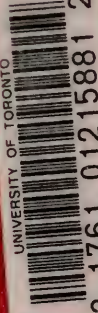



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A TREATISE

ON

PLANE AND SPHERICAL
TRIGONOMETRY.

BY

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UNIVERSITY OF KANSAS.



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PREFACE.

THIS *Treatise on Trigonometry* has been written for use primarily in the classes of the University of Kansas.

Throughout its entire preparation constant reference has been made to the works of Serret, Lonchampt, Young, Airy, Hind, Beasley, Todhunter, Newcomb, Chauvenet, Olney, "Oliver, Wait, and Jones," Wheeler, Peirce, Loomis, and others. The source of the material is to some extent to be found in those authors. The matter and the methods of presentation are designed to enable the student to become thoroughly acquainted with the principles and applications of Trigonometry; and care has been taken to render the demonstrations of the fundamental propositions as clear and as concise as possible, without in the least affecting their logical accuracy.

In this volume the theory of the science is based upon the analytic method, and every practical formula is illustrated by examples of numerical computation. The *Sets of Examples* given are believed to be sufficient for all practical purposes, furnishing abundance, as well as variety, of work.

The author is under obligations to Professor Webster Wells, of the Massachusetts Institute of Technology, for the Tables that appear in this volume.

Special acknowledgments are due Mr. H. B. Newson, Assistant in Mathematics, for a careful review of the manuscript, and for suggestions made.

E. MILLER,

University of Kansas.

JULY, 1894.

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TRIGONOMETRY.

CHAPTER I.

INTRODUCTION.

1. *Trigonometry* is a branch of Mathematics, and comprises all investigations relating to the numerical computation of angles and triangles.

2. *Plane Trigonometry* treats of the solution of plane triangles. It also includes the investigation of all the relations of angles, constituting the *Angular Analysis*, or *Analytical Trigonometry*.

3. *Measurement of Angles.* The *unit* of angular measurement is an angle of one degree.

A *degree* is *one-ninetieth* of a right angle, or of a quadrant of a circle.

Fractional parts of a degree are represented by *minutes* and *seconds*; thus,

$$\text{one minute} = \frac{1}{60} \text{ of a degree;}$$

$$\text{one second} = \frac{1}{60} \text{ of a minute.}$$

4. Symbols are used to designate degrees, minutes, and seconds. An angle or arc of 30 degrees, 35 minutes, 50 seconds, is written $30^{\circ} 35' 50''$. To compute angles or arcs by degrees, minutes, and seconds, is called the *sexagesimal* method, and is in common use.

5. The *centesimal* method consists in dividing a right angle into 100 equal parts, called *grades*; a grade into 100 equal parts, called *minutes*; and a minute into 100 equal parts, called *seconds*.

6. The ordinary conception of an angle, that it must be less than two right angles, is sufficient for geometric purposes and the solution of plane triangles and other rectilinear figures; but Trigonom-

etry shows that angular magnitudes admit of indefinite increase or diminution. That is to say, *an angle or arc may have a value anywhere between 0 and $+\infty$, or 0 and $-\infty$, in the same manner as linear, or any other kind of extension.*

7. In Art. 3, it is stated that the unit of angular measurement is an angle of one degree. For the solution of triangles, this method is to be preferred. But for certain theoretical purposes, another standard unit may be taken; namely, *the angle at the centre of a circle whose measuring arc is equal in length to the radius.*

If m represents the circumference of a circle, and r the radius, then, by Geometry,

$$m = 2\pi r; \text{ from which, if } r = 1,$$

$$m = 2\pi,$$

$$\frac{1}{2} m = \pi.$$

Now, let $ABCEG$ (Fig. 1) be a circle whose centre is at O . Then, the circumference may be represented by 2π ; the semicircumference, by π ; and the quadrant ABC , by $\frac{1}{2}\pi$.

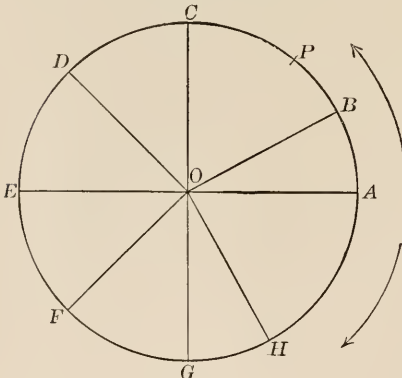


FIG. 1.

Let A be a fixed point upon the circumference; P , a point starting at A and moving in the direction of the upper arrow. The arcs AB , ABC , $ABCD$, etc., are, by common consent, *positive arcs*. The arc AB is the measure of the angle AOB ; the arc ABC is the measure of the angle AOC ; the arc $ABCD$ is the measure of the angle AOD , etc.

If the point P , however, should move in the direction of the lower arrow, then the arcs AH , AHG , $AHGF$, etc., are *negative arcs*.

In this volume, unless otherwise stated, radius is taken equal to unity.

8. The diameter AE (Fig. 1) is called the *initial diameter*, and the point A , the *origin of arcs*.

The diameter CG , perpendicular to AE , is the *secondary diameter*, and the point C , the *secondary origin*.

9. The arc AP has no value at the origin; at C , it is $\frac{1}{2}\pi$; at E , π ; at G , $\frac{3}{2}\pi$; and at A , or once round, it is 2π . For n circum-

ferences, the arc has a value of $2n\pi$. We may imagine the movement of the point P to continue indefinitely, so that it shall describe an arc composed of many circumferences.

10. The assumption of Art. 7 furnishes an *invariable unit of angular measurement*.

Let AB be the arc of a circle equal in length to the radius CA , the centre being at C .

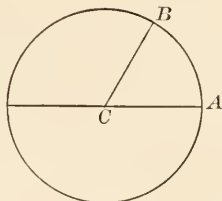


FIG. a'.

Since angles at the centre of a circle are proportional to their subtending arcs, we have

$$\frac{\text{angle } ACB}{4 \text{ right angles}} = \frac{\text{arc } AB}{\text{circumference}} = \frac{\text{radius}}{2\pi \times \text{radius}} = \frac{1}{2\pi};$$

$$\therefore \text{angle } ACB = \frac{4 \text{ right angles}}{2\pi} = \frac{2 \text{ right angles}}{\pi}$$

$$= \frac{180^\circ}{\pi} = \frac{180^\circ}{3.14159} = 57^\circ 17' 44.8''$$

= the unit of angular measurement, whatever may be the length of the radius of the circle.

11. *Complementary angles or arcs.* Two angles or arcs, both positive, or one positive and the other negative, are *complementary* when their sum equals a quadrant or $\frac{1}{2}\pi$. The complementary angle of 66° is 24° ; of 125° is -35° ; of -150° is 240° .

12. *Supplementary angles or arcs.* Two angles or arcs are *supplementary* when their sum equals a semicircle or π . The supplementary angle of 40° is 140° ; of 150° is 30° ; of 270° is -90° ; and of -190° is 370° .

13. EXAMPLES.

SET I.

1. Construct the angles, 75° ; 100° ; 120° ; 200° ; -75° ; -100° ; -300° ; 720° ; 1080° ; -500° ; -630° ; 1900° ; and name the quadrant to which each belongs.

2. How many degrees in $\frac{1}{4}\pi$? $\frac{3}{4}\pi$? 3π ? $3\frac{1}{2}\pi$? -5π ? $-\frac{3}{2}\pi$?

3. Express in terms of π , the arcs 15° ; 18° ; 36° ; 45° ; 90° ; 120° ; 150° ; $75^\circ 15' 15''$; 270° ; 360° ; 1800° ; -1440° ; $-85^\circ 25' 19''$.

4. How many times is the *unit arc* contained in 90° ? 360° ? 300° ? $\frac{3}{4}\pi$? 5π ? $4n\pi$?

5. What is the complement of $48^\circ 12'$? $125^\circ 15' 16''$? -80° ? -120° ? π ? $-\pi$? $\frac{3}{5}\pi$? $\pi + 30^\circ$? $\pi - 30^\circ$?

6. What is the supplement of $275^\circ 18'$? $48^\circ 12'$? -50° ? -180° ? π ? $-\pi$? $\frac{3}{5}\pi$? 24π ? $\pi + 50^\circ$? $\frac{3}{2}\pi - 50^\circ$? $2n\pi$?

7. The radius of a circle being 10 inches, what is the length of an arc of $5^\circ 30'$? 45° ? 360° ? π ? $\frac{3}{4}\pi$? π + the unit arc? 10 quadrants?

8. The radii of two concentric circles are 5 feet and 10 feet respectively; what is the difference in feet between an arc of 60° on the one and of 60° on the other?

9. The radius of a circle being 10 inches, how many degrees in an arc of 6 inches? Of 29 inches? Of 31.416 inches?

10. If radius equals one foot, how many degrees, minutes, and seconds in an arc of .56 of a foot? Of .275 of a foot? Of .9 of a foot?

11. The radius of a circle being 5 feet, what is the difference in degrees, minutes, and seconds between two arcs, one of which is 15 feet long and the other 12 feet?

12. How many degrees, minutes, and seconds in an arc of 5π ? Of 6π ? Of $8\frac{1}{2}\pi$? Of 9π ?

CHAPTER II.

THE TRIGONOMETRIC FUNCTIONS.

14. The terms used to designate the Trigonometric Functions or Ratios are the words *sine*, *cosine*, *tangent*, *cotangent*, *secant*, *cosecant*, *versed-sine*, and *covered-sine*, which are written *sin*, *cos*, *tan*, *cot*, *sec*, *cosec*, *vers*, and *covers*.

The investigation of the *properties and the relations* of these functions constitutes the chief part of Trigonometry.

The magnitude of an angle is independent of the lengths of the lines by which it is formed; and accordingly, since the ratios of the sides of a triangle remain unaltered, the magnitude of an angle may be determined by means of the Trigonometric Ratios, of which there are six.

A right triangle being used for this purpose, the definitions of the functions are

1. The *sine* of an angle is the ratio of the *opposite side* to the *hypotenuse*.

2. The *cosine* of an angle is the ratio of the *adjacent side* to the *hypotenuse*.

3. The *tangent* of an angle is the ratio of the *opposite side* to the *adjacent side*.

4. The *cotangent* of an angle is the ratio of the *adjacent side* to the *opposite side*.

5. The *secant* of an angle is the ratio of the *hypotenuse* to the *adjacent side*.

6. The *cosecant* of an angle is the ratio of the *hypotenuse* to the *opposite side*.

The definitions of *versed-sine* and *covered-sine* are

7. The *versed-sine* equals the difference between *unity* and the *cosine*.

8. The *covered-sine* equals the difference between *unity* and the *sine*.

15. Let ABC (Fig. 2) be any right triangle, right-angled at C , whose sides are a , b , and c , respectively.

Then

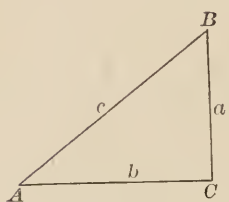


FIG. 2.

| | | | |
|-----|--|---|-----|
| (1) | $\sin A = \frac{a}{c}$, | } | [1] |
| (2) | $\cos A = \frac{b}{c}$, | | |
| (3) | $\tan A = \frac{a}{b}$, | | |
| (4) | $\cot A = \frac{b}{a}$, | | |
| (5) | $\sec A = \frac{c}{b}$, | | |
| (6) | $\operatorname{cosec} A = \frac{c}{a}$, | | |
| (7) | $\operatorname{vers} A^* = 1 - \cos A$, | | |
| (8) | $\operatorname{covers} A^* = 1 - \sin A$. | | |

16. Certain other relations are obtained from the foregoing formulæ, as follows :

| | | | | |
|-----|---|--|---|-----|
| (1) | $\tan A \times \cot A = \frac{a}{b} \times \frac{b}{a} = 1$; | $\therefore \tan A = \frac{1}{\cot A}$, | } | [2] |
| (2) | $\sin A \times \operatorname{cosec} A = \frac{a}{c} \times \frac{c}{a} = 1$; | $\therefore \sin A = \frac{1}{\operatorname{cosec} A}$, | | |
| (3) | $\cos A \times \sec A = \frac{b}{c} \times \frac{c}{b} = 1$; | $\therefore \cos A = \frac{1}{\sec A}$, | | |
| (4) | $\tan A = \frac{a}{b} = \frac{a}{c} \div \frac{b}{c} \dots \dots \dots = \frac{\sin A}{\cos A}$, | | | |
| (5) | $\cot A = \frac{b}{a} = \frac{b}{c} \div \frac{a}{c} \dots \dots \dots = \frac{\cos A}{\sin A}$. | | | |

17. In Fig. b' , we have

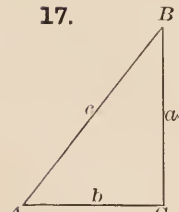


FIG. b' .

| | | | |
|--------------------------|--------------------------|--|--|
| $\sin A = \frac{a}{c}$, | $\sin B = \frac{b}{c}$, | $\tan A = \frac{a}{b}$, | $\tan B = \frac{b}{a}$, |
| $\cos A = \frac{b}{c}$, | $\cos B = \frac{a}{c}$, | $\cot A = \frac{b}{a}$, | $\cot B = \frac{a}{b}$, |
| $\sec A = \frac{c}{b}$, | $\sec B = \frac{c}{a}$, | $\operatorname{cosec} A = \frac{c}{a}$, | $\operatorname{cosec} B = \frac{c}{b}$. |

* The *vers* and *covers* being easily found from the *cos* and *sin*, we shall not use them hereafter.

Therefore, since $A + B = 90^\circ$, we find

$$\left. \begin{aligned} (1) \quad \sin A &= \frac{a}{c} = \cos B, \\ (2) \quad \cos A &= \frac{b}{c} = \sin B, \\ (3) \quad \tan A &= \frac{a}{b} = \cot B, \\ (4) \quad \cot A &= \frac{b}{a} = \tan B, \\ (5) \quad \sec A &= \frac{c}{b} = \operatorname{cosec} B, \\ (6) \quad \operatorname{cosec} A &= \frac{c}{a} = \sec B. \end{aligned} \right\} [3]$$

18. Since in any right triangle, as ABC (Fig. b'),

$$\overline{BC}^2 + \overline{AC}^2 = \overline{AB}^2,$$

then
$$\frac{\overline{BC}^2}{\overline{AB}^2} + \frac{\overline{AC}^2}{\overline{AB}^2} = 1.$$

Since
$$\frac{BC}{AB} = \sin A, \quad \text{and} \quad \frac{AC}{AB} = \cos A \quad \text{by [1]},$$

$$\therefore \sin^2 A + \cos^2 A = 1.$$

19. Using the equation $\overline{BC}^2 + \overline{AC}^2 = \overline{AB}^2$, derived from Fig. b' , we obtain

$$\frac{\overline{AB}^2}{\overline{AC}^2} = 1 + \frac{\overline{BC}^2}{\overline{AC}^2};$$

$$\therefore \sec^2 A = 1 + \tan^2 A.$$

20. Again, from the equation $\overline{BC}^2 + \overline{AC}^2 = \overline{AB}^2$, we obtain

$$\frac{\overline{AB}^2}{\overline{BC}^2} = 1 + \frac{\overline{AC}^2}{\overline{BC}^2};$$

$$\operatorname{cosec}^2 A = 1 + \cot^2 A.$$

21. Collecting the results of Arts. 18, 19, 20, and others that follow easily from the same, we shall obtain

$$\left. \begin{aligned}
 (1) \quad & \sin^2 A + \cos^2 A = 1, \\
 (2) \quad & 1 + \tan^2 A = \sec^2 A, \\
 (3) \quad & 1 + \cot^2 A = \operatorname{cosec}^2 A, \\
 (4) \quad & \cos A = \sqrt{1 - \sin^2 A}, \\
 (5) \quad & \tan A = \frac{\sin A}{\sqrt{1 - \sin^2 A}}, \\
 (6) \quad & \cot A = \frac{\sqrt{1 - \sin^2 A}}{\sin A}, \\
 (7) \quad & \sec A = \frac{1}{\sqrt{1 - \sin^2 A}}, \\
 (8) \quad & \operatorname{cosec} A = \frac{1}{\sin A}.
 \end{aligned} \right\} [4]$$

22. The relations already established for angles not exceeding a right angle, hold universally, whatever be the magnitude of an angle, and whether positive or negative.

It must be observed from (1) of [4] that $\sin A = \pm \sqrt{1 - \cos^2 A}$, or $\cos A = \pm \sqrt{1 - \sin^2 A}$ from (4) of [4], has a double sign. In such cases the angle or arc is either positive or negative, and it is necessary to determine from given conditions in any particular case *which sign must be used*. See Art. 25.

23. The functional values of the angles 30° , 45° , and 60° , are so often used, an application of the formulæ already obtained will now be made to find those values.

Let ABD (Fig. 3) be an equilateral triangle, divided into two right triangles by BC , a perpendicular from the vertex B upon the base AD .

In the triangle ABC ,

$$\begin{aligned}
 AC &= \frac{1}{2} AD = \frac{1}{2} AB \\
 &= b = \frac{1}{2} c.
 \end{aligned}$$

The angle $A = 60^\circ$,

and the angle $ABC = 30^\circ$.

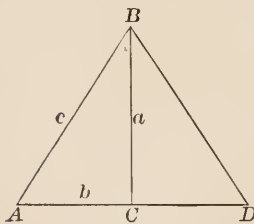


FIG. 3.

By [1], $\cos A = \frac{AC}{AB} = \frac{\frac{1}{2}c}{c} = \frac{1}{2}$. \therefore by [3], $\cos 60^\circ = \frac{1}{2} = \sin 30^\circ$.

By [4], $\sin A = \sqrt{1 - \cos^2 A} = \frac{1}{2}\sqrt{3}$. \therefore by [3], $\sin 60^\circ = \frac{1}{2}\sqrt{3} = \cos 30^\circ$.

By [2], $\tan A = \frac{\sin A}{\cos A}$. \therefore by [3], $\tan 60^\circ = \sqrt{3} = \cot 30^\circ$.

By [2], $\cot A = \frac{\cos A}{\sin A}$. \therefore by [3], $\cot 60^\circ = \frac{1}{\sqrt{3}} = \tan 30^\circ$.

By [2], $\sec A = \frac{1}{\cos A}$. \therefore by [3], $\sec 60^\circ = 2 = \operatorname{cosec} 30^\circ$.

By [2], $\operatorname{cosec} A = \frac{1}{\sin A}$. \therefore by [3], $\operatorname{cosec} 60^\circ = \frac{2}{\sqrt{3}} = \sec 30^\circ$.

24. Let the right triangle ABC (Fig. 4) have the angles A and B , each, equal to 45° . Then the sides AC and BC will be equal; i.e. $a = b$.

By Geometry, $\overline{AC}^2 + \overline{BC}^2 = \overline{AB}^2$, or

$$b^2 + a^2 = c^2, \text{ or}$$

$$2a^2 = c^2, \text{ or}$$

$$\frac{a^2}{c^2} = \frac{1}{2}, \text{ or}$$

$$\frac{a}{c} = \frac{1}{2}\sqrt{2}.$$

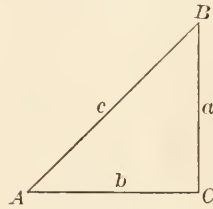


FIG. 4.

$\sin A = \frac{a}{c}$. \therefore by [3], $\sin 45^\circ = \frac{1}{2}\sqrt{2} = \cos 45^\circ$.

$\tan A = \frac{a}{b}$. \therefore by [3], $\tan 45^\circ = 1 = \cot 45^\circ$.

$\sec A = \frac{1}{\cos A}$. \therefore by [3], $\sec 45^\circ = \sqrt{2} = \operatorname{cosec} 45^\circ$.

25. We shall now investigate the Trigonometric Functions of all the quadrants of a circle.

Draw through O , the centre of the circle $ABCD$ (Fig. 5), the diameters AC and BD , at right angles to each other.

Let us take A as the origin of arcs, and those arcs that have the direction of $AMBII \dots$, etc., as positive arcs, and those whose direction is that of $AM'DT' \dots$, etc., as negative (Art. 7).

We shall further assume that all lines drawn in the *direction* of, or *parallel* to, OA and OB , are *positive*, and those that are drawn in the *direction* of, or *parallel* to, OC and OD , are *negative*.

The arc AMB is the first quadrant; BHC , the second; CTD , the third; and $DM'A$, the fourth.

Designate by θ the positive or negative quantity which represents the variable arc whose extremity M may take upon the circumference all possible positions. Let

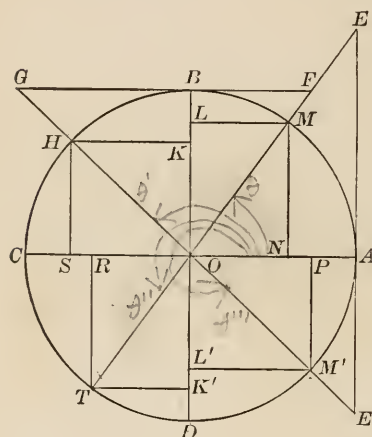


FIG. 5.

fall the perpendiculars, MN on OA , and ML on OB . Prolong the radius OM until it meets AE in E . The line OL or its equal MN , with its proper sign, is the *sine* of the arc AM , or θ . The line AE is the tangent of the arc θ , and the line OE is the secant.

MB , the complementary arc of AM , or θ , has for its *sine* the line ON or its equal ML ; for its *tangent* BF , and its *secant* OF . We therefore name the *sine*, *tangent*, and *secant*, of the arc MB , the *cosine*, *cotangent*, and *cosecant*, of

the arc AM , or θ . Now designating the arc AM , as before, by θ ; the arc ABH by θ' ; the arc $ABCT$ by θ'' ; and the arc $ABCDM'$ by θ''' , we shall have the following:

| | Arc θ . | Arc θ' . | Arc θ'' . | Arc θ''' . |
|------------|----------------|-----------------|------------------|-------------------|
| sin . . . | + MN | + HS | - TR | - $M'P$ |
| cos . . . | + ON | - OS | - OR | + OP |
| tan . . . | + AE | - AE' | + AE | - AE' |
| cot . . . | + BF | - BG | + BF | - BG |
| sec . . . | + OE | - OE' | - OE | + OE' |
| cosec. . . | + OF | + OG | - OF | - OG |

26. Therefore, the *sine* of an arc is a positive or negative quantity which measures the perpendicular let fall from the extremity of an arc upon the diameter which passes through the origin.

The tangent of an arc is the positive or negative quantity which measures that portion of the tangent line drawn from the origin of the arc and terminated by the diameter which passes through the extremity of the arc.

The secant of an arc is the positive or negative quantity which measures that portion of the diameter prolonged that is comprised between the centre and the tangent of the arc.

The cosine, cotangent, and cosecant may be described in the same way.

27. We shall now examine in what manner the six trigonometric functions of an arc vary, when that arc varies from 0 to $+\infty$, and from 0 to $-\infty$. If θ increases from 0 to $+\frac{1}{2}\pi$, the six functions remain positive. $\sin\theta$ increases from 0 to $+1$, while passing through all intermediate values. $\tan\theta$ increases from 0 to $+\infty$, and $\sec\theta$ from 1 to $+\infty$.

The cosine, cotangent, and cosecant, on the contrary, decrease; that is to say, the $\cos\theta$ decreases from 1 to 0; $\cot\theta$ decreases from $+\infty$ to 0; and $\operatorname{cosec}\theta$ decreases from ∞ to $+1$.

If the arc increases from $\frac{1}{2}\pi$ to π , then $\sin\theta$ decreases from $+1$ to 0; $\tan\theta$ increases from $-\infty$ to 0; $\sec\theta$ increases from $-\infty$ to -1 ; $\cos\theta$ decreases from 0 to -1 ; $\cot\theta$ decreases from 0 to $-\infty$; and $\operatorname{cosec}\theta$ increases from $+1$ to $+\infty$.

If the arc increases from π to $\frac{3}{2}\pi$, then $\sin\theta$ decreases from 0 to -1 ; $\tan\theta$ increases from 0 to $+\infty$; $\sec\theta$ decreases from -1 to $-\infty$; $\cos\theta$ increases from -1 to 0; $\cot\theta$ decreases from $+\infty$ to 0; and $\operatorname{cosec}\theta$ increases from $-\infty$ to -1 .

If the arc increases from $\frac{3}{2}\pi$ to 2π , then $\sin\theta$ increases from -1 to 0; $\tan\theta$ increases from $-\infty$ to 0; $\sec\theta$ decreases from $+\infty$ to $+1$; $\cos\theta$ increases from 0 to $+1$; $\cot\theta$ decreases from 0 to $-\infty$; and $\operatorname{cosec}\theta$ decreases from -1 to $-\infty$.

28. If the arc increases from 2π to 4π , or from 4π to 6π , or \dots to $2n\pi$, the six functions will have periodically the same values and in the same order.

If to the arc any number of circumferences be added, we shall have, whatever be the value of θ , and denoting by n any entire positive or entire negative quantity,

$$\begin{aligned} \sin(2n\pi + \theta) &= \sin \theta, & \cos(2n\pi + \theta) &= \cos \theta, \\ \tan(2n\pi + \theta) &= \tan \theta, & \cot(2n\pi + \theta) &= \cot \theta, \\ \sec(2n\pi + \theta) &= \sec \theta, & \operatorname{cosec}(2n\pi + \theta) &= \operatorname{cosec} \theta. \end{aligned}$$

29. If θ increases from 0 to $-\infty$, then whatever be the value of θ ,

$$\begin{aligned} \sin(-\theta) &= -\sin \theta, & \cos(-\theta) &= \cos \theta, \\ \tan(-\theta) &= -\tan \theta, & \cot(-\theta) &= -\cot \theta, \\ \sec(-\theta) &= \sec \theta, & \operatorname{cosec}(-\theta) &= -\operatorname{cosec} \theta. \end{aligned}$$

30. If θ be any arc, then θ and $\pi + \theta$ terminate at the extremities of the same diameter, and we shall have,

$$\begin{aligned} \sin(\pi + \theta) &= -\sin \theta, & \cos(\pi + \theta) &= -\cos \theta, \\ \tan(\pi + \theta) &= \tan \theta, & \cot(\pi + \theta) &= \cot \theta, \\ \sec(\pi + \theta) &= -\sec \theta, & \operatorname{cosec}(\pi + \theta) &= -\operatorname{cosec} \theta. \end{aligned}$$

31. If in the equations of Art. 30 we change θ to $-\theta$, we shall have,

$$\begin{aligned} \sin(\pi - \theta) &= \sin \theta, & \cos(\pi - \theta) &= -\cos \theta, \\ \tan(\pi - \theta) &= -\tan \theta, & \cot(\pi - \theta) &= -\cot \theta, \\ \sec(\pi - \theta) &= -\sec \theta, & \operatorname{cosec}(\pi - \theta) &= \operatorname{cosec} \theta. \end{aligned}$$

From which it follows that *if two arcs are supplementary, their sines and their cosecants are equal and of the same sign, but their cosines, tangents, cotangents, and secants are equal and of contrary signs.*

From the two preceding groups of equations, denoting by n any entire quantity positive or negative, we shall have,

$$\begin{aligned} \sin[(2n+1)\pi \pm \theta] &= \mp \sin \theta, & \cos[(2n+1)\pi \pm \theta] &= -\cos \theta, \\ \tan(n\pi \pm \theta) &= \pm \tan \theta, & \cot(n\pi \pm \theta) &= \pm \cot \theta, \\ \sec[(2n+1)\pi \pm \theta] &= -\sec \theta, & \operatorname{cosec}[(2n+1)\pi \pm \theta] &= \mp \operatorname{cosec} \theta. \end{aligned}$$

32. It is very important to remark that each of the trigonometric functions of an arc θ takes all values of which it is susceptible in the indefinite variation of θ throughout an interval of two quadrants.

33. To the functions $x = \sin \theta$, $x = \tan \theta$, $x = \cos \theta$, $x = \sec \theta$, $x = \cot \theta$, etc., corresponds another class of functions, which are usually written by the Germans and the French, $\theta = \operatorname{arc-sin} x$,

$\theta = \text{arc-tan } x$, $\theta = \text{arc-cos } x$, $\theta = \text{arc-sec } x$, $\theta = \text{arc-cot } x$, etc., and by others $\theta = \sin^{-1} x$, $\theta = \tan^{-1} x$, $\theta = \cos^{-1} x$, $\theta = \sec^{-1} x$, $\theta = \cot^{-1} x$, etc. The German and French method is to be preferred.

It is easily seen that $\theta = \text{arc-sin } x$, $\theta = \text{arc-tan } x$, etc., are not entirely determined, for they admit of an indefinite number of values for each value of x . The expressions $\text{arc-sin } x$, $\text{arc-tan } x$, $\text{arc-cot } x$, and $\text{arc-cosec } x$, become completely determined if their values are constantly comprised between $-\frac{1}{2}\pi$ and $+\frac{1}{2}\pi$; and in like manner, $\text{arc-cos } x$ and $\text{arc-sec } x$ will be determined if their values are constantly comprised between 0 and π . With these restrictions, the expressions $\text{arc-sin } x$, $\text{arc-tan } x$, $\text{arc-cos } x$, $\text{arc-cot } x$, $\text{arc-sec } x$, and $\text{arc-cosec } x$, may be considered as functions of x .

31. EXAMPLES.

SET II.

1. Construct :

| | | |
|-------------------------------|---------------------------------|--|
| $\sin \theta = \frac{2}{3}$, | $\sin \theta = \pi$, | $\theta = \text{arc-sin } \frac{1}{2}$, |
| $\cos \theta = \frac{2}{3}$, | $\cos \theta = \pi$, | $\theta = \text{arc-tan } \frac{3}{4}$, |
| $\tan \theta = 1$, | $\sin \theta = -\frac{1}{3}$, | $-\theta = \text{arc-cos } \sqrt{\frac{2}{3}}$, |
| $\sec \theta = 5$, | $\tan \theta = -\frac{9}{16}$, | $\theta = \text{arc-sec } 2$, |
| $\tan \theta = \infty$, | $\cot \theta = 6$, | $\theta = \text{arc-cot } 3$. |

2. Determine the values of the Trigonometric Ratios for an angle of 585° . Also for an angle of 690° . Also for an angle of 930° . Also for an angle of 6420° .

3. Find all the angles between 0 and 900° which satisfy $\tan \theta = 1$. Find all the angles between 0 and 900° which satisfy $\cos^2 \theta = \frac{1}{2}$.

4. Find the values of the other functions of θ , when

| | |
|--------------------------------|--|
| $\sin \theta = \frac{2}{3}$, | $\sin 135^\circ = \frac{1}{\sqrt{2}}$, <i>$\tau_2 = -1 \sec = \frac{1}{2}$</i> |
| $\sec \theta = 4$, | $\cos 120^\circ = -\frac{1}{2}$, <i>$\sin = +\frac{1}{2}\sqrt{3}$, $\tan = \dots$</i> |
| $\cot \theta = \frac{m}{n}$, | $\tan 1440^\circ = 0$, <i>$\cot = 2 \csc = 2\sqrt{3}$</i> |
| $\tan \theta = -\frac{1}{3}$, | $\cot 540^\circ = \infty$, <i>$\csc = 1 \csc = \dots$</i> |
| $\tan \theta = -3$, | $\sin(2\pi + 30^\circ) = \frac{1}{2}$, |
| $\cos \theta = -\frac{1}{3}$, | $\cos(\pi + 90^\circ) = 0$, <i>$\sin = -1 \tan = \infty \cot = 2$</i> |
| $\csc \theta = -1$, | $\sec(2\pi + 90^\circ) = \infty$, <i>$\sec = \infty \csc = +1$</i> |
| | <i>$\csc = 1$</i> |
| | <i>$\tan = \infty$</i> |
| | <i>$\cot = 0$</i> |
| | <i>$\sin = 1$</i> |
| | <i>$\cos = 0$</i> |

15. Given $\tan \theta = \sin \theta$; find the angle θ . 36°
6. Given $\cos \theta = \tan \theta$; find the angle θ .
7. Given $\operatorname{cosec} 45^\circ = \sec(180^\circ - \theta)$; find the angle θ .
8. Given $\cot(m+n)\theta = \tan \theta$; find θ .
9. Given $\sin \frac{1}{2}\theta = \cos(90 - 5\frac{1}{2}\theta)$; find θ .
10. Given $10\sin \theta = 2\tan \theta$; find $\cos \theta$, $\sin \theta$, and $\tan \theta$.
11. Given $2\sin^2 \theta = 3\cos \theta$; find θ .
12. Given $\sin^2 \theta - 2\cos \theta + \frac{1}{4} = 0$; find θ .
13. Given $\tan \theta + \cot \theta = 2$; find θ .
14. Show that $\tan \theta + \cot \theta = \frac{\sec^2 \theta + \operatorname{cosec}^2 \theta}{\sec \theta \operatorname{cosec} \theta}$.
15. Find the values of θ that will satisfy $\sin \theta \cos \theta = \tan \theta$.
16. Show that $\sin^4 \theta + \cos^4 \theta = 1 - 2\sin^2 \theta \cos^2 \theta$.
17. When is $\sin \theta + \cos \theta = 1$? When equal to -1 ? When is $\sin^2 \theta = 1$? $\cos^2 \theta = 1$? When is $\tan^2 \theta + \cot^2 \theta = 2$?
18. Find the value of $\sin \frac{3\pi}{12}$. Of $\sin(-4\pi)$. Of $\cos \frac{\pi}{4}$. Of $\cos(-6\pi)$.
19. Construct $\operatorname{arc-tan} 1$; $\operatorname{arc-cos}(-\frac{1}{5})$; $\operatorname{arc-tan}(-5)$; $\operatorname{arc-cosec}(-5)$.
20. Trace the changes in the sign and value of $\cos \theta - \sin \theta$, as θ passes from 0 to 2π . Also of $\tan \theta + \cot \theta$.
21. Find all the angles between 0 and $\frac{10\pi}{3}$ which satisfy the relation $\cos^2 \theta = \frac{1}{2}$.

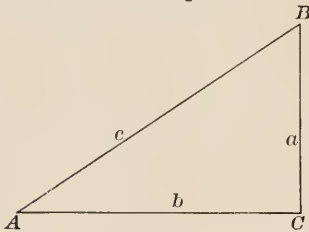


FIG. 6.

22. Find $\sin \theta$ and $\cos \theta$, when $a + b = \frac{5}{4}c$. In this example use Fig. 6, in which the angle A is denoted by θ , and the angle C is a right angle.

23. Find the value of θ , when $\tan 6\theta = 1$.
24. Find $\sin \theta$, when $\sec \theta + \tan \theta = 2$.
25. Show that $1 + \sin \theta = \frac{\cos^2 \theta}{1 - \sin \theta}$.

26. Letting $n = 0, 1, 2, 3, 4, 5, 6$, in succession, show that

$$\sin 4n \frac{\pi}{2} = 0; \quad \sin(4n + 2) \frac{\pi}{2} = 0; \quad \sin(4n + 3) \frac{\pi}{2} = -1;$$

$$\cos(4n + 2) \frac{\pi}{2} = -1; \quad \text{and} \quad \tan(2n + 1) \frac{\pi}{2} = \infty.$$

27. Show that $\sin(270^\circ - \theta) = -\cos \theta$.

28. Show that $\cos(270^\circ - \theta) = -\sin \theta$.

29. Show that $\cos(270^\circ + \theta) = \sin \theta$.

30. Show that $\sin(360^\circ - \theta) = -\sin \theta$.

31. Show that $\cos(360^\circ - \theta) = \cos \theta$.

32. Show that $\frac{\sec \theta + \operatorname{cosec} \theta}{\sec \theta - \operatorname{cosec} \theta} = \frac{1 + \cot \theta}{1 - \cot \theta} = \frac{\tan \theta + 1}{\tan \theta - 1}$.

33. From the table of natural functions, find the

| | |
|---------------------------------|----------------------------------|
| \sin of 15° , | \cos of $25^\circ 15' 18''$, |
| \sin of $18^\circ 15'$, | \cos of $135^\circ 25' 20''$, |
| \sin of $75^\circ 10' 35''$, | \tan of $60^\circ 55' 43''$. |

34. From the table of logarithmic functions, find the logarithmic \sin , \cos , \tan , and \cot of

| | |
|------------------------|------------------------|
| $18^\circ 18' 18''$, | $100^\circ 50'$, |
| $50^\circ 0' 20''$, | $175^\circ 14' 25''$, |
| $150^\circ 15' 25''$, | $75^\circ 16' 40''$. |

35. From the table of natural functions, find the angle whose \sin is .25256; \cos , .78543; \tan , 3.14156; and \cot , .56789.

36. From the table of logarithmic functions, find the angle whose logarithmic \sin is 9.12345; \cos , 9.34567; \tan , 10.43216; and \cot , 10.23456.

CHAPTER III.

TRIANGLES AND POLYGONS.

35. To solve a triangle is to calculate the numerical value of its unknown elements, when a sufficient number of parts are given.

In every triangle there are three angles and three sides.

In a right triangle, the right angle is always known; and to solve such a triangle, either *an oblique angle and a side* or *two sides* must be given.

When the given parts are the three angles of a triangle, the problem is indeterminate; that is to say, an indefinite number of triangles may, each, satisfy the conditions.

36.

CASE I.

Given two sides of a right triangle; to find the other parts.

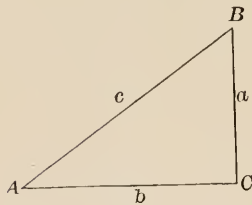


FIG. 7.

Let ABC (Fig. 7) be a triangle, right-angled at C . Let a and b be the given sides; then, by Art. 15, we have

$$\tan BAC = \frac{a}{b}, \quad \text{or,} \quad \cot ABC = \frac{a}{b}.$$

$$\therefore * \log \tan BAC = \log a - \log b + 10,$$

$$\text{or} \quad \log \cot ABC = \log a - \log b + 10.$$

By Art 15, $\sin BAC = \frac{a}{c}$; $\therefore \log c = \log a - \log \sin BAC + 10$.

Checks. $BAC + ABC = 90^\circ$, and $c = \sqrt{a^2 + b^2}$.

EXAMPLE. Given $a = 15.5$, and $b = 18.2$. Find the side c and the angles A and B .

Solution by logarithms :

$$(1) \log a = 1.190332$$

$$\log b = \underline{1.260071}$$

$$\log \tan A = 9.930261 = \log \cot B.$$

$$\therefore A = 40^\circ 25' 9''.6, \quad \text{and} \quad B = 49^\circ 34' 50''.4.$$

* See Chapter XIII.

$$(2) \log a = 1.190332$$

$$\log \sin A = 9.811828$$

$$\log c = 1.378504.$$

$$\therefore c = 23.905.$$

Checks. $40^\circ 25' 9''.6 + 49^\circ 34' 50''.4 = 90^\circ$; and

$$23.905 = \sqrt{15.5^2 + 18.2^2}.$$

37.

CASE II.

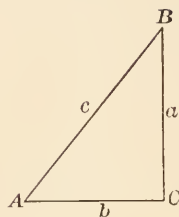
Given the hypotenuse and one side; to find the other parts.

Let c and a be given.

We have, to determine the unknown parts,

$$\sin A = \cos B = \frac{a}{c},$$

and
$$b^2 = c^2 - a^2 = (c + a)(c - a).$$



The direct determination of the angle B is obtained by the formula for the cosine; but if the hypotenuse differs little from the given side, as is sometimes the case, then the angle B is not *exactly* determined. To avoid the difficulty, we may first obtain the side b , and then, by

Art. 15, (3), [1], calculate the angle B from $\tan B = \frac{b}{a}$.

By logarithms :

$$(1) \quad \log b = \frac{1}{2} [\log(c + a) + \log(c - a)],$$

$$(2) \log \tan B = \log b - \log a + 10,$$

$$(3) \log \tan A = \log a - \log b + 10.$$

Checks. $A + B = 90^\circ$, and $c = \sqrt{a^2 + b^2}$.

EXAMPLE. Given $c = 5892.51$, and $a = 5439.24$. Find b , A , and B .

Solution : $c + a = 11331.75$, $c - a = 453.27$.

By (1), $\log(c + a) = 4.054297$ By (2), $\log b = 3.355327$

$\log(c - a) = 2.656357$ $\log a = 3.735538$

$2)6.710654$ $\log \tan B = 9.619789$

$\log b = 3.355327.$ $\therefore B = 22^\circ 37' 11''.4.$

$\therefore b = 2266.35.$

$$\text{By (3), } \log a = 3.735538$$

$$\log b = \overline{3.355327}$$

$$\log \tan A = \overline{10.380211}.$$

$$\therefore A = 67^\circ 22' 48''.6.$$

$$\text{Checks. } 67^\circ 22' 48''.6 + 22^\circ 37' 11''.4 = 90^\circ; \text{ and}$$

$$5892.51 = \sqrt{5439.24^2 + 2266.35^2}.$$

38.

CASE III.

Given an acute angle and one side; to find the other parts.

Let the angle A and the side a be given. Then the required parts may be determined by the formulæ

$$(1) A + B = 90^\circ; (2) \sin A = \frac{a}{c}; (3) \tan A = \frac{a}{b}.$$

(2) and (3) changed to the form of logarithms become

$$\log c = \log a - \log \sin A + 10,$$

$$\log b = \log a - \log \tan A + 10.$$

39.

CASE IV.

Given an acute angle and the hypotenuse; to find the other parts.

Let the angle A and the hypotenuse c be given. Then the required parts may be determined by the formulæ

$$(1) A + B = 90^\circ; (2) \sin A = \frac{a}{c}; (3) \cos A = \frac{b}{c}.$$

(2) changed to the logarithmic form becomes

$$\log a = \log \sin A + \log c - 10;$$

(3) changed to the logarithmic form becomes

$$\log b = \log \cos A + \log c - 10.$$

40. Whatever may be the given parts of a right triangle, the required parts can always be found by the use of the formulæ

$$(1) c = \sqrt{a^2 + b^2}; (2) A + B = 90^\circ; (3) [1] \text{ and } [3].$$

41. Isosceles Triangles.

A perpendicular let fall from the vertex of an isosceles triangle upon the base divides the triangle into two equal right triangles. *The triangle is solved by solving the right triangles.*

42. Oblique Triangles.

A perpendicular let fall from the vertex of an oblique triangle upon the side opposite divides the triangle into two right triangles. *The oblique triangle is solved by solving the two right triangles.*

43. Regular Polygons.

Let $ABCDEF$ (Fig. 8) be a regular polygon.

Lines drawn from the centre O to the middle points of the sides, as at G , are radii of the inscribed circle; and lines drawn from the centre to the vertices of the polygon are radii of the circumscribed circle. In this manner a regular polygon is divided into twice as many right triangles as the polygon has sides. Let n be the number of sides of a regular polygon; then the angle AOG will equal

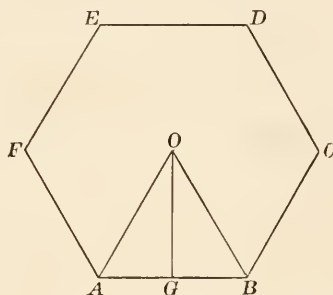


FIG. 8.

$$\frac{360^\circ}{2n} = \frac{180^\circ}{n}, \text{ and the angle } OAG \text{ will equal } 90^\circ - \frac{180^\circ}{n}.$$

If one of the two radii, OA or OG , or the side AB , be given, the angles having been determined as above, the remaining parts of the polygon may be found by the formulæ for right triangles.

44. Area of Right Triangles.

The base b and the perpendicular a of a right triangle being given, the area, by Geometry, is equal to $\frac{1}{2}ab$.

45. EXAMPLES.

SET III.

1. Given $A = 50^\circ$, $c = 15$; to find B , a , b .
2. Given $A = 80^\circ$, $b = 40$; to find B , a , c .
3. Given $A = 70^\circ 15'$, $a = 225$; to find B , b , c .
4. Given $A = 35^\circ 35' 35''$, $B = 54^\circ 24' 25''$; to find a , b , c .
 $b = 20^\circ 22' 18''$, $a = 1440.266$, $c = 502.71$
5. Given $A = 59^\circ 37' 42''$, $c = 1785.395$; to find B , a , b .
 $b = 400.447$, $a = 3.569$, $c = 20,2619$
6. Given $B = 40^\circ 45' 43''$, $a = 15.15$; to find A , b , c .
 $A = 39^\circ 9' 11''$, $a = 123$, $c = 200.66$
7. Given $B = 50^\circ 50' 50''$, $b = 201.356$; to find A , a , c .



8. Given $B = 75^\circ 30' 38''$, $c = 400$; to find A , a , b .
 9. Given $a = 65$, $b = 72$; to find A , B , c .
 10. Given $a = 2269$, $c = 3269$; to find A , B , b .
 11. Given $a = .00075$, $A = 75^\circ$; to find B , b , c .
 12. Given $b = 99.5$, $c = 100$; to find A , B , a .

13. The hypotenuse of a right triangle is 18 feet long, and one of the acute angles is 4 times the other. Find the angles and sides.

14. In a right triangle whose hypotenuse is 15, and the angle $A = \text{arc-tan} 3$; what are the other parts?

15. In a right triangle the side $a = 515.5$; and the angle B , $50^\circ 45'$. Find the other parts.

16. The uniform grade of a railroad track 500 feet long is 4° . What is the elevation at the end?

17. What are the values of the trigonometric functions of a right triangle whose sides are 30, 40, 50, respectively? Are there any other right triangles that give the same values?

18. The hypotenuse of a right triangle is 6 times the base. Find the angles.

19. A tower 300 feet high casts a shadow 150 feet long upon the horizontal plane upon which it stands. Find the altitude of the sun.

* Isosceles Triangles.

20. One of the two equal sides of an isosceles triangle is 18 feet long; one of the equal angles, 30° . Find the *third angle*, the *base*, and the *perpendicular* from the third angle upon the base.

21. Given the third angle of an isosceles triangle, and the perpendicular from that angle upon the base. Find the *equal angles*, the *equal sides*, and the *base*.

22. A chord 30 feet long is drawn in a circle whose diameter is 60 feet. Find the angle at the centre.

23. A circle whose diameter is 100 feet has two chords, one of which subtends an angle at the centre of 30° , and the other an angle of 50° . Find the difference in length between the two chords.

Regular Polygons.

24. Find the side of an equilateral triangle inscribed in a circle whose radius is 10.
25. Find the side of a regular decagon inscribed in a circle whose radius is 10.
26. Find the radius of a circle in which is inscribed a regular pentagon whose perimeter is 50 feet.
27. Find the radius of a circle in which is inscribed a regular dodecagon whose perimeter is 120 feet.
28. Find the side of a regular pentadecagon inscribed in a circle whose radius is 50.

Areas of Right Triangles and Regular Polygons.

29. Find the area of a right triangle, the angle A being 75° , and the side a equal to 50.
30. Find the area of a right triangle, A being equal to $50^\circ 50'$, and c equal to 100.
31. The area of a right triangle is 500, and the hypotenuse 200. Find the angles and sides.
32. Find the area of a regular pentagon inscribed in a circle whose radius is 10 feet.
33. Find the area of the space between a regular decagon inscribed in, and a regular decagon circumscribed about, a circle whose radius is 10 feet.
34. How much space between the circumference of a circle of 20 feet diameter, and the perimeter of a regular dodecagon inscribed in the circle?

Miscellaneous.

35. Solve the right triangle, when $A = 30^\circ$, $b = 100$, and $a = 40$.
36. $A = 18^\circ$, and $c = 4 + \sqrt{80}$. Find a , b , and B .
37. Show whether there can be a right triangle when

$$\log a + 10 = \log b + \log \sin A.$$

38. If $c \cos B = b \cos C$, show that the triangle is isosceles; that is, that $b = c$.

39. The elevation of a tower is 30° to a man 6 feet high at a distance of 140 feet from the foot of the tower. Find the height of the tower.

40. A man's shadow is twice his height. What is the altitude of the sun?

41. The sides of a right triangle are 20 and 32. Show that $A = \text{arc-tan } \frac{4}{3}$, $B = \text{arc-tan } \frac{3}{4}$, and the hypotenuse $= 4\sqrt{89}$.

42. Show that if $2 \sin \theta = \tan \theta$, $\theta = 0$, or 60° .

43. If $6 \cot^2 \theta - 4 \cos^2 \theta = 1$, then $\theta = \pm 60^\circ$.

44. If $\sin \theta + \text{cosec } \theta = 2$, then $\theta = 90^\circ$.

45. Show that $\sin \left(\frac{4n+3}{2} 180^\circ + \theta \right) = -\cos \theta$.

46. The difference of the lengths of the shadows of a vertical stick is 10 feet, when the sun's altitude is 45° and 30° respectively. Find the length of the stick.

47. The difference of two acute angles of a right-angled triangle is θ° . Find the angles.

48. Show that $\frac{\sin 45^\circ - \sin 30^\circ}{\sin 45^\circ + \sin 30^\circ} = (\sec 45^\circ - \tan 45^\circ)^2$.

49. The length of a kite string is 300 yards, and the elevation of the kite is 32° . Find its height.

50. If a rectangle, 3 feet long by 2 feet broad, be taken as the unit of surface, what quantity will represent two square feet?

CHAPTER IV.

FORMULÆ FOR THE SUM OR DIFFERENCE OF TWO ANGLES OR ARCS.

46. To determine the sine and the cosine of the sum of two angles or arcs, the sines and the cosines of the angles or arcs being known.

Let AB and BC be two positive arcs whose sum does not exceed $\frac{1}{2}\pi$. The origin of arcs (Fig. 9) being at A , represent the arc AB by θ , and BC by θ' . The arc BC may be considered as having its origin at B and its extremity at C .

Then $\theta + \theta' =$ the arc AC .

Draw CF perpendicular to the radius OB , and CG, FH, BK , perpendicular to $O.A$, and FE parallel to $O.A$.

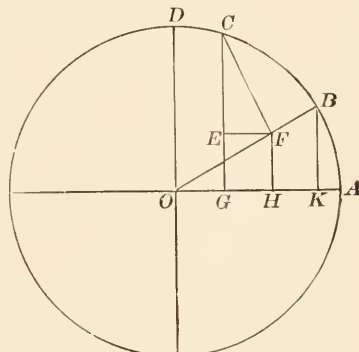


FIG. 9.

Then $\sin \theta = BK,$
 $\cos \theta = OK,$
 $\sin \theta' = CF,$
 $\cos \theta' = OF.$

$$(1) \sin(\theta + \theta') = CG = CE + FH,$$

$$(2) \cos(\theta + \theta') = OG = OH - EF.$$

Radius is, in all these demonstrations, taken equal to unity. The similar triangles OBK and OFH give

$$\frac{FH}{BK} = \frac{OH}{OK} = \frac{OF}{OB}.$$

From the first and third ratios we obtain

$$(3) FH = \frac{BK \cdot OF}{OB} = \sin \theta \cos \theta'.$$

From the second and third ratios we obtain

$$(4) \quad OH = \frac{OK \cdot OF}{OB} = \cos \theta \cos \theta'.$$

From the similar triangles OBK and CEF we have

$$\frac{CE}{OK} = \frac{FE}{BK} = \frac{CF}{OB}.$$

$$\therefore (5) \quad CE = \frac{OK \cdot CF}{OB} = \cos \theta \sin \theta'.$$

$$(6) \quad FE = \frac{BK \cdot CF}{OB} = \sin \theta \sin \theta'.$$

Now, substitute (3) and (5) in (1), and (4) and (6) in (2); then

$$\sin(\theta + \theta') = \sin \theta \cos \theta' + \cos \theta \sin \theta', \quad [5]$$

$$\cos(\theta + \theta') = \cos \theta \cos \theta' - \sin \theta \sin \theta'. \quad [6]$$

47. *To determine the sine and the cosine of the difference of two angles or arcs, the sines and cosines of the angles or arcs being known.*

If in [5] and [6], θ' be changed to $-\theta'$, then

$$\sin(\theta - \theta') = \sin \theta \cos \theta' - \cos \theta \sin \theta', \quad [7]$$

$$\cos(\theta - \theta') = \cos \theta \cos \theta' + \sin \theta \sin \theta'. \quad [8]$$

48. *To find the tangent and cotangent of the sum of two angles or arcs.*

By Art. 16, (4), [2],

$$\tan(\theta + \theta') = \frac{\sin(\theta + \theta')}{\cos(\theta + \theta')}.$$

By [5] and [6],

$$\frac{\sin(\theta + \theta')}{\cos(\theta + \theta')} = \frac{\sin \theta \cos \theta' + \cos \theta \sin \theta'}{\cos \theta \cos \theta' - \sin \theta \sin \theta'}.$$

Dividing both terms of the right member by $\cos \theta \cos \theta'$, then

$$\tan(\theta + \theta') = \frac{\tan \theta + \tan \theta'}{1 - \tan \theta \tan \theta'}. \quad [9]$$

Again, by Art. 16, (5), [2],

$$\cot(\theta + \theta') = \frac{\cos(\theta + \theta')}{\sin(\theta + \theta')}.$$

By [6] and [5],

$$\frac{\cos(\theta + \theta')}{\sin(\theta + \theta')} = \frac{\cos \theta \cos \theta' - \sin \theta \sin \theta'}{\sin \theta \cos \theta' + \cos \theta \sin \theta'}.$$

Dividing both terms of the right member by $\sin \theta \sin \theta'$, then

$$\cot(\theta + \theta') = \frac{\cot \theta \cot \theta' - 1}{\cot \theta' + \cot \theta}. \quad [10]$$

49. To find the tangent and cotangent of the difference of two angles or arcs.

If in [9] and [10], θ' be changed to $-\theta'$, then

$$\tan(\theta - \theta') = \frac{\tan \theta - \tan \theta'}{1 + \tan \theta \tan \theta'}. \quad [11]$$

$$\cot(\theta - \theta') = \frac{1 + \cot \theta \cot \theta'}{\cot \theta' - \cot \theta}. \quad [12]$$

50. Formulæ [5], [7], [9], and [11] have been demonstrated on the supposition that $\theta + \theta'$ is not greater than $\frac{1}{2}\pi$. It can be easily shown that they are generally true; that is to say, that the *sines*, *cosines*, *tangents*, and *cotangents* of the sum of two angles or arcs, greater than $\frac{1}{2}\pi$, π , $\frac{3}{2}\pi$, 2π , or $2n\pi$, n being any finite integer, are all represented by the four formulæ named.

For example,

$$\sin(\frac{3}{2}\pi + \theta + \theta') = \sin(\frac{3}{2}\pi + \theta)\cos \theta' + \cos(\frac{3}{2}\pi + \theta)\sin \theta'.$$

51. It is easily shown that

$$\begin{aligned} \sin(\theta + \theta' + \theta'') &= \sin \theta \cos \theta' \cos \theta'' + \sin \theta' \cos \theta \cos \theta'' \\ &\quad + \sin \theta'' \cos \theta \cos \theta' - \sin \theta \sin \theta' \sin \theta''. \end{aligned} \quad [13]$$

$$\begin{aligned} \cos(\theta + \theta' + \theta'') &= \cos \theta \cos \theta' \cos \theta'' - \cos \theta \sin \theta' \sin \theta'' \\ &\quad - \cos \theta' \sin \theta \sin \theta'' - \cos \theta'' \sin \theta \sin \theta'. \end{aligned} \quad [14]$$

Knowing thus the formulæ for the sine and cosine of the sum of three angles or arcs, we may obtain those which will give the sine and the cosine of the sum of four angles or arcs, or of five, or six, or of n angles or arcs.

52. *Important formulæ deduced from [5], [6], [7], and [8].*

$$\left. \begin{array}{l} \text{From [5] and [7], } \sin(\theta + \theta') + \sin(\theta - \theta') = 2 \sin \theta \cos \theta', \\ \qquad \qquad \qquad \sin(\theta + \theta') - \sin(\theta - \theta') = 2 \cos \theta \sin \theta'. \\ \text{From [6] and [8], } \cos(\theta + \theta') + \cos(\theta - \theta') = 2 \cos \theta \cos \theta', \\ \qquad \qquad \qquad \cos(\theta + \theta') - \cos(\theta - \theta') = -2 \sin \theta \sin \theta'. \end{array} \right\} [15]$$

Now, let $\theta + \theta' = \phi$, and $\theta - \theta' = \phi'$; then we shall have

$$\theta = \frac{1}{2}(\phi + \phi'), \text{ and } \theta' = \frac{1}{2}(\phi - \phi'),$$

and the preceding formulæ, [15], become

$$\left. \begin{array}{l} (1) \sin \phi + \sin \phi' = 2 \sin \frac{1}{2}(\phi + \phi') \cos \frac{1}{2}(\phi - \phi'), \\ (2) \sin \phi - \sin \phi' = 2 \sin \frac{1}{2}(\phi - \phi') \cos \frac{1}{2}(\phi + \phi'), \\ (3) \cos \phi + \cos \phi' = 2 \cos \frac{1}{2}(\phi + \phi') \cos \frac{1}{2}(\phi - \phi'), \\ (4) \cos \phi' - \cos \phi = 2 \sin \frac{1}{2}(\phi + \phi') \sin \frac{1}{2}(\phi - \phi'). \end{array} \right\} [16]$$

These last formulæ are frequently employed; they serve to express the sum or difference of two sines or of two cosines in terms of the product of sines, or cosines, or of a sine and a cosine.

53. We may express by a product the sum or the difference of a sine and of a cosine.

We have

$$\cos \phi \pm \sin \phi' = \sin\left(\frac{1}{2}\pi - \phi\right) \pm \sin \phi';$$

and using [16],

$$\left. \begin{array}{l} \cos \phi + \sin \phi' = 2 \sin\left(\frac{1}{4}\pi - \frac{\phi - \phi'}{2}\right) \cos\left(\frac{1}{4}\pi - \frac{\phi + \phi'}{2}\right), \\ \cos \phi - \sin \phi' = 2 \sin\left(\frac{1}{4}\pi - \frac{\phi + \phi'}{2}\right) \cos\left(\frac{1}{4}\pi - \frac{\phi - \phi'}{2}\right). \end{array} \right\} [17]$$

54. It is easily seen that, by division, a new set of important formulæ may be derived from [16].

$$\left. \begin{aligned}
 (1) \quad \frac{\sin \phi + \sin \phi'}{\sin \phi - \sin \phi'} &= \frac{\sin \frac{1}{2}(\phi + \phi') \cos \frac{1}{2}(\phi - \phi')}{\sin \frac{1}{2}(\phi - \phi') \cos \frac{1}{2}(\phi + \phi')} = \frac{\tan \frac{1}{2}(\phi + \phi')}{\tan \frac{1}{2}(\phi - \phi')}, \\
 (2) \quad \frac{\sin \phi + \sin \phi'}{\cos \phi + \cos \phi'} &= \frac{\sin \frac{1}{2}(\phi + \phi')}{\cos \frac{1}{2}(\phi + \phi')} = \tan \frac{1}{2}(\phi + \phi'), \\
 (3) \quad \frac{\sin \phi + \sin \phi'}{\cos \phi' - \cos \phi} &= \frac{\cos \frac{1}{2}(\phi - \phi')}{\sin \frac{1}{2}(\phi - \phi')} = \cot \frac{1}{2}(\phi - \phi'), \\
 (4) \quad \frac{\sin \phi - \sin \phi'}{\cos \phi + \cos \phi'} &= \frac{\sin \frac{1}{2}(\phi - \phi')}{\cos \frac{1}{2}(\phi - \phi')} = \tan \frac{1}{2}(\phi - \phi'), \\
 (5) \quad \frac{\sin \phi - \sin \phi'}{\cos \phi' - \cos \phi} &= \frac{\cos \frac{1}{2}(\phi + \phi')}{\sin \frac{1}{2}(\phi + \phi')} = \cot \frac{1}{2}(\phi + \phi'), \\
 (6) \quad \frac{\cos \phi + \cos \phi'}{\cos \phi' - \cos \phi} &= \frac{\cos \frac{1}{2}(\phi + \phi') \cos \frac{1}{2}(\phi - \phi')}{\sin \frac{1}{2}(\phi + \phi') \sin \frac{1}{2}(\phi - \phi')} \\
 &= \cot \frac{1}{2}(\phi + \phi') \cot \frac{1}{2}(\phi - \phi').
 \end{aligned} \right\} [18]$$

55. *Functions of double angles or arcs.*

If in formulæ [5], [6], [9], and [10], θ' be made equal to θ , then,

$$\sin 2\theta = 2 \sin \theta \cos \theta, \quad [19]$$

$$\cos 2\theta = \cos^2 \theta - \sin^2 \theta, \quad [20]$$

$$\tan 2\theta = \frac{2 \tan \theta}{1 - \tan^2 \theta}, \quad [21]$$

$$\cot 2\theta = \frac{\cot^2 \theta - 1}{2 \cot \theta}. \quad [22]$$

56. *Functions of half angles or arcs.*

By [19], $2 \sin \frac{1}{2} \theta \cos \frac{1}{2} \theta = \sin \theta$.

By Art. 21, (1), [4], $\cos^2 \frac{1}{2} \theta + \sin^2 \frac{1}{2} \theta = 1$;

from which, by addition and subtraction, we obtain

$$(\cos \frac{1}{2} \theta + \sin \frac{1}{2} \theta)^2 = 1 + \sin \theta,$$

$$(\cos \frac{1}{2} \theta - \sin \frac{1}{2} \theta)^2 = 1 - \sin \theta.$$

$$\therefore \cos \frac{1}{2} \theta + \sin \frac{1}{2} \theta = \pm \sqrt{1 + \sin \theta},$$

$$\cos \frac{1}{2} \theta - \sin \frac{1}{2} \theta = \pm \sqrt{1 - \sin \theta};$$

$$\therefore \sin \frac{1}{2}\theta = \pm \frac{1}{2}(\sqrt{1 + \sin \theta} \mp \sqrt{1 - \sin \theta}). \quad [23]$$

$$\cos \frac{1}{2}\theta = \pm \frac{1}{2}(\sqrt{1 + \sin \theta} \pm \sqrt{1 - \sin \theta}). \quad [24]$$

Resuming formulæ [20], and (1) of [4], Art. 21,

$$\cos^2 \frac{1}{2}\theta - \sin^2 \frac{1}{2}\theta = \cos \theta,$$

$$\cos^2 \frac{1}{2}\theta + \sin^2 \frac{1}{2}\theta = 1,$$

we obtain by addition and subtraction, and extracting the square root,

$$\cos \frac{1}{2}\theta = \pm \sqrt{\frac{1 + \cos \theta}{2}}, \quad [25]$$

$$\sin \frac{1}{2}\theta = \pm \sqrt{\frac{1 - \cos \theta}{2}}. \quad [26]$$

It will be noticed that [23] and [24] give four values for $\sin \frac{1}{2}\theta$, and four values for $\cos \frac{1}{2}\theta$, respectively; and it is remarkable that the values of $\cos \frac{1}{2}\theta$ are precisely the same as those of $\sin \frac{1}{2}\theta$.

By (4) of [2], Art. 16, and [25] and [26],

$$\tan \frac{1}{2}\theta = \frac{\sin \frac{1}{2}\theta}{\cos \frac{1}{2}\theta} = \sqrt{\frac{1 - \cos \theta}{1 + \cos \theta}},$$

which becomes, when both terms of the radical are multiplied by

$$\sqrt{1 + \cos \theta}, \text{ or by } \sqrt{1 - \cos \theta}.$$

$$\tan \frac{1}{2}\theta = \frac{\sin \theta}{1 + \cos \theta} = \frac{1 - \cos \theta}{\sin \theta}. \quad [27]$$

$$\text{In like manner, } \cot \frac{1}{2}\theta = \frac{1 + \cos \theta}{\sin \theta} = \frac{\sin \theta}{1 - \cos \theta}. \quad [28]$$

57. If we wish to express $\sin 2\theta$ or $\cos 2\theta$ in terms of $\sin \theta$ or $\cos \theta$ only, we must replace $\sin \theta$ by its value $\pm \sqrt{1 - \cos^2 \theta}$, and $\cos \theta$ by $\pm \sqrt{1 - \sin^2 \theta}$.

Formulæ [19] will then become

$$\sin 2\theta = \pm 2 \sin \theta \sqrt{1 - \sin^2 \theta} = \pm 2 \cos \theta \sqrt{1 - \cos^2 \theta}, \quad [29]$$

and [20] will become

$$\cos 2\theta = 1 - 2 \sin^2 \theta = 2 \cos^2 \theta - 1. \quad [30]$$

These results are such that if we know the values of $\sin \theta$ and $\cos \theta$, then $\cos 2\theta$ will be completely determined, but the $\sin 2\theta$ will have two equal values, one of which is positive and the other negative. It is important to remember the effect of the double sign, in order to determine the quadrant to which the function belongs.

58. EXAMPLES.

SET IV.

