



TECHNICAL REPORT

A PRACTICAL METHOD OF PREDICTING
SEA ICE FORMATION AND GROWTH

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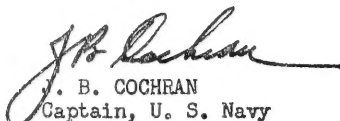
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ABSTRACT

A technique for predicting ice formation and growth is presented. The ice potential calculations originally discussed by Zubov and Defant form part of the method, as do the standard heat budget equations developed by various authors. In addition, new formulas are derived for computing ice growth in terms of known or predicted oceanographic and meteorological data. The method is applied to the problem of predicting the general features of the ice distribution in the Baffin Bay-Davis Strait area for the season 1952-53. It is pointed out that use of this method must be limited to open-sea areas where winter and not polar ice is the dominating feature. However, the technique has important applications to estimating the general ice features of such areas several months in advance.

FOREWORD

The increasing importance of defense installations in northern areas has increased greatly the responsibilities of the U. S. Navy in supplying bases in Arctic waters, where sea ice is often an operating obstacle. The Hydrographic Office is charged with the responsibility of developing and testing techniques for observing and forecasting sea ice conditions. Standardized techniques for observing, charting, and reporting sea ice are now in operational use by the Navy, as described in publications issued by the Hydrographic Office. Heretofore, techniques for forecasting the formation, growth, and movement of sea ice have not been published by this Office. This publication describes a method of long-range forecasting of ice formation and growth. Since this technique is still in the developmental stage, the Hydrographic Office welcomes comments as to its operational value.


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A. INTRODUCTION

The expanding program of ice observation and forecasting at the Hydrographic Office has emphasized the desirability of long-range ice forecasting. There are many phases of the ice program for which long range forecasts giving advance estimates of ice conditions of as much as 150 days are required. This paper deals with long-range forecasting of ice thickness in open seas whose salinity and density remain relatively constant, such as Baffin Bay and the Labrador Sea.

An operational method of forecasting for a long period must be easy to use, require a minimum number of involved calculations, and yield forecasts of reasonable accuracy. Most formulas previously developed have been complicated expressions which are not suited for operational use. In developing the following method, the goal has been to perfect a technique from which quantitative results can be derived with a minimum of computation and observation.

B. THE ICE POTENTIAL OF A WATER COLUMN

The severity of an ice season depends, among other things, upon the amount of thermal energy stored in the water mass and upon the rate at which convective mixing takes place. It is necessary to select a model of convective mixing which will explain the variation in the thermohaline conditions caused by heat removal and ice accretion. The method proposed by Defant (1949) and by Zubov (1938) of computing the ice potential and potential heat loss has been adopted as a basis for the present forecasting technique.

Before a forecast can be made, an analysis of the properties that inhibit ice formation and growth must be performed. Oceanographic measurements within the area in question must be secured in order to obtain information about salinity and thermal energy stored within the water mass. Unnecessary computation can be avoided by making the measurements at a time after the heat flux reverses, when thermal energy is being continually removed from the water. Otherwise the amount of heat which was added to the water column prior to the reversal of the heat flux would have to be computed before the method of Defant and Zubov could be utilized.

Establishing the ice potential of a given water column requires only the temperature and salinity at N levels within the column. The column is divided into $(N-1)$ layers and the mean temperature (\bar{T}_n), salinity (\bar{S}_n), and density ($\bar{\sigma}_n$), are computed for each layer. The mixing model, as defined by the method of Defant and Zubov is constructed by finding the mean temperature and salinity of the surface and second layers, i.e.,

$$\frac{\bar{S}_1 + \bar{S}_2}{2} = \bar{S}_{1,2} \quad , \quad \frac{\bar{T}_1 + \bar{T}_2}{2} = \bar{T}_{1,2} .$$

The column is then said to be partially mixed down to the second level. Complete mixing is achieved by cooling the partially mixed column until its density, $\sigma_{1,2}$, equals that of the original second layer, σ_2 . This mixing may be accomplished merely by changing the temperature of the partially mixed column, provided the water is not cooled below its freezing point. If the temperature change necessary for completely mixing the column requires a temperature below the freezing point, ice will form and the salinity of the remaining water in the column will be increased. The mixing process is carried out layer by layer until the potential heat loss is greater than the possible heat loss for a given ice season.

For convenience the expressions "partially mixed" and "completely mixed" have been used in connection with the ice potential computations. Two layers of water are termed "partially mixed" when the mixed column is defined completely by the means of the temperatures and salinities of the two original layers (i.e., no heat loss is involved). A "partially mixed" layer becomes "completely mixed" when the density of the partially mixed layer equals that of the original lower layer, with the density of the original lower layer remaining fixed throughout the process. In this latter case a heat loss is necessary, provided that the density distribution is stable. Temperature and salinity changes which result from this mixing model can be easily read from a T-S nomograph, or can be computed by use of standard hydrographic tables. (H.O. Pub. No. 615)

Complete mixing can be accomplished only by releasing q_m gram calories of sensible heat from the water column one square cm in cross section. Quantitatively, $q_T(h) = c \rho_w h \Delta T_w$ where c is the specific heat of sea water ρ_w is the density of sea water, h is the depth to which complete mixing reaches (or volume of $h \text{ cm}^3$), and ΔT_w is the amount of heat lost in changing the partially mixed column to a completely mixed column. When it is necessary to change the salinity of the column in order to achieve complete mixing, latent heat is involved in the process as well as sensible heat. Since a known percentage of the salt is frozen out of the ice, it is possible to write an expression for the latent heat as a function of the salinity change. Consequently, the ice accretion corresponding to a given salinity change can be expressed mathematically. As written by Defant, the ice thickness is given by

$$\xi_i = \frac{h \Delta S}{C \rho_w b S} \quad (1)$$

where S is the salinity of the partially mixed column and b is the percentage of the salts frozen out of the ice. The latent heat can now be evaluated from the well-known formula $q_\xi(Z) = K \xi(Z)$, where K is the latent heat of fusion, which decreases with increasing salinity of the ice. The total potential latent heat is given by

$$\int_0^h q_\xi dz = Q_l(h) \quad (2)$$

As the mixing model is developed, each layer will yield a certain amount of potential heat loss, q_T , and eventually, when the temperatures are low and the densities are high, each layer will yield a certain mass of potential ice (ξ) associated with convective mixing down through the corresponding layer. Thus it is possible to construct the very useful "potential curve" (Figure 2) from corresponding

$$\int_0^h \xi dz = I_i(h) \quad \text{and} \quad Q_T(h) = \tilde{Q}_T(h) - Q_0, \quad \text{where} \quad \tilde{Q}_T = \int_0^h q_T dz. \quad (3)$$

The potential curve is plotted, Q_T starting from zero within the layer where ice first appears. The remainder of the $\tilde{Q}_T - Q_0$, which is lost before ice is formed, determines the date of ice formation. The reason for taking Q_T as zero at this point becomes evident when one considers the lower limits of the integrals in equation (13). Obviously some question arises as to the exact quantity of heat that has been removed at the time ice is first formed. There is, of course, some error introduced, but it is not large as long as the water temperatures are near the freezing point and the water column is divided into layers of sufficiently small depth, for example five to ten meters. Recent work on the same type of model as Defant's has yielded exact values of the Q_T which must be removed before ice is formed, thus determining the proper point to start accumulating the Q_T for the potential curve (Brown, 1954).

In order to illustrate the computation of the ice potential and the drawing of the potential curve, a typical oceanographic station is used as an illustration. Station 37, at 66°N, 58°W, was occupied on 3 October 1952. A plot of the oceanographic variables at this station is given in Figure 1, and the complete numerical data are shown in Table 1.

TABLE 1
Oceanographic Data for Station #37
(66°N, 58°W), 3 October 1952

Depth m.	Temperature °C.	Salinity o/oo	Density Anomaly (σ_t) gm/liter
0	0.56	32.37	25.98
5	0.10	32.36	26.00
10	0.61	32.39	25.99
20	0.73	32.47	26.05
30	-0.41	32.78	26.36
50	-1.65	33.08	26.64
75	-1.61	33.69	27.13
99	-2.13	33.69	27.14
148	-0.52	34.04	27.38
197	1.52	34.21	27.40
296	0.08	34.34	27.59
394	-1.71	34.52	27.81

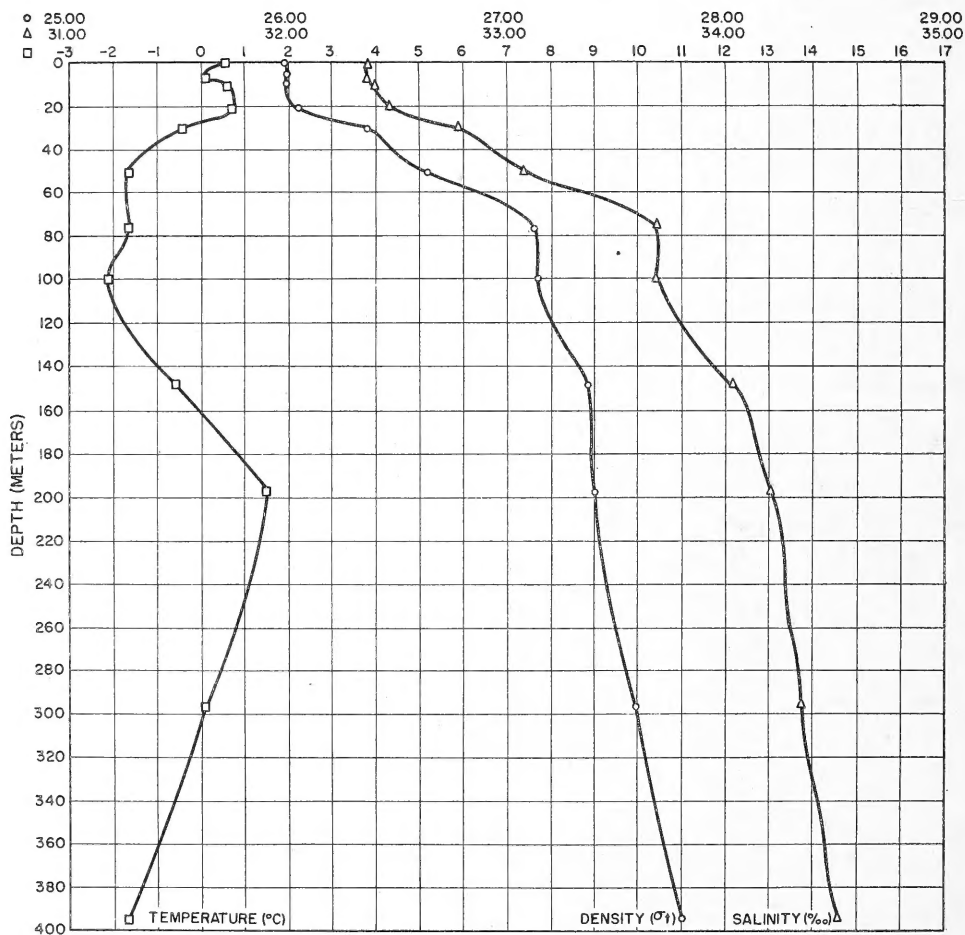


FIG. 1 OCEANOGRAPHIC PLOT FOR STATION NO. 37, 66°N 58°W, 3 OCTOBER 1952.

