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## A POCKET-BOOK

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FOR

## IINERS AND METALLURGISTS

## £itles, $\mathfrak{f o r m u l x}$, Cables, and Notes

FOR USE IN FIELD AND OFFICE WORK

COMPILED BY

## FREDERICK DANVERS POWER, F.G.S.

 MEMBER OF THE INSTITUTE OF MINING AND METATIURGY, MEMBER OF THE AMERICAN INSTITUTE OF MINING ENGINEERS, MEMBER OF THE AUSTRAIAASIAN INSTITUTE OF MINING ENGINEERS, ETC.Thiro Edition, $\operatorname{correcte}$


## LONDON

CROSBY LOCKWOOD AND SON
7 stationers' hall court, iudgate hilf and 5 broadway. wrstminstrer

1914
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## $\pi N 151$ <br> $P_{6}$

 HERTFORD.

## PREFACE.

This little work is intended as a vade mecum for those engaged in mining and metallurgical industries. It is designed to furnish them with a collection of rules, formulæ, tables, and other such information as may be found useful, if only to refresh the memory, in the multifarious operations falling within the daily duties of the practical miner and metallurgist.

In field work, especially, persons connected with mining have long felt the want of a suitable PocketBook which should contain concise notes of the various sciences with which metal-mining is concerned -a volume which they could carry about with them on the field, when travelling, or when engaged away from their head-quarters and thus debarred from consulting works of reference. The notes and other information comprised in the following pages have been put together in their present form in the spare time of the compiler. Having been found of use to him in the actual exercise of his profession, they are now published in the hope that they may be found of like service to others.

Such a work as this is of necessity a compilation. A list of books is accordingly given (see page xv.) to which reference has been made. Where the author of a table or formula previously published is known, care has been taken to give due acknowledgment. But it
is not always easy to discover the original authorit for material current in various publications.

The compiler's thanks are due to Messrs. S. J Becher and W. Harris for their assistance in checkin certain calculations contained in the work, and to th former gentleman, also, for his "Hints on Photo graphy." He is also indebted to Mr. E. Henry Darie for having revised the proof sheets.

The compiler will feel indebted to any one who wil kindly assist him by pointing out any errors which may possibly have escaped his observation, in orde: that they may be corrected in future editions. Hek will also welcome any suggestions for the improve ment of the work.
F. D. P.

> Melbourne (Victoria), March, 1892.

## NOTE TO THIRD EDITION.

In placing a new edition of this book before the public, the compiler has to thank Mr. F. A. Eastaugh, A.R.S.M., for rewriting the greater portion of the section on Assaying. The classifications of rocks adopted are those more likely to be of service to the miner than that given in former editions; the section on Slags has been extended, the portion on Ore Dressing has been brought up to date, while several additions, e.g. Knots and Splices, use of Slide Rules, and notes on Mine Sampling have been made, which it is hoped will cause the book to be of greater value to those who use it.
F. D. P.

$$
\text { Sydney, N.S.W., } 1913 .
$$

## CONTENTS.



## Arithmetic.

|  | PAGE |
| :--- | :--- |
| Tractions (Addition, Subtraction, Multiplication, Division, |  |
| Greatest Common Devisor, to reduce to Lowest Terms, |  |
| to reduce to a Decimal) |  |
| Jecimals (Addition, Subtraction, Multiplication, Division) | 1,2 |
| A volution (Extraction of Square Root) | 2 |

Algebra.
Powers, Roots . . . . . . . . 3
Equations . . . . . . . . . 3

## Trigonometry.

Formulæ . . . . . . . . . 4-6

## Mensuration.

Triangles, Squares, Parallelograms, Trapezoids, Trapeziums, Polygons, Circles, Sectors, Segments, Circular Rings, Ellipse, Parabola, Cubes, Prisms, Pyramids, Prismoids, Wedges, Cylinders, Cones, Spheres, Spherical Segments, Cylindrical Rings, Paraboloids . . . 6, 7

## Tables.

Logarithms of Numbers from 10 to 1200
Powers (Root, Circumference, Area, Square, Cube, Square
Root, and Cube Root)
Lengths of Circular Arcs, Chords and Heights of Ares to
Radius 1 .
Natural Sines and Tangents to Radius 1 . . 28-33
Underlie and Perpendicular in Feet and Inches to every
Degree of the Quadrant in Six Feet . . . 34
PAGE
Comparison of Angle Degrees and Slope ..... 35
Inclined Measure ..... 35
Weights and Measures.
Avoirdupois, Troy, Apothecaries' Weight ; Apothecaries'Fluid ; Liquid Measure U.S.A. ; Dry Measure U.S.A. ;Old Diggers' Measure ; Imperial Measure of Capacity ;Long Measure ; Surface Measure; Cubic Measure;Carpenters', Bricklayers', and Builders' Measurements;Measure of Timber; Sizes of Slates; Angular Measure;Power; Paper; Drawing Paper; Metrical Weightsand Measures36-46
Perpetual Calendar ..... 47
Various.
To convert American into English Money ..... 48-50
Equivalent Rates per Lb., Cwt., and Ton ..... 51
Income for Year, Quarter, Cal. Month, Week, or Day ..... 52
Compound Interest ..... 53-55
Wages Table for Eight Hours per Day ..... 56-65
Calculating Rules . ..... 66-72
Slide Rule for computing the Value of Ores ..... 73
Methods of computing Lode Values ..... 74, 75
Points of the Compass ..... 76
Morse Alphabet and Figures ..... 76
Knots and Splices . ..... 77-81
Mining Accounts and Costs ..... 81-91
Corrections for the Press ..... 92
Weight of Water (at $62 \frac{1}{4}$ lbs. per cubic foot) contained in One Foot Length of Pipes of Different Bores ..... 93
Approximate Proportions and Weights of Nine Feet Lengths of Cast-iron Pipes of various Sizes ..... 94
Weight of 100 Feet of Wire in Pounds, when the Size is measured by the New Standard Wire Gauge of 1884 ..... 95
Weight of a Square Foot of Lead, Copper, Gun-metal, Brass, White Metal, Steel, Wrought Iron, and Zinc, when the thickness is measured by the Board of Trade New Legal Standard Wire Gauge of 1884 ..... 96, 97
Sizes of Battery Screens ..... 98
Appropriate Sizes and Proportions for Pump Rods ..... 98
Acres required per Mile and per 100 Feet for different Widths ..... 99
PAGE
Area of Cross Sections of Cuttings or Embankments Fifteen Feet in Width at Formation Level, with Slopes of $1 \frac{1}{2}$ to 1 ..... 100
Area of Cross Sections of Cuttings or Embankments Twelve Feet in Width at Formation Level, with Slopes of $1 \frac{1}{2}$ to 1 ..... 101
Specific Gravity Degrees, comparing the Areometers of Baumé, Cartier, and Beck (for Liquids heavier than Water) ..... 102
Specific Gravity Degrees, comparing the Areometers of Baumé, Cartier, and Beck (for Liquids lighter than Water) ..... 103
Transformation of Columns of Water into Columns of Mercury ..... 104
Approximate Size and Weight of Rails for Loaded Waggons of certain Weights, the sleepers being 2 ft .2 in . apart. ..... 104
Railway Curves ..... 104 ..... 104
Heat.
Thermometers (comparison of Celsius, Réaumur, and
Fahrenheit Scales) ..... 105, 106
Specific Heat ..... 107
Specific Heat of Gases and Vapours ..... 107
Approximate Temperatures indicated by Colour of Fire ..... 107
Theoretical Heating Power ..... 108
Melting-point of Easily Fusible Alloys ..... 108
Walker's List of Frigorific Mixtures ..... 109, 110
Electricity.
Electro-plating (Copper-bronze, Silver, and Gold Solutions) ..... 110
Electrical Units ..... 111
Electro-motive Forces of various Cells ..... 112,113
Air and Water.
Wind ..... 114
Quantity of Water per Acre for a given Depth of Rainfall ..... 114
Statics.
Pressure against Walls . ..... 115

## Dynamics.

PAGE
Velocity at the Circumference per Second, with a given
Number of Revolutions per Minute for the Radius 1 116, 117 Falling Bodies, giving the Space fallen through to acquire certain Velocities ..... 118
Motors.
Self-acting Inclines ..... 119,120
Aerial Ropeways ..... 121
Work of a Man against Known Resistances ..... 122
Work of a Horse against Known Resistances ..... 122
Steam Engines (Horse Power, Composition of Fuel, Lubricants) ..... 123, 124
Steam Boilers (Boiling-point of Water under Different Pressures; to find the Nominal Horse-Power of a Boiler; to find the Number of Cubic Feet of Water evaporated per Hour; Weight of a Boiler) ..... 124, 125
Fuel (Evaporative Power of Fuels; British Thermal Unit; to find the Quantity of water in lbs. evapo- rated per lb. of Coal) ..... 12.5
Proper Diameter and Height of a Chimney for any kind of Fuel ..... 126
Pressures in Atmospheres ..... 126
Transmission of Power.
Belting ..... 127
Speeding of Machinery (Speeding by Pulleys; Speeding by Wheels) ..... 128
Hydraulics.
Greatest Velocity of Current close to the Bed of a Stream consistent with the Stability of the Material over which the Water Flows ..... 128
Proper Angle for the Sides of Aqueducts of Different Material, and the Rate of Flow that should not be exceeded ..... 129
Velocities of Water in Channels in Earth for various Slopes and Hydraulic Mean Depths ..... 129
Velocity of Efflux . ..... 130
PAGE
Discharge in Gallons ..... 130
Theoretical Discharge of Water by Round Apertures of various Diameters, and under different Heads of Water Pressure . ..... 130, 131
Discharge through an Orifice in a Thin Plate ..... 131
Discharge by Short Tubes ..... 132
Friction of Long Pipes ..... 132
Loss of Head by Bends ..... 132
Actual Discharge by Short Tubes of various Diameters, with Square Edges and under different Heads of Water Pressure ..... 133
Bends in Water Pipes showing the Loss of Head due to Change of Direction by One Bend of $90^{\circ}$ ..... 134, 135
Discharge of Pipes by Prony's Formula . ..... 136-138
Effect of Contour of Section ..... 139
General Laws for Pipes ..... 139
Head for very Low Velocities ..... 139
Head due to Velocity in Open Channels ..... 139
Velocities in Feet per Second due to given Heads ..... 140
Discharge of Water Courses ..... 140
Head to overcome Friction of Channel ..... 140
Submerged Openings ..... 140
Head for Low Velocities ..... 141
To find the Velocity ..... 141
To find the Fall ..... 141
The Discharge of Canals, Rivers, etc., by Eytelwein's Rule ..... 141
The Velocity of Discharge in Open Channels, Rivers, etc., with different Heads ..... 142-145
Weirs ..... 146
Square and Rectangular Pipes ..... 146
Common Overflow Pipe ..... 146
Discharge of Outlet Pipes ..... 147
Strength of Materials.
Strength of Thick Pipes ..... 147
Strength of Thin Pipes ..... 147
Moment of Resistance and Moment of Inertia for different Cross-sections ..... 148, 149
Round Ropes ..... 149
Round Taper Ropes ..... 150
Flat Ropes ..... 150
Weights and Breaking Loads of Manilla Ropes ..... 151
PAGE
Strength and Weight of Close-link Crane Chains and Size of equivalent Hemp Rope ..... 152
Softwood Timber ..... 153
Australian Hardwood Timber ..... 154
Table of the Symbols and Atomic Weights of the Elements ..... 155
Normal Solutions ..... 156
Chemical Arithmetic (To find the percentage Composi- tion having the Formula given. To find the Empirical Formula of a Body from its percentage Composition. To find the Weight of a Substance required to yield, liberate, or produce a given Weight of a Substance) ..... 157
Table for the Calculation of Analysis ..... 157-162
Blow-pipe Analysis ..... 163-175
Gold and Silver Assay (Scorification Assay, Pot Assay, Cupellation, Bullion Assay) ..... 175-178
Table for converting Percentages into Troy Weight per Statute Ton ..... 178
Table showing the quantity of Fine Gold in an ounce of any Alloy to one-eighth of a carat, and the Mint value of the Gold in an ounce of each Alloy ..... 179
Copper Assay (Cyanide, Iodide, and Electrolytic Methods) ..... 180, 181
Lead Assay (Ammonium Molybdate Method) ..... 181-183
Zinc Assay (Potassium Ferro-cyanide Method) ..... 183, 184
Tin Assay (Cyanide of Potassium Method) ..... 184
Slag Analysis (Determination of Copper, Iron, Silica, and Lime). ..... 184, 185
Combination of Acids and Bases in Water Analysis ..... 185
Composition of Air ..... 186
Taking a Sample of Air ..... 186
Testing Cyanide Solutions ..... 187
Table for Standardizing Sump Solutions ..... 188
Standard Screens for Laboratory use ..... 189
Sizing Test and Grading Analysis . ..... 189
Table for the Conversion of Percentages into cwt. andlbs. per ton, and into lbs. per cwt. . . . 190, 191
Assay of Fuel (External Appearance, Moisture, SpecificGravity, Volatile Hydrocarbons, Coke or Charcoal, Ash,Fixed Carbon, Sulphur ; other peculiarities of Fuels,absolute Heating Power, specific Heating Power) 191-193
Tests for Common Impurities found in Mine Waters(Hard or Soft Water, Carbonic Acid, Sulphuric Acid,Chlorides, Sulphuretted Hydrogen, Alkalies or AlkalineEarthy Matters, Lime, Magnesia, Iron, Copper) . 193, 194
Adulteration of Oils, Lard, and Tallow (Olive Oil, Oil of Sweet Almonds, Rapeseed Oil, Sesame Oil, Linseed Oil, Black Poppy Oil, Hempseed Oil, Castor Oil, Neat's foot Oil, Oleic Acid, Palm Oil, Cocoanut Oil, Lard, Tallows, Physical Properties of Oils)
194-197
Slags . . . . . 197-212
Humidity, Wet and Dry Bulb Thermometers
212

## Mineralogy and Geology.

List of Minerals, giving their Composition, Hardness, sp. gr., Crystalline System, and Colour . . 213-230
Scale of Hardness . . . . . . . 213
Scale of Fusibility . . . . . . . 213
Distinguishing Characteristics of Gems . . . 231-235
Specific Gravity of Solids . . . . . . 236
Specific Gravity Solutions . . . . . . 236
Table of Specific Gravities . . . . . . 237
Geological Formations . . . . . . . 238
Petrology (Classification of Igneous, Sedimentary, and Metamorphic Rocks) . . . . . . 238-243
Sampling . . . . . . . . 243-248
Mine Examination . . . . . . 248-252
Zimmermann's Rule for determining the Direction in which to drive to find a Dislocated Reef . . 252, 253
To calculate the true Thickness of an Inclined Bed when
passed through in a Bore-hole. . . . . . 253
To calculate the Expense of Sinking . . . . 254
Uses of Rocks and Minerals (Aluminium, Antimony, Arsenic, Bismuth, Cadmium, Chromium, Cobalt, Copper, Gold, Iridium, Iron, Lead, Manganese, Mercury, Molybdenum, Nickel, Osmium, Palladium, Platinum, Potassium, Silver, Sodium, Strontium, Tellurium, Tin, Titanium, Tungsten, Uranium, Vanadium, Zinc ; Building and Decorative Stones; Ornamental and Precious Stones ; Grinding, Whetting, and Polishing Materials; Refractory or Fire-resisting Substances; Clays we fabricate; Glazes, Enamels, Colours; Mineral Manures ; Food and Medicine; Fossil Fuels; Light Producers; Sand, Sulphur, Graphite, Talc, Soapstone, Mica, Infusorial Earth, Barytes, Fuller's Earth, Magnesite, Salt, Saltpetre, Diamonds, Asphaltum, Gypsum)

254-261
Ore Deposits . . . . . . 261-263
Occurrence of other Valuable Minerals . . . 263-264

# Ore Dressing. 

## Mechanical Drawing.

Hints; Colours ; Survey Scales; To divide a given line into two equal parts; To divide a given line into any number of equal parts; To divide a given line into two parts which shall have a given proportion to one another; To draw an Ellipse; Copying Drawings (Tracing, Blue Prints, Willis's Platinotype Process) 299-302

## Photography.

> Hints; Pyro solution; Restrainer ; Accelerator; Alum Bath; Fixing Bath; Clearing Bath; Frilling; Fogging; Flatness of Image; Pinholes; Printing; Toning Bath ; Mounting Solution . : . 302-306

Toxicology.
Poisons-Antidotes and Remedies . . . . 306-309
Solders and Fluxes for Soldering . . . . . 310

GLOSSARY OF TERMS . . . . . 311-358

INDEX . . . . . . . . . 359

## POCKET BOOK

## MINERS AND IETALLURGISTS.

## ARITHMETIC.

## Fractions.

Addition of Vulgar Fractions.-

$$
\frac{1}{2}+\frac{1}{2}=\frac{2}{2}=1 \quad \frac{9}{8}+\frac{3}{8}=\frac{9}{8}=1 \frac{1}{8} \quad \frac{3}{7}+\frac{2}{3}=\frac{2+14}{21}=\frac{23}{21}=1 \frac{2}{21}
$$

Subtraction of Vulgar Fractions.-
$\frac{1}{2}-\frac{1}{2}=0 \quad \frac{6}{8}-\frac{2}{8}=\frac{4}{8}=\frac{1}{2} \quad 3 \frac{4}{7}-1 \frac{2}{3}=\frac{25}{7}-\frac{5}{3}=7 \frac{5-35}{21}=\frac{40}{21}=1 \frac{12}{21}$
Mrultiplication of Vulgar Fractions.-

$$
\frac{1}{2} \times \frac{1}{2}=\frac{1}{4} \quad \frac{4}{5} \times \frac{2}{3}=\frac{8}{15} \quad \frac{2}{3} \times \frac{3}{7} \times \frac{1}{2}=\frac{6}{42}=\frac{1}{7}
$$

Division of Vulgar Fractions.-

$$
\frac{1}{2} \div \frac{1}{2}=\frac{2}{2}=1 \quad \frac{4}{5} \div \frac{2}{3}=\frac{12}{10}=\frac{0}{5}=1 \frac{1}{5}
$$

To find the greatest common divisor of a Vulgar Fraction.Thus $\frac{70}{176}$

$$
\begin{gathered}
70) 175(2 \\
140 \\
\hline 35) 70(2 \\
\frac{70}{\cdots}
\end{gathered}
$$

Ans. 35

To reduce a Vulgar Fraction to its lowest terms.-Find the gratest common divisor and divide both the numerator and denominator by it.

Thus $\frac{70}{175}$, whose greatcst common divisor as above is $35=\frac{2}{5}$. - To reduce a Vulgar Fraction to a decimal furm.-Divide the numerator by the denominator.

Thus $\frac{8}{25}$
25) $8 \cdot 0(\cdot 32$

$$
\begin{aligned}
& \frac{75}{50} \\
& \frac{50}{7}
\end{aligned}
$$

Ans. 32
$E x$.-Reduce 3 inches to the decimal of 1 foot, i.e., 12 inches The question is therefore reduce $\frac{3}{12}$ to a decimal as above.

Ex.-Hew many feet are there in • 75 of a yard?

$$
\cdot 75
$$

3 feet in a yard
Feet $\overline{2 \cdot 25}$
12 inches in a foot
In. $\overline{3 \cdot 00}$
Ans. 2 ft . 3 ins.

| Add together | -27 | $\cdot 439$ | $\cdot 073$ |
| :---: | :---: | :---: | :---: |
|  |  | $\stackrel{\cdot 27}{\cdot 439}$ |  |
|  |  | -073 |  |
|  |  | -01 |  |
|  |  | $\overline{792}$ |  |

Subtract $\cdot 23$ from $\cdot 94$; also $\cdot 0001$ from 1•3.
$\begin{array}{r}\cdot 94 \\ \cdot .93 \\ -71 \\ \hline\end{array}$
Multiply $\cdot 734$ by $1 \cdot 02$.

| $\cdot 734$ |
| ---: |
| $1 \cdot 02$ |
| 1468 |
| 734 |
| 74868 |

Divide 14357 by 07 .
7) $1435 \cdot 7(205 \cdot 1$

14
35
35
7
7

Evolution or Extraction of Roots.
Square root expressed thus, $\sqrt{36}=6$.
Rule.-Separate the given number inti periods of two figures each, by placing a point over the units figure, then over every second towards the left in whole numbers, and
over every second figure towards the right in decimals, and proceed thus-

| $\sqrt{5329} ;$ | $\text { 143) } \begin{aligned} & 5329(73 \\ & \frac{49}{429} \\ & \frac{429}{\cdots} \end{aligned}$ |
| :---: | :---: |
| $\sqrt{7.3441} ;$ | $7 \cdot 3441(2 \cdot 71$ |
|  | $\text { 47) } \begin{aligned} & 329 \\ & 329 \end{aligned}$ |
|  | $541)^{\frac{5}{5} 41} \begin{aligned} & 541 \\ & 541 \end{aligned}$ |

Note.-For square and cube roots see Tables. Fourth, fifth roots, \&c., are best done by logarithms.

## ALGEBRA.

## Powers, Roots.

$$
\begin{aligned}
& a^{m} \cdot a^{n}=a^{m+n} ;(a \cdot \bar{b})^{n}=a^{n} \cdot b^{n} ; a^{m} \div a^{n}=a^{m-n} ; a^{-n}=\frac{1}{a^{n}} ; \\
& \left(a^{n}\right)^{m}=a^{n \cdot m} ;\left(\frac{a}{b}\right)^{m}=\frac{a^{m}}{3^{m-2}} ; a^{-m} \cdot a^{n}=a^{-m+n} ;\left(a^{m}\right)^{-n}=a^{-m \cdot s} ; \\
& \frac{a^{2}-b^{2}}{a-b}=a+b ; \frac{a^{2}-b^{2}}{a+b}=a-b ;(a+b)(a-b)=a^{2}-b^{2} ; a^{0}=1 ;
\end{aligned}
$$

$$
(\sqrt[n]{\cdot \imath})^{n}=\sqrt[n]{a^{n}}=a ; \sqrt[n]{a \cdot b}=\sqrt[n]{a} \cdot \sqrt[n]{b} ; \sqrt[n]{\frac{a}{b}}=\sqrt[n]{a} ; \sqrt[n]{a^{m}}=a^{\frac{m}{n}} ;
$$

$$
\sqrt{u^{\prime n}}=\sqrt[n]{\overline{a^{n \cdot r}}} ; \sqrt[n]{\sqrt[n]{a}}=\sqrt[n \cdot m]{a}
$$

## Equations.

1st degree with one unknown quantity $a x+b=0 \ldots x=-\frac{b}{a}$; 1st degree with two unknown quantities $\left\{\begin{array}{l}a x+b y=c \\ a_{1} x+b_{1} y=c_{2}\end{array}\right\} \cdots$

$$
\left\{\begin{array}{l}
x=\frac{b_{1} c-b c_{1}}{a b_{1}-a_{1} b} \\
y=\frac{a c_{1}-a_{1} c}{a b_{1}-a_{1} b}
\end{array}\right.
$$

2nd degree, common form, $a x^{2}+b x+c=0 \quad x=\frac{-b \pm \sqrt{1^{2}-4 a c}}{2 a}$ 2nd degree, normal form, $x^{2}+p x+q=0 \quad x=-\frac{p}{2} \pm \sqrt{\frac{p^{2}}{4}-q}$; 3rd degree, $\mathrm{A} x^{3}+\mathrm{B} x^{2}+\mathrm{C} x+\mathrm{D}=0 \quad . \quad . x^{3}+a x^{2}+b x+c=0$

## TRIGONOMETRY.



$$
\begin{array}{ll}
\sin \alpha=\frac{y}{r} & \cos \alpha=\frac{x}{r} \\
\tan \alpha=\frac{y}{x} & \cot \alpha=\frac{x}{y} \\
\sec \alpha=\frac{r}{x} & \operatorname{cosec} x=\frac{r}{y}
\end{array}
$$

Between $0^{\circ}$ and $90^{\circ}$ the $\sin$ is $+\cos +\tan +\cot +$

$$
\begin{array}{rrrrr}
" & 90^{\circ} & 180^{\circ} & " & +, "-"-"- \\
" & 180^{\circ} & 270^{\circ} & " & -"-"+"+ \\
" & 270^{\circ} & " & 360^{\circ} & " \\
-, "+ & -,-
\end{array}
$$

Formulæ.
$\sin \alpha=\sin (180-\alpha)=-\sin (180+\alpha)=-\sin (360-\alpha)=$ $\cos (90-\alpha)\left\{\begin{array}{l}=-1 \\ > \\ <+1 \\ =\end{array}\right\}$
$\cos \alpha=-\cos (180-\alpha)=-\cos (180+\alpha)=+\cos (350-\alpha)=$ $\sin (90-a)\left\{\begin{array}{l}=-1 \\ > \\ < \\ =+1\end{array}\right\}$
$\sin (-\alpha)=-\sin \alpha$;
$\cos (-\alpha)=+\cos \alpha$;
$\tan \alpha=\frac{\sin \alpha}{\cos \alpha}\left\{\begin{array}{c}-\infty \\ \text { to } \\ +\infty\end{array}\right\} ;$

$$
\cot \alpha=\frac{\cos a}{\sin \alpha}\left\{\begin{array}{c}
-\infty \\
\text { to } \\
+\infty
\end{array}\right\} ;
$$

$\tan \alpha \cdot \cot \alpha=1 ;$
$\sin ^{2} \alpha+\cos ^{2} \alpha=1 ; \quad \sin \alpha=\sqrt{1-\cos ^{2}} \alpha ; \quad \cos \alpha=\sqrt{1-\sin ^{2} \alpha}$;
$\sin 2 \alpha=2 \sin \alpha \cos \alpha ; \quad \cos 2 \alpha=\cos ^{2} \alpha-\sin ^{2} \alpha$; $\sin (\alpha \pm \beta)=\sin \alpha \cos \beta \pm \cos \alpha \sin \beta ; \quad \sec \alpha \cdot \cos \alpha=1$; $\cos (\alpha \pm \beta)=\cos \alpha \cos \beta$ 事部 $\alpha \sin \beta ; \quad \operatorname{cosec} \alpha \cdot \sin \alpha=1$; $\tan (\alpha \pm \beta)=\frac{\tan \alpha \pm \tan \beta}{1 \mp \tan \alpha \cdot \tan \beta} \quad \cot (\alpha \pm \beta)=\frac{\cot \alpha \cot \beta \mp 1}{\cot \alpha \pm \cot \beta} ;$
$\tan 2 \alpha=\frac{2 \tan \alpha}{1-\tan ^{2} \alpha}$;

$$
\begin{aligned}
& \sin \frac{1}{2} \alpha= \pm \sqrt{\frac{1-\cos \alpha}{2}} ; \\
& \cos \frac{1}{2} \alpha= \pm \sqrt{\frac{1+\cos \alpha}{2}} ;
\end{aligned}
$$

$\sin 2 \alpha+\sin 2 \beta=2 \sin (\alpha+\beta) \cos (\alpha-\beta)$;
$\sin 2 \alpha-\sin 2 \beta=2 \sin (\alpha-\beta) \cos (\alpha+\beta)$;
$\cos 2 \alpha+\cos 2 \beta=2 \cos (\alpha+\beta) \cos (\alpha-\beta)$;
$\cos 2 \alpha-\cos 2 \beta=-2 \sin (\alpha+\beta) \sin (\alpha-\beta) ;$
$\sin \alpha=\frac{\tan \alpha}{\sqrt{1+\tan ^{2} \alpha}}=\frac{1}{\sqrt{1+\cot ^{2} \alpha}}=\frac{1}{\operatorname{cosec} \alpha}$;
$\cos \alpha=\frac{1}{\sqrt{1+\tan ^{2} \alpha}}=\frac{\cot \alpha}{\sqrt{1+\cot ^{2} \alpha}}=\frac{1}{\sec \alpha}$
In the oblique angled triangle, $\mathrm{A}, \mathrm{B}, \mathrm{C}$ -
(1) $\frac{a}{\sin \mathrm{~A}}=\frac{b}{\sin \mathrm{~B}}=\frac{c}{\sin \mathrm{C}}$.
(2) $a^{2}=b^{2}+c^{2}-2 b c \cos \mathrm{~A}$.
(3) $\tan \frac{A}{2}=\sqrt{\frac{(a+b-c)(a+c-b)}{(a+b+c)(b+c-a)}}$.
(4) $\frac{a+b}{a-b}=\frac{\tan \frac{A+B}{2}}{\tan \frac{A-B}{2}}$

(5) Area of the triangle, $\mathrm{A}, \mathrm{B}, \mathrm{C}=\frac{b \pi}{2}=\frac{a b \sin \mathrm{C}}{2}=$ $\frac{c^{2} \sin \mathrm{~B} \sin \mathrm{~A}}{2 \sin \mathrm{C}}=\sqrt{s(s-a)(s-b)(s-c)}$
where $l=$ height
$s=$ sum of the sides divided by 2.

## Examples

## Given.

1. One side and two adjacent angles

$$
a, \mathrm{~B}, \mathrm{C}
$$

Required.
$b$ and $c$ by equation (1)
$A=180-(B+C)$
Area from equation (5)

| Given. | Required. |
| :---: | :---: |
| 2. One side, one adjacent and one opposite angle $a, \mathrm{~B}, \mathrm{~A}$ | $\begin{aligned} & b \text { and } c \text { by equation (1) } \\ & C=180-(A+B) \\ & \text { area from equation (5) } \end{aligned}$ |
| 3. Three sides $a, b, c$ | Two angles by (2) or (3) When the third will be 180 the other two area by (5) |
| 4. Two sides and the included angle $b, c, A$ | $\begin{gathered} \mathrm{B}=\frac{\mathrm{B}+\mathrm{C}}{2}+\frac{\mathrm{B}-\mathrm{C}}{2} \\ \mathrm{C}=\frac{\mathrm{B}+\mathrm{C}}{2}-\frac{\mathrm{B}-\mathrm{C}}{2} \\ \frac{\mathrm{~B}+\mathrm{C}}{2}=\frac{180-\mathrm{A}}{2} ; \\ \frac{\mathrm{B}-\mathrm{C}}{2} \text { from } \end{gathered}$ <br> A from equation (1) area <br> (5) |
| 5. Two sides and the angle opposite the greater side $b, c, \mathrm{~B}$ | By equation (4) |

## MENSURATION.

$s=$ side ; $b=$ base ; $h=$ height ; $d=$ diameter ; $r=$ radius; $c=$ circumference; $a=$ area $; \mathrm{V}=$ volume $; \pi=3.1416 ; e=$ length of arc ; $o=$ chord ; $\alpha=$ central angle.

Triangles.- $a=\frac{1}{2} b \times h$;
Squares.- $a=s^{2}$;
Parallelograms.- $a=b \times h$;
Trapezoids. $-a=\frac{\text { the two parallel } s \times h}{2}$;
Trapeiums. $-a=$ divide into triangles and add their areas together.

Polygons.- $a=s \times h$ (from centre of figure to centre of side) $x$ half the number of sides.
Circles. $-a=\pi r^{2}=\pi \frac{d^{2}}{4} ; \quad c=2 \pi r=d \pi . \quad d=\frac{c}{\pi}=\frac{c \times 7}{22}$.

To find the diameter of a circle equal in area to a given square, multiply one side of the square by $1 \cdot 12838$.

To find the side of a square equal in area to a given circle, multiply the diameter by 0.88623 .

Sectors. $-a=\frac{e \times r}{2}=\frac{a}{360} \pi r^{2}=\frac{a}{360} \pi \frac{d^{2}}{4} ;$

$$
e=\frac{a}{360} \pi 2 r=\frac{a}{360} \pi d ;
$$

Segments. $-a=\left(\frac{a}{360} 2 \pi-\sin \alpha\right) \frac{r^{2}}{2} ;$
For flat segments $a=$ about $\frac{2}{3} o \hbar ; e=0\left(1+\frac{h}{3 r}\right)$.
Circular rings.- $a=$ area of the smaller circle subtracted from the area of the greater.

Ellipse. $-a=$ product of diameters $\times 0.78$. 4 .
Parabola.- $a=\frac{2}{3} b \times h$.
Cubes.- $\mathrm{V}=s^{3}$.
Prisms.-V $=$ area of base $\times h$.
Pyramids.-V $=\frac{\text { area of base } \times h}{3}$.
Prismoids.-Add together the areas of the two parallel surfaces, and four times the area of the section taken halfway between them and parallel to them : multiply the sum by the perpendicular distance between the two parallel sides, and divide the product by 6 .

Wedges. $-\mathrm{V}=$ (length of edge $+2 s$ parallel to the edge) $h \times s$ at right angles to edge.

6
Cylinders.- $\mathrm{V}=\pi r^{2} h$;
Cones.-V $=\frac{\text { area of base } \times \pi}{3}$.
To find the surface of any regular cone, multiply the circumference of its base by the slant height; take half the product.

Sphere. $-\mathrm{V}=0,5236 d^{3}=4 \cdot 1888 r^{3}=\frac{4}{3} \pi r^{3}=\frac{1}{6} \pi d^{3} . \quad$ Surface $=\pi l^{2}$ $=3 \cdot 1416 d^{2}=4 \pi r^{2}=12 \cdot 5664 r^{2}$.

Spherical segment.-Volume=square of the radius of its base multiplied by 3 , add to the product the square of its height, multiply the sum by the height, and multiply this last product by 0.5236 .

Cylindrical rings. - Volume $=$ area of cross section of bar of which ring is made $\times \frac{1}{2}$ sum of inner and outer diameters $x$ $3 \cdot 141593$. Surface $=$ circumference of bar of which ring is made $\times \frac{1}{2}$ sum of inner and outer diameters $\times 3 \cdot 141593$.

Paraboloid.- $\mathrm{V}=\frac{1}{2} \pi r^{2} \%$

## TABLES.

## TABLES.

Table of Logarithms of Numbers from 10 to 1200.
The index of the logarithm of a number greater than unity is one less than the number of figures in the integral part of that number.

The index of the logarithm of a number less than unity is negative, and is a higher number by one than the number of zeros that follow the decimal point.

Example.-1892 is $3: 18.92$ is $1: 0.1892$ is $\overline{1} ; 0.001892$ is $\overline{3}$.

| Nr . | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | Diff. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | 00000 | 00432 | 00860 | 01284 | 01703 | 02119 | 02531 | 02938 | 03342 | 03743 | 396 |
| 11 | 04139 | 04532 | 04922 | 05308 | 05690 | 06070 | 06446 | 06819 | 07188 | 07555 | 363 |
| 12 | 07918 | 08279 | 08636 | 08991 | 09342 | 09691 | 10037 | 10380 | 10721 | 11059 | 335 |
| 13 | 11394 | 11727 | 12057 | 12385 | 12710 | 13033 | 13354 | 13672 | 13988 | 14301 | 312 |
| 14 | 14613 | 14922 | 15229 | 15534 | 15836 | 16137 | 16435 | 16732 | 17026. | 17319 | 290 |
| 15 | 17609 | 17898 | 18184 | 18469 | 18752 | 19033 | 19312 | 19590 | 1986 | 20140 | 272 |
| 16 | 20412 | 20683 | 20952 | 21219 | 21484 | 21748 | 22011 | 22272 | 22531 | 22789 | 256 |
| 17 | 23045 | 23300 | 23553 | 23805 | 24055 | 24304 | 24551 | 24797 | 25042 | 25285 | 242 |
| 18 | 25527 | 25768 | 26007 | 26245 | 26482 | 26717 | 26951 | $\mid 27184$ | 27416 | 27646 | 229 |
| 19 | 27875 | 28103 | 28330 | 28556 | 23780 | 29003 | 29226 | 29447 | 2966 | 29885 | 218 |
| 20 | 30103 | 30320 | 30535 | 30750 | 30963 | 31175 | 31387 | 31597 | 3180 | 32015 | 207 |
| 21 | 32222 | 32428 | 32634 | 32838 | 33041 | 33244 | 33445 | 33645 | 3384 | 34044 | 198 |
| 22 | 34242 | 34439 | 34635 | 34830 | 35025 | 35218 | 35411 | 35603 | 3579 | 35984 | 189 |
| 23 | 36173 | 36361 | 36549 | 36736 | 36922 | 37107 | 37291 | 37475 | 3765 | 37840 | 181 |
| 24 | 38021 | 38202 | 38382 | 38561 | \|38739 | 38917 | 39094 | 39270 | 3944 | 39620 | 174 |
| 25 | 39794 | 39967 | 40140 | 40312 | 40483 | 40654 | 40824 | 40993 | 4116 | 41330 | 167 |
| 26 | 41497 | 41664 | 41830 | 41996 | 42160 | 42325 | 42488 | 42651 | 42813 | 42975 | 161 |
| 27 | 43136 | 43297 | 43457 | 4361 ' | 43775 | 43933 | 44091 | 44248 | 4440 | 44560 | 155 |
| 23 | 44716 | 44871 | 4502.5 | 45179 | 45332 | 45484 | 45537 | '45788' | 45939 | 46090 | 150 |
| 23 | 46240 | 46389 | 46538 | 46687 | 46835 | 46982 | 47129 | -47276 | 47422 | 47567 | 145 |
| 3) | 47712 | 47857 | 48001 | 48144 | 48287 | 48430 | 48572 | 48714 | 48855 | 48996 | 140 |
| 31 | 49136 | 49276 | 49415 | 49554 | 49693 | 498:31 | 49969 | 50106 | 50243 | 50379 | 136 |
| 32 | 50515 | 50651 | 50786 | 50920 | 51055 | 51188 | 51322 | 51455 | 51587 | 51720 | 132 |
| 33 | 51851 | 51983 | 52114 | 52344 | 5237 | 52504 | 52634 | 52763 | 52892 | $530 \%$ | 128 |
| 34 | 53148 | 53275 | 53403 | 53529 | 53656 | 53782 | 53908 | 54033 | 5415 | 54283 | 124 |
| 35 | 54407 | 54531 | 54654 | 54777 | 54900 | 55023 | 55145 | 55267 | 5538 | 55509 | 121 |
| 36 | 55630 | 55751 | 55871 | 55991 | 56110 | 56229 | 56348 | 56467 | 56585 | 56703 | 117 |
| 37 | 56820 | 56937 | 57054 | 57171 | 57287 | 57403 | 57519 | 57634 | 57749 | 57864 | 114 |
| 33 | 57978 | 58092 | 58206 | 58320 | 58433 | 58546 | 58659 | 58771 | 58883 | 58995 | 111 |
| 39 | 59106 | 59:218 | 59329 | 59439 | 59550 | 59660 | 59770 | 59879 | 59988 | 60097 | 109 |
| 40 | 60206 | 60314 | 60423 | 60531 | 60638 | 60746 | 60853 | 60959 | 61066 | 61172 | 106 |
| 41 | 61278 | 61384 | 61490 | 61595 | 61700 | 61805 | 61909 | 62014 | 62118 | . 62221 | 104 |
| 42 | 62325 | 62428 | 62531 | 62634 | 62737 | 62839 | 62941 | 63043 | 63144 | 63246 | 101 |
| 43 | 63347 | 63448 | 63548 | 63649 | 63749 | 63849 | 63949 | 64048 | 64147 | 64246 | 99 |
| 44 | 64345 | 64444 | 64542 | 64640 | 64738 | 64836 | 64933 | 65031 | 65128 | 65225 | 97 |
| 45 | 65321 | 65418 | 65514 | 65610 | 65706 | 65801 | 65896 | 65992 | 6 6,087 | 66181 | 95 |
| 46 | 66276 | 66370 | 66464 | 66558 | 66652 | 66745 | 66839 | 66932 | 67025 | 67117 | 93 |
| 47 | 67210 | 67302 | 67394 | 67486 | 67578 | 67669 | 67761 | 67852 | 67943 | 68034 | 90 |
| 48 | 68124 | 68215 | 68305 | 68395 | 68485 | 68574 | 68664 | 68753 | 68842 | 68931 | 89 |
| 49 | 69020 | 69108 | 69197 | 69285 | 69373 | 69461 | 69548 | 69636 | 69723 | 69810 | 87 |
| Nr. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | Uiff. |

Table of Logarithms of Numbers (continued).

| N | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | Diff. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5 | 69897 | 69984 | 70070 | 70157 | 70243 | 70329 | 70415 | 70501 | 70586 | 70672 | 86 |
| 51 | 70757 | 70842 | 70927 | 71012 | 71096 | 71181 | 71265 | 71349 | 71433 | 71517 | 84 |
| 52 | 71600 | 71684 | 71767 | 71850 | 71933 | 72016 | 72099 | 72181 | 72263 | 72346 | 83 |
| 53 | 72428 | 72509 | 72591 | 72673 | 72754 | 72835 | 72916 | 72997 | 73078 | 73159 | 81 |
| 54 | 73239 | 73320 | 73400 | 73480 | 73560 | 73640 | 73719 | 73799 | 73878 | 73957 | 0 |
| 55 | 74036 | 74115 | 74194 | 74273 | 74351 | 74429 | 74507 | 74586 | 74663 | 74741 | 8 |
| 56 | 74819 | 74896 | 74974 | 75051 | 75128 | 75205 | 75282 | 75358 | 75435 | 75511 | 77 |
| 57 | 75587 | 75664 | 75740 | 75815 | 75891 | 75967 | 76042 | 76118 | 76193 | 76268 | 76 |
| 58 | 76343 | 76418 | 76492 | 76567 | 76641 | 76716 | 76790 | 76864 | 76938 | 77012 | 74 |
| 59 | 77085 | 77159 | 77232 | 77305 | 77379 | 77452 | 77525 | 77597 | 77670 | 77743 | 73 |
| 60 | 77815 | 77887 | 77960 | 78032 | 78104 | 78176 | 78247 | 78319 | 78390 | 78462 | 72 |
| 61 | 78533 | 78604 | 78675 | 78746 | 78817 | 78888 | 78958 | 79029 | 79099 | 79169 | 71 |
| 62 | 79239 | 79309 | 79379 | 79449 | 79518 | 79588 | 79657 | 79727 | 79796 | 79865 | 69 |
| 63 | 79934 | 80003 | 80072 | 80140 | 80209 | 80277 | 80346 | 80414 | 80482 | 80550 | 68 |
| 64 | 80618 | 80686 | 80754 | 80821 | 80889 | 80956 | 81023 | 81090 | 81158 | 81224 | 67 |
| 6 | 81291 | 81358 | 81425 | 81491 | 81558 | 81624 | 81690 | 81757 | 81823 | 81889 | 66 |
| 6 | 81954 | 82020 | 82086 | 82151 | 82217 | 82282 | 82347 | 82413 | 82478 | 82543 | 65 |
| 67 | 82607 | 82672 | 82737 | 82802 | 82866 | 82930 | 82995 | 83059 | 83123 | 83187 | 64 |
| 68 | 83251 | 83315 | 83378 | 83442 | 83506 | 83569 | 83632 | 83696 | 83759 | 83822 | 63 |
| 69 | 83885 | 83948 | 84011 | 84073 | 84136 | 84198 | 84261 | 84323 | 84386 | 84448 | 63 |
| 70 | 84510 | 84572 | 84634 | S4696 | 84757 | S4819 | 84880 | 84942 | 85003 | 85065 | 62 |
| 7 | 85126 | 85187 | 85248 | 85309 | 85370 | 85431 | 85491 | 85552 | 85612 | 85673 | 61 |
| 72 | 85733 | 85794 | 85854 | 85914 | 85974 | 86034 | 86094 | 86153 | 86213 | 86273 | 60 |
| 73 | 86332 | 86392 | 86451 | 86510 | 86570 | 86629 | 86688 | 86747 | 86806 | 86864 | 59 |
| 74 | 86923 | 86982 | S7040 | 87099 | 87157 | 87216 | 87274 | 87332 | 87390 | 87448 | 58 |
| 75 | 87506 | 87564 | 87622 | 87679 | 87737 | 87795 | 87852 | 87910 | 87967 | 88024 | 58 |
| 76 | 88081 | 88138 | 88195 | 88252 | 88309 | 88366 | 88493 | 88480 | 8S5536 | 88503 | 57 |
| 7 | 88649 | 88705 | 88762 | 88818 | 88874 | 88930 | 88.986 | 89042 | 89098 | 89154 | 56 |
| 78 | 89209 | 89265 | 89321 | 89376 | 89432 | 89487 | 89542 | S9597 | 89653 | 89708 | 55 |
| 79 | 89763 | 89818 | 89873 | 89927 | 89982 | 90037 | 90091 | 90146 | 90200 | 90255 | 55 |
| 80 | 90309 | 90363 | 90417 | 90472 | 90526 | 90580 | 90634 | 90687 | 90741 | 90795 | 54 |
| 81 | 90849 | 90902 | 90956 | 91009 | 91062 | 91116 | 91169 | 91222 | 91275 | 91328 | 53 |
| 82 | 91381 | 91434 | 91487 | 91540 | 91593 | 91645 | 91698 | 91751 | 91803 | 91855 | 52 |
|  | 91908 | 91960 | 92012 | 92065 | 92117 | 92169 | 92221 | 92273 | 92324 | 92376 | 52 |
| 84 | 92428 | 9248 | 92531 | 92583 | 92634 | 92686 | 92737 | ©2788 | 92840 | 92891 | 51 |
| 85 | 92942 | 92993 | 93044 | 93095 | 93146 | 93197 | 93247 | 93298 | 93349 | 93399 | 51 |
| 86 | 93450 | 93500 | 93551 | 93601 | 93651 | 93702 | 93752 | 93802 | 93852 | 93902 | 50 |
| 87 | 93952 | 94002 | 94052 | 94101 | 94151 | 94201 | 94250 | 94300 | 94349 | 94399 | 50 |
| 88 | 94448 | 94498 | 94547 | 94596 | 94645 | 94694 | 94743 | 94792 | 94841 | 94 ¢90 | 49 |
| 89 | 94939 | 94988 | 95036 | 95085 | 95134 | 95182 | 95231 | 95279 | 95328 | 95376 | 49 |
| 90 | 95424 | 95472 | 95521 | 95569 | 95617 | 95665 | 95713 | 95761 | 95809 | 95856 | 48 |
| 91 | 95904 | 95952 | 95999 | 96047 | 96095 | 96142 | 96190 | 96237 | 96284 | 96332 | 47 |
| 92 | 96379 | 96426 | 96473 | 96520 | 96567 | 96614 | 96661 | 96708 | 96755 | 96802 | 47 |
| 93 | 96848 | 96895 | 96942 | 96988 | 97035 | 97081 | 97128 | 97174 | 97220 | 97267 | 46 |
| 94 | 97313 | 97359 | 97405 | 97451 | 97497 | 97543 | 97589 | 97635 | 97681 | 97727 | 46 |
| 95 | 97772 | 97818 | 97864 | 97909 | 97955 | 98000 | 98046 | 98091 | 98137 | 98182 | 45 |
| 96 | 95227 | 98272 | 98318 | 98363 | 98408 | 98453 | 98498 | 98543 | 98588 | 98632 | 45 |
| 97 | 98677 | 98722 | 98767 | 95811 | 98856 | 98900 | 98945 | 98989 | 09034 | 99078 | 45 |
| 98 | 99123 | 99167 | 99211 | 99255 | 99300 | 99344 | 99388 | 99432 | 99476 | 99520 | 44 |
| 99 | 99564 | 99607 | 99651 | 99695 | 99739 | 99782 | 99826 | 99870 | 99913 | 99957 | 44 |
| 100 | 00000 | 00043 | 00087 | 00130 | 00173 | 00217 | 00260 | 00303 | 00346 | 003S9 | 43 |
| Nr. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | Diff. |

Table of Logarithms of Numbers (contimed).

| Nr. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | Di |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 101 | 00432 | 00475 | 00518 | 00561 | 00604 | 00647 | 00689 | 00732 | 00775 | 00817 | 43 |
| 102 | 00860 | 00903 | 00945 | 00988 | 01030 | 01072 | 01115 | 01157 | 01199 | 01242 | 42 |
| 103 | 01284 | 01326 | 01368 | 01410 | 01452 | 01494 | 01536 | 01578 | 01620 | 01662 | 42 |
| 104 | 01703 | 01745 | 01787 | 01828 | 01870 | 01912 | 01953 | 01995 | 02036 | 02078 | 42 |
| 105 | 02119 | 02160 | 02202 | 02243 | 02284 | 02325 | 02366 | 02407 | 02449 | 02490 |  |
| 106 | 02531 | 02572 | 02612 | 02653 | 02694 | 02735 | 02776 | 02816 | 02857 | 02898 | 41 |
| 107 | 02938 | 02979 | 03019 | 03060 | 03100 | 03141 | 03181 | 03222 | 03262 | 03302 | 41 |
| 108 | 03342 | 03383 | 03423 | 03463 | 03503 | 03543 | 03583 | 03623 | 03663 | 03703 | 40 |
| 110 | 03743 | 03782 | 03822 | 03862 | 03902 | 03941 | 03981 | 04021 | 04060 | 04100 | 40 |
| 110 | 04139 | 04179 | 04218 | . 04258 | 04297 | 04336 | 04376 | 04415 | 04454 | 04493 | 39 |
| 111 | 04532 | 04571 | 04610 | 04550 | 04689 | 04727 | 04766 | 04805 | 04844 | 04883 |  |
| 112 | 04922 | 04961 | 04999 | 05038 | 05077 | 05115 | 05154 | 05192 | 05231 | 05269 | 39 |
| 113 | 05308 | 05346 | 05385 | 05423 | 05461 |  | 05538 | 05576 |  | 05652 |  |
| 114 | ${ }^{05690}$ | ${ }_{06108}^{05729}$ | ${ }_{06145}^{05767}$ | 05805 | 05843 | ${ }^{05881}$ | 05918 | ${ }_{0}^{05953}$ | 05994 | ${ }^{06032}$ | ${ }_{38} 38$ |
| 116 | 06446 | 06483 | 06521 | 06558 | 06595 | 06633 | 06670 | 06707 | 06744 | 06781 | 37 |
| 117 | 06819 | 06856 | 06893 | 06930 | 06967 | 07004 | 07041 | 07078 | 07115 | 07151 | 37 |
| 118 | 07188 | 07225 | 07262 | 07298 | 07335 | 07372 | 07408 | 07445 | 07482 | 07518 |  |
| 119 | 07555 | 07591 | 07628 | 07664 | 07700 | 07737 | 07773 | 07809 | 07846 | 07882 | 36 |
| Nr. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |  |  |

Examples:

Find log. of 5065

$$
\text { Log. of } 5060=3 \cdot 70415
$$

Prop. diff. $86 \times 5=$
Log. required

Find number of log. $3 \cdot 771442$
Log. of $5900=3 \cdot 770850$
592
Prop. diff. 73
$\frac{593}{73}=8 \quad \therefore$ number is 5900 5908

To multiply by logarithms, add the logarithms together and find the corresponding number.

To divide by logarithms, subtract one from the other and find the corresponding number.

To extract the root, divide the logarithm by the index of the root and find the corresponding number.

To raise a number to any power, multiply the logarithm by the index of the power and find the corresponding number.

The Hyperbolic or Napierian logarithm is the common logarithm of the Table multiplied by 2.3025851 .

Table of Powers (Root, Circumference, Area, Square, Cube, Square Root, and Cube Root).

To find the $\sqrt{n}$ of a number which is wholly decimal. If the number is not separable into twos, add another cipher to make it so. Then begin at the first numerical figure, and including it assume the number to be a whole one. In the table find the number nearest the assumed one, take out its tabular square root, move the decimal point of this tabular root to the left half as many places as the finally modified decimal number has figures. Example. $-\sqrt{\cdot 002 ?}$ 1).002 2) $\cdot 00 \cdot 20$; 3) $\sqrt{20}=4 \cdot 47$; 4) move decimal point two places: -0447 ans. This rule is good up to three numerals inclusire.

To find the $\sqrt[3]{n}$ of a number which is wholly decimal. Proceed as in the former case for $\sqrt{n}$, only divide the figures into threes and point off to the left $\frac{1}{3}$ as many places as the finally modified decimal number has figures. Example.$\sqrt[3]{\cdot 0 \Theta 2}$ ? 1) $\cdot 002$; 2) $\sqrt[3]{2}=1 \cdot 26 ; 3) \cdot 126$ ans.

To find the square or cube of any whole number ending with ciphers, 1) omit all the final ciphers ; 2) take from the table the square or cube (as the case may be) of the rest of the number ; 3) to this square add twice as many ciphers as there were final ciphers in the original number. To the cube add three times as many as the original number. Example.$28,000^{2}$ ? 1) $28^{2}=784$; 2) add six ciphers : $784,000,000$ ans. Example.- $28,000^{3}$ ? 1) $28^{3}=21,952$; 2) add nine ciphers : $21,952,000,000,000$ ans.

| $n$ | $n \pi$ | $n^{2} \frac{\pi}{4}$ | $n^{2}$ | $n^{3}$ | $\sqrt{n}$ | $\sqrt[3]{n}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $1 \cdot 0$ | $3 \cdot 142$ | $0 \cdot 7854$ | $1 \cdot 000$ | $1 \cdot 000$ | $1 \cdot 0000$ | $1 \cdot 0000$ |
| $1 \cdot 1$ | $3 \cdot 456$ | $0 \cdot 9503$ | $1 \cdot 210$ | $1 \cdot 331$ | $1 \cdot 0488$ | $1 \cdot 0323$ |
| $1 \cdot 2$ | $3 \cdot 770$ | 1•1310 | $1 \cdot 440$ | $1 \cdot 728$ | 1.0955 | $1 \cdot 0627$ |
| $1 \cdot 3$ | $4 \cdot 084$ | $1 \cdot 3273$ | $1 \cdot 690$ | $2 \cdot 197$ | $1 \cdot 1402$ | $1 \cdot \mathrm{C} 914$ |
| $1 \cdot 4$ | $4 \cdot 398$ | 1•5394 | 1.960 | $2 \cdot 744$ | 1-1832 | $1 \cdot 1187$ |
| 1.5 | $4 \cdot 712$ | $1 \cdot 7672$ | $2 \cdot 250$ | $3 \cdot 375$ | 1-2247. | $1 \cdot 1447$ |
| $1 \cdot 6$ | $5 \cdot 027$ | $2 \cdot 0106$ | $2 \cdot 560$ | $4 \cdot 096$ | $1 \cdot 2649$ | $1 \cdot 1696$ |
| 1.7 | $5 \cdot 341$ | 2.2698 | $2 \cdot 890$ | $4 \cdot 913$ | $1 \cdot 3038$ | $1 \cdot 1935$ |
| $1 \cdot 8$ | 5.655 | $2 \cdot 5447$ | $3 \cdot 240$ | $5 \cdot 832$ | $1 \cdot 3416$ | $1 \cdot 2164$ |
| $1 \cdot 9$ | 5.969 | $2 \cdot 8353$ | $3 \cdot 610$ | $6 \cdot 859$ | $1 \cdot 3784$ | $1 \cdot 2386$ |
| $2 \cdot 0$ | 6.283 | $3 \cdot 1416$ | $4 \cdot 000$ | $8 \cdot 000$ | $1 \cdot 4142$ | $1 \cdot 2599$ |
| $2 \cdot 1$ | $6 \cdot 597$ | $3 \cdot 4636$ | $4 \cdot 410$ | 9•261 | $1 \cdot 4491$ | $1 \cdot 2806$ |

Table of Powers (continued).

| $n$ | $n \pi$ | $n^{2} \frac{\pi}{4}$ | $n^{2}$ | $n^{3}$ | $\sqrt{n}$ | $\sqrt[3]{n}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $2 \cdot 2$ | 6.912 | $3 \cdot 8013$ | $4 \cdot 840$ | 10.648 | $1 \cdot 4832$ | $1 \cdot 3006$ |
| $2 \cdot 3$ | $7 \cdot 226$ | $4 \cdot 1548$ | $5 \cdot 290$ | $12 \cdot 167$ | 1.5166 | $1 \cdot 3200$ |
| $2 \cdot 4$ | $7 \cdot 540$ | $4 \cdot 5239$ | $5 \cdot 760$ | $13 \cdot 824$ | 1.5492 | $1 \cdot 3389$ |
| 2.5 | $7 \cdot 854$ | $4 \cdot 9087$ | $6 \cdot 250$ | 15.625 | 1.5811 | $1 \cdot 3572$ |
| $2 \cdot 6$ | $8 \cdot 168$ | $5 \cdot 3093$ | 6.760 | 17:576 | $1 \cdot 6125$ | $1 \cdot 3751$ |
| $2 \cdot 7$ | $8 \cdot 482$ | $5 \cdot 7256$ | $7 \cdot 290$ | $19 \cdot 683$ | $1 \cdot 6432$ | 1-3925 |
| $2 \cdot 8$ | $8 \cdot 797$ | $6 \cdot 1575$ | $7 \cdot 840$ | 21.952 | $1 \cdot 6733$ | $1 \cdot 4095$ |
| $2 \cdot 9$ | $9 \cdot 111$ | $6 \cdot 6052$ | $8 \cdot 410$ | 24•389 | $1 \cdot 7029$ | $1 \cdot 4260$ |
| $3 \cdot 0$ | $9 \cdot 425$ | $7 \cdot 0686$ | $9 \cdot 00$ | $27 \cdot 000$ | 1.7321 | $1 \cdot 4422$ |
| $3 \cdot 1$ | 9.739 | $7 \cdot 5477$ | $9 \cdot 61$ | $29 \cdot 791$ | $1 \cdot 7607$ | $1 \cdot 4581$ |
| $3 \cdot 2$ | 10.053 | $8 \cdot 0425$ | $10 \cdot 24$ | 32.768 | $1 \cdot 7889$ | $1 \cdot 4736$ |
| $3 \cdot 3$ | $10 \cdot 367$ | $8 \cdot 5530$ | $10 \cdot 89$ | 35.937 | $1 \cdot 8166$ | $1 \cdot 4888$ |
| $3 \cdot 4$ | 10.681 | $9 \cdot 0792$ | $11 \cdot 56$ | $39 \cdot 304$ | $1 \cdot 8439$ | 1.5037 |
| 3\% | 10.996 | 9•6211 | $12 \cdot 25$ | $42 \cdot 875$ | $1 \cdot 8708$ | $1 \cdot 5183$ |
| $3 \cdot 6$ | $11 \cdot 310$ | $10 \cdot 179$ | 12.96 | $46 \cdot 656$ | $1 \cdot 8974$ | 1-5326 |
| $3 \cdot 7$ | $11 \cdot 624$ | 10.752 | $13 \cdot 69$ | 50.653 | $1 \cdot 9235$ | $1 \cdot 5467$ |
| $3 \cdot 8$ | 11.938 | $11 \cdot 341$ | 14.44 | $54 \cdot 872$ | $1 \cdot 9494$ | 1-5605 |
| $3 \cdot 9$ | $12 \cdot 252$ | 11.946 | 15.21 | $59 \cdot 319$ | $1 \cdot 9748$ | 1.5741 |
| $4 \cdot 0$ | 12.566 | $12 \cdot 566$ | 16.00 | $64 \cdot 000$ | $2 \cdot 0000$ | $1 \cdot 5874$ |
| $4 \cdot 1$ | $12 \cdot 881$ | $13 \cdot 203$ | 16.81 | 68.921 | $2 \cdot 0249$ | $1 \cdot 6005$ |
| $4 \cdot 2$ | $13 \cdot 195$ | $13 \cdot 854$ | $17 \cdot 64$ | $74 \cdot 088$ | $2 \cdot 0494$ | 1-6134 |
| $4 \cdot 3$ | 13:509 | 14:22 | $18 \cdot 49$ | $79 \cdot 507$ | $2 \cdot 0736$ | $1 \cdot 6261$ |
| $4 \cdot 4$ | 13.823 | 15.205 | $19 \cdot 36$ | $85 \cdot 184$ | $2 \cdot 0976$ | $1 \cdot 6386$ |
| $4 \%$ | $14 \cdot 137$ | 15.904 | 20.25 | 91.125 | $2 \cdot 1213$ | 1-6510 |
| $4 \cdot 6$ | $14 \cdot 451$ | 16.619 | $21 \cdot 16$ | $97 \cdot 336$ | $2 \cdot 1448$ | $1 \cdot 6631$ |
| $4 \cdot 7$ | 14.765 | $17 \cdot 349$ | 22.09 | 103.823 | $2 \cdot 1680$ | 1.6751 |
| $4 \cdot 8$ | $15 \cdot 080$ | $18 \cdot 096$ | $23 \cdot 04$ | 110.592 | $2 \cdot 1909$ | 1-6869 |
| $4 \cdot 9$ | 15•394 | $18 \cdot 857$ | 24.01 | $117 \cdot 649$ | $2 \cdot 2136$ | $1 \cdot 6985$ |
| 5.0 | 15.708 | $19 \cdot 6350$ | 25.00 | 125.000 | $2 \cdot 2361$ | $1 \cdot 7100$ |
| $5 \cdot 1$ | 16.022 | $20 \cdot 4282$ | 26.01 | $132 \cdot 651$ | $2 \cdot 2583$ | 1.7213 |
| $5 \cdot 2$ | $16 \cdot 336$ | $21 \cdot 2372$ | $27 \cdot 04$ | $140 \cdot 608$ | $2 \cdot 2804$ | $1 \cdot 7325$ |
| $5 \cdot 3$ | $16 \cdot 650$ | $22 \cdot 0618$ | 28.09 | 148.877 | $2 \cdot 3022$ | 1.7435 |
| 5.4 | 16.965 | $22 \cdot 9022$ | $29 \cdot 16$ | $157 \cdot 464$ | $2 \cdot 3238$ | $1 \cdot 7544$ |
| 5.5 | $17 \cdot 279$ | 23-7583 | 30.25 | 166.375 | $2 \cdot 3452$ | 1.7652 |
| 5.6 | 17-593 | $24 \cdot 6301$ | $31 \cdot 36$ | $175 \cdot 616$ | $2 \cdot 3664$ | $1 \cdot 7758$ |
| $5 \cdot 7$ | $17 \cdot 907$ | 25.5176 | $32 \cdot 49$ | $185 \cdot 193$ | $2 \cdot 387.5$ | $1 \cdot 7863$ |
| $5 \cdot 8$ | $18 \cdot 221$ | 26.4208 | $33 \cdot 64$ | $195 \cdot 112$ | $2 \cdot 4083$ | 1.7967 |
| $5 \cdot 9$ | 18.535 | $27 \cdot 3397$ | $34 \cdot 81$ | 205.379 | $2 \cdot 4290$ | $1 \cdot 8070$ |
| $6 \cdot 0$ | $18 \cdot 850$ | $28 \cdot 2743$ | 36.00 | 216.000 | $2 \cdot 4495$ | $1 \cdot 8171$ |
| $6 \cdot 1$ | $19 \cdot 164$ | $29 \cdot 2247$ | 37.21 | 226.981 | $2 \cdot 4698$ | $1 \cdot 8272$ |
| $6 \cdot 2$ | $19 \cdot 478$ | $30 \cdot 1907$ | $38 \cdot 44$ | 238.328 | $2 \cdot 4900$ | $1 \cdot 8371$ |

TABLE OF Powers (continued).

| $n$ | $n \pi$ | $n^{2} \frac{\pi}{4}$ | $n^{2}$ | $n^{3}$ | $\sqrt{n}$ | $\sqrt[3]{n}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $6 \cdot 3$ | $19 \cdot 792$ | 31-1725 | $39 \cdot 69$ | $250 \cdot 047$ | 2.5100 | $1 \cdot 8469$ |
| $6 \cdot 4$ | $20 \cdot 106$ | $32 \cdot 1699$ | $40 \cdot 96$ | $262 \cdot 144$ | $2 \cdot 5298$ | $1 \cdot 8.56$ |
| 6.5 | 20.420 | $33 \cdot 1831$ | $42 \cdot 25$ | $274 \cdot 62$ 5 | $2 \cdot 5495$ | $1 \cdot 8663$ |
| $6 \cdot 6$ | 20.73.) | $34 \cdot 2119$ | $43 \cdot 56$ | $287 \cdot 496$ | $2 \cdot 5690$ | $1 \cdot 8758$ |
| $6 \cdot 7$ | $21 \cdot 049$ | $35 \cdot 2565$ | $44 \cdot 89$ | $300 \cdot 763$ | $2 \cdot 5884$ | 1.8852 |
| $6 \cdot 8$ | $21 \cdot 363$ | $36 \cdot 3168$ | $46 \cdot 24$ | $314 \cdot 432$ | $2 \cdot 6077$ | $1 \cdot 8945$ |
| $6 \cdot 9$ | $21 \cdot 677$ | 37-3928 | $47 \cdot 61$ | $328 \cdot 509$ | $2 \cdot 6268$ | $1 \cdot 9038$ |
| $7 \cdot 0$ | 21.991 | $38 \cdot 4845$ | $49 \cdot 00$ | $343 \cdot 000$ | $2 \cdot 64.8$ | $1 \cdot 9129$ |
| $7 \cdot 1$ | $22 \cdot 305$ | $39 \cdot 5919$ | $50 \cdot 41$ | $357 \cdot 911$ | $2 \cdot 66 \frac{1}{2} 6$ | $1 \cdot 9220$ |
| $7 \cdot 2$ | 22.619 | $40 \cdot 7150$ | $51 \cdot 84$ | $373 \cdot 248$ | $2 \cdot 6833$ | $1 \cdot 9310$ |
| $7 \cdot 3$ | 22.934 | $41 \cdot 8539$ | $53 \cdot 29$ | $389 \cdot 017$ | $2 \cdot 7019$ | $1 \cdot 9399$ |
| $7 \cdot 4$ | $23 \cdot 248$ | $43 \cdot 0084$ | $54 \cdot 76$ | $405 \cdot 224$ | $2 \cdot 7203$ | $1 \cdot 9487$ |
| $7 \cdot 5$ | $23 \cdot 562$ | $44 \cdot 1786$ | $56 \cdot 25$ | $421 \cdot 875$ | $2 \cdot 7386$ | 1-9.574 |
| $7 \cdot 6$ | $23 \cdot 876$ | $45 \cdot 3646$ | $57 \cdot 76$ | $438 \cdot 976$ | 2.7568 | 1-9661 |
| $7 \cdot 7$ | $24 \cdot 190$ | $46 \cdot 5663$ | $59 \cdot 29$ | $456 \cdot 533$ | $2 \cdot 7749$ | $1 \cdot 9747$ |
| $7 \cdot 8$ | $24 \cdot 504$ | $47 \cdot 7836$ | $60 \cdot 84$ | $474 \cdot 552$ | $2 \cdot 7928$ | $1 \cdot 9832$ |
| $7 \cdot 9$ | $24 \cdot 819$ | $49 \cdot 0167$ | $62 \cdot 41$ | $493 \cdot 039$ | $2 \cdot 8107$ | $1 \cdot 9916$ |
| $8 \cdot 0$ | $25 \cdot 133$ | $50 \cdot 2605$ | $64 \cdot 00$ | $512 \cdot 000$ | $2 \cdot 8284$ | $2 \cdot 0000$ |
| $8 \cdot 1$ | $25 \cdot 447$ | 51.5300 | 65.61 | $531 \cdot 441$ | $2 \cdot 8461$ | $2 \cdot 0083$ |
| $8 \cdot 2$ | $25 \cdot 761$ | $52 \cdot 8102$ | $67 \cdot 24$ | $551 \cdot 368$ | $2 \cdot 8636$ | $2 \cdot 0165$ |
| $8 \cdot 3$ | $26 \cdot 075$ | $54 \cdot 1061$ | $68 \cdot 89$ | $571 \cdot 787$ | $2 \cdot 8810$ | $2 \cdot 0247$ |
| $8 \cdot 4$ | $26 \cdot 389$ | 5.54177 | 70.56 | $592 \cdot 704$ | $2 \cdot 8983$ | $2 \cdot 0328$ |
| $8 \cdot 5$ | $26 \cdot 704$ | 56.74 .50 | $72 \cdot 25$ | $614 \cdot 125$ | $2 \cdot 9155$ | $2 \cdot 0408$ |
| $8 \cdot 6$ | $27 \cdot 018$ | $58 \cdot 0880$ | $73 \cdot 96$ | $636 \cdot 056$ | $2 \cdot 9326$ | $2 \cdot 0488$ |
| $8 \cdot 7$ | $27 \cdot 332$ | $59 \cdot 4468$ | $75 \cdot 69$ | $658 \cdot 503$ | $2 \cdot 9496$ | 2•0567 |
| $8 \cdot 8$ | $27 \cdot 646$ | $60 \cdot 8212$ | $77 \cdot 44$ | $681 \cdot 472$ | $2 \cdot 9665$ | $2 \cdot 0646$ |
| $8 \cdot 9$ | 27.960 | $62 \cdot 2114$ | $79 \cdot 21$ | $704 \cdot 969$ | $2 \cdot 9833$ | $2 \cdot 0724$ |
| $9 \cdot 0$ | 28.274 | $63 \cdot 6173$ | $81 \cdot 00$ | $729 \cdot 000$ | $3 \cdot 0000$ | $2 \cdot 0801$ |
| $9 \cdot 1$ | 28.588 | $65 \cdot 0388$ | $82 \cdot 81$ | 753.571 | $3 \cdot 0166$ | 2.0878 |
| $9 \cdot 2$ | $28 \cdot 903$ | $66 \cdot 4761$ | $84 \cdot 64$ | $778 \cdot 688$ | $3 \cdot 0332$ | $2 \cdot 0954$ |
| $9 \cdot 3$ | $29 \cdot 217$ | $67 \cdot 9291$ | $86 \cdot 49$ | $804 \cdot 357$ | $3 \cdot 0496$ | $2 \cdot 1029$ |
| $9 \cdot 4$ | 29:-31 | $69 \cdot 3978$ | $88 \cdot 36$ | $830 \cdot 584$ | $3 \cdot 0659$ | 2-1105 |
| 9:5 | $29 \cdot 845$ | $70 \cdot 8822$ | $90 \cdot 25$ | $857 \cdot 375$ | $3 \cdot 0822$ | $2 \cdot 1179$ |
| $9 \cdot 6$ | $30 \cdot 159$ | $72 \cdot 3823$ | $92 \cdot 16$ | $884 \cdot 736$ | 3-0984 | $2 \cdot 12.53$ |
| $9 \cdot 7$ | $30 \cdot 473$ | $73 \cdot 8981$ | $94 \cdot 09$ | $912 \cdot 673$ | $3 \cdot 1145$ | $2 \cdot 1327$ |
| $9 \cdot 8$ | $30 \cdot 788$ | $75 \cdot 4296$ | $96 \cdot 04$ | $941 \cdot 192$ | $3 \cdot 1305$ | $2 \cdot 1400$ |
| $9 \cdot 9$ | $31 \cdot 102$ | $76 \cdot 9769$ | $98 \cdot 01$ | $970 \cdot 299$ | $3 \cdot 1464$ | $2 \cdot 1472$ |
| $10 \cdot 0$ | $31 \cdot 416$ | $78 \cdot 540$ | $100 \cdot 00$ | $1000 \cdot 000$ | $3 \cdot 1623$ | $2 \cdot 1544$ |
| $10 \cdot 1$ | 31.730 | $80 \cdot 119$ | $102 \cdot 01$ | $1030 \cdot 301$ | $3 \cdot 1780$ | $2 \cdot 1616$ |
| $10 \cdot 2$ | $32 \cdot 044$ | $81 \cdot 713$ | $104 \cdot 04$ | $1061 \cdot 208$ | $3 \cdot 1937$ | $2 \cdot 1687$ |
| $10 \cdot 3$ | $32 \cdot 358$ | $83 \cdot 323$ | $106 \cdot 09$ | $1092 \cdot 727$ | $3 \cdot 2094$ | $2 \cdot 1757$ |

Table of Powers (continued).

| $n$ | $n \pi$ | $n^{2} \frac{\pi}{4}$ | $n^{2}$ | $n^{3}$ | $\sqrt{n}$ | $\sqrt[3]{n}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $10 \cdot 4$ | $32 \cdot 673$ | $84 \cdot 949$ | $108 \cdot 16$ | $1124 \cdot 863$ | $3 \cdot 2249$ | $2 \cdot 1828$ |
| $10 \cdot 5$ | $32 \cdot 987$ | 86.590 | $110 \cdot 25$ | $1157 \cdot 625$ | $3 \cdot 2404$ | 2-1897 |
| $10 \cdot 6$ | $33 \cdot 301$ | $88 \cdot 247$ | $112 \cdot 36$ | $1191 \cdot 016$ | $3 \cdot 2558$ | $2 \cdot 1967$ |
| $10 \cdot 7$ | $33 \cdot 615$ | $89 \cdot 920$ | $114 \cdot 49$ | $1225 \cdot 043$ | $3 \cdot 2711$ | $2 \cdot 2036$ |
| $10 \cdot 8$ | $33 \cdot 929$ | $91 \cdot 609$ | 116.64 | $1259 \cdot 712$ | $3 \cdot 2863$ | $2 \cdot 2104$ |
| $10 \cdot 9$ | $34 \cdot 243$ | $93 \cdot 313$ | $118 \cdot 81$ | $1295 \cdot 029$ | $3 \cdot 3015$ | $2 \cdot 2172$ |
| $11 \cdot 0$ | $34 \cdot 558$ | $95 \cdot 033$ | $121 \cdot 00$ | $1331 \cdot 000$ | $3 \cdot 3166$ | $2 \cdot 2239$ |
| $11 \cdot 1$ | $34 \cdot 872$ | 96.769 | $123 \cdot 21$ | $1367 \cdot 681$ | $3 \cdot 3317$ | $2 \cdot 2307$ |
| $11 \cdot 2$ | $35 \cdot 186$ | $98 \cdot 520$ | $125 \cdot 44$ | 1404.928 | $3 \cdot 3466$ | $2 \cdot 2374$ |
| $11 \cdot 3$ | $35 \cdot 500$ | $100 \cdot 29$ | $127 \cdot 69$ | $1442 \cdot 897$ | $3 \cdot 3615$ | $2 \cdot 2441$ |
| $11 \cdot 4$ | 35.814 | $102 \cdot 07$ | $129 \cdot 96$ | 1481-544 | 3-3764 | $2 \cdot 2506$ |
| 11.5 | $36 \cdot 128$ | $103 \cdot 87$ | $132 \cdot 25$ | $1520 \cdot 875$ | $3 \cdot 3912$ | $2 \cdot 2572$ |
| $11 \cdot 6$ | $36 \cdot 442$ | $105 \cdot 68$ | $134 \cdot 56$ | $1560 \cdot 896$ | $3 \cdot 4059$ | $2 \cdot 2637$ |
| $11 \cdot 7$ | 36.757 | $107 \cdot 51$ | $136 \cdot 89$ | $1601 \cdot 613$ | $3 \cdot 4205$ | $2 \cdot 2702$ |
| $11 \cdot 8$ | $37 \cdot 071$ | $109 \cdot 36$ | $139 \cdot 24$ | $1643 \cdot 032$ | $3 \cdot 4351$ | $2 \cdot 2766$ |
| $11 \cdot 9$ | $37 \cdot 385$ | $111 \cdot 22$ | $141 \cdot 61$ | $1685 \cdot 159$ | $3 \cdot 4496$ | $2 \cdot 2831$ |
| $12 \cdot 0$ | 37•699 | $113 \cdot 10$ | $144 \cdot 00$ | $1728 \cdot 000$ | $3 \cdot 4641$ | 2.2894 |
| $12 \cdot 1$ | $38 \cdot 013$ | 114.99 | $146 \cdot 41$ | 1771:561 | $3 \cdot 4785$ | $2 \cdot 2957$ |
| $12 \cdot 2$ | $38 \cdot 327$ | 116.90 | $148 \cdot 84$ | $1815 \cdot 848$ | $3 \cdot 4928$ | $2 \cdot 3021$ |
| $12 \cdot 3$ | $38 \cdot 642$ | $118 \cdot 82$ | $151 \cdot 29$ | $1860 \cdot 867$ | $3 \cdot 5071$ | $2 \cdot 3084$ |
| $12 \cdot 4$ | 38.956 | $120 \cdot 76$ | $153 \cdot 76$ | $1906 \cdot 624$ | $3 \cdot 5214$ | $2 \cdot 3146$ |
| 12.5 | $39 \cdot 270$ | $122 \cdot 72$ | $156 \cdot 25$ | $1953 \cdot 125$ | 3.5355 | $2 \cdot 3208$ |
| $12 \cdot 6$ | $39 \cdot 584$ | $124 \cdot 69$ | $158 \cdot 76$ | $2000 \cdot 376$ | $3 \cdot 5496$ | $2 \cdot 3270$ |
| $12 \cdot 7$ | 39.898 | $126 \cdot 68$ | $161 \cdot 29$ | $2048 \cdot 383$ | 3.5637 | $2 \cdot 3331$ |
| $12 \cdot 8$ | $40 \cdot 212$ | $128 \cdot 68$ | $163 \cdot 84$ | $2097 \cdot 152$ | $3 \cdot 5777$ | $2 \cdot 3392$ |
| $12 \cdot 9$ | $40 \cdot 527$ | $130 \cdot 70$ | $166 \cdot 41$ | $2146 \cdot 689$ | $3 \cdot 5917$ | $2 \cdot 3453$ |
| $13 \cdot 0$ | $40 \cdot 841$ | 132.73 | $169 \cdot 00$ | $2197 \cdot 000$ | $3 \cdot 6056$ | $2 \cdot 3513$ |
| $13 \cdot 1$ | $41 \cdot 155$ | $134 \cdot 78$ | $171 \cdot 61$ | $2248 \cdot 091$ | $3 \cdot 6194$ | $2 \cdot 3573$ |
| $13 \cdot 2$ | $41 \cdot 469$ | $136 \cdot 85$ | $174 \cdot 24$ | 2299.968 | $3 \cdot 6332$ | $2 \cdot 3633$ |
| $13 \cdot 3$ | 41.783 | $138 \cdot 93$ | 176.89 | $2352 \cdot 637$ | $3 \cdot 6469$ | $2 \cdot 3693$ |
| $13 \cdot 4$ | $42 \cdot 097$ | $141 \cdot 03$ | $179 \cdot 56$ | $2406 \cdot 104$ | $3 \cdot 6606$ | $2 \cdot 3752$ |
| $13 \cdot 5$ | $42 \cdot 412$ | $143 \cdot 14$ | $182 \cdot 25$ | $2460 \cdot 375$ | $3 \cdot 6742$ | $2 \cdot 3811$ |
| $13 \cdot 6$ | $42 \cdot 726$ | $145 \cdot 27$ | $184 \cdot 96$ | $2515 \cdot 456$ | $3 \cdot 6878$ | $2 \cdot 3870$ |
| $13 \cdot 7$ | $43 \cdot 040$ | $147 \cdot 41$ | $187 \cdot 69$ | 2571-353 | $3 \cdot 7013$ | $2 \cdot 3928$ |
| $13 \cdot 8$ | $43 \cdot 354$ | 149.57 | $190 \cdot 44$ | $2628 \cdot 072$ | $3 \cdot 7148$ | $2 \cdot 3986$ |
| $13 \cdot 9$ | $43 \cdot 668$ | $151 \cdot 75$ | $193 \cdot 21$ | $2685 \cdot 619$ | $3 \cdot 7283$ | $2 \cdot 4044$ |
| $14 \cdot 0$ | $43 \cdot 982$ | 153.94 | $196 \cdot 00$ | 2744.000 | $3 \cdot 7417$ | $2 \cdot 4101$ |
| $14 \cdot 1$ | $44 \cdot 296$ | $156 \cdot 15$ | $198 \cdot 81$ | $2803 \cdot 221$ | $3 \cdot 7550$ | $2 \cdot 4159$ |
| $14 \cdot 2$ | $44 \cdot 611$ | $158 \cdot 37$ | $201 \cdot 64$ | $2863 \cdot 288$ | $3 \cdot 7683$ | $2 \cdot 4216$ |
| $14 \cdot 3$ | $44 \cdot 92$ ) | $160 \cdot 61$ | $204 \cdot 49$ | $2924 \cdot 207$ | $3 \cdot 7815$ | $2 \cdot 4272$ |
| $14 \cdot 4$ | $45 \cdot 239$ | $162 \cdot 86$ | $207 \cdot 36$ | $2985 \cdot 984$ | $3 \cdot 7947$ | $2 \cdot 4329$ |

TABLE of Powers (continued).

| $n$ | $n \pi$ | $n^{2} \frac{\pi}{4}$ | $n^{2}$ | $n^{3}$ | $\sqrt{n}$ | $\sqrt[3]{n}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 14\% | 45.553 | $16.5 \cdot 13$ | $210 \cdot 25$ | 3048.62 | $3 \cdot 8079$ | $2 \cdot 4385$ |
| $14 \cdot 6$ | $45 \cdot 867$ | $167 \cdot 42$ | $213 \cdot 16$ | $3112 \cdot 136$ | $3 \cdot 8210$ | $2 \cdot 4441$ |
| $14 \cdot 7$ | 46.181 | $169 \cdot 72$ | $216 \cdot 09$ | $3176 \cdot 523$ | $3 \cdot 8341$ | $2 \cdot 4497$ |
| $14 \cdot 8$ | $46 \cdot 496$ | $172 \cdot 03$ | $219 \cdot 04$ | $3241 \cdot 792$ | $3 \cdot 8471$ | $2 \cdot 4552$ |
| 14.9 | 46.810 | $174 \cdot 37$ | $222 \cdot 01$ | 3307.949 | $3 \cdot 8600$ | $2 \cdot 4607$ |
| 15.0 | $47 \cdot 124$ | $176 \cdot 715$ | $225 \cdot 00$ | 3375.000 | $3 \cdot 8730$ | $2 \cdot 4662$ |
| $15 \cdot 1$ | $47 \cdot 438$ | $179 \cdot 079$ | $228 \cdot 01$ | 3442.951 | $3 \cdot 8859$ | $2 \cdot 4717$ |
| $15 \cdot 2$ | $47 \cdot 752$ | $181 \cdot 458$ | $231 \cdot 04$ | $3511 \cdot 808$ | $3 \cdot 8987$ | $2 \cdot 4771$ |
| $15 \cdot 3$ | $48 \cdot 066$ | $183 \cdot 854$ | $234 \cdot 09$ | $3581 \cdot 577$ | $3 \cdot 9115$ | $2 \cdot 4825$ |
| $15 \cdot 4$ | $48 \cdot 381$ | $186 \cdot 265$ | $237 \cdot 16$ | 3652-264 | $3 \cdot 9243$ | $2 \cdot 4879$ |
| 15.5 | $48 \cdot 695$ | $188 \cdot 692$ | $240 \cdot 25$ | $3723 \cdot 875$ | $3 \cdot 9370$ | $2 \cdot 4933$ |
| $15 \cdot 6$ | $49 \cdot 009$ | $191 \cdot 134$ | $243 \cdot 36$ | $3796 \cdot 416$ | $3 \cdot 9497$ | $2 \cdot 4987$ |
| $15 \cdot 7$ | $49 \cdot 323$ | $193 \cdot 593$ | $246 \cdot 49$ | $3869 \cdot 893$ | $3 \cdot 9623$ | $2 \cdot 5040$ |
| 15.8 | $49 \cdot 637$ | $196 \cdot 067$ | $249 \cdot 64$ | $39+4 \cdot 312$ | $3 \cdot 9749$ | $2 \cdot 5093$ |
| 15.9 | 49.951 | 198.5.57 | $252 \cdot 81$ | $4019 \cdot 679$ | $3 \cdot 9875$ | $2 \cdot 5146$ |
| 16.0 | $50 \cdot 265$ | 201•062 | 2.56.00 | $4096 \cdot 000$ | $4 \cdot 0000$ | 2.5198 |
| $16 \cdot 1$ | 50.580 | 203.583 | $259 \cdot 21$ | $4173 \cdot 281$ | $4 \cdot 0125$ | $2 \cdot 5251$ |
| $16 \cdot 2$ | 50.894 | $206 \cdot 120$ | 262.44 | $4251 \cdot 528$ | $4 \cdot 0249$ | $2 \cdot 5303$ |
| $16 \cdot 3$ | $51 \cdot 208$ | $208 \cdot 672$ | $265 \cdot 69$ | $4330 \cdot 747$ | $4 \cdot 0373$ | $2 \cdot 5355$ |
| $16 \cdot 4$ | $51 \cdot 522$ | $211 \cdot 241$ | $268 \cdot 96$ | $4410 \cdot 944$ | $4 \cdot 0497$ | 2:5407 |
| $16 \cdot 5$ | $51 \cdot 836$ | $213 \cdot 825$ | $272 \cdot 25$ | $4492 \cdot 125$ | $4 \cdot 0620$ | 2:5458 |
| $16 \cdot 6$ | $52 \cdot 150$ | 216.424 | $275 \cdot 56$ | $4574 \cdot 296$ | $4 \cdot 0743$ | $2 \cdot 5509$ |
| $16 \cdot 7$ | $52 \cdot 465$ | $219 \cdot 040$ | $278 \cdot 89$ | $4657 \cdot 463$ | $4 \cdot 0866$ | 2.5561 |
| $16 \cdot 8$ | 52.779 | 221.671 | $282 \cdot 24$ | $4741 \cdot 632$ | $4 \cdot 0988$ | 2.5612 |
| $16 \cdot 9$ | 53.093 | $22 \pm \cdot 318$ | 285.61 | $4826 \cdot 809$ | $4 \cdot 1110$ | $2 \cdot 5662$ |
| $17 \cdot 0$ | $53 \cdot 407$ | 226.980 | $289 \cdot 00$ | $4913 \cdot 000$ | $4 \cdot 1231$ | $2 \cdot 5713$ |
| $17 \cdot 1$ | $53 \cdot 721$ | $229 \cdot 658$ | $292 \cdot 41$ | $5000 \cdot 211$ | $4 \cdot 1352$ | $2 \cdot 5763$ |
| $17 \cdot 2$ | $54 \cdot 035$ | $232 \cdot 352$ | $29.5 \cdot 84$ | $5088 \cdot 448$ | $4 \cdot 1473$ | 2:5813 |
| $17 \cdot 3$ | $54 \cdot 350$ | $235 \cdot 062$ | $299 \cdot 29$ | $5177 \cdot 717$ | $4 \cdot 1593$ | $2 \cdot 5863$ |
| $17 \cdot 4$ | $54 \cdot 664$ | $237 \cdot 787$ | $302 \cdot 76$ | $5268 \cdot 024$ | $4 \cdot 1713$ | 2.5913 |
| 17\% | 54.978 | $240 \cdot 528$ | $306 \cdot 25$ | $5359 \cdot 375$ | $4 \cdot 1833$ | 2.5962 |
| $17 \cdot 6$ | 55.292 | $243 \cdot 285$ | $309 \cdot 76$ | $5451 \cdot 776$ | $4 \cdot 1952$ | $2 \cdot 6012$ |
| $17 \cdot 7$ | 55.606 | $246 \cdot 0.57$ | $313 \cdot 29$ | $5.545 \cdot 233$ | $4 \cdot 2071$ | $2 \cdot 6061$ |
| $17 \cdot 8$ | 55.920 | $248 \cdot 846$ | $316 \cdot 84$ | ธ639•752 | $4 \cdot 2190$ | $2 \cdot 6110$ |
| $17 \cdot 9$ | $56 \cdot 23.5$ | $2.51 \cdot 649$ | $320 \cdot 41$ | $5735 \cdot 339$ | $4 \cdot 2308$ | $2 \cdot 6159$ |
| $18 \cdot 0$ | 56.549 | 2 ¢ $4 \cdot 469$ | $324 \cdot 00$ | $5832 \cdot 000$ | $4 \cdot 2426$ | $2 \cdot 6207$ |
| $18 \cdot 1$ | ธ $6 \cdot 863$ | $2.57 \cdot 304$ | $327 \cdot 61$ | $5929 \cdot 741$ | $4 \cdot 2544$ | $2 \cdot 62.56$ |
| $18 \cdot 2$ | $57 \cdot 177$ | 260.155 | $331 \cdot 24$ | $6028 \cdot 508$ | $4 \cdot 2661$ | $2 \cdot 6304$ |
| $18 \cdot 3$ | $57 \cdot 491$ | $263 \cdot 022$ | $334 \cdot 89$ | $6128 \cdot 487$ | $4 \cdot 2778$ | $2 \cdot 6352$ |
| $18 \cdot 4$ | $57 \cdot 805$ | 265.904 | $338 \cdot 56$ | $6229 \cdot 504$ | $4 \cdot 2895$ | $2 \cdot 6400$ |
| $18 \cdot 5$ | $58 \cdot 119$ | $268 \cdot 803$ | $342 \cdot 25$ | $6331 \cdot 625$ | $4 \cdot 3012$ | $2 \cdot 6448$ |

Table of Powers (continued).

| $n$ | $n \pi$ | $n^{2}{ }_{4}^{\pi}$ | $n^{2}$ | $n^{3}$ | $\sqrt{n}$ | $\sqrt[3]{n}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $18 \cdot 6$ | 58.434 | $271 \cdot 716$ | $345 \cdot 96$ | $6434 \cdot 856$ | $4 \cdot 3128$ | 2.6495 |
| $18 \cdot 7$ | $58 \cdot 748$ | $274 \cdot 646$ | $349 \cdot 69$ | $6539 \cdot 203$ | $4: 3243$ | 2•6.543 |
| $18 \cdot 8$ | $59 \cdot 062$ | $277 \cdot 591$ | 353.44 | $6644 \cdot 672$ | $4 \cdot 3359$ | $2 \cdot 6590$ |
| $18 \cdot 9$ | $59 \cdot 376$ | 280.552 | $357 \cdot 21$ | $6751 \cdot 269$ | $4 \cdot 3474$ | $2 \cdot 6637$ |
| $19 \cdot 0$ | 59.690 | $283 \cdot 529$ | $361 \cdot 00$ | $6859 \cdot 000$ | $4 \cdot 3589$ | $2 \cdot 6684$ |
| $19 \cdot 1$ | $60 \cdot 004$ | 286.521 | $364 \cdot 81$ | $6967 \cdot 871$ | $4 \cdot 3704$ | $2 \cdot 6731$ |
| $19 \cdot 2$ | $60 \cdot 319$ | $289 \cdot 529$ | $368 \cdot 64$ | $7077 \cdot 888$ | $4 \cdot 3818$ | $2 \cdot 6777$ |
| $19 \cdot 3$ | $60 \cdot 633$ | 292-5.53 | $372 \cdot 49$ | $7189 \cdot 057$ | $4 \cdot 3932$ | $2 \cdot 6824$ |
| $19 \cdot 4$ | $60 \cdot 947$ | $295 \cdot 592$ | $376 \cdot 36$ | $7301 \cdot 384$ | $4 \cdot 4045$ | $2 \cdot 6870$ |
| $19 \cdot 5$ | $61 \cdot 261$ | $298 \cdot 648$ | $380 \cdot 25$ | $7414 \cdot 875$ | $4 \cdot 4159$ | $2 \cdot 6916$ |
| $19 \cdot 6$ | 61:575 | $301 \cdot 719$ | $384 \cdot 16$ | 7529.536 | $4 \cdot 4272$ | $2 \cdot 6962$ |
| $19 \cdot 7$ | $61 \cdot 889$ | $304 \cdot 805$ | $388 \cdot 09$ | $7645 \cdot 373$ | $4 \cdot 4385$ | $2 \cdot 7008$ |
| $19 \cdot 8$ | $62 \cdot 204$ | $307 \cdot 907$ | $392 \cdot 04$ | $7762 \cdot 392$ | $4 \cdot 4497$ | $2 \cdot 7053$ |
| $19 \cdot 9$ | 62.518 | $311 \cdot 026$ | 396.01 | $7880 \cdot 599$ | $4 \cdot 4609$ | $2 \cdot 7099$ |
| $20 \cdot 0$ | $62 \cdot 832$ | $314 \cdot 16$ | $400 \cdot 00$ | $8000 \cdot 000$ | $4 \cdot 4721$ | 2.7144 |
| $20 \cdot 1$ | $63 \cdot 146$ | $317 \cdot 31$ | $404 \cdot 01$ | $8120 \cdot 601$ | $4 \cdot 4833$ | 2.7189 |
| $20 \cdot 2$ | $63 \cdot 460$ | $320 \cdot 47$ | $408 \cdot 04$ | 8242.408 | $4 \cdot 4944$ | 2.7234 |
| $20 \cdot 3$ | $63 \cdot 774$ | $323 \cdot 66$ | $412 \cdot 09$ | $8365 \cdot 427$ | $4 \cdot 5055$ | $2 \cdot 7279$ |
| $20 \cdot 4$ | $64 \cdot 088$ | $326 \cdot 85$ | $416 \cdot 16$ | $8489 \cdot 664$ | $4 \cdot 5166$ | $2 \cdot 7324$ |
| $20 \cdot 5$ | $64 \cdot 403$ | $330 \cdot 06$ | $420 \cdot 2.5$ | $8615 \cdot 125$ | $4 \cdot 5277$ | 2.7368 |
| $20 \cdot 6$ | $64 \cdot 717$ | $333 \cdot 29$ | $424 \cdot 36$ | $8741 \cdot 816$ | $4 \cdot 5387$ | $2 \cdot 7413$ |
| $20 \cdot 7$ | 65.031 | 336.54 | $428 \cdot 49$ | $8869 \cdot 743$ | $4 \cdot 5497$ | $2 \cdot 74.57$ |
| $20 \cdot 8$ | $65 \cdot 345$ | $339 \cdot 80$ | $432 \cdot 64$ | $8998 \cdot 912$ | $4 \cdot 5607$ | 2.7502 |
| $20 \cdot 9$ | 65.659 | $343 \cdot 07$ | $436 \cdot 81$ | $9129 \cdot 329$ | $4 \cdot 5716$ | $2 \cdot 7545$ |
| $21 \cdot 0$ | 65.973 | $346 \cdot 36$ | $441 \cdot 00$ | $9261 \cdot 000$ | $4 \cdot 5826$ | $2 \cdot 7589$ |
| $21 \cdot 1$ | $66 \cdot 288$ | $349 \cdot 67$ | $445 \cdot 21$ | $9393 \cdot 931$ | $4 \cdot 5935$ | $2 \cdot 7633$ |
| $21 \cdot 2$ | $66 \cdot 602$ | $352 \cdot 99$ | $449 \cdot 44$ | $9528 \cdot 128$ | $4 \cdot 6043$ | 2.7676 |
| $21 \cdot 3$ | $66 \cdot 916$ | $356 \cdot 33$ | $453 \cdot 69$ | 9663.597 | $4 \cdot 6152$ | 2.7720 |
| $21 \cdot 4$ | $67 \cdot 230$ | $359 \cdot 68$ | 4.)7.96 | $9800 \cdot 344$ | $4 \cdot 6260$ | $2 \cdot 7763$ |
| $21 \cdot 5$ | $67 \cdot 544$ | $363 \cdot 05$ | $462 \cdot 25$ | $9938 \cdot 375$ | $4 \cdot 6368$ | $2 \cdot 7806$ |
| $21 \cdot 6$ | $67 \cdot 8.8$ | 366.44 | 466.56 | $10077 \cdot 696$ | $4 \cdot 6476$ | $2 \cdot 7849$ |
| $21 \cdot 7$ | $68 \cdot 173$ | $369 \cdot 84$ | $470 \cdot 89$ | 10218:313 | $4 \cdot 6.583$ | $2 \cdot 7893$ |
| $21 \cdot 8$ | $68 \cdot 487$ | $373 \cdot 25$ | $475 \cdot 24$ | $10360 \cdot 232$ | $4 \cdot 6690$ | $2 \cdot 7935$ |
| $21 \cdot 9$ | $68 \cdot 801$ | $376 \cdot 69$ | $479 \cdot 61$ | 10.503.459 | $4 \cdot 6797$ | $2 \cdot 7978$ |
| $22 \cdot 0$ | $69 \cdot 115$ | $380 \cdot 13$ | $484 \cdot 00$ | 10648.000 | $4 \cdot 6904$ | $2 \cdot 8021$ |
| $22 \cdot 1$ | $69 \cdot 429$ | $383 \cdot 60$ | $488 \cdot 41$ | 10793.861. | $4 \cdot 7011$ | $2 \cdot 8063$ |
| $22 \cdot 2$ | $69 \cdot 743$ | 387.08 | $492 \cdot 84$ | 10941.048 | $4 \cdot 7117$ | 2.810.) |
| $22 \cdot 3$ | 70.0.88 | 390.57 | $497 \cdot 29$ | 11089:567 | $4 \cdot 7223$ | $2 \cdot 8147$ |
| $22 \cdot 4$ | $70 \cdot 372$ | $394 \cdot 08$ | $501 \cdot 76$ | $11239 \cdot 424$ | 4.7329 | 2.8189 |
| $22 \cdot 5$ | $70 \cdot 686$ | $397 \cdot 61$ | 506.25 | 11390.625 | $4 \cdot 7434$ | 2.8231 |
| $22 \cdot 6$ | $71 \cdot 000$ | $401 \cdot 15$ | 510.76 | $11543 \cdot 176$ | $4 \cdot 7539$ | 2.8273 |

POWERS.
Table of Powers (continued).

| $n$ | $n \pi$ | $n^{2} \frac{\pi}{4}$ | $n^{2}$ | $n^{3}$ | $\sqrt{r}$ | $\sqrt[3]{n}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $22 \cdot 7$ | $71 \cdot 314$ | 404•71 | $515 \cdot 29$ | 11697.083 | $4 \cdot 7644$ | $2 \cdot 8314$ |
| $22 \cdot 8$ | $71 \cdot 628$ | $408 \cdot 28$ | $519 \cdot 84$ | 11852.352 | $4 \cdot 7749$ | $2 \cdot 8356$ |
| $22 \cdot 9$ | 71.942 | $411 \cdot 87$ | $524 \cdot 41$ | $12008 \cdot 989$ | $4 \cdot 7854$ | $2 \cdot 8397$ |
| $23 \cdot 0$ | $72 \cdot 257$ | $415 \cdot 48$ | $529 \cdot 00$ | $12167 \cdot 000$ | $4 \cdot 7958$ | $2 \cdot 8438$ |
| $23 \cdot 1$ | 72.571 | $419 \cdot 10$ | $533 \cdot 61$ | $12326 \cdot 391$ | $4 \cdot 8062$ | $2 \cdot 8479$ |
| $23 \cdot 2$ | $72 \cdot 885$ | $422 \cdot 73$ | $538 \cdot 24$ | $12487 \cdot 168$ | $4 \cdot 8166$ | 2.8521 |
| $23 \cdot 3$ | $73 \cdot 199$ | $426 \cdot 39$ | $542 \cdot 89$ | $12649 \cdot 337$ | $4 \cdot 8270$ | $2 \cdot 8562$ |
| $23 \cdot 4$ | $73 \cdot 513$ | $430 \cdot 05$ | $547 \cdot 56$ | $12812 \cdot 904$ | $4 \cdot 8373$ | $2 \cdot 8603$ |
| $23 \cdot 5$ | $73 \cdot 827$ | $433 \cdot 74$ | $552 \cdot 25$ | $12977 \cdot 875$ | $4 \cdot 8477$ | $2 \cdot 8643$ |
| $23 \cdot 6$ | $74 \cdot 142$ | $437 \cdot 44$ | $556 \cdot 96$ | $13144 \cdot 256$ | $4 \cdot 8580$ | $2 \cdot 8684$ |
| $23 \cdot 7$ | $74 \cdot 456$ | $441 \cdot 15$ | $561 \cdot 69$ | $13312 \cdot 053$ | $4 \cdot 8683$ | 2.8724 |
| 23:8 | 74.770 | $444 \cdot 88$ | 566.44 | $13481 \cdot 272$ | $4 \cdot 8785$ | $2 \cdot 8765$ |
| $23 \cdot 9$ | 75.084 | $448 \cdot 63$ | $571 \cdot 21$ | 13651.919 | $4 \cdot 8888$ | $2 \cdot 8805$ |
| $24 \cdot 0$ | $75 \cdot 398$ | $452 \cdot 39$ | $576 \cdot 00$ | $13824 \cdot 000$ | $4 \cdot 8990$ | $2 \cdot 8845$ |
| $24 \cdot 1$ | $75 \cdot 712$ | $456 \cdot 17$ | $580 \cdot 81$ | $13997 \cdot 521$ | $4 \cdot 9092$ | $2 \cdot 8885$ |
| $24 \cdot 2$ | $76 \cdot 027$ | 459.96 | $585 \cdot 64$ | 14172.488 | 4.9193 | $2 \cdot 8925$ |
| $24 \cdot 3$ | $76 \cdot 341$ | 46377 | $590 \cdot 49$ | $14348 \cdot 907$ | $4 \cdot 9295$ | $2 \cdot 8965$ |
| $24 \cdot 4$ | $76 \cdot 655$ | $467 \cdot 60$ | $595 \cdot 36$ | $14526 \cdot 784$ | $4 \cdot 9396$ | $2 \cdot 9004$ |
| $24 \%$ | 76.969 | $471 \cdot 44$ | $600 \cdot 25$ | $14706 \cdot 125$ | $4 \cdot 9497$ | $2 \cdot 9044$ |
| $24 \cdot 6$ | $77 \cdot 283$ | $475 \cdot 29$ | $605 \cdot 16$ | $14886 \cdot 936$ | $4 \cdot 9598$ | $2 \cdot 9083$ |
| $24 \cdot 7$ | $77 \cdot 597$ | $479 \cdot 16$ | $610 \cdot 09$ | $15069 \cdot 223$ | $4 \cdot 9699$ | $2 \cdot 9123$ |
| $24 \cdot 8$ | $77 \cdot 911$ | $483 \cdot 05$ | $615 \cdot 04$ | 15252.992 | $4 \cdot 9799$ | $2 \cdot 9162$ |
| 24.9 | $78 \cdot 226$ | $486 \cdot 96$ | $620 \cdot 01$ | $15438 \cdot 249$ | $4 \cdot 9899$ | $2 \cdot 9201$ |
| $25 \cdot 0$ | $78 \cdot 540$ | $490 \cdot 874$ | 625.00 | $15625 \cdot 000$ | $5 \cdot 0000$ | $2 \cdot 9240$ |
| $25 \cdot 1$ | $78 \cdot 854$ | $494 \cdot 809$ | $630 \cdot 01$ | $15813 \cdot 251$ | 5.0099 | $2 \cdot 9279$ |
| $25 \cdot 2$ | $79 \cdot 168$ | $498 \cdot 759$ | $635 \cdot 04$ | $16003 \cdot 008$ | 5.0199 | 2.9318 |
| $25 \cdot 3$ | $79 \cdot 482$ | $502 \cdot 726$ | 640.09 | $16194 \cdot 277$ | $5 \cdot 0299$ | $2 \cdot 9357$ |
| $25 \cdot 4$ | 79.796 | 506.708 | $645 \cdot 16$ | $16387 \cdot 064$ | 5.0398 | $2 \cdot 9395$ |
| 25.5 | $80 \cdot 111$ | 510.705 | $650 \cdot 25$ | $16581 \cdot 375$ | 5.0498 | $2 \cdot 9434$ |
| $25 \cdot 6$ | $80 \cdot 425$ | $514 \cdot 719$ | $655 \cdot 36$ | $16777 \cdot 216$ | $5 \cdot 0596$ | $2 \cdot 9472$ |
| $25 \cdot 7$ | 80.739 | $518 \cdot 748$ | $660 \cdot 49$ | $16974 \cdot 593$ | $5 \cdot 0695$ | $2 \cdot 9511$ |
| $25 \cdot 8$ | $81 \cdot 053$ | $522 \cdot 792$ | $665 \cdot 64$ | $17173 \cdot 512$ | $5 \cdot 0794$ | $2 \cdot 9549$ |
| $25 \cdot 9$ | $81 \cdot 367$ | $526 \cdot 853$ | $670 \cdot 81$ | 17373.979 | 5.0892 | $2 \cdot 9587$ |
| $26 \cdot 0$ | $81 \cdot 681$ | $530 \cdot 929$ | $676 \cdot 00$ | $17576 \cdot 000$ | 5.0990 | $2 \cdot 9625$ |
| $26 \cdot 1$ | 81.996 | 535.021 | $681 \cdot 21$ | $17779 \cdot 581$ | $5 \cdot 1088$ | $2 \cdot 9663$ |
| $26 \cdot 2$ | $82 \cdot 310$ | $539 \cdot 129$ | $686 \cdot 44$ | 17984.728 | $5 \cdot 1186$ | $2 \cdot 9701$ |
| $26 \cdot 3$ | 82.624 | $543 \cdot 252$ | $691 \cdot 69$ | $18191 \cdot 447$ | $5 \cdot 1284$ | $2 \cdot 9738$ |
| $26 \cdot 4$ | 82.938 | $547 \cdot 391$ | $696 \cdot 96$ | $18399 \cdot 744$ | $5 \cdot 1381$ | $2 \cdot 9776$ |
| 26.5 | $83 \cdot 2.2$ | $551 \cdot 546$ | $702 \cdot 25$ | $18609 \cdot 625$ | $5 \cdot 1478$ | $2 \cdot 9814$ |
| $26 \cdot 6$ | $83 \cdot 566$ | $555 \cdot 716$ | $707 \cdot 50$ | 18821•096 | $5 \cdot 1575$ | $2 \cdot 9851$ |
| 26.7 | $83 \cdot 881$ | $559 \cdot 903$ | $712 \cdot 89$ | $19034 \cdot 163$ | $5 \cdot 1672$ | 2.9888 |

Table of Powers (continued).

| $n$ | $n \pi$ | $n^{2} \frac{\pi}{4}$ | $n^{2}$ | $n^{3}$ | $\sqrt{n}$ | $\sqrt[3]{n}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $26 \cdot 8$ | $84 \cdot 195$ | $564 \cdot 104$ | 718.24 | 19248.832 | 5•1769 | $2 \cdot 9926$ |
| 26.9 | 84:509 | $568 \cdot 322$ | 723:61 | $19465 \cdot 109$ | $5 \cdot 1865$ | $2 \cdot 9963$ |
| $27 \cdot 0$ | $84 \cdot 823$ | 572\%5ั5 | $729 \cdot 00$ | $19683 \cdot 000$ | 5•1962 | $3 \cdot 0000$ |
| $27 \cdot 1$ | $85 \cdot 137$ | 576.804 | $734 \cdot 41$ | 19902:511 | $5 \cdot 2058$ | $3 \cdot 0037$ |
| $27 \cdot 2$ | $85 \cdot 451$ | $581 \cdot 069$ | $739 \cdot 84$ | 20123.648 | $5 \cdot 2154$ | $3 \cdot 0074$ |
| $27 \cdot 3$ | 85.765 | 585.349 | $745 \cdot 29$ | 20346417 | $5 \cdot 2249$ | $3 \cdot 0111$ |
| $27 \cdot 4$ | 86.080 | $589 \cdot 646$ | $750 \cdot 76$ | 20570.824 | $5 \cdot 2345$ | $3 \cdot 0147$ |
| 27-5 | 86.394 | 593.957 | $756 \cdot 25$ | 20796.875 | $5 \cdot 2440$ | $3 \cdot 0184$ |
| $27 \cdot 6$ | 86.708 | 598.285 | 761.76 | $21024 \div 576$ | 5-2536 | $3 \cdot 0221$ |
| $27 \cdot 7$ | $87 \cdot 022$ | $602 \cdot 628$ | $767 \cdot 29$ | 21253.933 | $5 \cdot 2631$ | $3 \cdot 0257$ |
| $27 \cdot 8$ | 87-336 | 606.987 | $772 \cdot 84$ | $21484 \cdot 952$ | $5 \cdot 2726$ | $3 \cdot 0293$ |
| 27.9 | $87 \cdot 650$ | 611-362 | $778 \cdot 41$ | 21717•639 | $5 \cdot 2820$ | $3 \cdot 0330$ |
| $28 \cdot 0$ | 87.965 | $615 \cdot 752$ | $784 \cdot 00$ | 21952.000 | $5 \cdot 2915$ | $3 \cdot 0366$ |
| $28 \cdot 1$ | 88.279 | $620 \cdot 158$ | $789 \cdot 61$ | $22188 \cdot 041$ | 5.3009 | $3 \cdot 0402$ |
| $28 \cdot 2$ | 88.593 | 624.580 | 795.24 | 22425.768 | $5 \cdot 3104$ | $3 \cdot 0438$ |
| $28 \cdot 3$ | 88.907 | $629 \cdot 018$ | 800.89 | 22665 187 | 5•3198 | $3 \cdot 0474$ |
| 28.4 | 89•221 | $633 \cdot 471$ | 806.56 | 22906.304 | 5-3292 | $3 \cdot 0510$ |
| 285 | 89:535 | $637 \cdot 940$ | $812 \cdot 25$ | 23149•125 | $5 \cdot 3385$ | $3 \cdot 0546$ |
| $28 \cdot 6$ | 89.850 | $642 \cdot 424$ | $817 \cdot 96$ | 23393.656 | 5•3479 | $3 \cdot 0581$ |
| 28.7 | 90.164 | 646.925 | $823 \cdot 69$ | $23639 \cdot 903$ | 5.3572 | $3 \cdot 0617$ |
| $28 \cdot 8$ | $90 \cdot 478$ | 651.441 | $829 \cdot 44$ | $23887 \cdot 872$ | $5 \cdot 3666$ | $3 \cdot 0652$ |
| $28 \cdot 9$ | 90.792 | 655.972 | 835.21 | 24137 ¢569 | 5•3759 | $3 \cdot 0688$ |
| $29 \cdot 0$ | $91 \cdot 106$ | $660 \cdot 520$ | 841.00 | $24389 \cdot 000$ | $5 \cdot 3852$ | $3 \cdot 0723$ |
| $29 \cdot 1$ | 91.420 | $665 \cdot 083$ | 846.81 | $24642 \cdot 171$ | $5 \cdot 3944$ | $3 \cdot 0758$ |
| $29 \cdot 2$ | 91.735 | $669 \cdot 662$ | 852.64 | $24897 \cdot 088$ | $5 \cdot 4037$ | 3•0794 |
| $29 \cdot 3$ | $92 \cdot 049$ | $674 \cdot 256$ | 858.49 | 25153.757 | 5-4129 | $3 \cdot 0829$ |
| $29 \cdot 4$ | 92.363 | $678 \cdot 867$ | $864 \cdot 36$ | 25412-184 | $5 \cdot 4222$ | $3 \cdot 0864$ |
| $29 \cdot 5$ | 92.677 | $683 \cdot 493$ | 870.25 | 25672.375 | $5 \cdot 4314$ | $3 \cdot 0899$ |
| $29 \cdot 6$ | 92.991 | $688 \cdot 134$ | $876 \cdot 16$ | 2ธ934*336 | $5 \cdot 4406$ | 3•0934 |
| $29 \cdot 7$ | 93-305 | 692.792 | 882.09 | $26198 \cdot 073$ | $5 \cdot 4498$ | $3 \cdot 0968$ |
| $29 \cdot 8$ | $93 \cdot 619$ | $697 \cdot 465$ | 888.04 | 26463:592 | $5 \cdot 4.59$ | 3•1003 |
| $29 \cdot 9$ | 93.934 | 702.154 | 894.01 | $26730 \cdot 899$ | $5 \cdot 4681$ | $3 \cdot 1038$ |
| $30 \cdot 0$ | $94 \cdot 248$ | $706 \cdot 86$ | 900.00 | $27000 \cdot 000$ | $5 \cdot 4772$ | 3•1072 |
| $30 \cdot 1$ | 94.562 | 711ヶ58 | 906.01 | 27270.901 | $5 \cdot 4863$ | $3 \cdot 1107$ |
| $30 \cdot 2$ | 94.876 | $716 \cdot 32$ | $912 \cdot 04$ | 27543.608 | $5 \cdot 4954$ | $3 \cdot 1141$ |
| $30 \cdot 3$ | 95.190 | $721 \cdot 07$ | $918 \cdot 09$ | $27818 \cdot 127$ | $5 \cdot 5045$ | $3 \cdot 1176$ |
| $30 \cdot 4$ | 95.504 | $725 \cdot 83$ | $924 \cdot 16$ | $28094 \cdot 464$ | $5 \cdot 5136$ | $3 \cdot 1210$ |
| $30 \cdot 5$ | 95.819 | $730 \cdot 62$ | 930.25 | 28372.625 | $5 \cdot 5226$ | $3 \cdot 1244$ |
| $30 \cdot 6$ | $96 \cdot 133$ | $735 \cdot 42$ | 936.36 | 28652.616 | 5•5317 | $3 \cdot 1278$ |
| $30 \cdot 7$ | 96.447 | $740 \cdot 23$ | $942 \cdot 49$ | $28934 \cdot 443$ | 5.5407 | 3-1312 |
| $30 \cdot 8$ | 96.761 | $745 \cdot 06$ | $948 \cdot 64$ | $29218 \cdot 112$ | 5.5497 | $3 \cdot 1346$ |

Table of Powers (continued).

| $n$ | $n \pi$ | $n^{2} \frac{\pi}{4}$ | $\iota^{2}$ | $n^{3}$ | $\sqrt{n}$ | $\sqrt[3]{n}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 30.9 | $97 \cdot 075$ | $749 \cdot 91$ | $954 \cdot 81$ | $29503 \cdot 629$ | 5\%587 | $3 \cdot 1380$ |
| $31 \cdot 0$ | $97 \cdot 389$ | $754 \cdot 77$ | $961 \cdot 00$ | $29791 \cdot 000$ | $5 \cdot 5678$ | $3 \cdot 1414$ |
| $31 \cdot 1$ | $97 \cdot 704$ | $759 \cdot 65$ | $967 \cdot 21$ | 30080.231 | $5 \cdot 5767$ | $3 \cdot 1448$ |
| $31 \cdot 2$ | 98.018 | $764 \cdot 54$ | 973-44 | 30371-328 | 5•ธ5857 | 3-1481 |
| $31 \cdot 3$ | $98 \cdot 332$ | $769 \cdot 45$ | $979 \cdot 69$ | $30664 \cdot 297$ | $5 \cdot 5946$ | $3 \cdot 1515$ |
| $31 \cdot 4$ | $98 \cdot 646$ | $774 \cdot 37$ | $985 \cdot 96$ | $30959 \cdot 144$ | $5 \cdot 6035$ | $3 \cdot 1548$ |
| $31 \cdot 5$ | $98 \cdot 960$ | $779 \cdot 31$ | $992 \cdot 25$ | 31255.875 | $5 \cdot 6124$ | $3 \cdot 1582$ |
| $31 \cdot 6$ | $99 \cdot 274$ | $784 \cdot 27$ | $998 \cdot 56$ | $31554 \cdot 496$ | $5 \cdot 6213$ | $3 \cdot 1615$ |
| $31 \cdot 7$ | $99 \cdot 588$ | $789 \cdot 24$ | 1004.89 | $31855 \cdot 013$ | 5.6302 | $3 \cdot 1648$ |
| $31 \cdot 8$ | $99 \cdot 903$ | $794 \cdot 23$ | 1011-24 | $32157 \cdot 432$ | $5 \cdot 6391$ | $3 \cdot 1681$ |
| $31 \cdot 9$ | $100 \cdot 22$ | $799 \cdot 23$ | 1017.61 | 32461•759 | $5 \cdot 6480$ | $3 \cdot 1715$ |
| $32 \cdot 0$ | $100 \cdot 53$ | $804 \cdot 25$ | $1024 \cdot 00$ | $32768 \cdot 000$ | 5.6569 | $3 \cdot 1748$ |
| $32 \cdot 1$ | $100 \cdot 85$ | $809 \cdot 28$ | $1030 \cdot 41$ | $33076 \cdot 161$ | $5 \cdot 6656$ | $3 \cdot 1781$ |
| $32 \cdot 2$ | 101•16 | $814 \cdot 33$ | $1036 \cdot 84$ | $33386 \cdot 248$ | $5 \cdot 6745$ | $3 \cdot 1814$ |
| $32 \cdot 3$ | 101•47 | $819 \cdot 40$ | 1043•29 | $33698 \cdot 267$ | $5 \cdot 6833$ | $3 \cdot 1847$ |
| $32 \cdot 4$ | 101.79 | $824 \cdot 48$ | $1049 \cdot 76$ | $34012 \cdot 224$ | 5.6921 | $3 \cdot 1880$ |
| 32.5 | $102 \cdot 10$ | 829.58 | 1056.25 | $34328 \cdot 125$ | $5 \cdot 7008$ | $3 \cdot 1913$ |
| $32 \cdot 6$ | $102 \cdot 42$ | $834 \cdot 69$ | 1062.76 | $34645 \cdot 976$ | $5 \cdot 7096$ | $3 \cdot 1945$ |
| $32 \cdot 7$ | $102 \cdot 73$ | $839 \cdot 82$ | $1069 \cdot 29$ | $34965 \cdot 783$ | $5 \cdot 7183$ | $3 \cdot 1978$ |
| $32 \cdot 8$ | $103 \cdot 04$ | $844 \cdot 96$ | 1075-84 | $35287 \cdot 552$ | $5 \cdot 7271$ | $3 \cdot 2010$ |
| $32 \cdot 9$ | $103 \cdot 36$ | $8.0 \cdot 12$ | 1082.41 | $35611 \cdot 289$ | ¢ -7358 | $3 \cdot 2043$ |
| $33 \cdot 0$ | $103 \cdot 67$ | 855.30 | 1089.00 | 35937•000 | $5 \cdot 7446$ | $3 \cdot 2075$ |
| $33 \cdot 1$ | $103 \cdot 99$ | $860 \cdot 49$ | $1095 \cdot 61$ | $36264 \cdot 691$ | 5.7592 | $3 \cdot 2108$ |
| $33 \cdot 2$ | $104 \cdot 30$ | $865 \cdot 70$ | $1102 \cdot 24$ | $36594 \cdot 368$ | $5 \cdot 7619$ | $3 \cdot 2140$ |
| $33 \cdot 3$ | $104 \cdot 62$ | $870 \cdot 92$ | $1108 \cdot 89$ | $36926 \cdot 037$ | $5 \cdot 7706$ | $3 \cdot 2172$ |
| $33 \cdot 4$ | $104 \cdot 93$ | $876 \cdot 16$ | $1115 \cdot 56$ | $37259 \cdot 704$ | $5 \cdot 7792$ | $3 \cdot 2204$ |
| $33 \cdot 5$ | 105•24 | $881 \cdot 41$ | 1122.25 | $37595 \cdot 375$ | $5 \cdot 7879$ | $3 \cdot 2237$ |
| $33 \cdot 6$ | $105 \cdot 56$ | $886 \cdot 68$ | $1128 \cdot 96$ | $37933 \cdot 056$ | $5 \cdot 7965$ | $3 \cdot 2269$ |
| $33 \cdot 7$ | $105 \cdot 87$ | $891 \cdot 97$ | $1135 \cdot 69$ | $38272 \cdot 753$ | $5 \cdot 80.51$ | $3 \cdot 2301$ |
| $33 \cdot 8$ | $106 \cdot 19$ | $897 \cdot 27$ | $1142 \cdot 44$ | $38614 \cdot 472$ | $5 \cdot 8137$ | $3 \cdot 2332$ |
| $33 \cdot 9$ | $106 \cdot 50$ | $902 \cdot 59$ | $1149 \cdot 21$ | $38958 \cdot 219$ | $5 \cdot 8223$ | 3-2364 |
| $34 \cdot 0$ | $106 \cdot 81$ | $907 \cdot 92$ | $1156 \cdot 00$ | $39304 \cdot 000$ | $5 \cdot 8310$ | $3 \cdot 2396$ |
| $34 \cdot 1$ | $107 \cdot 13$ | $913 \cdot 27$ | $1162 \cdot 81$ | $39651 \cdot 821$ | 5.8395 | $3 \cdot 2428$ |
| $34 \cdot 2$ | $107 \cdot 44$ | $918 \cdot 63$ | $1169 \cdot 64$ | $40001 \cdot 688$ | $5 \cdot 8480$ | $3 \cdot 2460$ |
| $34 \cdot 3$ | $107 \cdot 76$ | $924 \cdot 01$ | $1176 \cdot 49$ | $40353 \cdot 607$ | $5 \cdot 8566$ | $3 \cdot 2491$ |
| $34 \cdot 4$ | $108 \cdot 07$ | $929 \cdot 41$ | $1183 \cdot 36$ | $40707 \cdot 584$ | $5 \cdot 8651$ | $3 \cdot 2522$ |
| 34.5 | $108 \cdot 38$ | $934 \cdot 82$ | $1190 \cdot 25$ | $41063 \cdot 625$ | 5.8736 | $3 \cdot 2554$ |
| $34 \cdot 6$ | 108.70 | $940 \cdot 25$ | $1197 \cdot 16$ | $41421 \cdot 736$ | $5 \cdot 8821$ | $3 \cdot 2586$ |
| $34 \cdot 7$ | $109 \cdot 01$ | $945 \cdot 69$ | $1204 \cdot 09$ | 41781.923 | $5 \cdot 8906$ | $3 \cdot 2617$ |
| $34 \cdot 8$ | $109 \cdot 33$ | $951 \cdot 15$ | $1211 \cdot 04$ | $42144 \cdot 192$ | $5 \cdot 8991$ | $3 \cdot 2648$ |
| $34 \cdot 9$ | $109 \cdot 64$ | $956 \cdot 62$ | $1218 \cdot 01$ | $42508 \cdot 549$ | $5 \cdot 9076$ | $3 \cdot 2679$ |

TABLES.
Table of Powers (continued).

| $n$ | $n \pi$ | $n^{2} \frac{\pi}{4}$ | $n^{2}$ | $n^{3}$ | $\sqrt{10}$ | $\sqrt[3]{n}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 35.0 | 109.96 | $962 \cdot 113$ | $1225 \cdot 00$ | 42875.000 | 5.9161 | $3 \cdot 2711$ |
| $35 \cdot 1$ | $110 \cdot 27$ | $967 \cdot 618$ | 1232.01 | 43243:551 | $5 \cdot 9245$ | $3 \cdot 2742$ |
| $35 \cdot 2$ | 110.58 | $973 \cdot 140$ | $1239 \cdot 04$ | $43614 \cdot 208$ | $5 \cdot 9330$ | $3 \cdot 2773$ |
| $35 \cdot 3$ | 110.90 | $978 \cdot 677$ | $1246 \cdot 09$ | 43986.977 | 5.9414 | $3 \cdot 2804$ |
| 3.54 | 111.21 | $984 \cdot 230$ | $1253 \cdot 16$ | $44361 \cdot 864$ | 5.9498 | 3-2835 |
| 35.5 | 111:53 | 989.798 | 1260.25 | $44738 \cdot 875$ | 5.9582 | $3 \cdot 2866$ |
| $35 \cdot 6$ | $111 \cdot 84$ | 995.382 | 1267*36 | $45118 \cdot 016$ | 5.9666 | $3 \cdot 2897$ |
| 35.7 | 112-15 | $1000 \cdot 98$ | 127449 | $45499 \cdot 293$ | 5.9749 | $3 \cdot 2927$ |
| 35.8 | 112.47 | 1006.60 | 1281.64 | $45882 \cdot 712$ | 5.9833 | 3.29.5 |
| 35.9 | 112.78 | 1012.23 | $1288 \cdot 81$ | $46268 \cdot 279$ | $5 \cdot 9917$ | $3 \cdot 2989$ |
| $36 \cdot 0$ | $113 \cdot 10$ | 1017•88 | 1296.00 | $46656 \cdot 000$ | $6 \cdot 0000$ | 3•3019 |
| $36 \cdot 1$ | $113 \cdot 41$ | 1023-54 | 1303:21 | 47045.881 | 6.0083 | 3-3050 |
| $36 \cdot 2$ | 113.73 | 1029 22 | $1310 \cdot 44$ | $47437 \cdot 928$ | 6.0166 | 3.3080 |
| $36 \cdot 3$ | 114.04 | 1034.91 | $1317 \cdot 69$ | 47832-147 | 6.0249 | $3 \cdot 3111$ |
| $36 \cdot 4$ | 114.35 | 1040.62 | 1324.96 | 48228:544 | $6 \cdot 0332$ | $3 \cdot 3141$ |
| 36.5 | 114.67 | 1046.35 | $1332 \cdot 25$ | $48627 \cdot 125$ | $6 \cdot 0415$ | $3 \cdot 3171$ |
| $36 \cdot 6$ | 114.98 | $1052 \cdot 09$ | 1339:56 | $49027 \cdot 896$ | 6.0498 | 3•3202 |
| 36.7 | 115.30 | 10.57-84 | $1346 \cdot 89$ | $49430 \cdot 8: 33$ | 6.0581 | 3-3232 |
| $36 \cdot 8$ | 115.61 | 1063•62 | 1354.24 | 49836.032 | $6 \cdot 0663$ | $3 \cdot 3262$ |
| 36.9 | 115.92 | 1069•41 | 1361.61 | $50243 \cdot 409$ | 6.0745 | $3 \cdot 3292$ |
| $37 \cdot 0$ | 116.24 | 1075.21 | 1369.00 | 506.53.000 | 6.0828 | 3.3322 |
| $37 \cdot 1$ | 116.5. | 1081-03 | $1376 \cdot 41$ | $51064 \cdot 811$ | 6.0910 | 3.33.52 |
| $37 \cdot 2$ | 116.87 | $1086 \cdot 87$ | 1383-84 | $51478 \cdot 848$ | $6 \cdot 0992$ | $3 \cdot 3382$ |
| $37 \cdot 3$ | 117-18 | 1092.72 | 1391-29 | $51895 \cdot 117$ | $6 \cdot 1074$ | $3 \cdot 3412$ |
| $37 \cdot 4$ | 117.50 | 1098:58 | 1398.76 | $52313 \cdot 624$ | $6 \cdot 1156$ | $3 \cdot 3442$ |
| 37:5 | $117 \cdot 81$ | 1104.47 | 1406.25 | $52734 \cdot 375$ | $6 \cdot 1237$ | $3 \cdot 3472$ |
| $37 \cdot 6$ | $118 \cdot 12$ | 1110:36 | $1413 \cdot 76$ | $53157 \cdot 376$ | $6 \cdot 1319$ | 3.3501 |
| $37 \cdot 7$ | $118 \cdot 44$ | 1116.28 | 1421.29 | 53582.633 | $6 \cdot 1400$ | 3•3531 |
| $37 \cdot 8$ | 118.75 | 1122-21 | $1428 \cdot 84$ | $54010 \cdot 152$ | $6 \cdot 1482$ | 3-3561 |
| $37 \cdot 9$ | $119 \cdot 07$ | 1128-15 | $1436 \cdot 41$ | $54439 \cdot 939$ | $6 \cdot 1563$ | 3.3590 |
| 38.0 | 119.38 | $1134 \cdot 11$ | $1444 \cdot 00$ | $54872 \cdot 000$ | $6 \cdot 1644$ | 3•3620 |
| $38 \cdot 1$ | $119 \cdot 69$ | $1140 \cdot 09$ | $1451 \cdot 61$ | 5.5306 .341 | $6 \cdot 1725$ | $3 \cdot 3649$ |
| $38 \cdot 2$ | $120 \cdot 01$ | 1146.08 | 1459.24 | 55742.968 | $6 \cdot 1806$ | $3 \cdot 3679$ |
| $38 \cdot 3$ | $120 \cdot 32$ | $1152 \cdot 09$ | $1466 \cdot 89$ | $56181 \cdot 887$ | $6 \cdot 1887$ | $3 \cdot 3708$ |
| 38.4 | $120 \cdot 64$ | $1158 \cdot 12$ | 1474:56 | $56623 \cdot 104$ | $6 \cdot 1968$ | $3 \cdot 3737$ |
| 38.5 | 120.95 | $1164 \cdot 16$ | 1482 25 | $57066 \cdot 625$ | $6 \cdot 2048$ | $3 \cdot 3767$ |
| $38 \cdot 6$ | $121 \cdot 27$ | $1170 \cdot 21$ | 1489.96 | $57512 \cdot 456$ | $6 \cdot 2129$ | $3 \cdot 3796$ |
| $38 \cdot 7$ | $121 \div 5$ | $1175 \cdot 28$ | $1497 \cdot 69$ | $57960 \cdot 603$ | $6 \cdot 2209$ | $3 \cdot 3825$ |
| $38 \cdot 8$ | $121 \cdot 89$ | 1182.37 | $1505 \cdot 44$ | $58411 \cdot 072$ | $6 \cdot 2290$ | $3 \cdot 3854$ |
| $38 \cdot 9$ | $122 \cdot 21$ | $1188 \cdot 47$ | $1513 \cdot 21$ | $58863 \cdot 869$ | $6 \cdot 2370$ | $3 \cdot 3883$ |
| $39 \cdot 0$ | 122.52 | 1194:59 | 1521.00 | $59319 \cdot 000$ | $6 \cdot 2450$ | $3 \cdot 3912$ |

TABLE of Powers (continued).

| $n$ | $n \pi$ | $n^{2} \frac{\pi}{4}$. | $n^{2}$ | $n^{3}$ | $\sqrt{n}$ | $\sqrt[3]{11}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $39 \cdot 1$ | 122.84 | $1200 \cdot 72$ | $1528 \cdot 81$ | 59776.471 | 6.2530 | $3 \cdot 3941$ |
| $39 \cdot 2$ | $123 \cdot 15$ | $1206 \cdot 87$ | $1536 \cdot 64$ | $60236 \cdot 288$ | 6.2610 | $3 \cdot 3970$ |
| $39 \cdot 3$ | $123 \cdot 46$ | $1213^{*} 04$ | $1544 \cdot 49$ | $60698 \cdot 457$ | $6 \cdot 2690$ | $3 \cdot 3999$ |
| $39 \cdot 4$ | $123 \cdot 78$ | $1219 \cdot 22$ | $1552 \cdot 36$ | $61162 \cdot 984$ | $6 \cdot 2769$ | $3 \cdot 4028$ |
| 39.5 | $124 \cdot 09$ | 122542 | $1560 \cdot 25$ | $61629 \cdot 875$ | 6-2849 | $3 \cdot 4056$ |
| $39 \cdot 6$ | $124 \cdot 41$ | $1231 \cdot 63$ | $1568 \cdot 16$ | $62099 \cdot 136$ | $6 \cdot 2929$ | $3 \cdot 4085$ |
| $39 \cdot 7$ | $124 \cdot 72$ | 123786 | $1576 \cdot 09$ | $62570 \cdot 773$ | $6 \cdot 3008$ | $3 \cdot 4114$ |
| $39 \cdot 8$ | $125 \cdot 04$ | $1244 \cdot 10$ | $1584 \cdot 04$ | $63044 \cdot 792$ | $6 \cdot 3087$ | $3 \cdot 4142$ |
| $39 \cdot 9$ | $125 \cdot 35$ | $1250 \cdot 36$ | 1592.01 | $63521 \cdot 199$ | 6-3166 | $3 \cdot 4171$ |
| $40 \cdot 0$ | 125.66 | $1256 \cdot 64$ | $1600 \cdot 00$ | $64000 \cdot 000$ | $6 \cdot 3246$ | $3 \cdot 4200$ |
| $40 \cdot 1$ | $125 \cdot 98$ | $1262 \cdot 93$ | $1608 \cdot 01$ | 64481•201 | $6 \cdot 3325$ | $3 \cdot 4228$ |
| $40 \cdot 2$ | $126 \cdot 29$ | $1269 \cdot 23$ | $1616 \cdot 04$ | $64964 \cdot 808$ | $6 \cdot 3404$ | $3 \cdot 4256$ |
| $40 \cdot 3$ | 126.61 | $1275 \cdot 56$ | $1624 \cdot 09$ | $65450 \cdot 827$ | $6 \cdot 3482$ | $3 \cdot 4285$ |
| $40 \cdot 4$ | $126 \cdot 92$ | $1281 \cdot 90$ | $1632 \cdot 16$ | $65939 \cdot 264$ | $6 \cdot 3561$ | $3 \cdot 4313$ |
| $40 \cdot 5$ | $127 \cdot 23$ | $1288 \cdot 25$ | $1640 \cdot 25$ | $66430 \cdot 125$ | $6 \cdot 3639$ | $3 \cdot 4341$ |
| $40 \cdot 6$ | $127 \cdot 55$ | $1294 \cdot 62$ | $1648 \cdot 36$ | $66923 \cdot 416$ | $6 \cdot 3718$ | $3 \cdot 4370$ |
| $40 \cdot 7$ | $127 \cdot 86$ | $1301 \cdot 00$ | $1656 \cdot 49$ | $67419 \cdot 143$ | $6 \cdot 3796$ | $3 \cdot 4398$ |
| $40 \cdot 8$ | 128•18 | $1307 \cdot 41$ | $1664 \cdot 64$ | $67911 \cdot 312$ | $6 \cdot 3875$ | $3 \cdot 4426$ |
| $40 \cdot 9$ | $128 \cdot 49$ | $1313 \cdot 82$ | $1672 \cdot 81$ | $68417 \cdot 929$ | $6 \cdot 3953$ | $3 \cdot 4454$ |
| $41 \cdot 0$ | $128 \cdot 81$ | $1320 \cdot 25$ | $1681 \cdot 00$ | $68921 \cdot 000$ | $6 \cdot 4031$ | $3 \cdot 4482$ |
| $41 \cdot 1$ | $129 \cdot 12$ | $1326 \cdot 70$ | $1689 \cdot 21$ | $69426 \cdot 531$ | 6.4109 | $3 \cdot 4510$ |
| $41 \cdot 2$ | $129 \cdot 43$ | $1333 \cdot 17$ | $1697 \cdot 44$ | $69934 \cdot 528$ | $6 \cdot 4187$ | $3 \cdot 4538$ |
| $41 \cdot 3$ | $129 \cdot 75$ | $1339 \cdot 65$ | $1705 \cdot 69$ | 70444.997 | $6 \cdot 4265$ | $3 \cdot 4566$ |
| $41 \cdot 4$ | $130 \cdot 06$ | $1346 \cdot 14$ | $1713 \cdot 96$ | 70957-944 | $6 \cdot 4343$ | $3 \cdot 4594$ |
| 41.5 | $130 \cdot 38$ | $1352 \cdot 65$ | $1722 \cdot 25$ | $71473 \cdot 375$ | $6 \cdot 4421$ | $3 \cdot 4622$ |
| $41 \cdot 6$ | $130 \cdot 69$ | $1359 \cdot 18$ | $1730 \cdot 56$ | $71991 \cdot 296$ | $6 \cdot 4498$ | $3 \cdot 4650$ |
| $41 \cdot 7$ | $131 \cdot 00$ | $1365 \cdot 72$ | $1738 \cdot 89$ | 72511.713 | $6 \cdot 4575$ | $3 \cdot 4677$ |
| $41 \cdot 8$ | $131 \cdot 32$ | $1372 \cdot 28$ | $1747 \cdot 24$ | $73034 \cdot 632$ | $6 \cdot 4653$ | $3 \cdot 4705$ |
| $41 \cdot 9$ | $131 \cdot 63$ | $1378 \cdot 85$ | $1755 \cdot 61$ | $73560 \cdot 059$ | 6.4730 | $3 \cdot 4733$ |
| $42 \cdot 0$ | $131 \cdot 95$ | 1385.44 | $1764 \cdot 00$ | 74088•000 | $6 \cdot 4807$ | $3 \cdot 4760$ |
| $42 \cdot 1$ | $132 \cdot 26$ | $1392 \cdot 05$ | $1772 \cdot 41$ | $74618 \cdot 461$ | $6 \cdot 4884$ | $3 \cdot 4788$ |
| $42 \cdot 2$ | $132 \cdot 58$ | $1398 \cdot 67$ | $1780 \cdot 84$ | $75151 \cdot 448$ | $6 \cdot 4961$ | $3 \cdot 4815$ |
| $42 \cdot 3$ | $132 \cdot 89$ | $1405 \cdot 31$ | $1789 \cdot 29$ | 75686.967 | 6.5038 | $3 \cdot 4843$ |
| $42 \cdot 4$ | $133 \cdot 20$ | $1411 \cdot 96$ | $1797 \cdot 76$ | $76225 \cdot 024$ | 6.5115 | $3 \cdot 4870$ |
| $42 \cdot 5$ | $133 \cdot 52$ | $1418 \cdot 63$ | $1806 \cdot 25$ | $76765 \cdot 625$ | 6:5192 | $3 \cdot 4898$ |
| $42 \cdot 6$ | $133 \cdot 83$ | $1425 \cdot 31$ | $1814 \cdot 76$ | $77308 \cdot 776$ | 6.0̃268 | $3 \cdot 4925$ |
| $42 \cdot 7$ | $134 \cdot 15$ | $1432 \cdot 01$ | $1823 \cdot 29$ | $77854 \cdot 483$ | $6 \cdot 5345$ | $3 \cdot 4952$ |
| $42 \cdot 8$ | $134 \cdot 46$ | $1438 \cdot 72$ | $1831 \cdot 84$ | $78402 \cdot 752$ | $6 \cdot 5422$ | $3 \cdot 4980$ |
| $42 \cdot 9$ | $134 \cdot 77$ | $1445 \cdot 45$ | $1840 \cdot 41$ | $78953 \cdot 589$ | $6 \cdot 5498$ | $3 \cdot 5007$ |
| $43 \cdot 0$ | 135.09 | $1452 \cdot 20$ | $1849 \cdot 00$ | $79507 \cdot 000$ | $6 \cdot 5574$ | $3 \cdot 5034$ |
| $43 \cdot 1$ | $135 \cdot 40$ | $1458 \cdot 96$ | $1857 \cdot 61$ | 80062-991 | $6 \cdot 5651$ | $3 \cdot 5061$ |