1. Show that $\sin(45^\circ + \theta) = \cos(45^\circ - \theta)$.
2. Show that $\sin \theta = \frac{2 \tan \frac{1}{2} \theta}{1 + \tan^2 \frac{1}{2} \theta}$.
3. Show that $\frac{\cos \theta + \sin \theta}{\cos \theta - \sin \theta} = \tan 2\theta + \sec 2\theta$.
4. Show that $\frac{\cos(\theta + 45^\circ)}{\cos(\theta - 45^\circ)} = \sec 2\theta - \tan 2\theta$.
5. Find the value of x in $90^\circ + \text{arc-sin } x = \text{arc-tan } x$.
6. Show that $\frac{\sin(\theta \pm \theta')}{\sin \theta \sin \theta'} = \cot \theta' \pm \cot \theta$.
7. Show that $\frac{\cos(\theta \pm \theta')}{\sin \theta \sin \theta'} = \cot \theta \cot \theta' \mp 1$.
8. Show that $\frac{\sin(\theta + \theta')}{\sin(\theta - \theta')} = \frac{\tan \theta + \tan \theta'}{\tan \theta - \tan \theta'}$.
9. Show that $\frac{\sin(\theta \pm \theta')}{\cos(\theta \mp \theta')} = \frac{\tan \theta \pm \tan \theta'}{1 \pm \tan \theta \tan \theta'}$.
10. Show that $\tan(\theta + \theta' + \theta'')$

$$= \frac{\tan \theta + \tan \theta' + \tan \theta'' - \tan \theta \tan \theta' \tan \theta''}{1 - \tan \theta \tan \theta' - \tan \theta \tan \theta'' - \tan \theta' \tan \theta''}$$
11. Show that $\sin 3\theta = 3 \sin \theta - 4 \sin^3 \theta$.
12. Show that $\cos 3\theta = 4 \cos^3 \theta - 3 \cos \theta$.
13. Show that $\sin 4\theta = 4(\sin \theta - 2 \sin^3 \theta) \cos \theta$.
14. Show that $\sin 5\theta = 5 \sin \theta - 20 \sin^3 \theta + 16 \sin^5 \theta$.
15. Show that $\tan 5\theta = \frac{\tan 4\theta + \tan \theta}{1 - \tan 4\theta \tan \theta} = \frac{\tan 3\theta + \tan 2\theta}{1 - \tan 3\theta \tan 2\theta}$.

16. Find the value of θ in $3 \tan \theta \tan 3\theta + 1 = 0$, when $\theta < \frac{\pi}{2}$.
Also, when $\theta < \pi$.

17. Show that $2 \tan 2\theta = \tan(45^\circ + \theta) - \tan(45^\circ - \theta)$.

18. Show that $\frac{\cos \theta - \cos 3\theta}{\sin 3\theta - \sin \theta} = \tan 2\theta$.

19. Find the value of θ when $\sin 4\theta + \sin \theta = 0$.

20. Find the value of θ when $\tan \theta + \tan(\frac{1}{2}\pi + \theta) = 2$.

21. Find $\tan \theta$ when $\tan \theta + ab \cot \theta = a + b$.

22. If $\theta + \theta' + \theta'' = 180^\circ$, show that

$$\tan \theta + \tan \theta' + \tan \theta'' = \tan \theta \tan \theta' \tan \theta''.$$

23. Take (10), and show that $\tan 3\theta = \frac{3 \tan \theta - \tan^3 \theta}{1 - 3 \tan^2 \theta}$.

24. If $\theta + \theta' + \theta'' = 90^\circ$, show that

$$1 = \tan \theta \tan \theta' + \tan \theta \tan \theta'' + \tan \theta' \tan \theta''.$$

25. If $\theta + \theta' + \theta'' = 180^\circ$, show that

$$\sin \theta + \sin \theta' + \sin \theta'' = 4 \cos \frac{1}{2}\theta \cos \frac{1}{2}\theta' \cos \frac{1}{2}\theta''.$$

26. Show that $\cos \theta + \cos(120^\circ - \theta) + \cos(120^\circ + \theta) = 0$.

27. Show that $4 \sin \theta \sin(60^\circ - \theta) \sin(60^\circ + \theta) = \sin 3\theta$.

28. Show that $\frac{\tan \theta \pm \tan \theta'}{\cot \theta \pm \cot \theta'} = \pm \tan \theta \tan \theta'$.

29. Find the value of $\sin(45^\circ + 30^\circ)$.

30. The functions of 30° being given (Art. 23), find those of 15° .

31. Given $\sin \theta = m \sin \theta'$, and $\tan \theta = n \tan \theta'$; find $\sin \theta$ and $\cos \theta'$.

32. If $\theta + \theta' + \theta'' = 180^\circ$, show that

$$\sin^2 \theta + \sin^2 \theta' + \sin^2 \theta'' - 2 \cos \theta \cos \theta' \cos \theta'' = 2.$$

33. Given $\sin 210^\circ = -\frac{1}{2}$; find $\cos 105^\circ$.

34. Given $\tan 2\theta = -\frac{2}{7}$; find $\sin \theta$ and $\cos \theta$.

35. Find the value of θ when

$$\sin 3\theta + \sin 2\theta + \sin \theta = 0.$$

CHAPTER V.

ANGLES, OBLIQUE TRIANGLES, AND CIRCLES.

59. Relations between the angles and the sides of an oblique triangle.

THEOREM I. In every plane triangle, the sides are proportional to the sines of the angles opposite.

Let ABC (Fig. 10) be a triangle whose angles A and C are acute; from the vertices B and C draw the perpendiculars BD to the base AC , and CE to the side AB .

The two right triangles ABD and DBC will give, by Art. 15,

$$BD = c \sin A,$$

and

$$BD = a \sin C.$$

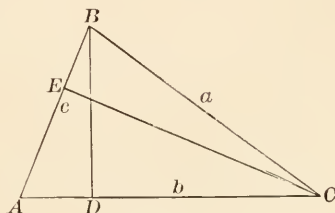


FIG. 10.

$$(1) \quad \therefore c \sin A = a \sin C.$$

The two right triangles CEA and CEB will, in like manner, give

$$CE = b \sin A, \quad \text{and} \quad CE = a \sin B.$$

$$(2) \quad \therefore b \sin A = a \sin B.$$

Hence

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}. \quad [31]$$

If an angle of the triangle ABC (Fig. 11), C , for example, be obtuse, the perpendicular BD will fall upon the base produced.

Since two supplementary angles have the same sine, the triangles ABD and CBD give, as before,

$$BD = c \sin A = a \sin C;$$

from which we conclude that the preceding formula is general.

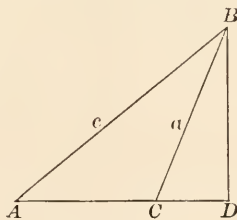


FIG. 11.

We have, therefore, the three following relations between the angles and the sides of a triangle :

$$\left. \begin{aligned} A + B + C &= 180^\circ, \\ \frac{a}{\sin A} &= \frac{b}{\sin B}, \\ \frac{a}{\sin A} &= \frac{c}{\sin C}. \end{aligned} \right\} [32]$$

It is readily seen that these three formulæ may be written

$$\begin{aligned} A &= 180^\circ - B - C, \\ b &= \frac{a \sin B}{\sin (B + C)}, \\ c &= \frac{a \sin C}{\sin (B + C)}. \end{aligned}$$

60. THEOREM II. *In any plane triangle the square of any side is equal to the sum of the squares of the other two sides, less twice the product of these two sides by the cosine of their included angle.*

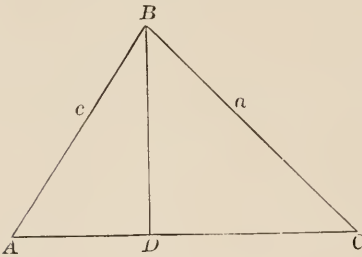


FIG. 12.

Let ABC (Fig. 12) be a triangle whose angle C is acute. Draw from the vertex B , to the base AC , the perpendicular BD . By Geometry, we have

$$c^2 = a^2 + b^2 - 2b \times CD;$$

but the right triangle BCD gives, Art 15,

$$CD = a \cos C.$$

$$\left. \begin{aligned} \therefore c^2 &= a^2 + b^2 - 2ab \cos C, \\ \text{In like manner, } a^2 &= b^2 + c^2 - 2bc \cos A, \\ b^2 &= a^2 + c^2 - 2ac \cos B. \end{aligned} \right\} [33]$$

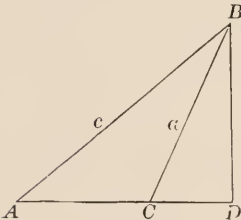


FIG. 13.

If the angle C (Fig. 13) be obtuse, we have

$$c^2 = a^2 + b^2 + 2b \times CD.$$

The right triangle CBD gives

$$CD = a \cos BCD.$$

But $\cos BCD = \cos(180^\circ - BCA) = -\cos BCA.$

$$\therefore c^2 = a^2 + b^2 - 2ab \cos BCA.$$

\therefore the formulæ [33] are general.

61. If each of the angles A , B , and C be made successively a right angle, what form will [31] assume? What form will [33] assume?

62. THEOREM III. *In any plane triangle, any side is equal to the sum of the other two, each multiplied by the cosine of the angle which that side makes with the first side.*

Let BD be a perpendicular from the vertex B upon the base AC of the triangle ABC (Fig. 14).

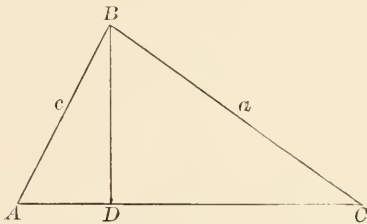


FIG. 14.

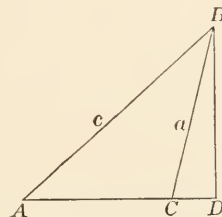


FIG. 15.

We have, if the angles A and C are acute,

$$b = AD + DC;$$

but if one of the angles, as C , is obtuse (Fig. 15), then

$$b = AD - DC.$$

In the first case, $DC = a \cos C.$

In the second case, $DC = a \cos(180^\circ - C) = -a \cos C.$

And in both cases, $AD = c \cos A.$

We shall have

$$\left. \begin{aligned} (1) \quad a &= b \cos C + c \cos B, \\ (2) \quad b &= c \cos A + a \cos C, \\ (3) \quad c &= a \cos B + b \cos A. \end{aligned} \right\} \quad [34]$$

63. Formulæ [34] may be obtained from [33] by adding those of [33] two and two, and reducing the results. Reciprocally, the first of [33] may be obtained from [34] by adding the three equations of [34], after having multiplied (1) by a , (2) by b , and (3) by $-c$.

In like manner the others may be obtained.

64. THEOREM IV. *In any triangle, the sum of two sides is to their difference as the tangent of half the sum of the opposite angles is to the tangent of half their difference.*

From the fundamental formulæ [31],

$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c},$$

we obtain

$$(1) \frac{a+b}{c} = \frac{\sin A + \sin B}{\sin C} = \frac{2 \sin \frac{1}{2}(A+B) \cos \frac{1}{2}(A-B)}{\sin C},$$

$$(2) \frac{a-b}{c} = \frac{\sin A - \sin B}{\sin C} = \frac{2 \sin \frac{1}{2}(A-B) \cos \frac{1}{2}(A+B)}{\sin C};$$

whence, dividing (1) by (2), we have

$$\frac{a+b}{a-b} = \frac{\tan \frac{1}{2}(A+B)}{\tan \frac{1}{2}(A-B)}. \quad [35]$$

65. *Other formulæ relating to oblique triangles.*

The relation $a^2 = b^2 + c^2 - 2bc \cos A$,

when changed to the form

$$\cos A = \frac{b^2 + c^2 - a^2}{2bc},$$

will give the angle A ; and the other two formulæ of [33] will, in like manner, give the angles B and C .

We shall now proceed to establish formulæ for the functions of $\frac{1}{2}A$, $\frac{1}{2}B$, and $\frac{1}{2}C$.

From [25] and [26] we have

$$(1) \cos \frac{1}{2}A = \sqrt{\frac{1 + \cos A}{2}},$$

$$(2) \sin \frac{1}{2}A = \sqrt{\frac{1 - \cos A}{2}};$$

and, substituting for $\cos A$ its value $\frac{b^2 + c^2 - a^2}{2bc}$ in (1), we have

$$(1) \cos \frac{1}{2}A \\ = \sqrt{\frac{2bc + b^2 + c^2 - a^2}{4bc}} = \sqrt{\frac{(b+c)^2 - a^2}{4bc}} = \sqrt{\frac{(a+b+c)(-a+b+c)}{4bc}};$$

and in (2) also,

$$(2) \sin \frac{1}{2}A \\ = \sqrt{\frac{2bc - b^2 - c^2 + a^2}{4bc}} = \sqrt{\frac{a^2 - (b-c)^2}{4bc}} = \sqrt{\frac{(a+b-c)(a-b+c)}{4bc}}.$$

Now divide (2) by (1);

then

$$(3) \frac{\sin \frac{1}{2}A}{\cos \frac{1}{2}A} = \tan \frac{1}{2}A = \sqrt{\frac{(a+b-c)(a-b+c)}{(a+b+c)(-a+b+c)}}.$$

If we put $a + b + c = 2s$,

then $-a + b + c = 2(s - a)$,

$$a - b + c = 2(s - b),$$

$$a + b - c = 2(s - c).$$

Now substitute these values in equations (2), (1), and (3), and developing similar equations for $\frac{1}{2}B$ and $\frac{1}{2}C$, we shall have three systems of formulæ:

$$\left. \begin{aligned} \sin \frac{1}{2}A &= \sqrt{\frac{(s-b)(s-c)}{bc}}, \\ \sin \frac{1}{2}B &= \sqrt{\frac{(s-a)(s-c)}{ac}}, \\ \sin \frac{1}{2}C &= \sqrt{\frac{(s-a)(s-b)}{ab}}. \end{aligned} \right\} [36]$$

$$\left. \begin{aligned} \cos \frac{1}{2}A &= \sqrt{\frac{s(s-a)}{bc}}, \\ \cos \frac{1}{2}B &= \sqrt{\frac{s(s-b)}{ac}}, \\ \cos \frac{1}{2}C &= \sqrt{\frac{s(s-c)}{ab}}. \end{aligned} \right\} [37]$$

$$\left. \begin{aligned} \tan \frac{1}{2} A &= \sqrt{\frac{(s-b)(s-c)}{s(s-a)}}, \\ \tan \frac{1}{2} B &= \sqrt{\frac{(s-a)(s-c)}{s(s-b)}}, \\ \tan \frac{1}{2} C &= \sqrt{\frac{(s-a)(s-b)}{s(s-c)}}. \end{aligned} \right\} [38]$$

In all of [36], [37], and [38], the radicals must be taken with the sign +; for the half-angles of any triangle are, each, less than 90° , and consequently their trigonometric functions are positive.

66. Area of Triangles.

Let the perpendicular BD be drawn from the vertex B of the triangle ABC to the base AC or AC produced.

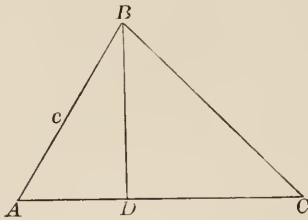


FIG. 16.

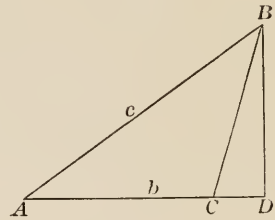


FIG. 17.

Designating the area of a triangle by K , we have

$$K = \frac{1}{2} b \times BD.$$

But from the right triangle ABD we have $BD = c \sin A$, in either figure.

$$\therefore K = \frac{1}{2} bc \sin A. \quad [39]$$

Therefore, *the area of a triangle equals one-half the product of two sides multiplied by the sine of the angle included between those sides.*

Show that *the area of any quadrilateral equals one-half the product of its diagonals multiplied by the sine of the angle between those diagonals.*

67. To find the area of a triangle in terms of its three sides.

If in formula [39] we replace c by its value taken from [31],

$$\frac{c}{b} = \frac{\sin C}{\sin B} = \frac{\sin C}{\sin(A+C)}, \text{ whence } c = \frac{b \sin C}{\sin(A+C)},$$

[39] will become
$$K = \frac{1}{2} \frac{b^2 \sin A \sin C}{\sin(A+C)}.$$

Finally, from equations,

$$\sin \frac{1}{2} A = \sqrt{\frac{(s-c)(s-b)}{bc}},$$

and
$$\cos \frac{1}{2} A = \sqrt{\frac{s(s-a)}{bc}},$$

established in Art. 65, we obtain

$$\sin A = 2 \sin \frac{1}{2} A \cos \frac{1}{2} A = 2 \frac{\sqrt{s(s-a)(s-b)(s-c)}}{bc};$$

and if we replace $\sin A$, in formula [39], by this value, then

$$K = \sqrt{s(s-a)(s-b)(s-c)}. \tag{40}$$

By means of [36], [37], [38], and [40], it may be shown that

$$\left. \begin{aligned} (1) \quad \sin \frac{1}{2} A \sin \frac{1}{2} B \sin \frac{1}{2} C &= \frac{(s-a)(s-b)(s-c)}{abc} = \frac{K^2}{sabc}, \\ (2) \quad \cos \frac{1}{2} A \cos \frac{1}{2} B \cos \frac{1}{2} C &= \frac{s \sqrt{s(s-a)(s-b)(s-c)}}{abc} = \frac{Ks}{abc}, \\ (3) \quad \tan \frac{1}{2} A \tan \frac{1}{2} B \tan \frac{1}{2} C & \dots \dots \dots = \frac{K}{s^2}. \end{aligned} \right\} \tag{41}$$

Show that
$$(1) \quad \frac{s}{c} = \frac{\cos \frac{1}{2} A \cos \frac{1}{2} B}{\sin \frac{1}{2} C},$$

$$(2) \quad \frac{s-c}{c} = \frac{\sin \frac{1}{2} A \sin \frac{1}{2} B}{\sin \frac{1}{2} C},$$

$$(3) \quad \frac{s-b}{c} = \frac{\sin \frac{1}{2} A \cos \frac{1}{2} B}{\cos \frac{1}{2} C},$$

$$(4) \quad \frac{s-a}{c} = \frac{\cos \frac{1}{2} A \sin \frac{1}{2} B}{\cos \frac{1}{2} C}.$$

68. Radii of circumscribed, inscribed, and escribed circles.

- (1) Having circumscribed the circle whose centre is O (Fig. 18) about the triangle ABC , draw from the vertex B the diameter $BD = 2R$, and draw CD . The angle $A =$ the angle D ; the triangle BCD is a right triangle.

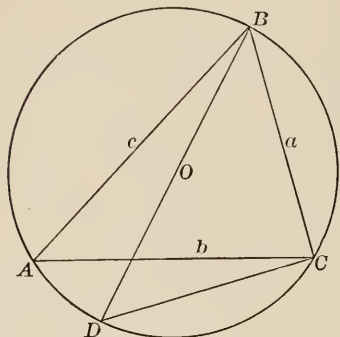


FIG. 18.

$$\therefore a = 2R \sin D = 2R \sin A.$$

$$\therefore R = \frac{a}{2 \sin A}.$$

Multiplying both terms of $\frac{a}{2 \sin A}$ by bc , we have

$$R = \frac{abc}{2bc \sin A};$$

then, multiplying both [39] and [40] by 4, we have

$$4K = 2bc \sin A = 4 \sqrt{s(s-a)(s-b)(s-c)}.$$

$$\therefore R = \frac{abc}{4 \sqrt{s(s-a)(s-b)(s-c)}}. \quad [42]$$

- (2) Let the circle (Fig. 19), whose centre is O and radius $= r$, be inscribed in the triangle ABC . The lines OA , OB , and OC divide the triangle into three triangles, whose bases are a , b , and c , respectively, and whose common altitude is r .

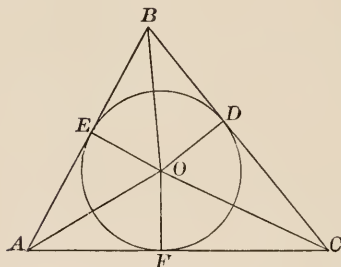


FIG. 19.

As before, let

$$K = \text{the area of } ABC,$$

$$\text{and } s = \frac{1}{2}(a + b + c);$$

$$\text{then } K = rs,$$

$$\text{and } r = \frac{K}{s}.$$

$$\text{But by [40]} \quad K = \sqrt{s(s-a)(s-b)(s-c)}.$$

$$\therefore r = \sqrt{\frac{(s-a)(s-b)(s-c)}{s}}. \quad [43]$$

(3) If we designate by r' , r'' , and r''' the radii of the escribed circles, that is to say, the circles which touch respectively the sides

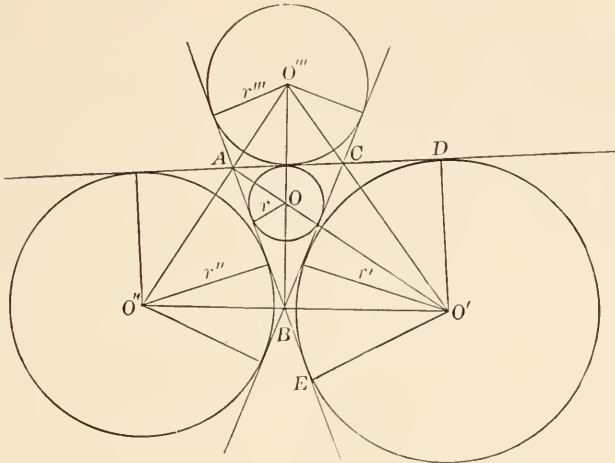


FIG. 20.

a , b , and c , and the prolongations of the other two sides, then it can be easily shown (Fig. 20) that from the area of the triangle ABC , which equals

$$\sqrt{s(s-a)(s-b)(s-c)} = K, \quad [40], \text{ Art. 67.}$$

$$= (s-a)r' = (s-b)r'' = (s-c)r''',$$

we can obtain

$$\left. \begin{aligned} r' &= \frac{K}{s-a} = \sqrt{\frac{s(s-b)(s-c)}{s-a}} \\ r'' &= \frac{K}{s-c} = \sqrt{\frac{s(s-a)(s-b)}{s-c}} \\ r''' &= \frac{K}{s-b} = \sqrt{\frac{s(s-a)(s-c)}{s-b}} \end{aligned} \right\} [44]$$

The formulæ just obtained may, by Art. 65, be written

$$\left. \begin{aligned} r' &= s \tan \frac{1}{2} A, \\ r'' &= s \tan \frac{1}{2} C, \\ r''' &= s \tan \frac{1}{2} B. \end{aligned} \right\} [45]$$

From the foregoing formulæ many others may be derived, among which are the following:

$$\left. \begin{aligned} \frac{1}{r} &= \frac{1}{r'} + \frac{1}{r''} + \frac{1}{r'''} \\ K &= \sqrt{r r' r'' r'''} \\ 4R^* &= r' + r'' + r''' - r. \end{aligned} \right\} [46]$$

EXERCISES.

SET V.

1. If a' , b' , c' be the perpendiculars from the centre of the circumscribed circle upon the sides a , b , c , respectively, of the triangle ABC ; then

$$\frac{a}{a'} + \frac{b}{b'} + \frac{c}{c'} = \frac{1}{4} \cdot \frac{abc}{a'b'c'}.$$

2. Prove that the product of the perpendiculars of a triangle from the angles on the opposite sides equals

$$\frac{[(a+b+c)r]^3}{abc},$$

r being the radius of the inscribed circle.

3. If R and r be radii of circles circumscribed about and inscribed in a regular polygon whose side is $2a$; then

$$R^2 - r^2 = a^2.$$

4. If r , r' be radii of the circumscribed and inscribed circles of a regular polygon of n sides, show that

$$r + r' = a \cot \frac{\pi}{2n},$$

where $2a$ is one of the sides.

5. If the radius of a circle be r , show that the length of an arc which subtends an angle of θ° at the centre is $\frac{\pi r \theta}{180}$.

* R = the radius of the circumscribed circle.

CHAPTER VI.

SOLUTION OF OBLIQUE TRIANGLES.

69. CASE I. *To solve a triangle, when two angles and one side are given.*

The unknown angle is obtained by the formula

$$A + B + C = 180^\circ.$$

If a be the given side, we obtain the sides b and c by the formulæ

$$b = \frac{a \sin B}{\sin A},$$

$$c = \frac{a \sin C}{\sin A}.$$

70. EXAMPLE. Given $A = 81^\circ 47' 12''.5$,

$$B = 38^\circ 12' 47''.5,$$

$$a = 7012.24; \quad \text{to find } C, b, \text{ and } c.$$

$$(1) \quad A + B + C = 180^\circ. \quad \therefore C = 60^\circ.$$

$$(2) \quad b = \frac{a \sin B}{\sin A}. \quad (3) \quad c = \frac{a \sin C}{\sin A}.$$

$$\log a = 3.845856 \quad \log a = 3.845856$$

$$\log \sin B = 9.791402 \quad \log \sin C = 9.937530$$

$$\log \sin A = 0.004477 \quad \text{colog } \sin A = 0.004477$$

$$\log b = 3.641735 \quad \log c = 3.787863$$

$$\therefore b = 4382.65. \quad \therefore c = 6135.71.$$

71. CASE II. *To solve a triangle, when two sides and the angle opposite one of them are given.*

If a , b , and A are the given elements, we may determine the unknown parts by the formulæ

$$\sin B = \frac{b \sin A}{a},$$

$$A + B + C = 180^\circ,$$

$$c = \frac{a \sin C}{\sin A}.$$

When the angle B differs but little from 90° , it cannot be exactly determined by means of the sine.

In the case of a right triangle there can be no uncertainty as to the angles, because one being a right angle, either of the other two angles can be exactly determined from the formula $A + B = 90^\circ$.

But when an angle of an oblique triangle is determined from its sine or cosecant, then uncertainty may exist, since there are two angles each less than 180° having a given sine or cosecant.

There can be no doubt as to the cosine, tangent, cotangent, or secant.

In this case, the solution may determine two triangles, one triangle, or none.

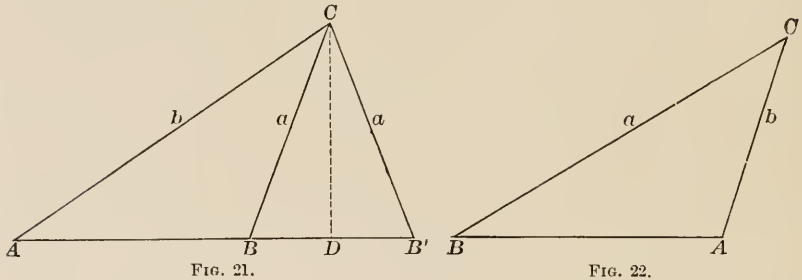


FIG. 21.

FIG. 22.

Suppose A to be the given angle, and a and b the given sides. The angle B is found by the formula

$$\sin B = \frac{b \sin A}{a}.$$

(1) If $\frac{b \sin A}{a} < 1$ (Fig. 21), then two angles, B and B' , will be determined, one $> 90^\circ$, and the other $< 90^\circ$.

Now, if $a > b$, then the angle $A >$ the angle B ; therefore B must be an acute angle, and there will be but one triangle.

But if $a < b$, then either B or B' will meet the conditions, and two triangles will be determined.

The angle C will have two values, and the side c also will have two values.

(2) If $\frac{b \sin A}{a} = 1$, it is clear that the figure is then a right triangle.

(3) If $\frac{b \sin A}{a} > 1$, no triangle exists.

(4) If $A > 90^\circ$ (Fig. 22), and $a > b$, there will be but one triangle, as in (1).

But if $A > 90^\circ$ and $a < b$, there will be no triangle.

EXAMPLE. Given $A = 27^\circ 47' 44''.77$,
 $a = 2199.12$,
 $b = 2513.28$; to find B , C , and c .

$$(1) \sin B = \frac{b \sin A}{a}$$

$$\log b = 3.400240$$

$$\log \sin A = 9.668685$$

$$\text{colog } a = \underline{4.657751}$$

$$\log \sin B = 1.726676$$

$$\therefore B = 32^\circ 12' 15''.23$$

$$\text{and } 147^\circ 47' 44''.77.$$

$$(2) C = 180^\circ - (A + B).$$

$$\therefore \text{when } B = 32^\circ 12' 15''.23, \quad C = 120^\circ 0' 0'';$$

$$\text{and when } B = 147^\circ 47' 44''.77, \quad C = 4^\circ 24' 30''.66.$$

$$(3) c = \frac{a \sin C}{\sin A}$$

$$\log a = 3.342248$$

$$\log a = 3.342248$$

$$\log \sin C = 9.937530$$

$$\log \sin C = 8.885735$$

$$\text{colog } \sin A = 0.331314$$

$$\text{colog } \sin A = \underline{0.331314}$$

$$\log c = 3.611092$$

$$\log c = 2.559297$$

$$\therefore c = 4084.08.$$

$$\therefore c = 362.493.$$

72. CASE III. *To solve a triangle, when two sides and their included angle are given.*

Let a , b , and C be the given parts; then, to find the angles A and B , we may employ formula [35],

$$\frac{a+b}{a-b} = \frac{\tan \frac{1}{2}(A+B)}{\tan \frac{1}{2}(A-B)},$$

and the side c by

$$c = \frac{a \sin C}{\sin A}.$$

EXAMPLE. Given $a = 153$,
 $b = 137$,
 $C = 40^\circ 33' 12''$.

$$(1) \quad a + b = 290, \quad a - b = 16, \quad \text{and} \quad \frac{1}{2}(A + B) = 69^\circ 43' 24''.$$

$$\log(a - b) = 1.204120$$

$$\log \tan \frac{1}{2}(A + B) = 10.432446$$

$$\text{colog}(a + b) = \overline{3.537602}$$

$$\log \tan \frac{1}{2}(A - B) = 9.174168$$

$$\therefore \frac{1}{2}(A - B) = 8^\circ 29' 37'',$$

$$\frac{1}{2}(A + B) + \frac{1}{2}(A - B) = A = 78^\circ 13' 1'',$$

$$\frac{1}{2}(A + B) - \frac{1}{2}(A - B) = B = 61^\circ 13' 47''.$$

$$(2) \quad c = \frac{a \sin C}{\sin A}.$$

$$\log a = 2.184691$$

$$\log \sin C = 9.813018$$

$$\text{colog} \sin A = \overline{0.009249}$$

$$\log c = 2.006958$$

$$\therefore c = 101.616.$$

Problems under this case may be readily solved by the formula

$$c = \sqrt{a^2 + b^2 - 2ab \cos C}, \quad [33], \text{ Art. } 60,$$

when the side c is required.

The angles A and B may then be found by [31].

73. *To solve a triangle, when the three sides are given.*

The formulæ of [33], which determine the angles A , B , and C , by the sides, are not adapted to logarithmic computation; but those of Art. 65 may be employed; particularly the last set, [38], which determine the angles $\frac{1}{2}A$, $\frac{1}{2}B$, and $\frac{1}{2}C$, by their tangents.

EXAMPLE. Given $a = 701.224$,
 $b = 438.265$,
 $c = 613.571$; to find A , B , and C .

$$(1) \quad \text{Let} \quad s = \frac{1}{2}(a + b + c) = 876.530,$$

$$s - a = 175.306,$$

$$s - b = 438.265,$$

$$s - c = 262.959.$$

$$(2) \tan \frac{1}{2} A = \sqrt{\frac{(s-b)(s-c)}{s(s-a)}}. \quad (3) \tan \frac{1}{2} B = \sqrt{\frac{(s-a)(s-c)}{s(s-b)}}.$$

$$\log(s-b) = 2.641736$$

$$\log(s-a) = 2.243796$$

$$\log(s-c) = 2.419888$$

$$\log(s-c) = 2.419888$$

$$\text{colog}(s-a) = \bar{3}.756203$$

$$\text{colog}(s-b) = \bar{3}.358263$$

$$\text{colog } s = \bar{3}.057233$$

$$\text{colog } s = \bar{3}.057233$$

$$\begin{array}{r} 2) \underline{1.875061} \end{array}$$

$$\begin{array}{r} 2) \underline{1.079180} \end{array}$$

$$\log \tan \frac{1}{2} A = 1.937530$$

$$\log \tan \frac{1}{2} B = 1.539590$$

$$\therefore \frac{1}{2} A = 40^\circ 53' 36''.22.$$

$$\therefore \frac{1}{2} B = 19^\circ 6' 23''.77.$$

$$A = 81^\circ 47' 12''.44.$$

$$B = 38^\circ 12' 47''.54.$$

$$(4) \tan \frac{1}{2} C = \sqrt{\frac{(s-a)(s-b)}{s(s-c)}}.$$

$$\log(s-a) = 2.243796$$

$$\log(s-b) = 2.641736$$

$$\text{colog}(s-c) = \bar{3}.580111$$

$$\text{colog } s = 3.057233$$

$$\begin{array}{r} 2) \underline{1.522876} \end{array}$$

$$\log \tan \frac{1}{2} C = 1.761438$$

$$\therefore \frac{1}{2} C = 30^\circ,$$

$$C = 60^\circ.$$

74. EXAMPLES.**SET VI.**

1. The sides of a triangle are in the ratio of $2 : \sqrt{6} : 1 + \sqrt{3}$. Determine the angles.

2. The sides of a triangle are 32, 40, and 66. Find the greatest angle.

3. Given $b = 14$, $c = 11$, and $A = 60^\circ$; to find B .

4. Given $a = 70$, $b = 35$, and $C = 36^\circ 52' 12''$. Solve the triangle.

5. Given $a = 18$, $c = 2$, and $B = 55^\circ$. Find the other angles.

6. $A = 45^\circ 50'$, $B = 60^\circ 15'$, and $c = 25$. Solve the triangle.

7. $B = 25^\circ 18'$, $C = 130^\circ 15'$, and $b = 480$. Solve the triangle.

8. Two sides of a triangle are 3 feet and 5 feet respectively, and the included angle is 120° . Solve the triangle.

9. The sides of a triangle are 4, 5, and 6. Find the angles.

10. In a triangle ABC , the side AB is 254.3, the side AC 396.8, and the angle B $94^\circ 29'$. Solve the triangle.

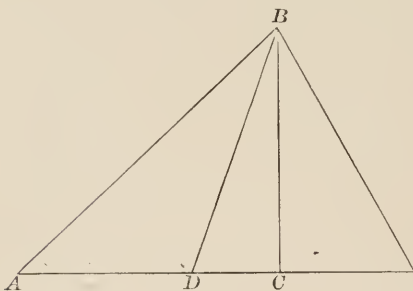
11. Given $a = 201$, $b = 140$, and $B = 36^\circ 44'$; to solve the triangle. Are there two triangles?

12. The sides of a triangle are 18, 19, and 20. Find the angles.

13. Given $A = 32^\circ$, $a = 40$, and $b = 50$; to solve the triangle. Are there two triangles?

14. Given $A = 18^\circ 52' 13''$, $a = 27.465$, and $b = 13.189$. Solve the triangle.

15. The distance $AB = 600$ yards; the angle $BAC = 57^\circ 35'$, and the angle $ABC = 64^\circ 51'$. Find AC and BC .



16. Find BC , the height of a hill above a horizontal plane; AD being equal to 1000 feet; the angle A , $15^\circ 36'$; and ABD , $27^\circ 29'$.

17. A tower 150 feet high throws a shadow 75 feet long upon the horizontal plane on which it stands. Find the altitude of the sun.

18. A person standing at the edge of a river observes that the top of a tower on the opposite edge makes an angle of 55° with a horizontal line drawn from his eye; walking 30 feet back from the edge, the angle then is 48° . Find the breadth of the river.

19. Find the area of a plane triangle whose sides are 24 feet, 30 feet, and 18 feet, respectively.

20. The sides of a triangle are 3, 5, and 6. Compare the radii of the circumscribed and inscribed circles.

21. The sides of a triangle are 75 and 85, and the difference of the angles opposite those sides is 60° . Find all the angles.

22. Find the area of a triangular field, one of whose sides is 45 rods long, and the two adjacent angles, respectively, 70° and $69^\circ 40'$.

23. How far off may a hill 500 feet high be seen, if the radius of the earth be 3962 miles?

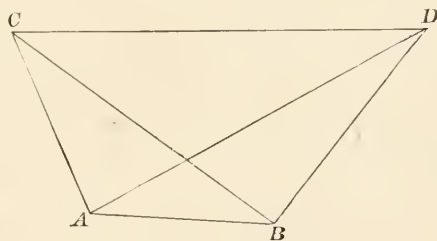
24. Two fixed objects, A and B , and a ship, were all observed to be in a line bearing N. $33^\circ 15'$ E. The ship then sailed northwest 10 miles, when the bearing of A was found to be east, and that of B northeast. Find the distance from A to B .

25. The perimeter of a triangle is 400 feet, and the angles are $65^\circ 15'$, $75^\circ 30'$, and $39^\circ 15'$, respectively. Find the sides.

26. Express the area of a triangle, in terms of the base b and the two adjacent angles, θ and θ' .

27. Two sides of a parallelogram are 90 feet and 110 feet, and one of the diagonals 120 feet. Find the other diagonal, and the angles of the parallelogram.

28. Given $AB = 100$ rods,
 angle $BAD = 32^\circ$,
 $BAC = 98^\circ$,
 $ABC = 37^\circ$,
 $ABD = 118^\circ$;



to find the distance between C and D .

29. Find the perpendiculars let fall from the vertices of a triangle upon the opposite sides, when $a = 25$, $b = 30$, $c = 35$.

30. What is the angle of depression from the top of a mountain 3 miles high, the earth's radius being 3962 miles?

31. A point of land was observed by a ship at sea to bear $11^\circ 15'$ S. of E.; and after sailing northeast 12 miles, it was found to bear $33^\circ 45'$ S. of E. How far was the point from the ship at the last observation?

32. A side of the base of a square pyramid is 200 feet, and each edge is 150 feet. Find the slope of each face.

33. From the top of a mountain, 3 miles high, the angle of depression of the remotest visible point of the earth's surface is

$2^{\circ} 13' 27''$. Find the radius of the earth and the utmost distance from which the mountain is visible.

34. Two sides of a triangle are 30.8 and 54.12, and the angle opposite the latter is $36^{\circ} 42' 11''$. How many triangles? Solve.

35. Two sides of a triangle are 600 and 250, and the angle opposite the latter is $42^{\circ} 12'$. Solve the triangle.

36. If $\cos \theta = \frac{\cos \theta' - \epsilon}{1 - \epsilon \cos \theta'}$, show that $\tan \frac{1}{2} \theta = \sqrt{\frac{1 + \epsilon}{1 - \epsilon}} \tan \frac{1}{2} \theta'$.

37. The angles of a triangle are as 3, 4, and 5, and the least side is 10. Find the other sides.

38. The radius of the earth being 3962 miles, what is the length of 1° of the meridian?

39. At three points in the same horizontal straight line the angles of elevation of an object were found to be $36^{\circ} 50'$, $21^{\circ} 24'$, and 14° , the middle station being 84 feet from each of the others. Required the height of the object. The three points are not in line with the foot of the object.

40. If r, r', r'', r''' , denote the radii of the inscribed and escribed circles of a triangle, show that

$$\tan^2 \frac{A}{2} = \frac{r r'}{r'' r'''}$$

41. Three circles, whose radii are r, r', r'' , touch one another; show that the radius of the circle passing through the three points of contact is

$$\sqrt{\frac{r r' r''}{r + r' + r''}}$$

42. The sides of a triangle are in arithmetical progression, and their common difference is 2 inches. If the area is $3\sqrt{15}$ square inches, find the sides.

43. The area of a triangle is 84 square inches, and two of its sides are 15 and 13 inches. Find the third side.

44. Given the vertical angle, the base, and the difference between the two sides of the triangle. Find the other angles.

CHAPTER VII.

SPHERICAL TRIANGLES.

75. The object of Spherical Trigonometry is the solution of spherical triangles.

The sides as well as the angles of a spherical triangle are expressed in degrees, minutes, and seconds.

Only those spherical triangles whose sides are, each, less than 180° will here be considered.

76. Let ABC (Fig. 23) be a spherical triangle traced upon the surface of a sphere, whose centre is O , and radii be drawn from O to the three vertices. A tri-edral angle will be formed whose plane angles AOB , AOC , and BOC , are respectively equal to the sides c , b , and a , since the latter are the arcs that measure those angles.

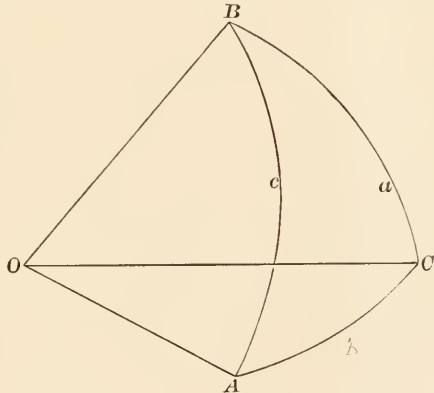


FIG. 23.

The di-edral angles AOB - AOC , AOB - BOC , and AOC - BOC are equal to the angles A , B , and C , respectively. The planes which form the tri-edral angle AOB - AOC - BOC always cut the surface of the sphere in arcs of great circles, thus tracing upon the surface of the sphere a spherical triangle, whose sides are arcs of great circles.

77. *Definitions.*

A spherical right triangle has one, two, or three, right angles.

When it has two right angles, the triangle is called *bi-rectangular*.

When it has three right angles, the triangle is *tri-rectangular*.

A spherical triangle having one side = 90° is called *quadrantal*. When it has two sides, each = 90° , it is *bi-quadrantal*; and when three sides, each = 90° , it is *tri-quadrantal* or *tri-rectangular*.

78. *Relations between the angles and the sides of a spherical triangle.*

Let ABC (Fig. 24) be a spherical triangle traced on the surface of a sphere whose centre is O , and with a radius taken equal to unity. Let the sides b and c , each, be less than 90° .

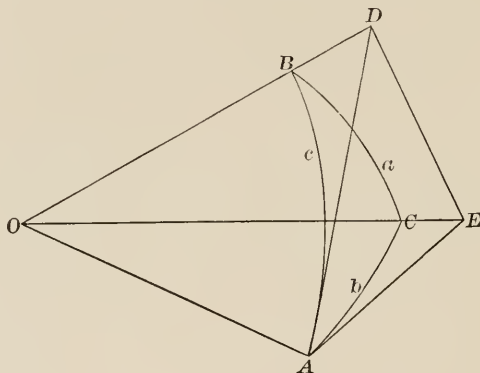


FIG. 24.

Draw the tangents AD and AE , meeting the radii OB and OC prolonged, in the points D and E , respectively.

We have $AD = \tan c$, $OD = \sec c$, $AE = \tan b$, $OE = \sec b$.

Also, the angle $DAE = A$, and the angle $DOE = a$.

The plane triangles DAE and DOE give

$$(1) \overline{DE}^2 = \overline{AD}^2 + \overline{AE}^2 - 2\overline{AD} \cdot \overline{AE} \cos DAE,$$

$$(2) \overline{DE}^2 = \overline{OD}^2 + \overline{OE}^2 - 2\overline{OD} \cdot \overline{OE} \cos DOE;$$

from which we obtain

$$(3)$$

$$2\overline{OD} \cdot \overline{OE} \cos DOE = (\overline{OD}^2 - \overline{AD}^2) + (\overline{OE}^2 - \overline{AE}^2) + 2\overline{AD} \cdot \overline{AE} \cos DAE.$$

Since AD and AE are tangents at the point A , the extremity of the radius OA , the angles DAO and EAO are right angles, and (3) becomes

$$(4) 2\overline{OD} \cdot \overline{OE} \cos DOE = 2\overline{OA}^2 + 2\overline{AD} \cdot \overline{AE} \cos DAE.$$

Replacing the various quantities in (4) by their values, we have

$$(5) \sec b \sec c \cos a = 1 + \tan b \tan c \cos A,$$

whence multiplying (5) by $\cos b \cos c$, we obtain

$$(6) \cos a = \cos b \cos c + \sin b \sin c \cos A.$$

79. We have supposed the sides b and c , each, less than 90° , but we shall now show that whatever values b and c may have between 0 and 180° , (6) holds good.

Suppose $c > 90^\circ$, and $b < 90^\circ$, and prolong the arcs BA and BC (Fig. 25) until they meet at B' . Let $AB' = c'$, and $CB' = a'$; then the triangle $AB'C$ will give

$$\begin{aligned} \cos a' &= \cos b \cos c' \\ &+ \sin b \sin c' \cos B'AC, \end{aligned}$$

for the sides c' and b are each less than 90° .

Replacing a' , c' , and $B'AC$ by their values $180^\circ - a$, $180^\circ - c$, and $180^\circ - A$, we obtain as before

$$\cos a = \cos b \cos c + \sin b \sin c \cos A.$$

Again, suppose $b > 90^\circ$ and $c > 90^\circ$.

Prolong the sides AB and AC (Fig. 26) until they meet at A' . Let $A'C = b'$, and $A'B = c'$; then the triangle $A'BC$ will give

$$\cos a = \cos b' \cos c' + \sin b' \sin c' \cos A'.$$

Replacing b' , c' , and A' by their values $180^\circ - b$, $180^\circ - c$, and A , we obtain as before

$$\cos a = \cos b \cos c + \sin b \sin c \cos A.$$

We conclude, therefore, that whatever values the sides may have between the limits of 0 and 180° , the formula holds.

Thus by a change of letters we have three equations,

$$\left. \begin{aligned} \cos a &= \cos b \cos c + \sin b \sin c \cos A, \\ \cos b &= \cos a \cos c + \sin a \sin c \cos B, \\ \cos c &= \cos a \cos b + \sin a \sin b \cos C, \end{aligned} \right\} [47]$$

which may be regarded as the fundamental formulæ of Spherical Trigonometry.

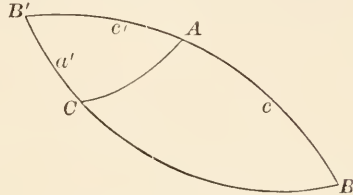


FIG. 25.

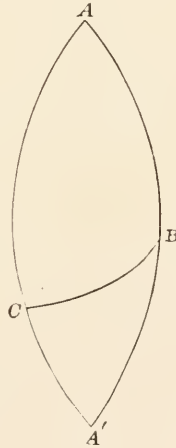


FIG. 26.

80. *Relations existing between a side and the three angles of a spherical triangle.*

Let ABC be a spherical triangle whose polar is the triangle $A'B'C'$ (Fig. 27).

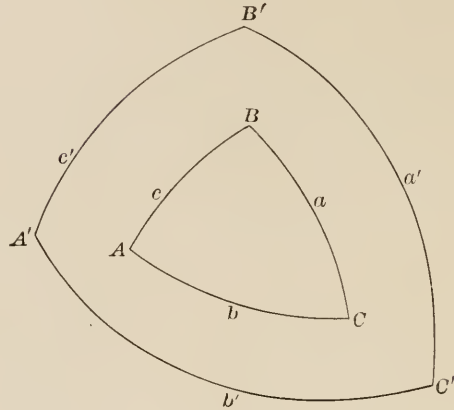


FIG. 27.

From the geometric principles of polar triangles, we have

$$\begin{aligned} A' &= 180^\circ - a, & a' &= 180^\circ - A, \\ B' &= 180^\circ - b, & b' &= 180^\circ - B, \\ C' &= 180^\circ - c, & c' &= 180^\circ - C. \end{aligned}$$

By [47],

$$\cos a' = \cos b' \cos c' + \sin b' \sin c' \cos A'.$$

Replacing the values of A' , B' , C' , a' , b' , and c' , we have

$$\begin{aligned} \cos(180^\circ - A) &= \cos(180^\circ - B) \cos(180^\circ - C) \\ &\quad + \sin(180^\circ - B) \sin(180^\circ - C) \cos(180^\circ - a), \end{aligned}$$

or
$$-\cos A = (-\cos B)(-\cos C) + \sin B \sin C(-\cos a).$$

This equation, after changing the signs, and two others similar to it, constitute the following group,

$$\left. \begin{aligned} \cos A &= -\cos B \cos C + \sin B \sin C \cos a. \\ \cos B &= -\cos A \cos C + \sin A \sin C \cos b. \\ \cos C &= -\cos A \cos B + \sin A \sin B \cos c. \end{aligned} \right\} \quad [48]$$

81. *Relations existing between two sides and the angles opposite.*

To obtain one relation between the sides a and b , and the angles A and B , is accomplished in a very simple manner by introducing into formulæ [47] the sines of the angles A , B , and C , in place of the cosines.

The first of [47] gives

$$\cos A = \frac{\cos a - \cos b \cos c}{\sin b \sin c},$$

from which

$$\begin{aligned} \sin^2 A &= 1 - \cos^2 A = \frac{\sin^2 b \sin^2 c - (\cos a - \cos b \cos c)^2}{\sin^2 b \sin^2 c} \\ &= \frac{(1 - \cos^2 b)(1 - \cos^2 c) - (\cos a - \cos b \cos c)^2}{\sin^2 b \sin^2 c} \\ &= \frac{1 - \cos^2 a - \cos^2 b - \cos^2 c + 2 \cos a \cos b \cos c}{\sin^2 b \sin^2 c}; \end{aligned}$$

and, dividing both members by $\sin^2 a$, we have

$$\frac{\sin^2 A}{\sin^2 a} = \frac{1 - \cos^2 a - \cos^2 b - \cos^2 c + 2 \cos a \cos b \cos c}{\sin^2 a \sin^2 b \sin^2 c}.$$

This value of $\frac{\sin^2 A}{\sin^2 a}$ does not change when we permute the letters a , b , and c . It follows, then, that the other two formulæ of [47] will give the same value for $\frac{\sin^2 B}{\sin^2 b}$ and $\frac{\sin^2 C}{\sin^2 c}$, precisely as for $\frac{\sin^2 A}{\sin^2 a}$. Therefore, since the angles and the sides of a triangle are, each, less than 180° , their sines are positive, and we have

$$\frac{\sin A}{\sin a} = \frac{\sin B}{\sin b} = \frac{\sin C}{\sin c}. \quad [49]$$

Therefore, *in a spherical triangle the sines of the angles are proportional to the sines of the opposite sides.*

82. *Relations existing between the three sides and two of the angles of a spherical triangle.*

If the value of the $\cos c$ given in the third equation of [47] be substituted in the first of those equations, we shall have

$$\cos a = \cos a \cos^2 b + \sin a \sin b \cos b \cos C + \sin b \sin c \cos A,$$

which by transposition, putting for $\cos^2 b$ its value $1 - \sin^2 b$, and dividing by $\sin b$, becomes

$$\cos a \sin b - \sin a \cos b \cos C = \sin c \cos A.$$

By permutation of the letters, five other similar formulæ may be obtained, so that we have

$$\left. \begin{aligned} \cos a \sin b - \sin a \cos b \cos C &= \sin c \cos A, \\ \cos b \sin a - \sin b \cos a \cos C &= \sin c \cos B, \\ \cos b \sin c - \sin b \cos c \cos A &= \sin a \cos B, \\ \cos c \sin b - \sin c \cos b \cos A &= \sin a \cos C, \\ \cos c \sin a - \sin c \cos a \cos B &= \sin b \cos C, \\ \cos a \sin c - \sin a \cos c \cos B &= \sin b \cos A. \end{aligned} \right\} \quad [50]$$

$\sin a$, $\sin b$, and $\sin c$, by [49], may be replaced by $\sin A$, $\sin B$, and $\sin C$, and thus we shall obtain

$$\left. \begin{aligned} \cos a \sin B - \cos b \cos C \sin A &= \cos A \sin C, \\ \cos b \sin A - \cos a \cos C \sin B &= \cos B \sin C, \\ \cos b \sin C - \cos c \cos A \sin B &= \cos B \sin A, \\ \cos c \sin B - \cos b \cos A \sin C &= \cos C \sin A, \\ \cos c \sin A - \cos a \cos B \sin C &= \cos C \sin B, \\ \cos a \sin C - \cos c \cos B \sin A &= \cos A \sin B. \end{aligned} \right\} \quad [51]$$

83. *Relations existing between two sides, the angle included between those two sides, and the angle opposite one of them.*

If we divide the first equation of [50] by

$$\sin a = \frac{\sin c \sin A}{\sin C}, \quad [49],$$

member by member, the first of the relations sought will be found. We may obtain the others by permutation of the letters.

$$\left. \begin{aligned} \cot a \sin b - \cot A \sin C &= \cos b \cos C, \\ \cot b \sin a - \cot B \sin C &= \cos a \cos C, \\ \cot b \sin c - \cot B \sin A &= \cos c \cos A, \\ \cot c \sin b - \cot C \sin A &= \cos b \cos A, \\ \cot c \sin a - \cot C \sin B &= \cos a \cos B, \\ \cot a \sin c - \cot A \sin B &= \cos c \cos B. \end{aligned} \right\} \quad [52]$$

84. *Formule relating to spherical right triangles, when there is but one right angle.*

If, in the third equation of [47], in two of the equations of [49], in the fourth, second, fifth, and first of [52], and in all of [48], each of which contains the angle C , we suppose the angle C equal to 90° , then the following formulæ, peculiar to spherical right triangles, will result.

$$\left. \begin{array}{l} \text{From [47], (1) } \cos c = \cos b \cos a, \\ \text{[49], (2) } \sin b = \sin c \sin B, \\ \text{(3) } \sin a = \sin c \sin A, \\ \text{[52], (4) } \tan b = \tan c \cos A, \\ \text{(5) } \tan b = \sin a \tan B, \\ \text{(6) } \tan a = \tan c \cos B, \\ \text{(7) } \tan a = \sin b \tan A, \\ \text{[48], (8) } \cos c = \cot B \cot A, \\ \text{(9) } \cos B = \cos b \sin A, \\ \text{(10) } \cos A = \cos a \sin B, \end{array} \right\} \quad [53]$$

85. *General formulæ adapted to logarithmic computation.*

In order to render [47] and [48] suitable for logarithmic computation, let us resume the fundamental formulæ [47],

$$\begin{aligned} \cos a &= \cos b \cos c + \sin b \sin c \cos A. \\ (1) \quad \cos A &= \frac{\cos a - \cos b \cos c}{\sin b \sin c}. \\ (2) \quad 1 - \cos A &= 1 - \frac{\cos a - \cos b \cos c}{\sin b \sin c}. \\ (3) \quad 1 + \cos A &= 1 + \frac{\cos a - \cos b \cos c}{\sin b \sin c}. \end{aligned}$$

But by substituting the values of $1 - \cos A$, and $1 + \cos A$, as found by [26] and [27], (Pl. Tr.), we shall find that (2) becomes

$$\begin{aligned} (4) \quad \sin \frac{1}{2} A &= \sqrt{\frac{\sin b \sin c + \cos b \cos c - \cos a}{2 \sin b \sin c}} \\ &= \sqrt{\frac{\cos(b-c) - \cos a}{2 \sin b \sin c}} \quad (\text{Art. 52.}) \\ &= \sqrt{\frac{\sin \frac{1}{2}(a-b+c) \sin \frac{1}{2}(a+b-c)}{\sin b \sin c}} \quad (\text{Art. 65, Pl. Tr.}) \\ &= \sqrt{\frac{\sin(s-b) \sin(s-c)}{\sin b \sin c}}. \end{aligned}$$

Operating upon (3) in a similar manner, we find

$$\begin{aligned}
 (5) \quad \cos \frac{1}{2} A &= \sqrt{\frac{\cos a - \cos b \cos c + \sin b \sin c}{2 \sin b \sin c}} = \sqrt{\frac{\cos a - \cos(b+c)}{2 \sin b \sin c}} \\
 &= \sqrt{\frac{\sin \frac{1}{2}(a+b+c) \sin \frac{1}{2}(b+c-a)}{\sin b \sin c}} \\
 &= \sqrt{\frac{\sin s \sin(s-a)}{\sin b \sin c}}.
 \end{aligned}$$

Now, if (4) be divided by (5), the result will be

$$(6) \quad \tan \frac{1}{2} A = \sqrt{\frac{\sin(s-b) \sin(s-c)}{\sin s \sin(s-a)}}.$$

By a simple change of letters, analogous expressions for the sine, cosine, and tangent, of the angles $\frac{1}{2} B$ and $\frac{1}{2} C$, may be found.

The three systems are as follows:

$$\left. \begin{aligned}
 \sin \frac{1}{2} A &= \sqrt{\frac{\sin(s-b) \sin(s-c)}{\sin b \sin c}}, \\
 \sin \frac{1}{2} B &= \sqrt{\frac{\sin(s-a) \sin(s-c)}{\sin a \sin c}}, \\
 \sin \frac{1}{2} C &= \sqrt{\frac{\sin(s-a) \sin(s-b)}{\sin a \sin b}}.
 \end{aligned} \right\} [54]$$

$$\left. \begin{aligned}
 \cos \frac{1}{2} A &= \sqrt{\frac{\sin s \sin(s-a)}{\sin b \sin c}}, \\
 \cos \frac{1}{2} B &= \sqrt{\frac{\sin s \sin(s-b)}{\sin a \sin c}}, \\
 \cos \frac{1}{2} C &= \sqrt{\frac{\sin s \sin(s-c)}{\sin a \sin b}}.
 \end{aligned} \right\} [55]$$

$$\left. \begin{aligned}
 \tan \frac{1}{2} A &= \sqrt{\frac{\sin(s-b) \sin(s-c)}{\sin s \sin(s-a)}}, \\
 \tan \frac{1}{2} B &= \sqrt{\frac{\sin(s-a) \sin(s-c)}{\sin s \sin(s-b)}}, \\
 \tan \frac{1}{2} C &= \sqrt{\frac{\sin(s-a) \sin(s-b)}{\sin s \sin(s-c)}}.
 \end{aligned} \right\} [56]$$

The foregoing formulæ express the sine, cosine, and tangent of one half an angle of a spherical triangle in terms of sides.

The radical quantities in each one of the formulæ must be taken positively, because $\frac{1}{2}A$, $\frac{1}{2}B$, and $\frac{1}{2}C$ are each less than 90° , and therefore their trigonometrical functions are positive.

36. *The sine, cosine, and tangent of a half side in terms of the angles of a spherical triangle.*

From the first of [48] we have

$$\cos a = \frac{\cos A + \cos B \cos C}{\sin B \sin C},$$

$$\therefore (1) \quad 1 - \cos a = 1 - \frac{\cos A + \cos B \cos C}{\sin B \sin C} = -\frac{\cos A + \cos(B + C)}{\sin B \sin C};$$

$$(2) \quad 1 + \cos a = 1 + \frac{\cos A + \cos B \cos C}{\sin B \sin C} = \frac{\cos A + \cos(B - C)}{\sin B \sin C};$$

$$\therefore (3) \quad \sin \frac{1}{2}a = \sqrt{-\frac{\cos \frac{1}{2}(A + B + C) \cos \frac{1}{2}(B + C - A)}{\sin B \sin C}};$$

$$(4) \quad \cos \frac{1}{2}a = \sqrt{\frac{\cos \frac{1}{2}(A - B + C) \cos \frac{1}{2}(A + B - C)}{\sin B \sin C}}.$$

Now, let $A + B + C = 2S$; then $B + C - A = 2(S - A)$;

$A - B + C = 2(S - B)$; and $A + B - C = 2(S - C)$;

and substituting in (3) and (4), they become

$$(5) \quad \sin \frac{1}{2}a = \sqrt{-\frac{\cos S \cos(S - A)}{\sin B \sin C}},$$

$$(6) \quad \cos \frac{1}{2}a = \sqrt{\frac{\cos(S - B) \cos(S - C)}{\sin B \sin C}}.$$

Divide (5) by (6) and obtain

$$(7) \quad \tan \frac{1}{2}a = \sqrt{-\frac{\cos S \cos(S - A)}{\cos(S - B) \cos(S - C)}}.$$

The functions of $\frac{1}{2}b$ and of $\frac{1}{2}c$ may be obtained from (5), (6), and (7), by a simple change of letters.

The three systems are as follows :

$$\left. \begin{aligned} \sin \frac{1}{2} a &= \sqrt{-\frac{\cos S \cos (S-A)}{\sin B \sin C}}, \\ \sin \frac{1}{2} b &= \sqrt{-\frac{\cos S \cos (S-B)}{\sin A \sin C}}, \\ \sin \frac{1}{2} c &= \sqrt{-\frac{\cos S \cos (S-C)}{\sin A \sin B}}. \end{aligned} \right\} \quad [57]$$

$$\left. \begin{aligned} \cos \frac{1}{2} a &= \sqrt{\frac{\cos (S-B) \cos (S-C)}{\sin B \sin C}}, \\ \cos \frac{1}{2} b &= \sqrt{\frac{\cos (S-A) \cos (S-C)}{\sin A \sin C}}, \\ \cos \frac{1}{2} c &= \sqrt{\frac{\cos (S-A) \cos (S-B)}{\sin A \sin B}}. \end{aligned} \right\} \quad [58]$$

$$\left. \begin{aligned} \tan \frac{1}{2} a &= \sqrt{-\frac{\cos S \cos (S-A)}{\cos (S-B) \cos (S-C)}}, \\ \tan \frac{1}{2} b &= \sqrt{-\frac{\cos S \cos (S-B)}{\cos (S-A) \cos (S-C)}}, \\ \tan \frac{1}{2} c &= \sqrt{-\frac{\cos S \cos (S-C)}{\cos (S-A) \cos (S-B)}}. \end{aligned} \right\} \quad [59]$$

REMARK I. The positive sign must be given to the radicals of [57], [58], and [59], because $\frac{1}{2}a$, $\frac{1}{2}b$, and $\frac{1}{2}c$ are, each, less than 90° .

REMARK II. The functions of $\frac{1}{2}a$, $\frac{1}{2}b$, and $\frac{1}{2}c$, in [57] and [59], are *real* quantities. For since the sum of the angles of a spherical triangle is greater than 180° , and less than six right angles, then S , or $\frac{1}{2}(A+B+C)$, in [57] and [59], is greater than 90° , and less than three right angles. Therefore the $\cos S$ is either in the second or third quadrant, and is negative. The quantities under the radical sign are, therefore, positive.

It is easily shown that $\cos(S-A)$, $\cos(S-B)$, and $\cos(S-C)$ are all positive and do not change the result.

37. *Formule of Delambre.*

From formulæ [54] and [55], we obtain

(1)

$$\sin \frac{1}{2} A \cos \frac{1}{2} B = \frac{\sin(s-b)}{\sin c} \sqrt{\frac{\sin s \sin(s-c)}{\sin a \sin b}} = \frac{\sin(s-b)}{\sin c} \cos \frac{1}{2} C.$$

(2)

$$\cos \frac{1}{2} A \sin \frac{1}{2} B = \frac{\sin(s-a)}{\sin c} \sqrt{\frac{\sin s \sin(s-c)}{\sin a \sin b}} = \frac{\sin(s-a)}{\sin c} \cos \frac{1}{2} C.$$

(3)

$$\cos \frac{1}{2} A \cos \frac{1}{2} B = \frac{\sin s}{\sin c} \sqrt{\frac{\sin(s-a) \sin(s-b)}{\sin a \sin b}} = \frac{\sin s}{\sin c} \sin \frac{1}{2} C,$$

(4)

$$\sin \frac{1}{2} A \sin \frac{1}{2} B = \frac{\sin(s-c)}{\sin c} \sqrt{\frac{\sin(s-a) \sin(s-b)}{\sin a \sin b}} = \frac{\sin(s-c)}{\sin c} \sin \frac{1}{2} C.$$

From (1) and (2) by addition and subtraction, we obtain

$$(5) \frac{\sin \frac{1}{2} A \cos \frac{1}{2} B \pm \cos \frac{1}{2} A \sin \frac{1}{2} B}{\cos \frac{1}{2} C} = \frac{\sin(s-b) \pm \sin(s-a)}{\sin c},$$

and from (3) and (4), we obtain

$$(6) \frac{\cos \frac{1}{2} A \cos \frac{1}{2} B \mp \sin \frac{1}{2} A \sin \frac{1}{2} B}{\sin \frac{1}{2} C} = \frac{\sin s \mp \sin(s-c)}{\sin c}.$$

By Art. 52,

$$(7) \sin(s-b) + \sin(s-a) = 2 \sin \frac{1}{2} c \cos \frac{1}{2} (a-b),$$

$$(8) \sin(s-b) - \sin(s-a) = 2 \cos \frac{1}{2} c \sin \frac{1}{2} (a-b),$$

$$(9) \sin s + \sin(s-c) = 2 \cos \frac{1}{2} c \sin \frac{1}{2} (a+b),$$

$$(10) \sin s - \sin(s-c) = 2 \sin \frac{1}{2} c \cos \frac{1}{2} (a+b),$$

also $\sin c = 2 \sin \frac{1}{2} c \cos \frac{1}{2} c.$

∴ substituting in (5) and (6) the values found in (7), (8), (9), (10), and that of $\sin c$, we have

$$\left. \begin{aligned}
 (1) \quad \frac{\sin \frac{1}{2}(A+B)}{\cos \frac{1}{2}C} &= \frac{\cos \frac{1}{2}(a-b)}{\cos \frac{1}{2}c}, \\
 (2) \quad \frac{\sin \frac{1}{2}(A-B)}{\cos \frac{1}{2}C} &= \frac{\sin \frac{1}{2}(a-b)}{\sin \frac{1}{2}c}, \\
 (3) \quad \frac{\cos \frac{1}{2}(A+B)}{\sin \frac{1}{2}C} &= \frac{\cos \frac{1}{2}(a+b)}{\cos \frac{1}{2}c}, \\
 (4) \quad \frac{\cos \frac{1}{2}(A-B)}{\sin \frac{1}{2}C} &= \frac{\sin \frac{1}{2}(a+b)}{\sin \frac{1}{2}c}.
 \end{aligned} \right\} [60]$$

REMARK. These formulæ were discovered by Delambre, in 1807, and published in *Connaissance des Temps* for 1809 (p. 443). Gauss, to whom they are sometimes attributed, did not publish them until two years later, in his work, *Theoria motus corporum caelestium*.

