



UNIVERSITY OF
ILLINOIS LIBRARY
AT URBANA-CHAMPAIGN
STACKS


Faculty Working Papers

REAL VS. NOMINAL RATES OF RETURN MATRICES
IN PORTFOLIO MANAGEMENT: A STATISTICAL
ANALYSIS

Cheng F. Lee and Jack C. Lee

#422

College of Commerce and Business Administration
University of Illinois at Urbana-Champaign



Digitized by the Internet Archive
in 2011 with funding from
University of Illinois Urbana-Champaign

FACULTY WORKING PAPERS

College of Commerce and Business Administration

University of Illinois at Urbana-Champaign

July 20, 1977

**REAL VS. NOMINAL RATES OF RETURN MATRICES
IN PORTFOLIO MANAGEMENT: A STATISTICAL
ANALYSIS**

Cheng F. Lee and Jack C. Lee

#422

...and the model-building process is a process of discovery. The model-building process is a process of discovery. The model-building process is a process of discovery.

...and the model-building process is a process of discovery. The model-building process is a process of discovery. The model-building process is a process of discovery.

REAL VS. NOMINAL RATES OF RETURN MATRICES IN
PORTFOLIO MANAGEMENT: A STATISTICAL ANALYSIS

by

Cheng F. Lee

Associate Professor of Finance
University of Illinois at Urbana-Champaign

and

Jack C. Lee

Associate Professor of Mathematics
Wright State University

ABSTRACT

Possible methods for testing the statistical relationships between nominal and real matrices in portfolio managements are explored. An exact relationship between real correlation coefficients and nominal correlation coefficients is derived to show the importance of real correlation coefficients for determining the diversification effect in the portfolio management.

I. Introduction

Kennedy (1960), Bodie (1976), Brian (1969), Johnson, Reilly and Smith (1971) [JRS], Hendershott and Van Horne (1973), Ondet (1973), Reilly, Smith and Johnson (1975) [RSJ] and others have shown that there exist some important impacts of inflation on common stock values and bond rates. Therefore, the impact of inflation on portfolio analysis is of interest to security analysts. Under a Markowitz algorithm [see Markowitz (1959)], information associated with both estimated covariance matrix and estimated correlation matrix is generally used to select the efficient portfolio. To investigate the possible effect of inflation on the portfolio selection, Sarnat (1973) and Biger (1975, 1976) have done some empirical studies to demonstrate how the portfolio selection can be affected by the inflation factor. However, none of these studies has statistically tested their empirical results.

The main purposes of this paper are: to examine the problem of testing the equality between nominal and real covariance matrices, and to investigate the possibility of testing the equality between nominal and real correlation matrices. The relationship between the real and the nominal correlation coefficients is also derived under a relative general condition. In the second section, the existing method of testing the equality between nominal and real covariance matrices is discussed; the problem associated with the existing method is demonstrated. In the third section the statistical relationship between real and nominal correlation coefficients are derived. Some implications associated with this relationship are explored. Possible methods of testing the equality between

nominal and real correlation matrices are examined and criticized. In the fourth section an alternative method based upon the asymptotic distribution of a sample correlation coefficient is used to re-examine Biger's conclusions associated with testing the relationship between nominal and real correlation matrices. The relative advantage of Biger's (1975, 1976) method of investigating the impact of inflation on portfolio selection relative to that of Sarnat's (1973) method is explored. Finally, results of this paper are summarized. Some concluding remarks are indicated.

II. The Relationship Between Real and Nominal Covariance Matrices

Based upon multivariate log normal assumption, Biger (1975, 1976) defined the relationship between the nominal and real rates of return on security in terms of logarithmic transformation as:

$$\tilde{R}_j^* = \log(\tilde{R}_j) - \log(\tilde{P}) = \tilde{r}_j - \tilde{p} \quad (1)$$

Where $\tilde{R}_j = 1 +$ nominal rates of return on j^{th} security

$\tilde{P} = 1 +$ inflation rate

$\tilde{R}_j^* =$ real rates of return on j^{th} security.

