

Florian Capor

Fram Charles Tweedie, rdinhurgh, Scotland, James gray died in 1810, but his work lived all the rough the 19th century, be in use in every parish school in cotland about 1860.00 remembered with enteriasus by my old man of 20 and ever, to whom I have men firmed it. It is still in use in out of the way corners; and b.might I recai from Her. This of Clives & Boyd the publishers, two copies fresh from Tweeddale Court, of the 101 st. edition Que of these I am sending taking the liberty of rending you as a enviority. This dells we the firm must have sold 500,000 copes? t. I trunk this beats Cocher gray was a schoolmaster in Peebles & gave the elementary instruction to Whit + Kak. Chambers, the founders of the well du sure

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GRAY'S ARITHMETIC.

publication of firm, but athervise next to nothing is known about him. If I can arrange that I ave gathered about him is a orm for publication I hope to But Spear I shall not be able to do much more serious work From Tweedie's ulter, Sec. 14, 192

Morian Ca

AN

INTRODUCTION

ARITHMETIC.

E Y JAMES GRAY, Late of Peobles and Lundee

WITH TABLES AND EXERCISES ON DECIMAL COINAGE · AND THE METRIC SYSTEM.

One Hundred and First Edition.

EDINBURGH:

OLIVER AND BOYD, TWEEDDALE COURT.

LONDON: SIMPKIN, MARSHALL, HAMILTON, KENT, AND CO., LIM.

Q AIOI G78 1890

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918323



SIGNS USED IN ARITHMETIC.

- + Plus, the sign of Addition.
- Minus, the sign of Subtraction.
- o The sign of the difference when it is not known which is the greater.

- × The sign of Multiplication.
 ∴ The sign of Division.
 : :: : The sign of Proportion.
 ✓ or ²⁄ The sign of the Square Root.
 ³⁄ The sign of the Cube Root.
 ⁴⁄ The sign of the Fourth Root.

ARITHMETICAL TABLES.

NUMERATION TABLE.

Old Style.	 A C M Billions A Billions A Billions A Billions Billions C Billions S C Billions S C Billions S Millions S M Millions S M Millions S M Millions S M Millions S Thousands S Tens Units 	
New Style.	A C Quadrillions Real of the second state of t	

ADDITION TABLE.

	1	2	3	4	5	6	7	8	9
1	2	3	4	5	6	7	8	9	10
2	3	4	5	6	7	8	9	10	11
3	4	5	6	7	8	9	10	11	12
4	5	6	7	8	9	10	11	12	13
5	6	7	8	9	10	11	12	13	14
6	7	8	9	10	11	12	13	14	15
7	8	9	10	11	12	13	14	15	16
8	9	10	11	12	13	14	15	16	17
9	10	11	12	13	14	15	16	17	18

SUBTRACTION TABLE.

	1	2	3	4	5	6	7	8	9	10
1	0	1	2	3	4	5	6	7	8	9
2	-	0	1	2	3	4	5	6	7	8
3	-		0	1	2	3	4	5	6	7
4	-		-	0	1	2	3	4	5	6
5	-				0	1	2	3	4	5
6				-	-	0	1	2	3	4
7	18 au	-	-				0	1	2	3
8		-		-		-	-	0	1	2
9	~	-	-	-			-	-	0	1
10	-	-	-	-	818				-	0

	2	3	4	5	6	7	8	9	10	11	12
2	4	6	8	10	12	14	16	18	20	22	24
3	6	9	12	15	18	21	24	27	30	33	36
4	8	12	16	20	24	28	32	36	40	44	48
5	10	15	20	25	30	35	40	45	50	55	60
6	12	18	24	30	36	42	48	54	60	66	72
7	14	21	28	35	42	49	56	63	70	77	84
8	16	24	32	40	48	56	64	72	80	38	96
9	18	27	36	45	54	63	72	81	90	99	108
10	20	30	40	50	60	70	80	.90	100	110	120
11	22	33	44	55	66	77	88	99	110	121	132
12	24	36	48	60	72	84	96	108	120	132	144

MULTIPLICATION TABLE.

DIVISION TABLE.

12	12	24	36	48	60	72	84	96	108
11	11	22	33	44	55	66	77	88	99
10	10	20	30	40	50	60	70	80	90
9	9	18	27	36	45	54	63	72	81
8	8	16	24	32	40	48	56	64	72
7	7.	14	21	28	35	42	49	56	63
6	6	12	18	24	30	36	42	48	54
5	5	10	15	20	25	30	35	40	45
4	4	8	12	16	20	24	28	32	36
3	3	6	9	12	15	18	21	24	27
. 2	2	4	6	8	10	12	14	16	18
1	1	2	3	4	5	6	7	8	9

Pence Table.

													-		
Pence		8.	D.	Pence		8.	D.	Pence		8.	D.	Pence		8.	D.
12	are	1	0	48	are	4	0	84	are	7	0	120	are	10	0
13	22	1	1	49	22	4	1	85	,,	7	1	121	79	10	1
14	,,	1	2	50	22	4	2	86	,,	7	2	122	22	10	2
15		ĩ	3	51		4	3	87		7	3	123	22	10	3
16	"	î	4	52	22	4	4	88	>7	7	4	124		10	4
17	33	1	5	53	99	4	5	89	,,	7	5	124	99	10	5
	>>	1	6	54	19	4	6	90	,,	7	6			10	6
18	**				17		7		"	7	7	126	22		
19	"	1	7	55	,,,	4		91	79			127	22	10	. 7
20		1	8	56	> 7	4	8	92	,,	7	8	128	9.9	10	8
21	19	1	9	57	,,	4	9	93	,,	7	9	129	19	10	9
22	>>	1	10	58	17		10	94	"	7	10	130	.,	10	10
23		1	11	59	22	4	11	95	,,	7	11	131		10	11
Penc	0	8,	D.	Penc	e	8.	D.	Pence		8,	D.	Pence		8.	D.
24	are	2	0	60	are	5	0	96	are	8	0	132	are		0
25	,,	2	1	61	22	5	1	97	99	8	1	133	22	11	1
26	11	2	2	62	22	5	2	98	,,	8	2	134	19	11	2
27	33	2	3	63	33	5	3	99	22	8	3	135		11	3
28		2	4	64	37	5	4	100	29	8	4	136	.,,	11	4
29	"	2	5	65		5	5	101		8	5	137	11	11	5
30	,,	2	6	66	>>	5	6	102	"	8	6	138	22	11	6
31	"	2	7	67	"	5	7	102	"	8	7	139		11	7
	"	2	8	68	99	5	8	103	>>	8	8	140	,,,	11	8
32	**	2	9		"	5	9		>>	8	9	140	,,,	11	9
33	97			69	99			105	59				,,,		10
34	• •	2	10	70	,,,	5	10	106	"	8	10	142		11	
35	"	2	11	71	٠,	5	11	107	39	8	11	143	22	11	11
										-					
Penc		8.		Pene		В.	D.	Pence		8.	D.	Pence		8.	D.
36	are		0	72	are		0	108	are	9	0	144	are		0
37	,,	3	1	73	39	6	1	109	59	9	1	145	99	12	1
38	17	3	2	74	,,	6	2	110	.,	9	2	150	77	12	6
39	22	3	3	75	,,	6	3	1111	22	9	3	156	59	13	0
40	12	3	4	76	11	6	4	112	,,	9	4	168	.,	14	0
41	22	3	5	77	19	6	5	113	,,	9	5	180	22	15	0
42	77	3	6	78	.,	6	6	114	77	9	6	192	22	16	0
43		3	7	79	.,	6	7	115		9	7	200	22	16	8
44	33	3	8	80	•••	6	8	116	"	9	8	204		17	õ
44	17	3	9	81		6	9	117	"	9	9	216	,,	18	Ő
	• 9	о 3	10	82	17	6	10	118	**	9	10	228	""	19	0
46	,,			83	"	6	11	119	59		11	228	33	20	Ő
47	19	3	11	83	> ?	0	11	1119	99	9	11	240	99	20	0

ń

Marked	STERLING MONEY.
f.	4 Farthings = 1 Penny,
d.	12 Pence $=1$ Shilling,
s.	20 Shillings $= 1$ Pound.
- 1 forthin	a. 1 - 9 forthings. 3 - 3 forthings

 $\frac{1}{4} = 1$ farthing; $\frac{1}{2} = 2$ farthings; $\frac{3}{4} = 3$ farthings; crown = 5s; guinea (not now coined) = 21s.

Obsolete Coins.—Noble = 6s. 8d.; mark sterling = 13s. 4d.; angel = 10s.; Jacobus = £1, 5s.; moidore = £1, 7s.; Joannes = £1, 16s.

TROY WEIGHT.

Mark	ed	Troy grains.
gr.	24 Grains = 1 Penny-weight	= 24
dwt.	20 Penny-weights $= 1$ Ounce	= 480
oz.	12 Ounces = 1 Pound, th	= 5760

Gold is supposed to be divided into 24 equal parts called carats. When pure it is said to be 24 carats fine; when, say, 18 parts are pure and 6 are alloy, it is said to be 18 carats fine.

The brass Troy pound, made in 1758, is the standard unit, from which all weights are taken; it contains 5760 grains, each grain being the $_{252}$, $_{455}$ part of a cubic inch of distilled water, at the temperature of 62° of Fah. thermometer, the barometer being at thirty inches. 7000 of such grains are equal to the Avoirdupois pound.

By this weight are weighed gold, silver, jewels, and liquors.

		APOT	HEC	ARIE	S' WE	IGH	r.*	
Marked							Troy grs.	
gr.	20 G	rains	=	1 Sc	ruple	=	20	Э
scr.	3 S	cruples	=	1 Dr	am	=	60	3
dr.	8 D	rams	=	1 00	nce	=	480	Z
oz.	12 0	unces	=	1 Po	und	=	5760	30

AVOIRDUPOIS WEIGHT.

Marked				Troy grs.
dr. 16 Drams	=	1 Ounce	=	437.5
oz. 16 Ounces	=	1 Pound	=	7000
lb. 28 Pounds	=	1 Quarter	=	196000
gr. 4 Quarters, or 112 lb.	=	1 Čwt.	=	784000
cwt. 20 Hundreds			= 1	15680000
14.11 1 4 0 4		1 100 11		

14 lbs. = 1 stone; 8 stones = 1 cwt.; 100 lbs. = 1 cental.

Note.-144 lb. Avoirdupcis are equal to 175 lb. Troy.

* In the British Pharmacopeia (1864), the oz. Trey of 480 grains has been abolished, while the lb. avoir of 7000 grains, and the oz. avoir. of 437 g grs., have been adopted.

1864

WOOL WEIGHT.

Marked				Troy grs.
lb. 7 Pounds Avoir.	=	1 Clove	=	49000
cl. 2 Cloves	=	1 Stone	=	98000
st. 2 Stones	=	1 Tod	=	196000
td. 61 Tods	=	1 Wey	=	1274000
wy. 2 Weys	=	1 Sack	=	2548000
sk. 12 Sacks	=	1 Last. la.	=	30576000
A Score $= 20$ lb. and a				

HAY AND STRAW WEIGHT.

Marked				Troy grs.
lb. 36 Pounds avoirdupois of Straw	=	1 Truss		252000
56 Pounds of old Hay	=	1 Truss	=	392000
60 Pounds of new Hay	=	1 Truss	=	420000
tr. 36 Trusses	=	1 Load,	ld.	
The base of a second second second second	· · · · 43	111 . 01.4	- 0	A

The hay of any year is reckoned new until the 31st of August.

CLOTH MEASURE.

in.	$2\frac{1}{4}$ Inches	= 1 Nail	incres.
nl.	4 Nails	= 1 Quarter	9
qr.	4 Quarters	= 1 Yard, yd.	36
= 0	amhanna 1 Tenna 11, 9	Owenters 1 Ellers all	6 Quer

5 Quarters = 1 Eng. ell; 3 Quarters = 1 Flem, ell; 6 Quarters = 1 French ell; 4 Quarters and 1 inch = 1 Scotch ell.

LONG MEASURE.

Mar	ked		Inches.
in.	12 Inches	= 1 Foot	12
E.	3 Feet	= 1 Yard	36
vd.	51 Yards	= 1 Pole or Perch	198
	40 [°] Poles	= 1 Furlong	7920
fur.	8 Furlongs, or 1760 yds.	= 1 Mile	63360
	69 English Miles	= 1 Degree, deg.	4371840

A Geographical or Nautical mile is = 72909.72 Inches, **3** Geographical miles = 1 league; 20 leagues = 1 Degree; 4 inches = 1 Hand; 6 Feet = 1 Fathom; 2½ Feet = 1 Military pace; 5 Feet = 1 Geometrical pace; 9 Inches = 1 Span; 1½ Foot = 1 Cubit; 66 Feet or 100 Links = 1 Chain.

The brass yard made by Bird, in 1760, is the standard unit from which all lineal measures are taken; it contains 36 inches, each inch being the a_{15} , $\frac{1}{1}$ a_{15} part of a pendulum vibrating seconds of mean time in the latitude of London in a vacuum at the level of the sea, Fah. thermometer being at 62°. A standard yard and a standard Avoirdupois pound are deposited in the Exchequer Office, London.

ENGLISH LAND, OR SQUARE MEASURE.

Aarked	!						Square in.
sq. in.	144	Square	inches	=	1 Square foot		144
sq. f.	9	Square	feet	=	1 Square yard	=	1296
vd.	301	Square	yards	=	1 Square pole	-	39204
po.	40	Square	poles	=	1 Rood	==	1568160
ro	4	Roods	-	=	l Acre	==	6272640
ac	640	Acres		=	1 Square mile		

 $272\frac{1}{4}$ square feet = 1 Rood brick work; 100 square feet = 1 square of flooring, &c.; 36 square yards = 1 Rood of Mason-work, &c.

By this Measure every thing that has length and breadth is estimated.

SOLID MEASURE.

DIATKEA		soun m
s. in. 1728 Solid inches = 1 Solid	d foot ==	1728
s. ft. 27 Solid feet = 1 Solid	d vard =	4665 6
40 solid feet of rough or 50 of hewr	timber = 1 L	oad : 42
solid Feet $= 1$ Ton of shipping.		,

By this Measure every thing which has length, breadth, and thickness, or depth, is estimated.

MEASURE OF CAPACITY.

DIUTISEU				cuoic in.
		1 Pint	=	34.65923
pt.	2 Pints	= 1 Quart	=	69·318 46
qt.	4 Quarts	= 1 Gallon	=	277.27384
gal.	2 Gallons	= 1 Peck	=	
pk.	4 Pecks	= 1 Bushel		2218 19074
bush.	8 Bushels	= 1 Quarter		17745.52595
qr.	4 Quarters	= Chaldron, ch.	====	70982.10380

This is now the only measure allowed by law for all liquids and all dry goods not measured by heaped measure. 100 gallons of this measure are very nearly equal to 120 old wine gallons, to 98°3 old ale gallons, or to 103°12 gallons old dry measure.

HEAPED MEASURE.

marrea				cuoic inches.
		1 Peck	=	703.87148
pk.	4 Pecks	= 1 Bushel	==	2815.48592
bush.	3 Bushels	= 1 Sack	==	8446.45776
sk.	12 Sacks	= 1 Chaldron, ch.		101357.49309

The diameter of the exterior brim of the bushel is 194 inches, and the height of the heap at least 6 inches; the cor-

tent of the heap is therefore 597 29518 cubic inches, which, added to 2218 19074, the content of the bushel, gives 2815 48592 cubic inches for the content of the heaped bushel, and the contents of the others are in proportion.

This Measure is used for Coals, Culm, Lime, Fish, Potatoes, Fruit; and all goods sold by heaped measure.

YARN MEASURE.

Marke	d d	
in.	90 Inches	= 1 Thread
th.	120 Threads	= 1 Cut
ct.	2 Cuts	= 1 Heer
h.	6 Heers	= 1 Slip, hank, or hasp
sl.	4 Slips	= 1 Spindle, sp.

CIRCLE.

M	arked			Sec.
"	60 Seconds	= 1 Minute	=	60
1	60 Minutes	= 1 Degree	=	3600
0	30 Degrees	= 1 Sign	=	108000
s	12 Signs or 360°	= 1 Circle	=	1296000

TIME.

Sec

Marked

sec.	60 Secor	nds	=]	Minute		=	60
min.	60 Minu	tes	=]	Hour		=	3600
ho.	24 Hour	s .	=]	Day		=	86400
da.	365 Days	, 6 Hours	=]	Julian	year,	Y. =	31557600

365 days, 5 hours, 48 minutes, 48 seconds = 1 solar year; 30 days = 1 month; 12 months = 1 year; 7 days = 1 week; 4 weeks = 1 month; 52 weeks and 1 day = 1 year.

> 30 days have September, April, June, and November; All the rest have 31; February 28 alone; but in leap years 29.

QUARTERLY TERMS.

In	England.	In Sco	otland.
Lady-day	25 March	Candlemas	2 February
Midsummer	24 June	Whitsunday	15 May
Michaelmas		Lammas	1 August
Christmas	25 Dec.	Martinmas	11 November

Old Measures now abolished.

Although the following measures are now entirely abolish ed, it is necessary to attend to their subdivisions, and the pro portion which they bear to the imperial standards.

OLD WINE MEASURE.

		Cub. In.		Imp. Galls.
	1 Pint	= 283	=	0.10414
2 Pints	= 1 Quart	$= 57\frac{3}{4}$	=	0.20828
4 Quarts	= 1 Gallon	= 231	=	0.83311
63 Gallons	= 1 Hogshead		=	52.48602
2 Hogsheads	= 1 Pipe		=	104.97204
2 Pipes	= 1 Tun		-	209.94408
2 Hogsheads 2 Pipes	= 1 Pipe			

10 Gallons make 1 Anker, 18 Gallons 1 Rundlet, 315 Gallons 1 Barrel, 42 Gallons 1 Tierce, and 84 Gallons I Puncheon.

OLD ALE AND BEER MEASURE.

			Cub. In.		Imp. Galls.
		1 Pint	= 351	=	0.12713
2 Pints		1 Quart	$= 70\frac{1}{3}$	=	0.25426
2 Quarts	=	1 Pottle	= 141	=	0.50852
2 Pottles	=	1 Gallon	= 282	=	1.01705
9 Gallons	=	1 Firkin		=	9.15341
2 Firkins	=	1 Kilderkin		=	18:30681
2 Kilderkins		1 Barrel		=	36.61362
13 Barrel		1 Hogshead		=	54.92043
2 Barrels		1 Puncheon		=	73.22725
2 Hogsheads		1 Pipe or Butt		=	109.84087
2 Pipes		1 Tun		=	219.68174

OLD DRY MEASURE. .

		Cub	. In.	Imp. Galls
	1 Pint	= ;	331 =	0.12118
2 Pints	= 1 Quart	= ($67\frac{1}{5} =$	0.24236
2 Quarts	= 1 Pottle	= 1	$34\frac{2}{5} =$	0.48472
2 Pottles	= 1 Gallon	= 2	68 =	0.96945
2 Gallons	= 1 Peck	= 5	$37\frac{1}{5} =$	1.93890
4 Pecks	= 1 Bushel	= 21.	503 =	7.75558
4 Bushels	= 1 Coom		=	31.02233
2 Cooms	= 1 Quarter		=	62.04465
5 Quarters	= 1 Wey or Loa	d	=	310.22328
2 Weys	= 1 Tun		=	620.44655

Old Monies, Weights, and Measures of Scotland.

	SCO	LCH	MONEY.			
2	Pennies	=	l Bodle	=	$\frac{1}{6}d$.	Sterling.
	Bodles		l Plack	=		
3	Placks or 12 Pennies			=	Id.	
20	Shillings	= 1	Pound	=	20d.	

3 Placks = 1 Penny Sterling, 4 Pennies = 1 Groat, $13\frac{1}{3}$ Pence = 1 Mark Scotch, 18 Marks or 12 Pounds Scotch = 1 Pound Sterling.

SCOTCH, TROY, OR DUTCH WEIGHT.

Marked								Tre	ny y	Y8.
dro.	16	Drops	. =	1	Ounce	=		475	.55	935
07.	16	Ounces	=	1	Pound	=		7608	·94	96
lb.	16	Pounds	5 =	1	Stone	=		121743	.19	36
The	Tron	Pound	kept	at	Edinbu	urgh	is	equal	to	9622.67

Troy Grains; it varies, however, in different places and for different purposes, but is always divided as above.

SCOTCH LAND MEASURE.

Marked		_				Sq:	Eng. in.
sq. ft.	9 Square	Feet	= 1	Square	Ell	=	1369
sq. e.	36 Square	Ells	= 1	Square	Fall	-	49284
fall	40 Falls		= 1	Rood		= 1	971360
ro.	4 Roods		= 1	Acre,	ac.	= 7	885440
The S	cotch stands	rd ell.	which	h was fo	rmerly	divid	led into

36 of its own inches, is equal to 37 0598 English inches, but by act of Parliament it ought only to be 37.

SCOTCH WHEAT MEASURE.

			Cr	bic Eng. inch.		ub. Eng. in. for barley.
4 Lippies		1 Peck	=		=	
4 Pecks		1 Firlot	=		==	
4 Firlots		1 Boll	=	8857	=	12920.8
16 Bolls	=	1 Chalder	=	141712	=	206732.8

The Linlithgow wheat firlot contained 21¹/₄ Scotch pints; it was also used for rye, pease, beans, salt, and grass-seeds. The barley firlot contained 31 Scotch pints, and was also used for malt, oats, fruit, and potatoes, and divided as above.

SCOTCH LIQUID MEASURE.

Marked				Cubic Eng. mches.
		1 Gill		6.5125
g.	4 Gills	= 1 Mutchkin	=	26.02
mut.	2 Mutchkins	= 1 Chopin	=	52.1
ch.	2 Chopins	$= 1 \operatorname{Pint}$	-	104.2
pt.	2 Pints	= 1 Quart	=	208.4
qt.	4 Quarts	= 1 Gallon	=	833.6
gall.	16 Gallons	= 1 Hogshead		13337.6

Three Scotch pounds, of the Water of Leith, was the standard of the above pint.

ARITHMETIC

Is the art of Computation, and the fundamental Rules are. NUMERATION, ADDITION, SUBTRACTION. MULTIPLICATION, and DIVISION.

NUMERATION

Is the Art of Reading and Writing any Number.

TABLE.

9 Units.

9 8 Tens.

9 8 7 Hundreds.

9 8 7 Hundreds.
9 8 7 6 Thousands.
9 8 7 6 5 Tens of Thousands.
9 8 7 6 5 4 Hundreds of Thousands.
9 8 7 6 5 4 3 Millions.
9 8 7 6 5 4 3 2 Tens of Millions.
9 8 7, 6 5 4, 3 2 1 Hundreds of Millions.

CHARACTERS OF FIGURES.

1, one; 2, two; 3, three; 4, four; 5, five; six, 6; 7, seven; 8, eight; 9, nine; 0, cipher.

ROMAN NUMERAL LETTERS.

I, one; V, five; X, ten; L, fifty; C, one hundred; D, five hundred; M, one thousand.

To read any number expressed in figures.

RULE. Divide the number into periods and half periods, if necessary, from right to left ; then begin at the left hand, and read towards the right.

EXAMPLES.

 1. Read
 83068.
 4. Write in words
 14065708.

 2. Read
 976705.
 5. Write in words
 980679120.

 3. Read
 8067900.
 6. Write in words
 800854029.

To write any number in figures.

Rule. Write every figure in its proper place, and supply vacant places with ciphers.

EXAMPLES.

1. Write in figures, one thousand and eighty.

2. Write in figures, sixty-four thousand and ninety.

3. Write in figures, seventy millions, two thousand and ten.

4. Write in figures, one hundred millions, sixtytwo thousand, eight hundred and eleven.

1. Write in letters, eight hundred and seventynine.

2. Write in letters, one thousand nine hundred and eighty-eight.

ADDITION

Is the collecting of two or more numbers into one sum.

SIMPLE ADDITION.

RULE 1. Place units under units, tens under tens, &c., and draw a line under them.

2. Add the Figures in the units column, and find how many times 10 that sum contains.

3. Set down the remainder, if any, at the foot of the column, and, for every 10 in that sum, carry 1 to the next column: proceed thus with every remaining column, and, under the last, write down the full sum.

PROOF. Draw a line under the uppermost number, add all the rest together, then add this lastfound number and the uppermost; that sum will be the same as the first.

SIMPLE ADDITION.

	EXAM	PLES.	
(1.) 34	(2.) 456	(3.) 5784	(4.) 6745
26	543	2673	2564
72	374	4645	4785
43	268	2476	7643
52	451	3524	2876
*			
(5.) 75426	(6.) 28769	(7.) 84623	(8.) 54962
57264	49384	46238	12845
38572	57263	67965	83453
92486	32765	75679	35276
37218	41834	84213	27637
13853	23413	34275	87698
		- 1	

9. Add 12, 34, 56, 78, 91, 23, 45, 67, and 89 together. Ans. 495.

10. Add 234, 567, 891, 234, 567, 892, 345, 678, and 906 together. Ans. 5314. 11. Add 9876, 5432, 1987, 6543, 2198, 7654.

3210, 6756, and 4693 together. Ans. 48379.

12. Add 6408, 3467, 5986, 7642, 8569, 2398, 8675, 21904, and 686 together. Ans. 65735. 13. Add 6845, 2867, 8490, 684, 1267, 4681,

20680, and 8045 together. Ans. 53559.

14. Add 5408, 1467, 4500, 89. 423, 60456, 8401, and 96 together. Ans. 80840.

* Ans. (1.) 227. (2.) 2092. (3.) 19102. (4.) 24613. (5.) 314819. (6.) 233428. (7.) 392993. (8.) 301871.

15. What is the sum of 54936, 789, 45, 3100, 7093, 84506, 379, and 480? Ans. 151328.

16. Add 79685, 37986, 48798, 76548, 497634, 56783, 698796, 49768, and 9873 together. Ans. 1555871.

17. Add 4869, 75486, 98743, 486, 97, 54868, 79633, 976854, and 796877 together. Ans. 2087913.

18. Add 987548, 69537, 6548, 898756, 48687, 796843, 6854868, 5487695, and 76854876 together. Ans. 92005358.

19. What is the sum of two hundred and eighty three, four hundred and seventy-six, three thousand five hundred and fifty-two, seven thousand six hundred and eighty-four, twenty-seven, eight hundred and seventy-six, two thousand nine hundred and eighty-five? Ans. 15883.

20. A man was born in the year 1761, when would he be 69 years of age? Ans. in 1830.
21. A lent B 30i. C 48i. D 120i. E 209i. F 44i.

21. A lent B 30*l*. C 48*l*. D 120*l*. E 209*l*. F 44*l*. and G 1340*l*. how much did he lend in all? Ans. 1791*l*.

22. A owes B 2359*l*. C 549*l*. D 875*l*. E 965*l*. F 1897*l*. G 1231*l*. H 2197*l*. I 978*l*. and K 841*l*. how much does he owe in all? Ans. 11892*l*.

SUBTRACTION

Is the method of taking a less number from a greater in order to find their difference.

SIMPLE SUBTRACTION.

RULE 1. Place the less number under the greater ; units ander units, tens under tens, &c., and draw a line under them.

2. Then begin at the right hand, and take each figure of the less number from the figure above it, and place the remainder directly under.

3. When the lower figure is equal to the upper write down

a cipher ; if greater than that above it, suppose 10 added to the upper figure ; then subtract the lower figure from the sum : but you must add 1 to the next lower figure before you subtract it.

PROOF. Add the two undermost numbers together, their sum will be equal to the uppermost when the work is right.

	E	XAMPLES			
From	(1.)756	(2.)	5476	(3.) 64276
Take	$(1.) \begin{array}{c} 756 \\ 294 \end{array}$. ,	2563		27354
	*	1.000			
From (4.	.) 104723	(5.) 100	4724	(6.)	2904731
Take	58631	3	4865		1207648
7 I	C004 / 1			A	
	6894 take 4				2808.
	1000 take 8				150.
	1480 take 9				
	5809 take 4				1729.
	846789 tak				
	6805389 ta				
	4000000 ta				
	5400001 ta				
	7654869 ta				
	m 2548697	4 take	19548	796.	Answer
5938178.		07	1 .	= (00000450
	at is the dif				86278456
	4257? An				0510 1
	at is the diff		betwee	n 797	6540 and
	? Ans. 25'		0.1700	1500	,
	ow much			4536	exceed
371547682	2? Ans. 4'	7613685	94.		
* (1.) 4	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	13. (3.)	3692	2.(4	.) 46092.
(5.) 96985	59. (6.) 16	97083.			