88. Napier's Analogies.

If (1) of [60] be divided by (3); (2) by (4); (4) by (3); and (2) by (1), we shall obtain the formulæ that are known as *Napier's Analogies*.

They are as follows :

$$\left. \begin{aligned}
 (1) \quad \tan \frac{1}{2}(A+B) &= \cot \frac{1}{2}C \frac{\cos \frac{1}{2}(a-b)}{\cos \frac{1}{2}(a+b)}, \\
 (2) \quad \tan \frac{1}{2}(A-B) &= \cot \frac{1}{2}C \frac{\sin \frac{1}{2}(a-b)}{\sin \frac{1}{2}(a+b)}, \\
 (3) \quad \tan \frac{1}{2}(a+b) &= \tan \frac{1}{2}c \frac{\cos \frac{1}{2}(A-B)}{\cos \frac{1}{2}(A+B)}, \\
 (4) \quad \tan \frac{1}{2}(a-b) &= \tan \frac{1}{2}c \frac{\sin \frac{1}{2}(A-B)}{\sin \frac{1}{2}(A+B)}.
 \end{aligned} \right\} [61]$$

CHAPTER VIII.

SOLUTION OF SPHERICAL RIGHT TRIANGLES.

89. The formulæ for the solution of spherical right triangles are those of [53], Art. 84.

From formula (1), $\cos c = \cos b \cos a$; it follows that either all the cosines are positive, or but one is positive.

Therefore, *in a right triangle, either all the sides are less than quadrants, or one side is less than a quadrant, and the other two sides are greater than quadrants.*

From (5) and (7) of [53], it follows that $\tan b$ and $\tan B$ have the same sign, and are, therefore, either both greater than 90° , or both less than 90° . When such is the case, b and B are of the *same species*. The same is true of a and A . When one is greater than 90° , and the other less than 90° , they are then of *different species*.

90. The ten equations of [53] constitute but six cases :

1. Given the two sides ; to find the other parts.
2. Given a side and its opposite angle ; to find the other parts.
3. Given the two angles ; to find the other parts.
4. Given the hypotenuse and one side ; to find the other parts.
5. Given the hypotenuse and an angle ; to find the other parts.
6. Given a side and an adjacent angle ; to find the other parts.

91. *Napier's Circular Parts.* Two rules, called *Napier's Rules of Circular Parts* of a spherical triangle, include all the possible cases.

The *circular parts* of a spherical triangle are five : the two sides b and a , the *complements* of the angles B and A , and the *complement* of the hypotenuse c . The complements of B , A , and c are generally written $\text{co. } B$, $\text{co. } A$, and $\text{co. } c$. The right angle is always excluded.

An examination of Fig. 28 shows that if any three parts be taken, as b , a , and $\text{co. } B$, all are adjacent ; but if b , a , and $\text{co. } c$ be taken, then one is separated from the other two by the remaining

parts *co. B* and *co. A*. No other arrangements of the five parts, when taken by threes, can be made. The three are either adjacent, or one is separated from the other two by intervening parts.

When the parts are adjacent, as *co. A*, *co. c*, and *co. B*, then one is called the *middle part*, and the other two the *adjacent parts*.

When the parts are separated, as *co. c*, *co. B*, and *b*, one, *b*, is the *middle part*, and the other two, *co. c* and *co. B*, are called the *opposite parts*.

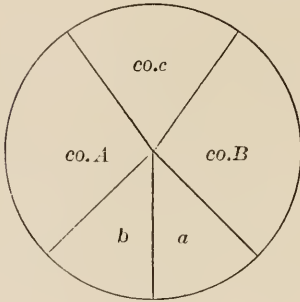


FIG. 28.

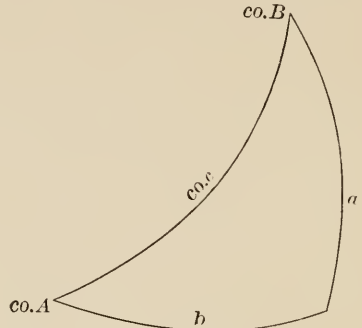


FIG. 29.

Let Fig. 29 be a spherical right triangle, in which *b* and *a* are taken as before; but the angle *B* is represented by *co. B*, or $90^\circ - B$, the angle *A* by *co. A*, or $90^\circ - A$, and the hypotenuse *c* by *co. c*, or $90^\circ - c$.

A comparison of Figs. 28 and 29 will show that *Napier's Rules* apply in either case.

92. *Napier's Rules.*

1. *The sine of the middle part equals the product of the tangents of the adjacent parts.*

2. *The sine of the middle part equals the product of the cosines of the opposite parts.*

93. That *Napier's Rules*, the *formulae* of [53], Art. 84, and the *six cases* of Art. 90, all agree, we shall now show.

Formula (8) of [53] is

$$\cos c = \cot B \cot A.$$

By Napier's first rule,

$$\sin(\text{co. } c) = \tan(\text{co. } B) \tan(\text{co. } A).$$

Replacing $\text{co. } c$, $\text{co. } B$, and $\text{co. } A$ by their values, the result becomes

$$\sin(90^\circ - c) = \tan(90^\circ - B) \tan(90^\circ - A),$$

or
$$\cos c = \cot B \cot A.$$

Again, formula (9) of [53] is

$$\cos B = \cos b \sin A.$$

By Napier's second rule,

$$\sin(\text{co. } B) = \cos b \cos(\text{co. } A),$$

or
$$\sin(90^\circ - B) = \cos b \cos(90^\circ - A),$$

or
$$\cos B = \cos b \sin A.$$

Six cases are to be considered.

94. Given b and a ; to find the other parts.

From (5), [53], $\tan b = \sin a \tan B$; $\therefore \tan B = \frac{\tan b}{\sin a}$

(7), $\tan a = \sin b \tan A$; $\therefore \tan A = \frac{\tan a}{\sin b}$

(1), $\cos c = \cos b \cos a.$

It is clear that no ambiguity exists in the solutions, since not one of the quantities required is to be found from its sine.

95. Given b and B ; to find the other parts.

From

(2), [53], $\sin b = \sin c \sin B$; $\therefore \sin c = \frac{\sin b}{\sin B}.$

(9), $\cos B = \cos b \sin A$; $\therefore \sin A = \frac{\cos B}{\cos b}.$

(5), $\tan b = \sin a \tan B$; $\therefore \sin a = \frac{\tan b}{\tan B}.$

In this case there is nothing to decide whether c , A , and a should be greater or less than 90° ; therefore the solution remains ambiguous, as the parts are determined from their sines. It is the only ambiguous case that occurs in spherical right triangles.

Let ABC (Fig. 30), right-angled at C , be a triangle

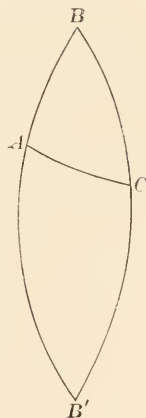


FIG. 30.

satisfying the given conditions. Prolong BA and BC until they meet at B' . Then the right triangle $AB'C$ also satisfies the given conditions; for it has the angle B' equal to B , the angle C a right angle, and the side AC the same as in ABC .

96. Given B and A ; to find the other parts.

From (8), [53], $\cos c = \cot B \cot A$.

$$(9), \quad \cos B = \cos b \sin A; \quad \therefore \cos b = \frac{\cos B}{\sin A}.$$

$$(10), \quad \cos A = \cos a \sin B; \quad \therefore \cos a = \frac{\cos A}{\sin B}.$$

There is no ambiguity in this case.

97. Given hypotenuse c and a side b ; to find the other parts.

From (1), [53], $\cos c = \cos b \cos a$; $\therefore \cos a = \frac{\cos c}{\cos b}$.

$$(2), \quad \sin b = \sin c \sin B; \quad \therefore \sin B = \frac{\sin b}{\sin c}.$$

$$(4), \quad \tan b = \tan c \cos A; \quad \therefore \cos A = \frac{\tan b}{\tan c}.$$

There can be no ambiguity in this case, except in the value of B , but this is removed by the consideration that B and b are always of the same species.

98. Given hypotenuse c and an angle A ; to find the other parts.

From (8), [53], $\cos c = \cot B \cot A$; $\therefore \cot B = \frac{\cos c}{\cot A}$.

$$(4), \quad \tan b = \tan c \cos A.$$

$$(3), \quad \sin a = \sin c \sin A.$$

There is no ambiguity in (3), when it is remembered that a and A are of the same species.

99. Given a side b and an adjacent angle A ; to find the other parts.

From (9), [53], $\cos B = \cos b \sin A$.

$$(7), \quad \tan a = \sin b \tan A.$$

$$(4), \quad \tan b = \tan c \cos A; \quad \therefore \tan c = \frac{\tan b}{\cos A}.$$

There is no ambiguity in this case.

100. *Isosceles and Quadrantal Triangles.*

An *isosceles triangle* is readily solved by dividing it into two right triangles by a perpendicular from the angle included by the equal sides, then applying formulæ [53].

A *quadrantal triangle* which is the polar triangle of a right triangle, has one of its sides equal to 90° . When such a triangle appears, it is easily solved by means of its polar triangle.

101. EXAMPLES.

SET VII.

Right Triangles.

1. In a spherical right triangle, $c = 145^\circ$, and $A = 23^\circ 28'$, C being the right angle. Find the other parts.
2. Given $c = 32^\circ 34'$, and $A = 44^\circ 44'$. Find B , a , and b .
3. Given $a = 141^\circ 11'$, and $c = 127^\circ 12'$. Find A , B , and b .
4. Given $a = 35^\circ 44'$, and $A = 37^\circ 28'$. Find B , b , and c .
This problem gives two triangles.
5. Given $a = 118^\circ 54'$, and $B = 12^\circ 19'$. Find A , b , and c .
6. Given $A = 91^\circ 11'$, and $B = 111^\circ 11'$. Find a , b , and c .
7. Given $a = 1^\circ$, and $b = 100^\circ$. Find A , B , and c .
8. Given $A = 23^\circ 28'$, and $b = 49^\circ 17'$. Find B , a , and c .
9. Given $a = 37^\circ 48'$, and $c = 66^\circ 32'$. Find A , B , and b .
10. Given $a = 59^\circ 38' 27''$, and $b = 48^\circ 24' 16''$.
Find A , B , and c .
11. Given $B = 111^\circ 14' 37''$, and $b = 121^\circ 26' 25''$.
Find A , a , and c .

Quadrantal Triangles.

12. Given $c = 90^\circ$, $A = 54^\circ 43'$, and $B = 42^\circ 12'$.
Find the other parts.
13. Given $c = 90^\circ$, $A = 112^\circ 2' 9''$, and $b = 67^\circ 3' 14''$.
Find the other parts.
14. Given $c = 90^\circ$, $a = 22^\circ 53' 30''$, and $b = 51^\circ 4' 35''$.
Find the other parts.
15. Given the quadrantal side AB , the angles A and B ; to find the other parts.

16. Prove $\sin^2 \frac{1}{2} c = \sin^2 \frac{1}{2} a \cos^2 \frac{1}{2} b + \cos^2 \frac{1}{2} a \sin^2 \frac{1}{2} b$. C being 90° .
 17. Prove $\tan^2 \frac{1}{2} b = \tan \frac{1}{2} (c + a) \tan \frac{1}{2} (c - a)$.
 18. Prove $\tan^2 \frac{1}{2} A = \sin (c - b) \operatorname{cosec} (c + b)$.
 19. Prove $\tan^2 \frac{1}{2} c = -\cos (A + B) \sec (A - B)$.
 20. Prove $\tan^2 (45^\circ - \frac{1}{2} b) = \sin (A - a) \operatorname{cosec} (A + a)$.
 21. In a right triangle show that

$$\sin (c - b) = 2 \sin^2 \frac{1}{2} A \cos b \sin c.$$

22. $C = 90^\circ$. Show that $\sin a \cos b = \tan \frac{1}{2} A \sin (b + c)$.
 23. The equal sides of an isosceles triangle are, each, 45° , and the angle included is 95° . Find the other parts.

24. In a right triangle, if θ be the length of the arc drawn from C , perpendicular to the hypotenuse c , show that

$$\cot \theta = \sqrt{\cot^2 a + \cot^2 b}.$$

25. a is one side of an equilateral triangle. Find the angle A .

26. Show that $\frac{\cos a}{\cos b} = \frac{\sin 2A}{\sin 2B}$.

27. Required the dihedral angles made by the faces of the regular polyhedrons.

28. Show that $\sin (c - a) = \sin b \cos a \tan \frac{1}{2} B$.

29. If $A = 36^\circ$, $B = 60^\circ$, and $C = 90^\circ$, show that

$$a + b + c = 90^\circ.$$

30. C being a right angle, show that

$$\sin A \sin 2b = \sin c \sin 2B.$$

CHAPTER IX.

SOLUTION OF SPHERICAL OBLIQUE TRIANGLES.

102. We shall consider only those triangles each of whose parts is less than 180° , keeping in mind always the following principles :

- (1) *The greater side is opposite the greater angle, and conversely,*
- (2) *Each side is less than the sum of the other two.*
- (3) *The sum $a + b + c$ is less than 360° .*
- (4) *The sum $A + B + C$ is greater than 180° .*
- (5) *If $A + B + C > 180^\circ$, then $A > 180^\circ - B - C$,*
 $B > 180^\circ - A - C$,
 $C > 180^\circ - A - B$.

(6) *A side differing more from 90° than another side is in the same quadrant as its opposite angle.*

(7) *An angle differing more from 90° than another angle is in the same quadrant as its opposite side.*

(8) *Two sides at least are in the same quadrants as their opposite angles respectively.*

(9) *The sum of two sides is $>$, $=$, or $< 180^\circ$, according as the sum of the two opposite angles is $>$, $=$, or $< 180^\circ$.*

103. CASE I. *Given the three sides; to find the angles.*

Formulae [54], [55], and [56], which express the sine, cosine, and tangent of one-half an angle in terms of the sides of a spherical triangle, may be used. The preference is to be given to [56].

EXAMPLE. Given the three sides,

$$a = 113^\circ 2' 56''.64,$$

$$b = 82^\circ 39' 28''.40,$$

$$c = 74^\circ 54' 31''.06;$$

to find the angles A , B , and C .

Solution :

| | |
|--|--------------------------------------|
| $s = \frac{1}{2}(a + b + c) = 135^\circ 18' 28''.05$ | $\log \sin s = \bar{1}.847139$ |
| $s - a = 22^\circ 15' 31''.41$ | $\log \sin(s - a) = \bar{1}.578398$ |
| $s - b = 52^\circ 38' 59''.65$ | $\log \sin(s - b) = \bar{1}.900336$ |
| $s - c = 60^\circ 23' 56''.99$ | $\log \sin(s - c) = \bar{1}.939264.$ |

$$(1) \tan \frac{1}{2} A = \sqrt{\frac{\sin(s - b) \sin(s - c)}{\sin s \sin(s - a)}}$$

$$(2) \tan \frac{1}{2} B = \sqrt{\frac{\sin(s - a) \sin(s - c)}{\sin s \sin(s - b)}}$$

| | |
|--|--|
| $\log \sin(s - b) = \bar{1}.900336$ | $\log \sin(s - a) = \bar{1}.578398$ |
| $\log \sin(s - c) = \bar{1}.939264$ | $\log \sin(s - c) = \bar{1}.939264$ |
| $\text{colog } \sin s = 0.152861$ | $\text{colog } \sin s = 0.152861$ |
| $\text{colog } \sin(s - a) = 0.421602$ | $\text{colog } \sin(s - b) = 0.099664$ |
| $2) \underline{0.414063}$ | $2) \underline{\bar{1}.770187}$ |

$$\log \tan \frac{1}{2} A = 0.207031$$

$$\log \tan \frac{1}{2} B = \bar{1}.885093$$

$$\frac{1}{2} A = 58^\circ 10' 1''.10.$$

$$\frac{1}{2} B = 37^\circ 30' 25''.8.$$

$$\therefore A = 116^\circ 20' 2''.20.$$

$$\therefore B = 75^\circ 0' 51''.6.$$

$$(3) \tan \frac{1}{2} C = \sqrt{\frac{\sin(s - a) \sin(s - b)}{\sin s \sin(s - c)}}$$

$$\log \sin(s - a) = \bar{1}.578398$$

$$\log \sin(s - b) = \bar{1}.900336$$

$$\text{colog } \sin s = 0.152861$$

$$\text{colog } \sin(s - c) = 0.060736$$

$$2) \underline{\bar{1}.692331}$$

$$\log \tan \frac{1}{2} C = \bar{1}.846166$$

$$\frac{1}{2} C = 35^\circ 3' 29''.58$$

$$\therefore C = 70^\circ 6' 59''.16.$$

104. CASE II. Given the three angles; to find the sides.

Formulae [57], [58], and [59] are applicable. But the three formulae of [59] are generally to be preferred.

105. CASE III. *Given two sides and the included angle; to find the other parts.*

We obtain the simplest solution of this problem by means of Napier's Analogies, formulæ [61], Art. 88.

If the given parts be a , b , and C , we compute at once A and B by (1) and (2) of [61]; then c by (3) or (4).

EXAMPLE. Given $a = 113^\circ 2' 56''.64$,
 $b = 82^\circ 39' 28''.40$,
 $C = 138^\circ 50' 13''.69$; to find A , B , and c .

Solution :

| | |
|---|---|
| $\frac{1}{2}(a - b) = 15^\circ 11' 44''.12$ | $\log \sin \frac{1}{2}(a - b) = \bar{1}.418492$ |
| $\frac{1}{2}(a + b) = 97^\circ 51' 12''.52$ | $\log \cos \frac{1}{2}(a - b) = \bar{1}.984544$ |
| $\frac{1}{2}C = 69^\circ 25' 6''.845$ | $\log \sin \frac{1}{2}(a + b) = \bar{1}.995907$ |
| | $\log \cos \frac{1}{2}(a + b) = \bar{1}.135578$ |
| | $\log \cot \frac{1}{2}C = \bar{1}.574616$ |

$$(1) \tan \frac{1}{2}(A + B) = \cot \frac{1}{2}C \frac{\cos \frac{1}{2}(a - b)}{\cos \frac{1}{2}(a + b)},$$

$$(2) \tan \frac{1}{2}(A - B) = \cot \frac{1}{2}C \frac{\sin \frac{1}{2}(a - b)}{\sin \frac{1}{2}(a + b)}$$

| | |
|---|---|
| $\log \cot \frac{1}{2}C = \bar{1}.574616$ | $\log \cot \frac{1}{2}C = \bar{1}.574616$ |
| $\log \cos \frac{1}{2}(a - b) = 1.984544$ | $\log \sin \frac{1}{2}(a - b) = 1.418492$ |
| $\text{colog} \cos \frac{1}{2}(a + b) = 0.864421$ | $\text{colog} \sin \frac{1}{2}(a + b) = 0.004093$ |
| $\log \tan \frac{1}{2}(A + B) = 0.423581$ | $\log \tan \frac{1}{2}(A - B) = \bar{2}.997201$ |

$$\therefore \frac{1}{2}(A + B) = 110^\circ 39' 35''.29. \quad \therefore \frac{1}{2}(A - B) = 5^\circ 40' 26''.91.$$

$$\frac{1}{2}(A + B) = 110^\circ 39' 35''.29,$$

$$\frac{1}{2}(A - B) = 5^\circ 40' 26''.91.$$

$$\therefore A = 116^\circ 20' 2''.20,$$

$$B = 104^\circ 59' 8''.38.$$

$$\log \cos \frac{1}{2}(A + B) = \bar{1}.547551. \quad \log \cos \frac{1}{2}(A - B) = \bar{1}.997867.$$

$$(3) \tan \frac{1}{2}c = \tan \frac{1}{2}(a+b) \frac{\cos \frac{1}{2}(A+B)}{\cos \frac{1}{2}(A-B)}.$$

$$\log \tan \frac{1}{2}(a+b) = \begin{cases} \log \sin \frac{1}{2}(a+b) = \bar{1}.995907 \\ \text{colog } \cos \frac{1}{2}(a+b) = 0.864421 \\ \log \cos \frac{1}{2}(A+B) = \bar{1}.547551 \\ \text{colog } \cos \frac{1}{2}(A-B) = 0.002133 \end{cases}$$

$$\log \tan \frac{1}{2}c = 0.410012$$

$$\frac{1}{2}c = 68^\circ 44' 32''.30.$$

$$\therefore c = 137^\circ 29' 4''.6.$$

106. CASE IV. *Two angles and the included side given; to find the other parts.*

If the given parts be A , B , and c , we compute a and b by formulæ (3) and (4), and C by (1) or (2), of Napier's Analogies.

107. CASE V. *Given two sides and an angle opposite one of them; to find the other parts.*

If the given parts be a , b , and A , we compute B at once by the formula $\frac{\sin B}{\sin b} = \frac{\sin A}{\sin a}$, and then obtain the corresponding value of C by (1) or (2) of Napier's Analogies, and the value of c by (3) or (4).

In order that the problem may be possible, it is necessary that the $\sin B$ or $\sin b$ be comprised between zero and 1. When this condition is satisfied, then B or b will have two values, supplementary to each other. But it is necessary that the corresponding values of $\tan \frac{1}{2}C$ and $\tan \frac{1}{2}c$ be positive, which requires that $A - B$ and $a - b$ have the same sign. If this condition be not satisfied for either of the two values of B or b , the problem admits of no solution. But, if it is satisfied, a solution will necessarily follow, $A - B$ and $a - b$ being of the same sign, C and c will be comprised between zero and 180° , by means of two formulæ of Napier. These values of C and c will be the same as those which the other two formulæ of Napier will give.

EXAMPLE. Given $a = 50^\circ 45' 20''$,

$b = 69^\circ 12' 40''$,

$A = 44^\circ 22' 10''$;

to find B , C , and c .

Solution :

$$(1) \sin B = \frac{\sin A \sin b}{\sin a}.$$

$$\log \sin 69^\circ 12' 40'' = \bar{1}.970763$$

$$\log \sin 44^\circ 22' 10'' = \bar{1}.844652$$

$$\text{colog} \sin 50^\circ 45' 20'' = 0.111004$$

$$\log \sin B = 1.926419$$

$$\therefore B = 57^\circ 34' 51''.4,$$

$$\text{or } 122^\circ 25' 8''.6.$$

There are then two solutions.

$$(2) \cot \frac{1}{2} C = \frac{\cos \frac{1}{2} (b + a)}{\cos \frac{1}{2} (b - a)} \tan \frac{1}{2} (A + B). \quad (1) \text{ of [61].}$$

$$\frac{1}{2} (B + A) = 50^\circ 58' 30''.7 \quad \log \cos 59^\circ 59' = \bar{1}.699189$$

$$\frac{1}{2} (B - A) = 6^\circ 36' 20''.7 \quad \log \tan 50^\circ 58' 30''.7 = 0.091246$$

$$\frac{1}{2} (b + a) = 59^\circ 59' \quad \text{colog} \cos 9^\circ 13' 40'' = 0.005657$$

$$\frac{1}{2} (b - a) = 9^\circ 13' 40'' \quad \log \cot \frac{1}{2} C = \bar{1}.796082$$

$$\frac{1}{2} C = 57^\circ 58' 55''.3.$$

When $B = 57^\circ 34' 51''.4,$ then $C = 115^\circ 57' 50''.6.$

But when $B = 122^\circ 25' 8''.6,$

then $\frac{1}{2} (B + A) = 83^\circ 23' 39''.3,$

$$\frac{1}{2} (B - A) = 39^\circ 1' 29''.3,$$

$$\frac{1}{2} (b + a) = 59^\circ 59',$$

$$\frac{1}{2} (b - a) = 9^\circ 13' 40''.$$

By (1) of [61],

$$\log \cos 59^\circ 59' = 1.699189$$

$$\log \tan 83^\circ 23' 39''.3 = 0.936270$$

$$\text{colog} \cos 9^\circ 13' 40'' = 0.005657$$

$$\log \cot \frac{1}{2} C = 0.641116$$

$$\therefore \frac{1}{2} C = 12^\circ 52' 15''.8.$$

For second value of $B,$ then $C = 25^\circ 44' 31''.6.$

(3) The values of c are found by (3) of [61].

$$\tan \frac{1}{2}c = \frac{\cos \frac{1}{2}(B+A)}{\cos \frac{1}{2}(B-A)} \tan \frac{1}{2}(b+a).$$

$$\log \cos 83^\circ 23' 39''.3 = \bar{1}.060837$$

$$\log \tan 59^\circ 59' = 0.238269$$

$$\text{colog } \cos 39^\circ 1' 29''.3 = 0.109650$$

$$\log \tan \frac{1}{2}c = \bar{1}.408756$$

$$\frac{1}{2}c = 14^\circ 22' 32''.6.$$

$$\therefore c = 28^\circ 45' 5''.2.$$

The other value of c is found by taking the other values of $\frac{1}{2}(B+A)$ and $\frac{1}{2}(B-A)$.

108. CASE VI. *Given two angles and the side opposite one of them; to find the other parts.*

This case gives rise to the same ambiguities that are found in Case V.

To solve the problem, the formulæ to be used are

$$(1) \sin b = \frac{\sin a \sin B}{\sin A};$$

$$(2) \text{Napier's Analogies. [61].}$$

109. *The two cases that admit of two solutions.*

Case V. and Case VI. are the only two cases of spherical triangles that admit of two solutions, and yet they do not *always* admit of such ambiguity. The formulæ which relate to these two cases make known the number of solutions, and determine without ambiguity the elements of each of them.

In order that the problem may be possible, it is necessary and sufficient that $\tan A$ and $\cos a$, $\cos A$ and $\tan a$, have the same sign: that is to say, that A and a be both less than 90° , or both greater than 90° . There is then but one solution.

Passing to the general case, it is necessary, in order that the problem be possible, that $\frac{\sin b \sin A}{\sin a}$ be less than 1; if this condition be satisfied, there are then two values of B that satisfy the equation $\sin B = \frac{\sin b \sin A}{\sin a}$, one of which is B and the other $180^\circ - B$.

Now, $A - B$ and $a - b$ must have the same sign, in order that B and $180^\circ - B$ may satisfy the problem.

In the cases in which two solutions are indicated, no solution is possible if $\sin a$ be less than $\sin b \sin A$.

If a lies between b and $180 - b$, there will be one solution.

If a does not lie between b and $180^\circ - b$, either there are two solutions or no solution. The cases in which $a = b$, or $a = 180^\circ - b$, are not included in the last supposition.

110. EXAMPLES.

SET VIII.

1. Given $a = 43^\circ 27' 36''$,
 $b = 82^\circ 58' 17''$,
 $A = 29^\circ 32' 29''$; to find B , C , and c .

In this problem, $A < 90^\circ$, and $b < 90^\circ$; therefore $a < b$ will give two solutions.

Take
$$\sin B = \frac{\sin b \sin A}{\sin a}$$

2. Given $a = 74^\circ 23'$,
 $b = 35^\circ 46' 14''$,
 $c = 100^\circ 39'$; to find A , B , and C .

- | | |
|---|---|
| 3. Given $A = 48^\circ 30'$, $B = 125^\circ 20'$, $C = 62^\circ 54'$; to find a , b , and c . | 4. Given $a = 70^\circ 14' 20''$, $b = 49^\circ 24' 10''$, $c = 38^\circ 46' 10''$; to find A , B , and C . |
|---|---|

- | | |
|--|---|
| 5. Given $A = 129^\circ 5' 28''$, $B = 142^\circ 12' 42''$, $C = 105^\circ 8' 10''$; to find a , b , and c . | 6. Given $a = 68^\circ 46' 2''$, $b = 37^\circ 10'$, $C = 39^\circ 23' 23''$; to find A , B , and c . |
|--|---|

- | | |
|--|---|
| 7. Given $A = 34^\circ 15' 3''$, $B = 42^\circ 15' 13''$, $c = 76^\circ 35' 36''$; to find a , b , and C . | 8. Given $a = 97^\circ 35'$, $b = 27^\circ 8' 22''$, $A = 40^\circ 51' 18''$; to find B , C , and c . |
|--|---|

9. Given $A = 50^\circ 12'$,
 $B = 58^\circ 8'$,
 $a = 62^\circ 42'$;
 to find b , c , and C .
10. Given $a = 150^\circ 17' 23''$,
 $b = 43^\circ 12'$,
 $c = 82^\circ 50' 12''$;
 to find A , B , and C .

How many solutions has (9)?

11. Given $A = 50^\circ$,
 $a = 40^\circ$,
 $b = 60^\circ$;
 to find B , C , and c .
12. Given $A = 135^\circ 5' 28''.8$,
 $C = 50^\circ 30' 8''.4$,
 $b = 69^\circ 34' 55''.9$;
 to find a , c , and B .
13. Given $A = 30^\circ 28' 11''$,
 $B = 130^\circ 3' 11''$,
 $c = 40^\circ$;
 to find a , b , and C .
14. Given $a = 68^\circ 46' 2''$,
 $b = 43^\circ 37' 38''$,
 $C = 37^\circ 10'$;
 to find A , B , and C .
15. Given $A = 31^\circ 34' 26''$,
 $B = 30^\circ 28' 12''$,
 $c = 70^\circ 2' 3''$;
 to find a , b , and C .
16. Given $a = 63^\circ 50'$,
 $b = 80^\circ 19'$,
 $A = 51^\circ 30'$;
 to find B , C , and c .
17. Given $A = 32^\circ 26' 6''.66$,
 $B = 130^\circ 5' 22''$,
 $a = 44^\circ 13' 42''$;
 to find b , c , and C .
18. Given $A = 120^\circ 43' 37''$,
 $B = 109^\circ 55' 42''$,
 $C = 116^\circ 38' 33''$;
 to find a , b , and c .

CHAPTER X.

AREA OF SPHERICAL TRIANGLES.

111. *Given the angles of a spherical triangle; to find its area.*

Let ABC (Fig. 31) be a spherical triangle traced upon the surface of a sphere, and CAE , CBE , AED , ABD , and ACD be semicircumferences. Then the triangle ABC will be a part of each of three lunes, $CAEB$, $CAB-BED$, and $ABDC$.

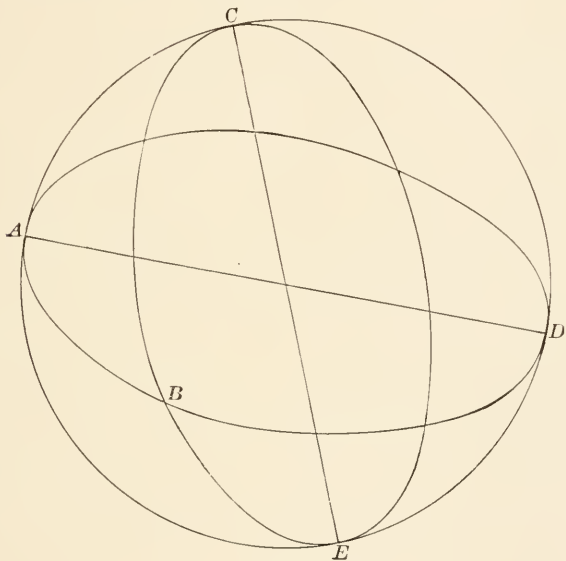


FIG. 31.

The surface of the hemisphere whose base is $ACDE$, is equal to the surface of the three lunes less twice the triangle ABC . Let r = the radius of the sphere.

- (1) The surface of the hemisphere = $2\pi r^2$,
- (2) The surface of the lune $CAEB$ = $2Cr^2$,
- (3) The surface of the lune $CAB-BED$ = $2Br^2$,
- (4) The surface of the lune $ABDC$ = $2Ar^2$.

$$\text{Therefore} \quad 2ABC = 2(A + B + C - \pi)r^2;$$

$$\text{or} \quad ABC = (A + B + C - \pi)r^2.$$

Denote $A + B + C - \pi$, which is called the spherical excess by E , the value of ABC then becomes $E r^2$.

$$\text{But} \quad E r^2 = \frac{E}{2\pi} \times 2\pi r^2,$$

$$\therefore ABC = \frac{E}{180^\circ} \times \pi r^2. \quad [62]$$

112. *Given the three sides of a spherical triangle; to find its area.*

An elegant formula due to Simon l'Huilier, of Geneva, furnishes a direct method for the solution of this problem.

$$\text{Since} \quad E = A + B + C - \pi,$$

$$\begin{aligned} \text{then} \quad \tan \frac{1}{4} E &= \frac{\sin \frac{1}{4}(A + B + C - \pi)}{\cos \frac{1}{4}(A + B + C - \pi)} \\ &= \frac{\sin \frac{1}{2}(A + B) - \sin \frac{1}{2}(\pi - C)}{\cos \frac{1}{2}(A + B) + \cos \frac{1}{2}(\pi - C)} \quad (\text{Pl. Trig., Art. 52}) \\ &= \frac{\sin \frac{1}{2}(A + B) - \cos \frac{1}{2}C}{\cos \frac{1}{2}(A + B) + \sin \frac{1}{2}C}, \end{aligned}$$

multiplying both terms of this fraction by $\cos \frac{1}{2}c$, it becomes

$$\frac{\sin \frac{1}{2}(A + B) \cos \frac{1}{2}c - \cos \frac{1}{2}c \cos \frac{1}{2}C}{\cos \frac{1}{2}(A + B) \cos \frac{1}{2}c + \cos \frac{1}{2}c \sin \frac{1}{2}C},$$

which by (1) and (3) of [60],

$$= \frac{[\cos \frac{1}{2}(a - b) - \cos \frac{1}{2}c] \cos \frac{1}{2}C}{[\cos \frac{1}{2}(a + b) + \cos \frac{1}{2}c] \sin \frac{1}{2}C},$$

and replacing $\cos \frac{1}{2}C$ and $\sin \frac{1}{2}C$ by their values, [55] and [54], we have this last

$$= \frac{\cos \frac{1}{2}(a - b) - \cos \frac{1}{2}c}{\cos \frac{1}{2}(a + b) + \cos \frac{1}{2}c} \sqrt{\frac{\sin s \sin(s - c)}{\sin(s - a) \sin(s - b)}}.$$

which, by Pl. Tr.,

$$= \frac{\sin \frac{1}{4}(a-b+c) \sin \frac{1}{4}(b+c-a)}{\cos \frac{1}{4}(a+b+c) \cos \frac{1}{4}(a+b-c)} \sqrt{\frac{\sin s \sin(s-c)}{\sin(s-a) \sin(s-b)}}$$

and since $s = \frac{1}{2}(a+b+c)$,

this last fraction becomes

$$= \sqrt{\frac{\sin^2 \frac{1}{2}(s-b) \sin^2 \frac{1}{2}(s-a) \sin s \sin(s-c)}{\cos^2 \frac{1}{2}s \cos^2 \frac{1}{2}(s-c) \sin(s-a) \sin(s-b)}};$$

and since $\sin s = 2 \sin \frac{1}{2}s \cos \frac{1}{2}s$,

$$\sin(s-c) = 2 \sin \frac{1}{2}(s-c) \cos \frac{1}{2}(s-c),$$

$$\sin(s-b) = 2 \sin \frac{1}{2}(s-b) \cos \frac{1}{2}(s-b),$$

and $\sin(s-a) = 2 \sin \frac{1}{2}(s-a) \cos \frac{1}{2}(s-a)$,

the foregoing radical then

$$= \sqrt{\frac{\sin^2 \frac{1}{2}(s-b) \sin^2 \frac{1}{2}(s-a) \sin \frac{1}{2}s \cos \frac{1}{2}s \sin \frac{1}{2}(s-c) \cos \frac{1}{2}(s-c)}{\cos^2 \frac{1}{2}s \cos^2 \frac{1}{2}(s-c) \sin \frac{1}{2}(s-a) \cos \frac{1}{2}(s-a) \sin \frac{1}{2}(s-b) \cos \frac{1}{2}(s-b)}};$$

therefore

$$\tan \frac{1}{4}E = \sqrt{\tan \frac{1}{2}s \tan \frac{1}{2}(s-a) \tan \frac{1}{2}(s-b) \tan \frac{1}{2}(s-c)}. \quad [63]$$

If E in [62] be replaced by its value in [63], then the area of a spherical triangle may be easily obtained in terms of its three sides.

113. *To find the area of a spherical polygon in terms of its angles.*

Draw arcs of great circles from one of the vertices to the others; the polygon will then be divided into triangles, whose areas may be computed separately. Their sum will be the area of the polygon.

If n be the number of sides of a polygon, T the sum of all its angles, and P its area, then

$$P = [T - (n-2)\pi]r^2. \quad [64]$$

114. *To find the angular radius of a small circle circumscribed about a spherical triangle.*

Let OA , OB , and OC , the arcs of great circles, be drawn from O , the pole of the small circle ABC , to the vertices of the spherical triangle ABC (Fig. 32). Three isosceles spherical triangles are formed, having the sides of the given triangle for their bases.

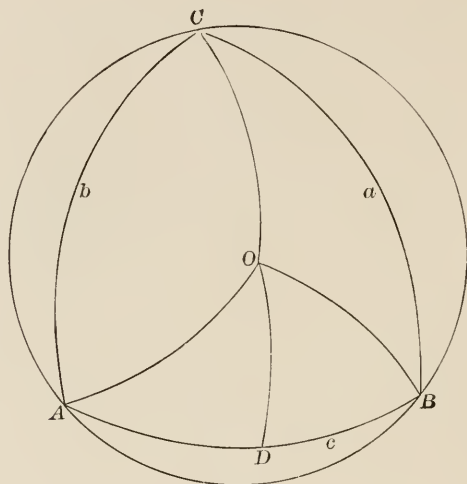


FIG. 32.

Let θ = each of the equal angles in the isosceles triangle OBA ; θ' , each equal angle in OAC ; and θ'' , each equal angle in OBC . Whether the pole of the circumscribed small circle be taken within or without the triangle, the formulæ will be the same.

Taking the pole within, then

$$\theta + \theta' = A; \quad \theta + \theta'' = B; \quad \text{and} \quad \theta' + \theta'' = C;$$

whence $\theta + \theta' + \theta'' = \frac{1}{2}(A + B + C) = 90^\circ + \frac{1}{2}E$.

Therefore

$$\theta = 90^\circ - (C - \frac{1}{2}E),$$

$$\theta' = 90^\circ - (B - \frac{1}{2}E),$$

$$\theta'' = 90^\circ - (A - \frac{1}{2}E).$$

Let the angular radius

$$OA = OB = OC = R.$$

Draw OD , an arc of a great circle, from O , perpendicular to the side c of the given triangle. The spherical right triangle ADO thus formed gives

$$\tan R \cos \theta = \tan \frac{1}{2}c.$$

Replacing θ by its value $90^\circ - (C - \frac{1}{2}E)$, we obtain

$$\tan R = \frac{\tan \frac{1}{2}c}{\cos(90^\circ - (C - \frac{1}{2}E))},$$

or
$$\tan R = \frac{\tan \frac{1}{2}c}{\sin(C - \frac{1}{2}E)}. \quad [65]$$

115. *To find the angular radius of a small circle inscribed in a spherical triangle.*

Join the pole O , of the small circle EFD (Fig. 33), to the vertices, by the arcs of great circles OA , OB , and OC . Draw OF , OD , and OE , arcs of great circles, from O , perpendicular to the three sides of the triangle. Let $OF = r$, $\triangle OFA$ being a right triangle, one of whose sides is r , another is $\frac{1}{2}(b + c - a)$ or $s - a$, and the angle $OA'F'$ adjacent to $s - a$ equals $\frac{1}{2}A = \frac{1}{2}\theta$.

Then

$$\tan r = \sin(s - a) \tan \frac{1}{2}\theta,$$

or, replacing $\tan \frac{1}{2}\theta$ by its value in terms of the sides of $\triangle ABC$, we obtain

$$\tan r = \sqrt{\frac{\sin(s - a) \sin(s - b) \sin(s - c)}{\sin s}}. \quad [66]$$

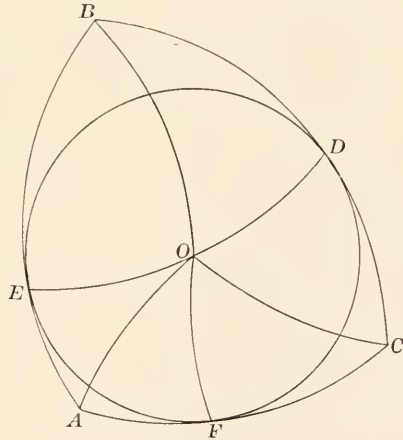


FIG. 33.

116. To find the angular radii of the small circles escribed upon the sides of a spherical triangle.

An *escribed circle* is one which is tangent to one side of a triangle and the other two sides produced.

Prolong the sides b and c (Fig. 34) of the triangle ABC , until they meet at D , 180° from A . In this manner, another triangle BDC will be formed whose sides are

- (1) a ,
- (2) $\pi - b$,
- (3) $\pi - c$.

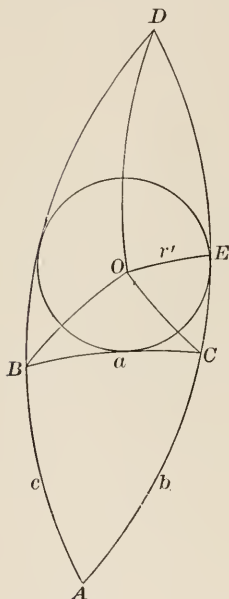


FIG. 34.

Let r' , an arc of a great circle, be the radius required. From the right triangle DOE , we obtain, by letting A or its equal $D = \theta$,

$$\tan r' = \tan \frac{\theta}{2} \sin s.$$

Remembering that $s = \frac{1}{2}(a + b + c)$, and that $\tan \frac{1}{2}\theta$ is equal to

$$\sqrt{\frac{\sin(s-b) \sin(s-c)}{\sin s \sin(s-a)}},$$

$$\left. \begin{aligned} \text{then } \tan r' &= \sin s \sqrt{\frac{\sin(s-b) \sin(s-c)}{\sin s \sin(s-a)}} = \sqrt{\frac{\sin s \sin(s-b) \sin(s-c)}{\sin(s-a)}}, \\ \tan r'' &= \sin s \sqrt{\frac{\sin(s-a) \sin(s-c)}{\sin s \sin(s-b)}} = \sqrt{\frac{\sin s \sin(s-a) \sin(s-c)}{\sin(s-b)}}, \\ \tan r''' &= \sin s \sqrt{\frac{\sin(s-a) \sin(s-b)}{\sin s \sin(s-c)}} = \sqrt{\frac{\sin s \sin(s-a) \sin(s-b)}{\sin(s-c)}}. \end{aligned} \right\} [67]$$

r'' and r''' are the angular radii of the two small circles tangent to the sides b and c and the prolongations of the others.

117. EXAMPLES.**SET IX.**

1. Find the area of a spherical triangle, whose angles are 140° , 92° , and 68° , respectively, described on a sphere whose radius is 15 feet.

2. What is the area of a spherical triangle whose angles are 150° , 110° , and 60° , respectively, described on a sphere whose radius is 10 feet?

3. Given $a = 98^\circ$, $b = 110^\circ$, and $c = 115^\circ$; to find the area of the triangle when traced on a sphere whose radius is 100 feet.

4. Each side of a spherical triangle is 10° . Required the spherical excess, the sphere's diameter being 10 feet.

5. Given $a = 88^\circ 12' 20''$, $b = 124^\circ 7' 17''$, and $C = 50^\circ 2' 1''$; to find the spherical excess.

6. If the angles of a spherical triangle be together equal to four right angles, show that

$$\cos^2 \frac{1}{2} a + \cos^2 \frac{1}{2} b + \cos^2 \frac{1}{2} c = 1.$$

7. A spherical polygon of five sides has $A = 75^\circ$, $B = 80^\circ$, $C = 115^\circ$, $D = 120^\circ$, and $E = 150^\circ$. Find its area.

CHAPTER XI.

APPLICATIONS OF SPHERICAL TRIGONOMETRY.

118. The theory of Spherical Trigonometry has one of its most useful applications in the solution of astronomical problems. The theory owes its origin in no small degree to the inquiries that have grown out of the subject of Astronomy. Nearly all the lines that are considered as traced on the surface of the earth are, by astronomers, extended to the heavens, thus constituting a sphere called the *Celestial Sphere*, whose radius is "greater than any assignable quantity."

119. *Definitions of Terms.*

(1) The *Horizon* is a great circle traced on the celestial sphere, whose poles are called the *Zenith* and the *Nadir*. The plane of the horizon touches the surface of the earth at the point of observation, and is then called the *Sensible Horizon*. But when that plane passes through the centre of the earth parallel to the sensible horizon, it is called the *Rational Horizon*.

(2) The *Zenith* is a point in the celestial sphere vertically overhead.

(3) The *Nadir* is a point in the celestial sphere directly opposite to the zenith.

(4) *Vertical Circles* are great circles passing through the zenith and nadir, perpendicular to the horizon. Upon them the altitudes of celestial objects are measured.

(5) The *Meridian* is the great circle that passes through both the *North Pole* and the *South Pole*, and the *Zenith* and the *Nadir*.

(6) The *Prime Vertical* is the vertical circle cutting the meridian at right angles at the zenith, and, therefore, having an east and west direction on the celestial sphere.

120. The *Equinoctial* or *Celestial Equator* is a great circle traced on the celestial sphere by the plane of the earth's equator extended to the heavens.

(1) The *Axis* of the celestial sphere is the axis of the earth extended in both directions until it meets the sky.

(2) The *North Pole* and the *South Pole* are the ends of the axis of the celestial sphere.

(3) *Hour Circles*, sometimes called *Celestial Meridians*, are great circles of the celestial sphere passing through its two poles, and perpendicular to the equinoctial.

121. The *Ecliptic* is a great circle traced by the sun in its apparent annual motion about the earth. The *Ecliptic* and the *Equinoctial* intersect at an angle of nearly $23^{\circ} 27'$, at two points, one, called the *Vernal Equinox*, the other, the *Autumnal Equinox*. The date of the Vernal Equinox, i.e., when the sun crosses the equinoctial going north, is the 20th of March; that of the Autumnal Equinox, the 22d of September.

(1) *Circles of Celestial Latitude* are great circles that pass through the poles of the ecliptic, perpendicular to the plane of the ecliptic.

(2) The point on the ecliptic from which celestial longitude is estimated is the vernal equinox, towards the east.

122. The position of a star in the celestial sphere may be described in several ways by means of great circles and their poles taken as standards of reference. Whatever these standards may be, the quantities employed are called the *Spherical Co-ordinates* of the star.

The standards of reference and the spherical co-ordinates are as follows:—

- | | | |
|--|---|---|
| (1) Horizon and Zenith | { | Azimuth, and Altitude or Zenith Distance. |
| (2) Equinoctial and North Pole | { | Right Ascension, and Declination; or, Declination, and Hour-Angle. |
| (3) Ecliptic and Pole | { | Latitude, and Longitude. |

Let $ENWS$ be the plane of the horizon (Fig. 35); Z , the zenith; O , the point of observation; WZE , the prime vertical; NZS , the meridian; and B , any star.

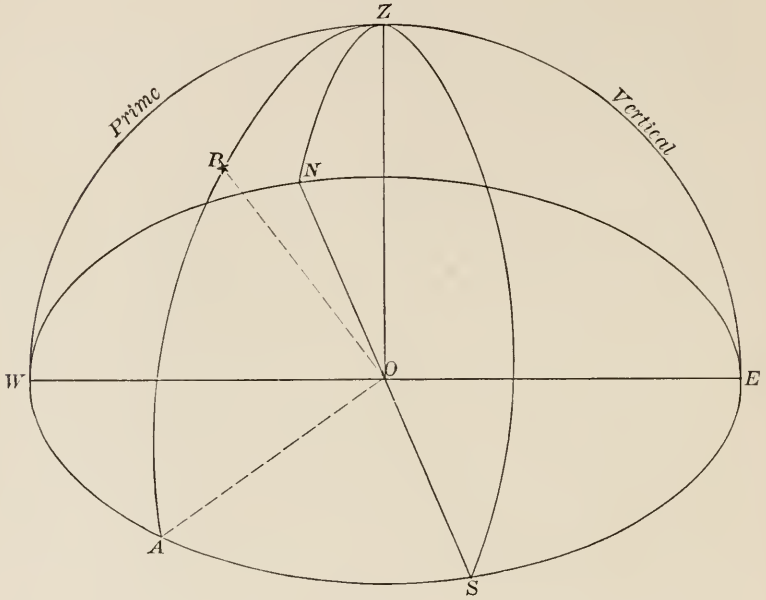


FIG. 35.

(1) The *Azimuth* of a star is its angular distance from either the north or the south point of the horizon to a vertical circle passing through the star.

The *Azimuth* of B , from the south point S , is the arc AS .

(2) The *Altitude* of a star is its angular elevation above the horizon, measured on a vertical circle passing through the star.

The *Altitude* of B is the arc AB . The *Zenith Distance* of B is BZ . The altitude + the zenith distance = 90° .

(3) The *Right Ascension* of a star is the arc of the equinoctial included between the vernal equinox and the foot of the hour-circle passing through the star. It is reckoned always *eastward* from the equinox completely around the circle.

Let $MWTE$ (Fig. 36) be the equinoctial; B , the vernal equinox; P and R , the poles of the equinoctial; POR , the axis of the celestial sphere; $SWNE$, the horizon; and A , any star.

The *Right Ascension* of the star A is the angle BPD , or the arc BD measured from the *vernal equinox* B .

The *Hour-Angle* of the star A is the angle DPM , or the arc MD .

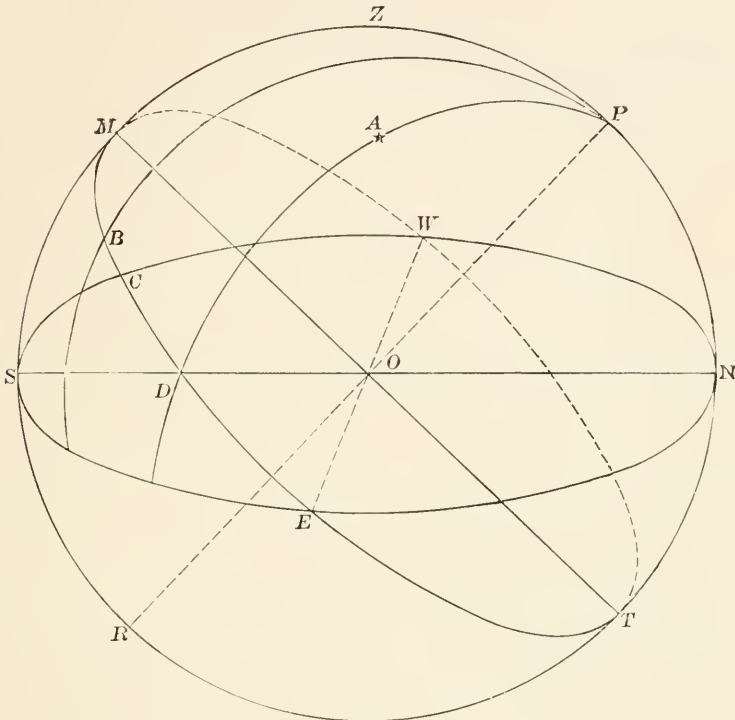


FIG. 36.

(4) The *Declination* of a star is its angular distance north or south of the *equinoctial*, and is measured by that arc of the *hour-circle* that extends from the equinoctial to the star.

The *North Polar Distance* is the arc of the *hour-circle* that extends from the star to the pole.

The *Declination* of the star A is the arc AD , and the *North Polar Distance* is the arc AP .

Let $EBFD$ (Fig. 37) be the equinoctial; $ABCD$, the ecliptic; P , the pole of the equinoctial; Z , the pole of the ecliptic; B , the vernal equinox; CBF , the obliquity of the ecliptic; S , any star; PSK , the *hour-circle*; and ZSM , the *circle of latitude* through S .

(1) The *Latitude* of a star is its angular distance from the star to the ecliptic, measured on a *circle of latitude*.

The arc SM is the *latitude* of the star S .

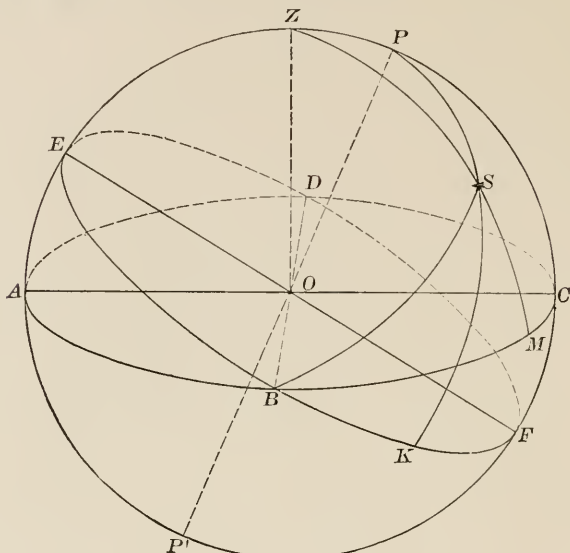


FIG. 37.

(2) The *Longitude* of a star measures the arc between the vernal equinox and the point on the ecliptic cut by the circle of latitude through the star.

The arc BM is the *longitude* of the star S .

123. Given the sun's right ascension and declination ; to determine his longitude and the obliquity of the ecliptic.

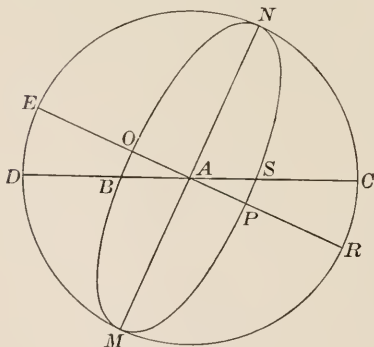


FIG. 38.

Let $EDRCN$ be the celestial meridian, passing through the points where the sun's declination is greatest; NM , the axis of the sphere; ER , the equator or equinoctial; DC , the ecliptic; NSM , the declination circle passing through the sun S . Then APS is a spherical triangle, right-angled at P . The right ascension is AP ; the declination, SP ;

and we are to find the longitude AS , and the obliquity SAP .
Solve by Napier's Rules for Circular Parts.

124. *Given the sun's declination ; to find the time of his rising at any place whose latitude is known.*

Let $NEMR$ (Fig. 39) be the meridian of the place; Z , the zenith; HO , the horizon; BC , the apparent path of the sun on the proposed day, cutting the horizon in S . EZ , then, will be the latitude, and EH or OR will be the complement of the latitude. EH or its equal measures the angle OAR . PS is the sun's declination, and AP , expressed in time, will be the time of sunrise. Degrees are changed into hours by dividing by 15. Therefore in the spherical right triangle APS , we have given PS , the declination, the angle SAP , to find AP , the time from 6 o'clock. Solve by Napier's Circular Parts.

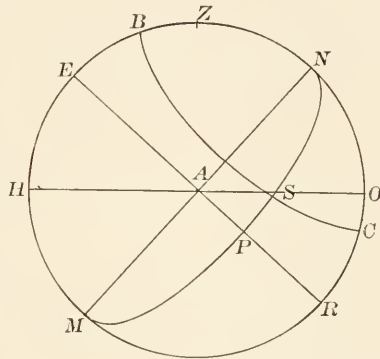


FIG. 39.

125. *Given the obliquity of the ecliptic and the declination of the sun ; to find his longitude and right ascension.*

Let OB (Fig. 40) represent the ecliptic; OC , the equinoctial; and P , the pole of the equinoctial. Let A be the sun's position, and PAD the arc of a great circle passing through the sun and the pole. Then OAD is a spherical triangle, right-angled at D , and AD is the sun's declination, AO his longitude, and AOD the obliquity of the ecliptic. AD and the angle AOD are given, and it is required to determine the *longitude* and *right ascension*.

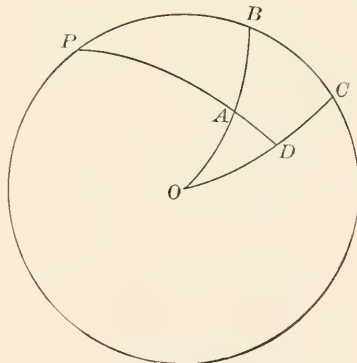
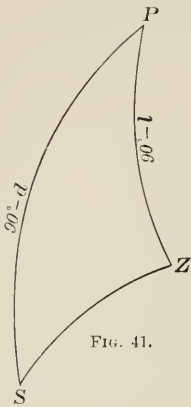


FIG. 40.

- 126.** Given the hour-angle, latitude, and declination of any star; to determine the altitude and azimuth.



In Fig. 41, PS = the complement of the declination, PZ equals the complement of the latitude, and the angle SPZ , the hour-angle. The angle SZP is the supplement of the azimuth, and the arc SZ is the complement of the altitude. P is the pole; Z , the zenith; and S , the star. This problem gives $90^\circ - d$, $90^\circ - l$, and the hour-angle SPZ , from which to determine the altitude and the azimuth.

The angle SZP may be found by (1) and (2) of Napier's Analogies; then by the law of sines SZ can readily be obtained.

127. EXAMPLES.

SET X.

- Given the sun's right ascension on a certain day, $53^\circ 38'$, and declination $19^\circ 15' 57''$; to determine his longitude and the obliquity of the ecliptic.
- On a certain day the sun's declination was observed to be $4^\circ 13' 31\frac{1}{2}''$, the obliquity of the ecliptic being $23^\circ 27' 51''$; required his right ascension.
- Given the sun's declination $23^\circ 28'$; what is the time of sunrise at latitude $52^\circ 13' N.$?
- Required the time of sunrise at latitude $57^\circ 2' 54''$, when the sun's declination is $23^\circ 28' N.$
- The obliquity of the ecliptic on a certain day was $23^\circ 27' 36''$, and the declination of the sun $21^\circ 52' 56''$. Find the sun's longitude and right ascension.
- On a certain day the declination of the sun was $5^\circ 58' 8''$, and the obliquity of the ecliptic $23^\circ 27' 38''$. Find the sun's longitude and right ascension.
- The latitude of a star is $40^\circ 36' 23''.9$, the declination $23^\circ 4' 24''.3$, and the hour-angle $46^\circ 40' 4''.5$. Find the star's altitude and azimuth.
- The latitude of a star is $40^\circ 36' 23''.9$, its altitude $47^\circ 15' 18''.3$, and the azimuth $80^\circ 23' 4''.47$. Find the star's declination and hour-angle.

CHAPTER XII.

MISCELLANEOUS EXAMPLES.

128.

SET XI.

1. The sides of a triangle are 17, 21, and 28. Prove that the length of a line bisecting the longest side and drawn from the opposite angle is 13.

2. Show that the area of a quadrilateral, whose diagonals a and b intersect at an angle A , is $\frac{1}{2}ab \sin A$.

3. If $\theta + \theta' + \theta'' = 180^\circ$, prove that

$$(a) \sin 2\theta + \sin 2\theta' + \sin 2\theta'' = 4 \sin \theta \sin \theta' \sin \theta'';$$

$$(b) \sin(\theta + \theta') \sin(\theta' + \theta'') = \sin \theta \sin \theta''.$$

4. If $\theta + \theta' + \theta'' = 90^\circ$, prove that

$$(a) \cos 2\theta + \cos 2\theta' + \cos 2\theta'' = 1 + 4 \sin \theta \sin \theta' \sin \theta'';$$

$$(b) \tan \frac{1}{2}\theta + \tan \frac{1}{2}\theta' + \tan \frac{1}{2}\theta'' - \tan \frac{1}{2}\theta \tan \frac{1}{2}\theta' \tan \frac{1}{2}\theta'' \\ = 1 - \tan \frac{1}{2}\theta \tan \frac{1}{2}\theta' - \tan \frac{1}{2}\theta \tan \frac{1}{2}\theta'' - \tan \frac{1}{2}\theta' \tan \frac{1}{2}\theta''.$$

5. If $\tan \theta = \frac{1}{3}$, and $\tan \theta' = \frac{1}{4}$, show that $2\theta + \theta' = 45^\circ$.

6. If $\cot 2\theta = -\tan \theta'$, show that $\tan(\theta - \theta') = \cot \theta$.

7. If $\cos 3\theta + \cos 2\theta + \cos \theta = 0$, show that $\theta = 45^\circ$, or 120° , or 135° , etc.

8. In a triangle ABC , right-angled at C , show that

$$\sin^2 \frac{1}{2}A = \frac{c-b}{2c}; \quad \cos^2 \frac{1}{2}A = \frac{c+b}{2c}; \quad \tan^2 \frac{1}{2}A = \frac{c-b}{c+b}.$$

9. In a triangle ABC , right-angled at C , show that

$$\sin 2A = \frac{2ab}{a^2 + b^2}, \quad \text{and} \quad \cos 2A = \frac{a^2 - b^2}{a^2 + b^2}.$$

10. In a triangle ABC , right-angled at C , show that the

$$\text{area} = \frac{1}{4}c^2 \sin 2A = \frac{1}{2}a^2 \tan B = \frac{1}{2}b^2 \tan A.$$

11. If $\cos B \sin C = \sin A$, show that the triangle will be isosceles.

12. The triangle ABC has its angles A , B , and C , in the proportion of the numbers 2, 3, and 4, respectively; show that

$$\cos \frac{1}{2} A = \frac{a+c}{2b}, \quad \text{and} \quad b^2 = \frac{a(a+c)^2}{2a+c}.$$

13. $\tan^{-1} \frac{1}{x-1} - \tan^{-1} \frac{1}{x+1} = \frac{\pi}{12}$; show that $x = \sqrt{3} + 1$.

14. If $(s-a)(s-b) = ab$, show that the triangle is impossible.

15. The area of a triangle is 84 square inches, and two of its sides are 15 and 13 inches, respectively; find the third side.

16. The sides of a triangle are 3, 7, and 8, respectively. Compare the radii of the inscribed and circumscribed circles.

17. Two sides of a triangle are 8 and 10 inches, respectively, and the included angle 30° . Find the area.

18. A, B, C, D are four trees in a row, such that AB, BC, CD subtend equal angles at a point P . If $AB = 40$ feet, $BC = 20$ feet, and $CD = 60$ feet, show that $PA = 24\sqrt{5}$ feet, $PB = 8\sqrt{10}$ feet, $PC = 12\sqrt{5}$ feet, and $PD = 24\sqrt{10}$ feet.

19. A lighthouse 60 feet high is just seen from the deck of a ship 12 feet above the water; how far is the ship from the lighthouse?

20. If the length of an arc of 60° is 11 feet, show that the radius of the circle is 10 feet 6 inches.

21. The supplement of one angle of a triangle is double the complement of another, and triple that of the third; find the angles.

22. A ship sailing N. sees two lighthouses due E. After sailing an hour they are S.E. and S.S.E., the distance between them is 8 miles; find the rate of the ship.

23. Show that the number of acres in a field, whose sides are 400, 300, 300, and 300 yards, respectively, and one angle adjacent to the largest side is a right angle, is $\frac{125}{242}(5\sqrt{11} + 24)$.

24. In Fig. 42, the line $ED = 200$ yards. $DC = 200$ yards, and $EF = 200$ yards. The angle $AFE = 83^\circ$, $BDE = 156^\circ 25'$, $BDC = 54^\circ 30'$, $AED = 53^\circ 30'$, $AEF = 54^\circ 31'$, and $BCD = 88^\circ 30'$. The length of AB is required.

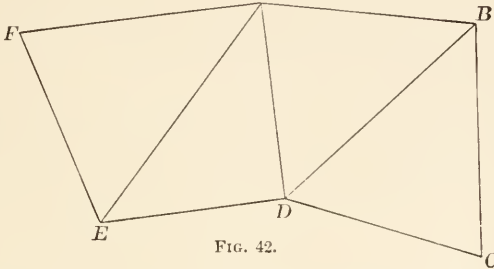


FIG. 42.

25. Given $AB = 800$ yards. $AC = 600$ yards, and $BC = 400$ yards. The angle $APC = 33^\circ 45'$, and $BPC = 22^\circ 30'$. Find the distances AP , CP , and BP . (Fig. 43.)

