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# PREFACE.

THE PACKARD COMMERCIAL ARITHMETIC, of which this is a revision, has been before the public for a space of five years, during which time it has attained a large sale and has given satisfaction to its patrons. No special effort has been made to increase the sale by advertising or making strong statements on its behalf. The authors and publisher have well understood from the beginning that the success of a text-book to be used by intelligent teachers was not in any sense dependent upon promises made in advance, or claims of particular merit which might otherwise escape attention. The book grew naturally out of the practice of the school-room, and the manuscript lessons which were afterwards utilized as copy were submitted to the most exacting tests, and their value in building up the student in a sound knowledge of principles and in the details of practice thoroughly established. And the satisfaction expressed by those who have used the book, has amply sustained the judgment of the authors. The present revision has not been undertaken on account of any dissatisfaction expressed with the old edition, nor because it had not proved in the broadest sense effective, but because the authors have felt that some additions, and particularly in the direction of preparatory work, would make it more acceptable to a large number who now use it, while it would not in any way detract from its utility or symmetry as a complete text-book. The omission of the fundamental rules in the old edition emphasized the fact that it was an advanced commercial text-book, intended for schools not requiring primary instruction. It has come to our knowledge, however,

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#### PREFACE.

that in many of such schools, the better methods of applying the fundamental rules would be acceptable, and that such an addition would make the book more useful in the class-room. In presenting this introductory matter, great care has been taken to divest it of all unnecessary rules and exercises, and to bring it into harmony with the other portions of the book for directness and forcible application of principles. The book, as now presented, is deemed to be a complete Commercial Arithmetic, with little that is redundant, and with all that is requisite to establish the learner in a thorough knowledge of commercial usages. A large number of practical examples have been added in the various departments, not with a view of parading them, but in order to satisfy teachers who wish a wider field to cull from. In making this addition the same rule has been observed which did so much to commend the old edition to practical teachers, viz.: to admit no puzzles nor conundrums, and in every case to test the example by the business standard. In all matters as to business customs or local laws care has been taken to get information from the highest source and of the latest date.

In short, in presenting this practically new book the authors have sought to meet the reasonable expectation of their friends and the public generally in keeping abreast with the times, and to show their faith in honest work.

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#### CONTENTS.

# ARITHMETIC.

# NOTATION AND NUMERATION.

1. Arithmetic is the science of numbers and the art of computation by them.

2. A Unit, or Unity, is one, or a single thing; as one, one foot, one dollar.

**3.** A **Number** is a unit, or a collection of units; as one, four, three feet, five dollars. Numbers are expressed by words, by letters, and by figures.

4. Notation is a system of representing numbers by symbols. There are two methods of notation in use, the *Roman* and the *Arabic*.

5. Numeration is a system of naming or reading numbers.

6. The Arabic method of notation employs ten characters or figures, viz. :

1	$\mathcal{Z}$	3	4	5	6	7	8	9	0
One,	Two,	Three,	Four,	Five,	Six,	Seven,	Eight,	Nine,	Zero.

The first nine of the above are called *significant figures*, because each, standing by itself, represents a value, or denotes some number. They are also called *digits*, from the Latin word *digitus*, which means a *finger*.

The last one is called *zero*, *naught*, or *cipher*, because when standing alone it has no value, or signifies nothing.





## ENGLISH NUMERATION TABLE.



Note .-- It will be observed by a comparison of the French and English systems, that numbers consisting of nine figures or less are read the same.

7. Copy and read the following numbers :

73	102	616	1064	8174	12741
69	333	348	3604	8006	20809
48	570	222	4364	7070	47038
90	895	843	7208	3300	68605

8. Express by figures the following :

- 1. Nineteen.
- 7. One hundred forty-four.
- 2. Twenty-two.
- 8. Three thousand sixteen.
- 3. Forty-six.

5.

- 9. Four thousand forty-four.
- 4. Sixty-eight. Ninety-two.
- 10. Six million two thousand six.
- 11. Sixteen million eight hundred two.
- Eighty-seven. 6.
- Eighty-seven thousand sixty-two. 12.

#### Art. 9.]

## ROMAN NOTATION.

9. In the Roman Notation, seven capital letters are used to express numbers, as follows :

I V X L C D M One, Five, Ten, Fifty, One Hundred, Five Hundred, One Thousand.

Other numbers are expressed by combining the letters according to the following principles :

1. If a letter is repeated, its value is repeated. Thus, III represents three; XX, twenty; CCC, three hundred.

2. If a letter of *less* value is placed *before* one of greater value, the less is taken from the greater. Thus, IV represents four; IX, nine; XL, forty.

3. If a letter of *less* value is placed *after* one of greater value, the less is added to the greater. Thus, VI represents six; XI, eleven; LX, sixty.

4. A bar ( $\overline{}$ ) placed over a letter increases its value a thousand times. Thus,  $\overline{X}$  represents ten thousand;  $\overline{M}$ , one million.

The Roman Notation is used for numbering dials, chapters, pages, etc.

I ADDE OF HOMAN MOTATION	10	. 1	ΓA	BLE	OF	ROMAN	N	OTATION.
--------------------------	----	-----	----	-----	----	-------	---	----------

Roman.	Arabic.	Roman.	Arabic.	Roman.	Arabic.	Roman.	Arabic.
I,	1.	IX,	9.	XX,	20.	XC,	90.
II,	2.	Х,	10.	XXI,	21.	C, •	100.
III,	3.	XIII,	13.	XXX,	30.	CCC,	300.
IV,	4.	XIV,	14.	XL,	40.	D,	500.
V,	5.	XV,	15.	L,	50.	DCC,	700.
VI,	6.	XVIII,	18.	LX,	60.	M,	1000.
VIII,	8.	XIX,	19.	LXXX,	80.	MD,	1500.

11. Express by Roman notation :

1.	Eighteen.	6. Eighty-seven.	11. 584.
2.	Thirty-six.	7. Three hundred sixty.	12. 777.
3.	Forty-eight.	8. Six hundred forty-nine.	<i>13</i> . 1638.
4.	Seventy-six.	9. Five hundred eighty-eight.	14. 1886.
5.	Sixty-four.	10. Two thousand sixty-two.	15. 80000
1	2. Express by	Arabic notation :	
1.	LXXVII.	6. DCCLXVI.   11. MMCCC	XXVII.
2.	CCXIX.	7. DCXLIV. 12. MMDCC	XVIII.
3.	XCVIII.	8. DCXLIV. 13. MMCCX	CIX.

- 4. CCCLIV. 9. MDCXLVI. 14. MMDCCCLXXV.
- 5. DCXXVI. | 10. MCCLXXIX. | 15. MDCCCLXXXVII.

# ADDITION.

13. The Sum or Amount of two or more numbers is a number which contains as many units as all the numbers combined.

14. Addition is the process of finding the sum of two or more numbers.

15. The sign of addition is +, and is read plus.

16. The sign of equality is =, and is read equals, or is equal to.

Thus, 6+2=8 is read 6 plus 2 equals 3, or the sum of 6 and 2 is equal to 3.

17. The sign of dollars is \$; of cents  $\phi$ , ct., or cts.

## 18. To find the sum of two or more numbers.

Ex. Find the sum of 416, 578, 695.

PERATION.	ANALYSIS.—Write the numbers so that like units stand
416	in the same column and begin to add at the right. The
578	sum of the units $(6 + 8 + 5)$ is $(14, 19)$ 19 units, equal to
695	1 ten 9 units. Write the 9 units under the column of units,
	and add the 1 ten to the column of tens, obtaining for the
1689 Sum.	sum (2, 9, 18) 18 tens, equal to 1 hundred 8 tens. Write
11	the O terrs on 1 11 1 61 1 1111, 1 have been 1

the 8 tens under the column of tens, and add the 1 hundred to the column of hundreds, obtaining for the sum (5, 10, 16) 16 hundreds, equal to 1 thousand 6 hundreds, which write in the hundreds' and thousands' places. Hence, the entire sum is 1689.

Notes.—1. Write the numbers in vertical lines. Irregularity in the placing of figures is the cause of many errors.

2. Think of results and not of the numbers themselves. Thus in the above example, do not say 6 and 8 are 14 and 5 are 19, but 14, 19.

3. To avoid repeating the work, in case of interruption, write the figures to be carried in pencil underneath.

-

19. RULE. - Write the numbers to be added so that like units stand in the same column.

Commencing at the right, add each column separately. and if the sum is less than 10, write it under the column added.

If the sum of any column is 10 or more than 10. write the right-hand figure under the column added, and add the remaining figure or figures to the next column.

PROOF.—Find the sum by adding the columns in the opposite direction, thus forming new combinations of figures. If the results agree, the work is probably correct.

	- 10				0
(1)	(2)	(3)	(4)	(5)	(6)
789	682	1234	1357	7812	9876
123	109	5678	9135	3625	6789
456	375	9012	8642	• 4875	9787
$\frac{246}{}$	488	$\underline{3456}$	$\frac{4109}{}$	$\frac{9850}{2}$	8678
(7)	(8)	(9)	(10)	(11)	(12)
568	431	9672	7812	8796	808
134	866	8738	1357	809	7612
680	219	4126	404	4205	37
419	581	1886	9686	6666	4123
723	49	7143	8072	7777	2264
842	376	8275	9706	8088	7714
906	408	9325	5555	4144	9008
294	792	4444	2009	9995	3348
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# EXAMPLES. 20. Conv or write from dictation and add the following.

the ability to add a column of figures easily, accurately, and rapidly. In order that his labor may be lightened and much valuable time saved, not only in after-life but in his school work, he should have various kinds of daily drill exercises in addition, especially in the earlier part of his course of study. The following suggestions will be found valuable in securing accuracy and rapidity:

21. There is nothing of more importance to the student than

ADDITION.

[Art. 22.

ž

22. The 45 simple combinations should be used as an exercise in addition. They may be copied on the blackboard in the following or in irregular order, and the sum should be announced by the student at sight :

1 1	2 2 -	$\frac{3}{1}$	2 2 -	4 1	3 2 -	$5 \\ 1 \\ -$	$\frac{4}{2}$	3 3 -	$6 \\ \frac{1}{2}$	5 2 -	$\frac{4}{3}$	7 1	$\frac{6}{2}$	$5 \\ 3 \\ -$
4 4 -	8 <u>1</u>	$\frac{7}{2}$	$6 \\ 3 \\ -$	5 $4$ $-$	9 1	8 2 -	$\frac{7}{3}$	$6 \\ 4 \\ -$	$5 \\ 5 \\ -$	$\frac{9}{2}$	8 <u>3</u>	$\frac{7}{4}$	$6 \\ 5 \\ -$	9 3 -
8 4	$\frac{7}{5}$	$\frac{6}{6}$	9 4	8 5	$\frac{7}{6}$	$9 \\ 5 \\ -$	$\frac{8}{6}$	77	9 6	87	9 7	8 8	9 8	9 9

23. The above should be supplemented by exercises similar to the following :

74	64	44	94	<b>34</b>	<b>24</b>	14	54	84
8	8	8	8	8	8	8	8	8
					_	—		
45	75	35	15	55	65	95	25	85
9	9	9	9	9	9	9	9	9
9	_9	_9	9	_9	9	_9		9

It is just as easy to add 74 and 8 as 4 and 8. It should be impressed on the mind of the student that 4 and 8 when added always produce 2 in units' place, whatever the number of tens, and the tens are increased by 1. If the student is thoroughly drilled, he will not hesitate when near the end of the column or when the sum is above 20 or 30.

24. Make combinations of 10, 20, 30, or other numbers as often as possible, and add them as single numbers.

Thus, add 9 and 1, 8 and 2, 5 and 5, 4, 3, and 3, etc., as 10; 7 and 2, 6. 2, and 1, etc., as 9; 2 and 3, 4 and 1, 2, 2, and 1, as 5; 8, 7, and 5, 9, 7, and 4, etc., as 20; etc., etc.

In Example 1, Art. 27, think only of the following results: 9, 19, 30, 50.

Drill on the following and similar combinations (10, 20, 30, etc.) until the student can announce the sums at sight:

3	2	1	4	5	3	8	2	2	6	1	2	2	1	3
4	3	4	1	1	1	1	7	6	<b>2</b>	8	1	4	5	3
3	$\frac{5}{2}$	$\frac{5}{2}$	$\frac{5}{2}$	4	6	1	1	$\frac{2}{2}$	2	1	7	4	$\underline{6}$	4

12

7	6	6	8	4	8	9	4	3	2	5	8	9	7	9
6	8	5	4	7	3	2	7	8	9	7	7	8	7	7
7	6	9	8	9	9	9	9	9	9	- 8	5	3	6	4
_	-	_	_	_		-					_			-
1	1	1	3	3	6	8	4	7	7	7	6	9	8	9
2	4	3	3	3	6	4	4	7	4	7	7	6	8	4
3	2	2	1	3	6	1	4	4	4	7	8	7	9	8
4	3	4	3	-1	2	7	8	2	5	9	9.	8	5	9
				_	_	-	_					_	_	

When a figure or number comes between two numbers that make 10, think of the total at once; as 7 + 6 + 3 = 16, 6 + 7 + 4 = 17.

Notes.—1. When three figures are in regular order, the sum may be found by multiplying the middle figure by 3. Thus, 9 + 8 + 7 = 24 ( $3 \times 8$ ); 5 + 6 + 7 = 18; 6 + 7 + 8 = 21.

2. When five figures are in regular order, the sum may be found by multiplying the middle figure by 5. Thus, 1 + 2 + 3 + 4 + 5 = 15 (5 × 3); 5 + 6 + 7 + 8 + 9 = 35.

3. When a figure is repeated several times, multiply it, instead of adding.

4. Do not think of numbers between 10 and 20 as a certain number of units and 1 ten as they are named, but as 1 ten and a certain number of units. Thus, think of 14 as 1 ten and 4 units (onety-four, or one-four), not 4 units and 1 ten (fourteen).

5. Add downwards, for then the sum is found just where it should be placed—at the foot of the column. In proving results, add upwards.

25. Adding two columns at once.—Drill on the following or similar combinations of numbers of two figures each, until the student can announce the sums at sight :

12	<b>24</b>	45	24	37	41	37	62	27	57
16	33	33	26	42	58	45	<b>34</b>	48	27

• When the above have been mastered, give exercises containing three or more numbers, as

12	16	22	<b>24</b>	19	42	56	37	51	27
31	29	33	36	31	<b>24</b>	21	33	25	34
<b>42</b>	38	56	22	44	17	<b>24</b>	28	38	45

26. The following "magic square" may be used as a drill exercise in addition. The sum downwards, from left to right, or diagonally is 54351. To vary the exercise, the teacher may dic-

#### ADDITION.

[Art. 26.

tate, to be added, all the numbers but one in any line or column. The sum can be found by subtracting the number omitted from 54351. The sum of the digits of any result will be a multiple of 9.

4536	9477	3726	8667	2916	7857	2106	7047	1296	6237	486
567	4617	9558	3807	8748	2997	7938	2187	7128	1377	5427
5508	648	4698	9639	3888	8829	3078	8019	2268	6318	1458
1539	5589	729	4779	9720	3969	8910	3159	7209	2349	6399
6480	1620	5670	810	4860	9801	4050	8100	3240	7290	2430
2511	6561	1701	5751	-891	4941	8991	4131	8181	3321	7371
7452	2592	6642	1782	5832	81	5022	9072	4212	8262	3402
3483	7533	2673	6723	972	5913	162	5103	9153	4293	8343
8424	3564	7614	1863	6804	1053	5994	243	5184	9234	4374
4455	8505	2754	7695	1944	6885	1134	6075	324	5265	9315
9396	3645	8586	2835	7776	2025	6966	1215	6156	405	5346

#### EXAMPLES.

27. Copy or write from dictation and add the following :

(1)		(2)		(3)		(4)	(5)
4)	-	(35)		12 85	)	123	382
559	1	<sup>5</sup> 183 { :	13	21 96		456	648
3) 10	0	(95)		\$ 44	21	789	584
75 19	З	0 (62)	90	31 2 66		462	765
81.00		\$ 755	\$U	( 38	1	315	· 406
$3\int^{30}$	4	0 (38).	26	43 7 92	5 31	829	483
6)		(68)	50	5 75	1.0	918	163
6 { 50	5	5 { 54 }	16	<sup>55</sup> 7 56	$\int \frac{42}{}$	234	852
8)		(46)	±0	62 77	49	789	574
(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)
48	71	39	12	77	312	514	376
13	43	34	34	88	123	627	499
82	36	<b>46</b>	<b>56</b>	66	456	842	678
67	94	25	78	99	789	462	437
54	69	83	190	. 41.	987	460	245
87	25	31	89	· 63	654	329	536
43	38	63	76	74	$\underline{321}$	411	984
		and other states of the state o					

14

					10
(14)	(15)	(16)	(17)	(18)	(19)
1234	4121	1728	3416	17642	18114
5678 .	1865	5280	4725	176	285
9212	3760	2246	8850	20048	28510
3456	4825	4153	4975	248	30048
9753	7145	4839	2137	24800	400
8642	3333	2437	8910	1149	17512
7531	7163	4627	2048	1216	8
1594	4943	7342	175	385	14150
7777	7289	8916	1075	19175	30032
the second se	and the second sec	Concession of the local division of the loca	Concession of the local division of the loca	Contraction of the local division of the loc	the second se

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20. Find the sum of the following numbers: Forty-five thousand forty-five; sixteen thousand three hundred sixty; one hundred sixty-seven thousand; eight hundred fifty thousand ninety-two; nine million twenty-four.

21. 46 + 72 + 89 + 93 + 75 + 31 + 58 + 45 + 52 = ?

22. 376 + 416 + 287 + 123 + 456 + 789 + 916 + 328 = ?

**23.** 42 + 175 + 287 + 56 + 63 + 324 + 189 + 172 + 96 = ?

24. 365 + 1728 + 64 + 172 + 89 + 38 + 9 + 5280 + 176 = ?

25. A bushel of corn weighs 56 pounds, a bushel of rye 56 pounds, a bushel of wheat 60 pounds, a bushel of barley 45 pounds, a bushel of oats 32 pounds, and a bushel of buckwheat 48 pounds. What would be the total weight of one bushel of each of the above grains?

26. A farmer raises 375 bushels corn, 419 bushels barley, 849 bushels wheat, 668 bushels oats, 957 bushels barley, and 389 bushels rye. Find how many bushels in all.

27. Find the total distance around a rectangular field 1728 feet long and 1683 feet wide.

28. An exporter of provisions buys 187 barrels hams, 428 barrels shoulders, 475 barrels pork, 229 barrels beef, and 392 barrels bacon. How many barrels in all?

29. In an orchard there are 375 apple trees, 416 pear trees, 37 quince trees, 98 cherry trees, 238 peach trees, and 276 plum trees. How many trees in all?

30. A man pays for a house and lot \$6375. For repairs as follows: mason-work, \$68; plumbing, \$78; carpenter-work, \$164; painting and decorating, \$277. For how much must he sell it to gain \$567 on the total cost? 31. A manufacturer sells on Monday 2387 barrels flour, on Tuesday 2618 bbls., on Wednesday 2178 bbls., on Thursday 2125 bbls., on Friday 2348 bbls., and on Saturday 2496 bbls. How many does he sell during the week ?

32. Find the total number of pounds of tobacco produced in the following states in 1879: Kentucky, 171,121,134; Virginia, 80,099,838; Pennsylvania, 36,957,772; Ohio, 34,725,405; Tennessee, 29,365,052; North Carolina, 26,986,448; Maryland, 26,082,147; Connecticut, 14,044,652; Missouri, 11,994,077; Wisconsin, 10,878,463.

Add the following numbers as they stand, from left to right, and from right to left. [In making out bills and in other commercial operations, a great deal of time can be saved by adding in this manner, without re-arranging the numbers.]

33. 17, 27, 36, 14, 43, 42, 65, 73, 81, 35.
34. 176, 340, 203, 62, 177, 96, 398, 75, 148, 96.
35. 137, 414, 528, 345, 678, 975, 864, 357, 121, 234.
36. 6716, 512, 375, 475, 3842, 5927, 3875, 17525.
37. 2345, 16, 375, 4218, 376, 7, 8475, 247, 39.
38. 123427, 34825, 775, 716, 8976, 37412, 567356, 39723.

Note.—In tally-sheets of pounds, gallons, yards, feet, etc., for convenience in adding, place 10 (20 or 30) numbers in each column as in the following example. (See Note 3, Art. 24.) Add the totals from left to right.

39. Find the total weight of the following 100 boxes of cheese:

***	***	***	***	***	***	***	***	***	***
62	64	66	66	63	61	$\underline{62}$	67	68	69
61	68	64	62	65	60	61	60	62	65
65	66	65	64	67	67	68	66	63	61
66	65	62	61	68	67	64	63	66	66
64	61	60	68	66	64	63	67	69	66
62	62	61	65	61	66	63	67	62	65
63	60	62	61	68	64	65	66	63	67
60	63	63	64	66	65	67	61	60	63
61	67	60	64	67	60	63	61	68	64
67	64	62	61	66	68	64	62	61	60

\*\*\*\*

40. Find the total estimated value of the following crops for the year 1884: Corn, \$640,735,589; wheat, \$330,861,254; rye, \$14,855,255; oats, \$161,528,470; barley, \$29,781,155.

41. Find the total number of bales of cotton produced in the following states in 1879: Mississippi, 955,808; Georgia, 814,441; Texas, 803,642; Alabama, 699,654; Arkansas, 608,256; South Carolina, 522,548; Louisiana, 508,569; North Carolina, 389,598.

42. Find the total number of bushels of wheat produced in the following states in 1879: Illinois, 51,136,455; Indiana, 47,288,989; Ohio, 46,014,869; Michigan, 35,537,097; Minnesota, 34,625,657; Iowa, 31,177,225; California, 28,787,132; Missouri, 24,971,727; Wisconsin, 24,884,689.

Complete the following statements by adding downwards and from left to right. The sums of the totals should be equal.

Days.	Dry Goods.	Shoes.	Furniture.	Books.	Crockery.	Millinery.	Totals.
Monday	647.18	176.42	376.40	117.13	92.17	111.40	**** **
Tuesday	356.25	97.20	184.00	64.72	38.15	57.65	*** **
Wednesday	716.40	200.48	417.65	156.25	127.16	328.40	**** **
Thursday	828.30	227.59	476.00	171.14	287.80	116.38	**** **
Friday	316.17	87.14	148.12	100.80	77.44	79.40	*** **
Saturday	929.12	249.67	417.13	426.00	225.98	429.75	**** **
Totals	**** **	**** **	**** **	*******	******	****.**	**** **

43. SALES FOR THE WEEK ENDING JAN. 21, 1887.

#### 44. SALES FOR 1887.

Months.	Domestics.	White Goods.	Notions.	Woolens.	Dress Goods.	Totals.
January	12248.10	6478.10	3429.12	8117.40	5276.40	********
February	13375.16	7149.37	4176.19	9190.56	6189.24	***** **
March	17177.48	8214.92	4375.94	8237.41	3416.48	***** **
April	15119.43	7175.12	4040.40	7116.40	5255.90	***** **
May	16284.19	8134.37	4287.38	3697.82	1716.32	*****
June	13484.25	6375.28	3343.72	2419.38	2100.58	***** **
July	9119.47	4569.34	2417.75	3129.16	3269.43	***** **
August	10219.36	5162.12	3412.96	4289.50	3716.96	***** **
September	14196.42	7289.40	4128.43	5391.42	4128.31	***** **
October	13184.16	6517.58	3692.29	7214.97	6247.39	***** **
November	14174.12	7288.49	4140.50	8345.68	7116.40	***** **
December	13184.96	6697.13	3990.82	8175.75	7348.19	***** **
Totals	********	*****.**	*******	*******	***** **	********

# SUBTRACTION.

28. The difference between two numbers is a number which, added to the smaller, will produce a result equal to the greater.

29. Subtraction is the process of finding the *difference* between two numbers.

The greater of two numbers whose difference is required is called the *minuend*, and the smaller the *subtrahend*. The result is called the *remainder*.

**30.** The sign of subtraction is -, and is read *minus* or *less*.

Thus, 8-5 is read 8 minus 5, or 8 less 5, and means that 5 is to be taken from 8.

### 31. To find the difference between two numbers.

Ex. Find the difference between 967 and 384.

OPERATION.							
967	Minuend.						
384	Subtrahend.						
583	Remainder.						

ANALYSIS.—Write the smaller number under the greater so that units are under units, tens under tens, etc. Commence to subtract at the right. 4 units from 7 units are 3 units, which write below the line under the column of units. Since 8 tens cannot be taken from 6 tens, take 1 hundred from 9 hundreds, leaving 8 hun-

dreds, and add it (1 hundred = 10 tens) to the 6 tens, making 16 tens. 8 tens from 16 tens are 8 tens, which write under the column of tens. 3 hundreds from 8 (9 - 1) hundreds are 5 hundreds. Hence the result is 583.

Instead of subtracting 1 from the figure of the *upper number* of the next higher order when it has been necessary to add 10 to the figure of the minuend, some persons add 1 to the figure of the *lower number* of the next higher order. This method depends on the principle that adding equivalent numbers to both minuend and subtrahend does not affect the remainder.

In practice, do not think of explanations, nor say 4 from 7 is 3, etc., but think only of results and write them at once. Thus, in the above example, say or think only 3, 8, 5.

Art. 32.]

**32.** RULE.—Write the subtrahend under the minuend so that units of the same order stand in the same column.

Commencing at the right, subtract each figure in the lower number from the one above it, and write the difference in the line below.

If any figure is greater than the one above it, add 10 to the latter, perform the subtraction, and then consider the next figure in the upper number decreased by 1 (or, consider the next figure in the lower number increased by 1).

#### EXAMPLES.

33. Find the difference between

1.	8716 and 4379.	11.	80706040 and 23456789.
2.	917642 and 9819.	12.	76483672 and 87132191.
3.	64321 and 23456.	13.	123456789 and 9897960.
4.	428165 and 317618.	14.	72081099 and 87643229.
5.	9371641 and 876543.	15.	16417528 and 90716801.
6.	7642878 and 6789119.	16.	43184296 and 37529510.
7.	8090403 and 7090508.	17.	100010001 and 9890978.
8.	6380912 and 5270937.	18.	30040050 and 29917168.
9.	7654321 and 1234567.	19.	20103040 and 19181746.
10.	7060509 and 6987969.	20.	40020003 and 20807064.

Find the difference between the numbers in each of the following groups. [In all of these cases the subtrahend is placed above the minuend, the purpose being to give the student practice in subtracting *downward* rather than upward, as the general custom is. It is often requisite in business to perform the work in this way, and the accountant should practice both methods.]

(21)	(22)	(23)	(24)	(25)	(26)
76534	19827	26347	72016	12345	81907
$\frac{81279}{}$	84362	71356	$\underline{99385}$	54321	94371
(27)	(28)	(29)	(30)	( <i>31</i> )	(32)
12467	31617	46789	24681	46897	36478
$\frac{75112}{1}$	42131	50000	$\underline{30502}$	50901	41516

33. There were 50017 post-offices in the United States in 1884 and 51252 in 1885. What was the increase during the year?

34. In 1880, the population of the United States was 50,152,866, and in 1870, 38,558,371. What was the increase during the decade?

35. The area of Alaska is 369,529,600 acres. How much greater is it than Texas, whose area is 175,587,840 acres?

36. The public debt of the United States Nov. 1, 1885, was \$1,447,657,568, and Nov. 1, 1886, \$1,354,347,947. What was the reduction of the debt during the year ?

37. The gross weights (weights of barrels and sugar) and tares (weights of barrels) of ten barrels of sugar are as follows: 326-19, 332-19, 307-18, 321-18, 324-19, 330-19, 313-18, 313-19, 317-17, 327-19. Find the total net weight.

Note.—Find the total gross weight and total tare, and then the difference, or the total net weight.

Population of the following cities of the United States in 1880:

New York, -	-	1,206,590	Buffalo, -	-	-	155,137
Philadelphia, -	-	846,984	Washington,	-	-	147,307
Brooklyn, -	-	580,370	Newark,	~	-	136,400
Chicago, -		503,304	Louisville,		-	123,645
Boston,	-	362,535	Jersey City,	-	-	120,728
St. Louis, -	-	350,522	Detroit,	-	-	116,342
Baltimore, -	-	332,190	Milwaukee,	-	-	115,578
Cincinnati, -	-	255,708	Providence,	-	-	104,850
San Francisco,	-	233,956	Albany,	-	<b>r</b> #	90,903
New Orleans, -	-	216,140	Rochester,	-	-	89,363
Cleveland, -	•• · · ·	160,142	Allegheny,	•	-	78,681
Pittsburg, -	-	156,381	Indianapolis,	-	-	75,074

38. What is the total population of the first column of the above cities? Of the second column? What is the total population of all?

39. What is the difference between the sums of the first and second columns?

40. How much does the total population of New York, Brooklyn, Newark, Jersey City, Hoboken (30,999), Yonkers (18,892), and Long Island City (17,117) lack of being 2,500,000?

41. How much does the total population of Pittsburg and Allegheny exceed that of San Francisco?

#### Art. 34.]

34. Short method of finding the balance of an account.

Ex. Find the balance of the following ledger account:

	r.		0.	Ľ. (	X V	V. E.	PE	CK.	Cr.	
1882.			1			1882.			1	
Mar.	16	Merchandise.	-	1192	97	Apr.	22	Cash.	800	
6.6	30	Sundries.		567	40	"	22	Bills receivable.	1000	
٤٤	31	Merchandise.		384	30	May	1	Merchandise.	317	28
Apr.	22	Interest.		16	48	66	17	Cash.	424	79
••	24	Merchandise.		846	51	July	1	Balance.	852	84
May	17	"		387	25					
				3394	91				3394	91
July	1	Balance.		852	84		-			

ANALYSIS.—It can readily be seen that the debit side is greater; therefore add that side first and write the sum as the total or footing of each side. Then pass to the other side of the account. The sum of the first column is 17, which subtracted from the next higher number, 21, ending with 1, the corresponding figure of the total, leaves 4, which write as the first figure of the balance, carrying the 2 to the next column. (If the right-hand figure of the sum of any column is the same as the corresponding figure of the total, subtract it from itself, and not from the next higher number ending with the same figure; or write 0 in the balance and carry the left-hand figure of the subtracted from 19 leaves 8, the second figure of the balance. Proceed in like manner until all the figures of the balance are obtained. Prove by adding all the numbers, including the balance.

#### EXAMPLES.

(	1.)	()	2.)	(6	(3.)			
Dr. Cr.		Dr.	Dr.	Cr.				
817.20	812.20	237.25	112.27	1075.	375.60			
222.22	214.13	900.	218.36	2318.42	218.24			
427.30	375.	800.	717.49	812.10	717.37			
810.75	412.	718.24	648.	938.40	244.45			
416.30	717.	218.75	118.75	4312.	946.33			
225.		-	538.98	-	222.48			
719.46			203.13		108.75			

35. Find the balances of the following accounts :

21

# MULTIPLICATION.

**36.** Multiplication is the operation of taking one number as many times as there are units in another.

The number taken or multiplied is called the *Multiplicand*. The number which indicates how many times the multiplicand is taken or multiplied, is called the *Multiplier*. The result obtained is called the *Product*.

**37.** The sign of multiplication is  $\times$ , and is read *times*, or *multiplied by*.

Thus,  $5 \times 4 = 20$ , is read 5 times 4 equals 20, or 5 multiplied by 4 equals 20.

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25
2	4	6	8	10	12	14	16	18	20	22	24	26	28	30	32	34	36	38	40	42	44	46	48	50
3	6	9	12	15	18	21	24	27	30	33	36	39	42	45	48	51	54	57	60	63	66	69	72	75
4	8	12	16	20	24	28	32	36	40	44	48	52	56	60	64	68	72	76	80	84	88	92	96	100
5	10	15	20	25	30	35	40	45	50	55	60	65	70	75	80	85	90	95	100	105	110	115	120	125
6	12	18	24	30	36	42	48	54	60	66	72	78	84	90	96	102	108	114	120	126	132	138	144	150
7	14	21	28	35	42	49	56	63	70	77	84	91	98	105	112	119	126	133	140	147	154	161	168	175
8	16	24	32	40	48	56	64	72	80	88	96	104	112	120	128	136	144	152	160	168	176	184	192	200
9	18	27	36	45	54	63	72	81	90	99	108	117	126	135	144	153	162	171	180	189	198	207	216	225
10	20	30	40	50	60	70	80	90	100	110	120	130	140	150	160	170	180	190	200	210	220	230	240	250
11	22	33	44	55	66	77	88	99	110	121	132	143	154	165	176	187	198	503	220	231	242	253	264	275
12	24	36	48	60	72	84	96	108	120	132	144	156	168	180	192	204	216	228	240	252	264	276	288	300
13	26	39	52	65	78	91	104	117	130	143	156	169	182	195	208	221	234	247	260	273	286	299	312	325
14	28	42	56	70	84	98	112	126	140	154	168	182	196	210	224	238	252	266	280	294	308	322	336	350
15	30	45	60	75	90	105	120	135	150	165	180	195	210	225	240	255	270	285	300	315	330	345	360	375
16	32	48	64	80	96	112	128	144	160	176	192	208	224	240	256	272	288	304	320	336	352	368	384	400
17	34	51	68	85	102	119	136	153	170	187	204	221	238	255	272	289	306	323	340	357	374	391	408	425
18	36	54	72	90	108	126	144	162	180	198	216	234	252	270	283	306	324	342	360	378	396	414	432	450
19	38	57	76	95	114	133	152	171	190	209	228	247	266	285	304	323	342	361	380	399	418	437	456	475
20	40	60	80	100	120	140	160	180	200	220	240	260	280	300	320	340	360	380	400	420	440	460	480	500
21	42	63	84	105	126	147	168	189	210	231	252	273	294	315	336	357	378	399	4:20	441	462	483	504	525
22	44	66	88	110	132	154	176	198	220	242	264	286	308	330	352	374	396	418	440	462	484	506	528	550
23	40	09	92	115	139	161	184	207	230	253	276	299	322	345	368	391	414	437	400	483	506	529	552	575
84	48	12	100	120	144	168	192	210	240	264	288	312	330	360	384	408	452	456	480	504	528	552	070	600
A9		-10	100	125	100	175	200	220	200	275	300	325	390	375	400	420	400	475	500	020	000	075	000	020
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25

## 38. Multiplication Table.

Art. 39.]

**39.** To find the product of two numbers when the multiplier does not exceed 12.

Ex. Multiply 456 by 7.

0PERATION. 456 \_\_\_\_\_7

3192

ANALYSIS.—7 times 6 units are 42 units=4 tens and 2 units. Write the 2 units under the figure of the multiplier (the column of units) and add the 4 tens to the next product (the column of tens). 7 times 5 tens are 35 tens, plus 4 tens from the preceding product, are 39 tens=3 hundreds and 9 tens. Write the

9 tens under the column of tens, and add the 3 hundreds to the next product (the column of hundreds). 7 times 4 hundreds are 28 hundreds, plus 3 hundreds from the preceding product are 31 hundreds = 3 thousands and 1 hundred. Write the 1 hundred under the column of hundreds and the 3 thousands in the column of thousands.

**40.** RULE.—Commencing at the right, multiply each figure of the multiplicand by the multiplier, writing the result and carrying as in addition.

#### EXAMPLES.

41.	Multi	ply					Multipl	у			
1.	23456	by	7;	by	8.	8.	789123	by	2;	by	3.
2.	37804	by	9;	by	6.	9.	123567	by	4;	by	5.
3.	24687	by	2;	by	4.	10.	781693	by	6;	by	9.
4.	36925	by	3;	by	8.	11.	417009	by	8;	by	7.
5.	48716	by	5;	by	9.	12.	509048	by	8;	by	7.
6.	90809	by	9;	by	8.	13.	637485	by	6;	by	9.
7.	26048	by	5;	by	7.	14.	748596	by	7;	by	5.

15. There are 5280 feet in one mile. How many feet in 11 miles ?

16. There are 4 gills in one pint, 2 pints in one quart, and 4 quarts in one gallon. How many gills in 63 gallons?

17. There are 2 pints in one quart, 8 quarts in one peck, and 4 pecks in one bushel. How many pints in 379 bushels?

18. There are 12 inches in one foot, and 3 feet in one yard. How many inches in 1760 yards?

19. In one gross there are 12 dozen, and in one dozen 12 units. Find the value of 45 gross lead-pencils at 3 cents each.

20. How many buttons on 6 dozen pair of shoes, if there are 9 buttons on each shoe ?

23

MULTIPLICATION.

42. To find the product of two numbers, when the multiplier is more than 12.

Ex. Multiply 456 by 237.

ANALYSIS .- Write the multiplier under the multipli-OPERATION. cand so that their right-hand figures are in the same ver-456 tical line. Since the multiplier consists of 7 units, 3 tens, 237 and 2 hundreds, the multiplicand is repeated or multiplied 3192 by 7, by 30, and by 200. 7 times 456 is 3192, the first partial product; 30 times 456 is 13680, the second partial 1368 product; 200 times 456 is 91200, the third partial product. 912 The sum of these partial products is 108072, the entire 108072 product. In practice, the ciphers are omitted. In the operation, observe that the first or right-hand figure of

each partial product is directly under the figure of the multiplier used.

**43.** RULE.—Write the multiplier under the multiplicand so that their right-hand figures are in the same vertical line.

Multiply the multiplicand by each significant figure of the multiplier, writing the first or right-hand figure of each partial product under the figure of the multiplier used.

Add the partial products. The sum will be the desired product.

#### EXAMPLES.

44.	Multiply	Mult	iply
1.	1728 by 37; by 481.	9.	23456 by 294; by 3742.
2.	2893 by 26; by 506.	10.	40607 by 144; by 4803.
3.	3904 by 18; by 624.	11.	32738 by 176; by 5964.
4.	5107 by 41; by 375.	12.	91609 by 201; by 6075.
5.	6079 by 59; by 208.	13.	24135 by 345; by 7186.
6.	8125 by 67; by 567.	14.	38246 by 678; by 8297.
7.	9236 by 78; by 781.	15.	94538 by 987; by 9410.
8.	7438 by 89; by 936.	16.	10908 by 406; by 2465.

17. How many hours in the month of January?

18. How many minutes in the month of April?

19. How many seconds in the month of February, 1899?

20. Find the cost of 375 barrels pork at \$14 per barrel.

21. There are 5280 feet in one mile. How many feet in 96 miles? In 208 miles?

22. How many pounds in 471 bushels corn, if there are 56 pounds in one bushel ?

23. In a bushel of timothy seed, there are 45 pounds. How many pounds in 2367 bushels? In 3416 bushels?

24. How many shoes in 24 boxes, if each box contains 12 pair?

25. A certain building has 192 windows, and each window contains 24 panes of glass. How many panes in all?

26. How many feet of wire will be required to fence a field 209 feet square, the fence being 6 wires high and on all sides of the field ?

45. To find the product of two numbers when there are ciphers at the right of the significant figures (6) of one or both.

Ex. Multiply 37600 by 47000.

OPERATION.	ANALYSIS.—Write the numbers so that the right-hand
37600	significant figures are in the same vertical line. 37600
47000	= $376 \times 100$ , and $47000 = 47 \times 1000$ . Since the product
	of two or more numbers is the same in whatever order
2632	they are multiplied, multiply 376 by 47, and their product
1504 -	by 100000 (100 $\times$ 1000), by annexing 5 (3 + 2) ciphers to
767200000	the right.

**46.** RULE.—Write the numbers so that their right-hand significant figures are in the same vertical line. Multiply the significant figures together as if there were no ciphers, and to their product annex as many ciphers as are found on the right of both numbers.

17.	Multiply		Mult	iply		
1.	3600 by 40; h	oy 300.	9.	48400 k	oy 200;	by 1400.
2.	1728 by 80; h	y 500.	10.	37000 k	y 500;	by 2500.
3.	3456 by 70; h	oy 420.	11.	12345 k	oy 600;	by 3600.
4.	3710 by 50; k	oy 360.	12.	28000 k	oy 420;	by 4700.
5.	4000 by 30; k	oy 800.	13.	19700 k	y 340;	by 5800.
<i>6</i> .	2800 by 90; h	oy 370.	14.	14320 k	y 560;	by 6900.
7.	1360 by 60; h	y 200.	15.	84000 k	y 800;	by 7320.
8.	4200 by 20 ; k	ov 500.	16.	96000 k	y 900;	by 4800.

EXAMPLES.

## SHORT METHODS.\*

## 48. To multiply any number of two figures by II.

**49.** RULE.—Place the sum of its digits between them when the sum is less than 10. When the sum is 10 or more than 10, write its right-hand figure in the second place and carry one to the left-hand figure of the multiplicand.

#### EXAMPLES.

50. 1. Multiply 34 by 11.

ANALYSIS. -3 + 4 = 7, which placed between 3 and 4 produces the product 374.

2. Multiply 68 by 11.

ANALYSIS. -6 + 8 = 14. Write 4 in the second place and carry 1 to the 6, the left-hand figure of the multiplicand producing the product 748.

3. Multiply the following numbers by 11: 24, 16, 18, 32, 43, 33, 72, 81, 37, 44, 92, 87, 93, 64, 35, 36, 47, 17, 19, 48, and 57.

## 51. To multiply any number by II.

52. RULE.—Write the 1st right-hand figure, add the 1st and 2nd, the 2nd and 3rd, and so on; finally write the left-hand figure, carrying as usual.

#### EXAMPLES.

53. 1. Multiply 783742 by 11.

Ans. 8621162.

ANALYSIS.—Write the right-hand figure 2; for the remaining figures of the product, add 2 to 4, 4 to 7, 7 to 3, 3 to 8, 8 to 7, and write the left-hand figure, carrying when necessary.

2. Multiply the following numbers by 11: 245, 346, 325, 416, 784, 517, 875, 918, 4218, 7324, 7218, 1728, 4375, and 8376.

# 54. To multiply by any number of two figures ending with 1.

55. RULE.—Multiply by the tens of the multiplier, writing the product under the multiplicand one place to the left, and add. Or,

<sup>\*</sup> It is suggested that these short methods be studied in connection with the more advanced work—one method with each lesson; or they may be presented to the student, one at a time, with the daily drill exercises on the fundamental rules.

Write as the first figure of the product the unit figure of the multiplicand; multiply each figure of the multiplicand by the tens of the multiplier, and at the same time, add mentally to each product the figure to the left of the one multiplied, carrying as usual.

#### EXAMPLES.

56. 1. Multiply 456 by 61.

1sт орен 456 <u>2736</u> 27816	$\times$ 61	2nd ope 45 	6 6 6	ANAI product. 4. 6 × 5 carry 3.	$\begin{array}{c} 6 \times \\ 6 + 4 \\ 6 \times \end{array}$	2nd : 6 + 5 carried 4 + 3	метної = 41. l) + 4 : (carried	Write = 38. W = 27.	te 6 i 1 and Write	n the carry 8 and
Mu	ltiply				Mul	tiply				
2.	864 b	y 61;	by 4	1.	5.	2345	by 12	1; by	111.	
3.	717 b	y 31;	by 7	1.	6.	7416	by 51	; by 8	1.	
4.	447 b	y 21;	by 81	1.	7.	8324	by 41	; by 2	1.	

NOTE.—The first method may be used with the following multipliers, by placing the products two places to the left.

Mul	tiply	Multiply
8.	375 by 301; by 401.	11. 483 by 701; by 801.
9.	425 by 201; by 101.	12. 376 by 201; by 901.
10.	469 by 601; by 501.	13. 875 by 301; by 401.

### 57. To multiply by any number between 12 and 20.

58. RULE.—Multiply by the units of the multiplier, writing the product under the multiplicand one place to the right, and add. Or,

Multiply the units of the multiplicand by the units of the multiplier, write the units of the product, and carry the tens, if any, to the next product; multiply the remaining figures of the multiplicand by the units of the multiplier, and at the same time add mentally to each product the figure to the right of the one multiplied, carrying as usual; finally, to the left-hand figure of the multiplicand, add the number to be carried, if any, and write the result.

#### [Art. 59.

#### EXAMPLES.

**59.** 1. Multiply 456 by 18.

522 by 15; by 19.

376 by 18; by 16.

$\begin{array}{cccc} \text{1st operation.} & 2 \text{nd operation.} \\ 456 & 456 \\ \underline{3648} & \underline{18} \\ 8208 & 8208 \end{array}$	ANALYSIS, 2ND METHOD. $-8 \times 6 = 48$ . Write 8 and carry 4. $8 \times 5 + 4$ (carried) $+6 = 50$ . Write 0 and carry 5. $8 \times 4 + 5$ (carried) $+5 = 42$ . Write 2 and carry 4. $4 + 4 = 8$ .
Multiply	Multiply
2. 785 by 13; by 17.	6. 1234 by 14; by 16.
3. 378 by 14; by 16.	7. 2345 by 16; by 18.

Note.—The first method may be used with the following multipliers by placing the products two places to the right.

8. 3456 by 19; by 13.

9. 7891 by 17; by 15.

Mul	tiply	Multiply	
10.	875 by 101; by 108.	14. 147 by 108; by 101	L.
<i>11</i> .	936 by 102; by 103.	15. 385 by 104; by 107	7.
12.	877 by 104; by 106.	16. 783 by 105; by 103	3.
13.	736 by 105; by 109.	17. 546 by 107; by 100	3.

# 60. To multiply by any number ending with 9.

**61.** RULE.—Multiply by 1 more than the given multiplier, and from the result subtract the multiplicand.

#### EXAMPLES.

62. 1. Multiply 387 by 49.

			0	PERATION.
387	product	by	1	
19350	"	66	50	
18963			$\overline{49}$	(Subtracted downwards.)

# Multiply

## Multiply

2.	76 by 49; by 39.	5. 312 by 19; by 89.
3.	87 by 29; by 99.	6. 427 by 39; by 79.
4.	45 by 59; by 69.	7. 825 by 29; by 69.

4. 5.

# 63. To multiply by any multiple of 9 less than 90.

**64.** RULE.—Multiply by the multiple of ten next higher than the given multiplier, and from the result subtract one-tenth of itself.

#### EXAMPLES.

#### 65. 1. Multiply 785 by 63.

785				
$\frac{70}{54050}$	- 7 - 1	1	NO	ANALYSIS. $-63 = 70 - 7$ . $785 \times 70 = 54950$ . Divide 54950 by 10 by placing its digits one
54950 5495	product	by 	70	place to the right. $54950-5495 = 48455$ .
49455			63	

Multiply

Multiply

OPERATION.

	<u>1</u> <u>1</u>	p-J
2.	67 by 18; by 27.	6. 345 by 36; by 45.
3.	34 by 36; by 45.	7. 567 by 18; by 72.
4.	77 by 54; by 63.	8. 518 by 27; by 63.
5.	84 by 72 ; by 81.	9. 724 by 54 ; by 81.

# 66. To multiply by 25.

67. RULE.—Add two ciphers and divide the result by 4. Or,

Divide the number by 4; if there is no remainder, add two ciphers; if there is a remainder of 1, add 25; of 2, add 50; of 3, add 75.

#### EXAMPLES.

68. 1. Multiply 446 by 25.

OPERATION.ANALYSIS.—Since 25 is equal to 100 divided by 4, multiplying by 100 and dividing the result by 4, is the same as multiplying by 25.

2. Multiply the following numbers by 25 :--24, 36, 37, 49, 62, 387, 448, 512, 746, 424, 817, 937, 544, 717, 318, 324, 256, 556, 9224, 8378, 5280, 1728, 5648.

[Art. 69.

69. To multiply by any number one part of which is a factor of another part.

EXAMPLES.

70. 1	. Multip	ly 57	76 by 287.	2	Mu	ultiply 56	17 k	y 936.
01	PERATION.					OPERATION.		
576					567			
287					936			
4032	product	by	7.	510	)3	product	by	9.
16128	66	66	$28 (4 \times 7)$	. 20	)412		"	$36(4 \times 9).$
530712	66	66	287.	530	712	66	66	936.
Multipl	у			Mult	iply			
3. 227	by 369;	by	427.	8.	932	by 183;	by	927.
4. 516	by 246;	by	568.	9.	718	by 284;	by	832.
5. 344	by 126;	by	124.	10.	529	by 546;	by	756.
6. 728	by 426;	by	189.	11.	638	by 217;	by	618.
7. 325	by 147;	by	273.	12.	435	by 248;	by	428.

71. To multiply by any number near and less than 100, 1000, etc.

72. The Complement of a number is the difference between the number and the unit of the next higher order.

**73.** RULE.—Add to the multiplicand as many cipher's as there are ciphers in the unit next higher than the multiplier, and from the result subtract the product obtained by multiplying the multiplicand by the complement of the multiplier.

#### EXAMPLES.

74. 1. Multiply 456 by 98.

						OPERATI	ION.				
					45600	produc	et by	100.			
					912	66	66	2.			
					44688	66	66	98.			
Mu	ltip	ly					Mu	ltiply			
2.	77	by	99;	by	93.		5.	387 b	y 93;	by	999.
3.	84	by	98;	by	95.		6.	416 b	y 95;	by	994.
4.	72	by	94;	by	96.		7.	528 b	y 93;	by	992.

30

# CROSS MULTIPLICATION.

75. Cross Multiplication depends upon the following principles:

Units	multiplied	by	units	produce	units
Tens	66	66	units		
Units	**	66	tens	ľ .	tens.
Hundreds	66	" "	units	í	
Tens	66	**	tens	4	hundreds.
Units	66	44	hundreds		
Thousand	.s * **	66	units	í í	
Hundreds	66	**	tens		
Tens	**	66	hundreds		thousands.
Units	6.6	66	thousands		
Ten-thous	ands "	"	units	í Í	
Thousand	S "	*6	tens		
Hundreds	46	**	hundreds	4	ten-thousands
Tens	66	66	thousands		
Units	66	66	ten-thousands	j	
	Etc., e	tc.			

Ex. Multiply 68 by 74.

1	ns.	9	U	D'A	2.

-

OPERATION.	ANALYSIS.
68	$4 \times 8 = 3   2$
74	$4 \times 6 + 3 \text{ (carried)} + 7 \times 8 = 8 3$
5032	$7 \times 6 + 8 \text{ (carried)} = 5 0$

Ex. Multiply 579 by 42.

Ans. 24318.

OPERATION.	ANALYSIS.
579	$2 \times 9 = 1 \mid 8$
42	$2 \times 7 + 1$ (carried) $+ 4 \times 9 = 5$ 1
24318	$2 \times 5 + 5$ (carried) $+ 4 \times 7 = 4$
	$4 \times 5 + 4$ (carried) = 2 4

Ex. Multiply 567 by 348.

Ans. 197316.

 OPERATION.
 ANALYSIS.

 567
  $8 \times 5 = 40$   $8 \times 6 = 48$   $8 \times 7 = 56$  

 348
  $4 \times 5 = 20$   $4 \times 6 = 24$   $4 \times 7 = 28$  

 197316
  $3 \times 5 = 15$   $3 \times 6 = 18$   $3 \times 7 = 21$  

 19
 7
 3
 1
 6

76. To multiply together numbers of two figures each, whose units are alike.

x. M	ultiply	76	by	46.					Ans.	349
OPERAT	ION.					1	ANALY	TSIS.		
71	5							$6 \times 6$	= 3	6
$\frac{40}{3490}$	3			$_{6\times 4}^{6\times 7}\Big\}$	$6 \times 1$	11 + 3	(car	ried)	= 6	9
				•	$4 \times$	7+6	(car	ried)	= 3	4

Ex. Multiply 135 by 65.

OPERATION. ANALYSIS.  $5 \times 5 = 2 \mid 5$ 135 $5 \times 13 \atop 5 \times 6$   $\overline{5 \times 19} + 2 \text{ (carried)} = 9$  7 65 8775  $\overline{6 \times 13} + 9$  (carried) = 8 7

77. RULE. -- Multiply units by units for the first figure of the product, the sum of the tens by units for the second figure, and tens by tens for the third figure, carrying when necessaru.

EXAMPLES.

78. Multiply 1. 56 by 56; 72 by 32; 94 by 44. 65 by 75; 87 by 37; 46 by 36. 2. 99 by 49; 85 by 75; 34 by 24. 3. 47 by 37; 67 by 57; 85 by 45. 4. 125 by 65; 126 by 36; 154 by 84. 5. 76 by 76; 36 by 36; 114 by 114. 6.

79. To multiply together numbers of two figures each, whose tens are alike.

Ex. Multiply 87 by 85.

Ans. 7395.

OPERATION.	ANALYSIS.
87	$5 \times 7 = 3 \mid 5$
<u>85</u> 7395	$\left\{\begin{array}{c}8\times5\\8\times7\end{array}\right\}8\times12+3=9\left 9\right$
	$8 \times 8 + 9 = 7 3$

F

96.

Ans. 8775.

 Ex. Multiply 127 by 122.
 Ans. 15494.

 OPERATION.
 127  $2 \times 7 = 1$  4

 127  $2 \times 7 = 1$  4

 122  $12 \times 2$  1
 2

 15494  $12 \times 7$   $12 \times 9 + 1 = 10$  9

  $12 \times 12 + 10 = 15$  4

80. RULE.—Multiply units by units for the first figure of the product, the sum of the units by tens for the second figure, and tens by tens for the remaining figures, carrying when necessary.

#### EXAMPLES.

81. Multiply

87 by 82; 81 by 87; 65 by 63.
 47 by 44; 56 by 52; 58 by 57.
 73 by 76; 79 by 75; 68 by 63.
 44 by 43; 52 by 55; 67 by 63.
 116 by 117; 107 by 105; 125 by 122.

82. To multiply together two numbers whose tens are alike, and the sum of whose units is ten.

83. RULE.—Multiply the units together for the two right-hand figures of the product, one of the tens by 1 more than itself for the remaining figures.

#### EXAMPLES.

84. 1. Multiply 76 by 74.

right hand figures of the product

Ans. 5624.

ANALYSIS.  $-6 \times 4 = 24$ , the two right-hand figures of the product.  $6 \times 7 (6 + 1) = 42$ , the remaining figures.

Multiply mentally

24 by 26; 85 by 85; 128 by 122.
 3. 17 by 13; 94 by 96; 112 by 118.
 4. 34 by 36; 37 by 33; 104 by 106.
 5. 25 by 25; 43 by 47; 143 by 147.
 6. 35 by 35; 56 by 54; 152 by 158.

# 85. To multiply by means of complements (72).

Ex. Multiply 991 by 996.

PERATION.	ALGEBRAIC MULTIPLICATION.
9919	991 = 1000 - 9 and $= 2000 - 12$
9964	$996 = 1000 - 4 \int sum = 2000 - 13$
987036	$1000 \times 1000 - 9 \times 1000$
	$-4 \times 1000 + 36$
	$(1000 - 13) \times 1000 + 36$

ANALYSIS.—From the above algebraic multiplication, it is observed : 1st, that as many of the right-hand figures as there are ciphers in the unit of comparison may be obtained by multiplying the complements together ; 2nd, that the second part of the result is equivalent to the sum of the numbers less the unit of comparison multiplied by that unit.

The sum of the numbers less the unit of comparison may be obtained by adding the numbers and omitting the 1 at the left-hand, or by subtracting either complement from the opposite number. Thus, 991 - 4 = 987.

86. RULE.—From either number subtract the complement of the other, and to the right of the remainder write the product of the complements.

Notes.—1. When there are less figures in the product of the complements than ciphers in the unit of comparison, write ciphers in the result to supply the deficiency.

2. When there are more figures in the product of the complements than ciphers in the unit of comparison, add the excess on the left-hand to the second part of the result.

3. After practice, the complements may be omitted in the operation.

#### EXAMPLES.

87. 1. Multiply 88 by 95; 975 by 993; 9999 by 9999.

8812 775225 9999.	1
	-1
955 9937 99999.	1
8360 769575 99980	001
Multiply Multiply	
2. 97 by 99; by 94. 8. 993 by 992; by	994.
3. 88 by 91; by 95. 9. 990 by 991; by	988.
4. 89 by 93; by 96. 10. 982 by 994; by	995.
5. 75 by 97; by 98. 11. 925 by 996; by	994.
6. 92 by 98; by 93. 12. 875 by 992; by	993.
7. 86 by 94; by 95. 13. 847 by 990; by	988.
88. To multiply together two numbers of the same number of figures over and near 100, 1000, etc.

Ex. Multiply 116 by 103.

PERATION.	ALGEBRAIC MULTIPLICATION.			
¥16	$116 = 100 + 16 \\ 103 = 100 + 3 \\ 3 \\ 3 \\ 3 \\ 3 \\ 3 \\ 3 \\ 3 \\ 3 \\ 3$			
105	$100 \times 100 + 16 \times 100$			
11948	+ 3 × 100 + 48			
	$(100 + 19) \times 100 + 48$			

89. RULE.—From the sum of the numbers subtract the unit of comparison, and to the right of the result write the product of the excesses. (See Notes to Art. 86.)

#### EXAMPLES.

90	• Multiply	Multiply
1.	112 by 106; by 111.	5. 145 by 107; by 112.
2.	102 by 103; by 104.	6. 176 by 111; by 108.
3.	122 by 108; by 105.	7. 1004 by 1006; by 1907.
4.	116 by 107; by 112.	8. 1125 by 1008; by 1012.

91. To multiply together two numbers, one of which is more and the other less than 100, 1000, etc.

Ex. Multiply 109 by 97.

OPERATION		ALGEBRAIC MULTIP	LICATION.	
<b>¥</b> 09	9 excess.	109 = 100 + 9		
97	3 complement.	$97 = 100 - 3 \int 200$	/ + 0	
$\overline{\frac{10600}{27}}$	Product of excess	$100 \times 100 +$	$\begin{array}{c} 9 \times 100 \\ 3 \times 100 \end{array}$	- 27
$\frac{1}{10573}$ (	and complement.	$(100 + 6) \times$	100	- 27

**92.** RULE.—Multiply the sum of the numbers less the unit of comparison by that unit, and from the product subtract the product of the excess and complement.

#### EXAMPLES.

93	. Multiply	Multiply
1.	107 by 97; by 95.	5. 1005 by 91; by 93.
2.	112 by 96; by 92.	6. 1007 by 95; by 97.
3.	116 by 94; by 98.	7. 1012 by 99; by 92.
4.	108 by 91; by 99.	8. 1018 by 94; by 96.

## DIVISION.

94. Division is the operation of finding how many times one number is contained in another.

The number divided is called the *dividend*. The number by which it is divided is called the *divisor*. The result obtained is called the *quotient*. The part of the dividend which remains after the operation is completed is called the *remainder*.

95. The sign of division is  $\div$  and is read *divided by*.

Thus,  $16 \div 2 = 8$  is read, sixteen divided by two equals eight.

## 96. To divide when the divisor does not exceed 12.

Note.—When the work is performed mentally, as in the following operation, the process is called *Short Division*.

Ex. Divide 1859 by 4.

 $\begin{array}{r} \text{operation.} \\ 4 \underline{) 1859} \\ 464 \underline{3} \\ 464 \underline{3} \\ 4\end{array}$ 

ANALYSIS.—Write the divisor at the left of the dividend, as in the operation, and begin to divide at the left. 4 is not contained in 1 thousand, the highest order of the dividend, therefore, divide 18 hundreds by 4. 4 is contained in 18 (hundreds), 4 (hundred) times, and 2 hundreds

remain. Write the 9 hundred under the line in hundreds' place, and reduce the 2 hundreds remaining to tens, making 20 tens, which added to the 5 tens of the dividend, make 25 tens. 4 is contained in 25 (tens), 6 (tens) times and 1 ten remains. Write the 6 tens under the line in tens' place, and reduce the 1 ten remaining to units, making 10 units, which added to the 9 units of the dividend, make 19 units. 4 is contained in 19 (units), 4 (units) times, and 3 units remain. Write the 4 units in units' place, and write the remainder over the divisor, with a line between them in the form of a fraction, thus,  $\frac{3}{4}$ (three-fourths). The complete result is  $464\frac{3}{4}$ .

Observe that each quotient figure is placed directly under the last figure of the dividend used.

In practice, do not think of explanations, etc.; but, think only of the partial dividends and quotient figures. Thus, in the above example, say or think, 4 into 18 4 times, into 25 6 times, into 19 4 times, etc.

#### DIVISION.

97. RULE. — Write the divisor at the left of the dividend with a curved line between them.

Beginning at the left, divide each figure of the dividend by the divisor, and place the quotient beneath the figure divided. Whenever a remainder occurs, prefix it to the following figure of the dividend, and divide as before.

Continue the operation until all the figures of the dividend have been divided, and place the remainder, if any, over the divisor at the right of the quotient.

**98.** PROOF.—Multiply the quotient by the divisor, and to the product add the remainder. If the result equals the dividend, the work is probably correct.

#### EXAMPLES.

99. Divide

#### Divide

1.	78912348 by 2; by 3.	11.	103050709 by 2; by 5.
2.	97652464 by 4; by 6.	12.	214161810 by 3; by 6.
3.	16327620 by 5; by 6.	13.	425262728 by 4; by 7.
4.	78070804 by 4; by 7.	14.	123456789 by 3; by 8.
5.	12345678 by 6; by 9.	15.	246801234 by 6; by 11.
6.	988654320 by 5 ; by 8.	16.	789123650 by 7; by 10.
7.	234568836 by 4; by 9.	17.	287236450 by 5; by 12.
8.	357212254 by 2; by 7.	18.	176111888 by 6; by 11.
9.	246886425 by 5; by 9.	19.	1010101010 by 7; by 9.
10.	217181916 by 7; by 9.	20.	200200200 by 8; by 12.

21. In one square yard there are 9 square feet. How many square yards in 41652 square feet ?

22. There are 12 pence in one shilling. How many shillings in 124656 pence?

23. In a barrel containing 1068 eggs, how many dozen? What is their value at 23 cents per dozen?

24. In one foot there are 12 inches. How many feet in 63360 inches?

25. There are 2 pints in one quart, and 4 quarts in one gallon. How many gallons in 160048 pints ?

26. There are 8 quarts in one peck, and 4 pecks in one bushel. How many bushels in 349056 quarts ?

## 100. To divide by any divisor greater than 12.

Note.—When the work is all written, as in the following operation, the process is called *Long Division*.

#### Ex. Divide 13218 by 43.

OPERATION.	ANALYSIS.—Since 43 is not contained in 13
Divisor. Dividend. Quotient.	(thousands), we take 132 (hundreds) for the
43 ) 13218 ( $307\frac{17}{43}$	first partial dividend. 43 is contained in 132
129	(hundreds), 3 (hundred) times. 43 × 3 (hun-
910	dreds) = $129$ (hundreds), which write under
010	the 132 (hundreds), and subtract. The re-
301	mainder is 3 (hundreds), to which annex the 1
17 Remainder.	(ten) of the dividend, and the second partial
	dividend is 31 (tens). 43 is not contained in 31

(tens), therefore write 0 as the next figure of the quotient. Annex to the partial dividend, 31 (tens), the 8 (units) of the dividend, and the next partial dividend is 318 (units). 43 is contained in 318 (units), 7 (units) times.  $43 \times 7$  (units) = 301 (units), which write under the 318 (units) and subtract. The remainder is 17 (units). Indicate the division of this remainder in the form of a fraction, thus:  $\frac{17}{43}$ , and annex it to the quotient, producing  $307\frac{17}{43}$  for the complete quotient.

**101.** RULE.—Write the divisor at the left of the dividend, with a curved line between them.

Take for the first partial dividend the least number of figures on the left that will contain the divisor, and write the quotient figures at the right.

Multiply the divisor by the quotient, write the product under the partial dividend, and subtract. To the remainder, annex the next figure of the dividend, for the second partial dividend.

Divide as before, and thus continue until all the figures of the dividend have been used.

Write the remainder, if any, over the divisor in the form of a fraction, and annex it to the quotient. The result will be the complete quotient.

**102.** PROOF.—Multiply the divisor by the quotient, and to the product add the remainder. If the sum equals the dividend, the work is probably correct.

#### EXAMPLES.

10:	3. Divide	Divi	ide	
1.	307845 by 26; by 143.	11.	8712460 by 73;	by 817.
2.	248916 by 19; by 249.	12.	1428716 by 84;	by 365.
3.	375428 by 38; by 375.	13.	2893429 by 69;	by 144.
4.	481369 by 48; by 116.	14.	7364128 by 14;	by 128.
5.	423706 by 25; by 208.	15.	2125639 by 70;	by 320.
в.	3064028 by 18; by 429.	16.	3756425 by 64;	by 231.
7.	1289434 by 64; by 567.	17.	4183691 by 36;	by 365.
8.	7090805 by 73; by 432.	18.	3804072 by 96;	by 729.
9.	6321457 by 87; by 618.	19.	1653891 by 33;	by 640.
10.	2304802 by 92; by 729.	20.	2763940 by 95;	by 160.

21. How many days in 8766 hours?

22. In 20000 pens, how many gross? (1 gross = 144.)

23. How many bushels in 21674 pounds of oats, if there are 32 pounds in one bushel?

24. There are 56 pounds in a bushel of rye. How many bushels in 19958 pounds ?

25. There were 31392893 gallons of molasses imported into the United States in 1885. How manys hogsheads of 63 gallons each?

26. How many cords in 47164 cubic feet, if there are 128 cubic feet in one cord ?

27. How many miles in 49164 rods, if there are 320 rods in one mile?

28. The expenditures of the United States for the year 1886 were \$287,034,182. How much was that per day (365 days in the year)?

29. During the year 1882, 788992 immigrants arrived in the United States. What was the average number per day?

30. The population of the 38 States was 49,371,340 in 1880, and there are 325 members in the House of Representatives. What is the average population to each member ?

31. The exports of cotton during the year 1885 were 1,889,514,368 pounds. How many bales averaging 476 pounds each?

32. How many rails 18 feet in length would be required for a railroad 51 miles long? (1 mile = 5280 feet.)

## SHORT METHODS OF DIVISION.

**104.** Leaving out the Products.—In long division the process may be shortened by the following rule :

**105.** RULE.—Subtract the several products from the next number greater ending with the corresponding figure in the dividend, and carry each time the left-hand figure of the minuend to the next product.

NOTE.—If the right-hand figure of any product is the same as the corresponding figure of the dividend, subtract it from itself, and not from the next higher number ending with the same figure; or, write 0 in the remainder, earrying the left-hand figure of the product.

#### Ex. Divide 42343014 by 973.

42343014   973	ANALYSIS.—The first quotient figure is 4, by
3423 43518	which we multiply. 4 times 3 are 12, which sub-
5040	tracted from 14 (the next number greater ending
1///21	with 4) leaves 2. Write 2 in the remainder and
1791	carry 1. 4 times 7 are 28, 1 carried makes 29,
7784	which subtracted from 33 (the next number
000	greater ending with 3) leaves 4. Write 4 in the
	remainder and carry 3 A times 9 are 36 3

carried makes 39, which subtracted from 42 leaves 3. Write 3 in the remainder and carry 4. 4 subtracted from 4 leaves 0. Bring down 3, the next figure of the dividend. So proceed until the division is finished.

NOTE.—Perform any of the examples in Art. 103 by this method.

## 106. To divide by 25.

# **107.** RULE.—Multiply the dividend by 4, and divide the product by 100 by cutting off two figures from the right.

Note.—To divide by 125, multiply by 8 and divide the product by 1000 by cutting off three figures from the right.

Ex. Divide 11175 by 25.

OPERATION.

11175ANALYSIS.—Since 25 is one-fourth of 100, multiplying4by 4 and dividing by 100, is the same as dividing by 25.447.00

#### EXAMPLES.

**108.** 1. Divide the following numbers by 25: 1175, 1650, 1700, 2875, 3825, 4950, 3800, 1725, 1775, 1825, and 2000.

# UNITED 'STATES MONEY.

109. United States Money is the legal currency of the United States. It consists of gold, silver, nickel, and copper coins, treasury and national bank notes, gold and silver certificates.

110. Legal Tender.—The term legal tender is applied to money which may be legally offered in the payment of debts.

111. The unit of value is the gold dollar of 25.8 grains.

#### TABLE.

10	Mills	=	1	Cent	c., ct.	
10	Cents	=	1	Dime	d.	
10	Dimes	=	1	Dollar	\$.	
10	Dollars		1	Eagle	E.	

Notes.—1. In business operations, dollars and cents are principally used. Eagles and dimes are used only as the names of coins.

2. The currency of the Canadian Provinces is nominally the same as that of the United States.

112. The legal coins of the United States are as follows :

Gold. Weight in grains.	Standard dollar,	SILVER. Weight. 412 <sup>1</sup> / <sub>2</sub> grains.
1 dollar piece, $25.8$ $2\frac{1}{2}$ dollar piece, or (64.5)	Half dollar, or 50 cent piece, }	12 <sup>1</sup> / <sub>2</sub> grams, or 192.9 grains.
Quarter-eagle, 5 3 dollar piece, 77.4	Quarter dollar, or 25 cent piece,	} 64 grams, or 96.45 grains.
5 dollar piece, or Half-eagle, } 129.	Dime, or 10 cent piece, }	$2\frac{1}{2}$ grams, or 38.58 grains.
10 dollar piece, or 2 958	Copper	AND NICKEL.
Eagle, $\int 200$ .	5 cent piece,	5 grams, or 77.16 grains.
20 dollar piece, or ) 516	3 cent piece,	30 grains.
Double-eagle,	1 cent piece,	48 grains.

113. The gold and silver coins of the United States contain 9 parts by weight of pure metal and 1 part alloy. The alloy of silver coins is copper; and of gold coins, copper, or copper and silver. (The silver in no case exceeds  $\frac{1}{10}$  of the whole alloy.)

114. Gold Coins are a *legal tender* in all payments at their nominal value when not below the standard weight \* provided by law; and, when reduced in weight, below said standard, are a legal tender at valuation in proportion to their actual weight.

115. Standard Silver Dollars are a *legal tender* at their nominal value for all debts except where otherwise expressly stipulated in the contract.

116. Silver Certificates.—Any holder of *standard silver dollars* may deposit the same with the Treasurer, or any Assistant Treasurer of the United States, in sums not less than \$10, and receive therefor certificates, corresponding with the denominations of United States notes (119). These certificates are receivable for customs, taxes, and all public dues.

117. Subsidiary Coins.—The present silver coins of the United States of smaller denominations than \$1 are a legal tender in all sums not exceeding \$10.

The holder of any of the silver coins of the United States of smaller denominations than \$1 may, on presentation of the same in sums of \$20, or any multiple thereof, at the office of the Treasurer or any Assistant Treasurer of the United States, receive therefor lawful money of the United States.

118. Minor Coins.—The 5 and 3 cent pieces contain  $\frac{3}{4}$  copper and  $\frac{1}{4}$  nickel. The 1 cent piece contains 95 per cent. copper and 5 per cent. tin and zinc. These coins are a legal tender for any amount not exceeding twenty-five cents.

119. United States Notes ("Greenbacks") are a legal tender for all debts except duties on imports and interest on the public debt.

Since Jan. 1, 1879, they have been redeemable in coin at the office of the Assistant Treasurers of the United States in the Cities of New York and San Francisco, in sums of not less than \$50. They represent the values of \$1, \$2, \$5, \$10, \$20, \$50, \$100, \$5000, \$10000, \$10,000. The Act of May 31, 1878, fixed their value at \$346,681,016, and forbade their further contraction.

<sup>\* &</sup>quot;Any gold coin of the United States, if reduced in weight by natural abrasion not more than one-half of one per centum below the standard weight prescribed by law, after a circulation of twenty years, as shown by its date of coinage, and at a ratable proportion for any period less than twenty years, is received at its nominal value by the United States treasury and its offices." The "Coinage Act of 1873" allows a deviation from the standard weight of 1 of a grain, or less, in the manufacture of the dollar piece.

120. National Bank Notes (640) are not a *legal tender*; but, since they are secured by bonds of the United States deposited with the U. S. Treasurer at Washington, and are redeemed in lawful money by the national banks and the Treasurer of the United States, they are usually accepted in the payment of debts in any part of the United States.

They are receivable in all parts of the United States in payment of taxes and other dues to the United States except duties on imports, and for debts owing by the United States to individuals and corporations, within the United States except interest on the public debt.

They represent the values of \$1, \$2, \$5, \$10, \$20, \$50, \$100, \$500, and \$1000. Since Jan. 1, 1879, no notes of the denomination of \$1 and \$2 have been issued to national banks. Nov. 1, 1886, their total circulation was \$301,529,889.

## 121. To write United States money.

122. In writing U. S. money, the decimal notation is used. *Dollars* are written at the left of the decimal point and form the integral part. *Cents* are written as *hundredths* of a dollar, and occupy the first two places at the right of the decimal point. *Mills* are written as *thousandths* of a dollar, and occupy the third decimal place.

Thus, twelve dollars, forty-eight cents, and six mills, is written \$12.486.

When the number of cents is less than ten, a cipher must be written in the first place at the right of the point. Thus, eight dollars and six cents is written, \$8.06.

In the final results of business operations, if the *mills* are more than *five*, they are regarded as an additional cent; if less than *five*, they are rejected.

In checks, notes, drafts, etc., *cents* are usually written as hundredths of a dollar in the form of a *fraction*. Thus, twenty-five cents may be written,  $\$_{100}^{*2}$ .

123. Express the following amounts by figures :

- 1. Eighty-six dollars, nineteen cents, five mills.
- 2. Fourteen dollars, seventy-five cents, three mills.
- 3. Five hundred twenty-six dollars, seventy cents.
- 4. Two thousand dollars, thirty cents, two mills.
- 5. Seven hundred dollars, nine cents.
- 6. Fifty thousand dollars, seven mills.
- 7. Four hundred eight dollars, two cents, five mills.
- 8. Two hundred fifty dollars, sixty cents, three mills.

124. To reduce dollars to cents and mills, or to reduce cents and mills to dollars.

125. Dollars may be reduced to cents by multiplying by 100 or by annexing two ciphers. Dollars may be reduced to mills by multiplying by 1000 or by annexing three ciphers.

Thus, \$64 = 6400 cents, or 64000 mills.

If the amount consists of dollars and cents, reduce to cents by removing the decimal point 2 places to the right; to mills, three places to the right. Thus, \$17.28 = 1728 cents, or 17280 mills; \$34.658 = 34658 mills.

126. Cents may be reduced to dollars by dividing by 100, or by pointing off two decimal places. Mills may be reduced to dollars by dividing by 1000, or by pointing off three decimal places.

Thus, 12345 cents = \$123.45; 37560 mills = \$37.56.

127. Reduce the following to cents:

1.	\$345.	4.	\$17.04.	7.	\$148.19
2.	\$2376.	5.	\$28.37.	8.	\$204.40.
3.	\$2004.	6.	\$49.75.	9.	\$317.04.

128. Change the following to mills :

1.	75 cents.	4.	\$38. `	7.	\$14.172.
2.	19 cents.	5.	\$376.	8.	\$4.866.
3.	47 cents.	6.	\$408.	9.	\$10.012.

**129.** Reduce the following to dollars :

1.	148 cents.	4.	705 cents.	7.	18000 mills.
2.	2300 cents.	5.	4212 cents.	8.	9370 mills.
3.	4617 cents.	6.	13409 cents.	9.	12375 mills.

## 130. To add or subtract in United States money.

131. RULE.—Write dollars under dollars, and cents under cents. Add or subtract as in simple numbers, and place the point in the result directly under the points in the numbers added or subtracted.

NOTE.—In subtraction of U. S. money, if there are cents in the subtrahend and none in the minuend, suppose ciphers to be added to the subtrahend in cents' place.

#### EXAMPLES.

132. 1. Add 5 dollars, 16 cents; 18 dollars, 5 cents; 404 dollars, 75 cents; 25 dollars, 8 cents; 2376 dollars, 40 cents; 8 dollars, 2 cents.

2. Add \$170, \$106.40, \$240, \$200.40, \$70, \$.70, \$234.75.

3. Add \$108.25, \$2345, \$6.04, \$7.10, \$192.43, \$117.05.

4. Add \$.06, \$6, \$108.16, \$500.64, \$564, \$5.64, \$117.10, \$2081.48.

5. From \$124.16 subtract \$109.25.

6. From \$117 subtract \$98.49.

7. From \$575 subtract 575 cents.

8. A merchant makes the following deposits in a bank: \$1875.24, \$416, \$234.70, \$558.96, and \$437.10. He draws the following checks: \$442.37, \$120.92, \$316.75, \$242.71, \$195, \$716.32, \$100.48, and \$76.19. What is the balance of his bank account?

## 133. To multiply United States money.

Ex. Find the cost of 9 desks at \$2.45 each.

OPERATION.

2.45 ANALYSIS.—Disregarding the decimal point, multiply as in 9 ordinary multiplication. 9 times 245 cents is 2205 cents = \$22.05

22.05

**134.** RULE.—Multiply as in simple numbers, and from the right of the product point off as many figures as there are figures to the right of the decimal points in both numbers.

Note.—If, as in Examples 6 and 7, the number expressing cents would make a convenient multiplier, use it as such, considered as an abstract number, and point off the result according to the rule.

#### 135. Multiply

1. 12 dollars and 18 cents by 8.

2. 4 dollars and 25 cents by 12.

- 3. 16 dollars and 9 cents by 17.
- 4. 27 dollars and 8 cents by 25.
- 5. 43 dollars and 50 cents by 76.
- 6. 8 cents by 2345; by 3456.

#### Multiply

- 7. \$.07 by 1239; by 13416.
- 8. \$20.04 by 20; by 108.
- 9. \$176 by 18; by 144.
- 10. \$36.25 by 36; by 117.
- 11. \$48.19 by 48; by 288.
- 12. \$50.08 by 75; by 192.

## 136. To divide in United States money.

Ex. If 9 desks are worth \$22.05, what is one worth ?

OPERATION.	ANALYSIS.—If 9 desks are worth 2205 cents	(\$22.05), 1
9) 22.05	desk is worth one-ninth of 2205 cents or 245 cents.	245 cents
\$2.45	= \$2.45.	

Ex. If 8 chairs are worth \$18, what is one worth?

OPERATION. ANALYSIS .- If the dividend consists of dollars only, and 8) 18.00 does not contain the divisor an exact number of times, reduce it to cents by annexing two ciphers. \$2.25

Ex. At \$6.25 each, how many sheep can be bought for \$50?

OPERATION.	ANALYSIS.—If 1 sheep costs \$6.25, as man	iy
\$6.25) \$50.00 (8	sheep can be bought for \$50 as \$6.25 is contained	ed
Or	times in \$50. $$50 = 5000$ cents. $$6.25 = 625$ cent	s.
01,	$5000 \text{ cents} \div 625 \text{ cents} = 8 \text{ times.}$ Hence the resu	It
625. ) 5000. ( 8	is 8 sheep.	

## 137. Rule.—Divide as in simple numbers, and point off from the right of the quotient as many decimal places as those in the dividend exceed those in the divisor.

NOTE.--If the divisor alone contains cents, make the dividend cents by annexing two ciphers; or, reduce both divisor and dividend to cents by annexing ciphers, omit the decimal points, and divide as in simple numbers.

#### EXAMPLES.

138. 1. If 12 books are sold for \$41.40, what is the price of one book ?

2. How many pounds of tea at 65 cents per pound can be bought for \$9.75 ?

Note.-In the following examples, if the quotient is in U. S. money and the result is not an exact number of dollars, continue the division to cents.

Divide

## Divide

7. \$106.56 by 72; by 576.

8. \$1884 by 75; by 1535.

- 3. \$25.44 by 48; by 106. 9. \$130.38 by \$2.46; by \$1.06. 4. \$476 by 25; by 35. 10. \$149.04 by \$0.36; by \$2.07. 5. \$1728 by 36; by 48. 11. \$156.24 by \$0.72; by \$4.34. 6. \$73.08 by 84; by 87.
  - 12. \$1728 by \$0.75; by \$6.75.
  - 13. \$3456 by \$2.25; by \$13.50.
  - 14. \$7154 by \$1.75; by \$25.55.

## REVIEW EXAMPLES.

139. 1. Find the sum of the following numbers : Twentysix thousand forty-eight; twelve thousand four hundred eighty; one hundred thirty-six thousand; seven hundred ninety thousand forty-three; four million fifty-eight.

2. Subtract eight hundred fourteen thousand nine hundred sixteen from four million nineteen thousand.

3. Multiply five hundred sixty thousand seven hundred eight by eighteen hundred sixty.

4. A quantity of merchandise was bought for \$27618.75, and sold for \$32418.25. What was the gain ?

5. Find the total length of the Brooklyn bridge, its measurements being as follows: Length of river span, 1596 feet; of each (2) land span, 930 feet; of New York approach, 1562 feet; of Brooklyn approach, 971 feet.

6. If I sell goods for \$23876, and gain \$5389, what did the goods cost me?

7. The estimated production of gold and silver of the world for 1884 was as follows: Gold, \$98,990,772; silver, \$116,525,949. For 1885, gold, \$101,562,748; silver, \$124,968,784. What was the total increase?

8. If the quotient is 375 and the divisor 246, what is the dividend?

9. If the product of two numbers is 450072, and one of the numbers is 987, what is the other number ?

10. Divide 76432801 by 783. Prove that your solution is correct.

11. A clerk receiving a salary of \$1256, pays \$468 a year for board, \$180 for clothing, and \$150 for other expenses. What amount has he left?

12. If I take 24889 from the sum of 9872 and 24967, divide the remainder by 50, and multiply the quotient by 18, what is the product?

13. If 160 acres of land cost \$10720, how many acres can be bought for \$8844 ?

14. If 75 head of cattle cost \$2550, what will 59 head cost?

15. Cash on hand at beginning of the day, \$6492.75; cash received, \$11456.75; cash paid out, \$13285.26. Required the cash balance at the end of the day.

16. A merchant sold 426 barrels of flour for \$2556, which was \$639 more than he gave for it. What did it cost him a barrel?

17. Mr. A has three farms, the first of which contains 158 acres, the second 32 acres less than the first, and the third as many as the other two. What is the value per acre, if all are worth \$26128?

18. A merchant bought 387 yards of cloth at 79 cts. per yard; he sold 298 yards at \$1.16 per yard, and the remainder at 97 cts. per yard; how much did he gain?

19. The United States nickel and copper coinage for the year 1886 was 5,519 five-cent pieces, 4,519 three-cent pieces, and 1,696,613 one-cent pieces. Find total value of minor coinage.

20. The silver coinage for 1886 was as follows: 29,838,905 dollars, 6,105 half-dollars, 14,505 quarter-dollars, 1,767,642 dimes. What was the total value of the silver coinage?

21. The gold coinage for 1886 was as follows : 243,584 doubleeagles, 1,042,847 eagles, 3,751,629 half-eagles, 101 three-dollar pieces, 4,086 quarter-eagles, 8,567 one-dollar pieces. What was the value of the gold coinage ?

22. There are four bidders to supply the government with 800 tons Lehigh, 500 tons Cumberland, and 700 tons Baltimore coal. A offers Lehigh at \$6.29, Cumberland at \$4.38, and Baltimore at \$7.23. B offers Lehigh at \$6.80, Cumberland at \$4.12, and Baltimore at \$7.24. C offers Lehigh at \$6.40, Cumberland at \$4.45, and Baltimore at \$7.18. D offers Lehigh at \$6.17, Cumberland at \$4.19, Baltimore at \$7.20. Who is the lowest bidder for the whole amount, and how much does each bid amount to ?

23. A drover bought a number of cattle for \$12204, and sold the same for \$13560, by which he gained \$4 per head. How many cattle were purchased ?

24. A farmer raised in one year 512 bushels of wheat, the next year twice as much as he raised the first year, and the third year four times as much as he did the second year. What was the value of the three crops at \$1.65 per bushel?

25. Bought 75 tons of hay at \$16 per ton; gave in payment 56 sheep at \$3.75 each, and the remainder I paid in butter at 33 cts. per pound. How many pounds of butter were required?

26. Bought 225 acres of land for \$12,600, and sold 116 acres at \$65 per acre, and the remainder at cost; how much did I gain?

27. A sold to B 175 acres of land at \$135 an acre, and by so doing gained \$1925; B sold the land at a loss of \$1750. What did A pay per acre, and what was B's selling-price per acre?

28. A merchant sold 800 barrels of flour for \$5867, 144 barrels of which he sold at \$7 per barrel, and 225 barrels at \$6.75. At how much per barrel did he sell the remainder?

29. According to the following table, what was the average immigration per year? What per month?

Years.	Number.	Years.	Number.	Years.	Number.
1875	227,498	1879	$177,826 \\ 457,257 \\ 669,431 \\ 788,992$	1883	603, 322
1876	169,986	1880		1884	518, 592
1877	141,857	1881		1885	395, 346
1878	138,469	1882		1886	334, 203

# PROPERTIES OF NUMBERS.

140. A Number is a unit, or a collection of units; as one, four, three feet, five dollars.

**141.** All numbers are either *integral* or *fractional*, *abstract* or *concrete*.

142. An Integral Number, or Integer is a number which expresses whole things; as *two*, *four* gallons, *seven* dollars.

143. A Fractional Number, or Fraction is a number which expresses one or more equal parts of a unit; as one-half, three-fourths.

144. An Abstract Number is a number which does not refer to any particular object; as one, six, ten.

145. A Concrete Number is a number applied to an object, or quantity; as *three* apples, *five* pounds, *ten* dollars.

**146.** Integral numbers are either *odd* or *even*, *prime* or *composite*.

**147.** An Odd Number is a number whose unit figure is 1, 3, 5, 7, or 9; as 7, 21, 39.

**149.** A **Prime Number** is a number which can be exactly divided only by itself and unity; as 1, 7, 13, 29.

150. Numbers are prime to each other when no integral number greater than 1 will divide each without a remainder.

Numbers that are prime to each other are not necessarily prime numbers. Thus, 25 and 28 are prime to each other, but they are not prime numbers.

**151.** A Composite Number is a number which can be exactly divided by other integers besides itself and unity.

Thus 28, the product of 4 and 7, is a composite number. It is exactly divisible by 4 and 7.

## DIVISIBILITY OF NUMBERS.

152. An Exact Divisor of a number is any number that will divide it without a remainder.

Thus 2, 3, 4, 6, 8, and 12 are exact divisors of 24.

153. A number is said to be *divisible* by another when the latter will divide the former without a remainder. Any number is divisible

1. By 2, if it is an even number; as 6, 28, and 32.

2. By 3, if the sum of its digits is divisible by 3; as 849 (8+4+9=21, 21) is divisible by 3), 7323, and 47892.

3. By 4, if the two right-hand figures are ciphers, or express a number divisible by 4; as 1100, 216, and 7328.

4. By 5, if the right-hand figure is 0 or 5; as 40 and 135.

5. By 6, if it is an even number and the sum of its digits is divisible by 3; as 216, 840, and 732.

6. By 8, if the three right-hand figures are ciphers, or express a number divisible by 8; as 3000 and 7168.

7. By 9, if the sum of its digits is divisible by 9; as 216, 783, and 12348.

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## PRIME FACTORS.

154. The Factors of a number are those numbers which when multiplied together will produce the number.

Thus 4 and 7; 2 and 14; 2, 2, and 7 are factors of 28. The number itself and unity are not regarded as factors.

The factors of a number are also the exact divisors of it.

155. A Prime Factor is a prime number used as a factor.

Thus, 2, 2, and 7 are the prime factors of 28. 4 is a factor of 28, but not a *prime* factor.

# 156. To find all the prime factors of a composite number.

Ex. What are the prime factors of 6930.

OPERATION.	ANALYSIS.—Any prime number that is an exact divi-
2) 6930	sor of the given number is a prime factor of it. Divide
3) 3465	the given number by 2 (153, 1), the least prime divisor of it obtaining the quotient 3465 Next divide this quo-
3) 1155	tient successively by 3 $(153, 2)$ , 3, 5 $(153, 4)$ , and 7.
5 ) 385	The last quotient 11 is a prime number and therefore a prime factor. The several divisors 2, 3, 3, 5, 7, and the
7)77	last quotient 11 are the prime factors required.
11	$2 \times 3 \times 3 \times 5 \times 7 \times 11 = 6930.$

157. RULE.—Divide by the least prime number which will divide the given number without a remainder. In like manner divide the resulting quotient, and continue the division until the quotient is a prime number. The several divisors and the last quotient are the prime factors.

#### EXAMPLES.

158. Resolve the following numbers into their prime factors :

1.	3465.	7.	6552.	13.	8192.	19.	6660.
2.	3003.	8.	7826.	14.	6561.	20.	2448.
3.	4158.	9.	6006.	15.	3125.	21.	8525.
4.	3150.	10.	5368.	16.	1800.	22.	9936.
5.	3675.	11.	3825.	17.	1935.	23.	9576.
6.	2310.	12.	5324.	18.	2475.	24.	5075.

## COMMON MULTIPLES.\*

159. A Multiple of a number is a number that is exactly divisible by it; or, it is any product of which the given number is a factor.

Thus, 12 is a multiple of 6; 15 of 5; etc.

160. A Common Multiple of two or more numbers is a number that is exactly divisible by each of them.

Thus, 12, 24, 36, and 48 are multiples of 4 and 6.

**161.** The Least Common Multiple of two or more numbers is the *least* number that is exactly divisible by each of them.

Thus, 12 is the least common multiple of 4 and 6.

**162.** PRINCIPLES.—1. A multiple of a number contains all the prime factors of that number.

2. A common multiple of two or more numbers contains all the prime factors of each of those numbers.

3. The least common multiple of two or more numbers contains all the prime factors of each of the numbers, and no other factors.

163. To find the least common multiple of two or more numbers.

Ex. What is the least common multiple of 12, 18, 20, and 40?

First operation.  $12 = 2 \times 2 \times 3$   $18 = 2 \times 3 \times 3$   $40 = 2 \times 2 \times 2 \times 5$   $2 \times 2 \times 2 \times 3 \times 3 \times 5 = 360$  ANALYSIS.—Since 40, a multiple of 20, contains all the prime factors of 20, the number 20 may be omitted in the operation. Resolve the numbers into their prime factors. The least common multiple must contain 2 as a factor 3 times in order to be divisible

by 40; it must contain 3 as a factor twice in order to be divisible by 18; and it must contain 5 as a factor, in order to be divisible by 40. 360, the product of the factors, 2, 2, 2, 3, 3, and 5, is the least common multiple of the given numbers, since it contains the different factors the greatest number of times that they occur in the given numbers, and no other factors (*Prin.* 3). 2

SE	COND C	PERATI	ON.
2)	12,	18,	40
2	) 6,	9,	20
3	) 3,	9,	10
	1,	3,	10
$\times 2 \times$	$(3 \times 3)$	$3 \times 10$	= 36

ANALYSIS.—The factors of the required multiple may be found by the following process. Divide the given numbers by any prime number that will divide two or more of them, writing the quotients and the undivided numbers beneath. Treat the resulting numbers in like manner, and continue the process until no two of the numbers have a com-

mon factor or divisor. The product of the several divisors and the remaining quotients and undivided numbers will be the least common multiple.

**164.** RULE.—Resolve the given numbers into their prime factors. The product of the different prime factors, taking each factor the greatest number of times it appears in any of the numbers, will be the least common multiple. Or,

Divide the given numbers by any prime number (see Note 2) that will exactly divide two or more of them, writing the quotients and undivided numbers beneath. Repeat the operation with the resulting numbers until there is no exact divisor of any two of them. The product of the several divisors and the last quotients and undivided numbers will be the least common multiple.

Notes.—1. In the operation, reject such of the smaller numbers as are divisors of the larger; also reject such of the quotients and undivided numbers as are divisors of the others.

2. Divide by composite numbers when they are exact divisors of all the numbers.

#### EXAMPLES.

165. Find the least common multiple of the following numbers:

1.	6, 10, 15, and 30.	12.	24, 36, and 40.
2.	16, 24, and 48.	13.	32, 48, and 72.
3.	30, 40, and 60.	14.	16, 22, 24, and 30.
4.	2, 4, 8, and 16.	15.	18, 28, 30, and 36.
5.	14, 21, and 28.	16.	12, 16, 20, and 24.
6.	5, 8, 15, and 18.	17.	33, 44, 55, and 66.
7.	6, 9, 21, and 24.	18.	27, 36, 42, and 48.
8.	12, 20, and 30.	19.	36, 45, 60, and 72.
9.	6, 10, 30, and 40.	20.	28, 35, 42, and 56.
0.	32, 48, and 60.	21.	45, 55, 60, and 75.
1.	24, 32, and 40.	22.	60, 72, 84, and 90.

## CANCELLATION.

**166.** Cancellation is a method of shortening an operation by rejecting equal factors from both dividend and divisor.

**167.** PRINCIPLE.—Dividing both dividend and divisor by the same number does not affect the value of the quotient.

Ex. Divide  $84 \times 36$  by  $27 \times 14$ .



ANALYSIS.—Indicate the operations to be performed as in the margin. Since 36 and 27 contain the common factor 9, cancel or reject it from both, retaining the factors 4 and 3 respectively. 14 and 84 contain the common factor 14; therefore reject it, retaining

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the factor 6 in the dividend. [Since cancellation is a process of division, the rejecting of 14 does not destroy it, but divides it, leaving 1 as a quotient. It is unnecessary to write 1 as a quotient, except when there are no other factors in the dividend.] 3 is a common factor of 6 and 3; therefore reject it from both, retaining the factor 2 in the dividend. The product of the remaining factors, 2 and 4, is the required quotient.

168. RULE. — Write the numbers denoting multiplication above a horizontal line, and the numbers denoting division below. The numbers above the line will form a dividend, and the numbers below, a divisor. Cancel the factors common to both dividend and divisor. The product of the remaining factors of the dividend divided by the product of the remaining factors of the divisor will be the required quotient.

#### EXAMPLES.

169. Find the value of the following expressions :

1.	$\frac{27 \times 48 \times 60}{54 \times 36 \times 40}$	4.	$\frac{1760\times175\times6}{36\times100\times10}.$	7.	$\frac{360 \times 28 \times 27 \times 5}{25 \times 42 \times 18 \times 12}$
2.	$\frac{1500\times144\times5}{365\times100}.$	5.	$\frac{40\times36\times42\times18}{9\times35\times30\times8}$	8.	$\frac{17\times36\times25\times144}{48\times60\times108\times51}.$
3.	$\frac{1760\times6\times145}{100\times365}.$	6.	$\frac{24 \times 30 \times 54 \times 35}{14 \times 15 \times 21 \times 64}.$	9.	$\frac{144\times 625\times 37\times 12}{288\times 375\times 185}$

10. Multiply 72 by  $3 \times 18$ , divide the product by 8 times 9, multiply the quotient by  $7 \times 20$ , divide the product by 360, multiply the quotient by 6 times 8.

11. If 42 tons of coal cost \$147, what will 16 tons cost?

12. A man gave 9 pounds of butter at 17 cents a pound for 3 gallons of molasses; how much was the molasses worth a gallon?

13. If 20 pounds of beef cost 250 cents, what cost 75 pounds?

14. How many potatoes at 65 cents per bushel will pay for 13 weeks' board at \$7.50 per week ?

15. A merchant bought 375 barrels of flour at \$5.50 per barrel, and paid in cloth at \$2.75 per yard; how many yards did it require?

16. How many pounds of coffee at 27 cents per pound should be given for 57 bushels of corn at 63 cents per bushel ?

17. Sold 28 bushels of apples for \$21; what should I receive for 42 bushels?

18. How many cows worth \$35 each must be given in exchange for 84 tons of hay at \$15 per ton ?

19. How many bushels of corn at 52 cents a bushel must be exchanged for 324 bushels of oats at 39 cents per bushel?

20. If 430 bushels of wheat are obtained from sowing 7 bushels, how much would be obtained from sowing 21 bushels?

21. What should be paid for the transportation of 3600 pounds of cheese at the rate of 47 cents per 100 pounds?

22. What must be paid for transporting 31600 pounds of iron at \$5 per ton of 2000 pounds ?

23. What will 7840 pounds of coal cost, at \$6 per ton of 2240 pounds?

24. If 3 men eat 7 pounds of meat in one week, how much would 6 men eat in 4 weeks?

25. How many canisters, each holding 40 ounces, can be filled from 3 chests of tea, each containing 55 pounds of 16 ounces?

26. How many times can 16 bottles, each holding 3 pints, be filled from 6 demijohns, each containing 10 gallons of 8 pints each?

27. A man exchanged 275 barrels of potatoes, each containing 3 bushels, at 54 cents per bushel, for a certain number of pieces of muslin each containing 45 yards, at 11 cents per yard. How many yards did he receive?

28. If a person travel 24 hours each day at the rate of 45 miles an hour, how many days would it require to pass around the globe, a distance of 25000 miles?

# FRACTIONS.

**170.** A Fraction is one or more of the equal parts of a unit; as one-half  $(\frac{1}{2})$ , two-thirds  $(\frac{2}{3})$ , one-fourth  $(\frac{1}{4})$ , seven-eights  $(\frac{7}{3})$ .

If a unit be divided into four equal parts, each part is called a fourth. If one of these parts be taken, the expression will be one-fourth  $(\frac{1}{4})$ ; if three parts, three-fourths  $(\frac{3}{4})$ , etc.

**171.** The greater the number of equal parts into which a unit is divided, the less will be each part; the less the number of parts, the greater will be each part.

One-half  $(\frac{1}{3})$  is greater than one-third  $(\frac{1}{3})$ ; one-fourth  $(\frac{1}{4})$  is less than one-third  $(\frac{1}{3})$ .

172. A fraction is usually expressed by two numbers, one written above the other, with a line between. Fractions written in this form are called Common Fractions.

173. The number below the line is called the **Denominator**, because while indicating the number of equal parts into which the unit is divided, it *denominates* or names those parts.

174. The number above the line is called the Numerator, because it shows how many of the parts are taken to form the fraction.

175. The numerator and denominator, taken together, are called the **Terms** of the fraction.

In the fraction  $\frac{3}{4}$ , 3 and 4 are the terms ; 4 is the denominator, and shows that the unit is divided into four equal parts, called fourths ; 3 is the numerator, and shows that three of these parts are taken to constitute the fraction.

176. A fraction is an expression of unperformed division. The numerator is the dividend, the denominator is the divisor, and the value of the fraction is the quotient.

177. A Simple Fraction is a single fraction, both of whose terms are integers.

178. Simple fractions are proper or improper.

**179.** A Proper Fraction is one that is less than a unit; the numerator being less than the denominator. Thus,  $\frac{1}{2}$ ,  $\frac{3}{4}$ , and  $\frac{7}{8}$  are proper fractions.

180. An Improper Fraction is one that is equal to, or greater than a unit; hence the numerator must be equal to, or greater than the denominator. Thus,  $\frac{3}{2}$ ,  $\frac{5}{4}$ ,  $\frac{3}{3}$ , and  $\frac{1}{8}$  are improper fractions.

181. A Mixed Number is an integer and a fraction united; as  $2\frac{1}{2}$ ,  $4\frac{3}{4}$ ,  $18\frac{7}{8}$ .

**182.** A Complex Fraction is one whose numerator is a fraction or a mixed number; as  $\frac{3}{4}$ ,  $\frac{105_3^2}{12}$ ,  $\frac{75_4^3}{16}$ ,  $\frac{3_2^2}{5}$ ,  $\frac{12_2^1}{15}$ ,  $\frac{16_3^2}{100}$ .

The expression  $\frac{3\frac{3}{4}}{5\frac{1}{2}}$  indicates division, and is not properly a fraction. A unit cannot be divided into  $5\frac{1}{4}$  equal parts.

**183.** PRINCIPLES.—1. Multiplying the numerator or dividing the denominator by a number multiplies the fraction by that number.

2. Dividing the numerator or multiplying the denominator by a number divides the fraction by that number.

3. Multiplying or dividing both numerator and denominator by the same number does not change the value of the fraction.

#### EXERCISES.

184. 1. Read the following fractions, and copy separately: 1, the simple fractions; 2, the proper fractions; 3, the improper fractions; 4, the mixed numbers; 5, the complex fractions:

2. Write the following fractions: three fourths; seven eighths; nineteen sixteenths; five, and one half; one hundred three thirty-seconds; one hundred, and three thirty-seconds; forty-eight, and five twelfths; eleven tenths; nine forty-fifths.

3. Write the following fractions: eight ninths; thirteen, and two-thirds; sixteen twenty-fourths; ten tenths; fourteen, and forty-six hundredths; sixty-five forty-eighths; nineteen one hundred nineteenths; thirty-six four hundred thirty-seconds.

## REDUCTION OF FRACTIONS.

185. Reduction of Fractions is the changing their form without changing their value.

186. A fraction is reduced to *lower terms* when the numerator and denominator are expressed in smaller numbers.

187. A fraction is in its *lowest terms* when its numerator and denominator have no common divisor.

**188.** A fraction is reduced to *higher terms* when the numerator and denominator are expressed in larger numbers.

## 189. To reduce a fraction to its lowest terms.

Ex. Reduce  $\frac{84}{126}$  to its lowest terms.

OPERATION.  $\frac{84}{126} = \frac{14}{21} = \frac{2}{3}$   $\frac{84}{126}$ , by the common divisor, 6, the result is  $\frac{14}{21}$ ; dividing both terms of  $\frac{14}{21}$  by the common divisor, 7, the result is  $\frac{2}{3}$ . Since 2 and 3 have no common divisor, the fraction is reduced to its lowest terms (187).

The value of the fraction has not been changed, because both terms have been divided by the same number (183, 3).

**190.** RULE.—Divide the terms of the fraction by any number that will divide both without a remainder, and continue the operation with the resulting fractions until they have no common divisor.

#### EXAMPLES.

191. Reduce to their lowest terms,

1.	32.48.	9.	<u>96</u> 108.	17.	<u>648</u> 1024	25.	288
2.	45.	10.	$\frac{132}{168}$ .	18.	325	26.	1056
3.	48.	11.	$\frac{105}{120}$ .	19.	375	27.	1136
4.	<u>63</u> 81.	12.	144.	20.	<u>625</u> 2000	28.	$\frac{1278}{3474}$
5.	72	13.	$\frac{1296}{1416}$ .	21.	86.946.	29.	2688
6.	85	14.	275	22.	125	30.	1024
7.	90	15.	528	23.	125	31.	1991.
8.	18 144.	16.	512.	24.	6125	32.	1440

## 192. To reduce a fraction to higher terms.

Ex. Reduce <sup>3</sup>/<sub>4</sub> to a fraction whose denominator is 32.

OPERATION.  $\frac{3}{4} = \frac{24}{39}$ 

ANALYSIS .- The fraction <sup>2</sup>/<sub>4</sub> is reduced to thirty- $32 \div 4 = 8$  seconds, without changing its value, by multiplying the terms by the number that will cause its denominator 4 to become 32 (183, 3). By dividing the required

denominator 32 by the given denominator 4, this number is found to be 8. Multiplying both terms of  $\frac{3}{4}$  by 8, the result is  $\frac{24}{32}$ . In practice, say or think, 4 into 32 8 times. 8 times 3 are 24.

193. RULE.—Divide the required denominator by the denominator of the given fraction, and multiply the numerator of the given fraction by the quotient.

#### EXAMPLES.

194. -1. Reduce <sup>3</sup> to 48ths.

2. Change  $\frac{7}{12}$  to an equivalent fraction having 60 for its denominator.

3. Reduce 3, 3, 5, 5 each to 24ths.

4. Reduce 1, 5, 7, 3 each to 36ths.

5. Reduce  $\frac{2}{3}$ ,  $\frac{5}{6}$ ,  $\frac{9}{16}$  each to 48ths.

6. Reduce \$, \$, \$\$ each to 105ths.

7. Reduce 41, 5, 1 each to 56ths.

8. Reduce 16, 11, 19 each to 96ths.

9. Reduce  $\frac{3}{8}$ ,  $\frac{3}{10}$  each to 360ths.

10. Reduce 17, 5, 11 each to 72ds.

11. Reduce 4, 29, 17 each to 108ths.

12. Reduce 5, 3, 11 each to 360ths.

## 195. To reduce two or more fractions to equivalent fractions having their least common denominator.

196. A Common Denominator of two or more fractions is a denominator to which they can all be reduced, and is the common multiple of their denominators.

197. The Least Common Denominator of two or more fractions is the least denominator to which they can be reduced, and is the least common multiple of their denominators.

Ex. Reduce  $\frac{2}{3}$ ,  $\frac{3}{4}$ ,  $\frac{5}{6}$ ,  $\frac{9}{10}$  to equivalent fractions having their least common denominator.

OPERATION.									
***	_	<u>40</u> 60	2	)	\$,	4,	6,	10	
34 :		45				2	3	5	
5 6 9 10			2	×	$2 \times$	(3)	× 5	=	60

ANALYSIS.—The least common multiple of the denominators is found to be 60 (163), which we take as the least common denominator. By Art. 193,  $\frac{2}{3}$  is reduced to  $\frac{4}{3}$ . We proceed in the same manner with each of the other fractions.

The value of each fraction remains unchanged, since both terms have been multiplied by the same number. In many cases, the least common denominator can be readily found by inspection.

**198.** RULE.—Find the least common multiple of the given denominators for the least common denominator, and reduce the given fractions to this denominator.

#### EXAMPLES.

**199.** Reduce the following fractions to equivalent fractions having their least common denominator :

1.	$\frac{2}{5}, \frac{7}{10}, \frac{4}{15}.$	5.	$\frac{20}{21}, \frac{25}{28}, \frac{11}{14}.$	9.	$\frac{17}{12}, \frac{13}{8}, \frac{10}{9}, \frac{17}{36}.$
2.	$\frac{3}{3}, \frac{1}{2}, \frac{5}{7}, \frac{5}{6}.$	в.	$\frac{3}{5}, \frac{7}{16}, \frac{13}{20}, \frac{9}{10}.$	10.	$\frac{13}{20}, \frac{16}{25}, \frac{3}{10}, \frac{3}{4}.$
3.	$\frac{11}{12}, \frac{8}{15}, \frac{27}{10}, \frac{9}{20}.$	7.	4, 13, 4.	11.	$\frac{5}{9}, \frac{13}{16}, \frac{17}{48}, \frac{47}{72}, \frac{11}{18}.$
4.	$\frac{7}{8}, \frac{13}{6}, \frac{9}{16}, \frac{11}{12}.$	8.	$\frac{23}{24}, \frac{8}{9}, \frac{17}{18}, \frac{1}{6}, \frac{3}{4}.$	12.	4, 22, 49, 16, 1.

200. To reduce an integer or a mixed number to an improper fraction.

Ex. In 18 units, how many fourths?

ANALYSIS.—In 1 there are 4 fourths (4), and in 18, eighteen times 4. fourths, or 72 fourths  $\binom{72}{4}$ . Hence,  $18 = \frac{72}{4}$ .

Ex. Reduce 167 to an improper fraction.

OPERATION. $16\frac{1}{8}$ ANALYSIS.—In 1 there are 8 eighths ( $\frac{8}{8}$ ), and in 16, $\frac{8}{128}$  eighths.sixteen times 8 eighths, or 128 eighths ( $\frac{128}{8}$ ). $\frac{7}{128}$  eighths.eighths and 7 eighths are 135 eighths. $16\frac{7}{8} = \frac{18}{8}$ .135 eighths.

**201.** RULE.—Multiply the integer by the required denominator, and to the product add the numerator of the fraction, and under the result write the denominator.

Note.—When the numerator of the fraction is a small number, add it mentally to the product of the integer and the denominator.

#### EXAMPLES.

202. 1. In 27, how many ninths?

2. Reduce  $46\frac{1}{2}$  to halves.

3. How many eighths of a peck in 377 pecks?

Reduce the following to improper fractions :

4.	$37\frac{3}{4}$ ; $19\frac{7}{8}$ ; $208\frac{9}{16}$ .	9.	$81\frac{2}{3}$ ; $196\frac{1}{2}$ ; $375\frac{3}{4}$ .
5.	$56_{\frac{2}{3}}; 49_{\frac{5}{6}}; 182_{\frac{5}{4}}.$	10.	$116\frac{1}{26}$ ; $456\frac{4}{11}$ ; $87\frac{13}{38}$ .
6.	$375\frac{1}{2}$ ; $94\frac{9}{10}$ ; $46\frac{5}{8}$ .	11.	$24\frac{3}{14}$ ; $179\frac{13}{16}$ ; $1767\frac{3}{4}$ .
7.	$44\frac{3}{4}$ ; $37\frac{5}{12}$ ; $19\frac{13}{16}$ .	12.	$87\frac{3}{8}$ ; $490\frac{5}{12}$ ; $168\frac{11}{18}$ .
8.	$12\frac{1}{2}$ ; $48\frac{7}{20}$ ; $45\frac{5}{12}$ .	13.	$384\frac{5}{8}$ ; $161\frac{3}{4}$ ; $175\frac{25}{3\frac{5}{2}}$ .

203. To reduce an improper fraction to an integer or a mixed number.

Ex. Reduce  $\frac{2}{4}$  to a mixed number.

ANALYSIS.— $1 = \frac{4}{4}$ ; hence in  $\frac{27}{4}$ , there are as many units as 4 fourths are contained times in 27 fourths, or  $6\frac{3}{4}$ .

**204.** RULE.—Divide the numerator by the denominator.

#### EXAMPLES.

205. 1. Change 317 to a mixed number.

2. Reduce  $\frac{64}{4}$  of a dollar to dollars.

Reduce to integers or mixed numbers :

3.	375; 416.	8.	3861; 1248.	13.	$\frac{387}{16};$	1416.
4.	138; 376.	9.	445; 785.	14.	517;	2387.
5.	518; 444.	10.	387; 441.	15.	$\frac{373}{45};$	449.
6.	303; 427.	11.	511; 937.	16.	$\frac{714}{32};$	$\frac{1000}{16}$ .
7.	542; 873.	12.	411; 1385.	17.	<u>875</u> ;	1276

## ADDITION OF FRACTIONS.

**206.** Addition of Fractions is the process of finding the sum of two or more fractions.

**207.** PRINCIPLE.—In order that fractions may be added, they must have like denominators and be parts of like units.

Ex. What is the sum of  $\frac{5}{12}$ ,  $\frac{9}{12}$ , and  $\frac{1}{12}$ ?

OPERATION.  $\frac{5}{12} + \frac{9}{12} + \frac{1}{12} = \frac{15}{12} = \frac{5}{4} = 1\frac{1}{4}$  ANALYSIS.—As these fractions have a common denominator, we add their numerators, and write their sum, 15, over the common denominator, 12.  $\frac{15}{12} = 1\frac{1}{4}$ , the

and write their sum, 15, over the common denominator, 12.  $\frac{16}{12} = 1\frac{1}{4}$ , the required result.

Ex. Add 3, 3, and 5.

OPERATION.

 $\frac{2}{3} + \frac{3}{4} + \frac{5}{6} = \frac{8 + 9 + 10}{12} = \frac{27}{12} = 2\frac{3}{12} = 2\frac$ 

ANALYSIS.—Reduce the given fractions to equivalent fractions having the least common denominator, 12 (198). Then proceed as in previous example.

Ex. Find the sum of 294, 383, 175, and 424.

OP	ERATION.	
	24ths.	
291	4	
$38\frac{3}{4}$	18	ANALYSIS.—The sum of the fractions is $15 - 17$ which added to the sum of the inte
175	15	$\frac{1}{24} - \frac{1}{8}$ , which added to the sum of the inte-
4213	8	gers, gives 1212, the required result.
1273	$\frac{45}{24} = 1\frac{7}{8}$	

Ex. How many yards in 12 pieces of prints containing  $46^1$ ,  $48^2$ ,  $51^2$ ,  $49^3$ ,  $44^1$ ,  $48^2$ ,  $47^1$ , 49,  $47^3$ ,  $50^3$ ,  $48^1$ ,  $48^2$  yards respectively?

OPER/	TION.	
<b>46</b> <sup>1</sup>	471	and the second
48 <sup>2</sup>	49	ANALYSIS.—The small figures represent
$51^{2}$	473	fourths (quarters). The sum of the fourths is
<b>4</b> 9 <sup>3</sup>	$50^{3}$	$\frac{21}{4} = 5\frac{1}{4}$ , which added to the sum of the in-
<b>44</b> <sup>1</sup>	48 <sup>1</sup>	tegers gives 580 <sup>‡</sup> , the total number of yards.
48 <sup>2</sup>	48 <sup>2</sup> 580 <sup>1</sup> .	
	and the second s	



**208.** RULE.—Reduce the given fractions to equivalent fractions having the least common denominator. Write the sum of the numerators over the common denominator, and reduce the resulting fraction to its simplest form.

When there are mixed numbers or integers, add the integers and fractions separately, and then add the results.

Note.—Before adding, reduce all fractions to their lowest terms, and all improper fractions to mixed numbers.

#### EXAMPLES.

209. Add the following :

1.	$\frac{5}{18}, \frac{11}{18}, \frac{7}{18}, \text{ and } \frac{15}{18}.$	5.	1277, 23, 23, 1753, and 5.
2.	3, 3, 5, and 3.	6.	141,9, 1973, and 4372.
3.	121, 73, 1616, and 383.	7.	75%, §, 1028%, and 18.
4.	484, 467, 313, and 171.	8.	7, 1191, 2403, and 173
0	101 102 102 10 182	1.09	

9. 46<sup>1</sup>, 48<sup>3</sup>, 40<sup>2</sup>, 49, 47<sup>3</sup>, and 46<sup>2</sup>. (See Analysis opposite.) 10. 40<sup>3</sup>, 41<sup>1</sup>, 48<sup>2</sup>, 44<sup>1</sup>, 49<sup>3</sup>, 48<sup>2</sup>, 49<sup>3</sup>, 49<sup>1</sup>, 47<sup>3</sup>, 48<sup>3</sup>, 48<sup>3</sup>, and 49<sup>1</sup>.

- 11.  $18\frac{8}{9}$ ,  $27\frac{1}{4}$ ,  $42\frac{2}{3}$ ,  $51\frac{5}{8}$ , and  $14\frac{1}{6}$ .
- 12.  $146\frac{3}{4}$ ,  $1\frac{4}{4}$ ,  $53\frac{5}{14}$ , and  $68\frac{1}{2}$ .

13.  $1172\frac{5}{4}$ ,  $19\frac{2}{3}$ ,  $440\frac{1}{4}$ ,  $6\frac{3}{4}$ , and  $10\frac{1}{12}$ .

14.  $\frac{7}{16}$ ,  $106\frac{5}{12}$ ,  $37\frac{8}{4}$ ,  $7\frac{1}{6}$ , and  $176\frac{13}{18}$ .

15. 175, 116-7, 1433, and 274.

16. 20%, 164%, 11, and 43%.

17. 441, 161, 291, 131, and 4423.

18. 311, 483, 621, 193, 272, 481, and 373.

19. 61<sup>3</sup>, 48<sup>1</sup>, 47<sup>3</sup>, 48, 48<sup>2</sup>, 49<sup>1</sup>, and 45<sup>3</sup>.

20.  $19\frac{3}{8}$ ,  $444\frac{5}{16}$ ,  $737\frac{1}{4}$ , and  $385\frac{1}{2}$ .

21. A farmer sold  $317\frac{28}{60}$  bushels wheat,  $176\frac{18}{46}$  bushels timothy seed,  $202\frac{31}{46}$  bushels buckwheat,  $526\frac{42}{66}$  bushels corn,  $175\frac{34}{52}$  bushels oats, and  $276\frac{45}{60}$  bushels clover seed. How many bushels did he sell altogether ? (See Note, Art. **208**.)

22. A jeweler has nine diamonds whose respective weights expressed in carats are  $\frac{3}{64}$ ,  $\frac{5}{8}$ ,  $\frac{1}{16}$ ,  $\frac{1}{2}$ ,  $\frac{1}{32}$ ,  $\frac{3}{4}$ ,  $\frac{7}{8}$ ,  $\frac{47}{64}$ ,  $\frac{1}{32}$ . Find their total weight.

23. How many inches of moulding would be required for three frames whose dimensions are as follows: first,  $11\frac{3}{8}$  inches wide,  $17\frac{1}{2}$  inches long; second,  $18\frac{1}{4}$  inches wide,  $26\frac{5}{8}$  inches long; third,  $17\frac{1}{4}$  inches wide,  $24\frac{3}{4}$  inches long?

## SUBTRACTION OF FRACTIONS.

**210.** Subtraction of Fractions is the process of finding the difference between two fractions.

**211.** PRINCIPLE.—In order that fractions may be subtracted, they must have like denominators and be parts of like units.

Ex. From & take §.

OPERATION.	ANALYSIS.—As these fractions have a common
$\frac{8}{9} - \frac{5}{9} = \frac{3}{9} = \frac{1}{3}$	denominator, we take the difference between the
	numerators, and place it over the common de-
nominator. $\frac{1}{2} = \frac{1}{2}$ is the	result required.

Ex. What is the difference between  $\frac{3}{4}$  and  $\frac{2}{3}$ ?

			OPE	RATION.			
34	—	colas	=	$\frac{9-8}{12}$	3 ==	$\frac{1}{12}$	

ANALYSIS.—Reduce the given fractions to equivalent fractions having the least common denominator (197). Then proceed as in the previous example.

Ex. From 1763 subtract 893.

OPERATION.

$176\frac{3}{8}$	3.	ANALYSIS.—§ from § we cannot take ; we therefore
893	6.8	take $1 = \frac{8}{8}$ from 176, leaving 175. $\frac{8}{8} + \frac{8}{8} = \frac{11}{8}$ . $\frac{11}{8} - \frac{6}{8}$
865		$=\frac{5}{8}$ , $175 - 89 = 86$ , $86 + \frac{5}{8} = 86\frac{5}{8}$ .

**212.** RULE.—Reduce the given fractions to equivalent fractions having the least common denominator. Write the difference between the numerators over the common denominator, and reduce the resulting fraction to its simplest form.

When there are mixed numbers, subtract the integers and fractions separately, and add the results.

#### EXAMPLES.

213. Find the difference between

1.	३ and ई.	4.	21 and 116.	7.	11 and §.
2.	$\frac{1}{8}$ and $\frac{5}{12}$ .	5.	7 and 8.	8.	§ and 4.
3.	3 and 11.	6.	4 and 3.	9.	1 and 11.

Find the difference between

10.	171 and 9	<u>4</u> . 17	$116\frac{5}{6}$	and $48\frac{2}{3}$ .	24.	7641 and	375-3.
11.	$175\frac{1}{4}$ and	86 <u>1</u> . 18	$3.381\frac{2}{3}$	and 173.	25.	8271 and	7373.
12.	1383 and	174. 18	. 1575	and 193.	26.	9193 and	447 5.
13.	$149\frac{1}{6}$ and	185. 2	. 1183	and 48 <sup>2</sup> .	27.	376 <sup>1</sup> and	2873.
14.	4163 and	493. 22	$1. 387\frac{3}{8}$	and 1163.	28.	4452 and	3183.
15.	$512\frac{3}{4}$ and	537. 22	2. $248_1$	$\frac{1}{2}$ and 1294	. 29.	7373 and	438 <sup>2</sup> .
16.	100 and	133. 28	8. 764	and 3751	. 30.	6481 and	5263.

## MULTIPLICATION OF FRACTIONS.

## 214. To multiply a fraction by an integer.

215. PRINCIPLE. - Multiplying the numerator or dividing the denominator by a number multiplies the value of the fraction by that number (183, 1).

Ex. What will 4 pounds of tea cost @ \$3 a pound?

OPERATIONS.  

$$4 \times \frac{7}{8} = \frac{4 \times 7}{8} = \frac{28}{8} = 3\frac{1}{2}$$
Or,  

$$4 \times \frac{7}{8} = \frac{7}{8 \div 4} = \frac{1}{2} = 3\frac{1}{2}$$
Or,  

$$\frac{4}{1} \times \frac{7}{8} = \frac{7}{2} = 3\frac{1}{2}$$

ANALYSIS.-If 1 pound costs \$3, 4 pounds will cost 4 times \$7, or \$<sup>28</sup>, equal to \$3<sup>1</sup>/<sub>4</sub>. Hence, 4 pounds of tea @ \$% will cost \$31.

To multiply 3 by 4, multiply the numerator 7 by 4, or divide the denominator 8 by 4; either operation will give  $3\frac{1}{2}$ , the required product (Prin.).

By cancellation (166), the operation is shortened, and the result is obtained in its lowest terms.

Multiplying the numerator, as in the first operation, increases the number of parts, their size remaining the same ; dividing the denominator multiplies the fraction by increasing the size of the parts, their number remaining the same.

Ex. Multiply 1233 by 9.

OPERATION.

ANALYSIS.-Multiply the fraction \$ and the integer 123 separately, and add the products. In practice, when possible, add the products mentally; e. g., 9 times  $\frac{3}{4}$  are  $\frac{27}{4}$ , equal to  $6\frac{3}{4}$ . Write the §. 9 times 3 are 27, and 6 are 33. Write the 3, carry, and proceed as in simple numbers.

	OPERATIONS.	ANALYSIS As in preceding ex-
$227\frac{3}{4}$	Or, $227\frac{3}{4}$	ample.
175	175	Or, by aliquot parts, when the
4) 295	01/1	fractions are fourths, eighths, etc.,
4 ) 323	012	the fractions generally used in com-
$131\frac{1}{2}$	$44\frac{3}{4}$	mercial operations.
1135	1135	9 1 . 1 /1 . 6 1
1590	1589	$\frac{1}{4} = \frac{1}{2} + \frac{1}{4} (\frac{1}{2} \text{ OI } \frac{1}{2}).$
1000	2.2.17	$\frac{1}{2}$ of $175 = 87\frac{1}{2}$ .
227	~~ *	1  of  175  or  1  of  971 - 498
$39856_{4}^{1}$	$39856rac{1}{4}$	$\frac{1}{4}$ or 110, or $\frac{1}{2}$ or $0.1\frac{1}{2} = 40\frac{1}{4}$ .

Ex. Multiply 227<sup>3</sup>/<sub>4</sub> by 175.

**216.** RULE.—Multiply the numerator or divide the denominator of the fraction by the integer.

When the multiplicand is a mixed number, multiply the fraction and integer separately, and add the results.

#### EXAMPLES.

217. 1. Find the cost of 20 yards of silk at \$3 a yard.

2. How much grain in 12 bins, each containing 767 bushels?

3. If 1 man earns  $\$_{\frac{3}{8}}$  in 1 day, how much will 16 men earn in 26 days ?

4. If a ton of hay cost  $16\frac{3}{4}$ , how much will 22 tons cost?

5. Required the cost of 60 yards of muslin at 353 cents a yard.

Multiply

6.	9 by 7.	17.	412 <sup>3</sup> / <sub>8</sub> by 47.	28.	$234\frac{1}{2}$ by 318.
7.	$\frac{11}{16}$ by 8.	18.	1483 by 40.	29.	6783 by 427.
8.	<sup>2</sup> <del>2</del> <sup>2</sup> by 3.	19.	412 <del>3</del> by 89.	30.	$625\frac{3}{4}$ by 516.
9.	110 <sup>1</sup> / <sub>2</sub> by 12.	20.	775½ by 65.	31.	718 <sup>1</sup> / <sub>4</sub> by 542.
10.	117 <u>3</u> by 16.	21.	119 <del>9</del> by 20.	32.	2753 by 287.
11.	248§ by 3.	22.	772 <u>3</u> by 17.	33.	813§ by 319.
12.	$146\frac{2}{3}$ by 3.	23.	338 <del>§</del> by 30.	34.	4443 by 412.
13.	197 <del>1</del> by 7.	24.	550 <del>5</del> by 27.	35.	555 <del>5</del> by 875.
14.	420-9 by 8.	25.	643 <u>3</u> by 121.	36.	817 <sup>3</sup> / <sub>4</sub> by 416.
15.	384 <sup>5</sup> / <sub>8</sub> by 12.	26.	8753 by 234.	37.	913 <sup>1</sup> / <sub>4</sub> by 375.
16.	375½ by 48.	27.	916 <sup>1</sup> / <sub>2</sub> by 275.	38.	7874 by 525.

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Art. 218.] MULTIPLICATION OF FRACTIONS.

218. To multiply an integer by a fraction, or to find a fractional part of an integer.

**219.** PRINCIPLE.—Multiplying by a fraction is taking such part of the multiplicand as the fraction is of a unit.

Ex. If 1 ton of hay cost \$18, what will  $\frac{3}{4}$  of a ton cost?

	OPERA	TIONS.
	Or,	Or,
4)18	18	
41	3	9
3	4) 54	$\frac{3}{4} \text{ of } \frac{18}{1} = \frac{21}{2} = 13\frac{1}{2}$
131	131	2

ANALYSIS.—If 1 ton cost \$18,  $\frac{3}{4}$  of a ton will cost  $\frac{3}{4}$  of \$18.  $\frac{3}{4}$  of \$18 is 3 times  $\frac{1}{4}$  of \$18.  $\frac{1}{4}$  of \$18 is \$4 $\frac{1}{2}$  (taking  $\frac{1}{4}$  is the same as dividing by 4), and 3 times \$4 $\frac{1}{4}$  is \$13 $\frac{1}{4}$ .

Or, # of \$18 is # of 3 times \$18. 3 times \$18 is \$54. # of \$54 is \$131.

Ex. Find the product of 175 and 83.

	OPERATION	5.
175	Or,	175
$8\frac{3}{4}$		83
4) 525		$43\frac{3}{4}$
1314		3
1400		$131\frac{1}{4}$
15311		1400
-		15311

ANALYSIS.—Multiply by the fraction  $\frac{3}{4}$  and by the integer 8 separately, and add the products,

The first method is preferable, when the denominator of the fraction is not an exact divisor of the multiplicand.

## Ex. Multiply 275 by 473.

FIRST OPERATION.	SECOND OPERATION,	THIRD OPERATION.	ANALYSIS.—For the first and
275	275	275	ceding examples.
473	473	473	county on the second
8)825	$34\frac{3}{8}$	$68\frac{3}{4}$	When the fractions are
1031	3	$34\frac{3}{8}$	fourths, eighths, etc., multiply
1925 <sup>°</sup>	1031	1925	by means of aliquot parts.
1100	1925	1100	$\frac{3}{6} = \frac{1}{4} + \frac{1}{6} (\frac{1}{2} \text{ of } \frac{1}{4}).$
130281	1100	$13028\frac{1}{8}$	$\frac{1}{4}$ of $275 = 68\frac{3}{4}$ .
Ŭ	130281		$\frac{1}{2}$ of 275, or $\frac{1}{2}$ of $68\frac{3}{4} = 34\frac{3}{4}$ .

67

**220.** RULE.—Multiply by the numerator of the fraction and divide the product by the denominator. Or,

Divide by the denominator of the fraction and multiply the quotient by the numerator.

When the multiplier is a mixed number, multiply by the fraction and integer separately, and add the results.

#### EXAMPLES.

**221.** 1. Find the cost of  $8\frac{3}{4}$  yds. of ribbon at 25 cts. a yard. 2. What is the cost of  $42\frac{7}{8}$  pounds of butter at 26 cts. a pound ? 3. Required the value of  $48\frac{7}{8}$  yards of flannel at 75 cts. a yard. Multiply

4.	84 by $\frac{3}{4}$ .	10.	216 by 143.	16.	780 by 645.
5.	126 by <del>4</del> .	11.	375 by 243.	17.	512 by 37 <del>1</del> .
6.	49 by <del>§</del> .	12.	375 by 223.	18.	611 by 87 <del>1</del> .
7.	128 by 9 <del>1</del> .	13.	146 by 28 <sup>3</sup> / <sub>4</sub> .	19.	625 by 923.
8.	156 by 8 <sup>1</sup> / <sub>4</sub> .	14.	184 by 16 <del>§</del> .	20.	937 by 753.
9.	187 by 103.	15.	110 by 413.	21.	575 by 817.

## 222. To multiply a fraction by a fraction.

Ex. At  $3\frac{1}{4}$  a pound, what will  $\frac{3}{4}$  of a pound of tea cost?

 OPERATION.

  $\frac{3}{4} \times \frac{7}{9} = \frac{21}{36} = \frac{7}{12}$  ANALYSIS.—If 1 pound cost  $\$_7^7$ ,  $\frac{3}{4}$  of a pound will cost  $\frac{3}{4}$  of  $\$_7^7$ .

 Or,
  $\frac{3}{4} \times \frac{7}{12} = \frac{7}{12}$   $\frac{1}{4}$  of  $\$_7^7$  is  $\$_7^7$ , and 3 times  $\$_7^7$  is  $\$_{36}^2$ , or  $\$_{72}^7$ .

Ex. What is the value of  $8 \times 8\frac{1}{3} \times \frac{1}{10} \times \frac{1}{14}$ ?

$\frac{4}{\frac{8}{1}}^{2}$	OPERATION. $\frac{5}{3} \times \frac{7}{10} \times \frac{1}{14} = \frac{10}{3} = 3\frac{1}{3}$	ANALYSIS.—Reduce the inte- ger 8 and the mixed number $8\frac{1}{3}$ to improper fractions, and mul-
	X X	tiply as in the preceding example.

**223.** Rule.—*Reduce integers and mixed numbers to improper fractions.* 

Cancel all factors common to the numerators and denominators.

Multiply the remaining numerators together for the numerator, and the remaining denominators for the denominator. Art. 224.] MULTIPLICATION OF FRACTIONS.

#### EXAMPLES.

224. Find the product of

1. $\frac{3}{8}$ a	nd z.	5. $\frac{5}{8}$ and	12.	9.	1/8, 131/3, and 1/3.
2. <sup>2</sup> / <sub>3</sub> a	nd Z.	6. 6, 3 <del>1</del>	, and <del>§</del> .	10.	261, \$, and 3.
3. $\frac{3}{4}$ a	nd 15.	7. 53, 4	, and $\frac{21}{34}$ .	<i>11</i> .	$\frac{3}{4}, \frac{8}{9}, \text{ and } 16\frac{4}{7}.$
4. $\frac{2}{5}$ a	nd $\frac{10}{7}$ .	$8, 12\frac{1}{2}, 1$	$10\frac{2}{3}$ , and $\frac{5}{12}$ .	12.	131, 4, and 3.

Reduce the following compound fractions to simple ones.

A Compound Fraction is a fraction of a fraction. The word "of" is equivalent to the sign  $\times$ .

13.	$\frac{1}{2}$ of $\frac{2}{3}$ of $\frac{3}{4}$ .	17. 5 of 8 of 18.	21.	5 of 48 of 15.
14.	<sup>2</sup> / <sub>3</sub> of 3 <sup>1</sup> / <sub>7</sub> of <sup>4</sup> / <sub>5</sub> .	18. $\frac{3}{8}$ of $11\frac{2}{3}$ of $\frac{5}{7}$ .	22.	2 of 3 of 5 of 8.
15.	3 of 5 of 71.	19. $\frac{16}{21}$ of $\frac{14}{15}$ .	23.	$\frac{1}{4}$ of $12\frac{1}{2}$ of $6\frac{2}{5}$ .
16.	$\frac{3}{4}$ of $\frac{7}{8}$ of $5\frac{1}{3}$ .	20. $\frac{7}{12}$ of $\frac{8}{9}$ of $\frac{5}{72}$ .	24.	5 of 18 of 43.