20. What is the difference between six hundred and forty-three thousand two hundred and eightyfive, and two hundred and fifty-six thousand seven hundred and forty-two? Ans. 386543.

21. A man was born in the year 1832, what is his age this present year? Ans.

22. A person whose present age is 73, was 37 years old at the birth of his eldest daughter, what is his daughter's age? Ans. 36 years.

MULTIPLICATION

Is a compendious method of adding any number.

The number to be multiplied is called the *Multiplicand*; the number by which you multiply is called the *Multiplier*; and the amount is called the *Product*.

Note. The Multiplicand and Multiplier are called Factors.

SIMPLE MULTIPLICATION.

RULE 1. Place the Multiplier under the Multiplicand, units under units, &c., and draw a line under them.

2. Multiply each figure in the Multiplicand, first by the units of the Multiplier, then by the other figures in their order, placing the first figure of each Product directly under the figure by which you multiply, and carry by 10, as in ADDI-TION; add these Products.

Note. If there is a cipher or ciphers at the right of one or of both Factors, multiply by the significant figures, and annex the ciphers to the Product.

PROOF. Make the former Multiplicand the Multiplier, and the Multiplier the Multiplicand; if this Product is equal to the former, the operation is right. Or thus:

1. Cast the nines out of the two Factors, and set down the Remainders.

2. Multiply the two Remainders together, and if the excess of nines in their Product is equal to the excess of nines in the total Product, the work is right.

	EXAMPLES.	(0.)
Multiplicand	(1.) 68945734	(2.) 48096784
Multiplier	2	3
roduat	*	

Product

3. Multiply 48679048 by 6. Ans. 292074288. 4. Multiply 80670912 by 9. Ans. 726038208. 5. Multiply 98765432 by 12. Ans. 1185185184. 6. Multiply 4606870 by 18. Ans. 82923660. 7. Multiply 2345678 by 47. Ans. 110246866. 8. Multiply 8970681 by 96. Ans. 861185376. 9. Multiply 459068 by 185. Ans. 84927580. 10. Multiply 7549636 by 345. Ans. 2604624420. 11. Multiply 3276894 by 672. Ans. 2202072768. 12. Multiply 9768458 by 894. Ans. 8733001452. 13. Multiply 7280473 by 289. Ans. 2104056697. 14. Multiply 809601 by 2400. Ans. 1943042400. 15. Multiply 601570 by 3068. Ans. 1845616760. 16. Multiply 406894 by 85237. Ans. 34682423878. 17. Multiply 238906 by 216894. Ans. 51817277964. 18. Multiply 54986304 by 729634.

Ans. 40119876932736.

RULE II. When the Multiplier is the product of two or more numbers, neither of which exceeds 12, multiply continually by these numbers.

EXAMPLES.

1. Multiply	68094568 by 24.	Ans.	1634269632.
2. Multiply	4096731 by 36.	Ans.	147482316.
3. Multiply	748695 by 48.	Ans.	35937360.
	947658 by 54.	Ans.	51173532.
5. Multiply	386909 by 81.	Ans.	31339629.

Ans. (1.) 137891468. (2) 144290352.

6. Multiply 729654 by 112. Ans. 81721248.

7. Multiply 8976543 by 108. Ans. 969466644.

8. A gentleman has 45*l*. a-week, how much is that in 52 weeks? Ans. 2340*l*.

9. How many seeds in a plant which consists of 9 stalks, on each of which are 45 flowers, and each flower bears 549 seeds? Ans. 222345.

10. How many square yards in a garden which is 53 yards long, and 32 yards broad? Ans. 1696.

DIVISION

Is a compendious method of subtracting any number.

The number to be divided is called the *Dividend*. The number you divide by is called the *Divisor*. The number of times the Dividend contains the Divisor is called the *Quotient*.

SIMPLE DIVISION.

RULE I. l. Draw a line on the right and left of the Dividend; write the Divisor on the left hand, and the Quotient as it arises on the right.

2. From the left hand of the Dividend point off as many figures as will contain the Divisor once or oftener; find how many times these figures contain the Divisor, and place the figure which represents the number of times in the Quotient.

3. Multiply the Divisor by the Quotient figure, and place the product under the figure or figures pointed off.

4. Draw a line, and subtract the Product from the figures under which it stands.

5. To the right hand of the Remainder bring down the next figure of the Dividend, and point it off; which number divide as before, and proceed in the same manner till all the Dividend be brought down.

Note. If the Divisor is 12, or under, the operation may be performed mentally, by putting down only the Quotient.

PROOF. Multiply the Quotient and Divisor together, adding the Remainder, if any; this Product will be equal to the Dividend.—Or, divide the Dividend after subtracting the Remainder, if

SIMPLE DIVISION.

any, by the Quotient; the result will be equal to the Divisor.

EXAMPLES.

1. Divide 84667 by 2.	Ans. 423333
2. Divide 489764 by 3.	Ans. 163254 ⁸
3. Divide 386457 by 4.	Ans. 96614 ¹ / ₄
4. Divide 490680 by 5.	Ans. 98136
5. Divide 867059 by 6.	Ans. 1445095
6. Divide 732845 by 7.	Ans. 1046924
7. Divide 411678 by 8.	Ans. 51459§
8. Divide 4912037 by 9.	Ans. 545781§
9. Divide 8695340 by 14.	Ans. 62109510
10. Divide 1234567 by 20.	Ans. 61728 20
11. Divide 7865432 by 38.	Ans. 206985 ² / ₃₈
12. Divide 75846972 by 46.	Ans. 164884748
13. Divide 54906734 by 59.	Ans. 93062238
14. Divide 48372864 by 75.	Ans. 64497138
15. Divide 9876540 by 87.	Ans. 11352338
16. Divide 14680598 by 108.	Ans. 135931 50 108
17. Divide 81407910 by 384.	Ans. 211999384
18. Divide 72986543 by 563.	Ans. $129638\frac{3}{5}\frac{49}{63}$
19. Divide 987213472 by 747.	Ans. 1321570444
20. Divide 428638726 by 1374.	Ans. 311964 190
21. Divide 729684786 by 4726.	Ans. 1543974588
22. Divide 40608370 by 1809.	Ans. 22447 1747
23. Divide 51406745 by 314689.	Ans. $163\frac{1}{3}\frac{1}{1}\frac{2}{4}\frac{3}{5}\frac{8}{9}$

RULE II. When the Divisor is the product of two or more numbers, none of which exceeds 12, divide successively by these numbers.

Note. To find the true Remainder, multiply the last Remainder into all the preceding Divisors (the last excepted), adding the several Remainders to the Products to which they belong.

EXAMPLES.

Divide 459323 by 48. Ans. 956911
 Divide 287536 by 56. Ans. 51344

3. Divide	679195 by 84.	Ans. 808553
4. Divide	7384675 by 96.	Ans. 76923
	5498653 by 108.	Ans. 50913
	8965437 by 121.	Ans. 74094
7. Divide	3846973 by 112.	Ans. 34347193
	549657 by 168.	Ans. 3271129

RULE III. When there are ciphers annexed to the Divisors cut them off; and cut off as many figures from the Dividend; aunex these figures to the Remainder.

EXAMPLES.

1.	Divide	41285	by	30.	Ans.	137635
	Divide				Ans.	
3.	Divide	45973	by	240.	Ans.	191133
4.	Divide	39768	by	7000.		54768
					0. Ar	54456

6. The area of a room 16 feet broad is 512 feet, what is its length? Ans. 32 feet.

SUPPLEMENT TO MULTIPLICATION AND DIVISION.

I. When the Multiplier contains a fraction.

RULE. First multiply by the upper figure of the fraction, and divide the Product by the under figure, then multiply by the whole number, and add the Product to the Quotient.

EXAMPLES.

1.	Multiply	7854769	by	9 ³ / ₄ . Ans. 76583997 ³ / ₄
2.	Multiply	3768473	by	163. Ans. 61708745
3.	Multiply	2965497	by	267. Ans. 794094198
4.	Multiply	3864738	by	312.4.
				Ans. 120790629448
5.	Multiply	3846768	by	416 ¹ . Ans. 1601217180
6.	Multiply	7486742	by	981. Ans. 737444087

II. When the Divisor contains a fraction.

RULE. Multiply the Divisor by the under figure of the fraction, and add the upper figure to the Product; multiply the Dividend also by the under figure of the fraction, and thendivide.

REDUCTION.

EXAMPLES.

1. Divide	785476 by 94.	Ans.	8491614
2. Divide	3876549 by 16	3. Ans.	23259247
	5469874 by 21		253234 98
4. Divide	7321095 by 41		174832 40
	5486953 by 29		18599834
	7654869 by 31		241573387

REDUCTION

Is the changing of numbers from one name to another, without altering their value.

To bring a greater name into a less.

RULE. Multiply the given number by as many of the less name as make one of the greater; adding to the Product the parts of the second name, if any; proceed in the same manner, till you have brought it as low as is required.

To bring a less name into a greater.

RULE. Divide by as many of the less name as make one of the greater; and thus proceed till you have brought it into that name required; the last Quotient, together with the several Remainders, if any, will be the answer.

Mixed Reduction is when both Multiplication and Division are used.

RULE. Reduce the given numbers into one name; then divide the one by the other.

PROOF. Reverse the Question.

STERLING MONEY.

EXAMPLES.

1. Reduce 12s. 11¹d. into farthings. Ans. 622. 2. In 1 pound, how many shillings, pence, and farthings? Ans. 20s. 240d. 960f.

3. In 7343 farthings, how many pounds? Ans. 71. 12s. 11⁸d.

4. In 40. 10s. 6d. how many pence, halfpence, and farthings? Ans. 9726d. 19452 halfpence, 38904 farthings.

REDUCTION

5. In 12s. 2¹/₂d. how many halfpence? Ans. 293.

6. In 900 guineas, how many sixpences and pence? Ans. 37800 sixpences, 226800d.

7. Reduce 3091. 15s. 10[§]₄d. into farthings. Ans. 297403.

8. In 912 farthings, how many shillings? Ans. 19s.

9. In 4089 farthings, how many pounds? Ans. 41. 5s. $2\frac{1}{4}d$.

10. In 4009 halfpence, how many pounds? Ans. 81. 7s. $0\frac{1}{2}d$.

11. In 42336 farthings, how many guineas? Ans. 42.

12. In 7200 farthings, how many crowns? Ans. 30.

13. Reduce 736*l*. 17*s*. $11\frac{1}{2}d$. to halfpence. Ans. 353711.

14. Reduce 275*l*. 10*s*. 10^{*s*}/₄*d*. to farthings. Ans. 264523.

15. Reduce 2051. 16s. 24d. to farthings. Ans. 197577.

16. Reduce 2101. 10s. 6d. to sixpences. Ans. 8421.

17. Reduce 2000?. 17s. 8d. to fourpences. Ans. 120053.

18. Reduce 74867 farthings to pounds. Ans. 771. 19s. $8\frac{3}{4}d$.

19. Reduce 650967 halfpence to guineas. Ans. 1291 guineas, 12s. 7¹/₄.

20. Reduce 74894 threepences to pounds. Ans. 9361. 3s. 6d.

21. Reduce 7486*l*. to guineas. Ans. 7129 guineas, 11s.

22. In 10864 farthings, how many crowns, halfcrowns, sixpences, and pence, and of each an equal number? Ans. 28 of each.

23. In 40 guineas, how many pounds? Ans. 421. 24. In 2831. 9s 6d. how many shillings, half-

REDUCTION.

crowns, and crowns, and of each an equal number? Ans. 667 of each.

25. In 842 crowns, how many guineas? Ans. 200 guineas, 10s.

TROY WEIGHT.

26. In 6 lb. 10 oz. 5 gr., how many grains? Ans. 39365.

27. In 213212 grains, how many pounds? Ans. 37 lb. 3 dwt. 20 gr.

28. In 9120 gr. of silver, how many teaspoons, each half an ounce? Ans. 38.

29. In 9 ingots of silver, each 2 lb. 10 oz. 10 dwt., how many grains? Ans. 149040 gr.

APOTHECARIES' WEIGHT.

30. In 2 lb., how many oz. dr. scr. and gr.? Ans. 24 oz. 192 dr. 576 scr. 11520 gr.

31. In 546 lb. 18 gr., how many grains? Ans. 3144978 gr.

32. In 56789 scruples, how many lb.? Ans. 197 lb. 2 oz. 1 dr. 2 scr.

AVOIRDUPOIS WEIGHT.

33. In 6 cwt. 1 qr. 18 lb., how many drams? Ans. 183808.

34. In 30 tons, 18 cwt. 2 qr. 20 lb. 12 oz. 15 dr., how many drams? Ans. 17738959 dr.

35. In 215040 oz., how many tons? Ans. 6 tons.

36. In 540 parcels of sugar, each 184 lb., how many cwt.? Ans. 87 cwt. 3 qr. 27 lb.

WOOL WEIGHT.

37. In 2 weys, how many pounds of wool? Ans. 364 lb.

38. In 13104 lb., how many lasts? Ans. 3.

39. In 8 lasts, how many stones? Ans. 2496.

HAY AND STRAW WEIGHT.

40. In two loads of straw, how many pounds? Ans. 2592.

41. In 10080 lb. of old hay, how many loads? Ans. 5.

42. In 3 loads, 30 trusses, 42 lb. of new hay, how many lb.? Ans. 8322 lb.

CLOTH MEASURE.

43. In 400 yds., how many nails? Ans. 6400 nails.

44. In 500 nails, how many vds.? Ans. 31 vds. 1 gr.

45. In 764 ells English, how many yds.? Ans. 955 yards.

46. In 6 pieces of cloth, each 201 yards, how many nails and inches? Ans. 1968 nails, 4428 inches.

LONG MEASURE.

47. Reduce 1 mile into inches. Ans. 63360.

48. In 1362240 inches, how many miles? Ans. 211.

49. Reduce 360 miles, 4 furlongs, 27 poles, 21 yards, to inches. Ans. 22846716 inches.

50. Reduce 7486973 feet to miles. Ans. 1417 miles, 7 furlongs, 35 poles, 5 yards, 6 inches.

51. How often will a wheel, of 181 feet circumference, turn in running betwixt Edinburgh and Glasgow, the distance being 44 miles? Ans. 1255721.

52. How many inches will reach round the world, which is 360 degrees, and each degree 69 miles? Ans. 1573862400.

53. How many inches will reach round the moon, of which the circumference is 6817 miles, 2 furlongs, 7 poles? Ans. 431942346 inches.

LAND MEASURE.

54. In 201 acres, how many poles? Ans. 3280 poles.

55. In 172425 yards, how many acres? Ans. 35 acres, 2 roods, 20 poles.

56. In 674 acres, 6 poles, how many yards? Ans. 32623411 yards.

57. In 20047964 square inches, how many acres? Ans. 3 acres, 31 poles, 11 yards, 3 feet, 32 inches.

58. In 740 acres, 51 yards, how many square feet? Ans. 322344491 square feet.

59. In 7854796 square feet, how many acres? Ans. 180 acres, 1 rood, 11 poles, 12 yards, 3¹/₂ feet.

SOLID MEASURE.

60. In 52 solid yards, how many solid inches? Ans. 2426112.

61. In 13856832 solid inches, how many solid yards? Ans. 297 yards.

MEASURE OF CAPACITY.

62. In 840 quarters, 3 pecks, how many pecks? Ans. 26883.

63. In 47 quarters, 6 bushels, how many pecks? Ans. 1528.

64. In 649 pecks of wheat, how many quarters? Ans. 20 quarters, 2 bushels, 1 peck.

65. In 6750 pecks of barley, how many quarters? Ans. 210 quarters, 7 bushels, 2 pecks.

YARN MEASURE.

66. In 7 spindles, how many cuts? Ans. 336.

67. In 48960 threads, how many slips? Ans. 34 slips.

68. In 27 spindles, 80 threads, how many threads? Ans. 155600.

69. In 71 slips, 4 heers, 1 cut, 64 threads, 25 inches, how many inches? Ans. 9304585.

CIRCLE.

70. In 36°, 24', 35", how many seconds? Ans. 131075".

REDUCTION.

71. In 120836", how many signs? Ans. 1*, 3°, 33', 56".

72. In 4*, 14°, 15', 44", how many seconds? Ans. 483344.

TIME.

73. In a year of 365 days, 6 hours, how many seconds? Ans. 31557600 seconds.

74. How many hours from the birth of Christ to Christmas 1818; reckoning 365 days 6 hours to a year? Ans. 15936588.

75. How many seconds are there in a solar year, which consists of 365 days, 5 hours, 48 minutes, and 48 seconds? Ans. 31556928.

76. From March 10 to December 25 (both days included), how many days and hours? Ans. 291 days = 6984 hours.

77. How long would it require to count five hundred millions of money, at the rate of 100*l*. a-minute, without intermission? Ans. 9 years, 187 days, 5 hours, 20 minutes.

MISCELLANEOUS QUESTIONS.

1. Reduce 17 tons, 13 cwt. 1 qr. 25 lb. 12 oz. 15 dr. to drams. Ans. 10134991 drs.

2. In 47875640 inches, how many miles, &c.? Ans. 755 ml. 4 fu. 36 p. 2 ft. 8 in.

3. In 3670 Julian years, 315 days, 16 ho. 35 m. 47 s., how many seconds? Ans. 115843667747 sec.

4. In 47872198 sq. in., how many acres? Ans. 7 ac. 2 ro. 21 per. 2³/₄ yd. 3 ft. 118 in.

5. In 359 solid yd. 21 s. ft. 1047 s. in., how many solid inches? Ans. 16786839 s. in.

6. In 4768 guin. 12s., how many half-crowns? Ans. 40056 half-crowns.

7. In 31861. 15s. 8d., how many guineas? Ans. 3035 gu. 8d.

REDUCTION.

8. In 36840 pounds Scotch, each 1s. 8d., how many pounds sterling? Ans. 3070l.

9. In 3879 English ells, how many Scotch ells, each 37 imperial inches? Ans. 4717 S. e. 26 in.

10. In \$74867 gallons, how many qrs.? Ans. 13669 qrs. 6 bu. 1 pk. 1 gal.

11. In 784 gal. 2 qt. 1 pt., how many pints? Ans. 6277 pints.

12. Reduce 746 ml. 5 fu. 37 po. 2 ft. 11 in., into inches. Ans. 47313521 inches.

13. Reduce 475 ac. 2 ro. 24 per. 29 yd. 7 ft. 138 in., into inches. Ans. 2983619946 sq. in.

14. How many lbs. of old hay in 25 loads? Ans. 50400 lbs.

15. In 5740 yds., how many French ells? Ans. 3826 Fr. ells, 4 grs.

16. How many seconds in 7875 solar years? Ans. 248510808000".

17. Reduce 2 cir. 7 s. 17°, 25', 57" to seconds. Ans. 3410757".

18. How many pints are in 74 qr. 3 bu. 2 pk. 1 gal. 3 qt. 1 pt.? Ans. 38127 pts.

19. In 7485 marks Scotch, each 131d., how many crowns and guineas? Ans. 1663 cr. 1s. 8d.; 396 gu. 8d.

20. In 786*l*. 12s., how many crowns, half-crowns, shillings, and sixpences, and of each an equal number? Ans. 1748.

21. How many pounds Scotch, each 1s. 8d., are in 729 gu. 3s. 4d.? Ans. 9187 pounds Scotch and 8d.

22. In 7486 half-guineas, how many marks, each 13s. 4d.? Ans. 5895 marks, 3s.

23. In 25 roods, 34 yds. of mason work, how many yards? Ans. 934 yds.

24. In 480 lbs. Scotch tron weight, each 22 oz., how many lbs. avoirdupois? Ans. 660 lbs.

29

С

RULE 1. Place all numbers of the same denomination directly under one another, and draw a line under them.

2. Add the figures in the lowest denominations, and find how many of the next higher denomination that sum contains.

3. Write down the remainder, if any, at the foot of the column, and carry 1, for each of the higher denomination, to the next column.

4. Proceed in the same manner through all the denominations till you come to the highest, the sum of which, together with the several remainders, will give the answer required.

PROOF. As in Simple Addition.

STERLING MONEY.

EXAMPLES.

10	20	12		10	20	12		10	20	12
£	s.	d.		£	s.	d.		£	8.	d.
(1.) 6	6		(2.)				(3.)	360	19	103
4	8	9	(1)	24	14	41	(+-)	496	14	11
43	5	6			18	83		306	18	91
4	9	7			14	4		459	19	6
4 5	6	6		69	15			304		
7	5	4			16			900		
				_		_				
		*								
		_				-	-			
£	<i>s</i> .	d.		£	<i>s</i> .	d.		£	s.	d.
(4.) 27	19	61	(5.)	321	16	113	(6.)	329	11	73
35	18	23	` '	213	17	101	. ,	48	17	103
43	16	111		312	18	61		189	19	93
72	15	101		476	13	31		45	13	68
72 84	15 17	101 91		476 764	13			45 789	13 16	
72 84 96	15 17 14	101 91 101		476 764 897	13 15 11	3 5 4 11 4		45 789 978	13 16 12	
(4.) 27 35 43 72 84 96	15 17 14	101 91 101 101		476 764 897	13 15 11	3 5 4 11 4		45 789 978	13 16 12	

⁶ Ans. (1.) 31*l*. 2s. 4d.—(2.) 220*l*. 9s. 84d.—(3.) 3830*l*. 0s. 84d. –(4.) 362*l*. 3s. 24d.—(5.) 2987*l*. 14s. 04d.—(6.) 2382*l*. 11s. 94d. 7. A owes B 450*l*. 16*s*. 10*d*., C 34*l*. 18*s*. 9*d*., D 545*l*. 16*s*. $7\frac{5}{4}d$., E 44*l*. 14*s*. $8\frac{1}{2}d$., F 300*l*. 9*s*. 10*d*., and G 84*l* 14*s*. Required A's debt? Ans. 1461*l*. 10*s*. $9\frac{1}{4}d$.

8. Ådd 326*l*. 12s. 3¹/₄*d*.; 274*l*. 15s. 4*d*.; 432*l*. 16s. 5³/₄*d*.; 376*l*. 19s. 8¹/₂*d*.; 741*l*. 14s. 5¹/₄*d*.; 279*l*. 2s. 4*d*. Ans. 2432*l*. 0s. 6³/₄*d*.

9. Add 471*l*. 15s. 21*d*. ; ²296*l*. 17s. 81*d*. ; 1432*l*. 15s. 41*d*. ; 273*l*. 12s. 6*d*. ; 354*l*. 14s. 51*d*. ; 2471*l*. 13s. 4*d*. Ans. 5301*l*. 8s. 61*d*.

10. Add 28*l*. 12*s*. 5¹/₂*d*.; 437*l*. 16*s*. 3*d*.; 7328*l*. 12*s*. 5¹/₄*d*.; 456*l*. 14*s*. 10*d*.; 3284*l*. 17*s*. 8³/₄*d*.; 27*l*. 16*s*. 3*d*. Ans. 11564*l*. 9*s*. 11¹/₄*d*.

11. What is the sum of $2\overline{46l}$. 14s. $3\frac{1}{2}d$; 741*l*. 13s. $2\frac{1}{4}d$; 79*l*. 2s. 8d.; 4284*l*. 16s. $2\frac{1}{4}d$.; 456*l*. 15s. 3d.; 36*l*. 8s. $4\frac{3}{4}d$.; 2841*l*. 12s. 9d.? Ans. 8687*l*. 2s. $8\frac{3}{4}d$.

12. Add 287l. 14s. 5¹/₂d.; 742l. 9s. 4d.; 28l. 17s. 5¹/₄d.; 4684l. 12s. 9¹/₂d.; 356l. 14s. 6d.; 3284l. 16s. 5⁵/₃d.; 4721l. 15s. 2¹/₂d. Ans. 14107l. 0s. 2¹/₂d.

13. What is the sum of 38*l*. 14s. $6\frac{1}{2}d$; 276*l*. 13s. 5d.; 29*l*. 10s. $7\frac{1}{4}d$; 4324*l*. 17s. $9\frac{1}{2}d$; 742*l*. 6s. $2\frac{3}{4}d$; 5426*l*. 15s. 3d.; 45*l*. 4s. $10\frac{1}{2}d$.; 2143*l*. 14s. 5d.? Ans. 13027*l*. 17s. $1\frac{1}{2}d$.

14. What is the sum of $1568\overline{l}$. 16s. $9\frac{1}{4}d$.; 5769*l*. 17s. 10 $\frac{1}{2}d$.; 8769*l*. 19s. $4\frac{3}{4}d$.; 7698*l*. 15s. 4d.; 49987*l*. 17s. $6\frac{1}{4}d$.; 50987*l*. 14s. $7\frac{3}{4}d$.; 97854*l*. 8s. $6\frac{1}{2}d$.; 9768*l*. 3s. $5\frac{1}{4}d$.; 376*l*. 9s. $7\frac{1}{4}d$.; 88768*l*. 15s. $6\frac{3}{4}d$.? Ans. 321550*l*. 18s. $8\frac{3}{4}d$.

15. Bought a parcel of goods for 100*l*. 10s., paid for packing them 18s. 6d., for carriage 1*l*. 18s., and spent about the bargain 12s. $8\frac{3}{4}d$. What do these goods stand me? Ans. 103*l*. 19s. $2\frac{3}{4}d$.

16. A servant went to market and laid out on beef 10s. 10¹/₂d., on mutton 5s. 9¹/₂d., on lamb 16s. 6d., on greens $5\frac{1}{2}d.$, on fish 10s. 3d., on eggs $10\frac{3}{2}d.$, and on butter 6s. 8d. How much was laid out in all? Ans. 2l. 11s. $5\frac{1}{4}d.$

17. A owes **B** for bread 8l. 9s. $6\frac{1}{4}d$., for cheese 5l. 10s., for tea 3l. 11s. $9\frac{1}{2}d$., for sugar 12l. 10s. $8\frac{5}{4}d$., and for other articles 20l. 8s. $4\frac{1}{4}d$. What is the amount of A's debt? Ans. 50l. 10s. $4\frac{3}{4}d$.

								7				
	10	20	4		10	16	16		10	12	20	24
	T.	cwt.	qr.		lb.	oz.	dr.		lb.	oz.	dwt	gr.
(18.)40	16	2	(19.)25	14	12	(20.)	20	10	14	16
`		18			30	15	14	` '	14	11	19	18
	45	14	1		24	14	11		50	8	16	21
	34	19	3		16	10	'8		34	6	18	22
	54	16	2		8	7	10		68	4	16	20
	36	15	1		13	6	9		46	1	10	4
		14			4	14	10		14	10	16	12
	10		0		8	10	15		50	8	14	6
			_		_							
			*									

21. What is the sum of 50 lb. 11 oz. 14 dwt. 20 gr.; 40 lb. 10 oz. 15 dwt.; 62 lb. 8 oz. 20 gr.; 34 lb. 8 oz. 14 dwt.; 36 lb. 4 oz. 10 dwt. 19 gr.; and 54 lb. 15 gr.? Ans. 279 lb. 7 oz. 16 dwt. 2 gr.

22. What is the sum of 45 lb. 6 oz. 5 dr. 1 scr. 14 gr.; 23 lb. 8 oz. 6 dr. 12 gr.; 31 lb. 4 oz. 3 dr. 2 scr.; 27 lb. 10 oz. 2 dr.; 3 dr. 1 scr. 15 gr.; 2 lb. 5 oz. 7 dr. 2 scr. 10 gr.? Ans. 131 lb. 4 dr. 2 scr. 11 gr.

23. A shopkeeper retails of sugars 3 qr. 4 lb. 12 oz. 4 dr.; of teas 1 qr. 15 lb. 10 oz.; of coffee

Ans. (18.) 369 tons, 4 cwt. 3 qr.—(19.) 133 lbs. 15 oz. 9 dr.—(20.) 301 lb. 4 oz. 7 dwt. 23 gr. 4 cwt. 1 qr. 6 lb. 14 oz.; of tobacco 5 cwt. 3 qr., and of snuff 2 cwt. 2 qr. 26 lb. 10 oz. 12 dr. What is the weight of the whole? Ans. 13 cwt. 3 qr. 25 lb. 15 oz.