From these data the ice potential has been calculated by the method of Defant and the results shown in Table 2A. Finally, the ice potential curve for Station 37 is shown in Figure 2. It will be noted that the ice potential curve is by no means a straight line or a smooth curve. In fact, for this station, the heat loss necessary to form a given amount of ice varies considerably. For this reason, the actual forecasting for this station is difficult, for a small additional heat loss at about 2 kg. cal. causes the formation of a large amount of ice. In this respect the example shown is not typical of many stations where the ice potential curve is quite regular and smooth; however, it is included to illustrate the kind of difficulties encountered in practice. In addition, the curve is atypical because Q_0 , the heat loss necessary to bring about formation of ice was found exactly at 25 meters when the temperature of the completely mixed layer (1-4, Table 2B) first dropped to -1.8°C . In general, Q_0 cannot be so easily determined.

C. METHOD OF COMPUTING DATE OF ICE FORMATION

There are two acceptable methods of computing the date of ice formation. Since the amount of heat that must be lost before ice is formed is known from the ice potential computations, it is only necessary to compute the time required to lose this heat. One method is to make actual observations of the heat loss per day per square cm and thus to find the mean heat loss which is representative of a given area. The other method is to compute the total heat loss by consideration of the climatological data, the sun's altitude, and oceanographic data. For this purpose the only known formulas are those of Jacobs (1942), which yield rates of heat loss of the right order of magnitude in the Arctic, although they were specifically derived for middle latitudes.

Jacobs' formulas for computing heat losses are:

$$Q_{ab} = .025 \bar{\alpha} \left[.29 + .71 \left(1 - \frac{\bar{c}}{100} \right) \right] (t - r) t, t \text{ in minutes} \quad (4)$$

$$Q_b = .94 \left[\text{eff. } Q_b (1 - .0083\bar{c}) \right] t, \quad t \text{ in minutes} \quad (5)$$

$$Q_e = 145.4 \bar{w} (e_w - e_a) \left[1 + .01 \left\{ \frac{T_w - T_a}{e_w - e_a} \right\} \right] t, t \text{ in days,} \quad (6)$$

where

- Q_{ab} = total incoming radiation in gm. cal/cm²,
- Q_b = total back radiation in gm. cal/cm²
- Q_e = total heat loss due to evaporation in gm. cal/cm²
- $\bar{\alpha}$ = mean altitude of the sun in degrees,
- \bar{c} = mean cloud amount in percent,
- \bar{w} = mean wind velocity in knots,

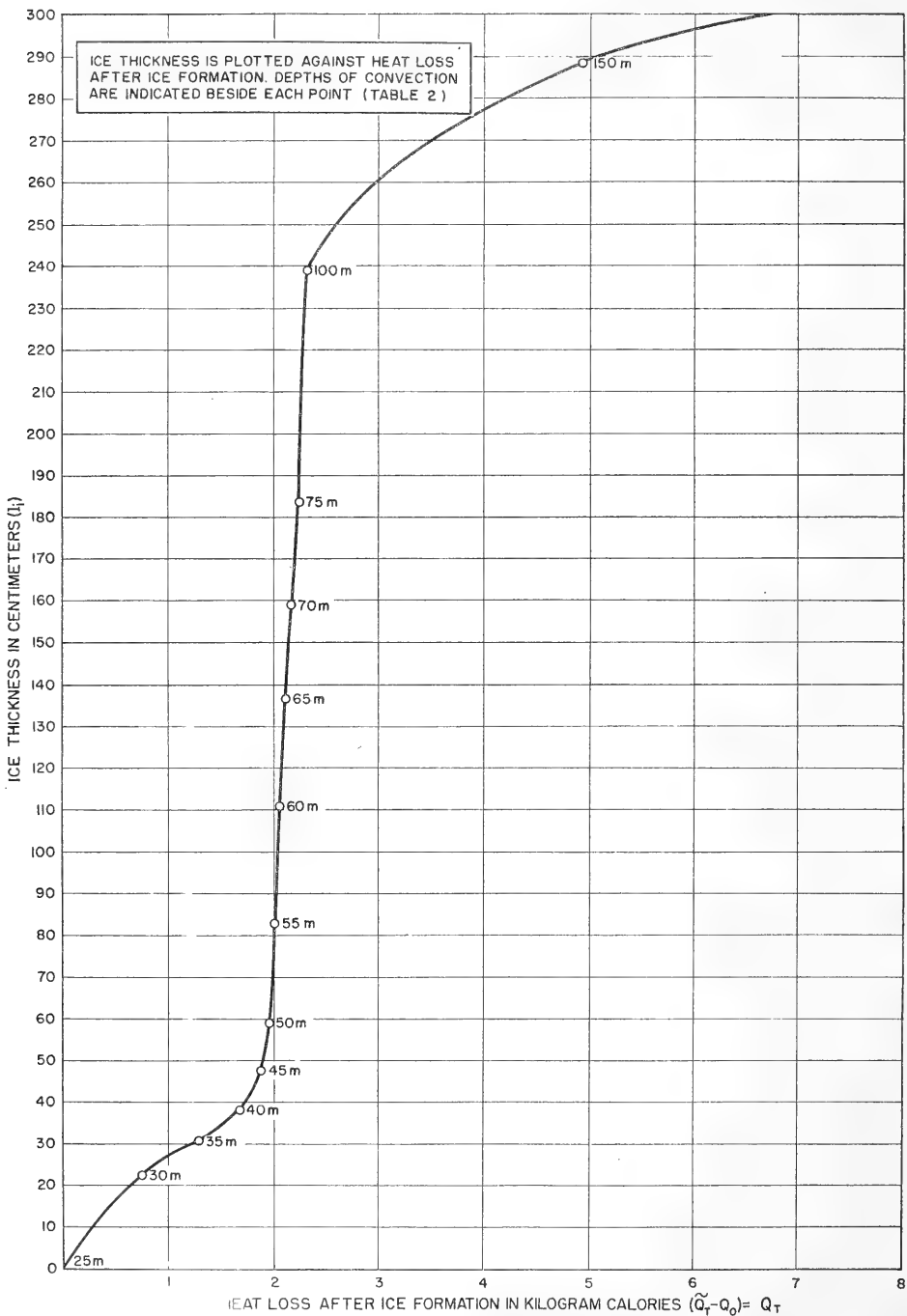


FIG. 2 ICE-POTENTIAL CURVE FOR STATION NUMBER 37.

e_w = vapor pressure of the water in inches Hg.,
 e_a = vapor pressure of the air in inches Hg.,
 T_w = temperature of the water in degrees F.,
 T_a = temperature of the air in degrees F.
 eff. Q_b (effective back radiation) = difference between

temperature radiation of the sea surface and long-wave radiation from the atmosphere,

t = time in units designated above, and

r = fractional part of the incoming radiation reflected from the sea surface.

The ice potential computations determine the amount of sensible heat which must be removed from the water column prior to the initial formation of ice. For example, let this value be Q_p . Then setting $Q_p = Q_b - Q_e - Q_{ab}$ and solving for t gives the number of days between the time that the oceanographic measurements were made and the time ice will form.

D. METHOD OF COMPUTING ICE GROWTH

From the time oceanographic observations are made until the time ice forms, it is assumed that the heat exchange results from incoming radiation, back radiation, and evaporation. After ice forms, the processes by which heat is removed from the water column are altered considerably. Any heat that is then removed from the water must be conducted through the solid layer of ice above it. Thus, the rate of further heat loss is determined by the temperature gradient through ice and snow. Hence, assuming steady-state conditions for finite increments of time,

$$\frac{d(Q_1 + Q_T)}{dt} = k_i \frac{\Delta T_i}{l_i} = k_s \frac{\Delta T}{l_s} \quad (7)$$

where,

Q_T is the amount of sensible heat loss (in kg. cal.),

Q_1 is the amount of latent heat loss (in kg. cal.),

k_i is the heat conductivity coefficient of sea ice,

k_s is the heat conductivity coefficient of snow,

ΔT_i is the temperature difference between the upper surface of the ice and freezing point of sea water (in °C.),

ΔT_s is the temperature difference between the surface of the snow and the surface of the ice (in °C.),

l_i is the thickness of the ice in cm.,

l_s is the thickness of the snow in cm., and

\bar{l}_s is the mean snow cover over a finite period of time.

Since $\Delta T = \Delta T_i + \Delta T_s$, where ΔT is the temperature difference between the freezing point of sea water (taken at $-1.8^\circ\text{C}.$) and the snow surface temperature, and from (7)

$$\frac{\Delta T_s}{\Delta T_i} = \frac{k_i \bar{l}_s}{k_s l_i} \quad (8)$$

then
$$\Delta T = \Delta T_i \left\{ 1 + \frac{k_i l_s}{k_s l_i} \right\} \quad \text{or} \quad \Delta T_i = \frac{\Delta T}{1 + \frac{k_i l_s}{k_s l_i}} \quad (9)$$

Then (7) becomes:
$$\frac{d(Q_1 + Q_T)}{dt} = \frac{k_i \Delta T}{l_i \left\{ 1 + \frac{k_i l_s}{k_s l_i} \right\}} \quad (10)$$

Substituting $Q_1 = \rho_i K l_i$ into (10) (ρ_o denotes ice density)

$$\rho_i K \frac{dl_i}{dt} + \frac{dQ_T}{dt} = \frac{k_i \Delta T}{l_i \left\{ 1 + \frac{k_i l_s}{k_s l_i} \right\}} \quad (11)$$

$$\rho_i K \left\{ 1 + \frac{k_i l_s}{k_s l_i} \right\} l_i dl_i + \left\{ 1 + \frac{k_i l_s}{k_s l_i} \right\} l_i dQ_T = k_i \Delta T dt \quad (12)$$

$$\rho_i K \int_0^{l_i(h)} l_i(Z) dl_i(Z) + \frac{\rho_i K k_i}{k_s} \int_0^{l_i(h)} l_s dl_i(Z) + \int_0^{Q_T(h)} l_i(Z) dQ_T(Z) +$$

$$\frac{k_i}{k_s} \int_0^{Q_T(h)} l_s dQ_T(Z) = k_i \int_{t_0}^t \Delta T dt \quad (13)$$

$$\frac{\rho_i K}{2} l_i^2(h) + \frac{\rho_i K k_i}{k_s} \bar{l}_s l_i(h) + \int_0^{Q_T(h)} l_i(Z) dQ_T(Z) + \frac{k_i}{k_s} \bar{l}_s Q_T(h) = k_i \int_{t_0}^t (T_F - T) dt \quad (14)$$

The right-hand expression in equation 14 is usually denoted by the title "degree-days of frost;" A degree-day of frost is defined as a day with a mean temperature 1-degree Centigrade below the freezing point of sea water. While the freezing temperature of sea water varies with salinity, it is here assumed to be -1.8°C . A degree-day of frost is then 1 day with a mean temperature of -2.8°C . Degree-days of frost usually are accumulated for forecasting over periods of 15 or 30 days. By giving the following values to some of the terms in equation 14:

$$\begin{aligned} \rho_i &= 0.9 \\ K &= .080 \frac{\text{Kg Cal}}{\text{gm}} \\ k_i &= .389 \frac{\text{Kg Cal}}{\text{cm } ^{\circ}\text{C day}} \\ k_s &= .062 \frac{\text{Kg Cal}}{\text{cm } ^{\circ}\text{C day}} \end{aligned}$$

the formula can be used directly to forecast the ice in terms of degree-days of frost

$$\int_{t_0}^{t_1} (T_F - T) dt.$$

Thus, for a given value of \bar{l}_s all terms in the equation are known except l_i and Q_T . A given l_i and likewise the corresponding Q_T , can be selected from the potential curve. By substituting l_i and Q_T into equation (14) and by evaluating the area under the potential curve between the proper limits for the expression

$$\int_0^{Q_T(h)} l_i(Z) dQ_T(Z)$$

the number of degree-days of frost required to form l_i centimeters of ice can be computed.