Find the value of the following expressions :

25.	3 of 1728.	30.	$(\frac{4}{5}+\frac{9}{10})\times(\frac{3}{7}+\frac{5}{14}).$
26.	$\frac{3}{4} \times 375.$	31.	$(\frac{3}{4}-\frac{2}{3})\times(\frac{7}{8}+\frac{3}{4}).$
27.	7 times 864.	32.	$\left(\frac{5}{12}+\frac{3}{4}\right)\times\left(\frac{5}{14}-\frac{1}{7}\right).$
28.	$\frac{2}{3}$ of 75 $\times \frac{3}{4}$ of 16 $\frac{2}{3}$ .	33.	$37\frac{1}{2}$ times $\frac{2}{3}$ of $\frac{9}{10}$ .
29.	$\frac{7}{8} \times \frac{3}{4}$ of $\frac{5}{12} \times \frac{8}{9}$ .	34.	$\frac{3}{8}$ of $\frac{5}{9} \times \frac{5}{6}$ of $\frac{2}{3}$ .

225. To multiply mixed numbers together.

Ex. Multiply 1473 by 415.

	OPERATION.				
	$147\frac{3}{4}$				
	$41\frac{5}{8}$				
	$\frac{15}{32}$	=	58	×	34
8)735	$91\frac{7}{8}$	=	58	$\times$	147
4)123	$30\frac{3}{4}$	=	41	$\times$	<u>3</u> 4
	147 )	_	11	~	117
	588 J	_	TI	^	TI!
	615033				

ANALVSIS.—Commencing at the right as in multiplication of integers, first multiply the fraction and integer of the multiplicand by the fraction of the multiplier; and then multiply the fraction and integer of the multiplicand by the integer of the multiplier. The separate steps are indicated at the right of the operation. The sum of the several partial products will be the required product.

[Art. 226.

**226.** RULE. —Multiply the fractions together, each integer by the fraction of the other number, and the integers together. The sum of the partial products will be the product required.

Note.—When both mixed numbers are small, reduce them to improper fractions and multiply as in multiplication of fractions (223).

1	EXAMPLES.										,	
22	7. M	ulti	ply				/ Mu	ltiply			7	
1.	8751	by	81;	by	374.		/ 6.	7163 by	271;	by	$58\frac{1}{2}$ .	
2.	7374	by	$10\frac{1}{2};$	by	$12\frac{1}{4}$ .	1	7.	447 <u>1</u> by	$45\frac{1}{2};$	by	$64\frac{3}{8}$ . /	
3.	5123	by	71;	by	$27\frac{1}{2}$ .		8.	4593 by	$37\frac{3}{4};$	by	$39\frac{3}{4}.$	
4.	4493	by	$16\frac{1}{4};$	by	$36\frac{1}{8}$ .		9.	$378\frac{1}{2}$ by	$43\frac{1}{2};$	by	404.	
5.	6121	by	131;	by	425.		10.	4791 by	564;	by	27 8./	
	-								_			

DIVISION OF FRACTIONS.

## 228. To divide a fraction by an integer.

**229.** PRINCIPLE.—Dividing the numerator or multiplying the denominator by a number, divides the value of the fraction by that number (183, 2).

Ex. What cost 1 pound of tea, if 5 pounds cost  $3\frac{1}{3}$ ?

OPERATIONS.  

$$\frac{10}{3} \div 5 = \frac{10 \div 5}{3} = \frac{2}{3}$$
  
r,  $\frac{10}{3} \div 5 = \frac{10}{3 \times 5} = \frac{10}{15} = \frac{2}{3}$   
Or,  $\frac{2}{3\frac{10}{3}} \times \frac{1}{3} = \frac{2}{3}$ 

0

ANALYSIS.—If 5 pounds cost \$3<sup>1</sup>/<sub>5</sub>, 1 pound will cost <sup>1</sup>/<sub>5</sub> of \$3<sup>1</sup>/<sub>3</sub>, or \$<sup>3</sup>/<sub>5</sub>.

To divide  $\frac{10}{2}$  ( $3\frac{1}{3}$ ) by 5, divide the numerator 10 by 5, or multiply the denominator 3 by 5; either operation will give  $\frac{9}{3}$ , the required quotient (*Prin.*).

Dividing the numerator, as in the first operation, decreases the number of parts, their size remaining the same ; multiplying the denominator divides the fraction by decreasing the size of the parts, their number remaining the same.

Ex. Divide  $867\frac{3}{4}$  by 4.

OPERATION.

$$\begin{array}{ccc} 4 \\ \underline{) 8673} \\ \hline 216\frac{15}{16} \\ \hline 3\frac{3}{4} = \frac{15}{4} \\ \hline 1\frac{5}{4} \div 4 = \frac{15}{16} \\ \hline 1\frac{5}{4} \div 4 = \frac{15}{16} \\ \hline \end{array}$$

ANALYSIS.—Dividing as in simple numbers, 4 is contained in 867 $\frac{3}{4}$ , 216 times and a remainder of  $3\frac{3}{4}$ .  $3\frac{3}{4}$  equals  $\frac{15}{4}$ , which divided by 4 is  $\frac{15}{4}$ .
#### Art. 230.] DIVISION OF FRACTIONS.

**230.** RULE.—Divide the numerator or multiply the denominator of the fraction by the integer.

When the dividend is a mixed number, divide the integer and the fraction separately, and add the results.

EXAMPLES.

~					
1.	<sup>3</sup> / <sub>4</sub> by 6.	/ 11.	637 <u>1</u> by 9.	21.	5316 <sup>2</sup> / <sub>3</sub> by 4.
2.	§ by 3.	12.	875 <u>5</u> by 12.	22.	71441 by 5.
3.	<sup>8</sup> / <sub>9</sub> by 6.	13.	17163 by 8.	23.	1729 <sup>3</sup> / <sub>4</sub> by 3.
4.	$\frac{5}{12}$ by 4.	14.	1729 <del>1</del> by 3.	24.	17491 by 9.
5.	$\frac{8}{17}$ by 4.	15.	$2418\frac{3}{4}$ by 5.	25.	8763 <sup>1</sup> / <sub>2</sub> by 6.
6.	$16\frac{3}{4}$ by 5.	16.	3516 <sup>3</sup> / <sub>7</sub> by 5.	26.	7385 <u>3</u> by 8.
7.	$172\frac{1}{2}$ by 3.	17.	$2428\frac{3}{4}$ by 3.	27.	4255 <sup>3</sup> / <sub>8</sub> by 9.
8.	875 <sup>2</sup> / <sub>3</sub> by 6.	18.	6375 <del>3</del> by 4.	28.	71343 by 7.
9.	935 <u>3</u> by 8.	19.	42873 by 2.	29.	9727 <del>1</del> by 12.
10.	729½ by 9.	20.	3281 <del>1</del> by 8.	30.	63453 by 16.

232. To divide by a fraction.

231 Divide

**233.** The **Reciprocal** of a number is 1 divided by that number. Thus, the reciprocal of 4 is 1 divided by 4, or  $\frac{1}{4}$ .

The Reciprocal of a Fraction is 1 divided by that fraction.

**234.** PRINCIPLE.—1 divided by a fraction is the fraction inverted.

Thus, 1 divided by  $\frac{3}{4}$  is  $\frac{4}{5}$ . This principle may be demonstrated as follows: In 1 there are 4 fourths. 1 fourth is contained in 4 fourths 4 times. Since  $\frac{3}{4}$  is 3 times  $\frac{1}{4}$ ,  $\frac{3}{4}$  is contained in 1  $\frac{1}{5}$  as many times as  $\frac{1}{4}$ . Hence,  $\frac{3}{4}$  is contained in 1  $\frac{1}{5}$  of 4 times, or  $\frac{4}{5}$  times.

The reciprocal of a fraction is the fraction inverted.

Ex. At  $\$_4^3$  a yard, how many yards of cloth can be bought for \$5?

OPERATIONS.

 $5 \div \frac{3}{4} = \frac{20}{4} \div \frac{3}{4} = 6\frac{2}{3}$ Or,  $5 \div \frac{3}{4} = \frac{5}{1} \times \frac{4}{3} = \frac{20}{3} = 6\frac{2}{3}$  ANALYSIS.—Since 1 yard cost \$\$, as many yards can be bought for \$5 as \$\$ is contained times in \$5. 5 is equal to  $\frac{29}{2}$ , and 3 fourths is contained in 20 fourths  $6\frac{5}{8}$  times.

Or,  $\$_{\frac{3}{4}}$  is contained in  $\$1_{\frac{3}{5}}$  times (*Prin.*), and in \$5, 5 times  $\frac{4}{5}$  or  $\frac{20}{5}$ , equal to  $6\frac{3}{5}$  times.

Ex. At  $\$_4^3$  a yard, how many yards of cloth can be bought for  $\$_6^5$ ?

· OPERATIONS.					
	$\frac{5}{6} \div \frac{3}{4} = \frac{10}{12} \div \frac{9}{12} = 1\frac{1}{9}$				
Or,	$\frac{5}{6} \div \frac{3}{4} = \frac{5}{6} \times \frac{4}{3} = \frac{20}{18} = 1\frac{1}{9}$				
0r,	$\frac{5}{6} \div \frac{3}{4} = \frac{5}{8} \times \frac{3}{3} = \frac{10}{9} = 1\frac{1}{9}$				

ANALYSIS.—Since 1 yard cost  $\$\frac{3}{4}$ , as many yards can be bought for  $\$\frac{5}{5}$  as  $\$\frac{3}{4}$  is contained times in  $\$\frac{5}{5}$ .  $\frac{3}{4}$  is equal to  $\frac{7}{15}$ , and  $\frac{5}{6}$  is equal to  $\frac{19}{2}$ .  $\frac{9}{15}$  is contained in  $\frac{19}{12}$   $\frac{11}{5}$  times. Or,  $\$\frac{3}{4}$  is contained in \$1

1/2 times (Prin.), and in \$5, 5 times 1/2 or 1/8, equal to 11/2 times.

Ex. If 6% yards of cloth cost \$5, what will 1 yard cost?

OPERATIONS.  $5 \div \frac{2}{30} = (5 \div 20) \times 3 = \frac{3}{4}$ Or,  $5 \div \frac{2}{30} = \frac{5}{1} \times \frac{3}{20} = \frac{15}{20} = \frac{3}{4}$ Or,  $5 \div \frac{2}{30} = \frac{5}{1} \times \frac{3}{20} = \frac{3}{4}$ 4

ANALYSIS.  $-6\frac{2}{3}$  yards are equal to  $\frac{2}{3}$  yards. Since  $\frac{2}{3}$ yards cost \$5,  $\frac{1}{3}$  of a yard will cost  $\frac{1}{20}$  of \$5 or \$ $\frac{1}{4}$ , and  $\frac{3}{4}$  or 1 yard will cost 3 times \$ $\frac{1}{4}$  or \$ $\frac{3}{4}$ .

Or, the price per yard equals the cost, divided by the quantity as an abstract number. 5 divided by  $\frac{20}{3}$  equals 5 times 1 divided by  $\frac{20}{5}$ , or 5 times  $\frac{3}{20}$  (*Prin.*), equal to  $\frac{3}{4}$ .

Ex. Divide 7552 by 783.

	OPE	RATI	ON.	
78	2)	755	2	
3			3	
236	) 2	265	6 (	96
	2	124		
	_	141	6	
		141	6	

ANALYSIS.—Reduce both divisor and dividend to thirds as in the operation, omitting the common denominators.  $\frac{22659}{5} \div \frac{236}{8}$  is the same as  $22656 \div 236$ .

Or, multiplying both divisor and dividend by the same number does not affect the quotient. Multiply both divisor and dividend by 3, and then divide as in simple numbers.

Ex. Divide 2195# by 175%.

0	PERATION.	
$175\frac{2}{3}$	$)\ 2195\frac{5}{6}$	
6	6	
1054 )	13175 (	$12\frac{1}{2}$
	1054	
	2635	
	2108	
	527	4
	$\overline{1054}$	= \$

ANALYSIS.—Reduce both divisor and dividend to sixths, their least common denominator, reject the common denominator, and divide the numerators as in simple numbers.

Or, multiply both divisor and dividend by 6, the least common denominator, and divide as in simple numbers (see preceding analysis).  $175\frac{3}{5} = 175\frac{4}{5}$ .

**235.** RULE.—Reduce the divisor and dividend to equivalent fractions having a common denominator, and divide the numerator of the dividend by the numerator of the divisor. Or,

Invert the terms of the divisor and proceed as in multiplication.

In dividing mixed numbers, multiply both divisor and dividend by the least common denominator, and divide as in simple numbers.

Note.—If both mixed numbers are small, reduce them to improper fractions, and apply the rule for division of fractions.

,	236. Divide	1		ŀ	
1.	1 by <del>3</del> .	14.	73 by 8 <del>1</del> .	27.	920 by 733.
2.	16 by <del>§</del> .	15.	45 by 7 <del>3</del> .	28.	720 by 43 <del>]</del> .
3.	28 by 3.	16.	$8\frac{1}{2}$ by $3\frac{3}{4}$ .	29.	700 by 37 <del>1</del> .
4.	49 by <del>]</del> .	17.	63 by 31.	30.	560 by 26 <del>1</del> .
5.	88 by 3.	18.	$4\frac{5}{7}$ by $3\frac{2}{3}$ .	31.	682½ by 45½.
6.	34 by 7.	19.	71 by 81.	32.	847 <del>3</del> by 894.
7.	5 by 3.	20.	97 by 181.	33.	984 <sup>3</sup> by 75 <sup>3</sup> .
8.	9 by 3.	21.	875 by 331.	24.	8623 by 183.
9.	<sup>7</sup> / <sub>12</sub> by <sup>5</sup> / <sub>8</sub> .	22.	625 by 83 <del>]</del> .	- 56	7311 by 561.
10.	3 by 3.	23.	516 by 34 <sup>2</sup> / <sub>5</sub> .	X.	431 <sup>1</sup> / <sub>4</sub> by 18 <sup>3</sup> / <sub>4</sub> .
11.	28 by 41.	24.	917 by 43 <sup>2</sup> / <sub>3</sub> .	5	983 <sup>1</sup> / <sub>3</sub> by 29 <sup>1</sup> / <sub>2</sub> .
12.	33 by 33.	25.	864 by 86 <sup>2</sup> / <sub>5</sub> .	38.	504 <sup>1</sup> / <sub>6</sub> by 36 <sup>2</sup> / <sub>3</sub> .
13.	64 by 5 <sup>2</sup> / <sub>5</sub> .	26.	702 by 304.	39.	583 <sup>1</sup> / <sub>3</sub> by 43 <sup>3</sup> / <sub>4</sub> .

Find the value of the following complex fractions (182) and expressions of division :

40.	$\frac{5\frac{1}{16}}{9}; \frac{4\frac{2}{3}}{35}; \frac{24\frac{3}{4}}{36}.$	43.	$\frac{\frac{3}{5} \text{ of } \frac{3}{4}}{\frac{1}{5} \text{ of } 2\frac{1}{4}}; \frac{\frac{1}{5} + 3\frac{1}{5}}{5\frac{2}{3} - 3\frac{1}{6}}.$
41.	$\frac{3\frac{1}{8}}{40}; \frac{8\frac{2}{3}}{13}; \frac{16\frac{2}{3}}{20}.$	44.	$\frac{18\frac{1}{2} \div 12\frac{1}{3}}{16\frac{1}{2} - 15\frac{1}{5}}; \frac{12\frac{1}{2} \times 11\frac{1}{5}}{68\frac{3}{4} + 1\frac{1}{4}}.$
42.	$\frac{5\frac{1}{2}}{7\frac{1}{3}}; \frac{\frac{3}{4}}{\frac{7}{8}}; \frac{\frac{9}{10}}{\frac{3}{8}}.$	45.	$\frac{175\frac{3}{4}-16\frac{7}{8}}{187\frac{1}{5}-186\frac{7}{8}};\frac{38\frac{3}{5}-30\frac{1}{5}}{16\frac{1}{5}+8\frac{2}{5}}.$

EXAMPLES.

737

## REVIEW EXAMPLES.

237. 1. Reduce 288 to its lowest terms.

2. Reduce 7 to forty-eighths.

3. Reduce  $727\frac{3}{2}$  to an improper fraction.

4. Reduce 13751 to a mixed number.

5. Add 171, 373, 183, 495, 133, and 56512.

6. From 17281 take 8651.

7. Multiply  $\frac{1}{2} \times 3\frac{1}{2} \times \frac{5}{14} \times \frac{3}{10} \times 16\frac{2}{3}$ .

8. Multiply 17273 by 175.

9. Multiply 1727 by 1753.

10. Divide  $1\frac{7}{8}$  by  $\frac{3}{16}$ .

11. Divide 1736 by 1442.

12. Divide 5779% by 275%.

13. Divide 123461 by 7; by 35.

14. What is the cost of 1583 pounds sugar @  $11\frac{3}{4}$  cts. per pound?

15. Add  $\frac{3}{5}$  of  $\frac{7}{5}$  of  $4\frac{1}{5}$ ,  $\frac{5}{5}$ ,  $136\frac{2}{5}$ , and  $\frac{5\frac{3}{5}}{2}$ .

16. A merchant sold a quantity of goods for \$144, which was 4 of the cost. What was the cost ?

ANALYSIS.—If \$144 is  $\frac{3}{4}$  of the cost,  $\frac{1}{4}$  of the cost is  $\frac{1}{4}$  ( $\frac{1}{4}$  is  $\frac{1}{5}$  of  $\frac{3}{4}$ ) of \$144, or \$48.  $\frac{4}{4}$ , or the total cost, is 4 times ( $\frac{4}{4}$  is 4 times  $\frac{1}{4}$ ) \$48, or \$192.

17. Required the value of 2993 pounds of sugar @  $9\frac{3}{8}$  cts. per pound ?

18. If  $\frac{1}{5}$  of a ship is worth \$42430 $\frac{1}{2}$ , what is the value of the whole ?

19. Bought  $47\frac{3}{4}$  yards of cloth at  $\$4\frac{1}{2}$  per yard, and paid for it in wheat at  $\$2\frac{1}{4}$  per bushel; how many bushels were required?

20. Find the value of 3113 pounds snuff @ 72 cts. per pound.

21. The less of two numbers is  $777\frac{3}{4}$  and their difference  $117\frac{3}{8}$ ; what is the greater number ?

22. A and B together have \$1728; if A's money is equal to  $\frac{3}{5}$  of B's, how much has each ?

23. A having  $2146\frac{3}{4}$  yards of cloth, sold  $\frac{5}{8}$  of it at  $\$1\frac{3}{4}$  a yard, and the remainder at  $\$2\frac{1}{4}$  a yard; how much did he receive?

24. A number being increased by  $\frac{6}{8}$  of itself, the sum is 546; what is the number ? (The number is  $\frac{6}{8}$  of itself.)

25. A man had \$5280; he bought goods with  $\frac{3}{8}$  of it, and then lent  $\frac{1}{4}$  of the balance to a friend; how much had he left?

26. Find the selling price of goods sold at a profit of \$75, being  $\frac{2}{3}$  of the cost.

27. Mr. A bought  $117\frac{3}{4}$  acres of land at one time, and  $87\frac{5}{3}$  at another; after selling  $110\frac{2}{3}$  acres, how much remained?

28. If  $8\frac{3}{4}$  tons of coal cost  $\$30\frac{5}{8}$ , what will  $27\frac{1}{2}$  tons cost? How many tons can be bought for  $\$127\frac{3}{4}$ ?

29. A man paid \$1145§ for a horse and carriage. What was the value of each, the carriage being valued at § as much as the horse ?

30. If  $\frac{3}{4}$  of a farm is valued at \$2253 $\frac{1}{2}$ , what is the value of  $\frac{2}{3}$  of it?

31. What is the value of  $2102^1$  yards prints at 7<sup>2</sup> cents per yard?

32. What number must be taken from  $96\frac{3}{4}$ , and the remainder multiplied by  $16\frac{3}{4}$ , that the product shall be  $770\frac{5}{4}$ ?

33. What is the value of  $164^2$  yards muslin at  $5\frac{3}{4}$  cents per yard?

34. If 7 barrels of oil contain  $313\frac{1}{4}$  gallons, how many gallons will  $2\frac{3}{4}$  barrels contain ?

35. An executor collects \$12724.84. He pays out \$4096.48, and the residue he pays to the widow and her four children as follows: The widow receives a third part, and the remainder is divided equally among the children. Find the share of each.

36. What number increased by 3 of itself will produce 24561?

37. Find the selling-price of goods, bought at \$144, and sold at 4 above cost.

38. A invests  $\frac{5}{8}$  of his capital in real estate, and has \$1725 remaining; what is his capital?

39. Bought a barrel of sugar containing 220 lbs., at  $8\frac{1}{2}$  cents per pound. During the sale, it dried away  $\frac{1}{10}$ . Did I gain or lose, and how much, by selling it at  $9\frac{1}{4}$  cents per pound?

40. Multiply 23751 by 81; by 104.

41. Multiply 17273 by 181; by 1073.

42. Multiply 3771 by 161; by 373.

43. Multiply 8751 by 221; by 95.

44. A merchant sold  $12\frac{1}{3}$  yards of silk to one customer,  $21\frac{1}{4}$  to another,  $20\frac{3}{8}$  to another, and  $28\frac{1}{2}$  to another; at  $2\frac{3}{3}$  per yard, how many dollars did he receive? 45. An army loses  $\frac{3}{16}$  of its number in battle and has 16042 remaining; how many did it originally contain?

46. What is the cost of 34 pieces prints, containing  $1604^2$  yards, at 5<sup>1</sup> cents per yard?

47. What is the value of 12 pieces prints containing 48,  $48^1$ ,  $48^2$ , 48,  $49^2$ ,  $48^3$ ,  $48^3$ ,  $49^2$ ,  $48^3$ ,  $49^2$ ,  $48^3$ ,  $49^2$ ,  $48^3$  yards respectively at  $4^3$  cents per yard?

48. A merchant purchased 29 pieces prints containing 48<sup>3</sup>, 48<sup>2</sup>, 41<sup>2</sup>, 48<sup>2</sup>, 48<sup>3</sup>, 4<sup>7</sup>, 49, 49<sup>2</sup>, 52<sup>1</sup>, 57<sup>3</sup>, 48<sup>3</sup>, 48<sup>2</sup>, 38, 48<sup>2</sup>, 48<sup>2</sup>, 48<sup>2</sup>, 48<sup>2</sup>, 47<sup>3</sup>, 48<sup>2</sup>, 48, 51, 48, 44<sup>1</sup>, 51<sup>2</sup>, 48, 42<sup>3</sup>, 46<sup>2</sup>, 48, 48<sup>2</sup>, 48<sup>3</sup> yards respectively; what was the cost at  $5^2$  cents per yard?

49. There are 5280 feet in one mile, and  $16\frac{1}{2}$  feet in one rod; how many rods in one mile?

50. A can do a certain piece of work in 10 days, and B can do it in 15 days; how long will it take them both to do it ?

51. A market-woman bought 120 oranges at the rate of 5 for 2 cents, and sold  $\frac{1}{2}$  of them at the rate of 3 for 1 cent, and the remainder at the rate of 2 for 1 cent. Did she gain or lose, and how much ?

52. What is the duty on 22375 pounds sugar at  $2\frac{13}{16}$  cts. per pound ?

53. A farmer sold  $1276\frac{19}{3\frac{12}{2}}$  bushels oats at 44 cts. per bushel,  $876\frac{22}{3\frac{12}{2}}$  bushels corn at  $52\frac{3}{4}$  cts., and  $3381\frac{4}{6\frac{12}{3}}$  bushels wheat at \$1.32; how much did he receive ?

54. How many bushels of corn at  $54\frac{1}{4}$  cts. per bushel must a farmer exchange for 62 yards of sheeting at  $8\frac{3}{4}$  cts. per yard, and <u>31</u> yards broadcloth at \$1.75 per yard?

55. What is the value of 45<sup>3</sup> yards damask at 77<sup>2</sup> cts. per yard.

56. The salary of the President of the United States is \$50000 per year; how much is that per day?

57.  $1\frac{4}{16}$  pounds of beef and  $1\frac{6}{16}$  pounds of flour are allowed to a ration; how much will 617 rations cost, if the price of beef is  $11\frac{3}{8}$  cts. per pound, and of flour  $3\frac{1}{4}$  cts. per pound?

58. What is the value of 36385 pounds of corn at  $48\frac{3}{4}$  cents per bushel, each bushel containing 56 pounds?

59. What is the least common multiple of the nine digits?

60. The total production of gold and silver in the United States from 1792 to 1886 was \$2,403,986,769. What was the average production per year?

## DECIMALS.

**238.** A Decimal (from the Latin *decem*, ten) Fraction is a fraction whose denominator is 1 followed by one or more ciphers; as  $\frac{3}{10}$ ,  $\frac{16}{100}$ ,  $\frac{7}{1000}$ ,  $\frac{146}{10000}$ .

239. Decimal fractions arise from dividing a unit into 10 equal parts, and then dividing these parts into 10 other equal parts, and so on.

Thus, if a unit be divided into 10 equal parts, each part is called a *tenth*. If a unit be divided into 100 equal parts, or 1 tenth into 10 equal parts, the parts are called *hundredths*. If a unit be divided into 1000 equal parts, or 1 hundredth into 10 equal parts, the parts are called *thousandths*.

**240.** All the rules, principles, operations, etc., of common fractions may be applied to decimal fractions. Since decimal fractions increase and decrease uniformly according to the scale of ten, a more simple notation, similar to that of integers, has been devised for them.

A hundred is written 100; a tenth part of a hundred (ten) is written 10, the 1 being written one place to the right; a tenth part of one ten (one unit) is written 1, the 1 being written one place to the right; in like manner, a tenth part of one unit (one-tenth) is written .1, the 1 being written one place to the right; the tenth part of one-tenth (one hundredth) is written .01, the 1 being written one place to the right, etc., etc.

Decimal fractions, like integers, decrease from left to right in a tenfold ratio, and increase from right to left in the same ratio.

241. In the decimal notation, the numerator only is written, the denominator being indicated by the position of a point (.) called the *decimal point*. The decimal point separates the integral from the fractional part.

#### DECIMALS.

242. The denominator of a decimal fraction is understood, and is 1 with as many ciphers annexed as there are figures in the decimal; thus,

Form of common frac	f ction	. decir	Form of nal fract	tion.			
7 10	is	written	.7	and	is	read	seven tenths.
100	66	66	.08	66		66	eight hundredths.
$\frac{16}{1000}$	66	66	.016	3 "		"	sixteen thousandths.

Hereafter, the first form, that of the common fraction, will be called a *fraction*, and the second, that of the decimal notation, a *decimal*.

**243.** The first place to the right of the point is called *tenths*, the second place *hundredths*, the third place *thousandths*, and so on.

**244.** The relation between integers and decimals is shown in the following



**245.** In the above table, observe that the first place to the left of units is called *tens*, and the first place to the right, *tenths*; the second place to the left of units is called *hundreds*, and the second place to the right, *hundredths*, etc. Hence the number of any order or place of the decimal, counting from the point, or from units' place, is the same as the number of ciphers in the denominator of the decimal.

**246.** A Complex Decimal has a fraction in its right-hand place.

Thus,  $.16\frac{3}{5}\left(\frac{16\frac{5}{5}}{100}\right)$  is a complex decimal, and is read  $16\frac{3}{5}$  hundredths, the fraction not being counted as a decimal place.

Art. 247.] NUMERATION OF DECIMALS.

**247.** PRINCIPLES.—1. Annexing ciphers to a decimal does not alter its value.

Annexing a cipher multiplies both the numerator and the denominator by 10, and hence does not alter the value of the decimal (**183**, 3). Thus,  $.7 \begin{pmatrix} 7 \\ T0 \end{pmatrix} = .70 \begin{pmatrix} 7 0 \\ 7 0 0 \end{pmatrix} = .700 \begin{pmatrix} 7 0 \\ 7 0 0 \end{pmatrix}$ .

2. Each removal of the decimal point one place to the right multiplies the value of the decimal by 10.

Removing the point one place to the right does not change the numerator, but divides the denominator by 10, and hence multiplies the value of the decimal (183, 1). Thus,  $.072\left(\frac{72}{100}\right)$  becomes  $.72\left(\frac{72}{100}\right)$ ;  $\frac{72}{100} = \frac{72}{100} \times 10$ .

3. Each removal of the decimal point one place to the left divides the value of the decimal by 10.

Removing the point one place to the left does not change the numerator, but multiplies the denominator by 10, and hence divides the value of the fraction by 10 (**183**, 2). Thus, .72  $(\frac{72}{100})$  becomes .072  $(\frac{72}{1000})$ ;  $\frac{72}{1000} = \frac{72}{100} \div 10$ .

## NUMERATION OF DECIMALS.

**248.** RULE.—Read the decimal as if it were an integer, and give it the name of its right-hand order.

#### EXERCISES.

249. Write in words, or read orally the following numbers :

1.	.6.	8.	17.6.	15.	$375.18\frac{3}{4}.$
2.	.008.	9.	8.029.	16.	$19.0033\frac{1}{3}$ .
3.	.27.	10.	24.000488.	17.	6.1483.
4.	.0375.	11.	400.000088.	18.	648.63.
5.	.0108.	12.	76.7071.	19.	347.18005.
6.	. **75.	13.	3000.0045.	20.	808.008.
7.	.1007.	14.	.3045.	21.	600.06.

## NOTATION OF DECIMALS.

**250.** Write sixty-four thousandths in the form of a decimal.

ANALVSIS.—Since there are only two figures in the numerator 64, and the right-hand figure of the decimal must occupy the third decimal place to express thousandths, it is necessary to prefix a cipher to bring the right-hand figure into its proper place. Therefore write *point*, *naught*, *six*, *four* (.064) in the order named.

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#### DECIMALS.

**251.** RULE.—*Prefix the decimal point, and decimal ciphers if necessary, to the numerator written as an integer, so that the right-hand figure will occupy the order named.* 

Note.—Before writing, determine mentally the place of the right-hand figure and the number of ciphers required. Write in all cases from left to right.

#### EXERCISES.

252. 1. What is the name of the third decimal order? The sixth? The first? The fourth? The second? The seventh?

2. How many decimal places are required to express hundredths? Millionths? Ten-thousandths? Tenths? Hundredmillionths? Hundred-thousandths?

3. How many ciphers must be written after the decimal point in writing 375 millionths? 27 hundredths? 875 thousandths? 446 ten-millionths? 37 ten-thousandths?

4. Write the following as decimals, so that the decimal-points stand in the same vertical line: 8 tenths; 16 hundredths; 175 thousandths; 1804 millionths; 56 ten-thousandths; 3004 tenmillionths; 1728 ten-thousandths.

5. Seventeen, and seventy-five hundredths.

6. Twenty-six, and twenty-six thousandths.

7. Two hundred forty-six ten-millionths.

8. Two hundred, and forty-six ten-millionths.

9. Three hundred seventy-five, and eighteen hundred-thousandths.

10. Eight thousand, and sixty-five ten-thousandths.

11. Eight thousand sixty-five ten-thousandths.

 $12. \frac{7}{10}, \frac{37}{100}, 19\frac{3}{10}, 218\frac{325}{1000}, \frac{1728}{10000}.$ 

13.  $16_{\frac{75}{100}}, 19_{\frac{37}{1000}}, 345_{\frac{12}{1000}}, \frac{75}{10000}, \frac{1234}{10000}$ 

14.  $28_{1000}$ ,  $37_{100}$ ,  $376_{100000}$ ,  $44_{10000}$ ,  $\frac{5387}{100000}$ .

15.  $170_{100000}$ ,  $16000_{100000}$ ,  $38_{100}$ ,  $\frac{16225}{100000}$ .

16.  $\frac{4}{10}$ ,  $300_{\frac{75}{1000}}$ ,  $\frac{375}{1000}$ ,  $1635_{\frac{216}{1000}}$ ,  $500_{\frac{63}{100}}$ .

17.  $1027\frac{13}{100}, \frac{16}{10000}, \frac{214}{100000}, \frac{387}{1000000}$ 

18.  $2016_{1000}, \frac{306}{10000}, \frac{1707}{100000}, 104_{100002}$ 

19.  $400_{1000}, \frac{414}{1000}, 8000_{10000}, \frac{8006}{10000}$ 

## REDUCTION OF DECIMALS.

## 253. To reduce a fraction to a decimal.

Ex. Reduce <sup>3</sup> to a decimal.

OPERATION.

Art. 253.]

ANALYSIS.—<sup>3</sup> equals <sup>1</sup>/<sub>4</sub> of 3 units. 3 units equal 300 4) 3.00 hundredths.  $\frac{1}{4}$  of 300 hundredths equal 75 hundredths. .75

254. RULE.—Annex decimal ciphers to the numerator. and divide by the denominator, pointing off as many decimal places in the quotient as there are ciphers annexed.

255. A fraction in its lowest terms can be reduced to a pure decimal only when its denominator contains no prime factors but 2 and 5. If the denominator or divisor contain any prime factor other than 2 and 5, the divisor will not end. The decimals thus produced are called Interminate or Repeating Decimals, and the figures repeated, Repetends.

When a fraction is in its lowest terms, its numerator and denominator have no common factors (187). Annexing ciphers to the numerator introduces the factors 2 and 5 only; hence, if the denominator is an exact divisor of the numerator with the ciphers annexed, it must contain these prime factors and no others.

#### EXAMPLES.

256. Reduce to equivalent decimals :

1.	12.	$4. \frac{3}{8}.$	7. $\frac{17}{40}$ .	$10. \frac{7}{12}.$	. 13.	$16\frac{5}{8}$ .
2.	78.	5. $\frac{7}{16}$ .	8. 3.	11. <del>5</del> 7.	14.	$27\frac{12}{13}$ .
3.	$\frac{3}{4}$ .	$6. \frac{25}{32}.$	9. $\frac{5}{6}$ .	12. 4.	15.	$36\frac{23}{24}$ .

## 257. To reduce a decimal to a fraction.

Ex. Reduce .075 to an equivalent fraction.

	ANALYSIS.—A decimal is changed to a
OPERATION.	fraction by writing its denominator, and omit-
$075 = \frac{75}{1000} \div \frac{3}{40}$	ting the decimal point and prefixed ciphers.
	$\frac{75}{1000} = \frac{3}{40}$ (189).

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#### DECIMALS.

[Art. 257.

Ex. Change  $.83\frac{1}{3}$  to a simple fraction.

OPERATION.	ANALYSIS.—Reduce the
$.83\frac{1}{3} = \frac{83\frac{1}{3}}{100} = \frac{83\frac{1}{3} \times 3}{100 \times 3} = \frac{250}{300} = \frac{5}{6}$	complex fraction $\frac{83\frac{1}{3}}{100}$ to a
	simple fraction by multi-
ying both terms by the denominator 3.	(183, 3.)

258. RULE. — Omit the decimal point, supply the proper denominator, and reduce the fraction to its lowest terms.

#### EXAMPLES.

259. Reduce to equivalent fractions :

1.	.25.	8128.	15. $.33\frac{1}{3}$ .	22445.
2.	.75.	900144.	<i>16.</i> .41 <sup>2</sup> / <sub>3</sub> .	231428574.
3.	.375.	10512.	17066 <del>3</del> .	240833 <del>1</del> .
4.	.625.	115625.	1837 <del>1</del> .	25. 28.0375.
5.	.875.	121875.	19. $.104\frac{1}{6}$ .	26. 107.1663.
6.	.125.	$1312\frac{1}{2}.$	200972.	27. 175.096.
7.	.016.	14. $.16\frac{2}{3}$ .	210053 <del>4</del> .	286.0175.

## ADDITION OF DECIMALS.

**260.** Since decimals, like integers, increase and decrease uniformly according to a scale of ten, with the exception of placing the decimal point in the result (usually called *pointing off*), they may be *added*, *subtracted*, *multiplied*, and *divided* in the same manner as integers.

Ex. What is the sum of 28.7, 175.28, .037, 25.0045, and 4.08?

OPERATION.
28.7
175.28
.037
25.0045
4.08
233.1015

ANALYSIS.—Write the numbers so that units of the same order stand in the same column.

If the decimal points are in the same vertical line, tenths will necessarily be under tenths, hundredths under hundredths, etc. Add as in integers, and place the point in the result directly under the points of the numbers.

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Ex. Add .6, .37<sup>3</sup>/<sub>4</sub>, 16.048<sup>1</sup>/<sub>3</sub>, 8.1234<sup>2</sup>/<sub>4</sub>, and 24.125.

OPERATION.				
.6	=	.6		
$.37\frac{3}{4}$	=	.3775		
$16.048\frac{1}{3}$	=	$16.0483\frac{1}{3}$		
$8.1234_{7}^{2}$	=	$8.1234\frac{2}{7}$		
24.125	=	24.125		
		$49.2742\frac{13}{21}$		

ANALYSIS.—Reduce the complex decimals as far as the decimal places extend in the other numbers. Since the fractions, now express parts of the same fractional unit, they may be added.

In practice, the fractions may be rejected if the decimals are carried one place, at least, farther than accuracy is required.

**261.** RULE.—Write the numbers so that their decimal points are in the same vertical line. Add as in integers, and place the decimal point in the result directly under the points in the numbers added.

#### EXAMPLES.

**262.** 1. Add ninety-seven hundredths; three hundred forty-seven thousandths; sixteen, and seventy-five hundred-thousandths; four hundred seventy-five, and two thousand thirty-seven millionths.

2. Add four, and eighty-one thousandths; thirty-seven, and two hundred one ten-thousandths; seven thousand eight hundredthousandths; seven thousand, and eight hundred-thousandths; nineteen hundredths; three hundred sixty-four, and nine tenths; and fifty-six, and fifty-four thousandths.

3. Add three hundred seventy-five, and eight hundredths; eighteen thousandths; ninety-six, and eighty-four hundredths; four, and four tenths; and eight hundred seven ten-millionths.

4. What is the sum of 18 hundredths; 716 hundred-thousandths; 6342 millionths; 11567 ten-millionths; 625 ten-thousandths; 9 tenths; 99 hundredths; and 512 thousandths?

Add 81.86; 12.593; 4.004; 18.00129; .443; 400.043; .12875; 175.00175; 17.3008; 9000.0016; and .9016.

6. Find the sum of 99 ten-thousandths;  $157\frac{1}{2}$  thousandths;  $789\frac{3}{4}$  millionths; 6 tenths;  $18\frac{3}{4}$  hundredths; 1728 ten-millionths; and 88 hundredths.

7. Add \$1728.64;  $0.37\frac{1}{2}$ ;  $18.44\frac{1}{2}$ ;  $10.18\frac{3}{4}$ ; 6.25; and  $0.16\frac{1}{4}$ .

Art. 260.]

DECIMALS.

8. What is the sum of  $12.37\frac{1}{2}$ ;  $144.18\frac{3}{4}$ ;  $6.62\frac{1}{2}$ ;  $175.06\frac{1}{4}$ ;  $40.17\frac{1}{8}$ ; and 398?

9. Add .1263 $\frac{1}{3}$ ; 12.875; 187.25; 9.1414 $\frac{5}{6}$ ; .12; 5.7604 $\frac{7}{12}$ ; and .0008 $\frac{2}{3}$ .

10. Add  $.26\frac{1}{2}$ ;  $4.18\frac{3}{4}$ ;  $.0017\frac{2}{3}$ ;  $.00864\frac{1}{3}$ ;  $.04\frac{2}{5}$ ;  $17.387\frac{1}{3}$ ; and .0102075.

## SUBTRACTION OF DECIMALS.

263. Ex. From 12.75 subtract 8.125.

OFERATION.ANALYSIS.—Write the subtrahend under the minuend so12.75that units of the same order stand in the same column. Sub-<br/>tract as in integers, and place the point in the result directly<br/>under the points of the numbers.

4.020 If, as in this example, the minuend has not as many decimal places as the subtrahend, suppose decimal ciphers to be annexed until the right-hand figures are of the same order. (247, 1.)

Reduce complex decimals as in addition (260).

**264.** Ryle.—Write the numbers so that their decimal points are in the same vertical line. Subtract as in integers, and place the point in the remainder directly under the points in the minuend and subtrahend.

#### EXAMPLES.

265. 1. From four, and sixty-five thousandths, subtract eight hundred forty-seven ten-thousandths.

2. From twenty-seven hundredths take twenty-nine hundredthousandths.

3. From nine thousand, and thirty-four ten-thousandths, subtract nine thousand thirty-four ten-thousandths.

Find the difference between

- 4. 8.3644 and 7.8996.
- 5. 17.4586 and .785.
- 6. 1.010101 and .999999.
- 7. \$173.46 and \$87.29.
- 8. 3 and .873845.
- 9. 17.241 and 18.9731.
- 10. \$510.60 and \$389.451.
- 11. \$1728 and \$.063.

- 12. 17.8643 and 16.94.
- 13. 144.433 and 113.3875.
- 14. 54.375 and .983.
- 15. 117.483 and 49.435.
- 16. 448.9874 and 389.284.
- 17. 5556.84 and 44.48.
- 18. 968.444 and 37.3864.
- 19. 49.451 and 48.98761.

## MULTIPLICATION OF DECIMALS.

266. Ex. Multiply .144 by .12.

0PERATION. .144 .12 .01728 ANALVSIS.—.144 ×  $.12 = \frac{144}{1000} \times \frac{102}{1000} = \frac{1728}{10000}$ . Multiply the numerators of the two factors for the numerator of the product, as in multiplication of fractions. In the above multiplication of fractions, it will be observed that the number of ciphers in the denominator of the product equals the sum of the ciphers in the denominators of the two

factors. Since each cigher represents a decimal place, the product should have as many decimal places as both factors.

If the number of figures in the product is less than the number of decimal places in the two factors, supply the deficiency by prefixing ciphers.

**267.** RULE.—Multiply as in integers, and from the right point off as many decimal places in the product as there are decimal places in the two factors.

Note.—To multiply a decimal by 10, 100, 1000, etc., remove the decimal point as many places to the right as there are ciphers in the multiplier, annexing eiphers to the multiplicand, if necessary.

#### EXAMPLES.

268. 1. Multiply three hundred forty-four ten-thousandths by twelve thousandths.

2. Multiply one hundred ninety-two thousandths by four, and nineteen hundredths.

3. What is six hundredths of six hundred five millionths?

4. What is five hundredths of \$864.32? Of \$3645.75?

5. What is .0584 of 784.65? Of 943.25?

6. What is  $.99 \times 1.106 \times .25$ ?  $4.105 \times .625 \times .512$ ?

## Multiply

## Multiply

7. 8.716 by .39; by .047. 12. 17.28 by 163; by 2.551.

8. .00865 by .625; by 97.75. 13. 64.325 by 1.44%; by .06%.

9. .00128 by 8756.8; by 7.865. 14. 86.75 by 1.33; by 5.76.

10. 387.25 by  $.0147\frac{1}{4}$ ; by  $.087\frac{5}{4}$ . 15. 5.78 by .0885; by  $.66\frac{2}{3}$ .

11. 58.625 by .488 $\frac{2}{3}$ ; by .375. 16. 237.5 by .345 $\frac{1}{3}$ ; by 4.468 $\frac{1}{8}$ .

17. Multiply 1728 by .331; by .25; by .125; by .20.

18. Multiply .01837 by 1000; .00145 by 100000; .6874 by 100;
 5.375 by 10; 17.056 by 10000. Find the sum of the products.

## DIVISION OF DECIMALS.

## 269. Ex. Divide .01728 by 1.44.

FIRST OPERATION.	
1.44 ) .01728 ( .012	
144	
288	
<u>288</u> .	

ANALYSIS.—Dividing as in integers, without reference to the decimal points and prefixed ciphers, the quotient is 12. Since the dividend is the product of the divisor and quotient, it must contain as many decimal places as both of them. Hence the number of decimal places in the quotient must equal

the number in the dividend less the number in the divisor.

second operation. .012 1.44 ) .01'728 <u>144</u> 288 288 ANALYSIS.—Since multiplying both divisor and dividend by the same number does not affect the quotient, make the divisor a whole number by placing the point two places to the right (or imagine the point to be omitted), and place the point of the dividend the same number of places to the right. (Compare 3rd analysis, page 72). Indicate the new position of the point of the dividend by placing an index (') or pointer between the figures as in the operation.

1728 thousandths divided by 144 is 12 thousandths. Observe that the number of decimal places in the quotient is equal to the number in the dividend at the right of the pointer. In practice, place the point in the quotient when all the figures in the dividend at the left of the pointer have been divided. Notice in the operation that the point of the quotient is directly above the pointer of the dividend, and that each figure of the quotient is directly above the figure of the dividend which produced it.

**270.** RULE.—Divide as in integers, and point off from the right of the quotient as many decimal places as the number in the dividend exceeds the number in the divisor. Or,

Make the divisor a whole number, by placing the point to the right, and place the point of the dividend the same number of decimal places to the right. Divide as in integers, and place a decimal point in the quotient when the figures of the dividend have been used as far as the new position of the point in the dividend.

Nores.—1. If the number of figures in the quotient is less than the number of decimal places to be pointed off, supply the deficiency by prefixing ciphers.

2. If the divisor contains more decimal places than the dividend, before dividing make them equal by annexing ciphers to the dividend. If necessary to continue the division, more ciphers may be added.

3. If, after dividing all the figures of the dividend, there is a remainder, the division may be continued by annexing ciphers (247, 1). The ciphers thus annexed must be regarded as decimal places of the dividend.

4. To divide a decimal by 10, 100, 1000, etc., remove the decimal point as many places to the left as there are ciphers in the divisor, prefixing ciphers to the dividend, if necessary.

#### EXAMPLES.

271. 1. Divide three thousand four hundred fifty-six hundred-thousandths by seventy-two hundredths.

2. Divide six, and twenty-five hundredths by twenty-five thousandths.

Divide

Divide

3.	35.88 by .345; by 4.16.	80648 by .00425; by .0288.
4.	.89958 by .47; by .319.	931752 by .648; by .00384.
5.	12.6 by 14.4; by 125.	101898 by $.33\frac{1}{3}$ ; by $.0048\frac{2}{3}$ .
6.	96.3 by .20; by .25.	11. 85.2451 by $4.56\frac{5}{6}$ ; by $8.27\frac{1}{2}$ .
7.	5.27 by 1.24; by .85.	12. 45.367 by .0163; by 1.0804.

13. Divide 17.28 by .20; by .25; by .33<sup>1</sup>/<sub>3</sub>; by .125; by .66<sup>2</sup>/<sub>3</sub>.

14. 321 is .1781 of what number?

15. 186 is five hundredths of what number?

16. What must 37.375 be multiplied by to produce 448.5?

17. What must 631.25 be divided by to produce 250?

18. Divide 176.824 by 100; 876.35 by 1000; 17380.5 by 10000; 2886.57 by 10; 375 by 100000. Find the sum of the quotients.

Note.—To produce a result in hundredths or cents, the dividend must contain two decimal places more than the divisor; to produce thousandths, three places, etc.

Find the results of the following examples in hundredths, and reduce the fractional remainders, if any, to their lowest terms.

## Divide

19. \$12.52 by \$375.60; by \$100.16.

20. \$288 by \$1728; by \$720.

21. \$232.50 by \$3720; by \$3875.

22. \$60.40 by \$2416; by \$1812.

23. \$72 by \$3456; by \$9000.

24. \$212 by \$1484; by \$508.80.

Note.—When the quotient is dollars and cents, it is customary in business operations to omit the fraction if less than  $\frac{1}{2}$  cent, and add 1 to the cents if the fraction is more than  $\frac{1}{2}$  cent.

In the following examples, the results are carried to cents only and the fractions are omitted.

Divide

T 1	2 .		1	
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- 25. \$18.08 by .05; by .04.
- 26. \$648 by .06; by 13.
- 27. \$17.28 by .48; by 21.

28. \$720 by .031; by .07.
29. \$12.25 by .061; by .08.
30. \$960 by .003; by .27.

Divide approximately to thousandths

 31. 176.4 by 13; by .17.

 32. 229.48 by 50.72; by 57.

 33. 91.20 by 65; by 14.60.

34. 120.96 by 70; by 64.
35. 348.50 by 36; by .84.
36. 1728 by 12.16; by 17.5.

272. To find the value of goods sold by the hundred or thousand.

Ex. Find the cost of 864 pounds of meal at \$1.15 per hundred pounds (cwt.).

OPERATION.

8.64ANALYSIS.—864 pounds equal 8 hundred weight and<br/>.64 of a hundred weight. Hence the cost of 864 pounds<br/>equals 8.64 times \$1.15, or \$9.94.9504C. is the sign for hundred, and M. for thousand (10).

\$9.9360

**273.** RULE.—Reduce the quantity to hundreds by pointing two places at the right, or to thousands by pointing off three places. Multiply the price by this result and point off the product as in multiplication of decimals.

Note.—If preferable, multiply the price by the quantity as given, and point off two additional places if the price is per hundred, and three additional places if the price is per thousand.

274. 1. Find the cost of 500 pounds of feed at \$1.20 per cwt.
2. Find the cost of 4000 feet of boards at \$8.50 per thousand feet.

EXAMPLES.

3. Find the cost of 4375 feet of lumber at \$11 per thousand.

4. What is the cost of 13280 bricks at \$7 per thousand ?

Art. 274.]

5. Find the cost of 6500 cigars at \$48 per M.

6. What is the value of 640 pounds of hay at 85c. per cwt.?

7. Find the freight on 18480 pounds of merchandise at 62 cents per cwt.

8. What is the cost of 5967 *lbs.* meal at \$1.10 per *cwt.*, and 4880 *lbs.* bran at 75*c.* per *cwt.*?

9. Find the cost of 26728 lbs. of feed at \$1.05 per cwt.

10. Find the cost of 11760 feet joists at \$14 per thousand.

11. Find the cost of 2 cwt. of oatmeal at \$2.40 per cwt., and 3 cwt. of cracked wheat at \$3.84 per cwt.

12. What is the cost of 4 C. bolts at \$2.70, and  $\frac{1}{2}$  C. bolts at \$3.20?

13. Find the cost of insuring a house for \$4500 at 35c. per \$100.

14. Find the cost of 25 M. needles at \$1.55 per M.

15. Find the value of 13450 feet of scantling at \$18 per thousand.

16. What is the cost of  $7\frac{1}{2}$  M. envelopes at \$2.20 per M.?

17. Find the cost of 12400 shingles at \$16 per thousand.

## REVIEW EXAMPLES.

275. 1. Add 16 hundredths, 137 millionths, 48 ten-thousandths, and 2016 ten-millionths.

2. Add 16.07, 240.1273, 6.041, 27.1234.

3. Reduce  $\frac{13}{16}$  to a decimal.

- 4. From 175 take 16.0833.
- 5. What is \$ of \$175.75?
- 6. What is .33 of 187.5?
- 7. Divide 43.75 by .0125.
- 8. Divide .063 by 1.663.

15. \$3.75 is how many hundredths times \$75?

16. \$86.40 is how many hundredths of \$2592?

17. 16.56 is .05 of what number?

18. What will 17280 bricks cost at \$3.25 per M.?

19. If 278 barrels of pork cost \$4378.50, what is the cost of 100 barrels ?

20. Find the cost of 12456 feet of plank at \$8.75 per M.

21. What is the value of 5 bbls. sugar, containing 312, 304, 301, 305, 304 pounds respectively, at 93 cents per pound?

- 9. Change .8375 to a fraction.
- 10. Multiply 117.084 by 7.37%.
- 11. Reduce .0831 to a fraction.
- 12. From 375.13 take 198.888.
- 13. 1.75 is 3 of what number?
- 14. What is .331 times 1728?

22. Find the cost of  $13\frac{3}{4}$  pounds of crackers at  $15\frac{1}{2}$  cents per pound.

ANALYSIS.—Instead of multiplying by the method given in Art. 226, change one of the fractions to a decimal and then multiply. Thus,  $\$.15\frac{1}{2} =$  \$.155.  $13\frac{3}{4} \times \$.155 = \$2.131\frac{1}{4}$ , or \$2.13.

Multiply according to the above method

23.	\$3.17 <sup>1</sup> / <sub>2</sub> by 13 <sup>1</sup> / <sub>4</sub> ; by 19 <sup>1</sup> / <sub>2</sub> .	26.	$$4.12\frac{1}{4}$	by 261;	by 11 <sup>1</sup> / <sub>2</sub> .
24.	$\$.68\frac{3}{4}$ by $24\frac{1}{2}$ ; by $16\frac{1}{4}$ .	27.	$1.79\frac{1}{2}$	by 37 <sup>3</sup> / <sub>4</sub> ;	by 44 <sup>1</sup> / <sub>8</sub> .
25.	\$.88½ by 32¾; by 36½.	28.	$$1.37\frac{1}{2}$	by 18¼;	by $45\frac{1}{2}$ .

29. A merchant paid for merchandise during the year \$137618.75, and sold merchandise to the amount of \$146347.87. What was the gain, if the net market value of the merchandise remaining unsold was \$24378?

30. A quartermaster has \$8345 on hand, and receives \$4379.62 from each of six sales of property; he turns over to quartermaster A \$2875.28, and pays \$120 for corn. Upon being relieved from duty, he turns over to quartermaster B one-third of the residue, and divides the remainder equally among three others, C, D, and E. What was paid over to each?

31. Merchandise on hand, Jan. 1, 1879, \$46312.85; merchandise sold during the year, \$317829.32; merchandise purchased in the same time, \$301449.72; merchandise on hand, Dec. 31, 1879, \$61378.12. What was the net gain or loss?

32. A farmer sold land for \$22.50 an acre, as follows: to A, 98<sup>3</sup>/<sub>5</sub> acres; to B,  $\frac{3}{8}$  of the number sold to A; and to C,  $\frac{1}{2}$  the number sold to A and B both. How much land was sold, how much did B and C each receive, and what was the amount realized?

33. At \$28.75 per thousand, how many feet of lumber should be given for 2816 pounds of sugar at  $7\frac{3}{16}$  cts. per pound?

34. A man bequeaths  $\frac{1}{3}$  of his property to his wife,  $\frac{1}{4}$  to his son,  $\frac{1}{6}$  to his daughter, and the remainder, which is \$36375, to charitable institutions. What is the amount bequeathed to each, and the total amount?

35. A gentleman after spending  $\frac{1}{3}$  of all his money, and  $\frac{3}{4}$  of the remainder, had \$177.50 remaining; how much had he at first?

36. A merchant bought 100 yards of cloth at  $3.62\frac{1}{2}$  per yard, and  $87\frac{1}{2}$  yards at  $4.12\frac{1}{2}$  per yard. At what average price per yard should he sell the whole, to realize a profit equal to  $\frac{1}{5}$  of the cost?

37. If  $31\frac{1}{4}$  bushels of corn cost \$17.50, how many bushels can be bought for \$616?

## DENOMINATE NUMBERS.

276. A Denominate Number is a concrete number (145), and may be either *simple* or *compound*.

Denominate numbers are used to express divisions of time, weights, measures, and moneys of different countries.

The scale of integers and decimals is uniform ; that of most denominate numbers is varying.

The moneys of nearly all countries excepting Great Britain, and the metric system of weights and measures have a uniform decimal scale.

277. A Simple Denominate Number refers to units of the same name and value; as 7 inches, 4 pounds.

278. A Compound Denominate Number refers to units of different names, but of the same nature ; as 3 feet 6 inches, 4 pounds 8 ounces.

## REDUCTION OF DENOMINATE NUMBERS.

279. Reduction of Denominate Numbers is the process of changing their denomination without changing their value.

# 280. To reduce denominate numbers from higher to lower denominations.

Ex. How many pence in £8 16s. 7d.?

OPERATION.

£ 8. d. ANALYSIS.—Since there are twenty shillings in 1 pound, 8 16 7 in 8 pounds there are 8 times 20 shillings, or 160 shillings. (For convenience multiply by 20 as an abstract number.) 20 160 shillings plus 16 shillings equal 176 shillings. Since 160s. there are 12 pence in 1 shilling, in 176 shillings there are 16s. 176 times 12 pence, or 2112 pence. 2112 pence plus 7 pence equal 2119 pence. When possible, add mentally 176s. the number of the lower denomination to the product, as 12 in the last step of this operation.

2119d.

**281.** RULE.—Multiply the number of the highest denomination given by the number of the next lower denomination required to make 1 of this higher, and to the product add the given number, if any, of such lower denomination.

Treat this result, and the successive results obtained, in like manner until the number is reduced to the required denomination.

### EXAMPLES.

	<b>282.</b> Reduce	Reduce
1.	£9 13s. 10d. to pence.	13. 8 bu. 3 pk. 6 qt. to pints.
2.	6 gal. 3 qt. 1 pt. to gills.	14. 13 gal. 3 qt. 1 pt. to pints.
3.	£112 18s. 5d. to farthings.	15. 1 mi. 32 rd. 10 ft. to inches.
4.	6 T. 12 cwt. 65 lb. to pounds.	16. 29 sq. rd. to square feet.
5.	8 mo. 16 da. to days.	17. 97 sq. rd. to square yards.
6.	£75 17s. 7d. to pence.	18. 5 sq. mi. to acres.
7.	£245 15s. 3 far. to farthings.	. 19. 11 mo. 24 da. to days.
8.	48 bu. 3 pk. 6 qt. to quarts.	20. 16 cords 112 cu. ft. to cu. ft.
9.	7 T. 9 cwt. 48 lb. to pounds.	21. £178 13s. 9d. to pence.
10.	18 lb. 8 oz. to pennyweights.	22. 2 yr. 8 mo. 22 da. to days.
11.	5 mi. 36 rd. 11 ft. to feet.	23. 13 T. 17 cwt. 82 lb. to pounds.
12.	456 miles to feet.	24. £31 11s. 11d. to pence.

283. To reduce denominate numbers from lower to higher denominations.

Ex. Reduce 2119 pence to higher denominations.

12	) 2119d.
20	) $176s. + 7d.$
	£8 +16s.

 $2119d = \pounds 8 \ 16s, \ 7d.$ 

OPERATION.

ANALYSIS.—Since there are 12 pence in 1 shilling, in 2119 pence there are as many shillings as 12 pence are contained times in 2119 pence, or 176 shillings, and 7 pence remaining. Since there are 20 shillings in 1 pound, in 176 shillings there are as many pounds as 20 shillings are contained times in 176 shillings, or 8 pounds, and 16

shillings remaining. Therefore,  $2119d. = \pounds 8$  16s. 7d.

**284.** RULE.—Divide the given number by the number of that denomination required to make 1 of the next higher, reserving the remainder, if any, as part of the answer.

Treat the quotient, and the successive quotients obtained, in like manner until the number is reduced to the required denomination. The last quotient and the several remainders will form the answer.

## EXAMPLES.

## 285. Reduce

- 1. 8475d. to pounds.
- 2. 9683 cu. ft. to cords.
- 3. 7534 pts. to bushels.
- 4. 9817 pts. to gallons.
- 5. 987 in. to yards.
- 6. 216 da. to months.
- 7. 875 rods to miles.
- 8. 6375 hrs. to weeks.
- 9. 9537 sec. to hours.
- 10. 6239 in. to yards.

Reduce

- 11. 13387d. to pounds.
- 12. 987 ft. to yards.
- 13. 17416 lbs. to tons.
- 14. 1809 in. to yards.
- 15. 4711 pts. to bushels.
- 16. 8370d. to pounds.
- 17. 5316 sq. rds. to acres.
- 18. 7418 oz. to cwt.
- 19. 8716 cu. ft. to cords.
- 20. 4829d. to pounds.

## REDUCTION OF DENOMINATE FRACTIONS.

**286.** A Denominate Fraction is a fraction whose integral unit is a denominate number.

The principles, analyses, and rules of denominate fractions are essentially the same as those of denominate integers; therefore, no special rules are necessary for their reduction. A sufficient number of illustrative examples are given to fully explain the different cases that may arise.

## 287. To reduce denominate fractions from higher to lower denominations.

Ex. Reduce  $\frac{7}{16}$  of a £ to pence.

OPERATIONS.

$$\frac{7}{14} \times \frac{5}{1} = \frac{35}{4}s.$$
$$\frac{35}{4} \times \frac{3}{1} = 105d.$$

Or, 
$$\frac{1}{\frac{1}{4}} \times \frac{5}{1} \times \frac{5}{1} \times \frac{3}{1} = 105d$$

ANALYSIS.—Since there are 20 shillings in £1, in  $\frac{7}{18}$  of a £ there are  $\frac{7}{18}$  of 20 shillings, or  $\frac{35}{4}$  shillings. Since there are 12 pence in 1 shilling, in  $\frac{35}{4}$  shillings there are  $\frac{35}{4}$  times 12 pence, or 105 pence. Or, multiply the given fraction by the numbers of the scale required to reduce its denomination to the required denomination.

Ex. Reduce  $\frac{7}{16}$  of a £ to shillings and pence.

 $\begin{aligned} \frac{7}{16} \times \frac{88}{1} &= \frac{5}{4} = 8\frac{3}{4}s. \\ \frac{3}{4} \times \frac{3}{16} &= 9d. \\ \pounds \frac{7}{16} &= 8s. 9d. \end{aligned}$ 

ANALYSIS.—Multiplying by 20,  $\pounds_{16}^{2} = 8\frac{3}{4}$ shillings. Reserve the integral part of the result, and reduce the fractional part to pence. Multiplying by 12,  $\frac{3}{4}$  shilling = 9 pence. Hence,  $\pounds_{14}^{2} = 8s$ . 9d.

#### EXAMPLES.

**288.** 1. Reduce  $\frac{9}{16}$  of a £ to pence.

2. Reduce  $\frac{11}{16}$  of a £ to integers of lower denominations.

3. Reduce  $\frac{3}{5}$  of a mile to feet.

4. Change  $\frac{31}{125}$  of a ton to pounds.

5. Reduce  $\frac{37}{4}$  of a £ to shillings and pence.

6. Change  $\frac{13}{64}$  of a bushel to pints.

7. Reduce  $\frac{23}{3}$  of a mile to feet.

8. Reduce  $\frac{1}{3}$  of a hundred-weight to integers of lower denominations.

9. Reduce  $\frac{11}{16}$  of a gallon to pints.

10. Change 13 of a cord to cubic feet.

## 289. To reduce denominate decimals from higher to lower denominations.

Ex. Reduce .4375 of a £ to pence.

OPERATION.

£.4375

 $\begin{array}{c} \underline{20} \\ \underline{20} \\ 8.7500s. \end{array} \begin{array}{c} \text{Analysis.} \\ \underline{5100s} \\ 12 \end{array} \begin{array}{c} \text{Analysis.} \\ \underline{5100s} \\ \underline{5100s} \\ \underline{510s} \\ \underline{5$ 

105.0000d.

Ex. Reduce .4375 of a £ to integers of lower denominations.

OPERATION.