24. A draper bought 308 yds. 2 qr. 1 nail; 500 yds. 1 qr. 3 nl.; 54 yds. 3 qr.; and 60 yds. 3 qr. 3 nls. How many yards did the whole contain? Ans. 924 yds. 2 qr. 3 nl.

25. From A to B is 5 miles, 1 fur. 8 po.; from B to C 19 m. 18 po.; from C to D 6 fur. 18 po. 4 yds.; and from D to E 5 m. 36 po. 4 yds. What is the distance from A to E? Ans. 30 mil. 1 fur. 1 po. $2\frac{1}{2}$ yds.

²**26.** A wine merchant imported 378 gal. 2 qt. 1 pt. of claret, 310 gal. 1 qt. 1 pt. of sherry, 71 gal. 3 qt. 1 pt. Lisbon, 239 gal. 1 qt. of port, 356 gal. 3 qt. Madeira, and 219 gal. 2 qt. 1 pt. Champagne; how much did he import in all? Ans. 1576 gal. 2 qts.

27. A surveyor having measured 5 pieces of land, found the first to contain 6 ac. 2 ro. 20 po.; the second, 20 ac. 1 ro. 15 po.; the third, 15 ac. 3 ro. 4 po.; the fourth, 2 ac. 2 ro. 24 yds. 8 feet; and the fifth, 1 ac. 1 ro. 39 po. 28 yds. 5 feet. How many English acres were surveyed in all? Ans. 46 ac. 2 ro. 39 po. $22\frac{3}{4}$ yds. 4 ft.

COMPOUND SUBTRACTION.

RULE 1. Place the less number under the greater, so that those parts which are of the same denomination may stand directly under each other, and draw a line under them.

2. Begin at the right hand, and subtract the number of each denomination in the lower line from the number above it, and set the remainder under it.

3. But if the lower number of any denomination is greater than the upper, add as many to the upper as make one of th² next higher denomination, then subtract the lower from that' sum, and add 1 to the lower number of the next denomination

COMPOUND SUBTRACTION.

before you subtract it; proceed in this manner till the whole is finished.

PROOF. As in Simple Subtraction.

STERLING MONEY.

	EXAMPLES		
(1.)	10 20 12	(2.) 10 20 12	
	£ s. d.	£ s. d.	
	6 14 6	From 20 10 10}	
Paid	4 15 8	Take 14 14 83	
Balance	*	Rem.	
Proof		Proof	
£ s. d.	£ 8.	d. £ s. d.	
(3.) 209 17 21	(4.) 1004 12	24 (5.) 1543 10 104	

31. 18s. $9\frac{3}{4}d$.

7. From 40*l*. 16*s*. take 30*l*. 18*s*. $6\frac{1}{4}d$. Ans. 9*l*. 17*s*. $5\frac{3}{4}d$.

8. From 436*l*. 17*s*. $4\frac{1}{2}d$. take 298*l*. 14*s*. $6\frac{3}{4}d$. Ans. 138*l*. 2*s*. $9\frac{3}{2}d$.

9. From 9781. 5s. 2¹/₂d. take 2841. 16s. 4⁸/₄d. Ans. 6931. 8s. 9³/₄d.

10. From 30457. take 30007. 10s. 8d. Ans. 441. 9s. 4d.

11. A borrowed from B 100*l*. and paid him 48*l*. 16s. $10\frac{3}{4}d$. What is due to B? Ans. 51*l*. 3s. $1\frac{1}{4}d$.

12. What is the difference between 2843*l*. 12s. 8¹/₄*d*. and 1761*l*. 13s. 4¹/₈*d*. ? Ans. 1081*l*. 19s. 3³/₈*d*.

13. What is the difference between 471*l*. 12s. $9\frac{1}{2}d$. and 7846*l*. 0s. $4\frac{1}{4}d$.? Ans. 7374*l*. 7s. $6\frac{5}{4}d$.

14. A merchant, who had owing him 10001. Ss. 9d.,

Ans. (1.) 1l. 18s. 10d. (2.) 5l. 16s. 13d. (3.) 19l. 17s. 43d. (4.) 156l. 19s. 113d. (5.) 646l. 17s. 43d.

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received at one time 108*l*. 14*s*. 4*d*., at another 112*l*. 10*s*. $6\frac{5}{4}d$., and at a third 258*l*. 8*s*. $5\frac{1}{4}d$. What remains due to him? Ans. 520*l*. 15*s*. $4\frac{5}{4}d$.

15. A merchant has in cash 480*l*. 6s. 7*d*., goods, value 3005l. 14s. 8*d*., a house 788*l*. 10s. 6 $\frac{5}{4}d$., debts due to him 850*l*. 18s. 9 $\frac{1}{4}d$. He owes A 100*l*. 6s. 8*d*., B 70*l*. 19s. 8*d*., and C 169*l*. 16s. 10 $\frac{5}{4}d$. Required his stock? Ans. 4784*l*. 7s. $4\frac{1}{4}d$.

16. Two women and a man received 30*l*. 5s. $6\frac{1}{2}d$. for their yearly wages; the oldest woman and the man received 22*l*. 7s. $6\frac{1}{4}d$., and the youngest woman and the man, 21*l*. 3s. 5d. Required the wages of each? Ans. the man's, 13*l*. 5s. $4\frac{3}{4}d$., the oldest woman's, 9*l*. 2s. $1\frac{1}{2}d$., the youngest woman's, 7*l*. 18s. $0\frac{1}{4}d$.

17. Bought 20 lb. 8 oz. 10 dwt. of silver plate, and sold 14 lb. 8 oz. 14 dwt. 16 grains. What remains? Ans. 5 lb. 11 oz. 15 dwt. 8 gr.

18. Bought 4 tons, 6 cwt. 1 qr. of sugar, and sold at one time, 1 ton, 20 lb., and at another, 1 ton, 10 cwt. 1 qr. 4 lb. 14 oz. What remains? Ans. 1 ton, 15 cwt. 3 qr. 3 lb. 2 oz.

19. From 850 yards take 500 yds. 2 qr. 1 nl. Ans. 349 yds. 1 qr. 3 nl.

20. A person intending to make a journey of 50 miles, was only able to go 30 miles, 6 fur. 21 po. 3 yds. What part of the journey remains unfinished? Ans. 19 m. 1 fur. 18 po. 2½ yds.

21. A farmer bought 111 qr. 7 bush. 2 pks. of barley, and afterwards sold 54 qr. 4 bush. 3 pks., How much did he retain in his possession? Ans. 57 qr. 2 bush. 3 pks.

22. A field of 25 ac. 2 ro. 17 per. 5 yds. is sown with wheat and oats; 14 ac. 3 ro. $27\frac{5}{4}$ yds. are wheat, and the remainder oats; how much is that? Ans 10 ac. 3 ro. 16 per. $7\frac{1}{4}$ yds. 23. From 84 qr. 2 bu. 2 pks. take 66 qr. 3 bu. 3 pks. 1 gal., and how much remains? Ans. 17 qr. 6 bu. 2 pks. 1 gal.

24. Subtract one farthing from 100*l*. Ans. 997. 19s. 11³/₂d.

25. An Account of Household Expenses.

			Recei		1	Pai	
1882.		£	<i>s</i> .	d.	t	S.	d.
Jan. 1. On		14	6	81			
3. Pai	d for tea,	i		~		4	6
	for sugar,	1				3	103
	for butter,				1	1	6
10.	for cheese,	1				9	83
	for butcher mea	t,			1	10	Q
14. Rec	eived,	4	10	6	1		
20. Paie	d Baker's account				1	14	6
21.	Tailor's do.					10	61
	Shoemaker's do	.			1	18	9
28.	Brewer's do.				1	19	113
		-			-	-	
31. On	hand,	£0	3	10	-		

COMPOUND MULTIPLICATION.

RULE I. 1. When the Multiplier does not exceed 12, write it under the lowest denomination of the Multiplicand.

2. Multiply its several denominations in order, beginning at the lowest, and carry according to the value of the next higher.

3. When the Multiplier exceeds 12, and is the product of two or more numbers, none of which exceeds 12, multiply successively by these numbers.

PROOF. By Division.

EXAMPLES.

1. What cost 2 yards at 1s. 44d.? Ans. 2s. 84d. 2. What cost 3 yards at 2s. 83d.? Ans. 8s. 24d.

3. What cost 4 lb. of sugar at 91d.? Ans. 3s. 2d. 4. What cost 6 lb. of tea at 4s. 6d.? Ans. 11. 7s. 5. What cost 8 lb. of butter at $10\frac{1}{4}d$? Ans. 6s. 10d. 6. What cost 10 lb. of cheese at $5\frac{1}{2}d$? Ans. 4s. 7d. 7. What cost 12 lb. of beef at $4\frac{1}{4}d$? Ans 4s. 3d. 8. What cost 14 lb. of mutton at 31d.? Ans. 4s. 1d. 9. What cost 16 lb. of yeal at 53d.? Ans. 7s. 8d. 10. What cost 24 gallons of brandy at 12s. 6d.? Ans. 15%. 11. What cost 28 firkins of herring at 7s. 3dd.? Ans. 101. 4s. 2d. 12. What cost 30 lb. of candle at 91d.? Ans. 11. 3s. 9d. 13. What cost 32 ells of holland at 8s. 41d.? Ans. 131. 7s. 4d. 14. What cost 36 bolls of meal at 14s. $6\frac{1}{4}d$.? Ans. 261. 2s. 9d. 15. What cost 56 firkins of butter at 16s. $3\frac{1}{2}d$.? Ans. 451, 12s. 4d. 16. What cost 60 bolls of wheat at 11. 4s. 6d.? Ans. 731. 10s. 17. What cost 72 stones of wool at 8s. 6d.? Ans. 301. 12s. 18. What cost 100 stones of coals at $1\frac{3}{4}d$? Ans. 14s. 7d.

19. What cost 108 cwt. of cheese at 1*l*. 5*s*. 3*d*. ? Ans. 136*l*. 7*s*.

20. What cost 120 cwt. of hops at 4l. 7s. 6d.? Ans. 525l.

21. What is the weight of 35 hhds. of sugar, each 14 cwt. 2 qr. 17 lb.? Ans. 512 cwt. 3 qr. 7 lb.

22. What quantity of land is there in 27 fields, each 15 ac. 2 ro. 19 poles, $22\frac{1}{2}$ yards? Ans. 421 ac. 3 ro. 13 po. $2\frac{1}{2}$ yds.

23. What quantity of ale is there in 49 casks,

each containing 54 gal. 3 qts. $1\frac{1}{2}$ pint? Ans. 2691 gal. 3 qts. $1\frac{1}{2}$ pt.

24. How much silver in 5 dozen dessert-spoons, each 2 oz. 11 dwt. 17 grains, and 6 dozen teaspoons, each 19 dwt. 23 grains? Ans. 18 lbs. 10 oz. 19 dwt. 12 grains.

RULE II. If the Multiplier is not the Product of any two or more numbers, first, Multiply by two such numbers as come nearest the given Multiplier, either greater or less. Next, Multiply the Multiplicand by the difference between this number and the Multiplier; then add or subtract the Product from that before found, according as the given number was greater or less than the assumed number.

25. What is the price of 17 pair of shoes at 6s. 3d.? Ans. 5l. 6s. 3d.

26. What is the value of 29 pair of stockings at 2s. 6d.? Ans. 3l. 12s. 6d.

27. What cost 37 pair of buckles at 4s. $4\frac{1}{2}d$? Ans. 8l. 1s. $10\frac{1}{2}d$.

28. What cost 46 gallons of whisky at 10s. 6d.? Ans. 24l. 3s.

29. What will the rent of a shop amount to in a year, at 14s. 8 d. a-week? Ans. 38l. 4s. 10d.

30. What cost 92 stones of flax at 9s. 83d.? Ans. 44l. 15s. 1d.

31. What cost 105 puncheons of rum at 241. 6s, 2d.? Ans. 25521. 7s. 6d.

32. What will 29 men's wages amount to in a year at $16s. 11\frac{3}{4}d$. each per week? Ans. 1280l.4s.7d.

33. What is the value of 39 oxen at $15l. 7s. 11\frac{1}{4}d$, each? Ans. 600*l.* 9s. $6\frac{8}{4}d$.

34. What is the value of 23 acres of turnips at 19l. 17s. $9\frac{3}{4}d$. per acre? Ans. 457l. 9s. $8\frac{1}{4}d$.

35. What must a farmer pay for cutting down his crop, supposing that he employs 63 reapers for 3 weeks at 2s. $5\frac{3}{2}d$. per day? Ans. 140*l*. 11s. $4\frac{1}{5}d$. RULE 111. When the Multiplier is large, multiply as many times by 10 as there are figures in the Multiplier above the unit's place; then multiply the Product of the last 10 by the left-hand figure, and the Product above that of the last 10 by the next figure, and so on till you have multiplied by all the figures in the Multiplier; then add the Products.

36. What will a man's wages amount to in 253 days at 1s. $4\frac{1}{2}d$. a-day? Ans. 17l. 7s, $10\frac{1}{2}d$.

37. A gentleman's yearly income is 500l. and he spends daily 19s. 1d., reckoning 365 days to a year; how much does he spend? and how much does he save yearly? Ans. Spends 348l. 5s. 5d.; saves 151l. 14s. 7d.

38. If a traveller's expenses are 2l. 13s. $4\frac{1}{2}d$. aday, what will they amount to in 486 days? Ans. 1297l. Os. 3d.

39. What cost 4880 cwt. at 18s. $7\frac{1}{4}d$.? Ans. 4539l. 8s. 4d.

40. What cost 3789 quarters of wheat at 3*l*. 17s. $6\frac{1}{4}d$? Ans. 14686*l*. 6s. $5\frac{1}{4}d$.

41. What is the rent of a farm containing 1786 acres at 2l. 11s. $2\frac{3}{2}d$. p. acre? Ans. 4574l. 15s. $3\frac{1}{2}d$.

42. What is the weight of 345 hogsheads of sugar, each 14 cwt. 1 qr. 20 lb.? Ans. 4977 cwt. 3 qr. 12 lb.

43. If a fleece of wool weigh 3 st. 1 clove, 5 lb., what will be the weight of 2430 fleeces, each fleece being supposed to contain the same quantity of wool? Ans. 9372 st. 1 clove, 5 lb.

44. How much wine will 46 casks contain, each holding 243 gallons, 2 qts. 1 pint? Ans. 11206 gal. 3 qts.

45. How much will a mill grind in a year at 2 qr. 3 bush. 3 pks. a-day? Ans. 901 qr. 3 pks.

46. What is the weight of 20 hogsheads of tobacco, each 4 cwt. 1 qr. 18 lb. 12 oz.? Ans. 4 ton 8 cwt. 1 qr. 11 lb.

BILLS OF PARCELS.

BILLS OF PARCELS.

1. A Hosier's Bill.

Mr John Grant

			Bou	ght of	Ja	mes	Brow	m.
1882.				-	s.	d.		
Jan. 4. 8 pa	air wor	sted s	tocking	rs, at	2	6		
9 p	air thr	ead	ditto,	at	3	1		
7 p	air sill	C (ditto,	at	12	101		
10 p	air cot	ton	ditto,	at	5	83		
	air hos		ŕ	at	1	9		
				A	ns.	£10	2	2

2. A Stationer's Bill.

Mr George Young

Bought of David Scott.

Feb. 15. 20 reams post paper, at 11. 1s.

- 18 reams foolscap, at 14s. 6d.
- 24 reams printing demy, at 18s. 10d.
- 30 reams royal, at 21. 4s. 2d.

6 reams cartridge, at 12s. 8d.

4 cwt. pasteboard, at 17s. 61d.

Ans. £130 4 2

3. A Woollen Draper's Bill.

Mr Richard Reid

1882.

1882.

Bought of Joseph Black. Feb. 24. 13 yards serge, at 3s. 6d.

- 18 yards drugget, at 1s. 44d.
- 25 yards scarlet cloth, at 18s. 9d.
- 14 yards black ditto, at 17s. 113d.
- 20 yards shalloon, at 1s. 10d.
- 17 yards drab, at 3s. 2d.

Ans. £44 1 21

COMPOUND DIVISION.

RULE 1. Place the Divisor and Dividend as in Simple Division.

2. Begin at the highest denomination of the Dividend. divide as in Simple Division ; and reduce the Remainder, if any, to the next lower denomination, adding the given number of that name ; divide this sum, and proceed in the same manner with all the denominations. The several parts of the Quotient, thus found, will be the answer required.

PROOF. By Multiplication.

EXAMPLES.

1. Divide 31. 10s. by 2. Ans. 11. 15s.

2. Divide 81. 6s. 6d. by 3. Ans. 21. 15s. 6d.

Divide 91. 10s. 10d. by 4. Ans. 21. 7s. 8¹/₂d.
 Divide 181. 16s. 9¹/₄d. by 5. Ans. 31. 15s. 4¹/₄d.

5. Divide 171. 13s. by 6. Ans. 21. 18s. 10a.

6. Divide 201. 6s. 7d. by 7. Ans. 2l. 18s. 1d.

7. Divide 21l. 8s. by 8. Ans. 2l. 13s. 6d.

8. Divide 2711. 1s. 21d. by 9. Ans. 301. 2s. 4 td.

9. Divide 431. 16s. 0 d. by 10. Ans. 41. 7s. 7 d.

10. Divide 3401. 10s. by 16. Ans. 211. 5s. 7 d.

11. Divide 2481. 17s. 31d. by 35. Ans. 7l. 2s. $2\frac{1}{2}d$.

12. Divide 35901. 12s. 6d. by 53. Ans. 671. 14s. 11 1d. 38.

13. Divide 5672l. 14s. by 96. Ans. 59l. 1s. 93 d.

14. Divide 6301. 7s. 81d. by 365. Ans. 11. 14s. 6 d.

15. Divide 178431. 18s. 101d. by 801. Ans. 221. $5s. 6 \frac{1}{2}d.$

16. Divide 345 cwt. 1 gr. 8 lb. by 11. Ans. 31 cwt. 1 gr. 16 lb.

17. Divide 47 lb. 2 oz. 13 dwt. by 7. Ans. 6 lb. 8 oz. 19 dwt.

18. Divide 19 lb. 6 oz. 3 dr. 2 scr. by 5. Ans. 3 lb. 10 oz. 7 dr. 8 gr.

19. The proprietor of a vineyard sold in equal quantities to 25 of his customers, 42834 gal. 1 qt. 1 pt. of wine; how much did each purchase? Ans. 1713 gal. 1 qt. 1 pt.

20. Divide 540 yards, 3 qr. 1 nl. by 28. Ans. 19 yards, 1 quarter, 1_{24} nail.

21. Divide 51 acres, 1 rood, 11 poles, by 51. Ans. 1 acre, 1 pole.

22. Divide 307 gallons, 1 pint, by 63. Ans. 4 gallons, 3 quarts, 1 pint.

23. If seven casks weigh 2 tons, 7 cwt. 3 quarters, 14 lb., what does 1 cask weigh? Ans. 6 cwt. 3 quarters, 10 lb.

24. If 6 lb. of tea cost 1*l*. 7*s*., what will 1 lb. cost? Ans. 4*s*. 6*d*.

25. If 9 pair of gloves cost 1*l*. 8s. $10\frac{1}{2}d$., what is that per pair? Ans. 3s. $2\frac{1}{2}d$.

26. Bought 12 lb. of beef for 4s. 3d. What did it cost the lb.? Ans. $4\frac{1}{4}d$.

27. Bought 24 gallons of rum for 16l. 15s. 6d. What did it cost per gallon? Ans. $13s. 11\frac{3}{4}d.$

28. If 29 yards of cloth cost 5l. 2s. $1\frac{1}{4}d^{*}$, what cost 1 yard? Ans. 3s. $6\frac{1}{4}d$.

29. A piece of land containing 45 acres is let for 113*l*. 12*s*. 6*d*. What is it let at per acre? Ans. 2*l*. 10*s*. 6*d*.

30. If a man spends 128*l*. 11*s*. 2*d*. in 12 months, what is that per month? Ans. 10*l*. 14*s*. $3\frac{1}{2}d$.

31. Three men make an adventure, each equally concerned, whereby they clear 740*l*. What was each man's share of the gain? Ans. 246*l*. 13s. 4d.

32. What is the value of 1 yard of cloth, when 4 yards cost 51l. 7s. 3d.? Ans. 12s. $2\frac{3}{2}d$.

33. A prize of 3850*l*. is to be equally divided among 742 sailors. What is each man's share. Ans. 5*l*. 3s. $9\frac{1}{4}d$. $9\frac{6}{42}$.

34. A gentleman has 560l. 12s. a-year. How

much is that a-month, a-week, and a-day? Ans. 46l. 14s. 4d. a-month; 10l. 15s. $7\frac{1}{4}d$. $\frac{2}{5}\frac{8}{2}$. a-week 1l. 10s. $8\frac{1}{2}d$. $\frac{1}{6}\frac{6}{5}\frac{9}{2}$. a-day.

When the Divisor is of different denominations.

RULE. Reduce both the Divisor and Dividend to the same denomination, and then proceed as in Simple Division.

35. A gentleman distributed 61. 12s. among some poor people, and gave each 5s. 6d. How many poor were there? Ans. 24.

36. The revenues of an infirmary amount to 1152*l*. 10s. 6d. How many patients will it maintain, when each patient requires 9*l*. 10s. 6d.? Ans. 121.

37. A farm is let at 1*l*. 2s. 6d. per acre, and the rent amounts to 569*l*. 16s. 3d. How many acres does it contain? Ans. 506 acres, 2 roods.

38. How long must a tradesman work, who gains 1s. 4d. a-day and spends $7\frac{1}{2}d$., in order to pay a debt of 201. 17s. $2\frac{1}{2}d$.? Ans. 589 days.

SUPPLEMENT TO COMPOUND MULTIPLICATION AND DIVISION.

I. When the Multiplier contains a fraction.

RULE. First multiply by the whole number, then multiply by the upper figure of the fraction, and divide by the lower figure, and add the Quotient to the former Product.

39. What cost $8\frac{3}{8}$ yds. at 14s. $6\frac{1}{2}d$? Ans. 6l. 1s $9\frac{1}{4}d$. $\frac{3}{4}$.

40. What cost 123 lb. at 6s. 2d.? Ans. 3l. 18s. 7 d.

41. What cost 14§ yards at 11s. $9\frac{3}{4}d$? Ans. 8*l*. 12s. $9\frac{9}{4}d$.

42. What cost 29 $\frac{1}{3}$ bushels of wheat at 15s. $6\frac{3}{4}d$.? Ans. 22l. 16s. 6d.

43. What cost $46\frac{5}{8}$ cwt. of hay at 6s. $7\frac{3}{4}d$. ? Ans. 15*l*. 8s. $2\frac{1}{4}d$. $\frac{5}{8}$.

44. Multiply 20 lb. 2 oz. 7 dwt. 21 gr. by 4³/₈. Ans. 92 lb. 11 oz. 5²/₇ grs. 45. Multiply 24 cwt. 1 qr. 14 lb. 10 oz. by 8%. Ans.202 cwt. 1 lb. 2% oz.

46. Multiply 20 m. 3 fur. 30 po. 2 yds. by 9§. Ans. 197 m. 7 fur. 1 yd.

47. Multiply 120 yds. 2 qr. 1 nl. by 10⁴. Ans. 1259 yds. 3¹/₂ nl.

48. Multiply 40 ac. 3 ro. 30 po. by 115. Ans. 467 ac. 3 ro. 174 po.

49. Multiply 57486 gallons, 3 quarts, 1 pint of wine by 7²/₅. Ans. 440732 gallons, 2 quarts, 1[§] pint.

II. When the Divisor contains a fraction.

RULE. Multiply both the Divisor and Dividend by the ander figure of the fraction, adding the upper figure to the Product of the Divisor, then divide the Product of the Dividend by the sum.

50. Bought $17\frac{1}{4}$ bolls of potatoes for 8*l*. 12*s*. 6*d*. What did they cost per boll? Ans. 10*s*.

51. Bought 131 yds. of cloth for 151. What did it cost per yard? Ans. 11. 2s. 6d.

52. Bought 22⁴/₄ stones of beef for 12*l*. 6s. 8¹/₄. What did it cost per stone? Ans. 10s. 10d. ¹⁹/₄.

53. Divide 276*l*. 16s. 8d. among 5 men and a boy, and give the boy $\frac{2}{5}$ of a man's share. Ans. A man's share, 48*l*. 17s. $0\frac{1}{2}d$. $\frac{1}{4}$. Boy's share, 32*l*. 11s. $4\frac{1}{4}d$. $\frac{1}{5}$.

54. Divide 2001. 14s. 6d. among 9 men and 7 women; and give a woman $\frac{5}{2}$ of a man's share. Ans. A man's share, 13l. 10s. $7\frac{1}{2}d$. $\frac{5}{2}\frac{5}{5}$. A woman's 11l. 5s. $6\frac{1}{2}d$. $\frac{5}{2}\frac{5}{5}$.

55. A, B, and C, have a ship in company: A has $\frac{4}{5}$, B $\frac{1}{4}$, and C $\frac{1}{4}$: they receive of freight for a voyage, 114*l*. 8s. 4d. What is each man's share of the freight? Ans. A's share, 71*l*. 10s. $2\frac{1}{4}d$. B's 28*l*. 12s. 1d. C's 14*l*. 6s. $0\frac{1}{4}d$.

BILLS OF PARCELS.

BILLS OF PARCELS.

4. A Grocer's Bill.

Mr Robert Ross		
1882.		Bought of William Smith,
March 1. 24 lb. lump sugar,	at	10 1 <i>d</i> .
26 lb. powder do.,	at	8 <u>å</u> d.
16 lb. soap,	at	71d.
4 lb. starch,	at	1s. 2d.
15 lb. tea,	at	4s. 6d.

Ans. £6 1 91

Bought of James Skinner.

5. A Leather Merchant's Bill.

Mr Gilbert Bruce 1882. April 5. 28 calf skins, at 48. 81d. 29 lamb do., at 81d. 34 sheep do., 1s. 3d. at 17 buck do., at 8s. 6d. 18 cow hides. 12s. 73d. at 110 lb. leather, 28. 8d. at

M. Oberlas Desert

Ans. £42 19 8

6. A Linen-Draper's Bill.

1882.	ies mussei			Bought of	f Adam	Waugh.
May 20.	453 yards	cambric,	at	11s. 6d.		0,
	355 yards	muslin,	at	$4s. 8\frac{3}{4}d.$		
	26 ⁷ / ₈ yards			3s. 4d.		
	234 yards		at	5s. 3d.		
	101 ells di		at	$1s. 4\frac{1}{2}d.$		
	$13\frac{3}{4}$ ells de	owlas, "	at	1s. 6d.		

Ans. £46 16 113 3

7. A Druggist's Bill.

Mr Samuel Orr		
1882.		Bought of Jones Paul,
June 4. 181 lb. rhubarb,	at	11. 10s. per lb.
14 lb. opium,	at	$18s.\ 11\frac{1}{2}d.$
371 lb. gum-arabic,	at	1s. 10d.
112 ³ / ₄ lb. jesuit's bark,	at	3s. 6d.

Ans. £64 3 01

D

SIMPLE PROPORTION

Teaches from three given numbers to find a fourth.

Of the three given numbers two are always of the same kind: the other is of the same kind as the fourth, or number required in the question.

RULE 1. Put down that number which is of the same kind with the number required for the third term.

2. Consider whether the answer ought to be greater or less than this number; if greater, make the greater of the two remaining numbers the second term, and the less the first : but if less, make the less of the two remaining numbers the second, and the greater the first term.

3. If the first and second terms are of different denominations, reduce them to the same, and the third to the lowest denomination mentioned in it.

4. Multiply the second and third terms together, and divide their product by the first; the quotient will be the answer in the same denomination to which the third term was reduced, and it may either be brought to a higher or reduced to a lower denomination, according as the answer requires.

PROOF. Invert the question.

Note 1. Multiply and divide as in Compound Multiplication and Division, when found convenient.

2. When the first number is 1, the answer is found by Multiplication. When the second or third number is 1, then the answer is found by Division.

3. If the first number, and either the second or third, can be exactly divided by the same divisor, let them be divided, and the quotients used instead of the original numbers.

4. To find a common measure: Divide the Divisor by the Remainder continually till nothing remain; the last Divisor is the common measure: then divide the Remainder and Divisor by it, and the quotient will be the lowest terms.

[The Method of Unity may also be employed. Thus, to find the answer to the question, " If 12 yards of cloth cost 11. 7s., what will 96 yards cost?"