TABLE OF Powers (continued).

| $n$ | $n \pi$ | $n^{2} \frac{\pi}{4}$ | $n^{2}$ | $n^{3}$ | $\sqrt{13}$ | $\sqrt[3]{n}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $43 \cdot 2$ | $135 \cdot 72$ | 1465.74 | 1866.24 | $80621: 568$ | $6 \cdot 5727$ | 3 5088 |
| $43 \cdot 3$ | $136 \cdot 03$ | $1472 \cdot 54$ | 1874.89 | $81182 \cdot 737$ | 6.5803 | $3 \cdot 5115$ |
| $43 \cdot 4$ | $136 \cdot 35$ | $1479 \cdot 34$ | $1883 \cdot 56$ | $81746 \cdot 504$ | $6 \cdot 5879$ | $3 \cdot 5142$ |
| $43 \cdot 5$ | $136 \cdot 66$ | $1486 \cdot 17$ | 1892.25 | 82312.875 | $6 \cdot 5954$ | $3 \cdot 5169$ |
| $43 \cdot 6$ | $136 \cdot 97$ | $1493 \cdot 01$ | $1900 \cdot 96$ | 82881•856 | 6.6030 | 3•5196 |
| $43 \cdot 7$ | $137 \cdot 29$ | $1499 \cdot 87$ | $1909 \cdot 69$ | $83453 \cdot 453$ | $6 \cdot 6106$ | $3 \cdot 5223$ |
| $43 \cdot 8$ | $137 \cdot 60$ | $1506 \cdot 74$ | 1918.44 | $84027 \cdot 672$ | $6 \cdot 6182$ | $3 \cdot 5250$ |
| $43 \cdot 9$ | $137 \cdot 92$ | $1513 \cdot 63$ | $1927 \cdot 21$ | $84604 \cdot$ ¢19 | $6 \cdot 6257$ | $3 \cdot 5277$ |
| $44^{\cdot} 0$ | $138 \cdot 23$ | $1520 \cdot 03$ | $1936 \cdot 00$ | $85184 \cdot 000$ | $6 \cdot 6332$ | $3 \div 5303$ |
| $44 \cdot 1$ | $138 \cdot 54$ | $1527 \cdot 45$ | $1944 \cdot 81$ | $85766 \cdot 121$ | $6 \cdot 6408$ | 3:5330 |
| $44 \cdot 2$ | $138 \cdot 86$ | $1534 \cdot 39$ | $1953 \cdot 64$ | $86350 \cdot 888$ | $6 \cdot 6483$ | 3.5357 |
| $44 \cdot 3$ | $139 \cdot 17$ | $1541 \cdot 34$ | 1962.49 | $86938 \cdot 307$ | $6 \cdot 6558$ | $3 \cdot 5384$ |
| $44 \cdot 4$ | $139 \cdot 49$ | $1548 \cdot 30$ | 1971•36 | $87528 \cdot 384$ | $6 \cdot 6633$ | $3 \cdot 5410$ |
| $44 \cdot 5$ | $139 \cdot 80$ | $1555 \cdot 28$ | $1980 \cdot 25$ | $88121 \cdot 125$ | $6 \cdot 6708$ | $3 \cdot 5437$ |
| $44 \cdot 6$ | $140 \cdot 12$ | 1562.28 | $1989 \cdot 16$ | $88716 \cdot 536$ | $6 \cdot 6783$ | $3 \cdot 5463$ |
| $44 \cdot 7$ | $140 \cdot 43$ | $1569 \cdot 30$ | $1998 \cdot 09$ | $89314 \cdot 623$ | $6 \cdot 6858$ | 3-5490 |
| $44 \cdot 8$ | $140 \cdot 74$ | $1576 \cdot 33$ | $2007 \cdot 04$ | $89915 \cdot 392$ | $6 \cdot 6933$ | $3 \cdot 5.516$ |
| $44 \cdot 9$ | $141 \cdot 06$ | $1583 \cdot 37$ | 2016.01 | $90518 \cdot 849$ | $6 \cdot 7007$ | $3 \cdot 5.543$ |
| 45.0 | $141 \cdot 37$ | $1590 \cdot 43$ | $2025 \cdot 00$ | $91125 \cdot 000$ | $6 \cdot 7082$ | 35569 |
| $45 \cdot 1$ | $141 \cdot 69$ | 1597.51 | $2034 \cdot 01$ | $91733 \cdot 851$ | $6 \cdot 7157$ | $3 \cdot 5595$ |
| $45 \cdot 2$ | $142 \cdot 00$ | $1604 \cdot 60$ | $2043 \cdot 04$ | $92345 \cdot 408$ | 6.7231 | $3 \cdot 5622$ |
| $45 \cdot 3$ | $142 \cdot 31$ | $1611 \cdot 71$ | $2052 \cdot 09$ | $92959 \cdot 677$ | 6.7305 | $3 \cdot 5648$ |
| $45 \cdot 4$ | $142 \cdot 63$ | $1618 \cdot 83$ | $2061 \cdot 16$ | $93576 \cdot 664$ | $6 \cdot 7380$ | $3 \cdot 5674$ |
| 45.5 | $142 \cdot 94$ | $1625 \cdot 97$ | $2070 \cdot 25$ | $94196 \cdot 375$ | $6 \cdot 7454$ | $3 \cdot 5700$ |
| $45 \cdot 6$ | $143 \cdot 26$ | $1633 \cdot 13$ | $2079 \cdot 36$ | $94818 \cdot 816$ | 6.7528 | $3 \cdot 5726$ |
| $45 \cdot 7$ | $143 \cdot 57$ | $1640 \cdot 30$ | $2088 \cdot 49$ | $95443 \cdot 993$ | $6 \cdot 7602$ | $3 \cdot 5752$ |
| $45 \cdot 8$ | $143 \cdot 88$ | $1647 \cdot 48$ | $2097 \cdot 64$ | $96071 \cdot 912$ | $6 \cdot 7676$ | $3 \cdot 5778$ |
| 45.9 | $144 \cdot 20$ | $1654 \cdot 68$ | $2106 \cdot 81$ | $96702 \cdot 579$ | $6 \cdot 7750$ | $3 \cdot 5805$ |
| $46 \cdot 0$ | 144.51 | 1661.90 | $2116 \cdot 00$ | $97336 \cdot 000$ | $6 \cdot 7823$ | $3 \cdot 5830$ |
| $46 \cdot 1$ | 144.83 | $1669 \cdot 14$ | $2125 \cdot 21$ | $97972 \cdot 181$ | $6 \cdot 7897$ | $3 \cdot 556$ |
| $46 \cdot 2$ | $145 \cdot 14$ | 1676.39 | $2134 \cdot 44$ | $98611 \cdot 128$ | $6 \cdot 7971$ | $3 \cdot 5882$ |
| $46 \cdot 3$ | 145.46 | $1683 \cdot 65$ | $2143 \cdot 69$ | $99252 \cdot 847$ | $6 \cdot 8044$ | $3 \cdot 5908$ |
| $46 \cdot 4$ | $145 \cdot 77$ | $1690 \cdot 93$ | $2152 \cdot 96$ | $99897 \cdot 344$ | $6 \cdot 8118$ | $3 \cdot 5934$ |
| $46 \cdot 5$ | $146 \cdot 08$ | $1698 \cdot 23$ | $2162 \cdot 25$ | $100544 \cdot 625$ | $6 \cdot 8191$ | $3 \cdot 5960$ |
| $46 \cdot 6$ | $146 \cdot 40$ | $1705 \cdot 54$ | $2171 \cdot 56$ | $101194 \cdot 696$ | $6 \cdot 8264$ | $3 \cdot 5986$ |
| $46 \cdot 7$ | $146 \cdot 71$ | $1712 \cdot 87$ | $2180 \cdot 89$ | $101847 \cdot 563$ | $6 \cdot 8337$ | $3 \cdot 6011$ |
| $46 \cdot 8$ | $147 \cdot 03$ | $1720 \cdot 21$ | $2190 \cdot 24$ | 102503.232 | $6 \cdot 8411$ | $3 \cdot 6037$ |
| $46 \cdot 9$ | $147 \cdot 34$ | $1727 \cdot 57$ | $2199 \cdot 61$ | $103161 \cdot 709$ | $6 \cdot 8484$ | $3 \cdot 6063$ |
| $47 \cdot 0$ | $147 \cdot 65$ | 1734.94 | $2209 \cdot 00$ | 103823-000 | $6 \cdot 8557$ | $3 \cdot 6088$ |
| $47 \cdot 1$ | $147 \cdot 97$ | $1742 \cdot 34$ | $2218 \cdot 41$ | $104487 \cdot 111$ | $6 \cdot 8629$ | $3 \cdot 6114$ |
| $47 \cdot 2$ | $148 \cdot 28$ | $1749 \cdot 74$ | $2227 \cdot 84$ | $105154 \cdot 048$ | $6 \cdot 8702$ | $3 \cdot 6139$ |

Table of Powers (emntinued).

| $n$ | $n \pi$ | $n^{2} \frac{\pi}{4}$ | $n^{2}$ | $n^{3}$ | $\sqrt{n}$ | $\sqrt[3]{10}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 47.3 | $148 \cdot 60$ | $1757 \cdot 16$ | $2237 \cdot 29$ | $105823 \cdot 817$ | $6 \cdot 8775$ | $3 \cdot 6165$ |
| $47 \cdot 4$ | $148 \cdot 91$ | $1764 \cdot 60$ | 2246.76 | 106496.424 | $6 \cdot 8848$ | 3•6190 |
| 47.5 | $149 \cdot 23$ | 1772.05 | 2256.25 | 107171-875 | $6 \cdot 8920$ | 3•6216 |
| $47 \cdot 6$ | $149 \cdot 54$ | 1779-52 | 2265.76 | $107850 \cdot 176$ | $6 \cdot 8993$ | 3.6241 |
| $47 \cdot 7$ | $149 \cdot 85$ | $1787 \cdot 01$ | $2275 \cdot 29$ | 108531-333 | $6 \cdot 9065$ | 3•6267 |
| 47.8 | $150 \cdot 17$ | 1794.51 | $2284 \cdot 84$ | 109215.352 | 6.9138 | $3 \cdot 6292$ |
| 47.9 | $150 \cdot 48$ | 1802.03 | $2294 \cdot 41$ | 109902 239 | $6 \cdot 9209$ | 3•6317 |
| $48 \cdot 0$ | $150 \cdot 80$ | 1809.56 | $2304 \cdot 00$ | 110592.000 | $6 \cdot 9282$ | 3•6342 |
| $48 \cdot 1$ | 151•11 | $1817 \cdot 11$ | $2313 \cdot 61$ | $111284 \cdot 641$ | 6.9354 | 3•6368 |
| $48 \cdot 2$ | $151 \cdot 42$ | $1824 \cdot 67$ | 2323.24 | $111980 \cdot 168$ | 6.9426 | $3 \cdot 6393$ |
| $48 \cdot 3$ | $151 \cdot 74$ | 1832.25 | $2332 \cdot 89$ | 112678.587 | 6.9498 | 3.6418 |
| $48 \cdot 4$ | 152.05 | $1839 \cdot 84$ | 2342.56 | $113379 \cdot 904$ | 6.9570 | 3.6443 |
| 48.5 | $152 \cdot 37$ | 1847.45 | $2352 \cdot 25$ | 114084•125 | $6 \cdot 9642$ | $3 \cdot 6468$ |
| $48 \cdot 6$ | $152 \cdot 68$ | $1855 \cdot 08$ | 2361.96 | 114791-256 | 6.9714 | $3 \cdot 6493$ |
| $48 \cdot 7$ | $153 \cdot 00$ | 1862.72 | $2371 \cdot 69$ | 115501•303 | $6 \cdot 9785$ | $3 \cdot 6518$ |
| $48 \cdot 8$ | $153 \cdot 31$ | $1870 \cdot 38$ | $2381 \cdot 44$ | 116214-272 | 6.9857 | 3.6543 |
| $48 \cdot 9$ | $153 \cdot 62$ | 1878.05 | $2391 \cdot 21$ | 116930 169 | 6.9929 | 3.6568 |
| $49 \cdot 0$ | $153 \cdot 94$ | 1885.74 | $2401 \cdot 00$ | 117649•000 | $7 \cdot 0000$ | 3.6593 |
| $49 \cdot 1$ | $154 \cdot 25$ | 1893.45 | $2410 \cdot 81$ | $118370 \cdot 771$ | $7 \cdot 0071$ | $3 \cdot 6618$ |
| $49 \cdot 2$ | 154:57 | 1901*17 | $2420 \cdot 64$ | $119095 \cdot 488$ | $7 \cdot 0143$ | 3.6643 |
| $49 \cdot 3$ | 154.88 | $1908 \cdot 90$ | $2430 \cdot 49$ | $119823 \cdot 157$ | $7 \cdot 0214$ | $3 \cdot 6668$ |
| $49 \cdot 4$ | $155 \cdot 19$ | $1916 \cdot 65$ | $2440 \cdot 36$ | 120553.784 | $7 \cdot 0285$ | 3•6692 |
| 49\% | 155.51 | 1924-42 | $2450 \cdot 25$ | 121287-375 | $7 \cdot 0355$ | 3.6717 |
| $49 \cdot 6$ | $155 \cdot 82$ | 1932.21 | $2460 \cdot 16$ | $122023 \cdot 936$ | $7 \cdot 0427$ | $3 \cdot 6742$ |
| 49.7 | $156 \cdot 14$ | $1940 \cdot 00$ | $2470 \cdot 09$ | $122763 \cdot 473$ | $7 \cdot 0498$ | $3 \cdot 6767$ |
| $49 \cdot 8$ | $156 \cdot 45$ | $1947 \cdot 82$ | $2480 \cdot 04$ | $123505 \cdot 992$ | $7 \cdot 0569$ | $3 \cdot 6791$ |
| $49 \cdot 9$ | 156.77 | $1955 \cdot 65$ | 2490.01 | 124251•499 | 7-0640 | $3 \cdot 6816$ |
| 50.0 | $157 \cdot 08$ | 1963:50 | $2500 \cdot 00$ | $125000 \cdot 000$ | $7 \cdot 0711$ | $3 \cdot 6840$ |
| $51 \cdot 0$ | $160 \cdot 22$ | $2042 \cdot 82$ | 2601.00 | 132651•000 | 7-1414 | 3.7084 |
| $52 \cdot 0$ | $163 \cdot 36$ | $2123 \cdot 72$ | 2704.00 | 140608.000 | $7 \cdot 2111$ | 3.7325 |
| 53.0 | 166.50 | 2206•19 | $2809 \cdot 00$ | 148877.000 | $7 \cdot 2801$ | $3 \cdot 7563$ |
| $54 \cdot 0$ | $169 \cdot 64$ | 2290.22 | 2916.00 | 157464.000 | $7 \cdot 3485$ | $3 \cdot 7798$ |
| 55.0 | 172.78 | $2375 \cdot 83$ | 3025.00 | 166375.000 | $7 \cdot 4162$ | $3 \cdot 8030$ |
| 56.0 | 175.93 | $2463 \cdot 01$ | $3136 \cdot 00$ | 175616.000 | $7 \cdot 4833$ | 3.8259 |
| 57.0 | 179.07 | 2551.76 | $3249 \cdot 00$ | 185193•000 | $7 \cdot 5498$ | $3 \cdot 8485$ |
| 58.0 | 182.21 | 2642.08 | 3364.00 | 195112.000 | $7 \cdot 6158$ | $3 \cdot 8709$ |
| $59 \cdot 0$ | 185.35 | 2733.97 | 3481.00 | 205379.000 | $7 \cdot 6811$ | 3.8930 |
| $60 \cdot 0$ | 188.49 | $2827 \cdot 44$ | $3600 \cdot 00$ | $216000 \cdot 000$ | $7 \cdot 7460$ | 3.9149 |
| 61.0 | $191 \cdot 64$ | $2922 \cdot 47$ | 3721.00 | 226981•000 | $7 \cdot 8102$ | $3 \cdot 9365$ |
| 62.0 | $194 \cdot 77$ | 3019-07 | $3844 \cdot 00$ | 238328.000 | $7 \cdot 8740$ | $3 \cdot 9579$ |
| 63.0 | $197 \cdot 92$ | $3117 \cdot 25$ | $3969 \cdot 00$ | 250047•000 | $7 \cdot 9373$ | 3.9791 |

Table of Powers (continued).

| $n$ | $n \pi$ | $n^{2} \frac{\pi}{4}$ | $n^{2}$ | $n^{3}$ | $\sqrt{n}$ | $\sqrt[3]{n}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $64 \cdot 0$ | 201.06 | 3216.99 | $4096 \cdot 00$ | 262144*000 | $8 \cdot 0000$ | . 0000 |
| 65.0 | 204.20 | $3318 \cdot 31$ | $4225 \cdot 00$ | $274625 \cdot 000$ | $8 \cdot 0623$ | 0207 |
| $66^{\circ} 0$ | 207•34 | $3421 \cdot 20$ | $4356 \cdot 00$ | $287496 \cdot 000$ | $8 \cdot 1240$ | $4 \cdot 0412$ |
| $67 \cdot 0$ | $210 \cdot 49$ | $3525 \cdot 65$ | $4489 \cdot 00$ | $300763 \cdot 000$ | $8 \cdot 1854$ | $4 \cdot 0615$ |
| $68 \cdot 0$ | $213 \cdot 63$ | $3631 \cdot 68$ | $4624 \cdot 00$ | $314432 \cdot 000$ | $8 \cdot 2462$ | $4 \cdot 0817$ |
| $69 \cdot 0$ | 216.77 | $3739 \cdot 28$ | $4761 \cdot 00$ | $328509 \cdot 000$ | $8 \cdot 3066$ | $4 \cdot 1016$ |
| $70 \cdot 0$ | $219 \cdot 91$ | $3848 \cdot 45$ | $4900 \cdot 00$ | $343000 \cdot 000$ | $8 \cdot 3666$ | $4 \cdot 1213$ |
| $71 \cdot 0$ | $223 \cdot 05$ | $3959 \cdot 19$ | $5041 \cdot 00$ | $357911 \cdot 000$ | $8 \cdot 4261$ | $4 \cdot 1408$ |
| $72 \cdot 0$ | $226 \cdot 19$ | 4071.50 | $5184 \cdot 00$ | $373248 \cdot 000$ | $8 \cdot 4853$ | $4 \cdot 1602$ |
| $73 \cdot 0$ | $229 \cdot 34$ | $4185 \cdot 39$ | $5329 \cdot 00$ | $389017 \cdot 000$ | $8 \cdot 5440$ | $4 \cdot 1793$ |
| $74 \cdot 0$ | $232 \cdot 48$ | $4300 \cdot 84$ | 5476.00 | $405224 \cdot 000$ | $8 \cdot 6023$ | $4 \cdot 1983$ |
| $75 \cdot 0$ | $235 \cdot 62$ | $4417 \cdot 86$ | $5625 \cdot 00$ | $421875 \cdot 000$ | $8 \cdot 6603$ | $4 \cdot 2172$ |
| $76 \cdot 0$ | $238 \cdot 76$ | 4536.46 | $5776 \cdot 00$ | $438976 \cdot 000$ | $8 \cdot 7178$ | $4 \cdot 2358$ |
| $77 \cdot 0$ | $241 \cdot 90$ | $4656 \cdot 63$ | $5929 \cdot 00$ | $456533 \cdot 000$ | $8 \cdot 7750$ | $4 \cdot 2543$ |
| $78 \cdot 0$ | $245 \cdot 04$ | 4778.36 | $6084 \cdot 00$ | $474552 \cdot 000$ | $8 \cdot 83$ | 2727 |
| $79 \cdot 0$ | $248 \cdot 19$ | $4901 \cdot 67$ | 6241.00 | $493039 \cdot 000$ | $8 \cdot 8882$ | $4 \cdot 2908$ |
| $80 \cdot 0$ | 251-32 | 5026.55 | $6400 \cdot 00$ | $512000 \cdot 000$ | $8 \cdot 9443$ | $4 \cdot 3089$ |
| $81 \cdot 0$ | $2.54 \cdot 47$ | $5153 \cdot 00$ | $6561 \cdot 00$ ! | $531441 \cdot 000$ | $9 \cdot 0000$ | $4 \cdot 3267$ |
| $82 \cdot 0$ | $257 \cdot 61$ | 5281.02 | $6724 \cdot 00$ | $5.51368 \cdot 000$ | $9 \cdot 0554$ | $4 \cdot 3445$ |
| $83 \cdot 0$ | $260 \cdot 75$ | $5410 \cdot 61$ | $6889 \cdot 00$ | $571787 \cdot 000$ | $9 \cdot 1104$ | 4-3621 |
| $84 \cdot 0$ | $263 \cdot 89$ | $5541 \cdot 77$ | 7056.00 | $592704 \cdot 000$ | $9 \cdot 1652$ | $4 \cdot 3795$ |
| 85.0 | $267 \cdot 04$ | $5674 \cdot 50$ | $7225 \cdot 00$ | $614125 \cdot 000$ | $9 \cdot 2195$ | $4 \cdot 3968$ |
| 86.0 | $270 \cdot 18$ | $5808 \cdot 80$ | 7396.00 | $636056 \cdot 000$ | $9 \cdot 2736$ | $4 \cdot 4140$ |
|  | $273 \cdot 32$ | $5944 \cdot 68$ | $7569 \cdot 00$ | $658503 \cdot 000$ | $9 \cdot 3274$ | $4 \cdot 4310$ |
|  | $276 \cdot 46$ | 6082•12 | $7744 \cdot 00$ | $681472 \cdot 000$ | $9 \cdot 3808$ | $4 \cdot 4480$ |
| $89 \cdot 0$ | $279 \cdot 60$ | $6221 \cdot 14$ | $7921 \cdot 00$ | $704969 \cdot 000$ | $9 \cdot 4340$ | $4 \cdot 4647$ |
| $90 \cdot 0$ | 282.74 | $6361 \cdot 73$ | $8100 \cdot 00$ | $729000 \cdot 000$ | $9 \cdot 4868$ | $4 \cdot 4814$ |
| $91 \cdot 0$ | $285 \cdot 88$ | $6503 \cdot 88$ | $8281 \cdot 00$ | $753571 \cdot 000$ | $9 \cdot 5394$ | $4 \cdot 4979$ |
| $92 \cdot 0$ | $289 \cdot 03$ | $6647 \cdot 61$ | $8464 \cdot 00$ | $778688 \cdot 000$ | $9 \cdot 5917$ | $4 \cdot 5144$ |
| $93 \cdot 0$ | $292 \cdot 17$ | 6792.91 | $8649 \cdot 00$ | $804357 \cdot 000$ | $9 \cdot 6437$ | $4 \cdot 5307$ |
| $94 \cdot 0$ | $295 \cdot 31$ | 6939•78 | $8836 \cdot 00$ | $830584 \cdot 000$ | $9 \cdot 6954$ | $4 \cdot 5468$ |
| 95.0 | $298 \cdot 45$ | 7088-22 | $9025 \cdot 00$ | $857375 \cdot 000$ | $9 \cdot 7468$ | $4 \cdot 5629$ |
| $96 \cdot 0$ | $301 \cdot 59$ | $7238 \cdot 23$ | 9216.00 | $884736 \cdot 000$ | $9 \cdot 7980$ | $4 \cdot 5789$ |
| $97 \cdot 0$ | $304 \cdot 73$ | $7389 \cdot 81$ | $9409 \cdot 00$ | $912673 \cdot 000$ | $9 \cdot 8489$ | $4 \cdot 5947$ |
| $98 \cdot 0$ | $307 \cdot 88$ | 7542.96 | $9604 \cdot 00$ | 941192-000 | $9 \cdot 8995$ | $4 \cdot 6104$ |
| $99 \cdot 0$ | $311 \cdot 02$ | $7697 \cdot 69$ | $9801 \cdot 00$ | 970299.000 | $9 \cdot 9499$ | $4 \cdot 6261$ |
| $100 \cdot 0$ | $314 \cdot 16$ | 7853.98 | $10000 \cdot 00$ | $1000000 \cdot 000$ | $10 \cdot 0000$ | $4 \cdot 6416$ |

LENGTHS OF ARCS，CHORDS，ETC．
Table of Lengths of Circular Arcs，Chords，and Heights of Arcs to Radius 1.

|  |  | $\begin{aligned} & \text { 菦 } \\ & \text { 号 } \end{aligned}$ |  |  |  | ت゙ E゙ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.0175 | 0.0175 | $0 \cdot 0000$ | 36 | 0.6283 | $0 \cdot 6180$ | $0 \cdot 0489$ |
| 2 | 0.0349 | 0.0349 | $0 \cdot 0002$ | 37 | $0 \cdot 6458$ | 0．6346 | $0 \cdot 0517$ |
| 3 | $0 \cdot 0524$ | 0.0524 | $0 \cdot 0003$ | 38 | 0.6632 | 10．6511 | 0.0545 |
| 4 | $0 \cdot 0698$ | $0 \cdot 0698$ | $0 \cdot 0006$ | 39 | 0．6807 | 0.6676 | $0 \cdot 0574$ |
| 5 | $0.0873^{\circ}$ | $0 \cdot 0872$ | $0 \cdot 0010$ | 40 | $0 \cdot 6981$ | － $0 \cdot 6840$ | $0 \cdot 0603$ |
| 6 | $0 \cdot 1047$ | $0 \cdot 1047$ | $0 \cdot 0014$ | 41 | 0.7156 | 0．7004 | $0 \cdot 0633$ |
| 7 | 0．1222 | $0 \cdot 1221$ | $0 \cdot 0019$ | 42 | 0.7330 | 0.7167 | 0．0664 |
| 8 | $0 \cdot 1396$ | $0 \cdot 1395$ | $0 \cdot 0024$ | 43 | 0.7505 | 0.7330 | $0 \cdot 0696$ |
| 9 | $0 \cdot 1571$ | $0 \cdot 1569$ | $0 \cdot 0031$ | 44 | 0.7679 | $0 \cdot 7492$ | $0 \cdot 0728$ |
| 10 | $0 \cdot 1745$ | $0 \cdot 1743$ | 0．0038 | 45 | 0.7854 | 0．7654 | $0 \cdot 0761$ |
| 11 | 0．1920 | $0 \cdot 1917$ | $0 \cdot 0046$ | 46 | 0.8029 | 0.7815 | 0.0795 |
| 12 | 0．2094 | $0 \cdot 2091$ | 0．0055 | 47 | 0.8203 | $\bigcirc 0.7975$ | 0.0829 |
| 13 | $0 \cdot 2269$ | $0 \cdot 2264$ | $0 \cdot 0064$ | 48 | 0.8378 | 0.8135 | $0 \cdot 0865$ |
| 14 | $0 \cdot 2443$ | 0.2437 | $0 \cdot 0075$ | 49 | $0 \cdot 8552$ | 0．8294 | $0 \cdot 0900$ |
| 15 | $0 \cdot 2618$ | $0 \cdot 2611$ | $0 \cdot 0086$ | 50 | $0 \cdot 8727$ | 10．8452 | $0 \cdot 0937$ |
| 16 | $0 \cdot 2793$ | $0 \cdot 2783$ | $0 \cdot 0097$ | 51 | 0.8901 | 0.8610 | $0 \cdot 0974$ |
| 17 | $0 \cdot 2967$ | $0 \cdot 2956$ | $0 \cdot 0110$ | 52 | 0.9076 | 0.8767 | 0－1012 |
| 18 | $0 \cdot 3142$ | $0 \cdot 3129$ | 0.0123 | 53 | 0.9250 | 0．8924 | $0 \cdot 1051$ |
| 19 | $0 \cdot 3316$ | $0 \cdot 3301$ | 0.0137 | 54 | 0.9425 | 10.9080 | 0－1090 |
| 20 | $0 \cdot 3491$ | 0.3473 | 0.0152 | 55 | 0.9599 | ｜0．9235 | $0 \cdot 1130$ |
| 21 | $0 \cdot 3665$ | $0 \cdot 3645$ | $0 \cdot 0167$ | 56 | 0.9774 | 10.9389 | $0 \cdot 1171$ |
| 22 | $0 \cdot 3840$ | $0 \cdot 3816$ | 0.0184 | 57 | 0.9948 | 0．9543 | $0 \cdot 1212$ |
| 23 | $0 \cdot 4014$ | $0 \cdot 3987$ | $0 \cdot 0201$ | 58 | $1 \cdot 0123$ | 0 | $0 \cdot 1254$ |
| 24 | $0 \cdot 4189$ | $0 \cdot 4158$ | $0 \cdot 0219$ | 59 | $1 \cdot 0297$ | 0．9848 | $0 \cdot 1296$ |
| 25 | $0 \cdot 4363$ | $0 \cdot 4329$ | $0 \cdot 0237$ | 60 | $1 \cdot 0472$ | $1 \cdot 0000$ | $0 \cdot 1340$ |
| 26 | $0 \cdot 4538$ | $0 \cdot 4499$ | $0 \cdot 0256$ | 61 | $1 \cdot 0647$ | 1.0151 | $0 \cdot 1384$ |
| 27 | $0 \cdot 4712$ | $0 \cdot 4669$ | $0 \cdot 0276$ | 62 | $1 \cdot 0821$ | 1.0301 | $0 \cdot 1428$ |
| 28 | $0 \cdot 4887$ | $0 \cdot 4838$ | $0 \cdot 0297$ | 63 | $1 \cdot 0996$ | $1 \cdot 0450$ | $0 \cdot 1474$ |
| 29 | 0.5061 | $0 \cdot 5008$ | 0.0319 | 64 | $1 \cdot 1170$ | 1.0598 | $0 \cdot 1520$ |
| 30 | $0 \cdot 5236$ | 0.5176 | $0 \cdot 0341$ | 65 | $1 \cdot 1345$ | 1.0746 | $0 \cdot 1566$ |
| 31 | 0.5411 | 0.5345 | $0 \cdot 0364$ | 66 | 1－1519 | 1.0893 | $0 \cdot 1613$ |
| 32 | 0.5585 | 0.5512 | 0.0387 | 67 | 1－1694 | 1－1039 | $0 \cdot 1661$ |
| 33 | 0.5760 | 0：5680 | $0 \cdot 0412$ | 68 | $1 \cdot 1868$ | $1 \cdot 1184$ | $0 \cdot 1710$ |
| 34 | $0 \cdot 5934$ | 0.5847 | 0.0437 | 69 | $1 \cdot 2043$ | 1－1328 | $0 \cdot 1759$ |
| 35 | 0.6109 | 0.6014 | 0.0463 | 70 | $1 \cdot 2217$ | 1－1472 | 0．1808 |

Table of Lengths of Circular Arcs, Chords, and Heights of Arcs to Radius 1 (continued).

|  |  | $\begin{aligned} & \text { प्ँ } \\ & \text { ठु } \end{aligned}$ |  |  |  | \% |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 71 | $1 \cdot 2392$ | $1 \cdot 1614$ | $0 \cdot 18.59$ | 106 | $1 \cdot 8500$ | 1:5972 | $0 \cdot 3982$ |
| 72 | $1 \cdot 2566$ | $1 \cdot 1756$ | - 1910 | 107 | $1 \cdot 8675$ | $1 \cdot 6077$ | $0 \cdot 4052$ |
| 73 | $1 \cdot 2741$ | $1 \cdot 1896$ | $0 \cdot 1961$ | 108 | $1 \cdot 8850$ | $1 \cdot 6180$ | $0 \cdot 4122$ |
| 74 | $1 \cdot 2915$ | $1 \cdot 2036$ | $0 \cdot 2014$ | 109 | $1 \cdot 9024$ | 1-6282 | $0 \cdot 4193$ |
| 75 | $1 \cdot 3090$ | $1 \cdot 2175$ | $0 \cdot 2066$ | 110 | $1 \cdot 9198$ | $1 \cdot 6383$ | $0 \cdot 4264$ |
| 76 | $1 \cdot 3265$ | $1 \cdot 2313$ | $0 \cdot 2120$ | 111 | 1.9373 | $1 \cdot 6483$ | 0.4336 |
| 77 | $1 \cdot 3439$ | $1 \cdot 2450$ | $0 \cdot 2174$ | 112 | 1.9548 | 1.6581 | 0.4408 |
| 78 | $1 \cdot 3614$ | $1 \cdot 2586$ | $0 \cdot 2229$ | 113 | 1.9722 | $1 \cdot 6678$ | $0 \cdot 4481$ |
| 79 | $1 \cdot 3788$ | $1 \cdot 2722$ | $0 \cdot 2284$ | 114 | $1 \cdot 9897$ | 1.6773 | $0 \cdot 4554$ |
| 80 | $1 \cdot 3963$ | $1 \cdot 2856$ | $0 \cdot 2340$ | 115 | $2 \cdot 0071$ | $1 \cdot 6868$ | $0 \cdot 4627$ |
| 81 | $1 \cdot 4137$ | $1 \cdot 2989$ | $0 \cdot 2396$ | 116 | $2 \cdot 0246$ | $1 \cdot 6961$ | 0.4701 |
| 82 | $1 \cdot 4312$ | $1 \cdot 3121$ | $0 \cdot 2453$ | 117 | $2 \cdot 0420$ | 1.7053 | $0 \cdot 4775$ |
| 83 | $1 \cdot 4486$ | $1 \cdot 325.2$ | $0 \cdot 2510$ | 118 | $2 \cdot 0595$ | $1 \cdot 7143$ | $0 \cdot 4850$ |
| 84 | $1 \cdot 4661$ | $1 \cdot 3383$ | $0 \cdot 2569$ | 119 | $2 \cdot 0769$ | 1.7233 | $0 \cdot 4925$ |
| 85 | $1 \cdot 4835$ | $1 \cdot 3512$ | $0 \cdot 2627$ | 120 | $2 \cdot 0944$ | $1 \cdot 7321$ | $0 \cdot 5000$ |
| 86 | $1 \cdot 5010$ | 1-3640 | $0 \cdot 2686$ | 121 | $2 \cdot 1118$ | $1 \cdot 7407$ | 0:5076 |
| 87 | 1.5184 | $1 \cdot 3767$ | $0 \cdot 2746$ | 122 | $2 \cdot 1293$ | 1.7492 | 0.5152 |
| 88 | 1•0559 | $1 \cdot 3893$ | $0 \cdot 2807$ | 123 | $2 \cdot 1468$ | 1.7576 | 0.5228 |
| 89 | 1.5533 | $1 \cdot 4018$ | $0 \cdot 2867$ | 124 | $2 \cdot 1642$ | $1 \cdot 7659$ | 0.5305 |
| 90 | 1.5708 | 1.4142 | 02.229 | 125 | $2 \cdot 1817$ | $1 \cdot 7740$ | 0.5383 |
| 91 | 1.5882 | $1 \cdot 4265$ | $0 \cdot 2991$ | 126 | $2 \cdot 1991$ | $1 \cdot 7820$ | 0.5460 |
| 92 | $1 \cdot 6057$ | 1.4387 | $0 \cdot 3053$ | 127 | $2 \cdot 2166$ | 1.7899 | 0.5538 |
| 93 | 1-6232 | $1 \cdot 4507$ | $0 \cdot 3116$ | 128 | $2 \cdot 2340$ | 1.7976 | 0.5616 |
| 94 | $1 \cdot 6406$ | $1 \cdot 4627$ | $0 \cdot 3180$ | 129 | $2 \cdot 2545$ | $1 \cdot 8052$ | 0.5695 |
| 95 | 1.6580 | $1 \cdot 4746$ | $0 \cdot 3244$ | 130 | $2 \cdot 2689$ | 1-8126 | 0.5774 |
| 96 | $1 \cdot 6755$ | $1 \cdot 4863$ | $0 \cdot 3309$ | 131 | $2 \cdot 2864$ | 1.8199 | 0.5853 |
| 97 | 1.6930 | $1 \cdot 4979$ | $0 \cdot 3374$ | 132 | $2 \cdot 3038$ | 1-8271 | $0 \cdot 5933$ |
| 98 | 1.7104 | 1 -5094 | $0 \cdot 3439$ | 133 | $2 \cdot 3213$ | $1 \cdot 8341$ | $0 \cdot 6013$ |
| 99 | 1.7279 | 1-5208 | $0 \cdot 3506$ | 134 | $2 \cdot 3387$ | $1 \cdot 8410$ | $0 \cdot 6093$ |
| 100 | 1.7453 | 1 -5321 | $0 \cdot 3572$ | 135 | 2-3562 | $1 \cdot 8478$ | 0.6173 |
| 101 | 1.7628 | 1:5432 | $0 \cdot 3639$ | 136 | $2 \cdot 3736$ | $1 \cdot 8544$ | $0 \cdot 6254$ |
| 102 | 1.78032 | $1 \div 5543$ | $0 \cdot 3707$ | 137 | 2.3911 | $1 \cdot 8608$ | $0 \cdot 6335$ |
| 103 | $1 \cdot 7977$ | $1 \cdot 5652$ | 0.3775 | 138 | $2 \cdot 4086$ | $1 \cdot 8672$ | $0 \cdot 6416$ |
| 104 | $1 \cdot 8151$ | $1 \cdot 5760$ | $0 \cdot 3843$ | 139 | $2 \cdot 4260$ | 1.8733 | $0 \cdot 6498$ |
| 105 | $1 \cdot 8326$ | $1 \div 5867$ | $0 \cdot 3912$ | 140 | $2 \cdot 4435$ | 1.8794 | $0 \cdot 6580$ |

Table of Levgths of Circular Arcs, Chords, and Heights of arcs to Radius 1 (continued).

|  |  | $\begin{aligned} & \text { 苞 } \\ & \text { تٍ } \end{aligned}$ |  |  |  | \% |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 141 | $2 \cdot 4609$ | 1.8853 | $0 \cdot 6662$ | 161 | $2 \cdot 8100$ | 1.9726 | 0.8350 |
| 142 | $2 \cdot 4784$ | $1 \cdot 8910$ | $0 \cdot 6744$ | 162 | $2 \cdot 8274$ | $1 \cdot 9754$ | $0 \cdot 8436$ |
| 143 | $2 \cdot 4958$ | $1 \cdot 8966$ | $0 \cdot 6827$ | 163 | $2 \cdot 8449$ | 1.9780 | $0 \cdot 8522$ |
| 144 | 2.5133 | 1.9021 | $0 \cdot 6910$ | 164 | $2 \cdot 8623$ | 1.9805 | $0 \cdot 8608$ |
| 145 | $2 \cdot 5307$ | $1 \cdot 9074$ | $0 \cdot 6993$ | 165 | $2 \cdot 8798$ | 1.9829 | $0 \cdot 8695$ |
| 146 | 2.5482 | 1.9126 | 0.7076 | 166 | $2 \cdot 8972$ | 1.98 .51 | 0.8781 |
| 147 | 2.5656 | 1.9176 | 0.7160 | 167 | 2.9147 | 1.9871 | $0 \cdot 8868$ |
| 148 | 2.5831 | 1.9225 | 0.7244 | 168 | $2 \cdot 9322$ | $1 \cdot 9890$ | $0 \cdot 8955$ |
| 149 | $2 \cdot 6005$ | 1.9273 | 0.7328 | 169 | $2 \cdot 9496$ | 1.9908 | 0.9042 |
| 150 | 2-6180 | 1.9319 | $0 \cdot 7412$ | 170 | $2 \cdot 9671$ | $1 \cdot 9924$ | $0 \cdot 9128$ |
| 151 | $2 \cdot 6354$ | $1 \cdot 9363$ | $0 \cdot 7496$ | 171 | $2 \cdot 9845$ | $1 \cdot 9938$ | $0 \cdot 9215$ |
| 152 | $2 \cdot 6529$ | $1 \cdot 9406$ | 0.7581 | 172 | $3 \cdot 0020$ | 1.9951 | 0.9302 |
| 153 | $2 \cdot 6704$ | $1 \cdot 9447$ | $0 \cdot 7666$ | 173 | $3 \cdot 0194$ | 1.9963 | $0 \cdot 9390$ |
| 154 | $2 \cdot 6878$ | $1 \cdot 9487$ | 0.7750 | 174 | 3•0369 | $1 \cdot 9973$ | $0 \cdot 9477$ |
| 155 | $2 \cdot 7053$ | 1.9526 | 0.7836 | 175 | $3 \cdot 0543$ | 1.9981 | 0.9564 |
| 156 | $2 \cdot 7227$ | $1 \cdot 9563$ | 0.7921 | 176 | $3 \cdot 0718$ | 1.9988 | $0 \cdot 9651$ |
| 157 | $2 \cdot 7402$ | 1.9598 | $0 \cdot 8006$ | 177 | $3 \cdot 0892$ | 1.9993 | 0.9738 |
| 158 | $2 \cdot 7576$ | $1 \cdot 9632$ | $0 \cdot 8092$ | 178 | $3 \cdot 1067$ | 1.9997 | $0 \cdot 9825$ |
| 159 | $2 \cdot 7751$ | $1 \cdot 9665$ | 0.8178 | 179 | $3 \cdot 1241$ | 1.9999 | 0.9913 |
| 160 | $2 \cdot 7925$ | 1.9696 | $0 \cdot 8264$ | 180 | $3 \cdot 1416$ | $2 \cdot 0000$ | $1 \cdot 0000$ |

Example.-If we have an arc " $b d c$ " of a circle whose radii $a b$ or $a c=1$, subtending an angle of $60^{\circ}$, the

Length of arc $b d c \quad . \quad=1 \cdot 0472$
Chord $b c$. . . $=1 \cdot 0000$
Height $f d$ of arc $\quad=0.1340$


Table of Natural Sines and Tangents to Radius 1.


Table of Natural Sines and Tangents (continucd).

| Deg. | Sine. |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $0^{\prime}$ | $10^{\prime}$ | $20^{\circ}$ | 30 | $40^{\prime}$ | $50^{\prime}$ |  |
| 38 | 0.616 | 0.618 | 0.620 | 0.623 | 0.625 | 0.627 | 51 |
| 39 | $0 \cdot 629$ | $0 \cdot 632$ | 0.634 | $0 \cdot 636$ | 0.638 | $0 \cdot 641$ | 50 |
| 40 | $0 \cdot 643$ | $0 \cdot 645$ | $0 \cdot 647$ | $0 \cdot 649$ | $0 \cdot 652$ | 0.654 | 49 |
| 41 | $0 \cdot 656$ | 0.658 | 0.660 | 0.663 | $0 \cdot 665$ | 0.667 | 48 |
| 42 | $0 \cdot 669$ | $0 \cdot 671$ | 0.673 | 0.676 | $0 \cdot 678$ | $0 \cdot 680$ | 47 |
| 43 | $0 \cdot 682$ | 0.684 | $0 \cdot 686$ | 0.688 | $0 \cdot 690$ | 0.693 | 46 |
| 44 | $0 \cdot 695$ | $0 \cdot 697$ | 0.699 | 0.701 | 0.703 | 0.705 | 45 |
| 45 | $0 \cdot 707$ |  |  |  |  |  | 44 |
|  | $60^{\prime}$ | $50^{\prime}$ | $40^{\prime}$ | $30^{\prime}$ | $20^{\prime}$ | $10^{\prime}$ |  |
|  | Cosine. |  |  |  |  |  | D. |
| Deg. | Cosine. |  |  |  |  |  |  |
|  | $0^{\prime}$ | $10^{\prime}$ | $20^{\prime}$ | $30^{\prime}$ | $40^{\prime}$ | $50^{\prime}$ |  |
| 0 | 1.000 | 1.000 | 1.000 | $1 \cdot 000$ | $1 \cdot 000$ | $1 \cdot 000$ | 89 |
| 1 | $1 \cdot 000$ | 1.000 | $1 \cdot 000$ | $1 \cdot 000$ | $1 \cdot 000$ | 0.999 | 88 |
| 2 | 0.999 | 0.999 | 0.999 | 0.999 | 0.999 | 0.999 | 87 |
| 3 | 0.999 | 0.998 | 0.998 | 0.998 | 0.998 | $0 \cdot 998$ | 86 |
| 4 | 0.998 | 0.997 | 0.997 | 0.997 | 0.997 | 0.996 | 85 |
| 5 | 0.996 | 0.996 | 0.996 | 0.995 | 0.995 | 0.995 | 84 |
| 6 | 0.995 | 0.994 | 0.994 | 0.994 | 0.993 | 0.993 | 83 |
| 7 | 0.993 | 0.992 | 0.992 | 0.991 | 0.991 | 0.991 | 82 |
| 8 | 0.990 | 0.990 | 0.989 | 0.989 | 0.989 | 0.988 | 81 |
| 9 | 0.988 | 0.987 | 0.987 | 0.986 | 0.986 | 0.985 | 80 |
| 10 | 0.985 | 0.984 | 0.984 | 0.983 | 0.983 | $0 \cdot 982$ | 79 |
| 11 | 0.982 | 0.981 | 0.981 | 0.980 | 0.979 | 0.979 | 78 |
| 12 | 0.978 | 0.978 | 0.977 | 0.976 | 0.976 | 0.975 | 77 |
| 13 | 0.974 | 0.974 | 0.973 | 0.972 | 0.972 | 0.971 | 76 |
| 14 | 0.970 | 0.970 | 0.969 | $0 \cdot 968$ | $0 \cdot 967$ | $0 \cdot 967$ | 75 |
| 15 | 0.966 | 0.965 | 0.964 | $0 \cdot 964$ | $0 \cdot 963$ | $0 \cdot 962$ | 74 |
| 16 | 0.961 | 0.960 | 0.960 | 0.959 | 0.958 | 0.957 | 73 |
| 17 | 0.956 | $0 \cdot 955$ | $0 \cdot 95$ ธ | 0.954 | $0 \cdot 953$ | 0.952 | 72 |
| 18 | 0.951 | $0 \cdot 950$ | 0.949 | 0.948 | $0 \cdot 947$ | $0 \cdot 946$ | 71 |
| 19 | 0.946 | $0 \cdot 945$ | 0.944 | 0.943 | 0.942 | 0.941 | 70 |
| 20 | 0.940 | 0.939 | 0.938 | 0.937 | 0.936 | 0.935 | 69 |
| 21 | 0.934 | 0.933 | 0.931 | 0.930 | 0.929 | 0.928 | 68 |
| 22 | $0 \cdot 927$ | $0 \cdot 926$ | $0 \cdot 925$ | 0.924 | 0.923 | 0.922 | 67 |
|  | $60^{\prime}$. | $50^{\prime}$ | $40^{\prime}$ | $30^{\prime}$ | $20^{\prime}$ | $10^{\prime}$ |  |
|  | Sine. |  |  |  |  |  | D. |

Table of Natural Sines and Tangents (continued).

| Deg. | Cosine. |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $0^{\prime}$ | $10^{\prime}$ | $20^{\prime}$ | $30^{\prime}$ | $40^{\prime}$ | $50^{\prime}$ |  |
| 23 | 0.921 | 0.919 | 0.918 | 0.917 | 0.916 | 0.915 | 66 |
| 24 | 0.914 | 0.912 | 0.911 | 0.910 | 0.909 | 0.908 | 65 |
| 25 | 0.906 | $0 \cdot 905$ | 0.904 | 0.903 | 0.901 | 0.900 | 64 |
| 26 | 0.899 | 0.898 | 0.896 | 0.895 | 0.894 | $0 \cdot 892$ | 63 |
| 27 | 0.891 | $0 \cdot 890$ | 0.888 | 0.887 | $0 \cdot 886$ | 0.884 | 62 |
| 28 | 0.883 | 0.882 | 0.880 | 0.879 | 0.877 | $0 \cdot 876$ | 61 |
| 29 | 0.875 | 0.873 | 0.872 | $0 \cdot 870$ | 0.869 | $0 \cdot 867$ | 60 |
| 30 | 0.866 | 0.865 | 0.863 | $0 \cdot 862$ | $0 \cdot 860$ | 0.859 | 59 |
| 31 | 0.857 | 0.856 | $0 \cdot 854$ | 0.853 | 0.851 | 0.850 | 58 |
| 32 | 0.848 | 0.847 | 0.845 | 0.843 | 0.842 | 0.840 | 57 |
| 33 | 0.839 | 0.837 | 0.835 | 0.834 | 0.832 | 0.831 | 56 |
| 34 | 0.829 | 0.827 | 0.826 | 0.824 | 0.822 | $0 \cdot 821$ | 55 |
| 35 | 0.819 | $0 \cdot 817$ | 0.816 | 0.814 | 0.812 | 0.811 | 54 |
| 36 | 0.809 | $0 \cdot 807$ | 0.806 | $0 \cdot 804$ | 0.802 | 0.800 | 53 |
| 37 | 0.799 | 0.797 | 0.795 | 0.793 | 0.792 | 0.790 | 52 |
| 38 | 0.788 | 0.786 | 0.784 | 0.783 | 0.781 | 0.779 | 51 |
| 39 | 0.777 | 0.775 | 0.773 | 0.772 | 0.770 | $0 \cdot 768$ | 50 |
| 40 | 0.766 | 0.764 | 0.762 | 0.760 | 0.759 | 0.757 | 49 |
| 41 | 0.755 | 0.753 | 0.751 | 0.749 | 0.747 | 0.745 | 48 |
| 42 | 0.743 | 0.741 | 0.739 | 0.737 | 0.735 | 0.733 | 47 |
| 43 | 0.731 | 0.729 | 0.727 | 0.72 .5 | 0.723 | 0.721 | 46 |
| 44 | 0.719 | 0.717 | 0.715 | 0.713 | 0.711 | $0 \cdot 709$ | 45 |
| 45 | $0 \cdot 707$ |  |  |  |  |  | 44 |
|  | $60^{\prime}$ | $50^{\prime}$ | $40^{\prime}$ | $30^{\prime}$ | $20^{\circ}$ | $10^{\prime}$ |  |
|  | Sine. |  |  |  |  |  | D. |

For angles under $90^{\circ}$.-For sine and tang. add the diff. for cosine and cotang. Subtract diff.
Lx. sine $25^{\circ} 17^{\prime}$. cosine $25^{\circ} 17^{\prime}$.

| $\begin{gathered} 25^{\circ} 10^{\prime}= \\ 428-425=3 \end{gathered}$ | $0 \cdot 4$ | $\begin{array}{r} 25^{\circ} 10^{\prime}= \\ 90.5-904=1 \end{array}$ | $0 \cdot 9050$ |
| :---: | :---: | :---: | :---: |
| Dif. $3 \times 7^{\prime}=$ | 21 | Dif. $1 \times 7^{\prime}=$ | 7 |
|  | 0.4271 |  | $0 \cdot 9043$ |

Versed sine.-From 1 take the nat. cosine.
Co-versed sine.-From 1 take the nat. sine.
Secant.-Divide 1 by the nat. cosine.
Cosecant.-Divide 1 by the nat. sine.

Table of Natural Sines and Tangents (continued).

| Deg. | Tang. |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $0^{\prime}$ | $10^{\prime}$ | $20^{\prime}$ | $30^{\prime}$ | $40^{\prime}$ | $50^{\prime}$ |  |
| 0 | 0.000 | 0.003 | 0.006 | 0.009 | 0.012 | 0.015 | 89 |
| 1 | 0.017 | 0.020 | 0.023 | $0 \cdot 026$ | 0.029 | 0.032 | 88 |
| 2 | 0.035 | 0.038 | 0.041 | 0.044 | 0.047 | 0.049 | 87 |
| 3 | 0.052 | 0.05 .5 | 0.058 | 0.061 | 0.064 | 0.067 | 86 |
| 4 | $0 \cdot 070$ | 0.073 | $0 \cdot 076$ | $0 \cdot 079$ | $0 \cdot 082$ | 0.085 | 85 |
| 5 | 0.087 | 0.090 | 0.093 | $0 \cdot 096$ | $0 \cdot 099$ | $0 \cdot 102$ | 84 |
| 6 | 0.105 | $0 \cdot 108$ | $0 \cdot 111$ | $0 \cdot 114$ | $0 \cdot 117$ | $0 \cdot 120$ | 83 |
| 7 | $0 \cdot 123$ | $0 \cdot 126$ | $0 \cdot 129$ | $0 \cdot 132$ | $0 \cdot 135$ | $0 \cdot 138$ | 82 |
| 8 | $0 \cdot 141$ | $0 \cdot 144$ | $0 \cdot 146$ | $0 \cdot 149$ | $0 \cdot 152$ | $0 \cdot 155$ | 81 |
| 9 | $0 \cdot 158$ | $0 \cdot 161$ | $0 \cdot 164$ | $0 \cdot 167$ | $0 \cdot 170$ | $0 \cdot 173$ | 80 |
| 10 | $0 \cdot 176$ | 0.179 | $0 \cdot 182$ | $0 \cdot 185$ | $0 \cdot 188$ | 0.191 | 79 |
| 11 | 0.194 | $0 \cdot 197$ | $0 \cdot 200$ | $0 \cdot 203$ | $0 \cdot 206$ | $0 \cdot 210$ | 78 |
| 12 | $0 \cdot 213$ | $0 \cdot 216$ | $0 \cdot 219$ | $0 \cdot 222$ | $0 \cdot 225$ | $0 \cdot 228$ | 77 |
| 13 | $0 \cdot 231$ | $0 \cdot 234$ | $0 \cdot 237$ | $0 \cdot 240$ | $0 \cdot 243$ | $0 \cdot 246$ | 76 |
| 14 | $0 \cdot 249$ | $0 \cdot 252$ | $0 \cdot 256$ | $0 \cdot 259$ | $0 \cdot 262$ | $0 \cdot 265$ | 75 |
| 15 | $0 \cdot 268$ | $0 \cdot 271$ | $0 \cdot 274$ | $0 \cdot 277$ | 0.280 | 0.284 | 74 |
| 16 | $0 \cdot 287$ | $0 \cdot 290$ | $0 \cdot 293$ | $0 \cdot 296$ | 0.299 | $0 \cdot 303$ | 73 |
| 17 | $0 \cdot 306$ | $0 \cdot 309$ | $0 \cdot 312$ | $0 \cdot 315$ | $0 \cdot 318$ | $0 \cdot 322$ | 72 |
| 18 | 0.325 | $0 \cdot 328$ | 0.331 | $0 \cdot 335$ | $0 \cdot 338$ | $0 \cdot 341$ | 71 |
| 19 | $0 \cdot 344$ | $0 \cdot 348$ | $0 \cdot 351$ | $0 \cdot 354$ | $0 \cdot 357$ | $0 \cdot 361$ | 70 |
| 20 | $0 \cdot 364$ | $0 \cdot 367$ | $0 \cdot 371$ | $0 \cdot 374$ | $0 \cdot 377$ | $0 \cdot 381$ | 69 |
| 21 | $0 \cdot 384$ | $0 \cdot 387$ | 0.391 | $0 \cdot 394$ | 0.397 | $0 \cdot 401$ | 68 |
| 22 | $0 \cdot 404$ | $0 \cdot 407$ | $0 \cdot 411$ | $0 \cdot 414$ | $0 \cdot 418$ | $0 \cdot 421$ | 67 |
| 23 | $0 \cdot 424$ | $0 \cdot 428$ | $0 \cdot 431$ | 0.435 | 0.438 | $0 \cdot 442$ | 66 |
| 24 | $0 \cdot 445$ | $0 \cdot 449$ | $0 \cdot 452$ | $0 \cdot 456$ | $0 \cdot 459$ | $0 \cdot 463$ | 65 |
| 25 | $0 \cdot 466$ | $0 \cdot 470$ | $0 \cdot 473$ | $0 \cdot 477$ | 0.481 | $0 \cdot 484$ | 64 |
| 26 | $0 \cdot 488$ | 0.491 | $0 \cdot 495$ | $0 \cdot 499$ | 0:502 | 0.506 | 63 |
| 27 | 0.510 | 0.513 | 0:517 | $0 \cdot 521$ | 0.524 | 0.528 | 62 |
| 28 | 0.532 | 0.535 | 0:539 | 0.543 | 0.547 | 0.551 | 61 |
| 29 | 0.5554 | 0:558 | 0:562 | 0.566 | 0:570 | 0.573 | 60 |
| 30 | 0:577 | 0.581 | 0:585 | 0:589 | 0.593 | 0.597 | 59 |
| 31 | $0 \cdot 601$ | 0.605 | $0 \cdot 609$ | 0.613 | $0 \cdot 617$ | 0.621 | 58 |
| 32 | $0 \cdot 625$ | 0.629 | $0 \cdot 633$ | 0.637 | 0.641 | $0 \cdot 645$ | 57 |
| 33 | 0.649 | 0.654 | $0 \cdot 658$ | $0 \cdot 662$ | $0 \cdot 666$ | 0.670 | 56 |
| 34 | $0 \cdot 675$ | $0 \cdot 679$ | $0 \cdot 683$ | 0.687 | 0.692 | 0.696 | 55 |
| 35 | 0.700 | $0 \cdot 705$ | 0.709 | 0.713 | 0.718 | 0.722 | 54 |
| 36 | 0.727 | 0.731 | 0.735 | 0.740 | 0.744 | 0.749 | 53 |
| 37 | 0.754 | 0.758 | 0.763 | 0.767 | 0.772 | 0.777 | 52 |
|  | $60^{\prime}$ | $50^{\prime}$ | $40^{\prime}$ | $30^{\prime}$ | $20^{\prime}$ | $10^{\prime}$ |  |
|  |  |  |  |  |  |  | D. |

Table of Natural Sines and Tangents (continued).


Table of Natural Sines and Tangents-(continued).

| Deg. | Cotang. |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $0^{\prime}$ | $10^{\prime}$ | $20^{\prime}$ | $30^{\prime}$ | $40^{\prime}$ | $50^{\prime}$ |  |
| 23 | $2 \cdot 356$ | 2.337 | $2 \cdot 318$ | 2•300 | 2.282 | $2 \cdot 264$ | 66 |
| 24 | $2 \cdot 246$ | 2-229 | $2 \cdot 211$ | $2 \cdot 194$ | $2 \cdot 177$ | $2 \cdot 161$ | 65 |
| 25 | $2 \cdot 145$ | $2 \cdot 128$ | $2 \cdot 112$ | $2 \cdot 097$ | 2.081 | $2 \cdot 066$ | 64 |
| 26 | $2 \cdot 050$ | $2 \cdot 035$ | $2 \cdot 020$ | $2 \cdot 006$ | 1.991 | 1.977 | 63 |
| 27 | 1.963 | 1.949 | 1.935 | 1.921 | 1.907 | 1.894 | 62 |
| 28 | 1.881 | 1.868 | 1.85.5 | 1.842 | 1.829 | $1 \cdot 816$ | 61 |
| 29 | $1 \cdot 804$ | 1.792 | $1 \cdot 780$ | 1.767 | 1.756 | 1.744 | 60 |
| 30 | 1.732 | 1.720 | $1 \cdot 709$ | 1.698 | 1.686 | $1 \cdot 675$ | 59 |
| 31 | $1 \cdot 664$ | $1 \cdot 653$ | 1•643 | $1 \cdot 632$ | $1 \cdot 621$ | $1 \cdot 611$ | 58 |
| 32 | $1 \cdot 600$ | 1.590 | 1.580 | 1\%570 | $1 \cdot 560$ | $1 \cdot 550$ | 57 |
| 33 | 1:540 | 1.530 | $1 \cdot 520$ | 1.511 | 1:501 | $1 \cdot 492$ | 56 |
| 34 | $1 \cdot 483$ | $1 \cdot 473$ | $1 \cdot 464$ | $1 \cdot 455$ | $1 \cdot 446$ | $1 \cdot 437$ | 55 |
| 35 | $1 \cdot 428$ | $1 \cdot 419$ | $1 \cdot 411$ | $1 \cdot 402$ | 1-393 | $1 \cdot 385$ | 54 |
| 36 | $1 \cdot 376$ | $1 \cdot 368$ | $1 \cdot 360$ | $1 \cdot 351$ | $1 \cdot 343$ | $1 \cdot 335$ | 53 |
| 37 | 1-327 | $1 \cdot 319$ | $1 \cdot 311$ | $1 \cdot 303$ | $1 \cdot 295$ | $1 \cdot 288$ | 52 |
| 38 | $1 \cdot 280$ | $1 \cdot 272$ | $1 \cdot 265$ | $1 \cdot 257$ | 1.2.50 | $1 \cdot 242$ | 51 |
| 39 | $1 \cdot 235$ | 1.228 | $1 \cdot 220$ | $1 \cdot 213$ | 1-206 | $1 \cdot 199$ | 50 |
| 40 | $1 \cdot 192$ | 1-185 | 1-178 | $1 \cdot 171$ | 1-164 | $1 \cdot 157$ | 49 |
| 41 | $1 \cdot 150$ | 1-144 | 1•137 | $1 \cdot 130$ | 1-124 | $1 \cdot 117$ | 48 |
| 42 | $1 \cdot 111$ | 1-104 | 1.098 | 1.091 | 1.085 | $1 \cdot 079$ | 47 |
| 43 | 1.072 | $1 \cdot 066$ | $1 \cdot 060$ | 1.054 | $1 \cdot 048$ | $1 \cdot 042$ | 46 |
| 44 | 1.036 | 1.030 | $1 \cdot 024$ | 1.018 | 1.012 | 1.006 | 45 |
| 45 | 1.000 |  |  |  |  |  | 44 |
|  | $60^{\prime}$ | $50^{\prime}$ | $40^{\prime}$ | $30^{\prime}$ | $20^{\prime}$ | $10^{\prime}$ |  |
|  | Tang. |  |  |  |  |  | D. |

Ex. Tang. $55^{\circ} 27^{\prime}$.

$$
55^{\circ} 20^{\prime}=1 \cdot 446
$$

$$
455-446=9
$$

$$
\text { Dif. } 9 \times 7=63+
$$

$$
\overline{1 \cdot 4523}
$$

Ex. $\quad$ Cot. $28^{\circ} 16^{\prime}$.

$$
\begin{array}{cl}
28^{\circ} 10^{\prime} & =1.868 \\
868-85.5=13 & = \\
\text { Dif. } 13 \times 6 & \frac{78}{1.8602}
\end{array}
$$

For angles exceeding $90^{\circ}$ : to find the sine, cosine, tangent, cotang., secant or cosec. (but not the versed sine), take the angle from $180^{\circ}$; if between $180^{\circ}$ and $270^{\circ}$ take $180^{\circ}$ from the angle ; if between $270^{\circ}$ and $360^{\circ}$ take the angle from $360^{\circ}$, and take the remainder from the table. For the versed sine : if between $90^{\circ}$ and $270^{\circ}$ add cosine to 1 ; if between $270^{\circ}$ and $360^{\circ}$ take cosine from 1.

Table showing the Underlie and Perpendicular in Feet and Inches to every Degree of the Quadrant, in Six Feet = One Fathom.

| Deg. | Base. | Perpendicular. | Deg. | Deg. | Base. | Perpendicular. | Deg. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | Ft. Ins. | Ft. Ins. | 90 | 23 | Ft. Ins. <br> $5 \quad 6 \frac{1}{4}$ | Ft. Ins. | 67 |
| 1 | $6 \quad 0$ | $0{ }^{0} 11 \frac{1}{4}$ | 89 | 24 | 56 | $25 \frac{1}{4}$ | 66 |
| 2 | $511 \frac{3}{4}$ | 0 | 88 | 25 | $5 \quad 5 \frac{1}{4}$ | $26^{\frac{3}{8}}$ | 65 |
| 3 | $511 \frac{2}{3}$ | 0 3 ${ }^{3}$ | 87 | 26 | 5 5 $4 \frac{3}{4}$ | $27 \frac{1}{2}$ | 64 |
| 4 | $511 \frac{5}{8}$ | 05 | 86 | 27 | 5 4i | 288 | 63 |
| 5 | $511 \frac{1}{2}$ | 0 0 61 | 85 | 28 | $5 \quad 3 \frac{5}{8}$ | $2{ }^{2} 97$ | 62 |
| 6 | $511 \frac{3}{8}$ | 0 7 ${ }^{1}$ | 84 | 29 | 53 | 211 | 61 |
| 7 | $511 \frac{1}{4}$ | 088 | 83 | 30 | $5 \quad 2{ }^{5}$ | 30 | 60 |
| 8 | $511 \frac{1}{8}$ | 010 | 82 | 31 | $51 \frac{3}{4}$ | 31 | 59 |
| 9 | 511 | 011 | 81 | 32 | 51 | $3{ }^{3} 12$ | 58 |
| 10 | $510 \frac{7}{8}$ | $10 \frac{1}{4}$ | 80 | 33 | $5 \quad 0 \frac{1}{2}$ | $3{ }^{1}$ | 57 |
| 11 | 5) $10 \frac{5}{8}$ | $1{ }^{1} 1{ }^{\frac{3}{4}}$ | 79 | 34 | $411 \frac{3}{4}$ | 3 41 | 56 |
| 12 | $510 \frac{3}{8}$ | 13 | 78 | 35 | 411 | $3{ }^{3} 5$ | 55 |
| 13 | $510 \frac{1}{8}$ | 14 | 77 | 36 | $410 \frac{1}{4}$ | $3{ }^{31}$ | 54 |
| 14 | 597 | $1{ }^{5} 5$ | 76 | 37 | $4{ }^{4} 9$ | $3{ }^{3} \mathbf{7 1}$ | 53 |
| 15 | ${ }_{5}^{5} \quad 95$ | $16 \frac{1}{2}$ | 75 | 38 | 487 | 381 | 52 |
| 16 | $59 \frac{1}{4}$ | 18 | 74 | 39 | 48 | 3 918 | 51 |
| 17 | 588 | 19 | 73 | 40 | 4 7 ${ }^{\frac{1}{4}}$ | $310 \frac{1}{8}$ | 50 |
| 18 | $58 \frac{1}{2}$ | $110 \frac{1}{4}$ | 72 | 41 | 4 6i | $311 \frac{1}{8}$ | 49 |
| 19 | 588 | $111 \frac{3}{8}$ | 71 | 42 | $45^{5}$ | 40 | 48 |
| 23 | $5 \quad 7 \frac{3}{4}$ | $20 \frac{1}{2}$ | 70 | 43 | $44^{\frac{3}{4}}$ | 41 | 47 |
| 21 | 571 | $2{ }^{2} \quad 1 \frac{3}{4}$ | 69 | 44 | $4 \quad 4$ | $4 \quad 2$ | 46 |
| 22 | $5 \quad 63$ | 23 | 68 | 45 | 43 | 43 | 45 |
|  | Ft. Ins. | Ft. Ins. |  |  | Ft. Ins. | Ft. Ins. |  |
| Deg. | Perpendicular. | Base. | Deg. | Deg. | Perpendicular. | Base. | Deg. |

This table is calculated for the quadrant taking its angles from the horizon.

When the angle exceeds $45^{\circ}$, read from foot of table and take base and perpendicular marked there.

Example.-Angle $25^{\circ}$, length 9 fm .3 ft . See opposite $25^{\circ}$, $5^{\prime} 5 \frac{1^{\prime \prime}}{4} \times 9 \mathrm{fm} .3 \mathrm{ft} .=51^{\prime} 7 \frac{7}{8}^{\prime \prime}$ for base and $2^{\prime} 6 \frac{3}{8}{ }^{\prime \prime} \times 9 \mathrm{fm} .3 \mathrm{ft}$. $=$ $24 \cdot 0_{16} \frac{3}{16} \mathrm{fm}$. perpendicular.

Compartson of Angle Degrees and Slope.

| Angle. | Slope. |  | Angle. | Slope. |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Angle. | Slope. |  |  |  |
|  | 1 in 19.08 | $10^{\circ}$ | 1 in 5.67 | $17^{\circ}$ | 1 in 3.27 |
| $4^{\circ}$ | 1 in 14.30 | $11^{\circ}$ | 1 in 5.14 | $18^{\circ}$ | 1 in 3.07 |
| $5^{\circ}$ | 1 in 11.43 | $12^{\circ}$ | 1 in 4.70 | $19^{\circ}$ | 1 in 2.90 |
| $6^{\circ}$ | 1 in 9.51 | $13^{\circ}$ | 1 in 4.33 | $20^{\circ}$ | 1 in 2.74 |
| $7^{\circ}$ | 1 in 8.14 | $14^{\circ}$ | 1 in 4.01 | $25^{\circ}$ | 1 in 2.14 |
| $8^{\circ}$ | 1 in | 7.11 | $15^{\circ}$ | 1 in 3.73 | $30^{\circ}$ |
| $9^{\circ}$ | 1 in 6.31 | $16^{\circ}$ | 1 in 3.48 |  |  |

Table of Inclined Measure. (G. G. André.)
Showing the reduction in links and decimals of a link to be made per chain for every half-degree of inclination from $3^{\circ}$ to $30^{\circ}(100 \times$ versed side of the inclination).

| Angle. | Reduction. | Angle | Reduction. | Angle. | Reduction. |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Links. |  | Links. |  | Links. |
| 30 | $0 \cdot 15$ | 1230 | $2 \cdot 37$ | 2130 | $6 \cdot 96$ |
| 330 | $0 \cdot 19$ | 130 | $2 \cdot 56$ | 220 | $7 \cdot 28$ |
| 40 | $0 \cdot 24$ | 1330 | $2 \cdot 76$ | 2230 | $7 \cdot 61$ |
| 430 | $0 \cdot 31$ | 140 | $2 \cdot 97$ | 230 | $7 \cdot 95$ |
| 50 | $0 \cdot 38$ | 1430 | $3 \cdot 19$ | 2330 | $8 \cdot 29$ |
| 530 | $0 \cdot 46$ | 150 | $3 \cdot 41$ | 240 | $8 \cdot 65$ |
| 60 | $0 \cdot 55$ | 1530 | $3 \cdot 64$ | 2430 | 9.01 |
| 630 | $0 \cdot 64$ | 160 | $3 \cdot 87$ | 250 | $9 \cdot 37$ |
| 70 | $0 \cdot 75$ | 1630 | $4 \cdot 12$ | 2530 | $9 \cdot 74$ |
| 730 | $0 \cdot 86$ | 170 | $4 \cdot 37$ | 260 | $10 \cdot 13$ |
| 80 | $0 \cdot 97$ | 1730 | $4 \cdot 63$ | 2630 | 10.51 |
| 830 | $1 \cdot 10$ | 180 | $4 \cdot 89$ | 270 | 10.90 |
| 90 | $1 \cdot 23$ | 1830 | $5 \cdot 17$ | 2730 | $11 \cdot 30$ |
| 930 | $1 \cdot 37$ | 190 | $5 \cdot 45$ | 280 | 11.71 |
| $10 \quad 0$ | $1 \cdot 53$ | 1930 | $5 \cdot 74$ | 2830 | $12 \cdot 11$ |
| 1030 | $1 \cdot 67$ | 200 | $6 \cdot 03$ | 290 | 12.53 |
| 110 | $1 \cdot 84$ | 2030 | $6 \cdot 33$ | 2930 | 12.96 |
| 1130 | $2 \cdot 01$ | 210 | $6 \cdot 64$ | $30 \quad 0$ | $13 \cdot 40$ |
| 120 | $2 \cdot 19$ |  |  |  |  |

Example.-An incline of $19^{\circ}$ is 12 chains 25 links long, what is the horizontal distance?

In column of angles, opposite $19^{\circ}$, we find 5.45 monks, this $\times 12$ chains $=65 \cdot 40$ links.

Since 25 links $=\frac{1}{4}$ of a chain, $5 \cdot 45$ links $\div 4=1 \cdot 36$ links.
65.40 links $+1 \cdot 36$ links $=66 \cdot 76$ links, which must be reduced from the original length.
12 chains 25 links -66.76 links $=11$ chains 58.24 links, the true horizonta ldistance.

## WEIGHTS AND MEASURES.

Avoirdupois Weight.


Troy Weight.

| Systematic <br> Name. | Grain. <br> gr. | Penny- <br> weight. <br> dwt. | Ounce. <br> oz. | Pound. <br> lb. | Metric <br> equivalent <br> (grammes). |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Grain <br> gr. <br> Pennyweight <br> dwt. | 1 | 0.04167 | 0.002083 | 0.0001736 | 0.0648 |  |
| Ounce <br> oz. <br> Pound <br> lb. | 480 | 20 | 1 | 0.05 | 0.004167 | 1.555 |

1 gr. troy avoirdupois and apothecaries are equal.
Troy weight is used for gold and silver. Perfectly pure gold is worth £4 $4 s .11 \cdot 45 d$., or $\$ 20 \cdot 67183$ per troy oz. Fine gold is said to be 24 -carat. Standard gold is 22 -carat alloyed with two parts of some other metal. Standard silver is 11 oz . 2 dwt. fine to 18 dwt . alloy.

The jeweller's carat is 3.17 gr . in England, $3 \cdot 18$ gr. in France, 3.0 gr . in Holland, and 3.2 gr . in the United States; the carat is divided into 4 jeweller's grains, and the jewellery ounce into $151 \frac{1}{2}$ carats.

Apothecaries' Weight.

| Systematic Name. | Grain. gr. | $\underset{Э}{\text { Scruple }}$ | ${ }_{3}^{\text {Dram. }}$ | Ounce. ${ }^{3}$ | Pound. <br> lb. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Grain gr. | 1 | 0.05 | 0.016 | $0 \cdot 002083$ | $0 \cdot 00017361$ |
| Scruple | 20 | 1 | $0 \cdot 3$ | $0 \cdot 0416$ | $0 \cdot 003472$ |
| $\underset{3}{\text { Dram }}$ | 60 | 3 | 1 | $0 \cdot 125$ | $0 \cdot 010416$ |
| Ounce | -480 | 24 | 8 | 1 | $0 \cdot 083$ |
| Pound lb. | 5760 | 288 | 96 | 12 | 1 |

In troy and apothecaries' weights the grain, ounce, and pound are the same. Used for medical prescriptions. Drugs are bought and sold in quantities by avoirdupois.

Apothecaries' Fluid Measurf.
60 minims ( $m$ ) . . $=1$ fluid drachm f 3 .
8 drachms . . . $=1$ ounce f 3.

20 ounces . . $=1$ pint 0 .
8 pints . . . $=1$ gallon gal.
1 drop . . . . $=1$ grain.
60 drops . . . . $=1$ drachm.
4 drachms . . $=1$ tablespoonful.
2 ounces . . . . $=1$ wineglassful.
3 ounces . . . . $=1$ teacupful.

Liquid Measure, U.S. only.
4 gills $\quad .=1$ pint $\quad=28.875$ cub. in.
2 pints . . $=1$ quart $=57.750$ "
4 quarts . . $=1$ gallon . $=231.000$ "
63 gallons . . $=1$ hogshead.
2 hogsheads . = 1 pipe or butt.
2 pipes . . $=1$ tun.

Dry Measure, U.S. only.
2 pints . $=1$ quart . . $=67 \cdot 2006$ cub. in.
4 quarts . $=1$ gallon . . $=268 \cdot 8025$ "
2 gallons . $=1$ peck . $=537.60500$ "
4 pecks . $=1$ struck bushel $=2150 \cdot 4200$,

## Old Diggers' Measure.

1 dish $=$ about 572 cub. in. $=1$ two-gall. household bucket.
2 two-gal. household buckets = 1 nail can.
4 nail cans . . . $=1$ tub.
1 tub . . . . . $=\frac{1}{2}$ a porter cask.
10 tubs . . . . $=1$ load.
1 load . . . . . = notquite 1 cub. yard loosegravel.
120 dishes . . . $=1$ cub. yard in situ.

British Imperial Measure of Capacity.

| Syster.atic Name. | Gill. | Pint. | Quart. | Pottle. | Gallon. | Peck. | Bushel. | Coomb. | Quarter. | Cub. Ft. | Litres. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Gill | 1 | 0.25 | $0 \cdot 125$ | . 0625 | -03125 | -015625 | $\cdot 003906$ | -0009765 | -0004882 | 0.005 | $0 \cdot 1419$ |
| Pint | 4 | 1 | $0 \%$ | $0 \cdot 25$ | $0 \cdot 125$ | 0.0625 | 0.01562 | -003905 | $0 \cdot 00195$ | 0.02 | 0.5676 |
| Quart | 8 | 2 | 1 | 0.55 | 0.25 | $0 \cdot 125$ | -03125 | -0078125 | -003906 | 0.04 | 1-1352 |
| Pottle | 16 | 4 | 2 | 1 | 0.5 | $0 \cdot 25$ | 0.0625 | -015625 | . 007812 | 0.08 | $2 \cdot 2704$ |
| Gallon | 32 | 8 | 4 | 2 | 1 | $0 \cdot 5$ | $0 \cdot 125$ | -03125 | 0.0156 | $0 \cdot 1604$ | $4 \cdot 541$ |
| Peck | 64 | 16 | 8 | 4 | 2 | 1 | $0 \cdot 25$ | -0625 | 0.03125 | 0.3208 | $9 \cdot 082$ |
| Bushel | 256 | 64 | 32 | 16 | 8 | 4 | 1 | $0 \cdot 25$ | $0 \cdot 125$ | $1 \cdot 283$ | $36 \cdot 32816$ |
| Coomb | 1024 | 256 | 128 | 64 | 32 | 16 | 4 | 1 | $0 \cdot 5$ | 5.132 | $145 \cdot 31264$ |
| Quarter | 2048 | 512 | 256 | 128 | 64 | 32 | 8 | 2 | 1 | 10.264 | 290.625 |




Galls.
9
18
36
54
72
108
10 lbs. distilled water $=2774$ cub. in. $=0.16$ cub. $\mathrm{ft} .=1$ gallon.


Long Measure.


Square or Surface Measure, for Land, Boards, Painting. Paving, Plastering, \&C.

|  | Sq. in. | Sq. ft. | Sq. yd. | Sq. pl. | Sq. ch. | Ro. | Ac. | Value in sq.metres |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 Square foot. | 144 | 1 | $0 \cdot 111$ | 0.00367309 | $0 \cdot 000229568$ | 8.000091827 0 | 0.0000229568 | -092894 |
| 1 Square yard. | 1296 | 9 | 1 | 0.0330578 | 0.00206611 | 0.00082644 | $0 \cdot 000206611$ | -836046 |
| $\left\{\begin{array}{r} 1 \text { Square pole } \\ \text { or rod } \end{array}\right\}$ | 39204 | $272\}$ | 304 | 1 | 0.0625 | 0.025 | 0.00625 | 25.302915 |
| 1 Square chain | 627264 | 4356 | 484 | 16 | 1 | $0 \cdot 4$ | $0 \cdot 1$ | 404•8466 |
| 1 Rood . | 1568160 | 10890 | 1210 | 40 | $2{ }^{\frac{1}{2}}$ | 1 | $0 \cdot 25$ | 1012-1166 |
| 1 Acre | 6272640 | 43560 | 4840 | 160 | 10 | 4 | 1 | 4048.4664 |
| 1 Square mile | 4014489600 | 27878400 | 3097600 | 102400 | 6400 | 2560 | 640 | 2591018-49 |

Cubic or Solid Measure, for Timber, Stone, Boxes, Packages, Rooms. \&C.

|  | Cub. in. | Cub. ft. | Cub. yd. | Value in cub. metre |
| :---: | :---: | :---: | :---: | :---: |
| 1 Cubic foot | 1728 | 1 | 0.057 | $\cdot 02881$ |
| 1 Cubic yard | 46656 | 27 | I | $\cdot 76437$ |

1 ton or load $=40$ cubic feet of rough or 50 cubic feet of hewn timber.

1 shipping ton $=42$ cubic feet of timber ; 1 ton shipping $=$ 40 cubic feet.

1 stack of wood $=108$ cubic feet; 1 cord of wood $=128$ cubic feet $=$ a pile 4 ft . high, 4 ft . wide, and 8 feet long; 1 cord foot is a foot in length of such a pile.

1 register ton $=100$ cubic feet; 1 cubic yard of ordinary earth is called a load; 1 board foot is 1 ft . long, 1 ft . wide, and 1 in. thick ; 12 board feet $=1$ cubic foot ; a barrel's bulk $=50$ cubic feet; 1 cubic foot of water $=$ about $6 \frac{1}{4}$ gallons $=$ 62.321 lbs. ; 1 gallon $=277 \frac{1}{4}$ cub. in. $=0.16$ cubic feet.

1 ton weight of shingle $. \quad=$ about 23 cubic feet.

|  |  | coarse |  | " | 19 | " |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | pit sand | = | " | 22 | ", |  |
|  |  | clay or marl | $=$ | " | 18 | , |  |

Calculate 100 tons of coal per insh per acre, which allows about $25 \%$ for loss of every kind.
Carpenters', Bricklayers', and Builders'
Measurements.

| Stock bricks | . | $8 \frac{3}{4}$ | inches $\times$ | $4 \frac{1}{4} \times 2 \frac{3}{4}$. |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Welsh fire-bricks | . | . | 9 | $\times$ | $4 \frac{1}{2} \times 2 \frac{3}{4}$. |  |
| Dutch clinkers | . | $-9 \frac{1}{4}$ | $\#$ | $\times$ | 3 | $\times 1 \frac{1}{2}$. |

500 bricks $=$ a load. $\quad 5$ courses of bricks in the height of a wall are called a foot. 1 rod of brickwork $=306$ cubic feet $=$ $11 \frac{1}{3}$ cubic yards, and contains about 4,500 bricks with about 75 cubic feet of mortar.

## Measure of Timber.

Boards of 7 in. wide $=$ battens.

$$
\begin{array}{rrrl}
" & 9 & =\text { deals. } \\
" & 12 & & =\text { planks. }
\end{array}
$$

100 superficial feet of planking . = 1 square.
120 deals . . . . . . = 1 hundred.

50 cub. ft. squared timber . . . $=1$ load.
40 cub. ft. unhewn timber . . = 1 load.
600 superficial feet of inch planking $=1$ load.
Props are bought and sold per 72 running feet, the price depending on the diameter.

Sizes of Slates.


60 seconds . . $=1$ minute.
60 minutes . . $=1$ degree.
30 degrees . . $=1$ sign.
90 degrees. . . $=1$ quadrant.
4 quadrants or $360^{\circ}=1$ circumference or great circle.

## Power.

A kilogrammetre $=7 \cdot 23308$ foot pounds.
A foot pound $=0.138254$ kilogrammetre.
A British horse-power $=550 \mathrm{ft}$. lbs. per sec. $=33,000 \mathrm{ft}$. lbs. per min.

The equivalent electrical energy of a H.-P. $=\frac{\text { volts } \times \text { amperes }}{746}$ $=\frac{\text { amperes }^{2} \times \text { ohms }}{746}=\frac{\text { volts }^{2}}{746 \times \text { ohms }}$.

Paper.
1 ream $\quad=20$ quires $=480$ sheets. 1 quire $=24$ sheets.

## Drawing Paper.


Metrical System of Weights and Measures. The Metrical system is based upon the length of the fourth part of a terrestrial meridian. The
ten-millionth part of this arc was chosen as the unit of measures of length, and called a Metre. The and denominated a Litre. Kilogramne, of which the roceedingand kilo, hecto, from the Latin.
Metre).
Yard
 $\begin{array}{rrr}\text { MeASURES OF } & \text { CAPACITY } & \text { Cubic Feet. } \\ \text { Cubic Inches. } & \text { Pints. } \\ 0 \cdot 06103 \ldots & 0 \cdot 000035 \ldots & 0 \cdot 00176 \ldots \\ 0 \cdot 61027 \ldots & 0 \cdot 000353 \ldots & 0 \cdot 01761 \ldots \\ 6 \cdot 10271 \ldots & 0 \cdot 003532 \ldots & 0 \cdot 17608 \ldots \\ 61 \cdot 02705 \ldots & 0 \cdot 035317 \ldots & 1 \cdot 76077 \ldots \\ 610 \cdot 27052 \ldots & 0 \cdot 353166 \ldots & 17 \cdot 60773 \ldots \\ 6102 \cdot 70515 \ldots & 3 \cdot 531658 \ldots & 176 \cdot 07734 \ldots \\ 61027 \cdot 05152 \ldots & 35 \cdot 316581 \ldots & 1760 \cdot 77341 \ldots\end{array}$ ข0 'DIGคD

'Cable for the Conversion of Merric Weights and Measures into English.

|  |  <br>  |
| :---: | :---: |
|  |  <br>  <br>  <br>  11 <br>  |
|  |  <br>  <br>  |
|  |  <br>  <br>  <br>  |
|  |  <br>  <br>  <br>  <br>  |
|  |  ○ 心 <br>  II <br>  |

Perpetual Calendar for Ascertaining the Day of the Week.

| Table of Dominical Letters. |  |  |  |  |  |  |  |  |  | onth. |  |  | Dor | mini | cal | Let | ter. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Year of the Century. |  |  |  | Centuries. |  |  |  | Jan. Oct. <br> Feb. Mar. Nov. <br> Jan. Apr. July <br> May <br> June <br> Feb. Aug. <br> Sept. Dec. |  |  |  | ADGBEECF | ${ }_{\text {A }}^{\text {A }}$ |  |  | EADFBGC | FBEGCAAD | GCFADBE |
|  |  |  |  | $\begin{aligned} & \text { Q } \\ & \text { N } \\ & \text { 8. } \\ & 1 \end{aligned}$ | $\begin{aligned} & 8.8 \\ & \text { Nิ } \\ & \text { 8, } \\ & \mathbf{\infty} \end{aligned}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 28 | 56 | 84 | C | E | G | A |  | 8 | 15 | $22 \quad 29$ | S | S | F | Th | W |  | M |
| 1 | 29 | 57 | 85 | B | D | F | G |  | 9 | 16 | $23 \quad 30$ | M | 5 | S | F | Th | W | Tu |
| 2 | 30 | 58 | 86 | A | C | E | F |  | 10 | 17 | 2431 | Tu | M | \% | S | F | Th | W |
| 3 | 31 | 59 | 87 | G | B | D | E |  | 11 | 18 | 25 | W | Tu | M | \$ | S | F | Th1 |
|  |  |  |  |  |  |  |  |  | 12 | 19 | 26 | Th |  |  | M | S | S | F |
| 4 | 32 | 60 | 88 | E | G | B | C |  | 13 | 20 | 27 | F | Th |  | Tu | M | S | S |
| 5 | 33 | 61 | 89 | D | F | A | B |  | 14 | 21 | 28 | S | F | Th | W | Tu | M |  |
| 5 | 34 | 62 | 90 | C | E | G | A |  |  |  |  |  |  |  |  |  |  |  |
| 7 | 35 | 63 | 91 | B | D | F | G |  |  |  |  |  |  |  |  |  |  |  |
| 8 | 36 | 64 | 92 | G | B | D | E |  |  |  |  |  |  |  |  |  |  |  |
| - | 37 | 65 | 93 | F | A | C | D | Explanation.-Under the Century, and in the line with the Year of the Century, |  |  |  |  |  |  |  |  |  |  |
| 10 | 38 | 66 | 94 | E | G | B | C |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 11 | 39 | 67 | 95 | D | F | A | B | is the Dominical Letter of the Year. |  |  |  |  |  |  |  |  |  |  |
| 12 | 40 | 68 | 96 | B | D | F | G | Then in the line with the month find the column containing this letter; in this |  |  |  |  |  |  |  |  |  |  |
| 13 | 41 | 69 | 97 | A | C | E | F | column containing this letter; in this column, and in the line with the day of |  |  |  |  |  |  |  |  |  |  |
| 14 | 42 | 70 | 98 | G | B | D | E | the month, is the day of the week. In |  |  |  |  |  |  |  |  |  |  |
| 15 | 43 | 71 | 99 | F | A | C | D | Leap-years, the letters for January and February are in the lines where these |  |  |  |  |  |  |  |  |  |  |
| 16 | 44 | 72 |  | D | F | A | B |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 17 | 45 | 73 |  | C | E | G | A | montlis are printed in italics. |  |  |  |  |  |  |  |  |  |  |
| 18 | 46 | 74 |  | B | D | F | G |  |  |  |  |  |  |  |  |  |  |  |
| 19 | 47 | 75 |  | A | C | E | F | Examples.-For Dee. 31st, 1871: for 1871 the letter is $\mathbf{A}$; under A, in a line with 31 , is Sunday; and for Jan. 1st, 1872 the letter is $F$; under $F$, and in a.line with 1, is Monday. |  |  |  |  |  |  |  |  |  |  |
| 20 | 48 | 76 |  | F | A | C | D |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 21 | 49 | 77 |  | E | G | B | C |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 22 | 50 | 78 79 |  | D | $\underset{\mathrm{F}}{\mathrm{F}}$ | A | B |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 23 | 51 | 79 |  | C | E | G | A |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 24 | 52 | 80 |  | A | C | E | F |  |  |  |  |  |  |  |  |  |  |  |
| 25 | 53 | 81 |  |  | B | D | E |  |  |  |  |  |  |  |  |  |  |  |
| 26 | 54 | 82 |  |  |  | C | D |  |  |  |  |  |  |  |  |  |  |  |
| 27 | 55 | 83 |  | E |  | B | C |  |  |  |  |  |  |  |  |  |  |  |

MONEY TABLES.
Table converting Amprican into English Money.

| American cents | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| English money | d. | $d$. | ${ }_{1}{ }_{1}$ i | $d$. | d. | $d$. 3 | d. | $d$. | d. | $\stackrel{d}{5}$ | ${ }_{5}{ }_{5}$ |
| American cents | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 |
| English money | $d$ | $\begin{gathered} d . \\ 6 \frac{1}{2} \end{gathered}$ | d. | $\underset{7 \frac{1}{2}}{d}$ | $\begin{gathered} d . \\ 8 \end{gathered}$ | $\begin{gathered} d . \\ 8 \frac{1}{2} \end{gathered}$ | $\begin{gathered} d . \\ 9 \end{gathered}$ | $\begin{gathered} d \\ 9 \frac{1}{2} \end{gathered}$ | $d$. 10 | d. | 11. |
| American cents | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 |
| English money | $11 \frac{1}{2}$ | $\begin{array}{cc}8 . & d . \\ 1 & 0\end{array}$ | $\begin{array}{ll}\text { s. } & d . \\ 1 & 0 \frac{1}{2}\end{array}$ | $\begin{array}{ll}s . & d . \\ 1 & 1\end{array}$ | $\begin{array}{lc}8 . & d . \\ 1 & 1 \frac{1}{2}\end{array}$ | $\begin{array}{cc}s . & d . \\ 1 & 2\end{array}$ | $\begin{array}{ll}s . & d . \\ 1 & 2 \frac{1}{2}\end{array}$ | $\begin{array}{ll}\text { s. } & d \\ 1 & 3\end{array}$ | s.  <br> 1 3 | $\begin{array}{cc}8 . & d . \\ 1 & 4\end{array}$ | $\begin{array}{ll}\text { s. } & d . \\ 1 & 4 \frac{1}{2}\end{array}$ |
| American cents | 34 | 35 | 36 | 37 | 38 | 39 | 40 | 41 | 42 | 43 | 44 |
| English money | $\begin{array}{ll}8 . & d \\ 1 & 5\end{array}$ | $\begin{array}{ll}8 . & d . \\ 1 & 5 \frac{1}{2}\end{array}$ | $\begin{array}{ll}8 . & 7 \\ 1 & 6\end{array}$ | $\begin{array}{ll}s . & d . \\ 1 & 6 \frac{1}{2}\end{array}$ | $\begin{array}{cc}8 . & 7 \\ 1 & 7\end{array}$ | $\begin{array}{ll} 8 . & \pi \\ 1 & 7 \frac{1}{2} \end{array}$ | $\begin{array}{cc}\text { s. } \\ 1 & 8\end{array}$ | $\begin{array}{cc}8 . & d . \\ 1 & 8 \frac{1}{2}\end{array}$ | $\begin{array}{cc}8 . & 7 \\ 1 & 9\end{array}$ | s. 17. | $\begin{array}{lc}\text { s. } & \\ 1 & 10\end{array}$ |

Table Converting American into English Money－continuerd．

| 12 | $\begin{aligned} & \stackrel{\sim}{\circ} \mathrm{N} \\ & \dot{\sim} \text { o } \end{aligned}$ | 5 | $\begin{aligned} & \dot{\approx} 0 \\ & \dot{\infty} \circ \end{aligned}$ | E | $\begin{aligned} & \dot{\sim} \text { N } \\ & \therefore \sim \end{aligned}$ | $\infty$ | $\begin{aligned} & \infty \infty \\ & \dot{s} \infty \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\stackrel{4}{6}$ | ご <br> $\infty \mathrm{C}$ | 18 | $\begin{aligned} & \therefore \infty \\ & \dot{\infty} \infty \end{aligned}$ | 0 | จั่ ค <br> $\dot{\infty}$ | $\pm$ | $\begin{aligned} & \underset{\sim}{\sim} N_{n}^{n} \\ & \therefore \infty \end{aligned}$ |
| ¢ |  | － | $\begin{aligned} & \approx \infty \\ & \dot{\infty} \infty \end{aligned}$ | 12 | $\begin{aligned} & \therefore \stackrel{\sim N}{\sim} \\ & \therefore \infty \end{aligned}$ | $\cdots$ | $\begin{aligned} & \dot{B} \\ & \therefore \infty \end{aligned}$ |
| 난 | ช่ ค <br> $\therefore$ © | $\mathscr{6}$ | $\underset{\sim}{\circ}$ <br> $\infty$ © | ＋ | $\begin{aligned} & \text { vir } \\ & \dot{\theta} \pi \end{aligned}$ | 10 | $\begin{aligned} & \dot{3} \cos ^{-1} \\ & \dot{x} \end{aligned}$ |
| $\sqrt{2}$ | $$ | 8 | $\begin{aligned} & \dot{s} \\ & \dot{s} N \end{aligned}$ | $\because$ | $\underset{\sim}{\sim}$ <br> $\therefore$ | $\infty$ | シo $\therefore \infty$ |
| 12 | ジ $\therefore$ © | 5 |  | $\stackrel{1}{1}$ | ふ் $\leftrightarrow$ | $\%$ | $\begin{aligned} & \stackrel{\sim i c x}{15} \\ & i \infty \end{aligned}$ |
| 9 | $\underset{\sigma}{-N}$ <br> i N | $\bigcirc$ | vio <br> ic |  | $\begin{aligned} & \therefore=1 \\ & \therefore \text { N } \\ & \therefore=1 \end{aligned}$ | $\stackrel{\square}{\infty}$ | $\underset{\sim}{8}$ <br> ゃ |
| $\underset{+}{\infty}$ | so $\dot{\infty} \text { © }$ | 8 |  | O | $\begin{aligned} & \dot{x}=\vec{\omega} \\ & \dot{\sim} \cdot 1 \end{aligned}$ | $\infty$ | $\stackrel{3}{3}$ $\because \wedge$ |
| $\stackrel{\text { ¢ }}{+}$ | $\begin{gathered} \stackrel{\sim}{\sim}= \\ \dot{\sim} \end{gathered}$ | $\therefore$ | ご心 $\therefore$ © | 9 | ®00 | $\infty$ | $\begin{aligned} & \dot{\varepsilon}+ \\ & \dot{\sim} \end{aligned}$ |
| 4 | $\begin{aligned} & \dot{\sim}= \\ & \dot{\Delta}= \end{aligned}$ | $\bigcirc$ | $\begin{aligned} & \dot{8} \underset{\sim}{n} \\ & \text { in } \end{aligned}$ | $\infty$ | $\begin{aligned} & \dot{\theta}= \\ & \dot{\infty} \sim \end{aligned}$ | 8 |  |
| 19 | $\begin{aligned} & \dot{s} 0_{0}^{-N} \\ & \dot{0}-1 \end{aligned}$ | $\stackrel{6}{6}$ | $\mathrm{O}+$ $\dot{\infty} \sim$ | 5 | N் \% <br> $\dot{\infty}$ | $\infty$ | s® $\infty$ |
|  |  | － | － | － | － | － | － |
|  | Кәuou чs!!ఠిu! | sұпәо пъо!̣.мәшV |  |  | English money | American conts | English money |

Table Converting American into English Money-continued.


Table shewing Equivalent Rates per Lb., Cwt., and Ton.

| Per lb. | Per cwt. | Per ton. | Per lb. | Per cwt. | Per ton. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $d .$ | ${ }_{2} . d_{4}$ | $\begin{array}{ccc} £ & s . & d . \\ 2 & 6 & 8 \end{array}$ | $d$. $6 \frac{1}{4}$ | $\begin{array}{rr} s . & d . \\ 58 & 4 \end{array}$ | $\begin{array}{lll} £ & s . & d . \\ 58 & 6 & 8 \end{array}$ |
| $\frac{1}{2}$ | 48 | 4134 | $6 \frac{1}{2}$ | 608 | $\begin{array}{llll}60 & 13 & 4\end{array}$ |
| $\frac{3}{4}$ | 70 | $\begin{array}{lll}7 & 0 & 0\end{array}$ | $6 \frac{3}{4}$ | $63 \quad 0$ | 6300 |
| 1 | 9 | $\begin{array}{llll}9 & 6 & 8\end{array}$ | 7 | $65 \quad 4$ | $65 \quad 6 \quad 8$ |
| $1 \frac{1}{4}$ | 118 | $\begin{array}{lll}11 & 13 & 4\end{array}$ | $7 \frac{1}{4}$ | 678 | $67 \quad 13 \quad 4$ |
| $1 \frac{1}{2}$ | 140 | 1400 | $7 \frac{1}{2}$ | 70 | $70 \quad 0$ |
| $1 \frac{3}{4}$ | $16 \quad 4$ | $\begin{array}{llll}16 & 6 & 8\end{array}$ | $7 \frac{3}{4}$ | $72 \quad 4$ | $\begin{array}{llll}72 & 6 & 8\end{array}$ |
| 2 | $18 \quad 8$ | $\begin{array}{llll}18 & 13 & 4\end{array}$ | 8 | $\begin{array}{ll}74 & 8\end{array}$ | $\begin{array}{llll}74 & 13 & 4\end{array}$ |
| $2 \frac{1}{4}$ | 210 | 2100 | $8 \frac{1}{4}$ | 77 | 7700 |
| $2 \frac{1}{2}$ | $23 \quad 4$ | $\begin{array}{llll}23 & 6 & 8\end{array}$ | $8 \frac{1}{2}$ | 79 | $\begin{array}{llll}79 & 6 & 8\end{array}$ |
| $2 \frac{3}{4}$ | 258 | 25134 | $8 \frac{3}{4}$ | 818 | $\begin{array}{llll}81 & 13 & 4\end{array}$ |
| 3 | $28 \quad 0$ | $28 \quad 00$ | 9 | 84 | 8400 |
| $3 \frac{1}{4}$ | $30 \quad 4$ | $\begin{array}{llll}30 & 6 & 8\end{array}$ | $9 \frac{1}{4}$ | 86 | $86 \quad 6 \quad 8$ |
| $3 \frac{1}{2}$ | 328 | $\begin{array}{llll}32 & 13 & 4\end{array}$ | $9 \frac{1}{2}$ | 88 | $\begin{array}{llll}88 & 13 & 4\end{array}$ |
| $3 \frac{3}{4}$ | 350 | 3500 | $9 \frac{3}{4}$ | 91 | 910 |
| 4 | $37 \quad 4$ | $\begin{array}{llll}37 & 6 & 8\end{array}$ | 10 | $93 \quad 4$ | $\begin{array}{lll}93 & 6 & 8\end{array}$ |
| $4 \frac{1}{4}$ | 398 | $\begin{array}{llll}39 & 13 & 4\end{array}$ | $10 \frac{1}{4}$ | $\begin{array}{ll}95 & 8\end{array}$ | 95134 |
| $4 \frac{1}{2}$ | 420 | 4200 | 101 | $98 \quad 0$ | $98 \quad 0$ |
| $4 \frac{3}{4}$ | $44 \quad 4$ | $\begin{array}{llll}44 & 6 & 8\end{array}$ | $10 \frac{3}{4}$ | 100 4 | $100 \quad 6 \quad 8$ |
| 5 | $46 \quad 8$ | $\begin{array}{llll}46 & 13 & 4\end{array}$ | 11 | 1028 | $10213 \quad 4$ |
| $5 \frac{1}{4}$ | $49 \quad 0$ | 4900 | $11 \frac{1}{4}$ | 1050 | 10500 |
| $5 \frac{1}{2}$ | 514 | $\begin{array}{llll}51 & 6 & 8\end{array}$ | 111 $\frac{1}{2}$ | 1074 | $\begin{array}{llll}107 & 6 & 8\end{array}$ |
| $5 \frac{3}{4}$ | 538 | -53 13 4 | $11 \frac{8}{4}$ | 1098 | $10913 \quad 4$ |
| 6 | $56 \quad 0$ | $56 \quad 0 \quad 0$ | 12 | 1120 | 11200 |

Income Table for the year, Quarter, Calendar Month, Week, or Day.

| Yearly. | Quarterly. | Monthly. | Weekly. | Daily. |
| :---: | :---: | :---: | :---: | :---: |
| £6 60 | £1 $10 \quad 0$ | £0 $10 \quad 0$ | £0 2033 | £0 00 |
| $610 \quad 0$ | 1126 | 01010 | $\begin{array}{lll}0 & 2 & 6\end{array}$ | $\begin{array}{llll}0 & 0 & 4 \frac{1}{4}\end{array}$ |
| $7 \quad 0$ | 1150 | 0118 | $\begin{array}{llll}0 & 2 & 8 \frac{1}{4}\end{array}$ | $0004 \frac{1}{2}$ |
| 7100 | 1176 | 0126 | $0 \quad 210 \frac{1}{2}$ | 0005 |
| $8 \quad 0 \quad 0$ | 200 | 0134 | $0 \quad 30{ }^{0}$ | $\begin{array}{llll}0 & 0 & 5 \frac{1}{4}\end{array}$ |
| 8100 | 226 | $\begin{array}{llll}0 & 14 & 2\end{array}$ | $\begin{array}{lll}0 & 3 & 3\end{array}$ | $00^{0} 0$ |
| 900 | 250 | $\begin{array}{ll}0 & 15 \\ 0\end{array}$ | $0{ }_{0} 3^{5} 5 \frac{1}{2}$ | $00^{0}{ }^{\text {c }}$ |
| 9100 | $\begin{array}{llll}2 & 7 & 6\end{array}$ | 01510 | $\begin{array}{lllll}0 & 3 & 7 \frac{3}{4}\end{array}$ | $0{ }_{0} 00618$ |
| 1000 | 2100 | $\begin{array}{llll}0 & 16 & 8\end{array}$ | $0 \quad 310$ | $0{ }_{0} 00618$ |
| $1010 \quad 0$ | 2126 | 0176 | $0480 \frac{1}{4}$ | $0 \quad 0{ }^{0}$ |
| 110 | 2150 | 0184 |  | $\begin{array}{llll}0 & 0 & 7 \frac{1}{4}\end{array}$ |
| 11100 | 2176 | 0192 | $0 \times 45$ | $\begin{array}{llll}0 & 0 & 7 \frac{1}{2}\end{array}$ |
| 1200 | 3000 | 100 | $\begin{array}{llll}0 & 4 & 7 \frac{1}{4}\end{array}$ | 0 0 $0{ }^{8}$ |
| 12100 | $\begin{array}{llll}3 & 2 & 6\end{array}$ | 1010 | $0 \quad 410 \frac{1}{2}$ | $\begin{array}{llll}0 & 0 & 8 \frac{1}{4}\end{array}$ |
| 1300 | 350 | $1 \begin{array}{lll}1 & 1 & 8\end{array}$ | 050 | $\begin{array}{llll}0 & 0 & 8 \frac{1}{2}\end{array}$ |
| 13100 | $\begin{array}{llll}3 & 7 & 6\end{array}$ | 126 | $0 \quad 5 \quad 2 \frac{1}{4}$ | $\begin{array}{llll}0 & 0 & 9\end{array}$ |
| 1400 | 3100 | $1 \begin{array}{lll}1 & 3\end{array}$ | $0544 \frac{1}{4}$ | $\begin{array}{llll}0 & 0 & 9 & \frac{1}{4}\end{array}$ |
| 14100 | 3126 | 142 | $056 \frac{3}{4}$ | 00098 |
| 1500 | 3150 | 150 | $\begin{array}{llll}0 & 5 & 9\end{array}$ | $0 \quad 010$ |
| 15100 | 3176 | 1510 | $\begin{array}{llllll}0 & 5 & 11 \frac{1}{4}\end{array}$ | $0 \quad 0010 \frac{1}{4}$ |
| 1600 | 400 | 168 | $0{ }_{0} 61 \begin{aligned} & \text { 3 }\end{aligned}$ | $0 \quad 010 \frac{1}{2}$ |
| 16100 | 426 | 176 | 064 | $0 \quad 011$ |
| 1700 | 450 | 188 | $\begin{array}{llll}0 & 6 & 6 \frac{1}{4}\end{array}$ | $0 \quad 011 \frac{1}{4}$ |
| 17100 | $4 \quad 76$ | $1 \begin{array}{lll}1 & 9 & \end{array}$ | $068 \frac{1}{2}$ | $00011 \frac{1}{2}$ |
| 1800 | 4100 | 1100 | 0611 | $\begin{array}{llllllllll}0 & 0 & 11 \frac{3}{4}\end{array}$ |
| 18100 | 4126 | 11010 | $\begin{array}{llll}0 & 7 & 1 \frac{1}{4}\end{array}$ | $0{ }_{0} 1{ }^{1} 0^{4}$ |
| 1900 | 4150 | 1118 | $\begin{array}{llll}0 & 7 & 3 \frac{1}{2}\end{array}$ | $0110 \frac{1}{2}$ |
| 19100 | 4176 | 1126 | $\begin{array}{llll}0 & 7 & 5 \frac{3}{4}\end{array}$ | $0{ }_{0} 11^{1}$ |
| $20 \quad 00$ | 500 | 1134 | $\begin{array}{lll}0 & 7 & 8\end{array}$ | $\begin{array}{llll}0 & 1 & 1 \frac{1}{4}\end{array}$ |
| 3000 | 7100 | 2100 | 0116 | $\begin{array}{llll}0 & 1 & 7 & 7\end{array}$ |
| 4000 | 1000 | 3 6 | $0154 \frac{1}{2}$ | $\begin{array}{llll}0 & 2 & 2 \frac{1}{4}\end{array}$ |
| 万0 000 | 12100 | $\begin{array}{llll}4 & 3 & 4\end{array}$ | $019{ }^{2}{ }^{\frac{3}{4}}$ | $\begin{array}{llll}0 & 2 & 9\end{array}$ |
| $60 \quad 0 \quad 0$ | 150 | 500 | $\begin{array}{lll}1 & 3 & 1\end{array}$ | $\begin{array}{llll}0 & 3 & 3 \frac{1}{2}\end{array}$ |
| $\begin{array}{lll}70 & 0 & 0\end{array}$ | 17100 | 5168 | 1611 | 0310 |
| $80 \quad 00$ | $20 \quad 0$ | 6134 | $110 \quad 9 \frac{1}{4}$ |  |
| 9000 | 22100 | 7100 | $1147 \frac{1}{4}$ | $0411 \frac{1}{2}$ |
| 10000 | 2500 | $8 \quad 68$ | $1185 \frac{1}{2}$ | 056 |
| 20000 | $50 \quad 00$ | $1613 \quad 4$ | 31611 | $01011 \frac{3}{4}$ |
| 3000 | 750 ט | 2500 | $\square_{6} 154$ | $01616{ }^{5}$ |
| 40000 | $100 \begin{array}{lll}10 & 0\end{array}$ | $\begin{array}{cccc}33 & 6 & 8\end{array}$ | 71310 | $11^{1} 11 \frac{3}{4}$ |
| $500 \quad 0 \quad 0$ | 12500 | 4113 | $9123 \frac{1}{2}$ | $1 \begin{array}{llll}1 & 7 & 5 \frac{3}{4}\end{array}$ |


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Wages Table. (Forty-eight Hours per Week.)
Detailing the wages from $\frac{1}{2}$ hour to 6 days-the day being reckoned at 8 hours-at rates per week of from 5s. to £5. (Original.)

| D. H. | 5s. <br> Per Week. | 6s. Per Week. | 7 s. Per Week. | 7s. 6d. Per Week. | 8 s. Per Week. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | £ s. ${ }_{\text {l }}$ | £ s. $\quad$ d. | £ s. d. | \& $s$ | s. | £ s. d |
|  | $00^{0}$ | $\begin{array}{llll}0 & 0 & 0 \frac{3}{4} & 0\end{array}$ | $\begin{array}{lll}0 & 0 & 0 \frac{7}{8} \\ 0\end{array}$ | 0 0 015 <br> 16   | $0 \quad 1$ | 0 0 $1 \frac{1}{6}$ |
|  | 0 1 $1 \frac{1}{4}$ | $\begin{array}{llll}0 & 0 & 1 \frac{1}{2} \\ 0\end{array}$ | $\begin{array}{llll}0 & 0 & 1 \frac{3}{4} \\ 0\end{array}$ | 0 0 17 | 0 | $\begin{array}{lll}0 & 0 & 2 \frac{1}{4}\end{array}$ |
|  | 0 21 | $00^{0}$ | $00^{0}$ | 0 0 ${ }^{0} 3 \frac{3}{4}$ | 04 | $\begin{array}{lll}0 & 0 & 4 \frac{1}{2}\end{array}$ |
|  | $0{ }^{0} \quad 3{ }^{3}$ | $\begin{array}{llll}0 & 0 & 4 \frac{1}{2},\end{array}$ | $0{ }_{0} 0$ | $\begin{array}{llll}0 & 0 & 5 \frac{5}{8} \\ 0\end{array}$ | $\begin{array}{lll}0 & 0 & 6\end{array}$ | 0 |
|  | 05 | 0 0 e | $\begin{array}{llll}0 & 0 & 7 & 0\end{array}$ | $0 \quad 0 \quad 7 \frac{1}{2}$ | 0 O 08 | $\begin{array}{llll}0 & 0 & 9\end{array}$ |
|  | 0 |  |  | $00^{0} 00938$ | 0 | 0 0-111 |
| 6 | $0 \quad 7 \frac{1}{2}$ | $\begin{array}{llll}0 & 0 & 9\end{array}$ | $0 \quad 0 \quad 10 \frac{1}{2} 0$ | $0 \quad 0 \quad 11 \frac{1}{4} 0$ | 010 | 0 |
|  | $\begin{array}{llll}0 & 0 & 8 \frac{3}{4}\end{array}$ | $0 \quad 0 \quad 10 \frac{1}{2} 0$ | $0 \quad 10 \frac{1}{4} 0$ | $\begin{array}{llll}0 & 1 & 18\end{array}$ | 012 | $\begin{array}{lllll}0 & 1 & 3 & 3 \\ 4\end{array}$ |
| $1=8$ | 0 | 0 1 10 | $012{ }^{4} 0$ | 013 | 0 | ${ }^{4}$ |
| $2=16$ | 0 | 0 | 024 | $0-26$ | 28 | 0 |
| $3=24$ | $0-26$ | 030 | 036 | $\begin{array}{lll}0 & 3 & 9\end{array}$ | 40 | $0 \quad 46$ |
| $4=320$ | 03 | 040 | 048 | 0 - 50 | 54 | 0 |
| $5=40$ | $0 \quad 42$ | 0 | $0 \quad 510$ | 063 | 68 | 0 |
| $6=48$ | $0 \quad 50$ | 060 | $0 \quad 70$ | 076 | 80 | $0 \quad 9$ |


| H. | 10 s. <br> Per Week. | 11s. <br> Per Week. | 12s. <br> Per Week. | $\begin{gathered} \text { 12s. 6d. } \\ \text { Per Week. } \end{gathered}$ | 13s. Per Week. | 14s. <br> Per Week. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | s. d. | £ s. $\quad d$. | $\pm$ s. $\quad$ d. | £ s. $\quad$. $£$ | £ s. $\quad d$. | L |
|  | $0{ }^{0} 110$ | $0 \quad 0 \quad 13$ | $0 \quad 0 \quad 1 \frac{1}{2}$ | $\begin{array}{llll}0 & 0 & 1 \frac{9}{16} 0\end{array}$ | $\begin{array}{llll}0 & 0 & 15 \\ 8\end{array}$ | $\begin{array}{llll}0 & 0 & 1 \frac{3}{4}\end{array}$ |
|  | $0 \quad 210$ | $0 \quad 0$ | 0 | $0 \quad 0 \quad 3 \frac{11}{81} 0$ | $0 \quad 3 \frac{1}{4} 0$ | $\begin{array}{llll}0 & 0 & 31\end{array}$ |
| 2 | $0 \quad 5$ | 0 0 0 51 | 0 |  | $0 \quad 0 \quad 6 \frac{1}{2} 0$ | $\begin{array}{lll}0 & 0 & 7\end{array}$ |
| 3 | $0 \quad 7 \frac{1}{2} 0$ | $0 \quad 0.8 \frac{1}{4}$ | $\begin{array}{lll}0 & 0 & 9\end{array}$ | $\begin{array}{lll}0 & 0 & 93\end{array}$ | $0 \quad 93$ | $0 \quad 0 \quad 10 \frac{1}{2}$ |
|  | 010 | 0011 | 0 | $0 \quad 1 \quad 0 \frac{1}{2} 0$ | $\begin{array}{llll}0 & 1 & 1\end{array}$ | - |
| 5 | $10 \frac{1}{2}$ | $0{ }_{0} 11130$ | $\begin{array}{lll}0 & 1 & 3\end{array}$ | 0 1 3 35 <br> 8    | $0{ }_{0} 1$ | ${ }^{2}$ |
| 6 | 130 | $0114 \frac{1}{2}$ | $\begin{array}{lll}0 & 1 & 6\end{array}$ | $0{ }_{0} 116_{4}^{3} 0$ | 017810 | 0 |
| 7 | $5 \frac{1}{2} 0$ | $017{ }^{0} 10$ | $\begin{array}{llll}0 & 1 & 9\end{array}$ | $\begin{array}{llll}0 & 1 & 97 \\ 8\end{array}$ | $\begin{array}{llllllll}0 & 1 & 10 \frac{3}{4}\end{array}$ | $\begin{array}{llll}0 & 2 & 0 \frac{1}{2}\end{array}$ |
| $1=8$ | $\begin{array}{llll}0 & 1 & 8\end{array}$ | $\begin{array}{llll}0 & 1 & 10\end{array}$ | 020 | $\begin{array}{llll}0 & 2 & 1\end{array}$ | $\begin{array}{lll}0 & 2 & 2\end{array}$ | 24 |
| $2=16$ | 0 | 038 | 040 | 0 | 44 | 0 |
| $3=24$ | $\begin{array}{llll}0 & 5 & 0\end{array}$ | $\begin{array}{llll}0 & 5 & 6\end{array}$ | 060 | 0 | 66 | $\begin{array}{lll}0 & 7 & 0\end{array}$ |
| $4=32$ | 0 | 07 | 080 | $\begin{array}{llll}0 & 8 & 4\end{array}$ | 88 | $0{ }^{9} 4$ |
| $5=40$ | $\begin{array}{llll}0 & 8 & 4\end{array}$ | $\begin{array}{lll}0 & 9 & 2\end{array}$ | 010 | $\begin{array}{llll}0 & 10 & 5\end{array}$ | $\begin{array}{llll}0 & 10 & 10\end{array}$ | 011 |
| $6=48$ | $010 \quad 0$ | 0110 | 0120 | $012 \quad 6$ | 0130 | 014 |

Wages Table (Forty-eight Hours per Week) (continued).

| i). H. | 15 s. <br> Per Week. | 16s. <br> Per Week. | 17s. <br> Per Week. | 17s. 6d. <br> Per Week. | 18s. <br> Per Week. | 19s. <br> Per Week. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1. | £ s. d. | d. | £ s. $\quad$ d. | £ s. d. | a. |
|  | $0{ }^{0} 1 \frac{7}{8}$ | $\begin{array}{lll}0 & 0 & 2\end{array}$ | $\begin{array}{lll}0 & 0 & 2 \frac{1}{8} \\ 0 & \end{array}$ | $\begin{array}{lll}0 & 0 & 2 \frac{3}{16}\end{array}$ | $\begin{array}{lll}0 & 0 & 2 \frac{1}{4} \\ 0\end{array}$ | 0 2 $2 \frac{3}{8}$ |
|  | $0{ }_{0} \quad 3 \frac{3}{4}$ | 0 | 0 | 0 | $00^{0}$ | $0{ }_{0} 4_{4}^{3}$ |
|  | $00^{0} 0$ | $\begin{array}{lll}0 & 0 & 8\end{array}$ | 0 | $0 \quad 0$ | $\begin{array}{lll}0 & 0 & 9\end{array}$ | $0 \quad 9 \frac{1}{2}$ |
|  | $00011 \frac{1}{4}$ | 0 |  | 0 | $\begin{array}{lll}0 & 1 & 1 \frac{1}{2}\end{array}$ | $12^{\frac{1}{4}}$ |
|  | 13 | 01 | 0 | $\begin{array}{llll}0 & 1 & 5 \frac{1}{2}\end{array}$ | $\begin{array}{llll}0 & 1 & 6\end{array}$ | 17 |
|  | $16 \frac{3}{4}$ | 0 1 18 | $\begin{array}{llll}0 & 1 & 9 \frac{1}{4}\end{array}$ | 0 | $\begin{array}{llll}0 & 1 & 10 \frac{1}{2}\end{array}$ | $111 \frac{3}{4}$ |
|  | $110 \frac{1}{2}$ | 0 | 0 | $0 \quad 2 \quad 2 \frac{1}{4}$ | 023 | $24 \frac{1}{2}$ |
|  | 10 | $\begin{array}{lll}0 & 2 & 4\end{array}$ | $10 \quad 2 \quad 5 \begin{array}{ll}0 \frac{3}{4}\end{array}$ | $0 \quad 26 \frac{5}{8}$ | $027 \frac{1}{2}$ | 291 |
| $1=8$ | $\begin{array}{lll}0 & 2 & 6\end{array}$ | $\begin{array}{lll}0 & 2 & 8\end{array}$ | $\left.\right\|_{0} \quad 2 \begin{aligned} & 10\end{aligned}$ | $0 \quad 211$ | $0 \begin{array}{lll}0 & 3 & 0\end{array}$ | 32 |
| $2=16$ | $\begin{array}{lll}0 & 5 & 0\end{array}$ | $\begin{array}{llll}0 & 5 & 4\end{array}$ | $\begin{array}{llll}0 & 5 & 8\end{array}$ | $\begin{array}{llll}0 & 510\end{array}$ | 0 | $\begin{array}{llll}0 & 6 & 4\end{array}$ |
| $3=24$ | $\begin{array}{lll}0 & 7 & 6\end{array}$ | $\begin{array}{llll}0 & 8 & 0\end{array}$ | 10 | $\begin{array}{llll}0 & 8 & 9\end{array}$ | $\begin{array}{llll}0 & 9 & 0\end{array}$ | $\begin{array}{llll}0 & 9 & 6\end{array}$ |
| $4=32$ | $\begin{array}{llll}0 & 10 & 0\end{array}$ | $0 \quad 108$ | 10114 | 0118 | $\begin{array}{lll}0 & 12 & 0\end{array}$ | $\begin{array}{lll}0 & 12 & 8\end{array}$ |
| $5=40$ | $0 \quad 12 \quad 6$ | 013 | 0 14 2 | 014 | 0150 | 01510 |
| $6=48$ | 0150 | 016 | $017 \quad 0$ | 017 | 0180 | 019 |


| D. H. | $20 \mathrm{~s}$ <br> Per Week. | 21s. Per Week. | 22 s. <br> Per Week. | $\begin{array}{\|c\|} \hline \text { 22s. 6d. } \\ \text { Per Week. } \end{array}$ | 23s. Per Week. | $\begin{gathered} 24 \mathrm{~s} . \\ \text { Per Week. } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | s. ${ }^{\text {a }}$ | £ s. a. | £ s. $\quad d$. | s. | £ s. d. | s. |
|  | $0 \quad 2 \frac{1}{2} 0$ | $0 \quad 0 \quad 2 \frac{5}{8}$ | $0 \quad 0 \quad 2 \frac{3}{4} 0$ | $\begin{array}{llll}0 & 0 & 213 \\ 18\end{array}$ |  | 03 |
|  | $0 \quad 50$ | 0 | $0 \quad 0 \quad 5 \frac{1}{2} 0$ | $0005 \frac{5}{8}$ | $\begin{array}{llll}0 & 0 & 5 \frac{3}{4}\end{array}$ | 0 |
| 2 | 010 | $0 \quad 0 \quad 10 \frac{1}{2}$ | 0 | $0 \quad 011 \frac{1}{4}$ | $0 \quad 0 \quad 11 \frac{1}{2}$ | 010 |
| 3 | 3 | $\begin{array}{llll}0 & 1 & 3 & 3\end{array}$ | $0 \quad 141410$ | $0114 \frac{7}{8} 0$ |  | 0 |
|  | 1 | $0 \begin{array}{lll}0 & 1 & 9\end{array}$ | $\begin{array}{llll}0 & 1 & 10\end{array}$ | $0 \quad 110 \frac{1}{2} 0$ | $0 \quad 111$ | 2 |
|  | 21 | $\begin{array}{llll}0 & 2 & 2 \frac{1}{4}\end{array}$ | $0 \quad 2 \quad 3{ }^{1} 0$ | $0 \quad 24 \frac{1}{8} 0$ | $\begin{array}{llll}0 & 2 & 4 \frac{3}{4}\end{array}$ | 02 |
| 6 | 26 | $27 \frac{1}{2}$ | $\begin{array}{llll}0 & 2 & 9\end{array}$ | $\begin{array}{lll}0 & 2 & 9 \frac{3}{4}\end{array}$ | $0 \quad 210 \frac{1}{2}$ | 03 |
|  | 0 | $3 \quad 0 \frac{3}{4}$ | $\begin{array}{llll}0 & 3 & 2 \frac{1}{2} & 0\end{array}$ | $\begin{array}{llll}0 & 3 & 3 & 3\end{array}$ | 0 | 03 |
| $1=8$ | 0 | 0 | 0 | $\begin{array}{llll}0 & 3 & 9\end{array}$ | $0 \quad 310$ | 0 |
| $2=16$ | 0 | $\begin{array}{llll}0 & 7 & 0\end{array}$ | $\begin{array}{llll}0 & 7 & 4\end{array}$ | $0{ }^{0} 76$ | $0 \quad 78$ | 08 |
| $3=24$ | 010 | $010 \quad 6$ | 01110 | $011 \begin{array}{ll}0\end{array}$ | 0116 | 012 |
| $4=32$ | 013 | 014 | 0148 | 0150 | 015.4 | 016 |
| $5=40$ | 0168 | $017 \quad 6$ | 0184 | 018 | $019 \quad 2$ | 10 |
| $6=48$ | 100 | 110 | 120 | 12 | 130 | 14 |

Wages Table (Forty-eight Hours per Week) (continued).

| D. H. | 25 s. <br> Per Week. | 26s. Per Week. | 27s. Per Week. | 27s. 6d. <br> Per Week. | 28s. <br> Per Week. | 29 s. <br> Per Week |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | ${ }_{\text {£ }}$ s. $\quad$ d. | ${ }^{1}$ | ${ }_{\text {¢ }}$ s. $\quad$ d. |  | £ s. d. | £ s. $\quad$ d. |
|  | 6 | 0 | 0 | 0 |  |  |
|  | $0 \quad 100$ | 0111 | $011 \frac{1}{2}$ | $\begin{array}{lllllllllllll}0 & 1 & 1 \frac{8}{4}\end{array}$ | 012 | $\begin{array}{llll}0 & 1 & 2 \frac{1}{2}\end{array}$ |
|  | 0 | $017 \frac{1}{2} 0$ | 018810 | 01885 | 01 | $\begin{array}{llll}0 & 1 & 9 & \\ \frac{3}{4}\end{array}$ |
|  | 0 | $\begin{array}{lll}0 & 2 & 20\end{array}$ | 023 | $0 \quad 2310$ | $0 \quad 24$ | 0 |
|  | $\begin{array}{llll}0 & 2 & 71\end{array}$ | $0 \quad 2818$ | $0 \quad 2 \quad 93$ | $0 \quad 210 \frac{3}{8}$ | $0 \quad 211$ | $\begin{array}{llll}0 & 3 & 0 \frac{1}{4}\end{array}$ |
|  | 0 | $\begin{array}{lllll}0 & 3 & 3\end{array}$ | 031410 | $0 \quad 3 \quad 5 \frac{1}{4} 10$ | 036 | $\begin{array}{llll}0 & 3 & 7 \frac{1}{2}\end{array}$ |
|  | $\begin{array}{lllll}0 & 3 & 7 \frac{3}{4}\end{array}$ | 03910 | $0311 \frac{1}{4}$ | $040 \frac{1}{8} 0$ | 04 | $\begin{array}{llll}0 & 4 & 2_{4}^{3}\end{array}$ |
| $1=8$ | 10 | 044 | $0 \quad 46$ | $\begin{array}{llll}0 & 4 & 7\end{array}$ | 04 | $\begin{array}{llll}0 & 4 & 10\end{array}$ |
| $2=16$ | $\begin{array}{llll}0 & 8 & 4\end{array}$ | $\begin{array}{llll}0 & 8 & 8\end{array}$ | $9 \quad 0$ | 0 | $0 \quad 9$ | $\begin{array}{llll}0 & 9 & 8\end{array}$ |
| $3=24$ | 0126 | 0130 | $013 \quad 6$ | $013 \quad 9$ | 014 | 0146 |
| $4=32$ | 0168 | $\begin{array}{llll}0 & 17 & 4\end{array}$ | 018 | 0184 | 018 | 019 |
| $5=40$ | 010 | $1 \begin{array}{lll}1 & 1 & 8\end{array}$ | 2 | 211 | $1 \begin{array}{lll}1 & 3\end{array}$ | 14 |
| $6=48$ | 50 | 160 | 17 | 76 | 18 | 90 |
| D. H. |  |  |  |  |  |  |
|  | $\begin{array}{ccc} £ & s . & d_{3} \\ 0 & 0 & 3 \\ \hline \end{array}$ |  |  | $\begin{array}{lll} \dot{L} & s & d . \\ 0 & 0 & 4 \frac{1}{10} \end{array}$ | $\begin{array}{ll} £ & s . \\ 0 & 0 \end{array}$ | $\begin{gathered} d \\ 4 \frac{1}{4} \end{gathered}$ |
|  | $0 \quad 0 \quad 7 \frac{1}{2} 0$ | $0{ }_{0} 0$ | 08 |  | 0 0 81 | $\begin{array}{llll}0 & 0 & 8 \frac{1}{2}\end{array}$ |
|  |  | 0131310 | 014 | $14 \frac{1}{4} 0$ | $0{ }_{0} 1$ | $\begin{array}{llll}0 & 1 & 5^{2}\end{array}$ |
|  | $0 \quad 110 \frac{1}{2} 0$ | $0 \quad 111 \frac{1}{4} 0$ | 020 | $20 \frac{3}{8} 0$ | $0 \quad 20_{4}^{3}$ | $\begin{array}{lll}0 & 2 & 1 \frac{1}{2}\end{array}$ |
|  | 0 | $\begin{array}{lllll}0 & 2 & 7\end{array}$ | $0 \quad 28$ | $0 \quad 28 \frac{1}{2}$ | 029 | $0 \quad 210^{2}$ |
|  | $0 \begin{array}{lll}0 & 3 & 1 \frac{1}{2}\end{array} 0$ | $0-31230$ |  | $\begin{array}{llll}0 & 3 & 4 \frac{5}{8} \\ 0\end{array}$ | $0{ }^{0} 3{ }^{51}$ | $\begin{array}{lll}0 & 3 & 6 \frac{1}{2}\end{array}$ |
|  | $\begin{array}{llll}0 & 3 & 9\end{array} 0$ | $0-310 \frac{1}{2} 0$ | 040 | $4 \quad 0 \frac{3}{4}$ | $0411 \frac{1}{2}$ | $\begin{array}{llll}0 & 4 & 3\end{array}$ |
|  | $\begin{array}{llll}0 & 4 & 4 \frac{1}{2} 0\end{array}$ | $0 \quad 4 \quad 6 \frac{1}{4} 0$ | 088 | $48 \frac{7}{8} 0$ | $0{ }_{0} \quad 4 \quad 9 \frac{3}{4}$ | $0{ }_{0} \quad 411 \frac{1}{2}$ |
| $1=$ | $\begin{array}{llll}0 & 5 & 0\end{array} 0$ | $\begin{array}{llll}0 & 5 & 2\end{array}$ | 0 | $\begin{array}{llll}0 & 5 & 5\end{array}$ | $\begin{array}{llll}0 & 5 & 6\end{array}$ | $\begin{array}{llll}0 & 5 & 8\end{array}$ |
| $2=16$ | $010 \quad 0$ | 010 | 0.108 | 01010 | 011 | $\begin{array}{llll}0 & 11 & 4\end{array}$ |
| $3=24$ | 0150 | $015 \quad 6$ | 016 | 0163 | $016 \quad 6$ | $017 \quad 0$ |
| $4=32$ | 100 | $1{ }^{1}$ | 1 | $\begin{array}{lll}1 & 1 & 8\end{array}$ | 2 | 12 |
| $5=40$ | 150 | $\begin{array}{llll}1 & 5 & 10\end{array}$ | $\begin{array}{lll}1 & 6 & 8\end{array}$ | 71 | 76 | 84 |
| $6=48$ | 1100 | 11110 | 1120 | 1126 | 113 | 114 |

## Wages Table (Forty-eight Hours per Week) (continued).

| D. H. | $\begin{gathered} 35 \mathrm{~s} . \\ \text { Per Week. } \end{gathered}$ | 36s. <br> Per Week. | 37s. Per Week. | 37s. 6d. Per Week. | 38s. Per Week. | 39s. Per Week. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{array}{ccc}\text { \& } & s . & d . \\ 0 & 0 & 4 \\ 4 \\ \frac{3}{8} \\ 0\end{array}$ | $\begin{array}{lll}\text { £ } & s . & d . \\ 0 & 0 & 4 \frac{1}{2}\end{array}$ | $\begin{array}{ccc}£ & s . & d . \\ 0 & 0 & 4 . \\ 8 \\ 8\end{array}$ |  | £ s.  <br> 0 0 $d$. <br> 1   | £ $s$. d. <br> 0 0 4 |
|  | 088 | $\begin{array}{llll}0 & 0 & 9\end{array}$ | 0 0 0 91 | 0 | $0{ }^{0}$ | $\begin{array}{llll}0 & 0 & 9 & 9\end{array}$ |
|  | $15 \frac{1}{2}$ | 0 1 6 | $0{ }_{0} 1$ | $\begin{array}{llll}0 & 1 & 6 \frac{8}{4}\end{array}$ | $17^{2}$ | $\begin{array}{llll}0 & 1 & 7 \frac{1}{2}\end{array}$ |
|  | $\begin{array}{llll}0 & 2 & 21\end{array}$ | $\begin{array}{lll}0 & 2 & 3\end{array}$ | $\begin{array}{lllll}0 & 2 & 3 \frac{3}{4} & 0\end{array}$ | 0 2 $4 \frac{1}{8}$ | $0 \quad 24 \frac{1}{2}$ | $0 \quad 2 \quad 5 \frac{1}{4}$ |
|  | $0 \quad 211$ | $\begin{array}{llll}0 & 3 & 0\end{array}$ | $\begin{array}{llll}0 & 3 & 1\end{array}$ | $\begin{array}{llll}0 & 3 & 1 \frac{1}{2}\end{array}$ | 0 | $\begin{array}{llll}0 & 3 & 3\end{array}$ |
|  | $\begin{array}{llll}0 & 3 & 7 \frac{3}{4}\end{array}$ | $\begin{array}{llll}0 & 3 & 9\end{array}$ | 0 O 31010 | 0 | $0 \quad 311 \frac{1}{2}$ | $\begin{array}{llll}0 & 4 & 0_{4}^{3}\end{array}$ |
|  | $0 \quad 4 \quad 4 \frac{1}{2}$ | $\begin{array}{llll}0 & 4 & 6\end{array}$ |  | 0 | $\begin{array}{lll}0 & 4 & 9\end{array}$ | $\begin{array}{llll}0 & 4 & 10 \frac{1}{2}\end{array}$ |
|  | $\begin{array}{llll}0 & 5 & 1 \frac{1}{4}\end{array}$ | 0 | $\begin{array}{lllll}0 & 5 & 4 \frac{3}{4} & 0\end{array}$ | 0 5 $5 \frac{8}{8}$ | $0 \quad 5 \quad 6 \frac{1}{2}$ | 0 |
| $1=$ | $\begin{array}{llll}0 & 5 & 10\end{array}$ |  | $\begin{array}{lll}0 & 6 & 2\end{array}$ | $0 \quad 6 \quad 3$ | 6 | $\begin{array}{llll}0 & 6 & 6\end{array}$ |
| $2=16$ | 0118 | 0120 | 0124 | $\begin{array}{llll}0 & 12 & 6\end{array}$ | 0128 | 0130 |
| $3=24$ | 017 | 018 0 | 0186 | $\begin{array}{llll}0 & 18 & 9\end{array}$ | 0190 | 019 |
| $4=32$ | 13 | 140 | 148 | 15 | 154 | 160 |
| $5=40$ | 9 | 110 | 11010 | 111 | 1118 | 112 |
| $6=48$ | 1150 | 1160 | 1170 | $117 \quad 6$ | 1180 | 1190 |
| D. H. | 40s. <br> Per Wee | 41s. <br> Per Week. | Per Week. | $\text { 42s. } 6 \mathrm{~d} .$ <br> Per Week. | 43s. <br> Per Week | 44s. |
|  | $\begin{array}{lll}£ & \text { s. } \\ 0 & \text { d. } \\ 0 & 0 & 5\end{array}$ |  | $\begin{array}{cccc}\text { £ } & \text { s. } \\ 0 & \text { d. } & \text { f } \\ \text { ¢ }\end{array}$ | $\begin{array}{ccc}£ & s & d . \\ 0 & 0 & 5.5 \\ \frac{5}{16}\end{array}$ | £ s. d. <br> 0 0 5 <br> $5 \frac{3}{8}$   |  |
|  | 010 | $0 \quad 0 \quad 10 \frac{1}{4}$ O | 0 O $10 \frac{1}{2} 0$ | $0 \quad 0 \quad 10 \frac{5}{8}$ | $0 \quad 0 \quad 10 \frac{3}{4}$ | $011{ }^{1}$ |
|  | 18 | $0 \quad 188$ | $\begin{array}{llll}0 & 1 & 9\end{array}$ | $\begin{array}{llll}0 & 1 & 9 \frac{1}{4}\end{array}$ | 0198 | $\begin{array}{llll}0 & 1 & 10\end{array}$ |
|  | 0 | $\begin{array}{llll}0 & 2 & 6 \frac{3}{4}\end{array}$ | 02710 | $\begin{array}{llll}0 & 2 & 7 \frac{7}{8} \\ 0\end{array}$ | $028 \frac{1}{4}$ | 0 |
|  | 0 | $\begin{array}{lll}0 & 3 & 5\end{array}$ | $\begin{array}{llll}0 & 3 & 6\end{array}$ | $\begin{array}{llll}0 & 3 & 6 \frac{1}{2}\end{array}$ | 037 | $0 \begin{array}{lll}0 & 3 & 8\end{array}$ |
|  | $10 \quad 4 \quad 2$ | 0 | $0 \quad 4 \quad 4 \frac{1}{2} 0$ | $0 \quad 4 \quad 5 \frac{1}{81}$ | $\begin{array}{llll}0 & 4 & 5 \frac{3}{4}\end{array}$ | 0 |
|  | 50 | $0 \quad 5 \quad 1 \frac{1}{2}$ | $0 \quad 5 \quad 3$ | $53{ }^{\frac{3}{4}}$ | 0 5 4 ${ }^{\frac{1}{2}}$ | 0 |
|  | $\begin{array}{llll}0 & 5 & 10\end{array}$ | $0 \quad 5 \quad 11 \frac{3}{4}$ | $0611 \frac{1}{2} 0$ | $0 \quad 6 \quad 2 \frac{3}{8}$ | $063 \frac{1}{4}$ | 0 |
| $1=$ | $\begin{array}{lll}0 & 6 & 8\end{array}$ | $\begin{array}{llll}0 & 6 & 10\end{array}$ | $\begin{array}{llll}0 & 7 & 0\end{array}$ | $\begin{array}{llll}0 & 7 & 1\end{array}$ | $\begin{array}{llll}0 & 7 & 2\end{array}$ | $\begin{array}{llll}0 & 7 & 4\end{array}$ |
| $2=16$ | $\begin{array}{llll}0 & 13 & 4\end{array}$ | 0-13 8 | 0140 | $014 \quad 2$ | 141 | 0148 |
| $3=24$ | 100 | 10 | 110 | 13 | $1 \begin{array}{lll}1 & 6\end{array}$ | $1 \begin{array}{lll}1 & 2 & 0\end{array}$ |
| $4=32$ | 16 | 7 | 80 | 84 | 188 | $\begin{array}{lll}1 & 9 & 4\end{array}$ |
| $5=40$ | 113 | 1142 | 1150 | 1155 | 11510 | 1168 |
| $6=48$ | 200 | 210 | $2 \quad 2002$ | $2 \quad 26$ | 30 | 240 |

## Wages Table (Forts-eight Hours per Week) (continued).

| D. H. | 45 s. <br> Per Week. | 46s. <br> Per Week. | 47s. Per Week. | 47s. 6d. Per Week. | 48s. Per Week. | 49s. <br> Per Week. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\begin{array}{ccc}£ & s . & d . \\ 0 & 0 & 5 \frac{7}{8} \\ \end{array}$ | $\begin{array}{ccc} \pm & s . & d . \\ 0 & 0 & 515 \\ 0\end{array}$ |  | $\begin{array}{llr}\text { ¢ } & \text { s. } & \text { d. } \\ 0 & 0 & 6 \frac{i}{8} \\ 0\end{array}$ |
|  | $0 \quad 0$ | $0 \quad 011 \frac{1}{2}$ | $0011 \frac{3}{4}$ | 0 | 010 | $\begin{array}{llll}0 & 1 & 0 \frac{1}{4}\end{array}$ |
|  | $0 \quad 110 \frac{1}{2} 0$ | 01110 | $\begin{array}{llll}0 & 1 & 11 \frac{1}{2}\end{array}$ | 0 | 020 | $\begin{array}{lll}0 & 2 & 0 \frac{1}{2}\end{array}$ |
|  | $0 \quad 2 \quad 9 \frac{3}{4} 0$ | $0 \quad 210 \frac{1}{2}$ | $02211 \frac{1}{4}$ | $0211 \frac{5}{81}$ | 030 | $\begin{array}{llll}0 & 3 & 0 \frac{3}{4}\end{array}$ |
|  | 0 | $\begin{array}{llll}0 & 3 & 10\end{array}$ | 0311 | $0 \quad 311 \frac{1}{2}$ | - | $0{ }^{0} 4{ }^{1} 1$ |
|  | $\begin{array}{llll}0 & 4 & 8 \frac{1}{4}\end{array}$ | $0-491$ | 0 | $0 \quad 411 \frac{3}{8}$ | - | $\begin{array}{llll}0 & 5 & 1 \frac{1}{4}\end{array}$ |
|  | $\begin{array}{llll}0 & 5 & 7 \frac{1}{2} & 0\end{array}$ | 0 | $0 \quad 510 \frac{1}{2}$ | $0 \quad 511 \frac{1}{4}$ | 06 | $\begin{array}{llll}0 & 6 & 1 \frac{1}{2}\end{array}$ |
|  | $\begin{array}{llll}0 & 6 & 6 \frac{3}{4}\end{array}$ | $0 \quad 688$ | $0610 \frac{1}{4}$ | $0611 \frac{1}{8}$ | 070 | $\begin{array}{llll}0 & 7 & 1 \frac{3}{4}\end{array}$ |
| $1=8$ | $\begin{array}{llll}0 & 7 & 6\end{array}$ | 07 | $\begin{array}{llll}0 & 710\end{array}$ | $\begin{array}{llll}0 & 7 & 11\end{array}$ | 08 | $8 \quad 2$ |
| $2=16$ | 0150 | 0154 | 158 | $\begin{array}{lllll}0 & 15 & 10\end{array}$ | 016 | $16 \quad 4$ |
| $3=24$ | 126 | 130 | 13 | $1 \begin{array}{lll}1 & 3\end{array}$ | 14 | 146 |
| $4=32$ | 1100 | 110 | 111 | 111 | 112 | 1128 |
| $5=40$ | $117 \quad 6$ | 118 | 119 | 119 | 2 | $2 \quad 0010$ |
| $6=48$ | $2 \quad 50$ | 260 | 27 | 27 | 280 | $2 \quad 9 \quad 0$ |
| H. | 50s. <br> Per Week. | 51s. <br> Per Week. | 52 s. <br> Per Week | 52s. 6d. <br> Per Week. | 53s. <br> Per Week | 54 s. <br> Per Week |
|  | £ | ${ }_{0}^{\text {£ }}$ s. ${ }^{\text {s. }}$ d. |  | $\begin{array}{lll}\text { £ } & s . & d . \\ 0 & 0 & 69\end{array}$ | $£$ $\varepsilon$ $d$ <br> 0 0 6. | ${ }_{6}{ }^{3}$ |
|  | $1{ }^{0}$ | $\begin{array}{llll}0 & 1 & 0^{\frac{3}{4}} \\ & 1\end{array}$ | $\begin{array}{lll}0 & 1 & 1\end{array}$ | $\left\lvert\, \begin{array}{lll}0 & 0 & 6 \frac{16}{16} \\ 0 & 1 & 1 \frac{1}{8} \\ 0\end{array}\right.$ | $1{ }^{1} 1$ | $1{ }^{1} 1$ |
|  | $\begin{array}{llll}0 & 2 & 1\end{array}$ | $0{ }_{0} \quad 21^{1}$ | 022 | $\begin{array}{llll}0 & 2 & 2 \frac{1}{4}\end{array}$ | 0 | 23 |
|  | 0 | 0 | $\begin{array}{llll}0 & 3 & 3\end{array}$ | $\begin{array}{llll}0 & 3 & 3 \frac{3}{8}\end{array}$ | $\begin{array}{llll}0 & 3 & 3 & 3\end{array}$ | $\begin{array}{lll}0 & 3 & 4 \frac{1}{2}\end{array}$ |
|  | 420 | 0 | $\begin{array}{lll}0 & 4 & 4\end{array}$ | $0 \begin{array}{lll}0 & 4 & 4 \frac{1}{2}\end{array}$ | 0 | 46 |
|  | 0 | $\begin{array}{llll}0 & 5 & 3 \frac{3}{4}\end{array}$ | - | $\begin{array}{llll}0 & 5 & 5 \frac{5}{8}\end{array}$ | $\begin{array}{llll}0 & 5 & 61\end{array}$ | $57 \frac{1}{2}$ |
|  | 0 | $0 \quad 6 \quad 4 \frac{1}{2}$ | 06 | $1066 \begin{array}{lll} & 6\end{array}$ | $0 \quad 678$ | 69 |
|  | $\begin{array}{llll}0 & 7 & 3 \frac{1}{2}\end{array}$ | $\begin{array}{llll}0 & 7 & 5 \frac{1}{4}\end{array}$ | 07 | $\begin{array}{llll}0 & 7 & 7 \frac{7}{8}\end{array}$ | $\mathrm{O}_{0} 788^{\frac{3}{4}}$ | $0{ }^{0} 710 \frac{1}{2}$ |
| $1=8$ | $\begin{array}{llll}0 & 8 & 4\end{array}$ | $0{ }^{0} 86.6$ | $\begin{array}{lll}0 & 8 & 8\end{array}$ | $\begin{array}{llll}0 & 8 & 9\end{array}$ | $\begin{array}{llll}0 & 8 & 10\end{array}$ | $\begin{array}{llll}0 & 9 & 0\end{array}$ |
| $2=16$ | $016 \quad 8$ | $017{ }^{\circ}$ | $017 \quad 4$ | 0176 | 0178 | $018 \quad 0$ |
| $3=24$ | 150 | 1556 | 166 | $1 \begin{array}{lll}1 & 6\end{array}$ | 166 | $1 \begin{array}{lll}1 & 7\end{array}$ |
| $4=32$ | 113 | 1140 | 114 | 115 | 115 | 116 |
| $5=40$ | $2 \begin{array}{lll}2 & 1 & 8\end{array}$ | $2 \quad 26$ | 234 | 23 | 242 | 250 |
| $6=48$ | $210 \quad 0$ | 2110 | 2120 | 212 | 213 | 2140 |

Wages Table (Forty-eight Hours per Week) (continued).