s. 8

90	ANALYSIS Multiplying by 20, £.4375 = 8.75 shil-
~~~~	lings. Reserve the integral part of the result, and reduce
.7500	the decimal part to pence. Multiplying by 12, .75 shilling
12	= 9 pence. Hence, $\pounds.4375 = 8s. 9d.$

d. 9|.0000

#### EXAMPLES.

**290.** 1. Reduce .625 of a £ to pence.

2. Reduce .875 of a £ to shillings and pence.

3. Reduce .6375 of a £ to pence.

4. Reduce .6825 of a  $\pounds$  to shillings and pence.

5. Change 2.3331 yrs. to integers of lower denominations.

6. Change £16.467 to integers of lower denominations.

7. If 1 pound sterling can be bought for \$4.87, how many pounds can be bought for \$1000?

8. Reduce 2.417 yr. to integers of lower denominations.

9. Reduce £15.3375 to integers of lower denominations.

10. A certain sum at a certain rate will in 1 yr. produce \$60 interest; in what time will the same sum at the same rate produce \$15.50 interest?

## 291. To reduce denominate numbers to fractions of higher denominations.

Ex. Reduce  $\frac{3}{2}$  of a penny to the fraction of a  $\pounds$ .

OPERATIONS.  $\frac{3}{5} \div 12 = \frac{1}{20} s.$   $\frac{1}{20} \div 20 = \frac{1}{400} \pounds.$  ANALYSIS.—Divide the given fraction by the numbers of the scale required to reduce pence to pounds.

Or,  $\frac{3}{5} \times \frac{1}{12} \times \frac{1}{20} = \frac{1}{400} \pounds$ .

If the answer is required in the form of a decimal, reduce the resulting fraction to a decimal by Art. **254**.  $\pounds_{4\overline{100}} = \pounds.0025$ .

Ex. Change 9 pence to a fraction of a  $\pounds$ .

ANALYSIS.—For first operation, as in previous example.

OPERATIONS.

Or, since there are 240 pence in £1, 1 penny equals  $\frac{1}{240}$  of a £, and 9 pence equal  $\frac{9}{240}$  or  $\frac{9}{20}$  of a £.

Ex. Reduce 12s. 9d. to the fraction of a  $\pounds$ .

OPERATION.

12s. 9d. = 153d.	ANALYSIS.—12 shillings 9 pence = $153$ pence.
f1 - 240d	Since $\pounds 1 = 240$ pence, 1 penny equals $\frac{1}{240}$ of a $\pounds$ ,
153 - 51.0	and 153 pence equal $\frac{158}{240}$ , or $\frac{51}{80}$ of a £.
$\frac{240}{240} = \frac{30}{80} \mathcal{L}.$	

#### EXAMPLES.

292. 1. Reduce § of a penny to the fraction of a pound.

2. Reduce 420 grains to the fraction of an ounce Troy.

- 3. Change 275 feet to the fraction of a mile.
- 4. Reduce 491 feet to the fraction of a mile.
- 5. Reduce 16s. 10d. to the fraction of a pound.
- 6. Reduce 3s. 6d. to the fraction of a pound.
- 7. Reduce 6 mo. 20 da. to the fraction of a year.
- 8. Reduce 84 pounds to the fraction of long ton (2240 pounds).
- 9. Reduce 3 qt. 1 pt. to the fraction of a bushel.
- 10. Reduce 16s. 8d. to the fraction of a pound.

293. To reduce denominate numbers to decimals of higher denominations.

Ex. Reduce .6 of a penny to the decimal of a £.

OPERATION.ANALYSIS.—Divide the given decimal by the num-12).6d.bers of the scale required to reduce pence to pounds.20).05 s.If the answer is required in the form of a fraction, $\pounds.0025$  $\pounds.0025 = \pounds_{400}^{-1}$ .

Ex. Reduce 9 pence to the decimal of a £.

OPERATIONS.	ANALYSIS.—For first operation, as in
12)9. d.	previous example.
20).75 8.	Or, since there are 240 pence in £1, 1 penny equals $\pm 1_{-}$ of a £, and 9 pence
.0375 £.	equal $\frac{9}{240}$ , or $\frac{3}{50}$ of a £. $\pounds \frac{3}{50} = \pounds.0375$
0.0 0.0000	(254)

Or,  $\pounds_{\frac{9}{240}} = \pounds_{\frac{3}{80}} = \pounds.0375.$ 

Ex. Reduce £18 12s. 9d. to the decimal of a £.

OPERATION.										
12	)	9.		d.						
20	)	12.	75	8.						
	£	18.	63	75						

ANALYSIS.—Write the denominations given in a vertical column, the lowest denomination at the top. Since there are 12 pence in 1 shilling, 9 pence are equal to .75 shilling; to which annexing the 12 shillings given we have 12.75 shillings. Since there are 20 shillings in £1, 12.75 shillings are equal to £.6375, to

which annexing the £18, we have £18.6375. Hence £18 12s. 9d. = £18.6375.

### EXAMPLES.

294. 1. Reduce .875 of a shilling to pounds.

2. Change 12 cwt. to the decimal of a ton.

- 3. What decimal of a £ are 18s. 6d.?
- 4. Reduce £14 15s. 9d. to the decimal of a pound.

5. Reduce 116 cu. ft. to the decimal of a cord.

6. Reduce £247 14s. 9d. to pounds.

7. What decimal of an acre are 64 sq. rds.?

8. Reduce £27 10s. 6d. to pounds.

9. What is the cost of 16 tons 12 cwt. of "Nut" coal at \$6.80 per ton, and 8 tons 16 cwt. of "Chestnut" coal at \$6.10 per ton?

10. If 1 pound is equivalent to  $4.87_4^3$ , what is the value of £123 16s. 9d. in U. S. money?

11. Reduce £25 12s. 6d. to the decimal of a £, multiply the result by .03, and reduce the resulting decimal to shillings and pence.

[Art. 293.

## ADDITION OF DENOMINATE NUMBERS.

**295.** Denominate numbers are *added*, *subtracted*, *multiplied*, and *divided* by the same general methods as are employed for like operations in abstract numbers. The only difference arises from the use of a *varying* scale instead of the uniform scale of 10.

Ex. Add £5 11s. 4d., £7 14s. 9d., £6 16s. 8d., and £7 5s. 9d. OPERATION. · ANALYSIS .- Write the numbers so that like denomina-£ 8. d. tions stand in the same column, and begin to add at the right. 5 11 4 The sum of the pence is 30d. = 2s. 6d. Write the 6d. under the column of pence, and add the 2s. to the column of shil-7 14 9 lings, obtaining for the sum  $48s = \pounds 2$  8s. Write the 8s. 6 16 8 under the column of shillings, and add the £2 to the column 7 5 9 of pounds, obtaining for the sum £27; which write under the column of pounds, producing the entire sum, £278s. 6d. 27 8 6

#### EXAMPLES.

**296.** 1. Add £16 5s. 4d., £12 8s. 9d., £13 14s. 8d., £42 0s. 7d., and 18s. 6d.

2. Add 3 T. 19 cwt. 46 lb., 4 T. 13 cwt. 14 lb., 18 T. 13 cut, 24 lb., and 42 T. 8 cwt. 82 lb.

3. Add £163 16s. 11d., £52 8s. 6d., £3 14s. 2d., £84 12s. 11d., £106 1s. 4d., and £49 13s. 8d.

4. Add 1 yr. 6 mo. 10 da., 3 yr. 8 mo. 24 da., 4 yr. 11 mo. 16 da., 3 mo. 18 da., and 1 yr. 8 mo. 8 da.

5. Add 8 cd. 106 cu. ft., 3 cd. 85 cu. ft., and 2 cd. 113 cu. ft.

Add 16 hr. 43 min. 48 sec., 3 hr. 12 min. 40 sec., 1 hr. 49 min.
 13 sec., and 5 hr. 19 sec.

7. Add 4 bu. 3 pk. 6 qt. 1 pt., 10 bu. 2 pk. 7 qt. 1 pt., 11 bu. 3 pk. 1 qt. 1 pt., 9 bu. 2 pk. 5 qt. 1 pt.

8. 7 yd. 2 ft. 10 in., 2 yd. 1 ft. 9 in., 8 yd. 1 ft. 8 in., 6 yd. 4 in., 1 yd. 2 ft. 9 in.

9. Add 1 lb. 11 oz. 18 pwt. 14 gr., 2 lb. 8 oz. 10 pwt., 4 lb. 5 oz. 18 gr., and 10 oz. 13 pwt. 12 gr.

10. Add 16 gal. 3 qt. 1 pt., 45 gal. 2 qt., 17 gal. 1 qt. 1 pt., 4 gal. 3 qt., 15 gal. 1 pt., and 24 gal. 3 qt. 1 pt.

11. Add £17 16s. 8d., £37 13s. 5d., £46 7d., £11 5s. 10d., £8 4s., £38 19s. 3d., and £45 12s. 8d.

12. Add £175 14s. 9d., £37 9s. 3d., £5 10s. 9d., 17s. 3d., £55 17s., £3 6s. 9d., £44 18s. 5d., £218 15s. 6d., and £3 11s. 11d.

## SUBTRACTION OF DENOMINATE NUMBERS.

#### From £10 6s. 4d. take £8 15s. 3d. Ex. 297.

OPERATION. ANALYSIS.-Write the numbers so that like denomina-£ 8. d. tions stand in the same column, and begin to subtract at the 10 6 4 right. 3d. from 4d. leaves 1d., which write under the col-8 15 3 umn of pence. Since 15s. cannot be subtracted from 6s., take  $\pounds 1 = 20s$ , from  $\pounds 10$ , leaving  $\pounds 9$ , and add it to the 6s. 1 11 1 making 26s. 15s. from 26s. leaves 11s., which write under

the column of shillings. £8 from £9 leaves £1, which write under the column of pounds. Hence the difference required is £1 11s. 1d.

### EXAMPLES.

298. 1. From £175 16s. 8d. take £87 12s. 6d.

2. From £84 10s. 2d. take £63 5s. 10d.

3. From £16 6s. 11d. take £12 12s. 8d.

4. From £48 10s. 8d. take £24 16s. 10d.

5. From 16 yr. 8 mo. 10 da. subtract 12 yr. 5 mo. 8 da.

6. From 80 yr. 10 mo. 16 da. take 76 yr. 5 mo. 24 da.

7. From 81 yr. 4 mo. 25 da. take 80 yr. 10 mo. 15 da.

8. From 82 yr. 3 mo. 20 da. take 79 yr. 8 mo. 26 da.

## MULTIPLICATION OF DENOMINATE NUMBERS.

Multiply £7 16s. 8d. by 11. 299. Ex.

ANALYSIS.—11 times 8d. are 88d. = 7s. 4. Write the OPERATION. 8. d. 4d. under the pence, and add the 7s. to the product of shil-16 - 8 lings. 11 times 16s. are 176s., plus 7s. from the preceding product are  $183s. = \pounds 9$  3s. Write the 3s. under the shil-11 lings, and add the £9 to the product of pounds. 11 times 3 4 £7 are £77, plus £9 from the preceding product are £86,

which write under the pounds. Hence the entire product is £86 3s. 4d.

Ex. Multiply £8 12s. 6d. by .05.

ANALYSIS.-Reduce the multiplicand to the decimal of a pound by Art. 293, perform the required multiplication, and reduce the result to shillings and pence by Art. 289.

£8 12s. 6d. = £8.625. £8.625 × .05 = £.43125. £.43125 = 8s. 7.5d.

Or, reduce the multiplicand to pence by Art. 281, perform the required multiplication, and reduce the result to shillings and pounds by Art. 284.

£8 12s, 6d = 2070d. 2070d.  $\times .05 = 103.5d$ . 103.5d = 8s. 7.5d.

£

7

86

### EXAMPLES.

**300.** *1.* Multiply £17 10s. 8d. by 7; by 9; by 11; by 15. 2. How many cords of wood in 12 loads, each load containing 2 cd. 108 cu. ft.?

3. What is the cost of 25 yd. of silk, at £1 2s. 6d. per yd.?

4. Find the weight of 24 spoons, each spoon weighing 1 oz. 13 pwt.

5. Multiply 1 hr. 38 min. 22 sec. by 10; by 12; by 15; by 18.

6. If 15 men perform a certain piece of work in 3 da. 16 hr. 52 min., how long would it take one man to perform it?

7. What will 50 gal. of wine cost at 8s. 3d. per gallon?

8. What is .05 of £127 16s. 6d.? Of £145 15s. 9d.?

9. Multiply £138 8s. 9d. by .021; by .04; by .06; by .07.

## DIVISION OF DENOMINATE NUMBERS.

**301.** Ex. If 6 yds. of cloth are worth £8 18s. 6d., what is 1 yd. worth?

ANALYSIS.—1 yd. is worth 1 sixth as much as 6 yd.  $\frac{1}{6}$  of £8 is £1 and £2 remaining. Write the £1 in the quotient, and reduce the £2 to shillings. £2=40s., plus 18s. in the dividend = 58s.  $\frac{1}{6}$  of 58s. is 9s. and 4s. remaining. Write the 9s. in the quotient, and reduce the

4s. to pence. 4s. = 48d., plus 6d. in the dividend = 54d.  $\frac{1}{6}$  of 54d. is 9d., which write in the quotient. £1 9s. 9d. is the quotient required.

Note.—When the divisor is a denominate number, as in Ex. 2, reduce both divisor and dividend to the same denomination, and divide as in simple numbers.

## EXAMPLES.

**302.** 1. Divide £13 12s. 3d. by 11; by 9; by 33.

2. How many yards of muslin at 7*d*. per yard can be bought for £5 12s.? For £9 9s.? For £10 5s. 4*d*.? (See note.)

3. How many yards of silk at £1 19s. 2d. per yard can be purchased for £86 3s. 4d.? (See note.)

4. Divide 85° 18' 30" by 12; by 15; by 18; by 27.

5. Divide 322 A. 90 sq. rd. by 8; by 10; by 13; by 16.

6. If 42 yd. of cloth cost £20 16s. 6d., what is the price of 1 yd.? Of 12 yd.? Of 20 yd.? Of 37 yd.?

7. Divide 17s. 3d. by .02½; by .04; by .05; by .09; by .15.

Reduce the dividend to the decimal of a pound or shilling, divide in the asual manner, and reduce the quotient to pounds, shillings, and pence.

## DIVISIONS OF TIME.

**303.** The natural divisions of time are the *year* and the *day*, the other divisions being artificial.

The year is the time in which the earth makes one revolution around the sun. The day is the time in which the earth makes one revolution on its axis.

TADTE

			LADIE.	
60	Seconds (sec.)	=	1 Minute min	2.
60	Minutes	=	1 Hour	r.
24	Hours	=	1 Day	ı.
7	Days	=	1 Week	Ċ.
365	Days,			
52	Weeks, 1 day, or }	- ==	1 Common Year yr	•
12	Calendar Months)			
366	Days	=	1 Leap Year yr	•.
100	Years	=	1 Century	γ.

Note.—In many business transactions the year is regarded as 360 days, or 12 months of 30 days each.

**304.** The Solar Day is the interval between two consecutive returns of the sun to the meridian.

On account of the varying motion of the earth around the sun, the solar days are of unequal length. For civil purposes in measuring time, the average of all the days in the year is taken as the unit.

**305.** The Solar Year is the time between two consecutive returns of the sun to the vernal equinox. Its exact length is  $365 \ da. 5 \ hr. 48 \ min. 50 \ sec.$  in mean solar time. For civil purposes, the year consists of  $365 \ or 366 \ days.$ 

In the calendar established by Julius Cæsar, B.C. 46, and thence called the Julian calendar, three successive years were made to consist of 365 days each; and the fourth, of 366 days. According to the Julian calendar, the average length of the year was 365<sup>1</sup>/<sub>4</sub> days, thus making an error of 11 min. 10 sec. each year ; which in 400 years would amount to 73 hours, or about 3 days. In the sixteenth century, in consequence of the excess of the Julian year above the true solar year, the error in the calendar was 10 days. To correct the calendar, and to prevent any error in the future, Pope Gregory XIII. decreed that 10 days should be omitted in the month of October, 1582, and that all centennial years not divisible by 400 should be common years. This calendar is sometimes called the Gregorian calendar. It is now used in all civilized countries except Russia.

[Art. 303.

5.] DIVISIONS OF TIME

The Julian and Gregorian calendars are also designated by the terms Gld, Style and New Style. In consequence of the years 1700 and 1809 being common years by the Gregorian calendar, the difference between the two styles is now 12 days. Thus, when it is July 4 in Russia, it is July 16 in other countries.

**306.** RULE FOR LEAP YEARS.—All years divisible by 4, except centennial years, are leap years.

All centennial years divisible by 400 are leap years.

**307.** The Calendar Months, with the number of days they contain, are as follows:

Season.			Days.	Season.			Days.
	(1.	January (Jan.)	31.		6.	June	30.
WINTER.	{ 2.	February (Feb.)	28.	SUMMER	{ 7.	July	31.
	l	" in leap yea	r 29.		L 8.	August (Aug.)	31.
	( 3.	March (Mar.)	31.		( 9.	September (Sep.	) 30.
SPRING.	{ 4.	April (Apr.)	30.	AUTUMN.	10.	October (Oct.)	31.
	5.	May	31.		11.	November (Nov.	) 30.
				WINTER.	12.	December (Dec.)	31.

The number of days in each month may be easily remembered from the following lines :

"Thirty days hath September, April, June, and November; February twenty-eight alone, All the rest have thirty-one; Except in Leap year, then is the time When February has twenty-nine."

### EXAMPLES ...

**308.** 1. Reduce 2 wk. 4 da. 16 hr. 40 min. to minutes.

2. How many days in 7 mo. 22 da.?

3. Reduce 2.375 years to years, months, and days.

4. If a person's income is \$1000 per day, how much is that per minute?

5. From 88 yr. 8 mo. 10 da. subtract 86 yr. 5 mo. 24 da.

6. Multiply 3 hr. 24 min. 32 sec. by 15.

7. How many leap years from 1886 to 1897? From 1795 to 1827? From 1887 to 1903?

8. How long from 14 min. 40 sec. past 9 A. M. to 37 min. 30 sec. past 5 P. M.?

9. Reduce 100000 sec. to higher denominations.

10. Find the value of  $76\frac{1}{2}$  hours of labor at \$3.50 per day of 8 hours.

Art. 305.]

[Art. 309.

## 309. To find the interval of time between two dates.

310. There are two riethods in common use for finding the time between two dates: 1, by compound subtraction, in which the result is given in years, months, and days, and in which 12 months are considered a year, and 30 days a month : 2, the result is given in days, or in years and days, and the true number of days is taken for each month.

Ex. Find the time in months and days from Apr. 24 to Nov. 10.

OPERATION. ANALYSIS .- Represent the months and days by their nummo. da. bers and find their difference by compound subtraction (297). 11 -10writing the later date as the minuend and the earlier as the subtrahend. 4 24

In many examples the interval may be found mentally as 16 6 follows : From Apr. 24 to Oct. 24 are 6 mo.; in Oct. there are 6 more days after the 24th (regarding each month as 30 days), and in November to Nov. 10th inclusive, there are 10 days. Hence the total time between the given dates is 6 mo. 16 da.

The above methods may be used for finding the exact interval in days by making the necessary corrections, 6 mo. 16  $da_{\star} = 196 da_{\star}$  From Apr. 24 to Nov. 10, there are 4 months containing 31 da. each ; hence the true answer is  $196 \, da. + 4 \, da., \, \text{or } 200 \, da.$ 

Note.-When the month of February is included, subtract 2 days in a common year, and 1 day in a leap year.

Ex. Find the time from May 18, 1884, to Mar. 2, 1896.

OP	ERATIO	DN.				
yr.	mo.	da.				
90	3	2	A A			
84	5	18	ANALYSIS.—AS	m	preceaing	example
5	9	14				

Ex. What is the exact number of days from July 20, 1888, to Nov. 10, 1889?

	OPERATION.	ANALYSIS.—In finding
365	from July 20, 1888, to July 20, 1889.	the interval between two
11	remaining in July.	dates the last day is count-
31	in August.	ed, and not the first. Since
30	in September.	the time is more than one
31	in October	year, write down 365 days
10	in November	the first date to the same
	in November.	date of the next year. Next
478	from July 20, 1888, to Nov. 10, 1889.	write down the number of

interval between two s the last day is countnd not the first. Since ime is more than one , write down 365 days e number of days from first date to the same of the next year. Next e down the number of days in the month of July after the 20th, then the number of days in each

of the full calendar months, and finally the number of days in November to Nov. 10 inclusive. The sum of these numbers will be the required time.

In solving examples by this method, the student should remember that the first quarter contains 90 days, the second quarter, 91 days, the third quarter, 92 days, and the last quarter, 92 days; the first six months, 181 days, and the last six months, 184 days.

### EXAMPLES.

**311.** Find the time by compound subtraction from

1. Jan. 10 to Aug. 28.

2. Mar. 16 to Dec. 4.

3. Feb. 5, 1886, to Oct. 16, 1887.

4. Jan. 27, 1885, to July 4, 1887.

5. May 16, 1886, to Mar. 24, 1887.

6. June 28, 1885, to Apr. 10, 1886.

7. July 30, 1886, to May 12, 1887.

8. Aug. 16, 1887, to Jan. 1, 1888.

Find also the exact number of days between the above dates.

9. How many days from Jan. 1, 1888, to Jan. 1, 1906?

10. Ninety days after June 21 is what date?

	OPE	RATIONS.	1	ANALYSIS.—Subtract from the given
90		Or, 9	June.	number of days, the number of days re-
9	June.	31	July.	maining in June, and from this remainder,
01		31	Ang	subtract successively the number of days
81			mug.	in the following months until the remain-
31	July.	71		der is equal to or less than the number of
50		90		days in the next following month. The
01		10	G 1	last remainder represents the required
31	Aug.	19	Sept.	date.
10	Sant			Or write the remaining number of

Or, write the remaining number of days in June, and the number of days

in a sufficient number of months to produce about the given number of days. Take their sum and subtract it (if possible) from the given number of days. The remainder will be the day of the following month representing the required date. If the sum is greater than the given number, subtract the excess from the number of days in the last month written. The remainder will be the required date.

If the time be 30, 60, or 90 days, regard each 30 days as a calendar month, and correct by subtracting 1 day for each intervening month containing 31 days, and adding 2 days for February (in leap year 1 day). Thus 3 months after June 21 is Sept. 21, and by subtracting 2 days for July and August, the correct result is Sept. 19.

11. 63 days after Oct. 4 is what date? 12. 90 days after Mar. 24 is what date?

## LINEAR MEASURES.

**312.** Linear or Long Measure is used in measuring distances; also the length, breadth, and height of bodies, or their linear dimensions.

In measuring length, the yard derived from the standard yard of England is the standard unit, the yards of the United States and England being identical. Theoretically, the yard is equal to  $\frac{3}{5} \frac{6}{1} \frac{1}{100} \frac{1}{100}$  of the length of a pendulum that vibrates seconds in a vacuum, at the level of the sea, in the latitude of London; that is, a pendulum that vibrates seconds under the above conditions is 39.1393 inches in length. The standard yard is, in fact, the distance between two points on a brass bar, preserved at Washington, the distance to be taken when the bar is at a temperature of 62° Fahrenheit.

#### TABLE.

								mi.	rd.		yd.		ft.		in.
12	Inches	(in.,'') =	1	Foot	•	•.	ft.,'.	1 :	= 320	=	1760	=	5280	=	63360
3	Feet	=	1	Yard			yd.		1	==	5	=	16	1=	198
$5\frac{1}{2}$	Yards	=	1	Rod			rd.				1	=	3	=	- 36
320	Rods	=	1	Mile			mi.						1	_	12

Notes.—1. The inch is usually divided into halves, quarters, eighths, and sixteenths.

2. The foot and inch are divided by civil engineers and others into tenths, hundredths, thousandths, etc.

3. In measuring cloth, ribbon, and other goods sold by the yard, the yard is divided into halves, quarters, eighths, and sixteenths.

4. At the U. S. Custom Houses, the yard is divided into tenths and hundredths.

5. The mile (5280 *ft.*) of the above table is the legal mile of the United States and England, and hence it is sometimes called the statute mile.

6. 1 furlong =  $\frac{1}{8}$  mile = 40 rods. (Rarely used.)

## 313. The following denominations are also used :

	1 Size	=	$\frac{1}{3}$ Inch. Used by shoemakers.							
	1 Hand	=	4 Inches. Used in measuring the height of horses.							
	1 Fathom	=	6 Feet. Used in measuring depths a, sea.							
	1 Cable-length	=	120 Fathoms, or 240 yards.							
	1 Geographic Mile	=	1.15 + Statute Miles. Used in measuring distances							
	at sea.									
	1 Knot	=	1 Geo. Mile. Used in determining the speed of vessels.							
6	0 Geo. Miles, or }	_	1 Degree f of latitude on a meridian, or of longitude							
6	9.16 Stat. Miles ∫	=	on the equator.							
6	0 Degrees		the Circumference of the Earth.							

3

314. Surveyors' Linear Measure is used in measuring land, roads, etc.

The unit of this measure is a chain, 4 rods or 66 feet in length, called Gunter's Chain. It is divided into 100 parts called *links*, each link being 7.92 inches in length.

## TABLE.

						mi		ch.		ft.		г.		in.
100 L	inks (l.)	= 1	Chain	•	ch.	1	=	80	=	5280	=	8000	=	63360
80 C	hains	= 1	Mile		mi.			1	=	66	=	100	=	792
										.66	=	1	=	7.92

Notes.-1. Links are written decimally as hundredths of a chain.

2. For railroad and other purposes, engineers use a chain or tape 100 feet long, the feet being divided into tenths.

3. 1 rod = 25 links.

#### EXAMPLES.

**315.** 1. Add 9 ft. 8 in., 12 ft. 6 in., 16 ft. 5 in., 15 ft. 11 in., 21 ft. 4 in., 17 ft. 3 in.

2. In  $\frac{5}{8}$  of a yard, how many inches?

3. How many feet in 17 miles? In 35 rods?

4. Find the difference between 5 ft.  $4\frac{1}{2}$  in. and  $16\frac{1}{2}$  hands.

5. Reduce 49175 ft. to higher denominations.

6. Reduce 32 rd. 4 yd. 2 ft. 10 in. to inches.

7. How many feet in  $\frac{1}{8}$  of a mile?

8. In 4376 feet, how many chains? How many inches?

9. In 396 rods, how many chains? How many feet?

10. In 37.56 chains, how many feet? How many rods?

11. Children's size 1 of shoemakers' measure is  $4\frac{1}{6}$  inches long; what is the length of boys' size 8, youths' size 1, and men's size 10? (Size 1 of the second series is one size longer than size 13 of the first series.)

12. How many fathoms in 1722 ft.?. In 3136 ft.?

13. Reduce 48276 ft. to higher denominations.

14. Add 4.16 ch., 3.75 ch., 8.08 ch., 17.28 ch., 46.10 ch., and 38.09 ch.

15. How much will it cost at \$3.25 per rod to fence a field whose sides are 808 ft., 975 ft., 822 ft., and 992 ft. respectively?

16. How many posts placed 8 ft. apart will be required to fence a railroad 14 miles in length? How many feet of wire will be required, the fence being 5 wires high?

## SQUARE MEASURES.

**316.** Square Measure is used in measuring surfaces, as land, paving, painting, plastering, roofing, etc.

The unit of square measure is a square bounded by lines of some known length. Thus, a square inch is a square whose sides are one inch long; a square foot, a square whose sides are one foot long; etc.

## TABLE.

144	Square	Inches (sq. in.)	=	1	Square	Foot	•	•	•	sq. ft.	
9	Square	Feet	=	1	Square	Yard				sq. yd.	
$30\frac{1}{4}$	Square	Yards	=	1	Square	Rod				sq. rd.	
160	Square	Rods	=	1	Acre					. A.	
640	Acres		=	1	Square	Mile				sq. mi.	

Notes.—1. 1 Rood = 40 sq. rds. =  $\frac{1}{4}$  A. The rood has practically gone out of use.

2. All of the above, excepting the acre, are derived from the corresponding units of Linear Measure. Thus, 1 sq.  $ft. = 144 (12 \times 12) sq. in.; 1 sq. yd. = 9 (3 \times 3) sq. ft.; 1 sq. yd. = 30_{\frac{1}{4}} (5\frac{1}{2} \times 5\frac{1}{2}) sq. rd.$ 

3. The acre is the common unit of land measure, and is equivalent to a square whose side is 208.71 feet, or a rectangle 10 rods by 16 rods (165 ft. by 264 ft.).

4. Roofers, plasterers, and carpenters sometimes call 100 square feet a square.

317. Surveyors' Square Measure is used in measuring land.

## TABLE.

Note.—In the vicinity of St. Louis, and in other parts of the Mississippi valley that were settled by the French, the old French *arpent* is still used as the unit of land measure. It contains about  $\frac{5}{6}$  of an English acre.

**318. U. S. Public Lands** are divided by north and south lines run according to the true meridian, and by others crossing them at right angles, so as to form *townships* of six miles square.

Townships are subdivided into *sections*, containing, as nearly as may be, 640 acres each, or 1 square mile.

Sections are subdivided into half-sections, quarter-sections, half-quarter-sections, and quarter-quarter-sections.
## TABLE.

1 Township	= 6	mi.	$\times 6$	mi.	= :	36 sq	. mi.	= 2	3040	$\boldsymbol{A}.$
1 Section	= 1	66	$\times 1$	66	=	1	"	=	640	"
1 Half-Section	= 1	"	׳	66	=	$\frac{1}{2}$	"	=	320	"
1 Quarter-Section	$=\frac{1}{2}$	"	׳	"	=	1	"	=	160	"
1 Half-Quarter-Section	$=\frac{1}{2}$	"	$\times \frac{1}{4}$	"	=	18	"	=	80	"
1 Quarter-Quarter-Section	$1 = \frac{1}{4}$	66	$\times \frac{1}{4}$	"	=	16	"	=	40	66

The following diagrams show the method of numbering the sections of a township, and that of naming the subdivisions of sections.



**319.** A **Rectangle** is a plane (flat) surface having four straight sides and four square corners (right angles).

A rectangle whose sides are equal is called a square.

**320.** The Area of a surface is an expression for that surface in terms of square units.



In the diagram each small square represents a square foot. Since there are 3 rows, and 4 square feet in each row, there are 3 times 4 square feet, or 12 square feet in the rectangle. Hence, the *area* of any rectangle may be found by multiplying together the numbers denoting its length and breadth, in the same denomination; or, more briefly,

To find the area of a rectangle, multiply its length by its breadth.

#### EXAMPLES.

**321.** 1. Reduce 28140 square rods to acres.

2. How many square feet in 3 acres?

3. Reduce 4 A. 100 sq. rd. 20 sq. yd. to square yards.

4. Reduce 46.3125 A. to integers of lower denominations.

5. How many acres in the State of Wisconsin, whose area is 53924 square miles?

6. How many square feet in a lot 25 feet front and 100 feet deep? (320.)

7. How many square feet in a roof 20 ft. wide and 45 ft. long?

8. How many square feet in a floor 42 feet long and 33 feet wide? How many square yards?

9. How many square feet in a tight board fence 8 ft, high and 120 ft, long?

10. How many building lots, each 36 ft. by 110 ft., can be made from a lot containing 5 acres?

11. How many acres in a farm 384 rods long and 245 rods wide?

12. How many acres in a rectangular field 28.50 chains by 46.38 chains ?

13. How many acres in a rectangular piece of land 224 links by 448 links?

14. How many square yards in a floor 16 ft. 6 in. by 12 ft. 9 in?

15. How many square feet of floor in a 3-story building 60 ft. by 98 ft?

16. A ceiling, whose area is 720 sq. ft., is 30 ft. long. What is its width?

17. What is the value of a field  $320 \ rd$ . long and  $160 \ rd$ . wide, at \$22.50 an acre?

18. A rectangular lot contains 24 acres; what is its width, its length being 1056 feet?

19. What part of a square foot is a surface 3 in. by 8 in.? 4 in. by 9 in.? 8 in. by 12 in.?

20. How many square yards of oil-cloth will cover a floor 15 ft. long,  $13\frac{1}{2} ft$ . wide ?

21. A railroad passes through 5808 feet of a farm. If the area occupied is 50 ft. wide, what is the cost of the right of way at \$66 per acre ?

Art. 321.]

22. How many square feet in 60 panes of glass each 24 in. by 30 in.?

23. How many square yards of paving in a street 1200 ft. long and 60 ft. wide?

24. How many square feet in a sidewalk 6 ft. wide and  $\frac{5}{6}$  of a mile long?

25. What part of a square yard is a surface 6 in.  $\times 8$  in.? 10 in.  $\times 14$  in.? 14 in.  $\times 20$  in.?

26. How many shingles, 3 in. wide and 4 in. of the length exposed to the weather, would be required for a square yard of roofing?

27. How many shingles, 5 in. wide and 4 in. of the length exposed to the weather, would be required for a roof 60 ft. long and 24 ft. wide?

28. How many square feet in a piece of tin 20 in.  $\times 14$  in.?

29. How many pieces of tin,  $14 \text{ in.} \times 20 \text{ in.}$ , will be required for a roof 60 ft. long and 49 ft. wide, making no allowance for seams and waste?

30. How many brick, upper surface 4 in.  $\times$  8 in., will be required for a walk, 6 ft. wide and 660 ft. long?

31. How many paving stones, 6 in. by 8 in., will be required for a street 50 ft. wide and 1248 ft. long?

32. Find the value of a quarter-section (318) of land at \$6.50 per acre.

33. <sup>2</sup>/<sub>3</sub> of the land in a western township (318) is assessed at \*6 per acre and the remainder at \$8. What is the total assessment?

34. How much will it cost to build a road from the common corner of sections 6, 5, 7, and 8 (see diagram, Art. **318**) to the common corner of sections 2, 1, 12, and 11 at \$1.25 per linear rod? How many acres of land will be occupied if the road is 4 rods wide?

35. How many square feet in the walls of a room, 16 ft. wide, 18 ft. long, and 9 ft. high ?

Note.—There are 2 ends each 16  $ft. \times 9$  ft., and 2 sides each 18 ft. by 9 ft.The following method is frequently used by mechanics: Multiply the perimeter (the distance around the room) by the height. To find the perimeter, add twice the length to twice the width.

36. How many square inches of gold leaf would be required to cover a box 7 in.  $\times 4$  in.  $\times 3$  in.? (Use crayon box as an illustration.)

37. How many square yards of plastering surface in the sides and ends of a room, 9 ft. high, 16 ft. long, 15 ft. wide? How many square yards in the ceiling?

38. How many square yards of plastering surface in a room 12 ft. high, 20 ft. long, and 18 ft. wide, deducting 120 sq. ft. for doors and windows?

39. How many square feet of painting surface, excepting the bottom, on the outside of a car, 30 ft. long, 8 ft. wide, 7 ft. high?

40. How many square feet of tin plate would be required for making 1000 rectangular cans 8  $in \times 6$   $in \times 15$  in., adding 7 sq. in. for seams and waste in making each can?

41. How many yards of paper border, 5 strips in a piece, would be required for a room 16 ft. 3 in. long and 12 ft. 6 in. wide, adding 2 ft. 6 in. for chimney, jambs, etc.?

42. How many squares (100 square feet) in a roof 40 ft. by 60 ft? 45 ft. by 64 ft?

NOTE.—Divide by 100 by pointing off 2 figures at the right.

43 How many shingles, exposed portion 5 in. by 5 in., in a square cf 100 square feet? If exposed portion is 4 in. by 4 in, how many? 4 in. by 5 in, how many?

44. How many sheets of tin 20 in. by 14 in. in a square of 100 square feet? 10 in. by 14 in.? 8 in. by 10 in.?

45. How many shingles would be required for a roof 60 ft. by 80 ft., if 500 shingles will cover a square? How many, 700 shingles to a square? How many, 800 shingles to a square?

46. How many sheets of tin would be required for a roof 30 ft. by 50  $ft_{\star}$ , if 50 sheets will cover a square ? How many, 62 sheets to a square ?

47. What part of a square yard in a piece of carpet 27 in. wide and 1 yd. long ?

48. How much will it cost to carpet a floor 15 ft. by 18 ft. with carpeting  $\frac{3}{4}$  yd. wide, at \$1.60 per yard, making no allowance for waste in matching figures, etc.?

Note.—If no allowance is made for waste in cutting, divide the number of square yards in the floor by the number of square yards in one linear yard of carpet. Carpet dealers in estimating the number of yards of carpet required for a room, multiply the length of the room (plus a proper allowance for matching the design) by the number of full widths. Ingrain carpet is usually 1 yd. wide, Brussels, Moquette, Wilton, Velvet, and Axminster,  $\frac{3}{4}$  yd. wide. 49. How many whole widths of carpet 1 yd. wide would be required for a room 14 ft. 8 in. wide, and how many inches would be folded under? If the room is 19 ft. 6 in. long, how many yards of carpet would be required, supposing the excess at the sides to be folded under, and  $2\frac{1}{2}$  yds. to be wasted in cutting and matching the figures?

50. How many yards of carpet border would be required for a room 21 ft. by  $16\frac{1}{2}$  ft.?

51. The height of a flight of stairs is 12 ft. How many steps, if they are each 8 *in*. high? How many yards of carpet would it be necessary to purchase if the tread of each step is 10 in., and allowing one yard for moving? (Find what part of a yard is required for one step.)

52. How many square yards in a roll of paper 8 yd. long and 18 in. wide? How many sq. ft.?

53. How many rolls of paper, 8 yd. long, 18 in. wide, would be required for the sides and ends of room 22 ft. 6 in. long, 13 ft. 6 in. wide, and 9 ft. high, deducting 12 sq. yd. for doors and windows, and making no allowance for waste in cutting?

Note.—If no allowance is made for waste in cutting, divide the surface to be papered by the number of square feet (or square yards) in one roll of paper.

In practice, there is a great deal of waste in cutting and matching wall paper. If the room is 9 ft, high, but two whole strips could be cut from a roll 8 yds. long. If double rolls (16 yds. each) are used, 5 whole strips could be cut from each roll. It is therefore more economical to use double rolls.

Paper-hangers in estimating the number of rolls required for a room, calculate the number of full strips that will be necessary for the regular surface of the walls, and divide this number by the number of whole strips that can be cut from one roll. The ends of rolls are used for the surface above the doors, and above and below the windows, and other irregular places.

54. How many strips of paper, 18 in. wide, would be required for a surface 24 ft. wide ?

55. How many whole strips of paper, 8 ft. 9 in. long, could be cut from a roll of paper, 8 yd. long? How many from a double roll, 16 yd. long?

56. How many rolls of paper (16 yd. long, 18 in. wide) would be required for the sides and ends of a room, 20 ft. long, 16 ft. wide, and 8 ft. 6 in. high, deducting 31 ft. for the width of doors, windows, mantels, etc.? (Paper-hangers' method.)

## SOLID OR CUBIC MEASURE.

322. Solid or Cubic Measure is used in measuring solids, or bodies which have length, breadth, and thickness or depth.

The unit of cubic measure is a cube, each of whose edges is a unit of some known length. Thus, a cubic inch is a cube, each of whose edges is one inch; a cubic foot is a cube, each of whose edges is one foot; etc.

## TABLE.

1728	Cubic	Inches	(cu.in.)	) ==	1	Cubic	Foot			. cu. ft.
27	Cubic	Feet	× .	=	1	Cubic	Yard	đ.		. cu. yd.
128	Cubic	Feet		_	1	Cord				cd.

Notes.—1. The above units, excepting the cord, are derived from the corresponding units of linear measure. Thus, 1 cubic foot contains 1728  $(12 \times 12 \times 12)$  cubic inches; 1 cubic yard, 27  $(3 \times 3 \times 3)$  cubic feet.

2. The U.S. measurement ton for freight contains 40 cubic feet.

3. The U. S. register tonnage (entire internal cubical capacity) of vessels is expressed in tons of 100 cubic feet each.

4. A perch of masonry is 1 rod long,  $1\frac{1}{2}$  feet thick, and 1 foot high, and is equal to  $24\frac{9}{4}$  ( $16\frac{1}{2} \times 1\frac{1}{2} \times 1$ ) or about 25 cubic feet.

323. The Volume or Solid Contents of a solid is an expression for that solid in terms of cubic or solid units.

The diagram represents a solid 4 feet long, 3 feet broad, and 2 feet thick.

Each small cube is a cubic foot. Since the end of the solid contains  $(3 \times 2)$  6 square feet of surface, it is evident, if a section 1 foot thick be cut off from this end, it can be divided into 6 cubes, with edges 1 foot in length, and therefore the section will contain 6 cubic feet; and since the whole solid is 4 feet long, and contains 4 like sections, it must contain 4 times 6 cubic feet, or twenty-four cubic feet. Hence the volume of a rectangular solid may be found by multiplying together the numbers expressing

4 Feet

its length, breadth, and thickness, in the same denomination; or, more briefly,

To find the volume of a rectangular solid, multiply together its length, breadth, and thickness.

**324.** A Rectangular Solid is a solid having six rectangular sides or faces.

A Cube is a rectangular solid whose sides are six equal squares.

### EXAMPLES.

325. 1. How many cords in 15744 cubic feet?

2. How many cubic inches in 175 cubic feet?

3. Reduce 37368 cubic feet to cubic yards.

4. Add 7 cd. 49 cu. ft., 13 cd. 92 cu. ft., 12 cd. 28 cu. ft., 16 cd. 110 cu. ft., 3 cd. 16 cu. ft., 14 cd. 80 cu. ft.

5. How many cubic yards in an excavation, 42 ft. long, 40 ft. wide, and 9 ft. deep?

6. How much will it cost to dig a cellar 36 ft. long, 30 ft. wide, and 6 ft. deep, at 30 cents per cubic yard?

7. What is a pile of wood, 20 ft. long, 4 ft. wide, and 7 ft. 6 in. high, worth at \$5.75 per cord ?

8. If a pile of bark is 40 ft. long and 4 ft. wide, how high must it be to contain 10 cords?

9. How many cords in a pile of bark, 22.5 ft. long, 4 ft. wide, and 4.8 ft. high ?

10. How many cubic feet in a box, 4 ft. 6 in. high, 8 ft. long, and 3 ft. 9 in. wide?

11. How many cubic inches in a rectangular cistern, 6  $ft. \times 5 ft. \times 4\frac{1}{2} ft.$ ?

12. How many tons in a shipment which occupies a space, 16 ft. by 15 ft. by 28 ft? (322, 2.)

13. What is the freight of 350 cu. ft. of merchandise at \$8 per ton? At 50 shillings per ton?

14. How many cubic feet in a vessel whose measurement is 2135 tons? (322, 3.)

15. How many perch of masonry in a wall, 40 ft. long, 9 ft. high, and  $1\frac{1}{2}$  ft. thick? (1 Perch = 25 cu. ft.) (322,4.)

16. How many bricks 2 in.  $\times 4$  in.  $\times 8$  in. in one cubic foot?

17. The space occupied by a bag containing 1000 standard silver dollars is 12 *in.* long, 9 *in.* wide, and 4 *in.* deep. How many cubic feet would be occupied by 1,000,000 such dollars?

18. How many cubic feet is a wall, 12 in. thick, 42 ft. long, and 30 ft. high? How many bricks would be required for the above wall allowing 21 to a cubic foot? What would be their value at \$9 per thousand?

[Art. 325.

Common North River brick are 8  $in. \times 4$   $in. \times 2\frac{1}{2}$  in. Brick manufactured in other localities are of various sizes.

Builders usually allow 7 common bricks for each square foot of the surface of the wall if the wall is one brick thick (4 *in.*), 14 to a square foot if 2 bricks thick (about 8 *in.*), 21 to a square foot if 3 bricks thick (about 12 *in.*), etc.

19. According to the above builder's rule, how many bricks would be required for a wall, 64 ft. long, 39 ft. high, and 2 bricks thick (about 8 in.)?

20. How many cubic feet of masonry in a cellar wall 2 ft. thick, 8 ft. high, outside measurement 25 ft. by 45 ft?

Builders sometimes multiply the total outside measurement (perimeter or girth) by the height and thickness to find the number of cubic feet. By this method, the corners are counted twice. To find the exact length of the wall, from the total outside measurement subtract four times the thickness of the wall. (See note, Ex. 35, Art. **321**.)

21. How many bricks will be required to build a chimney 28 ft. high, if there are 5 courses of brick to each foot, and 16 bricks in each course (flue 4 *in*. by 12 *in*., double wall)? How many, 8 bricks in a course (flue 8 *in*. by 16 *in*., single wall)?

22. How much stone, lime, and sand will be required for a wall 144 ft. by 10 ft. by 2 ft., if 128 cu. ft. of broken stone, 14 *bbls*. of lime, and a load (cubic yard) of sand will lay 100 cu. ft. of wall?

23. How many bricks will be required for a house 24 ft. wide, 63 ft. long, and 30 ft. high, allowing 21 bricks for each square foot of surface (the walls being 3 bricks thick), if 225 square feet are deducted for doors and windows, and if the walls are considered 1 ft. thick in making deductions for the corners ?

## BOARD MEASURE.

**326.** Lumber is measured by *board measure*. The board foot is 1 ft. long, 1 ft. wide, and 1 in. thick; hence it is  $\frac{1}{12}$  of a cubic foot.

In measuring boards one inch or less in thickness, the number of square feet of surface which they would cover is measured.

Plank, joists, etc., more than one inch in thickness are reduced to inch boards and measured by board measure.

Boards, plank, scantling, joists, beams, and sawed timber generally are measured by *board* measure; hewn and round timber are sometimes measured by *cubic* measure. Art. 327.]

**327.** When lumber is not more than one inch thick, to find the number of feet board measure : Multiply the length in feet by the width in inches, and divide the product by 12.

16 pieces each containing a board foot could be cut from a board 16 ft. long, 12 *in*. wide. A board 11 *in*. wide is  $\frac{11}{12}$  of a board, 12 *in*. wide and of the same length and thickness.

When more than 1 inch thick : Multiply the length in feet by the width and thickness in inches, and divide the product by 12.

Lumbermen use an automatic *rule* for measuring board, planks, etc. They also use table books for reducing logs or round timber to board measure.

#### EXAMPLES.

**328.** 1. How many square feet would be covered by a board 16 *ft*. long and 9 *in*. wide?

2. If a stick of timber 24 *ft*. long, 8 *in*. wide, 3 *in*. thick, is reduced to boards one inch in thickness, how many square feet would they cover?

3. How many feet of boards would be required for a floor 20 ft. wide and 24 ft. long? What would be their value at \$14 per thousand?

4. How many board feet in 475 cubic feet?

Find the number of feet, board measure, in each of the following boards, joists, beams, etc.:

	Length.	Width.	Thickness.		Length.	Width.	Thickness.
5.	12 ft.	12 in.	1 in.	9.	16 ft.	8 in.	11 in.
6.	14 ft.	8 in.	$\frac{1}{2}$ in.	10.	20 ft.	10 in.	2 in.
7.	16  ft.	6 in.	$\frac{3}{4}$ in.	<i>11</i> .	12 ft.	6 in.	4 in.
8.	18 ft.	14 in.	$\frac{7}{8}$ in.	12.	24 ft.	9 in.	3 in.

13. How many square feet would be covered by 45 boards, 16 ft. long, 8 in. wide, if they are laid side by side? (First find the total width in feet.)

14. How many board feet in a pile of lumber 8 ft. high, 7 ft. wide, and 18 ft. long? Find its value at \$15 per thousand feet.

15. How many feet, board measure, in 16 boards, each 18 ft. long, 10 in. wide, and 1 in. thick?

16. How many board feet in 24 joists, 20  $ft. \times 8$  in.  $\times 4$  in.?

17. How many feet of boards, 4 in. wide and 1 in. thick, would be required for a fence 5 boards high and one mile long?

18. How many posts 8 ft. apart would be required for above fence?

19. How many feet, board measure, in 12 planks, each 10 ft. long, 12 in. wide, and 2 in. thick ?

20. Making no allowance for the corners, how many feet of boards would be required to make a box 8 ft.  $\times 4 ft$ .  $\times 5 ft$ ?

21. How many feet in a tapering board 18 ft. long, 12 in. wide at the smaller end, and 16 in. at the other ?

Note.—To find the average width of a tapering board, measure it at the center, or take  $\frac{1}{4}$  the sum of the widths at the ends.

# LIQUID MEASURES.

329. Liquid Measure is used for measuring liquids.

The unit of this measure is the wine gallon, which contains 231 cubic inches.

## TABLE.

			1	gal.		qt.		pt.		gi.
4 Gills (gi.)	= 1 Pint .		pt.	1	=	4	=	8	=	32
2 Pints	= 1 Quart .		qt.			1	=	2	=	8
4 Quarts	= 1 Gallon		gal.					1	=	4

Notes.—1. In estimating the capacity of tanks, cisterns, reservoirs, etc., 1 barrel =  $31\frac{1}{2}$  gallons; 1 hogshead = 2 barrels = 63 gallons.

2. In commerce, the barrel, tierce, and hogshead are not fixed measures, but their capacity is found by gauging, or actual measurement.

3. The imperial gallon of England contains 277.274 cubic inches, and is equivalent to 1.2 U. S. wine gallons.

4. 1 cubic foot = 7.48 or about  $7\frac{1}{2}$  (1728 ÷ 231 = 7.48) wine gallons. Hence to find the number of gallons in a rectangular cistern, multiply the number of cubic feet by 7.48 or  $7\frac{1}{2}$ .

5. To find the number of gallons in a cylindrical vessel, multiply the square of the diameter by the height, and this product by  $5\frac{4}{5}$  (.7854×1728 + 231 = 5.8752).

**330.** Apothecaries' Fluid Measure is used in prescribing and compounding liquid medicines.

The gallon and pint of this measure are the wine gallon and pint.

## TABLE.

					Cong.	0.	$f$ $\mathfrak{F}$ .	f 3.	η.
60	Minims (M)	=	1 Fluidrachm	f 3.	1 =	8 =	128 =	1024 =	61440
8	Fluidrachms	=	1 Fluidounce	f 3.		1 =	16 =	128 =	7680
16	Fluidounces	=	1 Pint	0.			1 =	8 =	480
8	Pints	_	1 Gallon	Cong.				1 =	60

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Notes.-1. Cong. is for the Latin congius, gallon; O., for the Latin octavius, one-eighth.

2. The symbols precede the numbers to which they refer; thus, O.6 f 3 10, is 6 pints 10 fluidounces.

#### EXAMPLES.

**331.** 1. Reduce 8 gal. 3 qt. 1 pt. to pints.

2. Reduce 875 pints to gallons.

3. Add 4 gal. 2 qt. 1 pt., 3 gal. 3 qt. 1 pt., 9 gal. 1 pt., 11 gal. 1 qt.

4. How many barrels in 100000 gallons?

>5. 480 English gallons (329, 3) equal how many U. S. gallons? (Add  $\frac{1}{6}$ .)

6. How many cubic feet in 1000 gallons?

7. How many gallons in 300300 cubic inches?

8. How many gallons in a rectangular tank, 8  $ft. \times 4 ft. \times 6 ft.$ ?

OPERATION.  $-8 \times 4 \times 6 \times 7_{\frac{1}{2}} = 1440$ , approximate result (see Art. **329**, Note 4).  $8 \times 4 \times 6 \times 7.48 = 1436.16$ , accurate result.

9. How many gallons in a rectangular cistern 6 ft. long, 4 ft. wide, 3 ft. high?

10. How many gallons in a rectangular cistern 16 ft. long, 4 ft. high, and 5 ft. wide?

11. How many gallons in a rectangular reservoir, 40 ft. long, 16 ft. wide, and 8 ft. deep?

12. How many gallons in a cylindrical vessel, 3 ft. in diameter and 9 ft. high ?

**OPERATION.**— $3 \times 3 \times 9 \times 5\frac{7}{8} = 475\frac{7}{8}$  (see Art. **329**, Note 4).

13. How many gallons in a cylindrical tank 4 ft. in diameter and 16 ft. deep?

14. How many gallons in a circular reservoir, 40 ft. in diameter and 6 ft. deep?

15. How many gallons in a circular reservoir 60 ft. in diameter and 8 ft. deep ?

16. Reduce Cong.2 0.6  $f \ge 10 f \ge 5$  to fluidrachms.

17. From the sum of 51 gal. 2 qt. 1 pt., and 45 gal. 1 qt. 1 pt., subtract 27 gal. 1 qt., and divide the result by 9.

18. How many bottles, each holding 1 qt. 1 pt. 2 gi., can be filled from a barrel of cider ?

#### [Art. 332.

## DRY MEASURE.

**332.** Dry Measure is used in measuring dry articles; as salt, grain, fruits, etc.

The unit of this measure is the Winchester bushel, which contains 2150.42 eubic inches.

## TABLE.

2 Pints (pt.)	=	1	Quart .			•	qt.	bu.		pk.		qt.		pt.
8 Quarts	=	1	Peck	•	•		pk.	1	=	4	=	32	=	64
4 Pecks	=	1	Bushel	•			bu.			1	=	8	=	16

Notes.—1. The half-peck or gallon of this measure contains 268.8 cubic inches, and is 37.8 cubic inches larger than the liquid gallon (268.8 — 231 = 37.8).

2. The imperial bushel of England contains 2218.19 cubic inches, and is equal to 1.03 Winchester bushels. In certain localities in Great Britain, 8 bushels are called a quarter.

3. Grain, seeds, etc., are usually sold by weight. For table of equivalents see Art. **338**.

4. 36 bushels = 1 chaldron of coke or charcoal.

5. 1 bushel is equivalent to about 9.3 (2150.42  $\div$  231) wine gallons.

#### EXAMPLES.

333. 1. Reduce 2 bu. 3 pk. 5 qt. 1 pt. to pints.

2. Reduce 10000 pints to bushels.

3. Find the value of 5 bushels of nuts at 8c. per pint.

4. How many cubic inches in 75 bushels?

5. How many bushels in 322563 cubic inches?

6. How many bushels in 400 cubic feet?

Note.—Since a bushel is about  $1\frac{1}{4}$  cubic feet, the following approximate rules may be used for all practical purposes :

To reduce cubic feet to bushels: Deduct one-fifth, or multiply by .8

The result will be too small by about  $4\frac{1}{2}$  bushels for every 1000 bushels of the result.

To reduce bushels to cubic feet: Add one-fourth, or divide by .8.

The result will be too great by about  $4\frac{1}{2}$  cubic feet for every 1000 cubic feet of the result.

Solve the above example both exactly and approximately, and compare the results.

7. How many bushels will a box 10 ft. long, 5 ft. wide, and 4 ft. high contain? (Approximate method.)

Art. 333.]

8. How many bushels of grain will a bin 14 ft. long,  $3\frac{1}{2}$  ft. wide, and 6 ft. high contain ?

2150.42 ma 1.00

9. Find the capacity in bushels of a crib, 20 ft. long, 8 ft. high, 4 ft. wide at the bottom and 6 ft. wide at the top.

Note.—To find the average width, take one-half the sum of the top and bottom measurements.

10. A crib 24  $ft. \times 8 ft. \times 6 ft$  is filled with unshelled corn. How many bushels of shelled corn would this quantity produce, if two cubic feet of corn in the ear will make one bushel of shelled corn?

## MEASURES OF WEIGHT.

**334.** Troy Weight is used in weighing gold, silver, coins, and jewels; also in philosophical experiments.

The unit of weight is the Troy pound, which contains 5760 grains. A cubic inch of distilled water weighs 252.458 of these grains, when the height of the barometer is 30 inches, and the temperature of the air and water  $62^{\circ}$  Fahrenheit.

## TABLE.

<b>24</b>	Grains $(gr.)$		1	Pennyv	vei	ght	p	wt.	lb.		0Z.	pwt.		gr.
20	Pennyweights		1	Ounce				0z.	1	=	<b>12</b>	 240	=	5760
12	Ounces	=	1	Pound			•	<i>lb</i> .			1	 20		480

Note.-The carat, used in weighing diamonds, equals 3.2 Troy grains.

The term carat is also used to denote the fineness of gold, and means  $\frac{1}{24}$  part. Thus, gold 18 carats fine contains 18 parts pure gold and 6 parts alloy.

**335.** Apothecaries' Weight is used in prescribing and compounding medicines not liquid.

The pound, ounce, and grain of this weight are the same as those of Troy weight, the division of the ounce being different.

## TABLE.

20 Grains (	gr.) = 1 Scruple		<i>sc.</i> or	Э.	Ťb	3	3		Э		gr.
3 Scruples	= 1  Dram		dr. or	3.	1 =	12	= 96	= %	288	=	5760
8 Drams	= 1 Ounce	•-	<i>oz.</i> or	3.		1	= 8	=	24	_	480
12 Ounces	= 1 Pound		lb. or	Tb.			1	=	3	=	<b>3</b> 0

Notes.—1. The symbols precede the numbers to which they refer; thus,  $\frac{3}{5}$  6 3 4, is 6 ounces 4 drams.

2. Drugs and medicines are sold in large quantities by Avoirdupois weight.

[Art. 336.

**336.** Avoirdupois Weight is used in weighing all articles, excepting gold, silver, precious stones, and medicines in small quantities.

The Avoirdupois pound contains 7000 Troy grains.

TABLE.

16 Ounces (oz.)	=	1	Pound						<i>lb</i> .	T.	cwt.	16.			oz.
100 Pounds	_ !	1	Hundr	ed	•we	eigl	ht,	ord	cwt.	1 :	= 20	= 200	00 =	= 8	32000
100 I Ounus	-1	1	Cental						С.		1	= 10	6 =	=	1600
20 Hundred-weigh	t =	1	Ton						T.				1 =	=	16

Notes.-1. The ounce is divided into halves and quarters.

2. The dram,  $\frac{1}{16}$  of an ounce, is now little used, except by silk manufacturers.

3. The Long or Gross ton, formerly used, contained 2240 pounds; the hundred-weight, 112 pounds; and the quarter, 28 pounds.

These weights are still used in Great Britain, at the U. S. Custom Houses, in ocean freights, and by wholesale dealers in coal and iron.

**337.** Comparison of Troy and Avoirdupois weights. 5760 grains = 1 *lb*. Troy. 7000 grains = 1 *lb*. Avoirdupois. **480** grains = 1 *oz*. Troy. **437** grains = 1 *oz*. Avoirdupois.

**338.** In buying and selling grain, seeds, and other produce, the bushel is regarded as a certain number of pounds. The Boards of Trade of the principal cities of the United States use the equivalents given in the following table :

Commodities.	Lbs.	Commodities.	Lbs.	Commodities.	Lbs.
Barley	48	Corn, shelled	56	Peas	60
Beans	60	Corn in the ear.	70	Rye	56
Buckwheat	48	Malt	34	Timothy Seed	45
Clover Seed	60	Oats	32	Wheat	60

TABLE OF AVOIRDUPOIS POUNDS IN A BUSHEL.

. In the Liverpool, San Francisco, and some other markets, produce is bought and sold by the *cental* of 100 pounds. Railway freight tariffs in the United States on grain, provisions, etc., are reckoned per *cwt*. or cental.

**339.** The following units are used in commerce :

1	Quintal of Fish	=	100 lbs.
1	Barrel of Flour		196 <i>lbs</i> .
1	Barrel of Pork or Beef	-	200 lbs.
1	Gallon Petroleum	=	$6\frac{1}{2}$ lbs.
1	Keg of Nails	=	100 lbs.

#### EXAMPLES.

340. 1. Reduce 10000 grains to Troy pounds.

2. Reduce 2 lb. 8 oz. 16 pwt. to grains.

3. What is the weight in Troy ounces of 1000 silver dollars (112)? Of 1280 silver dollars ?

4. Find the weight in Troy ounces of 1000 gold dollars (112).

5. Find the weight in Troy ounces of 2000 half-dollars (112).

6. What is the cost of a 14 k. watch chain weighing  $37\frac{3}{8}$  pwt. at \$1.15 per pennyweight?

7. A watch case, 14 carats fine, and weighing 60 pwt., contains how many ounces of pure gold ?

8. Find the value of a diamond weighing 11 of a carat, at \$100 per carat.

9. How many Troy ounces of pure silver would be required for the coinage of 2,000,000 standard silver dollars (113)? How much copper?

10. Reduce 161 39 36 32 to grains.

11. How many powders, each containing 5 grains, can be made from 1 *lb*. Apothecaries (Troy) of quinine? How many from 1 *lb*. Avoirdupois?

12. Add 8 lb. 9 oz., 10 lb. 7 oz., 14 lb. 15 oz., and 17 lb. 13 oz. Avoirdupois.

13. How many grains in 16 lb. Avoirdupois?

14. In 70 lb. Avoirdupois, how many pounds Troy? (337)

15. In 175 oz. Troy, how many ounces Avoirdupois?

16. Find the cost of 58 lb. 4 oz. of butter at 28c. per pound.

17. Find the cost of 875 pounds of feed at \$1.15 per cwt. (273)

18. Find the cost of 17387 pounds of oats at \$1.85 per cental.

19. Find the cost of 21370 pounds of hay at \$8 per ton.

OPERATION.

2) 2137010.685 8

ANALYSIS.—21370 lb. = 70.685 (21370 ÷ 2000) tons. If 1 ton costs \$8, 10.685 tons will cost 10.685 times \$8, or \$85.48. To divide by 2000, divide by 2 and place the point in the quotient three places to the left.

\$85.480

20. What is the value of 28140 pounds of straw at 6.50 per ton?

21. Find the cost of 16480 pounds of hay at \$11.50 per ton.

[Art. 340.

22. Find the value of 28160 pounds of coal at \$5.25 per ton.

23. Find the value of 42250 pounds of coal at \$3.75 per ton of 2240 pounds. (336, 3)

How many bushels in

24.	8375 pounds of wheat?	29. 18174 pounds of rye?
25.	9116 pounds of corn?	30. 13275 pounds of wheat ?
26.	1128 pounds of beans?	31. 20000 pounds of barley?
27.	5172 pounds of peas?	32. 11419 pounds of clover seed ?
28.	3375 pounds of oats?	33. 12562 pounds of timothy seed

34. What is the value of 49375 pounds of corn at 64c. per bushel?

Note.—Usually in business computations, the number of bushels is also required. 49375  $lb. = 881\frac{29}{56} bu. 881\frac{29}{56} times 64c. = $564.29.$ 

When the number of bushels is not required, to avoid fractions, multiply the number of pounds by the price per bushel and divide the product by the number of pounds in one bushel.  $49375 \times \$.64 \div 56 = \$564.29$ .

<sup>•</sup>By both of the above methods, find the cost of

35. 8375 lb. wheat at \$1.10 per bushel.

36. 9416 lb. corn at 85c. per bushel.

37. 7428 lb. oats at 72c. per bushel.

38. 6224 lb. beans at \$2.25 per bushel.

39. 9118 lb. barley at \$1.25 per bushel.

40. 8128 lb. rye at 82c. per bushel.

41. 4170 lb. clover seed at \$4.25 per bushel.

42. 5160 lb. timothy seed at \$1.75 per bushel.

43. What is the freight on 52840 bushels corn at 32c. per cwt.?

44. What is the freight of 16 T. 17 cwt. 20 lb. at \$5 per ton of 2240 lb.?

## ENGLISH MONEY.

341. English or Sterling Money is the legal currency of Great Britain.

				IAI							U. S. Money.
4	Farthings	=	1	Penny			d.		•		\$ .02+
12	Pence	=	1	Shilling			8.		•		.243 +
90	Ch illin on		(1	Pound,	or		£.	1			1 9665
20	Summgs	=	11	Sovereig	rn			5	•	•	4.0000

Notes.—1. 1 Crown = 5 shillings, or  $\frac{1}{4}$  of a pound (\$1.216+).

2. 1 Guinea = 21 shillings (\$5.11). It is not now coined.

5. The gold coins of Great Britain are 22 carats  $(\frac{1}{1\frac{1}{2}})$ , or  $.916\frac{2}{5}$  fine. (The old carat system (**334**, note) is generally abandoned except for jewelry. 1 carat =  $.041\frac{2}{5}$ .) The silver coins of Great Britain are .925  $(\frac{2}{57})$  fine.

#### EXAMPLES.

**342.** 1. Add £27 16s. 10d., £6 10s. 8d., £47 15s. 11d., £25 7s. 6d., £3 14s. 8d., and £23 16s. 3d.

2. From £17 8s. 4d. subtract £10 12s. 8d.

3. Multiply £5 6s. 3d. by 8.

4. Reduce 8375d. to shillings and pounds.

5. Reduce £12 16s. 8d. to pence.

6. What is the cost of 466 yards of cloth at 91d. per yard?

7. Find the value of 4120 bu. wheat at 4s. 41d. per bushel.

8. In 47 guineas, how many pounds and shillings?

9. Divide £16 5s. 6d. by 9; by 7; by 31.

10. How many yards of cloth at 3s. 7d. per yard can be bought for £7? For £9 5s. 6d.?

11. What is the cost of 20 yd. silk at 10s. 6d. per yard?

12. Reduce £8 17s. 8d. to the decimal of a pound. (293)

Note.—The following method for reducing shillings and pence to the decimal of a pound is sufficiently accurate for most business purposes: Write one-half of the greatest even number of shillings as tenths, and if there be an odd shilling write 5 hundredths; multiply the number of pence by 4, and write the product as thousandths. If the product is between 12 and 36, add 1 to the thousandths; if between 36 and 43, add 2 to the thousandths. Thus,  $\pounds 8 \ 17s. \ 8d. = \pounds 8 + \pounds. 85 + \pounds. 033 = \pounds 8.883.$ 

Reduce mentally the following to the decimal of a pound :

13.	16 <i>s</i> .	2d.	15.	10s.	8d.	17.	7s. 3d.
14.	18s.	5 <i>d</i> .	16.	17s.	4d.	18.	13s. 11d.

19. Reduce  $\pounds$ .821 of a pound to shillings and pence. (289)

Note.—This example can be performed mentally by reversing the operation explained in note to Ex. 12. Multiply the number of tenths by 2, and write the product as shillings  $(2 \times 8 = 16)$ . Divide the number of thousandths expressed by the 2nd and 3rd figures by 4, and write the quotient as pence (21 + 4 = 5). £.821 = 16s. 5d.

If the second figure to the right of the point is 5 or more than 5, it is evident that there is an odd number of shillings, and the decimal must be separated into two parts before applying the above rule.

Thus,  $\pounds.875 = \pounds.85 + \pounds.025$ .  $\pounds.85 = 17s$ .  $(2 \times 8\frac{1}{2})$ .  $\pounds.025 = 6d$ .  $(25 \div 4)$ .

Reduce mentally the following to shillings and pence:

20.	£.425;	£.637.	22.	£.255;	£.183.	
21.	£.817;	£.245.	23.	£.376;	£.496.	

24. Divide £15 16s. 8d. by .10; by .20; by .25; by .40.

25. Multiply £16 12s. 9d. by .05; by .06; .04.

26. If £1 sterling is worth \$4.87, what is the value of £225 18s. 6d.? Of £140 8s. 8d.?

27. If £1 sterling is worth \$4.88, how many pounds can be bought for \$1000? How many for \$1625?

## MISCELLANEOUS TABLES.

343. The following table is used in counting certain articles:

12 U	Inits	=	1 Dozen		• •	doz.	g.gr.	gr.	doz.	units.
12 I	)ozen	=	1 Gross		• •	gr.	1 =	12 =	144 =	1728
12 G	ross	=	1 Great G	ross		g.gr.		1 =	12 =	144

344. The following table is used in the paper trade :

24	Sheets	=	1	Quire			qr.	rm.	qr.	81	heets.
20	Quires	=	1	Ream			rm.	1 =	$\overline{20}$	=	480

Manufacturers and wholesale dealers usually sell paper by the pound.

## EXAMPLES.

345. 1. Find the value of 5 gross pencils at 4c. each.

2. A merchant buys 6 gross pens at 95c. per gross, and sells them at 1c. each. What is his profit ?

3. How many sheets of paper in 12 quires? In 2 reams?

4. Find the difference between six dozen dozen and half a dozen dozen.

5. Combs are bought at \$2.70 per dozen. How much is that apiece ?

6. Find the value of 306 eggs at 22c. per dozen.

7. At 1 cent each, what is the value of 20 great gross pens?

8. A grocer buys 81 dozen eggs at 22c. per dozen, and sells them at the rate of 9 for 25 cents. What is his profit?

9. If 32 pages of a book are printed on one sheet, how many reams of paper would be required for 2000 copies containing 384 pages each ?

#### Art. 346.]

## CIRCULAR MEASURE.

**346.** Circular or Angular Measure is used in measuring angles and arcs of circles. It is employed principally by surveyors in determining directions, by navigators in determining latitude and longitude of places, and by astronomers in making observations.

The unit of this measure is the *degree*, which is  $\frac{1}{360}$  of the circumference of any circle.

#### TABLE.

60	Seconds $('') =$	=	1	Minute			1.
60	Minutes =	=	1	Degree			°.
360	Degrees =	=	1	Circle			C.

Notes.-1. A quadrant is one-fourth of a circle, or 90°.

2. A sextant is one-sixth of a circle, or 60°.

3. 1 minute of the circumference of the earth is called a nautical, or geographic mile, and is about 1.15 statute or common miles.

4. An arc of 1 degree of the circumference of the earth measured at the equator equals 69.16 statute miles.

#### EXAMPLES.

347. 1. Add 74° 0' 3" and 77° 49' 58".

2. Add 12° 27' 14" and 122° 26' 45".

3. From 84° 29' 31" subtract 77° 0' 45".

4. Multiply 13° 11' 16" by 5; by 15.

5. Divide 76° 11' 45" by 15; by 12.

6. Divide 179° 42' 15" by 15; by 16.

7. Reduce 1,000,000" to higher denominations.

8. Reduce 44° 16' 40" to seconds.

9. The angles of a triangle are  $67^{\circ}$  18' 40", 72° 39' 50", and  $40^{\circ}$  1' 30" respectively. What is their sum ?

## LONGITUDE AND TIME.

**348.** The whole circle of the earth, or 360°, passes under the sun in 24 hours, and in 1 hour passes  $\frac{1}{24}$  of 360°, or 15°; in 1 minute,  $\frac{1}{60}$  of 15° (15×60'), or 15'; and in 1 second,  $\frac{1}{60}$  of 15' (15×60''), or 15';

349. Comparison of Longitude and Time.

For	ad	lifference of	$\mathbf{Th}$	e	re is a	l di	fference of
15°	$\mathbf{in}$	Longitude	_ 1	L	hr.	in	Time.
15'	66	66	1	L	min.	66	66
$15^{\prime\prime}$	"	66	1	L	sec.	66	66
1°	66	66	4	F	min.	66	66
1'	66	66	4	£	sec.	66	ćć.
1"	"	66	Ļ	R	sec.	66	66

**350.** RULE.—1. The difference in longitude of two places, expressed in ° ' ", divided by 15 will produce their difference in time expressed in hours, minutes, and seconds.

2. The difference in solar time of two places, expressed in hr. min. sec., multiplied by 15 will produce their difference in longitude expressed in ° ' ".

351.	TABLE	<b>OF</b> .	LONGITUDES.
------	-------	-------------	-------------

73° 44	<b>4'</b> 50''	W.	New York 74° 0' 3	" W.
80° 48	3′	W.	New Orleans 90° 2' 30	" W.
71° 3	3′ 30′′	W.	Paris	″ E.
13° 28	3' 45''	E.	Philadelphia 75° 10'	W.
88° 19	)' .2''	E.	Rome 12° 27' 14	' E.
84° 29	9′ 31″	W.	Richmond, Va 77° 25' 45	יי w.
87° 3'	7' 45''	W.	San Francisco122° 26' 45	″ W.
92° 8	8′	W.	St. Paul, Minn 95° 4' 55	יי w.
0° (	5′ 38′′	W.	St. Louis, Mo 90° 15' 15	" W.
99° (	5′	W.	Washington, D. C 77° 0' 15	″ W.
	73° 44 80° 44 71° 4 13° 29 88° 19 88° 19 84° 29 87° 3 92° 4 0° 4 99° 4	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	73° 44' 50'' W. New York

**352.** Standard Time.—In 1883, the principal railroads and cities of the United States and Canada adopted the time of four different meridians as the standard time of four belts or sections comprising the whole of the above countries. The most eastern of these sections embraces the Eastern and Middle States, Maryland and Virginia, and extends about  $7\frac{1}{2}^{\circ}$  east and west of the meridian of  $75^{\circ}$  west of Greenwich (near Philadelphia). The time of this meridian, called Eastern time, is used in this section, and is 5 hours slower than Greenwich time. The time of the meridian of  $90^{\circ}$  west of Greenwich (near St. Louis) called Central time, is used in the next section, and is 1 hour slower than Eastern time. The time of the meridian of  $105^{\circ}$  west of Greenwich (near Denver), called Mountain time, is used in the Rocky Mountain region, and is 1 hour slower than Central time and 2 hours slower than Eastern time. The time of  $120^{\circ}$  west of Greenwich, called Pacific time, is used in the Pacific slope, and is 3 hours slower than Eastern time.

#### Art. 353.]

#### EXAMPLES.

#### 353. Find the difference in longitude between

- 1. New York and London. 4. St. Louis and Calcutta.
- 2. Boston and Paris. 5. Philadelphia and Berlin.
- 3. Chicago and San Francisco. 6. San Francisco and Calcutta.

Find the difference in solar time between

- 7. New York and Greenwich. 10. Rome and London.
- 8. Chicago and New York. 11. Paris and Albany.
- 9. Richmond and Calcutta. 12. Calcutta and Jefferson City.

Find mentally the difference in standard time between

- 13. Albany and Denver. 16. St. Louis and Richmond.
- 14. New York and Chicago. 17. St. Paul and Sacramento.
- 15. Boston and San Francisco. 18. Phila. and Portland, Me.

Find the difference between the standard time and the solar time of the following cities:

19. Boston. 21. San Francisco. 23. Chicago.

20. Philadelphia. 22. St. Louis. 24. St. Paul.

25. A navigator finds that when it is noon at his place of observation, it is 16 *min*. 34 *sec*. past 10 P.M. by his chronometer, Greenwich time; what is his longitude?

26. When it is 6 o'clock P.M., standard time, at Richmond, Va., what is the time at St. Louis, Mo.?

27. If the difference of solar time between two places is 1 hr. 18 min. 4 sec., what is the difference of longitude ?

28. When it is 20 min. past 2 P.M., standard time, at Boston, Mass., what o'clock is it at San Francisco?

29. When it is Monday, 10 P.M., standard time, in Chicago, what day and time is it in London (Greenwich time)?

30. When it is 9 o'clock P.M., solar time, in San Francisco, it is  $3 \min. 3\frac{2}{15}$  sec. past 11 A.M. in Calcutta; what is the longitude of San Francisco, if the longitude of Calcutta is 88° 19' 2" E.?

31. When it is noon, solar time, in Chicago, it is  $5 \text{ min. } 29\frac{1}{5}$  sec. of 1 P.M., solar time, in New York; what is the longitude of Chicago, the longitude of New York being 74° 3″ W.?

#### DENOMINATE NUMBERS.

## THE METRIC SYSTEM.\*

354. In the Metric System of weights and measures, the *Meter* is the basis of all the units which it employs.

**355.** The Meter is the unit of length, and is equal to one ten-millionth part of the distance measured on a meridian of the earth from the equator to the pole, and equals about 39.37 inches.

The standard meter is a bar of platinum carefully preserved at Paris. Exact copies of the meter and the other units have been procured by the several nations, including the United States, that have legalized the system. Comparisons with the standard units are made under certain conditions of temperature and atmospheric pressure.

**356.** The names of the *higher* denominations, or *multiples*, of the unit are formed by prefixing to the several *units* the Greek numerals, *deka* (10), *hecto* (100), *kilo* (1000), and *myria* (10000); as *dekameter*, 10 meters, *hectometer*, 100 meters, etc.

To assist the memory, observe that the initial letters of the multiples are in alphabetical order; thus, D, H, K, and M.

**357.** The names of the *lower* denominations, or *divisions*, of the unit are formed by prefixing to the several units the Latin numerals, deci  $(\frac{1}{10})$ , centi  $(\frac{1}{100})$ , milli  $(\frac{1}{1000})$ ; as decimeter,  $\frac{1}{10}$  meter, centimeter,  $\frac{1}{100}$  meter, etc.

To assist the memory observe that the following words are derived from the same roots: dime, decade, decimal, decimate, decennial, etc.; cent, cental, century, centennial, etc.; mill, millennium, etc.

#### LINEAR MEASURE.

#### 358. TABLE.

		1 Millimeter( $\frac{1}{1000}$ of a meter)	=	.03937 in.
10 mm.	=	1 Centimeter( $\frac{1}{100}$ of a meter)	===	.3937 in.
10 cm.	=	1 Decimeter( $\frac{1}{10}$ of a meter)	=	3.937 in.
10 dm.		1 METER	=	39.37 in.
10 m.	=	1 Dekameter (10 meters)	=	32.8 ft.
10 Dm.	===	1 Hectometer(100 meters)	=	328.09 ft.
10 Hm.	=	1 Kilometer(1000 meters)	==	.62137 mi.

Notes.—1. The meter, like the yard, is used in measuring cloths, ribbons, laces, short distances, etc.

2. The kilometer is used in measuring long distances, and is about  $\frac{5}{5}$  of a mile.

3. The centimeter and millimeter are use by artisans and others in measuring minute lengths. The other denominations are rarely used.

#### EXAMPLES.

**359.** 1. Reduce 875275 meters to kilometers.

ANALYSIS.—Since 1 kilometer equals 1000 meters, in 875275 meters there are as many kilometers as 1000 is contained times in 875275, or 875.275. To divide by 1000, place the point three places to the left (270, 4).

2. Reduce 675.318 kilometers to meters.

ANALYSIS.—Since 1 kilometer equals 1000 meters, in 675.318 kilometers there are 675.318 times 1000, or 675318 meters. To multiply by 1000, place the point three places to the right (267, note).

3. Reduce 383.64 meters to centimeters; to kilometers.

4. Reduce 175.16 centimeters to kilometers ; to meters.

5. Reduce to meters and find the sum of 876.2 decimeters, 30347 centimeters, 176.48 meters, 8.175 kilometers.

6. A ship sails 5712 kilometers in 48 days; how many kilometers does she sail per day?

7. What is the value of 56.4 meters of silk at \$1.75 per meter?

8. 16 pieces of cloth contain 38.5 meters each; 18 pieces contain 39 meters each; and 24 pieces contain 41.2 meters each; how many meters in all?

9. How many meters of ribbon at 27 cents per meter can be purchased for \$245.70?

10. If the forward wheels of a carriage are 3.5 meters in circumference, and the hind wheels 4.8 meters, how many more times will the forward wheels revolve than the hind wheels, in running a distance of 8.4 kilometers?

11. How much will it cost to sewer a street .64 Km. long, at \$3.75 per meter?

12. How many meters of wire will be required to fence a rectangular field,  $.72 \ Km$ . long and  $.56 \ Km$ . wide, if the fence is 4 wires high?

13. How long will it take a railway train, running 60 Km. per hour, to go from New York to Chicago, the distance being 1440 Km.?

Art. 358.]

#### [Art. 360

#### SQUARE MEASURE.

#### **360.** The unit of square measure is the square meter.

#### TABLE.

100 Square Centimeters, sq. cm. = 1 Square Decimeter = 15.5 + sq. in.100 Square Decimeters, sq. dm. = 1 Square METER, Sq. M. = 1.196 + sq. yd.

Notes.—1. The square meter is used in measuring flooring, ceilings, etc.; the square decimeter and the square centimeter are used for minute surfaces.

2. Since units of square measure form a scale of hundreds, each denomination must have two places of figures.

**361.** The unit of **Land Measure** is the *are*, and is equal to a square dekameter (100 square meters), or 119.6 square yards.

### TABLE.

			1 Centare(1 square meter)	=	1550 sq. in.
100 Centares,	ca.	$\cdot =$	1 Are(100 square meters)	=	119.6 sq. yd.
100 Ares,	А.	=	1 Hectare(10000 square meters)	=	2.471 acres.

Note.—The hectare is the ordinary unit for land.

#### EXAMPLES.

**362.** 1. Write 16 sq. m., 8 sq. dm., 24 sq. cm., having the square meter as the unit. (**360**, 2.) Ans. 16.0824.

2. Write 83 sq. m., 9 sq. dm., having the sq. m. as the unit.

3. In 47 ares how many square meters?

4. In 60.25 hectares how many centares?

5. How many square meters in a building lot 8 m. by 32 m.?

6. How many building lots, each containing 225 sq. m., can be formed from a field containing 9 hectares?

7. How many hectares in a farm 1.024 Km. in width and 1.625 Km. in length?

8. What is the cost of a mirror 2.25 m. by 1.44 m., at \$3.84 per sq. m.?

9. How many lots 25 m. wide and 60 m. deep, or having an equivalent area, can be laid out from 6 hectares ?

10. A man bought a piece of land for \$6950.50, and sold it for \$7603.30, by which transaction he made \$6.80 a hectare; how many hectares were there ?

#### CUBIC MEASURE.

**363.** The unit for measuring ordinary solids is the *cubic meter*.

## TABLE.

1000 Cu. Millimeters,	cu. mm.	=	1 Cu.	Centimeter	=	.061 cu. in.
1000 Cu. Centimeters	cu. cm.	=	1 Cu.	Decimeter	=	61.027 cu. in.
1000 Cu. Decimeters,	cu. dm.	=	1 Cv.	Meter	={	35.317 cu. ft. 1.308 cu. yd.

Notes.—1. The cubic meter is used in measuring embankments, excavations, etc.; cubic centimeters and cubic millimeters for minute bodies.

2. Since units of cubic measure form a scale of thousands, each denomination must have three places of figures.

**364.** The unit of Wood Measure is the *ster*, and is equal to a cubic meter, or 35.317 cubic feet.

#### TABLE.

10 Decisters, ds.	=	1 Ster(1 Cubic Meter) =	= {	.2759 cord. 35.317 cu. ft.
10 Sters, s.	=	1 Dekaster, Ds(10 Cubic Meters) =	= ;	2.759 cords.

#### EXAMPLES.

**365.** 1. Write 29 cu. m., 75 cu. dm., having the cubic meter as the unit. (**363**, 2) Ans. 29.075 cu. m.

2. Write 17 cu. m., 218 cu. dm., 27 cu. cm., having the cubic meter as the unit.

3. How many cubic meters in a box 3.5 m. by 3.2 m. by 2.5 m?

4. Bought 12 sters of wood ; having sold 8.7 cubic meters, how much remained ?

5. There are 13 blocks of marble, each containing 370.16 cu. dm.; how many cubic meters in all?

6. How many cubic meters in an excavation 13.2 m. by 18.5 m. by 8.4 m?

7. At \$1.25 a cubic meter, what will it cost to dig a cellar 6.5 m. long, 5.4 m. wide, and 2.5 m. deep ?

8. How many sters of wood in a pile of wood 2.5 m. high, 2 m. wide, and 16.5 m. long? What is the length of a pile of the same height and width containing 216 sters?

## DRY AND LIQUID MEASURE.

**366.** The unit of **Dry** and **Liquid Measure** is the *liter*, which is equal to a cubic decimeter, 1.0567 wine quarts, or .908 dry quart.

## TABLE.

					Dry Measure.	Li	quid Measure.
		1	Milliliter $\left(\frac{1}{1000} \text{ of a liter}\right)$	=	.06103 cu. in.,	or,	.0338 fl. oz.
10 ml.	=	1	Centiliter( $\frac{1}{100}$ of a liter)	=	.6103 cu. in.,	or,	.338 fl. oz.
10 cl.		1	Deciliter( $\frac{1}{10}$ of a liter)		6.1027 cu. in.,	or,	.845 gi.
10 dl.	=	1	LITER(1 liter)	=	.908 qt.,	or,	1.0567 qt.
10 <i>l</i> .		1	Dekaliter(10 liters)	=	9.08 qt.,	or,	2.6418 gal.
10 Dl.	==	1	Hectoliter(100 liters)	=	2.8375 bu.,	or,	26.418 gal.
10 Hl.	=	1	Kiloliter(1000 liters)	==	28.375 bu.,	or,	264.18 gal.

Notes.—1. The liter is commonly used in measuring wine, milk, etc., in moderate quantities. For minute quantities the centiliter and milliliter are employed; and for large quantities the dekaliter.

2. For measuring grain, etc., the hectoliter (2.8375 bushels) is commonly used.

3. Instead of the kiloliter and milliliter, it is customary to use their equals, the cubic meter and cubic centimeter.

#### EXAMPLES.

**367.** 1. How many liters in a vessel whose capacity is 1 cubic meter ?

2. What is the cost of sixteen liters of milk at 8 cents a liter?

3. How many hectoliters of wheat can be bought for \$396 at \$5.50 per hectoliter?

4. How many hectoliters of grain can be put in a rectangular bin, 4 m, long, 3.5 m, wide, and 1.2 m, high?

5. How many liters in 63.5 dekaliters? In 83.75 hectoliters?

6. At \$1.75 a liter, what is the cost of 85.6 dekaliters of wine?

7. How many hectoliters in 16 cubic meters?

. 8. How many bags, each holding 1 hectoliter, can be filled from a bin, 1.5 m. high, 2.4 m. wide, and 5 m. long?

9. A cistern 3.5 m. by 3.2 m., and 9 m. deep, will hold how many dekaliters?

10. A merchant bought 4 hectoliters of nuts at \$8.50 per hectoliter, and retailed them at 12 cents a liter; what was his profit?

#### Art. 368.]

#### WEIGHT.

**368.** The unit of weight is the *gram*, which is equal to the weight of a cubic centimeter of distilled water in a vacuum, at its greatest density  $(39.2^{\circ} \text{ F.})$ , or 15.432 grains.

## TABLE.

		1 Decigram( $\frac{1}{10}$ of a gram)	=	1.543 gr. Tr.
$10 \ dg.$	-	1 GRAM(1 gram)	=	15.432 gr. Tr.
10 g.	=	1 Dekagram(10 grams)	_	.3527 oz. Av.
10 Dg.	=	1 Hectogram(100 grams)	=	3.5274 oz. Av.
10 Hg.	=	1 Kilogram(1000 grams)	==	2.2046 lb. Av.
10 Kg.	=	1 Myriagram(10000 grams)	=	22.046 lb. Av.
100 Kilos	=	1 Quintal	=	220.46 lb. Av.
10 Q., or	1-1	1 Tonneau, ) (1000000 among)	5	2204.6 lb. Av.
1000 Kilos	$\int = 1$	or Ton J (1000000 grams)	= 5	1.1023 T.

Notes.—1. The above table is used in computing the weights of all objects from the smallest atom to the largest known body. The gram, kilogram (or kilo), and ton are principally used.

2. The gram is used in weighing letters, gold, silver, and medicines.

3. The kilogram, or kilo, like the pound, is used in weighing groceries and coarse articles. It is approximately 2<sup>1</sup>/<sub>5</sub> pounds Av.

4. The ton is the weight of a cubic meter of water, and is used in weighing very heavy articles, as coal, iron, etc.

5. The pound of Germany, Austria, and Denmark is equal to  $\frac{1}{2}$  of a kilogram; the centner, to 100 pounds, or  $\frac{1}{2}$  of a quintal.

#### EXAMPLES.

**369.** 1. What is the weight in grams of a cubic meter of water? Of a cu. dm. of water?

2. A farmer sells to A 3.716 T. of hay, to B 4.325 T., to C 8775 kilos; how many tons does he sell?

3. The U. S. 50-cent piece weighs 12.5 grams; how many can be coined from a kilogram of standard silver?

4. The U. S. 5-cent piece weighs 5 grams; how many 5-cent pieces are equivalent in weight to 12 50-cent pieces?

5. How much alloy must be used in making 1200 U.S. twentyfive-cent pieces? (See Art. 113.)

6. What is the cost of 75.6 kilos of sugar at 18 cents a kilo?

7. How many powders, each containing 6 grams, can be made from .372 kilogram ?

8. What is the weight of 10 cu. m. of ice, it being .93 as heavy as water?

## 370. TABLE OF EQUIVALENTS.

1	inch $= 2.54$ centimeters1	centimeter $= 0.3937$ inch.
1	foot = 3.048 decimeters1	decimeter = $0.328$ foot.
1	yard = 0.9144 meter1	meter = $1.0936$ yards = $39.37$ in.
1	rod = 0.5029 dekameter1	dekameter = $1.9884$ rods.
1	mile = $1.6093$ kilometers1	kilometer = $0.62137$ mile.
1	sq. inch = $6.452$ sq. centimeters1	sq. centimeter $= 0.155$ sq. inch.
1	sq. foot = $9.2903$ sq. decimeters1	sq. decimeter = $0.1076$ sq. foot.
1	sq. yard = $0.8361$ sq. meter1	sq. meter = $1.196$ sq. yards.
1	sq. rod = $25.293$ sq. meters1	are $= 3.954$ sq. rods $= 119.6$ sq. yards.
1	acre = 0.4047 hectare1	hectare $= 2.471$ acres.
1	sq. mile = $2.59$ sq. kilometers1	sq. kilometer = $0.3861$ sq. mile.
1	cu. inch = $16.387$ cu. centimeters1	cu. centimeter = $0.061$ cu. inch.
1	cu. foot = $28.317$ cu. decimeters1	cu. decimeter = $0.0353$ cu. foot.
1	cu. yard = 0.7645 cu. meter1	cu. meter $= 1.308$ cu. yards.
1	cord = 3.624 sters1	ster = $0.2759$ cord.
1	liquid quart = $0.9463$ liter1	liter = $1.0567$ liquid quarts.
1	gallon = $0.3785$ dekaliter1	dekaliter $= 2.6417$ gallons.
1	dry quart = 1.101 liters1	liter $= 0.908$ dry quart.
1	peck = 0.881 dekaliter1	dekaliter = $1.135$ pecks.
1	$bushel = 3.524 dekaliters \dots 1$	hektoliter $= 2.8375$ bushels.
1	ounce av. = 28.35 grams1	gram = 0.03527 ounce av.
1	pound av. = $0.4536$ kilogram1	kilogram = $2.2046$ pounds av.
1	pound av. $= 0.9072$ German pounds. 1	German pound = $1.1023$ pounds av.
1	ton (2000 lbs.) = $0.9072$ met. ton1	met. $ton = 1.1023 tons = 2204.6 lb. av.$
1	grain Troy = $0.0648$ gram1	gram = 15.432 grains Troy.
1	ounce $Troy = 31.1035$ grams1	gram = 0.03215 ounce Troy.
1	pound Troy = $0.3732$ kilogram1	kilogram $= 2.679$ pounds Troy.
	· · ·	

#### EXAMPLES.

371. 1. In 225 meters how many yards? How many inches?

2. Reduce 6 miles to kilometers; to meters.

3. Reduce 640 acres to hectares; to ares.

4. In 10 kilometers, how many feet? How many miles?

5. In 375.6 kilos, how many pounds?

6. How many German pounds in 225 English or U. S. pounds?

7. What is the weight of the U.S. standard silver dollar in grams? Of the trade dollar?

8. In 5000 U. S. bushels, how many hectoliters? How many dekaliters?

9. In 875 cu. yd. how many cu. m.?

- 10. In 1000 cu. m. how many cu. yd.?
- 11. Reduce 1728 gal. wine to liters; to dekaliters.
- 12. In 244 sq. m. how many sq. yd.? How many sq. ft.?
- 13. Reduce 220 oz. Av. to grams; to kilograms.

## 372. APPROXIMATE VALUES.

When no great accuracy is required, we may consider-

1 decimeter $-4$ inches. $1$ for the for ster $= 1\frac{1}{2}$ cu. yd. or $\frac{1}{4}$	coru.
1 meter $= 39$ inches. 1 liter $= 1$ quart.	
5 meters = 1 rod. 1 hectoliter = $2\frac{1}{2}$ bushels.	
1 kilometer $=\frac{5}{8}$ mile. 1 gram $=15\frac{1}{2}$ grains.	
1 square meter = $10\frac{3}{4}$ square feet. 1 kilogram = $2\frac{1}{5}$ pounds.	
1 hectare $=2\frac{1}{2}$ acres. 1 ton $=2200$ pounds.	

# APPROXIMATE RULES.

## 373. To reduce avoirdupois pounds to kilograms:

Divide by 2, and then deduct one-tenth.

Note.—Answer too small by about 8 kilos for every 1000 kilos of the result. If  $\frac{1}{11}$ , instead of  $\frac{1}{10}$ , be deducted, the answer will be too great by 2 kilos for every 1000 kilos of the result.

# **374.** To reduce avoirdupois pounds to half-kilograms, or German pounds:

#### Deduct one-tenth.

Note.—Answer too small by about 8 German pounds for every 1000 German pounds of the result. If  $\frac{1}{11}$  be deducted, the answer will be too great by 2 German pounds for every 1000 German pounds of the result.

## 375. To reduce yards to meters:

Deduct one-twelfth.

Note.—Answer too great by  $2\frac{1}{2}$  m. for every 1000 m. of the result.

# 376. To reduce square yards to square meters:

Deduct one-sixth.

Note.—Answer too small by about 3 sq. m. for every 1000 sq. m. of the result.

## 377. To reduce cubic yards to cubic meters:

Divide by 1.3.

Note.—Answer too great by about 6 cu. m. for every 1000 cu. m. of the result.

[Art. 378.

## 378. To reduce U. S. gallons to liters :

Multiply by 4, and then subtract one-twentieth (5 per cent.). Note.—Answer too great by about 4 l. for every 1000 l. of the result.

## 379. To reduce U. S. bushels to hectoliters:

Divide by 3, and then add one-twentieth (5 per cent.). NOTE.—Answer too small by about 7 hl. for every 1000 hl. of the result.

**380.** To reduce kilograms to avoirdupois pounds: Multiply by 2, and then add one-tenth. Note.—Answer too small by about 2 lb. for every 1000 lb. of the result.

381. To reduce German pounds, or half-kilograms, to avoirdupois pounds:

Add one-tenth.

Note.—Same error as in Art. 380.

## 382. To reduce meters to yards:

Add one-twelfth and 1% of the original number.

Note.—Answer too small by only  $\frac{1}{13}$  yd. for every 1000 yd. of the result. Dealers in dry goods add only  $\frac{1}{13}$  in reducing meters to yards, and thus make the result too small by about  $9\frac{1}{3}$  yd. for every 1000 yd. of the result.

If  $\frac{1}{11}$  be added, the answer will be too small by about  $2\frac{1}{2}$  yd. for every 1000 yd. of the result. If  $\frac{1}{10}$  be added, the answer will be too great by about 6 yd. for every 1000 yd. of the result.

## 383. To reduce square meters to square yards:

## Add one-fifth.

Note.—Answer too great by about 3 sq. yd. for every 1000 sq. yd. of the result.

## 384. To reduce cubic meters to cubic yards:

Multiply by 1.3.

Note.—Answer too small by about 6 cu. yd. for every 1000 cu. yd. of the result.

## 385. To reduce liters to U.S. gallons:

Multiply by 2.11, and then divide by 8.

NOTE.—Answer too small by about 1.7 gal. for every 1000 gal. of the result.

## 386. To reduce hectoliters to U.S. bushels:

Multiply by 3, and then subtract one-twentieth (5 per cent.). . NOTE.—Answer too great by about 4 bu. for every 1000 bu. of the result.

#### Art. 387.]

## REVIEW EXAMPLES.

**387.** 1. Add 17 $\frac{4}{5}$ ,  $26\frac{1}{2}$ ,  $35\frac{2}{5}$ ,  $48\frac{3}{4}$ , and  $8\frac{7}{18}$ ; multiply the sum by 59; subtract  $2309\frac{7}{12}$  from the product; and divide the remainder by  $162\frac{2}{3}$ .

2. Divide fourteen, and twenty-five hundredths by one hundred twenty-five thousandths; add nineteen, and sixty-four hundredths to the quotient; and multiply the sum by eight, and five tenths.

3. Find the time by Compound Subtraction and in exact days from March 24 to Sept. 18.

4. How many lengths of pipe, each 16 ft. (') 3 in. (") long, will be required for a well 130 ft. deep?

5. A horse trots a mile in 2 min. 45 sec. How many feet is that per second?

6. A grass plot 13 ft. by 54 ft. is surrounded by a stone walk  $1\frac{1}{2}ft$ . wide. The stone walk is surrounded by a gravel road  $7\frac{1}{2}ft$ . wide. How many square feet are covered by the grass, the stone, and the gravel respectively? (Make diagram.)

7. What is the cost of 15669 pounds meal at \$1.10 per cwt.?

8. What is the cost of 16450 pounds of hay at \$15.50 per ton?

9. How many square rods in a triangular piece of land, 360 rd. long and whose perpendicular width is 240 rd.?

Note.—To find the area of a triangle, take one-half the product of the length (base) and the height or width (altitude).

10. How many square feet in the gable of a house, 40 ft. long and 24 ft. high ?

11. How many feet of siding would be required for a house 40 ft. long, 24 ft. wide, 18 ft. high, with two gables each 24 ft. wide and 12 ft. high, adding one-fifth for the lap and waste in cutting?

12. How much will it cost to make an excavation, 40 ft. long, 30 ft. wide, and 9 ft. deep, at 32c. per cubic yard.

13. How many feet of 2-inch plank, making no deduction for the corners, would be needed to build a rectangular tank, without a cover, 10 ft. long,  $6\frac{1}{2}$  ft. deep, 8 ft. wide ?

14. The circumference of any circle is equal to the diameter multiplied by 3.1416 (about  $3\frac{1}{7}$ ). Find the circumference of a circle, whose diameter is 5 feet.

15. The area of any circle equals the square of the radius multiplied by 3.1416 (34), or the square of the diameter multiplied by .7854. What is the area of a circle whose diameter is 6 ft? Whose radius is 5 ft?

16. How many feet of 2-inch plank would be required to make a cylindrical cistern without a cover, 7 ft. in diameter and 8 ft. high ?

17. How many pounds in 16 T. 3 gr. 18 lb. (Long Ton Table)?

18. How many quarts in 3 bbl. 24 gal. cider ?

19. In 27318 pounds of corn, how many bushels? What is the value of the same at  $48\frac{3}{4}$  cents per bushel?

20. What is the value of 27318 pounds of corn, at 87.1 cents per cental ?

Note.—Examples 19 and 20 illustrate the present and the centar systems of buying and selling produce, and show the calculations saved by using the latter.

21. Paid \$222.75 for boards at \$13.50 per M.; how many feet were purchased ?

22. What is the value of 27315 ft. of lumber at \$12 per M.?

23. A quartermaster purchased 75000 pounds of corn, at  $31_{\frac{1}{2}}$  cents per bushel; 32113 pounds of oats, at  $32_{\frac{1}{2}}$  cents per bushel; and 79500 pounds of hay, at  $\$22.37_{\frac{1}{2}}$  per ton (2000 pounds). What was the total cost of the purchase?

24. A farmer sold 18360 pounds of corn, at 64 cents per cental; 22450 pounds of oats, at 94 cents per cental; and 36650 pounds of hay, at \$1.31 per cental. How much was realized from the sale?

25. Reduce £19 16s. 9d. to the decimal of a pound.

26. If £1 sterling is worth \$4.87, what is the value of £225 18s. 6d.?

27. From £16 12s. 9d. deduct .05 of itself.

28. What is the value of 20 yd. silk at 10s. 6d. per yard?

29. The difference in the local time of two places is 3 hr. 43 min. 12 sec.; what is the difference in longitude?

30. What is the capacity in liters of a cistern 25 meters long, 2.2 meters wide, and 3 meters deep ?

31. The specific duty on Brussels carpet is 44 cents per square yard ; what is the duty per square meter ?

32. The duty on tallow candles is  $2\frac{1}{2}$  cents per pound; what is the duty per kilogram ?

# ALIQUOT PARTS.

**388.** An Aliquot Part of a number or quantity is a number that will divide it without a remainder; as 20 of 60,  $12\frac{1}{2}$  of 100, 4 of 12, etc.

Any fraction having 1 as its numerator is an aliquot part of a unit.

Many of the ordinary business computations can be shortened by the use of aliquot parts.

#### EXAMPLES.

**389.** 1. Find the cost of 217 pounds of sugar at  $8\frac{3}{4}c$ . per pound? At  $9\frac{3}{5}c$ ? At  $7\frac{5}{5}c$ ?

OPERATION. 91ヴ	
.083	
1736	Note. $-\frac{3}{4} = \frac{1}{2} + \frac{1}{4} (\frac{1}{2} \text{ of } \frac{1}{2}).  \frac{3}{5} = \frac{1}{4} + \frac{1}{5} (\frac{1}{2} \text{ of } \frac{1}{4}).$
$109 \left(\frac{1}{2}\right)$	$\frac{5}{8} = \frac{1}{2} + \frac{1}{8} \left( \frac{1}{4} \text{ of } \frac{1}{2} \right).  \frac{7}{8} = \frac{1}{2} + \frac{1}{4} + \frac{1}{8}.$
$54 (\frac{1}{4} = \frac{1}{2} \text{ of } \frac{1}{2})$	
18.99	

Find the cost of

2. <sup>3</sup>/<sub>4</sub> doz. elbows at \$2.75 per dozen.

3. 141 lbs. raisins at 85c. per pound.

4. 200 *lbs.* lead at  $6\frac{3}{4}c$ . per pound.

5. 228 lbs. putty at 23c. per pound.

6. 207 lbs. currants at 54c. per pound.

7.  $102_{12}^{5}$   $(\frac{1}{4} + \frac{1}{6})$  ft. tubing at 16c. per foot.

8. 877 *lbs.* paper at  $3\frac{3}{4}c$ . per pound.

9. 102 *lbs.* oatmeal at  $3\frac{3}{5}c$ . per pound.

10. 700 lbs. soap at  $5\frac{3}{4}c$ . per pound.

11. 503 lbs. ham at 10<sup>3</sup>/<sub>4</sub>c. per pound.

12. 644 lbs. lard at 113c. per pound.

13. 2957 lbs. sugar at  $8\frac{5}{16}c$ .  $(\frac{1}{4} + \frac{1}{4} \text{ of } \frac{1}{4})$  per pound.

390. Aliquot parts of 100.

$2\frac{1}{2} = \frac{1}{40}$ .	$12\frac{1}{2} = \frac{1}{8}$ .	$37\frac{1}{2} = \frac{1}{4} + \frac{1}{8} \left(\frac{1}{2} \text{ of } \frac{1}{4}\right).$
$3\frac{1}{3} = \frac{1}{30}$ .	$16\frac{2}{3} = \frac{1}{6}$ .	$62\frac{1}{2} = \frac{1}{2} + \frac{1}{8} (\frac{1}{4} \text{ of } \frac{1}{2}).$
$4 = \frac{1}{25}$ .	$20 = \frac{1}{5}$ .	75 = $\frac{1}{2} + \frac{1}{4} (\frac{1}{2} \text{ of } \frac{1}{2}).$
$5 = \frac{1}{20}$ .	$25 = \frac{1}{4}$ .	$87\frac{1}{2} = \frac{1}{2} + \frac{1}{4} + \frac{1}{8}.$
$6\frac{1}{4} = \frac{1}{16}$ .	$33\frac{1}{3} = \frac{1}{3}$ .	$18\frac{3}{4} = \frac{1}{8} + \frac{1}{16} (\frac{1}{2} \text{ of } \frac{1}{8}).$
$10 = \frac{1}{10}$ .	$50 = \frac{1}{2}$ .	$31\frac{1}{4} = \frac{1}{4} + \frac{1}{16} (\frac{1}{4} \text{ of } \frac{1}{4}).$

Note.—In the following commercial problems, use as few figures as possible.

#### EXAMPLES.

**391.** 1. Find the cost of 13756 pounds of meal at \$1.05 per cwt.

OPERATION.

137.56ANALYSIS.—At \$1 per cwt. the cost would be \$137.56.6.88 $5c. = \frac{1}{20}$  of \$1. To divide by 20, divide by 2 and place the quotient figures one place to the right.

144.44

2. Find the value of 16345 *lbs.* of feed at \$1.10 per *cwt.*  $(10c = \frac{1}{10} \text{ of } \$1).$ 

3. What is the cost of 12 doz. hats at \$4.12 $\frac{1}{2}$  ( $\frac{1}{3}$ ) per doz.?

4. Find the cost of  $471\frac{59}{158}(1+\frac{1}{2})$  bushels of corn at 41c.

5. What is the cost of 96 doz. buttons at \$1.75  $(\frac{3}{4} = \frac{1}{2} + \frac{1}{4})$  per dozen ?

6. Find the cost of  $711\frac{20}{32}$   $(\frac{1}{2}+\frac{1}{3})$  bushels oats at 39c. per bushel.

7. Find the cost of 24 boxes note paper at  $16\frac{2}{3}c$ . per box.

8. Find the cost of 24116 lbs. bran at \$1.20 per cwt.

9. Find the cost of 1750 lbs. soap at 51c. per pound.

10. Find the cost of 131 *lbs.* coffee at  $16\frac{1}{2}c$ . per pound.  $(16\frac{1}{2} = 12\frac{1}{2} + 4.)$ 

11. Find the cost of 601 lbs. crackers at 121c. per pound.

12. Find the cost of 4880 lbs. feed @ 75c. per cwt.

13. Find the cost of 20 half-barrels fish at \$4.25 per halfbarrel. At \$5.35  $(1 + \frac{1}{10})$  per half-barrel.

14. Find the cost of 75 books at 25c. each.

15. Find the cost of 36 pairs shoes at \$2.25 per pair. At \$2.50 per pair.

16. Find the cost of 3019 lbs. bran at  $62\frac{1}{2}c$ . per cwt., and 24375 lbs. feed at \$1.05 per cwt.

# PERCENTAGE.

**392.** Percentage is a term applied to all operations in which 100 is used as the basis of computation.

It is also the name given to any number of hundredths of a number.

**393.** Per Cent. (%) is an abbreviation of the Latin per centum, meaning on or by the hundred.

Thus, 5% means 5 of every hundred, or 5 hundredths  $(\frac{5}{100}, \text{ or } .05)$ .

**394.** Any *per cent*. may be expressed in the form of a *decimal* or *fraction*.

Thus 5 per cent. = 5% = 5 hundredths =  $.05 = \frac{1}{5} \frac{5}{60} = \frac{1}{20}$ . The first two forms are used in the statements of questions; the others in the operations.

**395.** In percentage, three elements are considered, viz: the *Base*, the *Rate*, and the *Percentage*. Any two being given, the other can be found.

**396.** The **Percentage** is the result obtained by taking a certain number of hundredths of a number.

**397.** The **Base** is the number of which a certain number of hundredths are taken.

**398.** The **Rate** is the number of hundredths, or the number per cent.

Thus, in the statement, 6% of 300 is 18, the Percentage is 18, the Base 300, and 6 per cent. (.06) is the Rate.

**399.** Applications of Percentage.—The principles of percentage are applied to many of the most common business transactions. Among the most important of these are Trade Discounts, Commission, Insurance, Profit and Loss, Duties, Interest, and Exchange. 400. To find the percentage, the base and rate being given.

Ex. What is 6 per cent. of 300?

OPERATION.	ANALYSIS6% means 6 hundredths. 6% of 300 is
300 Base.	equivalent to .06 of (or times) 300. $.06 \times 300 = 18$ . The
.06 Rate.	percentage is the product of two factors, the base and
8 00 Percentage	the rate.

To find 1% of any number, place the point two places to the left.

**401.** RULE.—1. To find the percentage, multiply the base by the rate expressed decimally.

#### EXAMPLES.

	402. What is		What is		What is
1.	$.03 \times 1728$ ?	6.	8% of \$414?	11.	16% of \$375.60?
2.	.16 times 375 ?	7.	.08 of \$716?	12.	8% of \$414.60?
3.	4% of 448?	8.	$1.12 \times \$575$ ?	13.	6% of \$875.75?
4.	6 per cent. of 387?	9.	107% of \$385?	14.	113% of \$913.25?
5.	.06 of 945 ?	10.	9% of \$456?	15.	32% of \$485.50?

16. What is the difference between  $2\frac{1}{2}$ % of \$16000 and 5% of \$8475 ?

17. A merchant bought goods amounting to \$375.60, and sold them so as to gain 30% of the cost; how much did he gain?

18. A lawyer collected \$2875, and charged 5% for his services; how much did he retain for his services, and how much did he pay over? The amount paid over is what per cent. of the amount collected ?\*

19. An agent sells a house and lot for \$16450, and receives 2% for his services; what does he pay to the owner of the property?

20. What is the duty, at 25% of the value, on twelve watches worth \$75 each ?

21. Jan. 10, a merchant buys a bill of goods amounting to \$876.40 on the following terms: 4 months, or less 6% if paid in 10 days. How much would settle the bill Jan. 18?

22. A merchant, failing in business, pays 43% of his indebtedness. He owes A \$3750, and B \$6280. How much does he pay each?

<sup>\*</sup> In order to prepare the student for examples in which the conditions are the reverse of those in this example, the teacher should ask oral questions similar to the above in all examples in which an amount or difference is involved.
23. A commission merchant sold 450 barrels of flour at \$5.30 per barrel. How much should he send to the miller, if he charges  $2\frac{1}{2}$  per cent. for making the sale?

24. A manufacturer's list price of cans is \$2.50 per dozen. He sells a dealer 48 dozen at a discount of 30%. How much does he receive for them?

25. A broker sells merchandise amounting to \$916.64, at a commission of  $1\frac{1}{2}$  per cent. What is his commission?

OPERATION.

9.166 1%.	ANALYSIS1% of \$916.64 is \$9.166, to which add 1	
1.146 \$%.	of itself as in the operation. (See Art. 389.)	

10.312 13%.

According to the above method, find

26.	1% of \$375.60.	29.	$1\frac{3}{8}(\frac{1}{4}+\frac{1}{8})\%$ of \$287.96.
27.	$\frac{3}{4}(\frac{1}{2}+\frac{1}{4})\%$ of \$875.	30.	11% of \$5275.
28.	11% of \$1176.40.	31.	13% of \$3075.75.

32. A contracts to make an excavation containing 3456 cubic yards, at  $28\phi$  per cubic yard for earth, and \$1.20 per cubic yard for rock. When completed, it is found that 16% is rock, and the remainder earth. How much does he receive for the work?

**403.** When the rate is an aliquot part of 100, it is generally more convenient to use the equivalent fraction. Thus,

50%	=.50	$=\frac{1}{2}$ .	$16\frac{2}{3}\% = .16\frac{2}{3} = \frac{1}{6}.$	$6\frac{1}{4}\% = .06\frac{1}{4} = \frac{1}{16}.$
33 <u>1</u> %	$=.33\frac{1}{3}$	$=\frac{1}{3}$ .	$12\frac{1}{2}\% = .12\frac{1}{2} = \frac{1}{8}.$	$5\% = .06 = \frac{1}{20}$
25%	=.25	$=\frac{1}{4}$ .	$10\% = .10 = \frac{1}{10}.$	$3\frac{1}{3}\% = .03\frac{1}{3} = \frac{1}{30}$
20%	=.20	$=\frac{1}{5}$ .	$8\frac{1}{3}\% = .08\frac{1}{3} = \frac{1}{12}$ .	$2\frac{1}{2}\% = .02\frac{1}{2} = \frac{1}{40}$ .

#### EXAMPLES.

	<b>404</b> . What is	What is	What is
1.	1 of 1728.?	5. 33 <sub>3</sub> % of \$375?	9. 50% of \$487.20 ?
2.	25% of 3472?	6. 12½% of \$848?	10. 5% of \$9742?
3.	.25 of 6418?	7. $2\frac{1}{2}\%$ of \$6480?	11. 10% of \$1764.30?
4.	<sup>25</sup> / <sub>105</sub> of 7264?	8. 20% of \$9875?	12. $37\frac{1}{2}\%$ $(\frac{3}{8})$ of \$875.60?

13. From a bill of goods amounting to \$475.60, 5% is deducted for cash. What is the net amount of the bill ?

OPERATION.

51 82

14. A commission merchant pays \$2375.40 for a quantity of grain, and charges  $2\frac{1}{2}$ % for his services. What is the total cost ?

15. Mr. B's tax is \$175.60. If the collector is allowed 5% additional, what is the total amount paid ?

16. The gross amount of a bill of tinware is \$97.40. What is the net amount, if the trade discount is  $33\frac{1}{3}$ ?

17. A house is sold for \$16400, and 25% of the purchase money is allowed to remain on bond and mortgage. What is the amount of the mortgage ?

18. A house worth \$7200 is insured for  $62\frac{1}{2}\%$  ( $\frac{5}{8}$ ) of its value. What is the amount of the insurance ? What is its cost at  $\frac{3}{2}\%$  ?

# 405. To find the base, the percentage and rate being given.

Ex. 18 is 6% of what number.

OPERATION.	ANALYSIS.—The question "18 is 6% of what num-
Rate. Percentage.	ber?" is equivalent to " $18 = .06 \times$ what number?" If
.06) 18.00	18 is the product of two factors and one of the factors is.
Base. 300	.06, the other may be found by dividing 18 by .06.

Or, since the Percentage = the Base  $\times$  the Rate, the Base = the Percentage  $\div$  the Rate.

Or, if 18 is 6% of a certain number, 1% is  $\frac{1}{5}$  of 18, or 3; and the number, or 100%, is 100 times 3, or 300.

Note.—The student should remember that the Percentage = the Base  $\times$  the Rate, and that when the Percentage and one of its factors are given, in the operation of finding the other, the Percentage becomes the dividend and the given factor, the divisor. If the relation between the given terms is indicated in the form of an equation, the student will have no difficulty in determining which number should be the divisor in solving the great variety of examples which occur in percentage and its applications.

**406.** RULE.—To find the base, divide the percentage by the rate expressed decimally.

#### EXAMPLES.

**407.** Find the unknown term in the following equations:

- 1. 48 = 6 times —.
- 2.  $48 = .06 \times ---$ .
- 3. 324 is 6% of ——.
- 4. 448 = .08 of —.
- 5. .04 of = 375.
- 6. 6% of 380 = ---.
  - 7. 72 is 4% of ——.
  - 8.  $184 = .23 \times ---$
  - 9. 175 is .07 times -----,
  - 10.  $$576 \times .06 = ---$ .

#### Art. 407.]

11.	\$324 = 8% of —.	15.	$\$144 = \frac{1}{5}$ of
12.	$144 = .16 \times$	16.	$12\frac{1}{2}\%$ of $\$475 =$
13.	52% of \$440 =	17.	\$325 is 13% of —.
14.	\$875 = 25% of	18.	\$48.60 is 2½% of —.

19. The product of two factors is 75; if one of the factors is .03, what is the other factor ?

20. The percentage is 60, and the rate  $2\frac{1}{2}\%$ ; what is the base? NOTE.—Use the fractional method when convenient. See Art. **402**.

21.	\$18.08 are 5% of what?	125.	$165  ft.$ are $33\frac{1}{3}\%$ of what ?
22.	\$324 are 10% of what ?	26.	£240 are $3\frac{1}{3}\%$ of what ?
23.	$37.56$ are $2\frac{1}{2}\%$ of what?	27.	\$12.25 are 64% of what?
24.	\$17.28 are 25% of what?	28.	\$96 are $\frac{5}{8}\%$ of what?

29. Mr. A invests 42% of his capital in real estate, and has \$53070 left; what is his capital?

ANALYSIS.—100% of any amount is the amount itself. If 42% of his capital is invested in real estate, the remainder, \$53070, must be 58% (100% - 42%) of his capital.

30. A has 35% of his property invested in stocks, 10% in horses and cattle, 18% in grain, and the remainder, which is \$24235, in real estate. What is the total value of his property? 31. A horse was sold for \$658, which was  $16\frac{2}{3}\%$  more than it cost; what was the cost?

NOTE.—The cost of the horse was  $\frac{100}{100}$ , or 100% of itself; since the gain was  $16\frac{2}{3}\%$  of the cost, the selling price (the cost plus the gain) was  $116\frac{2}{3}\%$  of the cost. \$658 is  $116\frac{2}{3}\%$  of what number?

32. 25% of itself is 500? 35 5% of itself is \$307 80?	
33. 8% of itself is \$1004.40? 36. 40% of itself is 3726?	
34. 125% of itself is 999? 37. 25% of itself is \$342.60	62.0

38. A merchant sells goods for 5555.50, which is 10% more than they cost him. What did they cost?

39. In a cargo of oranges, consisting of 4275 boxes,  $33\frac{1}{3}\%$  are damaged. How many are damaged ?

40. A bankrupt whose assets are \$23625, pays 40% of his liabilities. What are his liabilities ?

41. A farm was sold at a commission of  $1\frac{1}{4}$ %. If the agent's commission was \$80.80, what was the price of the farm?

# 408. To find the rate, the percentage and base being given.

Ex. 18 is what per cent. of 300?

OPERATION.	ANALYSIS.—The question "18 is what per
Base. Percentage. Rate.	cent. of 300" is equivalent to " $18 = how$ many
300 ) 18.00 ( .06	hundredths times 300." If 18 is the product of
	two factors, and one of the factors is 300, the

other may be found by dividing 18 by 300. To find the rate per cent., the quotient must be produced in hundredths.

Or, since the Percentage = the Base × the Rate, the Rate = the Percentage + the Base,  $18 \div 300 = .06$  (6%), the required per cent.

Or, 18 is  $\frac{18}{800}$  or  $\frac{3}{50}$  of 300.  $\frac{3}{50} = \frac{6}{100}$ , or 6%.

**409.** RULE.—To find the rate, divide the percentage by the base.

Note.—In finding the rate, to produce a quotient of hundredths, make the decimal places of the dividend exceed those of the divisor by 2.

#### EXAMPLES.

**410.** *1.* The product of two numbers is 375; if one of the numbers is 30000, what is the other number? Express the answer in hundredths.

Find the unknown term in the following equations :

2.	75 is what per cent. of 375?	6. \$12.50 is what % of	\$1000?
3.	144 = .** times 1728.	7. \$232.50 is what % of	\$3720?
4.	$72 = .** \times 3456.$	8. \$60.40 is what % of	\$2416?
5.	165 ft. is what % of 5280 ft.?	9. \$21.20 is what % of	\$1484?

10. The assets of a bankrupt are \$27387, and his liabilities \$82161; what % of his indebtedness can he pay ?

 $\sqrt{11}$ . A merchant paid for goods \$345 and sold them for \$258.75; the loss is what % of the cost ?

12. If a paymaster receives \$150000 from the treasury, and fails to account for \$225 thereof, what is the percentage of loss to the government?

13. If the rate is 20% and the percentage 440, what is the base?

14. \$640 being increased by a certain % of itself equals \$720; required the rate %.

15. A person owing me \$2092, pays only \$1150.60. What  $\frac{7}{6}$  do I lose on the debt?

#### PERCENTAGE.

16. A house, insured for \$16500 in several companies, is damaged by fire to the extent of \$7260. What % of its insurance will each company pay?

17. A tax of \$18480 is levied upon a township whose valuation is \$3,696,000. What is the rate of the tax, and what tax should a man pay whose assessment is \$8500 ?

 $\sim$  18. The annual interest on a mortgage of \$7500 is \$337.50. What is the rate per cent.?

19. A merchant with a capital of \$24000 gains \$3840 in one year. His gain is what per cent. of his capital ?

20. A bankrupt has liabilities to the amount of \$12600 and his assets are only \$7087.50. What % dividend will he pay ?

21. The dividend of a manufacturing company, whose capital stock is \$125000, is \$6000. What % does it pay ?

22. A man's salary is \$1600 per year and his living expenses \$1300. What % of his salary does he save ?

23. A house cost \$8000, and rents for \$750 per year. If the taxes and other expenses are \$230 per year, what % does it pay on the investment?

 $\sqrt{24}$ . The cost of insuring a cargo for \$8500 is \$63.75. What is the rate of the insurance?

25. 1 meter = 1.0936 yards. The meter is what % greater than the yard ?

26. A man subscribes for 36 shares (\$100 each) of a gas company. He pays in \$1980. What % is still due?

27. The Avoirdupois pound (334) is what % greater than the Troy pound (336)?

28. A merchant bought a quantity of goods for \$425. Being damaged he sold them for \$340. What % of the cost did he lose?

29. A horse and wagon are worth \$600. What is the value of each, if the wagon is worth  $87\frac{1}{2}\%$  as much as the horse ?

30. A man bought a watch for \$160 and sold it for \$180. His gain was what % of the cost ?

31. A tea merchant mixes 40 *lbs.* tea at 45*c.* per pound with 50 *lbs.* at 27*c.* per pound. He sells the mixture at 42*c.* per pound. What % profit on the cost does he make ?

32. A consignment of flour was sold for \$3148, of which 3124.39 were the net proceeds. What was the rate % of the commission?

33. Mr. A's house is worth \$12500. He pays \$30 for insuring it for  $\frac{2}{5}$  of its value. What per cent. does he pay ?

[Art. 411

## REVIEW EXAMPLES.

**411**. *1*. What is 116% of 1200?

2. 144 is 120% of what number ?

3. 375 is what % of 300?

4. Find 95% of \$1260.

5. Of what number is 275, 100%?

6. \$187.50 is 21% of what?

7. What will be the charge for insuring a house for \$4500 at  $\frac{3}{4}\%$ ?

8. A merchant buys one gross jars for \$36. At what price must he sell them apiece to gain 20% on the cost?

9. The assets of a bankrupt are \$67850, which sum is 43% of his debts. What are his debts?

10. A tax collector, whose average commission was 31%, received \$892.08 for his services. How much did he collect ?

11. At what price must an article, which cost 4.80, be sold so as to gain 16% of the cost?

12. A clerk spends 48% of his income, and saves \$598. What is his income ?

13. A's property is assessed at \$7500, and the rate of taxation is \$2.165 on \$100. What is his tax, including a commission of 1%?

14. At  $1\frac{3}{8}$ %, the premium for insuring a factory was \$178.20. Find the amount of the insurance.

15. A bank collected a draft of \$9375.16. What were the proceeds, the charge for collection being  $\frac{1}{2}\%$ ?

16. A consignment of cheese was sold for \$375.60, of which \$365.27 were the net proceeds. What was the rate of the commission?

17. A commission merchant sold 24160 pounds of leather at  $29\frac{3}{4}$  cents a pound, paid transportation \$60.40, cartage \$20, his commission being  $2\frac{1}{2}$ %, and his charge for inspection \$20. What were the net proceeds?

18. A bankrupt who is paying 36% of his debts, divides among his creditors \$44442. What do his debts amount to, and how much does he pay a creditor whom he owes \$3648?

19. A merchant buys a bill of dry goods, Apr. 16, amounting to \$6377.84, on the following terms: 4 months, or less 5% 30

#### Art. 411.]

days. How much would settle the account May 16? The amount paid May 16, is what per cent. of the full amount of the bill? The above discount is equivalent to what rate per cent. per annum?

20. Mar. 16, a merchant buys a bill of goods amounting to \$2475 on the following terms: 4 months, or less 5% if paid in 30 days. Apr. 15, he makes a payment of \$1000, with the understanding that he is to have the benefit of the discount of 5%. With what amount should he be credited on the books of the seller? How much would be due July 16, the expiration of the 4 months?

Note.—As in Ex. 19, the amount paid within 30 days is 95% of that part of the bill which it settles or cancels.

21. A bought a bill of merchandise July 24, 1879, amounting to \$6287.45 on the following terms: 6 months, or less 4% 30 days. He paid on account Aug. 23, 1879, \$5000, with the understanding that the payment would cancel an equitable amount of the bill. How much was due Jan. 24, 1880?

22. Paid for transportation \$664.95 on an invoice of goods amounting to \$8866. What per cent. was the value of the goods thereby increased ? What per cent. must be added to the invoice cost to make a profit of 20% on the full cost ?

23. What is 3% of £247 13s. 6d. ?

	OPERATION		ANALYSIS.—Multiply the number of each de-
	£ 8.	d.	nomination by .03, as in the margin, and then re-
	247 13	6	duce the decimal parts to integers of lower denom-
		.03	inations ( <b>289</b> ).
£	$\begin{array}{c}7 .41  .39\\ \underline{20}\end{array}$	.18	Or, reduce shillings and pence to the decimal of a pound (see note, Ex. 12, Art. 342), take the re- quired per cent., and reduce the decimal result to
<i>s</i> .	8 .59		lower denominations. Thus,
	12		£247 13s. $6d. = £247.675$
d.	7.26		$\pounds 247.675 \times .03 = \pounds 7.43025 = \pounds 7 8s. 7d.$
			When the rate per cent. is an aliquot part of

100, use the equivalent fraction (403). Thus, 5% of £247 13s.  $6d. = \frac{1}{20}$  of £247 13s.  $6d. = \pounds 12$  7s. 8d.

- 24. Find 3% of £384.
   25. Find 6% of £440 16s.
   26. Find 5% of £375.
   27. Find 24% of £64 16s.
- 28. Find 4% of £75 12s. 6d. 29. Find 10% of £37 8s. 9d.
- 30. 16s. is 21% of what?
- 31. £1 8s. 4d. is 4% of what?

## PROFIT AND LOSS.

412. Profit and Loss treats of the gains (profits) and losses which arise in business transactions.

The profit or loss is always estimated on the cost price, or the amount invested. Discounts are reckoned on the marked or asking price. (See Art. **415**.)

413. The difference between the cost of goods and the price at which they are sold is a profit or a loss,—profit if the selling price is the greater, loss if the cost is the greater.

#### EXAMPLES.

**414.** 1. A man purchased a horse for \$250, and sold it at a gain of 16%. What was the gain? (Gain =  $.16 \times \text{cost.}$ )

2. A merchant sold goods that cost \$325 at an advance of 12%; what was the selling price? (Gain =  $.12 \times \text{cost}$ , and selling price = cost + gain; or, selling price =  $1.12 \times \text{cost}$ .)

. 3. Bought a farm for \$3600, and sold it at an advance of 25%; what was the gain ?

Note.—If, as in the above example, the rate per cent. is an aliquot part of 100, it is more convenient to use the equivalent fraction (403). Thus,  $25\% = .25 = \frac{1}{4}$ ; gain =  $\frac{1}{4}$  of cost.

4. Cloth is bought at \$6 per yard, and sold at a loss of 20%. What is the selling price ? (Selling price =  $\frac{4}{2}$  of cost.)

5. Bought a house for 3475; at what price must it be sold to gain 36%?

6. Purchased flour at \$6.25 per barrel; at what price must it be sold to gain 20%?

7. If I buy hats at \$27 per dozen, at what price must I sell them apiece to gain 334%?

8. A factory which cost \$8775 was sold at a gain of 16%. What was received for it?

9. If silk costs 1.68 per yard, and is sold at an advance of  $12\frac{3}{7}$ , what is the profit per yard?

10. A merchant purchased goods to the amount of \$8735, and sold them at a loss of 12%; what was his loss ?

11. Bought 125 barrels of flour for \$600. If sold at an advance of 15%, what was the profit per barrel?

12. A lot of dry goods was sold at an advance of 18%. If the gain was \$436.50, what was the cost? (Gain =  $.18 \times \text{cost}$ ; hence, gain  $\div .18 = \text{cost.}$ )

13. A farm was bought for \$7200, and sold at a gain of \$900; what was the gain per cent.? (Gain = gain  $\% \times \text{cost}$ ; hence, gain  $\% = \text{gain} \div \text{cost.}$ )

14. A man paid for merchandise \$875, and sold it for \$1015; what per cent. did he gain?

15. A man paid for merchandise \$1015, and sold it for \$875; what per cent. did he lose?

16. Find the rate % of profit on goods bought for \$324 and sold for \$364.50.

17. A painting was sold for \$2343, at a gain of 32%; what was the cost? [Selling price = 1.32 (100% + 32%) × cost; hence, cost = selling price  $\div 1.32$ .]

18. Find the cost of goods sold at an advance of  $12\frac{1}{2}\%$ , being a profit of \$76.

19. How much was paid for a farm sold for \$9878, at 12% below cost?

20. What is the profit on iron sold for \$4520, at an advance of 13% on cost?

21. What is the selling price of tea which cost 32 cents per pound and is sold at a profit of  $37\frac{1}{2}\%$ ?

22. Sold drugs for \$168, at an advance of 75%; what was the profit?

23. A merchant sold for \$2576 a lot of dry goods for which he paid \$3360. What was the per cent. of loss?

24. A mixture is made of 1 gallon of wine at 50 cents a gallon, 3 at 90 cents, 4 at \$1.20, and 12 at 40 cents. What per cent. would be gained by selling the mixture at \$1.60 a gallon?

25. If, by selling tea at  $47\frac{1}{2}$  cents per pound, 1 lose 5%, at what price must I sell it to gain 15%?

26. If, by selling goods for \$126, I lose 16%, what per cent. would I have lost or gained if I had sold them for \$168?

27. A merchant's price is 25% above cost price. If he allows a customer a discount of 12% on his bill, what per cent. profit does he make?

28. If cloth, when sold at a loss of 25%, brings \$5 per yard, what would be the gain or loss per cent. if sold at \$6.40 per yard?

29. Goods that cost \$168 are sold at an advance of 25%; what is the selling price ?

30. At what price must ribbon be sold per yard so as to gain 20%, if 22½ yards cost \$6.75 ?

31. A merchant gave \$25000 for seven houses. What per cent. does he gain by selling them at \$7000 each?

32. A woman buys a certain number of apples at the rate of 3 for 1 cent, and as many more at the rate of 2 for 1 cent. What per cent. does she gain or lose, if she sells them at the rate of 5 for 2 cents ?

33. Eggs are bought at 27 cents per dozen, and sold at the rate of 8 for 25 cents. What is the per cent. of profit ?

34. A merchant by selling goods for \$364, loses 9%. For what ought they to be sold to gain 8%?

35. A drover bought 160 sheep for \$400, and sold  $\frac{3}{4}$  of them at \$2.25 each. At what price must he sell the remainder so as to gain 10% on the whole?

36. A merchant sells goods to a customer at a profit of 60%, but the buyer becoming bankrupt pays only 70% on the dollar. What % does the merchant gain or lose by the sale ?

37. If a merchant adds to the cost price of his goods a profit of  $12\frac{1}{2}$ %, what is the cost of an article which he sells for \$7.20?

38. Sold a horse at a gain of  $33\frac{1}{3}\%$ , and with the proceeds purchased another horse, which I sold for \$120, at a loss of 20%. What was the gain or loss ?

39. A merchant's retail price for boots is \$4.75 per pair, by which he makes a profit of  $33\frac{1}{3}\%$ . He sells to a wholesale customer at a discount of 20% from the retail price. What per cent. does he gain or lose, and what does he receive per pair?

40. 40 head of cattle weighing 52770 pounds are purchased in Chicago at \$4.80 per *cwt.*, and are sold in New York at  $10\frac{1}{2}$  cents per pound, to dress 56 pounds to the hundred-weight. What was the total cost? The total selling price? What is the gain per cent., making no allowance for transportation?

Note.—The quantity bought or sold does not affect the gain or loss per cent.

41. A speculator sold two building lots for \$4800 each. On one he gained 20%, and on the other he lost 20%. Did he gain or lose, and how much ?

## DISCOUNTS.

415. It is customary in many branches of business for manufacturers and dealers to have fixed price-lists of certain kinds of merchandise; and when the value changes, instead of changing a long price-list, the rate of discount is changed. The fixed price is called the *List Price*, and the discount allowed the *Trade Discount*.

Books are usually sold by publishers and jobbers at certain discounts from the retail prices.

416. Many kinds of merchandise are sold at "time" prices, subject to certain rates of discount if paid at an earlier period.

1. Thus, the following or similar announcements are usually found upon the bill-heads of wholesale dealers : "Terms, 4 months, or 30 days less 5%"; or, "Terms 60 days, or 1% discount in 30 days, or 2% discount in 10 days."

2. In the same business house, certain goods are sold on long credit, and others on short credit.

3. When no rate of discount has been offered, merchants are generally willing, when bills are paid before maturity, to deduct the interest on the amount of the bill for the remainder of the time at the legal rate per annum.