To eliminate the necessity of computation, the end results of the derivation have been presented in the form of tables (Tables 3-12). In addition the integral

$$\int_0^{Q_T(h)} l_i(Z) dQ_T(Z)$$

had to be evaluated by approximation methods. It was found from the majority of potential curves that the integral could be approximated as

$$\frac{l_i}{2} Q_T(h),$$

The error introduced was found to be small unless the water temperature was unusually high, and in most cases ice will not form under such conditions. Since the potential curve $l_i(Q_T)$ must always be plotted, it is readily apparent when the above approximation is invalid; in this situation the formula can be used. In order to facilitate substitution of the actual integral for the approximation, an auxiliary table (Table 13) is included which gives the degree-days of frost associated with various values of l_i and Q_T . If the potential curve is very irregular, Table 13 is entered, and by comparison with the degree-day figure computed from an average l_i , one can determine the amount of error introduced into the total. Most frequently this will be found to be small, since the potential term is only one of four separate factors contributing to the total; however, the actual value can be added or subtracted and a more accurate figure secured.

The form of equation 14 which was used in the tables is

$$\int_{t_0}^t (T_F - T) dt = \frac{1}{k_i} \left[\frac{\rho_i K}{2} l_i^2 + \left\{ \frac{\rho_i K k_i l_s}{k_s} + \frac{Q_T}{2} \right\} l_i + \frac{k_i l_s}{k_s} Q_T \right] \quad (15)$$

The degree-days of frost for fixed $l_s = 0, 2.5, 5, 7.5, 10, 15, 20, 30, 40,$ and 50 cm. are given in Tables 3 to 12. The concept of degree-days has an advantage over one of calendar days because of its versatility as far as forecasting is concerned. An ice forecast in days is difficult because it requires a forecast of air temperatures as well as ice growth, while the degree-day forecast permits ice growth forecasts which fit all conceivable temperature variations.

E. USE OF THE ICE GROWTH TABLES IN FORECASTING

Forecasting the ice growth in a given area requires the following information: (1) oceanographic data taken after the water mass begins to cool and prior to ice formation, (2) the date of ice formation, and (3) an expression relating ice growth to degree-days of frost for the given area. With this information the forecaster can then proceed to make a forecast for the entire season. The procedure is as follows: (1) the ice potential of each oceanographic station is calculated and the ice potential curve (example, Figure 2) is drawn; (2) from available meteorological and oceanographic data, the date of ice formation is determined; and (3) the forecast is made in terms of degree-days of frost.

Since the calculation of the ice potential, the date of first ice formation, and the ice potential curve have been previously explained, the remaining discussion will describe the preparation of an actual forecast. As before, Station #37 is used as an example. The ice potential curve for this station is given in Figure 2. In order to draw the ice forecast curves for this station it is necessary to read the ice thickness figures corresponding to integral values of Q_T from the ice potential curve. The degree-days of frost corresponding to each combi-

nation of l_i and Q_T values are read from each of the tables 3 to 12. A plot of ice thickness vs degree-days of frost is made from each set of values obtained from the graphs, and a smooth curve is drawn for each value of snow depth (l_s). An example of a completed forecast is given in Figure 3. In Figure 3, $Q_T = 1$ corresponds to an ice thickness of 27 cm. and $Q_T = 2$ to an ice thickness of 72 cm. on the ice potential curve of Figure 2. To convert the completed forecast into a time forecast the meteorologist must provide temperature and snow depth forecasts in order to secure an ice thickness forecast of 120 to 150 days for this station.

Now let us suppose that the date of first ice formation at Station #37 is 12 November and that the meteorologist provides a forecast, including the following data for the succeeding months:

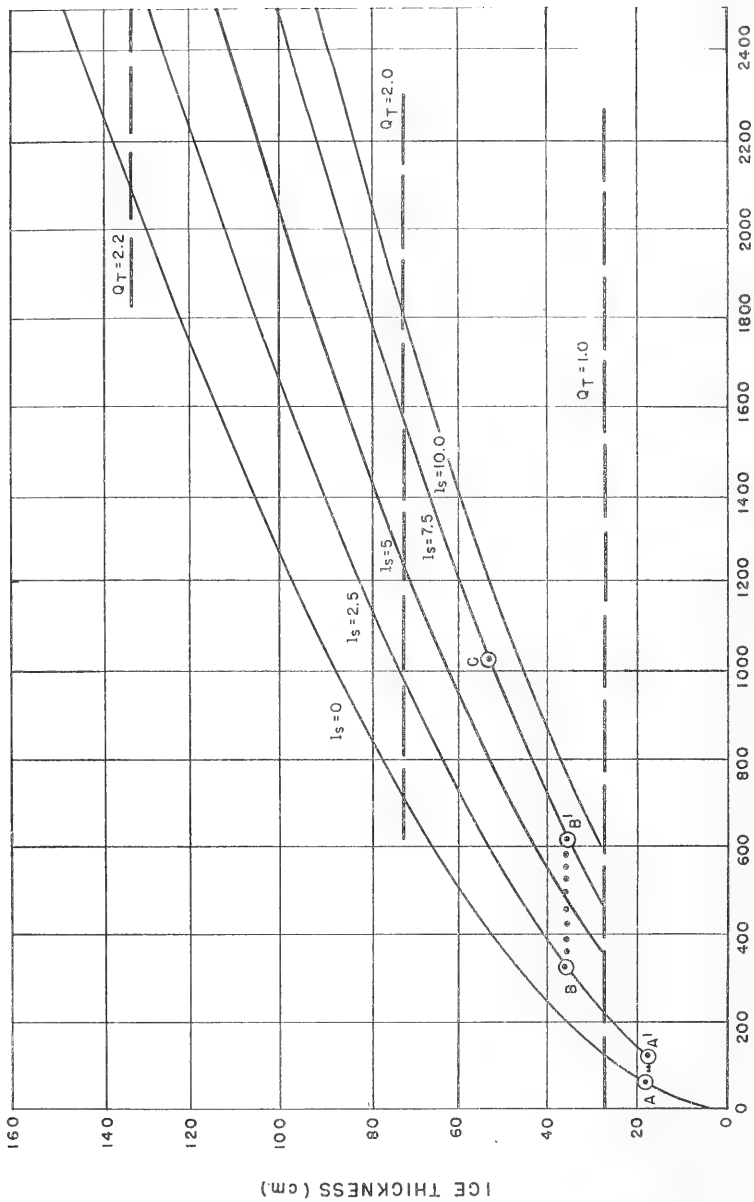
Period	Mean Temperature (°C)	Degree-Days of Frost	Snow Depth (cm.)
12 - 15 Nov.	-5.8	16	0
16 - 30 Nov.	-4.8	45	0
1 - 15 Dec.	-8.8	105	2.5
16 - 31 Dec.	-7.8	96	2.5
1 - 15 Jan.	-9.8	120	7.5
16 - 31 Jan.	-18.8	272	7.5

The ice thickness for any given date may be found from the above data and the forecast curve.

During the period when the snow depth is zero, the growth of ice will be along the upper curve on Figure 3; on 30 November, the final day with no snow, the total of degree-days of frost is $16 + 45$ or 61 and the ice thickness will be 17 cm. (point A on Figure 3).

During the month of December the ice grows under a snow depth of 2.5 cm. from a starting point of 17 cm. This point is marked A'. During December a total of 105 plus 96 or 201 degree-days of frost is counted, so that it is necessary to follow the curve $l_s = 2.5$ for 201 degree-days of frost beyond point A', or to point B. At point B, reached 31 December, the ice thickness will be 35 cm.

Similarly, during January the ice grows under a snow depth of 7.5 cm. for 120 plus 272 or 392 degree-days beyond the point B' corresponding to an ice thickness of 35 cm. On 31 January the point C is reached, and the ice thickness will be 53 cm. This constitutes an operational forecast, as the user of the forecast can determine the ice thickness on any day between 12 November and 31 January by counting the number of degree-days of frost and noting the snow depth applicable to the situation.



DEGREE DAYS OF FROST (°C)

FIG. 3. ICE GROWTH FORECAST FOR STATION # 37

F. BAFFIN BAY-DAVIS STRAIT LONG-RANGE ICE FORECAST FOR SEASON 1952-53.

During early autumn, 1952, oceanographic observations were taken at the locations shown on Figure 4. The method explained previously was employed to forecast the ice formation and growth of these locations. The dates of ice formation were computed and are shown beside each station. Since the thermohaline structure at some of the stations was such that no ice would be formed, it was possible to delineate the theoretical extreme ice boundary shown as a heavy line in Figure 4. This boundary agrees very well with the boundary which was actually observed in late March and early April 1953, (shown as a dashed line in Figure 4) except for the occurrence of ice south of Stations 39 and 40. It is possible that ice which was observed at these two stations was not formed there, but had drifted from nearby areas of ice formation. The dispersion of ice near the observed boundary in this area indicates that the ice actually was formed outside the area.

CONCLUSIONS

The methods of Zubov and Defant for ice potential calculation have proved in practice to give reasonable answers for open seas and for in-shore areas where local variations in the physical properties of the water are not large. In harbors and areas where runoff is important, changes in salinity and density are so rapid that it is difficult to attach a meaning to an average value of these parameters. Hence any ice potential calculation based on one or a few observations in a harbor may give a potential ice growth which is unreasonably high or low for a single season.

The forecast of ice growth based on the ice potential can be used only during the period when ice thickness is increasing. No theory has been included which accounts for decreasing ice thicknesses during the breakup period. Indeed, no mathematical theory has yet been developed for the breakup of ice.

Many refinements of the method presented in this paper are possible. Some of them are discussed in a paper by Brown (1954). The method described here was used to forecast during the 1952-53 ice season; the forecast proved to be satisfactory. The most important advancement discussed in this report is the use of the ice potential as a basis for forecasting ice growth.