Wages Table (Forty-eight Hours per Week) (continued).

| D. H. | 65s. Per Week. | 66s. Per Week. | 67 s. Per Week. | 67s. 6d. <br> Per Week. | 68 s. Per Week. | 69s. <br> Per Week. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $£$ $s$. $d$. <br> 0 0 8.1 <br> 1   | $\begin{array}{lll} \dot{E} & \text { s. } & d . \\ 0 & 0 & 8 \frac{3}{8} \end{array}$ | $\begin{array}{ccc}\text { £ } & s . & d . \\ 0 & 0 & 87 \\ 8\end{array}$ | $\begin{array}{llc}\text { £ } & s . & d . \\ 0 & 0 & 8 \frac{1}{2}\end{array}$ | $\begin{array}{llll}\text { £ } & \text { s. } & d . \\ 0 & 0 & 8 \\ 0 & \text { b }\end{array}$ |
|  | 0 | $0184 \frac{1}{2}$ | 0 | 0 | $01{ }^{-1}$ | $0{ }^{0}$ |
|  | 0288 | 0 | $0 \quad 2 \quad 9 \frac{1}{2}$ | $\begin{array}{llll}0 & 2 & 9 & 3\end{array}$ | $0 \quad 210$ | $0 \quad 210 \frac{1}{2}$ |
|  | $0 \pm 0 \frac{3}{4}$ | $0{ }^{0} 411 \frac{1}{2}$ | $0 \quad 4 \quad 2 \begin{array}{ll}1 \\ 4\end{array}$ | $\begin{array}{llll}0 & 4 & 2 \frac{5}{8} \\ 0\end{array}$ | 43 | $\begin{array}{llll}0 & 4 & 3 & 3 \\ 4\end{array}$ |
|  | $\begin{array}{llll}0 & 5 & 5\end{array}$ | $\begin{array}{llll}0 & 5 & 6\end{array}$ | $\begin{array}{llll}0 & 5 & 7\end{array}$ | $0 \quad 5 \quad 7 \frac{1}{2}$ | 58 | $0 \begin{array}{lll}0 & 5 & 9\end{array}$ |
|  | 6 9 ${ }^{\frac{1}{4}}$ | $0 \quad 610 \frac{1}{2}$ | $0 \quad 611 \frac{3}{4}$ | 0700 | 7 | $7 \quad 2$ <br> 1 |
|  | $\begin{array}{llll}0 & 8 & 11^{1} \\ 0\end{array}$ | 083 | $0884 \frac{1}{2}$ | $\begin{array}{llll}0 & 8 & 5 \frac{1}{4}\end{array}$ | 0886 | $87 \frac{1}{2}$ |
|  | 0 | $0 \quad 9 \quad 7 \frac{1}{2}$ | $0 \quad 9 \quad 9 \frac{1}{4}$ | $0 \quad 9 \quad 10 \frac{1}{81}$ | 0 | $\begin{array}{llll}0 & 10 & 0 \frac{3}{3}\end{array}$ |
| $1=$ | 01010 | 0110 | 0112 | 0113 | 0114 | 0116 |
| $2=16$ | $1 \begin{array}{lll}1 & 1 & 8\end{array}$ | 120 | $\begin{array}{llll}1 & 2 & 4\end{array}$ | $12{ }^{1}$ | 28 | 13 |
| $3=24$ | 112 | 1130 | 1136 | 1139 | $114 \quad 0$ | 1146 |
| $4=32$ | 23 | 240 | 248 | 250 | 5 | 260 |
| $5=40$ | $214 \quad 2$ | 2150 | 21510 | 2163 | 216 | 217 |
| $6=48$ | 5 | 6 | 7 | 7 | 8 | 9 |
| H. | 70s. Per Week. | 71s. Per Week. | 72 s. <br> Per Week. | 72s. 6d. Per Week. | 73 s. <br> Per Week. | 74s. Per Week. |
|  | ${ }^{3}$ | $\underbrace{}_{1}$ s. $\quad$ d. | ${ }^{2}$ | - | $\pm$ ¢. | £ $\quad$ s. $\quad$ d. |
|  | ${ }_{0}^{0} 883$ | 0 0 0 87 | 0 | $00^{0} 00910$ | 0 0 0 | $\begin{array}{lll}0 & 0 & 91 \\ 4\end{array}$ |
|  | $15 \frac{1}{2}$ | $\begin{array}{llllllllll}0 & 1 & 5 \frac{3}{4} \\ 0\end{array}$ | 0 | $0_{0}^{0} 1186 \frac{1}{8}$ | 0 | $1{ }^{6} 1$ |
|  | 211 | $0 \quad 211 \frac{1}{2} 0$ | 0 | $0 \quad 300$ | $0 \quad 3 \quad 0 \frac{1}{2}$ | $\begin{array}{llll}0 & 3 & 1\end{array}$ |
|  | $0 \quad 4 \quad 4 \frac{1}{2}$ | $0 \quad 4 \quad 5 \frac{1}{4} 0$ | 0 | $0 \quad 4 \quad 638$ | $0 \quad 46$ | $4.7 \frac{1}{2}$ |
|  | 510 | 0511 | 0 | $\left.0 \quad 6 \quad 0 \frac{1}{2} \right\rvert\, 0$ | 061 | $\begin{array}{llll}0 & 6 & 2\end{array}$ |
|  | $7 \quad 3 \frac{1}{2} 0$ |  | $\begin{array}{llll}0 & 7 & 6\end{array}$ | $\begin{array}{llll}0 & 7 & 6 \frac{5}{8} \\ 0\end{array}$ | $\begin{array}{llll}0 & 7 & 71\end{array}$ | 0, $788 \frac{1}{2}$ |
|  | $\begin{array}{lll}0 & 8 & 9\end{array}$ | $0{ }_{0} 810 \frac{1}{2} 0$ | 0 | $\begin{array}{llll}0 & 9 & 0 \frac{3}{4}\end{array}$ | $9 \quad 1 \frac{1}{2}$ | $\begin{array}{llll}0 & 9 & 3\end{array}$ |
|  | 010 | 010410 | 0106 | $\begin{array}{llll}0 & 10 & 6 \frac{7}{8}\end{array}$ | $010 \quad 7 \frac{3}{4}$ | $010{ }^{0} 10 \frac{1}{2}$ |
| $1=8$ | 0118 | $\begin{array}{llll}0 & 11 & 10\end{array}$ | 0120 | 0121 | 0122 | $012{ }^{4}$ |
| $2=16$ | 13 | 3 | $1 \begin{array}{lll}1 & 4 & 0\end{array}$ | 1 | 44 | 148 |
| $3=24$ | 115 | 115 | 1160 | 1163 | 1166 | 117 |
| $4=32$ | 26 | $\begin{array}{llll}2 & 7 & 4\end{array}$ | 2880 | $\begin{array}{llll}2 & 8 & 4\end{array}$ | 2888 | $\begin{array}{lll}2 & 9 & 4\end{array}$ |
| $5=40$ | 218 | 219 | 30 | $3 \quad 0 \quad 5$ | $\begin{array}{lll}3 & 0 & 10\end{array}$ | $\begin{array}{llll}3 & 1 & 8\end{array}$ |
| $6=48$ | $310 \quad 0$ | 3110 | 312 | 3126 | 3130 | 3140 |

## Wages table (Forty-eight Hours per Week) (continued).

| D. H. | 75s. <br> Per Week. | $76 s$. Per Week. | 77s. Per Week. | 77s. 6d. Per Week | 78 s. Per Week. | 79s. <br> Per Week. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{array}{ccc}£ & s . & d . \\ 0 & 0 & 9 \frac{3}{8} \\ \end{array}$ | $\begin{array}{ccc} \pm & s . & d . \\ 0 & 0 & 9 \frac{1}{2}\end{array}$ | £ $s$.  <br> 0 0  |  |  | £ s. $d$ <br> 0 0 $9 \frac{7}{8}$ |
|  | $16 \frac{3}{4}$ | 0 | $\begin{array}{llll}0 & 1 & 7 \frac{1}{4}\end{array}$ |  | 0 1 $7 \frac{7}{2}$ | $\begin{array}{llll}0 & 1 & 7 \frac{8}{4}\end{array}$ |
|  | $31 \frac{1}{2}$ | 032 | $\begin{array}{llll}0 & 3 & 2 \frac{1}{2}\end{array}$ | 0 | $0 \quad 3 \quad 3$ | $\begin{array}{llll}0 & 3 & 3 \frac{1}{2}\end{array}$ |
|  | $\begin{array}{llll}0 & 4 & 8 \frac{1}{4}\end{array}$ | $0 \begin{array}{lll}0 & 4\end{array}$ | 0 4 9 | $0 \quad 410 \frac{1}{81}$ | $0410 \frac{1}{2}$ | 0 |
|  | $\begin{array}{lll}0 & 6 & 3\end{array}$ | 64 | 0665 | $0 \quad 6 \quad 5 \frac{1}{2} 0$ | 066 | $\begin{array}{lll}0 & 6 & 7\end{array}$ |
|  | $7 \quad 9 \frac{3}{4}$ | $0 \quad 711$ | $\begin{array}{lll}0 & 8 & 0 \frac{1}{4}\end{array}$ | $\begin{array}{llll}0 & 8 & 07 \\ 0\end{array}$ | $0881 \frac{1}{2}$ | $\begin{array}{llll}0 & 8 & 2{ }_{4}^{3}\end{array}$ |
|  | 9 42 | $0 \quad 96$ | $\begin{array}{lll}0 & 9 & 7 \frac{1}{2}\end{array}$ | $0 \quad 98810$ | $\begin{array}{llll}0 & 9 & 9\end{array}$ | $0{ }^{0} 910 \frac{1}{2}$ |
|  | $01011 \frac{1}{4}$ | 011 | $011{ }^{2}$ | 0113 | 011 41 | $0116 \frac{1}{4}$ |
| $1=8$ | 0126 | 0128 | 01210 | 01211 | 0130 | $013 \quad 2$ |
| $=16$ | 150 | 1554 | 158 | $1 \begin{array}{llll}1 & 10\end{array}$ | 16 | $6 \quad 4$ |
| $3=24$ | 117 | 1180 | 1186 | 118 | 119 | 1196 |
| $4=32$ | 2100 | 2108 | 2114 | 2118 | 212 | 212 |
| $5=40$ | $3 \quad 26$ | 33 | 34 | $\begin{array}{llll}3 & 4 & 7\end{array}$ | 35 | $\begin{array}{lll}3 & 510\end{array}$ |
| $6=48$ | 3150 | 3160 | $317 \quad 0$ | 317 | 3180 | 3190 |
| H. | 80s. | 81s. | $82 \mathrm{~s} .$ |  | 83s. <br> r Week. | 84s. <br> Per Week |
|  |  | $\left.\begin{array}{\|cc\|} £ & s . \\ 0 & 0 \end{array}\right)$ | $\begin{array}{rrr} \boldsymbol{\varepsilon} & s . & d_{i} \\ 0 & 0 & 10 \frac{1}{4} \end{array}$ | $\begin{array}{cc} s . & d . \\ 0 & 10 \frac{5}{18} \end{array}$ | $\begin{array}{rrr} \& & s . & d . \\ 0 & 0 & 10 \frac{3}{8} \end{array}$ |  |
|  | 0 0 18 | 0 | $0188 \frac{1}{2}$ | 0 1 8880 | $\begin{array}{llll}0 & 1 & 8 \frac{3}{4}\end{array}$ | $\begin{array}{llll}0 & 1 & 9\end{array}$ |
|  | 3 | $0 \quad 3 \quad 4 \frac{1}{2}$ | $0 \quad 35$ | $035 \frac{1}{4}$ 0 | $0{ }^{-1} 5$ | $0 \quad 36$ |
|  | 5 | $\begin{array}{llll}0 & 5 & 0 \frac{3}{4}\end{array}$ | $0 \quad 5 \quad 1 \frac{1}{2}$ | 0 5 17 <br> 1   | 0 | 0 |
|  | 68 | $\begin{array}{lll}0 & 6 & 9\end{array}$ | $0 \quad 610$ | $\begin{array}{llll}0 & 610 \frac{1}{2}\end{array}$ | 0611 | $\begin{array}{lll}0 & 7 & 0\end{array}$ |
|  | $\begin{array}{llll}0 & 8 & 4\end{array}$ | 0 $\quad 8 \quad 85$ | 08861 | 088710 | $\begin{array}{llll}0 & 8 & 7 \frac{3}{4}\end{array}$ | $\begin{array}{llll}0 & 8 & 9\end{array}$ |
|  | 010 | $\begin{array}{llll}0 & 10 & 1 \\ 1\end{array}$ | $010 \quad 3$ | $010 \quad 3 \frac{3}{4}$ | $010 \quad 4 \frac{1}{2}$ | 0106 |
|  | 0118 | 011 | 011 11 $\frac{1}{2}$ | 012 03 | $012 \quad 1 \begin{aligned} & 1 \\ & 4\end{aligned}$ | 0123 |
| 8 | 0134 | $\begin{array}{lll}0 & 13 & 6\end{array}$ | 0138 | $013 \quad 9$ | 01310 | $014 \quad 0$ |
| $2=16$ | 168 | 1-7 0 | $1 \begin{array}{lll}1 & 7 & 4\end{array}$ | $1 \begin{array}{lll}1 & 7\end{array}$ | $1 \begin{array}{lll}1 & 7\end{array}$ | 1880 |
| $3=24$ | $2{ }^{2}$ | $\begin{array}{llll}2 & 0 & 6\end{array}$ | $2 \begin{array}{lll}2 & 1 & 0\end{array}$ | 2113 | 21 | 220 |
| $4=32$ | 2.134 | 2140 | 214 | 2150 | 215 | 2160 |
| $5=40$ | 6.8 | $\begin{array}{llll}3 & 7 & 6\end{array}$ |  | $\begin{array}{llll}3 & 8 & 9\end{array}$ | $3 \quad 9 \quad 2$ | $310 \quad 0$ |
| $6=48$ | $4 \quad 0 \quad 0$ | 410 | $4 \quad 20$ | $4 \quad 26$ | 430 | 44 |

Wages Table (Forty-eight Hours per W'eek) (continued).

| D. H. | $\begin{gathered} 85 \mathrm{~s} . \\ \text { Per Week. } \end{gathered}$ | 86s. Per Week. | 87s. <br> Per Week. | 87s. 6d. Per Week. | 88 s. <br> Per Week. | 89s. <br> Per Week. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | s. d. <br> 0 105 <br> 8  | $\begin{array}{cccc}\text { £ } & \text { s. } & \text { d. } \\ 0 & 0 & 10 \frac{3}{4} \\ 0\end{array}$ | $£$ $s$. $d$. <br> 0 0 $10 \frac{7}{8}$ |  | ${ }_{0}^{\text {\& }}$ |  |
|  | 0 1 91 <br> 0 9  | 0 I $19 \frac{1}{2}$ | 0 1 $10{ }^{\frac{3}{4}}$ | $0119 \frac{16}{18}$ | 0 | 0 1 $10 \frac{1}{4}$ |
|  | $0 \begin{array}{llll}0 & 3 & 6 \frac{1}{2} & 0\end{array}$ | $0 \begin{array}{lll}0 & 7\end{array}$ | $0 \quad 3 \quad 7 \frac{1}{2}$ | $\begin{array}{llll}0 & 3 & 7 \frac{3}{4}\end{array}$ | $0 \quad 38$ | $\begin{array}{llll}0 & 3 & 8 \frac{1}{2}\end{array}$ |
|  | $\begin{array}{lllll}0 & 5 & 3 \frac{3}{4} & 0\end{array}$ | $0 \quad 5 \quad 4 \frac{1}{2} 0$ | $0 \quad 5 \quad 5 \frac{1}{4}$ | $0 \quad 5 \quad 5{ }_{5}$ | $0 \times 56$ | $\begin{array}{lllll}0 & 5 & 6 \frac{3}{4}\end{array}$ |
|  | 0 7 1 0 | $\begin{array}{llll}0 & 7 & 2\end{array}$ | $\begin{array}{lll}0 & 7 & 3\end{array}$ | $0 \quad 7 \quad 3 \frac{1}{2}$ | 07 | $7 \quad 5$ |
|  |  | $0 \quad 811 \frac{1}{2} 0$ | $0{ }^{0} 980$ | 09813 | 0 | 0 9 3 <br> 1   |
|  | $010 \quad 7 \frac{1}{2} 0$ | 0109 | $01010 \frac{1}{2}$ | $01011 \frac{1}{4}$ | 0110 | $011{ }^{1} 1$ |
|  | 01243 | $012 \quad 6 \frac{1}{2}$ | $0128 \frac{1}{4}$ | $0129 \frac{1}{8}$ | 01210 | $\begin{array}{llllll}0 & 12 & 11{ }^{\frac{3}{4}}\end{array}$ |
|  | $014{ }^{1}$ | 0144 | $\begin{array}{llll}0 & 14 & 6\end{array}$ | 014 | 0148 | $\begin{array}{llll}0 & 14 & 10\end{array}$ |
| $2=16$ | $1 \begin{array}{lll}1 & 8 & 4\end{array}$ | 188 | 190 | $\begin{array}{lll}1 & 9 & 2\end{array}$ | $9 \quad 4$ | 19 |
| $3=24$ | $2 \quad 2 \quad 6$ | 230 | 236 | 23 | 48 | 24 |
| $4=32$ | 2168 | 217 | 218 | 2184 | 218 | 219 |
| $5=40$ | 31010 | 311 | 312 | 31211 | 313 | 314 |
| $6=48$ | 450 | $4 \quad 60$ | 470 | 476 | 80 | $4 \quad 90$ |
| H. | 90 s. <br> Per Week. | 91s. <br> Per Week | 92 s. <br> Per Week | 92s. 6d. <br> Per Week. | 93s. <br> Per Week | 94s. Per Wee |
|  | $\begin{array}{llr} £ & s . & d . \\ 0 & 0 & 11 \frac{1}{4} \end{array}$ | $\begin{array}{cc} £ & s . \\ 0 & d . \\ 0 & 11 \\ \hline \end{array}$ | $\begin{array}{rrr} \dot{f} & s . & d . \\ 0 & 0 & 11 \frac{1}{2} \end{array}$ |  | ${ }_{0}^{ \pm} \text {s. } \begin{array}{cc} d . \\ 0 & 0 \\ 11 & \frac{5}{8} \end{array}$ | $\begin{array}{lll} £ & s . & d . \\ 0 & 0 & 11 \end{array}$ |
|  | $0 \quad 110 \frac{1}{2} 0$ | $\begin{array}{llll}0 & 1 & 10_{4}^{\frac{8}{4}} \text { - }\end{array}$ | 0111 | $01111 \frac{1}{8}$ | $0111 \frac{1}{4}$ | 0 1 11 <br> 1   |
|  | $\begin{array}{lllll}0 & 3 & 9\end{array}$ | $0 \quad 3 \quad 9 \frac{1}{2}$ | 0 | $0 \quad 310 \frac{1}{4}$ | $0 \quad 310 \frac{1}{2}$ | 0 |
|  | $0 \quad 5 \quad 7 \frac{1}{2} 0$ | $0 \quad 5 \quad 8 \frac{1}{4}$ | $0 \times 59$ | $\begin{array}{llll}0 & 5 & 9 \frac{3}{8}\end{array}$ | $\begin{array}{llll}0 & 5 & 9 \frac{3}{4}\end{array}$ | $\begin{array}{llllllllll}0 & 5 & 10 \frac{1}{2}\end{array}$ |
|  | $\begin{array}{llll}0 & 7 & 6\end{array}$ | $\begin{array}{lll}0 & 7 & 7\end{array}$ | $0{ }_{0} 78$ | $\begin{array}{llll}0 & 7 & 8 \frac{1}{2}\end{array}$ | $0{ }_{0} 78$ | $\begin{array}{llll}0 & 7 & 10\end{array}$ |
|  | $0{ }_{0} 9814 \frac{1}{2}$ | $0 \quad 9 \quad 5 \frac{3}{4}$ | $0 \quad 9$ | 0 9 $7 \frac{5}{8}$ | $0{ }_{0}^{0} 988$ | $\begin{array}{llll}0 & 9 & 9 \frac{1}{2}\end{array}$ |
|  | 011130 | 011 4i | 01116 | $011 \quad 6 \frac{3}{4}$ | 0117 | 0119 |
|  | $\left\lvert\, l l l_{0} 131 \frac{1}{2} 0\right.$ | 013 31 | 013 | 013 57 | $013{ }^{0} 13$ | $\begin{array}{lll}0 & 13 & 8 \frac{1}{2}\end{array}$ |
| 8 | 0150 | $015 \quad 2$ | 015 | $015 \quad 5$ | 015 | 0158 |
| $2=16$ | 1100 | 1104 | 110 | 11010 | 111 | 11114 |
| $3=24$ | $2 \begin{array}{lll}2 & 5\end{array}$ | $2{ }^{2} 56$ | 26 | 26 | 26 | 27 |
| $4=32$ | $3 \begin{array}{lll}3 & 0 & 0\end{array}$ | $\begin{array}{llll}3 & 0 & 8\end{array}$ | 31 | 311 | $3 \quad 2$ | 3.2 |
| $5=40$ | 3150 | 31510 | 3168 | 317 | 3176 | 3184 |
| $6=48$ | $410 \quad 0$ | 4110 | 4120 | 4126 | 4130 | 4140 |

Wages Table (Forty-eight Hours per Week)
(continued).


## CALCULATING RULES. <br> Slide Rule.

The body of the rule is known as the "stock," the sliding portion as the "slide," the metal and glass slide is called the "cursor" or "runner," and enables one to align divisions on the different scales, besides acting as a guide in certain cases: it may have a digit register attached as shown.

The upper scale on the stock is known as A, and the upper scale of the slide as $B$; while the lower scale of the slide is known as C, and the lower scale of stock as D. The scales $A$ and $B$ are similarly divided, so are $C$ and $D$. The main divisions of the lower scales being twice the length of the corresponding divisions on the upper scales, the former are more suited for fine results.

Although the index figure is designated 1, it may be taken to represent any figure that is a multiple of 10 , e.g. $1,10,100$, or $0.1,0.01,0.001$, etc., but once the initial value is assigned to the index for a calculation, the ratio of values must be retained throughout the whole scale. In calculations that involve the use of the upper and lower scales in conjunction, the value assigned to the left index figure of the $D$ scale determines the value of all the divisions of the rule.

Multiplication.-Set the index of the B scale to the factor it is desired to multiply by on the A scale, and over the other factor on $B$ read the product on $A$; or the index of $C$ may be set to one factor on $D$ and under the other factor on $C$ read the product on $D$.

Division.-Set the divisor on B under the dividend on A , and read the quotient on $A$ over the index of $B$; or set the divisor on C over the dividend on D , and read the quotient on D under the index of C .

Combined Multiplication and Division.-
$\frac{a \times b \times c}{d \times e \times f}=x$. Set $d$ on C to $a$ on D , bring runner to $b$ on C . Bring $e$ on C to the runner, and the runner to $c$ on $\mathrm{C}, f$ on C to runner, then under the index of C read $x$ on D .

By inverting the slide so that the $C$ scale lies in contact with the A scale, and the right and left hand indices coinciding, it will be found that by multiplying any number on D by the coincident number on $\mathrm{C}^{\prime}$ is in all cases equal to 10 . In consequence of this the numbers on $\mathrm{C}^{\prime}$ scale are the reciprocals of those coinciding with them on D scale or vice versa. As multiplying by the reciprocal of a number is equivalent to dividing by that number, and dividing a factor by the reciprocal of a number is equivalent to multiplying by that number, it

follows that by using the slide inverted the operation of multiplying and dividing are reversed.

To determine the number of digits in the final results of the several calculations.
When using the lower scale. Rule for the number of digits in a product. The number of digits in a product is equal to the sum of the digits in the two factors if the result is obtained on the left of the first factor; if, however, the result is found to the right of the first factor, the number of digits in the result is equal to the sum of the digits in the two factors minus one.
In applying this rule to decimal values, when the first significant figure does not immediately follow the decimal point, the minus sign is to be prefixed to the number of digits, as many digits being counted minus as there are 0 's following the decimal point. Thus 15 has two digits, $1 \cdot 5$ has one digit, 0.15 has no digit, 0.015 has -1 digit, 0.0015 has - 2 digits, etc.

Rule for the number of digits in a quotient.
If the quotient is obtained with the result appearing on the right of the dividend, the number of digits in the result is found by subtracting the digits in the divisor from those in the dividend; but if the quotient is read on the left, one is to be added to the number of digits obtained as above.

In complicated calculations the digit registering cursor facilitates matters, the pointer being moved in the direction of + or - when a + or - is the result of an intermediate calculation.
When using the upper scale: if the figures cannot be read direct on the scale without making a decimal of it, then if in multiplication, the point moves to the left, add to the number of digits read off as many more as the number of places by which the point was moved. If the point moves to the right these places must be subtracted.
If in division, the point in the divisor is moved to the left, then the places must be subtracted at the end of the operation. If the point moves to the right, then these places must be added at the end of the operation.
Proportion.-Set the first term of a proportion on the C scale to the second term on the D scale, and opposite the third term on the C scale read the fourth term on the D scale.
Inverse proportion, or problems in which " more" requires "less" or "less" requires "more", the work may be simplified by inverting the slide so that the C scale is adjacent to the A scale. By aid of the runner the value on the inverted C (written $\mathrm{C}^{\prime}$ ) scale and on the D scale can be read off.

To reduce a vulgar fraction to the decimal equivalent, place the numerator on $\mathbf{C}$ to the denominator on D when over the index of D we read the decimal equivalent on C . For the inverse operation, set the decimal on C to the index of D , and then opposite to any numerator on $\mathbf{C}$ is found the corresponding denominator of the fraction on $C$.

Squares and Square Roots.-The scale is so constructed that over any number on D will be found its square on A ; likewise over any number on C will be found its square on $\mathbf{B}$. Conversely it follows that under any number on A is found its square root on D , and under any number on B is its square root on C.

To ascertain the number of figures in the square of a number, if the result is read on the right-hand scale of A , the number of digits is equal to twice the number of digits in the original numbers; but if the result is read on the left-hand scale of A the number of digits is one less than twice the number in the original numbers.

Cube and Cube Roots.-Bring the right or left-hand index of C to the given number on D , and over the same number on the left-hand B scale read the required cube on A.

To extract the cube root: move the slide, either from right to left or from left to right, until under the given number on A is found a number on the left-hand B scale identical with the number which is simultaneously found on D under the right- or left-hand index of C. This number is the required cube root.

As by using the four scales it becomes possible by working in the manner described to find three values for the root, in order to decide which of these is the value sought it is necessary to point off the given number into sections of three figures as in the arithmetical method of extraction, commencing at the decimal point and proceeding to the left for numbers greater than unity, and to the right for numbers less than unity; then if the first section of figures, reading from the left, consists of one figure, the number is to be taken on the left-hand scale of A, and the slide is to project to the right. If of two figures, the number is to be taken on the right-hand scale of A with the slide to the right. If of three figures, the number is to be taken on the left-hand scale of A, the slide projecting to the left.

Fourth Power and Roots.-Set the right- or left-hand index of C to the given number on D , and over the number on C read the fourth power on A.

The fourth root may also be extracted by extracting the square root of the square root.

Logarithms. -The mantissa of a logarithm may be read off on the scale $L$ marked on the reverse side of the slide. Set the left-hand index of the $\mathbf{C}$ scale to the given number on the D scale; then turn the rule over and the mantissa will be read on $L$ scale at the index line in the aperture at the right-hand end of the rule.

The number corresponding to a given logarithm may be readily determined by a reversal of the above method.

The characteristic of a logarithm is equal to the number of digits in the number minus 1 . If the number is wholly decimal, the index is equal to the number of ciphers following the decimal point plus 1. In the latter case the characteristic in negative, and is so distinguished by having the minus sign written over it.

To obtain higher roots than cubes it is easier to find the $\log$. of the number and divide it by the root, then set the quotient to the index line in the aperture when the number corresponding to the log. will be found on the scale D under the left-hand index of the $\mathbf{C}$ scale.

Scale of Sines.-On the under side of the slide of the Calculating Rule the scale marked S is the scale of sines, while that marked T is the scale of tangents. The S scale is used to determine the natural sines of angles of from 35 min . to 90 deg. In order to determine the sine of an angle the slide is withdrawn from the stock of the rule and reinserted in such a manner that the scale marked S lies adjacent to the A scale of the rule, and with the right- and left-hand indices coinciding. When the slide is so placed the sine of any angle may be read off on the A scale, immediately above the angle on the S scale. The value of the sines of all angles read on the first half of the A scale, i.e. between 1 and 10 , are such that the decimal point is always followed by 0 , while those read on the right-hand half of the scale A, between 10 and 100, are prefixed by the decimal point only.

To multiply a number by the sine of an angle, place the 1 of the sine scale under the number on the A scale, when the product will be found on the A scale above the stated angle on the sine scale. If the result cannot be read by setting the left-hand index to the number on A, then set the right-hand index to the number.

Scale of Tangents.-In order to determine the tangent of an angle, the slide being reversed is inserted as in the case for sines, the T scale being placed next to the D scale, so that the right and left-hand indices coincide; the respective tangents of the angles marked on the scale $T$ may then be read off on the D scale. The tangents of angles less than 5 deg .43 min .
cannot be read directly from the 10 in . rule, but the corresponding sines may be substituted for them without material error, as the discrepancy only affects the fourth decimal place. If the angle whose tangent is required is greater than 45 deg ., subtract the angle from 90 deg . and find the tangent of the remainder, then divide one by the figures obtained.

To multiply the tangent of an angle by a given figure, divide the tangent into the given number, and the quotient will be the figure required.

## Fuller's Calculating Rule.

Let $F$ be the fixed index, A the top movable index, and $B$ the lower movable index.

When the indices are to be moved, the term Set is used; when the cylinder has to be moved, the term Bring is used.

The scale $n$ is read from the lowest line of the top spiral, and $m$ from the vertical edge of the scale $n$.

The same figures do not always mean the same amount; 1 may stand for $10,100,1000$, or $0 \cdot 1,0 \cdot 01,0 \cdot 001$, etc. The value of results is obtained by rules based on the indices of the logarithms of numbers.

The index of the logarithms of numbers
between 1000 and 9999 is 3 between 0.1 and 0.9999 is $\overline{1}$
 1 and 9.999 is 0
Multiplication.-Start with F and read off the answer at F .
$a \times b=\begin{aligned} & \text { Set A to } 100\end{aligned}$
Bring $b$ to A or B Product read at F

$$
a \times b \times c \times d\left\{\begin{array}{l}
\text { Bring } a \text { to } \mathrm{F} \\
\text { Set A to } 100 \\
\text { Bring } b \text { to A or B } \\
\text { Set A to } 100 \\
\text { Bring } c \text { to A or B } \\
\text { Set A to } 100 \\
\text { Bring } a \text { to A or B } \\
\text { Product read at F }
\end{array}\right.
$$

To find the index of the product take the sum of the indices of the factors, and to this add one each time a factor is brought to B. The sum is the index of the product.

Division. - The numerator must have one factor more than the denominator; if it has not, make it so by bringing the 100 to A. Should there not be one factor less in the denominator than in the numerator, make it so by setting A to 100 for each factor wanting.

|  | (Bring $a$ to F |  | (Bring $a$ to F |
| :---: | :---: | :---: | :---: |
| $a$ | Set A or B to m | $a \times b$ | Set A or B to m |
| $m$ | Bring 100 to A | $m$ | Bring $b$ to A or B |
|  | Quotient read at F |  | Quotient read at F |
|  | (Bring $a$ to F |  | (Bring $a$ to F |
|  | Set A or B to $m$ |  | Set A or B to m |
| $\underline{a \times b \times c}$ | Bring $b$ to A or B | $a$ | Bring 100 to A |
| $m$ | Set A to 100 | $\overline{m \times n}$ | Set A or B to $n$ |
|  | Bring $c$ to A or B |  | Bring 100 to A |
|  | Quotient read at F |  | Quotient read at F |
|  | $($ Bring $a$ to F |  | (Bring $a$ to F |
|  | Set A or B to $m$ |  | Set A or B to $m$ |
| $a \times b$ | Bring $b$ to A or B | $\underline{a \times b \times c}$ | Bring $b$ to A or B |
| $m \times n$ | Set A or B to $n$ | $m \times n$ | Set A or B to $n$ |
|  | Bring 100 to A |  | Bring $c$ to A or B |
|  | Quotient read at F |  | Quotient read at F |

Find the algebraical difference between the sum of the indices of the numerator and the sum of the indices of the denominator, and then every time a factor of the numerator is brought to B , add one to this, and every time B is set to a factor of the denominator deduct one. The result gives the index of the quotient.

Ratio.-When either of the movable indices is at one number and the fixed index at another, and the cylinder is turned into any other position, though the number at the indices will be different their ratio will remain constant.

Logarithms.-Place the upper movable index A to the number, and read the scales $n$ and $m$. These together give the mantissa of the logarithm of the number. To this the index has to be added.

Powers.-To obtain powers not higher, than the seventh the quickest way is by direct multiplication. For powers higher than the seventh multiply the logarithm or the number by the power. Then place the cylinder so that it reads on the scales $n$ and $m$ the decimal part of the quotient. The power is then at the index $A$. In the result the number of figures before the decimal point is one more than the number in the integral part of the quotient.

Roots.-Proceed as in the case of finding
 the power, only divide the logarithm by the root instead of multiplying by the power.

Roots of Decimal Fractions.-Write them as vulgar fractions, and multiply numerator and denominator by ten or a power of ten, so that the denominator may have a complete root. Then take the required root of the numerator by the method given above, and of the denominator by inspection.

$$
\begin{gathered}
\text { Ex. } V \cdot \overline{4}=\sqrt{\frac{4}{10}}=\sqrt{\frac{\overline{40}}{10^{2}}}=\begin{array}{l}
\text { by rule } \\
\text { by inspection }
\end{array} \\
\frac{6 \cdot 3246}{10}=\cdot 6325
\end{gathered}
$$

## SLIDE RULE FOR COMPUTING THE VALUE OF ORES.

A convenient slide rule for rapidly determining the value of an ore containing two metals may be constructed as follows, and is useful when a number of calculations have to be made. Take a gold-bearing copper ore as an example. Gold is worth 4.24 s . per dwt., and let us assume Copper to be worth $£ 60$ per ton or 1,200 shillings, then one unit is worth 12 s . Divide one side of the stationary scale into a convenient number of parts of a suitable size to represent pennyweights, say three divisions or pennyweights to an inch, and subdivide each of these into tenths, having zero at the top of the scale. On the other side of the stationary portion of the scale divide into shillings, making every 10 s . more distinct. The zero for the shillings is also on the top of the scale, and the divisions of the scale are so made that $4 \cdot 24 \mathrm{~s}$. correspond to the 1 dwt. line. The sliding portion of the scale is now divided into percents of copper, for as much copper as the ore is ever likely to contain. The zero is towards the bottom end of the scale ; each percent is made equal to 12 s ., and is subdivided into tenths.

To use the scale, place the percentage of copper against the pennyweight of gold as shown by assay, and read off the combined value on the money scale.

## METHODS OF COMPUTING LODE VALUES.

1. Arithmetical Mean.-The sum of the values and the sum of the widths are added up separately, and each divided by the total number of samples. The results are incorrect since no allowance is made for the relative widths and values.
2. Geometrical Mean.-The width and corresponding value of each cut are multiplied together to give the width-assay expressed in feet-per cent, feet-ounces, inch-pennyweight, which happens to be most convenient. In the case of the first and last numbers, if at the beginning and end of a section the result should be divided by two, as these cuts only represent half the distance the other cuts do. The sum of the assaywidths are then divided by the sum of the widths, the result being the average proportional value.

This is the method commonly used as being simple, and if the samples are taken at short distances fairly correct, but it is based on the false assumption that the width and value remain the same for half the distance on each side of the cut.

The above assumes that the samples are taken at equal distances, but in practice this is often impossible. When the samples are taken at irregular distances the calculation becomes more tedious.

Let $w_{0}, w_{1}, w_{2}, w_{3}$, and $w_{4}=$ width of samples.
,, $v_{0}, v_{1}, v_{2}, v_{3}, \quad, \quad v_{4}=$ corresponding values.
,, $d_{0}, d_{1}, d_{2}$, and $d_{3} \quad=$ distances between samples.
Then the geometrical mean value over the whole area sampled $=$

$$
\frac{v_{0}\left(w_{0} \times \frac{d_{11}}{2}\right)+v_{1}\left(w_{1} \times \frac{d_{0}+d_{1}}{2}\right)+v_{2}\left(w_{2} \times \frac{d_{1}+d_{2}}{2}\right)+}{\left(w_{0} \times \frac{d_{11}}{2}\right)+\left(w_{1} \times \frac{d_{0}+d_{1}}{2}\right)+\left(w_{2} \times \frac{d_{1}+d_{2}}{2}\right)+}+\frac{v_{3}\left(w_{3} \times \frac{d_{3}+d_{3}}{2}\right)+v_{4}\left(w_{4} \times \frac{d_{3}}{2}\right)}{\left(w_{3} \times \frac{d_{2}+d_{3}}{2}\right)+\left(w_{4} \times \frac{d_{3}}{2}\right)}
$$

3. Prismoidal Method.-In this case the prismoidal formula is used :-

End area +4 times middle area + other end area

The area of each end of a prism is obtained by multiplying the width of the sample cut by the assay value. The middle area is obtained by adding the end areas and dividing by two. The length is the distance between the two adjoining samples under consideration. This is more accurate than the geometric mean as the assay-width gradually increases or decreases between two dissimilar cuts; but in nature the boundaries of lodes are generally irregular, not straight lines as assumed.
4. Planimeter Method, proposed by E. T. M. Garlick, is both quick and accurate, especially when the samples are taken at irregular distances and boundaries are not straight lines. Draw a base line, and mark off on it the distance apart of the various cuts to some convenient scale, say 10 feet to 1 inch. On one side of the base line and at right angles to it draw lines from these points to represent the assay-widths, also to scale. Draw connecting lines, straight or curved as they are likely to occur in nature, between the adjoining points, and close the ends of the figure. On the other side of the base draw a similar figure to represent the width of the lode. It is not necessary to use the same scale for the width as for the width-assay if the scale adopted would make the former area too small to measure accurately, or the latter area too unwieldy. If the scale adopted is 10 feet to 1 inch , and the assay-width lines are drawn to the scale of 30 feet to 1 inch, then the ratio would be $1: 3$, so the area of the assay-width would have to be multiplied by 3 in order to bring it to the same standard as the width area.

The area of the width figure obtained by means of a planimeter, divided into the assay-width area, gives the mean assay value.
5. Stoping Width.- It may be necessary in narrow lodes to take out a certain amount of rock in order to make room to work in, and it may be cheaper to treat than sort out the rock. Under such circumstances a correction must be made as follows:-
$\frac{\text { Width of lode } \times \text { assay }}{\text { Total stoping width }}=$ assay over stoping width.

## POINTS OF THE COMPASS.



## MORSE ALPHABET AND FIGURES.



## KNOTS AND SPLICES.

Simple Overhand or Thumb Knot (Fig. 1).-May be used as a stop on a rope to prevent the end from fraying or slipping through a block. A free end is necessary to make it.

Figure of Eight (Fig. 2).-Also used as a stop on a rope: it is less injurious to the fibre of the rope and is easier to undo than the overhand knot.

Reef Knot (Fig. 3).-Used for bending or joining ropes of the same size together.

Single Sheet Bend (Fig. 4).-For joining dry ropes of different sizes when no great strain is expected, also for small cords.

Double Sheet Bend (Fig. 5).-Used for greater security under the same circumstances as the single sheet bend; the second turn round the bight of the rope prevents jambing. It is also used for connecting wet ropes of different sizes.

Hawser Bend (Fig. 6).-For joining large cables. The half hitch bend as shown must have the ends seized, which makes a good permanent joint on heavy ropes, or the ends may be finished off with the bowline bend, which is strong and reliable but requires a considerable length of rope.

Sheep Shank (Fig. 7).-An effective method of quickly shortening a rope. The rope is doubled up so as to reduce it to the required length, a half hitch made round both ends of the fold, and the loop lashed as shown. No free end is required.

Bowline (Fig. 8).-Used to form a loop or bight at the end of a rope, which will not slip. It serves for a man to put his foot in when being lowered on the end of a rope, also for fastening a rope to a bucket.

Bowline on a Bight (Fig. 9).-For a loop in the middle with a doubled rope. The two loops may be used as a chair, a barrel sling, or as man harness, when one loop is placed under each shoulder and tightened it will not slip. When a man is being lowered down a shaft he may sit with one leg through the two loops so as to have the other leg free to guide himself with. If sampling, one loop can be made $2 \frac{1}{2}$ feet long and the other $3 \frac{1}{2}$ feet long : both loops are slipped over the shoulders, the smaller one arranged under the arm-pits, while the larger is fixed under the knees; this will allow the sampler to have the free use of his hands. An insensible man can be raised or lowered in a similar manner

KNOTS AND SPLICES.


without danger of falling out, and if the knot is made in the middle of the rope the lower portion can be used as a guy to steady him.

Two Half Hitches (Fig. 10).-Used for securing the loose ends of lashings, also for securing a rope to timber when no great pull is expected : the end must always be placed at the back away from the pull.

Clove Hitch (Fig. 11).-Used for the commencement and finish of lashings, for fastening guy lines to head of derrick, and all kind of rigging work. It is easily undone, or a bight may be put in instead of one end so as to use it as a slip. It will take a strain in either direction without slackening.

Timber Hitch (Fig. 12).-For handling timber when the weight will keep the bitch taut; for fastening a rope to a windlass barrel, also for starting lashings on scaffolding. For raising or lowering timber, a short length of rope should be left in the direction of the pull, and then a half hitch made higher, above the centre of gravity, to prevent the timber from canting over.

Round Turn and Two Half Hitches (Fig. 13).-For belaying or making a rope fast to an anchorage, so that the strain on the rope shall not jamb the hitch.

Fishermen's Bend (Fig. 14).-For making fast when there is a give-and-take motion, e.g. bending a cable to an anchor; also for securing a rope to a link or to the bail of a bucket. The free end may be lashed to the standing part of the rope to prevent it drawing through.

Man Harness Hitch (Fig. 15).-For forming a loop on drag ropes so that a number of men can get a good purchase for hauling, the loop being of a size to pass over a man's shoulder. This knot can be tied in a rope with neither end free.

Catspaw (Figs. 16, 17, and 18). -This can be made at the end or in the middle of a rope. Used for hooking a block on to.

Blackwall Hitch (Fig. 19).-Used with a pliant rope. It will only hold as long as the weight is applied: also convenient for returning an empty rope on a hook.

Stopper Hitch (Fig. 20).-Used when it is necessary to shift the strain off a rope temporarily, as when testing a cage from the drum.

To sling a Cask horizontally (Fig. 22).-Make a long bight with a bowline and adjust as shown.

To sling a Cask vertically (Fig. 23).-Place the cask in a bight at the end of the rope, and with the running end make a simple overhand knot round the standing part of the
rope; open out the thumb knot, slip it down the side of the cask and secure with a bowline.

To lash one Spar square across another (Figs. 24 and 25).Commence with a clove hitch on the spar $a$ below $b$ and twist the ends together, carry at least four times round the spars as shown in the figure, keeping outside previous turns on one spar and inside on the other; two or more frapping or cross turns are then taken, the corners of the lashings being well beaten in during the process, and finished off with two half hitches round the most convenient span.

To lash two Spars together that tend to spring apart (Fig. 21).-Begin with a timber hitch or running bowline round both spars and draw them together, then take three or four turns across each fork, and finish with frapping turns and two half hitches. Wedges with well-rounded points are often useful for tightening lashings; they should be driven in from the top.

To lash a Block to a Spar (Fig. 26).-Lay the back of the hook against the spar, make a clove hitch round the spar above the hook, then take several turns round the hook and spar, and finish off with two half hitches round the spar below the hook.

## MINING ACCOUNTS AND COSTS.

Every year or half-year a Company should publish a report which includes a Balance Sheet, Profit and Loss Account, and sometimes a Working Account, together with other data that should permit a shareholder or intending shareholder to size up the position of the Company. Frequently the information supplied is too meagre to enable one to analyse the figures as desired, so that further details may have to be sought, which may or may not be available. Certain headings may convey no meaning to a critic. Some accounts are purposely lumped together with the object of masking individual profits or losses. As a matter of fact the ordinary Balance Sheet of a Mining Company is scarcely worth the paper it is printed on, and in order to obtain even an approximate idea of the value of the property other information is necessary, some of which is obtained in the Report, while some must be sought elsewhere. The comparison with previous Reports often supplies required data, and certainly assists one in becoming better acquainted with the condition of things. Sometimes the excuse is given by Directors that it is not for the benefit of the Company to make certain information public for fear
competitors should make use of it. It is the part of a competitor's business to know what others in his line are doing, and knowing his own costs, it is not a very difficult matter to ascertain, near enough, the costs of others; while the shareholder, not having this knowledge, is kept in the dark. A shareholder wishes to ascertain if his capital is safe and what chance there is of legitimately earned profits being paid at stated times.

In order to get a fair insight into the real financial position of a Mining Company it is necessary for a critic to consider the items in detail and classify them in his own way. He must ascertain what assets have been hypothecated to secure special creditors; what is available for the benefit of unsecured creditors ; and after discharging all liabilities, what is left. He should ascertain whether the interest accrued to the date of the Balance Sheet on secured loans is included amongst the liabilities under the heading relating to secured creditors. Then he wants to know the amount due to creditors for goods supplied in the ordinary course of business. The more detail that is given in an annual report the better position one is in to determine the true position of affairs, but as this is likely to lead to questions, essential points are frequently omitted. Besides the total expenses and receipts, and the profit or loss that has been made, one wants to know how the profit or loss has been earned or made, whether it is likely to continue, and if so for how long, what changes may be expected, probable variations in metal market, prospect of labour troubles or lawsuits, life of mine, whether returns are given in long or short tons, for calendar or lunar months, whether the season has been exceptionally favourable or adverse, etc. Figures extending over a long period are more reliable than those for a short time.

The Balance Sheet is a collection of balances left on the Trial Balance after the Profit and Loss Account items have been extracted, and should state the financial position of the Company, i.e. what it is worth. Often the Credit side of a Balance Sheet is headed "Assets" and the debit side "Liabilities." As the term "Asset" is now used in business to mean all available property and rights which can be applied in satisfaction of the liabilities, or which can be turned into money or money's worth, it is better not to use this word here, since a number of items on the Credit side of Balance Sheets are neither valuable property nor rights, and cannot be applied in satisfaction of liabilities or turned into money or money's worth.

A mine is a wasting asset, yet it is usual to see the original
purchase price of the property passed on from year to year, with no attempt to write off the proper proportion, according to the assumed life of the mine. Besides the Mines Property Account, on the Credit side of the Balance Sheet, we have such headings as Mine Development, Mine Plant and Buildings, Office Furniture and Fittings, Stores on Hand, Reserve Fund Investment, Dividend Suspense Account, Ore Concentrates and Matte on Hand or in Transit (at estimated nett value, less advance payments), Sundry Debtors, Cash in Hand, Balance at Bank, and the Deficiency on Profit and Loss Account, if any. The Mine Development Account is the money which has been spent on developing the mine before it reached the producing stage, but should not include among preliminary expenses such items as commissions paid on issue of shares or debentures or discount given in respect of the issue of debentures, these being shown separately, and this has to be written off by degrees as Development Redemption. When once the mine becomes productive, the cost of development may either be added to the Mine Development Account and a certain proportion charged to each ton mined, or the mining has to stand the cost of all the fresh development done during the given period. The Plant and Building, and Furniture and Fittings Accounts should have depreciation written off every period. The depreciation should be so apportioned that the cost is nearly wiped off at the termination of the life of the mine, for the market value of the asset is very small by that time. If the life of a mine is long, some of the plant is out of date and has to be scrapped before it is worn out, for if taken care of, the machinery should in most cases be workable after many years of use. If the life of a mine is taken at, say, ten years, and 10 per cent. is written off for depreciation every year, the amount will not be redeemed in ten years, even if no additions are made in the meanwhile, for it is usual to write the 10 per cent. off the asset remaining, not 10 per cent. of the original asset. When comparing Balance Sheets of different years, should note if preliminary and other expenses are being gradually written off; if not, it is probably because the profit is too small to do this and pay dividends, or because there are no profits against which to charge it. Before the producing stage of a mine is reached, all expenditure should be charged to Capital Account, e.g. (1) Property, (2) Main Shafts and Adits, (3) Underground Development (including shafts sunk on ore), (4) Machinery and Plant, (5) Buildings, (6) Surface Work (reservoirs, railway sidings, roads, etc.), (7) General Expenditure (head office charges, etc.). Any Sundry Revenue received during this stage should be deducted from General Expenditure,
and the balance distributed proportionally over the remaining heads of expenditure. Main Shafts and Adits should be written off under the heading of Depreciation each year for its expected life. Development up to the Revenue stage may be placed to a Temporary Development Account, or may be charged to Capital Account finally. After the producing stage is reached, all expenses in connection with deepening main shafts, cutting stations, and development should be charged direct to Working Costs, or to a Development Redemption Account. In the latter case every ton treated is debited with its proportion of redemption. No expenditure should be debited to Capital Account, except for large special items, e.g. purchase of additional property, increase of machinery, plant, or buildings (but not merely the replacement of them when worn out), sinking of new main shafts, excessive development of payable ore. All such items should bear their proportion of administration and general expenses, but not repairs and maintenance. If an old shaft or mill is replaced by a new one, the old mill or shaft should be written off from Capital Account against Revenue, either at once or by instalments; if this is not done, they should be charged direct to Revenue, if necessary, by instalments, so as to spread the expense over a longer period, and so equalize matters. Depreciation, when written off Profit and Loss Account, only accumulates cash for future shareholders, which reduces the rate of dividends for existing shareholders. Its main object is to make adequate provision out of Revenue for such new machinery, plant, etc., as are almost certain to be required before the mine is worked out, and incidentally it reduces the Income Tax and Fire Insurance Premiums. Instead of deducting depreciation, some prefer to make a small charge on every ton of ore treated, or they appropriate every year a certain proportion of the profits for a Reserve Fund. The gross or nett value of unfinished products, e.g. ore at grass, should not be considered as an asset, but when taken into account should be credited only with the cost, provided the cost does not exceed the market value; but bullion, concentrates, blister copper, and other marketable products ready for shipment, should be shown as assets in the Balance Sheet, and included as Revenue, after deducting all possible returning and other realization charges.

The assets may be classified into (1) those that are actual cash or which can immediately be converted into cash, e.g. cash in hand or balance at bankers; (2) assets which can be realized at comparatively short notice, e.g. investments that can be sold readily on the Stock Exchange ; (3) assets which will take a certain time to realize, e.g. investments not
quoted on the Exchange or which must be realized gradually, also amounts due from debtors; (4) doubtful assets which are only expected to realize a certain percentage of their value, e.g. machinery and buildings, doubtful debts-when debts are known to be irrecoverable they should be written off; (5) other items which can only be realized as long as the business is a going concern, e.g. the amount paid for the property; (6) unrealizable items, the inclusion of which may be quite proper so long as the mining company exists. Some companies have had to go into liquidation in spite of a surplus of assets over liabilities, in consequence of their resources being locked up. If a reserve fund has been created, this only means that a provision has been made from a bookkeeping point of view for a possible deficieney or shrinkage in value of items appearing on the credit side of the Balance Sheet, and this amount should be represented by investments outside the business. When the balance brought forward from the Profit and Loss Account is on the credit side of the Balance Sheet it shows the concern has been working at a loss. A comparison with former Balance Sheets should show whether such loss has been persistent, or whether the profits and losses have fluctuated.

The grouped balances on the debit or liabilities side of the Balance Sheet often include items that are not strictly liabilities. On this side are set out the liabilities of the Company, including not only outside liabilities or debts due to creditors, but also the indebtedness of the concernitself to sundry impersonal accounts, including a surplus or undistributed balance standing to the credit of the Profit and Loss Account. It is usual to head the debit side with details in connection with the capital. The capital may consist of ordinary shares which bear the brunt of risks, and, in consequence, should be entitled to receive the larger share of the profits; preference shares which have the advantage of being entitled to a first claim on the profits of the undertaking, but usually to a limited extent; such shares may be given to vendors in part payment, or may be created when fresh capital is required. Preference shares may only be entitled to participate in profits earned in each particular year, without the right to have any deficiency made good out of the profits of succeeding years, or the shares may be known as cumulative preference shares, which entitles their holders to the full amount of their minimum dividends being satisfied out of future profits, no matter how much such dividends may be in arrear, before the owner of ordinary shares receives any return on their capital. The shares may be preferential for dividend-receiving purposes, but may or
may not be preferential with regard to the distribution of assets when the Company is wound up. Money may be borrowed on debentures secured by a mortgage. Power is generally given to buy up a certain number of debentures a year till they are all redeemed; in the meanwhile an agreed interest has to be paid on those outstanding. A shareholder should know the terms in connection with preference shares and debentures, and he should be able to ascertain from the Balance Sheet whether and to what extent any of the creditors are secured, and what portion of the property has been hypothecated. Paper or nominal capital is never decreased, unless it is considered too unwieldy or it is desired to evade taxation. Its main care is to let the shareholder know what proportion he holds in a mine. The actual value is indicated by the market price of shares, which should vary with the conditions of the mine. The shareholder should consider whether the capital is sufficient to open up and equip the mine properly. The nominal capital is not always fully subscribed, and the shareholder should note whether more shares have been subscribed for since the last period, as it is on the distributed shares that dividends have to be paid. The formation of the company should be carefully investigated. If the vendors have been paid heavy premiums this may prevent the mine from paying adequate dividends to subscribing shareholders. It is a mistake to have too many shares at first; if they rise in value they can always be divided so as to be less cumbersome for ordinary investors to handle. If a mine does not float well, and the shares are left in a few hands, there is always a chance that large parcels may be forced on the market at one time. A large amount of capital does not imply security. If too little capital is provided the company gets into debt, and has to create new shares (generally preference shares to encourage outsiders to subscribe to what has so far been a failure) or money has to be raised on debentures, so the original shareholders may have to wait a long time for interest on their capital, if indeed they ever receive it. Vendors are sometimes given paid-up shares in part payment, and this is often put forward to show the faith the vendors have in the property. In most cases they have no choice, so make a virtue of necessity, but if they accept shares in lieu of cash they generally demand shares of a larger face value than the cash they were prepared to take, as in many cases they sell below par and incidentally bring down the value of the subscribed shares. Anyhow the paid-up shares created absorb a certain amount of profit, lessening the dividends for the subscribed shares. The balance of Profit and Loss

Account when carried to the debit side of the Balance Sheet shows the amount available for distribution. The sum of this and other items on the debit side must correspond with the sum of the items on the credit side, but the apparent balance may be fictitious if the proper proportion has not been written off depreciating assets.
The Profit and Loss Account, or as it is sometimes called the "Revenue Account" is a statement of income and expenditure. The income side should show the sale of metals, etc., and other items of income grouped under suitable headings, e.g. rents of cottages, discounts, rebates, interest, etc., and a comparison should be made with the Profit and Loss Accounts of the preceding few years. The expenditure side should show the various items of expenditure under their proper headings, e.g. office expenses (including directors' and auditors' fees), agency expenses, advertising and stationery, postages, telegrams, and petty cash, general expenses, legal expenses, cables, travelling expenses, rent and other charges in connection with mining leases, exchange and bank charges, land-tax, insurances, interest, donations to hospital, mining account, smelting account, freight, realization charges, dividend and income taxes, depreciation (written off), etc., and should include all unpaid accounts owing at the end of the period, the balance (if any) being profit carried to Balance Sheet. Sometimes the Profit and Loss Account is split up, a working account being shown which is debited with such items as mining, ore treatment, and freight, and credited with value received from products. The balance is then carried to the Profit and Loss Account, which is debited with such items as office expenses, rent, taxes, general expenses, etc., the balance being gross profit or loss. If the former, this is carried over to the credit side of a subdivision of the Profit and Loss Account, and added to any credit balance over from the previous year. On the debit side is shown how the money has been distributed, e.g. in depreciation, purchase of debentures, interest on debentures, etc., the balance being net profit carried to the Balance Sheet and available, if sufficient, for the payment of dividends.

The main subdivisions of the ordinary Profit and Loss Account should correspond with the main subdivisions of the cost sheet, e.g. (1) development, (2) ore extraction, (3) sorting at surface, preliminary crushing, and transport, (4) ore treatment (dressing, amalgamation, smelting, etc.), (5) administration charges and general charges at mine, (6) realization charges on products, (7) taxes and royalties of all kinds, shown separately, (8) head office charges.

Cost keeping gives an intimate knowledge of the inner working of a concern. The object is to obtain the total cost of work and an analysis of such cost. Intelligently used it enables a manager to detect waste of material, loss of time, in fact to lay his finger on leakages, so that he can reduce his expenditure and increase his profits. Costs are useful for future reference, and serve as a check on similar work. Cost keeping is a system of recording the materials used and the labour employed on a particular job. To draw up a system suitable for any particular mine, requires a man with practical experience of the requirements of mining and methods employed. The system of cost keeping need not be complicated, but the smaller the company the less elaborate it should be. The fact that a company has a large capital is no excuse for extravagance. It is generally found that when once the mine officials have the object and utility of costing properly explained to them they take a great interest in it; and their co-operation is necessary for the success of the scheme. The system should be made as automatic as possible by getting others to fill in the forms as far as they can. There should be no repetition necessitating copying, except totals; any duplicates required are done with carbon paper. So far as possible everything is worked out on the double entry system, which serves as a check against fraud and personal error. Technical results are expressed in ounces, per cent., tons, or feet, and should not be confused with commercial results expressed in $£ s . d$. The card system is used where applicable, as being time and labour saving. If no proper accounts are kept, material may be used on a job and never be entered up. Except during construction when requirements are abnormal, the storekeeper has the best idea of what stock should be kept in hand to suit local requirements, taking time for transit into consideration, rainy seasons, droughts, etc. The various foremen know beforehand if any special stock is likely to be required, and may notify the storekeeper personally or on a special form. A list of stores likely to be required is often printed, and tenders called for supplies. From the tenders the storekeeper can ascertain the current prices for, say, a year. When any stock gets low the storekeeper fills out an order form, stating the size, quantity, and quality of the article required. A carbon copy is made to be filed in the office and the price entered on it. The original is sent to the merchant and to it is attached the Company's duplicate invoice form ; some of the blanks on it are filled in before the form leaves the office, others on its return, while the merchant fills in the other spaces. This serves the purpose of a Stores

Inward Book. The order number is the consecutive number of the order as sent out, commencing afresh every month; the storekeeper's progressive number also starts afresh every month, and is the consecutive number of invoice as received back. The sea freight is obtained from the agent, the railage from the railway company, but is of course checked as to rates. The total is then transferred to Stock Cards. The merchant returns the Company's duplicate invoice, together with his original invoice. The duplicate is filed at the mine, while the original is sent to the head office in support of vouchers for payment. There is a separate Stock Card for each kind or size of article, and they are printed on each side. The stock received is filled in from the duplicate invoice. What has been issued can be traced through the number of the Requisition form; the balance in stock can be seen at a glance, while the minimum stock that should be kept in hand is noted in one corner. Stores Requisition forms are printed in books with butts, and should be of such a size that they can easily fit in the foreman's pocket. They are worded in such a way that they can be filled in for any department. The form is filled in and initialled by a foreman, and when an article is given out it is signed for by the employee receiving it. Job cards are printed in two colours, one for surface jobs, the other for underground. Each job has its special number. A fresh card is used every month for each job. The total of the card is posted to its account in the Ledger, and the daily expenditure to the Daily Cost Sheet. Each man has a token with the number assigned to him on it. Before proceeding to work he hands this to the timekeeper who gives him a Labour Daily Time Check in exchange; this may be printed on different-coloured paper for the different shifts. The employee fills in the check with his name, the class of work he has been employed on, and the time occupied at the different jobs; this is signed by his foreman and handed to the timekeeper at the end of his day's work. The next day the timekeeper apportions the labour to the different jobs on which it has been employed and enters it on the Labour Job Cards, which, like the Stores Job Cards, are also in different colours for surface and underground jobs.

Cost Sheets are prepared periodically, say monthly, for the benefit of the Management and Directors (not for publication), in order to show the progress of business. All items which occur regularly should appear under the same heading each time. Suitable main headings are : (A) Mining. (1) Mine Capital Expenditure (shaft sinking, plat cutting, and shaft bins) ; (2) Mine Development (shaft sinking, plat cutting,
driving, cross - cutting, rising, winzing, diamond drilling) ;
(3) Ore Extraction (breaking ore, shovelling, filling stopes, trucking, hoisting ore). In connection with these, details should be given of gross figures for the following, as well as the cost per ton: (a) Shifts worked (by contract, by day labour), (b) Work done (footage sunk, risen, or driven, or tons broken), (c) Wages (miners, truckers, timbermen), (d) Management and General Office Expenses, (e) Stores (showing quantity and value of explosives, candles, timber, general), $(f)$ Power (hoisting, drills, pumping), ( $g$ ) General Charges, ( $h$ ) Sampling, Assaying, and Surveying, (i) Total Expenses for the month, (j) Total Expenses to the end of previous month, ( $k$ ) Total Expenses to date. (B) Sorting at Surface, Preliminary Crushing and Transport. This is intermediate work between the mine and the treatment works, and may have sub-headings, e.g. (a) Labour (pickers, breakers, truckers), (b) Management and General Office Expenses, (c) Stores, (d) Power, (e) General Charges, $(f)$ Total Cost, $(g)$ Gross Tonnage handled, ( $h$ ) Proportion of different Classes of Ore Sorted and Waste discarded. (C) Ore Treatment. This naturally varies with the class of treatment, whether ore dressing, amalgamating, cyaniding, smelting, etc., and whether one or more methods are employed. Each department should have its own special detailed Cost Sheet; for instance, a gold-mine might have the following sub-headings: (1) Milling, (2) Concentrating, (3) Roasting, (4) Fine Grinding, (5) Cyaniding, (6) Filter Pressing, (7) Precipitation and Smelting, (8) Disposal of Residues, giving items, e.g. (a)the Quantities treated, (b)Labour, (c)Salaries, (d) Stores, (e) Repairs and Maintenance, ( $f$ ) Power, ( $g$ ) Water, ( $h$ ) Assaying and Sampling, (i) Various Supplies (quicksilver, shoes, and dies, cyanide, lime, zinc, sulphuric acid, filter cloth, fluxes, coke, etc., giving their quantities and values). A smelting proposition, depending on its nature, may have headings such as Smelting, Calcining, Converting, Refining, etc., and the Various Supplies would contain such items as water-jackets, slag-pots, etc. (D) Management and General Office Expenses. This may have sub-headings such as (1) Consulting Engineer's and General Manager's Fees, (2) Office Staff, (3) Stationery, Postage, and Telegrams, (4) Medical and Sanitary Charges, (5) Travelling Expenses, (6) Fire and Accident Insurance, (7) Stabling, (8) Local Bank Charges. These are charged against different Departments in proportion to the costs of each Department. (E) Realization Charges on Products, with sub-headings of (1) Transport to Railway, (2) Railway Freight, (3) Shipping Charges, Agency, and Commission, (4) Sea Freight, Insurance, etc., (5) Selling Expenses, (6) Returning

Charges, etc. ( $F$ ) Income Tax, Royalties, and other Taxes. Head office charges, e.g. rent, directors' fees, legal expenses, bank charges, auditors' fees, foreignagency expenses, advertising, and interest on loan or debentures, are not known at the mine, so cannot be added.

Separate accounts should be shown, giving on the debit side the cost, and on the credit side how it has been distributed to the main headings for Power, Hoisting, Compressed Air, Pumping, Sampling, Assaying, and Surveying, Repairs and Maintenance, General Charges (blacksmith, foremen, etc.), and if Construction and Equipment is being proceeded with, show sub-headings (1) Machinery and Plant, (2) Buildings, giving the cost of any job to the end of the previous month, the cost for the present month of labour, machinery, timber, stores, management, and general office expenses, etc., and the total expenditure to date. A Distribution form shows the total cost of wages and stores for Mining and Treatment, Extraction, and other headings. A Stores Account shows the value of stores on hand at end of the previous month, what has been received during the month, issued during the month, and on hand at date. A Cash Account shows the balance at Bank at the commencement of the month, the money received from head office, sundry receipts, expenditure for the month, and balance in Bank at date. A Summary shows the Expenditure to end of previous month, Expenditure for present month, Total Expenditure to end of the period for (a) development, (b) mining, (c) ore treatment, (d) construction and equipment, (e) general expenses, $(f)$ realization on products, $(g)$ total ordinary working costs. Technical details according to the class of treatment should have in tabulated form the number of hours run, tons of ore treated (from the mine, purchased ore), tons of revert (first matte, convertor slag, flue dust, etc.), fluxes (ironstone and limestone), weight of products, value of metals, yield per ton, percentage of extraction, ore on hand, etc. The Capital Account shows Development (after deducting charges to ore extraction), Construction, and Equipment, Total Expenditure, Less Sales of Plant, Nett total of Capital Account. The Working Account shows Ore Extraction (including charges on Ore from Development), Treatment, General Expenses, Realization, Total Ordinary Working Costs, Retreatment, Grand Total Working Account, Gross Income from all Sources, Nett excess (or loss) over working expenditure, Nett excess (or loss) over all expenditure. The tonnage of broken ore in the stopes at date and its cost per ton.

## CORRECTIONS FOR THE PRESS.

O/ or 厅 (dele) delete, take out, expunge.
( turn a reversed letter.
a space or more space between words, letters, or lines.
less space or no space between words or letters.
Lor 」 carry a word further to the right or left.
$\square$ indent, to begin further in from the margin.
[ bring a word or words to the beginning of a line; also make a new paragraph.

- make a new paragraph.
- (underline), change from italic to roman, or roman to italic, as the case may be.
$\overline{7}$ (underline), put in small capitals.
7 elevate a letter, word, or character sunk below the proper level.
$\square$ sink or depress a letter, word, or character that is raised above the proper level.
shows that part of a paragraph projects laterally beyond the rest.
1 directs attention to a quadrat or space which improperly appears.
$\times$ or + directs attention to a broken or imperfect type.
w.f. wrong font, used when a character is of a wrong type, size, or style.
it. italic.
trs. transpose.
l.c. lower case, i.e. put in small or common letters a word or letter that has been printed in capitals or small capitals. s. cap. or sm. c. put in small capitals.
qu., qy., or ? query.
out s.c. words are wanted, see copy.


## WEIGHTS, DIMENSIONS, AND PROPERTIES OF VARIOUS ARTICLES.

Table of Weight of Water (at $62 \frac{1}{4}$ lbs. per Cubic Foot) contained in One Foot Length of Pipes of Different Bores (Trautwine).

| Bore. Ins. | Water. Lbs. | Bore, Ins. | Water. Lbs. | Bore. Ins. | Water. Lbs. | Bore. Ins. | Water. Lbs. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\frac{1}{8}$ | 0'005320 | 6 | 12.25712 | 23 | $180 \cdot 1116$ | 62 | $1308 \cdot 788$ |
| $\frac{8}{8}$ | $0 \cdot 021280$ | $6{ }^{1}$ | 13.29983 | 24 | 196.1139 | 63 | 1351.347 |
| \% | 0.047879 | 6 | 14.38509 | ${ }_{2}^{25}$ | ${ }_{212} 217972$ | 64 | 1394.588 |
| $\frac{2}{5}$ | 0.085119 | ${ }^{6}$ | 15.51292 | 26 | 230.1615 | 65 | 1438.509 |
| $\frac{3}{4}$ | ${ }_{0}^{0} 1191518$ | 7 | 16.68330 $17^{\circ} 89625$ | 27 28 | ${ }_{266.9328}^{248}$ | 66 67 | 1488.112 |
| $\frac{1}{8}$ | ${ }_{0}{ }^{\circ} 219060677$ | $7{ }^{7}$ | 1789625 1915175 | ${ }_{29}^{28}$ | 266.9328 2869 | 67 | 1528395 |
| $1{ }^{8}$ | $0 \cdot 340476$ | $7{ }^{\text {a }}$ | 20.44981 | 30 | 3064280 | 69 | 1621.004 |
| $1{ }^{16}$ | $0 \cdot 430914$ | 8 | 21'79044 | 31 | 327'1970 | 70 | $1668{ }^{\circ} 330$ |
| $1{ }^{18}$ | 0.531993 | 8 | 23.17362 | 32 | 348.6470 | 71 | 1716.337 |
| ${ }^{13}$ | 0.643712 | 8 | 24.59936 | 33 | $370 \times 7779$ | 72 | 1765.025 |
| 11 | $0 \cdot 766070$ | $8{ }^{3}$ | 26.06766 | 34 | $393 \times 5897$ | 73 | 1814.394 |
| 1章 | 0'899968 | 9 | 27.57852 | 35 | 417.0826 | 74 | 1864.444 |
| 1娄 | 1.042706 | $9{ }_{9}$ | 29.13194 | 36 | ${ }^{441 \cdot 2563}$ | 75 | 1915.175 |
| ${ }_{8}^{17}$ | 1.196984 | $9{ }^{9 \frac{1}{3}}$ | ${ }^{30} 72792$ | 37 | 466.1110 | 76 | 1966.587 |
| $\stackrel{2}{2 / 8}_{1}^{18}$ | ${ }_{1}^{1} 3631902$ | $10^{9 \frac{3}{4}}$ | 32.36646 34.04756 | 38 39 | 491:6467 5178633 | 77 | ${ }_{2} 201816850$ |
| 2 | 1'723658 | $10 \frac{1}{2}$ | 37.53743 | 40 | $544 \cdot 7609$ | 79 | 2124.908 |
| ${ }^{2 \frac{3}{8}}$ | 1.920495 | 11 | 41.19754 | 41 | 572'3394 | 80 | 2179.044 |
| $2{ }^{\frac{1}{2}}$ | ${ }^{2} 127972$ | $11 \frac{1}{2}$ | $45^{\circ} 02789$ | 42 | $600 \cdot 5989$ | 81 | $2233 \cdot 860$ |
| $2{ }^{\text {2 }}$ | 2'346089 | 12 | $49^{\circ} 02848$ | 43 | 629'5393 | 82 | 2289•358 |
| $2{ }^{2}$ | ${ }^{2} \cdot 574846$ | $12 \frac{1}{2}$ | 53.19931 | 44 | 659.1607 | 83 | 2345*536 |
| ${ }^{2 \frac{7}{8}}$ | ${ }^{2} 8814243$ | 13 | 57.54037 | 45 | 689.4630 | 84 | 2402:396 |
| $\stackrel{3}{1}$ | 3.064280 | $13^{\frac{1}{2}}$ | 62.05167 | 46 | $720 \cdot 4463$ | 85 | 2459.936 |
| ${ }^{31}$ | ${ }^{3 \cdot 324957}$ | 14 | ${ }^{66} 73321$ | 47 | 752.1105 | 86 | $2518 \cdot 157$ |
| $3^{3 \frac{1}{4}}$ | 3.596273 | 14 ${ }^{\frac{1}{2}}$ | 71.58499 | 48 | 784.4557 | 87 | 2577.060 |
| ${ }_{3}^{3 .}$ | 3.878229 | 15 | ${ }^{76660700}$ | 49 | 817.4818 | 88 | 2636.643 |
| 31 | 4.170826 | $15 \frac{1}{\frac{1}{2}}$ | 81.79925 | 50 | 851.1889 | 89 | 2696.907 |
| 38 3 3 | 4.474062 | 16 | 87.16174 | 51 | 885.5769 | 90 | 2757852 |
| ${ }^{3}$ | $4^{4} \cdot 7879388$ | ${ }^{16 \frac{1}{2}}$ | 92.69447 | 52 | 9206459 | 91 | 2819.478 |
| ${ }^{38}$ | 5.112453 | 17 | 98.39744 | 53 | 956'3958 | 92 | $2881 \cdot 785$ |
| 4 | 5.447609 | $17 \frac{1}{2}$ | 104.27064 | 54 | $992 \cdot 8267$ | 93 | 2944'773 |
| 4 | 6.149840 | 18 | 110.31448 | 55 | 1029.9386 | 94 | 3008.442 |
| $4{ }^{4 \frac{1}{2}}$ | 6.894630 7681980 | ${ }_{19}^{18}$ | ${ }_{122} 11.91168$ | 56 57 | 1067'7314 | 95 | 3072.792 3137.823 |
| 5 | 8.511889 | $19 \frac{1}{2}$ | $129 \cdot 46583$ | 58 | ${ }_{1145} \times 3598$ | 97 | ${ }_{3203} 535$ |
| 5 | 9.384358 | 20 | $136 \cdot 19022$ | 59 | $1185 \cdot 1954$ | 98 | 3269.927 |
| 5 5 | 10'299386 | 21 | 150'14972 | 60 | 1225 '7120 | 99 | 3337.001 |
| 5 | 11'256973 | 22 | $164 \cdot 79017$ | 61 | 1266'9096 | 100 | $3404 \times 756$ |

The weight of water in one foot length of any bore = inner diameter ${ }^{2} \times 0.339521$.

Table of Approximate Proportions and Weights of 9 Feet Lengths of Cast-iron Pipes of various Sizes.

|  |  |  |  |  |  |  |  | Weight. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ins. | In. | ${ }_{6}^{\text {In }}$ | In. $\frac{9}{16}$ | In. | In. | $\mathrm{In}_{4}$ | Cwts. | Qrs. $3$ | $\begin{gathered} \text { Lbs. } \\ 0 \end{gathered}$ |
| 3 | $\frac{3}{8}$ | $7 \frac{1}{2}$ | $\frac{8}{8}$ | 6 | $\frac{5}{8}$ | 4 | 1 | 0 | 3 |
| 4 | $\frac{1}{2}$ | $9 \frac{1}{2}$ | $\frac{3}{4}$ | $7 \frac{3}{4}$ | $\frac{3}{4}$ | 4 | 1 | 3 | 5 |
| 5 | $\frac{1}{2}$ | $10 \frac{1}{2}$ | $\frac{7}{8}$ | $8 \frac{3}{4}$ | $\frac{3}{4}$ | 4 | 2 | 1 | 12 |
| 6 | $\frac{8}{8}$ | 12 | $\frac{7}{8}$ | 10 | $\frac{7}{8}$ | 4 | 3 | 2 | 1 |
| 7 | $\frac{5}{8}$ | 14 | 1 | $11 \frac{3}{4}$ | ${ }^{7}$ | 6 | 4 | 3 | 17 |
| 8 | $\frac{3}{4}$ | 15 | 1 | $12 \frac{3}{4}$ | 1 | 6 | 5 | 2 | 9 |
| 9 | $\frac{3}{4}$ | 161 $\frac{1}{2}$ | $1 \frac{1}{16}$ | $14 \frac{1}{4}$ | 1 | 6 | 6 | 1 | 12 |
| 10 | $\frac{3}{4}$ | $17 \frac{1}{2}$ | $1 \frac{1}{8}$ | $15 \frac{1}{2}$ | 1 | 6 | 7 | 0 | 0 |
| 11 | $\frac{7}{8}$ | 19 | $1 \frac{3}{16}$ | $16 \frac{3}{4}$ | 1 | 6 | 8 | 3 | 24 |
| 12 | $\frac{7}{8}$ | 20 | $1 \frac{1}{4}$ | $17 \frac{3}{4}$ | $1 \frac{1}{8}$ | 6 | 9 | 3 | 5 |
| 13 | ${ }_{8}^{7}$ | 21 | $1 \frac{1}{4}$ | $18 \frac{3}{4}$ | $1 \frac{1}{8}$ | 8 | 10 | 2 | 0 |
| 14 | 8 | 22 | $1 \frac{1}{4}$ | $19 \frac{3}{4}$ | $1 \frac{1}{8}$ | 8 | 11 | 0 | 26 |
| 15 | $\frac{7}{8}$ | 23 | $1 \frac{1}{4}$ | $20 \frac{3}{4}$ | $1 \frac{1}{8}$ | 8 | 12 | 0 | 25 |
| 16 | ${ }^{7}$ | $24 \frac{1}{2}$ | $1 \frac{5}{16}$ | 22 | $1 \frac{1}{4}$ | 8 | 12 | 3 | 8 |
| 17 | ${ }_{8}^{7}$ | $25 \frac{1}{2}$ | $1 \frac{5}{16}$ | 23 | $1 \frac{1}{4}$ | 8 | 13 | 2 | 17 |
| 18 | 1 | $26 \frac{1}{2}$ | 138 | 24 | $1 \frac{1}{4}$ | 8 | 16 | 1 | 15 |
| 19 | 1 | 28 | $1 \frac{3}{8}$ | 25 | $1 \frac{3}{8}$ | 8 | 17 | 2 | 13 |
| 20 | 1 | 29 | $1 \frac{3}{8}$ | 26 | $1 \frac{3}{8}$ | 8 | 18 | 0 | 26 |

Table of the Weight of 100 Feet of Wire in Pounds, when the Size is measured by the New Standard Wire Gauge of 1884.

| Size by Gauge. | Diameter in Inches. | Copper Wire. | Brass <br> Wire. | Steel Wire. | Iron <br> Wire. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} \text { No. } \\ 1 \end{gathered}$ | -300 | $\underset{26 \cdot 8}{\text { Lbs. }}$ | $\underset{25 \cdot 7}{\text { Lbs. }}$ | $\underset{24 \cdot 0}{\text { Lbs. }}$ | $\begin{aligned} & \text { Lhs. } \\ & 23 \cdot 4 \end{aligned}$ |
| 2 | $\cdot 276$ | 22.5 | 21.6 | $20 \cdot 1$ | $19 \cdot 6$ |
| 3 | -252 | $18 \cdot 8$ | $18 \cdot 1$ | $16 \cdot 8$ | 16.4 |
| 4 | $\cdot 232$ | $15 \cdot 8$ | $15 \cdot 2$ | $14 \cdot 3$ | $13 \cdot 8$ |
| 5 | -212 | $13 \cdot 4$ | 12.7 | $11 \cdot 9$ | $11 \cdot 6$ |
| 6 | -192 | $10 \cdot 9$ | 10.5 | $9 \cdot 7$ | 9.5 |
| 7 | $\cdot 176$ | 9.2 | $8 \cdot 8$ | $8 \cdot 2$ | $8 \cdot 0$ |
| 8 | -160 | $7 \cdot 6$ | $7 \cdot 3$ | $6 \cdot 8$ | $6 \cdot 6$ |
| 9 | -144 | $6 \cdot 1$ | $5 \cdot 8$ | $5 \cdot 4$ | $5 \cdot 3$ |
| 10 | -128 | 4.99 | $4 \cdot 65$ | $4 \cdot 34$ | $4 \cdot 23$ |
| 11 | -116 | $4 \cdot 00$ | $3 \cdot 80$ | $3 \cdot 55$ | $3 \cdot 46$ |
| 12 | $\cdot 104$ | $3 \cdot 22$ | $3 \cdot 08$ | $2 \cdot 87$ | $2 \cdot 80$ |
| 13 | -092 | $2 \cdot 48$ | $2 \cdot 37$ | $2 \cdot 22$ | $2 \cdot 16$ |
| 14 | -080 | 1.91 | $1 \cdot 83$ | 1.70 | $1 \cdot 66$ |
| 15 | -072 | $1 \cdot 53$ | $1 \cdot 46$ | $1 \cdot 36$ | $1 \cdot 33$ |
| 16 | -064 | $1 \cdot 22$ | $1 \cdot 16$ | $1 \cdot 08$ | 1.06 |
| 17 | -056 | $0 \cdot 92$ | $0 \cdot 88$ | $0 \cdot 82$ | $0 \cdot 80$ |
| 18 | . 048 | $0 \cdot 69$ | $0 \cdot 66$ | 0.62 | 0.60 |
| 19 | -040 | $0 \cdot 46$ | $0 \cdot 44$ | 0.41 | $0 \cdot 40$ |
| 20 | -036 | $0 \cdot 38$ | $0 \cdot 36$ | $0 \cdot 34$ | $0 \cdot 33$ |

If any less quantity than 100 feet is required, multiply the weight of 100 feet as found in the table by the number of feet wanted, and divide by 100 thus-

Required the weight of 50 feet of No. 16 copper wire.
100 feet of No. 16 gauge copper wire weighs 1.22 lbs.; therefore $100: 1.22:: 50:$ required weight $=0.61 \mathrm{lbs}$.


| Thickness by Gauge. | Thickness in Inches. | Lead. | Copper. | Gun Metal. | Brass. | White Metal. | Steel. | Wronght Iron. | Zinc. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Lbs | Lbs. | Lbs. | Lbs. | Lbs. | Lbs. | Lhs. | Lis. |
| 13 | -092 | $5 \cdot 49$ | $4 \cdot 21$ | $4 \cdot 17$ | $4 \cdot 03$ | $3 \cdot 84$ | $3 \cdot 76$ | $3 \cdot 66$ | $3 \cdot 4.5$ |
| 14 | -080 | $4 \cdot 77$ | $3 \cdot 66$ | $3 \cdot 63$ | $3 \cdot 50$ | $3 \cdot 34$ | $3 \cdot 26$ | $3 \cdot 18$ | $3 \cdot 00$ |
| 15 | -072 | $4 \cdot 30$ | $3 \cdot 30$ | $3 \cdot 26$ | $3 \cdot 14$ | $3 \cdot 00$ | $2 \cdot 94$ | $2 \cdot 86$ | $2 \cdot 70$ |
| 16 | -064 | 3-81 | $2 \cdot 92$ | $2 \cdot 89$ | $2 \cdot 80$ | $2 \cdot 66$ | $2 \cdot 60$ | $2 \cdot 54$ | $2 \cdot 40$ |
| 17 | -056 | $3 \cdot 21$ | $2 \cdot 46$ | $2 \cdot 44$ | $2 \cdot 35$ | $2 \cdot 25$ | $2 \cdot 19$ | $2 \cdot 14$ | $2 \cdot 02$ |
| 18 | -048 | $2 \cdot 86$ | $2 \cdot 20$ | $2 \cdot 18$ | $2 \cdot 10$ | $2 \cdot 00$ | $1 \cdot 96$ | $1 \cdot 91$ | $1 \cdot 80$ |
| 19 | -040 | $2 \cdot 38$ | $1 \cdot 83$ | $1 \cdot 81$ | $1 \cdot 75$ | $1 \cdot 67$ | $1 \cdot 63$ | $1 \cdot 59$ | $1 \cdot 49$ |
| 20 | -036 | $2 \cdot 14$ | 1:64 | $1 \cdot 63$ | 1.57 | $1 \cdot 50$ | $1 \cdot 47$ | $1 \cdot 43$ | $1 \cdot 35$ |
| 21 | -032 | 1.92 | $1 \cdot 47$ | $1 \cdot 46$ | 1.41 | $1 \cdot 34$ | $1: 31$ | $1 \cdot 28$ | $1 \cdot 24$ |
| 22 | -028 | $1 \cdot 66$ | $1 \cdot 28$ | $1 \cdot 26$ | $1 \cdot 22$ | $1 \cdot 16$ | $1 \cdot 14$ | 1-11 | $1 \cdot 05$ |
| 23 | -024 | $1 \cdot 43$ | $1 \cdot 09$ | $1 \cdot 08$ | $1 \cdot 04$ | $1 \cdot 00$ | $0 \cdot 97$ | 0.95 | $0 \cdot 89$ |
| 24 | -022 | $1 \cdot 30$ | $1 \cdot 00$ | 0.99 | 0.96 | 0.91 | $0 \cdot 89$ | $0 \cdot 87$ | 0.82 |
| 25 | -020 | $1 \cdot 18$ | 0.91 | $0 \cdot 90$ | $0 \cdot 87$ | $0 \cdot 83$ | 0.81 | $0 \cdot 79$ | $0 \cdot 74$ |
| 26 | -018 | $1 \cdot 06$ | $0 \cdot 82$ | $0 \cdot 81$ | 0.78 | $0 \cdot 74$ | 0.73 | 0.71 | $0 \cdot 67$ |
| 27 | -0164 | 0.97 | $0 \cdot 75$ | $0 \cdot 74$ | $0 \cdot 71$ | $0 \cdot 68$ | $0 \cdot 67$ | $0 \cdot 6.5$ | $0 \cdot 62$ |
| 28 | -0148 | $0 \cdot 87$ | $0 \cdot 60$ | $0 \cdot 65$ | $0 \cdot 64$ | 0.61 | $0 \cdot 60$ | $0 \cdot 58$ | $0 \cdot 54$ |
| 29 | -0136 | 0.81 | $0 \cdot 62$ | $0 \cdot 61$ | $0 \cdot 60$ | 0.57 | 0\%5 | $0 \cdot 54$ | $0 \cdot 50$ |
| 30 | $\cdot 0124$ | 0.75 | $0 \% 8$ | $0 \cdot 57$ | 0.55 | 0.52 | $0 \cdot 51$ | $0 \% 0$ | $0 \cdot 47$ |

Table of Sizes, \&c., of Battery Screens.

| No. of Needle. | $\begin{aligned} & \text { Corre- } \\ & \text { sponding } \\ & \text { Mesh. } \end{aligned}$ | Width of Slot (inches) | Thickness of Iron (Russian Gange). | Thickness of Iron (American Gauge). | Weight per square foot. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 5 | 20 | $\frac{29}{1000}$ | No. 14 | No. $23 \frac{1}{4}$ | $1 \cdot 15$ pounds. |
| 6 | 25 | $\frac{27}{1000}$ | No. 13 | No. 24 | 1.08 |
| 7 | 30 | $\frac{24}{1000}$ | No. 12 | No. $24 \frac{1}{2}$ | 0.987 |
| 8 | 35 | 1000 | No. 11 | No. 25 | 0.918 |
| 9 | 40 | $\frac{20}{1000}$ | No. 10 | No. 26 | 0.827 |
| 10 | 50 | $\frac{18}{1000}$ | No. 9 | No. 27 | 0.735 |
| 11 | 55 | $\frac{18}{1000}$ | No. 8 | No. 28 | $0 \cdot 666$ |
| 12 | 60 | $\frac{15}{1000}$ | No. 8 | No. 28 | $0 \cdot 666$ |

Table of Appropriate Sizes and Proportions for PUMP Rods. (Curr.)

| Diameter <br> of <br> Pumps. | Spears. | Spear plates and bolts. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Scantling Square. | Length. | Breadth. | Thickness in the Middle | Thickness at the ends. | Diameter of Bolt. |
| Inches. 6 | Inches. 3 | Feet. $6$ | Inches. 2 $\frac{1}{2}$ | Inches. $\frac{3}{8}$ | Inches. $\frac{3}{16}$ | Inches. $\frac{5}{8}$ |
| 8 | $3 \frac{1}{2}$ | $6 \frac{1}{2}$ | $2 \frac{3}{4}$ | $\frac{7}{16}$ | $\frac{3}{18}$ | $\frac{11}{10}$ |
| 10 | 4 | 7 | 3 | $\frac{1}{2}$ | $\frac{1}{4}$ | $\frac{3}{4}$ |
| 12 | $4 \frac{1}{2}$ | $7 \frac{1}{2}$ | $3 \frac{1}{2}$ | $\frac{9}{16}$ | $\frac{5}{16}$ | $\frac{3}{4}$ |
| -14 | 5 | 8 | $3 \frac{1}{2}$ | $\frac{5}{8}$ | $\frac{3}{8}$ | $\frac{7}{8}$ |
| 16 | $5 \frac{1}{2}$ | $8 \frac{1}{2}$ | 4 | $\frac{3}{4}$ | 2 | $\frac{7}{8}$ |
| 18 | 6 | 9 | 4 | $\frac{13}{18}$ | $\frac{9}{16}$ | $\frac{15}{16}$ |
| $2)$ | $6 \frac{1}{2}$ | $9 \frac{1}{2}$ | $4 \frac{1}{2}$ | $\frac{7}{8}$ | $\frac{5}{8}$ | 1 |
| 22 | 7 | 10 | $4 \frac{1}{2}$ | $\frac{25}{18}$ | $\frac{12}{16}$ | $1 \frac{1}{8}$ |
| 24 | $7 \frac{1}{2}$ | $10 \frac{1}{2}$ | $4 \frac{3}{4}$ | 1 | $\frac{3}{4}$ | $1 \frac{1}{4}$ |

TABLE OF ACRES IN DIFFERENT WIDTHS．
Table of Acres Required per Mile and per Hundred Feet for different Widths．

| 品 | Acres per Mile． | $\begin{gathered} \text { Acres } \\ \text { per } \\ 100 \mathrm{Ft} . \end{gathered}$ | 花 | Acres per Mile． | Acres per 100 Ft ． | 运 | Acres per Mile． | $\begin{gathered} \text { Aeres } \\ \text { per } \\ 100 \mathrm{Ft} . \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Feet． |  |  | Feet． |  |  | Feet． |  |  |
| 1 | $0 \cdot 121$ | －002 | 35 | $4 \cdot 24$ | －080 | 68 | $8 \cdot 24$ | －156 |
| 2 | $0 \cdot 242$ | －005 | 36 | $4 \cdot 36$ | －083 | 69 | $8 \cdot 36$ | $\cdot 158$ |
| 3 | $0 \cdot 364$ | －007 | 37 | $4 \cdot 48$ | －085 | 70 | $8 \cdot 48$ | －161 |
| 4 | $0 \cdot 485$ | －06\％ | 38 | $4 \cdot 61$ | －087 | 71 | $8 \cdot 61$ | －163 |
| 5 | $0 \cdot 606$ | $\cdot 011$ | 39 | $4 \cdot 73$ | －020 | 72 | $8 \cdot 73$ | $\cdot 165$ |
| 6 | 0.727 | －014 | 40 | $4 \cdot 85$ | －092 | 73 | $8 \cdot 85$ | －168 |
| 7 | 0.848 | －016 | 41 | $4 \cdot 97$ | －094 | 74 | $8 \cdot 97$ | $\cdot 170$ |
| 8 | 0.970 | $\cdot 018$ | $41 \frac{1}{4}$ | $5 \cdot 0$ | －094 | 741 | $9 \cdot 0$ | $\cdot 170$ |
| $8 \frac{1}{4}$ | $1 \cdot 0$ | $\cdot 019$ | 42 | $5 \cdot 09$ | －096 | 75 | $9 \cdot 09$ | $\cdot 172$ |
| 9 | $1 \cdot 09$ | $\cdot 021$ | 43 | $5 \cdot 21$ | －099 | 76 | $9 \cdot 21$ | $\cdot 174$ |
| 10 | $1 \cdot 21$ | －023 | 44 | $5 \cdot 33$ | $\cdot 101$ | 77 | $9 \cdot 33$ | $\cdot 177$ |
| 11 | $1 \cdot 33$ | －025 | 45 | $5 \cdot 45$ | －103 | 78 | $9 \cdot 45$ | $\cdot 179$ |
| 12 | $1 \cdot 46$ | －028 | 46 | $5 \cdot 58$ | －106 | 79 | 9．58 | $\cdot 181$ |
| 13 | $1 \cdot 58$ | －030 | 47 | $5 \cdot 70$ | －108 | 80 | $9 \cdot 70$ | －184 |
| 14 | 1.70 | －032 | 48 | $5 \cdot 82$ | －110 | 81 | $9 \cdot 82$ | －186 |
| 15 | $1 \cdot 82$ | －034 | 49 | $5 \cdot 94$ | －112 | 82 | $9 \cdot 94$ | －188 |
| 16 | $1 \cdot 94$ | －037 | $49 \frac{1}{2}$ | 6.0 | －114 | $82 \frac{1}{2}$ | 10.0 | －189 |
| $16 \frac{1}{2}$ | $2 \cdot 0$ | －038 | $50^{2}$ | 6.06 | －115 | 83 | $10 \cdot 1$ | －190 |
| 17 | $2 \cdot 06$ | －039 | 51 | $6 \cdot 18$ | －117 | 84 | $10 \cdot 2$ | －193 |
| 18 | $2 \cdot 18$ | －041 | 52 | $6 \cdot 30$ | －119 | 85 | $10 \cdot 3$ | －195 |
| 19 | $2 \cdot 30$ | －044 | 53 | $6 \cdot 42$ | －122 | 86 | $10 \cdot 4$ | －197 |
| 20 | $2 \cdot 42$ | $\cdot 046$ | 54 | $6 \cdot 55$ | －124 | 87 | $10 \cdot 5$ | －200 |
| 21 | $2 \cdot 55$ | －048 | 55 | $6 \cdot 67$ | －126 | 88 | $10 \cdot 7$ | －202 |
| 22 | $2 \cdot 67$ | $\cdot 051$ | 56 | $6 \cdot 79$ | $\cdot 129$ | 89 | 10.8 | －204 |
| 23 | $2 \cdot 79$ | －053 | 57 | 6.91 | $\cdot 131$ | 90 | $10 \cdot 9$ | －207 |
| 24 | $2 \cdot 91$ | －055 | 578 | $7 \cdot 0$ | －133 | 903 | $11 \cdot 0$ | －209 |
| 243 | $3 \cdot 0$ | －057 | 58 | $7 \cdot 03$ | －133 | 91 | 11.0 | －09 |
| 25 | $3 \cdot 03$ | －057 | 59 | $7 \cdot 15$ | －135 | 92 | $11 \cdot 2$ | －211 |
| 26 | $3 \cdot 15$ | －060 | 60 | $7 \cdot 27$ | －138 | 93 | $11 \cdot 3$ | －213 |
| 27 | $3 \cdot 27$ | －062 | 61 | $7 \cdot 39$ | －140 | 94 | $11 \cdot 4$ | $\cdot 216$ |
| 28 | $3 \cdot 39$ | －064 | 62 | $7 \cdot 52$ | －142 | 95 | $11 \cdot 5$ | －218 |
| 29 | $3 \cdot 52$ | －067 | 63 | $7 \cdot 64$ | －145 | 96 | $11 \cdot 6$ | －220 |
| 30 | $3 \cdot 64$ | －069 | 64 | $7 \cdot 76$ | $\cdot 147$ | 97 | 11.8 | －223 |
| 31 | $3 \cdot 76$ | $\cdot 071$ | 65 | $7 \cdot 88$ | －149 | 98 | 11.9 | －225 |
| 32 | 3.88 | $\cdot 073$ | 66 | $8 \cdot 0$ | $\cdot 151$ | 99 | 12.0 | －227 |
| 33 | 4.0 | $\cdot 076$ | 67 | $8 \cdot 12$ | $\cdot 154$ | 100 | $12 \cdot 1$ | －230 |
| 34 | $4 \cdot 12$ | $\cdot 078$ |  |  |  |  |  |  |

Example．－To make a track 12 feet wide for $2 \frac{1}{2}$ miles，what area must be cleared？

In the second column，opposite 12 in the first，it will be found that 1 mile occupies an area of $1 \cdot 46$ acres；therefore 2 miles equals $1 \cdot 46 \times 2=2 \cdot 92$ ；and $\frac{1}{2}$ a mile equals $1 \cdot 46 \div 2=$ 0.73 so $2 \frac{1}{2}$ miles $=2.92+0.73=3.65$ acres，

Table showing Area of Cross-sections of Cuttings or Embankments 15 Feet in Width at FormationLevel, with Slopes of $1 \frac{1}{2}$ to 1.

| Depth in Feet. | $\begin{aligned} & \text { Area } \\ & \text { in Sq. } \\ & \text { Feet. } \end{aligned}$ | $\left\lvert\, \begin{aligned} & \text { Depth } \\ & \text { in } \\ & \text { Feet. } \end{aligned}\right.$ | $\begin{aligned} & \text { Area } \\ & \text { in Sq. } \\ & \text { Feet. } \end{aligned}$ | $\left\|\begin{array}{c} \text { Depth } \\ \text { in } \\ \text { Feet. } \end{array}\right\|$ | $\begin{aligned} & \text { Area } \\ & \text { in Sq. } \\ & \text { Feet. } \end{aligned}$ | $\left\lvert\, \begin{gathered} \text { Depth } \\ \text { in } \\ \text { Feet. } \end{gathered}\right.$ | $\begin{aligned} & \text { Area } \\ & \text { in Sq. } \\ & \text { Feet. } \end{aligned}$ | $\left\|\begin{array}{c} \text { Depth } \\ \text { in } \\ \text { Feet. } \end{array}\right\|$ | $\begin{aligned} & \text { Area } \\ & \text { in Sq. } \\ & \text { Feet. } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 05 | $\cdot 7$ | $2 \cdot 45$ | $45 \%$ | $4 \cdot 85$ | 108.0 | 5 | 187•5 | 9.65 | $284 \cdot 4$ |
| $\cdot 10$ | 1.5 | $2 \cdot 50$ | $46 \cdot 8$ | $4 \cdot 90$ | $109 \cdot 5$ | 7.30 | $189 \cdot 4$ | $9 \cdot 70$ | $286 \cdot 6$ |
| $\cdot 15$ | $2 \cdot 2$ | $2 \cdot 55$ | 48.0 | $4 \cdot 95$ | 111.0 | 7.35 | 191.2 | 9.75 | $288 \cdot 8$ |
| $\cdot 20$ | 3.0 | $2 \cdot 60$ | $49 \cdot 1$ | $5 \cdot 00$ | $112 \cdot 5$ | $7 \cdot 40$ | 193-1 | $9 \cdot 80$ | 291.0 |
| $\cdot 25$ | $3 \cdot 8$ | $2 \cdot 65$ | $50 \cdot 2$ | $5 \cdot 05$ | 114.0 | $7 \cdot 45$ | 195.0 | $9 \cdot 85$ | $293 \cdot 2$ |
| $\cdot 30$ | 4.6 | $2 \cdot 70$ | $51 \cdot 4$ | $5 \cdot 10$ | $115 \cdot 5$ | $7 \cdot 50$ | 196.8 | $9 \cdot 90$ | $295 \cdot 5$ |
| -35 | 5.4 | 2.75 | $52 \cdot 5$ | $5 \cdot 15$ | 117.0 | $7 \cdot 55$ | 198.7 | $9 \cdot 95$ | $297 \cdot 7$ |
| -40 | 6.2 | 2.80 | $53 \cdot 7$ | $5 \cdot 20$ | 118.5 | $7 \cdot 60$ | $200 \cdot 6$ | 10.00 | $300 \cdot 0$ |
| -45 | 7.0 | 2.85 | $54 \cdot 9$ | $5 \cdot 25$ | 120.0 | $7 \cdot 65$ | $202 \cdot 4$ | 10.05 | 302-2 |
| $\cdot 50$ | $7 \cdot 8$ | $2 \cdot 90$ | $56 \cdot 1$ | $5 \cdot 30$ | 121.6 | 7.70 | $204 \cdot 4$ | 10.10 | $304 \cdot 5$ |
| $\cdot 55$ | 8.7 | $2 \cdot 95$ | $57 \cdot 3$ | $5 \cdot 35$ | $123 \cdot 1$ | $7 \cdot 75$ | 206.3 | 10.15 | 3067 |
| -60 | $9 \cdot 5$ | 3.00 | 58.5 | $5 \cdot 40$ | 124.7 | $7 \cdot 80$ | 208.2 | 10-20 | 309.0 |
| -65 | $10 \cdot 3$ | 3.05 | 59.7 | $5 \cdot 45$ | $126 \cdot 3$ | $7 \cdot 85$ | $210 \cdot 1$ | 10.25 | $311 \cdot 3$ |
| $\cdot 70$ | 11.2 | $3 \cdot 10$ | $60 \cdot 9$ | $5 \cdot 50$ | $127 \cdot 8$ | 7.90 | 212 -1 | 10-30 | $313 \cdot 6$ |
| 75 | 12.0 | $3 \cdot 15$ | $62 \cdot 1$ | $5 \cdot 55$ | $129 \cdot 4$ | $7 \cdot 95$ | 214.0 | 10-35 | 315.9 |
| 80 | 12.9 | $3 \cdot 20$ | $63 \cdot 3$ | $5 \cdot 60$ | 131.0 | $8 \cdot 00$ | 216.0 | $10 \cdot 40$ | 318.2 |
| -85 | 13.8 | 3.25 | 64.5 | $5 \cdot 65$ | $132 \cdot 6$ | 8.05 | ${ }^{217} \cdot 9$ | $10 \cdot 45$ | $320 \cdot 5$ |
| .90 | $14 \cdot 7$ | 3.30 3.35 | 65.8 | 5.70 | 134.2 | 8.10 | ${ }^{219} 9$ | $10 \cdot 50$ | $322 \cdot 8$ |
| $1 \cdot 00$ | 16.5 | ${ }_{3 \cdot 40}^{3}$ | 68.3 | ${ }^{5} 8.80$ | $137 \cdot 4$ | 8.20 | $223 \cdot 8$ | $10 \cdot 55$ 10.60 | ${ }_{327}^{325} \cdot 5$ |
| 1.05 | $17 \cdot 4$ | $3 \cdot 45$ | $69 \cdot 6$ | $5 \cdot 85$ | 139.0 | $8 \cdot 25$ | $225 \cdot 8$ | $10 \cdot 65$ | $329 \cdot 8$ |
| $1 \cdot 10$ | $18 \cdot 3$ | $3 \cdot 50$ | 70.8 | $5 \cdot 90$ | $140 \cdot 7$ | 8.30 | $227 \cdot 8$ | 10'70 | $332 \cdot 2$ |
| 1-15 | 19.2 | $3 \cdot 55$ | $72 \cdot 1$ | $5 \cdot 95$ | 142.3 | 8.35 | $229 \cdot 8$ | 10*75 | $335 \cdot 6$ |
| $1 \cdot 20$ | $20 \cdot 1$ | $3 \cdot 60$ | $73 \cdot 4$ | 6.00 | 144.0 | $8 \cdot 40$ | 231.8 | 10:80 | $336 \cdot 9$ |
| 1.25 | 21.0 | $3 \cdot 65$ | $74 \cdot 7$ | 6.05 | 145.6 | 8.45 | $233 \cdot 8$ | $10 \cdot 85$ | $339 \cdot 3$ |
| 1.30 | 22.0 | 3.70 | 76.0 | $6 \cdot 10$ | 147.3 | $8 \cdot 50$ | 235.8 | $10 \cdot 90$ | $341 \cdot 7$ |
| 1.35 | $22 \cdot 9$ | $3 \cdot 75$ | $78 \cdot 3$ | 6.15 | $148 \cdot 9$ | $8 \cdot 55$ | $237 \cdot 9$ | 10-95 | $343 \cdot 1$ |
| 1.40 | $23 \cdot 9$ | 3.80 | $78 \cdot 6$ | 6.20 | $150 \cdot 0$ | $8 \cdot 60$ | $239 \cdot 9$ | 11.00 | $346 \cdot 5$ |
| 1.45 | 24.9 | $3 \cdot 85$ | 79.9 | 6.25 | $152 \cdot 3$ | $8 \cdot 65$ | 241.9 | 11.05 | $348 \cdot 9$ |
| 1.50 | $25 \cdot 8$ | $3 \cdot 90$ | $81 \cdot 3$ | 6.30 | 154.0 | 8.70 | 244.0 | $11 \cdot 10$ | $351 \cdot 3$ |
| 1.55 | ${ }^{26} \cdot 8$ | $3 \cdot 95$ | $82 \cdot 6$ | $6 \cdot 35$ | $156 \cdot 7$ | 8.75 | 246.0 | $11 \cdot 15$ | $353 \cdot 7$ |
| 1.60 | $27 \cdot 8$ | 4.00 | $84^{\circ} 0$ | $6 \cdot 40$ | $157 \cdot 4$ | $8 \cdot 80$ | $248 \cdot 1$ | $11 \cdot 20$ | $356 \cdot 1$ |
| $1 \cdot 65$ | 28.8 | 4.05 | $8{ }^{85 \cdot 3}$ | ${ }_{6}^{6.45}$ | ${ }^{159 \cdot 1}$ | 8.85 | ${ }_{20}^{250.2}$ | 11.25 | $358 \cdot 5$ |
| $1 \cdot 70$ | 29.8 30.9 | $4 \cdot 10$ | 86.7 | 6.50 | 160.8 | 8.90 | ${ }_{25}^{25 \cdot 3}$ | $11 \cdot 30$ | ${ }_{361.0}^{36}$ |
| 1.75 | $30 \cdot 9$ 31.8 | $4 \cdot 15$ | 88.0 80.4 | 6.55 6.60 | ${ }_{162 \cdot 6}^{162}$ | 8.95 | ${ }^{254} 4$ | 1135 | $363 \cdot 4$ |
| 1.80 | 31.8 32.8 | 4.20 4.25 | $80 \cdot 4$ $90 \cdot 8$ | $6 \cdot 60$ 6.65 | $164 \cdot 3$ 166.0 | 9.00 9.05 | ${ }_{25}^{256.5}$ | $11 \cdot 40$ | $365 \cdot 9$ 368.4 |
| 1.85 | 32.8 33.9 | $4 \cdot 25$ 4.30 | 90.8 ${ }_{92}{ }^{9}$ | $6 \cdot 65$ 6.70 | 166.0 | ${ }_{9}^{9.05}$ | ${ }_{260}^{258}$ | 11.45 | 368.4 |
| 1.90 1.95 | $33 \cdot 9$ $34 \cdot 9$ | $4 \cdot 30$ 4.35 | ${ }_{93} 92$ | 6.70 6.75 | ${ }_{169} 168$ | $9 \cdot 10$ $9 \cdot 15$ | $260 \cdot 7$ 262.8 | 11.50 | $370 \cdot 8$ |
| 1.95 2.00 | $34 \cdot 9$ 36.0 | $4 \cdot 35$ $4 \cdot 40$ | 93.6 95.0 | 6.75 6.80 | $169 \cdot 5$ $171 \cdot 3$ | $9 \cdot 15$ $9 \cdot 20$ | $262 \cdot 8$ 264 | ${ }_{11}^{11} \cdot 50$ | $373 \cdot 3$ $375 \cdot 8$ |
| $2 \cdot 05$ | $37 \cdot 0$ | $4 \cdot 45$ | $96 \cdot 4$ | $6 \cdot 85$ | $173 \cdot 1$ | $9 \cdot 25$ | $267 \cdot 0$ | $11 \cdot 65$ | 378.3 |
| $2 \cdot 10$ | $38 \cdot 1$ | 4.50 | $97 \cdot 8$ | $6 \cdot 90$ | $174 \cdot 9$ | 9.30 | 269.2 | $11 \cdot 70$ | $380 \cdot 8$ |
| $2 \cdot 15$ | $39 \cdot 1$ | 4.55 | $99 \cdot 3$ | $6 \cdot 95$ | $176 \cdot 7$ | $9 \cdot 35$ | 271.3 | $11 \cdot 75$ | 383.8 |
| $2 \cdot 20$ | $40 \cdot 2$ | $4 \cdot 60$ | $100 \cdot 7$ | 7.00 | 178.5 | $9 \cdot 40$ | 273.5 | $11 \cdot 80$ | 385.8 |
| $2 \cdot 25$ | 41.3 | $4 \cdot 65$ | 102.1 | 7.05 | $180 \cdot 3$ | $9 \cdot 45$ | ${ }^{275} \cdot$ | 11.85 | 388.3 |
| $2 \cdot 30$ | $42 \cdot 4$ | 4.70 | $103 \cdot 6$ | $7 \cdot 10$ | $182 \cdot 1$ | 9.50 | $277 \cdot 8$ | 11.90 | $390 \cdot 9$ |
| $2 \cdot 35$ | $43 \cdot 5$ | 4.75 4.80 | 105.0 | $7 \cdot 15$ | $183 \cdot 9$ | ${ }^{9.55}$ | $280.0$ | $11 \cdot 95$ | ${ }^{393} \cdot 4$ |
| $2 \cdot 40$ | $44 \cdot 6$ | $4 \cdot 80$ | $106 \cdot 5$ | $7 \cdot 2$ | $185 \%$ | $9 \cdot 60$ | $282 \cdot 2$ | 12.00 | 396.0 |

Table showing Area of enoss-sections of Cuttings or Embankments 12 Feet in Width at FormationLevel, with Slopes of $1 \frac{1}{2}$ to 1.

|  | $\begin{aligned} & \text { Area } \\ & \text { in Sq. } \\ & \text { Fect. } \end{aligned}$ | Depth in Feet. | Area in Sq. Feet. | $\left\lvert\, \begin{gathered} \text { Depth } \\ \text { in } \\ \text { Feet. } \end{gathered}\right.$ | $\begin{aligned} & \text { Area } \\ & \text { in Sq. } \\ & \text { Feet. } \end{aligned}$ | $\left\lvert\, \begin{aligned} & \text { Depth } \\ & \text { in } \\ & \text { Feet. } \end{aligned}\right.$ | $\begin{aligned} & \text { Area } \\ & \text { in Sq. } \\ & \text { Feet. } \end{aligned}$ | Depth in Feet. | $\begin{aligned} & \text { Area } \\ & \text { in Sq. } \\ & \text { Feet. } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -05 | -6 | $2 \cdot 45$ | 38.3 | $4 \cdot 85$ | $93 \cdot 4$ | $7 \cdot 25$ | $165 \cdot 8$ | $9 \cdot 65$ | $255 \cdot 4$ |
| -10 | $1 \cdot 2$ | $2 \cdot 50$ | $39 \cdot 3$ | $4 \cdot 90$ | $94 \cdot 8$ | $7 \cdot 30$ | $167 \cdot 5$ | 970 | $257 \cdot 5$ |
| $\cdot 15$ | $1 \cdot 8$ | $2 \cdot 55$ | $40 \cdot 3$ | $4 \cdot 95$ | $96 \cdot 1$ | $7 \cdot 35$ | $169 \cdot 2$ | $9 \cdot 75$ | $259 \cdot 5$ |
| ${ }^{2} 2$ | $2 \cdot 4$ | $2 \cdot 60$ | $41 \cdot 3$ | $5 \cdot 00$ | $97 \cdot 5$ | $7 \cdot 40$ | 1709 | $9 \cdot 80$ | 261.0 |
| $\cdot 25$ | $3 \cdot 0$ | $2 \cdot 65$ | $42 \cdot 3$ | 5.05 | 95.7 | $7 \cdot 45$ | 172.6 | 9.85 | $263 \cdot 7$ |
| -30 | $3 \cdot 7$ | $2 \cdot 70$ | $43 \cdot 3$ | $5 \cdot 10$ | $100 \cdot 2$ | $7 \cdot 50$ | $174 \cdot 3$ | $9 \cdot 90$ | 265.8 |
| -35 | $4 \cdot 3$ | $2 \cdot 75$ | $44 \cdot 3$ | $5 \cdot 15$ | $101 \cdot 5$ | $7 \cdot 55$ | $176 \cdot 1$ | 9.95 | $267 \cdot 9$ |
| -40 | $5 \cdot 0$ | $2 \cdot 80$ | $45 \cdot 3$ | $5 \cdot 20$ | $102 \cdot 9$ | $7 \cdot 60$ | $177 \cdot 8$ | $10 \cdot 00$ | $270 \cdot 0$ |
| -45 | $5 \cdot 7$ | $2 \cdot 85$ | $46 \cdot 3$ | $5 \cdot 25$ | $104 \cdot 3$ | $7 \cdot 65$ | 179.5 | 10.05 | $272 \cdot 1$ |
| $\cdot 50$ | $6 \cdot 3$ | $2 \cdot 90$ | $47 \cdot 4$ | $5 \cdot 30$ | $10{ }^{\circ} 7$ | $7 \cdot 70$ | 181.3 | $10 \cdot 10$ | $274 \cdot 2$ |
| -55 | $7 \cdot 0$ | $2 \cdot 95$ | $48 \cdot 4$ | $5 \cdot 35$ | $107 \cdot 1$ | $7 \cdot 75$ | 183.0 | $10 \cdot 15$ | $276 \cdot 3$ |
| -60 | $7 \cdot 7$ | 3.00 | $49 \cdot 5$ | $5 \cdot 40$ | $108 \cdot 5$ | $7 \cdot 80$ | 184.8 | $10 \cdot 20$ | 278.4 |
| -65 | $8 \cdot 4$ | 3.05 | $50 \cdot 5$ | $5 \cdot 45$ | $109 \cdot 9$ | $7 \cdot 85$ | 186.6 | 10.25 | $280 \cdot 5$ |
| $\cdot 70$ | $9 \cdot 1$ | $3 \cdot 10$ | $51 \cdot 6$ | $5 \cdot 50$ | $111 \cdot 3$ | $7 \cdot 90$ | 188.4 | $10 \cdot 30$ | $282 \cdot 7$ |
| .75 | $9 \cdot 8$ | $3 \cdot 15$ | $52 \cdot 6$ | $5 \cdot 55$ | $112 \cdot 7$ | $7 \cdot 95$ | $190 \cdot 2$ | $10 \cdot 35$ | 284.8 |
| -80 | $10 \cdot 5$ | $3 \cdot 20$ | $53 \cdot 7$ | $5 \cdot 60$ | 114*2 | 8.00 | 192.0 | $10 \cdot 40$ | $287 \cdot 0$ |
| -85 | $11 \cdot 2$ | $3 \cdot 25$ | $54 \cdot 8$ | $5 \cdot 65$ | $115 \cdot 6$ | 8.05 | 193.7 | $10 \cdot 45$ | $289 \cdot 2$ |
| $\cdot 90$ | $12 \cdot 0$ | $3 \cdot 30$ | $55 \cdot 9$ | $5 \cdot 70$ | $117 \cdot 1$ | $8 \cdot 10$ | $195 \cdot 6$ | 10.50 | $291 \cdot 3$ |
| $\cdot 95$ | $12 \cdot 7$ | $3 \cdot 35$ | $57 \cdot 0$ | 575 | 118.5 | 8.15 | $197 \cdot 4$ | $10 \cdot 55$ | $293 \cdot 5$ |
| $1 \cdot 00$ | $13 \cdot 5$ | $3 \cdot 40$ | $58 \cdot 1$ | $5 \cdot 80$ | $120 \cdot 0$ | 8.20 | 199.2 | $10 \cdot 60$ | $295 \cdot 7$ |
| $1 \cdot 05$ | $14 \cdot 2$ | $3 \cdot 45$ | $59 \cdot 2$ | $5 \cdot 85$ | $121 \cdot 5$ | $8 \cdot 25$ | $201 \cdot 0$ | $10 \cdot 65$ | $297 \cdot 9$ |
| $1 \cdot 10$ | $15 \cdot 0$ | $3 \cdot 50$ | $60 \cdot 3$ | $5 \cdot 90$ | 123.0 | $8 \cdot 30$ | $202 \cdot 9$ | 10.70 | $300 \cdot 1$ |
| $1 \cdot 15$ | $15 \cdot 7$ | $3 \cdot 55$ | $61 \cdot 4$ | $5 \cdot 95$ | 124.5 | $8 \cdot 35$ | $204 \cdot 7$ | 10.75 | $302 \cdot 3$ |
| $1 \cdot 20$ | $16 \cdot 6$ | $3 \cdot 60$ | $62 \cdot 6$ | 6.00 | 126.0 | $8 \cdot 40$ | $206 \cdot 6$ | $10 \cdot 80$ | $304 \cdot 5$ |
| $1 \cdot 25$ | $17 \cdot 3$ | $3 \cdot 65$ | $63 \cdot 7$ | 6.05 | $127 \cdot 4$ | 8.45 | 208.5 | 10.85 | 306.7 |
| $1 \cdot 30$ | 18.0 | $3 \cdot 70$ | $64 \cdot 9$ | $6 \cdot 10$ | $129 \cdot 0$ | $8 \cdot 50$ | $210 \cdot 3$ | 10.90 | 309.0 |
| $1 \cdot 35$ | $18 \cdot 9$ | $3 \cdot 75$ | $66^{\circ} 0$ | $6 \cdot 15$ | $130 \cdot 5$ | $8 \cdot 55$ | $212 \cdot 2$ | 10.95 | $311 \cdot 2$ |
| $1 \cdot 40$ | $19 \cdot 7$ | $3 \cdot 80$ | $67 \cdot 2$ | 6.20 | 132.0 | $8 \cdot 60$ | $214 \cdot 1$ | 11.00 | 313.5 |
| $1 \cdot 45$ | $20 \cdot 5$ | $3 \cdot 85$ | $68 \cdot 4$ | $6 \cdot 25$ | $133 \cdot 5$ | $8 \cdot 65$ | $216 \cdot 0$ | 11.05 | $315 \cdot 7$ |
| 1.50 | $21 \cdot 3$ | $3 \cdot 90$ | $69 \cdot 6$ | $6 \cdot 30$ | 135*1 | $8 \cdot 70$ | $217 \cdot 9$ | $11 \cdot 10$ | 318.0 |
| $1 \cdot 55$ | $22 \cdot 1$ | $3 \cdot 95$ | $70 \cdot 7$ | $6 \cdot 35$ | $136 \cdot 6$ | $8 \cdot 75$ | $219 \cdot 8$ | $11 \cdot 15$ | $320 \cdot 2$ |
| $1 \cdot 60$ | 23.0 | 4.00 | $72 \cdot 0$ | $6 \cdot 40$ | 138.2 | $8 \cdot 80$ | $221 \cdot 7$ | 11.20 | $322 \cdot 5$ |
| $1 \cdot 65$ | $23 \cdot 8$ | $4 \cdot 05$ | $73 \cdot 1$ | 6.45 | $139 \cdot 8$ | $8 \cdot 85$ | $223 \cdot 6$ | $11 \cdot 25$ | $324 \cdot 8$ |
| 1.50 | $24 \cdot 7$ | $4 \cdot 10$ | $74 \cdot 4$ | 6.50 | $141 \cdot 3$ | $8 \cdot 90$ | 226.6 | $11 \cdot 30$ | $327 \cdot 1$ |
| 1.75 | $25 \cdot 5$ | $4 \cdot 15$ | $75 \cdot 6$ | $6 \cdot 55$ | $142 \cdot 9$ | $8 \cdot 95$ | $227 \cdot 5$ | 11.35 | $329 \cdot 4$ |
| 1.80 | $26 \cdot 4$ | $4 \cdot 20$ | $76 \cdot 8$ | $6 \cdot 60$ | $144 \cdot 5$ | 9.00 | $229 \cdot 5$ | $11 \cdot 40$ | 331.7 |
| $1 \cdot 85$ | $27 \cdot 3$ | $4 \cdot 25$ | 78.0 | $6 \cdot 65$ | $146 \cdot 1$ | 9.05 | $231 \cdot 4$ | $11 \cdot 45$ | 334.0 |
| 1.90 | $25 \cdot 2$ | $4 \cdot 30$ | 79.3 | 6.70 | $147 \cdot 7$ | $9 \cdot 10$ | $233 \cdot 4$ | $11 \cdot 50$ | $336 \cdot 3$ |
| $1 \cdot 95$ | $29 \cdot 0$ | $4 \cdot 35$ | $80 \cdot 5$ | 6.75 | $149 \cdot 3$ | $9 \cdot 15$ | $235 \cdot 3$ | 11.55 | $335 \cdot 7$ |
| 2.00 | $30 \cdot 0$ | $4 \cdot 40$ | $81 \cdot 8$ | 6.80 | $150 \cdot 9$ | $9 \cdot 20$ | $237 \cdot 3$ | $11 \cdot 60$ | 341.0 |
| $2 \cdot 05$ | $30 \cdot 9$ | $4 \cdot 45$ | $82 \cdot 9$ | 6.85 | $152 \cdot 5$ | $9 \cdot 25$ | $239 \cdot 3$ | $11 \cdot 65$ | $343 \cdot 3$ |
| $2 \cdot 10$ | $31 \cdot 8$ | $4 \cdot 50$ $4 \cdot 55$ | $84 \cdot 3$ | 6.90 6.95 | $154 \cdot 2$ | 9.30 0.35 | $241 \cdot 3$ | 11.70 | $345 \cdot 7$ |
| $2 \cdot 15$ | $32 \cdot 7$ | $4 \cdot 55$ | $85 \cdot 6$ | $6 \cdot 95$ | $155 \cdot 8$ | $9 \cdot 35$ | $243 \cdot 3$ | $11 \cdot 75$ | 348.0 |
| $2 \cdot 20$ | $33 \cdot 6$ | $4 \cdot 60$ | 86.9 | 7.00 | $157 \cdot 5$ | $9 \cdot 40$ | $245 \cdot 3$ | 11.80 | $350 \cdot 4$ |
| $2 \cdot 25$ | $34 \cdot 5$ | $4 \cdot 65$ | $88 \cdot 2$ | $7 \cdot 05$ | $159 \cdot 1$ | $9 \cdot 45$ | $247 \cdot 3$ | 11.85 | $352 \cdot 8$ |
| $2 \cdot 30$ | $35 \cdot 5$ | $4 \cdot 70$ | $89 \cdot 5$ | $7 \cdot 10$ | $160 \cdot 8$ | $9 \cdot 50$ | $249 \cdot 3$ | 11.90 | $355 \cdot 2$ |
| $2 \cdot 35$ | $36 \cdot 4$ | $4 \cdot 75$ | $90 \cdot 8$ | $7 \cdot 15$ | $162 \cdot 4$ | $9 \cdot 55$ | $251 \cdot 4$ | 11.95 | $357 \cdot 6$ |
| $2 \cdot 40$ | $37 \cdot 4$ | $4 \cdot 80$ | $92 \cdot 1$ | $7 \cdot 20$ | $164 \cdot 1$ | $9 \cdot 60$ | $253 \cdot 4$ | 12.00 | 360.0 |

Specific Gravity Degreezs, comparing the Areo. meters of Baumé, Cartier, and Beck.
(For Liquids heavier than Water.)

| Degrees. Baumé and Beck. | Baumé. | Beck. | Degrees. <br> Baumé <br> and Beck. | Baumé. | Beck. |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Sp. Grv. | Sp. Grv |  | Sp. Grv. | Sp. Grv. |
| 0 | 1.000 | $1 \cdot 0000$ | 37 | 1.337 | 1.2782 |
| 1 | 1.007 | 1.00 .59 1.0119 | ${ }_{39}^{38}$ | 1.349 1.361 | 1.2879 |
| 3 | 1.020 | 1.0180 | 40 | 1.375 | 1:3077 |
| 4 | 1.028 | 1.0241 | 41 | $1 \cdot 388$ | 1-3178 |
| 5 | 1.035 | 1.0303 | 42 | $1 \cdot 401$ | 1-3281 |
| 6 | 1.041 | 1.0366 | 43 | $1 \cdot 414$ | 1-3386 |
| 7 | 1.049 | 1.0429 | 45 | 1.428 | $1 \cdot 3492$ |
| 8 | 1.057 | 1.0494 | 45 | 1-442 | $1 \cdot 3600$ |
| 9 | 1.064 | 1.0559 | 46 | $1 \cdot 456$ | 1-3710 |
| 10 | 1.072 | 1.0625 | 47 | $1 \cdot 470$ | $1 \cdot 3821$ |
| 11 | 1.080 | 1.0692 | 48 | $1 \cdot 485$ | $1 \cdot 3934$ |
| 12 | 1.088 | 1.0759 | 49 | $1 \cdot 500$ | $1 \cdot 4050$ |
| 13 | 1.096 | 1.0828 | 50 | $1 \cdot 515$ | $1 \cdot 4167$ |
| 14 | $1 \cdot 104$ | 1.0897 | 51 | $1 \cdot 531$ | $1 \cdot 4286$ |
| 15 | $1 \cdot 113$ | 1.0968 | 52 | 1.546 | $1 \cdot 4407$ |
| 16 | $1 \cdot 121$ | $1 \cdot 1039$ | 53 | 1.562 | $1 \cdot 4530$ |
| 17 | $1 \cdot 130$ | 1.1111 | 54 | 1.578 | $1 \cdot 4655$ |
| 18 | $1 \cdot 138$ | $1 \cdot 1184$ | 55 | 1.593 | $1 \cdot 4783$ |
| 19 | $1 \cdot 147$ | 1-1258 | 56 | 1615 | $1 \cdot 4912$ |
| 20 21 | $1 \cdot 157$ | $1 \cdot 1333$ | 57 | $1 \cdot 634$ | $1 \cdot 5044$ |
| 21 | $1 \cdot 160$ | 1.1409 | 58 | $1 \cdot 653$ | 1.5179 |
| 22 | $1 \cdot 176$ | $1 \cdot 1486$ | 59 | $1 \cdot 671$ | 1.5315 |
| 23 | $1 \cdot 185$ | $1 \cdot 1565$ | 60 | $1 \cdot 690$ | 1.5454 |
| $\stackrel{24}{25}$ | $1 \cdot 193$ | $1 \cdot 1644$ | 61 | $1 \cdot 709$ | 1.5596 |
| $\stackrel{25}{26}$ | 1.215 | 1.1724 | 62 | $1 \cdot 729$ | 1.5741 |
| 26 27 | ${ }_{1}^{1 \cdot 215}$ | 1.1506 1.1888 | 63 64 | $1 \cdot 750$ | 1.5888 |
| 28 | 1.235 | ${ }_{1}^{1 \cdot 1888}$ | 64 65 | 1.771 1.793 | 1.6038 1.6190 |
| 29 | $1 \cdot 245$ | $1 \cdot 2057$ | 66 | 1.815 | ${ }_{1} \cdot 6346$ |
| 30 | 1.256 | $1 \cdot 2143$ | 67 | 1-839 | $1 \cdot 6505$ |
| 31 | $1 \cdot 267$ | 1.2230 | 68 | 1.864 | $1 \cdot 6667$ |
| 32 <br> 3 | 1.278 | $1 \cdot 3319$ | 69 | $1 \cdot 885$ | $1 \cdot 6832$ |
| 33 34 | 1.289 1.300 | 1.2409 1.2509 | 70 71 | 1.909 1.935 | 1.7000 |
| ${ }_{36}^{35}$ | 1.312 | 1.2593 | 72 | 1.960 |  |
| 36 | 1.324 | 1.2680 |  |  |  |

Formulæ for different Areometers: $g=$ number of degrees, $s=\mathrm{sp}$. grv :--

$$
\begin{aligned}
& \text { Baumé } s=\frac{144}{144-g} . \\
& \text { Cartier } s=\frac{136 \cdot 8}{126 \cdot 1-g} \\
& \text { Beck } s=\frac{170}{170-g}
\end{aligned}
$$

Specific Gravity Degrees. comparing the Areometers of Baumé, Cartier, and Beck.
(For Liquids lighter than Water.)

| Degrees, Baumé | Baumé. | Cartier. | Beck. | Degrees, Baumé, | Baumé. | Cartier. | Beck. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cartier <br> \& Beck. | Sp. Grv. | Sp. Grv. | Sp. Grv. | Cartier <br> \& Beck. | Sp. Grv. | Sp. Grv. | Sp. Grv. |
| 0 | $\cdots$ | ... | 1.0000 0.9941 | 36 37 | 0.848 0.843 | 0.837 0.831 | 0.8252 0.8212 |
| 2 | $\ldots$ |  | $0 \cdot 9883$ | 38 | $0 \cdot 838$ | $0 \cdot 826$ | $0 \cdot 8173$ |
| 3 | ... |  | 0.9826 | 39 | 0.833 | 0.820 | 0.8133 |
| 4 | $\ldots$ |  | 0.9770 | 40 | $0 \cdot 829$ | 0.815 | $0 \cdot 8095$ |
| 5 |  | ... | 0.9714 | 41 | $0 \cdot 824$ | 0.810 | $0 \cdot 8061$ |
| 6 |  |  | 0.9659 | 42 | 0.819 | 0.805 | $0 \cdot 8018$ |
| 7 |  | $\ldots$ | 0.9604 | 43 | 0.815 | 0.800 | $0 \cdot 7981$ |
| 8 |  | $\ldots$ | $0 \cdot 9550$ | 44 | 0.810 | ... | $0 \cdot 7944$ |
| 9 |  |  | 0.9497 | 45 | 0.806 |  | 0.7907 |
| 10 | 1.000 0.993 |  | 0.9444 0.9392 | 46 47 | 0.801 0.797 |  | 0.7871 |
| 112 | 0.993 0.986 | 1.000 0.992 | 0.9392 0.9340 | 47 48 | 0.797 0.792 | $\ldots$ | 0.7834 0.7799 |
| 13 | $0 \cdot 979$ | $0 \cdot 985$ | $0 \cdot 9289$ | 49 | $0 \cdot 788$ | $\ldots$ | 0.799 0.763 |
| 14 | 0.973 | 0.977 | 0.9239 | 50 | 0.784 | ... | $0 \cdot 7727$ |
| 15 | 0.967 | 0.969 | $0 \cdot 9189$ | 51 | 0.781 |  | $0 \cdot 7692$ |
| 16 | 0.960 | 0.962 | 0.9139 | 52 | 0.776 | $\ldots$ | $0 \cdot 7658$ |
| 17 | 0.954 | -0.955 | 0.9090 | 53 | $0 \cdot 771$ |  | $0 \cdot 7623$ |
| 18 | 0.948 | $0 \cdot 948$ | 0.9042 | 54 | 0.769 | ... | 0.7589 |
| 19 | 0.942 | 0.941 | $0 \cdot 8994$ | 55 | 0.763 |  | 0.7556 |
| 20 | 0.935 | 0.934 | $0 \cdot 8947$ | 56 | 0.759 | ... | $0 \cdot 7522$ |
| ${ }_{22}^{21}$ | 0.929 | $0 \cdot 927$ | $0 \cdot 8900$ | 57 | 0.755 |  | 0.7489 |
| 22 | $0 \cdot 924$ | $0 \cdot 920$ | $0 \cdot 8854$ | 58 | $0 \cdot 751$ | ... | 0.7456 |
| 23 24 | 0.918 | 0.914 | 0.8808 | 59 | 0.748 |  | $0 \cdot 7423$ |
| $\stackrel{24}{25}$ | 0.912 | 0.908 | $0 \cdot 8762$ | 60 | 0.744 | ... | 0.7391 |
| 25 26 | $0 \cdot 906$ | $0 \cdot 901$ | 0.8717 | 61 | $0 \cdot 740$ |  | $0 \cdot 7359$ |
| 26 27 | 0.901 | 0.895 | 0.8673 | 62 | 0.736 | $\ldots$ | 0.7328 |
| 27 23 | 0.895 0.889 | 0.889 0.883 | $0 \cdot 8629$ | ${ }_{64}^{63}$ | ... | ... | 0.7296 |
| 23 29 | 0.889 0.884 | 0.883 0.877 | 0.8585 0.8542 | 64 65 | $\ldots$ | $\ldots$ | 0.7265 0.7234 |
| 30 | 0.879 | 0.871 | $0 \cdot 8500$ | 66 | $\ldots$ | $\ldots$ | $0 \cdot 7203$ |
| 31 | 0.873 0.868 | 0.865 0.859 | 0.8457 | 67 | $\ldots$ | $\ldots$ | 0.7173 |
| 32 33 | 0.868 | 0.859 | $0 \cdot 8415$ | 68 | $\ldots$ | $\ldots$ | 0.7142 |
| 33 34 | 0.863 0.858 | -0.853 | 0.8374 0.833 | 69 70 | $\ldots$ | $\cdots$ | 0.7112 0.7083 |
| 35 | ${ }_{0} \cdot 853$ | ${ }_{0} \cdot 842$ | 0.8292 | 7 | ... | ... | $0 \cdot 7083$ |

Formulæ for different Areometers : $g=$ number of degrees, $s=\mathrm{sp}$. grv. : -

$$
\text { Brix } s=\frac{400}{400+g}
$$

Gay Lussac $s=\frac{100}{100+g}$
Balling $s=\frac{200}{200+g}$.