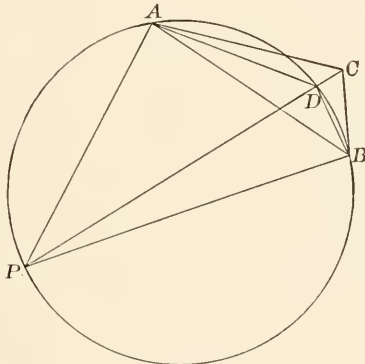


FIG. 43.

26. A balloon is observed from two stations 3000 feet apart. At the first station the horizontal angle of the balloon and the other station is $75^\circ 25'$, and the elevation of the balloon is 18° . The horizontal angle of the first station and the balloon, measured at the second station, is $64^\circ 30'$. Find the height of the balloon.

27. In a spherical equilateral triangle, show that

$$2 \cos \frac{a}{2} \sin \frac{A}{2} = 1.$$

28. In a spherical triangle, if $b + c = \pi$, show that

$$\sin 2B + \sin 2C = 0.$$

29. ABC is a spherical right triangle, in which A is not the right angle. Show that if $A = a$, then c and b are quadrants.

30. In a spherical triangle, if $A = \frac{\pi}{2}$, $B = \frac{\pi}{5}$, and $C = \frac{\pi}{3}$, show that $a + b + c = \frac{\pi}{2}$.

31. A spherical square is divided into four equal right triangles by two diagonal arcs. Find the angle A of the square, having given the side a .

32. If c_1 and c_2 be the two values of the third side of a spherical triangle, when A , a , and b , are given, and the triangle is ambiguous, show that

$$\tan \frac{1}{2}c_1 \tan \frac{1}{2}c_2 = \tan \frac{1}{2}(b - a) \tan \frac{1}{2}(b + a).$$

33. If the equal sides of a spherical isosceles triangle ABC be bisected by an arc DE , and BC be the base, show that

$$\sin \frac{1}{2}DE = \frac{1}{2} \sin \frac{1}{2}BC \sec \frac{1}{2}AC.$$

34. The sides of a spherical triangle are 105° , 90° , and 75° , respectively; find the sines of all the angles.

35. Find the area of a regular spherical polygon, whose angles are 50° , 95° , 130° , 140° , and 160° , respectively, on the surface of a sphere whose radius is 15 feet.

CHAPTER XIII.

TRIGONOMETRIC TABLES.

129. In order to use the trigonometric functions, it is necessary to compute the values of the functions of a given arc, and reciprocally be able to find the value of an arc when the value of one of its trigonometric functions is known. To reach this end, it is indispensable to have a table which will make known the values of the functions corresponding to the successive values of an arc comprised between 0° and $\frac{1}{2}\pi$, the intervals being sufficiently small.

Certain preliminary propositions must first be established, in order to show how such a table may be computed.

130. THEOREM I. *Every arc comprised between 0° and $\frac{1}{2}\pi$ is greater than its sine and less than its tangent.*

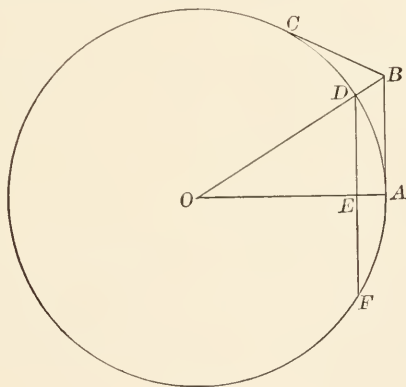


FIG. 44.

Let AD (Fig. 44) = θ , be an arc comprised between 0° and $\frac{1}{2}\pi$; DE , the sine, and AB the tangent of θ . Prolong DE to F , and draw the tangent BC ; we shall have the arc $DAF > DF$, and $ADC < AB + BC$.

The arc θ is one-half the arc DAF or the arc ADC ; $\sin \theta$ is one-half DF , and $\tan \theta$ is equal to each one of the lines AB and BC ; therefore $\theta > \sin \theta$, and $\theta < \tan \theta$.

131. COROLLARY. *If the arc θ decreases from $\frac{1}{2}\pi$ to 0, the ratio $\frac{\sin \theta}{\theta}$ approaches unity as a limit.*

Since $\tan \theta = \frac{\sin \theta}{\cos \theta}$,
we may write $\sin \theta < \theta < \frac{\sin \theta}{\cos \theta}$,

from which, dividing by $\sin \theta$,

$$1 < \frac{\theta}{\sin \theta} < \frac{1}{\cos \theta}.$$

Hence it follows that the ratio $\frac{\theta}{\sin \theta}$ is comprised between *unity* and the *fraction* $\frac{1}{\cos \theta}$, whose limit is *unity* when $\theta = 0$;

$$\therefore \text{limit of } \frac{\theta}{\sin \theta} = 1, \text{ or, limit of } \frac{\sin \theta}{\theta} = 1.$$

132. THEOREM II. *The excess of an arc comprised between 0 and $\frac{1}{2}\pi$ over its sine is less than the one-fourth, and also less than the one-sixth, of the cube of that arc.*

(1) To show that $\theta - \sin \theta < \frac{\theta^3}{4}$, it will suffice to consider the inequality established in Theorem I.;

$$\tan \frac{1}{2}\theta > \frac{1}{2}\theta.$$

Multiplying by $2 \cos^2 \frac{1}{2}\theta = 2(1 - \sin^2 \frac{1}{2}\theta)$,

$$\text{we obtain } \sin \theta > \theta - \theta \sin^2 \frac{1}{2}\theta,$$

whence $\theta - \sin \theta < \theta \sin^2 \frac{1}{2}\theta$;

but $\sin \frac{1}{2}\theta$ is less than $\frac{1}{2}\theta$, and, consequently, $\sin^2 \frac{1}{2}\theta$ is less than $\frac{1}{4}\theta^2$;

$$\therefore \theta - \sin \theta < \frac{\theta^3}{4}.$$

(2) To show that $\theta - \sin \theta < \frac{\theta^3}{6}$.

From Problem 11, Set IV., $\sin 3\theta = 3 \sin \theta - 4 \sin^3 \theta$.

Replace θ successively by

$$\frac{\theta}{3}, \frac{\theta}{3^2}, \dots, \frac{\theta}{3^n};$$

we obtain

$$\begin{aligned} 3 \sin \frac{\theta}{3} - \sin \theta &= 4 \sin^3 \frac{\theta}{3}, \\ 3 \sin \frac{\theta}{3^2} - \sin \frac{\theta}{3} &= 4 \sin^3 \frac{\theta}{3^2}, \\ &\dots \quad \dots \quad \dots \\ 3 \sin \frac{\theta}{3^n} - \sin \frac{\theta}{3^{n-1}} &= 4 \sin^3 \frac{\theta}{3^n}; \end{aligned}$$

multiplying these equations respectively by 1, 3, 3², ..., 3ⁿ⁻¹, and adding the results, the following equation is obtained,

$$3^n \sin \frac{\theta}{3^n} - \sin \theta = 4 \left(\sin^3 \frac{\theta}{3} + 3 \sin^3 \frac{\theta}{3^2} + \dots + 3^{n-1} \sin^3 \frac{\theta}{3^n} \right);$$

or
$$\theta \frac{\sin \frac{\theta}{3^n}}{\left(\frac{\theta}{3^n}\right)} - \sin \theta = 4 \left(\sin^3 \frac{\theta}{3} + 3 \sin^3 \frac{\theta}{3^2} + \dots + 3^{n-1} \sin^3 \frac{\theta}{3^n} \right).$$

If the integer n be indefinitely increased, the arc $\frac{\theta}{3^n}$ will tend towards 0, and the ratio

$$\frac{\sin \frac{\theta}{3^n}}{\frac{\theta}{3^n}}$$

towards unity; the first member of the preceding equality has then for its limit the difference $\theta - \sin \theta$, and consequently the second member tends also towards this limit.

But, as the sine is less than its arc, the limit of the second member is less than that towards which the geometrical progression

$$4 \left(\frac{\theta^3}{3^3} + \frac{\theta^3}{3^5} + \frac{\theta^3}{3^7} + \dots + \frac{\theta^3}{3^{2n+1}} \right) \text{ converges.}$$

The limit of this progression = $\frac{\theta^3}{6}$, consequently

$$\theta - \sin \theta < \frac{\theta^3}{6}.$$

133. The preceding theorems furnish two limits, that is θ and $\theta - \frac{\theta^3}{6}$, between which $\sin \theta$ is comprised. We may easily obtain two limits between which $\cos \theta$ is comprised.

$$\text{We have} \quad \cos \theta = 1 - 2 \sin^2 \frac{1}{2} \theta,$$

and, as $\sin \theta$ is comprised between $\frac{1}{2} \theta$ and $\frac{1}{2} \theta - \frac{\theta^3}{48}$, we have at once

$$\cos \theta > 1 - \frac{\theta^2}{2},$$

since $\cos \theta < 1 - 2 \left(\frac{\theta}{2} - \frac{\theta^3}{48} \right)^2$, or $< 1 - \frac{\theta^2}{2} + \frac{\theta^4}{24} - 2 \left(\frac{\theta^3}{48} \right)^2$,

and, for a stronger reason,

$$\cos \theta < 1 - \frac{\theta^2}{2} + \frac{\theta^4}{24}.$$

Therefore $\cos \theta$ is comprised between

$$1 - \frac{\theta^2}{2} \quad \text{and} \quad 1 - \frac{\theta^2}{2} + \frac{\theta^4}{24}.$$

134. *The construction of a table of sines and cosines.*

(1) Designate by θ the length of an arc of 10 seconds.

$$\text{Since} \quad \pi = 3.1415926535897932 \dots$$

may be taken as the circumference of a circle whose radius equals unity, by dividing 10π by the number of seconds in a semicircumference, we obtain

$$\theta = \frac{10 \pi}{648000} = 0.000048481368110 \dots$$

$$\text{By Art. 125,} \quad \sin \theta < \theta \quad \text{and} \quad \sin \theta > \theta - \frac{\theta^3}{6};$$

$$\text{also} \quad \frac{\theta^3}{6} < 0.0000000000000021;$$

$$\text{whence} \quad \sin 10'' < 0.000048481368110,$$

$$\sin 10'' > 0.000048481368089.$$

These two limits of $\sin 10''$ have the first twelve decimal figures common, and since they differ by less than half a unit in the thirteenth place, we may write

$$\sin 10'' = 0.0000484813681.$$

(2) To compute $\cos 10''$, we have, Art. 133,

$$\cos \theta > 1 - \frac{\theta^2}{2} \quad \text{and} \quad \cos \theta < 1 - \frac{\theta^2}{2} + \frac{\theta^4}{24};$$

and since θ is < 0.00005 or $< \frac{1}{2.10^4}$,

we have
$$\frac{\theta^4}{24} < \frac{1}{384.10^{16}} < \frac{1}{3.10^{18}};$$

from which it follows that $1 - \frac{\theta^2}{2}$ is a value of $\cos \theta$ that differs from $1 - \frac{\theta^2}{2} + \frac{\theta^4}{24}$ by a quantity less than half a unit of the eighteenth decimal order.

Performing the operation for the first thirteen decimal places, we find

$$\cos 10'' = 0.9999999988248.$$

135. *Sines and cosines of arcs for every 10'', up to 45°.*

If, in the formulæ

$$\begin{aligned} \sin(\theta + \theta') + \sin(\theta - \theta') &= 2 \cos \theta' \sin \theta, \\ \cos(\theta + \theta') + \cos(\theta - \theta') &= 2 \cos \theta' \cos \theta, \end{aligned}$$

we put $\theta = (m - 1)\theta'$, the result will be

$$(1) \begin{cases} \sin m \theta' = 2 \cos \theta' \sin(m - 1)\theta' - \sin(m - 2)\theta', \\ \cos m \theta' = 2 \cos \theta' \cos(m - 1)\theta' - \cos(m - 2)\theta'. \end{cases}$$

If θ' be made equal to $10''$ and m to 2, then these formulæ will give the values of $\sin 20''$ and $\cos 20''$. Generally, if the sine and the cosine of two consecutive multiples of the arc $\theta' = 10''$ be known, formulæ (1) will make known the sine and the cosine of the following multiple arc. That is to say, we may suppose θ' to be

constantly equal to $10''$, and m to be successively equal to 2, 3, 4, etc. We shall then obtain for the sines

$$\sin 20'' = 2 \cos 10'' \sin 10'' - \sin 0'' = .0000969627361$$

$$\sin 30'' = 2 \cos 10'' \sin 20'' - \sin 10'' =$$

$$\sin 40'' = 2 \cos 10'' \sin 30'' - \sin 20'' =$$

Etc.,

and for the cosines

$$\cos 20'' = 2 \cos 10'' \cos 10'' - \cos 0'' =$$

$$\cos 30'' = 2 \cos 10'' \cos 20'' - \cos 10'' =$$

$$\cos 40'' = 2 \cos 10'' \cos 30'' - \cos 20'' =$$

Etc.

The computation may be abridged in the following manner. Since the constant multiplier $2 \cos 10''$ differs but little from 2, then by placing

$$2 \cos 10'' = 2 - k,$$

we obtain

$$k = 0.0000000023504.$$

The sines may then be written

$$\sin 20'' = 2 \sin 10'' - \sin 0'' - k \sin 10'',$$

$$\sin 30'' = 2 \sin 20'' - \sin 10'' - k \sin 20'',$$

$$\sin 40'' = 2 \sin 30'' - \sin 20'' - k \sin 30'', \text{ etc.,}$$

and the cosines

$$\cos 20'' = 2 \cos 10'' - \cos 0'' - k \cos 10'',$$

$$\cos 30'' = 2 \cos 20'' - \cos 10'' - k \cos 20'',$$

$$\cos 40'' = 2 \cos 30'' - \cos 20'' - k \cos 30'', \text{ etc.}$$

This method of computing the sines and cosines of all arcs from $0''$ to 30° inclusive, at intervals of $10''$, is a very simple one.

136. The sines and cosines of angles or arcs above 30° up to and including 45° , are readily obtained by subtraction.

Remembering that $\sin 30^\circ = \frac{1}{2}$, we have

$$\sin(30^\circ + \theta) + \sin(30^\circ - \theta) = \cos \theta,$$

$$\cos(30^\circ - \theta) - \cos(30^\circ + \theta) = \sin \theta,$$

whence

$$\sin(30^\circ + \theta) = \cos \theta - \sin(30^\circ - \theta),$$

$$\cos(30^\circ + \theta) = \cos(30^\circ - \theta) - \sin \theta.$$

If θ be made equal to $10''$, $20''$, $30''$, etc., successively, then

$$\begin{aligned} \sin(30^\circ + 10'') &= \cos 10'' - \sin(30^\circ - 10''), \\ \sin(30^\circ + 20'') &= \cos 20'' - \sin(30^\circ - 20''), \\ \sin(30^\circ + 30'') &= \cos 30'' - \sin(30^\circ - 30''), \text{ etc.,} \end{aligned}$$

and

$$\begin{aligned} \cos(30^\circ + 10'') &= \cos(30^\circ - 10'') - \sin 10'', \\ \cos(30^\circ + 20'') &= \cos(30^\circ - 20'') - \sin 20'', \\ \cos(30^\circ + 30'') &= \cos(30^\circ - 30'') - \sin 30'', \text{ etc.} \end{aligned}$$

This process may be continued up to and including 45° .

The tables for tangents, cotangents, secants, and cosecants can be constructed by means of the formulæ

$$\begin{aligned} \tan \theta &= \frac{\sin \theta}{\cos \theta}, & \sec \theta &= \frac{1}{\cos \theta}, \\ \cot \theta &= \frac{\cos \theta}{\sin \theta}, & \operatorname{cosec} \theta &= \frac{1}{\sin \theta}. \end{aligned}$$

137. The sines and cosines of angles or arcs above 45° will be found by taking the cosines and sines of their complements below 45° , according to the formulæ of Art. 17.

138. The foregoing method is simple in principle, but laborious. A much more rapid and simple method is by infinite series.

TABLES OF LOGARITHMS OF TRIGONOMETRIC FUNCTIONS.

139. In numerical applications, computations are very often abbreviated by the use of logarithmic tables; hence there is much more need of knowing the logarithms of the sines, cosines, etc., of angles or arcs, than the *natural functions* whose development is shown by the preceding Articles.

If we take the logarithms of the natural sines and cosines of all the angles or arcs from $0''$ to 90° inclusive, another table, called the table of logarithmic sines and cosines, will be formed. This table once constructed, we may easily form a table of logarithms of tangents and cotangents by means of the formulæ

$$\begin{aligned} \log \tan \theta &= \log \sin \theta - \log \cos \theta, \\ \log \cot \theta &= \log \cos \theta - \log \sin \theta. \end{aligned}$$

When desirable the logarithms of secants and cosecants are found by means of the formulæ

$$\log \operatorname{cosec} \theta = 1 - \log \cos \theta,$$

$$\log \operatorname{cosec} \theta = 1 - \log \sin \theta.$$

140. The logarithms of sines and cosines are never positive quantities; the logarithms of tangents of angles less than 45° , and of cotangents of angles greater than 45° , are negative; therefore, to avoid negative quantities in the tables, 10 is added to the logarithm of every trigonometric function, thus forming the logarithms of the tables. This increase of the real logarithms by 10 must always be taken into consideration in logarithmic computations.

141. *Definitions.*

- (1) *Natural Numbers* are arithmetical numbers.
- (2) *Tables of Natural Functions* are the natural numbers representing the values of sines, cosines, etc., when radius is taken equal to unity.
- (3) The *Logarithm* of a natural number is the exponent of the power to which another number must be raised to produce the first number.
- (4) The *Base* is the number whose power is to be obtained.
- (5) The base of the Napierian system of logarithms is represented by the letter *e*, whose value = 2.71828 ...
- (6) The base of the common system is 10.
- (7) A logarithm consists of two parts — *characteristic* and *mantissa*. The characteristic is *integral*, and the mantissa *decimal*.

142. *Properties of Logarithms.*

- (1) *The logarithm of a product equals the sum of the logarithms of its factors.*
- (2) *The logarithm of a quotient equals the difference between the logarithm of the dividend and that of the divisor.*
- (3) *The logarithm of any power of a number equals the logarithm of the number multiplied by the exponent of the power.*
- (4) *The logarithm of any root of a number equals the logarithm of the number divided by the index of the root.*

143. The *Arithmetical Complement* of a logarithm is the remainder after subtracting the logarithm from zero.

The arithmetical complement, or co-log, as it is frequently called, is used when addition is substituted for subtraction, on the principle that *adding the co-logarithm of a number is the same precisely as subtracting the logarithm.*

144. The logarithmic and trigonometric tables that may be consulted present some variety in their mode of arrangement, and are usually accompanied with full explanation of their peculiarities and the methods of using the tables. It is not necessary to enter into any minute account of the way in which tables may be used with the greatest advantage. The student is referred to the explanations accompanying the tables to be used.

APPENDIX.

—◆—

THE formulæ of the preceding pages are of great importance. Collected and numbered the same as in the text, they will be found convenient for reference and use.

PLANE TRIGONOMETRY.

Trigonometric ratios.

PAGE 6.

| | | | |
|-----|---|---|--|
| (1) | $\sin A = \frac{a}{c},$ | } | |
| (2) | $\cos A = \frac{b}{c},$ | | |
| (3) | $\tan A = \frac{a}{b},$ | | |
| (4) | $\cot A = \frac{b}{a},$ | | |
| (5) | $\sec A = \frac{c}{b},$ | | |
| (6) | $\operatorname{cosec} A = \frac{c}{a},$ | | |
| (7) | $\operatorname{vers} A = 1 - \cos A,$ | | |
| (8) | $\operatorname{covers} A = 1 - \sin A.$ | | |

[1]

| | | | |
|-----|---|---|--|
| (1) | $\tan A \times \cot A = 1,$ | } | |
| (2) | $\sin A \times \operatorname{cosec} A = 1,$ | | |
| (3) | $\cos A \times \sec A = 1.$ | | |
| (4) | $\tan A = \frac{\sin A}{\cos A}$ | | |
| (5) | $\cot A = \frac{\cos A}{\sin A}$ | | |

[2]

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$$\begin{array}{l}
 (1) \quad \sin A = \frac{a}{c} = \cos B, \\
 (2) \quad \cos A = \frac{b}{c} = \sin B, \\
 (3) \quad \tan A = \frac{a}{b} = \cot B, \\
 (4) \quad \cot A = \frac{b}{a} = \tan B, \\
 (5) \quad \sec A = \frac{c}{b} = \operatorname{cosec} B, \\
 (6) \quad \operatorname{cosec} A = \frac{c}{a} = \sec B.
 \end{array}
 \left. \vphantom{\begin{array}{l} (1) \\ (2) \\ (3) \\ (4) \\ (5) \\ (6) \end{array}} \right\} [3]$$

PAGE 8.

$$\begin{array}{l}
 (1) \quad \sin^2 A + \cos^2 A = 1, \\
 (2) \quad 1 + \tan^2 A = \sec^2 A, \\
 (3) \quad 1 + \cot^2 A = \operatorname{cosec}^2 A, \\
 (4) \quad \cos A = \sqrt{1 - \sin^2 A}, \\
 (5) \quad \tan A = \frac{\sin A}{\sqrt{1 - \sin^2 A}}, \\
 (6) \quad \cot A = \frac{\sqrt{1 - \sin^2 A}}{\sin A}, \\
 (7) \quad \sec A = \frac{1}{\sqrt{1 - \sin^2 A}}, \\
 (8) \quad \operatorname{cosec} A = \frac{1}{\sin A}.
 \end{array}
 \left. \vphantom{\begin{array}{l} (1) \\ (2) \\ (3) \\ (4) \\ (5) \\ (6) \\ (7) \\ (8) \end{array}} \right\} [4]$$

Functions of the sum and the difference of two angles or arcs.

PAGE 24.

$$\sin(\theta + \theta') = \sin \theta \cos \theta' + \cos \theta \sin \theta'. \quad [5]$$

$$\cos(\theta + \theta') = \cos \theta \cos \theta' - \sin \theta \sin \theta'. \quad [6]$$

$$\sin(\theta - \theta') = \sin \theta \cos \theta' - \cos \theta \sin \theta'. \quad [7]$$

$$\cos(\theta - \theta') = \cos \theta \cos \theta' + \sin \theta \sin \theta'. \quad [8]$$

$$\tan(\theta + \theta') = \frac{\tan \theta + \tan \theta'}{1 - \tan \theta \tan \theta'}. \quad [9]$$

PAGE 25.

$$\cot(\theta + \theta') = \frac{\cot \theta \cot \theta' - 1}{\cot \theta' + \cot \theta}. \quad [10]$$

$$\tan(\theta - \theta') = \frac{\tan \theta - \tan \theta'}{1 + \tan \theta \tan \theta'}. \quad [11]$$

$$\cot(\theta - \theta') = \frac{1 + \cot \theta \cot \theta'}{\cot \theta' - \cot \theta}. \quad [12]$$

Functions of the sum of three angles or arcs.

$$\left. \begin{aligned} \sin(\theta + \theta' + \theta'') &= \sin \theta \cos \theta' \cos \theta'' + \sin \theta' \cos \theta \cos \theta'' \\ &\quad + \sin \theta'' \cos \theta \cos \theta' - \sin \theta \sin \theta' \sin \theta''. \end{aligned} \right\} [13]$$

$$\left. \begin{aligned} \cos(\theta + \theta' + \theta'') &= \cos \theta \cos \theta' \cos \theta'' - \cos \theta \sin \theta' \sin \theta'' \\ &\quad - \cos \theta' \sin \theta \sin \theta'' - \cos \theta'' \sin \theta \sin \theta'. \end{aligned} \right\} [14]$$

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$$\left. \begin{aligned} \sin(\theta + \theta') + \sin(\theta - \theta') &= 2 \sin \theta \cos \theta', \\ \sin(\theta + \theta') - \sin(\theta - \theta') &= 2 \cos \theta \sin \theta', \\ \cos(\theta + \theta') + \cos(\theta - \theta') &= 2 \cos \theta \cos \theta', \\ \cos(\theta + \theta') - \cos(\theta - \theta') &= -2 \sin \theta \sin \theta'. \end{aligned} \right\} [15]$$

Functions of the sum and the difference of the sines and cosines of two angles.

$$\left. \begin{aligned} (1) \quad \sin \phi + \sin \phi' &= 2 \sin \frac{1}{2}(\phi + \phi') \cos \frac{1}{2}(\phi - \phi'), \\ (2) \quad \sin \phi - \sin \phi' &= 2 \sin \frac{1}{2}(\phi - \phi') \cos \frac{1}{2}(\phi + \phi'), \\ (3) \quad \cos \phi + \cos \phi' &= 2 \cos \frac{1}{2}(\phi + \phi') \cos \frac{1}{2}(\phi - \phi'), \\ (4) \quad \cos \phi' - \cos \phi &= 2 \sin \frac{1}{2}(\phi + \phi') \sin \frac{1}{2}(\phi - \phi'). \end{aligned} \right\} [16]$$

$$\left. \begin{aligned} \cos \phi + \sin \phi' &= 2 \sin \left(\frac{1}{4}\pi - \frac{\phi - \phi'}{2} \right) \cos \left(\frac{1}{4}\pi - \frac{\phi + \phi'}{2} \right), \\ \cos \phi - \sin \phi' &= 2 \sin \left(\frac{1}{4}\pi - \frac{\phi + \phi'}{2} \right) \cos \left(\frac{1}{4}\pi - \frac{\phi - \phi'}{2} \right). \end{aligned} \right\} [17]$$

Combinations formed from [16].

PAGE 27.

$$\begin{aligned}
 (1) \quad & \frac{\sin \phi + \sin \phi'}{\sin \phi - \sin \phi'} = \frac{\sin \frac{1}{2}(\phi + \phi') \cos \frac{1}{2}(\phi - \phi')}{\sin \frac{1}{2}(\phi - \phi') \cos \frac{1}{2}(\phi + \phi')} = \frac{\tan \frac{1}{2}(\phi + \phi')}{\tan \frac{1}{2}(\phi - \phi')}, \\
 (2) \quad & \frac{\sin \phi + \sin \phi'}{\cos \phi + \cos \phi'} = \frac{\sin \frac{1}{2}(\phi + \phi')}{\cos \frac{1}{2}(\phi + \phi')} = \tan \frac{1}{2}(\phi + \phi'), \\
 (3) \quad & \frac{\sin \phi + \sin \phi'}{\cos \phi' - \cos \phi} = \frac{\cos \frac{1}{2}(\phi - \phi')}{\sin \frac{1}{2}(\phi - \phi')} = \cot \frac{1}{2}(\phi - \phi'), \\
 (4) \quad & \frac{\sin \phi - \sin \phi'}{\cos \phi + \cos \phi'} = \frac{\sin \frac{1}{2}(\phi - \phi')}{\cos \frac{1}{2}(\phi - \phi')} = \tan \frac{1}{2}(\phi - \phi'), \\
 (5) \quad & \frac{\sin \phi' - \sin \phi}{\cos \phi' - \cos \phi} = \frac{\cos \frac{1}{2}(\phi + \phi')}{\sin \frac{1}{2}(\phi + \phi')} = \cot \frac{1}{2}(\phi + \phi'), \\
 (6) \quad & \frac{\cos \phi + \cos \phi'}{\cos \phi' - \cos \phi} = \frac{\cos \frac{1}{2}(\phi + \phi') \cos \frac{1}{2}(\phi - \phi')}{\sin \frac{1}{2}(\phi + \phi') \sin \frac{1}{2}(\phi - \phi')} \\
 & = \cot \frac{1}{2}(\phi + \phi') \cot \frac{1}{2}(\phi - \phi').
 \end{aligned}
 \tag{18}$$

Functions of double angles.

$$\sin 2\theta = 2 \sin \theta \cos \theta. \tag{19}$$

$$\cos 2\theta = \cos^2 \theta - \sin^2 \theta. \tag{20}$$

$$\tan 2\theta = \frac{2 \tan \theta}{1 - \tan^2 \theta}. \tag{21}$$

$$\cot 2\theta = \frac{\cot^2 \theta - 1}{2 \cot \theta}. \tag{22}$$

Functions of half angles.

PAGE 28.

$$\sin \frac{1}{2} \theta = \pm \frac{1}{2} (\sqrt{1 + \sin \theta} \mp \sqrt{1 - \sin \theta}). \tag{23}$$

$$\cos \frac{1}{2} \theta = \pm \frac{1}{2} (\sqrt{1 + \sin \theta} \pm \sqrt{1 - \sin \theta}). \tag{24}$$

$$\cos \frac{1}{2} \theta = \pm \sqrt{\frac{1 + \cos \theta}{2}}. \tag{25}$$

$$\sin \frac{1}{2} \theta = \pm \sqrt{\frac{1 - \cos \theta}{2}}. \tag{26}$$

$$\tan \frac{1}{2} \theta = \frac{\sin \theta}{1 + \cos \theta} = \frac{1 - \cos \theta}{\sin \theta}. \quad [27]$$

$$\cot \frac{1}{2} \theta = \frac{1 + \cos \theta}{\sin \theta} = \frac{\sin \theta}{1 - \cos \theta}. \quad [28]$$

$$\sin 2\theta = \pm 2 \sin \theta \sqrt{1 - \sin^2 \theta} = \pm 2 \cos \theta \sqrt{1 - \cos^2 \theta}. \quad [29]$$

$$\cos 2\theta = 1 - 2 \sin^2 \theta = 2 \cos^2 \theta - 1. \quad [30]$$

Law of sines.

PAGE 31.

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}. \quad [31]$$

PAGE 32.

$$\left. \begin{aligned} A + B + C &= 180^\circ, \\ \frac{a}{\sin A} &= \frac{b}{\sin B}, \\ \frac{a}{\sin A} &= \frac{c}{\sin C}. \end{aligned} \right\} \quad [32]$$

Law of cosines.

$$\left. \begin{aligned} c^2 &= a^2 + b^2 - 2ab \cos C, \\ a^2 &= b^2 + c^2 - 2bc \cos A, \\ b^2 &= a^2 + c^2 - 2ac \cos B. \end{aligned} \right\} \quad [33]$$

Side of a triangle in terms of the cosines of the adjacent angles and the other two sides.

PAGE 33.

$$\left. \begin{aligned} (1) \quad a &= b \cos C + c \cos B, \\ (2) \quad b &= c \cos A + a \cos C, \\ (3) \quad c &= a \cos B + b \cos A. \end{aligned} \right\} \quad [34]$$

Law of tangents.

PAGE 34.

$$\frac{a+b}{a-b} = \frac{\tan \frac{1}{2}(A+B)}{\tan \frac{1}{2}(A-B)}. \quad [35]$$

Functions of half angles in terms of the sides of a triangle.

PAGE 35.

$$\left. \begin{aligned} \sin \frac{1}{2} A &= \sqrt{\frac{(s-b)(s-c)}{bc}}, \\ \sin \frac{1}{2} B &= \sqrt{\frac{(s-a)(s-c)}{ac}}, \\ \sin \frac{1}{2} C &= \sqrt{\frac{(s-a)(s-b)}{ab}}. \end{aligned} \right\} [36]$$

$$\left. \begin{aligned} \cos \frac{1}{2} A &= \sqrt{\frac{s(s-a)}{bc}}, \\ \cos \frac{1}{2} B &= \sqrt{\frac{s(s-b)}{ac}}, \\ \cos \frac{1}{2} C &= \sqrt{\frac{s(s-c)}{ab}}. \end{aligned} \right\} [37]$$

PAGE 36.

$$\left. \begin{aligned} \tan \frac{1}{2} A &= \sqrt{\frac{(s-b)(s-c)}{s(s-a)}}, \\ \tan \frac{1}{2} B &= \sqrt{\frac{(s-a)(s-c)}{s(s-b)}}, \\ \tan \frac{1}{2} C &= \sqrt{\frac{(s-a)(s-b)}{s(s-c)}}. \end{aligned} \right\} [38]$$

Area of triangles.

$$K = \frac{1}{2} bc \sin A. \quad [39]$$

PAGE 37.

$$K = \sqrt{s(s-a)(s-b)(s-c)}. \quad [40]$$

$$\left. \begin{aligned} (1) \quad \sin \frac{1}{2} A \sin \frac{1}{2} B \sin \frac{1}{2} C &= \frac{(s-a)(s-b)(s-c)}{abc} = \frac{K^2}{sabc}, \\ (2) \quad \cos \frac{1}{2} A \cos \frac{1}{2} B \cos \frac{1}{2} C &= \frac{s\sqrt{s(s-a)(s-b)(s-c)}}{abc} = \frac{Ks}{abc}, \\ (3) \quad \tan \frac{1}{2} A \tan \frac{1}{2} B \tan \frac{1}{2} C &= \frac{K}{s^2}. \end{aligned} \right\} [41]$$

Radii of circumscribed and inscribed circles.

PAGE 38.

$$R = \frac{abc}{4\sqrt{s(s-a)(s-b)(s-c)}}. \quad [42]$$

$$r = \sqrt{\frac{(s-a)(s-b)(s-c)}{s}}. \quad [43]$$

PAGE 39.

Radii of escribed circles.

$$\left. \begin{aligned} r' &= \frac{K}{s-a} = \sqrt{\frac{s(s-b)(s-c)}{s-a}}, \\ r'' &= \frac{K}{s-c} = \sqrt{\frac{s(s-a)(s-b)}{s-c}}, \\ r''' &= \frac{K}{s-b} = \sqrt{\frac{s(s-a)(s-c)}{s-b}}. \end{aligned} \right\} [44]$$

$$\left. \begin{aligned} r' &= s \tan \frac{1}{2} A, \\ r'' &= s \tan \frac{1}{2} C, \\ r''' &= s \tan \frac{1}{2} B. \end{aligned} \right\} [45]$$

PAGE 40.

$$\left. \begin{aligned} \frac{1}{r} &= \frac{1}{r'} + \frac{1}{r''} + \frac{1}{r'''}, \\ K &= \sqrt{r'r''r'''}, \\ 4R &= r' + r'' + r''' - r. \end{aligned} \right\} [46]$$

SPHERICAL TRIGONOMETRY.

Fundamental formulæ of spherical triangles.

PAGE 51.

$$\left. \begin{aligned} \cos a &= \cos b \cos c + \sin b \sin c \cos A, \\ \cos b &= \cos a \cos c + \sin a \sin c \cos B, \\ \cos c &= \cos a \cos b + \sin a \sin b \cos C. \end{aligned} \right\} [47]$$

PAGE 52.

$$\left. \begin{aligned} \cos A &= -\cos B \cos C + \sin B \sin C \cos a, \\ \cos B &= -\cos A \cos C + \sin A \sin C \cos b, \\ \cos C &= -\cos A \cos B + \sin A \sin B \cos c. \end{aligned} \right\} \quad [48]$$

Law of sines.

PAGE 53.

$$\frac{\sin A}{\sin a} = \frac{\sin B}{\sin b} = \frac{\sin C}{\sin c}. \quad [49]$$

Three sides and two angles of a spherical triangle.

PAGE 54.

$$\left. \begin{aligned} \cos a \sin b - \sin a \cos b \cos C &= \sin c \cos A, \\ \cos b \sin a - \sin b \cos a \cos C &= \sin c \cos B, \\ \cos b \sin c - \sin b \cos c \cos A &= \sin a \cos B, \\ \cos c \sin b - \sin c \cos b \cos A &= \sin a \cos C, \\ \cos c \sin a - \sin c \cos a \cos B &= \sin b \cos C, \\ \cos a \sin c - \sin a \cos c \cos B &= \sin b \cos A. \end{aligned} \right\} \quad [50]$$

Two sides and three angles of a spherical triangle.

$$\left. \begin{aligned} \cos a \sin B - \cos b \cos C \sin A &= \cos A \sin C, \\ \cos b \sin A - \cos a \cos C \sin B &= \cos B \sin C, \\ \cos b \sin C - \cos c \cos A \sin B &= \cos B \sin A, \\ \cos c \sin B - \cos b \cos A \sin C &= \cos C \sin A, \\ \cos c \sin A - \cos a \cos B \sin C &= \cos C \sin B, \\ \cos a \sin C - \cos c \cos B \sin A &= \cos A \sin B. \end{aligned} \right\} \quad [51]$$

Two sides and two angles of a spherical triangle.

$$\left. \begin{aligned} \cot a \sin b - \cot A \sin C &= \cos b \cos C, \\ \cot b \sin a - \cot B \sin C &= \cos a \cos C, \\ \cot b \sin c - \cot B \sin A &= \cos c \cos A, \\ \cot c \sin b - \cot C \sin A &= \cos b \cos A, \\ \cot c \sin a - \cot C \sin B &= \cos a \cos B, \\ \cot a \sin c - \cot A \sin B &= \cos c \cos B. \end{aligned} \right\} \quad [52]$$

Formule for solving spherical right triangles.

PAGE 55.

$$\begin{array}{l}
 (1) \cos a = \cos b \cos c, \\
 (2) \sin b = \sin a \sin B, \\
 (3) \sin c = \sin a \sin C, \\
 (4) \tan b = \tan a \cos C, \\
 (5) \tan b = \sin c \tan B, \\
 (6) \tan c = \tan a \cos B, \\
 (7) \tan c = \sin b \tan C, \\
 (8) \cos a = \cot B \cot C, \\
 (9) \cos B = \cos b \sin C, \\
 (10) \cos C = \cos c \sin B.
 \end{array}
 \left. \vphantom{\begin{array}{l} (1) \\ (2) \\ (3) \\ (4) \\ (5) \\ (6) \\ (7) \\ (8) \\ (9) \\ (10) \end{array}} \right\} [53]$$

Functions of half angles in terms of the sides of a spherical triangle.

PAGE 56.

$$\begin{array}{l}
 \sin \frac{1}{2} A = \sqrt{\frac{\sin(s-b)\sin(s-c)}{\sin b \sin c}}, \\
 \sin \frac{1}{2} B = \sqrt{\frac{\sin(s-a)\sin(s-c)}{\sin a \sin c}}, \\
 \sin \frac{1}{2} C = \sqrt{\frac{\sin(s-a)\sin(s-b)}{\sin a \sin b}}.
 \end{array}
 \left. \vphantom{\begin{array}{l} \sin \frac{1}{2} A \\ \sin \frac{1}{2} B \\ \sin \frac{1}{2} C \end{array}} \right\} [54]$$

$$\begin{array}{l}
 \cos \frac{1}{2} A = \sqrt{\frac{\sin s \sin(s-a)}{\sin b \sin c}}, \\
 \cos \frac{1}{2} B = \sqrt{\frac{\sin s \sin(s-b)}{\sin a \sin c}}, \\
 \cos \frac{1}{2} C = \sqrt{\frac{\sin s \sin(s-c)}{\sin a \sin b}}.
 \end{array}
 \left. \vphantom{\begin{array}{l} \cos \frac{1}{2} A \\ \cos \frac{1}{2} B \\ \cos \frac{1}{2} C \end{array}} \right\} [55]$$

$$\begin{array}{l}
 \tan \frac{1}{2} A = \sqrt{\frac{\sin(s-b)\sin(s-c)}{\sin s \sin(s-a)}}, \\
 \tan \frac{1}{2} B = \sqrt{\frac{\sin(s-a)\sin(s-c)}{\sin s \sin(s-b)}}, \\
 \tan \frac{1}{2} C = \sqrt{\frac{\sin(s-a)\sin(s-b)}{\sin s \sin(s-c)}}.
 \end{array}
 \left. \vphantom{\begin{array}{l} \tan \frac{1}{2} A \\ \tan \frac{1}{2} B \\ \tan \frac{1}{2} C \end{array}} \right\} [56]$$

Functions of half sides in terms of the angles of a spherical triangle.

PAGE 58.

$$\left. \begin{aligned} \sin \frac{1}{2} a &= \sqrt{-\frac{\cos S \cos (S-A)}{\sin B \sin C}}, \\ \sin \frac{1}{2} b &= \sqrt{-\frac{\cos S \cos (S-B)}{\sin A \sin C}}, \\ \sin \frac{1}{2} c &= \sqrt{-\frac{\cos S \cos (S-C)}{\sin A \sin B}}. \end{aligned} \right\} [57]$$

$$\left. \begin{aligned} \cos \frac{1}{2} a &= \sqrt{\frac{\cos (S-B) \cos (S-C)}{\sin B \sin C}}, \\ \cos \frac{1}{2} b &= \sqrt{\frac{\cos (S-A) \cos (S-C)}{\sin A \sin C}}, \\ \cos \frac{1}{2} c &= \sqrt{\frac{\cos (S-A) \cos (S-B)}{\sin A \sin B}}. \end{aligned} \right\} [58]$$

$$\left. \begin{aligned} \tan \frac{1}{2} a &= \sqrt{-\frac{\cos S \cos (S-A)}{\cos (S-B) \cos (S-C)}}, \\ \tan \frac{1}{2} b &= \sqrt{-\frac{\cos S \cos (S-B)}{\cos (S-A) \cos (S-C)}}, \\ \tan \frac{1}{2} c &= \sqrt{-\frac{\cos S \cos (S-C)}{\cos (S-A) \cos (S-B)}}. \end{aligned} \right\} [59]$$

Delambre's Formulæ.

PAGE 60.

$$\left. \begin{aligned} (1) \quad \frac{\sin \frac{1}{2}(A+B)}{\cos \frac{1}{2} C} &= \frac{\cos \frac{1}{2}(a-b)}{\cos \frac{1}{2} c}, \\ (2) \quad \frac{\sin \frac{1}{2}(A-B)}{\cos \frac{1}{2} C} &= \frac{\sin \frac{1}{2}(a-b)}{\sin \frac{1}{2} c}, \\ (3) \quad \frac{\cos \frac{1}{2}(A+B)}{\sin \frac{1}{2} C} &= \frac{\cos \frac{1}{2}(a+b)}{\cos \frac{1}{2} c}, \\ (4) \quad \frac{\cos \frac{1}{2}(A-B)}{\sin \frac{1}{2} C} &= \frac{\sin \frac{1}{2}(a+b)}{\sin \frac{1}{2} c}. \end{aligned} \right\} [60]$$

Napier's Analogies.

$$\left. \begin{aligned}
 (1) \quad \tan \frac{1}{2}(A + B) &= \cot \frac{1}{2}C \frac{\cos \frac{1}{2}(a - b)}{\cos \frac{1}{2}(a + b)}, \\
 (2) \quad \tan \frac{1}{2}(A - B) &= \cot \frac{1}{2}C \frac{\sin \frac{1}{2}(a - b)}{\sin \frac{1}{2}(a + b)}, \\
 (3) \quad \tan \frac{1}{2}(a + b) &= \tan \frac{1}{2}c \frac{\cos \frac{1}{2}(A - B)}{\cos \frac{1}{2}(A + B)}, \\
 (4) \quad \tan \frac{1}{2}(a - b) &= \tan \frac{1}{2}c \frac{\sin \frac{1}{2}(A - B)}{\sin \frac{1}{2}(A + B)}.
 \end{aligned} \right\} [61]$$

Area of spherical triangles.

PAGE 76.

$$ABC = \frac{E}{180^\circ} \times \pi r^2. \quad [62]$$

L'Huilier's Formula.

PAGE 77.

$$\tan \frac{1}{4}E = \sqrt{\tan \frac{1}{2}s \tan \frac{1}{2}(s - a) \tan \frac{1}{2}(s - b) \tan \frac{1}{2}(s - c)}. \quad [63]$$

Area of spherical polygons.

$$P = [T - (n - 2)\pi]r^2. \quad [64]$$

Angular radii of small circles circumscribed about, inscribed in, and escribed upon, the sides of spherical triangles.

PAGE 79.

$$\tan R = \frac{\tan \frac{1}{2}c}{\sin(C - \frac{1}{2}E)}. \quad [65]$$

$$\tan r = \sqrt{\frac{\sin(s - a) \sin(s - b) \sin(s - c)}{\sin s}}. \quad [66]$$

PAGE 80.

$$\begin{aligned}
 & \tan r' \\
 = \sin s & \sqrt{\frac{\sin(s-b) \sin(s-c)}{\sin s \sin(s-a)}} = \sqrt{\frac{\sin s \sin(s-b) \sin(s-c)}{\sin(s-a)}}, \\
 & \tan r'' \\
 = \sin s & \sqrt{\frac{\sin(s-a) \sin(s-c)}{\sin s \sin(s-b)}} = \sqrt{\frac{\sin s \sin(s-a) \sin(s-c)}{\sin(s-b)}}, \\
 & \tan r''' \\
 = \sin s & \sqrt{\frac{\sin(s-a) \sin(s-b)}{\sin s \sin(s-c)}} = \sqrt{\frac{\sin s \sin(s-a) \sin(s-b)}{\sin(s-c)}}.
 \end{aligned}
 \left. \vphantom{\begin{aligned} \tan r' \\ \tan r'' \\ \tan r''' \end{aligned}} \right\} [67]$$

SIX PLACE
LOGARITHMIC TABLES,

TOGETHER WITH A

TABLE OF NATURAL SINES, COSINES, TANGENTS,
AND COTANGENTS.

PREPARED BY

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INTRODUCTION.



I USE OF THE TABLE OF LOGARITHMS OF NUMBERS.

This table (pages 2 to 16) gives the mantissæ of the logarithms of all numbers of four figures from 1000 to 10000, calculated to six places of decimals.

To find the logarithm of any number of four figures.

Find in the column N. the first three figures of the given number. Then the required mantissa will be found in the corresponding horizontal line, in the vertical column headed by the fourth figure of the number.

If only the last four figures of the mantissa are found, the first two may be obtained from the nearest mantissa above, in the same column, which contains six figures.

Finally, prefix the proper characteristic.

For example, $\log 140.8 = 2.148603$;
 $\log .05837 = 8.766190 - 10$.

For numbers of one, two, or three figures, the column headed 0 may be used ; for $\log 167$ has the same mantissa as $\log 1670$, $\log 8.3$ the same mantissa as $\log 8300$, and $\log .9$ the same mantissa as $\log 9000$; thus,

$\log 167 = 2.222716$, $\log 8.3 = 0.919078$, and $\log .9 = 9.954245 - 10$.

To find the logarithm of a number of more than four figures.

Required the logarithm of 3296.78.

We find from the table, $\log 3296 = 3.517987$;
 $\log 3297 = 3.518119$.

That is, an increase of one unit in the number produces an increase of .000132 in the logarithm.

Then an increase of .78 of a unit in the number will produce an increase of $.78 \times .000132$ in the logarithm, or .000103 to the nearest sixth decimal place.

Whence, $\log 3296.78 = 3.517987 + .000103 = 3.518090$.

Note I. The foregoing method is based on the assumption that the differences of logarithms are proportional to the differences of their corresponding numbers, which, though not strictly accurate, is sufficiently exact for practical purposes.

Note II. The difference between any mantissa in the table and the mantissa of the next higher number of four figures, is called the *tabular difference*.

The following rule is derived from the above :

Find from the table the mantissa of the first four significant figures, and the tabular difference. (See Note III.)

Multiply the latter by the remaining figures of the number with a decimal point before them. (See Note IV.)

Add the result to the mantissa of the first four figures, and prefix the proper characteristic.

Example. Find the logarithm of .002243076.

| | |
|---------------------------|--------------------------|
| Mantissa of 2243 = 350829 | Tabular difference = 194 |
| 15 | .076 |
| 350844 | 1 164 |
| | 13 58 |
| | Correction = 14.744 |
| Result, 7.350844 - 10. | = 15, nearly. |

Note III. The tabular difference may be conveniently found as follows :

Subtract the last figure of the mantissa from the last figure of the next greater, and then take the nearest integer, ending in that figure, to the number in the column D. in the same line.

Thus, in the above example, the last figure of the mantissa of 2243 is 9, and of the next greater mantissa, 3 ; 9 from 13 leaves 4, and the nearest integer, ending in 4, to 193, the number in the column D., is 194, the proper tabular difference.

Note IV. In finding the correction to the nearest unit's figure, the decimal portion may be omitted provided that, if it is greater than .5, the unit's figure is increased by 1.

Thus, 13.26 would be taken as 13 ; 30.5 as 30 ; and 22.503 as 23.

To find the number corresponding to a logarithm.

1. Required the number whose logarithm is 1.693551.

Find in the table the mantissa 693551.

In the corresponding line, in the column N., we find 493, the first three figures of the required number, and at the head of the column we find 8, the fourth figure.

Since the characteristic is 1, there must be two figures to the left of the decimal point.

Whence, number corresponding to 1.693551 = 49.38.

2. Required the number whose logarithm is 3.950185.

We find in the table the mantissa 950170, whose corresponding number is 8916, and the mantissa 950219, whose corresponding number is 8917.

That is, an increase of 49 in the mantissa produces an increase of one unit in the number corresponding.

Then an increase of 15 in the mantissa will produce an increase of $\frac{15}{49}$ of a unit in the number corresponding, or .31 nearly.

Whence, number corresponding = $8916 + .31 = 8916.31$.

The following rule is derived from the above :

Find from the table the next less mantissa, the four figures corresponding, and the tabular difference. (See Note III.)

Subtract the next less mantissa from the given mantissa, and divide the remainder by the tabular difference. (See Note VI.)

Annex the quotient to the first four figures of the number, and point off the result. (See Note V.)

Note V. The rules for pointing off are the reverse of the rules for characteristic ; they may be stated as follows :

I. *If - 10 is not written after the mantissa, add 1 to the characteristic, giving the number of places to the left of the decimal point.*

II. *If - 10 is written after the mantissa, subtract the positive part of the characteristic from 9, giving the number of ciphers to be placed between the decimal point and first significant figure.*

Example. Find the number whose logarithm is 7.427662 - 10.

427662

Next less mantissa = 427648 ; four figures corresponding = 2677.

Tabular difference = 163)14.000(.0858 = .086, nearly.

13 04

960

815

Result, .002677086.

1450

Note VI. The correction can usually be depended upon to as many decimal places as there are figures in the tabular difference ; the division should be carried out to one more place in order to determine the last figure accurately. (See Note IV.)

II. USE OF THE TABLE OF LOGARITHMIC SINES, COSINES, ETC.

This table (pages 18 to 62) gives the logarithms of the sines, cosines, tangents, and cotangents of all angles at intervals of one minute from 0° to 90°.

For angles between 0° and 45° , the degrees will be found at the *top* of the page, the minutes in the *left-hand* column, and the functions in the columns designated by the names at the *top*; that is, sines in the first column, cosines in the second, tangents in the third, and cotangents in the fourth.

For angles between 45° and 90° , the degrees will be found at the *foot* of the page, the minutes in the *right-hand* column, and the functions in the columns designated by the names at the *foot*; that is, cosines in the first column, sines in the second, cotangents in the third, and tangents in the fourth.

The sines and cosines of all acute angles, the tangents of angles between 0° and 45° , and the cotangents of angles between 45° and 90° , being less than unity, the characteristics of their logarithms have been increased by 10, and -10 must be written after their mantissæ; in all other cases, the true value of the characteristic is given in the table.

$$\text{Thus,} \quad \log \sin 38^\circ 37' = 9.795259 - 10;$$

$$\log \tan 66^\circ 20' = 0.358253;$$

$$\log \cot 79^\circ 3' = 9.286624 - 10;$$

$$\log \cos 85^\circ 51' = 8.859546 - 10.$$

To find the logarithmic sine, cosine, tangent, or cotangent of any acute angle expressed in degrees, minutes, and seconds.

Find from the table the logarithmic sine, cosine, tangent, or cotangent of the degrees and minutes, and the difference for $1''$ corresponding. (See Note VII. below.)

Multiply this difference by the number of seconds. (See Note IV.)

If sine or tangent, add } *this correction.*
If cosine or cotangent, subtract }

Note VII. The columns immediately to the right of those headed "Sin.," "Cos.," and "Tan.," contain the respective differences for $1''$; the right-hand column of differences is also to be used with the column headed "Cot."

It will be observed that the differences do not stand in the same horizontal line with the logarithms, but opposite the intervals between consecutive logarithms. With the degrees at the *top* of the page, the difference next *below* should be taken; with the degrees at the *foot* of the page, the difference next *above*.

Note VIII. The rule given above assumes that the differences of the logarithmic functions are proportional to the differences of their corresponding angles, which, unless the angle is very near to 0° or 90° , is in general sufficiently exact for practical purposes. (See page x.)

1. Find $\log \tan 17^\circ 13' 51''$.

| | | |
|--|-----------------|---------------------------------|
| $\log \tan 17^\circ 13' = 9.491180 - 10$ | | $D. 1'' = 7.45$ |
| | <u>380</u> | <u>51</u> |
| Result, | $9.491560 - 10$ | 7.45 |
| | | <u>372.5</u> |
| | | $379.95 = 380, \text{ nearly.}$ |

2. Find $\log \cos 66^\circ 38' 23''$.

| | | |
|--|-----------------|---------------------------------|
| $\log \cos 66^\circ 38' = 9.598368 - 10$ | | $D. 1'' = 4.88$ |
| | <u>112</u> | <u>23</u> |
| Result, | $9.598256 - 10$ | 14.64 |
| | | <u>97.6</u> |
| | | $112.24 = 112, \text{ nearly.}$ |

To find the acute angle corresponding to a given logarithmic sine, cosine, tangent, or cotangent.

Take from the table, if sine or tangent, the next less, if cosine or cotangent, the next greater, logarithmic function, the degrees and minutes corresponding, and the difference for 1". (See Note IX. below.)

Find the difference between the given logarithm and that taken from the table, and divide it by the difference for 1", giving the correction in seconds.

Add the result to the degrees and minutes.

Note IX. In searching for the next less (or greater) logarithm, attention must be paid to the fact that the functions are found in different columns according as the angle is below or above 45° .

If, for example, the next less logarithmic sine is found in the column with "Sin." at the top, the degrees must be taken from the top of the page, and the minutes from the left-hand column; but if it is found in the column with "Sin." at the foot, the degrees must be taken from the foot of the page, and the minutes from the right-hand column. Similar considerations hold with respect to the other three functions.

1. Find the angle whose $\log \sin = 9.959345 - 10$.

| |
|--|
| $9.959345 - 10$ |
| Next less $\log \sin = 9.959310 - 10$; angle corresponding = $65^\circ 35'$. |
| $D. 1'' = .97)35 \quad (36.08 = 36.1, \text{ nearly.}$ |
| <u>291</u> |
| 590 |
| <u>582</u> |
| Result, $65^\circ 35' 36.1''$. <u>800</u> |

2. Find the angle whose $\log \cot = 0.169602$.

Next greater $\log \cot = 0.169651$; angle corresponding = $34^\circ 5'$.

$$\frac{0.169602}{}$$

$$D. 1'' = 4.53)49(10.81 = 10.8, \text{ nearly.}$$

$$\begin{array}{r} 453 \\ \hline 3700 \\ \hline 3624 \\ \hline \end{array}$$

Result, $34^\circ 5' 10.8''$.

$$760$$

Note X. In finding the logarithmic sine of an angle between 85° and 90° , or the logarithmic cosine of an angle between 0° and 5° , it is better to obtain the correction by multiplying the difference between the next less and next greater logarithms by the number of seconds, and dividing the result by 60.

In finding the angle corresponding in the same cases, the correction in seconds may be obtained by multiplying the difference between the given logarithm and that taken from the table by 60, and dividing the result by the difference between the next less and next greater logarithms.

To find the logarithmic secant or cosecant of any acute angle.

Since $\sec x = \frac{1}{\cos x}$ and $\csc x = \frac{1}{\sin x}$, we have

$$\log \sec x = \text{colog } \cos x, \text{ and } \log \csc x = \text{colog } \sin x.$$

Hence, to find the logarithmic secant, subtract the logarithmic cosine from $10 - 10$; and to find the logarithmic cosecant, subtract the logarithmic sine from $10 - 10$.

Example. Find $\log \sec 22^\circ 38'$.

From the table, we find $\log \cos 22^\circ 38' = 9.965195 - 10$.

Subtracting from $10 - 10$, $\log \sec 22^\circ 38' = 0.034805$.

Note XI. The logarithmic cotangent of an angle may be obtained by subtracting the logarithmic tangent from $10 - 10$.

To find the logarithmic functions of an angle not lying between the limits 0° and 90° .

Any function of any angle may be expressed as a function of a certain acute angle; and hence the table of functions of acute angles serves to determine the functions of angles of any magnitude whatever, positive or negative.

Let it be required, for example, to find $\log \sin 152^\circ 16'$.

We have, $\sin 152^\circ 16' = \sin(90^\circ + 62^\circ 16') = \cos 62^\circ 16'$.

Whence, $\log \sin 152^\circ 16' = \log \cos 62^\circ 16' = 9.667786 - 10$.

Or we may proceed as follows :

$$\sin 152^\circ 16' = \sin(180^\circ - 27^\circ 44') = \sin 27^\circ 44'.$$

Note XII. If the natural function is *negative*, as for example in the case of the cosine of an angle between 90° and 180° , there is no logarithmic function, strictly speaking.

In the solution of examples involving such functions, we may proceed as if the functions were positive, and determine the algebraic sign of the result irrespective of the logarithmic work.

III. USE OF THE TABLE OF NATURAL SINES, COSINES, ETC.

This table (pages 64 to 78) gives the natural values of the sines, cosines, tangents, and cotangents of all angles at intervals of $1'$ from 0° to 90° , calculated for sines, cosines, and tangents to five places of decimals, and for cotangents to five significant figures.

Its use is similar to that of the table of logarithmic functions, except that the tabular differences for $1''$ are not given, but are to be calculated from the table when required.

1. Required $\tan 41^\circ 27' 14''$.

$$\tan 41^\circ 27' = .88317.$$

The difference between this and $\tan 41^\circ 28'$ is 52.

Correction for $14'' = \frac{14}{60} \times 52 = 12$, nearly.

$$\begin{array}{r} .88317 \\ \quad 12 \\ \hline \text{Result, } .88329 \end{array}$$

2. Required the angle whose $\cos = .45854$.

Next greater $\cos = .45865$; angle corresponding = $62^\circ 42'$.

$$\begin{array}{r} .45854 \\ \hline 11 \end{array}$$

The difference between $\cos 62^\circ 42'$ and $\cos 62^\circ 43'$ is 26.

Correction in seconds = $\frac{11}{26} \times 60 = 25.4$, nearly.

Result, $62^\circ 42' 25.4''$.

Note XIII. To find a natural function to a greater degree of accuracy than is possible from the table of natural functions, we may find the logarithmic function of the angle, and take the number corresponding to the result.

IV. USE OF THE AUXILIARY TABLE FOR SMALL ANGLES.

This table (page 79) gives the values of the expressions

$$10 + \log \sin x - \log x \text{ and } 10 + \log \tan x - \log x.$$

x being expressed in seconds, for all angles at intervals of $1'$ from 0° to $4^\circ 59'$.

It may be used to find the logarithmic sines or tangents of angles between 0° and 5° , or the angles corresponding in the same cases, to a greater degree of accuracy than is possible from the table of logarithmic functions. (See Note VIII.)

To find the logarithmic sine or tangent of an angle between 0° and 5° .

Find from the auxiliary table the logarithm corresponding to the given function, add to the result the logarithm of the number of seconds in the angle, and write -10 after the mantissa.

Example. Find $\log \tan 0^\circ 43' 37''$.

The logarithms corresponding to $\tan 0^\circ 43'$ and $\tan 0^\circ 44'$ are 4.685597 and 4.685599; the difference between which is 2.

Correction for $37'' = \frac{37}{60} \times 2 = 1$, nearly.

Adding to 4.685597, the result is 4.685598.

The given angle, reduced to seconds, is 2617''.

$$\begin{array}{r} 4.685598 - 10 \\ \log 2617 = 3.417804 \\ \hline \text{Result, } 8.103402 - 10 \end{array}$$

This is correct to the sixth place of decimals; the result by the table of logarithmic tangents is 8.103375 - 10.

To find the angle corresponding to a given logarithmic sine or tangent, when between 0° and 5° .

Find from the table of logarithmic functions the angle corresponding to the given logarithm, to the nearest second.

Take from the auxiliary table the logarithm corresponding to this angle.

Subtract the result from the given logarithm, and find the number corresponding to the difference, giving the required angle in seconds.

Example. Find the angle whose $\log \sin = 7.632366 - 10$.

The angle corresponding is $0^\circ 14' 45''$, to the nearest second.

The logarithm corresponding to $\sin 0^\circ 14' 45''$ is $4.685573 - 10$.

$$7.632366 - 10$$

$$\underline{4.685573 - 10}$$

$$2.946793$$

The number corresponding to this logarithm is 884.69.

Then the required angle is $884.69''$, or $0^\circ 14' 44.69''$.

This is correct to the second decimal place of seconds; the result by the table of logarithmic sines is $0^\circ 14' 45.08''$.

Note XIV. The above methods serve to determine with accuracy the logarithmic cosine or cotangent of an angle between 85° and 90° , or the angle corresponding in the same cases.

To find accurately the logarithmic tangent of an angle between 85° and 90° , find the logarithmic cotangent of the angle as above, and subtract the result from $10 - 10$. (Note XI.)

To find the angle corresponding to a logarithmic tangent in the same case, find the logarithmic cotangent of the angle (Note XI), and find the angle corresponding to the result.

These methods also serve to determine the logarithmic cotangent of an angle between 0° and 5° , or the angle corresponding in the same case.