If 12 yards cost 1*l*. 7*s*., Then, 1 yard will cost $\frac{27s}{12} = 2s$. 3*d*.

96 yards will therefore cost 2s. 3d. \times 96 = 10l. 16s.]

EXAMPLES.

1. If 2 yards of cloth cost 4s. 6d., what will 16 yards cost? Ans. 11. 16s. 2. If 16 yards of cloth cost 11. 16s., what will

2 yards cost? Ans. 4s. 6d.

3. If 41 yards cost 12s. 81d., what will 20 yards cost? Ans. 21. 16s. 53d. 1.

4. If 20 yards cost 21. 16s. 53d. 1., what will 41 yards cost? Ans. 12s. 81d.

5. If $1\frac{1}{4}$ yard cost 2s. 6d., what cost $24\frac{1}{4}$ yards? Ans. 21. 9s.

6. If 241 yards cost 21. 9s., what will 11 yard cost? Ans. 2s. 6d.

7. If 1 lb. of sugar cost $10\frac{1}{2}d$, what will $1\frac{1}{2}$ cwt. cost? Ans. 71. 7s.

8. If 11 cwt. of sugar cost 7l. 7s., what will 1 lb. cost? Ans. $10\frac{1}{2}d$.

9. If $1\frac{1}{4}$ oz. of tea cost $6\frac{3}{4}d$, what will 24 lb. cost? Ans. 81. 12s. 91d. 2.

10. If 24 lb. cost 81. 12s. 91d. 2., what will 11 oz. cost? Ans. $6\frac{3}{4}d$.

11. If 1 oz. of coffee cost $6\frac{1}{2}d$, what will $2\frac{1}{2}$ cwt. cost? Ans. 1211. 6s. 8d.

12. If $2\frac{1}{5}$ cwt. of coffee cost 121*l*. 6s. 8d., what will 1 oz. cost? Ans. $6\frac{1}{2}d$.

13. If three quarters of cloth cost 3s. 6d., how much will three pieces, each 301 yards, cost? Ans. 211. 7s.

14. If three pieces of cloth, each 301 yards, cost 211. 7s., what will \$ of a yard cost? Ans. 3s. 6d.

15. If 4 cwt. 1 qr. 14 lb. of tobacco cost 40L 16s. 8d., what cost 1 ounce? Ans. $1\frac{1}{4}d$.

16. If 1 oz. cost $1\frac{1}{4}d$, what will 4 cwt. 1 gr. 14 lb. cost? Ans. 401. 16s. 8d.

17. If $1\frac{1}{2}$ oz. of snuff cost $2\frac{1}{2}d$., what cost 5 cwt. 3 qr. 18 lb.? Ans. 73*l*. 11s. $1\frac{1}{4}d$. $\frac{1}{3}$.

18. If 5 cwt. 3 qr. 18 lb. cost 73*l*. 11s. $1\frac{1}{4}d$. $\frac{1}{3}$., what cost $1\frac{1}{2}$ oz.? Ans. $2\frac{1}{2}d$.

19. If $1\frac{1}{2}$ lb. cost $1\frac{1}{2}d$., what will 2 tons weight cost? Ans. 18*l*. 13*s*. 4*d*.

20. What must I pay for 126 gallons of wine at 13s. 6d. the gallon? Ans. 85l. 1s.

21. If $3\frac{1}{2}$ ewt. of cheese cost 8*l*. 11*s*. 6*d*., what is that per lb.? Ans. $5\frac{1}{4}d$.

22. What is the price of 10 cheeses, each $15\frac{1}{4}$ lb., at $6\frac{3}{4}d$. the lb.? Ans. 4l. 5s. $9\frac{1}{4}d$. $\frac{1}{2}$.

23. A gentleman spends 17l. 13s. $9\frac{1}{2}d.$ a-week, and puts into the bank, at the year's end, 500l. What is his yearly income? Ans. 1422l. 7s. $8\frac{1}{2}d.$

24. If the daily expenses of the inhabitants of Edinburgh and Leith be 3240*l*. 9s. $9\frac{1}{2}d$. for maintenance, how much will support them $2\frac{1}{2}$ years? Ans. 2956946*l*. 14s. $10\frac{3}{2}d$.

25. If 1 yard of cloth cost 6s. 2d., what cost 5 quarters? Ans. 7s. $8\frac{1}{2}d$.

26. If a ton of iron cost 23*l*. 6s. 8*d*., what will $2\frac{1}{2}$ lb. cost? Ans. $6\frac{1}{4}d$.

27. If a manufacturer receives 1s. $6\frac{1}{2}d$. a-day for every week-day, how much will his wages amount to in a year? Ans. 24l. 2s. $6\frac{1}{2}d$.

28. Å farm, containing 400 acres, 2 ro. 20 poles, is let at 2*l*. 2s. per acre, what is the yearly rent of that farm? Ans. 841*l*. 6s. 3*d*.

29. If 1 quarter of oats cost 18s. 8d., how much will 61 quarters 7 bushels cost? Ans. 57l. 15s.

30. If 100 yards of cloth cost 20*l*. 9s. 4*d*., how many yards may I buy for 6s. $4\frac{3}{4}d$? Ans. 1 yd. 2 qr. 1 nl.

31. If 4 casks of raisins, each weighing 1 cwt.

2 qr. 16 lb. cost 23*l.*, I demand the value per cwt.? Ans. 3*l.* 10s.

32. What will a tax on 900l. amount to at 2s. 6d. the pound? Ans. 112l. 10s.

33. A bankrupt owes his creditors 1200*l.*, pays them only 750*l*. How much does he pay them per pound? Ans. 12s. 6d.

34. A bankrupt pays his creditors 12s. 6*d*. per pound, pays them in all 750*l*. What was his debt? Ans. 1200*l*.

35. A bankrupt owes his creditors 9000l. 10s. How much will he pay them at 15s. 6d. per pound? Ans. 6975l. 7s. 9d.

36. If 1 dwt. of gold costs 4s., what cost 6 pieces each $2\frac{1}{4}$ lb.? Ans. 648l.

37. If $1\frac{8}{4}$ oz. of silver plate cost 9s. $7\frac{1}{2}d$, what is the price of $24\frac{1}{2}$ lb.? Ans. 80l. 17s.

38. If 14 packs of wool, each 18 stones, cost 109*l*. 4s., what is that per lb.? Ans. $7\frac{1}{4}d$. §.

39. A trader bought 100 lb. of tea at 5s. 6a. per lb., but finding it of an inferior quality, he is willing to lose 2l. 10s. upon the whole. At what rate must he retail it per ounce? Ans. $3\frac{3}{4}d$.

40. If 30 gallons of water in 1 hour fall into a cistern containing 200 gallons, and there run out $22\frac{1}{2}$ gallons in one hour, in how many hours will the cistern be filled, if both the cocks keep running? Ans. 26 hours, 40 minutes.

41. If 2 cwt. 2 qr. 24 lb. of soap be bought for 8l. 13s. 4d., at how much must it be sold per lb. to gain 2l. 2s. on the whole? Ans. $8\frac{1}{2}d.$

42. A merchant bought 1008 gallons of oil for 640l.; it leaked out 48 gallons: at what rate must he sell it per gallon, so as to be no loser by it? Ans. 13s. 4d.

43. A draper bought 240 yards of broad cloth, and gave for it after the rate of 16s. $10\frac{1}{2}d$. the ell English. How much did he pay for the whole? Ans. 162l.

44. The valued rent of a parish amounts to 5840l. and a rate is granted of 109*l*. 10*s*. for the poor. What is that per pound? Ans. $4\frac{1}{2}d$.

45. A garrison has provisions for eight months, at the rate of 14 oz. to each person per day. How much must be allowed per day, in order that the provisions may last $10\frac{1}{2}$ months? Ans. 10 oz. $10\frac{2}{3}$ dr.

46. What is the interest of 47l. for a year at $4\frac{1}{2}l$. per cent.? Ans. 2l. 2s. $3\frac{1}{2}d$. $\frac{2}{2}$.

47. If 14 men perform a piece of work in 6 days, working 10 hours a-day, in what time will 24 men perform it? Ans. 3 days, 5 hours.

48. If the sixpence loaf weighs 3 lb. when wheat is at 30s., how much should it weigh when wheat is at 1l. 4s.? Ans. 3 lb. 12 oz.

49. What cost 50 pints of whisky, at $3\frac{1}{2}d$. per gill? Ans. 21. 18s. 4d.

50. Bought 4 cwt. 2 qr. 20 lb. of coffee for 113*l*. 10s. 8*d*. and retailed it at $3\frac{3}{4}d$. the ounce. What was the net gain? Ans. 17*l*. 9s. 4*d*.

51. If $1\frac{1}{2}$ peck of potatoes cost $10\frac{1}{2}d$, what will be the value of 40 qrs. 4 bu. 3 pks. of the same? Ans. 37l. 17s. 9d.

52. What is the value of $900\frac{1}{2}$ acres of land at three farthings the square vard? Ans. 13620*l*. 1s. 3*d*.

53. How much cloth at 6s. 8d. per yard ought to be given in barter for 13 cwt. 2 qr. of sugar, at 3l. 2s. 6d. per cwt.? Ans. 126 yards, 2 qr. 1 nl.

54. If a tailor can make a coat and vest with $3\frac{3}{4}$ yards of cloth, which is $1\frac{1}{2}$ yard broad, how many yards will he require to make the same when the breadth is only 3 qr.? Ans. $7\frac{1}{2}$ yards. 55. Bought for ready money $400\frac{1}{2}$ yards of shalloon, at 1s. $8\frac{1}{4}d$. a-yard— $54\frac{1}{4}$ yards of flannel, at 1s. 6d.—20 bushels of meal, at 14s. $6\frac{1}{2}d$.—106 lb. clover seed, at $8\frac{3}{4}d$.—14 $\frac{1}{2}$ stones iron, at 3s. $9\frac{1}{2}d$., and 31 casks train oil, at 1*l*. 4s. 6d. I demand the price of the whole? Ans. 96*l*. 19s. $9\frac{3}{4}d$. $\frac{1}{6}$.

56. Bartered $20\frac{1}{2}$ cwt. of sugar, at 3l. 4s. and 150 lb. tea, at $4\frac{1}{2}d$. per ounce, for $96\frac{1}{4}$ yards calico, at 4s. 2d. and $144\frac{3}{4}$ yards diaper, at 2s. $4\frac{1}{2}d$. How much money must be received besides the above? Ans. 73l. 7s. $2\frac{6}{4}d$. $\frac{1}{2}$.

8. BOOK DEBTS.

Mr James Brown, Dr. 1882.

To John Green,

- June 3. To $305\frac{1}{2}$ bushels salt, at 2s. 6d. per bushel.
 - 24. To $40\frac{1}{4}$ reams paper, at $17s. 6\frac{3}{4}d$. per ream.
- July 20. To 4091 gals. rum, at 13s. 4d. per gal.
 - 28. To 24 tons, 10 cwt. 2 qrs. cheese, at $6\frac{1}{4}d$. per lb.
- Aug. 1. To 1 ton, 1 qr. 7¹/₂ lb. sugar, at 8¹/₂d. per lb.
 - 15. To $283\frac{1}{2}$ gal. whisky, at $2\frac{1}{4}d$. per gill.
- Sept. 7. To 59 qrs. 5 bush. $2\frac{1}{2}$ pks. of meal, at $10\frac{1}{2}d$. per peck.

Ans. £2026 7 74 3

COMPOUND PROPORTION

Teaches from five given numbers to find a sixth. Of the five given numbers two are always of the same kind with other two, and the remaining one the same as the number required.

RULE I. Put down that number which is of the same kind with the number required for the third term.

2. Take two terms of the same kind with each other, and state them as in Simple Proportion; then take other two terms of the same kind, and state them in the same manner under the former, and so on till all the terms are stated.

3. Reduce like terms to the same name, and the third to the lowest name in it.

4. Multiply together the terms which stand below each other, which will reduce them to three; then multiply the second by the third, and divide the Product by the first, the Quotient will be the answer in the same name with the third term.

PROOF. Invert the question.

1. If 100l. in 12 months gain 5l. of interest, what will 60l. gain in 9 months? Ans. 2l. 5s.

2. If 100l. in 12 months gain 5l. interest, what principal will gain 2l. 5s. in 9 months? Ans. 60l.

3. If 100*l*. gain 5*l*. in 12 months, in what time will 60*l*. gain 2*l*. 5*s*.? Ans. 9 months.

4. If the interest of 60*l*. for 9 months be 2*l*. 5*s*. required the rate per cent. per annum? Ans. 5*l*.

5. If 24 acres of grass be mowed by 16 men in 21 days, how many acres may be mowed by 48 men in 84 days? Ans. 288.

6. If 3 horses in 7 days eat 14 pecks of corn, what quantity will serve 24 horses 52 weeks? Ans. 1456 bushels.

7. If 12 reapers cut 14 acres of corn in 6 days, how many acres will 48 reapers cut in 24 days? Ans. 224 acres.

8. If the wages of 8 men for 6 days be 3l. 10s., how much will pay 64 men for 32 days' work? Ans. 149l. 6s. 8d.

9. If 2 horses plough $4\frac{1}{2}$ acres of land in 6 days, when they work eight hours a-day, how many acres

52

will 16 horses plough in 156 days, when they work 12¹/₂ hours a-day? Ans. 1462 ac. 2 ro.

10. If a regiment of 654 soldiers consume 117 quarters of wheat in 45 days, how many soldiers will consume 468 quarters in 9 days? Ans. 13080.

11. If 20 roods of ditching be wrought by 4 men in 12 days, working 14 hours a-day, how many will be done by 6 men in 4 days, when they work only 8 hours a-day? Ans. 5 roods, 25 yds. 63 feet.

12. If a carrier receives 6l. 8s. for the carriage of 4 cwt. 248 miles, how much ought he to receive for the carriage of 8 cwt. 3 qr. 14 lb. for 62 miles? Ans. 3l. 11s.

13. If 20 masons build a wall 50 feet long, 2 teet thick, and 14 feet high, in 12 days, in how many days will 60 masons build a wall 500 feet long, 4 thick, and 16 high? Ans. $91\frac{3}{4}$ days.

14. If a thousand men besieged in a town with provisions for 5 weeks, allowing each man 16 oz. a-day, be reinforced with 500 men more, and hearing that they cannot be relieved till the end of 8 weeks, how many ounces a-day must each man have, that the provisions may last that time? Ans. $6\frac{2}{3}$ oz.

15. If 660 yards of a road, which was to be 1 mile in length, be done by 24 men in 30 days, in what time will 30 men finish it? Ans. 40 days.

16. A farmer engaged 60 reapers to cut down his crop in 30 days, bu⁴ after 10 days' work he engaged 40 more. In what time will it be cut down? Ans. 22 days.

17. If 24 men perform a piece of work in 20 days, how many men must be employed upon **a** piece of work 6 times as large, that it may be finished in one-fifth of the time? Ans. 720 men.

18. If a chest, 12 feet long, 6 deep, and 5 broad.

PRACTICE.

contains 40 quarters of oats, what must be the length of another, 5 feet deep and 3 broad, to contain 30 quarters? Ans. 18 feet.

RULES OF PRACTICE.

Practice is so called from the great use thereof by persons concerned in trade and business.

	TABLE OF ALIQUOT PARTS	
of a Shilling.	of a Pound.	of a Curt.
d. s.	s. d. £	lb. cwt.
$1 = \frac{1}{12}$	$1 3 = \frac{1}{16}$	$56 = \frac{1}{2}$
$1\frac{1}{2} = \frac{1}{2}$	$14 = \frac{10}{15}$	$28 = \frac{1}{4}$
$2^{2} = \frac{1}{4}$	$1 = \frac{1}{20}$	$16 = \frac{1}{4}$
$3 = \frac{3}{4}$	$1 8 = \frac{1}{12}$	$14 = \frac{1}{4}$
$4 = \frac{4}{1}$	$2 = \frac{1}{10}$	$8 = \frac{1}{14}$
$6 = \frac{3}{4}$	$26 = \frac{10}{10}$	$7 = \frac{1}{16}$
of a Sixpence.	34 = 1	lb. of a gr.
d.	4 = 4	$14 = \frac{1}{4}$
$3 = \frac{1}{2}$	$5 = \frac{1}{2}$	$7 = \frac{1}{4}$
$2 = \frac{1}{1}$	$6.8 = \frac{4}{1}$	4 1
$1\frac{1}{2} = \frac{3}{4}$	$10 = \frac{3}{10}$	$3\frac{1}{3} = \frac{1}{4}$
$\frac{12}{3} = \frac{4}{1}$	- 2	·2 - 8
A 8		

RULE 1. If the price is an aliquot part of a penny, shilling, or pound, the same part of the given quantity will be the answer in pence, shillings, or pounds, accordingly. 2. If the price is not an aliquot part of a penny, shilling,

2. If the price is not an aliquot part of a penny, shilling, or pound, divide it into divisions and subdivisions, so that each of them shall either be an aliquot part of a penny, shilling, or pound, or of a greater division, and the same parts of the given quantity added together will be the answer as formerly.

3. If the price contains pounds, multiply the given quantity by the number of them, take parts for the shillings, pence, and farthings, if there be any, as directed in the preceding rules, and the sum of the whole will be the answer.

4. If the given quantity contains a fraction, find the value of the integral part by any of the rules already given, then multiply the price by the numerator of the fraction, and divide the product by the denominator, and the result added to the value of the integral part will be the answer.

PRACTICE.

Note. In the same manner aliquot parts of weights and measures may be taken.

EXAMPLES.

1. 348 at $\frac{1}{4}$, $\frac{1}{2}$, $\frac{3}{4}d$. Ans. 7s. 3d.? 14s. 6d.; 1l. 1s. 9d.

2. 560 at 1, $1\frac{1}{4}$, $1\frac{1}{2}$, $1\frac{3}{4}d$. Ans. 2*l*. 6*s*. 8*d*.; 2*l*. 18*s*. 4*d*.; 3*l*. 10*s*.; 4*l*. 1*s*. 8*d*.

3. 430 at 2, $2\frac{1}{4}$, $2\frac{1}{2}$, $2\frac{3}{4}d$. Ans. 3*l*. 11*s*. 8*d*.; 4*l*. 0*s*. $7\frac{1}{2}d$.; 4*l*. 9*s*. 7*d*.; 4*l*. 18*s*. $6\frac{1}{2}d$.

4. 96 at 3, $3\frac{1}{4}$, $3\frac{1}{2}$, $3\frac{3}{4}d$. Ans. 1*l*. 4s.; 1*l*. 6s.; 1*l*. 8s.; 1*l*. 10s.

5. 84 at 4, $4\frac{1}{4}$, $4\frac{1}{2}$, $4\frac{3}{4}d$. Ans. 1*l.* 8s.; 1*l.* 9s. 9d.; 1*l.* 11s. 6d.; 1*l.* 13s. 3d.

6. 54 at 5, $5\frac{1}{4}$, $5\frac{1}{2}$, $5\frac{3}{4}d$ Ans. 1*l.* 2s. 6d.; 1*l.* 3s. $7\frac{1}{2}d$.; 1*l.* 4s. 9d.; 1*l.* 5s. $10\frac{1}{2}d$.

7. 45 at 6, $6\frac{1}{4}$, $6\frac{1}{2}$, $6\frac{3}{4}d$. Ans. 1*l.* 2s. 6d.; 1*l.* 3s. $5\frac{1}{4}d$.; 1*l.* 4s. $4\frac{1}{5}d$.; 1*l.* 5s. $3\frac{3}{4}d$.

^{*}8. ⁵8 at 7, $7\frac{1}{4}$, $7\frac{1}{2}$, $7\frac{3}{4}d$. Ans. 1l. 13s. 10d.; 1l. 15s. $0\frac{1}{2}d$.; 1l. 16s. 3d.; 1l. 17s. $5\frac{1}{2}d$.

9. \$5 at 8, $\$\frac{1}{4}$, $\$\frac{1}{2}$, $\$\frac{3}{4}d$. Ans. 2*l*. 16*s*. 8*d*.; 2*l*. 18*s*. $5\frac{1}{4}d$.; 3*l*. 0*s*. $2\frac{1}{2}d$.; 3*l*. 1*s*. $11\frac{3}{4}d$.

10. 88 at 9, $9\frac{1}{4}$, $9\frac{1}{2}$, $9\frac{3}{4}d$. Ans. 3l. 6s.; 3l. 7s. 10d.; 3l. 9s. 8d.; 3l. 11s. 6d.

11. 57 at 10, $10\frac{1}{2}$, $10\frac{3}{2}d$. Ans. 2*l*. 7*s*. 6*d*.; 2*l*. 8*s*. $8\frac{1}{4}d$.; 2*l*. 9*s*. $10\frac{1}{2}d$.; 2*l*. 11*s*. $0\frac{3}{4}d$.

12. 94 at 11, 11 $\frac{1}{4}$, 11 $\frac{1}{2}$, 11 $\frac{8}{4}d$. Ans. 4*l*. 6*s*. 2*d*.; 4*l*. 8*s*. 1 $\frac{1}{2}d$.; 4*l*. 10*s*. 1*d*.; 4*l*. 12*s*. 0 $\frac{1}{2}d$.

13. 96 at 12, $12\frac{1}{4}$, $12\frac{1}{2}$, $12\frac{3}{4}d$. Ans. 4l. 16s.; 4l. 18s.; 5l.; 5l. 2s.

14. 100 at 1s. 1¹/₄d. Ans. 5l. 10s. 5d.

15. 200 at 2s. 2¹/₂d. Ans. 22l. 1s. 8d.

16. 256 at 3s. 3³/₄d. Ans. 42l. 8s.

17. 40 at 4s. 4¹/₄d. Ans. 8l. 14s. 2d.

- 18. 37 at 5s. 5¹/₄d. Ans. 10l. 1s. 11¹/₄d.
- 19. 24 at 6s. 6 d. Ans. 7l. 16s. 6d.

20. 19 at 7s. 7 d. Ans. 7l. 4s. 10 d.

PRACTICE.

21. 12 at 8s. 83 d. Ans. 51. 4s. 9d. 22. 18 at 9s. 91d. Ans. 8l. 15s. 101d. 23. 300 at 10s. $10\frac{1}{2}d$. Ans. 163*l*. 2s. 6d. 24. 408 at 11s. $11\frac{3}{4}d$. Ans. 244*l*. 7s. 6d. 25. 50 at 12s. 11d. Ans. 301. 5s. 21d. 26. 55 at 13s. $2\frac{1}{2}d$. Ans. 36l. 6s. $5\frac{1}{2}d$. 27. 68 at 14s. 3¹/₄d. Ans. 48l. 10s. 5d. 28. 54 at 15s. 4¹/₂d. Ans. 41l. 10s. 3d. 29. 490 at 16s. 51d. Ans. 4021. 14s. 41d. 30. 454 at 17s. $6\frac{3}{2}d$. Ans. 398l. 3s. 11d. 31. 898 at 18s. $7\frac{3}{2}d$. Ans. 837l. 3s. $11\frac{1}{2}d$. 32. 405 at 19s. $8\frac{1}{4}d$. Ans. 398l. 13s. $5\frac{1}{4}d$. 33. 276 at 11. 14s. Ans. 4691. 4s. 34. 358 at 3*l*. 18s. 4*d*. Ans. 1402*l*. 3s. 4d. 35. 541 at 2*l*. 6s. 8¹/₄*d*. Ans. 1262*l*. 17s. 11¹/₄*d*. 36. 256 at 5*l*. 12s. 2¹/₂*d*. Ans. 1436*l*. 5s. 4*d*. 37. 842 at 41.2s. 63 d. Ans. 34751. 17s. 7 d. 38. 2731 at 11. 9s. 4d. Ans. 4001. 15s. 4d. 39. 751 at 21. 17s. 10d. Ans. 21731. 1s. 9d. 40. 4083 at 15s. 6d. Ans. 316l. 15s. 7 d. 41. 7623 at 11. 12s. 6d. Ans. 12391. 4s. 6d. 42. 2315 at 7s. 91d. Ans. 901. 4s. 83d. 3. 43. 7 bushels, 3 pecks, at 14s. 6d. Ans. 5l. 12s. 4 d. 44. 30 acres, 3 roods, 20 poles, at 21. 10s. 6d. Ans. 771. 19s. 2¹/₄d. 45. 20 gallons, 3 quarts, 1 pint, at 21. 8s. 6d. Ans. 501. 12s. 5¹/₄d. 46. 24 cwt. 2 quarters, 14 lb., at 4l. 5s. 8d. Ans. 1051. 9s. $6\frac{1}{9}d$. 47. 8 cwt. 3 quarters, 16 lb., at 3l. 18s. 6d. Ans. 341. 18s. 19d. %. 48. 16 cwt. 1 quarter, 18 lb., at 2l. 16s. 10d. Ans. 461. 12s. 8ºd. 3. 49. 87 cwt. 3 quarters, 20 lb., at 31. 18s. 41d. Ans. 3441. 11s. 43d. 4.

50. 129 cwt. 2 quarters, 27 lb., at 4*l*. 1s. $7\frac{1}{2}d$. Ans. 529*l*. 10s. $1\frac{1}{4}d$. $\frac{29}{8}$.

51. 29 lb. 4 oz. 16 dwt., at 3*l*. 6*s*. 0*d*. Ans 97*l*. 0*s*. $4\frac{3}{4}d$. $\frac{1}{2}$.

52. 31 lb. 7 oz. 12 dwt. 16 gr., at 0l. 8s. 6d. Ans. 13l. 8s. $10\frac{3}{4}d$. $\frac{5}{15}$.

53. 36 yds. 3 qr. 1 nl., at 1*l*. 12s. $6\frac{1}{2}d$. Ans. 59*l*. 17s. $11\frac{1}{4}d$. $\frac{1}{3}$.

54. 59 qr. 3 bush. 3 pks., at 3*l*. 17*s*. $10\frac{1}{2}d$. Ans. 231*l*. 11*s*. $1\frac{1}{2}d$. $\frac{3}{5\pi}$.

55. 540 acres, 2 roods, 38 perches, at 4*l*. 15*s*. 6*d*. Ans. 2582*l*. 0*s*. 5 $\frac{9}{2}$ *d*. $\frac{1}{\sqrt{5}}$.

56. 784 yards, 6 feet, 36 inches, at $0l. 15s. 6\frac{1}{2}d.$ Ans. 609l. 15s. $5\frac{1}{2}d. \frac{1}{2}s.$

57. 963 cwt. 2 qr. 25 lb., at 4l. 18s. $6\frac{3}{4}d$. Ans. 4749l. 6s. $11\frac{1}{2}d$. $\frac{5}{7}s$.

58. 798 4 at 31. 17s. 6d. Ans. 30931. 5s. 8d.

59. 206_{17}^{+} at 1*l*. 16s. 10d. Ans. 379*l*. 18s. 6d. 60. 509_{35}^{-} at 15*l*. 16s. 8d. Ans. 8061*l*. 10s. 10d.

TARE AND TRET.

Gross weight is the full weight of any merchandise, together with that of the cask, or other package in which it is contained.

Tare is an allowance made to the purchaser for the weight of the package.

Tret is an allowance of 4 lb. on 104 lb. or $\frac{1}{25}$ on goods subject to waste.

Cloff is an allowance of 2 lb. on every 3 cwt. or $1\frac{1}{68}$, for the turn of the scale after tare and tret are deducted.

Suttle is when part of the allowance is deducted from the gross.

Net weight is what remains after all allowances are made.

1. In 15 hhds. of tobacco, each 2 cwt. 1 qr. 12 lb. gross; tare 1 qr. 4 lb. per hhd.; how much net weight? Ans. 31 cwt. 8 lb.

2. What is the net weight of 6 hhds. of tobacco, weighing 95 cwt. 2 qr. 8 lb. gross; tare 7 lb. per

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cwt., tret 4 lb. per 104 lb., cloff 2 lb. for every 3 cwt.? Ans. 85 cwt. 2 qr. 15_{1479}^{+79} lb.

3. Suppose 17½ lb. per cwt. tare, and 4 lb. per 104 lb. tret, were allowed on seven casks of prunes, each 3 cwt. 1 qr. 5 lb. gross, what would their ne weight be? Ans. 18 cwt. 2 qr. 23485 lb.

4. What is the net weight of 14 hhds. of sugar, each 15 cwt. 3 qr. 14 lb. gross, tare 1 qr. 14 lb. per hhd., and allowing tret and cloff? Ans. 207 cwt. 1 qr. 18_{π^5} lb. net.