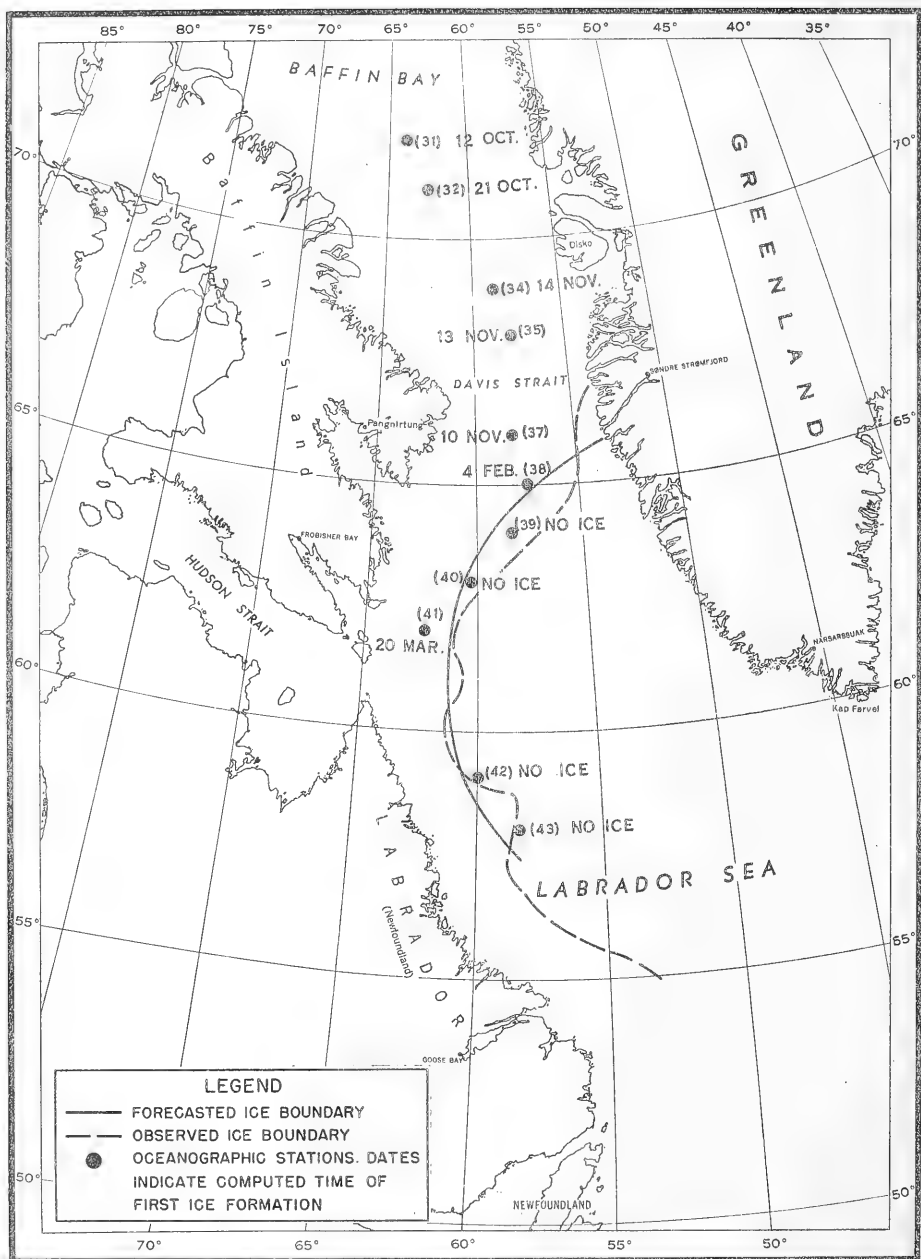


FIG. 4. FORECASTED AND OBSERVED ICE BOUNDARIES IN BAFFIN BAY AND DAVIS STRAIT FOR THE SEASON 1952-1953

TABLE 2 A
ICE POTENTIAL CALCULATIONS FOR STATION #37
(66°N, 58°W), 3 OCTOBER 1952

Depth Meters	T °C	S ‰	σ_t	Layer No.	Depth (Meters)	T °C	Mean Values	
							S ‰	σ_t
0	.56	32.38	25.98	1	0-10	.42	32.38	25.99
5	.10	32.36	26.00	2	10-15	.54	32.40	26.00
10	.61	32.39	25.99	3	15-20	.70	32.44	26.02
15	.67	32.41	26.00	4	20-25	.44	32.54	26.12
20	.73	32.47	26.05	5	25-30	-.13	32.70	26.28
25	.15	32.62	26.20	6	30-35	-.64	32.82	26.40
30	-.41	32.78	26.36	7	35-40	-1.02	32.90	26.45
35	-.86	32.86	26.43	8	40-45	-1.34	32.98	26.51
40	-1.18	32.94	26.48	9	45-50	-1.58	33.04	26.59
45	-1.50	33.01	26.54	10	50-55	-1.65	33.14	26.70
50	-1.65	33.08	26.64	11	55-60	-1.64	33.28	26.82
55	-1.65	33.20	26.76	12	60-65	-1.62	33.43	26.93
60	-1.62	33.36	26.88	13	65-70	-1.62	33.55	27.02
65	-1.62	33.50	26.98	14	70-75	-1.61	33.64	27.10
70	-1.61	33.60	27.07	15	75-80	-1.66	33.69	27.14
75	-1.61	33.69	27.13	16	80-85	-1.76	33.69	27.14
80	-1.72	33.69	27.14	17	85-90	-1.80	33.69	27.14
85	-1.80	33.69	27.14	18	90-95	-1.80	33.69	27.14
90	-1.80	33.69	27.14	19	95-100	-1.80	33.70	27.14
95	-1.80	33.69	27.14	20	100-150	-1.16	33.88	27.26
100	-1.80	33.70	27.14	21	150-200	.50	34.14	27.39
150	-0.51	34.06	27.38	22	200-300	.78	34.28	27.50
200	1.50	34.21	27.40	23	300-400	-.84	34.44	27.71
300	0.06	34.35	27.60					
400	-1.75	34.53	27.82					

TABLE 2 B

Layer	Depth (M)	Before Mixing		After Mixing		ΔT	ρ_T	$\bar{\rho}_T$	ΔS	ξ_i	l_i	ρ_T	
		T °C	S ‰	T °C	S ‰								
1-2	15	.46	32.39	26.00	.45	32.39	-.01	-.01	-.01				
1-3	20	.51	32.40	26.02	.30	32.40	-.21	.38	.39	0			
1-4	25	.33	32.44	26.12	-1.80	32.44	-2.13	4.79	5.18	0			
1-5	30	-1.52	32.48	26.28	-1.80	32.70	-.28	.76	5.94	.22	22.4	22.4	.76
1-6	35	-1.63	32.72	26.40	-1.80	32.79	-.17	.54	6.48	.07	8.2	30.6	1.30
1-7	40	-1.70	32.80	26.45	-1.80	32.86	-.10	.36	6.84	.06	8.0	38.6	1.66
1-8	45	-1.75	32.87	26.51	-1.80	32.93	-.05	.20	7.04	.06	9.0	47.6	1.86
1-9	50	-1.78	32.94	26.59	-1.80	33.01	-.02	.09	7.13	.07	11.7	59.3	1.95
1-10	55	-1.79	33.02	26.70	-1.80	33.15	-.01	.05	7.18	.13	23.8	83.1	2.00
1-11	60	-1.79	33.16	26.82	-1.80	33.30	-.01	.05	7.23	.14	27.7	110.8	2.05
1-12	65	-1.79	33.31	26.93	-1.80	33.43	-.01	.06	7.29	.12	25.6	136.4	2.11
1-13	70	-1.79	33.44	27.02	-1.80	33.54	-.01	.06	7.35	.10	23.0	159.4	2.17
1-14	75	-1.79	33.55	27.10	-1.80	33.65	-.01	.07	7.42	.10	24.5	183.9	2.24
1-19	100	-1.79	33.53	27.14	-1.80	33.70	-.01	.09	7.51	.17	55.4	239.3	2.33
1-20	150	-1.59	33.76	27.26	-1.80	33.86	-.21	2.83	10.34	.10	48.7	288.0	5.16
1-21	200	-1.22	33.93	27.39	-1.80	34.02	-.58	10.44	20.78	.09	58.2	346.2	15.60
1-22	300	-.94	34.11	27.50	-1.80	34.15	-.86	23.22	44.00	.04	36.7	384.9	38.82

TABLE 3

DEGREE-DAYS OF FROST ASSOCIATED WITH GIVEN ICE THICKNESS AND HEAT LOSSES FOR SNOW COVER = 0 cm.

Heat Loss kg. cal. (Q_f)

