

UC-NRLF



QB 272 082

TF

216

T7



15-10873

FBOM

THOMAS TENNENT'S

SURVEYING & NAVIGATION

WAREHOUSE,

SIGN OF WOODEN SAILOR,

New Merchants' Exchange,

Cor. Battery & Oregon sts

San Francisco



LIBRARY

OF THE

UNIVERSITY OF CALIFORNIA.

GIFT OF

Mrs Harriet Day Palmer

Received *August* 1897.

Accession No. *66938.* Class No. -

100
98.48
1.52
1.52
1.52
4.56

662.80
4.56
658.24
246.
719.

1726.00
2095.11

THE UNIVERSITY OF CHICAGO

PHYSICS DEPARTMENT

PHYSICS 311

LECTURE 10

LECTURE 10

LECTURE 10

THE
FIELD PRACTICE
OF
LAYING OUT CIRCULAR CURVES
FOR
RAILROADS.

BY JOHN C. TRAUTWINE,
CIVIL ENGINEER.

THIRD EDITION, REVISED.



PHILADELPHIA:

PUBLISHED BY WILLIAM HAMILTON,
HALL OF THE FRANKLIN INSTITUTE.

1853.

TF 216
T 7

Entered according to Act of Congress, in the year 1851, by
JOHN C. TRAUTWINE,
in the Clerk's Office of the District Court of the United States for the Eastern
District of Pennsylvania.

STEREOTYPED BY L. JOHNSON AND CO.
PHILADELPHIA.

6693-8



PREFACE.

I HAVE been induced to prepare this little volume almost entirely with reference to the wants of the many young men who desire to qualify themselves for field service in an Engineer Corps. On that account, I have endeavored, by the use of the plainest language, to render the subject intelligible to *them*,—dispensing with that mathematical brevity which would have better accorded with the requirements of those who have already attained to some degree of proficiency in elementary field operations. Still, I trust that it will not prove unacceptable even to the latter.

The Table of Natural Sines and Tangents to single minutes, in a form sufficiently portable for field use, will supply a want which I have myself frequently experienced, not only in the operation of laying out curves, but on many other occasions.

One object in preparing it, was to furnish the profession with a Table that should be not only portable, but *absolutely reliable*. Those whose occupations compel them to resort to the Tables in common use, must have frequently experienced, like myself, the extreme embarrassment which attends the inaccuracies to which they are all subject. So long as a Table is known to contain a single error, the position of which is not ascertained, its employment is attended with doubt in every instance in which we are obliged to refer to it. On this account, I have not only prepared these Tables with the most scrupulous care, while in common type, but in order to render their accuracy a matter of certainty, I had them stereotyped, and afterwards revised three times with the utmost caution. I therefore feel no hesitation in saying that they may be depended upon *absolutely*. The same remark applies to the other Tables contained in the volume.

As Hassler's and Hutton's Tables of Natural Sines and Tangents are those most in use among the profession, it will be desirable to

those persons who possess them, to be able to correct the following errors, which I detected in comparing them.

In Hutton's Tables, Fifth Edition, 1811.

Sine of $6^{\circ} 8'$, for $\cdot 1063425$, read $\cdot 1068425$.

Page 328, at top, for 25 Deg., read 40 Deg.

Tangent of $44^{\circ} 60'$, for $\cdot 1000000$, read $1\cdot 000000$.

Tangent of $41^{\circ} 60'$, for $\cdot 8994040$, read $\cdot 9004040$.

In Dr. Gregory's Corrected Edition (the 8th) of Hutton's Tables, 1838

Sine of $49^{\circ} 14'$, for $\cdot 7576751$, read $\cdot 7573751$.

In Hassler's Tables, 1830.

Sine of $78^{\circ} 24'$, read $\cdot 9795752$.

Sine of $20^{\circ} 60'$, " $\cdot 3583679$.

Sine of $66^{\circ} 19'$, " $\cdot 9157795$.

Sine of $56^{\circ} 39'$, " $\cdot 8353279$.

Sine of $55^{\circ} 20'$, " $\cdot 8224751$.

Sine of $53^{\circ} 4'$, " $\cdot 7993352$.

Sine of $48^{\circ} 12'$, " $\cdot 7454760$.

Sine of $45^{\circ} 3'$, " $\cdot 7077236$.

The foregoing I believe to be all the errors in the Natural Sines and Tangents to *whole* minutes, in the respective tables. The discrepancies of 1 in the 7th decimal, I have not considered as errors, as they are occasioned by a neglect of the value of the 8th decimal. For calculating curves, it is not necessary to use more than 4 decimals.

It is scarcely necessary to remark that, beyond 44° , the Sines, Tangents, &c. are read *upwards*, from the bottom of the page, using the corresponding column of minutes. To find the sine of an angle exceeding 90° , subtract the angle from 180° , and take out the sine of the remainder—because the sine of an angle, and that of what it wants of 180° , are the same.

In this edition the Tables of Radii and Ordinates have been extended.

JOHN C. TRAUTWINE.

ERRATA.—None.



FIELD PRACTICE

OF

LAYING OUT CIRCULAR CURVES

FOR

RAILROADS.

ARTICLE I.

PRINCIPLES OF LAYING OUT CURVES.

METHOD 1.

To lay out a Curve by means of Tangential Angles.

IF from any point B, fig. 1, in a straight line A D, we lay off any number of equal angles, as D B s, s B t, t B u, u B v, &c., and at the same time make the chords B s, s t, t u, u v, &c. equal to each other, then the points B, s, t, u, v, &c. will be situated in the circumference of a circle, which is tangential to the line A D at the point B.

The first of these angles, D B s, is called the *tangential angle*, as being that by which the curve is connected with the tangent A D; but inasmuch as the others are all equal to it, they also are called tangential angles.

If any obstacle, as *h*, should prevent our seeing from B farther than to *v*, the curve may be continued by removing

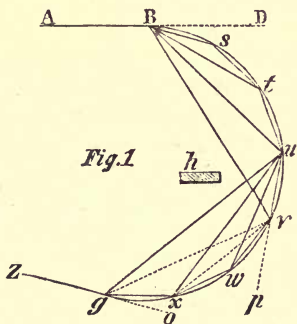


Fig. 1

the instrument to u , the point preceding v ; thence sighting first on v , continue to lay off additional tangential angles $v u w$, $w u x$, &c., as before. Or else, moving the instrument to v itself instead of to u , sight back to u , and lay off first the exterior angle $p v w$, equal to *double* the tangential angle, and afterward continue the tangential angles $w v x$, $x v g$, &c., as before, to the end of the curve.

Finally, in order to pass from the end of the curve at g , on to a tangent $g z$, place the instrument at g , and sighting back to x , lay off the tangential angle $x g o$; then $o g$ continued toward z will be the required tangent. (See Art. IV.)

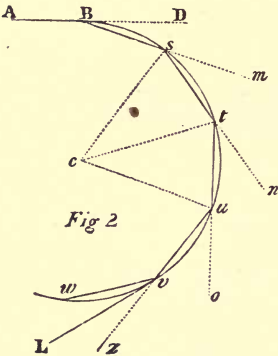
For the tangential angles corresponding to different radii, and chords of 100 feet, see page 25.

ARTICLE II.

METHOD 2.

To lay out a Curve by means of Deflection Angles.

Fig. 2. First, having, as in method 1, laid off a tangential angle $D B s$, and measured the chord $B s$, remove the instrument to the end s of the chord, and make the exterior angle $m s t$ equal to *twice* the tangential angle, and measure the chord $s t$; and so on at the other points t, u, v , &c., making each of the exterior angles $n t u$, $o u v$, &c. equal to twice the tangential angle, and all the chords equal; then will the points B, s, t, u, v , &c. be in the circumference of a circle which is tangential to the line $A D$ at the point B , as by the first method.



But if, at any of these points, as v , we wish to pass off to a tangent $v L$, employ at that point the *tangential* angle $z v L$, equal to half the deflection angle $z v w$. (See Art. IV.)

These exterior angles, included between any *chord* and the extension of the preceding *chord*, are called *deflection*

angles, or *angles of deflection*, or *angles of curvature*. In any given circle, the angle of deflection is always precisely double the tangential angle, supposing the chords to be equal. At page 25, we give tables of the angles corresponding to circles of different radii, embracing the limits of railroad practice; and calculated for chords 100 feet in length, that being the usual length for a measuring chain on public works.

N. B. The deflection angle of any curve is equal to the angle $t c u$, or $t c s$, &c. at the centre of the circle, subtended by one of the equal chords $t u$ or $t s$. This angle at the centre, so subtended, is called the *central angle*. The tangential angle, being always half the deflection angle, is, of course, always half the central angle.

ARTICLE III.

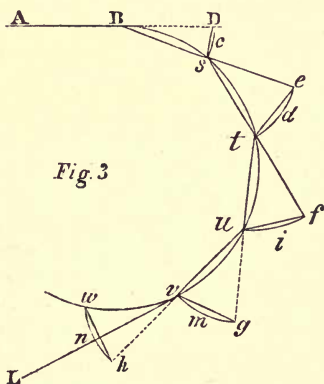
METHOD 3.

To lay out a Curve by Eye.

The *deflection angles*, fig. 3, $e s t$, $f t u$, $g u v$, $h v w$, &c., being double, the *tangential angle* $D B s$, the arcs $e d t$, $f i u$, $g m v$, $h n w$, &c., are double the arc $D c s$, since the arcs of circles are proportionate to the angles which they subtend; but the *chords* $e t$, $f u$, $g v$, $h w$, &c. are not double the chord $D s$, since the chords of arcs are not proportionate to the arcs, or to the angles which they subtend.

The chords $e t$, $f u$, $g v$, $h w$, &c., which subtend the deflection angles, are called *deflection distances*; and the chord $D s$, which subtends the tangential angle, is called the *tangential distance*.

But although, in any given circle, the deflection distance is not *truly* twice the tangential distance, yet the difference



is so trifling in large railroad curves, with chords of but 100 feet, that it may generally be neglected in curves of more than 300 feet radius.

In our tables the *precise* length of both will be found for different radii, and for chords of 100 feet.

Having these respective distances, we may frequently trace a curve on the ground by the eye only, with very tolerable accuracy, sufficient for guiding the excavations and embankments, especially on nearly level ground. Suppose, for instance, it be required to lay out in this manner a curve of 5730 feet radius.

First, find by the table, page 25, or by Art. XVI, the deflection distance et or fu , &c., corresponding to a radius of 5730 feet for a chord of 100 feet, viz. 1.745 feet; and also the tangential distance ds .873 of a foot.

Then from the starting point B, and in line with A B, measure B D equal 100 feet; and put a pin at D. Also from B, measure the chord B s, equal 100 feet; at the same time measuring with a graduated rod, from the pin D, the *tangential* distance D s, equal to .873 of a foot; and place a stake at s. The pin at D may then be removed.

Next, make se equal 100 feet, placing a pin at e , precisely in line with sB ; also from s measure st equal 100 feet; at the same time measuring with the rod from the pin e , the *deflection* distance et , equal to 1.745 feet. Place a stake at t , and remove the pin at e . In this manner proceed to find other points as far as the end of the curve at v .

In order to pass from the curve, as at v , to a tangent vL , proceed as before, only using the tangential distance hn , instead of the deflection distance hw . (See Art. IV.)

This method is abundantly accurate for laying out curves on a canal, or common road; and will occasionally answer very well, when carefully performed, for railroad curves, in the absence of an instrument. Thin straight rods, iron-pointed, and a plumb line should be used for ranging the points in the latter case.

The transit instrument is the best for tracing curves, and running lines generally. I prefer the graduations to run from the same zero, right and left, to 180° each way. There should be two verniers, graduated to minutes; by their means half, or even quarter minutes may generally be estimated with considerable certainty. The telescope revolving in a vertical plane, greatly expedites the laying off of exte-



rior angles, after having first sighted backward to the point behind.

The verniers are sometimes graduated to hundredths of a degree; and this division is, in certain cases, the best; but for *general* purposes, the division into minutes is to be preferred, as all the printed tables of sines, tangents, &c., are calculated for that division.

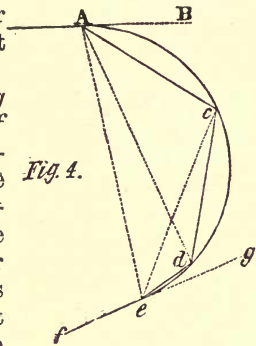
ARTICLE IV.

On Sub-Chords.

We have hitherto spoken of curves as if they were composed of equal chords, each of 100 feet in length. It frequently happens, however, that at the end of a curve, as at *e*, fig. 4, we are obliged to use a shorter, or sub-chord *d e*, in order to unite properly with the tangent *e f*.

In that case, and when using *Method 1., Art. I., of laying off curves by means of tangential angles*, we must, in order to fix the point *e*, lay off a *sub-tangential* angle *d A e*, as much smaller than the entire tangential angle *B A c*, or *c A d*, &c., as the sub-chord *d e* is smaller than an entire 100 feet chord, *a c*, *c d*, &c. Thus if the sub-chord be one-half, or one-fourth, &c. of the entire chord, the sub-tangential angle must be one-half, or one-fourth, &c. of the entire tangential angle.

Fig. 4.



This method is not mathematically exact, for the reason stated in Art. III. (viz. that the *chords* subtending different angles are not proportional to those angles;) yet, for curves of 300 or more feet radius, and with chords not exceeding 100 feet in length, the error is not observable in practice.

In like manner, when we pass off from a sub-chord, as at *e*, to a second tangent, *e f*, we must place the instrument at *e*, and lay off the same sub-tangential angle *d e g*; or which is better, take sight from *e* to *c*, and lay off the angle *c e g*, equal to the *sum* of a tangential and the sub-tangential angle.

But when using Method 2, Art. II. of deflection angles, or Method 3, Art. III. of deflection distances, we may calculate the sub-deflection angle, $a s e$, fig. 5, and sub-deflection distance $a e$, formed between a sub-chord $s e$, and the extension $s a$, of an entire chord $g s$, with sufficient accuracy for curves of 300 or more feet radius, and chords of not more than 100 feet, thus:

Rule.—Say, as an entire chord of 100 feet is to the sub-chord $s e$, so is the deflection angle of the curve, to a certain angle. Add these two angles together and divide their sum by 2, for the sub-deflection angle $a s e$, of the sub-chord.

Example.—The curve, fig. 5, has a radius of 319.6 feet, and an angle of deflection, $f g s$, of 18° for chords of 100 feet. The sub-chord $s e$ is 25 feet in length; what is the sub-deflection angle $a s e$; and also the sub-deflection distance $a e$, for the sub-chord $s e$?

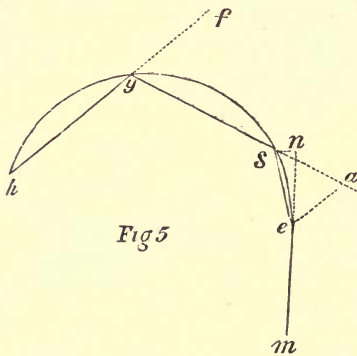


Fig 5

	Chord.	Sub-Chord.
Here, as	100	is to 25,
	Def. An. of	Certain
	100 ft. chord.	Angle.
So is	18°	to $4^\circ 30'$.

The sum of these two angles, 18° and $4^\circ 30' = 22^\circ 30'$, the half of which is $11^\circ 15'$, the required sub-deflection angle $a s e$.

Again, to find the sub-deflection distance $a e$, of the sub-chord $s e$; take from the table of sines, the natural sine of *one-half* the sub-deflection angle $a s e$, just found. Multiply this natural sine by 2, and multiply that product by the length of the sub-chord.

Example.—The sub-deflection angle is $11^\circ 15'$; one-half of it is $5^\circ 37\frac{1}{2}'$, the tabular natural sine of which is .0979, which multiplied by 2, gives .1958; and this multiplied by the sub-chord, 25 feet, gives 4.895 feet, the required sub-deflection distance $a e$.

Finally, to find the sub-tangential distance $s n$, by means of which to pass from e to the tangent $e m$, say, as 10000

is to the square of the sub-chord in feet; so is the *tangential* distance for a 100 feet chord, to $s n$. In this instance, we have as 10000 is to 625, so is 15.69 feet to .980 feet, or $s n$.

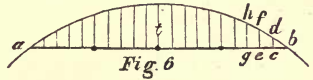
ARTICLE V.

Ordinates for Entire Chords.

It would be both tedious, and liable to inaccuracy, to attempt to fix all the necessary points in railroad curves by the foregoing means, which are employed only for entire chords, or for such sub-chords as may be required at the ends of curves.

The best method is to stretch a piece of twine $a b$, fig. 6,

100 feet long, between two adjacent chord-stakes, and measure off as nearly as may be at right angles to it, with a graduated rod, the previously



calculated ordinates, $c d, e f, g h$, &c., placing pegs at d, f, h , &c.* Our table of ordinates, page 28, is calculated for distances apart $b c, c e, e g$, &c., of 5 feet; and for all curves likely to occur in practice. The 5 feet distances on the twine should be marked by knots or otherwise; and those at the center, and half way between it and the ends, be further distinguished by tying on pieces of tape.

The 5 feet distances are only used (after the excavations and embankments are finished) for placing pegs to guide the laying of the rails, and then only for very sudden curves; for those of large radii, distances of 10 feet are quite sufficient, or even 25 feet for very easy curves. For guiding the curves of the cuttings and fillings, it is not necessary to place the stakes nearer than 50 feet apart; unless for those of less than about 1000 feet radius, when they may be placed 25 feet apart. Ordinates for radii intermediate of those in the table, may either be calculated by the rules given further on; or they may be taken proportionally intermediate of the tabular ones, with sufficient accuracy for practice.

Ordinates for Sub-Chords.

These may readily be calculated *approximately enough*

* On the tops of these stakes, small tacks are driven to define the precise point in the curve.

for railroad practice, for curves of over 300 feet radius, and for chords not exceeding 100 feet, thus: In a circle of given radius, not less than about 300 feet, the ordinates of an entire 100 feet chord may be assumed to be to those of a sub-chord, as the square of the chord is to the square of the sub-chord.

In all our tables the chord is supposed to be 100 feet, the square of which is 10000; the rule therefore becomes, as 10000 feet : to square of sub-chord in feet :: Ord. of Chord : Ord. of Sub-chord *approximately*.

Example.—In a curve of 5730 feet radius, the middle ordinate of a 100 feet chord is .218 of a foot; what will be the length of the middle ordinate of a sub-chord of 50 feet? Here,

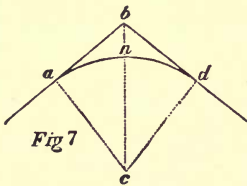
Sq. of 100 ft. :	Sq. of 50 ft. ::	Mid. Ord. of Chord. :	Mid. Ord. Sub-Chord <i>approximately</i> .
10000 :	2500 ::	.218 ft. :	.0545 ft.

And so of any other ordinate, always supposing the chord and sub-chord to be divided into the *same number of parts*.

ARTICLE VI.

Having given the angle a b d, fig. 7, it is required to find the point a or d, at which to commence a curve of given radius.

Rule.—Subtract half the angle $a b d$ from 90° ; the remainder will be the angle $b c a$, or $b c d$. From the table of tangents take the natural tangent of $b c a$, and multiply it by the given radius; the product will be $b a$, or $b d$.



Example.—Let the angle $a b d$ be 120° , how far from b must we begin, at a or d , to lay out a curve

$a n d$, of 2865 feet radius?

Here, half of the angle $a b d = 60^\circ$, which taken from 90° leaves the angle $b c a = 30^\circ$. The natural tangent of $30^\circ = .5773$, which multiplied by the radius of 2865 feet, gives 1653.96 feet for $b a$ or $b d$. (See Art. XII.)

ARTICLE VII.

Having given the angle $a b d$, fig. 7, and the distance from b to a or d , at one of which we wish to commence a curve, it is required to find what radius $a c$ or $c d$, the curve must have, in order to unite with $b a$ and $b d$ tangentially at a and d .

Rule.—Subtract the angle $a b c$, which is half the angle $a b d$, from 90° ; the remainder will be the angle $b c a$, or $b c d$. Then as nat. sine of $b c a$,* is to nat. sine of $a b c$,† so is $a b$ to $a c$, the radius required.

Example.—Let the angle $a b d$ be 120° , and the distance $b a$ or $b d$ 1654 feet; what will be the radius $a c$ or $c d$ of a circle that shall touch a and d tangentially.

Here the angle $a b c =$ half the angle $a b d$, is 60° , which taken from 90° , leaves the angle $b c a$, or $b c d = 30^\circ$. Then as the nat. sine of $b c a$ (30°) = .5000 is to nat. sine of $a b c$, (60°) = .8660, so is $b a$ (1654 feet) to $a c$, (2865 feet,) the radius required.

ARTICLE VIII.

Having given the radius $a c$, fig. 7, of a curve, and the angle $a b d$, it is required to find the number of chords of 100 feet that will constitute the curve.

Rule.—Subtract the angle $a b d$ from 180° , and divide the remainder by the angle of curvature, or deflection of the curve. The quotient will be the required number of chords.

Example.—Let the angle $a b d$ be 120° , and the radius $a c$, 2865 feet.

Here the angle $a b d$, 120° , subtracted from 180° , leaves a remainder of 60° ; which, divided by 2° , the angle of deflection for a curve of 2865 feet, gives a quotient of 30; which is the required number of chords of 100 feet.

N. B.—Had the quotient contained a *fraction* of a chord, it would have indicated that we should have had to employ a sub-chord at the end of the curve; for instance, had the number of chords been $30\frac{1}{2}$, a sub-chord of 50 feet (very approximately) would have been necessary.

* The angle opposite the given side, $a b$.

† The angle opposite the required side, $a c$.

ARTICLE IX.

How to proceed when the end of a curve does not correctly join the tangent.

We sometimes find, in running out a curve for the number of chords determined by the Rule in the preceding Article, that instead of uniting as it should with the previously determined tangent $d m$, fig. 8, at o , it ends tangentially to a line *parallel* to said tangent, either *within* it, as at c ; or *beyond* it, as at b . Being first certain that no error has occurred in tracing out the curve, ascertain with the compass the bearing of the tangent $a d$, and, removing the compass to the end of the curve at c or b , (as the case may be,) run the line $b o$ or $c o$, in the same course as $a d$, until it strikes the tangent $d o m$; which may be ascertained by ranging two stakes placed on the tangent.

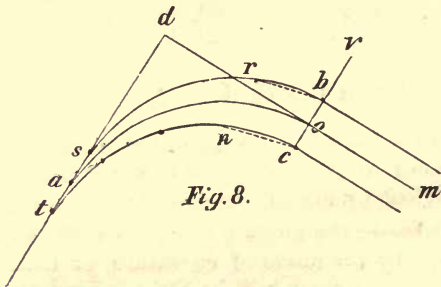


Fig. 8.

Then measure $b o$, or $c o$, (as the case may be,) and if the curve fall *within* the tangent $o m$, as at c , measure *forwards* from t towards d , the distance $t a$, equal to $c o$; or if the curve fall *beyond* the tangent, as at b , measure *backwards* from s , the distance $s a$ equal to $b o$. Then the curve retraced from a , will terminate tangentially in $d m$ at o .

N. B.—The direction of $c o$ or $b o$ may be ascertained without a compass, and better, thus: Multiply the *tangential* angle of the curve by *twice* the number of chords run, *less one*; subtract the product from 180° , and sighting back one chord to n or r , lay off the angle $n c b$, or $r b v$, equal to the remainder. For example, if the tangential angle be 10° , and from t to c be 4 chords, then 7 times 10° taken

from 180° leaves the angle $n c b$, or $r b v = 110^\circ$. When the product exceeds 180° , it must be subtracted from 360° , for the angle $n c b$, or $r b v$.*

This case occurs whenever an error has been made in measuring the distance from d to a . If $d a$ be made too short, the curve $s b$ is the result; and if too long, the curve $t c$.

If the error is small, it may be divided equally among the chords by measure, without retracing the curve with an instrument. This method may be employed with perfect security so long as the error does not exceed 1 foot to every chord of 100 feet; and it will never be so great if moderate care be taken.

Thus, if the curve be 20 chords long, and the error 20 feet, the last stake may be moved 20 feet, the next 19, the next 18, &c., as nearly at right angles to the curve as can be judged by the eye.

The same ordinates that would have been used had the curve been correct, will answer for the one so adjusted, without perceptible difference. For other cases, see Art. X.

ARTICLE X.

Again, it may happen that the error is not caused by a mismeasurement of the distance $a e$, figs. 9 and 10, as in the last case; but by mistake in obtaining the angle $a e f$.

Fig. 9.

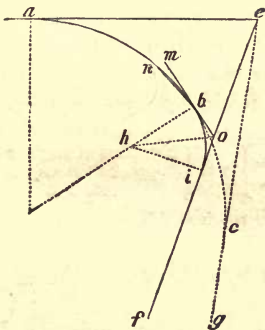
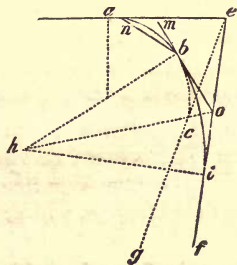


Fig. 10.



If $a e f$, fig. 9, be measured in excess, as $a e g$, then the

* In both cases the angle is measured *outwardly* from the curve; but when the curve falls beyond the tangent, as at b , then $b v$ must be continued inwardly as $b o$.

curve $a b c$, calculated for the incorrect angle $a e g$, will be found to fall *beyond* the true tangent $e f$, as at c ; and the tangents $e g$ and $e f$ not being parallel, the curve cannot be adjusted by either of the methods given in the preceding Article, unless the error be within about 1 foot to each 100 feet length of the curve; in which case, (supposing no other error to exist,) either of those methods may be employed, with sufficient accuracy for practice.

Also, if $a e f$, fig. 10, be measured too small, as $a e g$, then the curve $a b c$, calculated for the incorrect angle $a e g$, will be found to fall *within* the true tangent $e f$, as at c ; when so, the remarks contained in the preceding sentence are equally applicable here. If the error be within 1 foot to 100 feet length of curve, it may be equally divided among the chords. But if greater, we must either remeasure the angle $a e f$ correctly, and go over the whole work again, or resort to some other mode of obviating the difficulty. The angle $a e f$ may be difficult of access; or the curve may be so long that to retrace it would be a work of much labor. We may then adopt the method of *compound curves*, (see Art. XIII.) by which much trouble will be avoided, and a considerable portion of the first part of the curve be allowed to remain as it is.

Thus, whether the curve $a b c$ fall beyond the true tangent $e f$, as in fig. 9, or inside of it, as in fig. 10, place the instrument at b , figs. 9 and 10, (the point at which the change of radius is to take place,) and sighting back one chord to n , lay off the tangential angle $n b m$ of the curve $a b c$, and observe where the tangent $m b$ continued, strikes $e f$, as at o . Measure both $b o$, and the angle $b o f$. Half the angle $b o f$ taken from 90° , gives the angle $b h o$; then say,

As the $\left\{ \begin{array}{l} \text{Nat. Sine of angle } b h o \text{ op-} \\ \text{posite the given side, } b o, \end{array} \right\}$ is to $\left\{ \begin{array}{l} \text{Nat. Sine of angle } b o h \\ \text{opposite the required} \\ \text{side } b h, \end{array} \right\}$

So is The given side $b o$, to The required side, or new radius $b h$.

Ascertain from the table, or by calculation, the angle of deflection, and the tangential angle corresponding to this new radius $b h$; and the new curve commencing at b will terminate tangentially to $e f$ at i , as far from o as o is from b .

For the mode of uniting two curves of different radii, so as to form a *compound curve*, see Article XIII.

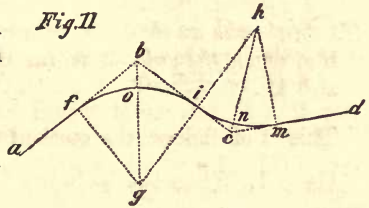
It will be observed, that when the first curve, $a b c$, fig. 10, falls *inside* the tangent $e f$, the new curve must be of *greater* radius; and when *beyond* fig. 9, of a *less* one.

ARTICLE XI.

Having given the angles $a b c$ and $b c d$, fig. 11, and the distance $b c$, it is required to find the greatest radius, $g i$, or $h i$, that can be employed in a REVERSE curve, (see Article XIV) $f o i n m$, for uniting $a b$ to $c d$.

Rule.—Half the angle $a b c$ taken from 90° , leaves the angle $b g i$; and half the angle $b c d$ taken from 90° , leaves the angle $i h c$.

From the table of tangents take the natural tangent ($b i$) of the angle $b g i$; and that ($i c$) of the angle $i h c$; and add them together.



Then as the sum of these two nat. tangents is to the nat. tang. of $b g i$, so is $b c$ to $b i$; and $b i$ taken from $b c$, gives $i c$.

Again, in the triangle $b g i$, as the nat. sine of the angle $b g i$, opposite the given side $b i$, just found, is to the nat. sine of the angle $g b i$, opposite the required side $g i$, so is $b i$, the given side, to $g i$, the required side or radius.

Example.—Let the angle $a b c$ be $71^\circ 40'$, the angle $b c d$ $129^\circ 15'$, and the distance $b c$ 950 feet. What is the length of radius $h i$ or $g i$, of the easiest reverse curve that can be traced for uniting $a b$ to $c d$?

Here, half the angle $a b c$ ($35^\circ 50'$) taken from 90° , leaves the angle $b g i$ $54^\circ 10'$; and half the angle $b c d$ ($64^\circ 37\frac{1}{2}'$) taken from 90° , leaves the angle $i h c = 25^\circ 22\frac{1}{2}'$.

From the table of tangents, we have nat. tang. of $b g i$ ($54^\circ 10'$) = 1.3848; and nat. tang. of $i h c$ ($25^\circ 22\frac{1}{2}'$) = .4743; their sum being 1.8591.