A TABLE

CONTAINING THE

LOGARITHMS OF NUMBERS

FROM 1 TO 10,000.

| N. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | D. |
|-----|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|-----|
| 100 | 00 0000 | 00 0434 | 00 0868 | 00 1301 | 00 1734 | 00 2166 | 00 2598 | 00 3029 | 00 3461 | 00 3891 | 432 |
| 101 | 4321 | 4751 | 5181 | 5609 | 6038 | 6466 | 6894 | 7321 | 7748 | 8174 | 428 |
| 102 | 8600 | 9026 | 9451 | 9876 | 01 0300 | 01 0724 | 01 1147 | 01 1570 | 01 1993 | 01 2415 | 424 |
| 103 | 01 2837 | 01 3259 | 01 3680 | 01 4100 | 4521 | 4940 | 5360 | 5779 | 6197 | 6616 | 420 |
| 104 | 7033 | 7451 | 7868 | 8284 | 8700 | 9116 | 9532 | 9947 | 02 0361 | 02 0775 | 416 |
| 105 | 02 1189 | 02 1603 | 02 2016 | 02 2428 | 02 2841 | 02 3252 | 02 3664 | 02 4075 | 02 4486 | 02 4896 | 412 |
| 106 | 5306 | 5715 | 6125 | 6533 | 6942 | 7350 | 7757 | 8164 | 8571 | 8978 | 408 |
| 107 | 9384 | 9789 | 03 0193 | 03 0600 | 03 1004 | 03 1408 | 03 1812 | 03 2216 | 03 2619 | 03 3021 | 404 |
| 108 | 03 3424 | 03 3826 | 4227 | 4628 | 5029 | 5430 | 5830 | 6230 | 6629 | 7028 | 400 |
| 109 | 7426 | 7825 | 8223 | 8620 | 9017 | 9414 | 9811 | 04 0207 | 04 0602 | 04 0998 | 397 |
| 110 | 04 1393 | 04 1787 | 04 2182 | 04 2576 | 04 2969 | 04 3362 | 04 3755 | 04 4148 | 04 4540 | 04 4932 | 393 |
| 111 | 5323 | 5714 | 6105 | 6495 | 6885 | 7275 | 7664 | 8053 | 8442 | 8830 | 390 |
| 112 | 9218 | 9606 | 9993 | 05 0380 | 05 0766 | 05 1153 | 05 1538 | 05 1924 | 05 2309 | 05 2694 | 386 |
| 113 | 05 3078 | 05 3463 | 05 3846 | 4230 | 4613 | 4996 | 5378 | 5760 | 6142 | 6524 | 383 |
| 114 | 6905 | 7286 | 7666 | 8046 | 8426 | 8805 | 9185 | 9563 | 9942 | 06 0320 | 379 |
| 115 | 06 0698 | 06 1075 | 06 1452 | 06 1829 | 06 2206 | 06 2582 | 06 2958 | 06 3333 | 06 3709 | 06 4083 | 376 |
| 116 | 4458 | 4832 | 5206 | 5580 | 5953 | 6326 | 6699 | 7071 | 7443 | 7815 | 373 |
| 117 | 8186 | 8557 | 8928 | 9298 | 9668 | 07 0038 | 07 0407 | 07 0776 | 07 1145 | 07 1514 | 370 |
| 118 | 07 1882 | 07 2250 | 07 2617 | 07 2985 | 07 3352 | 3718 | 4085 | 4451 | 4816 | 5182 | 366 |
| 119 | 5547 | 5912 | 6276 | 6640 | 7004 | 7368 | 7731 | 8094 | 8457 | 8819 | 363 |
| 120 | 07 9181 | 07 9543 | 07 9904 | 08 0266 | 08 0626 | 08 0987 | 08 1347 | 08 1707 | 08 2067 | 08 2426 | 360 |
| 121 | 08 2785 | 08 3144 | 08 3503 | 3861 | 4219 | 4570 | 4934 | 5291 | 5647 | 6004 | 357 |
| 122 | 6360 | 6716 | 7071 | 7426 | 7781 | 8136 | 8490 | 8845 | 9198 | 9552 | 355 |
| 123 | 9905 | 09 0258 | 09 0611 | 09 0963 | 09 1315 | 09 1667 | 09 2018 | 09 2370 | 09 2721 | 09 3071 | 352 |
| 124 | 09 3422 | 3772 | 4122 | 4471 | 4820 | 5169 | 5518 | 5866 | 6215 | 6562 | 349 |
| 125 | 09 6910 | 09 7257 | 09 7604 | 09 7951 | 09 8298 | 09 8644 | 09 8990 | 09 9335 | 09 9681 | 10 0026 | 346 |
| 126 | 10 0371 | 10 0715 | 10 1059 | 10 1403 | 10 1747 | 10 2091 | 10 2434 | 10 2777 | 10 3119 | 3462 | 343 |
| 127 | 3804 | 4146 | 4487 | 4828 | 5169 | 5510 | 5851 | 6191 | 6531 | 6871 | 341 |
| 128 | 7210 | 7549 | 7888 | 8227 | 8565 | 8903 | 9241 | 9579 | 9916 | 11 0253 | 338 |
| 129 | 11 0590 | 11 0926 | 11 1263 | 11 1599 | 11 1934 | 11 2270 | 11 2605 | 11 2940 | 11 3275 | 3609 | 335 |
| 130 | 11 3943 | 11 4277 | 11 4611 | 11 4944 | 11 5278 | 11 5611 | 11 5943 | 11 6276 | 11 6608 | 11 6940 | 333 |
| 131 | 7271 | 7603 | 7934 | 8265 | 8595 | 8926 | 9256 | 9586 | 9915 | 12 0245 | 330 |
| 132 | 12 0574 | 12 0903 | 12 1231 | 12 1560 | 12 1888 | 12 2216 | 12 2544 | 12 2871 | 12 3198 | 3525 | 328 |
| 133 | 3852 | 4178 | 4504 | 4830 | 5156 | 5481 | 5806 | 6131 | 6456 | 6781 | 325 |
| 134 | 7105 | 7429 | 7753 | 8076 | 8399 | 8722 | 9045 | 9368 | 9690 | 13 0012 | 323 |
| 135 | 13 0334 | 13 0655 | 13 0977 | 13 1298 | 13 1619 | 13 1939 | 13 2260 | 13 2580 | 13 2900 | 13 3219 | 321 |
| 136 | 3539 | 3858 | 4177 | 4496 | 4814 | 5133 | 5451 | 5769 | 6086 | 6403 | 318 |
| 137 | 6721 | 7037 | 7354 | 7671 | 7987 | 8303 | 8618 | 8934 | 9249 | 9564 | 316 |
| 138 | 9879 | 14 0194 | 14 0508 | 14 0822 | 14 1136 | 14 1450 | 14 1763 | 14 2076 | 14 2389 | 14 2702 | 314 |
| 139 | 14 3015 | 3327 | 3639 | 3951 | 4263 | 4574 | 4885 | 5196 | 5507 | 5818 | 311 |
| 140 | 14 6128 | 14 6438 | 14 6748 | 14 7058 | 14 7367 | 14 7676 | 14 7985 | 14 8294 | 14 8603 | 14 8911 | 309 |
| 141 | 9219 | 9527 | 9835 | 15 0142 | 15 0449 | 15 0756 | 15 1063 | 15 1370 | 15 1676 | 15 1982 | 307 |
| 142 | 15 2288 | 15 2594 | 15 2900 | 3205 | 3510 | 3815 | 4120 | 4424 | 4728 | 5032 | 305 |
| 143 | 5336 | 5640 | 5943 | 6246 | 6549 | 6852 | 7154 | 7457 | 7759 | 8061 | 303 |
| 144 | 8362 | 8664 | 8965 | 9266 | 9567 | 9868 | 16 0168 | 16 0469 | 16 0769 | 16 1068 | 301 |
| 145 | 16 1368 | 16 1667 | 16 1967 | 16 2266 | 16 2564 | 16 2863 | 16 3161 | 16 3460 | 16 3758 | 16 4055 | 299 |
| 146 | 4353 | 4650 | 4947 | 5244 | 5541 | 5838 | 6134 | 6430 | 6726 | 7022 | 297 |
| 147 | 7317 | 7613 | 7908 | 8203 | 8497 | 8792 | 9086 | 9380 | 9674 | 9968 | 295 |
| 148 | 17 0262 | 17 0555 | 17 0848 | 17 1141 | 17 1434 | 17 1726 | 17 2019 | 17 2311 | 17 2603 | 17 2895 | 293 |
| 149 | 3186 | 3478 | 3769 | 4060 | 4351 | 4641 | 4932 | 5222 | 5512 | 5802 | 291 |
| 150 | 17 6091 | 17 6381 | 17 6670 | 17 6959 | 17 7248 | 17 7536 | 17 7825 | 17 8113 | 17 8401 | 17 8689 | 289 |
| 151 | 8977 | 9264 | 9552 | 9839 | 18 0126 | 18 0413 | 18 0699 | 18 0986 | 18 1272 | 18 1558 | 287 |
| 152 | 18 1844 | 18 2129 | 18 2415 | 18 2700 | 2985 | 3270 | 3555 | 3839 | 4123 | 4407 | 285 |
| 153 | 4691 | 4975 | 5259 | 5542 | 5825 | 6108 | 6391 | 6674 | 6956 | 7239 | 283 |
| 154 | 7521 | 7803 | 8084 | 8366 | 8647 | 8928 | 9209 | 9490 | 9771 | 19 0051 | 281 |
| 155 | 19 0332 | 19 0612 | 19 0892 | 19 1171 | 19 1451 | 19 1730 | 19 2010 | 19 2289 | 19 2567 | 19 2846 | 279 |
| 156 | 3125 | 3403 | 3681 | 3959 | 4237 | 4514 | 4792 | 5069 | 5346 | 5623 | 278 |
| 157 | 5900 | 6176 | 6453 | 6729 | 7005 | 7281 | 7556 | 7832 | 8107 | 8382 | 276 |
| 158 | 8657 | 8932 | 9206 | 9481 | 9755 | 20 0029 | 20 0303 | 20 0577 | 20 0850 | 20 1124 | 274 |
| 159 | 20 1397 | 20 1670 | 20 1943 | 20 2216 | 20 2488 | 2761 | 3033 | 3305 | 3577 | 3848 | 272 |
| N. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | D. |

| N. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | D. |
|-----|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|-----|
| 160 | 20 4120 | 20 4391 | 20 4663 | 20 4934 | 20 5204 | 20 5475 | 20 5746 | 20 6016 | 20 6286 | 20 6556 | 271 |
| 161 | 6826 | 7096 | 7365 | 7634 | 7904 | 8173 | 8441 | 8710 | 8979 | 9247 | 269 |
| 162 | 9515 | 9783 | 21 0051 | 21 0319 | 21 0586 | 21 0853 | 21 1121 | 21 1388 | 21 1654 | 21 1921 | 267 |
| 163 | 21 2188 | 21 2454 | 2720 | 2986 | 3252 | 3518 | 3783 | 4049 | 4314 | 4579 | 266 |
| 164 | 4844 | 5109 | 5373 | 5638 | 5902 | 6166 | 6430 | 6694 | 6957 | 7221 | 264 |
| 165 | 21 7484 | 21 7747 | 21 8010 | 21 8273 | 21 8536 | 21 8798 | 21 9060 | 21 9323 | 21 9585 | 21 9846 | 262 |
| 166 | 22 0108 | 22 0370 | 22 0631 | 22 0892 | 22 1153 | 22 1414 | 22 1675 | 22 1936 | 22 2196 | 22 2456 | 261 |
| 167 | 2716 | 2976 | 3236 | 3496 | 3755 | 4015 | 4274 | 4533 | 4792 | 5051 | 259 |
| 168 | 5309 | 5568 | 5826 | 6084 | 6342 | 6600 | 6858 | 7115 | 7372 | 7630 | 258 |
| 169 | 7887 | 8144 | 8400 | 8657 | 8913 | 9170 | 9426 | 9682 | 9938 | 23 0193 | 256 |
| 170 | 23 0449 | 23 0704 | 23 0960 | 23 1215 | 23 1470 | 23 1724 | 23 1979 | 23 2234 | 23 2488 | 23 2742 | 255 |
| 171 | 2996 | 3250 | 3504 | 3757 | 4011 | 4264 | 4517 | 4770 | 5023 | 5276 | 253 |
| 172 | 5528 | 5781 | 6033 | 6285 | 6537 | 6789 | 7041 | 7292 | 7544 | 7795 | 252 |
| 173 | 8046 | 8297 | 8548 | 8799 | 9049 | 9299 | 9550 | 9800 | 24 0050 | 24 0300 | 250 |
| 174 | 24 0549 | 24 0799 | 24 1048 | 24 1297 | 24 1546 | 24 1795 | 24 2044 | 24 2293 | 2541 | 2790 | 249 |
| 175 | 24 3038 | 24 3286 | 24 3534 | 24 3782 | 24 4030 | 24 4277 | 24 4525 | 24 4772 | 24 5019 | 24 5266 | 248 |
| 176 | 5513 | 5759 | 6006 | 6252 | 6499 | 6745 | 6991 | 7237 | 7482 | 7728 | 246 |
| 177 | 7973 | 8219 | 8464 | 8709 | 8954 | 9198 | 9443 | 9687 | 9932 | 25 0176 | 245 |
| 178 | 25 0420 | 25 0664 | 25 0908 | 25 1151 | 25 1395 | 25 1638 | 25 1881 | 25 2125 | 25 2368 | 2610 | 243 |
| 179 | 2853 | 3096 | 3338 | 3580 | 3822 | 4064 | 4306 | 4548 | 4790 | 5031 | 242 |
| 180 | 25 5273 | 25 5514 | 25 5755 | 25 5996 | 25 6237 | 25 6477 | 25 6718 | 25 6958 | 25 7198 | 25 7439 | 241 |
| 181 | 7679 | 7918 | 8158 | 8398 | 8637 | 8877 | 9116 | 9355 | 9594 | 9833 | 239 |
| 182 | 26 0071 | 26 0310 | 26 0548 | 26 0787 | 26 1025 | 26 1263 | 26 1501 | 26 1739 | 26 1976 | 26 2214 | 238 |
| 183 | 2451 | 2688 | 2925 | 3162 | 3399 | 3636 | 3873 | 4109 | 4346 | 4582 | 237 |
| 184 | 4818 | 5054 | 5290 | 5525 | 5761 | 5996 | 6232 | 6467 | 6702 | 6937 | 235 |
| 185 | 26 7172 | 26 7406 | 26 7641 | 26 7875 | 26 8110 | 26 8344 | 26 8578 | 26 8812 | 26 9046 | 26 9279 | 234 |
| 186 | 9513 | 9746 | 9980 | 27 0213 | 27 0446 | 27 0679 | 27 0912 | 27 1144 | 27 1377 | 27 1609 | 233 |
| 187 | 27 1842 | 27 2074 | 27 2306 | 2538 | 2770 | 3001 | 3233 | 3464 | 3696 | 3927 | 232 |
| 188 | 4158 | 4389 | 4620 | 4850 | 5081 | 5311 | 5542 | 5772 | 6002 | 6232 | 230 |
| 189 | 6462 | 6692 | 6921 | 7151 | 7380 | 7609 | 7838 | 8067 | 8296 | 8525 | 229 |
| 190 | 27 8754 | 27 8982 | 27 9211 | 27 9439 | 27 9667 | 27 9895 | 28 0123 | 28 0351 | 28 0578 | 28 0806 | 228 |
| 191 | 28 1033 | 28 1261 | 28 1488 | 28 1715 | 28 1942 | 28 2169 | 2396 | 2622 | 2849 | 3075 | 227 |
| 192 | 3301 | 3527 | 3753 | 3979 | 4205 | 4431 | 4656 | 4882 | 5107 | 5332 | 226 |
| 193 | 5557 | 5782 | 6007 | 6232 | 6456 | 6681 | 6905 | 7130 | 7354 | 7578 | 225 |
| 194 | 7802 | 8026 | 8249 | 8473 | 8696 | 8920 | 9143 | 9366 | 9589 | 9812 | 223 |
| 195 | 29 0035 | 29 0257 | 29 0480 | 29 0702 | 29 0925 | 29 1147 | 29 1369 | 29 1591 | 29 1813 | 29 2034 | 222 |
| 196 | 2256 | 2478 | 2699 | 2920 | 3141 | 3363 | 3584 | 3804 | 4025 | 4246 | 221 |
| 197 | 4466 | 4687 | 4907 | 5127 | 5347 | 5567 | 5787 | 6007 | 6226 | 6446 | 220 |
| 198 | 6665 | 6884 | 7104 | 7323 | 7542 | 7761 | 7979 | 8198 | 8416 | 8635 | 219 |
| 199 | 8853 | 9071 | 9289 | 9507 | 9725 | 9943 | 30 0161 | 30 0378 | 30 0595 | 30 0813 | 218 |
| 200 | 30 1030 | 30 1247 | 30 1464 | 30 1681 | 30 1898 | 30 2114 | 30 2331 | 30 2547 | 30 2764 | 30 2980 | 217 |
| 201 | 3196 | 3412 | 3628 | 3844 | 4059 | 4275 | 4491 | 4706 | 4921 | 5136 | 216 |
| 202 | 5351 | 5566 | 5781 | 5996 | 6211 | 6425 | 6639 | 6854 | 7068 | 7282 | 215 |
| 203 | 7496 | 7710 | 7924 | 8137 | 8351 | 8564 | 8778 | 8991 | 9204 | 9417 | 213 |
| 204 | 9630 | 9843 | 31 0056 | 31 0268 | 31 0481 | 31 0693 | 31 0906 | 31 1118 | 31 1330 | 31 1542 | 212 |
| 205 | 31 1754 | 31 1966 | 31 2177 | 31 2389 | 31 2600 | 31 2812 | 31 3023 | 31 3234 | 31 3445 | 31 3656 | 211 |
| 206 | 3867 | 4078 | 4289 | 4499 | 4710 | 4920 | 5130 | 5340 | 5551 | 5760 | 210 |
| 207 | 5970 | 6180 | 6390 | 6599 | 6809 | 7018 | 7227 | 7436 | 7646 | 7854 | 209 |
| 208 | 8063 | 8272 | 8481 | 8689 | 8898 | 9106 | 9314 | 9522 | 9730 | 9938 | 208 |
| 209 | 32 0146 | 32 0354 | 32 0562 | 32 0769 | 32 0977 | 32 1184 | 32 1391 | 32 1598 | 32 1805 | 32 2012 | 207 |
| 210 | 32 2219 | 32 2426 | 32 2633 | 32 2839 | 32 3046 | 32 3252 | 32 3458 | 32 3665 | 32 3871 | 32 4077 | 206 |
| 211 | 4282 | 4488 | 4694 | 4899 | 5105 | 5310 | 5516 | 5721 | 5926 | 6131 | 205 |
| 212 | 6336 | 6541 | 6745 | 6950 | 7155 | 7359 | 7563 | 7767 | 7972 | 8176 | 204 |
| 213 | 8380 | 8583 | 8787 | 8991 | 9194 | 9398 | 9601 | 9805 | 33 0008 | 33 0211 | 203 |
| 214 | 33 0414 | 33 0617 | 33 0819 | 33 1022 | 33 1225 | 33 1427 | 33 1630 | 33 1832 | 2034 | 2236 | 202 |
| 215 | 33 2438 | 33 2640 | 33 2842 | 33 3044 | 33 3246 | 33 3447 | 33 3649 | 33 3850 | 33 4051 | 33 4253 | 202 |
| 216 | 4454 | 4655 | 4856 | 5057 | 5257 | 5458 | 5658 | 5859 | 6059 | 6260 | 201 |
| 217 | 6460 | 6660 | 6860 | 7060 | 7260 | 7459 | 7659 | 7858 | 8058 | 8257 | 200 |
| 218 | 8465 | 8665 | 8865 | 9064 | 9263 | 9461 | 9659 | 9858 | 34 0047 | 34 0246 | 199 |
| 219 | 34 0444 | 34 0642 | 34 0841 | 34 1039 | 34 1237 | 34 1435 | 34 1632 | 34 1830 | 2028 | 2225 | 198 |
| N. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | D. |

| N. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | D. |
|-----|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|-----|
| 220 | 34 2423 | 34 2620 | 34 2817 | 34 3014 | 34 3212 | 34 3409 | 34 3606 | 34 3802 | 34 3999 | 34 4196 | 197 |
| 221 | 4392 | 4589 | 4785 | 4981 | 5178 | 5374 | 5570 | 5766 | 5962 | 6157 | 196 |
| 222 | 6353 | 6549 | 6744 | 6939 | 7135 | 7330 | 7525 | 7720 | 7915 | 8110 | 195 |
| 223 | 8305 | 8500 | 8694 | 8889 | 9083 | 9278 | 9472 | 9666 | 9860 | 35 0054 | 194 |
| 224 | 35 0248 | 35 0442 | 35 0636 | 35 0829 | 35 1023 | 35 1216 | 35 1410 | 35 1603 | 35 1796 | 1989 | 193 |
| 225 | 35 2183 | 35 2375 | 35 2568 | 35 2761 | 35 2954 | 35 3147 | 35 3339 | 35 3532 | 35 3724 | 35 3916 | 193 |
| 226 | 4108 | 4301 | 4493 | 4685 | 4876 | 5068 | 5260 | 5452 | 5643 | 5834 | 192 |
| 227 | 6026 | 6217 | 6408 | 6599 | 6790 | 6981 | 7172 | 7363 | 7554 | 7744 | 191 |
| 228 | 7935 | 8125 | 8316 | 8506 | 8696 | 8886 | 9076 | 9266 | 9456 | 9646 | 190 |
| 229 | 9835 | 36 0025 | 36 0215 | 36 0404 | 36 0593 | 36 0783 | 36 0972 | 36 1161 | 36 1350 | 36 1539 | 189 |
| 230 | 36 1728 | 36 1917 | 36 2105 | 36 2294 | 36 2482 | 36 2671 | 36 2859 | 36 3048 | 36 3236 | 36 3424 | 188 |
| 231 | 3612 | 3800 | 3988 | 4176 | 4363 | 4551 | 4739 | 4926 | 5113 | 5301 | 188 |
| 232 | 5488 | 5675 | 5862 | 6049 | 6236 | 6423 | 6610 | 6796 | 6983 | 7169 | 187 |
| 233 | 7356 | 7542 | 7729 | 7915 | 8101 | 8287 | 8473 | 8659 | 8845 | 9030 | 186 |
| 234 | 9216 | 9401 | 9587 | 9772 | 9958 | 37 0143 | 37 0328 | 37 0513 | 37 0698 | 37 0883 | 185 |
| 235 | 37 1068 | 37 1253 | 37 1437 | 37 1622 | 37 1806 | 37 1991 | 37 2175 | 37 2360 | 37 2544 | 37 2728 | 184 |
| 236 | 2912 | 3096 | 3280 | 3464 | 3647 | 3831 | 4015 | 4198 | 4382 | 4565 | 184 |
| 237 | 4748 | 4932 | 5115 | 5298 | 5481 | 5664 | 5846 | 6029 | 6212 | 6394 | 183 |
| 238 | 6577 | 6759 | 6942 | 7124 | 7306 | 7488 | 7670 | 7852 | 8034 | 8216 | 182 |
| 239 | 8398 | 8580 | 8761 | 8943 | 9124 | 9306 | 9487 | 9668 | 9849 | 38 0030 | 181 |
| 240 | 38 0211 | 38 0392 | 38 0573 | 38 0754 | 38 0934 | 38 1115 | 38 1296 | 38 1476 | 38 1656 | 38 1837 | 181 |
| 241 | 2017 | 2197 | 2377 | 2557 | 2737 | 2917 | 3097 | 3277 | 3456 | 3636 | 180 |
| 242 | 3815 | 3995 | 4174 | 4353 | 4533 | 4712 | 4891 | 5070 | 5249 | 5428 | 179 |
| 243 | 5606 | 5785 | 5964 | 6142 | 6321 | 6499 | 6677 | 6856 | 7034 | 7212 | 178 |
| 244 | 7390 | 7568 | 7746 | 7923 | 8101 | 8279 | 8456 | 8634 | 8811 | 8989 | 178 |
| 245 | 38 9166 | 38 9343 | 38 9520 | 38 9698 | 38 9875 | 39 0051 | 39 0228 | 39 0405 | 39 0582 | 39 0759 | 177 |
| 246 | 39 0935 | 39 1112 | 39 1288 | 39 1464 | 39 1641 | 1817 | 1993 | 2169 | 2345 | 2521 | 176 |
| 247 | 2697 | 2873 | 3048 | 3224 | 3400 | 3575 | 3751 | 3926 | 4101 | 4277 | 176 |
| 248 | 4452 | 4627 | 4802 | 4977 | 5152 | 5326 | 5501 | 5676 | 5850 | 6025 | 175 |
| 249 | 6199 | 6374 | 6548 | 6722 | 6896 | 7071 | 7245 | 7419 | 7592 | 7766 | 174 |
| 250 | 39 7940 | 39 8114 | 39 8287 | 39 8461 | 39 8634 | 39 8808 | 39 8981 | 39 9154 | 39 9328 | 39 9501 | 173 |
| 251 | 9674 | 9847 | 40 0020 | 40 0192 | 40 0365 | 40 0538 | 40 0711 | 40 0883 | 40 1056 | 40 1228 | 173 |
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| 253 | 3121 | 3292 | 3464 | 3635 | 3807 | 3978 | 4149 | 4320 | 4492 | 4663 | 171 |
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| 255 | 40 6540 | 40 6710 | 40 6881 | 40 7051 | 40 7221 | 40 7391 | 40 7561 | 40 7731 | 40 7901 | 40 8070 | 170 |
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| 257 | 9933 | 41 0102 | 41 0271 | 41 0440 | 41 0609 | 41 0777 | 41 0946 | 41 1114 | 41 1283 | 41 1451 | 169 |
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| 260 | 41 4973 | 41 5140 | 41 5307 | 41 5474 | 41 5641 | 41 5808 | 41 5974 | 41 6141 | 41 6308 | 41 6474 | 167 |
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| 263 | 9956 | 42 0121 | 42 0286 | 42 0451 | 42 0616 | 42 0781 | 42 0945 | 42 1110 | 42 1275 | 42 1439 | 165 |
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| 274 | 7751 | 7909 | 8068 | 8226 | 8384 | 8542 | 8701 | 8859 | 9017 | 9175 | 158 |
| 275 | 43 9333 | 43 9491 | 43 9648 | 43 9806 | 43 9964 | 44 0122 | 44 0279 | 44 0437 | 44 0594 | 44 0752 | 158 |
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| 309 | 9958 | 49 0099 | 49 0239 | 49 0380 | 49 0520 | 49 0661 | 49 0801 | 49 0941 | 49 1081 | 49 1222 | 140 |
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| 313 | 5544 | 5683 | 5822 | 5960 | 6099 | 6238 | 6376 | 6515 | 6653 | 6791 | 139 |
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| 356 | 1450 | 1572 | 1694 | 1816 | 1938 | 2060 | 2181 | 2303 | 2425 | 2547 | 122 |
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| 442 | 5422 | 5521 | 5619 | 5717 | 5815 | 5913 | 6011 | 6110 | 6208 | 6306 | 98 |
| 443 | 6404 | 6502 | 6600 | 6698 | 6796 | 6894 | 6992 | 7089 | 7187 | 7285 | 98 |
| 444 | 7383 | 7481 | 7579 | 7676 | 7774 | 7872 | 7969 | 8067 | 8165 | 8262 | 98 |
| 445 | 64 8360 | 64 8458 | 64 8555 | 64 8653 | 64 8750 | 64 8848 | 64 8945 | 64 9043 | 64 9140 | 64 9237 | 97 |
| 446 | 9335 | 9432 | 9530 | 9627 | 9724 | 9821 | 9919 | 65 0016 | 65 0113 | 65 0210 | 97 |
| 447 | 65 0308 | 65 0405 | 65 0502 | 65 0599 | 65 0696 | 65 0793 | 65 0890 | 0987 | 1084 | 1181 | 97 |
| 448 | 1278 | 1375 | 1472 | 1569 | 1666 | 1762 | 1859 | 1956 | 2053 | 2150 | 97 |
| 449 | 2246 | 2343 | 2440 | 2536 | 2633 | 2730 | 2826 | 2923 | 3019 | 3116 | 97 |
| 450 | 65 3213 | 65 3309 | 65 3405 | 65 3502 | 65 3598 | 65 3695 | 65 3791 | 65 3888 | 65 3984 | 65 4080 | 96 |
| 451 | 4177 | 4273 | 4369 | 4465 | 4562 | 4658 | 4754 | 4850 | 4946 | 5042 | 96 |
| 452 | 5138 | 5235 | 5331 | 5427 | 5523 | 5619 | 5715 | 5810 | 5906 | 6002 | 96 |
| 453 | 6098 | 6194 | 6290 | 6386 | 6482 | 6577 | 6673 | 6769 | 6864 | 6960 | 96 |
| 454 | 7056 | 7152 | 7247 | 7343 | 7438 | 7534 | 7629 | 7725 | 7820 | 7916 | 96 |
| 455 | 65 8011 | 65 8107 | 65 8202 | 65 8298 | 65 8393 | 65 8488 | 65 8584 | 65 8679 | 65 8774 | 65 8870 | 95 |
| 456 | 8965 | 9060 | 9155 | 9250 | 9346 | 9441 | 9536 | 9631 | 9726 | 9821 | 95 |
| 457 | 9916 | 66 0011 | 66 0106 | 66 0201 | 66 0296 | 66 0391 | 66 0486 | 66 0581 | 66 0676 | 66 0771 | 95 |
| 458 | 66 0865 | 0960 | 1055 | 1150 | 1245 | 1339 | 1434 | 1529 | 1623 | 1718 | 95 |
| 459 | 1813 | 1907 | 2002 | 2096 | 2191 | 2286 | 2380 | 2475 | 2569 | 2663 | 95 |
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| 460 | 66 2758 | 66 2852 | 66 2947 | 66 3041 | 66 3135 | 66 3230 | 66 3324 | 66 3418 | 66 3512 | 66 3607 | 94 |
| 461 | 3701 | 3795 | 3889 | 3983 | 4078 | 4172 | 4266 | 4360 | 4454 | 4548 | 94 |
| 462 | 4642 | 4736 | 4830 | 4924 | 5018 | 5112 | 5206 | 5299 | 5393 | 5487 | 94 |
| 463 | 5581 | 5675 | 5769 | 5862 | 5956 | 6050 | 6143 | 6237 | 6331 | 6424 | 94 |
| 464 | 6518 | 6612 | 6705 | 6799 | 6892 | 6986 | 7079 | 7173 | 7266 | 7360 | 94 |
| 465 | 66 7453 | 66 7546 | 66 7640 | 66 7733 | 66 7826 | 66 7920 | 66 8013 | 66 8106 | 66 8199 | 66 8293 | 93 |
| 466 | 8386 | 8479 | 8572 | 8665 | 8759 | 8852 | 8945 | 9038 | 9131 | 9224 | 93 |
| 467 | 9317 | 9410 | 9503 | 9596 | 9689 | 9782 | 9875 | 9967 | 67 0060 | 67 0153 | 93 |
| 468 | 67 0246 | 67 0339 | 67 0431 | 67 0524 | 67 0617 | 67 0710 | 67 0802 | 67 0895 | 0988 | 1080 | 93 |
| 469 | 1173 | 1265 | 1358 | 1451 | 1543 | 1636 | 1728 | 1821 | 1913 | 2005 | 93 |
| 470 | 67 2098 | 67 2190 | 67 2283 | 67 2375 | 67 2467 | 67 2560 | 67 2652 | 67 2744 | 67 2836 | 67 2929 | 92 |
| 471 | 3021 | 3113 | 3205 | 3297 | 3390 | 3482 | 3574 | 3666 | 3758 | 3850 | 92 |
| 472 | 3942 | 4034 | 4126 | 4218 | 4310 | 4402 | 4494 | 4586 | 4677 | 4769 | 92 |
| 473 | 4861 | 4953 | 5045 | 5137 | 5228 | 5320 | 5412 | 5503 | 5595 | 5687 | 92 |
| 474 | 5778 | 5870 | 5962 | 6053 | 6145 | 6236 | 6328 | 6419 | 6511 | 6602 | 92 |
| 475 | 67 6694 | 67 6785 | 67 6876 | 67 6968 | 67 7059 | 67 7151 | 67 7242 | 67 7333 | 67 7424 | 67 7516 | 91 |
| 476 | 7607 | 7698 | 7789 | 7881 | 7972 | 8063 | 8154 | 8245 | 8336 | 8427 | 91 |
| 477 | 8518 | 8609 | 8700 | 8791 | 8882 | 8973 | 9064 | 9155 | 9246 | 9337 | 91 |
| 478 | 9428 | 9519 | 9610 | 9700 | 9791 | 9882 | 9973 | 68 0063 | 68 0154 | 68 0245 | 91 |
| 479 | 68 0336 | 68 0426 | 68 0517 | 68 0607 | 68 0698 | 68 0789 | 68 0879 | 68 0970 | 1060 | 1151 | 91 |
| 480 | 68 1241 | 68 1332 | 68 1422 | 68 1513 | 68 1603 | 68 1693 | 68 1784 | 68 1874 | 68 1964 | 68 2055 | 90 |
| 481 | 2145 | 2235 | 2326 | 2416 | 2506 | 2596 | 2686 | 2777 | 2867 | 2957 | 90 |
| 482 | 3047 | 3137 | 3227 | 3317 | 3407 | 3497 | 3587 | 3677 | 3767 | 3857 | 90 |
| 483 | 3947 | 4037 | 4127 | 4217 | 4307 | 4396 | 4486 | 4576 | 4666 | 4756 | 90 |
| 484 | 4845 | 4935 | 5025 | 5114 | 5204 | 5294 | 5383 | 5473 | 5563 | 5652 | 90 |
| 485 | 68 5742 | 68 5831 | 68 5921 | 68 6010 | 68 6100 | 68 6189 | 68 6279 | 68 6368 | 68 6458 | 68 6547 | 89 |
| 486 | 6636 | 6726 | 6815 | 6904 | 6994 | 7083 | 7172 | 7261 | 7351 | 7440 | 89 |
| 487 | 7529 | 7618 | 7707 | 7796 | 7886 | 7975 | 8064 | 8153 | 8242 | 8331 | 89 |
| 488 | 8420 | 8509 | 8598 | 8687 | 8776 | 8865 | 8953 | 9042 | 9131 | 9220 | 89 |
| 489 | 9309 | 9398 | 9486 | 9575 | 9664 | 9753 | 9841 | 9930 | 69 0019 | 69 0107 | 89 |
| 490 | 69 0196 | 69 0285 | 69 0373 | 69 0462 | 69 0550 | 69 0639 | 69 0728 | 69 0816 | 69 0905 | 69 0993 | 89 |
| 491 | 1081 | 1170 | 1258 | 1347 | 1435 | 1524 | 1612 | 1700 | 1789 | 1877 | 88 |
| 492 | 1965 | 2053 | 2142 | 2230 | 2318 | 2406 | 2494 | 2583 | 2671 | 2759 | 88 |
| 493 | 2847 | 2935 | 3023 | 3111 | 3199 | 3287 | 3375 | 3463 | 3551 | 3639 | 88 |
| 494 | 3727 | 3815 | 3903 | 3991 | 4078 | 4166 | 4254 | 4342 | 4430 | 4517 | 88 |
| 495 | 69 4605 | 69 4693 | 69 4781 | 69 4868 | 69 4956 | 69 5044 | 69 5131 | 69 5219 | 69 5307 | 69 5394 | 88 |
| 496 | 5482 | 5569 | 5657 | 5744 | 5832 | 5919 | 6007 | 6094 | 6182 | 6269 | 87 |
| 497 | 6356 | 6444 | 6531 | 6618 | 6706 | 6793 | 6880 | 6968 | 7055 | 7142 | 87 |
| 498 | 7229 | 7317 | 7404 | 7491 | 7578 | 7665 | 7752 | 7839 | 7926 | 8014 | 87 |
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| 500 | 69 8970 | 69 9057 | 69 9144 | 69 9231 | 69 9317 | 69 9404 | 69 9491 | 69 9578 | 69 9664 | 69 9751 | 87 |
| 501 | 9838 | 9924 | 70 0011 | 70 0098 | 70 0184 | 70 0271 | 70 0358 | 70 0444 | 70 0531 | 70 0617 | 87 |
| 502 | 70 0704 | 70 0790 | 0877 | 0963 | 1050 | 1136 | 1222 | 1309 | 1395 | 1482 | 86 |
| 503 | 1568 | 1654 | 1741 | 1827 | 1913 | 1999 | 2086 | 2172 | 2258 | 2344 | 86 |
| 504 | 2431 | 2517 | 2603 | 2689 | 2775 | 2861 | 2947 | 3033 | 3119 | 3205 | 86 |
| 505 | 70 3291 | 70 3377 | 70 3463 | 70 3549 | 70 3635 | 70 3721 | 70 3807 | 70 3893 | 70 3979 | 70 4065 | 86 |
| 506 | 4151 | 4236 | 4322 | 4408 | 4494 | 4579 | 4665 | 4751 | 4837 | 4922 | 86 |
| 507 | 5008 | 5094 | 5179 | 5265 | 5350 | 5436 | 5522 | 5607 | 5693 | 5778 | 86 |
| 508 | 5864 | 5949 | 6035 | 6120 | 6206 | 6291 | 6376 | 6462 | 6547 | 6632 | 85 |
| 509 | 6718 | 6803 | 6888 | 6974 | 7059 | 7144 | 7229 | 7315 | 7400 | 7485 | 85 |
| 510 | 70 7570 | 70 7655 | 70 7740 | 70 7826 | 70 7911 | 70 7996 | 70 8081 | 70 8166 | 70 8251 | 70 8336 | 85 |
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| 512 | 9270 | 9355 | 9440 | 9524 | 9609 | 9694 | 9779 | 9863 | 9948 | 71 0033 | 85 |
| 513 | 71 0117 | 71 0202 | 71 0287 | 71 0371 | 71 0456 | 71 0540 | 71 0625 | 71 0710 | 71 0794 | 0879 | 85 |
| 514 | 0963 | 1048 | 1132 | 1217 | 1301 | 1385 | 1470 | 1554 | 1639 | 1723 | 84 |
| 515 | 71 1807 | 71 1892 | 71 1976 | 71 2060 | 71 2144 | 71 2228 | 71 2313 | 71 2397 | 71 2481 | 71 2566 | 84 |
| 516 | 2650 | 2734 | 2818 | 2902 | 2986 | 3070 | 3154 | 3238 | 3322 | 3407 | 84 |
| 517 | 3491 | 3575 | 3659 | 3742 | 3826 | 3910 | 3994 | 4078 | 4162 | 4246 | 84 |
| 518 | 4330 | 4414 | 4497 | 4581 | 4665 | 4749 | 4833 | 4916 | 5000 | 5084 | 84 |
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| 521 | 6838 | 6921 | 7004 | 7088 | 7171 | 7254 | 7338 | 7421 | 7504 | 7587 | 83 |
| 522 | 7671 | 7754 | 7837 | 7920 | 8003 | 8086 | 8169 | 8253 | 8336 | 8419 | 83 |
| 523 | 8502 | 8585 | 8668 | 8751 | 8834 | 8917 | 9000 | 9083 | 9165 | 9248 | 83 |
| 524 | 9331 | 9414 | 9497 | 9580 | 9663 | 9745 | 9828 | 9911 | 9994 | 72 0077 | 83 |
| 525 | 72 0159 | 72 0242 | 72 0325 | 72 0407 | 72 0490 | 72 0573 | 72 0655 | 72 0738 | 72 0821 | 72 0903 | 83 |
| 526 | 0986 | 1068 | 1151 | 1233 | 1316 | 1398 | 1481 | 1563 | 1646 | 1728 | 82 |
| 527 | 1811 | 1893 | 1975 | 2058 | 2140 | 2222 | 2305 | 2387 | 2469 | 2552 | 82 |
| 528 | 2634 | 2716 | 2798 | 2881 | 2963 | 3045 | 3127 | 3209 | 3291 | 3374 | 82 |
| 529 | 3456 | 3538 | 3620 | 3702 | 3784 | 3866 | 3948 | 4030 | 4112 | 4194 | 82 |
| 530 | 72 4276 | 72 4358 | 72 4440 | 72 4522 | 72 4604 | 72 4685 | 72 4767 | 72 4849 | 72 4931 | 72 5013 | 82 |
| 531 | 5095 | 5176 | 5258 | 5340 | 5422 | 5503 | 5585 | 5667 | 5748 | 5830 | 82 |
| 532 | 5912 | 5993 | 6075 | 6156 | 6238 | 6320 | 6401 | 6483 | 6564 | 6646 | 82 |
| 533 | 0727 | 0809 | 0890 | 0972 | 1053 | 1134 | 1216 | 1297 | 1379 | 1460 | 81 |
| 534 | 7541 | 7623 | 7704 | 7785 | 7866 | 7948 | 8029 | 8110 | 8191 | 8273 | 81 |
| 535 | 72 8354 | 72 8435 | 72 8516 | 72 8597 | 72 8678 | 72 8759 | 72 8841 | 72 8922 | 72 9003 | 72 9084 | 81 |
| 536 | 9165 | 9246 | 9327 | 9408 | 9489 | 9570 | 9651 | 9732 | 9813 | 9893 | 81 |
| 537 | 9974 | 73 0055 | 73 0136 | 73 0217 | 73 0298 | 73 0378 | 73 0459 | 73 0540 | 73 0621 | 73 0702 | 81 |
| 538 | 73 0782 | 0863 | 0944 | 1024 | 1105 | 1186 | 1266 | 1347 | 1428 | 1508 | 81 |
| 539 | 1589 | 1669 | 1750 | 1830 | 1911 | 1991 | 2072 | 2152 | 2233 | 2313 | 81 |
| 540 | 73 2394 | 73 2474 | 73 2555 | 73 2635 | 73 2715 | 73 2796 | 73 2876 | 73 2956 | 73 3037 | 73 3117 | 80 |
| 541 | 3197 | 3278 | 3358 | 3438 | 3518 | 3598 | 3679 | 3759 | 3839 | 3919 | 80 |
| 542 | 3999 | 4079 | 4160 | 4240 | 4320 | 4400 | 4480 | 4560 | 4640 | 4720 | 80 |
| 543 | 4800 | 4880 | 4960 | 5040 | 5120 | 5200 | 5279 | 5359 | 5439 | 5519 | 80 |
| 544 | 5599 | 5679 | 5759 | 5838 | 5918 | 5998 | 6078 | 6157 | 6237 | 6317 | 80 |
| 545 | 73 6397 | 73 6476 | 73 6556 | 73 6635 | 73 6715 | 73 6795 | 73 6874 | 73 6954 | 73 7034 | 73 7113 | 80 |
| 546 | 7193 | 7272 | 7352 | 7431 | 7511 | 7590 | 7670 | 7749 | 7829 | 7908 | 79 |
| 547 | 7987 | 8067 | 8146 | 8225 | 8305 | 8384 | 8463 | 8543 | 8622 | 8701 | 79 |
| 548 | 8781 | 8860 | 8939 | 9018 | 9097 | 9177 | 9256 | 9335 | 9414 | 9493 | 79 |
| 549 | 9572 | 9651 | 9731 | 9810 | 9889 | 9968 | 74 0047 | 74 0126 | 74 0205 | 74 0284 | 79 |
| 550 | 74 0363 | 74 0442 | 74 0521 | 74 0600 | 74 0678 | 74 0757 | 74 0836 | 74 0915 | 74 0994 | 74 1073 | 79 |
| 551 | 1152 | 1230 | 1309 | 1388 | 1467 | 1546 | 1624 | 1703 | 1782 | 1860 | 79 |
| 552 | 1939 | 2018 | 2096 | 2175 | 2254 | 2332 | 2411 | 2489 | 2568 | 2647 | 79 |
| 553 | 2725 | 2804 | 2882 | 2961 | 3039 | 3118 | 3196 | 3275 | 3353 | 3431 | 78 |
| 554 | 3510 | 3588 | 3667 | 3745 | 3823 | 3902 | 3980 | 4058 | 4136 | 4215 | 78 |
| 555 | 74 4293 | 74 4371 | 74 4449 | 74 4528 | 74 4606 | 74 4684 | 74 4762 | 74 4840 | 74 4919 | 74 4997 | 78 |
| 556 | 5075 | 5153 | 5231 | 5309 | 5387 | 5465 | 5543 | 5621 | 5699 | 5777 | 78 |
| 557 | 5855 | 5933 | 6011 | 6089 | 6167 | 6245 | 6323 | 6401 | 6479 | 6556 | 78 |
| 558 | 6634 | 6712 | 6790 | 6868 | 6945 | 7023 | 7101 | 7179 | 7256 | 7334 | 78 |
| 559 | 7412 | 7489 | 7567 | 7645 | 7722 | 7800 | 7878 | 7955 | 8033 | 8110 | 78 |
| 560 | 74 8188 | 74 8266 | 74 8343 | 74 8421 | 74 8498 | 74 8576 | 74 8653 | 74 8731 | 74 8808 | 74 8885 | 77 |
| 561 | 8963 | 9040 | 9118 | 9195 | 9272 | 9350 | 9427 | 9504 | 9582 | 9659 | 77 |
| 562 | 9736 | 9814 | 9891 | 9968 | 75 0045 | 75 0123 | 75 0200 | 75 0277 | 75 0354 | 75 0431 | 77 |
| 563 | 75 0508 | 75 0586 | 75 0663 | 75 0740 | 0817 | 0894 | 0971 | 1048 | 1125 | 1202 | 77 |
| 564 | 1279 | 1356 | 1433 | 1510 | 1587 | 1664 | 1741 | 1818 | 1895 | 1972 | 77 |
| 565 | 75 2048 | 75 2125 | 75 2202 | 75 2279 | 75 2356 | 75 2433 | 75 2509 | 75 2586 | 75 2663 | 75 2740 | 77 |
| 566 | 2816 | 2893 | 2970 | 3047 | 3123 | 3200 | 3277 | 3353 | 3430 | 3506 | 77 |
| 567 | 3583 | 3660 | 3736 | 3813 | 3889 | 3966 | 4042 | 4119 | 4195 | 4272 | 77 |
| 568 | 4348 | 4425 | 4501 | 4578 | 4654 | 4730 | 4807 | 4883 | 4960 | 5036 | 76 |
| 569 | 5112 | 5189 | 5265 | 5341 | 5417 | 5494 | 5570 | 5646 | 5722 | 5799 | 76 |
| 570 | 75 5875 | 75 5951 | 75 6027 | 75 6103 | 75 6180 | 75 6256 | 75 6332 | 75 6408 | 75 6484 | 75 6560 | 76 |
| 571 | 6636 | 6712 | 6788 | 6864 | 6940 | 7016 | 7092 | 7168 | 7244 | 7320 | 76 |
| 572 | 7396 | 7472 | 7548 | 7624 | 7700 | 7775 | 7851 | 7927 | 8003 | 8079 | 76 |
| 573 | 8155 | 8230 | 8306 | 8382 | 8458 | 8533 | 8609 | 8685 | 8761 | 8836 | 76 |
| 574 | 8912 | 8988 | 9063 | 9139 | 9214 | 9290 | 9366 | 9441 | 9517 | 9592 | 76 |
| 575 | 75 9668 | 75 9743 | 75 9819 | 75 9894 | 75 9970 | 76 0045 | 76 0121 | 76 0196 | 76 0272 | 76 0347 | 75 |
| 576 | 76 0422 | 76 0498 | 76 0573 | 76 0649 | 76 0724 | 0799 | 0875 | 0950 | 1025 | 1101 | 75 |
| 577 | 1176 | 1251 | 1326 | 1402 | 1477 | 1552 | 1627 | 1702 | 1778 | 1853 | 75 |
| 578 | 1928 | 2003 | 2078 | 2153 | 2228 | 2303 | 2378 | 2453 | 2529 | 2604 | 75 |
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| 582 | 4923 | 4998 | 5072 | 5147 | 5221 | 5296 | 5370 | 5445 | 5520 | 5594 | 75 |
| 583 | 5669 | 5743 | 5818 | 5892 | 5966 | 6041 | 6115 | 6190 | 6264 | 6338 | 74 |
| 584 | 6413 | 6487 | 6562 | 6636 | 6710 | 6785 | 6859 | 6933 | 7007 | 7082 | 74 |
| 585 | 76 7156 | 76 7230 | 76 7304 | 76 7379 | 76 7453 | 76 7527 | 76 7601 | 76 7675 | 76 7749 | 76 7823 | 74 |
| 586 | 7898 | 7972 | 8046 | 8120 | 8194 | 8268 | 8342 | 8416 | 8490 | 8564 | 74 |
| 587 | 8638 | 8712 | 8786 | 8860 | 8934 | 9008 | 9082 | 9156 | 9230 | 9303 | 74 |
| 588 | 9377 | 9451 | 9525 | 9599 | 9673 | 9746 | 9820 | 9894 | 9968 | 77 0042 | 74 |
| 589 | 77 0115 | 77 0189 | 77 0263 | 77 0336 | 77 0410 | 77 0484 | 77 0557 | 77 0631 | 77 0705 | 0778 | 74 |
| 590 | 77 0852 | 77 0926 | 77 0999 | 77 1073 | 77 1146 | 77 1220 | 77 1293 | 77 1367 | 77 1440 | 77 1514 | 74 |
| 591 | 1587 | 1661 | 1734 | 1808 | 1881 | 1955 | 2028 | 2102 | 2175 | 2248 | 73 |
| 592 | 2322 | 2395 | 2468 | 2542 | 2615 | 2688 | 2762 | 2835 | 2908 | 2981 | 73 |
| 593 | 3055 | 3128 | 3201 | 3274 | 3348 | 3421 | 3494 | 3567 | 3640 | 3713 | 73 |
| 594 | 3786 | 3860 | 3933 | 4006 | 4079 | 4152 | 4225 | 4298 | 4371 | 4444 | 73 |
| 595 | 77 4517 | 77 4590 | 77 4663 | 77 4736 | 77 4809 | 77 4882 | 77 4955 | 77 5028 | 77 5100 | 77 5173 | 73 |
| 596 | 5246 | 5319 | 5392 | 5465 | 5538 | 5610 | 5683 | 5756 | 5829 | 5902 | 73 |
| 597 | 5974 | 6047 | 6120 | 6193 | 6265 | 6338 | 6411 | 6483 | 6556 | 6629 | 73 |
| 598 | 6701 | 6774 | 6846 | 6919 | 6992 | 7064 | 7137 | 7209 | 7282 | 7354 | 73 |
| 599 | 7427 | 7499 | 7572 | 7644 | 7717 | 7789 | 7862 | 7934 | 8006 | 8079 | 72 |
| 600 | 77 8151 | 77 8224 | 77 8296 | 77 8368 | 77 8441 | 77 8513 | 77 8585 | 77 8658 | 77 8730 | 77 8802 | 72 |
| 601 | 8874 | 8947 | 9019 | 9091 | 9163 | 9236 | 9308 | 9380 | 9452 | 9524 | 72 |
| 602 | 9596 | 9669 | 9741 | 9813 | 9885 | 9957 | 78 0029 | 78 0101 | 78 0173 | 78 0245 | 72 |
| 603 | 78 0317 | 78 0389 | 78 0461 | 78 0533 | 78 0605 | 78 0677 | 0749 | 0821 | 0893 | 0965 | 72 |
| 604 | 1037 | 1109 | 1181 | 1253 | 1324 | 1396 | 1468 | 1540 | 1612 | 1684 | 72 |
| 605 | 78 1755 | 78 1827 | 78 1899 | 78 1971 | 78 2042 | 78 2114 | 78 2186 | 78 2258 | 78 2329 | 78 2401 | 72 |
| 606 | 2473 | 2544 | 2616 | 2688 | 2759 | 2831 | 2902 | 2974 | 3046 | 3117 | 72 |
| 607 | 3189 | 3260 | 3332 | 3403 | 3475 | 3546 | 3618 | 3689 | 3761 | 3832 | 71 |
| 608 | 3904 | 3975 | 4046 | 4118 | 4189 | 4261 | 4332 | 4403 | 4475 | 4546 | 71 |
| 609 | 4617 | 4689 | 4760 | 4831 | 4902 | 4974 | 5045 | 5116 | 5187 | 5259 | 71 |
| 610 | 78 5330 | 78 5401 | 78 5472 | 78 5543 | 78 5615 | 78 5686 | 78 5757 | 78 5828 | 78 5899 | 78 5970 | 71 |
| 611 | 6041 | 6112 | 6183 | 6254 | 6325 | 6396 | 6467 | 6538 | 6609 | 6680 | 71 |
| 612 | 6751 | 6822 | 6893 | 6964 | 7035 | 7106 | 7177 | 7248 | 7319 | 7390 | 71 |
| 613 | 7400 | 7531 | 7602 | 7673 | 7744 | 7815 | 7885 | 7956 | 8027 | 8098 | 71 |
| 614 | 8168 | 8239 | 8310 | 8381 | 8451 | 8522 | 8593 | 8663 | 8734 | 8804 | 71 |
| 615 | 78 8875 | 78 8946 | 78 9016 | 78 9087 | 78 9157 | 78 9228 | 78 9299 | 78 9369 | 78 9440 | 78 9510 | 71 |
| 616 | 9581 | 9651 | 9722 | 9792 | 9863 | 9933 | 79 0004 | 79 0074 | 79 0144 | 79 0215 | 70 |
| 617 | 79 0285 | 79 0356 | 79 0426 | 79 0496 | 79 0567 | 79 0637 | 0707 | 0778 | 0848 | 0918 | 70 |
| 618 | 0988 | 1059 | 1129 | 1199 | 1269 | 1340 | 1410 | 1480 | 1550 | 1620 | 70 |
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| 625 | 79 5880 | 79 5949 | 79 6019 | 79 6088 | 79 6158 | 79 6227 | 79 6297 | 79 6366 | 79 6436 | 79 6505 | 69 |
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| 627 | 7268 | 7337 | 7406 | 7475 | 7545 | 7614 | 7683 | 7752 | 7821 | 7890 | 69 |
| 628 | 7960 | 8029 | 8098 | 8167 | 8236 | 8305 | 8374 | 8443 | 8513 | 8582 | 69 |
| 629 | 8651 | 8720 | 8789 | 8858 | 8927 | 8996 | 9065 | 9134 | 9203 | 9272 | 69 |
| 630 | 79 9341 | 79 9409 | 79 9478 | 79 9547 | 79 9616 | 79 9685 | 79 9754 | 79 9823 | 79 9892 | 79 9961 | 69 |
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| 632 | 0717 | 0786 | 0854 | 0923 | 0992 | 1061 | 1129 | 1198 | 1266 | 1335 | 69 |
| 633 | 1404 | 1472 | 1541 | 1609 | 1678 | 1747 | 1815 | 1884 | 1952 | 2021 | 69 |
| 634 | 2089 | 2158 | 2226 | 2295 | 2363 | 2432 | 2500 | 2568 | 2637 | 2705 | 68 |
| 635 | 80 2774 | 80 2842 | 80 2910 | 80 2979 | 80 3047 | 80 3116 | 80 3184 | 80 3252 | 80 3321 | 80 3389 | 68 |
| 636 | 3457 | 3525 | 3594 | 3662 | 3730 | 3798 | 3867 | 3935 | 4003 | 4071 | 68 |
| 637 | 4139 | 4208 | 4276 | 4344 | 4412 | 4480 | 4548 | 4616 | 4685 | 4753 | 68 |
| 638 | 4821 | 4889 | 4957 | 5025 | 5093 | 5161 | 5229 | 5297 | 5365 | 5433 | 68 |
| 639 | 5501 | 5569 | 5637 | 5705 | 5773 | 5841 | 5908 | 5976 | 6044 | 6112 | 68 |
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| 642 | 7535 | 7603 | 7670 | 7738 | 7806 | 7873 | 7941 | 8008 | 8076 | 8143 | 68 |
| 643 | 8211 | 8279 | 8346 | 8414 | 8481 | 8549 | 8616 | 8684 | 8751 | 8818 | 67 |
| 644 | 8886 | 8953 | 9021 | 9088 | 9156 | 9223 | 9290 | 9358 | 9425 | 9492 | 67 |
| 645 | 80 9560 | 80 9627 | 80 9694 | 80 9762 | 80 9829 | 80 9896 | 80 9964 | 81 0031 | 81 0098 | 81 0165 | 67 |
| 646 | 81 0233 | 81 0300 | 81 0367 | 81 0434 | 81 0501 | 81 0569 | 81 0636 | 0703 | 0770 | 0837 | 67 |
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| 648 | 1575 | 1642 | 1709 | 1776 | 1843 | 1910 | 1977 | 2044 | 2111 | 2178 | 67 |
| 649 | 2245 | 2312 | 2379 | 2445 | 2512 | 2579 | 2646 | 2713 | 2780 | 2847 | 67 |
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| 651 | 3581 | 3648 | 3714 | 3781 | 3848 | 3914 | 3981 | 4048 | 4114 | 4181 | 67 |
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| 653 | 4913 | 4980 | 5046 | 5113 | 5179 | 5246 | 5312 | 5378 | 5445 | 5511 | 66 |
| 654 | 5578 | 5644 | 5711 | 5777 | 5843 | 5910 | 5976 | 6042 | 6109 | 6175 | 66 |
| 655 | 81 6241 | 81 6308 | 81 6374 | 81 6440 | 81 6506 | 81 6573 | 81 6639 | 81 6705 | 81 6771 | 81 6838 | 66 |
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| 657 | 7565 | 7631 | 7698 | 7764 | 7830 | 7896 | 7962 | 8028 | 8094 | 8160 | 66 |
| 658 | 8226 | 8292 | 8358 | 8424 | 8490 | 8556 | 8622 | 8688 | 8754 | 8820 | 66 |
| 659 | 8885 | 8951 | 9017 | 9083 | 9149 | 9215 | 9281 | 9346 | 9412 | 9478 | 66 |
| 660 | 81 9544 | 81 9610 | 81 9676 | 81 9741 | 81 9807 | 81 9873 | 81 9939 | 82 0004 | 82 0070 | 82 0136 | 66 |
| 661 | 82 0201 | 82 0267 | 82 0333 | 82 0399 | 82 0464 | 82 0530 | 82 0595 | 0661 | 0727 | 0792 | 66 |
| 662 | 0858 | 0924 | 0989 | 1055 | 1120 | 1186 | 1251 | 1317 | 1382 | 1448 | 66 |
| 663 | 1514 | 1579 | 1645 | 1710 | 1775 | 1841 | 1906 | 1972 | 2037 | 2103 | 65 |
| 664 | 2168 | 2233 | 2299 | 2364 | 2430 | 2495 | 2560 | 2626 | 2691 | 2756 | 65 |
| 665 | 82 2822 | 82 2887 | 82 2952 | 82 3018 | 82 3083 | 82 3148 | 82 3213 | 82 3279 | 82 3344 | 82 3409 | 65 |
| 666 | 3474 | 3539 | 3605 | 3670 | 3735 | 3800 | 3865 | 3930 | 3996 | 4061 | 65 |
| 667 | 4126 | 4191 | 4256 | 4321 | 4386 | 4451 | 4516 | 4581 | 4646 | 4711 | 65 |
| 668 | 4776 | 4841 | 4906 | 4971 | 5036 | 5101 | 5166 | 5231 | 5296 | 5361 | 65 |
| 669 | 5426 | 5491 | 5556 | 5621 | 5686 | 5751 | 5816 | 5880 | 5945 | 6010 | 65 |
| 670 | 82 6075 | 82 6140 | 82 6204 | 82 6269 | 82 6334 | 82 6399 | 82 6464 | 82 6528 | 82 6593 | 82 6658 | 65 |
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| 672 | 7369 | 7434 | 7499 | 7563 | 7628 | 7692 | 7757 | 7821 | 7886 | 7951 | 65 |
| 673 | 8015 | 8080 | 8144 | 8209 | 8273 | 8338 | 8402 | 8467 | 8531 | 8595 | 64 |
| 674 | 8660 | 8724 | 8789 | 8853 | 8918 | 8982 | 9046 | 9111 | 9175 | 9239 | 64 |
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| 677 | 83 0589 | 0653 | 0717 | 0781 | 0845 | 0909 | 0973 | 1037 | 1102 | 1166 | 64 |
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| 679 | 1870 | 1934 | 1998 | 2062 | 2126 | 2189 | 2253 | 2317 | 2381 | 2445 | 64 |
| 680 | 83 2509 | 83 2573 | 83 2637 | 83 2700 | 83 2764 | 83 2828 | 83 2892 | 83 2956 | 83 3020 | 83 3083 | 64 |
| 681 | 3147 | 3211 | 3275 | 3338 | 3402 | 3466 | 3530 | 3593 | 3657 | 3721 | 64 |
| 682 | 3784 | 3848 | 3912 | 3975 | 4039 | 4103 | 4166 | 4230 | 4294 | 4357 | 64 |
| 683 | 4421 | 4484 | 4548 | 4611 | 4675 | 4739 | 4802 | 4866 | 4929 | 4993 | 64 |
| 684 | 5056 | 5120 | 5183 | 5247 | 5310 | 5373 | 5437 | 5500 | 5564 | 5627 | 63 |
| 685 | 83 5691 | 83 5754 | 83 5817 | 83 5881 | 83 5944 | 83 6007 | 83 6071 | 83 6134 | 83 6197 | 83 6261 | 63 |
| 686 | 6324 | 6387 | 6451 | 6514 | 6577 | 6641 | 6704 | 6767 | 6830 | 6894 | 63 |
| 687 | 6957 | 7020 | 7083 | 7146 | 7210 | 7273 | 7336 | 7399 | 7462 | 7525 | 63 |
| 688 | 7588 | 7652 | 7715 | 7778 | 7841 | 7904 | 7967 | 8030 | 8093 | 8156 | 63 |
| 689 | 8219 | 8282 | 8345 | 8408 | 8471 | 8534 | 8597 | 8660 | 8723 | 8786 | 63 |
| 690 | 83 8849 | 83 8912 | 83 8975 | 83 9038 | 83 9101 | 83 9164 | 83 9227 | 83 9290 | 83 9352 | 83 9415 | 63 |
| 691 | 9478 | 9541 | 9604 | 9667 | 9729 | 9792 | 9855 | 9918 | 9981 | 84 0043 | 63 |
| 692 | 84 0106 | 84 0169 | 84 0232 | 84 0294 | 84 0357 | 84 0420 | 84 0482 | 84 0545 | 84 0608 | 0671 | 63 |
| 693 | 0733 | 0796 | 0859 | 0921 | 0984 | 1046 | 1109 | 1172 | 1234 | 1297 | 63 |
| 694 | 1359 | 1422 | 1485 | 1547 | 1610 | 1672 | 1735 | 1797 | 1860 | 1922 | 63 |
| 695 | 84 1985 | 84 2047 | 84 2110 | 84 2172 | 84 2235 | 84 2297 | 84 2360 | 84 2422 | 84 2484 | 84 2547 | 62 |
| 696 | 2609 | 2672 | 2734 | 2796 | 2859 | 2921 | 2983 | 3046 | 3108 | 3170 | 62 |
| 697 | 3233 | 3295 | 3357 | 3420 | 3482 | 3544 | 3606 | 3669 | 3731 | 3793 | 62 |
| 698 | 3855 | 3918 | 3980 | 4042 | 4104 | 4166 | 4229 | 4291 | 4353 | 4415 | 62 |
| 699 | 4477 | 4539 | 4601 | 4664 | 4726 | 4788 | 4850 | 4912 | 4974 | 5036 | 62 |
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| 702 | 6337 | 6399 | 6461 | 6523 | 6585 | 6646 | 6708 | 6770 | 6832 | 6894 | 62 |
| 703 | 6955 | 7017 | 7079 | 7141 | 7202 | 7264 | 7326 | 7388 | 7449 | 7511 | 62 |
| 704 | 7573 | 7634 | 7696 | 7758 | 7819 | 7881 | 7943 | 8004 | 8066 | 8128 | 62 |
| 705 | 84 8189 | 84 8251 | 84 8312 | 84 8374 | 84 8435 | 84 8497 | 84 8559 | 84 8620 | 84 8682 | 84 8743 | 62 |
| 706 | 8805 | 8866 | 8928 | 8989 | 9051 | 9112 | 9174 | 9235 | 9297 | 9358 | 61 |
| 707 | 9419 | 9481 | 9542 | 9604 | 9665 | 9726 | 9788 | 9849 | 9911 | 9972 | 61 |
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| 709 | 0646 | 0707 | 0769 | 0830 | 0891 | 0952 | 1014 | 1075 | 1136 | 1197 | 61 |
| 710 | 85 1258 | 85 1320 | 85 1381 | 85 1442 | 85 1503 | 85 1564 | 85 1625 | 85 1686 | 85 1747 | 85 1809 | 61 |
| 711 | 1870 | 1931 | 1992 | 2053 | 2114 | 2175 | 2236 | 2297 | 2358 | 2419 | 61 |
| 712 | 2480 | 2541 | 2602 | 2663 | 2724 | 2785 | 2846 | 2907 | 2968 | 3029 | 61 |
| 713 | 3090 | 3150 | 3211 | 3272 | 3333 | 3394 | 3455 | 3516 | 3577 | 3637 | 61 |
| 714 | 3698 | 3759 | 3820 | 3881 | 3941 | 4002 | 4063 | 4124 | 4185 | 4245 | 61 |
| 715 | 85 4306 | 85 4367 | 85 4428 | 85 4488 | 85 4549 | 85 4610 | 85 4670 | 85 4731 | 85 4792 | 85 4852 | 61 |
| 716 | 4913 | 4974 | 5034 | 5095 | 5156 | 5216 | 5277 | 5337 | 5398 | 5459 | 61 |
| 717 | 5519 | 5580 | 5640 | 5701 | 5761 | 5822 | 5882 | 5943 | 6003 | 6064 | 61 |
| 718 | 6124 | 6185 | 6245 | 6306 | 6366 | 6427 | 6487 | 6548 | 6608 | 6668 | 60 |
| 719 | 6729 | 6789 | 6850 | 6910 | 6970 | 7031 | 7091 | 7152 | 7212 | 7272 | 60 |
| 720 | 85 7332 | 85 7393 | 85 7453 | 85 7513 | 85 7574 | 85 7634 | 85 7694 | 85 7755 | 85 7815 | 85 7875 | 60 |
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| 722 | 8537 | 8597 | 8657 | 8718 | 8778 | 8838 | 8898 | 8958 | 9018 | 9078 | 60 |
| 723 | 9138 | 9198 | 9258 | 9318 | 9379 | 9439 | 9499 | 9559 | 9619 | 9679 | 60 |
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| 728 | 2131 | 2191 | 2251 | 2310 | 2370 | 2430 | 2489 | 2549 | 2608 | 2668 | 60 |
| 729 | 2728 | 2787 | 2847 | 2906 | 2966 | 3025 | 3085 | 3144 | 3204 | 3263 | 60 |
| 730 | 86 3323 | 86 3382 | 86 3442 | 86 3501 | 86 3561 | 86 3620 | 86 3680 | 86 3739 | 86 3799 | 86 3858 | 59 |
| 731 | 3917 | 3977 | 4036 | 4096 | 4155 | 4214 | 4274 | 4333 | 4392 | 4452 | 59 |
| 732 | 4511 | 4570 | 4630 | 4689 | 4748 | 4808 | 4867 | 4926 | 4985 | 5045 | 59 |
| 733 | 5104 | 5163 | 5222 | 5282 | 5341 | 5400 | 5459 | 5519 | 5578 | 5637 | 59 |
| 734 | 5696 | 5755 | 5814 | 5874 | 5933 | 5992 | 6051 | 6110 | 6169 | 6228 | 59 |
| 735 | 86 6287 | 86 6346 | 86 6405 | 86 6465 | 86 6524 | 86 6583 | 86 6642 | 86 6701 | 86 6760 | 86 6819 | 59 |
| 736 | 6878 | 6937 | 6996 | 7055 | 7114 | 7173 | 7232 | 7291 | 7350 | 7409 | 59 |
| 737 | 7467 | 7526 | 7585 | 7644 | 7703 | 7762 | 7821 | 7880 | 7939 | 7998 | 59 |
| 738 | 8056 | 8115 | 8174 | 8233 | 8292 | 8350 | 8409 | 8468 | 8527 | 8586 | 59 |
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| 740 | 86 9232 | 86 9290 | 86 9349 | 86 9408 | 86 9466 | 86 9525 | 86 9584 | 86 9642 | 86 9701 | 86 9760 | 59 |
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| 745 | 87 2156 | 87 2215 | 87 2273 | 87 2331 | 87 2389 | 87 2448 | 87 2506 | 87 2564 | 87 2622 | 87 2681 | 58 |
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| 747 | 3321 | 3379 | 3437 | 3495 | 3553 | 3611 | 3669 | 3727 | 3785 | 3844 | 58 |
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| 750 | 87 5061 | 87 5119 | 87 5177 | 87 5235 | 87 5293 | 87 5351 | 87 5409 | 87 5466 | 87 5524 | 87 5582 | 58 |
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| 754 | 7371 | 7429 | 7487 | 7544 | 7602 | 7659 | 7717 | 7774 | 7832 | 7889 | 58 |
| 755 | 87 7947 | 87 8004 | 87 8062 | 87 8119 | 87 8177 | 87 8234 | 87 8292 | 87 8349 | 87 8407 | 87 8464 | 57 |
| 756 | 8522 | 8579 | 8637 | 8694 | 8752 | 8809 | 8866 | 8924 | 8981 | 9039 | 57 |
| 757 | 9006 | 9153 | 9211 | 9268 | 9325 | 9383 | 9440 | 9497 | 9555 | 9612 | 57 |
| 758 | 9669 | 9726 | 9784 | 9841 | 9898 | 9956 | 88 0013 | 88 0070 | 88 0127 | 88 0185 | 57 |
| 759 | 88 0212 | 88 0299 | 88 0356 | 88 0413 | 88 0471 | 88 0528 | 0585 | 0642 | 0699 | 0756 | 57 |
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| 762 | 1955 | 2012 | 2069 | 2126 | 2183 | 2240 | 2297 | 2354 | 2411 | 2468 | 57 |
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| 765 | SS 3661 | SS 3718 | SS 3775 | SS 3832 | SS 3888 | SS 3945 | SS 4002 | SS 4059 | SS 4115 | SS 4172 | 57 |
| 766 | 4229 | 4285 | 4342 | 4399 | 4455 | 4512 | 4569 | 4625 | 4682 | 4739 | 57 |
| 767 | 4795 | 4852 | 4909 | 4965 | 5022 | 5078 | 5135 | 5192 | 5248 | 5305 | 57 |
| 768 | 5361 | 5418 | 5474 | 5531 | 5587 | 5644 | 5700 | 5757 | 5813 | 5870 | 57 |
| 769 | 5926 | 5983 | 6039 | 6096 | 6152 | 6209 | 6265 | 6321 | 6378 | 6434 | 56 |
| 770 | SS 6491 | SS 6547 | SS 6604 | SS 6660 | SS 6716 | SS 6773 | SS 6829 | SS 6885 | SS 6942 | SS 6998 | 56 |
| 771 | 7054 | 7111 | 7167 | 7223 | 7280 | 7336 | 7392 | 7449 | 7505 | 7561 | 56 |
| 772 | 7617 | 7674 | 7730 | 7786 | 7842 | 7898 | 7955 | 8011 | 8067 | 8123 | 56 |
| 773 | 8179 | 8236 | 8292 | 8348 | 8404 | 8460 | 8516 | 8573 | 8629 | 8685 | 56 |
| 774 | 8741 | 8797 | 8853 | 8909 | 8965 | 9021 | 9077 | 9133 | 9190 | 9246 | 56 |
| 775 | SS 9302 | SS 9358 | SS 9414 | SS 9470 | SS 9526 | SS 9582 | SS 9638 | SS 9694 | SS 9750 | SS 9806 | 56 |
| 776 | 9862 | 9918 | 9974 | 9930 | 9986 | 99141 | 99197 | 99253 | 99309 | 99365 | 56 |
| 777 | 89 0421 | 89 0477 | 89 0533 | 0589 | 0645 | 0700 | 0756 | 0812 | 0868 | 0924 | 56 |
| 778 | 0980 | 1035 | 1091 | 1147 | 1203 | 1259 | 1314 | 1370 | 1426 | 1482 | 56 |
| 779 | 1537 | 1593 | 1649 | 1705 | 1760 | 1816 | 1872 | 1928 | 1983 | 2039 | 56 |
| 780 | 89 2095 | 89 2150 | 89 2206 | 89 2262 | 89 2317 | 89 2373 | 89 2429 | 89 2484 | 89 2540 | 89 2595 | 56 |
| 781 | 2651 | 2707 | 2762 | 2818 | 2873 | 2929 | 2985 | 3040 | 3096 | 3151 | 56 |
| 782 | 3207 | 3262 | 3318 | 3373 | 3429 | 3484 | 3540 | 3595 | 3651 | 3706 | 56 |
| 783 | 3762 | 3817 | 3873 | 3928 | 3984 | 4039 | 4094 | 4150 | 4205 | 4261 | 55 |
| 784 | 4316 | 4371 | 4427 | 4482 | 4538 | 4593 | 4648 | 4704 | 4759 | 4814 | 55 |
| 785 | 89 4870 | 89 4925 | 89 4980 | 89 5036 | 89 5091 | 89 5146 | 89 5201 | 89 5257 | 89 5312 | 89 5367 | 55 |
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| 793 | 9273 | 9328 | 9383 | 9437 | 9492 | 9547 | 9602 | 9656 | 9711 | 9766 | 55 |
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| 798 | 2003 | 2057 | 2112 | 2166 | 2221 | 2275 | 2329 | 2384 | 2438 | 2492 | 54 |
| 799 | 2547 | 2601 | 2655 | 2710 | 2764 | 2818 | 2873 | 2927 | 2981 | 3036 | 54 |
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| 803 | 4716 | 4770 | 4824 | 4878 | 4932 | 4986 | 5040 | 5094 | 5148 | 5202 | 54 |
| 804 | 5256 | 5310 | 5364 | 5418 | 5472 | 5526 | 5580 | 5634 | 5688 | 5742 | 54 |
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| 806 | 6335 | 6389 | 6443 | 6497 | 6551 | 6605 | 6658 | 6712 | 6766 | 6820 | 54 |
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| 808 | 7411 | 7465 | 7519 | 7573 | 7626 | 7680 | 7734 | 7787 | 7841 | 7895 | 54 |
| 809 | 7949 | 8002 | 8056 | 8110 | 8163 | 8217 | 8270 | 8324 | 8378 | 8431 | 54 |
| 810 | 90 8485 | 90 8539 | 90 8592 | 90 8646 | 90 8699 | 90 8753 | 90 8807 | 90 8860 | 90 8914 | 90 8967 | 54 |
| 811 | 9021 | 9074 | 9128 | 9181 | 9235 | 9289 | 9342 | 9396 | 9449 | 9503 | 54 |
| 812 | 9556 | 9610 | 9663 | 9716 | 9770 | 9823 | 9877 | 9930 | 9984 | 9937 | 53 |
| 813 | 91 0091 | 91 0144 | 91 0197 | 91 0251 | 91 0304 | 91 0358 | 91 0411 | 91 0464 | 91 0518 | 0571 | 53 |
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| 815 | 91 1158 | 91 1211 | 91 1264 | 91 1317 | 91 1371 | 91 1424 | 91 1477 | 91 1530 | 91 1584 | 91 1637 | 53 |
| 816 | 1690 | 1743 | 1797 | 1850 | 1903 | 1956 | 2009 | 2063 | 2116 | 2169 | 53 |
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| 823 | 5400 | 5453 | 5505 | 5558 | 5611 | 5664 | 5716 | 5769 | 5822 | 5875 | 53 |
| 824 | 5927 | 5980 | 6033 | 6085 | 6138 | 6191 | 6243 | 6296 | 6349 | 6401 | 53 |
| 825 | 91 6454 | 91 6507 | 91 6559 | 91 6612 | 91 6664 | 91 6717 | 91 6770 | 91 6822 | 91 6875 | 91 6927 | 53 |
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| 830 | 91 9078 | 91 9130 | 91 9183 | 91 9235 | 91 9287 | 91 9340 | 91 9392 | 91 9444 | 91 9496 | 91 9549 | 52 |
| 831 | 9601 | 9653 | 9706 | 9758 | 9810 | 9862 | 9914 | 9967 | 92 0019 | 92 0071 | 52 |
| 832 | 92 0123 | 92 0176 | 92 0228 | 92 0280 | 92 0332 | 92 0384 | 92 0436 | 92 0489 | 0541 | 0593 | 52 |
| 833 | 0645 | 0697 | 0749 | 0801 | 0853 | 0906 | 0958 | 1010 | 1062 | 1114 | 52 |
| 834 | 1166 | 1218 | 1270 | 1322 | 1374 | 1426 | 1478 | 1530 | 1582 | 1634 | 52 |
| 835 | 92 1686 | 92 1738 | 92 1790 | 92 1842 | 92 1894 | 92 1946 | 92 1998 | 92 2050 | 92 2102 | 92 2154 | 52 |
| 836 | 2206 | 2258 | 2310 | 2362 | 2414 | 2466 | 2518 | 2570 | 2622 | 2674 | 52 |
| 837 | 2725 | 2777 | 2829 | 2881 | 2933 | 2985 | 3037 | 3089 | 3140 | 3192 | 52 |
| 838 | 3244 | 3296 | 3348 | 3399 | 3451 | 3503 | 3555 | 3607 | 3658 | 3710 | 52 |
| 839 | 3762 | 3814 | 3865 | 3917 | 3969 | 4021 | 4072 | 4124 | 4176 | 4228 | 52 |
| 840 | 92 4279 | 92 4331 | 92 4383 | 92 4434 | 92 4486 | 92 4538 | 92 4589 | 92 4641 | 92 4693 | 92 4744 | 52 |
| 841 | 4796 | 4848 | 4899 | 4951 | 5003 | 5054 | 5106 | 5157 | 5209 | 5261 | 52 |
| 842 | 5312 | 5364 | 5415 | 5467 | 5518 | 5570 | 5621 | 5673 | 5725 | 5776 | 52 |
| 843 | 5828 | 5879 | 5931 | 5982 | 6034 | 6085 | 6137 | 6188 | 6240 | 6291 | 51 |
| 844 | 6342 | 6394 | 6445 | 6497 | 6548 | 6600 | 6651 | 6702 | 6754 | 6805 | 51 |
| 845 | 92 6857 | 92 6908 | 92 6959 | 92 7011 | 92 7062 | 92 7114 | 92 7165 | 92 7216 | 92 7268 | 92 7319 | 51 |
| 846 | 7370 | 7422 | 7473 | 7524 | 7576 | 7627 | 7678 | 7730 | 7781 | 7832 | 51 |
| 847 | 7883 | 7935 | 7986 | 8037 | 8088 | 8140 | 8191 | 8242 | 8293 | 8345 | 51 |
| 848 | 8396 | 8447 | 8498 | 8549 | 8601 | 8652 | 8703 | 8754 | 8805 | 8857 | 51 |
| 849 | 8908 | 8959 | 9010 | 9061 | 9112 | 9163 | 9215 | 9266 | 9317 | 9368 | 51 |
| 850 | 92 9419 | 92 9470 | 92 9521 | 92 9572 | 92 9623 | 92 9674 | 92 9725 | 92 9776 | 92 9827 | 92 9879 | 51 |
| 851 | 9930 | 9981 | 93 0032 | 93 0083 | 93 0134 | 93 0185 | 93 0236 | 93 0287 | 93 0338 | 93 0389 | 51 |
| 852 | 93 0440 | 93 0491 | 0542 | 0592 | 0643 | 0694 | 0745 | 0796 | 0847 | 0898 | 51 |
| 853 | 0949 | 1000 | 1051 | 1102 | 1153 | 1204 | 1254 | 1305 | 1356 | 1407 | 51 |
| 854 | 1458 | 1509 | 1560 | 1610 | 1661 | 1712 | 1763 | 1814 | 1865 | 1915 | 51 |
| 855 | 93 1966 | 93 2017 | 93 2068 | 93 2118 | 93 2169 | 93 2220 | 93 2271 | 93 2322 | 93 2372 | 93 2423 | 51 |
| 856 | 2474 | 2524 | 2575 | 2626 | 2677 | 2727 | 2778 | 2829 | 2879 | 2930 | 51 |
| 857 | 2981 | 3031 | 3082 | 3133 | 3183 | 3234 | 3285 | 3335 | 3386 | 3437 | 51 |
| 858 | 3487 | 3538 | 3589 | 3639 | 3690 | 3740 | 3791 | 3841 | 3892 | 3943 | 51 |
| 859 | 3993 | 4044 | 4094 | 4145 | 4195 | 4246 | 4296 | 4347 | 4397 | 4448 | 51 |
| 860 | 93 4498 | 93 4549 | 93 4599 | 93 4650 | 93 4700 | 93 4751 | 93 4801 | 93 4852 | 93 4902 | 93 4953 | 50 |
| 861 | 5003 | 5054 | 5104 | 5154 | 5205 | 5255 | 5306 | 5356 | 5406 | 5457 | 50 |
| 862 | 5507 | 5558 | 5608 | 5658 | 5709 | 5759 | 5809 | 5860 | 5910 | 5960 | 50 |
| 863 | 6011 | 6061 | 6111 | 6162 | 6212 | 6262 | 6313 | 6363 | 6413 | 6463 | 50 |
| 864 | 6514 | 6564 | 6614 | 6665 | 6715 | 6765 | 6815 | 6865 | 6916 | 6966 | 50 |
| 865 | 93 7016 | 93 7066 | 93 7117 | 93 7167 | 93 7217 | 93 7267 | 93 7317 | 93 7367 | 93 7418 | 93 7468 | 50 |
| 866 | 7518 | 7568 | 7618 | 7668 | 7718 | 7769 | 7819 | 7869 | 7919 | 7969 | 50 |
| 867 | 8019 | 8069 | 8119 | 8169 | 8219 | 8269 | 8320 | 8370 | 8420 | 8470 | 50 |
| 868 | 8520 | 8570 | 8620 | 8670 | 8720 | 8770 | 8820 | 8870 | 8920 | 8970 | 50 |
| 869 | 9020 | 9070 | 9120 | 9170 | 9220 | 9270 | 9320 | 9369 | 9419 | 9469 | 50 |
| 870 | 93 9519 | 93 9569 | 93 9619 | 93 9669 | 93 9719 | 93 9769 | 93 9819 | 93 9869 | 93 9918 | 93 9968 | 50 |
| 871 | 94 0018 | 94 0068 | 94 0118 | 94 0168 | 94 0218 | 94 0267 | 94 0317 | 94 0367 | 94 0417 | 94 0467 | 50 |
| 872 | 0516 | 0566 | 0616 | 0666 | 0716 | 0765 | 0815 | 0865 | 0915 | 0964 | 50 |
| 873 | 1014 | 1064 | 1114 | 1163 | 1213 | 1263 | 1313 | 1362 | 1412 | 1462 | 50 |
| 874 | 1511 | 1561 | 1611 | 1660 | 1710 | 1760 | 1809 | 1859 | 1909 | 1958 | 50 |
| 875 | 94 2008 | 94 2058 | 94 2107 | 94 2157 | 94 2207 | 94 2256 | 94 2306 | 94 2355 | 94 2405 | 94 2455 | 50 |
| 876 | 2504 | 2554 | 2603 | 2653 | 2702 | 2752 | 2801 | 2851 | 2901 | 2950 | 50 |
| 877 | 3000 | 3049 | 3099 | 3148 | 3198 | 3247 | 3297 | 3346 | 3396 | 3445 | 49 |
| 878 | 3495 | 3544 | 3593 | 3643 | 3692 | 3742 | 3791 | 3841 | 3890 | 3939 | 49 |
| 879 | 3989 | 4038 | 4088 | 4137 | 4186 | 4236 | 4285 | 4335 | 4384 | 4433 | 49 |
| N. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | D. |