Transformation of Columns of Water into Columns of Mercury.

| $\begin{aligned} & \text { Millim. } \\ & \text { of } \\ & \text { Water. } \end{aligned}$ | $\left.\begin{gathered} \text { Millim. } \\ \text { of } \\ \text { Mercury. } \end{gathered} \right\rvert\,$ | $\begin{array}{\|l\|l} \text { Millim. } \\ \text { of } \\ \text { Water. } \end{array}$ |  |  | $\begin{gathered} \text { Millim. } \\ \text { of } \\ \text { Mereury. } \end{gathered}$ |  | $\left.\begin{array}{\|c\|} \text { Millim. } \\ \text { of } \\ \text { Mercury. } \end{array} \right\rvert\,$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $\cdot 074$ | 8 | -59 | 35 | $2 \cdot 58$ | 65 | $4 \cdot 80$ |
| 2 | $\cdot 15$ | 9 | -66 | 40 | $2 \cdot 95$ | 70 | $5 \cdot 17$ |
| 3 | $\cdot 22$ | 10 | 74 | 45 | $3 \cdot 32$ | 75 | 5.54 |
| 4 | -30 | 15 | $1 \cdot 12$ | 50 | $3 \cdot 69$ | 80 | $5 \cdot 90$ |
| 5 | $\cdot 37$ | 20 | $1 \cdot 48$ | 55 | $4 \cdot 06$ | 85 | $6 \cdot 27$ |
| 6 | $\cdot 44$ | 25 | $1 \cdot 84$ | 60 | $4 \cdot 43$ | 90 | $6 \cdot 64$ |
| 7 | -52 | 30 | $2 \cdot 21$ |  |  |  |  |

Table of Approximate Size and Weight of Rails for Loaded Waggons of certain Weights, the Sleepers being 2 Feet 2 Inches apart.

| Weight of Loaded <br> Truck. | Height of Rail. | Width of Rail. | Weight per <br> Running Yard. |
| :---: | :---: | :---: | :---: |
|  | Cwt. | In. | In. |
| 6 | $1 \frac{1}{2}$ | $\frac{3}{8}$ | Lbs. |
| 10 | 2 | $\frac{3}{8}$ | $6 \cdot 26$ |
| 14 | $2 \frac{1}{8}$ | $\frac{1}{2}$ | $7 \cdot 83$ |
| 18 | $2 \frac{1}{6}$ | $\frac{3}{5}$ | $14 \cdot 22$ |
| 24 | $2 \frac{3}{4}$ | $\frac{3}{5}$ | $15 \cdot 76$ |
| 30 | $2 \frac{3}{7}$ | $\frac{11}{16}$ | 20.68 |

Weight and depth gives solidity; track and breadth of rail is necessary for the preservation of the wheels of the trucks.

## Railway Curves. (Pambour.)

The outer rail of curves requires to be raised above the inner as follows, for a speed of 20 miles per hour :


## HEAT.

Thermometers. Comparison of Celsius, Réaumur, and Fahrenheit Scales.

| Celsius. | Réaumur. | Fahrenheit. | Celsius. | Réaumur. | Fahrenheit. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $+100$ | +80 | $+212$ | $+63$ | $+50 \cdot 4$ | $+145 \cdot 4$ |
| 99 | $79 \cdot 2$ | $210 \cdot 2$ | 62 | $49 \cdot 6$ | $143 \cdot 6$ |
| 98 | 78.4 | $208 \cdot 4$ | 61 | $48 \cdot 8$ | $141 \cdot 8$ |
| 97 | $77 \cdot 6$ | $206 \cdot 6$ | 60 | 48 | 140 |
| 96 | $76 \cdot 8$ | $204 \cdot 8$ | 59 | $47 \cdot 2$ | $138 \cdot 2$ |
| 95 | 76 | 203 | 58 | $46 \cdot 4$ | 136.4 |
| 94 | $75 \cdot 2$ | $201 \cdot 2$ | 57 | $45 \cdot 6$ | $134 \cdot 6$ |
| 93 | $74 \cdot 4$ | $199 \cdot 4$ | 56 | $44 \cdot 8$ | $132 \cdot 8$ |
| 92 | $73 \cdot 6$ | $197 \cdot 6$ | 55 | 44 | 131 |
| 91 | $72 \cdot 8$ | 195.8 | 54 | $43 \cdot 2$ | 129.2 |
| 90 | 72 | 194 | 53 | $42 \cdot 4$ | $127 \cdot 4$ |
| 89 | $71 \cdot 2$ | $192 \cdot 2$ | 52 | $41 \cdot 6$ | $125 \cdot 6$ |
| 88 | $70 \cdot 4$ | $190 \cdot 4$ | 51 | $40 \cdot 8$ | 123.8 |
| 87 | 69.6 | $188 \cdot 6$ | 50 | 40 | 122 |
| 86 | $68 \cdot 8$ | 186.8 | 49 | $39 \cdot 2$ | $120 \cdot 2$ |
| 85 | 68 | 185 | 48 | $38 \cdot 4$ | 118.4 |
| 84 | $67 \cdot 2$ | 183.2 | 47 | $37 \cdot 6$ | 116.6 |
| 83 | $66 \cdot 4$ | $181 \cdot 4$ | 46 | $36 \cdot 8$ | $114 \cdot 8$ |
| 82 | 65.6 | $179 \cdot 6$ | 45 | 36 | 113 |
| 81 | $64 \cdot 8$ | $177 \cdot 8$ | 44 | $35 \cdot 2$ | 111.2 |
| 80 | 64 | 176 | 43 | $34 \cdot 4$ | $109 \cdot 4$ |
| 79 | $63 \cdot 2$ | $174 \cdot 2$ | 42 | $33 \cdot 6$ | $107 \cdot 6$ |
| 78 | $62 \cdot 4$ | 172.4 | 41 | $32 \cdot 8$ | $105 \cdot 8$ |
| 77 | $61 \cdot 6$ | $170 \cdot 6$ | 40 | 32 | 104 |
| 76 | $60 \cdot 8$ | 168.8 | 39 | $31 \cdot 2$ | $102 \cdot 2$ |
| 75 | 60 | 167 | 38 | $30 \cdot 4$ | $100 \cdot 4$ |
| 74 | $59 \cdot 2$ | 165.2 | 37 | $29 \cdot 6$ | $98 \cdot 6$ |
| 73 | $58 \cdot 4$ | $163 \cdot 4$ | 36 | $28 \cdot 8$ | $96 \cdot 8$ |
| 72 | $57 \cdot 6$ | $161 \cdot 6$ | 35 | 28 | 95 |
| 71 | $56 \cdot 8$ | $159 \cdot 8$ | 34 | $27 \cdot 2$ | $93 \cdot 2$ |
| 70 | 56 | 158 | 33 | $26 \cdot 4$ | $91 \cdot 4$ |
| 69 | $55 \cdot 2$ | 156.2 | 32 | $25 \cdot 6$ | $89 \cdot 6$ |
| 68 | $54 \cdot 4$ | $154 \cdot 4$ | 31 | $24 \cdot 8$ | $87 \cdot 8$ |
| 67 | $53 \cdot 6$ | 152.6 | 30 | 24 | 83 |
| 66 | $52 \cdot 8$ | $150 \cdot 8$ | 29 | $23 \cdot 2$ | $84 \cdot 2$ |
| 65 | 52 | 149 | 28 | $22 \cdot 4$ | $82 \cdot 4$ |
| 64 | $51 \cdot 2$ | $147 \cdot 2$ | 27 | $21 \cdot 6$ | $80 \cdot 6$ |

Thermometers, Comparison of-(continucd).

| Celsius. | Réaumur. | Fahrenheit. | Celsius. | Réaumur. | Fahrenheit. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $+26$ | $+20 \cdot 8$ | +78.8 | -8 | $-6.4$ | $+17 \cdot 6$ |
| 25 | 20 | 77 | 9 | $7 \cdot 2$ | -15.8 |
| 24 | $19 \cdot 2$ | $75 \cdot 2$ | 10 | 8 | 14 |
| 23 | $18 \cdot 4$ | $73 \cdot 4$ | 11 | $8 \cdot 8$ | $12 \cdot 2$ |
| 22 | $17 \cdot 6$ | $71 \cdot 6$ | 12 | $9 \cdot 6$ | $10 \cdot 4$ |
| 21 | $16 \cdot 8$ | $69 \cdot 8$ | 13 | $10 \cdot 4$ | $8 \cdot 6$ |
| 20 | 16 | 68 | 14 | $11 \cdot 2$ | $6 \cdot 8$ |
| 19 | $15 \cdot 2$ | $66 \cdot 2$ | 15 | 12 | 5 |
| 18 | $14 \cdot 4$ | $64 \cdot 4$ | 16 | $12 \cdot 8$ | $3 \cdot 2$ |
| 17 | $13 \cdot 6$ | $62 \cdot 6$ | 17 | $13 \cdot 6$ | $1 \cdot 4$ |
| 16 | $12 \cdot 8$ | $60 \cdot 8$ | 18 | $14 \cdot 4$ | $-0.4$ |
| 15 | 12 | 59 | 19 | $15 \cdot 2$ | $2 \cdot 2$ |
| 14 | 11.2 | $57 \cdot 2$ | 20 | 16 | 4 |
| 13 | $10 \cdot 4$ | $55 \cdot 4$ | 21 | 16.8 | $5 \cdot 8$ |
| 12 | $9 \cdot 6$ | 53.6 | 22 | $17 \cdot 6$ | $7 \cdot 6$ |
| 11 | $8 \cdot 8$ | $51 \cdot 8$ | 23 | $18 \cdot 4$ | $9 \cdot 4$ |
| 10 | 8 | 50 | 24 | $19 \cdot 2$ | $11 \cdot 2$ |
| 9 | $7 \cdot 2$ | $48 \cdot 2$ | 25 | 20 | 13 |
| 8 | $6 \cdot 4$ | $46 \cdot 4$ | 26 | $20 \cdot 8$ | $14 \cdot 8$ |
| 7 | $5 \cdot 6$ | $44 \cdot 6$ | 27 | $21 \cdot 6$ | $16 \cdot 6$ |
| 6 | $4 \cdot 8$ | $42 \cdot 8$ | 28 | $22 \cdot 4$ | $18 \cdot 4$ |
| 5 | 4 | 42 | 29 | $23 \cdot 2$ | $20 \cdot 2$ |
| 4 | $3 \cdot 2$ | $39 \cdot 2$ | 30 | 24 | 22 |
| 3 | $2 \cdot 4$ | $37 \cdot 4$ | 31 | $24 \cdot 8$ | $23 \cdot 8$ |
| 2 | 1.6 | $35 \cdot 6$ | 32 | $25 \cdot 6$ | $25 \cdot 6$ |
| 1 | $0 \cdot 8$ | $33 \cdot 8$ | 33 | $26 \cdot 4$ | $27 \cdot 4$ |
| 0 | 0 | 32 | 34 | $27 \cdot 2$ | $29 \cdot 2$ |
| -1 | $-0.8$ | $30 \cdot 2$ | 35 | 28 | 31 |
| 2 | $1 \cdot 6$ | $28 \cdot 4$ | 36 | $28 \cdot 8$ | $32 \cdot 8$ |
| 3 | 2.4 | $26 \cdot 6$ | 37 | $29 \cdot 6$ | $34 \cdot 6$ |
| 4 | $3 \cdot 2$ | $24 \cdot 8$ | 38 | $30 \cdot 4$ | 36.4 |
| 5 | 4 | 23 | 39 | $31 \cdot 2$ | $38 \cdot 2$ |
| 6 | $4 \cdot 8$ | $21 \cdot 2$ | 40 | 32 | 40 |
| 7 | $5 \cdot 6$ | $19 \cdot 4$ |  |  |  |

$$
\begin{aligned}
& \mathrm{F}^{\circ}: \mathrm{C}^{\circ}=\left(\mathrm{F}^{\circ}-32\right) \times 5 \div 9 . \\
& \mathrm{F}^{\circ}: \mathrm{R}^{\circ}=\left(\mathrm{F}^{\circ}-32\right) \times 4 \div 9 . \\
& \mathrm{C}^{\circ}: \mathrm{F}^{\circ}=\left(\mathbf{C}^{\circ} \times 9 \div 5\right)+32 . \\
& \mathrm{C}^{\circ}: \mathrm{R}^{\circ}=\mathrm{C}^{\circ} \times 4 \div 5 . \\
& \mathrm{R}^{\circ}: \mathrm{F}^{\circ}=\left(\mathrm{R}^{\circ} \times 9 \div 4\right)+32 . \\
& \mathrm{R}^{\circ}: \mathrm{C}^{\circ}=\mathrm{R}^{\circ} \times 5 \div 4 .
\end{aligned}
$$

## Specific Heat.

The specific heat of a body is the ratio of the quantity of heat required to raise that body one degree, to the quantity required to raise an equal weight of water one degree in temperature. It is ascertained by multiplying the absolute heating power by the specific gravity.

Taele of Specific Heat of Gases and Vapours.

|  | For Equal Volumes. | For Equal Weights. |
| :---: | :---: | :---: |
| Air | $\left\{\begin{array}{l}0 \cdot 2374 \\ 0 \cdot 2389\end{array}\right\}$ | $0 \cdot 2374$ |
| Oxygen . | $0 \cdot 2405$ | 0.2175 |
| Nitrogen | $0 \cdot 2368$ | $0 \cdot 2438$ |
| Hydrogen | $0 \cdot 2359$ | $3 \cdot 4090$ |
| Chlorine | $0 \cdot 2964$ | $0 \cdot 1210$ |
| Nitrous oxide | $\left\{\begin{array}{l}0.3447 \\ 0.3014\end{array}\right\}$ | $0 \cdot 2262$ |
| Nitric oxide | 0.2406 | $0 \cdot 2317$ |
| Carbonic oxide | $\left\{\begin{array}{l}0 \cdot 2370 \\ 0 \cdot 2346\end{array}\right\}$ | $0 \cdot 2450$ |
| Carbonic anhydride | $\{0.3307$ 0.2085 | $0 \cdot 20246$ |
| Carbonic disulphide | $\left\{\begin{array}{c}0.2985 \\ 0.4122\end{array}\right.$ | 0.1569 |
| Ammonia . . | $\left\{\begin{array}{l}0.2996 \\ 0.2952\end{array}\right\}$ | $0 \cdot 5083$ |
| Marsh gas | $0 \cdot 3277$ | 0.5929 |
| Sulphurous anhydride | $0 \cdot 3414$ | $0 \cdot 1553$ |
| Hydrochloric acid | $0 \cdot 2333$ | $0 \cdot 1852$ |
| Sulphuretted hydrogen | 0.2857 | 0.2432 |
| Water . . . | $0 \cdot 2989$ | $0 \cdot 4805$ |

Table of Approximate Temperatures indicated by Colour of Fire.

| , | 525 | Dark orange | . $1,100^{\circ} \mathrm{C}$. |
| :---: | :---: | :---: | :---: |
| Dark red | $700^{\circ}$ | Light orange | $1,200^{\circ}$ |
| Dark cherry red | $800^{\circ}$ | White heat | $1,300^{\circ}$ |
| Cherry red. | $900^{\circ}$ | Welding heat | 1,400 |
| Light cherry red | $1,000^{\circ}$ " | Dazzling white | 1,500 ${ }^{\circ}$, |

Table of Theoretical Heating Power developed by the burning of 1 Kilogram of

| C | to CO | 23 |  |
| :---: | :---: | :---: | :---: |
| C | ", $\mathrm{CO}_{2}$ | 8080 | ", |
| CO | , $\mathrm{CO}_{2}$ | 2442 | ", |
| H | , $\mathrm{H}_{2} \mathrm{O}$ liquid | $=34180$ | ", |
| H | " $\mathrm{H}_{2} \mathrm{O}$ gas | 28780 |  |
| $\mathrm{CH}_{4}$ | , $\mathrm{CO}_{2}+2 \mathrm{H}_{2} \mathrm{O}$ liquid | $=13346$ |  |
| $\mathrm{CH}_{4}$ | , $\mathrm{CO}_{2}+2 \mathrm{H}_{2} \mathrm{O}$ gas | 11996 | " |
| $\mathrm{C}_{2} \mathrm{H}_{4}$ | , $2 \mathrm{CO}_{2}+2 \mathrm{H}_{2} \mathrm{Ol}$ liquid | $=11957$ | ", |
| $\mathrm{C}_{2} \mathrm{H}_{4}$ | , $2 \mathrm{CO}_{2}^{2}+2 \mathrm{H}_{2}^{2} \mathrm{O}$ gas | 11186 | ", |
| Fe | , FeO . | 1353 | ", |
| Fe | ", $\mathrm{Fe}_{3} \mathrm{O}_{4}$ | 1582 | ., |
| Fe | " $\mathrm{Fe}_{2} \mathrm{O}_{3}$ | 2028 |  |
| Si | ", $\mathrm{SiO}_{2}$ | 7830 |  |
| Mn | , MnO | 1724 |  |
| Mn | ", $\mathrm{MnO}_{2}$ | 2113 |  |
| Pb | " $\mathrm{PbO}{ }^{2}$ | 266 |  |
| Cu | " CuO | 684 |  |
| $\mathrm{Cu}_{2} \mathrm{O}$ | ,, CuO | 256 |  |
| Zn | , ZnO | 1291 |  |
| Sn | , $\mathrm{SnO}_{2}$ | 1147 |  |
| P | " $\mathrm{P}_{2} \mathrm{O}_{5}^{2}$ | $=5747$ |  |
| S | , $\mathrm{SO}_{2}$. | $=2220$ |  |

If a fuel contains $c \%$ carbon, $\pi \%$ hydrogen, $0 \%$ oxygen, $s \%$ sulphur, and $w \%$ water, then the heat developed is :-

$$
\mathrm{H}=\frac{8080 c+28780\left(h-\frac{1}{8} 0\right)+2500 s+600 w}{100}
$$

Table of Melting-point of Easily Fusible Alloys.

| Degrees Cent. | Parts by Weight. |  |  |  | Degrees Cent. | Parts by Weight. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Tin. | Lead. | Bismuth. | Cadmium. |  | Tin. | Lead. |
| 65 | 4 | 8 | 15 | 3 | 135 | 3 | 2 |
| 77 | 3 | 5 | 8 | $\ldots$ | 137 | 2 | 1 |
| 99 | 1 | 1 | 1 | $\ldots$ | 144 | 3 | 1 |
| 116 | 2 | 2 | 1 | $\ldots$ | 151 | 1 | 1 |
| 124 | 3 | 3 | 1 | $\ldots$ | 155 | 6 | 1 |
| 128 | 4 | 4 | 1 | $\ldots$ | 183 | 1 | 2 |
|  |  |  |  |  | 207 | 1 | 4 |

## Walker's List of Frigorific Mixtures.

Thermometer sinks degrees $F$.
$\left.\begin{array}{l}\text { Ammonium nitrate . . . . . } 1 \text { part } \\ \text { Water . . . . }\end{array}\right\}$ From $+40^{\circ}$ to $+4^{\circ}$
Ammonium chloride
Potassium nitrate
Water . . . .
. .
$\left.\begin{array}{llll}\text { Ammonium chloride } & . & . & 5 \\ \text { parts } \\ \text { Potassium nitrate } & . & . & 5 \\ \text { Sodium sulphate } & . & . & 8 \\ \text { Water } & . & . & .\end{array}\right\}$ From $+50^{\circ}$ to $+4^{\circ}$
$\left.\begin{array}{l}\text { Sodium nitrate } \quad . \quad . \quad 3 \text { parts } \\ \text { Nitric acid, diluted } \quad . \quad 2,\end{array}\right\}$ From $+50^{\circ}$ to $-3^{\circ}$

$\left.\begin{array}{l}\text { Sodium phosphate } . ~ . ~ \\ \text { Nitric acid, diluted . } \\ \text { parts } \\ \text {. }\end{array}\right\}$ From $+50^{\circ}$ to $+12^{\circ}$
$\left.\begin{array}{l}\text { Sodium Sulphate } \\ \text { Sulphuric acid, diluted } . \quad . \quad 5 \text { parls } \\ \text {. }\end{array}\right\}$ From $+50^{\circ}$ to $+3^{\circ}$
$\left.\begin{array}{llll}\text { Sodium sulphate } & . & . & 6 \\ \text { parts } \\ \text { Ammonium chloride } & . & 4 & " \\ \text { Potassium nitrate } & . & 2 & " \\ \text { Nitric acid, diluted . } & . & 4 & ,\end{array}\right\}$ From $+50^{\circ}$ to - 10
$\left.\begin{array}{lll}\text { Sodium sulphate . . . . } & 6 \text { parts } \\ \text { Ammonium nitrate . . . } & 5 & , \\ \text { Nitric acid, diluted } & 4 & \text {. }\end{array}\right\}$ From $+50^{\circ}$ to $-40^{\circ}$
Snow, or pounded ice
2 parts
Sodium chloride
1 part $\}$
to $-3^{\circ}$
Snow, or pounded ice
5 parts
Sodium chloride
Ammonium chloride part $\}$
to $-12^{\circ}$
Snow, or pounded ice
24 parts
Sodium chloride . . . 10
$\left.\begin{array}{lll}\text { Ammonium chloride . . . } 5 & , \\ \text { Potassium nitrate . . . } 5 & ,\end{array}\right\}$
Snow, or pounded ice . . . 12 parts
Sodium chloride
5
Ammonium nitrate
$5,$,
Snow
Sulphuric acid, dilute?
$\left.\begin{array}{l}3 \\ \therefore\end{array}\right\}$ parts $+32^{\circ}$ to $-23^{\circ}$

## Walker's List of Frigorific Mixtures (continued).

> Thermometer sinks degrees F.
$\left.\begin{array}{l}\text { Snow } \\ \text { Hydrochloric acid . . . } \\ 5 \\ \text { parts }\end{array}\right\}$ From $+32^{\circ}$ to $-27^{\circ}$

Snow Calcium chloride . . . . 5 parts,$\}$ From $+32^{\circ}$ to $-40^{\circ}$
$\begin{array}{l}\text { Snow } \\ \text { Calcium chloride, crystallized : } \\ 3\end{array}{ }_{3}^{2}$ parts $\}$ From $+32^{\circ}$ to $-50^{\circ}$
$\left.\begin{array}{|c}\text { Snow } \\ \text { Potash . . . . . . } \\ 4 \\ \text { parts } \\ \text {. }\end{array}\right\}$ From $+32^{\circ}$ to $-51^{\circ}$

## ELECTRICITY.

## Electroplatirg.

Solutions for electroplating small articles with simply strips zinc and copper for a battery.

Copper bronze solution.
To 4 oz. nitrate of copper, and 1 gall. cold water add 12 oz. sulphuric acid and 4 oz . ammonic chloride.

Silver solution.
To 5 dwts. silver chloride, 6 grs. bicarbonate of soda
$1 \frac{1}{2} \mathrm{oz}$. cyanide of potassium
$1 \frac{1}{2}$ pints water.
Boil for 5 minutes.
Gold solution.
To 15 grs. gold chloride, 3 grs. bicarbonate of soda, 3 drams cyanide of potassium, 4 oz . water.

Boil for 3 minutes.

| Unit. |  | Name. | Derivation. | Value. |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | C. G. S. | Equivalent. |
| E. M. F. | E | Volt | Ampère $\times$ ohm | $10^{8}$ | 0.926 standard Daniell cell. |
| Resistance | R | Ohm | Volt $\div$ Ampère | $10^{9}$ | $\int 106 \mathrm{~cm}$. mercury $1 \mathrm{sq} . \mathrm{mm}$. 1 section at $0^{\circ}$ Cent. |
| Current . | C | Ampère | Volt $\div$ Ohm | $10^{-1}$ |  |
| Quantity . | Q | Coulomb | Ampère per second. | $10^{-1}$ | $\left\{\begin{array}{c}0 \cdot 0000105 \text { gramme of hydro- } \\ \text { gen liberated per second. }\end{array}\right.$ |
| Capacity . | K | Farad | $\text { Coulomb } \div \text { Volt }$ | $10^{-9}$ |  |
| " | " | Microfarad | 1 millionth Farad | $10^{-15}$ | 2.5 knots of D. U. S. cable. |
| Power . | P | Watt | Volt $\times$ Ampère | $10^{7}$ | $0 \cdot 0013405$ or $\frac{1}{746}$ horse power. |
| Work • \} |  |  | Volt $\times$ Coulomb | " | 0.7373 ft . lbs. |
| Heat . | W | Joule . | $\mathrm{Amp}^{2} \times$ Sec. $\times$ Ohm . | " | 0.238 Calorie. |

C. G. S. system is made up of the fundamental units ; centimetre (for length), the gramme (for mass), and the second (for time).
E. M. F. Electro-motive force.
Electro-motive Forces of various Cells.

| Batteries. | + Plate. | Porous Cell. | - Plate. | Volts. |
| :---: | :---: | :---: | :---: | :---: |
| Daniell | Zinc amalg. | Sulphuric acid $7 \frac{1}{2}$ to $1 \left\lvert\,\left\{\begin{array}{c}\text { Saturated solution } \\ \text { of copper sulphate }\end{array}\right\}\right.$ | Copper | $\cdot 079$ |
| " | ", | 22 to 1. . . Nitrate" of copper saturated | " | $0 \cdot 978$ |
| $"$ | " | Nitrate of copper saturated Sulphate of copper | " | $\begin{aligned} & 1 \cdot 000 \\ & 0.909 \end{aligned}$ |
| P.O. | " | Sulphäte of zinc" satu-Sulphate of copper <br> ,. | ". | 0.909 |
| Standärd P.O. | " | Sulphate of zinc satu- Saturated solution | $\cdots$ $\cdots$ | 1.079 |
| Grove |  | Sulphuric acid $7 \frac{1}{2}$ to 1 Nitric acid (fuming). | Platinum | 1.956 |
| " | ", | Salt water . . . Nitric acid, sp. gr. 1.33 | ", | 1.904 |
|  |  | Sulphuric acid 22 to 1 | , | $1 \cdot 810$ |
| " | " | Sulphate of zinc ${ }^{\text {c }}$. ${ }^{\text {c }}$ |  | $1 \cdot 672$ |
| Bunsen | " | Dilute sulphuric acid . Nitric acid | Carbon | 1.734 |
| Smee | Zinc | Sulphuric 1, Water 7 | $\left\{\begin{array}{r}\text { Platinised } \\ \text { silver }\end{array}\right\}$ | $0 \cdot 47$ |
| Walker |  |  | ,, carbon | $0 \cdot 65$ |
| Callan | Zinc amalg. | Dilute sulphuric acid . Nitric acid | ast iron . | 1.700 |
| Poggendorf | ," | - " $\quad$, Bichromate of potash | Carbon | 1.796 |
|  |  |  |  |  |
| Marié Davy | " | Sulphuric acid 22 to 1 \{ $\left.\begin{array}{c}\text { Paste of sulphate of } \\ \text { mercury . . . }\end{array}\right\}$ | " | . 524 |
|  | " | Dilute sulphuric acid . ", |  | .33 |
| Leclancié | " | $\left\{\begin{array}{c}\text { Solution of sal am- } \\ \text { moniac }\end{array}\right\}$ Binoxide of Manganese | " | -48 |
| De la Rue | Zinc | Chloride of ammonium | \{ Silver \& | $1 \cdot 030$ |
| Skrivanov |  |  |  |  |
| (pocket form) $\}$ | " | Solution 75 caustic potash to 100 water | " |  |
| Becquerel . | Zinc amalg. | Sulphate of zinc . . Sulphate of lead. | Lead. | 0.55 |

ELECTRO-MOTIVE FORCES OF VARIOUS CELLS (continurá).

| Batteries. | + Plate. | Porous Cell. |  | - Plate. | Volts. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Niaudet | Zinc amalg. | Common salt | Chloride of lime | Carbon | $1 \cdot 65$ |
| Duchemin |  |  | Perchloride of iron. | Lead | 1.541 |
|  | Platinum . | Dilute sulphuric aci | Dilute sulphuric acid | Platinum | 1.79 |
| $\left.\begin{array}{rr}\text { Latimer Clark } \\ \text { (standard cell) }\end{array}\right\}$ | Zinc amalg. | Sulphate of zinc | Paste of sulphate of | Mercury | $1 \cdot 457$ |
| $\left.\begin{array}{c} \text { Howell's Man- } \\ \text { ganese ; inter- } \\ \text { nal res. }=1 \\ \text { ohm (Hockin) } \end{array}\right\}$ | " | Ammonic sulphate 25 grms. crystallized salt to 1 litre water | mercury <br> Sulphuric acid, 1 acid to 5 parts water | $\begin{gathered} \text { Carbon } \\ \mathrm{MnO}_{2}+ \\ \mathrm{MnSO}_{4} \end{gathered}$ | \} $2 \cdot 04$ |
| Higgin's cascade, internal res. $=0 \cdot 170 \mathrm{ohm}$ ) | Zinc in mercury. | Chromic acid | Sulphuric acid | Carbon | $1 \cdot 9$ |
| Thame's . | Zinc |  |  | Carbon | 2 |
| Bennet's, internal res. $=5$ ohm |  | K H O with distilled water | Damped with $\mathrm{K} \mathrm{H}^{2}$ and water | Iron can with iron borings | $1 \cdot 3$ |
| $\left.\begin{array}{c} \text { Lalande - Cha- } \\ \text { peron } \end{array}\right\}$ | Zinc amalg. | Caustic soda solution | $\left\{\begin{array}{c} \text { Oxide of copper or } \\ \text { copper scale } \end{array}\right\}$ | Iron | 1 |
| $\begin{aligned} & \text { Faure's second- } \\ & \text { ary battery } \end{aligned}$ | Lead plate coated with minium | \} Dilute sulphuric acid | Dilute sulphuric acid $\{$ | Lead plate coated with minium | $\} \begin{aligned} & 2 \cdot 0 \\ & 2 \cdot 2\end{aligned}$ |
| $\begin{aligned} & \text { Sellon - Volck- } \\ & \text { mar } \end{aligned}$ | Lead plate primed with minium . | $\left\{\begin{array}{l} \text { Sol. sulphuric acid, sp. } \\ \text { gr. } 1 \cdot 100^{\circ} \end{array}\right.$ | $\begin{aligned} & \text { Sol. sulphuric acid, sp. } \\ & \text { gr. } 1 \cdot 100^{\circ} \end{aligned}$ | Lead plate primed with minium | $\}^{2 \cdot 15}$ |
| Planté | Lead | Dilute sulphuric acid | Dilute sulphuric acid | Lead(spongy) | $\left\{\begin{array}{l}2.0- \\ 2.2\end{array}\right.$ |

## AIR AND WATER.

Wind.

| Velocity in Miles per Hour. | Velocity in Feet per Second. | Pressure in Pounds per Square Foot. | Reuarks. |
| :---: | :---: | :---: | :---: |
| 1 | $1 \cdot 467$ | -005 | Hardly perceptible. |
| 2 | $2 \cdot 933$ | -020 | Pleasant. |
| 3 | $4 \cdot 400$ | -045 | , |
| 4 | $5 \cdot 867$ | -080 | ", |
| 5 | $7 \cdot 33$ | -125 | ", |
| 10 | $14 \cdot 67$ | -5 | F" breer |
| 122 | 18.33 | $\cdot 781$ | Fresh breeze. |
| 15 | $22 \cdot 0$ | $1 \cdot 125$ | ", |
| 20 | 29.33 | 2.0 | " |
| 25 | $36 \cdot 67$ | $3 \cdot 125$ | Brisk wind. |
| 30 | $44 \cdot 0$ | $4 \cdot 5$ | Strong wind. |
| 40 | 58.67 | $8 \cdot 0$ | High wind. |
| 50 | $73 \cdot 33$ | $12 \cdot 5$ | Storm. |
| 60 | 88.0 | 18.0 | Violent storm. |
| 80 | $117 \cdot 3$ | 32.0 | Hurricane. |
| 100 | 146.7 | 50.0 | $\left\{\begin{array}{c}\text { Violent hurricane, up- } \\ \text { rooting large trees. }\end{array}\right.$ |

Windmills make use of about 29 per cent. of the energy imparted to them.
Table of Quantity of Water per Acre for a given Depth of Rainfall.

| Fall in Inches. | Cubic Feet per Acre. | Fall in Inches. | Cubic <br> Feet per Acre. | Fall in Inches. | Cubic <br> Feet per Acre. | Fall in Inches. | Cubic <br> Feet per Acre. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 7,260 | $\frac{3}{8}$ | 1,361 | $\frac{1}{10}$ | 363 | $\frac{1}{40}$ | 91 |
| $1 \frac{3}{4}$ | 6,352 | $\frac{1}{4}$ | 907 | $\frac{1}{12}$ | 302 | $\frac{1}{50}$ | 73 |
| $1 \frac{1}{2}$ | 5,445 | $\frac{1}{5}$ | 726 | $\frac{1}{14}$ | 259 | $\frac{1}{601}$ | 61 |
| $1 \frac{1}{4}$ | 4,537 | $\frac{1}{6}$ | 605 | $\frac{1}{16}$ | 227 | $\frac{1}{70}$ | 52 |
| 1 | 3,630 | $\frac{1}{7}$ | 519 | $\frac{1}{20}$ | 181 |  |  |
| $\frac{3}{4}$ | 2,723 | $\frac{1}{8}$ | 454 | $\frac{1}{30}$ | 121 | 1 point | $\}^{00}$ |
| $\frac{1}{2}$ | 1,815 | $\frac{1}{8}$ | 403 |  |  |  |  |

Example.-What quantity of water has been deposited on 20 acres of land when the rainfall was $\frac{1}{9}$ th of an inch?

In the column for "Fall in inches," opposite $\frac{1}{8}$ th, we find 403, which is the number of cubic feet deposited on 1 acre for that rainfall. This multiplied by 20 gives the required
quantity -403 cubic feet $\times 20$ acres $=8,060$ cubic feet. The quantity of water absorbed by the earth depends on the nature of the rain, time of year, lie of country, sort of rock, and the angle at which it is placed, \&c.

One inch in depth per acre weighs 101 tons.

## STATICS.

## Pressure against Walls.

Multiply the square of the height of the wall in feet, by the number contained in the last column of the subjoined table, for the pressure in lbs. per sq. foot acting horizontally against the back of the wall, at a point one-third of the height above the base.

| Nature of the Earth. | Weight of Cubic Foot in Pounds. | Natural Slope. | Constant Multiplier. |
| :---: | :---: | :---: | :---: |
| Fine dry sand | 94 | $30^{\circ} 0^{\prime}$ | 15.666 |
|  | 119 | $40^{\circ} 0^{\prime}$ | 12.938 |
| Loose shingle, perfectly dry . | 106 | $39^{\circ} 0^{\prime}$ | 12.058 |
| Common earth, perfectly dry and pulverulent . | 94 | $43^{\circ} 10^{\prime}$ | 8.815 |
| Common earth, slightly moistened, or in its natural state $\}$ | 106 | $54^{\circ} 0^{\prime}$ | 5.595 |
| Earth, the most dense and \} compact | 125 | $55^{\circ} 0^{\prime}$ | 6.213 |

Vertical pressure of water per square foot $=62.5 \times$ depth of water.

Horizontal pressure of water per square foot $=31.25 \mathrm{lbs} . \times$ the square of the depth at centre of pressure.

The total pressure against an upright wall is:Length $\times \frac{2 \text { depth }}{3} \times 62.5 \mathrm{lbs}$.
The total pressure against a sloping bank is :--
Length $\times \frac{\text { depth }}{2} \times 62.5 \mathrm{lbs}$.
Centre of pressure : Of a rectangle is at two-thirds its depth from top. Of a triangle whose base is horizontal and upon the water-line at half depth.
Of a triangle whose summit is at the water-line, base horizontal and at the lower level, at three-quarters of depth.




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## DYNAMICS．

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| $n$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ${ }^{259}$ | ${ }^{26} 1.180$ | ${ }^{26 \cdot 285}$ | ${ }^{26} \mathbf{2 6} 3.39$ | 26.494 | ${ }^{26 \cdot 599}$ | ${ }^{26}{ }_{2} \cdot 7 \cdot 704$ | 26:808 | ${ }^{26} 9.913$ | ${ }^{27}{ }^{27} 018$ | ${ }^{27} 1.122$ |
| ${ }_{270}^{260}$ | ${ }_{28}^{27 \cdot 2274}$ | ${ }_{28}^{27 \cdot 3379}$ | 27.437 28.484 | ${ }_{28}^{27 \cdot 5858}$ | ${ }_{28}^{27.6693}$ | ${ }_{28}^{27.798}$ | ${ }_{2}^{27 \cdot 855}$ | ${ }_{2}^{27.960}$ | ${ }^{28 \cdot 065}$ | ${ }_{2}^{28 \cdot 170}{ }_{29}$ |
| 230 | 29:322 | ${ }^{29 \cdot 426}$ | 29.531 | ${ }^{29} 9636$ | ${ }^{29} \cdot 7740$ | ${ }_{29}^{29845}$ | 299950 | $30 \cdot 055$ | $30 \cdot 159$ | $30 \cdot 264$ |
| ${ }^{290}$ | 30-369 | ${ }^{30 \cdot 473}$ | 30.578 | ${ }^{30} 0.638$ | ${ }^{30} 7788$ | 30-892 | 30:997 | ${ }^{31} \cdot 102$ | $31-206$ | ${ }_{31} \cdot 311$ |
| 309 | ${ }^{31 \cdot 416}$ | ${ }^{31 \cdot 521}$ | ${ }_{31} 36.65$ | ${ }^{31 \cdot 730}$ | 31:835 | ${ }^{31 \cdot 940}$ | ${ }^{32} \cdot 0.044$ | ${ }^{32} \cdot 149$ | 32-254 | 32-358 |
| 310 323 | ${ }_{3}^{32 \cdot 463}$ | ${ }_{3}^{32 \cdot 5688}$ | $32 \cdot 673$ 38.720 | ${ }_{3}^{32 \cdot 7777}$ |  | ${ }^{32 \cdot 987}{ }_{34}$ | $33 \cdot 091$ $34 \cdot 139$ | ( ${ }_{3}^{33 \cdot 1963}$ | $33 \cdot 301$ <br> 34348 |  |
| 330 | ${ }_{34} 5588$ | ${ }_{34}{ }^{35662}$ | ${ }_{34}$ | ${ }_{34}+872$ | ${ }_{34} 979$ | ${ }_{35}{ }^{34} 081$ | 344139 $35 \cdot 186$ | ( $\begin{aligned} & 34.243 \\ & 35.291\end{aligned}$ | $34 \cdot 348$ $35 \cdot 395$ | 34453 <br> $35 \cdot 500$ |
| 340 3 300 | ${ }^{35 \cdot 605}$ | ${ }^{357709}$ | 35:814 | $35 \cdot 919$ | 36:024 | 36.128 | 36-233 | 36:338 | ${ }^{36} \cdot 442$ | $36 \cdot 547$ |
| 350 360 | $36 \cdot 652$ 37699 | ${ }_{\substack{36 \cdot 757 \\ 37 \cdot 804}}$ | 36.861 37909 | ${ }_{\text {cke }}^{36 \cdot 966}$ | 37.071 38.118 |  | ¢ 38.280 | ( 37.385 | (37490 | ${ }_{\substack{37 \\ 38.594 \\ 38.642}}$ |
| ${ }_{370}$ | ${ }_{38} / 746$ | ${ }_{38} 8.851$ | ${ }_{38} 9.956$ | ${ }_{39}^{39.060}$ | ${ }_{39} \cdot 165$ | ${ }_{39-270}^{38}$ | ${ }_{39} 3$ | ${ }_{39} \cdot 479$ | ${ }_{39} 584$ | ${ }_{39} 38.689$ |
| 380 | 39.794 | -39.898 | ${ }^{40 \cdot 003}$ | $40 \cdot 108$ 41.155 | 40.212 41.260 | ${ }_{4}^{40} 4.3178$ | + $40 \cdot 422$ | ${ }^{40 \cdot 527}$ | ${ }^{40 \cdot 631}$ | 40'736 |
| 400 | ${ }_{41} \cdot 888$ | ${ }_{41}+993$ | 42-097 | ${ }_{42} 42.202$ | ${ }_{4}^{42} 4207$ | ${ }_{42 \cdot 412}^{41.364}$ | ${ }_{442 \cdot 516}^{41} 4$ | ${ }_{42 \cdot 621}^{41574}$ | ${ }_{4}^{42} \cdot 7 / 726$ | ${ }_{4}^{41}{ }_{4}^{4} \cdot 7338$ |
| 410 | 42:935 | 43.000 | ${ }^{43} \cdot 145$ | ${ }^{43} 3.299$ | 43:354 | 43:599 | ${ }^{43} 5.563$ | ${ }^{43} \cdot 668$ | 43.773 | 43:878 |
| 420 | ${ }^{43 \cdot 982}$ | 44.087 | $44 \cdot 192$ | 44-296 | 44401 | $44 \cdot 506$ | $44 \cdot 611$ | $44 \cdot 715$ | 44-820 | $44 \cdot 925$ |
| ${ }_{440}^{430}$ | ${ }_{46}^{45 \cdot 0077}$ | ${ }_{46 \cdot 181}^{45 \cdot 134}$ | ${ }_{46}^{45 \cdot 239}$ | ${ }_{46}^{45 \cdot 394}$ | ${ }_{46 \cdot 496}^{45 \cdot 448}$ | ${ }_{46}^{45 \cdot 650}$ |  |  |  | ${ }^{45} 5 \cdot 972$ |
| 450 | ${ }_{47}$ | ${ }_{47}^{47 \cdot 29}$ | ${ }_{47}^{47} 333$ | ${ }_{47}^{47} 438$ | ${ }_{47}^{46} 543$ | ${ }_{47}^{40.647}$ | ${ }_{47}^{46} \cdot 752$ | ${ }_{47}^{46 \cdot 857}$ | ${ }_{47 \cdot 962}^{46 \cdot 974}$ | ${ }_{48}^{47} 8.006$ |
| 460 | ${ }_{4}^{48} 8171$ | 488.276 | 48:381 | ${ }^{48 \cdot 485}$ | ${ }^{48 \cdot 590}$ | - $48 \cdot 6.695$ | ${ }^{48} 8.799$ | ${ }_{48} 4 \cdot 904$ | ${ }^{49} 50.099$ | 49.114 |
| 480 480 | $49 \cdot 218$ <br> $50-265$ | 49:323 $50 \cdot 370$ | $49 \cdot 428$ $50 \cdot 475$ | 40.532 $50 \cdot 580$ |  | ¢9.742 $50 \cdot 789$ | 4.9.847 $50 \cdot 894$ | 49.951 $50 \cdot 999$ | 50.056 51.103 | 50.161 51.208 |
| 490 | 51.313 | $51 \cdot 417$ | 51.522 | 51.627 | 51.732 | 51 1836 | 51.941 | 52.046 | $52 \cdot 150$ | 52.255 |

Table of Falling Bodies, giving the Space fallen through to acquire certain Velocities.

| Velocity in Feet per Sec. | Space. | Velocity in Feet per sec. | Space. | Velocity in F eet per Sec. | Space. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $\begin{array}{cc}\text { Ft. } & \text { Ins. } \\ 0 & 0 \frac{3}{16}\end{array}$ | 21 | Ft.Ins. <br> 10 | 41 | Ft. Ins. |
| 2 | $0 \quad 0 \frac{3}{4}$ | 22 | 76 | 42 | 275 |
| 3 | 0 1 1 \% | 23 | 83 | 43 | $28 \quad 9$ |
| 4 | 03 | 24 | 90 | 44 | 301 |
| 5 | 0 4 48 | 25 | $9 \quad 9$ | 45 | 315 |
| 6 | 0 O $6 \frac{3}{4}$ | 26 | 106 | 46 | 3210 |
| 7 | 0 9 9 l | 27 | 11.4 | 47 | $34 \quad 4$ |
| 8 | 10 | 28 | 123 | 48 | 3610 |
| 9 | $13^{1} \frac{1}{4}$ | 29 | 130 | 49 | 374 |
| 10 | $1{ }^{1} \frac{3}{4}$ | 30 | 140 | 50 | 3811 |
| 11 | $110 \frac{1}{2}$ | 31 | 1411 | 52 | 420 |
| 12 | 23 | 32 | 1511 | 54 | 454 |
| 13 | 2 71 | 33 | 1611 | 56 | 50 |
| 14 | $3{ }^{3} \quad 0 \frac{3}{4}$ | 34 | 180 | 58 | 520 |
| 15 | 36 | 35 | 19 0 | 60 | 560 |
| 16 | 40 | 36 | 201 | 62 | 598 |
| 17 | 46 | 37 | 215 | 64 | 638 |
| 18 | 50 | 38 | 226 | 66 | 678 |
| 19 | 57 | 39 | 239 | 68 | 720 |
| 20 | 63 | 40 | 2411 | 70 | $76 \quad 0$ |

Falling Bodies.

| Time in Seconds. | Whole Space Fallen. | Velocity Acquired, Feet per Second. | Time in Seconds. | Whole Space Fallen. | Velocity Acquired, Feet per Second. |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Ft. Ins. | Ft. |  | Ft. Ins. | Ft. |
| $\frac{1}{10}$ | $0011 \frac{15}{18}$ | $3 \cdot 2$ | $1 \frac{1}{10}$ | 19 43 | $35 \cdot 2$ |
| $\frac{2}{10}$ | $0{ }^{0} 78$ | 6.4 | $1 \frac{2}{10}$ | $230 \frac{1}{2}$ | $38 \cdot 4$ |
| $\frac{3}{10}$ | $15 \frac{1}{4}$ | $9 \cdot 6$ | $1 \frac{3}{10}$ | 27 01 | $41 \cdot 6$ |
| $\stackrel{4}{10}$ | $2 \quad 6 \frac{3}{4}$ | $12 \cdot 8$ | $1{ }^{4} 10$ | $31 \quad 4 \frac{3}{8}$ | $44 \cdot 8$ |
| $\frac{5}{10}$ | 40 | $16 \cdot 0$ | 15 | 360 | $48 \cdot 0$ |
| $\frac{6}{10}$ | $5 \quad 9 \frac{1}{8}$ | $19 \cdot 2$ | $1{ }^{10}$ | 410 | $51 \cdot 2$ |
| $\frac{7}{10}$ | 710 | $22 \cdot 4$ | $1 \frac{7}{10}$ | $46 \quad 2 \frac{5}{8}$ | $54 \cdot 4$ |
| $\frac{10}{10}$ | $10 \quad 2 \begin{array}{ll}10\end{array}$ | $25 \cdot 6$ | $1 \frac{8}{10}$ | 511 | $57 \cdot 6$ |
| $\frac{9}{10}$ | $1211 \frac{1}{2}$ | $28 \cdot 8$ | 19 | 57 91 | $60 \cdot 8$ |
| 10 | 160 | $32 \cdot 0$ | 2 | 640 | $64 \cdot 0$ |

## MOTORS Self-acting Inclines. ${ }^{1}$

Let $a$ be the angle of inclination.
C the coefficient of friction of trucks and rope.
W the weight in lbs. of the loaded truck.
$w$ the weight in lbs. of the empty truck.
$r$ the weight of the rope for the length of the incline in lbs.
$\mathbf{C}^{\prime}$ the coefficient of friction for the drum.
$f$ the amount of resistance due to friction for drum in lbs., or $=2 \mathrm{C}^{\prime}[(w+r) \sin a+\mathbf{C}(w+r) \cos a]$.
The coefficient of friction is equal to the tangent of the angle of inclination (also known as "the angle of friction," "the limiting angle of frictional stability," or the "angle of repose"), on which the force exerted by gravity is exactly counterbalanced by the frictional resistance.

When a waggon (W) is placed on an inclined plane, the force with which it tends to move down the plane, disregarding friction, is-
$W \sin a$
As the amount of friction equals the pressure multiplied by the coefficient of friction, the amount of friction encountered in moving a waggon (W) on an inclined plane is-

WC $\cos a$.
When W $\sin a=\mathrm{WC} \cos a$ or $\frac{\sin a}{\cos a}=\tan a=\mathrm{C}$ the force with which the waggon tends to move downhill is exactly held in equilibrium by the amount of friction. The force with which a loaded waggon tends to move down the plane when the angle of inclination exceeds the angle of friction is-

$$
\mathrm{W} \sin a-W C \cos a
$$

and under the same conditions, the force with which the empty waggon resists motion up the hill is

$$
\mathrm{W} \sin a+\mathrm{WC} \cos a
$$

The smaller the difference between (W) and $(w)$ the greater the angle of slope required to make a self-acting plane.

One must also consider the weight of the rope and its friction on the rollers of the incline, and the friction on the periphery and axle of the drum round which the rope passes. The principal factors in determining the coefficient of friction for wheeled carriages moving on rails are the ratio of the diameter of the wheel to that of the axle, the quality of the lubricant, and the smoothness of the contact surfaces. Take the coefficient of friction for the rope on the rollers

[^0]as being the same as that of the waggon, though it should really be a little greater on account of the sag of the rope and the roughness of its surface ; the resistance offered by the rope will be continually decreasing as the empty car ascends the plane. The required angle of inclination will increase with the length of the incline.

So long as $\mathrm{W} \sin a>(w+r) \sin a+\mathrm{C}(\mathrm{W}+w+r) \cos a$, the conditions permit a self-acting plane, but when $W \sin a$ is equal to or smaller than the second number of this formula, no motion can be produced by gravity alone.

As the weights for steel ropes are nearly in proportion to their respective safe working strengths, if the load is increased the weight of the rope in the same ratio must also be increased. Therefore the angle sought would be the same for any number of waggons per trip as for one waggon. But if the rope used for a one waggon trip is stronger than necessary, so that additional waggons can be put on without using a heavier rope, then it may be possible to make the plane sufficiently self acting by simply increasing the number of waggons in a set.

As the resistance of the empty waggon and rope to the motion up the plane is-

$$
(w+r) \sin a+C(w+r) \cos a
$$

the strain executed by the loaded car to move down must be at least equal to this, hence the strain on the drum round which the connecting rope passes must be at least

$$
2[(w+r \sin a+\mathbf{C}(w+r) \cos a]
$$

The tangent of angle of minimum grade of a self-acting gravity incline when all resistance of gravity and friction are considered, equals-

$$
\frac{\mathrm{C}(\mathrm{~W}+w+r) \times \frac{f}{\cos a}}{\mathrm{~W}-(\nu,+r)}
$$

If there is not much to spare above the necessary grade, there should be a short piece of level track at the bottom of the incline, and, if necessary, a heavier grade at the top, so that the waggons can start easier. It is best practice to have the grade as nearly uniform as possible. Anyhow, there should not be too sudden a change in level, or else the waggon when passing from a steep grade to a lighter one may have the upper wheels lifted off the track by the rope. The frictional resistance encountered in starting from a state of rest may be taken as at about twice the friction of motion. If the grade is made greater at the top and lighter at the bottom, the speed due to acceleration will diminish, as the motive force varies with the size of the angle of inclination; the inertia carries the waggons over the flat portion.

## Aerial Ropeways.

In principal these may be classified under five headings.

1. One fixed rope down which carriers run uncontrolled. Suitable for goods that cannot be damaged. No intermediate supports are required; the rope which may be $\frac{1}{2}$ inch diameter is anchored at the top end, and tightened at the lower by a Spanish windlass. The speed may be regulated to a certain extent by the sag of the rope. Has been used for spans up to 7,000 feet.
2. One fixed rope and an endless hauling rope. One carrier is drawn backwards and forwards by an endless rope. The motive-power must have reversing gear. The return hauling rope is supported on a pulley attached to an arm outside each post. Will work on inclines of 1 in 1 , and for spans up to 6,000 feet. Can be used for loads up to 5 tons.
3. Two fixed ropes and one hauling rope with a carrier at each end. Worked by gravity, controlled by break gear if grade not less than 15 in 100 . Can run at a speed of $30-40$ miles per hour when towers are not used, otherwise must reduce speed to 10 miles per hour. Can use spans up to 6,000 feet and loads up to 6 tons. For ordinary work the carrier rope is $\frac{3}{4}$ inch diameter, and the hauling rope $\frac{1}{4}$ inch diameter. Must have a station at every change in direction.
4. Two fixed ropes with an endless hauling rope. The hauling rope is driven from one end and tightened at the other. A series of buckets, weighing when loaded 4 to 14 cwt ., are clipped to the hauling rope at intervals of about 130 feet. The carrying rope is from 0.8 to 1.4 inch diameter for full buckets, and 0.6 to 1.2 inch diameter for empties, and last from five to ten years. The hauling rope is 0.63 inch diameter and lasts about eight years. A gradient of 1 in 7 is self-operating. Travels at a speed of $3 \frac{1}{2}$ miles per hour. If distances are over 15,000-18,000 feet have intermediate stations, and where distances between stations exceed 8,000 feet have an intermediate tightening gear. May have spans 1,500 feet long. Two men with scoop buckets can load about 6 tons per hour into moving buckets. With automatic loader one man can fill 30 tons an hour. Suitable for quantities between 40 and 80 tons per hour. This system is economical in wear and tear, but first cost is great. The rope should be supported every 50 to 60 yards when possible. Clips may be fixed or adjustable.
5. Endless running rope with carriers hanging therefrom, either loose, fixed, or detachable. Suitable for flat or uneven country. It is advisable to have ropeways in a straight line, but can construct for angles if absolutely necessary. For quantities not exceeding 30 tons an hour. Speed not over 175 feet per minute. Can fill by hand, if not run faster than 2 to $2 \frac{1}{2}$ miles an hour.

Work of a Man against Known Resistances.

| Kind of Exertion. | L. R . | $\begin{aligned} & \text { V. } \\ & \text { Ft. per } \\ & \text { Sec. } \end{aligned}$ | $\begin{gathered} \frac{\mathrm{T}^{\prime \prime}}{} \\ \frac{3600}{} \\ \text { Hours } \\ \text { per } \\ \text { Day. } \end{gathered}$ | R.V. per Sec. | R.V.T. <br> Ft. Lbs. per Day. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1. Raising his own weight up stair or ladder | 143 | 0\% 5 | 8 | 72.5 | 2,088,000 |
| 2. Hauling up weights with rope, and lowering the rope unloaded | $\} 40$ | $0 \cdot 75$ | 6 | 30 | 648,000 |
| 3. Lifting weights by hand | $\} 44$ | $0 \cdot 55$ | 6 | 24.2 | 522,720 |
| 4. Carrying weights up stairs and returning unloaded | $\} 143$ | $0 \cdot 13$ | 6 | $18 \cdot 5$ | 399,600 |
| 5. Shovelling upearth to a height of $5^{\prime} 3^{\prime \prime}$ | $\}^{6} 6$ | $1 \cdot 3$ | 10 | $7 \cdot 8$ | 280,800 |
| 6. Wheeling earth in a barrow up slope of 1 in 12 $\frac{1}{2}$ horiz. veloc. 0.9 per ft. sec. and returning unloaded | 132 | 0.075 | 10 | $9 \cdot 9$ | 3506,400 |
| 7. Pushing or pulling horizontally(capstan or bar) | $\} 26.5$ | 2.0 | 8 | 53 | 1,526,400 |
| 8. Turning a crank or winch | $\left\{\begin{array}{l}12.5 \\ 18.0 \\ 20\end{array}\right.$ | $5 \cdot 0$ 2.5 | ? | 62.5 45 | 1,296,000 |
| 9. Working pump . | 180 20.0 13.2 | $14 \cdot 4$ $2 \cdot 5$ | 2 min . | 288 33 | 1.188,000 |

Seven men are considered equal to one horse.

## Work of a Horse against Known Resistances.

In the following table (page 115), $\mathrm{R}=$ resistance ; $\mathrm{V}=$ effective velocity $=$ dist. through which $R$ is overcome $\div$ total time occupied, including time of moving unloaded, if any; $T^{\prime \prime}=$ time of working, in sec., per day ; $\frac{T^{\prime \prime}}{3600}$, same time, in hours per day ; R.V., effective power in foot pounds per second ; R.V.T. daily work in foot pounds. A horse should be put down a pit
at about five to seven years of age; should travel from fourteen to sixteen miles per day in a fairly level mine at a walking pace, and last about seven years. One horse-keeper is required for twelve horses, or for sixteen ponies. A pony should not be put into the pit under three years of age.

A horse is most efficient at a low speed (two or three miles per hour), and can do $22,000 \mathrm{ft}$. lbs. per min., or about $\frac{2}{3}$ of a mechanical horse-power.

Three $14 \cdot$ hand ponies $=$ two horses ; two small ponies $=$ one horse.

| Kind of Exertion. | Lbs. | $\begin{aligned} & \text { V. } \\ & \text { Ft. per } \\ & \text { Sec. } \end{aligned}$ | $\begin{gathered} \frac{\mathrm{T}^{\prime \prime}}{} \begin{array}{c} 3,600 \\ \text { Hours } \\ \text { per } \\ \text { Day. } \end{array} \end{gathered}$ | $\begin{gathered} \text { R.V. } \\ \text { Ft. } \\ \text { Lbs. } \\ \text { per } \\ \text { Sec. } \end{gathered}$ | R.V.T. Ft. Lbs. per Day. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1. Cantering and trotting, drawing a light railway carriage (thoroughbred) | min. $22 \frac{1}{2}$ mean $30 \frac{1}{2}$ $\operatorname{max.} 50$ | \} $14 \frac{2}{3}$ | 4 | $447 \frac{1}{2}$ | 6,444,000 |
| 2. Horse drawing cart or boat walking (draught horse) | $\} 120$ | $3 \cdot 6$ | 8 | 432 | 12,441,600 |
| 3. Horse drawing a gin or mill, walking . | $\{100$ | $3 \cdot 0$ | 8 | 300 | 8,640,000 |
| 4. Ditto trotting . | 66 | $6 \cdot 5$ | $4 \frac{1}{2}$ | 429 | 6,950,000 |

## Steam Engines.

Horse Power.-One horse-power $=33,000$ foot pounds per minute $=42.75$ British thermal units per min.

For the actual horse-power exerted by an engine :-
Let $p=$ the mean effective pressure of steam in lbs. per sq. inch, less 3 pounds per sq. inch frictional allowance.
" A = the area of the cylinder in square inches.
, $\mathrm{L}=$ the length of the stroke in feet.
$\mathrm{N}=$ the number of strokes per min. $=$ revolution $\times 2$.
;, H.P. = the horse-power.

$$
\text { H.P. }=\frac{p \mathrm{~L} \mathrm{~A} \mathrm{~N}}{33,000}
$$

In the best class of engines, and with the best steam coal, the average consumption per indicated horse-power per hour should be as follows :-

Compound condensing engine . . from $1 \frac{1}{2} \mathrm{lbs}$. to 2 lbs . $\begin{array}{lllll}\text { Locomotive engines } \\ \text { High-pressure non-condensing engines } & " & 2 & 2 \frac{1}{2}, & 4,\end{array}$

Lubricants.-For light pressure where the temperature is low use mineral or rock oil. Equal parts of lard oil and paraffin make a good lubricant. For very heavy bearings use grease or tallow mixed with oil, or grease and plumbago.

## Steam Boilers.

The boiling point of any liquid is that point on the temperature scale when the tension throughout its mass just overcomes the surrounding pressure.

The boiling points of fresh water at different pressures are approximately as follows :-

| Under a pressure of | $\frac{1}{8}$ | atmosphere | $123^{\circ} \mathrm{F}$. |  |
| :---: | :---: | :---: | :---: | :---: |
| $"$ | $"$ | $\frac{1}{4}$ | $"$ | $150^{\circ}$ |
| $"$ | $"$ | $\frac{1}{2}$ | $"$ | $179^{\circ}$ |
| $"$ | $"$ | 1 | $"$ | $212^{\circ}$ |
| $"$ | $"$ | 2 | $"$ | $249^{\circ}$ |
| $"$ | $"$ | 3 | $"$ | $273^{\circ}$ |
| $"$ | $"$ | 4 | $"$ | $291^{\circ}$ |
| $"$ | $"$ | 5 | $"$ | $306^{\circ}$ |
| $"$ | $"$ | 6 | $"$ | $319^{\circ}$ |

To find the Nominal Horse-Power of Boilers.-Cornish Boilers:-Add the diameter of boiler and diameter of flue together in feet, multiply the sum by the length in feet, and divide the product by 8 .

Lancashire Boilers :-Add the diameters of both flues and the diameter of the boiler together in feet, multiply the sum by the length in feet, and divide the product by 8.

Vertical Tubular Boilers:-Add together the diameter of the shell, the diameter of the fire-box, and the diameters of all the tubes, all in feet; multiply the sum by the length in feet and divide by 12.

The actual horse-power of a boiler can be obtained by calculating the number of cubic feet water evaporated per hour.

To find the Number of Cubio Feet of Water Evaporated per Hour.-Multiply the number of square feet of water surface by the evaporation in inches of gauge glass, multiply the product by 5 , and divide the result by the number of minutes occupied in evaporation.

## The Lever Safety Valve-

Let $P=$ pressure of steam in lbs. per square inch less atmospheric pressure.
" $\mathrm{L}=$ length of lever from fulcrum to weight, in inches.
" $W$ =weight of load in pounds.
$\mathrm{W}^{\prime}=$ weight of lever in pounds.
$W^{\prime \prime}=$ weight of valve in pounds.
D = distance of the centre of gravity of the lever from the fulcrum in inches.
, $\mathrm{A}=$ area of valve in square inches.
I = length of lever between fulcrum and valve, ininches.

$$
P=\frac{\frac{W L}{I}+\frac{W^{\prime} D}{I}+W^{\prime \prime}}{A}
$$

Weight of a Boiler.-Weight in pounds=surface in square feet $\times 6$ for plates $\frac{1}{8}$ inch thick.

## Fuel.

Evaporative Power of Fuels.-The following quantities of fuels will evaporate 9 lbs . water when raised to $212^{\circ} \mathrm{F}$.

1 lb . steam coal. 2 lbs. dry peat. $2 \frac{1}{2}$ lbs. dry wood. $3 \frac{1}{4}$ lbs. cotton stalks.
$3 \frac{1}{2}$ lbs. brushwood.
$3 \frac{3}{4}$ lbs. straw.
4 lbs. sugar-cane refuse.

The British Thermal Unit is the quantity of heat required to raise 1 lb . of water $1^{\circ} \mathrm{F}$. when at its maximum density, i.e., from $39^{\circ} \cdot 1$ to $40^{\circ}$ ] F .

To find the Quantity of Water in Pounds Eraporated per Pound of Coal.-Multiply the number of cubic feet water evaporated per hour by 62.5 , and divide the product by the quantity of coals consumed per hour.

Table Showing the proper Diameter and Height of A Chimney for any Kind of Fuel. (Armstrong.)

| Nominal Horsepower of Boiler. | Height of Chimney in Feet. | Inside Diameter at Top. | Nominal HorseBoiler. | Height of Chimney in Feet. | Inside Diameter at Top. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | 60 | Ft. ${ }_{1}^{\text {In }}$. | 70 | 120 | $\begin{array}{rr}\text { Ft. } \\ 3 & \text { In. } \\ 6\end{array}$ |
| 12 | 75 | 18 | 90 | 120 | 40 |
| 16 | 90 | 110 | 120 | 135 | 46 |
| 20 | 99 | 20 | 160 | 150 | 50 |
| 30 | 105 | 26 | 200 | 165 | 56 |
| 50 | 120 | 30 | 250 | 180 | 60 |

The area of stacks for stationary boilers that have no other source of draught should be one-fifth greater than the total area of all the flues or tubes.

Pressures in Atmospheres.

| Atmo <br> spheres. | Lbs. on <br> the Square <br> Inch. | Lbs. on <br> the Square <br> Foot. | Kilo- <br> grammes <br> on the <br> Square <br> Metre. | Milli- <br> metres of <br> Mercury. | Inches <br> of <br> Mercury. | Feet <br> of <br> Water. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $14 \cdot 7$ | 2116 | 10333 | 760 | $29 \cdot 922$ | $33 \cdot 9$ |
| 2 | $29 \cdot 4$ | 4233 | 20666 | 1520 | $59 \cdot 844$ | $67 \cdot 8$ |
| 3 | $44 \cdot 1$ | 6349 | 30999 | 2280 | $89 \cdot 765$ | $101 \cdot 7$ |
| 4 | $58 \cdot 8$ | 8465 | 41332 | 3040 | $119 \cdot 687$ | $135 \cdot 6$ |
| 5 | $73 \cdot 5$ | 10581 | 51665 | 3800 | $149 \cdot 609$ | $169 \cdot 5$ |
| 6 | $88 \cdot 2$ | 12698 | 61998 | 4560 | $179 \cdot 531$ | $203 \cdot 4$ |
| 7 | $102 \cdot 9$ | 14814 | 72331 | 5320 | $209 \cdot 453$ | $237 \cdot 3$ |
| 8 | $117 \cdot 6$ | 16930 | 82664 | 6080 | $239 \cdot 374$ | $271 \cdot 2$ |
| 9 | $132 \cdot 3$ | 19047 | 92997 | 6840 | $269 \cdot 296$ | $305 \cdot 1$ |
| 10 | $147 \cdot 0$ | 21163 | 103330 | 7600 | $299 \cdot 218$ | $339 \cdot 0$ |

## TRANSMISSION OF POWER.

## Belting.

Castor oil is the best preservative for leather.
Driving-belts should be washed with warm water and greased three or four times a year. A good leather grease may be made from 4 parts fish oil ; 1 part lard or tallow; 1 part calophonium ; 1 part wood tar.
If a belt is dry or husky, should grease it with a mixture of neatsfoot oil and tallow, and dried in by the heat of the fire or sun.
Leather belts with the grain side to the pulley can drive $34 \%$ more than the flesh side.
When practicable, the driving half of horizontal belts should be the lower half, as, when the belt stretches, the upper half will cover more of the pulley's surface. Long horizontal belts are better than short ones, as their weight increases their contact with the pulley.
Belts running on pulleys perpendicular to each other should be kept tightly strained, as their weight tends to decrease their contact with the lower pulley. The full stretch of a belt is at least $2 \%$ or about 1 inch in 4 feet.
To calculate the width of belts required for transmitting different numbers of horse-power :-
Let $n=$ number of horse-power.
$v=$ length in feet the belt is to travel per minute. $s=$ feet or parts of a foot of belt in contact with smaller pulley.
$w=$ width of belt in inches.


To calculate the number of horse-power a belt will transmit :
Let $v=$ its velocity in feet per minute.
$s=$ number of square inches in contact with the smaller pulley.
$n=$ number of horse-power the belt will transmit.

$$
n=\frac{\frac{8}{2} \times v}{36,000}
$$

Cotton belting is made 4-ply from $1^{\prime \prime}$ to $6^{\prime \prime}, 6$-ply from $3^{\prime \prime}$ to $12^{\prime \prime}$, 8 -ply $6^{\prime \prime}$ to $30^{\prime \prime}$, and 10 -ply one to five feet wide.

Single leather belts are used for drums under $2 \frac{1}{2}$ feet diameter, and double belts over that diameter; more than two-fold leather is not used.

For the transmission of each horse-power there should be :45 superficial inchesin contact with the smaller pulley in leather. 50

| $200-30$ | $"$ | $"$ | $"$ |
| :---: | :---: | :---: | :---: |
| $"$ | $"$ |  |  |

india-rubber. cotton belting. Leather belts on smooth iron drums slip about . . . $3^{\circ} \%$ Rubber Cotton
", ",

## Speeding of Machinery.

## Speeding by Pulleys-

Let $\nabla=$ velocity or number of revolutions per minute of the driving pulley.
$v=$ velocity or number of revolutions per minute of the driven pulley.
$\mathrm{D}=$ diameter in inches of driving pulley.
$d=$ diameter in inches of driven pulley.
Then $v=\frac{\nabla \mathrm{D}}{d} ; \nabla=\frac{v d}{\mathrm{D}} ; d=\frac{\nabla \mathrm{D}}{v} ; \mathrm{D}=\frac{v d}{\mathrm{~V}}$.
Speeding by Wheels-
Let $N=$ number of teeth in driving wheel.
$n=$ number of teeth in driven wheel.
$\nabla=$ velocity or number of revolutions of driving wheel.
$v=$ veloc. or no. of revolutions of driven wheel per min.
Then $v=\frac{\mathrm{NV}}{n} ; \mathrm{V}=\frac{n v}{\mathrm{~N}} ; n=\frac{\mathrm{NV}}{v} ; \mathrm{N}=\frac{n v}{\mathrm{~V}}$.

## HYDRAULICS.

Greatest Velocities of Current close to the Bed of a Stream consistent with the Stability of the Material over which the Water Flows.

Ft. per Sec.

River mud, liquid earth $\quad 25$ Common clay, loam - 50 River sand . . . 1.00 Gravel, size of beans . $1 \cdot 50$ 1 inch . . . $2 \cdot 00$

Large shingle
Ft. per Sec.
3.00Broken stones .
$4 \cdot 00$Soft Schistose rockRockswithdistinctlayers $6 \cdot 00$

Hard rocks . . . $10 \cdot 00$
The mean velocities of current will be about $1 \frac{1}{3}$ times the velocities given above.

Table showing the Proper Angle for the Sides of Aqueducts of Different Material, and the Rate of Flow that should not re exceeded.

| Nature of Sides of Aqueduct. | Angle of Sides. | Maximum Rate of Flow. |
| :---: | :---: | :---: |
| Brickwork, masoury, or $\}$ solid rock . | Degrees. 90 | 5 feet to 10 feet per second. |
| Stone without mortar . | 60 | 4 feet per second. |
| Clay . | 45 |  |
| Coarse gravel | 40 | 3 feet per second. |
| Fine | 35 | 2 feet per second. |
| Sand . ${ }^{\text {S }}$ | 30 |  |
| Ordinary soil . | 20 | 3 inches per second. |

Water flows quicker over hard than soft material. The flow should be at least 1 to $1 \frac{1}{2}$ feet per second to prevent deposits or growth of plants.

Table showing Velocities of Water in Channels in Earth for various Slopes and Hydraulic Mean Depths, the Hydraulic Mean Depth being the Sectional Area of Waterway Divided by the Wetted Border of the Channel.

| Hydraulic Depth. | Fall per Mile. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $6 \mathrm{Ins}$. | 9 Ins. | 12 Ins. | 18 Ins. | 24 Ins. | 30 Ins. | $36 \mathrm{Ins}$. | 48 Ins. |
|  | ${ }^{\text {Ft. }}$ Miner | Min. per | Ft. ner | Ft. per | Ft. per | Ft. per | Ft. per | Ft. per |
| 5 |  |  |  |  | $3{ }^{3}$ | 41.3 | Min. | ${ }_{52.8}^{\text {Min. }}$ |
| -75) | $\ldots$ |  | 35.0 | $43 \cdot 6$ | $50 \cdot 8$ | $57 \cdot 2$ | $62 \cdot 8$ | $72 \cdot 9$ |
| $1 \cdot 00$ |  | $37 \cdot 7$ | $44 \cdot 1$ | $54 \cdot 8$ | 63.7 | $71 \cdot 6$ | 78.6 | 91.0 |
| $1 \cdot 25$ | $36 \cdot 2$ | $45 \cdot 1$ | $52 \cdot 6$ | $65 \cdot 1$ | 75.6 | $84 \cdot 9$ | 93.2 | $108 \cdot 0$ |
| 1.50 | $41 \cdot 8$ | $52 \cdot 0$ | $60 \cdot 6$ | $74 \cdot 8$ | 86.8 | $97 \cdot 3$ | 106.8 | 123.7 |
| 1.75 | $47 \cdot 3$ | $58 \cdot 6$ | $68 \cdot 1$ | $84 \cdot 0$ | $97 \cdot 4$ | $109 \cdot 1$ | 119.7 |  |
| $2 \cdot 00$ | 52.5 | $64 \cdot 9$ | $75 \cdot 3$ | 92.8 | 107.5 | $120 \cdot 4$ |  |  |
| $2 \cdot 50$ | $62 \cdot 4$ | 76.8 | 88.9 | 109.2 | $126 \cdot 3$ |  |  |  |
| $3 \cdot 00$ | $71 \cdot 6$ | $87 \cdot 8$ | $101 \cdot 8$ | 124.5 |  |  |  |  |
| $3 \cdot 50$ | $80 \cdot 4$ | $98 \cdot 3$ | 113.5 |  |  |  |  |  |
| $4 \cdot 00$ | 88.7 | $108 \cdot 3$ | $124 \cdot 8$ |  |  |  |  |  |
| $5 \cdot 00$ | $104 \cdot 4$ | $126 \cdot 9$ |  |  |  |  |  |  |
| 6.00 | 118.9 |  |  |  |  |  |  |  |

Velocity of Efflux. $-\mathrm{V}=$ velocity in feet per second; $\mathrm{H}=$ head of water in feet, then : $-\mathrm{V}=\sqrt{\mathrm{H}} \times 8$.

Discharge in Gallons. $-\mathrm{G}=$ gallons discharged per minute ; $\mathrm{H}=$ head of water in feet; $d=$ diameter of orifice in inches, then : $-\mathrm{G}=\sqrt{\mathrm{H}} \times \bar{d}^{2} \times 16.3$.

The above being the theoretical velocities discharged require modification according to the particular form of orifice.

Table of the Theoretical Discharge of Water by Round Apertures of various Diameters, and under different Heads of Water Pressure (Box.)

| Diam. inInches. | Head of Water in Inches. |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|  | Discharge in Gallons per Minute. |  |  |  |  |  |  |  |  |
| 1 | 4.7 | $6 \cdot 6$ | $8 \cdot 1$ | $9 \cdot 4$ | 10.5 | 11:5 | $12 \cdot 4$ | $13 \cdot 3$ | $14 \cdot 1$ |
| 2 | 18.8 | 26.4 | $32 \cdot 4$ | $37 \cdot 6$ | $42 \cdot 0$ | 46.0 | $49 \cdot 6$ | $53 \cdot 2$ | $56 \cdot 4$ |
| 3 | $42 \cdot 2$ | $59 \cdot 4$ | $72 \cdot 9$ | $84 \cdot 6$ | 94.5 | 103 | 112 | 120 | 127 |
| 4 | 75.2 | 106 | 130 | 150 | 168 | 184 | 198 | 213 | 225 |
| 5 | 117 | 165 | 203 | 235 | 262 | 287 | 310 | 332 | 352 |
| 6 | 169 | 237 | 291 | 338 | 378 | 414 | 446 | 479 | 507 |
| 7 | 230 | 310 | 397 | 460 | 514 | 563 | 607 | 652 | 691 |
| 8 | 301 | 422 | 518 | 601 | 672 | 736 | 793 | 851 | 902 |
| 9 | 381 | 534 | 656 | 761 | 850 | 931 | 1006 | 1077 | 1142 |
| 10 | 470 | 660 | 810 | 940 | 1050 | 1150 | 1240 | 1330 | 1411 |
| 12 | 676 | 9.2 | 1168 | 1353 | 1512 | 1656 | 1785 | 1915 | 2030 |
| 14 | 920 | 1241 | 1588 | 1842 | 2058 | 2254 | 2430 | 2606 | 2764 |
| 16 | 1203 | 1690 | 2074 | 2406 | 2688 | 2944 | 3174 | 3405 | 3610 |
| 18 | 1523 | 2138 | 2624 | 3045 | 3402 | 3726 | 4018 | 4309 | 4568 |
| 20 | 1880 | 2640 | 3240 | 3760 | 4200 | 4600 | 4960 | 5320 | 5640 |
| 22 | 2275 | 3194 | 3920 | 4550 | 5082 | 5566 | 6002 | 6437 | 6824 |
| 24 | 2704 | 3808 | 4672 | 5414 | 6048 | 6624 | 7140 | 7660 | 8120 |
| 30 | 4230 | 5.940 | 7290 | 8460 | 9450 | 10350 | 11160 | 11970 | 12690 |
| $\left\{\begin{array}{c} \text { Vel. in } \\ \text { ft. per } \\ \text { sec. } \end{array}\right\}$ | $2 \cdot 32$ | $3 \cdot 275$ | $4 \cdot 01$ | $4 \cdot 63$ | $5 \cdot 18$ | 5.67 | 6.13 | 6:\% | 6.95 |

Table of the Theoretical Discharge of Water by Round apertures of various Diameters, and under different Heads of Water Pressure (continued).

| Diam. in Inches. | Head of Water in Inches. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 10 | 12 | 14 | 16 | 18 | 20 | 22 | 24 |
|  | Discharge in Gallons per Minute. |  |  |  |  |  |  |  |
| 1 | 14.8 | 16.2 | $17 \cdot 6$ | $18 \cdot 8$ | $19 \cdot 9$ | 21 | 22 | 23 |
| 2 | 59.2 | $64 \cdot 8$ | $70 \cdot 4$ | $75 \cdot 2$ | $79 \cdot 6$ | 84 | 88 | 92 |
| 3 | 133 | 146 | 158 | 169 | 179 | 189 | 198 | 207 |
| 4 | 237 | 259 | 281 | 301 | 318 | 336 | 352 | 368 |
| 5 | 370 | 405 | 440 | 470 | 497 | 525 | 550 | 575 |
| 6 | 533 | 583 | 663 | 677 | 716 | 756 | 792 | 828 |
| 7 | 725 | 794 | 862 | 921 | 975 | 1029 | 1078 | 1127 |
| 8 | 947 | 1037 | 1126 | 1203 | 1273 | 1344 | 1408 | 1472 |
| 9 | 1199 | 1312 | 1425 | 1523 | 1612 | 1701 | 1782 | 1863 |
| 10 | 1480 | 1620 | 1760 | 1880 | 1990 | 2100 | 2200 | 2300 |
| 12 | 2134 | 2333 | 2534 | 2707 | 2865 | 3024 | 3170 | 3312 |
| 14 | 2!01 | 3175 | 3450 | 3684 | 3900 | 4116 | 4312 | 4508 |
| 16 | 3789 | 4147 | 4506 | 4813 | 5094 | 5376 | 5632 | 5888 |
| 18 | 4795 | 5249 | 5702 | 6091 | 6447 | 6804 | 7128 | 7452 |
| 20 | 5920 | 6480 | 7040 | 7520 | 7960 | 8400 | 8800 | 9200 |
| 22 | 7163 | 7841 | 8518 | 9099 | 9632 | 10164 | 10648 | 11132 |
| 24 | 8536 | 9332 | 10136 | 10829 | 11460 | 12096 | 12680 | 13248 |
| 30 | 13320 | 14580 | 15840 | 16920 | 17910 | 18900 | 19800 | 20700 |
| $\left.\begin{array}{l}\text { Vel. in } \\ \text { ft. per } \\ \text { sec. }\end{array}\right\}$ | $7 \cdot 32$ | $8 \cdot 03$ | $8 \cdot 67$ | $9 \cdot 27$ | $9 \cdot 83$ | $10 \cdot 36$ | 10.87 | $11 \cdot 35$ |

Example.-Find the theoretical discharge, through an aperture $8^{\prime \prime}$ in diameter, under a head of $18^{\prime \prime}$. Aus. 1273 gallons per minute.

Discharge through an Orifice in a Thin Plate. -The stream contracts at a distance from the plate of half the diameter of the orifice, and its diameter is 0.784 , that of the orifice being 1.

$$
\begin{aligned}
& \mathrm{G}=\sqrt{\mathrm{H}} \times d^{2} \times 10 \\
& \mathrm{H}=\left(\frac{\mathrm{G}}{d^{2} \times 10}\right)^{2} \\
& d=\left(\frac{\mathrm{G}}{\sqrt{\mathrm{H}} \times 10}\right)^{\frac{1}{2}}
\end{aligned}
$$

Discharge by Short Tubes when not less than twice the diameter of the orifice gives a greater discharge than thin plates. Used for calculating the miner's inch.

$$
\begin{aligned}
& \mathrm{G}=\sqrt{\mathrm{H} \times d^{2} \times 13} \\
& \mathrm{H}=\left(\frac{\mathrm{G}}{d^{2} \times 13}\right)^{2} \\
& d=\left(\frac{\mathrm{G}}{\sqrt{\mathrm{H}} \times 13}\right)^{\frac{1}{2}}
\end{aligned}
$$

Friction of Long Pipes.- To cailculate the loss of head by friction :-

Let $d=$ diameter of pipe in inches. $\mathrm{L}=$ length of pipe in yards. $H=$ head of water in feet. $G=$ gallons per minute.

$$
\begin{aligned}
& \mathrm{G}=\left(\frac{(3 d)^{5} \times \mathrm{H}}{\mathrm{~L}}\right)^{\frac{1}{2}} . \\
& \mathrm{H}=\frac{\mathrm{G}^{2} \times \mathrm{L}}{(3 d)^{5}} \\
& d=\left(\frac{\mathrm{G}^{2} \times \mathrm{L}}{\mathrm{H}}\right)^{\frac{1}{5}} \div 3 \\
& \mathrm{~L}=\frac{(3 d)^{5} \times \mathrm{H}}{\mathrm{G}^{2}}
\end{aligned}
$$

Loss of Head by Bends.-Let $\mathrm{H}=$ head due to change of direction in inches. $r=$ radins of the bore of the pipe in inches. $\mathrm{R}=$ radius of the centre line of the bend, in inches. $\phi=$ angle of bend in degrees. $V=$ velocity of discharge in feet per second.

$$
\begin{aligned}
\mathrm{H} & =\left\{0.131+\left(1.847 \times\left(\frac{r}{\mathrm{R}}\right)^{\frac{7}{2}}\right\} \times \frac{\mathrm{V}^{2} \times \phi}{960}\right. \\
\mathrm{V}^{2} & =\frac{960 \times \mathrm{H}}{\phi \times\left\{0.131+\left(1.847 \times\left(\frac{r}{\mathrm{R}}\right)^{\frac{7}{2}}\right\}\right.}
\end{aligned}
$$

TABLE OF THE ACTUAI DISCHARGE BY SHORT TUBES OF VARIOUS DIAMETERS, WITH SQUARE OF THE
Head of Water in Inches.

|  | 8 | 9 | 10 | 12 | 14 | 16 | 18 | 20 | 22 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 24 |  |  |  |  |  |  |  |  |  |

Discharge in Gallons per Minute.













 E.
$\vdots$
$\vdots$






TABLE FOR QUICK BENDS.

| Diam. of the Pipe in Inches. | Radius of Centre Line of Bend in Inches. | Head of Water in Inches Lost by One Bend of $90^{\circ}$. |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\frac{1}{8}$ | $\frac{1}{4}$ | $\frac{1}{2}$ | $\frac{3}{4}$ | 1 | - $1 \frac{1}{2}$ | 2 | 3 | 4 | 5 | 6 | 9 | 12 | 18 | 24 |
|  |  | Gallons Discharged per Minute. |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 2 | 3 | 23 | 32 | 46 | 56 | 65 | 79 | 92 | 112 | 130 | 145 | 159 | 195 | 214 | 276 | 318 |
| 3 | $3 \frac{1}{2}$ | 44 | 63 | 89 | 109 | 126 | 154 | 178 | 218 | 252 | 282 | 309 | 378 | 436 | 534 | 618 |
| 4 | 4 | 69 | 98 | 139 | 170 | 197 | 241 | 278 | 341 | 394 | 440 | 480 | 591 | 682 | 834 | 966 |
| 5 | $4 \frac{1}{2}$ | 96 | 136 | 172 | 236 | 272 | 333 | 38.5 | 472 | 544 | 608 | 666 | 816 | 944 | 1155 | 1332 |
| 6 | 5 | 128 | 181 | 256 | 314 | 362 | 443 | 512 | 629 | 724 | 809 | 886 | 1086 | 1258 | 1536 | 1774 |
| 7 | $5 \frac{1}{2}$ | 161 | 229 | 322 | 396 | 458 | 561 | 64.5 | 793 | 917 | 1024 | 1122 | 1374 | 1586 | 1935 | 2244 |
| 8 | 6 | 199 | 281 | 398 | 487 | 563 | 689 | 796 | 975 | 1126 | 1259 | 1379 | 1689 | 1950 | 2388 | 2758 |

Example.-A 6 -inch pipe with a bend having a radius of 18 inches, which discharges 1,607 gallons
per minute, consumes 6 inches of head.
Example.-A 6-inch pipe with a bend having a radius of 5 inches, which discharges 1,536 gallons per minute, consumes 18 inches of head.
The above table, although arranged for quarter bends or angles of $90^{\circ}$, is applicable to any other
angle, the radius being the same, as the head is proportional to the angle; thus, a half quarter bend,
i.e., angle of $45^{\circ}$, consumes half the head of a bend of $90^{\circ}$, and a bend of $180^{\circ}$ takes double, \&c.

Table of the Discharge of Pipes by Prony's Formula.

| $\frac{\mathrm{H} \times d}{\mathrm{~L}}$. | Velocity in Feet per Second. | Diameter of the Pipe in Inches. |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1 | $1 \frac{1}{2}$ | 2 | $2 \frac{1}{2}$ | 3 | $3 \frac{1}{2}$ | 4 |
|  |  | Gallons Discharged per Minute. |  |  |  |  |  |  |
| -00002402 | . 025 | -0511 | -1150 | - 2045 | -3196 | -4602 | - 6260 | -8180 |
| $\cdot 00005437$ | -05 | -1022 | -2301 | -4091 | -6392 | -9204 | $1 \cdot 252$ | $1 \cdot 636$ |
| -00009108 | $\cdot 075$ | -1534 | -3450 | -6136 | -9588 | $1 \cdot 381$ | 1.878 | $2 \cdot 454$ |
| -0001341 | -100 | - 2045 | $\cdot 4602$ | ${ }^{-8182}$ | 1.278 | 1.841 | $2 \cdot 504$ $3 \cdot 130$ | 3.273 4.090 |
| -0001836 | -125 | -2556 | $\cdot 5750$ | $1 \cdot 023$ | 1.598 | $2 \cdot 301$ | 3•130 | $4 \cdot 090$ |
| -0002394 | $\cdot 15$ | -3067 | - 6900 | 1-227 | 1.917 | $2 \cdot 761$ | $3 \cdot 756$ | 4-908 |
| -0003016 | $\cdot 175$ | - 3578 | -8053 | 1.432 | $2 \cdot 237$ | $3 \cdot 221$ | 4.382 | $5 \cdot 728$ |
| -0003702 | $\cdot 2$ | -4090 | -9204 | $1 \cdot 636$ | $2 \cdot 557$ | $3 \cdot 682$ | $5 \cdot 008$ | $6 \cdot 546$ |
| -0004452 | -225 | -4601 | $1 \cdot 035$ | 1.841 | $2 \cdot 876$ | $4 \cdot 142$ | $5 \cdot 634$ | $7 \cdot 363$ |
| -0005266 | -25 | -5112 | $1 \cdot 150$ | $2 \cdot 045$ | 3•196 | $4 \cdot 602$ | 6.260 | $8 \cdot 180$ |
| -0006140 | -275 | -5624 | $1 \cdot 265$ | $2 \cdot 250$ | $3 \cdot 515$ | $5 \cdot 062$ | 6.886 | 9.000 |
| -0007080 | $\cdot 3$ | -6135 | 1-381 | $2 \cdot 454$ | 3.835 | $5 \cdot 522$ | $7 \cdot 512$ | $9 \cdot 819$ |
| -0008087 | -325 | $\cdot 6646$ | $1 \cdot 496$ | $2 \cdot 659$ | $4 \cdot 154$ | 5.982 | $8 \cdot 138$ | $10 \cdot 64$ |
| -0009154 | -35 | $\cdot 7157$ | $1 \cdot 611$ | 2.864 | $4 \cdot 474$ | 6.443 | 8.764 | 11.46 |
| -0010286 | $\cdot 375$ | $\cdot 7669$ | $1 \cdot 726$ | $3 \cdot 068$ | 4.794 | 6.903 | 9-390 | 12.27 |
| -0011480 | $\bullet 4$ | -8180 | $1 \cdot 841$ | 3.273 | $5 \cdot 113$ | $7 \cdot 363$ | $10 \cdot 02$ | 13.09 |
| -001274 | -425 | -8691 | $1 \cdot 955$ | $3 \cdot 477$ | $5 \cdot 433$ | $7 \cdot 823$ | $10 \cdot 64$ | 13.91 |
| -001406 | $\cdot 45$ | -9202 | 2.071 | $3 \cdot 682$ | 5.757 | 8.284 | 11.27 | 14.73 |
| -001545 | -475 | -9713 | 2-186 | $3 \cdot 886$ | $6 \cdot 077$ | 8.744 | 11.89 | 15.55 |
| -001690 | $\cdot 5$ | 1.023 | 2-301 | $4 \cdot 091$ | 6.392 | 9-204 | 12.52 | $16 \cdot 37$ |
| -002 | $\cdot 55$ | $1 \cdot 125$ | $2 \cdot 531$ | $4 \cdot 500$ | $7 \cdot 031$ | $10 \cdot 12$ | $13 \cdot 77$ | 18.00 |
| -00233 | -6 | 1.227 | $2 \cdot 761$ | $4 \cdot 909$ | $7 \cdot 670$ | $11 \cdot 04$ | 15.02 | $19 \cdot 64$ |
| -002693 | $\cdot 65$ | 1.329 | $2 \cdot 991$ | 5.318 | $8 \cdot 309$ | 11.96 | 16.28 | $21 \cdot 27$ |
| -003079 | $\cdot 7$ | $1 \cdot 431$ | $3 \cdot 221$ | $5 \cdot 727$ | $8 \cdot 948$ | $12 \cdot 88$ | $17 \cdot 53$ | $22 \cdot 91$ |
| -003490 | $\cdot 75$ | 1.533 | $3 \cdot 450$ | 6•136 | $9 \cdot 588$ | $13 \cdot 81$ | 18.78 | $24 \cdot 54$ |
| -003926 | -8 | 1.636 | 3.682 | $6 \cdot 544$ | 10.23 | 14.73 | 20.03 | 26•18 |
| -004388 | -85 | 1.738 | $3 \cdot 912$ | 6.954 | 10.86 | $15 \cdot 65$ | 21.29 | $27 \cdot 82$ |
| -004876 | $\cdot 9$ | 1.841 | $4 \cdot 142$ | 7-363 | $11 \cdot 51$ | $16 \cdot 57$ | 22.53 | $29 * 46$ |
| -005928 | 1.0 | $2 \cdot 045$ | $4 \cdot 602$ | $8 \cdot 182$ | $12 \cdot 78$ | 18.41 | $25 \cdot 04$ | $32 \cdot 73$ |
| -00648 | $1 \cdot 05$ | $2 \cdot 147$ | 4.832 | $8 \cdot 591$ | $13 \cdot 42$ | $19 \cdot 33$ | $26 \cdot 29$ | 34.37 |
| -00708 | $1 \cdot 1$ | 2-249 | $5 \cdot 062$ | 9.000 | 14.06 | $20 \cdot 25$ | 27.54 | 36.00 |
| -007091 | $1 \cdot 15$ | $2 \cdot 351$ | $5 \cdot 292$ | $9 \cdot 409$ | 14.70 | $21 \cdot 15$ | $28 \cdot 80$ | $37 \cdot 64$ |
| -008338 | $1 \cdot 2$ | $2 \cdot 454$ | $5 \cdot 522$ | 9.818 | 15.34 | 22.09 | $30 \cdot 05$ | 39.28 |
| -009 | $1 \cdot 25$ | $2 \cdot 556$ | $5 \cdot 753$ | 10-23 | $15 \cdot 98$ | 23.01 | 31.30 | $40 \cdot 91$ |
| -009694 | $1 \cdot 3$ | $2 \cdot 658$ | $5 \cdot 983$ | 10.64 | $16 \cdot 62$ | 23.93 | $32 \cdot 55$ | $42 \cdot 55$ |
| -010407 | 135 | $2 \cdot 761$ | 6.213 | 11.04 | 17.26 | $24 \cdot 85$ | 33.80 | 44-18 |
| -01115 | $1 \cdot 4$ | $2 \cdot 863$ | $6 \cdot 443$ | $11 \cdot 45$ | $17 \cdot 90$ | $25 \cdot 77$ | $35 \cdot 06$ | $45 \cdot 82$ |
| -01192 | $1 \cdot 45$ | $2 \cdot 965$ | $6 \cdot 673$ | 11.86 | 18.53 | $26 \cdot 69$ | $36 \cdot 31$ | $47 \cdot 46$ |
| $\cdot 0127$ | 1.5 | 3.067 | 6.900 | 12-27 | $19 \cdot 18$ | $27 \cdot 61$ | 37.56 | 49.08 |

## Table of the Discharge of Pipes by Prony's Formula (continued).

| $\frac{\mathrm{H} \times d}{\mathrm{~L}} .$ | Velocity in Feet Second. | Diameter of the Pipe in Inches. |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 5 | 6 | 7 | 8 | 9 | 10 | 12 |
|  |  | Gallons Discharged per Minute. |  |  |  |  |  |  |
| -00002402 | . 025 | 1-278 | 1.841 | $2 \cdot 504$ | 3-272 | 4-142 | $5 \cdot 113$ | $7 \cdot 362$ |
| -00005437 | -05 | $2 \cdot 556$ | $3 \cdot 682$ | 5.008 | 6.544 | $8 \cdot 284$ | $10 \cdot 23$ | $14 \cdot 72$ |
| -000091108 | . 075 | $3 \cdot 834$ | $5 \cdot 523$ | $7 \cdot 512$ | ${ }^{9} 818$ | $12 \cdot 43$ | 15.34 | 22.09 29.45 |
| -0001341 | $\cdot 100$ | $5 \cdot 113$ | 7.363 | 10.02 | 13.09 | 16.57 | 20.45 | ${ }^{29 \cdot 45}$ |
| -0001836 | -125 | 6.390 | $9 \cdot 205$ | $12 \cdot 52$ | 16.36 | $20 \cdot 71$ | $25 \cdot 57$ | 36.81 |
| -0002394 | 15 | $7 \cdot 668$ | 11.05 | 15.02 | 19.63 | $24 \cdot 85$ | $30 \cdot 67$ | $44 \cdot 17$ |
| -0003016 | $\cdot 175$ | $8 \cdot 947$ | 12.88 | 17.53 | $22 \cdot 95$ | 28.99 | 35.79 | $51 \cdot 53$ |
| -0003702 | ${ }^{2}$ | 10.23 | 14.73 | 20.03 | $26 \cdot 18$ | ${ }_{33} \cdot 13$ | $40 \cdot 91$ | 58.90 |
| -0004452 | -225 | $11 \cdot 50$ | 16.57 | $22 \cdot 54$ | $29 \cdot 45$ | $37 \cdot 28$ | 46.02 | $66 \% 6$ |
| -0005266 | -25 | 12.78 | $18 \cdot 41$ | 25.04 | $32 \cdot 72$ | $41 \cdot 42$ | $51 \cdot 13$ | $73 \cdot 62$ |
| -0006140 | ${ }^{2} 75$ | 14.06 | 20.25 | $27 \cdot 54$ | 36.00 | $45 \cdot 56$ | 56.25 | 80.98 |
| -0007080 | -3 | 15.34 | 22.09 | 30.05 | $39 \cdot 27$ | 49.70 | $61 \cdot 36$ | 88.35 |
| .0008087 | - 325 | $16 \cdot 62$ | $23 \cdot 93$ | 32.55 | $42 \cdot 54$ | 53.84 | 66.46 | 95.71 |
| -0009154 | 35 | 17.89 | 25.77 | 35.06 | 45.81 | 57.98 | 71.59 | $103 \cdot 1$ |
| -0010286 | -375 | $19 \cdot 17$ | 27.61 | 37.56 | 49.08 | $62 \cdot 13$ | 76.69 | $110 \cdot 4$ |
| $\cdot 0011480$ | 4 | $20 \cdot 45$ | $29 \cdot 45$ | $40 \cdot 06$ | 52.36 | 66.27 | 81.81 | $117 \cdot 8$ |
| . 001274 | $\cdot 425$ | $21 \cdot 73$ | $31 \times 29$ | $42 \cdot 57$ | 55.63 | $70 \cdot 41$ | 86.94 | 125-2 |
| -001406 | 45 | 23.01 | $33 \cdot 13$ | 45.07 | 58.90 | 74.55 | 92.03 | $132 \cdot 5$ |
| $\cdot 001545$ | $\cdot 475$ | 24.29 | 34.97 | 47.58 | 62.17 | 78.70 | $97 \cdot 14$ | $139 \cdot 8$ |
| -001690 | ${ }^{5}$ | 25.57 | 36.82 | 50.08 | 65.45 | $82 \cdot 83$ | 102•3 | $147 \times 2$ |
| -002 | $\cdot 55$ | $28 \cdot 12$ | $40 \cdot 50$ | 55.09 | 72.00 | $91 \cdot 12$ | 112.5 | 162.0 |
| -00233 | - |  |  |  | 78.54 | 99-40 |  | 1767 |
| -002693 | $\bullet 65$ | 33.23 | 47.86 | 65.10 | 85.08 | $107 \cdot 7$ | $132 \cdot 9$ | $191 \cdot 4$ |
| -003079 | $\stackrel{7}{7}$ | 35.79 | 51.54 | 70.11 | ${ }^{91} \cdot 63$ | 116.0 | $143 \cdot 2$ | $206 \cdot 1$ |
| -003490 | 75 | $38 \cdot 34$ | 55.23 | $75 \cdot 12$ | 98.16 | $124 \cdot 3$ | $153 \cdot 4$ | $220 \cdot 9$ |
| -003926 | 8 | 40.90 | 58.90 | 80.13 | 104.7 | 132.5 | 163.6 | $235 \cdot 6$ |
| -004388 | 85 | $43 \cdot 46$ | $62 \cdot 59$ | 85.14 | 111.3 | $140 \cdot 8$ | 173.8 | $250 \cdot 3$ |
| -004876 | $\cdot 9$ | 46.02 | 66.27 | $90 \cdot 14$ | 1178 | 149-1 | 184-2 | $265 \cdot 1$ |
| . 005928 | 1.0 | $51 \cdot 13$ | $73 \cdot 63$ | $100 \cdot 2$ | $130 \cdot 9$ | $165 \cdot 7$ | 204.5 | 294.5 |
| -00648 | 1.05 | $53 \cdot 69$ | $77 \cdot 31$ | 105.2 | 137.4 | 174.0 | 214.7 | 309.2 |
| -00708 | $1 \cdot 1$ | 56.24 | 80.99 | $110 \cdot 2$ | 144.0 | 182.2 | 224.9 | 324.0 |
| -007691 | $1 \cdot 15$ | $58 \cdot 80$ | $84 \cdot 67$ | 115-2 | $150 \cdot 5$ | $190 \cdot 5$ | 235-2 | $338 \cdot 7$ |
| $\cdot 008338$ | 1.2 | $61 \cdot 36$ | 88.36 | $120 \cdot 2$ | $157 \cdot 1$ | 198.8 | $245 \cdot 4$ | 353•4 |
| ${ }^{\cdot 009}{ }_{-00969}$ | $1 \cdot 25$ | $63 \cdot 91$ | ${ }_{9}^{92} \cdot 04$ | $125 \cdot 2$ | 163.6 | $207 \cdot 1$ | $255 \cdot 7$ | ${ }^{368.1}$ |
| $\cdot 009694$ | 13 | $66 \cdot 47$ | 95.72 | $130 \cdot 2$ | 170.2 | $215 \cdot 4$ | $265 \cdot 9$ | 382.8 |
| $\cdot 010407$ | 1.35 | 69.02 | 99.40 | $135 \cdot 2$ | $176 \cdot 7$ | 223.6 | 276.1 | $397 \cdot 6$ |
| ${ }^{-01115}$ | 1.4 | 71.58 | $103 \cdot 1$ | $140 \cdot 2$ | 183.3 | ${ }^{231 \cdot 9}$ | 286 | 412.3 |
| -01192 | $1 \cdot 45$ | $74 \cdot 14$ | 106.8 | 145.2 | $189 \cdot \mathrm{~S}$ | $240 \cdot 2$ | 296.6 | 427.0 |
| -0127 | 1.5 | 76.68 | $110 \cdot 5$ | $150 \cdot 2$ | $196 \cdot 3$ | 248.5 | 306.8 | $441 \cdot \%$ |

## Table of the Discharge of Pipes by Prony's Formula (continued).

| $\frac{\mathrm{H} \times d}{\mathrm{~L}}$. | Velocity in Feet per Second. | Diameter of the Pipe in Inches. |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 14 | 15 | 16 | 18 | 20 | 21 | 24 |
|  |  | Gallons Discharged per Minute. |  |  |  |  |  |  |
| -00002402 | -025 | 10.02 | $11 \cdot 50$ | 13.09 | 16.56 | $20 \cdot 45$ | 22.53 | $29 \cdot 45$ |
| $\cdot 00005437$ | -05 | 20.03 | 23.00 | $26 \cdot 18$ | $33 \cdot 12$ | $40 \cdot 91$ | $45 \cdot 07$ | 58.90 |
| -00009108 | $\cdot 075$ | 30.05 | $34 \cdot 50$ | $39 \cdot 27$ | $49 \cdot 68$ | $61 \cdot 36$ | $67 \cdot 61$ | 88.35 |
| -0001341 | -100 | 40.06 | 46.02 | $52 \cdot 36$ | 66.23 | $81 \cdot 81$ | $90 \cdot 14$ | 117.8 |
| -0001836 | -125 | 50.08 | $57 \cdot 50$ | $65 \cdot 45$ | $82 \cdot 80$ | $102 \cdot 3$ | $112 \cdot 7$ | $147 \cdot 3$ |
| -0002394 | $\cdot 15$ | $60 \cdot 10$ | 69.00 | 78.54 | $99 \cdot 36$ | $122 \cdot 7$ | 135.2 | $176 \cdot 7$ |
| -0003016 | $\cdot 175$ | $70 \cdot 11$ | $80 \cdot 54$ | $91 \cdot 63$ | $115 \cdot 9$ | $143 \cdot 2$ | 157.7 | $206 \cdot 1$ |
| -0003702 | $\cdot 2$ | 80.13 | 92.04 | 1047 | $132 \cdot 5$ | $163 \cdot 6$ | $180 \cdot 3$ | 235.6 |
| -0004452 | $\cdot 225$ | $90 \cdot 14$ | 103.5 | 117.8 | $149{ }^{\circ} 0$ | $184 \cdot 1$ | $202 \cdot 8$ | $265 \cdot 1$ |
| $\cdot 0005266$ | -25 | 100.2 | 115.0 | $130 \cdot 9$ | $165 \cdot 6$ | $204 \cdot 5$ | $225 \cdot 3$ | 294.5 |
| -0006140 | $\cdot 275$ | $110 \cdot 2$ | 126.5 | 144.0 | $182 \cdot 1$ | 225.0 | $247 \cdot 9$ | $323 \cdot 9$ |
| -0007080 | $\cdot 3$ | $120 \cdot 2$ | $138 \cdot 1$ | $157 \cdot 1$ | $198 \cdot 7$ | $245 \cdot 4$ | $270 \cdot 4$ | 353.4 |
| -0008087 | -325 | $130 \cdot 2$ | 149.6 | $170 \cdot 2$ | $215 \cdot 2$ | 265.9 | 293.0 | 382.8 |
| -0009154 | -35 | $140 \cdot 2$ | $161 \cdot 1$ | $183 \cdot 3$ | 231.8 | 286.4 | $315 \cdot 5$ | $412 \cdot 3$ |
| -0010286 | $\cdot 375$ | $150 \cdot 2$ | $172 \cdot 6$ | $196 \cdot 4$ | $248 \cdot 4$ | 306.8 | 338.0 | $441 \cdot 7$ |
| -0011480 | $\cdot 4$ | $160 \cdot 2$ | 184.1 | $209 \cdot 4$ | $264 \cdot 9$ | 327 - 2 | $360 \cdot 6$ | 471.2 |
| -001274 | -425 | $170 \cdot 3$ | $195 \cdot 6$ | $222 \cdot 5$ | $281 \cdot 5$ | $347 \cdot 7$ | $383 \cdot 1$ | $500 \cdot 6$ |
| $\cdot 001406$ | -45 | $180 \cdot 3$ | $207 \cdot 1$ | $235 \cdot 6$ | 298.0 | 368.2 | $405 \cdot 6$ | $530 \cdot 1$ |
| -001545 | -475 | $190 \cdot 3$ | $218 \cdot 6$ | $248 \cdot 7$ | 314.6 | $388 \cdot 6$ | $428 \cdot 2$ | $559 \cdot 5$ |
| -001690 | $\cdot 5$ | $200 \cdot 3$ | $230 \cdot 1$ | $261 \cdot 8$ | $331 \cdot 1$ | $409 \cdot 1$ | $450 \cdot 7$ | 589.0 |
| -002 | -55 | $220 \cdot 3$ | $253 \cdot 0$ | 288.0 | $364 \cdot 3$ | $450 \cdot 0$ | $495 \cdot 8$ | 647.9 |
| -00233 | -6 | $240 \cdot 4$ | $276 \cdot 1$ | 314.2 | $397 \cdot 4$ | $490 \cdot 9$ | $540 \cdot 8$ | $706 \cdot 8$ |
| -002693 | -65 | $260 \cdot 4$ | $299 \cdot 1$ | $340 \cdot 3$ | $430 \cdot 5$ | $531 \cdot 8$ | $585 \cdot 9$ | $765 \cdot 7$ |
| -003079 | $\cdot 7$ | $280 \cdot 5$ | $322 \cdot 1$ | 366.5 | $463 \cdot 6$ | $572 \cdot 7$ | 631.0 | 824.6 |
| -003490 | $\cdot 75$ | $300 \cdot 5$ | 345.0 | $392 \cdot 7$ | 496.8 | $613 \cdot 6$ | 676.0 | 883.5 |
| -003926 | -8 | $320 \cdot 5$ | 368.2 | $418 \cdot 9$ | $529 \cdot 8$ | $654 \cdot 5$ | $721 \cdot 1$ | $942 \cdot 4$ |
| -004388 | -85 | $340 \cdot 5$ | 391.2 | $445 \cdot 1$ | $563 \cdot 0$ | $695 \cdot 4$ | 766.2 | 1001 |
| -004876 | $\cdot 9$ | $360 \cdot 6$ | 414.2 | 471.2 | $596 \cdot 1$ | $736 \cdot 3$ | 811.3 | 1060 |
| -005928 | $1 \cdot 0$ | $400 \cdot 6$ | $460 \cdot 0$ | $523 \cdot 6$ | $662 \cdot 3$ | $818 \cdot 1$ | $901 \cdot 4$ | 1178 |
| -00648 | $1 \cdot 05$ | $420 \cdot 6$ | 483.0 | $549 \cdot 8$ | 695.4 | 859.0 | $946 \cdot 5$ | 1237 |
| - 00708 | $1 \cdot 1$ | $440 \cdot 6$ | $506 \cdot 0$ | 576.0 | 728.5 | $900 \cdot 0$ | 991.6 | 1296 |
| . 007691 | $1 \cdot 15$ | $460 \cdot 7$ | 529.0 | $602 \cdot 1$ | 761.6 | $940 \cdot 9$ | 1037 | 1355 |
| -008338 | $1 \cdot 2$ | $480 \cdot 7$ | $552 \cdot 2$ | $628 \cdot 3$ | 794.8 | $981 \cdot 9$ | 1082 | 1414 |
| -009 | $1 \cdot 25$ | $500 \cdot 8$ | $575 \cdot 2$ | $654 \cdot 5$ | 827.9 | 1023 | 1127 | 1472 |
| -009694 | $1 \cdot 3$ | $520 \cdot 8$ | 598.2 | $680 \cdot 7$ | 861.0 | 1064 | 1172 | 1531 |
| -010407 | $1 \cdot 35$ | $540 \cdot 8$ | $621 \cdot 3$ | 706.9 | $894 \cdot 1$ | 1104 | 1217 | 1590 |
| -01115 | $1 \cdot 4$ | $560 \cdot 9$ | $644 \cdot 3$ | 733.0 | $927 \cdot 2$ | 1145 | 1262 | 1649 |
| -01192 | $1 \cdot 45$ | 580.9 | $667 \cdot 3$ | 759.2 | $960 \cdot 3$ | 1186 | 1307 | 1708 |
| $\cdot 0127$ | 1.5 | 601.0 | 690.0 | $785 \cdot 4$ | 993.6 | 1227 | 1352 | 1767 |

Effect of Contour of Section.-The hydraulic mean gradient corresponds to a straight line drawn between the points of entry and exit of a pipe. No loss of effect will arise from the pipe following the section of the ground, so long as the contour of the pipe does not anywhere along the line rise above the hydraulic mean gradient. Where it is necessary to conduct water over a hill above the hydraulic mean gradient, but below the top of the pipe, the first section of piping, having a low head, must be of a greater diameter than the subsequent section, which has a greater head.

General Laws for Pipes. - When the diameter and length are constant, the discharge varies directly as the square root of the head. Conversely, the head is directly as the square of the discharge.

When the head and length are constant, the discharge is directly as the 2.5 power of the diameter. Conversely, the diameter will vary directly as the 2.5 root of the discharge.

When the discharge and length are constant, the head will be inversely as the 5 th power of the diameter. Conversely, the diameter will be inversely as the 5th root of the head.

When the head and diameter are constant, the discharge will be inversely as the square root of the length. Conversely, the length varies inversely as the square of the discharge.

When discharge and diameter are constant, the head is directly and simply as the length.

Head for very Low Velocities.-Prony's Rule. Let $d=$ diameter of the pipe inches. $\mathrm{H}=$ head of water in inches. $L=$ length of pipe in feet. $G=$ gallons per minute.

$$
\begin{aligned}
& \left.\mathrm{G}=\left(16.353 \times \frac{\mathrm{H} \times d}{\mathrm{~L}}+0.00665\right)^{\frac{1}{2}}-0.0816\right) \times d^{2} \times 2.04 . \\
& \mathrm{H}=\frac{\left.\left(\frac{\mathrm{G}}{2.04 \times d^{2}}+0.0816\right)^{2}-0.00665\right) \times \frac{\mathrm{L}}{d}}{16.353}
\end{aligned}
$$

Head due to Velocity in Open Channels.-When a stream leaves a reservoir by a channel the bottom of which is level with that of the reservoir, and its entrance is well rounded, the velocity is 0.96 of that due to gravity; but if the sides of the inlet opening are square, the velocity will be 0.86 of that due to gravity. With an opening in a sluice gate of small thickness, the head of water being above the lower edge of the
gate, the velocity is only 0.635 of that due to gravity. In the case of a weir, the contraction occurring on three sides only, the co-efficient rises to 0.667 .

Table of the Velocities in Feet per Second due to given Heads. (Box.)

| $\begin{array}{\|c} \text { Head } \\ \text { in } \\ \text { inches. } \end{array}$ | $\begin{array}{\|c\|c} \text { A. } \\ \text { Coef. } \\ 1 & 100 . \end{array}$ | $\begin{gathered} \text { B. } \\ \text { Coef. } \\ 0.96 . \end{gathered}$ | Coef. $0 \cdot 86$. | D. <br> 0.6 . <br> 0.65. | $\begin{gathered} \text { Head } \\ \text { in } \\ \text { Inches. } \end{gathered}$ | $\begin{gathered} \text { A. } \\ \text { Coef. } \\ 1.0 \end{gathered}$ | $\xrightarrow{\mathrm{B} .}$ 0.96 . | $\begin{gathered} \text { C. } \\ \text { Coef. } \\ 0.86 . \end{gathered}$ | $\begin{gathered} \text { D. } \\ \text { Cof. } \\ 0 \cdot 635 . \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | -29 | -2784 | -2494 | $\cdot 18415$ |  | $2 \cdot 317$ | 2-2224 | 30 | $1 \cdot 4713$ |
|  | . 41 | -39 | -3524 | - 2603 | 1 | $2 \cdot 590$ | 2.4864 | $2 \cdot 2270$ | 1.6446 |
|  | . 58 | $\stackrel{556}{ } \cdot 78$ | . 4985 | - 5268 | 11 | ${ }_{3} \cdot 8.065$ | ${ }_{2 \cdot}^{2 \cdot 7424}$ | ${ }_{2 \cdot 6360}$ | ${ }_{1}^{1.8016}$ |
|  | 1.0 | -9600 | 8600 | - 635 | 2 | $3 \cdot 27$ | $3 \cdot 14$ | $2 \cdot 8174$ | 2.0803 |
|  | 1.158 | \|1-1117 | -9959 | $\cdot 7353$ | 21 | 3.475 | $3 \cdot 336$ | 2.9885 | $2 \cdot 2066$ |
|  | $1 \cdot 295$ | $1 \cdot 2432$ | $1 \cdot 1140$ | -8223 |  | $3 \cdot 663$ | $3 \cdot 516$ | $3 \cdot 1502$ | $2 \cdot 3260$ |
|  | $1 \cdot 418$ | $1 \cdot 3613$ | $1 \cdot 2195$ | -9004 | 2 | 3.842 | 3.688 | 3.3041 | $2 \cdot 4397$ |
|  | $1 \cdot 532$ | $1-4707$ | $1 \cdot 3175$ | $\cdot 9728$ | 3 | 4.012 | $3 \cdot 851$ | $3 \cdot 4503$ | $2 \cdot 5476$ |
|  | $1 \cdot 638$ | 1.5725 | $1 \cdot 4087$ | 1.0401 | 3 | $4 \cdot 176$ | $4 \cdot 009$ | 3.5914 | $2 \cdot 6517$ |
|  | $1 \cdot 737$ | 1.6675 | $1 \cdot 4938$ | 1.1030 |  | 4.334 | $4 \cdot 161$ 4.306 | 3.7272 3.850 | ${ }^{2} 77521$ |
|  | 1.831 1.921 | ${ }_{1}^{1.8442}$ | ${ }_{1} 1.6547$ | 1.1627 1.2198 | ${ }_{4}^{3}$ | ${ }_{4}^{4 \cdot 486}$ | $4 \cdot 306$ $4 \cdot 448$ | 3.8580 | 2.8486 |
|  | 2.006 | 1.9258 | $1 \cdot 725$ | $1 \cdot 2738$ | 2 | $4 \cdot 914$ | $4 \cdot 717$ | 4-2260 | 3•1204 |
|  | 2.088 | 2.0045 | ${ }^{1} 796$ | 1-3259 |  | 5.180 | 4.973 | $4 \cdot 455$ | $3 \cdot 2893$ |
|  | $2 \cdot 167$ | 2.0803 | $1 \cdot 863$ | $1 \cdot 376$ |  | $5 \cdot 433$ | 5-216 | $4 \cdot 672$ | $3 \cdot 450$ |
|  | $2 \cdot 243$ | $2 \cdot 1533$ | $1 \cdot 929$ | $1 \cdot 424$ | 6 | $5 \cdot 675$ | $5 \cdot 4$ | $4 \cdot 881$ | $3 \cdot 6036$ |

Discharge of Water Courses. Find the maximum central surface velocity by means of a float, take $84 \%$ of this for the mean velocity throughout the section, multiply this by the sectional area for the discharge per cubic foot.

Head to overcome Friction of Channel. Let $\mathrm{L}=$ length of channel in yards. $A=$ cross sectional area of the stream in square feet. $P=$ the perimeter, or wetted border in feet. $F=$ the fall, or difference of level at the two ends of the channel in inches. $\mathrm{C}=$ cubic feet discharged per minute.

$$
\mathrm{F}=\frac{\left(\frac{\mathrm{C}}{\mathrm{~A}}\right)^{2} \times \mathrm{L} \times \mathrm{P}}{874520 \times \mathrm{A}} ; \quad \mathrm{C}=\left(\frac{874520 \times \mathrm{F} \times \mathrm{A}}{\mathrm{~L} \times \mathrm{P}}\right)^{\frac{1}{2}} \times \Lambda
$$

Submerged Openings.-The velocity of discharge through a submerged opening is governed by the difference of the level of water at the two sides of it, or by the head, and is not affected by the depth below the surface at which it is placed.

Head for Low Velocities.
Let $\mathrm{V}=$ mean velocity over the whole area in feet per second.

$$
\begin{aligned}
& R=\text { the hydraulic radius in feet, or } \frac{\text { area in square feet }}{\text { border in feet }} . \\
& S=\text { the slope, or } \frac{\text { fall in inches }}{\text { length in inches. }} \\
& \frac{(V+109)^{2}-0 \cdot 0118858}{8975}=\text { R.S. }
\end{aligned}
$$

To find the VelocityArea of channel in square feet $\times$ fall in inches Border in feet $\times$ length of the channel in inches. find the nearest number thereto in column B of the following Table, and opposite to that number in column $\mathbf{A}$ is the required velocity.

To find the Fall in inches-
$\frac{\text { The given discharge }}{\text { The given area } \times 60}=$ mean velocity in feet per second.
Nearest number to velocity in feet per second in column A $\times$ horder in feet $\times$ length of channel in inches area in square feet.

For the Discharge of Canals, Rivers, etc., by Eytelwein's Rule.

| Mean Velocity in Feet per Second. | R. S. | $\begin{array}{\|l\|} \text { Mean } \\ \text { Velocity in } \\ \text { Feet per } \\ \text { Second. } \end{array}$ | R. S. | Mean <br> Velocity in Feet per Second. | R. S. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| -025 | -0000006734 | $\cdot 375$ | -00002477 | $\cdot 95$ | -0001236 |
| -05 | -000001489 | $\cdot 4$ | -00002753 | $1 \cdot 0$ | -0001357 |
| $\cdot 075$ | -00000244 | -425 | -00003043 | $1 \cdot 1$ | -00016146 |
| $\cdot 1$ | . 000003538 | -45 | -000033484 | $1 \cdot 2$ | -0001895 |
| -125 | -000004771 | $\cdot 475$ | -00003666 | $1 \cdot 3$ | -00021984 |
| $\cdot 15$ | -000006144 | ${ }^{5}$ | -00003998 | $1 \cdot 4$ | -0002524 |
| $\cdot 175$ | -000007656 | -55 | -00004705 | $1 \cdot 5$ | -00028703 |
| $\cdot 2$ | -000009307 | $\cdot 6$ | -00005466 | 1.6 | -00032402 |
| -225 | -0000111 | -65 | -00006284 | 1.7 | -0003632 |
| -25 | -00001303 | $\cdot 7$ | -00007158 | $1 \cdot 8$ | -0004047 |
| -275 | . 00001510 | $\cdot 75$ | -00008087 | $1 \cdot 9$ | -000448 |
| $\cdot 3$ | -00001730 | -8 | -00009072 | $2 \cdot 0$ | -0004943 |
| -325 | -00001966 | -85 | -00010112 | 2.5 | -000757 |
| -35 | -00002214 | $\cdot 9$ | -0001121 | $3 \cdot 0$ | -001075 |
| A. | B. | A. | B. | A. | B. |


| Hydraulic Radius in Feet. |  |  |  |  | Fall | IN |  | and | r Ya |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 15 | 18 |
|  | $\cdot 000568$ | $\cdot 00114$ | -0017 | -00227 | -00284 | .00341 | -00398 | -00454 | -00511 | -00568 | $\cdot 00625$ | $\cdot 00682$ | -00852 | . 01023 |
|  | Mean Velocity throughout the whole Cross Sectional Area, in Feet per Minute. |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $2 \cdot 8$ | $37 \cdot 3$ | $52 \cdot 8$ | $64 \cdot 6$ | $74 \cdot 6$ | $83 \cdot 4$ | 91.4 | 98.7 | 105.5 | 111.9 | 118.0 | $123 \cdot 7$ | $129 \cdot 2$ | 144.4 | 158.3 |
| $3 \cdot 0$ | $38 \cdot 6$ $39 \cdot 9$ | $54 \cdot 6$ | $66 \cdot 9$ | $77 \cdot 2$ | $86 \cdot 3$ | 94.6 | $102 \cdot 2$ | 109.2 | $115 \cdot 8$ | $122 \cdot 1$ | 128.1 | $133 \cdot 7$ | $149 \cdot 5$ | 163.8 |
| $3 \cdot 2$ $3 \cdot 4$ | $39 \cdot 9$ $41 \cdot 1$ | 56.4 | $69 \cdot 1$ | 79.8 | $89 \cdot 2$ | 97.7 $100 \cdot 7$ | $105 \cdot 4$ | 112.8 | 119.6 | 126.0 | $132 \cdot 2$ | 138.1 | $154 \cdot 4$ | 169.2 |
| $3 \cdot 4$ 3.6 | $41 \cdot 1$ | $58 \cdot 1$ 59.8 | $71 \cdot 2$ | $82 \cdot 2$ | $91 \cdot 9$ | $100 \cdot 7$ | $108 \cdot 7$ | 116.2 | $123 \cdot 3$ | $130 \cdot 0$ | 136.3 | 142.4 | $159 \cdot 2$ | $174 \cdot 4$ |
| $3 \cdot 6$ $3 \cdot 8$ | $42 \cdot 3$ $43 \cdot 5$ | $59 \cdot 8$ | $73 \cdot 3$ | $84 \cdot 6$ | $94 \cdot 6$ | 103.6 | $111 \cdot 9$ | $119 \cdot 6$ | 126.9 | $133 \cdot 8$ | $140 \cdot 2$ | 146.5 | $163 \cdot 8$ | 179.5 |
| $3 \cdot 8$ $4 \cdot 0$ | $43 \cdot 5$ | $61 \cdot 5$ | $75 \cdot 3$ | $86 \cdot 9$ | $97 \cdot 2$ | $106 \cdot 3$ | $115 \cdot 0$ | $122 \cdot 9$ | $130 \cdot 4$ | $137 \cdot 4$ | 144.0 | $150 \cdot 5$ | $168 \cdot 3$ | $184 \cdot 4$ |
| 4.0 $4 \cdot 4$ | $44 \cdot 6$ | $63 \cdot 1$ | $77 \cdot 2$ 81.0 | $89 \cdot 2$ 93.5 | 99•7 | $109 \cdot 1$ | $117 \cdot 9$ | $126 \cdot 1$ | $133 \cdot 7$ | $141 \cdot 0$ | 147.9 | $154 \cdot 5$ | $172 \cdot 7$ | $189 \cdot 1$ |
| $4 \cdot 4$ | $46 \cdot 8$ | $66 \cdot 1$ | 81.0 | $93 \cdot 5$ | $104 \cdot 6$ | 114.5 | $123 \cdot 7$ | $132 \cdot 3$ | $140 \cdot 3$ | $147 \cdot 9$ | 155.0 | $162 \cdot 0$ | $181 \cdot 1$ | 198.4 |
| $4 \cdot 8$ | $48 \cdot 8$ | $69 \cdot 1$ | 84.6 | $97 \cdot 7$ | $109 \cdot 2$ | $119 \cdot 6$ | $129 \cdot 2$ | $138 \cdot 1$ | $146 \cdot 5$ | $154 \cdot 4$ | $161 \cdot 9$ | $169 \cdot 2$ | $189 \cdot 1$ | $207 \cdot 2$ |
| $5 \cdot 2$ $5 \cdot 6$ | $50 \cdot 8$ 52.7 | $71 \cdot 9$ | $88 \cdot 1$ 91 | $101 \cdot 7$ | $113 \cdot 7$ | 124.5 | 134.5 | $143 \cdot 8$ | 152.5 | $160 \cdot 7$ | $168 \cdot 6$ | $176 \cdot 1$ | $196 \cdot 9$ | $215 \cdot 7$ |
| $5 \cdot 6$ 6.0 | $52 \cdot 7$ | 74.6 | $91 \cdot 4$ | $105 \cdot 5$ | 118.0 | 129.2 | $139 \cdot 5$ | 149.2 | 158.3 | $166 \cdot 8$ | $175 \cdot 0$ | $182 \cdot 7$ | $204 \cdot 3$ | $223 \cdot 8$ |
| $6 \cdot 0$ $7 \cdot 0$ | 54.6 | $77 \cdot 2$ | $94 \cdot 6$ | $109 \cdot 2$ | $122 \cdot 1$ | $133 \cdot 8$ | $144 \cdot 4$ | $154 \cdot 5$ | 163.8 | $172 \cdot 7$ | 181•1 | $189 \cdot 2$ | $211 \cdot 5$ | $231 \cdot 7$ |
| $7 \cdot 0$ | 59.0 | 83.4 | $101 \cdot 9$ | $118 \cdot 0$ | $131 \cdot 9$ | $144 \cdot 4$ | 156.0 | $166 \cdot 8$ | $176 \cdot 9$ | $186 \cdot 5$ | $195 \cdot 5$ | $203 \cdot 8$ | $228 \cdot 4$ | $250 \cdot 2$ |
| 9.0 | 63.9 | $89 \cdot 2$ 94.6 | $109 \cdot 1$ $115 \cdot 8$ | $126 \cdot 1$ 133 | 141.0 149.4 | $154 \cdot 4$ $163 \cdot 8$ | $166 \cdot 8$ 178.0 | $178 \cdot 3$ $189 \cdot 2$ | $189 \cdot 1$ $200 \cdot 6$ | $199 \cdot 3$ 211.5 | $209 \cdot 1$ 221.8 | 218.2 231.6 | 244.2 | $267 \cdot 5$ $283 \cdot 7$ |
| 10.0 | $70 \cdot 5$ | $99 \cdot 7$ | $122 \cdot 1$ | 141.0 | $157 \cdot 6$ | 172.7 | 186.5 | $199 \cdot 4$ | 211.5 | $222 \cdot 9$ | $233 \cdot 8$ | 244.2 | 273.0 | $299 \cdot 1$ |
| Example.-Find the discharge of a channel 8 fect wide, 3 feet deep, with a fall of 10 inches per mile. |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| perimeter |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| f 10 inches, we find $91 \cdot 9$, which, multiplied by the sectional area $24=2$ Example.-Find the fall in a similar channel 500 yards long, givin |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $\frac{2205 \cdot 6}{24}=91 \cdot 9$ feet per minute mean velocity. Looking along the line $1 \cdot 7$ we find 91.9 to be |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

TABLE OF THE VELOClTIES OF DISCHARGE IN OPEN



## Weirs.

Let $\mathrm{G}=$ gallons discharged per minute.
$d=$ depth of overflow in inches.
$l=$ length of weir in inches.
Then with thin plates we have

$$
\begin{aligned}
\mathrm{G} & =d \times \sqrt{d} \times l \times 2.67 \\
l & =\frac{\mathrm{G}}{d \times \sqrt{d} \times 2.67} \\
d & =\left(\sqrt[3]{\frac{G}{l \times 2.67}}\right)^{2} .
\end{aligned}
$$

If thin plate, weir $10^{\prime}$ long has a ratio of discharge $\quad 1 \cdot 000$ And plank $2^{\prime \prime}$ thick, square edged, weirs $3^{\prime}, 6^{\prime}, 10^{\prime}$ long . $0 \cdot 845$ ,$"$ crest $3^{\prime}$ thick level at the top . . . 0.712
" " $"$ sloped at top 1 in 12 to 1 in 18 . . 0.760 we have the coefficients which will enable us to adapt the following table to forms commonly met with in practice.

Example.-A river weir $30^{\prime}$ wide with $6 \frac{1}{2}{ }^{\prime \prime}$ overfall, the crest having a slope of 1 in 12 has a discharge of 44.25 gallons $\times 360^{\prime \prime} \times 0.76$ coefficient $=12.107$ gallons per minute, or $\frac{12107}{6 \cdot 23}=1943$ cubic feet.

If the channel is of small area the water will have a sensible velocity as it approaches the aperture, for which a correction must be made by adding to the measured head, that due to the observed velocity of approach.

For short weirs a correction must be made, as the stream suffers contraction at the ends; when contracted at both ends it is found that the effective length of the weir is reduced 0.2 inch for each inch in depth of overfall.

Square and Rectangular Pipes.-The case of square or rectangular pipes may be assimilated to that of round ones, and the head or discharge may then be calculated by the same rules that are given for the latter. The velocity of discharge, whatever may be the form of the pipe or channel, is proportional to the hydraulic radius, i.e., the sectional area, divided by the circumference or perimeter; in round pipes this is always equal to $\frac{1}{4}$ of the diameter; so by multiplying the hydraulic radius of a square or rectangular pipe by 4 , we obtain the diameter of the round pipe it is equal to.

Comnion Overflow Pipe.-When the water to be carried off is just sufficient to fill a short pipe, the discharge will be given approximately by the following rule :-

$$
\mathrm{G}=d^{2 \cdot 5} \times 3 \cdot 2
$$

in which $\mathrm{G}=$ gallons discharged per minute. $d=$ diameter of pipe in inches.
table of the Discharge of Outlet Pipes. (Box.)

| Diameter, | $\begin{aligned} & \text { Gallons } \\ & \text { per } \\ & \text { Minute. } \end{aligned}$ | Diameter, Inches. | Gallons per Minute. | Diameter, Inches. | Gallons Minute |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $3 \cdot 2$ | 5 | 179 | 13 | 1950 |
| $1{ }^{1}$ | $8 \cdot 8$ | 6 | 283 | 14 | 2346 |
| 2 | $18 \cdot 1$ | 7 | 415 | 15 | 2788 |
| 21 $\frac{1}{2}$ | $31 \cdot 6$ | 8 | 580 | 16 | 3277 |
| 3 | 50.0 | 9 | 778 | 17 | 3814 |
| 31 $\frac{1}{2}$ | $73 \cdot 3$ | 10 | 1012 | 18 | 4400 |
| 4 | $112 \cdot 4$ | 11 | 1284 | 19 | 5037 |
| 4 ${ }_{2}$ | 138.0 | 12 | 1600 | 20 | 5725 |

## STRENGTH OF MATERIALS.

## Thick Pipes.

Let $\mathrm{S}=$ the cohesive strength of the metal per square inch. $\mathrm{P}=$ the internal pressure per square inch, in the same terms as S .
$R=$ the radius of the inside of the pipe in inches.
$\mathrm{T}=$ the thickness of the metal in inches.
For cast iron may take $S$ as 7,142 tons, or $16,000 \mathrm{lbs}$. per square inch ; for lead as $2,745 \mathrm{lbs}$.

$$
\text { Then } \begin{aligned}
T & =\frac{R \times P}{S-P} \\
P & =\frac{S \times T}{R+T} \\
S & =\frac{(R+T) \times P}{T}
\end{aligned}
$$

## Thin Pipes.

Let $D=$ the diameter of the pipe in inches.
$H=$ the safe head of water in feet.
$t=$ the thickness of metal in inches.

$$
\text { Then } t=\left(\frac{\sqrt{D}}{10}+0.15\right)+\left(\frac{H \times D}{25000}\right) \text {. }
$$

Moment of Resistance ( $w$ ) and Moment of Inertia (J) FOR DIFFERENT CROSS-SECTIONS.