Given the definition of the real rate of return and the nominal rate of return, the variance of \tilde{R}_j^* and the convenience between \tilde{R}_j^* and \tilde{R}_i^* can be defined as:

$$\begin{aligned} \text{a) } \text{Var}(\tilde{R}_j^*) &= \text{Var}(\tilde{r}_j) + \text{Var}(\tilde{p}) - 2 \text{Cov}(\tilde{r}_j, \tilde{p}) \\ \text{b) } \text{Cov}(\tilde{R}_j^*, \tilde{R}_i^*) &= \text{Cov}(\tilde{r}_j, \tilde{r}_i) - \text{Cov}(\tilde{r}_j, \tilde{p}) - \text{Cov}(\tilde{r}_i, \tilde{p}) + \text{Var}(\tilde{p}) \end{aligned} \quad (2)$$

If the real rates of return is independent of the inflation,¹ then equation (2) can be rewritten as:

¹This kind of assumption has been used by Roll (1973), Hagerman and Kim (1976) and others.

$$\begin{aligned} \text{a) } \text{Var} (\tilde{R}_j^*) &= \text{Var} (\tilde{r}_j) - \text{Var} (\tilde{p}) \\ \text{b) } \text{Cov} (\tilde{R}_j^*, \tilde{R}_i^*) &= \text{Cov} (\tilde{r}_j, \tilde{r}_i) - \text{Var} (\tilde{p}) \end{aligned} \quad (3)$$

This implies that the real covariance matrix (RCM) is generally not equal to the nominal covariance matrix (NCM) unless the variance of inflation is zero.

To test whether the RCM is statistically significantly different from NCM, Anderson's (1958) approximate χ^2 statistic can be used to perform the test. To show the possible problem associated with using approximate χ^2 statistic in testing the equality between the nominal and real covariance matrices, the approximate χ^2 statistic is briefly described as follows.

Following Anderson (1958, Chapter 10), to test the equality of q covariance matrices, the null hypothesis can be defined as:

$$H_0: \Sigma_1 = \dots = \Sigma_i \dots = \Sigma_q \quad (4)$$

In equation (4), Σ_i ($i = 1, 2, \dots, q$) indicates the covariance matrix associated with i^{th} population. The testing statistic with approximate χ^2 distribution for the null hypothesis test of (4) can be defined as:

$$T = -2\rho \log W_1 \quad (5)$$

Where ρ is the function of the sample size and the dimension of the covariance matrix; W_1 is the function of sample size, dimension of covariance matrices and the determinants of covariance matrices.²

The approximate χ^2 distribution of T is derived under the assumption that the covariance matrices are from q independent populations. Now we

²See Anderson (1958, pp. 247-256) for detail.

will examine whether the nominal rates of return is independent of the real rates of return. Let $X = \tilde{R}^*$ and $Y = \tilde{P}$. If $X \sim N(\mu_1, \sigma_1^2)$, $Y \sim N(\mu_2, \sigma_2^2)$ and X and Y are independent. Then the joint density function of X and Y is:

$$f(X, Y) = (2\pi)^{-1} (\sigma_1^2)^{-\frac{1}{2}} (\sigma_2^2)^{-\frac{1}{2}} \exp \left[-\frac{1}{2\sigma_1^2} (X-\mu_1)^2 - \frac{1}{2\sigma_2^2} (Y-\mu_2)^2 \right] \quad (6)$$

From equation (1), the nominal rates of return is defined as:

$$W = X + Y \quad (7)$$

Then the joint distribution of W and Y is:

$$g(W, y) = (2\pi)^{-1} (\sigma_1^2)^{-\frac{1}{2}} (\sigma_2^2)^{-\frac{1}{2}} \exp \left[-\frac{1}{2\sigma_1^2} (W-y-\mu_1)^2 - \frac{1}{2\sigma_2^2} (y-\mu_2)^2 \right] \quad (8)$$

Since $g(W/y) \propto g(W, y)$ and the conditional distribution of W given y is $N(y + \mu_1, \sigma_1^2)$. But the marginal distribution of $W = X + Y$ is $N(\mu_1 + \mu_2, \sigma_1^2 + \sigma_2^2)$.

Hence: $g(W/y) \neq g(W)$

Thus, it can be concluded that W is not independent of Y . In other words, the real rates of return is generally not independent of the nominal rates of return. Therefore, the approximate χ^2 method of (5) is not an appropriate method for testing the equality between the real covariance matrix and the nominal covariance matrix.