| N. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | D. |
|-----|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|----|
| 880 | 94 4483 | 94 4532 | 94 4581 | 94 4631 | 94 4680 | 94 4729 | 94 4779 | 94 4828 | 94 4877 | 94 4927 | 49 |
| 881 | 4970 | 5025 | 5074 | 5124 | 5173 | 5222 | 5272 | 5321 | 5370 | 5419 | 49 |
| 882 | 5469 | 5518 | 5567 | 5616 | 5665 | 5715 | 5764 | 5813 | 5862 | 5912 | 49 |
| 883 | 5961 | 6010 | 6059 | 6108 | 6157 | 6207 | 6256 | 6305 | 6354 | 6403 | 49 |
| 884 | 6452 | 6501 | 6551 | 6600 | 6649 | 6698 | 6747 | 6796 | 6845 | 6894 | 49 |
| 885 | 94 6943 | 94 6992 | 94 7041 | 94 7090 | 94 7140 | 94 7189 | 94 7238 | 94 7287 | 94 7336 | 94 7385 | 49 |
| 886 | 7434 | 7483 | 7532 | 7581 | 7630 | 7679 | 7728 | 7777 | 7826 | 7875 | 49 |
| 887 | 7924 | 7973 | 8022 | 8070 | 8119 | 8168 | 8217 | 8266 | 8315 | 8364 | 49 |
| 888 | 8413 | 8462 | 8511 | 8560 | 8609 | 8657 | 8706 | 8755 | 8804 | 8853 | 49 |
| 889 | 8902 | 8951 | 8999 | 9048 | 9097 | 9146 | 9195 | 9244 | 9292 | 9341 | 49 |
| 890 | 94 9390 | 94 9439 | 94 9488 | 94 9536 | 94 9585 | 94 9634 | 94 9683 | 94 9731 | 94 9780 | 94 9829 | 49 |
| 891 | 9878 | 9926 | 9975 | 95 0024 | 95 0073 | 95 0121 | 95 0170 | 95 0219 | 95 0267 | 95 0316 | 49 |
| 892 | 95 0365 | 95 0414 | 95 0462 | 95 0511 | 95 0560 | 95 0608 | 95 0657 | 95 0706 | 95 0754 | 95 0803 | 49 |
| 893 | 0851 | 0900 | 0949 | 0997 | 1046 | 1095 | 1143 | 1192 | 1240 | 1289 | 49 |
| 894 | 1338 | 1386 | 1435 | 1483 | 1532 | 1580 | 1629 | 1677 | 1726 | 1775 | 49 |
| 895 | 1823 | 1872 | 1920 | 1969 | 2017 | 2066 | 2114 | 2163 | 2211 | 2260 | 48 |
| 896 | 2308 | 2356 | 2405 | 2453 | 2502 | 2550 | 2599 | 2647 | 2696 | 2744 | 48 |
| 897 | 2792 | 2841 | 2889 | 2938 | 2986 | 3034 | 3083 | 3131 | 3180 | 3228 | 48 |
| 898 | 3276 | 3325 | 3373 | 3421 | 3470 | 3518 | 3566 | 3615 | 3663 | 3711 | 48 |
| 899 | 3760 | 3808 | 3856 | 3905 | 3953 | 4001 | 4049 | 4098 | 4146 | 4194 | 48 |
| 900 | 95 4243 | 95 4291 | 95 4339 | 95 4387 | 95 4435 | 95 4484 | 95 4532 | 95 4580 | 95 4628 | 95 4677 | 48 |
| 901 | 4725 | 4773 | 4821 | 4869 | 4918 | 4966 | 5014 | 5062 | 5110 | 5158 | 48 |
| 902 | 5207 | 5255 | 5303 | 5351 | 5399 | 5447 | 5495 | 5543 | 5592 | 5640 | 48 |
| 903 | 5688 | 5736 | 5784 | 5832 | 5880 | 5928 | 5976 | 6024 | 6072 | 6120 | 48 |
| 904 | 6168 | 6216 | 6265 | 6313 | 6361 | 6409 | 6457 | 6505 | 6553 | 6601 | 48 |
| 905 | 95 6649 | 95 6697 | 95 6745 | 95 6793 | 95 6840 | 95 6888 | 95 6936 | 95 6984 | 95 7032 | 95 7080 | 48 |
| 906 | 7128 | 7176 | 7224 | 7272 | 7320 | 7368 | 7416 | 7464 | 7512 | 7559 | 48 |
| 907 | 7607 | 7655 | 7703 | 7751 | 7799 | 7847 | 7894 | 7942 | 7990 | 8038 | 48 |
| 908 | 8086 | 8134 | 8181 | 8229 | 8277 | 8325 | 8373 | 8421 | 8468 | 8516 | 48 |
| 909 | 8564 | 8612 | 8659 | 8707 | 8755 | 8803 | 8850 | 8898 | 8946 | 8994 | 48 |
| 910 | 95 9041 | 95 9089 | 95 9137 | 95 9185 | 95 9232 | 95 9280 | 95 9328 | 95 9375 | 95 9423 | 95 9471 | 48 |
| 911 | 9518 | 9566 | 9614 | 9661 | 9709 | 9757 | 9804 | 9852 | 9900 | 9947 | 48 |
| 912 | 9995 | 96 0042 | 96 0090 | 96 0138 | 96 0185 | 96 0233 | 96 0280 | 96 0328 | 96 0376 | 96 0423 | 48 |
| 913 | 96 0471 | 96 0518 | 96 0566 | 96 0613 | 96 0661 | 96 0709 | 96 0756 | 96 0804 | 96 0851 | 96 0899 | 48 |
| 914 | 0946 | 0994 | 1041 | 1089 | 1136 | 1184 | 1231 | 1279 | 1326 | 1374 | 48 |
| 915 | 96 1421 | 96 1469 | 96 1516 | 96 1563 | 96 1611 | 96 1658 | 96 1706 | 96 1753 | 96 1801 | 96 1848 | 47 |
| 916 | 1895 | 1943 | 1990 | 2038 | 2085 | 2132 | 2180 | 2227 | 2275 | 2322 | 47 |
| 917 | 2369 | 2417 | 2464 | 2511 | 2559 | 2606 | 2653 | 2701 | 2748 | 2795 | 47 |
| 918 | 2843 | 2890 | 2937 | 2985 | 3032 | 3079 | 3126 | 3174 | 3221 | 3268 | 47 |
| 919 | 3316 | 3363 | 3410 | 3457 | 3504 | 3552 | 3599 | 3646 | 3693 | 3741 | 47 |
| 920 | 96 3788 | 96 3835 | 96 3882 | 96 3929 | 96 3977 | 96 4024 | 96 4071 | 96 4118 | 96 4165 | 96 4212 | 47 |
| 921 | 4260 | 4307 | 4354 | 4401 | 4448 | 4495 | 4542 | 4590 | 4637 | 4684 | 47 |
| 922 | 4731 | 4778 | 4825 | 4872 | 4919 | 4966 | 5013 | 5061 | 5108 | 5155 | 47 |
| 923 | 5202 | 5249 | 5296 | 5343 | 5390 | 5437 | 5484 | 5531 | 5578 | 5625 | 47 |
| 924 | 5672 | 5719 | 5766 | 5813 | 5860 | 5907 | 5954 | 6001 | 6048 | 6095 | 47 |
| 925 | 96 6142 | 96 6189 | 96 6236 | 96 6283 | 96 6329 | 96 6376 | 96 6423 | 96 6470 | 96 6517 | 96 6564 | 47 |
| 926 | 6611 | 6658 | 6705 | 6752 | 6799 | 6845 | 6892 | 6939 | 6986 | 7033 | 47 |
| 927 | 7080 | 7127 | 7173 | 7220 | 7267 | 7314 | 7361 | 7408 | 7454 | 7501 | 47 |
| 928 | 7548 | 7595 | 7642 | 7688 | 7735 | 7782 | 7829 | 7875 | 7922 | 7969 | 47 |
| 929 | 8016 | 8062 | 8109 | 8156 | 8203 | 8249 | 8296 | 8343 | 8390 | 8436 | 47 |
| 930 | 96 8483 | 96 8530 | 96 8576 | 96 8623 | 96 8670 | 96 8716 | 96 8763 | 96 8810 | 96 8856 | 96 8903 | 47 |
| 931 | 8950 | 8996 | 9043 | 9090 | 9136 | 9183 | 9229 | 9276 | 9323 | 9369 | 47 |
| 932 | 9416 | 9463 | 9509 | 9556 | 9602 | 9649 | 9695 | 9742 | 9789 | 9835 | 47 |
| 933 | 9882 | 9928 | 9975 | 97 0021 | 97 0068 | 97 0114 | 97 0161 | 97 0207 | 97 0254 | 97 0300 | 47 |
| 934 | 97 0347 | 97 0393 | 97 0440 | 97 0486 | 95 533 | 95 79 | 96 26 | 96 72 | 97 19 | 97 65 | 46 |
| 935 | 97 0812 | 97 0858 | 97 0904 | 97 0951 | 97 0997 | 97 1044 | 97 1090 | 97 1137 | 97 1183 | 97 1229 | 46 |
| 936 | 1276 | 1322 | 1369 | 1415 | 1461 | 1508 | 1554 | 1601 | 1647 | 1693 | 46 |
| 937 | 1740 | 1786 | 1832 | 1879 | 1925 | 1971 | 2018 | 2064 | 2110 | 2157 | 46 |
| 938 | 2203 | 2249 | 2295 | 2342 | 2388 | 2434 | 2481 | 2527 | 2573 | 2619 | 46 |
| 939 | 2666 | 2712 | 2758 | 2804 | 2851 | 2897 | 2943 | 2989 | 3035 | 3082 | 46 |
| N. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | D. |

| N. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | D. |
|-----|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|----|
| 940 | 97 3128 | 97 3174 | 97 3220 | 97 3266 | 97 3313 | 97 3359 | 97 3405 | 97 3451 | 97 3497 | 97 3543 | 46 |
| 941 | 3590 | 3636 | 3682 | 3728 | 3774 | 3820 | 3866 | 3913 | 3959 | 4005 | 46 |
| 942 | 4051 | 4097 | 4143 | 4189 | 4235 | 4281 | 4327 | 4374 | 4420 | 4466 | 46 |
| 943 | 4512 | 4558 | 4604 | 4650 | 4696 | 4742 | 4788 | 4834 | 4880 | 4926 | 46 |
| 944 | 4972 | 5018 | 5064 | 5110 | 5156 | 5202 | 5248 | 5294 | 5340 | 5386 | 46 |
| 945 | 97 5432 | 97 5478 | 97 5524 | 97 5570 | 97 5616 | 97 5662 | 97 5707 | 97 5753 | 97 5799 | 97 5845 | 46 |
| 946 | 5891 | 5937 | 5983 | 6029 | 6075 | 6121 | 6167 | 6212 | 6258 | 6304 | 46 |
| 947 | 6350 | 6396 | 6442 | 6488 | 6533 | 6579 | 6625 | 6671 | 6717 | 6763 | 46 |
| 948 | 6808 | 6854 | 6900 | 6946 | 6992 | 7037 | 7083 | 7129 | 7175 | 7220 | 46 |
| 949 | 7266 | 7312 | 7358 | 7403 | 7449 | 7495 | 7541 | 7586 | 7632 | 7678 | 46 |
| 950 | 97 7724 | 97 7769 | 97 7815 | 97 7861 | 97 7906 | 97 7952 | 97 7998 | 97 8043 | 97 8089 | 97 8135 | 46 |
| 951 | 8181 | 8226 | 8272 | 8317 | 8363 | 8409 | 8454 | 8500 | 8546 | 8591 | 46 |
| 952 | 8637 | 8683 | 8728 | 8774 | 8819 | 8865 | 8911 | 8956 | 9002 | 9047 | 46 |
| 953 | 9093 | 9138 | 9184 | 9230 | 9275 | 9321 | 9366 | 9412 | 9457 | 9503 | 46 |
| 954 | 9548 | 9594 | 9639 | 9685 | 9730 | 9776 | 9821 | 9867 | 9912 | 9958 | 46 |
| 955 | 98 0003 | 98 0049 | 98 0094 | 98 0140 | 98 0185 | 98 0231 | 98 0276 | 98 0322 | 98 0367 | 98 0412 | 45 |
| 956 | 0458 | 0503 | 0549 | 0594 | 0640 | 0685 | 0730 | 0776 | 0821 | 0867 | 45 |
| 957 | 0912 | 0957 | 1003 | 1048 | 1093 | 1139 | 1184 | 1229 | 1275 | 1320 | 45 |
| 958 | 1366 | 1411 | 1456 | 1501 | 1547 | 1592 | 1637 | 1683 | 1728 | 1773 | 45 |
| 959 | 1819 | 1864 | 1909 | 1954 | 2000 | 2045 | 2090 | 2135 | 2181 | 2226 | 45 |
| 960 | 98 2271 | 98 2316 | 98 2362 | 98 2407 | 98 2452 | 98 2497 | 98 2543 | 98 2588 | 98 2633 | 98 2678 | 45 |
| 961 | 2723 | 2769 | 2814 | 2859 | 2904 | 2949 | 2994 | 3040 | 3085 | 3130 | 45 |
| 962 | 3175 | 3220 | 3265 | 3310 | 3356 | 3401 | 3446 | 3491 | 3536 | 3581 | 45 |
| 963 | 3626 | 3671 | 3716 | 3762 | 3807 | 3852 | 3897 | 3942 | 3987 | 4032 | 45 |
| 964 | 4077 | 4122 | 4167 | 4212 | 4257 | 4302 | 4347 | 4392 | 4437 | 4482 | 45 |
| 965 | 98 4527 | 98 4572 | 98 4617 | 98 4662 | 98 4707 | 98 4752 | 98 4797 | 98 4842 | 98 4887 | 98 4932 | 45 |
| 966 | 4977 | 5022 | 5067 | 5112 | 5157 | 5202 | 5247 | 5292 | 5337 | 5382 | 45 |
| 967 | 5426 | 5471 | 5516 | 5561 | 5606 | 5651 | 5696 | 5741 | 5786 | 5830 | 45 |
| 968 | 5875 | 5920 | 5965 | 6010 | 6055 | 6100 | 6144 | 6189 | 6234 | 6279 | 45 |
| 969 | 6324 | 6369 | 6413 | 6458 | 6503 | 6548 | 6593 | 6637 | 6682 | 6727 | 45 |
| 970 | 98 6772 | 98 6817 | 98 6861 | 98 6906 | 98 6951 | 98 6996 | 98 7040 | 98 7085 | 98 7130 | 98 7175 | 45 |
| 971 | 7219 | 7264 | 7309 | 7353 | 7398 | 7443 | 7488 | 7532 | 7577 | 7622 | 45 |
| 972 | 7666 | 7711 | 7756 | 7800 | 7845 | 7890 | 7934 | 7979 | 8024 | 8068 | 45 |
| 973 | 8113 | 8157 | 8202 | 8247 | 8291 | 8336 | 8381 | 8425 | 8470 | 8514 | 45 |
| 974 | 8559 | 8604 | 8648 | 8693 | 8737 | 8782 | 8826 | 8871 | 8916 | 8960 | 45 |
| 975 | 98 9005 | 98 9049 | 98 9094 | 98 9138 | 98 9183 | 98 9227 | 98 9272 | 98 9316 | 98 9361 | 98 9405 | 45 |
| 976 | 9450 | 9494 | 9539 | 9583 | 9628 | 9672 | 9717 | 9761 | 9806 | 9850 | 44 |
| 977 | 9895 | 9939 | 9983 | 99 0028 | 99 0072 | 99 0117 | 99 0161 | 99 0206 | 99 0250 | 99 0294 | 44 |
| 978 | 99 0339 | 99 0383 | 99 0428 | 0472 | 0516 | 0561 | 0605 | 0650 | 0694 | 0738 | 44 |
| 979 | 0783 | 0827 | 0871 | 0916 | 0960 | 1004 | 1049 | 1093 | 1137 | 1182 | 44 |
| 980 | 99 1226 | 99 1270 | 99 1315 | 99 1359 | 99 1403 | 99 1448 | 99 1492 | 99 1536 | 99 1580 | 99 1625 | 44 |
| 981 | 1669 | 1713 | 1758 | 1802 | 1846 | 1890 | 1935 | 1979 | 2023 | 2067 | 44 |
| 982 | 2111 | 2156 | 2200 | 2244 | 2288 | 2332 | 2377 | 2421 | 2465 | 2509 | 44 |
| 983 | 2554 | 2598 | 2642 | 2686 | 2730 | 2774 | 2819 | 2863 | 2907 | 2951 | 44 |
| 984 | 2995 | 3039 | 3083 | 3127 | 3171 | 3216 | 3260 | 3304 | 3348 | 3392 | 44 |
| 985 | 99 3436 | 99 3480 | 99 3524 | 99 3568 | 99 3613 | 99 3657 | 99 3701 | 99 3745 | 99 3789 | 99 3833 | 44 |
| 986 | 3877 | 3921 | 3965 | 4009 | 4053 | 4097 | 4141 | 4185 | 4229 | 4273 | 44 |
| 987 | 4317 | 4361 | 4405 | 4449 | 4493 | 4537 | 4581 | 4625 | 4669 | 4713 | 44 |
| 988 | 4757 | 4801 | 4845 | 4889 | 4933 | 4977 | 5021 | 5065 | 5108 | 5152 | 44 |
| 989 | 5196 | 5240 | 5284 | 5328 | 5372 | 5416 | 5460 | 5504 | 5547 | 5591 | 44 |
| 990 | 99 5635 | 99 5679 | 99 5723 | 99 5767 | 99 5811 | 99 5854 | 99 5898 | 99 5942 | 99 5986 | 99 6030 | 44 |
| 991 | 6074 | 6117 | 6161 | 6205 | 6249 | 6293 | 6337 | 6380 | 6424 | 6468 | 44 |
| 992 | 6512 | 6555 | 6599 | 6643 | 6687 | 6731 | 6774 | 6818 | 6862 | 6906 | 44 |
| 993 | 6949 | 6993 | 7037 | 7080 | 7124 | 7168 | 7212 | 7255 | 7299 | 7343 | 44 |
| 994 | 7386 | 7430 | 7474 | 7517 | 7561 | 7605 | 7648 | 7692 | 7736 | 7779 | 44 |
| 995 | 99 7823 | 99 7867 | 99 7910 | 99 7954 | 99 7998 | 99 8041 | 99 8085 | 99 8129 | 99 8172 | 99 8216 | 44 |
| 996 | 8259 | 8303 | 8347 | 8390 | 8434 | 8477 | 8521 | 8564 | 8608 | 8652 | 44 |
| 997 | 8695 | 8739 | 8782 | 8826 | 8869 | 8913 | 8956 | 9000 | 9043 | 9087 | 44 |
| 998 | 9131 | 9174 | 9218 | 9261 | 9305 | 9348 | 9392 | 9435 | 9479 | 9522 | 44 |
| 999 | 9565 | 9609 | 9652 | 9696 | 9739 | 9783 | 9826 | 9870 | 9913 | 9957 | 43 |
| N. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | D. |

A TABLE

OF THE

LOGARITHMIC SINES, COSINES, TANGENTS,
AND COTANGENTS,

FOR EVERY

DEGREE AND MINUTE FROM 0° TO 90° .

18 LOGARITHMIC SINES, COSINES, TANGENTS, AND COTANGENTS.

0°

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|---------|------------|--------|-----------|---------|-----------|----|
| 0 | — ∞ | | 10.000 000 | | — ∞ | | — ∞ | 60 |
| 1 | 6.463 726 | 5017.17 | .000 000 | .00 | 6.463 726 | 5017.17 | 3.536 274 | 59 |
| 2 | .764 756 | 2934.85 | .000 000 | .00 | .764 756 | 2934.85 | .235 244 | 58 |
| 3 | .940 847 | 2082.32 | .000 000 | .00 | .940 847 | 2082.32 | .059 153 | 57 |
| 4 | 7.065 786 | 1615.17 | .000 000 | .00 | 7.065 786 | 1615.17 | 2.934 214 | 56 |
| 5 | 7.162 696 | 1319.68 | 10.000 000 | .02 | 7.162 696 | 1319.70 | 2.837 304 | 55 |
| 6 | .241 877 | 999 999 | .999 999 | .00 | .241 878 | 1115.78 | .758 122 | 54 |
| 7 | .308 824 | 1115.78 | .999 999 | .00 | .308 825 | 966.53 | .691 175 | 53 |
| 8 | .366 816 | 966.53 | .999 999 | .00 | .366 817 | 852.55 | .633 183 | 52 |
| 9 | .417 968 | 852.53 | .999 999 | .02 | .417 970 | 762.62 | .582 030 | 51 |
| 10 | 7.463 726 | 762.63 | 9.999 998 | .00 | 7.463 727 | 689.88 | 2.536 273 | 50 |
| 11 | .505 118 | 689.87 | .999 998 | .02 | .505 120 | 629.82 | .494 880 | 49 |
| 12 | .542 906 | 629.80 | .999 997 | .00 | .542 909 | 579.38 | .457 091 | 48 |
| 13 | .577 668 | 579.37 | .999 997 | .02 | .577 672 | 536.42 | .422 328 | 47 |
| 14 | .609 853 | 536.42 | .999 996 | .00 | .609 857 | 499.38 | .390 143 | 46 |
| 15 | 7.639 816 | 499.38 | 9.999 996 | .02 | 7.639 820 | 467.15 | 2.360 180 | 45 |
| 16 | .667 845 | 467.15 | .999 995 | .00 | .667 849 | 438.83 | .332 151 | 44 |
| 17 | .694 173 | 438.80 | .999 995 | .02 | .694 179 | 413.73 | .305 821 | 43 |
| 18 | .718 997 | 413.73 | .999 994 | .00 | .719 003 | 391.35 | .280 997 | 42 |
| 19 | .742 478 | 391.35 | .999 993 | .00 | .742 484 | 371.28 | .257 516 | 41 |
| 20 | 7.764 754 | 371.27 | 9.999 993 | .02 | 7.764 761 | 353.17 | 2.235 239 | 40 |
| 21 | .785 943 | 353.15 | .999 992 | .02 | .785 951 | 336.73 | .214 049 | 39 |
| 22 | .806 146 | 336.72 | .999 991 | .02 | .806 155 | 321.75 | .193 845 | 38 |
| 23 | .825 451 | 321.75 | .999 990 | .02 | .825 460 | 308.07 | .174 540 | 37 |
| 24 | .843 934 | 308.05 | .999 989 | .00 | .843 944 | 295.50 | .156 056 | 36 |
| 25 | 7.861 662 | 295.47 | 9.999 989 | .02 | 7.861 674 | 283.90 | 2.138 326 | 35 |
| 26 | .878 695 | 283.88 | .999 988 | .02 | .878 708 | 273.18 | .121 292 | 34 |
| 27 | .895 085 | 273.17 | .999 987 | .02 | .895 099 | 263.25 | .104 901 | 33 |
| 28 | .910 879 | 263.23 | .999 986 | .02 | .910 894 | 254.00 | .089 106 | 32 |
| 29 | .926 119 | 254.00 | .999 985 | .02 | .926 134 | 245.40 | .073 866 | 31 |
| 30 | 7.940 842 | 245.38 | 9.999 983 | .02 | 7.940 858 | 237.37 | 2.059 142 | 30 |
| 31 | .955 082 | 237.33 | .999 982 | .02 | .955 100 | 229.82 | .044 900 | 29 |
| 32 | .968 870 | 229.80 | .999 981 | .02 | .968 889 | 222.73 | .031 111 | 28 |
| 33 | .982 233 | 222.72 | .999 980 | .02 | .982 253 | 216.10 | .017 747 | 27 |
| 34 | .995 198 | 216.08 | .999 979 | .02 | .995 219 | 209.83 | .004 781 | 26 |
| 35 | 8.007 787 | 209.82 | 9.999 977 | .02 | 8.007 809 | 203.92 | 1.992 191 | 25 |
| 36 | .020 021 | 203.90 | .999 976 | .02 | .020 044 | 198.35 | .979 956 | 24 |
| 37 | .031 919 | 198.30 | .999 975 | .02 | .031 945 | 193.03 | .968 055 | 23 |
| 38 | .043 501 | 193.03 | .999 973 | .02 | .043 527 | 188.03 | .956 473 | 22 |
| 39 | .054 781 | 188.00 | .999 972 | .02 | .054 809 | 183.28 | .945 191 | 21 |
| 40 | 8.065 776 | 183.25 | 9.999 971 | .02 | 8.065 806 | 178.75 | 1.934 194 | 20 |
| 41 | .076 500 | 178.73 | .999 969 | .02 | .076 531 | 174.43 | .923 469 | 19 |
| 42 | .086 965 | 174.42 | .999 968 | .02 | .086 997 | 170.33 | .913 003 | 18 |
| 43 | .097 183 | 170.30 | .999 966 | .02 | .097 217 | 166.43 | .902 783 | 17 |
| 44 | .107 167 | 166.40 | .999 964 | .02 | .107 203 | 162.67 | .892 797 | 16 |
| 45 | 8.116 026 | 162.65 | 9.999 963 | .02 | 8.116 063 | 159.12 | 1.883 037 | 15 |
| 46 | .126 471 | 159.08 | .999 961 | .02 | .126 510 | 155.68 | .873 490 | 14 |
| 47 | .135 810 | 155.65 | .999 959 | .02 | .135 851 | 152.42 | .864 149 | 13 |
| 48 | .144 953 | 152.38 | .999 958 | .02 | .144 996 | 149.27 | .855 004 | 12 |
| 49 | .153 907 | 149.23 | .999 956 | .02 | .153 952 | 146.25 | .846 048 | 11 |
| 50 | 8.162 681 | 146.23 | 9.999 954 | .02 | 8.162 727 | 143.35 | 1.837 273 | 10 |
| 51 | .171 280 | 143.32 | .999 952 | .02 | .171 328 | 140.58 | .828 672 | 9 |
| 52 | .179 713 | 140.55 | .999 950 | .02 | .179 763 | 137.88 | .820 237 | 8 |
| 53 | .187 985 | 137.87 | .999 948 | .02 | .188 036 | 135.33 | .811 964 | 7 |
| 54 | .196 102 | 135.28 | .999 946 | .02 | .196 156 | 132.83 | .803 844 | 6 |
| 55 | 8.204 070 | 132.80 | 9.999 944 | .02 | 8.204 126 | 130.45 | 1.795 874 | 5 |
| 56 | .211 895 | 130.42 | .999 942 | .02 | .211 953 | 128.13 | .788 047 | 4 |
| 57 | .219 581 | 128.10 | .999 940 | .02 | .219 641 | 125.90 | .780 359 | 3 |
| 58 | .227 134 | 125.88 | .999 938 | .02 | .227 195 | 123.77 | .772 805 | 2 |
| 59 | .234 557 | 123.72 | .999 936 | .02 | .234 621 | 121.67 | .765 379 | 1 |
| 60 | 8.241 855 | 121.63 | 9.999 934 | .02 | 8.241 921 | | 1.758 079 | 0 |

LOGARITHMIC SINES, COSINES, TANGENTS, AND COTANGENTS. 19

1-

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 8.241 855 | 119.63 | 9.999 934 | .03 | 8.241 921 | 119.68 | 1.758 079 | 60 |
| 1 | .249 033 | 117.68 | .999 932 | .05 | .249 102 | 117.72 | .750 898 | 59 |
| 2 | .256 094 | 115.80 | .999 929 | .05 | .256 165 | 115.83 | .743 835 | 58 |
| 3 | .263 042 | 113.98 | .999 927 | .03 | .263 115 | 114.02 | .736 885 | 57 |
| 4 | .269 881 | 112.22 | .999 925 | .03 | .269 956 | 112.25 | .730 044 | 56 |
| 5 | 8.276 614 | 110.48 | 9.999 922 | .03 | 8.276 691 | 110.53 | 1.723 309 | 55 |
| 6 | .283 243 | 108.83 | .999 920 | .03 | .283 323 | 108.88 | .716 677 | 54 |
| 7 | .289 773 | 107.23 | .999 918 | .03 | .289 856 | 107.27 | .710 144 | 53 |
| 8 | .296 207 | 105.65 | .999 915 | .03 | .296 292 | 105.70 | .703 708 | 52 |
| 9 | .302 546 | 104.13 | .999 913 | .05 | .302 634 | 104.17 | .697 366 | 51 |
| 10 | 8.308 794 | 102.67 | 9.999 910 | .05 | 8.308 884 | 102.70 | 1.691 116 | 50 |
| 11 | .314 954 | 101.22 | .999 907 | .05 | .315 046 | 101.27 | .684 954 | 49 |
| 12 | .321 027 | 99.82 | .999 905 | .05 | .321 122 | 99.87 | .678 878 | 48 |
| 13 | .327 016 | 98.47 | .999 902 | .05 | .327 114 | 98.52 | .672 886 | 47 |
| 14 | .332 924 | 97.15 | .999 899 | .03 | .333 025 | 97.18 | .666 975 | 46 |
| 15 | 8.338 753 | 95.85 | 9.999 897 | .05 | 8.338 856 | 95.90 | 1.661 144 | 45 |
| 16 | .344 504 | 94.62 | .999 894 | .05 | .344 610 | 94.65 | .655 390 | 44 |
| 17 | .350 181 | 93.37 | .999 891 | .05 | .350 289 | 93.43 | .649 711 | 43 |
| 18 | .355 783 | 92.20 | .999 888 | .05 | .355 895 | 92.25 | .644 105 | 42 |
| 19 | .361 315 | 91.03 | .999 885 | .05 | .361 430 | 91.08 | .638 570 | 41 |
| 20 | 8.366 777 | 89.90 | 9.999 882 | .05 | 8.366 895 | 89.95 | 1.633 105 | 40 |
| 21 | .372 171 | 88.80 | .999 879 | .05 | .372 292 | 88.83 | .627 708 | 39 |
| 22 | .377 499 | 87.72 | .999 876 | .05 | .377 622 | 87.78 | .622 378 | 38 |
| 23 | .382 762 | 86.67 | .999 873 | .05 | .382 889 | 86.72 | .617 111 | 37 |
| 24 | .387 962 | 85.65 | .999 870 | .05 | .388 092 | 85.70 | .611 908 | 36 |
| 25 | 8.393 101 | 84.63 | 9.999 867 | .05 | 8.393 234 | 84.68 | 1.606 766 | 35 |
| 26 | .398 179 | 83.67 | .999 864 | .05 | .398 315 | 83.72 | .601 685 | 34 |
| 27 | .403 199 | 82.70 | .999 861 | .05 | .403 338 | 82.77 | .596 662 | 33 |
| 28 | .408 161 | 81.78 | .999 858 | .07 | .408 304 | 81.82 | .591 696 | 32 |
| 29 | .413 068 | 80.85 | .999 854 | .05 | .413 213 | 80.92 | .586 787 | 31 |
| 30 | 8.417 919 | 79.97 | 9.999 851 | .05 | 8.418 068 | 79.15 | 1.581 932 | 30 |
| 31 | .422 717 | 79.08 | .999 848 | .07 | .422 869 | 79.15 | .577 131 | 29 |
| 32 | .427 462 | 78.23 | .999 844 | .05 | .427 618 | 78.28 | .572 382 | 28 |
| 33 | .432 156 | 77.40 | .999 841 | .05 | .432 315 | 77.45 | .567 685 | 27 |
| 34 | .436 800 | 76.57 | .999 838 | .07 | .436 962 | 76.63 | .563 038 | 26 |
| 35 | 8.441 394 | 75.78 | 9.999 834 | .05 | 8.441 560 | 75.83 | 1.558 440 | 25 |
| 36 | .445 941 | 74.98 | .999 831 | .07 | .446 110 | 75.05 | .553 890 | 24 |
| 37 | .450 440 | 74.22 | .999 827 | .05 | .450 613 | 74.28 | .549 387 | 23 |
| 38 | .454 893 | 73.47 | .999 824 | .07 | .455 070 | 73.52 | .544 930 | 22 |
| 39 | .459 301 | 72.73 | .999 820 | .07 | .459 481 | 72.80 | .540 519 | 21 |
| 40 | 8.463 665 | 72.00 | 9.999 816 | .05 | 8.463 849 | 72.05 | 1.536 151 | 20 |
| 41 | .467 985 | 71.30 | .999 813 | .07 | .468 172 | 71.37 | .531 828 | 19 |
| 42 | .472 263 | 70.58 | .999 809 | .07 | .472 454 | 70.65 | .527 546 | 18 |
| 43 | .476 498 | 69.92 | .999 805 | .07 | .476 693 | 69.98 | .523 307 | 17 |
| 44 | .480 693 | 69.25 | .999 801 | .07 | .480 892 | 69.30 | .519 108 | 16 |
| 45 | 8.484 848 | 68.58 | 9.999 797 | .05 | 8.485 050 | 68.67 | 1.514 950 | 15 |
| 46 | .488 963 | 67.95 | .999 794 | .07 | .489 170 | 68.00 | .510 830 | 14 |
| 47 | .493 040 | 67.30 | .999 790 | .07 | .493 250 | 67.38 | .506 750 | 13 |
| 48 | .497 078 | 66.70 | .999 786 | .07 | .497 293 | 66.75 | .502 707 | 12 |
| 49 | .501 080 | 66.08 | .999 782 | .07 | .501 298 | 66.15 | .498 702 | 11 |
| 50 | 8.505 045 | 65.48 | 9.999 778 | .07 | 8.505 267 | 65.55 | 1.494 733 | 10 |
| 51 | .508 974 | 64.88 | .999 774 | .08 | .509 200 | 64.97 | .490 800 | 9 |
| 52 | .512 867 | 64.32 | .999 769 | .07 | .513 098 | 64.38 | .486 902 | 8 |
| 53 | .516 726 | 63.75 | .999 765 | .07 | .516 961 | 63.82 | .483 039 | 7 |
| 54 | .520 551 | 63.20 | .999 761 | .07 | .520 790 | 63.27 | .479 210 | 6 |
| 55 | 8.524 343 | 62.65 | 9.999 757 | .07 | 8.524 586 | 62.72 | 1.475 414 | 5 |
| 56 | .528 102 | 62.10 | .999 753 | .08 | .528 349 | 62.18 | .471 651 | 4 |
| 57 | .531 828 | 61.58 | .999 748 | .07 | .532 080 | 61.65 | .467 920 | 3 |
| 58 | .535 523 | 61.05 | .999 744 | .07 | .535 779 | 61.13 | .464 221 | 2 |
| 59 | .539 186 | 60.55 | .999 740 | .08 | .539 447 | 60.62 | .460 553 | 1 |
| 60 | 8.542 819 | | 9.999 735 | | 8.543 084 | | 1.456 916 | 0 |
| | Cos. | D. 1". | Sin. | D. 1". | Cot. | D. 1". | Tan. | M. |

20 LOGARITHMIC SINES, COSINES, TANGENTS, AND COTANGENTS.

20

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 8.542 819 | 60.05 | 9.999 735 | .07 | 8.543 084 | 60.12 | 1.456 916 | 60 |
| 1 | .546 422 | 59.55 | .999 731 | .08 | .546 691 | 59.62 | .453 309 | 59 |
| 2 | .549 995 | 59.55 | .999 726 | .07 | .550 268 | 59.62 | .449 732 | 58 |
| 3 | .553 539 | 59.07 | .999 722 | .08 | .553 817 | 59.15 | .446 183 | 57 |
| 4 | .557 054 | 58.58 | .999 717 | .07 | .557 336 | 58.65 | .442 664 | 56 |
| 5 | 8.560 540 | 58.10 | 9.999 713 | .08 | 8.560 828 | 58.20 | 1.439 172 | 55 |
| 6 | .563 999 | 57.65 | .999 708 | .07 | .564 291 | 57.72 | .435 709 | 54 |
| 7 | .567 431 | 57.20 | .999 704 | .08 | .567 727 | 57.27 | .432 273 | 53 |
| 8 | .570 836 | 56.75 | .999 699 | .07 | .571 137 | 56.83 | .428 863 | 52 |
| 9 | .574 214 | 56.30 | .999 694 | .08 | .574 520 | 56.38 | .425 480 | 51 |
| 10 | 8.577 566 | 55.87 | 9.999 689 | .07 | 8.577 877 | 55.95 | 1.422 123 | 50 |
| 11 | .580 892 | 55.43 | .999 685 | .08 | .581 208 | 55.52 | .418 792 | 49 |
| 12 | .584 193 | 55.02 | .999 680 | .07 | .584 514 | 55.10 | .415 486 | 48 |
| 13 | .587 469 | 54.60 | .999 675 | .08 | .587 795 | 54.68 | .412 205 | 47 |
| 14 | .590 721 | 54.20 | .999 670 | .07 | .591 051 | 54.27 | .408 949 | 46 |
| 15 | 8.593 948 | 53.78 | 9.999 665 | .08 | 8.594 283 | 53.87 | 1.405 717 | 45 |
| 16 | .597 152 | 53.40 | .999 660 | .07 | .597 492 | 53.48 | .402 508 | 44 |
| 17 | .600 332 | 53.00 | .999 655 | .08 | .600 677 | 53.08 | .399 323 | 43 |
| 18 | .603 489 | 52.62 | .999 650 | .07 | .603 839 | 52.70 | .396 161 | 42 |
| 19 | .606 623 | 52.23 | .999 645 | .08 | .606 978 | 52.32 | .393 022 | 41 |
| 20 | 8.609 734 | 51.85 | 9.999 640 | .07 | 8.610 094 | 51.93 | 1.389 906 | 40 |
| 21 | .612 823 | 51.48 | .999 635 | .08 | .613 189 | 51.58 | .386 811 | 39 |
| 22 | .615 891 | 51.13 | .999 629 | .10 | .616 262 | 51.22 | .383 738 | 38 |
| 23 | .618 937 | 50.77 | .999 624 | .08 | .619 313 | 50.85 | .380 687 | 37 |
| 24 | .621 962 | 50.42 | .999 619 | .07 | .622 343 | 50.50 | .377 657 | 36 |
| 25 | 8.624 965 | 50.05 | 9.999 614 | .08 | 8.625 352 | 50.15 | 1.374 648 | 35 |
| 26 | .627 948 | 49.72 | .999 608 | .10 | .628 340 | 49.80 | .371 660 | 34 |
| 27 | .630 911 | 49.38 | .999 603 | .08 | .631 308 | 49.47 | .368 692 | 33 |
| 28 | .633 854 | 49.05 | .999 597 | .10 | .634 256 | 49.13 | .365 744 | 32 |
| 29 | .636 776 | 48.70 | .999 592 | .08 | .637 184 | 48.80 | .362 816 | 31 |
| 30 | 8.639 680 | 48.40 | 9.999 586 | .10 | 8.640 093 | 48.48 | 1.359 907 | 30 |
| 31 | .642 563 | 48.05 | .999 581 | .08 | .642 982 | 48.15 | .357 018 | 29 |
| 32 | .645 428 | 47.75 | .999 575 | .10 | .645 853 | 47.85 | .354 147 | 28 |
| 33 | .648 274 | 47.43 | .999 570 | .08 | .648 704 | 47.52 | .351 296 | 27 |
| 34 | .651 102 | 47.13 | .999 564 | .10 | .651 537 | 47.22 | .348 463 | 26 |
| 35 | 8.653 911 | 46.82 | 9.999 558 | .08 | 8.654 352 | 46.92 | 1.345 648 | 25 |
| 36 | .656 702 | 46.52 | .999 553 | .10 | .657 149 | 46.62 | .342 851 | 24 |
| 37 | .659 475 | 46.22 | .999 547 | .08 | .659 928 | 46.32 | .340 072 | 23 |
| 38 | .662 230 | 45.92 | .999 541 | .10 | .662 689 | 46.02 | .337 311 | 22 |
| 39 | .664 968 | 45.63 | .999 535 | .08 | .665 433 | 45.73 | .334 567 | 21 |
| 40 | 8.667 689 | 45.35 | 9.999 529 | .10 | 8.668 160 | 45.45 | 1.331 840 | 20 |
| 41 | .670 393 | 45.07 | .999 524 | .08 | .670 870 | 45.17 | .329 130 | 19 |
| 42 | .673 080 | 44.78 | .999 518 | .10 | .673 563 | 44.88 | .326 437 | 18 |
| 43 | .675 751 | 44.52 | .999 512 | .08 | .676 239 | 44.60 | .323 761 | 17 |
| 44 | .678 405 | 44.23 | .999 506 | .10 | .678 909 | 44.35 | .321 100 | 16 |
| 45 | 8.681 043 | 43.97 | 9.999 500 | .08 | 8.681 544 | 44.07 | 1.318 456 | 15 |
| 46 | .683 665 | 43.70 | .999 493 | .10 | .684 172 | 43.80 | .315 828 | 14 |
| 47 | .686 272 | 43.45 | .999 487 | .08 | .686 784 | 43.53 | .313 216 | 13 |
| 48 | .688 863 | 43.18 | .999 481 | .10 | .689 381 | 43.28 | .310 619 | 12 |
| 49 | .691 438 | 42.92 | .999 475 | .08 | .691 963 | 43.03 | .308 037 | 11 |
| 50 | 8.693 998 | 42.67 | 9.999 469 | .10 | 8.694 529 | 42.77 | 1.305 471 | 10 |
| 51 | .696 543 | 42.42 | .999 463 | .08 | .697 081 | 42.53 | .302 919 | 9 |
| 52 | .699 073 | 42.17 | .999 456 | .10 | .699 617 | 42.27 | .300 383 | 8 |
| 53 | .701 589 | 41.93 | .999 450 | .08 | .702 139 | 42.03 | .297 861 | 7 |
| 54 | .704 090 | 41.68 | .999 443 | .10 | .704 646 | 41.78 | .295 354 | 6 |
| 55 | 8.706 577 | 41.45 | 9.999 437 | .08 | 8.707 140 | 41.57 | 1.292 860 | 5 |
| 56 | .709 049 | 41.20 | .999 431 | .10 | .709 618 | 41.30 | .290 382 | 4 |
| 57 | .711 507 | 40.97 | .999 424 | .08 | .712 083 | 41.08 | .287 917 | 3 |
| 58 | .713 952 | 40.75 | .999 418 | .10 | .714 534 | 40.85 | .285 466 | 2 |
| 59 | .716 383 | 40.52 | .999 411 | .08 | .716 972 | 40.63 | .283 028 | 1 |
| 60 | 8.718 800 | 40.28 | 9.999 404 | .10 | 8.719 396 | 40.40 | 1.280 604 | 0 |
| | Cos. | D. 1". | Sin. | D. 1". | Cot. | D. 1". | Tan. | M. |