Ice Thickness in cm. (I_i)	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	20	25	30	
5																				
10	2	9	15	22	28	34	41	47	54	60	67	73	80	86	92	99	131	163	195	
10	9	22	35	48	61	74	86	99	112	125	138	151	163	176	189	202	266	330	395	
10	21	37	50	79	98	117	136	156	175	194	214	233	252	271	291	310	406	503	599	
15	15	31	47	63	80	96	114	131	149	168	186	204	223	241	259	278	351	438	525	
20	20	37	53	70	87	104	121	138	155	172	189	206	223	240	257	274	344	431	518	
25	25	42	58	74	90	106	122	138	154	170	186	202	218	234	250	266	334	421	508	
30	30	47	62	77	92	107	122	137	152	167	182	197	212	227	242	257	325	412	499	
35	35	50	65	80	95	110	125	140	155	170	185	200	215	230	245	260	328	415	502	
40	40	53	68	83	98	113	128	143	158	173	188	203	218	233	248	263	331	418	505	
45	45	56	71	86	101	116	131	146	161	176	191	206	221	236	251	266	334	421	508	
50	50	59	74	89	104	119	134	149	164	179	194	209	224	239	254	269	337	424	511	
55	55	62	77	92	107	122	137	152	167	182	197	212	227	242	257	272	340	427	514	
60	60	65	80	95	110	125	140	155	170	185	200	215	230	245	260	275	343	429	517	
65	65	68	83	98	113	128	143	158	173	188	203	218	233	248	263	278	346	432	520	
70	70	73	88	103	118	133	148	163	178	193	208	223	238	253	268	283	349	434	523	
75	75	78	93	108	123	138	153	168	183	198	213	228	243	258	273	288	352	436	526	
80	80	83	98	113	128	143	158	173	188	203	218	233	248	263	278	293	355	438	529	
85	85	88	103	118	133	148	163	178	193	208	223	238	253	268	283	298	358	440	532	
90	90	93	108	123	138	153	168	183	198	213	228	243	258	273	288	303	361	442	535	
95	95	98	113	128	143	158	173	188	203	218	233	248	263	278	293	308	364	444	538	
100	100	103	118	133	148	163	178	193	208	223	238	253	268	283	298	313	367	446	541	
110	110	113	128	143	158	173	188	203	218	233	248	263	278	293	308	323	370	448	544	
120	120	123	138	153	168	183	198	213	228	243	258	273	288	303	318	333	373	450	547	
130	130	133	148	163	178	193	208	223	238	253	268	283	298	313	328	343	376	452	550	
140	140	143	158	173	188	203	218	233	248	263	278	293	308	323	338	353	379	454	553	
150	150	153	168	183	198	213	228	243	258	273	288	303	318	333	348	363	382	456	556	
160	160	163	178	193	208	223	238	253	268	283	298	313	328	343	358	373	383	458	559	
170	170	173	188	203	218	233	248	263	278	293	308	323	338	353	368	383	393	460	562	
180	180	183	198	213	228	243	258	273	288	303	318	333	348	363	378	393	403	462	565	
190	190	193	208	223	238	253	268	283	298	313	328	343	358	373	388	403	413	464	568	
200	200	203	218	233	248	263	278	293	308	323	338	353	368	383	398	413	423	466	571	
210	210	213	228	243	258	273	288	303	318	333	348	363	378	393	408	423	433	468	574	
220	220	223	238	253	268	283	298	313	328	343	358	373	388	403	418	433	443	470	577	
230	230	233	248	263	278	293	308	323	338	353	368	383	398	413	428	443	453	472	580	
240	240	243	258	273	288	303	318	333	348	363	378	393	408	423	438	453	463	474	583	
250	250	253	268	283	298	313	328	343	358	373	388	403	418	433	448	463	473	476	586	
260	260	263	278	293	308	323	338	353	368	383	398	413	428	443	458	473	483	486	589	
270	270	273	288	303	318	333	348	363	378	393	408	423	438	453	468	483	493	496	592	
280	280	283	298	313	328	343	358	373	388	403	418	433	448	463	478	493	503	506	595	
290	290	293	308	323	338	353	368	383	398	413	428	443	458	473	488	503	513	516	598	
300	300	303	318	333	348	363	378	393	408	423	438	453	468	483	498	513	523	526	601	
310	310	313	328	343	358	373	388	403	418	433	448	463	478	493	508	523	533	536	604	
320	320	323	338	353	368	383	398	413	428	443	458	473	488	503	518	533	543	546	607	
330	330	333	348	363	378	393	408	423	438	453	468	483	498	513	528	543	553	556	610	
340	340	343	358	373	388	403	418	433	448	463	478	493	508	523	538	553	563	566	613	
350	350	353	368	383	398	413	428	443	458	473	488	503	518	533	548	563	573	576	616	
360	360	363	378	393	408	423	438	453	468	483	498	513	528	543	558	573	583	586	619	
370	370	373	388	403	418	433	448	463	478	493	508	523	538	553	568	583	593	596	622	
380	380	383	398	413	428	443	458	473	488	503	518	533	548	563	578	593	603	606	625	
390	390	393	408	423	438	453	468	483	498	513	528	543	558	573	588	603	613	616	628	
400	400	403	418	433	448	463	478	493	508	523	538	553	568	583	598	613	623	626	631	
410	410	413	428	443	458	473	488	503	518	533	548	563	578	593	608	623	633	636	639	
420	420	423	438	453	468	483	498	513	528	543	558	573	588	603	618	633	643	646	649	
430	430	433	448	463	478	493	508	523	538	553	568	583	598	613	628	643	653	656	659	
440	440	443	458	473	488	503	518	533	548	563	578	593	608	623	638	653	663	666	669	
450	450	453	468	483	498	513	528	543	558	573	588	603	618	633	648	663	673	676	679	
460	460	463	478	493	508	523	538	553	568	583	598	613	628	643	658	673	683	686	689	
470	470	473	488	503	518	533	548	563	578	593	608	623	638	653	668	683	693	696	699	
480	480	483	498	513	528	543	558	573	588	603	618	633	648	663	678	693	703	706	709	
490	490	493	508	523	538	553	568	583	598	613	628	643	658	673	688	703	713	716	719	
500	500	503	518	533	548	563	578	593	608	623	638	653	668	683	698	713	723	726	729	
510	510	513	528	543	558	573	588	603	618	633	648	663	678	693	708	723	733	736	739	
520	520	523	538	553	568	583	598	613	628	643	658	673	688	703	718	733	743	746	749	
530	530	533	548	563	578	593	608	623	638	653	668	683	698	713	728	743	753	756	759	
540	540	543	558	573	588	603	618	633	648	663	678	693	708	723	738	753	763	766	769	
550	550	553	568	583	598	613	628	643	658	673	688	703	718	733	748	763	773	776	779	
560	560	563	578	593	608	623	638	653	668	683	698	713	728	743	758	773	783	786	789	
570	570	573	588	603	618	633	648	663	678	693	708	723	738	753	768	783	793	796	799	
580	580	583	598	613	628	643	658	673	688	703	718	733	748	763	778	793	803	806	809	
590	590	593	608	623	638	653	668	683	698	713	728	743	758	773	788	803	813	816	819	
600	600	603	618	633	648	663	678	693	708	723	738	753	768	783	798	813	823	826	829	
610	610	613	628	643	658	673	688	703	718	733	748	763	778	793	808	823	833	836	839	
620	620	623	638	653	668	683	698	713	728	743	758	773	788	803	818	833	843	846	849	
630	630																			

TABLE 4.

DEGREE-DAYS OF FROST ASSOCIATED WITH GIVEN ICE THICKNESSES AND HEAT LOSSES FOR SNOW COVER = 2.5 cm.
Heat Loss kg. cal. (Q_p)

Ice cm.	0	0	1	2	3	4	5	6	7	8	9	10	10	11	12	13	14	15	20	25	30
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
5	17	64	110	157	204	250	297	344	391	433	483	531	573	624	671	713	759	806	1009	1210	1419
10	38	91	144	198	251	304	357	410	462	514	570	623	676	730	783	836	891	946	1102	1369	1634
15	10	124	164	213	263	312	362	412	462	511	561	610	660	710	760	810	860	910	1056	1354	1652
20	95	151	227	293	359	425	491	557	623	689	755	821	888	954	1020	1086	1152	1217	1416	1746	2076
25	130	203	275	348	420	493	565	638	710	782	855	927	1000	1072	1145	1217	1290	1350	1590	1942	2304
30	170	249	328	407	486	565	644	723	802	880	959	1038	1117	1196	1275	1354	1433	1512	1718	2112	2537
35	215	300	386	471	556	642	727	812	898	983	1068	1153	1239	1324	1409	1494	1579	1664	1921	2318	2774
40	264	356	448	539	631	723	815	906	998	1090	1182	1273	1365	1457	1548	1640	1731	1822	2059	2558	3015
45	313	416	514	612	711	809	907	1005	1103	1202	1300	1398	1496	1594	1692	1790	1888	1986	2281	2772	3283
50	377	481	586	687	795	900	1004	1109	1213	1318	1423	1527	1632	1736	1841	1945	2050	2154	2488	2991	3514
55	440	551	662	773	881	995	1106	1217	1328	1439	1550	1661	1772	1883	1994	2105	2216	2326	2705	3215	3770
60	507	625	742	860	977	1095	1212	1330	1447	1564	1682	1799	1917	2034	2152	2269	2386	2503	2926	3441	4031
65	580	704	827	951	1075	1199	1323	1447	1571	1695	1819	1942	2066	2190	2314	2438	2562	2686	3057	3676	4296
70	657	787	917	1048	1178	1308	1438	1568	1698	1828	1958	2088	2218	2348	2478	2608	2738	2868	3281	3914	4566
75	738	875	1012	1148	1285	1422	1559	1695	1832	1969	2106	2242	2379	2516	2654	2791	2928	3065	3473	4156	4840
80	825	968	1111	1254	1397	1540	1683	1827	1970	2113	2256	2399	2542	2686	2829	2972	3115	3258	3683	4373	5079
85	915	1065	1214	1364	1514	1664	1813	1962	2111	2260	2409	2558	2707	2856	3005	3154	3303	3452	3903	4613	5339
90	1011	1167	1323	1479	1635	1791	1947	2103	2259	2415	2571	2727	2883	3039	3195	3351	3507	3663	4131	4861	5601
95	1111	1273	1436	1598	1761	1923	2086	2248	2410	2573	2735	2898	3060	3223	3385	3547	3710	3872	4360	5112	5884
100	1215	1384	1553	1722	1891	2060	2229	2398	2567	2735	2904	3073	3242	3411	3580	3749	3918	4087	4600	5437	6281
110	1439	1621	1803	1984	2166	2348	2529	2711	2893	3075	3256	3438	3620	3802	3983	4165	4347	4529	5073	5982	6931
120	1681	1876	2070	2265	2459	2654	2848	3043	3238	3432	3627	3821	4016	4210	4405	4599	4794	4989	5572	6545	7518
130	1941	2149	2356	2564	2771	2978	3186	3393	3601	3808	4016	4223	4430	4638	4845	5053	5260	5468	6080	7127	8164
140	2220	2441	2661	2881	3102	3322	3542	3762	3983	4203	4423	4643	4864	5084	5304	5524	5744	5964	6606	7727	8829
150	2518	2751	2984	3217	3450	3683	3916	4150	4383	4616	4849	5082	5315	5548	5781	6014	6247	6480	7153	8316	9513
160	2834	3080	3326	3572	3818	4064	4310	4556	4802	5048	5294	5540	5786	6032	6278	6524	6770	7016	7727	8933	10113
170	3168	3427	3686	3945	4203	4462	4721	4980	5239	5498	5756	6015	6274	6533	6792	7050	7309	7568	8313	9563	10713
180	3522	3794	4066	4337	4609	4880	5151	5421	5692	5962	6233	6503	6773	7043	7313	7583	7853	8123	8903	10214	11414
190	3892	4177	4461	4745	5029	5313	5596	5880	6164	6448	6732	7016	7300	7584	7868	8152	8436	8720	9540	10894	12114
200	4282	4570	4857	5145	5432	5719	6006	6293	6580	6867	7154	7441	7728	8015	8302	8589	8876	9163	10020	11404	12714
210	4691	5001	5311	5622	5932	6242	6552	6862	7173	7483	7793	8104	8414	8724	9034	9344	9654	9964	10860	12284	13614
220	5113	5441	5769	6107	6445	6783	7121	7459	7797	8135	8473	8811	9149	9487	9825	10163	10501	10839	11770	13224	14514
230	5563	5909	6255	6601	6947	7293	7639	7985	8331	8677	9023	9369	9715	10061	10407	10753	11099	11445	12400	13884	15114
240	6027	6376	6725	7074	7423	7771	8120	8469	8818	9167	9515	9864	10212	10560	10908	11256	11604	11952	12930	14444	15614
250	6510	6872	7233	7595	7957	8318	8680	9042	9403	9764	10125	10486	10847	11208	11569	11930	12291	12652	13650	15194	16314
260	7011	7385	7760	8134	8509	8883	9258	9632	10007	10381	10756	11130	11505	11880	12255	12630	13005	13380	14400	15964	17114
270	7530	7918	8305	8692	9080	9467	9854	10241	10628	11015	11402	11789	12176	12563	12950	13337	13724	14111	15150	16734	17814
280	8069	8469	8869	9269	9669	10069	10469	10869	11269	11669	12069	12469	12869	13269	13669	14069	14469	14869	15930	17534	18614
290	8625	9038	9451	9864	10277	10690	11103	11516	11929	12342	12755	13168	13581	13994	14407	14820	15233	15646	16720	18334	19414
300	9200	9626	10052	10478	10904	11330	11756	12182	12608	13034	13460	13886	14312	14738	15164	15590	16016	16442	17530	19164	20214

TABLE 5

DEGREE-DAYS OF FROST ASSOCIATED WITH GIVEN ICE THICKNESSES AND HEAT LOSSES FOR SNOW COVER = 5 cm.