5. What is the net weight of 19 bales of cotton, each 1 cwt. 3 qr. 10 lb. gross, tare 8 lb. per cwt., allowing also tret and cloff? Ans. 31 cwt. 0 qr. $1\frac{1}{2}\frac{2}{3}\frac{7}{2}$ lb. net.

6. What is the net weight of 30 tierces of coffee, each 8 cwt. 3 qr. 16 lb. gross, tare 18 lb. per cwt., alloying tret and cloff? Ans. 214 cwt. 0 qr. 1_{101772}^{80772} lb.

7. What is the value of 12 bales of pepper, each weighing 2 cwt. 2 qr. 22 lb., tare 3 lb. per bale, allowing also tret and cloff, at 1s. $3\frac{1}{4}d$. per lb.? Ans. 2171. 18s. $3\frac{1}{4}d$. $\frac{9}{8\pi}$.

8. In three casks of oil weighing 10 cwt. 1 qr. 11 lb., how many gallons, allowing 18 lb. per cwt. tare, and 71 lb. net, to a gallon? Ans. 129233 gal.

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RULE. As the whole stock or sum : is to the whole gain or loss, or the number to be divided : : so is each particular stock, or number : to the parts sought.

PROOF. Add the quotients.

1. Divide 140*l*. among 3 persons, so that their shares shall be to each other as 1, 2, and 3? Ans. 23*l*. 6s. 8*d*.—46*l*. 13s. 4*d*.—70*l*.

2. Three merchants trade together, A puts in 301.,

40*l.*, and C 56*l.*, they gain 130*l.*, what is each man's share of the gain? Ans. A's 30*l.* 19*s.* $0\frac{1}{2}d.\frac{9}{2}f.$ B's 41*l.* 5*s.* $4\frac{3}{4}d.\frac{1}{2}f.$ C's 57*l.* 15*s.* $6\frac{1}{2}d.\frac{1}{2}f.$

3. A bankrupt is indebted to B 250l., to C 280*l.*, to D 300*l.*, and to E 102*l.*10*s.*, his estate is worth only 600*l.*, how must it be divided among his creditors? Ans. B's 160*l.* 17*s.* $1\frac{8}{4}d.\frac{271}{5}$. C's 180*l.* 3*s.* $2\frac{1}{4}d.\frac{1}{2}\frac{4}{5}\frac{8}{5}$. D's 193*l.* 0*s.* 7*d.* $\frac{1}{3}\frac{1}{7}\frac{5}{5}$. E's 65*l.* 19*s.* $0\frac{1}{4}d.\frac{2}{5}\frac{5}{5}\frac{1}{5}$.

4. A common, consisting of 200 acres, is to be divided among R, S, and T, in proportion to their estates; R's estate is worth 300*l*., S's 350*l*., and T's 200*l*., what is each man's share of the common? Ans. R's 70 ac. 2 ro. $14\frac{9}{17}$ po. S's 82 ac. 1 ro. $16\frac{8}{17}$ po. T's 47 ac. 9 $\frac{7}{17}$ po.

5. A, B, and Ĉ join stocks in trade; their stocks amount to 2001. A's gain was 3l., B's 5l., and C's 8l., what was each man's stock? Ans. A's 37l. 10s., B's 62l. 10s., and C's 100l.

6. The stock of a trading company is 21804l.16s. $0\frac{1}{2}d.$ and consists of 84 shares, what is C's stock, who has 7 shares? Ans. $1817l.1s.42d.\frac{1}{8}$.

Nore. Multiply the stock by 7, and divide by 84. Or divide by 12.

When the times of continuing the stock in company are unequal.

RULE. Multiply each sum into its respective time.

7. Three graziers rent a piece of land at 30*l*. 10*s.*, A puts in 12 sheep for $3\frac{1}{2}$ months, B puts in 8 sheep for $8\frac{1}{2}$ months, and C puts in 10 for 5 months, how much must each pay of the rent? Ans. A 8*l*. 0*s*. $1\frac{1}{2}d$., B 12*l*. 19*s*. 3*d*., and C 9*l*. 10*s*. $7\frac{1}{2}d$.

8. Two merchants enter into partnership for 16 months, A put in at first 250*l*., and at 8 months' end he put in 80*l*. more, B put in at first 360*l*., and

at 12 months' end took out 90*l*., they gained 510*l*.. what was each man's share? Ans. A's 235*l*. 13*s*. $11\frac{1}{4}d$. $\frac{25}{237}$., B's 274*l*. 6*s*. $0\frac{1}{2}d$. $\frac{1}{4}7\frac{9}{7}$.

9. A, B, and C enter into partnership, A puts in at first 500*l*., and 4 months after 150*l*. more, but 2 months after he takes out 350l.; B puts in at first 300*l*., and 6 months after 400*l*. more, but 3 months after he takes out 600*l*.; C puts in 200*l*., and is to have 150*l*. for managing the business. At the end of 12 months they gain 500*l*. Required each man's share? Ans. A's 152*l*. 11s. 3d. $\frac{5}{13}$., B's 125*l*. 12s. 9d. $\frac{1}{13}$., and C's 221*l*. 15s. 10d. $\frac{1}{19}$.

10. A common, consisting of 500 acres, 2 roods, 30 perches, is to be divided among 6 persons, whose estates upon which their claims are founded are respectively 1500*l*., 2000*l*., 3000*l*., 3600*l*., 4000*l*., and 4800*l*., and the values of the land allotted te each are respectively 20s., 25s., 30s., 40s., 50s., and 60s., per acre. Required the quantity each receives? Ans. 1st, 74 acres, 1 rood, 17 $_{155}^{157}$ perches; 24, 5th, and 6th, each 79 acres, 1 rood, 10_{1701}^{701} perches; 3d, 99 acres, 23_{157}^{157} perches; and the 4th, 89 acres, 37_{151}^{15} perches.

11. Four graziers rented a grass-park for six months, for which they paid 40*l*. Now, A put in 20 oxen, and paid 8*l*.; B put in 25 oxen, and paid 12*l*.; C put in 16 oxen, and paid 10*l*.; and D put in 30 oxen and paid 10*l*. Required the time that each person's oxen continued? Ans. A's continued $1_{110,37}^{15.7}$ month, B's $1_{110,37}^{62.5}$ month, C's $2_{114,37}^{44.5}$ months, and D is $1_{113,37}^{9.7}$ month.

INTEREST

Is the allowance given by the borrower of any sum of money to the lender. Principal is the money lent.

Rate per cent. is the sum agreed on.

Amount is the principal and interest added to gether.

I. To find the interest for one year.

RULE. Multiply the principal by the rate per cent., and divide by 100.

Note. If the rate per cent. is an aliquot part of 100, take the same part of the principal for the interest.

II. To find the interest for several years.

RULE. Multiply the interest for one year by the number of years.

Note. If there is a fraction annexed to the years or the rate per cent., take aliquot parts for it.

III. To find the commission, brokerage, insurance, and value of stock.

RULE. Multiply the sum by the rate, and divide the product by 100.

IV. To find the quantity of stock that can be purchased for a given sum.

RULE. Multiply the sum by 100, and divide by the rate.

SIMPLE INTEREST.

1. What is the interest of 851. for a year, at 51. per cent.? Ans. 41. 5s.

2. What is the interest of 108*l*. 10s. for a year, at 4*l*. per cent.? Ans. 4*l*. 6s. $9\frac{1}{2}d$. $\frac{2}{3}$.

3. What is the interest of 1000l. for a year, at $4\frac{1}{3}l$, per cent.? Ans. 45l.

4. What is the amount of 40l. 10s. for three years, at $3\frac{1}{2}l$. per cent.? Ans. 44l. 15s. $0\frac{1}{2}d$.

5. What is the interest of 119*l*. 1s. 8*d*. for five years, at 4*l*. per cent.? Ans. 23*l*. 16s. 4*d*.

6. What is the interest of 450*l*. 8s. 6d. for 43 years, at 5*l*. per cent.? Ans. 106*l*. 19s. 6⁴₂d. 10.

7. What is the interest of 342*l*. 16s. 9*d*. for 5 years, at 5*l*. per cent.? Ans. 85*l*. 14s. 24*d*.

8. What is the interest of 845l. 10s. for $\frac{1}{4}$ of a year, at 5l. per cent.? Ans. 10l. 11s. $4\frac{1}{4}d$.

9. What is the interest of 248*l*. 10s. 10*d*. for 8 months, at 2*l*. per cent.? Ans. 3*l*. 6s. 3¹/₂*d*. ¹/₄.

10. What is the commission on 345l, at $2\frac{1}{2}l$ per cent.? Ans. 8l. 12s. 6d.

11. What is the interest of 295l. 8s. 4d. for 10 months, at 3l. per cent.? Ans. 7l. 7s. $8\frac{1}{2}d$.

12. What is the interest of 360l. for 26 weeks, at 24l. per cent.? Ans. 4l. 10s.

13. What is the brokerage on 152*l*., at 4s. 6d. per cent.? Ans. 6s. $10\frac{9}{2}d$. $\frac{3}{25}$.

14. What is the interest of 240*l*. for 28 weeks, at $4\frac{1}{4}l$. per cent.? Ans. 5*l*. 9s. $10\frac{1}{5}d$.

15. What is the insurance of 195l. 5s., at $10\frac{1}{2}l.$ per cent.? Ans. 20l. 10s. $0\frac{1}{4}d. \frac{1}{2}$.

16. What is the purchase of 710l. South Sea stock, at 103§l. per cent.? Ans. 735l. 14s. 9d.

17. What is the purchase of 918*l*. 14*s*. Bank stock, at 127³/₄*l*. per cent.? Ans. 1173*l*. 12*s*. 9¹/₄*d*. ¹/₇.

18. What is the purchase of 816*l*. Bank annuities, at $85\frac{3}{3}l$. per cent.? Ans. 696*l*. 13s. $2\frac{1}{4}d$. $\frac{3}{4}$.

19. What is the purchase of 2018*l*. 15*s*. 6*d*. India stock, at 140¹/₂*l*. per cent.? Ans. 2831*l*. 6*s*. 7¹/₂*d*. ⁵/₅.

20. How much Bank stock, at 213*l*. per cent., can be purchased for 8000*l*.? Ans. 3755l. 17s. $4\frac{1}{4}d$. $\frac{57}{4}$.

21. How much stock in the 3 per cents., at $72\frac{1}{4}$. per cent., can be purchased for 1000*l*.? Ans. 1384*l*. 1s. $7\frac{3}{4}d$. $\frac{3}{2}\frac{9}{8}$.

22. How much stock in the 4 per cent. consols at $96\frac{1}{2}$, per cent., can be purchased for 8500l.? Ans 8808l. 5s. $9\frac{1}{2}d.$ $18\frac{2}{3}$.

23. What interest will be obtained by purchasing 3 per cents., at 634*l*. per cent.? Ans. 444*l*.

24. What interest will be obtained by purchasing 4 per cents., at $90\frac{3}{5}l$, per cent.? Ans. $450\frac{3}{5}l$.

25. At what price should I purchase in the 4 per cents. to obtain 5*l*. per cent. interest? Ans. 80*l*.

26. At what price should I purchase in the 3 per cents. to obtain 5l. per cent. interest? Ans. 60l.

To calculate interest for days.

RULE. Multiply the principal by the number of days, and by double of the rate per cont., then divide the Product by 73000.

27. What is the interest of 10001, 10s, 6d, for 12

days, at 5l. per cent.? Ans. 1l. 12s. $10\frac{1}{2}d$. $1\frac{6}{3}\frac{2}{3}$. 28. What is the interest of 345l. for 80 days, at 51. per cent.? Ans. 31. 15s. 71d. 43.

29. What is the amount of 2501. 10s. 6d. for 40 days, at 31/2. per cent.? Ans. 2511. 9s. 81/2d. 878.

30. What is the interest of 1841, from 12th May to 19th November, at 5l. per cent.? Ans. 41. 16s. 31d. 247.

31. What is the interest of 4081. for 60 days, at 41. per cent.? Ans. 21. 13s. 73d. 363.

32. What is the interest of 2451. 16s. for 73 days. at 21/2. per cent.? Ans. 11. 4s. 63/d. 21/2.

33. What is the interest of 3511. from 5th March to 6th August, at 41/l. per cent.? Ans. 6l. 13s. 31/d. 1139.

When partial payments are made.

RULE. Multiply the principal and the different balances by the number of days they are at interest, and by double of the rate per cent. Add these Products, and divide the sum by 73000.

34. A bill of 4001. was due April 20, of which 1101. was paid June 15, 281. August 4, and the balance October 2. Required how much interest is due, at 5*l*. per cent.? Ans 7*l*. 3s. $5\frac{1}{4}d$. $\frac{1}{5}\frac{5}{5}$.

35. A bill of 350l. was due January 10, of which 701. was paid on the 10th of each succeeding month till the whole was paid. Required how much interest was due, at 41 . per cent.? Ans. 31.17s.10 46 d.

36. A bill of 1000l. was due April 4, of which 150%. was paid May 10; 250%. July 12; 300%. September 18; 1001. November 10; 1501. January 20, and the balance March 4. Required the amount of the last payment, including the interest at 412. per cent.? Ans. 701. 0s. 1113d.

To calculate interest on accounts-current.

RULE. Add and subtract the sums paid and received in the order of their dates; and if the balance is sometimes due to the one party, and sometimes to the other, the Products must be extended in different columns.

37. Required the interest on the following account from January 8 to July 30, allowing 51. per cent. when the balance is due to B. D., and 4l. per cent, when due to M. N.

Dr. Mr B. D. his acccount-current with M. N. Cr. Jan. 8. Tobalance1007. Mar. 15. By cash 2507. Feb. 14. To cash 1147. May 30. By cash 1007 April24. To cash 4007. July 2. By cash 4007. June 18. To cash 701.

Ans. Balance due by B. D. 3l. 2s. 8d. 1\$\$5. 38. Required the interest on the following account from April 3 to March 31, allowing 51. per cent. when the balance is due to A. B., and 411 when due to C. D.

Dr. A. B's account-current with C. D. Cr. April 3. To balance 135%. June 1. By cash 397%. July 16. To cash 270%. Sept. 8. By cash 214%. Oct. 20. To cash 258%. Nov. 13. By cash 128%. Dec. 15. To cash 460?. Jan. 30. By cash 296?. Jan. 1. To cash 2311. Mar. 18. By cash 3741. Ans. 21. 16s. 24d. 1831 due to C. D.

To calculate interest on bills or bonds when the intervals between the payments are greater than a vear.

RULE. Add the interest due at the date of each payment to the principal, and deduct the payment from the amount.

39. A bond of 500*u*. became due January 1, 1864, of which 100*l*. were paid May 14, 1865; 200*l*. April 10, 1866; 150*l*. June 1, 1867; and the balance August 1, 1868. Required the sum then due, interest at 5*l*. per cent.? Ans. 125l. 3s. $10\frac{1}{2}d$.

40. Borrowed on bond at 14. per cent. May 14, 1865, 700*l.*, of which I paid June 1, 1866, 250*l.*; June 30, 1867, 200*l.*; July 10, 1868, 200*l.*; and retired the bond September 20, 1869. How much was then paid? Ans. 127*l.* 3s. 94*d.*

DISCOUNT

Is an allowance given for the payment of any sum of money before it becomes due.

To find the present worth.

RULE. As the amount of 100%, for the given rate and time: is to 100 : : so is the debt : to the present worth.

To find the discount.

RULE. As the amount of 100% for the given rate and time : is to the interest of 100% for that time : : so is the given sum or debt : to the discount.

or debt : to the discount. Nore. These rules give the true discount or present worth; but bankers in discounting bills charge the interest upon the amount of the bill for the time it has to run, including three days of grace, by which means the holder loses the interest of the true discount.

1. What is the present worth of 240*l*. due 100 days hence, at 5*l*. per cent.? Ans. £236*l*. 15*s*. 1¹/₁*d*. ¹/₂?

2. What ready money will discharge a debt of 5607. 10s. due 48 days hence, at 57. per cent.? Ans. 5567. 16s. $9\frac{1}{4}d$. $\frac{188}{1887}$.

3. Required the discount of 1000*l*. due 70 days hence, at 5*l*. per cent. ? Ans. 9*l*. 9s. 11¹/₂d. 7³/₃.

4. What is the discount of 284*l*. 8s. 6*d*. for 184 days, at 3¹/₂*l*. per cent.? Ans. 4*l*. 18s. 7¹/₂*d*. 4²/₄²/₂.

5. Sold goods for 8421. 5s. to be paid 350 days hence, what is the present worth at 51. per cent.? Ans. 8031. 14s. $3\frac{3}{4}d$.

EQUATION OF PAYMENTS

Is the finding a time at which a debt due at different times may be discharged at once, without disadvantage to either party.

RULE. Multiply each payment by the time at which it is due; divide the sum of the products by the amount of the debt: the quotient is the time required.

1. I owe B 1007. payable in 50 days, 1307. in 40 days, 2307. in 140 days; at what time should I pay the whole together? Ans. 92_{24}^{4} days.

2. Paid 480*l*. as follows: 60*l*. in 40 days, 180*l*. in 96 days, 50*l*. in 200 days, and the rest in a year and 45 days; required the equated time for paying the whole? Ans. $224\frac{1}{8}$ days.

3. A owes B 100*l*. payable in 60 days, 200*l*. in 80 days, 350*l*. in 180 days, and 500*l*. in a year; at what time may he pay the whole without loss to either party? Ans. 23214 days.

COMPOUND INTEREST

Is calculated by making the amount at each stated time of payment the principal for the next.

1. What is the compound interest of 2001. for three years, at 51. per cent.? Ans. 311. 10s. 6d.

2. What is the amount of 300*l*. in 4 years, at 5*l*. per cent. per annum? Ans. 364*l*. 13s. 04*d*. 4.

3. Required the interest of 500*l*. for three years, at 4*l*. per cent.? Ans 62l. 8s. $7\frac{1}{2}d$. $\frac{1}{2}\frac{8}{3}$.

4. What is the amount of 240l. 10s. for two years, six months, at 3 per cent.? Ans. 258l. 19s. 5gd.

5. What is the interest of 129*l*. 15*s*. for three years, 9 months, and 10 days, at 44*l*. per cent.? Ans. 23*l*. 9*s*. 11*d*

PROFIT AND LOSS.

CASE 1. Given the buying and selling price, to discover the profit or loss per cent.

Rule. As the prime cost : Is to the profit or loss on it : : So is 100 : To the profit or loss on it.

1. Bought a hogshead of wine for 50l. 8s. and sold it for 63l., what did I gain per cent.? Ans. 25l.

2. Bought cloth at 4s. 6d. per yard, and sold it at 4s. 10d., what was the gain per cent.? Ans. $7\frac{1}{2}\frac{1}{4}$.

3. Bought cloth at 18s. 6d. per yard, and sold it at 15s. 4d., what was the loss per cent.? Ans. 17151.

4. How much per cent. is $3\frac{1}{2}d$. per shilling? Ans. 29¹/₄l.

CASE II. Given the prime cost and rate per cent. to find the selling price.

RULE. As 100 :

Is to 100 with the rate per cent. added in case of gain, or subtracted in case of loss : : So is the prime cost : To the selling price.

5. If I gained 25*l*. per cent. by wine which 1 bought at 50*l*. 8s. per hhd., at what did I sell it? Ans. 63*l*. per hhd.

6. Bought cloth at 4s. 6d. per yard, at what must I sell it to gain $7\frac{1}{2}\frac{1}{4}l$. per cent.? Ans. 4s. 10d.

7. Bought a cwt. of sugar, for 3*l*. 3*s*., at what rate must I sell it per lb. to gain 12*l*. per cent. r Ans. $7\frac{1}{2}d$. $\frac{\sigma}{\sigma_{c}}$.

8. Bought sugar at 8¹/₄*d*. per lb., at what must I sell it per lb. to gain 17¹/₄*l*. per cent by it? Ans. 10*d*.

CASE III. Given the selling price and rate per cent. profit or loss, to find the prime cost. RULE. As 100, with the rate per cent. added, or subtracted : Is to 100 : : So is the selling price :

To the prime cost.

9. If I gain 17441. per cent. on sugar I sold at 10d. the lb., what was the prime cost? Ans. 81d.

10. Lost 81. per cent. on tea which I sold at 5s. 6d. per lb., what was the prime cost? Ans. 5s. 11 d. 3%.

11. Gained 34% per cent. on sugar which I sold at 51. 9s. 8d. per cwt., what was the prime cost per lb.? Ans. 83d.

CASE IV. Given two selling prices and the rate per cent. of one of them, in order to find the rate per cent. of the other selling price.

RULE. As the price whose rate per cent. is given :

Is to 100, with the given rate added or subtracted : . So is the other given price :

To a fourth number ;

From which number subtract 100 in case of gain ; but which

Subtract from 100 in case of loss.

12. By selling cheese at 5s.9d. per stone, I gained 151. per cent., what did I gain per cent. by selling it at 6s.? Ans. 201.

13. A merchant selling wool at 8s. per stone, gained 121. per cent., what will he gain or lose per cent. by selling the same wool at 7s. the stone? Ans. He will lose 21. per cent.

14. By selling cloth at 18s. 4d. per yard, I gained 121. per cent., what will I gain or lose per cent. by selling it at 16s. 10d. per yard? Ans. 2491. per cent. gain.

15. By selling muslin at 5s. 10d. per yard, I lost 161. per cent., how much will I gain or lose per cent. by selling it at 6s. 3d. per yard? Ans. 101. per cent. loss.

VULGAR FRACTIONS.

A Fraction is a part or parts of a unit, written thus $\frac{5}{5}$ numerator,

 $\overline{8}$ denominator.

The numerator is the remainder after division; and the denominator the divisor.

1. A proper fraction is when the numerator is less than the denominator, as $\frac{3}{2}$.

2. An improper fraction is when the numerator is equal to, or greater than, the denominator, as $\frac{2}{3}, \frac{1}{3}$.

3. A simple fraction has but one numerator and one denominator, as $\frac{3}{2}$.

4. A compound fraction is a fraction of a fraction, as $\frac{1}{2}$ of $\frac{3}{2}$.

5. A mixed number is composed of a whole number and a fraction, as $4\frac{1}{4}$.

Note 1. Any whole number may be expressed like a frac tion, by writing 1 under it.

2. Multiplying or dividing both terms of a fraction by the same number does not change its value.

REDUCTION OF VULGAR FRACTIONS.

PROB. 1. To reduce a fraction to its lowest terms.

RULE. Find a common measure thus: Divide the denom mator by the numerator, and that divisor by the remainder continually, till nothing remain. The last divisor is the com mon measure; then divide both the numerator and denomi nator by this measure:

Or divide the numerator and denominator by any number which will divide them without a remainder.

Note. Any number ending with 5 or 0 is divisible by δ Any number is divisible by 3 or 9, if the sum of its digits be divisible by 3 or 9. Any number is divisible by 11, if the sums of its alternate digits are equal to each other.

Reduce ⁶/₁₂₆ to its lowest terms. Ans. ¹/₂.
 Reduce ⁴/₃₆₆ to its lowest terms. Ans. ²/₇₈.
 Reduce ¹/₃₆₆ to its lowest terms. Ans. ⁶/₆₄₇.

4. Reduce \$25 to its lowest terms. Ans. \$74.

5. Reduce $\frac{72.9}{5.61}$ to its lowest terms. Ans. $\frac{1}{5}$. 6. Reduce $\frac{78.925}{5.45}$ to its lowest terms. Ans. $\frac{1}{11}$

PROB. 2. To reduce a mixed number to an improper fraction.

RULE. Multiply the whole number by the denominator adding the numerator; under this sum write the denominator.

Reduce 5³/₄ to an improper fraction. Ans. ²³/₄.
 Reduce 7¹/₅ to an improper fraction. Ans. ³⁶/₅.

3. Reduce 61 to an improper fraction. Ans. 55.

4. Reduce 815 to an improper fraction. Ans. 152.

5. Reduce 1937 to an improper fraction. Ans. 516.

6. Reduce 2911 to an improper fraction. Ans. 562.

PROB. 3. To reduce an improper fraction to a whole or mixed number.

RULE. Divide the numerator by the denominator.

1. Reduce $\frac{101}{4}$ to a whole or mixed number. Ans. $25\frac{1}{4}$.

2. Reduce $\frac{146}{4}$ to a whole or mixed number. Ans. 361.

3. Reduce $\frac{541}{14}$ to a whole or mixed number. Ans. 24-5₁

4. Reduce $\frac{1425}{94}$ to a whole or mixed number. Ans 59콜.

5. Reduce $\frac{7854}{97}$ to a whole or mixed number. Ans. 2908.

6. Reduce $\frac{54867}{571}$ to a whole or mixed number. Ans. 147339.

PROB. 4. To reduce a compound fraction to a simple one.

RULE. Multiply all the numerators together for the nu-merator, and all the denominators together for the denominator.

1. Reduce $\frac{2}{3}$ of $\frac{3}{4}$ to a simple fraction. Ans. $\frac{1}{2}$. 2. Reduce \$ of \$ to a simple fraction. Ans. 19.

3. Reduce $\frac{4}{2}$ of $\frac{19}{12}$ of $\frac{7}{12}$ to a simple fraction. Ans. 24.

4. Reduce 11 of 13 of 15 to a simple fraction. Ans. 289.

5. Reduce $\frac{2}{5}$ of $\frac{4}{5}$ of $\frac{4}{5}$ of $\frac{4}{5}$ to a simple fraction. Ans. \$9.

6. Reduce $\frac{5}{8}$ of $\frac{4}{15}$ of $\frac{3}{15}$ of $8\frac{9}{15}$ to a simple fraction. Ans. 205.

PROB. 5. To reduce fractions to a common denominator.

RULE. Multiply each numerator into all the denominators, except its own, for a new numerator ; and multiply all the denominators together for a common denominator.

Note. Fractions may often be reduced to a common denominator, by multiplying their numerators and denominators by such numbers as will make the denominators in both equal.

1. Reduce 2 and 7 to a common denominator. Ans. 16, 35.

2. Reduce § and § to a common denominator. Ans. 35, 18.

3. Reduce 1, 3, and 5, to a common denominator. Ans. 36, 54, 40.

4. Reduce $\frac{5}{8}$, $\frac{4}{5}$, $\frac{8}{13}$, and $\frac{1}{21}$, to a common denom-

inator. Ans. $\frac{1}{2}$ \frac

nominator. Ans. $\frac{578}{1008}$, $\frac{448}{1008}$, $\frac{4558}{1008}$, $\frac{720}{1008}$. 6. Reduce $\frac{1}{3}$ of $\frac{3}{4}$ of $3\frac{1}{2}$, $\frac{7}{12}$, $\frac{1}{16}$, $7\frac{5}{6}$, and $\frac{1}{2}$ of $\frac{3}{4}$ of 75 to a common denominator. Ans. 168, 112, 152. 1504, 549

PROB. 6. To reduce a fraction from one denomination to another, which shall have the same value.

RULE. Find how many of the less denomination make one of the greater ; if from a higher to a lower, multiply the numerator by that number : or the denominator, if to a greater.

1. Reduce § of a farthing to the fraction of a pound. Ans. 1728.

2. Reduce 17 as of a pound to the fraction of a farthing. Ans. §.

3. Reduce 2 of a penny to the fraction of a pound. Ans. 360.

4. Reduce § of a farthing to the fraction of a guinea. Ans. 50^{4} of a crown to the fraction of a 5. Reduce $\frac{3}{4}$ of a crown to the fraction of a

pound. Ans. Ja.

6. Reduce 4 of a farthing to the fraction of a shilling. Ans. 10.

7. Reduce *f* of a pound to the fraction of a guinea. Ans. 40.

8. Reduce 1 of half a crown to the fraction of a pound. Ans. 1.

9. Reduce § 1b. to the fraction of a ton. Ans. 2885.

10. Reduce 2 dwt. to the fraction of a lb. Ans. 100.

11. Reduce \$ oz. to the fraction of a cwt. Ans.

12. Reduce $\frac{6}{11}$ yd. to the fraction of a mile. Ans. 30800

13. Reduce $\frac{1}{360}$ of a pound to the fraction of a penny. Ans. §.

14. Reduce 1480 of a ton to the fraction of a lb. Ans. 1.

Note. When the given number is of different denominations, reduce it to the lowest for a numerator, and reduce the denominator to the same name.