The coefficient of resistance of any given material equals 18 times the centre breaking load of a beam of the given material, 1 inch square, 1 foot span, supported at both ends. For average rolled iron this is about 20 tons per square inch ; for cast iron 16 tons; for good straight-grained well seasoned white pine or spruce, $3 \frac{6}{10}$ tons ; yellow pine, 4 tons ; good oak, $4 \frac{1}{2}$ tons, but owing to defects in large beams and imperfect
seasoning should not take more than about $\frac{\pi}{8}$ of these constants.

Total break- Moment of Inertia $\times$ Coefficient of resistance $\times m$ ing load in $=\overline{\text { Distance in inches from neutral axis to farthest }}$ pounds
fibre $\times$ span in inches
When the beam is firmly fixed at one end and loaded at the other
$m=1$
When the beam is firmly fixed at one end and loaded uniformly
$m=2$
When the beam is merely supported at both ends and loaded at the centre
When the beam is merely supported at both ends and loaded uniformly
$m=8$
When the beam is firmly fixed at both ends and loaded at the centre
$m=8$
When the beam is firmly fixed at both ends and loaded uniformly
$m=16$

## Round Ropes.

$\mathrm{W}=$ Breaking load in tons.
$C=$ Circumference of rope in inches.
Hemp ropes $W=0.25 \mathrm{C}^{2} \therefore \mathrm{C}=\sqrt{\frac{\mathrm{W}}{0 \cdot 25}}$.
Irnn wire ropes $W=1 \cdot 50 C^{2} \cdot \therefore C=\sqrt{\frac{W}{1 \cdot \tilde{o}}}$.
Crucible steel wire ropes $W=3 C^{2}=\sqrt{\frac{W}{3}}$. Improved plough steel wire ropes $W=4 C^{2} \cdot C=\sqrt{\frac{W}{4}}$. $A=$ Area in square inches. $d=$ Diameter in inches.
$C=3 \cdot 1416 d=\sqrt{12 \cdot 5664 A}$.
$\mathrm{A}=0.7854 d^{2}=\frac{\mathrm{C} d}{4}=0.07958 \mathrm{C}^{2}$.
$d=\frac{\mathrm{C}}{3 \cdot 1416}=0.3183 \mathrm{C}=\sqrt{\frac{\mathrm{A}}{0.7854}}$
$\mathrm{L}=\mathrm{Load}$ in tons.
$\mathrm{M}=$ Factor of safety (from 6-10).
$F=$ Depth of shaft in fathoms.
For hemp. $\quad \mathbf{C}=\sqrt{\frac{L}{\frac{0.25}{M}-\frac{F}{4 \times 2240}}}$.
For iron. $\quad C=\sqrt{\frac{L}{\frac{1.5}{M}-\frac{F}{1.2 \times 2240}}}$.

For crucible steel. $\mathbf{C}=$

$$
\mathrm{L}
$$

Yor improved plough steel. $\mathrm{C}=$


## Round Taper Ropes.

$A=$ Area of rope at any point in square inches.
$a=$ Area of rope at bottom end in square inches.
$w=$ Weight of one cubic inch of the rope in lbs. (Approx. for iron and steel, $\mathrm{W}=0.14$; for hemp rope, $\mathrm{W}=0.043$.)
$\mathrm{L}=$ Safe load in lbs. per square inch of section of rope. (Say iron, 7,000; steel, 11,500; plough steel, 13,440; hemp, 740.)
$D=$ Distance in inches from $A$ to $a$.
$\mathrm{W}=$ Weight of rope in lbs.
$\theta=2 \cdot 7182$.

$$
\begin{aligned}
\mathrm{A} & =a e^{\frac{w \mathrm{D}}{\mathrm{~L}}} \\
\mathrm{~W} & =\mathrm{L} a^{\left(e^{\frac{w \mathrm{D}}{\mathrm{~L}}}-1\right)=\mathrm{L}(\mathrm{~A}-a)}
\end{aligned}
$$

## Flat Ropes.

The strength of flat ropes is equal to the sum of the strength of the round ropes of which it is made, minus $10 \%$.

Weights and Breaking Loads of Manilla Ropes.

| Diameter. | Circumference. | Weight per foót. | Breaking Load |  |
| :---: | :---: | :---: | :---: | :---: |
| Inches. | Inches. | Lbs. | Tons. | Lbs. |
| $\cdot 239$ | $\frac{3}{4}$ | $\cdot 019$ | $\cdot 25$ | 560 |
| $\cdot 318$ | 4 | $\cdot 033$ | $\cdot 35$ | 784 |
| -477 | $1 \frac{1}{2}$ | $\cdot 074$ | $\cdot 70$ | 1,568 |
| $\cdot 636$ | 2 | $\cdot 132$ | $1 \cdot 21$ | 2,733 |
| -795 | $2 \frac{1}{2}$ | -206 | 1.91 | 4,278 |
| -955 | 3 | -297 | 2.73 | 6,115 |
| $1 \cdot 11$ | $3 \frac{1}{2}$ | -404 | $3 \cdot 81$ | 8,534 |
| $1 \cdot 27$ | 4 | -528 | $5 \cdot 16$ | 11,558 |
| $1 \cdot 43$ | $4 \frac{1}{2}$ | -668 | $6 \cdot 60$ | 14,784 |
| 1•59 | 5 | -825 | $8 \cdot 20$ | 18,368 |
| $1 \cdot 75$ | $5 \frac{1}{2}$ | $\cdot 998$ | $9 \cdot 80$ | 21,952 |
| $1 \cdot 91$ | 6 | $1 \cdot 19$ | $11 \cdot 4$ | 25,536 |
| $2 \cdot 07$ | $6 \frac{1}{2}$ | $1 \cdot 39$ | $13 \cdot 0$ | 29,120 |
| $2 \cdot 23$ | 7 | $1 \cdot 62$ | $14 \cdot 6$ | 32,704 |
| $2 \cdot 39$ | 71 | 1.86 | $16 \cdot 2$ | 36,288 |
| 2.55 | 8 | $2 \cdot 11$ | $17 \cdot 8$ | 39,872 |
| $2 \cdot 86$ | 9 | $2 \cdot 67$ | $21 \cdot 0$ | 47,040 |
| $3 \cdot 18$ | 10 | $3 \cdot 30$ | $24 \cdot 2$ | 54,208 |
| $3 \cdot 50$ | 11 | $3 \cdot 99$ | $27 \cdot 4$ | 61,376 |
| $3 \cdot 82$ | 12 | 4.75 | $30 \cdot 6$ | 68,544 |
| $4 \cdot 14$ | 13 | $5 \cdot 58$ | $33 \cdot 8$ | 75,712 |
| $4 \cdot 45$ | 14 | $6 \cdot 47$ | $37 \cdot 0$ | 82,880 |

The above figures are for ropes of average quality, as pieces from the same coil may vary 25 per cent.

A few months of exposed work weakens ropes 20 per cent. to 50 per cent.

Example.-What is the weight of 300 feet of a 2.07 inch diameter Manilla rope?

Opposite 2.07 inch, under the heading of "weight per foot," is found 1.39 lbs . ; this multiplied by 300 will give the desired weight, $1 \cdot 39$ lbs. $\times 300$ feet $=417 \mathrm{lbs}$.

A rope wound round a barrel offers the following frictional resistance to sliding:-

24 when the rope is wound 1 time round the barrel.

| 111 | $"$ | , | $1 \frac{1}{2}$ | $"$ |
| ---: | ---: | ---: | ---: | ---: |
| 535 | $"$ | $"$ | 2 | $"$ |
| 2,575 | $"$ | $"$ | $i \frac{1}{2}$ | $"$ |

Wet ropes expand in diameter and contract in length. Tarred ropes are weaker than white ropes.

## Chains.

$\mathrm{W}=$ Breaking load in tons.
$\mathrm{D}=$ Diameter in sixteenths of an inch.

$$
\mathrm{W}=\frac{\mathrm{D}^{2}}{9} ; \quad \mathrm{D}=\sqrt{9 \mathrm{~W}}
$$

Strength and Weight of Close-Link Crane Chains. and Size of equivalent Hemp Rope.

| $\left\lvert\, \begin{gathered} \text { Dia- } \\ \text { meter of } \\ \text { tron } \end{gathered}\right.$ Iron. | Weight of Chain. | Breaking Strength. | Testing Load. | Girth of Equivalent Rope | Weight of Rope. | $\begin{aligned} & \text { Greatest } \\ & \text { Working } \\ & \text { Load. } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Inches. | Lbs. per fathom. | Tons. | Tons. | Inches. | Lbs. per fathom. |  |
| $\frac{1}{4}$ | 35 | 1.9 | -75 | 2 | 13 ${ }^{\frac{3}{8}}$ |  |
| $\frac{5}{16}$ | $6 \cdot 0$ | $3 \cdot 0$ | $1 \cdot 10$ | $2 \frac{1}{2}$ | $1 \frac{1}{2}$ |  |
| $\frac{3}{8}$ | $8 \cdot 5$ | $4 \cdot 3$ | $1 \cdot 6$ | $3 \frac{1}{4}$ | $2 \frac{1}{2}$ |  |
| $\frac{7}{16}$ | $11 \cdot 0$ | $5 \cdot 9$ | $2 \cdot 3$ | 4 | $3 \frac{3}{4}$ |  |
| $\frac{1}{2}$ | $14 \cdot 0$ | $7 \cdot 7$ | $3 \cdot 0$ | $4 \frac{3}{4}$ | 5 |  |
| $\frac{9}{16}$ | $18 \cdot 0$ | $9 \cdot 7$ | $3 \cdot 8$ | $5 \frac{1}{2}$ | 7 | $\bigcirc$ |
| $\frac{5}{8}$ | $24 \cdot 0$ | $12 \cdot 0$ | $4 \cdot 6$ | $6 \frac{1}{4}$ | $8 \frac{1}{2}$ | ${ }_{0}$ |
| $\frac{11}{16}$ | $28 \cdot 0$ | $14 \cdot 6$ | $5 \cdot 6$ | 7 | $10 \frac{1}{2}$ | $\pm$ |
| $\frac{3}{4}$ | 31\% | $17 \cdot 3$ | $6 \cdot 8$ | $7 \frac{1}{2}$ | 12 | $\stackrel{ \pm}{ \pm}$ |
| $\frac{13}{10}$ | $37 \cdot 0$ | $20 \cdot 4$ | $7 \cdot 9$ | $8 \frac{1}{4}$ | 15 | 4 |
| $\begin{array}{r}10 \\ 7 \\ \hline 8\end{array}$ | $44 \cdot 0$ | $23 \cdot 1$ | $9 \cdot 1$ | 9 | $17 \frac{1}{2}$ | สี |
| $\frac{15}{16}$ | $50 \cdot 0$ | $26 \cdot 1$ | $10 \cdot 5$ | $9^{1 \frac{1}{2}}$ | $19 \frac{1}{2}$ | $\stackrel{7}{3}$ |
| 1 | $56 \cdot 0$ | $29 \cdot 3$ | $12 \cdot 0$ | 10 | 22 | E |
| 11 $\frac{1}{8}$ | $71 \cdot 0$ | $36 \cdot 3$ | $15 \cdot 3$ | $11 \frac{1}{4}$ | $27 \frac{3}{4}$ |  |
| $1 \frac{1}{4}$ | $87 \cdot 5$ | $44 \cdot 1$ | $18 \cdot 8$ | $12 \frac{1}{2}$ | $34 \frac{1}{2}$ |  |
| $1{ }^{3} 8$ | $105 \cdot 8$ | $52 \cdot 8$ | $22 \cdot 6$ | $13 \frac{3}{4}$ | $41 \frac{1}{2}$ |  |
| $1 \frac{1}{2}$ | 126.0 | $62 \cdot 3$ | $27 \cdot 0$ | 15 | $49 \frac{1}{2}$ |  |

The greatest working load for studded link cables is onehalf greater than that for close-link crane chains of the same diameter of iron.

The strength of chains varies as the square of the diameter of the iron in the link.
Softwood Timber. (F, A. Campbell.)

| Weight. | Tensile. Pounds per Square Inch. | Compression. |  |
| :---: | :---: | :---: | :---: |
| per |  | Along Grain. . | Across Grain. |
| Cubic <br> Foot. |  | Pounds per | Pounds per |
| Foot. |  | Square Inch. | Square Inch. |

Red and yellow deal-
(P. Silvestris)
White deal-
(P. Abies)
American red pine-
(P. Rubra)
American yellow pine-
(P. Variabilis)
American pitch pine-
(P. Resinosa) .
American white pine -
(P. Strobus) .
Oregon-
(Abies Douglasii)-
Kauri-
(Dammara Australis)


(E, Campbell.)

## CHEMISTRY, ASSAYING, ETC.

Table of the Symbols and Atomic Weights of the
Elements.

| Element. Symbol. | Atomic Weight. | Element. Symbol. | Atomic Weight. |
| :---: | :---: | :---: | :---: |
| Aluminium . Al | $27 \cdot 1$. | Molybdenum . Mo | 96.0 |
| Antimony . Sb | $120 \cdot 2$ | Neodymium . Nd | $144 \cdot 3$ |
| Argon. . A | $39 \cdot 9$ | Neon . . . Ne | $20 \cdot 0$ |
| Arsenic . . As | $74 \cdot 96$ | Nickel . . . Ni | 58.68 |
| Barium . . Ba | $137 \cdot 37$ | Nitrogen . . N | 14.01 |
| Bismuth . . Bi | 208.0 | Osmium . . Os | 190.9 |
| Boron. . . B | $11^{\circ} 0$ | Oxygen . . . 0 | $16 \cdot 00$ |
| Bromine . . Br | $79 \cdot 92$ | Palladium . . Pd | 106.7 |
| Cadmium . Cd | 112.40 | Phosphorus . P | $31^{\circ} 0$ |
| Cæsium . . Cs | $132 \cdot 81$ | Platinum . . Pt | $195^{\circ} 0$ |
| Calcium . . Ca | 40.09 | Potassium . . K | $39 \cdot 10$ |
| Carbon . . C | 12.00 | Praseodymium Pr | 140.6 |
| Cerium . . Ce | $140 \cdot 25$ | Radium . . Ra | 226.4 |
| Chlorine . . Cl | 35.46 | Rhodium . . Rh | $102 \cdot 9$ |
| Chromium : Cr | $52 \cdot 0$ | Rubidium . . Rb | 85.45 |
| Cobalt. . . Co | 58.97 | Ruthenium . Ru | $101 \cdot 7$ |
| Columbium . Cb | $93 \cdot 5$ | Samarium . . Sa | $150 \cdot 4$ |
| Copper . . Cu | 63.57 | Scandium . . Sc | $44 \cdot 1$ |
| Dysprosium. Dy | 162.5 | Selenium . . Se | $79 \cdot 2$ |
| Erbium . . Er | $167 \cdot 4$ | Silicon . . . Si | $28 \cdot 3$ |
| Europium . Eu | 152.0 | Silver . . . Ag | 107*88 |
| Fluorine . F | $19^{\circ} 0$ | Sodium . . Na | 23.00 |
| Gadolinium Gd | $157 \cdot 3$ | Strontium . . Sr | $87 \cdot 62$ |
| Gallium . . Ga | $69 \cdot 9$ | Sulphur. . . S | 32.07 |
| Germanium. Ge | $72 \cdot 5$ | Tantalum . . Ta | $181 \cdot 0$ |
| Glucinum . Gl | $9 \cdot 1$ | Tellurium . . Te | $127 \cdot 5$ |
| Gold . . . Au | 197. 2 | Terbium . . Tb | $159 \cdot 2$ |
| Helium . . He | 4.0 | Thallium . . Tl | 204.0 |
| Hydrogen . H | 1.008 | Thorium . . Th | $232 \cdot 42$ |
| Indium . . In | $114 \cdot 8$ | Thulium . . Tm | 168.5 |
| Iodine . . I | 126.92 | Tin . . . . Sn | 119.0 |
| Iridium . . Ir | $193 \cdot 1$ | Titanium . . Ti | $48 \cdot 1$ |
| Iron . . . Fe | $55 \cdot 85$ | Tungsten . . W | 184.0 |
| Krypton . . Kr | 83.0 | Uranium : U | $238 \cdot 5$ |
| Lanthanum. La | 139.0 | Vanadium . . V | $51 \cdot 2$ |
| Lead . . . Pb | $207 \cdot 10$ | Xenon . . . Xe | $130 \cdot 7$ |
| Lithium . . Li | $7 \cdot 00$ | Ytterbium |  |
| Lutecium . Lu | 174.0 | (Neoytterbium) Yb | 172.0 |
| Magnesium . Mg | 24.32 | Yttrium . . . Y | 89.0 |
| Manganese . Mn | 54.93 | Zinc . . . Zn | $65 \cdot 37$ |
| Mercury . . Hg | $200 \cdot 0$ | Zirconium . Zr | $90 \cdot 6$ |

## NORMAL SOLUTIONS.

Normal solutions as used in volumetric analysis are so prepared that. one liter at 16 deg. C . shall contain the hydrogen equivalent of the active reagent weighed in grams $(\mathrm{H}=1)$ : a decinormal solution $(\mathrm{N} / 10)$ is one-tenth of the normal strength. Thus in the case of univalent substances, e.g. silver, iodine, hydrochloric acid, sodium, etc., the equivalent of the atomic (or in the case of salts, molecular) weights are identical : thus a normal solution of HCl must contain 36.45 grams of the acid in a litre of fluid, and Na Ho 40 grams. In the case of bivalent substances, e.g. lead, calcium, sulphurous acid, oxalic acid, carbonates, etc., the equivalent is one-half the atomic (or in the case of salts, molecular) weight. Thus a normal solution of oxalic acid would be made by dissolving 63 grams of the crystallized acid in distilled water, and diluting the liquid to one litre. In the case of trivalent substances, e.g. phosphoric acid, a normal solution of sodium phosphate would be made by weighing $358 \div 3=119 \cdot 4$ grams of the salt, dissolving in distilled water, and diluting to one litre. One must remember that when preparing solutions for volumetric analysis, the value of a reagent as expressed by its equivalent hydrogen-weight must not always be regarded, but rather its particular reaction in any given analysis; for instance, tin is a quadrivalent metal, but when using stannous chloride as a reducing agent in the analysis of iron, the half and not the fourth of its molecular weight is required as shown by the equation $\mathrm{Fe}_{2} \mathrm{Cl}_{6}+\mathrm{Sn} \mathrm{Cl}_{2}=2 \mathrm{FeCl}_{2}+\mathrm{SnCl}_{4}$. In like manner, with a solution of $\mathrm{Mn} \mathrm{K}_{4}$ when used as an oxidizing agent, it is the available oxygen which has to be taken into account, therefore in making a normal solution one-fifth of its molecular weight $(158 \div 5) 31 \cdot 6$ grams must be contained in a litre. (F. Sutton.)

To find the Percentage Composition having the Formula given.-Multiply the atomic weight of the element by the number of the atoms of the element there are in the molecule ; multiply the number thus obtained by 100 and divide by the molecular weight of the compound.

To find the Empirical Formula of a Body from its Percentage Composition.-Divide the percentage of each element by the atomic weight of that element to three places of decimals, and divide all the numbers thus obtained by the lowest ; if the quotients are not whole numbers, reduce them to their simplest relation in whole numbers, and to these whole numbers prefix the symbol to which each refers.

To find the Weight of a Substance required to yield, liberate, or produce a given Weight of a Substance. - Write the equation expressing the chemical change : then-


## Table for the Calculation of analysis.

Let $w$ be the weight of the analysed substance, and $a$ the weight of the determined constituent of the same; then the percentage $\mathrm{P}=\frac{100 \times a}{w}$ or $\log . \mathrm{P}=\log . a+2-\log . w$.

When the required constituent is weighed in a different combination than that in which it occurs in the analysed substance (e.g., S of $\mathrm{FeS}_{2}$ as $\mathrm{BaSO}_{4}$ ), let $f$ be the factor by which the determined compound must be multiplied; then $\mathrm{P}=\frac{a \times 100 \times f}{w}$ or $\log . \mathrm{P}=\log . a+\log . f+2-\log . w$.

Example. -1 grm. of iron pyrites yielded 20.5 grm. $\mathrm{BaSO}_{4}$; what percentage of sulphur in the pyrites does that represent?

$$
\frac{20.5 \times 100 \times 0.13748}{1}=28.18 \% \mathrm{~S}
$$

| Found. | Sought. | Factor. | Log. | Found. | Sought. | Factor. | Log. | Found. | Sought. | Factur. | Log. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Aluminium$\mathrm{Al}^{2} \mathrm{O}^{3}$ |  | 0.53279 | 1•72655 | Antimony $\mathrm{Na}^{2} \mathrm{H}^{2} \mathrm{Sb}^{2} \mathrm{O}^{7}$ | $\mathrm{Sb}^{2} \mathrm{O}^{3}$ | 0•72301 | 1•85015 | Arsenic |  |  |  |
|  | $2 \mathrm{AlCl}^{3}$ | $2 \cdot 60363$ | $2 \cdot 41558$ | $\mathrm{Na}^{2} \mathrm{H}^{2} \mathrm{Sb}^{2} \mathrm{O}^{7}$ | $\mathrm{Sb}^{2} \mathrm{O}^{5}$ | $0 \cdot 80208$ | $1 \cdot 90422$ |  | As ${ }^{2} \mathbf{S}^{5}$ | $0 \cdot 81642$ | 1.91191 |
|  |  |  |  | $\mathrm{Sb}^{2} \mathrm{~S}^{3}$ | $\mathrm{Sb}^{2}$ | $0 \cdot 71777$ | 1-85599 | $\mathrm{Mg}^{2} \mathrm{As}^{2} \mathrm{O}^{7}$ | $\mathrm{As}^{2}$ | $0 \cdot 48416$ | $1 \cdot 68499$ |
| $\underset{\mathrm{NH}+\mathrm{Cl}}{\text { Ammonia }}$ |  |  |  |  | $\mathrm{Sb}^{2} \mathrm{O}^{3}$ | 0.85862 | $1 \cdot 93380$ |  | $\mathrm{As}^{2} \mathrm{O}^{3}$ | $0 \cdot 63891$ | $1 \cdot 80544$ |
|  | $\mathrm{H}^{3}$ | 0.31866 | $1 \cdot 50333$ |  | $\mathrm{Sb}^{2} \mathrm{O}^{5}$ | $0 \cdot 95252$ | 1-97887 |  | $\mathrm{As}^{2} \mathrm{O}^{5}$ | $0 \cdot 74208$ | 1-87045 |
|  | $\mathrm{NH}^{4} . \mathrm{OH}$ | $0 \cdot 65511$ | 1.81631 |  | $\mathrm{Sb}^{2} \mathrm{~S}^{5}$ | 1-18815 | $2 \cdot 07487$ |  | $\mathrm{As}^{2} \mathrm{~S}^{3}$ | $0 \cdot 79425$ | 1.89996 |
| $\underset{\text { PtCl }}{\text { 2 }}$ | $\left(\mathrm{NH}^{4}\right)^{2} \mathrm{O}$ | 0-48689 | $1 \cdot 68743$ | $\mathrm{Sb}^{2} \mathrm{~S}^{5}$ | $\mathrm{Sh}^{2}$ | 0.60411 | $1 \cdot 78112$ |  | $\mathrm{As}^{2} \mathrm{~S}^{5}$ | 1-00097 | $2 \cdot 00042$ |
|  | 2(NH3) | $0 \cdot 07685$ | $0 \cdot 88562$ |  | $\mathrm{Sb}^{2} \mathrm{O}^{3}$ | 0•72265 | $1 \cdot 85893$ | $\mathrm{BiAsO}^{4}$ | As | $0 \cdot 21477$ | $1 \cdot 33198$ |
|  | $\left(2 \mathrm{NH}^{4} . \mathrm{OH}\right)$ | $0 \cdot 15799$ | $1 \cdot 19862$ |  | $\mathrm{Sb}^{2} \mathrm{O}^{5}$ | 0-80168 | 1.90400 | $2 \mathrm{BiAsO}^{4}$ | $\mathrm{As}^{2} \mathrm{O}^{3}$ | $0 \cdot 28342$ | $1 \cdot 45243$ |
|  | $\left(\underset{\mathrm{N}^{2}}{\left(\mathrm{NH}^{4}\right)^{2} \mathrm{O}}\right.$ | $0 \cdot 11742$ | 1.06973 |  | $\mathrm{Sb}^{2} \mathrm{~S}^{3}$ | 0-84164 | $1 \cdot 92513$ |  | $\mathrm{As}^{2} \mathrm{O}^{5}$ | 0.32919 | $1 \cdot 51744$ |
|  |  | $0 \cdot 06329$ | $0 \cdot 80136$ | $\begin{aligned} & \text { Arsenic } \\ & \mathrm{As}^{2} \mathrm{O}^{3} \end{aligned}$ |  |  |  |  | Ass ${ }^{2} \mathbf{S}^{3}$ | $0 \cdot 35233$ | $1 \cdot 54695$ |
|  | $2 \mathrm{NH}^{4} \mathrm{Cl}$ | $0 \cdot 24116$ $0 \cdot 14409$ | $1 \cdot 38230$ $1 \cdot 15864$ |  | $\mathrm{As}^{2}$ | $0 \cdot 75780$ | $1 \cdot 87955$ |  | As ${ }^{2} \mathrm{~S}^{5}$ | $0 \cdot 44403$ | $1 \cdot 64741$ |
| Pt$\left(\mathrm{NH}^{4}\right)^{2} \mathrm{SO}^{4}$ | $2\left(\mathrm{NH}^{3}\right)$ | $0 \cdot 17495$ | $1 \cdot 24290$ 1 |  | $\mathrm{As}^{2} \mathrm{O}^{5}$ | $1 \cdot 16147$ | $2 \cdot 06501$ | Barium |  |  |  |
|  | 2( $\mathrm{NH}^{4} \mathrm{Cl}$ ) | $0 \cdot 54901$ | $1 \cdot 73958$ |  | $\mathrm{As}^{2} \mathrm{~S}^{3}$ | 1-24312 | 2.09452 | $\mathrm{BaSO}^{4}$ | Ba | 0.55808 | $1 \cdot 76944$ |
|  |  | $0 \cdot 25804$ | 1.41168 |  | $\mathrm{As}^{2} \mathbf{S}^{5}$ | $1 \cdot 56667$ | $2 \cdot 19498$ |  | BaO | $0 \cdot 65669$ | 1-81736 |
|  | $\begin{gathered} 2\left(\mathrm{NH}^{4} \mathrm{OH}\right) \\ \left(\mathrm{NH}^{4}\right)^{2} \mathrm{O} \\ 2\left(\mathrm{NH}^{4} \mathrm{Cl}\right) \end{gathered}$ | $0 \cdot 53050$ | $1 \cdot 72468$ | $\mathrm{As}^{2} \mathrm{O}^{5}$ | $\mathrm{As}^{2}$ | $0 \cdot 65244$ | 1-81454 |  | $\mathrm{BaCl}^{2}$ | $0 \cdot 89218$ | $1 \cdot 95045$ |
|  |  | $0 \cdot 39427$ | $1 \cdot 59579$ |  | $\mathrm{As}^{2} \mathrm{O}^{3}$ | $0 \cdot 86098$ | $1 \cdot 93499$ | $\mathrm{BaCO}^{3}$ | Ba | $0 \cdot 69565$ | $1 \cdot 84239$ |
|  |  | $0 \cdot 80977$ | 1.90836 |  | $\mathrm{As}^{2} \mathrm{~S}^{3}$ | 1.07030 | $2 \cdot 02950$ |  | BaO | $0 \cdot 77681$ | $1 \cdot 89032$ |
|  |  |  |  |  | As ${ }^{2} \mathrm{~S}^{5}$ | $1 \cdot 34887$ | $2 \cdot 12997$ |  | $\mathrm{BaCl}^{2}$ | 1.05538 | $2 \cdot 02341$ |
| $\underset{\mathrm{Sb}^{2} \mathrm{O}^{3}}{\text { Antimony }}$ |  |  |  | $\mathrm{As}^{2} \mathrm{~S}^{3}$ | $\mathrm{As}^{2}$ | 0.60959 | $1 \cdot 78504$ | $\mathrm{BaCrO}^{4}$ | Ba | $0 \cdot 54063$ | $1 \cdot 73290$ |
|  | $\mathrm{Sb}^{2}$ | 0.83596 | $1 \cdot 92219$ |  | $\mathrm{As}^{2} \mathrm{O}^{3}$ | $0 \cdot 80443$ | 1-90548 |  | BaO | $0 \cdot 60370$ | $1 \cdot 78082$ |
|  | $\mathrm{Sb}^{2} \mathrm{~S}^{3}$ | 1-11647 | $2 \cdot 06620$ |  | $\mathrm{As}^{2} \mathrm{O}^{5}$ | $0 \cdot 93432$ | 1-97049 |  | $\mathrm{BaCl}^{2}$ | $0 \cdot 82019$ | $1 \cdot 91391$ |
|  | $\mathrm{Sb}^{2} \mathrm{O}^{5}$ | 1-10936 | $2 \cdot 04507$ |  | As $s^{2} \mathrm{~S}^{5}$ | $1 \cdot 26028$ | $2 \cdot 10046$ | BaSiFl ${ }^{6}$ | Ba | $0 \cdot 48962$ | $1 \cdot 68986$ |
|  | $\mathrm{Sb}^{2} \mathrm{~S}^{5}$ | 1-38279 | $2 \cdot 14107$ | $\begin{gathered} 2\left(\mathrm{MgNH}^{4} \mathrm{As}^{2}\right. \\ \left.\mathrm{O}^{4}\right)+\mathrm{H}^{2} \mathrm{O} \end{gathered}$ |  |  |  |  | $\mathrm{BaO}^{\text {a }}$ | $0 \cdot 54674$ | $1 \cdot 73778$ |
| $\mathrm{Sb}^{2} \mathrm{O}^{5}$ | $\mathrm{Sb}^{2}$ | $0 \cdot 75355$ | 1.87711 |  | $A s^{2}$ | $0.39490$ | 1.59648 |  | $\mathrm{BaFl}^{2}$ | $0.62634$ | $1 \cdot 79681$ |
|  | $\mathrm{Sb}^{2} \mathrm{O}^{3}$ | 0.90142 | 1.95493 |  | $\mathrm{As}^{2} \mathrm{O}^{3}$ | 0.52112 | $1 \cdot 71693$ | $\mathrm{BaCl}^{2}$ | Ba | $0.65915$ | 1.81898 |
|  | $\mathrm{Sb}^{2} \mathrm{~S}^{3}$ | $1 \cdot 04985$ | $2 \cdot 02113$ |  | $\mathrm{As}^{2} \mathrm{O}^{5}$ | $0 \cdot 60526$ 0.64781 | $1 \cdot 78194$ 1.81145 |  | $\begin{gathered} \mathrm{BaO} \\ \mathrm{Ba} \end{gathered}$ | $\begin{aligned} & 0 \cdot 73605 \\ & 0.52498 \end{aligned}$ | 1-86691 |
|  | $\mathrm{Sb}^{2} \mathrm{~S}^{5}$ | $1 \cdot 24738$ | $2 \cdot 09600$ |  | $\mathrm{As}^{2} \mathbf{S}^{3}$ | 0•64781 | 1.81145 | $\mathrm{Ba}\left(\mathrm{NO}^{3}\right)^{2}$ | Ba | $0 \cdot 52498$ | $1 \cdot 72015$ |

TABLE FOR THE CALCULATION OF ANALYSIS. 159



TABLE FOR THE CALCULATION OF ANALYSIS． 161

| 800 |  <br>  －TNo |  |
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TABLE FOR THE CALCULATION OF ANALYSIS (continued)


* Adapted from J. Landauer's "Systematischer Gang der Löthrohr-analyse."
Blow-pipe Analysis.*
Preliminary Tests.
Exp. 1.-Heat in a piece of hard glass tubing closed at one end.
(a) Gas and vapour is given off which is:-
Colourless and Odourless. Water $\left(\mathrm{H}_{2} \mathrm{O}\right)$ of crystallisation, of hydration, or moisture. $\qquad$ chlorates, bromates, and iodates. Recognized by a glowing chip burning brighter when inserted
in the tube. Carbonic anhydride $\left(\mathrm{CO}_{2}\right)$ many carbonates and oxalates. Carbonic oxide (CO) oxalates and formates (the latter carbonize).
(b) Sublimates.

| White Sublimates. | Black or Grey Sublimates. | Coloured Sublimates. |
| :---: | :---: | :---: |
| Ammonic salts. | Arsenic (As) metallic arsenic | Sulphur (S) hot, yellowish- |
| Mercurous chloride ( $\mathrm{Hg}_{2} \mathrm{Cl}_{2}$ ) sub- | and many arsenical combina- | brown ; cold, yellow. |
| limes without previous fusion. | tions give a metallic reflec- | Antimony-trisulphide ( $\left.\mathrm{Sb}_{2} \mathrm{~S}_{3}\right)$ |
| Mercuric chloride $\left(\mathrm{HgCl}_{2}\right)$ smelts before subliming |  | hot, black; cold, reddish-yellow. Arsenic-trisulphide $\left(\mathrm{As}_{2} \mathrm{~S}_{3}\right)$ hot, |
| Antimony-trioxide $\left(\mathrm{Sb}_{2} \mathrm{O}_{3}\right)$ fuses and sublimes in shining needles. | combinations give metallic globules. | brownish-red ; cold, reddishyellow. |
| Tellurium dioxide $\left(\mathrm{TeO}_{2}\right)$ fuses and sublimes to an amorphous mass. |  | Mercuric-iodide ( $\mathrm{HgI}_{2}$ ) yellow, on rubbing turns red. <br> Mercuric-sulphide $(\mathrm{HgS})$ black, |
| Arsenic-trioxide $\left(\mathrm{As}_{2} \mathrm{O}_{3}\right)$ sublimes without smelting to octahedral crystals. |  | on rubbing becomes red. Selenium (Se) reddish to black; powder dark red. |


(d) Fusible.

Alkaline salts.
(e) Carbonises.

Organic substances.

## ( $f$ ) Phosphorescence.

Alkaline earths, earths, zinc oxide, tin oxide.

$$
\text { ( } g \text { ) Decrepitates. }
$$

Alkaline chlorides, and many minerals.
Exp. 2.-Heat in a piece of hard glass tubing open at both ends.
(a) Gas and vapour is given off.

Sulphurous anhydride $\left(\mathrm{SO}_{2}\right)$ known by its characteristic smell; sulphur and metallic sulphides.

Selenium dioxide $\left(\mathrm{SeO}_{2}\right)$ smells like rotten radishes; selenium and metallic selenides.
(b) Formation of sublimates.

Arsenis trioxide $\left(\mathrm{As}_{2} \mathrm{O}_{3}\right)$ very volatile, a white sublimate is deposited some distance from the assay ; arsenic and metallic arsenides.

Antimony trioxide $\left(\mathrm{Sb}_{2} \mathrm{O}_{3}\right)$ white fumes, some volatilise and some sublime ; antimony and antimony compounds.

Tellurium dioxide $\left(\mathrm{TeO}_{2}\right)$ white fumes sublime to colourless drops; tellurium and compounds of tellurium with metals. white, generally found below
Lead sulphate $\left(\mathrm{PbSO}_{4}\right)$ the assay ; compounds of Bismuth sulphate $\left(\mathrm{Bi}_{2}\left(\mathrm{SO}_{4}\right)^{3}\right) \begin{aligned} & \text { sulphur with lead: resp. } \\ & \text { bismuth. }\end{aligned}$ Exp. 3.-Heat on charcoal.

## (a) Fusibility.

| Fusible. | Infusible. |
| :---: | :---: |
| Alkalies and some of the <br> alkaline earthy salts. | Salts of the earths and alka- <br> line earthy metals, silica. |
| Antimony, lead, cadmium, <br> tellurium, bismuth, zinc, <br> tin (easily fusible). <br> Copper, silver, gold (fusible <br> with difficulty). | Iron, cobalt, nickel, man- <br> ganese, molybdenum, <br> wolfram, platinum, pal- <br> ladium, iridium, rhodium <br> and osmium. |

(b) Detonates.

Nitrates and halogen salts.
(c) Swells up.

Expulsion of water, borates and alum.
(d) Colouring of the flame, reduction of metals, and formation of incrustations will be mentioned under the heading of characteristic examinations.

## Characteristic Examinations.

## Discovery of the bases.

Exp.4.-Heat the substance with soda on charcoal with the reducing flame.
If one of the following group reactions takes place by itself, then the examination can be shortened in the following manner :-
(a) The substance gives an incrustation

Begin with Exp. 4, No. 1
(b) The substance gives a metallic bead without an incrustation
(c) The substance gives a grey or black residue.
(d) The substance colours the flame, especially when moistened with HCl
(e) The substance leaves behind a white luminous residue. .
$(f)$ The substance is completely volatile .

| $"$ | $"$ | $4, \ldots 10$ |
| :--- | :--- | :--- |
| $"$ | $"$ | $5, \not, 13$ |
| $"$ | $"$ | $7, \ldots 32$ |
| $"$ | $"$ | $8, \not, 43$ |
| $"$ | $"$ | $9,, 52$ |

The formation of hepar is an indication that sulphides or sulphates are present.
(1) White incrustation.-Very volatile; disappears with a light blue halo and propagates a garlic odour. Arsenic.

Special test.-When heated with cyanide of potassium and soda in a small glass tube closed at one end a steel-grey mirror is formed.
(2) Reddish-brown incrustation.-Variegated like the eye of a peacock's feather, driven off by 0 and $R$ flame without a coloured halo.

Cadmiun.
Special test.-The scraped-off incrustation when heated with sodium thiosulphate $\left(\mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}\right)$ in a glass tube closed at one end is coloured yellow.
(3) Incrustation yellow when hot white when cold.-Is luminous and not volatilized. Zinc.

Special test.-When heated with nitrate of cobalt solution it is coloured green. If Cd and Zn are both present the Cd incrustation is first formed, and later on that of the zinc.
(4) Steel-grey incrustation.-Disappears in the R flame with a blue colour, and gives off the smell of rotten radishes.

Selenium.
(5) White incrustation with a dark yellow to red edge. Disappears in the R flame with a green colour. Tellurium.

Special test.-If Te and Se are both present, transfer the incrustation to a test tube, moisten with a few drops of conc. $\mathrm{H}_{2} \mathrm{SO}_{4}$ and heat slightly, Te is soluble at once to a carmine red colour, while the dirty green colour of the Se first appears on heating more strongly.
(6) Bluish-white incrustation.-Volatile, driven off with the O. flame, and it disappears with a green colour in the R. flame.

Bead, white, brittle, and oxidizable. Antimony.
Special test.-The detached incrustation is dissolved in dilute HCl on platinum foil ; when Zn is added the Sb is thrown down on the platinum and stains it black.
(7) Incrustation orange when hot, lemon-yellow when cold. -Driven off by $O$ and R flame without colouring them.

Bead, reddish-white, brittle, and oxidizable. Bismuth.
Special test.-When treated on charcoal with a mixture of iodide of potassium and sulphur in the $O$ flame a fine red incrustation of iodide of bismuth is formed.
(8) Incrustation lemon-yellow when hot, sulphur-yellow when cold.- Driven off by $O$ and R flames, colours the R flame a fine blue.

Bead, white. malleable and oxidizable.
Lead.
Special test.-Moisten the assay with $\mathrm{HNO}_{3}$, evaporate the acid, add some $\mathrm{H}_{2} \mathrm{SO}_{4}$, and heat till white fumes are evolved; a white powder remains that is insoluble in $\mathrm{H}_{2} \mathrm{SO}_{4}$ acidulated water.
(9) Incrustation yellow when hot, white when cold.-Very small and found close to the assay, not volatile.

Bead, white, malleable and very oxidizable. Tin.
Special test.-Dissolve in HCl and precipitate the metallic tin as a grey spongy mass out of the acid solution by means of metallic zinc ; this will not cling to platinum as Sb does.
(10) Bead white, malleable, and very bright. -In the strong O flame, a reddish-brown incrustation is formed; in the presence of Pb or Sb it becomes carmine-red. Silver.

Special test.-Dissolve in $\mathrm{HNO}_{3}$; on the addition of HCl a white curdy precipitate of AgCl is thrown down.
(11) Bead yellow.-Very bright, malleable, and not oxidizable.

Gold.
Special test.-When dissolved in aq. regia, and $\mathrm{SnCl}_{2}$ is added, purple of Cassius is formed.
(12) Bead red.-Malleable and oxidizable.

Copper. Special test.-See Nos. 13 and 39.

## Remarks.

As a grey, infusible powder remaining behind, we have iron, nickel, cobalt (magnetic), molybdenum, wolfram, and the metals of the platinum group. The first-named bodies can be tested by burax in Exp. 5, but the platinum metals cannot be well tested by blowpipe reactions. Some combinations of the metals with $\mathrm{Cl}, \mathrm{I}, \mathrm{Br}$ and S , form white, not very characteristic incrustations without reduction of the metal: these incrustations must not be mistaken for the above reactions. The substances which give these incrustations will be otherwise determined in the course of these tests.

Exp. 5.-The assay is dissolved in a borax bead on platinum wire.
(a) The bead is coloured by the 0 or R flame. No. 13.
(b) The bead is not coloured by either flame. Ex. 7, No. 32.

The colour of the bead is

| In the Oxidizing Flame. |  | In the Reducing Flame. |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Hot. | Cold. | Hot. | Cold. |  |
| (13) Green <br> (14) Blue <br> (15) Violet to black | Bluish-green. <br> Blue. <br> Reddish- <br> violet <br> . | Colourless Blue Colourless . | Brown Blue. Rose-red | Copper. <br> Cobalt. <br> Manganese. |
| (16) Violet • \{ | Reddish brown | Yellowishgrey . | $\underset{\text { grey }}{\substack{\text { Yellowish. }}}\}$ | Nickel. |
| (17) Red to yellow | Colourless | Green . . | Green . . | Iron. |
| $\left.\begin{array}{c} \text { (18) Brown- } \\ \text { ish-red to } \\ \text { yellow } \end{array}\right\}$ | Colourless . | $\left\{\begin{array}{r} \text { Reddish- } \\ \text { yellow } \end{array}\right\}$ | Green . - | Uranium. |
| (19) Yellow . | $\left\{\begin{array}{l} \text { Colourless } \\ \text { 1.q.opaque } \end{array}\right\}$ | Brown | $\left\{\begin{array}{c} \text { Brownand } \\ \text { opaque } \end{array}\right\}$ | Molybdenum. |
| $\left.\begin{array}{r} (20) \text { Brown- } \\ \text { ish red to to } \\ \text { red dish- } \\ \text { yellow } \end{array}\right\}$ | Grass-green . | Green | $\left\{\begin{array}{c} \text { Emerald- } \\ \text { green } \end{array}\right\}$ | Chromium. |
| (21) Red | $\left\{\begin{array}{c}\text { Colourless } \\ \text { to yellow }\end{array}\right\}$ | Colourless | Colourless | Cerium. |
| (22) Yellow | $\left\{\begin{array}{c} \text { Greenish- } \\ \text { yellow } \end{array}\right.$ | Brownish | $\left\{\begin{array}{l} \text { Emerald- } \\ \text { green } \end{array}\right\}$ | Vanadium. |
| (23) Yellow | $\left\{\begin{array}{c} \text { Colourless } \\ \text { to yellow } \end{array}\right\}$ | Yellow . - | $\left\{\begin{array}{c} \text { Yellowish- } \\ \text { brown } \end{array}\right\}$ | Wolfram. |
| (24) Yellow . | Colourless . | $\left\{\begin{array}{c} \text { Yellow to } \\ \text { brown } \end{array}\right\}$ |  | Titanium. |

13*. Special test.-When heated with microcosmic salt and tin in the reducing flame, the bead becomes red; if it is black, roast it on charcoal and get rid of Sb and Bi with boric acid in the 0 flame.

14*. Special test.-The metal reduced on charcoal if rubbed on paper and treated with $\mathrm{HNO}_{3}$ forms a red solution, on adding HCl and drying a green spot is developed, which on moistening with $\mathrm{H}_{2} \mathrm{O}$ disappears.

15*. Special test.-Fusing with soda and nitre on platinum foil gives a green mass.

16*. Special test.-If the metal reduced on charcoal is rubbed on paper and treated with $\mathrm{HNO}_{3}$, a green solution is formed, which on the addition of $\mathrm{Na}_{2} \mathrm{Co}_{3}$ gives an apple-green spot.

17*. Special test.-Rub the metal reduced on charcoal on a piece of paper, treat with $\mathrm{HNO}_{3}$ and a drop of HCl ; when warmed over a flame a yellow spot is left ; if moistened with potassium ferrocyanide $\left(\mathrm{K}_{4} \mathrm{FeCy}_{0}\right)$ it turns a blue colour.

18*. Special test.-The microcosmic salt bead is in the 0 . flame, yellow when hot, yellowish-green when cold; in the R. flame a dirty green when hot, and a fine green when cold (distinction from Fe ).

Insoluble combinations of uranium are smelted on platinum with $\mathrm{HKSO}_{4}$, and the fused mass rubbed up with $\mathrm{Na}_{2} \mathrm{CO}_{3}$ moistened and the liquid absorbed by paper, which, when moistened with acetic acid, gives a reddish-brown spot with $\mathrm{K}_{4} \mathrm{FeCy}_{6}$.

19*. Special test.-By digesting with $\mathrm{H}_{2} \mathrm{SO}_{4}$ on platinum foil, the $\mathrm{MoO}_{3}$ colours the acid a deep blue on the addition of alcohol or by breathing on it.

20*. Special test.-By smelting with soda and nitre on platinum foil a yellow mass is obtained.

21*. Special test.-Cannot be well determined by the blowpipe.

22*. Special test.-Fuse with soda and saltpetre, dissolve in water, acidulate with acetic acid, add $\mathrm{AgNO}_{3}$, which gives a yellow precipitate.

23*. Special test.-The microcosmic salt bead is colourless in the O. flame both hot and cold ; in the R. flame it is a dirty green when hot, and blue when cold ; in the presence of iron it is a blood red. (See No. 27.)

24*. Special test.-The microcosmic salt bead is colourless both when hot and cold in the 0 . flame; but in the R. flame it is yellow when hot, and violet when cold; in the presence of iron it is blood-red. (See No. 30.)
(25.) When more than one coloured oxide is present, double reactions take place, for instance :-

| In the Oxidizing Flame. |  | In the Reducing Flame. |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Hot. | Cold. | Hot. | Cold. |  |
| Violet to blood-red. | $\left.\begin{array}{c} \text { Brownish- } \\ \text { violet } \end{array}\right\}$ | Yellow | Bottle-green | $M n$ and Fe. |
| Plumcoloured | $\left.\begin{array}{c}\text { Plum- } \\ \text { coloured }\end{array}\right\}$ | Bluish-green | Blue | $\left\{\begin{array}{l}\mathrm{Mn}, \mathrm{Fe} \text { and } \\ \mathrm{Co} .\end{array}\right.$ |
| Green - | Greyish-blue | Bluish-green | Green | $\left\{\begin{array}{c}M n, F e, C o, \\ a n d \text { Ni. }\end{array}\right.$ |
| Yellowish. green | Green | $\left\{\begin{array}{r} \text { Greenish- } \\ \text { blue } \end{array}\right\}$ | Blue | $1 \mathrm{Fe}, \mathrm{Co}$, and i little Ni. |
| Violet-brown | Brown . - | Blue . . | Blue | $\left\{\begin{array}{l}\text { Coand much } \\ \mathrm{Ni} .\end{array}\right.$ |
| Green. . | Light green, blue or yellow, according to quantity |  |  | Fe and Co. Fe and Cu . Fe and Ni. |

25*. Special test.-Several borax beads, with some of the assay dissolved in them, are collected and reduced ou charcoal, with the addition of lead. After a few blasts separate the borax ( $a$ ) from the lead (b).
(a) Dissolve some of the old borax slag in fresh borax in a platinum wire loop.
(a) The bead is blue.

Cobalt.
( $\beta$ ) The bead in the 0 . flame is green when hot, blue when cold.

Iron and Cobalt.
( $\gamma$ ) In the O. flame violet to blood-red when hot, brownishviolet when cold; in the R. flame yellow when hot, bottlegreen when cold ; when reduced on charcoal with tin gives a vitriol-green colour.

Manganese and Iron.
( $\delta$ ) In the 0 . flame the bead is plum-colour both hot and cold; in the R. flame is bluish-green when hot, and blue when cold.

Manganese, Iron and Cobalt.
(b) Drive off the lead from the lead button with boric acid on charcoal in the 0 . flame, and dissolve the residue in microcosmic salt.
(a) The bead in the $O$. flame is blue when cold; with tin on charcoal it is reduced to a red colour.

Copper.
( $\beta$ ) The bead in the 0 . flame is yellow when cold. Nickel.
$(\gamma)$ The bead in the 0 . flame is green when cold.
Copper and Nickel.

Exp. 6.-Decompose the substance with bi-sulphate of potash, treat with $H C l$, and add a strip of zinc.*

The solution is coloured :-
(26) Blue, then green, and finally blackish-brown. (No. 19.) Molybdic acid.
(27) Blue, then copper-red. (No. 23.) Tungstic acid.
(28) Blue, then green, and finally violet. (No. 22.)

Vanadic acid.
(29) Green. (No. 20.) Chromic acid.
(30) Violet. (No. 24.) Titanic acid.
(31) Blue, in strongly acid solutions brown. Niobic acid.

Exp. 7.-The substance, held in clean platinum forceps or wire, is placed in the non-luminous flame.
(a) The flame is coloured (especially after moistening it with HCl or $\mathrm{H}_{2} \mathrm{SO}_{4}$ ).

No. 32.
(b) The flame is not coloured.

Exp. 8, No. 43.

* Exp. 6 can be omitted when wolfram, vanadium, titanium, and niobium are not sought.
Testing for bases.

|  | By Itself. | Through Blue Glass. | Through Green Glass. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| After moistening with $\mathrm{H}_{3} \mathrm{SO}_{4}$ bring substance in to the flame for a short time only, | (32) Violet . | Reddish-violct . | Bluish-green | Potasiium. |  |
|  | (33) Orange | Reddish-violet . | Orange-yellow | Potassium and sodium. |  |
|  | (34) Orange | $\left\{\begin{array}{c} \text { Invisible or } \\ \text { weak blue } \end{array}\right\}$ | Orange-yellow. | Sodium. |  |
|  | (35) Carmine-red. | Violet-red . . | Invisible . . | Lithium. | 3a, Ca , and Sr can be |
| Moisten again with $\mathrm{H}_{2} \mathrm{SO}_{4}$, dry, and then use the greatest heat. | $\left\{\begin{array}{c} \text { (36) Yellowish- } \\ \text { green } \end{array}\right\}$ | Bluish-green . . | Green | Barium. | recognized when together by noting the different coloured jets |
|  | (37) Yellowish-red | Greenish-grey . | Siskin-green . | Calcium. | after the assay, moistened with HCl , has |
|  | (38) Carmine-red. | Purple | Weak yellow | Strontium. | been brought into the flame. |

(39) Green ; after moistening with HCl , blue.

## Testing for acids.

(40) Yellowish-green, similar to the barium flame.

Molybdic acid.
Special test.-Gives with borax the reaction of No. 19.
(41) Yellowish-green (the salt is moistened with $\mathrm{H}_{2} \mathrm{SO}_{4}$ ).

Phosphoric acid.
Special test.-When heated with Mg in a closed tube, and moistened with water, it smells of phosphoretted hydrogen.
(42) Fine green (the salt is moistened with $\mathrm{H}_{2} \mathrm{SO}_{4}$ ).

Boric acid.
Special test.-Heat on platinum with $\mathrm{CaFl}_{2}$ and $\mathrm{HKSO}_{4}$, when the intense green flame of boric fluoride is obtained.

## Remarks.

HCl and $\mathrm{HNO}_{3}$ also produce green-coloured flames, but they are weak and rapidly disappear.

The flame colourations of the already recognised elements, $\mathrm{As}, \mathrm{Sb}, \mathrm{Pb}$ (blue), Zn (greenish-white), are removed by the employment of conc. $\mathrm{H}_{2} \mathrm{SO}_{4}$.

Exp. 8.-Moisten the substance with cobalt solution on charcoal, and heut strongly.
(43) Blue infusible mass. Alumina.

Special test.-Does not colour the flame as No. 41, and does not give a Si-skeleton with microcosmic salt.
(44) Blue infusible mass. Earthy phosphates.

Special test.-Gives a yellowish-green coloured flame : see No. 41.
(45) Blue infusible mass. Earthy silicates.

Special test.-Gives a Si-skeleton in the microcosmic salt bead.
(46) Blue glass. Alkaline borates.

Special test.-Gives a fine green-coloured flame : see No. 42.
(47) Blue glass.

Alkaline phosphates.
Special test.-Gives a yellowish-green flame: see No. 41.
(48) Blue glass. Alkaline silicates.

Special test.-In the microcosmic salt bead gives a Si skeleton.
(49) Flesh-coloured mass.

Magnesia.
(50) Violet mass. Zirconia.
(51) Green mass. Zinc oxide, tin oxide, antimony oxide, titanic acid (already found).
Exp. 9.-Heat the substance with soda in a glass tube closed at one end.
(52) Metallic sublimate, which, when rubbed, unites into globules.

Quicksilver.

Special test.-Heat with $\mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}$ in a closed tube, black HgS is formed.
(53) Odour of $\mathrm{NH}_{3}$. Ammonia.

Special test.-With HCl fumes, forms a white cloud of AmCl.

## Discovery of the acids.

Exp. 10.-Heat the substance with bisulphate of potash in a tube closed at one end.
(a) It forms a coloured gas. No. 54.
(b) It forms a colourless, smelling gas.
(c) It forms a colourless and odourless gas. No. 60. No. 68.
(d) It gives no reaction.

Exp. 11, No. 71.
(54) Red fumes, with a smell of nitrous acid.

Nitric or nitrous acid.
Special test.-If a strip of paper, saturated with a solution of $\mathrm{FeSO}_{4}$, is pushed in the tube, it is coloured brown.

Nitrates deflagrate with an explosion, and flame when heated on platinum foil with KCy .
(55) Yellowish-green gas, which smells of chlorine.

Chloric acid.
Special test.-The substance deflagrates on charcoal.
(56) Violet fumes, turns starch-paste blue.

Iodine.
Special test.-The substance, together with oxide of copper in a microcosmic salt bead, colours the flame a pure green.
(57) The previous reaction takes place on the addition of $\mathrm{FeSO}_{4}$.

Iodic acid.
Special test.-The substance deflagrates on charcoal.
(58) Red-brown fumes, colours damp starch paper yellowishbrown.

Bromine.
Special test.-The substance, together with oxide of copper in a microcosmic salt bead, colours the flame a greenish-blue.
(59) The same reaction.

Bromic acid.
Special test.-The substance deflagrates on charcoal.
(60) Fumes, which, with $\mathrm{NH}_{3}$, form white clouds, and have the smell of

Hydrochloric acid.
Special test.-The substance, together with oxide of copper in a microcosmic salt bead, colours the flame an intense blue.
(61) Strong-smelling pungent gas, which etches glass.

Hydrofluoric acid.
Special test.-Heat the salt in a borax bead with bisulphate of potash; the flame is coloured green.
(62) Smell of sulphuretted hydrogen.

Sulphuretted hydrogen.
Special test.-When heated in an inclined glass tube open at both ends, metallic sulphides give a smell of $\mathrm{SO}_{2}$, and the fumes turn blue litmus paper red.
(63) Smell of burning sulphur ; no separation of sulphur.

Sulphurous acid.
(64) The same reaction, but with the separation out of sulphur.

Thiosulphuric acid.
(65) A pungent-smelling gas that brings tears to the eyes and makes lime-water cloudy.

Cyanic acid.
(66) Smell of vinegar.
(67) Smell of almonds.

Acetic acid.
(68) A gas is driven off that makes lime-water turbid.

Carbonic acid.
(69) The gas burns with a blue flame. Carbonic oxide.
(70) The substance is carbonised. Organic acids.

Exp. 11.-Heat the substance, that forms a hepar with soda on charcoal, with caustic potash on platinum foil; place the whole in a vessel of water with a clean silver cuin.
(71) The coin is not browned.

Sulphuric acid.
Special test.-To recognise sulphuric acid in the presence of sulphides (No. 62), dissolve the substance in water acidulated with $\mathrm{HNO}_{3}$, and precipitate the $\mathrm{H}_{2} \mathrm{SO}_{4}$ with $\mathrm{BaCl}_{2}$. Insoluble sulphates are first boiled in a solution of carbonate of soda, filtered and acidulated.

The following have already been found.
(72) Phosphoric acid (No. 41), boric acid (No. 42), silicic acid (No. 45).

## ASSAYS.

## Gold and Silver.

Grind the ore to pass through an 80 mesh sieve. If metallics remain behind, either dissolve in acid, dilute, sprinkle over sample, and dry at 100 deg . C., or else take the proportion of metallics to the whole and assay separately.

Scorification Assay.-Suitable for rich silver ores or ores that contain much copper, which would be reduced in the pot assay. Granulated lead may be prepared by taking silverfree red-lead in the proportion of 300 grams to 15 grams of charcoal, and reducing to lead in a clay crucible. Pour into a wooden box that has been coated with black-lead; keep the molten lead just moving till solidification begins, then shake violently. The lead will break into fine particles, which can be separated from the larger pieces by sieving. Take 5 grams (or 0.2 of an assay ton), mix with $30-60$ grams of granulated lead, place in a scorifier, cover with a little borax-glass, and heat in a hot muffle-furnace till the slag covers the lead completely; then add 0.5 gram of powdered
charcoal to clean the slag, and when the lead thus formed disappears, pour into a mould, allow to cool, break off slag, clean and square button by hammering, cupel, weigh, add silver if necessary, part, weigh again, and calculate. Silver has to be added when the amount already present is less than $2 \frac{1}{2}$ times the amount of gold, as otherwise the parting is not complete. The silver may be added by recupelling or by fusion under a blowpipe on charcoal or a cupel.

Parting is performed by brushing the adherent bone-ash from the lead, flattening with a hammer, first treating with dilute nitric acid, 1 to 2 , in a porcelain crucible, then with stronger acid, 1 to 1 , pouring off and washing with water. The parted gold should be heated to redness before weighing. If much silver is present, weaker acid should be used to prevent the gold from breaking up into very fine particles, when it is liable to be poured off with the acid or washwater. When making up parting acids, a few drops of silver nitrate should be added in order to precipitate any chlorides present in the water. The silver chloride thus formed may be allowed to settle.

Pot Assay. Roasting.-If the ore is a heavy sulphide, arsenide, or antimonide, roast sweet in a muffle surface, stirring constantly to prevent clinkering. Should the ore be very fusible, mix a little clean fine sand with the assay. If As or Sb are present, re-roast with the addition of a little C to decompose the arsenates and antimonates that are formed. Roasting in the pot to be used for the subsequent fusing is sometimes performed, chiefly for antimonides, nitre being added.

Fusion.-Mix 50 grams (or an assay ton) of the ore with red-lead or litharge and charcoal so as to form lead, which will dissolve and settle with the gold and silver, also carbonate of soda and borax to flux the silica and metallic oxides respectively. The amounts of the fluxes to be added will vary with the nature of the ore. The following typical charges may be taken as examples in which $A$ is ore with a siliceous gangue, B with a basic (iron oxide) gangue, C pyrites ore without roasting:-


Place the pot containing the charge in a wind furnace, heat till the mass becomes pasty, keep at this stage for about ten
minutes, then raise the temperature, and when the mass is fluid and all action has ceased, pour into a black-leaded mould, allow to cool, detach the slag, cupel, weigh bead and part. If button is brittle due to the presence of $\mathrm{S}, \mathrm{As}, \mathrm{Sb}$, or Zn , if hard due to Cu or Sb , or if too large, scorify before cupelling. When assaying poor ore or tailings, scorify two or more buttons together till of a convenient size to cupel.
Cupellation.-Place a clean dry cupel, which must weigh more than the lead button to be treated, in a muffle. When the cupel is red-hot place the lead button in it, and allow the action to continue till all the lead has been oxidized and absorbed by the cupel. The temperature, which should be increased towards the finish of the cupellation, is right when the fumes from the assay do not creep over the cupel or shoot straight up, but rise slightly and are carried by the draught approximately parallel to the roof of the muffle. A large silver bead is apt to spit on cooling; this can be avoided by slow cooling, best by covering with another cupel, or by removing from the muffle and, at the moment of complete solidification, quenching with a jet of cold water.

Bullion Assay.-After smelting the bullion so as to make its composition as uniform as possible, a sample may be taken by drilling, but if very impure it is better to take a dip sample from the molten mass in a charcoal or clay spoon. Weigh 0.5 gram of the sample accurately, cupel with 8 grams of lead foil, clean bead, weigh and part, wash, dry, ignite, and weigh again. This gives the approximate value of the bullion. The difference between the weight of bullion taken, and the gold-silver bead being considered as base metal; the difference between the gold and silver bead and the parted gold being taken as silver. Make a "check" by weighing pure gold, silver, and copper to form 0.5 gram of alloy of the composition of the bullion found by the trial assay and cupel, with two lots of 0.5 gram of the bullion in separate cupels each with 8 grams of lead foil. By comparing the weight of the assay after cupelling with that of the check, the loss of gold and silver in the bullion due to cupellation may be ascertained. After parting, the loss or apparent gain of gold on the " check," known as " surcharge," and which should not exceed 0.0003 gram , will show the amount to be added or deducted to the gold weights to give the true amount present in the bullion. The true silver content is found by adding the cupellation loss to the ascertained weight of the bead, and deducting the corrected fine gold. The difference between the combined fine gold and silver and the weight of bullion taken is counted as impurities. Of course
the weight of any silver added in order to form an alloy capable of being parted, must be deducted from the total silver found. Before parting, the button should be hammered flat, rolled into a "fillet" $\frac{2}{3} \mathrm{in}$. long annealed, then coiled into a "cornet" having the original bottom of the button on the outside.

Gold in Blister Copper.-Four lots of $\frac{1}{4}$ assay-ton of the borings are weighed and placed in 3 inch scorifiers, mixed with 60 grams granulated test-lead, and covered with 30 grams of the same; a little silica and borax glass may also be added. Scorify twice, adding fresh lead the second time, then combine two buttons and continue scorifying with fresh addition of lead till all the copper is removed. The slags should be saved, and either scorified after mixing with powdered charcoal or run down in a crucible. The buttons from the slag and assay should be scorified together till of convenient size, then cupelled, parted, and the gold determined in the usual manner. As an extra precaution, the button from the blister copper may be cupelled first, and then the cupel broken up and run down with the slags, the gold thus obtained being added to the first result.

## Table for converting Percentages into Troy Weight per statute Ton.

| Percentage. | Per Ton. | Per- centage. | Per Ton. | Percentage. | Per Ton. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0001 | oz. dwt. gr. | 0.008 | oz. dwt. gr. | 0.5 | oz. dwt. gr. |
| 0.0002 | $\begin{array}{lll}0 & 1 & 7 \times 36\end{array}$ | 0.009 | ${ }_{2} 18$ 19*2 | 0.6 | 1960 |
| $0 \cdot 0003$ | 0 1 123.04 | $0 \cdot 01$ | 3 5 880 | $0 \cdot 7$ | 228138 |
| $0 \cdot 0004$ | ${ }_{0} \mathbf{2} 14{ }^{17} 72$ | 002 | 61016.0 | 08 | 261616 |
| $0 \times 0005$ | 08640 | $0 \cdot 03$ | 91600 | 0.9 | 29400 |
| 0.0006 | $\begin{array}{lll}0 & 3 & 22.08 \\ 0\end{array}$ | 0.04 | $1318{ }^{18.0}$ | 1.0 | 326138 |
| 0.0007 | 0 O 41376 | $0 \cdot 05$ | $16 \quad 616^{\circ} 0$ | 20 | 653616 |
| 0.0008 | $05 \quad 5.44$ | $0 \cdot 06$ | 19120 | 30 | 98000 |
| 0.0009 | $\begin{array}{llll}0 & 5 & 21.12\end{array}$ | $0 \cdot 07$ | 22178 | 4.0 | 1,306 138 |
| $0 \cdot 001$ | $0612{ }^{\circ} 8$ | $0 \cdot 08$ | $26 \quad 216$ | 50 | 1,633 616 |
| 0.002 | ${ }_{0} 131816$ | $0 \cdot 09$ | 2980 | 6.0 | 1,960 00 |
| 0.003 | ${ }_{0} 191914.4$ | 0.1 | 32138 | $7{ }^{7} 0$ | 2,28613 |
| 0.004 | ${ }^{1} 1663.2$ | 0.2 | 65616 | $8{ }^{\circ} 0$ | 2,613 616 |
| 0.005 | 11216.0 | 0.3 | 980 | $9{ }^{9} 0$ | $2,940{ }^{0} 0$ |
| 0.006 0.007 | 1 19 4 | $0 \cdot 4$ | 130138 | $10^{\circ} 0$ | 3,266 138 |

Example. -500 grs . of ore gave $0^{\circ} 044 \mathrm{grs}$. gold, what is the yield per ton?

One hundred grs. of the ore will give $0^{\circ} 044 \div 5=0^{\circ} .0088$ grs. ; and, Per cent. oz. dwt. gr.
According to table $0.008=2 \quad 12 \quad 6.4$

$$
\text { So } 0 \cdot 0088=2 \quad 171184 \text { per ton. }
$$

Table showing the quantity of Fine Gold in One Ounce of any Alloy to One-Eighth of a Carat and the Mint Value of the Gold in One Ounce of each Alloy.

| Fine Gold. | Carat Gold. | Sterling Value. |
| :---: | :---: | :---: |
| Oz. dwt. gr. | Carats. grs. eighths. | £ s. d. |
| 100 | 2400 | $4 \quad 4 \quad 11 \cdot 454$ |
| 0194 | 2300 | $\begin{array}{llll}4 & 1 & 4.975\end{array}$ |
| 0188 | $22 \quad 00$ | $31710 \cdot 500$ |
| 01712 | 2100 | $314{ }^{\circ} 4 \cdot 023$ |
| 01616 | $20 \quad 00$ | 310 9•545 |
| 01520 | 19 0 0 | $\begin{array}{llll}3 & 7 & 3.068\end{array}$ |
| 0150 | 1800 | $\begin{array}{llll}3 & 3 & 8.591\end{array}$ |
| 0144 | 1700 | $\begin{array}{llll}3 & 0 & 2 \cdot 113\end{array}$ |
| 0138 | 1600 | $216 \quad 7 \cdot 636$ |
| 01212 | 1500 | $2131 \cdot 159$ |
| 01116 | 1400 | $2 \begin{array}{llll}2 & 9 & 6.682\end{array}$ |
| 01020 | 1300 | $\begin{array}{llll}2 & 6 & 0.204\end{array}$ |
| 0100 | 1200 | $\begin{array}{llll}2 & 2 & 5.727\end{array}$ |
| $\begin{array}{llll}0 & 9 & 4\end{array}$ | 1100 | $11811 \cdot 250$ |
| 0888 | 1000 | 1154.773 |
| $0 \quad 712$ | $9 \quad 0 \quad 0$ | $11110 \cdot 295$ |
| $\begin{array}{lll}0 & 616\end{array}$ | $8 \quad 00$ | $\begin{array}{llll}1 & 8 & 3.818\end{array}$ |
| $0 \quad 5 \quad 20$ | $7 \quad 00$ | $\begin{array}{llll}1 & 4 & 9 \cdot 341\end{array}$ |
| 0 5 5 0 | 600 | $1 \begin{array}{lll}1 & 1 & 2 \cdot 863\end{array}$ |
| 044 | 500 | 01788886 |
| $0 \begin{array}{lll}0 & 3\end{array}$ | 400 | 0141.909 |
| $0 \quad 212$ | 3000 | $\begin{array}{llll}0 & 10 & 7 \cdot 432\end{array}$ |
| 0 O 116 | 200 | $\begin{array}{llll}0 & 7 & 0.954\end{array}$ |
| $0 \quad 020$ | 100 | $\begin{array}{llll}0 & 3 & 6 \cdot 477\end{array}$ |
| $0 \quad 015$ | 030 | $\begin{array}{llll}0 & 2 & 7.858\end{array}$ |
| $\begin{array}{llll}0 & 0 & 10\end{array}$ | 020 | $\begin{array}{llll}0 & 1 & 9 \cdot 239\end{array}$ |
| 0 0 5 | 010 | $\begin{array}{llll}0 & 0 & 10.619\end{array}$ |
| $\begin{array}{llll}0 & 0 & 4.375\end{array}$ | $\begin{array}{lll}0 & 0 & 7\end{array}$ | $\begin{array}{llll}0 & 0 & 9.292\end{array}$ |
| $\begin{array}{llll}0 & 0 & 3.750\end{array}$ | $0 \times 6$ | $\begin{array}{llll}0 & 0 & 7.964\end{array}$ |
| $\begin{array}{llll}0 & 0 & 3 \cdot 125\end{array}$ | 0 0 5 | $\begin{array}{llll}0 & 0 & 6.637\end{array}$ |
| 0000500 | $0 \begin{array}{llll}0 & 0 & 4\end{array}$ | $\begin{array}{llll}0 & 0 & 5 \cdot 309\end{array}$ |
| $\begin{array}{llll}0 & 0 & 1.875\end{array}$ | 0 0 03 | $\begin{array}{llll}0 & 0 & 3.982\end{array}$ |
| $\begin{array}{llll}0 & 0 & 1 \cdot 250\end{array}$ | $0 \quad 0 \quad 2$ | $\begin{array}{llll}0 & 0 & 2655\end{array}$ |
| $\begin{array}{llll}0 & 0 & 0.625\end{array}$ | $\begin{array}{llll}0 & 0 & 1\end{array}$ | $\begin{array}{llll}0 & 0 & 1 \cdot 327\end{array}$ |

\& $s . d$.
1 oz pure gold is worth . . . $4.411 \frac{1}{2}$
1 dwt.
$0 \quad 43$
1 gr .
$\begin{array}{ll}0 & 0\end{array}$

## Copper Assay.

The Cyanide Method.-This is the simplest method, and generally accurate enough for mine work.

Standard Solution.-Weigh pure potassium cyanide and dissolve in water in the ratio of 40 grams of KCy to a litre of water. The solution should be kept in a dark stoppered bottle, and not too much made at a time as it becomes weaker on standing. It must always be re-standardised at intervals of about a week.

Standardising. -Weigh exactly three lots of 0.3 gram of pure electro-copper; if a little too heavy may fetch the copper to the exact amount by rubbing on a fine file. Dissolve in nitric acid, heat to drive off all nitrous fumes, cool, dilute, neutralize with ammonia, add 5 c.c. of ammonia in excess, then dilute to 500 c.c. From a burette run in potassium cyanide solution into the copper solution, a little at a time, till the blue colour shows signs of fading: then proceed slowly, waiting between each fresh addition of cyanide till the last trace of blue colour disappears on standing.

The Assay.-Take from 0.5 gram to 5.0 grams, depending on the richness of the ore, and dissolve in aqua regia or nitric acid, adding a little sulphuric acid towards the end of the action, then dilute, add ammonia, and proceed as during standardisation. If a heavy precipitation of iron is formed, it should not be removed by filtration but allowed to settle, or a little of the liquid filtered into a test-tube, and the colour compared with that of a test-tube containing water.

The above method is only suitable for fairly pure ores. A more satisfactory procedure is to boil down with sulphuric acid after dissolving the ore, then to dilute and boil with a strip of aluminium foil in the beaker. This precipitates the copper, which may be separated by filtering off the liquid, dissolving in nitric acid, titrating as in the case of a standard.

The Iodide Method.-The copper is determined by titration with sodium thiosulphate (hypo) after the addition of potassium iodide.

Standard Solutions. - Sodium thiosulphate $39 \cdot 18$ grams per litre. Potassium iodide 75 grams in 500 c.c. A freshly made starch solution.

Standardising.-Three lots of 0.3 gram of pure copper are dissolved in the least possible quantity of nitric acid, and carefully heated till all nitrous fumes are expelled. After diluting to about 50 c.c., sodium carbonate or ammonia is added carefully till just neutral, then a drop or two of acetic acid to re-dissolve the small precipitate formed. Twenty c.c. of the iodide solution are added, and the sodium thiosulphate solution run in from a burette till the brown colour due to
free iodide becomes faint, then starch is added, and the titration continued till the blue colour disappears and the assay is quite white.

The Assay.-Alloys with Cu and Zn may be treated direct by this method, but the copper must be separated from nearly all ores by aluminium or some suitable method, and then treated as in standardising.

The Electrolytic Method.-The copper in blister may be determined by the Iodide method, but the following is that most generally used for accurate work.

The Assay.-Twenty grams of the ground borings are treated with a mixture of 200 c.c. water, 20 c.c. $\mathrm{H}_{2} \mathrm{~S} \mathrm{O}_{4}$, and 60 c.c. $\mathrm{HNO}_{3}$ till solution is complete. Sodium chloride solution is then added in sufficient quantity to precipitate all the silver present, and leave only a small excess of common salt. Boil till all nitrous fumes are expelled, then dilute to a litre at room temperature, keeping the solution well agitated. Filter part through a dry filter; take two lots of 50 c.c. each ( $=1$ gram borings), place in a beaker, dilute to 125 c.c., and electrolyse, using a current of 0.3 amp . overnight. The increase in the weight of the cathodes multiplied by 100 gives the copper per cent.

The ordinary lighting circuit may be used for electrolytic copper assays if D.C., but if A.C. a rectifier must be used. This can be made by placing a saturated solution of ammonium phosphate in four small beakers, and using rods of aluminium for anodes and strips of sheet lead for cathodes. The current is led from a small switchboard, fitted with lamp connections to the rectifiers as shown, Figure, and from the rectifiers to the terminals to which the cones on which the copper is deposited are attached. With a 100 volt circuit one lamp does for two 1 gram assays ; two lamps in parallel for 4 assays, and so on.


> Lead Assay.

Dry Method.-To be used for fairly pure, rich ores only. Otherwise use the wet process. The results are always low owing to the formation of a double sulphide of lead and iron
not decomposed in the process. Fuse a weighed amount of the crushed ore in a crucible in a wind furnace with one of the following charges, depending on the nature of the gangue, till all action ceases, then pour into a mould, allow to cool, detach the button, hammer, clean, and weigh. The fusion should be begun at a low temperature and raised towards the end of the operation, which will take about half an hour.

| Ore | ${ }^{\text {A }}$. ${ }^{\text {a }}$ | B. |  |
| :---: | :---: | :---: | :---: |
| Carbonate of Soda | 30 | 35 | 35 |
| Argol of Flour | 3 ," | 3 ,", |  |
| Borax. | - | 5 |  |

Unless performed in an iron pot, hoop iron or nails should be put in with the charge and withdrawn just before pouring.
A. For pure Galena. B. For less pure Galena with base metals present. The borax may be used as a cover, and, if arsenic is present, as shown by the presence of a hard metallic speiss on the lead button, the argol should be reduced in quantity, and the finishing temperature raised a little higher than before. C. For oxidised ores.

Wet Assay. Ammonium Molybdate Method.-This process consists of dissolving the lead in nitric acid and separating it as sulphate, dissolving the precipitate in ammonium acetate and titrating with a standard solution of ammonium molybdate, using a solution of tannin as indicator on a spot plate.

Standard Solution.-The ammonium molybdate solution is made by dissolving the finely powdered salt in water in the proportion of 10 grams to the litre. The indicator solution should be freshly made by dissolving 0.1 gram of tannin in 30 c.c. of water.

Standardising.-To determine the lead value of the ammonium molybdate, take three lots of 0.3 gram of pure lead, and dissolve in dilute nitric acid. When solution is complete add enough sulphuric acid to just cover the bottom of the beaker, and boil till heavy white fumes show that all the nitric acid has been expelled ; cool, dilute, and filter, leaving as much of the lead sulphate as possible in the beaker. Put the filter-paper back into the beaker with the precipitate, and heat with a strong solution of ammonium acetate. When all the lead sulphate is dissolved, dilute to about 150 c.c. and boil, then run in the ammonium molybdate solution from a burette till a drop of the mixture gives a bright yellow colour when placed on a spot of the tannin solution on a plate or white tile. The three titrations should agree closely, and their average will show how many c.c. of the molybdate solution are equal to 0.3 gram of lead, and by calculation how much lead each c.c. of the solution is equal to.

The Assay.-Take 0.5 gram of ore and dissolve in nitric acid, evaporate down with sulphuric acid, dilute, boil, filter, wash with dilute sulphuric, dissolve the lead sulphate in ammonium acetate, and titrate as in standardising. The number of c.c. used to give the yellow colour, multiplied by the lead value of each c.c., shows the amount of lead in the 0.5 gram of ore taken, and that result multiplied by 200 gives the percentage of lead.

## Zinc Assay.

Potassium Ferro-cyanide Method.-Standard Solution. -Dissolve 41.25 grams of potassium ferro-cyanide in 1 litre of water. The test solution is made by dissolving 1 gram of uranium acetate in 30 c.c. of water.

Standardising.-Weigh out 0.5 gram of pure zinc, dissolve in hydrochloric acid, boil, and then run in the standard solution from a burette till a drop of the mixture gives a bright brown colour with a drop of the uranium acetate solution on a spot plate.

The Assay.-Weigh out 1 gram of the finely powdered ore, and dissolve in hydrochloric acid with the addition of a few drops of nitric acid towards the end of the action. Add a few drops of sulphuric acid and evaporate down to fuming to precipitate lead. Cool, dilute with weak hydrochloric acid, and pass sulphuretted hydrogen gas through it till all the metals of Group II are precipitated. Boil, filter, boil the filtrate till free from sulphuretted hydrogen, oxidise by adding nitric acid, care being taken not to add excess, boil, cool, and precipitate iron by ammonia. Filter, dissolve the precipitate in hydrochloric acid, re-precipitate with ammonia, filter, and add the second filtrate to the first. If much iron is present, a third precipitation will be necessary to remove all the zinc from the iron. To the mixed filtrates add bromine water and boil, adding more ammonia if necessary, filter, wash precipitate with water, acidify filtrate with hydrochloric acid, boil and titrate hot with the standard ferro-cyanide solution.

Alternative method for zinc, chiefly used when lead has not to be determined in the same sample. Treat 0.5 gram of the ore with about 10 c.c. of nitric acid until the first violent action ceases, then add from time to time a few crystals of chlorate of potash. When all action has ceased, the vessel, preferably a casserole, is uncovered and taken to complete dryness. To the dry mass is then added 7 grams of solid ammonium chloride, 20 c.c. of ammonia, and 25 c.c. of hot water in succession. The mixture is well stirred,
boiled for about one minute, and filtered. If much precipitate is present it is re-treated with nitric acid and potassium chlorate to remove the last trace of zinc. The mixed filtrates are acidified with hydrochloric acid; copper, if present, is separated by boiling with granulated lead, which need not be removed, and the titration performed as before.

## Tin Assay.

Preparation of the Sample.-Crush fine and weigh enough ore to leave about 10 grams of tin oxide as concentrates after panning. Pan carefully from one dish to another ; if sulphides or arsenides are present wash and pan again or treat with acid. If wolfram is present, treat with aqua regia for half an hour, decant, wash, dissolve tungstic acid in ammonia, decant, wash, and dry.

Cyanide of Potassium Method.-Having weighed the concentrate prepared as above, take about three times as much potassium cyanide and mix with a little powdered charcoal, place in a small hot Cornish crucible, then add the tin oxide and heat at a bright yellow heat for about twenty minutes. Pour into a mould, allow to cool, dissolve the slag in water, weigh the tin button or buttons, noting if any undecomposed ore is left. The tin button may be examined for purity by fracture or analysis.

## Slags.

Properly chilled slag, if not too high in silica (i.e. $40-45 \%$ ) may be completely dissolved in HCl after crushing to pass through a 100 mesh screen. Other slags will have to be fused with alkalies for analysis.

Determination of Copper by Colour.-Two grams of the slag are placed in a small beaker, and 50 c.c. of hot water added together with 15 c.c. H Cl , and the mixture stirred vigorously. Practically everything dissolves, with the exception of copper sulphide and a little matte. After filtering, the residue is ignited, dissolved in 5 c.c. $\mathrm{HNO}_{3}$, boiled till red fumes cease to come off, diluted, made alkaline with 20 c.c. Am Ho, boiled, and either filtered or decanted into a colormetric tube. The amount of standard copper solution required to give the same depth of colour to an equal volume in another colour-tube shows the amount of copper present in the slag.

Determination of Iron.-Half a gram of slag is placed in a beaker, and 25 c.c. of boiling water added; the mixture is then placed on a hot plate and well stirred while 20 c.c. of strong HCl is added. After boiling for a few minutes to remove $\mathrm{H}_{2} \mathrm{~S}$, a few drops of stannous chloride solution are
added to reduce all iron present to the ferrous condition, as shown by the solution becoming colourless, and then it is quickly cooled. When cold 20 c.c. of a strong solution of mercuric chloride are added, and a standard solution of potassium dichromate run in from a burette till a drop of the mixture gives no blue colour on adding to a drop of dilute potassium ferro-cyanide on a spot plate. The standard potassium dichromate contains 4.392 grams per litre, and is standardised by dissolving pure iron wire in hydrochloric acid, reducing with stannous chloride and adding mercuric chloride as above.

Determination of Silica.-Half a gram of slag after dissolving as before is taken to dryness, then heated till all hydrochloric acid fumes have disappeared. After cooling, the residue is moistened with 5 c.c. of hydrochloric acid and a few drops of nitric acid, diluted with hot water, filtered, and the residue, which is silica, ignited and weighed.

Determination of Lime.-To the filtrate from the silica, ammonia is added till it is alkaline, then solid oxalic acid till the precipitated ferric hydrate has been dissolved. A faint permanent precipitate is produced by adding more arnmonia, and again dissolved by the careful addition of small quantities of oxalic acid. Boil and filter. The precipitate, which is calcium oxalate, together with the filter paper, is placed in a beaker of hot dilute $\mathrm{H}_{2} \mathrm{SO}_{4}$, and titrated with standard potassium permanganate. The permanganate solution containing $5.991 \mathrm{~K} \mathrm{Mn} 0_{4}$ per litre may be standardised by oxalic acid, in which case the amount of oxalic acid taken multiplied by 0.444 gives the equivalent weight of lime; or if standardised with metallic iron the iron value of the solution divided by two gives the lime value.

## Water.

It is usual to combine the acids and bases found in water analysis as follows, though it may be necessary to make modifications in special cases.

Combine Cl first with Na , and if any excess with Ca and Mg .
If Na is in excess of Cl combine as $\mathrm{Na}_{2} \mathrm{O}$ with $\mathrm{SO}_{3}$. If $\mathrm{SO}_{3}$ is insufficient, calculate excess of $\mathrm{Na}_{2} \mathrm{O}$ to $\mathrm{Na}_{2} \mathrm{CO}_{3}$.

If $\mathrm{SO}_{3}$ is in excess combine first with Ca O and then with Mg 0 .

Calculate excess of CaO or MgO to $\mathrm{Ca} \mathrm{CO}_{3}$ and $\mathrm{Mg} \mathrm{C} \mathrm{O}_{3}$.
Calculate $\mathrm{Fe}_{2} \mathrm{O}_{3}$ to $\mathrm{FeS} \mathrm{O}_{4}$ if any $\mathrm{SO}_{3}$ remains after satisfying the other bases, otherwise to $\mathrm{Fe} \mathrm{CO}_{3}$.

## AIR.

Pure outside air is a mixture of :-

| Oxygen | $20.93 \%$ by volu |
| :---: | :---: |
| Carbon dioxide | $0 \cdot 03$ |
| Nitrogen, including 0.94 Argo | 79.04 |

The $\mathrm{CO}_{2}$ may vary in the lower strata of air from 0.025 to $0.035 \%$.

The allowable amount of $\mathrm{CO}_{2}$ in mine air is $0.3 \%$ by volume.
The 0 should not be decreased to less than $20 \%$ by volume.
At a temperature over $85^{\circ} \mathrm{F}$., when the air is saturated with moisture, it is not possible to do continuous hard bodily labour.

To take a sample of air.-Secure a suitable bottle, say a Winchester quart, clean and dry thoroughly. In its neck fit a rubber stopper provided with two holes. Insert a short piece of glass tubing into one hole and a long piece which reaches to the bottom of the bottle into the other; the outer end of the latter is connected to the nozzle of a small pair of bellows by a rubber tube. When the atmosphere to be tested is reached work the bellows steadily for three minutes, by which time the original air in the bottle will be replaced. Take out the rubber stopper, replace it by a well-ground and vaselined glass stopper, lute it with candle grease, and tie it down with string.

Apparatus.-The most suitable apparatus to use is Haldane's larger apparatus for gas analysis. About 20 c.c. of air is required for each test; the gas burette is graduated to 0.1 c.c., but can be read to 0.05 . The reagents required are a solution of about $20 \% \mathrm{KHO}$ to absorb the $\mathrm{CO}_{2}$, and an alkaline pyrogallic solution made by dissolving 10 grm . pyrogallic acid in 100 c.c. of a nearly saturated solution of K H O (sp. gr. $1 \cdot 55$ ) to absorb the oxygen. These solutions placed in their pipettes will serve for several analyses, as they do not deteriorate with standing, but are changed when absorption of gases becomes sluggish. CO and $\mathrm{CH}_{4}$ are burnt in a combustion pipette by means of an electric current which heats a platinum wire, forming respectively $\mathrm{CO}_{2}$ and $\mathrm{CO}_{2}+\mathrm{H}_{2} \mathrm{O}$.

Small quantities of nitrous fumes may be recognized by exposing a strip of paper moistened with a solution of starch and a little iodide of potassium slightly acidified: this will turn blue.

## TESTING CYANIDE SOLUTIONS.

Gold.-Of the many methods for determining the gold in cyanide solutions the following are those most generally used, all of which give satisfactory results. The amount of solution taken varies with the richness of the solution, also according to whether the amount of gold is compared to weight or volume of solution.

Method 1.-A known amount of solution is evaporated to dryness in a dish made of test lead, the dish and contents are then folded up and cupelled, the resulting bead being parted, if necessary, and weighed.

Method 2. - Litharge is mixed with the solution before evaporating in a porcelain dish, the dry residue is then fluxed in a crucible so as to produce a lead button, which is treated for gold in the ordinary way.

Method 3.-To a measured quantity of solution silver nitrate is added till no more precipitate is formed. This precipitate, which contains the gold, is mixed with litharge, soda, argol, and glass, and melted in a crucible to give a lead button, from which the gold is extracted as before.

Method 4.-A known quantity of solution is boiled with zinc turnings, then a solution of lead acetate and hydrochloric acid are added, and the boiling continued till all zinc has dissolved, and a spongy mass of lead is left. This lead is dried and cupelled to obtain the gold.

Available Cyanide. - This is determined by titrating a measured quantity of the solution against standard silver nitrate, using potassium iodide as an internal indicator. A faint permanent yellow precipitate shows the end of the reaction. The standard silver nitrate solution is made by dissolving 13.076 grams of pure silver nitrate crystals per litre of water, then if 10 c.c. of the cyanide solution are taken, each c.c. of silver solution used represents $0.1 \%$ of potassium cyanide.

Total Cyanide.-The estimation is performed in the same manner as the preceding with the exception that the cyanide solution is made alkaline by the addition of excess sodium hydrate before titrating.


## The Institution of Mining and Metallurgy Standard Screens for Laboratory Use.

> "'I.M.M." SERIES.

| Wire Diameter. | Apertures. |  | Mesh, per Linear inch | \% screening Area. |
| :---: | :---: | :---: | :---: | :---: |
| Decimal of an in. | in. | mm . |  |  |
| $\cdot 0100$ | $0 \cdot 1000$ | $2 \cdot 540$ | 5 | 25.00 |
| -0630 | $0 \cdot 0620$ | $1 \cdot 574$ | 8 | $24 \cdot 60$ |
| -0500 | 0.0500 | 1-270 | 10 | 25.00 |
| -0417 | 0.0416 | $1 \cdot 056$ | 12 | 24.92 |
| -0313 | 0.0312 | 0.792 | 16 | 24.92 |
| -0250 | 0.0250 | 0.635 | 20 | $25 \cdot 00$ |
| -0167 | 0.0166 | $0 \cdot 421$ | 30 | 24.80 |
| -0125 | 0.0125 | $0 \cdot 317$ | 40 | 25.00 |
| -0100 | 0.0100 | $0 \cdot 254$ | 50 | $25 \cdot 00$ |
| -0083 | 0.0083 | $0 \cdot 211$ | 60 | $24 \cdot 80$ |
| -0071 | $0 \cdot 0071$ | $0 \cdot 180$ | 70 | $24 \cdot 70$ |
| -0063 | $0 \cdot 0062$ | $0 \cdot 157$ | 80 | 24.60 |
| -0055 | 0.0055 | $0 \cdot 139$ | 90 | $24 \cdot 50$ |
| -0050 | 0.0050 | $0 \cdot 127$ | 100 | 25.00 |
| -0041 | 0.0042 | $0 \cdot 107$ | 120 | $25 \cdot 40$ |
| -0033 | $0 \cdot 0033$ | 0.084 | 150 | 24.50 |
| -0025 | $0 \cdot 0025$ | 0.063 | 200 | 25.00 |

## Sizing Tests and Grading Analysis.

A sizing test gives the engineer an idea of the percentage of different-sized material produced by various fine-crushing machinery, and the analysis of the different grades enables him to ascertain which sizes carry payable values.

Table for the Conversion of Percentage into Cwts. and Lbs. per ton and into Lbs. per Cwt.

| $\begin{gathered} \text { Per } \\ \text { Cent. } \end{gathered}$ | Per Ton. |  | Per Cwt. | $\begin{aligned} & \text { Per } \\ & \text { Cent. } \end{aligned}$ | Per Ton. |  | Per |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Cwt. | Lbs. | Lbs. |  | Cwt. | Lbs. | Lbs. |
| 1 | ... | $22 \cdot 4$ | $1 \cdot 12$ | 40 | 8 | $0 \cdot 0$ | $44 \cdot 80$ |
| 2 | ... | $44 \cdot 8$ | $2 \cdot 24$ | 41 | 8 | $22 \cdot 4$ | $45 \cdot 92$ |
| 3 |  | $67 \cdot 2$ | $3 \cdot 36$ | 42 | 8 | $44 \cdot 8$ | $47 \cdot 04$ |
| 4 |  | $89 \cdot 6$ | $4 \cdot 48$ | 43 | 8 | $67 \cdot 2$ | $48 \cdot 16$ |
| 5 | 1 | $0 \cdot 0$ | $5 \cdot 60$ | 44 | 8 | $89 \cdot 6$ | $49 \cdot 28$ |
| 6 | 1 | $22 \cdot 4$ | 6.72 | 45 | 9 | $0 \cdot 0$ | 50.40 |
| 7 | 1 | $44 \cdot 8$ | $7 \cdot 84$ | 46 | 9 | $22 \cdot 4$ | $51 \cdot 52$ |
| 8 | 1 | $67 \cdot 2$ | $8 \cdot 96$ | 47 | 9 | $44 \cdot 8$ | 52.64 |
| 9 | 1 | $89 \cdot 6$ | $10 \cdot 08$ | 48 | 9 | $67 \cdot 2$ | 53.76 |
| 10 | 2 | $0 \cdot 0$ | $11 \cdot 20$ | 49 | 9 | $89 \cdot 6$ | 54.88 |
| 11 | 2 | $22 \cdot 4$ | 12.32 | 50 | 10 | $0 \cdot 0$ | 56.00 |
| 12 | 2 | $44 \cdot 8$ | $13 \cdot 44$ | 51 | 10 | $22 \cdot 4$ | $57 \cdot 12$ |
| 13 | 2 | $67 \cdot 2$ | $14 \cdot 56$ | 52 | 10 | $44 \cdot 8$ | $58 \cdot 24$ |
| 14 | 2 | $89 \cdot 6$ | $15 \cdot 68$ | 53 | 10 | $67 \cdot 2$ | $59 \cdot 36$ |
| 15 | 3 | $0 \cdot 0$ | 16.80 | 54 | 10 | $89 \cdot 6$ | $60 \cdot 48$ |
| 16 | 3 | $22 \cdot 4$ | $17 \cdot 92$ | 55 | 11 | $0 \cdot 0$ | $61 \cdot 60$ |
| 17 | 3 | $44 \cdot 8$ | $19 \cdot 04$ | 56 | 11 | $22 \cdot 4$ | 62.72 |
| 18 | 3 | $67 \cdot 2$ | $20 \cdot 16$ | 57 | 11 | $44 \cdot 8$ | 63.84 |
| 19 | 3 | $89 \cdot 6$ | 21.28 | 58 | 11 | $67 \cdot 2$ | 64.96 |
| 20 | 4 | $0 \cdot 0$ | $22 \cdot 40$ | 59 | 11 | 89.6 | 66.08 |
| 21 | 4 | $22 \cdot 4$ | 23.52 | 60 | 12 | $0 \cdot 0$ | $67 \cdot 20$ |
| 22 | 4 | $44 \cdot 8$ | $24 \cdot 64$ | 61 | 12 | $22 \cdot 4$ | $68 \cdot 32$ |
| 23 | 4 | $67 \cdot 2$ | 25.76 | 62 | 12 | $44 \cdot 8$ | $69 \cdot 44$ |
| 24 | 4 | 89.6 | 26.88 | 63 | 12 | $67 \cdot 2$ | 70:56 |
| 25 | 5 | $0 \cdot 0$ | 28.00 | 64 | 12 | 89.6 | $71 \cdot 68$ |
| 26 | 5 | $22 \cdot 4$ | 29•12 | 65 | 13 | $0 \cdot 0$ | $72 \cdot 80$ |
| 27 | 5 | $44 \cdot 8$ | $30 \cdot 24$ | 66 | 13 | $22 \cdot 4$ | 73.92 |
| 28 | 5 | $67 \cdot 2$ | $31 \cdot 36$ | 67 | 13 | $44 \cdot 8$ | $75 \cdot 04$ |
| 29 | 5 | 89.6 | $32 \cdot 48$ | 68 | 13 | $67 \cdot 2$ | $76 \cdot 16$ |
| 30 | 6 | 0.0 | $33 \cdot 60$ | 69 | 13 | $89 \cdot 6$ | $77 \cdot 28$ |
| 31 | 6 | $22 \cdot 4$ | 34.72 | 70 | 14 | $0 \cdot 0$ | $78 \cdot 40$ |
| 32 | 6 | $44 \cdot 8$ | 35.84 | 71 | 14 | $22 \cdot 4$ | 79.52 |
| 33 | 6 | $67 \cdot 2$ | 36.96 | 72 | 14 | $44 \cdot 8$ | $80 \cdot 64$ |
| 34 | 6 | $89 \cdot 6$ | 38.08 | 73 | 14 | $67 \cdot 2$ | $81 \cdot 76$ |
| 35 | 7 | 0.0 | $39 \cdot 20$ | 74 | 14 | 89.6 | 82.88 |
| 36 | 7 | $22 \cdot 4$ | 40.32 | 75 | 15 | $0 \cdot 0$ | 84.00 |
| 37 | 7 | $44 \cdot 8$ | $41 \cdot 44$ | 76 | 15 | $22 \cdot 4$ | $8{ }^{8} \cdot 12$ |
| 38 | 7 | 67.2 | 42.56 | 77 | 15 | $44 \cdot 8$ | 86.24 |
| 39 | 7 | $89 \cdot 6$ | $43 \cdot 68$ | 78 | 15 | $67 \cdot 2$ | $87 \cdot 36$ |

Table for the Conversion of Percentage into Cwts. and Libs. per Ton and into Lbs. per Cwt. (continued).

| $\begin{aligned} & \text { Per } \\ & \text { Cent. } \end{aligned}$ | Per Ton. |  | Per Cwt. | Per | Per Ton, |  | Per Cwt. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Civt. | Lbs. | Lbs. |  | Cwt. | Lbs. |  |
| 79 | 15 | $89 \cdot 6$ | 88.48 | 90 | 18 | $0 \cdot 0$ | $100.80$ |
| 80 | 16 | $0 \cdot 0$ | $89 \cdot 60$ | 91 | 18 | $22 \cdot 4$ | 101.92 |
| 81 | 16 | $22 \cdot 4$ | 90.72 | 92 | 18 | $44 \cdot 8$ | 103.04 |
| 82 | 16 | $44 \cdot 8$ | 91.84 | 93 | 18 | $67 \cdot 2$ | $104 \cdot 16$ |
| 83 | 16 | $67 \cdot 2$ | 92.96 | 94 | 18 | 89.6 | 105.28 |
| 84 | 16 | $89 \cdot 6$ | 94.08 | 95 | 19 | $0 \cdot 0$ | 106.40 |
| 85 | 17 | $0 \cdot 0$ | 95.20 | 96 | 19 | $22 \cdot 4$ | 107.52 |
| 86 | 17 | $22 \cdot 4$ | 96.32 | 97 | 19 | $44 \cdot 8$ | 108.64 |
| 87 | 17 | $44 \cdot 8$ | $97 \cdot 44$ | 98 | 19 | $67 \cdot 2$ | 109•76 |
| 88 | 17 | $67 \cdot 2$ | 98:56 | 99 | 19 | $89 \cdot 6$ | $110 \cdot 88$ |
| 89 | 17 | $89 \cdot 6$ | 99.68 | 100 | 20 | $0 \cdot 0$ | 112.00 |

Example.-A lead ore contains 60 per cent. of lead, how much is that per ton?

Opposite 60 per cent. see 12 cwt. per ton.

## Assay of Fuel.

1. Eaternal appearance.-Porosity, compactness, fracture, size, shape, cleavage, \&c.
2. Moisture. -Weight 5 grm . powdered fuel into a watch glass; heat over a water bath at $212^{\circ} \mathrm{F}$. for about an hour; allow to cool in a dessicator ; weigh. Repeat the heating till the weight is constant : the loss is hygroscopic moisture.
3. Specific Gravity.-Place a coarse homogeneous fragment of the fuel in a sling of silk thread; suspend it from one of the pans of a balance and weigh it in air, having previously cleaned it from any dust. Thoroughly soak the fuel in distilled water, for about 12 hours; brush off any adhering air bubbles, and weigh in water.

Spc. Grv. $=\frac{\text { weight of coal in air }}{\text { diff. of wt. in air and in water. }}$
4. Volatile hydrocarbons.-Weigh out 5 grm. of the fuel ; place it in a covered porcelain crucible and heat gradually in a muffle furnace, till the flame that shows on the top disappears; then raise the temperature to red heat for a minute or two ; allow to cool and weigh. The loss equals the volatile hydrocurbons plus the moisture, and is returned in percent.
5. Coke or Charcoal.-This is the residue left after driving off the volatile hydrocarbons.
6. Ash.-Powder the coke fine, and heat it in a muffle furnace with free access of air, till all the black portion has disappeared ; allow to cool, then weigh. Note the colour of the ash, also its condition, whether pulverulent clinkered, \&c.
7. Fixed carbon. - This is found by the difference between the weight of the coke, and that of the ash, minus half the sulphur in the coal, which is retained by the coke.
8. Sulphur.-This may be hurtful when driven off by heat; or harmless when it remains in the ash : the two together form the total sulphur.

For the total sulphur, mix 1 grm. finely powdered coal with $7-8 \mathrm{grm}$. Nitre, 4 grm . carbonate of potash or soda, and 16 grm. sodic chloride, all of which must be pure. Fuse gently in a platinum crucible, placed in a muffle furnace until thoroughly white and fluid, allow to cool, by placing it on a cold iron ; dissolve out with hot water slightly acidulated with Hydrochloric acid. Heat nearly to boiling, then add a solution of baric chloride in moderate excess; allow to settle at a gentle heat; decant through a filter paper, wash the precipitate in the beaker till free from chlorine, finally transfer the precipitate to the filter paper, dry, ignite precipitate at a moderate red heat apart from the filter paper, weigh.

The percentage of sulphur $=$

$$
\frac{\mathrm{Wt} . \text { of } \mathrm{Ba} \mathrm{SO}}{4} \mathrm{ppt} .- \text { wt. filter ash } \times 13.7
$$

For the harmless sulphur boil 5 grm . finely powdered coal in a solution containing about 5 grm . pure sodium or potassium carbonate. Filter : acidify with HCl ; add $\mathrm{BaCl}_{2}$; allow to settle; dry ; incinerate; weigh as $\mathrm{BaSO}_{4}$, and calculate as above. The difference between this and the total sulphur gives the percentage of hurtful sulphur.
9. Other peculiarities of Fuels.-Notice whether-(a.) It is easily inflammable. (b.) Any smell is evolved during combustion. (c.) It is good for coking. (d.) It burns with a large or small flame, smoky or luminous. (e.) It burns quietly or with decrepitation. ( $f$.) The resulting coke burns for a long time or easily goes out.
10. Absolute heating power:-Berthier's method. Weigh 1 grm . finely powdered dry coal, mix thoroughly with 40-50 grm. pure PbO ; place in a clay crucible, add a layer of 30 grm. more PbO , and then a cover of borax glass; lute on a lid : heat gradually till fused, then raise to red heat for 10 minutes; tap the crucible to collect all the lead to the bottom, and allow to sool, then break out the reduced lead.

To find the number of calories or heat units, multiply the weight of lead reduced by $237 \cdot 6$.
11. Specific heating power.-Multiply the absolute heating power by the specific gravity.

## Tests for Common Impurities found in Mine Waters.

The usual impurities found in mine water are lime, magnesia, potash, soda, iron, copper, sulphuric acid, hydrochloric acid, carbonic acid, and sulphuretted hydrogen.
Test for Hard or Soft Water.-Dissolve a small quantity of soap in alcohol, let a few drops fall into a glass of water. If it curdles it is hard, if it remains clear it may be considered soft. Hard water may contain carbonic acid, carbonate of lime, carbonate of iron, sulphate of lime, \&c. If soft it may contain alkalies.
Test for Acid.-If blue litmus paper turns red when moistened with the water, it contains a free acid.

Test for Carbonic Acid.--If a precipitate occurs when clear lime water is added, carbonic acid is present. If on evaporating the water to dryness, the residue effervesces, a carbonate is present.

Test for Sulphuric Acid.-If a solution of chloride of barium gives a white precipitate which is not redissolved by pure nitric acid, sulphuric acid is present.

Test for a Chloride.-If water turns turbid on the addition of a drop of nitrate of silver, a chloride is present, probably a chloride of lime, soda, or magnesia.

Test for Sulphuretted Hydrogen.-Place a bright silver coin in the water, if it gets a brown or black coating it indicates sulphuretted hydrogen.

Test for Alkalies or Alkaline Earthy Matters.-If red litmus paper turns blue when moistened with the water, an alkali or alkaline earth is present.

Test for Lime.-Neutralise the water if acid with ammonia, and add oxalate of ammonia; a white precipitate indicates lime.

Test for Magnesia.-After the last solution has stood for some hours, to allow all the lime to settle, filter off, evaporate down to $\frac{x_{20}}{}$ th its bulk and add a few drops of phosphate of soda; stir well, the formation of a white precipitate after a little while indicates magnesia.

Test for Iron.-Add a few drops of yellow prussiate of potash to a glass of the water, it will immediately become of a blue colour if iron is present.

Test for Copper.-A polished piece of iron immersed in the water for a few minutes will have any copper present pre-
cipitated on it. Ammonia added to water containing copper in solution turns it blue.

## Adulteration of Oils, Lard, and Tallow.

Fats and oils are subject to adulteration and falsification, particularly those of great commercial value, and generally with fats and oils of lower prices. By exposure to the air they absorb oxygen and become rancid; some oils dry into a kind of varnish, and are called drying oils. . The fats are adulterated with foreign substances to increase their weight. We cannot here go into a gencral analysis of all these important materials, but will examine such as are in common use and most liable to sophistication.

Clive Oil.-Olive oil for the manufacture of soaps is ordinarily adulterated with cole-seed oil, cotton-seed oil, and poppy oil. These mixtures are sometimes disguised by colouring them green with indigo, so as to create the impression that green olive oil is present. The adulteration with black poppy oil is the most frequent, not only on account of the cheapness of this oil, but also on account of its sweet taste, and its odour being but little pronounced.

Oil of Sueet Almonds.-The oil of sweet almonds is principally falsified with poppy oil and with sesame oil. Several processes have been proposed for detecting this falsification. Oil of sweet almonds becomes cloudy at $20^{\circ} \mathrm{C}$. ( $4^{\circ}$ below $0^{\circ} \mathrm{F}$.), and solidifies at $25^{\circ} \mathrm{C}$. ( $13^{\circ}$ below $0^{\circ} \mathrm{F}$.), while poppy oil begins to solidify between $3 \cdot 9^{\circ} \mathrm{C} .\left(39^{\circ} \mathrm{F}\right.$.), and $6^{\circ} \mathrm{C}$. $\left(42 \cdot 8^{\circ} \mathrm{F}\right.$.). One part of aqua ammonia, mixed with nine parts of oil of sweet almonds, forms a white soft soap, very smooth and homogeneous if the oil be pure ; on the contrary, it is clotted if it contains more than one-fifth of poppy oil.

Rapesecd Oil.-This oil is falsified with linseed, mustard, and whale oils, olcic acid, \&c. Ammonia with pure oil gives a milk-white soap; and a yellowish-white soap when the musiard and whale oils are present. Gaseous chlorine colours rapesced oil brown, when it contains whale oil; if pure it remains colourless.

Sesame Oil.-This oil is ordinarily mixed with earth-nut oil.

Linseed Oil.-This oil is falsified with hemp seed, and especially with fish oil. Pure linseed vil treated by hyponitric acid becomes pale pink ; by ammonia, dark yellow, and gives a thick and homogeneous soap.

Black Poppy Oil.-This oil is often mixed with sesame and beech-nut oils. The pure oil is coloured a light yellow with hyponitric acid, while beech oil acquires a pink colour.

Ammonia colours it a light yellow ; the consistency is slightly thick, and the soap is a little granular.

Hempseed Oil.- The adulteration of this oil is always done with linseed oil. The pure oil treated by ammonia becomes yellow, thick, and granular.

Castor Oil.-This oil is generally mixed with black poppy oil. The adulteration is easy to detect with alcohol at $95^{\circ} \mathrm{B}$.; a certain quantity of oil agitated with this liquid is dissolved, and leaves the foreign oil as a residuum.

Neat's Foot Oil.-This oil is without doubt the most adulterated oil found in commerce. It is mixed with whale, black poppy oil, and olein.

Oleic Acid.-This acid is often mixed with resin oil. The pure acid, treated with an acid solution of nitrate of mercury, yields a pale straw-coloured foam; the resin oil yields a very dark orange foam.

Palnı Oil.-This oil has been mixed with or manufactured entirely of yellow wax, lard, mutton suet, coloured with turmeric, and aromatised with powdered orris root, without any genuine palm oil. By treating the suspected oil with ether, all the fatty bodies are dissolved; the turmeric and orris root remain insoluble. By saponification the mixed or artificial oil takes a reddish shade, due to the action of the alkali on turmeric. Sometimes powdered resin has been mixed with it ; this falsification is easily detected by treating the oil with alcohol : the resin is dissolved while the oil remains insoluble.

Cocoanut Oil.-The commercial oil is often adulterated with mutton suet, beef marrow, or other animal greases, sometimes also with the oil of sweet almonds and wax. The oil falsified by these substances does not completely dissolve in cold ether. The ethereal solution is muddy like that given by pure butter. The oil thus falsified has a taste and an odour less agreeable, a colour rather greyish than yellowish, and has less consistency. The melting point is the best method of ascertaining the purity. Adulterated with greases or tallows the oil melts at $26^{\circ}$ to $28^{\circ} \mathrm{C}$. $\left(78 \cdot 8^{\circ}\right.$ to $82 \cdot 4^{\circ} \mathrm{F}$.) ; with oil of sweet almonds it melts at $23^{\circ} \mathrm{C}$. $\left(73 \cdot 4^{\circ} \mathrm{F}\right.$.)

Lard.-Alterations.-Lard exposed to the air in jars not well closed becomes rancid and turns yellow. If kept in copper vessels, or in earthen jars glazed with sulphide of lead, it may, by contact with the air, attack the copper or the glazing, and then contain stearate and oleate of copper or lead. The copper is detected by pouring on the grease a few drops of ammonia, which immediately becomes blue. A red colouration is given by a solution of yellow prussiate of potash. Lead is detected by burning the lard, and carefully examining
the residuum to see if there are any metallic globules. The residuum is then treated by nitric acid, which dissolves the metal. Filter, and to the filtrate add sulphuric acid, which gives a white precipitate. Lard may also contain an excess of water, which is ascertained by pressing and softening it with a wooden spatula; the water oozes from it in the form of drops. By melting it at a low temperature the water separates from the grease. The principal adulterations of lard are the addition of common salt, the admixture of a grease of inferior quality, or that of a kind of grease obtained by the cooking of pork meat. Plaster of Paris is sometimes added. The addition of salt is easily detected by digesting the lard with hot distilled water. The salt in the water is abundantly precipitated with nitrate of silver. The precipitate is white, soluble in ammonia, and insoluble in nitric acid; it becomes black when exposed to the light. Plaster of Paris is detected by melting in warm water the suspected lard. If it contains plaster, this falls to the bottom in the form of a white powder. The inferior greases are often very difficult of detection; they are ascertained by the less white colour of the lard, and by a taste entirely different. The greases from the cooking of pork meat give to the lard a greyish colour, a soft consistency, a salted and disagreeable taste.

Tallows.-Tallows are generally adulterated with greases of inferior quality. Water is also incorporated in them by a long beating. Cooked and mashed potatoes have been also introduced into them. Fecula, kaolin, white marble, and sulphate of baryta, are also added to tallows. The principal adulteration is the addition of bone tallow; properly speaking, it is not a falsification, it is only a change in the quality of the product. The mineral matters, the fecula, and the cooked potatoes are easily ascertained by disolving the tallow in ether or sulphide of carbon. All the foreign substances remain insoluble, and their nature is then easily determined. Iodine water, or the alcoholic tincture of iodine, will colour blue the insoluble residuum if it contains fecula. This fecula can be determined in the tallow by triturating the grease with iodine water and adding a few drops of sulphuric acid. The blue colour will appear immediately if there be fecula. For the mineral substances there is a process as simple as the above to ascertain their presence in tallow. It is to melt the tallow in twice its weight of water; the foreign substances are precipitated, and the grease floats on the surface. Instead of using ordinary water, the tallow may also be boiled for a few minutes with two parts acidulated water for one part of tallow. The whole is allowed to rest in a test glass, or in a funnel placed over a water bath, kept at a temperature of
about $40^{\circ} \mathrm{C} .\left(104^{\circ} \mathrm{F}\right.$.), so as to prevent the too rapid cooling of the tallow, and to give time to the impurities to separate and deposit. Iodine added in this last treatment will disclose the presence of fecula or starch. To ascertain the presence of water, knead dried powdered sulphate of copper with the tallow (half its volume of the powder). If there be much water, the mixture will take a blue colour if the tallow is white, and greenish if the grease is yellowish. As for the quantity of water added, the only way to ascertain it is by drying a sample in an oven.

Physical Properties of Oils.-Fixed oils, at the ordinary temperature, are nearly always liquid; some, however, such as palm oil, cocoa-nut oil, \&c., are more or less consistent. They are also more or less mucilaginous, with a feeble taste, sometimes disagreeable. Some are colourless, but generally they have a slight yellow tint; some are of a greenish-yellow colour, and this colour is due to a peculiar principle they hold in solution. Their specific gravity is less than that of water, all floating on this liquid, but it varies.*

## SLAGS.

Formulæ for silicates of bases having the composition R O; e.g. $\mathrm{CaO}, \mathrm{Mg} \mathrm{O}, \mathrm{BaO}, \mathrm{Fe} \mathrm{O}, \mathrm{Mn} \mathrm{O}$, and ZnO .

Oxygen Ratio.
Subsilicate. . $4 \mathrm{RO}+\quad \mathrm{Si}_{2}=\mathrm{R}_{4} \mathrm{Si}_{6} \quad 2$ in base : 1 in acid Monosilicate . $2 \mathrm{RO}+\mathrm{SiO}_{2}=\mathrm{R}_{2} \mathrm{Si}_{4} 1 \quad$, 11 , Bisilicate . $\mathrm{RO}+\mathrm{SiO}_{2}=\mathrm{R} \mathrm{Si} \mathrm{O} 1 \quad$, $\quad 2$,, Trisilicate . . $2 \mathrm{RO} 0+3 \mathrm{SiO}_{2}=\mathrm{R}_{2} \mathrm{Si}_{3} \mathrm{O}_{8} \quad 1 \quad, \quad: 3 \quad$, Sesquisilicate. $4 \mathrm{RO}+3 \mathrm{SiO}_{2}=\mathrm{R}_{4} \mathrm{Si}_{3} \mathrm{O}_{10} 2$,, $: 3$,,

Formulæ for silicates of bases having the composition $\mathrm{R}_{2} \mathrm{O}_{3}$; e.g. $\mathrm{Al}_{2} \mathrm{O}_{3}, \mathrm{Fe}_{2} \mathrm{O}_{3}, \mathrm{Mn}_{2} \mathrm{O}_{3}$.

Oxygen Ratio.
Subsilicate. $4 \mathrm{R}_{2} \mathrm{O}_{3}+3 \mathrm{Si}_{2}=\mathrm{R}_{8} \mathrm{Si}_{3} \mathrm{O}_{18} 2$ in base : 1 in acid Monosilicate. $2 \mathrm{R}_{2} \mathrm{O}_{3}+3 \mathrm{Si}_{2}=\mathrm{R}_{4} \mathrm{Si}_{3} \mathrm{O}_{12} 1$ Bisilicate. . $\mathrm{R}_{2} \mathrm{O}_{3}+3 \mathrm{SiO}_{2}=\mathrm{R}_{2} \mathrm{Si}_{3} \mathrm{O}_{9} 1 \quad, \quad: 2$ Trisilicate . $2 \mathrm{R}_{2} \mathrm{O}_{3}+9 \mathrm{Si}_{2}=\mathrm{R}_{4} \mathrm{Si}_{9} \mathrm{O}_{24} 1 \quad,, \quad: 3 \quad$, Sesquisilicate $4 \mathrm{R}_{2} \mathrm{O}_{3}+9 \mathrm{Si}_{2}=\mathrm{R}_{8} \mathrm{Si}_{9} \mathrm{O}_{30} 2$

| ,$"$ | $: 1$ | $"$ |
| :--- | :--- | :--- |
| $"$, | $: 3$ | $"$, |
| $"$, | $: 3$ | $"$, |

Each sesquisilicate can be broken up into a monosilicate and a bisilicate ; for instance :-

$$
\left.\begin{array}{l}
\mathrm{R}_{4} \mathrm{Si}_{3} \mathrm{O}_{10}=\mathrm{R}_{2} \mathrm{Si}_{\mathrm{Si}_{4}}+2\left(\begin{array}{ll}
(\mathrm{R} & \mathrm{Si}_{3}
\end{array}\right) \\
\mathrm{R}_{8} \mathrm{Si}_{8} \mathrm{SO}_{30}=\mathrm{R}_{4} \mathrm{Si}_{3} \mathrm{O}_{12}+2\left(\mathrm{R}_{2} \mathrm{Si}_{3} \mathrm{O}_{9}\right.
\end{array}\right)
$$

If a silicate contains but one base it is called monobasic, but if two or more a double silicate or multibasic silicate.

Subsilicates are easily fusible, flow thinly, but consolidate
quickly and break up in doing so. Their colour is usually dark, and they have a high specific gravity: formed mostly during the refining of metals. Subsilicates are only used for special purposes, e.g. when it is cheaper to lose some of the metal in the slag than go to the expense of flux and the necessary fuel to melt a larger quantity of more siliceous slag.

Monosilicates are not so readily fusible as the former, neither are they so thinly fluid, but they cool quickly and form crumbly pieces that don't hold together. Specific gravity $4^{\cdot} 2$ to $3 \cdot 6$.

Monosilicates eat into the furnace lining when not kept sufficiently cool, and on account of solidifying easily they entangle globules of metal. They also form deposits in the furnace, and if heated too strongly reduce iron, causing sows, thus shortening the life of the campaign. Monosilicates dissolve simple metallic sulphides of $\mathrm{Fe}, \mathrm{Zn}, \mathrm{Ca}$, etc.

A monosilicate is used when converting copper matte.
Slags used in smelting lead ores are usually monosilicates, the bisilicates not being suitable as they carry away too much lead as a silicate; they are also more viscous, and cause irregularities in the working of the furnace. The monosilicate, however, requires more base for fluxing the silica, and is, therefore, not always economical, so other slags are aimed at having oxygen ratios of 2 to 3,4 to 5 , and so forth.

Sesquisilicates are a mixture of a monosilicate with a bisilicate. It has a low melting-point, and runs smoothly without forming a thick crust over its surface. Its specific gravity allows a complete and rapid settlement of the matte.

Bisilicates are still more difficult to fuse, flow thickly, and can be drawn out into threads. They cool slowly. Specific gravity 3 to $3 \cdot 5$.

Bisilicates are often made because they are not too difficult to fuse, and do not corrode the acid lining of furnaces so easily as more basic slags, and on account of cooling slower do not deposit so readily in the furnace, besides giving time for the metal to settle through it.

In copper smelting generally aim for a bisilicate slag from the ore, but it may be necessary to vary this in order to obtain the required grade of matte, since this may be raised or lowered by adding more or less silica to flux off the iron that would otherwise pass into the matte. If the ore reduces with difficulty, flux it in such a manner as to give the metals time to reduce before the slag separates out. When concentrating a matte, make a sesquisilicate slag; it works slower, giving the matte time to roast.

In blast furnace work, if too high a copper matte is not formed, the slag may be sufficiently poor to be discarded, and the gases, which escape at a temperature of about 300 C ., are relatively free from metals. The slag from copper convertors is so foul that it has to be re-treated, and convertor gases escape at a temperature of about $1,500 \mathrm{C}$., which carry away large quantities of metals. The volatilization losses of Au and Ag from a convertor may be increased by the long period required to blow too low a grade of matte.

Trisilicates flow slowly, cool gradually, and can also be drawn out into threads; they are porcelain-like in appearance. They require a very great temperature to form them, and are seldom used. Specific gravity 2.94 to 2.57 .

The choice of a slag depends on the object of the operation, the composition of the materials at hand, taking their cost into consideration, and the cleanliness of the slag. One wants to use the least possible amount of fluxes and fuel. An unnecessary amount of flux increases the quantity of slag and the loss of metals in it. Besides the heat-producing substances in a fuel, one must consider the ash which has to be slagged off, likewise impurities in the fluxes used. Many of the difficulties met with in smelting are due to an excess of fuel, e.g. the reduction of iron which forms sows and shortens the life of a campaign.

The monobasic silicates generally require more heat to form than double or multibasic silicates, and of the compound silicates those composed of monoxide bases are more difficult to fuse than a mixture of monoxide and sesquioxide bases.

Of the monobasic silicates those of-

| Iron and Manganese require |
| :--- |
| Lime |
| Baryta |
| . | $1789^{\circ} \mathrm{C}$. to $1832^{\circ} \mathrm{C}$.

Of double silicates those of-
Lime and Alumina form at from $1918^{\circ} \mathrm{C}$. to $1950^{\circ} \mathrm{C}$.
Lime and Magnesia ,, ,, $2000^{\circ} \mathrm{C}$.
Baryta and Alumina ", ", $2050^{\circ} \mathrm{C}$.
Baryta and Lime
," $\quad, \quad 2100^{\circ} \mathrm{C}$.
Slags already formed fuse at a lower temperature than that required for their formation.

Slag calculations are based on the ratio of the 0 in the bases to that of the silica.

When calculating a slag to contain BaO or Mg O it simplifies matters to bring these substances to their equivalent of CaO . This is done by multiplying the percentage of BaO by 0.368 , and the percentage of Mg O by 1.4 .

$$
\begin{array}{cl}
\text { Molecular weight of } \mathrm{CaO} \frac{56}{152}=0.368 . & \mathrm{CaO} \frac{56}{40}=1 \cdot 4 .
\end{array}
$$

In like manner MnO is calculated to its equivalent of Fe O .
The volatilization of sulphur in ordinary copper smelting may be as much as $75 \%$, leaving $25 \%$ active sulphur.

The following type slags are taken from the private notebook of H. C. Bellinger. A slag is called whole, half, or quarter, according to the ratio of $\mathrm{FeO}+\mathrm{MnO}$ to the $\mathrm{CaO}+$ $\mathrm{Mg} \mathrm{O}+\mathrm{Ba} \mathrm{O}$.

Lead Slag and Eiler's Pueblo Slag and Leadville.

$$
\begin{aligned}
& \text { One-quarter slag \% Fe O:\% Ca O:: } 4: 1 \\
& \text { One-half slag } \\
& \begin{array}{ll}
x=\mathrm{Fe} \mathrm{O} & \mathrm{Fe}: \% \mathrm{CaO}:: 2: 1 \\
y=\mathrm{CaO} & x+y=1 \\
\text { Fe O }=72 \\
\text { For quarter slag } & x \mathrm{FeO}=4 y \mathrm{CaO} \\
\text { For half slag } & x \mathrm{FeO}=2 y \mathrm{CaO}
\end{array}
\end{aligned}
$$

Quarter slag.

$$
\left.\begin{array}{l}
x+y=1 \\
\begin{array}{l}
x \\
7 \\
-
\end{array} \frac{4 y}{9}=0 \\
x: 4 y=\frac{1}{72}: \frac{1}{56} \\
\frac{x}{56}=\frac{4 y}{72} \text { whence } x=\frac{28 y}{9} \\
x+y=1 \text {, so } \frac{28 y}{9}+y=1 \\
\begin{array}{l}
28 y+9 y=9 \\
37 y=\frac{28}{37} \\
y=\frac{9}{37}
\end{array} \quad y=\frac{9}{37}
\end{array}\right\} \text { For quarter slag. } \quad \text { RO } \begin{aligned}
& \frac{28}{37} \mathrm{Fe} 0+\frac{9}{37} \mathrm{CaO} .
\end{aligned}
$$

Half slag.
$\left.\begin{array}{ll}x+y=1 & x=\frac{14}{23} \\ \frac{x}{7}-\frac{2 y}{9}=0 & y=\frac{9}{23}\end{array}\right\}$ R O $=\frac{14}{23} \mathrm{FeO}+\frac{9}{23} \quad \mathrm{CaO}$.

Examples.
(1) Subsilicate. $3 \mathrm{RO}+\mathrm{Si} \mathrm{O}_{2}$

Quarter slag.

$$
\begin{gathered}
3\left(\frac{28}{37} \mathrm{Fe} \mathrm{O}+\frac{9}{37} \mathrm{CaO}\right)+\mathrm{Si} \mathrm{O}_{2}=3\left(\frac{28}{37} \times 72+\frac{9}{37} \times 56\right) \\
+(28+32)=3(54 \cdot 487+13.622)+60=3(68 \cdot 11)+60=264.33 \\
\frac{3 \times 54 \cdot 49}{264 \cdot 33}=61 \cdot 84 \% \mathrm{FeO} \\
\frac{3 \times 13 \cdot 62}{264 \cdot 33}=15 \cdot 46 \% \mathrm{CaO} \\
\frac{60}{264 \cdot 33}=\frac{22 \cdot 70}{100 \cdot 00} \% \mathrm{Si} \mathrm{O}_{2}
\end{gathered}
$$

Half slag.
$3\left(\frac{14}{23} \mathrm{FeO}+\frac{9}{23} \mathrm{CaO}\right)+\mathrm{SiO}_{2}=3(43 \cdot 826+21 \cdot 913)+60=$ $257 \cdot 22$

$$
\left.\begin{array}{r}
131.49 \\
65 \cdot 73 \\
60.00
\end{array}\right\}=\begin{aligned}
& 51 \cdot 12 \% \mathrm{Fe} \mathrm{O} \\
& 25 \cdot 55 \% \mathrm{CaO} \\
& 23 \cdot 33 \% \mathrm{Si} \mathrm{O}_{2}
\end{aligned}
$$

(2) 2 Mono and 1 Bisilicate $2\left(2 \mathrm{RO}+\mathrm{Si}_{2}\right)+\left(\mathrm{RO}+\mathrm{Si} \mathrm{O}_{2}\right)$ Quarter slag.
$5 \mathrm{RO}+3 \mathrm{Si} \mathrm{O}_{2}=5\left(\frac{28}{37} \mathrm{FeO}+\frac{9}{37} \mathrm{CaO}\right)+3 \mathrm{Si} \mathrm{O}_{2}=5(54 \cdot 487$ $+13 \cdot 622)+180$
\(\left.\begin{array}{r}180.00 <br>
272.45 <br>

68.10\end{array}\right\}=\)| $34.58 \%$ | $\mathrm{Si} \mathrm{O}_{2}$ |
| ---: | :--- |
| 520.55 |  |$\frac{13.34 \% \mathrm{Fe} \mathrm{O}}{100.00} \mathrm{Ca} \mathrm{O}$

Half slag.
$5 \mathrm{RO}+3 \mathrm{SiO}_{2}=5\left(\frac{14}{23} \mathrm{FeO}+\frac{9}{23} \mathrm{CaO}\right)+3 \mathrm{Si} \mathrm{O}_{2}=5(43 \cdot 826$ $+21.913)+180$
\(\left.\begin{array}{l}180.00 <br>
219.15 <br>
109.56 <br>

\hline 508.71\end{array}\right\}\)| $35 \cdot 38 \% \mathrm{Si} \mathrm{O}_{2}$ |
| :--- |
| $=$$43.08 \% \mathrm{Fe} \mathrm{O}$ <br> $21.54 \% \mathrm{Ca} \mathrm{O}$ |
| 100.00 |

(3) 2 Mono and 1 Bisilicate.

2 parts by weight of Monosilicate ( $2 \mathrm{RO}+\mathrm{SiO}_{2}$ ). 1 part ,, Bisilicate ( $\mathrm{RO}+\mathrm{SiO}_{2}$ ).

Quarter Slag.

$$
\begin{aligned}
& \frac{(2 \times 30.58)+46.83}{3}=\frac{107.99}{3}=36.0 \% \mathrm{Si} 0 \\
& \frac{(2 \times 55.54)+42.54}{3}=\frac{153.61}{3}=51.2 \% \mathrm{Fe} \mathrm{O} \\
& \frac{(2 \times 13.08)+10.63}{3}=\frac{38.39}{3}=\frac{12.8 \% \mathrm{CaO}}{100.00} .
\end{aligned}
$$

Half Slag.

$$
\left.\begin{array}{l}
\frac{(2 \times 31 \cdot 33)+47 \cdot 11}{3}=36.8 \% \text { Si O} \\
\frac{(2 \times 45 \cdot 78)+34.86}{3}=42.1 \% \mathrm{Fe} \mathrm{O} \\
\frac{(2 \times 22 \cdot 89)+17 \cdot 43}{3}=\frac{21.1 \% \mathrm{Ca} \mathrm{O}}{100.00}
\end{array}\right\}
$$

Contrast with results above.

Example of Pueblo and Leadville Lead Slag.


Quarter Slag.

$$
\left.\begin{array}{l}
36.0 \% \mathrm{Si} \mathrm{O}_{2}=36 \quad \times \frac{32}{60}=19.20 \\
51.2 \% \mathrm{FeO}=51.2 \times \frac{16}{72}=11.38 \\
12.8 \% \mathrm{CaO}=12.8 \times \frac{16}{56}=3.66
\end{array}\right\} \begin{gathered}
15 \cdot 04: 19 \cdot 20 \\
3: 4
\end{gathered}
$$

Half Slag.

$$
\left.\begin{array}{l}
36.0 \% \operatorname{Si~O}_{2}=36 \quad \times \frac{32}{60}=19.20 \\
42.66 \% \mathrm{Fe} \mathrm{O}=42.66 \times \frac{16}{72}=9.48 \\
21.33 \% \mathrm{CaO}=21.33 \times \frac{16}{56}=6.10
\end{array}\right\} \quad \begin{gathered}
15 \cdot 58: 19 \cdot 20 \\
3 \quad 4
\end{gathered}
$$

| Class of Slag. | Formula. | $x \mathrm{FeO}=4 y \mathrm{CaO}$. |  |  | $x \mathrm{FeO}=2 y \mathrm{CaO}$. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathrm{SiO} \mathrm{O}_{2}$ | Fe 0 | Ca O | SiO 2 | FeO | CaO |
| Subsilicate . | $3 \mathrm{RO}+\mathrm{Si} \mathrm{O}$ | $22^{\prime} 70$ | 61*84 | 15.46 | $23^{\circ} 33$ | $51^{\prime} 12$ | 25.55 |
| Monosilicate | $2 \mathrm{RO}+\mathrm{SiO}_{2}$ | 30.58 | $55^{\circ} 54$ | $13^{*} 88$ | $31^{\prime} 33$ | 45.78 | $22^{\circ} 89$ |
| Sesquisilicate | $4 \mathrm{RO}+3 \mathrm{Si} \mathrm{O} 2$ | $39^{\circ} 78$ | 48.17 | 12.05 | 40.64 | 39.58 | $19^{\circ} 78$ |
| Bisilicate | $\mathrm{RO}+\mathrm{SiO}_{2}$ | 46.83 | 42.53 | $10^{\circ} 64$ | 47'71 | $34^{\circ} 86$ | 17.43 |
| Trisilicate . | $2 \mathrm{RO}+3 \mathrm{SiO}$ | 56.92 | $34^{\circ} 46$ | 8.62 | 57'79 | $28^{\circ} 14$ | $14^{\circ} 07$ |
| 2 Mono and 1 Bi silicate | $5 \mathrm{RO}+3 \mathrm{Si} \mathrm{O} 2$ | $34^{\circ} 58$ | $52 \cdot 34$ | 13.08 | $35 * 38$ | 43.08 | 21.54 |
| 3 Mono and 2 Bi silicate | $8 \mathrm{RO}+5 \mathrm{Si} \mathrm{O}_{2}$ | 35.50 | 51'60 | 12.90 | 36'32 | $42 \cdot 45$ | 21.23 |
| 1 Mono and 1 Ses- | $3 \mathrm{RO}+2 \mathrm{Si} \mathrm{O}_{2}$ | $37 \times 0$ | $50 \cdot 40$ | 12.60 | 37*83 | 41.45 | $20 \cdot 72$ |
| 1 Mono and 2 Sesquisilicate | $10 \mathrm{RO}+7 \mathrm{Si} \mathrm{O} 2$ | $38^{\circ} 14$ | $49^{\circ} 49$ | $12 \cdot 37$ | $38^{\prime} 99$ | $40^{\circ} 67$ | $20^{\circ} 34$ |


| Type. | $x$. | $y$. | Slag formula $5 \mathrm{RO}+3 \mathrm{Si}_{2}$. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\mathrm{Si} \mathrm{O}_{2}$. | Fe 0. | Ca 0 . |
| 1: 4 | $\frac{28}{37}$ | $\frac{9}{37}$ | $34 \cdot 6$ | 52.3 | $13 \cdot 1$ |
| 3: 11 | $\frac{77}{104}$ | ${ }^{27}{ }^{27}$ | $34 \cdot 7$ | $51 \cdot 3$ | $14 \cdot 0$ |
| 2:7 | ${ }^{4} 8$ | ${ }^{18}$ | $34 \cdot 7$ | $50 \cdot 8$ | 14.5 |
| 3: 10 | 79 7 | $\frac{97}{97}$ | $34 \cdot 8$ | $50 \cdot 2$ | $15 \cdot 0$ |
| 1: 3 | $\frac{7}{10}$ | $\frac{3}{10}$ | $34 \cdot 9$ | $48 \cdot 8$ | $16 \cdot 3$ |
| $3: 8$ | $\frac{56}{83}$ | 278 | $35 \cdot 0$ | $47 \cdot 3$ | $17 \cdot 7$ |
| 2: 5 | $\begin{array}{r}35 \\ \hline\end{array}$ | $\frac{1}{5} \frac{8}{3}$ | $35 \cdot 1$ | $46 \cdot 3$ | 18.5 |
| 3: 7 | ${ }^{4} 9$ |  | $35 \cdot 2$ | $45 \cdot 4$ | 19.5 |
| 1: 2 | $\frac{14}{2} 3$ | $\frac{9}{23}$ | $35 \cdot 4$ | $43 \cdot 1$ | 21.5 |
| 3: 5 | $\stackrel{35}{62}$ | $\frac{27}{6}$ | $35 \cdot 6$ | $40 \cdot 2$ | 24.2 |
| 2: 3 | ${ }^{7} 1$ | ${ }^{6} 13$ | $35 \cdot 8$ | 38.5 | $25 \cdot 7$ |

Slags by A. Raht.

| Type. | $\mathrm{Si} \mathrm{O}_{2}$. | Fe 0. | Ca 0. | R 0 . |
| :---: | :---: | :---: | :---: | :---: |
| $\frac{1}{2}$ with 14 R O | $35 \cdot 43$ | $33 \cdot 31$ | $17 \cdot 26$ | $14 \cdot 00$ |
| $\frac{1}{2}$,, 12 RO | 35.43 | $34 \cdot 60$ | 18.00 | $12 \cdot 00$ |
| $\frac{1}{2}$, , 10 R O | 35.43 | $35 \cdot 93$ | 18.63 | 10.00 |
| $\frac{1}{2}, \quad 6 \mathrm{RO}$ | 37.5 | 44.9 | 11.6 | 6.0 |
| $\frac{1}{2} \quad, \quad 4 \mathrm{R}$ O | 36.0 3.98 | $40 \cdot 0$ 31.35 |  |  |
| $\begin{array}{cccc} \frac{1}{2} & , & 17 \mathrm{R} \mathrm{O} \\ \\ \hline \end{array}$ | 35.98 | 31.35 | 15.68 | $17 \cdot 00$ |

## One-half Slag used in E. Helena on account of lack of Siliceous Ores. <br> $3(\mathrm{FeO}) 2 \mathrm{Si}_{2}+(\mathrm{CaO}) 2 \mathrm{SiO}_{2}$. That is at 18 RO . $31 \cdot 38 \mathrm{Si} \mathrm{O}_{2}=100=1 \cdot 2116$ $33.32 \mathrm{Fe} \mathrm{O}=82 \cdot 53=1 \cdot 000$ $17 \cdot 28 \mathrm{CaO}=55=0.667$ <br> $81.98 \quad 2.8786$ <br> $18 \cdot 02$ <br> $100 \cdot 00$

Lime is generally added in the form of limestone; it is used to remove silica; it cleans the slag and lessens its specific gravity, allowing the matte to settle more perfectly. About $15 \% \mathrm{CaO}$ gives the best results for copper ore smelting when plenty of iron is available. A high lime slag makes it low in lead, except when the presence of zinc interferes and requires more iron. When required to slag off a small amount of sulphur, as in iron smelting, it may be got rid of as sulphide of calcium or barium. The sulphur may be considered as equal to half its own amount of silica-really 28 to 60 .