Then as

$$\left. \begin{array}{l} \text{Sum of Tang's.} \\ 1.8591 \end{array} \right\} \text{ is to } \left\{ \begin{array}{l} \text{Tang. of} \\ 54^{\circ} 10' \\ 1.3848, \end{array} \right\} \text{ so is } \left\{ \begin{array}{l} b c \\ 950 \text{ ft.,} \end{array} \right\} \text{ to } \left\{ \begin{array}{l} b i \\ 707.63 \text{ ft.,} \end{array} \right\}$$

and $b i$, 707.63 feet, taken from $b c$, 950 feet, leaves $i c$ 242.37 feet.

Again, as the

$$\left. \begin{array}{l} \text{Nat. Sine} \\ \text{of angle} \\ b g i \\ .8107 \end{array} \right\} \text{ is to } \left\{ \begin{array}{l} \text{Nat. sine of} \\ \text{Angle } g b i \\ .5854, \end{array} \right\} \text{ so is } \left\{ \begin{array}{l} b i \\ 707.63 \\ \text{feet} \end{array} \right\} \text{ to } \left\{ \begin{array}{l} g i \text{ or } h i, \text{ the} \\ \text{required ra-} \\ \text{dius, } 510.97 \\ \text{feet.} \end{array} \right\}$$

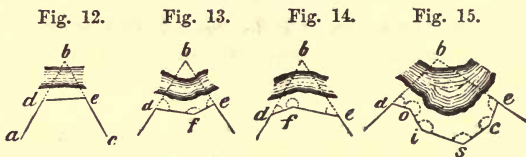
ARTICLE XII.

To obtain the angle $d b e$, formed by two tangents, $d b$, and $b e$, when the point b is inaccessible. Figs. 12, 13, 14, and 15.

This is of frequent occurrence.

CASE 1. When the included figure, fig. 12, has but *three* sides.

Rule.—Subtract the angle $a d e$ from 180° for the angle $b d e$; and subtract the angle $d e c$ from 180° , for the angle $d e b$. Add together $b d e$ and $d e b$, and subtract their sum from 180° , for the angle $d b e$.



CASE 2. When the included figure, $d b e f$, figs. 13 and 14, has *four* sides.

Rule.—Subtract the sum of the three *internal* angles of the figure marked by dotted segments of circle, from 360° , for the angle $d b e$.

CASE 3. When the included figure, 15, has *more than four* sides.

Rule.—Add together all the *internal* angles, marked by dotted segments of circles; and subtract their sum from twice as many right angles as the figure has sides, less four, for the angle $d b e$.

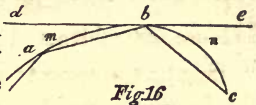
Example.—Let the angles denoted by the dotted segments at the different letters be as follows: That at d , 70° ; at o , 220° ; at i , 150° ; at s , 110° ; at c , 160° ; at e , 100° . The sum of these is 810° . The figure has 7 sides; and twice 7, less 4 = 10; and 10 right angles = 900° ; from which the sum of the designated internal angles (810°) being subtracted, leaves 90° , for the angle $d b e$.

N. B.—When the angle $d b e$ has to be deduced from a figure of many sides, as fig. 15, the errors spoken of in Articles IX. and X. are apt to occur, unless the several sides and the angles o , i , s , &c., be measured with much care. For tracing curves with any accuracy and satisfaction, the instrument should be divided at least into minutes; as before remarked, the transit instrument is the best for the purpose. With moderate care in the preparatory measurement of the sides and angles, errors will seldom occur that may not be adjusted with all the accuracy required in practice, by the very simple method of dividing them equally among the chords, as explained in Articles IX. and X.

ARTICLE XIII.

To pass from one curve, $a m b$, fig. 16, to another, $b n c$, of different radius, but running in the same direction, constituting a COMPOUND curve.

Rule.—Placing the instrument at b , sight back to the other end of the 100 feet chord at a ; and lay off the *tangential* angle $a b d$, of the curve $a m b$; then from the common tangent $d b e$, lay off the *tangential* angle $e b c$, of the curve $b n c$, making at the same time the chord $b c$ equal to 100 feet.

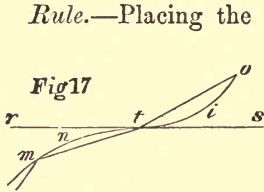


N. B.—If running the curve by eye, use the *tangential distances* instead of the angles.



ARTICLE XIV.

To pass from one curve, $m n t$, fig. 17, to another, $t i o$, of either the same, or of a different radius, but running in an opposite direction; constituting a REVERSE curve.



Rule.—Placing the instrument at t , sight back to the other end of the 100 feet chord at m , and lay off the tangential angle $m t r$, of the curve $m n t$; then from the common tangent $r t s$, lay off the tangential angle $s t o$, of the curve $t i o$; making at the same time the chord $t o$,

equal to 100 feet.

N. B.—If running the curve by eye, use the tangential distances instead of the angles.

ARTICLE XV.

RADII.

To find the radius corresponding to any given angle of deflection, and to equal chords of any given length.

Rule 1.—Subtract the angle of deflection from 180° , then say, as nat. sine of angle of deflection, is to nat. sine of half the remainder, so is the given chord to the radius required.

Example.—Let the angle of deflection be 2° , and the chord 100 feet, required the radius.

Here 2° subtracted from 180° , leaves 178° , the half of which is 89° , and as

$$\begin{array}{ccccccc} \text{Nat. Sine of } 2^\circ & : & \text{Nat. Sine of } 89^\circ & :: & \text{Chord} & : & \text{Radius} \\ \cdot 034899 & : & \cdot 999848 & :: & 100 \text{ feet} & : & 2865 \text{ feet.} \end{array}$$

Rule 2.—The radius for 100 feet chords may be found approximately, by dividing 5730 by the deflection angle.

This rule is very close for radii of not less than 500 feet. For 500 feet it gives eight-tenths of a foot too little, but is more approximate for larger radii.

Example.—What is the radius to a deflection angle of 2° , the chords being 100 feet long?

Here, 5730 divided by 2, gives 2865 feet, the radius required.

ARTICLE XVI.

TANGENTIAL AND DEFLECTION ANGLES.

To find either the Tangential or Deflection Angle corresponding to any given radius, and to equal chords of any given length.

Rule 1.—Divide *half* the chord by the radius; the quotient will be the natural sine of the *tangential* angle. Therefore, the angle corresponding to this sine, in the table of natural sines, will be the tangential angle required; and the tangential angle multiplied by 2 will give the deflection angle.

Example.—Let the radius be 2865 feet, and the chord 100 feet; what will be the tangential and deflection angles?

Here, half the chord, (50 feet,) divided by the radius, (2865 feet,) gives $\cdot 01745$; and the tangential angle in the table corresponding to the natural sine $\cdot 01745$ is 1° , twice which is 2° , the deflection angle required.

Rule 2.—The deflection angle for 100 feet chords may be found approximately by dividing 5730 by the radius. This is very close for curves of over 500 feet radius. For 500 feet it gives about one minute too little.

Example.—What is the deflection angle for a radius of 2865 feet, the chords being 100 each?

Here, 5730 divided by the radius 2865, gives 2° , the deflection angle required.

ARTICLE XVII.

DEFLECTION DISTANCES.

To find the Deflection Distance (exactly) for any given radius, when the chords are 100 feet long.

Rule.—Divide the constant number 10000 by the radius in feet; the quotient will be the deflection angle required.*

Example.—What is the deflection distance to a radius of 5730 feet, the chords being 100 feet long?

Here, 10000 divided by 5730 radius, gives 1.745 feet, the deflection distance required.

To find the Deflection Distance for any given radius, and for equal chords of any given length.

Rule.—Divide half the given chord by radius, the quotient will be the natural sine of one-half the deflection angle; and double this natural sine, multiplied by the chord, will give the deflection distance required. By this rule our table was prepared.

Example.—As before, what is the deflection distance to a radius of 5730 feet, the chords being 100 feet long?

Here, half the chord, (50 feet,) divided by radius, (5730 feet,) gives .008727, which is the natural sine of half the deflection angle. Now .008727, multiplied by 2, gives .017454, which, multiplied by the chord, (100 feet,) gives 1.745 feet, the required deflection distance, the same as in the preceding example.

ARTICLE XVIII.

TANGENTIAL DISTANCES.

To find the Tangential Distance corresponding to any given radius, and to equal chords of any given length.

Rule.—First find the tangential angle by Article XVI., and take from the table of natural sines, that correspond-

* Because the deflection distance to a radius of 10000 feet, with chords of 100 feet, is 1 foot; and the deflection distances for other radii increase *inversely* as the radii.

ing to one-half of the *tangential* angle. Then multiply *double* this sine by the given chord, for the tangential distance. By this rule our table was prepared.

Example.—Let the radius be 2865 feet, and the chords 100 feet each; what will be the tangential distance?

Here we find, by Article XVI., the tangential angle 1° for a radius of 2865 feet.

The natural sine corresponding to 30 minutes, or one-half of this tangential angle, is, by the table of sines, .008727; the double of which is .017454, which, multiplied by the chord, or 100 feet, gives 1.745 feet for the tangential distance required.

ARTICLE XIX.

ORDINATES.

To find the Middle Ordinate to any given radius, and to any given chord.

Rule 1.—From the square of the radius subtract the square of *half* the chord; and take the square root of the remainder from the radius, for the middle ordinate.

Example.—What is the length of the middle ordinate *d e*, fig. 18, the radius *c a* being 819 feet, and the chord *a b* 100 feet?

Here, the square of *c a* (819) is 670761, and the square of *a e* (50) is 2500; which, being subtracted from the former, leaves 668261; the square root of which is *e c*, 817.472; which, taken from the radius 819, leaves 1.528 feet, the required middle ordinate, *d e*.

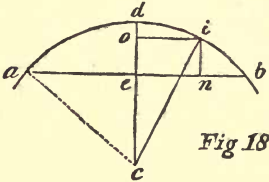
Rule 2.—Subtract the tabular cosine of the *tangential* angle from 1, and multiply the remainder by the radius.

Example.—Same as foregoing, namely, radius 819 feet, angle of deflection 7° , to chords of 100 feet. What will be the length of the middle ordinate?

Here, tabular cosine of $3\frac{1}{2}^\circ$ (the tangential angle) is .998135; which, subtracted from 1, leaves .001865; which, multiplied by 819, the radius, gives 1.527, the middle ordinate required.

ARTICLE XX.

Having given the Middle Ordinate $d e$, fig. 18, it is required to find any other one, as $i n$.



Rule 1.—Subtract the middle ordinate $d e$, from the radius $d c$, the remainder will be $e c$: then from the square of the radius $c i$, subtract the square of the distance $o i$, which the required ordinate $i n$ is from the middle

ordinate $d e$, and extract the square root of the remainder. This square root will be $o c$. From this square root $o c$, subtract $e c$; the remainder will be $o e$, which is equal to $i n$, the required ordinate.

Example.—The middle ordinate $d e$, of a 100 feet chord $b a$, to a radius of 819, being 1.528 feet, it is required to find the length of the ordinate $i n$, 20 feet from the middle one.

Here, the middle ordinate $d e$, 1.528, subtracted from the radius 819, leaves $e c$, 817.472. The square of the radius is 670761; and the square of 20 (the distance of the required ordinate from the middle one) is 400; which taken from 670761, leaves 670361; the square root of which is 818.756, or $o c$; from which take $e c$, or 817.472, and the remainder, 1.284, will be $o e$, which is equal to $i n$, the required ordinate.

Rule 2.—Multiply the ordinates of a 1° curve by the deflection angle of the curve whose ordinates are required, (chords being 100 feet.) This is a sufficiently close approximation for curves of not less than 500 feet radius; and for placing ordinates for guiding the excavations and embankments, it is close enough for the smallest curves in our table.

TABLE OF RADII, &c.—CHORD 100 FEET.

The Tangential Angle is always one-half of the Angle of Deflection.

Angle of Deflection.	Radius in feet.	Deflection distance in feet.	Tangential distance in feet.	Angle of Deflection.	Radius in feet.	Deflection distance in feet.	Tangential distance in feet.
° 1	343800	·029	·014	° 44	7814	1·279	·639
2	171900	·058	·029	45	7640	1·308	·654
3	114600	·087	·043	46	7474	1·337	·668
4	85950	·116	·058	47	7315	1·366	·683
5	68760	·145	·072	48	7162	1·395	·697
6	57300	·174	·087	49	7016	1·424	·712
7	49116	·203	·101	50	6876	1·453	·726
8	42975	·232	·116	51	6741	1·482	·741
9	38200	·262	·131	52	6611	1·511	·755
10	34380	·291	·145	53	6487	1·540	·770
11	31256	·320	·160	54	6367	1·569	·784
12	28650	·349	·174	55	6251	1·598	·799
13	26446	·378	·189	56	6139	1·627	·813
14	24558	·407	·203	57	6032	1·656	·828
15	22920	·436	·218	58	5928	1·685	·842
16	21487	·465	·232	59	5827	1·715	·857
17	20224	·494	·247	i 2	5730	1·745	·872
18	19100	·523	·261	4	5545	1·802	·901
19	18094	·552	·276	6	5372	1·860	·930
20	17190	·581	·290	8	5209	1·918	·959
21	16372	·610	·305	10	5056	1·976	·988
22	15628	·639	·319	12	4912	2·036	1·018
23	14948	·668	·334	14	4775	2·094	1·047
24	14325	·697	·348	16	4646	2·152	1·076
25	13752	·727	·363	18	4524	2·210	1·105
26	13223	·756	·378	20	4408	2·268	1·134
27	12733	·785	·392	22	4298	2·326	1·163
28	12279	·814	·407	24	4193	2·384	1·192
29	11856	·843	·421	26	4093	2·443	1·221
30	11460	·872	·436	28	3998	2·501	1·250
31	11090	·900	·450	30	3907	2·559	1·279
32	10744	·930	·465	32	3820	2·617	1·308
33	10419	·959	·479	34	3737	2·676	1·338
34	10112	·988	·494	36	3657	2·734	1·367
35	9823	1·017	·508	38	3581	2·793	1·396
36	9550	1·046	·523	40	3508	2·851	1·425
37	9292	1·075	·537	42	3438	2·908	1·454
38	9047	1·104	·552	44	3370	2·967	1·483
39	8815	1·133	·566	46	3306	3·025	1·512
40	8595	1·162	·581	48	3243	3·083	1·541
41	8385	1·191	·595	50	3183	3·141	1·570
42	8186	1·221	·610	52	3126	3·199	1·599
43	7995	1·250	·625		3069	3·258	1·629

TABLE OF RADII, &c.—CHORD 100 FEET.

CONTINUED.

The Tangential Angle is always one-half of the Angle of Deflection.

Angle of Deflection.	Radius in feet.	Deflection distance in feet.	Tangential distance in feet.	Angle of Deflection.	Radius in feet.	Deflection distance in feet.	Tangential distance in feet.
1° 54'	3016	3.316	1.658	3° 20'	1719	5.817	2.908
56	2964	3.374	1.687	22	1702	5.875	2.937
58	2914	3.432	1.716	24	1685	5.933	2.966
1° 20'	2865	3.490	1.745	26	1669	5.992	2.996
2	2818	3.548	1.774	28	1653	6.050	3.025
4	2772	3.606	1.803	30	1637	6.108	3.054
6	2729	3.665	1.832	32	1621	6.166	3.083
8	2686	3.723	1.861	34	1606	6.224	3.112
10	2644	3.781	1.890	36	1591	6.282	3.141
12	2604	3.839	1.919	38	1577	6.340	3.170
14	2566	3.897	1.948	40	1563	6.398	3.199
16	2528	3.956	1.978	42	1549	6.456	3.228
18	2491	4.014	2.007	44	1534	6.515	3.257
20	2456	4.072	2.036	46	1521	6.574	3.287
22	2421	4.130	2.065	48	1508	6.632	3.316
24	2387	4.188	2.094	50	1495	6.690	3.345
26	2355	4.246	2.123	52	1482	6.748	3.374
28	2323	4.305	2.152	54	1469	6.806	3.403
30	2292	4.363	2.182	56	1457	6.864	3.432
32	2262	4.421	2.210	58	1445	6.922	3.461
34	2232	4.479	2.239	4	1433	6.980	3.490
36	2204	4.538	2.269	5	1403	7.125	3.562
38	2176	4.596	2.298	10	1375	7.270	3.635
40	2149	4.653	2.326	15	1348	7.416	3.708
42	2122	4.712	2.356	20	1322	7.563	3.781
44	2096	4.770	2.385	25	1298	7.708	3.854
46	2071	4.828	2.414	30	1274	7.853	3.927
48	2046	4.886	2.443	35	1251	7.998	3.999
50	2023	4.944	2.472	40	1228	8.143	4.071
52	1999	5.002	2.501	45	1207	8.289	4.145
54	1976	5.060	2.530	50	1185	8.432	4.216
56	1953	5.118	2.559	55	1166	8.577	4.288
58	1932	5.176	2.588	5	1146	8.722	4.361
30	1910	5.235	2.618	5	1127	8.869	4.434
2	1889	5.293	2.646	10	1109	9.014	4.507
4	1868	5.351	2.675	15	1092	9.159	4.579
6	1848	5.409	2.704	20	1074	9.304	4.652
8	1828	5.468	2.734	25	1058	9.449	4.724
10	1810	5.526	2.763	30	1042	9.595	4.798
12	1790	5.584	2.792	35	1026	9.740	4.870
14	1772	5.642	2.821	40	1011	9.885	4.942
16	1754	5.700	2.850	45	996.8	10.03	5.015
18	1736	5.758	2.879	50	982.7	10.18	5.090

TABLE OF RADII, &c.—CHORD 100 FEET.

CONTINUED.

The Tangential Angle is always one-half of the Angle of Deflection.

Angle of Deflection.	Radius in feet.	Deflection distance in feet.	Tangential distance in feet.	Angle of Deflection.	Radius in feet.	Deflection distance in feet.	Tangential distance in feet.
5 55	969.0	10.32	5.160	12 30	459.3	21.79	10.90
6	955.4	10.47	5.235	45	450.3	22.21	11.12
5	947.5	10.62	5.310	13	441.7	22.64	11.34
10	939.7	10.76	5.380	15	433.4	23.07	11.56
15	917.0	10.90	5.450	30	425.5	23.51	11.77
20	905.0	11.04	5.520	45	417.7	23.94	11.99
25	893.5	11.20	5.600	14	410.3	24.37	12.21
30	882.0	11.34	5.670	15	403.1	24.81	12.43
35	870.7	11.48	5.740	30	396.2	25.24	12.65
40	859.5	11.63	5.815	45	389.6	25.67	12.86
45	849.3	11.78	5.890	15	383.1	26.11	13.08
50	838.9	11.92	5.960	15	376.9	26.52	13.30
55	828.9	12.06	6.030	30	370.8	26.94	13.52
7	819.0	12.21	6.105	45	365.0	27.37	13.73
5	813.3	12.36	6.180	16	359.3	27.83	13.95
10	807.4	12.50	6.250	30	348.4	28.70	14.38
15	790.8	12.64	6.320	17	338.3	29.56	14.82
20	781.9	12.79	6.395	30	328.7	30.43	15.25
25	773.2	12.94	6.470	18	319.6	31.29	15.69
30	764.5	13.08	6.540	30	311.0	32.15	16.12
35	756.1	13.22	6.610	19	302.9	33.01	16.56
40	748.0	13.37	6.685	30	295.3	33.87	16.99
45	739.9	13.51	6.755	20	287.9	34.73	17.43
50	732.0	13.66	6.830	21	274.4	36.44	18.30
55	724.3	13.80	6.900	22	262.0	38.15	19.17
8	716.8	13.95	6.975	23	250.8	39.87	20.02
15	695.1	14.38	7.190	24	240.5	41.58	20.91
30	674.6	14.81	7.405	25	231.0	43.28	21.77
45	655.5	15.25	7.625	26	222.3	44.98	22.64
9	637.3	15.68	7.840	27	214.2	46.68	23.51
15	620.2	16.12	8.060	28	206.7	48.38	24.37
30	603.8	16.55	8.275	29	199.7	50.07	25.24
45	588.4	16.99	8.495	30	193.2	51.76	26.11
10	573.7	17.43	8.715	31	187.1	53.45	26.97
15	559.7	17.87	8.935	32	181.4	55.13	27.83
30	546.4	18.30	9.150	33	176.0	56.80	28.70
45	533.8	18.73	9.365	34	171.0	58.47	29.56
11	521.7	19.17	9.585	35	166.3	60.14	30.42
15	510.1	19.61	9.805	36	161.8	61.80	31.29
30	499.1	20.05	10.03	37	157.6	63.46	32.15
45	488.5	20.50	10.25	38	153.6	65.11	33.01
12	478.3	20.94	10.47	39	149.8	66.76	33.87
15	468.7	21.36	10.69	40	146.2	68.40	34.73

TABLE OF ORDINATES.

Ordinates five feet apart.—Chord one hundred feet.

Distances of the Ordinates from the end of the 100 feet Chord.										
Angle of Def'n.	Middle, 50 feet.	45 feet.	40 feet.	35 feet.	30 feet.	25 feet.	20 feet.	15 feet.	10 feet.	5 feet.
0										
2	·007	·007	·007	·006	·006	·005	·003	·003	·002	·001
4	·014	·014	·014	·013	·012	·010	·008	·008	·005	·003
6	·021	·021	·021	·020	·019	·016	·013	·011	·008	·004
8	·029	·029	·028	·026	·024	·022	·018	·015	·010	·005
10	·036	·036	·035	·033	·031	·027	·023	·019	·013	·007
12	·043	·043	·041	·038	·037	·033	·028	·022	·015	·008
14	·050	·050	·048	·044	·043	·038	·032	·026	·017	·010
16	·058	·058	·056	·052	·049	·044	·037	·030	·020	·011
18	·065	·065	·063	·059	·055	·050	·042	·033	·023	·013
20	·073	·072	·070	·066	·061	·055	·047	·037	·026	·014
22	·080	·079	·076	·071	·067	·060	·051	·041	·029	·015
24	·087	·086	·083	·077	·074	·066	·056	·045	·031	·017
26	·094	·093	·090	·084	·080	·071	·060	·048	·034	·018
28	·102	·101	·098	·092	·086	·077	·065	·052	·036	·019
30	·109	·108	·105	·099	·092	·082	·070	·055	·039	·020
32	·116	·115	·112	·106	·098	·088	·075	·058	·042	·022
34	·123	·122	·118	·111	·104	·094	·079	·062	·044	·023
36	·131	·130	·126	·119	·110	·099	·084	·066	·047	·024
38	·138	·137	·133	·126	·116	·105	·089	·070	·049	·025
40	·145	·144	·140	·133	·123	·110	·093	·074	·052	·027
42	·152	·150	·146	·138	·128	·115	·098	·077	·055	·028
44	·160	·158	·153	·145	·135	·121	·103	·081	·057	·030
46	·167	·165	·160	·152	·141	·126	·107	·085	·060	·032
48	·174	·172	·167	·158	·147	·132	·112	·088	·062	·033
50	·182	·180	·175	·166	·153	·138	·117	·092	·065	·034
52	·189	·187	·181	·171	·159	·143	·122	·095	·068	·035
54	·196	·194	·188	·178	·165	·148	·126	·099	·070	·036
56	·204	·202	·195	·185	·171	·154	·131	·103	·073	·038
58	·211	·209	·202	·192	·177	·159	·136	·107	·075	·039
i	·218	·216	·209	·198	·183	·164	·140	·111	·078	·041
2	·225	·223	·215	·204	·189	·169	·145	·114	·081	·042
4	·233	·231	·223	·211	·196	·175	·150	·118	·083	·043
6	·240	·238	·230	·217	·202	·180	·155	·121	·086	·045
8	·247	·245	·237	·224	·208	·186	·159	·125	·088	·046
10	·254	·252	·244	·231	·214	·191	·163	·130	·091	·048
12	·262	·260	·252	·237	·220	·196	·168	·133	·094	·049
14	·269	·267	·258	·244	·226	·202	·173	·136	·096	·050
16	·276	·274	·265	·251	·232	·207	·177	·140	·099	·052
18	·284	·282	·273	·257	·238	·213	·182	·144	·101	·053
20	·291	·288	·279	·264	·244	·218	·187	·148	·104	·055

TABLE OF ORDINATES—CONTINUED.

Ordinates five feet apart.—Chord one hundred feet.

Distances of the Ordinates from the end of the 100 feet Chord.

Angle of Def'n.	Middle, 50 feet.	45 feet.	40 feet.	35 feet.	30 feet.	25 feet.	20 feet.	15 feet.	10 feet.	5 feet.	
0											
1	22	.298	.295	.285	.270	.250	.224	.192	.151	.107	.056
	24	.306	.303	.293	.277	.256	.229	.197	.155	.109	.057
	26	.313	.310	.300	.284	.263	.235	.201	.159	.112	.059
	28	.320	.317	.307	.291	.269	.240	.206	.163	.114	.060
	30	.327	.324	.314	.297	.275	.246	.210	.167	.117	.062
	32	.334	.331	.321	.304	.281	.251	.215	.171	.120	.063
	34	.341	.338	.328	.310	.287	.257	.219	.174	.122	.065
	36	.349	.345	.335	.317	.293	.262	.224	.178	.125	.066
	38	.356	.353	.342	.323	.299	.268	.228	.182	.127	.068
	40	.364	.360	.349	.330	.305	.273	.233	.185	.130	.069
	42	.371	.367	.356	.337	.312	.278	.238	.189	.133	.070
	44	.378	.374	.363	.343	.318	.284	.242	.192	.135	.072
	46	.385	.382	.370	.350	.324	.289	.247	.196	.138	.073
	48	.393	.389	.377	.356	.330	.295	.251	.200	.141	.075
	50	.400	.396	.384	.364	.336	.300	.256	.204	.144	.076
	52	.407	.403	.391	.370	.342	.305	.261	.208	.147	.077
	54	.414	.410	.398	.376	.348	.311	.265	.211	.149	.079
	56	.422	.418	.405	.383	.354	.316	.270	.215	.152	.080
	58	.429	.425	.412	.389	.360	.322	.275	.219	.154	.082
120		.436	.432	.419	.397	.366	.327	.280	.222	.157	.083
	2	.443	.439	.426	.402	.373	.332	.284	.226	.160	.084
	4	.451	.446	.433	.409	.379	.338	.289	.230	.162	.086
	6	.458	.454	.440	.416	.385	.343	.293	.234	.165	.087
	8	.465	.461	.447	.425	.391	.349	.298	.237	.167	.088
	10	.473	.468	.454	.430	.397	.355	.303	.241	.170	.089
	12	.480	.475	.461	.437	.403	.360	.308	.245	.173	.090
	14	.487	.482	.468	.443	.409	.366	.312	.248	.175	.092
	16	.495	.490	.475	.450	.415	.371	.317	.252	.178	.093
	18	.502	.497	.482	.456	.421	.377	.321	.256	.180	.095
	20	.509	.504	.489	.463	.428	.382	.326	.260	.183	.096
	22	.516	.511	.496	.470	.434	.387	.330	.264	.186	.097
	24	.523	.518	.503	.476	.440	.393	.334	.267	.188	.099
	26	.531	.526	.510	.483	.446	.398	.338	.271	.191	.100
	28	.538	.533	.517	.489	.452	.404	.346	.275	.194	.102
	30	.545	.540	.524	.496	.458	.409	.350	.278	.196	.103
	32	.552	.547	.531	.503	.465	.415	.355	.282	.199	.104
	34	.560	.554	.538	.509	.471	.420	.359	.285	.201	.106
	36	.567	.562	.545	.516	.477	.425	.364	.289	.204	.107
	38	.574	.569	.552	.522	.483	.431	.368	.293	.206	.109
	40	.582	.576	.559	.529	.489	.436	.373	.297	.209	.110

TABLE OF ORDINATES—CONTINUED.

Ordinates five feet apart.—Chord one hundred feet.

Distances of the Ordinates from the end of the 100 feet Chord.										
Angle of Def'n.	Middle, 50 feet.	45 feet.	40 feet.	35 feet.	30 feet.	25 feet.	20 feet.	15 feet.	10 feet.	5 feet.
0										
2	42	.589	.583	.566	.536	.495	.441	.378	.301	.212
	44	.596	.590	.573	.542	.501	.447	.382	.304	.214
	46	.603	.598	.580	.549	.507	.452	.387	.308	.217
	48	.611	.605	.587	.555	.513	.458	.391	.312	.219
	50	.618	.612	.594	.562	.519	.464	.396	.315	.222
	52	.625	.619	.601	.569	.526	.469	.401	.319	.225
	54	.632	.626	.608	.575	.532	.474	.405	.322	.227
	56	.640	.634	.615	.582	.538	.480	.410	.326	.230
	58	.647	.641	.622	.588	.544	.485	.414	.330	.232
3		.654	.648	.629	.595	.550	.491	.419	.334	.235
	2	.661	.655	.636	.602	.556	.496	.424	.338	.238
	4	.669	.662	.643	.608	.562	.502	.428	.341	.240
	6	.676	.670	.650	.615	.568	.507	.433	.345	.243
	8	.683	.677	.657	.621	.574	.512	.438	.349	.246
	10	.691	.684	.664	.629	.581	.518	.443	.353	.249
	12	.698	.691	.671	.635	.587	.523	.448	.357	.251
	14	.706	.698	.678	.642	.593	.529	.452	.360	.254
	16	.713	.705	.685	.649	.599	.534	.457	.364	.257
	18	.720	.713	.692	.655	.605	.540	.462	.368	.259
	20	.727	.720	.699	.662	.611	.545	.466	.371	.262
	22	.734	.727	.706	.668	.617	.550	.471	.375	.264
	24	.742	.734	.713	.675	.623	.556	.475	.378	.267
	26	.749	.742	.720	.682	.629	.561	.480	.382	.270
	28	.756	.749	.727	.688	.635	.567	.485	.386	.272
	30	.764	.756	.734	.695	.642	.573	.489	.390	.275
	32	.771	.763	.741	.702	.648	.578	.494	.394	.278
	34	.779	.770	.748	.708	.654	.584	.498	.397	.280
	36	.786	.777	.755	.715	.660	.589	.503	.401	.283
	38	.793	.785	.762	.721	.666	.594	.508	.405	.285
	40	.800	.792	.769	.728	.673	.600	.512	.408	.288
	42	.807	.799	.776	.734	.679	.605	.517	.412	.291
	44	.814	.806	.783	.741	.685	.611	.521	.415	.293
	46	.822	.814	.790	.748	.691	.616	.526	.419	.296
	48	.829	.821	.797	.754	.697	.621	.531	.423	.298
	50	.836	.828	.804	.761	.703	.627	.536	.427	.301
	52	.843	.835	.811	.768	.709	.632	.541	.431	.304
	54	.850	.842	.818	.774	.715	.638	.545	.434	.306
	56	.858	.850	.825	.781	.721	.643	.550	.438	.309
	58	.865	.857	.832	.787	.728	.648	.555	.442	.311
4		.873	.864	.839	.794	.734	.655	.559	.445	.314

TABLE OF ORDINATES—CONTINUED.