III. The Relationship Between Real and Nominal Correlation Matrices and its Implications

If the real rates of return are independent of the inflation as indicated in (3), then the nominal correlation coefficient can be defined as:

$$\rho_{i,j} = \frac{\text{Cov}(\tilde{r}_i, \tilde{r}_j)}{\sqrt{\text{Var}(\tilde{r}_i) \cdot \text{Var}(\tilde{r}_j)}} \quad (9)$$

The real correlation coefficient can be defined as:

$$\rho_{i.j}^* = \frac{\text{Cov}(\tilde{r}_i, \tilde{r}_j) - \text{Var}(\tilde{p})}{\sqrt{[\text{Var}(\tilde{r}_i) - \text{Var}(\tilde{p})] \cdot [\text{Var}(\tilde{r}_j) - \text{Var}(\tilde{p})]}} \quad (10)$$

It can be shown that the relative magnitude between ρ^* and ρ can be determined by the magnitude of $\text{Var}(\tilde{p})$, i.e.³

$$\text{Var}(\tilde{p}) \begin{cases} > \\ < \end{cases} \rho_{i.j}^* \begin{cases} > \\ < \end{cases} \rho_{i.j} \quad \text{when} \\ \text{Var}(\tilde{p}) \begin{cases} \geq \\ \leq \end{cases} \frac{2 \text{Cov}(\tilde{r}_i, \tilde{r}_j) - \rho_{i.j}^2 \text{Var}(\tilde{r}_i) - \rho_{i.j}^2 \text{Var}(\tilde{r}_j)}{1 - \rho_{i.j}^2} \quad (11)$$

Equation (11) implies that the real correlation coefficient is not necessarily equal to the nominal correlation coefficient. To test the equality between ρ^* and ρ , it is shown that Anderson's (1958) Z approximate statistic for testing the equality of two simple correlation coefficients as defined in (12) can be used to test the statistical relationship between $\rho_{i.j}^*$ and $\rho_{i.j}$.

$$Z = \frac{(Z_1 - Z_2)}{\sqrt{\frac{1}{(n_1-3)} + \frac{1}{(n_2-3)}}} \quad (12)$$

Where

$$Z_1 = \frac{1}{2} \log \left[\frac{1 + \hat{\rho}_{i.j}^*}{1 - \hat{\rho}_{i.j}^*} \right]; \quad Z_2 = \frac{1}{2} \log \left[\frac{1 + \hat{\rho}_{i.j}}{1 - \hat{\rho}_{i.j}} \right]$$

and n_1 and n_2 are the sample sizes associated with $\hat{\rho}_{i.j}^*$ and $\hat{\rho}_{i.j}$ respectively.

Now, it is shown that the approximate Variance of $(Z_1 - Z_2)$ is $\left[\frac{1}{n_1-3} + \frac{1}{n_2-3} \right]$. According to the definition of variance,

³See Appendix (A) for the derivation of this relationship.

$$\text{Var} (Z_1 - Z_2) = \text{Var} (Z_1) + \text{Var} (Z_2) - 2 \text{Cov} (Z_1, Z_2) \quad (13)$$

Following Anderson (1958, Chapter 2), equation (13) can be rewritten as:

$$\text{Var} (Z_1 - Z_2) = \frac{1}{n_1-3} + \frac{1}{n_2-3} - 2 \text{Corr} (Z_1, Z_2) \left[\frac{1}{n_1-3} \right] \left[\frac{1}{n_2-3} \right] \quad (13)'$$

As $\text{Corr} (Z_1, Z_2)$ is between -1 and 1, the second term of (13)' is of order $O(n^{-2})$ and hence asymptotically negligible. Therefore, the approximate

Variance of $(Z_1 - Z_2)$ is $\left[\frac{1}{n_1-3} + \frac{1}{n_2-3} \right]$.