Magnesia is generally added in the form of dolomite. Magnesia has 1.4 times the fluxing power of lime, and gives little trouble when used alone under $8 \%$, but in the presence of Zn or $\mathrm{Al}_{2} \mathrm{O}_{3}$ is objectionable. It makes the slag less fluid, and when high magnesia slags are formed must have at least $20 \%$ iron.

Baryta is used as heavy spar, it makes a slag fluid but heavy; some of it enters the matte as BaS. Matte does not separate well from slags carrying barium.

Zinc decreases the fluidity of the slag and requires more fuel; by entering the matte it decreases its specific gravity and makes it more difficult to settle. Being volatile zinc causes a loss of silver and forms accretions; $10 \% \mathrm{Zn}$ is the maximum limit that should be present in a charge.

Alumina tends to purify a slag, but if over $10 \%$ is apt to make the slag sticky. Used in the form of clay-slate or alumina-bearing rocks; employed when smelting ores rich in lime. Aluminous slags are generally slow running, and require a high heat to make them flow properly.

Iron and Manganese, in the form of oxide or carbonate, are used to flux siliceous ores.

Silica as quartz and natural silicates is used for removing excess of bases.

A wide range in the composition of slags is allowable in
copper smelting, depending on the class of smelting employed; yet the proportion of silica to iron and lime will be found to correspond approximately to definite silicates.

One must determine whether it is cheaper to use a lime or iron flux, and whether conditions are such that it is better to make a concentrating or converting matte. If the matte is lower than, say, $35 \%$ copper, it is generally better to concentrate it by re-smelting, which serves at the same time to reduce the amount of $\mathrm{As}, \mathrm{Sb}, \mathrm{Pb}$, and Zn present. Matte suitable for converting generally ranges between $35 \%$ and $60 \%$ of copper ; if too high it is apt to chill when being transported from the furnace to the converter, and the ore slag is liable to be too rich in copper.

The size of a charge depends on a combination of circumstances, e.g. the size of the furnace and the relative amounts of the various ores to be smelted.

Draw up a table as shown, noting the assays of the various ingredients in their proper column. Take the greatest weight from the chief ore, and proportion the other constituents according to their production, or, if that is capable of regulation, according to the probable requirements for matte and slag formation. It does not matter whether the total weights exceed or are less than that required for the charge, for they can be adjusted later when the relative proportions of the ores and fluxes have been ascertained. If several ores are to be smelted, blend those of small bulk to make a mixture so that there are only two classes of ore to deal with. If desired to blend two ores, one containing $30 \%$ and the other $45 \%$, in order to get a blende of $35 \%$, then-

$$
\begin{aligned}
& 45-30=15 \\
& 35-30=5 ; \frac{5 \times 100}{15}=33.33 \text { pts. by weight of the } 45 \% \text { ore. }
\end{aligned}
$$

The proportion of the $30 \%$ ore required is $100-33 \cdot 33=$ 66.67 parts.

From the quantities assumed in the trial calculations and the assays, calculate the number of lbs. of each constituent, and add those of the same kind together.

The proportion of sulphur burnt off varies with the furnace, the ore, the length of time the charge is in the furnace, the flux, and the pressure of the blast. Of the sulphur that is left most passes into the matte while about $1 \%$ goes into the slag. The amount of sulphur retained for the matte will determine the matte fall. The usual matte fall is from $10: 1$ to $15: 1$. Let us assume in our particular case that there is a loss of $70 \%$ of the sulphur in the ore and concentrates by volatilization and in the slag, then $70 \%$ of 156 lbs . equals

## CHARGE CALCULATION.

Trial Method.


| Desired Compo sition of Slag. | Total S in ore and conc. . . ${ }_{\text {l }} 156$ | Total Cu. . ${ }^{\text {l }}$ 8s ${ }^{\text {c }} 50$ |
| :---: | :---: | :---: |
| $\mathrm{SiO}_{2} \quad 42 \%$ | Less 70\% vol. and in slag . 109 | Lostin slag ${ }^{\text {P12 }}$ |
| Fe 0 |  | Cu available |
| Ca 0 | . ${ }^{47}$ | for matte 78.38 |
| Other com | S in old slag and coke ash |  |
|  |  | $\mathrm{Fe}+$ |
| 100 | atio between S and $\mathrm{Fe}+$ |  |

S. Matte. $\mathrm{Fe}+\mathrm{Cu}$ in matte . . . . $182 \cdot 4$
$\mathrm{Fe} \cdot 104.02$ " Slag formed $42: 100:: 4373=1041$
$\mathrm{Cu} .78^{\circ} 38$ " If loss of Cu in slag is $0.3 \%$, then

$$
\overline{243^{\circ} 20}
$$

Total Fe . $456 \times 70$
Required for
matte . . $104{ }^{\circ} 02$
Available
for slag . 352 68
Slag.
Assume this to $\mathrm{SiO}_{2} 437{ }^{\circ} 3=233^{\circ} 2$ acid units oxygen be $95 \%$ of total $\mathrm{FeO} 453^{\circ}=100^{\circ} 7$ basic " " matte, which $\mathrm{CaO} 49^{\circ} 6=14^{\circ} 1$,, , , would then be 256 lbs . of $300^{\circ} 6 \%$ Cu .
$352 \cdot 68 \times \frac{9}{7}=453 \cdot 4 \mathrm{FeO}$
Matte-fall. $\frac{256 \times 100}{1620}=15.8 \%$
$\mathrm{BU}: \mathrm{AU}$ as $114^{\circ} 8: 233^{\circ} 2=1: 2^{\circ} 03$ or approx. R O Si O 2

109 lbs., leaving 47 lbs . sulphur available for matte making, plus 13.8 lbs . in the slag and coke ash, from which there was little or no loss, making $60^{\circ} 8 \mathrm{lbs}$. altogether.

| $\mathrm{Cu}_{2}$ | $126=$ | $51.2 \%$ | 74\% | 74 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Fe | $56=$ | $22 \cdot 8$ | \} $74 \%$ | $\frac{74}{26}$ | $\mathrm{Se}_{\mathrm{S}} \mathrm{Cu}=3$ |
| $\mathrm{S}_{2}$ | $64=$ | $26 \cdot 0$ | 26\% | 26 |  |
|  | 246 | 00\% 0 |  |  |  |

The matte formed may or may not have the above composition, and actually all the copper in the matte is not combined as $\mathrm{Cu}_{2} \mathrm{~S}$, but for the present we will take it that the sulphur constitutes about one-quarter the weight of the matte, so multiplying the matte-making sulphur by 3 will give the amount of $\mathrm{Fe}+\mathrm{Cu}$ in the matte, viz. 182.4 lbs .

To determine the quantity of slag formed :-
As $\mathrm{SiO}_{2}$ in assumed slag : $100:: \mathrm{lbs} . \mathrm{SiO}_{2}$ in charge : weight of slag 42

$$
: 100:: 437 \times 3
$$

: 1041
Assume the loss of copper in the slag to be $0.3 \%$, then $\frac{1041 \times 0.3}{100}=3.123 \mathrm{lbs} . \mathrm{Cu}$. Deduct this from the 81.5 lbs . in the charge, we then have 78.38 lbs . copper available for matte making. Deducting the 78.38 lbs . copper from the 182.4 lbs . combined Fe and Cu leaves 104.021 lbs . in the matte. If we consider the $\mathrm{Fe}, \mathrm{Cu}$, and S to form $95 \%$ of the total matte, we have 256 lbs. matte containing $30.6 \% \mathrm{Cu}$.

Note down the composition of the slag it is desired to make. If the available sulphur makes too low a matte, we may have to abandon the slag originally desired and increase the $\mathrm{SiO}_{2}$ of the slag in order to reduce the $S$ in the matte by smelting slower. This increase of $\mathrm{SiO}_{2}$ can only go on to a stage when the slag becomes uneconomical.

The balance of the Fe not required by the matte passes into the slag, and is calculated as its equivalent of FeO .
$\mathrm{Fe}: \mathrm{FeO}:: 56: 72 \frac{72}{56}=\frac{9}{7}$; therefore, to convert Fe to Fe O
multiply the Fe by $\frac{9}{7}$
The CaO in limestone, allowing for reasonable impurities, is approximately $50 \%$, therefore the required amount of lime has to be multiplied by 2 to bring it to limestone.

The combined weights of $\mathrm{SiO}_{2}, \mathrm{FeO}$, and CaO in the slag amounts to $940 \cdot 3$, but these constituents only form $91 \%$
of the desired slag, so the total weight of the slag will be $91: 940 \cdot 3:: 100: 1033$.

Total wt. of slag : total wt. of constituent :: 100 : theoretical \% of constituent.

| 1033 | $437 \cdot 3$ | :: 100 : | $42 \cdot 3 \% \mathrm{Si}_{2}$ |
| :---: | :---: | :---: | :---: |
| 1033 | $453 \cdot 4$ | :: 100 : | $43 \cdot 9 \% \mathrm{Fe} 0$ |
| 33 | $49 \cdot 6$ | :: 100 : | $4 \cdot 8 \% \mathrm{Ca} 0$ |
|  | $940 \cdot 3$ |  | 91. |

If the theoretical result comes within $2 \%$ of the desired slag, that is considered near enough, owing to variations in the ores, imperfect weighing, and other irregularities. If over $2 \%$ another trial calculation must be made with other figures.

The matte fall is-

$$
\begin{gathered}
\text { Weight of charge : weight of matte :: } 100: x \\
1620 \quad: \begin{array}{cc}
256
\end{array} \quad: 100: 15 \cdot 8
\end{gathered}
$$

Supposing the ore, concentrates, and old slags available form the commercial basis of the charge, and it is desired to use only a limestone flux, there would be no occasion to make a trial calculation, but the required amount of limestone could be obtained by a straight out calculation. A bisilicate slag requires to have twice the percentage of 0 on the silica or acid side as on the base side.

| Si 28 | Ca 40 | $\mathrm{Fe} 56 ; 72: 60:: 1: 0.833 \mathrm{Fe} \mathrm{O}$ factor. |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{O}_{2} 32$ | O | 16 | O | $\mathbf{1 6} ; 56: 60:: 1: 1: 07 \mathrm{CaO}$ factor. |
| $\overline{60}$ | $\overline{56}$ | $\overline{72}$ |  |  |

The available Fe for slag is $414-104=310 \times \frac{9}{7}=398 \cdot 6 \mathrm{Fe} 0$; multiply this by the factor $0.833=332.03 \mathrm{Si}_{2}$ satisfied.

The $\mathrm{Si}_{\mathrm{O}} \mathrm{O}_{2}$ less that in the limestone and ironstone as shown in the table is 424 lbs ., deduct 332.03 satisfied by the Fe O , this leaves 91.97 unsatisfied. To find the amount of CaO necessary to form a bisilicate, divide the $\mathrm{Si}_{2}$ in the limestone by 1.07 , in our case $7 \%$ equals 6.5 . Subtract this from the $47 \% \mathrm{CaO}$ in the limestone, which leaves $40.5 \% \mathrm{CaO}$ available. The 91.97 lbs . $\mathrm{Si}_{2}$ to be fluxed with CaO is divided by the factor 1.07 , which gives 85 . As the available CaO in the limestone is $40.5 \%$, then-
$40 \cdot 5: 85:: 100: 209 \cdot 9 \mathrm{lbs}$. limestone in the charge.

| TABLE A. <br> For ascertaining then amounts of Bases to given amounts of Si slag. | cessary convert $\mathrm{O}_{2}$ into | Table B. <br> For ascertaining the amounts of $\mathrm{Si} \mathrm{O}_{2}$ to given amounts of ba slag. | cessary convert es into |
| :---: | :---: | :---: | :---: |
| One part by weight of $\mathrm{Si} \mathrm{O}_{2}$ requires- | Parts by weight of bases. | One part by weight of base rèquires- | Parts by weight of silica |
| For Monosilicate |  | For Monosilicates- |  |
| Ca 0 | 1.86 | CaO | 0.535 |
| Mg 0 | $1 \cdot 33$ | Mg 0 . | 0.750 |
| $\mathrm{Al}_{2} \mathrm{O}_{3}$ | $1 \cdot 14$ | $\mathrm{Al}_{2} \mathrm{O}_{3}$ | 0.873 |
| Fe 0 | $2 \cdot 40$ | Fe 0 . | $0 \cdot 416$ |
| Mn 0 | $2 \cdot 36$ | Mn 0 . | $0 \cdot 422$ |
| For Bisilicates- |  | For Bisilicates- |  |
| Ca 0 | 0.93 | CaO | 1.070 |
| Mg 0 | $0 \cdot 66$ | Mg 0. | 1.500 |
| $\mathrm{Al}_{2} \mathrm{O}_{3}$ | 0.57 | $\mathrm{Al}_{2} \mathrm{O}_{3}$ | 1.747 |
| Fe 0 | $1 \cdot 20$ | Fe 0 . | 0.833 |
| Mn 0 . | $1 \cdot 18$ | Mn 0 . | 0.845 |
| For Sesquisilicates- |  | For Sesquisilicates |  |
| CaO . . . | $1 \cdot 24$ | CaO . . | 0.803 |
| Mg O | 0.88 | Mg 0 . | $1 \cdot 125$ |
| $\mathrm{Al}_{2} \mathrm{O}_{3}$ | $0 \cdot 76$ | $\mathrm{Al}_{2} \mathrm{O}_{3}$ | 1.310 |
| Fe 0 | $1 \cdot 60$ | Fe 0 . | 0.625 |
| Mn O | 1.57 | Mn 0 . | 0.633 |
| Ratio of molecular weight of bases to that of $\mathrm{Si} \mathrm{O}_{2}$;$\begin{gathered} 2 \mathrm{CaO} \\ \mathrm{SiO}_{2} \frac{112}{60}=1 \cdot 86 \end{gathered}$ |  | Ratio of molecular weight of $\mathrm{Si}_{2}$ to that of the base $\begin{aligned} & \mathrm{Si} \mathrm{O}_{2} \\ & 2 \mathrm{CaO} \\ & \mathrm{Ca} \\ & 112\end{aligned}=0.5357$ |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |

The use of these tables saves much calculation. If the slag-forming bases are multiplied by their corresponding factors in table B , and the amounts of $\mathrm{SiO}_{2}$ so formed added up, this can be deducted from the amount of $\mathrm{SiO}_{2}$ in the ore should that be in excess, in which case the balance of $\mathrm{Si}_{2}$
must be multiplied by the factor of the base in table A with which it is intended to flux it. If the flux is lime, then as the lime is generally added in the form of limestone, $\begin{array}{ll}\mathrm{Ca} \mathrm{C} \\ \mathrm{Ca} \mathrm{O} & \frac{100}{56}=1785 \text {, the amount of lime required must be }\end{array}$ multiplied by $1 \cdot 785$ in order to ascertain the necessary amount of limestone.

## Graphic Method.

On squared paper draw two lines at right angles to each other and divide them into equal parts, making zero the point of intersection. Let the horizontal line represent the bases, and the vertical the $\mathrm{Si}_{2}$ of a monosilicate. From the point where the two lines meet, draw lines to represent different bases required in the formation of a slag at such an angle that the $\mathrm{Al}_{2} \mathrm{O}_{3}$ line cuts the horizontal line opposite $10 \mathrm{Si} \mathrm{O}_{2}$ at $11 \cdot 3$, the Mg O at $13 \cdot 3$, the CaO O e, and Mn at $18 \%$, FeO and MnO at 24, and BaO at 50.7 . For convenience in calculating the fluxes required, lines for $\mathrm{Fe}_{2} \mathrm{O}_{3}$ cutting the $10 \mathrm{Si} \mathrm{O}_{2}$ line at $26 \cdot 6$, and $\mathrm{CaCO}_{3}$ at $33 \cdot 3$ are added. The atomic weights of Fe and Mn being so close to the molecular weights of CaO , the same line does for all of them.

The above distances are determined as follows:-


Likewise 2 Mg 0 . $\mathrm{SiO}_{2}=60: 80:: 10: 13 \cdot 2$
2 Fe O. $\mathrm{Si}_{2}=60: 144:: 10: 24$
2 BaO . $\mathrm{SiO}_{2}=60: 304:: 10: 50 \cdot 7$
$2 \mathrm{Al}_{2} \mathrm{O}_{3} .3 \mathrm{Si}_{2}=180: 204:: 10: 11 \cdot 3$
Alumina having the composition $\mathrm{R}_{2} \mathrm{O}_{3}$ requires $3 \mathrm{Si} \mathrm{O}_{2}$ to form a monosilicate.
$\mathrm{Fe}_{2} \mathrm{O}_{3}$ is equal to 2 Fe O from a slag-making point of view; therefore, as the molecular weight of $\mathrm{Fe}_{2} \mathrm{O}_{3}$ is 160 ,

$$
60: 160:: 10: 26 \cdot 6
$$

and as $2 \mathrm{CaCO}_{3}$ is equal to 2 CaO , and the molecular weight of $2 \mathrm{CaCO}_{3}$ is 200 , then-

$$
60: 200:: 10: 33 \cdot 3
$$

Two vertical lines should be drawn parallel to the monosilicate line, one divided into double the number of spaces in the same distance as the monosilicate line to represent bisilicates, the other into one and a half the number of spaces to represent

the sesquisilicates. All sesquisilicates may be resolved into a monosilicate and a bisilicate, for instance $\mathrm{R}_{4} \mathrm{Si}_{3} \mathrm{O}_{10}=$ $\mathrm{R}_{2} \mathrm{Si}_{4}+2\left(\mathrm{R} \mathrm{Si}_{3}\right)$, and $\mathrm{R}_{8} \mathrm{Si}_{9} \mathrm{O}_{30}=\mathrm{R}_{4} \mathrm{Si}_{3} \mathrm{O}_{12}+2\left(\mathrm{R}_{2} \mathrm{Si}_{3} \mathrm{O}_{9}\right)$.

To use the diagram it is advisable to employ set squares. By following the horizontal line cut by each base-line above the percentage of any particular base given by analysis, one can ascertain the amount of $\mathrm{SiO}_{2}$ required in order to form the particular class of slag desired according to the silica line read off. The excess of each base or $\operatorname{Si} \mathrm{O}_{2}$, as the case may be, over that necessary to form the slag considered advisable, can then be ascertained by reference to the analysis. By using the diagram, and noting the corresponding amount of $\mathrm{SiO}_{2}$ or base necessary to satisfy the excess, the amount of flux required can be ascertained. One can also find out from the analysis of a slag whether it is of the type required, by comparing the amount of $\mathrm{Si}_{2}$ in the analysis with that calculated as necessary to combine with the bases present. In this way we can ascertain whether or not an excess of flux is being used.

## WET AND DRY BULB THERMOMETERS.

Used to determine the humidity of air (i.e. the percentage relation between the amount of moisture present and the amount which air saturated at the same temperature would contain). To calculate the humidity and the weight of moisture in a cubic foot of air use Glaisher's well-known tables.

For preference use thermometers with the graduations marked on the glass itself: test the accuracy of the thermometer before using it. Use pure water for the wet bulb, and see that the muslin leading from the bulb to the water is clean. The readings should be taken in a draught: if the air is stagnant wave the thermometer vigorously till the readings of both are constant.

List of Minerals, giving their Composition, Hardness, Specific Gravity, Crystalline System, and Colour.
C. = colourless, W. = white, R. = red, Bl. = blue, Y. = yellow, $\mathrm{Ge} .=$ green, Br. = brown, B. = black, V. = violet, Gr. = grey, Or. = orange.

Scale of Hardness. $-1=$ Talc, $2=$ Gypsum, $3=$ Calcite, $4=$ Fluorspar, $5=$ Apatite, $=$ Orthoclase, $7=$ Quartz, $8=$ Topaz, $9=$ Corundum, $10=$ Diamond.

Crystalline Systems.-I Isometric, II Tetragonal, III Hexagonal, IV Orthorhombic, V Monoclinic, VI Triclinic, O Amorphous.

The inclined hemihedral forms for I-IV are indicated by $\times$, the parallel hemihedral forms by $\pi$.

Scale of Fusibility (v. Kobell).-1 Antimonite, 2 Natrolite, 3 Alamandite, 4 Actinolite, 5 Orthoclase (smelts only in small splinters in the hottest part of the blowpipe flame), 6 Bronzite (only the sharp edges of small splinters fuse round).

| Name. | Composition. | Hardness. | Specific Gravity. |  | Colour. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Actinolite | $(\mathrm{Ca}, \mathrm{Mg}, \mathrm{Fe})_{\mathrm{SiO}^{3}}$ | 5-6 | 3.02-3.16 | V | Ge. |
| Adamite . | $\mathrm{Zn}^{2}(\mathrm{OH}) \mathrm{AsO}^{4}$. | $3 \cdot 5$ | $4 \cdot 3$ | V? | Y. Bl. R, Ge. |
| Adularia | $\mathrm{K}^{2} \mathrm{O}, \mathrm{Al}^{2} \mathrm{O}^{3}, \mathrm{SiO}^{2}$ | 6-6.5 | $2 \cdot 5-2 \cdot 69$ | V |  |
| Agalmatolite | $\begin{aligned} & \mathrm{K}^{2} \mathrm{O}, 3 \mathrm{Al}^{2} \mathrm{O}^{3} \\ & 9 \mathrm{SiO}^{2}, 3 \mathrm{H}^{2} \mathrm{O} \end{aligned}$ | $2 \cdot 5-3$ | $2 \cdot 75-2 \cdot 9$ | 0 | Y. Gr. R. Ge. |
| Agate | $\mathrm{SiO}^{2}$. . . | 7 | 2.5-2.8 | 0 | R. Ge. Gr. C. Br. W. |
| Aikinite . | $\mathrm{Pb}^{2} \mathrm{Cu}^{2} \mathrm{Bi}^{2} \mathrm{~S}^{6}$ | $2-2 \cdot 5$ | $6 \cdot 1-6 \cdot 8$ | IV | Gr. B. |
| Alabandite | $\mathrm{MnS} \mathrm{SO}^{3}{ }^{\text {a }}$ | $3 \cdot 5-4$ | $3 \cdot 9.4$ | I | B. Br. |
| Alabaster | $\mathrm{CaO}, \mathrm{SO}^{3}+{ }_{2}^{+} \mathrm{H}^{2} \mathrm{O}$ | 1-5-2 | $2 \cdot 4$ | 0 | W. |
| Albite | $\mathrm{Na}^{2} \mathrm{O}, \mathrm{Al}^{2} \mathrm{O}^{3}$ $6 \mathrm{SiO}^{2}$ | 6-7 | $2 \cdot 5-2 \cdot 64$ | VI | C. Gr. Ge. Bl. |
| Allophane | $\mathrm{Al}^{2} \mathrm{SiO}^{5}, 5 \mathrm{H}^{2} \mathrm{O}$. | 3 | $1 \cdot 8-1 \cdot 9$ | 0 | Bl. Ge. Y. Br. |
| Almandite (garnet) | $3 \mathrm{FeO}, \mathrm{Al}^{2} \mathrm{O}^{3}$ $3 \mathrm{SiO}^{2}$ | 6.5-7.5 | 3-4.3 | I | R. RBr . |
| Altraite | $\stackrel{\mathrm{PbTe}}{\mathrm{Al}^{2} \mathrm{O}^{3}} \mathrm{SO}^{\dot{3}} \quad$. | 3-3.5 | $8 \cdot 2$ | 1 | W. Y. |
| Aluminite | $\mathrm{Al}^{2} \mathrm{O}^{3}, \mathrm{SO}^{3}, \mathrm{H}^{2} \mathrm{O}$ | 1-2 | $1 \cdot 6$ | 0 | W. |
| Alunite | $\begin{gathered} \mathrm{K}^{2} \mathrm{O}, \mathrm{Al}^{2} \mathrm{O}^{3} \\ 4 \mathrm{SO}^{3}, 24 \mathrm{aq} . \end{gathered}$ | 2-2.5 | 1-7-2 | $\mathrm{I} \pi$ | C. Y. Gr. |
| Amalgam. . | $\mathrm{Ag}+\mathrm{Hg}, 2{ }^{\text {a }}$ | 3-3.5 | $13 \cdot 7-14 \cdot 1$ | V | W. (silver). |
| Amazon stone (orthoclase) | $\mathrm{K}^{2} \mathrm{O}, \mathrm{Al}^{2} \mathrm{O}^{3}, 6 \mathrm{SiO}^{2}$ | 6-6.5 | 2.4-2.6 | V | Ge. |
| $\begin{aligned} & \text { Ainber } \\ & \text { (succinite) } \end{aligned}$ | Fossil resin . | $2-2.5$ | $1 \cdot 0$ | 0 | W. Y. Br. R. |

IIST OF MINERALS (continued).

| Name. | Composition. | Hardness. | Specific Gravity. |  | Colour. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Amblygonite | $\mathrm{Al}^{2} \mathrm{O}^{3}, \mathrm{P}^{2} \mathrm{O}^{5}$ 2( $\mathrm{LiF}, \mathrm{LiOH}$ ) | 6 | $3 \cdot 05-3 \cdot 1$ | VI | W. Gr. Ge. |
| Ambrite | $\mathrm{C}, \mathrm{O}, \mathrm{H}$. . | 2 | $1.034$ |  | Y. Gr. Ge. |
| Amethyst (quartz) | $\mathrm{SiO}^{2}$. | 7 | $2 \cdot 64-2 \cdot 66$ | III | Bl. V. |
| Amphibole . | $\mathrm{SiO}^{2}(\mathrm{Ca}, \mathrm{Mg}$, <br> $\mathrm{Fe}, \mathrm{Mn}, \mathrm{Na}^{2}$, | 5-6 | $2 \cdot 9-3 \cdot 4$ | V | C. Ge. B. |
| Analcime (analcite) | $\begin{aligned} & \mathrm{Na}^{2} \mathrm{O}, \mathrm{Al}^{2} \mathrm{O}^{3} \\ & 4 \mathrm{SiO}^{2}, 2 \mathrm{H}^{2} \mathrm{O} \end{aligned}$ | 5-5.55 | $2 \cdot 29$ | I | C. W. R. Gr. Ge. Y. |
| Anatase | $\mathrm{TiO}^{2}$. . . | 5.5-6 | $3 \cdot 8-3 \cdot 9$ | II | C. Br. B. Bl. |
| Andalusite . | $\mathrm{Al}^{2} \mathrm{O}$ | $7 \cdot 5$ | 3-3.2 | IV | Gr. R. Br. W. |
| Andesine (andesite) | $\left(\mathrm{CaNa}{ }^{2}\right) \mathrm{O}, \mathrm{Al}^{2} \mathrm{O}^{3}$, | 5-6 | $2 \cdot 65-2 \cdot 74$ | VI | C. Y. Gr. W. Ge. R. |
| Andradite (garnet) | $\mathrm{Ca}^{3} \mathrm{Fe}^{2} \mathrm{Si}^{3} \mathrm{O}^{12}$. | 6.5-7.5 | 3.6-4 | I | W. Y. Gr. R. |
| Anglesite . | $\mathrm{PbO}, \mathrm{SO}^{3}$ | $2 \cdot 7-3$ | 6-6.37 | IV | C. Y. Ge. Gr. |
| Anhydrite | $\mathrm{CaO}, \mathrm{SO}^{3}$ | 3-3.5 | $2 \cdot 8-2.98$ | IV | C. W. Gr. Bl. |
| Annabergite. | $3 \mathrm{NiO}, \mathrm{As}^{2} \mathrm{O}^{5}+$ | $2-2.5$ | $3-3 \cdot 1$ | V | Ge. W. |
| Anorthite | $\mathrm{CaO}, \mathrm{Al}^{2} \mathrm{O}^{3}$, | 6-7 | $2 \cdot 6-2 \cdot 78$ | VI | W. Gr. R. C. |
| Anthophyllite | $(\mathrm{Mg}, \mathrm{Fe}) \mathrm{O}, \mathrm{SiO}^{2}$ | $5 \cdot 5$ | 3.18-3.22 | IV | Br. Gr. Ge. Y. |
| Anthracite . | C ( $95 \%$ ) | 2-2.5 | $1 \cdot 3-1 \cdot 75$ | O | B. |
| Antimonite (stibnite) | $\mathrm{Sb}^{2} \mathrm{~S}^{3}$ | 2 | $4 \cdot 5$ | IV | Gr. B. |
| Antimony | $\mathrm{Sb}(\mathrm{Ag}, \mathrm{As}, \mathrm{Fe})$ | 3-3.5 | 6.6 | III $\times$ | W. Gr. |
| Apatite - | $\begin{aligned} & 3 \mathrm{Ca}^{3} \mathrm{P}^{2} \mathrm{O}^{3}+ \\ & \mathrm{CaCl}^{2}\left(\mathrm{CaF}^{2}\right) \end{aligned}$ | 5 | 2.9-3.2 | III $\pi$ | $\begin{aligned} & \text { C. Ge. Bl. Y. } \\ & \text { V.W. R. Gr. } \\ & \text { Br. } \end{aligned}$ |
| Apophyllite | $4\left(\mathrm{H}^{2} \mathrm{CaSi}\right.$ | 4.5-5 | 2.3--2.4 | II | C. R. Gr. Ge. |
| Aquamarine. | $\mathrm{Al}^{2} \mathrm{O}^{3}, 3 \mathrm{BeO}$, $6 \mathrm{SiO}^{2}$ | 7-5-8 | 2.6-2.7 | III | Bl-Ge. |
| Aragonite | $\mathrm{CaOCO}^{2}$. . | 3.5-4 | $2 \cdot 95$ | IV | C. W. Y. Gr. Ge. V. |
| Argentite | $\mathrm{Ag}^{2} \mathrm{~S}$ | 2-2.5 | $7 \cdot 1-7 \cdot 36$ | I | Gr. |
| Arkansite (brookite) | $\mathrm{TiO}_{2}$ | 5.5-6 |  | IV? | $\underset{\text { Gr. Y. R. B. }}{\text { Br. }}$ |
| $\underset{\text { (native) }}{\text { Arsenic }}$ | As (traces of $\mathrm{Sb}, \mathrm{Ag}, \mathrm{Fe}$, | $3 \cdot 5$ | $5 \cdot 9$ | III $\times$ | W. Gr. B. |
| Arsenolite | $\mathrm{As}^{2} \mathrm{O}^{3}$ | $1 \cdot 5$ | , | I |  |
| Asbestos | $(\mathrm{Mg}, \mathrm{Ca}) \mathrm{O}, \mathrm{SiO}^{2}$ | 5 | $3 \cdot 02-3 \cdot 1$ | V | W. Ge. |
| (amianthus) | C (76\%) H, 0 . | 1-2 | $1-1 \cdot 7$ | 0 | Br. B. |

List of Minerals (continued).

| Name. | Composition. | Hardness. | Specific Gravity. |  | Colour. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Atacamite | $3 \mathrm{CuO}, \mathrm{CuCl}^{2},$ | $3-3 \cdot 5$ | 4-3.7 | IV | Ge. |
| Augite (pyroxene) | $\begin{aligned} & \left(\mathrm{Ca}, \mathrm{Mg}, \underset{\mathrm{Fe}}{ } \mathrm{SiO}^{2}\right. \\ & \mathrm{SiO}^{2} \end{aligned}$ | 5-6 | 3.2-3.5 | V | B. Gr. Ge. Br. |
| Aurichalcite. | $2 \mathrm{CuO}, 3 \mathrm{ZnO}$, $2 \mathrm{CO}^{2}, 3 \mathrm{H}^{2} \mathrm{O}$ | 2 | ... | ? | Ge |
| Autunite (uranite) | $\begin{gathered} 2 \mathrm{CO}^{2}, 3 \mathrm{H}^{2} \mathrm{O} \\ \mathrm{CaU}^{2} \mathrm{P}^{2} \mathrm{O}^{2}+ \\ \text { 10aq } \end{gathered}$ | 2-2.3 | 3-3.2 | IV | Y. |
| Aventurine . | Partly quartz, partly felspar | ... | ... | $\ldots$ | Y. R. Br. Gr. |
| Axinite | partly felspa $\left(\mathrm{CaO}, \mathrm{Al}^{2} \mathrm{O}^{3}\right)$, | $6 \cdot 5-7$ | $3 \cdot 3$ | VI | C. Br. V. Gr. |
| Azurite | $\mathrm{CuO}, \mathrm{H}^{2} \mathrm{O}$, 2(CuO, $\mathrm{CO}^{2}$ ) | $3 \cdot 5-4 \cdot 2$ | $3 \cdot 5-3 \cdot 8$ | v | B1. |
| Babingtonite | $9(\mathrm{CaFeMn}) \mathrm{SiO}^{3}$ | 5•5-6 | $3 \cdot 4$ | VI | B. |
| Barytes (heavyspar) | $\mathrm{BaO}, \mathrm{SO}^{3}$. | $2 \cdot 5-3 \cdot 5$ | 4.4-4.7 | IV | C. Y. Gr. Bl. R. Br. |
| Barytocalcite | $\mathrm{BaOCO}^{2}$ | 4 | $3 \cdot 6$ | V | \%. Gr. Y. Ge. |
| Basanite (touchstone) | $\mathrm{SiO}^{2}$ impure with Fe , \&c. | 7 | 2.8 | 0 | B. |
| Beauxite . | $\mathrm{Al}^{2}\left(\mathrm{Fe}^{2}\right) \mathrm{O}^{3}+2 \mathrm{aq}$ | ... | 2.5 | 0 | . B |
| Beryl | 31 | 7-5-8 | $2 \cdot 67-2 \cdot 7$ | III | Ge. Y. Bl. W. |
| Bieberite (co- | $\mathrm{CoO}, \mathrm{SO}^{3}$ | ... | $1 \cdot 9$ | v | R. |
| Biotite. | $\begin{aligned} & \mathrm{K}^{4} \mathrm{SSO}^{4},(\mathrm{Fe}[\mathrm{Mg}])^{2} \\ & \mathrm{SiO}^{2}+(\mathrm{Al}+(\mathrm{Fe}])^{2} \end{aligned}$ | 2.5-3 | $2 \cdot 7-3 \cdot 1$ | V | Ge. Br. B. Gr. |
| Bismite (bismuth ochre) | ${ }^{\mathrm{Si}^{2} \mathrm{O}^{3}}$ | Soft | $4 \cdot 3-4 \cdot 7$ | ? | Gr. Y. Ge. |
| Bismuth (native) | $\mathrm{Bi}(\mathrm{As}, \mathrm{S}, \mathrm{Te})$. | 2-2.5 | $9 \cdot 7$ | IIIX | W. R. |
| Bismuthinite | $\mathrm{Bi}^{2} \mathrm{~S}^{3}$ | 2.0 | 6.4-7.2 | IV | W. Gr. Y |
| Bismutite - | $\mathrm{Bi}^{2} \mathrm{O}^{3}, \mathrm{CO}^{2}$ | $4-4 \cdot 5$ | $6 \cdot 8-6.9$ | ? | Gr. Ge. Y. W. |
| Blende (sphalerite) | ZuS | 3.5-4 | 3.9-4.2 | Ix | Y. Br. Ge. B. |
| Blodite. . | $\mathrm{Na}^{2} \mathrm{O}, \mathrm{MgO},$ $2 \mathrm{SO}^{3}, 4 \mathrm{H}_{0} \mathrm{O}$ | $2 \cdot 5-3 \cdot 5$ | $2 \cdot 25$ | V | C. Ge. Gr. R. |
| Bole (halloysite) | Ferruginous clay | 1-2 | 2-2.5 | 0 | Br. Y. B |
| Boracite ${ }^{\text {a }}$ | $\mathrm{Mg}^{7} \mathrm{Bo}^{16} \mathrm{O}^{30} \mathrm{Cl}^{2}{ }^{2}$. | 7 | $2 \cdot 97$ | I $\times$ | C. Gr. Ge. Y. |
| Borax (tinkal) | $\mathrm{Na}^{2} \mathrm{Bo}^{4} \mathrm{O}^{7}$, $10 \mathrm{H}^{2} \mathrm{O}$ | $2-2 \cdot 5$ | 1.71 | V | C. W. Gr. Bl. Ge. |
| Bornite | $3 \mathrm{Cu}^{2} \mathrm{~S}, \mathrm{Fe}^{2} \mathrm{~S}^{3}$. | 3 | $4 \cdot 4-5 \cdot 5$ | I | R. Br. |
| Boulangerite | $3 \mathrm{PbS}+\mathrm{Sb}^{2} \mathrm{~S}^{3}$ | 2.5-3 | 5•7-6 |  | Gr. |
| Bournonite. | $\mathrm{Sb}^{2} \mathrm{~S}^{3}, 2 \mathrm{PbS}$, $\mathrm{Cu}^{2} \mathrm{~S}$ | $2 \cdot 5-3$ | $5 \cdot 7-5 \cdot 87$ | IV | Gr. |

List of Minerals (continued).

| Name. | Composition. | Hardness. | Specific Gravity. |  | Colour. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Braunite | Mn | 6-6.5 | 4.7-4.9 | II | Br. B. |
| Bred bergite (garnet) | $(\mathrm{CaMg})^{3} \mathrm{Fe}^{2 \mathrm{Si}^{3}} \mathrm{O}^{12}$ | $6 \cdot 5-7 \cdot 5$ | 3.2-4.3 | I |  |
| Breithauptite | $\mathrm{NiSb} \cdot$ | 5 | 7.5-7.6 | III | R. |
| Bronzite (enstatite) | $\mathrm{MgO}, \mathrm{SiO}^{2}$. | $5 \cdot 5$ | 3.12-3.3 | IV | Br. Y. Gr. Ge. |
| Brookite ${ }^{\text {(enstate }}$ | $\mathrm{TiO}^{2}$. | 5.5-6 | 4 | IV? | Br. Y. R. B. |
| (arkansite) | C | ... | 1/2-1/4 | 0 |  |
| (lignite) |  | $2 \cdot 5$ | $2 \cdot 35$ | III $\times$ |  |
| Brucite . |  | 2.5 | $2 \cdot 35$ | III $\times$ | B1. |
| Cacholong | $\mathrm{SiO}^{2}+3-9$ | 5-6 | 2 | 0 | R. |
| Cacoxenite . | 2 F | ... | $2 \cdot 3$ | V. or | Y. |
| Cairngorm | $\mathrm{SiO}^{2}$. | 7 | 2.5-2.8 | III | Y. Br. |
| Calamine (quartz) |  | $4 \cdot 5-5$ | 3•1-3.9 | IV | C. W. |
|  |  |  | $31-3$ | IV | R. Br. Gr. |
| Calcite | $\mathrm{CaO}, \mathrm{CO}^{2}$. | 2.5-3 | $2 \cdot 723$ | III $\times$ | C. Ge. Gr. Br. |
|  |  |  |  |  | R. Bl. V. Y. <br> B. |
| Caledonite | $\begin{array}{r} 5 \mathrm{PbSO}^{4}+3 \mathrm{H}^{2} \\ \mathrm{CuO}^{2}+2 \mathrm{H}^{2} \end{array}$ | 2.5-3 | $6 \cdot 4$ | v | Gr. |
|  | $\mathrm{CuO}^{2}+\mathrm{PbO}^{2}$ |  |  |  |  |
| Calomel . | $\mathrm{Hg}^{2} \mathrm{Cl}^{2}$ | 1-2 | 6.5 | IIT |  |
| Cancrinite (nepheline) | $(\mathrm{NaK})^{2} \mathrm{O}, \mathrm{Al}^{2} \mathrm{O}^{3}$ | 5-6 | $2 \cdot 45$ | III | $\begin{aligned} & \text { Gr. Bl. R. Ge. } \\ & \text { Y. W. } \end{aligned}$ |
| Carnallite | $\mathrm{KCl}, \mathrm{MgCl}^{2},$ | ... | 1.618 | IV | C. R. |
| Carnelian | $\mathrm{SiO}^{2}$ with $\mathrm{Fe}^{2} \mathrm{O}^{3}$ | 7 |  | 0 | R. Br. |
| Cassiterite | $\mathrm{SnO}^{2} \text { (up to } 9 \%$ | 6-7 | $6 \cdot 4-7 \cdot 1$ | II | Y. Br. Gr. R. |
| Cats-eye |  | 7 | $2 \cdot 6$ | $\bigcirc$ |  |
| Celestine | $\mathrm{SrO}, \mathrm{SO}^{3}$ - | 3-3.5 | $3 \cdot 96$ | IV | ${ }_{\text {C. W. W. }}$ R. $\mathrm{Bl}^{\mathrm{Bl}}$. |
| Cerargyrite Cerite | $\left.{ }_{2(\mathrm{Ce}, \mathrm{La},}^{\mathrm{Ag}} \mathrm{D}\right)$ | $1-1.5$ | $\begin{gathered} 5 \cdot 6 \\ 4 \cdot 9-5 \end{gathered}$ | IV | Ge. Gr. V. W. Br. R. |
| Cerussite | $\mathrm{PbO}, \mathrm{CO}^{2}{ }^{\text {2 }}{ }^{\text {a }}$, | 3-3.5 | $6 \cdot 4$ | IV |  |
| Cervantite |  | 4-5 |  |  |  |
| Chabazite | CaO, | 4-5 | 㖪 | IIIX | C. R. |
| Chalcanthite | $\mathrm{CuO}, \mathrm{SO}^{3}, 5 \mathrm{H}^{2} \mathrm{O}$ | $2 \cdot 5$ | 22 | VI |  |
| Chalcedony (quartz) | $\mathrm{SiO}^{2}$. | 7 | $2 \cdot 65$ | 0 | W. Gr. B. Y. Ge. R. Bl. |
| Chalcopyrite | $\mathrm{Cu}^{2} \mathrm{~S}, \mathrm{Fe}^{2} \mathrm{~S}^{3}$. | 3.5-4 | 4•1-4.3 | II $\times$ |  |
| (copper <br> pyrites) |  |  |  |  |  |

COMPOSITION, HARDNESS, ETC., OF MINERALS. 217
List of Minerals (continued).

| Name. | Composition. | Hardness. | Specific Gravity. |  | Colour. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Chalcocite (copper | $\mathrm{Cu}^{2} \mathrm{~S}$ | 2.5-3 | $5 \cdot 5-5 \cdot 8$ | IV | Gr. |
| $\begin{gathered} \text { glance } \\ \text { Chalcosti- } \end{gathered}$ | $\mathrm{Cu}^{2} \mathrm{~S}, \mathrm{Sb}^{2} \mathrm{~S}^{3}$ | 3.5 | $4 \cdot 7$ | IV | Gr. B. |
| Chalybite | FeO | 3.5-4.5 | $3 \cdot 7-3 \cdot 9$ | III $\times$ | C. Gr. R. |
| (siderite | $\mathrm{Al}^{2} \mathrm{O}^{3}, \mathrm{SiO}^{2}$ | 5-5.5 | 2. | IV |  |
| (andalusite) |  |  |  |  |  |
| Chlorite . | $\begin{aligned} & 8 \mathrm{MgO}, \mathrm{Al}^{2} \mathrm{O}^{3} \\ & 5 \mathrm{SiO}^{2}, 7 \mathrm{H}^{2} \mathrm{O} \end{aligned}$ | 1-1.5 | $2 \cdot 8$ | III | Ge. |
| Chondrodite. | $\begin{gathered} 5 \mathrm{MgO}, 2 \mathrm{SiO}^{2}, \mathrm{or} \\ 4 \mathrm{MgO}, \mathrm{MgFl}^{2} \\ 2 \mathrm{SiO}^{2} \end{gathered}$ | 6-6.5 | 3.17-3.23 | v | Y. R. Br. Ge. Gr. B. |
| Chromite | $\mathrm{FeCr}^{2} \mathrm{O}^{4}{ }^{\text {a }}$. | $5 \cdot 5$ | 4.3-4.5 | 1 | B. |
| Chrysoberyl. | $\mathrm{BeO}, \mathrm{Al}^{2} \mathrm{O}^{3}$ | $8 \cdot 5$ | 3.65-3.8 | IV | Ge. |
| Chrysocolla. | $\mathrm{CuO}, \mathrm{SiO}^{2},$ | 2-4 | 2-2.3 | 0 | Ge. Br. Bl. B. |
| Chrysolite <br> (olivine or peridot) | $2 \mathrm{MgO}, \mathrm{SiO}^{2}$ | 6-7 | $3 \cdot 1-3 \cdot 5$ | IV | Y. Gr. Ge. Br. |
| Chrysoprase (chalcedony) | $\mathrm{SiO}^{2}$ | 7 | $2 \cdot 65$ | 0 | Ge. |
| Cinnabar | HgS . | 2-2.5 | $8 \cdot 99$ | III | R. G |
| Clausthalite. | PbSe | 2.5-3 | 7.6-8.8 | I |  |
| Clinochlore (ripidolite) | $\begin{gathered} 5 \mathrm{Mg}\left(\mathrm{Fe} \mathrm{O}, \mathrm{Al}^{2} \mathrm{O}^{3}\right. \\ 3 \mathrm{SiO}^{2}+4 \mathrm{H}^{2} \mathrm{O} \end{gathered}$ | $2-2.5$ | $2 \cdot 65-2 \cdot 78$ | v | Ge. B. Bl. R. |
| Clinoclasite. |  | 2.5-3 | $4 \cdot 1-4 \cdot 4$ | v | Ge. B. |
| Coal(mineral) | $\mathrm{C}(+\mathrm{O}+\mathrm{H}+\mathrm{N})$ | 0.5-2.5 | 1-1.8 | 0 | B. |
| Cobaltite (glance | $\mathrm{CoS}^{2}+\mathrm{CoAss}^{2}$ | $5 \cdot 5$ | 6-6.3 | $\mathrm{I} \pi$ | R. W. Gr. |
| Collyrite ${ }^{\text {a }}$ | 2A | 1.2 | 2 | 0 | W. |
| Columbite | $\mathrm{FeO}(\mathrm{Nb}, \mathrm{Ta})^{2} \mathrm{O}^{5}$ | 6 | 5.4-6.4 | IV | Br. Gr. B. |
| Copiapite |  | 1.5 | $2 \cdot 14$ | III |  |
| Copper |  | 2.5-3 | 8.8 | I | R. |
| (native) <br> Copper glance | $\mathrm{Cu}^{2} \mathrm{~S}$ | $2 \cdot 5$ |  | IV |  |
| Coppernickel | NiAs | 5-5.5 | 7.33-7. | III | R. Gr. |
| Copper <br> pyrites |  |  |  |  |  |
| Copper vitriol | $\mathrm{CuO}, \mathrm{SO}^{3}, 5 \mathrm{H}^{2} \mathrm{O}$ | $2 \cdot 5$ | , | VI | Bi. |
| Coquimbite . | $(\mathrm{FeAl})^{2} \mathrm{O}^{3}, 3 \mathrm{SO}^{3}$, | 2-2.5 | 2-2•1 | III | e. |
| Cordierite (iolite) | $\begin{gathered} 3 \mathrm{MgO}, 3 \mathrm{Al}^{2} \mathrm{O}^{3} \\ 8 \mathrm{SiO}^{2} \end{gathered}$ | $7-7 \cdot 5$ | $2 \cdot 6-2 \cdot 7$ | IV | W. Br. Y. Gr. B1. |

List of Minerals (continued).

| Name. | Composition. | Hard- | Specific Gravity. | $\dot{\sim}$ | Colour. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Corundum (emerald, sapphire, ruby) <br> Cotunnite | $\mathrm{Al}^{2} \mathrm{O}^{3}$ $\mathrm{PbCl}^{2}$ | 2 | $3.9-4.2$ 5.2 | IIIX IV | C. W. Gr. Y. Br . Bl. J. <br> W |
| Covellite (in- | CuS. | 1.5-2 | 3.8-3.9 | III | Bi. B. |
| Crocoisite | $\mathrm{PbO}, \mathrm{CrO}^{3}$ | 2.5-3 | 5.9-6.1 | V | R. |
| Cryolite - | $\mathrm{Al}^{2} \mathrm{Fl}^{6}$, 6 NaFl | $2 \cdot 5$ | 2.9-3 | VI | W. Gr. B. R. |
| Cuprite Cyanite (disthene) | $\begin{aligned} & \mathrm{Cu}^{2 \mathrm{O}} \\ & \mathrm{Al}^{2} \mathrm{O}^{3}, \mathrm{SiO}^{2} . \end{aligned}$ | $\begin{aligned} & 3 \cdot 5-4 \\ & 5-7 \end{aligned}$ | $\begin{aligned} & 5 \cdot 7-6 \cdot 1 \\ & 3 \cdot 4-3 \cdot 68 \end{aligned}$ | $\stackrel{\text { I }}{\text { VI }}$ | R. <br> B. Bl. W. Gr. Ge. |
| Danburite |  | 7 | $2 \cdot 95$ | IV | Y. |
| Datolite | $2 \mathrm{CaO} .2 \mathrm{SiO}^{2}$, $\mathrm{Bn}^{2} \mathrm{O}^{3}, \mathrm{H}^{2} \mathrm{O}$ | 5-5.5 | 2.8-3 | V | W. Gr. Ge. Y. R. V. |
| Descloizite | $4(\mathrm{~Pb}, \mathrm{Zn}) \mathrm{O},$ | 3.5 | $5 \cdot 8$ | IV | R |
| Desmine (stilbite) | $\mathrm{CaO}, \mathrm{Al}^{2} \mathrm{O}^{3}$, $6 \mathrm{SiO}^{2}, 6 \mathrm{H}^{2} \mathrm{O}$ | 3.5-4 | $2 \cdot 1$ | IV | W. C. Y. Br. R. |
| Diallage . - | ( $\mathrm{Ca}, \mathrm{Mg}, \mathrm{Fe}$ ) ${ }_{\text {SiO }}{ }^{2}$ | 4 | 3.2-3.3 | V | Ge. B |
| Dialogite | $\left.\mathrm{Mn}_{\mathrm{C}} \mathrm{Ca}\right) \mathrm{O}, \mathrm{CO}^{2}$. | 3.5-4.5 | $3 \cdot 4-3 \cdot 7$ | III | R. W. Y. Br. |
| Diamond. | C - | 10 | $3 \cdot 5$ | Ix | C. R. Y. BI. B. Br, Ge. |
| Diaspore | $\mathrm{Al}^{2} \mathrm{O}^{3}, \mathrm{H}^{2} \mathrm{O}$ | 6.5-7 | 3.3-3.5 | IV | Gr. Ge. Y. R. |
| Dichroite | $3 \mathrm{MgO}, 3 \mathrm{Al}^{2}$ | $7-7 \cdot 5$ | $2 \cdot 6-2.7$ | IV |  |
| Diopside | $(\mathrm{Ca}, \mathrm{Mg}) 0, \mathrm{SiO}^{2}$ | 5-6 | 3.2-3.38 | v | ge. |
| (pyroxene) <br> Dioptase | $\mathrm{CuO}, \mathrm{SiO}^{2}, \mathrm{H}^{2} \mathrm{O}$ | 5 | 3.27-3.348 | III $\times$ |  |
| the | $\mathrm{Al}^{2} \mathrm{O}^{3}, \mathrm{SiO}^{2}$. | 5-7.2 | 3.4-3.68 | VI | . Bl. |
| (cranite) <br> Dolomite. |  | 3.5-4 | 2.8-2.9 | III $\times$ | Gr. Ge. R. |
|  |  |  |  |  | Br. B. ${ }^{\text {B. }}$ B. |
| Dufrenite | $3 \mathrm{H}^{2} \mathrm{O}$ | $3.5-$ | $3 \cdot 3-3 \cdot 5$ | IV | . B. Y. Br. |
| Dufrenoysite Durangite | $\begin{aligned} & 2 \mathrm{PbS}, \mathrm{As}^{2} \mathrm{~S}^{3} \\ & \mathrm{Al}^{2} \mathrm{O}^{3}, \mathrm{As}^{2}{ }^{2}, \end{aligned}$ | $3$ | $\begin{aligned} & 5 \cdot 57 \\ & 3 \cdot 9-4 \end{aligned}$ | $\stackrel{\text { IV }}{\text { V }}$ | R. Y. |
| Dyscrasite . | $\mathrm{Ag}^{4} \mathrm{Sb}$ or ${ }^{2 \mathrm{Ng}} \mathrm{S}^{6 \mathrm{Sb}}$ | 3.5-4 | $9 \cdot 4-9 \cdot 8$ | IV | W. Gr. |
| Elaterite | $\mathrm{C}^{\mathrm{n}} \mathrm{H}^{2 \mathrm{n}}$ |  | $0 \cdot 8-1.23$ |  | B. B |
| Electrum | ${ }_{\text {Au }}{ }^{\text {Au }}+\mathrm{Ag}$ | 2.5-3 | ${ }_{3 \cdot 9-4 \cdot 2}^{13-15}$ | III× |  |
| Emplectite : | $\mathrm{Cu}^{2} \mathrm{~S}, \mathrm{Bi}^{2} \dot{S}^{3}$. | 2 | 5•1-5.26. | IV | W. Gr. |

List of Minerals (continued).

| Name. | Composition. | Hardness. | Specifle Gravity. | Cig sid | Colour. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Enstatite. | $\mathrm{MgO}, \mathrm{SiO}^{2}$ | $5 \cdot 5$ | 3•1-3.3 | IV | C. W. Ge. Y. |
| Epidote | $3 \mathrm{Al}^{2} \mathrm{O}^{3}, 4 \mathrm{CaO}$, | 6-7 | $3 \cdot 5$ | V | $\underset{\text { Gr. }}{\substack{\text { Gr. } \\ \text { Ge. B. R. }}}$ |
| Epistilbite | $\mathrm{CaO}, \mathrm{Al}^{2} \mathrm{O}^{3},$ | 4-5 | 2.2-2.36 | IV | W. Bl. |
|  | $\mathrm{MgSO} 4,7 \mathrm{H}^{2} \mathrm{O}$ | $2-2 \cdot 5$ | $17$ | $\operatorname{IV} \times$ | C. W. Gr. |
| Erubescite (purple copper ore) | $3 \mathrm{Cu}^{2} \mathrm{~S}, \mathrm{Fe}^{2} \mathrm{~S}^{3}$ | $3$ | $4 \cdot 4-5 \cdot 5$ | I | R. Br. |
| Erythrite (cobalt bloom) | $3 \mathrm{CoO}, \mathrm{As}^{2} \mathrm{O}^{5},{ }^{2} \mathrm{O}$ $8 \mathrm{H}^{2} \mathrm{O}$ | $1.5-2.5$ | 3 | v | R. Gr. |
| Euchroite . | $4 \mathrm{CuO}, \mathrm{As}^{2} \mathrm{O}^{5}$ | 3.5-4 | $3 \cdot 4$ | IV | Ge. |
| Euclase | $2 \mathrm{BeO}, \mathrm{Al}^{2} \mathrm{O}^{3},$ | $7 \cdot 5$ | $3 \cdot 1$ | V | C. Gr. B. |
| Eudialyte | $2 \mathrm{Na}^{2012}, \mathrm{CaO}$ | 5-5.5 | 2.8-3 | III $\times$ | R. Br. |
| Eulytite Euxenite . | $\begin{aligned} & 2 \mathrm{Bi}^{2} \mathrm{O}^{3}, 3 \mathrm{SiO}^{2} \\ & 4 \mathrm{R}^{2} \mathrm{O}_{3} 3 \mathrm{TiO}^{2}, \\ & 3 \mathrm{Nb}^{2} \mathrm{O}^{5}(\mathrm{R=}= \\ & \mathrm{Y}, \mathrm{Er}, \mathrm{U}, \mathrm{Ce}, \\ & \mathrm{Fe}) \end{aligned}$ | $4_{6 \cdot 5} \cdot 5$ | $\begin{aligned} & 6 \cdot 106 \\ & 4 \cdot 6-5 \end{aligned}$ | IV | Br. Gr. Y. W. $\mathrm{Br} . \mathrm{B} \text {. }$ |
| Fahlerz |  | 3-4.5 | $4 \cdot 5-5 \cdot 1$ | I | Gr. B. |
| Fahlunite Fassaite (pyroxene augite) |  | $3 \cdot 5-5$ | $\begin{gathered} 2 \cdot 6-2 \cdot 8 \\ 3 \cdot 25-3 \cdot 5 \end{gathered}$ | $\stackrel{?}{\mathrm{~V}}$ | $\begin{aligned} & \text { Gr. Ge. Br. B. } \\ & \text { Ge. B. } \end{aligned}$ |
| Fayalite (olivine) | $\begin{aligned} & 2 \mathrm{Fe}(\mathrm{Mn}, \mathrm{Ca}, \\ & \mathrm{Mg}) \mathrm{O}, \mathrm{SiO}^{2} \end{aligned}$ | 6 | 4-4•15 | IV | Ge. Br. B. |
| Felspar(anorthite, albite, andesite, labradorite, microcline, oligoclase, orthoclase) |  |  |  |  |  |
| Fergusonite . | $\begin{aligned} & R^{R^{3} Q^{2} O^{8}}(\mathrm{R}=\mathrm{Y}, \\ & \mathrm{Ce}, \quad \mathrm{~F}, \mathrm{Fe} \\ & \mathrm{Ca} ; \quad \mathrm{Q}=\mathrm{Nb}, \\ & \mathrm{Ta)} \end{aligned}$ | 5.5-6 | $5 \cdot 8$ | II | B. |
| Fibrolite (sillimanite) | $\mathrm{Al}^{2} \mathrm{O}^{3}, \mathrm{SiO}^{2}$. | 6-7 | $3 \cdot 23$ | V | $\mathrm{Gr} . \mathrm{Br}, \mathrm{Ge}$. |
| Fichtelite. | $\mathrm{C}^{\mathrm{n}} \mathrm{H}^{2 \mathrm{a} \sim 4}$ | 1 | ... | V | Br. W. |

List of Minerals (continued).

| Name. | Composition. | Hardness. | Specific Gravity. |  | Colour. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Flint (quartz) | $\mathrm{SiO}^{2}$ | 7 | $2 \cdot 63$ | 0 | Gr. Br. B. Bl. |
| Fluorspar (fluorite) | $\mathrm{CaFl}^{2}$ | 4 | $3 \cdot 18$ | I | $\begin{aligned} & \text { K. Y. } \\ & \text { C. V. G. Bl. } \\ & \text { Y. R. } \end{aligned}$ |
| Fowlerite | $\mathrm{Mn}, \mathrm{Fe}, \mathrm{Zn},$ | 4-5 | $3 \cdot 4$ | VI | Br. R. v. |
| Franklinite . | $(\mathrm{Fe}, \mathrm{Zn}, \mathrm{Mn})$ | 5.5-6.5 | $5 \cdot 06$ | I | B. |
| Freibergite |  | 3-4 | $4 \cdot 8-5$ | I× | Gr. B. |
| Fuchsite . |  | $2-2 \cdot 5$ | $2 \cdot 75$ | v | Ge. |
| Gadolinite | 3(Y, | 6.5-7 | 4.2-4.35 | v | B. Ge. |
| Gahnite | $\mathrm{ZnO}, \mathrm{Al}^{2} \mathrm{O}^{3}$. | $7.5-8$ | 4-4.6 | I | Gr. Bl. B. |
| Galena | PbS . | $2 \cdot 5-2 \cdot 7$ | $7 \cdot 2-7 \cdot 7$ | I |  |
| Garnet (almandite, melanite, grossularite, |  | 6.5-7.5 | 3•1-4 3 | I | B. Ge. Y. R. Br . W. |
| \& \& ${ }^{\text {che.) }}$ |  |  |  | v |  |
| ylussite | $\mathrm{Na}^{2} \mathrm{O}, \mathrm{CaO}$, $2 \mathrm{CO}^{2}, 5 \mathrm{H}^{2} \mathrm{O}$ | 2-3 | 1.99 | V | C. Y. |
| Genthite . | $\mathrm{H}^{4}(\mathrm{Ni}, \mathrm{Mg})^{4}$ | 3-4 | $2 \cdot 4$ | 0 | Ge. Y. |
| Gersdorffite | $\mathrm{NiS}^{2}+\mathrm{NiAs}^{2}$. | $5 \cdot 5$ | $5 \cdot 6-6 \cdot 9$ |  | W. |
| Geyserite | $\mathrm{SiO}^{2}+\mathrm{Aq}$. | 5 | 2 | 0 |  |
| Gibbsite ${ }^{\text {(opal) }}$ | $\mathrm{Al}^{2} \mathrm{O}^{3}, 3 \mathrm{H}^{2} \mathrm{O}$ | $2 \cdot 5-3 \cdot 5$ | $2 \cdot 35$ | v | e. |
| Gismondite . | $\mathrm{CaO}, \mathrm{Al}^{2} \mathrm{O}^{3}$, | 5 | $2 \cdot 26$ | II | Gr. R. |
| Glauberite . |  |  |  |  |  |
| Glaubersalt ${ }^{\text {a }}$ | $\mathrm{Na}{ }^{2} \mathrm{O}, \mathrm{CaO}, 2 \mathrm{SO}^{3}$ $\mathrm{Na}^{2} \mathrm{O}, \mathrm{SO}^{3}$, | ${ }_{1} \cdot 5-2$ | 1.4-1.5 | v | C. R. Y. <br> C. |
| (mirabilite) | (10 $\mathrm{H}^{2} \mathrm{U}$ |  |  |  |  |
| Gold . . | $\mathrm{Au}(\mathrm{Ag}, \mathrm{Cu}, \mathrm{Fe}$, | $2 \cdot 5-3$ | 15.6-19.5 | I | Y. |
| Goslarite . | $\mathrm{ZnO}, \mathrm{SO}^{3}+$ | $2-2.5$ | 1.9-2.1 | IV $\times$ | W. C. |
| Göthite | $\mathrm{Fe}^{2} \mathrm{O}^{3}, \mathrm{H}^{2} \mathrm{O} \mathrm{H}^{2}$. | 5-5.5 |  | IV | Br. Y. |
| Graphite | C. often associ- | 0.5-2 | 2.1-2.2 | III | Gr. B. |
| (plumbago) | ated with $\mathrm{SiO}^{2}$ <br> $\mathrm{CaO}, \quad \mathrm{Fe}^{2} \mathrm{O}^{3}$, |  |  |  |  |
| Greenockite . |  | 3-3.5 |  | III |  |
| Grossularite | $\mathrm{Ca}^{3} \mathrm{Al}^{2} \mathrm{Si}^{3} \mathrm{O}^{12}$ | $6 \cdot 5-7 \cdot 5$ | 3.1-3.7 | I | Ge. Br. W. |
| $\underset{\substack{\text { Gypsum } \\ \text { (satin spar) }}}{\substack{\text { (s) }}}$ | $\mathrm{CaO}, \mathrm{SO}^{3}, 2 \mathrm{H}^{2} \mathrm{O}$ | 1.5-2 | $2 \cdot 33$ | v | C. Y. Br. W. R. Gr. Bl. |

List of Minerals (continued).

| Name. | Composition. | Hardness. | Specific Gravity. |  | Colour. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Haidingerite. | $2 \mathrm{CaO}, \mathrm{As}^{2} \mathrm{O}^{5}$ $\qquad$ | 2-2.5 | 2.8-2.9 | IV | C. W. |
| Halite (rock | $\mathrm{NaCl}{ }^{\text {a }}$. | $2-2 \cdot 5$ | -2 | I | Gr. R. Bl. W. |
| Halloysite . | Al | 1.5-2.5 | 1.9-2.1 | 0 | W. Bl. Y. Gr. |
| Harmotome. | $\mathrm{BaO}, \mathrm{Al}^{2} \mathrm{O}^{3}$, $5 \mathrm{SiO}^{2}, 5 \mathrm{H}^{2} \mathrm{O}$ | 4.5 | $2 \cdot 45$ | V | C. W. Br. Gr. R. Y. |
| Hauerite . | $\mathrm{MnS}^{2}{ }^{\text {a }}$, | 4 | $3 \cdot 46$ | I $\pi$ | Br. B. |
| Hausmannite | $\mathrm{Mn}^{3} \mathrm{O}{ }^{4}$. | 5-5.5 | $4 \cdot 7-4 \cdot 9$ | II | $\mathrm{Br} . \mathrm{B}$. |
| Haüynite. | $2 \mathrm{Na}^{2}(\mathrm{Ca}) \mathrm{Al}^{2} \mathrm{Si}^{2}{ }^{2}$ $\mathrm{O}^{8}+\mathrm{CaSO}^{4}$ | 5.5-6 | 2.4-2.5 | 1 | Bl. Gr. |
| Heavy spar (barytes) | $\mathrm{BaO}, \mathrm{SO}^{3}$. | $2 \cdot 5-3 \cdot 5$ | $4 \cdot 3-4 \cdot 7$ | IV | C. Y. Gr. Bl. R. Br. |
| $\begin{aligned} & \text { Heliotrype } \\ & \text { (bloodstone) } \end{aligned}$ | Chalcedony | 7 | $2 \cdot 65$ | 0 | Ge. with R. spots. |
| Helvite . | (B) | 6-6.5 | 3.1-3.3 | I $\times$ | B |
| Hematite (specular iron) | $\mathrm{Fe}^{2} \mathrm{O}^{3}$ | 5.5-6.5 | 4.5-5.28 | III $\times$ | Gr. R. B. |
| Hessite ${ }^{\text {a }}$. | $\mathrm{Ag}^{2} \mathrm{~T}$ | $2-3 \cdot 5$ | $8 \cdot 13-8 \cdot 6$ | IV |  |
| Heulandite (stilbite) | $\begin{aligned} & \mathrm{CaO}_{2}, \mathrm{AlO}^{2} \mathrm{O}^{3} \\ & \hline \end{aligned}$ | 3.5-4 |  |  | C. R. Gr. Br. |
| Hornblende (amphibole) | ( $\mathrm{Ca}, \mathrm{Mg}, \mathrm{Fe} \mathrm{O}$, $\mathrm{SiO}^{2}$ | 5-6 | $2 \cdot 9-3 \cdot 4$ | v | B. |
| Hornsilver | AgCl | 1-1*5 | $5 \cdot 5$ | 1 | Ge. Gr. W. V. |
| Hornstone (chert) | $\mathrm{SiO}^{2}$ | 7 | $2 \cdot 65$ | Compact |  |
| Huantajayite | ( $\mathrm{Na}, \mathrm{Ag}$ ) Cl |  |  | I |  |
| Hiibnerite Humite | $\mathrm{MnO}, \mathrm{WO}^{3}$ | ${ }_{6}^{4 \cdot 5}$ | ${ }^{7} \cdot 1 \cdot 14$ | $\stackrel{\text { v }}{ }$ |  |
| Humite |  | 6-6.5 | 3.01-3.23 | IV | Y. R. Br, W. |
| Hyacinth | $\mathrm{ZrO}^{2}+\mathrm{SiO}^{2}$ | $7 \cdot 5$ | 4-4.7 | II |  |
| Hyalite(opal) | $\mathrm{SiO}^{2}+\mathrm{Aq}$ |  | $2 \cdot 15-2 \cdot 18$ | O |  |
| Hyalophane. | $\begin{aligned} & \mathrm{K}^{2} \mathrm{O}, \mathrm{Sl}^{2} \mathrm{Al}^{2} \mathrm{O}^{3}, \\ & 6 \mathrm{SiO}^{2} \\ & \mathrm{BaO}^{2} \end{aligned}$ | 6-6.5 | $2 \cdot 8$ | v | W. C. R. |
| Hyalosiderit | $4 \mathrm{MgO}, 2 \mathrm{FeO}$ | 6-6.5 | $3 \cdot 5$ | IV | B |
| Hydromag- | 4N | $3 \cdot 5$ | $2 \cdot 15$ | V |  |
| Hydrozincite | $\begin{array}{r} 4 \mathrm{ZnOCO}^{2}, 2 \mathrm{ZnO} \\ \mathrm{ZnO}^{2} \end{array}$ | $2-2 \cdot 5$ | 3.6-3.8 | ? | W. Gr. |
| Hypersthene | $\begin{aligned} & (\mathrm{Mg}, \mathrm{Fe}) \mathrm{O}, \mathrm{SiO}^{2} \mathrm{O} \end{aligned}$ | 5-6 | 3.4 | IV | . Gr. Ge. B. |
| Id |  | $6 \cdot 5$ | 3.3-3.45 | II | $\mathrm{Ge} . \mathrm{Br} . \mathrm{Bl}$. |
| Idrialite | $\mathrm{C}^{n} \mathrm{H}^{2 n-12}$. | 1-1*5 | 1-4-1 6 | 0 | Br. B. R. |

List of Minerals (continued).

| Name. | Composition. | Hardness. | Specific Gravity. |  | Colour. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Ilmenite (titanic iron) | $\mathrm{FeO}, \mathrm{TiO}^{2}$ | 5-6 | 4.5-5 | IIIX | B. Br. R. |
| Ilvaite . Iolite | $\mathrm{H}^{2} \mathrm{Ca}^{2} \mathrm{Fe}^{6} \mathrm{Si}^{4} \mathrm{O}^{18}$ $3 \mathrm{MgO}, 3 \mathrm{Al}^{2} \mathrm{O}^{3}$, | $\begin{aligned} & 5 \cdot 5-6 \\ & 7-7 \cdot 5 \end{aligned}$ | $\begin{aligned} & 3 \cdot 7-4 \cdot 2 \\ & 2 \cdot 6-2 \cdot 7 \end{aligned}$ | IV | $\begin{aligned} & \text { B. } \\ & \text { W. Br. Y. Gr. } \end{aligned}$ |
|  |  |  |  | IV | W. Br. Y. Gr. W. |
| Iridosmine | $\begin{aligned} & \mathrm{Ir}(\mathrm{Pt}, \mathrm{OR}(\mathrm{Rh}, \mathrm{Pd}) \\ & \mathrm{Fe}, \mathrm{P} \end{aligned}$ | 6-7 | $12-21 \cdot 12$ | III $\times$ | W. G |
| Jamesonite | $2 \mathrm{PbS}, \mathrm{Sb}$ | $2-3$ | 5.5-5.8 | IV |  |
| Jasper (quartz) | $\mathrm{SiO}^{2}\left(\mathrm{Fe}^{2} \mathrm{O}^{3}\right)$ | 7 |  |  | R. Y. Br. Ge. |
| Jeffersonite . | $\begin{gathered} \mathrm{Ca}(\mathrm{Fe}, \mathrm{Mn}, \mathrm{Zn}, \\ \mathrm{Mg}) \mathrm{O}, \mathrm{SiO}^{2} \end{gathered}$ | $4 \cdot 5$ | $3 \cdot 5$ | vI | Ge. Br. B. |
| Kainite | $\mathrm{KCl}, \mathrm{MgO}, \mathrm{SO}^{3}{ }^{3}$ | $2 \cdot 5$ | 2-13-2.2 | v | C. Gr. Y. |
| Kaluszite (syngenite) | $\begin{aligned} & \mathrm{K}^{2} \mathrm{O}, \mathrm{SO}^{3}+\mathrm{CaO}, \\ & \mathrm{SO}^{3}+\mathrm{H}^{2} \mathrm{O} \end{aligned}$ | $2 \cdot 5$ | $2 \cdot 6$ | v | C. |
| Kaolinite . | $\mathrm{Al}^{2} \mathrm{O}^{3}, 2 \mathrm{SiO}^{2}$, | 1-2.5 | 2.4-2.6 | IV | W. Gr. Y. Br. |
| Kermesite <br> Kieserite . | $\begin{aligned} & \mathrm{Sb}^{2} \mathrm{SO}^{2} \mathrm{O} \\ & \mathrm{SO}^{3}, \mathrm{H}^{2} \dot{0} \end{aligned}$ | $\underset{3}{1-1 \cdot 5}$ | $\stackrel{4.5}{2 \cdot 51-2.57}$ | $\stackrel{\mathrm{v}}{\mathrm{v}}$ | R. <br> C. W. Gr. Y |
| Labradorite. | $\mathrm{CaO}, \mathrm{Al}^{2} \mathrm{O}^{3},$ <br> $3 \mathrm{SiO}^{2}$ | 6 | 2.67-2.76 | VI | Br. Gr. |
| Lanarkite | $\mathrm{PbO}, \mathrm{SO}^{3}, \mathrm{PbO}^{2}$ | $2-2 \cdot 5$ | 6.3-6.4 | V | Ge. |
| Lanthanite. ${ }^{\text {- }}$ | $\mathrm{La}, \mathrm{CO}^{2}, 3 \mathrm{H}^{2} \mathrm{O}$ | $2 \cdot 5 \cdot 5$ |  | IV | W. |
| Lapis lazuli. | $\begin{gathered} \text { Varies, } \mathrm{Al}^{2}{ }^{20}{ }^{3}+ \\ \mathrm{NO}^{2} \mathrm{CaO}+\mathrm{CaO}^{2}+\mathrm{SiO}^{2} \end{gathered}$ | $5 \cdot 5$ | $2 \cdot 4$ |  |  |
| Lazulite | $\left(\mathrm{Mg}, \mathrm{FeO}, \mathrm{Al}^{2}\right.$ | 5-6 | $3 \cdot 1$ | v | B1. |
| Leadhillite | $\begin{aligned} & \mathrm{PbO}, \mathrm{SO}^{3}, \\ & 2\left(\mathrm{PbO}, \mathrm{CO}^{2}\right), \end{aligned}$ | $2 \cdot 5$ | 6.26-6.4 | IV | Y. W. Ge. Gr. |
| Lepidolite | (Al, K, Li), FI, | 2.5-4 | 2•84-3 | IV | V. Y. W. |
| Lepidomelane | $\begin{aligned} & 2\left(\mathrm{Fe}, \mathrm{Mg}, \mathrm{~K}^{2}\right) \\ & \mathrm{OAl}^{2} \mathrm{O}^{3}, \mathrm{SiO}^{2} \end{aligned}$ | 3 | 3 | v | c. |
| Leucite | $\mathrm{K}^{2} \mathrm{O}, \mathrm{Al}^{2} \mathrm{O}^{3}$ | 5.5-6 | 2.45-2.5 | II | Gr. w. |
| Leucophanite | $5(\mathrm{CaBe}) 0,5 \mathrm{SiO}^{2},$ | 3.5-4 | $2 \cdot 97$ | IV | e. Br. |
| Leucopyrite. | $\mathrm{Fe}^{2} \mathrm{As}^{3}{ }^{2 \mathrm{NaFl}}$ | $5-5 \cdot 5$ | $6 \cdot 8-8.7$ | IV | G |
| Libethenite. | $4 \mathrm{CuO}, \mathrm{P}^{2} \mathrm{O}^{5} \mathrm{H}^{2} \mathrm{O}$ | 4 | 3.6-3.8 | IV |  |
| Lievrite (ilvaite) | $\mathrm{H}^{2} \mathrm{Ca}^{2} \mathrm{Fe}^{6} \mathrm{Si}^{4} \mathrm{O}^{18}$ | 5.5-6 | $3 \cdot 7-4 \cdot 2$ | IV | B. |
| Lignite. | 60 | $\ldots$ | 1-2-1.3 | 0 | Br . B. |
| Limonite. | H. O, and ash $2 \mathrm{Fe}^{2} \mathrm{O}^{3}, 3 \mathrm{H}^{2} \mathrm{O}$. | 5-5.5 | 3.6-4 | 0 | Br. Y. B. |

List of Minerals (continued).

| Name. | Composition. | Hardness. | Specific Gravity. |  | Colour. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Linarite | $(\mathrm{PbCu}) \mathrm{O}, \mathrm{SO}^{3}+$ | $2 \cdot 5$ | 5.3-5.45 | V | B1. |
| Liroconite | $\begin{gathered} (\mathrm{PbCu}) \mathrm{H}^{\mathrm{H}^{2} 0} \\ \mathrm{Cu}^{3}\left(\mathrm{Al}^{2}\right) \mathrm{As}^{2}\left(\mathrm{P}^{2}\right)+\mathrm{H}^{6}\left(\mathrm{Cu}^{3},\right. \end{gathered}$ | $2-2 \cdot 5$ | $2 \cdot 8-2 \cdot 9$ | v | Bl. Ge. |
|  | $\mathrm{Al}^{2} \mathrm{O}^{6}+9 \mathrm{Aq} \mathrm{Cl}^{\text {a }}$, |  |  | 0 |  |
| Lowweite . | ${ }_{\text {2 }}$ (Mgosos ${ }^{\text {a }}$, $\mathrm{Na}^{\text {a }}$ | $2 \cdot 5-3$ | $\begin{array}{r} 2.3-27 \\ 2.37 \end{array}$ | II | W. R. Y. |
| Lydian stone | $\mathrm{SiO}^{2}$ impure with Fe , \&c. | 7 | $2 \cdot 8$ | 0 | B. |
| Magnesite | $\mathrm{MgO}, \mathrm{CO}^{2}$ | 3.5-4.5 | 2.9-3.1 | III× | W. Y. |
| Magnetite | $\mathrm{Fe}^{3} \mathrm{O}^{4} \mathrm{CO}^{2} \mathrm{H}^{2} \dot{ }$ | 5 5-6.6.5 | 4.9-5.2 |  |  |
| Malachite | $2 \mathrm{CuO}, \mathrm{CO}^{2}, \mathrm{H}^{2} \mathrm{O}$ | 3.5-4 | 3.7-4 |  |  |
| Manganite ${ }_{\text {Marble }}$ | $\xrightarrow{\mathrm{Mn} \mathrm{O}^{3}, \mathrm{H}^{2} \mathrm{O}} \mathrm{CaO}, \mathrm{CO}^{2}$. | ${ }^{\text {. }}$ - 3.5 | $4 \cdot 2-4 \cdot 4$ $2 \cdot 5-2 \cdot 8$ | ${ }_{0}^{\text {IV }}$ | Gr. $B$. <br> W.Gr. Bl. Ge. |
| Marble (calcite) | $\mathrm{CaO}, \mathrm{CO}^{2}$. | .5-3.5 | $2 \cdot 5-2 \cdot 8$ | 0 | $\begin{aligned} & \text { W.Gr. Bl. Ge. } \\ & \text { Y. R. B. } \end{aligned}$ |
| Marcasite . | Fe | $6-6 \cdot 5$ $3 \cdot 5-4 \cdot 5$ | 4.6-4.8 | IV | Y. Gr. |
| Mascagnite | $\begin{gathered} \mathrm{SiO}^{2} \\ \left(\mathrm{NH}^{4} \mathrm{O}\right)^{2} \mathrm{~S} \end{gathered}$ | 2-2.5 | $1 \cdot 7-1 \cdot 8$ | IV | C. W. Y. |
| Meerschaum | $2 \mathrm{MgO}, 3 \mathrm{SiO}^{2}$ | 2-2.5 | 0.98-1.2 | 0 | Y. R. |
| Meionite ${ }^{\text {(sepiolite }}$ ) | 6 C | 5.5-6 | $2 \cdot 6-2 \cdot 74$ | II | C. W. |
| Melanite | $\mathrm{Ca}^{3} \mathrm{Fe}^{2} \mathrm{Si}^{3} \mathrm{O}^{12}{ }^{12}$. | 6.5-7 | 3.5 | I |  |
| (garnet) |  | 2 | 1.8 | $v$ |  |
| (iron vitriol) | ${ }^{2}{ }^{7} \mathrm{H}^{2} \mathrm{O}$ |  |  |  |  |
| Melilite | $\begin{gathered} 2 \mathrm{Al}^{2}\left(\mathrm{Fe}^{2}\right) \mathrm{O}^{3}, \\ 12 \mathrm{CaO}, \\ 0 \mathrm{Mg}, \end{gathered}$ | 5-6 | $2 \cdot 9$ | II | W. Y. Br. |
| Mellite | $\mathrm{C}^{6}\left(\mathrm{CO}^{2}\right)^{6} \mathrm{~A}$ | 2-2.5 | 1.55-1.6 | II | Br. W. |
| Menaccan | $\mathrm{FeO}, \mathrm{TiO}^{2}$. | 5-6 | 4.5-5 | III $\times$ | B. Br. R. |
| (ilmenite) <br> Meudipite | $\mathrm{Pb}^{3} \mathrm{O}^{2} \mathrm{C}$ | $2 \cdot 5$ |  | IV |  |
|  | $2 \mathrm{PbO}, \mathrm{Pr}$ |  |  |  |  |
| sitite |  | 4 |  |  |  |
| Mesolite | $\mathrm{CaO}, \mathrm{Na}^{2} \mathrm{O}, 2 \mathrm{~A}$ | 5 | 2.2-2.4 | V or | C. W. Y. |
|  | $\mathrm{Al}^{2} \mathrm{O}^{3}, \mathrm{Na}^{2} \mathrm{O}$ | 5-5 |  | IV |  |
| (natrolite) | $3 \mathrm{SiO}^{2}, 2 \mathrm{H}^{2}$ |  | 217-2 |  |  |
| Miargyrite Microcline |  | $\underset{6}{2-2 \cdot 5}$ | $5 \cdot 2-5 \cdot 4$ | $\begin{gathered} \text { VI } \end{gathered}$ | $\begin{aligned} & \text { Gr. B. } \\ & \text { W. R. B } \end{aligned}$ |
|  |  |  |  |  |  |
| Millerite Mimetite | NiS $3\left(3 \mathrm{PbO}, \dot{\mathrm{~A}}^{2}\right.$ | $3-3 \cdot 5$ | $\begin{gathered} 4 \cdot 6-5 \cdot 6 \\ 7 \cdot 2-7 \cdot 25 \end{gathered}$ | $\underset{\text { III }}{\text { III }}$ | Y. Y. Gr. Br. |
| Minium | $\mathrm{Pb}_{3} \mathrm{PbCl}^{2}$ | 2-3 | 4.6 | 0 | R. Y. |

List of Minerals (continued).

| Name. | Composition. | Hardness. | Specific Gravity. |  | Colour. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Mirabilite | $\mathrm{Na}^{2} \mathrm{O}, \mathrm{SO}^{3},$ | 1.5-2 | $1 \cdot 4-1 \cdot 5$ | V | C. |
| (glauber salt) <br> Mispickel <br> (arsenical <br> pyrites | $\mathrm{FeS}^{2}+\mathrm{FeAs}^{2}{ }^{10 \mathrm{H}}$. | 5•5-6 | 6-6.4 | IV | W. Gr. |
| Molybdenite. | $\mathrm{MoS}^{2}$ | 1-1.5 | 4.4-4.8 | III? | Gr. |
| Molybdite . | $\mathrm{MoO}^{3}$ | 1-2 |  | IV |  |
| Monazite . | $\begin{array}{r} \left(\mathrm{Ce}, \mathrm{La}, \mathrm{Di}_{1}, \mathrm{Th}\right)^{3} \\ \left(\mathrm{PO}^{4}\right)^{2} \end{array}$ | 5-5.5 | 4.9-5.2 | V | Br. R. Y. |
| Monticellite. | $2\left(\mathrm{Ca}, \mathrm{Mg}, \mathrm{Fe}^{\mathrm{Fe}) \mathrm{O}} \mathrm{SiO}^{2}\right.$ | 5-5.5 | $3 \cdot 1$ | v | C. Gr. |
| Morenosite (nickel | $\mathrm{NiOSO}{ }^{3}+7 \mathrm{H}^{2} \mathrm{O}$ | $2-2 \cdot 25$ | 2 | IV | Ge. |
| Mosandrite . | $\begin{aligned} & 3 \mathrm{CaO}, 2(\mathrm{Ce}, \mathrm{La}, \\ & \mathrm{Di})^{2} \mathrm{O}^{3} 5\left(\mathrm{SiO}^{2},\right. \\ & \left.\mathrm{TiO}^{2}\right) \end{aligned}$ | 4 | 3 | IV | Br. R. Gr. |
| Nagyagite | PbT | 1-1:5 | 6.8-7.2 | II | Gr |
| Naphtha (rock oil) | Cn |  |  | 0 | C. |
| Natrolite (mesotype) | $\begin{aligned} & \mathrm{Al}^{2} \mathrm{O}^{3}, \mathrm{Na}^{2} \mathrm{O}, \\ & 3 \mathrm{SiO}^{2}, 2 \mathrm{H}^{2} \mathrm{O} \end{aligned}$ | 5-5.5 | $2 \cdot 17-2 \cdot 2$ | IV | C. W. Y. Gr. <br> R. |
| Naumannite. | $\mathrm{Ag}^{2} \mathrm{Se}{ }^{2}{ }^{\text {a }}$ | 2.5 | 8 | 1 |  |
| Nephelite | $4 \mathrm{Na}^{2} \mathrm{O}, 4 \dot{\mathrm{~A}}^{2} \mathrm{aSO}^{2}{ }^{\circ}$ | 5.5-6 | 2.56--2.6 | III $\times$ | Gr. C. W. Y. Ge. Br. R. |
| Nephrite . | ( $\mathrm{Ca}, \mathrm{Mg}, \mathrm{Fe}) \mathrm{O}{ }^{2}$ | 6.5 | 2.9-3.1 | V | W. Gr. Ge. |
| Niccolite (copper nickel) | NiAs | 5-5.5 | 7.33-7.6 | III | R. Gr |
| Niobite | $\mathrm{FeO}(\mathrm{Nb}, \mathrm{Ta})^{2} \mathrm{O}^{5}$ | 6 | 5•4-6.4 | IV | r. B. G |
| Nitre (columbite) | $\mathrm{Na}^{2} \mathrm{O}, \mathrm{N}^{2} \mathrm{O}^{5}$ | 1.5-2 | 2.1-2.3 | IV | C. Gr. Y. R. |
| Nosea $n$ (haiiyn) | $\begin{aligned} & \mathrm{Na}^{2} \mathrm{O}, \mathrm{Al}^{2} \mathrm{O}^{3}, \\ & 2 \mathrm{SiO}^{2}+\mathrm{Na}^{2} \mathrm{O} \\ & \mathrm{SO}^{3} \end{aligned}$ | $5 \cdot 5$ | 2.28-2.4 | I | Y. Ge. B. Br. |
| Octahedrite | $\mathrm{TiO}^{2}$. | 5.5-6 | 3.8-3.9 | II | 31. |
| (anatase) | $\mathrm{Na}^{2} \mathrm{O}$ | 6-7 | 2.63-2.73 | VI | Ge. R. Gr. |
|  | $\begin{aligned} & \mathrm{Al}^{2} \mathrm{SO}^{3}, 2 \mathrm{CaO}^{2}, \\ & \mathrm{AlO}^{2} \end{aligned}$ |  |  |  |  |
| Olivine (chrysolite) | ${ }_{2} \mathrm{MgO}, \mathrm{SiO}^{2}$. | $6-7$ | 3.3-3.5 | IV | $\underset{\text { Gr. Ge. Y. Br. }}{\text { R. }}$ |
| Olivenite. . | $\mathrm{AsO}^{4} \mathrm{Cu}, \mathrm{CuO}$ | 3 | 4.1-4.4 | IV | Ge. Y. Br. |
| Ouvarovite | ${ }_{\text {Ca }}{ }^{3} \mathrm{Cr}^{2} \mathrm{Si}^{3} \mathrm{Cl}^{12}$ | $7 \cdot 5$ | $3 \cdot 4-3 \cdot 5$ | I | Ge. |
| $\begin{aligned} & \text { Onyx } \\ & \text { Opal } \\ & \text { (pre: } \end{aligned}$ | $\xrightarrow{\mathrm{SiO}^{2}} \mathrm{SiO}^{2}, 10 \mathrm{H}^{2} \mathrm{O}$ | $5.5-6.5$ | $\stackrel{2 \cdot 65}{1 \cdot 9-2.3}$ | $\begin{aligned} & 0 \\ & 0 \end{aligned}$ | Gr. W. B. Br. C. Y. Gr. R. |
| cious, fire, common, |  |  |  |  | Br . Ge. |
| $\underset{\text { wood, \&c.) }}{\substack{\text { crpiment }}}$ | $\mathrm{As}^{2} \mathrm{~S}^{3}$ | 1.5-2 | $3 \cdot 48$ | IV |  |

List of Minerals (continued).

| Name. | Composition. | Hardness. | Specific Gravity: |  | Colour. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Orthite. | $\begin{array}{r} \left(\mathrm{Al}^{2}, \mathrm{Fe}^{2}, \mathrm{Ce}^{2}\right)^{3}, \\ 2(\mathrm{CaFe}) \mathrm{O}^{2} \\ 3 \mathrm{SiO}^{2} \end{array}$ | 4-6 | $3 \cdot 1-4$ | V | B. |
| Orthoclase (felspar) | $\mathrm{K}^{2} \mathrm{O}, \mathrm{Al}^{2} \mathrm{O}_{6}^{3}{ }_{6}^{3}$ | 6-6.5 | $2 \cdot 4-2.7$ | V | C. R. Gr. Ge. |
| Ozocerite. | $\mathrm{C}^{\mathrm{n}} \mathrm{H}^{2 \mathrm{n}}$. . | 1 | 0.85-0.9 | 0 | W. Y. Br. B. |
| Palladium (native) | $\mathrm{Pd}(\mathrm{PtIr})$ | $4 \cdot 5-5$ | 11.3-11.8 | I | Gr. |
| Paragonite . | $\mathrm{Na}^{2} \mathrm{O}, \mathrm{Al}^{2} \mathrm{O}^{3}$ $2 \mathrm{SiO}^{2}$ | $2 \cdot 5-3$ | 2.78 | 0 | W. Gr. Y. Ge. |
| Pectolite . . | $\begin{aligned} & \mathrm{Na}^{2} \mathrm{O}, 4 \mathrm{CaO}, \\ & 6 \mathrm{SiO}^{2}+\mathrm{Aq} . \end{aligned}$ | 5 | $2 \cdot 8$ | V | W. Gr. |
| Periclase | MgO | 6 | $3 \cdot 67$ | I | Gr. |
| Pericline (albite) | $\mathrm{Na}^{2} \mathrm{O}, \mathrm{Al}^{2} \mathrm{O}^{3}$, $6 \mathrm{SiO}^{2}$ | 6-6.5 | $2 \cdot 6-2 \cdot 64$ | VI | W. |
| Peridot (chrysolite, olivene) | $2 \mathrm{MgO}, \mathrm{SiO}^{2}$ | $6-7$ $5 \cdot 5$ | $3 \cdot 3-3 \cdot 5$ | IV. | Gr. Ge. Y. Br. |
| Perofskite Petalite | ( $\mathrm{Ca}, \mathrm{Fe}) \mathrm{O}, \mathrm{TiO}^{2}$ | ${ }_{6-6.5}^{5 \cdot 5}$ | $2 \cdot$ | I | R. Y. B. W. R. Gr. Ge. |
| Petalite - | Ca) $\mathrm{O}, \mathrm{SiO}^{2}$ | 6-6.5 | 2 | $\checkmark$ | W. R. Gr. Ge. |
| Petroleum (mineral oil) | $\mathrm{C}^{4} \mathrm{H}^{2 n+2}$. . | ... | 0.7-0.9 | 0 | C. Y. Br. |
| Pharmacolite | $\begin{gathered} 2 \mathrm{CaO}, \mathrm{As}^{2} \mathrm{O}^{5}, \\ \mathrm{H}^{2} \mathrm{O}+5 \mathrm{H}^{2} \mathrm{O} \end{gathered}$ | 2-2.5 | $2 \cdot 6-2 \cdot 7$ | V | W. Gr. R. |
| Pharmacosiderite | $\begin{aligned} & 3 \mathrm{Fe}^{2} \mathrm{As}^{2} \mathrm{O}^{3}+ \\ & \mathrm{H}^{6} \mathrm{Fe}^{2} \mathrm{O}^{6} \end{aligned}$ | $2 \cdot 5$ | $2 \cdot 9-3$ | I $\times$ | Ge. Br. Y. R. |
| Phenacite | $2 \mathrm{BeO}, \mathrm{SiO}^{2}$. | 7.5-8 | 3 | III | C. Y. |
| Phillipsite | $\mathrm{CaO}, \mathrm{Al}^{2} \mathrm{O}^{3},$ | 4-4.5 | $2 \cdot 2$ | V | C. W. R. |
| Phosgenite | $\mathrm{PbO}, \mathrm{CO}^{2} \mathrm{PbCl}^{2}$ | $2 \cdot 5-3$ | -6-6.3 | II | W. Y. Gr. |
| Phosphorite (earthy apatite) | $\begin{aligned} & 3 \mathrm{Ca}^{3} \mathrm{P}^{2} \mathrm{O}^{8}+ \\ & \mathrm{CaF}(\mathrm{Cl})^{2} \end{aligned}$ | 5 | $3 \cdot 15$ | 0 | W. Gr. Y. |
| Piauzite . | Fossil resin. . | 1.5 |  | 0 | Br. B. |
| Pimelite . . | $\begin{aligned} & \left(\mathrm{Al}, \mathrm{Ni}^{2} \mathrm{O}^{3}\right. \\ & \mathrm{MgO}, \\ & \mathrm{SiO}^{2} \end{aligned}$ | $2 \cdot 5$ | $2 \cdot 2-2 \cdot 7$ | 0 | Ge. |
| Pisanite (iron copper vitriol) | $\begin{array}{r} (\mathrm{FeO}, \mathrm{CuO}) \mathrm{SO}^{3} \\ +7 \mathrm{aq} . \end{array}$ | $\cdots$ | ... | VI | B1. |
| Pistazite (epidote) | $\begin{gathered} 3 \mathrm{Al}^{2} \mathrm{O}^{3}, 4 \mathrm{CaO}, \\ 6 \mathrm{SiO}^{2}+\mathrm{H}^{2} \mathrm{O} \end{gathered}$ | 6-7 | $3 \cdot 3-3 \cdot 5$ | V | Ge. Y. B. |
| Pitchblende (uraninite) | $\begin{gathered} \mathrm{U}^{3} \mathrm{O}^{4}(\mathrm{~Pb}, \mathrm{Fe}, \mathrm{Ag}, \\ \mathrm{Ca}_{2} \mathrm{Mg}, \mathrm{Bi}, \\ \left.\mathrm{SiO}^{2}, \& \mathrm{C} .\right) \end{gathered}$ | 3-6 | 4*8-8 |  | B. |
| Plagionite - | $4 \mathrm{PbS}, 3 \mathrm{Sb}^{2} \mathrm{~S}^{3}$. | $2 \cdot 5$ | $5 \cdot 4$ | V | Gr. |
| Platinum (native) | $\begin{aligned} & \mathrm{Pt}(\mathrm{Fe}, \mathrm{Ir}, \mathrm{Rh}, \\ & \mathrm{Pd}, \mathrm{Os}, \mathrm{Cu}) \end{aligned}$ | 4-4.5 | 16-19 | I |  |
| Platiniridium | $\begin{array}{r} \mathrm{Pt}+\operatorname{Ir}(\mathrm{Rh}, \mathrm{Fe}, \\ \mathrm{Cu}, \mathrm{Pd}) \end{array}$ | 6-7 | 22.6-23 | I | W. Gr. |

List of Minerals (continued).


List of Minerals (continued).

| Name. | Composition. | Hardness. | Specific Gravity. |  | Colour. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Rainmels- | $\overline{(\mathrm{Ni}, \mathrm{Co}, \mathrm{Fe}) \mathrm{As}^{2}}$ | $5 \cdot 5$ | $7 \cdot 1-7 \cdot 2$ | IV | W. |
| bergite | $\Delta s \mathrm{~S}$ | 1.5-2 | 3.4-3.6 | $\checkmark$ | ${ }_{\text {R. }}^{\text {Y }}$. |
| $\mathrm{Retinite}_{\text {Rea }}$ R ${ }^{\text {a }}$ |  | 1.5 | $1.01-1.5$ $3.4-3.7$ | $\stackrel{\text { O }}{\text { Iİ }}$ | ${ }_{\text {Rr. }}^{\text {Br. Y. Y. }}$ Br. |
| Rhodochrosite | $\mathrm{Mn}(\mathrm{Ca}) \mathrm{O}, \mathrm{CO}^{2}$. |  | 3.4-3.7 |  |  |
| Rhodonite Ripidolite | ${ }_{6 \mathrm{Mg}(\mathrm{Fe}) \mathrm{O}}^{\mathrm{MnO}, \mathrm{SiO}^{2}} \mathrm{Al}^{2}$ | $5 \cdot 5-6.5$ $2-2.5$ | $3 \cdot 4-3 \cdot 7$ $2 \cdot 65-2 \cdot 78$ | $\stackrel{\text { VI }}{\mathbf{V}}$ | R. Br. Ge. R |
| (clinochlore) | $\begin{aligned} & 6 \mathrm{Mg} \\ & \mathbf{O}^{3} \mathrm{H}^{2} \mathrm{O} \\ & 3 \mathrm{SiO}^{2}+ \end{aligned}$ |  |  |  |  |
| Rocksalt (halite) | NaCl | 2-2.5 | $2 \cdot 25$ | I | $\underset{\text { Y. }}{\text { Gr. R. Bl. W. }}$ |
| Roselite | $(\mathrm{CoCa})^{3}\left(\mathrm{AsO}^{4}\right)^{2}{ }^{2}$ | 3.5 | $3 \cdot 58$ | VI | R. |
| Ruby <br> Rutile | $\begin{aligned} & \mathrm{Al}^{2} \mathrm{O}^{3} \\ & \mathrm{TiO}^{2} \end{aligned}$ | $\stackrel{9}{6-6}$ | $\left\lvert\, \begin{gathered} 3 \cdot 9-4 \cdot 1 \\ 4 \cdot 18-4 \cdot 25 \end{gathered}\right.$ | $\mathrm{III}_{\text {II }} \times$ | R. <br> Br. B. R. Y. <br> Bl. V. Ge. |
| Sal ammoniac | $\mathrm{NH}^{4}$ | 1.5-2 | - |  | W. Y. R. Br. |
| Samarskite . | $\begin{aligned} & \mathrm{UO}^{3}, \mathrm{Cb}^{2} \mathrm{O}^{5}, \mathrm{Ta}^{2} \\ & \mathrm{O}^{5}, \mathrm{WO}^{3}, \mathrm{SNO}^{2} \end{aligned}$ | 5.5-6 | 5.6-5.75 | IV |  |
|  | $\mathrm{ZrO}^{2}, \mathrm{ThO}^{2}$ |  |  |  |  |
|  | ( $\mathrm{Fe}, \mathrm{Cu}, \mathrm{Mg}$, $\mathrm{Ce} \mathrm{Ca}_{3} \mathrm{Y} \mathrm{O}$ |  |  |  |  |
| Sanidin | $\mathrm{K}^{2} \mathrm{O}, \mathrm{Al}^{2} \mathrm{O}^{3}$ | 6-6.5 | 2.5-2.6 | v | Gr. W. |
| Sapphire | $\mathrm{Al}^{2} \mathrm{O}^{3}$ | 9 | 3.9-4.16 | IIIX | B1. |
| (corundum) | $\mathrm{Al}^{2} \mathrm{O}^{3}, \mathrm{Na}^{2} \mathrm{O}$, | 6 | $2 \cdot 5-2 \cdot 9$ | II | R. |
| Sartorite | PbS , ${ }^{\text {as }}$ |  |  |  |  |
| Sartorite | $\mathrm{Bo}^{2} \mathrm{O}^{3}, 3 \mathrm{H}^{2} \mathrm{O}$ | ${ }_{1}^{3}$ | $1 \cdot 48$ | VI | C. Y. Gr. |
| Satinspar | $\mathrm{CaO}, \mathrm{SO}^{3}, 2 \mathrm{H}^{2} \mathrm{O}$ | 1.5-2 | $2 \cdot 33$ | V | C. Y. Br. R. |
| Scapolite | Al | 5-6 | $2 \cdot 6-2 \cdot 8$ | II |  |
| (wernerite) | $\mathrm{CaO}, \mathrm{WO}^{3}{ }^{2 \mathrm{SiO}^{2}}$. | 4.5-5 | 5.9-6 | II× | . |
| Schillerspar | 3M | 3.5-4 | 2.6-2.8 | 0 | Gr. ${ }_{\text {Gr. Y. }}$ |
| (decomposed | - $2 \mathrm{H}^{2} \mathrm{O}$ |  |  |  |  |
| Scolecite ${ }^{\text {bronzte) }}$ | $\mathrm{CaO}, \mathrm{Al}^{2} \mathrm{O}^{3}$, | 5-5.5 | $2 \cdot 2$ | v | C. |
| Scorodite. | $\mathrm{Fe}^{2} \mathrm{O}^{3}, \mathrm{As}^{2}$ | 3.5-4 | 3•1-3.3 | IV | $\mathrm{Ge} . \mathrm{B}$ |
| Selenite | CaO , |  |  | V |  |
| Senarmonite. |  | 2.5-4 | 2.5-2.6 | IV? | Gr. Br |
| Sepiolite | $2 \mathrm{MgO}, 3 \mathrm{SiO}^{2}$ | $2-2 \cdot 5$ | 0.98-1.2 | 0 | W. Gr. Y. R. |
| Serpentine . |  | $2 \cdot 5-4$ | $2 \cdot 5-2 \cdot 6$ | IV? | $\mathrm{Ge} . \mathrm{Br} . \mathrm{Y}$. |

List of Minerals (continued).

| N:me. | Composition. | Hardness. | Specific Gravity. |  | Colour. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Siderite | $\mathrm{FeO}, \mathrm{CO}^{2}$ | 3.5-4.5 | $3 \cdot 7-3.9$ | III $\times$ | c. Gr. F |
| Sillimanite | $\mathrm{Al}^{2} \mathrm{O}^{3}, \mathrm{SiO}^{2}$ | 6-7 | 3•23 | IV | Gr. Br. Ge. |
| Silver native | ${ }^{\mathrm{Ag}}$ | 2.5-3 | $10 \cdot 1-11 \cdot 1$ | I | W. Gr. |
| Silver glance (argentite) | Ag ${ }_{\text {Sb, }}$ | 2-2.5 | 7•19-7•36 | I | Gr. |
| Skutterudite | CoA | 5.5-6 | 6. | I | W. |
| Smaltine ${ }_{\text {Smithsonite }}$. | (Co, Fe, Ni) | 5.5-6 | $6 \cdot 4-7 \cdot 2$ | I $\pi$ |  |
| Smithsonite. Sodalite - | $\mathrm{ZuO}, \mathrm{CO}^{2}$ $3 \mathrm{Na}^{2} \mathrm{O} .3 \mathrm{Al}^{2} \mathrm{O}$ | $5 \cdot 5{ }^{5}$ | $4 \cdot 4 \cdot 5$ $2 \cdot 1-2 \cdot 4$ | IIIX |  |
|  | ${ }_{\text {caO }}^{6 \mathrm{SiO}^{2}, 2 \mathrm{NaCl}}{ }^{2} \mathrm{NaCl}^{2}$ |  |  |  | R. B. W. |
| Sphne (titanite) | $\mathrm{CaO}, \mathrm{SiO}^{2}, \mathrm{TiO}^{2}$ | 5-5.5 | 3.4-3.56 | V | Gr. Br. Y. Ge. B. |
| Spessartite | $(\mathrm{MnFe})^{3} \mathrm{Al}^{2} \mathrm{Si}^{\text {i }}{ }^{12}$ | $6 \cdot 5-7 \cdot 5$ | $3 \cdot 7-4 \cdot 4$ | I | R. |
| Spinel (pleonaste) | $\mathrm{MgO}, \mathrm{Al}^{2} \mathrm{O}^{3}$ | 8 | 3.5-4.1 | I | $\begin{aligned} & \text { R. Bl. Ge. Y. } \\ & \text { Br. B. } \end{aligned}$ |
| Spodumene. | $3\left(\mathrm{Li}^{2}, \mathrm{Na}^{2}, \mathrm{Ca}\right) \mathrm{O}$, | 6.5-7 | $3 \cdot 1$ | V | , |
| Stannite | Cu'S, FeS, ${ }^{\text {d }}$, ${ }^{2}$ | 7 | $4 \cdot 3-4 \cdot 5$ | I $\times$ | Gr. |
| Staurolite | $4(\mathrm{Fe}, \mathrm{Mg}) \mathrm{O}$ | 7-7.5 | 3.4-3.8 |  | Br. |
| Steatite (tale, soapstone) | $3 \mathrm{MgO}, 4 \mathrm{SiO}^{2}$, $\mathrm{H}^{2} \mathrm{O}$ | $1-1 \cdot 5$ | $2 \cdot 6$ | 0 | Ge. Gr. W. Br. Y. |
| Stephanite . | ${ }_{5} \mathrm{Ag}^{2} \mathrm{~S}+\mathrm{Sb}^{2} \mathrm{~S}^{3}$ | 2-2.5 | $6 \cdot 2-6 \cdot 3$ | IV |  |
| Stibnite (antimonite) | Sb | 2 | $4 \cdot 5$ | IV | Gr. B |
| Stilbite . . | $\mathrm{CaO}, \mathrm{Al}^{2} \mathrm{O}^{3}$, $6 \mathrm{SiO}^{2} 5 \mathrm{H}^{2} \mathrm{O}$ | 3.5-4 | $2 \cdot 1$ | V |  |
| Stilpnomelane | $\begin{aligned} & \left(\mathrm{Fe}^{2} \mathrm{Ca}^{2} \mathrm{Mg},\right. \\ & \left.\mathrm{K}^{2}\right) \mathrm{O}, \mathrm{Al}^{2} \mathrm{O}^{3}, \end{aligned}$ | 3-4 | 3-3.4 | ? | B. |
| Stolzite | $\mathrm{PbO}, \mathrm{WO}^{3}$ | 3 | 7.9-8•1 | II $\pi$ | Br. Gr. R. Y. |
| Stromeyerite | $\mathrm{Ag}^{2} \mathrm{~S}, \mathrm{Cu}^{2} \mathrm{~S}$ | 2.5-3 | $6.2-6.3$ | IV | Gr. |
| Strontianite. | $\mathrm{SrO}, \mathrm{CO}^{2}$. | 3.5- | -6 | IV |  |
| Succinite. | Fossil resin | 2-2.5 |  |  | W. Y. Br. R. |
| Sulphur |  | -2.5 | $2 \cdot 072$ | IV |  |
| Sylvanite | ( $\mathrm{Au}, \mathrm{Ag}$ ) $\mathrm{Te}^{3}$ | 1.5-2 | $7.9-8.3$ | V | Gr. |
| Sylvite . - |  | ${ }_{2}^{2}$ | $1 \cdot 9.2$ | V |  |
| Syngenite (kaluszite) | $\begin{array}{r} \mathrm{K}^{2} \mathrm{O}, \mathrm{SO}^{3}+\mathrm{CaO} \\ \mathrm{SO}^{3}+\mathrm{H}^{2} \mathbf{0} \end{array}$ | 2 26 | $2 \cdot 6$ | V |  |
| Tachhydrite | $\mathrm{CaCl}^{2}, 2 \mathrm{M}$ | 2 | 1.9-2 | III $\times$ | C. |
| Talc (steatite, soapstone) | $3 \mathrm{MgO}, 4 \mathrm{SiO}^{2}$, $\mathrm{H}^{2} \mathrm{O}$ | 1-1.5 | $2 \cdot 5-2 \cdot 8$ | IV | Ge. Gr. W. |

COMPOSITION, HARDNESS, ETC., OF MINERALS. 229
List of Minerals (continued).

| Nime. | Composition. | Hardness. | - Specific Gravity. |  | Colour. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Tantalite . | $\mathrm{FeO}, \mathrm{Ta}^{2} \mathrm{O}^{5}$ | 6-6.5 | 7-8 | IV | B. |
| Tennantite | $4 \mathrm{Cu}^{2} \mathrm{~S}, \mathrm{As}^{2} \mathrm{~S}^{3}$ | 3.5-4 | $4 \cdot 3-4 \cdot 5$ | I | Gr. B. |
| Tenorite (melaconite) | CuO . | 3 | $6 \cdot 25$ | IV | Gr. B. |
| Tetradymite. | $2 \mathrm{Bi}^{2} \mathrm{Te}^{3}+\mathrm{Bi}^{2} \mathrm{~S}^{3}$. | 1-5-2 | $7 \cdot 2-7 \cdot 9$ | III $\times$ | Gr. W |
| Thenardite. | $\mathrm{Na}^{2} \mathrm{O}, \mathrm{SO}^{3}$ | $2 \cdot 5$ | 2.73 | IV | C. |
| Thomsonite (comptonite) | $\begin{gathered} (\mathrm{CaNa})^{2} \mathrm{O}, \mathrm{Al}^{2} \mathrm{O}^{3} \\ 2 \mathrm{SiO}^{2}, 5 \mathrm{H}^{2} \mathrm{O} \end{gathered}$ | $5-5 \cdot 5$ | 2.3-2.4 | IV | C. Br. |
| Thorite. . | $\mathrm{ThSiO}^{4}, 2 \mathrm{H}^{2} \mathrm{O}$ | $4 \cdot 5-5$ | $5-5 \cdot 4$ | II | Y. Br. B. |
| Tile ore . . | Limonite+ Cuprite |  | ... | 0 | R. Br. |
| Tinkal | $\mathrm{Na}^{2} \mathrm{~B}^{4} \mathrm{O}^{7}+10 \mathrm{aq}$ | $2-2.5$ | 17 | V | C. W. Gr. Bl. Ge. |
| Titanite ${ }^{\text {(borax) }}$ | $\mathrm{CaO}, \mathrm{SiO}^{2}, \mathrm{TiO}^{2}$ | $5-5 \cdot 5$ | 3 $4-3 \cdot 56$ | V | Y. Ge. Br. Gr. |
| (sphene) |  |  |  |  |  |
| Topaz . . | ${ }^{5\left(\mathrm{Al}^{2}\right) \mathrm{SiO}^{5}+} \mathrm{Al}^{2} \mathrm{SiF}^{10}$ | 8 | 3*4-3 | IV | Y. Br. R. |
| Torbernite (uranite) | $\begin{gathered} \mathrm{CuO}, 2 \mathrm{U}^{2} \mathrm{O}^{3} \\ \mathrm{P}^{2} \mathrm{O}^{5}, 8 \mathrm{H}^{2} \mathrm{O} \end{gathered}$ | 2-2.5 | $3 \cdot 4-3 \cdot 6$ | II | Ge. |
| Touchstone . | $\mathrm{SiO}_{2}$ impure | 7 | $2 \cdot 8$ | 0 | B. |
| Tourmaline . | (Al, Fe, Mn, <br> $\mathrm{Mg}) \mathrm{SiO}^{2}, \mathrm{~B}^{2} \mathrm{O}^{3}$ | 7-7•5 | $2 \cdot 9-3 \cdot 3$ | III $\times$ | B. Br. R. Bl. Ge. |
| Tremolite (amphibole) | $(\mathrm{CaMg}) \mathrm{OSiO}^{2}$. | 5-6.5 | 2.9-3•1 | V | W. Gr. |
| Tridymite . | $\mathrm{SiO}^{2}$. | 7 | 2.28-2.3 | III | C. W. |
| Triphylite - | $(\mathrm{Mn}, \mathrm{Fe}) \mathrm{LiPO}^{4}$ | $5 \stackrel{5}{5}$ | 3.5-3.6 | IV | Ge. Gr. Br. |
| Triplite . | ( $\mathrm{Mn}, \mathrm{Fe})^{3} \mathrm{P}^{2} \mathrm{O}^{8}$, <br> ( $\mathrm{Mn}, \mathrm{Fe}$ ) $\mathrm{Fl}^{2}$ | 5-5.5 | 3.4-3.8 | IV | Br. B. |
| Tripolite (infusorial | $\mathrm{SiO}^{2}$. . | $5 \cdot 5-6 \cdot 5$ | 1-9-2 | O | W. |
| Trona earth) | $\begin{gathered} \left(\mathrm{Na}^{2} \mathrm{O}\right)^{2}\left(\mathrm{CO}^{2}\right)^{3}, \\ 3-4 \mathrm{H}^{2} \mathrm{O} \end{gathered}$ | $2 \cdot 5-3$ | $2 \cdot 11$ | V | C. Gr. Y. |
| Tungstite | $\mathrm{WO}^{3}$. . | Snft |  | IV | Y. Ge. |
| Turgite. | $\mathrm{H}^{2} \mathrm{Fe}^{2} \mathrm{O}^{7}$ | $5-6$ | $4 \cdot 1-4 \cdot 6$ | O | R. B. RB |
| Turquois . | $\begin{array}{r} 2 \mathrm{Al}^{2} \mathrm{O}^{3}, \mathrm{P}^{2} \mathrm{O}^{5} \\ 5 \mathrm{H}^{2} \mathrm{O} \end{array}$ | 6 | $2 \cdot 6-2 \cdot 8$ | 0 | Bl. Ge. |
| Ulexite. | $\begin{aligned} & \mathrm{Na}^{2} \mathrm{O}, 2 \mathrm{CaO}, \\ & 5 \mathrm{Bo}^{2} \mathrm{O}^{3}, 14 \mathrm{H}^{2} \mathrm{O} \end{aligned}$ | Soft | 1.6-1.8 | ? | W. |
| Ullmannite | NiSbS. . | 5-5.5 | $6 \cdot 2-6 \cdot 5$ | $\mathrm{I} \times$ | Gr. B. |
| Uraninite (pitchblende) | $\begin{aligned} & \mathrm{U}^{3} \mathrm{O}^{4}(\mathrm{~Pb}, \mathrm{Fe}, \\ & \mathrm{Ag}, \mathrm{Ca}, \mathrm{Mg}, \mathrm{Bi}, \end{aligned}$ | 3-6 | $4 \cdot 8-8$ | I | B. |
| Uranite | $\mathrm{CuO} 2 \mathrm{U}^{2} \mathrm{O}^{2} \mathrm{P}^{2} \mathrm{O}^{5}$, | 2-2.5 | 3.4-3.6 | II | Ge. |
| (torbernite) | $\mathrm{U}^{3} \mathrm{O}^{4}(\mathrm{Fe}, \mathrm{Cn}$, Ca) $\mathrm{O}, \mathrm{SO}^{3}, \mathrm{H}^{2} \mathrm{O}$ | $2-2.5$ | $3 \cdot 19$ | IV | Ge. |
| Valentinite . | $\mathrm{Sb}^{2} \mathrm{O}^{3}$ | $2 \cdot 5-3$ | $5 \cdot 6$ | IV | W. Y. Gr. R. |

List of Minerals (eontinued).

| Name. | Composition. | Hardness. | Specific Gravity. |  | Colour. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Vanadinite | $3 \mathrm{~Pb}^{3} \mathrm{~V}^{2} \mathrm{O}^{8}+\mathrm{Pb}$ | $2 \cdot 7-3$ | 6.6-7.2 | IIIT | Y. Br. R. |
| Vauquelinite. | $3(\mathrm{PbCu}) \mathrm{O}, \mathrm{Cr}^{2} \mathrm{O}^{3}$ | 2.5-3 | 5.5-5.8 | V | Ge. Br. B. |
| Vesuvianite (idocrase) | $\left.{ }^{2( } \mathrm{Al}^{2} \mathrm{Ca}^{3}\right) \mathrm{O}^{3}{ }^{3} \mathrm{SO}^{2}$ | 6.5 | 3.3-3.45 | II | Ge. Br. Bl. Y. |
| Vivianite. - | $3 \mathrm{FeO}, 2 \mathrm{P}^{2} \mathrm{O}^{5}$, | 1.5-2 | 2.58-2.68 | v | Bl. Ge. W. |
| Volborthite . | $\begin{array}{r} \left(\mathrm{Cu}, \mathrm{Ca} \mathrm{~V}^{2} \mathrm{O}^{5}{ }^{5} \mathrm{O}\right. \\ \hline \end{array}$ | 3-3.5 | $3 \cdot 5$ | ? | Ge |
| Wad | $2 \mathrm{MnO}^{2}+\mathrm{aq}$ ? | 0.5-6 | 3-4.2 | 0 | Br. B. |
| Wagnerite | ${ }_{2}^{2 \mathrm{MgPO}^{4}} \mathrm{Mg}^{\text {a }} \mathrm{MgFl}^{2}$ | 5-5.5 | ${ }^{3}$ | $\stackrel{\text { v }}{ }$ | ${ }_{\text {Y. Gr }}$ Gr. |
| Wavellite | $2 \mathrm{Al}^{2} \mathrm{P}^{2} \mathrm{O}^{8}+$ | 3.25-4 | . 33 | IV | Gr. Y. Ge. |
| Witherite | $\mathrm{BaO}, \mathrm{CO}^{2}$. | 3-3.75 | 4.3-4.35 | IV | C. W. Y. Ge. |
| Wöhlerite | $\left(\mathrm{Ca}, \mathrm{Na}^{2}, \underset{\mathrm{SiO}^{2}}{ }\right.$ <br> $\mathrm{Mn}) \mathrm{O}, \mathrm{SiO}^{2}$ | 5.5 |  | V | Y. Br. |
| Wolfram . | $\left(\mathrm{Fe}, \mathrm{Mn}\right.$ ) O , $\mathrm{WO}^{3}$ | 5-5.5 | 7•1-7•5 | v | Gr. B. |
| Wollastonite | $\mathrm{CaO}, \mathrm{SiO}^{2}$ | 4.5-5 | 28 | v | C. Ge. Y. Gr. |
| Wulfenite | $\mathrm{PbO}, \mathrm{MoO}^{3}$ | 3 | 6.0-7.1 | $\mathrm{II} \pi$ | C. Gr. Ge. R. |
| Wurtzite . | ZnS . | 3.5-4 | 3.9-4 | III | Br. B. |
| Xanthophyl- | $2(\mathrm{Mg}, \mathrm{Ca})^{3} \mathrm{SiO}^{8}$ | 4.5-5.5 | 3 | v | Y. Ge. |
| Xanthoside- | $\stackrel{+3 \mathrm{~S}^{2} \mathrm{O}^{3}, \mathrm{SiO}^{2}}{+}{ }^{\text {a }}$ | 2.5 | ... | ? | Y. Br. |
| Xenotime ${ }^{\text {rite }}$. | (Y, Ce, ) PO | 4.5 | $4 \cdot 5$ | II | Br. R. Y. Gr. |
| Yttrocerite | $2\left(9 \mathrm{CaF}^{2}+2 \mathrm{Y}\right.$ | 4-5 | $3 \cdot 45$ | ? | W. Gr. V. R. |
| Yttrotantalite | $(\mathbf{Y}, \mathrm{Ca}, \mathrm{Fe},)^{2}$ | 5-5.5 | 5•4-5.9 | IV | B. Br . |
| Yttrotitanite | $\begin{aligned} & \mathrm{SiO}^{2}+\mathrm{TiO}^{2}+ \\ & \mathrm{Al}^{2} \mathrm{O}^{3}+\mathrm{Fe}^{2} \mathrm{O}^{3} \\ & +\mathrm{CaO}+\mathrm{YO}+ \\ & \mathrm{CeO} \end{aligned}$ | 6-7 | 3.5-3.7 | V | Br. B. |
| Zaratite | $\mathrm{NiO}, \mathrm{CO}^{2}, 2 \mathrm{Ni}$ | 3 | 2.6-2.69 | ? | Ge. |
| Zincite | $\mathrm{ZnO})^{2}$, | 4-4.5 | 5.4-5.7 | III | R. Y . |
| Zircon . | $\mathrm{ZrO}^{2}, \mathrm{SiO}^{2}$ | 7.5 | 4-4.75 | II | R. Br. Y. C. |
| Zoisite | $\mathrm{Ca}^{4}\left(\mathrm{Al}^{2}\right)^{3} \mathrm{H}^{2} \mathrm{Sib}^{6}$ | 6-6.5 | 3.1-3.4 | IV | C. Gr. Ge. Y. |
| Zwieselite (triplite) |  | 5-5.5 | 3.4-3.8 | IV | Br . B. |



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Table of the Distinguishing Characteristics of Gems（continued）．

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TABLE of THE Distinguishing Characteristics of Gems（continued）．

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## SPECIFIC GRAVITY OF SOLIDS.

Let $(a)$ be the weight of dry substance in air.
(b) the increased weight of a given quantity of water to which the substance has been added, free from air bubbles; in other words the weight of the displaced water.

Then the specific gravity $=a \div b$.
Or weigh one or more small pieces of the substance in the air, partly fill a burette with water and take its reading; place the weighed material in the burette and shake to get rid of air-bubbles; read the burette again.

The difference is the volume of the material, and if the burette is divided into cubic centimetres, the weight in grams divided by the increased volume gives the specific gravity. If taking the specific gravity of tailings or other finely crushed material, weigh about 10 gram., add slowly to the water in the burette until its reading has been increased exactly 1 c.c., then weigh the portion remaining, and the difference in weight is the specific gravity.

## Specific Gravity Solutions.

These are used for determining the specific gravity of gems and other stones; they can be easily carried about and are of great practical utility.

Sonstedt's Solution.-Double iodide of mercury and potassium. The density can be reduced by the addition of water. The solution is very poisonous.

Klein's Solution.-Boro-tungstate of cadmium. This can also be diluted with water. It has the disadvantage of rapidly darkening on exposure to light, but the transparency can be restored.

Methylene Iodide.-This is non-poisonous ; it is also lightcoloured so that the mineral fragment can be readily seen. It can be clarified by shaking with a few drops of mercury, and can be diluted with benzine.

Of the above methylene iodide is the most convenient; by means of it any density between 0.9 and 3.3 can be readily obtained, and it is also possible to reach 3.6 by saturating it with iodoform.

Use standard solutions in stoppered tubes, and obtain a series of minerals of known density for comparison.

## SPECIFIC GRAVITY

(after Miers).

| 1.89 Melanterite | 3.53 Topaz | 5.57 Proustite |
| :---: | :---: | :---: |
| 1.98 Sylvite | $3^{3} 54$ Rhodonite | 5.57 Valentinite |
| 2.00 Goslarite | $3 \times 56$ Realgar | 5.65 Iodyrite |
| 2.07 Sulphur | ${ }^{3} 62$ Cyanite | 5.68 Arsenic |
| $2 \cdot 12$ Chrysocolla | 3.65 Staurolite | 5.68 Columbite |
| $2 \cdot 12$ Chabazite | 3.67 Chrysoberyl | 5.70 Samarskite |
| 2.13 Nitre | 3.69 Strontianite | 5.75 Copper Glance |
| $2 \cdot 14$ Salt | 3.72 Pyrope | 5.75 Jamesonite |
| 215 Opal | $3 \times 76$ Atacamite | 5.80 Bournonite |
| $2{ }^{16} 6$ Graphite | 3.80 Limonite | 5.80 Fergusonite |
| ${ }^{2} 16$ Stilbite | 3*80 Azurite | 5.85 Pyrargyrite |
| $2 \cdot 21$ Chalcanthite | 8.86 Chalybite | 6.00 Cuprite |
| $2 \cdot 26$ Analcite | 3.96 Celestite | 6.00 Crocoite |
| 2.30 Sodalite | 4.03 Ilvaite | 6.00 Scheelite |
| $2 \cdot 32$ Gypsum | 4.03 Corundum | 6.05 Mispickel |
| 2.33 Wavellite | 4.06 Blende | 6.10 Polybasite |
| $2 \times 35$ Apophyllite | 4.10 Spinel (from 3.55) | 6.15 Cobaltite |
| ${ }^{2} 47$ Leucite | 4.15 Almandine | 6.22 Smaltite |
| 2.55 Bauxite | 4.20 Gothite | 6.25 Stephanite |
| $2 \cdot 56$ Serpentine | 4.20 Psilomelane | 6.25 Anglesite |
| 2.56 Orthoclase | 4.20 Copper Pyrites | 6.45 Bismuthinite |
| ${ }^{2} 600$ Nepheline | 4.22 Rutile (up to $5^{\circ} 2$ ) | 6.51 Cerussite |
| $2 \cdot 62$ Chalcedony | 4.30 Witherite | ${ }^{6.69}$ Antimony |
| 2.63 Vivianite | 4.30 Garnet (from 315) | 6.80 Pyromorphite |
| $2 \cdot 64$ Albite | 4.37 Calamine | 6.83 Vanadinite |
| 2.65 Quartz | 4.41 Stannite | ${ }^{6} 885$ Wulfenite |
| $2 \cdot 66$ Oligoclase | 4.44 Enargite | 6.88 Bismutite |
| $2 \cdot 66$ Alunite | 4.45 Chromite | 6.95 Cassiterite |
| 2'69 Beryl | 4.48 Barytes | 712 Mimetite |
| $2 \cdot 70$ Talc | 4.55 Kermesite | 715 Tantalite |
| 2*71 Labradorite | 4.57 Antimonite | $7{ }^{7} 28$ Argentite |
| 2.72 Turquoise | 4.61 Pyrrhotite | 735 Wolfram |
| 2.72 Calcite | 4.69 Zircon | 7.40 Tetrady mite |
| $2 \cdot 85$ Dolomite | 4.75 Molybdenite | 7.50 Galena |
| 2.85 Lepidolite | 4.79 Pyrolusite | 7.55 Iron |
| 2.85 Wollastonite | 4.79 Fahlore | 8.00 Stolzite |
| 287 Prehnite | 4.84 Ilmenite | 8.00 Clausthalite |
| 2.90 Biotite | 4.88 Marcasite | 8.10 Cinnabar |
| 2.93 Muscovite | 4.90 Thorite | 8.10 Sylvanite |
| 2.94 Aragonite | 4.90 Cerite | 8.84 Copper |
| 3.06 Magnesite | 5.03 Pyrite | $8{ }^{\circ} 86$ Petzite |
| $3 \cdot 10$ Actinolite | $5 \cdot 10$ Monazite | $9^{\circ} 00$ Calaverite |
| ${ }^{3} 14$ Tourmaline | ${ }_{5}{ }^{15}$ Franklinite | 9.35 Pitchblende |
| ${ }^{3} 32$ Dioptase | 5.17 Magnetite | 9.60 Dyscrasite |
| ${ }_{3} 333$ Olivine | 5.20 Erubescite | ${ }^{9} 76$ Bismuth |
| $3: 34$ Jaderite | $5 \cdot 20$ Rutile (from 4*22) | 10*60 Silver |
| 3*40 Epidote | 5.23 Hematite (from $5^{\circ} 0$ ) | 13.60 Mercury |
| 3.45 Orpiment | 5.25 Senarmontite | 18.90 Amalgam |
| ${ }^{3} 45$ Hypersthene | 5.35 Embolite | 17.00 Platinum |
| 3.50 Sphene | 5.48 Millerite | 19.00 Gold |
| $3^{3} 52$ Diamond | 5.55 Cerargyrite | $20^{\circ} 00$ Iridosmine |
| 3.52 Rhodocrosite | 5.55 Zincite | $23^{\circ} 00$ Iridium |



## PETROLOGY.

The rocks of the earth's crust are best classified in three main groups, according to their mode of origin as follows:-

1. Igneous. 2. Aqueous. 3. Metamorphic.

## 1. Classification of Igneous Rocks.

The classification and nomenclature of igneous rocks is a matter of exceptional difficulty. They are complex in chemical constitution and mineralogical composition, and are often found grading into one another imperceptibly. There is no generally accepted principle, and great confusion exists. Moreover, igneous rocks in the vicinity of ore deposits are usually much altered ; their character may, indeed, be completely obliterated.
The methods of classification in most general use necessitate the exact determination of the minerals present $\frac{\text { and }}{\text { or }}$ a chemical analysis. The precise determination of the minerals involves the use of special microscopes and the preparation of slides; it can only be satisfactorily employed by the specialist. Similarly, the making of a chemical analysis is usually impracticable.
A. Outline Classification by Silica and Alkali Percentages, combined with Texture.

|  | Acid <br> (Silica greater than $60 \%$ ). | InTE (Silica grea Orthoc Plagio | EDIATE <br> than $52 \%$ ). <br> felspar. <br> e felspar. | Basic (Silica less than 52 ) . | Ultrabasic. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Holocrystalline | Granite Monzonite Quartz-diorite Grano-diorite | Syenite | Diorite | Gabbro <br> Dolerite | Peridotite, etc. |
| Hemicrystalline | Quartz-porphyry <br> Rhyolite | Trachyte | Andesite | Basalt | Limburgite |
| Glassy . | Pitchstones |  |  | Tachylite | - |

B. Outline of Classification based primarily upon Mode of Occurrence, and secondarily upon Texture and Mineral Constitution.

1. Plutonic (holo-
crystalline rock
masses consoli-
dated at a
depth). $\quad \begin{cases}\text { Granite. } & \begin{array}{c}\text { Quartz and alkali-felspar, } \\ \text { with other minerals. }\end{array} \\ \text { Syenite. } & \begin{array}{l}\text { Alkali-felspar the chief con- } \\ \text { stituent. }\end{array} \\ \text { Liorite. } & \begin{array}{l}\text { Lime - felspar and horn- } \\ \text { blende. }\end{array} \\ \begin{array}{l}\text { Gabbro. } \\ \text { Lime-felspar and pyroxene. } \\ \text { Olivine the most prominent } \\ \text { constituent. }\end{array} \\ \text { Peridotite. }\end{cases}$
2. Volcanic | (mainly lavas). $\begin{cases}\text { Rhyolite. } & \text { All truly acid lavas. } \\ \text { Trachyte and } & \text { Alkaline lavas without } \\ \text { phonolite. } & \text { quartz. } \\ \text { Andesite. } & \text { Alkali - felspar with ferro- } \\ \text { masalt. } & \text { magnesium minerals. } \\ \text { All basic lavas not high in } \\ \text { Alkali-basalt. } & \text { alkali. }\end{cases}$ |
| :--- |
| Alkaline basic lavas. |



## TABLE FOR DISCRIMINATION OF THE PRINCIPAL MINERALS of which Igneous Rocks are composed.

Quartz.
Felspar.
Mica.

Amphibole (usually hornblende).
Pyroxene
(usually augite). Olivine.

Vitreous lustre. No cleavage. Not touched by steel.
Vitreous lustre. Good cleavage. Just scratched by good steel. May be striated. Glistening appearance. Very easily split into flexible laminæ. Readily scratched. May be of any colour, but frequently black.
May show cleavage. Scratched with some difficulty, producing a streak much lighter than the mineral. Green to black. These minerals are difficult to distinguish from one another.
Vitreous lustre. No cleavage. Not touched with a knife. Often granular and green. (Only found in dark basic rocks, never in granitic varieties.)
Calcite.

Readily scratched, effervesces with cold dilute acid.

## 2. Classification of Sedimentary Rocks.

Conglomerate. Pebbles cemented by iron oxide or other substances.
Sandstone. Sand cemented by iron oxide or other substances.
A sandstone is approximately uniform in grainsize. Different sandstones vary greatly in colour and grain-size. The constituent grains can generally be distinguished with a lens.
Breccia.
Shale.

Clayslate.
Slate.
Phyllite.

The constituent fragments are angular, and may vary in size.
Laminated, indurated mudstone. Dark in colour, but may become reddened or even bleached by atmospheric agencies, Earthy odour when scratched and breathed upon.
A shale splitting along planes of cleavage induced by pressure.
Clayslate with perfect and regular fissility.
Clayslate showing a not very conspicuous development of mica along the cleavage planes.

Limestone.

Magnesian
Limestone.

May exhibit every grade of colour and texture. Readily scratched. Effervesces freely under a drop of dilute cold acid.
Differs from normal limestone in effervescing less freely or not at all unless warm acid is used.

## 3. Classification of Metamorphic Rocks.

Gneiss.

Schist.

Mica-schist, Chlorite-schist, Hornblende-schist, Talc-schist, etc.

Crystalline Limestone.

Serpentine. Quartzite.

Comparable to a banded granite, the constituent minerals being respectively grouped in parallel bands.
Highly foliated, consisting of layers of mica, chlorite, and other minerals, with or without more or less quartz between them.

Dark green, homogeneous, usually mottled. Easily scratched with a knife.

Sandstone in which the grains are toughly cemented by silica. May even appear homogeneous to the eye, in extreme cases.

## SAMPLING.

Truscott states that "Sampling includes all operations which result in obtaining from any bulk of ore a smaller quantity which fairly represents the bulk in all respects, except amount; and which in amount is convenient for testing, so as to enable the value or composition of the whole bulk to be ascertained.'

One should sample what the miners will work, and classify it into (a) ore suitable for treatment, (b) ore to be dressed, (c) waste; if it occurs in such a manner. With a vein too narrow to stope in, some of the wall rock must be broken to make room for working; if it is cheaper to treat this than to pick it out, allowance must be made for the adulterant. In many veins the wall rocks are rotten and fall in, or the miners may put in a heavy charge and fetch down some of the rock, which increases the tonnage, but decreases the value per ton of ore. This is a frequent cause of discrediting systematic
sampling by those who do not know any better. When once a fair amount of work has been done, a factor may be ascertained for any particular instance, with which a correction can be made. To standardise values to a fixed stoping width, suppose the average width of the true vein to be $17 \cdot 5$ inches and the average value 14.7 dwt ., then to standardise this to 36 in ., as $36: 17 \cdot 5:: 14 \cdot 7: 7 \cdot 1 \mathrm{dwt}$. When treating the ore, we must allow for tailings carrying away more of the values if increased in bulk by waste.

Every mine is not suitable for sampling. The more uniform the grade the more correct the sampling will be, while the greater the number of samples taken, the better any irregularities are averaged. Every precaution should be taken against salting, either by others or unintentionally by oneself. Where a sampler has to work alone amongst strangers it is almost impossible for him to take his samples and protect them too. : The only thing is to use his judgment, take several duplicates in important places, mix barren samples among his other bags, be careful to clean down the faces to be sampled, keep strangers at a distance, and take any other precautions that local circumstances may suggest, but they should be done tactfully and without ostentation, otherwise men may be tempted to salt out of devilment. A salter generally gives himself away by overdoing it. He may prepare the place to be sampled, e.g. by firing gold into a face, or by packing alluvial deposits, or he may drop rich ore into the sample, or pick pieces of mullock out of a sample so as to enrich it. It is not always the wish of the man who shows one round that a so-called "good report" should be made; he may wish the mine to appear bad so that he can take it up himself later on, but more generally the desire is to make the mine appear better than it is. If a mine is "dressed" for sale, the faces are generally left off in rich ore, while poor or worked-out places are boarded over or filled up, and attention is specially drawn to the richer ore. Look carefully at timber that seems unnecessary. Some people are in favour of socalled bulk samples in preference to chip samples, i.e. several tons are taken and treated. If the salting danger can be eliminated, this is the better method for ores of irregular values, provided the tonnage is systematically distributed, and not taken from two or three places as is generally the case. Of course, the ore must be carefully weighed and the products and residues properly sampled. A man may salt his own samples by being careless, or adopting wrong means : he may take too much of one class of ore; he may take drillings where brittle or heavy minerals have separated out from the
others. If he relies on grab samples, he may unconsciously give preference to fine or lump ore ; if he does not clean down a face in the old workings of a copper-mine, he may get effloresced sulphate of copper that has migrated there; if he is not careful to clean the box or cloth in which he catches his samples, he may impoverish a rich sample and enrich a poor one.