Ice Thickness in cm. (I ₁)	Heat Loss in kg. cal. (Q _r)																													
	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	20	25	30											
0	0	81	161	242	323	403	484	564	645	726	806	887	968	1049	1129	1210	1413	2016	2619	3219										
5	31	118	206	292	380	467	554	641	728	815	902	989	1076	1163	1250	1337	1543	2146	2749	3349										
10	67	161	254	348	441	535	628	722	815	907	1000	1092	1185	1278	1370	1462	1668	2271	2874	3474										
15	108	208	308	408	508	608	708	807	907	1007	1107	1207	1307	1407	1507	1607	1813	2416	3019	3619										
20	153	259	366	472	578	685	791	898	1004	1110	1217	1323	1429	1536	1642	1748	1954	2557	3160	3760										
25	203	316	429	542	654	767	880	992	1106	1218	1331	1444	1556	1669	1782	1895	2101	2704	3307	3907										
30	258	377	496	615	734	854	973	1092	1211	1330	1450	1569	1688	1807	1926	2046	2252	2855	3458	4058										
35	316	442	568	693	819	945	1070	1195	1322	1447	1573	1698	1824	1950	2075	2201	2407	3010	3613	4213										
40	380	512	644	776	909	1041	1173	1305	1437	1569	1701	1833	1965	2097	2229	2361	2567	3170	3773	4373										
45	449	587	726	864	1001	1131	1280	1413	1547	1695	1834	1972	2110	2249	2388	2526	2732	3335	3938	4538										
50	522	667	812	956	1101	1246	1391	1536	1681	1828	1971	2116	2261	2406	2550	2695	2901	3504	4107	4707										
55	599	751	902	1053	1205	1356	1507	1659	1810	1961	2113	2264	2415	2567	2718	2869	3075	3678	4281	4881										
60	682	832	997	1155	1313	1470	1628	1786	1944	2101	2259	2417	2575	2733	2890	3048	3254	3857	4460	5060										
65	768	932	1097	1265	1435	1604	1784	1962	2140	2324	2506	2687	2869	3051	3232	3413	3619	4222	4825	5425										
70	860	1031	1201	1372	1542	1713	1894	2082	2246	2410	2574	2739	2907	3078	3249	3419	3625	4228	4831	5431										
75	956	1133	1310	1484	1661	1841	2018	2195	2372	2550	2726	2904	3081	3258	3435	3612	3818	4421	5024	5624										
80	1057	1240	1424	1607	1791	1974	2158	2341	2525	2708	2892	3075	3258	3442	3625	3809	4015	4618	5221	5821										
85	1162	1352	1542	1732	1922	2112	2302	2491	2681	2871	3061	3251	3441	3631	3821	4011	4217	4820	5423	6023										
90	1272	1468	1665	1861	2056	2254	2450	2646	2843	3039	3235	3432	3628	3824	4021	4217	4425	5028	5631	6231										
95	1387	1590	1792	1995	2198	2400	2603	2806	3009	3212	3414	3617	3820	4023	4225	4428	4634	5237	5840	6440										
100	1506	1715	1926	2131	2343	2552	2761	2971	3180	3389	3598	3807	4016	4225	4434	4644	4854	5457	6060	6660										
110	1758	1980	2203	2425	2647	2869	3091	3313	3535	3757	3979	4201	4423	4645	4867	5089	5311	5914	6517	7117										
120	2029	2334	2499	2734	2969	3204	3429	3674	3908	4143	4378	4613	4848	5083	5318	5553	5787	6390	6993	7593										
130	2319	2666	2814	3062	3310	3558	3805	4053	4301	4548	4796	5044	5292	5539	5787	6035	6283	6886	7489	8089										
140	2627	2967	3148	3408	3669	3930	4190	4451	4712	4972	5233	5493	5754	6014	6275	6536	6796	7399	7999	8599										
150	2953	3227	3500	3774	4047	4320	4594	4867	5141	5414	5688	5961	6235	6508	6782	7055	7328	7931	8531	9131										
160	3298	3584	3871	4157	4443	4730	5016	5302	5589	5875	6161	6448	6734	7020	7306	7593	7879	8482	9082	9682										
170	3662	3961	4260	4559	4858	5157	5456	5756	6055	6354	6653	6952	7252	7551	7850	8149	8448	9051	9651	10251										
180	4044	4356	4668	4980	5291	5601	5911	6222	6532	6842	7151	7461	7771	8081	8391	8701	9011	9614	10214	10814										
190	4444	4769	5094	5419	5744	6068	6393	6718	7043	7368	7692	8016	8341	8666	8991	9317	9642	10245	10845	11445										
200	4863	5201	5538	5876	6213	6552	6889	7227	7565	7902	8240	8578	8916	9253	9591	9929	10268	10871	11471	12071										
210	5301	5651	6002	6352	6703	7053	7404	7755	8105	8456	8806	9157	9507	9857	10208	10559	10910	11513	12113	12713										
220	5757	6120	6484	6847	7210	7574	7937	8300	8664	9027	9391	9754	10118	10481	10845	11208	11571	12174	12774	13374										
230	6231	6607	6984	7360	7736	8112	8489	8865	9241	9618	9994	10371	10748	11125	11502	11879	12256	12859	13459	14059										
240	6724	7113	7502	7892	8281	8670	9059	9448	9837	10226	10615	11004	11393	11782	12171	12560	12949	13552	14152	14752										
250	7236	7638	8040	8442	8844	9246	9648	10050	10452	10854	11256	11658	12060	12462	12864	13266	13668	14271	14871	15471										
260	7766	8180	8594	9010	9426	9842	10258	10674	11090	11506	11922	12338	12754	13170	13586	14002	14418	15021	15621	16221										
270	8314	8742	9170	9597	10025	10453	10881	11309	11737	12165	12593	13021	13449	13877	14305	14733	15161	15764	16364	16964										
280	8881	9322	9763	10203	10643	11083	11523	11963	12403	12843	13283	13723	14163	14603	15043	15483	15923	16526	17126	17726										
290	9467	9920	10374	10837	11301	11765	12229	12693	13157	13621	14085	14549	15013	15477	15941	16405	16869	17472	18072	18672										
300	10071	10537	11014	11491	11968	12445	12922	13399	13876	14353	14830	15307	15784	16261	16738	17215	17692	18295	18895	19495										

TABLE 6

DEGREE-DAYS OF FROST ASSOCIATED WITH GIVEN ICE THICKNESSES AND HEAT LOSSES FOR SNOW COVER = 7.5 cm.

Ice Thickness in cm. (I_1)	Heat Loss in kg. cal. (Q_1)																		
	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	20	25	30
0	121	212	363	484	605	726	817	969	1089	1210	1331	1452	1573	1694	1814	2119	2594	3024	3699
5	146	173	301	428	555	683	810	938	1065	1192	1320	1447	1574	1702	1829	1957	2294	2731	3406
10	96	230	364	498	632	765	909	1033	1167	1301	1434	1563	1692	1821	1950	2104	2473	2942	3617
15	251	292	432	572	712	853	993	1133	1273	1414	1554	1694	1834	1975	2115	2255	2656	3125	3799
20	211	359	504	651	798	944	1091	1238	1385	1531	1678	1825	1971	2119	2265	2411	2812	3281	3955
25	276	429	582	735	888	1041	1194	1347	1500	1653	1806	1959	2113	2266	2419	2572	2973	3442	4116
30	345	504	664	823	983	1142	1302	1461	1621	1780	1940	2099	2259	2418	2578	2738	3139	3608	4282
35	413	584	750	916	1082	1248	1414	1580	1746	1912	2078	2244	2410	2576	2742	2908	3309	3778	4452
40	486	669	841	1011	1185	1358	1531	1698	1876	2045	2220	2393	2565	2738	2910	3082	3483	3952	4626
45	579	768	937	1116	1295	1473	1652	1831	2010	2189	2367	2546	2725	2904	3083	3261	3662	4131	4805
50	667	852	1037	1223	1408	1593	1778	1964	2149	2334	2519	2704	2889	3075	3260	3445	3846	4315	5089
55	759	951	1142	1334	1526	1717	1909	2101	2292	2484	2676	2867	3059	3250	3442	3634	4035	4504	5278
60	856	1054	1252	1450	1648	1846	2044	2242	2440	2639	2837	3035	3233	3431	3629	3827	4228	4697	5471
65	957	1162	1366	1571	1775	1980	2184	2389	2593	2798	3002	3207	3411	3616	3820	4025	4426	4895	5669
70	1063	1274	1485	1696	1907	2118	2329	2540	2751	2962	3173	3384	3594	3806	4016	4227	4628	5097	5871
75	1171	1391	1603	1826	2043	2261	2478	2695	2913	3130	3348	3565	3782	4000	4217	4434	4835	5304	6078
80	1289	1513	1737	1960	2183	2408	2632	2856	3079	3303	3527	3751	3975	4200	4422	4646	5047	5516	6290
85	1409	1639	1869	2100	2330	2560	2790	3020	3251	3481	3711	3941	4172	4402	4632	4862	5263	5732	6506
90	1531	1770	2007	2243	2480	2717	2953	3190	3427	3663	3900	4136	4373	4610	4846	5083	5484	5953	6727
95	1663	1906	2149	2392	2635	2878	3121	3364	3607	3850	4093	4336	4580	4823	5066	5309	5710	6179	6953
100	1796	2046	2295	2545	2794	3043	3293	3543	3792	4042	4292	4541	4790	5039	5289	5538	5939	6408	7182
110	2078	2310	2603	2865	3127	3390	3652	3914	4177	4439	4702	4964	5226	5489	5751	6013	6414	6883	7657
120	2378	2653	2928	3203	3479	3754	4029	4304	4579	4855	5130	5405	5680	5955	6231	6506	6907	7376	8150
130	2696	2984	3272	3560	3849	4137	4425	4713	5001	5289	5577	5865	6153	6441	6729	7017	7418	7887	8661
140	3033	3334	3635	3936	4237	4538	4839	5140	5441	5742	6042	6343	6644	6945	7246	7547	7948	8417	9191
150	3389	3703	4016	4330	4644	4958	5272	5585	5900	6213	6526	6840	7154	7468	7782	8095	8506	8975	9749
160	3763	4089	4416	4743	5069	5396	5722	6049	6376	6702	7029	7356	7683	8009	8335	8662	9073	9542	10316
170	4155	4495	4834	5174	5513	5852	6192	6532	6871	7210	7550	7889	8229	8568	8908	9247	9658	10127	10901
180	4566	4919	5271	5623	5976	6328	6680	7032	7384	7737	8090	8442	8794	9146	9499	9851	10262	10731	11505
190	4996	5361	5726	6091	6456	6822	7187	7552	7917	8282	8648	9013	9378	9743	10108	10473	10895	11364	12138
200	5444	5822	6200	6578	6956	7334	7712	8090	8468	8846	9224	9602	9980	10358	10736	11114	11532	11950	12724
210	5910	6301	6692	7083	7474	7865	8256	8646	9037	9428	9819	10210	10601	10992	11383	11774	12165	12556	13330
220	6399	6799	7203	7606	8010	8414	8818	9222	9626	10029	10433	10837	11241	11645	12049	12453	12857	13261	14035
230	6915	7315	7732	8149	8565	8982	9398	9815	10232	10649	11066	11483	11900	12317	12734	13151	13568	13985	14759
240	7461	7850	8280	8709	9139	9568	9998	10427	10856	11285	11714	12143	12572	13001	13430	13859	14288	14717	15491
250	7962	8340	8846	9285	9731	10173	10615	11057	11499	11941	12383	12825	13267	13709	14151	14593	15035	15477	16251
260	8520	8976	9431	9886	10341	10797	11253	11709	12165	12621	13077	13533	13989	14445	14901	15357	15813	16269	17043
270	9098	9566	10034	10502	10970	11438	11906	12374	12842	13310	13778	14246	14714	15182	15650	16118	16586	17054	17828
280	9694	10175																	18602
290	10309																		
300																			

TABLE 7

DEGREE-DAYS OF FROST ASSOCIATED WITH GIVEN ICE THICKNESSES AND HEAT LOSSES FOR SNOW COVER = 10 cm.

