \\ 10.407407 \end{array}$ |  | $\begin{aligned} & \text { 荡 } \\ & \stackrel{\rightharpoonup}{\Delta} \end{aligned}$ |  | ¢ E. 0 0 0 | $\begin{aligned} & \stackrel{\leftrightarrow}{\hat{\omega}} \\ & \stackrel{\rightharpoonup}{a} \end{aligned}$ |  |  | 渵 |
| .I | 10.407407 | 10.48148I | 10.4 | 10.5 | 2.8 | 319.4 | 12.5 | 5.5 | 682.4 | 14.5 |
| . 2 | 20.888888 | 10.555555 | 20.9 | 10.5 | . 9 | 331.9 | 12.5 | . 6 | 696.9 | 14.5 |
| . 3 | 31.444444 | 10.629629 | 31.4 | 10.7 | 3.0 | 344.4 | 12.7 | . 7 | 711.4 | 14.7 |
| . 4 | 42.074074 | 10.703703 | $42.1{ }^{\text {- }}$ | 10.7 | . 1 | 357.1 | 12.7 | . 8 | 726.1 | 14.7 |
| . 5 | 52.777777 | 10.777777 | 52.8 | 10.8 | . 2 | 369.8 | 12.8 | . 9 | 740.8 | 14.8 |
| . 6 | 63.555555 | 10.851851 | 63.6 | 10.8 | - 3 | 382.6 | 12.8 | 6.0 | 755.6 | 14.8 |
| . 7 | 74.407407 | 10.925925 | 74.4 | 10.9 | 4 | 395.4 | 12.9 | . 1 | 770.4 | I 4.9 |
| . 8 | 85.333333 | 11.0 | 85.3 | 11.0 | . 5 | 408.3 | 13.0 | . 2 | 785.3 | 15.0 |
| . 9 | 96.333333 | 11.074074 | 96.3 | 11.1 | . 6 | 421.3 | 13.1 | - 3 | 800.3 | 15.1 |
| I. 0 | 107.407407 | II.148148 | 107.4 | 11.2 | . 7 | 434.4 | 13.2 | -4 | 815.4 | 15.2 |
| . 1 | 118.555555 | 11.222222 | 118.6 | 11.2 | . 8 | 447.6 | 13.2 | . 5 | 830.6 | 15.2 |
| . 2 | 129.777777 | 11.296296 | 129.8 | 11.3 | . 9 | 460.8 | 13.3 | . 6 | 845.8 | r 5.3 |
| . 3 | 141.074074 | 11.370370 | 141.I | 11.3 | 4.0 | 474.1 | 13.3 | . 7 | 861.1 | 15.3 |
| 4 | 152.444444 | II. 444444 | 152.4 | 11.5 | . 1 | 487.4 | 13.5 | . 8 | 876.4 | 15.5 |
| .5 | 163.888888 | 11.518518 | 163.9 | 11.5 | . 2 | 500.9 | 13.5 | . 9 | 891.9 | I5.5 |
| . 6 | 175.407407 | 11.592592 | 175.4 | 11.6 | - 3 | 514.4 | 13.6 | 7.0 | 907.4 | 15.6 |
| .7 | 187.0 | 11.666666 | 187.0 | 11.7 | $\cdot 4$ | 528.0 | 13.7 | . 1 | 923.0 | 15.7 |
| . 8 | 198.666666 | 11.740740 | 198.7 | 11.7 | . 5 | 541.7 | 13.7 | . 2 | 938.7 | 15.7 |
| . 9 | 210.407407 | 11.814814 | 210.4 | 11.8 | . 6 | 555.4 | 13.8 | - 3 |  | 15.8 |
| 2.0 | 222.222222 | 11.888888 | 222.2 | 11.9 | .7 | 569.2 | 13.9 | - 4 |  | 15.9 |
| . 1 | 234.111111 | 11.962962 | 234.1 | 12.0 | . 8 | 583.1 | I 4.0 | . 5 |  | 16.0 |
| . 2 | 246.074074 | 12.037037 | 246.1 | 12.0 | . 9 | 597.I | 14.0 | . 6 |  | 16.0 |
| $\cdot 3$ | 258.111111 | 12.111111 | 258.1 | 12.1 | 5.0 | 6 II .1 | 14.1 | . 7 |  | 16.1 |
| . 4 | 270.222222 | 12.185185 | 270.2 | 12.2 | . 1 | 625.2 | 14.2 | . 8 |  | 16.2 |
| . 5 | 282.407407 | 12.259259 | 282.4 | 12.3 | . 2 | 639.4 | 14.3 | . 9 |  | 16.3 |
| . 6 | 294.666666 | 12.333333 | 294.7 | 12.3 | - 3 | 653.7 | 14.3 | 8.0 |  | 16.3 |
| 2.7 | 307.0 | 12.407407 | 307.0 | 12.4 | . 4 | 668.0 | 14.4 | 8.I | 1083.0 | 16.4 |
| 2.8 | 319.407407 |  | 319.4 |  |  |  |  |  |  |  |

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[^0]:    * In this article, whether the end sections are carried to intersection of side slopes or not, their areas are expressed by $A$ and $A^{\prime}$.

[^1]:    * "Easy Rules for the Measurement of Earthworks by means of the Prismoidal Formula. By Ellwood Morris, C.E." Philadelphia: 1872.

[^2]:    * See article on the application of the prismoidal formula, page 16.

[^3]:    * When centre heights and transverse surface slopes only are given, if $r=$ ratio to 1 of surface slope $=$ cotangent of surface angle, and $s^{\prime}=8$, then the equivalent level height $=h=\left(c+\frac{b}{2 s}\right) \frac{r}{\sqrt{r^{2}-8^{2}}}-\frac{b}{28}$.

[^4]:    * In case the second column does not give a whole number at the height of 2.7, it should be carried out to 5.4 , or to the requisite multiple of 2.7 .