First size up the nature of the deposit if possible; then arrange a scheme of sampling. Most mineral properties are unprofitable and likely to remain so. Some can be condemned at sight, others are worth a little sampling, while the minority are worth going to some expense to sample thoroughly. The ore is the main asset of a mine, and if ore of sufficient quantity and quality has been judiciously opened up, money can always be raised on it. If a mine is being sampled as developed, this sampling can be done systematically by a properly qualified official, but if the sampling has to be done some time after, it is not always possible to take regular samples, for the ore overhead may have been worked out so that one has to take samples underfoot, or rotten country may require timbering which it is not safe to remove. Take samples from roof, floor, or face at whichever the most complete section can be obtained. The tools used depend on the nature of the ore. For soft material a pick may be used, for harder a hammer and moil, or a pneumatic hand-hammer drill. Very hard ore may have to be shaken by explosives. The broken material may be caught on a sheet of canvas, protected if necessary by boards, but this is not very good as the pieces are apt to fly off the sheet, the sample is apt to be contaminated with dirt from the men's boots, and if there is fine ore it may hang back on the cloth. Another way is to catch it in a suitable wooden box held by an assistant, or if the sample has to be taken in an awkward place a canvas bag may be used, tied at the bottom, mounted on a rim which can be attached to a long handle if necessary like a landing net. Where possible, samples should be taken in the face or overhead. If it is necessary to take samples underfoot, any drainage water should be kept back by a dam of clay and carried away by a launder, and crevices carefully cleaned out both before and while sampling. In any case the place to be sampled should be carefully cleaned by chipping, and any loose pieces removed before taking the proper sample. Samples should be taken across the deposit at right angles to its strike. If arched it may be necessary to break off the wings before sampling, otherwise take off-sets. One sample should not be too large. If the deposit is wide and uniform, one sample should represent, say,

4-5 feet in length, but judgment should be used in this, for if there should be a change in the nature of the ore, the sample should be taken accordingly. The depth of the cut may be, say, 2 inch and the width 3 inch, representing from 2 to 5 lbs. per foot. The proportion taken should be uniform. At first, samples may be taken, say, 20 feet apart, then, if satisfactory, the distance may be reduced till the samples are taken every 5 feet across or less for narrow lodes which are liable to fluctuate, and 10 feet for wide lodes. If too large to remove to the surface, as in places where the sampler has to carry his own samples, the sample may be reduced in some convenient place underground, using a hammer-head as an anvil. Each sample should be properly labelled and a corresponding note made in the sampler's notebook. It is advisable not to stencil the sample bags as strangers may note the mark; it is better to have stamped metal tags, or pieces of wood with Roman figures cut on them, which can be thrown in with the sample, to be picked out by the man who prepares the sample later on. Occasional dummy samples containing no values should be placed with the others as a check on the assay office, in case the numbers get mixed. If the assays are done at the mine, a certain number of duplicates are taken as a check on the sampling by another man, say $5-10$ per cent. Each cut is given a special number, so when the assays are completed the engineer can go round, book in hand, comparing the look of the cuts with the assay results. If, as is often the case, the samples have to be taken elsewhere for assay, then a large proportion of check samples have to be taken in case of accident, say 20 per cent., as it might not be convenient to re-sample. If a lode is wide, then drive samples are incomplete, only the cross-cuts giving a fair indication. Stope samples are taken to ensure the face carrying payable ore. An extra poor sample is less likely to affect results than an extra rich one. If an abnormally high assay is obtained, it is usual to average it with others on either side and take the mean. Do not assume the number of cubic feet of ore that go to a ton, but take the specific gravity of different classes of ore and work it out. When sampling coal : clean a face, cut a channel at right angles to the bedding planes, and take out a sample of about 5 lbs. per foot of thickness of coal. Include everything in the sample except partings of more than $\frac{1}{4} \mathrm{in}$. thick, and concretions of "sulphur" greater than 2 in . diameter and $\frac{1}{2}$ in. thick. A seam of coal of 1.3 specific gravity will contain about 130 tons per acre for every inch in thickness; allowing for waste, pillars, etc., 100 tons per acre per inch will be the probable yield.

It is not necessary to hand a sample of more than 3 lb . weight to the assayer. The ore is gradually reduced in size and bulk, being generally mixed, coned, and quartered on an iron plate or canvas sheet and finished up on American cloth. The samples should not be out of sight of a reliable man till reduced and under lock and key.

The results of the sampling and assaying are plotted on an assay plan. The workings as shown on an assay plan differ from the ordinary longitudinal section in so much as all bends in the drive, crosscuts, winzes, etc., are straightened out. With a narrow vein the width of the sample is put on one side of the workings, while the assay is placed on the other; the units taken may be inches, or feet for width, and dwt., ozs., or per cent. for values, according to convenience. If more than one metal of value is present, the figures belonging to it are generally noted in ink of a different colour. If a deposit consists of, say, a hanging-wall vein, a band of mullock and a foot-wall vein, or ore that can be mined direct for the smelters, concentrating ore, and waste; then these may be designated $\mathrm{A}, \mathrm{B}$, and C , a line drawn at the point sampled, and the width and value written opposite each. In order to catch the eye quicker, small circles may be drawn and filled in with washes of blue, red, etc., according to the value of the ore within certain limits, or the limits of different classes of ore may be plotted out and coloured. A sampler should make full notes of any geological features, change in country, faults, horses, etc. A graph drawn out to show the variation of values with depth is of interest; this may show that in certain cases payable ore does not go below the zone of secondary enrichment. On the other hand, if payable primary ore is going strongly underfoot, and geological conditions are favourable, e.g. an ore lens still widening, there is every chance of a fair quantity of ore ahead. A graph may show the ore to be nearly as rich as before, but a cross section may show the ore body to be narrowing. Both physical and chemical features must be studied. Ore may be classified as "ore blocked" and "ore which may reasonably be assumed to exist, though not actually blocked out.' The less a mine is developed the more one must allow for horses, intrusions, and pinches.

When examining old workings it must be borne in mind that ground stoped was not necessarily profitable, and that what appears as wide stopes may be due to the presence of a horse, or winded wall rock having fallen in. A word of caution should also be given about old crushing returns, putting aside the probability of the upper part of a lode being
naturally richer than that lower down, and that a larger volume of partly leached ore goes to a ton, In the early days of a mine ore sent away for treatment was generally picked, so as to save freight, and the tonnage was generally taken by measurement, the miners trying to get as many cubic feet into a ton as possible, a dray load often being taken as equivalent to a ton. When ore has to be sold to custom works, calculate an example for each tariff submitted. One tariff may be submitted in what appears to be a favourable form; but when worked out, on the short ton, an inferior assay, and various deductions, the terms are often found to be worse than that of a buyer who makes a straight out higher returning charge.

## MINE EXAMINATION.

When called upon to make a report, an engineer should state the facts clearly and concisely. His opinion is asked for, and there should be no ambiguity or indecision about it. If there is not sufficient work done in a mine to enable him to give a definite opinion as to its value, then he should recommend a working option, should the property in his opinion warrant the expense.

Before proceeding to a mine, the engineer should provide himself with the necessary authority to inspect, take samples, abstract information from the books, etc. He should ascertain the route which has to be taken by machinery or ore, and follow that, noting the dimensions of any railway tunnels and such other information affecting transport. If in a foreign country it is better to obtain the necessary outfit in that country, experience dictating to the inhabitants what is most suitable for the climate and local conditions.
Any information about the mine or district, official or otherwise, should be secured, that obtained from interested parties being accepted with reserve. Insist on seeing everything, and if there is a chance of any doubt being thrown on your work, get a signed statement from the man in charge to the effect that you have been shown everything. There are many points that should be noted when reporting on mining properties, but those mentioned below are not likely to all occur at one mine, neither is it necessary to embody all one notes in a report.

Name. -The name or names and numbers by which the property is known. Note if the name has been changed.

Locality.-Parish, county, country. Nearest town.
Area.-Plan showing area, and relative position to other properties if near. Show position of deposit on area.

Lease.-Give conditions, royalty, taxes, labour condition, clear title.
How Reached.-Distance from nearest railway station or port. Nature of harbour, shelter, depth of water at low tide. Condition of road. Rivers to cross. Transport. Freight.

Topography.-Mountainous or flat; altitude; character of surface vegetation, timber supply.

Water.-Annual rainfall, rainy seasons, droughts, creeks and rivers, frequency and height of floods. Water available for power. Conservation of water.

Climate.-Tropical, temperate, or frigid. Can one work all the year round? is the climate injurious to health?
Labour.-Efficient or inefficient; plentiful or scarce; if liable to strikes and labour troubles, or labour likely to be interfered with by unstable government, or raids from unfriendly tribes.

History.-Dates of opening, abandoning, reopening. Reasons for closing down. Past and present owners. Reported yields. What contracts are in existence.

Geology.-Country rocks; their relation to the deposit, their strikes and dips, hardness and toughness. Faults: their relative ages, strike, hade, throw, and heave. Nature of deposit, vein, bed, stock, stockwork, pocket, shallow alluvial, deep lead, etc.; strike, underlie, dimensions, nature of walls, dig, ores, veinstones; how the ores occur, massive, bands, disseminated ; associated minerals; leached, secondary enrichment, and primary zones; irregularities, e.g. horses, pinches, folds; shoots, pipes. If coal, its nature, gas, steam, household, coking or non-coking; liability to spontaneous combustion; presence of clay bands or "sulphur"; size of lumps into which it breaks; nature of roof and floor. Examine similar deposits in neighbourhood.

Extent of Workings.-Shafts, levels, winzes, crosscuts, their dimensions and state of preservation.

Drainage. - Water-level, quantity of water making per hour; whether corrosive or can be utilized; if mine subject to flood.

Ventilation.-Natural, furnace, fan (force or exhaust), sufficient or insufficient ; gases.

Method of Working.-Variety of stoping, caving, sluicing, dredging, longwall, bord, and pillar. Condition of workings.

Method of Supporting Ground.-Timbering, filling; if subject to creeps.

Power.-Steam, water, air, gas, electricity.
Buildings and Machinery. - Nature, conditions, and suitability.

Maps and Plans.-District, surface and underground, assay and geological plans.

Market.-Disposal of products ; tariffs.
Costs.-Present ; what may be expected with improvements.
Conclusion.-Quantity of ore blocked out and ore partly blocked, average value of ore, probable life of the mine with a certain annual output, the proper metallurgical treatment and probable cost of same. Value of mine and plant. Profit that may be expected. Capital it will stand. Working capital required. Improvements suggested. The interest required on capital put into a mine increases with the risk incurred.

Mines must be operated according to their nature. Some are only suitable for co-operative working parties, e.g. small high-grade deposits from which wages men might steal ore; others are suitable for companies with a small capital on which to pay interest; while a third class, e.g. large low-grade propositions, or those that require expensive deep shafts, require a large capital to open them up and supply the necessary plant. It is unnecessary to lock up capital by fully developing a promising deposit before equipment, but it is well to have, say, two years ore blocked out, so that one can work a mine regularly and continuously. The cost of mining generally diminishes as a mining field gets older, owing to improved transport facilities, conservation of water, improved methods, etc., so that a low-grade ore, originally valueless, may be worked at a profit, thus lengthening the life of the mine. The object of mining is to get the greatest profit from a given body of ore. One might get cleaner residues, but it might cost more to extract the last fraction than it is worth. The sooner one can get a return on his capital the better, as it saves the loss of interest through locked up profits. By working on a large scale men can be placed to better advantage, and one can make better terms for freight, purchase of stores, etc., go in for schemes (e.g. water-supply) that smaller concerns could not afford. In addition to a suitable interest on the capital invested in a mine, the shareholders require the return of their capital and that within a fairly short period, since a mine is a wasting property. This money may be put aside by the Directors for the purchase of another property, or it may be handed over to the shareholders with the dividends to apportion as they think fit. The redemption of the capital is known as amortization. Plants should be built in convenient units, which may be multiplied from time to time if circumstances warrant. This may be determined in the following manner:-Working expenses may be divided into those which vary with tonnage, e.g. development, haulage,
and treatment, which may be called fixed ; and those which vary partly with tonnage and partly with time, e.g. management, and pumping which have to go on no matter how many tons are dealt with. All the additional profit due to the expanded output (of course not including the ordinary profit on the ore) is termed the "increment of profit." According to Hoover, "If by vigorous development the visible life of a mine, as shown by the ore reserves, is lengthened, so as to exceed the time required for a unit of treatment capacity to earn an amount, through the increment of profits, equal to amortization of the capital invested in that unit, then the instalment of another unit becomes not only justifiable but an obligation of good management." Also, "The economic and advisable ore reserves should be equal in volume to the annual output multiplied by a number of years just under that needed by the increment of profits to equalize the amortization required to construct increased treatment units." In practice this principle cannot always be carried out as shareholders may refuse ta subscribe or borrow the necessary money to put their mine on a better footing. Some locally owned mines are allowed to linger on, as the storekeeper and hotel-keeper shareholders look for their profits to goods sold to the men rather than out of the mine itself. There are many other factors to be considered in successful mining besides the mine itself and its surroundings, not the least of which are the management and directorate. Because a mine has and is paying good dividends, it is no proof that it is in a condition to continue doing so. On the other hand, a property may have been developing for some years and never paid a dividend, but on account of the policy followed may be in a position to provide adequate interest for many years. Mines have been classified for speculation and investment purposes into (1) Excellent, (2) Fair, (3) Moderate, (4) Indifferent, (5) Remote, according to their prospects. J. H. Curle writes, "My formula is that a share is worth buying if the net profit in the mine-assuming developments in the bottom are normal as to worth and value-is equal to two-thirds of the market price of that mine. That means that I expect enough additional ore will be exposed in depth to at least return the one-third of the capital which is unguarded, and also pay a good interest on the whole of the capital at stake." This, of course, would only hold good where the market price of shares was not inflated. In mining expediency often predominates over system. The intrinsic value of a mine cannot be altered by market operations, but it can be very materially altered by mismanagement. Some people who are not acquainted with the technicalities of
mining think they can judge which is the better worked of two mines by comparing the working costs. In most cases the mines are not comparable, as the conditions are different, but even where the conditions are similar one wants to know if in both cases the depleted stopes have been properly secured, whether the ore obtained in development was added to the stoped ore without being debited with its proportional cost or not, whether only the easily get-at-able ore was broken, whether the various incidental expenses were charged in each case, or whether in one they simply give the cost of breaking, etc. It is well to have the technical work of a mine examined by an independent man periodically, for a similar reason that it is advisable for an auditor to go through the books of a company.

## Zimmermann's Rule for Determining the Direction in which to Drive to Find a Dislocated Reef.



Fig. 1.


Fig. 2.

Determine the strike and underlie both of the reef and dislocator. Project this on paper to scale, at two different levels. Connect the points of intersection at the two levels as shown on the projection, by a straight line, and produce it through the dislocator. Draw another line from the upper point of intersection, on the far side of the dislocator, and at right angles to it. On whichever side of the line of intersection the line at right angles to the dislocator is found, is the direction to search for the lost reef.

Figs. 1, 2, and 3 show three examples in which $d d^{\prime}$ is the dislocator at two different levels; $r, r^{\prime}, r^{\prime \prime}$, the reef ; $i, i^{\prime}$, the points of intersection; $i^{\prime} l$, the line of intersection; and ip the line drawn at right angles to the dislocator. The small arrows show the direction of the dip or underlie. Then in

Fig. 1 on passing the dislocator we would have to drive on the left hand. In Fig. 2 the reef is not displaced at all, as the lines $i^{\prime} l$, $i p$, coincide; therefore, on passing the crosscourse the reef will be immediately cut. In Fig. 3 we would have to drive to the right hand. The dotted lines in the figures show how the case would be if we approached the dislocator on its footwall, instead of its hanging wall, as shown by the


Fig. 3.


Fig. 4.
full lines of the diagram. Fig. 4 illustrates how you can easily set out the proportional distances of the underlie of the dislocator and reef at different levels for the purpose of projection.

The distance to drive before finding a lost reef can only be determined in certain cases, which requires some geological knowledge.

## To Calculate the True Thickness of an Inclined Bed when passed through in a Bore-hole.

Let AB be the thickness bored.
Then the angle $\mathrm{ACB}=$ the angle $\mathrm{ABD}=$ the dip of the bed.
$D B($ the true thickness sought $)=A B \cos . A C I$.


## To Calculate the Expense of Sinking,

Let $a=$ the amount to be paid for the first unit of depth.
$b=$ the rate of increase for each additional unit.
$n=$ the number of units to be sunk.
Then the total cost will be:-

$$
[2 a+(n-1) b] \frac{n}{2}
$$

## Uses of Rocks and Minerals.

Aluminium.-Ores.-Beauxite and cryolite.
Use.-For plating, various ornaments, instruments, aluminium bronze.

Antimony.-Ores.-Stibnite, $71 \cdot 76 \%$; valentinite, $83.56 \%$; cervantite, $79 \%$; kermesite, $75 \cdot 3 \%$; native antimony.

Use.-Various alloys (type metal, britannia metal, stereotype metal, \&c.), pigments (orange and yellow), medicine, making shot.
Market.-Crude antimony (sulphide of antimony sweated out from its gangue), star metal. Impurities, iron, lead, tin, sulphur, arsenic.
Arsenic. - Ores. - Native arsenic; orpiment $60.90 \%$; realgar, $70 \%$; arsenolite, $75.76 \%$; mispickel, $46 \%$; leucopyrite, $72.8 \%$.

Use.-Manufacture of opal glass, pigments (Scheeles green, yellow, red), various alloys, fireworks, medicine, poison for animals.

Market.-White arsenic, red arsenic. Impurities, sulphur.
Bismuth.-Ores.-Native bismuth ; bismuth ochre, $89.5 \%$; bismuthite, $75 \%$; bismuthglance, $81 \cdot 4 \%$.

Use.-Alloys (soft solder, fusible metal, \&c.), medicine, porcelain, and glass painting.

Market.-Impurities in commercial bismuth are copper, antimony, sulphur, arsenic.

Cadmium.-Ores.-Greenockite, $77 \cdot 7$, also in some ores of zinc.

Use.-The iodide and bromide used in photography, the sulphide as a yellow pigment, also in pyrotechny, Wood's alloy for stopping teeth.

Chromium.-Ores.-Chromite, $40-68 \% \mathrm{Cr}^{2} \mathrm{O}^{3}$.
Use.-Pigments (yellow, orange, red, green, blue) used in dying, calico printing, and colouring glass and porcelain. Chemicals (chromate and bichromate of potash, \&c.).

Cobalt.-Ores.-Cobaltine, $35.4 \%$; smaltine, $28.1 \%$; danaite, $5-10 \%$; erytbrine, $29 \cdot 4 \%$; asbolite, $2-15 \%$; linnæite, $22 \%$; glaucodite, $23 \cdot 8 \%$.

Use.--Pigments (smalt, cobalt or Thárard's blue, printers' blue, cobalt bronze, Rinmann's green) for colouring glass, porcelain, and stoneware.

COPPER.-Ores.-Atacamite, $59 \cdot 45 \%$; azurite, $55.26 \%$; bornite, $55.58 \%$; bournonite, $13 \%$; chalcanthite, $24 \cdot 45 \%$; chalcocite, $79 \cdot 8 \%$; chalcopyrite, $34 \cdot 6 \%$; chrysocolla, $37 \%$; covellite, $66.5 \%$; cuprite, $88 \cdot 8 \%$; dioptase, $40 \%$; domeykite, $71 \cdot 7 \%$; enargite, $48 \cdot 4$; libethanite, $53 \%$; malachite, $57.5 \%$; native copper, olivenite, stromeyerite, $31.2 \%$; tennantite, $51 \%$; tenorite, 79.85 ; tetrahedrite, $35-48 \%$; stannite.

Use.-Pipes, wire, various utensils, plates for ships, roofing, gold-saving mills, coins, alloys (brass, Prince's metal, gun metal, bell metal, German silver, yellow metal, mosaic gold, Bath metal, pinchbeck, statuary bronze), pigments (blue and green), electrical purposes, sheep-wash.
Market.-Matte, precipitate (cement copper), Chili bars (purple or blister copper in bars weighing about one and three quarter hundredweight, and containing about $95 \%$ copper). The chief brands are : common marks, good named brands, best marks, Australian P C C (Burra) cake, Wallaroo cake English longcake ( $9^{\prime \prime} \times 12 \frac{1}{2}^{\prime \prime} \times 1 \frac{3}{4}^{\prime \prime}$, weigh 1 cwt. 1 qr.), tough ingot ( $11^{\prime \prime} \times 3 \frac{12^{\prime \prime}}{} \times 1 \frac{1}{2}^{\prime \prime}$, weigh $14-16 \mathrm{lbs}$.), best selected ingot, sheets and rod, sheets ( $4^{\prime} \times 4^{\prime}$ ) for India, yellow metal sheets (4' $\times 4^{\prime}$ ) for India, sheathing.

Impuritics.-Best selected is nearly pure; tough cake and tile copper contain traces of $\mathrm{As}, \mathrm{Ni}, \mathrm{Sn}, \mathrm{Fe}, \mathrm{Bi}, \mathrm{Pb}, \mathrm{Sb}, \mathrm{S}$. Commercial copper is also contaminated with $\mathrm{Pb}, \mathrm{Fe}$, and Sb . The best copper is that refined by the electrical process.

GoLD.-Ores.-Native gold, electrum, sylvanite, $25-41 \%$, nagyagite, $6-9 \%$; also in native bismuth, iron pyrites, copper pyrites, zinchlende, galena, mispickel, stibnite, magnetic pyrites, cinnabar, hematite, \&c.

Use.-Coinage, ornaments, gold plating, gold leaf, wire, alloys, stopping teeth, pigments.

Market.-Gold may be produced as amalgam, retorted gold, or bar gold. The standard of purity is 24 carat; but this being too soft for most purposes is alloyed with silver or copper in various proportions; standard gold contains 22 pts. pure gold and 2 pts . of some other metal.

Iridium.-Ores.-Osmium-iridium, also in connection with platinum and palladium.

Use.-Sesquioxide of iridium is used in porcelain painting to produce black and grey colours; for the nibs of gold pens; knife edges of fine balances; tips of rubber cutting tools; in the construction of electric apparatus; alloys with copper, gold, mercury, and platinum.

Iron.-Ores.-Chalybite, $48.3 \%$; goethite, $62.9 \%$; hematite, $70 \%$; limonite, 59.9 ; magnetite, $72.4 \%$; menaccanite, chromite, franklinite.

Use.-Rails, various machines, tools, instruments and utensils; in architecture, shipbuilding, nails, bridges, pigments, medicine, pipes, wire.

Market.-Iron is sold in pigs, bars, rods, hoops, sheets, plates, \&c., and as copperas. Impurities in iron are silica, phosphorus, carbon, manganese, and sulphur. Besides cast iron, we get wrought iron, spiegeleisen, steel, chrome-steel, \&c., blue billy (a ferruginous residue).

Lead.-Ores.-Anglesite, $68.32 \%$; bournonite, $42.58 \%$; Cerussite, $77.53 \%$; crococite, $64 \%$; galena, $86.55 \%$; mimetite, $69.57 \%$; minium, $90 \%$; pyromorphite, $76.35 \%$.

Use.-Pipes, sheets for lining tanks, sulphuric acid chambers, roofing, flooring, shot, alloys (type metal, solders, \&c.), white lead for paint, litharge, glass and pottery, medicine.

Market.-Sold in pigs as English favourite shipping brands, ordinary brands, Spanish pig with silver, rich with silver, or without silver. Litharge powdered and English flake. Red lead. Impurities: hard lead contains antimony, zinc, copper, iron, bismuth, nickel, cadmium, sulphur.

Manganese.-Ores.-Alabandite, $63.3 \%$; braunite, $69.6 \%$; dialogite, $47.7 \%$; hauerite, $46.3 \%$; Hausmannite, $76.9 \%$; manganite, $62.5 \%$; psilomelane, $52 \%$; pyrolusite, $63.2 \%$; rhodonite, $42 \%$; wad.

Use.-Glass staining and pottery painting ; in the production of oxygen and chlorine (for bleaching powder), added to iron to improve steel. Chemicals (permanganate of potash).

Impuritics.-Silica, phosphoric acid, sulphur, \&c.
Mercury.-Ores.-Native quicksilver, native amalgam, $64.93-73.53 \%$; calomel, $84.93 \%$; cinnabar, $86.21 \%$; some fahlerz contain from $3-16 \%$ mercury.

Use.-For amalgamating gold, for scientific purposes, manufacture of instruments (barometers, thermometers, \&c.), silvering mirrors and reflectors. Chemicals (corrosive sublimate, calomel) for preserving skins, dyeing, printing, etching, pigments (vermilion), fulminate for percussion-caps, medicine.

Market.-Sold in iron bottles containing 75 lbs. each.
Molybdenum.-Ores.-Molybdenite, $60 \%$; molybdite, wulfenite. Use.-Blue pigment for pottery ware.

Nickel.-Ores.-Annabergite, $29.6 \%$; chloanthite, $28 \%$; garnierite, $10-30 \%$; gersdorffite, $35.1 \%$; nickeline, $43.6 \%$; noumeite, $5-20 \%$; millerite, $64 \cdot 4 \%$; pentlandite to $20 \%$; linnæite, $33 \%$; zaratite ; breithauptite, $32.2 \%$.

Use.-Alloys (German silver for coins and trinkets, nickelsteel, \&c.), plating wares.

Osmium.-Used in the examination, staining, and preservation of microscopical anatomical specimens.

Palladium.-Ores.-Native.
Use.-Sometimes used for finely divided scales of mathematical and astronomical instruments, for smaller chemical weights, $1 \%$ added to steel produces a smoother cutting edge; palladium amalgam used by dentists for stopping teeth. Alloys, $60-75$ pts. Pd, $15-25 \mathrm{pts} . \mathrm{Cu}$, and 1-5 pts. Fe, used for nonmagnetic watches.

Impurities.-Rhodium.
Platinum.-Ores.-Native.
Use.-Chemical apparatus (evaporating dishes, crucibles, retorts, funnel points, spatulas, combustion boats, blowpipe tips, forceps, weights, foil, wire, \&c.), pins in artificial teeth, tops of lightning-rods, electric lights, galvanic apparatus, trinkets, medals, mirrors, porcelain painting.

Impurities.-Iridium, gold, palladium, osmium, iron, copper, sulphur, phosphorus, arsenic.

POTASSIUM.-Used as a chemical (cyanide, yellow and red prussiate, bromide, iodide, chloride, chlorate, carbonate, caustic, chromate, bichromate, nitrate, sulphate).

Silver.-Ores.-Amalgam, $26.5-65 \%$; argentite, $87 \cdot 1 \%$; bromargyrite, $57.45 \%$; discrasite, $64 \%$; embolite, $66 \%$; hessite, $62 \%$; iodargyrite, $46 \%$; cerargyrite, $73.3 \%$; miargyrite, $37 \%$; native silver; polybasite, $64 \cdot 2-72 \cdot 4 \%$; stephanite, $68.35 \%$; sternbergite, $33 \%$; stromeyerite, $53.1 \%$; proustite, $65.45 \%$; pyrargyrite, $59 \cdot 78 \%$; besides occurring in the following: galena, zincblende, up to $0.88 \%$, iron and magnetic pyrites up to $0.09 \%$, fahlerz, copper pyrites, mispickel, bournonite, \&c.

Use.-Coinage, various ornaments and utensils, plating, photography, marking ink, alloys.

Market.-Sold as bar and fine silver. Standard silver is 11 oz. 2 dwts. fine, and 18 dwts. alloy; it is always alloyed with copper, as it is too soft to use by itself.

SodiUM.-Ores.-Soda, trona, common salt.
Use.-Employed in the manufacture of aluminium and magnesium, and amalgamation of gold and silver. Common salt is used for food, in roasting certain ores, \&c. Salts of sodium are used as chemicals.

Market.-Sold as metallic sodium, washing soda, bicarbonate of soda, caustic soda, salt (rock and table).

Strontium.-Ore.-Strontianite, celestine.
Use.-Manufacture of coloured lights, as nitrate; sugar refining.

Tellurium.-Ores.-Native, nagyagite, hessite, petzite, sylvanite, calaverite.

Use.-To alloy with copper.
Tin.-Ore.-Cassiterite, $78.67 \%$.
Use.-For coating thin sheets of iron, commonly known as tin-plates, manufactured into various utensils. Alloys (solder, pewter, gun-metal, britannia metal, bell-metal, type-metal, bronze, \&c.), tinfoil for protecting certain edibles, amalgamated with quicksilver employed in the construction of mirrors, dyeing and calico-printing.

Market.-Brands, English common blocks and ingots, English common bars, Australian and Straits, Banca Billiton. Tin-plates, charcoal I. C., coke I. C.

Impurities.-Chiefly antimony and iron.
Titanium.-Used in the manufacture of false teeth.
TUNGSTEN (WOLFRAM). - Ore. - Wolfram, scheelite, tungstite.

Use.-Tungstate of soda and tungstic acid are employed in dyeing and in the production of bronze powder. Used to give a greater hardness to some metals, e.g., tin and steel. Used as a substitute for tin in the manufacture of purple of cassius.

Uranium.-Ores.-Pitchblende, $84.91 \%$.
Use.-Urinate of soda gives a yellow colour for painting porcelain and colouring glass.

Vanadium.-Ores.-Vanadinite, dechanite, descloizite, purchesite, psittacinite, volborthite, roscœlite, mottramite.

Use.-Chemicals, photography, pigment (yellow), ink (blue black), indestructible by acids. For producing aniline black.

Market.-Ammonium vanadate, vanadium chloride, metavanadic acid.

Zinc.-Ores.-Calamine, $54 \cdot 17 \%$; Smithsonite, $52 \%$; Willemite, $58.56 \%$; zincblende, $67 \%$; zincbloom, $56 \%$; zincite, $80 \cdot 26 \%$; zine vitriol.

Use.-For coating sheet iron (galvanised iron) when it is used for building purposes and manufacturing into various articles, coating wire for fences, \&c., in electrical batteries, castings, dentistry, alloys, pigments (oxide and chromate), sulphate of zinc, as a mordant in dyeing, medicine.

Market.-Known as spelter, silesian (ordinary brand), and special brand, sheets.

Impurities chiefly cadmium.
Building and Decorative Stones.-Granites, porphyries, basalts, sandstones, slates, limestones, marbles, serpentine, breccias, puddingstone, alabaster, malachite, fluorspar, gypsum, rock crystal, agates, jasper, jade.

Ornamental and Precious Stones.-Diamond, sapphire (oriental ruby, oriental topaz, oriental amethyst, oriental
emerald), chrysoberyl (oriental chrysolite, alexandrite), spinel (pleonast, blas ruby), topaz, beryl (aquamarine, emerald), zircon (hyacinth, jargon), garnet (alamandine, carbuncle, cinnamon, pyrope), tourmaline (Brazilian emerald, rubellite, indicolite, achroite), quartz (rock crystal, amethyst, cairngorm, chrysoprase, cat's eye, plasma, jasper, bloodstone, carnelian, agate, onyx, sardonyx, mocha-stone), opal, turquoise, malachite, amber.

Grinding, Whetting, and Polishing Materials.-For sharpening tools and instruments; crushing and grinding various substances, food-stuff, chemicals, paper-pulp, clays, mortars, and cements; polishing and burnishing mineral and metals.

Millstones.-Grits, hard tough silicious sandstone, burrstone, quartzites, lavas.

Grindstones.-Sandstones and grits.
Polishing and Cutting.-Quartz sand, tripoli, rotten-stone, crocus, bath-brick, pumice, emery, diamond.

Whetstones and Hones.-Baths or sandstones, ragstones, hones or oilstones (metamorphic schists and slates).

Burnishers.-Agate, bloodstone, carnelian, jasper.
Refractory or Fire-resisting Substances.-Fire-clay, 'silicious sand, infusorial earth (tripolite), graphite, magnesite, limestone, potstone (steatite), sandstone, trap, asbestos, alum.

Clays we Fabricate.-Kaolin, pipe-clay, pottery-clay, brick- and tile-clay, fireclay, terra-cotta.

Glazes, Enamels, Colours.-Glazings for hard porcelain which are transparent are formed by admixtures of quartz, kaolin, lime, or gypsum and broken porcelain. Lead glazes are also transparent. Enamel, or opaque glazes, may be white or coloured; contain oxide of tin as well as oxide of lead. Colours made from oxide of iron (red, brown, violet, yellow, and sepia), oxide of manganese (violet, brown, and black), oxide of copper (green, red), oxide of chromium (green), oxide of cobalt (blue-black), oxide of iridium (black), oxide of uranium (orange and black), oxide of titanium (yellow), oxide of antimony (yellow), chromate of iron (brown), chromate of lead (yellow), chromate of barium (yellow), chloride of silver (red), chloride of gold (purple and rose-red), sulphide of mercury (vermilion), carbonate of lead (white), sulphate of barium (for adulterating white lead).

Mineral Mandres.-Carbonaceous (peat, coal slack, ashes, coke, soot) ; calcareous (marl, shell-sand, chalk, lime-
stone, gypsum, apatite, coprolites, guano) ; saline (sulphate of ammonia, carbonates of potash and soda, nitrate of potash and soda, sulphates of potash, soda, lime, and magnesia, chloride of soda, silicates of soda and potash, soda-alum, magnesia-alum, borax, chloride of calcium, bromide of sodium, borate of lime).

Food and Medicine.-Sodic chloride, lithia, lime, sulphate of magnesia.

Fossil Fuels. - Peat, lignite, brown coal, bituminous coals, anthracite, coke, petroleum, coal gas.

Light Producers.-Gas and naphtha springs, petroleum, pitch, asphalt, albertite, pyroschists, magnesium. Incandescent light use oxides of calcium, thorium, lanthanum, cerium, zirconium, yttrium, neodymium, erbium, præsodymium, tantalum. Monazite (thorium, lanthanum, cerium and didymium), orthite (cerium and didymium), zircon (zirconium), gadolinite (yttrium).

Miscellaneous.-Sand.-Used in glass making, for the preparations of mortars, concretes, and cements; as moulds for metals ; for cutting and polishing; to mix with clayey soil; ballast.

Sulphur.-In manufacture of sulphuric acid and other chemicals, medicine, plugging holes.

Graphite.-Manufacture of refractory articles (crucibles retorts, dippers, stirrers, bricks, stoppers, nozzles, \&c.), lubricating compounds, electrical supplies, stone polish, pencils, pigments.

Talc.-For dressing skins, leather, gloves ; as an adulterant, on account of its lightness; as a filler, chiefly in the manufacture of soap, paper, and rubber ; as a lubricant when mixed with other substances.

Soapstone.-Used for making ovens, lining lime-kilns, and hearths ; for sizing rolls in cotton factories, on account of it not being attacked by acids; slate-pencils; ornaments.

Mica.-Large white sheets for panelling stove doors, lamps, placed over gas globes, electrical insulating material. Smaller bits used for decorative purposes on wall-papers, steam and valve seats, lubricant, fertilizer.

Infusorial Earth. - In the manufacture of dynamite as an absorbent; polishing powder; as a protection to steam boilers and pipes ; moulds for casting medallions, \&c. ; manufacture of porcelain.

Barytes.-For adulterating white lead; for the surface finish of paper collars; in fireworks ; sugar refining; clarifying water for use in boilers.

Fuller's Earth.-For cleaning cloths.
Magnesite.-Fireproof furnace linings ; medicine.
Salt (sodic chloride).-Food; pickling; manure.
Saltpetre.-Preparing meat; chemical; manure; fireworks.
Diamonds.-Ornaments; cutting and grinding ; drilling.
Asphaltum.-For paving, flooring, roofing, varnish, water and acid proof paint; cement; foundations of buildings when mixed with sand or carbonate of lime; bed for machinery; pipes when covering cylinders of paper.

Gypsum.-Fertilizer ; stucco (plaster of Paris) casts, moulds, decorative purposes, surgery, dentistry, for adulterating flour, tamping blasts, cement when mixed with other substances, e.g., alum, borax, potash; used in converting carbonate of ammonia into sulphate of ammonia; mixed with colouring matter under the name of "terra alba."

## Ore Deposits.

Antimony.-In lodes with quartz and sometimes associated with heavy spar ; in Australia it is frequently auriferous.

Arsenic.-Found in metalliferous veins, especially those of silver, gold, and lead.

Bismuth.-Generally found accompanying cobalt, nickel, silver, lead or gold ores associated with quartz, molybdenum, mispickel, and cassiterite in lodes, pipe veins, \&c., in altered slates and granite.

Cadmium.-Found in zinc deposits.
Chromium.-Occurs as magmatic segregation in serpentine.
Cobalt.-Generally occurs in veins with nickel ores, also in wad which is found in veins, stockwork, and nodules.

Copper:-Copper lodes occur in rocks of all ages, including eruptive rocks (porphyry, melaphyre, diorite, gabbro, serpentine), crystalline schists and sedimentary strata up to Tertiary times. Copper ores are frequently associated with galena, zincblende, iron pyrites, quartz, fluorspar, calcspar, \&c. Copper pyrites and erubcscite, being sulphides of copper and iron, have an iron cap or gossan where the lode crops out at the surface caused by the oxidation of the iron; the copper generally being weathered out gives the gossan a boneycombed appearance. Copper ores may also occur in beds, e.g., copper slates, or native copper may be won from alluvial working.

Gold.-Gold reefs occur in shales, and sandstones of the Silurian and Devonian ages, also in various granites, porphyries, diorites, gneisses, and other metamorphic schists, serpentine, \&c.; associated with quartz, calcspar, barytes, oxides of iron, iron pyrites, mispickel, scorodite, magnetic pyrites, copper pyrites, zincblende, galena, stibnite, cinnabar, \&c. Gold may also
occur disseminated throughout a rock, also in stockworks. Loam gold is found in the soil from the decomposition of auriferous rocks and minerals. Alluvial gold is found in the beds of creeks and rivers, and on the sea-beach of the present day, also in alluvial deposits of the Miocene and Pliocene age (so-called deep leads) associated with shingle, sand, and clay, sometimes containing titaniferous iron, cassiterite, platınum, garnets, zircons, rutile, sapphires, diamonds, \&c.

Iridium.-In alluvial deposits associated with gold aud platinum.

Iron.-Occurs in lodes, beds, segregations, and impregnations of various ages, also in sheets from the decomposition of some basic igneous rock, e.g., basalt. Clay and black band are beds of iron ore found in carboniferous formation.

Lead.-These ores are found in lodes and irregular deposits in crystalline schists, shales, sandstones, and limestones, also in serpentine associated with copper and zinc ores, iron pyrites, barytes, quartz, fluorspar, calcite, \&c., and are almost always more or less argentiferous.

Manganese.-In veins in the earliest formations, also in irregular deposits in sedimentary rocks, limestone, porphyry, and granite. Frequently associated with iron ores in beds.

Mercury.-Cinnabar is found impregnating rocks, in stockworks and lodes, also in nests, in porphyry, melaphyre, bituminous shales, dolomitic sandstones, and limestones, from the upper silurian to the triassic age, also in schists and serpentine.

Molybdenum.-In quartz reefs with lead, tin, and bismuth ores.

Nickel.-Found in veins and impregnations in the older rocks, e.,.. granite, gneiss, serpentine, diorite, gabbro, talcose, hornblendic and other schists, associated with lead, copper, and cobalt ores, and magnetic pyrites.

Palladium.-In alluvial with gold, platinum, and iridium.
Platinum. -Only occurs in payable quantities in alluvial deposits generally associated with gold and iridium.

Silver.-In lodes and irregular deposits. Occurs in andesite, gneiss, and other crystalline schists, shales, sandstones, and limestones generally associated with lead, copper, zinc or antimony ores.

Sodium minerals occur in beds, also in the sea and lakes.
Strontium. - In veins generally associated with baryta and galena; also in the craters of extinct valcanoes.

Tellurium.-In reefs with gold and silver.
Tin.-Cassiterite is associated with granitic rocks, porphyries, gneiss, slate, or sandstone, where it is found to occur in lodes, stocks and stockworks, together with quartz, lithium mica, tourmaline, fluorspar, apatite, topaz, beryl, wolfram, molyb,
denite, mispickel, garnet, \&c. Tin-stone is also found in ancient and modern streams associated with gems, gold, \&c., when it is termed stream-tin.

Tungsten (Wolfram).-Wolfram occurs in lodes and in alluvial associated with tin-stone. Scheelite is found as irregular masses in quartz reefs.

Uranium.-This is found in veins with lead ores.
Zinc.-Zincblende, the chief ore of zinc, occurs in lodes of all ages associated with lead, copper, iron, tin, silver, and gold ores in slate, sandstone, limestone, granite and gneisses.

## Occurrence of other Valuable Minerals.

Alum.-Occurs in alum slates, also in small veins, and in some springs.

Amber.-In tertiary brown coal and diluvial deposits.
Apatite. -In archæan rocks.
Asbestos.-In serpentine rocks in veins.
Anthracite and Coals.-In seams or beds.
Asphaltum.-Lakes.
Alabaster.-In veins and beds.
Bitumen.-In layers.
Barytes.-In veins.
Basalt.-Sheets, dykes.
Borax.-In lakes.
Bituminous Shales.-In beds.
Burrstone.-A porous silicious rock from tertiary formation,
Brick-clays.-Decomposed rock near the surface.
Cerium. -In veins.
Dydmium.-In veins.
Emery.-Beds in mica-schist, and granular limestone.
Fuller's Earth. -In beds of jurassic and cretaceous formations, also the result of decomposition of diabase and gabbro.

Fire-clay.-From coal measures, also decomposed dykestone.
Guano.-On islands on the coast of rainless regions; caves.
Graphite (Plumbago).-Beds in crystalline schists and granular limestone.

Gypsum.-In heds and lodes.
Iodine.-Associated with Chili saltpetre in beds.
Infusorial Earth (Tripolite).-In beds.
Kaolin.-In veins and beds.
Lignite.-Beds.
Mica.-In pegmatite veins.
Meerschaum.-Loose or distributed in limestone and serpentine.

Nitre.-Beds in rainless tracts.
Petroleum.-Permeating shales, sandstones, and limestones of nearly all geological ages from the lower silurian.

Precious Stones.-Diamonds (detritus of crystalline metamorphic rock), sapphires (dykes of serpentine and chrysolite), spinel (granular limestone and serpentine, also in lodes), topaz (rhyolite, quartz porphyry), beryl (limestone, clay-slate), zircon (decomposition of felspathic rocks), garnet (rhyolite, peridot trap-dykes, chlorite, granite, crystalline schists, limestone, sandstone), tourmaline (granite, limestone), turquoise (small veins in clay-slate), opal (small veins in igneous rocks).

Talc.-In veins in schists, serpentine, and granite.

## ORE DRESSING. General.

Ore dressing is carried out by mechanical means ; smelting by chemical means. Must calculate which is the cheaper for any particular ore, taking local conditions into consideration. When calculating the cost of ore dressing, must take into consideration the cost of wages, stores, water, fuel, wear and tear, depreciation of plant, and the loss of ore in the waste. On the other side of the ledger place the saving by not having to handle flux and smelt, worthless material, depreciation of extra smelting plant, extra value of products, and if the tailings are used for filling underground credit must be given for this value. The increased value of the ore must at least fully cover the cost of dressing. The object of dressing is to separate the useful minerals from those that are worthless, and the former from one another for subsequent treatment. Associated minerals may be useful as fluxes, useless, or harmful. Ores may be too poor to smelt without previous concentration. Much dressing may be avoided by careful mining. The different sorts of minerals must first be set free from each other by reducing the ore in size, they can then be sorted, sized, classified, and concentrated. Results of ore dressing are generally given in percentages, but it would be better were the losses given in weight; for though a 75 per cent. saving might be good in a 3 per cent. copper ore, it would be bad work in a 10 per cent. ore.

The method of dressing employed depends on the nature of the valuable minerals to be saved, and that of the worthless material from which they must be separated. Ores that are easily converted into powder or are soluble in water are either difficult to treat or are not suitable for concentration, e.g. carbonates of copper or lead, and sulphate of copper. The latter would be lost in wet concentration, but may be precipitated out of solution as cement copper on scrap-iron.

Minerals that are hurtful often vary with the method
employed for extracting the metal. If silver is to be amalgamated, then lead and antimony ores, clay and talc, are injurious. For gold, when it is to be chlorinated, talc and lime are objectionable. In antimony ores, lead is not desired. Cobalt when used for a blue paint should be free from calcite, manganese spar, hornstone, ferruginous quartz and galena, also nickel when predominating; arsenic intensifies the blue colour. Lead and bismuth should be separated from copper ores. Over 10 per cent. zinc is objected to in lead smelting. Sulphur and phosphorus are hurtful in iron ores. The degree of concentration may depend on the process necessary to extract the metal ; for instance, tin smelters require 68-75 per cent. tin for treatment; wolfram buyers demand at least 60 per cent. W $\mathrm{O}_{3}$; the minimum for molybdenite is 90 per cent. Mo $S_{2}$. The percentage of metal required may depend on what is available. While users of chrome iron could handle lowergrade ore, they will not do so when there is plenty of 54 per cent. $\mathrm{Cr}_{2} \mathrm{O}_{3}$ available. Freight also affects the degree of concentration; in one place it may be necessary to dress an ore up to 30 per cent. Cu or higher, whereas under other conditions they might smelt 3 per cent. ore at a profit.

Some machines are made a standard size found by experience to be most suitable for general work, others have to be specially made. The capacity of a machine varies not only according to its size, but also according to the way in which it is run, and the nature of the material treated. The speed and quantity of water required must also be determined in each instance. Beware of freak machines, especially in out-of-theway places where alterations and repairs are not easily obtained. A machine should be simple, strong, as far as possible fireproof, and the same type of machine should be of the same make so that only one kind of spares will be necessary.

Avoid as much manipulation as possible. As a rule dressing floors are better located at the mine than at the smelters, so as to avoid the expense of handling worthless stuff that might be used at the mine for filling depleted stopes. It is generally cheaper to pump water to the mine than convey ore to the water. By erecting works on the side of a hill one gets the advantage of gravity in handling the stone. A good inclination for a dressing site is 1 to 3 , or 19 degrees. Must have a good tip for the tailings, and a suitable water-supply. Build the plant in units; leave ample space for handling machinery and adding possible improvements. Every machine has its economic limits. Proportion the capacity of the machines employed in successive stages.

The following properties of minerals affect ore dressing:-Hardness.-This affects the wear of machinery.
Tenacity and Brittleness.-A hard brittle mineral like proustite will slime more readily than one that is soft and tough like hornsilver. Tough minerals are difficult to break, e.g. native copper, mica, talc, rhodonite, and some forms of hornblende. Mica may choke up the screens of a battery and cause them to burst.

Form. - The shape of particles, governed by their structure and fracture. May be cubical like galena; elongated like antimonite; scaly like mica, etc. It affects their power of settling in water, and adhesion to surfaces with which they come in contact.

Mineral Aggregation.-Valuable minerals may occur in a massive form in large pieces mixed with waste rock from which it may be hand-picked; or it may occur in fine particles intimately associated with waste so that the whole must be crushed small. It may occur as laminations through waste; or as loose grains like gold, platinum, and tin stone in alluvial, which requires no reduction in size.

Colour and Lustre.-These are useful to enable one to readily recognize certain minerals when hand-picking.

Specific Gravity.-This is one of the most useful properties of minerals in connection with their concentration. See specific gravity in table of minerals. The economic effect of specific gravity is greatly reduced when a mineral is in a fine powder. Of two particles the same shape and size the heavier will settle first. Of two particles of different specific gravity but of same settling velocity, that of higher specific gravity will be the smaller. Of two particles of same shape and size, the heavier will have the longer trajectory, and of two particles of different. specific gravity but same trajectory, that of the higher specific gravity will be of smaller diameter than the other.

Adhesion.-Such as the attraction gold has for quicksilver, and diamonds have for a greasy surface.

Greasiness.-The tendency that certain minerals have to float on water as if they were greasy, owing to the difficulty of wetting the particles, e.g. zinc blende, copper pyrites, graphite, etc.

Magnetism.-The attraction of certain minerals to a magnet, e.g. magnetite, wolfram, and pyrrhotite. Useful for keeping bolts, nuts, and other pieces of iron or steel accidentally mixed with ore from getting into crushers.

Change of Magnetism by Heat.-Certain minerals, especially some of those containing iron, when heated lose $\mathrm{O}, \mathrm{CO}_{2}$, or S , and become magnetic.

Change of Porosity by Heat.-Iron pyrites when calcined loses its S , becomes porous, and lighter in specific gravity, so that it can be easily separated from other heavy minerals, e.g. cassiterite, not so affected.

Decrepitation.-Some minerals when heated fly to pieces on account of unequal expansion, e.g. calcite, fluorspar, and barite, which may then be separated by sizing.

## DESICCATION.

It is necessary that some ores be dried before they are treated, or else they might clog crushing machinery or otherwise interfere with the subsequent process to be adopted. It is not always desirable to dry fine concentrates for transport too thoroughly, as it becomes too dusty ; besides, a little moisture causes the material of the bags to swell, thus saving loss. With some material, e.g. pyrites, moisture may set up chemical decomposition that will rot the bags. Must consider the cost of drying, the degree of dryness desired, whether the mineral will be injured by passing through fire, and whether the ore is sandy or clayey. It is more difficult to dry down to $\frac{1}{2}$ per cent. than to 2 per cent., which is generally sufficient. If ore has to be transported, the saving in freight by getting rid of the bulk of the moisture is often an important item.

Weathering.-In dry climates a large amount of moisture may be got rid of by exposure to the weather.

Stalls or Kilns.-The ore is heated in enclosed places, often built in the side of a bank or hill, the ore being placed on layers of wood. Used for run-of-mine ore.

Rotary Drier.-A slowly revolving iron cylinder, placed at a slight angle, at one end of which is a fire-box. The ore, which must be fairly fine, is lifted up inside the cylinder by blades, and allowed to shower down through the heated air. The cylinder is about 24 ft . long, 6 ft . in diameter, given a pitch of 1 in 3 , and has 7 revolutions per minute.

Pans.-Iron plates or pans are placed over flues; mostly used for drying concentrates; or a special fire may be made under the pan, and an iron chimney pass up through it, against which the concentrates are directed by inverted cones.

Filters.-Filter presses and vacuum filters may be used to get rid of the excess of water.

Draining Belts. - Rubber belts revolving at an angle; generally serving as a conveyor at the same time.

## REDUCTION.

The object of reducing in size is either to make the ore more convenient to handle, or else to separate particles for
subsequent treatment. The finer the ore is reduced the greater the loss, and, as a rule, the more difficult it is to treat. Reduce in stages, never crush finer than that from which a payable quantity of ore can be concentrated. Use that method of reduction for which the ore in size and nature is most suitable, having regard to the product required.

A rough rule for power is $1 \mathrm{~h} . \mathrm{p}$., will reduce per twenty-four hours 24 tons to $2 \frac{1}{2} \mathrm{in}$. ring; 3.48 tons to $\frac{1}{16} \mathrm{in}$. mesh; 1 ton to 60 mesh.

Weathering or Heating.- Ore may be allowed to weather naturally, or a similar effect may be obtained more rapidly by heating in kilns if no objectionable chemical changes take place that will spoil subsequent treatment, e.g. the formation of sulphates when desired to amalgamate gold ores. Such treatment makes the ore break up easier. Can break up about 15 per cent. more stone after it has been burnt in kilns. Weathering does not require special apparatus, but causes loss of interest on the mined ore.

1. Crushing: (A) Jaw-breakers.-These have a knapping motion, which causes the ore to break along the lines of least resistance. They are used for reducing coarse ore, and do not make an undue proportion of very fine stuff. Jaw-breakers are measured by the length and breadth of the upper opening between the jaws. They have 150 to 200 strokes per minute. The ends of the toggle should be oiled every half-hour while the machine is in motion; all other working joints are lubricated every hour when the breaker is stopped. The ore is broken dry. Though jaw-breakers may break ore down to $\frac{5}{8} \mathrm{in}$. it is better to reduce ore to below 2 in . by some other means. Ore is not reduced in one operation from very coarse to fine, as the efficacy of an ore-breaker rapidly falls off when the reduction exceeds 1 to 4. The horse-power required varies according to the size of the machine and the work it does. A breaker that will crush 11-12 tons per h.p. per twenty-four hours to $1 \frac{1}{2}$ in., will crush $15 \frac{1}{2}-19$ tons to 2 in., and $18-22$ tons to $2 \frac{1}{2} \mathrm{in}$. The jaws of breakers as well as the shells of rolls are made of chilled white iron, manganese steel, or chrome steel. To avoid the breakage of some important part of the machine should a lump of iron find its way between the jaws, one of the toggles may be made of two pieces which overlap and are riveted together ; the copper rivets being the weakest portion are sheared if too great a strain is brought to bear on them. There are two great types of jaw-breakers, $(a)$ the Blake type, which has the movable jaw pivoted from above; this puts through a large quantity of ore, but the product is not regular in size ; (b) the Dodge type, which has its movable
jaw pivoted from below; this puts through less material but the grade of the product is more uniform.
(B) Gyratory Crushers.-With these crushing may take place the whole time, instead of intermittently as with a jawbreaker, if the hopper is kept full. Power required about $1 \mathrm{~h} . \mathrm{p}$., crushes 1 ton per hour to $2 \frac{1}{2} \mathrm{in}$.
(C) Rolls. - These crush ore by squeezing it between revolving cylinders placed horizontally and parallel, which revolve toward each other, so that they draw in and gradually crush up the material fed between them. In some places rolls are now employed to reduce ore formerly crushed by gravity stamps. If required to crush fine must do so in stages. Ore should be reduced to 2 inches before being fed into rolls. Rolls reach their limit at $\frac{1}{50}$ in., but in practice seldom reduce finer than $\frac{1}{20}$ in., as beyond this ball and tube mills are more efficient. May crush wet or dry, the former being used for fine crushing so as to lay the dust and keep the rolls cool. Since cylinders placed parallel and close together can only touch along a line, the grade to which the ore is crushed depends on the distance the rolls are apart at that line, and when once past that mark the ore is not further acted upon by the machine, therefore any coarse ore that finds its way through must be re-crushed. To avoid breakages to machinery when hard pieces get between the rolls, some device, e.g. rubber or steel springs, weighted levers, or breaking-cups, are employed. The faces of rolls vary between 12 and 24 inches; if too long, a large quantity of coarse material passes through should the rolls be forced apart by a hard piece. The diameter of the rolls is between 14 and 36 inches, the most useful size being 26 inches. If too small, the angle formed by the rolls is so obtuse that they cannot well grip the ore which slips, thus wearing down the shells by friction; if too large the rolls become unwieldy to handle. Fine crushing rolls have a greater peripheral speed than coarse rolls. The minimum peripheral speed for rolls is considered to be 200 feet per minute, and the maximum 1,500 feet per minute. If rolls are worked too fast power is lost; if too slow they are apt to stop should a hard piece get between them. Three sets of rolls $36 \times 16$ inches will treat 200-250 tons per twenty-four hours, according to the material, and size of finished product. Rolls receiving $1 \frac{1}{4} \mathrm{in}$. cube should be run with a peripheral speed of $300-400$ feet per minute; receiving $\frac{1}{4} \mathrm{in}$. feed, $550-600$ feet per minute; 14 mesh, 700-750 feet per minute; 20 mesh, for reduction to 40 mesh, 1,000 feet per minute. Over 1,000 feet per minute is not to be recommended. The surface of rolls is generally smooth but has been made corrugated; also one roll has been
given a concave face and the other a corresponding convex face. Ordinary rolls are apt to hollow out in the middle because most ore is fed to that part. Small rolls wear away quicker than large rolls, because the same point comes into action more frequently than with large rolls. The distance between rolls can be regulated by screws. The wearing part of rolls is borne by the shells which are slipped over cores. The shells can be re-turned when worn till reduced to $\frac{1}{4} \mathrm{in}$. thick. When both fine and coarse rolls are employed, generally use the same size for both, so that the shells when worn on the fine rolls can be transferred to the coarse rolls. It is well to have a spare core and shell ready to replace an old one, so as to save time in changing. The journal boxes of rolls should be long and self-oiling. With Cornish rolls the bearings of one are fixed, while the bearings of the other can slide horizontally for adjustment. The driving-roll may be geared to the follower with long-toothed spur wheels, so as to allow sufficient play when hard particles push the rolls apart; or the follower may be worked by friction only or assisted by a separate belt. Coarse Cornish rolls, $36 \times 16$ inches, set to crush to $\frac{1}{2}$ in., have a duty of $5 \frac{1}{2}$ tons per hour, and require $11 \mathrm{~h} . \mathrm{p}$. Krom rolls will crush from 12 to 50 tons a day.
2. Percussion.-This breaks up ore with a pounding action irrespective of its nature.
(A) By Hand. (a) Hammers.-Ragging, spalling, and cobbing are only different degrees of the same thing. Ragging hammers weigh from 10 to 16 lbs . and should have a handle in length from the palm of the operator's hand to his shoulder ; it must be of springy wood to prevent jarring of the hands. It must have two faces, or one face and a sharp pean ; the edges may be bevelled or sharp. Spalling hammers weigh from 2 to 3 lbs . and also have long handles; both faces are rounded. Cobbing hammers weigh from $1 \frac{1}{2}$ to 4 lbs. and have a handle the length of the forearm; they vary in shape according to the nature of the ore; generally they have one flat square face and a chisel-shaped pean, which latter may be either parallel with or at right angles to the handle, and is used for splitting purposes. Must use judgment in breaking stone, take advantage of joints, avoid striking the ore itself more than necessary as it is easily pulverized. Cobbing is done on a cast-iron die, 9 to 12 in . square and 4 to 6 in . thick, unless iron is objectionable, as with quicksilver ores, or in the subsequent treatment of tin or cobalt, when hard stone dies may be used. If ore is apt to fly, place a ring round it. Only rich ore is broken by hand; the poorer by machinery. The place where larger pieces of ore are broken up should
be well stamped or cemented to prevent the loss of fines, or their contamination with mud or dirt. When working with a long-handled hammer, it is better to employ two men, one to hammer, the other to sort the ore.
(b) Dollying.-With a pestle and mortar; the pestle is often attached to a spring pole. Used for breaking up samples, also for reducing rich hand-picked specimens of gold, tin, or wolframfor subsequent concentration.
(B) Tilt Hammer.-This is practically a large hammer with a horizontal stem worked by machinery.
(C) Gravity Stamp. - These are hammers, with vertical stems, which work in a mortar-box. The standard number in one box is five. To find the mechanical effective power of the stampers in a battery per second, multiply the weight of one stamp by the number of stamps in the battery, by the lift in feet, by the number of lifts per minute, and divide by 60 seconds. Allow one-third of the effective power for friction. Then the effective power plus one-third the effective power, equals foot-pounds per second, including the coefficient of friction. Foot-pounds per second divided by 550 give the horse-power required for the battery. The capacity of a stamp per twenty-four hours varies with its weight, class of ore, size of feed, and size of discharge. Formerly pieces as large as would pass the feed hole were put through; the larger pieces reduced the drop of the stamp and prevented the effective crushing of the smaller pieces, which in turn cushioned the blow on the larger pieces. Now, the feed is generally reduced to $1 \frac{1}{2}-2$ inches by ore-breakers. A stamp that will crush 3 tons a day to 40 mesh, will crush 10-12 tons a day to pass $\frac{1}{4} \mathrm{in}$. mesh, which shows that most of the time is occupied in crushing from $\frac{7}{4} \mathrm{in}$. to 40 mesh . To increase the capacity of gravity stamps, the tendency is to increase the size of the discharged material, which is then reduced by some more suitable machine, e.g. a tube mill or grinding pan; also to separate by screening material too fine for the stamps. Formerly the foundations for mortar-boxes were made of timber, now they are generally of concrete. When timber is employed there are generally two vertical mortar-blocks for each five-head mortar-box, let 6 to 10 feet deep into the ground. Where possible a solid rock bottom is levelled off, a squared $\log 18$ by 12 inches laid horizontally, on which are placed the mortar-blocks, connected together by $1 \frac{1}{4}$ inch rods and cross timbers, having 12 inch section. The space all round the mortar-blocks for 2 feet is well packed with concrete or clay and stone. Auger holes are made in the mortar-blocks for $1 \frac{1}{4}$ inch bolts by which the mortar-box is
fastened to the mortar-blocks, all other holes and cracks are filled with sulphur, the top is placed level and coated with tar, a triple layer of well-tarred blanket is placed on the top, and the mortar-box bolted in position. If solid rock is at the surface, a horizontal mortar-block is anchored to it by $1 \frac{1}{2}$ inch blocks 3 feet long. Sometimes good sound timber cannot be obtained; in such a case vertical mortar-blocks can be built up of 2 inch planks fastened together and placed on end.

Where the battery site is on marshy ground, one must use a horizontal foundation spread over a wide area; the ground is dug out for 1 to 3 feet deep, carefully levelled, and timbers laid.

Concrete foundations are wider at the base than on the top. The top is carefully levelled off with a stiff mixture of sand and cement $2: 1$. On this is placed a sheet $\frac{3}{8} \mathrm{in}$. rubber, then a piece of 6 inch thick wood, and finally the mortar-box. Holes are left in the concrete for the tie down bolts, and when they are in position they are held there by the space around the bolts being filled with sand, a little cement being placed on top to keep the sand in place; this enables a bolt to be readily withdrawn and replaced if necessary.

The framework may be of wood, steel, cast-iron, or wroughtiron, or a combination of them. Wood combines firmness with elasticity. Iron lasts longer, but the constant vibrations loosen the bolts. Frameworks are fastened to different timbers to those of the mortar-box, so as to make them less subject to vibrations.

There are two sets of guides for the stamp stems, one 3 feet above the top of the mortar-box, the other near the top of the stem; they may be of wood or iron, preferably the former ; when the latter, they are lined with hardwood or brass. The mortar-box is generally one heavy iron casting, unless it has to be transported over difficult country. When used for inside amalgamation, the boxes are made wide, otherwise narrow boxes give a better discharge. If hand-fed, the feed platform should be level with the feed hole, so that a man can shovel instead of having to lift the ore into the mortar. The width of the feed hole is about 3 inches so as to prevent a piece of ore entering that is too large to be economically crushed. The slit does not extend right across the box, as it is desired to feed the centre stamps. To avoid having to renew mortarboxes, 1 in. chilled cast-iron linings are used. Mortar-boxes generally have a front-discharge, but may have a back-discharge as well. The screens may be placed vertically or at an angle, the top leaning outwards. The height of the bottom of the screen from the top of the dies may be regulated, so as to get the most economic discharge as the dies wear down, either
by placing a false bottom under the worn dies so as to raise them, or, better still, by placing chuck blocks of different heights below the screen frame.

Screens may have clean or burred punched holes, which may be circular or slotted in shape, or they may be of wire cloth. The smallest practicable clean punched hole is 0.3 mm .; can punch thicker sheets for burred holes than for clean holes; if burred holes are too large they can be closed by hammering. Screens may be distinguished by the number of holes per linear inch or square inch, but one also wants to know the proportion of hole area to the rest of the sheet. Wire cloth has a larger discharge area than punched iron, but only lasts about half as long. If chips of wood, mica, and such-like substances are likely to get into the mortar-box and choke the screen holes, thereby endangering the screen, it is well to have a slit in the mortar-box near the top of the screen so that this material can splash or be scraped out. Two holes are left in the cover of the mortar-box for the entrance of water; the quantity of water used varies from 100 to 500 gallons per stamp head per hour. Sand requires about six times its weight of water to wash it over the plates.

Modern heavy stamps have bearings for the cam shaft between each stem, and a separate motor is used for every ten stamps, being placed between each set of five, so as to reduce the torsional strain of the cam shaft, which generally serves two batteries of five stamps each.

If a number of batteries are driven by one engine placed at the end of a long line of shafting, those sections of shafting nearest the engine must be made proportionally stronger. The belt-wheel on the cam-shaft is best built up of iron and wood, as this is subject to less vibration than one of iron, and is therefore less likely to work loose. The cams usually have two wings, the face of which is a modified involute of a circle, the radius of which is equal to the horizontal distance between the axis of the cam-shaft and the centre of the stamp-stem. May have key-ways cast in the same place in each cam, in which case the same cam can be used for any stamp, key-ways being cut in different positions on the cam-shafting ; or keyways may be cut in different positions in each cam according to the stamp it has to serve, and one key-way only is cut right along the cam-shaft. The Blanton cam can be readily adjusted in any position.

The stamp proper includes the stem, disc, head, and shoe, the combined weights of which vary from 600 to $1,000 \mathrm{lbs}$. in light stamps, up to $2,000 \mathrm{lbs}$. in heavy stamps, which appears to be the economic maximum for cam-lifted stamps. The very
light stamps are given a high drop, $16-20$ inches, in a roomy mortar with a high discharge, and have twenty-eight to thirty-two drops per minute. The heavy stamps are given a low drop of about 8 inches and fall about ninety-five times per minute. The best order of drop, facing the battery from the front, counting from left to right, is $1,4,2,5,3$.
The stem is solid wrought iron; both ends are generally tapered so that either can fit into the head. The stem may have a simple key-way cut on it, or be threaded where the disc is attached for about 2 feet long. If threaded, the threads should be rounded, not sharp, as they are stronger and easier to use.
The dise or tappet enables the lifting motion to be transmitted from the cam to the stem. It is made reversible so that when one face is worn, the other can be used; an annular groove is cut out near the stem, as that part is not worn by friction with the cam, so would leave a projection, which if everything was not in perfect order might cause the breakage of a cam. Discs may be keyed to the stem or fastened with a gib or wedge. When provided with a screw this is for nice adjustment. When out of commission, stamps are held up by fingers or stamp hangers placed under the dises. Oil is not suitable for lubricating tappets and cams, as it prevents the revolving of the stamp; it is better to use some tough grease, or a mixture of oil tar, resin, and tallow which turns thick on cooling.

The head is a cylindrical casting having the same diameter as the shoe; it is the connecting link between the stem and the shoe, and has a socket at either end for each, and channels for inserting an instrument to loosen the stem and shoe when desired to change either of them. The head also adds considerable weight to the stamp.
The shoe is cylindrical in shape, with a tapered shank that fits into the head; it is mostly made of cast steel or the hardest and toughest white iron. Strips of soft wood are tied round the shank, and the head carefully lowered on to it ; the stem is then dropped two or three times, and the connection is complete. The crushing is done between the shoes and dies; the former wear faster than the latter. The dies may be cylindrical with a square base, or may be octagonal. One has to see that there are no blow-holes in the castings, which are sometimes hidden by filling with lead.
(D) Steam Stamps.-These may be large single stamps, e.g. Ball, Leavitt, Allis, etc. They are lifted and forced down by steam, with a striking weight of $2,500-5,570$ lbs., having a capacity per h.p. per twenty-four hours of $1 \cdot 745-1.852$ tons ;
height of drop 4-6 inches, and 100 drops per minute; water required, $5 \frac{1}{2}$ tons per ton of ore crushed.

Tremain stamps consist of two steam stamps in a box; individually they are light weights, being only 300 lbs . each; they are given a drop of 5-8 inches and 140-200 drops each per minute.
3. Grinding Machinery.-With this class of machinery the ore receives a rubbing motion which tears the particles asunder. Used for reducing fine ore to sand and slime. Grinding machinery may be subdivided into:-
(A) Edge-Runners.-A cylinder will roll on a plane surface in a straight line without sliding friction; a cone also rolls on a plane surface without sliding friction, but in a circular path. Edge-running mill generally only have two runners, but may have three or four.

Chilian Mill.-This is a shallow cast-iron pan or annular ring in which short cylinders of comparatively large diameter work. The mills are measured by the diameter of pan, diameter of cylindrical rumners, and the width of their faces. The tires on the runners are of hard white iron 2 inches thick; the die or false bottom is 1 inch thick made in two sections of the best chilled iron. The pan has three holes at different levels for discharging the pulp. The feed is $\frac{\frac{1}{2}}{2}$ to $\frac{1}{4} \mathrm{in}$. in size. The runners revolve six to ten times per minute. The driving gear of the runners may be above or below the pan; or the bottom of the pan may be made to revolve which causes the runners to revolve by friction on their axle which is fixed. Chilian mills have not a positive discharge. They slime more than a ball mill. Modern fast running, 33 r.p.m., 6 feet mills, reduce about 4 tons per hour with a feed of $\frac{3}{8} \mathrm{in}$., and of the discharge 60 per cent. will pass 150 mesh.

Schranz Mill.-This consists of a pan which revolves $12 \frac{1}{2}$, times per minute; its bottom is cone-shaped, having an angle of 1 in 10 . This causes three conical runners, 18 inches at their smaller end and 28 inches in diameter at their larger end, to revolve by friction. Each runner is raised a different distance from the die so as to reduce the ore gradually. Rubber springs are so arranged against one end of each runner-axle that the runner can rise when passing over a hard bit of iron, etc. The machine requires $3-3 \frac{1}{2}$ h.p., and will break up 675 lbs. ore per hour, requiring 28 gallons of water per minute.

Bryan Roller Mill.-Consists of three steel-tired rollers 30 inches diameter, 6 in . face, each weighing $1,200 \mathrm{lbs}$.; tires $2 \frac{1}{2}$ inches thick, which last about 240 days. The die weighs $1,661 \mathrm{lbs}$. and lasts 120 days. The five screens weigh

19 lbs. and last four days. Total weight of mill $5 \frac{1}{2}$ tons. The belt-pulley is an iron tank so arranged above the rollers as to add weight to them. The mill revolves about forty times per minute, and requires $18 \mathrm{~h} . \mathrm{p}$.
(B) Centrifugal Roller Mill.- In which rollers are made to fly against the side of the pan by means of centrifugal force and crush the ore between them and the ring die.

Huntington Mill.-This consists of a cast-iron pan, in the centre of which is a spindle with a yoke, from which four arms are suspended, with a roller 13 inches diameter and $1 \frac{1}{2}$ inches thick at the bottom of each, so arranged that they are 1 inch above the bottom of the pan. The rollers are free to revolve on their axis, and are caused to do so by friction against the hardened ring-die inside the pan. The discharge screen is just above this die. The central spindle revolves $45-75$ times per minute. Ore is fed in the size of walnuts or a little smaller. The rollers are apt to wear irregularly, assuming polygonal shapes. Made in sizes $3 \frac{1}{2}$ feet, 5 feet, and 6 feet diameter. The usual size is 5 feet, which weighs $5 \frac{1}{2}$ tons, and requires a space of 6 ft .7 ins . by $4 \mathrm{ft} .8 \frac{3}{4} \mathrm{ins}$. It will crush 10-20 tons per twenty-four hours through a 30 -mesh screen and requires $10-12 \mathrm{~h} . \mathrm{p}$.

The Griffin Roller Mill consists of a single roller suspended on a single vertical axis, which flies out by means of centrifugal force against an annular die. The size of a mill is measured by the inside diameter of the die ring. A 30 in . mill weighs $10,500 \mathrm{lbs}$., requires $15-25 \mathrm{~h} . \mathrm{p}$. , and is fed with $1 \frac{1}{2} \mathrm{in}$. diameter ore. It may work wet with screens, or dry with fans. The roller revolves 190-200 times per minute on its own axis. The shell of a 30 in . mill is $18-20$ inches diameter, 6 inches deep, and weighs about 100 lbs . Under the roller are ploughs which are arranged to stir up the ore on the bottom.
(C) Mills with Drags.-Instead of revolving runners, drags are used which conform to the surface of the die.

Arastras.-Like a Chilean Mill, only the runners are replaced by two shoes or drags, which are pulled round the pan twentyfour times per minute.

Berdan Pan.-A cast-iron basin, with a curved bottom, 3 feet in diameter, arranged on a spindle placed at an angle of 25 degrees from the vertical. The basin revolves twenty-eight times per minute. A drag is hung up by a hook so as to be a little off the lowest point of the basin. Cap. 10 cwt. per twentyfour hours. The pan is $2 \frac{1}{4}$ inches thick and 15 inches deep. Iron balls are sometimes used instead of drags.
(D) Grinding Pans consist of a circular iron vessel, generally 5 to 8 feet diameter and $2 \frac{1}{2}$ to $3 \frac{1}{2}$ feet deep. On the bottom
are segmental dies, above which revolve shoes, also in segments, fastened to a muller or circular plate attached to a yoke. The muller and yoke can be raised or lowered by working a set screw that presses on top of the vertical shafting. Shoes and dies are 2 to 3 inches thick, they may have a plain or corrugated surface, be placed horizontally or at an angle, and the segments may be placed close together so as to form the so-called positive pan, where the material is forced to pass between the shoes and dies before it can escape at the periphery, or there may be a space between the segments. In the positive pans the ends of the shoes nearest the centre of the pan are made trumpet-shaped so as to allow the feed to enter between the shoes and dies. Iron wings are keyed to the inside of the pans so as to direct the pulp towards the centre. Pans may work on a charge intermittently or continuously; the latter may have a classifier in connection with it. A pan may also be used as a stirrer or agitator. Pans revolve about sixty times per minute, and are suitable for grinding from one-twentieth to one-sixtieth of an inch. Some people prefer pans to tube mills for the same class of work, but the wear is very great.
(E) Ball Mills. Loose balls are mixed up with ore in a cylinder.

Common Ball Mill.-A pan having an annular ring, round which large cast-iron balls are pushed by guiding-rods attached to a revolving cross-arm.

Krupp Ball Mill.-This is a revolving drum, made of hard steel segmental plates arranged in steps; outside these is a perforated sheet steel cylinder, and outside that a cylindrical sieve; the whole being housed in so as to be dust-tight. A number of chrome-steel balls of various sizes are fed inside with the ore. The machine is used chiefly for dry crushing. It requires very careful feeding, and is apt to be overfed and choked. Used for reducing a feed of $2 \frac{1}{2}$ inches to 25 or 27 mesh.

Tube Mills.-These will grind to any fineness required, depending on their length. The standard size for gold ores is $22 \times 5 \frac{1}{2}$ feet; use one to every ten head of stamps; allow $100 \mathrm{~h} . \mathrm{p}$. to drive it. Pulp of 50 per cent. and even 60 per cent. thickness has been found to give satisfactory results. When not required to slime make tubes shorter. Drive from dischargeend so as to have feed-end free. May line tubes with flints or steel or both. Steel linings $\frac{3}{4}$ to $1 \frac{1}{4}$ inches thick, last from five to ten months, depending on material crushed, and are worn down to $\frac{1}{4} \mathrm{in}$. thickness ; one set will grind 6,000 to 12,000 tons of quartz sand. Manganese steel linings are nearly double the cost of ordinary steel linings, but will serve for
about 18,000 tons. Use hard flints from 3 to 4 inches diameter for balls; 1 cwt. flints will slime about 100 tons quartz sand, or will grind about 150 tons to, say, 40 mesh . Rate of revolution about thirty-eight per minute.
(F) Cone Mills used mostly for reducing samples or coal. They consist of a cylindrical or funnel-shaped ring, which serves as a die, inside of which revolves a cone attached to a vertical spindle.
(G) Disc Mills.-Two or more discs rub up ore between them.

Dingey's Disc Mill.-This consists of a large borizontal dise, with 1 to 4 other dises rotating on it, those on the top working faster than those on the bottom.

Heberle's Disc Mill.-In this case the dises are placed vertically, and arranged eccentrically to one another; they revolve in opposite directions, and the space between them gradually diminishes towards the periphery. One disc rotates 250 times per minute, the other only 0.3 time. The machine is 9 ft .9 in . long, 3 ft . wide, 3 ft .3 in . high; it uses 5 gallons water per minute. Total weight 882 lbs .
4. Disintegrator.-Carr's disintegrator consists of two rings arranged vertically and parallel, each having two circles of steel-rod beaters, the circles on the same rings being 6 inches apart. The beaters attached to one ring work between those of the other in opposite directions and at different rates, which breaks up any soft material, e.g. coal that gets between the beaters. The diameters of the four circles of beaters are $48,42,36$, and 30 inches. One ring rotates at the rate of $300-400$ per minute, and the other at the rate of $450-600$ r.p.m. Coal should not be fed in larger than $\frac{3}{4} \mathrm{in}$. Requires 8-16 h.p.

## SEPARATION.

1. Washing or Cleaning Ore.-Some ores are associated with clay or earth which makes subsequent ore - dressing operations more difficult by clogging machinery, thickening the water, etc. In some cases it may be allowed to weather off, or it may be played upon by water from a hose ; at other times certain washing apparatus are employed.
(A) Stationary: (a) Sluices or troughs made in 12 ft . sections known as a box, $1 \frac{1}{2}$ to 2 feet wide and 1 foot deep; the material may be stirred about with hand tools, and the coarser pieces thrown out by a sluice fork.
(b) Step Sluices.-Every 4 feet or so a section is dropped a short distance from the one above, so as to give the ore a better chance of being cleaned by falling from step to step; the bottom of each division slants upwards from the back.
(B) Movable: (a) Log Washer.-This is a trough about 17 feet long placed at an angle of $\frac{3}{4} \mathrm{in}$. per foot, in which revolves an axle at the rate of 13 r.p.m., provided with blades set at an angle to the axis. The ore is fed at the lower end, and the water at the upper ; the blades slowly convey the ore uphill, and discharge it at the top, the clay floating out at the lower end.
(b) The Mud Wheel is a paddle wheel 5-6 feet diameter, which revolves in a curved box; the paddles lift the ore to be washed, and allow it to fall again.
(c) Puddler.-This is a vat in which vertical stirrers attached to revolving arms work up the stone and water together. A horse puddler is an annular ring, 6 feet wide and 20 inches deep, the outer diameter being 16 feet. A horse pulls round two sweeps to which are attached harrows which are circular or triangular iron frameworks from which vertical rods project and scrape on the bottom. There are gates through which the clayey water and the washed gravel can be discharged. Can treat 16-28 loads of gravel a day. A mechanical puddler is somewhat similar to a horse puddler, but uses mechanical means for motive-power. Can treat 120 cubic yards per twenty-four hours. Stir for 15-20 minutes, and then sluice.
(d) Wash Trommels.-A wash trommel may be cylindrical, in which case its axis is inclined about 1 in 12 ; or it may be conical when the axis is horizontal. They are 3-5 feet in diameter, $8-15$ feet long, and require $\frac{1}{2}-\frac{3}{4} \mathrm{~h} . \mathrm{p}$. to work them. They may revolve on shafting or friction rollers. They may be made of steel plate, sometimes with 4 in . spikes to break up clayey matter, or with ribs for lifting the ore, or may consist of bars of iron. Water may play on the dirty ore, or the drums may partly revolve in a trough of water. Lifting blades may be attached to an axle which rotates independently of the drum, which revolves on friction rollers. Work up $3-10$ cubic yards per hour. Use 12-25 gallons of water per minute. Speed at periphery 1 to $2 \frac{1}{2}$ feet per second.
2. Sorting.-Dressing by hand is more completely carried out with valuable ores than with those that are poorer, which are better treated in bulk by machinery. Ore may be sorted to a certain extent underground, where the mullock is used to support worked-out places, and the transport of worthless material to the surface is avoided. If the ore is very rich or very fine it may be bagged underground to avoid loss. At the surface the ore is sorted into " firsts" ready to be sent to have the metal extracted from it; "seconds" to be sent to the dressing floors for further treatment; " waste," including bits of iron and wood, to be thrown away. These three
divisions, which may be further subdivided, according to the nature and conditions of the minerals present, are carried through each department of the dressing floor. If the ore is associated with two or more sorts of gangues which greatly differ in specific gravity, e.g. baryta and slate, keep each class by itself as far as possible and treat separately. When handpicking, may use water to lay the dust and clean the ore, so that it can be more easily recognized by its colour as well as its structure, for sorting mostly depends on the eye; or by breaking a doubtful stone and exposing a fresh fracture the quality of the ore may be seen.
(a) Picking Belts may be of rubber or consist of linked sheetiron trays (steel rusts too easily), $2-3$ feet wide, with sides turned up for 2 inches, which travel about 35 feet per minute. Boys on either side may pick out the waste to enrich the balance if going direct to a furnace; or they may pick out the richer ore to save it from being crushed if desired to dress the balance; or each boy may pick out some particular class of ore as it passes by him, and the larger quality is allowed to fall over the end. The capacity depends on the size of the ore and the speed at which the belt moves.
(b) Revolving Table.-This is a circular table round which the pickers stand. The ore falls on to one part of the table, each boy selects his particular class, after which the residue is swept off.
(c) Fixed Sorting Tables are generally used when it is necessary to break up stones, mostly rich ore. Each sorter works at his own bench, in front of which is a bin from which he draws fresh ore when he requires it. The floor about a sorting table should be of cement or other hard substance that can be easily cleaned up.
(d) Heat. Asphalt may be separated from sand by heating them to $180^{\circ} \mathrm{F}$.

## SIZING.

Ore should be sized or classified before concentrating in order to get the best work from the concentrators. Sizing may be done wet or dry. The larger stones in run-of-mine may be roughly separated from the finer by tipping the lot over a wall, when the coarser lumps fall to the bottom where they can be collected. Ore is conveniently separated into the following sizes :-1st group, $2 \frac{2}{3}$ in., 2 in., $1 \frac{1}{3} \mathrm{in}$., 1 in ., which require No. 11-18 B.W.G. sheet iron ; 2nd group, $\frac{2}{3}$ in., $\frac{1}{2}$ in., $\frac{1}{3}$ in., $\frac{1}{4}$ in., requiring No. $12-14$ B.W.G. sheet iron; 3rd group, $\frac{1}{6}$ in., $\frac{1}{8}$ in., $\frac{1}{12}$ in., $\frac{1}{16}$ in., $\frac{1}{24}$ in., requiring No. $15-19$ B.W.G. sheet ; 4th group, that under $\frac{1}{2} \frac{1}{2}$ in., requiring No. 25 B.W.G.
sheet. Sheet iron is used for the coarser grains, but finer holes are apt to rust up, so may use punched copper instead, but this is more expensive. For the finest grain, iron or brass wire gauze is employed. Material which passes through a hole 0.01 in . diameter is too small to separate economically by means of sieves.

1. Stationary: (a) Grizzlies are made of bars of iron or wood; the section of the bars or rods may be circular, square, oblong, or trapezoidal with the broader end up, say, $\frac{3}{4} \mathrm{in}$. wide on top, $\frac{1}{2} \mathrm{in}$. wide on bottom, and $2 \frac{1}{2}$ inches deep. In the latter case the larger surface is exposed to wear, and the space between the bars being wider below large pieces of ore are less likely to become jambed. They are 8-12 feet long and generally bolted together to make a grating 4 feet wide with bars $1 \frac{1}{4}-2$ inches apart. Different ores slide at different angles, but for general purposes iron grizzlies are placed at an angle of 45 degrees, while wooden grizzlies are placed at an angle of 55 degrees. The grizzlies must have high sides to prevent the ore from jumping over. The bars are sometimes kept apart by small rollers, thus forming a large mesh, and preventing large, flat pieces from falling through. Grizzlies are used to relieve ore-breakers and stamps from having to deal with fine material.
(b) Screens.-These may be made of wooden or iron rods fixed in a frame which can be placed at any convenient angle, against which the material to be screened is thrown. Screens are sometimes made of punched sheet iron, the space between the holes generally being half the diameter of the hole.
2. Movable: (a) Hand Sieves are limited in their usefulness. If used for sizing tests or sampling purposes the sieve should have a cap, also an airtight tray below, in which the firie material collects without loss by dusting. Hand sieves for other purposes are generally run backwards and forwards on two strips of wood which support the weight.
(b) Mechanical Sieves.-These may receive a horizontal, vertical, or gyrating motion ; the first is less likely to choke up the holes than the second; a series of sieves should be independent of each other, so that their inclination and speed can be regulated to suit the material treated on each. The sieves are rectangular boxes bound round with iron, having wood or sheet iron at one end for the ore to fall on so as not to damage the perforated portion. They vary in length between 3 and 7 feet and their inclination between 1 and 5 inches per foot; the number of strokes they receive varies between 30 and 68 , and the quantity of water required is 20 to 100 gallons per minute. "The sieves receiving a horizontal motion may be classified according to the kind of motion imparted, as
percussion-riddles and swinging-riddles; likewise those with a vertical motion may be divided into jarring-riddles, springriddles, and rocking-riddles; these may be single or compound. The constant shaking causes much wear and tear.
(c) Grizzlies.-These are sometimes made so that alternate bars are moved slightly by means of an eccentric; this not only helps the ore forward, but prevents the spaces between the bars from becoming clogged. If grizzlies are fixed at such an angle that the ore runs down before the fine material has time to be separated, it may be retarded in its progress by a series of knives or short rods that project up between the bars in a line across the middle; these are counterbalanced, so that when the pressure of ore against the knives is too great they are depressed, and the ore passes onwards, but when relieved of the pressure the counterweight draws the knives up to their original position again.
(d) Trommels are cylindrical, prismatic, or conical in shape, and are made to revolve on an axle 8-30 times per minute, mostly 16-20; the shell may be of perforated iron or copper sheet, or wire gauze. A series of drums may be placed side by side or end to end ; in either case each drum is on a different level. They are usually $2-4$ feet in diameter, and must be long enough to give each particle a reasonable number of chances to get through, say, 9 feet long. The mantle may be perforated with holes of one size, or may be made up in sections of different sizes. The holes may be prevented from choking by jets of water playing on the mantle from the outside, or by blows from a hammer. The ore may be sized by first passing over the finest holes, or by commencing with the coarsest ; the wear is greatest in the former case. Drums may be made double by having a smaller one inside a larger. The angle of the cone or axle of the horizontal trommel varies from $\frac{1}{2}$ to 2 inches to the foot. Some trommels with a prismatic frame have the feed presented to the outside of the mantle instead of to the inside; the holes when fine may be kept free by jets of exhaust steam.
(e) Spiral Sieves are made up of sheets of iron, each section being punched with holes of a different size ; these are coiled up into a spiral, and from four to twenty-seven different sizes of material may be obtained, according to the number of sections employed; the whole revolves seven to nine times per minute.

## CLASSIFYING.

Classifiers are used for settling particles that are too fine for economical sizing. The horizontal current conveying the pulp
slows down as it opens out into boxes of successively larger areas. This allows the free settling of particles of similar weight but different sizes. Sometimes an upward current of fresh water is used to make a better classification. The sizes of grain fed into hydraulic classifiers vary from 5 mm . to 30 mesh. Some form of classifier or settling tank may also be used for dewatering purposes so as to thicken pulp or clarify water.

1. Settling Tank.-May consist either of a large box or an excavation in the ground lined with wood or cement. Owing to surface currents, and the fact that the coarsest particles fall as soon as the pulp reaches the settling tank, the deposit is not regular. The water may be pumped, syphoned, or more generally run off ; in the latter case there is usually a built-up wooden pipe at the far end. There may be a false bottom with a filter to allow the water to drain off. The tanks are of various sizes and may be emptied by hand or mechanical means, e.g. with an archimedian screw; in the former case, if the tanks are very large, rails are laid and trucks run in. In forming triangular slime basins a large rhomb-shaped excavation is dug out and divided into two triangles by a diagonal division or weir, a little lower than the top of the excavation; the pulp passes over a distributor at one corner of the first triangle, and spreads out fan-shaped, allowing the particles in suspension to gradually settle out. The water and finer slimes from the first triangle pass over the weir into a launder which convey them to the corner of a second triangle where the former process is repeated. Tailings may be settled from water so as to form a heap, the sides being built up with brushwood and tailings as the hollow gets silted up; when the heap rises too high for the pulp to flow on to it by gravity, the pulp has to be elevated by some form of pump.
2. Trough Classifiers: (a) Labyrinths.-These are launders which increase in width and decrease in depth with their length, and which wind about, constantly changing the direction of the current. The first lengths may be 9 inches in width, the following 12 inches, 15 inches, 18 inches, etc.
(b) Shallow Pocket Trough Classifiers are used for the coarser sands, e.g. those treated on fine jigs. They consist of troughs, in the bottom of which are occasional pockets where the horizontal current is momentarily retarded, giving the sand a chance to settle. A stream of fresh water is generally caused to rise from the bottom of each pocket.
3. Pointed Boxes.-Each box is a large wooden or sheetiron inverted pyramid. A baffle board is placed across the end where the pulp enters, so as to prevent surface currents.

The pulp is strained through a 20 mesh sieve before passing into the pointed box so as to strain off chips of wood, etc. The launder conveying pulp to the box should have 5 square inches cross-section for each cubic foot of pulp per minute, and its inclination should be for every 6 feet in length 1 to $1 \frac{1}{2}$ inches for coarse sand, $\frac{1}{2}-\frac{3}{4} \mathrm{in}$. for middle sand, $\frac{1}{4}-\frac{1}{2} \mathrm{in}$. for fine sand, and $\frac{1}{8}-\frac{1}{4} \mathrm{in}$. for slime. The inclination of the longer sides of the box is $50^{\circ}$. At the bottom of the box is a hole to which a $\mathbf{T}$ tube is attached; one opening is plugged when not required for cleaning-out purposes, the other has a tube connected with it which rises within 2-3 feet of the top of the box. It is through this latter tube that the pulp is forced by hydrostatic pressure. A rising column of fresh water enters the box near the bottom. In a series of boxes, that one made to catch the coarsest sand must have $\frac{1}{10}$ of a foot of material flowing through it per minute; each of the succeeding boxes is given twice the width of the preceding. A pointed box lasts six to eight years. Such a box without the upward current of fresh water may be used to thicken the pulp without any attempt at classification.
4. Tubular Hydraulic Classifier.-The Spitz-lutten consists of a box with a $V$-shaped cross-section the sides of which slope at an angle of $60^{\circ}$. Inside is a wedge-shaped displacer which can be moved up and down in order to vary the space between it and the box. The length of the tube between the box and the displacer along which the pulp flows, from the highest to lowest part, should be about 914 mm . for coarse material, the width may be 620 mm ., and the thickness will depend on the size grain it is desired to lift. The pulp Hows down one side and up the other, the coarser particles settle at the lowest point where it comes in contact with a sorting column of fresh water. Classifiers of this type are now made of sheet metal of a conical shape, this offering less disturbance from eddies.
5. Pneumatic Classifiers.-These depend on currents of air. Either the material is blown through chambers of increasing cubic contents, in which the dust settles, or else the material travelling on a belt is subjected to blasts of different velocities.

## CONCENTRATING.

Determine the most advantageous degree of concentration for commercial purposes; close concentration is difficult, and generally there is a larger proportional loss in the tailings, but if transportation costs are great it may be cheaper to lessen the bulk of concentrates and leave a higher percentage of values
than would otherwise be considered good work in the tailings. Concentration may be carried out by hydraulic, pneumatic, flotation, or magnetic means. The apparatus may be stationary, steady moving, vibrating, percassive, or oscillating. The chief principle used in concentration is the resistance due to friction of a grain sliding down an incline plane to the impulse of water on the surface of the grain; the larger the surface of a grain exposed the greater the hindrance. A 1 in . cube has an area of 6 square inches; if this is broken up into cubes $\frac{1}{10} \mathrm{in}$. in size, they would in the aggregate have an area of 600 square inches. When treating slime, the adhesion between the particles and the water impedes the action resulting from specific gravity. Important factors are the angle of the incline plane, the quantity of water and its rate of flow, also the size and specific gravity of grains.

1. Concentration by Flow of Water: (A) Apparatus on which the concentrates are allowed to collect and are cleaned off immediately.
(a) The Dish and Batea are used mostly for testing ore and cleaning up small quantities of rich material. The former is a flat-bottomed dish with bevelled sides, made of sheet iron, black for gold, tinned for tinstone ; while the batea is a shallow, cone-shaped dish made of wood. The Vanning Shovel has a shallow, basin-like blade, and is good for separating several varieties of fine material of different specific gravity.
(b) Round Buddles are used for fine sand and slime, which should be previously classified. They consist of a fixed basin lined with wood, cement, or asphalt, 10 to 30 feet in diameter ; they may have either a convex or concave bottom; the latter works quicker than the former, but occasions more loss, so should only be used for poor material or to get the bulk of the concentrates out of pulp. The inclination of the bottom is $\check{\mathscr{r}}-10$ degrees. A central shaft, from which four adjustable arms radiate, revolves ten to twelve times per minute. The arms have brushes or canvas sweeps attached, to level off any irregularities on the surface of the deposit. When concave bottoms are used, the launder conveying the pulp to the periphery also revolves with the arms. The machine requires $\frac{1}{20}$ to $\frac{1}{2} \mathrm{~h} . \mathrm{p}$. The length of the diameter of the table does not effect the cleanliness of the ore so much as guards against loss. As the material builds up, plugs are inserted in holes in the tailboard till 9-12 inches of material have collected on the table. The revolving of the arms is then stopped, and the concentrates classified into three lots by drawing concentric rings, and the different qualities of material dug out separately. If the sand builds up too fast at the upper end, it shows that
the pulp is too thick, or is fed in insufficient quantity. If it settles too thick below, it shows the pulp is too thin or that it is fed in too great a quantity.
(c) Sluices are long, wooden or iron launders with false bottoms or riffles of various design. They may consist of boards with holes about $1 \frac{1}{2} \mathrm{in}$. diameter, or blocks of wood with or without similar holes, venetian riffles of cast iron, or strips of wrought iron let into wooden sides made in convenient sections for handling, angle iron or old rails placed either length or crossways, expanded metal riffles, curly riffles, etc.
(d) Tye.-This is a wooden box 12-14 feet long, 22 inches deep, and 22 inches broad. The angles at which it is placed are $8,6,3 \frac{1}{2}$, and $2 \frac{1}{2}$ degrees, according to the size of the material to be treated. At the foot of the box is a tailboard with holes in it, which are plugged up as the settled material rises. The settled material is divided into three qualities, the lines between these being determined by panning off samples.
(e) End Percussion Table. - This is an oblong table $9-12$ feet long, 4-5 feet wide, with low sides and ends. The frame is suspended by four rods or chains. The whole table is pushed forward by a cam, and then falls back against a prell-block, thus causing the heavier particles to collect towards the back of the machine. As the concentrates collect upon the table, the tail-board is raised until the material nearly reaches the top of the sides, when it is classified into three portions and dug out. The richer portion must never be allowed to advance more than one-half to two-thirds the length of the table. A table 5 feet wide will take $0.5-0.7$ cubic feet pulp, containing $20-40 \mathrm{lbs}$. sand. The length of stroke is 4 to $\frac{1}{2}$ inches, the number of blows $12-80$ per minute, the inclination per 6 feet when treating sand is $5-8$ inches, when treating slime $2-3$ inches. Two men can attend to three machines. The surface of the concentrated material on the table should be free from furrows, and the pulp should flow over it in regular waves. The first third of the material on the table must show a distinct difference in colour to the other two-thirds, easily seen by stopping the pulp and allowing fresh water to flow over.
(f) Blanket Table.-This is a fixed inclined table of various lengths $20-30$ inches wide, given a fall of 1 in 10 to 1 in 6 ; the angle can be adjusted by wedges between the table and its support ; the table is covered with blankets so arranged that the bottom of the upper blanket overlaps the top of the next below it. When the blankets have accumulated sufficient concentrates, they are folded up and washed in tubs close
to the tables every two to four hours. The tables are often made double, so that one can be working while the other is being cleaned.
(g) Sweeping Table.-This is a table 12 feet long and 4 feet wide, given an angle of 10 to 12 degrees for coarse sand, and 5 to 6 degrees for fine sand. The former treats 0.3 to 0.5 cubic feet pulp per minute, the latter 0.08 to 0.12 cubic feet, and requires 0.6 and 0.15 cubic feet wash-water per minute respectively. The pulp is allowed to flow over the table for four minutes, and the wash-water for two minutes, after which the concentrates are swept down slits placed across the table when required to classify different materials, which were covered by flaps during concentration and washing. Capacity 4 to 30 cwt. material per twenty-four hours.
(h) Canvas Table.-Generally used as a save-all. They consist of a large area of wooden tables placed at an angle of 5 to 7 degrees, each about 20 inches wide and covered with 6 to 20 oz . cotton duck or cloth, which is shifted up periodically to prevent it getting worn at the joints of the planks. There are always one or two extra tables, so that the pulp can be turned on to them while others are being swept or hosed down.
(i) Keeve or Tossing Tub is used to enrich concentrates saved on buddles, mostly in the case of tin. The tub is 30 inches deep and 48 inches diameter on top, and 42 inches diameter on bottom, made of wooden staves 2 inches thick bound together with three iron hoops 2 inches wide and $\frac{1}{4} \mathrm{in}$. thick. Passing through the tub is a 3 in . spindle, on the top of which is a yoke carrying eight flat iron stirrers 2 inches wide. During the process of filling the tub, the stirrers rotate forty-eight times per minute; they are then withdrawn and two hammers commence to work against the side of the tub, delivering from 80 to 150 blows per minute. At the end of forty to fifty minutes the water is syphoned off, and the contents of the tub classified into tops, middles, and bottoms.
(j) Cradle or Rocker. - This is a box 40 inches long by 16 inches wide, being 12 inches high at the back, but tapering down to nothing at the front end. On the top of the back end is a sieve 20 inches long, 16 inches wide, and 4 inches high, perforated with $\frac{1}{2} \mathrm{in}$. holes. The material that passes through this is guided by a canvas apron to the back end of the bottom of the box. On the bottom of the cradle are two riffles about ${ }_{4}^{3} \mathrm{in}$. high, one placed across near the middle, the other near the lower end. The whole apparatus is fixed on two transverse rockers, so that it can be worked from side to side by means of a handle. A pin in the centre of each rocker serves as
a pivot to prevent the cradle from walking. The cradle is set at an angle. Gravel is shovelled into the hopper on the top, and the cradle rocked with one hand, while the operator pours water into the charge from a dipper with the other hand.
(B) Apparatus which are continuously cleaned up.-This class of concentrator being automatic and labour-saving is more generally in use than intermittent concentrators.
(a) Revolving Buddles.-As in the case of stationary round buddles, these may be either concave or convex ; frequently one is placed above the other on the same vertical shaft, so as to save floor-space. The table is made of wood, and is from 10 to 16 feet diameter, the slope being 6-9 degrees. The surface of the table may be in one plane, or may be stepped; the pulp may flow over the surface of the wood, or the wood may be coated with enamel paint or other substance. The table revolves once in 1-5 minutes. Round the centre of the convex table is a fixed launder ; 120-150 degrees of this is used to distribute the pulp on the revolving table; the remaining section of 240-210 degrees is used for the wash-water. Tailings flow down one-half of the table, middlings flow over the next third of the buddle area assisted by fresh water, and the headings are cleaned off by fixed brushes or jets of water, just before a revolution of the table is completed. Each product passes into its own division of an outside circular launder. There are 10 lbs . of sand or 5 lbs . solid slime in a cubic foot of pulp. A table requires 15 cubic feet water per minute when treating sand, and 8 cubic feet water when treating slime. When sand is treated, can put through $6-8$ tons in twenty-four hours, when treating slime $2 \cdot 8-3 \cdot 6$ tons. Concave buddles have the pulp fed over $\frac{1}{5}-\frac{1}{4}$ of its circumference.
(b) Side Percussion Table. -The bump is given at right angles to the flow of the water. The surface of the table may be plane or riffled, the latter being grooves or strips of wood. The Rittinger table is 8 feet long and 4 feet wide, suspended by four $\frac{1}{4} \mathrm{in}$. iron rods. The inclination of the table varies from 6 degrees for sand to 3 degrees for the finest slime. The pulp passes on to the table at one corner for a length of $8-12$ inches ; over the rest of the upper part of the table washwater flows down. Can treat $0 \cdot 2$ cubic feet sand pulp per minute or $0 \cdot 1$ cubic feet slime; the sand requires 0.20 cubic feet washwater, and the slime $0 \cdot 12$ cubic feet for every foot in width. The table is pushed to one side by a cam, and forced back by a spring against a bumping post. From 70 to 80 thrusts of $2 \frac{1}{2}$ inches per minute is given when treating sand, and $90-100$ thrusts of $\frac{3}{4}-1$ in. when treating slime. The bumping action causes the heavier particles to move across the table in jerks,
while the wash-water causes them to move down the table at the same time. Dividing fingers can guide the various products into their different boxes. The Luhrig table has a swinging frame the length of which is horizontal, while the width is given a slope depending on the material treated. This frame receives a shaking motion at right angles to the flow of the pulp from 150 to 210 strokes per minute of $\frac{1}{8}-1 \frac{1}{2} \mathrm{in}$. A travelling belt 19 feet long and 4 feet wide passes over the frame, being supported on corrugated iron to give it a level surface with little friction; it travels at the rate of 18-20 feet per minute. The feed passes on to the belt near one end, and wash-water over the rest of the upper side. The Wilfley table, which is 16 by 7 feet, is arranged somewhat similarly to the Luhrig, only the moving frame is covered with linoleum, it does not have any travelling belt passing over it, and the head and lower end have tapering riffles nailed to its surface to assist in concentrating and guiding the ore. Many shaking tables, instead of being suspended by rods or chains, are mounted on wooden toggle rods. As a rule it is well not to make the main adjustments of such machines too easy, otherwise the men in charge are apt to be constantly altering them for every little abnormal irregularity in feed, water, or power. By directing the feed uphill instead of down, the flow of pulp is momentarily retarded, which gives the heavier particles a better chance of clinging to the surface of the table. The stroke of the Wilfley should not be less than $\frac{5}{8} \mathrm{in}$. or more than 1 in. The speed should be 240 strokes per minute. Most of the ore treated on these machines is between 16 and 30 mesh. The capacity depends on the size of the material, generally about one ton an hour. The Card table has grooves instead of raised riffles, and is good for rough concentration of sands. The Buss table is something like the Luhrig vanner, consisting of an endless canvas belt which revolves round a swinging table inclined sideways, which receives four to six oscillations per second. The frame is mounted on vertical wooden springs which give the table an oscillating motion in an arc approximately cylindrical ; this prevents any packing of the material on the belt.
(c) End Shaking Tables.-These have a bump or shaking motion in the opposite direction to the flow of the water. The Gilpin County concentrator is a continuous-working bumping-table with cam, spring, and bumping-post. The bump sends the mineral back uphill, but the flow of washwater carries the lighter material down grade quicker than the jerk can send it up; the heavier material remains on the table till discharged over the top end. The table receives $120-180$
shocks per minute, the movement being $1 \frac{1}{2}$ to 3 inches. The maximum size grain fed is generally between 40 and 80 mesh. Unlike most concentrators, the pulp for these tables should not be classified, as fine material does not discharge well without coarser grains to drag it over. This table is generally mounted in pairs, each being about 7 feet long by 18 inches wide; the lower $5 \frac{1}{2}$ feet is a flat surface with a slope of about $\frac{8}{8} \mathrm{in}$. per foot, while the upper portion has a concave cylindrical surface to a height of about 2 inches above the flat surface.
(d) Vanners.-By a quick shaking motion the heavier minerals settle down on to a moving belt which then conveys it away to one end, while wash-water carries the lighter material away at the other end. These may have a side shake, e.g. the Frue Vanner, or end shake, e.g. the Triumph or Embrey Vanners. The Frue Vanner consists of an endless rubber belt, either plain or corrugated, with raised sides, which revolves over suitably arranged rollers; it is 4 feet wide and has a total length of $27 \frac{1}{2}$ feet. The upper portion of this belt is horizontal for its width, but has a grade of $\frac{1}{4}$ to $\frac{1}{2} \mathrm{in}$. per foot for its length, and travels at the rate of 2 to 7 feet per minute uphill and against the flow of water that carries the tailings over the foot of the machine. The heavier particles cling to the belt and are carried past the wash-water over the head roller into a tank of water, where they fall off. The vanner receives from 180 to 200 lateral thrusts per minute of 1 in . in length. Each machine requires about $\frac{1}{4}$ h.p. and has a capacity of $6-10$ tons per twenty-four hours. Use 1-3 gallons wash-water per minute. One man can look after sixteen machines. This class of table can only form two products, headings and tailings.
2. Pulsating Machinery.-Jigs. The German method is to size the ore before jigging; the English method is to jig coarse and fine together. The former is the better. When pieces of mineral of the same size but of different specific gravity are allowed to settle through some medium, the heaviest sink fastest ; if forced upwards, the lightest pieces will go highest. In jigging, the drop is not long enough for the ore to separate with one blow, so several short perpendicular blows or pulsations are given. The limits of size for jigging are $1 \frac{5}{8}$ to $\frac{1}{32}$ in. If coarse, too much power is required; if fine, the action due to its specific gravity is too much hindered by friction, and the material lies too close together. Jigs are divided into coarse and fine, according to the size of particles they deal with. Much material formerly used on fine jigs is now worked on tables as the latter use less water than jigs, and it is easier to see how work is proceeding. The shape of
the particles has a great influence on their treatment; they may be roundish, oblong, or tabular. These fall in water at the following proportional rates, 112, 97 , and 79 . Jigs may be worked intermittently or continuously; by hand or machinery. The sieve may move up and down in water, or water may be caused to pulsate through a stationary sieve. Hand jigs are of the movable sieve type, the sieve with the charge or ore being worked up and down in box of water by means of a lever. When the heavier and lighter materials have separated into layers, the latter is skimmed off by hand. A jig is the best form of coarse concentrator. It may be used to separate two or more kinds of products, generally " heads," " middlings," and "tailings," the first and last often being final products; hutch product is that which passes through the sieve into the hutch. The ordinary Hartz jig is a box 3 ft .6 in . deep, the length depending on the number of compartments required; this is divided lengthways by a board 18 inches deep to separate the plungers from the sieves. The sieve compartment is about 2 ft .4 in . by 1 ft .6 in .; the first sieve is 8 inches below the top of the box; the difference in height between each succeeding sieve is 2 to 3 inches. Coarse jigs work material down to 4 mm ., while fine jigs work that between 4 mm . and 2 mm . The length of stroke must be sufficient to lift the grains the height of their diameter, and the time between each stroke must be sufficient to allow the grains to settle. The stroke for coarse jigs is $\frac{1}{2}$ to 3 inches, and for fine jigs $\frac{3}{4}$ to $\frac{1}{2} \mathrm{in}$. The number of strokes for coarse jigs is about 100 per minute, and for fine jigs $120-150$. The stroke may be communicated by an eccentric, or a pulsating mechanism may be arranged so as to give a quick down stroke and a slow up stroke. The total depth.of the ore being worked is $3 \frac{1}{2}$ to 4 inches, the depth of the coarse concentrate is about 2 inches. Coarse jigs make their own bedding. For fine jigs the bedding should be of about the same specific gravity as the ore; if too heavy it requires too much power to lift it, and causes boiling of the top layer ; if too light it lets tailings through to the hutch. A grating divided into coarse cells is placed above the sieve so as to keep the ragging from working down lengthways. For coal jigs use felspar as bedding. Must not have the ragging too large ; it is preferable to use coarse pieces of the ore being treated. Ore with a large percentage of concentrates requires a thin bottom bed, for the reverse a thick bed; the thicker the bed the cleaner the hutch work. May use iron punchings or shot as bedding. Fine jigs have 12-14 mesh sieves. Coarse jigs have special outlets for the concentrates, either a slit in the side of the sieve compartment, protected by a slide which regulates the
discharge, or else a tube passing through the sieve, protected by a cylinder which does not quite reach the bottom of the sieve; this serves to keep back the upper layer, while the lower layer of concentrates can pass up from below. The capacity of jigs varies very considerably, but is largely governed by the sieve area, more especially by the width, the limit being from about 0.15 ton per square foot of sieve per twenty-four hours to 9.6 tons, but averaging 0.5 to 2.0 tons. Hard banks form from the suction, and boils are due to vents from the upward current. The horse-power varies according to the number of sieves; it is well to provide $1 \frac{1}{2}$ h.p. for one sieve; $2 \mathrm{~h} . \mathrm{p}$. for a two sieve; $2 \frac{1}{2} \mathrm{~h} . \mathrm{p}$. for a three sieve; and $3 \mathrm{~h} . \mathrm{p}$. for a four sieve jig. Coarse jigs require more water than fine jigs, but average about 34,000 gallons per twenty-four hours for a three sieve jig. The Handcock jig is an example of a mechanically worked jig with movable sieve. The Willoughby is a kind of finishing jig used in New South Wales for cleaning tin from heavy sands, and fetching it up to 75 per cent. metallic tin. It consists of a pressure box 5 feet high, and the width of the sieve box 2 feet square by 18 inches deep, with which it is connected near the bottom, below the sieve, by a short wooden pipe. The sieve consists of a copper plate with $\frac{1}{32} \mathrm{in}$. perforations. About 4 cwt . of ore is put into this box, making a layer about 6 inches deep. The valve between it and the pressure box is suddenly opened, causing the lighter impurities to ascend to the top where they are scraped off. The operation is repeated about five times, the water being let out of the concentrating box through a valve at the bottom.
3. Pneumatic Concentration.-Air as a medium for concentration is chiefly used (a) as a continuous blast which grades the particles subjected to it ; (b) as intermittent pulsations. In both cases the ore should be dry. The former principle may be used to separate coal dust from slate with which it is mixed; if the mixture is blown up an inclined plane, the floor of which is composed of overlapping boards like a venetian blind, the coal will be kept in suspension by the air current, while the slate in its passage will sooner or later present its edge to the blast, fall down, and escape between the boards. The latter consists of some form of pneumatic jig, or dry blower, used in districts where water is scarce. They are used for concentrating alluvial gold, tin, precious stones, dollied wolfram, horn silver, and other substances that will not stand the expense. Dry blowers on alluvial fields are generally mounted on wheelbarrows so that they can be readily moved from one place to another. They consist of an inclined coarse screen resting on thin legs, into
which the ore is fed so as to separate the large pebbles; this is caused to shake by means of a rod or cam connected to the handle that works the bellows. The fine material that passes through the coarse screen falls into a steeply inclined perforated plate, forming the top of the wind chest of the bellows. Riffles are placed horizontally across this to catch the heavier particles; the blast of air blows the lighter particles away. The capacity of these machines is about four to five loads a day under normal conditions.
4. Flotation.-The first attempt at flotation by Everson was to make use of the selective action of oily substances in bulk to float up certain minerals by means of the inferior specific gravity of the oil. This has given way to the use of much smaller quantities of oil with which the powdered mineral is agitated, with or without the addition of acid. The acid may have the effect of cleaning sulphides so that they can be more readily oiled, or it mayset free $\mathrm{C}_{2}$, which, clinging to the particles, helps to buoy them up. Various patents have been taken out claiming certain actions, dependent on the employment of different mediums and reagents in varying quantities. It is doubtful if any of the flotation processes work to advantage on their original claims. The cause of the flotation may be due to (a) the buoyancy of a large quantity of thick oily substances, $(b)$ bubbles of air or gas caused by agitation or chemical means which carry up certain particles, (c) emulsification entangling certain particles. Most of the flotation processes are not suitable for slimes, but the float of the Mineral Separation process matts together better with a certain percentage of slime, and will even work on slime alone. For this process, the ore is reduced to pass through a 40 mesh screen, it is then agitated with 24 in . diameter propeller-like stirrers, which revolve 250-300 times per minute, with three to five times its weight of water, to which is added, for Broken Hill zinc-lead ore, about 15-20 lbs. sulphuric acid per ton ore, and the liquid is passed on to another agitator where 1 lb . oleic acid per ton of ore is added. From this the mixture passes into a separating wedge-shaped box, where the liquid being comparatively quiet, allows the float to rise to the surface and pass away down a launder. The liquid is sucked through from the bottom into another agitator, and the agitation and separation repeated about five times altogether. For copper ores there is no occasion to use sulphuric acid, and about $\frac{1}{2} \mathrm{lb}$. eucalyptus oil is used per ton of ore instead of oleic acid.
5. Magnetic Concentration. - When substances are attracted by magnets, they are said to be paramagnetic; they
are few in number, and vary considerably in their power of attraction. Those substances which are not attracted by a magnet are said to be diamagnetic. The minerals mostly attracted by magnets are those containing iron, e.g. magnetite, pyrrhotite, wolfram, zinc blende (black jack), etc. If, say, wolfram and bismuth have been concentrated together, and it is desired to separate them by an electro-magnet, the wolfram product will not be clean, as being in a concentrated form it entangles some bismuth mechanically when attracted by the magnet. The practical use of magnetic concentration is at present confined to the concentration of iron ores. Magnetic separators may be classed into those $(a)$ where a cylinder revolves round a series of fixed electro-magnets wound in such a manner that opposite poles are adjacent to one another: these are so placed as to attract those minerals affected by magnets when touching a certain portion of the cylinder. As the ore is fed on to the top of the cylinder, the magnetic particles cling to the cylinder, while the non-magnetic particles fall into a receptacle prepared for them; as soon as the magnetic particles pass beyond the field of the magnets, they are flung off by centrifugal force. The capacity of a Monarch Magnetic Separator with two drums, 2 feet diameter and 2 feet face, varies from 15 to 20 tons crude ore per hour which has passed through a 16-20 mesh sieve. For the best work the feed should not be over 1 mm . in size and perfectly dry. The power required is $1-1 \frac{1}{2} \mathrm{~h} . \mathrm{p}$. for the magnets of each drum, and $\frac{1}{2}-\frac{3}{4} \mathrm{~h} . \mathrm{p}$. for revolving the drums. The first drum makes forty revolutions per minute and uses a current of $10 \frac{1}{2} \mathrm{amp}$., uses a current of 13 amp . The Wenstrom Magnetic Separator while the second drum makes fifty revolutions per minute and consists of a revolving drum made up of alternate magnetic and non-magnetic bars parallel to the axis; within this cylinder, and placed eccentrically to it, is a fixed electromagnet. This machine is specially suitable for treating coarse stuff which need not be dry. A 5 ton per hour machine requires $1 \frac{1}{2} \mathrm{~h} . \mathrm{p}$. to furnish the current and $\frac{1}{2} \mathrm{~h} . \mathrm{p}$. to revolve the drum. (b) Magnetic separators with conveying belts. The idea is to have a conveyor belt to bring the ore under the influence of powerful magnets; another belt travels between the magnets and the ore on the conveyor belt, the magnetic ore clings to this as it passes under the magnets, and is thus carried to its proper receptacle. The Wetherill Magnetic Separator is one of this type; it has a very strong magnetic field and can be used for weakly magnetic material. (c) A single electro-magnet is sometimes suspended above the belt conveying ore to a breaker, in order to extract nails,
hammer-heads, and other pieces of foreign iron and steel that may have accidentally fallen among the ore.

## SUNDRY APPLIANCES.

A. Tipplers: (a) End Tipplers, or kick ups, used when the empty truck is withdrawn the same way as the full truck is introduced.
(b) Side Tipplers, may be used for box trucks; the empty truck is pushed out at the far end by the incoming full truck; the side tippler is balanced so that it revolves automatically, the motion being regulated by a brake. Tipplers may be fixed over the place where the ore is tipped, or may be made to travel on rails. If the material to be tipped is soft and must not be broken up, e.g. coal, it may be discharged against a hinged iron sheet down which it slides. Sometimes a threetruck side tippler is used which revolves slowly the whole time so that trucks can be run in, out, and emptied at the same time.
B. Elevators and Conveyors: (a) Cage or Platform Elevators.-Worked by compressed air, steam, water, electricity, or friction. Mostly used for raising ore in trucks.
(b) Inclined Plane. -Trucks of ore are often drawn up an inclined plane to the necessary height by a rope, a movable trigger being placed between the rails to open the gate of the truck where desired to discharge it.
(c) Creeper Chain.-This is a strong long-link endless chain, in which at regular intervals a link has a vertical projection or horn sufficiently long to engage the axle of a truck. Trucks are pushed to the foot of an incline where the creeper chain takes them in charge and delivers them to a flat or oppositely inclined place higher up.
(d) Raff Wheel.-Somewhat like a water-wheel with the buckets inside instead of out. Its diameter depends on the height it is required to raise the material, which is tipped out at $\frac{8}{10}$ ths, the inner diameter of the wheel. The breadth is seldom more than 1 foot; the angle of the buckets is $40-50$ degrees for dry material, and 30 degrees for pulp. The speed at the periphery is 1 to 4 feet per minute.
(e) Bucket Elevators.-These consist of buckets attached to chains or belts which revolve, taking the buckets with them, the latter being filled in the boot or pit and emptying themselves at a higher level, depending on the length of chains or belt. Should provide drain holes in the boot. If the elevator is housed-in to prevent splashing or dust, have panels that can be removed so that one can get to any part of the elevator.
(f) Endless Belt Conveyor.-A rubber three-ply belt resting on bottom and side friction rollers which give it the shape of a trough. May be used to convey ore or products of dressing from one part of a shed to another, or to stack tailings, when the belt may be placed, if required, at an angle of 22 degrees from the horizontal; when required to discharge material from different parts of a belt, may employ a travelling unloader. Speed 300 to 900 feet per minute. While conveying ore on a belt the opportunity is often taken to hand-pick the ore; or if conveying a wet product, the belt may be used for draining purposes.
(g) Flight Conveyor.-This is an endless belt made up of a series of iron plates, the ends of which are turned up and form the sides of the conveyor.
(h) Scraper Conveyors.-Scrapers attached to an endless belt pass along a trough into which the material is tipped and dragged along.
(i) Push Conveyor.-Generally used for hot material. It consists of a rod to which rectangular pieces of plate iron are attached which remain vertical when moving forward, but can work on a hinge when moving backwards.
(j) Screw Conveyor.-This is a large screw cased round, which screws up fine material from settling-pits. The angle of its axis is 30 degrees; the width of the thread 6 inches, the peripheral speed 3 feet.
(k) Hydraulic Elevator.-This is a large iron pipe on a stand placed in a pit where the material to be elevated collects; a jet connected with a smaller pipe containing water under sufficient pressure is placed in the bottom of the larger pipe; the force of water issuing from the jet draws up the material in the pit and delivers it higher up.
(l) Sand Pump.-This is similar to a Cornish plunger pump, only provision is made to force in a small quantity of clean water so as to prevent the sand from entering the gland.
( $m$ ) Centrifugal Pumps.-These in one form or another are sometimes used to elevate tailings; they wear out very rapidly and require frequent renewals.
( $n$ ) Chinamen. -These are covered in wooden chutes built at various angles, used to guide ore in its descent.
(o) Sluices.-Wooden or iron launders in which material is conveyed by water. The former may be lined with cement to make them last longer. Launders are best made of rectangular cross-section, twice as wide as deep.
C. Agitators.-The object of agitation is generally to keep fine particles in suspension; this is generally done by stirrers arranged vertically or horizontally that are made to rotate in
a vessel ; or air, steam, or water under pressure is caused to pass into the pulp from below, thus keeping it in motion.
D. Feeders.-Apparatus for automatically supplying material to various machines for treatment. When properly set they ensure a regular feed and reduce labour.
(a) Shaking Feeder. -This has a reciprocating motion similar to shovelling by hand, e.g. Stanford's; suitable for fairly coarse stone.
(b) Roller Feeder.-A cylinder arranged at the bottom of a hopper revolves slowly, drawing out the stone above it, e.g. Tullock's.
(c) Disc Feeder.-A rotating disc arranged below the hopper containing the ore placed at an angle, e.g. Hendy's challenge ore feeder.
(d) Water Feeder. - Used for fine materal. Water cuts a channel through sand contained in a box, fresh sand falls into the space to replace that washed out.
E. Distributors.-Used for dividing pulp into proper proportions for different machines, or for spreading it evenly at the head of a machine.
(a) Nicking Board.-A fan-shaped shallow trough over the surface of which diamond-shaped buttons are fastened in regular order by a screw through the centre; these buttons may be turned in different directions so as to make the flow at the lower and broader side even. Sometimes the diamonds are replaced by longer strips or fingers.
(b) Pipe Distributor.-When required to distribute pulp to various machines from one centre or to spread it evenly over a circular vat, may feed it into an annular trough from which pipes radiate. Butter's distributor used for filling vats has pipes of different lengths arranged so as to balance each other ; the outflow ends are bent in such a manner that as the pulp escapes the distributor is caused to revolve.
F. Filters, either pressure or vacuum, may be used to clarify solutions or for leaching purposes.
(a) The ordinary filter press of the Dehne's type consists of a series of frames into which the pulp is forced from montejus by compressed air. The filling takes about eighteen minutes, the washing twenty minutes, while discharging, cleaning, and closing require thirty-seven minutes. The thickness of cake formed depends on the build of the press, from $1 \frac{1}{2}$ to 3 inches. The pressure used in filling is 60 lbs . per square inch, and in washing 80 lbs . The pulp consists of one part by weight of water to one part of solid. On account of the time and labour required to discharge these presses they have largely given place to Merrill's or some form of vacuum filter.
(b) Merrill's filter press is also of the flush-plate and distanceframe pattern, but is larger than the ordinary type, containing ninety-two frames. The pulp is charged under pressure of about 30 lbs ., and consists of three parts of water to one of solid. The cyanide treatment is carried out in the press itself. The cake formed in the frame is 2 to 4 inches thick. When leached and washed, it is sluiced out without opening the press. In addition to the ordinary channels for introducing pulp and solutions, at the bottom of the frame is a continuous chamber, within which lies a sluicing pipe with a nozzle projecting into each compartment. This nozzle can be revolved through an arc of any magnitude so as to wash the cake down to the channel. It takes four tons of water to sluice one ton of slime. Requires one-tenth horse-power per ton of slime treated.
(c) Moore's vacuum filter consists of vertical frames forming a "basket" suspended in a tank containing the pulp, which has been previously agitated with cyanide solution. Each frame is connected with the vacuum pump which sucks through the solution, at the same time building up a cake of slime about 0.75 to 1.75 inches thick. The basket is then hoisted up by an overhead crane, and lowered into a wash tank, where the cakes are washed by the vacuum pump sucking through water; the basket is again raised and traversed to the tip, where compressed air is forced into each frame, which causes the cake to fall off. The whole operation occupies seventy-five minutes. Butter's filter remains stationary in the same tank all the time, the contents of the tank being changed for each stage in the process. The pulp has a specific gravity of 1.3 to $1 \% 4$, and the thickness of the cake is the same as in Moore's. The amount of wash-water left in the cake varies from 20 to 30 per cent.
(d) The Ridgway continuous type of vacuum filter consists of a series of cast-iron filtering frames, the form of a sector of a circle 12 feet in diameter. The under surface is corrugated and has a screen attached ; to this a filter-cloth is fixed. The frame is suspended horizontally and makes one revolution a minute. The underside of the filter frame dips into an annular trough divided into three compartments, one for the pulp, the next for wash-water, and the last is the discharge chamber. Each sector has three pipes provided with valves which work automatically; one carries away the solution, the second wash-water, while the third has compressed air blown through it to discharge the cake of slime, which is 0.125 to 0.375 in. thick. The cake takes thirteen seconds to build up, thirty seconds to wash, and seventeen seconds passing between the divisions and being discharged. The machine requires $5 \mathrm{~h} . \mathrm{p}$. Each frame has 4 square feet filtering area, and each machine treats 50 tons per twenty-four hours of clean quartz

## MECHANICAL DRAWING.

Hints.-When choosing instruments look well to workman. ship. With bad instruments no good work can be done.

Bowpens should be broad, thick, and strong, and not much bowed-the points should be rounded off.

Needle-pointed instruments are much to be preferred.
Never draw more pencil lines than necessary.
Accuracy is all important, small errors are multiplied in long construction.

Always ink-in circles and curves before straight lines.
When many concentric circles are required, use a horn centre, to avoid making a big hole in the paper and consequent false lines.

Never leave a pen with ink between the nibs to dry.
Use bread in preference to indiarubber, especially when cleaning the whole surface of a drawing.

Shade lines are drawn outside the outline of the object, and dimensions are measured from inside the shade line.

When shading or shade lines are employed, the light is supposed to come over the left shoulder.

Shade lines should never be drawn to indicate the outline or contour of a curved surface.

Colours.-Illuminated plane surfaces parallel to the plane of projection receive flat tints. .The nearer the surface is to the eye the lighter such tints should be.

Illuminated plane surfaces inclined to the plane of projection receive graduated tints, becoming darker as such surfaces recede from the eye.

Unilluminated plane surfaces parallel to the plane of projection receive flat tints. The nearer the surface is to the eyc the darker such tints should be.

Unilluminated plane surfaces inclined to the plane of projection receive graduated tints becoming lighter as the surface recedes from the eye.

Shading in colour is done in strips, softening the edges each time, beginning always with the darkest portions of the object, and washing over and beyond the previously coloured portion each time.

The following colours are in general use to represent the more common materials :-

1. Cast Iron.-Payne's Grey or mixture of in ligo, sepia, and lake.
2. Wrought Iron.-Prussian blue.
3. Steel.-Prussian blue and crimson lake.
4. Brass. $-\left\{\begin{array}{l}\text { Elevarion . . Gamboge. } \\ \text { Section }\end{array}\right.$
5. Copper--Gamboge and crimson lake.
6. Ordinary building.-Sepia and yellow ochre.
7. Brick (common). - $\begin{aligned} & \text { Elevation . . } \text { Light red. } \\ & \text { Section }\end{aligned}$
8. Brick (fire). $-\left\{\begin{array}{l}\text { Elevation . Light red and yellow ochre. } \\ \text { Section }\end{array}\right.$ Section . . Ditto with crimson lake.
9. Wood.- $\left\{\begin{array}{l}\text { Elevation ... Yellow ochre. } \\ \text { Section }\end{array}\right.$. Burnt sienna.
10. Earth.-Burnt umber.

Lines. - $\left\{\begin{array}{l}\text { Red } \\ \text { Blue }\end{array}\right.$ : $\begin{array}{l}\text { Carmine. } \\ \text { French ultramarine. }\end{array}$
Cast shadows are seldom used, but if desired they should be washed in neutral tint or Indian ink before colouring.

In Mine plans the spaces left by the removed ore masses are coloured purple for tin; green for copper ; blue for lead. The adit level is coloured blue and the levels below it red, green, yellow, violet, and brown in succession.

Survey Scales.-The scales usually employed for the plans of metalliferous mines are 4 or 8 fathoms to the inch, sometimes 5 or 10 fathoms. For colliery plans scales of 2 or 3 chains to the inch, or of 25.34 inches to the mile, are the most usual. In the construction of maps of the Ordnance Survey of Great Britain, the following scales are used :-

| Towns | $1: 500$ | or $126 \cdot 72$ | inches to the mile. |  |
| :--- | :--- | :--- | :--- | :--- | :---: |
| Parishes | $1: 2500$ | $25 \cdot 34$ | $"$ | $"$ |
| Counties | $1: 10560$ | i | $"$, | $"$ |
| The Kingdom | $1: 63360$ | 1 | $"$ | $"$ |



To divide a given line a $b$ into two equal parts.-From its ends $a$ and $b$ as centres, and with any radius greater than half $a b$, describe the arcs $c$ and $d$, cutting each other at $c$ and $f$; join $c$ and $f$; $a b$ is bisected at $k$.

If $a b$ is very long first lay off equal distances $a 0, b g$ from $a$ and $b$, and then proceed as if $o g$ were the line to be divided.

To divide a given line into any number of equal parts. -Let $m n$ be the given line, from $m$ draw $m o$ of indefinite length, and from $m$ along $m o$ step off the required number of equal parts, say 6 , join $n 6$ and
 draw lines parallel to $n 6$ through $5,4,3,2,1$, and cutting $m n$, when $m n$ will be divided into six equal parts.

To divide a given line into two parts which shall have a given proportion to one another. -This is done on the same principle as the last: thus let the proportion be as 1 to 2. First draw any line $m o$ (last fig.) and with any convenient opening of the dividers make $m x$ equal to one step; and $x z$ equal to two steps. Join $z n$ and draw $x y$ parallel to $z n$. Then $m y$ is to $y n$ as 1 is to 2 .

To draw an ellipse.-An ellipse may be quickly and fairly accurately drawn thus:-Given the major and minor axes A B, C D. With C and D as centres and radius equal to A F (semimajor axis) drawing arcs cutting A B in E and G. Stick in two ordinary pins, through the paper and into the drawing

board, at E and G and tie to them a piece of silk or thread of such a length that it equals $\mathbf{E ~ C + C G}$. If the point of a pencil be carried round in this loop so the thread will take up such positions as E $a$ G, E $a^{\prime}$ G, E $a^{\prime \prime}$ G. \&c., and the pencil point will trace an ellipse having the major and minor axes A B and C D.

Copying drawings.-To trace on to ordinary drawing paper, stretch the paper over the drawing and saturate it with benzine by means of a cotton pad; this makes it transparent so that the drawing below may be traced. Pencil, Indian ink, and water colours, take equally well on the benzinized surface.

When the copy is completed the benzine rapidly evaporates and leaves the paper in its original condition. Large drawings only have benzine applied to a portion at a time.
Blue prints or cyanotypes: giving white lines on blue ground :-

Sir John Herschel's. 140 grs. ferric ammonic citrate. 120 grs. potassic ferri-cyanide. 2 oz . distilled water.

Marion's.
$9 \frac{3}{8} \mathrm{oz}$. ferric ammonic citrate. $6 \frac{1}{4} \mathrm{oz}$. potassic ferric oxide.
Dissolve separately in pure water, and make up to 1 quart.

Willis's platinntype process, giving white lines on black ground :-
Sensitising solution. 60 grs. potassic-platinous chloride. 60 grs. ferric oxalate. 1 oz . water.
Expose until the paper acquires a dull orange tint.
Developing solution. 130 grs. potassic oxalate.

## 1 oz . water.

Develop for 4 seconds at temp. of $150^{\circ}-200^{\circ} \mathrm{F}$., then wash for 10 minutes in 1 pt. hydrochloric acid with 60 pts. water, and finally for 15 minutes in relays of fresh water.

## PHOTOGRAPHY.

By S. J. Becher.

Hints.-When choosing a camera study good workmanship, good material, compactness, and lightness combined with rigidity; so-called cheap sets are not to be recommended. Never expose double backs or film carriers to more direct sunlight or heat than can be helped; they are easily warped or cracked, and the plates or films within them consequently fogged.

For landscape and general outdoor-work, a single meniscus lens gives brilliant pictures. For architectural or structural work, a doublet or triplet is necessary, to avoid distortion of marginal lines.

For a complete outfit for outdoor-work it is well to have:-
(1.) An ordinary wide angle single landscape lens.
(2.) A narrow angle single landscape lens (for distant views).
(3.) A rapid rectilinear doublet lens.

If only one can be provided, No. (3) should be given the preference.

Always clean a lens carefully with silk, and not coarse material, before making an exposure. Avoid dust inside camera. The smaller the stop used the longer the exposure may be, and the better the marginal definition will be. For interiors use very small stop, and give very long exposure.

Do not use a lens which will more than cover the plate, lest rays be reflected from the sides of the bellows on to the plate.

It is better to over expose than under expose. Over exposure can be compensated by slow and careful development ; an under exposed plate can never produce good prints. A good rule for exposure, "Expose for the shadows, and the lights will take care of themselves."

Never have harsh contrasts of bright light and deep shade.
Having found a brand of plates or films that give satisfaction, always work with them, so that knowing their capabilities and peculiarities, you can by comparison with notes of former exposures, light, stop, \&c., be more certain of your results. Always note details of exposure, plate, stop, light, time, subject, and when complete, results. These references are invaluable. It is generally advisable to use the Developer recommended by the manufacturers of the brand of plate used, but a good all round set for Pyro development are the following 3 solutions :-


These are practically 10 per cent. solutions, and are used in the usual way. A correctly exposed plate will require about 20 minims of each solution to each ounce respectively of water. B. \& C. being added according to requirement.


Always wash well between each operation, and after fixing wash for 12 hours.
"Frilling" is when the gelatine leaves the glass plate during development or subsequent operations, and occurs more especially in hot climates. It is sometimes due to bad manufacture. The best preventive is the unfailing use of the alum bath both before and after fixing.
"Fogging."-Chiefly caused by unintentional admission of light to the plate, either through cracks or holes in the doublebacks, film-holders, camera, or dark room. Also by sudden addition of excess of ammonia during deve'opment.
"Flatness of Image," usually due to over exposure and development with alkaline developer.

Yellow stain or veil may be removed by the clearing bath.
Too great density is also reduced by clearing bath.
Want of density may be caused by excessive over exposure, or poorness of quality of the plate.

Thin transparent negatives are due to excessive under exposure.
"Pinholes," are due to dust on the surface of the plate. Always dust the plate with a soft flat brush before changing, and again before development.

Brown stains on the fingers after pyro-development may be removed with dilute Hydrochloric Acid.

Dishes used for negatives should never be used for prints, and special disbes should be used for each operation and for no other purpose. Cleanliness is all important.

Printing.-The fresher the paper the better. Preserve it irom all access of light and damp. Do not finger it more than is necessary. If possible, trim prints before washing and toning, as they lie flatter, and much toning bath and space therein is saved.

When using ready sensitized paper (silver) always print considerably darker than the resulting shade desired. A good negative will require to be printed from till the whites just commence to color and the shadows to bronze.

The sooner toned, \&c., the better, but a few days' keeping will not ruin the prints. Variety of shade from brown to purple is regulated in the toning bath. Tone slightly darker than the resulting tone desired, as both colour and shade are reduced in the fixing bath. Wash well between all operations.

Take great care that the fixing bath is not acid, the addition of a few drops of ammonia is a good preventive.

Wash for 12 hours at least after fixing.

Formula for good Toning Baths.


No. (1) must be mixed the day before it is used, but will keep indefinitely, and may be used repeatedly, more stock gold solution and soda being added occasionally.

No. (2) must be used the same day it is made, and will not keep.

> Fixing Bath.
Sodium Hyposulphite . . . . . 4 oz.
Water . . 1 pint.

This can be used several times, as long as it is not acid.
A test for presence of hypo in last washing water in order to ascertain whether extraction is complete.
Potassium permanganate
Potassium carbonate . . . . . . . . . .
Water
20 grs.
1 quart.

Add a few drops of this rose-coloured solution to sample of water. If any trace of hypo is present, the colour will be of a greenish hue.

Dishes for toning and fixing should be labelled and used for no other purpose. Porcelain dishes are the best.

A good mounting solution.


When this mountant is used the prints need not be damped as when using starch, paste, \&c. Thus the mounts, or leaves of books, are not cockled up or bent.

A simple method of burnishing unmounted silver prints is to lay them when wet, after the final washing, face downwards on a sheet of highly polished vulcanite; smooth out any bubbles and the surplus water. As they dry they peel off of their own accord, and retain the burnished surface which the albumen in contact with the vulcanite has taken. This shows up detail.in the shadows. With other papers such as platino-
type, bromide, \&c., follow the instructions given by the makers. Matt surface papers are more artistic than shiny ones.

Platinotype, \&c., have the immense advantage of being permanent, and are especially valuable in hot, damp, climates.

When rolling silver prints for storage put them face outwards.

If prints look chalky and cold, they may be dyed in a very weak solution of a pink or rose dye with advantage.

Measliness or yellow dirty prints are due to bad paper, acidity of fixing bath, or want of cleanliness in manipulation.

If prints soon fade and turn yellow, it shows that the extraction of hypo has not been complete, i.e., insufficient washing.

## TOXICOLOGY.

| Poison. | Antidote and Remedies. |
| :---: | :---: |
| Acid, acetic | Chalk, whiting, magnesia, soap or oil. Alkaline bicarbonates, white of egg, or almost any demulcent. |
| Acid, hydrocyanic | Drink at once one teaspoonful of am- |
| or prussic acid ; | monic hydrate (spirits of hartshorn) |
| bitter almonds | in one pint of water. Inhale odour |
| (oil of laurel | of ammonia. Chlorine either taken |
| water | in vapour or internally. Cold infusions, artificial respiration, stimulating injections. Sulphate of iron. |
| Acid hydrochloric | Neutralise the acid by chalk or calcined |
| (muriatic or marine acid). | magnesia, or a dilute solution of an alkaline carbonate, milk, white of egg, strong soapsuds and lime. Large draughts of tepid water or mucilage should follow antidote. |
| Acid, sulphuric (oil of vitriol). | Same as hydrochloric acid. |
| Acid, oxalic. | Powdered chalk ; magnesia, or its carbonate, suspended in water or milk. An emetic, if free vomiting is not induced by the above means. |
| Acid, phosphoric. | Magnesia, emetics, and emollient drink. |
| Acid, nitric, or aquafortis. | Same as hydrochloric acid. |


| Poison. | Antidote and Remedies. |
| :---: | :---: |
| Alcohol. | The stomach pump. Cold affusions, ammonic hydrate (spirits of hartshorn). |
| Chloroform and ether. | Cold affusions on the head and neck, ammonia to the nostrils, artificial respiration, electricity, opening the trachea. |
| Ammonic hydrate (Ammonia or spirits of hartshorn), potash or soda. | Weak acids as vinegar and water, fol- |
|  | lowed by acidulated demulcent drinks: |
|  | lemon juice, olive oil in large quantities, large draughts of cream or milk. |
|  | Use no emetic. In poisoning by the vapour of ammonia the inhalation of the vapour of acetic acid or of dilute HCl. |
| Iodine and iodide of potassium (potassic iodide). | Take a mustard emetic. Drink a mixture of starch, gruel, or arrowroot beaten up in water. |
| Toadstools (nonedible mushrooms). | Prof. Maurice Schiff of Florence has demonstrated, that the non-edible mushrooms contain a common poison, muscarin, and that its effects are counteracted by atropin or daturine. |
| Arsenic, cobalt (fly powder), king's yellow, ratsbane, Scheele's green. | An emetic, stomach-pump, zincic sul- |
|  | phate, cupric sulphate ; or mustard |
|  | may be used as an emetic, or salt and |
|  | by tickling the throat with a feather. The vomiting should be assisted by demulcent drinks. After free vomiting give large quantities of calcined magnesia. The antidote for arsenic is hydrated sesquioxide of iron freshly precipitated. If the poison has passed into the bowels, castor oil. |
| Antimony (wine of), tartaremetic. | Vomiting should be produced by tepid water; any astringent infusion, such as tea, oak, bark, tannin (ground nutgall) ; afterward opiates (paregoric), warm bath and mustard poultices. |

Poison.
Baryta salts, copper, verdigris, blue vitriol.