Ex. The list-price of a scale is \$80; what is the net price if a discount of 25% and 10% is allowed ?

Arrithmen The first wate of discount is made	mad.
\$80 List-price. ANALYSIS.—The first rate of discount is reck	mea
upon, and deducted from the list price, and the ot	hers
$\frac{20}{20\%}$ , or $\frac{1}{4}$ . are deducted from the successive remainders.	
60 The result is not affected by the order in which	the
6 10%, or 1. discounts are taken. A discount of 25% and 10% is	the
54 Net-price. same as a discount of 10% and 25%.	

## EXAMPLES.

417. 1. The gross amount of a bill of shoes is \$82.68. What is the net amount, the rate of discount being 5%? (See Ex. 1, Art. 391.)

2. A stove is sold for \$45 less 30%; required the net price?

Note.—If the discount is not required, multiply by .70 (100% - 30%); the product will be the net price. To multiply by .70, multiply by 7 and place the figures of the product one place to the right.

3. What is the value of 466 *lb*. O.W. casing @ 45 *cts*. per pound, less 14 per cent.?

4. The gross amount of a bill of mdse. is \$106.36; what is the net amount, the rates of discount being 20% and 10%?

5. The gross amount of a bill of notions is \$49.75; what is the net amount, the rates of discount being 10% and 10%?

6. What is the value of 12 pair shoes @ \$1.60 per pair, less 5%?

7. What single discount is equivalent to a discount of 20% and 10%?

ANALYSIS .- Represent the gross amount by 100% OPERATION. (1.00). 20% ( $\frac{1}{5}$ ) of 100% = 20% (.20), which subtracted 1.00from 100% (1.00), leaves 80% (.80). 10% (10) of 80%  $.20\ 20\% = \frac{1}{5}$ (.80)=8% (.08), which subtracted from 80% (.80), leaves .80 72% (.72). 100% - 72% = 28%, the direct discount.

By the following rule, a single discount can be cal-.08 1 of 80. culated from two discounts mentally: From the sum of the discounts, subtract  $\frac{1}{100}$  of their product. The remainder will be the real discount. Thus, 20% + 10% = 30%. 30% $-2\% (20 \times 10 \div 100) = 28\%$ . When a third discount is

given, combine it with the result obtained from the other two.

When the sums of two or more discount series are the same, the series, in which the discounts are the most uniform, will produce the least single discount; and the series, in which the discount is most concentrated in one discount, will produce the greatest single discount.

Thus, a discount of 10, 10, and 10% is equivalent to  $27_{10}$ %; 20, 5, and 5 to 274 %; and 25, 24, and 24 % to 2843 %.

8. What single discount is equivalent to a discount of 15% and 10%? 45% and 10%? 20% and 121%? 60% and 10%? 75% and 121%? 20%, 20%, and 10%? 60%, 20%, and 20%?

9. The net amount of a bill of goods is \$74.20. What is the gross amount, the discount being 30%?

10. The net amount of a bill of files was \$36.75; what was the gross amount, the rate of discount being 10%?

11. A is offered dress goods at 26<sup>2</sup> cts. per yd., "4 months or less 6% cash"; how many yards can he purchase for \$49.82 cash?

12. The net amount of a bill of hardware is \$175.26; what is the gross amount, the rate of discount being 45% and 10%?

13. What is the net value of one case prints containing 2273 yd., @ 4<sup>3</sup> cts., less 5%, cooperage 25 cts.?

14. A bill of merchandise amounting to \$442.38 was bought Aug. 18, 1879, on the following terms: "4 months or 5% off 30 days." How much would settle the bill Sept. 16, 1879?

15. What is the net value of a bill of iron amounting to \$1103.75, at a discount of 45, 10, and 2 per cent.?

.72

.28

16. What is the net value of 1 case prints containing 3039<sup>2</sup> yd.
@ 5 cts. per yd., less a discount of 3%; cooperage \$.25?

17. What is the difference on a bill of \$875 between a discount of 40% and a discount of 30% and 10%?

18. A bill of tinware is sold at the following discounts: 74.20 at 20% and 10%; 43.75 at 40% and 5%; 69 at  $33\frac{1}{3}\%$  and 10%; and 49.17 net. What is the total net amount of the bill?

19. A bill of dry goods amounting to \$914.37 is sold, Aug. 19, on the following terms: "60 days, or less 1% if paid in 30 days, or less 2% if paid in 10 days." How much would settle the bill Sept. 18? How much Aug. 27?

20. Of a bill of hardware, \$61.51 are sold at a discount of 60 and 5%; \$18.75 at a discount of 10%; \$16.86 at a discount of  $12\frac{1}{2}\%$ ; \$44.25 at a discount of 40 and 5%; \$29.60 at a discount of 40,  $12\frac{1}{2}$ , and 10%; \$28.04 at a discount of 55%; \$16 at a discount of 65, 10, and 10%; \$18.70 at a discount of 50%; \$19.75 at a discount of 20%; \$18.50 at a discount of 15%; \$307.55 at a discount of 75 and  $12\frac{1}{2}\%$ ; \$36.61 at a discount of 60 and 10%; and \$218.25 net. What is the total net amount of the bill?

21. Goods are bought at a discount of 30% from a list price, and sold at the list price. What is the gain per cent.?

ANALYSIS.—Assuming \$1 as the list price, the cost is 70c., selling price \$1, and the gain 30c. 30c. is what % of 70c.?

22. Books are purchased at a discount of 25% from the list price. What is the gain per cent. by selling at the list price?

23. What per cent. is gained by selling pans at 21 cents apiece, that cost \$2.56 per dozen less 20 and  $12\frac{1}{2}\%$ ?

24. Plows are bought at a discount of 50% from the list price. What per cent. is gained by selling at the list price ?

25. A merchant purchases goods at a discount of 25% from the list price. What per cent. is gained by selling at the list price? What per cent. if goods are purchased at a discount of  $33\frac{1}{3}\%$ ? 35%? 25% and 5%? 20% and  $12\frac{1}{2}\%$ ? 15% and 10%?

26. A merchant buys goods at a discount of 40 and 20% from the list price, and sells at a discount of 30 and 10%. What is the gain per cent.?

ANALYSIS.—Assume \$1 as the list price, find the net cost and selling prices, and then the gain per cent.

27. If a merchant buys goods at a certain price 10 and 5 off, and sells them at the same price, 5 off, what per cent. profit does he make ?

28. What per cent. profit does a merchant make who buys at a discount of 20, 10, and  $12\frac{1}{2}$ %, and sells at the list price ?

29. What must be the marked price of goods costing \$32, that I may deduct 20% from it, and still gain 25% on the cost?

ANALYSIS.—First find the selling price, and then the marked or list price. If the cost is \$32, the gain will be 25% ( $\frac{1}{4}$ ) of \$32, or \$8; and the selling price will be \$32 + \$8, or \$40. If the goods are sold at a discount of 20%, the selling or net price is 80% of the marked price. \$40 = .80 of \$50.

30. What must be the asking price for books that cost \$1.60, in order to abate 20%, and still make a profit of 25%?

31. What must be the list price of goods that cost \$18, in order to make a profit of  $33\frac{1}{3}\%$ , if they are sold at a discount of 40%2

32. Find the list price of goods that cost \$75 and are sold at a discount of 60 and 10%, at a profit of 20%.

33. A manufacturer sells his goods at a discount of 30 and 10%, and thereby gains  $12\frac{1}{2}$ %. What is the list price, if the cost is \$28?

34. A hardware dealer sells certain goods at a discount of 75 and  $12\frac{1}{2}\%$ , and gains 20%. What is the list price, if the cost is \$2.80?

35. What per cent. must be added to cost price in order to give a discount of 25%, and make a profit of 20%?

ANALYSIS.—Assuming 100% as the cost price, the selling price is 120% of the cost. 120% is 75% (100% - 25%), or  $\frac{3}{4}$ , of 160%. 160% - 100% = 60%, the per cent. to be added to the cost price.

36. What advance on cost would be necessary in order to give a discount of 20%, and still make a profit of 20%?

37. At what per cent. above cost must goods be marked, so that when sold at a discount of 5%, there would be a profit of 25%?

38. If goods are bought at a discount of 2 10's and a 5 from a manufacturer's list price, and sold at a discount of  $12\frac{1}{2}\%$  ( $\frac{1}{8}$ ), what is the gain per cent.?

39. I purchase books at \$2 each less  $33\frac{1}{3}\%$ , and 5% for each. What is the net cost, and what per cent. discount may be given on the list price to produce a net profit of 10%?

30

BILLS.

## BILLS.\*

418. A Bill is a detailed statement of merchandise sold, or of services rendered. Bills of merchandise state the place and date of the sale, the names of the buyer and seller, the terms of the sale, the quantity, price, and distinguishing marks and numbers of the merchandise, and other details.

The terms *Bill* and *Invoice* are used by many interchangeably. The term Invoice is applied more particularly to statements rendered by consignees to commission merchants, showing marks, numbers, values, and accrued charges of goods shipped; to bills rendered to jobbers; and to bills received from foreign countries.

#### EXAMPLES.

419. Copy and extend the following bills:

(1. Canned Goods.)

WILMINGTON, DEL., Nov. 16, 1889.

Messrs. WM. DOLTON & Co.,

Bought of JAMES MORROW & SON.

Cases.	Doz.			
2 $1$ $1$ $2$	4 2 2	3 lb. Peaches $- \not<$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	
1 1	22	21 "Col. Pears	400         *         **           400         *         **           50         **         **	*

(2. Flour.)

BUFFALO, N. Y., Dec. 6, 1888.

Messrs. DANIEL CROUSE & SONS,

Bought of Schoellkopf & Matthews.

Interest charged on all accounts after 30 days. We allow no Expressage or Exchange.

20 25 25	Bbls. Flo	our "Sunlight'	' Sacks - Bbls	\$7.05 7.25 6.05	*** ***	**		
	66 6 66 6 66 6	"Dakota"	Bbls Sacks -	6.25 5.30 8.55	*** ** **	** **		
20 bags 70 "	2177 lb. 264 <sub>52</sub> bu	S. Meal I. Oats		1.20° .56 <sup>b</sup>	**	**	***	**

\* \$1.20 per hundredweight. b 56c. per bushel.

\* It is suggested that a part of these bills be reserved for review. One or two of them may be given each week as a general exercise. PERCENTAGE.

## (3. Window Glass.)

PITTSBURGH, May 14, 1888.

#### EUREKA GLASS CO.,

#### Bought of CUNNINGHAMS & Co.

Terms 30 days .- If not promptly paid, interest will be charged from date of bill.

	D	c A 99								PER	4.4.		
2	BX'S 7×9	A	-	-	-	-	-	-	-	100	**		
15	" 8×10	66	-	-	-	-	-	-	-	750	***	**	
2	" 9×12	66	-	-	-	-	-	-	-	750	**		
1	" 10 × 14	6.6	-		-	-	-	-	-	750	*	**	
2	" 12 × 26	66	-	-	-	-	-	-	-	850	**		
2	" 13 × 36	66	-	-	-	-	-	-	-	1075	**	**	
2	" 14×20	66	-	-	-	-	-	-	-	850	**		
2	" 15 × 30	6.6	-	-	-	-	-	-	-	975	**	**	
										1	***		
		Less	60	ar	nd	209	10	-	-	-	***		**
1 1	1									1			

## (4. Provisions.)

CLEVELAND, O., Oct. 9, 1886.

Messrs. L. C. MAGAW & Son,

Bought of J. P. Robison & Co.

Terms Net Cash.-No goods sold on 30 days.

$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	** **	*** *	** ** ** **	** *** ** **	10 <u>75</u> 14¢ 9¢ 14¢ 11¢	****d *** *** ***	-98° -57 -22 -60	1376 <sup>b</sup> 744 241 406	90ª 58 33	Mess Beef Hams Shoulders Dr. Beef Lard	5 5 1 1 Tc.	5 5 3 1 1	
-------------------------------------------------------	-------	-------	----------------------	-----------------------	-----------------------------------------	----------------------------	---------------------------	----------------------------------------	-----------------	----------------------------------------------------	----------------------	-----------------------	--

\* Number of pieces. <sup>b</sup> Gross weight. <sup>c</sup> Tare, or weight of barrel or tierce. <sup>d</sup> Net weight.

## (5. Fish.)

GLOUCESTER, MASS., Sept. 28, 1886.

Messrs. DANIEL WEIDMAN & Co.,

Bought of CLARK & SOMES.

Subject to sight draft without notice after thirty days.

10       Kits 15 lbs. Ex. *1 Mackerel 1.80       **       **         10       Kits 15 lbs. Ex. *1 Mackerel 1.80       **       **         2       Bbls. #2 Shore       '' lg 12.00       **       **         10       Kits 20 lbs. #2 Shore       '' lg 15.0       **       **         10       Kits 20 lbs. #2 Shore       '' - 2.80       **       **         10       Kits 20 lbs. #2 Shore       '' - 2.90       **       **         5       Halfs New Labrador Herring - 3.82       **       **       **         3       '' Round Shore       - 2.95       *       **         Box **, ctg. in Boston **       **       **       **	**
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Art. 419.]

#### BILLS.

(6. Groceries.)

#### Day Book, 115-797.

Messrs. Edwards & Co.,

NEW YORK, Feb. 1, 1889.

Bought of H. K. & F. B. THURBER & Co.

	(		: 1	
1 # 4385	1.	Cask Old Prunes $1544 - 134 = ****$ lbs 48	**	**
	3	Boxes Old Muscatel Raisins 1	*	**
	3	" New " " 210	*	**
	4	" " Laver " 195	*	**
7	1	" Cream Tartar, 1 foil 20 lbs39	*	**
	2	"Yeast-Cakes, 3 doz. ea., - 6 doz65	*	**
	25	lbs. Whole Pepper	*	
	10	" Nutmegs \$1 100	**	
	1	Box O. K. Mustard, <sup>1</sup> / <sub>4</sub> 's 12 lbs25	*	
	1	" $\frac{1}{2}$ 's 12 "25	*	
		Cartage on all	1	
			***	**
		1	1 1	

1st item—"M #4385" is mark and number upon the cask; 1544, gross wt; 134, tare or weight of cask. 5th item— $\frac{1}{4}$  foil, put up in  $\frac{1}{4}$  lb. packages and wrapped in tin foil.

## (7. Groceries.)

NEW YORK, Aug. 13, 1886.

Messrs. HORTON, CRARY & Co.,

Bought of AUSTIN, NICHOLS & Co.

			1	1
W. B.	1	Bag *20 Rio Coffee 132 23	30	56
A #99	1	" <sup>•</sup> ·20 " 131 21 <del>1</del>	**	**
	1	Bbl. $^{25}$ Roa. Java Coffee $\frac{121}{21} - 100 25\frac{1}{2}$	**	**
-	2	" .50 " Rio " 112-22 221 - *** 24	**	**
H. R. P.	1	Case Conc. Lye	5	50
Union.	2	Boxes Yeast Čakes, ea. 3 * 65	*	**
	25	lbs. Spice. Bag 20% 151	*	**
	5	Mats Cassia 211 26	*	**
A. N. & Co.	1	Keg Gr. Mustard 50 35	**	**
10.10	10	lbs. White Glue 40	*	**
		257-20 ****		
	~	269-20. **		
A. N. & Co.	Э	Bols. A. C. Sugar - $-\frac{250-21}{253-18}$		
	-	$253-20 - **** 11\frac{3}{4}$	***	**
#134	1	" W. D. Syrup 47 *** 60	**	**
\$114	1	" C. D. " 45" *** 50	**	**
		Ctg	1	50
			\$***	**

The small figures at the right of the words "bag" and "bbl." are the prices of the same. 3rd item—121 *lbs.*, gross *wt.*, 21 *lbs.* tare, 100 *lbs.* net *wt.* 4th item—112 and 109, gross weights; 22 and 20, tare; 221, total gross weight; 42, total tare. 12th item— $\frac{1}{2}$ ,  $\frac{1}{2}$  gallon allowance for leakage.

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PERCENTAGE.

[Art. 419.

# (8. Dry Goods.)

NEW YORK, March 20, 1889.

Messrs. MARSHAL FIELD & Co.,

Bought of H. B. CLAFLIN & Co.

Terms Cash in 30 days less 5%, or 4 months' note delivered within 30 days, and payable at Bank in New York exchange.

2875 8039 3369 1290- 1590	1 1 1 1 1	Bale Boott M. Brown         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -         -	yd. 800 800 967 1111 \$ ** *	c. 6 <sup>3</sup> 7 <sup>1</sup> 7 <sup>2</sup> 7 <sup>1</sup> **	54 ** ** **	** **
6888 2179 2507 6515 2985 1650	1 1 1 1 1 1	<ul> <li>Boott F. F</li> <li>Pepperell 600 Drill</li> <li>Case Blackstone A. A</li> <li>Dwight Anchor</li> <li>Great Falls Q</li> <li>Pearl River Ticking</li> <li>Cooperage -</li> </ul>	800 622 1649 1139 1492 708	$7^{1}$ $7^{3}$ $7^{1}$ 9 8 $15^{2}$	** ** *** *** ***	** ** ** 75

How much would settle the above bill April 19, 1889 ?

(9. Dry Goods.)

NEW YORK, March 23, 1888.

Messrs. DAVIDGE, LANDFIELD & Co.,

Bought of TEFFT, WELLER & Co.

			_		_		and coming ray	the second s			
								yd.	C.		
	2	Naumkeag Bl. Jean		48 47	-	-	-	95	9	8	55
	4	Roll Cambric		46 401	46 46	-	-	****	5²	*	**
	3	Pepperell Drill		47 <sup>3</sup> 30 <sup>3</sup>	-	-	-	****	8	*	**
	1	Lowell 10/4 Brown		- 40	-	-	-	38	142	*	**
	3	Continental C		40 40 40	-	-	-	***	72	*	
	5	New Market N		45 <sup>3</sup> 45 <sup>1</sup> 46 <sup>2</sup>	45 581		-	****	61	**	**
	2	Champion Cheviot		48 <sup>1</sup> 50 <sup>1</sup>	-	-	-	***	9	*	**
	2	Otis B. B. Dk Stripe		573	-	-	-	***	10	**	**
	1	Hamilton 30 in. Tick	-	-	-	-	-	488	112	*	**
	2	Thorndyke C		58 <sup>3</sup> 61	-	-	-	****	82	**	**
	2	Wamsutta C. Blea.		581 681	-	-	-	***	12	**	**
	8	Andros L 55	2 52	49	511		-	***	78	**	**
	1	Pepperell 10/4		-	-	-	-	368	22	*	**
l										444	**

1st item-2 pieces Naumkeag Bleached Jean containing 48 and 47 yards respectively; total, 95 yards at 9 cents per yard.

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### BILLS.

## (10. Dry Goods.)

#### Book 174, Page 148.

NEW YORK, March 30, 1888.

Mr. JAMES MORGAN, Milwaukee, Wis.

#### Bought of H. B. CLAFLIN & Co.

Terms: Net 60 Days, or 1% discount in 30 days, or 2% discount in 10 days, N.Y. Funds. No Exchange allowed.

											n – T		1	26
#4641	53	Pe's	Gord	lon	Pri	nts (	Job	)						1137
		212	482	38	401	482	483	372	48	48				1.6
		44	492	448	482	492	498	492	42	56				- B.
		482	491	282	491	49	488	491	28	488				
		37	332	102	52	333	10	18	101	101				1.2.5
		94	192	192	59	198	10	172	101	192				1. 50
		401	402	408	402	409	409	401	402	±0-	*****			
		49-	49- 4	40-	40-	40-	40-	40	49-	-				
#2601	54	Pc's	Do	•										
		488	48 4	49	42	$22^{1}$	<b>49</b> <sup>1</sup>	49	<b>48</b> <sup>2</sup>	532				
		482	478	$48^{3}$	$48^{2}$	49	44	49	<b>49</b> <sup>2</sup>	$48^{2}$				
		492	49	49	$48^{2}$	478	47	48 <sup>2</sup>	$49^{1}$	56				
		50 <sup>2</sup>	491	411	481	50	$27^{1}$	49	$48^{2}$	48 <sup>3</sup>				
		213	291	518	463	482	482	282	482	491				
		492	452	47	482	40 <sup>2</sup>	501	392	482	461	****			
\$ 4765	61	Pe's	Do	-										
		302	492	42	492	32	48	46	482	46 <sup>2</sup>				
		423	472	221	33	46	48	492	482	48				
		42	42	48	28	481	492	482	49	49				
		402	182	2.82	192	43	491	182	492	18				
		202	90	95	968	101	403	101	10	192				
		248	108	20 45	10	401	402	40-	96	40-				
	-	040	403	409	40	402	49"	40*	00	40	****			
		29-	490 4	48*	91.	40"	49	48	-	-				
										4	****	.042	***	**

How much would settle the above bill April 8, 1888? How much April 28, 1888?

## (11. Dry Goods.)

NEW YORK, March 20, 1888.

Messrs. Jordan, Marsh & Co.

Bought of A. T. STEWART & Co.

Job. J. U. S. B. R. H. Z. S. J. L. G. Q. J. B. J. Z. J. H.	8	Cases Gor # 4561 4157 3473 4224 2777 3504 3970 4198	don Fancy 2810 2902 <sup>1</sup> 2787 <sup>2</sup> 2880 <sup>2</sup> 2821 <sup>1</sup> 2842 <sup>2</sup> 2883 <sup>1</sup> 2863 <sup>1</sup> -	- ***** Less 5%	.05	***	**	****	**
------------------------------------------------------------------------------------	---	-----------------------------------------------------------------------------	------------------------------------------------------------------------------------------------------------------------------------------------------------------------	--------------------	-----	-----	----	------	----

1st column, distinguishing number of each case. 2d column, number of yards in the several cases.

[Art. 419.

## (12. Hosiery.)

Claims for Damages or Errors must be made on receipt of Goods.

NEW YORK, June 28, 1880.

Messrs. JOHN FORD, SONS & Co.,

Bought of JAMES TALCOTT.

Net 30 Days .- Note to your own order payable at a Bank in New York City.

	1							1	1		1
1789	35	Doz.	3458	Mixed 1/2 Fanor "	Hose	-	80	28			
*	12	66	853	Col'd	66		- 1.00	**			
	12	66	1691	Fancy	66		- 1.00	**			
	18	66	1759	66	66		75	**	**		
	20	66	1713	66	6.6		- 1.00	**			
	16	66	1716	66	66		- 1.10	**	**		
	6	66	3438	Fch. mx.	1/ 16		90	*	**		
	22	66	Job	Misses	~ 66		75	**	**	\$***	**
						<u>t</u> - 1				*	
		Shi	pped 1	per P.R.R.	& C.I	3. & (	Q.R.R.				
1.1		l									

Number on margin (1789), number of case. Numbers 3458, 2032, etc., manufacturer's distinguishing numbers (stock numbers).

## (13. Books.)

CHICAGO, ILL., May 7, 1878.

Mr. JOHN BERWOLD,

Terms Cash.

Bought of HADLEY BROS.

12 18	Randall's Arithmetics, Part 160	~~*	20	-	
24	Smith's Primers (paper)06	*	**		
36	" Spellers22	*	**		
18	" 2d Readers45	*	**		
12	" 3d "70	*	**		
6	" 4th " 1.15	*	**		
6	" 5th " 1.35	*	**		
6	Doz. Brown's Copy Books 1.80	**	**		
		**	**		
	Less 331/3 %	**	**	**	** /
				_	
6	Jones' Geographies #135		10		
6	" " 263	*	**		
6	" " 3 1.10	*	**		
6	" 4 2.00	**			
		**	**		
	Less 25% -	*	**	**	**
3	Boxes Chalk Crayons18				**
3	Doz. Blank Copy Books50			*	**
			1	\$**	**

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## BILLS.

## (14. Hardware.)

PHILADELPHIA, PA., Aug. 13, 1889.

Messrs. N. RUTTER, Son & Co.,

Bought of BIDDLE HARDWARE CO.

Terms 60 days.

	24	Sets W'd Wh'	l Bed (	Casters #1	2 in18	*	**		
				F	50%			*	**
	-1	Dor Puscell's	CDV	nives 14 in	#1540			11	
1	1	Doz. mussell s	5.D.A.	mives 14 m	.#1040 -		1.1	11	
	000	Comis no Dilto	1/	2.40 2.55	8.15 8.20	**	**		
	200	Carriage Dons	74 ×	1 21/4	01/4 01/2				
	100	11 11	91	5.95 6.25	6.50 6.85	**	**		
	100		% × ·	04 0	01/4 01/4				
	100	<i>(1 11</i>	21	7.15 7.45		**	**		
	100		%8 ×	1/4 1/4					
	100		0.7	7.90	8.05	**	***		
	100		3/8 ×	81/2	8%				
	100			7.25 7.75	9.25	**	**		
	100	66 66	$\frac{1}{2} \times$	2 21/2	4		4.4		
	100			11.25 11.75	13.25				
	100		1/2 ×	$6  6\frac{1}{2}$	8	~~~			
						***	**	- 1	
				75 &	121/2% -			**	**
	1/	C. Machine B	alte 1/	× 8	8 70	*	**		
	/2	C. machine D	1105 72	1= 10	10 00				
	1/	66 66	66 3/	15.10	10.00	**	**		
	72		/4	XU					
-	99	Ibs. "	*4	× 11	.1034	**	**		
						**	**		
	-			60	& 10% -			**	**
								**	**
								1	

3rd item—200 bolts of each of the following sizes:  $\frac{1}{4}$  in. thick  $\times 1$  in. long,  $\frac{1}{4}$  in. thick  $\times 2\frac{1}{4}$  long,  $\frac{1}{4}$  in. thick  $\times 5\frac{1}{4}$  long,  $\frac{1}{4}$  in. thick  $\times 5\frac{1}{2}$  in. long. The numbers 2.40, 2.55, 3.15, and 3.20 represent the prices per hundred of the several sizes.

(15. Watches and Jewelry.)

NEW YORK, Mar. 7, 1887.

#### Mr. CHARLES BABCOCK,

Bought of A. S. GARDNER & Co.

Terms: Net Cash 4 months, or less 5% 30 days, with Exchange on New York.

H 658 20422	1 1 1 2 1	18 k. Ancre full Engrd. & Enld. S. W. 14 k. Russell flat C. B. " 18 k. Plain Ring $3\frac{3}{4}$ dwts 1 <sup>0.5</sup> 14 k. Guards with slides $\frac{37\frac{3}{2}}{222}, \frac{56}{208}$ - 1 <sup>1.5</sup> Pr. Solid Roman Sl. Buttons 908	90 46 * *** 10	50 ** ** 50	***	**
----------------	-----------------------	------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------	----------------------------	----------------------	-----	----

How much would settle the above bill, Apr. 2, 1887?

The letters and numbers on the margin refer to the numbers of the watches. 4th item—numbers 222 and 208 refer to the style numbers (stock numbers) of the guards (chains), and the numbers above  $(37\frac{3}{8} \text{ and } 56)$  express the weights in penuyweights ; \$1.15 per penuyweight.

#### PERCENTAGE.

## (16. Tinware.)

Rochester, N. Y., Oct. 16, 1889.

Messrs. McCarthy & Redfield,

Bought of JOHN H. HILL.

Terms 60 days. If paid in 10 days 2 per cent. discount.

2 1/2 3 3 3 2 6	Doz. $#21$ Pieced Dish Pans - 8.25 "9 in. Wash Boilers - 36.00 "Pieced Bread Pans $3 \times 9 \times 3 = 2.00$ """" $5 \times 9 \times 2 = 2.00$ "#13 Pieced Cups90 "#25 Dippers 1.75 Nests $#021$ Flaring P'ls & Dippers 1.14	**	** ** **		
	20 & 121/6 % -	**	**	**	**
1 1 1	Doz. Champion Nutmeg Graters "Nests #4 Fancy Cov'd Pails #4 Burnished Tea Pots	6 6	00 75	1	75
	25 & 12½% -	**	**	*	**
$\frac{2}{\frac{1}{2}}$	Doz. # 10 Pudding Pans 4.25 " # 200 Pressed Kettles 5.50	*	** **		
		**	**		
	371/2 % -	*	**	*	**
6	.75 .90 Enameled Kettles Ea. 4-5 qt	*	**		
12	" " <u>6-8 qt.</u> -	**	**		
		**	**		
	60% -	**	**	**	**
8	N.Y.C. & H.R.R.R. 975 lbs. @ 124			**	**

What amount would be due on the above bill Oct. 26, 1889?

(17. Wooden Ware.)

CHICAGO, July. 9, 1887.

Messrs. OLIVER & BACON,

BACON, Bought of JAMES S. BARRON & Co. Terms Cash, with exchange on Chicago or New York.

6	Oak Churns #1 1.60 Less 20% -	*	**	**
2	Doz. 1 bu. Corn Baskets 4.00		*	
1/2	" Potato Mashers 1.00			**
1	" 6 ft. Ladders	4		
1	"8 ft. "	5		
1	" 10 ft. "	6		
	•	**		
	Less 50 & 10% -	*	** *	**
2	" #10 Shoe Brushes 2.25		*	**
			**	**

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#### BILLS.

Note.—In the preparation of bills in the usual form, from the following items, use your own name as the seller, the name of your teacher as the buyer, and the present date and place.

**18.**  $\frac{1}{2}$  gro. Table Knives and Forks @ \$8.40.  $\frac{1}{12}$  doz. Cheese Knives @ \$9.60.  $\frac{1}{2}$  doz. Razors each #100 \$9, #101 \$10, #102 \$10.50.  $\frac{1}{2}$  doz. Pocket Knives each #337 \$6, #427 \$7.50, #204 \$3.75. 6 sets Champion Irons @ \$1.50. 1 doz. Tacks each #1 22c., #2 22c., #3 25c., #4 27c.  $\frac{2}{3}$  doz. Panel Saws @ \$20 less 20%. Box and drayage, 75c. Terms: Cash. (See Ex. 14.)

19. 2293 *lbs.* S. Meal @ \$145 per *cwt.* 200 *bbl.* Dakota Flour @ \$725. 11890 *lb.* Feed @ \$140. 170 Bags (To be returned) @ 25*c.* Expressage on Empty Bags, 25*c.* Car #30808. (See Ex. 2.)

20. 2 doz. Wrought Butts each  $3\frac{1}{2} \times 3 \$2.40$ ,  $3\frac{1}{2} \times 4 \$3$ , less 55 and 10%.  $\frac{19}{12}$  doz. Locks #184 @ \$48 less 30%. 1 doz. Locks #476 \$15; 1 doz. Knobs #700 \$6.50; 1 doz. Escutcheons #16 \$2, less 45 and 5%. (On last three items.) 3 doz. Sash Fasteners #15 @ \$2.25. 4 doz. Solid Eye Mattocks @ \$15.50, less  $33\frac{1}{3}(\frac{1}{3})$ %. Box and cartage, 63c. Terms: 60 days. (See Ex. 14.)

21. 2 doz. Smith's Bitters @ \$7.25. 110 lb. Epsom Salts @ 34c. 2 doz. Sweet Oil #3 @ \$1.75. 2 doz. Sweet Oil #4 @ \$1.25. 2 doz. Sweet Oil #4 @ \$1.25. 2 doz. Paregoric 2 oz. @ \$1.25. 2 doz. Laudanum 2 oz. @ \$2.25. 2 doz. S. M. Oil @ \$1.25. 2 doz. Extract Lemon 2 oz. @ \$2. 2 doz. Brown's Syrup @ \$1.75. 2 doz. Fancy Soap @ 67c. 2 doz. Castor Oil @ \$1.75. 2 doz. Golden Liniment @ \$1.85. Cartage 50c. Terms: Net Cash, without discount.

22. 2 bbl. Prunes 248-20, 285-20, @ 6c. 2 bbl. Rice 240-19, 229-20, @  $6\frac{1}{8}c$ . 5 bbl. "A" Sugar 319, 306, 288, 319, 306 lb. @  $9\frac{5}{8}c$ . 5 bbl. Yellow C Sugar 314-19, 319-20, 329-20, 311-21, 328-19, @  $8\frac{3}{4}c$ . 1 bbl. Cut Loaf Sugar 236-20 @  $10\frac{5}{8}c$ . Cartage, \$1.25. (See Ex. 7, 11th item.)

23. 8 lengths 8" Drive Pipe 129' 10" @ \$2.25 (per foot); 44 lengths  $5\frac{5}{8}$ " Casing 801' 8" @ 70c.; 233 lengths 2" O. W. Tubing 4507' @ 21c., less 7 $\frac{1}{4}$  and 2%. Less freight 29400 *lb*. @ 23c. per *cwt*.

24. 12 Pr. Women's Grain B't. #443 Shoes @ \$1.25. 12 Pr.
Wos. Kid B't. #407 @ \$1.50. 12 Pr. Wos. Kid B't. #406 @
\$1.75. 12 Pr. Misses Kid B't. #301 @ \$1.50. 12 Pr. Misses
Goat B't. #302 @ \$1.60. 12 Pr. Wos. Goat B't. #428 @ \$1.75.
12 Pr. Children's Goat B't. #200 @ \$1.30. 12 Pr. Ch. Grain B't. #202 @ \$1.20. 12 Pr. Ch. Glove Kid B't. #222 @ \$1.10.

## COMMISSION AND BROKERAGE.

420. Commission or Brokerage is an allowance made to an agent for transacting business for another; as, the sale or purchase of property, the collection or investment of money, etc.

An additional percentage is usually charged by commission merchants for guaranteeing the payment of sales made on credit.

421. The party who transacts the business is called a Commission Merchant, or Broker; and the one for whom he acts is called the Principal.

Notes.—1. Commission Merchants usually have possession of the subjectmatter of the negotiation, and make sales and purchases in their own name.

2. Brokers do not have possession of the merchandise bought or sold, and generally make contracts in the name of those who employ them and not in their own. They simply effect bargains and contracts.

The name *broker* is often erroneously applied to dealers in stocks, bonds, etc., who buy and sell on their own account only.

422. A Consignment is a quantity of merchandise sent by one party to another. The party who sends it is called the Consigner; and the party to whom it is sent, the Consignee.

**423.** The **Net Proceeds** of a consignment is the balance due the consignor after all charges or expenses have been deducted.

The whole amount realized from a sale is called the *gross proceeds*. The commission is usually a certain per cent. of this amount.

424. An Account Sales is a detailed statement rendered by the Commission Merchant to the Consignor, showing the sales of certain goods, the charges or expenses attending the same, and the difference or net proceeds.

The charges embrace freight, cartage, inspection, advertising, storage, insurance, commission and guarantee, etc.

425. An Account Purchase is a detailed statement rendered by the Commission Merchant to his Principal, showing the cost of certain goods bought, and the charges or expenses attending the purchase.

426. Commission or brokerage is usually computed at a certain per cent. of the amount realized or invested, or of the amount involved in the transaction. In such cases the general principles of percentage are applied.

Notes.—1. In buying and selling stocks, bonds, etc., the par value, and not the actual value, is taken as the base.

2. The commission for buying and selling some kinds of merchandise is usually computed at a certain price per unit of weight or measurement; as, grain per bushel, cotton per bale, etc.

## EXAMPLES.

427. 1. A commission merchant sold goods to the amount of \$864; what was his commission at  $2\frac{1}{2}$  ( $\frac{1}{2}$  of 10) %?

2. A salesman sells goods at a commission of  $2\frac{1}{2}\%$ ; what must be his sales, that he may have a yearly income of \$5000?

3. What is the brokerage for selling 850 bales of cotton at the rate of \$25 per 100 bales?

4. A lawyer collected a note of \$2375; how much did he pay to the owner of the note, his commission being 5%?

5. My agent in Chicago purchases for me 600 barrels of flour at \$3.75 per barrel; how much do I owe him, his commission for purchasing being 2%?

6. An officer collected \$17850, and deposited \$17493 in the Treasury, retaining the remainder as his commission. What was the rate per cent. of the commission?

7. Sent to a commission merchant in Toledo \$2080.80 to invest in flour, his commission being 2% on the amount expended; how many barrels of flour would be purchased at \$4.25 per barrel?

8. A commission merchant sells merchandise amounting to \$3325; how much is paid to the consignor of the merchandise, the charges being, for transportation \$117.50, for advertising \$10, for storage \$15, for commission 24%?

9. My agent in Chicago buys for me 1187.76 centals wheat at \$2.123 per cental. What is his commission at  $\frac{1}{2}$  per cent.?

10. A commission merchant purchased for me 928 bushels of clover seed at \$8.55 per bushel. How much should I send to him in settlement, if his commission for purchasing is 1 per cent.?

11. A broker buys 8375 pounds of leather at 26 cents per pound. What is his brokerage at  $\frac{2}{3}$ %, and what is the net amount received by the seller, the brokerage being paid by him ?

12. A freight broker procures transportation for 375 tons of merchandise at \$3.50 per ton; what is his brokerage at 5%?

13. A collector deposits \$28117, retaining 3% on the whole amount collected. What amount did he collect and what was his commission ?

14. A lawyer, collecting a note at a commission of 5% thereon, received \$6.25; what was the face of the note?

15. An agent sold 6 mowing-machines at \$120 each, and 12 at \$140 each. He paid for transportation \$72, and, after deducting his commission, remitted \$2208 to the manufacturer. What was the % of his commission ?

16. A merchant instructs his agent in Cincinnati to buy pork to the amount of \$5000. The charges on the pork being \$16, and the agent's commission  $1\frac{1}{2}\%$ , how much must be remitted to settle the bill ?

17. What are the net proceeds of the sale of 12372 pounds of leather at 22 cents per pound, the charges being \$31, and a commission of  $2\frac{1}{2}$ % being paid for selling and  $2\frac{1}{2}$ % for guaranteeing payment?

18. A real estate agent, who charged  $2\frac{1}{2}\%$  for making the sale, paid to the owner of a house and lot \$42412.50; what was the value of the property?

19. A commission merchant sells 240 *bbl.* of potatoes at \$3.75 per *bbl.*, and 260 *bbl.* at \$3.60 per *bbl.* How much is due the consignor, the commission being  $12\frac{1}{2}$  cents per barrel?

20. John Smith is a disbursing agent of the United States. Jan. 1, 1880, there is in his hands \$11870.63. Feb. 1, he pays out \$3220.34, on which he is entitled to a commission of  $1\frac{7}{8}$ %. Mar. 1, he receives \$3750.87. May 1, he pays out \$3795.01, on which he is entitled to a commission of  $2\frac{1}{2}$ %. Make a statement of his account, showing balance due the United States.

21. A lawyer collected 75% of an account of \$3416, charging 5% commission. What amount should he pay over?

22. A, having a claim against the government of \$10970, agreed to pay an agent 8 per cent. of the amount collected. The amount collected was 22 per cent. less than the amount of the claim. How much was received by A?

23. B sends \$2240.70 to his agent in Cleveland, requesting him to invest in provisions after deducting his commission of 3% for purchasing; what was the sum invested ?

24. A broker received \$62.50 for selling some bonds, charging \$% brokerage. What was the par value of the bonds ?

#### Art. 427.] COMMISSION AND BROKERAGE.

Copy the following account, and make the necessary extensions, etc.

## (25. Account Sales.)

NEW YORK, Oct. 19, 1889.

Sold for account of A. W. RANDOLPH & Co.,

By DAVID Dows & Co.

1880. Sept.  Oct.	$12 \\ 18 \\ 30 \\ 14 \\ 18$	100 Bbls. "Sunshine" 5.75       ***         125 " "Pride of the West" - 6.25       ***         150 " "Sunshine" 6.       ***         75 " "Pride of the West" - 6.50       ***         50 " " '' a " " - 6.60       ***	**** **
Sept. Oct. 	10 10 19 19 19	$\begin{array}{c c} Charges. \\ \hline Transportation 500 Bbls. @ 27$ \\ Cartage 400 `` @ 5$ \\ Storage 400 `` @ 3$ \\ Insurance \frac{1}{16} + ** \\ Commission and Guarantee 5% \\ Net proceeds \\ \end{array}$	*** **

26. According to the above form, prepare an Account Sales of 10 bbl. Yellow C Sugar, 3031 lb. @ 8c.; 10 bbl. Standard A Sugar, 2957 lb. @  $9\frac{1}{16}c.$ ; 10 bbl. Soft A Sugar, 2839 lb. @  $8\frac{3}{4}c.$ ; 2 Tc. Lard, 713 lb. @  $9\frac{1}{2}c.$ ; 1 Tc. Rice, 608 lb. @ 7c. Charges as follows : Cooperage, \$1.80; Cartage, \$3.60; Commission,  $1\frac{1}{4}$ %. Present date and place; Student & Co., commission merchants; and sold for account of Teacher & Co.

27. If an agent's commission is \$145.20, when he sells \$5808 worth of goods, how much would it be when he sells \$7416 worth?

28. A creditor receives on a debt of \$1725, a dividend of 60%, on which he allows his attorney 5%. He receives a further dividend of 25%, on which he allows his attorney 6%. What is the net amount that he receives ?

29. A gentleman left a sum of money to be divided equally among 7 persons, subject to an inheritance tax of 5%, which caused a deduction of \$364 from the whole amount. What did each receive ?

30. An agent's commission for the month was \$128.40. If his sales had been \$864 more, his commission would have been \$150. Find the amount of his sales.

31. A man allows his agent 5% on his gross rentals, and receives a net rental of \$3488.40. If the gross rental is 6% of the value of the property, what is the value of the property?

169

PERCENTAGE.

[Art. 427.

## (32. Account Purchase.)

TOLEDO, O., Mar. 6, 1887.

Purchased by A. L. BACKUS & Sons,

170

erson

For account and risk of L. A. & W. B. SHAW.

9 227 9 <u>28</u> 9 <u>31</u>	Bags "Montauk" - Bu. Mammoth Clover "Clover Seed "Timothy Seed - Charge	See	ed - -	 	9 9 8 1	21 00 55 75	* ** ** **	** ** ** **	***	**
	Cartage Commission 1% Charge your %	-		 		-	*	25 **	****	**

Note.—The small figures at the left represent pounds. See Art. 338.

33. According to the above form, prepare an Account Purchase of 3 Half-Chests Gunpowder Tea, 165 *lb.* @ 35*c.*; 2 *Hfc.* Oolong Tea, 86 *lb.* @ 20*c.*; 20 bags Rio Coffee, 2388 *lb.* @ 13*c.*; 2 mats Java Coffee, 133 *lb.* @  $19\frac{1}{2}c.$ ; 1 *Hhd.* P. R. Molasses, 143 *gal.* @ 54*c.* Charges as follows: Drayage, \$1.75; Commission, 1%. Commission Merchants, Student & Co.; bought for Teacher & Co.; present place and date.

 $\sim$  34. After paying an auctioneer 5%, a man received \$1172.30 for his furniture. What were the gross sales ?

35. A bankrupt's assets are \$17415, and his liabilities, \$48375. I place my claim of \$2560 in the hands of my attorney for collection. How much do I receive if the attorney retains 5% commission?

36. A landlord received \$822 as the net rental of a house, after his agent had paid \$60 for repairs and charged 2% commission on the gross rental. What was the gross rental?

37. C of New York sells for D of Atlanta, a quantity of cotton, amounting to \$7317.83, and charges a commission of  $2\frac{1}{2}\%$ . By instructions, he invests the proceeds in dry goods, after deducting a commission of  $1\frac{1}{2}\%$  on the amount expended. What was the total commission ?

38. A commission merchant sold 300 bales of cotton, averaging 462 *lb*. to the bale, at 15.7¢, his commission being 25¢ per bale, and the charges \$161. He purchased for the consignor dry goods amounting to \$2576.37, charging a commission of  $1\frac{1}{2}\%$ . How much was still due the consignor ?

# INTEREST.

428. Interest is a sum charged for the use of money, or its equivalent; or more strictly speaking, it is the use of money, or the service rendered in its use.

**429.** The **Principal** is the sum for the use of which interest is charged.

**430.** The **Rate** is the per cent., or number of hundredths, of the principal, charged for its use for a certain time, usually for one year (per annum). When no time is mentioned with the rate in the contract, a year is understood.

431. The Amount is the sum of the principal and interest.

If \$1000 is loaned for one year at 6% per annum, \$60 would be the interest, \$1000 the principal, and \$1060 the amount.

432. Simple Interest is interest on the principal only for the full time.

**433.** Compound Interest is interest not only on the principal, but on the interest also after it becomes due.

If \$1000 is loaned Jan. 1, 1881, for 2 years, the amount due Jan. 1, 1883, at 6% simple interest, would be \$1000 (Principal) plus \$120 (Simple Interest), or \$1120. At compound interest the amount due Jan. 1, 1882, would be \$1060 (\$1000 + \$60); the amount due Jan. 1, 1883, would be \$1060 plus \$63.60 (6% of \$1060), or \$1123.60. The simple interest for 2 years would be \$120; the compound interest for the same time, \$123.60. When the word interest is used alone, simple interest is understood.

**434.** Legal Interest is the interest according to the rate per cent. fixed by law for cases in which the rate per cent. is not specified. By special agreement between parties in certain States, interest may be received at a rate higher than the legal rate. In most of the States, this rate is limited. See Art. **436**.

**435.** Usury is the taking of a higher rate of interest than that allowed by law. A person taking usury is liable to certain penalties differing in the several States.

State or Territory.	Ra	ite.	State or Territory.	Rate.	
Alabama	8%	8%	Mississippi	6%	10%
<sup>a</sup> Alaska (Ter.)			Missouri	6%	10%
Arkansas	6%	10%	Montana (Ter.)	10%	Any
Arizona (Ter.)	10%	Any	Nebraska	7%	10%
<sup>b</sup> California	7%	Any	Nevada	7%	Any
°Colorado	10%	Any	New Hampshire	6%	6%
Connecticut	6%	6%	New Jersey	6%	6%
Dakota (Ter.)	7%	12%	New Mexico (Ter.)	6%	12%
Delaware	6%	6%	<sup>a</sup> New York	6%	6%
Florida	8%	Any	North Carolina	6%	8%
Georgia	7%	8%	Ohio	6%	8%
Idaho (Ter.)	10%	18%	Oregon	8%	10%
Illinois	6%	8%	Pennsylvania	6%	6%
Indian (Ter.)	6%	Any	Rhode Island	6%	Any
Indiana	6%	8%	South Carolina	7%	7%
Iowa	6%	10%	Tennessee	6%	6%
Kansas	7%	12%	Texas	8%	12%
Kentucky	6%	6%	Utah (Ter.)	10%	Any
Louisiana	5%	8%	Vermont	6%	6%
Maine	6%	Any	Virginia	6%	6%
Maryland	6%	6%	Washington (Ter.)	10%	Any
Massachusetts	6%	Any	West Virginia	6%	6%
Michigan	7%	10%	Wisconsin	7%	10%
Minnesota	7%	10%	Wyoming (Ter.)	12%	Any

**436.** The following table shows in the first column the legal rate of interest when no rate is specified in the contract, and in the second column the maximum rate allowed by law.

(<sup>a</sup>) Not organized.

(b) "On judgments recovered in the courts 7%, but must not be compounded in any manner."

(°) "Most banks pay 6% on time deposits and charge from 1 to 2% per month on loans."

(<sup>4</sup>) "Advances payable on demand (call loans), of not less than \$5000, on negotiable collaterals, are not subject to the interest laws, but may be made for any compensation agreed upon in writing."

437. Interest for Parts of a Year.—Although many of the States have rigid laws in regard to the rate per cent. to be charged per annum, few of them specify on what basis interest should be reckoned for a period of time less than a year. The following methods are in common use :

1. Finding the time in months and days (Compound Subtraction, Art. **310**), and regarding the months as twelfths of a year, and the days as thirtieths of a month or 360ths of a year. This method, although implied by the general interest laws\* of the State of New York, is not uniform, since it allows the same interest for February with its 28 days as for March with its 31 days. Its results are sometimes greater and sometimes less than those of accurate interest.

2. Finding the exact time in days (**310**) and regarding the days as 360ths of a year. Since a day is  $\frac{1}{365}$  of a year, this method produces too great a result. It is used by merchants and bankers generally, and by many banks  $\ddagger$  in discounting notes. 6% by this method is equivalent to  $6\frac{1}{75}\%$  accurate interest.

3. Accurate Interest.—Finding the exact time in days (310) and regarding the days as 365ths of a year. <sup>•</sup> This method is used by the United States government, and by some merchants and banks; but, on account of its inconvenience when interest tables are not used, it is not generally adopted.

Notes.—1. By the first method, the time from July 10 to Sept. 10, would be 2 months, and the interest would be  $\frac{2}{18}$  or  $\frac{1}{6}$  of the interest for one year. On \$10000 at 6% for 2 months, the interest would be \$100 ( $\frac{1}{6}$  of .06 of \$10000).

2. By the second method, the interval between the same dates would be 62 days, and the interest would be  $\frac{62}{660}$  of the interest for one year. On \$10000 at 6% for  $\frac{62}{660}$  of a year, the interest would be \$103.33 ( $\frac{62}{660}$  of .06 of \$10000).

3. By the third method, the interval between the same dates would be 62 days as in the second method, and the interest would be  $\frac{62}{375}$  of the interest for one year. On \$10000 at 6% for  $\frac{62}{365}$  of a year, the interest would be \$101.92 ( $\frac{62}{365}$  of .06 of \$10000).

4. The difference between ordinary interest and accurate interest for the same number of days is  $\frac{1}{73}$  of the former, or  $\frac{1}{72}$  of the latter. Thus in the above example, the difference between the results, \$1.41 (\$103.33-101.92), is  $\frac{1}{73}$  of \$103.33, or  $\frac{1}{73}$  of \$101.92.

<sup>\* &</sup>quot;For the purpose of calculating interest, a month shall be considered the twelfth part of a year, and as consisting of thirty days; and interest for any number of days less than a month shall be estimated by the proportion which such number of days shall bear to thirty."

 $<sup>\</sup>pm$  According to the banking laws of the State of New York, banks are authorized in discounting notes to charge interest in advance for the exact number of days which the note has to run (Ch. XVIII, Title 2, §300).

This law appears to conflict with the law quoted above which implies that the time shall be found in months and days. It does not state whether the days shall be regarded as 360ths or 365ths of a year.

INTEREST.

**438.** Interest is an application of percentage, the element of time being introduced. Therefore the four elements or parts in interest are the Principal (the Base), the Rate, the Interest (the Percentage), and the Time; any three of which being given, the other may be found.

439. To find the interest \* for any number of years and months.

Ex. What is the interest and amount of \$324, for 2 yr. 3 mo., at 8%?

	OPERATIONS	3.	
\$324	Principal.	Or	\$324
.08			.18
25.92	Interest for 1 yr.		2592
$2\frac{1}{4}$			324
648			58.32
5184			324.
58.32	Interest for 24 yr.		\$382.32
324	Principal.		
\$382.32	Amount for $2\frac{1}{4}$ yr.		

ANALYSIS.—At 8%, the interest of \$324 for 1 year is .08 of \$324 (the Principal), or \$25.92. If the interest of \$324 for 1 year at 8% is \$25.92, for 2 yr. 3 mo.  $(2\frac{1}{4}$  yr.), it is  $2\frac{1}{4}$  times \$25.92, or \$58.32. The amount is \$324 plus \$58.32, or \$382.32.

**440.** RULE.—To find the interest, multiply the principal by the rate per cent. expressed decimally, and that product by the number of years, and the months as a fraction of a year.

To find the amount, add the principal to the interest.

Notes.—1. When the rate per month is given, apply the same rule, i. e., multiply the principal by the rate per month expressed decimally, and that product by the number of months.

2. Instead of multiplying by the rate and time separately, the process may be shortened by multiplying the principal by the product of the rate and time. In the above example, multiply 324 by .18 ( $24 \times .08$ ).

<sup>\*</sup> Unless the words "Accurate Interest" are used, all computations in this book are made on the basis of 330 days to the year.

INTEREST.

Art. 441.]

#### EXAMPLES.

441. Find the interest of

1. \$875 for 2 yr. at 7%. 6. \$816.40 for 5 yr. 3 mo., at 5%.

2. \$642.50 for 3 yr. at 6%. 7. \$1275 for 7 yr. at 6%.

3. \$1010.10 for 6 yr. 6 mo., at 8%. 8. \$2789.40 for 3 yr. 2 mo., at 41%.

4. \$3010.75 for 3 yr. 4 mo., at 7%. 9. \$456.75 for 4 yr. 8 mo., at 5%.

5. \$3745.80 for 4 yr.1 mo., at 6%. 10. \$10180 for 3 yr. 4 mo., at 10%. In the following examples, find the time by Compound Subtraction (310).

11. What is the interest of \$6488 from May 3, 1889, to Sept. 3, 1891, at 7%?

12. What is the amount of \$396.60 from Aug. 16, 1890, to Dec. 16, 1892, at 8%?

13. Compute the interest of \$250.75 from Nov. 20, 1892, to July 20, 1894, at 41%.

14. Loaned on interest, New York, Dec. 16, 1880, \$1739.75 (no rate specified); what amount should I receive, June 16, 1881?

442. To find the ordinary interes' (360 days to the year) for any rate and time.\*

#### First or Day Method. 443.

Гhe	interest of	81	for	1	year at	36%	is	\$.36.	
6	6 66	\$1	66	1	day at	36%	is	\$.001.	
6	·	\$1	66	1	**	6%	is	\$.0001.	
6	с. сс.	\$1	66	1	"	9%	is	\$.0001.	
6	6 66	\$1	66	1	66	4%	is	\$.0001.	
6	.e .e	\$1	"	1	66	12%	is	\$.0001.	
6	.e ee	\$1	"	1	66	3%	is	\$.00012	•
6	·	\$1	66	1	66	412%	6 is	\$.0001	•

What is the interest of \$1735 for 73 days at 6%? Ex. OPERATION.

\$1735

ANALYSIS .- The interest of \$1735 for 73 days is equivalent to the interest of 73 times \$1735, or \$126655 for 1 day. Since the interest of \$1 for 1 day is 1 of a mill, the interest of \$126655 for 1 day is as many mills as 6 is contained times in 126655, or 21109 mills, or \$21.11.

\* The student should be taught at least two (to be selected by the teacher) of the following methods of reckoning interest.

[Art. 444.

444. Rule.—Multiply the principal by the number of days, and place the point three places to the left. The result will be the interest at 36%. To find the interest at 6%, divide by 6; at 4%, by 9; at 9%, by 4; at 3%, by 12; at 12%, by 3; at 44%, by 8.

Notes.-1. Observe in the above rule that the rate and divisor, when multiplied together, produce 36.

2. To find the interest at other rates, find it first at 6%, and then apply the following rules : At 1%, divide by 6 (second time); at  $1\frac{1}{2}$ %, divide by 4; at 2%, divide by 3; at 5%, subtract 1; at 7%, add 1; at 8%, add 1; at 10%, divide by 6, and multiply by 10 by placing the point one place to the right; at any per cent., divide by six (second time) and multiply by the rate.

3. If the principal is a multiple of the divisor (6 in the model example), time can be saved by performing the division first. Thus, to find the interest of \$1200 for 113 days, divide 1200 by 6, and multiply the quotient 200 by 113, producing 22600. By pointing off three places, the required interest is \$22.60.

4. When the time is expressed in years, months, and days, reduce it to days by regarding each year as 360 days and each month as 30 days.

#### EXAMPLES.

## 445. Find the interest of

- 1. \$1000 for 80 days at 9%. 6. \$375.60 for 29 days at 3%.
- 2. \$1700 for 77 days at 6%. 7. \$414.40 for 47 days at 12%.
- 3. \$487 for 33 days at 4%.
  4. \$1375 for 17 days at 4½%.
  8. \$516 for 95 days at 5%.
  9. \$474 for 19 days at 7%.
- 5. \$2416 for 117 days at 6%. 10. \$876 for 83 days at 8%.
- 11. \$387.60 for 3 mo. 17 da., at 6%. At 5%.
- 12. \$1728 for 1 yr. 2 mo. 23 da., at 6%. At 7%.
- 13. \$2345 for 8 mo. 19 da., at 6%. At 54%.
- 14. \$1846 for 5 mo. 23 da., at 6%. At 41%.
- 15. \$3456 for 2 mo. 28 da., at 6%. At 4%.
- 16. \$5000 for 2 yr. 2 mo. 16 da., at 6%. At 10%.

In the following examples, find the time both by Compound Subtraction and exact days (310).

17. \$875 from May 16, 1888, to Jan. 4, 1889, at 6%. At 41%. 18. \$412.40 from Jan. 5, to Dec. 12, at 6%. At 71%.

- 19. \$1000 from Mar. 19, 1889, to Oct. 5, 1890, at 6%. At 12%.
- 20. \$2420 from June 17, 1887, to Feb. 1, 1888, at 6%. At 10%.
- 21. \$7000 from Oct. 12, 1888, to May 3, 1890, at 6%. At 8%.
- For additional examples, see Art. 459.

#### INTEREST.

# Second or 6% Method.

**446.** At 6%, the interest of one dollar for 1 year is \$0.06. For 1 month,  $\frac{1}{12}$  of a year, it is  $\frac{1}{12}$  of \$0.06, or \$0.00 $\frac{1}{2}$  (.005). For 1 day,  $\frac{1}{30}$  of a month, it is  $\frac{1}{30}$  of \$0.005, or \$0.000 $\frac{1}{6}$ .

Ex. What is the interest of \$864, at 6%, for 2 yr. 7 mo. 20 da.?

	OPERATION.		
$2 \times .06$	= .12	1	864
$7 \times .00\frac{1}{2}$	=.035		$158\frac{1}{3}$
$20 \times .000$	$\frac{1}{6} = .003\frac{1}{3}$		288
	.1581	6	912
		43	20
		86	4
		\$136.	800

ANALYSIS.—If the interest of \$1 for 1 yr. is \$.06, for 2 yr., it is twice \$.06, or \$.12. If the interest of \$1 for 1 mo. is \$.00 $\frac{1}{2}$ , for 7 mo., it is 7 times \$.00 $\frac{1}{2}$ , or \$.035. If the interest of \$1 for 1 day is \$.000 $\frac{1}{6}$ , for 20 days, it is 20 times \$.000 $\frac{1}{6}$ , or \$.003 $\frac{1}{3}$ . Hence the interest of \$1 for 2 yr. 7 mo. 20 da. is \$.12 + \$.035 + \$.003 $\frac{1}{6}$ , or \$.158 $\frac{1}{5}$ . The interest of \$864 is 864 times \$.158 $\frac{1}{5}$ , or \$136.80.

**447.** RULE.—Take as the interest of one dollar, six cents for each year, one-half cent (or five mills) for each month, and one-sixth of a mill for each day. Multiply the principal by the sum of these amounts (as an abstract number). The product will be the interest at 6%.

To find the amount, add the principal to the interest.

Notes.—1. In using this method, to multiply by  $\frac{3}{5}$ , write  $\frac{1}{5}$  twice ; to multiply by  $\frac{5}{5}$ , take  $\frac{1}{2}$  and  $\frac{1}{3}$ .

2. If the time is less than 60 days, and the rate is 6% or less, reckon the interest on the nearest number of dollars. The result will be sufficiently accurate.

**448.** The interest for any other rate may be found from the interest at 6% as follows: At 1%, divide by 6; at  $1\frac{1}{2}$ %, divide by 4; at 2%, divide by 3; at 3%, divide by 2; at 4%, subtract  $\frac{1}{3}$ ; at  $\frac{1}{2}$ %, subtract  $\frac{1}{4}$ ; at 5%, subtract  $\frac{1}{6}$ ; at  $5\frac{1}{4}$ %, subtract  $\frac{1}{4}$ ; at 5%, subtract  $\frac{1}{6}$ ; at  $5\frac{1}{4}$ %, subtract  $\frac{1}{4}$ ; at  $6\frac{1}{2}$ %, add  $\frac{1}{12}$ ; at  $6\frac{3}{4}$ %, add  $\frac{1}{8}$ ; at 7%, add  $\frac{1}{6}$ ; at  $7\frac{1}{2}$ %, add  $\frac{1}{4}$ ; at 8%, add  $\frac{1}{3}$ ; at 9%, add  $\frac{1}{2}$ ; at 10%, divide by 6, and multiply by 10 by placing the point one place to the right; at 12%, multiply by 2. At any per cent., divide by 6 and multiply by the rate.

449. For examples to be worked by the above method, see Art. 445 and Art. 459.

## Third or Month Method.

**450.** Ex. What is the interest of \$875 for 2 yr. 8 mo. 14 da., at 4%?

OPERATIO	Ν.	
\$875		
.04		
12) 35.00	Int. for 1 yr.	ANALYSIS.—The interest of \$875 for 1 yr.
2.917	Int. for 1 mo.	at 4% is \$35 (.04 × \$875), and for 1 mo. is $\frac{1}{12}$ of \$35, or \$2.917, 2 yr. 8 mo. = 32 mo. 14 da. =
$32.4\frac{2}{3}$	Number of mos.	$.3\frac{2}{3}$ mo. (To reduce days to tenths of a month,
972		divide the number of days by 3 and place the
972		point one place to the left.) If the interest for
11668		\$2.917, or \$94.71.
5834	•	
8751		
\$94.7052		

**451.** RULE.—Multiply the principal by the rate per cent., and divide the product by 12. The result will be the interest for one month at the given rate per cent. Multiply this result by the total number of months, the years being reduced to months and the days being expressed as tenths of a month.

452. For examples to be worked by this method, see Art. 445 and Art. 459.

## Fourth or 60-day Method at 6%.

**453.** 6% for 12 months or 1 year, is equivalent to 1% for 2 months (60 days), or  $\frac{1}{6}$  of one year. 1% of any amount is readily ascertained by placing the point two places to the left. Hence the interest of any sum at 6% per annum for 2 months, or 60 days, may be found by placing the point two places to the left. The interest for 6 days may be found by placing the point three places to the left.

Note.—It will be found advantageous to use a perpendicular line as a separatrix in solving examples by this method. All necessity for pointing off will then be dispensed with, and confusion prevented.
Art. 453.]

Ex. 1. What is the interest of \$1236 for 80 da., at 6%?

	OI	ERAT	ION.				ANA	LYS	IS.—'	The	inter	est o	f \$1	1236	i at
\$12	36 =	int.	for	60	da.	6%	for	60	da.	is fo	und	to be	\$12	.36,	by
4	12 =	"	66	20	da.	the	pro	cess	alr	eady	exp	laine	1.	If	the
\$16	48 =	66	"	80	da.	$\frac{1}{3}$	erest of 60	for ), it	60 wil	<i>da</i> . 1 be	is \$	12.36, \$12.3	for 6, or	20 \$4.	da. 12.
Hence	for 80	da.,	it wi	ll b	e \$12.36	plus	\$4.1	2, 0	r \$1	6.48.					

Ex. 2. Find the interest of \$864 for 1 yr. 10 mo. 15 da., at 6%.

	OPERATION.	ANALYSIS.—The interest of
\$8	64 = int. for 2 mo., or 60 da.	\$864 at 6% for 2 mo. is \$8.64.
	11	For 1 yr. 10 mo. (22 mo.), it
95	04 = int. for 22 mo.	will be 11 times \$8.64, or \$95.04. If the interest for
2	16 =  " " 15 da.	60 da. is \$8.64, for 15 da.
\$97	20 = required interest.	$(\frac{1}{4} \text{ of } 60)$ , it will be $\frac{1}{4} \text{ of } \$8.64$ , or $\$2.16$ Hence the interest
for th	a minor time will be 005 04 plug 00 16	or \$0% 90

tor the given time will be \$95.04 plus \$2.16, or \$97.20.

Ex. 3. What is the interest of 375.60 for 55 days, at 6%?

\$3	$75.60 = 313^{-} =$	int.	for 60	) da.	ANALYSIS, $-55$ days = 60 days less 5 days. The interest for 60 days is \$3.756, for 5 days ( $\frac{1}{12}$ of 60), \$.313, and
3	443 =	66		5	for 55 days, \$3.443 (\$3.756 - \$.313).

**454.** Aliquot Parts of 60.— $1 = \frac{1}{60}$ ;  $2 = \frac{1}{30}$ ;  $3 = \frac{1}{20}$ ;  $4 = \frac{1}{15}$ ;  $5 = \frac{1}{12}$ ;  $6 = \frac{1}{10}$ ;  $10 = \frac{1}{6}$ ;  $12 = \frac{1}{5}$ ;  $15 = \frac{1}{4}$ ;  $20 = \frac{1}{3}$ ;  $30 = \frac{1}{2}$ .

Notes.--1. To divide by 10, place the figures of the basis one place to the right.

2. To divide by 20, 30, or 60, divide by the first figure and write the quotient figures one place to the right.

455. Ex. 1. What is the interest of \$976 for 26 days, at 6%?

OPERATION							
\$9	76	=	int.	for	<u>60</u>	da.	
3	253	=	66	66	20	da.	
1	976	=	66	66	_6	da.	
4	229	=	66	"	26	da.	

ANALYSIS.—As 26 is not an aliquot part (**388**) of 60, take 20, which is  $\frac{1}{3}$  of 60, and 6, which is  $\frac{1}{10}$  of 60. Divide the basis which is the interest for 60 da. by 3 to find the interest for 20 da. (§3.253); and the same sum by 10, to find the interest for 6 da. (§.976). (See Art. **454**, 1.)

The sum of these two results will be the interest for '26 days.

Ex. 2. Find the interest of \$732.80 for 2 yr. 8 mo. 27 da., at 6%?

	· OPERATION.	ANALYSIS.—The interest
\$7	32.8 = int. for 2 mo., or 60 da.	for 2 mo., forming the basis,
	16	is \$7.328. Multiply this by
12	069	16 to find the interest for 32
40	500	mo. $(2 yr. 8 mo.)$ , $27 = 15 +$
73	28	12. To find the interest for
1	832 = int. for 15 da.	15 $da$ ., divide the basis by 4
1	466 =  " " 12 da.	$(15 = \frac{1}{4} \text{ of } 60)$ ; and the same
4.1.0.0		sum by 5 to find the interest.
\$120	546 = required int.	for 12 da. By adding these
7.1		

results, we have the interest for the given time at 6%.

**456.** If the number of days given is not an aliquot part of 60, it will need to be so separated that the component parts will be aliquot parts of 60.

Numbers not aliquot parts of 60, with best divisions: 7 = 6+1; 8 = 6+2; 9 = 6+3; 11 = 6+5, or 10+1; 13 = 10+3; 14 = 12+2; 16 = 10+6; 17 = 12+5, or 15+2; 18 = 12+6. (The interest for 18 days may be found by multiplying the basis by 3, and placing the figures of the product one place to the right); 19 = 15+4, or 10+6+3; 21 = 15+6; 22 = 20+2 ( $2 = \frac{1}{10}$  of 20); 23 = 20+3; 24 = 12+12 (or multiply by 4 and place the figures of the product one place to the right); 25 = 20+5 ( $5 = \frac{1}{4}$  of 20); 26 = 20+6; 27 = 15+12; 28 = 12+12+4 ( $4 = \frac{1}{8}$  of 12), or 20+6+2; 29 = 12+12+5, or 20+6+3.

**457.** RULE.—Draw a perpendicular line two places to the left of the decimal point; the result will be the interest at 6% for 2 months, or 60 days, the dollars being on the left, and the cents on the right of this line. Multiply this result by one-half the total number of months. To this product, add that proportion of the interest for 60 days, which the given number of days is of 60.

Note.—The interest at any other rate per cent. may be found as in Art, **448**.

**458.** The interest at 6% may be found for 6 days by placing the point three places to the left (**453**). In many examples, when the time is less than 100 days, the process is shortened by taking as the basis the interest for 6 days instead of 60 days.

Ex. Find the interest of \$375 for 8 days at 6%. \$425 for 79 days. \$500 for 47 days.

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Art. 458.]

#### INTEREST.

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1	ST OPER	ATION.		2n	D OPERATION.	3.	RD OPE	RATION.
\$	375	6 da.	\$	425	6 da.	\$	500	6 da.
	125	$\frac{2}{2}$ da.	5	525	78 da. $(13 \times 6)$	4	000	48 da.
	500	8 da.		071	1 da.	1000	083	1 da.
			5	596	79 da.	3	917	47 da.
		•						

# EXAMPLES.

459. Find the interest of the following at 6%. (See Arts. 453 and 454.)

		<i>.</i>	
1.	\$864 for 60 days.	/ 11.	\$1275 for 50 days.
2.	\$396 for 20 days.	/ 12.	\$2345 for 30 days.
3.	\$290 for 72 days.	13.	\$1728 for 63 days.
4.	\$785 for 66 days.	14.	\$375.60 for 5 days.
5.	\$636 for 62 days.	15.	\$414.80 for 54 days.
6.	\$400 for 90 days.	16.	\$1024 for 59 days.
7.	\$525 for 61 days.	17.	\$2375 for 90 days.
8.	\$600 for 10 days.	18.	\$1000 for 57 days.
9.	\$728 for 65 days.	19.	\$2480 for 63 days.
10.	\$340 for 15 days.	20.	\$5000 for 56 days.

What is the interest of

21. \$375.60 for 8 mo. 20 da., at 6%? At 5%? (See Ex. 2, Art. 453.)

22. \$1727 for 7 mo. 15 da., at 1%? At 3%? (448)

23. \$449.38 for 1 yr. 4 mo. 12 da., at 05? At 7%?

24. \$285 for 1 yr. 5 mo. 10 da., at 6%? At 5%?

25. \$432.65 for 2 yr. 2 mo. 6 da., at 6%? At 8%?

26. \$1235 for 2 yr. 5 mo. 5 da., at 6%? At 4%?

27. \$445.25 for 5 mo. 4 da., at 6%? At 9%?

28. \$2440.50 for 97 days, at 6%? At 7%? (See Ex. 1, Art. 455.)

29. \$3125 for 38 days, at 6%? At 7%?

30. \$247.50 for 69 days, at 6%? At 5%?

31. \$512.45 for 5 mo. 11 da., at 6%? At 7%? (See Ex. 2, Art. 455.)

32. \$1478 for 1 yr. 2 mo. 13 da., at 6%? At 8%?

33. \$2810.60 for 9 mo. 24 da., at 6%? At 5%?

34. \$944.50 for 1 yr. 10 mo. 22 da., at 6%? At  $4\frac{1}{2}\%$ ?

35. \$575 for 2 yr. 8 mo. 16 da., at 6%? At 9%?

#### INTEREST.

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[Art. 459.

N	
36. \$1112 for 3 mo. 14 da., at	$6\%$ ? At $4\frac{1}{2}\%$ ?
37. \$5285 for 1 yr. 6 mo. 21 de	a., at 6%? At 3%?
38. \$7218 for 11 mo. 18 da., at	6%? At 12%?
Find the amount of	
39. \$416.75 for 8 mo. 17 da., a	at 6%? At 7%?
40. \$1235 for 2 yr. 1 mo. 19 de	a., at 6%? At 8%?
41. \$575.60 for 1 yr. 4 mo. 23	da., at 6%? At 5%?
42. \$2214 for 4 mo. 25 da., at	6%? At 4%?
43. \$6315 for 5 mo. 29 da., at	6%? At 9%?
44. \$4312 for 4 mo. 26 da., at	6%? At 41%?
45. \$384.30 for 2 mo. 28 da., a	t 6%? At 3%?
46. \$1296 for 1 yr. 11 mo. 27 a	la., at 6%? At 12%?
47. \$4375 for 2 yr. 8 mo. 24 de	a., at 6%? At $5\frac{1}{2}$ %?
Find the interest of the followi	ing at 6%. (See Art. 458.)
48. \$2000 for 6 da.	53. $3748$ for 53 da. (54-1.)
49. \$1728 for 37 da.	54. \$4126 for 89 da.
50. \$3485 for 92 da.	55. \$1289 for 39 da.
51. \$1234 for 69 da.	56. \$4000 for 17 da.
52. \$375.60 for 8 da.	57. \$2000 for 28 da.
NT	1 1-41 * 41 11

NOTE.—Find the time in the following examples both in months and days, and in exact days (310).

58. \$1234 from May 10 to Dec. 4, at 5%? At 43%?

59. \$444.40 from Jan. 13 to Nov. 2, at 4%? At 51%?

60. \$575.20 from June 5, 1882, to Feb. 4, 1883, at 7%? At 5%?

61. \$2375 from July 17, 1884, to Nov. 27, 1885, at 6%? At 31%? (Exact time, 1 yr. 133 da.)

62/\$3212 from Aug. 24, 1881, to Jan. 20, 1884, at 4%? At 41/??

63. \$475.80 from May 12, 1882, to Feb. 1, 1884, at 7%? At 10%?

64. Find the interest of \$180 for 253 days, at 6%. At 8%.

Note.—In many examples, labor can be saved by having the time and principal exchange places. In the above example, the interest of \$180 for 253 days is the same as \$253 for 180 days ( $$2.53 \times 3$ ).

65. Find the interest of \$600 for 173 days at 9%. At 4%.
66. Find the interest of \$3000 for 111 days at 12%. At 3%.

Find the interest of

67. \$1800 from Jan. 17 to Oct. 2, at 6%. At 43%.

68. \$540 from May 11 to Dec. 18, at 5%. At  $4\frac{1}{2}$ %.

69. \$3000 from Feb. 4 to July 13, at 4%. At  $4\frac{1}{2}$ %.

70. \$2400 from July 13 to Dec. 1, at 5%. At 54%.

71. \$600 from Aug. 16 to Nov. 24, at 6%. At 51%.

72. \$1200 from May 19 to July 3, at 7%. At 61%.

73. \$480 from March 13 to Sept. 3, at 8%. At 3½%.

74. \$720 from Feb. 27 to May 15, at 9%. At 43%.

75. \$2100 from Sept. 2 to Nov. 30, at 10%. At 71%.

76. If \$9200 is loaned Sept. 18, 1882, at 6%, what is due May 9, 1885? (Time by C. S.)

77. What is a banker's gain in 1 year on \$10000 deposited at 6%, and loaned 11 times at  $1\frac{1}{2}$ % a month ?

78. A note for \$1421, with interest after 4 months, at 7%, was given Dec. 1, 1881, and paid Aug. 12, 1883. What was the amount due? (C. S.)

79. Nov. 6, 1881, I bought a lot of grain for \$753.20; Dec. 16, I sold a part of it for \$375.60; and, Dec. 31, I sold the remainder for \$411.40. Money being worth 6%, how much did I gain by the transaction?

80. A merchant marks his goods with two prices, the one for cash and the other for 4 months' credit. If the cash price is \$28, what ought the credit price to be, money being worth 10%?

81. May 27, \$328 is loaned at 6%, and Aug. 16, \$1000 is loaned at 5½%. What is the total amount due Dec. 11?

82. A banker borrows \$100000 at  $3\frac{1}{2}\%$ , and pays the interest at the end of the year; he loans it at 5% and receives the interest semi-annually. How much does he gain in one year, if he loans the semi-annual interest until the end of the year?

83. A buys a bill of goods amounting to \$2776.40, on the following terms: —"4 months, or less 5% cash." He accepts the latter terms, and borrows the money at 6% to pay the bill. How much does he gain?

84. A person buying a building lot for \$5400, agreed to pay for it in four equal semi-annual installments, with interest at 6%; what was the total amount of money paid, the first payment being made at the time of the purchase ?

85. A banker borrows \$10000 at  $4\frac{1}{2}$ %, and lends half of it at 6% and half at 8%. What does he gain in 2 yr. 4 mo. 26 da.?

# ACCURATE INTEREST.

460. To find the accurate interest (365 days to the year) for any rate and time. (See Art. 437.)

Ex. What is the accurate interest of \$865, at 4%, from June 21 to Dec. 13?

OPERAT	ION.	
\$865	Principal.	ANALYSIS.—From June 21 to Dec. 13,
.04		there are 175 days. The interest of \$865
		for 1 yr., at 4%, is \$34.60. For 175 days,
34.60	Interest for 1 yr.	$(175 \times 34.60)$
175		$\frac{1}{365}$ of 1 yr., it is $\frac{175}{365}$ of \$34.60 (365),
) 6055.00	( 16.59	or \$16.59.

**461.** RULE.—Multiply the principal by the rate per cent. expressed decimally. The result will be the interest for one year.

Multiply the interest for one year by the number of days, and divide the product by 365.

Notes.—1. When the number of days is a multiple of 5, multiply by  $\frac{1}{6}$  the number of days, and divide the product by 73. In the above example,  $\$865 \times .04 \times 35 \div 73 = \$16.59$ .

2. To find the interest at any per cent., multiply by twice the rate as an integer, by the number of days, divide the product by 73, and point off 3 places. In the above example,  $\$865 \times 8 \times 175 + 73000 = \$16.59$ .

3. To find the interest at 5%, multiply the principal by the number of days, divide the product by 73, and point off 2 places. From this result to find the interest at 6%, add  $\frac{1}{5}$ ;  $4\frac{1}{2}$ %, subtract  $\frac{1}{10}$ ; 4%, subtract  $\frac{1}{5}$ .

462. Accurate Interest from Ordinary Interest.—The difference between ordinary interest and accurate interest for 1 day equals the difference between  $\frac{1}{360}$  and  $\frac{1}{365}$  of a year's interest.

 $\frac{1}{360} - \frac{1}{365} = \frac{365 - 360}{365 \times 360} = \frac{5}{365 \times 360} = \frac{5}{365} \text{ of } \frac{1}{360} = \frac{1}{73} \text{ of}$  $\frac{1}{360} \cdot \frac{5}{365 \times 360} = \frac{5}{360} \text{ of } \frac{1}{365} = \frac{1}{72} \text{ of } \frac{1}{365}.$ 

The difference between the two methods is  $\frac{1}{75}$  of ordinary interest, or  $\frac{1}{75}$  of accurate interest (**437**, Note 4). Therefore, from ordinary interest to find accurate interest subtract  $\frac{1}{75}$ .

365

Art. 462.]

In reckoning accurate interest, on account of the many short methods of ordinary interest, many accountants prefer to calculate ordinary interest first, and then make the necessary deduction.

Since  $\frac{1}{18}$  is about  $1\frac{1}{3}\%$ , the following approximate method may be used in reducing ordinary interest to accurate interest: From the ordinary interest subtract 1% and  $\frac{1}{3}\%$  of itself.

Ex. Reduce \$32.70 ordinary interest to accurate interest.

#### OPERATION.

32.70		NOTE.—The exact result should be \$32.252. The
.327	1%	results by this method are too great by 1 cent for each \$27
32.373	1.0%	interest; \$.036 for each \$100 interest; \$.36 for each \$1000 interest. Where greater accuracy is required, the neces-
.100	3/0	sary correction can be made.
32.264		

#### EXAMPLES.

463. What is the accurate interest of

1. \$435.32, at 6%, for 25 days? 5. \$292, at 31%, for 140 days?

2. \$6030, at 5%, for 141 days? 6. \$438, at 6%, for 210 days?

3. \$780, at 6%, for 90 days? 7. \$350, at 4%, for 150 days?

4. \$437.80, at 7%, for 63 days? 8. \$500, at 41%, for 100 days?

9. \$3110.45, at 51%, for 90 days?

10. \$373.70, at 7%, from June 4 to Dec. 28?

11. \$500, at 6%, from July 24, to Sept. 16?

12. \$365, at 6%, from June 30 to Dec. 21?

13. \$1080, at 5%, from May 9, 1878, to Jan. 30, 1879?

14. \$1728, at 7%, from Jan. 6, 1878, to Jan. 21, 1880?

1. Required the exact interest on three U. S bonds of \$5000 each, at  $3\frac{1}{2}$ %, from July 1 to Aug. 11.

16. What is the interest on three U. S. bonds of \$1000 each, at  $4\frac{1}{2}$ %, from Sept. 1 to Nov. 15?

17. What is the interest on a \$5000 U.S. bond, at 4%, from Oct. 1 to Dec. 16?

18. What is the interest on a U. S. bond of \$1000, bearing  $3\frac{1}{2}\%$  interest, from May 1 to July 19?

19. What is the interest on a \$500 U. S. bond, at 4%, from Apr. 1 to May 10,?

20. What is the interest on a \$5000 U. S. bond from Nov. 1, 1881, to Jan. 3, 1832, at  $3\frac{1}{2}$ ?

21. What is the difference between ordinary and accurate interest of \$10000 for 219 days at 6%?

# PROBLEMS IN INTEREST.

# 464. To find the rate, the principal, interest or amount, and time being given.

Ex. At what rate will \$720, in 1 yr. 4 mo. 10 da., produce \$44.10 interest?

	OPERATION.	ANALYSIS. — The interest on a
\$7	20	given principal for a given time is in
	8	proportion to the rate per cent. At one
57	60	per cent. \$720 will, in 1 yr. 4 mo. 10 da., produce \$9.80 interest. To produce
1	20	\$44.10 interest, the required rate must
$6)\overline{58}^{$	80	be as many times 1%, as \$9.80 is con-
\$9	80) \$44.10 ( 41 Ans.	tained times in \$44.10, or $4\frac{1}{2}$ times. Hence the answer is $4\frac{1}{2}$ %.

**465.** RULE.—Divide the given interest by the interest of the given principal, for the given time, at 1%.

Note.—When the amount is given, find the interest by subtracting the principal from the amount.

# EXAMPLES.

466. At what rate will

1. \$864 in 8 mo. 10 da. produce \$42 interest?

2. \$1000 in 9 mo. 9 da. produce \$54.25 interest ?

3. \$852 in 1 yr. 7 mo. 16 da. amount to \$935.21 ?

- 4. \$1926 in 2 yr. 8 mo. 24 da. produce \$263.22 interest?
- 5. \$375.60 in 1 yr. 10 mo. 22 da. amount to \$425.41?

6. \$1872 in 7 mo. 17 da. produce \$41.31 interest?

7. \$435.60 in 1 yr. 2 mo. 18 da. amount to \$478?

8. \$1338.72 in 6 mo. 27 da. produce \$34.64 interest?

9. \$1728 in 8 mo. 21 da. amount to \$1778.11?

10. \$3456 in 5 mo. 8 da. produce \$91.01 interest ?

11. \$5280 in 11 mo. 11 da. amount to \$5720.12?

12. \$1234 in 8 mo. 22 da. produce \$80.83 interest?

13. \$6975 in 3 mo. 28 da. amount to \$7215.06?

14. \$525 in 1 yr. 11 mo. 18 da. produce \$309.75 interest?

15. \$500 in 3 yr. 11 mo. 12 da. amount to \$658?

16. \$4680 in 2 yr. 6 mo. 11 da. produce \$710.58 interest?

17. \$614.45 in 162 days amount to \$633.805?

Art. 467.]

467. To find the time, the principal, interest or amount, and rate being given.

Ex. In what time will \$426, at 6%, produce \$59.427 interest?

	OPERATIONS.		
\$426	Or,	\$426	
.06		.06	
\$25.56) \$59.427 ( y	r. 2.325	\$25.56)	\$59.427 ( 2 yr.
51 12	12		51 12
8 307 m	o. 3.900		8.307
7 668	30		12
	a. 27.000	\$25.56	99.684 ( 3 mo.
5112	·		76.68
12780			23.004
12780			30
0		\$25.56	690.120 ( 27 da

ANALYSIS.—The interest on a given principal at a given rate % is in proportion to the time. In one year \$426, at 6%, will produce \$25.56 interest. To produce \$59.427 interest, it will require as many years as \$25.56 is contained times in \$59.427, or 2.325 yr. 2.325 yr. equal 2 yr. 3 mo. 27 da. (289).

**468.** RULE.—Divide the given interest by the interest of the given principal, at the given rate, for one-year.

The integral part of the quotient will be years. Reduce the decimal, if any, to months and days (289).

### EXAMPLES.

469. In what time will

1. \$3000, at 7%, produce \$108.50 interest?

2. \$1728, at 6%, amount to \$1872?

3. \$3932, at 7%, produce \$597.88 interest?

4. \$735, at 5%, amount to \$742.66?

5. \$1222.25, at 6%, produce \$39.52 interest?

6. \$375.60, at 7%, amount to \$425.41?

7. \$1461.75, at 6%, produce \$420.25 interest?

8. \$1200, at  $3\frac{3}{4}$ %, amount to \$1413?

9. \$4500, at 5%, produce \$181.25 interest?

10. \$276.50, at 10%, amount to \$303.46?

In what time will

11. \$1020, at 6%, produce \$89.25 interest?

12. \$6495, at 7%, amount to \$7161.81?

13. \$100, at 6%, produce \$100 interest?

14. \$125, at 7%, amount to \$375?

470. To find the principal, the interest, time, and rate being given.

Ex. What principal will produce \$152.64 interest, in 1 yr. 5 mo. 20 da., at 6%?

	OPERATION.
\$.0883	) \$152.64 (1728
3	3
.265	) 457.920
	265
	1929
	1855
	742
	530
	2120
	2120

ANALYSIS.—The interest on any principal is as many times greater than the interest of \$1, as that principal is greater than \$1. One dollar, in 1 *yr*. 5 *mo*. 20 *da*., at 6% (**447**), will produce \$.088 $\frac{1}{3}$  interest. To produce \$152.64, the principal must be as many times \$1 as \$.088 $\frac{1}{3}$  is contained times in \$152.64, or \$1728.

**471.** RULE.—Divide the given interest by the interest of \$1 for the given time, at the given rate.

# EXAMPLES.

472. What principal will produce

1. \$1235 interest, in 1 yr. 8 mo. 12 da., at 6%?

2. \$49.81, in 9 mo. 24 da., at 7%?

3. \$186.75, in 1 yr. 4 mo. 20 da., at 6%?

4. \$244.44, in 7 mo. 18 da., at 5%?

5. \$375.60, in 2 yr. 4 mo. 6 da., at 8%?

6. \$54.25, in 3 mo. 3 da., at 7%?

7. \$387.40, in 2 yr. 8 mo., at 41%?

8. \$456, in 93 da., at 6%?

9. \$375, in 63 da., at 7%?

10. \$1000, in 1 yr. 18 da., at 3%?

11. \$538.80, in 10 mo. 24 da., at 5%?

12. \$416.75, in 8 mo. 21 da., at 4%?

13. \$645.39, in 4 yr. 8 mo. 10 da., at 4%?

Art. 473.]

473. To find the principal, the amount, time, and rate, being given.

Ex. What principal will amount to \$1880.64, in 1 yr. 5 mo. 20 da., at 6%?

OPERATION. \$1.088<del>1</del>) \$1880.64 (1728.

3 3	
$\begin{array}{c} 3.265 \\ \hline 3.265 \\ \hline 3265 \\ \hline 23769 \\ \hline 22855 \\ \hline 9142 \\ \hline 6530 \\ \hline 26120 \\ \hline 26120 \\ \hline 0 \\ \hline \end{array}$	ANALYSIS. — The amounts of different principals for the same time and rate $\%$ , are to each other as the principals. One dollar, in 1 gr. 5 mo. 20 da., at 6% will amount to $\$1.088\frac{1}{3}$ . To amount to $\$1880.64$ , the prin- cipal must be as many times $\$1$ as $\$1.088\frac{1}{3}$ are contained times in $\$1880.64$ , or $\$1728$ .

**474.** RULE.—Divide the given amount by the amount of \$1 for the given time, at the given rate.

# EXAMPLES.

47	5. What principal will amount to
1.	\$1272.254, in 6 mo. 6 da., at 6%?
2.	\$5538.72, in 8 mo. 12 da., at 7%?
3.	\$3695.04, in 1 yr. 4 mo. 18 da., at 5%?
4.	\$442.71, in 2 yr. 2 mo. 24 da., at 8%?
5.	\$14794.31, in 3 yr. 3 mo. 3 da., at 6%?
6.	\$1793.38, in 7 mo. 17 da., at 6%?
7.	\$1010.65, in 5 yr. 8 mo. 6 da., at 7%?
8.	\$977.75, in 1 yr. 10 mo. 10 da., at 6%?
9.	\$1716.75, in 3 yr. 4 mo. 21 da., at 4%?
10.	\$2808.08, in 2 yr. 8 mo. 12 da., at 8%?
11.	\$4312.22, in 1 yr. 2 mo. 11 da., at 12%?
12.	\$6528.49, in 4 yr. 7 mo. 6 da., at 5%?
13.	\$1763.02, in 1 yr. 2 mo. 21 da., at 6%?
14.	\$2457.28, in 2 yr. 5 mo. 23 da., at 6%?
15.	\$5375.34, in 1 yr. 6 mo. 15 da., at 4%?
16.	\$3536.87, in 2 yr. 7 mo. 10 da., at 9%?
17.	$4221.50$ , in 3 yr. 10 mo. 27 da., at $4\frac{1}{2}$ %

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# PRESENT WORTH AND TRUE DISCOUNT.

476. The Present Worth of a debt due at some future time is its value now. Theoretically, it is a sum that, if placed at interest to-day for the given time, would amount to the face of the debt.

**477.** The **True Discount** is the difference between the face of the debt and the present worth.

This subject is an application of the principle illustrated in Art. 473, the face of the debt being the amount, the present worth the principal, and the true discount the interest.

In actual business true discount is little used, banks and merchants generally using bank discount (496). True discount is the interest on the present worth for the given time, while bank discount is interest on the face of the debt. The difference is therefore equivalent to the interest on the true discount. For discount on bills, etc., when time does not enter as an element, see Art. 415.

Ex. Mr. B owes me \$212, payable one year from to-day without interest; what is the present worth of the debt, the current rate of interest being 6%?

ANALYSIS.—Since \$1 in one year, at 6%, amounts to \$1.06, it would require as many dollars to amount to \$212, as \$1.06 is contained times in \$212, or \$200. The true discount is \$212—\$200, or \$12.

**478.** RULE.—I. To find the present worth, divide the face of the debt by the amount of \$1 for the given time, at the given rate.

II. To find the true discount, subtract the present worth from the face of the debt.

# EXAMPLES.

479. The current rate of interest being 6%, what is the present worth and true discount of

1. \$1000, due 2 years hence? 3. \$600, due in 1 yr. 7 mo.?

2. \$500, due in 2 yr. 4 mo.? 4. \$800, due in 9 mo. 24 da.?

5. \$325, due in 2 yr. 5 mo. 12 da.?

6. \$175, due in 1 yr. 4 mo. 16 da.?

7. \$800, due in 5 yr. 8 mo. 22 da.?

8. \$900, due in 6 yr. 8 mo. 14 da.?

9. Mr. C. desiring to pay a bill of \$1728 4 months before it was due, was allowed a discount equivalent to the interest on the face of the bill for the unexpired time at 6% per annum (bank discount). How much greater was this discount than the true discount?

10. Goods to the amount of \$3750 are sold on a credit of 4 months. For how much cash could the merchant afford to sell the same goods, money being worth 10% per annum?

11. If \$10000 will be due me May 28, and \$8000 May 16, what discount should I make on the two claims Apr. 1, money being worth 8%?

# REVIEW EXAMPLES.

**480.** 1. What is the interest of \$375.60, for 1 yr. 10 mo. 16 da., at 6%?

2. What is the amount of \$1765 for 7 mo. 20 da., at 7%?

3. At what rate will \$1234, in 2 yr. 2 mo. 26 da., produce \$138.14 interest?

4. In what time will \$585, at 6%, produce \$67.08 interest?

5. What principal will, in 1 yr. 8 mo. 14 da., at 6%, produce 176.22 interest?

6. The semi-annual interest on a mortgage at 7% is \$350. What is the face of the mortgage ?

7. Mr. B. invests \$49500 in a business that pays him \$594 per month. What annual rate of interest does he receive ?

8. Which is the better investment, and what per cent., one of \$8400, yielding \$336 semi-annually, or one of \$15000, producing \$1425 annually?

9. May 18th, a speculator bought 1600 bushels of wheat, at \$1.50 a bushel. He afterward sold the whole for \$2472 cash, his profit being equivalent to 8% per annum on the amount invested. What was the date of the sale ?

10. The par value of Mr. A.'s bank stock is \$9000, and he receives a semi-annual dividend of \$315. What per cent. is the dividend per annum?

11. Mrs. C.'s son is now 16 yr. old; how much must she invest for him at 6%, that, on arriving at age, he may have, with simple interest, \$25000?

12. A bill of goods amounting to \$4316.75 is due May 27; how much would settle it May 1 at 6%? How much July 3?

13. A gentleman loaned \$15000, at 6%. Jan. 1, 1880, interest and principal together equalled \$20000. When was the money loaned?

14. Find the interest on \$3000, from Mar. 16 to Dec. 4, at 6%, by the following methods (437): 1, ordinary interest and compound subtraction; 2, ordinary interest and exact number of days; 3, accurate interest.

15. A man loaned another a sum of money, payable in 5 months, with interest at the rate of 6%, and at the end of that time received \$666.25 in return. How much did he loan?

16. A speculator borrowed \$10925 at 6%, May 16, 1882, with which he purchased flour at \$6.25 per barrel. June 11, 1883, he sold the flour at \$7.50 per barrel, cash. What did he gain ?

17. B bought 225 A. 24 sq. rd. of land, Aug. 18, 1882, at \$4 an acre, borrowing the money to pay for it, at 5%. He sold the land April 7, 1886, at an advance of \$299.40 on cost. If mean-while he paid \$46.50 for taxes on the land, did he gain or lose, and how much ?

18. A speculator bought 9000 bu. grain at \$1.80 per bushel, Mar. 18, 1875, the money paid for it being borrowed at  $5\frac{1}{2}\%$ . Dec. 12, 1875, he sold  $\frac{2}{5}$  of the grain at \$2.00 per bushel, and the remainder at \$1.90 per bushel. What was gained or lost by the transaction?

19. A owes B £260 9s. 6d., with interest at 5%, for 143 days. He pays 25% of the amount due; how much remains?

Note.—In England, interest is usually computed on the basis of 365 days to the year, when the time is given in days. The legal rate in England is 5%. To calculate interest on English money, reduce the shillings and pence to the decimal of a pound (see Art. 342, Ex. 12, Note), apply any of the methods under Art. 461, and reduce the resulting decimal to shillings and pence.

# Find the accurate interest of

£425, from Aug. 4 to Dec. 28, at 5%.
 £625 12s., from Jan. 12 to Apr. 1, at 4%.
 £717 16s. 10d., from Mar. 3 to June 16, at 4½%.\*
 £429 10s. 8d., from Sept. 16 to Nov. 30, at 3%.
 £516 18s. 3d., from Aug. 1 to Oct. 18, at 3½%.
 £612 6s. 11d., from July 1 to Nov. 3, at 5%.

\* When the time is less than 1 year, and the rate is 6% or less, reject the pence, if less than 6; add 1 shilling, if more than 6. The result will be sufficiently accurate.

# **COMPOUND INTEREST.\***

**481.** Compound Interest is interest not only on the principal, but also on the interest after it becomes due (433).

1. Interest may be compounded annually, semi-annually, quarterly, etc.

2. Interest upon interest due, or compound interest, cannot be collected by law, that is, payment cannot be enforced; but such a payment is equitable, and the receiving of it, if the debtor is willing or can be induced to pay it, does not constitute usury in the legal sense of the word. In the State of Missouri, parties may contract in writing for the payment of interest upon interest, but it shall not be compounded oftener than once a year.

Ex. What is the compound interest of \$1000 for 3 years, at 6%?

\$1000.00	Principal.	$\mathbf{Or}$	\$1000
60.00	Interest for 1 yr.		1.06
1060	Amount for 1 yr., or 2d principal.		1060
63.60	Interest of \$1060 for 1 yr.		1.06
1123.60	Amount for 2 yr., or 3d principal.		1123.60
67.416	Interest of \$1123.60 for 1 yr.		1.06
1191.016	Amount for 3 yr.		1191.016
1000	Original principal.		1000
191.016	Compound interest for 3 yr.		191.016

**482.** RULE.—Find the amount of the given principal for the first period of time, and make it the principal for the second. Find the amount of the second principal for the second period of time, and make it the principal for the third; and so continue for the whole time. The last amount is the amount required.

The last amount, less the given principal, will be the compound interest.

Notes.—1. When the time is not a multiple of the interest period, find the amount of the principal to the end of the last period; then compute the simple interest on this amount for the remaining time, and add it to the last amount. The sum will be the required amount.

2. The work of computing compound interest may be shortened by using the tables on pages 194 and 195.

\* For Annual Interest, see page 319.

#### INTEREST.

[Art. 483

Yrs.	2%.	21%.	- 3,0.	3 <sup>1</sup> <sub>2</sub> %.	4%.	41%.	5%.	6%.	7%.	Yrs.
1 2 3 4 5	$\begin{array}{r} 1.0200\\ 1.0404\\ 1.0612\\ 1.0824\\ 1.1041 \end{array}$	$\begin{array}{r} 1.0250 \\ 1.0506 \\ 1.0769 \\ 1.1038 \\ 1.1314 \end{array}$	$\begin{array}{r} 1.0300 \\ 1.0609 \\ 1.0927 \\ 1.1255 \\ 1.1593 \end{array}$	$\begin{array}{r} 1.0350 \\ 1.0712 \\ 1.1087 \\ 1.1475 \\ 1.1877 \end{array}$	$\begin{array}{r} 1.0400\\ 1.0816\\ 1.1249\\ 1.1699\\ 1.2167\end{array}$	$\begin{array}{r} 1.0450 \\ 1.0920 \\ 1.1412 \\ 1.1925 \\ 1.2462 \end{array}$	$\begin{array}{r} 1.0500\\ 1.1025\\ 1.1576\\ 1.2155\\ 1.2763\end{array}$	$\begin{array}{r} 1.0600\\ 1.1236\\ 1.1910\\ 1.2625\\ 1.3382 \end{array}$	$\begin{array}{r} 1.0700\\ 1.1449\\ 1.2250\\ 1.3108\\ 1.4026\end{array}$	1 2 3 4 5
6 7 8 9 10	$\begin{array}{r} 1.1262 \\ 1.1487 \\ 1.1717 \\ 1.1950 \\ 1.2190 \end{array}$	$\begin{array}{r} 1.1597 \\ 1.1887 \\ 1.2184 \\ 1.2489 \\ 1.2801 \end{array}$	$\begin{array}{c} 1.1941 \\ 1.2299 \\ 1.2668 \\ 1.3048 \\ 1.3439 \end{array}$	$\begin{array}{r} 1.2293 \\ 1.2723 \\ 1.3168 \\ 1.3629 \\ 1.4106 \end{array}$	$\begin{array}{r} 1.2653 \\ 1.3159 \\ 1.3686 \\ 1.4233 \\ 1.4802 \end{array}$	$\begin{array}{r} 1.3023 \\ 1.3609 \\ 1.4221 \\ 1.4861 \\ 1.5530 \end{array}$	$\begin{array}{r} 1.3401 \\ 1.4071 \\ 1.4775 \\ 1.5513 \\ 1.6289 \end{array}$	$\begin{array}{c} 1.4185 \\ 1.5036 \\ 1.5928 \\ 1.6895 \\ 1.7908 \end{array}$	$\begin{array}{r} 1.5007 \\ 1.6058 \\ 1.7182 \\ 1.8385 \\ 1.9672 \end{array}$	6 7 8 9 10
11 12 13 14 15	$\begin{array}{r} 1.2434 \\ 1.2682 \\ 1.2936 \\ 1.3195 \\ 1.3459 \end{array}$	$\begin{array}{c} 1.3121 \\ 1.3449 \\ 1.3785 \\ 1.4130 \\ 1.4483 \end{array}$	$\begin{array}{r} 1.3842 \\ 1.4258 \\ 1.4685 \\ 1.5126 \\ 1.5580 \end{array}$	$\begin{array}{r} 1.4600 \\ 1.5111 \\ 1.5640 \\ 1.6187 \\ 1.6753 \end{array}$	$\begin{array}{r} 1.5395 \\ 1.6010 \\ 1.6651 \\ 1.7317 \\ 1.8009 \end{array}$	$\begin{array}{r} 1.6229 \\ 1.6959 \\ 1.7722 \\ 1.8519 \\ 1.9353 \end{array}$	$\begin{array}{r} 1.7103 \\ 1.7956 \\ 1.8856 \\ 1.9799 \\ 2.0789 \end{array}$	$\begin{array}{r} 1.8983 \\ 2.0122 \\ 2.1329 \\ 2.2609 \\ 2.3966 \end{array}$	$\begin{array}{r} 2.1049 \\ 2.2522 \\ 2.4098 \\ 2.5785 \\ 2.7590 \end{array}$	11 12 13 14 15
16 17 18 19 20	$\begin{array}{r} 1.3728 \\ 1.4002 \\ 1.4282 \\ 1.4568 \\ 1.4859 \end{array}$	$\begin{array}{r} 1.4845 \\ 1.5216 \\ 1.5597 \\ 1.5987 \\ 1.6386 \end{array}$	$\begin{array}{r} 1.6047 \\ 1.6528 \\ 1.7024 \\ 1.7535 \\ 1.8061 \end{array}$	$\begin{array}{r} 1.7340 \\ 1.7947 \\ 1.8575 \\ 1.9225 \\ 1.9898 \end{array}$	$\begin{array}{r} 1.8730 \\ 1.9479 \\ 2.0258 \\ 2.1068 \\ 2.1911 \end{array}$	$\begin{array}{r} 2.0224 \\ 2.1134 \\ 2.2085 \\ 2.3079 \\ 2.4117 \end{array}$	$\begin{array}{r} 2.1829 \\ 2.2920 \\ 2.4066 \\ 2.5270 \\ 2.6533 \end{array}$	2.5404 2.6928 2.8543 3.0256 3.2071	$\begin{array}{r} 2.9522 \\ 3.1588 \\ 3,3799 \\ 3.6165 \\ 3.8697 \end{array}$	16 17 18 19 20
21 22 23 24 25	$\begin{array}{r} 1.5157 \\ 1.5460 \\ 1.5769 \\ 1.6084 \\ 1.6406 \end{array}$	$\begin{array}{r} 1.6796 \\ 1.7216 \\ 1.7646 \\ 1.8087 \\ 1.8539 \end{array}$	$\begin{array}{r} 1.8603 \\ 1.9161 \\ 1.9736 \\ 2.0328 \\ 2.0938 \end{array}$	2 0594 2.1315 2.2061 2.2833 2.3632	2.2788 2.3699 2.4647 2.5633 2.6658	$\begin{array}{r} 2.5202 \\ 2.6337 \\ 2.7522 \\ 2.8760 \\ 3.0054 \end{array}$	2.7860 2.9253 3.0715 3.2251 3.3864	3.3996 3.6035 3.8197 4.0489 4.2919	$\begin{array}{r} 4.1406\\ 4.4304\\ 4.7405\\ 5.0724\\ 5.4274\end{array}$	21 22 23 24 25
26 27 28 29 30	$\begin{array}{r} 1.6734 \\ 1.7069 \\ 1.7410 \\ 1.7758 \\ 1.8114 \end{array}$	$\begin{array}{r} 1.9003 \\ 1.9478 \\ 1.9965 \\ 2.0464 \\ 2.0976 \end{array}$	$\begin{array}{r} 2.1566\\ 2.2213\\ 2.2879\\ 2.3566\\ 2.4273\end{array}$	$\begin{array}{r} 2.4460\\ 2.5316\\ 2.6202\\ 2.7119\\ 2.8068\end{array}$	$\begin{array}{c} 2.7725\\ 2.8834\\ 2.9987\\ 3.1187\\ 8.2434 \end{array}$	$\begin{array}{r} 3.1407 \\ 8.2820 \\ 3.4297 \\ 3.5840 \\ 3.7453 \end{array}$	$\begin{array}{r} 3.5557 \\ 3.7335 \\ 3.9201 \\ 4.1161 \\ 4.3219 \end{array}$	$\begin{array}{r} 4.5494 \\ 4.8223 \\ 5.1117 \\ 5.4184 \\ 5.7435 \end{array}$	5.8074 6.2139 6.6488 7.1143 7.6123	26 27 28 29 30
81 82 83 34 35	$\begin{array}{r} 1.8476 \\ 1.8845 \\ 1.9222 \\ 1.9607 \\ 1.9999 \end{array}$	$\begin{array}{c} 2.1500 \\ 2.2038 \\ 2.2589 \\ 2.3153 \\ 2.3732 \end{array}$	2.5001 2.5751 2.6523 2.7319 2.8129	2.9050 3.0037 3.1119 8.2209 8.3336	3.3731 3.5081 3.6434 3.7943 3.9461	$\begin{array}{r} 3.9139 \\ 4.0900 \\ 4.2740 \\ 4.4664 \\ 4.6673 \end{array}$	$\begin{array}{r} 4.5380 \\ 4.7649 \\ 5.0031 \\ 5.2538 \\ 5.5160 \end{array}$	6.0881 6.4534 6.8406 7.2510 7.6861	$\begin{array}{r} 8.1451 \\ 8.7153 \\ 9.3253 \\ 9.9781 \\ 10.6766 \end{array}$	31 32 33 34 85
36 37 38 39 40	$\begin{array}{c} 2.0399\\ 2.0807\\ 2.1223\\ 2.1647\\ 2.2080 \end{array}$	$\begin{array}{r} 2.4325\\ 2.4933\\ 2.5557\\ 2.6196\\ 2.6851 \end{array}$	2 8983 2.9852 3.0748 3.1670 3.2620	8.4503 8.5710 8.6960 8.8254 8.9598	$\begin{array}{r} 4.1039\\ 4.2681\\ 4.4388\\ 4.6164\\ 4.8010\end{array}$	$\begin{array}{r} 4.8774 \\ 5.0969 \\ 5.3262 \\ 5.5659 \\ 5.8164 \end{array}$	$5.7918 \\ 6.0814 \\ 6.3855 \\ 6.7048 \\ 7.0400$	8.1473 8.6361 9.1543 9.7035 10.2857	$\begin{array}{c} 11.4239 \\ 12.2236 \\ 13.0793 \\ 13.9948 \\ 14.9745 \end{array}$	36 37 38 39 40
41 42 43 44 45	2.2522 2.2972 2.3432 2.3901 2.4379	2.7522 2.8210 2.8915 2.9638 3.0379	3.3599 3.4607 3.5645 3.6715 3.7816	$\begin{array}{r} 4.0978 \\ 4.2413 \\ 4.3897 \\ 4.5433 \\ 4.7024 \end{array}$	4.9931 5.1928 5.4005 5.6165 5.8412	$\begin{array}{c} 6.0781 \\ 6.3516 \\ 6.6374 \\ 6.9361 \\ 7.2482 \end{array}$	7,3920 7.7616 8.1497 8.5572 8.9850	$\begin{array}{c} 10.9029 \\ 11.5570 \\ 12.2505 \\ 12.9855 \\ 13.7646 \end{array}$	$\begin{array}{c} 16.0227\\ 17.1443\\ 18.3444\\ 19.6285\\ 21.0025 \end{array}$	41 42 43 44 45

**483.** Table showing the sum to which \$1 will increase, at compound interest, in any number of years not exceeding 45.

To find the sum to which a given amount will increase, at compound interest, at any of the rates per cent. and number of years expressed in the above Table :

Multiply the given amount by the sum to which one dollar will increase at the rate and for the number of years required, marking off as many decimals from the product as there are decimals in the multiplier and multiplicand.

Notes.—1. The amount for any number of years not given in the table may be computed by finding the product for any two numbers of years whose sum equals the given time. Thus, the compound amount of \$1 at 6% for 55 years, may be found by multiplying \$13.7646, the amount for 45 years, by 1.7908, the amount for 10 years.

2. If the interest is compounded semi-annually, to find the amount from the table, take twice the number of years at one-half the rate. Thus, the amount at 8%, compounded semi-annually, for 5 years, is equivalent to the amount for 10 periods of 6 months each, at 4% for each period, and is the same as the amount for 10 years at 4%. If the interest is compounded quarterly, take 4 times the number of years at one-fourth the rate.

3. The compound interest of \$1 is \$1 less than the amounts in the above table.

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								T	
Yrs.	3%.	31%.	4%.	5%.	6%.	77.	8%.	10%.	Yrs.
1	1.0300	1.0350	1.0400	1.0500	1.0600	1.0700	1 0800	1.1000	1
2	2.0909	2.1062	2.1216	2.1525	2.1836	2.2149	2 2464	2.3100	2
3	3.1836	3.2149	3.2465	3.3101	3,3746	3.4399	3.5061	3.6410	3
4	4.3091	4.3625	4.4163	4.5256	4.6371	4.7507	4.8666	5.1051	4
5	5.4684	5,5502	5.6330	5.8019	5.9753	6.1533	6.3359	6.7156	5
6	6 6695	6 77701	6 9099	7 1490	7 2029	7 6540	7 0998	8 4970	G
	7 0020	0.1101	0.0000	0 5401	8 8075	0 9508	0.6966	10 4950	- 77
	0.1501	0.0011	0.4140	10.0991	10.4012	10.0790	11 1076	10.4000	
0	9.1091	10 7914	11 0001	11 5770	10.1000	19 8164	12 4966	14 0974	0
30	11.4003	10 1014	10.4004	11.0779	19 0716	14 7998	15.4600	17 5919	9
10	11.0010	14.1440	12.4004	15.2005	10.3110	12.7000	10.0400	11.0012	-10
11	13.1920	13.6020	14.0258	14.9171	15.8699	16.8885	17.9771	20.3843	11
12	14.6178	15 1130	15.6268	16.7130	17.8821	19.1406	20.4952	23.5227	12
13	16.0863	16.6770	17.2919	18.5986	20.0151	21.5505	23.2149	26.9750	13
14	17.5989	18.2957	19.0236	20.5786	22.2760	24.1290	26.1521	30.7725	14
15	19.1569	19.9710	20.8245	22.6575	24.6705	26.8881	29.3243	34.9497	15
16	90 7616	21 7050	99 6075	94 8404	27 2129	20 8402	32,7502	89 5447	16
17	29 4144	23 4997	94 6454	97 1394	29,9057	32,9990	36 4502	44 5002	17
10	94 1160	95 9579	06 6719	90 5900	89 7600	36 9700	40 4463	50 1501	19
10	95 9704	97 9707	00.0112	29.0000	95 7856	20.0055	14 7690	56 9750	10
90	97 6765	90 9605	20.0609	94 7/109	38 0027	12 9650	40 4990	62 0025	20
~	21.0100	A3.A030	00.0092	04,1190	00.0001	10.0002	20.2000	00.0020	20
21	29.5368	31.3290	33.2480	37.5052	42.3923	48.0058	54.4568	70.4027	21
22	31.4529	33.4604	35.6179	40.4305	45.9958	52.4361	59.8963	78.5430	22
23	33.4265	35.6665	38.0826	43,5020	49.8156	57.1767	65.7648	87.4973	23
24	35,4593	37.9499	40.6459	46.7271	53.8645	62.2490	72.1059	97.3471	24
25	37.5530	40.3131	43.3117	50.1135	58.1564	67.6765	78.9544	108.1818	25
26	39 7096	42,7591	46 0842	53 6961	62.7058	73 4838	86 3508	120,0999	26
27	41,9309	45.2906	48 9676	57 4026	67.5281	79 6977	94,3358	133.2099	27
98	44 9188	47 9108	51 0669	61 9997	72 6398	86 9465	102 0650	147 6800	98
20	46 5754	50 6997	55 0840	65 /1999	78 0582	03 4609	119 9999	163 4940	- <u>90</u>
20	40.0007	53.4205	50.0010	60.7600	83 8017	101 0720	199 9450	180 0494	20
00	10.0021	00-1000	00.0400	03.1000	00.0011	101.0100	100.0100	100.0101	00
31	51.5028	56.3345	61.7015	74.2988	89.8898	109.2182	133.2135	200.1378	31
32	54.0778	59.3412	65.2095	79.0638	96.3432	117.9334	144.9506	221.2515	32
33	56.7302	62.4532	68.8579	84.0670	103.1838	127.2588	157.6267	244.4767	33
34	59.4621	65.6740	72.6522	89.3203	110.4348	137.2369	171.3168	270.0244	34
35	62.2719	69.0076	76.5983	94.8363	118,1209	147.9135	186.1021	298.1268	35
36	65,1742	72.4579	80 7022	100.6281	126.2681	159.3374	202.0703	329.0395	36
37	68.1594	76.0289	84 9703	106 7095	134 9042	171.5610	219.3159	363.0434	37
38	71 9342	79 7949	89 4091	118 0050	144 0585	184 6403	237 9412	400.4478	38
30	74 4013	83 5503	04 0255	110.0000	152 7690	108 6951	258 0565	441 5996	30
40	77 6693	87 5005	08 8965	126 8308	164 0477	913 6006	279 7810	496 8518	40
-10	11.0000	01.0000	00.0400	140.0000	101.010	210.0000	210.1010	200.0010	10
41	81.0232	91.6074	103.8196	134.2318	174.9506	229.6322	303.2435	536.6370	41
43	84.4539	95.8486	109.0124	141.9933	136.5076	246.7765	328.5830	091.4007	42
43	88.0484	100.2383	114.4129	150.1430	198.7580	205.1208	335.9496	001.0408	43
44	91.7199	104.7817	120.0294	158.7002	211.7435	284.7493	385.5056	111.9048	44
45	95.5015	109.4840	125.8706	167.6852	225.5081	305.7518	417.4261	790.7953	45
46	99.3965	114.3510	131.9454	177.1194	240.0986	328,2244	451.9002	870.9749	46
47	103.4084	119.3883	138.2632	187.0254	255.5645	352.2701	489.1322	959.1723	47
48	107.5406	124.6018	144.8337	197.4267	271.9584	377,9990	529.3427	1056.1896	48
49	111.7969	129.9979	151.6671	208.3480	289.3359	405.5289	572.7702	1162,9085	. 49
50	116.1807	135.5828	158.7738	219.8154	307.7561	434.9859	619.6718	1280.2993	50

**484.** Table showing the sum to which \$1, paid at the beginning of each year will increase at compound interest, in any number of years not exceeding 50.

To find the sum to which a given amount, per annum, will increase at compound interest, at any of the rates per cent. and number of years expressed in the above Table:

Multiply the given amount, per annum, by the sum to which one dollar per annum will increase at the rate and for the number of years required, marking off as many decimals from the product as there are decimals in the multiplier and multiplicand.

Note.—If the amount be payable semi-annually, and compound interest is to be allowed semi-annually, take the amount for double the number of years at one-half the rate per cent. Thus, for a semi-annual payment of \$1 for 10 years at 10 per cent., take the amount of \$1 for 20 years at 5 per cent. = \$34.7193. For a quarterly payment, take the amount for four times the number of years at one-fourth the rate per cent.

# EXAMPLES.

**485.** 1. What will \$450 amount to at compound interest, in 4 years, compounded annually at 4%? At 3%?

2. Find the compound interest of \$360, for 2 years, interest compounded semi-annually at 6%. At 5%.

3. What is the compound interest of \$800 for 1 yr. 3 mo. at 8%, interest compounded quarterly?

4. At compound interest, what is the amount of \$1728 for 3 yr. 4 mo. 16 da., interest compounded annually at 3%? At 6%?

Note.—First find the amount for 3 years, and use this amount as the principal for the remaining time.

5. B holds a mortgage against A's property dated Apr. 1, 1881, for \$20000, interest payable annually at 6%. The interest due Apr. 1, 1882, is not paid until May 26, 1882. How much is then due, A having consented to pay interest upon interest? (See Note 2, Art. **481**.)

Note.—In solving the following examples, use the tables in Art. 483-484.

6. A gentleman deposits in a savings bank \$100 when his child is one year old. How much will this amount to when the child is 21 years old, interest being compounded semi-annually at 4%? At 5%?

7. If, at the age of 25 years, a person places \$2000 on interest, compounded annually at 6%, what will be the amount due him when he is 50 years old ?

8. What will \$625 amount to at compound interest, in 36 years, compounded annually at 3%? At 4%?

9. At the age of 20, and every year thereafter, a young man places \$200 at compound interest at 6%. How much will he have at the age of 30? At the age of 40? (See Art. **484**.)

19. How much will a gentleman have at the end of three years, if he places at compound interest at 5% \$300 at the beginning of each year?

11. Mr. B., whose life is insured for \$4000, pays an annual premium of \$114. How much would this amount to at 6% compound interest in 20 years?

12. A lady deposits \$50 in a savings bank Jan. 1 and July 1, of each year; how much will be placed to her credit in 15 years, money being worth 6%, compound interest? 13. What sum must be placed at compound interest, at 6%, to amount to \$1000 in 5 years ?

Note.—In compound interest, as in simple interest, the amounts are proportional to the principals; hence the amount of any principal is as many times greater than the amount of \$1, as that principal is greater than \$1.

To find the principal, divide the given amount by the amount of \$1 for the given time and rate.

In simple interest, the interest on a given principal for a given time is in proportion to the rate per cent., and at a given rate, in proportion to the time; but, in compound interest, such is not the case. If the rate or time be doubled, the interest is more than doubled.

14. How much should a gentleman invest at compound interest, 6%, for his son who is now 6 years old, so that, when he becomes 21 years of age, he may have \$10000?

15. In the above example, how much should be invested at the beginning of each year to produce the same sum ?

16. A gentleman at his death left \$7850 for the benefit of his only son, 12 years old, the money to be paid to him when he should be 21 years of age. How much did he receive, interest at 6%, compounded semi-annually?

17. How much must a person at the age of 25 years, place at compound interest at 6%, so that the amount due him, when he is 50 years old, will be \$20000 ?

18. In the above example, how much should he invest annual to produce the same sum ?

# COMMERCIAL PAPER.

486. Commercial Paper embraces notes, drafts, bill exchange, etc.

**487.** A Note (also called a Promissory Note) is a well on promise to pay a certain sum of money on demand or at a specified time.

**488.** The Maker of a note is the person who signs it, and thus becomes responsible for its payment. The **Payee** is the person to whom, or to whose order, it is made payable. The **Face** of a note is the sum promised.

In Note 1, Art. **495**, Peter Cooper is the maker ; George Peabody is the payee; the face of the note is \$1000.

**489.** A Negotiable Note is a note which is made payable to bearer or to the order of some person. (See Notes, Art. **495.**)

1. A note is *non-negotiable* when it is payable only to the party named in the note.

2. A negotiable note made in New Jersey must contain the words "without defalcation or discount;" in Missouri, the words "negotiable and payable without defalcation or discount."

3. Negotiable notes payable to order may be sold or transferred by the payee writing his name upon the back of the note. He then becomes an indorser.

4. Negotiable securities are good in the hands of one who purchases in good faith and before maturity, although the seller may have found or stolen them.

5. Where no place of payment is specified, a promissory note is payable at the maker's place of business, or if none is known, at the residence of the maker.

6. A note or draft must be presented at the place where it is made payable. If at a bank, during banking hours; if at a place of business, during business hours; if at a residence, during family hours; and if the maker, or some one for him, is not ready with legal tender currency to pay it, the holder need not call again. A check, even if certified, is not a legal tender, and may be lawfully refused.

**490.** The **Indorser** of a note or draft is the person who writes his name on the back of it, and by so doing guarantees its payment.

If Mr. Erastus Corning desires to sell or transfer Note 3, Art. **495**, it will be necessary for him to indorse it. If he writes his name only, it is called an indorsement *in blank*, and the note is then payable without further indorsement to any person lawfully holding the same. He may indorse it *in full* by making it payable to a particular person, thus—"Pay to the order of Henry R. Pierson, Erastus Corning." Before it can be again transferred, it will require the indorsement of Henry R. Pierson. For greater security, checks, notes, drafts, etc., are indorsed in full when sent by mail.

If an indorser does not wish to guarantee the payment of a note, draft, etc., he writes "Without recourse" over his name at the time of the indorsement.

Sometimes notes and drafts are drawn to the order of the maker or the drawer (to the order of myself or ourselves) to facilitate their transfer without the indorsement of the holder.

**491.** A Draft, or Bill of Exchange is an order or request addressed by one person to another, directing the payment of a specified sum of money to a third person or to his order.

492. The Drawer of the draft is the person who signs it. The Drawee is the person on whom it is drawn. The Payee is the person to whom, or to whose order, it is made payable.

In Draft 5, Art. 495, C. P. Huntington is the drawer; Drexel, Morgan & Co. are the drawees; J. & W. Seligman & Co. are the payees.

1. The person in whose favor the bill is drawn is sometimes called the buyer, and becomes the "remitter." After the bill is presented and accepted, the drawee is called the acceptor, and the draft, an acceptance. The draft then has the same legal significance as a promissory note.

2. A person accepts or promises to pay a draft by writing the word "Accepted" and the date over his name across its face.

3. Drafts are sometimes accepted in the following form :---" Accepted August 20, 1881, and payable at the National Park Bank, New York, G. B. Horton & Co."

4. In the State of New York, both by law and custom, the drawee of a draft may demand 24 hours consideration from the time the draft is presented for acceptance.

When accepted, it must bear the date when first seen by him.

5. To "honor" a draft is to accept it or pay it on being presented.

493. A Protest is a formal statement made by a Notary Public, declaring that a draft or note has been presented for payment or acceptance, and was refused.

494. Days of Grace and Maturity.-The day of maturity is the day on which a note becomes legally due. According to the laws of most of the States, a note is not legally due until three days after the expiration of the time specified in the note, except the note contain the words "without grace." These days are called *days of grace*, but they are of no advantage to the payer, since interest is charged for them as for any others.

1. California has abolished days of grace altogether. In Georgia, Alabama, and Kentucky, grace is allowed on promissory notes only in case they are made payable, or are discounted or left for collection, at a bank or private banker's.

2. The following is an analysis of the Holiday law of 1887 of the State of New York :

Paper due on a holiday is payable the following business day.

Paper due on Saturday, except when payable at sight or on demand, is payable the following business day.

Paper due on Sunday must be paid on the business day following it. If one of the mentioned holidays falls on Sunday, paper due on that day must be paid the following business day.

Paper due on Monday, where the preceding Sunday is a holiday, is not payable until the following business day.

3. In nearly all of the States, excepting New York, paper due on Sunday, or on a legal holiday, must be paid the preceding business day. Thus, if a holiday falls on Thursday, all notes, etc., must be paid on Wednesday; if a holiday falls on Monday, all notes due Sunday or Monday would be payable on Saturday; if a holiday falls on Saturday, notes due Saturday or Sunday would be payable on Friday.

4. The legal holidays in the State of New York are New Year's Day (Jan. 1), Washington's Birthday (Feb. 22), Decoration Day (May 30), Independence Day (July 4), Labor Day (the first Monday of September), Election Day (the first Tuesday after the first Monday of November), Thanksgiving Day (the day appointed by the President of the United States and Governor of the State, usually the last Thursday of November), Christmas Day (Dec. 25), and every Saturday from 12 o'clock at noon until 12 o'clock at midnight (Saturday Half-Holiday).

When a legal holiday falls on Sunday, Monday is, by the statute of New York, made a legal holiday.

5. A note made due at a fixed date in the future, carries 3 days' grace (unless the words "without grace" are used in the contract). Thus, a note stating that "on May 1, 1882, I promise, etc.," would carry 3 days' grace, and would be payable May 4, 1882.

6. When the time of a note is expressed in months, calendar months are used to determine the day of maturity; when in days, the exact number of days is used.

Thus, a note dated July 16, and payable two months from date, would nominally mature Sept. 16, and, including the three days of grace, would legally mature Sept. 19. A note having the same date, and payable sixty days from date, would nominally mature Sept. 14, and, including the three days of grace, would legally mature Sept. 17.

7. A note due in one or more months from date, matures on the corresponding day of the month up to which it is reckoned, *if there are so many days in that month*; but if not so many, it then matures on the last day of said month, to which the usual grace must be added. Thus, notes dated Jan. 28, 29, 30, or 31, and payable one month from date, would become due Mar. 3 (Feb. 28 with 3 days' grace added).

8. When drafts are payable a certain time after *sight*, the date of acceptance and the time of the draft determine the day of maturity. Thus, if a draft is dated May 16, accepted May 20, and payable sixty days after sight, it would mature or be due 63 (including 3 days of grace) days after May 20, or July 22. If payable 60 days after *date*, it would mature 63 days after May 16, or July 18. It is not necessary to present for acceptance drafts drawn a certain time after date, but as a courtesy to the drawee, it is usually done.

9. Days of grace are allowed on drafts according to the custom of the place where they are payable. The statute of New York forbids grace on all sight drafts, no matter on whom drawn, and on all time drafts which appear on their face to be drawn "upon any bank, or upon any banking association or individual banker, carrying on the banking business under the act to authorize the business of banking."

# 495. FORMS OF NOTES AND DRAFTS.

# 1. DEMAND NOTE.

# NEW YORK, August 19, 1887.

On demand, I promise to pay GEORGE PEABODY, or bearer, One Thousand Dollars. Value received.

# PETER COOPER.

The above note is payable on demand,—that is, whenever presented; is negotiable (payable to bearer); and bears interest from date at the legal rate of the State in which it is made. If the words "or bearer" were omitted the note would not be negotiable.

How much would be due on the above note, Jan. 1, 1888, finding the time by compound subtraction?

# 2. TIME NOTE-INTEREST-BEARING.

# CINCINNATI, OHIO, July 16, 1888.

Six months after date, I promise to pay GEO. C. MILLER, or order, Eight Hundred Seventy-five and  $\frac{44}{100}$  Dollars, with interest at eight per cent. Value received.

# ALEX. MCDONALD.

The above note is payable 6 mo. 3 da. after its date, or Jan. 19, 1889; is negotiable (payable to order); and draws interest from its date at 8% per annum. If the rate of interest was omitted, it would bear interest at the legal rate of the State for such cases, 6%. (See Art. **436**.)

How much would be due on the above note at its maturity? How much, March 1, 1889? Supposing the rate of interest to be omitted in the note, how much would be due May 4, 1889?

3. TIME NOTE—WITHOUT INTEREST—PAYABLE AT A BANK. \$6000. ALBANY, N. Y., December 4, 1889.

Sixty days after date, I promise to pay to the order of ERASTUS CORNING, Six Thousand Dollars, at the Second National Bank. Value received.

# DAVID MURRAY.

The above note is payable 63 days from Dec. 4, 1889, or Feb. 5, 1890. It is payable at the Second National Bank. No interest will be due at maturity (Feb. 5). If the note is not paid at maturity, it will bear interest from that date.

Supposing the above note was payable 90 days from date, what would be its due date (**311**, Ex. 10)? The note as given not being paid at maturity, how much would be due Feb. 25, 1890, protest fees \$2.10?

\$1000.

\$875 44.

# INTEREST.

[Art. 495.

# 4. JOINT AND SEVERAL NOTE.

WORCESTER, MASS., May 27, 1888.

Four months after date, we jointly and severally promise to pay JOHN S. BALLARD & Co., or order, Four Hundred Sixteen  $\frac{32}{100}$  Dollars, with interest from date, value received.

T. K. EARLE.

# CHAS. W. SMITH.

If the above note were written "we jointly promise, etc.," it would be called a *joint note*. The makers of a joint note must be sued jointly, each being responsible for one-half of the amount of the note. The makers of a joint and several note may be sued separately, either being responsible for the full amount of the note.

How much would be due on the above note, Dec. 30, 1888? How much Sept. 30, 1888, the date of maturity?

# 5. SIGHT DRAFT.

SAN FRANCISCO, CAL., May 1, 1882.

At sight, pay to the order of J. & W. SELIGMAN & Co., Eight Thousand Dollars, value received.

C. P. HUNTINGTON.

To DREXEL, MORGAN & Co., New York.

6. TIME DRAFT.

#### \$5000.

\$8000.

BURLINGTON, IOWA, June 18, 1887.

At sixty days' sight, pay to the order of ADDISON BALLARD, Five Thousand Dollars, value received, and charge to account of A. G. ADAMS.

To BARTON & JONES, Chicago, Ill.

Drafts are sometimes drawn a certain number of "days after date." (See Art. **494**, Note 8.)

For Foreign Bills of Exchange, see Art. 555.

If the above draft was accepted June 19, 1887, what was the date of maturity?

7. A sixty-day (63) day note given on Monday will mature on what day?

8. A note payable 90 (93) days from date and given on Thursday will fall due on what day of the week? If payable in 30 (33) days and given on Friday, on what day will it become due?

9. A note dated July 22, and payable in 90 (93) days, would mature on what date?

\$416-32.

# BANK DISCOUNT.

**496.** Bank Discount is simple interest of a note, paid in advance, for the number of days the note has to run. It may be computed by any of the methods given for simple interest.

On notes without interest (the usual case of notes discounted at banks), bank discount is reckoned on their face, the amount due at maturity; on notes with interest, it is reckoned on the amount due at maturity, or their face plus the interest for the full time of the note.

**497.** The **Proceeds** of a note is the amount received by the holder from the bank when the note is discounted. It is the amount on which the discount is reckoned less the discount.

498. Call Loans.—Banks in the large cities loan large amounts of money upon stocks, bonds, negotiable warehouse receipts for grain, cotton, petroleum, etc., as collateral security, payable on demand or on giving one day's notice. Such loans are termed "call" or demand loans, and interest on them is paid at the end of the time. (See Art. 436, Note d.)

**499.** The time to be reckoned on a loan or note is exclusive of the day of date, but includes the day of maturity or payment. Thus, in discounting a note in the City of New York, Apr. 4, which would mature Apr. 24, the discount would be calculated for 20 days.

1. In Philadelphia, Baltimore and some other cities it is the custom of banks in finding time to include both the day of discount and the day of maturity. Thus, the discount on the above note would be reckoned for 21 days.

2. Banks of the City of New York reckon discount both on the basis of 360 and 365 days to the year, the greater number on the former basis.

3. When notes are payable in other cities or towns, some banks charge interest for the time required for the collecting bank to remit the money, in addition to the interest on the note from the day of discount to the legal day of maturity. Thus, if a note, maturing June 10 and payable at a Chicago bank, is discounted at a bank in New York, the remittance in settlement would not be received before June 12 in New York, and the New York bank in discounting the note would be justified in charging interest for two days beyond the day of maturity.

4. Some banks charge a small fee for collection and exchange in addition to the interest in discounting notes which are payable in other cities or towns.

#### EXAMPLES.

500. Find the date of maturity and proceeds of the following notes:

(1.) NEW YORK, July 16, 1889. Four months after date, I promise to pay to the order of FISK & HATCH, Ten Thousand Dollars, at the first National Bank, value received.

Discounted July 16, 1889, at 6%.

ANALYSIS.—The note is due 4 months (494, 6) and 3 days (days of grace, 494) after July 16, or Nov. 19. From the day of discount (July 16) to the day of maturity (Nov. 19) there are 126 days.

The interest of \$10000 for 126 days at 6%, if reckoned on the basis of 360 days to the year, is \$210, and the proceeds are \$10000 less \$210, or \$9790.

The interest on the basis of 365 days to the year would be \$2.88 less, or \$207.12, and the proceeds would be \$9792.88.

If the note was discounted Sept. 1, the interest or discount would be reckoned for 79 days (Sept. 1 to Nov. 19).

# BROOKLYN, N. Y., July 16, 1891.

Ninety days from date, I promise to pay S. B. CHITTENDEN, or order, Eight Thousand Dollars, value received.

A. A. Low.

Discounted Aug. 31, 1891, at 6%.

ANALYSIS.—The note is due 93 days (494) after July 16, or Oct. 17. Compute the discount for 47 days (Aug. 31 to Oct. 17) on \$8000.

If the note had been discounted July 16, the date of the note, the interest would have been computed for 93 days, the full time of the note.

NOTE.-The results of the following examples will be given on the basis of both 360 and 365 days to the year.

No.	Date of Note.	Time.	Face.	Date of Discount.	Rate of Discount.
3	Jan. 24	90 days	\$1200	Jan. 24	6%
4	May 18	3 mo.	\$5280	May 18	6%
5	Aug. 31	60 days	\$2560	Aug. 31	8%
6	June 4	4 mo.	\$3756	June 4	7%
7	Oct. 16	30 days	\$6425	Oct. 16	5%
8	Mar. 13.	6 mo.	\$8375	Mar. 13	$5\frac{1}{2}\%$

\$10000.

\$8000.

S. D. BABCOCK.

No.	Date of Note.	Time.	Face.	Date of Discount.	Rate of Discount.
9 10 11 19	May 29 July 27 Mar. 28 Nar. 27	3 mo. 60 days 90 days	\$4500 \$8240 \$4324 \$4955	July 7 Sept. 2 Apr. 14	$   \begin{array}{c}     10\% \\     6\% \\     5\frac{1}{4}\% \\     8\%   \end{array} $
12 13 14 15	Jan. 3 Sept. 12 Nov. 1	0 mo. 120 days 4 mo. 90 days	\$9000 \$5000 \$6000	Feb. 28         Oct. 14         Nov. 28	6% 6% 7% 5 <u></u> \$%

16. What were the proceeds of Note 3, Art. 495, if discounted Dec. 16, 1889, at the legal rate?

17. Find the date of maturity and proceeds of a note of \$5000 payable 60 days from date, dated and discounted at a Philadelphia bank, Aug. 3. (See Art. **499**, 1.)

18. Find the date of maturity and proceeds of a note of \$3750, payable 60 days from date, dated and discounted at a Maryland bank, Jan. 31, 1882.

Note.—In the following examples, the charge for collection and exchange is a certain per cent. of the face of the notes, without reference to the time they have to run (499, 4).

No.	Date of Note.	Time.	Face.	Date of Discount.	Rate of Discount.	Rate of Collection.
19	May 5	90 days	\$7000 \$9000	May 5	6% 5%	18%0 1-%
21 22 23	June 18 July 28	6 mo. 60 days	\$5000 \$4500 \$9000	July 31 Aug. 1	8% 6% 51%	$\frac{1}{20}\%$ $\frac{1}{10}\%$ $\frac{1}{10}\%$
24	Aug. 5	4 mo.	\$3000	Oct. 18	6%	18%

Required the proceeds and date of maturity of the following notes discounted (360 days to the year) through a broker, his commission being  $\frac{1}{7}$  of the face of the notes.

No.	Date of Note.	Time.	Face.	Date of Discount.	Rate of Discount.
25	Feb. 21           June 8           Jan. 10           Mar. 3	4 mo.	\$10000	Feb. 21	4 <sup>8</sup> / <sub>4</sub> %
26		4 mo.	\$6000	June 12	4 <sup>1</sup> / <sub>2</sub> %
27		4 mo.	\$6000	Jan. 10	4 <sup>1</sup> / <sub>4</sub> %
28		6 mo.	\$8775	Apr. 30	4 <sup>8</sup> / <sub>4</sub> %

#### INTEREST.

29. May 4, a New York bank discounts, at 6%, a note of \$8000, payable in St. Louis, Sept. 1. What are the proceeds, if interest is charged for the two days required for the remittance of a draft in settlement?

30. A note dated Mar 27, for \$9000, payable in 4 months at a bank in Omaha, is discounted the same date at a bank in Providence, R. I. What were the proceeds, if interest for 3 days beyond the day of maturity is charged ?

31. A broker discounts a note payable in 4 months at  $4\frac{3}{4}\%$ , and charges  $\frac{1}{4}\%$  brokerage. This is equivalent to what rate of interest per annum, making no allowance for the days of grace?

32. A merchant can discount a note at his bank at 6%, 365 days to the year, or through a broker at  $4\frac{3}{4}$ %, 360 days to the year, broker's commission  $\frac{1}{4}$ %. How much better is the latter method on a note of \$10000, payable in 4 months, dated and discounted May 21 ?

Find the date of maturity and proceeds of the following interest-bearing notes

# (33.)

ALBANY, N. Y., September 16, 1881.