Ordinates five feet apart.—Chord one hundred feet.

Distances of the Ordinates from the end of the 100 feet Chord.											
Angle of Def'n.	Middle, 50 feet.	45 feet.	40 feet.	35 feet.	30 feet.	25 feet.	20 feet.	15 feet.	10 feet.	5 feet.	
4	5	.891	.882	.856	.810	.749	.668	.571	.454	.320	.169
	10	.909	.900	.874	.827	.764	.682	.582	.464	.327	.173
	15	.927	.918	.891	.844	.780	.695	.594	.473	.334	.176
	20	.945	.936	.909	.860	.795	.709	.606	.482	.340	.179
	25	.963	.954	.926	.877	.810	.723	.617	.491	.347	.183
	30	.981	.972	.944	.893	.825	.736	.629	.501	.354	.186
	35	.999	.990	.961	.909	.840	.750	.640	.510	.360	.189
	40	1.017	1.008	.979	.926	.855	.764	.652	.519	.367	.193
	45	1.036	1.026	.996	.943	.871	.777	.664	.529	.373	.196
	50	1.054	1.044	1.014	.959	.886	.791	.676	.538	.380	.199
5	55	1.072	1.062	1.031	.976	.901	.804	.687	.547	.386	.203
	5	1.091	1.080	1.048	.993	.917	.818	.699	.557	.393	.207
	10	1.109	1.098	1.065	1.009	.932	.831	.711	.566	.400	.210
	15	1.127	1.116	1.083	1.026	.947	.845	.722	.576	.406	.214
	20	1.146	1.134	1.100	1.042	.963	.859	.734	.585	.413	.217
	25	1.164	1.152	1.118	1.058	.978	.872	.746	.594	.419	.220
	30	1.182	1.170	1.135	1.075	.993	.886	.757	.603	.426	.224
	35	1.200	1.188	1.153	1.092	1.009	.900	.769	.613	.432	.228
	40	1.218	1.206	1.170	1.108	1.024	.913	.781	.622	.438	.231
	45	1.236	1.224	1.188	1.124	1.039	.927	.792	.631	.445	.235
	50	1.255	1.242	1.205	1.141	1.055	.941	.804	.640	.452	.238
	55	1.273	1.260	1.223	1.157	1.070	.954	.816	.649	.458	.241
6	55	1.291	1.278	1.240	1.174	1.085	.967	.827	.658	.465	.245
	5	1.309	1.296	1.258	1.191	1.100	.982	.839	.668	.472	.248
	10	1.327	1.314	1.275	1.207	1.115	.995	.851	.677	.478	.251
	15	1.345	1.332	1.293	1.224	1.130	1.009	.862	.686	.485	.255
	20	1.364	1.350	1.310	1.240	1.146	1.023	.874	.696	.492	.259
	25	1.382	1.368	1.328	1.256	1.161	1.036	.886	.705	.498	.262
	30	1.400	1.386	1.345	1.273	1.176	1.050	.897	.714	.505	.266
	35	1.419	1.404	1.362	1.290	1.192	1.064	.909	.724	.511	.269
	40	1.437	1.422	1.379	1.306	1.207	1.077	.921	.733	.517	.272
	45	1.455	1.440	1.397	1.323	1.222	1.091	.932	.742	.524	.276
	50	1.473	1.458	1.415	1.339	1.238	1.105	.944	.752	.531	.280
	55	1.491	1.476	1.432	1.355	1.253	1.118	.956	.761	.537	.283
7	55	1.509	1.494	1.450	1.372	1.268	1.132	.967	.770	.544	.287
	5	1.528	1.512	1.467	1.389	1.284	1.146	.979	.779	.551	.290
	10	1.546	1.530	1.484	1.405	1.299	1.159	.991	.788	.557	.293
	15	1.564	1.548	1.502	1.422	1.314	1.173	1.002	.798	.564	.297
	20	1.582	1.566	1.520	1.438	1.330	1.187	1.014	.807	.570	.301
	25	1.600	1.584	1.537	1.454	1.345	1.200	1.026	.816	.576	.304

TABLE OF ORDINATES—CONTINUED.

Ordinates five feet apart.—Chord one hundred feet.

Distances of the Ordinates from the end of the 100 feet Chord.											
Angle of Def'n.	Middle, 50 feet.	45 feet.	40 feet.	35 feet.	30 feet.	25 feet.	20 feet.	15 feet.	10 feet.	5 feet.	
7	25	1.618	1.602	1.555	1.471	1.360	1.214	1.037	.825	.583	.308
	30	1.637	1.620	1.572	1.488	1.375	1.228	1.048	.835	.590	.311
	35	1.655	1.638	1.589	1.504	1.390	1.241	1.060	.844	.596	.314
	40	1.673	1.656	1.607	1.521	1.405	1.255	1.071	.854	.603	.318
	45	1.692	1.674	1.624	1.537	1.421	1.269	1.083	.863	.610	.321
	50	1.710	1.692	1.641	1.553	1.436	1.282	1.095	.872	.616	.324
	55	1.728	1.710	1.659	1.570	1.451	1.296	1.106	.881	.623	.328
8		1.746	1.728	1.677	1.587	1.467	1.310	1.118	.891	.629	.332
	15	1.801	1.782	1.729	1.637	1.513	1.351	1.153	.918	.649	.342
	30	1.855	1.836	1.782	1.687	1.559	1.392	1.188	.946	.669	.353
	45	1.910	1.890	1.834	1.737	1.605	1.433	1.223	.974	.689	.363
9		1.965	1.944	1.886	1.787	1.651	1.474	1.258	1.002	.708	.373
	15	2.019	1.998	1.939	1.837	1.696	1.515	1.293	1.030	.728	.384
	30	2.074	2.052	1.991	1.887	1.742	1.556	1.328	1.057	.748	.394
	45	2.128	2.106	2.044	1.937	1.788	1.597	1.363	1.085	.767	.405
10		2.183	2.161	2.096	1.987	1.834	1.637	1.398	1.114	.787	.415
	15	2.238	2.215	2.148	2.037	1.880	1.678	1.433	1.142	.807	.425
	30	2.292	2.269	2.201	2.087	1.926	1.719	1.468	1.170	.827	.436
	45	2.347	2.323	2.254	2.136	1.972	1.761	1.503	1.198	.846	.446
11		2.401	2.377	2.306	2.186	2.018	1.802	1.538	1.226	.866	.457
	15	2.456	2.432	2.359	2.236	2.064	1.843	1.574	1.254	.886	.467
	30	2.511	2.486	2.411	2.286	2.110	1.884	1.609	1.282	.906	.478
	45	2.566	2.540	2.464	2.336	2.156	1.926	1.644	1.310	.926	.488
12		2.620	2.594	2.516	2.386	2.203	1.967	1.680	1.339	.946	.499
	15	2.675	2.649	2.569	2.436	2.249	2.008	1.715	1.367	.966	.509
	30	2.730	2.703	2.621	2.485	2.295	2.049	1.750	1.395	.985	.520
	45	2.785	2.757	2.674	2.535	2.341	2.091	1.785	1.423	1.005	.530
13		2.839	2.811	2.726	2.585	2.387	2.132	1.820	1.451	1.025	.541
	15	2.894	2.865	2.779	2.635	2.433	2.173	1.855	1.479	1.045	.551
	30	2.949	2.920	2.832	2.685	2.479	2.214	1.891	1.507	1.065	.562
	45	3.000	2.974	2.884	2.735	2.525	2.256	1.926	1.535	1.085	.572
14		3.058	3.028	2.937	2.785	2.571	2.297	1.961	1.564	1.105	.583
	15	3.113	3.082	2.989	2.834	2.618	2.338	1.996	1.592	1.124	.593
	30	3.168	3.136	3.042	2.884	2.664	2.379	2.031	1.620	1.144	.604
	45	3.222	3.191	3.094	2.934	2.710	2.421	2.067	1.648	1.164	.614
15		3.277	3.245	3.147	2.984	2.756	2.462	2.102	1.676	1.184	.625
	15	3.332	3.299	3.200	3.034	2.802	2.503	2.137	1.704	1.204	.635
	30	3.387	3.354	3.252	3.084	2.848	2.544	2.172	1.732	1.224	.646
	45	3.442	3.408	3.305	3.134	2.895	2.586	2.208	1.760	1.244	.656
16		3.496	3.462	3.358	3.184	2.941	2.627	2.243	1.789	1.264	.667

TABLE OF ORDINATES—CONTINUED.

Ordinates five feet apart.—Chord one hundred feet.

Distances of the Ordinates from the end of the 100 feet Chord.										
Angle of Def'n.	Middle, 50 feet.	45 feet.	40 feet.	35 feet.	30 feet.	25 feet.	20 feet.	15 feet.	10 feet.	5 feet.
16 30	3.606	3.571	3.463	3.284	3.033	2.710	2.314	1.845	1.304	.688
17	3.716	3.680	3.569	3.384	3.125	2.792	2.384	1.902	1.344	.709
18 30	3.826	3.788	3.674	3.484	3.218	2.875	2.455	1.958	1.384	.730
19	3.935	3.897	3.779	3.584	3.310	2.958	2.525	2.014	1.424	.751
20 30	4.045	4.006	3.885	3.684	3.403	3.040	2.596	2.071	1.464	.772
21	4.155	4.115	3.990	3.784	3.495	3.123	2.666	2.127	1.504	.793
22 30	4.265	4.223	4.096	3.884	3.588	3.205	2.737	2.184	1.544	.814
23	4.375	4.332	4.201	3.984	3.680	3.288	2.808	2.240	1.583	.836
24	4.595	4.549	4.412	4.184	3.864	3.454	2.950	2.353	1.663	.879
25	4.815	4.768	4.624	4.386	4.050	3.620	3.093	2.467	1.744	.922
26	5.035	4.986	4.836	4.587	4.237	3.786	3.236	2.581	1.824	.965
27 30	5.255	5.204	5.048	4.789	4.423	3.952	3.379	2.695	1.905	1.008
28	5.476	5.422	5.260	4.989	4.609	4.119	3.522	2.809	1.986	1.051
29	5.697	5.642	5.473	5.192	4.798	4.286	3.665	2.924	2.068	1.094
30	5.918	5.860	5.685	5.393	4.984	4.454	3.808	3.039	2.150	1.137
31 30	6.139	6.079	5.898	5.595	5.171	4.622	3.952	3.154	2.232	1.181
32	6.361	6.298	6.110	5.796	5.357	4.790	4.095	3.269	2.314	1.224
33	6.582	6.517	6.323	5.999	5.544	4.958	4.239	3.385	2.396	1.268
34	6.804	6.737	6.537	6.202	5.733	5.127	4.384	3.502	2.481	1.312
35 30	7.027	6.957	6.751	6.406	5.922	5.297	4.530	3.619	2.565	1.356
36	7.249	7.178	6.965	6.609	6.111	5.467	4.676	3.737	2.649	1.401
37	7.472	7.398	7.179	6.813	6.300	5.637	4.822	3.854	2.733	1.445
38 30	7.694	7.619	7.393	7.017	6.489	5.807	4.968	3.972	2.817	1.490
39	7.918	7.841	7.609	7.222	6.679	5.978	5.115	4.090	2.901	1.535
40 30	8.143	8.063	7.825	7.427	6.870	6.149	5.262	4.209	2.985	1.581
41	8.367	8.286	8.041	7.633	7.060	6.320	5.410	4.327	3.069	1.626
42 30	8.592	8.508	8.257	7.838	7.251	6.491	5.557	4.446	3.153	1.672
43	8.816	8.731	8.474	8.044	7.442	6.663	5.705	4.565	3.238	1.718

ARTICLE XXI.

ON LONG CHORDS.

It is sometimes convenient, in preliminary locations, to lay off curves by chords longer than 100 feet. For instance, in fig. 19, instead of running from a by chords ab , bc , cd , &c. of but 100 feet, points d , f , g , &c. may be obtained with less trouble by using three times the tangential or deflection angles of the table, (as the case may be,) and employing chords ad , df , fg , &c. *nearly* three times as

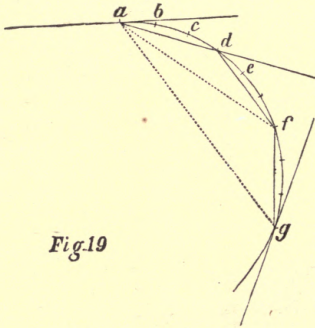


Fig. 19

long as the chords ab , bc , &c.; or if ad , df , fg be either 2 or 4 stations apart, then 2 or 4 times the tangential and deflection angles would be used; and chords nearly 2 or 4 times 100 feet in length.

The following table contains the precise length of chord required to subtend respectively 1, 2, 3, or 4 stations. It is seldom desirable to exceed the latter limit.

TABLE OF LONG CHORDS.

Radius in feet.	Angle of Deflection.	Length of Chord in feet required to subtend			
		1 Station.	2 Stations.	3 Stations.	4 Stations.
5730.0	1°	100	200.0	300.0	400.0
4584.0	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	200.0	300.0	399.9
3820.0	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	200.0	300.0	399.9
3274.0	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	200.0	300.0	399.8
2865.0	2°	100	200.0	299.9	399.7
2547.0	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	200.0	299.9	399.6
2292.0	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	200.0	299.8	399.5
2084.0	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	200.0	299.8	399.4
1910.0	3°	100	200.0	299.7	399.3
1763.0	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	200.0	299.7	399.2
1637.0	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	200.0	299.6	399.1
1528.0	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	200.0	299.6	399.0
1433.0	4°	100	199.9	299.6	398.9
1348.0	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	199.9	299.5	398.7
1274.0	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	199.9	299.4	398.5
1207.0	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	199.9	299.3	398.3
1146.0	5°	100	199.9	299.2	398.0
1092.0	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	199.8	299.1	397.8
1042.0	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	199.8	299.0	397.6
996.8	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	199.7	298.9	397.5
955.4	6°	100	199.7	298.8	397.3
917.0	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	199.7	298.7	397.0
882.0	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	199.7	298.6	396.7
849.3	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	199.6	298.5	396.5
819.0	7°	100	199.6	298.4	396.2
790.8	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	199.6	298.3	396.0
764.5	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	199.6	298.2	395.7
739.9	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	199.6	298.1	395.4
716.8	8°	100	199.6	298.0	395.1
695.1	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	199.5	297.9	394.8
674.6	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	199.5	297.8	394.5
655.5	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	199.4	297.7	394.3
637.3	9°	100	199.4	297.5	394.1
620.2	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	199.4	297.4	393.7
603.8	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	199.3	297.3	393.2
588.4	$\frac{1}{4} \frac{1}{2} \frac{3}{4}$	100	199.2	297.2	392.8
573.7	10°	100	199.2	297.0	392.4

For radii less than 573.7 feet, it is never required to use longer chords than 100 feet.

When this method of laying out curves by long chords is used, the instrument should be moved to each successive point after it is determined, in order to fix the next one, instead of attempting to obtain more than one point from one position of the instrument; because when the chords are longer than one chain, they cannot be measured in the right direction by eye, but must be guided by the instrument.

It must be especially borne in mind that, in any given curve, only the tangential and deflection *angles* increase in the same proportion as the number of 100 feet stations subtended by the long chord. Therefore, *these* long chords cannot be used for laying out curves *by eye*, as their tangential and deflection *distances* are not known.

When it is required to use long chords for turning a curve *by eye*, they must be composed of a number of *whole chains*, being made say 200, 300, or 400, &c. feet in length. The tangential and deflection *distances* of curves of more than 500 feet radius may then be assumed, in practice, to increase as the *squares* of the number of chains in the length of the long chord. For instance, to lay off a 5° curve by chords of 200, 300, or 400 feet in length, the tangential and deflection distances of the table must be multiplied by 4, 9, or 16, as the case may be. In this case the tangential and deflection *angles* are unknown.

This is not mathematically correct, but will answer in practice for the curves on a canal or common road, where great nicety is not needed.

The only proper instrument for running lines of survey is the *transit*, furnished with a compass and with a revolving telescope. The deflections being measured in *angles*, serve as a check to the numerous sources of error to which the compass is liable, arising from local attraction, electrical action in the glass cover, diurnal variation, &c. &c. Besides, when the compass alone is used, it is necessary to test every course or bearing from each end of each station; and this involves loss of time.

The following is a good form of field-book for the transit and compass combined.

Station.	Distance.	Total Distance.	Course.	Deflection in Degrees.		The right hand page is left blank for Remarks, and Sketches of Topogra- phy.
				Left.	Right.	

In every locating party there should be one person whose duty is to obtain, and record the transverse slopes of the ground at each station. His observations will usually extend to from fifty feet, to one hundred yards on each side of the centre stakes, depending on a variety of circumstances of locality which cannot be alluded to here. In preliminary locations these slopes need not be taken with very great nicety, as they will be used chiefly for ascertaining, approximately, the amount of excavation and embankment, by the rapid process described in my little volume on that subject, and which dispenses with nearly all the labor of the usual calculations.

After the final location is made, the slopes should be taken again, with great care, to the nearest quarter of a degree; but need not extend beyond the width actually occupied by the road. Their use in this second operation will be for determining the cubic contents with more precision than before, for final estimates; and also for obtaining the positions of the *side-stakes*.

Should the duty of *recording* these slopes devolve upon the compassman, (which it should not,) it will be necessary to add another column to his field-book, after that containing the deflections. In this column he will insert the slopes, thus, (Fig. 20.) the dot representing the center stake. The degrees of slope are written above the lines, and the distance in feet to which they extend, below.

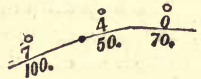


Fig. 20.

The slopes are taken by laying a long rod on the ground, at *right angles to the line of survey*, as nearly as may be judged by eye, and measuring the angles by means of a small *slope instrument* placed upon the rod. These are made by most of our instrument-makers.

ARTICLE XXII.

TO ADJUST A TRANSIT INSTRUMENT.

Having placed the transit firmly at *a*, fig. 21, and levelled it, clamp all fast, and direct the cross-hairs, by means of the tangent screw, to some convenient object, *b*. Then, revolving the telescope *vertically*, but without moving it in the least *horizontally*, let the cross-hairs fix upon a second

object in the opposite direction, as *c*; or, if there be no such object, place one, as for instance a chain-pin, at any convenient distance.



Fig. 21

Then unclamp the *lower* clamp, and revolve *horizontally* the entire upper part of the instrument above the parallel plates. Clamp it again, and fix the cross-hairs upon *b*; then again revolve the *telescope* vertically. If the sight now strikes *c*, as before, it is in adjustment; but if not, place another object, *d*, where it does strike; and with the adjusting pin alter the vertical cross-hair so as to strike halfway between *d* and *c*. The instrument will then be in adjustment.

Two or more trials will generally be needed before the adjustment is perfect.

With care, and on a firm floor, the operation may be performed in a long room, or by placing the instrument in a doorway communicating with two rooms of moderate size. Fine pins, or needles should then be used as the objects to be sighted at. It is better, however, to adjust out of doors, with more distant objects. It is also a good precaution to hang up a long plumb-line, or select some vertical object, and see whether the vertical hair coincides with it, as the telescope is raised or lowered. If from any accident, or carelessness in its construction, it does not, the defect must be remedied by an instrument-maker.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

0 Deg.

0 Deg.

0 Deg.

°	Sine.	l. a. g.	Cotang.	Cosine.	' /	Sine.	Tang.	Cotang.	Cosine.	' /	Sine.	Tang.	Cotang.	Cosine.	'
0	.0000000	.000000	Infinit.	1.0000000	60	.21	.0061086	163.7001	.9999813	39	.41	.011927	83.84350	.9999289	19
1	.0002909	.000291	3437.746	1.0000000	59	.22	.0063995	156.2590	.9999795	38	.42	.012217	81.84704	.9999254	18
2	.0005818	.000582	1718.873	.9999998	58	.23	.0066904	149.4650	.9999776	37	.43	.0125079	79.94343	.9999218	17
3	.0008727	.000872	1145.915	.9999996	57	.24	.0069813	143.2371	.9999756	36	.44	.0127987	78.12634	.9999181	16
4	.0011636	.001163	859.4363	.9999993	56	.25	.0072721	137.5075	.9999736	35	.45	.0130896	76.39000	.9999143	15
5	.0014544	.001454	687.5488	.9999989	55	.26	.0075630	132.2185	.9999714	34	.46	.0133805	74.72910	.9999105	14
6	.0017453	.001745	572.9572	.9999985	54	.27	.0078539	127.3213	.9999692	33	.47	.0136713	73.13899	.9999065	13
7	.0020362	.002036	491.1060	.9999979	53	.28	.0081448	122.7739	.9999668	32	.48	.0139622	71.61507	.9999025	12
8	.0023271	.002327	429.7175	.9999973	52	.29	.0084357	118.5401	.9999644	31	.49	.0142530	70.15334	.9998984	11
9	.0026180	.002618	381.9709	.9999966	51	.30	.0087265	114.5886	.9999619	30	.50	.0145439	68.75008	.9998942	10
10	.0029089	.002908	343.7737	.9999958	50	.31	.0090174	110.8920	.9999593	29	.51	.0148348	67.40185	.9998900	9
11	.0031998	.003199	312.5213	.9999949	49	.32	.0093083	107.4264	.9999567	28	.52	.0151256	66.10547	.9998856	8
12	.0034907	.003490	286.4777	.9999939	48	.33	.0095992	104.1709	.9999539	27	.53	.0154165	64.85800	.9998812	7
13	.0037815	.003781	264.4408	.9999928	47	.34	.0098900	101.1069	.9999511	26	.54	.0157073	63.65674	.9998766	6
14	.0040724	.004072	245.5519	.9999917	46	.35	.0101809	98.21794	.9999482	25	.55	.0159982	62.49915	.9998720	5
15	.0043633	.004363	229.1816	.9999905	45	.36	.0104718	95.48947	.9999452	24	.56	.0162890	61.38290	.9998675	4
16	.0046542	.004654	214.8576	.9999892	44	.37	.0107627	92.90848	.9999421	23	.57	.0165799	60.30582	.9998625	3
17	.0049451	.004945	202.2187	.9999878	43	.38	.0110535	90.46333	.9999389	22	.58	.0168707	59.26587	.9998577	2
18	.0052360	.005236	190.9841	.9999863	42	.39	.0113444	88.14357	.9999357	21	.59	.0171616	58.26117	.9998527	1
19	.0055268	.005526	180.9322	.9999847	41	.40	.0116353	85.93979	.9999323	20	.60	.0174524	57.28996	.9998477	0
20	.0058177	.005817	171.8854	.9999831	40										

Deg. 89

Deg. 89.

Deg. 89

NATURAL SINES AND TANGENTS TO A RADIUS 1

1 Deg.

1 Deg.

1 Deg.

'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'		
0	-0.174524	-0.17455	57-28996	.9998477	60	.21	-0.235598	-0.23566	42-43346	.9997224	39	41	-0.293755	-0.29388	34-02730	.9995684	19
1	-0.177432	-0.17746	56-35059	.9998426	59	.22	-0.238506	-0.23857	41-91579	.9997156	38	42	-0.296662	-0.29679	33-69350	.9995599	18
2	-0.180341	-0.18037	55-44151	.9998374	58	.23	-0.241414	-0.24148	41-41058	.9997086	37	43	-0.299570	-0.29970	33-36619	.9995512	17
3	-0.183249	-0.18328	54-56130	.9998321	57	.24	-0.244322	-0.24439	40-91741	.9997015	36	44	-0.302478	-0.30261	33-04517	.9995424	16
4	-0.186158	-0.18619	53-70858	.9998267	56	.25	-0.247230	-0.24730	40-43583	.9996943	35	45	-0.305385	-0.30552	32-73026	.9995336	15
5	-0.189066	-0.18910	52-88211	.9998213	55	.26	-0.250138	-0.25021	39-96546	.9996871	34	46	-0.308293	-0.30843	32-42129	.9995247	14
6	-0.191974	-0.19201	52-08067	.9998157	54	.27	-0.253046	-0.25312	39-50589	.9996798	33	47	-0.311200	-0.31135	32-11809	.9995157	13
7	-0.194883	-0.19492	51-30315	.9998101	53	.28	-0.255954	-0.25603	39-05677	.9996724	32	48	-0.314108	-0.31426	31-82051	.9995066	12
8	-0.197791	-0.19783	50-54850	.9998044	52	.29	-0.258862	-0.25894	38-61773	.9996649	31	49	-0.317015	-0.31717	31-52839	.9994974	11
9	-0.200699	-0.20074	49-81572	.9997986	51	.30	-0.261769	-0.26185	38-18845	.9996573	30	50	-0.319922	-0.32008	31-24157	.9994881	10
10	-0.203608	-0.20365	49-10388	.9997927	50	.31	-0.264677	-0.26477	37-76861	.9996497	29	51	-0.322830	-0.32299	30-95992	.9994788	9
11	-0.206516	-0.20656	48-41208	.9997867	49	.32	-0.267585	-0.26768	37-35789	.9996419	28	52	-0.325737	-0.32591	30-68330	.9994693	8
12	-0.209424	-0.20947	47-73950	.9997807	48	.33	-0.270493	-0.27059	36-95600	.9996341	27	53	-0.328644	-0.32882	30-41158	.9994598	7
13	-0.212332	-0.21238	47-08534	.9997745	47	.34	-0.273401	-0.27350	36-56265	.9996262	26	54	-0.331552	-0.33173	30-14461	.9994502	6
14	-0.215241	-0.21529	46-44886	.9997683	46	.35	-0.276309	-0.27641	36-17759	.9996182	25	55	-0.334459	-0.33464	29-88229	.9994405	5
15	-0.218149	-0.21820	45-82935	.9997620	45	.36	-0.279216	-0.27932	35-80055	.9996101	24	56	-0.337366	-0.33755	29-62449	.9994308	4
16	-0.221057	-0.22111	45-22614	.9997556	44	.37	-0.282124	-0.28223	35-43128	.9996020	23	57	-0.340274	-0.34047	29-37110	.9994209	3
17	-0.223965	-0.22402	44-63859	.9997492	43	.38	-0.285032	-0.28514	35-06954	.9995937	22	58	-0.343181	-0.34338	29-12200	.9994110	2
18	-0.226873	-0.22693	44-06611	.9997426	42	.39	-0.287940	-0.28805	34-71511	.9995854	21	59	-0.346088	-0.34629	28-87708	.9994009	1
19	-0.229781	-0.22984	43-50812	.9997360	41	.40	-0.290847	-0.29097	34-36777	.9995770	20	60	-0.348995	-0.34920	28-63625	.9993908	0
20	-0.232690	-0.23275	42-96407	.9997292	40												
'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'		

Deg 88.

Deg. 88.

Deg. 88.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

2 Deg.

2 Deg.

2 Deg.

/	Sine.	Tang.	Cotang.	Cosine.	/	Sine.	Tang.	Cotang.	Cosine.	/	Sine.	Tang.	Cotang.	Cosine.	/
0	.0348995	-.034920	28.63625	.9993908	60	.21	-.0410037	24.36750	.9991590	39	.41	-.0468159	21.33685	.9989035	19
1	.0351902	-.035212	28.39939	.9993806	59	.22	-.0412944	24.19571	.9991470	38	.42	-.0471065	21.20494	.9988899	18
2	.0354809	-.035503	28.16642	.9993704	58	.23	-.0415850	24.02632	.9991350	37	.43	-.0473970	21.07466	.9988761	17
3	.0357716	-.035794	27.93723	.9993600	57	.24	-.0418757	23.85927	.9991228	36	.44	-.0476876	20.94596	.9988623	16
4	.0360623	-.036085	27.71174	.9993495	56	.25	-.0421663	23.69453	.9991106	35	.45	-.0479781	20.81882	.9988484	15
5	.0363530	-.036377	27.48985	.9993390	55	.26	-.0424569	23.53205	.9990983	34	.46	-.0482687	20.69322	.9988344	14
6	.0366437	-.036668	27.27148	.9993284	54	.27	-.0427475	23.37177	.9990859	33	.47	-.0485592	20.56911	.9988203	13
7	.0369344	-.036959	27.05655	.9993177	53	.28	-.0430382	23.21366	.9990734	32	.48	-.0488498	20.44648	.9988061	12
8	.0372251	-.037250	26.84498	.9993069	52	.29	-.0433288	23.05767	.9990609	31	.49	-.0491403	20.32530	.9987919	11
9	.0375158	-.037542	26.63669	.9992960	51	.30	-.0436194	22.90376	.9990482	30	.50	-.0494308	20.20555	.9987775	10
10	.0378065	-.037833	26.43160	.9992851	50	.31	-.0439100	22.75189	.9990355	29	.51	-.0497214	20.08719	.9987631	9
11	.0380971	-.038124	26.22963	.9992740	49	.32	-.0442006	22.60201	.9990227	28	.52	-.0500119	19.97021	.9987486	8
12	.0383878	-.038416	26.03073	.9992629	48	.33	-.0444912	22.45409	.9990098	27	.53	-.0503024	19.85459	.9987340	7
13	.0386785	-.038707	25.83482	.9992517	47	.34	-.0447818	22.30809	.9989968	26	.54	-.0505929	19.74029	.9987194	6
14	.0389692	-.038998	25.64183	.9992404	46	.35	-.0450724	22.16398	.9989837	25	.55	-.0508835	19.62729	.9987046	5
15	.0392598	-.039290	25.45170	.9992290	45	.36	-.0453630	22.02171	.9989706	24	.56	-.0511740	19.51558	.9986898	4
16	.0395505	-.039581	25.26436	.9992176	44	.37	-.0456536	21.88125	.9989573	23	.57	-.0514645	19.40513	.9986748	3
17	.0398411	-.039872	25.07975	.9992060	43	.38	-.0459442	21.74256	.9989440	22	.58	-.0517550	19.29592	.9986598	2
18	.0401318	-.040164	24.89782	.9991944	42	.39	-.0462347	21.60563	.9989306	21	.59	-.0520455	19.18793	.9986447	1
19	.0404224	-.040455	24.71851	.9991827	41	.40	-.0465253	21.47040	.9989171	20	.60	-.0523360	19.08113	.9986295	0
20	.0407131	-.040746	24.54175	.9991709	40										

Deg. 87.