A generalized multivariate distribution method for testing the equality of two correlation matrices is still not available. However, if two sample statistics are obtained from two independent populations, we can test the equality of two correlation matrices by testing the equality of two covariance matrices. Besides the approximate χ^2 test as discussed in the previous section, Lee, Chang and Krishnaiah (1976) have derived the likelihood ratio test tables for testing the equality of two covariance matrices. As the real covariance matrix and nominal covariance matrix are not from two independent populations. The method of testing of covariance matrices can not be used to test the equality of correlation matrices. Furthermore, it can be shown that the equality of covariance matrix implies the equality of correlation matrices. However, the inequality of covariance matrices does not necessarily imply the inequality of correlation matrices.⁴

Now, the implications of the relationship between real and nominal correlation coefficients are discussed. The magnitude and the sign of the correlation coefficient among securities are generally used to determine the degree of diversification associated with a portfolio analysis. If the

⁴See Appendix (B) for the proof.

real rates of return instead of the nominal rates of return are concerned by the investors, then the real correlation coefficient instead of nominal correlation coefficient should be used to analyze the diversification effect. If the nominal correlation coefficient is not equal to the real correlation coefficient, then the diversification effect estimated by the nominal correlation coefficient will be biased. Therefore, it is of importance to test whether the nominal correlation coefficient is equal to the real correlation coefficient in the portfolio management. A portfolio manager can use the relationship defined either in equation (11) or in equation (12) to perform the empirical test.

Equation (11) indicates that the magnitude of variance associated with inflation is an important factor in determining the relationship between real correlation coefficient and nominal correlation coefficient. It is well-known that the variance associated with inflation is essentially determined by the economic condition and the stage of business cycle. Hence, the portfolio management based upon real instead of nominal rates of return can more explicitly take impact of business cycle on portfolio management into account. In investigating the causal relationship between stock market index and other economic indicators--GNP, inflation rate and money supply. Kraft and Kraft (1977) found that only inflation rate has direct causal impact on the change of stock market index. This finding has reinforced the importance of using real instead of nominal rates of return in the portfolio management.

IV. Re-examine Biger and Sarnat's Studies

In accordance with the definition of correlation coefficient, both Biger (1975, 1976) and Sarnat (1973) have calculated nominal correlation coefficient

matrix, N , and real correlation coefficient matrix, R . To test the relationship between these two correlation matrices, Biger postulated a 16×16 transformation T_1 and defined a relationship as:⁵

$$N \times T_1 = R \quad (14)$$

Using the relationship of equation (14), he posited two alternative hypotheses for T_1 , i.e. (i) T_1 is either an identity matrix or a scale matrix, and, (ii) T_1 is neither an identity matrix nor a scale matrix. If the first hypothesis is true, then he would conclude that the inflation will have no impact on the portfolio selection. However, he found that the second hypothesis was true. Therefore, he concluded that inflation generally affects the portfolio selection. Now we will examine the possible problems faced by Biger in testing the relationship between N and R . To test his two alternative hypotheses, he calculated the transformation matrix by using the relationship as defined in equation (15).

$$T_1 = N^{-1}R \quad (15)$$

After comparing the elements in T_1 , he concluded that the transformation matrix T_1 is far from being close to either identity matrix or constant matrix.⁶ Biger's method of testing the relationship between N and R is subject to following three criticisms, i.e. (i) his method is a mathematical instead of a statistical method, (ii) his results are sensitive to the degree of singularity of N matrix, and (iii) T_1 is not a

⁵In his JFQA article, Biger used the rates of return of 16 industries to calculate N and R . However, he used only 15 industries in his JF paper.

⁶In his JFQA study, he found that the transformation matrix contains values as high as 648.6 and as low as -559.6.

symmetric matrix. The last criticism can be proved by transposing T_1 matrix as follows. From (15) we know that:

$$T_1' = (N^{-1}R)' = R' (N^{-1})' = R'N^{-1} \quad (16)$$

As $N^{-1}R$ is generally not equal to $R'N^{-1}$, therefore, the T_1' is not a symmetric matrix.

Using the formula given by equation (12), the z statistics are calculated for the pairwise nominal and real correlation coefficients, and the results are listed in table 1.⁷ From the z statistics listed in table 1, it is found that there exists no nominal correlation coefficient which is statistically different from the real correlation coefficient. This implies that the nominal correlation matrix is not significantly different from the real correlation matrix.⁸ This finding is similar to Sarnat's (1973) finding.

Besides testing the equality of two correlation matrices, Biger (1975, 1976) also derived the efficient frontiers by using both nominal and real rates of return. He has concluded that the portfolio constructed by using real rates of return is more efficient than that obtained from nominal rates of return. It would be noted that both nominal and real monthly T-Bill rates are included in Biger's portfolio selection. It has been shown that the impacts of inflation on rates of return on equity are generally different from that on the rates of return on Treasury Bill.