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Four months after date, I promise to pay W. J. KLINE or order, Three Thousand Dollars, with interest at 5%, value received.

J. M. THOMAS.

Discounted Nov. 3, 1881, at 6%.

Note.—Compute the discount at 6% for 77 days (Nov. 3 to Jan. 19) on the amount due at maturity (\$3000 plus the interest of \$3000 for 4 months and 3 days at 5%).

34. A note dated May 27, 1879, payable in 3 months, for \$3750, with interest at 7%; discounted May 27, 1879, at 8%.

35. A note dated Jan. 16, 1879, payable in 4 months, for \$1632, with interest at 6%; discounted Mar. 5, 1879, at 7%.

36. A note dated Oct. 12, 1878, payable in 6 months, for \$875, with interest at 7%; discounted Jan. 10, 1879, at 10%.

37. For what amount must a note be given for 60 days to afford 1000 proceeds, if discounted at 6%?

ANALYSIS.—The proceeds of any note is as many times greater than the proceeds of \$1, as the face of the note is greater than \$1. If a note of \$1 is discounted for 63 days at 6%, it will afford \$.9895 proceeds; to afford \$1000 proceeds, the face of the note must be as many times \$1, as \$.9895 is contained times in \$1000, or \$1010.61.

\$3000.

The following approximate method is generally used by business men: To the given proceeds, add the interest for the given time.

The interest of \$1000 for 63 days is 10.50. 1000 + 10.50 = 1010.50. Since the interest is reckoned on the proceeds instead of the face of the note, the error, 11 cents, is equivalent to the interest of the interest (\$10.50) for the given time.

Where greater accuracy is required, the necessary correction may be made. The interest of \$10.50 for 63 days is 11 cents. 1010.50 + 11 = 1010.61.

38. A owes B \$1500; how large a 90-day note must A give B that when discounted at a bank at 6%, the proceeds will be sufficient to pay the debt?

39. I hold a note of \$3000 against Mr. C., which he pays by giving a new note at 90(93) days for \$1500, and the balance, including the discount on the new note, in cash. Required the amount of cash paid.

40. A merchant having \$8000 to pay, gets a note for \$5000, that will mature in 40 days, discounted at a bank at 6%. How large a note must he draw, payable in 90 (93) days, for discount at the same rate, that the proceeds of the two notes may enable him to meet his payment?

# PARTIAL PAYMENTS.

**501.** Partial Payments are payments in part of a note, mortgage, or other debt, made at different times.

502. Indorsements are the acknowledgments of the payments, written on the back of the note, mortgage, etc., and stating the amount and date of the payment.

Special receipts are sometimes given for such payments.

# UNITED STATES RULE.

503. Ex. How much would be due Sept. 1, 1882, on a note of \$600, dated March 1, 1882, with interest at 6%? Suppose a payment of \$100 be made Sept. 1, 1882, to pay the interest and part of the principal, how much would then be due? Ans. \$518.

Ex. How much would be required to settle the above note Jan. 1, 1883, the balance of \$518 remaining on interest at the same rate from Sept. 1, 1882? Ans. \$528.36. Ex. Find the amount due on the following note, Jan. 19, 1885:

\$1000.

BOSTON, MASS., Aug. 1, 1881.

One year after date, I promise to pay JORDAN, MARSH & Co., or order, One Thousand Dollars, for value received, with interest from date, at 6 per cent.

# ALEXANDER H. RICE.

On this note are the following indorsements: Received Apr. 21, 1882, \$200. Received Dec. 1, 1882, \$25. Received July 7, 1884, \$400.

NOTE.—The method given in the following operation, is that adopted by the Supreme Court of the United States, and has been made the legal method of nearly all the States. By the United States Rule, as this is generally called, settlements are made whenever the payments are equal to or exceed the interest due; if the payment exceeds the interest, it is applied first to discharge the interest, and the surplus is applied towards paying the principal; if the payment is less than the interest, it is not applied until the payments, taken together, are sufficient to pay all interest due; since no unpaid interest is added to the principal to draw interest, a new principal can never be greater than the preceding principal.

OPERATION.	
Face of note, or principal, from Aug. 1, 1881	\$1000
Interest from Aug. 1, 1881, to Apr. 21, 1882 (8 mo. 20 da.), added	43.33
Amount, Apr. 21, 1882,	1043.33
First payment, Apr. 21, 1882,	200.00
New principal from Apr. 21, 1882	843.33
Interest of \$843.33 from Apr. 21, 1882, to Dec. 1, 1882,	
(7 mo. 10 da.) \$30.92	
(Interest exceeds the payment, and a new principal is	
not formed.)	
Interest of \$843.33 from Dec. 1, 1882, to Aug. 1, 1883,	
(8 mo.)	64.65*
[Payments \$125 (\$25 + \$100), now greater than the interest due	
(\$64.65)].	
Amount, Aug. 1, 1883,	907.98
Second and third payments, \$25 + \$100	125
New principal from Aug. 1, 1883	782.98

<sup>\*</sup> In many cases it can be determined mentally in advance whether the payment is greater or less than the interest. In this case the interest could be taken at once from Apr. 21, 1883, to Ang. 1, 1883 (1 yr. 3 mo. 10 da.), since it is evident that the payment (\$25) is less than the interest of \$843.33 for 7 mo. 10 da. (The interest of \$800 for 7 mo. is  $3\frac{1}{2} \times \$3$ , or \$33, and it would be more on \$433.33 for 7 mo. 10 da.) If it is doubtful whether the payment is greater or less than the interest, perform all the work.

209 PARTIAL PAYMENTS. Art. 503.1 New principal from Aug. 1, 1883 . . \$782.98 Interest of \$782.98 from Aug. 1, 1883, to July 7, 1884 (11 mo. 6 da.) 43.85 Amount, July 7, 1884. 826.83 Fourth payment, July 7, 1884, 400 426.83 New principal from July 7, 1884 Interest of \$426.83 from July 7, 1884, to Jan. 19, 1885 (6 mo. 13.66 12 da.) . Amount due Jan. 19, 1885, the final day of settlement, Ans. \$440.49

504. UNITED STATES RULE.—Find the amount of the given principal to the time when the payment or the sum of the payments exceeds the interest due; subtract from this amount the payment or the sum of the payments. Treat the remainder as a new principal, and proceed as before, to the time of settlement.

EXAMPLES.

**505.** Notes.—1. In the following examples, find the time by compound subtraction.

2. In the first five examples, all the payments exceed the interest. \$1680. TRENTON, N. J., Oct. 9, 1880.

1. On demand, I promise to pay COOPER, HEWITT & Co., or order, Sixteen Hundred Eighty Dollars. Value received.

JOHN A. ROEBLING.

On this note were indorsed the following payments : Dec. 21, 1881, received \$289.12. June 9, 1883, received \$991.50.

How much was due Jan. 30, 1884?

2. On a note dated May 11, 1877, for \$2000, are the following indorsements : — Aug. 6, 1879, \$361; Feb. 11, 1880, \$901.60; Nov. 2, 1882, \$1000. What remained due Feb. 2, 1883, at 6%? At 5%?

S. On a note dated July 11, 1878, for \$2400, are the following.
indorsements : — Sept. 17, 1879, \$200; Jan. 29, 1880, \$400; Nov.
29, 1881, \$1150. What is the amount due Jan. 11, 1882, the interest being at 6%? At 7%?

4. On a mortgage for \$1700, dated May 28, 1880, there was paid Nov. 12, 1880, \$80; Sept. 20, 1881, \$314; Jan. 2, 1882, \$50; Apr. 17, 1882, \$160. What was due Dec. 12, 1882, at 6%? At 8%?

#### INTEREST.

5. On a note dated May 30, 1879, for \$1666, are the following indorsements:—Apr. 9, 1880, \$314; Nov. 4, 1880, \$180; Aug. -25, 1881, \$575. What was due June 30, 1882, at 6%? At 8%?

6. What was the amount due Oct. 17, 1881, upon a note for \$1000, dated New York, Mar. 2, 1880, and on which the following payments were indorsed:—June 2, 1880, \$80; Dec. 15, 1880, \$20; May 2, 1881, \$32; June 2, 1881, \$60?

7. A note for \$3600, dated May 12, 1880, bore the following indorsements:—Jan. 2, 1881, \$255; Mar. 15, 1881, \$225; June 3, 1881, \$120; Aug. 6, 1881, \$300; Feb. 3, 1882, \$30. What was due June 2, 1882, at 6%? At 10%?

8. A note for \$4000, dated Mar. 9, 1874, was indorsed as follows:—Jan. 18, 1876, \$300; June 4, 1876, \$400; Dec. 9, 1876, \$1800; Sept. 1, 1879, \$2000. How much had to be paid Jan. 1, 1880, to take up the note, at 6%? At 7%?

9. A mortgage of \$6000 is dated May 9, 1877, on which there were the following payments:—July 15, 1878, \$500; Nov. 27, 1878, \$1000; June 1, 1879, \$100; May 9, 1880, \$275; Sept. 27, 1880, \$2000. What was due Nov. 9, 1880, the interest being at 6%? At 12%?

# MERCANTILE RULES.

**506.** The following methods are frequently used by merchants in finding the balance due on a note where partial payments have been made. They are similar to the methods in general use for finding the balance due on an open account (**592**).

# 507. When the note runs for one year only, or less.

**508.** RULE.—Compute the interest on the principal from the time it commenced to draw interest, and on each payment from the time it was made until the time of settlement, and deduct the amount of all the payments, including interest, from the amount of the principal and interest.

Notes.—1. This rule is used by some merchants when the note runs more than one year, although it is greatly to the disadvantage of the creditor, or holder of the note.

2. In solving examples by this rule, the different methods for finding time and interest, given in Art. 437, are used. The results of the following examples will be given for the first method (Compound Subtraction and 360 days to the year).

# EXAMPLES.

**509.** 1. According to the mercantile rule, find the balance due May 12, 1882, on a note for \$2400, dated July 12, 1881, on which the following payments have been made : Dec. 16, 1881, \$40; Jan. 2, 1882, \$100; Mar. 15, 1882, \$150.

OPERATION.		
Face of note, or principal, July 12, 1881,		\$2400.00
Interest on the same to May 12, 1882 (10 mo.)		120.00
Amount, May 12, 1882;		2520.00
First payment, Dec. 16, 1881,	\$40.00	
Interest on the same to May 12, 1882 (4 mo. 26 da.)	.97	
Second payment, Jan. 2, 1882,	190.00	
Interest on the same to May 12, 1882 (4 mo. 10 da.)	2.17	
Third payment, Mar. 15, 1882,	150.00	
Interest on the same to May 12, 1882 (1 mo. 27 da.)	1.42	294.56
Balance due May 12, 1882,		\$2225.44

2. On a note dated Jan. 13, 1882, for \$1234, are the following indorsements:—May 17, 1882, \$234; June 16, 1882, \$345; July 27, 1882, \$123; Sept. 19, 1882, \$135. What remained due Nov. 13, 1882, at 6%? At 7%?

3. A note for \$1567, dated Jan. 14, 1881, bore the following indorsements:—Mar. 11, 1881, \$50; May 13, 1881, \$245; June 19, 1881, \$374; Aug. 30, 1881, \$412; Sept. 28, 1881, \$316.40. What was due Jan. 1, 1882, at 6%? At 5%?

4. On a note dated Aug. 17, 1881, for \$3300, were the following indorsements:—Dec. 18, 1881, \$320; Feb. 5, 1882, \$425; Apr. 13, 1882, \$550; June 29, 1882, \$630; July 16, 1882, \$375; Aug. 1, 1882, \$500. What amount was due Aug. 17, 1882, at 6%? At 10%?

# 510. When the note runs for more than one year.

511. Since it is the custom of merchants and bankers to balance their accounts annually, the following method is used by them in computing the balance due on a note when it runs more than one year.

It is equivalent to finding the balance due yearly by the previous rule, and treating the balance as a new principal. The periodical settlements are made annually, semi-annually, or quarterly, depending upon the custom of the merchant or banker in balancing his accounts. Some merchants make the end of the business year, Jan. 1 or July 1, the periodical rest, or date of settlement for notes and accounts. **512.** RULE.—Find the amount of the principal for one year; also of each payment made during the year from the time the payment was made to the end of the year (1 yr. from the date of the note). From the amount of the principal, subtract the sum of the payments, including interest. With the remainder as a new principal, proceed thus for each entire year that follows, and for the interval between the end of the last year and the final date of settlement.

Note.—When payments are made yearly greater than the interest due, this rule is the same as the New Hampshire rule (675) for notes "with interest annually."

#### EXAMPLES.

**513.** *1.* By the above rule, find the balance due Jan. 19, 1885, at 6%, on a note for \$2400 dated Aug 1, 1881, on which the following payments have been made:—Apr. 21, 1882, \$200; Dec. 1, 1882, \$25; Aug. 1, 1883, \$100; July 7, 1884, \$400. (Time by Compound Subtraction.)

#### OPERATION.

Face of note, or principal, Aug. 1, 1881,					\$2400.00
Interest on the same for 1 year,					144.00
Amount, Aug. 1, 1882,					2544.00
First payment, Apr. 21, 1882,				\$200.00	
Interest on the same to Aug. 1, 1882 (3 mo.	10 d d	ı.)		3.33	203.33
Balance and new principal, Aug. 1, 1882,					2340.67
Interest on the same for 1 year,					140.44
Amount, Aug. 1, 1883,					2481.11
Second payment, Dec. 1, 1882,				\$25.00	
Interest on the same to Aug. 1, 1883 (8 mo.)	).			1.00	
Third payment, Aug. 1, 1883,				100.00	126.00
Balance and new principal, Aug. 1, 1883,					2355.11
Interest on the same for 1 year,					141.31
Amount, Aug. 1, 1884,					2496.42
Fourth payment, July 7, 1884,				\$400.00	
Interest on the same to Aug. 1, 1884, (24 da	i)			1.60	401.60
Balance and new principal, Aug. 1, 1884,					2094.82
Interest on the same to date of settlement, Jan	n. 19,	1885 (	5 m	o.18 da.)	58.65
Balance due Jan. 19, 1885,					\$2153.47

2-9. Solve Examples 2-9, Art. 505, according to the mercantile rule.

# RATIO AND PROPORTION.

**514.** Ratio is the relation of two numbers as expressed by the quotient of the first divided by the second. Thus the ratio of 6 to 3 is  $6 \div 3$ , or 2.

1. There is no ratio between quantities of different kinds; as 6 bu. and 3 ft. But a ratio exists between quantities of the same kind though of different denominations; as 6 ft. and 8 in. To express the ratio in such cases, the quantities must first be reduced to the same denomination. Thus, the ratio of 6 ft. to 8 in. is 72 in.+8 in, or 9.

2. The ratio between two numbers is denoted by placing a colon (the sign of division without the horizontal line) between them. Thus, the ratio of 6 to 3 is expressed 6:3.

**515.** A Simple Ratio is a ratio between two numbers; as 4:5.

**516.** A Compound Ratio is a ratio formed by the combination of two or more simple ratios.

Thus,  $\frac{4:5}{3:2}$  is a compound ratio, and is equivalent to  $4 \times 3:5 \times 2$ , or 12:10.

**517.** The numbers whose ratio is expressed are the terms of the ratio. The two terms of a ratio form a couplet, the first of which is the antecedent, and the second, the consequent.

518. Proportion is an equality of ratios.

The ratio of 6 yd. to 3 yd. is 2, and the ratio of \$24 to \$12 is 2; hence from the two equal ratios the following proportion can be formed—6 yd.: 3 yd. =\$24: \$12. This expression is read, "The ratio of 6 yd. to 3 yd. equals the ratio of \$24 to \$12." In place of the sign of equality (=), four dots (::) are generally used; thus, 6 yd.: 3 yd.:: \$24: \$12. The expression is also read, "6 yd. is to 3 yd. as \$24 is to \$12."

519. The first and fourth terms of a proportion are called the extremes; and the second and third, the means.

**520.** PRINCIPLES.—1. The product of the means is equal to the product of the extremes.

2. A missing mean may be found by dividing the product of the extremes by the given mean.

3. A missing extreme may be found by dividing the product of the means by the given extreme.

# SIMPLE PROPORTION.

**521.** Simple Proportion is an equality of two simple ratios; as 9 16.: 16 16.:: \$27: \$48.

If 24 hats cost \$27, what will 32 hats cost ? Ex.

ANALYSIS.—For convenience, make the fourth term the missing term, or the required answer. Since the third and fourth terms must be of the same denomination and the denomination of the answer will be dollars, take \$27 as the third term. From the nature of the example, the answer will be more than \$27, the third term, therefore make 32 hats the second term, and 24 hats the first term. The proportion will then be stated as follows: 24 hats: 32 hats:: \$27:x (Let x represent the unknown term). Multiplying 32 by 27, and dividing the product by 24, the fourth or missing term will be \$36.

522. RULE.—For convenience, take for the third term the number that may form a ratio with, or is of the same denomination as, the answer. If from the nature of the example, the answer is to be greater than the third term, make the greater of the two remaining terms (which must be of the same denomination) the second term; when not, make the smaller the second term. Then multiply the means (the second and third) together, and divide their product by the siven extreme (the first term).

Notes.-1. After the example is stated, any factor of the given extreme may be cancelled with an equal factor of either of the means.

2. The above rule is sometimes called the "Rule of Three."

#### EXAMPLES.

**523.** Find the missing term (represented by x) in each of the following proportions (See Principles, Art. 520).

- 1. 16: x :: 24: 18.
- 2. x: 27: 18: 54.
- 3. 32:27::x:135.
- 5. \$48: \$75:: \$32: x.
- 6. \$375:\$144::625 lb.: x.
- 7. \$1728: \$288 :: \$666; x.
- 4. 24 bu.: 32 bu.:: \$27:x. 8. 144 yd.: 175 yd.:: \$18:x.

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9. If 19 yd. of silk cost \$28.50, what will 37 yd. cost?

10. If 64 yd. of carpet 36 in. wide will cover a floor, how many yards 27 in. wide will be required to cover the same floor?

11. A cane 3 ft. 3 in. high casts a shadow  $5\frac{1}{2}$  ft. long; how long a shadow is cast by the steeple of a church which is 234 feet high?

12. If the freight of a long ton (336, 3) is 70 shillings, what is the freight of 16375 pounds?

13. The net assets of a bankrupt are \$27675, and the liabilities \$138375. How much must be paid to Mr. A, whom he owes \$4800?

14. A building is insured in several companies for \$28000. During a fire the building is damaged to the amount of \$13500. What is the loss of company A, whose risk is \$5000?

15. A invests in business \$8450, and B \$7200, and the gain or loss is divided according to the investments. What is each partner's share of gain, the total gain being \$3474.30?

16. The U. S. gold dollar (181, 183) contains 23.22 (25.8  $-\frac{1}{10}$ ) grains of pure gold, and the standard silver dollar 371.25 (412.5 $-\frac{1}{10}$ ) grains of pure silver. What is the relative value of pure gold to pure silver?

17. The assessed value of the property of a certain town is \$325000, and the total tax is \$10238. How much is the tax of Mr. A, whose property is valued at \$5700?

18. A company with a capital of \$250000 divides \$8750 among its stockholders. How much will be received by a stockholder who owns 36 100-dollar shares ?

19. If a long ton of coal is worth \$4.25, what is the value of a short ton ?

20. If a farm valued at \$4500 is taxed \$26.24, what should be the tax on property valued at \$23500?

21. A merchant gains \$625 by selling \$12000 worth of goods; what amount must he sell to gain \$8000?

22. How many feet of boards will be required for a fence 764 feet long, if 888 feet of boards are required for 288 feet ?

23. If one franc is worth \$0.193, and one pound sterling, \$4.8665, what is the value of the pound sterling expressed in francs?

24. If 2175 yards of cloth are made from 458 pounds of yarn, how many pounds of yarn would be required to make 1200 yards of cloth ?

25. If a railway train goes 412 miles in 9 hr. 30 min., how many hours would it require to go 900 miles?

26. The railway fare from A to B, a distance of 228 miles, is \$6.75. What should be the fare from A to C, a distance of 375 miles?

27. A certain quantity of grain will last 92 horses 48 days. How long will it last 64 horses?

28. A house and lot are worth \$9600, and the value of the lot is to the value of the house as 5 to 11. Find the value of the lot.

29. A merchant failing, owes \$11375, and has property worth \$4425. How much will he pay a creditor whom he owes \$2345?

30. The distance between two poles was measured as 48 yards, but the yard measure was  $\frac{1}{2}$  of an inch too short. What was the actual distance ?

31. From a field of wheat containing 375 acres, 4850 bushels are harvested. How many bushels would be harvested from a field containing 344 acres of similar wheat?

32. If the tax on property, valued at \$6500, is \$144, what should be the tax on property valued at \$3800?

33. If a Troy ounce of standard silver is worth 85 cents, what is the intrinsic value of the standard silver dollar (112)?

34. If the freight on 575 pounds is \$1.84, what should be the freight on 975 pounds ?

35. If a railway company charges \$13 for carrying one ton 480 miles, what should be the charge on one ton for 650 miles?

36. The through rate from A to C, a distance of 900 miles, is \$48 per car. What should be the portion of the A. & B. R.R. (425 miles), and the portion of the B. & C. R.R. (475 miles)?

37. If 48 men can do a certain piece of work in 60 days, in what time can 64 men do the same work  $^{9}$ 

38. If a Troy ounce (337) of silver is worth \$1.20, what is the value of an Avoirdupois ounce?

39. The ratio of the diameter of a circle to its circumference is 1:3.1416. What is the circumference of a circle whose diameter is 475 feet?

40. If 276 long tons of coal last a manufacturer 21 months, how long would 276 short tons last him ?

41. A bankrupt can pay 48 cents on a dollar. If his assets were \$1887 more, he could pay 65 cents. Find his debts and his assets.

# COMPOUND PROPORTION.

**524.** Compound Proportion is an equality of a compound ratio and a simple ratio, or of two compound ratios.

Thus,  $\begin{cases} 4 \text{ men : 6 men} \\ 8 \text{ days : 16 days} \end{cases}$  :: \$10: \$30, and  $\begin{cases} 2:3 \\ 4:5 \end{cases}$  ::  $\begin{cases} 8:5 \\ 4:12 \end{cases}$  are compound proportions.

Ex. If 12 men earn \$60 in 4 days, how much will 16 men earn in 2 days?

ANALYSIS.—Since the answer (fourth term) is required in dollars, make \$60 the third term of the proportion. If 12 men earn \$60, 16 men will earn more; therefore make 12 the first term and 16 the second term of one ratio. If they earn \$60 in 4 days, in 2 days they will earn less; therefore make 4 the first term and 2 the second term. The proportion will then be stated as in the operation. To find the fourth or unknown term, divide the continued product of the means by the continued product of the extremes.

The quotient will be the answer. Apply cancellation as in the operation, by placing the means at the right of a vertical line, and the extremes at the left.

**525.** RULE.—Take for the third term the number that may form a ratio with, or is of the same denomination as, the answer.

With each pair of similar terms remaining form a ratio as if the result depended upon these terms alone.

Multiply the means together, and divide their product by the product of the extremes. The quotient will be the required answer.

Note.—Compound Proportion is sometimes called the "Double Rule of Three."

#### EXAMPLES.

**526.** *1.* If it costs \$39 to carpet a floor 16 feet long and 12 feet wide, what will it cost to carpet a floor 26 feet long and 20 feet wide?

2. If a man can walk 360 miles in 12 days, walking 8 hours each day, how many hours a day must he walk at the same rate to complete 450 miles in 20 days?

3. If 4 men can cut 56 acres of grass in 8 days, how many acres can 6 men cut in 12 days?

4. If it costs \$1728 to pave a street 800 feet long and 50 feet wide, what will it cost to pave a street 1200 feet long and 90 feet wide?

5. How many hours a day must 42 men work, to do in 45 days what 27 men can do in 28 days of 10 hours each ?

6. If the gas for 5 burners, 5 hours every evening for 10 days, costs \$2.55, how many burners may be lighted 4 hours every evening for 15 days at a cost of \$76.50 ?

7. If 22 men can dig a ditch 4200 feet long, 5 feet wide, and 3 feet deep, in 35 days of 9 hours each, in how many days of 11 hours each will 252 men dig a ditch 2100 feet long, 3 feet wide, and 2 feet deep?

8. If 3 men working 11 hours a day can reap a field of 20 acres in 11 days, in how many days can 9 men working 12 hours a day reap a field 360 yards long and 320 yards wide?

9. A person can read a book containing 220 pages, each of which contains 28 lines, and each line an average of 12 words, in  $5\frac{1}{2}$  hours. How long will it take him to read a book containing 400 pages, each of which contains 36 lines, and each line an average of 14 words?

10. Two gangs of 6 and 9 men are set to reap two fields of 35 and 45 acres respectively. The first gang works 7 hours a day, and the latter 8 hours. If the first gang complete their work in 12 days, in how many days will the second gang complete theirs?

11. A transportation company charges \$20 for carrying 15000 pounds 400 miles. How much ought they to charge for carrying 60000 pounds 320 miles?

12. If 6 men build a wall 20 feet long, 6 feet high, and 4 feet thick, in 16 days, in what time will 24 men build a wall 200 feet long, 8 feet high, and 6 feet thick ?

13. If the interest of \$100 for 1 year (360 days), at 6%, is \$6, what is the interest of \$1200 for 248 days at 8%?

14. If the freight of 18 *hhd.* of sugar, each weighing 1200 *lb.*, for 200 miles, is \$320, what must be paid for the freight of 50 *hhd.* each weighing 960 *lb.*, for 420 miles ?

15. If 18 men, working 10 hours a day, can hoe 60 acres in 20 days, how long will it take 50 boys, working 6 hours a day, to hoe 96 acres, 6 men being equal to 10 boys?

16. If a block of marble  $2 \times 1 \times 3$  ft. weight 1020 pounds, what is the weight of a block  $3 \times 4 \times 8$  ft.?

# INSURANCE.

**527.** Insurance is a contract by which one party (The Insurer or Underwriter) engages for a stipulated consideration (The Premium) to make up a loss which another may sustain.

Insurance is effected on property against loss or damage by fire and water, and on lives of persons. (For Life Insurance, see Art. 651.)

Insurance is also effected against accidents to persons, the breakage of plate-glass, the loss of live stock, and the dishonesty of employees.

**528.** An **Insurance Company** is a company or corporation which insures against loss or damage.

**529.** Insurance companies may be classified according to principles of organization as follows :---1, Stock; 2, Mutual; 3, Mixed, or Stock and Mutual.

**530.** A Stock Insurance Company is one in which the capital is owned by individuals, called stockholders. They alone share the profits and are liable for the losses.

The business of a stock company and also of a mixed company, is managed by directors chosen by the stockholders. No policyholder, unless a stockholder, has any voice in auy way in the election of the officers, or in the management of its business.

531. A Mutual Insurance Company is one in which there are no stockholders, and the profits and losses are shared among those who are insured (the policyholders).

Non-participating policies, the holders of which do not share in the profits or losses, are issued by certain mutual and mixed companies.

532. A Mixed Insurance Company is one which is conducted upon a combination of the stock and mutual plan.

Usually in a mixed company, all profits above a limited dividend to the stockholders are divided among the participating policyholders.

533. The Policy is the contract between the Insurance Company (the Insurer or Underwriter) and the Insured. It contains a description of the property insured, the amount of the insurance, and the conditions under which the policy is issued.

#### 534. The Premium is the amount paid for the insurance.

1. Premium rates are expressed by giving the cost in cents of \$100 insurance. The rate is sometimes expressed as a certain per cent. of the amount of the risk. Thus, a rate of 75 cents per \$100 is equivalent to  $\frac{3}{4}\%$ .

2. The premium rates depend upon the nature of the risk, and the length of time for which the policy is issued. The rate for 3 years in many Fire Insurance Companies is twice the rate for one year.

535. Short Rates are rates for a term less than a year.

If an insurance policy is terminated at the request of the policyholder, the company retains the customary "short rates" for the time the policy has been in force; if terminated at the option of the company, a ratable proportion of the premium is refunded for the unexpired term of the policy.

536. An Insurance Agent is a person who represents an insurance company or several companies, and acts for them in soliciting business, collecting premiums, adjusting losses, etc.

537. An Insurance Broker is a person who effects insurance, for negotiating which he receives a commission or brokerage from the company taking the risk.

Brokers are regarded as agents of the insured, and not of the insurance company.

538. The Surplus of an insurance company is the excess of the assets over the liabilities (including capital and unearned premium).

#### FIRE INSURANCE.

539. Fire Insurance refers to insurance against loss or damage by fire.

540. Adjustment of Losses.—In an ordinary fire insurance policy, a person who insures will be paid the extent of his loss up to the amount of his insurance; but in policies containing the "average clause," the payment is such proportion of the loss as the amount of the insurance bears to the total value of the property. 1. The following is the usual form of the "average clause" above referred to: "It is a condition of this insurance, that if the whole value of the above described property, contained in any or all of the above mentioned buildings and premises, shall exceed the whole amount of insurance thereon, then, in case of loss or damage by fire, this policy shall contribute to the payment of said loss or damage in the proportion only that the whole amount of insurance on said property shall bear to the whole value of said property, in all of said buildings, at the time said loss or damage may occur."

2. Under a policy containing the "average clause," a person who insures \$5000 on property worth \$10000, would receive only \$2500 in case of an actual loss of \$5000; \$1500 in a loss of \$3000.

3. Insurance companies usually reserve the privilege of replacing or repairing the damaged premises.

# MARINE INSURANCE.

541. Marine Insurance refers to insurance of vessels and their cargoes against the dangers of navigation.

1. Inland and Transit Insurance refer to insurance of merchandise while being transported from place to place either by rail or water routes, or both.

2. Policies on cargoes are issued for a certain voyage, or from port to port, and on vessels for a specified time or for a certain voyage.

3. The particular average clause is the clause which exempts the insurance company from the payment of any partial loss or particular average, unless it exceeds a certain per cent. of the value of the property. The particular average clause is sometimes applied to the value of each parcel or series of parcels, according to invoice numbers.

4. Insurance Certificates, showing that certain property has been insured, and stating the amount of the insurance and the name of the party abroad who is authorized to make the settlement, are issued by marine companies. They are negotiable, and are usually sent to the consignee of the merchandise to make the loss payable at the port of destination, and to otherwise facilitate the adjustment of the insurance in case of loss.

542. Adjustment of Losses.—In marine insurance, in case of loss or damage, the insurance company contributes such proportion of the loss as the amount of the insurance bears to the total value of the property.

1. The adjustment of marine losses is on the same principle as the adjustment of fire policies containing the "average clause" (540, 1).

2. In the adjustment of marine losses, the pound sterling is usually estimated at \$4.95.

543. An Open Policy is one upon which additional insurances may be entered at different times. It covers merchandise which may be shipped on "Vessel or Vessels" from "Ports and Places" to "Ports and Places," for amounts "as endorsed" and at rates "as agreed."

1. The date of the shipment, name of vessel, ports of shipment and destination, the amount of the insurance, rate, premium, and a description of the property are entered on the policy or in a pass-book, which is regarded as part of the policy. (See Ex. 27, Art. **544**.)

2. Open policies with pass-books attached and insuring merchandise against loss or damage by fire, are issued by fire insurance companies.

3. Open policies, which cover all risks whether accepted and endorsed on the policy or not, are issued to merchants who are receiving merchandise from foreign countries, and who do not always have a definite knowledge of the time of shipment. Such policies usually contain the following clause: "The company are to be entitled to premiums at their usual rates on all shipments reported or not. It is warranted by the assured to report every shipment on the day of receiving advice thereof, or as soon thereafter as practicable, when the rate of premium shall be fixed by the President of the Company."

The above policies cover the invoice cost and 10% additional until the amount of the risk is endorsed on the policy or pass-book.

4. Open policies are sometimes issued which cover only such risks as may be accepted and endorsed on the policy by the company.

#### EXAMPLES.

**544.** 1. A building was insured for \$2500 in one company at  $1\frac{4}{5}$ , and for \$5000 in another company at 125 cents. What was the total premium paid ?

2. A cargo of goods was insured for \$9000 at  $\frac{3}{4}$ %. What was the cost of the insurance, \$1.25 being charged for the policy ?

.3. What is the total premium of the following insurances:  $$5000 \text{ at } 1\frac{1}{2}\%$ ,  $$7000 \text{ at } 45\phi$ , \$2000 at 5%,  $$3500 \text{ at } 45\phi$ ,  $$2000 \text{ at } 70\phi$ ,  $$4000 \text{ at } 1\frac{1}{2}\%$ ,  $$2000 \text{ at } 60\phi$ ,  $$4500 \text{ at } 25\phi$ , and  $$3600 \text{ at } 125\phi$ ?

4. \$20 was paid for an insurance of \$2500; what was the premium rate?

5. \$25.20 was paid for an insurance at the rate of 70¢ per \$100. What was the amount of the risk ?

6. A factory was insured for \$7500 for 1 year at  $2\frac{1}{2}$ %, stock for \$2500 at  $2\frac{1}{2}$ %, and raw material for \$2500 at  $1\frac{1}{4}$ %. What was the total premium ?

7. What is the cost of insuring a house for \$5000 at the rate of  $45\phi$  per \$100?

8. A cargo of merchandise was insured for \$6500 at  $\frac{1}{8}$ %, including the risk of fire while on wharf awaiting shipment. What was the premium ?

9. A building was insured Jan. 1, 1880, for \$2000, for 7 years, at 5%; what was the value of the unearned premium, Jan. 1, 1882?

10. A shipment of goods was insured in the Pacific Mutual Insurance Co. for 9600 at  $75 \notin 1ess 20\%$  in lieu of scrip and interest. What was the net cost of the insurance?

11. A house was insured for \$5000 for 4 years at  $60\phi$  per annum. The house was destroyed by fire. What was the actual loss of the company, making no allowance for interest?

12. Find the cost of insuring a house for 3 years for \$4000 at  $60\phi$ , and the furniture for \$1200 at  $80\phi$ , less 15% on both premiums.

13. A cargo of hides having increased in value since the insurance was effected, the anticipated profits were insured for \$3000 at  $1\frac{3}{7}$  less 20%. What was the premium ?

14. A factory (worth \$3000) and its contents are insured for \$10000 as follows: \$2000 on building, \$3000 on machinery (worth \$5000), and \$5000 on stock (worth \$8000). The building is damaged by fire to the amount of \$1000, the machinery \$4000, and stock is a total loss. How much is the claim against the insurance company?

15. A cargo of goods valued at \$20000 was insured for \$12000. If the goods were damaged to the amount of \$15000, how much of the loss would be paid by the insurance company? (542.)

16. A building is insured in several companies for \$60000, and is damaged by fire to the extent of \$24000. What per cent. of its risk is paid by each company?

17. A stock of goods was insured, May 1, for 1 year, for \$6000, at  $90\phi$ . The policy was cancelled Nov. 1, at the request of the insured. How much was the return premium, the short rate for 6 months being  $63\phi$ ? How much would have been returned by the company, if the policy had been cancelled at its request?

18. A quantity of merchandise valued at \$6000 is insured for \$5000. It is damaged by fire to the amount of \$1728. How much of the loss is paid by the insurance company, the policy containing the "average clause"? (540.)

19. What was paid for insuring a cargo of merchandise for \$8750 at  $\frac{1}{2}$  less 20%?

20. A factory and its contents are insured for \$5000 in company M, \$5000 in N, \$5000 in O, \$4000 in P, and \$2500 in each of the following companies: Q, R, S, T, U, V, W, X, Y, and Z. What was the total premium, the rate being 2% less 10%?

21. The above insurance covered the following property: \$4000 on building marked A on plan, \$4000 on B, \$5000 on C, \$500 on D, \$500 on E, \$3500 on stock and materials in building marked A on plan, \$8000 on machinery, etc., in A, \$11500 on stock and materials in B and C, \$4000 on machinery, etc., in B and C, \$2500 on horses in D, \$500 on harness, hay, feed, etc., in D. Suppose building A and its contents were totally destroyed by fire, what would be the loss of company M? Of P? Of T?

NOTE.—The above insurance was divided pro rata among the several companies, each policy designating the exact amount on each building, etc.

22. In the above example, what is the amount of the risk of company M on the building marked A on plan? On C?

23. The net invoice value of a quantity of goods is \$6325, and, the insured value \$6500. The insured value is what per cent. greater than the invoice value?

24. A quantity of merchandise valued at \$9035, is insured for \$9000. What is the insurance on part of the same, the estimated value being \$2638?

25. If 500 packages of merchandise are insured for \$2627.78, what is the insurance on 60 packages?

26. The estimated sound value of a quantity of merchandise, damaged at sea, was \$328.55, and the proceeds when sold at auction, \$299.35. How much of the loss was shared by the Insurance Co., the insurance having been \$315.33 ?

27. Make the extensions of the following "open policy" and find the total amount.

Dat	е.	Name of vessel.	From.	To.	On.		Panount Rate.		Amount of pre- mium.		
188: Sept.	<sup>1.</sup> 2	Othello.	N. Y. via Hull.	Stockholm.	50	Ba.	Mdse.	5100	11	**	**
"	7	Algeria.	New York.	Liverpool.	68	"	"	6675	-8	**	**
**	16	Germanic.	New York.	Liverpool.	92	a	<b>6</b> 6	13500	1.	**	**
66	17	Rialto.	N. Y. via Hull.	Christiania.	6	66	"	600	1	*	
	23	Otranto.	N.Y. via Hull.	Orebro,	30	66	"	2700	11	**	**
										\$***	**
								Less	20%	**	**

\*\*\* \*\*

# EXCHANGE.

545. Exchange is the system by which merchants in distant places discharge their debts to each other without the transmission of money.

Suppose, for example, A of New York owes B of Chicago \$1000 for grain, and C of Chicago owes D of New York \$1000 for dry goods. The two debts may be discharged by means of one draft or bill of exchange without the transmission of money. Thus, B of Chicago draws on A of New York for \$1000, and sells the draft to C of Chicago, who remits it to D of New York. D of New York presents the draft to A of New York for acceptance or payment, and thus both debts are cancelled. There is in effect a setting-off or exchange of one debt for the other.

The business of exchange is usually conducted through the medium of banks and bankers, who buy commercial bills and transmit them for credit to the places on which they are drawn. They also sell their own drafts on their correspondents in any amounts demanded.

The greater part of the exchange in the United States is effected through the banks of New York, Boston, Philadelphia, Chicago, St. Louis, Baltimore, and San Francisco. The financial centres of Europe are London, Paris, Antwerp, Geneva, Amsterdam, Hamburg, Frankfort, Bremen, Berlin, and Vienna.

546. A Bill of Exchange, or Draft, is an order or request addressed by one person (the Drawer) to another (the Drawee), directing the payment of a specified sum of money to a third person (the Payee) or to his order. It is issued at one place and payable at another. (See Art. 495, 5-6.)

For brevity, bills of exchange are frequently called "exchange."

According to the laws of most States, drafts drawn in one State and payable in another, are termed *foreign* bills of exchange. For the purposes of this book, the term "domestic exchange" will be applied to bills drawn and payable in the United States.

547. Bills of exchange are of two kinds, Inland or Domestic, and Foreign.

548. A Domestic or Inland Bill of Exchange is one which is payable in the same country in which it is drawn.

549. A Foreign Bill of Exchange is one which is payable in a different country from the one in which it is drawn; as a draft drawn in the United States and payable in England.

550. When drafts sell for more than their face value, exchange is above par or at a premium ; when for less than their face, below par or at a discount.

When Chicago owes New York the same amount that New York owes Chicago, exchange will be at par; that is, drafts will sell at their face value. When Chicago owes New York more than New York owes Chicago, drafts on New York will sell at a premium; there will be more buyers of exchange than sellers, and drafts will sell for more than their face value. When Chicago owes New York less than New York owes Chicago, the demand in Chicago for drafts on New York will be less than the supply, and drafts will sell for less than their face value, or at a discount.

# DOMESTIC EXCHANGE.

**551.** Domestic or Inland Exchange relates to drafts drawn at one place on another in the same country.

552. The domestic exchanges on New York at the places named were quoted as follows, May 7, 1881 : Savannah,  $\frac{1}{6} @ \frac{3}{8}$  premium ; Charleston,  $\frac{1}{6} @ \frac{1}{4}$  premium ; New Orleans, \$1.50 @ \$2.50 premium; St. Louis, 25 cents premium ; Chicago, 50 @ 75 cents premium ; and Boston, 25 cents discount.

1. At Savannah and Charleston the rates per cent. of the premium or discount are given. Thus, when exchange is quoted at  $\frac{1}{4}$  premium, a draft of \$100 may be purchased for \$100 $\frac{1}{4}$  (\$100.25).

2. At New Orleans, St. Louis, Chicago, and Boston, the premium or discount per \$1000 is given. Thus, a draft of \$1000 at \$2.50 premium may be purchased for \$1002.50. \$2.50 per \$1000 premium is equivalent to  $\frac{1}{4}$ % premium.

3. The selling rates are about  $\frac{1}{8}$ % (\$1.25) higher than the buying rates, and bankers' exchange is usually higher than commercial.

4. The rate of domestic exchange is limited by the cost of shipping gold or currency by express, and the premium or discount will not exceed this cost. Thus, if a merchant in Chicago is charged a premium of \$10 for a draft of \$10000, and he can send the currency by express for \$7.50, it will be to his advantage to remit by the latter method.

The following appeared in a New York financial paper, May 8, 1881, the date of the above quotations: — " The domestic exchanges at the West are sufficiently high to permit of a movement of funds Eastward, but at the East,

New York funds are still at a discount and some shipments of gold and currency continue to be made to the Eastern cities."

5. The preceding quotations refer to sight exchange. Time drafts are discounted in the same manner as promissory notes. In certain cases bankers in discounting notes and drafts payable in distant places, charge interest for the time required for the return of the money when the note or draft is paid; and in the case of drafts drawn a certain number of days after sight, bankers sometimes charge interest for the time required for the acceptance of the drafts. Thus, if a draft was drawn in New York on St. Louis and pavable 60 days after sight, it would require, in the ordinary course of the mails, 3 days for the acceptance of the draft. The draft would be paid in 63 days (including the days of grace), and 3 days would elapse before the money would be returned to New York. The banker would be justified in charging interest for 69 days, the interval between the day he advanced the money in New York, and the day it was returned to him again. If the draft was drawn on San Francisco, fully 19 days (8 days for the acceptance, 3 days of grace, and 8 days for the return of the money) would be added to the time of the draft. Between New York and San Francisco and other distant places, money is frequently transferred by telegraph. (See Art. 499, 3.)

#### EXAMPLES.

553. 1. What is the value in Savannah of a draft on New York for \$8750 at  $\frac{3}{2}\%$  premium?

2. Find the cost in New Orleans of a draft on New York for \$8375 at \$2.50 premium.

Find the value of the following drafts :

	Face.	Exchange.		Face.	E	Exchange.
3.	\$5000,	18% premium.	8.	\$4287.75,	$15^{\phi}$	discount.
4.	\$4375,	3% discount.	9.	\$3416.33,	$25^{\phi}$	premium.
5.	\$8417,	18% premium.	10.	\$2825.49,	\$1.25	discount.
6.	\$9873,	1% premium.	11.	\$9873.62,	\$2.50	premium.
7.	\$5284,	1% discount.	12.	\$8412.75,	75%	discount.

13. A of Chicago buys cattle for B of New York to the amount of \$9858.07. How large a draft should be drawn on B, so that when sold at a discount of  $50^{\text{o}}$  ( $\frac{1}{20}$ %), the proceeds would be sufficient to pay the bill?

NOTE.—To find the face of a draft, instead of dividing the value of the draft by the rate of exchange (in the above example,  $.99\frac{1}{20}$  or .9995), business men and bankers calculate the premium or discount on the value of the draft, and subtract or add it to the value as the case requires. Thus, in the above example, the discount would be  $\frac{1}{2}$  of  $\frac{1}{10}$ % of \$9858.07, or \$4.93, which added to the given proceeds would produce the face \$9863. This method produces too small a result in all cases, the error being equivalent to the percentage of the premium or discount. In this example the error is less than  $\frac{1}{4}$  cent.

For ordinary examples in business, the foregoing method is sufficiently accurate. At  $\frac{1}{2}$ %, or \$5.00 (a very high rate for domestic exchange) on a draft whose value is \$10000, the error would be only 25 cents. If greater accuracy is required, the necessary correction can be made by adding the percentage of the premium or discount. Thus, if the value of the draft is \$10000, and exchange is  $\frac{1}{2}$ % discount, the face would be \$10000 + \$50 ( $\frac{1}{2}$ % of \$10000) + \$0.25 ( $\frac{1}{2}$ % of \$50) = \$10050.25. If at  $\frac{1}{2}$ % premium, the face would be \$10000 - \$50 + \$0.25 = \$9950.25.

By	the above	method, find the	face of the fo	ollowing drafts:
	Value.	Exchange.	Value.	Exchange.
14.	\$1876.16,	1% premium.	19. \$7375,	25¢ premium.
15.	\$2437.75,	1% discount.	20. \$9218,	50¢ discount.
16.	\$3342.38,	$\frac{1}{8}\%$ discount.	21. \$6438,	\$1.00 premium.
17.	\$2238.42,	$\frac{1}{2}\%$ premium.	22. \$9243,	\$1.25 premium.
18.	\$8175.50,	3% premium.	23. \$5280.	75¢ discount.
01	A .C M.	- Orlean him	: J-14. J 4.	D . C . T. T. I

24. A of New Orleans being indebted to B of New York \$9316.75, forwards to him a check on a New Orleans bank for that amount, to cash which B is obliged to allow a discount of  $\frac{1}{2}$ . How much does A still owe B, and for what amount should the check have been drawn to net B the amount due ?

25. What is the value of a draft on New York for \$3000, payable in 60 days (63 days) after date (494, 7), exchange being  $\frac{1}{3}\%$  premium, and interest 6%?

NOTE.—From the face of the draft, subtract the interest, and to the result add the exchange.

26. Find the proceeds of a draft drawn at Chicago on New York for \$12000, and payable 90 days after sight, exchange  $50\phi$  discount, interest 5%, and allowing 3 days additional for the acceptance of the draft.

27. A banker in New York discounts a draft for \$8000, payable in San Francisco 60 days after sight; what would be the proceeds, exchange being  $\frac{1}{2}\%$  discount, interest 6%, and allowing 8 days for the acceptance and 8 days for the return of the money?

28. A merchant paid \$6920.64 in Charleston for a sight draft of \$6912; what was the rate of exchange?

29. A commission merchant sold 13475 pounds of leather at 26<sup>3</sup>/<sub>4</sub> cents a pound. If his commission is 5%, and exchange  $\frac{1}{8}\%$  premium, how large a draft can he buy to remit to the consignor?

30. How large a 60-days' draft must I draw, so that when sold it will produce \$10000, exchange  $\frac{1}{6}$  discount, interest 6%?

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#### Art. 554.]

# FOREIGN EXCHANGE.

**554.** Foreign Exchange relates to drafts or bills of exchange drawn in one country and payable in another.

555. To secure safety and speed in the transmission of foreign bills of exchange, they are drawn in sets of two or three of the same tenor and date. The separate bills are sent by different steamers, and when any one of them is paid, the others become void. Some merchants send only the first and second, and preserve the third.

#### SET OF EXCHANGE.

## (1.)

EXCHANGE FOR £1000. NEW YORK, May 16, 1889. Sixty days after sight of this FIRST of Exchange (Second and Third unpaid), pay to the order of A. T. STEWART & Co., One Thousand Pounds Sterling, value received, and charge the same to account of

No. 1738. To BROWN, SHIPLEY & Co., London, England.

(2.)

EXCHANGE FOR £1000. NEW YORK, May 16, 1889. Sixty days after sight of this SECOND of Exchange (First and Third unpaid), pay to the order of A. T. STEWART & Co., One Thousand Pounds Sterling, value received, and charge the same to account of

BROWN BROTHERS & Co.

BROWN BROTHERS & Co.

To BROWN, SHIPLEY & Co., London, England.

No. 1738.

#### $(\mathbf{3.})$

EXCHANGE FOR £1000. NEW YORK, May 16, 1889.

Sixty days after sight of this THIRD of Exchange (First and Second unpaid), pay to the order of A. T. STEWART & Co., One Thousand Pounds Sterling, value received, and charge the same to account of

No. 1738. To Brown, Shipley & Co., London, England. BROWN BROTHERS & CO.

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Foreign bills of exchange are usually drawn in the moneys of account of the countries in which they are payable. Thus, drafts on England are usually drawn in pounds, shillings, and pence; on France, Belgium, and Switzerland, in francs; on Germany, in marks; on the Netherlands (Holland), in guilders.

Foreign bills of exchange are usually drawn at sight (3 days) or at sixty (63 days) days' sight. Sight drafts are frequently called "short" exchange, and 60 day drafts, "long" exchange. "Long" exchange is sold at a rate below that for "short" exchange, sufficient to equalize the difference in interest between the dates of maturity of the two classes of bills.

556. A Letter of Credit is an instrument issued by a banker and addressed to bankers generally, by which the holder may draw funds at different places and in amounts to suit his convenience, the total amount drawn not exceeding the limit of the letter of credit.

A *bill of exchange* is payable at a certain place, at a certain fixed time, and for a certain amount, while a *letter of credit* is payable at different places, at different times, and in different amounts.

A person who intends to travel in foreign countries, may procure a letter of credit by depositing either cash or securities with a foreign exchange banker for the amount of the letter. When the American banker is notified of the payment of the traveler's drafts in London, he debits the account of the holder of the letter of credit with the amount drawn and the charges, at the current rate of exchange. A small rate of interest is sometimes allowed on the account, and a settlement is made on the return of the traveler.

557. The Intrinsic Par of Exchange is the value of the monetary unit of one country expressed in that of another, and is based on the comparative fineness and weight of the coins, as determined by assay. (See Art. 566.)

558. The Commercial Par of Exchange is the market value in one country of the *coins* of another.

559. The Commercial Rate of Exchange is the market or buying and selling value in one country of the *drafts* on another.

1. In giving quotations of foreign exchange, no reference is made to the par value, the quotations being given by means of equivalents.

2. Premium or discount for exchange cannot long exceed the transportation charges and insurance of shipping coin; for, if a merchant can ship gold cheaper than he can buy a bill of exchange, he will choose the former method of paying his indebtedness. When sight exchange is 4.84, gold can be imported at a small profit; and when sight exchange is  $4.89\frac{1}{4}$ , gold can be exported at a profit. 3. When exchange is above par, we are exporters of gold; when below par, we are importers of gold.

**560.** Exchange on England (Sterling exchange) is quoted by giving the value of  $\pounds$ 1 in dollars and cents.

Thus, when exchange is 4.84, a draft of £1 will cost \$4.84; of £100, \$484. The intrinsic par value of £1 is \$4.8665 (566).

561. Exchange on France, Belgium, and Switzerland is quoted by giving the value of \$1 in francs and centimes (hundredths of a franc).

Thus, when exchange is  $5.27\frac{1}{2}$ , \$1 will buy a bill of 5 francs and  $27\frac{1}{2}$  centimes; a draft of 1000 francs will cost \$189.57 (1000 +  $5.27\frac{1}{2}$ ). The intrinsic par value of 1 franc is  $19\frac{3}{10}$  cents (**566**); of the equivalent exchange,  $5.18\frac{1}{5}$  (1.00 + .193).

In French, Belgian, and Swiss exchange, the higher the apparent rate, the less the value of the draft. Thus, when exchange is 5.13, a draft of 1000 frances is worth \$194.93, and each franc is worth  $19_{100}^{49}$  cents. When exchange is 5.26<sup>3</sup>/<sub>8</sub>, the same draft would be worth \$189.98, and each franc 19 cents.

562. Exchange on Amsterdam (Netherlands) is quoted by giving the value of one guilder (gülden) or florin in U. S. cents.

The intrinsic par value of 1 guilder is  $40\frac{2}{10}$  cents (566).

**563.** Exchange on Germany is quoted by giving the value of 4 reichsmarks in cents.

The intrinsic par value of 1 mark is  $23_{10}^{s}$  cents (566); of 4 marks  $95_{10}^{2}$  cents.

564. Documentary Exchange is a bill drawn by a shipper upon his consignee against merchandise shipped, accompanied by the letter of hypothecation, the bill of lading "to order," and the insurance certificates covering the property against which the bill is drawn.

**565.** Exchange on London in the countries named, and at London on the same countries, is quoted as follows:

United States, by giving the value of  $\pounds 1$  in dollars and cents. France and Belgium, by giving the value of  $\pounds 1$  in francs and centimes. Germany, by giving the value of  $\pounds 1$  in marks and pfenniges. Austria, by giving the value of  $\pounds 1$  in florins and kreutzers. Netherlands, by giving the value of  $\pounds 1$  in guilders and cents. India, by giving the value of 1 rupee in shillings and pence.

566. FOREIGN	MONEYS OF A	ACCOUNT.
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Country.	Standard.	Monetary Unit.	Value in U S. Gold.
Argentine Republic.	Gold and silver.	Peso of 100 centavos	.96,5
Austria	Silver	Florin of 100 kreutzers.	.35,9
Belgium	Gold and silver.	*Franc of 100 centimes	.19,3
Bolivia	Silver	<sup>b</sup> Boliviano, 100 centavos.	.72,7
Brazil	Gold	Milreis of 1000 reis	.54,6
British America	Gold	Dollar of 100 cents	\$1.00
Chili	Gold and silver.	Peso of 100 centavos	.91,2
Cuba	Gold and silver.	Peso of 100 centavos	.93,2
Denmark	Gold	Crown of 100 öre	.26,8
Ecuador	Silver	<sup>b</sup> Sucre of 100 centavos	.72,7
Egypt	Gold	Pound of 100 piasters	4.94,3
France	Gold and silver.	•Franc of 100 centimes	.19,3
German Empire	Gold	Mark of 100 pfennige	.23,8
Great Britain	Gold	Pound of 20 shillings	$4.86, 6\frac{1}{2}$
Greece	Gold and silver.	*Drachma of 100 lepta	.19,3
Hayti	Gold and silver.	<sup>d</sup> Gourde of 100 centavos.	.96,5
India	Silver	Rupee of 16 annase	.34,6
Italy	Gold and silver.	*Lira of 100 centesimi	.19,3
Japan	Gold and silver.	Yen of 100 sen { Gold	.99,7 78.4
Liberia	Gold	Dollar of 100 cents	1.00
Mexico	Silver.	Dollar of 100 centavos.	79
Netherlands	Gold and silver.	Florin of 100 cents	40.2
Norway	Gold	Crown of 100 öre	.26.8
Peru	Silver	<sup>b</sup> Sol of 100 centavos	.72.7
Portugal	Gold	Milreis of 100 reis	1.08
Russia	Silver	Rouble of 100 copecks .	.58.2
Spain	Gold and silver.	*Peseta of 100 centimes.	.19.3
Sweden	Gold	Crown of 100 öre	.26.8
Switzerland	Gold and silver.	•Franc of 100 centimes	.19.3
Tripoli	Silver	Mahbub of 20 piasters .	.65,6
Turkey	Gold	Piaster of 40 paras	.04,4
U.S. of Colombia	Silver	<sup>b</sup> Peso of 100 centavos	.72.7
Venezuela	Gold and silver.	Bolivar of 100 centavos.	.19,3

The above rates, proclaimed by the Secretary of the Treasury, Jan. 1, 1887, are used in estimating, for Custom House purposes, the values of all foreign merchandise made out in any of said currencies.

(\*) The *franc* of France, Belgium, and Switzerland, the *peseta* of Spain, the *drachma* of Greece, the *lira* of Italy, and the *bolivar* of Venezuela have the same value.

(\*) The sucre of Ecuador, the peso of United States of Colombia, the boliviano of Bolivia, and the sol of Peru have the same value.

(°) The crowns of Norway, Sweden, and Denmark have the same value.

(d) The gourde of Hayti and the peso of the Argentine Republic have the same value.

(°) The anna contains 12 pies,

#### EXAMPLES.

**567.** 1. Find the cost of a bill of exchange on London for £225 at 4.81<sup>§</sup>. (560)

ANALYSIS .--- If £1 costs \$4.813, £225 will cost 225 times \$4.813.

2. What is the value of a draft for £324 16s. at  $4.87\frac{1}{2}$ ?

ANALYSIS.—Write one-half of the greatest even number of shillings as tenths of a pound, and if there be an odd shilling write 5 hundredths.  $\pounds 324 \ 16s. = \pounds 324.8$ . (See Art. **342**, Ex. 12, Note.) The value of  $\pounds 324 \ 16s.$ at  $4.87\frac{1}{9}$  is found by multiplying  $\$4.87\frac{1}{9}$  by 324.8.

3. Find the value of a draft on London for £379 12s. 7d., at 4.863.

OPERATION.

379.6

4.86불	
	ANALYSIS.—If each penny be regarded as 2 cents, the
949	result will be sufficiently accurate. For 11d. the maximum
475	number of pence in any example, and exchange at 4.91, the
22776	error would be only $\frac{1}{2}$ cent. $$4.86\frac{3}{8} \times 379.6 = $1846.28$ .
30368	\$1846.28 + \$0.14 = \$1846.42. To save one addition, add
5184	the 14 cents to the partial products as in the operation.
14	

1846.420

Fi	nd the value of	Fi	nd the value of
4.	£500 at 4.81 <sup>1</sup> / <sub>2</sub> .	8.	£512 13s. at 4.84§.
5.	£775 at 4.85 <sup>1</sup> / <sub>4</sub> .	9.	$\pounds 834 \ 6s. \ 6d. \ at \ 4.88\frac{5}{8}.$
6.	£837 at 4.833.	10.	£675 11s. 8d. at 4.871.
7.	£84 8s. at 4.85.	11.	£225 7s. 5d. at $4.82\frac{3}{4}$ .

12. Find the cost of a bill of exchange on Liverpool, for £875 12s. 6d. at the par value. (560)

13. What are the proceeds of a draft of £959 5s. 4d., sold through a broker, at  $4.79\frac{1}{2}$ , brokerage  $\frac{1}{2}\%$ ?

14. An exporter sold a draft for £540 3s. on Manchester, payable in London, at 4.84, brokerage  $\frac{1}{2}$ . What were the proceeds ?

15. Find the proceeds of a draft on Newcastle-on-Tyne, at 60 days' sight for £1764 15s., payable in London, at 4.82, brokerage on exchange  $\frac{1}{5}$ .

16. An importer purchased a bill of exchange on London, at 3 days' sight, for £488 16s. 6d., at  $4.85\frac{1}{2}$ . What was the cost ?

17. How much exchange on London at 4.81<sup>3</sup>/<sub>4</sub> will \$821.99 buy ?

ANALYSIS.— $$4.81\frac{3}{4}$  will buy exchange for £1; hence, \$821.99 will buy as many pounds as \$4.81 $\frac{3}{4}$  are contained in \$821.99, or £170.625. £170.625 = £170 12s. 6d. (See Art. **289**, and Art. **342**, Ex. 19, Note.)

18. What will be the face of a 3 days' bill of exchange on London that can be bought for \$5964.13, exchange  $4.86\frac{1}{2}$ ?

19. The face of a bill of exchange was £875, and its cost was \$4233.91. What was the rate of exchange ?

20. An exporter received \$9063.22 for a bill of exchange that was sold through a broker at \$4.86 $\frac{3}{4}$ ; what was the face of the bill, the broker's commission being  $\frac{1}{8}\%$ ?

21. Find the cost of a bill of exchange on Paris for 7000 francs at  $5.21\frac{3}{8}$ .

5.213) 7000	ANALYSIS.—Since 5.217 francs cost \$1,
$\frac{8}{41.75} \frac{8}{56000.0000} $	7000 francs will cost as many dollars as $5.21\frac{2}{8}$ francs are contained times in 7000 francs.

Find the value of 22. 6000 francs at 5.16.

23. 5000 francs at  $5.18\frac{1}{8}$ .

24. 4000 francs at 5.213.

Find the value of 25. 8475 frances at  $5.19\frac{1}{2}$ .

26. 7216 francs at 5.17<sup>3</sup>/<sub>4</sub>.

27. 987.60 francs at  $5.20\frac{7}{8}$ .

28. Find the cost of a draft on Antwerp at 3 days' sight, for 9640 francs, at  $5.19\frac{3}{8}$ .

29. What is the value of a draft on London for £416 16s. 3d., at  $4.85\frac{3}{8}$ ?

30. Sold exchange on Geneva, through a broker, for 8000 francs at 60 days' sight; what were the proceeds of the draft, exchange being  $5.20\frac{5}{8}$ , brokerage  $\frac{1}{8}\%$ ?

31. What are the proceeds of a draft on Paris for 12420 francs, at  $5.19\frac{3}{4}$ , brokerage on exchange  $\frac{1}{8}\%$ ?

32. What will it cost to remit to Antwerp 8750 francs at the par value? (561)

33. Sold through a broker a draft on Geneva for 7324 francs. What were the proceeds, exchange being  $5.18\frac{3}{5}$ , brokerage  $\frac{1}{5}\%$ ?

34. What will be the face of a bill of exchange on Geneva that can be bought for \$15372, exchange selling at 5.223?

35. Paid for a draft on Paris 3460.32; what was the face of the draft, exchange being  $5.19\frac{3}{2}$ ?

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36. A merchant paid \$6272 for a bill of exchange of 32512.48 francs; what was the rate of exchange?

37. Find the cost of a bill of exchange on Hamburg for 14400 marks (Reichsmarks) at  $94\frac{1}{8}$ .

OPERATION.

4)14400

3600 .941 ANALYSIS.—Since 4 marks cost  $0.94_{\frac{1}{5}}$ , 14400 marks will cost 3600 (14400 + 4) times  $0.94_{\frac{1}{5}}$ , or 0.3288.50.

3388.50

Find the value of

38. 7200 marks at 94. 41. 1237 marks at 93§.

39. 8416 marks at 93<sup>1</sup>/<sub>2</sub>. 42. 9894 marks at 95<sup>3</sup>/<sub>8</sub>.

40. 3456 marks at 95<sup>1</sup>/<sub>4</sub>. 43. 6515 marks at 94<sup>3</sup>/<sub>4</sub>.

44. What is the cost of a bill of exchange on Frankfort for 16200 marks at  $95\frac{1}{2}$ ?

45. Sold a bill of exchange on Hamburg for 13200 marks, at 941; what was the amount received, brokerage  $\frac{1}{3}$ ?

46. An importer purchased a bill of exchange on London for  $\pm 318$  10s. 7*d.*, at  $4.85\frac{3}{4}$ ; what did it cost?

47. What were the proceeds of a draft, sold through a broker, for 8748 marks, at  $94\frac{8}{5}$ , brokerage  $\frac{1}{5}\%$ ?

48. An exporter sold a draft on Paris for 12275 francs, at  $5.19\frac{5}{3}$ ; what were the proceeds, brokerage  $\frac{1}{3}\%$ ?

49. What is the face of a bill on Hamburg that cost \$816, exchange 941?

ANALYSIS.—Since  $$.94\frac{1}{3}$  will buy 4 marks, \$816 will buy 4 times as many marks as  $$0.94\frac{1}{3}$  is contained times in \$816.

50. What is the face of a 3 days' draft on Bremen, that was purchased in New York for \$3261.60, exchange  $94\frac{2}{3}$ ?

51. The cost of a draft of 12320 marks was \$2922.15; what was the rate of exchange?

52. Find the cost of a bill of exchange on Amsterdam, for 7240 guilders, at 404.

53. Find the cost of a bill of exchange on Amsterdam, at 60 days' sight, for 12480 guilders, exchange 394.

54. An exporter received \$1890.86 for a bill of exchange on Amsterdam; what was its face, exchange being  $41\frac{1}{2}$ , brokerage  $\frac{1}{2}$ ?

55. At 40<sup>§</sup>, how much exchange on Amsterdam will \$2877.93 buy?

56. The value of a draft of 5280 guilders is \$2145; what is the quotation?

57. The dividends of the N. Y. C. and H. R. R. Co., are paid in London at the rate of 49<sup>4</sup>/<sub>8</sub> pence to the dollar. What is the equivalent rate of exchange?

58. Find the value in U. S. money of 16319 bushels of wheat at 4s.  $4\frac{1}{4}d$ . per bushel, exchange 4.86 $\frac{1}{4}$ .

59. A merchant sent a messenger with a bill of exchange of 20000 frances to two bankers, A and B, with instructions to sell it to the best advantage. A offered 5.27 and B 5.27<sup>1</sup>/<sub>2</sub>. The messenger imprudently accepted the latter offer. How much did the merchant lose by the ignorance of the messenger?

60. When United States 4 per cent. consols are quoted in New York at  $114\frac{1}{2}$ , and sterling exchange at  $4.83\frac{1}{2}$ , what should be the London quotation of the bonds? What should be the London quotation of  $4\frac{1}{4}$  per cent. bonds, the New York quotation being  $113\frac{1}{4}$ ?

NOTE.—In London, all American securities are quoted on an assumed value of the pound sterling of \$5, instead of the actual value of \$4.8665, or, more definitely speaking, its commercial value determined by the rate of exchange. Multiplying the New York quotation by 5 and dividing by the rate of exchange, the result will be the equivalent London quotation.

61. When American railway stocks are quoted in London at 88, what is the equivalent New York quotation, sterling exchange being quoted in New York at 4.88<sup>1</sup>?

62. What is the London equivalent of a New York quotation of 142, exchange being 4.83?

63. At Paris, what is the value of a draft on London of £550, exchange being 25.364?

64. At London, what is the cost of a draft on Hamburg of 8000 marks, exchange being 20.45?

65. At Vienna, what is the cost of a draft on London of £625, exchange being 11.75?

66. At London, what is the value of a draft on Calcutta of 12000 rupees, exchange being quoted at 1s.  $8\frac{3}{16}d$ ?

67. A commission merchant wishes to remit \$2475 to his principal in England. How large a draft must he purchase, exchange being 4.831?

# EQUATION OF ACCOUNTS.

568. Equation of Accounts (called also Equation of Payments and Averaging Accounts) is the process of finding the time when several debts due at different dates may be paid in one amount without loss of interest to either party. It is also the process of finding the time when the balance of an account having both debits and credits may be paid without loss of interest to either party. This time is called the *equated* or *average time*.

Note.—It is important that the commercial student be thoroughly drilled in the theory and practice of Equation of Accounts, as examples in this subject are of frequent occurrence in many wholesale and commission houses.

# 569. To find the equated time when the items of the account are all on the same side, i. e., all debits or all credits.

ANALYTICAL STEPS.—By assuming a certain date as the time of settlement, we find what the loss or gain of interest would be to the payer if all the bills were paid by him on that date. We next find in how many days the total amount of the bills would produce a sum equivalent to this loss or gain of interest, and find the true day of settlement by counting forward or backward this number of days from the assumed date. Thus, if the sum of the several bills is \$1000, and the loss of interest to the payer at the assumed date of settlement is \$10 (the interest of \$1000 at 60 days at 6%), it is evident that the true date of settlement, or the time when there would be no loss of interest to either party, must be 60 days after the assumed date.

NOTES.—1. The interest on the bills paid after they became due would equal the interest on the bills paid in advance, the former being a gain to the payer, and the latter, a loss.

2. Any date may be assumed as the time of settlement. For convenience, the earliest or latest date is generally used. If the earliest date is taken, the estimated interest is a loss to the payer; if the latest is taken, the interest is a gain. When the time is found by Compound Subtraction, or each month is regarded as 30 days, the last day of the month preceding the earliest item is

the most convenient. (See second interest method.)

In Equation Tables, Dec. 31 or Jan. 1 is taken for all examples.

The assumed date is sometimes called the *focal date*.

3. Any rate of interest may be used in making the computations, 6 and 12 being the most convenient rates.

570. Ex. At what date may the following bills of merchandise be paid in one amount without loss of interest to either party? Due Apr. 10, \$114; due Apr. 26, \$140; due May 22, \$320; due June 6, \$976.

OPERATION.-PRODUCT METHOD.

Due	Apr.	10,	\$114	$\times$	0	=	0		
66	66	26,	140	$\times$	16	=	2240		
66	May	22,	320	×	42	=	13440		
66	June	e 6,	976	×	57	=	55632		
			1550			)	71312	( 46 day	ys
					a	ftei	Apr. 1	10. or M	Iav 26.

ANALYSIS.—For convenience, assume Apr. 10, the earliest due date, as the time of settlement. If the first bill, which is due Apr. 10, is paid on that date, there will be no loss or gain of interest to either party. If the second bill, which is due Apr. 26, is paid Apr. 10, 16 days before it is due, there will be a loss to the payer of the interest or the use of \$140 for 16 days, or \$2240 for 1 day. On the third bill, there will be a loss of the interest of \$320 for 42 days, or \$13440 for 1 day. On the fourth bill, there will be a loss of the interest of \$976 for 57 days, or \$55632 for 1 day. If all the bills are paid Apr. 10, there will be a loss of interest to the payer is equivalent to the interest of the total amount of the bills for 46 days, it is evident that the day when there would be no loss of interest must be 46 days after Apr. 10, or May 26. The payer is entitled to defer payment 46 days after the assumed date as a compensation for the estimated loss.

The gain of interest to the payer on the first three bills, which are paid after they are due, equals the loss of interest on the fourth bill, which is paid before it is due.

						PR	00 <b>F.</b>								
The	interest	of	\$114	for	<b>4</b> 6	days	at 6%	is	•						\$0.874
66	66	"	140	66	30	66	66		•						.70
66	66	"	320	66	4	66	66								.213
Tota	al gain o	f ir	nteres	t to	th	e pay	er	•							1.787
The	interest	(a	loss t	to tl	10 ]	payer)	of \$9	976	fo	or 1	<b>1</b> d	lays	s is	•	1.789

Notes.—1. In finding the number of days from the assumed date to the other dates, instead of calculating from the assumed date each time, find the interval from one date to the next and add it to the last number of days. Thus, from Apr. 10 to May 22 is 42 days, and from May 22 to June 6, 15 days; hence, from Apr. 10 to June 6 is 57 (42+15) days. (See Art. **310**, Ex. 3.)

2. To determine the due date, find the number of days in the operation nearest to the quotient, and add or subtract, as may be necessary, the difference between it and the quotient, to its corresponding date. Thus, in the above example, the number of days in the operation nearest to the quotient is 42; hence the due date is 4 (46-42) days after May 22, or May 26. (See Art. **311**, Ex. 10.)

S. If the fraction of the quotient is less than  $\frac{1}{2}$ , disregard it; if more than  $\frac{1}{2}$ , add 1 day to the integral number of days in the quotient.

571. RULE FOR THE PRODUCT METHOD.—Assume the earliest due date as the day of settlement for all the items. Multiply each item by the number of days intervening between the assumed date of settlement and the date of the item; and divide the sum of the several products by the sum of the account. Count forward from the assumed date the number of days obtained in the quotient. The result will be the equated time.

572. OPERATION .- FIRST INTEREST METHOD.

				Days.	Interest.			
Due	Apr.	10,	\$114	0	\$.00			
66	66	96	140	16	.233	for	10	days.
		20,	140	10 .	.14	"	6	66
" ]	Mor	99	320	42	1.60	66	30	66
	wray	~~,			.64	66	12	<i>c s</i>
					4.88	66	30	66
66	June	6,	976	57 -	2.44	66	15	66
		60)	15.50		1.952	"	12	"
			.258	)	11.885	( 4(	3 da	iys
					aft	er A	nr.	10. or

ANALYSIS.—Assume Apr. 10, the earliest due date, as the time of settlement. If the total amount (\$1550) of the bills is paid Apr. 10, the assumed date of settlement, there will be a loss of interest to the payer of \$11.885. The interest of \$1550 for 60 days at 6% is \$15.50, and for 1 day, \$0.258. It will take \$1550 to produce \$11.885 interest as many days as \$0.258 is contained times in \$11.885, or 46 days. If, at the assumed date of settlement, there is a loss to the payer of the interest of \$1550 for 46 days, the true day of settlement must be 46 days later, or May 26.

May 26.

573. OPERATION.-SECOND INTEREST METHOD.

Mo.		Days.		Interest.				
0	Apr.	10,	\$114	\$0.19				
0		26,	140	$\{ .466 \\ .14 \}$	for "	20 days. 6 "		
1	Mor	99	390	1.60	66 66	1 mo.		
1	May	~~,	520	.107	66	2 "		
9	Tuno	G	076	5 9.76	66	2 mo.		
N	June	2	$)\overline{15.50}$	.976	66	6 days.		
			7.75	) 14.306	(1)	mo. 25 da. :	after Mar. 3	1,
				7.75		or May	25.	
				6.556				
				3(	)			
			7.75	) 196.680	. 2	5 days.		
				1550				
				4168				
				3875				
				293				

ANALYSIS.—By this method, the last day of the month preceding the earliest due date is assumed as the date of settlement, and the time is found by Compound Subtraction, each month being regarded as 30 days.

The months are placed on the margin and the days correspond with the number of days in the given dates.

Mar. 31, the assumed day of settlement, there is a loss to the payer of \$14.306 interest, or the interest of \$1550 for 1 mo. 25 da. The equated time is therefore 1 mo. 25 da. after Mar. 31, or May 25.

Since this method regards all months as 30 days each, its results are not strictly accurate. The error in this example is 1 day. (See preceding results.)

When this method is used, and accurate results are required, the necessary corrections may be made by adding to the intervals of time 1 day for each intervening month containing 31 days. If the month of February is included, 2 days should be subtracted in a common year and 1 day in a leap year.

In counting forward to find the equated time, the opposite correction should be made. Thus, if the assumed date is June 30 and the quotient is 2 mo. 20 da., the equated time would be Sept. 18, 2 days being subtracted for July and August.

The following is the corrected operation for the given example, 1 day being added to the time of the fourth item for the month of May. The result is the same as by the product and the first interest methods.

\*

			OPERATION.					
Mo.	Days.		Interest.					
0	Apr. 10,	\$114	\$0.19					
0	·· 26,	140 {	.466	for	20 6	days.		
			1.60	"	1	mo.		
1	May 22,	320 {	1.067	66	20	days.		
			.107	66	2	"		
			9.76	66	2	mo.		
2	June 6-	+1, 976 -	.976	66	6	days.		
		2) 15.50	.162	66	1	66		
		7.75 )	) 14.468	(1	mo.	26 da	. after	Mar. 31,
			7.75		0	r May	26.	
			6.718					
			3	0				
		7.75	) 201.54	0 (	26 č	avs.		

#### EXAMPLES.

574. 1. At what date may the following bills be paid in one amount without loss of interest to either party? Due Sept. 10, \$145; Sept. 28, \$144; Oct. 8, \$75; Oct. 23, \$512.

2. What is the equated time for the payment of the following bills? Due Mar. 28, \$446; May 3, \$212; May 15, \$116; May 31, \$475; June 12, \$345.

3. What is the average due date of the following bills, each being due at the date given? Jan. 5, \$127.85; Jan. 26, \$134.18; Feb. 5, \$249.40; Feb. 23, \$418.73; Feb. 28, \$176.25.

NOTE.—The result will be practically the same if the nearest dollar is used in multiplying or in calculating the interest. Thus, in the above example, regard the amounts as 128, 134, 249, 419, and 176 respectively.

When there are several items in the example, some accountants omit the cents and units of dollars, and use the nearest number of tens. Thus, if the above account were of sufficient length, the numbers might be regarded as 13, 13, 25, 42, and 18 respectively. In this example the result is the same, but in some examples, containing the same number of items, there would be a discrepancy of one or more days.

4. Sold a customer bills at the due dates and to the amounts specified : June 1, \$152.73; June 15, \$114.28; July 16, \$247.84; July 25, \$88.90; Aug. 18, \$735.42; Aug. 29, \$416.34. When may the whole indebtedness be equitably discharged at one payment?

5. Average the following account :

NEW YORK, July 1, 1882.

MESSRS. RICE, STIX & Co.,

To LORD & TAYLOR, Dr.

188	2.			•				1	
Apr.	4	Mdse.	30	days ;	per bill	l rendered.		\$816	37
66	21	66	30	66	66	66		724	25
May	13	66	30	66	66	66		342	46
66	25	66	30	"	66	66		535	84
June	16	"	30	"	66	"	4	628	62
		Due b	y eo	quatic	on Jun	e *, 1882.		****	**

NOTE.—When several bills are sold on a common term of credit, first find the average date of purchase, and to the result add the common term of credit.

Certain merchants sell uniformly on the same term of credit, while others sell on different credits, depending upon the class of goods, the standing of the customer, the state of the market, ctc. (See Art. 416.)

6. A. Hamilton bought of F. A. Leggett & Co., several bills of goods, as follows :

May 16,	a bill	of \$212.46	$\mathbf{on}$	60	days'	credit
·· 28,	66	318.40	"	60	66	66
June 6,	66	275.64	"	60	66	66
" 21,	.66	187.83	66	60	"	66
July 13.		835.60	66	60	66	66

A 60-day note for the whole amount is given in settlement. What must be its date, no allowance being made for the days of grace?

7. Sold on a credit of 90 days the following bills of goods: Mar. 4, \$194.13; Mar. 27, \$222.36; Apr. 12, \$538.72; May 3, \$432.64; May 28, \$303.10. What is the equated time of payment? How much will settle the account Aug. 1, at 6%? How much July 1?

NOTE.—When monthly statements are sent to customers the accounts are frequently averaged. (See Ex. 5.) When the account is averaged, the simplest method of finding the cash balance due at a certain date, is to calculate the interest on the total amount from the average date to the time of payment, and add it, if the time of settlement is after the average date, and subtract it, if before.

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Since a fraction of a day is not considered in determining the average date, this method of finding the cash balance is not as accurate as that of Art. 589, in which the interest is reckoned on cach item separately.

8. A commission merchant sold several bills of goods, on a credit of 4 months, as follows : Aug. 16, 1881, \$387; Sept. 4, 1881, \$243.60; Sept. 18, 1881, \$637.75; Oct. 28, 1881, \$165.50; Dec. 10, 1881, \$856.45. What is the equated time of payment?

Note.—The above account may be averaged by first finding the average date of purchase, and adding the common term of credit; or by finding the due date of each bill separately, and determining the average due date from the dates thus found. Since the months have not uniformly the same number of days, the results by the two methods sometimes differ by one or more days, when the common term of credit is expressed in months.

9. Bought goods on 6 months' credit as follows: Feb. 16, 1881, \$376.50; Mar. 12, 1881, \$287.40; Mar. 19, 1881, \$612.87; Apr. 5, 1881, \$345.60; Apr. 26, 1881, \$134.80; June 1, 1881, \$612.35. What is the average time of maturity? How much would balance the account Jan. 1, 1882? How much Oct. 1, 1881?

10. Park and Tilford sold to R. M. Bishop & Co. the following bills of merchandise on 60 days' credit: Feb. 24, \$176.82; Feb. 28, \$327.49; Mar. 16, \$282.75; Mar. 28, \$512.14; Apr. 7, \$438.36; Apr. 14, \$109.70; May 1, \$632.65. What is the equated time of payment, and how much would be required to balance the account June 1? How much July 1?

11. The following bills of merchandise were purchased on 4 months' credit: June 1, \$237.16; June 18, \$146.75; June 30, \$333.84; July 5, \$416; July 16, \$535.62; July 27, \$912.33; Aug. 13, \$345.60. A note payable in 4 months was given in settlement. What was its date, no allowance being made for the days of grace?

12. Bought goods on 60 days' credit as follows: Aug. 11, \$487.60; Aug. 20, \$398.30; Sept. 1, \$411.26; Sept. 13, \$283.36; Sept. 22, \$112.43; Sept. 30, \$555.55; Oct. 20, \$342.48; Nov. 4, \$337.64. What is the average due date?

13. What is the average time for the payment of the following bills, each being sold on a credit of 4 months? Feb. 29, \$224.37; Mar. 13, \$642.50; Mar. 31, \$377.65; May 4, \$510.10; May 19, \$388.84; June 3, \$476.25; June 19, \$227.30; June 30, \$562.75.

14. Bought several bills of goods as stated below :

June	3, a	bill o	of	\$375	on	30	days'	credit.
"	28,	66		420	"	60	66	"
July	16,	66		560	"	4	month	s' "
Sept	4,	66		228	66	90	days'	66

What is the equated time of payment?

NOTE.—When the bills are sold on different terms of credit, first find the due date of each bill separately as in the following operation.

OPERATION .- PRODUCT METHOD.

Date of purchase	. Credit.	Due date.	Amount.	Days.	Products.
June 3,	30 days,	July 3,	\$375 ×	0 =	0
·· 28,	60 "	Aug. 27,	$420 \times$	55 =	****
July 16,	4 mo.,	Nov. 16,	$560 \times$	*** =	****
Sept. 4,	90 days,	Dec. 3,	$228 \times$	*** ==	****
			****	)	****** ( ** days.

OPERATION. - APPROXIMATE INTEREST METHOD.\*

Mo.		Days.		Credit.	Interest.			
0	Juna	3	\$275	20 dava	J \$1.875	for	1 mo.	
U	oune	ο,	<i>QU10</i> ,	ou uays,	1.187	66	3 days.	
					( 4.20	66	2 mo.	
0	66	28,	420,	60 "	{ 1.68	66	24 days.	
					( .28	66	4	
					€ 11.20	66	4 mo.	
1	Tulu	16	560	1 mo	2.80	66	1 "	
Т	July	10,	200,	± 1110.,	] .933	66	10 days.	
					.56	"	6	
	~ .				( 6.84	66	6 mo.	
3	Sept.	4,	228,	90 days,	1.153	66	4 days.	
		2 )	15.83					
			7.915	-7.915	5) 30.708	(3)	no. 26 da.	after
					23.745	Μ	ay 31, or S	Sept. 26.
					6.963			
					3	0		
				17 91	5 ) 208 89	$\frac{1}{2}$	6 dowg	
				1.010	, , , , 00.000	12	<u> </u>	

\* See second interest method, Art. 573

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15. What is the equated time for the payment of the following bills?

July	5,	1882,	\$516.60	$\mathbf{on}$	4	months'	credit.
	28,	66	327.35	66	60	days'	66
Aug.	15,	66	147.84	66	4	months'	66
Sept.	. 8,	66	485.42	66	30	days'	66
66	-25,	66	230.39	66	60	66	66

16. Sold several bills of goods as follows:

May	4,	a bill of	\$418.75	on	30	days'	credit.
66	16,	66	322.86	66	60	66	66
June	1,	66	513.44	66	4	month	s' "
66	12,	66	118.70	66	60	days'	66
66	30,	66	786.30	66	6	month	s' "
July	16,	66	274.85	66	60	days'	66

What is the average time of payment, and how much would balance the account Sept. 1? How much Oct. 1?

17. What is the average time of maturity for the payment of the following bills?

Mar.	4,	1883,	\$117.26	$\mathbf{on}$	4	months'	credit
66	21,	66	97.43	66	30	days'	66
66	29,	66	243.84	66	60	66	66
Apr.	16,	66	376.14	66	4	months'	66
66	30,	66	182.75	66	90	days'	66
May	18,	66	412.50	66	60	66	66
June	1,	66	518.65	66	30	66	66

18. Bought goods of Henry Welsh as follows:

Nov.	13,	1881,	a bill of	\$138.42	on	30	days' d	credit.
66	30,	66	66	416.10	66	60	66	66
Dec.	16,	66	66	324.70	"	30	66	66
Jan.	5,	1882,	66	586.85	"	4	month	s' 66
66	26,	66	66	234.38	66	60	days'	66
Feb.	12,	66	66	93.60	66	4	months	5' 66
66	23,	66	66	618.75	66	30	days'	""
Mar.	5,	66	66	374.36	"	60	66	66

What is the equated time for the payment of the whole?

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19. Average the following sales :

Sept.	4,	1881,	\$187.16	on	6	months'	credit.
66	16,	66	332.40	66	30	days'	66
66	24,	66	512.75	66	6	months'	. 66
Oct.	5,	66	164.60	66	6	66	66
66	27,	"	187.30	66	6	66	66
Nov.	5,	66	436.75	66	60	days'	66
66	16,	66	126.00	"	6	months'	66

20. Average the following account :

Dec.	1,	1882,	\$246.75	on	30	days'	credit.
66	12,	66	312.40	66	60	66	66
66	26,	66	819.46	66	4	month	.s' ''
Jan.	2,	1883,	674.32	"	4	66	66
"	10,	66	126.60	66	60	days'	66
Feb.	4,	66	434.50	"	4	month	.s' ''

575. To find the equated time for the payment of the balance of an account having both debit and credit items.

576. Ex. At what date may the balance of the following account be paid without loss of interest to either party?

Dr. JOHN ROACH in account with GEO. H. STUART. Cr.

188	1882.			1882.						
June	6	Mdse.	30	da.	456	00	July 26	Cash.	400	00
66	20	66	60	da.	384	00	Aug. 10	66	375	00
July	5	66	3	mo.	216	00	·· 10	Mdse. 60 da.	288	00
66	26	66	3	mo.	552	00				

# 577. OPERATION.-PRODUCT METHOD.

Du	e			Dr.			Du	е			Cr.		
July	6,	\$456	$\times$	0	=	0	July	26,	\$400	$\times$	20	=	8000
Aug.	19,	384	$\times$	44	=	16896	Aug.	10,	375	$\times$	35	=	13125
Oct.	5,	216	$\times$	91	=	19656	Oct.	9,	288	×	95	=	27360
66	26,	552	$\times$	112	=	61824			1063				$\overline{48485}$
		1608				98376							
		1063				48485							
		545			)	49891	( 92 da	ys a	fter J	uly	6,	or (	Oct. 6.

ANALYSIS.—First find the due date of each item. For convenience, assume July 6, the earliest due date, as the day of settlement for all the items on each side of the account. (See Art. **569**, Note 2.) If the balance of the account is paid July 6, the assumed date of settlement, there would be a loss to the payer, on the debit side of the account, equivalent to the interest of \$98376 for 1 day, and a gain on the credit side, equivalent to the interest of \$48485 for 1 day; or a net loss of \$49891 for 1 day, or of \$545 for 92 days. Since the loss of interest to the payer by settling the account July 6, is equivalent to the interest of the balance, or the amount paid, for 92 days, it is evident that the day when there would be no loss of interest must be 92 days after July 6, 1882, or Oct. 6, 1882.

If the greater sum of the products had been on the credit side, there would have been a gain to the payer by settling the account July 6, and the day that the balance of the account would commence to draw interest would have been 92 days before July 6, or Apr. 5, 1882.

578. RULE FOR THE PRODUCT METHOD.—First find the due date of each item. Assume the earliest due date as the day of settlement for all the items on both sides of the account. Multiply each item by the number of days intervening between the assumed date of settlement and the due date of the item, and find the sum of the products on each side of the account. Divide the balance (the difference between the sums of the debit and credit products) of the products by the balance of the account. The quotient will be the number of days intervening between the assumed date and the true date of settlement.

To find the true date of settlement, count forward from the assumed date, when the balance of the account and the balance of the products are on the same side (both debits or both credits); and count backward, when on opposite sides.

Notes.—1. The rule for counting backward and forward is the reverse of the above, when the latest date or a date after the latest date is taken as the assumed date of settlement.

2. Although the principles of equation of accounts are theoretically correct, they are not always practicable and can not be legally enforced. Thus, if a debt of \$4000 is due Feb. 1, no merchant would accept a payment of \$3600, Jan. 1, with the understanding that the remaining \$400 would remain unsettled 9 months after Feb. 1, or until Nov. 1. The merchant would undoubtedly be willing to allow a discount equivalent to the interest of \$3600 for the unexpired time, or 1 month.

3. In finding the equated time, reject the cents when less than 50; and add 1 dollar to the dollars when the cents are more than 50. The results will be sufficiently accurate.

		Dr	•.				Cr.		
Due	e		Days.	Interest.	Du	е		Days.	Interest.
July	6,	\$456	• 0	\$0.00	July	26,	\$400	20	\$1.333
Aug.	19,	384	44	2.816	Aug.	10,	375	35	2.187
Oct.	5,	216	91	3.276	Oct.	9,	288	95	4.56
66	26,	552	112	10.304			1063		8.080
		1608		16.396					
		1063		8.08					
	60	) 5.45		) 8.3160	( 92 days	after	r July	6, or	
		.090	8					Oct. (	3, 1882.

579. Operation.-First Interest Method.\*

ANALYSIS.—If the account is settled July 6, the assumed date of settlement, Mr. R. would be entitled to a discount on the debit side of \$16.396, and Mr. S. on the credit side of \$8.08; or, Mr. R. would be entitled to a net discount of \$8.316. If, by paying the balance of the account, July 6, Mr. R. is entitled to a discount of \$8.316, it is evident that he should be all wed to defer payment until the balance would produce an equivalent interest, or 92 days. Hence, the true date of settlement is 92 days after July 6, 1882, or Oct. 6, 1882.

When the balance of the account and the balance of interest are both due the same party, the equated time is previous to the assumed date of settlement; and, when the balance of the account and the balance of interest are due different parties, the equated time is after the assumed date.

**580.** In the following operation, the latest due date is assumed as the date of settlement for all the items :

				OPE	RATION.				
Due	в		Days.	Interest.	Du	е		Days.	Interest
July	6,-	\$456	112	8.512	July	26,	\$400	92	\$6.133
Aug.	19,	384	68	4.352	Aug.	10,	375	77	4.812
Oct.	5,	216	21	.756	Oct.	9,	288	17	.816
66	26,	552	0	.00			1063		11.761
		1608		13.620					
		1063		11.761					
	60	) 5.45	.0908	3) 1.8590	( 20 days	befo	re Oct.	26, or	
		.090	8					Oct. (	6, 1882.

ANALYSIS.—If the account is settled Oct. 26, the assumed date of settlement, the payer will be obliged to pay \$1.859 interest in addition to the balance of the account. Hence, the date when the balance only may be paid without loss to either party must be 20 days before Oct. 26, 1882, or Oct. 6, 1882.

# Art. 581.] EQUATION OF ACCOUNTS.

581. OPERATION.-APPROXIMATE INTEREST METHOD.\*

	1	Dr.			(	Jr.	
Mo.	Days.	Credit.	Interest.	Mo.	Days.	Credit.	Interest.
0 Tuno	C GAEC	20 7.	\$2.28				(\$2.00
0 June	0, \$400	30 aa. 3	.456	1 July	26, \$400	) .	1.333
			3.84	J			40
0 "	20, 384	$60  da. \ $	1 90				( 9.195
			1.40	2 Aug	. 10, 375	<b>;</b> .	) 0.70
1 July	5. 216	3 mo.	4.32		· ·		( .625
- • ····J	-,	(	18	9. 66	10 989	2 60 da	5.76
		(	11.04	~	10, 200	) 00 <i>aa</i> .	.48
1 "	26, 552	$3 mo. \prec$	1.84		1069	2	14 348
		(	.552		2000	Í	11.010
	1000		05 MOO				
	1008		29.788				
	1063		14.348				
	2)5.45	2.725)	11.440 (	4 mo.	6 da. afte	er May 3	1, or
	2.72	5	10.900				Oct. 6.
			.540				
			30				
		2.725	) $\overline{16.200}$	(6 day	7S.		

#### EXAMPLES.

582. 1. At what date may the balance of the following account be paid without loss to either party ?

Dr.		ISAI	AH I	B. PRICE.	•	Cr.		
1889. May 16 ·· 31	To Mdse.	437 324	00 00	1889. May 23 June 16	By Cash.	400 300	00	

2. Find the average date of maturity for the balance of the following account :

Dr.		W	ILLIA	м С	. Dougla	.s.	Cr	•
1888. Jan. 4 ·· 28 Feb. 4	Mdse. 	30 da. 60 da. 4 mo.	$516 \\ 325 \\ 437$	00 00 00	<sup>1888.</sup> Feb. 1 '' 1	Cash Note 60 da. (63 da.)	500 300	00 00

\* See second interest method, Art. 573, and second method, Ex. 14, page 244.

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(In

3. 1	Avera	ge the	e follo	wing	account:	
------	-------	--------	---------	------	----------	--

Dr.		J	OSEPI	вΗ		Cr.					
1882. Mar. 27 Apr. 16 May 1 June 4	Mdse, "	4 mo. 60 da. 4 mo. 4 mo.	716 325 413 716	48 75 40 87	1882. Apr. 1 May July	L6 2 8	Cash. "	•	•	300 400 500	

4. What is the equated time for the payment of the balance of the following account?

Dı	r.		1	1 in a	accou	int wit	with B.					
188	1882.					1882	1.					
Mar.	16	Mdse.	4 mo.	444	57	July	1	Cash.			400	
66	30	66	60 da.	376	82	66	20	66			375	
Apr.	20	"	30 da.	712	19	Aug.	16	66			700	
May	17	66	4 mo.	628	75		30	66			600	
66	28	٠٠	4 mo.	419	31							

5. Average the following account. What will be the amount due Jan. 1, 1882? C in account with D

DI	•						ciio witoii	<i>L</i> .	01.	
1881							1881.			
June	16	Mdse.	30	da.	517	25	June 16	Note 60 (63) $da$ .	1000	
66	28	66	60	da.	487	50	July 30	Cash	375	
July	5	66	4	mo.	816	75	Aug. 13	Mdse. 4 mo.	900	
دد	21	66	6	mo.	924	30	Oct. 5	Cash	500	
Aug.	<b>12</b>	"	4	mo.	317	65				

6. When will the balance of the following account commence drawing interest? How much would be due Mar. 1, 1883.

Dr.	•	Andrey	W CARN	CARNEGIE, Pittsburg, Pa.							
1882.				1882							
Sept.	4	Cash	100	Aug.	16	Mdse.	4	mo.	647	13	
· · ·	4	Note 4 mo.	900	66	29	66	4	mo.	322	85	
Oct.	31	Cash	250	Sept.	4	66	4	mo.	412	90	
Dec.	28	<b>66</b>	600		17	66	4	mo.	588	33	
				66	17	66	30	da.	246	12	
5 2	4			Nov.	4	66	4	mo.	683	45	

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Dr
7. Find the equated time for the payment of the balance of the following account.

Dr	•		JAN	IES I	<b>B. F</b>	. FARWELL, Chicago, Ill.							
1881	l.						1881						
Jan.	4	Mdse.	4	mo.	637	20	Mar.	16	Cash.	300	00		
66	14	66	4	mo.	412	87	Apr.	20	66	400	00		
66	14	66	60	da.	214	35	May	3	66	200	00		
Mar.	16	66	4	mo.	298	60	66	3	Note 4 mo.	800	00		
66	28	66	30	da.	973	25							

8. Average the following account :

Dr			ARN	OLD,	Co	, Cr.			
1882		1				1882			T
Apr.	4	Mdse.	4 mo.	426	32	Apr.	25	Cash.	375
66	20	66	Cash.	387	40	June	30	66	600
May	13	66	60 da.	622	39	July	31	Note 60 da.	600
"	27	66	30 da.	584	75	Aug.	15	Cash.	500
July	5	66	4 mo.	224	50	Oct.	31	66	400
66	16	66	4 mo.	838	95				

583. To find the equated time for the payment of the net proceeds (423) of an account sales (424).

584. 1. The sales form the credit side of the account, and the charges and advances the debit side.

2. The charges for transportation, cartage, and other items paid by the commission merchant are considered due at the time of the payment of the same.

3. The commission and other after-charges of the commission merchant are considered due by some at the average *due* date of the sales; and by others, at the average date of the sales. Since the commission is so small compared with the gross sales, in many examples, it makes no difference which date the commission is considered due. Certain merchants enter the commission at the date the account sales is rendered, and, by so doing, produce a result sufficiently accurate.

4. Many commission merchants, when the consignments are not separated and numbered, enter the sales and commission only on the account sales (See Ex. 4, Art. 586), and enter the advances

[Art. 584.

and the general charges in the account current (See Ex. 6, Art. **594**). Accounts sales, when the shipments are continuous, are rendered monthly to the manufacturers or consignors, and "sketches" weekly or whenever a sale is made.

5. With the exception of finding the date for the commission and other after-charges, the process of averaging an account sales is exactly the same as that of averaging an account containing both debit and credit items.

585. Ex. What is the equated time for the payment of the net proceeds of the following account sales?

NEW YORK, Dec. 1, 1881.

Account sales of Seed

For account of William Stephens & Co. By Franklin Edson & Co.

1881.			-	
Nov.	4	4520 bu. Timothy Seed . 30 da. $115$	79 53	
66	18	50 " Mammoth Cl. Seed 60 da. 990	450	
66	28	4948 " Clover Seed Cash. 840	418 32	947 85
		CHARGES.		
Oct.	31	Transportation	60 00	
Dec.	1	Commission 5% as Dec. 22, 1881.	47 39	107 39
		Net proceeds due Dec. 26, 1881		840 46

ANALYSIS.—The average *due* date of the sales is Dec. 22, 1881, which is taken as the due date for the commission.

The account sales to be averaged will now be as follows :

	Dr.					Cr.							
Due	Oct.	31,	1881,	\$60.00	Due	Dec.	4,	1881,	\$79.53				
66	Dec.	22,	66	47.39	66	Jan.	17,	1882,	450.00				
					66	Nov.	28,	1881,	418.32				

By averaging the above, we find the net proceeds, \$849.46, are due Dec. 26, 1881.

If the commission is considered due Nov. 21, 1881, the average date of the sales, the net proceeds will be due Dec. 28, 1881.

Note.—If the same assumed date, or focal date, be taken in finding the average due date of the sales as in finding the average due date of the net proceeds, the operation of the former will form the credit side of the latter operation.

## EXAMPLES.

**586.** Find the net proceeds and equated time of the following accounts sales. (Unless otherwise stated, the commission is considered due at the average due date of the sales.)

1. Sales of 400 bbls. flour received per N. Y. C. & H. R. R. R., for account of A. W. ARCHIBALD, Ottumwa, Iowa.

1881.			
May	11	125 bbls. "Kirkwood" cash, 675	*** **
66	12	150 " "Iowa" 4 mo., . 650	***
66	18	125 " "Kirkwood" 4 mo., . 700	*** *** **
		CHARGES.	
		CHINGLO	
May	3	Transportation and Cartage,	425
66	4	Inspection,	15
66	18	Storage,	45
		Commission and Guaranty 5%,	*** ** ***
		Net proceeds due per average,, 1881,	****
E	. &	O. E. E. R.	LIVERMORE.

NEW YORK, May 20, 1881.

What would be the equated time for the payment of the above proceeds, if the commission and guaranty were considered due at the average due date of the sales? At the average date of the sales? If considered due May 18, the date of the last sale?

2. Account sales of 900 sides hemlock sole leather by MAS-SEY & JANNEY, for account of GRANT & HORTON, Ridgway, Pa.

1881.		Sides.	Description	•	Terms.	Weight.	Price.			1	1	
Aug.	14	400	"Ridgway"	'#7	4 mo.	9407	27	****	**			
66	18	300	66	#7	4 mo.	6875	$27\frac{1}{4}$	****	**			
66	21	200	66	271	****	**	****	**				
_		CHARGES.										
Aug.	2	Tran	ransportation \$70, Cartage \$9, **									
66	3	Inspe	ection, .	• •				9				
		Com	mission and	Gu	aranty a	5%, .		***	**	***	**	
1	114	Proce	eeds due	—,	1881,				_	****	**	
E. & O. E. Massey & Janney.												
PHILADELPHIA, PA., Aug. 22, 1881.												

3. Find the equated time for the payment of the net proceeds of Ex. 25, Art. 427, supposing that the merchandise was sold for cash, and that the commission was due at the date given.

4. Sales by JAMES TALCOTT, New York, for account of Phenix Mills, Cohoes, N. Y. March 31, 1882.\*

Date	э.	Cases.	No.	D	escription.	Time.	Yards.	Price.	Amount.
Mar.	1	2	7619	Fancy	Cassimere.	30 da.	9662	1.35	**** **
66	10	4	3475	66	66	10 da.	1994	1.70	**** **
66	13	3	4157	66	66	30 da.	15061	2.30	**** **
66	17	4	6283	66	66	4 mo.	19363	1.65	**** **
"	26	2	3971	66	66	Cash.	978	1.85	**** **
				•					****
			Less	Comm	ission 5%,				*** **

Proceeds due —, 1882,		
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5. Account Sales of merchandise by JOHN F. COOK, for account of Excelsior Packing Co., Cincinnati, Ohio.

													_		
1881.															_
Oct.	16	50	Bbls.	Mess	Bee	ef,			Ca	sh.	1125	***	**		
66	24	100	66	N. M.	Po	rk,				"	1750	****			
66	31	25	66	Hams	63	76 1	bs.,		10	da.	13‡¢	***	**		
Nov.	9	25	66	Shoul	der	s 57	17	lbs.	, 60	da.	9¢	***	**		
"	18	75	66	С. М.	Po	rk,			4	mo.	1315	****	**	****	**
		- 0													
					Сн.	ARG	ES.								
Oct.	13	Tra	nspor	tation,								325			
66	15	Car	tage,			. 1						37	50		
66	15	Coo	perag	e, .								15			
66	15	Insp	pectio	n, 📜								13	75		
Nov.	18	Stor	rage,	• •	•			•				48	75		
		Con	nmissi	ion $5\%$	, .							***	**	***	**
		Net	proc	eeds d	ue		-,	188:	1, .	•			-	****	**
• E	. &	; O.	E.								Joi	IN F.	С	00K.	
N	EW	Y	DRK, N	V. Y.,	No	v. 2	0, 3	1881	L.						

\* If the commission is considered due at the average due date of the sales, and since there are no other changes, the net proceeds will be due at the same date.

# ACCOUNTS CURRENT.

587. An Account Current is an itemized account of the business transactions between two houses, showing the balance or amount due at the current date. The amount due is sometimes called the *cash balance*.

1. An account current is a transcript of the ledger account with the addition of certain details taken from the books of original entry, and is arranged in a different form.

2. Interest is charged, or not, according to the custom of the business, or the agreement between the parties. This chapter treats only of accounts in which interest is charged. When interest is not charged, the balance due is the difference between the two sides of the account as originally entered in the ledger. The interest may be reckoned according to any of the methods of Art. **437.** In the illustrative example the exact time in days is found, and the days are regarded as 360ths of a year. In the examples for practice, unless otherwise stated, the interest is reckoned on the same basis.

3. Accounts current are rendered by merchants, bankers, and brokers annually (Ex. 2), semi-annually (Ex. 1), quarterly (Ex. 3), or monthly (Ex. 6). Since the interest draws interest after the account is balanced, the oftener the account is balanced, or the interest is added to the account, the greater the amount due. Some merchants render partial accounts current monthly, but do not carry the interest to the main column until the end of the year (Ex. 11). The twelve partial accounts current make, when combined, the complete account current for the whole year.

4. There are three methods in common use for finding the amount due on an account, including interest, at a certain date, all of which are presented in the following illustrative example: 1. By interest; 2. By products; 3. By daily balances. 588. Ex. Find the amount due, including interest at 6%, on the following account Jan. 1, 1882.

188	l.				1881	ι.			
Oct.	1	Balanc	e.	1800	Oct.	31	Cash.	1000	
66	16	Mdse.	30 da.	360	Nov.	16	Note 30 da.	600	
Nov.	27	66	30 da.	432	Dec.	4	Cash.	240	
Dec.	18	Bill of	H.C. & Co.	420	66	26	66	300	

Dr. GEO. W. CHILDS in account with A. A. Low. Cr.

589.	Operation]	INTEREST	M	ETHOD.
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		Dr.					Cr.		
Du	e.	Amount.	Days.	Interest.	Du	e.	Amount.	Days.	Interest.
Oct.	1,	\$1800	92	\$27.60	Oct.	31,	\$1000	62	\$10.33
Nov.	15,	360	47	2.82	Dec.	19,	600	13	1.30
Dec.	27,	432	5	.36	66	4,	240	28	1.12
66	18,	420	14	.98	66	26,	300	6	.30
		\$3012		\$31.76			\$2140		\$13.05
		2140		13.05					
		872	+	18.71	= 89	90.71.			

ANALYSIS.—First find the due date of each item of the account. Each item will draw interest from its due date until the day of settlement, or Jan. 1, 1882. The total interest on the debit side of the account is \$31.76, and on the credit side, \$13.05. The balance of interest, \$18.71, is therefore in favor of the debit side, or is due Mr. Low.

Since both the balance of the account (\$872) and the balance of interest (\$18.71) are due the same party, the net amount due Jan. 1, 1882, is \$872 plus \$18.71, or \$890.71.

If the balance of interest had been on the credit side of the account, the net amount due would have been \$872 minus \$18.71, or \$853.29.

Notes.—1. It will sometimes happen that certain items will fall due after the day of settlement. The interest on such items should be transferred to the opposite side of the account. (See Ex. 8.)

2. If the account has been averaged, the amount due at a given date may be found by calculating the interest on the balance of the account from the time it is due to the date of settlement. If the date of settlement is earlier than the average date, subtract the interest from the balance of the account; if later than the average date, add the interest. (See Art. **574**, Ex. 7, Note.)

3. The interest method is generally used in business. Since it gives the interest on each item and is readily understood, it is more satisfactory to those to whom accounts current are sent than the product method. When interest tables are used, it is shorter than any other method.

### Art. 590.]

**590.** The following is a common form of an account current including interest :

Dr. (	feo. 1	W. 1	CHILDS	in	%	current	with	A.	A. ]	Low.	C	)
-------	--------	------	--------	----	---	---------	------	----	------	------	---	---

				1		11	1	<u></u>		
188	1.		Days.	Interest.	Amounts.	1881.		Days.	Interest.	Amounts.
Oct.	1	Balance.	92	27.60	1800.00	Oct. 31	Cash.	62	10.33	1000.00
66	16	Mdse. as Nov. 1	5. 47	2.82	360.00	Nov. 16	Note as Dec. 19.	13	1.30	600.00
Nov.	27	" " Dec. 2	7. 5	.36	432.00	Dec. 4	Cash.	28	1.12	240.00
Dec.	18	Bill of H. C. & Co	. 14	.98	420.00	" 26	**	6	.30	300.00
1882				100		1882.				
Jan.	1	Bal. of Interest.			18.71	Jan. 1	Bal. of Interest.		18.71	
						· 1	" " Account.			890.71
1832				31.76	3030.71				31.76	3030.71
Jan.	1	Balance.	1		890.71		. · · · · · · · · · · · · · · · · · · ·			

**591.** RULE FOR THE INTEREST METHOD.—First find the due date of each item of the account. Then find the interest on each item from the date it becomes due to the day of settlement. The difference between the sums of the debit and the credit interest will be the balance of interest.

To find the net amount due, when the balance of interest and the balance of items are on the same side, take their sum; when on opposite sides, take their difference.

592. OPERATION .- PRODUCT METHOD.

		$D_{2}$	r.				Cr.							
Due	э.	Am't.	]	Days	3.	Products.	Du	le.	Am't.		Days.		Products.	
Oct.	1,	\$1800	×	92	=	165600	Oct.	31,	\$1000	×	62	=	62000	
Nov.	15,	360	×	47	=	16920	Dec.	19,	600	X	13	=	7800	
Dec.	27,	432	×	5	=	2160	66	4,	<b>240</b>	×	28	=	6720	
66	18,	420	×	14	=	5880	66	26,	300	×	6	=	1800	
		\$3012				190560			\$2140				78320	
		2140				78320	\$8	372 -	+.\$18.7	1 :	= \$	890	.71.	
		872			6)	112240								
					_	\$18.706								

ANALYSIS.—By multiplying the number of dollars by the number of days, and taking the sum of the products on each side of the account, we find that the total debit interest is equivalent to the interest of \$190560 for 1 day, and the total credit interest to the interest of \$78320 for 1 day. The balance of interest is therefore equivalent to the interest of \$112240 for 1 day. The interest of \$1 for 1 day is  $\frac{1}{2}$  of a mill (446), and of \$112240, 18706 ( $\frac{1}{2}$  of 112240) mills, or \$18.71. Since the balance of items (\$872) and the balance of interest (\$18.71) are both due the same party, the net amount due is their sum, or \$890.71.

Date.	Dr.	Cr.	Dr. Balances.	Days.	Dr. Products.
Oct. 1	1800		1800	30	54000
" 31	-	1000	800	15	12000
Nov. 15	360		1160	19	22040
Dec. 4		240	920	14	12880
" 18	420		1340	1	· 1340
" 19		600	740	7	5180
·· 26		300	440	1	440
" 27	432	1	872	5	4360
	3012	2140		92	6) 112240
	2140				18.706

593. OPERATION.-BY DAILY BALANCES.

872 + 18.71 = 890.71.

ANALYSIS.—Arrange the debit and the credit items in the order of their dates as in the operation. Find the balance of the items at each of the dates. There is a debit balance of \$1800 for 30 days ; the interest of which is equivalent to the interest of \$54000 for 1 day. The interest of the next balance, \$800, for 15 days is equivalent to the interest of \$12000 for 1 day, etc. The total balance of interest is equivalent to the interest of \$112240 for 1 day, or \$18.71. The net amount due is \$872 plus \$18.71, or \$890.71. (See Art. **446.**)

Notes.—1. If, at any time in the above operation, there had been a credit balance, it would have been necessary to have had additional columns for "Cr. Balances" and "Cr. Products."

2. The above method is used by bankers and trust companies that pay interest to depositors upon their "daily balances."

## EXAMPLES.

Cp.

**594.** *1.* Find the balance due on the following account, Jan. 1, 1889, interest being reckoned at 6%.

Dr. Howard			рŢ	HORNTON	Cr.		
1888.				1888.		-	
July 1	Balance.	1830	45	Sept. 13	Net Proceeds.	876	40
Aug.24	Mdse.	448	00	Oct. 31	66 66	912	36
Oct. 18	Draft C. & C.	387	40	Nov. 5	Cash.	1000	00
Dec. 12	Draft H. & C.	516	88				

### Art. 594.]

2. What is the net amount due on the following account, July 1, 1882, at 6%?

Dr.	C. H.	MILLS	$\mathbf{in}$	%	current	with	G.	F.	SWORTFIGUER.	Cr.
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1881						1881		1			
July	1	Balan	ce.	1275	46	Nov.	14	Mdse.	4 mo.	587	19
Sept.	13	Draft	#1012.	871	52	1882					
1882						Mar.	13	66	30 da.	612	35
Jan.	4	66	#1017.	913	27	Apr.	27	66	60 da.	846	93
May	17	66	<b>#1024.</b>	345	63	June	3	Cash.		500	00

3. What is the balance of the following account, Apr. 1, 1882, at 6%?

Dr. W. J. HILLIS in account with LANGRAVE SHULTS. Cr.

1882						1882	2.			
Jan.	16	Dft.	M. & C.	937	64	Jan.	1	Balance.	3456	75
66	31	66	B. & D.	856	75	66	27	Sales as Mar. 15	1225	19
Mar.	3	66	W.&Y.	1749	30	Feb.	4	Mdse as Mar. 6	673	75
66	24	66	V. & C.	912	38	66	28	Sales as Mar. 19	2428	35

4. Find the amount due Aug. 1, at 6%, on the account represented in Ex. 7, Art. 574. (See Note, Ex. 7, Art. 574.)

5. Find the amount due Oct. 1, 1882, at 6%, on the account represented in Ex. 4, Art 582.

6. Find the balance due Apr. 1, 1882, at 6%, on the following account current.

PHENIX MILLS in % current with JAMES TALCOTT, New York, Apr. 1, 1882.

Date	e.	Dr.	Amoun	its.	Date.	Cr.	Amounts.
1382	).				1882.		
Mar.	1	Balance.	45108	34	Mar. 31	Net Proceeds	-
66	<b>1</b> 6	Draft #676.	1000			of Account	
66	18	·· #675.	2000			Sales due Apr.	
"	24	·· #678.	5000			26, 1882.	12505 70
"	28	Cotton Bill.	3176	42		(See Ex. 4,	
66	30	Transportation.	875	10		Art. 586.)	

7. Find the gain or loss on the following consignment account, taking as the day of settlement Jan. 29, 1881, the day the draft for the balance of the account was drawn and sold, and reckoning interest at 6% (365 days to the year).

1880.		Dr.	Days.	Inter	rest.	Amoun	ts.
Apr.	25	Mdse. Net Cash	970	900	17	\$ 6544	72
66	25	Clearance.	210	000	11	11	20
May 1881.	10	Insurance.	***	*	**	40	
Jan.	29	Balance of Interest to debit.				***	**
66	29	Gain.		1		***	**
				***	**	****	**
1880.		Cr.					
May	7	Draft 18000 Reichsmarks	***	***	**	4258	42
Nov. 1881.	20	" 2000 "	**	*	**	468	75
Jan.	29	" 9998 "	0			2368	28
"	29	Balance of Interest to debit.		***	**		
				***	**	****	**

Cons. F. L. BRUCKMANN, #14.

8. What was the amount due on the following account Feb. 13, 1881, the estimated due date of a sight draft drawn Jan. 29, 1881, for the balance, reckoning interest at 5% (365 days to the year)?

F. L. BRUCKMANN on account of Consignment #14.

1880.		Dr.	Days.	Interest.	Amounts.
Oct. Dec.	25 31	Account Sales due Jan. 9, 1881 " " Mar. 7, 1881	35	44 80	9344 82 22417 54
1381. Feb.	13	Balance of Interest to credit.		*** **	****
1880.		Cr.			
June	30	Freight due May 14, 1880	***	** **	1100 20
May	6	Draft 60 days' sight "July 18, 1880 }	***	*** **	\$ 8000
Nov.	19	" 60 " " Feb. 1, 1881	**	* **	¢ 10000 2000
1881.	10				
Feb.	13	Interest Rm. 22417.54 ** Mar. 7, 1881	**	** **	
Tom	13	Dalance of Interest to credit.			*** **
Juli.	29	Drant at sight to outdate due Feb. 13, 1881			**** **
		and see a second se		*** **	***** **

NOTES.—1. The interest on all items falling due after the day of settlement should be entered in the interest column on the opposite side of the account.

Some accountants enter these items of interest on the same side of the account in *red* ink so that they will not be added to the other items, and transfer the "red interest" in one amount to the opposite side.

2. The foregoing represents an account in German marks (reichsmarks) kept in an auxiliary book by a consignor of merchandise to a commission merchant at Hamburg, Germany.

The due dates of drafts, accounts sales, and other items are obtained from the letters from the commission merchant and from accounts sales and memoranda rendered by him. The corresponding consignment account as entered in the books of the consignor is represented in Ex. 7.

9. What was the balance due Jan. 1, 1882, at 6%, on the account represented in Ex. 5, Art. 582.

10. Find the amount due Mar. 1, 1883, at 6%, on the account represented in Ex. 6, Art. 582.

11. Calculate the interest Jan. 1, 1883, in the following partial account current, and find the total amounts. (Interest 6%, 365 days to the year.) (See Art. **587**, 3.)

1882.		Dr.	Days.	Intere	est.	Amoun	its.
May	1	Totals from statement of May 1. 1882.		1387	63	28765	72
46	6	Draft H. B. Claffin & Co.	240	50	71	1285	43
**	9	" Austin, Nichols & Co.	***	**	**	674	89
**	13	" W. H. Schieffelin & Co.	***	**	**	346	27
66	25	" Early & Lane.	***	**	**	418	43
66	28	" Mitchell, Vance & Co.	***	**	**	576	80
				****	**	*****	**
					_		=
1882.		Cr.					
May	1	Totals from statement of May 1, 1882.		973	42	22413	71
66	5	Sales as June 28, 1882.	***	***	**	7316	84
**	12	" " Aug. 1, 1882.	***	**	**	2110	92
66	18	" " July 13, 1882.	***	***	**	13446	85
66	25	Cash.	***	**	**	2000	
				****	**	*****	**
	1						_

G. D. SLOCUM in account with W. B. MCMECHAN.

12. Find the balance due on the following account Feb. 13, 1881. (5%, 365 days to the year.)

A. WEINGREEN & Co., on account of Cons. #25.



13. Find the net gain or loss on the following consignment account, Jan. 29, 1881. (Interest 6%, 365 days to the year.)

Cons., A. WEINGREEN & Co., #25.

Days. Interest. Amounts. Days. Date. Date. Interest Amounts. 1890. 1880. June 30 Mdse. \*\*\* 4932 Nov. 20 Draft Rm. 18000 \*\* \*\* \*\* 4218 75 \*\* 86 \*\*\* 3 Clearance. \*\*\* \*\* 21) July 1881. Aug. 1 Insurance. \*\*\* \*\* 25 66 " 3869 Jan. 29 0 916 47 44 \*\*\* \*\* 1881. 2: Bal. of Interest. Jan. 29 Bal. of Interest. \*\*\* \*\* 65 29 Gain. \*\* \*\* \*\*\* \*\* \*\*\*\* \*\* \*\*\* \*\* \*\*\*\* \*\*

14. Find the amount due July 1, 1881, on the account represented in Ex. 7, Art. 582.

15. What was the balance due Jan. 1, 1883, on the account represented in Ex. 8, Art. 582?

16. Find the balance of the following account, Mar. 31, 1882, at 6%.

Dr.	JAMES A.	DOUGLAS	in ?	current	with	J.	H.	Ноут.	Cr.	
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1882.	-				188	2.			Γ
Feb. 2	8	Balance.	18452	50	Mar.	8	100 N. Y.C.	14537	50
Mar.	2	Draft.	700		66	11	50 H. & St. J.	5162	50
-" 1	1	100 N. W.	14062	50	66	17	Cash.	16000	
" 1	.8	200 H. & St. J.	20875		66	24	100 N. W.	14437	50

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Dr.

[Art. 594.

Cr.

Cr.

# STOCKS AND BONDS.

595. "Stock" is a term applied to the share capital of a company, and represents an interest in its property over and above its liabilities, and in the profits of its business after the expenses and interest on its bonds have been paid.

1. A *Dividend* is that part of the profits of a company which is divided among the stockholders, and is a certain amount per share or a certain per cent. of the par value of the stock.

2. The Capital Stock of a company is divided into shares usually of \$100 each. Shares of \$50 and \$25 are called half-stock and quarter-stock respectively.

3. A Stock Certificate is a written instrument issued by a company, and signed by the proper officers, certifying that the holder is the owner of a certain number of shares of its Capital Stock.

4. The *Par Value* is the sum for which the shares or certificates were issued, or the amount mentioned on their face. The *Market Value* is the amount for which they can be sold.

**596.** A Preferred Stock is one taking preference of the ordinary stock of a corporation in the payment of dividends.

Thus, the holders of preferred stock of a certain railroad are entitled to 6 per cent. on their stock out of any one year's earnings, before the common stock can receive any dividend. After such payment, the balance of earnings, if any remain, may be divided to the common stock.

Preferred stocks are generally the result of a reorganization of a railroad. For instance, the holders of the common stock may save the road from passing out of their hands by the payment of a certain sum of money, for which preferred stock is issued. In other cases, preferred stocks have been issued in payment of floating or unsecured debts.

In some reorganizations, there are two or more classes of preferred stock.

**597.** A **Bond** is the obligation of a Corporation, City, County, State, or Government to pay a certain sum of money at a certain time, with a fixed rate of interest payable at certain periods.

1. Bonds of business corporations are usually secured by a mortgage on the whole or some specified portion of their property.

2. Coupon Bonds are those with small certificates attached representing the different installments of interest payable at the different periods specified, during the time the bond has to run, which are to be cut off and collected from time to time as the interest becomes due.

3. Bonds are also issued without coupons, in what is known as the registered form. In this case the bond is only payable to the registered owner, or his assignee, and the interest is paid by check or in eash, to the owner or his attorney.

4. Bonds are sometimes issued with coupons attached payable to bearer, but the principal of which may or may not be registered at the choice of the owner.

5. Bonds are known as First Mortgage, Second Mortgage, etc., Consols, Sinking Fund, Income or otherwise, according to their priority of lien, the class of property upon which they are secured, or other characteristics. *Income bonds* are generally bonds on which the interest is only payable if earned, and ordinarily are not secured by a mortgage.

Bonds are also named from the rate of interest they bear, or from the dates at which they are payable or redeemable, or from both; as, U. S. 4's 1907, Virginia 6's, Western Union 7's, coupon, 1900, Lake Shore reg. 2d, 1903.