Deg. 87.

Deg. 87.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

3 Deg.

3 Deg.

°	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'
0	0.52336	0.52407	19.08113	9986295	60	21	0.584352	0.58535	17.08372	9982912	39	41	0.642420	0.64375	15.53398
1	0.526264	0.52699	18.97552	9986143	59	22	0.587256	0.58827	16.99895	9982742	38	42	0.645323	0.64667	15.46381
2	0.529169	0.52991	18.87106	9985989	58	23	0.590160	0.59119	16.91502	9982570	37	43	0.648226	0.64959	15.39427
3	0.532074	0.53282	18.76775	9985835	57	24	0.593064	0.59410	16.83191	9982398	36	44	0.651129	0.65251	15.32535
4	0.534979	0.53574	18.66556	9985680	56	25	0.595967	0.59702	16.74961	9982225	35	45	0.654031	0.65543	15.25705
5	0.537883	0.53866	18.56447	9985524	55	26	0.598871	0.59994	16.66811	9982052	34	46	0.656934	0.65835	15.18934
6	0.540788	0.54158	18.46447	9985367	54	27	0.601775	0.60286	16.58739	9981877	33	47	0.659836	0.66127	15.12224
7	0.543693	0.54449	18.36553	9985209	53	28	0.604678	0.60578	16.50745	9981701	32	48	0.662739	0.66419	15.05572
8	0.546597	0.54741	18.26765	9985050	52	29	0.607582	0.60870	16.42827	9981525	31	49	0.665641	0.66712	14.98978
9	0.549502	0.55033	18.17080	9984891	51	30	0.610485	0.61162	16.34985	9981348	30	50	0.668544	0.67004	14.92441
10	0.552406	0.55325	18.07497	9984731	50	31	0.613389	0.61454	16.27217	9981170	29	51	0.671446	0.67296	14.85961
11	0.555311	0.55616	17.98015	9984570	49	32	0.616292	0.61746	16.19522	9980991	28	52	0.674349	0.67588	14.79537
12	0.558215	0.55908	17.88631	9984408	48	33	0.619196	0.62038	16.11899	9980811	27	53	0.677251	0.67880	14.73167
13	0.561119	0.56200	17.79344	9984245	47	34	0.622099	0.62330	16.04348	9980631	26	54	0.680153	0.68173	14.66852
14	0.564024	0.56492	17.70152	9984081	46	35	0.625002	0.62622	15.96866	9980450	25	55	0.683055	0.68465	14.60591
15	0.566928	0.56784	17.61055	9983917	45	36	0.627905	0.62914	15.89454	9980267	24	56	0.685957	0.68757	14.54383
16	0.569832	0.57075	17.52051	9983751	44	37	0.630808	0.63206	15.82110	9980084	23	57	0.688859	0.69049	14.48227
17	0.572736	0.57367	17.43138	9983585	43	38	0.633711	0.63498	15.74833	9979900	22	58	0.691761	0.69342	14.42123
18	0.575640	0.57659	17.34315	9983418	42	39	0.636614	0.63790	15.67623	9979716	21	59	0.694663	0.69634	14.36069
19	0.578544	0.57951	17.25580	9983250	41	40	0.639517	0.64082	15.60478	9979530	20	60	0.697565	0.69926	14.30066
20	0.581448	0.58243	17.16933	9983082	40										

Deg. 86.

Deg. 86.

Deg. 86.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

4 Deg.

4 Deg.

4 Deg.

'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'
0	.0697565	.069926	14.30066	.9975641	60	.210758489	.076068	13.14612	.9971193	39	.4108116486	.081922	12.20671	.9966612	19
1	.0700467	.070219	14.24113	.9975437	59	.220761390	.076360	13.09575	.9970972	38	.420819385	.082215	12.16323	.9966374	18
2	.0703368	.070511	14.18209	.9975233	58	.230764290	.076653	13.04576	.9970750	37	.430822284	.082507	12.12006	.9966135	17
3	.0706270	.070803	14.12353	.9975028	57	.240767190	.076945	12.99616	.9970528	36	.440825183	.082800	12.07719	.9965895	16
4	.0709171	.071096	14.06545	.9974822	56	.250770091	.077238	12.94692	.9970304	35	.450828082	.083093	12.03462	.9965655	15
5	.0712073	.071388	14.00785	.9974615	55	.260772991	.077531	12.89805	.9970080	34	.460830981	.083386	11.99234	.9965414	14
6	.0714974	.071680	13.95071	.9974408	54	.270775891	.077823	12.84955	.9969854	33	.470833880	.083679	11.95037	.9965172	13
7	.0717876	.071973	13.89404	.9974199	53	.280778791	.078116	12.80141	.9969628	32	.480836778	.083972	11.90868	.9964929	12
8	.0720777	.072265	13.83782	.9973990	52	.290781691	.078409	12.75363	.9969401	31	.490839677	.084265	11.86728	.9964685	11
9	.0723678	.072558	13.78206	.9973780	51	.300784591	.078701	12.70626	.9969173	30	.500842576	.084558	11.82616	.9964440	10
10	.0726580	.072850	13.72673	.9973569	50	.310787491	.078994	12.65912	.9968945	29	.510845474	.084851	11.78533	.9964195	9
11	.0729481	.073143	13.67185	.9973357	49	.320790391	.079287	12.61239	.9968715	28	.520848373	.085144	11.74477	.9963948	8
12	.0732382	.073435	13.61740	.9973145	48	.330793290	.079579	12.56599	.9968485	27	.530851271	.085437	11.70450	.9963701	7
13	.0735283	.073727	13.56339	.9972931	47	.340796190	.079872	12.51994	.9968254	26	.540854169	.085730	11.66449	.9963453	6
14	.0738184	.074020	13.50979	.9972717	46	.350799090	.080165	12.47422	.9968022	25	.550857067	.086023	11.62476	.9963204	5
15	.0741085	.074312	13.45662	.9972502	45	.360801989	.080458	12.42883	.9967789	24	.560859966	.086316	11.58529	.9962954	4
16	.0743986	.074605	13.40386	.9972286	44	.370804889	.080750	12.38376	.9967555	23	.570862864	.086609	11.54609	.9962704	3
17	.0746887	.074897	13.35151	.9972069	43	.380807788	.081043	12.33902	.9967321	22	.580865762	.086902	11.50715	.9962452	2
18	.0749787	.075190	13.29957	.9971851	42	.390810687	.081336	12.29460	.9967085	21	.590868660	.087195	11.46847	.9962200	1
19	.0752688	.075482	13.24803	.9971633	41	.400813587	.081629	12.25050	.9966849	20	.600871557	.087488	11.43005	.9961947	0
20	.0755589	.075775	13.19688	.9971413	40										
'	Cosine.	Cotan.	Tang.	Sine.	'	Cosine.	Cotan.	Tang.	Sine.	'	Cosine.	Cotan.	Tang.	Sine.	'

Deg. 85.

Deg. 85.

Deg. 85.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

5 Deg.

5 Deg.

5 Deg.

'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'
0	·0871557	·087488	11·43005	·9961947	60	·21	·0932395	·093647	10·67834	·9956437	39	·41	·0990303	·099519	10·04828
1	·0874455	·087781	11·39188	·9961693	59	·22	·0935291	·093940	10·64499	·9956165	38	·42	·0993197	·099813	10·01871
2	·0877353	·088074	11·35297	·9961438	58	·23	·0938187	·094234	10·61184	·9955892	37	·43	·0996092	·100107	9·989305
3	·0880251	·088368	11·31630	·9961183	57	·24	·0941083	·094527	10·57889	·9955620	36	·44	·0998986	·100400	9·960072
4	·0883148	·088661	11·27888	·9960926	56	·25	·0943979	·094821	10·54615	·9955345	35	·45	·1001881	·100694	9·931008
5	·0886046	·088954	11·24171	·9960669	55	·26	·0946875	·095114	10·51360	·9955070	34	·46	·1004775	·100988	9·902112
6	·0888943	·089247	11·20478	·9960411	54	·27	·0949771	·095408	10·48126	·9954794	33	·47	·1007669	·101282	9·873382
7	·0891840	·089540	11·16808	·9960152	53	·28	·0952666	·095701	10·44911	·9954517	32	·48	·1010563	·101576	9·844816
8	·0894738	·089834	11·13163	·9959892	52	·29	·0955562	·095995	10·41715	·9954240	31	·49	·1013457	·101870	9·816414
9	·0897635	·090127	11·09541	·9959631	51	·30	·0958458	·096289	10·38539	·9953962	30	·50	·1016351	·102164	9·788173
10	·0900532	·090420	11·05943	·9959370	50	·31	·0961353	·096582	10·35382	·9953683	29	·51	·1019245	·102458	9·760092
11	·0903429	·090713	11·02367	·9959107	49	·32	·0964248	·096876	10·32244	·9953403	28	·52	·1022138	·102752	9·732171
12	·0906326	·091007	10·98815	·9958844	48	·33	·0967144	·097169	10·29125	·9953122	27	·53	·1025032	·103046	9·704407
13	·0909223	·091300	10·95285	·9958580	47	·34	·0970039	·097463	10·26024	·9952840	26	·54	·1027925	·103339	9·676800
14	·0912119	·091593	10·91777	·9958315	46	·35	·0972934	·097757	10·22942	·9952557	25	·55	·1030819	·103634	9·649347
15	·0915016	·091887	10·88292	·9958049	45	·36	·0975829	·098050	10·19878	·9952274	24	·56	·1033712	·103928	9·622048
16	·0917913	·092180	10·84828	·9957783	44	·37	·0978724	·098344	10·16833	·9951990	23	·57	·1036605	·104222	9·594902
17	·0920809	·092473	10·81387	·9957515	43	·38	·0981619	·098638	10·13805	·9951705	22	·58	·1039499	·104516	9·567906
18	·0923706	·092767	10·77967	·9957247	42	·39	·0984514	·098932	10·10795	·9951419	21	·59	·1042392	·104810	9·541061
19	·0926602	·093060	10·74568	·9956978	41	·40	·0987408	·099225	10·07803	·9951132	20	·60	·1045285	·105104	9·514364
20	·0929499	·093354	10·71191	·9956708	40										

Deg. 84.

Deg. 84.

Deg. 84.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

6 Deg.

6 Deg.

6 Deg.

/	Sine.	Tang.	Cotang.	Cosine.	/	Sine.	Tang.	Cotang.	Cosine.	/	Sine.	Tang.	Cotang.	Cosine.	/			
0	.1045285	.105104	9.514364	.9945219	60	21	.1106017	.111284	8.985984	.9938648	39	41	.1163818	.117178	8.534017	.9932045	19	
1	.1048178	.105398	9.487814	.9944914	59	22	.1108908	.111578	8.992266	.9938326	38	42	.1166707	.117473	8.512594	.9931706	18	
2	.1051070	.105692	9.461411	.9944609	58	23	.1111799	.111873	8.938672	.9938003	37	43	.1169596	.117767	8.491277	.9931367	17	
3	.1053963	.105986	9.435153	.9944303	57	24	.1114689	.112168	8.915200	.9937679	36	44	.1172485	.118062	8.470065	.9931026	16	
4	.1056856	.106280	9.409038	.9943996	56	25	.1117580	.112462	8.891850	.9937355	35	45	.1175374	.118357	8.448957	.9930685	15	
5	.1059748	.106575	9.383066	.9943688	55	26	.1120471	.112757	8.868620	.9937029	34	46	.1178263	.118652	8.427953	.9930342	14	
6	.1062641	.106869	9.357235	.9943379	54	27	.1123361	.113051	8.845510	.9936703	33	47	.1181151	.118947	8.407051	.9929999	13	
7	.1065533	.107163	9.331545	.9943070	53	28	.1126252	.113346	8.822518	.9936375	32	48	.1184040	.119242	8.386251	.9929655	12	
8	.1068425	.107457	9.305993	.9942760	52	29	.1129142	.113641	8.799644	.9936047	31	49	.1186928	.119537	8.365553	.9929310	11	
9	.1071318	.107751	9.280580	.9942448	51	30	.1132032	.113935	8.776887	.9935719	30	50	.1189816	.119832	8.344955	.9928965	10	
10	.1074210	.108046	9.255303	.9942136	50	31	.1134922	.114230	8.754246	.9935389	29	51	.1192704	.120127	8.324457	.9928618	9	
11	.1077102	.108340	9.230162	.9941823	49	32	.1137812	.114525	8.731719	.9935058	28	52	.1195593	.120423	8.304058	.9928271	8	
12	.1079994	.108634	9.205156	.9941510	48	33	.1140702	.114819	8.709307	.9934727	27	53	.1198481	.120718	8.283757	.9927922	7	
13	.1082885	.108929	9.180283	.9941195	47	34	.1143592	.115114	8.687008	.9934395	26	54	.1201368	.121013	8.263554	.9927573	6	
14	.1085777	.109223	9.155543	.9940880	46	35	.1146482	.115409	8.664822	.9934062	25	55	.1204256	.121308	8.243448	.9927224	5	
15	.1088669	.109517	9.130934	.9940563	45	36	.1149372	.115703	8.642747	.9933728	24	56	.1207144	.121603	8.223488	.9926873	4	
16	.1091560	.109812	9.106456	.9940246	44	37	.1152261	.115998	8.620783	.9933393	23	57	.1210031	.121898	8.203523	.9926521	3	
17	.1094452	.110106	9.082107	.9939928	43	38	.1155151	.116293	8.598929	.9933057	22	58	.1212919	.122194	8.183704	.9926169	2	
18	.1097343	.110401	9.057886	.9939610	42	39	.1158040	.116588	8.577183	.9932721	21	59	.1215806	.122489	8.163978	.9925816	1	
19	.1100234	.110695	9.033793	.9939290	41	40	.1160929	.116883	8.555546	.9932384	20	60	.1218693	.122784	8.144346	.9925462	0	
20	.1103126	.110989	9.009826	.9938969	40													
/	Cosine.	Cotan.	Tang.	Sine.	/	Cosine.	Cotan.	Tang.	Sine.	/	Cosine.	Cotan.	Tang.	Sine.	/			

Deg. 83.

Deg. 83.

Deg. 83.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

7 Deg.

7 Deg.

7 Deg.

'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'
0	.1218693	-1.22784	8.144346	.9925462	60	.21	.1279302	-1.28990	7.752536	.9917832	39	.41	.1336979	-1.34909	7.412397
1	.1221581	-1.23079	8.124807	.9925107	59	.22	.1282186	-1.29285	7.734802	.9917459	38	.42	.1339862	-1.35205	7.396159
2	.1224468	-1.23375	8.105359	.9924751	58	.23	.1285071	-1.29581	7.717148	.9917086	37	.43	.1342744	-1.35501	7.379990
3	.1227355	-1.23670	8.086004	.9924394	57	.24	.1287956	-1.29877	7.699573	.9916712	36	.44	.1345627	-1.35797	7.363891
4	.1230241	-1.23965	8.066739	.9924037	56	.25	.1290841	-1.30173	7.682076	.9916337	35	.45	.1348509	-1.36094	7.347861
5	.1233128	-1.24261	8.047564	.9923679	55	.26	.1293725	-1.30469	7.664658	.9915961	34	.46	.1351392	-1.36390	7.331898
6	.1236015	-1.24556	8.028479	.9923319	54	.27	.1296609	-1.30764	7.647317	.9915584	33	.47	.1354274	-1.36686	7.316004
7	.1238901	-1.24852	8.009483	.9922959	53	.28	.1299494	-1.31060	7.630053	.9915206	32	.48	.1357156	-1.36983	7.300178
8	.1241788	-1.25147	7.990575	.9922599	52	.29	.1302378	-1.31356	7.612865	.9914828	31	.49	.1360038	-1.37279	7.284418
9	.1244674	-1.25442	7.971755	.9922237	51	.30	.1305262	-1.31652	7.595754	.9914449	30	.50	.1362919	-1.37575	7.268725
10	.1247560	-1.25738	7.953022	.9921874	50	.31	.1308146	-1.31948	7.578717	.9914069	29	.51	.1365801	-1.37872	7.253098
11	.1250446	-1.26033	7.934375	.9921511	49	.32	.1311030	-1.32244	7.561756	.9913688	28	.52	.1368683	-1.38168	7.237537
12	.1253332	-1.26329	7.915815	.9921147	48	.33	.1313913	-1.32540	7.544869	.9913306	27	.53	.1371564	-1.38465	7.222042
13	.1256218	-1.26624	7.897339	.9920782	47	.34	.1316797	-1.32836	7.528057	.9912923	26	.54	.1374445	-1.38761	7.206611
14	.1259104	-1.26920	7.878948	.9920416	46	.35	.1319681	-1.33132	7.511317	.9912540	25	.55	.1377327	-1.39058	7.191245
15	.1261990	-1.27216	7.860642	.9920049	45	.36	.1322564	-1.33428	7.494651	.9912155	24	.56	.1380208	-1.39354	7.175943
16	.1264875	-1.27511	7.842419	.9919682	44	.37	.1325447	-1.33724	7.478057	.9911770	23	.57	.1383089	-1.39651	7.160705
17	.1267761	-1.27807	7.824279	.9919314	43	.38	.1328330	-1.34020	7.461535	.9911384	22	.58	.1385970	-1.39947	7.145530
18	.1270646	-1.28103	7.806221	.9918944	42	.39	.1331213	-1.34316	7.445085	.9910997	21	.59	.1388850	-1.40244	7.130419
19	.1273531	-1.28398	7.788245	.9918574	41	.40	.1334096	-1.34612	7.428706	.9910610	20	.60	.1391731	-1.40540	7.115369
20	.1276416	-1.28694	7.770350	.9918204	40										
'	Cosine.	Cotan.	Tang.	Sine.	'	Cosine.	Cotan.	Tang.	Sine.	'	Cosine.	Cotan.	Tang.	Sine.	'

Deg. 82.

Deg. 82.

Deg. 82.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

8 Deg.		8 Deg.		8 Deg.		8 Deg.		8 Deg.		8 Deg.		8 Deg.			
'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'
0	·1391731	·140540	7·115369	·9902681	60	·1452197	·146775	6·813122	·9893994	39	·1509733	·152723	6·547767	·9885378	19
1	·1394612	·140837	7·100382	·9902275	59	·1455075	·147072	6·799356	·9893572	38	·1512608	·153021	6·535029	·9884939	18
2	·1397492	·141134	7·085457	·9901869	58	·1457953	·147369	6·785644	·9893148	37	·1515484	·153319	6·522339	·9884498	17
3	·1400372	·141430	7·070593	·9901462	57	·1460830	·147667	6·771986	·9892723	36	·1518359	·153617	6·509698	·9884057	16
4	·1403252	·141727	7·055790	·9901055	56	·1463708	·147964	6·758382	·9892298	35	·1521234	·153914	6·497104	·9883615	15
5	·1406132	·142024	7·041048	·9900646	55	·1466585	·148261	6·744831	·9891872	34	·1524109	·154212	6·484558	·9883172	14
6	·1409012	·142321	7·026366	·9900237	54	·1469463	·148559	6·731334	·9891445	33	·1526984	·154510	6·472059	·9882728	13
7	·1411892	·142617	7·011744	·9899826	53	·1472340	·148856	6·717889	·9891017	32	·1529858	·154808	6·459607	·9882284	12
8	·1414772	·142914	6·997180	·9899415	52	·1475217	·149153	6·704496	·9890588	31	·1532733	·155106	6·447201	·9881838	11
9	·1417651	·143211	6·982678	·9899003	51	·1478094	·149451	6·691156	·9890159	30	·1535607	·155404	6·434842	·9881392	10
10	·1420531	·143508	6·968233	·9898590	50	·1480971	·149748	6·677867	·9889728	29	·1538482	·155701	6·422530	·9880945	9
11	·1423410	·143805	6·953847	·9898177	49	·1483848	·150045	6·664630	·9889297	28	·1541356	·155999	6·410263	·9880497	8
12	·1426289	·144102	6·939519	·9897762	48	·1486724	·150343	6·651444	·9888865	27	·1544230	·156297	6·398042	·9880048	7
13	·1429168	·144399	6·925248	·9897347	47	·1489601	·150640	6·638310	·9888432	26	·1547104	·156595	6·385866	·9879599	6
14	·1432047	·144696	6·911035	·9896931	46	·1492477	·150938	6·625225	·9887998	25	·1549978	·156893	6·373735	·9879148	5
15	·1434926	·144993	6·896879	·9896514	45	·1495353	·151235	6·612191	·9887564	24	·1552851	·157191	6·361650	·9878697	4
16	·1437805	·145290	6·882780	·9896096	44	·1498230	·151533	6·599208	·9887128	23	·1555725	·157490	6·349609	·9878245	3
17	·1440684	·145587	6·868737	·9895677	43	·1501106	·151830	6·586273	·9886692	22	·1558598	·157788	6·337612	·9877792	2
18	·1443562	·145884	6·854750	·9895258	42	·1503981	·152128	6·573389	·9886255	21	·1561472	·158086	6·325660	·9877338	1
19	·1446440	·146181	6·840819	·9894838	41	·1506857	·152426	6·560553	·9885817	20	·1564345	·158384	6·313751	·9876883	0
20	·1449319	·146478	6·826943	·9894416	40										
'	Cosine.	Cotan.	Tang.	Sine.	'	Cosine.	Cotan.	Tang.	Sine.	'	Cosine.	Cotan.	Tang.	Sine.	'

Deg. 81.

Deg. 81.

Deg. 81.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

9 Deg.

9 Deg.

9 Deg.

'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'		
0	.1561345	.158384	6.313751	.9876883	60	.21	.1624650	.164652	6.073397	.9867143	39	.41	.1682026	.170633	5.860505	.9857524	19
1	.1567218	.158682	6.301886	.9876428	59	.22	.1627520	.164951	6.062396	.9866670	38	.42	.1684894	.170933	5.850241	.9857035	18
2	.1570091	.158980	6.290065	.9875972	58	.23	.1630390	.165250	6.051434	.9866196	37	.43	.1687761	.171232	5.840011	.9856544	17
3	.1572963	.159279	6.278286	.9875514	57	.24	.1633260	.165548	6.040510	.9865722	36	.44	.1690628	.171532	5.829817	.9856053	16
4	.1575836	.159577	6.266551	.9875057	56	.25	.1636129	.165847	6.029624	.9865246	35	.45	.1693495	.171831	5.819657	.9855561	15
5	.1578708	.159875	6.254858	.9874598	55	.26	.1638999	.166146	6.018777	.9864770	34	.46	.1696362	.172130	5.809531	.9855068	14
6	.1581581	.160174	6.243208	.9874138	54	.27	.1641868	.166445	6.007967	.9864293	33	.47	.1699228	.172430	5.799440	.9854574	13
7	.1584453	.160472	6.231600	.9873678	53	.28	.1644738	.166744	5.997195	.9863815	32	.48	.1702095	.172730	5.789382	.9854079	12
8	.1587325	.160770	6.220034	.9873216	52	.29	.1647607	.167043	5.986461	.9863336	31	.49	.1704961	.173029	5.779358	.9853583	11
9	.1590197	.161069	6.208510	.9872754	51	.30	.1650476	.167342	5.975764	.9862856	30	.50	.1707828	.173329	5.769368	.9853087	10
10	.1593069	.161367	6.197027	.9872291	50	.31	.1653345	.167641	5.965104	.9862375	29	.51	.1710694	.173628	5.759412	.9852590	9
11	.1595940	.161666	6.185586	.9871827	49	.32	.1656214	.167940	5.954481	.9861894	28	.52	.1713560	.173928	5.749488	.9852092	8
12	.1598812	.161964	6.174186	.9871363	48	.33	.1659082	.168239	5.943895	.9861412	27	.53	.1716425	.174228	5.739598	.9851593	7
13	.1601683	.162263	6.162827	.9870897	47	.34	.1661951	.168539	5.933345	.9860929	26	.54	.1719291	.174527	5.729741	.9851093	6
14	.1604555	.162561	6.151508	.9870431	46	.35	.1664819	.168838	5.922832	.9860445	25	.55	.1722156	.174827	5.719917	.9850593	5
15	.1607426	.162860	6.140230	.9869964	45	.36	.1667687	.169137	5.912355	.9859960	24	.56	.1725022	.175127	5.710125	.9850091	4
16	.1610297	.163159	6.128992	.9869496	44	.37	.1670556	.169436	5.901913	.9859475	23	.57	.1727887	.175427	5.700366	.9849589	3
17	.1613167	.163457	6.117794	.9869027	43	.38	.1673423	.169735	5.891508	.9858988	22	.58	.1730752	.175727	5.690639	.9849086	2
18	.1616038	.163756	6.106636	.9868557	42	.39	.1676291	.170035	5.881138	.9858501	21	.59	.1733617	.176027	5.680944	.9848582	1
19	.1618909	.164055	6.095517	.9868087	41	.40	.1679159	.170334	5.870804	.9858013	20	.30	.1736482	.176327	5.671281	.9848078	0
20	.1621779	.164353	6.084438	.9867615	40												

Deg. 80.

Deg. 80.

Deg. 80.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

10 Deg.

10 Deg.

10 Deg.

'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	
0	.1736482	.176327	5.671281	.9848078	60	.21	.1796607	1.82632	5.475478	.9837286	39	.41	1.853808	5.300801	.9826668	19
1	.1739346	.176626	5.661650	.9847572	59	.22	.1799469	1.82933	5.466481	.9836763	38	.42	1.856666	5.292350	.9826128	18
2	.1742211	.176926	5.652051	.9847066	58	.23	.1802330	1.83233	5.457512	.9836239	37	.43	1.859524	5.283925	.9825587	17
3	.1745075	.177226	5.642483	.9846558	57	.24	.1805191	1.83534	5.448571	.9835715	36	.44	1.862382	5.275525	.9825046	16
4	.1747939	.177527	5.632947	.9846050	56	.25	.1808052	1.83835	5.439659	.9835189	35	.45	1.865240	5.267151	.9824504	15
5	.1750803	.177827	5.623442	.9845542	55	.26	.1810913	1.84135	5.430775	.9834663	34	.46	1.868098	5.258803	.9823961	14
6	.1753667	.178127	5.613968	.9845032	54	.27	.1813774	1.84436	5.421918	.9834136	33	.47	1.870956	5.250480	.9823417	13
7	.1756531	.178427	5.604524	.9844521	53	.28	.1816635	1.84737	5.413090	.9833608	32	.48	1.873813	5.242183	.9822873	12
8	.1759395	.178727	5.595112	.9844010	52	.29	.1819495	1.85038	5.404290	.9833079	31	.49	1.876670	5.233911	.9822327	11
9	.1762258	.179027	5.585730	.9843498	51	.30	.1822355	1.85339	5.395517	.9832549	30	.50	1.879528	5.225664	.9821781	10
10	.1765121	.179327	5.576378	.9842985	50	.31	.1825215	1.85639	5.386771	.9832019	29	.51	1.882385	5.217442	.9821234	9
11	.1767984	.179628	5.567057	.9842471	49	.32	.1828075	1.85940	5.378053	.9831487	28	.52	1.885241	5.209245	.9820686	8
12	.1770847	.179928	5.557766	.9841956	48	.33	.1830935	1.86241	5.369363	.9830955	27	.53	1.888098	5.201073	.9820137	7
13	.1773710	.180228	5.548505	.9841441	47	.34	.1833795	1.86542	5.360699	.9830422	26	.54	1.890954	5.192926	.9819587	6
14	.1776573	.180529	5.539274	.9840924	46	.35	.1836654	1.86843	5.352062	.9829888	25	.55	1.893811	5.184803	.9819037	5
15	.1779435	.180829	5.530072	.9840407	45	.36	.1839514	1.87144	5.343452	.9829353	24	.56	1.896667	5.176705	.9818485	4
16	.1782298	.181129	5.520900	.9839889	44	.37	.1842373	1.87446	5.334869	.9828818	23	.57	1.899523	5.168631	.9817933	3
17	.1785160	.181430	5.511757	.9839370	43	.38	.1845232	1.87747	5.326313	.9828282	22	.58	1.902379	5.160581	.9817380	2
18	.1788022	.181730	5.502644	.9838850	42	.39	.1848091	1.88048	5.317783	.9827744	21	.59	1.905234	5.152555	.9816826	1
19	.1790884	.182031	5.493560	.9838330	41	.40	.1850949	1.88349	5.309279	.9827206	20	.60	1.908090	5.144554	.9816272	0
20	.1793746	.182331	5.484505	.9837808	40											
'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'	

Deg. 79.