⁷These z statistics are calculated by using Biger's JFQA data. Z statistics also are calculated by using his JF data, the conclusions are identical with what we have here.

⁸As the individual elements of nominal correlation matrix are pairwise equal to the individual elements of real correlation matrix, the nominal correlation matrix will be equal to the real correlation matrix.

TABLE 1 z STATISTICS

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
1.	0															
2.	.04945	0														
3.	.06827	.06187	0													
4.	.06410	.06558	.04818	0												
5.	.01195	.04321	.07839	.07383	0											
6.	.02138	.02715	.09841	.10965	.06317	0										
7.	.08974	.08227	.04829	.06460	.08177	.09314	0									
8.	.04976	.04632	.01661	.02125	.03835	.03295	.01422	0								
9.	.00754	.02486	.03019	.01197	.00164	.01338	.04966	.02423	0							
0.	.02722	.00365	.04179	.03616	.02624	.00902	.05165	.01301	.03330	0						
1.	.29866	.58730	.04359	1.36763	.77569	.97307	.05921	.01474	.57636	1.56107	0					
2.	.06815	.08180	.06461	.06624	.08018	.07530	.06995	.02904	.01624	.02464	.98454	0				
3.	.06285	.06559	.02922	.04088	.06180	.20306	.03690	.00260	.03553	.04200	.54440	.04684	0			
4.	.00068	.02182	.04820	.03998	.00592	.02197	.05112	.02213	.00249	.01619	.03176	.03957	.04079	0		
5.	.01823	.02249	.05552	.04783	.01624	.06911	.06876	.03577	.00230	.02611	.60477	.04469	.05527	.00782	0	
6.	.06888	.12177	.08082	.11139	.04033	.00795	.05252	.11274	.02371	.04033	.10484	.10689	.01786	.03355	.00351	0

This argument is essentially based upon the theory that the "Fisher Effect" is applicable to analyze the impact of inflation on rates of return on Treasury Bill and is not necessarily applicable to analyze the impact of inflation on rates of return on common equity.⁹ In sum, the different conclusions drawn by Biger and Sarnat on the relationship between inflation and portfolio selection may well be due to the fact that Biger (1975, 1976) instead of Sarnat (1973) treated Treasury Bill rates of return as one of the risky assets.

Now, the advantage of including Treasury Bills in the portfolio is analyzed. If one assumes that index-linked T-Bills are available, and that their return is r_f^* , then it can be shown that the yield on nominal T-Bills is:¹⁰

$$r_{TB} = r_f^* + \beta_f [E(r_m^*) - (r_f^*)] \quad (17)$$

Where r_m^* is the real market rate of return; β_f is the systematic risk of the nominal T-Bills, or their non-diversifiable purchasing power risk.

This coefficient is equal to

$$\beta_f = \frac{\text{Var}(\tilde{p}) - \text{Cov}(\tilde{r}_m^*, \tilde{p})}{\text{Var}(\tilde{r}_m) + \text{Var}(\tilde{p}) - 2 \text{Cov}(\tilde{r}_m^*, \tilde{p})} \quad (18)$$

Equation (18) indicates that $\beta_f \neq 0$ even if $\text{Cov}(\tilde{r}_m^*, \tilde{p}) = 0$, hence the yield on nominal T-Bills would include risk premium even if $E(\tilde{p}) = 0$. Thus, in markets which are dominated by expected utility maximizers who have no "money illusion", then nominal Treasury Bills are risky. Under this circumstance, the Treasury Bill should be treated as one of the risky assets in selecting efficient portfolio. Thus, Biger's (1975, 1976)

⁹ See Jaffe and Mandelker (1976) for detail.

¹⁰ This relationship is based upon the capital asset pricing model developed by Sharpe (1964), Lintner (1965) and Mossin (1966).

proach in investigating the impact of inflation on portfolio selecting more acceptable relative to that used by Sarnat (1973).