6. In speaking of the income from bonds the term "interest" is used, as it is the consideration received for the use of money loaned, while that derived from an investment in stock is called "dividend," because it is money divided to the stockholders from the profit of carrying on the business, after the fixed charges have all been paid.

7. Bonds are issued in denominations of \$50 to \$50000.

## GOVERNMENT BONDS.

**598.**  $4\frac{1}{2}$ 's of 1891. Redeemable at the option of the Government after Sept. 1, 1891. The amount outstanding July 1, 1887, was \$250,000,000. Interest is payable Mar. 1, June 1, Sept. 1, and Dec. 1.

**599.** 4's of 1907. Redeemable at the option of the Government after July 1, 1907. The amount outstanding July 1, 1887, was \$737,800,600. Interest is payable Jan. 1, Apr. 1, July 1, and Oct. 1.

600. Refunding Certificates. These certificates are of the denomination of \$10, bear interest at 4%, and are convertible at any time, with accrued interest, into 4% bonds. The amount outstanding July 1, 1887, was \$175,250.

**601.** Currency 6's. These bonds were issued to aid in the construction of the Pacific railroads. Principal and interest are payable in lawful money of the United States. Payable 30 years after date, and maturing at different dates from 1895 to 1899. The amount outstanding July 1, 1887, was \$64,623,512, all registered.

**602.** Denominations. The coupon bonds of the various issues are in denominations of \$50, \$100, \$500, and \$1000. The registered bonds are in denominations of \$50, \$100, \$500, \$1000, \$5000, and \$10000. Of the  $4\frac{1}{2}$ 's of 1891, and the 4's of 1907, there are, in addition to the above, registered bonds of the denominations of \$20,000 and \$50,000.

**603.** Coupon bonds, being payable to bearer, pass by delivery without assignment, and are therefore more convenient for sale and delivery than registered bonds, which must be assigned by the party in whose name they are registered. The interest coupons being also payable to the bearer will be cashed by any bank or banker in any part of the United States.

1. The interest on registered bonds is paid by checks, made to the order of the registered owner and sent to him by mail. These checks, when properly endorsed, can be collected and cashed through any bank or banker.

2. Coupon bonds may be converted into registered bonds of the same issue, but there is no provision of law for converting registered bonds into coupon bonds.

**604.** The quotations of government bonds at the New York Stock Exchange were as follows, July 1, 1887:

	Bid.	Asked.		Bid.	Asked.
U. S. 41/s, '91 reg.	$109\frac{3}{8}$	$109\frac{5}{8}$	U. S. cur. 6's, 1896	$126\frac{3}{4}$	
U. S. 41/s, '91 c.	$109\frac{1}{2}$	$109\frac{3}{4}$	U. S. cur. 6's, 1897	$129\frac{3}{4}$	
U. S. 4's, 1907 reg.	$128\frac{1}{4}$	1281	U. S. cur. 6's, 1898	$132\frac{3}{4}$	
U. S. 4's, 1907 c.	1281	$128\frac{1}{2}$	U. S. cur. 6's, 1899	$134\frac{3}{4}$	
U. S. cur. 6's, 1895	1231		Dist. of Col. 3-65's	$121\frac{1}{2}$	

All Government Bonds are dealt in and quoted "flat"—*i. e.*, the quoted market price is for the bond as it stands at the time, including the accrued interest—except that after the closing of the transfer books \* the registered bonds are quoted ex-interest—that is to say, the interest then coming due belongs to the holder of the bond at the time of the closing of the books, and does not go with the bond to the purchaser.

\* The transfer books of U. S. registered bonds are closed for the month preceding the day on which the interest is paid.

During the period in which the transfer books remain closed, the quoted price of coupon bonds includes the accrued interest falling due on the first of the ensuing month, while that of registered bonds does not. If, in the month of December, when the books are closed preparatory to the payment of the interest due January 1, the coupon Four per cents are quoted at 118, the equivalent for the registered bonds of the same issue would be 117, the three months' interest being equal to one per cent.

## NEW YORK STOCK EXCHANGE.

605. The New York Stock Exchange is an unincorporated body of brokers, whose business is to buy and sell stocks, bonds, and other representatives of value.

1. The floor of the Exchange is open for business from 10 A. M. to 3 P. M. There are two regular calls of Stocks daily; three of State and Railroad Bonds; and three of United States Bonds. Transactions are not, however, confined to the regular calls, but are continually taking place on the floor of the Exchange between the hours named above.

2. In Wall Street, there are what are known as strictly commission houses, who take and execute orders for securities, charging the regular commission, and, when customers desire, loaning funds on the securities on a deposit of 10 to 20% of market value being made. This is what is known as buying on a margin (609), where the customer intends to sell soon again, and merely buys for speculative purposes. Such houses will usually sell stocks "short" (610, 10) for their customers on a similar margin.

There are other houses which make no advances, and require customers to pay outright for securities when bought.

There are also houses which combine a banking and brokerage business, taking deposits and loaning money on any securities marketable at the Exchange, and buying and selling stocks on commission. Some of these extend the privilege of marginal business to their customers, while others do not.

There are other members who operate exclusively for their own account.

**606.** Quotations are made at so much per cent. on the basis of a par value of \$100 per share of stock, except in the case of mining securities and Sutro Tunnel stock, which are quoted at so much per share, without reference to their par value.

For example, the par value of Morris and Essex stock is 50, but the quotation, if the stock were worth just par in the market, would be 100%; or, if the quotation is 110, it means \$110 for \$100 worth of the par value, which, in the case of this stock, would be two shares, while in the case of a stock the par value of which is \$100 per share, it would be for one share.

On the other hand, if Sutro Tunnel, the par value of which is \$10 per share, is quoted at 2, it means \$2 per share; and, in like manner, if Home-stake, the par value of which is \$100, is quoted at 30, it means \$30 per share.

## Art. 607.] NEW YORK STOCK EXCHANGE.

**607.** Commission.—The regular charge for buying and selling securities dealt in at the Stock Exchange, except mining stocks, is one-eighth of one per cent.  $(\frac{1}{5}\%)$  on par value, or \$12.50 on 100 shares of stock of the par value of \$100 each.

**608.** Stocks are usually bought or sold either "cash," "regular way," "seller three," or "buyer three." A stock sold "cash" is deliverable the day sold; a stock sold "regular way" is deliverable the next day, or bought "regular way" is to be paid for the next day. Where nothing else is specified, "regular way" is always understood. When a stock is reported as bought "seller three," it is meant that the seller of the stock can deliver it on either of the three days at his option, but is not required to deliver until the third day. On the other hand, when a transaction is made "buyer three," the buyer can demand delivery of the stock at any time within three days, but must take it and pay for it by the third day.

1. Transactions on any of the above terms carry no interest.

2. If the option is over three days, six per cent. on the selling value of the stock is paid by buyer to seller.

3. One day's notice is required of intention to terminate an option of a longer period than three days.

4. The Stock Exchange does not recognize any contract for over sixty days. Should a stock pay a dividend during the pendency of a contract, the dividend belongs to the purchaser of the stock, unless otherwise previously agreed.

**609.** A Margin is a deposit made with a broker, by a person who wishes to buy or sell stock for speculation to enable the broker to "carry" the stock and protect himself against loss. It is usually 10% of the par value of the stock.

1. A person desiring to speculate in stocks, deposits with his broker \$1000 as a margin, and directs him to purchase 100 shares of a certain stock at 90. The broker would pay for the stock \$9000, \$1000 of which being furnished by the speculator, and the remainder, \$8000, by the broker. The broker charges legal interest on the amount furnished by him for "carrying" the stock. (See Ex. 52, Art. **G11**.)

2. The margin deposited with the broker is simply to protect the broker 'against losing any money should the stock move in the wrong direction. In case of its so doing, the margin must be made good by the deposit of an additional amount, otherwise the broker will sell the stock to protect himself from losing any of the money he has advanced.

### [Art. 610.

## 610. Explanation of Words and Phrases used in Wall Street.

1. Bear. An operator who is "short" of stock. He wishes to buy at a lower rate, and tries to depress the price of the stock of which he is "short."

2. *Bull.* An operator who is holding stock for an advance. He is said to be "long" of the stock. Bulls try to advance the prices of the stocks of which they are "long."

3. b. 3 (Buyer 3), 10, 20, 30, etc. Meaning at the buyer's option, within three days, ten days, etc. When in a stock transaction, the buyer has the privilege of taking the stock at any time during the number of days mentioned. In buyer's options, when the option is for more than three days, six per cent. interest is charged the buyer, and the seller is entitled to one day's notice.

4. b. c., "between calls." The sale not taking place on the call of the stock, but after the first call and before the second.

5. Collaterals. Stocks, bonds, notes, or other value given in pledge as security, when money is borrowed.

6. Cover, to "cover one's shorts." Where stock has been sold short, and the seller buys it in to realize his profit, or to protect himself from loss, or to make his delivery. This is "covering short sales."

7. Differences. When the price at which a stock is bargained for and the rate on day of delivery are not the same, the broker against whom the variation exists, frequently pays the "difference" in money, instead of furnishing or receiving the stock.

8. Ex.-Div., Ex.-Dividend. When the price of a stock does not include, and the stock does not carry to the buyer a recently declared dividend.

9. Seller, 3, 10, 20, 30, etc. Sold deliverable at seller's option, within the number of days named. When seller's options are for more than three days, the buyer pays six per cent. interest, unless "flat" is specified in the contract, and the seller must give one day's notice of delivery.

10. Short. When one has sold stock which he does not own, hoping to realize a profit by buying in at lower prices, he is said to be "short."

11. Watering a Stock. The act of increasing the quantity of a stock without a corresponding increase in the value of the property which it represents. This is usually done in the reorganization of a railroad, or in the consolidation of two or more railroads.

## EXAMPLES.

**611.** 1. A bank with a capital (**595**) of \$250,000, declares a semi-annual dividend of  $3\frac{1}{2}\%$ . What is the amount of the dividend, and how much will a stockholder receive who owns 16 shares of \$100 each (**595**, 2)?

2. An insurance company divides among its stockholders \$18000. What is the rate of the dividend, the capital stock being \$225000 ? How much is paid to Mr. A., who has a certificate (595, 3) for 25 shares ? 3. A gas company declares a dividend of 5%, and divides among its stockholders \$125000. What is its capital stock ?

4. The board of directors of a mining company declared a dividend of \$100,000, being five cents per share (par value \$10) on the capital stock of the company. What was the capital stock, and in how many shares was it divided ? The dividend was what per cent. of the capital stock ?

5. An installment of 10% was assessed and called on the capital stock of a new railroad company. How much was paid by Mr. B., who had subscribed for 50 shares (par value \$100)?

6. A railway company, whose capital stock is 1,750,000, declares a dividend of  $3\frac{1}{2}$  per cent. What was the amount of the dividend?

7. The Union Pacific Railway paid to its stockholders, in 1879, \$2,204,700. What was the par value of its stock, the rate of the dividend being 6%?

8. A quarterly dividend of  $3\frac{1}{2}\%$  was declared by a manufacturing company. What was the capital stock, the amount of the dividend being \$2100?

9. What is the market value of 200 shares of stock at 116§?
10. How many shares of W. U. Tel. can be bought for \$43725 at 791%?

11. What is the total par value (**595**, 4) and the total market value of 100 shares Lake Shore at  $118\frac{5}{8}$  (**606**), 300 sh. N. J. Central at  $89\frac{3}{4}$ , 500 sh. W. U. Telegraph at  $78\frac{1}{8}$ , 200 sh. U. S. Express at  $73\frac{1}{4}$ , 500 sh. N. Y., L. E. & W. com. at  $40\frac{1}{5}$ , and 800 sh. N. Y., L. E. & W. pref. (**596**) at  $90\frac{3}{8}$ ?

12. What is the cost of 250 shares Tex. & Pac. at  $50\frac{5}{8}$  and 100 shares Ohio & Miss. pref. at 104, brokerage  $\frac{1}{8}\%$  (607)?

13. What are the proceeds of 600 shares Morris and Essex (half stock, **595**, 2) sold through a broker at 121<sup>1</sup>/<sub>2</sub>?

14. What are the proceeds of the following stocks sold through a broker ? 200 shares Union Pacific at  $117\frac{3}{8}$ , 2000 shares N. Y., O. & W. at  $27\frac{1}{4}$ , 800 shares A. & T. H. pref. at 88, and 600 shares Chi. & Alton at 131 $\frac{1}{4}$ .

15. Find the cost of 10 shares Manhattan Bank at 135, \$5000 Erie 7's (**597**, 5) cons. gold bonds (**597**) at 128, \$1000 Toledo and Wabash 2d (**597**, 5) at  $108\frac{1}{8}$ , \$5000 C. R. I. & P. 6's, 1907, coupon (**597**, 2) at 129, and \$5000 Ohio Southern Income (**597**, 5) at 45, usual brokerage. 16. Find the proceeds of \$15000 U. S. 4's, registered, 1907 (**599**), b. 3, at  $117\frac{1}{2}$ , and \$10000 U. S.  $4\frac{1}{2}$ 's coupon (**598**) at  $114\frac{1}{2}$ , usual brokerage.

17. How much must be invested in U. S.  $4\frac{1}{2}$ 's, 1891, to produce a quarterly income of \$675, bonds selling at  $114\frac{3}{8}$ ?

18. When Ohio 6's are sold at  $109\frac{1}{2}$ , what is received for six \$500 bonds, brokerage  $\frac{1}{4}$ ?

19. When Pittsburg, Fort Wayne and Chicago 2d 7's, 1912, are worth 135, what will \$12000 in bonds cost ?

20. How many \$500 bonds shall I receive for \$4735 invested in U. S. 4's at  $118\frac{3}{2}$ ?

21. How much must be sent to a broker that he may purchase \$8000 U. S. 4½'s at  $102\frac{3}{4}$ , commission  $\frac{1}{8}\%$ ?

22. An executor sold Central of New Jersey stock at  $52\frac{6}{3}$ , and purchased with the proceeds \$42000 in U. S. 4's, 1907, at  $100\frac{7}{8}$ . What was the par value of the stock sold, usual brokerage ?

23. A broker bought on his own account 200 sh. Nor. Pac. pf. at  $69\frac{2}{3}$ , and sold the same the same day at  $73\frac{3}{4}$ . What was his gain ?

24. How many shares of Ill. Cen. bought at  $129\frac{3}{8}$ , and sold at  $132\frac{3}{8}$ , usual brokerage, will produce a gain of \$1375?

25. What income will be produced by investing \$235250 in 4% bonds at  $117\frac{5}{4}$ ?

26. The common stock of a railroad company is \$46,000,000, and the preferred stock (**596**) \$8,000,000. The company declares a dividend of  $3\frac{1}{2}\%$  on the preferred stock and 2% on the common stock. What is the surplus, if the net earnings are \$1,317,645 ?

27. Bought June 4, 800 sh. Ohio & Miss. pref. at  $35\frac{1}{2}$ , s. 30. The stock was delivered June 24. What was the amount paid including interest (**610**, 9)?

28. Bought May 16, 200 sh. Lake Shore at  $116\frac{3}{4}$ , b. 60, and called for the stock July 5. What was the cost including interest?

29. Jan. 10, sold 100 sh. Phil. & Read. at  $65_4$ , s. 3. Jan. 13 the stock was quoted at  $68_2$ . How much was the difference (**610**, 7) paid by the seller in settlement ?

30. How much must one invest in  $4\frac{1}{2}\%$  bonds, when they are selling at  $121\frac{1}{2}$ , in order to have an income of \$1800 per year ?

31. A man invests \$28020 in 4% stock at  $116\frac{4}{5}$ , brokerage  $\frac{1}{5}$ %. What is his income ?

32. I sell 200 sh. H. & St. J. pf. at  $111\frac{3}{8}$ , and 10000 N. Y. Elevated 1st mortgage bonds at 119. What will be the net proceeds of the sale, allowing usual brokerage?

33. A person sells 26 shares  $3\frac{1}{2}$ % stock at 86, and loans the proceeds at 5%. What is the increase in his income ?

34. July 1, 1887, the interest-bearing debt of the United States was as follows:  $4\frac{1}{2}$ 's, \$250,000,000; 4's, \$737,975,850; 3's \$14,000,000; Pacific R. R. 6's, \$64,623,512. What is the total interest for one year?

35. The capital stock of a railroad company was "watered" (**610**, 11) by declaring a stock dividend of 10%. If the market value of the old stock was 110, what should be the value of the new stock?

36. Jan. 1, 1882, the A. & B. R. R., having a capital stock of \$20,000,000, was consolidated with the B. & C. R. R., having a capital stock of \$32,000,000. The new company was organized under the name of the A., B., & C. R. R. For every share of the A. & B. R. R. there was issued  $1\frac{1}{2}$  shares of the new stock, and for every share of the B. & C. R. R. there was issued  $1\frac{1}{3}$  shares of the new stock. What was the capital stock of the new company, and how much was the stock "watered"?

37. Before the consolidation, the stock of the A. & B. R. R. was worth 1.20 in the market, and the stock of the B. & C. R. R. 90. What should be the quotation of the new stock?

38. During the year 1881, the A. & B. R. R. divided among its stockholders \$1,600,000, and the B. & C. R. R., \$1,920,000. During the year 1882, the new company divided an amount equal to the total dividends of the two companies in the preceding year. What were the rates of the dividends of the two companies in 1881, and the rate of the dividend of the consolidated company in 1882?

39. Mr. A. had 10 shares of the A. & B. R. R., and 16 shares of the B. & C. R. R. What was the total amount of his dividend in 1881? How many shares of the new stock did he receive, and what was the amount of his dividend in 1882?

40. The gross earnings of the M. C. R. R. for the year ended Dec. 31, 1880, were \$9,085,749; operating expenses and taxes, \$5,738,751; interest and rentals, \$1,586,410. After declaring a dividend, there was a surplus of \$261,532. What was the rate of the dividend, if the amount of the stock was \$18,738,200? 41. A gentleman bought bank stock, paying regular annual dividends of 6%, at 120. What was the rate per cent. of his income, or what per cent. did he receive on the money invested?

ANALYSIS.—Since dividends are reckoned on the par value of the stock, the dividend on 1 share of \$100 would be \$6. Since each share costs \$120, and pays \$6 income, the per cent. would be  $$6 \div $120$ , or 5%.

Note.—The above analysis will not apply to bonds that mature at a certain fixed time, unless the investor expects to sell the bonds before maturity at the cost price. If 6% bonds that mature in 1899 are purchased in 1889 at 120, and are sold at the same rate before maturity, they will pay 5% on the investment, or cost. If the bonds are held until maturity (1899), or for 10 years, the owner would receive from the government the par value only, or \$100 for a bond of that amount, and the bonds would yield less than 5%. If 6% bonds, maturing in 10 years, are purchased at  $1.07_{100}^{+2}$  and held until maturity, they will pay 5% on the investment. (See Ex. 59.) If 6% bonds, that mature in 2 years, are purchased at more than 112, there would be a loss of interest to the purchaser instead of a gain.

42. Which is the better investment, stock paying a regular annual dividend of 5% and bought at 80, or stock paying 8% dividends, and bought at 120 ?

43. If insurance stock paying regular dividends of 10% annually is bought at 1374, brokerage 4%. what per cent. of income will it produce ?

44. Which investment will produce the greater annual income and how much, \$20,000 invested in Chemical Bank stock at 2000 which pays dividends of 15% every two months, or the same amount invested in Chatham Bank stock at 125 which pays regular semiannual dividends of 3%?

45. What rate can you afford to pay for stock paying regular annual dividends of 10%, in order to realize 6% on the investment?

46. At what price must 8% stocks be purchased to afford 5% on the investment? To afford 6%?

47. Stocks bought at 80 pay regular dividends of 5%. What is the rate per cent. on the investment? At what rate should they be purchased to afford 4% on the investment? To afford 8%?

48. Purchased 400 shares Lake Shore at  $118\frac{1}{2}$ , and 200 shares Chesapeake and Ohio 2d pref., at  $24\frac{3}{8}$ . Sold the Lake Shore at  $113\frac{5}{8}$ , and the Chesapeake and Ohio at  $22\frac{3}{4}$ . What was the loss, usual brokerage, no interest ? 49. The gross earnings of the Union Pacific Railway Co. for 1879, were \$13,201,077.66; the operating expenses were \$5,475,-503.44. What were the surplus earnings, and what per cent. of the gross earnings were the operating expenses?

50. A synopsis of the report of the N. Y. C. & H. R. R. R. for its fiscal year ended Sept. 30, 1881, is as follows: Gross earnings from passengers, \$6,958,038; from freight, \$20,736,749; from miscellaneous, \$4,653,608; expenses, \$19,464,786; interest, rentals, and taxes, \$4,990,783. What was the surplus for the year after the declaration of a dividend of 8% on a capital stock of \$89,229,300? The expenses were what per cent. of the total earnings?

51. The L. S. & M. S. Railway reported as follows for the year ended Dec. 31, 1880: Gross earnings, \$18,749,461; operating expenses and taxes, \$10,418,105; interest, rentals, dividend on guaranteed stock, and \$250,000 for the sinking fund, \$3,000,374. After paying a dividend of 8%, there was a surplus for the year of \$1,373,662. What was the amount of the dividend, and the capital stock?

52. July 26, a broker received from a customer a remittance of \$1000 as a margin (**609**) and purchased for him 100 shares of St. Paul Common at 59. On Aug. 2, the broker sold the stock at  $64\frac{1}{2}$ . What was the customer's profit ?

OPERATION.

	Dr.	1			[
July 26.	To 100 shares St. Paul Com. 59 . \$5900				
	Commission $\frac{1}{8}\%$ 12.50	5912	50		
Aug. 2.	Interest \$5912.50, 7 days	*	**	****	**
	Cr.				
July 26.	By margin deposited	1000			
Aug. 2.	" 100 shares St. Paul Com. 641 . \$6450				
	Commission $\frac{1}{8}\%$ 12.50	6437	50		
Aug. 2.	Interest \$1000, 7 days	*	**	****	**
	Balance			****	**

The profit is equal to the balance less \$1000, the original deposit.

53. Aug. 30, a broker purchased for the account of a customer 300 shares Northwestern Railroad stock at 78. He deposited as a margin \$3000. On Sept. 22, the stock was sold at  $74\frac{3}{4}$ . What was the loss? (Interest 6%, usual commission.)

54. May 10, a speculator deposited with his broker \$5000 as a margin, and directed him to purchase for his account 500 shares N. Y., L. E., & W., pref. at  $90\frac{3}{8}$ . May 20, the stock was sold at  $94\frac{1}{8}$ . What was the gain, interest 6%, usual brokerage ?

55. Sept. 10, I deposited with my broker \$5000 as a margin, and he purchased for me 200 sh. Cen. Pac. at  $90\frac{1}{2}$ , 200 sh. Morris & Essex (half stock) at  $122\frac{1}{4}$ , 200 sh. Tex. & Pac. at  $49\frac{3}{4}$ . The stocks on Sept. 30 were quoted as follows : Cen. Pac.  $80\frac{3}{4}$ , Morris & Essex  $120\frac{1}{8}$ , Tex. & Pac.  $41\frac{5}{8}$ . How much should I have deposited with my broker to make my margin of 10% good, and to cover commission for buying and selling, and interest? If I had been unable to have made an additional deposit, and the broker had "sold me out," what would have been my loss?

56. An operator, supposing Erie would decline in value, ordered his broker to sell short 100 shares at 50, and at the same time deposited with him as a margin \$1000. The broker on receiving the order sold for his account 100 shares at 50, and borrowed the stock for delivery. When the market price declined to 45, he ordered the broker to "cover his short sale" (buy the stock for delivery), and return the stock to the party from whom it was borrowed. What was the gain, usual brokerage ?

OD	1028 1	200	20	37.
U.F		 		
~ ~		_		

	- $Cr.$		
By	margin deposited	\$****.**	
66	100 shares Erie borrowed and sold at 50	**** **	\$****.**
	Dr.		
то	100 shares Erie bought and returned at 45 .	\$****.**	
66	commission for selling the stock $\frac{1}{8}\%$	**.**	
66	" buying and returning the stock $\frac{1}{8}\%$	** **	**** **
44	amount to credit		**** **

The net profit equals the balance less the margin deposited.

Note.—There is no interest charged on short sales, but it sometimes happens that a small bonus has to be paid for the use of the borrowed stock.

57. A broker sold "short" for me 400 sh. C. B. & Q., at 135<sup>3</sup>/<sub>4</sub>, and 100 sh. C. R. I. & P., at 132<sup>1</sup>/<sub>2</sub>. My "short" sale on C. B. & Q. was "covered" at 131<sup>1</sup>/<sub>2</sub>, and C. R. I. & P. at 133<sup>3</sup>/<sub>4</sub>. What was my net profit, usual brokerage? (No interest.)

58. Sold Aug. 11, 500 shares Chicago & Alton, s. 3, at  $94\frac{1}{2}$ , and covered my short sale Aug. 14, at 91. What was my profit, allowing the usual brokerage?

59. At what price may 6% bonds, maturing in 10 years, be purchased, so that the investment will pay 5%?

Note.—Tables have been constructed on various plans, and different methods are used by bankers and financiers, for the solution of problems relating to bond investments; two of which are given below.

ANALYSIS.—1. In the following method, it is presumed that the accruing interest is not reinvested, but that a sufficient part of it is set aside as a sinking fund to make up the amount which was originally paid out as premium.

A \$1000 bond in 10.years at 6% would amount to  $\$1600(\$1000+10 \times \$60)$ . \$1 in 10 years at 5% would amount to \$1.50. To amount to \$1600, the principal, or the amount paid for the bond, must be as many times \$1 as \$1.50 are contained times in \$1600, or \$1066.66 $\frac{2}{3}(106\frac{2}{3}\%)$ .

If a \$1000 bond is purchased at  $106\frac{2}{3}$ , it will be necessary to set aside as a sinking fund each year  $6.66\frac{2}{3}$  ( $\frac{2}{3}\%$ ) to make up the premium in 10 years. The annual interest, \$60, less  $86\frac{2}{3}$ , the annual sinking fund, is  $53\frac{1}{3}$ , which is 5% of \$1066\frac{2}{3}, the cost of the bond or the amount invested.

If the amount set aside as a sinking fund is placed at interest, either simple or compound, 6% bonds, maturing in 10 years and purchased at  $106\frac{2}{5}$ , would pay a little more than 5%.

2. The following method anticipates compound interest throughout; *i. e.*, the interest is immediately reinvested at compound interest.

The holder of a \$1000 bond would receive \$60 interest annually, and \$1000, the face of the bond, in 10 years. If money is worth 5%, the several interests in the 10 years at compound interest would amount to \$754.674 (\$1 placed at compound interest at the beginning of each year would amount in 9 years to \$11.5779 (**484**). \$11.5779 plus \$1 of the last interest = \$12.5779. \$60 would amount to 60 times \$12.5779, or \$754.674). \$1000, the principal, plus \$754.674, the compound amount of the interest, equals \$1754.674, the total value of the bond at maturity, money being worth 5%. The present worth of \$1754.64, due in 10 years, at 5% compound interest, is \$1754.64 + \$1.6289 (**483**), or \$1077.19. Hence the bonds must be purchased at  $1.07\frac{72}{100}$  to pay 5% on the investment. (See Ex. 41. Note.)

60. What must I pay for 6% bonds, maturing in 15 years, that my investment may yield  $3\frac{1}{2}\%$ ? (Both methods.)

61. 6% bonds, maturing in 10 years and bought at  $106\frac{2}{3}$ , pay what per cent. on the investment? (See 1st analysis, Ex. 59.)

ANALYSIS.—A \$1000 bond would amount in 10 years at 6% to \$1600. If \$1066.66 $\frac{2}{3}$  is paid for the bond, the net interest for 10 years is \$1600—\$1066.66 $\frac{2}{3}$ , or \$533.33 $\frac{1}{3}$ ; and for one year \$533.33 $\frac{1}{3}$ +10, or \$53.33 $\frac{1}{3}$ . An income of \$53.33 $\frac{1}{3}$ on an investment of \$1066.66 $\frac{2}{3}$  is equivalent to 5% (\$53.33 $\frac{1}{3}$  ÷ \$1066.66 $\frac{2}{3}$ ).

62. What rate of interest do I receive on my investment, if I buy 7% bonds maturing in 20 years at 1334?

## TAXES.

612. A Tax is a sum of money assessed on persons and property to defray the expenses of a State, county, town, corporation, or district.

1. In certain States all citizens above 21 years of age are required by law to pay a certain tax on the person. This tax is called a *Capitation* or *Poll Tax*.

2. The expenses of States, counties, towns, etc., are paid by a direct tax upon the property or polls of the same. The methods of assessing taxes differ in the several States. In some States, a certain percentage of the whole tax is assessed upon the polls, while in others the poll tax is a fixed amount for each citizen. In certain States, the whole tax is paid by the owners of the property of the same. In the States of New York, Pennsylvania, and some other: States, there is a direct tax levied upon certain corporations doing business in the State.

3. The expenses of the United States government are paid by duties on imports; the internal revenue (the tax upon distilled spirits, fermented liquors, tobacco, snuff, and cigars); sales of public lands; tax on circulation of national banks; customs fees, fines, penalties, and forfeitures; fees, consular, letters patent, and land; profits on coinage, etc.

613. Real Estate is fixed property; as land, houses, etc.

614. Personal Property is movable property, as money, stocks, bonds, mortgages, furniture, merchandise, etc.

**615.** An Assessor is a person appointed or elected to estimate the valuation of all property liable to taxation.

**616.** A Collector or Receiver of taxes is a person appointed or elected to collect or receive the taxes of a city, town, village, or district.

Collectors receive a commission on the amount collected or a fixed salary.

## EXAMPLES.

**617.** 1. For the fiscal year 1879, the N. Y. State tax levy was at the rate  $2\frac{863}{1000}$  mills. How much would this rate produce, the valuation of the taxable property being \$2,686,140,000?

2. The rate of taxation of a certain county was  $3\frac{1}{2}$  mills, and the amount of the tax \$40,653.48. What was the valuation of the property?

3. The following were the rates of taxation of New York for State purposes, 1880: — schools, 1.085 mills; general purposes, 1.475 mills; new capitol, .6 mills; canals, .34 mills. What was the total rate of taxation, and how much was raised by a county whose valuation was fixed by the State Board of Equalization at \$11,047,-534? How much was raised for school purposes?

4. Taxes were levied in a certain town for the following purposes :—support of poor, \$2,000; roads and bridges, \$500; accounts andited by town auditors, \$2,876.10; accounts audited by supervisors, \$19.48; county expenses, \$9,774.72 less a surplus of \$6,055.90 in the county treasury; state and school tax, \$15,079.88; surplus tax, \$868.98. What was the rate of taxation, the total valuation of the property, as made by the town assessors, being \$4,321,252? What was the tax of Mr. A., whose valuation was \$7,300?

Note.—To save labor in the calculation of taxes, a table similar to the following is usually prepared by the accountant.

7 8 9	6	5	4	3	2	1	0	
28 .0986 .1044 .110	.0928	.0870	.0812	.0754	.0696	.0638	.0580	1
$08 \left  .1566 \right  .1624 \left  .1682 \right $	.1508	.1450	.1392	.1334	.1276	.1218	.1160	2
88  .2146  .2204  .2262	.2088	.2030	.1972	.1914	.1856	.1798	.1740	3
68   .2726   .2784   .2842	.2668	.2610	.2552	.2494	.2436	.2378	.2320	4
48   .3306   .3364   .3422	.3248	.3190	.3132	.3074	.3016	.2958	.2900	5
28   .3886   .3944   .4002	.3828	.3770	.3712	.3654	.3596	.3538	.3480	6
$08 \left  .4466 \right  .4524 \left  .4582 \right  $	.4408	.4350	.4292	.4234	.4176	.4118	.4060	7
88 .5046 .5104 .5162	.4988	.4930	.4872	.4814	.4756	.4698	.4640	8
68.5626.5684.574	.5568	.5510	.5452	.5394	.5336	.5278	.5220	9
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	.2668 .3248 .3828 .4408 .4988 .5568	.2610 .3190 .3770 .4350 .4930 .5510	$\begin{array}{c} .2552\\ .3132\\ .3712\\ .4292\\ .4872\\ .5452\end{array}$	.2494 .3074 .3654 .4234 .4814 .5394	.2436 .3016 .3596 .4176 .4756 .5336	.2378 .2958 .3538 .4118 .4698 .5278	.2320 .2900 .3480 .4060 .4640 .5220	4 5 6 7 8 9

TAX TABLE.—Rate, 5.8 mills on \$1.

5. Find from the above table the tax on \$16750.

OPERATION. ANALYSIS .- By looking in the table opposite 1 and under 6, we find that the tax on Tax on \$16000 is \$92.80 \$16 is \$.0928, and by removing the point 3 " 750 " 4.35 places to the right, we find the tax on " 16750 " 97.15 \$16000 to be \$92.80. In the same manner, the tax on \$750 is found to be \$4.35. The tax on \$16750 is \$92.80 plus \$4.35, or \$97.15. 

6. How much was paid by Mr. B. on an assessment of \$6400, the collector charging a commission of 1% additional ? (Use table.)

7. Mr. D. being delinquent was charged 5% additional. How much was he obliged to pay on a valuation of \$9500 ?

8. What was the total tax, including commission of 1%, of Mr. C., whose real estate was assessed at \$24000, and personal property at \$15500 ?

Find the tax onFind the tax on9. \$7200 at 8.4 mills on \$1.13. \$248000 at \$2.131 on \$100.10. \$27500 at \$2.174 on \$100.14. \$14100 at \$16.476 on \$1000.11. \$4800 at \$21.871 on \$1000.15. \$240500 at \$0.889 on \$100.12. \$9600 at 6.8 mills on \$1.16. \$13500 at \$29.142 on \$1000.

17. A has 6 lots worth \$1200 each; B has 8 lots worth \$1500 each; and C has 10 lots worth \$1000 each. Divide a tax of \$1360 for street improvements between them.

18. A rate of \$6.34 on \$100 produces a tax of \$4216.10. What is the property assessed at ?

19. A pays \$17.25 more tax than B, their valuations being equal. Living in different towns, the rates of taxation are \$3.176 and \$3.291 on \$100 respectively. What is the valuation of their property?

20. The cost of a new school house was \$3800. What was the rate of the tax on \$100, the valuation of the district being \$325000?

21. If the assessor's valuation of certain property is 60% of its actual value, and the tax is  $2\frac{3}{4}\%$  of the assessment, the tax is what % of the actual value ?

22. In the City of Brooklyn, N. Y., the following is the rule regarding the payment of taxes :

Rebate at the rate of  $7\frac{2}{10}$ % per annum allowed on payments made during the month of December for the unexpired portion thereof. On all bills paid after Jan. 1, interest at the rate of 9% per annum will be added, to be computed from Dec. 1 to the date of payment.

According to the above rule, how much tax was paid Dec. 16, by Mr. A., the valuation of whose property was \$7500, the rate of tax being \$2.376 per \$100? How much was paid by Mr. B., on a valuation of \$12500, Mar. 26? (365 days to the year.)

23. What is the total tax on 8375 pounds tobacco at 8c., 4360 gallons distilled spirits at 70c., 2165 barrels beer at \$1?

## DUTIES.

**618.** Duties or Customs are taxes assessed by the Govern-. ment upon imported merchandise for the purpose of revenue for the support of the government and for the protection of home industry.

1. The waters and shores of the United States are divided into collection districts; in each of which there is a port of entry and one or more ports of delivery. Thus, the district of Boston and Charlestown comprises all the waters and shores within the counties of Middlesex, Suffolk, and Norfolk. Hingham, Weymouth, Cambridge, Roxbury, and Dorchester, the ports of delivery. All ports of entry are also ports of delivery.

2. The principal officer of every district is the collector, who is assisted by deputy-collectors, surveyors, appraisers, weighers, gaugers, inspectors, etc. The duties of the above vary in the several cohection districts and ports. There is also in the leading ports of entry, a "naval officer," whose department is a check upon that of the collector.

**619.** A Custom-House Broker is a person who makes entries, secures permits, and transacts other business at custom-houses for merchants. He is familiar with the tariff laws and the details and regulations of custom-house business, and usually acts under a power of attorney.

620. Duties are of two kinds, ad valorem and specific.

**621.** An Ad valorem Duty is a tax assessed at a certain per cent. on the dutiable value of the merchandise; as silks at 60%, watches at 25%, linens 30, 35 and 40\%, china 45 and 50\%.

1. The dutiable value of merchandise is its market value at the port of export, but not less than its invoiced cost, commission added, whether paid or not. There is no duty on the freight or transportation from the port of export. The appraised value is sometimes greater than the invoice value (623).

2. In reducing foreign money to U. S. money for the purpose of calculating duties, if the cents of the result are less than 50, they are rejected : if more than 50, \$1 is added to the dollars.

622. A Specific Duty is a tax assessed at a certain sum per ton, pound, foot, yard, gallon, or other weight or measure, without reference to the value; as leaf tobacco at 35¢ per pound, clay \$5 per ton, plate glass per square foot, brandy \$2 per proof gallon, lumber per M feet board measure, salt (in bulk) 8 cts. per 100 lbs., cotton goods per square yard.

1. Before specific duties are calculated, allowances are made for tare (the weight of the box, barrel, or cask), leakage (of liquids in barrels), and breakage (of liquids in bottles, usually 5%).

2. The U. S. Custom House ton contains 2240 lbs. (336, 3) the hundred-weight 112 lbs., and the quarter 28 lbs.

3. On certain goods, there is both a specific and an ad valorem duty (sometimes called a combined duty); as statuary marble, \$1 per cubic foot and 25%, woollen goods, 50 cts. per pound and 35%.

623. An Invoice (418) is a statement made by the seller or shipper of merchandise giving a description of the same, and showing marks, numbers, quantity, value, charges, and other details. (See Ex. 24, Art. 628.)

1. All invoices shall be made out in the weights and measures of the country from which the importation is made.

2. All invoices of merchandise subject to a duty ad valorem, shall be made out in the currency of the country or place from whence the importation is made.

3. When the value of the foreign currency is fixed by law (see Art. 566), the value is to be taken in estimating the duties; when the value is not fixed by law, the invoice must be accompanied by a consular certificate showing its value.

**624.** An **Appraiser** is an officer of the customs who examines imported merchandise and determines the dutiable value and the rate of duty of the same.

1. The place where the examinations are usually made is called the "Public Store."

2. One package of every invoice, and one package at least out of every ten similar packages, shall be sent to the public store for examination. Certain bulky and heavy articles are examined at the wharf where unloaded. Weighable and gaugeable goods on which the duties are specific, are not sent to the public store for examination.

3. When the appraised value of any merchandise subject to an ad valorem duty is 10% more than the invoice value as entered by the importer, then in addition to the duty imposed by law on the same, there shall be collected 20% of the duty imposed on the same.

625. A Bonded Warehouse is a place for the storage of merchandise on which the duties or taxes have not been paid.

1. If an importer does not desire to place his goods at once in the market, or anticipates exporting the same, by giving a bond for the payment of the duties and making the entry in the proper form, he may have the merchandise stored at his own risk in a bonded warehouse, and thus defer the payment of the duties.

2. Merchandise may be withdrawn from a bonded warehouse for exportation to Canada or other foreign country, without the payment of the duty on the same.

3. Merchandise is frequently sold "in bond" at prices which do not include the duty.

4. Merchandise that may be in warehouse under bond for more than one year, will be liable when withdrawn for 10% additional duty.

5. Any goods remaining in public store or bonded warehouse beyond three years shall be regarded as abandoned to the government, and sold under certain regulations and the proceeds paid into the Treasury.

**626.** Drawback.—When distilled spirits, fermented liquors and tobacco upon which an internal revenue tax has been paid, and foreign merchandise upon which an import duty has been paid, are exported, the tax or duty upon the same is refunded. Such return of the tax or duty is called a Drawback,

627. The Free List is a list of articles which are exempt from duty.

In making entries of free goods, the value as given in foreign money must be reduced to U. S. money (See Ex. 23, Art. **628**), permits must be obtained to land the goods, and certain packages are sent to the public store for examination.

#### EXAMPLES.

**628.** 1. A merchant imported from Lyons an invoice of silk, the dutiable value (**621**, 1) of which was 48765 francs. What was the dutiable value of the same in U. S. money, and what was the duty at 60% (**621**)?

Notes.-1. For foreign moneys of account and their values in United States money, see Art. 566.

2. 48765 francs at 19.3% = \*\*\*\*. (See Art. **621**, 2.) 60% of \*\*\*\* = \*\*\*\*\*.\*\*.

2. Find the duty on 1617 pounds of almonds, at 6 cts. per pound.

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#### DUTIES.

3. Find the total duty on 3 cases machinery, total value £23 7s. 4d. at 45%; 7 cwt. 0 qr. 14 lb. (622, 2) castings at 14c. per pound; 4 cwt. 0 qr. 26 lb. chain at  $2\frac{1}{2}c$ . per pound; and 3 cwt. 1 qr. 4 lb. chain at 2c. per pound.

4. An invoice of woollen cloth weighing 516 pounds, and valued at £327 16s., was imported from England. What was the duty at 50 cts. per pound and 35%?

5. An importer on making his entry at the custom-house, paid the duty on 38716 pounds (Invoice weight) of tobacco, at 35 cts. per pound. According to the return of the custom-house weigher, the net weight was 38472 pounds. How much of the duty was refunded when the entry was liquidated?

6. The duty on 28432 pounds of sugar was paid at the rate of  $2\frac{3}{4}$  cts. per pound. According to the weigher's return, the net weight was 28218 pounds. How much additional duty was collected, the appraiser having fixed the duty at  $3\frac{1}{4}$  cts. per pound?

7. What is the duty on an invoice of linens from Ireland, dutiable value  $\pounds 424$  15s. 6d., at 35%? Dutiable value  $\pounds 384$  14s. 9d., at 40%?

8. What is the duty on an invoice of porcelain vases from Paris at 50%, dutiable value 9843 francs? Dutiable value 7896 francs, at 40%?

9. Find the duty on 475 cu. ft. of statuary marble imported from Italy, dutiable value 16425 lire, at \$1 per cubic foot, and 25%.

10. What is the duty on 37420 pounds of pig iron at \$7 per ton (622, 2)?

11. Find the duty on an invoice of leather goods from Vienna, dutiable value 6429 florins, at 35%.

12. What is the duty on an importation of toys from Germany, dutiable value 8437 marks, at 50%? Dutiable value 7416 marks, at 45%?

13. What is the duty at 28 cents per sq. yd. and 35%, on 1248 yards of Brussels carpet, 27 in. wide, invoiced at 3s. 6d. per yard, shipping charges (less consul's fee) £2 16s. 9d.?

14. Find the duty on an importation from Canada of 5284 bushels of potatoes, invoiced at 45 *ets.* per bushel, and 37475 pounds of hay, invoiced at \$12.50 per ton (2000 *lbs.*), the duty on potatoes being 15 *ets.* per bushel, and on hay 20%.

16. The duty on burlaps is 30% ad valorem. What is the amount chargeable on a bale containing 50 webs, each being 54 yds. and 16 in. long, and 27 in. wide, and valued at 30 cents per sq. yd.?

17. What is the amount of duty chargeable on 2465 pounds of wool, valued at  $\pounds$ 171 8s., when the rate of duty is 10 cts. per pound and 11% ad valorem?

18. The duty on certain glass plates being 35 cents per sq. ft., find the duty on 316 boxes, each containing 20 plates, and each plate being 24 *in.* by 30 *in.* 

19. Find the duty at 25%, on one engraving, cost in London  $\pm$ 34 5s., case and shipping charges 15s., commission  $2\frac{1}{2}$ %.

20. What is the duty at \$1 per cu. ft. and 25%, on a block of marble  $2 \times 3 \times 7$  ft., imported from Italy, dutiable value 3450 lire?

21. Find the duty on 4175 *lbs.* cloves at 5¢ per *lb.*, 476 *lbs.* cinnamon at 20¢, and 5437 *lbs.* rice at  $2\frac{1}{2}\phi$ .

Make the extensions, find the dutiable value, and calculate the duty on the following invoices and accompanying entries:

22. Entry of merchandise, imported by TEFFT, WELLER & Co., from Berlin in the Str. "Silesia." Arrived Jan. 14, 1882. New York, Jan. 16, 1882.

Marks.	Nos.	Packages and Contents.		60%.
<b>T.W.</b>	351	One case half silk goods, Commission $2\frac{1}{2}\%$ ,	Rm.	2399.80 **.
$\sim$				**** **
		Rm. ****.** @ $23.8\phi = 60\%$ of **** = ****.		\$***.**

NOTE.—The following is an entry of free goods. Free goods are entered and the foreign monetary units reduced to U.S. money for statistical purposes in the same manner as dutiable goods.

23. Entry for consumption of merchandise, imported by W. H. SCHIEFFELIN & Co., in the Str. "Ailsa" from Savanilla, on the 10th day of January, 1882. New York, Jan. 12, 1882.

	Free.
33 bales Medicinal Bark,	2310.
Packing,	12.
Commission $2\frac{1}{2}\%$ ,	** **
(Pesos of U. S. of Columbia),	**** **
@ 82.3¢,	\$****.

24. Invoice of one package merchandise, purchased by GLAD-HILL & Co. for account of D. BUCKLEY & Co., New York, and forwarded for shipment to D. & C. MACIVER, Liverpool.

		±.	8.	<i>d</i> .
D. B.	4 Pieces Drab Cotton Pantaloon 32 in. wide, .			
207	$#1729 79 yd, \ldots \ldots \ldots \ldots$			
	30 80,		1	
	31 77 <del>1</del> ,			
	32 79, $315\frac{1}{2}$ (less $\frac{1}{37}$ ) 307 @ 2s. 2d.,	**	*	*
	$1\frac{1}{2}$ % discount,		**	
	and the second sec	**	**	*
	Verification and Commissioner's fee, .		14	10
	$2\frac{1}{2}\%$ Commission,		16	5
		**	*	*
	Less Consul's Certificate (not dutiable),		14	10
		33	11	7

Entry of merchandise, imported by D. BUCKLEY & Co. in the Str. "Catalonia" from Liverpool. New York, Jan. 12, 1882.

				35%.
D. B.	One case cotton,			33-11-7
207	@ 4.8665			\$***.
	Duty 35% of \$***	=	<b>***</b> .**	)

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### DUTIES.

25. Invoice of 700 bales leaf tobacco shipped by F. B. DEL RIO & Co., per Str. "Niagara" for New York, and consigned to FREDERICK DE BARY & Co.

F. B.	700 bales 83077 lbs. (See page 343, Spain)						\$35000	
	Сна	RGE	s.					
3328/4027	Baling,					\$525.		
	Export duties, .					3407.39		
	Consul fee,		•			2.75		
-	Small charges, .	•	•			49	****	**
							****	**
	Commission	21/2	6,				***	**
	Spanish gold	1,	•				\$****	**

HAVANA, Dec. 27, 1881.

Custom House, New York, Collector's Office, Jan. 4, 1882. Bond No. 9817.

Entry of merchandise, imported on the third day of January, 1882, by FREDERICK DE BARY & Co., in the Str. "Niagara" from Havana.

Marks.	Nos.	Packages and Contents.	35c.	
<b>F.</b> B.	<u>\$828</u> 4027	700 bales Leaf Tobacco,	84240 768.	\$39958.74 @.93,2= \$*****.

26. What is the duty on an invoice of crockery invoiced at £1275 16s. 6d. f. o. b. (free on board), at 40%?

27. What is the duty on 28916 pounds of steel rails at  $1\frac{1}{4}$  per pound, and 11438 pounds of tin plates at  $1\frac{1}{10}$  per pound?

28. The duty on spool thread of cotton, containing 100 yds. to the spool, is  $6\phi$  per dozen spools and in addition thereto 30% ad valorem. What is the duty on 11160 spools valued at  $3\phi$  a spool?

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## PARTNERSHIP.

**629.** Partnership is the association of two or more persons who join their capital and services for the purpose of conducting business, the gains or losses being shared in such proportion as may be stipulated in the agreement.

The business association is called a Firm, House, or Company; and each individual of the association is called a Partner.

**630.** A Special Partner is one who takes no active part in the business, and whose liability is limited to the amount of his investment. In order to thus limit his liability, the amount of his investment must be duly advertised, and he must take no active part in the business.

The partners who conduct the business are called **General Partners.** Their private property is liable for the debts of the partnership.

631. The Capital or Capital Stock is the money or other property which is invested in a business.

The partners' accounts are used to show the amounts invested.

In most firms, the investments are entered in the partners' "stock accounts," and the amounts withdrawn by the partners during the year and their salaries are entered in their "private accounts."

632. A Resource or Asset is any kind of property belonging to the concern having a financial value.

633. A Liability is a debt owing by the concern.

634. The Net Worth of a concern is the excess of its resources over its outside liabilities.

**635.** The **Net Insolvency** of a concern is the excess of its outside liabilities over its resources. The concern being unable to pay its debts in full, it is said to be insolvent.
636. Gains or Losses, how shared.—In most partnerships, the gains or the losses are divided according to certain fractions or percentages; the inequalities of the investments are adjusted by allowing interest upon the same; and the partners receive salaries for their services rendered. (See Ex. 36, Art. 639.) Sometimes the net gain or net loss is shared in proportion to the investments (Ex. 13, Art. 639), or the average investments. (Ex. 17, Art. 639.) In joint stock companies the gains (dividends) and the losses (assessments) are shared in proportion to the investments or the amounts of stock held.

**637.** Gains or Losses, how found.—When the books have been kept by "Single entry," and when no books have been kept, the gain is found by subtracting the net worth (**634**) at commencing, or the investment, from the net worth at closing; and the loss, *vice versa*.

When the books have been kept by "Double entry," the gain may be found as above, or by subtracting the sum of the separate losses from the sum of the separate gains. The results by the two methods should be the same and should prove each other.

#### EXERCISES.

638. In the following exercises find the gain or the loss :

1. Capital at commencing, \$5000; capital at closing, \$3000.

2. Capital at commencing, \$5000; capital at closing, \$8000.

3. Capital at commencing, \$5000; insolvency at closing, \$1000.

4. Capital at commencing, \$5000; insolvency at closing, \$7000.

5. Insolvency at commencing, \$5000; capital at closing, \$2000.

6. Insolvency at commencing, \$5000; capital at closing, \$6000.

7. Insolvency at commencing, \$5000; insolvency at closing, \$4000.

8. Insolvency at commencing, \$5000; insolvency at closing, \$9000.

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Find the capital or the insolvency at closing :

9. Capital at commencing, \$5000; gain during the year, \$3000.

10. Capital at commencing, \$5000; gain during the year, \$6000.

11. Capital at commencing, \$5000; loss during the year, \$2000.

12. Capital at commencing, \$5000; loss during the year, \$8000.

13. Insolvency at commencing, \$5000; gain during the year, \$1000.

14. Insolvency at commencing, \$5000; gain during the year, \$7000.

15. Insolvency at commencing, \$5000; loss during the year, \$4000.

16. Insolvency at commencing, \$5000; loss during the year, \$9000.

Find the capital or the insolvency at commencing :

Capital at closing, \$5000; gain during the year, \$3000.
 Capital at closing, \$5000; gain during the year, \$6000.
 Capital at closing, \$5000; loss during the year, \$4000.
 Capital at closing, \$5000; loss during the year, \$4000.
 Capital at closing, \$5000; gain during the year, \$4000.
 Capital at closing, \$5000; gain during the year, \$4100.
 Capital at closing, \$3700; gain during the year, \$4100.
 Capital at closing, \$5000; gain during the year, \$4100.
 Insolvency at closing, \$5000; gain during the year, \$1000.
 Insolvency at closing, \$5000; gain during the year, \$8000.
 Insolvency at closing, \$5000; loss during the year, \$2000.
 Insolvency at closing, \$5000; loss during the year, \$2000.

#### EXAMPLES.

639. 1. A and B are partners, A sharing  $\frac{2}{3}$  of the gain or loss and B  $\frac{1}{3}$ . A invests \$5000, and B \$2350. At the end of the year their resources and liabilities are as follows : merchandise on hand, per inventory, \$2000; real estate, \$7000; cash on hand and in bank, \$1532; due on personal accounts, \$1640.25; notes on hand, \$1000; notes outstanding, \$800; owing by the concern to sundry persons, \$4471.69. What is the amount of net resources belonging to each partner?

# FIRST OPERATION.

R	LES	OURCES.		
Merchandise on hand,			\$2000	
Real estate,			7000	
Cash on hand, .			1532	
Personal accounts,			1640.25	
Bills receivable, .	•		1000	\$13172.25

#### LIABILITIES.

Bills payable,	\$80	00	
Personal accounts, .	447	1.69	5271.69
Present worth,			\$7900.56
Investments (subtracted),			7350.
Total net gain,			\$550.56

 $\frac{2}{3}$  of \$550.56 = \$367.04, A's share of the gain.  $\frac{1}{3}$  of \$550.56 = 183.52, B's share of the gain.

A's investment,	. \$5000	B's investment, .	\$2350.
Plus his gain,	. 367.04	Plus his gain, .	183.52
A's present worth,	\$5367.04	B's present worth,	\$2533.52
AFOR 01 . 60500			

\$5367.04 + \$2533.52 = \$7900.56, total present worth, as above.

# SECOND OPERATION.

ANALYSIS.—Theoretically, all the resources of a business belong to the creditors and the partners (proprietors), the partners' investments being regarded as liabilities ; hence, the resources and liabilities—including the partners' accounts—should be equal. If, in a statement of the condition of a business, the resources and liabilities thus considered should not be equal, it is evident that the partners' accounts do not show their true interests, and the inference is that a gain or loss has occurred which has not been entered to their accounts. The excess of resources over liabilities would in such case show the gain, as would the excess of liabilities over resources show the loss. In order to restore the equilibrium, the gain should be credited or the loss debited to the partners' accounts.

## 1. STATEMENT BEFORE ADJUSTING PARTNERS' ACCOUNTS.

R	ESOU	RCES		LIABI	LITIES	5.	
Merchandise,			2000	Bills payable, .			800
Real estate,			7000	Personal accounts,			4471.69
Cash, .			1532	A's investment,			5000
Personal account	nts,		1640.25	B's do.			2350
Bills receivable	,		1000				12621.69
			13172.25				
			12621.69				
							0

Excess of resources (net gain). 550.56 | A's  $\frac{2}{5}$ , \$367.04; B's  $\frac{1}{5}$ , \$183.52.

Resou	RCE	s.		LIABILITIES.				
Merchandise, . Real estate, . Cash, Personal accounts, Bills receivable,	•	• • • •	$\begin{array}{r} 2000\\ 7000\\ 1532\\ 1640.25\\ 1000\\ \overline{13172.25} \end{array}$	Bills payable Personal acc A's investme B's do.	, ounts, . nt and gain do.	$ \begin{array}{r} 806 \\ 4471.69 \\ 5367.04 \\ 2533.52 \\ \hline 13172.25 \\ \end{array} $		

2. STATEMENT AFTER ADJUSTING PARTNERS' ACCOUNTS. Resources Liabilities.

2. A and B are partners, A sharing  $\frac{2}{3}$  of the gain or loss and B  $\frac{1}{3}$ . A invested \$5000, and B \$2350. During the year the concern gained on merchandise, \$955.56; on real estate, \$315. The expense account showed a loss of \$675; the interest account, \$45. What was the net gain, and the balance of each partner's account.

Note.—The above example is the complement of Ex. 1. The books having been kept by double entry, the separate gains and losses are given, and the net gain thus found. The loss and gain account and the partners' accounts are shown in the following operation in "skeleton ledger" form.



3. A and B started in business July 1, 1881. Each put into the concern \$2200. The resources on Jan. 1, 1882, were as follows: goods, \$4000; bills receivable, \$1500. The liabilities were \$580. A has drawn out cash, \$3000; and B, \$2000. How much is due each partner, the gain or loss being divided equally?

Notes.—1. It must be borne in mind that the amounts drawn out by the partners are as fully resources of the business as if charged to an outside party.

2. In examples 3, 4, 5, and 7, open accounts with the partners and make statements of resources and liabilities.

OPERATION.

4. A and B are partners. They have cash and notes on hand to the amount of \$6475.28. A has drawn from the concern \$2478.30, and B has drawn \$1016.48. A invested \$4287.46, and B, \$1037.75. The firm owes sundry persons \$5016.82. What is each partner's present interest in the concern, if they share equally in gains and losses ?

5. On Jan. 1, my brother and I started a business in which I invested \$900, and he \$400. We now propose to separate, and the business stands as follows: stock in store \$1800; cash on hand and in bank, \$1200; outstanding accounts, considered good, \$1200. According to the agreement, I am entitled to  $\frac{2}{3}$  of the net gain, and my brother  $\frac{1}{3}$ . During the time of the copartnership, I have drawn \$4000 and he, \$2800. Of the assets given above, how much are we each entitled to ?

6. C, D, and E are partners, each investing \$10000, and each to share  $\frac{1}{3}$  of the gain or loss. The resources and liabilities at the close of business are found to be as follows, viz.: Merchandise on hand, per inventory, \$8159.50; cash on hand, \$5012.88; personal accounts due the firm, \$4235; notes and accepted drafts (bills receivable) on hand, \$5000; real estate, \$8000; bonds and stocks, \$12000; owing by the firm to sundry persons, \$5505; firm's notes outstanding (bills payable), \$3000. C has withdrawn during the year \$1247.87; D, \$1400; and E, \$1489. What is each partner's interest in the concern at closing ?

7. C, D, and E are partners, sharing the gains and losses equally. C's net investment was \$8752.13; D's, \$8600; and E's \$8511. During the year the firm's gains were as follows: Merchandise, \$8529; stocks and bonds, \$650; interest, \$985.25. The cost of conducting the business was \$2125. What was each partner's interest at closing? (See Ex. 2.)

8. M and N are partners, M sharing  $\frac{3}{4}$  of the gain or loss and N  $\frac{1}{4}$ . M invested \$15000 and N \$5000. At the close of the business year, the resources and liabilities of the concern are as follows: cash on hand, \$2128; bills payable, \$4000; bills receivable, \$3000; the firm owes sundry persons, \$8375; due the firm from sundry persons, \$16427; rent paid in advance, \$375; mortgage held by the concern on the property of A. G. Pope, \$5000; accrued interest on the same, \$150; store fixtures valued at \$835; merchandise on hand, \$9416; accrued interest on firm's notes outstanding, \$112; accrued interest on notes held by the firm, \$75.

M has withdrawn \$2465; and N, \$2275. According to the agreement, each partner is to receive a salary of \$2500. What are the separate interests at the close of the business ?

9. A owns a business, the good will of which is estimated at \$10000, and the stock on hand at \$15000. B and C agree tc unite with him on the following conditions: B to invest \$25000 cash, and C to devote his entire time to the business, for which he is to receive, in addition to his interest, an annual salary of \$1000. The capital is to be kept intact, and no interest to be allowed therefor. The gain or loss to be divided equally between the three partners. At the end of the year the resources, including amounts drawn by the partners, amount to \$67000, and the liabilities to outside parties, to \$10500. C has drawn out during the year \$2500; B, \$1575; A, \$2000. Of the resources above named there are bad debts not to be counted, amounting to \$575. What is the condition of each partner's account?

10. A and B are partners, A investing  $\frac{2}{3}$  of the capital, and B  $\frac{1}{3}$ ; the gains or losses to be shared in the same proportion. The following is an exhibit of the business, excepting the partners' accounts, at the close of a certain period : *Resources*, cash, \$3775; Stone & Co., \$150; A. R. Mead, \$1200; bills receivable, \$5500; interest on the same, \$125; merchandise, \$5140. *Liabilities*, L. Blair, \$500; W. H. Rice, \$723; Martens & Bultman, \$517.64; bills payable, \$3300; interest on the same, \$169. The net gain during the year was \$3174. What was each partner's original investment?

11. Upon a close valuation of the personal accounts due the firm in the preceding example, the partners are convinced that Stone & Co.'s is worth no more than 50% of its face; and A. R. Mead's, 25% of its face. Upon this valuation what would be the gain, and what the condition of the partners' accounts at closing ?

12. A, B, and C are partners, A investing \$25000 capital, B \$5000, and C nothing. The proportionate interests are : A 60%, B 25%, C 15%. At the expiration of the term of copartnership, and after the gains and losses have been adjusted, A's credit of capital stands intact, B has a credit of only \$1000, while C has overdrawn his account \$8534. C being insolvent, how much must B pay into the concern to adjust his share of the loss ?

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13. A and B are partners in business, the gain or loss to be divided in proportion to investment. A invested \$8750; B invested \$4000. The net gain is \$2726.15. What is each partner's share?

# FIRST OPERATION.-FRACTIONAL METHOD.

ANALYSIS.—Since A's investment, \$8750, is  $\frac{87750}{127750}$  of the total investment, he is entitled to  $\frac{8750}{12750}$  of the gain ; and for a similar reason, B is entitled to  $\frac{4000}{12750}$  of the gain.

> $\frac{8760}{127560} = \frac{85}{51}$ ;  $\frac{85}{51}$  of \$2726.15 = \$1870.89, A's gain.  $\frac{4000}{12760} = \frac{1}{51}$ ;  $\frac{1}{51}$  of \$2726.15 = \$855.26, B's gain.

SECOND OPERATION.-BY PROPORTION.

ANALYSIS.—The total investment is to each partner's investment as the total gain is to each partner's gain.

\$12750: \$8750: \$2726.15: \$1870.89, A's gain. \$12750: \$4000:: \$2726.15: \$855.26, B's gain.

Note.—Cancel any factor common to the given extreme and either of the means.

THIRD OPERATION.—BY PERCENTAGE.

ANALYSIS.—\$2226.15, the gain, is 21.3816% of \$12750, the total investment. The partners' gains are therefore 21.3816% of their respective investments.

> 21.3816% of \$8750 = \$1870.89, A's gain. 21.3816% of \$4000 = \$855.26, B's gain.

Note.—In order to produce exact results by this method, it is necessary to extend the number expressing the rate per cent. of the gain or loss to several decimal places.

14. E, F, G, and H enter into a joint speculation. E advances \$5000, F \$7000, G \$8000, and H \$10000, the gain or loss to be divided according to investment. They gain \$14285. What is the share of each?

15. Four merchants ship goods on joint account. A puts in \$6000, B \$5500, C \$4200, and D \$4800. What will be each man's share, if the gain is \$9200 ?

16. Five persons having claims against the government, placed their claims in the hands of an agent for collection. A's claim amounted to \$500, B's to \$425, C's to \$300, D's to \$250, and E's to \$175; but, after the agent had deducted his fees, there remained only \$1237.50. How much did each claimant receive ?

17. A and B are partners, gain or loss to be divided in proportion to average investment. A invests, Jan. 1, \$4000; Mar. 1, \$2000; Oct. 1, \$3000; and withdraws July 1, \$1500; Dec. 1, \$1000. B invests, Jan. 1, \$6000; Sept. 1, \$3000. They close their books Jan. 1 of the following year and find they have gained \$3456. What is each partner's share?

NOTE.—An Average Investment is an investment for a certain period of time equivalent to several investments for different periods of time.

		OPERAT	ION	τ.			
A invested	Jan. 1,	\$4000	×	12	=	\$48000	
66	Mar. 1,	2000	×	10	_	20000	
66	Oct. 1,	3000	×	3		9000	77000
A withdrew	July 1,	1500	×	6	=	9000	
66	Dec. 1,	1000	×	1	=	1000	10000
A's average	investment	t for 1	mo	onth	L,		67000
		Or,					
A invested	Jan. 1,	\$4000	×	2	=	\$8000	•
66	Mar. 1,	2000					
		6000	×	4	=	24000	
withdrew	July 1	1500					
		4500	×	3	=	19500	
invested	Oct. 1,	3000					
		7500	×	2	=	15000	
withdrew	Dec. 1,	1000					
		6500	×	1	=	6500	
A'a attora	invoctmont	for 1	mo	nth		\$67000	

A's average investment for 1 month, \$67000

ANALYSIS.—By the first operation, we suppose each investment to be made for the remainder of the time. To find the average investment, multiply each investment and withdrawal by the interval between its date and time of settlement. Subtract the products obtained from the withdrawals from the products obtained from the investments. The remainder will be the average investment for 1 month, if the time is found in months. A's investment of Jan. 1 is in the business 12 months (Jan. 1 to Jan. 1); the use of \$4000 for 12 months is equivalent to the use of \$48000 for 1 month. Treating the other investments in like manner, we find A's total investments are equivalent to \$77000 for 1 month. A's withdrawals are equivalent to \$10000 for 1 month. A's net average investment is therefore equivalent to \$67000 for 1 month.

By the second operation, we find the actual amount in the business for each month of the year. Jan. 1, A invested \$4000, which was in the business until Mar. 1, or for 2 months. Mar. 1, he added \$2000, making his total investment \$6000, which was in the business until July 1, or for 4 months. July 1, he withdrew \$1500, leaving in the business \$4500 until Oct. 1, or 3 months, etc. The several net investments as found in this manner are equivalent to \$67000 for 1 month.

B's average investment, as found by either of the above methods, is \$84000 for 1 month.

A's average investment for the year is  $5583.33\frac{1}{3}$ ; and B's \$7000. To avoid fractions, divide the gain in proportion to the average investments for 1 month. After the average investments are found for a common time, the gain may be divided according to either of the methods under Ex. 15. By the fractional method, A would be entitled to  $\frac{157}{151}$  of the gain, and B to  $\frac{87}{151}$ .

18. C and D are partners, gain or loss to be divided in proportion to average investment. C puts in \$6000 for one year, and \$7000 for one and a half years; D puts in \$6000 for two and a half years. The net loss is \$1565.40. What is each one's share?

19. A, B, and C are partners. A puts into the concern \$3000, but withdraws half of it at the end of 6 months; B puts in \$2000, and adds \$500 to it at the end of 4 months; C puts in \$2500 for the whole year. The gain during the year is \$1700. What is each one's share?

20. Three contractors agree to build a road for \$10000. A has 25 men at work for 16 days and 30 men for 34 days. B has 40 men for 10 days and 45 men for 40 days. C has 48 men for 50 days. C receives \$200 extra for superintending the work. How much is each contractor entitled to ?

21. J, K, and L are partners, gain or loss to be divided according to average investment. J invests as follows: Jan. 1, \$6000; Apr. 1, \$4000; K invests, Jan. 1, \$8000; L invests, Jan. 1, \$7000; Apr. 16, \$2500; and draws out June 16, \$3500. At the end of the year the net gain is found to be \$4135.60. What is each partner's share ? (Time by Compound Subtraction.)

22. A, B, C, and D were partners for two years. When the firm commenced business, A's investment was \$6000, B's \$3500, C's \$2800, and D's \$1700. At the end of 8 months, A withdrew \$3000. At the end of 10 months, D added \$1300 to his former investment. At the end of one year, B withdrew \$800. At the close of the two years, they had gained \$4727. What was each partner's share of the gain?

23. A and B are partners for one year, the gain or loss being divided in proportion to their average investments. A invested, Jan. 1, \$8000; June 16, \$1500; Aug. 1, \$2500; and drew out

May 1, \$1500. B invested Jan. 1, \$10000; Apr. 1, \$500; and withdrew Aug. 16, \$2500. How much should A invest Sept. 1 to entitle him to one-half the gain?

24. C and D are partners. According to agreement C is to share  $\frac{3}{4}$  of the gain or loss, and D  $\frac{1}{4}$ . At the end of the year, D desires to increase his investment so that he will be entitled to a  $\frac{1}{2}$  interest. How much must D invest, the partners' accounts after the books are closed being as follows: C's debit, \$6712.38; C's credit, \$27000; D's credit, \$9000?

25. R, S, T, and U enter into copartnership with equal capital, upon the following conditions: R to receive as a salary \$2000; S, \$1500; T, \$1200; and U, \$1000; the gain or loss to be divided equally. At the close of the year, the net gain, exclusive of salaries, proves to be \$5400. To how much of this amount is each entitled ?

Note.—The excess of the salaries (losses) over the gain is the net loss to the business, and should be charged equally to the partners.

26. X, Y, and Z commence business without capital. According to the partnership contract, X is to receive a salary of \$3000; Y, \$2500; and Z, \$2000; the gain or loss to be divided equally. During the year, X withdraws \$3000; Y, \$2800; and Z, \$1800. What is the balance due each partner, if the gain, without taking into account the partners' salaries, is \$9000?

27. A merchant's assets are \$12000, and he owes A \$1900, B \$5000, C \$3000, and D \$6100. As he is unable to pay his debts in full, he is compelled to make an assignment for the benefit of his creditors. If the expense of making the settlement is \$1600, what % of his indebtedness can he pay ? What amount will each creditor receive ?

28. A and B failed in business. Their liabilities were \$64000. The firm's assets amounted to 37500. If the assignee's fees and other expenses were \$2300, what % of their indebtedness can they pay? What will C receive, whose claim is \$16400?

29. D and E have made an assignment. They owe F \$4200, G \$16000, H \$2500, and K \$11800. Their assets amount to \$25400, and the expense of making the settlement was \$1630. G being a preferred creditor, what % will be paid to the other creditors, and what amount will each receive?

Note.—A preferred creditor is one who is paid in full, before any dividend is paid to the other creditors.

30. A lot, whose front is 240 feet, and whose depth is 100 feet, is bought by A, B and C, who pay respectively \$3000, \$4000, and \$5000. How many feet front is each entitled to, if it is divided in proportion to their investments?

31. M, the owner of a mill, employs S, a miller, under the following conditions : M is to furnish the requisite capital, and S to receive, in lieu of salary,  $\frac{1}{3}$  of the profits. M has a store connected with the mill, on the books of which are entered all time sales of mill products. The grain, etc., for the mill is furnished by M. At the beginning of the year the value of the grain, flour, feed, etc. is \$1727. During the year M's purchases for the mill amount to \$19275. S has received for cash sales \$16337, of which he has paid over to M \$15550. The sales on account, as shown on M's books, amount to \$8375; and the value of the products on hand is \$2828. During the year S has purchased goods at M's store to the amount of \$837.65. How much is owing to S at the expiration of the year ?

32. P and Q are partners, each to receive interest on his net investment at the rate of 6% per annum, and the net gain or loss to be divided equally. P invests, Jan. 1, \$5000; Mar. 1, \$4000; June 16, \$1500; and draws out Apr. 16, \$2500. Q invests, Jan. 1, \$8000; Sept. 16, 2000; and draws out June 1, \$1500; Nov. 11, \$500. At the close of the year the net gain is found to be \$4475.25, without taking into account the interest on the partners' accounts. What is the amount due each partner after the gain is adjusted? (Time by Compound Subtraction.)

Note.-Open accounts with P, Q, and Loss and Gain.

33. A and B have been doing business as partners, A sharing 3 and B 3 of the gains and losses. A invested \$4500, average date Mar. 25, 1882; and drew out \$2700, average date Sept. 12, 1882. B invested \$7200, average date June 17, 1882; and drew out \$3750, average date Oct. 25, 1882. At the time of their dissolution, Jan. 1, 1883, the debts of the firm were all paid and they had on hand belonging to the firm \$8750 in cash. How shall the money be divided, each being allowed interest at 6% on his investment and charged with interest at the same rate on the amounts drawn? (Exact days. Interest 360 days to the year.)

Note.—In Examples 33 and 34, open accounts with A and B, and make statements of Resources and Liabilities.

34. A and B are partners, A having  $\frac{3}{5}$  and B  $\frac{3}{5}$  interest. A advanced in business \$12000, average date Jan. 12, 1883; and drew out \$1265, average date Oct. 20, 1883. B advanced \$7500, average date Apr. 5, 1883; and drew out \$2560, average date Nov. 25, 1883. Jan. 1, 1884, the assets are as follows: Cash, \$5800; merchandise, \$6250; notes on hand, \$7300; accrued interest on the same, \$387.14; personal accounts, \$5700. The liabilities are as follows: Notes outstanding, \$4200; accrued interest on the same, \$227.65; personal accounts, \$2500. Find the balance of each partner's account, 5% of the personal accounts being considered uncollectible, and interest being reckoned on the partners' accounts at 6% per annum (365 days to the year).

35. A, B, and C form a copartnership under the following conditions: A is to manage the business, and to receive therefor \$2400 per annum, which amount is to be credited as July 1. He is to receive interest on his salary and to pay interest on sums withdrawn at the rate of 6% per annum. B and C are to furnish the capital, and to receive interest therefor at the rate of 6% per annum. The net gain or loss to be divided equally. B invests, Jan. 1, \$10000; Apr. 1, \$5000. C invests, Jan. 1, \$10000; July 1, \$5000; and draws out Sept. 16, \$500. A draws out, Feb. 1, \$200; Mar. 1, \$400; July 11, \$500; Oct. 1, \$200; Nov. 21, \$100. At the end of the year, the gain—without taking into account either the salary to be paid to A or the interest on the partners' accounts—is \$8437.16. What will be the balance of each partner's account, when all the items have been properly entered ?

Note.—In Examples 35 and 36 open accounts with the partners and with Loss and Gain.

36. A, B, and C are partners, A sharing  $\frac{2}{5}$  of the gain or loss, B  $\frac{2}{5}$ , and C  $\frac{1}{5}$ . Interest is to be reckoned at the rate of 6% per annum (365 days to the year) on the partners' accounts, and each partner is to receive a salary of \$1800, to be credited as July 1. A invested, Jan. 1, \$16000; and withdrew during the year \$4875, average date, Aug. 21. B invested, Jan. 1, \$20000; and withdrew \$6224, average date, June 18. C invested, Jan. 1, \$5000; and withdrew \$2625, average date, July 31. Jan. 1, of the following year, the merchandise account shows a gain of \$18437.16; the interest account (not including the interest on the partners' accounts) a gain of \$586.38; sundry consignment accounts show a net gain of \$1287.14. The expense account (not including the partners' salaries) shows a loss of \$3424.75. What is each partner's interest in the business at closing? How will A be affected if each partner's salary is increased to \$2500?

37. A and B unite in conducting a summer hotel, on the following basis: 1. Each is to receive interest at the rate of 6% per annum on his investment; 2. A is to receive a salary of \$1000 and B of \$800 for the season; 3. The profit or loss of the general business is to be divided in the proportion of A  $\frac{2}{3}$ , B  $\frac{1}{3}$ ; the profit or loss of the livery business attached thereto in the proportion of A  $\frac{1}{3}$ , B  $\frac{2}{3}$ ; the profit or loss of the bathing business in the proportion of A  $\frac{1}{2}$ , B  $\frac{1}{2}$ . A invests an average of \$10150 for four months, and B an average of \$6750 for the same time. At the close of the business the accounts showing loss and gain stand as follows:

Outgo.	HOTEL.	Income.	Outgo.	LIVERY. I	acome.
15150.	75   2	5175.19	1592.	.75 327	9.50
		Outgo. BAT	HING. Income.		
		759.12	1275.30		

There is besides an item of service amounting to \$375, which at the time could not be easily apportioned in the charges, and which does not appear in the above outgoes. It is agreed that this item, as also the sums severally due the partners for interest and salaries, shall be charged to the several departments of the business in proportion to the net gains. There is, also, an inventory in the livery business amounting to \$429.33. How much gain from all sources will each partner get out of the business?

38. A, B, and C are equal partners in a mill, each to receive 6% per annum interest on his average investment. C is to superintend the business and receive therefor a yearly salary of \$3000; B keeps a store at which the operatives trade, and is to pay to A and C 5% on sales to operatives. A negotiates the products of the mill, for which he is allowed 10% on the net profits as existing before his percentage is taken. A's average investment for the year is \$9750; B's \$5750; C's \$5000. Leaving out the interest, salary and percentages, the net gain for the year is \$15000. B's sales to operatives amount to \$1575. What share of the \$15000 is each partner entitled to ?

# NATIONAL BANKS.

**640.** A National Bank is a bank organized under the laws of, and chartered by, the United States.

1. National banks are authorized to discount and negotiate notes, drafts, etc.; to receive deposits; to buy and sell exchange, coin and bullion; to loan money on personal security; and to issue circulating notes.

2. National banks are prohibited from making loans on real estate or on security of their own shares of capital except to secure debts previously contracted.

Real Estate purchased or mortgaged to secure a pre-existing debt shall not be held for a longer period than five years.

They are also prohibited from making loans to one person or association, excepting on business paper representing actually existing value as security, in excess of one-tenth of the capital of the bank.

3. The stockholders of a national bank are individually liable (equally and ratably, and not one for another) for an amount equal to the par value of the capital stock held by them.

**641.** Circulation. Upon a deposit of registered bonds, the association making the same shall be entitled to receive from the Comptroller of the Currency circulating notes of different denominations (**120**) equal in amount to 90% of the current market value, not exceeding par, of the United States bonds so transferred and delivered, and at no time shall the total amount of such notes issued to any association exceed 90% of the amount at such time actually paid in of its capital stock.

1. Any national bank desiring to decrease its circulation, in whole or in part, may deposit lawful money (specie or legal tenders) with the Treasurer of the United States in sums of not less than \$9,000, and withdraw a proportionate amount of bonds held as security for such notes.

No national bank which makes any deposit of lawful money in order to withdraw its circulating notes, shall be entitled to receive any increase of its circulation for the period of six months from the time it made such deposit. Not more than \$3,000,000 shall be deposited during any calendar month for this purpose.

2. The State bank circulation wholly ceased after Congress had imposed a penalty of 10% in the form of a tax every time it should be issued. This act took effect Aug. 1, 1866.

#### Art. 642.]

**642.** Redemption.—The circulating notes of national banks are redeemed in lawful money by the banks which issued them and by the Treasurer of the United States at Washington, D. C.

1. Every national bank shall, at all times, keep and have on deposit in the Treasury of the United States in lawful money of the United States, a sum equal to 5% of its circulation, to be held and used for the redemption of such circulation.

2. All national banks which go into voluntary liquidation shall, within six months thereafter, deposit in the Treasury an amount of lawful money equal to the amount of their circulating notes outstanding. The law also requires that full provision shall be made for the redemption of the circulating notes of any insolvent bank before a dividend is made to its creditors. Thus it will be seen that no association can close up its business without first providing for the payment of all its circulating notes, and that the amount deposited for their redemption must remain in the Treasury until the last outstanding note shall have been presented. It is therefore plain that the government, and not the bank, receives all the benefit arising from lost or unredeemed circulating notes.

**643.** Reserve.—The national banks in the reserve cities \* are required by law to hold a lawful money reserve of 25% of their deposits; all other national banks 15%. The excess above legal requirements is called "surplus reserve."

**644.** Surplus Fund.—The law provides that a surplus fund shall be accumulated, by setting aside, before the usual semiannual dividend is declared, one-tenth part of the net profits of the bank for the preceding half-year, until the surplus fund shall amount to 20% of its capital stock.

#### EXAMPLES.

**645.** 1. The impairment of the capital stock (\$300000) of an insolvent national bank was \$216000. What was the rate per cent. of the assessment made upon the stockholders for the purpose of making good the deficiency (**640**, 3)? How much was Mr. A. obliged to pay, who owned 80 shares?

2. What amount of bank notes is issued to a national bank that deposits \$780000 in U. S. bonds to secure circulation (641)? How much is its redemption fund (642, 1)?

<sup>\*</sup> The reserve cities are New York, Boston, Philadelphia, Baltimore, Albany, Pittsburgh, Washington, New Orleans, Louisville, Cincinnati, Cleveland, Chicago, Detroit, Milwaukee, Saint Louis, and San Francisco.

3. A national bank, desiring to reduce its circulation, deposits with the Treasurer of the United States \$27000 in legal-tenders, and sells the bonds withdrawn (641) in the market at  $118\frac{3}{4}$ . What were the proceeds?

4. The circulation of a national bank having a capital of \$150000 is \$57600; what is the remaining amount of circulation which it may call for by depositing the necessary amount of bonds (641)? What is the par value of the bonds now on deposit? What additional amount of bonds must the bank deposit if the circulation is increased to the maximum ?

5. How much is the redemption fund of a bank whose circulaation is \$427500? What is the amount of bonds on deposit to secure its circulation?

6. The New York associated banks, Mar. 25, 1882, held \$58,602,100 in specie and \$16,150,900 in legal-tenders. Their deposits on the same date were \$285,659,600. What was the excess of reserve (643) above legal requirements?

7. Oct. 1, 1881, the national banks of Boston had \$8,286,182 in specie, \$3,457,379 in legal-tenders, \$75,000 in U. S. certificates of deposit, \$11,735,499 due from reserve agents, and a redemption fund with U. S. Treasurer of \$1,603,628. What was the ratio of the reserve to the deposits, which were \$95,776,386? What amount of reserve was required? What was the surplus reserve?

8. What amount of reserve was required by the national banks of the State of Maine, their deposits being \$9,558,878?

9. The net earnings of a bank, whose surplus (644) is less than 20% of its capital (\$300000), are \$10475.38. What amount must be carried to the surplus account, and what are the undivided profits after declaring a dividend of 3%?

10. What is the semi-annual tax\* at  $\frac{1}{2}$ % upon a national bank whose average circulation is \$462,730 (641)?

11. A bank having a capital of \$250,000, and a surplus of \$50,000, for a period of six months, earned \$58693, and declared a dividend of \$30000. What was the rate of the dividend? The dividend is what % of the capital and surplus? The net earnings are what % of the capital and surplus?

12. The average daily exchanges at the New York Clearing House for 1886 were \$109,000,000, and the average daily balances \$5,000,000. The balances were what % of the exchanges ?

<sup>•</sup> The tax upon capital and deposits was repealed by Act of March 3, 1883.

# SAVINGS BANKS.

**646.** Savings Banks are institutions for the deposit and safe keeping of small sums of money. They are designed to encourage thrift and economy among the working classes.

**647.** Interest is usually declared Jan. 1st and July 1st of each year, and when declared is carried at once to the credit of each depositor on the books of the bank, when it stands as a deposit, and is entitled to interest the same as any other deposit. Savings banks, therefore, pay compound interest.

No interest is allowed on the fractional parts of a dollar, nor is any interest allowed on any sum withdrawn previous to the first day of January or July, for the period which may have elapsed since the last dividend.

**648.** Deposits are practically payable on demand, though the right to require a notice of 60 or 90 days is reserved.

In some savings banks, deposits commence to draw interest Jan. 1st, April 1st, July 1st, Oct. 1st; in others, deposits made on or before the first of any month draw interest from the first days of those months respectively.

Note.—In certain savings banks, money must be on deposit at least three months hefore it will be entitled to any interest. In a bank that has the above by-law and that pays interest from the first of each month, money deposited on or before May 1 would draw interest for 8 months on the following Jan. 1, and deposits made on or before June 1 would draw interest for 7 months, Jan. 1. Deposits made in October and November would be treated in a similar manner on the following July 1.

649. According to the laws of the State of New York,

No person shall have a deposit larger than the sum of three thousand dollars, exclusive of accrued interest, unless such deposit was made prior to the passage of the act (May 17, 1875), or pursuant to the order of a court of record, or of a surrogate.

Savings banks are restricted to 5% per annum regular interest or dividend. They must, however, declare an extra dividend at least once in three years, when their surplus earnings amount to 15% of their deposits.

Savings banks are allowed to pay interest on all sums deposited during the first ten days of January and July, and the first three days of April and October from the first of those months respectively.

#### EXAMPLES.

**650.** Perform the following examples according to both methods mentioned in Art. **648.** Where no rate is mentioned, 4% is understood.

1. A person deposited Dec. 30, 1881, \$150; Feb. 20, 1882, \$40; April 1, 1882, \$120; May 30, 1882, \$60. What amount was due July 1, 1882, nothing having been withdrawn?

ANALYSIS.—If interest begin on the first of each quarter, the first deposit, \$150, will draw interest from Jan. 1, or for 6 mo.; the second and third deposits, \$160 (\$40 + \$120), will draw interest from April 1, or for 3 mo.; the last deposit, made May 30, will draw no interest July 1.

4% per annum is 2% for 6 months and 1% for 3 months.

If interest begin on the first of each month, the first deposit, \$150, will draw interest from Jan. 1, or for 6 mo.; the second deposit, \$40, made Fcb. 20, will draw interest from March 1, or for 4 mo.; the third deposit, \$120, made April 1, will draw interest from April 1, or 3 mo.; the fourth deposit, \$160, made May 30, will draw interest from June 1, or for 1 mo.

2. The following deposits were made in a savings bank : July 1, 1881, \$100; July 16, \$40; Aug. 1, \$75; Aug. 29, \$45; Sept. 30, \$75; Oct. 28, \$200; Nov. 25, \$30; Dec. 31, \$100. What was due Jan. 1, 1882?

NOTE.-Balance the following accounts Jan. 1 and July 1 of each year.

3. How much interest was due on the following account July 1,1883? Deposits, Oct. 1, 1881, \$200; Dec. 31, 1881, \$160; Mar. 24, 1883, \$100.

4. Mr. A. made the following deposits in a savings bank : Jan. 1, 1879, \$100; May 1, 1879, \$140; June 30, 1879, \$40; Oct. 1, 1879, \$60; Feb. 28, 1880, \$120; June 30, 1880, \$45; Aug. 29, 1881, \$200. What was the balance due Jan. 1, 1882 ?

5. What is the balance of the following account July 1, 1879, interest being reckoned at 6% until July 1, 1877, and at 5% thereafter : Deposits, Oct. 14, 1876, \$200; Mar. 30, 1878, \$135; April 1, 1879, \$90?

6. Balance the following account July 1. Balance due Jan. 1,
\$103. Deposits, Jan. 28, \$40; Mar. 30, \$125; May 26, \$80. Drafts, Feb. 20, \$20; April 18, \$15; May 3, \$25; June 16, \$100.

Da	ite.	Deposits.	Drafts.		
Jan.	1,	103			
66	28,	AØ			
Feb.	20,	20	2Ø		
Mar.	30,	125			
Apr,	18,	85	XÞ		
May	3,	6 5	2\$		
"	26,	\$Ø			
June	16,	1 4	xøø		

ANALYSIS.—In order to determine the amounts that are entitled to interest, arrange the account in the following form, and deduct the drafts from the *last* deposits made, by the system of cancellation indicated below. The draft of \$20 made Feb. 20 is deducted from the deposit, \$40, of Jan. 28, leaving \$20. The drafts made April 18, \$15, and May 3, \$25, are deducted from the deposit of March 30, leaving \$85. The draft of June 16, \$100, cancels all of the deposit of May 26, and \$20 of the deposit of March 30, leaving

\$65 (\$85—\$20). The net deposits are as follows : Jan. 1, \$103 ; Jan. 28, \$20; March 30, \$65.

If interest commence the first of each quarter, the several amounts will draw interest as follows: \$103 from Jan. 1, or 6 mo.; \$20, deposited Jan. 28, and \$65 deposited Mar. 30, making \$85 from April 1, or 3 mo.

If interest commence the first of each month, the several amounts will draw interest as follows: \$103 from Jan 1, or 6 mo.; \$20, deposited Jan. 28, from Feb. 1, or 5 mo.; \$65, deposited Mar. 30, from April 1, or 3 mo.

7. What is the balance of the following account July 1? Balance due Jan. 1, \$30; deposits, Feb. 16, \$50; Apr. 1, \$185. Drafts, Mar. 12, \$60; May 10, \$50; June 20, \$60.

8. Balance the following Jan. 1, 1881. Deposits, July 1, 1880,
\$300; Aug. 1, \$150; Sept. 27, \$60; Oct. 12, \$325. Drafts, July 16, \$150; Sept. 1, \$150; Nov. 17, \$70; Dec. 18, \$140.

9. Balance the following account July 1. Balance due Jan. 1, \$364.48. Deposits, Jan. 24, \$50; Feb. 16, \$80; Apr. 30, \$40; June 28, \$100. Drafts, Mar. 30, \$75; May 19, \$10.

10. What was due July 1, 1882, on the following pass-book?

Dr.	FRANKLIN	SAVINGS	BANK in account	with A.	C. LOBECK.	Cr.
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1881.				1881.		
Jan. 1	Four Hundred Dollars.	400		Aug. 1	Two Hundred Dollars.	200
Mar. 15	Ninety Dollars.	90		1882.		
1881.	Interest to July.	*	**	Jan. 16	One Hundred and	
Sept. 16	Two Hundred Dollars.	200			Sixty dollars.	160
1882.	Interest to January.	*	**	June 1	Eighty Dollars.	80
Feb. 27	Two Hundred and Sixty Dollars.	260				
Mar. 8	One Hundred Dollars.	100				

# LIFE INSURANCE.

651. Life Insurance is a contract by which a company (the insurer), in consideration of certain payments, agrees to pay to the heirs of a person, when he dies, or to himself, if living at a specified age, a certain sum of money.

Life Insurance Companies may be classified according to principles of organization the same as Fire Insurance Companies (529).

652. The principal kinds of policies issued by Life Insurance Companies are the following: Ordinary Life, Limited Payment Life, Endowment, and Annuity.

Tontine Investment, Reserve Endowment, Semi-Tontine, Semi-Endowment, Yearly Renewable, and other special policies are issued by some companies.

653. Ordinary Life Policies.—On this kind of policy, a certain premium is to be paid every year until the death of the insured, when the policy becomes payable to the persons named in the policy as the beneficiaries.

654. Limited Payment Life Policies.—On a policy of this kind, premiums are paid annually for a certain number of years fixed upon at the time of insuring—or, until the death of the insured, should that occur prior to the end of the selected period. The policy is payable on the death of the insured.

These policies are issued with single payments, or with 5, 10, 15, 20, or 25 annual payments.

655. Endowment Policies.—An Endowment Policy provides (1) insurance during a stipulated period, payable at the death of the insured should he die within the period; and (2) an endowment, of the same amount as the policy, payable at the end of the period if the insured survive until that time.

These policies are issued for endowment periods of 10, 15, 20, 25, 30, or 35 years, and may be paid up by a single payment, by annual premiums during the endowment period, or by 5 or 10 annual payments.

#### Art. 656.]

**656.** Annuity Policies.—An Annuity Policy secures to the holder the payment of a certain sum of money every year during his life-time. It is secured by a single cash payment.

657. The Reserve of life insurance policies is the present value of the amount to be paid at death less the present value of all the net premiums to be paid in the future.

**658.** The **Reserve Fund** of a Life Insurance Company is that sum in hand which, invested at a given rate of interest together with future premiums on existing policies, should be sufficient to meet all obligations as they become due. It is the sum of the separate reserves of the several policies outstanding.

The legal rate for the reserve fund according to the laws of the State of New York, is  $4\frac{1}{2}\%$ ; of Massachusetts, 4%.

659. A Non-Forfeiting Policy is one which does not become void on account of non-payment of premiums.

1. According to the laws of the State of New York, after three full annual premiums have been paid, the legal reserve of the policy, calculated at the date of the failure to make the payments, shall, on surrender of the policy within six months after such lapse, be applied as a single payment at the published rates of the company in either of two ways, at the option of the assured. (1) To the continuance of the full amount of the insurance so long as such single premium will purchase term insurance for that amount, or (2) to the purchase of a non-participating paid-up policy.

2. According to the Massachusetts limited forfeiture law of 1880, after two full annual premiums have been paid, and without any action on the part of the assured, the net value (Massachusetts standard) of the policy less a surrender charge of 8% of the present value of the future premiums which the policy is exposed to pay in case of its continuance, shall be applied as a single payment to the purchase of paid-up insurance.

3. Certain companies voluntarily apply all credited dividends to the continuance of the insurance; others voluntarily apply the legal reserve to the purchase of term insurance at the regular rates.

4. In some companies, all limited payment life policies and all endowment policies, after premiums for three (or two) years have been paid and the original policy is surrendered within a certain time, provide for paid-up assurance for as many parts (tenths, fifteenths, twentieths, etc., as the case may be), of the original amount assured, as there shall have been complete annual premiums received in cash by the Company.

660. The Surrender Value of a policy is the amount of cash which the company will pay the holder on the surrender of the policy. It is the legal reserve less a certain per cent. for expenses.

#### [Art. 661.

## TABLE OF RATES.

	Ll Pays	IFE POL	ICIES. ath, only.		Pays	ENDOWI able as Indica	MENT PO ated, or at	POLICIES. It Death, if Prior.		
AGE.	ANNUAL PAYMENTS.				AGE.	In 10	In 15	In 20	AGE.	
	For Life.	10 Years.	15 Years.	20 Years.		Years.	Years.	Years.		
25	\$19 89	\$42 56	\$32 34	\$27 39	25	\$103 91	\$66 02	\$47 68	25	
26	20 40	43 37	32 97	27 93	26	104 03	66 15	47 82	26	
27	20 93	44 22	33 62	28 50	27	104 16	66 29	47 98	27	
28	21 48	45 10	34 31	29 09	28	104 29	66 44	48 15	28	
29	22 07	46 02	35 02	29 71	29	104 43	66 60	48 33	29	
30	22 70	46 97	35 76	30 36	30	104 58	66 77	48 53	30	
31	23 35	47 98	36 54	31 03	31	104 75	66 96	48 74	31	
32	24 05	49 02	37 35	31 74	32	104 92	67 16	48 97	32	
33	24 78	50 10	ę 38 20	32 48	33	105 11	67 36	49 22	33	
34	25 56	51 22	39 09	33 26	34	105 31	67 60	49 49	34	
35	26 38	52 40	40 01	34 08	35	105 53	67 85	49 79	35	
36	27 25	53 63	40 98	34 93	36	105 75	68 12	50 11	36	
37	28 17	54 91	42 00	35 83	37	106 00	68 41	50 47	37	
38	29 15	56 24	43 06	36 78	38	106 28	08 73	51 20	38	
39	30 19	57 03	44 17	37 78	39	100 00	09 09	01 00	39	
40	31 30	59 09	40 33	38 83	40	107 90	60 09	59 91	40	
41	02 41	69 10	40 00	39 93	41	107 65	70 40	52 80	41	
40	25 05	69 94	40 10	41 10	40	108 08	70 92	53 54	43	
140	36 46	65 57	50 61	12 64	14	108 55	71 50	54 25	44	
45	37 97	67 37	52 11	45 03	45	109 07	72 14	55 04	45	
46	39 58	69 26	53 68	46 50	46	109 65	72 86	55 91	46	
47	41 30	71 25	55 35	48 07	47	110 30	73 66	56 89	47	
48	43 13	73 32	57 10	49 73	48	111 01	74 54	57 96	48	
49	45 09	75 49	58 95	51 50	49	111 81	75 51	59 15	49	
50	47 18	77 77	60 91	53 38	50	112 68	76 59	60 45	50	
					1			A DESCRIPTION OF THE OWNER OF THE		

# 661. Annual premium for an Insurance of \$1,000, with profits.

1. The above table represents the maximum rates of the leading New York companies. Surplus premiums or dividends are returned annually commencing at the payment of the second premium.

2. Policies which do not share in the dividends of the company, are issued at fixed rates 15 to 20% less than the above.

3. The above rates are for annual payments only. To obtain semi-annual payments, add 4% and divide by 2. To obtain quarterly payments, add 6% and divide by 4.

#### EXAMPLES.

662. 1. Find the amount of premium for an ordinary life policy (653, 661) of \$5000, issued to a person 35 years of age.

2. What is the first annual premium of a life policy of \$6000, issued to a person 30 years old, \$1.00 being charged for the policy?

Note.—The policy fee is added to the first premium only.

3. Find the annual premium for a 20-payment life policy (654, 661) of \$4000, issued to a person 28 years old.

4. What annual premium must be paid for a 20-year endowment policy (655) of \$8000, age of the insured at nearest birthday, 40 years? If the insured dies during the tenth year, how much more would have been paid than if he had been insured on the ordinary life plan?

5. What is the average daily cost of a life policy for \$1000, no allowance being made for probable dividends, insurance commencing at age 25 ? At 35 ? At 45 ?

6. How much must a person, aged 35, lay aside weekly to secure a life policy of \$1000, payable in 20 annual payments ?

7. When 40 years old, a person took out a 20-year endowment policy of \$10000. He survived the endowment period. How much less did he receive than he paid as premiums, not reckoning interest?

8. Mr. A. when 26 years old took out an ordinary life policy of \$20000. He died aged 41 years 2 months. How much more did his heirs receive than had been paid premiums, no allowance being made for interest?

9. In the above example, supposing money to be worth 6% (simple interest), what was the net gain of the above insurance?

10. The annual premium, without profits, on a life policy of \$10000 at age 35 is \$222. How much would it be necessary to invest at 6% interest to secure the payment of the annual premium? How much would the insured leave his family at his death?

11. A gentleman, age 30, insures his life for \$20000, ordinary life plan. How much must he place in trust so that the interest at 5% will be sufficient to pay the premiums on the policy? At his death, how much does he leave his family?

[Art. 662.

12. If a man 32 years old takes out a life policy for \$5000 and dies just before reaching the age of 40 years, how much less will his total payments be than if he had taken a 20-year endowment policy for the same amount?

13. Mr. C. when 25 years of age secured a 20-year endowment policy of \$6000; when he was 30 years of age, he obtained an ordinary life policy of \$4000; when 35 years of age, he took out a 20-payment life policy of \$10000. What was the total annual premium after taking the last policy ?

14. Suppose Mr. C. had died at the age of 40<sup>1</sup>/<sub>2</sub> years, how much more would his heirs receive than had been paid as premiums ?

15. A single premium for an assurance of \$1000, without profits, for a person 32 years old, is \$300. What would be the excess of the assurance over the amount produced by placing the money at compound interest (**483**) at 4%, supposing the insured to live 20 years? 30 years? What would be the excess of the sum produced by the money at interest at 5%, over the assurance in 30 years?

16. Mr. B., age 40, has \$10000 at interest at 6%, which he intends to leave his family. What will this amount to at compound interest (483) in 25 years at 6%? How much will he leave his family if he takes out a life policy and pays the premium with the intesest on his investment of \$10000?

17. Mr. A., aged 30, secures an ordinary life policy, annual premium \$100. How much more would his heirs receive from the insurance company than from the money at compound interest (484) at 5%, should he die at the age of 32? Of 40? Of 50? At about what age would the amount received from the money at interest exceed the assurance?

18. What is the semi-annual premium (661, 3) on a 20-year endowment policy for \$6000, age 32? The quarterly premium?

19. Mr. A., who will be 35 years of age July 1, takes out Apr. 1 a 20-payment life policy for \$10000, premium payable semi-annually. Mr. B., of the same age, takes out Apr. 1 the same kind of policy for \$5000, and Oct. 1, another policy of the same kind for \$5000, premium payable annually. How much less does Mr. B. pay as premium each year than Mr. A? (661, 3.)

20. An ordinary life policy issued at age 35 for \$10000 has, at age 45, a 4% reserve of \$1262.60. How much non-participating paid-up insurance will this amount purchase, the single premium rate per \$1000 at age 45 being \$475.44?

# **REVIEW EXAMPLES.**

**663.** 1. Add  $17\frac{1}{3}, 28\frac{3}{4}, 36\frac{1}{2}, 44\frac{5}{8}, 89\frac{7}{12}$ , and  $76\frac{5}{6}$ ; multiply the sum by 87; subtract  $1022\frac{1}{24}$  from the product; and divide the remainder by  $234\frac{2}{3}$ .

2. Divide eighty-three, and seventy-five hundredths by one hundred twenty-five ten-thousandths; add to the quotient sixty-eight, and six hundred twenty-five thousandths; and multiply the sum by three, and two-tenths.

3. How many minutes in the month of February, 1900?

4. Find the cost of 7312 pounds of meal at \$2.25 per cwt.

5. The difference in the local time of two places is 1 hr. 7 min. 13 sec.; what is the difference in longitude?

6. Find the number of square yards of paving in a street, 3000 ft. long and 50 ft. wide.

7. What is the charge for packing, marking, and shipping 251 bales merchandise at 5s. 6d. per bale?

8. If 46 T. 12 cwt. of coal are worth \$174.75, what is the value of 37 T. 8 cwt.?

9. How many square yards of linoleum would cover a floor 22 ft. 6 in. by 15 ft. 4 in.? Find its value at  $63\phi$  per sq. yd.

10. What is the freight of 5 T. 9 cwt. 2 qr. 8 lb., at 70 shillings per ton (2240 lb.)?

11. Bought 280 cords of hard wood, at \$6.75, and 790 cords of soft wood, at  $3.62\frac{1}{2}$  per cord. Also, 750 bushels of corn, at  $62\frac{1}{4}$  cents, and 925 bushels of oats, at  $37\frac{1}{2}$  cents per bushel. What was paid for the whole, and what was the average price of wood per cord, and of grain per bushel?

12. Bought on contract 350 reams of foolscap paper, at  $$3.83\frac{1}{2}$  per ream,  $45\frac{1}{2}$  reams of which were returned as unsuitable, and 275 reams of letter, at  $$2.67\frac{1}{2}$  per ream,  $37\frac{1}{2}$  reams of which were rejected. How much was paid for the remainder?

13. Feb. 26, 1879, the Nevada Bank of San Francisco sold 100,000 ounces of pure silver to the United States, at  $1.08\frac{1}{2}$  per ounce. At this rate, what is the intrinsic gold value of the standard silver dollar?

14. What is the value of 45000 tons of steel rails at 97s. 6d. per ton? What is the value per ton in U. S. money? Of total in U. S. money?

15. What will be the cost of painting the walls and ceiling of a room, whose height, length, and breadth are 12 ft. 6 in., 27 ft., and 20 ft., respectively, at 24 cents per square yard?

16. What is the total cost of  $561^{23}$  bushels oats at 43 cents per bushel, and  $411^{14}$  bushels corn at 46 cents per bushel ?

17. Find the total freight on 68 cu. ft. mdse. at 35 shillings per ton (40 cu. ft.), and 123 cu. ft. at 40 shillings per ton, plus 10% primage on each item.

18. What is the cost of 250 ft. 3-ply hose, at 60 cts. per foot, less 30 and 10%, and 5 sets couplings at \$1.50 each?

19. May 10, A buys a bill of goods amounting to \$5000 on the following terms: 60 days, or 1% discount in 30 days, or 2% discount in 10 days. May 20, he makes a payment of \$2000, and June 9, of \$2500. How much would be due July 9, the end of the 60 days' credit?

20. Oct. 16, B bought a bill of merchandise amounting to \$2000 on the following terms: 4 months, or 5% discount in 30 days, or 6% discount in 10 days. Oct. 26 he made a payment of \$1000. How much would settle the bill Nov. 15?

21. B bought a bill of merchandise May 16 amounting to \$3416.72 on the following terms:  $4 \mod 5\% 30$  days. He paid on account June 21 (6 days after the expiration of the 30 days) \$3000, with the understanding that he should have the benefit of the discount by paying interest for the time elapsed, at 6% per annum. How much was due Sept. 16, no compound interest being reckoned?

22. A commission merchant in Chicago sells for me 12 bales brown sheeting, each bale containing 800 yards, at 7 *cts*. per yard; pays transportation and other charges amounting to \$72; and invests the proceeds in flour at \$4.80 per barrel. If he charges  $2\frac{1}{2}$ % for selling and  $1\frac{1}{4}$ % for purchasing, how many barrels of flour does he send me ?

23. A of Chicago, sends to B of New Orleans, 8000 *bu*. of wheat and 500 *bbls*. of flour with instructions to sell it and invest the proceeds in sugar. B pays freight and cartage \$3420; sells the wheat at \$1.60 per bushel and the flour at \$5.25 per barrel; charges  $2\frac{1}{2}\%$  commission on the flour and  $1\psi$  per bushel on the wheat. How many pounds of sugar are purchased at  $8\frac{1}{2}$  cents per pound, the commission for purchasing being 3%?

#### Art. 663.]

24. Mr. B. purchased 36150 pounds of hay at \$16.50 per ton, and 16438 pounds of oats at 70 cents per bushel. He sold the hay at a gain of 16%, and the oats at a loss of 8%. What were the proceeds?

25. If I purchase two building lots for \$3750 each, and sell one for  $\frac{1}{3}$  more than it cost, and the other for  $33\frac{1}{3}\%$  less, what is the gain or loss on the two lots?

26. A speculator sells two farms for \$6000 each; how much does he gain or lose, if he sells one for 20% more than it cost, and the other for  $\frac{1}{4}$  less than it cost?

27. Bought coal by the long ton at \$3.64, and sold by the short ton at \$4.25. What was the gain per cent?

28. Mr. A offered to sell his horse for 12% more than it cost him, but afterward sold it for \$504, which was 10% less than his first asking price. How much did his horse cost him?

29. Find the interest of \$375.60 for 1 yr. 10 mo. 22 da., at 5%?

30. Find the interest of \$4128 for 8 mo. 26 da., at 41%.

31. What is 21% of £159 13s. 10d.?

32. Find the date of maturity and the net proceeds of a note for \$5000, dated May 16, payable 4 months after date, and discounted July 21 at 6%.

33. When the above note became due, its maker had discounted at 6% a new note, payable 90 days after date, whose proceeds were sufficient to pay the first note. What was the face of the new note ?

34. Apr. 1, a merchant buys a quantity of coffee on 90 days' credit, with privilege of discounting within 30 days from date of purchase at the rate of 6% per annum for the unexpired time. Apr. 16, he makes a payment of \$28000 on account, no actual invoice having been rendered. May 1, he receives the invoice, amounting to \$29215, and on the same date full settlement is made What amount is required to cancel the bill? (Exact days, 360 days to the year.)

35. Divide \$2000 in such a manner between two brothers, aged 16 and 19 years respectively, so that when they arrive at 21 years of age they will have equal amounts, money being worth 6% simple interest.

36. What would be the share of each if money is worth 6% compound interest?

37. Find the interest on \$5000 from May 18 to Sept. 28, at 4%: 1, Ordinary interest and compound subtraction; 2, Ordinary interest and exact days; 3, Accurate interest.

38. Find the amount due on the following note Jan. 1, 1883, by the United States and the Mercantile Rules :

**5**000 00 Too. On demand, I promise to pay EDWIN D. MORGAN, or order, Five thousand dollars, with interest at six per cent., for value received. E. H. CONGER.

On this note the following payments were indorsed :

Received Jan. 16, 1879, \$400. Received Dec. 12, 1880, \$150.
Received Sept. 7, 1879, \$100. Received Aug. 18, 1881, \$850.
Received May 1, 1880, \$500. Received Apr. 23, 1882, \$100.
39. How much would have been due on the above note at 10% ?
40. What is the value of a draft on Hamburg of 17468 marks at 95<sup>3</sup>/<sub>8</sub> ?

41. C. of London owes me for goods sold on my account, £129 18s. 7d. How much do I receive in payment, if I draw a bill of exchange for the amount and sell it at  $4.85\frac{5}{8}$ ?

42. My agent in Paris buys an invoice of merchandise amounting to 12488 francs, at a commission of  $2\frac{1}{2}\%$ . What is the cost of the draft which I remit in payment, exchange being  $5.17\frac{3}{3}$ ?

43. An exporter sold the following bills of exchange through a broker : 10000 francs on Paris at 5.16<sup>3</sup>/<sub>8</sub>, £375 16s. 8d. on London at  $4.83\frac{5}{8}$ , 16480 marks on Hamburg at  $94\frac{7}{8}$ , 5287 guilders on Amsterdam at  $41\frac{1}{8}$ . What were the proceeds, brokerage  $\frac{1}{8}$ ?

44. A commission merchant at New York sells goods for A. of Havre to the amount of \$3435.27, and charges a commission of  $2\frac{1}{2}\%$  for selling. What is the face of the draft which he purchases and remits in settlement, exchange being 5.27?

45. My agent in London has purchased for me, at a commission of  $2\frac{1}{2}$ %, 375 dozen kid gloves at 49*d*. per dozen, and 636 yards silk at 9*s*. 6*d*. per yard. When exchange is \$4.86 $\frac{3}{4}$ , what will be the cost of the draft which I remit to him in settlement?

46. Purchased in Figiand, merchandise amounting to £324 10s. 7d., and paid irright and duties \$487.34. How much per £ must I sell these goods to gain  $12\frac{1}{2}\%$  on the full cost, and what must I charge for an article invoiced at 6s. 8d., exchange 4.88?

47. What is the cost of insuring \$18000 at  $75\phi$  less 15%?

#### Art. 663.]

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48. Average the following account, and find the amount due Sept. 28, 1882, at 6%.

Mar.	16,	1882,	\$874.32	on	30	days	credit.
66	31,	66	518.65	"	60	66	66
May	5,	66	373.78	66	4	months	66
66	21,	66	429.31	66	60	days	66
June	18,	66	657.70	66	30	66	66
July	3,	66	242.28	دذ	60	66	66
66	24,	66	983.75	66	4	months	66
Aug.	19,	66	716.30	66	4	66	66
Sept.	13,	66	536.60	66	60	days	66

49. Average the following account. What will be the amount due Jan. 1, 1883?

Dr. DAMIEL N. LANONI, Albung, N. I. Or.										
1882.					1882.					
July 16	Mdse.	., 4 mo.	\$876	14	Sept.10	Cash,	\$900	00		
Aug. 4	66	60 da.	415	65	·· 21		700	00		
Sept.10	66	30 da.	797	38	Oct. 13		500	00		
·· 21	- 66	30 da.	686	96	·· 31	Mdse., 30 da.	322	16		
Oct. 13	66	4 mo.	524	27	Nov. 2	Cash,	400	00		
·· 31	66	30 da.	859	75	·· 28	Note, 4 mo	800	00		
Nov.28	66	60 da.	263	31	Dec. 27	Cash,	500	00		
Dec. 1	66	60 da.	172	64						
·· 30	66	30 da.	938	52						

50. Prepare an account current, including interest at 6% to Jan. 1, 1883, from the above ledger account, according to the form and method of Art. **590.** 

51. Sold five \$1000 bonds at  $116\frac{3}{8}$ , and invested the proceeds in railroad stock at  $92\frac{1}{8}$ , which I sold at  $98\frac{1}{4}$ . What was the gain on the stock, allowing usual brokerage ?

52. Sold Aug. 11, 1879, 500 shares Chicago & Alton, at 94<sup>1</sup>/<sub>2</sub>, and covered my short sale Aug. 16, 1879, at 91. What was my profit, allowing the usual brokerage ?

53. What annual income will be obtained by investing \$9923.75 in bonds, bearing 5% interest, and purchased at  $116\frac{3}{4}$ ?

54. Bought stock at  $116\frac{3}{8}$  and sold at  $112\frac{7}{8}$ . Loss, \$1295. What was the par value of the stock ?

= 315

REVIEW EXAMPLES.

55. The tax levied in a town, having a valuation of \$1800000, is \$22500. What is the tax on \$1, and what is the tax of A, whose real estate is assessed \$5000 and personal property \$1500?

56. What is the duty at 60% on an invoice of silk amounting to 36475 francs ?

57. What is the duty on 50 cwt. 3 qr. 14 lb. (Long ton table) of steel at  $2\frac{1}{4}c$ . per pound ?

58. Find the duty at 25% on an invoice of mdse. valued at  $\pounds 243$  2s. 3d.

59. What is the duty on a block of marble  $2 \times 3 \times 7$  ft., imported from Italy, dutiable value 3450 lire, and duty \$1 per cubic foot and 25%?

60. A, B, and C are partners in business, investing as follows : A, \$4000; B, \$6000; C, \$8000. The partners are to share the profits and losses in proportion to their investments. Each is entitled to compensation for services at the rate of \$150 per month. to be credited the first day of the following month. Interest is to be reckoned on the salaries and on the amounts drawn out at the rate of 6% per annum. At the end of the year B and C purchase the interest of A, and in the payment therefor, it is desired that the remaining members shall so invest that their interests shall be equal. It is mutually agreed that the "good will" of the business shall be valued at \$3000 in the final settlement. It is also agreed that a discount of 5% shall be allowed upon all uncollected accounts as a fund to meet debts and costs for collecting. A statement of the business previous to closing shows the following results : merchandise, horses, wagon, office fixtures, and cash on hand, \$12410; sundry debtors, \$17030; sundry creditors, \$4050; expense account (not including partners' salaries), \$2400; profit on merchandise sold, \$15290. A withdrew on account of salary Apr. 1, \$450; July 1, \$300; Oct. 1, \$400. B withdrew Mar. 1, \$400; Apr. 1, \$150; June 1, \$400; Oct. 1, \$800; Dec. 1, \$500. C withdrew Apr. 1, \$600; July 1, \$700; Oct. 1, \$600; Nov. 1, \$200. How much must B and C each invest or pay A, and how should the books of the new firm be opened?

Notes.—1. B and C, not desiring to have the new books encumbered with the contingent accounts of "good will" and "reserve fund," closed these accounts after a settlement was made with A.

2. The loss or gain may be found from a statement of resources and liabilities, or from the Loss and Gain account.

# APPENDIX.

# GREATEST COMMON DIVISOR.

**664.** The **Greatest Common Divisor** of two or more numbers is the *greatest* number that will divide each without a remainder; hence it is their greatest common factor.

Thus, 2, 3, 4, and 12 are common divisors of 36, 48, and 60; 12 is their greatest common divisor.

# 665. To find the greatest common divisor of two or more numbers.

Ex. What is the greatest common divisor of 168, 252, and 420?

OPERATION.								
<b>4</b> ) 168,	252,	420						
7) 42,	63,	105						
3)6,	9,	15						
2,	3,	5						
$4 \times 7$	$7 \times 3 =$	=84.						

ANALYSIS.—Divide the given numbers by any number that will divide them all without a remainder, and divide the quotients in the same manner until the last quotients have no common divisor. Since 4 will divide all the given numbers, and 3 and 7 will divide succeasively the resulting quotients, their prod <sup>7</sup>, 84, is a common divisor of the given numbers. Since the last quotients have no