Ice Thickness in in. (I _i)	Heat Loss in kg. cal. (°C)																			
	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	20	25	30	
0																				
5	60	323	351	364	371	386	392	406	4290	4452	4613	4774	4936	5097	5258	5419	5576	5732	5892	
10	125	310	374	404	422	439	457	475	492	510	528	546	564	582	600	618	636	654	672	
15	195	556	737	817	897	977	1057	1137	1217	1297	1377	1457	1537	1617	1697	1777	1857	1937	2017	
20	349	456	613	830	1017	1204	1391	1578	1765	1952	2139	2326	2513	2700	2887	3074	3261	3448	3635	
25	516	512	735	923	1122	1315	1509	1702	1896	2089	2282	2476	2669	2863	3056	3250	3443	3636	3829	
30	532	632	831	1031	1231	1431	1631	1831	2030	2230	2430	2630	2830	3030	3230	3430	3629	3828	4027	
35	520	925	1139	1349	1551	1757	1964	2170	2376	2583	2789	2995	3201	3408	3614	3820	4026	4232	4438	
40	612	929	1148	1367	1587	1806	2024	2242	2461	2680	2901	3120	3339	3558	3778	3997	4216	4435	4654	
45	710	929	1148	1367	1587	1806	2024	2242	2461	2680	2901	3120	3339	3558	3778	3997	4216	4435	4654	
50	812	1131	1353	1575	1797	2019	2241	2463	2685	2907	3129	3351	3573	3795	4017	4239	4461	4683	4905	
55	919	1231	1453	1675	1897	2119	2341	2563	2785	3007	3229	3451	3673	3895	4117	4339	4561	4783	5005	
60	1030	1263	1485	1707	1929	2151	2373	2595	2817	3039	3261	3483	3705	3927	4149	4371	4593	4815	5037	
65	1146	1381	1606	1830	2054	2278	2502	2726	2950	3174	3398	3622	3846	4070	4294	4518	4742	4966	5190	
70	1266	1513	1749	2020	2272	2523	2774	3025	3276	3527	3779	4030	4281	4532	4783	5034	5285	5536	5787	
75	1372	1625	1897	2165	2422	2680	2938	3195	3453	3711	3968	4226	4484	4742	5000	5258	5516	5774	6032	
80	1521	1785	2050	2311	2578	2842	3106	3370	3634	3898	4162	4427	4691	4955	5219	5483	5747	6011	6275	
85	1656	1926	2197	2467	2738	3008	3279	3550	3820	4091	4362	4632	4902	5173	5443	5714	5984	6254	6524	
90	1795	2072	2349	2626	2903	3180	3457	3734	4011	4288	4564	4841	5118	5395	5672	5949	6226	6503	6780	
95	1938	2222	2505	2789	3072	3355	3639	3922	4206	4489	4772	5056	5339	5623	5906	6189	6472	6755	7038	
100	2097	2376	2666	2956	3246	3536	3826	4115	4405	4695	4985	5275	5565	5854	6144	6434	6724	7014	7304	
110	2397	2700	3003	3305	3608	3910	4213	4516	4819	5121	5424	5727	6029	6332	6634	6937	7240	7543	7846	
120	2726	3042	3357	3673	3988	4304	4619	4934	5249	5564	5879	6194	6509	6824	7139	7454	7769	8084	8399	
130	3071	3402	3730	4059	4387	4715	5044	5372	5701	6029	6358	6686	7015	7343	7671	8000	8328	8657	8985	
140	3440	3781	4122	4463	4805	5146	5487	5828	6169	6510	6851	7192	7533	7874	8215	8556	8897	9238	9579	
150	3824	4173	4522	4866	5211	5556	5901	6246	6591	6936	7281	7626	7971	8316	8661	9006	9351	9696	10041	
160	4227	4594	4961	5328	5695	6062	6429	6796	7163	7530	7897	8264	8631	8998	9365	9732	10099	10466	10833	
170	4649	5029	5408	5788	6168	6548	6928	7307	7687	8067	8447	8827	9206	9586	9965	10345	10724	11104	11483	
180	5089	5482	5874	6267	6660	7052	7445	7837	8230	8623	9015	9408	9801	10193	10586	10979	11372	11765	12158	
190	5547	5953	6358	6764	7170	7575	7980	8386	8791	9197	9602	10008	10413	10819	11224	11629	12034	12439	12844	
200	6022	6441	6859	7278	7696	8114	8533	8951	9369	9788	10206	10624	11042	11460	11878	12296	12714	13132	13550	
210	6520	6951	7382	7811	8240	8670	9100	9530	9960	10390	10820	11250	11680	12110	12540	12970	13400	13830	14260	
220	7031	7478	7922	8366	8810	9254	9698	10142	10586	11030	11474	11918	12362	12806	13250	13694	14138	14582	15026	
230	7567	8024	8480	8936	9392	9848	10304	10760	11216	11672	12128	12584	13040	13496	13952	14408	14864	15320	15776	
240	8118	8588	9057	9527	9997	10467	10937	11407	11877	12347	12817	13287	13757	14227	14697	15167	15637	16107	16577	
250	8687	9170	9653	10136	10619	11102	11585	12068	12551	13034	13517	14000	14483	14966	15449	15932	16415	16898	17381	
260	9275	9771	10266	10761	11256	11751	12246	12741	13236	13731	14226	14721	15216	15711	16206	16701	17196	17691	18186	
270	9882	10390																		
280	10507																			

TABLE 8

DEGREE-DAYS OF FROST ASSOCIATED WITH OTHER ICE THICKNESSES AND HEAT LOSSES FOR SNOW COVER = 15 cm.

Ice Thickness in cm. (I)	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	20	25	30	
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
5	92	333	586	796	969	1210	1450	1690	1936	2177	2419	2651	2873	3085	3287	3479	3661	3834	3998	4153
10	183	633	993	1304	1683	2131	2550	2948	3326	3685	4024	4344	4645	4927	5191	5437	5665	5876	6070	6248
15	282	943	1405	1898	2402	2918	3446	3984	4532	5090	5658	6236	6824	7422	8030	8648	9276	9914	10562	11220
20	395	1333	1921	2538	3186	3864	4562	5280	6018	6776	7554	8352	9170	10008	10866	11744	12642	13560	14498	15456
25	525	1813	2541	3308	4116	4964	5842	6750	7688	8656	9654	10682	11740	12828	13946	15084	16242	17420	18618	19836
30	668	2313	3181	4138	5186	6324	7552	8870	10278	11776	13364	15042	16810	18668	20616	22654	24772	26970	29248	31596
35	818	2833	3841	4938	6126	7404	8772	10230	11778	13416	15144	16962	18870	20868	22956	25134	27402	29760	32208	34746
40	975	3373	4511	5738	7056	8464	9962	11550	13228	14996	16854	18802	20840	22968	25186	27494	29892	32380	34958	37626
45	1138	3933	5191	6538	7976	9504	11122	12830	14628	16516	18494	20562	22720	24968	27306	29734	32252	34860	37558	40346
50	1308	4513	5901	7388	8976	10664	12452	14340	16328	18416	20604	22892	25280	27768	30356	33044	35832	38720	41708	44796
55	1488	5133	6651	8238	9926	11714	13602	15590	17678	19866	22154	24542	27030	29618	32306	35094	37982	40970	44058	47246
60	1678	5773	7421	9138	10926	12814	14802	16890	19078	21366	23754	26242	28830	31518	34306	37194	40182	43270	46458	49746
65	1878	6433	8201	10038	11946	13924	16072	18320	20668	23116	25664	28312	31060	33908	36856	39904	43052	46300	49648	53096
70	2088	7113	9001	10968	13006	15114	17292	19540	21868	24286	26794	29392	32080	34868	37756	40744	43832	47020	50308	53696
75	2308	7813	9801	11838	13946	16124	18372	20690	23088	25566	28124	30772	33510	36338	39266	42294	45422	48650	51978	55406
80	2538	8533	10621	12718	14886	17124	19432	21810	24268	26796	29394	32072	34830	37678	40616	43644	46762	49970	53268	56656
85	2778	9273	11451	13608	15846	18154	20532	22980	25498	28086	30754	33502	36330	39248	42256	45354	48542	51810	55158	58586
90	3028	10033	12301	14528	16826	19194	21632	24140	26718	29366	32094	34902	37790	40768	43836	46994	50242	53580	57008	60526
95	3288	10813	13181	15468	17826	20204	22652	25170	27758	30416	33144	35952	38840	41808	44856	47984	51192	54480	57848	61296
100	3548	11613	14141	16428	18846	21324	23872	26490	29178	31936	34764	37672	40660	43728	46876	50104	53412	56800	60268	63816
105	3808	12433	15181	17428	20006	22584	25232	27950	30738	33596	36524	39532	42620	45788	49036	52364	55772	59260	62828	66476
110	4068	13273	16241	18468	21166	23814	26532	29320	32178	35106	38104	41182	44340	47578	50896	54294	57772	61330	64968	68686
115	4328	14133	17321	19528	22326	25054	27852	30720	33658	36666	39744	42892	46120	49428	52816	56284	59832	63460	67168	70946
120	4588	15013	18421	20608	23486	26284	29152	32090	35098	38176	41324	44552	47860	51248	54716	58264	61892	65600	69388	73256
125	4848	15913	19521	21708	24646	27504	30452	33410	36428	39506	42654	45882	49190	52578	56046	59594	63232	66950	70748	74626
130	5108	16833	20641	22828	25806	28764	31792	34830	37978	41136	44404	47782	51240	54778	58396	62094	65872	69730	73668	77686
135	5368	17773	21781	24008	27006	29944	33052	36150	39318	42556	45864	49242	52690	56208	59796	63464	67212	71040	74948	78936
140	5628	18733	22941	25208	28206	31104	34252	37400	40618	43896	47234	50632	54090	57608	61186	64834	68552	72350	76228	80186
145	5888	19713	24081	26428	29406	32304	35502	38700	41968	45296	48684	52132	55640	59208	62836	66534	70302	74140	78048	82026
150	6148	20713	25241	27668	30606	33504	36752	39950	43218	46546	49934	53382	56890	60458	64086	67784	71552	75390	79298	83276
155	6408	21733	26421	28908	31806	35004	38252	41450	44718	48046	51434	54882	58390	61958	65586	69274	73032	76860	80758	84726
160	6668	22773	27581	30168	33006	36204	39452	42650	45918	49246	52634	56082	59590	63158	66786	70474	74232	78060	81958	85926
165	6928	23833	28761	31428	34206	37404	40652	43850	47118	50446	53834	57282	60790	64358	67986	71674	75432	79260	83158	87126
170	7188	24913	29941	32708	35406	38604	41802	45000	48258	51576	54954	58392	61890	65448	69066	72744	76482	80280	84148	88086
175	7448	26013	31141	34008	36606	39804	43002	46200	49458	52776	56154	59592	63090	66648	70266	73944	77682	81480	85338	89256
180	7708	27133	32341	35308	37806	41004	44202	47400	50658	53976	57354	60792	64290	67848	71466	75144	78882	82680	86538	90456
185	7968	28273	33541	36608	39206	42404	45602	48800	52058	55376	58754	62192	65690	69248	72866	76544	80282	84080	87938	91856
190	8228	29433	34741	37908	40606	43804	47002	50200	53458	56776	60154	63592	67090	70648	74266	77944	81682	85480	89338	93256
195	8488	30593	35941	39208	42006	45204	48402	51600	54858	58176	61554	64992	68490	72048	75666	79344	83082	86880	90738	94656
200	8748	31773	37141	40508	43406	46604	49802	53000	56258	59576	62954	66392	69890	73448	77066	80744	84482	88280	92138	96056
205	9008	32973	38341	41808	44806	47804	51002	54200	57458	60776	64154	67592	71090	74648	78266	81944	85682	89480	93338	97256
210	9268	34193	39541	43108	46206	49204	52402	55600	58858	62176	65554	68992	72490	76048	79666	83344	87082	90880	94738	98656
215	9528	35433	40741	44408	47606	50604	53802	57000	60258	63576	66954	70392	73890	77448	81066	84744	88482	92180	95938	99756
220	9788	36693	41941	45708	49006	52004	55202	58400	61658	64976	68354	71792	75290	78848	82466	86144	89882	93580	97338	101156
225	10048	37953	43141	47008	50406	53404	56602	59800	63058	66376	69754	73192	76690	80248	83866	87544	91282	95080	98838	102656
230	10308	39233	44341	48308	51806	54804	58002	61200	64458	67776	71154	74592	78090	81648	85266	88944	92682	96480	100238	104056
235	10568	40533	45541	49608	53206	56204	59402	62600	65858	69176	72554	75992	79490	83048	86666	90344	94082	97880	101638	105456
240	10828	41853	46741	50908	54606	57604	60802	64000	67258	70576	73954	77392	80890	84448	88066	91744	95482	99280	103038	106856
245	11088	43193	47941	52208	56006	59004	62202	65400	68658	71976	75354	78792	82290	85848	89466	93144	96882	100580	104338	108156
250	11348	44553	49141	53508	57406	60404	63602	66800	70058	73376	76754	80192	83690	87248	90866	94544	98282	101980	105738	109556