Deg. 79.

Deg. 79.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

11 Deg.

11 Deg.

11 Deg.

°	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'		
0	.1908090	.194380	5.144554	.9816272	60	.21	.1968018	.200727	4.981881	.9804433	39	.11	.2025024	.206786	4.835901	.9792818	19
1	.1910945	.194682	5.136576	.9815716	59	.22	.1970870	.201030	4.974381	.9803860	38	.42	.2027873	.207090	4.828817	.9792228	18
2	.1913801	.194984	5.128622	.9815160	58	.23	.1973722	.201332	4.966903	.9803286	37	.43	.2030721	.207393	4.821753	.9791638	17
3	.1916656	.195286	5.120692	.9814603	57	.24	.1976573	.201635	4.959447	.9802712	36	.44	.2033669	.207696	4.814709	.9791047	16
4	.1919510	.195588	5.112785	.9814045	56	.25	.1979425	.201938	4.952012	.9802136	35	.45	.2036618	.208000	4.807685	.9790455	15
5	.1922365	.195890	5.104902	.9813486	55	.26	.1982276	.202240	4.944599	.9801560	34	.46	.2039565	.208303	4.800680	.9789862	14
6	.1925220	.196192	5.097042	.9812927	54	.27	.1985127	.202543	4.937206	.9800983	33	.47	.2042513	.208607	4.793695	.9789268	13
7	.1928074	.196494	5.089206	.9812366	53	.28	.1987978	.202846	4.929835	.9800405	32	.48	.2045461	.208910	4.786730	.9788674	12
8	.1930928	.196796	5.081392	.9811805	52	.29	.1990829	.203149	4.922485	.9799827	31	.49	.2048408	.209214	4.779783	.9788079	11
9	.1933782	.197098	5.073602	.9811243	51	.30	.1993679	.203452	4.915157	.9799247	30	.50	.2051355	.209518	4.772856	.9787483	10
10	.1936636	.197400	5.065835	.9810680	50	.31	.1996530	.203755	4.907849	.9798667	29	.51	.2054302	.209821	4.765949	.9786886	9
11	.1939490	.197703	5.058090	.9810116	49	.32	.1999380	.204058	4.900562	.9798086	28	.52	.2057249	.210125	4.759060	.9786288	8
12	.1942344	.198005	5.050369	.9809552	48	.33	.2002230	.204361	4.893295	.9797504	27	.53	.2060195	.210429	4.752190	.9785689	7
13	.1945197	.198307	5.042670	.9808986	47	.34	.2005080	.204664	4.886049	.9796921	26	.54	.2063142	.210733	4.745340	.9785090	6
14	.1948050	.198610	5.034993	.9808420	46	.35	.2007930	.204967	4.878824	.9796337	25	.55	.2066088	.211036	4.738508	.9784490	5
15	.1950903	.198912	5.027339	.9807853	45	.36	.2010779	.205270	4.871620	.9795752	24	.56	.2069034	.211340	4.731695	.9783889	4
16	.1953756	.199214	5.019707	.9807285	44	.37	.2013629	.205573	4.864435	.9795167	23	.57	.2071980	.211644	4.724901	.9783287	3
17	.1956609	.199517	5.012098	.9806716	43	.38	.2016478	.205876	4.857271	.9794581	22	.58	.2074926	.211948	4.718125	.9782684	2
18	.1959461	.199819	5.004511	.9806147	42	.39	.2019327	.206180	4.850128	.9793994	21	.59	.2077872	.212252	4.711368	.9782080	1
19	.1962314	.200122	4.996945	.9805576	41	.40	.2022176	.206483	4.843004	.9793406	20	.60	.2080817	.212556	4.704630	.9781476	0
20	.1965166	.200424	4.989402	.9805005	40												
'	Cosine.	Cotang.	Tang.	Sine.	'	'	Cosine.	Cotang.	Tang.	Sine.	'	'	Cosine.	Cotang.	Tang.	Sine.	'

Deg. 78.

Deg. 78.

Deg. 78.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

12 Deg.

12 Deg.

'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'			
0	.2079117	.212556	4.704630	.9781476	60	.21	.2138829	.218949	4.567261	.9768593	39	41	.2195624	.225054	4.443376	.9755985	19	
1	.2081962	.212860	4.697910	.9780871	59	.22	.2141671	.219254	4.560911	.9767970	38	42	.2198462	.225359	4.437350	.9755345	18	
2	.2084807	.213164	4.691208	.9780265	58	.23	.2144512	.219559	4.554577	.9767347	37	43	.2201300	.225665	4.431339	.9754706	17	
3	.2087652	.213468	4.684524	.9779658	57	.24	.2147353	.219864	4.548260	.9766723	36	44	.2204137	.225971	4.425343	.9754065	16	
4	.2090497	.213773	4.677859	.9779050	56	.25	.2150194	.220169	4.541960	.9766098	35	45	.2206974	.226276	4.419364	.9753423	15	
5	.2093341	.214077	4.671212	.9778441	55	.26	.2153035	.220474	4.535677	.9765472	34	46	.2209811	.226582	4.413399	.9752781	14	
6	.2096186	.214381	4.664583	.9777832	54	.27	.2155876	.220779	4.529410	.9764845	33	47	.2212648	.226888	4.407450	.9752138	13	
7	.2099030	.214685	4.657972	.9777222	53	.28	.2158716	.221084	4.523160	.9764217	32	48	.2215485	.227194	4.401516	.9751494	12	
8	.2101874	.214990	4.651378	.9776611	52	.29	.2161556	.221389	4.516926	.9763589	31	49	.2218321	.227500	4.395597	.9750849	11	
9	.2104718	.215294	4.644803	.9775999	51	.30	.2164396	.221694	4.510708	.9762960	30	50	.2221158	.227806	4.389694	.9750203	10	
10	.2107561	.215598	4.638245	.9775386	50	.31	.2167236	.221999	4.504507	.9762330	29	51	.2223994	.228112	4.383805	.9749556	9	
11	.2110405	.215903	4.631705	.9774773	49	.32	.2170076	.222305	4.498322	.9761699	28	52	.2226830	.228418	4.377931	.9748909	8	
12	.2113248	.216207	4.625183	.9774159	48	.33	.2172915	.222610	4.492153	.9761067	27	53	.2229666	.228724	4.372073	.9748261	7	
13	.2116091	.216512	4.618678	.9773544	47	.34	.2175754	.222915	4.486000	.9760435	26	54	.2232501	.229030	4.366229	.9747612	6	
14	.2118934	.216816	4.612190	.9772928	46	.35	.2178593	.223221	4.479863	.9759802	25	55	.2235337	.229336	4.360400	.9746962	5	
15	.2121777	.217121	4.605720	.9772311	45	.36	.2181432	.223526	4.473742	.9759168	24	56	.2238172	.229642	4.354586	.9746311	4	
16	.2124619	.217425	4.599268	.9771693	44	.37	.2184271	.223831	4.467637	.9758533	23	57	.2241007	.229949	4.348786	.9745660	3	
17	.2127462	.217730	4.592832	.9771075	43	.38	.2187110	.224137	4.461548	.9757897	22	58	.2243842	.230255	4.343001	.9745008	2	
18	.2130304	.218035	4.586414	.9770456	42	.39	.2189948	.224442	4.455475	.9757260	21	59	.2246676	.230561	4.337231	.9744355	1	
19	.2133146	.218340	4.580012	.9769836	41	.40	.2192786	.224748	4.449418	.9756623	20	60	.2249511	.230868	4.331475	.9743701	0	
20	.2135988	.218644	4.573628	.9769215	40													

Deg. 77.

Deg. 77.

Deg. 77.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

13 Deg.

13 Deg.

13 Deg.

'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'		
0	.2249511	.230868	4.331475	.9743701	60	.21	.2308989	.237311	4.213869	.9729777	39	.41	.2365555	.243465	4.107356	.9716180	19
1	.2252345	.231174	4.325734	.9743046	59	.22	.2311819	.237618	4.208419	.9729105	38	.42	.2368381	.243773	4.102164	.9715491	18
2	.2255179	.231481	4.320007	.9742390	58	.23	.2314649	.237926	4.202983	.9728432	37	.43	.2371207	.244081	4.096985	.9714802	17
3	.2258013	.231787	4.314295	.9741734	57	.24	.2317479	.238233	4.197560	.9727769	36	.44	.2374033	.244390	4.091817	.9714112	16
4	.2260846	.232094	4.308597	.9741077	56	.25	.2320309	.238541	4.192151	.9727104	35	.45	.2376859	.244698	4.086662	.9713421	15
5	.2263680	.232400	4.302913	.9740419	55	.26	.2323138	.238848	4.186754	.9726440	34	.46	.2379684	.245006	4.081519	.9712729	14
6	.2266513	.232707	4.297244	.9739760	54	.27	.2325967	.239156	4.181371	.9725773	33	.47	.2382510	.245315	4.076389	.9712036	13
7	.2269346	.233014	4.291588	.9739100	53	.28	.2328796	.239463	4.176001	.9725106	32	.48	.2385335	.245623	4.071270	.9711343	12
8	.2272179	.233320	4.285947	.9738439	52	.29	.2331625	.239771	4.170644	.9724438	31	.49	.2388159	.245932	4.066164	.9710649	11
9	.2275012	.233627	4.280319	.9737778	51	.30	.2334454	.240078	4.165299	.9723769	30	.50	.2390984	.246240	4.061070	.9709953	10
10	.2277844	.233934	4.274706	.9737116	50	.31	.2337282	.240386	4.159968	.9723102	29	.51	.2393808	.246549	4.055987	.9709258	9
11	.2280677	.234241	4.269107	.9736453	49	.32	.2340110	.240694	4.154650	.9722433	28	.52	.2396633	.246857	4.050917	.9708561	8
12	.2283509	.234547	4.263521	.9735789	48	.33	.2342938	.241001	4.149344	.9721768	27	.53	.2399457	.247166	4.045859	.9707863	7
13	.2286341	.234854	4.257950	.9735124	47	.34	.2345766	.241309	4.144051	.9721104	26	.54	.2402280	.247475	4.040812	.9707165	6
14	.2289172	.235161	4.252392	.9734458	46	.35	.2348594	.241617	4.138771	.9720439	25	.55	.2405104	.247783	4.035777	.9706466	5
15	.2292004	.235468	4.246848	.9733792	45	.36	.2351421	.241925	4.133504	.9719776	24	.56	.2407927	.248092	4.030755	.9705766	4
16	.2294835	.235775	4.241317	.9733125	44	.37	.2354248	.242233	4.128249	.9719110	23	.57	.2410751	.248401	4.025744	.9705065	3
17	.2297666	.236082	4.235800	.9732457	43	.38	.2357075	.242541	4.123007	.9718440	22	.58	.2413574	.248710	4.020744	.9704363	2
18	.2300497	.236389	4.230297	.9731789	42	.39	.2359902	.242849	4.117778	.9717778	21	.59	.2416396	.249019	4.015757	.9703660	1
19	.2303328	.236697	4.224808	.9731119	41	.40	.2362729	.243157	4.112561	.9717116	20	.60	.2419219	.249328	4.010780	.9702957	0
20	.2306159	.237004	4.219331	.9730449	40												
'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'		

Deg. 76.

Deg. 76.

Deg. 76.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

14 Deg.

14 Deg.

14 Deg.

/	Sine.	Tang.	Cotang.	Cosine.	/	Sine.	Tang.	Cotang.	Cosine.	/	Sine.	Tang.	Cotang.	Cosine.
0	.2419219	.249328	4.010780	.9702957	60	.21	.2478445	3.908901	.9687998	39	.41	.2534766	3.816295	.9673415
1	.2422041	.249637	4.005816	.9702253	59	.22	.2481263	3.904171	.9687277	38	.42	.2537579	3.811773	.9672678
2	.2424863	.249946	4.000863	.9701548	58	.23	.2484081	3.899451	.9686555	37	.43	.2540393	3.807260	.9671939
3	.2427685	.250255	3.995922	.9700842	57	.24	.2486899	3.894742	.9685832	36	.44	.2543206	3.802758	.9671200
4	.2430507	.250564	3.990992	.9700135	56	.25	.2489716	3.890044	.9685108	35	.45	.2546019	3.798266	.9670459
5	.2433329	.250873	3.986073	.9699428	55	.26	.2492533	3.885357	.9684383	34	.46	.2548832	3.793783	.9669718
6	.2436150	.251182	3.981166	.9698720	54	.27	.2495350	3.880680	.9683658	33	.47	.2551645	3.789310	.9668977
7	.2438971	.251491	3.976271	.9698011	53	.28	.2498167	3.876014	.9682931	32	.48	.2554458	3.784848	.9668234
8	.2441792	.251801	3.971386	.9697301	52	.29	.2500984	3.871358	.9682204	31	.49	.2557270	3.780395	.9667490
9	.2444613	.252110	3.966513	.9696591	51	.30	.2503800	3.866713	.9681476	30	.50	.2560082	3.775951	.9666746
10	.2447433	.252420	3.961651	.9695879	50	.31	.2506616	3.862078	.9680748	29	.51	.2562894	3.771518	.9666001
11	.2450254	.252729	3.956801	.9695167	49	.32	.2509432	3.857453	.9680018	28	.52	.2565705	3.767094	.9665255
12	.2453074	.253038	3.951961	.9694453	48	.33	.2512248	3.852839	.9679288	27	.53	.2568517	3.762680	.9664508
13	.2455894	.253348	3.947133	.9693740	47	.34	.2515063	3.848235	.9678557	26	.54	.2571328	3.758276	.9663761
14	.2458713	.253658	3.942315	.9693025	46	.35	.2517879	3.843642	.9677825	25	.55	.2574139	3.753881	.9663012
15	.2461533	.253967	3.937509	.9692309	45	.36	.2520694	3.839059	.9677092	24	.56	.2576950	3.749496	.9662263
16	.2464352	.254277	3.932714	.9691593	44	.37	.2523508	3.834486	.9676358	23	.57	.2579760	3.745120	.9661513
17	.2467171	.254587	3.927929	.9690875	43	.38	.2526323	3.829923	.9675624	22	.58	.2582570	3.740754	.9660762
18	.2469990	.254896	3.923156	.9690157	42	.39	.2529137	3.825370	.9674888	21	.59	.2585381	3.736398	.9660011
19	.2472809	.255206	3.918393	.9689438	41	.40	.2531952	3.820828	.9674152	20	.60	.2588190	3.732050	.9659258
20	.2475627	.255516	3.913642	.9688719	40									

Deg. 75.

Deg. 75.

Deg. 75.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

15 Deg.

15 Deg.

15 Deg.

'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'		
0	.2588190	.267949	3.732050	.9659258	60	.21	.2647147	.274507	3.642891	.9643268	39	.41	.2703204	.280773	3.561590	.9627704	19
1	.2591000	.268261	3.727713	.9658505	59	.22	.2649952	.274820	3.638744	.9642497	38	.42	.2706004	.281087	3.557613	.9626917	18
2	.2593810	.268572	3.723384	.9657751	58	.23	.2652757	.275133	3.634606	.9641726	37	.43	.2708805	.281401	3.553644	.9626130	17
3	.2596619	.268884	3.719065	.9656996	57	.24	.2655561	.275445	3.630477	.9640954	36	.44	.2711605	.281715	3.549684	.9625342	16
4	.2599428	.269196	3.714756	.9656240	56	.25	.2658366	.275758	3.626356	.9640181	35	.45	.2714404	.282029	3.545732	.9624552	15
5	.2602237	.269508	3.710455	.9655484	55	.26	.2661170	.276071	3.622244	.9639407	34	.46	.2717204	.282343	3.541788	.9623762	14
6	.2605045	.269820	3.706164	.9654726	54	.27	.2663973	.276385	3.618141	.9638633	33	.47	.2720003	.282657	3.537852	.9622972	13
7	.2607853	.270132	3.701883	.9653968	53	.28	.2666777	.276698	3.614046	.9637858	32	.48	.2722802	.282971	3.533925	.9622180	12
8	.2610662	.270444	3.697610	.9653209	52	.29	.2669581	.277011	3.609960	.9637081	31	.49	.2725601	.283285	3.530005	.9621387	11
9	.2613469	.270757	3.693346	.9652449	51	.30	.2672384	.277324	3.605883	.9636305	30	.50	.2728400	.283599	3.526093	.9620594	10
10	.2616277	.271069	3.689092	.9651689	50	.31	.2675187	.277637	3.601814	.9635527	29	.51	.2731198	.283914	3.522190	.9619800	9
11	.2619085	.271381	3.684847	.9650927	49	.32	.2677989	.277951	3.597754	.9634748	28	.52	.2733997	.284228	3.518294	.9619005	8
12	.2621892	.271694	3.680611	.9650165	48	.33	.2680792	.278264	3.593702	.9633969	27	.53	.2736794	.284543	3.514407	.9618210	7
13	.2624699	.272006	3.676384	.9649402	47	.34	.2683594	.278578	3.589659	.9633189	26	.54	.2739592	.284857	3.510527	.9617413	6
14	.2627506	.272318	3.672166	.9648638	46	.35	.2686396	.278891	3.585624	.9632408	25	.55	.2742390	.285172	3.506655	.9616616	5
15	.2630312	.272631	3.667957	.9647873	45	.36	.2689198	.279205	3.581597	.9631626	24	.56	.2745187	.285486	3.502791	.9615818	4
16	.2633118	.272943	3.663757	.9647108	44	.37	.2692000	.279518	3.577579	.9630843	23	.57	.2747984	.285801	3.498935	.9615019	3
17	.2635925	.273256	3.659566	.9646341	43	.38	.2694801	.279832	3.573569	.9630060	22	.58	.2750781	.286115	3.495087	.9614219	2
18	.2638730	.273569	3.655384	.9645574	42	.39	.2697602	.280145	3.569568	.9629275	21	.59	.2753577	.286430	3.491247	.9613418	1
19	.2641536	.273881	3.651211	.9644806	41	.40	.2700403	.280459	3.565574	.9628490	20	.60	.2756374	.286745	3.487414	.9612617	0
20	.2644342	.274194	3.647046	.9644037	40												
'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'		

Deg. 74.

Deg. 74.

Deg. 74.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

16 Deg.

16 Deg.

16 Deg.

'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'			
0	.2756374	.286745	3.487414	.9612617	60	.21	.2815042	.293368	3.408688	.9595600	39	.41	.2870819	.299697	3.336699	.9579060	19	
1	.2759170	.287060	3.483589	.9611815	59	.22	.2817833	.293683	3.405021	.9594781	38	.42	.2873605	.300014	3.333173	.9578225	18	
2	.2761965	.287375	3.479772	.9611012	58	.23	.2820624	.293999	3.401361	.9593961	37	.43	.2876391	.300331	3.329654	.9577389	17	
3	.2764761	.287690	3.475963	.9610208	57	.24	.2823415	.294316	3.397708	.9593140	36	.44	.2879177	.300648	3.326141	.9576552	16	
4	.2767556	.288005	3.472161	.9609403	56	.25	.2826205	.294632	3.394063	.9592318	35	.45	.2881963	.300965	3.322636	.9575714	15	
5	.2770352	.288320	3.468367	.9608598	55	.26	.2828995	.294948	3.390424	.9591496	34	.46	.2884748	.301283	3.319137	.9574875	14	
6	.2773147	.288635	3.464581	.9607792	54	.27	.2831785	.295264	3.386793	.9590672	33	.47	.2887533	.301600	3.315645	.9574035	13	
7	.2775941	.288950	3.460802	.9606984	53	.28	.2834575	.295580	3.383169	.9589848	32	.48	.2890318	.301917	3.312159	.9573195	12	
8	.2778736	.289265	3.457031	.9606177	52	.29	.2837364	.295897	3.379553	.9589023	31	.49	.2893103	.302235	3.308681	.9572354	11	
9	.2781530	.289580	3.453267	.9605368	51	.30	.2840153	.296213	3.375943	.9588197	30	.50	.2895887	.302552	3.305209	.9571512	10	
10	.2784324	.289896	3.449512	.9604558	50	.31	.2842942	.296529	3.372340	.9587371	29	.51	.2898671	.302870	3.301743	.9570669	9	
11	.2787118	.290211	3.445763	.9603748	49	.32	.2845731	.296846	3.368745	.9586543	28	.52	.2901455	.303187	3.298285	.9569825	8	
12	.2789911	.290526	3.442022	.9602937	48	.33	.2848520	.297163	3.365156	.9585715	27	.53	.2904239	.303505	3.294833	.9568981	7	
13	.2792704	.290842	3.438289	.9602125	47	.34	.2851308	.297479	3.361575	.9584886	26	.54	.2907022	.303823	3.291387	.9568136	6	
14	.2795497	.291157	3.434563	.9601312	46	.35	.2854096	.297796	3.358000	.9584056	25	.55	.2909805	.304141	3.287948	.9567290	5	
15	.2798290	.291473	3.430844	.9600499	45	.36	.2856884	.298112	3.354433	.9583226	24	.56	.2912588	.304458	3.284516	.9566443	4	
16	.2801083	.291789	3.427153	.9599684	44	.37	.2859671	.298429	3.350872	.9582394	23	.57	.2915371	.304776	3.281090	.9565595	3	
17	.2803875	.292104	3.423429	.9598869	43	.38	.2862458	.298746	3.347319	.9581562	22	.58	.2918153	.305094	3.277671	.9564747	2	
18	.2806667	.292420	3.419733	.9598053	42	.39	.2865246	.299063	3.343772	.9580729	21	.59	.2920935	.305412	3.274258	.9563898	1	
19	.2809459	.292736	3.416044	.9597236	41	.40	.2868032	.299380	3.340232	.9579895	20	.60	.2923717	.305730	3.270852	.9563048	0	
20	.2812251	.293052	3.412362	.9596418	40													
'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'			

Deg. 73.

Deg. 73.

Deg. 73.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

17 Deg.

17 Deg.

17 Deg.

'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.		
0	.2923717	.305730	3.270852	.9563048	60	.2982079	3.12422	3.200789	.9545009	39	.41	.3037559	.318820	3.136563	.9527499	19
1	.2926499	.306048	3.267452	.9562197	59	.2984856	.312742	3.197521	.9544141	38	.42	.3040331	.319140	3.133414	.9526615	18
2	.2929280	.306367	3.264059	.9561345	58	.2987632	.313061	3.194259	.9543273	37	.43	.3043102	.319461	3.130270	.9525730	17
3	.2932061	.306685	3.260672	.9560492	57	.2990408	.313381	3.191003	.9542403	36	.44	.3045872	.319781	3.127131	.9524844	16
4	.2934842	.307003	3.257292	.9559639	56	.2993184	.313700	3.187754	.9541533	35	.45	.3048643	.320102	3.123999	.9523958	15
5	.2937623	.307321	3.253918	.9558785	55	.2995959	.314020	3.184510	.9540662	34	.46	.3051413	.320423	3.120872	.9523071	14
6	.2940403	.307640	3.250550	.9557930	54	.2998734	.314339	3.181272	.9539790	33	.47	.3054183	.320744	3.117750	.9522183	13
7	.2943183	.307958	3.247189	.9557074	53	.3001509	.314659	3.178040	.9538917	32	.48	.3056953	.321064	3.114635	.9521294	12
8	.2945963	.308277	3.243834	.9556218	52	.3004284	.314979	3.174814	.9538044	31	.49	.3059723	.321385	3.111525	.9520404	11
9	.2948743	.308595	3.240486	.9555361	51	.3007058	.315298	3.171594	.9537170	30	.50	.3062492	.321706	3.108421	.9519514	10
10	.2951522	.308914	3.237143	.9554502	50	.3009832	.315618	3.168380	.9536294	29	.51	.3065261	.322027	3.105322	.9518623	9
11	.2954302	.309233	3.233807	.9553643	49	.3012606	.315938	3.165172	.9535418	28	.52	.3068030	.322348	3.102229	.9517731	8
12	.2957081	.309551	3.230478	.9552784	48	.3015380	.316258	3.161970	.9534542	27	.53	.3070798	.322670	3.099141	.9516838	7
13	.2959859	.309870	3.227154	.9551923	47	.3018153	.316578	3.158774	.9533664	26	.54	.3073566	.322991	3.096059	.9515944	6
14	.2962638	.310189	3.223837	.9551062	46	.3020926	.316898	3.155584	.9532786	25	.55	.3076334	.323312	3.092983	.9515050	5
15	.2965416	.310508	3.220526	.9550199	45	.3023699	.317218	3.152399	.9531907	24	.56	.3079102	.323633	3.089912	.9514154	4
16	.2968194	.310827	3.217221	.9549336	44	.3026471	.317538	3.149220	.9531027	23	.57	.3081869	.323955	3.086846	.9513258	3
17	.2970971	.311146	3.213922	.9548473	43	.3029244	.317859	3.146047	.9530146	22	.58	.3084636	.324276	3.083786	.9512361	2
18	.2973749	.311465	3.210630	.9547608	42	.3032016	.318179	3.142880	.9529264	21	.59	.3087403	.324598	3.080732	.9511464	1
19	.2976526	.311784	3.207344	.9546743	41	.3034788	.318499	3.139719	.9528382	20	.60	.3090170	.324919	3.077683	.9510565	0
20	.2979303	.312103	3.204063	.9545876	40											
'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.		

Deg. 72.

Deg. 72.

Deg. 72.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

18 Deg.

18 Deg.

18 Deg.

/'	Sine.	Tang.	Cotang.	Cosine.	/'	Sine.	Tang.	Cotang.	Cosine.	/'	Sine.	Tang.	Cotang.	Cosine.
0	.3090170	.3249190	3.077683	.9510565	60	.21	.3148209	3.014892	.9491511	39	.41	.3203374	2.957205	.9473035
1	.3092936	.325241	3.074640	.9509666	59	.22	.3150969	3.011960	.9490595	38	.42	.3206130	2.954372	.9472103
2	.3095702	.325563	3.071602	.9508766	58	.23	.3153730	3.009033	.9489678	37	.43	.3208885	2.951545	.9471170
3	.3098468	.325884	3.068569	.9507865	57	.24	.3156490	3.006110	.9488760	36	.44	.3211640	2.948722	.9470236
4	.3101234	.326206	3.065542	.9506963	56	.25	.3159250	3.003193	.9487842	35	.45	.3214395	2.945905	.9469301
5	.3103999	.326528	3.062520	.9506061	55	.26	.3162010	3.000282	.9486922	34	.46	.3217149	2.943092	.9468366
6	.3106764	.326850	3.059503	.9505157	54	.27	.3164770	2.997375	.9486002	33	.47	.3219903	2.940284	.9467430
7	.3109529	.327172	3.056492	.9504253	53	.28	.3167529	2.994473	.9485081	32	.48	.3222657	2.937480	.9466493
8	.3112294	.327494	3.053487	.9503348	52	.29	.3170288	2.991576	.9484159	31	.49	.3225411	2.934682	.9465555
9	.3115058	.327816	3.050486	.9502443	51	.30	.3173047	2.988685	.9483237	30	.50	.3228164	2.931888	.9464616
10	.3117822	.328138	3.047491	.9501536	50	.31	.3175805	2.985798	.9482313	29	.51	.3230917	2.929099	.9463677
11	.3120586	.328461	3.044501	.9500629	49	.32	.3178563	2.982916	.9481389	28	.52	.3233670	2.926315	.9462736
12	.3123349	.328783	3.041517	.9499721	48	.33	.3181321	2.980040	.9480464	27	.53	.3236422	2.923535	.9461795
13	.3126112	.329105	3.038538	.9498812	47	.34	.3184079	2.977168	.9479538	26	.54	.3239174	2.920761	.9460854
14	.3128875	.329428	3.035564	.9497902	46	.35	.3186836	2.974301	.9478612	25	.55	.3241926	2.917990	.9459911
15	.3131638	.329750	3.032595	.9496991	45	.36	.3189593	2.971439	.9477684	24	.56	.3244678	2.915225	.9458968
16	.3134400	.330073	3.029632	.9496080	44	.37	.3192350	2.968583	.9476756	23	.57	.3247429	2.912464	.9458023
17	.3137163	.330395	3.026673	.9495168	43	.38	.3195106	2.965731	.9475827	22	.58	.3250180	2.909708	.9457078
18	.3139925	.330718	3.023720	.9494255	42	.39	.3197863	2.962884	.9474897	21	.59	.3252931	2.906957	.9456132
19	.3142686	.331041	3.020772	.9493341	41	.40	.3200619	2.960042	.9473966	20	.60	.3255682	2.904210	.9455186
20	.3145448	.331363	3.017830	.9492426	40									
/'	Cosine.	Cotang.	Tang.	Sine.	/'	Cosine.	Cotang.	Tang.	Sine.	/'	Cosine.	Cotang.	Tang.	Sine.

Deg. 71.

Deg. 71.