common divisor or factor, 84 is the greatest common divisor.

**666.** RULE.—Divide the given numbers by any factor that will divide all of them without a remainder. In like manner divide the resulting quotients, and continue the division until the quotients have no common factor. The product of the several divisors will be the greatest common divisor.

### EXAMPLES.

667. Find the greatest common divisor of the following numbers:

- 1. 108, 144, and 360.
   5. 405, 5.

   2. 144, 336, and 240.
   6. 378, 5.

   3. 165, 550, and 220.
   7. 375, 4.

   4. 792, 144, and 216.
   8. 288, 5.
- 5. 405, 243, and 324.
   6. 378, 126, and 252.
   7. 375, 625, and 250.
   8. 288, 720, and 864.

GREATEST COMMON DIVISOR. [Art. 668.

668. To find the greatest common divisor of two numbers when they are not readily factored.

669. PRINCIPLES. -1. A common divisor of two numbers is a divisor of their sum, and also of their difference.

2. A divisor of a number is a divisor of any multiple of that number.

670. RULE.—Divide the greater number by the smaller, and divide the last divisor by the remainder; and so continue until there is no remainder. The last divisor will be the greatest common divisor.

NOTES.-1. When the greatest common divisor of more than two numbers is required, find the greatest common divisor of the smallest two first, and of this greatest common divisor and the next greater, and so on, until all the numbers are used. The last divisor will be the greatest common divisor of all the given numbers.

3. If the remainder at any time is a prime number, and it is not contained in the last divisor, there is no common divisor greater than 1; it will therefore be useless to further continue the division.

Ex. Find the greatest common divisor of 391 and 437.

OPERATION. 391)437(1 391 46) 391 (8 368 23)46(2)46 0

DEMONSTRATION.-Since 23 is a divisor of 46, it is a divisor of 368, a multiple of 46 (Prin. 2). Since 23 is a divisor of itself and 368, it is a divisor of their sum, 391 (Prin. 1). Since 23 is a divisor of 46 and 391, it is a divisor of their sum, 437. 23 is therefore a common divisor of 391 and 437, the given numbers.

The greatest common divisor of 391 and 437, whatever it may be, is a divisor of their difference, 46 (Prin. 1); also of 368, a multiple of 46 (Prin. 2); also of 23, 391 - 368 (Prin. 1). Since the divisor

of a number cannot be greater than itself, the greatest common divisor of the given numbers cannot be greater than 23. 23 is therefore the greatest common divisor.

#### EXAMPLES.

671. Find the greatest common divisor of the following numbers :

1.	319 and 377.	5.	611,	799,	and	987.
2.	259 and 629.	6.	744,	984,	and	522.
3.	589 and 713.	7.	391,	667,	and	920.
4.	903 and 989.	8.	451.	481.	and	737.

8. 451, 481, and 737.

318

#### Art. 672.]

\$10000.

# ANNUAL INTEREST.

**672.** When a note contains the words "with interest annually," the laws of New Hampshire and Vermont, if the interest is not paid when due, allow simple interest on the annual interests from the time they become due to the time of payment.

ILLUSTRATION.—A agrees to pay B \$6000 in three years from Jan. 1, 1880, with interest annually at 6%. By this contract, \$360 becomes due Jan. 1, 1881, and on the first day of January in each year thereafter, until paid; this is the "annual interest." Suppose A does not pay any portion of this interest until Jan. 1, 1883, when the principal becomes due; then A, having had the use of money that his contract required him to pay to B, and B having been deprived of its use, B is entitled to have simple interest added to the annual interest, from the time when the same became due to Jan. 1, 1883; so that on Jan. 1, 1883, B would be entitled to the following sums as interest:

First :	year's	int.	\$360	+ 2	yrs.	$\mathbf{simpl}$	le int.	thereo	n, \$	\$43.20	=	\$403	3.20
Secon	d "	46	360	+1	"	66	66	**		21.60	=	381	.60
Third	66	66	360	+ 0	(paid	l whe	en due	)		00	=	360	)
		4	\$1080						-	64.80	=	\$114	1.80
Amou	nt of	annu	al in	teres	t.							\$1080	0.00
Amou	nt of	$\operatorname{simp}$	le int	teres	acci	rued	upon	annual	inte	erest	•	64	1.80
Total.	amon	int of	finto	roat d	and							@114/	1.90

In calculating the simple int. upon the annual int., shorten the operation by finding the int. upon the annual int. for the sum of the several periods.

Ex. What is the amount due on the following note July 1, 1885?

CONCORD, N. H., January 1, 1882.

Three years after date, for value received, I promise to pay A. B. THOMPSON, or order, Ten Thousand Dollars, with interest payable annually.

C. A. Downs.

	OPERATION.	
Fac	of note, on interest from Jan. 1, 1882	00.00
Inte	rest from Jan. 1, 1882, to July 1, 1885, 3 yr. 6 mo	00.00
3 ite	ms of annual interest (\$600 each) are unpaid:	
1st	from Jan. 1, 1883, to July 1, 1885, 2 yr. 6 mo.	
2nd	from Jan. 1, 1884, to July 1, 1885, 1 ur. 6 mo.	
3rd	from Jan. 1, 1885, to July 1, 1885, 6 mo.	
Int.	on the annual int. = int. on \$600 for $\overline{4 \text{ yr. 6 mo.}}$	62.00
	Total amount due July 1, 1885	62.00

#### APPENDIX.

[Art. 673.

**673.** RULE.—To the given principal and its interest to the date of settlement, add the interest on each annual interest from the time it is due to the date of settlement. The sum will be the amount due at annual interest.

#### EXAMPLES.

674. 1. At 6%, interest payable annually, how much would be due Oct. 1, 1884, according to the laws of New Hampshire, on a note of \$8000, dated June 1, 1881, no payments having been made?

2. What amount would be due Jan. 1, 1886, at 6%, on a note for \$4200, dated Concord, N. H., May 16, 1882, interest payable annually, and no payments having been made?

3. A note for \$10000 was dated Apr. 1, 1882, and payable four years from date without interest. Attached to this note were 8 notes of \$400 each for the semi-annual interest due Oct. 1, 1882, Apr. 1, 1883, Oct. 1, 1883, Apr. 1, 1884, Oct. 1, 1884, Apr. 1, 1885, Oct. 1, 1885, Apr. 1, 1886. How much was due, at 8%, Apr. 1, 1886, nothing having been paid ?

NOTE.—It is the custom of certain corporations when making loans for long periods of time on collateral security or on bond and mortgage, to have a note or mortgage given without interest for the principal, and to have separate notes given for each sum of annual, semi-annual, or quarterly interest, due and maturing at the time the interest is payable. These notes draw interest after maturity like any other note, and may be collected without disturbing the original loan.

4. What amount would be due July 1, 1884, on a note of \$5000, dated July 1, 1882, given for 2 years, with notes for quarterly interest, no payments having been made?

5. Required the amount due Jan. 1, 1883, on a note of \$3600, dated Jan. 1, 1881, due in two years, notes for semi-annual interest from date, at 6%, having been given, and nothing having been paid.

6. Find the amount of \$1200, at 6%, interest payable annually, from June 16, 1882, to Dec. 28, 1886, no interest having been paid except for the first year.

7. What must be paid, Oct. 16, 1885, in settlement of a note for \$2500, dated Manchester, N. H., May 6, 1880, said note promising interest annually, and no interest having been paid?

#### Art. 675.]

## **NEW HAMPSHIRE RULE.\***

675. According to the laws of New Hampshire, when payments are made upon a note, or other contract, by virtue of which interest is payable *annually* (672), they should be applied in the following order to the payment of—

1. Any simple interest that may have accrued upon the annual interest.

2. The annual interest. 3. The principal.

676. RULE.—Find the interest due upon the principal and the annual interest at the annual rest (the time when the annual interest becomes due from year to year) next after the first payment. To the payment or payments made before this rest, add interest from the dates when they were made to the date of the rest, unless there is no interest due upon the principal, excepting that which is accruing during the year in which the payment or payments were made, and the payments together are less than the interest thus accruing, in which last case no interest is to be added to the payments. Deduct the payment or payments, with or without interest, as aforesaid, from the amount of principal, annual interest, and simple interest upon the annual interest due at the time of said rest, if such payment or payments equal or exceed the annual and simple interest then due; if less than such annual and simple interest, but greater than the simple interest due upon the annual interest. deduct the same from the sum of the annual and simple interest, and upon the balance of such annual interest find simple interest to the time when the next payment or payments are applied; if less than the simple interest due upon the annual interest, deduct the same from such simple interest and add the balance without interest to the other interest due at the time when the next payment or payments are applied.

Proceed in like manner to the time of the first annual rest following the next payment, and to the end of the time required.

<sup>\*</sup> From Report of State Superintendent of Public Instruction (1877).

#### APPENDIX.

#### EXAMPLES.

677. 1. According to the law of New Hampshire, how much is due Jan. 1, 1886, on a note dated Jan. 1, 1880, for \$2000, with interest annually at 6%, the following payments having been made: July 1, 1882, \$500; Oct. 1, 1883, \$50.

#### OPERATION.

First annual interest due Jan. 1, 1881, \$120+2 yr. simple interest	
thereon, \$14.40	\$134.40
Second annual interest due Jan. 1, 1882, $120 + 1 yr$ . simple interest	
thereon, \$7.20	127.20
Third annual interest due Jan. 1, 1883,	120.00
Principal	2000.00
real to a second s	\$2381.60
First payment, July 1, 1882,	
Interest thereon from July 1, 1882, to Jan. 1, 1883, . 15	515.00
Balance of principal due Jan. 1, 1883,	1866.60
Fourth annual interest of \$1866.60, due Jan. 1, 1884,	112.00
Second payment, Oct. 1, 1883 (being less than the interest accruing	
during the year, it does not draw interest)	50.00
Balance of fourth annual interest unpaid	62.00
Fifth annual interest of \$1866.60, due Jan. 1, 1885,	112
Sixth annual interest of \$1866.60, due Jan. 1, 1886,	112
Simple interest on unpaid balance of fourth annual in for 2 ym.	7.44
Simple interest on fifth annual interest for 1 year	6.72
Balance of principal	1866.60
Amount due Jan. 1, 1886	2166.76

Solve Examples 2, 4, 8, and 9, Art. 505, according to the New Hampshire Rule, at the legal rate (436), supposing each note to contain the words "with interest annually."

# VERMONT RULE.

678. The Vermont Rule for notes with interest is essentially the same as the United States Rule (504); and for notes "with interest annually," it is the same as the New Hampshire Rule, except that when payments are made on account of interest accruing but not yet due, they draw interest from the date they were made to the annual rest, whether they are greater or not than the interest accruing during the year.

Thus, by the Vermont Rule, the payment of \$50, in the above example, would draw interest from Oct. 1, 1883 to Jan. 1, 1884, or 3 months. The unpaid balance of fourth annual interest would be \$61.25 (\$112 - \$50.75).
# STORAGE.

679. Storage is keeping or storing of goods in a warehouse until they are required for use, sale, or transportation.

Storage is also the name applied to the price or compensation for storing goods in a warehouse.

680. Storage is usually calculated at a certain rate per barrel, bale, bushel, box, or other unit for a certain time.

1. The storage term is one week, 10 days, 20 days, or one month.

2. In some warehouses, storage for a part of a term is charged at the same rate as for a full term.

# CASH STORAGE.

6S1. When the storage is paid or estimated when the goods are taken out of store or the receipt is surrendered, it is sometimes called *cash storage*.

# EXAMPLES.

**682.** 1. What was paid for the following storage at 6 cents per barrel per month or part of a month, the calculation being made at each delivery? Received Oct. 1, 1800 *bbl.*; Nov. 15, 360 *bbl.*; Dec. 18, 420 *bbl.*; Dec. 27, 432 *bbl.* Delivered Oct. 31, 1000 *bbl.*; Dec. 4, 240 *bbl.*; Dec. 19, 600 *bbl.*; Dec. 26, 300 *bbl.* 

		OPE
Date.	Received.	Delivered.
Oct. 1	-1800	1000 070
" 31	888	tøøø
Nov. 15	36Ø	240
Dec. 4	380.20	
18	420	¢øø
" 19		3ØØ
·· 26		
dec 27	432	And all the second second
On hand	872	in the state

RATION.		1111	11.1	
10	00 @	0.06	<u></u>	30.00
2	40 @	.18	= 4	13.20
5	60 @	.18	= 10	00.80
	40 @	0 .12	- <del>200</del> -1	4.80
3	00 @	.12	= 2	36.00
			\$24	4.80

ANALYSIS.—All goods delivered are deducted from the oldest receipt on hand. By the system of cancellation indicated in the operation, it can be easily determined when the storage commences. The 1000 *bbl*. taken out Oct. 31 were placed in store Oct. 1, and pay 1 month's storage. The 240 *bbl.* taken out Dec. 4 were placed in store Oct. 1, and pay 3 months' storage. Of the delivery of 600 *bbl.*, 560 were placed in store Oct. 1, and pay 3 months' storage, and the remainder, 40 *bbl.*, were placed in store Nov. 15, and pay 2 months' storage, Dec. 19. The lot of 300 *bbl.* withdrawn Dec. 26, were placed in store Nov. 15, and pay 2 months' storage. The separate calculations are placed at the right in the above operation.

Notes.—1. Certain warehouses render bills at the end of each month for all goods taken out during the month. Others render bills monthly for all storage dues, whether the goods have been withdrawn or not.

2. Storage on goods for which negotiable receipts have been issued, and in many other cases, is collected when the receipt is surrendered or the goods delivered.

2. What will be the storage at 5 cents per barrel per month on the following? Received Aug. 1, 800 bbl.; Aug. 15, 700 bbl.; Aug. 26, 900 bbl. Delivered Aug. 12, 400 bbl.; Aug. 20, 800 bbl.; Sept. 1, 400 bbl.; Sept. 8, 800 bbl.

3. Find the storage due on the following account June 24, at 3 cents a bale per month or part of a month. Received Apr. 13, 400 bales; Apr. 30, 800 bales; May 16, 200 bales; May 25, 400 bales; June 19, 600 bales. Delivered May 10, 600 bales; May 20, 100 bales; May 28, 700 bales; May 31, 400 bales; June 24, 600 bales.

4. Complete the following storage bill, the rate being 10c. per bale per month or part of a month.

When When Marks and Numbers. Rate. Amount. received. delivered. 20c. 80 4 Bales A C #174-177 June 4 Aug. 2 66 4 66 A C #298 May 21 30c. 30 " ... 5 A. C. & Co. #21-25 July 26 7 10c. " 3 66 A C #170-172 June 4 Aug. 17 16 \*\* \*\* 66 2 6 " C # 29-28 20 \*\* \*\* 66 66 22 \*\* \*\* A. C. & Co. #15-20 July 26 66 \*\* \*\* 1 66 24 AC#173 June 4 " 66 27 \*\* \*\* 4 A C #299-302 May 21 \*\* 66 \* 66 31 5 A. C. & Co. #26-30 July 26 \*\*

Messrs. ARMSTRONG, CATOR & Co.,

BALTIMORE, MD., Aug. 31, 1887. To Merchants' Storage Co., Dr.

Nore.—In many cases (see above example), storage is charged for the time the particular packages withdrawn have been in store.

5. The following quantities of wheat were stored at 1c. a bushel per month or part of a month. What was the amount of

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storage due June 1, a full settlement being made on that date and a new receipt being given ? Received Apr. 7, 600 bushels; Apr. 25, 400 bushels; May 9, 400 bushels; May 27, 300 bushels.

## AVERAGE STORAGE.

**683.** At some warehouses, in computing storage on grain, flour, etc., when there are frequent receipts and deliveries, it is customary to average the time and charge a certain rate per month of 30 days. The process is called *average storage*, or *storage on account*.

**684.** Ex. Merchandise was received and delivered at a warehouse as follows: Received Oct. 1, 1800 *bbl.* flour; Nov. 15, 360 *bbl.*; Dec. 18, 420 *bbl.*; Dec. 27, 432 *bbl.* Delivered Oct. 31, 1000 *bbl.*; Dec. 4, 240 *bbl.*; Dec. 19, 600 *bbl.*; Dec. 26, 300 *bbl.* Find the average storage due on the above Jan. 1, at 6 cents per barrel per month of 30 days.

Dat	te.	Received.	Days.	Products.	Dat	e	Delivered.	Days.	Products.
Oct.	1	1800	92	165600	Oct.	31	1000	62	62000
Nov.	15	360	47	16920	Dec.	4	240	28	6720
Dec.	18	420	14	5880	66	19	600	13	7800
66	27	432	5	2160	66	26	300	6	1800
		3012		190560			2140	1 I I	78320
		2140		78320					
On hand		872	3(	)) 112240	$3741\frac{1}{8} \times .06 = 224.48$				
				37411					

685. OPERATIONPRO	DUCT METHOD.
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ANALYSIS.—Assuming that there was nothing withdrawn, the 1800 *bbl.* would be in store from Oct. 1 to Jan. 1, or 92 days. The storage of 1800 *bbl.* for 92 days is equivalent to the storage of 1 *bbl.* for 165600 days. The storage of 360 *bbl.* for 47 days is equivalent to the storage of 1 *bbl.* for 16920 days. In the same manner, we find the total storage, if nothing had been withdrawn, to be equivalent to the storage of 1 *bbl.* for 190560 days. The storage on the goods withdrawn is equivalent to the storage of 1 *bbl.* for 78320 days, thus making the net storage 1 *bbl.* for 112240 days, or 3741<sup>1</sup>/<sub>8</sub> months. 6 cents multiplied by 3741<sup>1</sup>/<sub>4</sub> equals \$224.48, the total storage.

	GOOL OTHERETORY DI DITHE DIMERICON										
Date. Received			Delivered.	Balances.	Days.	Products.					
Oct.	1	1800		1800	30	54000					
66	31		1000	800	15	12000					
Nov.	15	360		1160	19	22040					
Dec.	4		240	920	14	12880					
66	18	420		1340	1	1340					
	19	100 00	600	740	7	5180					
66	26	at any la pe	300	440	-1 -	440					
	27	432		872	5	4360					
		3012	2140		92	30) 112240					
Jan.	1	Bal. on har	nd 872			37413					
		: 3012	3012	$37414 \times .0$	6 = 224	4.48					

686. OPERATION .- BY DAILY BALANCES.

S. S. A.L.

ANALYSIS.—Arrange the receipts and deliveries in the order of their dates as in the operation. Find the number of barrels on hand at each of the dates. The 1800 *bbl*. are in store from Oct. 1 to Oct. 31, or 30 days. The storage of 1800 *bbl*. for 30 days is equivalent to 1 *bbl*. for 54000 days. The total storage is equivalent to the storage of 1 *bbl*. for 112240 days, or  $3741\frac{1}{3}$  months. 6 cents multiplied by  $3741\frac{1}{3}$  equals \$224.48, the total storage.

#### EXAMPLES.

687. 1. Find by either of the above methods the average storage at 5 cents per month of 30 days, of the account given in Ex. 2, Art. 682.

2. Find the average storage, at 3 cents per month of 30 days, of the account given in Ex. 3, Art. 682.

3. Find the total charge for pasturing cattle per the following statement, at 30 cents a head per week: Received July 5, 18 head; July 12, 10 head; July 20, 30 head; Aug. 2, 40 head; Aug. 10, 20 head; Sept. 1, 10 head; Sept. 4, 24 head; Sept. 17, 26 head; Oct. 2, 20 head; Oct. 27, 18 head; Nov. 1, 6 head; Nov. 2, 16 head. Withdrawn July 7, 4 head; July 9, 8 head; July 14, 10 head; July 17, 6 head; July 23, 20 head; Aug. 4, 20 head; Aug 13, 20 head; Aug. 21, 12 head; Aug. 29, 4 head; Sept. 8, 10 head; Sept. 14, 30 head; Sept. 21, 18 head; Oct. 30, 20 head; Nov. 5, 10 head; Nov. 9, 20 head; Nov. 16, 26 head.

NOTE.—When the account is long, the first method is preferable.

# ALLIGATION.

688. Alligation treats of mixing ingredients of different values to find the value of the mixture, or to produce a mixture of a given value.

Note.-Alligation is sometimes and more properly called Average.

# ALLIGATION MEDIAL.

**689.** Alligation Medial is the process of finding the average value of a mixture, the rates and quantities of the ingredients being given.

### EXAMPLES.

**690.** 1. A grocer mixes together 7 pounds of coffee at 26 cents per pound, 4 pounds at 27 cents per pound, and 10 pounds at 34 cents per pound. What is the value of a pound of the mixture ?

### OPERATION.

7	$\times$	26 <i>c</i> .	_	\$1.82	
4	×	27c.		1.08	
10	×	34c.	=	3.40	
21	<i>lb</i> .	wor	$\mathbf{th}$	\$6.30	
1	17.	66		.30	

ANALYSIS.—7 *lb*. at 26*c*. are worth \$1.82. 4 *lb*. at 27*c*. are worth \$1.08. 10 *lb*. at 34*c*. are worth \$3.40. Hence the total mixture containing 21 *lb*. is worth \$6.30, and 1 *lb*. is worth \$6.30  $\div$  21, or 30*c*.

2. A wine merchant mixed together 10 gallons of wine at 40 cents a gallon, 15 gallons at 50 cents, and 25 gallons at 70 cents. What is the value of a gallon of the mixture ?

3. A grocer mixed 60 *lb*. of tea at 25 cents a *lb*., 75 *lb*. at 30 cents, and 65 *lb*. at 50 cents. What was the value of a pound of the mixture ?

4. A farmer mixes together 20 bu. of oats at 40 cents a bushel, 30 bu. of corn at 50 cents a bushel, and 50 bu. of rye at 70 cents a bushel. What is the value of a bushel of the mixture?

# ALLIGATION ALTERNATE.

**691.** Alligation Alternate is the process of finding the quantities of different values required to produce a mixture of a given value.

692. The values of several ingredients being given, to produce a mixture of a given value.

### EXAMPLES.

**693.** 1. How much tea worth 24, 28, 36, and 42 cents a pound must be mixed together, so that the mixture will be worth 30 cents a pound?

	OFERATIONS										
		(1)	(2)	(3)	(4)	(5)	$(\mathcal{C})$	(7)	(8)	(9)	
	24	1	0	1	0	1	2	3	1	3	etc.
30-	28	0	$\frac{1}{2}$	0	6	6	6	6	12	12	etc.
1	36	16	0	1	0	1	2	3	1	3	etc.
	42	0	$\frac{1}{12}$	0	1	1	1	1	2	2	etc.

ANALYSIS.—If we sell 1 pound for 30 cents, that is worth 24 cents, we gain 6 cents, and to gain 1 cent, we take  $\frac{1}{6}$  of a pound. We must now take a kind that is worth more than the average price so as to lose one cent. If we take a pound worth 36 cents and sell it at 30 cents, we will lose 6 cents, and to lose one cent, we must take  $\frac{1}{6}$  of a pound. In the same manner, we find that if we take  $\frac{1}{2}$  of a pound of the 28-cent tea and mix it with  $\frac{1}{12}$  of a pound of the 42-cent tea, there will be no gain nor loss by selling at 30 cents a pound.

 $\frac{1}{6}$  is to  $\frac{1}{6}$  as 1 is to 1, and  $\frac{1}{2} \begin{pmatrix} e_3 \\ 1 \end{pmatrix}$  is to  $\frac{1}{18}$  as 6 is to 1. Or, columns 3 and 4 may be found by multiplying columns 1 and 2 respectively by the least common denominators of the fractions.

Column 5 is the sum of columns 3 and 4. An unlimited number of answers may be found to examples of this kind by combining 1, 2, or 3, etc., times column 3 with 1, 2, or 3, etc., times column 4.

2. A grocer has sugar at  $5\phi$ ,  $7\phi$ ,  $12\phi$ , and  $13\phi$  per pound. How much of each kind will form a mixture worth 10 cents per pound?

3. A jeweler wishes to make a compound of gold that shall be 20 carats fine. He has gold of 15, 19, 23, and 24 carats fine. What quantity of each must he take ?

4. How much tea at 25 cents, 50 cents, 60 cents, and 80 cents per pound must be taken to form a mixture worth 55 cents per pound ?

Art. 693.]

5. How much wine at 50 cents, 70 cents, 80 cents, \$1.00, and \$1.20 a gallon must be mixed together that the mixture may be worth 90 cents a gallon ?

### 694. When the quantity of one ingredient is given.

### EXAMPLES.

**695.** 1. How much coffee at 30, 34, and 44 cents per pound, must be mixed with 10 pounds at 36 cents a pound, to make a mixture worth 40 cents a pound?

### OPERATION.

		(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
40	30	1	0	0	2	0	0	0	2
	34	0	16	0	0	2	0	0	2
	44	14	14	14	5	3	1	10	18
	36	0	0	1	0	0	1	10	10

ANALYSIS.—We find the relative quantities (columns 4, 5, and 6) as in Art. **693.** In order to use 10 pounds of the 36-cent coffee, we multiply column 6 by 10, producing column 7. Column 8 is found by adding columns 4, 5, and 7.

Other combinations may be found, by multiplying columns 4 and 5, and adding the results to column 7.

2. How much coffee at 15c., 17c., and 22c. a pound must be mixed with 5 *lb*. at 18c. per pound to make a mixture worth 20c. per pound.

3. How much gold of 21 and 23 carats fine, must be mixed with 30 oz. of 20 carats fine, so that the mixture may be 22 carats fine?

4. How much tea at 20 cents, 25 cents, and 45 cents a pound, must be mixed with 36 *lb*. at 60 cents a pound, so that the mixture will be worth 40 cents a pound ?

5. How much wine at \$1.25 and \$1.75 a gallon, must be mixed with 15 gallons of water, so that the mixture may be worth \$1 a gallon?

6. How much tea at 30 cents, 46 cents, and 48 cents a pound, must be mixed with 12 pounds at 38 cents, so that the mixture may be worth 40 cents a pound?

[Art. 696.

696. When the total quantity of the ingredients is given.

### EXAMPLES.

**697.** 1. A grocer mixed tea worth 20, 25, and 35 cents a pound. The mixture consisted of 50 pounds, worth 29 cents a pound. How many pounds of each did he take ?

ANALYSIS.—We find columns 3 and 4 as in Art. **693**. Column 5 is the sum of columns 3 and 4. The required amount is 50 = 5 times 10, the sum of column 5. Hence the quantity of each may be found by multiplying each number in column 5 by 5.

Note.—Many results may be obtained for examples of this kind. Thus, in the above example, 9 times column 3 plus once column 4, 8 times column 3 plus 2 times column 4, etc., would each produce correct results.

2. How much wine worth 50 cents, 60 cents, 90 cents, and \$1.20 a gallon, must be mixed together so as to make a hogshead of 110 gallons at 80 cents a gallon ?

3. A man bought 20 barrels of flour for \$120, paying  $\$4\frac{1}{2}$ , \$5,  $\$6\frac{1}{2}$ , and \$7 per barrel. How many barrels of each did he buy?

						OI	PERATIC	DN.					
		(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)
	$ 4\frac{1}{2} $	coko	0	1	0	1	1	0	2	2	0	3	3
0	5	0	1	0	8	0	8	6	0	6	4	0	4
0-	$6\frac{1}{2}$	2	0	3	0	3	3	0	6	6	0	9	9
	7	0	1	0	8	0	8	6	0	6	4	0	4
			2	4			20		•	20			20

ANALYSIS.—Find columns 2 and 3 as in Art. **693.** Since 6, the sum of columns 2 and 3, is not an exact divisor of 20, the required amount, we must take a certain number of times column 2 and a certain number of times column 3. By trial, we find that 8 times column 2 plus once column 3 equals 20. Therefore multiply column 2 by 8, producing column 4, and column 3 by 1, producing column 5. Column 6 is the sum of columns 4 and 5. In the same manner, we find the results given in columns 9 and 12.

4. A man bought 50 animals for \$50, paying for lambs  $\frac{1}{2}$  each, for sheep \$1\frac{1}{3}\$ each, and for calves \$3\frac{1}{2}\$ each. How many of each did he buy ?

### Art. 698.]

### SQUARE ROOT.

**698**. The Square Root of a number is one of the two equal factors of a number. Thus, the square root of 25 is 5.  $5 \times 5 = 25$ .

# 699. To find the square root of a number.

**'700**. RULE.—Beginning at units' place, separate the given number into periods of two figures each.

Find the greatest square in the left-hand period, and write its root at the right in the form of a quotient in division. Subtract this square from the left-hand period, and to the remainder annex the next period to form a dividend.

Double the part of the root already found for a trial divisor. Find how many times this divisor is contained in the dividend, exclusive of the right-hand figure, and write the quotient as the next figure of the root. Annex this quotient to the right of the trial divisor to form the complete divisor. Multiply the complete divisor by the last figure of the root, and subtract the product from the dividend.

To the remainder annex the next period, and proceed as before.

Note.—When the given number is a decimal, separate the number into periods of two figures each, by proceeding in both directions from the decimal point.

### EXAMPLES.

701. 1. Find the square root of 1156.

 $64 \begin{array}{|c|c|c|} \hline 0 \\ \hline 9 \\ \hline 256 \\ \hline 256 \\ \hline 0 \\ \hline 0 \\ \hline \end{array}$ 

ANALYSIS.—Beginning at units' place, separate the number into periods of two figures each. The greatest square in the left-hand period (11) is 9, and the root is 3, which is written in the quotient. By subtracting this square (9) from the left-hand period (11) and annexing to the remainder (2) the next period (56), we form the dividend, 256. By taking twice the root already found (3), we have 6 as a trial divisor, which is contained in the dividend (25), exclu-

sive of the last figure, 4 times. Write 4 in the quotient, and also to the right of the trial divisor, forming the complete divisor, 64. Multiplying the complete divisor, 64, by 4, the last figure of the root, and subtracting the product (256) from the dividend (256), there is no remainder. 34 is the required root.

Find the square root of

2.	1089.	6.	47524.	10.	119025.	14.	3976036.
3.	14641.	7.	65025.	11.	1406.25.	15.	431.8084.
4.	18225.	8.	86436.	12.	512656.	16.	7463824.
5.	46656.	9.	97344.	13.	232.5625.	17.	387420489.

18. Find the square root of  $\frac{256}{625}$ . Of  $\frac{1369}{1600}$ . Of  $\frac{5625}{12321}$ .

Note.—In finding the square root of a fraction, extract the square root of the numerator and denominator separately.

19. Find the side of a square field whose area is 412164 square rods.

20. Find the side (in feet) of a square whose area is one acre.

21. Extract the square root of 2 to 5 decimal places.

### CUBE ROOT.

702. The Cube Root of a number is one of the three equal factors of that number. Thus, the cube root of 8 is 2.  $2 \times 2 \times 2 = 8$ .

### 703. To find the cube root of a number.

'704. RULE.—Beginning at units' place, separate the given number into periods of three figures each.

Find the greatest cube in the left-hand period, and write its root at the right in the form of a quotient in division. Subtract this cube from the left-hand period, and to the remainder annex the next period to form a dividend.

Multiply the square of the root already found by 300 for a trial divisor. Find how many times this divisor is contained in the dividend, and write the quotient as the next figure of the root. Add to the trial divisor thirty times the product of the last figure of the root and the other figures of the root, and the square of the last figure to form the complete divisor. Multiply the complete divisor by the last figure of the root, and subtract the product from the dividend.

To the remainder annex the next period, and proceed as before.

### EX.AMPLES.

### 705. 1. Find the cube root of 39304.

OPERATION.	
	39'304 ( 34 27
Trial divisor. $300 \times 3^2 = 2700$ $30 \times 3 \times 4 = 360$	12 304
$4^2 = 16$	19 204
complete urvisor,	0

ANALVSIS.—Beginning at units' place, separate the number into periods of three figures each. The greatest cube in the left-hand period (39) is 27, and its root is 3, which is written in the quotient. By subtracting this cube (27) from

the left-hand period (39), and annexing to the remainder (12) the next period (304), we form the dividend, 12304. By multiplying the square of the root already found by 300 (multiply by 3 and add two ciphers), we form the trial divisor, 2700 ( $300 \times 3^2 = 2700$ ). The trial divisor, 2700, is contained in the dividend, 12304, 4 times. Write 4 as the next figure of the root. To form the complete divisor, add to the trial divisor (2700) 30 times the product of the last figure (4) of the root and the other figure (3) ( $30 \times 3 \times 4 = 360$ ) and the square of the last figure ( $4^2 = 16$ ). Multiplying the complete divisor, 3076, by 4, the last figure of the root, and subtracting the product (12304) from the dividend (12304), there is no remainder. 34 is the required cube root.

Note.—When the given number is a decimal, separate the number into periods of three figures each, by proceeding in both directions from the decimal point.

Extract the cube root of

$\mathcal{Z}$ .	5832.	6.	551368.	10.	98611128.
3.	10.648.	7.	7529536.	11.	279.726264.
4.	314432.	8.	9.663597.	12.	435519.512.
5.	474552.	9.	13651.919.	13.	676836152.

14. The product of three equal numbers is 551368. What are the numbers ?

15. A cubical block of marble contains 103823 cubic inches. What is its length ?

16. Find the cube root of 3375. Of 8000. Of 35937.

Note.—In finding the cube root of a fraction, extract the cube root of the numerator and denominator separately.

17. A cubical box holds 20 bushels. Find the length of its side.

# MENSURATION.

706. To find the area of a rectangle (319) or parallelogram.

707. RULE.—Multiply the length by the width. (320)

708. To find the area of a triangle.

**709.** RULE.—Multiply the base by half the perpendicular height.

710. To find the area of a triangle when the three sides are given.

**'711.** RULE.—From half the sum of the three sides subtract each side separately. Then multiply the half sum and the three remainders together, and extract the square root of the continued product.

712. To find the area of a trapezoid.

**'713.** RULE.—Multiply half the sum of its parallel sides by the perpendicular distance between them.

714. A Trapezoid is a four-sided figure having only two of its sides parallel.

715. To find the area of a circle.

716. RULE.—Multiply the square of the diameter by .7854; or multiply the square of the radius by 3.1416.

717. To find the surface of a sphere.

718. RULE.—Multiply the square of the diameter by 3.1416.

719. To find the solid contents of a prism or cylinder.

720. RULE.—Multiply the area of the base by the height or length of the prism or cylinder.

721. To find the solid contents of a sphere.

722. RULE.—Multiply the cube of the diameter by .5236.

# 723. GEOMETRICAL CONSTANTS.

## CIRCLES.

Circumference :	$=$ Diameter $\times$ 3.1416.
Circumference :	$=$ Radius $\times$ 6.2832.
Radius :	$=$ Circumference $\div$ 6.2832.
Radius :	$=$ Circumference $\times$ .1592.
Radius =	$=\sqrt{\text{Area}\div 3.1416}.$
Radius :	$= \sqrt{\text{Area}} \times .5642.$
Diameter :	$=$ Circumference $\div$ 3.1416.
Diameter :	$=$ Circumference $\times$ .3183.
Diameter :	$=\sqrt{\text{Area}\div.7854}.$
Diameter	$=\sqrt{\text{Area}} \times 1.1284.$
Area	= Radius square $\times$ 3.1416.
Area	$=$ Diameter square $\times$ .7854.
Side of inscribed squar	re $=$ Diameter $\times$ .7071
Side of equal square	$=$ Diameter $\times$ .886%
Side of inscribed equila	lateral triangle = Diameter $\times$ .8603

### SPHERES.

Surface	=	Diameter square $\times$ 3.1416.
Surface	=	Circumference square $\times$ .3183.
Volume	=	Diameter cubed $\times$ .5236.
Volume	=	Circumference cubed $\times$ .0169.
Diameter	=	$\sqrt{\text{Surface}} \times .5642.$
Diameter	=	$\sqrt[3]{\text{Volume}} \times 1.2407.$
Radius	=	$\sqrt{\text{Surface}} \times .2821.$
Radius	=	$\sqrt[3]{\text{Volume}} \times .6204.$
Circumference	=	$\sqrt{\text{Surface}} \times 1.7725.$
Circumference	=	$\sqrt[3]{\text{Volume}} \times 3.8978.$
Side of inscribed cub	e =	Diameter $\times$ .5774.
Side of inscribed cub	e =	Radius $\times$ 1.1547.

# ROOTS, ETC.

Diagonal of square = Side  $\times$  1.4142. Square root of 2 = 1.4142. Side of square = Diagonal  $\times$  :7071. 335

### EXAMPLES.

724. 1. What is the area of a rectangular piece of land 15.50 chains long and 12.25 chains wide?

2. Find the area of a triangular pièce of land whose base is 5.25 chains and perpendicular width 5.20 chains.

3. What is the area of a triangular piece of ground whose sides are 20, 30, and 40 rods respectively ?

4. A piece of land in the form of a trapezoid has two parallel sides, 1225 ft. and 750 ft. respectively, and the perpendicular distance between them is 1540 ft. What is its area?

5. The circumference of a circular race-course is one mile. What is its diameter in feet?

6. Find the circumference of a circle whose diameter is 150 feet.

7. A cow is tied to a stake by a rope 42 feet long. Upon how much surface can she graze ?

8. The diameter of a globe is 26 inches. What is the area of its surface ?

9. How many gallons of water will a cistern hold whose diameter is 10 ft. and depth 6 ft.?

10. What are the solid contents of a globe whose diameter is 26 inches?

11. A lake, whose diameter is 1000 ft, is covered with ice 8 in. thick. What is the weight of the ice in tons, if a cubic ft. of ice weighs 920 oz. avoirdupois?

12. Find the length of the side of a cubical bin, whose contents are 100 bushels.

13. The area of a square field is 5 acres. What is the length of a side ?

14. Find the solid contents of a log 24 ft. long and 2 ft. in diameter.

15. In making a square pond whose side was 204 ft., 10000 cubic yards of earth were taken out. What was its depth?

16. A room is 13 ft. 4 in. by 13 ft. 6 in. How many yards of carpet,  $\frac{5}{2}$  of a yard wide, will cover it ?

17. Find the diameter and circumference (in rods) of a circular field containing 10 acres.

18. How many acres in a field one mile in diameter?

# GENERAL AVERAGE.

725. If, in time of danger or distress, any loss or expense is voluntarily incurred for common safety of vessel, freight, and cargo, such loss or expense is made good by a "General Average;" the amount or value of such loss or expense being assessed upon the value of all interests involved and benefited.

All other losses and expenses are of a "Particular Average" nature, and are to be borne by the specific interests to which they apply.

726. The losses and expenses constituting general average are as follows :

1. Jettison, or throwing overboard of cargo to lighten the ship; damage to cargo by water going down the hatches during jettison; damage by chafing or breaking after jettison; freight on cargo jettisoned.

2. Sacrificing ship's materials, as the cutting away of masts, spars, etc. One-third of the cost of repairs of ship's materials is a special charge on the ship, as the new work is considered better than the old. No deduction is made for anchors.

3. Expense of floating a stranded ship.

4. Expense of entering a port of refuge, either to repair damage which renders it dangerous to remain at sea, whether such damage were caused by accident or sacrifice; or otherwise to avert a common danger.

5. Expense of discharging cargo for the purpose of making repairs, warehouse rent, reloading cargo, outward expenses, etc.

6. Wages and provisions of crew from the date of bearing up until ready for sea.

727. Contributory Interests and Values. — The ship contributes on its full value at the time which is made the basis of contribution. The cargo contributes on its net market value at the port of destination, less freight and charges saved.

The freight contributes on the full amount, less  $\frac{1}{3}$  for the wages, etc., of crew. In the States of New York, Virginia, California, and some others,  $\frac{1}{3}$  is deducted.

The underwriters (Insurance companies) contribute to the general average such a part of the expense as the insured value is of the market value of the goods (542). If, for example, a cargo is insured for \$10000 and is worth in the market \$12000, the underwriters are liable to pay  $\frac{5}{6}$  of the general average expense.

728. To give rise to general average, it must be shown that there was an imminent common danger, that the sacrifice was voluntary and necessary, and that the act was prudent and successful.

729. An Average Adjuster is a person who is familiar with the general average laws of the leading commercial nations, and who adjusts and apportions the losses and expenses of a general average.

The principal difficulty of an adjuster is to decide whether the loss should be made good by a general average or should be made a special charge (particular average) upon some particular interest. After the general average charges are determined, the apportionment of the loss among the several contributory interests is a simple arithmetical problem.

### EXAMPLES.

**730.** 1. The bark Liberty sailed from New York for Galveston with the following cargo: Shipped by A, \$5600; by B, \$8700; by C, \$16308; by D, \$8360. After two days out the bark encountered heavy gales and was damaged to the amount of \$630.14. On the fifth day the vessel began to take water, and for the safety of the vessel and the cargo the bark bore away for New York for repairs. The disbursements of the agent at New York were as follows: Custom-house fees, pilotage, protest, towage, unloading and reloading cargo, wharfage, inspection, consul fees, \$1369.43; bill of H. Robin & Co., shipwrights, etc., \$436; bill of Joseph Patti, ceiling ship, \$194.14. Agent's commission for advancing funds and paying above bills, 5%; on value of cargo landed, \$17388,  $1\frac{4}{7}$ . Wages and provisions of seamen from point of deviation, \$630.47.

Art. 730.]

freight. How is the settlement to be made, the value of the ship being \$10000 and the adjuster's fee \$100?

Notes.—1. In a general average, extracts from the log of the ship, the testimony of its officers, a complete statement of all expenses incurred, with the vouchers for the same, and all papers having any bearing upon the case are presented to the adjuster. The total amount of each item is entered in a column at the left of his statement of charges, and the amount is also entered in its proper column at the right. In addition to the general average column, there are usually columns to the right for the special charges upon the ship, owners, or cargo.

2. After determining the general average loss, divide it among the contributory interests in proportion to their values, by any of the methods given in Ex. 13, page 293.

Total.			General Average.		Ship and Owners.	
1369	43	Expense of entering harbor, landing cargo, etc.	1369	43		
436		Bill of H. Robin & Co., shipwrights, etc.	-		436	
194	14	" " Joseph Patti, ceiling ship.			194	14
		Agent's commission for advancing funds and				
99	98	paying above bills, 5%.	68	47	31	51
		Agent's commission on value of cargo landed,				
217	35	$17388, 1\frac{1}{4}\%.$	217	35		
630	47	Wages, etc., of seamen.	630	47		
100		Adjuster's fee.	100			
		General average.	2385	72		
3047	37	Ship and owners.			661	65

### STATEMENT OF CHARGES.

CONTRIBUTORY INTERESTS AND APPORTIONMENTS IN GENERAL AVERAGE.

Ship,	value	10000	@	.045	pays			450	
$\begin{array}{c} Freigh\\ \text{Less } \frac{1}{2}, \end{array}$	t, 8096 4048	4048	@	.045	"			182	16
Cargo,	5600		Ø	045	"	959		-	
А, В,	8700		@	.045	"	391	50		
C,	16308		@	.045	66	733	86		
D,	8360	38968	@	.045		376	20	1753	56
		53016	@	.045	"			2385	72

 $2385.72 \div 53016 = .045.$ 

	Dr		Cp		BALANCES.			
	DR		CA		To pay.		To receive.	
Vessel and Owners.					-			
Pay ship's proportion of Gen. Aver.	450							
" freight's "	182	16			1.0			
" owner's column.	661	65						
Receive seamen's wages.			630	47	663	34		
Cargo.					1.00			
Pay proportion of Gen. Average.	1753	56			1753	56		
Agents of Vessel.							1	
Receive their disbursements.			1999	57				
" " commission.			317	33			2316	90
Adjusters.								
Receive their fee.			100				100	
	3047	37	3047	37	2416	90	2416	90

### SETTLEMENT

2. The general average charges were \$4375.86, and the contributory interests \$64325. What was the per cent. of loss? What was the loss of Mr. B., whose goods were valued at \$7250?

3. Suppose A's goods in Ex. 1 were insured for \$5000, how much of the loss would be shared by the insurance company?

4. The ship Amazon, from Aspinwall to New York, being in distress, threw overboard part of the cargo, cut away the masts, and finally bore away to a port of refuge to repair in order to complete the voyage. The cost of replacing masts and rigging cut away was \$6000 (less  $\frac{1}{3}$  new for old); the cargo jettisoned was worth compared with sound cargo delivered at destination \$2000; freight on cargo jettisoned, \$200; expenses of entering port of refuge, discharging, storing and reloading cargo, \$1000; wages of master and crew from time of bearing away until ready for sea, \$600; provisions of master and crew for same time, \$500; adjuster's fee, \$100. The vessel was valued at destination at \$20000 (deduct gross repairs and add amount made good); cargo, value on arrival, \$40000 (add amount made good); freight collected, \$4000 (add amount made good and deduct  $\frac{1}{2}$ ). What was the per cent. of loss, and how was the settlement made ?

5. The cargo of the ship Amazon was insured for \$36000. How much was the claim against the insurance company?

6. The ship Union, in her passage from Liverpool to Boston, during a storm threw overboard cargo to the amount of \$1580, and cut away masts and rigging. She then entered the port of Halifax for repairs. The cost of replacing the masts and rigging which were voluntarily sacrificed, was \$4578 (less  $\frac{1}{2}$  new for old); cost of repairing accidental damage, \$568; freight on cargo jettisoned, \$314.75; expense of entering port of refuge, discharging cargo, etc., \$716.87; wages and provisions of crew, \$608; adjuster's fee, \$150. The value of vessel on arrival at Boston was \$30000 (deduct gross repairs and add amount made good); value of cargo delivered, less freight and duty, \$48475 (add amount jettisoned); total expected earning of freight, \$16320 (less  $\frac{1}{2}$  in Boston. See Art. 727). The cargo was shipped by the following persons: A \$8519, B \$20376, C \$6875, and D \$14285. The cargo jettisoned was a part of A's shipment. How ought the settlement to be made?

7. The ship Ocean Queen, from Pernambuco to New York, sprang a leak off Cape St. Roque, and for the safety of the vessel and cargo, threw overboard part of the cargo and put into Maranham for repairs. The disbursements at Maranham by the master of the vessel, including commissions, were as follows : Expenses of entering harbor, discharging, storing, and reloading cargo, 648.75; caulking and painting ship, carpenter work, etc., 843. Value of cargo delivered at New York, 334310.24; of cargo jettisoned, 1580.76; freight on cargo jettisoned, 3364; wages and provisions of crew, 304; adjuster's fee, 150; agent's commission for collecting amount in general average,  $2\frac{1}{2}\%$ . How shall the settlement be made, if the net value of the ship was 3157 (value on arrival 4000, less repairs 8843), and the total expected earning of freight was 2516 (less  $\frac{1}{2}$ )?

8. A vessel which put into a port of refuge for repairs was without funds. It being very difficult to obtain a loan on bottomry, or to negotiate a draft on the owners of the vessel, the master was obliged to sell part of the cargo to raise funds. Value of cargo sold compared with cargo delivered at destination, \$4566.06; produced at sale, \$2985.30; freight on cargo sold compared with freight on cargo delivered, \$363.93. What was the cost of funds, and how much should be apportioned to each interest, the general average charges being \$773.52, the special charges on ship \$956.10, and on the owners \$1181.06? ARGENTINE CONFEDERATION.

Metric system used in the assessment of duties. Old Spanish weights and measures (See Spain) in common use.

AUSTRIA, (AS GERMANY.)

BELGIUM, (METRIC SYSTEM.)

### BOLIVIA.

The metric system is the legal system, but the law has not been rigidly enforced. Old Spanish weights and measures (see Spain) still in use. For coin weight the metric gram is used.

BRAZIL, (METRIC SYSTEM.)

Diamonds are permitted to be sold according to the old Portuguese *outava* (55.34 grains).

Ships' freights are for the most part, settled according to the English ton (2240 *lb*.).

CANADA, (AS GREAT BRITAIN.)

### CHILI, (AS BOLIVIA.)

For custom purposes the metric system is enforced.

### CHINA.

1	Tael	=	$1\frac{1}{3}$ oz. av.
1	Catty	=	11 lb. av.
1	Picul	=	1331 lb. av.
1	Chih	=	14.1 inches.
1	Chang	=	11.75 feet.

COLUMBIA, (METRIC SYSTEM.)

#### DENMARK.

Pound (<sup>1</sup>/<sub>2</sub> kilogram) = 1.102 *lb*. av.
 Centner (100 *lb*.) = 110.23 *lb*. av.
 Tönde of grain = 3.948 U. S. *bu*.

1 Tönde of coal = 4.825 U.S. by

l Fod (Foot)	=	1.03 U. S. ft.
l Viertel	=	2.04 U. S. gal.
l Alen (Ell)	=	.6864 yd.

Coinage laws are metric. The introduction of complete metric system is in prospect.

ECUADOR, (METRIC SYSTEM )

EGYPT, (METRIC SYSTEM.)

### FRANCE, (METRIC SYSTEM.)

The old French  $aune = 1\frac{1}{4}$  yd. is still used to some extent in the silk industries of France and the U. S.

#### GERMANY.

Metric system with a few changes in subdivisions in general use.

1 Pound ( $\frac{1}{2}$  kilogram) = 1.1023 *lb*. av. 1 Centner (100 pounds)= 110.23 *lb*. av. 1 Wispel (metric ton) = 2204.6 *lb*. av.

### GREAT BRITAIN.

1	Imp.	Gallon		=	1.2	<b>U.</b>	S. $g$	al.
1	"	Bushel		=	1.03	U.	S. 7	n.
1	66	Quarter		=	8.25	5 U.	S. 7	'n.
1	Ale o	r Beer Ga	allon	<u></u>	1.22	U.	S.g	al.
1	Centa	al		=	100	lb.		
1	Quar at Lo	ter of Wh ondon	$\left  \begin{array}{c} \text{reat} \right\rangle \\ \end{array} \right\}$	=	480	lb.		
1	Quarter and Nev	of Wheat at wcastle.	Hull }	=	504	lb.		
1	Quarter dee and	of Wheat at other places.	Dun- }	=	496	lb.		
	Metr	ic system	n peri	nit	ted	by	law	of
18	864.							

#### GREECE.

Metric system with the common Grecian names in general use.

= 110.23 lb. av.
= 3.948 U. S. bu.
= 4.825 U. S. bu.
legalized since 1829.

TNDIA	1 Norwegian Pund - 11 th av
1 Seer - 16 abattucks	1 Swedish Fot $-11.7$ inches
1 Bombay Maund of 40 soors - 28 lb av	1 Normagian Fod $= 12.02$ (6
1 " " $49$ " $-204$ "	In Norway the metric system is used
$1 \qquad 42 \qquad -20.1$	to some extent
1 Surat $40 = 51_{\frac{5}{3}}$	To Some extent.
42 = 505	In Sweden, the coin weight and the
1 Den mal Electrone Max d $742$ (6	medicinal and apothecary weight are
1 Bengal Factory Maund $=74\frac{2}{3}$	metric. The complete metric system
1 ··· Bazaar ··· $=82\frac{1}{2}$ ···	has been obligatory since 1882.
1 Madras Maund $=20$ ···	PORTUGAL.
1 Bom y Candy of 20 Maunds $= 560$	Metric system compulsory since Oct.
1 Surat $1 = 740\frac{2}{3}$	1. 1868.
1 Madras " " $=500$ "	The chief old measures are-
1 Travancore $\cdots \cdots = 660 \cdots$	1 Libra $=1.012$ <i>lb</i> , av.
1 Tola $=180 \ gr.$	1 Almunde of Lisbon $=4.42$ U.S. <i>gal.</i>
1 Guz of Bengal $=1$ yard.	1 Alguiere $-3928$ II S by
1 Corge $=20$ units.	
1 Corge Pound $=20 lb.$	RUSSIA.
Metric system permissive.	1 Pound =0.9 <i>lb</i> . av.
TTALX	1 Pood (63 to a ton) =36 "
1  Palm = 555  cm  ft	1 Berkowitz =360 "
Metric system in general use	1 Chetvert $=5.956$ U.S. bu.
	1 Vedro =3.25 U. S. gal.
JAPAN.	1 Arsheen $=28$ inches.
1 Picul = $133\frac{1}{8}$ <i>lb</i> . av.	1 Ship Last $=2$ tons.
For coinage, in part, the metric unit	Metric system partially in use.
of weight is used.	
Turn	SPAIN, (METRIC SYSTEM.)
JAVA.	In many of the South American
1 Amsterdam Pond = $1.09lo$ . av.	States and in Cuba, the old Spanish
1 Picul $= 133\frac{1}{3}$	weights and measures, principally
1 Catty $= 1\frac{1}{3}$	Castilian, are used. They are as fol-
1 Chang $= 4$ yards.	lows :
MEXICO.	1 Libra $= 1.014 lb. av.$
Weights and measures are legally	1 Arroba (25 Libras) $= 25.36$ "
the metric, but the metric system is	1 Quintal (100 Libras) = $101.44$ "
not generally in force, the old Spanish	1 Vara $= .914 yd.$
weights and measures (see Spain) being	Current and
still employed.	SWITZERLAND.
	changes of names and subdivisions
NETHERLANDS.	Dure metric system optional
Metric system with a change in	r ure metric system optional.
names in general use.	TURKEY, (METRIC SYSTEM.)
1 Last (30 hectoliters) = $85.134 \ bu$ .	
Nonway and Sumpress	URUGUAY, (AS ARGENTINE CONFED-
1 Swedish Skalpond $= 0.931$ <i>lb</i> av	ERATION.)
1 Swedish Centner $= 931$	VENEZUELA, (METRIC SYSTEM.)

# DETECTION OF ERRORS

IN

## TRIAL BALANCES.

732. The following hints apply to the detection of errors in trial balances, or in any operation in which errors are made in addition or subtraction, or in transferring numbers from one place to another.

1. Ascertain the exact amount of the error. Much time is sometimes wasted in looking for errors which do not actually exist.

2. Revise carefully the additions of the trial balance before looking for the error in the ledger or other books.

3. If the error is in one figure only (as 2000, 100, 50, etc.), it is probably an error in addition or subtraction.

4. If an amount is entered on the wrong side of an account, or is added when it should be subtracted or *vice versa*, the error will be twice the amount.

5. If the digits of any number are written to the right or left one, two, or three places, and the error be divided by 9, 99, or 999 respectively, the quotient will be the number.

Thus, if \$427 be written \$4.27, the error will be \$422.73; which divided by 99 (by 9 and 11), the quotient will be \$4.27.

The number of 9's by which the number can be exactly divided is equal to the number of places which the number has been transferred to the right or the left.

6. If two consecutive digits of any number are transposed, the error will be a multiple of nine; and the quotient obtained by dividing the error by 9 will express the difference between the digits transposed.

Thus, if 437, be written 473, the error will be 36; which divided by 9 produces 4, the difference between 3 and 7. The same error, 36, will arise if the figures transposed are 0 and 4, 1 and 5, 2 and 6, 4 and 8, or 5 and 9.

7. If the error contains a number of figures, it is probable that some account or item has been omitted.

8. Look for the error systematically, and not in certain portions of the work selected at random.

# ANSWERS.

	Art. 20.	3. 40865.	3. 49374; 98748.	11. 5.761.888:
1.	1614.	4. 110547.	4. 110775;	195,249,432
2.	1654.	5. 8495098.	295400.	12. 18.413.409
3	19380	6. 853759.	5. 243580:	556 524 675
4	23243	7. 999895.	438444.	13 8 326 575
5	26162	8. 1109975.	6. 817281.	173 434 110
6	25120	9. 6419754.	726479	11 95 020 700
- /y	1566	10. 72540.	7 130240.	217 207 060
0	2000.	11. 57249251	189336	15 09 900 000
0.	52600	12, 10648519	8 1 578 946	20. 00,000,000
3.	44001	73 113558829	9 967 960	10 1 400 040
10.	44001.	14 15569180	0 404969.	10. 4,428,048;
11.	00480.	15 74 900 978	0. 404200; 817995	20,888,220.
1%.	54914,	16 5 654 798	10 4 800 150.	17. 744.
	Ant 214	17 00 110 099	10. 4,090,100;	18. 43200.
		10 100,000	7,050,257.	19. 2,419,200.
4.	4915. 9. 435.	10. 122,002.	11. 5,536,072;	20. 5250.
5.	4857. 10. 508.	19. 921294.	2,919,063.	21. 506880;
6.	394. 11. 3642.	20. 19,212,959.	12. 4,072,384;	1,098,240.
7.	376. 12. 3645.	21. 4740.	3,563,336.	22. 26376.
8.	321. 13. 3755.	22. 64535.	13. 3,824,910;	23. 106515;
14.	54877.	23. 45009.	5,737,365.	153720.
15.	44444.	24. 27369.	14. 5,240,172;	24. 576.
16.	41568.	25. 41976.	3,742,980.	25. 4608.
17.	36311.	26. 12464.	15. 58080.	26. 5016.
18.	84839.	27. 62645.	16. 2016.	
19.	139059.	28. 10514.	17. 24256.	Art. 47.
20.	10078521.	29. 3211.	18. 63360.	1. 144000:
21.	561. 26. 3657.	30. 5821.	19. \$194.40.	1080000.
22.	3691. 27. 6822.	31. 4004.	20. 1296.	2. 138240:
23.	1404, 28, 1711.	32. 5038.		864000.
24.	7921, 29, 1440	33. 1235.	Art. 44.	3. 241920:
25.	297. 30. 7529	34. 11,594,495.	1. 63936: 831168	1 451 520
31.	14152.	35. 193,941,760.	2. 75218:	4 185500 .
32	442 254 988	36. \$93,309,621.	1.463.858	1 335 600
33.	433	37. 3025.	3. 70272.	5 120000.
34.	1771	38. 6558830.	2.436.096.	3 200 000
35	4653	39. 3850814.	4 209387	6 252000.
36	39247	40. 388904.	1 915 125	1 036 000
37	16098	41. 1106.	5 358661 .	7 81600.
38	813210	.,	1 264 432	272000
29	6300	Art. 35.	6 544375.	8 84000.
10	1 177 761 793	7. 1107.90	4 606 875	2 100 000
1.1	5 309 516	2. 317 26	7 790408.	0 0 680 000.
1.0	324 423 840	3. 6622.70	7 912 916	67 760 000;
1.0	\$0258 04		2 661089.	10 19 500,000.
11.	\$110260.97	Art. 41.	6 061 069	10. 10,000,000;
+4.	фт10000.01.	1 164109.	0,501,500.	92,000,000.
	Art. 33.	187648	9. 0,090,004;	11. 1,407,000;
1	4337	2 340936.	10 5 947 409.	44,442,000.
0	907823	2. 040200; 998894	10, 0,847,408;	12. 11,760,000;
No	001020.	NAUOA4	190.000.421.	131 600 000

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[Art. 47.

13.	6,698,000;	10. 88375: 94500.	Art. 74.	11. 921300:
	114.260.000.	11, 95472: 96408	0 0000, 0101	919450
11,	8 019 200 .	12 91208 92962	2. 7025; 7101.	12 868000.
140	08 808 000	12 77980 . 80994	3. 8232; 7980.	000000,
15	C <sup>17</sup> 200 000.	11 15076. 14047	4. 6768; 6912.	000070.
10.	01,200,000;	14. 10010; 14041.	5.35991; 386613.	13. 838930;
	614,880,000.	15. 40040; 41195.	6. 39520; 413504.	836836.
16.	86,400,000;	16. 82215; 80649.	7. 49104: 523776.	Art. 90.
	460,800,000.	17. 58422; 57876.		1 11000. 10490
			Art. 78.	1. 11072; 12402.
	Art. 50.	Art. 62.	1 9190, 9904.	2. 10506; 10608.
3	264 . 176 . 198 .	2 3724 2964	1. 3130; 2304;	3. 13176; 12810.
0.	352 . 473 . 363 .	2 9593 · 8619	4130.	4. 12412; 12992.
	709. 901. 407.	/ 9655, 9105	2.4875; 3219;	5. 15515; 16240.
	192; 091; 401;	4. 2000; 5100.	1656.	6. 19536; 19008.
	404; 1012;	5. 0928; 21108.	3. 4851; 6375;	7. 1.010.024:
	957; 1023;	<i>6</i> . 16653; 33733.	816.	1 011 028
	704; 385; 396;	<i>7</i> . 23925; 56925.	4. 1739: 3819:	8 1 134 000.
	517; 187; 209;	1.00	3825.	1 199 500
	528; 627.	Art. 65.	5 8125 4536	1,100,000.
		2. 1206: 1809.	12036	Art. 93.
	Art. 53.	3. 1224: 1530.	6 5776 . 1996 .	1 10970 . 10165
0	9605 . 3806 .	4. 4158: 4851.	19008	0 10759, 10100.
~.	2575, 4578,	5 6048 . 6804	12990.	2. 10/02; 10004.
	0004. 5000;	6 19490 15595	Art. 81.	3. 10904; 11368.
	8024; 0087;	~ 10000 · 10020.	1 19194. 19045.	4. 9828; 10692.
	9625; 10098;	7. 10200; 40024.	1. (134; (047;	<i>5</i> . 91455; 93465.
	46398; 80564;	8. 13980; 32034.	4095.	<i>6.</i> 95665; 97679.
	79398; 19008;	9. 39096; 58644.	2. 2068; 2912;	7. 100188; 93104
	48125; 92136.	1.1 00	3306.	8. 95692; 97728.
		Art. 08.	3.5548;5925;	1 . 00
	Art. 56.	2.600;900;925;	4284.	Art. 99.
2	52704: 35424	1225; 1550;	4. 1892; 2860;	1. 39,456,174;
3	22227 50907	9675; 11200;	4221.	26.304.116.
1.	0387 . 36907	12800: 18650:	5. 13572: 11235:	2. 24.413.116:
4.	0001,00001.	$10600 \cdot 20425$	15250	16 275 4104
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0	200290.	17025 - 7050 -	Art. 84.	9 791 970
6.	378210;	9100, 6400,	0 604. 2005.	10517 201.
	600696.	12000, 020000,	2. 024; 1220;	4. 19,017,701;
- 7.	341284;	13900; 250000;	13010.	11,152,972.
	174804.	209400;	3.221;9024;	5. 2,057,613;
8.	112875;	132000; 43200;	13216.	1,371,742.
-	150375.	141200.	4. 1224; 1221;	6. 197,730,864;
9.	85425; 42925.	And NO	11024.	123,581,790.
10.	281869;	ATT. 70.	5. 625; 2021;	7. 58,642,209;
	234969.	3. 83763; 96929.	21021.	26.063,204.
11.	338583 :	4. 126936;	6. 1225; 3024;	8. 178,606,127;
	386883	293088.	24016.	51,030,322.
12	75576 . 338776	5. 43344; 42656.		9. 49.377.285:
12	963375.	6. 310148:	Art. 87.	27,431,825.
10.	250975	137592	2 9603·9118	10 31 025 988
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	Art. 59.	8 170556	1 8977 8544	11 51 595 2541.
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2.	10200; 13340.	000004.	0. 1210; 1500.	20,010,1415.
3.	5292; 6048.	9. 203912;	6. 9016; 8006.	12. 11,387,270;
4.	7830; 9918.	597376.	7. 8084; 8170.	35,693,635.
5.	6768; 6016.	10. 288834;	8. 985056;	13. 106,315,682;
6.	17276; 19744.	399924.	987042.	60,751,818
7.	37520; 42210.	11. 138446;	9. 981090;	14. 41,152,263;
8.	65664; 44928.	394284.	978120.	15,432,098§.
9.	134147:	12. 107880:	10. 976108;	15. 41,133,539;
	118365.	186180.	977090.	22,436,475

21. 365 6 16. 112.731.950; 8. \$25.12: 14. 38. 22. 138128. \$1.227. 78.912.365. 15. 55. 23. 67719 17. 57.447.290; 9. 53: 123. 16. 23, 32, 52,  $\begin{array}{c} 17. \ 3^2, 5, 43. \\ 18. \ 3^2, 5^2, 11. \\ 19. \ 2^2, 3^2, 5, 37. \end{array}$ 23.936.37018. 24. 356¥ 10. 414: 72. 25. 49829958. 18. 29,351,9812; 11. 217; 36. 26.  $368_{128}^{60}$ . 27.  $153_{320}^{204}$ . 16,010,171 $_{1}^{7}$ . 19. 144,300,144 $_{7}^{2}$ ; 12. 2304; 256. 20. 24, 32, 17. 13. 1536; 256. 21. 52, 11, 31. 28. 786395365. 112.233.445%. 14. 4088: 280. 20. 25,025,025; 29.  $2161\frac{227}{365}$ . 30.  $151911\frac{265}{365}$ . 22. 24, 33, 23. 23. 28, 32, 7, 19. Art. 139. 16.683.350. 31. 3,969,568. 24. 52, 7, 29. 21. 4628 sq. yds. 1. 4.964.629. 22. 10388s. 32. 14960. 2. 3.204.084. Art. 165. 23. 89 doz.; 3. 1.042.916.880. Art. 108. \$20.47. 4. \$4799.50. 1. 30. 12. 360. 24. 5280 ft. 2. 48. 47: 66: 68: 5. 5989 ft. 13. 288. 25. 20006 gal. 115; 153; 198; 5. \$18487. 3. 120. 14. 2640. 26. 10908 bu. 152; 69; 71; 7. \$11,014,811. 4. 16. 15. 1260. 8. 92250. 73; 80. 5. 84. 16. 240. Art. 103. 9. 456. 6. 360. 17. 660. Art. 132. 1. 11840 5 ; 11. \$458. 7. 504. 18. 3024. 2152109 12. 3582. 8. 60. 1. \$2837.46. 19. 360. 2. 1310018; 13. 132 acres. 9, 120, 20. 840. 2. \$1022.25. 999345. 14. \$2006. 10. 480. 21, 9900. 3. \$2775.87. 3.  $9879\frac{26}{38};$  $1001\frac{53}{375}$ 4. \$3383.08. 15. 4664.24. 22. 2520. 11. 480. 16. \$4.50. 5. \$14.91. Art. 169. 4. 1062825; 6. \$18.51. 17. \$46. 18. \$126.28. 4149 85. 7. \$569.25. 1. 1. 5. 14%. 5. 16948 6; 8. \$1311.26. 19. \$17377.65. 2. 2943. 6. 423. 3. 41347. 2037-20. \$30,022,347.95. 7. 6.  $\begin{array}{c} 2037_{\overline{208}},\\ 6. 170223_{\overline{18}}^{14}; \end{array}$ Art. 135. 21. \$34,077,380. 4. 511. 8. 5 7142 $\frac{110}{429}$ 7. 20147 $\frac{26}{64}$ ; 22. A, \$12283; 9. 2. 1. \$97.44. 2. \$51. B, \$12568; 10. 1008.  $\begin{array}{r} 2274_{\frac{76}{567}},\\ 8. 97134_{\frac{73}{5}}^{23}; \end{array}$ C, \$12371; .11. \$56. 3. \$273.53. D, \$12071; 4. \$677. 12. \$0.51. 16413<sup>389</sup>/<sub>432</sub> D. lowest. 5. \$3306. 13. \$9.371 9. 72660<sup>§</sup> 23. 339 head. 14. 150 bu. 6. \$187.60;  $\begin{array}{c} 10228_{553}^{553},\\ 10.\ 25052_{92}^{18}; \end{array}$ 24. \$9292.80. \$276.48. 15. 750 yd. 16. 133 lb. \$86.73; 25. 3000 lb. 7. 3161433 26. \$1044. 17. \$31.50. \$939.12.11. 11934856; 27. A, \$124; 18. 36 cows. 8. \$400.80;  $10663\frac{789}{817}$ . \$2164.32. B, \$125. 19. 243 bu. 12. 17008 § 28. \$7.75. 20. 1290 bu. 9. \$3168; 3914<u>1</u> \$25344. 29. 385231+; 21. \$16.92. 22. \$79. 13. 4193352; 32102 + .10. \$1305; 20093 34 \$4241.25. 23. \$21. Art. 158. 14.  $526009\frac{2}{14};$ 24. 56 lb. 11. \$2313.12;  $\begin{array}{c} 57532 \frac{32}{128}, \\ 15. \ 30366 \frac{19}{70}; \\ 6642 \frac{19}{320}. \end{array}$ 25. 66. 27. 90. \$13878.72.1. 32, 5, 7, 11.  $\begin{array}{c} 1.\\ 2.\\ 3.\\ 2, 3^3, 7, 11.\\ 3.\\ 2, 3^2, 5^2, 7.\\ 9.\\ 3^2, 5^2, 7.\\ 72 \end{array}$ 2. 3, 7, 11, 13. $3. 2, 3^3, 7, 11.$ 26. 10. 28. 23 47. 12. \$3756; \$9615.36. 16.  $58694_{64}^{29};$ 16261 $\frac{134}{231}.$ Art. 191. Art. 138. 5. 3, 52, 72. 23. 10. 1. 1.  $\begin{array}{c} 6. & 2, 3, 5, 7, 11. \\ 7. & 2^8, 3^2, 7, 13. \\ 8. & 2, 7, 13, 43. \end{array}$ 2. 3. 17. 11621338; 1. \$3.45. 11. \*.  $\begin{array}{r} 11462 \frac{61}{365}, \\ 18. \ 39625 \frac{79}{96}; \\ 5918 150 \end{array}$ 3. 4. 2. 15 lb. 12. 4. 13. \$4. 3. \$.53; \$.24.  $5218\frac{150}{729}.$ 19.  $50117\frac{30}{38};$ 5.  $\frac{9}{16}$ . 6.  $\frac{17}{21}$ . 9. 2, 3, 7, 11, 13. 4. \$19.04; 14. 11. \$13.60. 23 501 $2584_{640}^{131}$ . 10. 11, 61. 15. 3 11. 32 7. 20 5. \$48; \$36. , 52, 17. 16. 64.  $17. \ \frac{81}{128} \\ 18. \ \frac{13}{30}.$ 12. 2º, 113. 20. 290941 \$.87; \$.84. 8. 1/2000 5 17274188. 7. \$1.48; \$.185. 13. 218. 9.

10	3 06 2	Art 205	00 701	1 7 1916
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20.	Pr. 27. 100.	1 205	21. 2708.	8. 1287.
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5	82.40.27	11. 2025, 1000.	Ant 21%	10 500048
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	54	12. 270 5.	19. 00100%.	10. 07. 02. 4.
	72.	10 100017	20 504071	17, 131, 33, 221
9	102.117.80.	13. 100024.	20. 0010 g.	01 95
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10	65 . 64 . 80 .	$15.463^{1}_{77}$	22. 101004.	1.1 00N
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11.	144; 144; 144;	10 00000	05 779093	0 77111.00915
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12	180. 110. 147.	19. 049.	000 000001	1 10031
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	220, 220.	21. 1675	28. 14911.	1020084.
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2	803	Art. 213.	30 700395	419297
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7.	170, 990, 1970	0 11 85	01 1000001	000013
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7	179.449.317	4. 15. 9. 5	36, 340184,	$18275 \pm 1$
1.	4 , 12 , 16 .	4. 16. 0. 16.	00. 010101	0 104048
8.	20 907 546	$5. \pm 10. 81$	37. 3424687.	9. $16404\frac{3}{4}$ ;
0	845 . 898 . 1508	11 008	00 1195693	150945
9.	8, 2, 4, 4	11. 38%.	38. 4130084.	102048.
10	2911. 5020.	10 1015		10. 2695718.
10.	25, 11,	14. 18118.	Ant 001	10. 1000116,
	3145	13, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 130111, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13011, 13	Art. 221.	13239-9
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	4.	10. 4008.	». 011.14 <u>7</u> .	
12	699 . 5885 .	16. 861.	3. \$36.655.	1 1. 5. 2
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10	8077 . 647 .	10 98911	5 170	0 4 14 571
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11. 107.	11.	14.	Art. 256.	10. 00.0415.
12. 1232.	1%.	21.	1 50 0 85	16. 59.7023.
13. $214\frac{7}{12}$ .	13.	$1763\frac{3}{4}; 352\frac{3}{4}.$	100. 370.	<i>17</i> . 5512.33 <sup>3</sup> / <sub>7</sub> .
$14.576\frac{1}{3}$	14.	186.001.	2875. 4375.	18. 931.0574.
15 4838	15	145211	54375.	19 46571
10 7092	10.	0000 F0	6. 78125	10100.8.
10. 1007.	17.	\$200.09.	7 495	A wt 968
$17.809_{13}$	18.	\$48492.	7	ATC. 200.
18. $1593\frac{27}{32}$ .	19.	951 bu.	800 .	10004128.
19. 2143 <sup>15</sup> .	20.	22.901.	9. $.833\frac{1}{3}$ .	280448.
20 4101	01	8051	105831.	\$ 0000363
<i>a1</i> 19901	A1.	1 6010.	11. 7142855	1 \$42.916
20. 1400 B	22.	A, \$040;	10 1114	4. \$10.210;
22. 1420 <sub>10</sub> .		В, \$1080.	10 10 005	\$182.2870.
23. $576\frac{7}{12}$ .	23.	$$4360\frac{75}{128}$ .	13. 10.020.	5. 45.77125;
24. 194 <del>1</del> 8.	24	336.	14. 27.923076 $\frac{13}{18}$ .	55.02291#.
25. 1460-7	25	\$2475	$15. 36.9583\frac{1}{8}.$	6. 273735:
06 093 7	ac.	00601 ·	1	1 9196
AMO7	20.	\$202g.	Art. 259.	1.0100.
27. 4725.	27.	94.	1 1. 1/ 1.	7. 3.39924;
$28.\ 1019\frac{1}{4}.$	28.	$\$96\frac{1}{4}; 36\frac{1}{2}.$		.409652.
29. 8108.	29.	Horse, \$705:	2. <del>4</del> . 10. <del>3</del> .	800540625;
30. 3968.		Carriage	$3. \frac{3}{8}.$ 16. $\frac{3}{12}.$	.8455375.
		@1105	$4.\frac{5}{8}.$ 17. $\frac{1}{15}.$	0 11 208704 .
Apt. 236.	00	\$440g.	5. 7. 18. 4.	0100000
1110. 2000	30.	\$20035.	6 1 19 5	.0100072.
$1. 1\frac{1}{7}. 21. 26\frac{1}{4}.$	31.	\$157.67.	N 2 00 7	$10. 5.705483\frac{1}{3};$
$2.20.$ $22.7\frac{1}{3}.$	32.	501.	1. 125. 20. 72.	$34.01345\frac{5}{2}$ .
3. 371. 23. 15.	33	\$9.46	8. 125. 21. 560.	11. 28.6480831:
1 63 94 21	21	193.1 mal	9. 3250. 22. 9.	21 984375
F 1101 05 10	04.	Will gal.	10. 64 23. 1.	10 000, 44 0000
$0.117_{3}$ . 20.10.	35.	widow,	11 19 24 1	12200; 44.0920.
8. $1\frac{1}{2}$ . 26. $22\frac{3}{4}$ .		\$2876.12;	10 3 05 99 8	13. 93.05683 $\frac{1}{3}$ ;
9. $\frac{14}{15}$ . 27. $12\frac{1}{2}$ .		Each child,	12. 16. 20. 2080.	$4.02031\frac{1}{4}$ .
10. 11. 28. 163.		\$1438.06.	13. 8. 20. 1078.	14. 115.6666 <sup>2</sup> :
11 62 09 183	26	1/031	$27.175_{125}$ .	500 40291
	an.	0100 g.	28. 6-70.	15 51159.
12. J. JU. 213.	37.	\$19%.	100	1001100;
13. 1188. 31. 10.	38.	\$4600.	Art. 262.	8 80381
A1	00	Lost \$0.381.	1 100 010000	0.00005.
$14. 9. 32. 9\frac{1}{2}.$	39.		1 492 319787.	16. $82.0166\frac{2}{3};$
14. 9. 32. $9\frac{1}{2}$ . 15. $6\frac{3}{23}$ . 33. 13.	39.	201913:	1. 492.519707.	$16. 82.0166\frac{2}{3};$ $1061.1796\frac{7}{4}.$
$14. 9.$ $32. 9\frac{1}{2}.$ $15. 6\frac{3}{52}.$ $33. 13.$ $16. 2\frac{4}{5}.$ $34. 46$	39. 40.	20191 <sup>8</sup> ; 24348 <sup>7</sup>	1. 492.319787. 2. 7462.31526.	16. $82.0166\frac{2}{3};$ 1061.1796 $\frac{7}{5}.$ 17. 576: 432: 216:
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	39. 40.	20191 <sup>8</sup> ; 24348 <sup>7</sup> . 31062 <sup>8</sup> .	1. 492.319787. 2. 7462.31526. 3. 476.3380807.	$\begin{array}{c} 5.005_{5}^{\circ}.\\ 16. 82.0166_{5}^{\circ};\\ 1061.1796_{5}^{\circ}.\\ 17. 576; 432; 216;\\ 845.6\end{array}$
14.       9. $32.$ $9\frac{1}{2}.$ 15. $6\frac{3}{52}.$ $33.$ $13.$ 16. $2\frac{4}{15}.$ $34.$ $46.$ 17. $2\frac{1}{1}.$ $35.$ $13.$	39. 40. 41.	$20191\frac{3}{4};$ 243487. 31963 $\frac{3}{8};$	1. 492.319787. 2. 7462.31526. 3. 476.3380807. 4. 2.6591587.	<i>16.</i> 82.0166 <i><sup>2</sup></i> ; 1061.1796 <i><sup>2</sup></i> . <i>17.</i> 576; 432; 216; 345.6.
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	39. 40. 41.	$\begin{array}{c} 20191\frac{8}{4};\\ 243487.\\ 31963\frac{3}{2};\\ 185517\frac{5}{82}. \end{array}$	1. 492.319787. 2. 7462.31526. 3. 476.3380807. 4. 2.6591587. 5. 9710.27879.	16. 82.0166 <sup>3</sup> / <sub>5</sub> ; 1061.1796 <sup>3</sup> / <sub>5</sub> . 17. 576; 432; 216; 345.6. 18. 170845.86.
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	39. 40. 41. 42.	$\begin{array}{c} 20191\frac{5}{4};\\ 24348\frac{7}{5},\\ 31963\frac{3}{5};\\ 185517\frac{5}{319},\\ 6224\frac{5}{5}; \end{array}$	1. 492.319787. 2. 7462.31576. 3. 476.3380807. 4. 2.6591587. 5. 9710.27879. 6. 1.83586255.	16. 82.0166§; 1061.1706§. 17. 576; 432; 216; 345.6. 18. 170845.86.
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	39. 40. 41. 42.	$\begin{array}{c} 20191\frac{3}{4};\\ 24348\frac{7}{4},\\ 31963\frac{3}{4};\\ 185517\frac{5}{395},\\ 6224\frac{5}{2};\\ 14241\frac{3}{4},\\ \end{array}$	1. 492.319787. 2. 7462.31526. 3. 476.3380807. 4. 2.6591587. 5. 9710.27879. 6. 1.83586255. 7. 1764.06	16. 82.0166; 1061.1796; 17. 576; 432; 216; 345.6. 18. 170845.86. Art. 271.
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	39. 40. 41. 42.	$\begin{array}{c} 20191\frac{3}{4};\\ 24348\frac{7}{5},\\ 31963\frac{3}{5};\\ 185517\frac{5}{3}\frac{5}{5},\\ 6224\frac{5}{5};\\ 14241\frac{3}{16},\\ 19479\frac{7}{5}. \end{array}$	$\begin{array}{c} 1. \ 492.31576.\\ 2. \ 7462.31526.\\ 3. \ 476.3850807.\\ 4. \ 2.6591587.\\ 5. \ 9710.27879.\\ 6. \ 1.83586255.\\ 7. \ 1764.06.\\ 9. \ 675. \ 497. \end{array}$	6.0006; 16. 82.0166; 1061.1796; 17. 576; 432; 216; 345.6. 18. 170845.86. Art. 271. 1048.
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	<ul> <li>39.</li> <li>40.</li> <li>41.</li> <li>42.</li> <li>43.</li> </ul>	$\begin{array}{c} 20191\frac{3}{4};\\ 24348\frac{7}{4},\\ 31963\frac{3}{8};\\ 185517\frac{5}{533},\\ 6224\frac{5}{2};\\ 14241\frac{3}{4},\\ 19479\frac{7}{2};\\ 842611 \end{array}$	$\begin{array}{c} 1. \ 492.319761.\\ 2. \ 7462.31526.\\ 3. \ 476.3380807.\\ 4. \ 2.6591587.\\ 5. \ 9710.27879.\\ 6. \ 1.83586255.\\ 7. \ 1764.06.\\ 8. \ \$776.423.\\ \end{array}$	16. 82.0166 <sup>2</sup> ; 1061.1796 <sup>7</sup> ; 17. 576; 432; 216; 345.6. 18. 170845.86. Art. 271. 1. 048. 2 250
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	<ul> <li>39.</li> <li>40.</li> <li>41.</li> <li>42.</li> <li>43.</li> </ul>	$\begin{array}{c} 20191\frac{8}{4};\\ 24348\frac{7}{4};\\ 31963\frac{8}{5};\\ 185517\frac{5}{5};\\ 6224\frac{6}{5};\\ 14241\frac{8}{5};\\ 19479\frac{7}{4};\\ 84261\frac{1}{4};\\ 0100001\end{array}$	$\begin{array}{c} 1. \ 492.31576.\\ 2. \ 7462.31526.\\ 3. \ 476.3380807.\\ 4. \ 2.6591587.\\ 5. \ 9710.27879.\\ 6. \ 1.83586255.\\ 7. \ 1764.06.\\ 8. \ \$776.42\frac{7}{2}.\\ 9. \ 215.2741\frac{5}{18}. \end{array}$	$\begin{array}{c} 5.0505 \\ 5.0505 \\ 16. 82.0166 \\ ; \\ 1061.1796 \\ \hline \\ 5.76; 432; 216; \\ 345.6. \\ 18. 170845.86. \\ \hline \\ Art. 271. \\ 1048. \\ 2. 250. \\ 2. 250. \\ 9. 104. 8. 625 \end{array}$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	<ul> <li>39.</li> <li>40.</li> <li>41.</li> <li>42.</li> <li>43.</li> <li>44.</li> </ul>	$\begin{array}{c} 20191\overset{8}{4};\\ 24348\overset{7}{4};\\ 31963\overset{8}{5};\\ 185517\overset{5}{3}\overset{5}{3};\\ 6224\overset{6}{5};\\ 112241\overset{7}{1}\overset{8}{3};\\ 19479\overset{7}{4};\\ 84261\overset{1}{4};\\ \$198,31,\\ \$198,31,\\ \end{array}$	$\begin{array}{c} 1. \ 492.31576.\\ 2. \ 7462.31526.\\ 3. \ 476.3850807.\\ 4. \ 2.6591587.\\ 5. \ 9710.27879.\\ 6. \ 1.83586255.\\ 7. \ 1764.06.\\ 8. \ \$776.42\frac{5}{3}.\\ 9. \ 215.2741\frac{5}{15}.\\ 1. \ 215.02741\frac{5}{2}.\\ 1. \ 21.9026730\frac{5}{5}.\\ \end{array}$	$\begin{array}{c} 6.0005_{a},\\ 6.82.0166_{a};\\ 1061.1796_{a},\\ 17.576; 432; 216;\\ 345.6,\\ 18.170845.86,\\  Art. 271.\\ 1.048,\\ 2.250,\\ 3.104; 8.625,\\ 1.04; 8.625,\\ 1.042, 9.00 \end{array}$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	<ul> <li>39.</li> <li>40.</li> <li>41.</li> <li>42.</li> <li>43.</li> <li>44.</li> <li>45.</li> </ul>	$\begin{array}{c} 20191\frac{5}{4};\\ 24348\frac{7}{4},\\ 31963\frac{8}{5};\\ 185517\frac{5}{38},\\ 6224\frac{5}{5};\\ 14241\frac{3}{76},\\ 19479\frac{7}{7};\\ 84261\frac{1}{6},\\ 8198.31,\\ 19744. \end{array}$	$\begin{array}{c} 1. \ 492.319787.\\ 2. \ 7462.31526.\\ 3. \ 476.3380807.\\ 4. \ 2.6591587.\\ 5. \ 9710.27879.\\ 6. \ 1.83586255.\\ 7. \ 1764.06.\\ 8. \ \$776.42\frac{5}{3}.\\ 9. \ 215.2741\frac{5}{15}.\\ 10. \ 21.9026730\frac{5}{3}.\\ \end{array}$	$\begin{array}{c} \textbf{16. 82.0166} \\ \textbf{16. 82.0166} \\ \textbf{1061.1796} \\ \textbf{17. 576; 432; 216;} \\ \textbf{345.6.} \\ \textbf{18. 170845.86.} \\ \textbf{Art. 271.} \\ \textbf{1. 048} \\ \textbf{2. 250.} \\ \textbf{3. 104; 8.625.} \\ \textbf{4. 1.914; 2.82.} \end{array}$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	<ul> <li>39.</li> <li>40.</li> <li>41.</li> <li>42.</li> <li>43.</li> <li>44.</li> <li>45.</li> <li>46.</li> </ul>	$\begin{array}{c} 20191\frac{8}{4};\\ 24348\frac{7}{4},\\ 31963\frac{8}{5};\\ 185517\frac{5}{5},\\ 6224\frac{6}{5};\\ 14241\frac{3}{4},\\ 19479\frac{7}{5};\\ 84261\frac{1}{6},\\ \$198.31.\\ 19744,\\ \$84.24. \end{array}$	1. $492.315767.$ 2. $7462.31526.$ 3. $476.3830807.$ 4. $2.6591587.$ 5. $9710.27879.$ 6. $1.83586255.$ 7. $1764.06.$ 8. $\$776.42\frac{7}{2}.$ 9. $215.2741\frac{6}{2}.$ 10. $21.9026730\frac{5}{2}.$ Art. 265.	$\begin{array}{c} 5.0505 a_{7}, \\ 16. 82.0166 a_{7}, \\ 1061.1796 a_{7}, \\ 17. 576; 432; 216; \\ 345.6, \\ 18. 170845.86, \\ aaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaa$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	39. 40. 41. 42. 43. 44. 45. 46. 47.	$\begin{array}{c} 20191\frac{8}{4};\\ 24348\frac{7}{4},\\ 31963\frac{8}{5};\\ 185517\frac{5}{83};\\ 6224\frac{5}{5};\\ 14241\frac{3}{4},\\ 19479\frac{4}{5};\\ 84261\frac{1}{4},\\ \$4261\frac{1}{4},\\ \$4261\frac{1}{4},\\ \$4264\frac{1}{4},\\ \$84.24,\\ 27.80. \end{array}$	1. $492.319787.$ 2. $7462.31526.$ 3. $476.3850807.$ 4. $2.6591587.$ 5. $9710.27879.$ 6. $1.83586255.$ 7. $1764.06.$ 8. $\$776.42\frac{5}{4}.$ 9. $215.2741\frac{5}{4}.$ 10. $21.9026730\frac{5}{5}.$ Art. 265. 1. $3.9803.$	$\begin{array}{c} \textbf{b}, \textbf{c}, \textbf{b}, \textbf{c}, \textbf{c}, \textbf{s}, \textbf{c}, \textbf{c}, \textbf{s}, \textbf{c}, \textbf{s}, \textbf{s},$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	39. 40. 41. 42. 43. 44. 45. 46. 47. 48	$\begin{array}{c} 20191\frac{8}{4};\\ 24348\frac{7}{4},\\ 31963\frac{8}{5};\\ 185517\frac{5}{33};\\ 185517\frac{5}{33};\\ 14241\frac{3}{4},\\ 19479\frac{7}{5};\\ 84261\frac{1}{6},\\ 84261\frac{1}{6},\\ 8198.31,\\ 19744,\\ \$84.24,\\ 27.80,\\ 76.66\end{array}$	$\begin{array}{c} 1. \ 492.319787.\\ 2. \ 7462.31526.\\ 3. \ 476.3880807.\\ 4. \ 2.6591587.\\ 5. \ 9710.27879.\\ 6. \ 1.83586255.\\ 7. \ 1764.06.\\ 8. \ \$776.423.\\ 9. \ 215.2741.\frac{5}{5}.\\ 10. \ 21.90267305.\\ \textbf{Art. 265.}\\ 1. \ 3.9803.\\ 2. \ 96971 \end{array}$	$\begin{array}{c} 5.0505 a, \\ 5.0505 a, \\ 1061.1796 a, \\ 1061.1796 a, \\ 17.576; 432; 216; \\ 345.6. \\ 18.170845.86. \\ \hline {\it Art. 271.} \\ 1.048 a, \\ 2.250, \\ 3.104; 8.625, \\ 4.1.914; 2.82, \\ 5.875; 100.8, \\ 6.481.5; 385.2, \\ 7.4.25; 6.2, \\ \end{array}$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	39. 40. 41. 42. 43. 44. 45. 46. 47. 48. 49.	$\begin{array}{c} 20191\frac{8}{4};\\ 24348\frac{7}{4},\\ 31963\frac{8}{5};\\ 185517\frac{5}{5},\\ 6224\frac{6}{5};\\ 14241\frac{3}{4},\\ 19479\frac{5}{4};\\ 84261\frac{1}{5},\\ \$198.31,\\ 19744,\\ \$84.24,\\ 27.80,\\ 76.66,\\ 320\ \mathrm{rod}_5 \end{array}$	1. $492.319787.$ 2. $7462.31526.$ 3. $476.3830807.$ 4. $2.6591587.$ 5. $9710.27879.$ 6. $1.83586255.$ 7. $1764.06.$ 8. $\$776.42\frac{7}{4}.$ 9. $215.2741\frac{6}{12}.$ 10. $21.9026730\frac{6}{3}.$ Art. 265. 1. $3.9808.$ 2. $.26971.$ 8. $\$090.1$	$\begin{array}{c} 5.0505q_*\\ 5.0505q_*\\ 1061.1796q_*\\ 1061.1796q_*\\ 17.576; 432; 216;\\ 345.6.\\ 18.170845.86.\\ \phantom{\phantom{\phantom{\phantom{\phantom{\phantom{\phantom{\phantom{\phantom{\phantom{\phantom{\phantom{\phantom{\phantom{\phantom{\phantom{\phantom{\phantom{$
14. 9. 32. 9 $\frac{1}{2}$ . 15. 6 $\frac{2}{6}$ , 33. 13. 16. 2 $\frac{2}{16}$ , 35. 13. 16. 2 $\frac{2}{16}$ , 35. 13. 17. 21. 35. 13. 18. 1 $\frac{3}{2}$ , 36. 23. 19. $\frac{1}{70}$ , 37. 33 $\frac{1}{3}$ , 20. $\frac{1}{6}$ , 38. 13 $\frac{3}{4}$ . 39. 13 $\frac{1}{3}$ . 40. $\frac{1}{76}$ ; $\frac{2}{16}$ ; $\frac{11}{16}$ . 41. $\frac{5}{64}$ ; $\frac{3}{2}$ ; $\frac{5}{6}$ . 42. $\frac{3}{4}$ ; $\frac{5}{7}$ ; $1\frac{1}{2}$ . 43. 2; $1\frac{1}{2}$ . 44. 2 $\frac{1}{4}$ ; 2. 45. 635 $\frac{1}{2}$ ; $\frac{1}{3}$ .	39. 40. 41. 42. 43. 44. 45. 46. 47. 48. 49.	20191 $\frac{5}{4}$ ; 24348 $\frac{7}{4}$ . 31963 $\frac{5}{8}$ ; 185517 $\frac{5}{832}$ . 6224 $\frac{5}{8}$ ; 14241 $\frac{3}{6}$ . 19479 $\frac{5}{4}$ ; \$4261 $\frac{1}{6}$ . \$198.31. 19744. \$84.24. 27.80. 76.66. 320 rods.	1. $492.319787.$ 2. $7462.31526.$ 3. $476.3380807.$ 4. $2.6591587.$ 5. $9710.27879.$ 6. $1.83586255.$ 7. $1764.06.$ 8. $\$776.423.$ 9. $215.2741_{1}^{5}5.$ 10. $21.9026730_{5}^{5}.$ Art. 265. 1. $3.9808.$ 2. $.26971.$ 3. $8999.1.$	$\begin{array}{c} 5.0505 g_{\star} \\ 5.0505 g_{\star} \\ 1061.1796 g_{\star} \\ 1061.1796 g_{\star} \\ 17.576; 432; 216; \\ 345.6. \\ 18.170845.86. \\ \hline {\it Art. 271.} \\ 1.048. \\ 2.250. \\ 3.104; 8.625. \\ 4.1914; 2.82. \\ 5.875; 100.8. \\ 6.481.5; 385.2. \\ 7.4.25; 6.2. \\ 8.15.24706; \\ 9.95 \end{array}$
14. 9. 32. 9 $\frac{1}{2}$ . 15. $6\frac{3}{62}$ . 33. 13. 16. $2\frac{1}{15}$ . 35. 13. 17. $2\frac{1}{1}$ . 35. 13. 18. $1\frac{3}{2}$ . 36. 23. 19. $\frac{9}{10}$ . 37. 33 $\frac{1}{3}$ . 20. $\frac{3}{15}$ . 38. 13 $\frac{3}{2}$ . 20. $\frac{3}{15}$ . 38. 13 $\frac{3}{2}$ . 20. $\frac{3}{15}$ . 38. 13 $\frac{3}{2}$ . 20. $\frac{3}{15}$ . $\frac{3}{15}$ . $\frac{11}{15}$ . 20. $\frac{3}{15}$ . $\frac{3}{15}$ . $\frac{11}{15}$ . 20. $\frac{3}{15}$ . $\frac{3}{15}$ . $\frac{11}{15}$ . 20. $\frac{3}{15}$ . $\frac{3}{15}$ . 21. $\frac{3}{15}$ . $\frac{3}{15}$ . 22. $\frac{3}{15}$ . 23. $\frac{3}{15}$ . 24. $\frac{3}{2}$ ; $\frac{3}{2}$ . 25. $\frac{3}{15}$ . 26. $\frac{3}{15}$ . 27. $\frac{15}{15}$ . 27. $$	39. 40. 41. 42. 43. 44. 45. 46. 47. 48. 49. 50.	20191 $\frac{3}{4}$ ; 24348 $\frac{7}{4}$ . 31963 $\frac{3}{8}$ ; 185517 $\frac{5}{33}$ . 6224 $\frac{6}{4}$ ; 14241 $\frac{3}{4}$ . 19479 $\frac{7}{4}$ ; 84261 $\frac{1}{6}$ . \$198.31. 19744. \$84.24. 27.80. 76.66. 320 rods. 6 days.	1. $492.319787.$ 2. $7462.31526.$ 3. $476.3880807.$ 4. $2.6591587.$ 5. $9710.27879.$ 6. $1.83586255.$ 7. $1764.06.$ 8. $\$776.423.$ 9. $215.2741.$ 9. $21.90267305.$ Art. 265. 1. $3.9808.$ 2. $.26971.$ 3. $8999.1.$ 4. $4648.$	$\begin{array}{c} 5.0505 a,\\ 5.0505 a,\\ 1061.1796 a,\\ 1061.1796 a,\\ 1061.1796 a,\\ 345.6,\\ 18. 170845.86,\\ \\ 1. 048,\\ 2. 250,\\ 3. 104; 8.625,\\ 4. 1.914; 2.82,\\ 5875; 100.8,\\ 6. 481.5; 385.2,\\ 7. 4.25; 6.2,\\ 8. 15.24706;\\ 2.25,\\ 0. 02000000000000000000000000000000000$
14. 9. 32. 9 $\frac{1}{2}$ . 15. 6 $\frac{1}{2}$ , 32. 13. 16. 2 $\frac{1}{15}$ , 35. 13. 16. 2 $\frac{1}{15}$ , 35. 13. 17. 21. 35. 13. 18. 1 $\frac{1}{2}$ , 36. 23. 19. $\frac{1}{10}$ , 37. 33 $\frac{1}{2}$ , 20. $\frac{1}{15}$ , 38. 13 $\frac{3}{4}$ . 39. 13 $\frac{1}{3}$ . 40. $\frac{1}{15}$ , $\frac{1}{15}$ ; $\frac{11}{16}$ . 41. $\frac{5}{15}$ ; $\frac{1}{15}$ ; $\frac{11}{16}$ . 42. $\frac{3}{4}$ ; $\frac{6}{15}$ ; $\frac{1}{15}$ . 43. 2; 1 $\frac{1}{2}$ . 44. 2 $\frac{1}{4}$ ; $\frac{2}{2}$ . 45. 635 $\frac{1}{2}$ ; $\frac{1}{3}$ . Art. 237. 1. $\frac{9}{16}$ .	39. 40. 41. 42. 43. 44. 45. 46. 47. 48. 49. 50. 51.	20191 $\frac{3}{4}$ ; 24348 $\frac{7}{4}$ . 31963 $\frac{8}{5}$ ; 18551 $7\frac{5}{53}$ . 6224 $\frac{6}{5}$ ; 14241 $\frac{3}{45}$ . 19479 $\frac{7}{6}$ ; $\$12841\frac{1}{45}$ . \$198.31. 19744. \$84.24. 27.80. 76.66. 320 rods. 6 days. Gained 2 cts.	1. $492.319787.$ 2. $7462.31526.$ 3. $476.3380807.$ 4. $2.6591587.$ 5. $9710.27879.$ 6. $1.83586255.$ 7. $1764.06.$ 8. $\$776.42\frac{7}{4}.$ 9. $215.2741\frac{6}{12}.$ 10. $21.9026730\frac{5}{3}.$ Art. 265. 1. $3.9803.$ 2. $.26971.$ 3. $8999.1.$ 4. $.4648.$ 5. $16.6736.$	$\begin{array}{c} 5.0505q_{\star}\\ 5.0505q_{\star}\\ 16. 82.0166q_{\star}\\ 1061.1796q_{\star}\\ 17. 576; 432; 216; \\ 345.6. \\ 18. 170845.86. \\ \hline {\it Art. 271.}\\ 1048. \\ 2. 250. \\ 3. 104; 8.625. \\ 4. 1.914; 2.82. \\ 5875; 100.8. \\ 6. 481.5; 385.2. \\ 7. 4.25; 6.2. \\ 8. 15.24706; \\ 2.25. \\ 949; 82.6875. \end{array}$
14. 9. 32. 9 $\frac{1}{2}$ . 15. 6 $\frac{2}{6}$ , 33. 13. 16. 2 $\frac{2}{16}$ , 34. 46. 17. 2 $\frac{1}{2}$ , 35. 13. 18. 1 $\frac{3}{4}$ , 36. 23. 19. $\frac{1}{70}$ , 37. 33 $\frac{1}{2}$ , 38. 13 $\frac{3}{4}$ . 20. $\frac{1}{6}$ , 38. 13 $\frac{3}{4}$ . 20. $\frac{1}{6}$ , $\frac{2}{6}$ , $\frac{1}{76}$ , $\frac{11}{76}$ . 41. $\frac{5}{64}$ ; $\frac{9}{75}$ ; $\frac{1}{12}$ . 42. $\frac{3}{4}$ ; $\frac{9}{5}$ ; $\frac{1}{12}$ . 44. 2 $\frac{1}{4}$ ; $\frac{2}{5}$ ; $\frac{1}{2}$ . 44. 2 $\frac{1}{4}$ ; $\frac{2}{5}$ . Art. 237. 1. $\frac{9}{16}$ . 2. $\frac{4}{48}$ .	39.         40.         41.         42.         43.         44.         45.         46.         47.         48.         49.         50.         51.         52.	$\begin{array}{c} 20191\frac{8}{4};\\ 243487.\\ 31963\frac{8}{5};\\ 185517\frac{6}{538}.\\ 6224\frac{5}{5};\\ 14241\frac{3}{6}.\\ 19479\frac{4}{5};\\ 84261\frac{1}{6}.\\ 8198.31.\\ 19744.\\ 884.24.\\ 27.80.\\ 76.66.\\ 320 \text{ rods.}\\ 6 \text{ days.}\\ \text{Gained 2 cts.}\\ 8629.30. \end{array}$	1. $492.319787.$ 2. $7462.31526.$ 3. $476.3380807.$ 4. $2.6591587.$ 5. $9710.27879.$ 6. $1.83586255.$ 7. $1764.06.$ 8. $\$776.423.$ 9. $21.5.2741_{1}^{5}.$ 10. $21.90267305.$ Art. 265. 1. $3.9803.$ 2. $2.6971.$ 3. $8999.1.$ 4. $4648.$ 5. $16.6736.$ 6. $010102.$	$\begin{array}{c} 6.82.0166_{3}^{*}, \\ 1061.1796_{3}^{*}, \\ 1061.1796_{3}^{*}, \\ 17.576; 432; 216; \\ 345.6, \\ 18.170845.86, \\ \hline {\it Art. 271.} \\ 1.048, \\ 2.250, \\ 3.104; 8.625, \\ 4.1.914; 2.82, \\ 5.875; 100.8, \\ 6.481.5; 385.2, \\ 7.4.25; 6.2, \\ 8.15.24706; \\ 2.25, \\ 9.49; 82.6875, \\ 10.5694; 39. \\ \end{array}$
14. 9. 32. 9 $\frac{1}{2}$ . 15. $6\frac{2}{632}$ . 33. 13. 16. $2\frac{1}{15}$ . 35. 13. 17. $2\frac{1}{1}$ . 35. 13. 18. $1\frac{3}{2}$ . 36. 23. 19. $\frac{9}{10}$ . 37. 33 $\frac{1}{3}$ . 20. $\frac{8}{15}$ . 38. 13 $\frac{3}{4}$ . 20. $\frac{8}{15}$ . 38. 13 $\frac{3}{4}$ . 20. $\frac{8}{15}$ . 38. 13 $\frac{3}{4}$ . 20. $\frac{8}{15}$ . $\frac{3}{15}$ . $\frac{11}{15}$ . 20. $\frac{8}{15}$ . $\frac{2}{15}$ . $\frac{11}{15}$ . 20. $\frac{8}{15}$ . $\frac{2}{15}$ . $\frac{11}{15}$ . 21. $\frac{4}{15}$ . 23. $\frac{4}{15}$ . 24. $\frac{4}{25}$ . 25. $\frac{4}{15}$ . 27. $\frac{1}{15}$ . 27. $\frac{1}{15}$ . 28. $\frac{4}{15}$ . 29. $\frac{1}{15}$ . 29. $\frac{1}{15}$ . 20. $\frac{1}{15}$ . 20. $\frac{1}{15}$ . 21. $\frac{1}{15}$ . 21. $\frac{1}{15}$ . 22. $\frac{4}{15}$ . 23. $\frac{1}{15}$ . 24. $\frac{1}{15}$ . 25. $\frac{1}{15}$ . 26. $\frac{1}{15}$ . 27. $$	39.         40.         41.         42.         43.         44.         45.         46.         47.         48.         49.         50.         51.         52.         53.	20191 $\frac{3}{4}$ ; 24348 $\frac{7}{4}$ . 31963 $\frac{3}{8}$ ; 18551 $7_{33}$ . 6224 $\frac{4}{5}$ ; 14241 $\frac{3}{4}$ . 19479 $\frac{7}{5}$ ; 84261 $\frac{1}{6}$ . $\frac{4}{6}$ . $\frac{8}{198.31}$ . 19744. $\frac{884.24}{27.80}$ . 76.66. 320 rods. 6 days. 6 days. 6 days. 6 days. 6 days. 85487.98.	$\begin{array}{c} 1.\ 492.31978.\\ 2.\ 7462.31526.\\ 3.\ 476.3850807.\\ 4.\ 2.6591587.\\ 5.\ 9710.27879.\\ 6.\ 1.83586255.\\ 7.\ 1764.06.\\ 8.\ \$776.423.\\ 9.\ 215.2741.\frac{5}{4.}.\\ 10.\ 21.90267305.\\ \hline {\it Art.\ 265.}\\ 1.\ 3.9808.\\ 2.\ .26971.\\ 3.\ 8999.1.\\ 4.\ 4648.\\ 5.\ 16.6736.\\ 6.\ .010102.\\ 7.\ \$86.17.\\ \end{array}$	$\begin{array}{c} 6.82.0166_{3}^{\circ}, \\ 1061.1796_{5}^{\circ}, \\ 1061.1796_{5}^{\circ}, \\ 17.576; 432; 216; \\ 345.6, \\ 18.170845.86, \\ \hline {\it Art. 271.} \\ 1.048, \\ 2.250, \\ 3.104; 8.625, \\ 4.1.914; 2.82, \\ 5.875; 100.8, \\ 6.481.5; 385.2, \\ 7.4.25; 6.2, \\ 8.15.24706; \\ 2.25, \\ 9.49; 82.6875, \\ 10.5694; 39, \\ 11.8, 66; \\ \end{array}$
14. 9. 32. 9 $\frac{1}{2}$ . 15. 6 $\frac{1}{2}$ , 32. 13. 16. 2 $\frac{1}{15}$ , 34. 46. 17. 2 $\frac{1}{2}$ , 35. 13. 18. 1 $\frac{1}{2}$ , 36. 23. 19. $\frac{1}{10}$ , 37. 33 $\frac{1}{3}$ , 39. 13 $\frac{1}{3}$ , 39. 13 $\frac{1}{3}$ , 39. 13 $\frac{1}{3}$ , 40. $\frac{1}{15}$ , $\frac{1}{15}$ , $\frac{1}{15}$ , $\frac{11}{12}$ , 42. $\frac{1}{4}$ ; $\frac{1}{4}$ ; $\frac{1}{7}$ ; $\frac{1}{15}$ , $\frac{1}{12}$ , 43. 2; 1 $\frac{1}{2}$ , 43. 2; 1 $\frac{1}{2}$ , 44. 2 $\frac{1}{4}$ ; $\frac{2}{4}$ ; $\frac{2}{5}$ ; $\frac{1}{5}$ . <b>Art. 237.</b> 1. $\frac{9}{15}$ , $\frac{1}{15}$ , $\frac{1}{15}$ , $\frac{1}{15}$ , $\frac{4}{15}$ , $\frac{1}{19}$ , 4 4. $\frac{1}{17}$ , $\frac{1}{182}$	39.         40.           41.         42.           43.         44.           45.         46.           47.         48.           49.         50.           51.         52.           53.         54.	20191 $\frac{3}{4}$ ; 24348 $\frac{7}{4}$ . 31963 $\frac{8}{5}$ ; 18551 $7\frac{5}{533}$ . 6224 $\frac{6}{5}$ ; 14241 $\frac{3}{45}$ . 19479 $\frac{7}{4}$ ; \$198.31. 19744. \$84.24. 27.80. 76.66. 320 rods. 6 days. Gained 2 cts. \$629.30. \$5487.98. 110 hm	1. $492.319787.$ 2. $7462.31526.$ 3. $476.3380807.$ 4. $2.6591587.$ 5. $9710.27879.$ 6. $1.83586255.$ 7. $1764.06.$ 8. $\$776.42\frac{7}{4}.$ 9. $215.2741\frac{6}{14}.$ 10. $21.9026730\frac{6}{5}.$ Art. 265. 1. $3.9808.$ 2. $2.6971.$ 3. $8999.1.$ 4. $4448.$ 5. $16.6736.$ 6. $.010102.$ 7. $\$86.17.$ 8. $2126155$	$\begin{array}{c} 5.0505q_{\star}\\ 5.0505q_{\star}\\ 16. 82.0166q_{\star}\\ 1061.1796q_{\star}\\ 17. 576; 432; 216; \\ 345.6. \\ 18. 170845.86. \\  \boldsymbol{Art. 271.}\\ 1048. \\ 2. 250. \\ 3. 104; 8.625. \\ 4. 1.914; 2.82. \\ 5875; 100.8. \\ 6. 481.5; 385.2. \\ 7. 4.25; 6.2. \\ 8. 15.24706; \\ 2.25. \\ 949; 82.6875. \\ 103604; 39. \\ 11. 18.66; \\ 10.30152 + \end{array}$
14. 9. 32. 9 $\frac{1}{2}$ . 15. 6 $\frac{2}{6}$ , 33. 13. 16. 2 $\frac{2}{16}$ , 35. 13. 16. 2 $\frac{2}{16}$ , 35. 13. 17. 21. 35. 13. 18. 1 $\frac{3}{2}$ , 36. 23. 19. $\frac{1}{90}$ , 37. 33 $\frac{1}{3}$ , 20. $\frac{1}{6}$ , 38. 13 $\frac{3}{2}$ . 39. 13 $\frac{1}{3}$ . 40. $\frac{1}{96}$ ; $\frac{2}{16}$ ; $\frac{1}{16}$ . 41. $\frac{5}{64}$ ; $\frac{6}{2}$ ; $\frac{1}{12}$ . 42. $\frac{5}{4}$ ; $\frac{6}{5}$ ; $\frac{1}{12}$ . 44. 2 $\frac{1}{2}$ ; $\frac{1}{2}$ . 44. 2 $\frac{1}{2}$ ; $\frac{1}{2}$ . 45. 635 $\frac{1}{2}$ ; $\frac{1}{3}$ . Art. 237. 1. $\frac{1}{16}$ . 3. $\frac{5819}{8}$ . 4. 17187. 5. 10218	39.         40.         41.         42.         43.         44.         45.         46.         47.         48.         49.         50.         51.         52.         53.         55.         55.	20191 $\frac{1}{3}$ ; 24348 $\frac{7}{5}$ . 31963 $\frac{3}{6}$ ; 185517 $\frac{5}{533}$ . 6224 $\frac{5}{5}$ ; 14241 $\frac{3}{6}$ . 19479 $\frac{4}{5}$ ; \$198.31. 19744. \$34.24. 27.80. 76.66. 320 rods. 6 days. Gained 2 cts. \$629.30. \$5487.98. 110 bu. eq 2 46	1. $492.319787.$ 2. $7462.31526.$ 3. $476.3380807.$ 4. $2.6591587.$ 5. $9710.27879.$ 6. $1.83586255.$ 7. $1764.06.$ 8. $\$776.42\frac{3}{4}.$ 9. $21.52741_{1}\frac{5}{2}.$ 10. $21.9026730\frac{5}{5}.$ Art. 265. 1. $3.9803.$ 2. $2.6971.$ 3. $8999.1.$ 4. $.4648.$ 5. $16.6736.$ 6. $0.10102.$ 7. $\$86.17.$ 8. $2.126155.$ 9. $1.7981$	$\begin{array}{c} 6.82.0166_{3}^{\circ};\\ 1061.1796_{3}^{\circ},\\ 1061.1796_{3}^{\circ},\\ 17.576; 432; 216;\\ 345.6,\\ 18.170845.86,\\ 000000000000000000000000000000000000$
14. 9. 32. 9 $\frac{1}{2}$ . 15. $6\frac{2}{6}\frac{2}{5}$ . 33. 13. 16. $2\frac{2}{16}$ . 34. 46. 17. 2 $\frac{1}{2}$ . 35. 13. 18. 1 $\frac{3}{2}$ . 36. 23. 19. $\frac{9}{10}$ . 37. 33 $\frac{1}{3}$ . 20. $\frac{8}{15}$ . 38. 13 $\frac{3}{2}$ . 20. $\frac{8}{15}$ . 37. 33 $\frac{1}{3}$ . 20. $\frac{8}{15}$ . $\frac{2}{15}$ . $\frac{11}{12}$ . 40. $\frac{9}{16}$ ; $\frac{9}{15}$ ; $\frac{11}{12}$ . 41. $\frac{6}{15}$ ; $\frac{9}{15}$ ; $\frac{11}{12}$ . 42. $\frac{8}{4}$ ; $\frac{9}{5}$ ; $\frac{1}{12}$ . 44. 2 $\frac{1}{4}$ ; 2. 45. 635 $\frac{1}{2}$ ; $\frac{1}{2}$ . Art. 237. 1. $\frac{9}{16}$ . 2. $\frac{48}{248}$ . 4. $\frac{17187}{2}$ . 5. 103 $\frac{138}{28}$ . 5. 103 $\frac{138}{28}$ .	39.         40.         41.         42.         43.         44.         45.         46.         47.         48.         49.         50.         51.         52.         53.         54.         55.	20191 $\frac{3}{4}$ ; 24348 $\frac{7}{4}$ . 31963 $\frac{3}{8}$ ; 18551 $7_{33}$ . 6224 $\frac{4}{5}$ ; 14241 $\frac{3}{4}$ . 19479 $\frac{7}{5}$ ; 84261 $\frac{1}{6}$ . 49198.31. 19744. \$84.24. 27.80. 76.66. 320 rods. 6 days. 6 days. 6 days. 6 days. 6 days. 6 days. 6 days. 95487.98. 110 bu. \$35.46.	1. $492.31978.$ 2. $7462.31526.$ 3. $476.3850807.$ 4. $2.6591587.$ 5. $9710.27879.$ 6. $1.83586255.$ 7. $1764.06.$ 8. $\$776.423.$ 9. $215.2741.$ 9. $21.90267305.$ Art. 265. 1. $3.9808.$ 2. $.26971.$ 3. $8999.1.$ 4. $.4648.$ 5. $16.6736.$ 6. $.010102.$ 7. $\$86.17.$ 8. $2.126155.$ 9. $1.728\frac{1}{2}.$ 1. $1.9141.41.$	$\begin{array}{c} 6.82.0166_{3}^{*}, \\ 1061.1796_{7}^{*}, \\ 1061.1796_{7}^{*}, \\ 17.576; 432; 216; \\ 345.6, \\ 18.170845.86, \\ \hline {\it Art. 271.} \\ 1.048, \\ 2.250, \\ 3.104; 8.625, \\ 4.1.914; 2.82, \\ 5.875; 100.8, \\ 6.481.5; 385.2, \\ 7.4.25; 6.2, \\ 8.15.24706; \\ 2.25, \\ 9.49; 82.6875, \\ 10.5694; 39, \\ 11.18.66; \\ 10.30152 +, \\ 12.272.02; 42, \\ 19.640, 60, 40, \\ 10.30152 +, \\ 19.660, \\ 10.660, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\ 10.60, \\$
14. 9. 32. 9 $\frac{1}{2}$ . 15. 6 $\frac{1}{8}$ , 32. 13. 16. 2 $\frac{1}{15}$ , 35. 13. 16. 2 $\frac{1}{15}$ , 35. 13. 17. 21. 35. 13. 18. 1 $\frac{1}{2}$ , 36. 23. 19. $\frac{1}{9}$ , 37. 33 $\frac{1}{3}$ , 39. 13 $\frac{1}{3}$ . 20. $\frac{1}{15}$ , $\frac{1}{95}$ ; $\frac{1}{15}$ ; $\frac{11}{15}$ . 40. $\frac{1}{95}$ ; $\frac{1}{95}$ ; $\frac{1}{15}$ ; $\frac{11}{15}$ . 40. $\frac{1}{95}$ ; $\frac{1}{95}$ ; $\frac{1}{15}$ . 44. $\frac{4}{24}$ ; $\frac{2}{5}$ ; $\frac{5}{5}$ . 44. $\frac{4}{24}$ ; 22. 45. 635 $\frac{1}{2}$ ; $\frac{1}{5}$ . Art. 237. 1. $\frac{9}{178}$ . 4. $\frac{1}{718}$ , $\frac{1}{5}$ . 5. 103 $\frac{1}{24}$ . 6. $862$ , $\frac{1}{72}$ .	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	20191 $\frac{3}{4}$ ; 24348 $\frac{7}{4}$ . 31963 $\frac{8}{5}$ ; 18551 $7\frac{5}{533}$ . 6224 $\frac{6}{5}$ ; 14241 $\frac{7}{16}$ . 19479 $\frac{7}{4}$ ; $\$192451\frac{1}{4}$ . $\$19479\frac{7}{4}$ ; \$198.31. 19744. \$84.24. \$7.80. 76.66. 320 rods. 6 days. Gained 2 cts. \$629.30. \$5487.98. 110 bu. \$35.46. \$35.46. \$136.99.	1. $492.319787.$ 2. $7462.31526.$ 3. $476.3380807.$ 4. $2.6591587.$ 5. $9710.27879.$ 6. $1.83586255.$ 7. $1764.06.$ 8. $\$776.42$ 9. $215.2741_{15}^{5}.$ 10. $21.9026730_{5}^{5}.$ Art. 265. 1. $3.9808.$ 2. $.26971.$ 3. $8999.1.$ 4. $.4648.$ 5. $16.6736.$ 6. $.010102.$ 7. $\$86.17.$ 8. $2.126155.$ 9. $1.728_{1.}^{4}.$ 10. $\$12.14\frac{1}{2}.$	$\begin{array}{c} 5.0505_{3};\\ 5.0505_{4};\\ 1061.1796_{5};\\ 17.576; 432; 216;\\ 345.6;\\ 18.170845.86;\\ \end{tabular}\\ \textbf{Art. 271.}\\ 1.048;\\ 2.250;\\ 3.104; 8.625;\\ 4.1914; 2.82;\\ 5.875; 100.8;\\ 6.481.5; 385.2;\\ 7.4.25; 6.2;\\ 8.15.24706;\\ 2.25;\\ 9.49; 82.6875;\\ 10,36152+,\\ 12.2722.02; 42;\\ 13.86.40; 69.12;\\ \end{array}$
14. 9. 32. 9 $\frac{1}{3}$ . 15. 6 $\frac{1}{6}\frac{1}{6}$ . 33. 13. 16. 2 $\frac{1}{7}$ . 5. 4. 46. 17. 21. 35. 13. 18. 1 $\frac{3}{2}$ . 36. 23. 19. $\frac{1}{70}$ . 37. 33 $\frac{1}{3}$ . 20. $\frac{1}{8}$ . 38. 13 $\frac{3}{7}$ . 30. 13 $\frac{1}{3}$ . 40. $\frac{1}{70}$ ; $\frac{1}{76}$ ; $\frac{1}{16}$ . 41. $\frac{1}{64}$ ; $\frac{3}{75}$ ; $\frac{5}{6}$ . 42. $\frac{3}{45}$ ; $\frac{6}{7}$ ; 1 $\frac{1}{2}$ . 44. 2 $\frac{1}{2}$ ; 2. 45. 635 $\frac{1}{2}$ ; $\frac{1}{3}$ . Art. 237. 1. $\frac{1}{76}$ . 2. $\frac{4}{85}$ . 3. $\frac{5}{8}$ . 4. 17187. 5. 193 $\frac{1}{24}$ . 6. 802 $\frac{7}{72}$ . 7. 3 $\frac{1}{3}$ .	39.         40.         41.         42.         43.         44.         45.         46.         47.         48.         49.         50.         51.         52.         53.         54.         55.         56.         57.	20191 $\frac{1}{3}$ ; 24348 $\frac{7}{5}$ . 31963 $\frac{8}{5}$ ; 185517 $\frac{5}{533}$ . 6224 $\frac{5}{5}$ ; 14241 $\frac{3}{76}$ . 19479 $\frac{4}{5}$ ; 84261 $\frac{1}{6}$ . 84261 $\frac{1}{6}$ . 8198.31. 19744. 884.24. 27.80. 76.66. 320 rods. 6 days. Gained 2 cts. \$629.30. \$5487.98. 110 bu. \$35.46. \$136.99. \$115.30.	1. $492.319787.$ 2. $7462.31526.$ 3. $476.3380807.$ 4. $2.6591587.$ 5. $9710.27879.$ 6. $1.83586255.$ 7. $1764.06.$ 8. $\$776.42\frac{5}{3}.$ 9. $215.2741.\frac{5}{5}.$ 10. $21.9026730\frac{5}{5}.$ Art. 265. 1. $3.9803.$ 2. $26971.$ 3. $8999.1.$ 4. $4648.$ 5. $16.6736.$ 6. $0.010102.$ 7. $\$86.17.$ 8. $2.126155.$ 9. $1.728\frac{1}{4}.$ 10. $\$1727.93\frac{1}{4}.$	$\begin{array}{c} 6.82.0166_{3}^{\circ};\\ 1061.1796_{3}^{\circ},\\ 17.576; 432; 216;\\ 345.6.\\ 18.170845.86.\\ \hline {\it Art. 271.}\\ 1.048,\\ 2.250,\\ 3.104; 8.625,\\ 4.1.914; 2.82,\\ 5.875; 100.8,\\ 6.481.5; 385.2,\\ 7.4.25; 6.2,\\ 8.15.24706;\\ 2.25,\\ 9.49; 82.6875,\\ 10.5694; 39,\\ 11.18.66;\\ 10.30152+,\\ 12.272.02; 42,\\ 13.86.40; 69.12;\\ 51.84; 138.24;\\ \end{array}$

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14	1800.	11.	1	17.	29341 sq. vd.		Art. 292
15	2790	10	176 977	10	3900 A		
10.	10	10	0	10.	954 Ja	1.	\$ 384.
10.	13.	10.	No.	19.	304 da.	2.	$\frac{7}{8}$ OZ.
17.	2.525.	14.	576.	20.	2160 eu. ft.	3.	$\frac{5}{6\pi}$ m.
18.	293.040015.	15.	5.	21.	42885d.	4	_3_ m
19.	.031: .121.	16.	$3\frac{1}{2}$ .	22.	982 da.	7.	320
20	162. 40	17	331 2	03	27782 lbs	0.	£120.
01	061, 06	10	@56 16	01	7599.1	0.	\$ 40.
41.	.007, .00.	10.	\$10.10.	44.	10000.	7.	<sup>b</sup> / <sub>9</sub> y.
22.	.023; .033.	19.	\$1070.		Ant DOF	8.	$\frac{3}{30}$ T.
23.	$.02\frac{1}{12}; .00\frac{4}{5}.$	20.	\$108.99.		ATL. 200.	9.	7 bu.
24.	$.14\frac{2}{7}; .41\frac{2}{8}.$	21.	\$143.06.	1.	£35 6s. 3d.	10.	£5
25.	\$361.60: \$452.	23.	\$42.07:	2.	75 ed. 83 eu. ft.	10.	~ 6 ·
26	\$10800		\$61.91	3	117 hu 2 nk		Art. 294.
~0.	¢ 10.95	01	@16.84 ·	0.	Mat.	1	£ 04375
any	\$10.00. \$10.00	24.	\$11 1/7	,	1007 1 1+	0	с T
21.	<b>\$30; \$0.0%</b> .	0-	<b>D</b> 11.17.	4.	1227 gal. 1 pt.	<i>A</i> .	.0 1.
28.	\$21600;	25.	\$28.98;	5.	27 yd. 1 ft. 3 m.	3.	£.920.
	\$10285.71.		\$32.30.	6.	7 mo. 6 da.	4.	£14.7875.
29.	\$200;	26.	\$108.22;	7.	2 mi. 235 rd.	5.	.90625 cd.
	\$153.125.		\$47.41.	8.	37 wk. 6 da. 15	6.	£247.7375.
30.	\$256000:	27.	\$67.76:		hr.	7.	.4 A.
	\$3555.56.		\$79.20.	9	2 hr 38 m 57 s	8.	£27.525.
21	13 560 .	08	\$25.09.	10	172 vd 11 in	9	\$166.56
01.	1027 647	20.	\$co.5c	11	055 15- MI	10	¢604 09
00	1001.0±1.	00	002.00. 000107 10	11.	200 105. 1a.	11	15- 453
3%.	4.024; 4.020.	29.	\$33107.12.	12.	329 yd.	11.	105. 4.00.
33.	1.403; 6.247.	30.	B, \$10542.48;	13.	8 T. 14 cwt.		Art. 296.
34.	1.728; 1.89.		C, D, E, each		16 lb.	1	005 7 103
35.	9.681; 414.881.		\$7028.32.	14.	50 yd. 9 in.	1.	200 /S. 100.
36.	142.105;	31.	\$31444.87.	15.	73 bu. 2 pk.	2.	69 T. 14 ewt.
	98.743.	32.	20338 A.;		3 at. 1 pt.		66 lb.
			R 2639 A .	16	094 172 64	3.	£460 7s. 6d.
					Transfer 1 4 S FM 1		
	Art. 274.		C 6763 A	17	33 A 36 sq ml	4.	12 y. 2 m. 16 d.
7	Art. 274.		D, $50\frac{40}{80}$ A.; C, $67\frac{63}{80}$ A.;	17.	33 A. 36 sq. rd.	4. 5.	12 y. 2 m. 16 d. 15 cd. 48 cu. ft.
1.	<i>Art.</i> 274. \$6. 2. \$34.	00	D, $50\frac{46}{50}$ A.; C, $67\frac{6}{50}$ A.; \$4575.66.	17. 17. 18.	234 175. 6d. 33 A. 36 sq. rd. 4 cwt. 63 lb.	4. 5. 6.	12 y. 2 m. 16 d. 15 cd. 48 cu. ft. 26 h. 46 m.
1. 3.	<i>Art. 274.</i> \$6. 2. \$34. \$48.13.	33.	D, $50\frac{46}{50}$ A.; C, $67\frac{63}{50}$ A.; \$4575.66. 7040 ft.	17. 17. 18.	234 175. 6d. 33 A. 36 sq. rd. 4 ewt. 63 lb. 10 oz.	4. 5. 6. 7.	12 y. 2 m. 16 d. 15 ed. 48 eu. ft. 26 h. 46 m. 37 bu. 5 ot.
1. 3. 4.	<i>Art. 274.</i> \$6. <i>2.</i> \$34. \$48.13. \$92.96.	33. 34.	D, $30\frac{1}{5}$ A.; C, $67\frac{6}{5}$ A.; \$4575.66. 7040 ft. Wife, $$48500$ ;	10. 17. 18.	234 115. 0d. 33 A. 36 sq. rd. 4 ewt. 63 lb. 10 oz. 68 cd. 12 cu. ft.	4. 5. 6. 7. 8	12 y. 2 m. 16 d. 15 cd. 48 cu. ft. 26 h. 46 m. 37 bu. 5 qt. 27 yd. 4 in
1. 3. 4. 5.	Art. 274. \$6. 2. \$34. \$48.13. \$92.96. \$312.	33. 34.	D, 3046 A.; C, 6758 A.; \$4575.66. 7040 ft. Wife, \$48500; Son, \$36375;	10. 17. 18. 19. 20.	234 115. 6d. 33 A. 36 sq. rd. 4 cwt. 63 lb. 10 oz. 68 cd. 12 cu. ft. £20 2s. 5d.	4. 5. 6. 7. 8. 9	12 y. 2 m. 16 d. 15 cd. 48 cu. ft. 26 h. 46 m. 37 bu. 5 qt. 27 yd. 4 in. 10 lb. 2 pwt
1. 3. 4. 5. 6.	Art. 274. \$6. 2. \$34. \$48.13. \$92.96. \$312. \$5.44.	33. 34.	D, $50\frac{10}{58}$ A.; C, $67\frac{6}{58}$ A.; \$4575.66. 7040 ft. Wife, $\$48500;$ Son, $\$36375;$ Daughter,	10. 17. 18. 19. 20.	233 A. 36 sq. rd. 33 A. 36 sq. rd. 4 cwt. 63 lb. 10 oz. 68 cd. 12 cu. ft. £20 2s. 5d.	4. 5. 6. 7. 8. 9.	12 y. 2 m. 16 d. 15 ed. 48 eu. ft. 26 h. 46 m. 37 bu. 5 qt. 27 yd. 4 in. 10 lb. 2 pwt. 20 cr
1. 3. 4. 5. 6. 7.	Art. 274. \$6. 2. \$34. \$48.13. \$92.96. \$312. \$5.44. \$114.58.	33. 34.	$\begin{array}{c} \text{D, } 50^{+}_{55} \text{ A.};\\ \text{C, } 67^{+}_{58} \text{ A.};\\ \$4575.66.\\ 7040 \text{ ft.}\\ \text{Wife, } \$48500;\\ \text{Son, } \$36375;\\ \text{Daughter,}\\ \$24250; \end{array}$	10. 17. 18. 19. 20.	233 1.3, 60. 33 A. 36 sq. rd. 4 ewt. 63 lb. 10 oz. 68 cd. 12 cu. ft. £20 2s. 5d. Art. 288.	4. 5. 6. 7. 8. 9.	12 y, 2 m, 16 d, 15 cd, 48 cu, ft, 26 h, 46 m, 37 bu, 5 qt, 27 yd, 4 in, 10 lb, 2 pwt, 20 gr, 194 cu, 9 ct
1. 3. 4. 5. 6. 7. 8.	Art. 274. \$6. 2. \$34. \$48.13. \$92.96. \$312. \$5.44. \$114.58. \$102.24.	33. 34.	$\begin{array}{c} \text{D, } 50^{+}_{56} \text{ A.};\\ \text{C, } 67^{+}_{58} \text{ A.};\\ \text{$4575.66.}\\ \text{7040 ft.}\\ \text{Wife, $48500;}\\ \text{Son, $36375;}\\ \text{Daughter,}\\ \text{$24250;}\\ \text{Total, $145500.} \end{array}$	10. 17. 18. 19. 20.	233 A. 36 sq. rd. 33 A. 36 sq. rd. 4 cwt. 63 lb. 10 oz. 68 cd. 12 cu. ft. £20 2s. 5d. Art. 288. 135d.	4. 5. 6. 7. 8. 9. 10.	12 y. 2 m. 16 d. 15 cd. 48 cu. ft. 26 h. 46 m. 37 bu. 5 qt. 27 yd. 4 in. 10 lb. 2 pwt. 20 gr. 124 gal. 2 qt.
1. 3. 4. 5. 6. 7. 8. 9.	Art. 274. \$6. 2. \$34. \$48.13. \$92.96. \$312. \$5.44. \$114.58. \$102.24. \$280.64.	33. 34. 35.	D, $00^{+}_{5}$ A.; C, $67^{+}_{5}$ A.; \$4575.66. 7040 ft. Wife, $$48500;$ Son, $$36375;$ Daughter, \$24250; Total, $$145500.$ \$1065.	10. 17. 18. 19. 20.	23 A. 36 sq. rd. 33 A. 36 sq. rd. 4 cwt. 63 lb. 10 oz. 68 cd. 12 cu. ft. £20 2s. 5d. Art. 288. 135d. 13s. 9d.	4. 5. 6. 7. 8. 9. 10. 11.	$\begin{array}{c} 12 \ y, \ 2 \ m, \ 16 \ d, \\ 15 \ cd, \ 48 \ cu, \ ft, \\ 26 \ h, \ 46 \ m, \\ 37 \ bu, \ 5 \ qt, \\ 27 \ yd, \ 4 \ in, \\ 10 \ lb, \ 2 \ pwt, \\ 20 \ gr, \\ 124 \ gal, \ 2 \ qt, \\ \pounds 205 \ 12s, \ 5d, \end{array}$
1. 3. 4. 5. 6. 7. 8. 9. 10	Art. 274. \$6. 2. \$34. \$48.13. \$02.96. \$312. \$5.44. \$114.58. \$102.24. \$280.64. \$164.44.	33. 34. 35.	D, 00 <sup>+</sup> 5 A.; C, 67 <sup>+</sup> 8 A.; \$4575.66. 7040 ft. Wife, \$48500; Son, \$36375; Daughter, \$24250; Total, \$145500. \$1065. \$4.63.	10. 17. 18. 19. 20. 1. 2. 3.	<ul> <li>23 A. 36 sq. rd.</li> <li>33 A. 36 sq. rd.</li> <li>4 cwt. 63 lb.</li> <li>10 oz.</li> <li>68 cd. 12 cu. ft.</li> <li>£20 2s. 5d.</li> <li>Art. 288.</li> <li>135. 9d.</li> <li>1980 ft.</li> </ul>	4. 5. 6. 7. 8. 9. 10. 11. 12.	12 y, 2 m, 16 d, 15 cd, 48 cu, ft, 26 h, 46 m, 37 bu, 5 qt, 27 yd, 4 in, 10 lb, 2 pwt, 20 gr, 124 gal, 2 qt, £205 128, 5d, £546 18, 7d,
1. 3. 4. 5. 6. 7. 8. 9. 10.	Art. 274. \$6. 2. \$34. \$48.13. \$92.96. \$312. \$5.44. \$114.58. \$102.24. \$280.64. \$164.64. \$16.39.	33. 34. 35. 36.	b), $00_{10}^{+0}$ A.; C, $67_{88}^{+0}$ A.; 84575.66. 7040 ft. Wife, $848500$ ; Son, $836375$ ; Daughter, \$24250; Total, $$145500$ . \$1065. \$4.63. 1100 bu.	10. 17. 18. 19. 20. 1. 2. 3.	233 A. 36 sq. rd. 33 A. 36 sq. rd. 4 cwt. 63 lb. 10 oz. 68 cd. 12 cu. ft. £20 2s. 5d. Art. 288. 135d. 135d. 138s. 9d. 1980 ft. 496 lbs	4. 5. 6. 7. 8. 9. 10. 11. 12.	12 y. 2 m. 16 d. 15 cd. 48 cu. ft. 26 h. 46 m. 37 bu. 5 qt. 27 yd. 4 in. 10 lb. 2 pwt. 20 gr. 124 gal. 2 qt. £205 125. 5d. £546 15. 7d.
1. 3. 4. 5. 6. 7. 8. 9. 10. 11. 19.	Art. 274. \$6. 2. \$34. \$48.13. \$92.96. \$312. \$5.44. \$114.58. \$102.24. \$280.64. \$164.84. \$164.84. \$16.32. \$12.40	33. 34. 35. 36. 37.	D, $00^{+}_{55}$ A.; C, $67^{+}_{58}$ A.; 4575.66. 7040 ft. Wife, $48500$ ; Son, $336375$ ; Daughter, \$24250; Total, $$145500$ . \$1065. \$4.63. 1100 bu.	10. 17. 18. 19. 20. 1. 2. 3. 4. 5	233 A. 36 sq. rd. 33 A. 36 sq. rd. 4 cwt. 63 lb. 10 oz. 68 cd. 12 cu. ft. £20 2s. 5d. Art. 288. 135d. 13s. 9d. 1980 ft. 496 lbs. 15s. 5d	4. 5. 6. 7. 8. 9. 10. 11. 12.	12 y. 2 m. 16 d. 15 cd. 48 cu. ft. 26 h. 46 m. 37 bu. 5 qt. 27 yd. 4 in. 10 lb. 2 pwt. 20 gr. 124 gal. 2 qt. £205 12s. 5d. £546 1s. 7d. Art. 298.
$ \begin{array}{c} 1. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 9. \\ 10. \\ 11. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\ 12. \\$	Art. 274. \$6. 2. \$34. \$48.13. \$92.96. \$312. \$5.44. \$114.58. \$102.24. \$280.64. \$164.04. \$16.32. \$12.40. \$12.40.	33. 34. 35. 36. 37.	D, 00 <sup>45</sup> A.; C, 67 <sup>48</sup> A.; \$4575.66. 7040 ft. Wife, \$48500; Son, \$36375; Daughter, \$24250; Total,\$145500. \$1065. \$4.63. 1100 bu. Art. 282.	10. 17. 18. 19. 20. 1. 2. 3. 4. 5.	23 A. 36 sq. rd. 33 A. 36 sq. rd. 4 cwt. 63 lb. 10 oz. 68 cd. 12 cu. ft. £20 2s. 5d. Art. 288. 135d. 138. 9d. 1980 ft. 496 lbs. 15s. 5d. 19 at	4. 5. 6. 7. 8. 9. 10. 11. 12.	12 y. 2 m. 16 d. 15 cd. 48 cu. ft. 26 h. 46 m. 37 bu. 5 qt. 27 yd. 4 in. 10 lb. 2 pwt. 20 gr. 124 gal. 2 qt. £205 12s. 5d. £546 1s. 7d. <b>Art. 298.</b> £88 4s. 2d.
$\begin{array}{c} 1.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 11.\\ 12.\\ 13.\\ 1.\\ 13.\\ 1.\\ 12.\\ 13.\\ 1.\\ 12.\\ 13.\\ 1.\\ 12.\\ 13.\\ 1.\\ 1.\\ 12.\\ 13.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1$	Art. 274. \$6. 2. \$34. \$92.96. \$312. \$5.44. \$114.58. \$102.24. \$280.64. \$164.64. \$164.64. \$16.32. \$12.40. \$12.40. \$12.40. \$12.40.	33. 34. 35. 36. 37.	D, 00 <sup>45</sup> A.; \$4575.66. 7040 ft. Wife, \$48500; Son, \$36375; Daughter, \$24250; Total, \$145500. \$1065. \$4.63. 1100 bu. Art. 282. 0296 l	10. 17. 18. 19. 20. 1. 2. 3. 4. 5. 6.	233 A. 36 sq. rd. 33 A. 36 sq. rd. 4 cwt. 63 lb. 10 oz. 68 cd. 12 cu. ft. £20 2s. 5d. Art. 288. 135d. 138. 9d. 1980 ft. 496 lbs. 15s. 5d. 13 pts.	4. 5. 6. 7. 8. 9. 10. 11. 12.	12 y. 2 m. 16 d. 15 cd. 48 cu. ft. 26 h. 46 m. 37 bu. 5 qt. 27 yd. 4 in. 10 lb. 2 pwt. 20 gr. 124 gal. 2 qt. £205 128. 5d. £546 18. 7d. Art. 298. £88 48. 2d. £21 48. 4d.
$\begin{array}{c} 1.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 11.\\ 12.\\ 13.\\ 14.\\ \end{array}$	Art. 274. \$6. 2. \$34. \$48.13. \$92.96. \$312. \$5.44. \$102.24. \$102.24. \$102.24. \$102.24. \$102.24. \$103.24. \$16.32. \$12.40. \$15.75. \$38.75. \$38.75. \$38.75. \$38.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$39.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30.75. \$30	33. 34. 35. 36. 37. 1.	D, 00 <sup>+</sup> 5 A.; C, 67 <sup>+</sup> 8 A.; §4575.66. 7040 ft. Wife, \$48500; Son, \$36375; Daughter, \$24250; Total,\$145500. \$1065. \$4.63. 1100 bu. Art. 282. 2326d.	$ \begin{array}{c} 10. \\ 17. \\ 17. \\ 18. \\ 19. \\ 20. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 7. \\ 8. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 7. \\ 8. \\ 1. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 1. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 1. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 1. \\ 1. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 1. \\ 1. \\ 1. \\ 1. \\ 1. \\ 1. \\ 1. \\ 1$	233 A. 36 sq. rd. 33 A. 36 sq. rd. 4 cwt. 63 lb. 10 oz. 68 cd. 12 cu. ft. £20 2s. 5d. Art. 288. 135d. 13s. 9d. 1980 ft. 496 lbs. 15s. 5d. 13 pts. 4785 ft.	4. 5. 6. 7. 8. 9. 10. 11. 12. 1. 2. 3.	$\begin{array}{c} 12 \text{ y}, 2 \text{ m}, 16 \text{ d}, \\ 15 \text{ cd}, 48 \text{ eu}, \text{ ft}, \\ 26 \text{ h}, 46 \text{ m}, \\ 37 \text{ bu}, 5 \text{ qt}, \\ 27 \text{ yd}, 4 \text{ in}, \\ 10 \text{ lb}, 2 \text{ pwt}, \\ 20 \text{ gr}, \\ 124 \text{ gal}, 2 \text{ qt}, \\ \pounds 205 128, 5d, \\ \pounds 546 18, 7d, \\ \textbf{Art. 298.} \\ \pounds 88 48, 2d, \\ \pounds 21 48, 4d, \\ \pounds 3 148, 3d, \\ \end{array}$
$\begin{array}{c} 1.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 11.\\ 12.\\ 13.\\ 14.\\ 15. \end{array}$	Art. 274. \$6. 2. \$34. \$48.13. \$92.96. \$312. \$5.44. \$114.58. \$102.24. \$280.64. \$164.32. \$12.40. \$15.75. \$287.5. \$242.10.	33. 34. 35. 36. 37. 1. 2.	D, 00 <sup>45</sup> A.; C, 67 <sup>2</sup> / <sub>8</sub> A.; \$4575.66. 7040 ft. Wife, \$48500; Son, \$36375; Daughter, \$24250; Total,\$145500. \$1065. \$4.63. 1100 bu. Art. 282. 2326d. 220 gills.	10. 17. 18. 19. 20. 1. 2. 3. 4. 5. 6. 7. 8.	23 A. 36 sq. rd. 33 A. 36 sq. rd. 4 cwt. 63 lb. 10 oz. 68 cd. 12 cu. ft. £20 2s. 5d. Art. 288. 135d. 138. 9d. 1980 ft. 496 lbs. 15s. 5d. 13 pts. 4785 ft. 87 lbs. 8 oz.	4. 5. 6. 7. 8. 9. 10. 11. 12. 1. 2. 3. 4.	$\begin{array}{c} 12 \text{ y}, 2 \text{ m}, 16 \text{ d}, \\ 15 \text{ cd}, 48 \text{ cu}, \text{ ft}, \\ 26 \text{ h}, 46 \text{ m}, \\ 37 \text{ bu}, 5 \text{ qt}, \\ 27 \text{ yd}, 4 \text{ in}, \\ 10 \text{ lb}, 2 \text{ pwt}, \\ 20 \text{ gr}, \\ 124 \text{ gal}, 2 \text{ qt}, \\ \pounds 205 \text{ 12s}, 5d, \\ \pounds 546 \text{ 1s}, 7d, \\ \textbf{Art. 298.} \\ \pounds 88 \text{ 4s}, 2d, \\ \pounds 21 \text{ 4s}, 4d, \\ \pounds 21 \text{ 4s}, 4d, \\ \pounds 23 \text{ 14s}, 3d, \\ \pounds 28 \text{ 13s}, 10d, \\ \end{array}$
$\begin{array}{c} 1. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 9. \\ 10. \\ 11. \\ 12. \\ 13. \\ 14. \\ 15. \\ 16. \end{array}$	Art. 274. \$6. 2. \$34. \$48.13. \$92.96. \$312. \$5.44. \$114.58. \$102.24. \$280.64. \$164.064. \$16.32. \$12.40. \$15.75. \$38.75. \$242.10. \$16.50.	33. 34. 35. 36. 37. 1. 2. 3.	D, 00 <sup>+</sup> 5 A.; \$4575.66. 7040 ft. Wife, \$48500; Son, \$36375; Daughter, \$24250; Total, \$145500. \$1065. \$4.63. 1100 bu. Art. 282. 2326d. 220 gills. 108404 f.	10. 17. 18. 19. 20. 1. 2. 3. 4. 5. 6. 7. 8. 9.	$\begin{array}{c} \textbf{234.3}\\ \textbf{334.3}\\ \textbf{68 cd. 12 cu. ft.}\\ \textbf{10 oz.}\\ \textbf{68 cd. 12 cu. ft.}\\ \textbf{£20 2s. 5d.}\\ \textbf{Art. 288.}\\ \textbf{135.9d.}\\ \textbf{135.9d.}\\ \textbf{1980 ft.}\\ \textbf{496 lbs.}\\ \textbf{15s. 5d.}\\ \textbf{13 pts.}\\ \textbf{4785 ft.}\\ \textbf{87 lbs. 8 oz.}\\ \textbf{5\frac{1}{2} pts.}\\ \textbf{9ts.}\\ \end{array}$	4. 5. 6. 7. 8. 9. 10. 11. 12. 3. 4. 5.	12 y, 2 m, 16 d, 15 cd, 48 cu, ft, 26 h, 46 m, 37 bu, 5 qt, 27 yd, 4 in, 10 lb, 2 pwt, 20 gr, 124 gal, 2 qt, £205 128, 5d, £546 18, 7d, <b>Art. 298.</b> £88 48, 2d, £21 48, 4d, £3 148, 3d, £23 138, 10d, 4 y, 3 m, 2 d,
$\begin{array}{c} 1.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 11.\\ 12.\\ 13.\\ 14.\\ 15.\\ 16.\\ 17. \end{array}$	Art. 274. \$6. 2. \$34. \$48.13. \$92.96. \$312. \$5.44. \$114.58. \$102.24. \$280.64. \$16.404. \$15.75. \$38.75. \$242.10. \$16.50. \$198.40.	33. 34. 35. 36. 37. 1. 2. 3. 4.	D, 00 <sup>+</sup> 5 A.; C, 67 <sup>+</sup> 8 A.; §4575.66. 7040 ft. Wife, \$48500; Son, \$36375; Daughter, \$24250; Total, \$145500. \$1065. \$4.63. 1100 bu. <b>Art. 282.</b> 2326d. 220 gills. 108404 f. 13265 lb.	10. 17. 18. 19. 20. 1. 2. 3. 4. 5. 6. 7. 8. 9. 10.	233 A. 36 sq. rd. 33 A. 36 sq. rd. 4 ewt. 63 lb. 10 oz. 68 cd. 12 cu. ft. $\pounds 20$ 2s. 5d. Art. 288. 135d. 13s. 9d. 1980 ft. 496 lbs. 15s. 5d. 13 pts. 4785 ft. 87 lbs. 8 oz. $5\frac{1}{2}$ pts. 104 cu. ft.	4. 5. 6. 7. 8. 9. 10. 11. 12. 3. 4. 5. 6.	12 y, 2 m, 16 d, 15 cd, 48 cu, ft, 26 h, 46 m, 37 bu, 5 qt, 27 yd, 4 in, 10 lb, 2 pwt, 20 gr, 124 gal, 2 qt, £205 12s, 5d, £546 1s, 7d, Art. 298. £88 4s, 2d, £21 4s, 4d, £3 14s, 3d, 4 y, 3 m, 2 d, 4 y, 4 m, 22 d,
$\begin{array}{c} 1.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 11.\\ 12.\\ 13.\\ 14.\\ 15.\\ 16.\\ 17. \end{array}$	Art. 274. \$6. 2. \$34. \$48.13. \$92.90. \$312. \$14.58. \$102.24. \$104.04. \$16.32. \$12.40. \$15.75. \$38.75. \$242.10. \$16.50. \$198.40.	33. 34. 35. 36. 37. 1. 2. 3. 4. 5.	D, $00^{+}_{5}$ A.; $(2, 67^{+}_{5}$ A.; \$4575.66. 7040 ft. Wife, $$48500$ ; Son, $$36375$ ; Daughter, \$24250; Total, $$145500.$ \$1065. \$4.63. 1100 bu. <i>Art. 282.</i> 2326d. 220 gills. 108404 f. 13265 lb. 256 days.	10. 17. 18. 19. 20. 1. 2. 3. 4. 5. 6. 7. 8. 9. 10.	23 A. 36 sq. rd. 33 A. 36 sq. rd. 4 cwt. 63 lb. 10 oz. 68 cd. 12 cu. ft. £20 2s. 5d. Art. 288. 135d. 13s. 9d. 1980 ft. 496 lbs. 15s. 5d. 13 pts. 4785 ft. 87 lbs. 8 oz. 5½ pts. 104 cu. ft.	4. 5. 6. 7. 8. 9. 10. 11. 12. 1. 2. 3. 4. 5. 6. 7	12 y, 2 m, 16 d, 15 cd, 48 cu, ft, 26 h, 46 m, 37 bu, 5 qt, 27 yd, 4 in, 10 lb, 2 pwt, 20 gr, 124 gal, 2 qt, $\pounds 205$ 128, 5d, $\pounds 546$ 18, 7d, <b>Art. 298.</b> $\pounds 88$ 48, 2d, $\pounds 21$ 48, 4d, $\pounds 3$ 148, 3d, $\pounds 23$ 138, 10d, 4 y, 3 m, 2 d, 4 y, 4 m, 22 d, 6 m, 10 d
$\begin{array}{c} 1.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 11.\\ 12.\\ 13.\\ 14.\\ 15.\\ 16.\\ 17. \end{array}$	Art. 274. \$6. 2. \$34. \$48.13. \$02.96. \$312. \$5.44. \$114.58. \$102.24. \$280.64. \$164.32. \$12.40. \$15.75. \$38.75. \$38.75. \$38.75. \$38.40. Art. 275.	33. 34. 35. 36. 37. 1. 2. 3. 4. 5. 6.	D, 00 <sup>+</sup> 5 A.; \$4575.66. 7040 ft. Wife, \$48500; Son, \$36375; Daughter, \$24250; Total, \$145500. \$1065. \$4.63. 1100 bu. Art. 282. 2326d. 2326d. 2320 gills. 108404 f. 13265 lb. 256 days. 18211d.	10. 17. 18. 19. 20. 1. 2. 3. 4. 5. 6. 7. 8. 9. 10.	23 A. 36 sq. rd. 33 A. 36 sq. rd. 4 ewt. 63 lb. 10 oz. 68 cd. 12 eu. ft. £20 2s. 5d. Art. 288. 135d. 138. 9d. 1080 ft. 496 lbs. 15s. 5d. 13 pts. 4785 ft. 87 lbs. 8 oz. $5\frac{1}{2}$ pts. 104 cu. ft. Art. 290.	4. 5. 6. 7. 8. 9. 10. 11. 12. 1. 2. 3. 4. 5. 6. 7. 8	12 y, 2 m, 16 d, 15 cd, 48 cu, ft, 26 h, 46 m, 37 bu, 5 qt, 27 yd, 4 in, 10 lb, 2 pwt, 20 gr, 124 gal, 2 qt, $\pounds$ 205 128, 5d, $\pounds$ 546 18, 7d, <b>Art. 298.</b> $\pounds$ 88 48, 2d, $\pounds$ 21 48, 4d, $\pounds$ 23 148, 3d, $\pounds$ 23 148, 3d, $\pounds$ 23 148, 3d, $\pounds$ 23 148, 2d, $\pounds$ 23 2d, 4 y, 4 m, 22 d, 6 m, 10 d, 2 y, 6 m, 24 d,
$\begin{array}{c} 1.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 11.\\ 12.\\ 13.\\ 14.\\ 15.\\ 16.\\ 17.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1$	Art. 274. \$6. 2. \$34. \$92.96. \$312. \$5.44. \$114.58. \$102.24. \$164.64. \$164.64. \$1632. \$12.40. \$15.75. \$38.75. \$242.10. \$16.50. \$198.40. Art. 275. .1651386.	33. 34. 35. 36. 37. 1. 2. 3. 4. 5. 6. 7	D, 00 <sup>45</sup> A.; C, 07 <sup>48</sup> A.; \$4575.66. 7040 ft. Wife, \$48500; Son, \$36375; Daughter, \$24250; Total, \$145500. \$1065. \$4.63. 1100 bu. Art. 282. 2326d. 2320 gills. 108404 f. 13265 lb. 256 days. 18211d. 235923 f.	10.         17.         18.         19.         20.         1.         2.         3.         4.         5.         6.         7.         8.         9.         10.         1	233 A. 36 sq. rd. 33 A. 36 sq. rd. 4 ewt. 63 lb. 10 oz. 68 ed. 12 eu. ft. £20 2s. 5d. Art. 288. 135d. 135d. 138. 9d. 1980 ft. 496 lbs. 15s. 5d. 13 pts. 4785 ft. 87 lbs. 8 oz. $5\frac{1}{2}$ pts. 104 cu. ft. Art. 290. 150d.	4. 5. 6. 7. 8. 9. 10. 11. 12. 3. 4. 5. 6. 7. 8.	$\begin{array}{c} 12 \ y, \ 2 \ m, \ 16 \ d, \\ 15 \ cd, \ 48 \ cu, \ ft. \\ 26 \ h, \ 46 \ m, \\ 37 \ bu, \ 5 \ qt. \\ 27 \ yd. \ 4 \ m, \\ 10 \ lb, \ 2 \ pwt. \\ 20 \ gr. \\ 124 \ gal. \ 2 \ qt. \\ 4205 \ 128, \ 5d. \\ \pounds 205 \ 128, \ 5d. \ 128, \ 5d. \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, \ 128, $
$\begin{array}{c} 1. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 9. \\ 10. \\ 12. \\ 13. \\ 4. \\ 15. \\ 17. \\ 1. \\ 2\end{array}$	Art. 274. \$6. 2. \$34. \$48.13. \$92.96. \$312. \$5.44. \$114.58. \$102.24. \$280.64. \$16.32. \$12.40. \$15.75. \$38.75. \$242.10. \$16.50. \$198.40. Art. 275. .1651386. 289.862432.	33. 34. 35. 36. 37. 1. 2. 3. 4. 5. 6. 7. 8	D, $00^{+}_{15}$ A.; $(2, 67^{+}_{28}$ A.; $(3, 57^{+}_{28}$ A.;	10. 17. 18. 19. 20. 1. 2. 3. 4. 5. 6. 7. 8. 9. 10. 10. 2. 10. 2. 10. 2. 10. 2. 10. 2. 10. 2. 10. 2. 10. 2. 10. 2. 10. 2. 10. 2. 10. 2. 10. 2. 10. 2. 10. 10. 10. 10. 10. 10. 10. 10	23 A. 36 sq. rd. 33 A. 36 sq. rd. 10 oz. 68 cd. 12 cu. ft. $\pm 20$ 2s. 5d. Art. 288. 135d. 135d. 135d. 135d. 135s. 9d. 1980 ft. 496 lbs. 15s. 5d. 13 pts. 4785 ft. 87 lbs. 8 oz. $5\frac{1}{2}$ pts. 104 cu. ft. Art. 290. 150d. 17s. 6d.	4. 5. 6. 7. 8. 9. 10. 11. 12. 3. 4. 5. 6. 7. 8. 8.	12 y, 2 m, 16 d, 15 cd, 48 cu, ft, 26 h, 46 m, 37 bu, 5 qt, 27 yd, 4 in, 10 lb, 2 pwt, 20 gr, 124 gal, 2 qt, $\pounds 205$ 128, 5d, $\pounds 546$ 18, 7d, <b>Art.</b> 298. $\pounds 84$ 8s, 2d, $\pounds 21$ 4s, 4d, $\pounds 3$ 148, 3d, $\pounds 23$ 138, 10d, 4 y, 3 m, 2 d, 4 y, 4 m, 22 d, 6 m, 10 d, 2 y, 6 m, 24 d, <b>Art.</b> 300.
$\begin{array}{c} 1. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 9. \\ 10. \\ 112. \\ 13. \\ 4. \\ 15. \\ 16. \\ 17. \\ 1. \\ 2. \\ 2\end{array}$	Art. 274. \$6. 2. $$34.$92.96.$512.$5.44.$114.58.$102.24.$280.64.$164.04.$16.32.$12.40.$15.75.$38.75.$242.10.$16.50.$198.40.Art. 275..1651386.289.3624\frac{2}{2}9.$12.55.$	33. 34. 35. 36. 37. 1. 2. 3. 4. 5. 6. 7. 8. 0	D, 00 <sup>45</sup> A.; (C, 67 <sup>48</sup> A.; \$4575.66. 7040 ft. Wife, \$48500; Son, \$36375; Daughter, \$24250; Total,\$145500. \$1065. \$4.63. 1100 bu. Art. 282. 2326d. 220 gills. 108404 f. 13265 lb. 256 days. 18211d. 235923 f. 1566 qt. 14948 lbs	10. 17. 18. 19. 20. 1. 2. 3. 4. 5. 6. 7. 8. 9. 10. 1. 2. 2. 3. 4. 5. 6. 7. 8. 9. 10. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2	23 A. 36 sq. rd. 33 A. 36 sq. rd. 4 cwt. 63 lb. 10 oz. 68 cd. 12 cu. ft. £20 2s. 5d. Art. 288. 135d. 138. 9d. 1980 ft. 496 lbs. 15s. 5d. 13 pts. 4785 ft. 87 lbs. 8 oz. 5½ pts. 104 cu. ft. Art. 290. 158d. 17s. 6d. 158d	4. 5. 6. 7. 8. 9. 10. 11. 12. 3. 4. 5. 6. 7. 8. 9.	12 y, 2 m, 16 d, 15 cd, 48 cu, ft, 26 h, 46 m, 37 bu, 5 qt, 27 yd, 4 in, 10 lb, 2 pwt, 20 gr, 124 gal, 2 qt, $\pounds 205$ 128, 5d, $\pounds 546$ 18, 7d, <b>Art. 298.</b> $\pounds 88$ 48, 2d, $\pounds 21$ 48, 4d, $\pounds 23$ 148, 3d, $\pounds 23$ 148, 3d, $\pounds 23$ 138, 10d, 4 y, 3 m, 2 d, 4 y, 4 m, 22 d, 6 m, 10 d, 2 y, 6 m, 24 d, <b>Art. 300.</b> $\pounds 122$ 148, 8d
$\begin{array}{c} 1.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 11.\\ 13.\\ 14.\\ 15.\\ 16.\\ 17.\\ 1.\\ 2.\\ 3.\\ 1.\\ 1.\\ 2.\\ 3.\\ 1.\\ 1.\\ 1.\\ 2.\\ 3.\\ 1.\\ 1.\\ 2.\\ 3.\\ 1.\\ 1.\\ 1.\\ 1.\\ 2.\\ 3.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1$	Art. 274. \$6. 2. \$34. \$52.96. \$312. \$5.44. \$114.58. \$102.24. \$102.24. \$164.64. \$164.64. \$16.32. \$12.40. \$15.75. \$38.75. \$242.10. \$16.50. \$198.40. Art. 275. .1651386. $289.3624\frac{2}{2}9.$ .8125. 158.9162	33. 34. 35. 36. 37. 1. 2. 3. 4. 5. 6. 7. 8. 9.	D, 00 <sup>+</sup> 5 A.; \$4575.66. 7040 ft. Wife, \$48500; Son, \$36375; Daughter, \$24250; Total, \$145500. \$1065. \$4.63. 1100 bu. Art. 282. 2326d. 2326d. 2320 gills. 108404 f. 13265 lb. 256 days. 18211d. 235923 f. 1566 qt. 14948 lbs.	10. 17. 18. 19. 20. 1. 2. 3. 4. 5. 6. 7. 8. 9. 10. 1. 2. 3. 4. 5. 6. 7. 8. 9. 10. 10. 10. 10. 10. 10. 10. 10	23 A. 36 sq. rd. 33 A. 36 sq. rd. 4 ewt. 63 lb. 10 oz. 68 cd. 12 eu. ft. £20 2s. 5d. Art. 288. 135. 9d. 1080 ft. 496 lbs. 15s. 5d. 13 pts. 4785 ft. 87 lbs. 8 oz. $5\frac{1}{2}$ pts. 104 cu. ft. Art. 290. 150d. 17s. 6d. 13s. 8d.	4. 5. 6. 7. 8. 9. 10. 11. 12. 3. 4. 5. 6. 7. 8. 9. 1.	12 y. 2 m. 16 d. 15 cd. 48 cu. ft. 26 h. 46 m. 37 bu. 5 qt. 27 yd. 4 in. 10 lb. 2 pwt. 20 gr. 124 gal. 2 qt. $\pounds$ 205 128. 5d. $\pounds$ 546 18. 7d. Art. 298. $\pounds$ 88 48. 2d. $\pounds$ 21 48. 4d. $\pounds$ 23 138. 10d. 4 y. 3 m. 2 d. 4 y. 4 m. 22 d. 6 m. 10 d. 2 y. 6 m. 24 d. $\pounds$ 148. 8d.; $\pounds$ 148. 8d.; $\pounds$ 148. 8d.; $\pounds$ 148. 8d.; $\pounds$ 148. 8d.; $\pounds$ 148. 8d.; $\pounds$ 167. 168.
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	Art. 274. \$6. 2. $$34.$92.96.$312.$5.44.$114.58.$102.24.$104.64.$164.64.$1632.$12.40.$15.75.$242.10.$15.75.$242.10.$15.65.$198.40.Art. 275..1651386.289.3624\frac{29}{2}..8125..165.916\frac{2}{2}..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..8125..81$	33. 34. 35. 36. 37. 1. 2. 3. 4. 5. 6. 7. 8. 9. 10.	D, $00^{+}_{15}$ A.; $(\zeta, 67^{+}_{28}$ A.; $(\xi, 67^{+}_{28}$ A.;	$\begin{array}{c} 10. \\ 17. \\ 18. \\ 19. \\ 20. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 9. \\ 10. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 9. \\ 10. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 9. \\ 10. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 9. \\ 10. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 9. \\ 10. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 9. \\ 10. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 9. \\ 10. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 9. \\ 10. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 9. \\ 10. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 9. \\ 10. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 9. \\ 10. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 9. \\ 10. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 9. \\ 10. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 9. \\ 10. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 9. \\ 10. \\ 1. \\ 1. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 10. \\ 1. \\ 1. \\ 1. \\ 1. \\ 1. \\ 1. \\ $	23 A. 36 sq. rd. 33 A. 36 sq. rd. 10 oz. 68 cd. 12 cu. ft. $\pm 20$ 2s. 5d. Art. 288. 135d. 135d. 135d. 135d. 135s. 9d. 1980 ft. 496 lbs. 15s. 5d. 13 pts. 4785 ft. 87 lbs. 8 oz. $5\frac{1}{2}$ pts. 104 cu. ft. Art. 290. 150d. 17s. 6d. 153d. 13s. 8d. 9 x 4 x	4. 5. 6. 7. 8. 9. 10. 11. 12. 3. 4. 5. 6. 7. 8. 9. 11. 2. 8. 1.	12 y, 2 m, 16 d, 15 cd, 48 cu, ft, 26 h, 46 m, 37 bu, 5 qt, 27 yd, 4 in, 10 lb, 2 pwt, 20 gr, 124 gal, 2 qt, $\pounds 205$ 128, 5d, $\pounds 546$ 18, 7d, <b>Art.</b> 298. $\pounds 88$ 48, 2d, $\pounds 21$ 48, 4d, $\pounds 31 48, 3d,$ $\pounds 23$ 138, 10d, 4 y, 3 m, 2 d, 4 y, 4 m, 22 d, 6 m, 10 d, 2 y, 6 m, 24 d, <b>Art.</b> 300. $\pounds 122$ 148, 8d,; $\pounds 157$ 168,; $\ell 109$ 7°, 4d,