Summary and Concluding Remarks

This paper has investigated the possible problems of testing real and nominal matrices in portfolio analysis. It is shown that real rates of return are generally not independent of nominal rates of return and the approximate χ^2 technique is not suitable for testing the relationship between nominal and real matrices. To resolve this problem, the exact relationship between the nominal correlation coefficient and real correlation coefficients is derived. In addition, it is also shown that the approximate statistic can be used to test the equality between real and nominal correlation coefficients. Furthermore the relative advantage of including Treasury Bill rates of return in the portfolio selection is also analyzed in accordance with the capital asset pricing theory and the effect of inflation on rates of return on common equity and Treasury bond.

The degree of stability of portfolio components over time based on real rates of return relative to those based upon nominal rates of return should be investigated in the future research in the portfolio managements. In addition, it is very worthwhile to note that a generalized method for testing the statistical relationship between real and nominal matrices should be developed to improve the portfolio management under a economic environment with non-negligible unexpected inflation.

APPENDIX A

From equations (9) and (10), the relationship between $\rho_{i \cdot j}^*$ and $\rho_{i \cdot j}$ can be written as:

$$\rho_{i \cdot j}^* = \rho_{i \cdot j} \frac{1 - \frac{\text{Var}(\tilde{p})}{\text{Cov}(\tilde{r}_i, \tilde{r}_j)}}{\sqrt{\left(1 - \frac{\text{Var}(\tilde{p})}{\text{Var}(\tilde{r}_i)}\right) \left(1 - \frac{\text{Var}(\tilde{p})}{\text{Var}(\tilde{r}_j)}\right)}} \quad [A]$$

From equation [A], the relationship between $\rho_{i \cdot j}^*$ and $\rho_{i \cdot j}$ can be analyzed as follows:

$\rho_{i \cdot j}^* \geq \rho_{i \cdot j}$ implies that

$$\frac{1 - \frac{\text{Var}(\tilde{p})}{\text{Cov}(\tilde{r}_i, \tilde{r}_j)}}{\sqrt{\left(1 - \frac{\text{Var}(\tilde{p})}{\text{Var}(\tilde{r}_i)}\right) \left(1 - \frac{\text{Var}(\tilde{p})}{\text{Var}(\tilde{r}_j)}\right)}} \geq 1 \quad [B]$$

Equation [B] implies that:

$$1 - 2 \frac{\sigma_p^2}{\rho_{i \cdot j} \sigma_i \sigma_j} + \frac{\sigma_p^4}{\rho_{i \cdot j}^2 \sigma_i^2 \sigma_j^2} \geq 1 - \frac{\sigma_p^2}{\sigma_i^2} - \frac{\sigma_p^2}{\sigma_j^2} + \frac{\sigma_p^4}{\sigma_i^2 \sigma_j^2} \quad [C]$$

Where $\sigma_p = \text{Var}(\tilde{p})$, $\sigma_i = [\text{Var}(\tilde{r}_i)]^{\frac{1}{2}}$ and $\sigma_j = [\text{Var}(\tilde{r}_j)]^{\frac{1}{2}}$. Equation [C] implies that:

$$\sigma_p^2 \left[\frac{\sigma_p^2 - 2 \rho_{i \cdot j} \sigma_i \sigma_j}{\rho_{i \cdot j} \sigma_i^2 \sigma_j^2} \right] \geq \sigma_p^2 \left[\frac{\sigma_p^2 - \sigma_i^2 - \sigma_j^2}{\sigma_i^2 \sigma_j^2} \right] \quad [D]$$

After some arrangements, we know that equation [D] implies that:

$$\sigma_p^2 \geq \frac{2 \rho_{i \cdot j} \sigma_i \sigma_j - \rho_{i \cdot j}^2 \sigma_i^2 - \rho_{i \cdot j}^2 \sigma_j^2}{1 - \rho_{i \cdot j}^2} \quad [E]$$

Equation [E] can be used to determine the relationship between real correlation coefficient and nominal correlation coefficient.