Deg. 71.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

19 Deg.

19 Deg.

19 Deg.

'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'		
0	.325582	.344327	2.904210	.9455186	60	.21	.3313379	.351175	2.847583		.9435122	.3941	.3368214	.357723	2.795453	.9415686	19
1	.3258432	.344653	2.901468	.9454238	59	.22	.3316123	.351501	2.844935		.9434157	.3842	.3370953	.358051	2.792891	.9414705	18
2	.3261182	.344978	2.898731	.9453290	58	.23	.3318867	.351828	2.842292		.9433192	.3743	.33738691	.358380	2.790333	.9413724	17
3	.3263932	.345304	2.895998	.9452341	57	.24	.3321611	.352155	2.839653		.9432227	.3644	.3376429	.358708	2.787780	.9412743	16
4	.3266681	.345629	2.893270	.9451391	56	.25	.3324355	.352482	2.837019		.9431260	.3545	.3379167	.359036	2.785230	.9411760	15
5	.3269430	.345955	2.890546	.9450441	55	.26	.3327098	.352809	2.834389		.9430293	.3446	.3381905	.359365	2.782685	.9410777	14
6	.3272179	.346281	2.887827	.9449489	54	.27	.3329841	.353136	2.831763		.9429324	.3347	.3384642	.359693	2.780144	.9409793	13
7	.3274928	.346606	2.885113	.9448537	53	.28	.3332584	.353464	2.829142		.9428355	.3248	.3387379	.360022	2.777606	.9408808	12
8	.3277676	.346932	2.882403	.9447584	52	.29	.3335326	.353791	2.826525		.9427386	.3149	.3390116	.360350	2.775073	.9407822	11
9	.3280424	.347258	2.879697	.9446630	51	.30	.3338069	.354118	2.823912		.9426415	.3050	.3392852	.360679	2.772544	.9406835	10
10	.3283172	.347584	2.876997	.9445675	50	.31	.3340810	.354446	2.821304		.9425444	.2951	.3395589	.361008	2.770019	.9405848	9
11	.3285919	.347910	2.874300	.9444720	49	.32	.3343552	.354773	2.818700		.9424471	.2852	.3398325	.361337	2.767499	.9404860	8
12	.3288666	.348236	2.871608	.9443764	48	.33	.3346293	.355101	2.816100		.9423498	.2753	.3401060	.361666	2.764982	.9403871	7
13	.3291413	.348563	2.868921	.9442807	47	.34	.3349034	.355428	2.813504		.9422525	.2654	.3403796	.361994	2.762469	.9402881	6
14	.3294160	.348889	2.866238	.9441849	46	.35	.3351775	.355756	2.810913		.9421550	.2555	.3406531	.362324	2.759960	.9401891	5
15	.3296906	.349215	2.863560	.9440890	45	.36	.3354516	.356084	2.808326		.9420575	.2456	.3409265	.362653	2.757456	.9400909	4
16	.3299653	.349542	2.860886	.9439931	44	.37	.3357256	.356411	2.805743		.9419598	.2357	.3412000	.362982	2.754955	.9399907	3
17	.3302398	.349868	2.858216	.9438971	43	.38	.3359996	.356739	2.803164		.9418621	.2258	.3414734	.363311	2.752458	.9398914	2
18	.3305144	.350195	2.855551	.9438010	42	.39	.3362735	.357067	2.800590		.9417644	.2159	.3417468	.363640	2.749966	.9397921	1
19	.3307889	.350521	2.852891	.9437048	41	.40	.3365475	.357395	2.798019		.9416665	.2060	.3420201	.363970	2.747477	.9396926	0
20	.3310634	.350848	2.850234	.9436085	40												
'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'		

Deg. 70.

Deg. 70.

Deg. 70.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

20 Deg.

20 Deg.

20 Deg.

'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'			
0	.3420201	.363970	2.747477	.9396926	60	21	.3477540	.370903	2.696118	.9375858	39	41	.3532027	.377536	2.648753	.9355488	19	
1	.3422935	.364299	2.744992	.9395931	59	22	.3480267	.371234	2.693714	.9374846	38	42	.3534748	.377868	2.646423	.9354440	18	
2	.3425668	.364629	2.742512	.9394935	58	23	.3482994	.371565	2.691314	.9373833	37	43	.3537469	.378201	2.644096	.9353412	17	
3	.3428400	.364958	2.740035	.9393938	57	24	.3485720	.371896	2.68919	.9372820	36	44	.3540190	.378533	2.641774	.9352382	16	
4	.3431133	.365288	2.737562	.9392940	56	25	.3488447	.372227	2.686526	.9371806	35	45	.3542910	.378866	2.639454	.9351352	15	
5	.3433865	.365618	2.735093	.9391942	55	26	.3491173	.372559	2.684138	.9370790	34	46	.3545630	.379198	2.637139	.9350321	14	
6	.3436597	.365948	2.732628	.9390943	54	27	.3493898	.372890	2.681753	.9369774	33	47	.3548350	.379531	2.634827	.9349289	13	
7	.3439329	.366277	2.730167	.9389943	53	28	.3496624	.373221	2.679372	.9368758	32	48	.3551070	.379864	2.632518	.9348257	12	
8	.3442060	.366607	2.727710	.9388942	52	29	.3499349	.373553	2.676995	.9367740	31	49	.3553789	.380197	2.630213	.9347223	11	
9	.3444791	.366937	2.725256	.9387940	51	30	.3502074	.373884	2.674621	.9366722	30	50	.3556508	.380530	2.627912	.9346189	10	
10	.3447521	.367268	2.722807	.9386938	50	31	.3504798	.374216	2.672251	.9365703	29	51	.3559226	.380863	2.625614	.9345154	9	
11	.3450252	.367598	2.720362	.9385934	49	32	.3507523	.374547	2.669885	.9364683	28	52	.3561944	.381196	2.623319	.9344119	8	
12	.3452982	.367928	2.717920	.9384930	48	33	.3510246	.374879	2.667522	.9363662	27	53	.3564662	.381529	2.621028	.9343082	7	
13	.3455712	.368258	2.715482	.9383925	47	34	.3512970	.375211	2.665163	.9362641	26	54	.3567380	.381862	2.618741	.9342045	6	
14	.3458441	.368589	2.713048	.9382920	46	35	.3515693	.375543	2.662808	.9361618	25	55	.3570097	.382196	2.616457	.9341007	5	
15	.3461171	.368919	2.710618	.9381913	45	36	.3518416	.375875	2.660456	.9360595	24	56	.3572814	.382529	2.614176	.9339968	4	
16	.3463900	.369250	2.708192	.9380906	44	37	.3521139	.376207	2.658108	.9359571	23	57	.3575531	.382863	2.611899	.9338928	3	
17	.3466628	.369580	2.705769	.9379898	43	38	.3523862	.376539	2.655764	.9358547	22	58	.3578248	.383196	2.609625	.9337888	2	
18	.3469357	.369911	2.703351	.9378889	42	39	.3526584	.376871	2.653423	.9357521	21	59	.3580964	.383530	2.607355	.9336846	1	
19	.3472085	.370242	2.700936	.9377880	41	40	.3529306	.377203	2.651086	.9356495	20	60	.3583679	.383864	2.605089	.9335804	0	
20	.3474812	.370572	2.698525	.9376869	40													

Deg. 69.

Deg. 69.

Deg. 69.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

21 Deg.

21 Deg.

21 Deg.

'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'
0	.3533679	.383864	2.605089	.9335804	60	.213640641	.390889	2.558268	.9313739	39	.413694765	.397611	2.515018	.9292401	19
1	.3586395	.384197	2.602825	.9334761	59	.223643351	.391224	2.556075	.9312679	38	.423697468	.397948	2.512889	.9291326	18
2	.3589110	.384531	2.600565	.9333718	58	.233646059	.391560	2.553885	.9311619	37	.433700170	.398235	2.510762	.9290250	17
3	.3591825	.384865	2.598309	.9332673	57	.243648768	.391895	2.551699	.9310558	36	.443702872	.398522	2.508639	.9289173	16
4	.3594540	.385199	2.596056	.9331628	56	.253651476	.392231	2.549516	.9309496	35	.453705574	.398809	2.506519	.9288096	15
5	.3597254	.385533	2.593806	.9330582	55	.263654184	.392567	2.547335	.9308434	34	.463708276	.399096	2.504402	.9287017	14
6	.3599968	.385867	2.591560	.9329535	54	.273656891	.392902	2.545159	.9307370	33	.473710977	.399384	2.502289	.9285938	13
7	.3602682	.386202	2.589317	.9328488	53	.283659599	.393238	2.542985	.9306306	32	.483713678	.399671	2.500178	.9284858	12
8	.3605395	.386536	2.587078	.9327439	52	.293662306	.393574	2.540815	.9305241	31	.493716379	.400008	2.498070	.9283778	11
9	.3608108	.386870	2.584842	.9326390	51	.303665012	.393910	2.538647	.9304176	30	.503719079	.400346	2.495966	.9282696	10
10	.3610821	.387205	2.582609	.9325340	50	.313667719	.394246	2.536483	.9303109	29	.513721780	.400684	2.493864	.9281614	9
11	.3613534	.387539	2.580380	.9324290	49	.323670425	.394582	2.534323	.9302042	28	.523724479	.401021	2.491766	.9280531	8
12	.3616246	.387874	2.578153	.9323238	48	.333673130	.394918	2.532165	.9300974	27	.533727179	.401359	2.489670	.9279447	7
13	.3618958	.388209	2.575931	.9322186	47	.343675836	.395255	2.530011	.9299905	26	.543729878	.401697	2.487578	.9278363	6
14	.3621669	.388543	2.573711	.9321133	46	.353678541	.395591	2.527859	.9298835	25	.553732577	.402035	2.485488	.9277277	5
15	.3624380	.388878	2.571495	.9320079	45	.363681246	.395928	2.525711	.9297765	24	.563735275	.402373	2.483402	.9276191	4
16	.3627091	.389213	2.569283	.9319024	44	.373683950	.396264	2.523566	.9296694	23	.573737973	.402711	2.481319	.9275104	3
17	.3629802	.389548	2.567073	.9317969	43	.383686654	.396601	2.521424	.9295622	22	.583740671	.403049	2.479238	.9274016	2
18	.3632512	.389883	2.564867	.9316912	42	.393689358	.396937	2.519286	.9294549	21	.593743369	.403387	2.477161	.9272928	1
19	.3635222	.390218	2.562664	.9315855	41	.403692061	.397274	2.517150	.9293475	20	.603746066	.403725	2.475086	.9271839	0
20	.3637932	.390554	2.560464	.9314797	40										

Deg. 68.

Deg. 68.

Deg. 68.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

22 Deg.

22 Deg.

22 Deg.

'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosiné.	'	Sine.	Tang.	Cotang.	Cosine.	'		
0	.3746066	.404026	2.475086	.9271839	60	.21	.3802634	.411149	2.432204	.9248782	39	.41	.3856377	.417967	2.392531	.9226503	19
1	.3748763	.404364	2.473015	.9270748	59	.22	.3805324	.411489	2.430193	.9247676	38	.42	.3859060	.418309	2.390576	.9225381	18
2	.3751459	.404703	2.470947	.9269658	58	.23	.3808014	.411830	2.428186	.9246568	37	.43	.3861744	.418650	2.388625	.9224258	17
3	.3754156	.405041	2.468881	.9268566	57	.24	.3810704	.412170	2.426181	.9245460	36	.44	.3864427	.418992	2.386675	.9223134	16
4	.3756852	.405380	2.466819	.9267474	56	.25	.3813393	.412510	2.424180	.9244351	35	.45	.3867110	.419334	2.384729	.9222010	15
5	.3759547	.405719	2.464759	.9266380	55	.26	.3816082	.412851	2.422181	.9243242	34	.46	.3869792	.419676	2.382785	.9220884	14
6	.3762243	.406057	2.462703	.9265286	54	.27	.3818770	.413191	2.420185	.9242131	33	.47	.3872474	.420019	2.380844	.9219758	13
7	.3764938	.406396	2.460649	.9264192	53	.28	.3821459	.413532	2.418191	.9241020	32	.48	.3875156	.420361	2.378906	.9218632	12
8	.3767632	.406735	2.458598	.9263096	52	.29	.3824147	.413872	2.416201	.9239908	31	.49	.3877837	.420703	2.376970	.9217504	11
9	.3770327	.407074	2.456551	.9262000	51	.30	.3826834	.414213	2.414213	.9238795	30	.50	.3880518	.421046	2.375037	.9216375	10
10	.3773021	.407413	2.454506	.9260902	50	.31	.3829522	.414554	2.412228	.9237682	29	.51	.3883199	.421388	2.373106	.9215246	9
11	.3775714	.407753	2.452464	.9259805	49	.32	.3832209	.414895	2.410246	.9236567	28	.52	.3885880	.421731	2.371179	.9214116	8
12	.3778408	.408092	2.450425	.9258706	48	.33	.3834895	.415236	2.408267	.9235452	27	.53	.3888560	.422073	2.369254	.9212986	7
13	.3781101	.408431	2.448389	.9257606	47	.34	.3837582	.415577	2.406290	.9234336	26	.54	.3891240	.422416	2.367331	.9211854	6
14	.3783794	.408771	2.446355	.9256506	46	.35	.3840268	.415918	2.404316	.9233220	25	.55	.3893919	.422759	2.365411	.9210722	5
15	.3786486	.409110	2.444325	.9255405	45	.36	.3842953	.416259	2.402345	.9232102	24	.56	.3896598	.423102	2.363494	.9209589	4
16	.3789178	.409450	2.442298	.9254303	44	.37	.3845639	.416601	2.400377	.9230984	23	.57	.3899277	.423445	2.361580	.9208455	3
17	.3791870	.409790	2.440273	.9253201	43	.38	.3848324	.416942	2.398411	.9229865	22	.58	.3901955	.423788	2.359668	.9207320	2
18	.3794562	.410129	2.438251	.9252097	42	.39	.3851008	.417284	2.396449	.9228745	21	.59	.3904633	.424131	2.357759	.9206185	1
19	.3797253	.410469	2.436233	.9250993	41	.40	.3853693	.417625	2.394488	.9227624	20	.60	.3907311	.424474	2.355852	.9205049	0
20	.3799944	.410809	2.434217	.9249888	40												
'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'		

NATURAL SINES AND TANGENTS TO A RADIUS 1.

23 Deg.

23 Deg.

23 Deg.

'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'			
0	3907311	424474	2-355852	9205049	60	21	3963468	431703	2-316407	9181009	39	41	4016814	4388622	2-279865	9157795	19	
1	3909989	424818	2-353948	9203912	59	22	3966139	432048	2-314557	9179855	38	42	4019478	438969	2-278063	9156626	18	
2	3912666	425161	2-352046	9202774	58	23	3968809	432393	2-312709	9178701	37	43	4022141	439316	2-276264	9155456	17	
3	3915343	425505	2-350148	9201635	57	24	3971479	432738	2-310863	9177546	36	44	4024804	439663	2-274467	9154286	16	
4	3918019	425848	2-348251	9200496	56	25	3974148	433084	2-309020	9176391	35	45	4027467	440010	2-272672	9153115	15	
5	3920695	426192	2-346358	9199356	55	26	3976818	433429	2-307180	9175234	34	46	4030129	440357	2-270880	9151943	14	
6	3923371	426536	2-344467	9198215	54	27	3979486	433775	2-305342	9174077	33	47	4032791	440705	2-269090	9150770	13	
7	3926047	426880	2-342578	9197073	53	28	3982155	434120	2-303506	9172919	32	48	4035453	441052	2-267303	9149597	12	
8	3928722	427223	2-340692	9195931	52	29	3984823	434466	2-301673	9171760	31	49	4038114	441400	2-265518	9148422	11	
9	3931397	427568	2-338809	9194788	51	30	3987491	434812	2-299842	9170601	30	50	4040775	441747	2-263735	9147247	10	
10	3934071	427912	2-336928	9193644	50	31	3990158	435158	2-298014	9169440	29	51	4043436	442095	2-261955	9146072	9	
11	3936745	428256	2-335050	9192499	49	32	3992825	435504	2-296188	9168279	28	52	4046096	442443	2-260177	9144895	8	
12	3939419	428600	2-333174	9191353	48	33	3995492	435850	2-294365	9167118	27	53	4048756	442791	2-258401	9143718	7	
13	3942093	428944	2-331301	9190207	47	34	3998158	436196	2-292544	9165955	26	54	4051416	443139	2-256628	9142540	6	
14	3944766	429289	2-329431	9189060	46	35	4000825	436542	2-290725	9164791	25	55	4054075	443487	2-254857	9141361	5	
15	3947439	429633	2-327563	9187912	45	36	4003490	436889	2-288909	9163627	24	56	4056734	443835	2-253088	9140181	4	
16	3950111	429978	2-325697	9186763	44	37	4006156	437235	2-287095	9162462	23	57	4059393	444183	2-251322	9139001	3	
17	3952783	430323	2-323834	9185614	43	38	4008821	437582	2-285284	9161297	22	58	4062051	444531	2-249558	9137819	2	
18	3955455	430668	2-321974	9184464	42	39	4011486	437928	2-283475	9160130	21	59	4064709	444880	2-247796	9136637	1	
19	3958127	431012	2-320116	9183313	41	40	4014150	438275	2-281669	9158963	20	60	4067366	445228	2-246036	9135455	0	
20	3960798	431357	2-318260	9182161	40													

Deg. 66.

Deg. 66.

Deg. 66.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

24 Deg.

24 Deg.

24 Deg.

	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'
0	.4067366	.4452228	2.246036	.9135455	60	.4123096	.452568	2.209611	.9110438	39	.4176028	.459596	2.175822	.9086297	19
1	.4070024	.445577	2.244279	.9134271	59	.4125745	.452918	2.207901	.9109238	38	.4178671	.459948	2.174155	.9085082	18
2	.4072681	.445926	2.242524	.9133087	58	.4128395	.453269	2.206193	.9108038	37	.4181313	.460301	2.172491	.9083866	17
3	.4075337	.446274	2.240772	.9131902	57	.4131044	.453620	2.204487	.9106837	36	.4183956	.460653	2.170828	.9082649	16
4	.4077993	.446623	2.239021	.9130716	56	.4133693	.453970	2.202784	.9105635	35	.4186597	.461006	2.169167	.9081432	15
5	.4080649	.446972	2.237273	.9129529	55	.4136342	.454321	2.201083	.9104432	34	.4189239	.461359	2.167509	.9080214	14
6	.4083305	.447321	2.235528	.9128342	54	.4138990	.454672	2.199384	.9103223	33	.4191880	.461711	2.165852	.9078995	13
7	.4085960	.447670	2.233784	.9127154	53	.4141638	.455023	2.197687	.9102024	32	.4194521	.462064	2.164198	.9077775	12
8	.4088615	.448020	2.232043	.9125965	52	.4144285	.455375	2.195992	.9100819	31	.4197161	.462417	2.162546	.9076554	11
9	.4091269	.448369	2.230304	.9124775	51	.4146932	.455726	2.194299	.9099613	30	.4199801	.462771	2.160895	.9075333	10
10	.4093923	.448718	2.228567	.9123584	50	.4149579	.456077	2.192609	.9098406	29	.4202441	.463124	2.159247	.9074111	9
11	.4096577	.449068	2.226833	.9122393	49	.4152226	.456429	2.190921	.9097199	28	.4205080	.463477	2.157601	.9072888	8
12	.4099230	.449417	2.225100	.9121201	48	.4154872	.456780	2.189234	.9095990	27	.4207719	.463831	2.155957	.9071665	7
13	.4101883	.449767	2.223370	.9120008	47	.4157517	.457132	2.187551	.9094781	26	.4210358	.464184	2.154315	.9070440	6
14	.4104536	.450117	2.221643	.9118815	46	.4160163	.457483	2.185869	.9093572	25	.4212966	.464538	2.152675	.9069215	5
15	.4107189	.450467	2.219917	.9117620	45	.4162808	.457835	2.184189	.9092361	24	.4215634	.464891	2.151037	.9067989	4
16	.4109841	.450817	2.218194	.9116425	44	.4165453	.458187	2.182511	.9091150	23	.4218272	.465245	2.149402	.9066762	3
17	.4112492	.451167	2.216473	.9115229	43	.4168097	.458539	2.180836	.9089938	22	.4220909	.465599	2.147768	.9065535	2
18	.4115144	.451517	2.214754	.9114033	42	.4170741	.458891	2.179163	.9088725	21	.4223546	.465953	2.146136	.9064307	1
19	.4117795	.451867	2.213037	.9112835	41	.4173385	.459243	2.177492	.9087511	20	.4226183	.466307	2.144506	.9063078	0
20	.4120445	.452217	2.211323	.9111637	40										

Deg. 65.

Deg. 65.

Deg. 65.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

25 Deg.

25 Deg.

25 Deg.

'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'		
0	.4226183	.466307	2.144506	.9063078	60	.21	.4281467	.473765	2.110747	.9037093	39	.41	.4333970	.480909	2.079394	.9012031	19
1	.4228819	.466661	2.142879	.9061848	59	.22	.4284095	.474122	2.109161	.9035847	38	.42	.4336591	.481267	2.077846	.9010770	18
2	.4231455	.467016	2.141253	.9060618	58	.23	.4286723	.474478	2.107577	.9034600	37	.43	.4339212	.481625	2.076300	.9009508	17
3	.4234090	.467370	2.139630	.9059386	57	.24	.4289351	.474834	2.105995	.9033353	36	.44	.4341832	.481984	2.074756	.9008246	16
4	.4236725	.467725	2.138008	.9058154	56	.25	.4291979	.475191	2.104415	.9032105	35	.45	.4344453	.482342	2.073214	.9006982	15
5	.4239360	.468079	2.136389	.9056922	55	.26	.4294606	.475548	2.102836	.9030856	34	.46	.4347072	.482701	2.071674	.9005718	14
6	.4241994	.468434	2.134771	.9055688	54	.27	.4297233	.475904	2.101260	.9029606	33	.47	.4349692	.483060	2.070135	.9004453	13
7	.4244628	.468789	2.133155	.9054454	53	.28	.4299859	.476261	2.099686	.9028356	32	.48	.4352311	.483418	2.068599	.9003188	12
8	.4247262	.469143	2.131542	.9053219	52	.29	.4302485	.476618	2.098114	.9027105	31	.49	.4354930	.483777	2.067064	.9001921	11
9	.4249895	.469498	2.129930	.9051983	51	.30	.4305111	.476975	2.096543	.9025853	30	.50	.4357548	.484136	2.065531	.9000654	10
10	.4252528	.469853	2.128321	.9050746	50	.31	.4307736	.477332	2.094975	.9024600	29	.51	.4360166	.484495	2.064000	.8999386	9
11	.4255161	.470209	2.126713	.9049509	49	.32	.4310361	.477689	2.093408	.9023347	28	.52	.4362784	.484855	2.062471	.8998117	8
12	.4257793	.470564	2.125108	.9048271	48	.33	.4312986	.478047	2.091843	.9022092	27	.53	.4365401	.485214	2.060944	.8996848	7
13	.4260425	.470919	2.123504	.9047032	47	.34	.4315610	.478404	2.090280	.9020838	26	.54	.4368018	.485573	2.059418	.8995578	6
14	.4263056	.471275	2.121903	.9045792	46	.35	.4318234	.478762	2.088720	.9019582	25	.55	.4370634	.485933	2.057895	.8994307	5
15	.4265687	.471630	2.120303	.9044551	45	.36	.4320857	.479119	2.087161	.9018325	24	.56	.4373251	.486293	2.056373	.8993035	4
16	.4268318	.471986	2.118705	.9043310	44	.37	.4323481	.479477	2.085603	.9017068	23	.57	.4375866	.486652	2.054853	.8991763	3
17	.4270949	.472342	2.117110	.9042068	43	.38	.4326103	.479835	2.084048	.9015810	22	.58	.4378482	.487012	2.053334	.8990489	2
18	.4273579	.472697	2.115516	.9040825	42	.39	.4328726	.480193	2.082495	.9014551	21	.59	.4381097	.487372	2.051818	.8989215	1
19	.4276208	.473053	2.113924	.9039582	41	.40	.4331348	.480551	2.080943	.9013292	20	.60	.4383711	.487732	2.050303	.8987940	0
20	.4278838	.473409	2.112334	.9038338	40												
'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'		

Deg. 64.

Deg. 64.

Deg. 64.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

26 Deg.		26 Deg.		26 Deg.		26 Deg.		26 Deg.		26 Deg.		26 Deg.		26 Deg.			
/	Sine.	Tang.	Cotang.	Cosine.	/	Sine.	Tang.	Cotang.	Cosine.	/	Sine.	Tang.	Cotang.	Cosine.	/		
0	.4383711	.487732	2-050303	.8987940	60	21	.4438534	.495317	2-018908	.8960994	39	41	.4490591	.502583	1-989720	.8935021	19
1	.4386326	.488092	2-048791	.8986665	59	22	.4441140	.495679	2-017433	.8959703	38	42	.4493190	.502947	1-988278	.8933714	18
2	.4388940	.488453	2-047280	.8985389	58	23	.4443746	.496041	2-015959	.8958411	37	43	.4495789	.503312	1-986838	.8932406	17
3	.4391553	.488813	2-045770	.8984112	57	24	.4446352	.496404	2-014486	.8957118	36	44	.4498387	.503676	1-985400	.8931098	16
4	.4394166	.489173	2-044263	.8982834	56	25	.4448957	.496766	2-013016	.8955824	35	45	.4500984	.504041	1-983963	.8929789	15
5	.4396779	.489534	2-042757	.8981555	55	26	.4451562	.497129	2-011547	.8954529	34	46	.4503582	.504406	1-982528	.8928480	14
6	.4399392	.489894	2-041254	.8980276	54	27	.4454167	.497492	2-010080	.8953234	33	47	.4506179	.504771	1-981095	.8927169	13
7	.4402004	.490255	2-039751	.8978996	53	28	.4456771	.497855	2-008615	.8951938	32	48	.4508775	.505136	1-979663	.8925858	12
8	.4404615	.490616	2-038251	.8977715	52	29	.4459375	.498218	2-007151	.8950641	31	49	.4511372	.505501	1-978233	.8924546	11
9	.4407227	.490977	2-036753	.8976433	51	30	.4461978	.498581	2-005689	.8949344	30	50	.4513967	.505866	1-976805	.8923234	10
10	.4409838	.491338	2-035256	.8975151	50	31	.4464581	.498944	2-004229	.8948045	29	51	.4516563	.506232	1-975378	.8921920	9
11	.4412448	.491699	2-033761	.8973868	49	32	.4467184	.499308	2-002771	.8946746	28	52	.4519158	.506597	1-973953	.8920606	8
12	.4415059	.492061	2-032268	.8972584	48	33	.4469786	.499671	2-001314	.8945446	27	53	.4521753	.506963	1-972529	.8919291	7
13	.4417668	.492422	2-030776	.8971299	47	34	.4472388	.500035	1-999859	.8944146	26	54	.4524347	.507329	1-971107	.8917975	6
14	.4420278	.492783	2-029287	.8970014	46	35	.4474990	.500398	1-998405	.8942844	25	55	.4526941	.507694	1-969687	.8916659	5
15	.4422887	.493145	2-027799	.8968727	45	36	.4477591	.500762	1-996953	.8941542	24	56	.4529535	.508060	1-968269	.8915342	4
16	.4425496	.493507	2-026313	.8967440	44	37	.4480192	.501126	1-995503	.8940240	23	57	.4532128	.508426	1-966851	.8914024	3
17	.4428104	.493868	2-024828	.8966153	43	38	.4482792	.501490	1-994055	.8938936	22	58	.4534721	.508792	1-965436	.8912705	2
18	.4430712	.494230	2-023346	.8964864	42	39	.4485392	.501854	1-992608	.8937632	21	59	.4537313	.509159	1-964022	.8911385	1
19	.4433319	.494592	2-021865	.8963575	41	40	.4487992	.502218	1-991163	.8936326	20	60	.4539905	.509525	1-962610	.8910065	0
20	.4435927	.494954	2-020386	.8962285	40												

Deg. 63.

Deg. 63.

Deg. 63.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

27 Deg.

27 Deg.

27 Deg.

/	Sine.	Tang.	Cotang.	Cosine.	/	Sine.	Tang.	Cotang.	Cosine.	/	Sine.	Tang.	Cotang.	Cosine.	/		
0	.453905	.509525	1.962610	.8910065	60	.21	.4594248	5.17244	1.933323	.8882166	.39	41	.4615845	.524640	1.906066	.8855288	19
1	.4542497	.509891	1.961200	.8908744	59	.22	.4596832	5.17612	1.931945	.8880830	.38	12	.4618420	.525011	1.904719	.8858936	18
2	.4545088	.510258	1.959791	.8907423	58	.23	.4599415	.517981	1.930569	.8879492	.37	43	.4650996	.525382	1.903373	.8852584	17
3	.4547679	.510625	1.958383	.8906100	57	.24	.4601998	.518350	1.929195	.8878154	.36	44	.4653571	.525754	1.902029	.8851230	16
4	.4550269	.510991	1.956978	.8904777	56	.25	.4604580	.518719	1.927822	.8876815	.35	15	.4656145	.526125	1.900687	.8849876	15
5	.4552859	.511358	1.955573	.8903453	55	.26	.4607162	.519089	1.926451	.8875475	.34	16	.4658719	.526496	1.899346	.8848522	14
6	.4555449	.511725	1.954171	.8902128	54	.27	.4609744	.519458	1.925081	.8874134	.33	47	.4661293	.526868	1.898006	.8847166	13
7	.4558038	.512093	1.952770	.8900803	53	.28	.4612325	.519827	1.923713	.8872793	.32	48	.4663866	.527240	1.896668	.8845810	12
8	.4560627	.512460	1.951371	.8899476	52	.29	.4614906	.520197	1.922347	.8871451	.31	49	.4666439	.527612	1.895332	.8844453	11
9	.4563216	.512827	1.949973	.8898149	51	.30	.4617486	.520567	1.920982	.8870108	.30	50	.4669012	.527983	1.893997	.8843095	10
10	.4565804	.513195	1.948577	.8896822	50	.31	.4620066	.520936	1.919618	.8868765	.29	51	.4671584	.528356	1.892663	.8841736	9
11	.4568392	.513562	1.947182	.8895493	49	.32	.4622646	.521306	1.918256	.8867420	.28	52	.4674156	.528728	1.891331	.8840377	8
12	.4570979	.513930	1.945789	.8894164	48	.33	.4625225	.521676	1.916896	.8866075	.27	53	.4676727	.529100	1.890000	.8839017	7
13	.4573566	.514298	1.944398	.8892834	47	.34	.4627804	.522046	1.915537	.8864730	.26	54	.4679298	.529472	1.888671	.8837656	6
14	.4576153	.514665	1.943008	.8891503	46	.35	.4630382	.522417	1.914179	.8863383	.25	55	.4681869	.529845	1.887343	.8836295	5
15	.4578739	.515033	1.941620	.8890171	45	.36	.4632960	.522787	1.912823	.8862036	.24	56	.4684439	.530217	1.886017	.8834933	4
16	.4581325	.515401	1.940233	.8888839	44	.37	.4635538	.523157	1.911469	.8860688	.23	57	.4687009	.530590	1.884692	.8833569	3
17	.4583910	.515770	1.938848	.8887506	43	.38	.4638115	.523528	1.910116	.8859339	.22	58	.4689578	.530963	1.883369	.8832206	2
18	.4586496	.516138	1.937464	.8886172	42	.39	.4640692	.523899	1.908764	.8857989	.21	59	.4692147	.531336	1.882047	.8830841	1
19	.4589080	.516506	1.936082	.8884838	41	.40	.4643269	.524269	1.907414	.8856639	.20	60	.4694716	.531709	1.880726	.8829476	0
20	.4591665	.516875	1.934702	.8883503	40												
/	Cosine.	Cotang.	Tang.	Sine.	/	Cosine.	Cotang.	Tang.	Sine.	/	Cosine.	Cotang.	Tang.	Sine.	/		

Deg. 62.