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	Art. 274. \$6. 2. $$34.$48.13.$92.96.$312.$5.44.$114.58.$102.24.$280.64.$164.04.$16.32.$12.40.$15.75.$242.10.$16.50.$198.40.Art. 275..1651386.289.3624\frac{2}{2}9..8125..158.916\frac{2}{3}.$114.76.$124.9.$15.75.$242.10.$16.50.$198.40.Art. 275..1651386.289.3624\frac{2}{2}9..8125..158.916\frac{2}{3}.\$114.7.16\frac{2}{3}.$	33. 34. 35. 36. 37. 1. 2. 3. 4. 5. 6. 7. 8. 9. 10. 11.	b), $00_{16}^{+}$ A.; c), $67_{28}^{+}$ A.; s), $34575.66.$ 7040 ft. Wife, $348500$ ; Son, $36375$ ; Daughter, 24250; Total, $3145500.$ 31065. 34.63. 1100 bu. Art. 282. 2326d. 220 gills. 108404 f. 13265 lb. 2566 days. 18211d. 235923 f. 1566 qt. 14948 lbs. 4480 pwt. 27005 ft. 240720 et.	$\begin{array}{c} 10.1\\ 17.1\\ 18.\\ 19.\\ 20.\\ 1.\\ 2.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 1.\\ 2.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 1.\\ 2.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 1.\\ 2.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 1.\\ 2.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 1.\\ 2.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 1.\\ 2.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 1.\\ 2.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 1.\\ 2.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 1.\\ 2.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 1.\\ 2.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 1.\\ 2.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 1.\\ 2.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 1.\\ 2.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 1.\\ 2.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 1.\\ 2.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 1.\\ 1.\\ 2.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1$	23 A. 36 sq. rd. 33 A. 36 sq. rd. 4 cwt. 63 lb. 10 oz. 68 cd. 12 cu. ft. £20 2s. 5d. Art. 288. 135d. 138. 9d. 1980 ft. 496 lbs. 15s. 5d. 13 pts. 4785 ft. 87 lbs. 8 oz. 5½ pts. 104 cu. ft. Art. 290. 150d. 17s. 6d. 153d. 13s. 8d. 2 y. 4 m. ete 0. 4d.	4. 5. 6. 7. 8. 9. 9. 10. 11. 12. 1. 2. 3. 4. 5. 6. 7. 8. 1.	12 y, 2 m, 16 d, 15 cd, 48 cu, ft, 26 h, 46 m, 37 bu, 5 qt, 20 yd, 4 in, 10 lb, 2 pwt, 20 gr, 124 gal, 2 qt, $\pounds 205$ 128, 5d, $\pounds 546$ 18, 7d, <b>Art. 298.</b> $\pounds 88$ 48, 2d, $\pounds 21$ 48, 4d, $\pounds 23$ 138, 10d, 4 y, 3 m, 2 d, 4 y, 4 m, 22 d, 6 m, 10 d, 2 y, 6 m, 24 d, <b>Art. 300.</b> $\pounds 125$ 148, 8d.; $\pounds 157$ 168.; $\pounds 192$ 178, 4d.; e 9ee
$\begin{array}{c} 1.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 112.\\ 13.\\ 14.\\ 15.\\ 16.\\ 17.\\ 1.\\ 2.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 1.\\ 2.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 1.\\ 2.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 1.\\ 2.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1.\\ 1$	Art. 274. \$6. 2. $$34.$6.$ 2. $$34.$02.96.$512.$5.44.$114.58.$102.24.$104.54.$164.%4.$16.32.$12.40.$12.40.$15.75.$38.75.$242.10.$16.50.$198.40.Art. 275..1651386.289.3624\frac{2}{2}\frac{9}{4}..8125.158.916\frac{8}{5}.\$117.16\frac{8}{5}.61.875.$	33. 34. 35. 36. 37. 1. 2. 3. 4. 5. 6. 7. 8. 9. 10. 11. 12.	D, 00 <sup>+</sup> 5 A.; \$4575.66. 7040 ft. Wife, \$48500; Son, \$36375; Daughter, \$24250; Total, \$145500. \$1065. \$4.63. 1100 bu. Art. 282. 2326d. 220 gills. 108404 f. 13265 lb. 256 days. 18211d. 235923 f. 1566 qt. 14948 lbs. 4480 pwt. 27005 ft. 2407680 ft.	$\begin{array}{c} 10. \\ 17. \\ 18. \\ 19. \\ 20. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 9. \\ 10. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ \end{array}$	23 A. 36 sq. rd. 33 A. 36 sq. rd. 4 cwt. 63 lb. 10 oz. 68 cd. 12 cu. ft. $\pounds 20$ 2s. 5d. Art. 288. 135d. 138, 9d. 1080 ft. 496 lbs. 15s. 5d. 13 pts. 4785 ft. 87 lbs. 8 oz. $5\frac{1}{2}$ pts. 104 cu. ft. Art. 290. 150d. 17s. 6d. 153d. 13s. 8d. 2 y. 4 m. $\pounds 16$ 9s. 4d.	4. 5. 6. 7. 8. 9. 9. 10. 11. 12. 1. 2. 3. 4. 5. 6. 7. 8. 1.	12 y, 2 m, 16 d, 15 cd, 48 cu, ft, 26 h, 46 m, 37 bu, 5 qt, 27 yd, 4 in, 10 lb, 2 pwt, 20 gr, 124 gal, 2 qt, $\pounds$ 205 128, 5d, $\pounds$ 546 18, 7d, <b>Art. 298.</b> $\pounds$ 88 48, 2d, $\pounds$ 21 48, 4d, $\pounds$ 23 148, 3d, $\pounds$ 24 168, $\pounds$ $\pounds$ 157 168, $\pounds$ $\pounds$ 192 178, 4d, $\pounds$ $\pounds$ 263, 24 d, 16 m, 5
$\begin{array}{c} 1.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 112.\\ 13.\\ 14.\\ 15.\\ 16.\\ 17.\\ 1.\\ 2.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ \end{array}$	Art. 274. \$6. 2. $$34.$6.$ 2. $$34.$92.96.$312.$5.44.$114.58.$102.24.$164.64.$164.64.$1632.$12.40.$15.75.$38.75.$242.10.$15.650.$198.40.Art. 275.1651386.289.3624\frac{2}{2}\frac{9}{4}.$125.158.916\frac{2}{3}.\$117.16\frac{2}{3}.\$117.16\frac{2}{3}.\$117.16\frac{2}{3}.$	33. 34. 35. 36. 37. 1. 2. 3. 4. 5. 6. 7. 8. 9. 11. 12. 11. 12.	b), $00_{16}^{+}$ A.; C, $07_{88}^{+}$ A.; $k_{4575,66}$ . 7040 ft. Wife, $k_{48500}$ ; Son, $k_{36375}$ ; Daughter, $k_{24250}$ ; Total, $k_{145500}$ . $k_{4.63}$ . 1100 bu. Art. 282. 2326d. 2326d. 2326d. 2326d. 2326d. 2326d. 2326d. 2326d. 2326d. 23292 fl. 1566 days. 18211d. 235923 f. 1566 qt. 14948 lbs. 4480 pwt. 27005 ft. 2407680 ft. 572 pts.	$\begin{array}{c} 10. \\ 17. \\ 18. \\ 19. \\ 20. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 9. \\ 10. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 8. \\ 9. \\ 10. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 10. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 10. \\ 1. \\ 2. \\ 3. \\ 4. \\ 5. \\ 6. \\ 7. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. \\ 10. $	233 A. 36 sq. rd. 33 A. 36 sq. rd. 4 ewt. 63 lb. 10 oz. 68 ed. 12 eu. ft. £20 2s. 5d. Art. 288. 135d. 135s. 9d. 1980 ft. 496 lbs. 15s. 5d. 13 pts. 4785 ft. 87 lbs. 8 oz. $5\frac{1}{2}$ pts. 104 cu. ft. Art. 290. 150d. 17s. 6d. 153d. 13s. 8d. 2 y. 4 m. £16 9s. 4d. £205 6s. 9d.	4. 5. 6. 7. 8. 9. 10. 11. 12. 8. 4. 5. 6. 7. 8. 9. 1. 2. 8. 1. 2.	12 y. 2 m. 16 d. 15 cd. 48 cu, ft. 26 h. 46 m. 37 bu. 5 qt. 27 yd. 4 in. 10 lb. 2 pwt. 20 gr. 124 gal. 2 qt. $\pounds$ 205 128, 5d. $\pounds$ 546 18, 7d. Art. 298. $\pounds$ 88 48, 2d. $\pounds$ 21 48, 4d. $\pounds$ 3 148, 3d. $\pounds$ 23 138, 10d. 4 y. 3 m. 2 d. 6 m. 10 d. 2 y. 6 m. 24 d. Art. 300. $\pounds$ 122 148, 8d.; $\pounds$ 157 168.; $\pounds$ 192 178, 4d.; $\pounds$ 263. 34 cd. 16 cu. ft.
$\begin{array}{c} 1.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 112.\\ 13.\\ 14.\\ 15.\\ 17.\\ 1.\\ 2.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8. \end{array}$	Art. 274. \$6. 2. $$34.$48.13.$92.96.$312.$5.44.$114.58.$102.24.$280.64.$164.04.$16.32.$12.40.$15.75.$242.10.$16.50.$198.40.Art. 275.158.916\frac{2}{3}.\$117.16\frac{2}{3}.\$117.16\frac{2}{3}.$500..04.$	33. 34. 35. 36. 37. 1. 2. 3. 4. 5. 6. 7. 8. 9. 10. 11. 12. 13. 14.	b), $00_{15}^{+}$ A.; $(2, 67_{28}^{+}$ A.; $(3, 67_{28}^{+}$ A.; $(3, 67_{28}^{+}$ A.; (3, 70, 66, 7040 ft. Wife, $(3, 86375; 10, 10, 10, 10, 10, 10, 10, 10, 10, 10,$	10.       17.         117.       18.         119.       20.         1.2.       3.         4.5.       6.         7.       8.         9.       10.         1.2.       3.         4.5.       6.         7.8.       9.         10.       1.         2.3.       4.         5.6.       7.         8.       9.         10.       1.         2.3.       4.         5.6.       7.         8.       6.         7.       8.	23 A. 36 sq. rd. 33 A. 36 sq. rd. 4 ewt. 63 lb. 10 oz. 68 ed. 12 cu. ft. $\pounds 20$ 2s. 5d. Art. 288. 135d. 13s. 9d. 1980 ft. 496 lbs. 15s. 5d. 13 pts. 4785 ft. 87 lbs. 8 oz. 5 $\frac{1}{2}$ pts. 104 cu. ft. Art. 290. 150d. 17s. 6d. 153d. 13s. 8d. 2 y. 4 m. $\pounds 16$ 9s. 4d. $\pounds 20$ 5 s. 9d. 2 y. 5 m.	4.5. 6.7. 8.9. 10. 11. 12. 3. 4.5. 6.7. 8. 1. 2.3. 3.	12 y, 2 m, 16 d, 15 cd, 48 cu, ft, 26 h, 46 m, 37 bu, 5 qt, 27 yd, 4 in, 10 lb, 2 pwt, 20 gr, 124 gal, 2 qt, $\pounds 205$ 128, 5d, $\pounds 546$ 18, 7d, <b>Art. 298.</b> $\pounds 88$ 48, 2d, $\pounds 21$ 48, 4d, $\pounds 3$ 148, 3d, $\pounds 23$ 138, 10d, 4 y, 3 m, 2 d, 4 y, 4 m, 22 d, 6 m, 10 d, 2 y, 6 m, 24 d, $\pounds 122$ 148, 8d, $\sharp 157$ 168, $\sharp 157$ 168, $\pounds 192$ 178, 4d, $\pounds 263$ . 34 cd, 16 cu, ft, $\pounds 28$ 28, 6d,
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	Art. 274. \$6. 2. $$34.$6.$ 2. $$34.$92.96.$512.$5.44.$114.58.$102.24.$104.32.$164.32.$164.34.$16.32.$12.40.$15.75.$98.75.$98.75.$12.40.$16.50.$198.40.Art. 275..1651386.289.3624\frac{2}{9}..8125.158.916\frac{2}{5}.\$117.16\frac{2}{3}.61.875.3500..04.\frac{87}{7}.$	33.       34.         35.       36.         37.       1.2.         3.4.       5.6.         7.8.       9.         10.       11.         12.       13.         13.       14.         15.       15.	D, $00^{+}_{5}$ A.; $(\xi, 67^{+}_{5}, A.;$ $(\xi, 67^{+}_{5}, A.;$ $(\xi, 67^{+}_{5}, A.;$ $(\xi, 67^{+}_{5}, A.;$ $(\xi, 67^{+}_{5}, A.;$ $(\xi, 64, A.;$ $(\xi,$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	23 A. 36 sq. rd. 33 A. 36 sq. rd. 4 cwt. 63 lb. 10 oz. 68 cd. 12 cu. ft. $\pounds 20$ 2s. 5d. Art. 288. 135d. 138. 9d. 1980 ft. 496 lbs. 15s. 5d. 13 pts. 4785 ft. 87 lbs. 8 oz. $5\frac{1}{2}$ pts. 104 cu. ft. Art. 290. 150d. 17s. 6d. 153d. 13s. 8d. 2 y. 4 m. $\pounds 16$ 9s. 4d. $\pounds 205$ 6s. 9d. 2 y. 5 m. $\pounds 15$ 6s. 9d.	4.5. 6.7.8.9. 10.111.12. 1.2.3.45.6.7.8. 1. 2.3.4. 4.	$\begin{array}{c} 12 \ y, 2 \ m, 16 \ d, \\ 15 \ cd, 48 \ cu, \ ft, \\ 26 \ h, 46 \ m, \\ 37 \ bu, 5 \ qt, \\ 27 \ yd, 4 \ in, \\ 10 \ lb, 2 \ pwt, \\ 20 \ gr, \\ 124 \ gal, 2 \ qt, \\ 4205 \ 128, 5d, \\ \pounds 205 \ 128, 5d, \\ \pounds 21 \ 48, 4d, \\ \pounds 21 \ 48, 8d, \\ \pounds 21 \ 48, 8d, \\ \pounds 21 \ 48, 8d, \\ \pounds 157 \ 168, \\ \pounds 157 \ 168, \\ \pounds 157 \ 168, \\ \pounds 192 \ 178, 4d, \\ \pounds 192 \ 178, 4d, \\ \pounds 28 \ 6d, \\ 34 \ cd, 16 \ cu, \ ft, \\ \pounds 28 \ 28, \ 6d, \\ 3 \ lb, 3 \ oz, \ 12 \end{array}$

Art. 271.]

5.	16 h. 23 m.	Art. 311.	7.	900 sq. ft.	Art. 325.
	40 s.;	1 7 mo 18 de	8.	1386 sq. ft.;	1. 123 cd.
	19 h. 40 m.	2 8 mo 18 da		154 sq. yd.	2. 302400 cu. in.
	24 s.;	2 1 yr 8 mg	9.	960 sq. ft.	3. 1384 cu. vd.
	24 h. 35 m.	11 do	10.	55.	4. 67 cds. 119
	30 s.;	19 vr 5 mo	1.1.	588 a.	cu. ft.
	29 h. 30 m.	4. 2 yr. 0 mo.	12.	132.183 a.	5. 560 cu. vd.
	36 s.	5 10 mg 8 da	13.	1.00352 a.	6. \$72.
6.	55 da. 13 h.	2. 10 mo. 19 do.	14.	23 <sup>§</sup> sq. yd.	7. \$26.95.
7.	£20 12s. 6d.	0. 9 mo. 12 da.	15.	17640 sq. ft.	8. 8 ft.
8.	£6 7s. 10d.;	7. 9 mo. 15 da.	16.	24 ft.	9. 33 cd.
	£7 5s. 9d.	8. 4 mo. 10 ua.	17.	\$7200.	10. 135 cu. ft.
9.	£3 9s. 3d.;	1. 250 days.	18.	990 ft.	11. 233280 cu. in.
	£5 10s. 9d.;	2. 200 days.	19.	<sup>1</sup> / <sub>b</sub> sq. ft.; <sup>1</sup> / <sub>4</sub> sq.	12. 168 tons.
	£8 6s. 1d.;	3. 010 days.		ft.; <sup>2</sup> / <sub>3</sub> sq. ft.	13. \$70:
	£9 13s. 10d.	4. 000 days.	20.	221 sq. yd.	£21 17s. 6d.
		2. 512 days.	21.	\$440.	14. 213500 cu. ft.
	Art. 302.	6. 280 days.	22.	300 sq. ft.	15. 21 <sup>§</sup> perches.
1	01 4- 01 ·	7. 280 days.	23.	8000 sq. yd.	16. 27.
1.	£1 48. 9d.;	8. 138 days.	24.	19800 sq. ft.	17, 250 cu. ft.
	£1 10s. 3d.;	9. 6574 days.	25.	1 sq. yd.;	18. 1260 cu. ft.:
0	88. 30.	11. Dec. 0.		35 sq. yd;	26460:
z.	192 ya.;	12. June 22.		35 sq. yd.	\$238.14
	324 ya.;	1.1 914	26.	108.	19. 34944.
~	352 yd.	Art. 315.	27.	10368.	20. 2112 cn. ft.
3.	44 yd.	1. 93 ft. 1 in.	28.	117 sq. ft.	21 2240 · 1120
4.	$7^{\circ} 6 32\frac{1}{2}$ ;	2. $22\frac{1}{2}$ in.	29.	1512.	22 3686 4 cu ft :
	$5^{\circ} 41' 14'';$	3. 89760 ft.;	30.	17820.	36 bbl :
	$4^{\circ} 44' 21\frac{2}{3}'';$	577 <sup>1</sup> / <sub>3</sub> ft.	31.	187200.	28.8 cu vd.
_	3° 9' 345''.	4. $1\frac{1}{2}$ in.	32.	\$1040.	23 102375
5.	$40 \text{ a.} 51\frac{1}{4} \text{ sq. rd.};$	5. 9 mi. 100 rd.	33.	\$153600.	NO. TONO 10.
	32 a. 41 sq. rd.;	1 yd. 2 ft.	34	\$1600: 32 a.	Art. 328.
	24a.130sq.rd.;	6. 6514 in.	35.	612 sq. ft.	1 19 so ft
	20 a. 25 sq. rd.	7. 4620 ft.	36.	122 sq. in.	0 18 sq. 10.
6.	9s. 11d.;	8. 66 ch. 20 ft.;	37.	62 sq. vd.:	3 180 sq. ft .
	£5 19s.;	52512 in.	1	262 sq. vd.	\$6 72
	£9 18s. 4d.;	9. 99 ch.;	38.	128 sq. vd.	4 5700 ft
	£18 6s. 11d.	6534 ft.	39.	772 sq. ft.	4. 0100 10. 5 19 ft
7.	£34 10s.;	10. 2478.96 ft.;	40.	363117 sq. ft.	6 01 ft 7 8 ft
	£21 11s. 3d.;	150.24 rd.	41.	4 vd.	Q 91 ft
	£17 5s.;	11. 61 in.; 81 in.;	12.	24: 28.8.	0. 16 ft
	£9 11s. 8d.;	111 in.	43	576: 900: 720.	10 331 ft
	£5 15s.	12. 287 fathoms;	44	518: 1026:	11 24 ft
		522 <sup>2</sup> / <sub>3</sub> fathoms.	174.	180.	12 54 ft
	Art. 308.	13. 9 mi. 45 rd. 4	15.	24000: 33600:	13 480 sq ft
1	26020 min	yd. 1 ft. 6 in.	170.	38400.	1% 12006 ft •
0	939 19	14. 117.46 ch.	46.	750: 930.	\$181.44
3	2 vr 4 mo 15	15. \$708.50.	147.	\$ sa. vd.	15 240 ft.
0.	da.	16. 18480 posts;	48.	\$64.	16 1280 ft.
4	\$0.69	739200 ft.	49.	5 widths and	17 8800 ft.
5	2 vr. 2 mo		70.	4 in.; 35 vd.	18. 661 posts.
0.	16 da	Art. 321.	50.	25 vd.	19 240 ft.
6	51 hr 8 min	7, 175 a. 140 sq.	51	18: 10 vd.	20 184 ft.
7	3: 7: 3.	rd.	52	4 sq. vd.;	21 21 ft.
8	8 h. 22 m.	2. 130680 sq. ft.	1	36 sq. ft.	NI. NI IU
0.	50 s.	3. 22405 sq. vd.	53.	15 rolls.	Art. 331.
9	1 d. 3 h. 46 m	4, 46 a, 50 sq. rd.	54.	16.	1. 71 pt.
	40 s.	5. 34.511.360 a.	55.	2: 5.	2. 109 gal. 1 qt.
10	\$83.17	6. 2500 sq. ft.	56.	6 rolls.	1 pt.

3.	28 gal. 3 at.	24, 139 <u>35</u> bu.	2. \$2.94.	28. 11 hr. 20 min.
	1 nt	95 16944 hu	2 288. 060	A 37
	1 pt.	20. 102- Du.	0. 200; 900.	A. M.
4.	3174 bbl.	26. 1848 bu.	4. 792.	29. 4 A. M. Tues-
	19 cral	27 8612 hu	5 2210	dev
~	rea 1	00 10515 h	0.0501	100 1000 001 151
5.	576 gal.	28. 10010 bu.	6. \$0.61.	30. 122° 26' 45''
6.	133.68 + cu. ft	29. 32430 bu.	7. \$345.60.	W
~	1200	20 00115 has	0 00 10	01 000 001 APII TTT
1.	1500 gai.	ou. waine bu.	0. 00.10.	31. 01 31 40" W.
9.	538.56 gal.	31. 416 <sup>32</sup> bu.	9. 50.	
10	2202 6 gal	32 10019 hu		Ant 250
10.	0000.0 gai.	00 0000 1	1.040	A10. 000.
11.	38297.6 gal.	33. 2791 bu.	Art. 347.	3 38364 am .
13.	1504 gal.	35. \$153.54.		50004 IZ
11	56400 mal	2C @149.09	<i>I</i> . 151° 50′ 1″.	.38364 Km.
14.	50400 gai.	50. 0142.92.	2. 134° 53' 59''	40017516 Km.:
15.	169200 gal.	37. \$167.13.	0 170 001 ACII	1 7516 m
16	f z 2901	38 \$233.40	3. 1 20 40'.	1.7010 11.
10.	7	00 0007 15	4. 65° 56′ 20′′;	5. 8742.57 m.
17.	7 gal. 5 qt.	39. \$257.40.	107° 40/	6 119 Km
18.	72.	40. \$119.02.		~ #00 m0
		11 0905 98	5. 5 4' 4''';	7. \$98.70.
-		41. 0200.00.	6° 20′ 588″	<i>8</i> . 2306.8 m.
	Art. 333.	42. \$200.67.	6 110 59/ 10/1.	9 910 m
		13. \$94.75.	0. 11 00 49 ;	0. 010 m.
1.	187 pt.	11 001 00	$11^{\circ} 13' 53_{16}''$	10. 650.
0	156 hu 1 pk	44. 004.29.	7 277° 46' 40'	11. \$2400
~.	100 bu. 1 pk.		0 1 0 10 TU .	10 10010
3.	\$25.60.	Art. 342.	8. 159400".	1%. 10240 m.
1.	161281.5 cu. in.	11.0.01.00	9, 180°,	13. 24 hr.
5	150 by	1. £135 1s. 10d.		
э.	100 bu.	9 £3 159 8d		1
6.	321.4, ex.;	0 040 10.	Art. 353.	Art. 362.
	320 ann	3. £42 10s.		
~	100 happ.	4. £34 17s. 11d.	1. 73° 54′ 25″.	2. 83.09 sq. m.
- 7.	100 bu., app.	5 2080 d	0 173° 931 5911	3 4700 sa m
8.	235.2 bu., app.	J. 5000 u.	A. 10 AO 0A .	1 000500
0	640 hu ann	6. £18 8s. 11d.	3. 34 49'.	4. 602500 ca.
0.	040 bu., app.	7. £901 5s.	4. 178° 34' 17"	5. 256 sq. m.
7/1	b // 6 b a a			
10.	970 DU.	0 010 1%	5 99° 991 1511	6 400
10.	910 DU.	8. £49 7s.	5. 88° 33′ 45″.	<i>6</i> . 400.
10.	10 Du.	8. £49 7s. 9. £1 16s. 2d.;	5. 88° 33′ 45″. 6. 149° 14′ 13″.	6. 400. 7. 166.4 H.
10.	Art. 340.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d	5. 88° 33′ 45″. 6. 149° 14′ 13″. 7 4 br 56 min	6. 400. 7. 166.4 H. 8. \$12.44
10.	Art. 340.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.;	5. 88° 33' 45". 6. 149° 14' 13". 7. 4 hr. 56 min.	6. 400. 7. 166.4 H. 8. \$12.44.
10.	<b>Art. 340.</b> 1 lb. 8 oz.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d.	5. 88° 33' 45". 6. 149° 14' 13". 7. 4 hr. 56 min. $\frac{1}{5}$ sec.	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40.
10.	<i>Art.</i> 340. 1 lb. 8 oz. 16 pwt. 16 gr.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d. 10. 39.5; 5135.	5. 88° 33' 45". 6. 149° 14' 13". 7. 4 hr. 56 min. 1 sec. 8. 54 min. 304	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H.
10.	<i>Art.</i> 340. 1 lb. 8 oz. 16 pwt. 16 gr.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d. 10. $39\frac{3}{45}$ ; $51\frac{88}{45}$ . 11. 10 10s	5. 88° 33' 45". 6. 149° 14' 13". 7. 4 hr. 56 min. $\frac{1}{5}$ sec. 8. 54 min. 30 $\frac{4}{5}$	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H.
10. 1. 2.	<i>Art.</i> 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d. 10. 39 <sup>3</sup> / <sub>48</sub> ; 51 <sup>88</sup> / <sub>48</sub> . 11. £10 10s.	5. 88° 33′ 45″. 6. 149° 14′ 13″. 7. 4 hr. 56 min. $\frac{1}{5}$ sec. 8. 54 min. 30 $\frac{4}{5}$ sec.	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. 4 att. 265
10. 1. 2. 3.	Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d. 10. 39 <sup>2</sup> / <sub>48</sub> ; 51 <sup>2</sup> / <sub>48</sub> . 11. £10 10s. 13. £.808.	5. 88° 33′ 45″. 6. 149° 14′ 13″. 7. 4 hr. 56 min. $\frac{1}{5}$ sec. 8. 54 min. 30 $\frac{4}{5}$ sec. 9. 11 hr. 2 min.	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. Art. 365.
10. 1. 2. 3.	Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.:	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d. 10. 39 \$ 51 \$ 51 \$ 5 11. £10 10s. 13. £.808. 14. £.921.	5. 88° 33' 45". 6. 149° 14' 13''. 7. 4 hr. 56 min. § sec. 8. 54 min. 30§ sec. 9. 11 hr. 2 min. 59.% sec.	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. Art. 365.
10. 1. 2. 3.	Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d. 10. 39 <sup>4</sup> / <sub>4</sub> , 51 <sup>4</sup> / <sub>4</sub> 11. £10 10s. 13. £.808. 14. £.921. 15. £ 523	5. 88° 33′ 45″. 6. 149° 14′ 13″. 7. 4 hr. 56 min. $\frac{1}{5}$ sec. 8. 54 min. 30 $\frac{4}{5}$ sec. 9. 11 hr. 2 min. $59\frac{2}{15}$ sec. 10. 50 min. 11 J	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <b>Art. 365.</b> 2. 17.218027
1. 2. 3.	Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d. 10. $39\frac{2}{45}$ ; $51\frac{28}{45}$ . 11. £10 10s. 13. £.808. 14. £.921. 15. £.533.	5. 88° 33' 45". 6. 149° 14' 13". 7. 4 hr. 56 min. $\frac{1}{5}$ sec. 8. 54 min. 30 $\frac{4}{5}$ sec. 9. 11 hr. 2 min. $59\frac{2}{15}$ sec. 10. 50 min. $11\frac{7}{15}$	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <i>Art.</i> 365. 2. 17.218027 cu. m.
1. 2. 3. 4.	Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10. $39\frac{2}{5}; 51\frac{28}{14}$ . 11. £10 10s. 13. £.808. 14. £.921. 15. £.533. 16. £.867.	5. 88° 33′ 45″. 6. 149° 14′ 13″. 7. 4 hr. 56 min. $\frac{1}{5}$ sec. 8. 54 min. 30 $\frac{4}{5}$ sec. 9. 11 hr. 2 min. $59_{\frac{7}{16}}$ sec. 10. 50 min. $11_{\frac{7}{15}}$ sec.	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <i>Art.</i> 365. 2. 17.218027 cu. m. 8. 28 cu. m.
1. 2. 3. 4. 5.	Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 803 oz. 15 pwt.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d. 10. $39\frac{3}{48}$ ; $51\frac{88}{48}$ . 11. £10 10s. 13. £.808. 14. £.921. 15. £.533. 16. £.867. 17. £.363.	5. 88° 33′ 45″. 6. 149° 14′ 13″. 7. 4 hr. 56 min. $\frac{1}{5}$ sec. 8. 54 min. 30 $\frac{4}{5}$ sec. 9. 11 hr. 2 min. $59\frac{2}{15}$ sec. 10. 50 min. 11 $\frac{7}{15}$ sec. 11. 5 hr. 4 min.	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <i>Art.</i> 365. 2. 17.218027 cu. m. 3. 28 cu. m.
1. 2. 3. 4. 5.	Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 803 oz. 15 pwt.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d. 10. $39\frac{8}{45}$ ; $51\frac{88}{45}$ . 11. £10 10s. 13. £.808. 14. £.921. 15. £.533. 16. £.867. 17. £.363. 18. £.606.	5. 88° 33' 45". 6. 149° 14' 13". 7. 4 hr. 56 min. $\frac{1}{5}$ sec. 8. 54 min. 30§ sec. 9. 11 hr. 2 min. $59_{1\overline{6}}^{-2}$ sec. 10. 50 min. 11 $\frac{7}{16}$ sec. 11. 5 hr. 4 min. 204 sec	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <b>Art. 365.</b> 2. 17.218027 cu. m. 3. 28 cu. m. 4. 3.3 cu. m.
1. 2. 3. 4. 5. 6.	Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 803 oz. 15 pwt. \$42.98.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d. 10. $39\frac{2}{48}$ ; $51\frac{28}{48}$ . 11. £10 10s. 13. £.808. 14. £.921. 15. £.533. 16. £.867. 17. £.363. 18. £.696. 19. 62.	5. 88° 33′ 45″. 6. 149° 14′ 13″. 7. 4 hr. 56 min. $\frac{1}{5}$ sec. 8. 54 min. 30 <sup>4</sup> sec. 9. 11 hr. 2 min. $59\frac{2}{16}$ sec. 10. 50 min. 11 $\frac{7}{17}$ sec. 11. 5 hr. 4 min. 20 <sup>4</sup> / <sub>2</sub> sec.	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <i>Art.</i> 365. 2. 17.218027 cu. m. 3. 28 cu. m. 4. 3.3 cu. m. 5. 4.81208 cu. m.
1. 2. 3. 4. 5. 6. 7.	Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 803 oz. 15 pwt. \$42.98. 1 <sup>§</sup> oz.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d. 10. $39\frac{3}{45}$ ; $51\frac{35}{45}$ . 11. £10 10s. 13. £.808. 14. £.921. 15. £.533. 16. £.867. 17. £.363. 18. £.696. 20. 8s. 6d.; 12s. 9d.	5. 88° 33' 45". 6. 149° 14' 13". 7. 4 hr. 56 min. $\frac{1}{4}$ sec. 8. 54 min. 30 $\frac{4}{5}$ sec. 9. 11 hr. 2 min. $59\frac{2}{16}$ sec. 10. 50 min. 11 $\frac{7}{16}$ sec. 11. 5 hr. 4 min. 20 $\frac{4}{5}$ sec. 12. 11 hr. 58 min.	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <b>Art. 365.</b> 2. 17.218027 cu. m. 3. 28 cu. m. 4. 3.3 cu. m. 5. 4.81208 cu. m.
1. 2. 3. 4. 5. 6. 7. 8.	Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 803 oz. 15 pwt. \$42.98. 1 <sup>‡</sup> oz. \$68.75	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d. 10. $39\frac{3}{45}$ ; $51\frac{38}{45}$ . 11. £10 10s. 13. £.808. 14. £.921. 15. £.533. 16. £.867. 17. £.363. 18. £.606. 20. 8s. 6d.; 12s. 9d. 21. 16s. 4d.; 4s.	5. 88° 33′ 45″. 6. 149° 14′ 13″. 7. 4 hr. 56 min. $\frac{1}{5}$ sec. 8. 54 min. 30 $\frac{4}{5}$ sec. 9. 11 hr. 2 min. $59\frac{2}{16}$ sec. 10. 50 min. $11\frac{2}{17}$ sec. 11. 5 hr. 4 min. 20 $\frac{4}{5}$ sec. 12. 11 hr. 58 min. 11 $\frac{14}{5}$ sec.	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <b>Art. 365.</b> 2. 17.218027 cu. m. 3. 28 cu. m. 4. 3.3 cu. m. 5. 4.81208 cu. m. 6. 2051.28 cu. m.
1. 2.3. 4.5.6.7.8.	Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 803 oz. 15 pwt. 842.98. 1 <sup>§</sup> oz. \$68.75. 1546 975 oz.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d. 10. $39\frac{3}{45}$ ; $51\frac{35}{45}$ . 11. £10 10s. 13. £.808. 14. £.921. 15. £.533. 16. £.867. 17. £.363. 18. £.696. 20. 8s. 6d.; 12s. 9d. 21. 16s. 4d.; 4s.	5. 88° 33' 45". 6. 149° 14' 13". 7. 4 hr. 56 min. $\frac{1}{4}$ sec. 8. 54 min. 30 $\frac{4}{5}$ sec. 9. 11 hr. 2 min. $59\frac{4}{15}$ sec. 10. 50 min. 11 $\frac{7}{15}$ sec. 11. 5 hr. 4 min. 20 $\frac{4}{5}$ sec. 12. 11 hr. 58 min. 11 $\frac{1}{4}\frac{5}{5}$ sec.	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <b>Art. 365.</b> 2. 17.218027 cu. m. 3. 28 cu. m. 4. 3.3 cu. m. 5. 4.81208 cu. m. 6. 2051.28 cu. m. 7. \$109.69.
1. 2. 3. 4. 5. 6. 7. 8. 9.	Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 803 oz. 15 pwt. \$42.98. 1 <sup>‡</sup> oz. \$68.75. 1,546,875 oz.;	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10. $39\frac{2}{5}$ ; $51\frac{23}{5}$ . 11. £10 10s. 13. £.808. 14. £.921. 15. £.533. 16. £.867. 17. £.363. 18. £.606. 20. 8s. 6d.; 12s. 9d. 21. 16s. 4d.; 4s. 11d.	5. 88° 33' 45". 6. 149° 14' 13". 7. 4 hr. 56 min. $\frac{1}{5}$ sec. 8. 54 min. 30 $\frac{4}{5}$ sec. 9. 11 hr. 2 min. $59_{1\overline{1}}$ sec. 10. 50 min. $11_{1\overline{5}}$ sec. 11. 5 hr. 4 min. $20\frac{4}{5}$ sec. 12. 11 hr. 58 min. $11\frac{4}{5}$ sec. 13. 2 hr.	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <b>Art. 365.</b> 2. 17.218027 cu, m. 3. 28 eu. m. 4. 3.3 cu, m. 5. 4.81208 cu, m. 6. 2051.28 cu, m. 7. \$109.69. 8. 82.5 sters:
1. 2. 3. 4. 5. 6. 7. 8. 9.	Art. 340. 1 lb, 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 803 oz. 15 pwt. 842.98. 1 <sup>3</sup> oz. \$68.75. 1,546,875 oz.; 171875 oz.	<ul> <li>8. £49 7s.</li> <li>9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d.</li> <li>10. 39 \$ 51\$ \$ 51\$ \$ 5.</li> <li>11. £10 10s.</li> <li>13. £.808.</li> <li>14. £.921.</li> <li>15. £.533.</li> <li>16. £.867.</li> <li>17. £.363.</li> <li>18. £.606.</li> <li>20. 8s. 6d.; 12s. 9d.</li> <li>21. 16s. 4d.; 4s. 11d.</li> <li>22. 5s. 1d.; 3s. 8d.</li> </ul>	<ul> <li>5. 88° 33' 45".</li> <li>6. 149° 14' 13".</li> <li>7. 4 hr. 56 min. <sup>1</sup>/<sub>4</sub> sec.</li> <li>8. 54 min. 30<sup>4</sup>/<sub>5</sub> sec.</li> <li>9. 11 hr. 2 min. 59<sup>4</sup>/<sub>15</sub> sec.</li> <li>10. 50 min. 11<sup>7</sup>/<sub>15</sub> sec.</li> <li>11. 5 hr. 4 min. 20<sup>4</sup>/<sub>5</sub> sec.</li> <li>12. 11 hr. 58 min. 11<sup>4</sup>/<sub>4</sub> sec.</li> <li>13. 2 hr.</li> <li>14. 1 hr.</li> </ul>	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <b>Art. 365.</b> 2. 17.218027 cu. m. 3. 28 cu. m. 4. 3.3 cu. m. 5. 4.81208 cu. m. 6. 2051.28 cu. m. 7. \$109.69. 8. 82.5 sters; 42.2 m.
1. 2. 3. 4. 5. 6. 7. 8. 9.	Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 803 oz. 15 pwt. \$42.98. 1 <sup>2</sup> oz. \$68.75. 1,546,875 oz.; 171875 oz. 10480 gr.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d. 10. $39\frac{2}{45}$ ; $51\frac{28}{45}$ . 11. £10 10s. 13. £.808. 14. £.921. 15. £.533. 16. £.867. 17. £.363. 18. £.696. 20. 8s. 6d.; 12s. 9d. 21. 16s. 4d.; 4s. 11d. 22. 5s. 1d.; 3s. 8d.	5. 88° 33' 45". 6. 149° 14' 13". 7. 4 hr. 56 min. $\frac{1}{5}$ sec. 8. 54 min. 30§ sec. 9. 11 hr. 2 min. $59_{1\overline{6}}$ sec. 10. 50 min. 11 $\frac{1}{15}$ sec. 11. 5 hr. 4 min. $20\frac{1}{5}$ sec. 12. 11 hr. 58 min. $11\frac{1}{15}$ sec. 13. 2 hr. 14. 1 hr. 15 8 hr	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <b>Art. 365.</b> 2. 17.218027 cu.m. 3. 28 cu.m. 4. 3.3 cu.m. 5. 4.81208 cu.m. 6. 2051.28 cu.m. 7. \$109.69. 8. 82.5 sters; 43.2 m.
1. 2. 3. 4. 5. 6. 7. 8. 9. 10.	Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 803 oz. 15 pwt. 842.98. 14 oz. \$68.75. 1,546,875 oz.; 171875 oz. 10480 gr.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d. 10. $39\frac{3}{48}$ ; $51\frac{38}{48}$ . 11. £10 10s. 13. £.808. 14. £.921. 15. £.533. 16. £.867. 17. £.363. 18. £.606. 20. 8s. 6d.; 12s. 9d. 21. 16s. 4d.; 4s. 11d. 22. 5s. 1d.; 3s. 8d. 23. 7s. 6d.; 9s. 11d.	5. 88° 33′ 45″. 6. 149° 14′ 13″. 7. 4 hr. 56 min. $\frac{1}{8}$ sec. 8. 54 min. 30 <sup>4</sup> / <sub>5</sub> sec. 9. 11 hr. 2 min. $59\frac{2}{16}$ sec. 10. 50 min. $11\frac{7}{118}$ sec. 11. 5 hr. 4 min. $20\frac{3}{8}$ sec. 12. 11 hr. 58 min. $11\frac{14}{15}$ sec. 13. 2 hr. 14. 1 hr. 15. 3 hr. 11. 1 hr.	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <b>Art. 365.</b> 2. 17.218027 cu. m. 3. 28 cu. m. 4. 3.3 cu. m. 5. 4.81208 cu. m. 6. 2051.28 cu. m. 7. \$109.69. 8. 82.5 sters; 43.2 m.
1. 2. 3. 4. 5. 6. 7. 8. 9. 10. 11.	Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 803 oz. 15 pwt. \$42.98. 1 <sup>§</sup> oz. \$68.75. 1,546,875 oz.; 171875 oz. 10480 gr. 1152; 1400.	8. $\pounds49$ 7s. 9. $\pounds1$ 16s. 2d.; $\pounds2$ 6s. 6d.; 10s. 6d. 10. $39\frac{3}{45}$ ; $51\frac{3}{45}$ . 11. $\pounds10$ 10s. 13. $\pounds.808$ . 14. $\pounds.921$ . 15. $\pounds.533$ . 16. $\pounds.867$ . 17. $\pounds.363$ . 18. $\pounds.696$ . 20. 8s. 6d.; 12s. 9d. 21. 16s. 4d.; 4s. 11d. 22. 5s. 1d.; 3s. 8d. 23. 7s. 6d.; 9s. 11d. 24. $\pounds158$ 6s. 8d.;	5. 88° 33' 45". 6. 149° 14' 13". 7. 4 hr. 56 min. $\frac{1}{5}$ sec. 8. 54 min. 30 $\frac{4}{5}$ sec. 9. 11 hr. 2 min. $59\frac{2}{16}$ sec. 10. 50 min. 11 $\frac{7}{16}$ sec. 11. 5 hr. 4 min. $20\frac{4}{5}$ sec. 12. 11 hr. 58 min. $11\frac{1}{15}$ sec. 13. 2 hr. 14. 1 hr. 15. 3 hr. 16. 1 hr.	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <b>Art. 365.</b> 2. 17.218027 cu. m. 3. 28 cu. m. 4. 3.3 cu. m. 5. 4.81208 cu. m. 6. 2051.28 cu. m. 7. \$109.69. 8. 82.5 sters; 43.2 m. <b>Art. 367.</b>
1.         2.         3.         4.         5.         6.         7.         8.         9.         10.         11.         12.	Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 803 oz. 15 pwt. 842.98. 1 <sup>‡</sup> oz. \$68.75. 1,546.875 oz.; 171875 oz. 10480 gr. 1152; 1400. 51 lb. 12 oz.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d. 10. $39\frac{3}{45}$ ; $51\frac{3}{45}$ . 11. £10 10s. 13. £.808. 14. £.921. 15. £.533. 16. £.867. 17. £.363. 18. £.606. 20. 8s. 6d.; 12s. 9d. 21. 16s. 4d.; 4s. 11d. 22. 5s. 1d.; 8s. 8d. 23. 7s. 6d.; 9s. 11d. 24. £158 6s. 8d.; £79 8s. 4d.;	5. 88° 33′ 45″. 6. 149° 14′ 13″. 7. 4 hr. 56 min. $\frac{1}{5}$ sec. 8. 54 min. 30 $\frac{4}{5}$ sec. 9. 11 hr. 2 min. $59\frac{2}{16}$ sec. 10. 50 min. $11\frac{2}{17}$ sec. 11. 5 hr. 4 min. $20\frac{4}{5}$ sec. 12. 11 hr. 58 min. $11\frac{14}{5}$ sec. 13. 2 hr. 14. 1 hr. 15. 3 hr. 16. 1 hr. 17. 2 hr.	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <b>Art. 365.</b> 2. 17.218027 cu. m. 3. 28 cu. m. 4. 3.3 cu. m. 5. 4.81208 cu. m. 6. 2051.28 cu. m. 7. \$109.69. 8. 82.5 sters; 43.2 m. <b>Art. 367.</b>
1. 2. 3. 4. 5. 6. 7. 8. 9. 10. 11. 12. 12.	Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 803 oz. 15 pwt. \$42.98. 14 oz. \$68.75. 1,546,875 oz.; 171875 oz. 10480 gr. 1152; 1400. 51 lb. 12 oz.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d. 10. $39\frac{3}{45}$ ; $51\frac{33}{45}$ . 11. £10 10s. 13. £.808. 14. £.921. 15. £.533. 16. £.867. 17. £.363. 18. £.696. 20. 8s. 6d.; 12s. 9d. 21. 16s. 4d.; 4s. 11d. 22. 5s. 1d.; 3s. 8d. 23. 7s. 6d.; 9s. 11d. 24. £158 6s. 8d.; £79 3s. 4d.; £69 6s. 8d.	<ul> <li>5. 88° 33' 45".</li> <li>6. 149° 14' 13".</li> <li>7. 4 hr. 56 min. <sup>1</sup>/<sub>4</sub> sec.</li> <li>8. 54 min. 30<sup>4</sup>/<sub>5</sub> sec.</li> <li>9. 11 hr. 2 min. 59<sup>+2</sup>/<sub>15</sub> sec.</li> <li>10. 50 min. 11<sup>-7</sup>/<sub>15</sub> sec.</li> <li>11. 5 hr. 4 min. 20<sup>4</sup>/<sub>4</sub> sec.</li> <li>12. 11 hr. 58 min. 11<sup>4<sup>3</sup>/<sub>5</sub></sup> sec.</li> <li>13. 2 hr.</li> <li>14. 1 hr.</li> <li>15. 3 hr.</li> <li>16. 1 hr.</li> <li>17. 2 hr.</li> </ul>	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <b>Art. 365.</b> 2. 17.218027 cu. m. 3. 28 cu. m. 4. 3.3 cu. m. 5. 4.81208 cu. m. 6. 2051.28 cu. m. 7. \$109.69. 8. 82.5 sters; 43.2 m. <b>Art. 367.</b> 1. 1000 l
1. 2. 3. 4. 5. 6. 7. 8. 9. 10. 11. 12. 13.	Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 803 oz. 15 pwt. 842.98. 1 <sup>‡</sup> oz. \$68.75. 1,546,875 oz.; 171875 oz. 10480 gr. 1152; 1400. 51 lb. 12 oz. 112000 gr.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10. $39_{\frac{3}{5}}$ ; $51_{\frac{3}{5}}$ . 11. £10 10s. 13. £.808. 14. £.921. 15. £.533. 16. £.867. 17. £.363. 18. £.606. 20. 8s. 6d.; 12s. 9d. 21. 16s. 4d.; 4s. 11d. 22. 5s. 1d.; 3s. 8d. 23. 7s. 6d.; 9s. 11d. 24. £1158 6s. 8d.; £79 3s. 4d.; £63 6s. 8d.;	5. 88° 33' 45". 6. 149° 14' 13". 7. 4 hr. 56 min. $\frac{1}{5}$ sec. 8. 54 min. 30 $\frac{4}{5}$ sec. 9. 11 hr. 2 min. $59_{1\overline{1}}$ sec. 10. 50 min. $11_{1\overline{5}}$ sec. 11. 5 hr. 4 min. $20\frac{4}{5}$ sec. 12. 11 hr. 58 min. $11\frac{14}{5}$ sec. 13. 2 hr. 14. 1 hr. 15. 3 hr. 16. 1 hr. 17. 2 hr. 18. 0 hr.	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <b>Art. 365.</b> 2. 17.218027 cu. m. 3. 28 eu. m. 4. 3.3 cu. m. 5. 4.81208 cu. m. 6. 2051.28 cu. m. 7. \$100.69. 8. 82.5 sters; 43.2 m. <b>Art. 367.</b> 1. 1000 l.
$\begin{array}{c} 1.\\ 2.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 11.\\ 12.\\ 13.\\ 14. \end{array}$	Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 803 oz. 15 pwt. 842.98. 14 oz. \$68.75. 1,546,875 oz.; 171875 oz. 10480 gr. 1152; 1400. 51 lb. 12 oz. 112000 gr. 85 lb. 16 pwt.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d. 10. $39\frac{3}{45}$ ; $51\frac{38}{45}$ . 11. £10 10s. 13. £.808. 14. £.921. 15. £.533. 16. £.867. 17. £.363. 18. £.606. 20. 8s. 6d.; 12s. 9d. 21. 16s. 4d.; 4s. 11d. 22. 5s. 1d.; 3s. 8d. 23. 7s. 6d.; 9s. 11d. 24. £158 6s. 8d.; £63 6s. 8d.; £39 11s. 8d.	5. 88° 33' 45". 6. 149° 14' 13". 7. 4 hr. 56 min. $\frac{1}{4}$ sec. 8. 54 min. 30 $\frac{4}{5}$ sec. 9. 11 hr. 2 min. $59\frac{3}{16}$ sec. 10. 50 min. 11 $\frac{7}{16}$ sec. 11. 5 hr. 4 min. $20\frac{4}{3}$ sec. 12. 11 hr. 58 min. $11\frac{1}{15}$ sec. 13. 2 hr. 14. 1 hr. 15. 3 hr. 16. 1 hr. 18. 0 hr. 19. 15 min. 46 sec.	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <b>Art. 365.</b> 2. 17.218027 cu. m. 3. 28 cu. m. 4. 3.3 cu. m. 5. 4.81208 cu. m. 6. 2051.28 cu. m. 7. \$109.69. 8. 82.5 sters; 43.2 m. <b>Art. 367.</b> 1. 1000 l. 2. \$1.28.
1.         2.         3.         4.         5.         6.         7.         8.         9.         10.         11.         12.         13.         14.	Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 803 oz. 15 pwt. 803 oz. 15 pwt. \$42.98. 1 <sup>‡</sup> oz. \$68.75. 1,546,875 oz.; 171875 oz. 10480 gr. 1152; 1400. 51 lb. 12 oz. 112000 gr. 85 lb. 16 pwt. 16 gr	8. $\pounds49$ 7s. 9. $\pounds1$ 16s. 2d.; $\pounds2$ 6s. 6d.; 10s. 6d. 10. $39\frac{3}{45}$ ; $51\frac{3}{45}$ . 11. $\pounds10$ 10s. 13. $\pounds.808$ . 14. $\pounds.921$ . 15. $\pounds.533$ . 16. $\pounds.867$ . 17. $\pounds.363$ . 18. $\pounds.696$ . 20. 8s. 6d.; 12s. 9d. 21. 16s. 4d.; 4s. 11d. 22. 5s. 1d.; 3s. 8d. 23. 7s. 6d.; 9s. 11d. 24. $\pounds158$ 6s. 8d.; $\pounds79$ 3s. 4d.; $\pounds33$ 6s. 8d.; $\pounds39$ 11s. 8d. 25. 16s. 8d.;	5. 88° 33' 45". 6. 149° 14' 13". 7. 4 hr. 56 min. $\frac{1}{5}$ sec. 8. 54 min. 30 $\frac{4}{5}$ sec. 9. 11 hr. 2 min. $59_{1\overline{8}}$ sec. 10. 50 min. $11_{1\overline{5}}$ sec. 11. 5 hr. 4 min. $20\frac{4}{5}$ sec. 12. 11 hr. 58 min. $11\frac{14}{15}$ sec. 13. 2 hr. 14. 1 hr. 15. 3 hr. 16. 1 hr. 17. 2 hr. 18. 0 hr. 19. 15 min. 46 sec. 20. 40 sec.	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <b>Art. 365.</b> 2. 17.218027 cu. m. 3. 28 cu. m. 4. 3.3 cu. m. 5. 4.81208 cu. m. 6. 2051.28 cu. m. 7. \$109.69. 8. 82.5 sters; 43.2 m. <b>Art. 367.</b> 1. 1000 l. 2. \$1.28. 3. 72 HI.
1.         2.         3.         4.         5.         6.         7.         8.         9.         10.         11.         12.         13.         14.         15	Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 803 oz. 15 pwt. 842.98. 1 <sup>‡</sup> oz. \$68.75. 1,546,875 oz.; 171875 oz. 10480 gr. 1152; 1400. 51 lb. 12 oz. 112000 gr. 85 lb. 16 pwt. 16 gr. 109 gr. ext	8. $\pounds49$ 7s. 9. $\pounds1$ 16s. 2d.; $\pounds2$ 6s. 6d.; 10s. 6d. 10. $39_{\frac{3}{5}5}$ ; $51_{\frac{3}{5}5}$ . 11. $\pounds10$ 10s. 13. $\pounds.808$ . 14. $\pounds.921$ . 15. $\pounds.533$ . 16. $\pounds.867$ . 17. $\pounds.363$ . 18. $\pounds.606$ . 20. 8s. 6d.; 12s. 9d. 21. 16s. 4d.; 4s. 11d. 22. 5s. 1d.; 3s. 8d. 23. 7s. 6d.; 9s. 11d. 24. $\pounds158$ 6s. 8d.; $\pounds79$ 3s. 4d.; $\pounds363$ 6s. 8d.; $\pounds39$ 11s. 8d. 25. 16s. 8d.; $\pounds1$ 12s. 4d.	<ul> <li>5. 88° 33' 45".</li> <li>6. 149° 14' 13".</li> <li>7. 4 hr. 56 min. <sup>1</sup>/<sub>4</sub> sec.</li> <li>8. 54 min. 30<sup>4</sup>/<sub>5</sub> sec.</li> <li>9. 11 hr. 2 min. 59<sup>4</sup>/<sub>15</sub> sec.</li> <li>10. 50 min. 11<sup>7</sup>/<sub>15</sub> sec.</li> <li>11. 5 hr. 4 min. 20<sup>4</sup>/<sub>5</sub> sec.</li> <li>12. 11 hr. 58 min. 11<sup>4</sup>/<sub>15</sub> sec.</li> <li>13. 2 hr.</li> <li>14. 1 hr.</li> <li>15. 3 hr.</li> <li>16. 1 hr.</li> <li>17. 2 hr.</li> <li>18. 0 hr.</li> <li>19. 15 min. 46 sec.</li> <li>20. 40 sec.</li> <li>21. 0 min. 47 sec.</li> </ul>	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <b>Art. 365.</b> 2. 17.218027 cu. m. 3. 28 cu. m. 4. 3.3 cu. m. 5. 4.81208 cu. m. 7. \$109.69. 8. 82.5 sters; 43.2 m. <b>Art. 367.</b> 1. 1000 l. 2. \$1.28. 5. 72 HI. 4. 168 HI
$\begin{array}{c} 1.\\ 2.\\ 3.\\ 4.\\ 5.\\ 6.\\ 7.\\ 8.\\ 9.\\ 10.\\ 11.\\ 12.\\ 13.\\ 14.\\ 15.\\ \end{array}$	Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 803 oz. 15 pwt. \$42.98. 1 <sup>2</sup> oz. \$68.75. 1,546,875 oz.; 171875 oz. 10480 gr. 1152; 1400. 51 lb. 12 oz. 112000 gr. 85 lb. 16 pwt. 16 gr. 192 oz. av.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d. 10. $39\frac{2}{45}$ ; $51\frac{28}{45}$ . 11. £10 10s. 13. £.808. 14. £.921. 15. £.533. 16. £.867. 17. £.363. 18. £.696. 20. 8s. 6d.; 12s. 9d. 21. 16s. 4d.; 4s. 11d. 22. 5s. 1d.; 3s. 8d. 24. £158 6s. 8d.; £79 8s. 4d.; £39 11s. 8d. 25. 16s. 8d.; £1; 13s. 4d.	5. 88° 33' 45". 6. 149° 14' 13". 7. 4 hr. 56 min. $\frac{1}{5}$ sec. 8. 54 min. 30§ sec. 9. 11 hr. 2 min. $59_{1\overline{6}}$ sec. 10. 50 min. 11 $\frac{7}{16}$ sec. 11. 5 hr. 4 min. $20\frac{2}{5}$ sec. 12. 11 hr. 58 min. $11\frac{1}{15}$ sec. 13. 2 hr. 14. 1 hr. 15. 3 hr. 16. 1 hr. 17. 2 hr. 18. 0 hr. 19. 15 min. 46 sec. 20. 40 sec. 21. 9 min. 47 sec.	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <b>Art. 365.</b> 2. 17.218027 cu.m. 3. 28 cu.m. 4. 3.3 cu.m. 5. 4.81208 cu.m. 7. \$109.69. 8. 82.5 sters; 43.2 m. <b>Art. 367.</b> 1. 1000 l. 2. \$1.28. 3. 72 Hl. 4. 168 Hl.
1.         2.         3.         4.         5.         6.         7.         8.         9.         10.         11.         12.         13.         14.         15.         16.	Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 803 oz. 15 pwt. 842.98. 1 <sup>3</sup> oz. \$68.75. 1,546.875 oz.; 171875 oz. 10480 gr. 1152; 1400. 51 lb. 12 oz. 112000 gr. 85 lb. 16 pwt. 16 gr. 192 oz. av. \$16.31.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d. 10. $39\frac{3}{5}$ ; $51\frac{3}{48}$ . 11. £10 10s. 13. £.808. 14. £.921. 15. £.533. 16. £.867. 17. £.363. 18. £.606. 20. 8s. 6d.; 12s. 9d. 21. 16s. 4d.; 4s. 11d. 22. 5s. 1d.; 3s. 8d. 23. 7s. 6d.; 9s. 11d. 24. £158 6s. 8d.; £79 3s. 4d.; £39 11s. 8d. 25. 16s. 8d.; £1; 13s. 4d. 26. \$1100.25;	<ul> <li>5. 88° 33' 45".</li> <li>6. 149° 14' 13".</li> <li>7. 4 hr. 56 min. <sup>1</sup>/<sub>4</sub> sec.</li> <li>8. 54 min. 30<sup>4</sup>/<sub>5</sub> sec.</li> <li>9. 11 hr. 2 min. 59<sup>2</sup>/<sub>16</sub> sec.</li> <li>10. 50 min. 11<sup>7</sup>/<sub>15</sub> sec.</li> <li>11. 5 hr. 4 min. 20<sup>4</sup>/<sub>5</sub> sec.</li> <li>12. 11 hr. 58 min. 11<sup>4</sup>/<sub>8</sub> sec.</li> <li>13. 2 hr.</li> <li>14. 1 hr.</li> <li>15. 3 hr.</li> <li>16. 1 hr.</li> <li>17. 2 hr.</li> <li>18. 0 hr.</li> <li>19. 15 min. 46 sec.</li> <li>21. 9 min. 47 sec.</li> <li>21. 1 min. 1 sec.</li> </ul>	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <b>Art. 365.</b> 2. 17.218027 cu. m. 3. 28 cu. m. 4. 3.3 cu. m. 5. 4.81208 cu. m. 6. 2051.28 cu. m. 7. \$109.69. 8. 82.5 sters; 43.2 m. <b>Art. 367.</b> 1. 1000 l. 2. \$1.28. 3. 72 Hl. 4. 168 Hl. 5. 635 l.;
1.         2.         3.         4.         5.         6.         7.         8.         9.         10.         11.         12.         13.         14.         15.         16.         17	Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 803 oz. 15 pwt. 842.98. 14 oz. \$68.75. 1,546,875 oz.; 171875 oz. 10480 gr. 1152; 1400. 51 lb. 12 oz. 112000 gr. 85 lb. 16 pwt. 16 gr. 192 oz. av. \$16.31. \$10 06	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d. 10. $39\frac{3}{45}$ ; $51\frac{33}{45}$ . 11. £10 10s. 13. £.808. 14. £.921. 15. £.533. 16. £.867. 17. £.363. 18. £.696. 20. 8s. 6d.; 12s. 9d. 21. 16s. 4d.; 4s. 11d. 22. 5s. 1d.; 3s. 8d. 23. 7s. 6d.; 9s. 11d. 24. £158 6s. 8d.; £79 3s. 4d.; £39 11s. 8d. 25. 16s. 8d.; £1; 13s. 4d. 26. \$1100.25; \$663 91	<ul> <li>5. 88° 33' 45".</li> <li>6. 149° 14' 13".</li> <li>7. 4 hr. 56 min. <sup>1</sup>/<sub>4</sub> sec.</li> <li>8. 54 min. 30<sup>4</sup>/<sub>5</sub> sec.</li> <li>9. 11 hr. 2 min. 59<sup>12</sup>/<sub>15</sub> sec.</li> <li>10. 50 min. 11<sup>7</sup>/<sub>15</sub> sec.</li> <li>11. 5 hr. 4 min. 20<sup>4</sup>/<sub>5</sub> sec.</li> <li>12. 11 hr. 58 min. 11<sup>4<sup>3</sup>/<sub>5</sub></sup> sec.</li> <li>13. 2 hr.</li> <li>14. 1 hr.</li> <li>15. 3 hr.</li> <li>16. 1 hr.</li> <li>17. 2 hr.</li> <li>18. 0 hr.</li> <li>19. 15 min. 46 sec.</li> <li>21. 9 min. 47 sec.</li> <li>22. 1 min. 1 sec.</li> <li>23. 9 min. 29 sec.</li> </ul>	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <b>Art. 365.</b> 2. 17.218027 cu. m. 3. 28 cu. m. 4. 3.3 cu. m. 5. 4.81208 cu. m. 7. \$109.69. 8. 82.5 sters; 43.2 m. <b>Art. 367.</b> 1. 1000 l. 2. \$1.28. 3. 72 Hl. 4. 168 Hl. 5. 635 1.; 8875 1
1.         2.         3.         4.         5.         6.         7.         8.         9.         10.         11.         12.         13.         14.         15.         16.         17.	Art. 340. Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 803 oz. 15 pwt. 842.98. 1 <sup>‡</sup> oz. \$68.75. 1,546,875 oz.; 171875 oz. 10480 gr. 1152; 1400. 51 lb. 12 oz. 112000 gr. 85 lb. 16 pwt. 16 gr. 192 oz. av. \$16.31. \$10.06. 9201 cg.	8. $\pounds49$ 7s. 9. $\pounds1$ 16s. 2d.; $\pounds2$ 6s. 6d.; 10s. 6d. 10. $39\frac{3}{5}$ ; $51\frac{3}{48}$ . 11. $\pounds10$ 10s. 13. $\pounds.808$ . 14. $\pounds.921$ . 15. $\pounds.533$ . 16. $\pounds.867$ . 17. $\pounds.363$ . 18. $\pounds.606$ . 20. 8s. 6d.; 12s. 9d. 21. 16s. 4d.; 4s. 11d. 22. 5s. 1d.; 3s. 8d. 23. 7s. 6d.; 9s. 11d. 24. $\pounds158$ 6s. 8d.; $\pounds39$ 11s. 8d. 25. 16s. 8d.; $\pounds135$ 16s. 8d.; $\pounds135$ 16s. 8d.; $\pounds1100.25$ ; \$683.91.	5. 88° 33' 45". 6. 149° 14' 13". 7. 4 hr. 56 min. $\frac{1}{4}$ sec. 8. 54 min. 30 $\frac{4}{5}$ sec. 9. 11 hr. 2 min. $59_{1\overline{4}}$ sec. 10. 50 min. $11_{1\overline{5}}$ sec. 11. 5 hr. 4 min. $20\frac{4}{3}$ sec. 12. 11 hr. 58 min. $11\frac{4}{5}$ sec. 13. 2 hr. 14. 1 hr. 15. 3 hr. 16. 1 hr. 17. 2 hr. 18. 0 hr. 19. 15 min. 46 sec. 20. 40 sec. 21. 9 min. 47 sec. 22. 1 min. 1 sec. 23. 9 min. 29 sec. 24. 90 sec. 24. 90 sec. 25. 9 min. 29 sec. 26. 9 sec.	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <b>Art. 365.</b> 2. 17.218027 cu. m. 3. 28 eu. m. 4. 3.3 cu. m. 5. 4.81208 cu. m. 6. 2051.28 cu. m. 7. \$109.69. 8. 82.5 sters; 43.2 m. <b>Art. 367.</b> 1. 1000 l. 2. \$1.28. 3. 72 Hl. 4. 168 Hl. 5. 635 l.; 8375 l. 6. \$1409
1.         2.         3.         4.         5.         6.         7.         8.         9.         10.         11.         12.         13.         14.         15.         16.         17.         18.	Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 803 oz. 15 pwt. 803 oz. 15 pwt. 842.98. 14 oz. 868.75. 1,546,875 oz.; 171875 oz. 10480 gr. 1152; 1400. 51 lb. 12 oz. 112000 gr. 85 lb. 16 pwt. 16 gr. 192 oz. av. \$16.31 \$10.06. \$321.66.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d. 10. $39\frac{2}{45}$ ; $51\frac{23}{45}$ . 11. £10 10s. 13. £.808. 14. £.921. 15. £.533. 16. £.867. 17. £.363. 18. £.696. 20. 8s. 6d.; 12s. 9d. 21. 16s. 4d.; 4s. 11d. 22. 5s. 1d.; 3s. 8d. 23. 7s. 6d.; 9s. 11d. 24. £158 6s. 8d.; £39 11s. 8d. 25. 16s. 8d.; £11 10s. 4d. 25. 16s. 8d.; £39 11s. 8d. 25. 16s. 8d.; £11 10s. 4d. 26. \$1100.25; \$663.91. 27. £204 18s. 4d.;	<ul> <li>5. 88° 33' 45".</li> <li>6. 149° 14' 13".</li> <li>7. 4 hr. 56 min. <sup>1</sup>/<sub>4</sub> sec.</li> <li>8. 54 min. 30<sup>4</sup>/<sub>5</sub> sec.</li> <li>9. 11 hr. 2 min. 59<sup>1</sup>/<sub>15</sub> sec.</li> <li>10. 50 min. 11<sup>7</sup>/<sub>15</sub> sec.</li> <li>11. 5 hr. 4 min. 20<sup>4</sup>/<sub>5</sub> sec.</li> <li>12. 11 hr. 58 min. 11<sup>4<sup>3</sup>/<sub>5</sub></sup> sec.</li> <li>13. 2 hr.</li> <li>14. 1 hr.</li> <li>15. 3 hr.</li> <li>16. 1 hr.</li> <li>17. 2 hr.</li> <li>18. 0 hr.</li> <li>19. 15 min. 46 sec.</li> <li>20. 40 sec.</li> <li>21. 1 min. 1 sec.</li> <li>23. 9 min. 29 sec.</li> <li>24. 20 min. 19<sup>5</sup>/<sub>8</sub></li> </ul>	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <b>Art. 365.</b> 2. 17.218027 cu. m. 3. 28 cu. m. 4. 3.3 cu. m. 5. 4.81208 cu. m. 6. 2051.28 cu. m. 7. \$109.69. 8. 82.5 sters; 43.2 m. <b>Art. 367.</b> 1. 1000 l. 2. \$1.28. 3. 72 Hl. 4. 168 Hl. 5. 635 1.; 8375 1. 6. \$1498.
1.         2.         3.         4.         5.         6.         7.         8.         9.         10.         11.         12.         13.         14.         15.         16.         17.         18.         20.	Art. 340. Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 803 oz. 15 pwt. 842.98. 1 <sup>‡</sup> oz. \$68.75. 1,546,875 oz.; 171875 oz. 10480 gr. 152; 1400. 51 lb. 12 oz. 112000 gr. 85 lb. 16 pwt. 16 gr. 192 oz. av. \$16.31. \$321.66. \$321.66.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10.s. 6d. 10. $39\frac{2}{45}$ ; $51\frac{2}{45}$ . 11. £10 10s. 13. £.808. 14. £.921. 15. £.533. 16. £.867. 17. £.363. 18. £.696. 20. 8s. 6d.; 12s. 9d. 21. 16s. 4d.; 4s. 11d. 22. 5s. 1d.; 3s. 8d. 23. 7s. 6d.; 9s. 11d. 24. £158 6s. 8d.; £39 11s. 8d. 25. 16s. 8d.; £11 100.25; \$668.91. 27. £204 18s. 4d.; £332 19s. 10d.	5. 88° 33' 45". 6. 149° 14' 13". 7. 4 hr. 56 min. $\frac{1}{5}$ sec. 8. 54 min. 30 $\frac{4}{5}$ sec. 9. 11 hr. 2 min. $59_{1\bar{8}}$ sec. 10. 50 min. 11 $_{1\bar{8}}$ sec. 11. 5 hr. 4 min. $20\frac{4}{3}$ sec. 12. 11 hr. 58 min. $11\frac{18}{15}$ sec. 13. 2 hr. 14. 1 hr. 15. 3 hr. 16. 1 hr. 17. 2 hr. 18. 0 hr. 19. 15 min. 46 sec. 20. 40 sec. 21. 9 min. 47 sec. 22. 1 min. 1 sec. 23. 9 min. 29 sec. 24. 20 min. $19\frac{3}{2}$ sec.	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <b>Art. 365.</b> 2. 17.218027 cu. m. 3. 28 cu. m. 4. 3.3 cu. m. 5. 4.81208 cu. m. 6. 2051.28 cu. m. 7. \$109.69. 8. 82.5 sters; 43.2 m. <b>Art. 367.</b> 1. 1000 l. 2. \$1.28. 3. 72 Hl. 4. 168 Hl. 5. 635 l.; 8375 l. 6. \$1498. 7. 160 Hl.
1.         2.         3.         4.         5.         6.         7.         8.         9.         10.         11.         12.         13.         14.         15.         16.         17.         18.         20.         91	Art. 340. Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 803 oz. 15 pwt. 842.98. 14 oz. \$68.75. 1,546,875 oz.; 171875 oz. 10480 gr. 1152; 1400. 51 lb. 12 oz. 112000 gr. 85 lb. 16 pwt. 16 gr. 192 oz. av. \$16.31. \$321.66. \$91.46. \$91.46.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d. 10. $39\frac{2}{45}$ ; $51\frac{23}{45}$ . 11. £10 10s. 13. £.808. 14. £.921. 15. £.533. 16. £.867. 17. £.363. 18. £.606. 20. 8s. 6d.; 12s. 9d. 21. 16s. 4d.; 4s. 11d. 23. 7s. 6d.; 9s. 11d. 24. £158 6s. 8d.; £39 11s. 8d. 25. 16s. 8d.; £39 11s. 8d. 25. 16s. 8d.; £110.25; §663.91. 27. £204 18s. 4d.; £332 19s. 10d.	<ul> <li>5. 88° 33' 45".</li> <li>6. 149° 14' 13".</li> <li>7. 4 hr. 56 min. <sup>1</sup>/<sub>4</sub> sec.</li> <li>8. 54 min. 30<sup>4</sup>/<sub>5</sub> sec.</li> <li>9. 11 hr. 2 min. 59<sup>1</sup>/<sub>16</sub> sec.</li> <li>10. 50 min. 11<sup>7</sup>/<sub>15</sub> sec.</li> <li>11. 5 hr. 4 min. 20<sup>4</sup>/<sub>5</sub> sec.</li> <li>12. 11 hr. 58 min. 11<sup>4</sup>/<sub>5</sub> sec.</li> <li>13. 2 hr. 14. 1 hr. 15. 3 hr. 16. 1 hr. 17. 2 hr. 18. 0 hr. 19. 15 min. 46 sec.</li> <li>20. 40 sec.</li> <li>21. 9 min. 47 sec.</li> <li>22. 1 min. 1 sec.</li> <li>23. 9 min. 29 sec.</li> <li>24. 20 min. 19<sup>2</sup>/<sub>5</sub> sec.</li> <li>25. 54<sup>6</sup>/<sub>5</sub> % 20<sup>4</sup> W</li> </ul>	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <b>Art. 365.</b> 2. 17.218027 cu. m. 3. 28 cu. m. 4. 3.3 cu. m. 5. 4.81208 cu. m. 6. 2051.28 cu. m. 7. \$109.69. 8. 82.5 sters; 43.2 m. <b>Art. 367.</b> 1. 1000 l. 2. \$1.28. 3. 72 Hl. 4. 168 Hl. 5. 635 L.; 8375 l. 6. \$1498. 7. 160 Hl. 8. 180 bags
1.       2.         3.       4.         5.       6.         7.       8.         9.       10.         11.       12.         13.       14.         15.       16.         17.       18.         20.       21.	Art. 340. Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 808 oz. 15 pwt. 808 oz. 15 pwt. \$42.98. 1 <sup>§</sup> oz. \$68.75. 1,546,875 oz.; 171875 oz. 10480 gr. 1152; 1400. 51 lb. 12 oz. 112000 gr. 85 lb. 16 pwt. 16 gr. 192 oz. av. \$16.31. \$10.06. \$321.66. \$91.46. \$94.76.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d. 10. $39\frac{2}{45}$ ; $51\frac{2}{45}$ . 11. £10 10s. 13. £.808. 14. £.921. 15. £.533. 16. £.867. 17. £.363. 18. £.696. 20. 8s. 6d.; 12s. 9d. 21. 16s. 4d.; 4s. 11d. 22. 5s. 1d.; 3s. 8d. 23. 7s. 6d.; 9s. 11d. 24. £158 6s. 8d.; £79 3s. 4d.; £63 6s. 8d.; £11 13s. 4d. 25. 16s. 8d.; £11 13s. 4d. 26. \$1100.25; \$683.91. 27. £204 18s. 4d.; £332 19s. 10d. Art. 345.	5. 88° 33' 45". 6. 149° 14' 13". 7. 4 hr. 56 min. $\frac{1}{4}$ sec. 8. 54 min. 30§ sec. 9. 11 hr. 2 min. $59_{1\bar{8}}$ sec. 10. 50 min. 11 $\frac{1}{15}$ sec. 11. 5 hr. 4 min. $20\frac{1}{3}$ sec. 12. 11 hr. 58 min. $11\frac{1}{15}$ sec. 13. 2 hr. 14. 1 hr. 15. 3 hr. 16. 1 hr. 17. 2 hr. 18. 0 hr. 19. 15 min. 46 sec. 20. 40 sec. 21. 9 min. 47 sec. 22. 1 min. 1 sec. 23. 9 min. 29 sec. 24. 20 min. $19\frac{1}{3}$ sec. 25. 154° 8' 30' W.	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <b>Art. 365.</b> 2. 17.218027 cu. m. 3. 28 cu. m. 4. 3.3 cu. m. 5. 4.81208 cu. m. 6. 2051.28 cu. m. 7. \$109.69. 8. 82.5 sters; 43.2 m. <b>Art. 367.</b> 1. 1000 l. 2. \$1.28. 5. 72 Hl. 4. 168 Hl. 5. 635 l.; 8375 l. 6. \$1498. 7. 160 Hl. 8. 180 bags. 5. 100 bags.
1.       2.         3.       4.         5.       6.         7.       8.         9.       10.         11.       12.         13.       14.         15.       16.         17.       18.         20.       22.	Art. 340. Art. 340. 1 lb. 8 oz. 16 pwt. 16 gr. 15744 gr. 859 oz. 7 pwt. 12 gr.; 1100 oz. 53 oz. 15 pwt. 803 oz. 15 pwt. 803 oz. 15 pwt. 842.98. 14 oz. \$68.75. 1,546,875 oz.; 171875 oz. 10480 gr. 1152; 1400. 51 lb. 12 oz. 112000 gr. 85 lb. 16 pwt. 16 gr. 192 oz. av. \$16.31. \$321.66. \$91.46. \$94.76. \$73.92.	8. £49 7s. 9. £1 16s. 2d.; £2 6s. 6d.; 10s. 6d. 10. $39\frac{3}{45}$ ; $51\frac{33}{45}$ . 11. £10 10s. 13. £.808. 14. £.921. 15. £.533. 16. £.867. 17. £.363. 18. £.696. 20. 8s. 6d.; 12s. 9d. 21. 16s. 4d.; 4s. 11d. 22. 5s. 1d.; 3s. 8d. 23. 7s. 6d.; 9s. 11d. 24. £158 6s. 8d.; £03 6s. 8d.; £39 11s. 8d. 25. 16s. 8d.; £1; 13s. 4d. 26. \$1100.25; \$683.91. 27. £204 18s. 4d.; £332 19s. 10d. Art. 345.	<ol> <li>5. 88° 33' 45".</li> <li>6. 149° 14' 13".</li> <li>7. 4 hr. 56 min. <sup>1</sup>/<sub>4</sub> sec.</li> <li>8. 54 min. 30<sup>4</sup>/<sub>5</sub> sec.</li> <li>9. 11 hr. 2 min. 59<sup>4</sup>/<sub>15</sub> sec.</li> <li>10. 50 min. 11<sup>4</sup>/<sub>15</sub> sec.</li> <li>11. 5 hr. 4 min. 20<sup>4</sup>/<sub>5</sub> sec.</li> <li>12. 11 hr. 58 min. 11<sup>4<sup>4</sup>/<sub>5</sub></sup> sec.</li> <li>13. 2 hr. 14. 1 hr. 15. 3 hr. 16. 1 hr. 19. 15 min. 46 sec.</li> <li>20. 40 sec.</li> <li>21. 9 min. 47 sec.</li> <li>22. 1 min. 1 sec.</li> <li>23. 9 min. 29 sec.</li> <li>24. 20 min. 19<sup>3</sup>/<sub>5</sub> sec.</li> <li>25. 154° 8' 30' W. 26. 5 F. M.</li> </ol>	6. 400. 7. 166.4 H. 8. \$12.44. 9. 40. 10. 96 H. <b>Art. 365.</b> 2. 17.218027 cu. m. 3. 28 cu. m. 4. 3.3 cu. m. 5. 4.81208 cu. m. 6. 2051.28 cu. m. 7. \$109.69. 8. 82.5 sters; 43.2 m. <b>Art. 367.</b> 1. 1000 l. 2. \$1.28. 3. 72 Hl. 4. 168 Hl. 5. 635 l.; 8375 l. 6. \$1498. 7. 160 Hl. 8. 180 bags. 9. 10080 Dl.

Aut 900	1 01 10500 ft	1 11 \$60.10	1 11 09500
Art. 309.	21. 10000 10.		14. 55000.
1. 1,000,000 g.;	22. \$321.18.	12. \$33.17.	15. \$720.
1000 g.	23. \$1634.09.	13. \$52.55.	16. \$59.38.
2 16 816 T	24. \$808.65.	14. \$1031.97.	17. \$2500.
2 80	25. £19.8375.	15. \$155.36.	18. \$1944.
	26. \$1100.25.	16. \$23.75.	19, 2500,
4. 30.	97 £15 16: 1d	17. \$112.68.	20. 2400
5. 750 g.	00 C10 100 Itt.	10 @149 75	91 \$361.60
<i>6</i> . \$13.608.	28. 210 105.	0, 0140.10	00 00010
7. 62.	29. 33 48.	02101.20.	22. 00240.
8. 9300 Kg.	<i>30</i> . 165000 I.	19. \$16121.	23. \$1502.40.
	31. \$0.526.	20. \$225.	24. \$69.12.
A mt 2141	32. \$0.055.	21. \$823.82.	25. 495 ft.
Art. 011.		22. \$1612.50;	26. £7200.
1. 246.06 vd.:	Apt 389.	\$2700.40.	27. \$196.
8858 25 in	2110.0000	23 \$2325 38	28 \$15360
@ 0.6559 Km	1. \$18.99;	01 00A	20 01500
2. 9.0000 Min.	\$20.34:	24. 004.	29. 091000.
3. 239.008 H.;	\$16.55	26. \$0.94.	30. \$00000.
25900.8 A.	0 00 06	27. \$6.56.	31. \$564.
4. 32808.3 ft.;	2. \$2.00.	28. \$14.71.	32. 400.
6.2137 mi.	3. \$12.10.	29. \$3.96.	33. \$930.
5. 828.04776 lb.	4. \$13.50.	30. \$79.13.	34 \$444.
6 904 19	5. \$5.42.	01 059 99	25 @304
0. 201.12. N 0.0 120 million a .	6. \$12.16.	01. 00.00.	00. 00010
7. 20.75 grams;	7 \$16.39	3%. \$1470.40.	36. 50210.
27.216 grams.	0 029 80		37. \$456.80.
8. 1762 Hl.	0. 00.44	Art. 404.	38. \$505.
9. 668.9375 cu. m.	9. \$5.44.	1110 1010	39. 1425 boxes.
10, 1308 cu. vd.	10. \$40.25.	1. 432.	40. \$59062.50.
11 6540 48 1	11. \$54.07.	2, 868,	11 \$6464
10 901 894 so rd	12. \$76.48.	3. 1604 5	41. 00101.
12. 201.024 Sq. yu.	13. \$245.80.	/ 1916	4.4 4.10
	TO TO TO TO TO TO		
2020.410 Sq. 11.	-	F @105	Art. TLV.
13. 6237 g.;	A art 201	5. \$125.	101 <sup>1</sup> .
<i>13.</i> 6237 g.; 6.237 Kg.	Art. 391.	5. \$125. 6. \$106.	$\begin{array}{c} 1. 0.01\frac{1}{4}.\\ 2. 20\%. \end{array}$
<i>13.</i> 6237 g.; 6.237 Kg.	Art. 391.	5. \$125. 6. \$106. 7. \$162.	$\begin{array}{c} 1. 0.1\frac{1}{4}.\\ 2. 20\%.\\ 3 0.81 \end{array}$
<i>13.</i> 6237 g.; 6.237 Kg.	Art. 391. 2. \$179.80. 3 \$49.50	5. \$125. 6. \$106. 7. \$162. 8. \$1975.	$\begin{array}{c} A & 1. \\ 1. & .01\frac{1}{4}. \\ 2. & 20\%. \\ 3. & .08\frac{1}{3}. \\ 4 & .02 \\ 1. \end{array}$
<i>13.</i> 6237 g.; 6.237 Kg. <i>Art.</i> 387.	Art. 391. 2. \$179.80. 3. \$49.50. 4. \$192.45	5. \$125. 6. \$106. 7. \$162. 8. \$1975. 9. \$243.60.	$\begin{array}{c} A & 1 \\ 1 & .01 \\ 2 & 20 \\ 3 & .08 \\ 4 & .02 \\ 4 & .02 \\ 1 \\ 4 \\ 5 & 21 \\ 1 \\ 8 \\ \end{array}$
<i>13.</i> 6237 g.; 6.237 Kg. <i>Art.</i> 387. 1. 3548	Art. 391. 2. \$179.80. 3. \$49.50. 4. \$193.45.	5. \$125. 6. \$106. 7. \$162. 8. \$1975. 9. \$243.60. 10. \$487.10.	$\begin{array}{c} A & 1 \\ 1 & .01 \\ 2 & 20 \\ 3 & .08 \\ 4 & .02 \\ 1 \\ 5 & 3 \\ 4 \\ 5 \\ 5 \\ 5 \\ 5 \\ 5 \\ 5 \\ 5 \\ 5 \\ 5$
2020.410 Sq. 10. 13. 6237 Kg. Art. 387. 1. 35 129. 2. 1135.94.	Art. 391. 2. \$179.80. 3. \$49.50. 4. \$193.45. 5. \$168.	7. \$125. 6. \$106. 7. \$162. 8. \$1975. 9. \$243.60. 10. \$487.10. 11. \$126.43	Art. $1.01\frac{1}{4}$ . 2. 20%. 308 $\frac{1}{4}$ . 402 $\frac{1}{18}$ . 5. $3\frac{1}{8}$ %. 6. $1\frac{1}{4}$ %.
2.50.37 ft; 6.237 Kg. Art. 387. 2. 1135.94. 3. 5 mo. 24 da.;	Art. 391. 2. \$179.80. 3. \$40.50. 4. \$193.45. 5. \$168. 6. \$277.53.	7. \$125. 6. \$106. 7. \$162. 8. \$1975. 9. \$243.60. 10. \$487.10. 11. \$176.43. 19. \$299.25	$\begin{array}{c} 1.014\\ 2.20\%\\ 3.084\\ 4.027\\ 5.35\%\\ 6.14\%\\ 7.64\%. \end{array}$
2000.410 Sq. 11. 13. 6237 G.; 6.237 Kg. Art. 387. 1. 35 42 2. 1135.94. 3. 5 mo. 24 da.; 178 da.	Art. 391. 2. \$179.80. 3. \$49.50. 4. \$193.45. 5. \$168. 6. \$277.53. 7. \$4.	7. \$125. 6. \$106. 7. \$162. 8. \$1975. 9. \$243.60. 10. \$487.10. 11. \$176.43. 12. \$328.35. 14. \$924.70	$\begin{array}{c} 1. 0.1_{4}.\\ 2. 20\%.\\ 3. 0.8_{3}.\\ 4. 0.2_{19}.\\ 5. 3_{4}\%.\\ 6. 1_{4}\%.\\ 7. 6_{4}\%.\\ 8. 2_{2}\%.\\ \end{array}$
2000.410 Sq. 11. 13. 6237 g.; 6.237 Kg. Art. 387. 1. 35 192. 2. 1135.94. 3. 5 mo. 24 da.; 178 da. 4 8	Art. 391. 2. \$179.80. 3. \$49.50. 4. \$193.45. 5. \$168. 6. \$277.53. 7. \$4. 8. \$289.39.	7. \$125. 6. \$106. 7. \$162. 8. \$1975. 9. \$243.60. 10. \$487.10. 11. \$176.43. 12. \$328.35. 14. \$2494.79.	$\begin{array}{c} 1. 0.1\frac{1}{4}.\\ 2. 20\%.\\ 3. 0.8\frac{1}{4}.\\ 4. 0.2\frac{1}{18}.\\ 5. 3\frac{1}{8}\%.\\ 6. 1\frac{1}{4}\%.\\ 7. 6\frac{1}{4}\%.\\ 8. 2\frac{1}{2}\%.\\ 9. 1\frac{1}{8}\%. \end{array}$
2020.410 Sq. 11. 13. 6237 G; 6.237 Kg. Art. 387. 2. 1135.94. 3. 5 mo. 24 da.; 178 da. 4. 8. 5. 90 ft	Art. 391. 2. \$179.80. 3. \$40.50. 4. \$193.45. 5. \$168. 6. \$277.53. 7. \$4. 8. \$289.39. 9. \$96.25.	$\begin{array}{c} 7. \ \$125. \\ 6. \ \$106. \\ 7. \ \$162. \\ 8. \ \$1975. \\ 9. \ \$243.60. \\ 10. \ \$487.10. \\ 11. \ \$176.43. \\ 12. \ \$328.35. \\ 14. \ \$2434.79. \\ 15. \ \$184.38. \end{array}$	$\begin{array}{c} 1.014.\\ 2.20\%.\\ 3.084.\\ 4.0218.\\ 5.31\%.\\ 6.14\%.\\ 7.64\%.\\ 8.22\%.\\ 9.18\%.\\ 10.334\%.\\ \end{array}$
2020.410 Sq. 11. 13. 6237 G.; 6.237 Kg. Art. 387. 1. 35 42 2. 1135.94. 3. 5 mo. 24 da.; 178 da. 4. 8. 5. 32 ft.	Art. 391. 2. \$179.80. 3. \$49.50. 4. \$193.45. 5. \$168. 6. \$277.53. 7. \$4. 8. \$289.39. 9. \$96.25. 10. \$21.69.	$\begin{array}{c} 7. \\ 5. \\ 8.125. \\ 6. \\ 8.106. \\ 7. \\ 8. \\ 8. \\ 9.75. \\ 9. \\ 8243.60. \\ 10. \\ 8487.10. \\ 11. \\ 8176.43. \\ 12. \\ 8328.35. \\ 14. \\ 82434.79. \\ 15. \\ 8184.38. \\ 16. \\ 864.94. \\ \end{array}$	$\begin{array}{c} 1. 0.1_{1}.\\ 2. 20\%.\\ 3. 0.8_{1}.\\ 4. 0.2_{1}.\\ 5. 3_{1}\%.\\ 6. 1_{4}\%.\\ 7. 6_{1}\%.\\ 8. 2_{2}\%.\\ 9. 1_{7}\%.\\ 10. 33_{1}\%.\\ 11. 95\%.\\ \end{array}$
2020.410 Sq. 1. 13. 6237 g.; 6.237 Kg. Art. 387. 1. 35 49. 2. 1135.94. 3. 5 mo. 24 da.; 178 da. 4. 8. 5. 32 ft. 6. 702 sq. ft.;	Art. 391. 2. \$179.80. 3. \$49.50. 4. \$193.45. 5. \$168. 6. \$277.53. 7. \$4. 8. \$289.39. 9. \$96.25. 10. \$21.62. 11. \$7.56.	$\begin{array}{c} 7. \\ 5. \\ 8.125. \\ 6. \\ 8.106. \\ 7. \\ 8.1075. \\ 9. \\ 8243.60. \\ 10. \\ 8487.10. \\ 11. \\ 8176.43. \\ 12. \\ 8328.35. \\ 14. \\ 82434.79. \\ 15. \\ 8184.38. \\ 16. \\ 864.94. \\ 17. \\ 84100. \end{array}$	$\begin{array}{c} 1. 0.1 \frac{1}{4}.\\ 2. 20\%.\\ 3. 0.8 \frac{1}{4}.\\ 4. 0.2 \frac{1}{19}.\\ 5. 3 \frac{1}{5}\%.\\ 6. 1\frac{1}{4}\%.\\ 7. 6\frac{1}{4}\%.\\ 8. 2\frac{1}{5}\%.\\ 9. 1\frac{3}{5}\%.\\ 10. 33\frac{1}{5}\%.\\ 10. 33\frac{1}{5}\%.$
2020.410 Sq. 1. 23. 6237 Kg. Art. 387. 2. 135.42 3. 5 mo. 24 da.; 178 da. 4. 8. 5. 32 ft. 6. 702 sq. ft.; 210 sq. ft.;	Art. 391. 2. \$179.80. 3. \$40.50. 4. \$193.45. 5. \$168. 6. \$277.53. 7. \$4. 8. \$289.39. 9. \$06.25. 10. \$21.62. 11. \$7.56. 12. \$26.00	7. $$125.$ 6. $$106.$ 7. $$162.$ 8. $$1975.$ 9. $$243.60.$ 10. $$487.10.$ 11. $$176.43.$ 12. $$328.35.$ 14. $$24347.79.$ 15. $$184.38.$ 16. $$64.94.$ 17. $$4100.$ 18. $$4500:$	$\begin{array}{c} 1.014.\\ 1.014.\\ 2.20\%.\\ 3.084.\\ 4.0218.\\ 5.38\%.\\ 6.14\%.\\ 7.64\%.\\ 8.22\%.\\ 9.18\%.\\ 10.334\%.\\ 10.334\%.\\ 11.25\%.\\ 12.3\%0.\\ 12.3\%0.\\ \end{array}$
200.0.410 sq. 1. 13. 6237 g.; 6.237 Kg. Art. 387. 1. $35\frac{49}{129}$ . 2. 1135.94. 3. 5 mo. 24 da.; 178 da. 4. 8. 5. 32 ft. 6. 702 sq. ft.; 1320 sq. ft.;	Art. 391. 2. \$179.80. 3. \$40.50. 4. \$193.45. 5. \$168. 6. \$277.53. 7. \$4. 8. \$289.39. 9. \$06.25. 10. \$21.62. 11. \$7.56. 12. \$36.60. 13. \$25. \$107.	7. $\$125.$ 6. $\$106.$ 7. $\$162.$ 8. $\$1975.$ 9. $\$243.60.$ 10. $\$487.10.$ 11. $\$176.43.$ 12. $\$2838.35.$ 14. $\$2434.79.$ 15. $\$184.38.$ 16. $\$64.94.$ 17. $\$4100.$ 18. $\$4500;$ \$16.88.	$\begin{array}{c} 1. 0.1 \frac{1}{4}.\\ 2. 20\%.\\ 3. 0.8 \frac{1}{3}.\\ 4. 0.2 \frac{1}{18}.\\ 5. 3\frac{1}{5}\%.\\ 6. 1\frac{1}{4}\%.\\ 7. 6\frac{1}{4}\%.\\ 7. 6\frac{1}{4}\%.\\ 9. 1\frac{1}{5}\%.\\ 10. 33\frac{1}{8}\%.\\ 11. 25\%.\\ 12. \frac{9}{5}\%.\\ 13. 2200.\\ \end{array}$
2020.4.10 Sq. 1. 13. 6237 G.; 6.237 Kg. Art. 387. 1. $35_{\frac{19}{22}}$ . 2. 1135.94. 3. 5 mo. 24 da.; 178 da. 4. 8. 5. 32 ft. 6. 702 sq. ft. ; 210 sq. ft.; 1320 sq. ft. 7. \$172.36.	Art. 391. 2. \$179.80. 3. \$49.50. 4. \$193.45. 5. \$168. 6. \$277.53. 7. \$4. 8. \$289.39. 9. \$06.25. 10. \$21.62. 11. \$7.56. 12. \$36.60. 13. \$85 ; \$107.	$\begin{array}{c} 7. \ 8125. \\ 6. \ 8106. \\ 7. \ 8162. \\ 8. \ 81975. \\ 9. \ 8243.60. \\ 10. \ 8487.10. \\ 11. \ 8176.43. \\ 12. \ 8328.35. \\ 14. \ 82434.79. \\ 15. \ 8184.38. \\ 16. \ 864.94. \\ 17. \ 84100. \\ 18. \ 84500; \\ \ 816.88. \end{array}$	$\begin{array}{c} A76. \pm 100 \\ 1014. \\ 2. 20\%. \\ 308\frac{1}{3}. \\ 402\frac{1}{19}. \\ 5. 3\frac{1}{3}\%. \\ 6. 1\frac{1}{4}\%. \\ 7. 6\frac{1}{4}\%. \\ 8. 2\frac{1}{2}\%. \\ 9. 1\frac{3}{7}\%. \\ 10. 33\frac{1}{3}\%. \\ 11. 25\%. \\ 12. \frac{3}{20}\%. \\ 13. 2200. \\ 14. 12\frac{1}{2}\%. \end{array}$
2000.710 Sq. 11. 2000.710 Sq. 11. 21. 6237 Kg. Art. 387. 2. 1135.94. 3. 5 mo. 24 da.; 178 da. 4. 8. 5. 32 ft. 6. 702 sq. ft.; 210 sq. ft.; 1320 sq. ft. 7. \$172.36. 8. \$127.49.	Art. 391. 2. \$179.80. 3. \$40.50. 4. \$193.45. 5. \$168. 6. \$277.53. 7. \$4. 8. \$289.39. 9. \$06.25. 10. \$21.62. 11. \$7.56. 12. \$36.60. 13. \$85; \$107. 14. \$18.75.	7. \$125. 6. \$106. 7. \$162. 8. \$1975. 9. \$243.60. 10. \$487.10. 11. \$176.43. 12. \$328.35. 14. \$2434.79. 15. \$184.38. 16. \$64.94. 17. \$4100. 18. \$4500; \$16.88.	$\begin{array}{c} 1. 0.1\frac{1}{4}.\\ 2. 20\%.\\ 3. 0.8\frac{1}{4}.\\ 4. 0.2\frac{1}{18}.\\ 5. 3\frac{1}{4}\%.\\ 6. 1\frac{1}{4}\%.\\ 7. 6\frac{1}{4}\%.\\ 7. 6\frac{1}{4}\%.\\ 8. 2\frac{1}{2}\%.\\ 10. 33\frac{1}{8}\%.\\ 11. 25\%.\\ 12. \frac{3}{2}0\%.\\ 13. 2200.\\ 14. 12\frac{1}{8}\%.\\ 15. 45\%.\\ \end{array}$
200.0.40 sq. 1. 13. 6237 g.; 6.237 Kg. Art. 387. 1. $35\frac{49}{129}$ . 2. 1135.94. 3. 5 mo. 24 da.; 178 da. 4. 8. 5. 32 ft. 6. 702 sq. ft. ; 1320 sq. ft. ; 1320 sq. ft. 7. \$172.36. 8. \$127.49. 9. 43200 sq. rd.	Art. 391. 2. \$179.80. 3. \$40.50. 4. \$193.45. 5. \$168. 6. \$277.53. 7. \$4. 8. \$289.39. 9. \$06.25. 10. \$21.62. 11. \$7.56. 12. \$36.60. 13. \$85 ; \$107. 14. \$18.75. 15. \$81; \$90.	7. \$125. 6. \$106. 7. \$162. 8. \$1975. 9. \$243.60. 10. \$487.10. 11. \$176.43. 12. \$328.35. 14. \$2434.79. 15. \$184.38. 16. \$64.94. 17. \$4100. 18. \$4500; \$16.88. Art. 407.	$\begin{array}{c} 1. 0.1\frac{1}{4}.\\ 2. 20\%.\\ 3. 0.8\frac{1}{3}.\\ 4. 0.2\frac{1}{18}.\\ 5. 3\frac{1}{5}\%.\\ 6. 1\frac{1}{4}\%.\\ 7. 6\frac{1}{4}\%.\\ 7. 6\frac{1}{4}\%.\\ 9. 1\frac{1}{5}\%.\\ 10. 33\frac{1}{8}\%.\\ 11. 25\%.\\ 12. \frac{3}{2}0\%.\\ 13. 2200.\\ 14. 12\frac{1}{2}\%.\\ 15. 45\%.\\ 16. 44\%.\\ \end{array}$
200.0.410 Sq. 11. 13. 6237 G.; 6.237 Kg. Art. 387. 1. $35\frac{49}{128}$ . 2. 1135.94. 3. 5 mo. 24 da.; 178 da. 4. 8. 5. 32 ft. 6. 702 sq. ft. ; 210 sq. ft.; 1320 sq. ft. 7. \$172.36. 8. \$127.49. 9. 43200 sq. rd.	Art. 391. 2. \$179.80. 3. \$49.50. 4. \$193.45. 5. \$168. 6. \$277.53. 7. \$4. 8. \$289.39. 9. \$96.25. 10. \$21.62. 11. \$7.56. 12. \$36.60. 13. \$85 ; \$107. 14. \$18.75. 15. \$81; \$90. 16. \$274.81.	7.       \$125.         6.       \$106.         7.       \$162.         8.       \$1975.         9.       \$243.60.         10.       \$487.10.         11.       \$176.43.         12.       \$328.35.         14.       \$2434.79.         15.       \$184.38.         16.       \$64.94.         17.       \$4100.         18.       \$4500;         \$16.88.       Art. 407.         1.       8.	$\begin{array}{c} A76. \pm 100 \\ 1014. \\ 2. 20\%. \\ 308\frac{1}{3}. \\ 402\frac{1}{19}. \\ 5. 3\frac{1}{3}\%. \\ 6. 14\%. \\ 7. 6\frac{1}{4}\%. \\ 7. 6\frac{1}{4}\%. \\ 7. 6\frac{1}{3}\%. \\ 10. 33\frac{1}{3}\%. \\ 11. 25\%. \\ 12. \frac{1}{9}\%. \\ 13. 2200. \\ 14. 12\frac{1}{2}\%. \\ 15. 45\%. \\ 16. 44\%. \\ 17. \frac{1}{4}\%; \end{array}$
2020.710 Sq. 11. 2020.710 Sq. 11. 21. 6237 Kg. Art. 387. 2. 1135.94. 3. 5 mo. 24 da.; 178 da. 4. 8. 5. 32 ft. 6. 702 sq. ft.; 210 sq. ft.; 1320 sq. ft. 7. \$172.36. 8. \$127.49. 9. 43200 sq. ft. 10. 480 sq. ft.	Art. 391. 2. \$179.80. 3. \$40.50. 4. \$193.45. 5. \$168. 6. \$277.53. 7. \$4. 8. \$289.39. 9. \$06.25. 10. \$21.62. 11. \$7.56. 12. \$36.60. 13. \$85 ; \$107. 14. \$18.75. 15. \$31; \$90. 16. \$274.81.	7. \$125. 6. \$106. 7. \$162. 8. \$1975. 9. \$243.60. 10. \$487.10. 11. \$176.43. 12. \$328.35. 14. \$2434.79. 15. \$184.38. 16. \$64.94. 17. \$4100. 18. \$4500; \$16.88. Art. 407. 1. 8. 9. \$000	$\begin{array}{c} 1. 014.\\ 2. 20\%.\\ 3. 084.\\ 4. 0274.\\ 5. 34\%.\\ 6. 14\%.\\ 7. 64\%.\\ 8. 22\%.\\ 9. 18\%.\\ 10. 334\%.\\ 11. 25\%.\\ 12. 36\%.\\ 13. 2200.\\ 14. 124\%.\\ 15. 45\%.\\ 16. 44\%.\\ 17. 12\%;\\ 842.50.\\ \end{array}$
2000.410 Sq. 11. 23. 6237 G.; 6.237 Kg. Art. 387. 1. 35 49. 2. 1135.94. 3. 5 mo. 24 da.; 178 da. 4. 8. 5. 32 ft. 6. 702 sq. ft.; 120 sq. ft.; 1320 sq. ft. 7. \$172.36. 8. \$127.49. 9. 43200 sq. rd. 10. 480 sq. ft. 11. 3110 ft.	Art. 391. 2. \$179.80. 3. \$40.50. 4. \$193.45. 5. \$168. 6. \$277.53. 7. \$4. 8. \$289.39. 9. \$06.25. 10. \$21.62. 11. \$7.56. 12. \$36.60. 13. \$85; \$107. 14. \$18.75. 15. \$91; \$90. 16. \$274.81.	7. \$125. 6. \$106. 7. \$162. 8. \$1975. 9. \$243.60. 10. \$487.10. 11. \$176.43. 12. \$328.35. 14. \$2434.79. 15. \$184.38. 16. \$64.94. 17. \$4100. 18. \$4500; \$16.88. Art. 407. 1. 8. 2. 800. 2. 5400	$\begin{array}{c} 1. 014. \\ 1. 014. \\ 2. 20\%. \\ 3. 084. \\ 4. 0274. \\ 5. 31\%. \\ 6. 14\%. \\ 7. 64\%. \\ 8. 21\%. \\ 9. 15\%. \\ 10. 331\%. \\ 10. 331\%. \\ 10. 331\%. \\ 11. 25\%. \\ 12. 5\%. \\ 12. 5\%. \\ 13. 2200. \\ 14. 124\%. \\ 15. 45\%. \\ 16. 44\%. \\ 17. \frac{1}{1}\%; \\ \frac{3}{1}\%. \\ 16. 44\%. \\ 17. \frac{1}{1}\%; \\ \frac{3}{1}\%. \\ 16. 41\%. \\ 17. \frac{1}{1}\%; \\ \frac{3}{1}\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10. 10\%. \\ 10.$
2020.410 Sq. 11. 23. 6237 G.; 6.237 Kg. Art. 387. 1. 35 42 2. 1135.94. 3. 5 mo. 24 da.; 178 da. 4. 8. 5. 32 ft. 6. 702 sq. ft. ; 210 sq. ft.; 1320 sq. ft. 7. \$172.36. 8. \$127.49. 9. 43200 sq. rt. 10. 480 sq. rt. 11. 3110 ft. 12. \$128.	Art. 391. 2. \$179.80. 3. \$40.50. 4. \$193.45. 5. \$168. 6. \$277.53. 7. \$4. 8. \$289.39. 9. \$96.25. 10. \$21.62. 11. \$7.56. 12. \$36.60. 13. \$85 ; \$107. 14. \$18.75. 15. \$\$1; \$90. 16. \$274.81. Art. 402.	7.       \$125.         6.       \$106.         7.       \$162.         8.       \$1975.         9.       \$243.60.         10.       \$487.10.         11.       \$176.43.         12.       \$328.35.         14.       \$2434.79.         15.       \$184.38.         16.       \$64.94.         17.       \$4100.         18.       \$4500;         \$16.88. <b>Art. 407.</b> 1.       8.         2.       \$00.         3.       5400.         5.       5400.	Art. $100$ 1. $014$ . 2. $20\%$ . 3. $08\frac{1}{2}$ . 4. $02\frac{1}{19}$ . 5. $3\frac{1}{2}\%$ . 6. $14\%$ . 7. $6\frac{1}{4}\%$ . 9. $1\frac{1}{2}\%$ . 10. $33\frac{1}{4}\%$ . 10. $33\frac{1}{4}\%$ . 11. $25\%$ . 12. $\frac{3}{2}\%$ . 13. $2200$ . 14. $12\frac{1}{2}\%$ . 15. $45\%$ . 16. $44\%$ . 17. $\frac{1}{4}\%$ ; $\frac{4}{4}\%$ . 19. $1\frac{4}{2}\%$ . 10. $1\frac{4}{2}\%$ . 10. $1\frac{4}{2}\%$ . 11. $1\frac{4}{2}\%$ . 12. $\frac{1}{2}\%$ . 13. $2200$ . 14. $12\frac{1}{2}\%$ . 15. $45\%$ . 16. $44\%$ . 17. $\frac{1}{2}\%$ ; $\frac{1}{2}\%$ . 18. $4\frac{1}{2}\%$ . 19. $1\frac{4}{2}\%$ . 19
20.0.37 ft; 6.237 Kg. Art. 387. 2. 35 42. 2. 1135.94. 3. 5 mo. 24 da.; 178 da. 4. 8. 5. 32 ft. 6. 702 sq. ft.; 210 sq. ft.; 1320 sq. ft.; 1320 sq. ft. 7. \$172.36. 8. \$127.49. 9. 43200 sq. ft. 11. 3110 ft. 12. \$128. 13. 628 ft.	Art. 391. 2. \$179.80. 3. \$40.50. 4. \$193.45. 5. \$168. 6. \$277.53. 7. \$4. 8. \$289.39. 9. \$06.25. 10. \$21.62. 11. \$7.56. 12. \$36.60. 13. \$85 ; \$107. 14. \$18.75. 15. \$81; \$90. 16. \$274.81. Art. 402. 1. 51.84.	7. \$125. 6. \$106. 7. \$162. 8. \$1975. 9. \$243.60. 10. \$487.10. 11. \$176.43. 12. \$328.35. 14. \$2434.79. 15. \$184.38. 16. \$64.94. 17. \$4100. 18. \$4500; \$16.88. Art. 407. 1. 8. 2. 800. 3. 5400. 4. 5600.	$\begin{array}{c} 1. 014.\\ 2. 20\%.\\ 3. 084.\\ 4. 0214.\\ 5. 34\%.\\ 6. 14\%.\\ 7. 64\%.\\ 8. 25\%.\\ 9. 18\%.\\ 10. 334\%.\\ 11. 25\%.\\ 12. 34\%.\\ 13. 2200.\\ 14. 124\%.\\ 15. 45\%.\\ 16. 44\%.\\ 17. 12\%;\\ 842.50.\\ 18. 44\%.\\ 19. 16\%.\\ 19. 16\%.\\ 19. 16\%.\\ 19. 16\%.\\ 10. 31\%.\\ 19. 16\%.\\ 10. 31\%.\\ 19. 16\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 31\%.\\ 10. 3$
2000.410 Sq. 11. 23. 6237 G.; 6.237 Kg. Art. 387. 1. 35 49. 2. 1135.94. 3. 5 mo. 24 da.; 178 da. 4. 8. 5. 32 ft. 6. 702 sq. ft.; 1320 sq. ft.; 1320 sq. ft. 7. \$172.36. 8. \$127.49. 9. 43200 sq. rd. 10. 480 sq. ft. 11. 3110 ft. 12. \$128. 13. 628 ft. 14. 15.708 ft.	Art. 391. 2. \$179.80. 3. \$40.50. 4. \$193.45. 5. \$168. 6. \$277.53. 7. \$4. 8. \$289.39. 9. \$96.25. 10. \$21.62. 11. \$7.56. 12. \$36.60. 13. \$85; \$107. 14. \$18.75. 15. \$91; \$90. 16. \$274.81. Art. 402. 1. 51.84. 2. 60.	7. \$125. 6. \$106. 7. \$162. 8. \$1975. 9. \$243.60. 10. \$487.10. 11. \$176.43. 12. \$328.35. 14. \$2434.79. 15. \$184.38. 16. \$64.94. 17. \$4100. 18. \$4500; \$16.88. Art. 407. 1. 8. 2. 800. 3. 5400. 4. 5600. 5. 9375.	$\begin{array}{c} 1. 0.1\frac{1}{4}.\\ 2. 20\%.\\ 3. 0.8\frac{1}{4}.\\ 4. 0.9\frac{1}{12}.\\ 5. 3\frac{1}{5}\%.\\ 6. 1\frac{1}{4}\%.\\ 7. 6\frac{1}{4}\%.\\ 8. 2\frac{1}{2}\%.\\ 9. 1\frac{1}{5}\%.\\ 10. 33\frac{1}{5}\%.\\ 10. 33\frac{1}{5}\%.\\ 11. 25\%.\\ 12. \frac{3}{2}0\%.\\ 13. 2200.\\ 14. 12\frac{1}{5}\%.\\ 15. 45\%.\\ 16. 44\%.\\ 17. \frac{1}{5}\%:\\ \frac{842.50}{18. 4\frac{1}{4}\%.}\\ 19. 16\%.\\ 20. 56\frac{1}{5}\%.\\ \end{array}$
2020.410 Sq. 11. 23. 6237 G.; 6.237 Kg. Art. 387. 1. 35 49 2. 1135.94. 3. 5 mo. 24 da.; 178 da. 4. 8. 5. 32 ft. 6. 702 sq. ft.; 210 sq. ft.; 1320 sq. ft. 7. \$172.36. 8. \$127.49. 9. 43200 sq. rd. 10. 480 sq. ft. 11. 3110 ft. 12. \$128. 13. 628 ft. 14. 15.708 ft. 15. 28.27 sq. ft.	Art. 391. 2. \$179.80. 3. \$40.50. 4. \$193.45. 5. \$168. 6. \$277.53. 7. \$4. 8. \$289.39. 9. \$06.25. 10. \$21.62. 11. \$7.56. 12. \$36.60. 13. \$85; \$107. 14. \$18.75. 15. \$81; \$90. 16. \$274.81. Art. 402. 1. 51.84. 2. 60. 3. 17.92.	7.       \$125.         6.       \$106.         7.       \$162.         8.       \$1975.         9.       \$243.60.         10.       \$487.10.         11.       \$176.43.         12.       \$328.35.         14.       \$2434.79.         15.       \$184.38.         16.       \$64.94.         17.       \$4100.         18.       \$4500;         \$16.88. <b>Art. 407.</b> 1.       8.         2.       \$00.         3.       \$400.         4.       \$600.         5.       \$9875.         6.       \$22.8.	$\begin{array}{c} A16. \ 1000 \\ 1. \ 0.014. \\ 2. \ 20\%. \\ 3. \ 0.08\frac{1}{2}. \\ 4. \ 0.02\frac{1}{10}. \\ 5. \ 31\frac{1}{2}\%. \\ 6. \ 14\%. \\ 7. \ 6\frac{1}{4}\%. \\ 7. \ 6\frac{1}{4}\%. \\ 9. \ 1\frac{2}{5}\%. \\ 10. \ 33\frac{1}{4}\%. \\ 10. \ 33\frac{1}{4}\%. \\ 11. \ 25\%. \\ 12. \ \frac{9}{6}\%. \\ 13. \ 2200. \\ 14. \ 12\frac{1}{2}\%. \\ 15. \ 45\%. \\ 16. \ 44\%. \\ 17. \ \frac{1}{2}\%; \\ \frac{8}{42.50}. \\ 18. \ 4\frac{1}{2}\%. \\ 19. \ 16\%. \\ 20. \ 56\frac{1}{4}\%. \\ 21. \ 4\frac{1}{4}\%. \end{array}$
2000.7 ft. 2000.7 ft.; 6.237 Kg. Art. 387. 2. 1135.94. 3. 5 mo. 24 da.; 178 da. 4. 8. 5. 32 ft. 6. 702 sq. ft.; 210 sq. ft.; 1320 sq. ft.; 1320 sq. ft. 7. \$172.36. 8. \$127.49. 9. 43200 sq. rd. 10. 480 sq. ft. 11. 3110 ft. 12. \$128. 13. 628 ft. 14. 15.708 ft. 15. 28.27 sq. ft.; 78.54 sq. ft.	Art. 391. 2. \$179.80. 3. \$40.50. 4. \$193.45. 5. \$168. 6. \$277.53. 7. \$4. 8. \$289.39. 9. \$06.25. 10. \$21.62. 11. \$7.56. 12. \$36.60. 13. \$85 ; \$107. 14. \$18.75. 15. \$81; \$90. 16. \$274.81. Art. 402. 1. 51.84. 2. 60. 3. 17.92. 4. 23.22.	7. 5125. 6. \$125. 6. \$106. 7. \$162. 8. \$1975. 9. \$243.60. 10. \$487.10. 11. \$176.43. 12. \$328.35. 14. \$2434.79. 15. \$184.38. 16. \$64.94. 17. \$4100. 18. \$4500; \$16.88. Art. 407. 1. 8. 2. 800. 3. 5400. 4. 5600. 5. 9375. 6. 22.8. 7. 1800.	$\begin{array}{c} 1. 014.\\ 2. 20\%.\\ 3. 084.\\ 4. 0274.\\ 5. 34\%.\\ 6. 14\%.\\ 7. 64\%.\\ 8. 22\%.\\ 9. 14\%.\\ 10. 334\%.\\ 10. 334\%.\\ 11. 25\%.\\ 12. 36\%.\\ 13. 2200.\\ 14. 124\%.\\ 15. 45\%.\\ 16. 44\%.\\ 17. \frac{1}{2}\%.\\ 16. 44\%.\\ 17. \frac{1}{2}\%.\\ 18. 44\%.\\ 19. 16\%.\\ 20. 564\%.\\ 21. 44\%.\\ 22. 184\%.\\ \end{array}$
2000.410 Sq. 11. 2000.710 Sq. 11. 21. 6237 Kg. Art. 387. 2. 1135.94. 3. 5 mo. 24 da.; 178 da. 4. 8. 5. 32 ft. 6. 702 sq. ft.; 120 sq. ft.; 1320 sq. ft. 7. \$172.36. 8. \$127.49. 9. 43200 sq. rd. 10. 480 sq. ft. 11. 3110 ft. 12. \$128. 13. 628 ft. 14. 15.708 ft. 15. 28.27 sq. ft.; 78.54 sq. ft. 16. 429 ft. 17. 509 ft. 16. 429 ft. 13. 628 ft. 14. 15.708 ft. 15. 28.27 sq. ft.; 16. 429 ft. 17. 509 ft. 17. 500 ft. 17. 50	Art. 391. 2. $\$179.80.$ 3. $\$40.50.$ 4. $\$193.45.$ 5. $\$168.$ 6. $\$277.53.$ 7. $\$4.$ 8. $\$289.39.$ 9. $\$96.25.$ 10. $\$21.62.$ 11. $\$7.56.$ 12. $\$36.60.$ 13. $\$85$ ; $\$107.$ 14. $\$18.75.$ 15. $\$91$ ; $\$90.$ 16. $\$274.81.$ Art. 402. 1. 51.84. 2. 60. 3. $17.92.$ 4. 23.22. 5. 56.7	7. \$125. 6. \$106. 7. \$162. 8. \$1975. 9. \$243.60. 10. \$487.10. 11. \$176.43. 12. \$328.35. 14. \$2434.79. 15. \$184.38. 16. \$64.94. 17. \$4100. 18. \$4500; \$16.88. Art. 407. 1. 8. 2. 800. 3. 5400. 4. 5600. 5. 9375. 6. 22.8. 7. 1800. 8. 800.	1. 014. 2. 20%. 3. 08 $\frac{1}{2}$ . 4. 02 $\frac{1}{12}$ . 5. 3 $\frac{1}{2}$ %. 6. 1 $\frac{1}{4}$ %. 7. 6 $\frac{1}{4}$ %. 9. 1 $\frac{1}{2}$ %. 9. 1 $\frac{1}{2}$ %. 10. 33 $\frac{1}{2}$ %. 11. 25%. 12. $\frac{3}{20}$ %. 13. 2200. 14. 12 $\frac{1}{2}$ %. 15. 45%. 16. 44%. 17. $\frac{1}{2}$ %. 18. 4 $\frac{1}{2}$ %. 19. 16%. 20. 56 $\frac{1}{4}$ %. 21. 4 $\frac{4}{8}$ %. 23. 6 $\frac{1}{4}$ %.
2020.410 Sq. 11. 23. 6237 G.; 6.237 Kg. Art. 387. 1. 35 49 2. 1135.94. 3. 5 mo. 24 da.; 178 da. 4. 8. 5. 32 ft. 6. 702 sq. ft. ; 210 sq. ft. ; 1320 sq. ft. 7. \$172.36. 8. \$127.49. 9. 43200 sq. rd. 10. 480 sq. ft. 11. 3110 ft. 12. \$128. 13. 628 ft. 14. 15.708 ft. 15. 28.27 sq. ft. ; 78.54 sq. ft. 19. 25042 lb.	Art. 391. 2. \$179.80. 3. \$40.50. 4. \$193.45. 5. \$168. 6. \$277.53. 7. \$4. 8. \$289.39. 9. \$06.25. 10. \$21.62. 11. \$7.56. 12. \$36.60. 13. \$85 ; \$107. 14. \$18.75. 15. \$81; \$90. 16. \$274.81. Art. 402. 1. 51.84. 2. 60. 3. 17.92. 4. 23.22. 5. 56.7. 6. \$23.19.	7. $125.$ 6. $\$106.$ 7. $\$162.$ 8. $\$1975.$ 9. $\$243.60.$ 10. $\$487.10.$ 11. $\$176.43.$ 12. $\$328.35.$ 14. $\$2434.79.$ 15. $\$184.38.$ 16. $\$64.94.$ 17. $\$4100.$ 18. $\$4500;$ \$16.88. <b>Art. 407.</b> 1. 8. 2. $\$00.$ 3. $5400.$ 4. $5600.$ 5. $9375.$ 6. $22.8.$ 7. $1800.$ 8. $800.$ 3. $5400.$ 4. $5600.$ 5. $9375.$ 6. $22.8.$ 7. $1800.$ 8. $800.$ 9. $3500.$ 9. $3500.$	$\begin{array}{c} A16. \ 100\ 1.\ 0.014. \\ 2.\ 20\%. \\ 3.\ 0.08\frac{1}{3}. \\ 4.\ 0.02\frac{1}{18}. \\ 5.\ 31\frac{1}{3}\%. \\ 6.\ 14\%. \\ 7.\ 6\frac{1}{4}\%. \\ 7.\ 6\frac{1}{4}\%. \\ 9.\ 18\%. \\ 10.\ 33\frac{1}{4}\%. \\ 10.\ 33\frac{1}{3}\%. \\ 11.\ 25\%. \\ 12.\ \frac{9}{3}\%. \\ 13.\ 2200. \\ 14.\ 12\frac{1}{3}\%. \\ 15.\ 45\%. \\ 16.\ 44\%. \\ 17.\ \frac{1}{8}\%: \\ \frac{842.50}{18}. \\ 19.\ 16\%. \\ 20.\ 56\frac{1}{4}\%. \\ 20.\ 56\frac{1}{4}\%. \\ 21.\ 4\frac{1}{8}\%. \\ 22.\ 18\frac{1}{8}\%. \\ 23.\ 6\frac{1}{8}\%. \\ 24.\ \frac{8}{8}\%. \\ 24.\ \frac{8}{8}\%. \end{array}$
2000.710 Sq. 11. 2000.710 Sq. 11. 21. 6237 Kg. Art. 387. 2. 1135.94. 3. 5 mo. 24 da.; 178 da. 4. 8. 5. 32 ft. 6. 702 sq. ft.; 210 sq. ft.; 1320 sq. ft. 7. \$172.36. 8. \$127.49. 9. 43200 sq. rd. 10. 480 sq. ft. 11. 3110 ft. 12. \$128. 13. 628 ft. 14. 15.708 ft. 15. 28.27 sq. ft.; 78.54 sq. ft. 16. 429 ft. 17. 35942 lb. 19. 474 st. 19. 474 st. 19. 474 st. 10. 474 st. 1	Art. 391. 2. $\$179.80.$ 3. $\$40.50.$ 4. $\$193.45.$ 5. $\$168.$ 6. $\$277.53.$ 7. $\$4.$ 8. $\$289.39.$ 9. $\$06.25.$ 10. $\$21.62.$ 11. $\$7.56.$ 12. $\$36.60.$ 13. $\$85 ; \$107.$ 14. $\$18.75.$ 15. $\$51; \$90.$ 16. $\$274.81.$ Art. 402. 1. $51.84.$ 2. 60. 3. $17.92.$ 4. $23.22.$ 5. $56.7.$ 6. $\$33.12.$ 7. $\$7.92.$ 4. $\$23.22.$ 5. $56.7.$ 6. $\$33.12.$ 7. $\$7.92.$ 4. $\$25.92.$ 5. $56.7.$ 6. $\$33.12.$ 7. $\$7.92.$ 5. $56.7.$ 7. $\$7.92.$ 5. $56.7.$ 7. $\$7.92.$ 5. $56.7.$ 7. $\$7.92.$ 5. $56.7.$ 7. $\$7.92.$ 5. $56.7.$ 5. $56.$	7. \$125. 6. \$106. 7. \$162. 8. \$1975. 9. \$243.60. 10. \$487.10. 11. \$176.43. 12. \$328.35. 14. \$2434.79. 15. \$184.38. 16. \$64.94. 17. \$4100. 18. \$4500; \$16.88. Art. 407. 1. 8. 2. 800. 3. 5400. 4. 5600. 5. 9375. 6. 22.8. 7. 1800. 8. 800. 9. 2500. 10. \$45.60. 10. \$45.60.\\ 10. \$45.60.\\ 10. \$45.60.	1. 014. 2. 20%. 3. 084. 4. 0274. 5. 34%. 6. 14%. 7. 64%. 8. 22%. 9. 14%. 10. 334%. 11. 25%. 12. $\frac{3}{2}$ %. 13. 2200. 14. 124%. 15. 45%. 16. 44%. 17. $\frac{1}{2}$ %; $\frac{3}{4}$ %. 18. 44%. 19. 16%. 20. 564%. 21. 44%. 22. 184%. 23. 64%. 24. 64%. 23. 64%. 24. 64%. 23. 64%. 24. 64%. 25. 64%. 26. 64%. 27. 64%. 27. 64%. 28. 64%. 29. 64%. 29. 64%. 29. 64%. 20. 64%. 2
20.0.3.7 g.; 6.237 Kg. Art. 387. 1. 6237 Kg. Art. 387. 2. 1135.94. 3. 5 mo. 24 da.; 178 da. 4. 8. 5. 32 ft. 6. 702 sq. ft. ; 1320 sq. ft.; 1320 sq. ft.; 1320 sq. ft. 7. \$172.36. 8. \$127.49. 9. 43200 sq. rd. 10. 480 sq. ft. 11. 3110 ft. 12. \$128. 13. 628 ft. 14. 15.708 ft. 15. 28.27 sq. ft.; 78.54 sq. ft. 16. 429 ft. 17. 35942 lb. 18. 474 qt.	Art. 391. 2. $\$179.80.$ 3. $\$40.50.$ 4. $\$193.45.$ 5. $\$168.$ 6. $\$277.53.$ 7. $\$4.$ 8. $\$289.39.$ 9. $\$96.25.$ 10. $\$21.62.$ 11. $\$7.56.$ 12. $\$36.60.$ 13. $\$85$ ; $\$107.$ 14. $\$18.75.$ 15. $\$91;$ $\$90.$ 16. $\$274.81.$ Art. 402. 1. $51.84.$ 2. $60.$ 3. $17.92.$ 4. $23.22.$ 5. $56.7.$ 6. $\$33.12.$ 7. $\$57.28.$ 9. $e64.$	7. \$125. 6. \$106. 7. \$162. 8. \$1975. 9. \$243.60. 10. \$487.10. 11. \$176.43. 12. \$328.35. 14. \$2434.79. 15. \$184.38. 16. \$64.94. 17. \$4100. 18. \$4500; \$16.88. Art. 407. 1. 8. 2. 800. 3. 5400. 4. 5600. 5. 9375. 6. 22.8. 7. 1800. 8. 800. 9. 2500. 10. \$34.56. 11. \$1050. 2. \$1050. 3. \$1050. 3. \$1050. 3. \$1050. 3. \$1050. 3. \$1050. 5. \$1	1. 014. 2. 20%. 3. 08 $\frac{1}{2}$ . 4. 02 $\frac{1}{18}$ . 5. 3 $\frac{1}{8}$ %. 6. 1 $\frac{1}{4}$ %. 7. 6 $\frac{1}{4}$ %. 9. 1 $\frac{1}{8}$ %. 9. 1 $\frac{1}{8}$ %. 10. 33 $\frac{1}{8}$ %. 11. 25%. 12. $\frac{3}{80}$ %. 13. 2200. 14. 12 $\frac{1}{2}$ %. 15. 45%. 16. 44%. 17. $\frac{1}{8}$ %. 24. 25%. 28. 4 $\frac{1}{8}$ %. 29. 16%. 20. 56 $\frac{1}{8}$ %. 21. 4 $\frac{4}{8}$ %. 22. 18 $\frac{1}{8}$ %. 23. 6 $\frac{1}{8}$ %. 24. $\frac{3}{8}$ %. 25. 9 $\frac{1}{8}$ %. 26. 4 $\frac{5}{8}$ %.
2000.410 Sq. 11. 23. 6237 G.; 6.237 Kg. Art. 387. 1. 35 49 2. 1135.94. 3. 5 mo. 24 da.; 178 da. 4. 8. 5. 32 ft. 6. 702 sq. ft. ; 210 sq. ft. ; 1320 sq. ft. ; 1320 sq. ft. 7. \$172.36. 8. \$127.49. 9. 43200 sq. rd. 10. 480 sq. ft. 11. 3110 ft. 12. \$128. 13. 628 ft. 14. 15.708 ft. 15. 28.27 sq. ft. ; 78.54 sq. ft. 17. 35942 lb. 18. 474 qt. 19. 487 46 bu, ;	Art. 391. 2. $\$179.80.$ 3. $\$40.50.$ 4. $\$193.45.$ 5. $\$108.$ 6. $\$277.53.$ 7. $\$4.$ 8. $\$289.39.$ 9. $\$06.25.$ 10. $\$21.62.$ 11. $\$7.56.$ 12. $\$36.60.$ 13. $\$85 ; \$107.$ 14. $\$18.75.$ 15. $\$81; \$90.$ 16. $\$274.81.$ Art. 402. 1. $51.84.$ 2. $60.$ 3. $17.92.$ 4. $23.22.$ 5. $56.7.$ 6. $\$33.12.$ 7. $\$57.28.$ 8. $\$644.$	7. $125.$ 6. $\$106.$ 7. $\$162.$ 8. $\$1975.$ 9. $\$243.60.$ 10. $\$487.10.$ 11. $\$176.43.$ 12. $\$328.35.$ 14. $\$2434.79.$ 15. $\$184.38.$ 16. $\$64.94.$ 17. $\$4100.$ 18. $\$4500;$ \$16.88. <b>Art. 407.</b> 1. 8. 2. $\$00.$ 3. $5400.$ 4. $5600.$ 5. $9375.$ 6. $22.8.$ 7. $1800.$ 8. $800.$ 9. $9500.$ 10. $\$34.56.$ 11. $\$4050.$ 2. $84050.$ 2. $84050.$ 2	$\begin{array}{c} A16. \ 100 \\ 1. \ 0.01 \\ 4. \ 2. \ 20\%. \\ 3. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \\ 1. \ 0.05 \ 0.05 \ 0.05 \\ 1. \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.05 \ 0.$
20.0.3.7 fo; 6.237 Kg. Art. 387. [. 6.237 Kg. Art. 387. [. 6.237 Kg. Art. 387. [. 135.94. [. 135.94. [. 5 mo. 24 da.; 178 da. 4. 8. 5. 32 ft. 6. 702 sq. ft.; 1320 sq. ft.; 1320 sq. ft.; 1320 sq. ft. [. 172.36. [. 172	Art. 391. 2. $\$179.80.$ 3. $\$40.50.$ 4. $\$193.45.$ 5. $\$168.$ 6. $\$277.53.$ 7. $\$4.$ 8. $\$289.39.$ 9. $\$06.25.$ 10. $\$21.62.$ 11. $\$7.56.$ 12. $\$36.60.$ 13. $\$85 ; \$107.$ 14. $\$18.75.$ 15. $\$51; \$90.$ 16. $\$274.81.$ Art. 402. 1. $51.84.$ 2. $60.$ 3. $17.92.$ 4. $23.22.$ 5. $56.7.$ 6. $\$33.12.$ 7. $\$57.28.$ 8. $\$644.$ 9. $\$411.95.$	7.       \$125.         6.       \$106.         7.       \$162.         8.       \$1975.         9.       \$243.60.         10.       \$487.10.         11.       \$176.43.         12.       \$328.35.         14.       \$243.479.         15.       \$184.38.         16.       \$64.94.         17.       \$4100.         18.       \$4500;         \$16.88.       Art. 407.         1.       8.         2.       \$00.         3.       5400.         4.       5600.         5.       9375.         6.       \$22.8.         7.       1800.         8.       800.         9.       \$2500.         10.       \$34.56.         11.       \$4050.         12.       \$900.	1. 014. 2. 20%. 3. 084. 4. 0274. 5. 34%. 6. 14%. 7. 64%. 8. 22%. 9. 14%. 10. 334%. 11. 25%. 12. $\frac{3}{8}$ %. 13. 2200. 14. 124%. 15. 45%. 16. 44%. 17. $\frac{1}{8}$ %; $\frac{3}{8}$ 42.50. 18. $\frac{41}{8}$ %. 20. 564%. 21. 44%. 22. 184%. 23. 64%. 23. 64%. 24. $\frac{3}{8}$ %. 25. 925%. 24. $\frac{3}{8}$ %. 25. 925%. 26. 45%. 27. 2148%.

354	- ANS	WERS.	[Art. 410
29. \$320·	192 \$72	1 21 @10	1 17 49554 75
\$280	03 931 06	00 0050	10 @42500
30 121%	01 1500	00 050	10. 01000.
21 200	05 5710	00. 015.90	19. 01110.00.
00 8 dt	20. 0129.	34. \$10.30.	20. \$8450.89.
3.3. 7/0.	20. 12%.	36. 50%.	21. \$2433.90.
33. \$%.	27. 10%.	$37. 31 \frac{1}{19} \%$ .	22. \$7872.07.
	28. 4%.	$38. 13\frac{1093}{1539}\%$ .	23. \$2175.44.
Art. 411.	29. \$210.	$39. $1.26\frac{2}{3};$	24. \$50000.
1. 1392.	30. 36%.	$30\frac{1}{8}\%$ .	25. \$2751.14.
2. 120.	31. 96%.		26. \$852.91.
3. 125%.	32. Loss, 4%.	Art. 419.	27. \$185.40.
4 \$1197	33. 388%.	7 \$44.10	28. \$1388.63.
5 275	34. \$432.	0 0008 19	29. \$988.
6 \$7500	35, \$4.25, each.	0 070	30. \$5136.
7 \$16.88	36. 12%	0. 01%.	37 \$61200
2 90d	37 \$640	4. \$000.22.	32 \$123 31
0. 00%.	88 97 50	3. \$135.73.	22 \$405.10
J. \$137790.70.	29 62 0. \$3.80	6. \$118.73.	21 \$1994
10. \$28340.30.	10 00520 06.	7. \$360.07.	05 0075 50
11. \$0.07.	40. \$2002.00,	8. \$900.43; N	20. 0010.0%.
12. \$1150.	\$0102.00;	\$855.41.	30. 5900.
13. \$164.	223/0.	9. \$149.05.	37. \$200.39.
14. \$12960.	41. \$400, loss.	10. \$340.64;	38. \$18909.18.
15. \$9363.44.	4. 4. 4. 4. 10	\$333.83;	
$16. 2\frac{3}{4}\%.$	APt. 417.	\$337.23.	Art. 441.
17. \$6907.51.	1. \$78.55.	11. \$1082.55.	1 \$199.50
18. \$123450;	2. \$31.50.	12. \$145.	0 @115.65
\$1313.28.	3. \$206.55.	13. \$65.64.	2 \$595.95
19. \$6058.95:	4. \$76.58.	14. \$54.71	0. 0020.20.
95%: 20%.	5. \$40.30.	15 \$258.32	4. 0102.01.
20. \$1052.63:	6. \$18.24	\$245.40	0. 0014.01
\$1422.37	8 231% . 501%.	16 \$74.31.	0. \$214.31.
21. \$1079.12.	30% . 64%.	\$72.82	7. \$333.50.
22 71 0 · 20 %	- 781 0 . 492 0 .	17 097 12	8. \$397.49.
24 £11 10s 5d	17/20/	10 010 76	9. \$106.58.
25 £96 0g	0 \$106	10. 01000 40	10. \$3393.33.
<i>QE</i> £18 15c	10 \$100.	19. 01092.40.	11. \$1059.71.
27 £1 19a 5d	11 200 ml	20. 00.00.	12. \$470.63.
$a_7, a_1 a_5, b_4, a_6$	11. 200 yu.	21. \$00.12.	<i>13</i> . \$18.81.
20, 20 05, 00.	12. 004.00.	22. 000.00.	<i>14.</i> \$1791.94.
29. 20 145. 11u.	13. \$102.82.	23. \$1005.07.	
01 695 0- 41	14. \$420.20.	24. \$155.40.	Art. 445.
51. ±00 0S. 40.	15. \$353.42.	Ant 19M	
Ant AIA	16. \$147.07.	ATC. 446.	1. \$20.
Art. 414.	17. \$26.25.	1. \$21.60.	2. \$21.82.
1. \$40.	18. \$168.93.	2. \$200000.	3. \$1.79.
<i>2.</i> \$364.	19. \$905.23;	3. \$212.50.	4. \$2.92.
5. \$4726.	\$896.08.	4. \$2256.25.	5. \$47.11.
7. \$3.	20. \$450.96.	5. \$2295.	6. \$0.91.
8. \$10179.	$21. 42\frac{6}{7}\%$ .	6. 2%.	7. \$6.48.
10. \$1048.20.	$22. 33\frac{1}{3}\%$ .	7. 480.	8. \$6.81.
11. 72%.	23. 405%.	8. \$3099.37.	9. \$1.75.
12. \$2425.	24. 100%.	9. \$12.61.	10. \$16.16.
14. 16%.	25. 331%: 50%:	10. \$81.75.	11. \$6.91:
15. 1328 %	5311%:	11. \$2161.17 net	\$5.76
16, 121%	4020%: 426%.	amount	12 \$127.58.
17. \$1775	301100, 10770,	12 \$65.63	\$148.85
18 \$608	26 311%	13 \$869.60 com	12 \$101.00.
19 \$11995	07 111 0/	1/ \$195	0. 0101.20;
20 \$590	00 5846 0	15 50	00.01. 11 @52.02.
OI AAd	20. 00 53 %.	10. 0%.	14. 000.20;
A1. 117.	00. pr.00.	10. 0001.	\$01.10.

.

15.	\$50.69;	34.	\$107.36;	68.	\$16.28; \$	14.65.		Art. 466.
	\$33.79.		\$80.52.		\$16.57; \$	14.92.	1.	7%. 10.6%.
16.	\$663.33;	35.	\$93.53;	69.	\$53; \$59	.63.	2.	7%. 11. 84%.
	\$1105.56.		\$140.30.	70.	\$46;		3.	6%. 12.9%.
17.	\$33.25; \$24.94.	36.	\$19.27;		\$48.30.		4.	5%. 13. 101%.
	\$33.98; \$25.48.		\$14.46.		\$47;		5.	7%. 14. 30%.
18.	\$23.16; \$28.95.	37.	\$494.15;		\$49.35.		6.	31%.15.8%.
	\$23.44; \$29.30.		\$247.07.	71.	\$9.80;		7.	8%. 16.6%.
19.	\$92.67;	38.	\$418.64;		\$8.98.		8.	41%.17.7%.
	\$185.33.		\$837.29.		\$10; \$9.1	17.	9.	4%.
	\$93.33;	39.	\$434.60;	72.	\$10.27;			
	\$186.67.		\$437.58.		\$9.54.	1		Art. 469.
20.	\$90.35;	40.	\$1393.29;		\$10.50;		-	0 0 1
	\$150.58.		\$1446.05.		\$9.75.	•	1.	0 m. 0 d.
	\$92.37;	41.	\$623.85;	73.	\$18.13;	-	~.	1 y. 4 m. 20 d.
	\$153.95.		\$615.81.		\$7.93.	•	3.	2 y. 2 m. 2 d.
21.	\$654.50;	42.	\$2267.51;		\$18.56;		4.	2 m. 15 d.
	\$872.67.		\$2249.67.		\$8.12.		5.	0 m. 14 d.
	\$656.83;	43.	\$6503.40;	74.	\$14.04;		0.	1 y. 10 m. 22 d.
	\$875.88.		\$6597.60.		\$7.41.		17.	4 y. 9 m. 15 d.
		44.	\$4416.93;		\$13.86;		8.	4 y. 8 m. 34 d.
	Art. 459.		\$4390.69.		\$7.32.		9.	9 m. 20 d.
1.	\$8.64.	45.	\$389.94;	75.	\$51.33;		10.	11 m. 21 d.
2.	\$1.32.		\$387.12.		\$38.50;		10	1 y. o m. 10 d.
3.	\$3.48.	46.	\$1450.87;		\$51.91;		1%.	1 y. 5 m. 18 d.
h.	\$8.64.		\$1605.74.		\$38.93.		13.	16 y. 8 m.
5.	\$6.57.	47.	\$5092.50;	76.	\$10658.20	).	14.	28 y. 6 m. 26 d.
6.	\$6.		\$5032.71.	77.	\$1050.	-		
7.	\$5.34.	48.	\$2.	78.	\$1556.66.			Art. 472.
8.	\$1.	49.	\$10.66.	79.	\$27.84.		1.	\$12107.84.
9.	\$7.89.	50.	\$53.44.	80.	\$28.93.		2.	\$871.31.
10.	\$0.85.	51.	\$14.19.	81.	\$1356.18.	-	3.	\$2241.
11.	\$10.63.	52.	\$0.50.	82.	\$1562.50.		4.	\$7719.16.
12.	\$11.73.	53.	\$33.11.	83.	\$86.07.		5.	\$1997.87.
13.	\$18.14.	54.	\$61.20.	84.	\$0043.		6.	\$3000.
14.	\$0.31.	55.	\$8.38.	85.	\$601.39.		7.	\$3228.33.
15.	\$3.73.	56.	\$11.55.		1 10	0	8.	\$29419.35.
16.	\$10.07.	57.	\$9.33.		Art. 46	J.	9.	\$30612.25.
17.	\$35.63.	58.	\$34.90; \$33.21.	1.	\$1.79.		10.	\$31746.03.
18.	\$9.50.	50	\$00.00; \$00.87. \$14 07. \$10 79	2.	\$116.47.		11.	\$11973.33.
19.	\$26.04.	09.	@14.27; @10.70.	3.	\$11.54.		12.	\$14370.69.
20.	\$46.67.	60	\$96 72. \$10.00.	4.	\$5.29.		13.	\$3436.99.
21.	\$16.28; \$13.57.	00.	\$27 20. \$19.09.	5.	\$3.92.			Ant ATS
22.	\$04.70;	61	\$193.96.	6.	\$15.12.		-	A100 ±100
00	\$32.38.	01.	\$113.14	7.	\$0.70.		1.	\$1234.
23.	\$30.80; \$42.99.		\$195.15	8.	\$0.10.		2.	\$0280.
24.	\$24.10; \$20.08. \$50.00, \$175.57		\$113.83.	9.	\$42.18.		3.	\$0400. #975 CO
20.	\$190.00; \$10.01. \$190.10.	62.	\$309.07:	10.	φ14.00. Φ1 11		4.	\$19275
~0.	¢100.10;		\$347.70.	10	\$10-44		6	@1/000
ON	@11 /2. @17 1/		\$310.14:	10	φ10.44. φ20 25	-	14	\$1120. \$702.01
28	\$39 45. \$46 02		\$348.90.	10.	\$946.80		8	\$879.54
20	\$19.79. \$92.00	62	\$57 97. 001 01	14.	\$58.07		0.	\$1511 67
30	\$2.85. \$2.37	00.	\$57 82 . \$89 60	16	\$27 74		10	\$2309.28
31	\$13.75 . \$16.04	64	\$7 59 . \$10.12	17	\$41 64		11	\$3770 52
32	\$106.66:	65	\$25.95: \$11.53	18	\$7.58.		12	\$5307.72.
5.00	\$142.22	66.	\$111: \$27.75	19	\$2.14		13	\$1642.31.
33.	\$137.72:	67.	\$76.50: \$60.56	20.	\$30.21.		14.	\$2138.94.
	\$114.77.		\$77.40; \$61.28.	21.	\$5.	1	15.	\$5063.11.

16.	\$2863.86.	3. \$83.26.	9.	Sept. 1;	39. \$1523.25.
17.	\$3590.09.	4. \$1909.63;		\$4430, or	40. \$3081.09.
		\$2104.72.		\$4430.96.	
	Art. 479.	5. \$1211.	10.	Sept. 28;	Art. 505.
	0000 00	6. \$220.80:		\$8204.29. or	1. \$678.54.
1.	\$892.86;	\$268.51.		\$8204.78.	2. \$242.17:
-	\$107.14.	7. \$8583.80	11.	June 29:	\$148.16.
2.	\$438.60;	8 \$1811 44.		\$4276.08 or	3. \$1102.69:
	\$61.40.	\$2564.94		\$4276 73	\$1184.37
3.	\$547.95;	0 \$9704 39.	10	Nov 30.	4 \$1327.21.
	\$52.05.	\$7708 54	14.	\$4768.85 or	\$1410.94
4.	\$762.63;	10 0002 02		@4770 44	5 \$835 774.
	\$37.37.	11 04445 17	10	\$110.11. Mor 6.	0. 000.11,
5.	\$283.35;	10 00450 19	10.	may 0;	C 0000 89
	\$41.65.	12. 02400.10.	1	\$0099.00, 0r	v \$2072.
6.	\$161.64:	13. \$147.27.	1	\$8900.88.	7. \$0070;
	\$13.36.	14. \$4172.57.	14.	Jan. 10;	\$0000.00.
7.	\$595.39:	15. \$405.34.		\$4909.58, or	8. \$317.82;
	\$204.61.	16. \$13363.84.	1	\$4910.82.	\$716.62.
8	\$641 79.	17. \$4659.94.	15.	Feb. 2;	9. \$3260.23;
0.	\$258.21	18. \$343.90.		\$5936.20, or	\$4539.19.
a	\$0.68			\$5937.07.	1
10	\$3690.03	Ant AQ5	16.	\$5949.	Art. 509.
11	\$0020.00. \$004.00	Art. 200.	17.	Oct. 5;	2. \$440;
11.	ф204.2J.	7 \$1022		\$4946.67.	\$447.16.
	1	2 \$911 04.	18.	Apr. 4;	3. \$223.31:
	Art. 480.	\$010.21.		\$3710.	\$214.37.
1.	\$42.32.	\$017.46	19.	Aug. 6;	4. \$651.97:
2.	\$1843.93.	9 Man 7 1800.	1	\$6882.75.	\$753.30.
3.	5%.	a. mar. 1, 1090,	20.	July 4:	<b>\$100.000</b>
4.	1 v. 10 m. 28 d.	\$0022.10.	1	\$8909.75.	Art. 513.
5.	\$1722.02.	4. 0401.10;	21.	Dec. 21:	2 \$262.24·
7.	142%	\$424.00.	1~1.	\$4838.61	\$161.40
8.	Latter 11%	6. Aug. 21, 1887.	00	Sent 29.	2 @1109.57.
0.	better.	7. Monday.	1~~.	\$4451.25	\$1100.07,
9.	Oct. 3.	8. Saturday;	02	Dec 5.	1 01204 175.
10	7%	Wednesday.	20.	\$8870.37	4. 01024.10;
11	\$19230 77	9. Oct. 23.	01	Dog 8:	# 0000 0m.
12	\$4298.04		~4.	\$2070.75	0. 0000.01;
Tw.	\$4342.65	Art 500.	05	\$2010.10. June 94.	\$920.94.
19	June 11 1874	11.0.0000	20.	00010 m1	0. 0001.11.
11	@100.	2. \$7937.33, or	00	\$9012.11.	7. \$3067.14;
14.	\$120, \$191 50.	\$7938.19.	20.	001. 11;	\$3347.31.
	¢101.00;	3. Apr. 27;	0m	\$0894.20. Mars 19	8. \$549.89;
15	\$129.70. \$650	\$1181.40, or	27.	May 13;	\$764.05.
10.	\$000. @1409.00	\$1181.65.		\$5897.87.	9. \$3260.51;
10.	\$1400.90.	4. Aug. 21;	28.	Sept. 6;	\$4594.82.
17.	\$89.17.	\$5196.40, or		\$8603.70.	1.1 200
18.	\$606.60.	\$5197.55.	29.	\$7837.33.	Art. 573.
19.	£199 3s. 8d.	5. Nov. 2:	30.	\$8808.	1. 12.
20.	£8 10s.	\$2524.16. or	31.	$5\frac{1}{2}\%$ .	3. 160.
21.	£5 8s. 4d.	\$2524.65.	32.	\$15.87.	4. \$36.
22.	£9 5s. 10d.	6. Oct. 7:	33.	\$3012.09.	5. \$50.
23.	£2 12s. 11d.	\$3664 71 or	01	Aug 30.	6. 240 lb.
24.	£3 17s. 4d.	\$3665.96	04.	Aug. 00;	7. \$111.
25.	£10 9s. 8d.	7 Nov 18.		ф0101.01.	8. \$21.875.
		\$6305.55 or	35.	May 19;	9. \$55.50.
	Art. 485.	\$6305.06		\$1641.17.	10. 851 vd.
1	\$596 AA .	8 Sont 16.	36.	Apr. 15:	11. 396 ft.
1.	\$0.20.44; \$506.49	@ 9125 72 or		\$882.22.	12 £25 11s. 9d.
	milU0.40.	00100.10, 0r	1		The deno TTO out
A	#1# 10. 00M 0M	00100 01	00	@1592.69	19 \$960

11	@9/10/71		Apt. 567.	62 147
14.	\$\$\$410.71. 1 \$\$1975.00.	8 \$56.88	1 @1002.04	63. 13950.75 fr.
10.	A, @1010.00,	0 \$71.43	1. \$1083.94.	64 £391 4s
10	D, \$1090.40.	10 257 60	2. \$1583.40.	65 7343 75 fl
10.	10.9000: 1.	11 @1990	4. \$2407.50.	66 £1009 7g 6d
17.	\$179.50.	10 000 58	5. \$3760.69.	67 <b>£</b> 519 20 9d
18.	\$126.	12. \$20.00.	6. \$4050.03.	07. 2012 0S. 2u.
19.	\$3.79.	13. \$42.	7. \$409.34.	Art. 574.
20.	\$137.03.	14. \$9000.	8. \$2483.15.	1 0-4 10
<i>\$</i> 1.	\$153600.	15. \$9000.	9. \$4076.72.	1. Oct. 10.
₹2.	2355 <sup>2</sup> / <sub>3</sub> ft.	16. 40%.	10. \$3290.93.	2. May 11.
23.	25.215 fr.	17. \$16.20;	11. \$1087.98.	3. Feb. 11.
84.	252 <del>§</del> <sup>9</sup> / <sub>7</sub> yd.	\$27.	12. \$4261.23.	4. Aug. 4.
<i>25</i> .	20 hr. 45 min.	18. \$1440.	13. \$4593.93.	5. June 5, 1882.
	9 sec.	19. \$61.25.	14. \$2611.06.	6. June 20.
26.	\$11.10.	20. \$792.	15. \$8495.46.	7. July 18;
27.	69 da.	21M, \$1761.36;	16. \$2373.24.	\$1694.90;
28.	\$3000.	P, \$1409.09;	18, £1225 18s, 6d.	\$1686.16.
29.	\$912.23.	Т, \$880.68.	19, 4.837.	8. Feb. 15, 1882.
30.	471 vd.	22. A, \$454.54;	20) £1864 6s. 4d.	9. Oct. 6, 1881;
31.	4449 - bu.	C, \$568.18.	21 \$1341 32	\$2403.88;
32.	\$84.18.	23. 2.767%.	22 \$1162.79	\$2367.55.
33.	\$0.73.	24. \$2627.78.	23 \$965 02	10. May 31;
34	\$3.12.	25. \$315.33.	21 \$767 20	\$2480.32;
35	\$17 60	26. \$28.03.	05 \$1621 38	\$2492.72.
36	\$22.67 . \$25.33	27. \$155.70.	ac \$1909.79	11. July 14.
214	45 dave		AU. 01000.12.	12. Nov. 15.
00	@1 003		27. 01050.00.	13. Sept. 5.
20.	1409 96 ft	4	20. \$1000.00.	15. Oct. 26, 1882.
00.	1492.20 It. 198 mg	Art. 553.	29. \$2023.10.	16. Sent. 25:
40.	107 IIIU. 05900 aggeta		30. \$1334.09.	\$2425.16
141.	\$0030, assets;	1. \$8782.81.	31. \$2386.62.	\$2437 33
	\$11100, debts.	2. \$8395.94.	32. \$1688.75.	17 July 8
		3. \$5006.25.	33. \$1411.11.	18 Mar 21 1882
	Art. 526.	4. \$4358.59.	34. 80318.70 fr.	10 Fab 19 1889
	A107 00	5. \$8427.52.	35. 17972.04 fr.	20 April 19 1883
1.	\$100.05.	<i>6</i> . \$9922.37.	$36. 5.18\frac{3}{8}.$	20. April 12, 1005.
2.	6 hr.	7. \$5270.79.	38. \$1692.	Art. 582.
3.	126 A.	8. \$4287.11.	39. \$1967.24.	
4.	\$4665.60.	9. \$3417.18.	40. \$822.96.	1. Jan. 17, 1889.
5.	4 hr.	10. \$2821.96.	41. \$289.54.	2. May 25, 1888.
6.	125.	11. \$9898.30.	42. \$2359.10.	3. Dec. 3, 1882.
7.	½ day.	12. \$8406.44.	43. \$1543.24.	4. May 13, 1882.
8.	4 days.	14. \$1871.48.	44. \$3867.75.	5. Sept. 6, 1882;
9.	15 hr.	15. \$2443.86.	45. \$3102.24.	\$276.53.
10.	9 days.	16. \$3346.56.	46. \$1547.25.	6. Feb. 15, 1883;
11.	\$64.	17. \$2227.28.	47. \$2061.40.	\$1053.23.
12.	80 days.	18. \$8144.96.	48. \$2359.33.	7. Feb. 8, 1881.
13.	\$66.13.	19. \$7373.16.	49. 3467.73 marks.	8. Aug. 25, 1882
14.	\$1493.33.	20. \$9222.61.	50. 13824 marks.	
15.	32 days.	21. \$6431.57.	51. 947.	Art. 586.
16.	16320 lb.	22, \$9231.46.	52. \$2905.05.	1. \$2074.06;
		23. \$5283.96.	53. \$4976.40.	Aug. 28;
		24. \$23.29:	54. 4562 guilders.	Sept. 2;
	Art. 544.	\$9340 10.	55, 7128 guilders.	Sept. 2.
1	\$93 75	25. \$2972.25.	56. 405.	2. \$5324.48:
0	\$68 75	26 \$11834	57. 4.885.	Nov. 28.
20	\$354 50	27 \$7854 67	58 \$17366.99	3. \$2751.14:
0.	\$0¢	28 1% premium	59. \$3.60	Sept. 27.
4.	\$2600	29 \$3420.05	60 1184.1171	4. \$12505.70:
D.	<b>\$3000.</b>	#0. @10110.00.	<i>C1</i> 05 00	Apr 26
C	000105		01 01 20	

Dec. 10. $32.$ $845,066,444,72.$ $20.$ $81.1692.$ $B.$ $8322$ $Art.$ $594.$ $36.$ $866,000,000;$ $21.$ $1.69\%.$ $12.$ $8150.$ $2.$ $8986.02.$ $37.$ $80.$ $22.$ $A,$ $8177.63;$ $12.$ $8130.$ $2.$ $8986.02.$ $37.$ $80.$ $23.$ $8587.$ $G.$ $8332.$ $2.$ $81604.89.$ $30.$ $8176;$ $33.$ $Art.$ $622.$ $I.$ $832.$ $4.$ $81604.89.$ $30.$ $8176;$ $33.$ $Art.$ $622.$ $I.$ $832.$ $7.$ $8160.97.57.$ $42.$ $Latter \frac{1}{12}\%.$ $I.$ $89412:$ $I.$ $8215.$ $7.$ $8097.87.$ $43.$ $7\frac{1}{7}\%.$ $I.$ $89412:$ $I.$ $85242.$ $I.$ $81153.21.$ $I.$ $81764.29.$ $I.$ $R.$ $897.22.$ $I.$ $R.$ $I.$ $81153.22.$ $I.$ $I.$ $85242.$ $I.$ $I.$ $8515.21.$ $I.$ $R.$ $89192.$ $I.$ $81704.29.$ $47.$ $64.\%.125.02.42.$ $I.$ $8.$ $8500.$ $I.$ $R.$ $89192.$ $I.$ $8523.23.$ $I.$ $I.$ $8575.32.0.$ $I.$ $8.$ $8500.$ $I.$ $8.$ $I.$ $81704.29.$ $47.$ $8.$ $8.$ $8.$ $8.$ $8.$ $8.$ $8.$ $I.$ $8.$ $8.$ $8.$ $8.$ $8.$ $8.$ $8.$ $8.$ $8.$	0.24;
Art. 594.Jo. 100. $21.$ 1.65%. $12.$ \$14,000,000;1. \$431,37. $36.$ \$66,000,000; $$14,000,000.$ $22.$ A, \$177.63; $14.$ E, \$2382. \$986.02. $37.$ 80. $32.$ A, \$177.63; $14.$ E, \$2383. \$3361.51. $35.$ 8%; 6%; 5 $\frac{1}{2}$ %. $35.$ 8%; 6%; 5 $\frac{1}{2}$ %. $14.$ 9.4. \$1604.89. $39.$ \$176; 33. $40.$ 8%. $1.$ \$0412; $18.$ \$2405. \$4. $40.$ 8%. $1.$ \$04412; $18.$ \$2466. \$44055.75. $42.$ Latter $\frac{1}{2}$ % $5547.20.$ $C.$ \$1858. Rm. 9997.87. $43.$ $7\frac{1}{4}$ %. $3.$ \$804.9. $16.$ A, \$3759. \$276.54.greater. $5.$ \$55.40. $C.$ \$22511. \$1513.77; $45.$ 166 $\frac{3}{2}.$ $6.$ \$1053.22. $17.$ \$4. $832067.54;$ $46.$ \$6. \$60.\$1333. $7.$ \$723.45; $E.$ \$135.21. $832067.54;$ $45.$ \$2425. $6.$ \$135.21. $D.$ \$187 $$822667.54;$ $45.$ \$774.452; $10.$ \$116.94. $19.$ A, \$54012. Rm. 3860.18. $50.$ \$774452; $10.$ \$116.94. $19.$ A, \$54013. \$852.23. $41.48\%.$ $9.$ \$1267.50. $B.$ \$56014. \$886.19. $75.$ \$6%. $1.$ \$807.80. $R.$ \$836.90.60. $8.$ \$8.90.92.15. \$852.42. $75.$ \$6%. $1.$ \$807.80. $R.$ \$836.91.14. \$89750; \$56. $53.$ \$1128.34. $14.$ \$839.40. $C.$ \$4102. \$8750; \$56. $53.$ \$1128.34. $14.$ \$839.40. $C.$ \$4102. \$8750; \$56. $53.$ \$1128.34. $14.$ \$838.40. $27.$ \$483.90.15. \$8122.40.000;	5.12.
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	0.09.
1.       93.1.3.       97.90.90.0       23.       9587.       6, \$30.0         2.       \$3361.51. $32.$ $37.80.$ $47.80.0$ $47.80.0$ $47.80.0$ $47.83.0$ 3.       \$3169.53. $37.80.$ $37.80.$ $47.83.0$ $47.83.0$ $47.83.0$ $47.84.0$ $48.87.0$ $47.84.0$ $48.87.0$ $47.84.0$ $48.87.0$ $47.84.0$ $48.87.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.0$ $47.84.80$ $47.84.80$ $47.84.80$ $47.84.80$ $47.84.86.0$ $47.84.86.0$ $47.84.86.0$ $47.84.86.0$ $47.84.86.0$ $48.84.66.0$ $48.84.66.0$ $48.84.66.0$ $48.84.66.0$ $48.84.66.0$ $48.84.66.0$ $48.84.466.50.0$ $47.84.25.0$ $48.84.466.50.0$ $48.85.86.0$	0.00;
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	9.33
4\$1604.69. \$518.52. $39$ \$176; 33. \$518.52. $Art. 628.$ $15.$ \$9412; \$5400.91. $40.$ \$8%. $15.$ \$9. \$276.54. $43.$ \$4. \$1513.77; \$45. $43.$ \$74. $74.$ \$6. $43.$ \$80.49. $16.$ \$880.49. $16.$	1.67.
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	2.68;
6. \$44955.75.       42. Latter $\frac{1}{5}$ % better.       \$5647.20.       C, \$188         7. \$400.91.       better.       2. \$97.02.       D, \$215         8. Rm. 9907.87.       44. Chatham \$60       4. \$816.25.       B, \$318         9. \$276.54.       44. Chatham \$60       4. \$816.25.       B, \$318         10. \$1053.22.       greater.       5. \$85.40.       C, \$225         11. \$151.377:       46. 160; 1334.       7. \$723.45;       E, \$131         \$47288.32.       48. \$2425.       \$8000.0       B, \$192         12. Rm. 3860.18.       49. \$7,725,574.22;       \$600.60.       18. C, \$819         13. \$52.23.       41.48%.       9. \$1267.50.       B, \$420         15. \$602.42.       75.6%.       11. \$807.80.       B, \$600         16. \$4016.22.       51. \$3.957.320;       12. \$1004;       C, \$433         16. \$4016.22.       51. \$3.912.7.       13. \$803.03.       B, \$358         1. \$8750; \$56.       53. \$1128.34.       14. \$839.40.       C, \$410         2. \$8%; \$200,000;       56. \$475.       15. \$1623.80.       21. \$1, \$155         3. \$80,00.       57. \$1450.       15. \$1623.80.       21. \$1, \$155         3. \$80000.       56. \$475.       16. \$1623.80.       21. \$1, \$155	3.29;
7. $\$400.91$ ,       better,       2. $\$97.02$ ,       D, $\$213$ 8. Rm. 9997.87.       43. $7_{47}^{*}$ %.       3. $\$80.49$ ,       16. A, $\$375$ 9. $\$276.54$ ,       greater,       5. $\$85.40$ ,       C, $\$225$ 10. $\$1053.22$ ,       greater,       5. $\$85.40$ ,       C, $\$225$ 11. $\$1513.77$ ;       45. $166\frac{2}{5}$ ,       6. $\$135.21$ ,       D, $\$135$ 12. Rm. 3860.18.       49. $\$7.725.574.22$ ; $\$748.80$ ,       17. A, $\$153$ 12. Rm. 3860.18.       49. $\$7.725.574.22$ ; $\$609.60$ ,       18. C, $\$19$ 13. $\$52.23$ ,       41.48%,       9. $\$1267.50$ ,       D, $\$745$ 14. $\$856.19$ ,       50. $\$754482$ ;       10. $\$10.94$ ,       19. A, $\$540$ 15. $\$622.42$ ,       75.6 (\%.       11. $\$807.80$ ,       B, $\$520$ 16. $\$401622$ ,       51. $\$19.27$ ,       13. $\$633.40$ ,       C, $\$410$ 17. $\$75.856$ ,       53. $\$1128.34$ ,       14. $\$839.40$ ,       C, $\$410$ 18. $\$20,000,000$ ;       54. $\$1682.91$ ,       15. $\$1623.80$ ,       21. $\$, \$138$ 19. $\$200,000,000$ ;       56. $\$4030.292$ ,       17. $\$338.24$ ,       L, $\$119$ 19. $\$200,000,00$ ;       54. $\$1625$ ,       20. $\$20.80$ ,       22. $\$351$ ,       23. $\$1167$ <td>4.88;</td>	4.88;
8.       Rm. 9997.87.       44.       Chatham \$60       4.       § \$80.49.       1.       B, \$818         9.       \$276.54.       44.       Chatham \$60       4.       \$816.25.       B, \$818         11.       \$1513.77;       45.       166 $\frac{8}{5}$ 6.       \$135.21.       D, \$187         \$82007.54;       46.       160;       133 $\frac{1}{5}$ .       7.       \$728.45;       E, \$131         \$\$47288.32.       48.       \$\$2425.       \$748.80.       17.       A, \$540         12.       Rm. 3860.18.       49.       \$7.725.574.22;       \$609.60.       18.       C, \$819         13.       \$52.33.       41.48%.       9.       \$1267.50.       D, \$745       J.       \$8, \$560         14.       \$8%.       9.       \$1267.50.       D, \$74, \$543       J.       \$8, \$560         14.       \$8%.       9.       \$1267.50.       D, \$745       J.       \$630.03.       B, \$580         14.       \$8%.       9.       \$1267.50.       D, \$74.55       J.       \$8163.00.       K, \$8410         15.       \$602.42.       75.6%.       II.       \$80.30.       K, \$8130       K, \$8135         16.       \$87400.22.	4.15.
9.9.82.76.34.44.6.00 $4.$ $8816.25.$ D. $5.$ 10.\$1053.22.greater.5. $855.40.$ C. $8225.$ 11.\$1513.77; $45.$ $166\frac{3}{2}.$ $7.$ $8723.45;$ E. $8135.21.$ \$82067.54; $46.$ $1061$ $133\frac{1}{2}.$ $7.$ $8723.45;$ E. $8135.21.$ \$81704.29; $47.$ $6\frac{1}{2}.62\frac{1}{2}.$ $8.$ $8955.40.$ D. $8187.$ \$82767.54; $46.$ $45.$ $8245$ $8.$ $8950;$ B. $8192$ 12.Rm. 3869.18. $49.$ $87.725.574.22;$ $8609.60$ $18.$ C. $81192$ 13. $852.23$ $41.48\%$ $9.$ $81267.50$ D. $8745$ 14. $8856.19$ $50.$ $8754482;$ $10.$ $8116.94$ $19.$ $A.$ $8560$ 16. $$4016.22$ $51.$ $$3.957.320;$ $12.$ $$1004!$ $C.$ $$80$ $863.00$ $B.$ $$560$ 15. $$822.00$ $54.$ $$1128.34$ $14.$ $$80$ $C.$ $$8403.29!$ $17.$ $$863.80$ $Z1.$ $J.$ $$453.80$ $Z1.$ $J.$ $$453.80$ $Z2.$ $A.$ $$8125$ 1. $$82000.000;$ $$54.81029!$ $17.$ $$838.94$ $Z1.$ $J.$ $$11.89$ $X.$ $$8119$ 2. $$86125$ $57.81625$ $20.$ $$20.850$ $C.$ $$8119$ $$8118$ </td <td>775.</td>	775.
10. $*1053.2.$ 45. $1663$ 6. $$503.40.$ 5. $$503.40.$ 5. $$503.40.$ 5. $$503.40.$ 5. $$503.40.$ 5. $$503.40.$ 5. $$503.40.$ 5. $$503.40.$ 5. $$503.40.$ 5. $$503.40.$ 5. $$503.40.$ 5. $$503.40.$ 5. $$503.40.$ 5. $$503.40.$ 5. $$503.40.$ 5. $$503.40.$ 5. $$503.40.$ 5. $$503.40.$ 5. $$503.40.$ 5. $$503.40.$ 5. $$503.40.$ 5. $$503.40.$ 5. $$503.40.$ 5. $$573.4125.$ 5. $$575.4122.$ $$5050.$ 5. $$5110.27.$ $$10.597.50.$ 5. $$560.$ 5. $$5128.32.$ $$20.04.4.88.20.$ 5. $$500.4.88.20.$ $$21.4.883.90.$ $$21.4.883.90.$ $$21.4.883.90.$ $$21.4.883.90.$ $$21.4.883.90.$ $$21.4.883.90.$ $$21.4.883.90.$ $$22.4.883.90.$ $$22.4.883.90.$ $$22.4.883.90.$ $$22.4.883.90.$ $$22.4.883.90.$ $$22.4.883.90.$ $$22.4.883.90.$ $$22.4.883.90.$ $$22.4.883.90.$ $$22.4.883.90.$ $$22.4.883.90.$	10;
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12.Rm. 3869.18.49. $\$7,725,574.22;$ $\$609.60.$ 18.C. $\$819.$ 13. $\$52,23.$ 41.48%.9. $\$1267,50.$ D. $\$745$ 14. $\$856.19.$ 50. $\$754482;$ 10. $\$116.94.$ 19.A. $\$560$ 15. $\$622.42.$ 75.6%.11. $\$807.80.$ B. $\$560$ 16. $\$4016.22.$ 51. $\$3.957,320;$ 12. $\$1004;$ 20.A. $\$231$ Art.611.52. $\$519.97.$ 13. $\$639.03.$ B. $\$5560$ 2. $\$75.9,57.320;$ 13. $\$639.03.$ B. $\$558$ S. $\$8558$ 1. $\$8750;$ $\$56.6$ 53. $\$1128.34.$ 14. $\$839.00.$ C. $\$4108.291.$ 2. $\$75.5, 128.819.27.$ 15. $\$1623.80.$ 21.J. $\$155.23.80.$ K. $\$18.82.90.$ 4. $\$20,000,000;$ $\$4030.291.$ 15. $\$1623.80.$ 22.A. $\$152.$ $$1.6,00.000;$ $$56.81625.$ 20. $$208.50.$ C. $$107.75.$ $$1.6,813.90.$ 128.80.22. $$3511.$ 23. $$1750.$ 8. $$60000.$ 62. $4\%.$ 23. $$1959.$ 24. $$11287.4$ 9. $$23325.$ Art.617.23. $$1959.$ 24. $$11287.4$ 10. $$50.$ $$5.$ $$1617.$ 23. $$1959.$ 24. $$11287.4$ 11. $$240,000;$ 1. $$7.690.418.82.$ 26. $$23326.$	2.54.
13. $\$52.23.$ 41.48%.       9. $\$1267.50.$ 19. $\Lambda, \$540$ 14. $\$856.19.$ 50. $\$754482;$ 10. $\$116.94.$ 19. $\Lambda, \$540$ 15. $\$622.42.$ 75.6%.       11. $\$807.80.$ 5.8 $\$540$ 16. $\$4016.22.$ 51. $\$3,957,320;$ 12. $\$1004;$ 20. $\Lambda, \$231$ 1. $\$8750;$ $\$56.$ 52. $\$1128.34.$ 14. $\$839.03.$ 20. $\Lambda, \$231$ 1. $\$8750;$ $\$56.$ $\$5.$ $\$1283.4.$ 14. $\$839.40.$ C. $\$4410.$ 2. $\$\%;$ $\$200.000.$ $\$40.406.50.$ $\$1483.90.$ K. $\$138.$ 4.8 $\$20.900.000;$ $\$4030.29;$ 17. $\$338.24.$ L. $\$119.$ 2. $\$\%2,500.000.$ $\$56.$ $\$475.$ 18. $\$11060.$ $22.$ $\Lambda, \$138.$ 4. $\$20.000.000;$ $\$4030.29;$ 17. $\$338.24.$ L. $\$119.$ $\$43.75.$ B. $\$118.$ 5. $\$500.$ $56.$ $\$475.$ 10. $\$43.75.$ B. $\$118.$ D. $\$940$ 7. $\$36.745.000.$ $12.8.80.$ $22.$ $\$31.818.$ D. $\$31.88.$ D. $\$39.$ D. $\$3940.$ D. $\$3940.$ D. $\$3940.$ D. $\$3940.$ D. $\$3940.$ D. $\$3940.$ D. $\$38.$ D. $\$3$	97;
14. $\$856(1.9.$ 10. $$10+482;$ 10. $\$15.$ $\$622.42.$ 15. $\$622.42.$ 75.6%.11. $\$807.80.$ B. $\$560$ 16. $\$4016.22.$ 51. $\$3.957;320;$ 12. $\$104;$ C. $\$600.$ Art.611.52. $\$519.27.$ 13. $\$639.03.$ C. $\$40.$ 2. $\$75.6\%.$ 53. $\$1128.34.$ 14. $\$839.40.$ C. $\$410.$ 2. $\$6; 200.$ $54.$ $\$1682.91.$ 15. $\$1623.80.$ 21.J. $\$15.$ 3. $\$2,500,000.$ $55.$ $\$4030.29;$ 16. $\$163.80.$ 21.J. $\$15.$ 4. $\$20,000,000;$ $\$64.930.29;$ 16. $\$163.80.$ 21.J. $\$15.$ $\$2,000,000;$ $$56.$ $\$4030.29;$ 17. $\$338.24.$ L.J. $\$119.$ $\$2,000,000;$ $$56.$ $\$4030.29;$ 17. $\$338.24.$ L. $\$119.$ $$$1025.$ 20. $$20.$ $$20.8.50.$ C. $$119.$ $$$1025.$ 20. $$22.$ $$351.$ 22. $$311.8.5.$ $$$18.20.$ 22. $$32325.$ 20.22. $$351.$ 23. $$1750.$ $$$2.3225.$ 2. $$$11.965.7.$ 2. $$$11.985.7.$ 2. $$$1128.7.6.$ $$$2.3825.$ 2. $$$11.965.7.$ 2. $$$11.985.7.$ 2. $$$142.34.$ $$$1.52.27.50.$ 2. $$$11.915.280.$ 2. $$$1750.$ 2. $$$$11.985.2.$ $$$2.3825.$ 2.	43.
15. $5022.42.$ 10.07.2.11. $$807.80.$ 12.16. $$4016.22.$ 51. $$3.957.320;$ 12. $$1004;$ 50.00,Art.611.52. $$51.9.27.$ 13. $$639.03.$ 12.17. $$8750;$ $$56.$ 53. $$1128.34.$ 14. $$839.40.$ 2.2. $$8\%;$ $$2000.$ $54.$ $$1082.91.$ 15. $$1623.80.$ 21. $$1.5.82.30.$ 2. $$8\%;$ $$2000.$ $55.$ $$4030.29;$ 16. $$1623.80.$ 21. $$1.5.835.24.$ 4. $$22,000,000;$ $$56.84030.29;$ 16. $$8183.90.$ K. $$138.90.$ 4. $$22,000,000;$ $$56.84030.29;$ 16. $$8183.90.$ K. $$138.90.$ $$2300,000;$ $$56.84030.29;$ 16. $$8183.90.$ 22. $A.8512.5.20.$ $C.$ $$11.985.5.2.20.$ $C.$ $$11.985.5.2.20.$ $C.$ $$11.985.5.2.20.$ $C.$ $$11.912.22.2.2.2.5.5.1.2.2.5.2.2.5.2.5.2.5.2.$	,
$Art. 611.$ $\$40,406,500.$ $\$2,\$104;$ $20.$ $4,\$231.$ $Art. 611.$ $52.$ $\$519,27.$ $13.$ $\$639,03.$ $2.$ $4.$ $\$231.$ $1.$ $\$8750;$ $\$56.$ $53.$ $\$1128.34.$ $14.$ $\$839,40.$ $21.$ $J.$ $\$358.$ $1.$ $\$8750;$ $\$56.$ $53.$ $\$1128.34.$ $14.$ $\$839,40.$ $21.$ $J.$ $\$430,406,500.$ $2.$ $\$64030.29;$ $16.$ $\$1682.90.$ $17.$ $\$38,940.$ $21.$ $J.$ $\$155.$ $3.$ $\$2,000,000;$ $\$4030.29;$ $16.$ $\$183.90.$ $Z1.$ $J.$ $\$119.$ $\$2,0000,000;$ $\$6.$ $\$475.$ $18.$ $\$11060.$ $22.$ $A,\$128.$ $4.$ $\$20,000,000;$ $56.$ $\$475.$ $18.$ $\$11060.$ $22.$ $A,\$152;$ $\frac{1}{7}.$ $570.$ $56.$ $\$1625.$ $20.$ $\$208.50.$ $C.$ $\$118;$ $5.$ $\$500.$ $62.$ $4\%.$ $22.$ $\$328.$ $D.$ $\$940$ $7.$ $\$36,745,000.$ $128.80.$ $22.$ $\$3515.$ $23.$ $\$1750.$ $2.$ $\$32325.$ $Art. 617.$ $22.$ $\$1128.62.$ $22.$ $\$311287.62.$ $12.$ $\$240,000;$ $1.$ $\$7,690,418.82.$ $\$197.75.$ $2.$ $\$11287.62.$ $2.$ $\$32317.50.$ $2.$ $\$11,615,280.$ $2.$ $\$11,986.57.$ $2.$ $\$11,986.57.$ $12.$ $\$32412.50.$ $\$38,616.57.$ $\$11,986.57.$ $3.$ $$16.$	i
Art. 611. $52, $519.27.$ $3, $639.03.$ $B, $358$ 1. \$8750; \$56. $53, $1128.34.$ $14, $839.40.$ $2.4, $569.03.$ $B, $358$ 2. \$8%; \$2000. $54, $1682.91.$ $15, $1623.80.$ $21, J, $155.$ 3. \$2,500,000. $54, $4030.29.$ $16, $183.90.$ $K, $138.$ 4. \$20,000,000;\$4030.29. $17, $338.24.$ $L, $119.$ $$2,000,000;$ $56, $475.$ $18, $11060.$ $22. A, $152.$ $$4, $20,000,000;$ $56, $475.$ $18, $11060.$ $22. A, $152.$ $$4, $20,000,000;$ $56, $475.$ $19, $843.75.$ $B, $118.$ $$5, $500.$ $58, $1625.$ $20, $208.50.$ $C, $1070.$ $6, $61250.$ $60, 124.59;$ $21, $439.88.$ $D, $940.$ $7, $36,745,000.$ $128.80.$ $22, $351.$ $23, $1750.$ $8, $60000.$ $62. 4\%.$ $23, $1959.$ $24, $11287.0$ $9, $23325.$ $Art. 617.$ $25, $37242;$ $S, $1423.$ $10, 550$ shares. $Art. 617.$ $25, $37242;$ $S, $1423.$ $11, $240,000;$ $1, $7,690,418.82.$ $$197.75.$ $T, $1123.$ $$12, $$23100.$ $3, 34, mills;$ $27, $487.27.$ $26, $2483.60.$ $U, $925.$ $12, $$2240.$ $3, 34, mills;$ $27, $487.27.$ $26, $2, $700.$ $12, $$230.5.$ $$11,986.57.$ $$11,986.57.$ $$3, $4, $1960.$ $$3, $3, $156.30.$ $Y, $200.$ $14, $$2200.2, $2, $8, $8, $231.39.$ $$3, $4, $1960.6.$ $$3, $5\%.$ $$3, $4, $1960.5.$ $$2, $705.$ $15, $8020.0, $20, $8, $8, $231.39.$ $$$	.63:
1. $\$8750$ ; $\$56$ . $53$ . $\$1128.34$ . $14$ . $\$839.40$ .C, $\$410$ 2. $8\%$ ; $\$200$ . $54$ . $\$1682.91$ . $15$ . $\$633.90$ . $21$ . J, $\$155$ 3. $\$2.000,000$ ; $55$ . $\$4030.29$ ; $16$ . $\$183.90$ . $21$ . J, $\$155$ 4. $\$20,000,000$ ; $\$4030.29$ . $17$ . $\$338.24$ . $L$ . $\$119$ $\$20,000,000$ ; $$56$ . $\$475$ . $18$ . $\$11060$ . $22$ . A, $\$152$ . $$1\%$ . $$57$ . $\$1450$ . $19$ . $\$43.75$ .B, $\$118$ . $5$ . $\$500$ . $66$ . $\$175$ . $20$ . $\$208.50$ .C, $\$1070$ $6$ . $\$61250$ . $60$ . $124.59$ ; $21$ . $\$439.88$ .B, $\$192$ . $7$ . $\$36,745,000$ . $128.80$ . $22$ . $\$351$ . $23$ . $\$1750$ . $8$ . $\$60000$ . $62$ . $4\%$ . $23$ . $\$1959$ . $24$ . $\$1287.4$ $9$ . $\$23325$ . $Art.$ $617$ . $25$ . $\$37242$ ; $8$ . $\$1287.4$ $10$ . $\$36,745,000$ . $1$ . $\$7,690,418.82$ . $\$197.75$ . $T$ . $\$1423$ . $11$ . $\$24,0000$ ; $1$ . $\$7,690,418.82$ . $\$197.75$ . $T$ . $\$192$ . $11$ . $\$24,0000$ ; $1$ . $\$7,690,418.82$ . $$26$ . $\$2483.60$ . $U$ . $\$925$ . $12$ . $\$24,0000$ . $3$ . $\$11,918$ . $27$ . $\$487.27$ . $26$ . $X$ . $\$500$ . $12$ . $\$24,0000$ . $8$ . $\$2,311,918$ . $27$ . $\$487.27$ . $26$ . $X$ . $\$500$ . $12$ . $\$24,900$ . $8$ . $\$231.39$ . $8$ . $\$2960$ . $8$ . $\$327.50$ . $12$ . $\$29043.75$ . $\$42.84$ . $5$ . $\$33666.67$ . $8$ . $\$29200$ . $13$ . <t< td=""><td>.40;</td></t<>	.40;
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3.97.
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	3.97;
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10. 550 shares. $Art. 617.$ 25. $\$37242;$ S. $\$143;$ 11. $\$240,000;$ 1. $\$7,690,418.82.$ $\$197.75.$ T. $\$113;$ $\$185,237.50.$ 2. $\$11,615,280.$ 26. $\$2483.60.$ U. $\$925.$ 12. $\$23100.$ 3. $3!$ mills;       27. $\$487.27.$ 26. X. $\$500.$ X. $\$500.$ 13. $\$36412.50.$ $\$38,666.37;$ 28. $\$156.30.$ Y. $\$200.$ X. $\$500.$ 14. $\$226675.$ $\$11,986.57.$ 4. Rate 5.8 mills;       3. A. $\$1960;$ A, $\$123;$ 16. $\$29043.75.$ $\$42.34.$ 3. A. $\$1960;$ A. $\$123;$ 17. $\$668625:$ 6. $\$37.49.$ B. $\$2960.$ B. $\$3257.50.$ S. $\$231.39.$ B. $10.$ S. $\$326.66.7;$ D. $\$3366.7;$ S. $\$3366.67.$ D. $\$326.0.$ D. $\$3925.2,$ S. $\$323.33.$ bro; $$164.71.$ D. $\$3926.2,$ S. $\$231.39.$ B. $10.$ S. $\$55\%;$ S. $$3366.67.$ S. $$3366.67.$ S. $$3366.67.$ S. $$3366.67.$ S. $$3366.67.$ S. $$3200.$ S. $$200.$ S. $$225.8,$ S. $$3366.67.$ S. $$255\%;$ S. $$3200.$ S. $$25\%;$ S. $$220.0.$ S. $$25\%;$ S. $$230.0.$ S. $$25\%;$ S. $$2300.$ S. $$25\%;$	i;
$II. \ \$240,000;$ $I. \ \$7,600,418.82.$ $\$197,75.$ $I. \ \$112;$ $\$185,237.50.$ $I. \ \$11,615,280.$ $26. \ \$2483.60.$ $U. \ \$925.$ $II. \ \$22010.$ $3. \ \$ \ mills;$ $27. \ \$487.27.$ $26. \ \$2483.60.$ $V. \ \$925.$ $II. \ \$220675.$ $\$11,986.57.$ $II. \ \$487.27.$ $26. \ \$497.27.$ $26. \ \$529043.75.$ $\$11,986.57.$ $I6. \ \$29043.75.$ $\$42.34.$ $3. \ A. \ \$1960;$ $A. \ \$126. \ \$700.$ $27. \ \$65\%.$ $I7. \ \$68625:$ $6. \ \$37.49.$ $B. \ \$29060.$ $B. \ \$2960.$ $B. \ \$2956.$ $I9. \ \$2060. \ 20. \ \$. \ \$. \ \$231.39.$ $B. \ Dr. \ \$164.71.$ $D. \ \$396.$ $22. \ \$30800. \ 10. \ \$597.85.$ $\$3366.67.;$ $\$28. \ $55\%;$ $\$39020.$ $21. \ \$8230. \ 10. \ 597.85.$ $\$366.48. \ 5. \ \$3366.67.;$ $\$28. \ 55\%;$ $\$39020.$ $28. \ $55\%;$ $\$29020.$ $23. \ \$775. \ 11. \ \$104.98. \ 22. \ $50. \ 8. \ $2366.82. \ 20. \ $11279.75; \ F. \ \$176.62. \ 12. \ \$602.92. \ 12. \ $5020.52. \ 11190.75; \ F. \ \$176.62. \ 1190.75. \ 11. \ \$105.62. \ 11190.75. \ 11. \ \$105.62. \ 11190.75. \ 11. \ \$105.62. \ 11190.75. \ 11. \ \$105.62. \ 11190.75. \ 11. \ \$105.62. \ 11190.75. \ 11. \ \$105.62. \ 11190.75. \ 11. \ \$105.62. \ 11190.75. \ 11. \ \$105.62. \ 11190.75. \ 11. \ \$105.62. \ 11190.75. \ 11. \ \$105.62. \ 11190.75. \ 11. \ \$105.62. \ 11190.75. \ 11. \ \$105.62. \ 1$	;
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12. $52.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ $53.$ <t< td=""><td></td></t<>	
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17. $517560.$ 4. Rate 5.8 mills;       Art. 639.       27.       65%.         16.       \$29043.75.       \$42.34.       3. A, \$1960;       A, \$123;         17.       \$68625:       6.       \$37.49.       B. \$2960,       B, \$3250;         18.       \$3277.50.       7.       \$57.85.       4. A, Cr.\$1623.17;       C. \$1956;         19.       \$16200, 20. 8.       8.       \$2231.39.       B, Dr. \$164.71.       D, \$3963;         21.       \$83800.       10.       \$557.85.       \$33666.67.       \$9020.         23.       \$775.       11.       \$104.98.       6.       C, \$11431.88;       29. 42%;         24.       500 shares.       12.       \$5284.88.       D, \$11270.75;       F, \$1764;         25.       \$8000.       13.       \$5284.88.       E, \$11190.75;       H, \$1056;	1
16. $\$29043.75.$ $\$42.34.$ 3. A, $\$1960;$ A, $\$123;$ 17. $\$68625:$ 6. $\$37.49.$ B, $\$2960.$ B, $\$3256.$ 18. $\$3277.50.$ 7. $\$57.85.$ 4. A, Cr. $\$1623.17;$ C, $\$1956.$ 19. $\$16200.$ 20. 8.       8. $\$231.39.$ B, Dr. $\$164.71.$ D, $\$3963.$ 21. $\$8230.$ 9. $\$60.48.$ 5. $\$833.33.$ bro.       28. $55\%;$ 22. $\$80800.$ 10. $\$597.85.$ $\$3366.67.$ $\$9020.$ 23. $\$775.$ 11. $\$104.98.$ 6. C, $\$11431.88;$ 29. $42\%;$ 24. 500 shares.       12. $\$65.28.$ D, $\$11279.75;$ F, $\$176.$ 25. $\$8000.$ 13. $\$5284.88.$ E, $\$11190.75.$ H, $\$105.$	
17. $\$68625$ :       6. $\$37.49$ .       B. $\$2960$ .       B. $\$3250$ 18. $\$3277.50$ .       7. $\$57.85$ .       4. A,Cr. $\$1623.17$ ;       C. $\$1950$ 19. $\$16200$ .       20. 8.       8. $\$231.39$ .       B, Dr. $\$164.71$ .       D, $\$3963$ 21. $\$8230$ .       9. $\$60.48$ .       5. $\$833.33$ , bro.       28. $55\%$ ;         22. $\$80800$ .       10. $\$597.85$ . $\$3366.67$ . $\$9020$ .         23. $\$775$ .       11. $\$104.98$ .       6. C, $\$11431.88$ ;       29. $42\%$ ;         24. 500 shares.       12. $\$65.28$ .       D, $\$11279.75$ ;       F, $\$1766$ 25. $\$9000$ .       13. $\$5284.88$ .       E, $\$11190.75$ .       H, $\$1056$	;
18. \$3277.50.       7. \$57.85.       4. A,Cr.\$1623.17;       C, \$1956         19. \$16200. 20. 8.       8. \$221.39.       B, Dr. \$1647.11.       D, \$3963         21. \$8230.       9. \$60.48.       5. \$833.33. bro.       28. 55%;         22. \$80800.       10. \$597.85.       \$3366.67.       \$9020.         23. \$775.       11. \$104.98.       6. C, \$11431.88;       29. 42%;         24. 500 shares.       12. \$65.28.       D, \$11279.75;       F, \$1766         25. \$8000.       13. \$5284.88.       E, \$11190.75.       H, \$1050	;
19. $\$10200$ , 20. 8.       8. $\$231.39$ .       B. Dr. $\$164.71$ .       D. $\$396.22$ 21. $\$8230$ .       9. $\$60.48$ .       5. $\$833.33$ , bro.       28. $\$5\%$ ;         22. $\$80800$ .       10. $\$597.85$ . $\$3366.67$ . $\$9020$ .         23. $\$775$ .       11. $\$104.98$ .       6. C, $\$11431.88$ ;       29. $42\%$ ;         24. $500$ shares.       12. $\$65.28$ .       D, $\$11279.75$ ;       F, $\$105.426$ .         26. $\$4000$ .       13. $\$5284.88$ .       E. $\$11190.75$ .       H. $\$105.426$ .	;
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25. \$8000. 13. \$5284.88. E, \$11190.75. H, \$1050	:
20 0117017 1 11 0000 01 0 DE 010700 07 TZ 01070	;
$20. \ \$117040. \qquad 14. \ \$232.31. \qquad 8. \ M, \ \$18029.20; \qquad K, \ \$4900$	
27. \$28494.67. 15. \$2138.05. N, \$6389.75. 30. A, 60 ft.	;
28. \$23044.58. 16. \$393.42. 9. A, \$26666.67; B, 80 ft.	; _
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	•
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32. \$34137.50, 18. \$66500, B. \$2502.12, 0. \$1024	5.54.
## Art. 639.]

### ANSWERS.

33.	A, \$3847.56;	10.	\$636.58;	17.	£10. 0s. 9d.	Í	Cr. B, \$12695;
	B, \$4902.44.		\$637.45.	18.	\$102.		Cr. C, \$12695;
34.	A, \$12346.82;		1 . 000	19.	\$433.93.		Cr. Sundry
	B, \$5877.67.		Art. 662.	20.	\$889.36.		Creditors,
35.	A, \$2505.74;	1	@131.00	21.	\$261.83.		\$4050.
	B, \$17307.58;	10	\$127 90	22.	120 bbl.		
	C, \$16723.84.	10	\$107.40. \$110.90	23.	135458 lb.		Art. 667.
36.	A, \$17527.74;	0.	\$110.00. \$10.00	24.	\$676.77.	1	26 5 91
	B. \$20323.76;	4.	\$1030.40.	25.	<b>0</b> .	0	19 6 196
	C. \$6310.43:	0.	\$0.034;	26.	Loss. \$500.	0	40. 0. 120.
	Will lose \$140.		\$0.072;	27.	3010%.	0.	00. 7. 120.
37	A \$7331 20.		\$0.104.	28	\$500	4.	12. 8. 144.
01.	B \$4950.50	6.	\$0.655.	29	\$35.58		Ant CN1
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1.	72.06 .		\$29080.	34.	\$001.90.		Art. 674,
	\$5760	12.	\$996.80.	35.	\$920.02;	1.	\$9715.20.
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4.	\$11400; \$C1000;		φ20.30, Φ906 57		\$73.89;	6	@1/7/ 97
	\$04000;	10	\$290.07. \$49010.		\$72.88.	14	\$2196 6 <sup>19</sup>
~	\$86000.	10.	\$42919;	38.	\$4166.30;	1.	\$0420.0 · ·
5.	\$21375;	1 100	\$29169.33.		\$4160.47.		Art GYY
	\$475000.	17.	\$4190.03;	39.	\$5171.73:		
6.	\$3,338,100.		\$3084.60;		\$5181.19.	2.	\$261.58.
7.	26.26%;		\$933.35;	1.0	\$4165.03	4.	\$1327.61.
	\$23,944,096.50;		54 yr.	1.1	\$630.97	8.	\$549.51.
	\$1,213,591.50.	18.	\$152.79;	1.0	\$2474.07	9.	\$3260.51.
8.	\$1,433,831.70.		\$77.86.	1.0	Q0895 02		1 . 000
9.	\$1047.54;	19.	\$13.63.	40.	17651 90 fr	-	Art. 682.
	\$427.84.	20.	\$2655.65.	44.	01001.20 11.	2.	\$120.
10.	\$2313.65.			40.	\$1009.22. \$7 10. \$9 90	3.	\$72.
11.	12%:		Art. 663.	40.	φ1.10; φ2.00. 0114 75	4.	\$6.20.
	10%:		10.11	41.	\$114.70.	5.	\$27.
	19.56%.	1.	1041.	48.	Aug. 29;		
12	4.64 0/0	2.	21659.6.		\$0309.30.		Art. 687.
1~.	-109/0.	3.	40320.	49.	Jan. 14, 1883;	1	\$50.17
	Art 650	4.	\$164.52.		\$1409.40.	0	\$36.60
-		5.	16° 48′ 15″.	50.	\$1409.37.	2	\$159
1.	\$374.60;	6.	16666 <sup>2</sup> / <sub>3</sub> sq. yd.	51.	\$320.31.	0.	φ100.
	\$374.93.	7.	£69 0s. 6d.	52.	\$1625.		Art. 690.
2.	\$669.35;	8.	\$140.25.	53.	\$425.		50.
	\$671.70.	9.	$38\frac{1}{8}$ sq. yd.;	54.	\$37000.	2.	950
3.	\$25.14.		\$24.15.	55.	\$81.25.	5.	00C.
4.	\$755.28:	10.	£19 3s. 6d.	56.	\$4224.	4.	986.
.,.	\$757.38.	11.	\$5567.50:	57.	\$128.21.		Ant GOR
5.	\$462.10:		\$4.443. wood :	58.	\$295.75.	-	A.r., 000.
	\$464.38		\$.486. grain.	59.	\$208.50.	2.	2, 1, 5, 1;
6	\$190.91	12	\$1803 07	60	B. \$5011.83:		3. 2. 3. 5.
0.	\$101.04	12	\$ 8302	00.	C \$1794.53	3	3, 4, 5, 1;
ry	\$06.15	11.	¢.000%.		Dr Mdse etc	0.	4 3 1 5
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0	\$029.07. 9557 91	15	\$1007088.44.		Dr. Sunary	E	1 1 2 6 1.
9.	\$007.31;	15.	\$40.73. \$400 mg		Deptors,	0.	1, 1, 0, 0, 1;
	\$007.86.	16.	\$430.72.		\$17030;		0, 0, 1, 1, 0.

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	Art. 695.	12. 716.	$16. \frac{5}{7}; \frac{5}{8}; \frac{33}{85}.$	18. 502.656 A.
07	10 10 45	13. 15.25.	17. 35.03 in.	
3	30 90	14. 1994.		Art. 730.
1	12 48 48.	15. 20.78.	Art. 724.	
4.	36 36 108	16. 2732.		2. 6.8027%;
5	15 15	17. 19683.	1. 18.9875 A.	\$493.20.
6	9 15 3.	$18. \frac{16}{25}; \frac{87}{40}; \frac{75}{111}.$	2. 1.625 A.	3. \$225.
0.	16 4 20	19. 642 rods.	3. 290.47 sq. rd.	4. V r. \$3581.16;
	10, 1, 20.	20. 208.71 ft.	4. 34 A. 145 sq.	C p. \$3681.16;
	Ant GOY	21. 1.41421.	rd. 25 sq. yd.	Adj. rec. \$100.
	Art. 077.	1	8 sq. ft. 108	5. \$4869.57.
2.	5, 60, 15, 30;	Art. 705.	sq. in.	6. Ship receives
	8, 52, 24, 26.	<i>L.</i> 18.	5. 1680.6 ft.	\$1888.08;
4.	33, 12, 5.	3. 2.2.	6. 471.24 ft.	A r. \$964.23:
	1	4. 68.	7. 5541.78 sq. ft.	B p. \$1472.82;
	Art. 701.	5. 78.	8. 14.7 sq. ft.	C p. \$496.94;
2.	33.	6. 82.	9. 3525 gal.	D p. \$1032.55;
3.	121.	7. 196.	10. 5.32 cu. ft.	Adj. rec. \$150.
4.	135.	8. 2.13	11. $15053\frac{1}{2}$ tons.	7. C p. \$1200.79;
5.	216.	9. 23.9.	12. 59.9 in.	S rec. \$974.60;
6.	218.	10. 462.	13. 466.69 ft.	Adj. rec. \$150;
7.	255.	11. 6.54.	14. 75.3984 cu. ft.	Agent receives
8.	294.	12. 75.8.	15. 6 ft. 6 in.	\$76.19.
9.	312.	13. 878.	16. 32 yd.	8. G. A., \$516.81;
10.	345.	14. 82.	17. 45.14 rd.;	S, \$638.79;
11.	37.5.	15. 47 in.	141.8 rd.	0, \$789.09.

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