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| M. | Sin. | D. 1'' | Cos. | D. 1'' | Tan. | D. 1'' | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 8.718 800 | 40.07 | 9.999 404 | .10 | 8.719 396 | 40.17 | 1.280 604 | 60 |
| 1 | .721 204 | 39.85 | .999 398 | .12 | .721 806 | 39.97 | .278 194 | 59 |
| 2 | .723 595 | 39.62 | .999 391 | .12 | .724 204 | 39.77 | .275 796 | 58 |
| 3 | .725 972 | 39.42 | .999 384 | .10 | .726 588 | 39.52 | .273 412 | 57 |
| 4 | .728 337 | 39.18 | .999 378 | .12 | .728 959 | 39.30 | .271 041 | 56 |
| 5 | 8.730 688 | 38.98 | 9.999 371 | .12 | 8.731 317 | 39.10 | 1.268 683 | 55 |
| 6 | .733 027 | 38.78 | .999 364 | .12 | .733 663 | 38.88 | .266 337 | 54 |
| 7 | .735 354 | 38.55 | .999 357 | .12 | .735 996 | 38.68 | .264 004 | 53 |
| 8 | .737 667 | 38.37 | .999 350 | .12 | .738 317 | 38.48 | .261 683 | 52 |
| 9 | .739 969 | 38.17 | .999 343 | .12 | .740 626 | 38.27 | .259 374 | 51 |
| 10 | 8.742 259 | 37.95 | 9.999 336 | .12 | 8.742 922 | 38.08 | 1.257 078 | 50 |
| 11 | .744 536 | 37.77 | .999 329 | .12 | .745 207 | 37.87 | .254 793 | 49 |
| 12 | .746 802 | 37.55 | .999 322 | .12 | .747 479 | 37.68 | .252 521 | 48 |
| 13 | .749 055 | 37.37 | .999 315 | .12 | .749 740 | 37.48 | .250 260 | 47 |
| 14 | .751 297 | 37.18 | .999 308 | .12 | .751 989 | 37.30 | .248 011 | 46 |
| 15 | 8.753 528 | 36.98 | 9.999 301 | .12 | 8.754 227 | 37.10 | 1.245 773 | 45 |
| 16 | .755 747 | 36.80 | .999 294 | .12 | .756 453 | 36.92 | .243 547 | 44 |
| 17 | .757 955 | 36.60 | .999 287 | .13 | .758 668 | 36.73 | .241 332 | 43 |
| 18 | .760 151 | 36.43 | .999 279 | .12 | .760 872 | 36.55 | .239 128 | 42 |
| 19 | .762 337 | 36.23 | .999 272 | .12 | .763 065 | 36.35 | .236 935 | 41 |
| 20 | 8.764 511 | 36.07 | 9.999 265 | .13 | 8.765 246 | 36.18 | 1.234 754 | 40 |
| 21 | .766 675 | 35.88 | .999 257 | .12 | .767 417 | 36.02 | .232 583 | 39 |
| 22 | .768 828 | 35.70 | .999 250 | .13 | .769 578 | 35.82 | .230 422 | 38 |
| 23 | .770 970 | 35.52 | .999 242 | .12 | .771 727 | 35.62 | .228 273 | 37 |
| 24 | .773 101 | 35.37 | .999 235 | .13 | .773 866 | 35.48 | .226 134 | 36 |
| 25 | 8.775 223 | 35.17 | 9.999 227 | .12 | 8.775 995 | 35.32 | 1.224 005 | 35 |
| 26 | .777 333 | 35.02 | .999 220 | .13 | .778 114 | 35.13 | .221 886 | 34 |
| 27 | .779 434 | 34.83 | .999 212 | .12 | .780 222 | 34.97 | .219 778 | 33 |
| 28 | .781 524 | 34.68 | .999 205 | .13 | .782 320 | 34.80 | .217 680 | 32 |
| 29 | .783 605 | 34.50 | .999 197 | .13 | .784 408 | 34.63 | .215 592 | 31 |
| 30 | 8.785 675 | 34.35 | 9.999 189 | .13 | 8.786 486 | 34.47 | 1.213 514 | 30 |
| 31 | .787 736 | 34.18 | .999 181 | .12 | .788 554 | 34.32 | .211 446 | 29 |
| 32 | .789 787 | 34.02 | .999 174 | .13 | .790 613 | 34.15 | .209 387 | 28 |
| 33 | .791 828 | 33.85 | .999 166 | .13 | .792 662 | 33.98 | .207 338 | 27 |
| 34 | .793 859 | 33.70 | .999 158 | .13 | .794 701 | 33.83 | .205 299 | 26 |
| 35 | 8.795 881 | 33.55 | 9.999 150 | .13 | 8.796 731 | 33.68 | 1.203 269 | 25 |
| 36 | .797 894 | 33.38 | .999 142 | .13 | .798 752 | 33.52 | .201 248 | 24 |
| 37 | .799 897 | 33.25 | .999 134 | .13 | .800 765 | 33.37 | .199 237 | 23 |
| 38 | .801 892 | 33.07 | .999 126 | .13 | .802 765 | 33.22 | .197 235 | 22 |
| 39 | .803 876 | 32.93 | .999 118 | .13 | .804 758 | 33.07 | .195 242 | 21 |
| 40 | 8.805 852 | 32.78 | 9.999 110 | .13 | 8.806 742 | 32.92 | 1.193 258 | 20 |
| 41 | .807 819 | 32.63 | .999 102 | .13 | .808 717 | 32.77 | .191 283 | 19 |
| 42 | .809 777 | 32.48 | .999 994 | .13 | .810 683 | 32.63 | .189 317 | 18 |
| 43 | .811 726 | 32.48 | .999 986 | .15 | .812 641 | 32.63 | .187 359 | 17 |
| 44 | .813 667 | 32.35 | .999 977 | .13 | .814 589 | 32.47 | .185 411 | 16 |
| 45 | 8.815 599 | 32.20 | 9.999 969 | .13 | 8.816 529 | 32.33 | 1.183 471 | 15 |
| 46 | .817 522 | 32.05 | .999 961 | .13 | .818 461 | 32.20 | .181 539 | 14 |
| 47 | .819 436 | 31.78 | .999 953 | .15 | .820 384 | 32.05 | .179 616 | 13 |
| 48 | .821 343 | 31.62 | .999 944 | .13 | .822 298 | 31.90 | .177 702 | 12 |
| 49 | .823 240 | 31.50 | .999 936 | .15 | .824 205 | 31.78 | .175 795 | 11 |
| 50 | 8.825 130 | 31.35 | 9.999 927 | .13 | 8.826 103 | 31.63 | 1.173 897 | 10 |
| 51 | .827 011 | 31.22 | .999 919 | .15 | .827 992 | 31.48 | .172 008 | 9 |
| 52 | .828 884 | 31.08 | .999 910 | .13 | .829 874 | 31.37 | .170 126 | 8 |
| 53 | .830 749 | 30.97 | .999 902 | .15 | .831 748 | 31.23 | .168 252 | 7 |
| 54 | .832 607 | 30.82 | .998 893 | .15 | .833 613 | 31.08 | .166 387 | 6 |
| 55 | 8.834 456 | 30.68 | 9.998 884 | .13 | 8.835 471 | 30.97 | 1.164 529 | 5 |
| 56 | .836 297 | 30.55 | .998 876 | .15 | .837 321 | 30.83 | .162 679 | 4 |
| 57 | .838 130 | 30.43 | .998 867 | .15 | .839 163 | 30.70 | .160 837 | 3 |
| 58 | .839 956 | 30.30 | .998 858 | .15 | .840 998 | 30.58 | .159 002 | 2 |
| 59 | .841 774 | 30.18 | .998 850 | .13 | .842 825 | 30.45 | .157 175 | 1 |
| 60 | 8.843 585 | 30.18 | 9.998 841 | .15 | 8.844 644 | 30.32 | 1.155 356 | 0 |
| | Cos. | D. 1'' | Sin. | D. 1'' | Cot. | D. 1'' | Tan. | M. |

| M. | Sin. | D. 1'' | Cos. | D. 1'' | Tan. | D. 1'' | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 8.843 585 | 30.03 | 9.998 941 | .15 | 8.844 644 | 30.18 | 1.155 356 | 60 |
| 1 | .845 387 | 29.93 | .998 932 | .15 | .846 455 | 30.08 | .153 545 | 59 |
| 2 | .847 183 | 29.80 | .998 923 | .15 | .848 260 | 29.95 | .151 740 | 58 |
| 3 | .848 971 | 29.67 | .998 914 | .15 | .850 057 | 29.82 | .149 943 | 57 |
| 4 | .850 751 | 29.57 | .998 905 | .15 | .851 846 | 29.70 | .148 154 | 56 |
| 5 | 8.852 525 | 29.43 | 9.998 896 | .15 | 8.853 628 | 29.58 | 1.146 372 | 55 |
| 6 | .854 291 | 29.30 | .998 887 | .15 | .855 403 | 29.47 | .144 597 | 54 |
| 7 | .856 049 | 29.20 | .998 878 | .15 | .857 171 | 29.35 | .142 820 | 53 |
| 8 | .857 801 | 29.08 | .998 869 | .15 | .858 932 | 29.23 | .141 068 | 52 |
| 9 | .859 546 | 28.95 | .998 860 | .15 | .860 686 | 29.12 | .139 314 | 51 |
| 10 | 8.861 283 | 28.85 | 9.998 851 | .17 | 8.862 433 | 29.00 | 1.137 567 | 50 |
| 11 | .863 014 | 28.73 | .998 841 | .15 | .864 173 | 28.88 | .135 827 | 49 |
| 12 | .864 738 | 28.62 | .998 832 | .15 | .865 906 | 28.77 | .134 094 | 48 |
| 13 | .866 455 | 28.50 | .998 823 | .15 | .867 632 | 28.65 | .132 368 | 47 |
| 14 | .868 165 | 28.38 | .998 813 | .15 | .869 351 | 28.55 | .130 649 | 46 |
| 15 | 8.869 868 | 28.28 | 9.998 804 | .15 | 8.871 064 | 28.43 | 1.128 936 | 45 |
| 16 | .871 565 | 28.17 | .998 795 | .17 | .872 770 | 28.32 | .127 230 | 44 |
| 17 | .873 255 | 28.05 | .998 785 | .15 | .874 469 | 28.22 | .125 531 | 43 |
| 18 | .874 938 | 27.95 | .998 776 | .17 | .876 162 | 28.12 | .123 838 | 42 |
| 19 | .876 615 | 27.83 | .998 766 | .15 | .877 849 | 28.00 | .122 151 | 41 |
| 20 | 8.878 285 | 27.73 | 9.998 757 | .17 | 8.879 529 | 27.88 | 1.120 471 | 40 |
| 21 | .879 949 | 27.63 | .998 747 | .15 | .881 202 | 27.78 | .118 798 | 39 |
| 22 | .881 607 | 27.52 | .998 738 | .17 | .882 869 | 27.68 | .117 131 | 38 |
| 23 | .883 258 | 27.42 | .998 728 | .17 | .884 530 | 27.58 | .115 470 | 37 |
| 24 | .884 903 | 27.32 | .998 718 | .17 | .886 185 | 27.47 | .113 815 | 36 |
| 25 | 8.886 542 | 27.20 | 9.998 708 | .15 | 8.887 833 | 27.38 | 1.112 167 | 35 |
| 26 | .888 174 | 27.12 | .998 699 | .17 | .889 476 | 27.27 | .110 524 | 34 |
| 27 | .889 801 | 27.00 | .998 689 | .17 | .891 112 | 27.17 | .108 888 | 33 |
| 28 | .891 421 | 26.90 | .998 679 | .17 | .892 742 | 27.07 | .107 258 | 32 |
| 29 | .893 035 | 26.80 | .998 669 | .17 | .894 366 | 26.97 | .105 634 | 31 |
| 30 | 8.894 643 | 26.72 | 9.998 659 | .17 | 8.895 984 | 26.87 | 1.104 016 | 30 |
| 31 | .896 246 | 26.60 | .998 649 | .17 | .897 596 | 26.78 | .102 404 | 29 |
| 32 | .897 842 | 26.50 | .998 639 | .17 | .899 203 | 26.67 | .100 797 | 28 |
| 33 | .899 432 | 26.42 | .998 629 | .17 | .900 803 | 26.58 | .099 197 | 27 |
| 34 | .901 017 | 26.32 | .998 619 | .17 | .902 398 | 26.48 | .097 602 | 26 |
| 35 | 8.902 596 | 26.22 | 9.998 609 | .17 | 8.903 987 | 26.38 | 1.096 013 | 25 |
| 36 | .904 169 | 26.12 | .998 599 | .17 | .905 570 | 26.28 | .094 430 | 24 |
| 37 | .905 736 | 26.02 | .998 589 | .17 | .907 147 | 26.20 | .092 853 | 23 |
| 38 | .907 297 | 25.93 | .998 578 | .17 | .908 719 | 26.10 | .091 281 | 22 |
| 39 | .908 853 | 25.85 | .998 568 | .17 | .910 285 | 26.02 | .089 715 | 21 |
| 40 | 8.910 404 | 25.75 | 9.998 558 | .17 | 8.911 846 | 25.92 | 1.088 154 | 20 |
| 41 | .911 949 | 25.65 | .998 548 | .18 | .913 401 | 25.83 | .086 599 | 19 |
| 42 | .913 488 | 25.57 | .998 537 | .17 | .914 951 | 25.73 | .085 049 | 18 |
| 43 | .915 022 | 25.47 | .998 527 | .18 | .916 495 | 25.65 | .083 505 | 17 |
| 44 | .916 550 | 25.38 | .998 516 | .17 | .918 034 | 25.57 | .081 966 | 16 |
| 45 | 8.918 073 | 25.30 | 9.998 506 | .18 | 8.919 568 | 25.47 | 1.080 432 | 15 |
| 46 | .919 591 | 25.20 | .998 495 | .17 | .921 096 | 25.38 | .078 904 | 14 |
| 47 | .921 103 | 25.12 | .998 485 | .18 | .922 619 | 25.28 | .077 381 | 13 |
| 48 | .922 610 | 25.03 | .998 474 | .17 | .924 136 | 25.22 | .075 864 | 12 |
| 49 | .924 112 | 24.95 | .998 464 | .18 | .925 649 | 25.12 | .074 351 | 11 |
| 50 | 8.925 609 | 24.85 | 9.998 453 | .18 | 8.927 156 | 25.03 | 1.072 844 | 10 |
| 51 | .927 100 | 24.78 | .998 442 | .18 | .928 658 | 24.95 | .071 342 | 9 |
| 52 | .928 587 | 24.68 | .998 431 | .17 | .930 155 | 24.87 | .069 845 | 8 |
| 53 | .930 068 | 24.60 | .998 421 | .18 | .931 647 | 24.78 | .068 353 | 7 |
| 54 | .931 544 | 24.52 | .998 410 | .18 | .933 134 | 24.70 | .066 866 | 6 |
| 55 | 8.933 015 | 24.43 | 9.998 399 | .18 | 8.934 616 | 24.62 | 1.065 384 | 5 |
| 56 | .934 481 | 24.35 | .998 388 | .18 | .936 093 | 24.53 | .063 907 | 4 |
| 57 | .935 942 | 24.27 | .998 377 | .18 | .937 565 | 24.45 | .062 435 | 3 |
| 58 | .937 398 | 24.20 | .998 366 | .18 | .939 032 | 24.37 | .060 968 | 2 |
| 59 | .938 850 | 24.10 | .998 355 | .18 | .940 494 | 24.30 | .059 506 | 1 |
| 60 | 8.940 296 | | 9.998 344 | | 8.941 952 | | 1.058 048 | 0 |
| | Cos. | D. 1'' | Sin. | D. 1'' | Cot. | D. 1'' | Tan. | M. |

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 8.940 296 | | 9.998 344 | .18 | 8.941 952 | | 1.050 048 | 60 |
| 1 | .941 738 | 24.03 | .998 333 | .18 | .943 404 | 24.20 | .050 596 | 59 |
| 2 | .943 174 | 23.93 | .998 322 | .18 | .944 852 | 24.13 | .055 148 | 58 |
| 3 | .944 606 | 23.87 | .998 311 | .18 | .946 295 | 24.05 | .053 705 | 57 |
| 4 | .946 034 | 23.80 | .998 300 | .18 | .947 734 | 23.98 | .052 266 | 56 |
| 5 | 8.947 456 | 23.70 | 9.998 289 | .20 | 8.949 168 | 23.90 | 1.050 832 | 55 |
| 6 | .948 874 | 23.63 | .998 277 | .18 | .950 597 | 23.82 | .049 403 | 54 |
| 7 | .950 287 | 23.55 | .998 266 | .18 | .952 021 | 23.73 | .047 979 | 53 |
| 8 | .951 696 | 23.48 | .998 255 | .18 | .953 441 | 23.67 | .046 559 | 52 |
| 9 | .953 100 | 23.40 | .998 243 | .20 | .954 856 | 23.58 | .045 144 | 51 |
| 10 | 8.954 499 | 23.32 | 9.998 232 | .18 | 8.956 267 | 23.52 | 1.043 733 | 50 |
| 11 | .955 894 | 23.25 | .998 220 | .20 | .957 674 | 23.45 | .042 326 | 49 |
| 12 | .957 284 | 23.17 | .998 209 | .18 | .959 075 | 23.35 | .040 925 | 48 |
| 13 | .958 670 | 23.10 | .998 197 | .20 | .960 473 | 23.30 | .039 527 | 47 |
| 14 | .960 052 | 23.03 | .998 186 | .18 | .961 866 | 23.22 | .038 134 | 46 |
| 15 | 8.961 429 | 22.95 | 9.998 174 | .20 | 8.963 255 | 23.15 | 1.036 745 | 45 |
| 16 | .962 801 | 22.87 | .998 163 | .18 | .964 639 | 23.07 | .035 361 | 44 |
| 17 | .964 170 | 22.82 | .998 151 | .20 | .966 019 | 23.00 | .033 981 | 43 |
| 18 | .965 534 | 22.73 | .998 139 | .18 | .967 394 | 22.92 | .032 606 | 42 |
| 19 | .966 893 | 22.65 | .998 128 | .20 | .968 766 | 22.87 | .031 234 | 41 |
| 20 | 8.968 249 | 22.60 | 9.998 116 | .18 | 8.970 133 | 22.78 | 1.029 867 | 40 |
| 21 | .969 600 | 22.52 | .998 104 | .20 | .971 496 | 22.72 | .028 504 | 39 |
| 22 | .970 947 | 22.45 | .998 092 | .18 | .972 855 | 22.65 | .027 145 | 38 |
| 23 | .972 289 | 22.37 | .998 080 | .20 | .974 209 | 22.57 | .025 791 | 37 |
| 24 | .973 628 | 22.32 | .998 068 | .18 | .975 560 | 22.52 | .024 440 | 36 |
| 25 | 8.974 962 | 22.23 | 9.998 056 | .20 | 8.976 906 | 22.43 | 1.023 094 | 35 |
| 26 | .976 293 | 22.18 | .998 044 | .18 | .978 244 | 22.37 | .021 752 | 34 |
| 27 | .977 619 | 22.10 | .998 032 | .20 | .979 586 | 22.30 | .020 414 | 33 |
| 28 | .978 941 | 22.03 | .998 020 | .18 | .980 921 | 22.25 | .019 079 | 32 |
| 29 | .980 259 | 21.97 | .998 008 | .20 | .982 251 | 22.17 | .017 749 | 31 |
| 30 | 8.981 573 | 21.90 | 9.997 996 | .18 | 8.983 577 | 22.10 | 1.016 423 | 30 |
| 31 | .982 883 | 21.83 | .997 984 | .20 | .984 899 | 22.03 | .015 101 | 29 |
| 32 | .984 189 | 21.77 | .997 972 | .18 | .986 217 | 21.97 | .013 783 | 28 |
| 33 | .985 491 | 21.70 | .997 959 | .20 | .987 532 | 21.92 | .012 468 | 27 |
| 34 | .986 789 | 21.63 | .997 947 | .18 | .988 842 | 21.83 | .011 158 | 26 |
| 35 | 8.988 083 | 21.57 | 9.997 935 | .20 | 8.990 149 | 21.78 | 1.009 851 | 25 |
| 36 | .989 374 | 21.52 | .997 922 | .18 | .991 451 | 21.70 | .008 549 | 24 |
| 37 | .990 660 | 21.43 | .997 910 | .20 | .992 750 | 21.65 | .007 250 | 23 |
| 38 | .991 943 | 21.38 | .997 897 | .18 | .994 045 | 21.58 | .005 955 | 22 |
| 39 | .993 222 | 21.32 | .997 885 | .20 | .995 337 | 21.53 | .004 663 | 21 |
| 40 | 8.994 497 | 21.25 | 9.997 872 | .18 | 8.996 624 | 21.45 | 1.003 376 | 20 |
| 41 | .995 768 | 21.18 | .997 860 | .20 | .997 908 | 21.40 | .002 092 | 19 |
| 42 | .997 036 | 21.13 | .997 847 | .18 | .999 188 | 21.33 | .000 812 | 18 |
| 43 | .998 299 | 21.05 | .997 835 | .20 | 9.000 465 | 21.28 | 0.999 535 | 17 |
| 44 | .999 560 | 21.02 | .997 822 | .18 | .001 738 | 21.22 | .998 262 | 16 |
| 45 | 9.000 816 | 20.93 | 9.997 809 | .20 | 9.003 007 | 21.15 | 0.996 993 | 15 |
| 46 | .002 069 | 20.88 | .997 797 | .18 | .004 272 | 21.08 | .995 728 | 14 |
| 47 | .003 318 | 20.82 | .997 784 | .20 | .005 534 | 21.03 | .994 466 | 13 |
| 48 | .004 563 | 20.75 | .997 771 | .18 | .006 792 | 20.97 | .993 208 | 12 |
| 49 | .005 805 | 20.70 | .997 758 | .20 | .008 047 | 20.92 | .991 953 | 11 |
| 50 | 9.007 044 | 20.65 | 9.997 745 | .18 | 9.009 298 | 20.85 | 0.990 702 | 10 |
| 51 | .008 278 | 20.57 | .997 732 | .20 | .010 546 | 20.80 | .989 454 | 9 |
| 52 | .009 510 | 20.53 | .997 719 | .18 | .011 790 | 20.73 | .988 210 | 8 |
| 53 | .010 737 | 20.45 | .997 706 | .20 | .013 031 | 20.68 | .986 969 | 7 |
| 54 | .011 962 | 20.42 | .997 693 | .18 | .014 268 | 20.62 | .985 732 | 6 |
| 55 | 9.013 182 | 20.33 | 9.997 680 | .20 | 9.015 502 | 20.57 | 0.984 498 | 5 |
| 56 | .014 400 | 20.30 | .997 667 | .18 | .016 732 | 20.50 | .983 268 | 4 |
| 57 | .015 613 | 20.22 | .997 654 | .20 | .017 959 | 20.45 | .982 041 | 3 |
| 58 | .016 824 | 20.18 | .997 641 | .18 | .019 183 | 20.40 | .980 817 | 2 |
| 59 | .018 031 | 20.12 | .997 628 | .20 | .020 403 | 20.33 | .979 597 | 1 |
| 60 | 9.019 235 | 20.07 | 9.997 614 | .18 | 9.021 620 | 20.28 | 0.978 380 | 0 |

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.019 235 | 20.00 | 9.997 614 | .22 | 9.021 620 | 20.23 | 0.978 380 | 60 |
| 1 | .020 435 | 19.95 | .997 601 | .22 | .022 834 | 20.17 | .977 166 | 59 |
| 2 | .021 632 | 19.88 | .997 588 | .23 | .024 044 | 20.12 | .975 956 | 58 |
| 3 | .022 825 | 19.85 | .997 574 | .22 | .025 251 | 20.07 | .974 749 | 57 |
| 4 | .024 016 | 19.78 | .997 561 | .23 | .026 455 | 20.00 | .973 545 | 56 |
| 5 | 9.025 203 | 19.72 | 9.997 547 | .22 | 9.027 655 | 19.95 | 0.972 345 | 55 |
| 6 | .026 386 | 19.68 | .997 534 | .23 | .028 852 | 19.90 | .971 148 | 54 |
| 7 | .027 567 | 19.62 | .997 520 | .22 | .030 046 | 19.85 | .969 954 | 53 |
| 8 | .028 744 | 19.57 | .997 507 | .23 | .031 237 | 19.80 | .968 763 | 52 |
| 9 | .029 918 | 19.52 | .997 493 | .22 | .032 425 | 19.73 | .967 575 | 51 |
| 10 | 9.031 089 | 19.47 | 9.997 480 | .23 | 9.033 609 | 19.70 | 0.966 391 | 50 |
| 11 | .032 257 | 19.40 | .997 466 | .23 | .034 791 | 19.63 | .965 209 | 49 |
| 12 | .033 421 | 19.35 | .997 452 | .22 | .035 969 | 19.58 | .964 031 | 48 |
| 13 | .034 582 | 19.32 | .997 439 | .23 | .037 144 | 19.53 | .962 856 | 47 |
| 14 | .035 741 | 19.25 | .997 425 | .23 | .038 316 | 19.48 | .961 684 | 46 |
| 15 | 9.036 806 | 19.20 | 9.997 411 | .23 | 9.039 485 | 19.43 | 0.960 515 | 45 |
| 16 | .038 048 | 19.15 | .997 397 | .23 | .040 651 | 19.37 | .959 349 | 44 |
| 17 | .039 197 | 19.08 | .997 383 | .23 | .041 813 | 19.33 | .958 187 | 43 |
| 18 | .040 342 | 19.05 | .997 369 | .23 | .042 973 | 19.28 | .957 027 | 42 |
| 19 | .041 485 | 19.00 | .997 355 | .23 | .044 130 | 19.23 | .955 870 | 41 |
| 20 | 9.042 625 | 18.95 | 9.997 341 | .23 | 9.045 284 | 19.17 | 0.954 716 | 40 |
| 21 | .043 762 | 18.88 | .997 327 | .23 | .046 434 | 19.13 | .953 566 | 39 |
| 22 | .044 895 | 18.85 | .997 313 | .23 | .047 582 | 19.08 | .952 418 | 38 |
| 23 | .046 026 | 18.80 | .997 299 | .23 | .048 727 | 19.03 | .951 273 | 37 |
| 24 | .047 154 | 18.75 | .997 285 | .23 | .049 869 | 18.98 | .950 131 | 36 |
| 25 | 9.048 279 | 18.68 | 9.997 271 | .23 | 9.051 008 | 18.93 | 0.948 992 | 35 |
| 26 | .049 400 | 18.65 | .997 257 | .25 | .052 144 | 18.88 | .947 856 | 34 |
| 27 | .050 519 | 18.60 | .997 242 | .23 | .053 277 | 18.83 | .946 723 | 33 |
| 28 | .051 635 | 18.57 | .997 228 | .23 | .054 407 | 18.80 | .945 593 | 32 |
| 29 | .052 749 | 18.50 | .997 214 | .25 | .055 535 | 18.73 | .944 465 | 31 |
| 30 | 9.053 859 | 18.45 | 9.997 199 | .23 | 9.056 659 | 18.70 | 0.943 341 | 30 |
| 31 | .054 966 | 18.42 | .997 185 | .25 | .057 781 | 18.65 | .942 219 | 29 |
| 32 | .056 071 | 18.35 | .997 170 | .23 | .058 900 | 18.60 | .941 100 | 28 |
| 33 | .057 172 | 18.32 | .997 156 | .25 | .060 016 | 18.57 | .939 984 | 27 |
| 34 | .058 271 | 18.27 | .997 141 | .23 | .061 130 | 18.50 | .938 870 | 26 |
| 35 | 9.059 367 | 18.22 | 9.997 127 | .25 | 9.062 240 | 18.47 | 0.937 760 | 25 |
| 36 | .060 460 | 18.18 | .997 112 | .23 | .063 348 | 18.42 | .936 652 | 24 |
| 37 | .061 551 | 18.13 | .997 098 | .25 | .064 453 | 18.38 | .935 547 | 23 |
| 38 | .062 639 | 18.08 | .997 083 | .25 | .065 556 | 18.32 | .934 444 | 22 |
| 39 | .063 724 | 18.03 | .997 068 | .25 | .066 655 | 18.28 | .933 345 | 21 |
| 40 | 9.064 806 | 17.98 | 9.997 053 | .23 | 9.067 752 | 18.23 | 0.932 248 | 20 |
| 41 | .065 885 | 17.95 | .997 039 | .25 | .068 846 | 18.20 | .931 154 | 19 |
| 42 | .066 962 | 17.90 | .997 024 | .25 | .069 938 | 18.15 | .930 062 | 18 |
| 43 | .068 036 | 17.85 | .997 009 | .25 | .071 027 | 18.10 | .928 973 | 17 |
| 44 | .069 107 | 17.82 | .996 994 | .25 | .072 113 | 18.07 | .927 887 | 16 |
| 45 | 9.070 176 | 17.77 | 9.996 979 | .25 | 9.073 197 | 18.02 | 0.926 803 | 15 |
| 46 | .071 242 | 17.73 | .996 964 | .25 | .074 278 | 17.97 | .925 722 | 14 |
| 47 | .072 306 | 17.67 | .996 949 | .25 | .075 356 | 17.93 | .924 644 | 13 |
| 48 | .073 366 | 17.63 | .996 934 | .25 | .076 432 | 17.88 | .923 568 | 12 |
| 49 | .074 424 | 17.60 | .996 919 | .25 | .077 505 | 17.85 | .922 495 | 11 |
| 50 | 9.075 480 | 17.55 | 9.996 904 | .25 | 9.078 576 | 17.80 | 0.921 424 | 10 |
| 51 | .076 533 | 17.50 | .996 889 | .25 | .079 644 | 17.77 | .920 356 | 9 |
| 52 | .077 583 | 17.47 | .996 874 | .27 | .080 710 | 17.72 | .919 290 | 8 |
| 53 | .078 631 | 17.42 | .996 858 | .25 | .081 773 | 17.67 | .918 227 | 7 |
| 54 | .079 676 | 17.38 | .996 843 | .25 | .082 833 | 17.63 | .917 167 | 6 |
| 55 | 9.080 719 | 17.33 | 9.996 828 | .27 | 9.083 891 | 17.60 | 0.916 109 | 5 |
| 56 | .081 759 | 17.30 | .996 812 | .25 | .084 947 | 17.55 | .915 053 | 4 |
| 57 | .082 797 | 17.25 | .996 797 | .25 | .086 000 | 17.50 | .914 000 | 3 |
| 58 | .083 832 | 17.20 | .996 782 | .27 | .087 050 | 17.47 | .912 950 | 2 |
| 59 | .084 864 | 17.17 | .996 766 | .25 | .088 098 | 17.43 | .911 902 | 1 |
| 60 | 9.085 894 | | 9.996 751 | | 9.089 144 | | 0.910 856 | 0 |

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.085 894 | 17.13 | 9.996 751 | .27 | 9.089 144 | 17.38 | 0.910 856 | 60 |
| 1 | .086 922 | 17.08 | .996 735 | .25 | .090 187 | 17.35 | .909 813 | 59 |
| 2 | .087 947 | 17.05 | .996 720 | .27 | .091 228 | 17.30 | .908 772 | 58 |
| 3 | .088 970 | 17.00 | .996 704 | .27 | .092 266 | 17.27 | .907 734 | 57 |
| 4 | .089 990 | 16.97 | .996 688 | .25 | .093 302 | 17.23 | .906 698 | 56 |
| 5 | 9.091 008 | 16.93 | 9.996 673 | .27 | 9.094 336 | 17.18 | 0.905 664 | 55 |
| 6 | .092 024 | 16.88 | .996 657 | .27 | .095 377 | 17.13 | .904 633 | 54 |
| 7 | .093 037 | 16.83 | .996 641 | .27 | .096 395 | 17.12 | .903 605 | 53 |
| 8 | .094 047 | 16.82 | .996 625 | .25 | .097 422 | 17.07 | .902 578 | 52 |
| 9 | .095 056 | 16.77 | .996 610 | .27 | .098 446 | 17.03 | .901 554 | 51 |
| 10 | 9.096 062 | 16.72 | 9.996 594 | .27 | 9.099 468 | 16.98 | 0.900 532 | 50 |
| 11 | .097 065 | 16.68 | .996 578 | .27 | .100 487 | 16.95 | .899 513 | 49 |
| 12 | .098 066 | 16.65 | .996 562 | .27 | .101 504 | 16.92 | .898 496 | 48 |
| 13 | .099 065 | 16.62 | .996 546 | .27 | .102 519 | 16.88 | .897 481 | 47 |
| 14 | .100 062 | 16.57 | .996 530 | .27 | .103 532 | 16.83 | .896 468 | 46 |
| 15 | 9.101 056 | 16.53 | 9.996 514 | .27 | 9.104 542 | 16.80 | 0.895 458 | 45 |
| 16 | .102 048 | 16.48 | .996 498 | .27 | .105 550 | 16.77 | .894 450 | 44 |
| 17 | .103 037 | 16.47 | .996 482 | .28 | .106 556 | 16.72 | .893 444 | 43 |
| 18 | .104 025 | 16.42 | .996 465 | .27 | .107 559 | 16.68 | .892 441 | 42 |
| 19 | .105 010 | 16.37 | .996 449 | .27 | .108 560 | 16.65 | .891 440 | 41 |
| 20 | 9.105 992 | 16.35 | 9.996 433 | .27 | 9.109 559 | 16.62 | 0.890 441 | 40 |
| 21 | .106 973 | 16.30 | .996 417 | .28 | .110 556 | 16.58 | .889 444 | 39 |
| 22 | .107 951 | 16.27 | .996 400 | .27 | .111 551 | 16.53 | .888 449 | 38 |
| 23 | .108 927 | 16.23 | .996 384 | .27 | .112 543 | 16.50 | .887 457 | 37 |
| 24 | .109 901 | 16.20 | .996 368 | .28 | .113 533 | 16.47 | .886 467 | 36 |
| 25 | 9.110 873 | 16.15 | 9.996 351 | .27 | 9.114 521 | 16.43 | 0.885 479 | 35 |
| 26 | .111 842 | 16.12 | .996 335 | .28 | .115 507 | 16.40 | .884 493 | 34 |
| 27 | .112 809 | 16.08 | .996 318 | .27 | .116 491 | 16.35 | .883 509 | 33 |
| 28 | .113 774 | 16.05 | .996 302 | .28 | .117 472 | 16.33 | .882 528 | 32 |
| 29 | .114 737 | 16.02 | .996 285 | .27 | .118 452 | 16.28 | .881 548 | 31 |
| 30 | 9.115 698 | 15.97 | 9.996 269 | .28 | 9.119 429 | 16.23 | 0.880 571 | 30 |
| 31 | .116 656 | 15.95 | .996 252 | .28 | .120 404 | 16.22 | .879 596 | 29 |
| 32 | .117 613 | 15.90 | .996 235 | .27 | .121 377 | 16.18 | .878 623 | 28 |
| 33 | .118 567 | 15.87 | .996 219 | .28 | .122 348 | 16.15 | .877 652 | 27 |
| 34 | .119 519 | 15.83 | .996 202 | .28 | .123 317 | 16.12 | .876 683 | 26 |
| 35 | 9.120 469 | 15.80 | 9.996 185 | .28 | 9.124 284 | 16.08 | 0.875 716 | 25 |
| 36 | .121 417 | 15.75 | .996 168 | .28 | .125 249 | 16.03 | .874 751 | 24 |
| 37 | .122 362 | 15.73 | .996 151 | .28 | .126 211 | 16.02 | .873 789 | 23 |
| 38 | .123 306 | 15.70 | .996 134 | .28 | .127 172 | 15.97 | .872 828 | 22 |
| 39 | .124 248 | 15.65 | .996 117 | .28 | .128 130 | 15.95 | .871 870 | 21 |
| 40 | 9.125 187 | 15.63 | 9.996 100 | .28 | 9.129 087 | 15.90 | 0.870 913 | 20 |
| 41 | .126 125 | 15.58 | .996 083 | .28 | .130 041 | 15.88 | .869 959 | 19 |
| 42 | .127 060 | 15.55 | .996 066 | .28 | .130 994 | 15.83 | .869 006 | 18 |
| 43 | .127 993 | 15.53 | .996 049 | .28 | .131 944 | 15.82 | .868 056 | 17 |
| 44 | .128 925 | 15.48 | .996 032 | .28 | .132 893 | 15.77 | .867 107 | 16 |
| 45 | 9.129 854 | 15.45 | 9.996 015 | .28 | 9.133 839 | 15.75 | 0.866 161 | 15 |
| 46 | .130 781 | 15.42 | .995 998 | .30 | .134 784 | 15.70 | .865 216 | 14 |
| 47 | .131 706 | 15.40 | .995 980 | .28 | .135 726 | 15.68 | .864 274 | 13 |
| 48 | .132 630 | 15.35 | .995 963 | .28 | .136 667 | 15.63 | .863 333 | 12 |
| 49 | .133 551 | 15.32 | .995 946 | .30 | .137 605 | 15.62 | .862 395 | 11 |
| 50 | 9.134 470 | 15.28 | 9.995 928 | .28 | 9.138 542 | 15.57 | 0.861 458 | 10 |
| 51 | .135 387 | 15.27 | .995 911 | .28 | .139 476 | 15.55 | .860 524 | 9 |
| 52 | .136 303 | 15.22 | .995 894 | .30 | .140 409 | 15.52 | .859 591 | 8 |
| 53 | .137 216 | 15.20 | .995 876 | .28 | .141 340 | 15.48 | .858 660 | 7 |
| 54 | .138 128 | 15.15 | .995 859 | .30 | .142 269 | 15.45 | .857 731 | 6 |
| 55 | 9.139 037 | 15.12 | 9.995 841 | .30 | 9.143 196 | 15.42 | 0.856 804 | 5 |
| 56 | .139 944 | 15.10 | .995 823 | .28 | .144 121 | 15.38 | .855 879 | 4 |
| 57 | .140 850 | 15.07 | .995 806 | .30 | .145 044 | 15.37 | .854 956 | 3 |
| 58 | .141 754 | 15.02 | .995 788 | .28 | .145 966 | 15.32 | .854 034 | 2 |
| 59 | .142 655 | 15.00 | .995 771 | .30 | .146 885 | 15.30 | .853 115 | 1 |
| 60 | 9.143 555 | | 9.995 753 | | 9.147 803 | | 0.852 197 | 0 |

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.143 555 | 14.97 | 9.995 753 | .30 | 9.147 803 | 15.25 | 0.852 197 | 60 |
| 1 | .144 453 | 14.93 | .995 735 | .30 | .148 718 | 15.23 | .851 282 | 59 |
| 2 | .145 349 | 14.90 | .995 717 | .30 | .149 632 | 15.20 | .850 368 | 58 |
| 3 | .146 243 | 14.88 | .995 699 | .30 | .150 544 | 15.17 | .849 456 | 57 |
| 4 | .147 136 | 14.83 | .995 681 | .28 | .151 454 | 15.15 | .848 546 | 56 |
| 5 | 9.148 026 | 14.82 | 9.995 664 | .30 | 9.152 363 | 15.10 | 0.847 637 | 55 |
| 6 | .148 915 | 14.78 | .995 646 | .30 | .153 269 | 15.08 | .846 731 | 54 |
| 7 | .149 802 | 14.73 | .995 628 | .30 | .154 174 | 15.05 | .845 826 | 53 |
| 8 | .150 686 | 14.72 | .995 610 | .32 | .155 077 | 15.02 | .844 923 | 52 |
| 9 | .151 569 | 14.70 | .995 591 | .30 | .155 978 | 14.98 | .844 022 | 51 |
| 10 | 9.152 451 | 14.65 | 9.995 573 | .30 | 9.156 877 | 14.97 | 0.843 123 | 50 |
| 11 | .153 339 | 14.63 | .995 555 | .30 | .157 775 | 14.93 | .842 225 | 49 |
| 12 | .154 208 | 14.58 | .995 537 | .30 | .158 671 | 14.90 | .841 329 | 48 |
| 13 | .155 083 | 14.57 | .995 519 | .30 | .159 565 | 14.87 | .840 435 | 47 |
| 14 | .155 957 | 14.55 | .995 501 | .32 | .160 457 | 14.83 | .839 543 | 46 |
| 15 | 9.156 830 | 14.50 | 9.995 482 | .30 | 9.161 347 | 14.82 | 0.838 653 | 45 |
| 16 | .157 700 | 14.48 | .995 464 | .30 | .162 236 | 14.78 | .837 764 | 44 |
| 17 | .158 569 | 14.43 | .995 446 | .32 | .163 123 | 14.75 | .836 877 | 43 |
| 18 | .159 435 | 14.43 | .995 427 | .30 | .164 008 | 14.73 | .835 992 | 42 |
| 19 | .160 301 | 14.38 | .995 409 | .32 | .164 892 | 14.70 | .835 108 | 41 |
| 20 | 9.161 164 | 14.35 | 9.995 390 | .30 | 9.165 774 | 14.67 | 0.834 226 | 40 |
| 21 | .162 025 | 14.33 | .995 372 | .32 | .166 654 | 14.63 | .833 346 | 39 |
| 22 | .162 885 | 14.30 | .995 353 | .30 | .167 532 | 14.62 | .832 468 | 38 |
| 23 | .163 743 | 14.28 | .995 334 | .32 | .168 409 | 14.58 | .831 591 | 37 |
| 24 | .164 600 | 14.23 | .995 316 | .32 | .169 284 | 14.55 | .830 716 | 36 |
| 25 | 9.165 454 | 14.22 | 9.995 297 | .32 | 9.170 157 | 14.53 | 0.829 843 | 35 |
| 26 | .166 307 | 14.20 | .995 278 | .30 | .171 029 | 14.50 | .828 971 | 34 |
| 27 | .167 159 | 14.15 | .995 260 | .32 | .171 899 | 14.47 | .828 101 | 33 |
| 28 | .168 008 | 14.13 | .995 241 | .32 | .172 767 | 14.45 | .827 233 | 32 |
| 29 | .168 856 | 14.10 | .995 222 | .32 | .173 634 | 14.42 | .826 366 | 31 |
| 30 | 9.169 702 | 14.08 | 9.995 203 | .32 | 9.174 499 | 14.38 | 0.825 501 | 30 |
| 31 | .170 547 | 14.03 | .995 184 | .32 | .175 362 | 14.37 | .824 638 | 29 |
| 32 | .171 389 | 14.02 | .995 165 | .32 | .176 224 | 14.33 | .823 776 | 28 |
| 33 | .172 230 | 14.00 | .995 146 | .32 | .177 084 | 14.30 | .822 916 | 27 |
| 34 | .173 070 | 13.97 | .995 127 | .32 | .177 942 | 14.28 | .822 058 | 26 |
| 35 | 9.173 908 | 13.93 | 9.995 108 | .32 | 9.178 799 | 14.27 | 0.821 201 | 25 |
| 36 | .174 744 | 13.90 | .995 089 | .32 | .179 655 | 14.22 | .820 345 | 24 |
| 37 | .175 578 | 13.88 | .995 070 | .32 | .180 508 | 14.20 | .819 492 | 23 |
| 38 | .176 411 | 13.85 | .995 051 | .32 | .181 360 | 14.18 | .818 640 | 22 |
| 39 | .177 242 | 13.83 | .995 032 | .32 | .182 211 | 14.13 | .817 789 | 21 |
| 40 | 9.178 072 | 13.80 | 9.995 013 | .33 | 9.183 059 | 14.13 | 0.816 941 | 20 |
| 41 | .178 900 | 13.77 | .994 993 | .32 | .183 907 | 14.08 | .816 093 | 19 |
| 42 | .179 726 | 13.75 | .994 974 | .32 | .184 752 | 14.08 | .815 248 | 18 |
| 43 | .180 551 | 13.72 | .994 955 | .33 | .185 597 | 14.03 | .814 403 | 17 |
| 44 | .181 374 | 13.70 | .994 935 | .32 | .186 439 | 14.02 | .813 561 | 16 |
| 45 | 9.182 196 | 13.67 | 9.994 916 | .33 | 9.187 280 | 14.00 | 0.812 720 | 15 |
| 46 | .183 016 | 13.63 | .994 896 | .32 | .188 120 | 13.97 | .811 880 | 14 |
| 47 | .183 834 | 13.62 | .994 877 | .33 | .188 958 | 13.93 | .811 042 | 13 |
| 48 | .184 651 | 13.58 | .994 857 | .32 | .189 794 | 13.92 | .810 206 | 12 |
| 49 | .185 466 | 13.57 | .994 838 | .33 | .190 629 | 13.88 | .809 371 | 11 |
| 50 | 9.186 280 | 13.53 | 9.994 818 | .33 | 9.191 462 | 13.87 | 0.808 538 | 10 |
| 51 | .187 092 | 13.52 | .994 798 | .32 | .192 294 | 13.83 | .807 706 | 9 |
| 52 | .187 903 | 13.48 | .994 779 | .33 | .193 124 | 13.82 | .806 876 | 8 |
| 53 | .188 712 | 13.45 | .994 759 | .33 | .193 953 | 13.78 | .806 047 | 7 |
| 54 | .189 519 | 13.43 | .994 739 | .32 | .194 780 | 13.77 | .805 220 | 6 |
| 55 | 9.190 325 | 13.42 | 9.994 720 | .33 | 9.195 606 | 13.73 | 0.804 394 | 5 |
| 56 | .191 130 | 13.38 | .994 700 | .33 | .196 430 | 13.72 | .803 570 | 4 |
| 57 | .191 933 | 13.35 | .994 680 | .33 | .197 253 | 13.68 | .802 747 | 3 |
| 58 | .192 734 | 13.33 | .994 660 | .33 | .198 074 | 13.67 | .801 926 | 2 |
| 59 | .193 534 | 13.30 | .994 640 | .33 | .198 894 | 13.65 | .801 106 | 1 |
| 60 | 9.194 332 | | 9.994 620 | | 9.199 713 | | 0.800 287 | 0 |
| | Cos. | D. 1". | Sin. | D. 1". | Cot. | D. 1". | Tan. | M. |

LOGARITHMIC SINES, COSINES, TANGENTS, AND COTANGENTS. 27

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| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.194 332 | 13.28 | 9.994 620 | .33 | 9.199 713 | 13.60 | 0.800 287 | 60 |
| 1 | .195 129 | 13.27 | .994 600 | .33 | .200 529 | 13.60 | .799 471 | 59 |
| 2 | .195 925 | 13.23 | .994 580 | .33 | .201 345 | 13.57 | .798 655 | 58 |
| 3 | .196 719 | 13.20 | .994 560 | .33 | .202 159 | 13.53 | .797 841 | 57 |
| 4 | .197 511 | 13.18 | .994 540 | .35 | .202 971 | 13.52 | .797 029 | 56 |
| 5 | 9.198 302 | 13.15 | 9.994 519 | .33 | 9.203 782 | 13.50 | 0.796 218 | 55 |
| 6 | .199 091 | 13.13 | .994 499 | .33 | .204 592 | 13.47 | .795 408 | 54 |
| 7 | .199 879 | 13.12 | .994 479 | .33 | .205 400 | 13.45 | .794 600 | 53 |
| 8 | .200 666 | 13.08 | .994 459 | .33 | .206 207 | 13.43 | .793 793 | 52 |
| 9 | .201 451 | 13.05 | .994 438 | .33 | .207 013 | 13.40 | .792 987 | 51 |
| 10 | 9.202 234 | 13.05 | 9.994 418 | .33 | 9.207 817 | 13.37 | 0.792 183 | 50 |
| 11 | .203 017 | 13.00 | .994 398 | .35 | .208 619 | 13.35 | .791 381 | 49 |
| 12 | .203 797 | 13.00 | .994 377 | .33 | .209 420 | 13.33 | .790 580 | 48 |
| 13 | .204 577 | 12.95 | .994 357 | .35 | .210 220 | 13.30 | .789 780 | 47 |
| 14 | .205 354 | 12.95 | .994 336 | .33 | .211 018 | 13.28 | .788 982 | 46 |
| 15 | 9.206 131 | 12.92 | 9.994 316 | .35 | 9.211 815 | 13.27 | 0.788 185 | 45 |
| 16 | .206 906 | 12.88 | .994 295 | .35 | .212 611 | 13.23 | .787 389 | 44 |
| 17 | .207 679 | 12.88 | .994 274 | .33 | .213 405 | 13.22 | .786 595 | 43 |
| 18 | .208 452 | 12.83 | .994 254 | .33 | .214 198 | 13.18 | .785 802 | 42 |
| 19 | .209 222 | 12.83 | .994 233 | .35 | .214 989 | 13.18 | .785 011 | 41 |
| 20 | 9.209 992 | 12.80 | 9.994 212 | .35 | 9.215 780 | 13.13 | 0.784 220 | 40 |
| 21 | .210 760 | 12.77 | .994 191 | .33 | .216 568 | 13.13 | .783 432 | 39 |
| 22 | .211 526 | 12.75 | .994 171 | .33 | .217 356 | 13.10 | .782 644 | 38 |
| 23 | .212 291 | 12.73 | .994 150 | .35 | .218 142 | 13.07 | .781 858 | 37 |
| 24 | .213 055 | 12.72 | .994 129 | .35 | .218 926 | 13.07 | .781 074 | 36 |
| 25 | 9.213 818 | 12.68 | 9.994 108 | .35 | 9.219 710 | 13.03 | 0.780 290 | 35 |
| 26 | .214 579 | 12.65 | .994 087 | .35 | .220 492 | 13.00 | .779 508 | 34 |
| 27 | .215 338 | 12.65 | .994 066 | .35 | .221 272 | 13.00 | .778 728 | 33 |
| 28 | .216 097 | 12.62 | .994 045 | .35 | .222 052 | 12.97 | .777 948 | 32 |
| 29 | .216 854 | 12.58 | .994 024 | .35 | .222 830 | 12.95 | .777 170 | 31 |
| 30 | 9.217 609 | 12.57 | 9.994 003 | .35 | 9.223 607 | 12.92 | 0.776 393 | 30 |
| 31 | .218 363 | 12.55 | .993 982 | .37 | .224 382 | 12.90 | .775 618 | 29 |
| 32 | .219 116 | 12.53 | .993 960 | .35 | .225 156 | 12.88 | .774 844 | 28 |
| 33 | .219 868 | 12.50 | .993 939 | .35 | .225 929 | 12.85 | .774 071 | 27 |
| 34 | .220 618 | 12.48 | .993 918 | .35 | .226 700 | 12.85 | .773 300 | 26 |
| 35 | 9.221 367 | 12.47 | 9.993 897 | .37 | 9.227 471 | 12.80 | 0.772 529 | 25 |
| 36 | .222 115 | 12.43 | .993 875 | .35 | .228 239 | 12.80 | .771 761 | 24 |
| 37 | .222 861 | 12.42 | .993 854 | .35 | .229 007 | 12.77 | .770 993 | 23 |
| 38 | .223 606 | 12.38 | .993 832 | .37 | .229 773 | 12.77 | .770 227 | 22 |
| 39 | .224 349 | 12.38 | .993 811 | .35 | .230 539 | 12.72 | .769 461 | 21 |
| 40 | 9.225 092 | 12.35 | 9.993 789 | .35 | 9.231 302 | 12.72 | 0.768 698 | 20 |
| 41 | .225 833 | 12.33 | .993 768 | .35 | .232 065 | 12.68 | .767 935 | 19 |
| 42 | .226 573 | 12.30 | .993 746 | .37 | .232 826 | 12.67 | .767 174 | 18 |
| 43 | .227 311 | 12.28 | .993 725 | .35 | .233 586 | 12.65 | .766 414 | 17 |
| 44 | .228 048 | 12.27 | .993 703 | .37 | .234 345 | 12.63 | .765 655 | 16 |
| 45 | 9.228 784 | 12.23 | 9.993 681 | .35 | 9.235 103 | 12.60 | 0.764 897 | 15 |
| 46 | .229 518 | 12.23 | .993 660 | .35 | .235 859 | 12.58 | .764 141 | 14 |
| 47 | .230 252 | 12.20 | .993 638 | .37 | .236 614 | 12.57 | .763 386 | 13 |
| 48 | .230 984 | 12.18 | .993 616 | .37 | .237 368 | 12.53 | .762 632 | 12 |
| 49 | .231 715 | 12.15 | .993 594 | .37 | .238 120 | 12.53 | .761 880 | 11 |
| 50 | 9.232 444 | 12.13 | 9.993 572 | .37 | 9.238 872 | 12.50 | 0.761 128 | 10 |
| 51 | .233 172 | 12.12 | .993 550 | .37 | .239 622 | 12.48 | .760 378 | 9 |
| 52 | .233 899 | 12.10 | .993 528 | .37 | .240 371 | 12.45 | .759 629 | 8 |
| 53 | .234 625 | 12.07 | .993 506 | .37 | .241 118 | 12.45 | .758 882 | 7 |
| 54 | .235 349 | 12.07 | .993 484 | .37 | .241 865 | 12.42 | .758 135 | 6 |
| 55 | 9.236 073 | 12.03 | 9.993 462 | .37 | 9.242 610 | 12.40 | 0.757 390 | 5 |
| 56 | .236 795 | 12.00 | .993 440 | .37 | .243 354 | 12.38 | .756 646 | 4 |
| 57 | .237 515 | 12.00 | .993 418 | .37 | .244 097 | 12.37 | .755 903 | 3 |
| 58 | .238 235 | 11.97 | .993 396 | .37 | .244 839 | 12.33 | .755 161 | 2 |
| 59 | .238 953 | 11.95 | .993 374 | .38 | .245 579 | 12.33 | .754 421 | 1 |
| 60 | 9.239 670 | | 9.993 351 | | 9.246 319 | | 0.753 681 | 0 |

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.239 670 | 11.93 | 9.993 351 | .37 | 9.246 319 | 12.30 | 0.753 681 | 60 |
| 1 | .240 386 | 11.92 | .993 329 | .37 | .247 057 | 12.28 | .752 943 | 59 |
| 2 | .241 101 | 11.88 | .993 307 | .38 | .247 794 | 12.27 | .752 206 | 58 |
| 3 | .241 814 | 11.87 | .993 284 | .38 | .248 530 | 12.23 | .751 470 | 57 |
| 4 | .242 526 | 11.85 | .993 262 | .37 | .249 264 | 12.23 | .750 736 | 56 |
| 5 | 9.243 237 | 11.83 | 9.993 240 | .38 | 9.249 998 | 12.20 | 0.750 002 | 55 |
| 6 | .243 947 | 11.82 | .993 217 | .38 | .250 730 | 12.18 | .749 270 | 54 |
| 7 | .244 656 | 11.78 | .993 195 | .37 | .251 461 | 12.17 | .748 539 | 53 |
| 8 | .245 363 | 11.77 | .993 172 | .38 | .252 191 | 12.15 | .747 809 | 52 |
| 9 | .246 069 | 11.77 | .993 149 | .38 | .252 920 | 12.13 | .747 080 | 51 |
| 10 | 9.246 775 | 11.72 | 9.993 127 | .38 | 9.253 648 | 12.10 | 0.746 352 | 50 |
| 11 | .247 478 | 11.72 | .993 104 | .38 | .254 374 | 12.10 | .745 626 | 49 |
| 12 | .248 181 | 11.70 | .993 081 | .38 | .255 100 | 12.07 | .744 900 | 48 |
| 13 | .248 883 | 11.67 | .993 059 | .37 | .255 824 | 12.05 | .744 176 | 47 |
| 14 | .249 583 | 11.65 | .993 036 | .38 | .256 547 | 12.03 | .743 453 | 46 |
| 15 | 9.250 282 | 11.63 | 9.993 013 | .38 | 9.257 269 | 12.02 | 0.742 731 | 45 |
| 16 | .250 980 | 11.62 | .992 990 | .38 | .257 990 | 12.00 | .742 010 | 44 |
| 17 | .251 677 | 11.60 | .992 967 | .38 | .258 710 | 11.98 | .741 290 | 43 |
| 18 | .252 373 | 11.57 | .992 944 | .38 | .259 429 | 11.95 | .740 571 | 42 |
| 19 | .253 067 | 11.57 | .992 921 | .38 | .260 146 | 11.95 | .739 854 | 41 |
| 20 | 9.253 761 | 11.53 | 9.992 898 | .38 | 9.260 863 | 11.92 | 0.739 137 | 40 |
| 21 | .254 453 | 11.52 | .992 875 | .38 | .261 578 | 11.90 | .738 422 | 39 |
| 22 | .255 144 | 11.50 | .992 852 | .38 | .262 292 | 11.88 | .737 708 | 38 |
| 23 | .255 834 | 11.48 | .992 829 | .38 | .263 005 | 11.87 | .736 995 | 37 |
| 24 | .256 523 | 11.47 | .992 806 | .38 | .263 717 | 11.85 | .736 283 | 36 |
| 25 | 9.257 211 | 11.45 | 9.992 783 | .40 | 9.264 428 | 11.83 | 0.735 572 | 35 |
| 26 | .257 898 | 11.42 | .992 759 | .38 | .265 138 | 11.82 | .734 862 | 34 |
| 27 | .258 583 | 11.42 | .992 736 | .38 | .265 847 | 11.80 | .734 153 | 33 |
| 28 | .259 268 | 11.38 | .992 713 | .38 | .266 555 | 11.77 | .733 445 | 32 |
| 29 | .259 951 | 11.37 | .992 690 | .40 | .267 261 | 11.77 | .732 739 | 31 |
| 30 | 9.260 633 | 11.35 | 9.992 666 | .38 | 9.267 967 | 11.73 | 0.732 033 | 30 |
| 31 | .261 314 | 11.33 | .992 643 | .40 | .268 671 | 11.73 | .731 329 | 29 |
| 32 | .261 994 | 11.32 | .992 619 | .38 | .269 375 | 11.70 | .730 625 | 28 |
| 33 | .262 673 | 11.30 | .992 596 | .40 | .270 077 | 11.70 | .729 923 | 27 |
| 34 | .263 351 | 11.27 | .992 572 | .38 | .270 779 | 11.67 | .729 221 | 26 |
| 35 | 9.264 027 | 11.27 | 9.992 549 | .40 | 9.271 479 | 11.65 | 0.728 521 | 25 |
| 36 | .264 703 | 11.23 | .992 525 | .40 | .272 178 | 11.63 | .727 822 | 24 |
| 37 | .265 377 | 11.23 | .992 501 | .40 | .272 876 | 11.62 | .727 124 | 23 |
| 38 | .266 051 | 11.20 | .992 478 | .38 | .273 573 | 11.60 | .726 427 | 22 |
| 39 | .266 723 | 11.20 | .992 454 | .40 | .274 269 | 11.58 | .725 731 | 21 |
| 40 | 9.267 395 | 11.17 | 9.992 430 | .40 | 9.274 964 | 11.57 | 0.725 036 | 20 |
| 41 | .268 065 | 11.15 | .992 406 | .40 | .275 658 | 11.55 | .724 342 | 19 |
| 42 | .268 734 | 11.13 | .992 382 | .38 | .276 351 | 11.53 | .723 649 | 18 |
| 43 | .269 402 | 11.12 | .992 359 | .38 | .277 043 | 11.52 | .722 957 | 17 |
| 44 | .270 069 | 11.10 | .992 335 | .40 | .277 734 | 11.50 | .722 266 | 16 |
| 45 | 9.270 735 | 11.08 | 9.992 311 | .40 | 9.278 424 | 11.48 | 0.721 576 | 15 |
| 46 | .271 400 | 11.07 | .992 287 | .40 | .279 113 | 11.47 | .720 887 | 14 |
| 47 | .272 064 | 11.03 | .992 263 | .40 | .279 801 | 11.45 | .720 199 | 13 |
| 48 | .272 726 | 11.03 | .992 239 | .40 | .280 488 | 11.43 | .719 512 | 12 |
| 49 | .273 388 | 11.02 | .992 214 | .40 | .281 174 | 11.40 | .718 826 | 11 |
| 50 | 9.274 049 | 10.98 | 9.992 190 | .40 | 9.281 858 | 11.40 | 0.718 142 | 10 |
| 51 | .274 708 | 10.98 | .992 166 | .40 | .282 542 | 11.38 | .717 458 | 9 |
| 52 | .275 367 | 10.97 | .992 142 | .40 | .283 225 | 11.37 | .716 775 | 8 |
| 53 | .276 025 | 10.93 | .992 118 | .42 | .283 907 | 11.35 | .716 093 | 7 |
| 54 | .276 681 | 10.93 | .992 093 | .40 | .284 588 | 11.33 | .715 412 | 6 |
| 55 | 9.277 337 | 10.90 | 9.992 069 | .42 | 9.285 268 | 11.32 | 0.714 732 | 5 |
| 56 | .277 991 | 10.90 | .992 044 | .40 | .285 947 | 11.28 | .714 053 | 4 |
| 57 | .278 645 | 10.87 | .992 020 | .40 | .286 624 | 11.28 | .713 370 | 3 |
| 58 | .279 297 | 10.85 | .991 996 | .42 | .287 301 | 11.27 | .712 699 | 2 |
| 59 | .279 948 | 10.85 | .991 971 | .40 | .287 977 | 11.25 | .712 023 | 1 |
| 60 | 9.280 599 | | 9.991 947 | | 9.288 652 | | 0.711 348 | 0 |

| | Cos. | D. 1". | Sin. | D. 1". | Cot. | D. 1". | Tan. | M. |
|--|------|--------|------|--------|------|--------|------|----|
|--|------|--------|------|--------|------|--------|------|----|

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.280 599 | 10.82 | 9.991 947 | | 9.288 652 | | 0.711 348 | 60 |
| 1 | .281 248 | 10.82 | .991 922 | -42 | .289 326 | 11.23 | .710 674 | 59 |
| 2 | .281 897 | 10.78 | .991 897 | -42 | .289 999 | 11.22 | .710 001 | 58 |
| 3 | .282 544 | 10.77 | .991 873 | -42 | .290 671 | 11.20 | .709 329 | 57 |
| 4 | .283 190 | 10.77 | .991 848 | -42 | .291 342 | 11.18 | .708 658 | 56 |
| 5 | 9.283 836 | 10.73 | 9.991 823 | -40 | 9.292 013 | 11.15 | 0.707 987 | 55 |
| 6 | .284 480 | 10.73 | .991 799 | -42 | .292 682 | 11.13 | .707 318 | 54 |
| 7 | .285 124 | 10.70 | .991 774 | -42 | .293 350 | 11.12 | .706 650 | 53 |
| 8 | .285 766 | 10.70 | .991 749 | -42 | .294 017 | 11.12 | .705 983 | 52 |
| 9 | .286 408 | 10.67 | .991 724 | -42 | .294 684 | 11.08 | .705 316 | 51 |
| 10 | 9.287 048 | 10.67 | 9.991 699 | -42 | 9.295 349 | 11.07 | 0.704 651 | 50 |
| 11 | .287 688 | 10.63 | .991 674 | -42 | .296 013 | 11.07 | .703 987 | 49 |
| 12 | .288 326 | 10.63 | .991 649 | -42 | .296 677 | 11.03 | .703 323 | 48 |
| 13 | .288 964 | 10.60 | .991 624 | -42 | .297 339 | 11.03 | .702 661 | 47 |
| 14 | .289 600 | 10.60 | .991 599 | -42 | .298 001 | 11.02 | .701 999 | 46 |
| 15 | 9.290 236 | 10.57 | 9.991 574 | -42 | 9.298 662 | 11.00 | 0.701 338 | 45 |
| 16 | .290 870 | 10.57 | .991 549 | -42 | .299 322 | 10.97 | .700 678 | 44 |
| 17 | .291 504 | 10.55 | .991 524 | -43 | .299 980 | 10.97 | .700 020 | 43 |
| 18 | .292 137 | 10.52 | .991 498 | -42 | .300 638 | 10.95 | .699 362 | 42 |
| 19 | .292 768 | 10.52 | .991 473 | -42 | .301 295 | 10.93 | .698 705 | 41 |
| 20 | 9.293 399 | 10.50 | 9.991 448 | -43 | 9.301 951 | 10.93 | 0.698 049 | 40 |
| 21 | .294 029 | 10.48 | .991 422 | -42 | .302 607 | 10.90 | .697 393 | 39 |
| 22 | .294 658 | 10.47 | .991 397 | -42 | .303 261 | 10.88 | .696 739 | 38 |
| 23 | .295 286 | 10.45 | .991 372 | -42 | .303 914 | 10.88 | .696 086 | 37 |
| 24 | .295 913 | 10.43 | .991 346 | -42 | .304 567 | 10.85 | .695 433 | 36 |
| 25 | 9.296 539 | 10.42 | 9.991 321 | -43 | 9.305 218 | 10.85 | 0.694 782 | 35 |
| 26 | .297 164 | 10.40 | .991 295 | -42 | .305 869 | 10.83 | .694 131 | 34 |
| 27 | .297 788 | 10.40 | .991 270 | -42 | .306 510 | 10.82 | .693 481 | 33 |
| 28 | .298 412 | 10.37 | .991 244 | -43 | .307 168 | 10.80 | .692 832 | 32 |
| 29 | .299 034 | 10.35 | .991 218 | -42 | .307 816 | 10.78 | .692 184 | 31 |
| 30 | 9.299 655 | 10.35 | 9.991 193 | -43 | 9.308 463 | 10.77 | 0.691 537 | 30 |
| 31 | .300 276 | 10.32 | .991 167 | -43 | .309 109 | 10.75 | .690 891 | 29 |
| 32 | .300 895 | 10.32 | .991 141 | -43 | .309 754 | 10.75 | .690 246 | 28 |
| 33 | .301 514 | 10.30 | .991 115 | -42 | .310 399 | 10.72 | .689 601 | 27 |
| 34 | .302 132 | 10.27 | .991 090 | -43 | .311 042 | 10.72 | .688 958 | 26 |
| 35 | 9.302 748 | 10.27 | 9.991 064 | -43 | 9.311 685 | 10.70 | 0.688 315 | 25 |
| 35 | .303 364 | 10.25 | .991 038 | -43 | .312 327 | 10.68 | .687 673 | 24 |
| 37 | .303 979 | 10.23 | .991 012 | -43 | .312 968 | 10.67 | .687 032 | 23 |
| 38 | .304 593 | 10.23 | .990 986 | -43 | .313 608 | 10.65 | .686 392 | 22 |
| 39 | .305 207 | 10.20 | .990 960 | -43 | .314 247 | 10.63 | .685 753 | 21 |
| 40 | 9.305 819 | 10.18 | 9.990 934 | -43 | 9.314 885 | 10.63 | 0.685 115 | 20 |
| 41 | .306 430 | 10.18 | .990 908 | -43 | .315 523 | 10.60 | .684 477 | 19 |
| 42 | .307 041 | 10.15 | .990 882 | -43 | .316 159 | 10.60 | .683 841 | 18 |
| 43 | .307 650 | 10.15 | .990 855 | -45 | .316 795 | 10.58 | .683 205 | 17 |
| 44 | .308 259 | 10.13 | .990 829 | -43 | .317 430 | 10.57 | .682 570 | 16 |
| 45 | 9.308 867 | 10.12 | 9.990 803 | -43 | 9.318 064 | 10.55 | 0.681 936 | 15 |
| 46 | .309 474 | 10.10 | .990 777 | -45 | .318 697 | 10.55 | .681 303 | 14 |
| 47 | .310 080 | 10.08 | .990 750 | -43 | .319 330 | 10.52 | .680 670 | 13 |
| 48 | .310 685 | 10.07 | .990 724 | -43 | .319 961 | 10.52 | .680 039 | 12 |
| 49 | .311 289 | 10.07 | .990 697 | -43 | .320 592 | 10.50 | .679 408 | 11 |
| 50 | 9.311 893 | 10.03 | 9.990 671 | -43 | 9.321 222 | 10.48 | 0.678 778 | 10 |
| 51 | .312 495 | 10.03 | .990 645 | -45 | .321 851 | 10.47 | .678 149 | 9 |
| 52 | .313 097 | 10.02 | .990 618 | -45 | .322 479 | 10.45 | .677 521 | 8 |
| 53 | .313 698 | 9.98 | .990 591 | -43 | .323 106 | 10.45 | .676 894 | 7 |
| 54 | .314 297 | 10.00 | .990 565 | -45 | .323 733 | 10.42 | .676 267 | 6 |
| 55 | 9.314 897 | 9.97 | 9.990 538 | -45 | 9.324 358 | 10.42 | 0.675 642 | 5 |
| 55 | .315 495 | 9.95 | .990 511 | -43 | .324 983 | 10.40 | .675 017 | 4 |
| 57 | .316 092 | 9.95 | .990 485 | -45 | .325 607 | 10.40 | .674 393 | 3 |
| 58 | .316 689 | 9.92 | .990 458 | -45 | .326 231 | 10.37 | .673 769 | 2 |
| 59 | .317 284 | 9.92 | .990 431 | -45 | .326 853 | 10.37 | .673 147 | 1 |
| 60 | 9.317 879 | | 9.990 404 | | 9.327 475 | | 0.672 525 | 0 |