Deg. 62.

Deg. 62

NATURAL SINES AND TANGENTS TO A RADIUS 1.

28 Deg.

28 Deg.

28 Deg.

'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	
0	4694716	531709	1880726	8829476	60	21	4748564	539570	1853325	8800633	39	41	4799683	547106	1827799	8772858
1	4697284	532082	1879407	8828110	59	22	4751124	539946	1852035	8799251	38	42	4802235	547484	1826537	8771462
2	4699852	532455	1878089	8826743	58	23	4753663	540322	1850747	8797869	37	43	4804786	547862	1825276	8770064
3	4702419	532829	1876773	8825376	57	24	4756242	540698	1849461	8796486	36	44	4807337	548240	1824017	8768666
4	4704986	533202	1875458	8824007	56	25	4758801	541074	1848176	8795102	35	45	4809888	548618	1822759	8767268
5	4707553	533576	1874145	8822638	55	26	4761359	541450	1846892	8793717	34	46	4812438	548997	1821502	8765868
6	4710119	533950	1872833	8821269	54	27	4763917	541826	1845609	8792332	33	47	4814987	549375	1820247	8764468
7	4712685	534324	1871523	8819898	53	28	4766474	542202	1844328	8790946	32	48	4817537	549754	1818993	8763067
8	4715250	534698	1870214	8818527	52	29	4769031	542579	1843049	8789559	31	49	4820086	550133	1817740	8761665
9	4717815	535072	1868906	8817155	51	30	4771588	542955	1841770	8788171	30	50	4822634	550512	1816489	8760263
10	4720380	535446	1867600	8815782	50	31	4774144	543332	1840494	8786783	29	51	4825182	550891	1815239	8758859
11	4722944	535820	1866295	8814409	49	32	4776700	543709	1839218	8785394	28	52	4827730	551270	1813990	8757455
12	4725508	536195	1864992	8813035	48	33	4779255	544086	1837944	8784004	27	53	4830277	551650	1812743	8756051
13	4728071	536569	1863690	8811660	47	34	4781810	544463	1836671	8782613	26	54	4832824	552029	1811496	8754645
14	4730634	536944	1862389	8810284	46	35	4784364	544840	1835399	8781222	25	55	4835370	552409	1810252	8753239
15	4733197	537319	1861090	8808907	45	36	4786919	545217	1834129	8779830	24	56	4837916	552789	1809008	8751832
16	4735759	537694	1859792	8807530	44	37	4789472	545595	1832861	8778437	23	57	4840462	553168	1807766	8750425
17	4738321	538069	1858496	8806152	43	38	4792026	545972	1831593	8777043	22	58	4843007	553548	1806525	8749016
18	4740882	538444	1857201	8804774	42	39	4794579	546350	1830327	8775649	21	59	4845552	553928	1805286	8747607
19	4743443	538819	1855908	8803394	41	40	4797131	546728	1829062	8774254	20	60	4848096	554309	1804047	8746197
20	4746004	539195	1854615	8802014	40											
'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'	

Deg. 61.

Deg. 61.

Deg. 61.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

30 Deg.

30 Deg.

30 Deg.

/	Sine.	Tang.	Cotang.	Cosine.	/	Sine.	Tang.	Cotang.	Cosine.	/	Sine.	Tang.	Cotang.	Cosine.	/			
0	.5000000	.577350	1.732050	.8660254	60	21	.5052809	.585524	1.707871	.8623549	39	41	.5102928	.5933363	1.685308	.8600007	19	
1	.5002519	.577738	1.730887	.8658799	59	22	.5055319	.585914	1.706732	.8628079	38	42	.5105429	.593756	1.684191	.8598523	18	
2	.5005037	.578126	1.729726	.8657344	58	23	.5057828	.586305	1.705595	.8626608	37	43	.5107930	.594150	1.683076	.8597037	17	
3	.5007556	.578514	1.728565	.8655887	57	24	.5060338	.586696	1.704458	.8625137	36	44	.5110431	.594543	1.681962	.8595551	16	
4	.5010073	.578902	1.727406	.8654430	56	25	.5062846	.587087	1.703323	.8623664	35	45	.5112931	.594937	1.680848	.8594064	15	
5	.5012591	.579291	1.726247	.8652973	55	26	.5065355	.587478	1.702189	.8622191	34	46	.5115431	.595331	1.679736	.8592576	14	
6	.5015107	.579679	1.725090	.8651514	54	27	.5067863	.587870	1.701055	.8620717	33	47	.5117930	.595725	1.678625	.8591088	13	
7	.5017624	.580068	1.723934	.8650055	53	28	.5070370	.588261	1.699923	.8619243	32	48	.5120429	.596119	1.677515	.8589599	12	
8	.5020140	.580457	1.722779	.8648595	52	29	.5072877	.588653	1.698792	.8617768	31	49	.5122927	.596514	1.676406	.8588109	11	
9	.5022655	.580846	1.721626	.8647134	51	30	.5075384	.589045	1.697663	.8616292	30	50	.5125425	.596908	1.675298	.8586619	10	
10	.5025170	.581235	1.720473	.8645673	50	31	.5077890	.589436	1.696534	.8614815	29	51	.5127923	.597303	1.674192	.8585127	9	
11	.5027685	.581624	1.719322	.8644211	49	32	.5080396	.589828	1.695406	.8613337	28	52	.5130420	.597697	1.673086	.8583635	8	
12	.5030199	.582013	1.718172	.8642748	48	33	.5082901	.590221	1.694280	.8611859	27	53	.5132916	.598092	1.671981	.8582143	7	
13	.5032713	.582403	1.717023	.8641284	47	34	.5085406	.590613	1.693155	.8610380	26	54	.5135413	.598487	1.670878	.8580649	6	
14	.5035227	.582793	1.715875	.8639820	46	35	.5087910	.591005	1.692030	.8608901	25	55	.5137908	.598882	1.669775	.8579155	5	
15	.5037740	.583182	1.714728	.8638355	45	36	.5090414	.591398	1.690907	.8607420	24	56	.5140404	.599278	1.668674	.8577660	4	
16	.5040252	.583572	1.713582	.8636889	44	37	.5092918	.591791	1.689785	.8605939	23	57	.5142899	.599673	1.667574	.8576164	3	
17	.5042765	.583962	1.712438	.8635423	43	38	.5095421	.592183	1.688664	.8604457	22	58	.5145393	.600069	1.666474	.8574668	2	
18	.5045276	.584352	1.711294	.8633956	42	39	.5097924	.592576	1.687544	.8602975	21	59	.5147887	.600464	1.665376	.8573171	1	
19	.5047788	.584743	1.710152	.8632488	41	40	.5100426	.592969	1.686426	.8601491	20	60	.5150381	.600860	1.664279	.8571673	0	
20	.5050298	.585133	1.709011	.8631019	40													
/	Cosine.	Cotang.	Tang.	Sine.	/	Cosine.	Cotang.	Tang.	Sine.	/	Cosine.	Cotang.	Tang.	Sine.	/			

Deg. 59.

Deg. 59.

Deg. 59.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

31 Deg.

31 Deg.

31 Deg.

°	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'		
0	.5150381	.600860	1.664279	.8571673	60	.21	.5202646	.609205	1.641482	.8540051	39	.41	.5252241	.617210	1.620192	.8509639	19
1	.5152874	.601256	1.663183	.8570174	59	.22	.5205130	.609604	1.640408	.8538538	38	.42	.5254717	.617612	1.619138	.8508111	18
2	.5155367	.601652	1.662088	.8568675	58	.23	.5207613	.610003	1.639335	.8537023	37	.43	.5257191	.618014	1.618085	.8506582	17
3	.5157859	.602049	1.660994	.8567175	57	.24	.5210096	.610402	1.638263	.8535508	36	.44	.5259665	.618416	1.617033	.8505053	16
4	.5160351	.602445	1.659901	.8565674	56	.25	.5212579	.610801	1.637191	.8533992	35	.45	.5262139	.618818	1.615982	.8503522	15
5	.5162842	.602841	1.658809	.8564173	55	.26	.5215061	.611201	1.636121	.8532475	34	.46	.5264613	.619221	1.614932	.8501991	14
6	.5165333	.603238	1.657718	.8562671	54	.27	.5217543	.611601	1.635052	.8530958	33	.47	.5267085	.619623	1.613982	.8500459	13
7	.5167824	.603635	1.656629	.8561168	53	.28	.5220024	.612000	1.633984	.8529440	32	.48	.5269558	.620026	1.612934	.8498927	12
8	.5170314	.604032	1.655540	.8559664	52	.29	.5222505	.612400	1.632917	.8527921	31	.49	.5272030	.620429	1.611787	.8497394	11
9	.5172804	.604429	1.654452	.8558160	51	.30	.5224986	.612800	1.631851	.8526402	30	.50	.5274502	.620832	1.610741	.8495860	10
10	.5175293	.604826	1.653366	.8556655	50	.31	.5227466	.613201	1.630786	.8524881	29	.51	.5276973	.621235	1.609696	.8494325	9
11	.5177782	.605224	1.652280	.8555149	49	.32	.5229945	.613601	1.629722	.8523360	28	.52	.5279443	.621638	1.608652	.8492790	8
12	.5180270	.605621	1.651196	.8553643	48	.33	.5232424	.614002	1.628659	.8521839	27	.53	.5281914	.622041	1.607609	.8491254	7
13	.5182758	.606019	1.650112	.8552135	47	.34	.5234903	.614402	1.627597	.8520316	26	.54	.5284383	.622445	1.606567	.8489717	6
14	.5185246	.606417	1.649030	.8550627	46	.35	.5237381	.614803	1.626536	.8518793	25	.55	.5286853	.622848	1.605526	.8488179	5
15	.5187733	.606814	1.647949	.8549119	45	.36	.5239859	.615204	1.625476	.8517269	24	.56	.5289322	.623252	1.604485	.8486641	4
16	.5190219	.607213	1.646868	.8547609	44	.37	.5242336	.615605	1.624417	.8515745	23	.57	.5291790	.623656	1.603446	.8485102	3
17	.5192705	.607611	1.645789	.8546099	43	.38	.5244813	.616006	1.623359	.8514219	22	.58	.5294258	.624060	1.602408	.8483562	2
18	.5195191	.608009	1.644711	.8544588	42	.39	.5247290	.616407	1.622302	.8512693	21	.59	.5296726	.624465	1.601370	.8482022	1
19	.5197676	.608408	1.643633	.8543077	41	.40	.5249766	.616809	1.621246	.8511167	20	.60	.5299193	.624869	1.600334	.8480481	0
20	.5200161	.608806	1.642557	.8541564	40												
°	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'		

Dec. 58.

Deg. 58.

Deg. 58.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

32 Deg.

32 Deg.

/	Sine.	Tang.	Cotang.	Cosine.	/	Sine.	Tang.	Cotang.	Cosine.	/	Sine.	Tang.	Cotang.	Cosine.	/		
0	.5299193	.624869	1.600334	.8490481	60	.21	.5350898	.633395	1.578791	.8447952	39	.41	.5399555	.641577	1.558657	.8416679	19
1	.5301659	.625273	1.599299	.8478939	59	.22	.5353355	.633803	1.577776	.8446395	38	.42	.5402403	.641988	1.557660	.8415108	18
2	.5304125	.625678	1.598264	.8477397	58	.23	.5355812	.634211	1.576761	.8444838	37	.43	.5404851	.642399	1.556663	.8413536	17
3	.5306591	.626083	1.597231	.8475853	57	.24	.5358268	.634619	1.575747	.8443279	36	.44	.5407298	.642810	1.555668	.8411963	16
4	.5309057	.626488	1.596198	.8474309	56	.25	.5360724	.635027	1.574735	.8441720	35	.45	.5409745	.643221	1.554674	.8410390	15
5	.5311521	.626893	1.595167	.8472765	55	.26	.5363179	.635435	1.573723	.8440161	34	.46	.5412191	.643632	1.553680	.8408816	14
6	.5313986	.627298	1.594136	.8471219	54	.27	.5365634	.635844	1.572712	.8438600	33	.47	.5414637	.644044	1.552688	.8407241	13
7	.5316450	.627704	1.593107	.8469673	53	.28	.5368089	.636252	1.571702	.8437039	32	.48	.5417082	.644456	1.551696	.8405666	12
8	.5318913	.628109	1.592078	.8468126	52	.29	.5370543	.636661	1.570693	.8435477	31	.49	.5419527	.644867	1.550705	.8404090	11
9	.5321376	.628515	1.591050	.8466579	51	.30	.5372996	.637070	1.569685	.8433914	30	.50	.5421971	.645279	1.549715	.8402513	10
10	.5323839	.628921	1.590023	.8465030	50	.31	.5375449	.637479	1.568678	.8432351	29	.51	.5424415	.645691	1.548726	.8400936	9
11	.5326301	.629327	1.588997	.8463481	49	.32	.5377902	.637888	1.567672	.8430787	28	.52	.5426859	.646104	1.547738	.8399357	8
12	.5328763	.629733	1.587973	.8461932	48	.33	.5380354	.638297	1.566666	.8429222	27	.53	.5429302	.646516	1.546751	.8397778	7
13	.5331224	.630139	1.586949	.8460381	47	.34	.5382807	.638707	1.565662	.8427657	26	.54	.5431744	.646929	1.545764	.8396199	6
14	.5333685	.630546	1.585926	.8458830	46	.35	.5385257	.639116	1.564659	.8426091	25	.55	.5434187	.647341	1.544779	.8394618	5
15	.5336145	.630953	1.584904	.8457278	45	.36	.5387708	.639526	1.563656	.8424524	24	.56	.5436628	.647754	1.543794	.8393037	4
16	.5338605	.631359	1.583883	.8455726	44	.37	.5390158	.639936	1.562654	.8422956	23	.57	.5439069	.648167	1.542810	.8391455	3
17	.5341065	.631766	1.582862	.8454172	43	.38	.5392608	.640346	1.561654	.8421388	22	.58	.5441510	.648580	1.541828	.8389873	2
18	.5343523	.632173	1.581843	.8452618	42	.39	.5395058	.640756	1.560654	.8419819	21	.59	.5443951	.648994	1.540846	.8388290	1
19	.5345982	.632581	1.580825	.8451064	41	.40	.5397507	.641167	1.559655	.8418249	20	.60	.5446390	.649407	1.539865	.8386706	0
20	.5348440	.632988	1.579807	.8449508	40												
/	Cosine.	Cotang.	Tang.	Sine.	/	Cosine.	Cotang.	Tang.	Sine.	/	Cosine.	Cotang.	Tang.	Sine.	/		

Deg. 57.

Deg. 57.

Deg. 57.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

33 Deg.

33 Deg.

33 Deg.

'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'		
0	·5446390	·649407	1·539865	·8386706	60	·21	·5497520	·658127	1·519463	·8353279	39	·41	·5546024	·666496	1·500382	·8321155	19
1	·5448830	·649821	1·538884	·8385121	59	·22	·5499950	·658544	1·518501	·8351680	38	·42	·5548444	·666917	1·499436	·8319541	18
2	·5451269	·650235	1·537905	·8383536	58	·23	·5502379	·658961	1·517540	·8350080	37	·43	·5550864	·667337	1·498492	·8317927	17
3	·5453707	·650649	1·536927	·8381950	57	·24	·5504807	·659378	1·516579	·8348479	36	·44	·5553283	·667758	1·497548	·8316312	16
4	·5456145	·651063	1·535949	·8380363	56	·25	·5507236	·659796	1·515620	·8346877	35	·45	·5555702	·668178	1·496605	·8314696	15
5	·5458583	·651477	1·534972	·8378775	55	·26	·5509663	·660213	1·514661	·8345275	34	·46	·5558121	·668599	1·495663	·8313080	14
6	·5461020	·651891	1·533996	·8377187	54	·27	·5512091	·660631	1·513703	·8343672	33	·47	·5560539	·669020	1·494722	·8311463	13
7	·5463456	·652306	1·533021	·8375598	53	·28	·5514518	·661049	1·512746	·8342068	32	·48	·5562956	·669441	1·493782	·8309845	12
8	·5465892	·652721	1·532047	·8374009	52	·29	·5516944	·661467	1·511790	·8340463	31	·49	·5565373	·669863	1·492842	·8308226	11
9	·5468328	·653136	1·531074	·8372418	51	·30	·5519370	·661885	1·510835	·8338858	30	·50	·5567790	·670284	1·491903	·8306607	10
10	·5470763	·653551	1·530102	·8370827	50	·31	·5521795	·662304	1·509880	·8337252	29	·51	·5570206	·670706	1·490965	·8304987	9
11	·5473198	·653966	1·529130	·8369236	49	·32	·5524220	·662722	1·508927	·8335646	28	·52	·5572621	·671128	1·490028	·8303366	8
12	·5475632	·654381	1·528160	·8367643	48	·33	·5526645	·663141	1·507974	·8334038	27	·53	·5575036	·671550	1·489092	·8301745	7
13	·5478066	·654797	1·527190	·8366050	47	·34	·5529069	·663560	1·507022	·8332430	26	·54	·5577451	·671972	1·488157	·8300123	6
14	·5480499	·655212	1·526221	·8364456	46	·35	·5531492	·663979	1·506071	·8330822	25	·55	·5579865	·672394	1·487222	·8298500	5
15	·5482932	·655628	1·525253	·8362862	45	·36	·5533915	·664398	1·505121	·8329212	24	·56	·5582279	·672816	1·486288	·8296877	4
16	·5485365	·656044	1·524286	·8361266	44	·37	·5536338	·664817	1·504171	·8327602	23	·57	·5584692	·673239	1·485355	·8295252	3
17	·5487797	·656460	1·523320	·8359670	43	·38	·5538760	·665237	1·503222	·8325991	22	·58	·5587105	·673662	1·484423	·8293628	2
18	·5490228	·656877	1·522354	·8358074	42	·39	·5541182	·665657	1·502275	·8324380	21	·59	·5589517	·674085	1·483491	·8292002	1
19	·5492659	·657293	1·521389	·8356476	41	·40	·5543603	·666076	1·501328	·8322768	20	·60	·5591929	·674508	1·482561	·8290376	0
20	·5495090	·657710	1·520426	·8354878	40												
'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'		

Deg. 56.

Deg. 56.

Deg. 56.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

34 Deg.

34 Deg.

34 Deg.

'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'			
0	.5591929	.674508	1.482561	.8290376	60	.21	.5642467	.683433	1.463200	.8256062	.39	.41	.5690403	.692002	1.445081	.8223096	19	
1	.5594340	.674931	1.481631	.8288749	59	.22	.5644869	.683860	1.462287	.8254420	.38	.42	.5692795	.692432	1.444183	.8221440	18	
2	.5596751	.675355	1.480702	.8287121	58	.23	.5647270	.684287	1.461374	.8252778	.37	.43	.5695187	.692863	1.443286	.8219784	17	
3	.5599162	.675779	1.479773	.8285493	57	.24	.5649670	.684714	1.460463	.8251135	.36	.44	.5697577	.693293	1.442389	.8218127	16	
4	.5601572	.676202	1.478846	.8283864	56	.25	.5652070	.685141	1.459552	.8249491	.35	.45	.5699968	.693724	1.441494	.8216469	15	
5	.5603981	.676626	1.477919	.8282234	55	.26	.5654469	.685569	1.458642	.8247847	.34	.46	.5702357	.694155	1.440599	.8214811	14	
6	.5606390	.677050	1.476993	.8280603	54	.27	.5656868	.685996	1.457732	.8246202	.33	.47	.5704747	.694586	1.439704	.8213152	13	
7	.5608798	.677475	1.476068	.8278972	53	.28	.5659267	.686424	1.456824	.8244556	.32	.48	.5707136	.695018	1.438811	.8211492	12	
8	.5611206	.677899	1.475144	.8277340	52	.29	.5661665	.686852	1.455916	.8242909	.31	.49	.5709524	.695449	1.437918	.8209832	11	
9	.5613614	.678324	1.474221	.8275708	51	.30	.5664062	.687281	1.455009	.8241262	.30	.50	.5711912	.695881	1.437026	.8208170	10	
10	.5616021	.678749	1.473298	.8274074	50	.31	.5666459	.687709	1.454102	.8239614	.29	.51	.5714299	.696313	1.436135	.8206509	9	
11	.5618428	.679174	1.472376	.8272440	49	.32	.5668856	.688137	1.453197	.8237965	.28	.52	.5716686	.696745	1.435245	.8204846	8	
12	.5620834	.679599	1.471455	.8270806	48	.33	.5671252	.688566	1.452292	.8236316	.27	.53	.5719073	.697177	1.434355	.8203183	7	
13	.5623239	.680024	1.470535	.8269170	47	.34	.5673648	.688995	1.451388	.8234666	.26	.54	.5721459	.697609	1.433466	.8201519	6	
14	.5625645	.680450	1.469615	.8267534	46	.35	.5676043	.689424	1.450485	.8233015	.25	.55	.5723844	.698042	1.432578	.8199854	5	
15	.5628049	.680875	1.468696	.8265897	45	.36	.5678437	.689853	1.449582	.8231364	.24	.56	.5726229	.698474	1.431690	.8198189	4	
16	.5630453	.681301	1.467778	.8264260	44	.37	.5680832	.690283	1.448680	.8229712	.23	.57	.5728614	.698907	1.430803	.8196523	3	
17	.5632857	.681727	1.466861	.8262622	43	.38	.5683225	.690712	1.447779	.8228059	.22	.58	.5730998	.699340	1.429917	.8194856	2	
18	.5635260	.682153	1.465945	.8260983	42	.39	.5685619	.691142	1.446879	.8226405	.21	.59	.5733381	.699774	1.429032	.8193189	1	
19	.5637663	.682580	1.465029	.8259343	41	.40	.5688011	.691572	1.445980	.8224751	.20	.60	.5735764	.700207	1.428148	.8191520	0	
20	.5640066	.683006	1.464114	.8257703	40													
'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'			

Deg. 55

Deg. 55.

Deg. 55.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

35 Deg.

35 Deg.

35 Deg.

'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'		
0	.5735764	.700207	1.428148	.8191520	60	.21	.5785696	.709350	1.409740	.8156330	39	.41	.5833050	.718131	1.392501	.8122532	19
1	.5738147	.700641	1.427264	.8189852	59	.22	.5788069	.709787	1.408871	.8154647	38	.42	.5835412	.718572	1.391647	.8120835	18
2	.5740529	.701074	1.426381	.8188182	58	.23	.5790440	.710225	1.408003	.8152963	37	.43	.5837774	.719014	1.390793	.8119137	17
3	.5742911	.701508	1.425498	.8186512	57	.24	.5792812	.710663	1.407136	.8151278	36	.44	.5840136	.719455	1.389940	.8117439	16
4	.5745292	.701943	1.424617	.8184841	56	.25	.5795183	.711100	1.406270	.8149593	35	.45	.5842497	.719897	1.389087	.8115740	15
5	.5747672	.702377	1.423736	.8183169	55	.26	.5797553	.711539	1.405404	.8147906	34	.46	.5844857	.720338	1.388235	.8114040	14
6	.5750053	.702811	1.422856	.8181497	54	.27	.5799923	.711977	1.404539	.8146220	33	.47	.5847217	.720780	1.387384	.8112339	13
7	.5752432	.703246	1.421976	.8179824	53	.28	.5802292	.712415	1.403674	.8144532	32	.48	.5849577	.721222	1.386534	.8110638	12
8	.5754811	.703681	1.421097	.8178151	52	.29	.5804661	.712854	1.402811	.8142844	31	.49	.5851936	.721665	1.385684	.8108936	11
9	.5757190	.704116	1.420220	.8176476	51	.30	.5807030	.713293	1.401948	.8141155	30	.50	.5854294	.722107	1.384835	.8107234	10
10	.5759568	.704551	1.419342	.8174801	50	.31	.5809397	.713732	1.401086	.8139466	29	.51	.5856652	.722550	1.383986	.8105530	9
11	.5761946	.704986	1.418466	.8173125	49	.32	.5811765	.714171	1.400224	.8137775	28	.52	.5859010	.722993	1.383139	.8103826	8
12	.5764323	.705422	1.417590	.8171449	48	.33	.5814132	.714610	1.399363	.8136084	27	.53	.5861367	.723436	1.382292	.8102122	7
13	.5766700	.705858	1.416715	.8169772	47	.34	.5816498	.715050	1.398503	.8134393	26	.54	.5863724	.723879	1.381445	.8100416	6
14	.5769076	.706294	1.415840	.8168094	46	.35	.5818864	.715489	1.397644	.8132701	25	.55	.5866080	.724322	1.380600	.8098710	5
15	.5771452	.706730	1.414967	.8166416	45	.36	.5821230	.715929	1.396785	.8131008	24	.56	.5868435	.724766	1.379755	.8097004	4
16	.5773827	.707166	1.414094	.8164736	44	.37	.5823595	.716369	1.395927	.8129314	23	.57	.5870790	.725210	1.378910	.8095296	3
17	.5776202	.707602	1.413222	.8163056	43	.38	.5825959	.716810	1.395069	.8127620	22	.58	.5873145	.725654	1.378067	.8093588	2
18	.5778576	.708039	1.412350	.8161376	42	.39	.5828323	.717250	1.394213	.8125925	21	.59	.5875499	.726098	1.377224	.8091879	1
19	.5780950	.708476	1.411479	.8159695	41	.40	.5830687	.717691	1.393357	.8124229	20	.60	.5877853	.726542	1.376381	.8090170	0
20	.5783323	.708913	1.410609	.8158013	40												
'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'		

Deg. 54.

Deg. 54.

Deg. 54.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

36 Deg.

36 Deg.

36 Deg.

'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'		
0	.5877853	.726542	1.376381	.8090170	60	.21	.5927163	.735917	1.358848	.8054113	39	.41	.5973919	.744924	1.342417	.8019495	19
1	.5880206	.726987	1.375540	.8088460	59	.22	.5929505	.736366	1.358020	.8052389	38	.42	.5976251	.745377	1.341602	.8017756	18
2	.5882558	.727431	1.374699	.8086749	58	.23	.5931847	.736814	1.357193	.8050664	37	.43	.5978583	.745829	1.340788	.8016018	17
3	.5884910	.727876	1.373859	.8085037	57	.24	.5934189	.737263	1.356367	.8048938	36	.44	.5980915	.746282	1.339975	.8014278	16
4	.5887262	.728321	1.373019	.8083325	56	.25	.5936530	.737712	1.355541	.8047211	35	.45	.5983246	.746735	1.339162	.8012538	15
5	.5889613	.728767	1.372180	.8081612	55	.26	.5938871	.738162	1.354716	.8045484	34	.46	.5985577	.747188	1.338350	.8010797	14
6	.5891964	.729212	1.371342	.8079899	54	.27	.5941211	.738611	1.353891	.8043756	33	.47	.5987906	.747642	1.337538	.8009056	13
7	.5894314	.729658	1.370504	.8078185	53	.28	.5943550	.739061	1.353068	.8042028	32	.48	.5990236	.748095	1.336727	.8007314	12
8	.5896663	.730104	1.369667	.8076470	52	.29	.5945889	.739511	1.352244	.8040299	31	.49	.5992565	.748549	1.335917	.8005571	11
9	.5899012	.730550	1.368831	.8074754	51	.30	.5948228	.739961	1.351422	.8038569	30	.50	.5994893	.749003	1.335107	.8003827	10
10	.5901361	.730996	1.367995	.8073038	50	.31	.5950566	.740411	1.350600	.8036838	29	.51	.5997221	.749457	1.334298	.8002083	9
11	.5903709	.731442	1.367161	.8071321	49	.32	.5952904	.740861	1.349779	.8035107	28	.52	.5999549	.749911	1.333490	.8000338	8
12	.5906057	.731889	1.366326	.8069603	48	.33	.5955241	.741312	1.348958	.8033375	27	.53	.6001876	.750366	1.332682	.7998593	7
13	.5908404	.732336	1.365493	.8067885	47	.34	.5957577	.741763	1.348139	.8031642	26	.54	.6004202	.750821	1.331875	.7996847	6
14	.5910750	.732783	1.364660	.8066166	46	.35	.5959913	.742214	1.347319	.8029909	25	.55	.6006528	.751276	1.331068	.7995100	5
15	.5913096	.733230	1.363827	.8064446	45	.36	.5962249	.742665	1.346501	.8028175	24	.56	.6008854	.751731	1.330262	.7993352	4
16	.5915442	.733677	1.362996	.8062726	44	.37	.5964584	.743117	1.345683	.8026440	23	.57	.6011179	.752186	1.329457	.7991604	3
17	.5917787	.734125	1.362165	.8061005	43	.38	.5966918	.743568	1.344865	.8024705	22	.58	.6013503	.752642	1.328652	.7989855	2
18	.5920132	.734573	1.361335	.8059283	42	.39	.5969252	.744020	1.344049	.8022969	21	.59	.6015827	.753098	1.327848	.7988105	1
19	.5922476	.735021	1.360505	.8057560	41	.40	.5971586	.744472	1.343233	.8021232	20	.60	.6018150	.753554	1.327044	.7986355	0
20	.5924819	.735469	1.359676	.8055837	40												
'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'		

Deg. 53.