1. Reduce 6s. 4d. to the fraction of a pound. Ans. 19.

2. Reduce 2¹/₄d. to the fraction of a shilling. Ans. ⁵/₁

3. Reduce 8¹/₄d. to the fraction of a crown. Ans. 120.

4. Reduce 2 roods, 15 poles, to the fraction of an acre. Ans. 19.

5. Reduce 3 cwt. 14 lb. to the fraction of a ton. Ans. $\frac{5}{3\sigma}$.

6. Reduce $6\frac{3}{4}$ inches to the fraction of a foot. Ans. $\frac{9}{4}$.

PROB. 7. To find the value of a fraction.

RULE. Multiply the numerator by the next lower denomnation, and divide the product by the denominator. Reduce the remainder, if any, into the next lower denomination; and divide as before, and so on as far as is necessary.

Or, consider the numerator as so many of the same name as the fraction, and divide it by the denominator as in Compound Division.

1. What is the value of \$1.? Ans. 13s. 4d.

2. What is the value of \$1.? Ans. 12s. 6d.

3. What is the value of $\frac{3}{4}$ of a guinea? Ans. 15s. 9d.

4. What is the value of \$ of half a crown? Ans. 2s.

5. What is the value of $\frac{3}{7}$ lb. avoirdupois? Ans. 6 oz. $13\frac{3}{2}$ dr.

6. What is the value of $\frac{4}{5}$ of a cwt.? Ans. 1 qr. 21 lb. 12 oz. $7\frac{1}{5}$ dr.

7. What is the value of $\frac{3}{4}$ lb. troy? Ans. 5 oz. 2 dwt. 204 gr.

8. Reduce $\frac{3}{2}$ of an ell English to its proper quantity. Ans. 1 qr. $3\frac{1}{2}$ nl.

9. What is the proper quantity of $\frac{4}{5}$ of a mile? Ans. 6 fur. 16 po.

10. What is the value of § of 63 gallons of port wine? Ans. 52 gal. 2 qts.

11. What is the value of $\frac{5}{8}$ of an acre? Ans. 1 rood, 20 po.

12. What is the proper quantity of $\frac{3}{5}$ of a day? Ans. 14 ho. 24 min.

ADDITION OF VULGAR FRACTIONS.

RULE. Reduce compound fractions to simple ones; mixed numbers to improper fractions; fractions of different denominations to those of the same ; and all of them to a common denominator ; then add the numerators together, and under their sum place the common denominator.

1. Add $\frac{2}{5}$ and $\frac{3}{4}$ together. Ans. $1\frac{3}{20}$. 2. Add $\frac{3}{4}$ and $\frac{2}{5}$ together. Ans. $1\frac{1}{24}$.

3. Add 3, 2, and 5 together. Ans. 158.

4. Add 2, 5, and 5 together. Ans. 210.

Note 1. When mixed numbers are given, find the sum of the fractions, to which add the whole numbers.

5. Add $4\frac{1}{2}$ and $6\frac{1}{3}$ together. Ans. $10\frac{8}{15}$.

6. Add $6\frac{1}{4}$, $2\frac{1}{5}$, and $3\frac{3}{4}$ together. Ans. $12\frac{1}{5}$.

7. What is the sum of 51, 67, and 43? Ans. 17, 18.

8. Add 2, 41, and 1 of 4 together. Ans. 531.

2. When the fractions are of different denominations, reduce them into the same; and add their numerators together; or find their value, and add as in Compound Addition.

9. Add $\frac{2}{3}s$. and $\frac{3}{2}d$. together. Ans. $8\frac{1}{2}d$. $\frac{2}{5}$.

10. Add 21. 5s. and § of a penny together. Ana. 13s. 113d. 1.

11. Add 3 of a guinea to 3 of a crown, 3 of a

shilling, and $\frac{4}{5}$ of a penny. Ans. 12s. $1\frac{9}{4}d$. $\frac{29}{5}$. 12. What is the sum of $\frac{3}{4}$ of a foot, $\frac{9}{5}$ of a yard, and 7 of a mile? Ans. 1540 yds. 2 feet, 9 inches.

13. Required the sum of $5\frac{1}{2}$ yards, $4\frac{3}{4}$ English ells, and ²/₂ of a nail. Ans. 11 vds. 1 gr. 0²/₃ nl.

14. What is the sum of $\frac{5}{15}$ of a ton, and $\frac{9}{15}$ of a cwt.? Ans. 9 cwt. 16 lb. 15 oz. 17.

15. Add $\frac{1}{3}$ of a day and $\frac{5}{24}$ of an hour together? Ans. 8 hours, 12 minutes, 30 seconds.

SUBTRACTION OF VULGAR FRACTIONS.

RULE. Prepare the fractions as in Addition ; then take the difference of the numerators, and place it over the common denominator.

1. What is the difference of $\frac{3}{4}$ and $\frac{5}{3}$? Ans. $\frac{7}{36}$. 2. What is the difference of $\frac{4}{5}$ and $\frac{9}{20}$? Ans. $\frac{7}{20}$. 3. From 2 of 3, take 1 of 2. Ans. 3.

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4. From # of 9, take 11. Ans. 223.

5. From 161 take 2 of 18. Ans. 41.

6. From 3 of a pound, take 2 of a shilling. Ans. 14s. 79d. 4.

7. From 4 of a guinea, take 1 of a pound. Ans. 5s. 4d.

8. From $\frac{7}{2}$ of a pound, take $\frac{1}{2}$ of $\frac{2}{3}$ of a shilling. Ans. 17s. 2d.

9. From $\frac{4}{5}$ oz. take $\frac{3}{5}$ dwt. Ans. 15 dwt. 15 gr. 10. From $3\frac{1}{2}$ cwt. take $15\frac{9}{10}$ lb. Ans. 3 cwt. 1 gr. 121 lb.

MULTIPLICATION OF VULGAR FRACTIONS.

RULE. Prepare the fractions as in Addition ; then multiply all the numerators together, for the numerator of the product, and all the denominators for the denominator.

NOTE. When the same number is found in the numerators and denominators of any of the fractions, strike them out before multiplication.

- 1. Multiply 3 by 4. Ans. 3.

- Multiply ⁴/₅ by ⁵/₈. Ans. ⁴/₈.
 Multiply ⁴/₁₆ by ⁵/₁₈. Ans. ⁵/₉₅.
 Multiply ⁴/₄ by ²/₈ of ³/₄. Ans. 2⁷/₁₈.
- 5. Multiply 2, 3, and 5 together. Ans. 52.
- 6. Multiply $48\frac{1}{4}$ by 7. Ans. $337\frac{3}{4}$. 7. Multiply $\frac{1}{2}$ of 9 by $\frac{3}{4}$. Ans. $1\frac{1}{4}\frac{3}{4}$.
- 8. Multiply \$ of 5 by 1 of 2. Ans. 1g.
- 9. Multiply 2 of 3 by 5 of 21. Ans 5.
- 10. What cost 141 yds. at 111.? Ans. 31. 18s. 41d.

DIVISION OF VULGAR FRACTIONS.

RULE. Prepare the fractions as before; then invert the divisor, and proceed exactly as in Multiplication.

- 1. Divide $\frac{4}{5}$ by $\frac{2}{5}$. Ans. $\frac{2}{5}$. 2. Divide $\frac{3}{4}$ by $\frac{1}{5}$. Ans. $1\frac{1}{2}$.
- 3. Divide 11 by 5. Ans. 1 2.

4. Divide 18 by 5. Ans. 48.

5. Divide 143 by 381. Ans. 18842.

6. Divide 4561 by 31. Ans. 13018.

7. Divide 2 of 4 by 4. Ans. 9.

8. Divide ⁸/₄ by ¹/₅ of ¹/₁. Ans. 32¹/₁₉.
 9. Divide ¹/₅ of 4 by ²/₅ of ⁴/₅. Ans. 4.

10. Divide a prize of 245011. into 402 shares. Ans. 601. 12s. 11d. 20.

PROPORTION OF VULGAR FRACTIONS.

RULE. State the terms as in whole numbers, and prepare them by the former rules : invert the first term of the proportion, then multiply as directed in Multiplication.

1. If 3 yard cost 71., what cost 51 yards? Ans. 51. 8s. 10 d. 2.

2. If § of a gallon cost §l., what will § of 252 gal. cost? Ans. 1051.

3. If 1 of a ship cost 4451. 15s., what is 30 of her worth ? Ans. 7801. 1s. 3d.

4. If $\frac{3}{4}$ of a yard cost $\frac{5}{4}l$, what is the price of $31\frac{1}{3}$ ells Flemish? Ans. 192. 11s. 8d.

5. If 15 lb. of gold is worth 6151. Sterling, what is 2 grains worth? Ans. 3d.

6. If $\frac{11}{12}$ of a ship cost 390*l*. 6s. 4*d*., what will $\frac{15}{18}$ of the same cost? Ans. 345*l*. 19s. 3*d*.

7. A can perform a piece of work in 10 days, B in 12 days, and C in 16 days: in what time will

they perform it working together? Ans. 4_{59}^4 days. 8. A, B, and C together can perform a piece of work in 12 days; A and B together can do it in 18 days, and B and C together can do it in 16 days: in what time could A and C together do it, and in what time could each do it separately? Ans. A and C in 204 days. A in 48 days, B in 284 days, C in 36 days.

DECIMAL FRACTIONS

Are such as have a unit for their denominator, with as many ciphers annexed as there are figures in the numerators; as $\frac{9}{10}$ $\frac{76}{100}$, $\frac{560}{1000}$, usually written with a point prefixed without the denominator '2, '34, '564, and read thus: '2, two tenths; '34, thirty-four hundredth parts; '564, five hundred and sixty-four thousand parts; and so on.

Note. Ciphers on the right hand of decimals do not alter their value.

REDUCTION OF DECIMALS.

PROB. 1. To reduce a vulgar fraction to a decimal.

RULE. Annex ciphers to the numerator, and divide by the denominator.

1. What is the decimal of $\frac{1}{4}$, $\frac{1}{2}$, and $\frac{3}{4}$? Ans. 25, $\cdot 5$, $\cdot 75$.

2. Reduce z to a decimal. Ans. .6.

3. What is the decimal of 1? Ans. 125.

4. Reduce § to a decimal. Ans. 375.

5. What is the decimal of $\frac{5}{5}$? Ans. 625.

6. Reduce 7 to a decimal. Ans. . 5834.

7. Reduce 15 to a decimal. Ans. 34094.

8. What is the decimal of 124? Ans. 098116.

NOTE. If there are not as many figures in the quotient as eiphers annexed, supply the defect by writing ciphers on the left hand.

PROB. 2. If the given number consists of several denominations.

RULE. Reduce it to the lowest denomination for a numerator, and reduce the denominator to the same ; then annex ciphers, and divide as before. Or :

Begin at the lowest, and reduce them in their order.

1. Reduce 15s. $6\frac{3}{4}d$. to the decimal of a pound Ans. $\cdot 778125l$.

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2. Reduce 9d. to the decimal of a pound. Ans. 03751.

3. Reduce 8s. 6d. to the decimal of a pound. Ans. -4251.

4. Reduce 12s. $8\frac{1}{2}d$. to the decimal of a guinea. Ans. $\cdot 605158756$.

5. Reduce $6\frac{1}{2}d$. to the decimal of a shilling. Ans. $\cdot 5416\frac{32}{2}$.

6. Reduce 8 oz. 12 dwt. 16 gr. to the decimal of a lb. troy. Ans. $\cdot 719444_{256}$.

7. Reduce 2 qr. 16 lb. to the decimal of a cwt. Ans. .64285716.

8. Reduce 20 yds. 2 f. 6 in. to the decimal of a mile. Ans. $\cdot 01183711344$.

9. Reduce 2 qr. 2 nl. to the decimal of a yard. Ans. 625.

10. Reduce 1 rood, 20 po. to the decimal of an acre. Ans. 375.

11. Reduce 3 bush. 1 pk. to the decimal of a quarter. Ans. 40625.

12. Reduce 15 gallons of wine to the decimal of 252 gallons. Ans. 0595238²⁴.

13. Reduce $6\frac{3}{4}$ inches to the decimal of a foot. Ans. $\cdot 5625$.

PROB. 3. To find the value of a decimal.

RULE. Multiply it by the value of the given denomination, and point off as many decimals from the right hand of the product as there are places in the given decimal. The figures on the left hand are integers of the next lower denomination; reduce the figures pointed off into the next lower denomination; proceed in this manner till you come to the lowest.

1. What is the value of $\cdot 85$ of a \pounds ? Ans. 17s. 2. What is the value of $\cdot 1875l$? Ans. 3s. 9d.

3. What is the value of $\cdot 125s$? Ans. $1\frac{1}{2}d$.

4. What is the value of '6845 cwt.? Ans. 2 qr. 20 lb. 10 oz. 9 dr. 984.

5. What is the value of .121 of 252 gallons? Ans. 30 gal. 1 qt. 1 pt. <u>936</u>.

6. What is the value of .03125 of 36 gallons? Ans. 1 gal. 1 pt.

7. What is the value of 28 of a mile? Ans. 2 fur. 9 po. 3 yds. 10 in. ⁸⁰.

PROB. 4. To find the decimal of Sterling money by inspection.

RULE. Take half the even number of shillings for the first decimal figure; and the number of farthings in the remainder, increased by 1, if they amount to 24, or upwards; by 2, if they amount to 48, or upwards; and by 3, if they amount to 72, or upwards, for the second and third figures; if there is but one figure, prefix a cipher to it.

To complete the decimal, call these two figures or their excess above 25, 50, or 75, pence; the farthings in them inoreased by 1 for every 24, give other two figures; continue this method till the decimal ends or repeats.

1. Reduce 6s. $4\frac{1}{2}d$. to the decimal of a pound. Ans. $\cdot 31875l$.

2. Reduce 9s. $6\frac{3}{4}d$. to the decimal of a pound. Ans. $\cdot 478125l$.

3. Find by inspection the decimal of 10s. $8\frac{1}{4}d$. Ans. $\cdot 534375l$.

4. Reduce 12s. $7\frac{3}{2}d$ to the decimal of a pound. Ans. $\cdot 6322916l$.

5. Reduce 16s. $11\frac{1}{4}d$. to the decimal of a pound. Ans. $\cdot 846875l$.

6. Reduce 19s. $11\frac{3}{4}d$ to the decimal of a pound. Ans. $\cdot 9989583l$.

PROB. 5. To value the decimal of a pound Sterling by inspection.

RULE. Double the figure next the point for shillings, if the next figure is 5, or upwards, take 5 from it, and add 1 to the shillings; then the second and third figures are farthings, after deducting 1 for every 25 in them.

1.	Value .3181.	Ans.	6s.	41d.
2.	·478l.			$6\frac{3}{4}d$.
3.	·5341.]	10s.	81d.
4.	·7691.]	155.	$4\frac{3}{4}d.$
5.	·9841.		195.	$8\frac{1}{4}d.$
6.	·994l.			$10\frac{3}{4}d.$

ADDITION AND SUBTRACTION OF DECIMALS.

RULE. Write down the given numbers, placing the decimal points directly under each other; then proceed as in whole numbers.

ADDITION.

1. What is the sum of 2.64, 85.6, .945, 14.8, 5.3456, and 84? Ans. 193.3306.

2. What is the sum of 785.1, 84.35, 1.654, .8956, .009, and 10.161? Ans. 882.1696.

3. What is the sum of 25·3, 2·78, 324·67, 1·294, 63·14, and 345·6? Ans. 762·784.

4. What is the sum of 325.7, 63.451, 275.34. 6.473, 25.68, and 287.435? Ans. 984.079.

5. What is the sum of 3285.64, 287.458, 4550.67, 38.4526, 324.578, and 4761.29? Ans. 13248.0886.

SUBTRACTION.

1. What is the difference between .8406 and .58975? Ans. .25085.

2. What is the difference of 84.95 and 3.6954? Ans. 81.2546.

3. What is the difference of 246 and .8154? Ans. 245.1846.

4. L borrowed from M 20.78125*l*. and afterwards paid him 14*l*. 18*s*. 9*d*. What remains due to M? Ans. 5*l*. 16*s*. 10¹/₂*d*.

5. Find the difference between 40 yards, 2 quarters, and 29.625 yards? Ans. 10 yds. 3 qr. 2 nl.

MULTIPLICATION OF DECIMALS.

RULE 1. Place the factors, and multiply as in whole numbers.

2. Point off as many decimal places in the product towards the right hand as there are in both factors; and if the product has not so many, supply the defect by writing ciphers on the left hand.

1. Multiply 346.549 by 3.15. Ans. 1091.62935.

2. Multiply 516.8945 by 44.89. Ans. 23203.394105.

3. Multiply .84615 by .065. Ans. .05499975.

4. Multiply .346809 by .00546. Ans. .00189357714.

5. A gentleman has 831251. a-day, how much is that a-year? Ans. 3031. 8s. 11d.

DIVISION OF DECIMALS.

RULE. Divide as in whole numbers, and point off as many decimal places in the quotient as the dividend has more than the divisor.

NOTE 1. If there are not as many decimal places in the quotient as required, supply the defect by writing ciphers on the left hand.

2. If there is a remainder, the quotient may be carried to any degree of exactness by annexing ciphers ; or, if the decimal places in the divisor are more than those in the dividend. ciphers may be annexed to the dividend.

3. If the dividend will not contain the divisor, annex ciphers, or suppose them to be annexed, to the dividend.

- 1. Divide 176.4 by 24. Ans. 7.35.
- 2. Divide 45.3496 by 3.68. Ans. 12.32120.

3. Divide 24.694 by .45. Ans. 54.834.

4. Divide 8496 by .546. Ans. 15560240.

5. Divide ·21468 by 2.5. Ans. ·085818.

- 6. Divide ·80468 by ·075. Ans. 10·7268. 7. Divide 8·4567 by 25. Ans. ·338217.

8. Divide .06548 by 215. Ans. .0003098.

9. Divide 216.4 by 100. Ans. 2.164.

10. A merchant bought a cwt. of sugar for 3.851. and intends to gain $1\frac{1}{2}d$. on each lb., at what rate must he retail it per lb.? Ans. 93d.

DECIMAL FRACTIONS.

PROPORTION OF DECIMALS.

1. If 1:25 yard of cloth cost .625*l*., what cost 30³ yards? Ans. 15*l*. 7*s*. 6*d*.

2. If 1 stone of cheese cost $\cdot 33125l$, what cost $50\frac{1}{3}$ stones? Ans. 16l. 14s. $6\frac{3}{4}d$.

3. If $\frac{1}{4}$ of a pound of silk cost 8s. 6d., what will 20.5 pounds cost? Ans. 34.85l.

4. A grocer bought 3 cwt. 1 qr. 14 lb. of sugar, at $\cdot 034375l$. per lb., and sold it in wholesale for $16\cdot5375l$, what did he gain or lose by the bargain, and how much per cent.? Ans. Gained 3l. 10s. $10\frac{1}{2}d$. and $27\frac{1}{27}l$. per cent.

INTERMINATE DECIMALS.

When a vulgar fraction is reduced to a decimal, if nothing at last remains, it is called *finite* or *terminate*; if not, it is called *interminate*.

An interminate decimal is called a *repeater*, when the same figure is constantly repeated ; and when several figures recur in the same order, it is called a *circulate*. When the repeating figures begin at the point, the decimal is called pure, but when there are other figures before them, it is said to be mixed, and the figures before the repeating ones are called the finite part.

A repeater is marked with a point above it, and a circulate with a point above the first and last figures of the circle.

REDUCTION.

I. To reduce an interminate decimal to a vulgar fraction.

RULE. If it is a pure repeater, or circulate, place nine for the denominator of the repeater, or nine for every figure of the circle.

If the decimal is mixed, subtract the finite part from the whole for the numerator, and place a nine for every repeating figure, with a cipher annexed for every finite place for the denominator.

1. Reduce .5, .7, .37, .45, .327, and .714285 to vulgar fractions. Ans. 8, 7, 87, 51, 138, and 8.

2. Reduce ·276, ·384, ·345, ·97142857 to vulgar fractions. Ans. $\frac{35}{300}, \frac{475}{475}, \frac{13}{53}, \frac{54}{53}$.

II. To value an interminate decimal.

RULE. If it is a repeater, carry at 9 instead of 10 on the right hand; and if there is a cipher on the right hand of the multiplier, annex the repeating figure of the product instead of it.

If it is a circulate, multiply as usual; but to the right-hand figure of the product add the carriage from the left-hand figure of the circle. And when there are more lines than one of the product, the circles, or repeaters, must be carried the same length in them all; and the carriage from the left of the circles must be added to the right-hand figure of the sum.

1. What is the value of .7561.? Ans. 15s. 14d. %.

2. What is the value of $\cdot 479$ of a cwt.? Ans. 1 qr. 25 lb. $12\frac{4}{25}$ oz.

3. What is the value of $\cdot 876$ of an acre? Ans. 3 roods, $20_{\frac{1}{2}}$ perches.

4. What is the value of 3634 of a pound? Ans. 7s. $3\sqrt{3}\pi d$.

5. What is the value of 5307 of a guinea? Ans. 11s. $1\frac{1}{2}d$.

6. What is the value of '7386 of a cwt.? Ans. 2 gr. 26 lb. 11 oz. 11.6298 drams.

III. To make circles similar.

RULE. Point off by a comma on the right as many figures from the left of each as there are places in the longest finite part; then extend each of them as many places to the right as is denoted by the least common multiple of the number of places in the several repetends.

1. Make .436 and .573689 similar.

2. Make .729, .5486, and .73654 similar.

3. Make .754, .3, .7298 and .74869 similar.

ADDITION.

RULE. When there are only repeaters, extend them one place beyond the finite ones, and carry at 9 when you add the right-hand column.

When there are circulates, make them similar, and to the right of the sum add the carriage from the left of the circle.

1. Add ·4712, 3·7, ·546, and ·3 together? Ans. 5·129.

2. Add 4.783, 54.721, 7.6, 3 and 54769 together. Ans. 68.05214.

3. Add 161, 241, 31, 511, and 2567 together. Ans. 305.267857142.

4. Add .7186, 34.6734, .21893, and 25.71263 together. Ans. 61.323667394.

5. Add 25, 311, 5619, 495, and 25732 together. Ans. 369.41885891.

SUBTRACTION.

RULE. Extend repeaters one place beyond the finite ones, and borrow 9 on the right when the under figure is the greater. Make circulates similar ; and when there is a carriage from the left of the circle, it must be added to the right-hand figure of the under line before subtracting.

1. From 74.5283 take 5.6. Ans. 68.8616.

2. From 21.5462 take 18.75. Ans. 2.7906.

3. From 27.3836 take 7.1869. Ans. 20.19664937.

4. From 1.87263 take .75428.

Ans. 1.1183488207609.

MULTIPLICATION.

RULE. When the multiplicand is interminate, carry at 9 on the right of a repeater; or multiply as usual in a circulate, and to the right of the product add the carriage from the left of the circle; and, before adding the several products, extend the repeaters the same length in each, and make the circulates similar.

When the multiplier is also interminate, reduce it to a vulgar fraction ; then multiply by the numerator, and divide the product by the denominator.

1. Multiply 74·7386 by 258 Ans. 19282·576. 2. Multiply 38·5436 by 29. Ans. 1117·7654.

3. Multiply 384.5763 by 47.5. Ans. 18267.37698.

4. Multiply 7.3846 by 2.3. Ans. 17.23084175.

5. Multiply 5.4763 by 21.72. Ans. 118.98578.

6. Multiply 38.729 by 45.45. Ans. 1760.4224, &c.

DIVISION.

RULE. When the dividend only is interminate, divide as usual, but annex the repeating figures instead of ciphers in order to carry out the quotient. But when the divisor is in-terminate it must be reduced to a vulgar fraction, and the dividend multiplied by the denominator, and the product divided by the numerator.

1. Divide 7.38467 by 21. Ans. .35165 2465.

2. Divide 3.486 by 15.3. Ans. 22739 3.

3. Divide 27.654 by 16.6. Ans. 1.65926.

4. Divide 8.1 by .93. Ans. 8.6344.8.

5. Divide 27.3 by 2.76. Ans. 9.879518.5.

6. Divide 4.736 by 82.73. Ans. 057248554395

EXTRACTION OF THE SQUARE ROOT.

RULE 1. Divide the given number into periods of two figures each, beginning at the right hand, and pointing to-ward the left in integers, and toward the right in decimals. Every period will give one figure in the root.

2. Find the greatest square number contained in the left. hand period, place its root in the quotient, subtract its square from the said period, and to the remainder bring down the second period for a dividend.

3. Write the double of the part of the root found on the

loft hand of the dividend, divide by it, omitting the units place; set the result in the quotient, and annex it also to the divisor.

4. Multiply the divisor thus completed by the last figure placed in the root : subtract the product from the dividend, and to the remainder bring down the third period for a new dividend ; proceed in the same manner till all the periods are brought down.

Note 1. The root consists of as many whole numbers and decimals as there are periods belonging to each.

 If there is a remainder after all the periods are used, the operation may be continued at pleasure by annexing periods of eiphers.

3. Roots of vulgar fractions are found by extracting the root of the numerator for a new numerator, and the root of the denominator for a new denominator; but, if that cannot be done exactly, reduce the vulgar fraction to a decimal, and proceed as before.

1. Required the square root of 144? Ans. 12.

2. What is the square root of 1728? Ans. 41.5575.

3. What is the square root of 40804? Ans. 202.

4. What is the root of 531118116? Ans. 23046.

5. What is the square root of 56085121? Ans. 7489.

6. What is the square root of 100040004? Ans. 10002.

7. What is the square root of 1020304030201? Ans. 1010101.

8. What is the square root of 00002209? Ans. -0047.

9. What is the root of 2916? Ans. 54.

10. What is the root of 42.1685? Ans. 6.49484.

11. What is the root of 288? Ans. 17.

12. What is the root of $51\frac{2}{5}$? Ans. $7\frac{1}{5}$.

To find a mean proportional between two given numbers extract the square root of their product.

13. What is the mean proportional between 16 and 9? Ans. 12.

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14. What is the mean proportional between 64 and 9? Ans. 24.

To find the side of a square, equal in area to any given superficies, extract the square root of the given area.

15. In a square plantation, containing 505521 trees, each six feet distant, what is the length of the side? Ans. 4266 feet.

16. A gentleman has two fields; the first contains 8 acres, 2 roods, 1 pole,—the second 6 acres, 2 roods; he wishes to exchange them for a square field; required the side of the square? Ans. 49 po.

Note. Circles are to each other as the squares of their diameters.

17. A gentleman has two circular ponds in his pleasure grounds; the diameter of the one is 200 feet, and the other three times as large; what is its diameter? Ans. $346 \cdot 470 \cdot 4$.

18. A maltster has a kiln, 14 feet in diameter, which is too little by $\frac{4}{5}$ for his business, what is the diameter of one that will answer his purpose? Ans. 18.78 feet.

Given any two sides of a right-angled triangle, to find the other side.

The square of the hypothenuse, or longest side, is equal to the sum of the squares of the other two sides; therefore the difference of the squares of the hypothenuse, and either of the other sides, is the square of the remaining side.

19. A wall is 48 feet high, and a ditch before it is 36 feet wide, required the length of a ladder that will reach from the opposite side of the ditch to the top of the wall? Ans. 60 feet.

20. A line, of 205 feet in length, reaches from the top of a steeple to a point 140 feet from its foundation, what is the height of the steeple? Ans. 149.75 feet.

EXTRACTION OF THE CUBE ROOT.

RULE 1. Divide the given number into periods of three figures each, beginning at the right hand in integers, and pointing toward the left. But in decimals, begin at the place of thousands, and point toward the right.

2. Find the greatest cube number, in the left-hand period, and place the root of that number as the first figure of the root sought : subtract the number itself from the said period, and to the remainder bring down the next period for a dividend.

3. Find a divisor by multiplying the square of the part of the root found by 300, divide the dividend by it, and put the quotient figure for the next figure of the root.

4. Multiply the part of the root formerly found by the last figure placed in it, and this product by 30; place this last product under the divisor, and under this product write the square of the figure last placed in the root.

5. Multiply the sum of these three by the figure last placed in the root, and subtract the product from the dividend.

6. To the remainder bring down the next period for a new dividend, with which proceed as before.

Or add up the three last numbers, reckoning the middle one twice in the operation; to this sum annex two eiphers, the result will be the next trial-divisor, with which divide and complete as before.