TABLE 10

DEGREE-DAYS OF FROST ASSOCIATED WITH GIVEN DEPTHS OF ICE THICKNESSES AND HEAT LOSSES FOR STICH POWER = 30 cw.

Ice Thickness in m. (L_1)	Heat Loss kg. cal. (Q_1)																
	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	20
0																	
5	176	667	1157	1644	2134	2624	3113	3602	4091	4580	5069	5557	6046	6534	7022	7510	9982
10	353	854	1351	1848	2344	2841	3338	3835	4331	4828	5325	5822	6319	6815	7312	7808	10202
20	734	1243	1753	2262	2772	3282	3791	4301	4810	5320	5830	6339	6849	7358	7868	8377	
30	1128	1651	2173	2696	3218	3741	4263	4786	5308	5830	6353	6875	7398	7920	8442	8965	
40	1512	2077	2612	3147	3683	4218	4753	5289	5824	6359	6894	7430	7965	8500	9036	9571	
50	1973	2522	3070	3618	4166	4714	5262	5810	6358	6906	7454	8003	8551	9099	9647	10195	
60	2424	2981	3535	4086	4641	5196	5751	6306	6861	7416	7971	8526	9081	9636	10191	10746	
70	2882	3466	4040	4611	5188	5762	6335	6909	7483	8057	8631	9204	9778	10352			
80	3337	3968	4593	5210	5826	6441	7057	7673	8289	8904	9519	10134	10749				
90	3805	4455	5081	5694	6303	6913	7522	8131	8740	9349	9958	10567					
100	4409	5022	5634	6247	6859	7472	8084	8696	9308	9920	10532						
110	4952	5577	6203	6828	7453	8078	8703	9328	9953	10578							
120	5513	6151	6789	7428	8067	8706	9345	9984	10623								
130	6093	6744	7395	8046	8697	9348	9999										
140	6691	7355	8019	8683	9347	10011	10674										
150	7308	7985	8661	9338	10015												
160	7943	8633	9322	10012													
170	8587	9300	10002														
180	9270	9985															
190	9960	10688															
200	10670																

TABLE 11
DEGREE-DAYS OF FROST ASSOCIATED WITH GIVEN ICE THICKNESSES AND HEAT LOSSES FOR SNOW COVER = 10 cm.

Ice Thickness in cm. (I_1)	Heat Loss kg. cal. (Q_m)															
	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	645	1290	1936	2581	3226	3871	4516	5161	5806	6452	7097	7742	8387	9032	9677
5	235	396	1538	2189	2841	3492	4144	4796	5447	6099	6750	7402	8054	8705	9357	10008
10	474	1132	1790	2448	3106	3764	4422	5080	5738	6396	7054	7712	8370	9028	9686	
20	966	1637	2308	2979	3649	4320	4991	5662	6333	7004	7675	8346	9016	9687	10358	
30	1477	2451	2844	3528	4212	4895	5579	6263	6947	7630	8314	8998	9681	10365		
40	2006	2703	3399	4096	4792	5489	6186	6882	7579	8275	8972	9669	10365			
50	2554	3264	3973	4682	5392	6101	6811	7520	8229	8939	9648	10358				
60	3120	3843	4565	5287	6009	6732	7454	8176	8899	9621	10343					
70	3705	4440	5175	5910	6646	7381	8116	8851	9586	10321						
80	4308	5056	5804	6552	7300	8048	8796	9544	10292							
90	4930	5691	6452	7213	7974	8734	9495	10256								
100	5571	6344	7118	7892	8665	9439	10213									
110	6230	7016	7803	8589	9376	10162										
120	6907	7706	8506	9305	10104											
130	7603	8415	9227	10040												
140	8317	9142	9967													
150	9050	9888	10726													
160	9802	10652														
170	10571															

TABLE 12
 DEGREE-DAYS OF FROST ASSOCIATED WITH GIVEN ICE THICKNESSES AND HEAT LOSSES FOR SNOW COVER = 50 cm.

Ice Thickness in g. (I _f)	Heat Loss kg. cal. (Q _f)													
	0	1	2	3	4	5	6	7	8	9	10	11	12	13
0	0	806	1612	2419	3226	4032	4839	5645	6452	7259	8064	8871	9677	10484
5	293	1105	1918	2731	3544	4357	5170	5983	6796	7608	8421	9234	10047	
10	590	1409	2228	3048	3867	4686	5506	6325	7144	7964	8783	9602		
20	1198	2030	2837	3695	4527	5359	6191	7023	7856	8688	9520	10352		
30	1825	2670	3515	4360	5205	6050	6895	7740	8585	9430	10275			
40	2471	3328	4186	5044	5902	6760	7618	8476	9334	10191				
50	3135	4005	4876	5747	6613	7488	8359	9230	10100					
60	3817	4701	5584	6468	7351	8235	9118	10002						
70	4518	5414	6311	7207	8104	9000	9896							
80	5238	6147	7056	7965	8875	9784	10693							
90	5975	6898	7820	8742	9664	10586								
100	6732	7667	8602	9537	10472									
110	7507	8455	9403	10350										
130	8300	9261	10222											
150	9112	10086												
170	9943													
190	10792													

TABLE 13

DEGREE-DAYS OF FROST FOR DIFFERING HEAT LOSS AND ICE THICKNESS $\left(\frac{Q_T - 1.1}{2k_i}\right)$

Ice Thickness (in.)	Heat Loss (Kg. Cal.)														
	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
5	6	13	19	26	32	39	45	51	58	64	71	77	84	90	96
10	13	26	39	51	64	77	90	103	116	129	141	154	167	180	193
20	26	51	77	103	129	154	180	206	231	257	283	308	334	360	386
30	39	77	116	154	193	231	270	308	347	386	424	462	501	540	578
40	51	103	154	207	257	308	360	411	463	514	566	617	668	720	771
50	64	129	193	257	321	386	450	514	578	643	707	771	835	900	964
60	77	154	231	308	386	463	540	617	694	771	848	925	1003	1080	1157
70	90	180	270	360	450	540	630	720	810	900	990	1080	1170	1260	1350
80	103	206	308	411	514	617	720	823	925	1029	1131	1234	1337	1440	1542
90	116	231	347	463	578	694	810	925	1041	1157	1272	1388	1504	1620	1735
100	129	257	386	514	643	771	900	1029	1157	1285	1414	1542	1671	1799	1928
110	141	283	424	566	707	848	990	1131	1272	1414	1555	1697	1838	1979	2121
120	154	308	463	617	771	925	1080	1234	1388	1542	1697	1851	2005	2159	2314
130	167	334	501	668	835	1003	1170	1337	1504	1671	1838	2005	2172	2339	2506
140	180	360	540	720	900	1080	1260	1440	1620	1799	1979	2159	2339	2519	2699
150	193	386	578	771	964	1157	1350	1542	1735	1928	2121	2314	2506	2699	2892
160	206	411	617	823	1029	1234	1440	1645	1851	2057	2262	2468	2674	2879	3085
170	219	437	656	874	1093	1311	1530	1748	1967	2185	2404	2622	2841	3059	3278
180	231	463	694	925	1157	1388	1640	1851	2082	2314	2545	2776	3008	3239	3470
190	244	488	733	977	1221	1465	1710	1954	2198	2442	2686	2931	3175	3419	3663
200	257	514	771	1028	1285	1542	1799	2057	2314	2571	2828	3085	3342	3599	3856
210	270	540	810	1080	1350	1620	1889	2159	2429	2699	2969	3239	3509	3779	4049
220	283	566	848	1131	1414	1697	1979	2262	2545	2828	3111	3393	3676	3959	4242
230	296	591	887	1183	1478	1774	2069	2365	2661	2956	3252	3548	3843	4139	4434
240	308	617	925	1234	1542	1851	2159	2468	2776	3085	3393	3702	4010	4319	4627
250	321	643	964	1285	1607	1928	2249	2570	2892	3213	3535	3856	4177	4499	4820
260	334	668	1003	1347	1671	2005	2339	2674	3008	3342	3676	4010	4344	4679	5013
270	347	694	1041	1388	1735	2082	2429	2776	3123	3470	3817	4165	4512	4859	5206
280	360	720	1080	1440	1799	2159	2519	2879	3239	3599	3959	4319	4679	5039	5398
290	373	746	1118	1491	1864	2237	2609	2982	3355	3728	4100	4473	4856	5219	5591
300	386	771	1157	1542	1928	2314	2699	3085	3470	3856	4242	4627	5013	5398	5784

BIBLIOGRAPHY

BROWN, A. L. An analytical method of ice potential calculation. U. S. Hydrographic Office, Technical Report 5. Washington. September 1954. 13p.

DEFANT, A. Konvektion und Eisbereitschaft in polaren Schelfmeeren (Convection and ice formation in polar shelf seas), Geografiska Annaler, Arg. 31, pp. 25-35, 1949.

JACOBS, W. C. On the energy exchange between sea and atmosphere, Journal of Marine Research, Vol. 5, pp. 37-66, 1942.

ZUBOV, N. N. Morskoe vody i l'dy (Marine water and ice). Moskva: Gidrometeorologicheskoe Izdatel'stvo, 1938. 451p.



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Growth

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iii. H. O. TR-4

U. S. Navy Hydrographic Office
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