APPENDIX B

If two by two covariance matrices V and V' are defined as:

$$V = \begin{pmatrix} \sigma_1^2 & \rho \sigma_1 \sigma_2 \\ \rho \sigma_1 \sigma_2 & \sigma_2^2 \end{pmatrix}, \quad V' = \begin{pmatrix} \sigma_1'^2 & \rho' \sigma_1' \sigma_2' \\ \rho' \sigma_1' \sigma_2' & \sigma_2'^2 \end{pmatrix}$$

and the correlation matrices associated with C_1 and C_2 are defined as:

$$R = \begin{pmatrix} 1 & \rho \\ \rho & 1 \end{pmatrix}, \quad R' = \begin{pmatrix} 1 & \rho' \\ \rho' & 1 \end{pmatrix}$$

If $V = V'$, then $\sigma_1^2 = \sigma_1'^2$, $\sigma_2^2 = \sigma_2'^2$, and $\rho \sigma_1 \sigma_2 = \rho' \sigma_1' \sigma_2'$.

These equalities imply that $\rho = \rho'$. Hence $R = R'$. However, if $R = R'$, then V will not equal to V' unless $\sigma_1 = \sigma_1'$ and $\sigma_2 = \sigma_2'$.

REFERENCES

1. Anderson, T.W. (1958). An Introduction to Multivariate Statistical Analysis. New York: John Wiley & Sons Inc.
2. Biger, N. (1976), "Portfolio Selection and Purchasing Power Risk-- Recent Canadian Experiences," Journal of Financial and Quantitative Analysis, 11, pp. 251-267.
3. Biger, N. (1975), "The Assessment of Inflation and Portfolio Selection," Journal of Finance, 30, pp. 451-467.
4. Bodie, Z. (1976), "Common Stocks as Hedge against Inflation," Journal of Finance, 31, pp. 459-470.
5. Brian, M. (1969), "Inflation and Common Stock Values," Journal of Finance, 24, pp. 530-535.
6. Hagerman, R.L. and E.H. Kim (1976), "Capital Asset Pricing with Price Level Change," Journal of Financial and Quantitative Analysis, 11, pp. 381-391.
7. Hendershott, P.H. and J.C. Van Horne (1973), "Expected Inflation Implied by Capital Market Rates," Journal of Finance, 28, pp. 301-314.
8. Jaffe, J.F. and G. Mandelker (1976), "The 'Fisher Effect' for Risky Assets: An Empirical Investigation," Journal of Finance, 31, pp. 447-458.
9. Johnson, Glenn L., Frank K. Reilly and Ralph E. Smith (1971), "Individual Common Stocks and Inflation Hedges," Journal of Financial and Analysis, 6, pp. 1015-1024.
10. Kennedy, Charles (1960), "Inflation and the Bond Rate," Oxford Economic Papers, 12, pp. 269-274.
11. Kraft J. and A. Kraft (1977), "Common Stock Price: Some Observation," Southern Economic Journal, 27, pp. 294-298.
12. Lintner, J. (1965), "Security Prices, Risk, and Maximal Gains from Diversification," Journal of Finance, 20, pp. 587-616.
13. Markowitz, H. (1959). Portfolio Selection: Efficient Diversification of Investments, New York, John Wiley and Sons.
14. Mossin, J. (1966), "Equilibrium in a Capital Asset Market," Econometrica, 34, pp. 768-783.
15. Lee, J.C., T.C. Chang and P.R. Krishnaiah (1976), "Approximations to the Distributions of the Likelihood Ratio Statistics for Testing Certain Structures on the Covariance Matrices of Real Multivariate Normal Populations," Multivariate Analysis IV, P.R. Krishnaiah, ed., North-Holland, In. Press.

16. Oudet, B.A. (1973), "The Variation of the Return on Stocks in Periods Inflation," Journal of Financial Quantitative Analysis, pp. 247-258.
17. Reilly, Frank K., Ralph E. Smith and Glenn L. Johnson (1975), "A Correction and Update Regarding Individual Common Stocks as Inflation Hedges," Journal of Financial and Quantitative Analysis, 10, pp. 871-880.
18. Roll, Richard (1973), "Assets, Money, and Commodity Price Inflation Under Uncertainty," Journal of Money, Credit and Banking.
19. Sarnat, M. (1973), "Inflation and Portfolio Selection," paper presented to the XX International Meeting of the Institute of Management Sciences, Israel (June, 1973).
20. Sharpe, W.F. (1964), "Capital Asset Prices: A Theory of Market Equilibrium Under Condition of Risk," Journal of Finance, 19, pp. 425-442.



UNIVERSITY OF ILLINOIS-URBANA



3 0112 060296503