Required the Cube Root of the following numbers?

1.	1728	Ans.	12
2.	54872	Ans.	38
3.	48228544	Ans.	364
4.	41063625	Ans.	345
5.	40107047967	Ans.	3423
6.	12821119155125	Ans.	23405
7.	14706.125	Ans.	24.5
8.	51.064811	Ans.	3.71
9.	13824	Ans.	24
10.	911	Ans.	41
	0		2

To find the side of a cube, equal in solidity to any given solid, extract the cube root of its solid content.

11. The solid content of a globe is 32768 feet, what is the side of a cube of equal solidity? Ans. 32 feet.

12. Required the side of a cubical mound equal to one whose length is 840 feet, breadth 500 feet, and depth 340 feet? Ans. 522.68 feet.

13. Required the side of a cubical vessel which will contain 100 imperial gallons? Ans. 30.267 inches.

Similar solids are to each other as the cubes of their diameters, sides, &c.

14. A ball, 12 inches diameter, weighs 30 lb., what will a ball weigh whose diameter is 18 inches? Ans. $101\frac{1}{4}$ lb.

15. A ball, 16 inches diameter, weighs 56 lb., what will be the diameter of a ball which weighs 6 times as much? Ans. 29.07 inches.

16. The length of a stone is 10 feet, breadth $4\frac{1}{2}$ feet, and thickness 3 feet, required the dimensions of another 6 times as large? Ans. 18.17 feet long, 8.177 broad, 5.45 thick.

SLIDING RULE.

RULES for working on the Carpenter's Sliding Rule and on Gunter's Scale.

Note. The Rules are commonly marked with A on the Rule, B and C on the Slider, and D on the Girt or Square Line.

To multiply by the Sliding Rule.

RULE. Set 1 on B to one of the factors on A ; then against the other factor on B, you have the product on A.

By Gunter's Scale.

RULE. Extend the compasses from the beginning of the line of numbers to one of the factors ; the same distance shall reach from the other factor to the product.

To divide by the Sliding Rule.

RULE. Set the divisor on B to the dividend on A; they against 1 on B, you have the quotient on A.

SLIDING RULE.

By Gunter's Scale.

RULE. Extend the compasses from the dividend to the divisor ; the same distance will reach from 1 to the quotient.

Proportion by the Sliding Rule.

RULE. Set the first number on B to the second on A; then against the third number on B is the answer on A.

By Gunter's Scale.

RULE. Extend the compasses from the first number to the second ; that extent will reach in the same direction from the third number to the fourth.

Superficial Measure by the Sliding Rule.

RULE. Set the breadth in inches on B to 12 on A; then against the length in feet on A is the content on B, in square feet, &c.

By Gunter's Scale.

RULE. Extend the compasses from 12 to the breadth; that extent set the same way will reach from the length to the content.

Solid Measure by the Sliding Rule.

RULE. Set the length in feet on C to 12 on D, or girt line; then against the side of the square on D you have the answer on C.

By Gunter's Scale.

RULE. Extend the compasses from 12 to the side of the Square ; that extent twice set will reach from the length to the answer.

To extract the Square Root by the Sliding Rule.

RULE. Set the middle division on C to 10 on D; then opposite to the given number on C you have the answer on D.

Note. If the given number consists of 2, 4, 6, &c. figures, the answer is to be found on the left hand of the line C; but if it consists of 3, 5, 7, &c. figures, it is found on the right hand of the line C.

To find a Mean Square by the Sliding Rule.

RULE. Multiply the breadth and depth together, and extract the square root of the product; the root is the mean square. Or set the breadth in inches on C to ditto on D; then against the depth or thickness in inches on C you have the mean square in inches on D, or girt line.

By Gunter's Scale.

RULE. The middle point, between the breadth and depth is the mean square.

DUODECIMALS, OR CROSS MULTIPLICATION,

Is a rule by which artificers cast up the contents of their work.

RULE 1. Write the multiplier under the multiplicand, feet under feet, inches under inches, seconds under seconds, &c.

2. Multiply each denomination of the length by the feet of the breadth, beginning at the lowest, and place each product under that denomination of the multiplicand from which it arises, always carrying one for every 12.

3. Multiply by the inches, and set each product one place farther to the right hand.

4. Multiply by the seconds or parts, and set each product another place toward the right hand.

5. Proceed in this manner with all the rest of the denominations, and their sum will be the answer.

Feet multiplied by feet give feet.
Feet multiplied by inches give inches.
Feet multiplied by seconds give seconds.
Inches multiplied by inches give seconds.
Inches multiplied by seconds give thirds.
Seconds multiplied by seconds give fourths.
12 Fourths = 1 Third,

12 Thirds = 1 Second, or part,

12 Seconds = 1 Inch,

12 Inches = 1 Foot.

1. Multiply 6 feet, 3 inches, by 3 feet, 2 inches. Ans. 19 feet, 9 in. 6 s.

2. Multiply 4 feet, 5 inches, by 3 feet, 6 inches. Ans. 15 f. 5 in. 6 s.

3. Multiply 5 feet, 6 in. by 4 feet, 3 in. Ans. 23 f. 4 in. 6 s.

4. Multiply 6 feet, 6 in. by 3 feet, 8 in. Ans. 23 f. 10 in.

5. Multiply 24 feet, 3 in. by 16 feet, 7 in. Ans. 402 f. 1 in. 9 s.

6. Multiply 48 feet, 7 in. by 36 feet, 6 in. Ans. 1773 f. 3 in. 6 s.

7. Multiply 6 feet, 4 in. 3 s. by 4 feet, 3 in. 6 s. Ans. 27 f. 3 in. 2 s. 10 th. 6 fourths.

8. Multiply 56 feet, 1 in. 4 s. by 48 feet, 3 in. 6 s. Ans. 2709 f. 8 in. 4 s. 8 th.

9. Multiply 68 feet, 8 in. by 9 feet, 10 in. 11 s. Ans. 680 f. 5 in. 7 s. 4 th.

MENSURATION

Is of three kinds; lineal, superficial, and solid. Lineal measure respects length only. Superficial includes length and breadth. Solid measure comprehends length, breadth, and thickness.

PROB. I. To find the superficial content of a board or plank.

RULE. Multiply the length by the breadth.

10. In a board 12 feet long, and $8\frac{1}{2}$ inches broad, how many square feet? Ans. 8 feet, 6 in.

11. Required the area of a plank 14 in. broad, and 16 feet, 6 in. long? Ans. 19 feet, 3 in.

12. In a deal 15 feet, 6 in. long, and 10 in. 6 sec. broad, how many square feet? Ans. 13 f. 6 in. 9 s.

13. Required the content of a plank $20\frac{3}{4}$ feet long, and $12\frac{1}{2}$ inches broad? Ans. 21 f. 7 in. 4 s. 6 th.

14. In a deal $10\frac{1}{3}$ feet long, and $8\frac{1}{4}$ in. broad, how many square feet? Ans. 7 f. 1 in. 3 sec.

Note. If the two ends of a plank or board differ in breadth, add the two breadths and multiply the length by half the sum.

15. How many square feet in a board 12 feet, 9 inches long, the breadth at one end being 15 in., and at the other 10? Ans. 13 f. 3 in. 4 s. 6 th.

PROB. II. To find the solid content of square or anequal-sided timber or stone.

RULE. Multiply the length, breadth, and thickness to-gether.

16. Required the solid content of a tree 16 feet long, and 14 inches the side of the square? Ans. 21 f. 9 in. 4 s.

17. Required the solid content of a tree 14 feet long, and $10\frac{1}{2}$ in. the side of the square? Ans. 10 f. 8 in. 7 s. 6 th.

18. What is the solid content of a tree 24 feet, 6 in. long, and 20 in. the side of the square? Ans. 68 f. 8 s.

19. A piece of timber is $18\frac{1}{2}$ feet long, 14 inches broad, and 9 deep, what is its solid content? Ans. 16 f. 2 in. 3 s.

20. What is the solid content of a piece of timber or stone whose sides are 10 in. by 18, and the length 18 feet? Ans. 22 f. 6 in.

21. What is the solid content of a piece of timber 15 feet, 3 in. in length, breadth 15 in. and depth $4\frac{1}{4}$ in.? Ans. 7 f. 1 in. 9 s. 4 th. 6 fourths.

22. How much timber is there in a tree 2 feet, 6 in. by 1 foot, 10 in. and $38\frac{3}{4}$ feet long? Ans. 177 f. 7 in. 3 p.

Note 1. The usual way to measure round timber is to girt the tree in the middle with a small cord, then $\frac{1}{4}$ of the girt is considered as the side of the square.

2. Tapering timber is measured by girting it in two or more places, and dividing the sum of the girts by their number, for the mean girt.

23. What is the solid content of a round tree 25 feet long, and girt in the middle 45 inches? Ans. 21 f. 11 in. 8 s. 9 fourths.

24. How much timber in a round tree 30 feet

G

MENSURATION.

long, and the girt 42 inches? Ans. 22 f. 11 in. 7 s. 6 th.

25. How many solid feet in a round tree 28 feet, 6 in. long, and the girts 48 in. 42 in. and 36 in.? Ans. 21 f. 9 in: 10 s. 1 th. 6 fo.

3. A more accurate way to measure round timber is to multiply the square of $\frac{1}{4}$ of the girt by twice the length for the solidity.

26. If the length of a tree is 24 feet, and the girt 8 feet, what is the content? Ans. 122.88 feet.

27. The girts of a tree, in 5 different places, are 9.43 ft. 7.92 ft. 6.15 ft. 4.74 ft. and 3.16 ft. and the length of it $17\frac{1}{4}$ feet, what is its solidity? Ans. 54.424992 feet.

			Content
	Length in feet.	Breadth in inches.	in sq. feet, &c.
28.	14	18	21
29.	9	17불	13 1' 6"
30.	$11\frac{1}{4}$	$7\frac{\tilde{3}}{4}$	7 3' 2" 3"
31.	934	$13\frac{1}{4}$	10 9' 2" 3"
32.	$8\frac{1}{4}$	22	15 1' 6"
33.	14 5	20	24 2'
34.	$18\frac{1}{9}$	14	21 7'
35.	$24\frac{3}{4}$	$21\frac{1}{4}$	43 9' 11" 3"
36.	$12\frac{1}{4}$	9	9 2' 3"
37.	30	22	55

BOARD OR SUPERFICIAL MEASURE.

EQUAL-SIDED OR ROUND TIMBER.

	Length in feet.	Side square in inches.	Solid Content in feet, &c.
38.	18	15	28 1' 6"
39.	14	16	24 10' 8"
40.	$16\frac{1}{4}$ 18	94	10 2' 2" 6" 9""
41.	18	8	8

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EQUAL-SIDED OR ROUND TIMBER.

	Length in feet.	Side square in inches.	Solid Content in feet, &c.
12.	12	15	18 9'
43.	22	81	11 0' 5" 6"
44.	27븅	19	68 11' 3" 6"
45.	$6\frac{3}{4}$	$22\frac{1}{4}$	23 2' 5" 8"' 0 ^s
46.	241	$30\frac{3}{4}$	160 10' 6" 3" 4 J
47.	34	61	9 11' 8" 6'''
48.	9	14	12 3'
49.	4	16	7 1' 4"
50.	13	17	26 1' 1"
51.	15불	181	36 10' 0" 10" 6""
52.	17	13	19 11' 5"
53.	191	28	106 2'
54.	24	$32\frac{1}{4}$	173 4' 1" 6"
55.	$29\frac{1}{4}$	31	195 2' 5" 3"'
.56.	$40\frac{3}{4}$	19	102 1' 10" 9"

UNEQUAL-SIDED TIMBER OR STONE.

	Breadth in inches.	Depth or Thick- ness in inches.	Length in feet.	Content in Solid feet, &c.
57.	32	18	141	58
58.	13	10	18	16 3'
59.	81	71	14	6 2' 4" 6"
60.	14	111	9	10 0' 9"
61.	19	$8\frac{3}{4}$	24	27 8' 6"
62.	154	$3\frac{1}{4}$	16	5 7' 2"
63.	11	9	16	11
64.	17	11	41	53 2' 11"
65.	30	19	183	74 2' 7" 6"

MENSURATION.

A CARPENTER'S ACCOUNT.

James Donaldson, Esq. Dr. 1882. July 15. To 753 yds. 3 f. 8 in. flooring at 3s. 6d.

To 151 yds. 9 in. painting at $7\frac{1}{2}d$. To 158 yds. 1 f. 3 in. plastering at $4\frac{1}{2}d$.

- Aug. 3. To 1737 feet of timber at 1s. 6¹/₂d. To 6 roods, 6 yds. 6f. slating at 14s. 6d. To 196 feet, 10 in. 6 p. sawing at ¹/₂d.
- Sept. 7. To 12 deals, each 14 feet, 8 in. long, and 10¹/₂ inches broad, at 2¹/₂d. per foot.
 To 6 Memel logs, each 14¹/₂ feet long, and 11³/₂ inches the side of the square,

at 1s. 8d. the solid foot.

Ans. £286 17 54

66. In a piece of tapering unequal-sided timber, 24 feet 9 inches long, the base at the greater end being 34 inches by 20, and at the other end 17 inches by 10, how many solid feet? Ans. 62 f. 7 in. 9 s. 4 th. 6 fourths.

NOTE. Add the length and the breadth of the bases separately; divide each of the sums by 2, then multiply the quotients together, and that product by the length.

67. How many square feet in the floor, roof, and walls of a house 50 feet long, 18 feet broad, and 15 feet high? Ans. 3840 feet.

68. What is the weight of a plank $24\frac{1}{2}$ feet long, 2 broad, and $1\frac{1}{4}$ thick, at 25 lb. the solid foot? Ans. $1531\frac{1}{4}$ lb.

69. Required the price of the same, viz. $61\frac{1}{4}$ feet, at 1s. 2d. per foot, and the expense of carrying it at $\frac{1}{2}d$. per lb.? Ans. Price 3l. 11s. $5\frac{1}{3}d$.; carriage 3l. 3s. $9\frac{1}{3}d$. $\frac{1}{3}$.

70. How many square feet of paving in a court-

yard, 68 feet 4 inches, by 60 feet 6 inches, and what will it cost at $3\frac{1}{4}d$. the square yard? Ans. 4134 feet, 2 in. cost 6l. 4s. $4\frac{6}{4}d$. $\frac{5}{5}\frac{1}{4}$.

71. A house has three rows of windows, 5 in a row; the height of the first is 5 feet 6 in., the second 5 feet 3 in., and the third 4 feet 9 in.; the breadth of each is 2 feet 6 in. Required the number of feet, and the expense of glazing at $9\frac{1}{2}d$. per square foot? Ans. 193 f. 9 in.; expense 7*l*. 13s. $4\frac{1}{2}d$. $\frac{1}{2}$.

72. How many square yards of flooring are in a house of 4 floors, the ground one included, 60 feet by 30 within the walls, deducting from each floor the vacancy for the stair, 12 feet 4 in. by 8 feet 6 in.; required also the value at 3s. 6d. the square yard? Ans. 753 yds. 3 f. 8 in.; value, 131l. 16s. $11\frac{1}{3}d.$

73. How many square yards of painting in a room 40 feet 6 inches long, 24 feet 3 in. broad, and 10 feet 6 in. high; and how much does it come to at $7\frac{1}{2}d$. the yard? Ans. 151 yds. 9 in. comes to 4l. 14s. $5\frac{6}{4}d$. $\frac{1}{2}$.

74. How many yards of plastering in the roof and walls of a room, 32 feet 6 in. long, 16 feet 6 in. broad, and 9 feet 3 in. high, deducting a door 6 feet 6 in. by 3 feet; and what will it cost at $4\frac{1}{2}d$. the square yard? Ans. 158 yds. 1 f. 3 in. cost 21. 19s. $3\frac{1}{2}d$. $\frac{1}{2}$.

75. A log of wood, 12 feet 6 inches long, was sawed into 9 deals, each 1 foot 9 in. broad; how many superficial feet did they contain? and what is the sawer's wages at $\frac{1}{2}d$. per square foot? Ans. 196 feet, 10 in. 6 s.; and sawer's wages $8s. 2\frac{1}{2}d. \frac{3}{4}$.

76. How many deals, 12 feet 6 in. long, and $8\frac{1}{2}$ in. broad, will floor a room 50 feet by 16? Ans. 90 1^6_7 .

MENSURATICN.

77. How many roods of mason-work in a wall $50\frac{1}{2}$ feet long and $24\frac{1}{4}$ feet high? and what will it cost at 40s. per rood? Ans. 3 ro. 28 yds. $7\frac{1}{2}$ in. cost 7l. 11s. $2\frac{1}{4}d$. $\frac{1}{2}$.

Note. Two feet thick is generally accounted the standard for stone walls, and three half-bricks is reckoned the standard for brick walls: Walls of any other thickness must be reduced to the above standards.

78. What is the expense of a wall 64 feet long, 20 feet high, and three feet thick, at 40s. per rood? Ans. 117. 17s. $0\frac{1}{4}d$. $\frac{1}{4}$.

79. How many square yards of brick-work in a wall 48 feet long, 28 feet high, and $2\frac{1}{2}$ bricks thick? Ans. 248 yds. 8 feet.

Note. In the following question one foot is added to the height of the side-walls as an allowance for levelling.

The content of the gables above the side-walls is found by multiplying $\frac{1}{2}$ the sum of the breadth of the house, and the breadth of the chimney-stalk by the height from the level of the side-walls to the bottom of the chimney-stalk ; and the content of the chimney-stalk is found by multiplying the sum of its breadth and thickness by its height.

80. A house 41 feet long, 20 feet 9 inches wide, and 18 feet 9 inches high; the gables above the side-walls 8 feet 6 inches; the gables are $2\frac{1}{2}$ feet thick; the two chimney-stalks 4 feet wide, $2\frac{1}{2}$ feet thick, and 5 feet 1 inch high.

THE BROACHED HEWN WORK

Of said house is, four skews, each 11 feet 6 inches by 1 foot 7 inches. Four corners, each 18 feet 9 inches by 2 feet 6 inches. Two chimney-stalks, the girt of each 13 feet, and the height 5 feet 3 in.

THE DROVED HEWN WORK.

The rybats and lintels of 6 windows, each 13 feet 11 inches, by 1 foot 3 inches; 6 soles of ditto, each 3 feet 11 inches, by 1 foot 7 inches; one window, the rybats and lintel 9 feet 3 inches, by 1 f. 3 in.; sole of ditto 3 f. 3 in. by 1 f. 7 in. The rybats and lintel of a door 19 f. 3 in. by 1 f. 3 in.; the sole of ditto 4 f. 3 in. by 1 f. 7 in. Three pair of jambs, each 6 f. by 2 f.; the lintels of ditto, each 4 f. 5 in. by 1 f. 3 in. Three inner hearths, each 3 f. 1 in. by 1 f. 6 in. Three outer hearths, each 3 f. 8 in. by 1 f. 8 in. Kitchen-jambs, 8 f. 8 in. by 2 f. 3 in.; lintel of ditto 5 f. 8 in. by 1 f. 3 in.; hearth 4 f. by 1 f. 9 in.; likewise $106\frac{1}{2}$ feet of vents.

How many roods of building are in said house? how many feet of broached hewn work? and how many feet of droved ditto? Also, what are the expenses for workmanship, the building being at 30s. per rood? the broached hewn work at 4d. per square foot, the droved ditto at 5d. and the vents at 6d. per lineal foot? Ans. 9 ro. 5 f. $2\frac{1}{2}$ in. building; 396 f. 10 in. broached hewn work; 307 f. $5\frac{1}{4}$ in. droved ditto; -29*l*. 4s. $1\frac{1}{4}d$. $\frac{95}{103}$ expenses for workmanship.

\$1. How many roods in a slated roof, the length of the ridge being 41 f. 9 in.; and girt from eave to eave, 46 f. 6 in.; allowing 9 in. additional on each side for the eaves; and what will the expense of slating come to at 14s. 6d. the rood? Ans. 6 ro. 6 vds. 6 feet. Expense 41. 9s. 8 d.

FORMS OF BILLS AND PROMISSORY NOTES.

INLAND BILL.

£100. Edinburgh, December 25, 1882. Three months after date, pay to me or order, at the Royal Bank of Scotland here, the sum of one hundred pounds sterling, value received.

To Mr Robert Wilson, { Merchant, Leith.

JOHN ALLAN. ROBERT WILSON.

FORMS OF BILLS.

BILL PAYABLE BY INSTALMENTS.

£150. Edinburgh, December 25, 1882. At three, six, and nine months after date, by equal instalments, pay to me or my order, at your house, the sum of one hundred and fifty pounds sterling, for value received. To Mr John Williams, merchant, ROBERT DUNDAS.

High Street, Edinburgh.

JOHN WILLIAMS.

FOREIGN BILL.

£1356, 16s. Demerara, May 10, 1882. Two months after sight of this my first of exchange, (second and third of the same tenor and date unpaid,) pay to the order of Messrs Brisbane & Co. one thousand three hundred and fifty-six pounds sixteen shillings sterling, value of John Ritchie, Esq., and place it to the account of, as per advice, from JAMES WHITE.

To Mr James Elliot, merchant, Accepted Dec. 25, 1882, Edinburgh. JAMES ELLIOT.

A PROMISSORY NOTE.

£50, 10s. Edinburgh, December 25, 1882. Sixty days after date, I promise to pay to Mr James Brown or order, at my office here, the sum of fifty pounds ten shillings sterling, value received. JOHN YOUNG.

RECEIPTS.

Edinburgh, December 25, 1882.

Received from William Anderson, Ésq., the sum of thirty. five pounds ten shillings and sixpence halfpenny, in full of his account to this date. JOHN GRIEVE.

Edinburgh, November 11, 1882.

Received from William Brown, Esq., the sum of thirty guineas, being the half-year's rent, ending at Martinmas, of that house possessed by him, No 10, North St David Street. John OLIPHANT.

MISCELLANEOUS QUESTIONS.

1. A merchant, on balancing his books, finds he has in cash 412*l*. 10*s*. 6*d*.; goods to the value of 650*l*. 16*s*. 7*d*.; and in the stocks 1509*l*. 16*s*. 10[§]*d*. At that same time he owes A 47*l*. 15*s*. 8*d*., B 105*l*. 18*s*. 9¹/₂*d*., C 14*l*. 15*s*. 2[§]/₄*d*., and D 304*l*. 10*s*., and his household and personal expenses

100

amounted to 2161. 18s. 6d., what is his net estate?. Ans. 18831. 5s. 91d.

2. A privateer takes a prize to the value of 2851l. 4s., of which the captain gets $\frac{1}{15}$, each of 6 officers $\frac{1}{5}$ of the remainder, and the private men, being 45 in number, get the rest equally divided among them: what is each man's share?

Ans. Captain's share,

Each officer's share,

178*l.* 4*s.* 83*l.* 10*s.* $7\frac{1}{2}d.$

Each private man's share, 48l. 5s. 3d. 3. There is a prize of 212l. 14s. 7d. to be divided among a captain, four men, and a boy; the captain is to have a share and a half, the men each a share, and the boy $\frac{1}{3}$ of a share; what ought each person to have? Ans. The captain 54l. 14s. $0\frac{1}{4}d$. $\frac{5}{4}$., each man 36l. 9s. $4\frac{1}{4}d$. $\frac{1}{4}$., and the boy 12l. 3s. $1\frac{1}{4}d$. $\frac{5}{4}$.

4. How many planks will floor a house $60\frac{1}{2}$ feet tong, $33\frac{1}{2}$ feet wide, when the planks are 15 feet long, and 15 inches wide? Ans. 108 $\frac{7}{15}$.

5. Queen Elizabeth came to the throne of England the 17th of November, 1558, and died the 24th of March, 1603, in the 70th year of her age; in what year was she born, and how many months, of 28 days each, did she reign, reckoning 365 days, 6 hours to a year? Ans. She was born in the year 1533, and reigned 578 months, 2 weeks, and one day.

6. A stationer sold quills at 11s. a-thousand, by which he cleared $\frac{3}{8}$ of the money : but growing scarce, he raised them to 13s. 6d. a-thousand : what did he clear per cent. by the latter price? Ans. 96l. 7s. $3\frac{1}{4}d$. $\frac{1}{11}$.

7. A grocer bought 2 hhds. of sugar, the one weighed net 17 cwt. 3 qr. 14 lb. at 2l. 6s. 8d. per cwt., the other weighed net 18 cwt. 1 qr. 21 lb. at $4\frac{1}{2}d$. per lb., which he mingled together; I demand

how much a cwt. of this mixture is worth? Ans. $2l. 4s. 3\frac{1}{2}d. \frac{1}{4}\frac{67}{6}$.

8. Shipped for Jamaica 550 pair of stockings at 11s. 6d. per pair, and 460 yards of stuff at 14d. per yard; in return for which I had 46 ewt. 3 qr. of sugar at 1l. 4s. 6d. per cwt., and 1570 lb. of indigo at 2s. 4d. per lb.; what remains due to me of my adventure? Ans. 102l. 12s. $11\frac{1}{2}d$.

9. My correspondent writes me that he has purchased goods on my account to the amount of 560*l*. 10s., what does his commission come to at $2\frac{1}{2}l$. per cent.? Ans. 14*l*. 0s. 3*d*.

10. A manufacturer having an equal number of men, women, boys, and girls employed, distributes 14*l*. among them per day; to each man he gave 1s. 2*d*., to each woman $7\frac{1}{2}d$., to each boy $3\frac{1}{2}d$., and to each girl 3*d*.; how many had he of each? Ans. 120.

11. If the expenses of building a church that holds 2400 persons amount to 1600*l*., and if $\frac{1}{4}$ of the seats are let at 3s. 6d., $\frac{1}{4}$ at 2s. 6d., $\frac{1}{4}$ at 1s. 6d., and the remaining fourth at 1s., how much per cent. do the heritors receive for their money, after paying their minister yearly 120*l*. of stipend? Ans. 8.4375*l*. or $8_{7\pi}$.

12. A labourer receives 14d. for every weekday from 5th March (beginning on the 6th) to 4th November inclusive, and $11\frac{1}{2}d$. per day during the rest of the year; how much do his wages amount to in a year? Ans. 17l. 4s. 8d.

13. A ship's crew took a prize of $1000\overline{l}$, which they agreed to divide among them according to their pay and the time they had been on board: the officers and midshipmen were 6 months on board, and the sailors 3 months: the officers had 40s. amonth, the midshipmen 30s., and the sailors 22s.; the crew consisted of 4 officers, 12 midshipmen,

and 110 sailors; what share of the prize was each man entitled to?

Ans.	Each	officer's share,	$\pounds 23$	2	54 173
	Each	midshipman's,	17	6	$50 \\ 93 \\ 69 \\ 173 \\ 93 \\ 173 \\ 173 $
	Each	sailor's,			24 173

14. The silk-mill at Derby contains 26586 wheels, and 97746 movements, which wind off or throw 73726 yards of silk every time the great water-wheel, which gives motion to all the rest, goes about, which is three times in a minute. The question is, how many yards of silk may be thrown by this machine in a day, reckoning 10 hours to a day's work; and how many in the compass of a year, deducting for Sundays and holidays 63 days, provided no part of it stands still? Ans. 40077453600 yards.

15. A merchant sends to Spain 1300 pieces of broad cloth, each 47 yards, at 15s. 6d. per yard, to have returns from thence, the one half in wine, at 65l. per 252 gallons, and the other half in oranges, at 3l. 10s. per chest; what quantity of each will he have? Ans. 91791 gallons of wine, and $6764\frac{9}{14}$ chests of oranges.

16. Three farmers, A, B, and C, hired a shepherd for 12*l*. 10s. a-year; they are to pay his wages in proportion to the number of sheep each commits to his care; A has 608, B 1200, and C 1500; what part of the wages must each farmer pay? Ans. A 2*l*. 5s. 11 $\frac{1}{4}d$. $\frac{59}{27}$, B 4*l*. 10s. 8 $\frac{1}{4}d$. $\frac{69}{527}$, and C 5*l*. 13s. $4\frac{1}{4}d$. $\frac{29}{27}$?

17. How much cloth at 5s. 6d. per yard must be given in barter for 14 ewt. 3 qrs. of sugar at 3l. 10s. per cwt.? Ans. 187 yards, 2 qrs. 3_{77} nls.

18. If 2 qts. of linseed sow 121 sq. yds., how much will sow an acre? and what will it cost at 1s. 51d. for 2 qts.? Ans. 10 pks.; cost 2l. 18s. 4d.