Deg. 53.

Deg. 53.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

37 Deg. 37 Deg.

37 Deg.	Sine.	Tang.	Cotang.	Cosine.	'	''	Sine.	Tang.	Cotang.	Cosine.	'	''	Tang.	Cotang.	Cosine.	'
0	.6018150	.753554	1.327044	.7986355	60	21	.6066824	.763175	1.310314	.7949444	39	41	.772423	1.294627	.7914014	19
1	.6020473	.754010	1.326242	.7984604	59	22	.6089136	.763636	1.309523	.7947678	38	42	.772887	1.293948	.7912235	18
2	.6022795	.754466	1.325439	.7982853	58	23	.6071447	.764096	1.308731	.7945913	37	43	.773352	1.293071	.7910456	17
3	.6025117	.754923	1.324638	.7981100	57	24	.6073758	.764557	1.307945	.7944146	36	44	.773817	1.292294	.7908676	16
4	.6027439	.755379	1.323837	.7979347	56	25	.6076069	.765018	1.307157	.7942379	35	45	.774282	1.291517	.7906896	15
5	.6029760	.755836	1.323036	.7977594	55	26	.6078379	.765480	1.306369	.7940611	34	46	.774748	1.290742	.7905115	14
6	.6032080	.756294	1.322237	.7975839	54	27	.6080689	.765941	1.305582	.7938843	33	47	.775213	1.289966	.7903333	13
7	.6034400	.756751	1.321437	.7974084	53	28	.6082998	.766403	1.304796	.7937074	32	48	.775679	1.289192	.7901550	12
8	.6036719	.757209	1.320639	.7972329	52	29	.6085306	.766864	1.304010	.7935304	31	49	.776145	1.288418	.7899767	11
9	.6039038	.757666	1.319841	.7970572	51	30	.6087614	.767327	1.303225	.7933533	30	50	.776611	1.287644	.7897983	10
10	.6041356	.758124	1.319044	.7968815	50	31	.6089922	.767789	1.302440	.7931762	29	51	.777078	1.286871	.7896198	9
11	.6043674	.758582	1.318247	.7967058	49	32	.6092229	.768251	1.301656	.7929990	28	52	.777544	1.286099	.7894413	8
12	.6045991	.759041	1.317451	.7965299	48	33	.6094535	.768714	1.300873	.7928218	27	53	.778011	1.285327	.7892627	7
13	.6048308	.759499	1.316655	.7963540	47	34	.6096841	.769177	1.300090	.7926445	26	54	.778478	1.284556	.7890841	6
14	.6050624	.759958	1.315861	.7961780	46	35	.6099147	.769640	1.299308	.7924671	25	55	.778946	1.283786	.7889054	5
15	.6052940	.760417	1.315066	.7960020	45	36	.6101452	.770103	1.298526	.7922896	24	56	.779413	1.283016	.7887266	4
16	.6055255	.760876	1.314273	.7958259	44	37	.6103756	.770567	1.297745	.7921121	23	57	.779881	1.282246	.7885477	3
17	.6057570	.761336	1.313480	.7956497	43	38	.6106060	.771030	1.296964	.7919345	22	58	.780349	1.281477	.7883688	2
18	.6059884	.761795	1.312687	.7954735	42	39	.6108363	.771494	1.296185	.7917569	21	59	.780817	1.280709	.7881898	1
19	.6062198	.762255	1.311895	.7952972	41	40	.6110666	.771958	1.295405	.7915792	20	60	.781285	1.279941	.7880108	0
20	.6064511	.762715	1.311104	.7951208	40											

Deg. 52.

Deg. 52.

Deg. 52.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

38 Deg.

38 Deg.

38 Deg.

'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'		
0	.6156615	.781285	1.279941	.7880108	60	.21	.6204636	.791170	1.263950	.7842352	39	.41	.6250156	.800673	1.248948	.7806123	19
1	.6158907	.781754	1.279174	.7878316	59	.22	.6206917	.791643	1.263195	.7840547	38	.42	.6252427	.801151	1.248204	.7804304	18
2	.6161198	.782222	1.278407	.7876524	58	.23	.6209198	.792116	1.262440	.7838741	37	.43	.6254696	.801628	1.247460	.7802485	17
3	.6163489	.782691	1.277641	.7874732	57	.24	.6211478	.792590	1.261686	.7836935	36	.44	.6256966	.802106	1.246716	.7800665	16
4	.6165780	.783161	1.276876	.7872939	56	.25	.6213757	.793064	1.260932	.7835127	35	.45	.6259235	.802584	1.245974	.7798845	15
5	.6168069	.783630	1.276111	.7871145	55	.26	.6216036	.793537	1.260179	.7833320	34	.46	.6261503	.803063	1.245232	.7797021	14
6	.6170359	.784100	1.275347	.7869350	54	.27	.6218314	.794012	1.259426	.7831511	33	.47	.6263771	.803541	1.244490	.7795202	13
7	.6172648	.784570	1.274583	.7867555	53	.28	.6220592	.794486	1.258674	.7829702	32	.48	.6266038	.804020	1.243749	.7793380	12
8	.6174936	.785040	1.273820	.7865759	52	.29	.6222870	.794961	1.257923	.7827892	31	.49	.6268305	.804499	1.243008	.7791557	11
9	.6177224	.785510	1.273057	.7863963	51	.30	.6225146	.795435	1.257172	.7826082	30	.50	.6270571	.804979	1.242268	.7789733	10
10	.6179511	.785980	1.272295	.7862165	50	.31	.6227423	.795911	1.256421	.7824270	29	.51	.6272837	.805458	1.241529	.7787909	9
11	.6181798	.786451	1.271534	.7860367	49	.32	.6229698	.796386	1.255672	.7822459	28	.52	.6275102	.805938	1.240790	.7786084	8
12	.6184084	.786922	1.270773	.7858569	48	.33	.6231974	.796861	1.254922	.7820646	27	.53	.6277366	.806418	1.240051	.7784258	7
13	.6186370	.787393	1.270013	.7856770	47	.34	.6234248	.797337	1.254174	.7818833	26	.54	.6279631	.806898	1.239313	.7782431	6
14	.6188655	.787864	1.269253	.7854970	46	.35	.6236522	.797813	1.253426	.7817019	25	.55	.6281894	.807378	1.238576	.7780604	5
15	.6190939	.788336	1.268494	.7853169	45	.36	.6238796	.798289	1.252678	.7815205	24	.56	.6284157	.807859	1.237839	.7778777	4
16	.6193224	.788808	1.267735	.7851368	44	.37	.6241069	.798765	1.251931	.7813390	23	.57	.6286420	.808340	1.237103	.7776949	3
17	.6195507	.789280	1.266977	.7849566	43	.38	.6243342	.799242	1.251184	.7811574	22	.58	.6288682	.808821	1.236367	.7775120	2
18	.6197790	.789752	1.266219	.7847764	42	.39	.6245614	.799719	1.250438	.7809757	21	.59	.6290943	.809302	1.235631	.7773290	1
19	.6200073	.790224	1.265462	.7845961	41	.40	.6247885	.800196	1.249693	.7807940	20	.60	.6293204	.809784	1.234897	.7771460	0
20	.6202355	.790697	1.264706	.7844157	40												

Deg. 51.

Deg. 51.

Deg. 51.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

39 Deg.

39 Deg.

39 Deg.

°	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'		
0	.6293204	.809784	1.2334897	.7771460	60	.21	.6340559	.819948	1.219588	.7732872	39	.41	.6385440	.829724	1.205219	.7695853	19
1	.6295464	.810265	1.234162	.7769629	59	.22	.6342808	.820435	1.218865	.7731027	38	.42	.6387678	.830216	1.204505	.7693996	18
2	.6297724	.810747	1.233429	.7767797	58	.23	.6345057	.820922	1.218142	.7729182	37	.43	.6389916	.830707	1.203793	.7692137	17
3	.6299983	.811230	1.232696	.7765965	57	.24	.6347305	.821409	1.217419	.7727336	36	.44	.6392153	.831199	1.203081	.7690278	16
4	.6302242	.811712	1.231963	.7764132	56	.25	.6349553	.821896	1.216698	.7725489	35	.45	.6394390	.831691	1.202369	.7688418	15
5	.6304500	.812195	1.231231	.7762298	55	.26	.6351800	.822384	1.215976	.7723642	34	.46	.6396626	.832183	1.201658	.7686558	14
6	.6306758	.812678	1.230499	.7760464	54	.27	.6354046	.822871	1.215256	.7721794	33	.47	.6398862	.832675	1.200947	.7684697	13
7	.6309015	.813161	1.229768	.7758629	53	.28	.6356292	.823359	1.214535	.7719945	32	.48	.6401097	.833168	1.200237	.7682835	12
8	.6311272	.813644	1.229038	.7756794	52	.29	.6358537	.823847	1.213816	.7718096	31	.49	.6403332	.833661	1.199527	.7680973	11
9	.6313528	.814128	1.228308	.7754957	51	.30	.6360782	.824336	1.213097	.7716246	30	.50	.6405566	.834154	1.198818	.7679110	10
10	.6315784	.814611	1.227578	.7753121	50	.31	.6363026	.824825	1.212378	.7714395	29	.51	.6407799	.834648	1.198109	.7677246	9
11	.6318039	.815095	1.226849	.7751283	49	.32	.6365270	.825314	1.211660	.7712544	28	.52	.6410032	.835141	1.197401	.7675382	8
12	.6320293	.815580	1.226121	.7749445	48	.33	.6367513	.825803	1.210942	.7710692	27	.53	.6412264	.835635	1.196693	.7673517	7
13	.6322547	.816064	1.225393	.7747606	47	.34	.6369756	.826292	1.210225	.7708840	26	.54	.6414496	.836129	1.195986	.7671652	6
14	.6324800	.816549	1.224665	.7745767	46	.35	.6371998	.826782	1.209508	.7706986	25	.55	.6416728	.836624	1.195279	.7669785	5
15	.6327053	.817034	1.223938	.7743926	45	.36	.6374240	.827271	1.208792	.7705132	24	.56	.6418958	.837118	1.194573	.7667918	4
16	.6329306	.817519	1.223212	.7742086	44	.37	.6376481	.827762	1.208076	.7703278	23	.57	.6421189	.837613	1.193867	.7666051	3
17	.6331557	.818004	1.222486	.7740244	43	.38	.6378721	.828252	1.207361	.7701423	22	.58	.6423418	.838108	1.193162	.7664183	2
18	.6333809	.818490	1.221761	.7738402	42	.39	.6380961	.828742	1.206646	.7699567	21	.59	.6425647	.838604	1.192457	.7662314	1
19	.6336059	.818976	1.221036	.7736559	41	.40	.6383201	.829233	1.205932	.7697710	20	.60	.6427876	.839099	1.191753	.7660444	0
20	.6338310	.819462	1.220312	.7734716	40												
°	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'		

Deg. 50.

Deg. 50.

Deg. 50.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

40 Deg.				40 Deg.													
Sine.	Tang.	Cotang.	Cosine.	/	Sine.	Tang.	Cotang.	Cosine.	/	Sine.	Tang.	Cotang.	Cosine.	/			
0	.6427876	.839099	1.191753	.7660444	60	21	.6474551	.849563	1.177075	.7621036	39	41	.6518778	.859629	1.163291	.7583240	19
1	.6430104	.839595	1.191049	.7658574	59	22	.6476767	.850064	1.176382	.7619152	38	42	.6520984	.860135	1.162607	.7581343	18
2	.6432332	.840091	1.190346	.7656704	58	23	.6478984	.850565	1.175688	.7617268	37	43	.6523189	.860641	1.161923	.7579446	17
3	.6434559	.840587	1.189643	.7654832	57	24	.6481199	.851066	1.174996	.7615383	36	44	.6525394	.861148	1.161240	.7577548	16
4	.6436785	.841084	1.188941	.7652960	56	25	.6483414	.851568	1.174303	.7613497	35	45	.6527598	.861655	1.160557	.7575650	15
5	.6439011	.841581	1.188239	.7651087	55	26	.6485628	.852070	1.173612	.7611611	34	46	.6529801	.862162	1.159874	.7573751	14
6	.6441236	.842078	1.187538	.7649214	54	27	.6487842	.852572	1.172920	.7609724	33	47	.6532004	.862669	1.159192	.7571851	13
7	.6443461	.842575	1.186837	.7647340	53	28	.6490056	.853075	1.172229	.7607837	32	48	.6534206	.863176	1.158511	.7569951	12
8	.6445685	.843073	1.186136	.7645465	52	29	.6492268	.853577	1.171539	.7605949	31	49	.6536408	.863684	1.157830	.7568050	11
9	.6447909	.843570	1.185437	.7643590	51	30	.6494480	.854080	1.170849	.7604060	30	50	.6538609	.864192	1.157149	.7566148	10
10	.6450132	.844068	1.184737	.7641714	50	31	.6496692	.854583	1.170160	.7602170	29	51	.6540810	.864700	1.156469	.7564246	9
11	.6452355	.844567	1.184038	.7639838	49	32	.6498903	.855087	1.169471	.7600280	28	52	.6543010	.865209	1.155789	.7562343	8
12	.6454577	.845065	1.183340	.7637960	48	33	.6501114	.855591	1.168782	.7598389	27	53	.6545209	.865718	1.155110	.7560439	7
13	.6456798	.845564	1.182642	.7636082	47	34	.6503324	.856095	1.168094	.7596498	26	54	.6547408	.866227	1.154431	.7558535	6
14	.6459019	.846063	1.181944	.7634204	46	35	.6505533	.856599	1.167407	.7594606	25	55	.6549607	.866736	1.153753	.7556630	5
15	.6461240	.846562	1.181247	.7632325	45	36	.6507742	.857103	1.166720	.7592713	24	56	.6551804	.867246	1.153075	.7554724	4
16	.6463460	.847062	1.180551	.7630445	44	37	.6509951	.857608	1.166033	.7590820	23	57	.6554002	.867755	1.152397	.7552818	3
17	.6465679	.847561	1.179855	.7628564	43	38	.6512158	.858113	1.165347	.7588926	22	58	.6556198	.868265	1.151721	.7550911	2
18	.6467898	.848061	1.179159	.7626683	42	39	.6514366	.858618	1.164661	.7587031	21	59	.6558395	.868776	1.151044	.7549004	1
19	.6470116	.848561	1.178464	.7624802	41	40	.6516572	.859124	1.163976	.7585136	20	60	.6560590	.869286	1.150368	.7547096	0
20	.6472334	.849062	1.177769	.7622919	40												
Cosine.	Cotang.	Tang.	Cotang.	Sine.	/	Cosine.	Tang.	Cotang.	Sine.	/	Cosine.	Cotang.	Sine.	/			

Deg. 49.

Deg. 49.

Deg. 49.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

41 Deg.

41 Deg.

41 Deg.

'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'		
0	.6560590	.869286	1.150368	.7547096	60	21	.6606570	.880068	1.136274	.7506879	39	41	.6650131	.890445	1.123032	.7468317	19
1	.6562785	.869797	1.149692	.7545187	59	22	.6608754	.880585	1.135608	.7504957	38	42	.6652304	.890967	1.122375	.7466382	18
2	.6564980	.870308	1.149017	.7543278	58	23	.6610936	.881101	1.134942	.7503034	37	43	.6654475	.891489	1.121718	.7464446	17
3	.6567174	.870820	1.148342	.7541368	57	24	.6613119	.881618	1.134277	.7501111	36	44	.6656646	.892011	1.121061	.7462510	16
4	.6569367	.871331	1.147668	.7539457	56	25	.6615300	.882135	1.133612	.7499187	35	45	.6658817	.892534	1.120405	.7460574	15
5	.6571560	.871843	1.146994	.7537546	55	26	.6617482	.882653	1.132947	.7497262	34	46	.6660987	.893056	1.119749	.7458636	14
6	.6573752	.872355	1.146321	.7535634	54	27	.6619662	.883170	1.132283	.7495337	33	47	.6663156	.893579	1.119094	.7456699	13
7	.6575944	.872868	1.145648	.7533721	53	28	.6621842	.883688	1.131620	.7493411	32	48	.6665325	.894103	1.118439	.7454760	12
8	.6578135	.873380	1.144976	.7531808	52	29	.6624022	.884206	1.130957	.7491484	31	49	.6667493	.894626	1.117784	.7452821	11
9	.6580326	.873893	1.144304	.7529894	51	30	.6626200	.884725	1.130294	.7489557	30	50	.6669661	.895150	1.117130	.7450881	10
10	.6582516	.874406	1.143632	.7527980	50	31	.6628379	.885244	1.129632	.7487629	29	51	.6671828	.895674	1.116476	.7448941	9
11	.6584706	.874920	1.142961	.7526065	49	32	.6630557	.885763	1.128970	.7485701	28	52	.6673994	.896199	1.115823	.7446999	8
12	.6586895	.875433	1.142290	.7524149	48	33	.6632734	.886282	1.128308	.7483772	27	53	.6676160	.896723	1.115170	.7445058	7
13	.6589083	.875947	1.141620	.7522233	47	34	.6634910	.886801	1.127647	.7481842	26	54	.6678326	.897248	1.114518	.7443115	6
14	.6591271	.876462	1.140950	.7520316	46	35	.6637087	.887321	1.126987	.7479912	25	55	.6680490	.897773	1.113866	.7441173	5
15	.6593458	.876976	1.140281	.7518398	45	36	.6639262	.887841	1.126327	.7477981	24	56	.6682655	.898299	1.113214	.7439229	4
16	.6595645	.877491	1.139612	.7516480	44	37	.6641437	.888361	1.125667	.7476049	23	57	.6684818	.898825	1.112563	.7437285	3
17	.6597831	.878006	1.138944	.7514561	43	38	.6643612	.888882	1.125008	.7474117	22	58	.6686981	.899351	1.111912	.7435340	2
18	.6600017	.878521	1.138276	.7512641	42	39	.6645785	.889403	1.124349	.7472184	21	59	.6689144	.899877	1.111262	.7433394	1
19	.6602202	.879037	1.137608	.7510721	41	40	.6647959	.889924	1.123690	.7470251	20	60	.6691306	.900404	1.110612	.7431448	0
20	.6604386	.879552	1.136941	.7508800	40												
'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'		

Deg. 48.

Deg. 48.

Deg. 48.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

42 Deg.

42 Deg.

42 Deg.

°	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'			
0	.6691306	.900404	1.110612	.7431448	60	.21	.6736577	.911526	1.097060	.7390435	39	.41	.6779459	.922235	1.084322	.7351118	19	
1	.6693468	.900930	1.109963	.7429502	59	.22	.6738727	.912059	1.096420	.7388475	38	.42	.6781597	.922773	1.083689	.7349146	18	
2	.6695628	.901458	1.109314	.7427554	58	.23	.6740876	.912592	1.095779	.7386515	37	.43	.6783734	.923312	1.083057	.7347173	17	
3	.6697789	.901985	1.108665	.7425606	57	.24	.6743024	.913125	1.095139	.7384553	36	.44	.6785871	.923851	1.082425	.7345199	16	
4	.6699948	.902513	1.108017	.7423658	56	.25	.6745172	.913659	1.094500	.7382592	35	.45	.6788007	.924390	1.081793	.7343225	15	
5	.6702108	.903041	1.107369	.7421708	55	.26	.6747319	.914192	1.093861	.7380629	34	.46	.6790143	.924930	1.081162	.7341250	14	
6	.6704266	.903569	1.106721	.7419758	54	.27	.6749466	.914727	1.093222	.7378666	33	.47	.6792278	.925470	1.080532	.7339275	13	
7	.6706424	.904097	1.106075	.7417808	53	.28	.6751612	.915261	1.092584	.7376703	32	.48	.6794413	.926010	1.079901	.7337299	12	
8	.6708582	.904626	1.105428	.7415857	52	.29	.6753757	.915796	1.091946	.7374738	31	.49	.6796547	.926550	1.079271	.7335322	11	
9	.6710739	.905155	1.104782	.7413905	51	.30	.6755902	.916331	1.091308	.7372773	30	.50	.6798681	.927091	1.078642	.7333345	10	
10	.6712895	.905685	1.104136	.7411953	50	.31	.6758046	.916866	1.090671	.7370808	29	.51	.6800813	.927632	1.078013	.7331367	9	
11	.6715051	.906214	1.103491	.7410000	49	.32	.6760190	.917402	1.090034	.7368842	28	.52	.6802946	.928173	1.077384	.7329388	8	
12	.6717206	.906744	1.102846	.7408046	48	.33	.6762333	.917937	1.089398	.7366875	27	.53	.6805078	.928715	1.076756	.7327409	7	
13	.6719361	.907274	1.102201	.7406092	47	.34	.6764476	.918474	1.088762	.7364908	26	.54	.6807209	.929257	1.076128	.7325429	6	
14	.6721515	.907805	1.101557	.7404137	46	.35	.6766618	.919010	1.088126	.7362940	25	.55	.6809339	.929799	1.075500	.7323449	5	
15	.6723668	.908336	1.100914	.7402181	45	.36	.6768760	.919547	1.087491	.7360971	24	.56	.6811469	.930342	1.074873	.7321467	4	
16	.6725821	.908867	1.100270	.7400225	44	.37	.6770901	.920084	1.086857	.7359002	23	.57	.6813599	.930884	1.074246	.7319486	3	
17	.6727973	.909398	1.099628	.7398268	43	.38	.6773041	.920621	1.086222	.7357032	22	.58	.6815728	.931428	1.073620	.7317503	2	
18	.6730125	.909930	1.098985	.7396311	42	.39	.6775181	.921159	1.085588	.7355061	21	.59	.6817856	.931971	1.072994	.7315521	1	
19	.6732276	.910461	1.098343	.7394353	41	.40	.6777320	.921696	1.084955	.7353090	20	.60	.6819984	.932515	1.072368	.7313537	0	
20	.6734427	.910994	1.097702	.7392394	40													

Deg. 47.

Deg. 47.

Deg. 47.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

43 Deg.

43 Deg.

43 Deg.

°	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	
0	.6819984	.932515	1.072368	.7313537	60	.21	.6864532	.944001	1.059320	.7271740	39	.41	.6906721	1.047049	.7231681	19
1	.6822111	.933059	1.071743	.7311553	59	.22	.6866647	.944551	1.058703	.7269743	38	.42	.6908824	1.046440	.7229671	18
2	.6824237	.933603	1.071118	.7309568	58	.23	.6868761	.945102	1.058086	.7267745	37	.43	.6910927	1.045831	.7227661	17
3	.6826363	.934147	1.070494	.7307583	57	.24	.6870875	.945653	1.057470	.7265747	36	.44	.6913029	1.045222	.7225651	16
4	.6828489	.934692	1.069870	.7305597	56	.25	.6872988	.946204	1.056854	.7263748	35	.45	.6915131	1.044613	.7223640	15
5	.6830613	.935238	1.069246	.7303610	55	.26	.6875101	.946755	1.056238	.7261748	34	.46	.6917232	1.044005	.7221628	14
6	.6832738	.935783	1.068623	.7301623	54	.27	.6877213	.947307	1.055623	.7259748	33	.47	.6919332	1.043397	.7219615	13
7	.6834861	.936329	1.068000	.7299635	53	.28	.6879325	.947859	1.055008	.7257747	32	.48	.6921432	1.042790	.7217602	12
8	.6836984	.936875	1.067377	.7297646	52	.29	.6881435	.948411	1.054394	.7255746	31	.49	.6923531	1.042183	.7215589	11
9	.6839107	.937421	1.066755	.7295657	51	.30	.6883546	.948964	1.053780	.7253744	30	.50	.6925630	1.041576	.7213574	10
10	.6841229	.937968	1.066134	.7293668	50	.31	.6885655	.949517	1.053166	.7251741	29	.51	.6927728	1.040970	.7211559	9
11	.6843350	.938515	1.065512	.7291677	49	.32	.6887765	.950070	1.052553	.7249738	28	.52	.6929825	1.040364	.7209544	8
12	.6845471	.939062	1.064891	.7289686	48	.33	.6889873	.950624	1.051940	.7247734	27	.53	.6931922	1.039758	.7207528	7
13	.6847591	.939610	1.064271	.7287695	47	.34	.6891981	.951178	1.051327	.7245729	26	.54	.6934018	1.039153	.7205511	6
14	.6849711	.940157	1.063651	.7285703	46	.35	.6894089	.951732	1.050715	.7243724	25	.55	.6936114	1.038548	.7203494	5
15	.6851830	.940706	1.063031	.7283710	45	.36	.6896195	.952287	1.050103	.7241719	24	.56	.6938209	1.037944	.7201476	4
16	.6853948	.941254	1.062411	.7281716	44	.37	.6898302	.952842	1.049492	.7239712	23	.57	.6940304	1.037340	.7199457	3
17	.6856066	.941803	1.061792	.7279722	43	.38	.6900407	.953397	1.048880	.7237705	22	.58	.6942398	1.036736	.7197438	2
18	.6858184	.942352	1.061174	.7277728	42	.39	.6902512	.953952	1.048270	.7235698	21	.59	.6944491	1.036133	.7195418	1
19	.6860300	.942901	1.060556	.7275732	41	.40	.6904617	.954508	1.047659	.7233690	20	.60	.6946584	1.035530	.7193398	0
20	.6862416	.943451	1.059938	.7273736	40											

Deg. 46.

Deg. 46.

Deg. 46.

NATURAL SINES AND TANGENTS TO A RADIUS 1.

44 Deg.

44 Deg.

44 Deg.

'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'	Sine.	Tang.	Cotang.	Cosine.	'
0	.6946584	.965688	1.035530	.7193398	60	.216990396	.977564	1.022950	.7150830	39	.417031879	.989006	1.011115	.7110041	19
1	.6948676	.966251	1.034927	.7191377	59	.226992476	.978133	1.022355	.7148796	38	.427033947	.989582	1.010527	.7107995	18
2	.6950767	.966813	1.034325	.7189355	58	.236994555	.978702	1.021760	.7146762	37	.437036014	.990158	1.009939	.7105948	17
3	.6952858	.967376	1.033723	.7187333	57	.246996633	.979272	1.021166	.7144727	36	.447038081	.990734	1.009352	.7103901	16
4	.6954949	.967939	1.033122	.7185310	56	.256998711	.979842	1.020572	.7142691	35	.457040147	.991311	1.008764	.7101854	15
5	.6957039	.968503	1.032520	.7183287	55	.267000789	.980412	1.019978	.7140655	34	.467042213	.991888	1.008178	.7099806	14
6	.6959128	.969067	1.031919	.7181263	54	.277002866	.980983	1.019385	.7138618	33	.477044278	.992465	1.007591	.7097757	13
7	.6961217	.969631	1.031319	.7179238	53	.287004942	.981554	1.018792	.7136581	32	.487046342	.993042	1.007005	.7095707	12
8	.6963305	.970196	1.030719	.7177213	52	.297007018	.982125	1.018199	.7134543	31	.497048406	.993620	1.006420	.7093657	11
9	.6965392	.970761	1.030119	.7175187	51	.307009093	.982697	1.017607	.7132504	30	.507050469	.994199	1.005834	.7091607	10
10	.6967479	.971326	1.029520	.7173161	50	.317011167	.983269	1.017015	.7130465	29	.517052532	.994777	1.005249	.7089556	9
11	.6969565	.971891	1.028921	.7171134	49	.327013241	.983841	1.016423	.7128426	28	.527054594	.995356	1.004665	.7087504	8
12	.6971651	.972457	1.028322	.7169106	48	.337015314	.984414	1.015832	.7126385	27	.537056655	.995935	1.004080	.7085451	7
13	.6973736	.973023	1.027724	.7167078	47	.347017387	.984987	1.015241	.7124344	26	.547058716	.996515	1.003496	.7083398	6
14	.6975821	.973590	1.027126	.7165049	46	.357019459	.985560	1.014651	.7122303	25	.557060776	.997095	1.002913	.7081345	5
15	.6977905	.974156	1.026528	.7163019	45	.367021531	.986133	1.014061	.7120262	24	.567062835	.997675	1.002329	.7079291	4
16	.6979988	.974724	1.025931	.7160989	44	.377023601	.986707	1.013471	.7118218	23	.577064894	.998256	1.001746	.7077236	3
17	.6982071	.975291	1.025334	.7158959	43	.387025672	.987282	1.012881	.7116174	22	.587066953	.998837	1.001164	.7075180	2
18	.6984153	.975859	1.024738	.7156927	42	.397027741	.987856	1.012292	.7114130	21	.597069011	.999418	1.000581	.7073124	1
19	.6986234	.976427	1.024141	.7154895	41	.407029811	.988431	1.011703	.7112086	20	.607071068	1.000000	1.000000	.7071068	0
20	.6988315	.976995	1.023546	.7152863	40										
'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'	Cosine.	Cotang.	Tang.	Sine.	'

Deg. 45.

Deg. 45.

Deg. 45.





THIS BOOK IS DUE ON THE LAST DATE
STAMPED BELOW

AN INITIAL FINE OF 25 CENTS
WILL BE ASSESSED FOR FAILURE TO RETURN
THIS BOOK ON THE DATE DUE. THE PENALTY
WILL INCREASE TO 50 CENTS ON THE FOURTH
DAY AND TO \$1.00 ON THE SEVENTH DAY
OVERDUE.

NOV 16 1937
" 30 - 1937
12-14-37

MAY 28 1941

AUG 23 1977

JAN 27 1978

JUL 26 1978

JAN 27 1979

REC. CIR. AUG 2 '78

YB 10873

TF216

T7

66958