Iron.
Lead, acetate of lead (sugar of lead), white lead, litharge.

Iodine.

Mercury, corrosive sublimate (bugpowder), white precipitate, red precipitate (vermilion).

Nitrate of potash (saltpetre), nitrate of soda (Chili saltpetre).

Pearl-ash ley (from woodashes),salts of tartar.

Phosphorus matches, rat exterminator.

Carbonic acid gas (charcoal fumes), chlorine gas, nitrous oxide gas, or ordinary gas, burning fluid.

Antidote and Remedies.
Stomach-pump, or emetics, magnesia sulphate of soda. Demulcent fluids to induce vomiting, stomach-pump, albumen in large excesses, milk, cooking soda, iron filings, manna, preparations of sulphur.
Sodic carbonate ; mucilaginous drinks.
Emetic-mustard. Follow with zincic sulphate (Epsom or Glauber salts). Antidote is weak sulphuric acid. Take large draughts of milk, containing white of eggs.
Starch or wheat flour beaten up in water. taken in large quantities. Take a mustard emetic ; tepid baths.
Beat the white of six eggs (albumen) in one quart of cold water ; give a cupful every two minutes. Induce vomiting. A substitute for eggs is soapsuds slightly thickened with wheat flour. The white of one egg neutralises four grains of the poison. Emetics should not be given.
Take at once a mustard emetic ; drink copious draughts of warm water, followed with oil or cream.

Drink freely of vinegar and water ; followed with a mucilage, as flax-seed tea.

Give two tablespoonfuls of calcined magnesia, followed by mucilaginous drinks.

Fresh air, and artificial respiration; may inhale ammonia, ether, or the vapour of warm water.

| Poison. | Antidote and Remedies. |
| :---: | :---: |
| Aconite or aconitin (Monkshood). | Thorough evacuation of the stomach, either by an emetic (mustard) or the stomach-pump; ammonia and brandy, and the use of stimulating injections; free use of finely powdered animal charcoal; vegetable infusion containing tartaric acid, tincture of nux vomica, iodine and potassic iodide. Keep patient active. Emetics-mustard, zinc sulphate, or ipecacuanha wine, vegetable acids, (vinegar, acid fruits). |
| $\begin{aligned} & \text { Atropin, bella- } \\ & \text { donna (deadly } \\ & \text { nightshade). } \end{aligned}$ | An emetic and use of stomach pump, as with aconite. Morphine administered by the mouth or subcutaneous injection. Drink black coffee. |
| Daturine. | Same as above. |
| Hellebore (Hellebore niger). | Emesis and subsequent stimulation. Opium has been used. |
| Nicotin. | Same as above. |
| Opium. | Any portion of the unabsorbed poison should be removed quickly from the stomach. Use the stomach pump or an emetic of gr. xx or gr . xxx zincic sulphate, or about gr. x cupric sulphate, or powdered mustard or salt. Keep patient in motion. Apply cold water to head and chest. Belladonna is recommended as an antidote. |
| Strychnine, nux vomica. | An emetic, or use of the stomach pump ; internal use of chloroform by inhalation, tannic acid, 25 parts of tannin to 1 of strychnine ; solution of potassic iodide, iodine, chlorine, camphor, animal charcoal, lard or fat, nicotin. |

As a rule for vegetable poisons give an emetic of mustard, drink freely of warm water, irritate the throat to induce vomiting. Keep the patient awake until a physician arrives.

## Receipts for Solders．

| Metal． | E | \％ | 込 | E E E E | 嶌 | 㟧 | － |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| For lead | 1 | $\ldots$ | $\ldots$ | $\ldots$ | $1 \frac{1}{2}$ | $\ldots$ | $\ldots$ |  |
| ，tin | 1 | $\ldots$ | $\ldots$ | $\ldots$ | 2 | $\ldots$ | $\ldots$ | ．．． |
| ＂，pewter ．${ }^{\text {a }}$ | 2 | $\cdots$ | $\cdots$ | $\ldots$ | 1 | ．．． | ．．． | $\cdots$ |
| ＂，brazing（hardest） | ．． | 3 | 1 | $\ldots$ | ．．． | ．．． | $\ldots$ | $\ldots$ |
| ＂，＂，（hard）． | $\cdots$ | 1 | 1 | $\ldots$ | $\cdots$ | ．．． | $\ldots$ | ．．． |
| ，＂＂，（soft）． | 1 | 4 | 3 | 1 | $\ldots$ | $\ldots$ | $\ldots$ |  |
| ＂$"$＂or | 2 | ¢ | 1 | 1 | $\cdots$ | $\cdots$ | $\cdots$ | $\ldots$ |
| ＂iron | $\cdots$ | 2 | 1 | $\cdots$ | $\ldots$ | 19 | $\ldots$ |  |
| ＂，steel | $\ldots$ | 3 | 1 | $\ldots$ | $\ldots$ | 19 | $\ldots$ |  |
| ＂，silver（hard） | $\ldots$ | 1 | $\ldots$ | $\ldots$ | $\ldots$ | 4 | $\ldots$ | ， |
| ＂${ }^{\prime}$（soft） | $\ldots$ | － | $\cdots$ | $\ldots$ | $\ldots$ | 2 | 21 | 1 |
| ，gold |  | 1 |  | $\ldots$ |  | 2 | 24 |  |

Fluxes for Soldering or Welding．

| Metal． | Flux． |
| :---: | :---: |
| Iron or steel． | Borax and sal－ammoniac． |
| Tinned iron ．． | Resin or chloride of zinc． |
| Copper and brass ． | Sal－ammoniac or chloride of zinc． |
| Zinc | Chloride of zinc． |
| Lead | Tallow or resin． |
| Lead and tin pipes | Resin and sweet oil． |

## GLOSSARY OF TERMS

UNED IN PROSPECTING, MINING, METALLURGY, ETC.
Abbreviations. $-($ Chem. $)=$ Chemistry. $(\mathrm{Mec})=$. Mechanics. (Met.) $=$ Metallurgy. (Eng.) $=$ Engineering. (Min.) $=$ Mining. (Geo.) $=$ Geology. (As.) $=$ Assaying. (Phy.) $=$ Physics. (Sur.) = Surveying.

Acid (Chem.). A compound containing one or more atoms of hydrogen, which become displaced by a metal when the latter is presented in the form of a hydrate.
Adit (Adit level). (Min.) An underground level which comes to the surface, generally used for drainage purposes.
Afterdamp (Min.). The deadly gases resulting from an explosion of fire-damp, composed chiefly of carbonic anhydride.
Air compartment (Min.). An air-tight portion of any shaft, winze, rise, or level, used for improving ventilation.
Air course (Min.). Any underground roadway for the special purpose of ventilation.
Air crossing (Min.). A bridge that conveys one air course over another.
Air cushion (Phy.). A spring caused by confined air.
Air door (Min.). A door for the regulation of currents of air through the workings of a mine.
Air hole (Min.). A hole drilled in advance, to improve ventilation by communication with other workings on the surface.
Air oven (As.). A heated chamber for drying samples of ore, \&c.
Air shaft (Min.). A shaft sunk for ventilation purposes, e.g., at the end of a long tunnel.
Air sollar (Min.). An air-tight wooden flooring in a level at a sufficient height above the rock bottom to allow the drainage water to flow out, and cool air to pass in.
Air stack (Min.). A stack or chimney built over a shaft for ventilation.
Alkalies (Chem.). Soluble hydroxides which turn red litmus paper blue, and neutralize acids, e.g., potash, soda.
Alloy (Met.). A homogeneous mixture of two or more metals by fusion.

Alluvial (Geo.). Clay, sand, and gravel deposited by water.
Alluvial gold (Min.). Gold found associated with water-worn material.
Amalgam (Met.). An alloy of quicksilver with some other metal. Amalgam is said to be wet, dry, crisp, \&c.
Amalgamator (Met.). One who amalgamates gold and silver ores.
Amygdaloidal (Geo.). Almond-shaped.
Analysis (Chem.). Qualitative-separates matter into its various elements.
Quantitative-states their relative proportions.
Anemometer (Phy.). An instrument for measuring the velocity of ventilating currents in mines.
Angle beam (Min.). A two-limbed beam used for turning angles in shafts, \&c.
Anhydride (Chem.). The residue obtained by the extraction (in combination with oxygen as water) of all the displaceable hydrogen from one or more molecules of an oxygen acid.
Anhydrous (Chem.). Without water in its composition.
Anneal (Met.). To toughen certain metals, glass, \&c., by heating and then allowing to cool slowly.
Anticlinal (Geo.). When rocks are bent over in the form of an arch.
Antimony crude (Met.). The mineral antimonite sweated out from its gangue.
Antimony star (Met.). The metal antimony when crystallized, showing fernlike markings on the surface.
Apron (Eng.). A covering of timber, stone, or metal, to protect a surface against the action of water flowing over it.
Aqua fortis (Chem.). Another name for nitric acid.
Aqua regia (Chem.). A mixture of hydrochloric acid and nitric acid.
Aqueduct (Eng.). An artificial elevated way for carrying water.
Archean (Geo.). Crystalline schists supposed to be of metamorphic origin.
Arenaceous (Geo.). Sandy.
Argentiferous. Silver bearing.
Argillaceons (Geo.). Clayey.
Argol (As.). Crude tavtar deposited from wine,
Arrastra (Met.). A circular trough in which drags are pulled round by being connected with a central revolving shaft by an arm and chain. Used for grinding and amalgamating gold ores.

Artesian well (Eng.). An artificial channel of escape, made by a bore hole, for a subterranean stream, subject to hydrostatic pressure.
Assay (As.). The determination of the amount of metal or other substances in the material treated chemically. The assay may be of a picked specimen, or an average sample. If treated on a large scale it is called a bulk assay.
Assayer (As.). One who performs assays.
Attle (Addle) (Min.). The waste of a mine.
Attrition (Geo.). The act of wearing away by friction.
Auriferous. Gold bearing.
Axle (Axle tree) (Mec.). The central bar on which the axle box revolves.
Axle box (Mec.). The thimble or shell that turns upon the axle.
Azimuth (Sur.). The azimuth of a body is that arc of the horizon that is included between the meridian circle at the given place, and another great circle passing through the body.
Azoic (Geo.). The age of rocks that were formed before animal life existed.

Backing (Eng.). The rough masonry of a wall faced with finer work; earth deposited behind a retaining wall, \&c.
Backlash (Min.). Backward suction of air currents, produced after an explosion of fire damp.
Backs (Min.). The overlying portion of a lode that has not been worked.
Back shift (Min.). Afternoon shift of miners.
Back stay (Min.). A wrought iron forked bar attached to the back of trucks when ascending an inclined plane, so as to throw them off the track in case the hauling rope, or coupling, gives way.
Baffends (Min.). Long wooden wedges for adjusting tubbing plates or cribs in sinking pits during the operation of fixing the tubbing.
Balance box (Min.). A large box placed on one end of a balance bob, and filled with old iron, rock, \&c., to counterbalance the weight of pump rods.
Balance brow (Min.). A self-inclined plane in steep seams on which a platform on wheels travels and carries the tubs of coal.
Balance pit. The pit in which the balance moves.
Balk. A large beam of timber (Min.). (1) Timber for supporting the roof of a mine, or for carrying any heavy load.
(2) A more or less thinning out of a seam of coal.

Ballast (Eng.). Broken stone, gravel, sand, \&c., used for keer-
ing railroad sleepers steady; also used to keep ships down in the water when out of cargo.
Bank (Min.). The top of a pit; the surface around the mouth of a shaft.
Bank-claim (Min.). A claim which includes the bank of a river or creek.
Banket (Min.). Auriferous conglomerate of South Africa.
Bar (Min.). (1) A ridge deposited in a river's bed.
(2) A "hard bar of ground" is a harder belt of rock than usually met with in a district.
Baring (Min.). See Stripping.
Bar mining (Min.). Working bars above river level.
Barrel amalgamation (Met.). Amalgamating ores in revolving barrels.
Barrow. A box with two handles at one end, and a wheel at the other.
(Min.) Heap of waste stuff raised from a mine.
Base metal (Met.). One that is not classed with the precious metals, gold, silver, platinum, \&c., that are not easily oxydized.
Basin (Geo.). A natural surface hollow.
Basset (Min.). Outcrop of a lode or stratum.
Batch (Min.). An assorted parcel of ore, sometimes called doles, when divided into equal quantities.
Batea (Min.). A wooden bowl for washing off gold, \&c.
Batt (Min.) A highly bituminous shale found in the coal measures.
Batten. A piece of thick board of less than 12 inches in width.
Batter (Eng.). The slope backwards of a face of masonry.
Battery. A set, e.g., a set of stamps for crushing purposes.
Bay of Biscay country (Geo.). See Crabholes 2.
Beach-combing (Min.). Working the sands on a beach for gold, tin, or platinum.
Beans (Min.). All coal which will pass through about $\frac{1}{2} \mathrm{in}$. screen.
Bear (Met.). A deposit of iron at the bottom of a furnace.
Bearers (Min.). Pieces of timber 3 ft . or 4 ft . longer than the breadth of a shaft, which are fixed into the solid rock at the sides, at certain intervals apart ; used as foundations for sets of timber.
Bearing (Sur.) The course of a compass.
(Mec.) The points of support of a beam, shaft axle pirot, \&c.
Bearing-up-pulley (Eng.). A pulley wheel fixed in a frame, and arranged to tighten or take up the slack of an endless belt or rope.

Beataway (Min.). Working hard ground by means of wedges and sledge-hammers.
Bed (Geo.). A layer of one sort of rock.
Bed claim (Min.). A claim which includes the bed of a river or creek.
Bed-plate (Eng.). A large plate of iron laid as a foundation for something to rest on.
Bed rock (Min.). The rock on or in which alluvial deposits collect.
Belland. A kind of lead poisoning lead miners are subject to. Belly (Min.). A swelling mass of ore in a lode.
Ben, Benhayl (Min.). The productive portion of a tin stream.
Bench (Min.). A terrace on the side of a river having at one time formed its bank.
Bench mark (Sur.). A mark, cut in a tree or rock by surveyors for future reference.
Bessemer steel (Met.) Formed by forcing air into a mass of melted cast iron, by which means the excess of carbon present is separated from it until only enough remains to constitute cast steel.
Beton (Eng.). Concrete of hydraulic cement with broken stone, bricks, gravel, \&c.
Bevel. The slope formed by trimming away an edge.
Bevel gear (Eng.). Cogwheels, with teeth so formed that they can work into each other at an angle.
Bin. A box with cover, used for tools, stones, ore, \&c.
Bind (Min.) Indurated argillaceous shales or clay, very commonly forming the roof of a coal seam and frequently containing clay ironstone.
Bing ore (Min.). The largest and best kind of lead ore.
Bit (Min.). Steeled point of a borer, or drill.
Black band (Min.). Carbonaceous ironstone in beds, mingled with coaly matter, sufficient for its own calcination.
Black batt, or Black stone (Min.). Black carbonaceous shale.
Black-jack (Min.). Properly speaking dark varieties of zinc blende, but many miners apply it to any black mineral.
Black ore (Min.). Partlydecomposed pyrites containing copper.
Black sand (Min.). Black minerals (magnetite, titaniferous iron, chromic iron, wolfram pleonaste, tournaline, cassiterite, \&c.) accompanying gold in alluvial.
Black tin (Min.). Dressed cassiterite, oxide of tin.
Blanch (Min.). A piece of ore found isolated in the hard rock.
Blanket tables (Min.). Inclined planes covered with blankets, to catch the heavier minerals passing over them.
Blast (Min.). To bring down minerals, rock, \&c., by an explosion.
(Met.) Air forced into a furnace.

Blast pipe (Met.). A pipe for supplying air to furnaces.
Blende (Geo.). Sulphide of zinc.
Blind coal (Min.). Coal altered by the heat of a trap dyke.
Blind creek (Geo.). A creek in which water only flows in very wet weather.
Blind lode (Min.). Having no visible outcrop.
Blind shaft (Min.). A shaft not coming to the surface.
Block coal (Min.). Coal in large lumps.
Blocking out (Min.). Working deep leads in blocks; somewhat like horizontal stoping.
Block reefs (Min.). Reefs showing frequent contractions longitudinally.
Blossom rock (Min.). Coloured vein stone detached from an outcrop.
Blow (Min.). A large increase in the size of a lode.
Blower (Min.). A sudden emission or outburst of firedamp in a mine.
Blow in (Met.) To commence a smelting process.
Blow off (Eng.). To let off excess of steam from a boiler.
Blow out (Met.). To finish a smelting campaign.
(Min.) Blown out shot, a blast that has gone off but not done its work.
Blow-pipe (As.). An instrument for creating a blast whereby the flame of a candle or lamp can be better utilised.
Blue-cap (Min.). A blue or brownish coloured halo of ignited firedamp and air on the top of a safety lamp in a dangerous atmosphere.
Blue-john (Min.). Fluorspar.
Blue-stone (Min.). (1) Sulphate of copper.
(2) Lapislazuli.
(3) Basalt.

Board or Bord (Min.). A wide heading or road.
Bob (Min.). A large crank for transmitting power from the motor to pump rods in a shaft ; may have L bobs, $\perp$ bobs, V bobs.
Body. The thickness of a lubricating oil or other liquid; also the measure of that thickness expressed in the number of seconds in which a given quantity of the oil at a given temperature flows through a given aperture.
Bonanza (Min.). An aggregation of rich ore in a mine.
Bond (Eng.). The arrangement of blocks of stone or brickwork to form a firm structure, by a judicious overlapping of each other so as to break joint.
Bone ash (As.). Burnt bones, pulverised and sifted.
Bonnet (Eng.). A cap over the end of a pipe or aperture.
Booming (Min.). Ground sluicing on a large scale, by empty-
ing the contents of a reservoir at once on material collected below, thus removing boulders.
Bosh (Met.). The plane in a blast furnace where the greatest diameter is reached.
Boss (Eng.). An increase of the diameter at any part of a shaft (2).
Botryoidal (Geo.). In grape-like bunches.
Bottle-jack (Eng.). An appliance for lifting heavy weights.
Bottom (Min.). In alluvial, the bed rock or reef.
Bottomer (Min.). The person who loads the cages at the pit's bottom and gives the signal to bank.
Bottom lift (Min.). The deepest column of a pump.
Bottom pillars (Min.) See Shaft pillars.
Boulders (Geo.). Loose rounded masses of stone detached from the parent rock.
Bow (Min.). The handle of a kibble.
Bowl metal (Met.). The impure antimony obtained from doubling.
Box (Min.). A 12 ft .-14ft. section of a sluice.
Boxing (Min.). A method of securing shafts solely by slabs and wooden pegs.
Brace (Eng.). An inclined beam, bar, or strut, for sustaining compression.
(Min.). A platform at the top of a shaft on which miners stand to work the tackle.
Brace-heads (Min.). Wooden handles or bars for raising and rotating the rods when boring a deep hole.
Brasque (Met.). A mixture of clay and coke or charcoal, used for furnace bottoms.
Brass (Min.). Iron pyrites.
Brasses (Eng.). Fitting of brass in plummer blocks, \&c., for diminishing the friction of revolving journals which rest upon them.
Brattice (Min.). A partition in a drive or shaft for ventilation purposes.
Breakstaff (Min.). The lever for blowing a blacksmith's bellows, or for working bore rods up and down.
Breast (Met.). The front part of a cupala furnace.
(Min.). (1) The standing end of rock, lode, \&c., immediately before one.
(2) Timber placed across a drive behind the main set of timber, used in soft ground.
Breastwall (Eng.). One built to prevent the falling of a vertical face cut into the natural soil.
Breccia (Geo.). A rock composed of angular fragments cemented together.
Breese (Min.). Fine slack.

Bridle-chains (Min.). Short chains by which a cage is attached to a winding rope.
Brow (Min.). An underground roadway leading to a working place driven either to the rise or to the dip.
Brown spar (Min.). Dolomite containing carbonate of iron.
Brown stone (Min.). Decomposed iron pyrites.
Brush (Min.). To mix gas with air in a mine by buffeting it with a jacket, \&c.
Bucket (Min.). A vessel used for holding rock, water, \&c., to be hauled to the surface.
(Eng.). (1) Each division on a water-wheel for holding water.
(2) The top valve or clack of a lifting set of pumps.
Bucketsword (Min.). A wrought-iron rod to which the pump bucket is attached.
Bucket tree (Min.). The pipe between the working barrel and the wind bore.
Bucking hammer (Min.). An iron disk provided with a handle, used for breaking up minerals by hand.
Buck quartz (Min.). Hard non-auriferous quartz.
Buck-staff (Met.). Uprights for bracing reverberatory furnaces together.
Buddle (Min.). An inclined table, circular or oblong, on which ore is concentrated.
Buller shot (Min.). A second shot put in close to, and to do the work not done by, a blown out shot, loose powder being used.
Bullion (Met.). The metallic product from ore.
Bull-wheel (Min.). A wheel upon which the rope carrying the boring rod is coiled, when boring by steam machinery.
Bunch (Min.). A small rich deposit of ore.
Burrow (Min.). See Dump.
Bush (Eng.). To line a circular hole with a ring of metal, to prevent the hole from wearing out.
Butterfly-valve (Eng.). A circular valve which revolves on an axis passing through its centre.
Butty (Min.). A contractor for getting coal.
By level (Min.). A side level driven for some unusual but necessary purpose.

Cab (Min.). The side parts of a lode, nearest the walls, which are generally hard and deficient in ore.
Cage (Min.). (1) An iron vehicle used to convey men, \&c., up and down shafts.
(2) The hollow drum of a horse whim round which the rope is wound.

Cage-seat (Min.). Scaffolding, sometimes fitted with strong springs, to take off the shock, and upon which the cage drops when reaching the pit bottom.
Cage sheets (Min.). Short props or catches on which cages stand during caging or changing tubs.
Cainozoic (Geo). Tertiary.
Cake (Met.). An agglomeration, as when ore sinters together in roasting, or coal cakes together in coking. A cake of gold is retorted gold before melting.
Calcareous (Geo.). Containing lime.
Calcine (Met.). To heat a substance; not sufficiently to melt it, but enough to drive off the volatile contents.
Californian pump (Min.). A rude pump made of a wooden box through which an endless belt with floats circulates; used for pumping water from shallow ground.
Cam (Eng.). A curved arm or wiper attached to a revolving shaft for raising stamps.
(Min.). Carbonate of lime and fluorspar, found upon the joints of lodes.
Campaign (Met.). The length of time a furnace remains in blast.
Canker. The ochreous sediment in mine waters; being bicarbonate of iron, precipitated by the action of air upon that mineral.
Cannel-coal. A coal that burns like a candle. Highly bituminous.
Cants (Eng.). The pieces forming the ends of buckets of a water-wheel.
Cap (Min.). (1) The upper portion of a lode.
(2) A piece of wood placed on props or legs in a drive.
Cap-rock (Min.). The uncertain upper rock that covers the older bed rock.
Capstan (Eng.). A vertical axle used for heavy hoisting, and worked by horizontal arms or bars.
Captain (Min.). Cornish name for manager or boss of a mine.
Car. A waggon or truck.
Carat. A weight nearly equal to four grains.
Carbona (Min.). A rich bunch of ore in the country rock connected with the lode by a mere thread of mineral.
Carbonaceous. Containing carbon.
Carbonate (Chem.). Carbonic acid combined with a base.
Cartridge (Min.). A cylindrical shell for containing blasting material, made just the size of the hole to be fired.
Case-harden. To convert the outer surface of wrought iron into steel by heating it while in contact with charcoal.

Casing (Min.). (1) The material found between a reef and its walls.
(2) A partition of planks dividing a shaft into compartments.
(3) The lining of shafts.

Cast-iron (Met.). Pig iron resulting from the reduction of iron ores which contain carbon (up to 5 per cent.), silicon, sulphur, phosphorus, \&c.
Catch-pit (Min.). A reservoir for saving tailings from reduction works.
Caulk. To fill seams or joints with something to prevent leaking.
Caunter lode (Min.). A vein running obliquely across the regular veins of the district.
Caved in (Min.). Undermined ground that has fallen in.
Cement (Min.). Auriferous gravel consolidated together.
Cementation (Met.). The process of converting wrought iron into steel by heating it in contact with charcoal : this produces blisters on the steel bars; hence blister steel. When the blisters are removed and the steel made more compact by reheating and subjecting it to a tilthammer, it is called tilted or shear steel. If the blister steel is broken up, remelted, and run into ingots, it is called ingot steel, which is harder and closer grained than tilted steel.
Center (Eng.). The supports of an arch while being built.
Centrifugal force (Phy.). Flying off from the centre.
Centripetal force (Phy.). Drawing towards the centre.
Chain (Sur.). A measure 66 feet long, divided into 100 links.
Chamber (Min.). See Plat.
Chamois leather. Soft untanned buckskin.
Charge (Met.). The material fed into a furnace at one time.
Chili-bars (Met.). Bars of impure copper, weighing about 200 lbs. ; imported from Chili, corresponding to the Welsh blister copper, containing 98 per cent. of copper.
Chill hardening. Giving a greater hardness to the outside of cast iron by pouring it into iron moulds which causes the skin of the casting to cool rapidly.
Chinese pump (Min.). Like a Californian pump, but made entirely of wood.
Chloride (Chem.). Chlorine chemically united with some base. Chock. Any piece of material used for filling up a chance hole or vacancy.
Choke-damp (Min.). Carbonic acid gas left after an explosion of fire-damp.
Chromate (Chem.). Chromic acid with a base.
Churn-drill (Min.). A long iron bar with a cutting end of
steel, used in quarrying, and worked by raising and letting it fall. When worked by blows of a hammer or sledge it is called a jumper.
Jhnte (shoot) (Min.). (1) A wooden or metal pipe or hole in the ground for passing down minerals to a lower level.
(2) The mineralized portion of a vein.

Clack (Eng.). A common pump valve.
Clack-door (Eng.). A cap near the valve that can be easily taken off, to allow an examination of the clack.
Clack-seat (Eng.). The receptacle for the valve to rest on.
Claim (Min.). A portion of ground pegged out and held by virtue of a miner's right.
Clasp (Eng.). A snugly fitting ferrule for connecting pumprods together. Cast and step when the rods clutch in cross steps. Clasp and tongue when the tongue of one rod lies in a corresponding recess of the other.
Clay course (Min,). A clay seam or gouge found at the sides of some veins.
Claying-bar (Min.). For moulding clay in a wet bore-hole.
Clean-up (Met.). To collect all the quicksilver and amalgam about a battery, after crushing.
Cleavage (Geo.). The planes at which cleavable stones break into plates or laminæ.
Clinometer (Sur.). An instrument for measuring vertical angles.
Clutch (Eng.). An arrangement at the end of separate shafts by means of which they catch into each other, so that both can revolve together.
Coarse (coose) (Min.). When lede stuff is not rich, the ore being only thinly disseminated throughout it.
Coarse metal (Met.). In copper smelting, the compound containing the copper concentrated in it after the first smelting to get rid of the bulk of the gangue in the ore.
Cobbing hammer (Min.). A short double-ended hammer for breaking minerals to sizes.
Cock (Eng.). A kind of valve for the discharge of water, gas, steam, \&c.
Coffer (Min.). Mortar box of a battery.
Coffer dam (Eng.). An inclosure built in the water, and then pumped dry, so as to permit masonry or other work to be carried on inside of it.
Cog (Eng.). A tooth of a cogwheel.
Coke (Met.). The fixed carbon and ash of coal sintered together.
Collar. A flat ring surrounding anything closely.
(Min.). Collar of a shaft is the first wood frame of a shaft.

Colour (Min.). Minute traces or individual spees of gold. Concentric. Circles having the same centre.
Conchoidal. Shell-like, such as the curved fracture of flint. Concrete (Eng.). Artificial stone, formed by mixing broken stone, gravel, sc., with common lime. When hydraulic cement is used instead of lime the mixture is called beton.
Concretion (Geo.). A cemented aggregation of one or more kinds of minerals around a nucleus.
Conduit (Eng.). A covered waterway.
Conduit hole (Min.). A flat hole drilled for blasting up a thin piece in the bottom of a level.
Conformable (Geo.): Strata are conformable when they lie one over the other with the same dip.
Conglomerate (Geo.). Rounded stones cemented together to form a massive rock.
Connecting rod (Eng.). A piece which connects a crank with something that moves it, or to which it gives motion.
Contact lode (Geo.). A vein lying between two differently constituted rocks.
Contour (Sur.). The line which bounds the figure of an object.
Copper plate (Met.). A sheet of copper which, when coated with mercury, is used in amalgamation.
Copper regulus or matt (Met.). $\mathrm{Cu}_{2} \mathrm{~S}$ with $\mathrm{Fe} \mathrm{S}, \mathrm{Zn} \mathrm{S}, \mathrm{Pb} \mathrm{S} \& c$., as impurities.
Cord of wood. A pile of wood $8 \mathrm{ft} . \times 4 \mathrm{ft} . \times 4 \mathrm{ft} .=128 \mathrm{c} . \mathrm{ft}$. Costeaning (Min.). Trenching for a lode.
Cotter bolt (Eng.). A key bolt ; or a bolt, which instead of a screw and nut at one end, has a slot cut through it at that end for the insertion of a wedge-shaped key or cotter, which is sometimes split.
Counter (Eng.). An apparatus for recording the number of strokes made by the Cornish pumping engine.
Counter shaft (Eng.). A secondary shaft or axte which receives motion from the principal one.
Country rock (Min.). The rock in which a mineral vein occurs.
Couplings (Eng.). Arrangements for connecting two shafts so that they shall revolve together.
Course (Min.). The direction of a lode.
Crab (Eng.). A variety of windlass or capstan being a short shaft or axle, either horizontal or vertical, which serves as a rope drum for raising weights, it may be worked by a winch or handspikes.
Crab holes (Min.). Holes often met with in the bed rock of alluvial. Also depression on the surface, owing to unequal decomposition of the underlying rock.

Cradle (Min.). A box with a sieve mounted on rockers for washing auriferous alluvial.
Cramp (Eng.). A short bar of metal having its two ends bent cownwards at right angles, for insertion into two adjoining pieces of stone, wood, \&c., to hold them together.
Crane (Eng.). A hoisting machine consisting of a revolving vertical post or stalk, a projecting jib and a stay for sustaining the outer end of the $j i b$; these do not change their relative positions as they do in a dervick. There is also a rope drum, with winding rope, \&c.
Crark (Eng.). A double bend at right angles in a shaft or axle to enable it to revolve.
Creaze (Min.). The middle of a buddle.
Creep (Min.). The gradual movement of the mineral matter of a mine, cansed by improper support.
(Eng.). Also, a very slow movement of the winding engine when the brake is not sufficiently applied.
Crevicing. Picking out the gold caught in cracks and crevices in the rocks, over which it has been washed.
Crib (Min.). A cast iron or wooden ring upon which tubbing or the brick lining of a shaft is built.
Crop (Min.). Ore of the first quality after it is dressed for smelting.
Croppings (Min.). Portions of a vein as seen exposed above ground.
Cross course (Min.). A vein lying more or less at right angles to the regular vein of the district.
Cross cut (Min.). A level driven across the regular veins or workings of a district.
Cross spur (Min.). A vein of quartz which crosses the reef.
Crow bar. A strong iron bar with a slightly curved and flattened end.
Crown-wheel (Eng.): A cogwheel in which the teeth stand nct upon its outer circumference as usual, but upon the plane of its circle.
Cracible (Met.). The bottom of a cupola furnace in which the molten materials collect.
(As.). Pots for smelting assays in.
Crushing (Min.). Reduction of mineral in size by machinery (Met.). Ditto, together with amalgamation.
Crystal (Geo.). A solid of definite geometrical form, which mineral (or sometimes organic) matter has assumed.
Culm (Min.). Inferior anthracite, and the smaller or slack of smokeless coal.
Cupel (As.). A cup made of bone ash for absorbing litharge.

Cut (Min.). (1) To strike or reach a vein.
(2) To excavate in the side of a hill.

Cutting down (Min.). To cut down a shaft is to increase its size.

Dam (Eng.). An embankment for stopping backwater.
Damp (Min.). Fire damp, choke damp, ground damp, \&c.. light carburetted hydrogen, carbon dioxide, and other gases injurious to life.
Damper (Eng.). A sliding door or valve to regulate the admission of air to a furnace.
Datum water level (Min.). The level at which water was first struck in a shaft sunk on a reef or gutter.
Day (Min.). Light seen at the top of a shaft.
Deadmen's graves (Geo.). Applied to country, generally basaltic, when owing to the unequal decomposition of the underlying rocks, heaps like graves occur.
Dead points (Eng.). Those two positions in the revolution of a crank where the crank-arm is parallel with the rod which connects it with the moving power, when the said rod exerts no tendency to turn the crank.
Dead roast (Met.). To completely drive off all volatile substances.
Deads (Min.). Waste or rubbish from a mine.
Dead work (Min.). The opening up or preparatory work for miniug which produces no ore.
Débris (Geo.). Fragments from any kind of disintegration.
Decrepitate (Met.). To fly to pieces with a crackling sound when heated.
Delta (Geo.). A triangular-shaped piece of alluvial land at the mouth of a river.
Denudation (Geo.). Rock laid bare by water or other agency.
Derrick (Eng.). A kind of crane in which the rope or chain forming the stay can be let out or hauled in at pleasure, thus altering the inclination of the $j i b$.
Detritus (Geo.). Finely powdered deposits worn from hard substances.
Devil's dice (Min.). Cubes of limonite, pseudomorphs after pyrites.
Dial, miners' (Sur.). An instrument for measuring angles when surveying underground.
Diaphragm. A thin plate or partition placed across a tube or other hollow body.
Die (Min.). The bottom iron block of a battery, or grinding pan on which the shoe acts.

Diggings (Min.). Where gold and other minerals are dug out from shallow alluvials.
Diluvium (Geo.). Allurial deposits of the Pleistucene period.
$\operatorname{Dip}$ (Geo.). The angle which the slope of a stratum forms with the horizontal.
Dirt (Min.). See Wash Dirt.
Disintegration (Geo.). Separated by mechanical means; not by decomposition.
Ditch (Min.). A narrow excavated channel for carrying water.
Divining or Dowsing rod (Min.). A small forked hazel twig, which when lield loosely in the hands is supposed to dip downwards when passing over water or metallic minerals.
Dog-iron. A short bar of iron with both ends pointed and bent down, so as to hold together two pieces of wood, into which the points are driven. Or one end may be bent down and pointed, while the other is formed into an eye, so that if the point be driven into a $\log$, the other end may be used to haul on.
Doles (Min.). Small piles of assorted or concentrated ore.
Dolly (Min.). A machine for breaking up minerals, being a rough pestle and mortar, the former being attached to a spring pole by a rope.
Donkey engine (Eng.). A small steam engine attached to a large one, and fed from the same boil er; used for pump ing water into the boiler.
Doorpiece (Eng.). The portion of a lift of pumps in whichthe clack or ralve is situated.
Dradge (Min.). Pulverized refuse.
Draftage. A deduction made from the gross weight of ore when transported, to allow for loss.
Draw a charge, To (Met.). To take a charge from a furnace.
Drawlift (Eng.). A mump that receives its water by suction, and which will not force it above its head.
Dressing (Min.). Preparing poor or mixed ores mechanically, for metallurgical operations.
Dressing floors (Min.). The floors or places where ores are dressed.
Drift (Min.). (1) Ver y loose alluvial deposits requiring close timbering to enable one to work them.
(2) Sce Drive.

Drifting (Min.). Winning paydirt from the ground by means of drives.
Drill (Min.). An instrument used in boring holes.
Drive (drift) (Min.). A horizontal passage in a lode.
Dropper (Min.). A spur dropping into the lode. A feeder.
Dropshaft (Min.). A monkey shaft down which earth and other matter is lowered by means of a drop (i.e., a kind of
pulley with break attached ; the empty bucket is brought up as the full one is lowered).
Drum (Min.). A revolving cylinder around which ropes are wound.
Drum rings (Min.) Cast-iron wheels with projections to which are bolted the staves or laggings forming the surface for the ropes to lap upon. The outside rings are shrouded to prevent the ropes from slipping off the sides of the drum.
Drusy (Geo.). A hollow cavity lined with small crystals.
Dry ore (Met.). Argentiferous ores which do not contain enough lead for smelting process.
Duck-machine (Min.). An arrangement of two boxes, one working within the other, for forcing air into mines.
Dump (Min.). The pile of mullock as discharged from a mine. Dust gold (Min.). Pieces under 2-3 dwt.
Dyke (Geo.). A vein of intrusive rock.
Eccentric (Eng.). A disc attached to a revolving shaft at some other point than its centre, which is surrounded by a loose ring, that receives an alternating motion.
Efforescence (Geo.). An incrustation by a secondary mineral ; due to loss of water of crystallization.
Elbow. A sharp bend as in a lode, or pipe.
Electric blast (Min.). Instantaneous blasting of rock by means of electricity.
Elevator pump (Eng.). An endless band with buckets attached, running over two drums for draining shallow ground.
Elvan (Min.). A Cornish name applied to most dyke rocks of that county, irrespective of the mineral constitution, but in the present day restricted to quartz porphyries.
Erosion (Geo.) The scooping out or wearing away of rocks, as by rains, \&c.
Escarpment (Geo.) A nearly vertical natural face of rock or soil.
Eye (Eng.). A circular hole in a bar for receiving a pin and for other purposes.
(Min.). The cye of a shaft is the very beginning of a pit.
Face (Min.): The extreme end of a tunnel or other mining excavation.
Face wall (Eng.). A wall built to sustain a face cut into the natural earth, in distinction to a retaining wall which supports earth deposited behind it.
False bedding (Geo.). Irregular lamination, wherein the laminæ though for short distances parallel to each other, are oblique to the general stratification of the mass at varying angles and directions.

False bottom (Min.). (1) A movable bottom in some apparatus.
(2) A stratum on which pay dirt lies, but which has other layers below it.
False set (Min.). A temporary set of timber placed in a drive until work is far enough advanced to put in a permanent sct.
Fan (Min.). A machine for forcing air into, or sucking it out of a mine.
Fascines (Eng.). Bunches of twigs and small branches for forming foundations on soft ground.
Faucet (Eng.). (1) A short tube for emptying liquids from a cask and stopped by a spigot.
(2) The wider end of a common cast-iron water or gas pipe.
Fault (Geo.). A dislocation in a rock, lode, or seam.
Feather (Eng.). A slightly projecting narrow rib lengthwise on a shaft, arranged to catch into a corresponding groove in anything that surrounds and slides along the shaft.
Feather edge (Min.). A passage from false to true bottom.
Feather ore (Min.). Sulphide of lead and antimony.
Feeder (Min.) A small vein running into a main lode.
Feed-pump (Eng.) A small pump for forcing water into a steam boiler.
Felloe (Eng.). The circular rim of a wheel into which the outer ends of the spokes fit, and which is often surrounded by a tire.
Fencing (Min.). Fencing in a claim is to make a drive round the boundaries of an alluvial claim, to prevent wash-dirt from being worked out by adjoining claim-holders.
Fend-off (Eng.). A sort of bell crant for turning a pamp-rod past the angle of a crooked shaft.
Fire bars (Eng.). The iron bars of a grate on which the fuel rests.
Fire-damp (Min.). Carburetted hydrogen, an explosive gas.
Firsts (Min.). The best ore picked from a mine.
Fish (Eng.) To join two beams, rails, etc. together, by long pieces at their sides.
Fissure (Geo.). An extensive crack.
Flags (Geo.). Broad flat stones for paving.
Flange (Eng.). A projecting ledge or rim.
Flat rod (Eng.). A horizontal rod for conveying power to a distance.
Flats (Min.). Narrow decomposed parts of limestones which are mineralized.
Flat sheet (Min.). Sheet-iron flooring at the brace and in the plats, chambers and junctions of drives, to facilitate the turning and management of trucks.

Float-gold (Met.). Gold in thin scales which float on water. Float-stones (Min.). Loose boulders from lodes lying on or near the surface.
Floodgate (Eng.). A gate to let off excess of water in flood or other times.
Floor (Min.) (1) A lode bent into a flat bcd.
(2) A seam or joint in a rock.
(3) A false bottom.

Flour-gold (Min.). The finest alluvial gold.
Flouring (Met.). Reducing mercury to fine globules, that being coated do not readily unite.
Flucan (Min.). A soft greasy clayey substance found in the joints of teins.
Flume (Eng.). An artificial watercourse.
Fluming (Eng.). Lifting a river out of its bed with wooden launders or pipes, in order to get at the bed for working.
Flush (Eng.). (1) To clean out a line of pipes, gutters, etc., by letting in a sudden rush of water.
(2) The splitting of the edges of stone under pressure.
(3) Forming an even continuous line or surface.
Flux (Met.). Used for promoting fusion when reducing ores. Fly-wheel (Eng.). A heavy revolving wheel for equalizing the motion of machinery.
Foaming (Eng.). An undue amount of boiling, caused by grease or dirt in a boiler.
Foliated (Geo.). Lamellar or leaf-like.
Follower (Eng.). Any cog-wheel that is driven by another which is called the leader.
Foot-hole (Min.) Holes cut in the sides of shafts or winzes to enable miners to ascend and descend them.
Foot-piece (Min). (1) A wedge of wood or part of a slab placed on the footwall against which a stull piece is jammed.
(2) A piece of wood placed on the floor of a drive to support a leg or prop of timber.
Footwall (Min.). The lower boundary of a lode.
Footway (Min.). Ladders in mines.
Force-pump (Min.). A pump that forces water above its valves.
Fore bay (Eng.). Penstock. The reservoir from which water passes directly to a water-wheel.
Fork (Eng.). A deep receptacle in the rock to enable a pump to extract the bottom water. A pump is said to be "going in fork" when the water is so low that air is sucked through the wind-bore.

Formation (Geo.). A series of strata comprising those that belong to a single geological age.
Fossicking (Min.) Overhauling old workings and refuse heaps for gold.
Fossil (Geo.). Organic remains found in mineral matter.
Frame (Min.). A table composed of boards, slightly inclined, over which water runs to wash off waste from slime tin.
Frame set (Min.). The legs and cap arranged so as to support a passage mined out of the rock or lode.
Friction rolls (Eng.). Hard cylinders placed under a body, so that it may be moved more readily than by sliding.
Friction wheels (Eng.). Wheels so placed that the journals of a shaft may rest upon their rims and thus be enabled to revolve with diminished friction.
Fulcrum (Eng.). The point about which a lever turns.
Furnace (Met.). A suitable heating apparatus for roasting and smelting ores.
Fuse (Min.). A hollow tube filled with an explosive mixture for igniting cartridges. (Met.) To melt.

Gad (Min.). A small steel wedge used for loosening jointy ground.
Gangue (Min.). Waste material from lodes.
Gannister (Min.). A hard compact extremely siliceous fireclay.
Gas. Any air like elastic vapour.
Gash vein (Min.). A wedge-shaped vein.
Gasket (Eng.). Rope, yarn or hemp, used for stuffing at the joints of water-pipes, etc.
Gearing (Eng.). A train of cog-whecls.
Geodes (Min.). Large nodules of stone with a hollow in the centre.
Géyser (Geo.). Natural fountains of hot water and steam.
Gib (Min.). A short prop of timber by which coal is supported whilst being holed or undercut.
(Eng.) A piece of metal often used in the same hole with a wedge-shaped key for holding pieces together.
Gin (Eng.). A revolving vertical axis, usually furnished with a rope drum, and having one or more long arms or levers by means of which it is worked by horses walking in a circle round it.
Giraffe (Min.). A mechanical appliance for receiving and tipping a car full of ore or waste rock, when it arrives at the surface.
Girder (Eng.). A beam larger than a common joist.
Gland (Eng.). The lid of a stuffing bex.

Gob or Goaf (Min.) That part of a mine from which the coal, etc. has been worked away, and the space more or less filled up.
Gold (Min.). See Alluvial, Paint, Flour, Rust gold, etc.
Gossan (Min.). A spongy ferruginous oxide, left after the soluble substances have heen dissolved out of a lode.
Governor (Eng.). Two balls, so attached to an upright revolving shaft, as to fly outward by their centrifugal force, thus regulating a valve.
Grade (Eng.). The amount of fall or inclination in ditches, flumes, roads, etc.
Grass (Min.). The surface of the ground.
Grating (Min.). A perforated iron sheet or wire-gauze placed in front of reducing machinery.
Gravel (Geo.). Water-worn stones about the size of marbles.
Greenstone (Geo.). A general term employed to designate green-coloured igneous rocks as diorite, dolorite, diabase, gabbro, etc.
Greywacke (Geo.). A compact grey sandstone frequently found in Paleozoic formations.
Griddle (Min.). A coarse sieve used for sifting ores, clay, etc.
Groin (Eng.). An arch formed by two segmental arches or vaults intersecting each other at right angles.
Groundsill (Min.). A log laid on the floor of a drive on which the legs of a set rest.
Ground sluicing (Min.). Washing alluvial, loosened by pick and shovel, in trenches cut out of the bed rock, using bars of rock as natural riftles. Used in shallow placers, hill claims, bank claims, and stream diggings.
Grout (Eng.). Thin mortar poured into the interstices between stones and bricks.
Guano (Geo.). A brown, grey, or white, light powdery deposit, consisting mainly of the excrement of seafowl in rainless tracts, or of bats in caves.
Gudgeons (Eng.). The metal journals of a horizontal shaft.
Guides (Min.). Continuous lengths of ropes or squared timber which run down the drawing compartment of a shaft for keeping the cage in position, while ascending and descending.
Gussets (Eng.). Plain triangular pieces of plate iron riveted by their vertical and horizontal legs to the sides, tops, and bottoms of box-girders, tubular bridges, etc., inside, for strengthening their angles.
Gutter (Min.). (1) A small water-draining channel.
(2) The lowest part of a lead that contains the most highly auriferous dirt.
Guy (Eng.). A stay of iron, wood, rope or chain.

H-piece (Eng.). A strong pipe cast in the form of the letter H , containing the bottom clack of a set of pumps.
Hade (Min.). The dip or inclination of a vein or fault, taking the horizontal (America) or vertical (England) as zero.
Half set (Min.). One leg piece and a cap.
Halvans (Min.). Gangue containing a little ore.
Hand-barrow (Min.). A long box with handles at each end.
Hand-dog (Min.). A kind of spanner or wrench for screwing up and disconnecting the joints of boring rods at the surface.
Hand-spike (Eng.). A wooden lever for working a capstan or windlass.
Hand-whip (Min.). An apparatus used in shallow alluvial workings, consisting of an upright, at the top of which is balanced a long sapling; at the thick end of the sapling a bag of earth is fastened, to counter-balance the bucket of dirt to be raised at the other end.
Hanger-on (Min.). The man who runs the full trucks on to the cage, and gives the signal to bank.
Hangers (Eng.). Fixtures projecting below a ceiling to support the journals of long lines of shafting.
Hanging-spear-rod (Min.). Wooden pump-rods adjustable by screws, etc., by which a sinking set of pumps is suspended in a shaft.
Hanging wall (Min.). The rock on the upper side of a reef.
Harrow (Min.). Somewhat like an agricultural harrow ; it is fixed to the pole of a puddling machine and dragged round to mix and break up the auriferous clays with water.
Hat-follers (Eng.). Cast-iron or steel rollers shaped like a hat, revolving on a vertical pin for guiding inclined hauling ropes around curves.
Hatter (Min.). A miner working by himself on his own account.
Hauling (Min.). The drawing or conveying of the produce of the mine from the working places to the bottom of the winding shaft, also elevating it to the surface.
Haunches (Eng.). The parts of an arch from the keystone to the skewback.
Hawser. A strong and tightly-made hempen rope.
Head (Eng.). Pressure of water in lbs. per square inch.
(Min.). Any subterraneous passage driven in solid coal. Also, that part of a face nearest the roof.
Head-board (Min.). A wedge of wood placed against the
harging wall, and against which one end of the stuli piece is jammed.
Header (Min.). (1) A rock that heads off or delays progress.
(2) A blast hole at or above the head.
(Eng.). A stone or brick laid lengthwise at right angles to the face of the masonry.
Heading (Min.). (1) A small driftucay or passage excavated in advance of the main body of a tunnel, but forming part of it, for facilitating the work.
(2) Coarse gravel or drift overlying the wash-durt.
Head-race (Min.). An aqueduct for bringing a supply of water on to the ground.
Heave (Min.). The shifting of rocks, seams, or lcdes upon the face of a erosscourse, etc.
Helve (Min.). The handle of a pick or mandrill.
Hewer (Min.). A collzer who cuts coal.
High-reef (Min.). The bedrock or reef is frequently found to rise more abruptly on onc side of a gutter than on the other, and this abrupt reff is termed a ligh-reef.
Hitch (Min.). A fault or dislocation of less throw than the thickness of the scam in which it occurs.
Hitches (Min.). Steps cut in the rock or lode for holding stay-beams, beams, or timber, etc., for various purposes.
Hoarding. A temporary close fence of boards placed around a work in progress.
Hod. A V-shaped trough with a long handle, used for carrying bricks, mortar, etc., to masons.
Hole (Min.). To undercut a seam of coal, etc.
Horn (Min.). A piece of bullock's horn about $8^{\prime \prime}$ in length, cut boat shape, for concentrating by water on a small scale.
Horse (Min.). A large enclosure of rock in a lude.
(Eng.). A mechanical support for anything.
Horse-power (Eng.). Work equal to raising $33,000 \mathrm{lbs}$. one foot high per minute.
Horse-whim (Min.). A vertical drum worked by a horse for hauling.
Hose (Min.). A strong flexible pipe, made of leather, canvas, rubber, etc., and used for the conveyance of water under pressure to any particular point.
Hub. The central part of a wheel through which the axletree passes, and from which the spokes radiate.
Hurdy-gurdy (Eng.). A water-wheel which receives motion from the force of travelling water.
Hydranlic cement (Eng.). A mixture of lime, magnesia, alumina and silica that solidifies beneath water.

Hydrometer (Chem.). An instrument for ascertaining the densities or specific gravities of liquids, by the depth of flotation as read on its graduated columu.

Igneous rocks (Geo.). Those that have been in a more or less fused state.
Inbye (Min.). Going into the interior of a mine away from the entrance.
Indicator (Eng.). A mechanical contrivance to show the position of the cage in the shaft.
Indoor-catches (Eng.). Stiong beams in Cornish pumpingengine houses to catch the beam in case of a smash, thus preventing damage to the engine itself.
In-fork (Min.). When a pump continues working after water has receded below the holes of the windbore.
Ingot (Met.). A lump of cast metal.
Inset (Min.). The entrance of a mine pathway down a shaft, or at the bottom, where the cages are loaded.
Iron hat or cap (Min.). The oxidised ferruginous material overlying lodes.

Jack (Eng.). An apparatus for raising heavy objects, consisting of an iron rack, supported on a short stout block of wood, and worked by cog-wheels and a winch. A screw. jack is a large screw working in a strong frame, the base of which serves for it to stand on.
Jacket (Eng.). An extra surface covering, as a steam jacket.
(Met.). A water jacket is a furnace having double iron walls, between which water circulates.
Jib (Eng.). The upper projecting arm of a crane supported by a stay.
Jig (Min.). An apparatus with a perforated bottom, on which ore is placed, which is frequently disturbed by vertical throws, giving the heavier particles an opportunity to collect on the bottom.
Jockey (Min.). A self-acting apparatus carried on the front truck of a set for releasing it from the hauling rope.
Joggle. A joint of trusses or sets of timber for receiving pressure at right angles or nearly so.
Joint (Geo.). Natural division, crack or parting in strata.
Journal boxes (Eng.). A fixture upon which a jourral rests and revolves, instead of a plummer block.

Journals (Eng.). The cylindrical supporting ends of a revolving horizontal shaft.
Jump (Min.). (1) To take clandestine possession of another's claim.
(2) An up-throw or down-throw fault.

Jumper (Min.). A drill used for boring in stone by simply lifting and dropping. It frequently has an enlarged knob or weight in the middle, and may be sharpened at one or both ends.

Kaolin (Geo.). A white clay produced from decomposed orthoclase felspar.
Keelwedge (Eng.). A long iron wedge for driving over the top of a pick hilt.
Keeve (Min.). A large wooden tub used for the final concentration of tin oxide.
Key (Eng.). (1) An iron bar of suitable size and taper for filling the keyways of shaft and pulley so as to keep both together.
(2) A kind of spanner used in deep boring by hand.
Keybolt. See Cotter-bolt.
Keystone. The centre stone of an arch.
Keyways (Eng.). Suitable corresponding grooves in shaft and pulley for receiving the key.
Kibble (Min.). The bucket used for raising stones, etc., from shafts.
Kick-up (Min.). An apparatus for emptying trucks.
Kiln (Met.). A chamber built of stone or brick or sunk in the ground for burning minerals in.
Kind (Min.). (1) Tender, soft, easy.
(2) Likely looking stone.

King post (King rod). The centre post, vertical rod or piece, in a truss; similar posts or rods when not at the centre, are Queen posts or rods.
Kit. Any workman's really necessary travelling outfits, as tools, etc.
Knee-piece (Eng.). A bent piece of piping.
Knocker (Min.). A lever which strikes on a plate of iron at the mouth of a shaft, by means of which miners below can signal to those on the top.
Knocker-line (Min.). The signal line extending down a shaft from the knocker.
Knuckle-joint (Eng.). Two rods connected together by a pin in such a way, that one laps each side of the other, thus affording a free side motion.

Ladder way (Ladder road) (Min.). The particular shaft or compartment of a shaft used for ladders.
Lagging (Min.). Thick flat boards fastened over the outside of regular frame timber of shafts and levels, in order to more safely secure the ground.
Laminæ. Sheets not naturally separated but which may be forced apart.
Lander (Min.). The man who receives a load of ore at the mouth of a shaft.
Lander's crook (Min.). A hook or tongs for upsetting the bucket of hoisted rock.
Lap. (1) To place one piece upon another with the edge of one reaching beyond that of the other.
(2) One coil of rope upon a drum or pulley.

Laths. See Slabs.
Launder (Eng.). A fume or aqueduct.
Lava (Geo.). A common term for all rock matter that has flowed from a volcano or fissure.
Leaching (Met.). To dissolve out by some liquid.
Lead (pronounced leed) (Min.). (1) Ledge (America), Reef (Australia), Lode or rion (England). A more or less vertical deposit of ore, formed after the rock in which it occurs.
(2) A bed of alluvial paydirt or auriferous gutter.
(3) The distance to which earth is hauled or wheeled.
(Eng.). A certain amount of opening
of the port-valre of a
steam engine, before
each stroke of the piston begins.
Leader (Min.). A small vein supposed to lead to a larger one. (Eng.). A cog-wheel that gives motion to the next one or follower.
Leat. A small water ditch.
Leg-piece (Min.). An upright log placed against the side of a drive to support the cap-piece.
Level (Min.). An underground road driven in the rock or lode. Lifting guard (Min.). Fencing placed around the mouth of a pit or shaft which is lifted out of the way for decking by the cages as they reach the surface.

Lift of pumps (Eng.). The column or set of pipes, with valves, etc., reaching from one cistern to another.
Lignite (Geo.). Altered vegetable matter showing ligneous structure.
Linch pin (Eng.). A pin near the end of an axle to hold the wheel on.
Lining (Min.). The planks arranged against frame sets.
Little giant (Min.). The name given to a special sort of hydraulic nozzle used for sluicing purposes.
Lixiviating (Met.). See Leaching.
Loam (Geo.). Any natural mixture of sand and clay which is neither distinctly sandy nor clayey.
Lock (Eng.). A short basin in a river or canal, with gates at each end, for raising and lowering barges, etc.
Lode (Geo.). A mineral vein.
Lode- or Loadstone (Min.). (1) Magnetic iron ore.
(2) Stone found in veins or lodes.

Logs (Min.). Portions of trunks of trees cut to lengths and built up so as to raise the mouth or collar of a shaft from the surface, in order to give the requisite space for the lodgment of mullock and ore.
Long tom (Min.). A wooden sluice about 24 feet long, 2 feet wide, and 1 foot high, for washing auriferous gravel.
Long wall (Min.). A system of working low beds and seams with long faces, by means of which all the valuable mineral is won.
Low grade (Min.). Not rich in mineral.
Lug (Eng.). Small projections on castings made for various purposes, e.g., for support, for connections, for lifting the casting by, \&c.
Lumber. Timber cut to the various sizes and shapes for carpenter's purposes.
Lute. An adhesive clay used either to protect any iron vessel from too strong a heat, or for securing air and gas-tight joints.
Lydian stone (Geo.). A hard black siliceous rock used as a touchstone for testing the quality of gold.

Macadamize (Eng.). A method of making roads with small stones which become settled and firm under pressure of the traffic.
Made ground (Geo.). Recent deposit.
Man-engine (Min.). An apparatus consisting of one or two reciprocating rods, to which suitable stages are attached, used for lowering and raising men in shafts.
Manhole (Eng.). An opening through which a man can pass
to enter a boiler, culvert, or get the other side of a ladderstage, \&c.
Marl (Geo.). Clay containing calcareous matter.
Marlin-spike. A sharp-pointed and gradually tapered round iron, used in splicing ropes.
Marsh gas (Min.). Fire-damp. $\mathrm{CH}_{4}$.
Massive rocks (Geo.). Igneous or eruptive rocks.
Match (Min.). Gunpowder put into a paper several inches long, and used for igniting charges of explosives.
Matrix (Geo.). The associated rocks and minerals in which an ore naturally occurs.
Matte (Met.). A product obtained when smelting certain kinds of ores whereby the valuable metals are concentrated in a sulphide.
Mattock (Min.). A kind of pick with broad ends for digging with.
Maul (Min.). A driver's hammer.
Manndril (Min.). A pick with two shanks and points, used for getting coal, \&c.
Meridian (Sur.) A north and south line.
Mesozoic (Gco.). The second great division of sedimentary rocks.
Metal (Min.). In coal-mining, indurated clay or slate. (Met.). Certain elements which are solid at ordinary temperature (with the exception of quicksilver), are opaque (except in the thinnest possible films), have a metallic lustre, and are better conductors of heat and electricity, and as a rule have higher specific gravity, than the non-metals.
Mill (Met.). Works for crushing and amalgamating gold and silver ores.
Miner (Min.). An underground workman skilled in extricating rock and minerals.
Mineral (Geo.). A natural homogeneous inorganic substance.
Miner's dial (Sur.). An instrument used in surveying underground workings.
Miner's inch (Min.). A measure of water varying in different districts, being the quantity of water that passes through a slit an inch high, of a certain width under a given head.
Miner's right (Min.). An annual permit from the Government to occupy and work mineral land.
Mining engineer (Min.). A man having knowledge and experience in the many departments of mining.
Monkey (Eng.). The hammer or ram of a pile-driver.
Monkey-shaft (Min.). A shaft rising from a lower to a higher level.

Monkey-wrench (Eng.). A screw-wrench or spanner, the gripping end of which can be adjusted by means of a screw to fit objects of different sizes.
Mop (Min.). Some material surrounding a drill in the form of a disc, to prevent water from splashing up.
Mortar (Min.). The vessel in which ore is put to be pulverised by a pestle or shoe.
Mortise. A hole cut in one piece of timber, \&c., to receive the tenon which projects from another piece.
Mote (moat) (Min.). A straw filled with gunpowder for igniting a shot.
Mother lode (main lode) (Min.). The principal vein of any district.
Mouth (Min.). The top of a shaft.
(Met.). The hole at the top of a blast furnace that the charges are fed in at.
Moyle (Min.). An iron with a sharp steel point, for driving into clefts when levering off rock.
Mudstone (Geo.). A fine more or less sandy argillaceous rock, having no fissile structure, and somewhat harder than clay.
Muffle (As.) A thin clay oven heated from the outside.
Muller (Met.). The upper grinding iron or rubbing shoe of amalgamating pans, $\&$ c.
Mullock (Min.). Country rock and worthless minerals taken from a mine.
Mundic (Min.). Iron pyrites.
Naked light (Min.). A candle, or any form of lamp which is not a safety-lamp.
Native metal (Geo.). A metal found naturally in that state.
Natural ventilation (Min.). When the workings of a mine are so arranged that air currents are produced without having to resort to artificial means.
Nave. The hub of a wheel.
Neck (Geo.). A cylindrical body of rock, differing from the country around it.
Needle (Min.). A sharp-pointed copper or brass rod with which a small hole is made through the stemming to the cartridge in blasting operations.
Nichol's prism (Phy.). A crystal of Iceland spar specially cut and prepared for optical purposes, to enable rays of light to be polarised.
Nick (Min.). To cut or shear coal after holing.
Nip (Min.). When the roof and fluor of a coal seam come close together, pinching the coal between.
Nitrate (Chem.). Nitric acid chemically combined with a base.

Nodules (Geo.). Concretions which are frequently found to enclose organic remains.
Nozzle. The front nose piece of bellows of a blast-pipe for a furnace, or of a water-pipe.
Nugget (Geo.). A natural lump of gold or other metal, applied to any size above $2-3$ dwts.
Nutt (Eng.). A short piece with a central female screw, used on the end of a screw-bolt, \&c., for keeping it in place.
Nutts (Min.). Small lumps of coal which will pass through a screen, the bars of which vary in the distance they are apart, from $\frac{1_{2}^{\prime \prime}}{}$ to $2 \frac{2^{\prime \prime}}{}$.

Off-take (Min.). (1) The raised portion of an upcast shaft above the surface.
(2) The length of boring rods taken off at the top of the bore-hole.
0il-smellers (Min.). In Pennsylvania men who profess to be able to indicate where petroleum oil is to be found.
Old man (Min.). Old workings in a mine.
Oolitic (Geo.). A structure peculiar to certain rocks, resembling the roe of a fish.
Open-cast (Min.). Workings having no roof.
Open-cut (Min.). To commence working after sinking the shaft.
Open-cutting (Min.). An excavation made on the surface for the purpose of getting a face wherein a tunnel can be driven.
Ores (Min.). Minerals or mineral masses from which metals or metallic combinations can be extracted on a large scale, in an economic manner.
Organic. Something animal or vegetable, that has life or has lived.
Out-bye (Min.). In the direction of the pit bottom.
Out-crop (Min.). The exposure of a mineral deposit at the surface.
Out-set (Min.). The walling of shafts built up above the original level of the ground.
0 verburden (Min.). The covering of rock, earth, \&c., overlying a mineral deposit which must be removed before effective work can be performed.
Overhand stoping (Min.). The ordinary method of stoping upwards.
Overlap fault (Geo.). A fault in which the shifted strata double back over themselves.
0xide (Chem.). A chemical combination of oxygen and a base
Pack (Min.). A rough wall built up to support the roof.
Packing (Eng.). The material placed in a stuffing-box to prevent leaks.

Paddock (Min.). (1) An excavation made for procuring washdirt in shallow ground.
(2) A place built near the mouth of a shaft where ore is stored.
Paint, gold (Min.). The very finest films of gold coating other minerals.
Palæozoic (Geo.). The oldest series of rocks in which fossils of animals occur.
Palm. A piece of stout leather fitting the palm of the hand, and secured by a loop to the thumb; this has a flat indented plate for forcing the needle.
Palm-needle. A straight triangular sectioned needle, used for sewing canvas.
Pan (Min.). A thin sheet-iron dish 16 inches across the top, and 10 inches at the bottom, used for panning off.
Panel (Min.). A large rectangular block of coal in situ. In panel workings the mine is divided into several panels, each worked by its own board and pillar.
Panning-off (Min.). Separating gold or tin from its accompanying minerals, by washing off the latter in a pan.
Parrot-coal (Min.). A kind of coal that splits or cracks with a chattering noise when on the fire.
Pass (Min.). (1) A convenient hole for throwing down ore to a lower level.
(2) A passage left in old workings for men to travel in from one level to another.
Pass-by (Min.). A siding in which tubs pass one another underground.
Pass into (Min.). When one mineral gradually passes into another without any sudden change.
Patent fuel. Small coal mixed with 8 to 10 per cent. of pitch or tar, and compressed by machinery into bricks.
Pay-dirt (Min.). That portion of an allurial deposit that contains gold in payable quantities.
Pay-out. To slacken or let out rope.
Peas (Min.). Small coal about $\frac{1}{2}$ to $\frac{3}{4}$ inch cube.
Peat (Geo.). Tbe decayed organic matter of bogs, swamps, \&c.
Penstock (Eng.). See Forebay.
Pentice (Min.) A few pieces of timber laid as a roof over men's heads, to screen them when working in dangerous places, e.g., at the bottom of shafts.
Pent-house (Min.). A wooden covering for the protection of sinkers working in a pit bottom.
Pestle. A hard rod for pounding minerals, etc.
Petrification (Geo.). Organic remains converted into stone.
Picker (Min.). A pointed instrument for picking out the tamping from a blast-hnle that has missed fire.

Pier (Eng.). (1) The support of two adjacent arches.
(2) The wall space between windows.
(3) A structure built out into water.

Pig (Met.). A piece of lead or iron cast into a long iron mould.
Pigsty timbering (Min.). Hollow pillars built up of logs of wood laid crossways, for supporting heavy weights.
Piling (Min.). A method of sinking a shaft through drift by driving piles down into it behind frames of timber.
Pillar (Min.). A portion of natural or artificial ground, left to support the roof.
Pillar and stall (Min.). A method of working seams or beds by first learing blocks of coal or ore to support the roof, and then robbing them.
Pillow-block (Eng.). See Plummer block.
Pinched out (Min.). When a lode runs out to nothing.
Pinion wheel (Eng.). The smaller of two cogwheels, which gives motion to the larger one.
Pipe-clay (Geo.). A soft white clay.
Piping (Min.). Hydraulicing.
Pit (Min.). The shaft and workings of a coal mine.
Pitch (Min.). Dip or rise in a seam.
(Eng.). (1) The slope of a roof.
(2) The distance apart of rivets; the cogs of a cogwheel or the thread of a screw.
(3) Boiled tar.

Pit's eye (Min.). Pit-bottom or entrance into a shaft.
Pitman (Min.). The man who attends to the pumps and timbers in the engine shaft ; and the security of permanent levels.
Pivot (Eng.). The lower end of a vertical revolving shaft.
Placer mining (Min.). Surface mining for gold, where there is but little depth of alluvial.
Plane (Min.). A main road either level or inclined, along which coals, \&c., are conveyed by gravity or engine power.
Piane table (Sur.). A simple surveying instrument by means of which one can plot on the field.
Plant (Eng.). All the appliances, machinerÿ, shcds, \&c., belonging to a mine or works.
rlat (Min.). A chamber or excavation made at the point of departure of a level from a shaft.
Plugging (Min.). When drift water forces its way through the puddle clay into the shaft; holes are bored through the slabs near the leakage point, and plugs of clay forced into them until the leakage is stopped.
Plumb. Vertical.
Plummer block (Eng.). A metal chair or support on which the journals of horizontal shafts generally rest and revolve

Plummet (Sur.). A plumb-bob or weight at the lower end of a string.
Plunger (Eng.). A cylinder used to force water up a column of pump pipes.
Pocket (Met.). A receptacle for fumes to collect in.
(Min.). A cavity in a rock.
Poling (Met.). Refining metal when in a molten condition by stirring it up with a green pole of wood.
Poll pick (Min.). A pick having the longer end pointed and the shorter end hammer shaped.
Poppet-heads (Min.). The pulley frame or hoisting gear over a shaft.
Porphyry (Geo.). A rock having a felsitic matrix, in which are developed crystals of quartz or other minerals.
Port (Eng.). The opening or passage controlled by a valve.
Post-tertiary (Geo.). Strata younger than the Tertiary formation.
Prian (Min.). A soft and soapy white clay found in the joints of veins.
Pricker (Min.). (1) A thin brass rod for making a hole in the stemming of blast holes for the insertion of a fuse, so that the flame can obtain access to the cartridge.
(2) A bent wire for regulating the size of a

Prill (Min.). An extra rich stone of ore.
(As.). A bead of metal.
Prime (Eng.). When water passes into a steam cylinder together with the steam.
Primitive rocks (Geo.). Those of the earliest formation.
Prong (Eng.). The forked end of the bucket-pump rods for attachment to the travelling valve and seat.
Prop (Min.). A piece of timber of varying dimensions, generally 1 inch diameter for every 1 foot in length, used in securing the ground of a mine.
Prospect (Min.). The yield of gold by panning off.
Prospecting (Min.). Searching for valuable minerals.
Prospector (Min.). One engaged in searching for minerals.
Pseudomorph (Geo.). When a mineral occurs in a false form, or one belonging to another species.
Pudding stone (Geo.). A conglonerate or breccia.
Puddle (Eng.). Earth well rammed into a trench, \&c., to prevent leaking.
(Met.). A process for converting cast-iron into
Paddling machine (Min.). A circular machine for washing pay dirt.

Pug-mill. A mill for tempering clay for bricks, pottery, \&c.
Pulley (Eng.). A wheel which carries a belt for driving purposes, or over which a rope passes.
Pulleying (Min.). Overwinding or drawing up a cage into the pulley frame.
Pulp (Met.). The moist pulverised mineral from a mill.
Pump-ring (Eng.). A flat iron ring which when lapped with tarred baize orengineshag secures the joints of water columns.
Pump rod (Eng.). The rods which connect the motive power to the pump.
Pumptree (Eng.). Cast iron pipes generally 9 feet long of which the column or sett is formed.
Punch-prop (Min.). A short timber prop set on the top of a crown tree, or used in holing as a sprag.
Putty-stones (Min.). Soft pieces of decomposed rock found in placer deposits.
Pyrometers (Met.). Instruments for measuring high degrees of heat.

Quarry (Min.). (1) An open surface excavation for working valuable rocks or minerals.
(2) An underground excavation for obtaining stone for stowage or packwalls.
Quaternary (Geo.). Post-tertiary period.
Queen post. Vertical ties employed to support roofs when kingbolts are not sufficient.
Quick (Geo.). Soft watery strata, e.g., running sand, (Met.). Abbreviation for quick lime.

Rabbling (Mct.). Stirring up a charge of ore in a reverberatory furnace with specially designed iron rods.
Race (Eng.). A channel for conducting water to or from the place where it performs work. The former is tcrmed the head race, and the latter the tail race.
Rack-pinion (Eng.). The rack is a straight row of cogs on a bar called a rack-bar ; the pinion is a small cogwheel that works into it.
Raff (Min.). The coarse ore after crushing by Cornish rolls.
Raff-wheel (Min.). A revolving wheel with side buckets for elevating the raff.
Rag-wheel (Eng.). Sprocket wheel. A wheel with teeth or pins that catch into the links of chains.
Ram (Eng.). The plunger of a pump.
Raw ore (Met.). Not roasted or calcined.
Reaming (Min.). Enlarging a bore hole.
Receiving pit (Met.). A shallow pit for holding material run into it.

Reduced (Chem.). When a metal is freed from its chemical associate it is said to be reduced to the metallic state.
(Min.). To make smaller in size.
Reduction works (Met.). Works for reducing metals from their ores.
Reef (Min.). (1) A vein of quartz.
(2) Bed rock of alluvial claims.

Reef-drive (Min.). In alluvial mines, drives made in the country rack or reef.
Refining (Met.). The freeing of metals from impurities.
Refractory (Met.). Rebellious ore, not easily treated by ordinary processes.
Refuge-hole (Min.). A place formed in the side of an underground plane in which a man can take refuge during the passing of a train or when firing shots.
Regulus (Met.). See Matte.
Reserve (Min.). Mineral already opened up by shafts, winzes, levels, f.c., which may be broken at short notice for any emergency.
Reservoir (Eng.). An artificially built, dammed or excavated place for holding a reserve of water.
Retaining wall (Eng.). Built to retain earth behind it.
Retort (Met.). An iron vessel with a long neck used for distilling the quicksilver from amalgam.
Reverberatory (Met.). A class of furnaces in which the flame from the fire grate is made to beat down on the charge in the body of the furnace.
Reversed fault (Geo.). See Overlap fault.
Riddle (Min.). An oblong frame holding iron bars parallel to each other, used for sifting material that is thrown against it.
Rider (As.). The movable weight on a beain of a balance.
Riffle or Ripple (Min.). Cross pieces placed on the bottom of a sluice to save gold; or grooves cut across inclined tables.
Right shore. The right shore of a river is on the right hand when descending the river.
Rill (Min.). The coarse ore at the periphery of a pile.
Ring bolt. A bolt with an eye and a ring at one end.
Rise (Geo.). The inclination of strata when viewed in the opposite direction to their dip.
(Min.). A hole worked from below upwards.
River Mining (Min.). Working beds of existing rivers by deflecting their course, or by dredging.
Roasting (Met.). Heating ores at a temperature sufficient to
cause a chemical change, but not enough to smelt them. Oxidising, chloridizing, and reducing roasting.
Rob (Min.). To cut away or reduce the size of pillars of coal.
Rock (Geo.). A mixture of different minerals in varying proportions.
Rock-breaker (Min.). A machine for reducing ore in size by crunching it between powerful jaws.
Rock-drill (Min.). A rock boring machine worked by hand, compressed air, or steam.
Rocker (Min.). See Cradle.
Rock-shaft (Eng.). A shaft which only rocks from side toside, instead of making a complete revolution.
Rodding (Min.). The operation of fixing or repairing wooden eye guides in shafts.
Rolling ground (Geo.). When the surface is much varied by many small hills and valleys.
Roof (Min.). The upper portion of any under-ground excavation.
Room and Rance (Min.). See Pillar and stall.
Round-coal (Min.). Coal in large lumps, either hand picked or after passing over sereens to take out the smalls.
Rubble. Coarse pieces of rock.
Run (Min.). (1) A chute of ore.
(2) A run of ground, means that the ground has given way.
Rang, Rundle or Round. A step or cross bar of a ladder.
Runner (Min.). See Guides.
Running lift (Min.). A sinking sett of pumps constructed to lengthen or shorten at will, by means of a sliding or telescoping windbrre.
Rush (Min.). An old-fashioned way of exploding blasts by filling a hollow stalk with slow powder and then igniting it.
Rush-together (Min.). See Caved in.
Rust-gold (Min.). Gold coated with oxide of iron or manganese.
Rusty (Min.). Stained by iron oxide.
Saddle reef (Geo.). A reef having the form of an inverted V.
Safety cage (Min.). A cage used for hoisting and lowering in shafts which is provided with a safety catch.
Safety catch (Min.). An apparatus attached to cages to prevent them from falling in case the rope or chain connecting them with the motive power should break.
Safety door (Min.). A strongly constructed dour hinged to the roof of a coal mine, and always kept open and hung near to a main door for immediate use in case of damage to the main door.

Safety fuse (Min.). A cord with slow burning powder in the centre for exploding charged blast holcs.
Safety lamp (Min.). A coal miner's lamp protected from explosive gases by glass and wire gauze.
Safety valve (Eng.). A valve loaded with a certain weight or a spring of given strength, so that when steam or air of great pressure is present, it can escape.
Sag. A depression, e.g., in ropes, ranges of mountains, \&c.
Salting (Min.). Fraudulently enriching mineral matter.
Sampler (Min.). An instrument or apparatus for taking samples.
Sand bag (Eng.). A bag filled with sand for stopping leaks.
Scaffolding (Met.). Incrustations on the inside of a blast furnace.
Scantling. The depth and breadth of pieces of timber.
Scorifier (As.). A small dish used in assaying.
Schist (Geo.). Crystalline or metamorphic rocks having a slaty structure.
Scoriæ (Geo.). Ashes.
Scraper (Min.). An instrument for cleaning a hole that has been bored or drilled.
Screen (Min.). (1) A mechanical apparatus for separating smalls from large.
(2) A cloth brattice or curtain hung across a road in a mine to direct the ventilation.
Scupper nails. Nails with broad heads for nailing down canvas, \&c.
Seam (Geo.) A horizontal bed of coal.
Seating (Eng.). (1) The stone masonry in which a steam boiler is set.
(2) The ring upon which a valve shuts tightly.
Secondary rocks (Geo.). Those situated above the primitive and below the tertiary formations.
Seconds (Min.). The second class ore of a mine that requires dressing.
Section (Geo.). A rertical exposure of strata.
Sedimentary rocks (Geo.). Rocks formed from deposits by wind or water.
Segregated (Gco.). Separated from its surroundings and collected together.
Self-acting inclined plane (Eng.). An inclined plane on which the full set draws the empties up hill.
Self-feeders (Min.). Automatic appliances for feeding ore dressing machines.
Selvage (Min.). The clay seam on the walls of veins.
Serpentine (Geo.). A hydrated magnesian silicate formed by the alteration of certain igneous rocks.

Set-hammer. The flat-faced hammer held upon hot iron by a blacksmith when shaping or smoothing a surface by aid of his striker's sledge.
Set of timber (Min.). Those timbers used in a level consisting of a ground sill, cap piece and two leg pieces.
Set-off (Eing.). An iron projection from the main pump-rod on which the bucket pumping rod is fixel.
Set-screw (Eng.). A screw passing through a fixed piece so as to adjust or secure a movable piece.
Sett (Eng.). A column of pumptrees with buckets or ram, \&c., complete.
Shackle. An U-shaped link in a chain, closed by a pin; when the latter is withdrawn the chain is severed at that point.
Shaft (Min.). A vertical or diagonal hole in the ground, used for the working way of a mine.
(Eng.). A large axle.
Shaft pillar (Min.). Solid coal left unworked beneath colliery buildings and around the shafts, to support them against creeps.
Shaking table (Min.). An inclined table for concentrating fine grains of ore which is rapidly shaken by a short motion.
Shale (Geo.). A fine grained rock with fissile structure.
Shank. The body of a bolt exclusive of its lead.
Shear legs (Eng.). A high wooden frame placed over an engine or pumping shaft fitted with small pulleys and rope for lifting heavy weights.
Shears or Sheers (Eng.). Two tall poles with their feet some distance apart and their tops fastened together for supporting hoisting tackle.
Sheave (Eng.). A wheel or round block, with a groove around its circumference, for guiding a rope.
Shoad stones (Min.). Stray stones or floaters from the croppings of a deposit of minerals.
Shoes (Min.). (1) Steel or iron guides fixed to the ends or sides of cages to fit and run upon the conductors.
(2) The upper working face of a stamp or qrinding pan.
Shoot (Shute, Chute) (Min.). (1) A run of minerals in a vein.
(2) A pass down which minerals are tipped.
Shore (Eng.). A studdle or thrusting stay.
Shot (Min.). The firing of a blast.
Shotty gold (Min.). Granular pieces like shot.
Sickening (Met.). A coating of impurities on Quicksilver
that retards amalgamation or the coalescence of globules of quicksilver.
Sidelong reef (Min.). An overhanging wall of bed rock in alluvial formations running parallel with the course of the gutter; generally only on one side of it.
Siding (Eng.). A short piece of railroad track branching off from the main one to serve as a passing place.
Sill (Min.). A piece of wood placed across the bottom of a drive on which the legs of a set stand.
Silver (Met.). (1) A white ductile metal.
(2) Short for quicksilver.

Sink (Min.). To excavate strata in a downward direction.
Sizing (Min.). To sort minerals into sizes.
Skew-back (Eng.). The inclined stone from which an arch springs.
Skid (Min.). Guides on which sledges, trucks, buckets, bags, or cages are run.
Skip (Min.). A long waggon used for hoisting rock from mines.
Slab (Min.). Split pieces of timber from $2^{\prime \prime}$ to $3^{\prime \prime}$ thick, $4^{\prime}$ to $6^{\prime}$ long, and $7^{\prime \prime}$ to $14^{\prime \prime}$ wide, placed behind sets or frames of timber in shafts or levels.
Slack (Min.). Small coal that passes through a $\frac{3}{4 \prime \prime}$ screen.
Slag (Met.). The molten gangue from treating ores in furnaces.
Slate (Geo.) Compact clay which has assumed a hard regular laminated structure.
Sledge. A heavy double-handed hammer.
Sleeper (Eng.). The foundation pieces on which rails rest.
Sleeve (Eng.). A hollow cylinder fitting over two pieces to hold them together.
Sleigh. A vehicle with double kiel-runners instead of wheels.
Slicken side (Geo.). The smooth striated surface on opposite walls of joints, caused by motion of the rock.
Slide (Geo.). A vein of clay intersecting the rock when the latter has been faulted.
Sliding wind bore (Eng.). The bottom pipe or suction piece of a sinking sett of pumps, having a lining made to slide like a telescope within it; to give length without altering the adjustment of the whole column of pipes.
Slime, Sludge (Min.). The pulp or fine mud from a mill, or from a drill-hole.
Slings. Pieces of ropes or chains to be put around stones, \&c., for raising them by.
Slip. The sliding down of the sides of earthworks or banks.
Sluice-box (Min.). A trough with ripples or false bottom for catching gold.

Sluice-head (Min.). A measure to gauge the quantity of water that flows in a channel.
Sluicing (Min.). Ground sluicing is working gravel by excavating with pick and shovel, and washing the débris in trenches with water not under pressure.
Snag (Eng.). A lug with a hole through it for a bolt.
Snift (Min.). A match for igniting a train of gunpowder, arranged to give miners time to retire.
Snore-piece (Eng.). The lowest end of a pump sett through which the water passes.
Sole (Eng.). That lining round a water-wheel which forms the bottoms of the buckets.
Sole-plate (Min.). See Foot-piece.
Sollar (Min.). A wooden platform fixed in a shaft for the ladders to rest on.
Sows (Met.). Iron deposits at the bottom of furnaces.
Spall (Min.). To break up rocks with a large hammer for hand-sorting.
Span-beam (Eng.). A long wooden beam supporting the head pivot of the drum-axle of a gin, and resting at its extremities upon inclined legs.
Spanner (Eng.). A lever with a square eye at one end, for tightening nuts on screw-bolts, \&c.
Spar (Min.). A name given to certain white quartz-like minerals, e.g., calcspar, felspar, fluorspar.
Spear-plate (Eng.). Wrought-iron plates bolted to the sides of spears when joined together.
Specific gravity (Phy.). A comparative degree of weight; that of water being taken as unity.
Specimen (Min.). A picked piece of mineral.
Speiss (Met.). Combinations of arsenic or antimony with iron, copper, nickel, \&c.
Spelter (Met.). The commercial name for zinc.
Spent-shot (Min.). A blast-hole that has been fired, but has not done its work.
Spew (Min.). The extension of mineral matter on the surface past the ordinary limits of the lode.
Spider. See drum-ring.
Spiking-curbs (Min.). A light ring of wood to which planks are spiked when plank-tubbing is used.
Splay. To widen or flare like the wing walls of most culverts. Splint (Min.). A laminated, coarse, inferior, dull-looking, hard coal, intermediate between cannel and pit coal.
Spoil (Min.). Débris from a coal mine.
Sprag (Min.). A short wooden prop set in a slanting position for keeping up the coal during the operation of holing.
spring-beams (Min.). Two short parallel timber beams built
with a Cornish pumping-engine house, nearly on a level with the engine beam, for catching the beam, \&c., and preventing a smash in case of a breakdown.
Spring of an arch (Eng.). The rise or vertical height between the skew-back and the highest part of the arch.
Spring-pole (Min.). An elastic wooden pole from which boring-rods are suspended.
Sprocket-wheel (Eng.). Rag-wheel. A wheel with teeth or pins which catch in the links of a chain.
Spur (Min.). An off-setting pointed branch from a lode or mountain.
Spur-wheel (Eng.). A comparatively small driving cog-wheel.
Stack (Met.). A high chimney built on a separate foundation. (Min.). To heap ore or wood into piles.
Stage-pumping (Min.). Draining a mine by means of two or more pumps placed at different levels in the shaft, so that the lower passes on the water to the upper one.
Staging. The temporary flooring of a scaffold, platform, \&c.
Stalactites (Geo.) Icicle-shaped appendages of mineral matter suspended from above.
Stalagmites (Geo.). Lumps of mineral matter which accumulate on the floor below stalactites.
Stall (Min.). A working place in a coal mine.
Stamps (Min.). Large pestles worked mechanically ; used for pulverising stone.
Stanchion (Eng.). A vertical prop or strut.
Standing bolt. See Stud-bolt.
Standing sett (Eng.). A fixed lift of pumps in a sinking set.
Staple. An U-shaped band with screw ends, for tightening two or more pieces together. Also an U-shaped double pointed nail for driving into wood.
Starved (Eng.). When a pump is choked at the brass holes.
Station (Min.). A plat or convenient resting place in a shaft or level.
Stave. A ladder step.
Stay (Eng.). Props, struts, or ties for keeping anything in its place.
Stay-bolts (Eng.). Long bolts placed across the inside of a boiler, \&c., to give it greater strength.
Steam coal (Min.). A hard, free-burning, non-caking white ash variety of coal.
Steel needle (Min.). An instrument used in preparing blasting holes before the safety fuse was invented.
Stemmer (Min.). A copper rod used for stemming.
Stemming (Min.). See Tamping.
Step (Eng.). The cavity in a piece for receiving the pivot of an upright shaft, or the end of an upright piece.

Stobb (Min.). A long steel wedge used in bringing down coal after it has been holed.
Stock (Eng.). The eye with handles attached to it, in which the dies for the cutting of screws are held. (Geo.). A body of rock with ore disseminated through it
Stockwork (Geo.). A rock run through with a number of small veins close together, the whole of which has to be worked when mining such deposits.
Stomp (Min.). A short wooden plug fixed in the roof of a level to serve as a bench-marlh for surveys.
Stone coal (Min.). Anthracite; also other hard varieties of coal.
Stone-tubbing (Min.). Water-tight stone-walling of a shaft cemented at the back.
Stoop and room (Min.). A system of working coal similar to pillar and stall.
Stoping (Min.). Working out ore between two levels or on the surface by stopes or steps.
Stove up or stoved. Upset. When a rod of iron heated at one end is hammered endwise, so that that part becomes stouter than the remainder.
Straight end and walls (Min.). A system of working coal, somewhat similar to board and pillar.
Straightwork (Min.). A system of getting coal by headings or narrow work.
Strake (Min.). A slightly inclined table for separating heavier minerals from lighter ones.
Strap (Eng.). A long thin narrow piece of metal bolted to two bodies to hold them together.
Strapping-plate (Eng.). Strong iron plates used in connecting wooden pump-rods with transverse bolts and nuts.
Stratum, strata (Geo.). A layer or bed of rocks.
Streak (Geo.). The colour of a mineral when scratched.
Strike (Geo.). (1) The line of outcrop of a stratum in the direction at right angles to the dip. (2) To meet with.

Strike joints (Geo.). Joints in strata parallel to the strike.
Striking deal (Min.). Planks fixed in a sloping direction just within the mouth of a shaft to guide the $t u b$ to the surface. Stringer (Eng.). Any longitudinal timber on beam, \&c.
Stripping (Min.). Baring a lode by removing the rock, generally on its footwall preparatory to breaking it down.
Strut (Eng.). A prop to sustain compression whether vertical or inclined.
Stud (Eng.). A short stout projecting pin.
Stud-bolt (Eng.). A bolt with a worm cut at both ends ; one to be screwed into something permanently, the other to
hold by means of a nut something that may have to be removed at times.
Studdle (Min.). A piece of squared timber placed vertically between two sets of timber in a shaft.
Stuffing box (Eng.). A small box round the piston rod, at the end of the cylinder, so arranged as to prevent the escape of steam, air, or water.
Stull (Min.). A piece of timber laid across a drive or workings, inclined upwards towards the hanging wall, when it is fixed against a head board, while the lower end rests in a hole in the footwall. Slabs are placed on these stullpieces when required to store mullock.
Stumping (Min.). A kind of pillar-and-stall plan of getting coal.
Substratum (Geo.). The underlying rock formation.
Subsoil (Geo.) The broken upper part of a rock immediately under the soil.
Suction-pump (Eng.). A pump wherein by the movement of a piston, water is drawn up into the vacuum caused.
Sulphate (Chem.). Sulphuric acid combined with a base.
Sulphide (Chem.). A combination of sulphar and a base.
Sulphuret (Chem.). See Sulphide.
Sump (Min.). The lowest part of a shaft into which the water drains.
Surface deposits (Geo.). Those which are ex osed and can be mined from the surface.
Swabstick (Min.). A short wooden rod bruised into a kind of brush at one end, used for cleaning out a drilled hole.
Swage or Swedge. A hammer-like instrument, on one face of which is an indenture, which being held upon a piece of hot iron and struck with a heavy hammer, leaves the impression of the indentation upon the iron.
Sweet roast (Met.). To roast dead or completely.
Swing (Phy.). The arc or curve described by the point of an instrument such as a pick or hammer when being used.
Swinging plate (Met.). Amalgamated copper plates hung in sluices to catch float gold.
Switch (Eng.) The moveable tongue or rail by which a train is diverted from one track to another.
Synclinal curve (Geo.). A trough-shaped curve.
Tackle (Eng.). Ropes, chain, detaching hooks, cages, and all other apparatus for raising coal or ore in shafts.
Tailings (Met.). The detritus from reduction works or goldwashing machinery.
Tail-race (Min.). The channel along which water flows after it has done its work.

Tail-rope (Min.). A rope working in conjunction with a main rope in a system of underground haulage on slightly inclined planes, also used as a balance in shafts.
Tamp (Min.). To fill up a blast-hole above the explosive charge with some substance before firing a shot.
Tamping (Min.) The material used to $\operatorname{tamp}$ with.
Tamping bar (Min.) A copper bar for ramming down the tamping.
Tap (Min.). To cut or bore into old workings for the purpose of liberating accumulations of water or gas.
Tape, Tap (Eng.). Plug-tap. A steel screw suitably grooved and sharpened for cutting out the mother screws in nuts.
Tappet (Eng.). A short arm or projection from a revolving shaft or alternating bar, intended to come in contact with, or tap something at each revolution or stroke.
Teeth (Eng.). See Cog.
Telluride (Chem.). Tellurium combined with a base.
Temper. (1) To change the hardness of metals by first heating and then plunging them into water, oil, \&c.
(2) To mix mortar, or to prepare clay for bricks, \&c.

Tenon. A projecting tongue fitting into a corresponding cavity called a nortise.
Terrace (Geo.). A raised level bank, such as river terraces, lake terraces, \&c.
Tertiary (Geo.). The third great division of rocks in which the highest class of vertebrate animals first appear.
Test (Met.). An iron framework which is filled with bone-ash for cupelling on a large scale.
Test-tubes (Chem.). Very thin glass tubes closed at one end for testing substances in the wet way.
Theodolite (Sur.). An instrument used in surveying. For taking both vertical and horizontal angular measurements.
Thick seams (Geo.). Coal seams of greater thickness than (say) 8 feet.
Thimble (Eng.). (1) A short piece of tube slid over another piece to strengthen a joint, etc.
(2) An iron ring with a groove round it on the outside, used as an eye when a rope is doubled about it.
Thin seam (Geo.). Coal seams less than (say) 3 feet thick.
Thread (Eng.). The continuous spiral projection or worm of a screw.
Through and through (Min.). A system of getting bituminous coal without regard to the size of the lump.
Throw (Geo.). The throw of a fault is the vertical displacement of the rocks faulted.

Thrast (Geo.) A creep due to weight.
Ticketing (Min.). English periodical markets for the sale of ores.
Tie (Eng.). Any piece that sustains tension or pull.
Tie-back (Min.). A beam serving a similar purpose as a fendoff beam, but fixed at the opposite side of the shaft or inclined road.
Tip (Tipper, Tippler) (Min.). (1) A platform with rails attached, fixed upon an axle and connected with a lever on which a car is run and tilted over.
(2) Also a place where ore or mullook is tipped.
Token (Min.). A mutually understood mark placed upon a bucket of ore when it is hoisted or lowered into a shaft, to acquaint the lander or filler of some important matter.
Topit (Min.). A kind of brace-head screwed to the top of boring rods when withdrawing them from the hole.
Tramway (Eng.). A small roughly constructed iron track for ranning waggons or trucks on.
Transome (Eng.). A heavy wooden bed or supporting piece.
Trap (Geo.). Igneous rocks that form "trappen" or steps.
Trass (Geo.). A rock composed of earthy or compact pumiceous dust ; in which fragments of pumice, trachyte, greywacke, basalt, carbonised wood, etc., are imbedded.
Tree-nail. A long wooden pin for securing planks or beams together.
Trestle (Eng.). Any structure which is composed of a network of timbers securely stayed.
Tribute (Min.). A method of working mines by contract, whereby the mirrers receive a certain share of the products won.
Trig. A sprag used to block or stop a wheel or any machinery.
Trommel (Min.). A drum, consisting of a cylindrical or conical shaped sheet-iron mantle, generally punched with holes, which revolves; used for washing or sorting ores.
Trompe (Min.). A water-blast for producing ventilation by the fall of water down a shaft.
Trough fault (Geo.). A mass of rock letdown between two faults.
Truck system (Min.). Paying miners in food instead of money.
Trundle (Eng.). Two parallel circular pieces some distance apart, connected by a central axis and by cylindrical rods placed round near the periphery and parallel to the axis, which serve the purpose of teeth in a cog-wheel.
Trunnions (Eng.). Cylindrical projections, forming a sort of interrupted shaft, attached to some vessel, so that it can have a vertical movement.

Tabbing (Min.). The cast iron, timber, or walling of a shaft for keeping back springs of water.
Tubbing wedges (Min.). Small wooden wedges hammered between the joints of tubbing plates.
Tubing (Min.). The lining of borc-holes with wrought-iron tubes to keep the sides from giving way.
Tuff (Geo.). The finer kinds of volcanic detritus, generally more or less stratified.
Tunnel (Min.). A level put in from the surface.
Turbine (Eng.). A rapidly revolving water-wheel impelled by the pressure of water upon curved blades.
Turnbuckle (Eng.). A tightening swirel.
Turntable (Eng.). A horizontal table revolving on a vertical axis supported by small wheels; used to turn trucks round on.
Turn-out (Min.). A siding or pass-by upon an underground level.
Tut-work (Min.). Breaking ground at so much per foot or fathom.
Tuyeres (Met.). The nozzles through which the blast passes into a furnace.
Two-throw (Min.). When in sinking a depth of about 12 feet has been reached, and the débris has to be raised to the surface by two lifts or throws with the shovel, one man working above another.
Tye (Min.) An inclined table used for dressing ores.
Unconformability (Geo.). When one layer of rock, resting on another layer, does not correspond in its angle of bedding.
Undercast (Min.). An air course carried underneath a waggon way.
Undercut (Min.). To hole.
Underhand stoping (Min.). Working out ground downwards in stopes or steps.
Underlie or Underlay (Min.). The inclination of a lode at right angles to its course.
Underpin (Eng.). To introduce additional support of any kind beneath anything already completed.
Unit (Met.). The unit of metals is 1 per cent. of whatever ton is used. Generally the 20 cwt . ton, equal to 2240 lbs ., is employed, but when dealing with copper ores the 21 cwt . ton of 2352 lbs . is taken ; therefore, the unit equals 22.4 lbs. and 23.52 lbs . respectively.
Upcast (Min.): A shaft through which return air ascends.
Upheaved (Geo.). When a seam or lode has been broken and oue part shifted upwards.

Valve (Eng.). Stops for steam, air, water, \&c., generally used in pipes, e.g., safety, stide, ball or spherical, conical or puppet, clap, clack, flap or door, butterfly, throttle, rotary, snifting, port, double seat or double beat, cup, check valve, \&c.
Vat (Met.). Large wooden tub used for leaching or precipitation.
V-bob (Min.). Fend-off-bob, or Pull-back. A two-limbed bellcrank secured with bridles for connecting with pumping rods over angles in a shaft.
Veins (Geo.). Sheets of mineral matter which have been formed since the rocks in which they occur.
Veinstone (Min.). The non-metallic portion of a vein associated with the ore.
Vernier-scale (Eng.). One scale moving upon another of different graduation, so as to enable one to read intermediate distances.
Vice (Eng.). Bench-vice, Hand-vice. Two strong iron jaws so hinged that they may be opened and closed by a powerful screw and lever.
Viewer (Min.). The general manager or mining engineer of one or more collieries.

Walking beam (Eng.). See Working beam.
Wall (Min.). The face of a stall called the coal wall.
Walling (Min.). The brick or stone lining of shafts.
Walling crib (Min.). Wooden cribs upon which walling is built.
Wallow (Eng.). A water-wheel, \&c., is said to wallow when it does not revolve evenly in its journals.
Wall-plates (Min.). The two longest pieces of timber in a set used in a rectangular shaft.
Wash (Min.). Drift, clay, gravel, \&c., from old river beds, \&c.
Wash-dirt (Min.). That portion of alluvial working in which most of the gold is found.
Washer (Eng.). A flat disc with a round hole in the centre, used around bolts to receive the tightening strain from screw-nuts.
Wash-fault (Min.). A portion of a seam of coal replaced by shale or sandstone.
Waste (Min.). (1.) The more or less empty space between two packs.
(2.) Mullock.

Waste-gate (Eng.). A door for regulating discharge of surplus water.
Waste-weir (Eng.). An orerfall provided along a canal, \&c.,
over which the water may discharge itself in case of becoming toc high. Sometimes called a tumbling bay.
Water cartridge (Min.). When the cartridge containing the explosive is surrounded by another containing water to destroy the flames produced by the shot when fired.
Watercourse. A channel or passage for water.
Watergate (Eng.). See Waste-gate.
Water gauge (Eng.). A tap or float for showing the height of water in boilers, \&c.
Water hammer (Min.). The hammering noise caused by the intermittent escape of gas through water in mines.
Water level (Min.). That level in a mine at which water would remain constant if not drained. This varies slightly in winter and summer.
Water-right (Min.). The privilege of taking a certain quantity of water from a water-course.
Water-shed. The elevated land which divides drainage areas.
Water-wheel (Eng.). Overshot, undershot, breast-wheels. A wheel provided with buckets, which is set in motion by the weight or impact of a stream of water.
Weather (Geo.). To fall down or crumble when exposed to atmospheric agencies, \&c.
Web (Min.). The face of a long wall stall in course of being holed and broken down for removal.
Wedging.crib (Min.). A crib of hollow cast iron upon which tubbing is built up, and to which it is tightly wedged, to stop back all water.
Weigh-bridge (Eng.). A platform large enough to carry a waggon, resting on a series of levers, by means of which heavy bodies are weighed.
Weir (Eng.). A dam over which water flows.
Weld (Eng.). To join two pieces of metal by first softening them by heat, and then hammering them together.
Well (Met.). The well of a furnace is the deepest lying portion or hollow in which the metal collects.
Whim (Min.). A large horizontal drum, supported by suitable framework, round which the rope attached to a bucket in the shaft is fixed. The whole is worked by a horse which walks round it.
Whip (Min.). A post fixed in the ground at an inclination of $45^{\circ}$, its upper end, to which a pulley is attached, overhanging a shaft. A rope with a bucket fixed to one end is passed over the pulley, and is drawn up by a horse moving along a horse-walk.
White damp (Min.). Carbonic oxide.
White tin (Met.). The commercial name for metallic tin.

Winch (Eng.). A strong power machine for hoisting heavy weights by winding a rope round a barrel.
Wind-bore (Eng.). The bottom or suction pipe of a lift of pumps which has suitable brass holes or perforations for suction of water or air.
Windlass (Min.). A long horizontal barrel with hook handles attached at one or both ends; used for winding ropes and weights.
Windmill (Eng.). A horizontal axle with vertical divergent arms and sails for obtaining power from the wind.
Windsail (Min.). The top part of canvas-piping which is used for conveying air down shallow shafts.
Wing-bore (Min.). A side or flank bore-hole.
Wing-dam (Eng.). A projection carried out part way across a shallow river for the temporary diversion of the water.
Winnowing gold (Min.). Air-blowing. Tossing up dry powdered auriferous material in the air, and catching the heavier particles not blown away.
Winze (Min.). A shaft extending from one level to another; but which does not come to the surface.
Wiper (Eng.). See Cam.
Work lead (Met.). Base bullion, silver lead.
Working barrel (Eng.). The pump-tree or cylinder in which the bucket moves up and down.
Working beam (Eng.). A beam having a vertical motion on a rock shaft at its centre, one end being connected with the piston rod and the other with a crank or pump rod, \& $\cdot$.
Worm (Eng.). The so-called endless screw which by revolving without advancing, gives motion to a cog-wheel (wormwheel), the teeth of which catch in the thread of the screw.
Wrench (Eng.). A handle with an eye or $j a w$ at one end, for gripping nuts when screwing them on or off.
Wrought iron (Met.). Iron in its minimum state of carburization.

## INDEX.

ACCELERATOR, 299
Accessory appliances for ore dressing, 264, 295
Accounts, 81, 91
Acids, discovery of blowpipe, 174
Acres required per mile and per hundred feet, table of, 99
Actinolite, 213
Adamite, 213
Adularia, 213
Adulterants of lard, 195
of oils, 194
of tallow, 193
Aerial ropeways, 121
Agalmatolite, 213
Agate, 213
Agitators, 296-7
Aikinite, 213
Air, 186

- sample, 186

Alabandite, 213
Alabaster, 263
Albite, 213
Algebra, 3
Alkali-basalt, 240
Allophane, 213
Alloys, fine gold in, 178

- melting-points of, 108

Almandite, 213
Altaite, 213
Alum, 263
A bath, 299
Aluminite, 213
Aluminium, 254
occurrence of, 254
use of, 254
Alunite, 213
Amalgam, 213
Amazon stone, 213
Amber, 213
——un occurrence of, 263
Amblygonite, 214
Ambrite, 214
Amethyst, 214
Amianthus, 214
Ampère, 111
Amphibole, 214, 242
Amphibolite, 214
Analcime, 214
Analcite, 214
Analysis, blowpipe, 163
158

Anatase, 214
Andalusite, 214
Andesine, 214
Andesite, 240
Andradite, 214
Angles, degrees of comparison with slope, 35
Anglesite, 214
Angular measure, 43
Anhydrite, 214
Annabergite, 214
Anorthite, 214
Anthophyllite, 214
Anthracite, 214
occurrence of, 263
Antimonite, 214
Antimony, 214, 261
——native, 214

- occurrence of, 261
use of, 254
Apatite, 214, 263
Apophyllite, 214
Apothecaries' third measure, 38
weight, 37
Aquamarine, 214
Aqueducts, angle for sides of, and rate of flow, 129
Aragonite, 214
Arastras, 276
Archrean, 238
Arcs, lengths, chords, and heights of, 25
Areas, table of, 41
Areometers, 102
- Balling, 103

Baumé, 102
Beck, 102
Brix, 103

- Cartier's, 102
-Twadde, 103
Argentite, 214
Arithmetic, 1
chemists', 157
Arithmetical method of lode calculation, 74
Arkansite, 214
Arsenic, 214
- occurrence of, 261
use of, 254
Arsenolite, 214
Asbestos, 214
- occurrence of, 263
use of, 263
Ash in fuel, 192

Asphaltum, 214, 261, 263
occurrence of, 263
Assaying, 155, 168-97
Assets, 82, 85
Atacamite, 215
Atmospheric pressure, 126
Atomic weights, 155
Augite, 215
Aurichalcite, 215
Australian hardwood, 154
Autunite, 215
Aventurine, 215
Avoirdupois weight, 36
conversion into per-
centages, 190-1
Axinite, 215
Azurite, 215
B
ABINGTONITE, 215
Balance-sheets, 82
Ball mills, 277
Balling's areometer, 103
Barytes, 215

- occurrence of, 263
- use of, 259-60

Barytocalcite, 215
Basalt, 239-41, 263
Basanite, 215
Batea, 285
Battery stamp, 271-4
Baumé areometer, 103
Bechilite, 215
Beck's areometer, 102
Belting, 126
Belts, 267, 280, 296
Bends, loss of head by, 184
Berdan pan, 276
Beryl, 215
Bieberite, 215
Biotite, 215
Bisilicate slag, 197-8
Bismite, 215
Bismuth, 215, 261
—— occurrence of, 261

- ochre, 215
use of, 254
Bismuthinite, 215
Bitumen, 263
Blake crusher, 268
Blanket table, 286
Blende, 215
Blister copper, gold in, 178
Block mortar, 271
Blödite, 215
Bloodstone, 215
Blower, dry, 292-3
Blowpipe analysis, 163
Blue prints, 302
Boiler, horse power of, 124
Boilers, 124

Bole, 215
Boracite, 215
Borax, 215, 263
Bornite, 215
Boulangerite, 215
Bournonite, 215
Box, mortar, 271

- pointed, 283-4

Brass, fluxes required for soldering, 310
_- weight of, 96
Braunite, 216
Brazing solder, 310
Breakers, 268-9
Breaking load of ropes, 149
Breccias, 242
Bredbergite, 216
Breithauptite, 216
Brick clays, 263
Bricklayers' measurements, 42
Bricks, load of, 42
——rod of, 42

- stock, 42
- Welsh fire, 42

British thermal unit, 125
Brix areometer, 103
Bronzite, 216
Brookite, 216
Brown coal, 216
Brucite, 216
Bryan roller mill, 275-6
Bucket elevators, 295
Buddles, 285, 288
Builders' measurements, 42
Building and decorating stone, 258
Bullion assay, 177-8
Burnishing silver prints, 306
Burrstone, 263
Buss table, 289
Butter's distributor, 297
—ulter, 298

CACHOLONG, 216
Cacoxenite, 216
Cadmium, 254, 261
Cainozoic, 238
Cairngorm, 216
Calamine, 216
Calcite, 216, 242
Calculating rules, 66-74
Calculation of analysis, table of, 158
Caledonite, 216
Calendar, perpetual, 47
Calomel, 216
Cam shaft, 273
Cambrian, 238
Cancrinite, 216
Canvas table, 287
Capacity, measure of, 39

Capital, 83, 86
Carboniferous, 238
Card, job, 89
table, 289
Carnallite, 216
Carnelian, 216
Carpenters' measurements, 42
Carr's disintegrator, 278
Cartier's areometer, 102
Cassiterite, 216
Cats-eye, 216, 231
Celestine, 216
Cells, electro-motive force of, 112
Cement copper, 255
Centrifugal pumps, 296
roller mill, 276
Cerargyrite, 216
Cerite, 216
Cerium, 263
Cerussite, 216
Cervantite, 216
Chabazite, 216
Chain conveyor, 295
Chains, strength and weight of, 152
Chalcanthite, 216
Chalcedony, 216
Chalcocite, 217
Chalcopyrite, 216
Chalcostibite, 217
Challenge feeder, 297
Chalybite, 217
Channels, velocities of discharge in, 141
Charge calculations, 206, 210
Chemistry, 155
Chiastolite, 217
Chilian mill, 275
Chimney, diameter and height of, 126
Chinaman, 296
Chlorite, 217
-_ schist, 243
Chondrodite, 217
Chromite, 217
Chromium, 261

- occurrence of, 261
use of, 254
Chrysoberyl, 217, 231
Chrysocolla, 217
Chrysolite, 217
Chrysoprase, 213, 234
Cinnabar, 217
Circles, 6
Circular rings, 6
Circumferences, table of, 11
Circumferential velocities, 116
Classification of rocks, 238-43
of slags, 197, 203
Classifiers, 282, 284
Clausthalite, 217
Clay, 259, 263

Clayslate, 242
Clearing bath, 303
Clinochlore, 217
Clinoclasite, 217
Coal, 217

- occurrence of, 263

Cobalt, 261
—— glance, 217
— occurrence of, 261
use of, 255
Cobaltite, 217
Cobbing hammer, 270
Code, the Morse, 76
Collyrite, 217
Colour indicating temperature, 107
Colours, 259, 284
Columbite, 217
Column of mercury, 104
——of water, 104
Company reports, 81
Compass, points of the, 76
Compound interest, table of, 53
Concentration of ores, 284-95
Cone, 7

- mill, 278

Conglomerate, 242
Contour of section, 139
Conveyors, 295-6
Copiapite, 217
Copper, 217, 255
—— assay of, 180
—— electro-plating, 110
_ flux for soldering, 310
—— glance, 217

- nickel, 217
- occurrence of, 261
- precipitation, 193
—— pyrites, 217
use of, 255
- vitriol, 217. See Pisanite.
weight of, 96
Coquimbite, 217
Cordierite, 217
Cornet, 178
Corrections for the Press, 92
Corundum, 218
Cosecant, 30
Cosines, 28
Costs, 81-91
Cotangents, 31
Coulomb, 111
Countess slates, sizes of, 43
Covellite, 218
Co-versed sines, 30
Cradle, 287
Creeper chain conveyor, 295
Cretaceous, 238
Crocoisite, 218
Crucible steel rope, 149
Crushing ores, 268-70
Cryolite, 218

Crystalline system, 209
Cabes, 6

- table of, 11

Cubic measure, 41
Cumulative preference shares, 85
Cupellation, 177
Cuprite, 218
Current, electrical, 110
Curves, railway, 104
Cuttings, area of cross sections, 100
Cyanide solutions, 187-8
Cyanite, 218
Cylinders, 7

DANBURITE, 218 Datolite, 218
Decorating stone, 258
Decrepitation, 267
Dehne's filter, 297
Deposits, ore, 261
Depreciation, 83-4
Descloizite, 218
Desiccation, 267
Desmine, 218
Developers, 303
Development redemption, 83
Devonian, 238
Diallage, 218
Dialogite, 218
Diamond, 231

- use of, 261

Diaspore, 218
Dichroite, 218
Diopside, 218
Dioptase, 218
Diorite, 239-41
Disc feeder, 297

- mill, 278
- stamp, 274

Discharge of canals, etc., Eytelwine's rule, 141

- to determine, 130
- through an orifice in a thin plate, 131
- of outlet pipes, table of, 147
- of pipes by Prony's method, table of, 136
—— by short tubes, 132-3
———of tubes, 133-4 velocity of, in channels, etc., 129, 142
Dish, 285
Disintegrators, 278
Dislocated reef, rule for determining direction of, 252-3
Disthene, 218
Distributors, 297
Dodge breaker, 268
Dolerite, 239-41

Dollying, 271
Dolomite, 218
Doubles, slates, sizes of, 43
Drag mill, 276
Draining belt, 267, 296
Drawing, mechanical, 299
Drawing paper.measurements of,4
Dressing ore, 264-98
Drier, rotary, 267
Dry blower, 292-3

- bulb thermometer, 212
- measure, 38

Duchesses, slates, sizes of, 43
Dufrenite, 218
Dufrenoysite, 218
Dunite, 218
Durangite, 218
Dutch clinkers, measurements of 42
Dydmium, 263
Dynamics, 116
Dyscrasite, 218

EDGE-RUNNER, 275
Efflux, velocity of, 130
Elaterite, 218
Electrical units, 111
Electrolysis, in assaying, 180
Electro-motive force of various cells, 112
Electro-plating, 110
Electrum, 218
Elements, table of, 155
Elevators, 295-6
Embankments, area of cross section, 100
Emerald, 218, 231-2
Emery, 263
Emplectite, 218
Enamels, 259
End percussion table, 286

- shaking table, 289

Endless belts, 296
Engine, horse-power of, 123
Enstatite, 219
Epidote, 219
Epistilbite, 219
Epsomite, 219
Equivalent rates, table of, 51
Erubescite, 219
Eruptive rocks, 239-41
Erythrite, 219
Euchroite, 219
Euclase, 219
Eudialyte, 219
Eulytite, 219
Euxenite, 219
Examination, mine, 248-52
Examinations, characteristic blowpipe, 166

FAHLERZ, 219 Fahlunite, 219
Falling bodies, 118
Farad, 111
Fussaite, 219
Faults: rules of dislocation, 252-3
Fayalite, 219
Feeders, 297
Felspar, 219, 242
Fergusonite, 219
Fibrolite, 219
Fichtelite, 219
Fillet, 178
Filter-pressing, 297-8
Filters, 267, 297-8
Fingers, battery, 274
Fireclay, 263
Fire-resisting substances, 259
Fixing bath, 303, 305
Flat ropes, 150
Flight conveyor, 296
Flint, 220
Flotation, 293
Fluorite, 220
Fluorspar, 220
Fluxes for soldering or welding, 310
Fogging, 304
Food and medicine, 260
Foot of bricks, 42
Formations, geological, 238
Fossil fuels, 260
Fowlerite, 220
Franklinite, 220
Freibergite, 220
French metrical weights and measurements, 44
Friction of long pipes, 132

- of water channels, head to overcome, 140
Frigorific mixtures, 109
Frilling, 304
Frue vanner, 290
Fuchsite, 220
Fuel, 125
- assay of, 191
- evaporative powers of various. 125
- fossil, 260
- heat in, 192

Fuller's earth, 263
Fusibility, scale of, 209

$G$ABBRO, 239-41
Gadolinite, 220
Gahnite, 220
Galena, 220
Garnet, 220, 233
Gases and vapours, specific heats of, 107

Gaylussite, 220
Gems, table of characteristics, 231
General laws for pipes, 139
Genthite, 220
Geological formations, 238
Geology and mineralogy, 213-35
Geometrical method, lode calculation, 74
Geometry; 6
Gersdorffite, 220
Geyserite, 220
Gibbsite, 220
Gilpin County concentrator, 289
Gismondite, 220
Glaubasalt, 220
Glauberite, 220
Glazes, 259
Glossary, 311
Gneiss, 243
Goethite, 220
Gold, 220, 265

- alloys, value of, 179
-_ assay of, 175-9
- electro-plating, 110
- occurrence of, 261
—— solder, 310
use of, 255
Goslarite, 220
Granite, 239-41
Graphite, 220
- occurrence of, 263
- use of, 260

Gravity, specific, table of comparison, 102
—— stamps, 271-4
Greasiness of minerals, 266
Greenockite, 220
Griffin roller mill, 276
Grinding machinery, 275-8

- material, 259
pans, 276-7
Grizzlies, 281-2
Grossularite, 220
Guano, 263
Guides, stamps, 272
Gun-metal, weight of, 96
Gypsum, 220
occurrence of, 263
use of, 261

HAIDINGERITE, 221
Half-slags, 200-1
Halite, 221
Halloysite, 221
Hammers, 270-1
Handcock jig, 292
Hard water, 193
Hardness, scale of, 213
Harmotome, 221
Hartz jig, 291

Hauerite, 221
Haüynite, 221
Hausmannite, 221
Head, loss of, by bends, 134

- to overcome friction of water channels, 140
- for low velocities, 141
—— for very low velocities, 141
- stamp, 274

Heat, 105

- electrical, 111
- in fuel, 192

Heating powers, theoretical, 108
Heavy spar, 221
Height of discharge, 272-3
Heliotrope, 221
Helvite, 221
Hematite, 221
Hemp ropes, 149
Hendry's challenge feeder, 297
Hessite, 221
Heulandite, 221
Hornblende, 221

- schist, 243

Hornsilver, 221
Hornstone, 221
Horse, work of a, 123
Horse-power, 123
126
a belt will transmit, of boiler, 124
of engine, 123
Huantajayite, 221
Hübnerite, 221
Humidity, 212
Humite, 221
Huntingdon mill, 276
Hyacinth, 221, 232
Hyalite, 221
Hyalophane, 221
Hyalosiderite; 221
Hydraulic classifier, 283
elevator, 296
Hydraulics, 128
Hydrocarbon, 191
Hydromagnesite, 221
Hydrozincite, 221
Hypabyssal rocks, 240
Hypersthene, 221

IDOCRASE, 221
Idrialite, 221
Igneous rocks, 239-42
Ilmenite, 222
Ilvaite, 222
Improved crucible steel ropes, 149
Impurities in mine waters, tests for, 193

Incline bed, to calculate true thickness, 253

- measure, table of, 35

Inclined plane, 295
Inclines, self-acting, 119-20
Income table, 52
Inertia, moment of, 148
Infusorial earth, 260, 263
Interest table, compound, 53
Iodide method, copper assay, 180
Ioaine, 263
Iolite, 222
Iridium, 222, 255

- occurrence of, 262
use of 255
Iridosmine, 222
Iron, 256
- fluxes for soldering and welding, 310
- occurrence of, 262
- ropes, 149
- solder, 310
- use of, 256

JAMESONITE, 222
Jarring riddles, 282
Jasper, 222
Jaw-breakers, 268
Jeffersonite, 222
Jigs, 290-3
Job card, 89
Joull, 111
Jurassic, 238
KAINITE, 222
Kaluszite, 222
Kaolin, 263
Kaolinite, 222
Keeve, 287
Kermesite, 222
Kieserite, 222
Kilns, 267
Knots and splices, 77-81
Krupp ball mill, 277

LABRADORITE, 222
Labyrinth, 283
Ladies' slates, sizes of, 43
Lamprophyre, 240
Lanarkite, 222
Lanthanite, 222
Lapis lazuli, 222
Lard, adulterants of, 195
Lazulite, 222
Lead, 256
-_ assay of, 181-3
-_ flux for soldering, 310
——— occurrence of, 262
——_solders, 310

Lead, use of, 256
_weight of, 96
Leadhillite, 222
Lense, 302
Lepidolite, 222
Lepidomelane, 222
Leucite, 222
Leucophanite, 222
Leucopyrite, 222
Liabilities, 82, 85
Libethenite, 222
Lievrite, 222
Life, mine, 82
Light producers, 260
Lignite, 263
Limburgite, 239
Limestone, calcareous, 243

- crystalline, 243

Limonite, 222
Linarite, 223
Linseed oil, 194
Liquid measure, 38
Liquids heavier than water, 102
-lighter than water, 103
Liroconite, 223
Lithomarge, 223
Load of timber, 42
Lode values, 74-5
Log washer, 279
Logarithms of numbers, table of, 8
Long measure, 40
Löweite, 223
Lubricants, 124
Luhrig table, 289
Lydianstone, 223
M
AGNESIAN limestone, 243
Magnesite, 223
use of, 260
Magnetic concentrators, 294
Magnetite, 223
Malachite, 223
Man, work of, 122
Manganese, 256

- occurrence of, 262
use of, 256
Manganite, 223
Manures, mineral, 259
Marble, 223
Marcasite, 223
Marchioness slates, sizes of, 43
Margarite, 223
Mascagnite, 223
Materials, strength of, 147
Matte, converting, 205
Measures, 36 apothecaries' fluid, 38
bricklayers', 42
British Imperial, 39
builders', 42

Measures, carpenters', 42

- cubic, 41
- dry, 38
——French system of, 44
long, 40
—— of angles, 43
———of drawing paper, 43
—— of paper, 43
of timber, 42
old diggers', 38
solid, 41
- square, 41 surface, 41
Mechanical drawing, 299 sieves, 281
Meerschaum, 223
occurrence of, 263
Meionite, 223
Melanite, 223
Melanterite, 223
Melilite, 223
Mellite, 223
Melting-point of easily fusible alloys, 108
Menaccanite, 223
Mendipite, 223
Mensuration, 7
Mercury, 256
— occurrence of, 256, 262
- use of, 256
transformation of
columns of, into columns of water, 104
Merrill's filter, 298
Mesitite, 223
Mesolite, 223
Mesotype, 223
Mesozoic, 238
Metals, weight per square foot, 96
Metamorphic rocks, 243
Metric system, weights and measures, 44
Miargyrite, 223
Mica, occurrence of, 242, 263
- use of, 260
- schist, 243

Microcline, 223
Microfarad, 111
Millerite, 223
Mine examination, 248-52

- salting, 244
- sampling, 243-8
waters, tests for impurities, 193
Mineral manures, 259
Mineralogy and geology, 213-43
Minerals, list of, 213
Minium separation process, 293
Minium, 223
Mint value of gold in alloys, 179
Miocene, 238

Mirabilite, 224
Mispickel, 224
Mixtures, frigorific, 109
Molybdenite, 224
Molybdenum, 256, 262
Moment of inertia, 148
——of resistance, 148
Monarch magnetic separator, 294
Monazite, 224
Money, conversion of American into English, 48
Monosilicate slag, 197-8
Monticellite, 224
Morenosite, 224
More's filter, 298
Morse code, 76
Mortar block, 271

- box, 271

Mosandrite, 224
Motors, 119-20

- animal, 122-3
——self-acting inclined, 119-20
-- steam-engine, 123
Mounting solution for photos, 305
Mud-wheel, 279

NAGYAGITE 224
Naphtha, 224
Natrolite, 224
Naumannite, 224
Nepheline, 224
Nephelite, 224
Nephrite, 224
Niccolite, 224
Nickel, 256
—— occurrence of, 256, 262
use of, 256
Nicking board, 297
Niobite, 224
Nitre, 224

- occurrence of, 263

Nominal capital, 86
Normal solution, 156
Nosean, 224

0
CTAHEDRITE, 224 Ohm, 111
Oil, adulterants of, 194

- physical properties of, 197

Oligocene, 238
Oligoclase, 224
Olivenite, 224
Olivine, 224, 242
Onyx, 224
Opal, 224-5
Open channels, head due to velocity in, 139, 142
Ore blocked out, 247

- deposits, 261

Ore dressing, 264-98
Ornamental and precious stones, 259
Orpiment, 224
Orthite, 225
Orthoclase, 225
Osmium, 257
Outlet-pipes, table of discharge of, 136
Ouvarovite, 224
Overflow-pipe, 146
Oxygen ratio, 199
Ozocerite, 225

PAID shares, 86
Palæozoic, 238
Palladium, 257, 262
Pans, 267, 276-7
Paper, 43

- measurements, 43

Parabola, 7
Paraboloid, 7
Paragonite, 225
Parallelogram, 6
Parting, 176
Pectolite, 225
Percentage composition, calculation of, 157
Percentages, conversion intoavoirdupois weight, 190-1

- conversion into Troy weight, 178
Percussion tables, 286, 288
Percussive machinery, 270-5
Periclase, 225
Pericline, 225
Peridot, 225
Peridotite, 239-41
Permian, 238
Perofskite, 225
Perpendicular, an underlie table of, 34
Perpetual calendar, 47
Petalite, 225
Petroleum, occurrence of, 264
use of, 264
Petrology, 238-43
Pewter solder, 310
Pharmacolite, 225
Pharmacosiderite, 225
Phenacite, 225
Phillipsite, 225
Phonolite, 225, 240
Phosgenite, 225
Phosphorite, 225
Photography, hints on, 302
Phyllite, 242
Physical properties of oil, 197
Pianzite, 225
Picking belt, 280

Pimelite, 225
Pin-holes, 304
Pipe distributors, 297
Pipes, cast-iron, proportion and weights of, 94

- common overflow, 146
-_ general laws for, 139
long, friction of, 132
146
square and rectangular, 1
strength of, 147
table of discharge of, by Prony's method, 136
weight of water contained in, 93
Pisanite, 225
Pistazite, 225
Pitchblende, 225
Pitchstone, 241
Plagionite, 225
Plane, inclined, 295
Planimeter, in lode calculation, 75
Platiniridium, 225
Platinotype, 306
Platinum, 257
- occurrence of, 262
- use of, 257

Plattnerite, 226
Pleistocene, 238
Pleonaste, 226, 232
Pliocene, 238
Plumbago, occurrence of, 262
use of, 257
Plutonic rocks, 240
Pneumatic classifiers, 284

- concentrators, 292

Pointed box, 283-4
Points of the compass, 76
Poisons, antidotes and remedies for, 306
Polianite, 226
Polishing material, 259
Pollucite, 226
Polybasite, 226
Polycrase, 226
Polygons, 6
Polyhalite, 226
Porphyrite, 240
Post-Tertiary, 238
Pot assay, 176
Potassium, use of, 257
Power, 43

- electrical, 111
- measurement of, 43
of, 126
Powers, table of, 11
Prase, 226
Praseolite, 226
Precious stones, 259, 264
Preference shares, 85
Prehnite, 226

Pressure against walls, 115

- filters, 297-8

Primary rocks, 239-42
Princess slates, sizes of, 43
Printing plates, 304
Prism, 7
Prismoidal method, lode calculation, 75
Prismoids, 7
Profit and loss accounts, 87
Proustite, 226
Psilomelane, 226
Pucherite, 226
Puddler, 279
Pulley, speeding of, 128
Pulsating machinery, 290-2
Pump-rods, sizes and proportions. for, 98
Pumps, centrifugal, 296
Pund, 296
Purple copper ore, 261
Push conveyor, 296
Pyramid, 7
Pyrargyrite, 226
Pyrites, 226
Pyro solution, 303
Pyrochlore, 226
Pyrolusite, 226
Pyromorphite, 226
Pyrope, 226, 233
Pyrophillite, 226
Pyroxene, 226, 242
Pyrrhotite, 226
$Q^{2}$
UARTATION, 176
Quartz, 226, 234, 242
Quartzite, 243
Quartz-porphyry, 239-41
Quaternary, 238
D AFF wheel, 295
Ragging hammer, 270
Ragging for jigs, 291
Rails, height of outer, in curves, 104
_-size and weight of, 104
Rammelsbergite, 227
Rate per lb., cwt., and ton, 51
Realgar, 227
Redemption, development, 83
Reduction of ores, 267-78
Reef, dislocated, rule for determining direction of, 252-3
Refractory substances, 259
Report, company, 81
on a mineral property, 248-52
Requisition form, 89
Reserve fund, 84
Resistance, electrical, 111

- moment of, 148

Restrainer, 303
Retinite, 227.
Revenue accounts, 87
Revolving buddle, 288
table, 280
Rhodochrosite, 227
Rhyolite, 239-40
Riddles, 282
Ridgway filter, 298
Ripidolite, 227
Rittinger's side percussion table, 288
Rivers, velocity of discharge in, 141
Roasting assay, 176
Rocker, 287
Rocks, classification of, 238-43
Rocksalt, 227
Rod of brickwork, 42
Roller feeder, 297

- mill, 275-6

Rolls, 269
Roots, table of, 11
Ropes, 149
——crucible steel, 149

- flat, 150
- hemp, weight of, 149
—— improved crucible steel, 149 iron, 149
- knots and splices, 77-81
—— manilla, weight of, 151
- round, 149
——taper, 150
Roselite, 227
Rotary driers, 267
Round buddles, 285
Ruby, 227, 231
Rutile, 227

CAFETY valve, 125
Salammoniac, 227
Salt, 260
-use of, 260
Salting a mine, 244
Saltpetre, occurrence of, 261
_use of, 261
Samarskite, 227
Sampling, 243-8
Sand, 260
-use of, 260
Sand pump, 296
Sandstone, 242, 258
Sanidin, 227
Sapphire, 227, 231
Sarcolite, 227
Sartorite, 227
Sassolite, 227
Satinspar, 227
Scales of maps, 300
Scapolite, 227
Scheelite, 227

Schiller spar, 227
Schist, 243
Schranz mill, 275
Scolecite, 227
Scorification, 175
Scorodite, 227
Scraper conveyor, 296
Screens, 98, 189, 272, 281
Screw conveyor, 296
Secant, 4
Section, effect of contour of, 139
Sectors, 7
Sedimentary rocks, 242
Segments, 7
Selenite, 227
Self-acting inclined motors, 119-20
Senarmontite, 227
Separation, minerals, process, 293

- of ores, 278-80

Sepiolite, 227
Serpentine, 227, 243
Sesquisilicate, slag, 197-8
Settling tank, 283
Shafting, 273
Shaking feeder, 297
Shales, 242
——bituminous, 263
Shares, 85-6
Shoe, stamp, 274
Shovel, vanning, 285
Side percussion table, 288
Siderite, 228
Sieves, 281-2
Sillimanite, 228
Silurian, 238
Silver, 228, 257
_- assay of, 175
-- electro-plating, 110

- glance, 228
- native, 228
- occurrence of, 262
—— solder, 310
—— spitting of, 177
- use of, 257

Sines, table of, 28
Sinking, to calculate expense of, 254
Site, mill, 265
Sizing ore, 280-2

- tests, 189

Slags, 184, 195-208
——assay of, 184

- bases, 204
-- calculations, 197, 206, 208
- characteristics, 197-9

Slates, sizes of, 43
Slide rules, 66-74
Slope, comparison of, with angle, 35
Sluices, 278, 286, 296
Smaltine, 228
Smithsonite, 228

Sodalite, 228
Sodium, 257

- occurrence of, 257, 262
use of, 257
Soft water, 193
Soft wood timber, 153
Soldering fluxes, 310
Solders, 310
Solid measure, 41
Solutions, standard, 180, 182-3
-testing cyanide, 187
Sorting ore, 279
Spalting hammer, 270
Specific heat (gases and vapours), 107
Suravity, 102, 213-37, 266
Specular iron, 221
Speeding of machinery, 128
- of pulleys, 128
- of wheels, 128

Spessartite, 228
Sphene, 228
Sphere, 7
Spherical segments, 7
Spinel, 228, 232
Spiral sieves, 282
Spitting of silver, 177
Spitzlutten, 283
Splices and knots, 77-81
Spodumene, 228
Square measure, 41
Squares, table of, 11
Stalls, 267
Stamp-hangers, 274
Stamps, gravity, 271-4

- steam, 274

Standard screens, 189

- solutions, 180, 182-3

Standardizing lode values, 244

- sump solutions, 188

Stannite, 228
Statics, 115
Staurolite, 114
Steam boilers, 124
—_ engine, 123
-_ stamp, 274
Steatite, 228
Steel solder, 310

- weight of, 96

Stem of stamp, 274
Step sluices, 278
Stephanite, 228
Stilbite, 228
Stilpnomelane, 228
Stock bricks, measurements of, 42
Stolzite, 228
Stoping, width of, 74
Stores-book, 88-9
Streams, velocity of water in, 128
Strength of materials, 147
Stromeyerite, 228

Strontianite, 228
Strontium, 257

- occurrence of, 257, 262
use of, 257
Submerged openings, 140
Subsilicate slag, 197, 201
Succinite, 228
Sulphur, 228, 260
—— native, 228
——occurrence of, 228, 260
- use of, 260

Sump solutions, 188
Surcharge in assaying, 177
Surface measure, 41
Sweeping table, 287
Syenite, 239-41
Sylvanite, 228
Sylvite, 228
Syngenite, 228

TABLES, concentrating, 280,286-9 Tachydrite, 228
Tachylite, 239
Talc, 228, 260, 264
——schist, 243, 264
Tallow, adulterants of, 196
Tangents, table of, 28
Tanks, settling, 283
Tantalite, 229
Taper ropes, 150
Tappet, 274
Tellurium, 257
——occurrence of, 257, 262 use of, 257
Temperatures, high, 107
Tennantite, 229
Tenorite, 229
Terms used in prospecting, mining, metallurgy, etc., glossary of, 311
Tertiary formation, 238
Tetradymite, 229
Thenardite, 229
Theoretical discharge of water by round tubes, table of, 130
Thermal units, British, 125
Thermometers, comparison of, 105
dry and wet bulbs, 212
Thomsonite, 229
Thorite, 229
Tile ore, 229
Tilt hammer, 271
Timber, soft wood, 153

- Australian hard wood, 154 measure, 42
Time checks, 89
Tin, 258
_- assay of, 184
- occurrence of, 258, 262
—— solders, 310

Tin, use of, 257
Tinkal, 229
Tinned iron, fluxes required for soldering, 310
Tippler, 295
Titanic iron, see Iron
Titanite, 229
Titanium, 258

- occurrence of, 258
- use of, 258

Toning bath, 305
Topaz, 229, 232
Torbernite, 229
Tossing tub, 287
Touchstone, 229
Tourmaline, 229, 234
Toxicology, 306
Trachyte, 239-40
Tracing, 301
Transmission of power, 126
Trapeziums, 6
Trapezoids, 6
Tremolite, 229
Triangles, 6
Triassic, 238
Tridymite, 229
Trigonometry, 4
Triphylite, 229
Triplite, 229
Tripolite, 229
Trisilicate, slag, 197, 199
Trommels, 279, 282
Trona, 229
Trough, 278, 283
Troy weight, conversion of, into percentages, 178
Tub, tossing, 287
Tube mill, 277-8
Tubular hydraulic classifier, 283
Tungsten, 257

- occurrence of, 257, 263
——use of, 257
Tungstite, 229
Turgite, 229
Turquoise, 229, 235
Twaddle's areometer, 103
Tye, 286

ULLMANNITE, 229
Underlie, table of, 34
Uraninite, 229
Uranite, 229
Uranium, 258, 263
Uranochalcite, 229

VACUUM filters, 297-8
Valentinite, 230
Vanadinite, 230
Vanadium, 258

Vanners, 290
Vanning shovel, 290
Vapours, specific heat of, 107
Vaquelinite, 230
Velocity of efflux, rule for determining, 130

- at circumference, 116
- of currents close to bed of a stream, 128
—— head for, 141
- to find, of watercourses, 141
- of water in channels of earth, 129
- in open channels, head due to, 144
-     - table of, in watercourses, 143
Versed sines, 30
Vesuvianite, 230
Viscountess slates, 43
Vivianite, 230
Volatile bydrocarbons, 191
Volborthite, 230
Volcanic rocks, 240
Volt, 111

W AD, 230 Wages table, 57
Wagnerite, 230
Walls, pressure against, 115
Wash trommels, 279
Washer, log, 279
Water, analysis of, 185 evaporation of, 124
——— feeders, 297
—— hard and soft. 193

- pipes, table for bends in, 134
quantity of, for given depths of rainfall, 116
- transformation of columns of, into columns of mercury, 104
- velocities of, in channels in earth, table of, 129
- weight of, in pipes, 93

Watercourse, to find fall of, 141
— to find velocity of, 141 140
Watt, 111
Wavellite, 230
Weathering, 267-8
Wedge, 7
Weights and measures, 36,42

- apothecaries', 37-8
—— avoirdupois, 36
$\longrightarrow$ metric, 44
- of substance to yield a given weight of substance, 157

Weights, old diggers', 38

- troy, 37

Weirs, 146
Welding fluxes, 310
Welsh fire-bricks, 42
Wenstrom magnetic separator, 294
Wet bulb thermometer, 212
Wetherill magnetic separator, 429
Wheel, mud, 279
——raff, 295
Wheels, speeding of, 128
Whetting material, 259
White metal, weight of, 96
Wilfley table, 289
Willoughby jig, 292
Wind, velocity and pressure of, 114
Wire, weight of, 95
Witherite, 230
Woehlerite, 230
Wolfram, 230, 258

- occurrence of, 258
use of, 258 ;
Tungsten
Wollastonite, 230
Work of horse, 123
-- of man, 122
Working cost, 84

Wrought iron, weight of, 96
Wulfenite, 230
Wurtzite, 230
X ANTHOPHYLLITE, 230
$\Lambda$ Xanthosiderite, 230
Xenotime, 230
Yttrocerite, 230
Yttrotantalite, 230
Yttrotitanite, 230
Yaratite, 230
Zimmermann's rules for faults, 252-3
Zinc, $2 \overline{5} 8$

- assay of, 183-4
-- fluxes for soldering, 310
-_ occurrence of, 263
see -use of, 258
_ weight of, 96
Zincite, 230
Zircon, 230
Zoisite, 230
Zwieselite, 230

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