19. If a peck of potatoes plant $84_{3\pi}$ sq. yds., how many will plant an acre? Ans. 1 qr. 6 tu. 1 pk. $1\frac{1}{3}$ gal.

20. If the half of a mark buy the fourth of a pound, how much cochineal can I have for a crown? Ans. 3 ounces.

21. If a soldier is allowed 12 lb. of bread in 8 days, how much will serve a regiment, consisting of 750 privates, a year? Ans. 183 tons, 6 cwt. 1 qr. 5 lb.

22. There is gained by trading with a ship 120*l*. 14s.; now suppose that $\frac{1}{4}$ of her belongs to S, $\frac{3}{5}$ to T, $\frac{1}{5}$ to V, and the rest to W, what must each have of the gain? Ans. S 30*l*. 3s. 6*d*., T 45*l*. 5s. 3*d*., V 15*l*. 1s. 9*d*., and W 30*l*. 3s. 6*d*.

23. An apothecary mixes 2 oz. 5 dr. of syrup with 3 oz. 4 dr. of rectified spirit of wine, and also 5 dr. 2 scr. 15 gr. of the bark with 4 oz. 3 dr. 1 scr. 8 gr. of mint-water; how much do all these weigh? Ans. 11 oz. 2 scr. 1 dr. 3 gr.

24. A gentleman has an estate consisting of $12,000\frac{1}{2}$ acres; what is his yearly and daily income at $3\frac{3}{4}d$. for every square pole? Ans. 30,001*l*. 5s. yearly; 82*l*. 3s. $10\frac{3}{4}d$. $\frac{2}{3}\frac{3}{3}$ daily income.

25. There is a lodging of 5 rooms; the circumference of the first is 95 feet 7 inches, of the second 84 feet 9 inches, of the third 79 feet 11 inches, of the fourth 71 feet 6 inches, and of the fifth 59 feet; the height of each room is 10 feet 8 inches; how many yards of paper $32\frac{1}{2}$ inches wide will paper the lodging? Ans. 512 yards, $35\frac{33}{6.2}$ inches.

26. How many allowances for seamen, each 7 oz. 14 dr., may be cut out of 73 cheeses, each weighing 17 lb. $10\frac{1}{5}$ oz.? Ans. $2618\frac{4}{5}$.

27. A draper sells cloth for 350¹, and gains at the rate of 10¹, per cent.; what was the principal

and clear gain? Ans. Principal, 318*l*. 3s. $7\frac{1}{2}d$. $\frac{6}{11}$. Gain, 31*l*. 16s. $4\frac{1}{4}d$. $\frac{5}{11}$.

28. A and B, venturing equal sums of money, clear by joint trade 154*l*.; by agreement A was to have 8*l*. per cent., because he spent his time in the execution of the project, and B was only to have 5*l*. per cent.; what was A allowed for his trouble? Ans. 35*l*. 10s. $9\frac{\alpha}{4}d$. $\frac{1}{4}\frac{2}{3}$.

29. A grocer bought an equal quantity of sugar, tea, and tobacco, for 704*l*. 3s. 4*d*.; he gave $10\frac{1}{2}d$. per pound for the sugar, 5s. 9*d*. per pound for the tea, and 1s. $8\frac{1}{2}d$. per pound for the tobacco; I demand how many pounds he had of each sort? Ans. 1690 lb. of each.

30. A cheesemonger bought 650 cheeses weighing one with another 10 lb. each, which cost him 80 guineas; now he sold them by retail in his shop for $3\frac{1}{2}d$. per lb.; I demand what he gained or lost by them? Ans. He gained 10l. 15s. 10d.

31. A tobacconist sent abroad 20 hogsheads of tobacco, each weighing 11 cwt. 3 qr., and sold them at the rate of 7*l*. 10s. per cwt.; his correspondent remitted him in part payment 1500 guineas; I demand the balance? Ans. 187*l*. 10s.

32. A wine merchant imported 2268 gallons of wine, which cost him at first purchase 549*l*. 10s. 6*d.*, the freight of it cost him 33*l*. 12s., customs, 61*l*. 1s., loading and unloading, carts and porters, 17*l*. 6s. 6*d.*; I demand what this wine stood him per gallon? Ans. 5s. 10*d*.

33. Bought a ton of iron and steel, (there being in number 130 bars,) which cost me 29*l*. 3*s*. 4*d*.; there were 70 bars of steel, which weighed each 8 lb. and cost 5*d*. per lb.; I demand what the iron and steel weighed each? what they cost separately? what the iron cost per lb.? and what each bar weighed one with another? Ans. There were 15 cwt. of iron, and 5 cwt. of steel; the iron cost 171. 10s. and the steel cost 111. 13s. 4d., and each bar of iron weighed 28 lb. and cost $2\frac{1}{5}d$. per lb.

34. Bought 1000 ells of holland by the Flemish ell, and paid down 90*l*.; how must I charge it per ell English to gain 10*l*. on the whole? Ans. 3s. 4d.

35. A butcher buys an ox for 10l. 16s. and after feeding him with 24 pecks of oats at 18s. per qr., and 20 trusses of hay at 1s. 4d., slaughters him and sells the beef, being 36 stones, at $5\frac{1}{2}d$. per lb., 6 stones tallow at 7d. per lb. allowing 14 lb. per stone, and the hide for 1l. 5s.; required his gain or loss ? Ans. Gain 2l. 8s. 10d.

36. A tradesman engages an apprentice for 5 years, and receives 25*l*. of apprentice-fee. He agrees to maintain him, the expense of which is reckoned at 8*d*. per day, and allow him 3*l*. each of the fhree first years, 5*l*. the fourth, and 8*l*. the fifth, for clothes. Now if nothing is reckoned for his work the first year, but the second year the value of it amounts to 6l, the third year to 12l, and the two remaining years always to 6l. more than the year preceding, what does the master gain or lose by his service? Ans. He gains 2l. 3s. 4d.

37. I bought stockings in London at 3s. 10d. per pair, and sold them afterwards in Dublin for 5s. 6d.? in remitting my money home I lost $8\frac{1}{3}l$. per cent., and the charges attending the freight, &c. of the stockings at an average was $1\frac{1}{2}d$. per pair; what did I gain or lose per cent. by them? Ans. I gained 27l. 7s. $4\frac{1}{4}d$. $\frac{3}{4}$ per cent.

38. Divide 43*l*. 12*s*. 9*d*. among 7 men, 9 women, and 3 boys, and give a woman 3 of a man's share, and a boy 9 of a woman's. Ans. A boy's share 1*l*. 12s. $2\frac{1}{4}d$. $\frac{69}{122}$; a woman's 1*l*. 17s. $6\frac{1}{2}d$. $\frac{89}{122}$; and a man's 3*l*. 2s. $7\frac{9}{4}d$. $\frac{67}{122}$.

39. A person paved a court-yard 42 feet 9 in. in front, and 68 feet 6 inches in depth, and in this he laid a footpath, the depth of the court, of 5 feet 6 inches in breadth; the footpath is laid with Purbeck stone, at 3s. 6d. per yard, and the rest with pebbles, at 3s. per yard; what will the whole come to? Ans. 49l. 17s. $0\frac{1}{2}d$. $\frac{2}{3}$.

40. Suppose 2*l*. and $\frac{3}{5}$ of $\frac{1}{2}$ of a pound sterling will buy 3 yds. and $\frac{2}{5}$ of $\frac{3}{5}$ of a yard of cloth, how much will $\frac{3}{4}$ of a yd. cost? Ans. 9s. $4\frac{1}{2}d$.

41. A ladder 40 feet long may be so placed as to reach a window 33 feet from the ground on one side of the street, and by only turning it over, without moving the foot out of its place, it will do the same by a window 21 feet high on the other side; required the breadth of the street? Ans. 56 f. 7.788 inches.

42. If 36 oxen eat up the grass of 10 acres in 4 weeks, and 21 oxen eat up the same in 9 weeks, how many oxen will it maintain for 18 weeks, supposing the grass to grow uniformly during the time? Ans. 15 oxen.

43. A tradesman increased his estate annually a third part, abating 100*l*., which he usually spent in his family, and at the end of $3\frac{1}{4}$ years he found that he was worth 3179*l*. 11*s*. 8*d*.; required how much he had at beginning? Ans. 1421*l*. 7*s*. $6\frac{1}{2}d$.

44. A person making his will, gave to one son $\frac{19}{9}$ of his estate, and to another $\frac{1}{34}$. The first turned out 540*l*. 10s. more than the other; what did the testator leave? Ans. 1538*l*. 12s. 11 $\frac{3}{4}$ *d*. $\frac{24}{491}$.

45. When the hour and minute hands of a clock are exactly together, between 4 and 5 o'clock, what is the time? Ans. $21\frac{9}{11}$ minutes past 4.

46. A hare is 100 of her own leaps before a greyhound, and she takes 5 leaps for the dog's 4, but 3 of the dog's leaps are equal to 4 of the hare's; how many leaps must the dog make before he catches her? Ans. 1200 leaps.

47. A and B can perform a piece of work in 6 days, A and C in 8 days, and B and C in 12 days; in what time would each do it separately? Ans. A would take $9\frac{3}{2}$ days, B 16 days, and C 48 days.

48. In a straight line between two columns, the one 64 feet high, and the other 50 feet, stands a small statue, the head of which is 97 feet from the summit of the higher and 86 feet from that of the lower column, of which the base is just 76 feet from the centre of the base of the statue; what is the distance between the tops of the two columns? Ans. 157.0368 feet.

49. What ought I to charge per yard for cloth which cost me 19s. per English ell, that I may have 25 per cent. profit, after allowing a discount of 5 per cent. and 6 months' credit? Ans. 1l. 0s. $5\frac{1}{2}d$. $\frac{2}{3}$.

DECIMAL COINAGE.

TABLE OF DECIMAL MONEY.

 $\begin{array}{ll} 1 \text{ mil } (m.) &= \frac{1}{10} \frac{1}{00} \frac{1}{0} l. = \frac{2}{3} \frac{1}{3} f. \\ 10 \text{ mils} = 1 \text{ cent } (c.) &= \frac{1}{10} \frac{1}{0} l. = 2\frac{2}{3} d. \\ 100 \text{ mils} = 10 \text{ cents} = 1 \text{ florin } (fl.) = \frac{1}{10} l. = 2s. \\ 1000 \text{ mils} = 100 \text{ cents} = 10 \text{ florins} = 1l. = 20s. \end{array}$

This system is the one most likely, in course of time, to be adopted in this country; the pound sterling will thus be divided into 1000 parts or mils, instead of 960 parts or farthings as at present. Calculations would then be performed, as in Simple Numbers, by placing a point after the pounds and then writing the florins, cents, and mils in their order.

EXAMPLE 1. Express 4l. 5fl. 3c. 7m., and 2l. 5c. 8m. as decimals of 1l. Ans. 4.537l.; 2.058l.

Express in the decimal form,

1.	7 <i>fl</i> .	8c.	5m.	=	·7851.	5.	41.	9fl.	7c.	5m.	= 4.975l.
2.	5	0	8	=	.508	6.	7	Ő	6	.4	= 7.064
3.	6	7	0		·670	7.	8	3	6	0	= 8.360
4.	0	5	4	=	.054	8.	9	0	0	2	= 9.002

Ex. 2. Write 8.475*l*. in pounds, florins, &c. Ans. 8*l*. 4*fl*. 7*c*. 5*m*.

	Writ	e in	ı pou	inds, florins, &c.,	
9 4781.	=4fl.	7c.	8m.	13.2.674l. = 2l.6fl.7c.4m.	
10. 06 3	=0	6	3	14.4.705 = 4 7 0 5	
11407	=4	0	7	$15.5 \cdot 820 = 5 8 2 0$	
12540	=5	4	0	$16.7.042 = 7 \ 0 \ 4 \ 2$	

ADDITION, SUBTRACTION, MULTIPLICATION, AND DIVISION.

RULE. Express the amounts decimally, proceed as in the Simple Rules, and point off 3 figures from the right of the result.

Ex. 3. Add 791. 8fl. 4c. 5m.; 971. 4fl. 5m., and 871. 9m .; also from 2471. 3fl. 4m. take 189.4581. (1.)79.8451. (2.)97.405 247.3041 87.009 189.458 264.2591. Diff. 57.846L Sum. Ex. 4. 41. 8f. 4m. × 26; 3391. 2fl. 5c. 5m. ÷ 15. (1.) 4.8041. (2.) $15 \begin{cases} 5 \ 339 \cdot 255l. \\ 3 \ 67 \cdot 851 \end{cases}$ 28824 9608 Quotient, 22.6171. Product. 124.9042.

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H

17. Add 27*l*. 5*fl*. 6*c*. 7*m*.; 72*l*. 5*fl*. 8*m*.; 56*l*. 7*c*. 5*m*.; 65*l*. 4*fl*. 5*c*.; 49*l*. 6*c*. 8*m*.; 94*l*. 6*m*. Ans. 364[.]674*l*.

18. Add 79l. 5fl. 7c. 5m.; 97l. 4fl. 3c. 2m.; 67l. 3c. 4m.; 45l. 5fl. 6m.; 54l. 8fl.; 76l. 2c. Ans. 420.367l.

19. Add 951. 2m.; 591. 7c. 3m.; 841. 5fl. 2c. 5m.; 481. 2fl. 4m.; 681. 2fl. 3c. 5m.; 861. 7c. 5m. Ans. 441.1141.

20. 148l. 2c. 5m.; 184l. 9c. 8m.; 841l. 7fl. 8c. 9m.; 481l. 7c. 4m.; 418l. 9fl. 9c. 9m.; 814l. 2fl. 1c. 3m. Ans. 2888.198l.

21. From 1841. 2fl. 5m. take 981. 4fl. 5c. 8m. Ans. 85.7471.

22. From 4631. 2fl. 5c. 2m. take 2781. 3fl. 8m. Ans. 184.9441.

685*l*. 2*c*.—398*l*. 4*f*. 7*m*. Ans. 286·613*l*.
 401*l*. 2*c* 5*m*.—197*l*. 3*fl*. 8*m*. Ans. 203·717*l*.
 Mult. 5*l*. 8*fl*. 7*c*. 5*m*. by 25. Ans. 146·875*l*.
 Multiply 7*fl*. 8*c*. 4*m*. by 47. Ans. 36·848*l*.
 Mult. 8*l*. 4*fl*. 5*m*. by 131. Ans. 1101·055*l*.
 Mult. 2*l*. 5*c*. 7*m*. by 542. Ans. 1114·894*l*.
 Divide 487*l*. 5*fl*. 7*c*. 5*m*. by 25. Ans. 19·503*l*.
 Divide 847*l*. 8*fl*. 7*c*. 2*m*. by 36. Ans. 23·552*l*.
 Divide 963*l*. 8*fl*. 2*c*. 9*m*. by 47. Ans. 20·507*l*.
 Divide 796*l*. 8*c*. 1*m*. by 143. Ans. 5·567*l*.

Ex. 5. Reduce 71. 9s. 9d. from the present to the decimal system. Ans. 7.48751.

By Prob. 4, p. 79, 71. 9s. 9d. = 7.48751.

 Reduce from the present to the decimal system,

 33.
 7s. 6d. = $\cdot 375l.$

 34.
 9
 = $\cdot 4875$

 35.
 10
 3
 = $\cdot 5125$

 36.
 13
 $7\frac{1}{2}$ = $\cdot 68125$ 40.

 44.
 10
 14
 10
 14

 55.
 10
 3
 = $\cdot 5125$ 39.
 12
 6
 8
 = $12 \cdot 3333$

 36.
 13
 $7\frac{1}{2}$ = $\cdot 68125$ 40.
 1410
 7
 = $14 \cdot 52916$

Ex. 6. 41. 8/l. 2c. 5m. from the decimal to the present system. Ans. 41. 16s. 6d.

By Prob. 5, p. 79, 4l. 8fl. 2c. 5m., or 4.825l. = 4l. 16s. 6d.

Reduce from the decimal to the present system,

41.9%	1.70	.5n	n = 19s	.6d.	45.	4l	.7	A.8c	.5m	ı.=	4l	.15s	$.8\frac{1}{2}d.$
			=14										
43.5	3	1	=10	71	47.	9	9	3	6	=	9	18	83
44.6	9	8	=13	111	48.	12	6	6	6	=1	2	13	4

PRACTICAL EXERCISES.

1. Find the value of 87 lbs. of tea at 1*fl.* 7*c.* 4*m.* per lb. Ans. 15.138*l.*

2. What is the yearly rent of a house at the rate of 11. 6fl. 7c. 5m. per week? Ans. 87.100l.

3. If 45 quarters of wheat cost 106l. 8f. 7c. 5m., what will one quarter cost? Ans. 2:375l.

4. A bankrupt who owed 3125*l.*, paid his creditors 8*fl.* 2c. 5m. per 1*l.*; what was the amount of his effects? Ans. 2578.125*l.*

5. If a traveller's expenses are 2*l*. 5*f*. 6*c*. 8*m*. per day, what will they be in a year? Ans. 937.320*l*.

6. A farm is let at 1*l*. 3*fl*. 7*c*. 5*m*. per acre, and the whole is 680*l*. 6*fl*. 2*c*. 5*m*.; how many acres does it contain? Ans. 495 acres.

7. If a pound of sugar cost 2c. 5m., what will $2\frac{1}{2}$ cwt. cost? Ans. 7l.

⁸. If 15 men earn 242*l*. 5*fl*. 7*c*. 5*m*., how much will 48 men earn? Ans. 776.240*l*.

9. How much should a man receive for 438 days' work, if he receives 49*l*. 8*fl*. 5*c*. 5*m*. for a year's service? Ans. 59.826*l*.

10. If the wages of 10 men for 24 days be 41*l.* 2*fl.* 6*c.* 4*m.*, what should 36 men receive for 15 days? Ans. 92.844*l.* . 11. What is the commission on 560l. 4fl. 2c. 4m. at $2\frac{1}{2}$ per cent.? Ans. 14 010,6l.

12. What is the interest upon 4857. 8f. 9c. 6m. for 5 years at 21 per cent.? Ans. 60.7377.

13. Required the amount of 363*l*. 6*fl*. 2c. 5m. for 4 years at 4 per cent.? Ans. 421.805*l*.

14. Find the amount of 5001. 3fl. 7c. 5m. for a year and 292 days, at 4 per cent. Ans. 536.4021.

15. How much should be paid for insuring 1050*l*. at 31 per cent.? Ans. 36.750*l*.

16. What is the present worth of 75*l*. 8*f*. 5*c*. 2*m*. due 3 years hence at $2\frac{1}{2}$ per cent.? Ans. 70.560*l*.

17. Find the discount allowed for present payment of 6991. 8f. 7c. 5m. due 219 days hence, at 3 per cent. Ans. 12:3751.

18. At what rate should goods which cost 548l. 9f. 4c. be sold to gain $6\frac{2}{3}$ per cent.? Ans. $585 \cdot 536l.$

19. What part of 28*l*. 3*f*. 6*c*. 8*m*. is 2*l*. 3*f*. 6*c*. 4*m*.? Ans. r_{σ}^{1} .

20. Find the value of 21 cwt. 2 qrs. 14 lbs. of tea at 20*l*. 2*fl*. 5*c*. 6*m*. per cwt. Ans. 438.036*l*.

21. Reduce 181. 1fl. 4c. 4m. to the decimal of 241. Ans. 756.

22. Bought goods for 4971. 8f. 7c. 5m., and sold them for 5371. 7f. 5m.; what was the gain per cent.? Ans. 8 per cent.

23. In 403*l.* 2*fl.* 9*c.* 3*m.*, how many pounds, florins, cents, and mils, and the same number of each? Ans. 363 of each.

THE METRIC SYSTEM

DERIVES its name from the *metre*, which is the unit of length, and is the ten-millionth part of a quadrant of the meridian, or the ten-millionth part of the distance between the poles and the equator.

The principle on which it is founded is, that *ten* of any name make *one* of the next higher name; hence arithmetical operations in this system are performed as in simple numbers.

In the following tables the unit of length is the metre; of surface, the are; of solidity, the stere; of capacity, the litre; of weight, the gram. The Latin derivatives—deci, tenth of; centi, hundredth of; and milli, thousandth of—are prefixed to the several units to denote their subdivisions: while the Greek derivatives—deca or deka, ten; hecto, hundred; kilo, thousand; and myria, ten thousand—are prefixed to the several units to denote their multiples.

TABLES OF THE METRIC OR DECIMAL SYSTEM.

I. Measures of Length.

10 millimetres	=	1 centimetre	=	·394 inches.
10 centimetres	=	1 decimetre	=	3.937 "
10 decimetres	=	1 metre		
10 metres		1 dekametre	=	10.936 yards.
10 dekametres	=	1 hectometre	=	109.363 "
10 hectometres		1 kilometre		
10 kilometres		1 myriametre	=	6.2138 miles.

100 yd. = 91.438 metres; 100 ml. = 160.932 kilometres.

Long distances are stated in kilometres.

II. Measures of Surface.

10 centiares = 1 deciare = 11.960 sq. yards.
10 deciares = 1 are = 119.603 ,
10 ares $= 1$ dekare $= 39.538$ sq. poles.
10 dekares = 1 hectare = 2.471 acres.
100 square metres $= 1$ are.
100 square yards = 83.610 square metres.
100 square poles = 25.292 ares.
100 acres = 40.467 hectares.
Town of the state

Large surfaces are stated in hectares.

THE METRIC SYSTEM.

III. Measures of Solidity.

10 centisteres = 1 decistere = 3.532 cu. feet. 10 decisteres = 1 stere = 35.317 " 10 steres = 1 dekastere = 353.167 "

1 cubic metre = 1 stere; 1 dekastere = 13 c. yards.

IV. Measures of Capacity.

10	centilitres	=	1	decilitre	=	·704 gill.	
10						1.761 pint.	
						2.201 gallons.	
10	dekalitres	=	1	hectolitre	=	2.751 bushels.	
10	hectolitres	=	1	kilolitre	=	3.439 quarters.	

1 cubic decimetre = 1 litre = 61 cu. inches nearly.

100 gallons = 454·346 litres. 100 bushels = 36·348 hectolitres.

V. Measures of Weight.

10 milligram	ns = 1 centig	ram =	·154 grain.	
10 centigram	ms = 1 decign	am = 1	l·543 "	
	ms = 1 gram			
10 grams	= 1 dekag	ram = 5	5.644 drams av.	
10 dekagran	ns = 1 hectog	gram = 3	3.527 ounces "	
10 hectogra	ms = 1 kilogr	am = 2	2.205 pounds "	
10 kilogram	is = 1 myria	$\operatorname{gram} = 22$	2.046 " "	

1 cubic centimetre of distilled water, at its greatest density, weighed in a vacuum = 1 gram.

100 kilograms = 1 quintal; 1000 kilog. = 1 millier. 100 lb. av.=45:359 kilograms; 100 tons=101:605 milliers.

VI. Measures of Value.

10 centimes = 1 decime. 10 decimes = 1 franc = $9\frac{1}{2}d$. ster. nearly.

The par of exchange with London, deduced from the gold coins, is 25 francs $22\frac{1}{2}$ centimes per £1. The decime is seldom mentioned, accounts being kept in francs and centimes.

EXERCISES ON THE METRIC SYSTEM.

1. How many centimetres are in a dekametre, and in a kilometre? Ans. 1000 and 100,000 centim.

2. Write in words-403.035 metres. Ans. 4 hectom., 3 metres, 3 centim., 5 millimetres.

3. Write in metres—75 hectometres and 7.325 myriametres. Ans. 7500 and 73250 metres.

4. How many centiares are in 10 hectares? Ans. 100000 centiares.

5. Write in words—2034.05 ares. Ans. 20 hectares, 3 dekares, 4 ares, 5 centiares.

6. Write in ares-4457 centiares and 425 hectares. Ans. 44.57 ares and 42500 ares.

7. How many centisteres are in 10 dekasteres? Ans. 10000 centisteres.

8. Write in words-33.75 steres. Ans. 3 dekasteres, 3 steres, 7 decisteres, 5 centisteres.

9. Write in centisteres—371 dekasteres. Ans. 371000 centisteres.

10. How many decilitres are in a hectolitre and in a kilolitre? Ans. 1000 and 10000 decilitres.

11. Write in words—307.25 litres. Ans. 3 hectolitres, 7 litres, 2 decilitres, 5 centilitres.

12. Write in litres-37 kilolitres and 75432 centilitres. Ans. 37000 and 75432 litres.

13. How many centigrams are in a kilogram? Ans. 100000 centigrams.

14. Write in words—4053.025 grams. Ans. 4 kilograms, 5 dekagrams, 3 grams, 2 centigr., 5 milligrams.

15. Write in grams—5 quintals and 73452 milligrams. Ans. 500000 and 73:452 grams.

16. How many centimes are in 100 francs? Ans. 10000 centimes.

17. Write in words—240.75 francs. Ans. 240 francs, 7 decimes, 5 centimes.

18. Write in francs-21542 centimes. Ans. 215.42 francs.

Find the sum of,-

19. 7 kilom., 5 dekam., 9 centim.; 79 hectom., 7 metres, 5 millim.; 44 dekam., 8 centim., 3 millim.; 3 myriam., 19 hectom., 12 metres, 15 centim.; and 347 dekam., 15 decim., 15 millim. Ans. 50780.843 metres.

20. 29.575 hectares; 3759 centiares; 1155 deciares; 9.75 ares; and 37.675 dekares. Ans. 3497.09 ares.

21. 14.692 dekasteres; 341.75 steres; 19745 centisteres; 1734 decisteres; and 17.975 dekasteres. Ans. 1039.27 steres.

22. 347 kilol., 17 dekal., 15 decil.; 19 hectol., 15 litres, 25 centil.; 17 kilol., 8 dekal., 7 decil.; 125 kilol., 7 litres, 25 centil.; and 47 hectol. Ans. 495874.7 litres.

23. 55 quintals, 5 kilog., 9 dekag., 5 decig.; 5 quintals, 7 myriag., 9 hectog., 5 grams; 25 dekag., 17 decig., 25 millig.; and 14 kilog., 8 dekag., 7 grams, 8 centig. Ans. 6090334:305 grams.

24. 14 hectog., 4 grams, 8 centig.; 327 dekag., 17 decig., 2 centig.; 9 kilog., 7 hectog., 4 decig.; 141 grams, 17 centig.; 9 dekag., 7 grams, 10 decig. Ans. 14615:37 grams.

25. 17.43 grams; 1.729 decig.; 14 hectograms; 17.9 dekag.; 1735 millig.; 2134 decig. Ans. 1811.7379 grams.

26. 1750 francs, 75 cents.; 17.49 fr.; 379 fr., 25 cts.;
 1743 decimes; 197450 cents. Ans. 4296.29 francs.
 27. 9 myriam., 5 dekam., 7 decim.—24 kilom., 7

27. 9 myriam., 5 dekam., 7 decim.-24 kilom., 7 hectom., 19 decim., 4 millim. Ans. 65348-796 metres.

28. 7569 francs, 75 cents.—789 francs, 3 decimes. Ans. 6780.45 francs.

29. 73 hectoin., 5 metres, 75 decim.-219 dekam. 75 decim., 6 centim. Ans. 5114.94 metres.

30. 175.45 hectares-1695 centiares.

Ans. 17528.05 ares.

31. 5 hectog., 7 grams, 15 centig. \times 25 and 47. Ans. 12678.75 and 23836.05 grams.

32. 25 kilolit., 7 litres, 15 centilit. \times 96 and 205. Ans. 2400686.4 and 5126465.75 litres.

33. 7 myriag., 8 hectog., 15 decig. \div 35 and 52. Ans. 2022.9 and 1361.56 $\frac{19}{29}$ grams.

34. 74593.75 francs ÷ 48 and 365. Ans. 1554.03 and 204.36 and 204.

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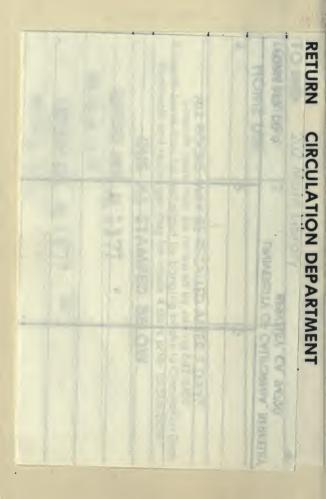
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