30 LOGARITHMIC SINES, COSINES, TANGENTS, AND COTANGENTS.

12°

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.317 879 | | 9.990 404 | | 9.327 475 | | 0.672 525 | 60 |
| 1 | .318 473 | 9.90 | .990 378 | .43 | .328 095 | 10.33 | .671 905 | 59 |
| 2 | .319 066 | 9.88 | .990 351 | .45 | .328 715 | 10.33 | .671 285 | 58 |
| 3 | .319 658 | 9.87 | .990 324 | .45 | .329 334 | 10.32 | .670 666 | 57 |
| 4 | .320 249 | 9.85 | .990 297 | .45 | .329 953 | 10.32 | .670 047 | 56 |
| 5 | 9.320 840 | 9.83 | 9.990 270 | | 9.330 570 | 10.28 | 0.669 430 | 55 |
| 6 | .321 430 | 9.82 | .990 243 | .45 | .331 187 | 10.27 | .668 813 | 54 |
| 7 | .322 019 | 9.80 | .990 215 | .45 | .331 803 | 10.25 | .668 197 | 53 |
| 8 | .322 607 | 9.78 | .990 188 | .45 | .332 418 | 10.25 | .667 582 | 52 |
| 9 | .323 194 | 9.77 | .990 161 | .45 | .333 033 | 10.22 | .666 967 | 51 |
| 10 | 9.323 780 | 9.77 | 9.990 134 | | 9.333 646 | 10.22 | 0.666 354 | 50 |
| 11 | .324 366 | 9.73 | .990 107 | .45 | .334 259 | 10.20 | .665 741 | 49 |
| 12 | .324 950 | 9.73 | .990 079 | .47 | .334 871 | 10.18 | .665 129 | 48 |
| 13 | .325 534 | 9.72 | .990 052 | .45 | .335 482 | 10.18 | .664 518 | 47 |
| 14 | .326 117 | 9.72 | .990 025 | .47 | .336 093 | 10.15 | .663 907 | 46 |
| 15 | 9.326 700 | 9.68 | 9.989 997 | | 9.336 702 | 10.15 | 0.663 298 | 45 |
| 16 | .327 281 | 9.68 | .989 970 | .45 | .337 311 | 10.13 | .662 689 | 44 |
| 17 | .327 862 | 9.67 | .989 942 | .47 | .337 919 | 10.13 | .662 081 | 43 |
| 18 | .328 442 | 9.65 | .989 915 | .45 | .338 527 | 10.10 | .661 473 | 42 |
| 19 | .329 021 | 9.63 | .989 887 | .47 | .339 133 | 10.10 | .660 867 | 41 |
| 20 | 9.329 599 | 9.62 | 9.989 860 | | 9.339 739 | 10.08 | 0.660 261 | 40 |
| 21 | .330 176 | 9.62 | .989 832 | .47 | .340 344 | 10.07 | .659 656 | 39 |
| 22 | .330 753 | 9.60 | .989 804 | .47 | .340 948 | 10.07 | .659 052 | 38 |
| 23 | .331 329 | 9.57 | .989 777 | .45 | .341 552 | 10.05 | .658 448 | 37 |
| 24 | .331 903 | 9.58 | .989 749 | .47 | .342 155 | 10.03 | .657 845 | 36 |
| 25 | 9.332 478 | 9.55 | 9.989 721 | | 9.342 757 | 10.02 | 0.657 243 | 35 |
| 26 | .333 051 | 9.55 | .989 693 | .47 | .343 358 | 10.00 | .656 642 | 34 |
| 27 | .333 624 | 9.52 | .989 665 | .47 | .343 958 | 10.00 | .656 042 | 33 |
| 28 | .334 195 | 9.52 | .989 637 | .47 | .344 558 | 9.98 | .655 442 | 32 |
| 29 | .334 767 | 9.50 | .989 610 | .45 | .345 157 | 9.97 | .654 843 | 31 |
| 30 | 9.335 337 | 9.48 | 9.989 582 | | 9.345 755 | 9.97 | 0.654 245 | 30 |
| 31 | .335 906 | 9.48 | .989 553 | .48 | .346 353 | 9.93 | .653 647 | 29 |
| 32 | .336 475 | 9.47 | .989 525 | .47 | .346 949 | 9.93 | .653 051 | 28 |
| 33 | .337 043 | 9.45 | .989 497 | .47 | .347 545 | 9.93 | .652 455 | 27 |
| 34 | .337 610 | 9.43 | .989 469 | .47 | .348 141 | 9.90 | .651 859 | 26 |
| 35 | 9.338 176 | 9.43 | 9.989 441 | | 9.348 735 | 9.90 | 0.651 265 | 25 |
| 36 | .338 742 | 9.42 | .989 413 | .47 | .349 329 | 9.88 | .650 671 | 24 |
| 37 | .339 307 | 9.40 | .989 385 | .47 | .349 922 | 9.87 | .650 078 | 23 |
| 38 | .339 871 | 9.38 | .989 356 | .48 | .350 514 | 9.87 | .649 486 | 22 |
| 39 | .340 434 | 9.37 | .989 328 | .47 | .351 106 | 9.85 | .648 894 | 21 |
| 40 | 9.340 996 | 9.37 | 9.989 300 | | 9.351 697 | 9.83 | 0.648 303 | 20 |
| 41 | .341 558 | 9.35 | .989 271 | .48 | .352 287 | 9.82 | .647 713 | 19 |
| 42 | .342 119 | 9.33 | .989 243 | .47 | .352 876 | 9.82 | .647 124 | 18 |
| 43 | .342 679 | 9.33 | .989 214 | .48 | .353 465 | 9.80 | .646 535 | 17 |
| 44 | .343 239 | 9.30 | .989 186 | .47 | .354 053 | 9.78 | .645 947 | 16 |
| 45 | 9.343 797 | 9.30 | 9.989 157 | | 9.354 640 | 9.78 | 0.645 360 | 15 |
| 46 | .344 355 | 9.28 | .989 128 | .48 | .355 227 | 9.77 | .644 773 | 14 |
| 47 | .344 912 | 9.28 | .989 100 | .47 | .355 813 | 9.75 | .644 187 | 13 |
| 48 | .345 469 | 9.25 | .989 071 | .48 | .356 398 | 9.73 | .643 602 | 12 |
| 49 | .346 024 | 9.25 | .989 042 | .47 | .356 982 | 9.73 | .643 018 | 11 |
| 50 | 9.346 579 | 9.25 | 9.989 014 | | 9.357 566 | 9.72 | 0.642 434 | 10 |
| 51 | .347 134 | 9.22 | .988 985 | .48 | .358 149 | 9.70 | .641 851 | 9 |
| 52 | .347 687 | 9.22 | .988 956 | .48 | .358 731 | 9.70 | .641 269 | 8 |
| 53 | .348 240 | 9.20 | .988 927 | .48 | .359 313 | 9.67 | .640 687 | 7 |
| 54 | .348 792 | 9.18 | .988 898 | .48 | .359 893 | 9.68 | .640 107 | 6 |
| 55 | 9.349 343 | 9.17 | 9.988 869 | | 9.360 474 | 9.65 | 0.639 526 | 5 |
| 56 | .349 893 | 9.17 | .988 840 | .48 | .361 053 | 9.65 | .638 947 | 4 |
| 57 | .350 443 | 9.15 | .988 811 | .48 | .361 632 | 9.63 | .638 368 | 3 |
| 58 | .350 992 | 9.13 | .988 782 | .48 | .362 210 | 9.62 | .637 790 | 2 |
| 59 | .351 540 | 9.13 | .988 753 | .48 | .362 787 | 9.62 | .637 213 | 1 |
| 60 | 9.352 088 | | 9.988 724 | | 9.363 364 | | 0.636 636 | 0 |
| | Cos. | D. 1". | Sin. | D. 1". | Cot. | D. 1". | Tan. | M. |

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.352 088 | 9.12 | 9.988 724 | .48 | 9.363 364 | 9.60 | 0.636 636 | 60 |
| 1 | .352 635 | 9.10 | .988 695 | .48 | .363 940 | 9.58 | .636 060 | 59 |
| 2 | .353 181 | 9.08 | .988 666 | .50 | .364 515 | 9.58 | .635 485 | 58 |
| 3 | .353 726 | 9.08 | .988 636 | .48 | .365 090 | 9.57 | .634 910 | 57 |
| 4 | .354 271 | 9.07 | .988 607 | .48 | .365 664 | 9.55 | .634 336 | 56 |
| 5 | 9.354 815 | 9.05 | 9.988 578 | .50 | 9.366 237 | 9.55 | 0.633 763 | 55 |
| 6 | .355 358 | 9.05 | .988 548 | .48 | .366 810 | 9.53 | .633 190 | 54 |
| 7 | .355 901 | 9.03 | .988 519 | .48 | .367 382 | 9.53 | .632 618 | 53 |
| 8 | .356 443 | 9.02 | .988 489 | .50 | .367 953 | 9.52 | .632 047 | 52 |
| 9 | .356 984 | 9.00 | .988 460 | .50 | .368 524 | 9.50 | .631 476 | 51 |
| 10 | 9.357 524 | 9.00 | 9.988 430 | .48 | 9.369 095 | 9.48 | 0.630 906 | 50 |
| 11 | .358 064 | 8.98 | .988 401 | .50 | .369 663 | 9.48 | .630 337 | 49 |
| 12 | .358 603 | 8.97 | .988 371 | .48 | .370 232 | 9.45 | .629 768 | 48 |
| 13 | .359 141 | 8.95 | .988 342 | .48 | .370 799 | 9.45 | .629 201 | 47 |
| 14 | .359 678 | 8.95 | .988 312 | .50 | .371 367 | 9.47 | .628 633 | 46 |
| 15 | 9.360 215 | 8.95 | 9.988 282 | .50 | 9.371 933 | 9.43 | 0.628 067 | 45 |
| 16 | .360 752 | 8.92 | .988 252 | .48 | .372 499 | 9.42 | .627 501 | 44 |
| 17 | .361 287 | 8.92 | .988 223 | .50 | .373 064 | 9.42 | .626 936 | 43 |
| 18 | .361 822 | 8.90 | .988 193 | .50 | .373 629 | 9.40 | .626 371 | 42 |
| 19 | .362 356 | 8.88 | .988 163 | .50 | .374 193 | 9.38 | .625 807 | 41 |
| 20 | 9.362 889 | 8.88 | 9.988 133 | .50 | 9.374 756 | 9.38 | 0.625 244 | 40 |
| 21 | .363 422 | 8.87 | .988 103 | .50 | .375 319 | 9.37 | .624 681 | 39 |
| 22 | .363 954 | 8.85 | .988 073 | .50 | .375 881 | 9.35 | .624 119 | 38 |
| 23 | .364 485 | 8.85 | .988 043 | .50 | .376 442 | 9.35 | .623 558 | 37 |
| 24 | .365 016 | 8.83 | .988 013 | .50 | .377 003 | 9.33 | .622 997 | 36 |
| 25 | 9.365 546 | 8.82 | 9.987 983 | .50 | 9.377 563 | 9.32 | 0.622 437 | 35 |
| 26 | .366 075 | 8.82 | .987 953 | .52 | .378 122 | 9.32 | .621 878 | 34 |
| 27 | .366 604 | 8.78 | .987 922 | .50 | .378 681 | 9.30 | .621 319 | 33 |
| 28 | .367 131 | 8.80 | .987 892 | .50 | .379 239 | 9.30 | .620 761 | 32 |
| 29 | .367 659 | 8.77 | .987 862 | .50 | .379 797 | 9.28 | .620 203 | 31 |
| 30 | 9.368 185 | 8.77 | 9.987 832 | .52 | 9.380 354 | 9.27 | 0.619 646 | 30 |
| 31 | .368 711 | 8.75 | .987 801 | .50 | .380 910 | 9.27 | .619 090 | 29 |
| 32 | .369 236 | 8.75 | .987 771 | .50 | .381 466 | 9.25 | .618 534 | 28 |
| 33 | .369 761 | 8.73 | .987 740 | .52 | .382 020 | 9.25 | .617 980 | 27 |
| 34 | .370 285 | 8.72 | .987 710 | .52 | .382 575 | 9.23 | .617 425 | 26 |
| 35 | 9.370 808 | 8.70 | 9.987 679 | .50 | 9.383 129 | 9.22 | 0.616 871 | 25 |
| 36 | .371 330 | 8.70 | .987 649 | .52 | .383 682 | 9.20 | .616 318 | 24 |
| 37 | .371 852 | 8.68 | .987 618 | .50 | .384 234 | 9.20 | .615 766 | 23 |
| 38 | .372 373 | 8.68 | .987 588 | .50 | .384 786 | 9.18 | .615 214 | 22 |
| 39 | .372 894 | 8.67 | .987 557 | .52 | .385 337 | 9.18 | .614 663 | 21 |
| 40 | 9.373 414 | 8.65 | 9.987 526 | .50 | 9.385 888 | 9.17 | 0.614 112 | 20 |
| 41 | .373 933 | 8.65 | .987 496 | .52 | .386 438 | 9.15 | .613 562 | 19 |
| 42 | .374 452 | 8.63 | .987 465 | .52 | .386 987 | 9.15 | .613 013 | 18 |
| 43 | .374 970 | 8.62 | .987 434 | .52 | .387 536 | 9.13 | .612 464 | 17 |
| 44 | .375 487 | 8.60 | .987 403 | .52 | .388 084 | 9.12 | .611 916 | 16 |
| 45 | 9.376 003 | 8.60 | 9.987 372 | .52 | 9.388 631 | 9.12 | 0.611 369 | 15 |
| 46 | .376 519 | 8.60 | .987 341 | .52 | .389 178 | 9.10 | .610 822 | 14 |
| 47 | .377 035 | 8.57 | .987 310 | .52 | .389 724 | 9.10 | .610 276 | 13 |
| 48 | .377 549 | 8.57 | .987 279 | .52 | .390 270 | 9.08 | .609 730 | 12 |
| 49 | .378 063 | 8.57 | .987 248 | .52 | .390 815 | 9.08 | .609 185 | 11 |
| 50 | 9.378 577 | 8.53 | 9.987 217 | .52 | 9.391 360 | 9.05 | 0.608 640 | 10 |
| 51 | .379 089 | 8.53 | .987 186 | .52 | .391 903 | 9.07 | .608 097 | 9 |
| 52 | .379 601 | 8.53 | .987 155 | .52 | .392 447 | 9.03 | .607 553 | 8 |
| 53 | .380 113 | 8.52 | .987 124 | .53 | .392 989 | 9.03 | .607 011 | 7 |
| 54 | .380 624 | 8.50 | .987 092 | .52 | .393 531 | 9.03 | .606 469 | 6 |
| 55 | 9.381 134 | 8.48 | 9.987 061 | .52 | 9.394 073 | 9.02 | 0.605 927 | 5 |
| 56 | .381 643 | 8.48 | .987 030 | .52 | .394 614 | 9.00 | .605 386 | 4 |
| 57 | .382 152 | 8.48 | .986 998 | .53 | .395 154 | 9.00 | .604 846 | 3 |
| 58 | .382 661 | 8.45 | .986 967 | .52 | .395 694 | 8.98 | .604 306 | 2 |
| 59 | .383 168 | 8.45 | .986 936 | .53 | .396 233 | 8.97 | .603 767 | 1 |
| 60 | 9.383 675 | | 9.986 904 | | 9.396 771 | | 0.603 229 | 0 |

32 LOGARITHMIC SINES, COSINES, TANGENTS, AND COTANGENTS.

14°

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.383 675 | | 9.986 904 | | 9.396 771 | | 0.603 229 | 60 |
| 1 | .384 182 | 8.45 | .986 873 | .52 | .397 309 | 8.97 | .602 691 | 59 |
| 2 | .384 687 | 8.42 | .986 841 | .53 | .397 846 | 8.95 | .602 154 | 58 |
| 3 | .385 192 | 8.42 | .986 809 | .53 | .398 383 | 8.93 | .601 617 | 57 |
| 4 | .385 697 | 8.40 | .986 778 | .53 | .398 919 | 8.93 | .601 081 | 56 |
| 5 | 9.386 201 | 8.38 | 9.986 746 | .53 | 9.399 455 | 8.92 | 0.600 545 | 55 |
| 6 | .386 704 | 8.38 | .986 714 | .53 | .399 990 | 8.90 | .600 010 | 54 |
| 7 | .387 207 | 8.37 | .986 683 | .52 | .400 524 | 8.90 | .599 476 | 53 |
| 8 | .387 709 | 8.35 | .986 651 | .53 | .401 058 | 8.88 | .598 942 | 52 |
| 9 | .388 210 | 8.35 | .986 619 | .53 | .401 591 | 8.88 | .598 409 | 51 |
| 10 | 9.388 711 | 8.33 | 9.986 587 | .53 | 9.402 124 | 8.87 | 0.597 876 | 50 |
| 11 | .389 211 | 8.33 | .986 555 | .53 | .402 656 | 8.85 | .597 344 | 49 |
| 12 | .389 711 | 8.32 | .986 523 | .53 | .403 187 | 8.85 | .596 813 | 48 |
| 13 | .390 210 | 8.30 | .986 491 | .53 | .403 718 | 8.85 | .596 282 | 47 |
| 14 | .390 708 | 8.30 | .986 459 | .53 | .404 249 | 8.82 | .595 751 | 46 |
| 15 | 9.391 206 | 8.28 | 9.986 427 | .53 | 9.404 778 | 8.83 | 0.595 222 | 45 |
| 16 | .391 703 | 8.27 | .986 395 | .53 | .405 308 | 8.80 | .594 692 | 44 |
| 17 | .392 199 | 8.27 | .986 363 | .53 | .405 836 | 8.80 | .594 164 | 43 |
| 18 | .392 695 | 8.27 | .986 331 | .53 | .406 364 | 8.80 | .593 636 | 42 |
| 19 | .393 191 | 8.23 | .986 299 | .53 | .406 892 | 8.78 | .593 108 | 41 |
| 20 | 9.393 685 | 8.23 | 9.986 266 | .53 | 9.407 419 | 8.77 | 0.592 581 | 40 |
| 21 | .394 179 | 8.23 | .986 234 | .53 | .407 945 | 8.77 | .592 055 | 39 |
| 22 | .394 673 | 8.22 | .986 202 | .53 | .408 471 | 8.75 | .591 529 | 38 |
| 23 | .395 166 | 8.20 | .986 169 | .55 | .408 996 | 8.75 | .591 004 | 37 |
| 24 | .395 658 | 8.20 | .986 137 | .55 | .409 521 | 8.73 | .590 479 | 36 |
| 25 | 9.396 150 | 8.18 | 9.986 104 | .53 | 9.410 045 | 8.73 | 0.589 955 | 35 |
| 26 | .396 641 | 8.18 | .986 072 | .55 | .410 569 | 8.72 | .589 431 | 34 |
| 27 | .397 132 | 8.15 | .986 039 | .53 | .411 092 | 8.72 | .588 908 | 33 |
| 28 | .397 621 | 8.17 | .986 007 | .55 | .411 615 | 8.70 | .588 385 | 32 |
| 29 | .398 111 | 8.15 | .985 974 | .53 | .412 137 | 8.68 | .587 863 | 31 |
| 30 | 9.398 600 | 8.13 | 9.985 942 | .55 | 9.412 658 | 8.68 | 0.587 342 | 30 |
| 31 | .399 088 | 8.12 | .985 909 | .55 | .413 179 | 8.67 | .586 821 | 29 |
| 32 | .399 575 | 8.12 | .985 876 | .55 | .413 699 | 8.67 | .586 301 | 28 |
| 33 | .400 062 | 8.12 | .985 843 | .55 | .414 219 | 8.65 | .585 781 | 27 |
| 34 | .400 549 | 8.10 | .985 811 | .55 | .414 738 | 8.65 | .585 262 | 26 |
| 35 | 9.401 035 | 8.08 | 9.985 778 | .55 | 9.415 257 | 8.63 | 0.584 743 | 25 |
| 36 | .401 520 | 8.08 | .985 745 | .55 | .415 775 | 8.63 | .584 225 | 24 |
| 37 | .402 005 | 8.07 | .985 712 | .55 | .416 293 | 8.62 | .583 707 | 23 |
| 38 | .402 489 | 8.05 | .985 679 | .55 | .416 810 | 8.60 | .583 190 | 22 |
| 39 | .402 972 | 8.05 | .985 646 | .55 | .417 326 | 8.60 | .582 674 | 21 |
| 40 | 9.403 455 | 8.05 | 9.985 613 | .55 | 9.417 842 | 8.60 | 0.582 158 | 20 |
| 41 | .403 938 | 8.03 | .985 580 | .55 | .418 358 | 8.58 | .581 642 | 19 |
| 42 | .404 420 | 8.02 | .985 547 | .55 | .418 873 | 8.57 | .581 127 | 18 |
| 43 | .404 901 | 8.02 | .985 514 | .55 | .419 387 | 8.57 | .580 613 | 17 |
| 44 | .405 382 | 8.00 | .985 480 | .55 | .419 901 | 8.57 | .580 099 | 16 |
| 45 | 9.405 862 | 7.98 | 9.985 447 | .55 | 9.420 415 | 8.53 | 0.579 585 | 15 |
| 46 | .406 341 | 7.98 | .985 414 | .55 | .420 927 | 8.55 | .579 073 | 14 |
| 47 | .406 820 | 7.98 | .985 381 | .55 | .421 440 | 8.53 | .578 560 | 13 |
| 48 | .407 299 | 7.97 | .985 347 | .57 | .421 952 | 8.52 | .578 048 | 12 |
| 49 | .407 777 | 7.95 | .985 314 | .57 | .422 463 | 8.52 | .577 537 | 11 |
| 50 | 9.408 254 | 7.95 | 9.985 280 | .55 | 9.422 974 | 8.50 | 0.577 026 | 10 |
| 51 | .408 731 | 7.93 | .985 247 | .57 | .423 484 | 8.48 | .576 516 | 9 |
| 52 | .409 207 | 7.92 | .985 213 | .55 | .423 993 | 8.50 | .576 007 | 8 |
| 53 | .409 682 | 7.92 | .985 180 | .55 | .424 503 | 8.47 | .575 497 | 7 |
| 54 | .410 157 | 7.92 | .985 146 | .55 | .425 011 | 8.47 | .574 989 | 6 |
| 55 | 9.410 632 | 7.90 | 9.985 113 | .57 | 9.425 519 | 8.47 | 0.574 481 | 5 |
| 56 | .411 106 | 7.88 | .985 079 | .57 | .426 027 | 8.45 | .573 973 | 4 |
| 57 | .411 579 | 7.88 | .985 045 | .57 | .426 534 | 8.45 | .573 466 | 3 |
| 58 | .412 052 | 7.87 | .985 011 | .55 | .427 041 | 8.43 | .572 959 | 2 |
| 59 | .412 524 | 7.87 | .984 978 | .55 | .427 547 | 8.42 | .572 453 | 1 |
| 60 | 9.412 996 | | 9.984 944 | | 9.428 052 | | 0.571 948 | 0 |

Cos. D. 1". Sin. D. 1". Cot. D. 1". Tan. M.

75°

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.412 996 | | 9.984 944 | | 9.428 052 | | 0.571 948 | 60 |
| 1 | .413 497 | 7.85 | .984 910 | .57 | .428 558 | 8.43 | .571 442 | 59 |
| 2 | .413 938 | 7.85 | .984 876 | .57 | .429 062 | 8.40 | .570 938 | 58 |
| 3 | .414 408 | 7.83 | .984 842 | .57 | .429 566 | 8.40 | .570 434 | 57 |
| 4 | .414 878 | 7.83 | .984 808 | .57 | .430 070 | 8.38 | .569 930 | 56 |
| | | 7.82 | | .57 | | | | |
| 5 | 9.415 347 | 7.80 | 9.984 774 | .57 | 9.430 573 | 8.37 | 0.569 427 | 55 |
| 6 | .415 815 | 7.80 | .984 740 | .57 | .431 075 | 8.37 | .568 925 | 54 |
| 7 | .416 283 | 7.80 | .984 706 | .57 | .431 577 | 8.37 | .568 423 | 53 |
| 8 | .416 751 | 7.77 | .984 672 | .57 | .432 079 | 8.35 | .567 921 | 52 |
| 9 | .417 217 | 7.78 | .984 638 | .58 | .432 580 | 8.33 | .567 420 | 51 |
| | | | | .58 | | | | |
| 10 | 9.417 684 | 7.77 | 9.984 603 | .57 | 9.433 080 | 8.33 | 0.566 920 | 50 |
| 11 | .418 150 | 7.75 | .984 569 | .57 | .433 580 | 8.33 | .566 420 | 49 |
| 12 | .418 615 | 7.73 | .984 535 | .58 | .434 080 | 8.32 | .565 920 | 48 |
| 13 | .419 079 | 7.73 | .984 500 | .57 | .434 579 | 8.32 | .565 421 | 47 |
| 14 | .419 544 | 7.72 | .984 466 | .57 | .435 078 | 8.30 | .564 922 | 46 |
| | | | | .57 | | | | |
| 15 | 9.420 007 | 7.72 | 9.984 432 | .58 | 9.435 576 | 8.28 | 0.564 424 | 45 |
| 16 | .420 470 | 7.72 | .984 397 | .57 | .436 073 | 8.28 | .563 927 | 44 |
| 17 | .420 933 | 7.70 | .984 363 | .58 | .436 570 | 8.28 | .563 430 | 43 |
| 18 | .421 395 | 7.70 | .984 328 | .58 | .437 067 | 8.27 | .562 933 | 42 |
| 19 | .421 857 | 7.68 | .984 294 | .57 | .437 563 | 8.27 | .562 437 | 41 |
| | | | | .58 | | | | |
| 20 | 9.422 318 | 7.67 | 9.984 259 | .58 | 9.438 059 | 8.25 | 0.561 941 | 40 |
| 21 | .422 778 | 7.67 | .984 224 | .57 | .438 554 | 8.23 | .561 446 | 39 |
| 22 | .423 238 | 7.65 | .984 190 | .58 | .439 048 | 8.25 | .560 952 | 38 |
| 23 | .423 697 | 7.65 | .984 155 | .58 | .439 543 | 8.22 | .560 457 | 37 |
| 24 | .424 156 | 7.65 | .984 120 | .58 | .440 036 | 8.22 | .559 964 | 36 |
| | | | | .58 | | | | |
| 25 | 9.424 615 | 7.63 | 9.984 085 | .58 | 9.440 529 | 8.22 | 0.559 471 | 35 |
| 26 | .425 073 | 7.62 | .984 050 | .58 | .441 022 | 8.20 | .558 978 | 34 |
| 27 | .425 530 | 7.62 | .984 015 | .57 | .441 514 | 8.20 | .558 486 | 33 |
| 28 | .425 987 | 7.60 | .983 981 | .58 | .442 006 | 8.18 | .557 994 | 32 |
| 29 | .426 443 | 7.60 | .983 946 | .58 | .442 497 | 8.18 | .557 503 | 31 |
| | | | | .58 | | | | |
| 30 | 9.426 899 | 7.58 | 9.983 911 | .60 | 9.442 988 | 8.18 | 0.557 012 | 30 |
| 31 | .427 354 | 7.58 | .983 875 | .58 | .443 479 | 8.15 | .556 521 | 29 |
| 32 | .427 809 | 7.57 | .983 840 | .58 | .443 968 | 8.17 | .556 032 | 28 |
| 33 | .428 263 | 7.57 | .983 805 | .58 | .444 458 | 8.15 | .555 542 | 27 |
| 34 | .428 717 | 7.55 | .983 770 | .58 | .444 947 | 8.13 | .555 053 | 26 |
| | | | | .58 | | | | |
| 35 | 9.429 170 | 7.55 | 9.983 735 | .58 | 9.445 435 | 8.13 | 0.554 565 | 25 |
| 36 | .429 623 | 7.53 | .983 700 | .60 | .445 923 | 8.13 | .554 077 | 24 |
| 37 | .430 075 | 7.53 | .983 664 | .58 | .446 411 | 8.12 | .553 589 | 23 |
| 38 | .430 527 | 7.52 | .983 629 | .58 | .446 898 | 8.10 | .553 102 | 22 |
| 39 | .430 978 | 7.52 | .983 594 | .60 | .447 384 | 8.10 | .552 616 | 21 |
| | | | | .60 | | | | |
| 40 | 9.431 429 | 7.50 | 9.983 558 | .58 | 9.447 870 | 8.10 | 0.552 130 | 20 |
| 41 | .431 879 | 7.50 | .983 523 | .60 | .448 356 | 8.08 | .551 644 | 19 |
| 42 | .432 329 | 7.48 | .983 487 | .58 | .448 841 | 8.08 | .551 159 | 18 |
| 43 | .432 778 | 7.47 | .983 452 | .60 | .449 326 | 8.07 | .550 674 | 17 |
| 44 | .433 226 | 7.48 | .983 416 | .58 | .449 810 | 8.07 | .550 190 | 16 |
| | | | | .58 | | | | |
| 45 | 9.433 675 | 7.45 | 9.983 381 | .60 | 9.450 294 | 8.05 | 0.549 706 | 15 |
| 46 | .434 122 | 7.45 | .983 345 | .60 | .450 777 | 8.05 | .549 223 | 14 |
| 47 | .434 569 | 7.45 | .983 309 | .60 | .451 260 | 8.05 | .548 740 | 13 |
| 48 | .435 016 | 7.43 | .983 273 | .58 | .451 743 | 8.03 | .548 257 | 12 |
| 49 | .435 462 | 7.43 | .983 238 | .60 | .452 225 | 8.02 | .547 775 | 11 |
| | | | | .60 | | | | |
| 50 | 9.435 908 | 7.42 | 9.983 202 | .60 | 9.452 706 | 8.02 | 0.547 294 | 10 |
| 51 | .436 353 | 7.42 | .983 166 | .60 | .453 187 | 8.02 | .546 813 | 9 |
| 52 | .436 798 | 7.40 | .983 130 | .60 | .453 668 | 8.00 | .546 332 | 8 |
| 53 | .437 242 | 7.40 | .983 094 | .60 | .454 148 | 8.00 | .545 852 | 7 |
| 54 | .437 686 | 7.38 | .983 058 | .60 | .454 628 | 7.98 | .545 372 | 6 |
| | | | | .60 | | | | |
| 55 | 9.438 129 | 7.38 | 9.983 022 | .60 | 9.455 107 | 7.98 | 0.544 893 | 5 |
| 56 | .438 572 | 7.37 | .982 986 | .60 | .455 586 | 7.97 | .544 414 | 4 |
| 57 | .439 014 | 7.37 | .982 950 | .60 | .456 064 | 7.97 | .543 936 | 3 |
| 58 | .439 456 | 7.35 | .982 914 | .60 | .456 542 | 7.95 | .543 458 | 2 |
| 59 | .439 897 | 7.35 | .982 878 | .60 | .457 019 | 7.95 | .542 981 | 1 |
| 60 | 9.440 338 | | 9.982 842 | | 9.457 496 | | 0.542 504 | 0 |

| M. | Sin. | D. 1'' | Cos. | D. 1'' | Tan. | D. 1'' | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.440 338 | | 9.982 842 | .62 | 9.457 496 | | 0.542 504 | 60 |
| 1 | .440 778 | 7.33 | .982 805 | .60 | .457 973 | 7.95 | .542 027 | 59 |
| 2 | .441 218 | 7.33 | .982 769 | .60 | .458 449 | 7.93 | .541 551 | 58 |
| 3 | .441 658 | 7.33 | .982 733 | .62 | .458 925 | 7.93 | .541 075 | 57 |
| 4 | .442 096 | 7.32 | .982 696 | .60 | .459 400 | 7.92 | .540 600 | 56 |
| 5 | 9.442 535 | 7.30 | 9.982 660 | .60 | 9.459 875 | 7.90 | 0.540 125 | 55 |
| 6 | .442 973 | 7.28 | .982 624 | .62 | .460 349 | 7.90 | .539 651 | 54 |
| 7 | .443 410 | 7.28 | .982 587 | .60 | .460 823 | 7.90 | .539 177 | 53 |
| 8 | .443 847 | 7.28 | .982 551 | .62 | .461 297 | 7.88 | .538 703 | 52 |
| 9 | .444 284 | 7.27 | .982 514 | .62 | .461 770 | 7.87 | .538 230 | 51 |
| 10 | 9.444 720 | 7.25 | 9.982 477 | .60 | 9.462 242 | 7.88 | 0.537 758 | 50 |
| 11 | .445 155 | 7.25 | .982 441 | .62 | .462 715 | 7.85 | .537 285 | 49 |
| 12 | .445 590 | 7.25 | .982 404 | .62 | .463 186 | 7.85 | .536 814 | 48 |
| 13 | .446 025 | 7.25 | .982 367 | .60 | .463 658 | 7.87 | .536 342 | 47 |
| 14 | .446 459 | 7.23 | .982 331 | .62 | .464 128 | 7.83 | .535 872 | 46 |
| 15 | 9.446 893 | 7.22 | 9.982 294 | .62 | 9.464 599 | 7.85 | 0.535 401 | 45 |
| 16 | .447 326 | 7.22 | .982 257 | .62 | .465 069 | 7.83 | .534 931 | 44 |
| 17 | .447 759 | 7.20 | .982 220 | .62 | .465 539 | 7.82 | .534 461 | 43 |
| 18 | .448 191 | 7.20 | .982 183 | .62 | .466 008 | 7.82 | .533 992 | 42 |
| 19 | .448 623 | 7.18 | .982 146 | .62 | .466 477 | 7.80 | .533 523 | 41 |
| 20 | 9.449 054 | 7.18 | 9.982 109 | .62 | 9.466 945 | 7.80 | 0.533 055 | 40 |
| 21 | .449 485 | 7.17 | .982 072 | .62 | .467 413 | 7.78 | .532 587 | 39 |
| 22 | .449 915 | 7.17 | .982 035 | .62 | .467 880 | 7.78 | .532 120 | 38 |
| 23 | .450 345 | 7.17 | .981 998 | .62 | .468 347 | 7.78 | .531 653 | 37 |
| 24 | .450 775 | 7.15 | .981 961 | .62 | .468 814 | 7.77 | .531 186 | 36 |
| 25 | 9.451 204 | 7.13 | 9.981 924 | .63 | 9.469 280 | 7.77 | 0.530 720 | 35 |
| 26 | .451 632 | 7.13 | .981 886 | .62 | .469 746 | 7.77 | .530 254 | 34 |
| 27 | .452 060 | 7.13 | .981 849 | .62 | .470 211 | 7.75 | .529 789 | 33 |
| 28 | .452 488 | 7.12 | .981 812 | .63 | .470 676 | 7.75 | .529 324 | 32 |
| 29 | .452 915 | 7.12 | .981 774 | .62 | .471 141 | 7.75 | .528 859 | 31 |
| 30 | 9.453 342 | 7.10 | 9.981 737 | .62 | 9.471 605 | 7.73 | 0.528 395 | 30 |
| 31 | .453 768 | 7.10 | .981 700 | .63 | .472 069 | 7.72 | .527 931 | 29 |
| 32 | .454 194 | 7.08 | .981 662 | .62 | .472 532 | 7.72 | .527 468 | 28 |
| 33 | .454 619 | 7.08 | .981 625 | .63 | .472 995 | 7.72 | .527 005 | 27 |
| 34 | .455 044 | 7.08 | .981 587 | .63 | .473 457 | 7.70 | .526 543 | 26 |
| 35 | 9.455 469 | 7.07 | 9.981 549 | .62 | 9.473 919 | 7.70 | 0.526 081 | 25 |
| 36 | .455 893 | 7.05 | .981 512 | .63 | .474 381 | 7.70 | .525 619 | 24 |
| 37 | .456 316 | 7.05 | .981 474 | .63 | .474 842 | 7.68 | .525 158 | 23 |
| 38 | .456 739 | 7.05 | .981 436 | .62 | .475 303 | 7.68 | .524 697 | 22 |
| 39 | .457 162 | 7.03 | .981 399 | .63 | .475 763 | 7.67 | .524 237 | 21 |
| 40 | 9.457 584 | 7.03 | 9.981 361 | .63 | 9.476 223 | 7.67 | 0.523 777 | 20 |
| 41 | .458 006 | 7.02 | .981 323 | .63 | .476 683 | 7.65 | .523 317 | 19 |
| 42 | .458 427 | 7.02 | .981 285 | .63 | .477 142 | 7.65 | .522 858 | 18 |
| 43 | .458 848 | 7.00 | .981 247 | .63 | .477 601 | 7.63 | .522 399 | 17 |
| 44 | .459 268 | 7.00 | .981 209 | .63 | .478 059 | 7.63 | .521 941 | 16 |
| 45 | 9.459 688 | 7.00 | 9.981 171 | .63 | 9.478 517 | 7.63 | 0.521 483 | 15 |
| 46 | .460 108 | 6.98 | .981 133 | .63 | .478 975 | 7.62 | .521 025 | 14 |
| 47 | .460 527 | 6.98 | .981 095 | .63 | .479 432 | 7.62 | .520 568 | 13 |
| 48 | .460 946 | 6.97 | .981 057 | .63 | .479 889 | 7.60 | .520 111 | 12 |
| 49 | .461 364 | 6.97 | .981 019 | .63 | .480 345 | 7.60 | .519 655 | 11 |
| 50 | 9.461 782 | 6.95 | 9.980 981 | .65 | 9.480 801 | 7.60 | 0.519 199 | 10 |
| 51 | .462 199 | 6.95 | .980 942 | .63 | .481 257 | 7.58 | .518 743 | 9 |
| 52 | .462 616 | 6.93 | .980 904 | .63 | .481 712 | 7.58 | .518 288 | 8 |
| 53 | .463 032 | 6.93 | .980 866 | .65 | .482 167 | 7.57 | .517 833 | 7 |
| 54 | .463 448 | 6.93 | .980 827 | .63 | .482 621 | 7.57 | .517 379 | 6 |
| 55 | 9.463 864 | 6.92 | 9.980 789 | .65 | 9.483 075 | 7.57 | 0.516 925 | 5 |
| 56 | .464 279 | 6.92 | .980 750 | .63 | .483 529 | 7.55 | .516 471 | 4 |
| 57 | .464 694 | 6.90 | .980 712 | .65 | .483 982 | 7.55 | .516 018 | 3 |
| 58 | .465 108 | 6.90 | .980 673 | .63 | .484 435 | 7.53 | .515 565 | 2 |
| 59 | .465 522 | 6.88 | .980 635 | .65 | .484 887 | 7.53 | .515 113 | 1 |
| 60 | 9.465 935 | | 9.980 596 | | 9.485 339 | | 0.514 661 | 0 |

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.465 935 | 6.88 | 9.980 596 | .63 | 9.485 339 | 7.53 | 0.514 661 | 60 |
| 1 | .466 348 | 6.88 | .980 558 | .65 | .485 791 | 7.52 | .514 209 | 59 |
| 2 | .466 761 | 6.87 | .980 519 | .65 | .486 242 | 7.52 | .513 758 | 58 |
| 3 | .467 173 | 6.87 | .980 480 | .65 | .486 693 | 7.50 | .513 307 | 57 |
| 4 | .467 585 | 6.85 | .980 442 | .65 | .487 143 | 7.50 | .512 857 | 56 |
| 5 | 9.467 996 | 6.85 | 9.980 403 | .65 | 9.487 593 | 7.50 | 0.512 407 | 55 |
| 6 | .468 407 | 6.83 | .980 364 | .65 | .488 043 | 7.48 | .511 957 | 54 |
| 7 | .468 817 | 6.83 | .980 325 | .65 | .488 492 | 7.48 | .511 508 | 53 |
| 8 | .469 227 | 6.83 | .980 286 | .65 | .488 941 | 7.48 | .511 059 | 52 |
| 9 | .469 637 | 6.82 | .980 247 | .65 | .489 390 | 7.47 | .510 610 | 51 |
| 10 | 9.470 046 | 6.82 | 9.980 208 | .65 | 9.489 838 | 7.47 | 0.510 162 | 50 |
| 11 | .470 455 | 6.80 | .980 169 | .65 | .490 286 | 7.45 | .509 714 | 49 |
| 12 | .470 863 | 6.80 | .980 130 | .65 | .490 733 | 7.45 | .509 267 | 48 |
| 13 | .471 271 | 6.80 | .980 091 | .65 | .491 180 | 7.45 | .508 820 | 47 |
| 14 | .471 679 | 6.78 | .980 052 | .67 | .491 627 | 7.43 | .508 373 | 46 |
| 15 | 9.472 086 | 6.77 | 9.980 012 | .65 | 9.492 073 | 7.43 | 0.507 927 | 45 |
| 16 | .472 492 | 6.77 | .979 973 | .65 | .492 519 | 7.43 | .507 481 | 44 |
| 17 | .472 898 | 6.77 | .979 934 | .65 | .492 965 | 7.42 | .507 035 | 43 |
| 18 | .473 304 | 6.77 | .979 895 | .67 | .493 410 | 7.40 | .506 590 | 42 |
| 19 | .473 710 | 6.75 | .979 855 | .65 | .493 854 | 7.42 | .506 146 | 41 |
| 20 | 9.474 115 | 6.73 | 9.979 816 | .67 | 9.494 299 | 7.40 | 0.505 701 | 40 |
| 21 | .474 519 | 6.73 | .979 776 | .65 | .494 743 | 7.38 | .505 257 | 39 |
| 22 | .474 923 | 6.73 | .979 737 | .67 | .495 186 | 7.40 | .504 814 | 38 |
| 23 | .475 327 | 6.72 | .979 697 | .65 | .495 630 | 7.38 | .504 370 | 37 |
| 24 | .475 730 | 6.72 | .979 658 | .67 | .496 073 | 7.37 | .503 927 | 36 |
| 25 | 9.476 133 | 6.72 | 9.979 618 | .65 | 9.496 515 | 7.37 | 0.503 485 | 35 |
| 26 | .476 536 | 6.70 | .979 579 | .67 | .496 957 | 7.37 | .503 043 | 34 |
| 27 | .476 938 | 6.70 | .979 539 | .67 | .497 399 | 7.37 | .502 601 | 33 |
| 28 | .477 340 | 6.68 | .979 499 | .67 | .497 841 | 7.35 | .502 159 | 32 |
| 29 | .477 741 | 6.68 | .979 459 | .65 | .498 282 | 7.33 | .501 718 | 31 |
| 30 | 9.478 142 | 6.67 | 9.979 420 | .67 | 9.498 722 | 7.35 | 0.501 278 | 30 |
| 31 | .478 542 | 6.67 | .979 380 | .67 | .499 163 | 7.33 | .500 837 | 29 |
| 32 | .478 942 | 6.67 | .979 340 | .67 | .499 603 | 7.32 | .500 397 | 28 |
| 33 | .479 342 | 6.65 | .979 300 | .67 | .500 042 | 7.32 | .499 958 | 27 |
| 34 | .479 741 | 6.65 | .979 260 | .67 | .500 481 | 7.32 | .499 519 | 26 |
| 35 | 9.480 140 | 6.65 | 9.979 220 | .67 | 9.500 920 | 7.32 | 0.499 080 | 25 |
| 36 | .480 539 | 6.63 | .979 180 | .67 | .501 359 | 7.30 | .498 641 | 24 |
| 37 | .480 937 | 6.62 | .979 140 | .67 | .501 797 | 7.30 | .498 203 | 23 |
| 38 | .481 334 | 6.62 | .979 100 | .68 | .502 235 | 7.28 | .497 765 | 22 |
| 39 | .481 731 | 6.62 | .979 059 | .67 | .502 672 | 7.28 | .497 328 | 21 |
| 40 | 9.482 128 | 6.62 | 9.979 019 | .67 | 9.503 109 | 7.28 | 0.496 891 | 20 |
| 41 | .482 525 | 6.60 | .978 979 | .67 | .503 546 | 7.27 | .496 454 | 19 |
| 42 | .482 921 | 6.58 | .978 939 | .68 | .503 982 | 7.27 | .496 018 | 18 |
| 43 | .483 316 | 6.60 | .978 898 | .67 | .504 418 | 7.27 | .495 582 | 17 |
| 44 | .483 712 | 6.58 | .978 858 | .68 | .504 854 | 7.25 | .495 146 | 16 |
| 45 | 9.484 107 | 6.57 | 9.978 817 | .67 | 9.505 289 | 7.25 | 0.494 711 | 15 |
| 46 | .484 501 | 6.57 | .978 777 | .67 | .505 724 | 7.25 | .494 276 | 14 |
| 47 | .484 895 | 6.57 | .978 737 | .68 | .506 159 | 7.23 | .493 841 | 13 |
| 48 | .485 289 | 6.55 | .978 696 | .68 | .506 593 | 7.23 | .493 407 | 12 |
| 49 | .485 682 | 6.55 | .978 655 | .67 | .507 027 | 7.22 | .492 973 | 11 |
| 50 | 9.486 075 | 6.53 | 9.978 615 | .68 | 9.507 460 | 7.22 | 0.492 540 | 10 |
| 51 | .486 467 | 6.55 | .978 574 | .68 | .507 893 | 7.22 | .492 107 | 9 |
| 52 | .486 860 | 6.52 | .978 533 | .67 | .508 326 | 7.22 | .491 674 | 8 |
| 53 | .487 251 | 6.53 | .978 493 | .68 | .508 759 | 7.20 | .491 241 | 7 |
| 54 | .487 643 | 6.52 | .978 452 | .68 | .509 191 | 7.18 | .490 809 | 6 |
| 55 | 9.488 034 | 6.50 | 9.978 411 | .68 | 9.509 622 | 7.20 | 0.490 378 | 5 |
| 56 | .488 424 | 6.50 | .978 370 | .68 | .510 054 | 7.18 | .489 946 | 4 |
| 57 | .488 814 | 6.50 | .978 329 | .68 | .510 485 | 7.18 | .489 513 | 3 |
| 58 | .489 204 | 6.48 | .978 288 | .68 | .510 916 | 7.17 | .489 084 | 2 |
| 59 | .489 593 | 6.48 | .978 247 | .68 | .511 346 | 7.17 | .488 654 | 1 |
| 60 | 9.489 982 | | 9.978 206 | | 9.511 776 | | 0.488 224 | 0 |

| M. | Sin. | D. 1''. | Cos. | D. 1''. | Tan. | D. 1''. | Cot. | M. |
|----|-----------|---------|-----------|---------|-----------|---------|-----------|----|
| 0 | 9.489 982 | | 9.978 206 | | 9.511 776 | | 0.488 224 | 60 |
| 1 | .490 371 | 6.48 | .978 165 | .68 | .512 206 | 7.17 | .487 794 | 59 |
| 2 | .490 759 | 6.47 | .978 124 | .68 | .512 635 | 7.15 | .487 365 | 58 |
| 3 | .491 147 | 6.47 | .978 083 | .68 | .513 064 | 7.15 | .486 936 | 57 |
| 4 | .491 535 | 6.45 | .978 042 | .68 | .513 493 | 7.13 | .486 507 | 56 |
| 5 | 9.491 922 | | 9.978 001 | .70 | 9.513 921 | | 0.486 079 | 55 |
| 6 | .492 308 | 6.43 | .977 959 | .68 | .514 349 | 7.13 | .485 651 | 54 |
| 7 | .492 695 | 6.45 | .977 918 | .68 | .514 777 | 7.13 | .485 223 | 53 |
| 8 | .493 081 | 6.43 | .977 877 | .68 | .515 204 | 7.12 | .484 796 | 52 |
| 9 | .493 466 | 6.42 | .977 835 | .68 | .515 631 | 7.12 | .484 369 | 51 |
| 10 | 9.493 851 | | 9.977 794 | .70 | 9.516 057 | | 0.483 943 | 50 |
| 11 | .494 236 | 6.42 | .977 752 | .68 | .516 484 | 7.12 | .483 516 | 49 |
| 12 | .494 621 | 6.42 | .977 711 | .68 | .516 910 | 7.10 | .483 090 | 48 |
| 13 | .495 005 | 6.40 | .977 669 | .70 | .517 335 | 7.08 | .482 665 | 47 |
| 14 | .495 388 | 6.38 | .977 628 | .68 | .517 761 | 7.10 | .482 239 | 46 |
| 15 | 9.495 772 | | 9.977 586 | .70 | 9.518 186 | | 0.481 814 | 45 |
| 16 | .496 154 | 6.37 | .977 544 | .68 | .518 610 | 7.07 | .481 390 | 44 |
| 17 | .496 537 | 6.38 | .977 503 | .68 | .519 034 | 7.07 | .480 966 | 43 |
| 18 | .496 919 | 6.37 | .977 461 | .70 | .519 458 | 7.07 | .480 542 | 42 |
| 19 | .497 301 | 6.35 | .977 419 | .70 | .519 882 | 7.07 | .480 118 | 41 |
| 20 | 9.497 682 | | 9.977 377 | .70 | 9.520 305 | | 0.479 695 | 40 |
| 21 | .498 064 | 6.37 | .977 335 | .70 | .520 728 | 7.05 | .479 272 | 39 |
| 22 | .498 444 | 6.33 | .977 293 | .70 | .521 151 | 7.05 | .478 849 | 38 |
| 23 | .498 825 | 6.35 | .977 251 | .70 | .521 573 | 7.03 | .478 427 | 37 |
| 24 | .499 204 | 6.32 | .977 209 | .70 | .521 995 | 7.03 | .478 005 | 36 |
| 25 | 9.499 584 | | 9.977 167 | .70 | 9.522 417 | | 0.477 583 | 35 |
| 26 | .499 963 | 6.32 | .977 125 | .70 | .522 838 | 7.02 | .477 162 | 34 |
| 27 | .500 342 | 6.32 | .977 083 | .70 | .523 259 | 7.02 | .476 741 | 33 |
| 28 | .500 721 | 6.30 | .977 041 | .70 | .523 680 | 7.00 | .476 320 | 32 |
| 29 | .501 099 | 6.28 | .976 999 | .70 | .524 100 | 7.00 | .475 900 | 31 |
| 30 | 9.501 476 | | 9.976 957 | .72 | 9.524 520 | | 0.475 480 | 30 |
| 31 | .501 854 | 6.30 | .976 914 | .70 | .524 940 | 7.00 | .475 060 | 29 |
| 32 | .502 231 | 6.28 | .976 872 | .70 | .525 359 | 6.98 | .474 641 | 28 |
| 33 | .502 607 | 6.27 | .976 830 | .70 | .525 778 | 6.98 | .474 222 | 27 |
| 34 | .502 984 | 6.27 | .976 787 | .70 | .526 197 | 6.97 | .473 803 | 26 |
| 35 | 9.503 360 | | 9.976 745 | .72 | 9.526 615 | | 0.473 385 | 25 |
| 36 | .503 735 | 6.25 | .976 702 | .72 | .527 033 | 6.97 | .472 967 | 24 |
| 37 | .504 110 | 6.25 | .976 660 | .70 | .527 451 | 6.95 | .472 549 | 23 |
| 38 | .504 485 | 6.25 | .976 617 | .72 | .527 868 | 6.95 | .472 132 | 22 |
| 39 | .504 860 | 6.23 | .976 574 | .70 | .528 285 | 6.95 | .471 715 | 21 |
| 40 | 9.505 234 | | 9.976 532 | .72 | 9.528 702 | | 0.471 298 | 20 |
| 41 | .505 608 | 6.23 | .976 489 | .72 | .529 119 | 6.95 | .470 881 | 19 |
| 42 | .505 981 | 6.22 | .976 446 | .72 | .529 535 | 6.93 | .470 465 | 18 |
| 43 | .506 354 | 6.22 | .976 404 | .72 | .529 951 | 6.92 | .470 049 | 17 |
| 44 | .506 727 | 6.20 | .976 361 | .72 | .530 366 | 6.92 | .469 634 | 16 |
| 45 | 9.507 099 | | 9.976 318 | .72 | 9.530 781 | | 0.469 219 | 15 |
| 46 | .507 471 | 6.20 | .976 275 | .72 | .531 196 | 6.92 | .468 804 | 14 |
| 47 | .507 843 | 6.18 | .976 232 | .72 | .531 611 | 6.92 | .468 389 | 13 |
| 48 | .508 214 | 6.18 | .976 189 | .72 | .532 025 | 6.90 | .467 975 | 12 |
| 49 | .508 585 | 6.18 | .976 146 | .72 | .532 439 | 6.90 | .467 561 | 11 |
| 50 | 9.508 956 | | 9.976 103 | .72 | 9.532 853 | | 0.467 147 | 10 |
| 51 | .509 326 | 6.17 | .976 060 | .72 | .533 266 | 6.88 | .466 734 | 9 |
| 52 | .509 696 | 6.17 | .976 017 | .72 | .533 679 | 6.88 | .466 321 | 8 |
| 53 | .510 065 | 6.15 | .975 974 | .72 | .534 092 | 6.87 | .465 908 | 7 |
| 54 | .510 434 | 6.15 | .975 930 | .73 | .534 504 | 6.87 | .465 496 | 6 |
| 55 | 9.510 803 | | 9.975 887 | .72 | 9.534 916 | | 0.465 084 | 5 |
| 56 | .511 172 | 6.15 | .975 844 | .72 | .535 328 | 6.87 | .464 672 | 4 |
| 57 | .511 540 | 6.13 | .975 800 | .73 | .535 739 | 6.85 | .464 261 | 3 |
| 58 | .511 907 | 6.12 | .975 757 | .72 | .536 150 | 6.85 | .463 850 | 2 |
| 59 | .512 275 | 6.13 | .975 714 | .72 | .536 561 | 6.85 | .463 439 | 1 |
| 60 | 9.512 642 | | 9.975 670 | .73 | 9.536 972 | | 0.463 028 | 0 |

Cos. D. 1''. Sin. D. 1''. Cot. D. 1''. Tan. M.

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.512 642 | 6.12 | 9.975 670 | .72 | 9.536 972 | 6.83 | 0.463 028 | 60 |
| 1 | .513 009 | 6.10 | .975 627 | .73 | .537 382 | 6.83 | .462 618 | 59 |
| 2 | .513 375 | 6.10 | .975 583 | .73 | .537 792 | 6.83 | .462 208 | 58 |
| 3 | .513 741 | 6.10 | .975 539 | .73 | .538 202 | 6.82 | .461 798 | 57 |
| 4 | .514 107 | 6.08 | .975 496 | .73 | .538 611 | 6.82 | .461 389 | 56 |
| 5 | 9.514 472 | 6.08 | 9.975 452 | .73 | 9.539 020 | 6.82 | 0.460 980 | 55 |
| 6 | .514 837 | 6.08 | .975 408 | .72 | .539 429 | 6.80 | .460 571 | 54 |
| 7 | .515 202 | 6.07 | .975 365 | .73 | .539 837 | 6.80 | .460 163 | 53 |
| 8 | .515 566 | 6.07 | .975 321 | .73 | .540 245 | 6.80 | .459 755 | 52 |
| 9 | .515 930 | 6.07 | .975 277 | .73 | .540 653 | 6.80 | .459 347 | 51 |
| 10 | 9.516 294 | 6.05 | 9.975 233 | .73 | 9.541 061 | 6.78 | 0.458 939 | 50 |
| 11 | .516 657 | 6.05 | .975 189 | .73 | .541 468 | 6.78 | .458 532 | 49 |
| 12 | .517 020 | 6.03 | .975 145 | .73 | .541 875 | 6.77 | .458 125 | 48 |
| 13 | .517 382 | 6.05 | .975 101 | .73 | .542 281 | 6.78 | .457 719 | 47 |
| 14 | .517 745 | 6.03 | .975 057 | .73 | .542 688 | 6.77 | .457 312 | 46 |
| 15 | 9.518 107 | 6.02 | 9.975 013 | .73 | 9.543 094 | 6.75 | 0.456 906 | 45 |
| 16 | .518 468 | 6.02 | .974 969 | .73 | .543 499 | 6.77 | .456 501 | 44 |
| 17 | .518 829 | 6.02 | .974 925 | .75 | .543 905 | 6.75 | .456 095 | 43 |
| 18 | .519 190 | 6.02 | .974 880 | .73 | .544 310 | 6.75 | .455 690 | 42 |
| 19 | .519 551 | 6.00 | .974 836 | .73 | .544 715 | 6.73 | .455 285 | 41 |
| 20 | 9.519 911 | 6.00 | 9.974 792 | .73 | 9.545 119 | 6.75 | 0.454 881 | 40 |
| 21 | .520 271 | 6.00 | .974 748 | .75 | .545 524 | 6.73 | .454 476 | 39 |
| 22 | .520 631 | 5.98 | .974 703 | .73 | .545 928 | 6.72 | .454 072 | 38 |
| 23 | .520 990 | 5.98 | .974 659 | .73 | .546 331 | 6.73 | .453 669 | 37 |
| 24 | .521 349 | 5.97 | .974 614 | .73 | .546 735 | 6.72 | .453 265 | 36 |
| 25 | 9.521 707 | 5.98 | 9.974 570 | .75 | 9.547 138 | 6.70 | 0.452 862 | 35 |
| 26 | .522 066 | 5.97 | .974 525 | .73 | .547 540 | 6.72 | .452 460 | 34 |
| 27 | .522 424 | 5.95 | .974 481 | .75 | .547 943 | 6.70 | .452 057 | 33 |
| 28 | .522 781 | 5.95 | .974 436 | .75 | .548 345 | 6.70 | .451 655 | 32 |
| 29 | .523 138 | 5.95 | .974 391 | .73 | .548 747 | 6.70 | .451 253 | 31 |
| 30 | 9.523 495 | 5.95 | 9.974 347 | .75 | 9.549 149 | 6.68 | 0.450 851 | 30 |
| 31 | .523 852 | 5.93 | .974 302 | .75 | .549 550 | 6.68 | .450 450 | 29 |
| 32 | .524 208 | 5.93 | .974 257 | .75 | .549 951 | 6.68 | .450 049 | 28 |
| 33 | .524 564 | 5.93 | .974 212 | .75 | .550 352 | 6.67 | .449 648 | 27 |
| 34 | .524 920 | 5.92 | .974 167 | .75 | .550 752 | 6.68 | .449 248 | 26 |
| 35 | 9.525 275 | 5.92 | 9.974 122 | .75 | 9.551 153 | 6.65 | 0.448 847 | 25 |
| 36 | .525 630 | 5.90 | .974 077 | .75 | .551 552 | 6.67 | .448 448 | 24 |
| 37 | .525 984 | 5.92 | .974 032 | .75 | .551 952 | 6.65 | .448 048 | 23 |
| 38 | .526 339 | 5.90 | .973 987 | .75 | .552 351 | 6.65 | .447 649 | 22 |
| 39 | .526 693 | 5.88 | .973 942 | .75 | .552 750 | 6.65 | .447 250 | 21 |
| 40 | 9.527 046 | 5.90 | 9.973 897 | .75 | 9.553 149 | 6.65 | 0.446 851 | 20 |
| 41 | .527 400 | 5.88 | .973 852 | .75 | .553 548 | 6.63 | .446 452 | 19 |
| 42 | .527 753 | 5.87 | .973 807 | .77 | .553 946 | 6.63 | .446 054 | 18 |
| 43 | .528 105 | 5.88 | .973 761 | .75 | .554 344 | 6.62 | .445 656 | 17 |
| 44 | .528 458 | 5.87 | .973 716 | .75 | .554 741 | 6.63 | .445 259 | 16 |
| 45 | 9.528 810 | 5.85 | 9.973 671 | .77 | 9.555 139 | 6.62 | 0.444 861 | 15 |
| 46 | .529 161 | 5.87 | .973 625 | .75 | .555 536 | 6.62 | .444 464 | 14 |
| 47 | .529 513 | 5.85 | .973 580 | .75 | .555 933 | 6.60 | .444 067 | 13 |
| 48 | .529 864 | 5.85 | .973 535 | .77 | .556 329 | 6.60 | .443 671 | 12 |
| 49 | .530 215 | 5.83 | .973 489 | .75 | .556 725 | 6.60 | .443 275 | 11 |
| 50 | 9.530 565 | 5.83 | 9.973 444 | .77 | 9.557 121 | 6.60 | 0.442 879 | 10 |
| 51 | .530 915 | 5.83 | .973 398 | .77 | .557 517 | 6.60 | .442 483 | 9 |
| 52 | .531 265 | 5.82 | .973 352 | .75 | .557 913 | 6.58 | .442 087 | 8 |
| 53 | .531 614 | 5.82 | .973 307 | .77 | .558 308 | 6.58 | .441 692 | 7 |
| 54 | .531 963 | 5.82 | .973 261 | .77 | .558 703 | 6.57 | .441 297 | 6 |
| 55 | 9.532 312 | 5.82 | 9.973 215 | .77 | 9.559 097 | 6.57 | 0.440 903 | 5 |
| 56 | .532 661 | 5.80 | .973 169 | .75 | .559 491 | 6.57 | .440 509 | 4 |
| 57 | .533 009 | 5.80 | .973 124 | .77 | .559 885 | 6.57 | .440 115 | 3 |
| 58 | .533 357 | 5.78 | .973 078 | .77 | .560 279 | 6.57 | .439 721 | 2 |
| 59 | .533 704 | 5.80 | .973 032 | .77 | .560 673 | 6.55 | .439 327 | 1 |
| 60 | 9.534 052 | | 9.972 986 | | 9.561 066 | | 0.438 934 | 0 |

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.534 052 | | 9.972 986 | | 9.561 066 | | 0.438 934 | 60 |
| 1 | .534 399 | 5.78 | .972 940 | .77 | .561 459 | 6.55 | .438 541 | 59 |
| 2 | .534 745 | 5.77 | .972 894 | .77 | .561 851 | 6.53 | .438 149 | 58 |
| 3 | .535 092 | 5.78 | .972 848 | .77 | .562 244 | 6.55 | .437 756 | 57 |
| 4 | .535 438 | 5.77 | .972 802 | .77 | .562 636 | 6.53 | .437 364 | 56 |
| 5 | 9.535 783 | 5.75 | 9.972 755 | .77 | 9.563 028 | 6.52 | 0.436 972 | 55 |
| 6 | .536 129 | 5.75 | .972 709 | .77 | .563 419 | 6.53 | .436 581 | 54 |
| 7 | .536 474 | 5.73 | .972 663 | .77 | .563 811 | 6.52 | .436 189 | 53 |
| 8 | .536 818 | 5.75 | .972 617 | .77 | .564 202 | 6.52 | .435 798 | 52 |
| 9 | .537 163 | 5.73 | .972 570 | .77 | .564 593 | 6.50 | .435 407 | 51 |
| 10 | 9.537 507 | 5.73 | 9.972 524 | .77 | 9.564 983 | 6.50 | 0.435 017 | 50 |
| 11 | .537 851 | 5.72 | .972 478 | .78 | .565 373 | 6.50 | .434 627 | 49 |
| 12 | .538 194 | 5.73 | .972 431 | .77 | .565 763 | 6.50 | .434 237 | 48 |
| 13 | .538 538 | 5.70 | .972 385 | .78 | .566 153 | 6.48 | .433 847 | 47 |
| 14 | .538 880 | 5.72 | .972 338 | .78 | .566 542 | 6.50 | .433 458 | 46 |
| 15 | 9.539 223 | 5.70 | 9.972 291 | .77 | 9.566 932 | 6.47 | 0.433 068 | 45 |
| 16 | .539 565 | 5.70 | .972 245 | .78 | .567 320 | 6.48 | .432 680 | 44 |
| 17 | .539 907 | 5.70 | .972 198 | .78 | .567 709 | 6.48 | .432 291 | 43 |
| 18 | .540 249 | 5.68 | .972 151 | .77 | .568 098 | 6.47 | .431 902 | 42 |
| 19 | .540 590 | 5.68 | .972 105 | .78 | .568 486 | 6.45 | .431 514 | 41 |
| 20 | 9.540 931 | 5.68 | 9.972 058 | .78 | 9.568 873 | 6.47 | 0.431 127 | 40 |
| 21 | .541 272 | 5.68 | .972 011 | .78 | .569 261 | 6.45 | .430 739 | 39 |
| 22 | .541 613 | 5.67 | .971 964 | .78 | .569 648 | 6.45 | .430 352 | 38 |
| 23 | .541 953 | 5.67 | .971 917 | .78 | .570 035 | 6.45 | .429 965 | 37 |
| 24 | .542 293 | 5.65 | .971 870 | .78 | .570 422 | 6.45 | .429 578 | 36 |
| 25 | 9.542 632 | 5.65 | 9.971 823 | .78 | 9.570 809 | 6.43 | 0.429 191 | 35 |
| 26 | .542 971 | 5.65 | .971 776 | .78 | .571 195 | 6.43 | .428 805 | 34 |
| 27 | .543 310 | 5.65 | .971 729 | .78 | .571 581 | 6.43 | .428 419 | 33 |
| 28 | .543 649 | 5.63 | .971 682 | .78 | .571 967 | 6.42 | .428 033 | 32 |
| 29 | .543 987 | 5.63 | .971 635 | .78 | .572 352 | 6.43 | .427 648 | 31 |
| 30 | 9.544 325 | 5.63 | 9.971 588 | .80 | 9.572 738 | 6.42 | 0.427 262 | 30 |
| 31 | .544 663 | 5.62 | .971 540 | .78 | .573 123 | 6.40 | .426 877 | 29 |
| 32 | .545 000 | 5.62 | .971 493 | .78 | .573 507 | 6.42 | .426 493 | 28 |
| 33 | .545 338 | 5.60 | .971 446 | .80 | .573 892 | 6.40 | .426 108 | 27 |
| 34 | .545 674 | 5.62 | .971 398 | .78 | .574 276 | 6.40 | .425 724 | 26 |
| 35 | 9.546 011 | 5.60 | 9.971 351 | .80 | 9.574 660 | 6.40 | 0.425 340 | 25 |
| 36 | .546 347 | 5.60 | .971 303 | .78 | .575 044 | 6.38 | .424 956 | 24 |
| 37 | .546 683 | 5.60 | .971 256 | .80 | .575 427 | 6.38 | .424 573 | 23 |
| 38 | .547 019 | 5.58 | .971 208 | .78 | .575 810 | 6.38 | .424 190 | 22 |
| 39 | .547 354 | 5.58 | .971 161 | .80 | .576 193 | 6.38 | .423 807 | 21 |
| 40 | 9.547 689 | 5.58 | 9.971 113 | .78 | 9.576 576 | 6.38 | 0.423 424 | 20 |
| 41 | .548 024 | 5.58 | .971 066 | .80 | .576 959 | 6.37 | .423 041 | 19 |
| 42 | .548 359 | 5.57 | .971 018 | .80 | .577 341 | 6.37 | .422 659 | 18 |
| 43 | .548 693 | 5.57 | .970 970 | .80 | .577 723 | 6.35 | .422 277 | 17 |
| 44 | .549 027 | 5.55 | .970 922 | .80 | .578 104 | 6.37 | .421 896 | 16 |
| 45 | 9.549 360 | 5.55 | 9.970 874 | .78 | 9.578 486 | 6.35 | 0.421 514 | 15 |
| 46 | .549 693 | 5.55 | .970 827 | .80 | .578 867 | 6.35 | .421 133 | 14 |
| 47 | .550 026 | 5.55 | .970 779 | .80 | .579 248 | 6.35 | .420 752 | 13 |
| 48 | .550 359 | 5.55 | .970 731 | .80 | .579 629 | 6.33 | .420 371 | 12 |
| 49 | .550 692 | 5.53 | .970 683 | .80 | .580 009 | 6.33 | .419 991 | 11 |
| 50 | 9.551 024 | 5.53 | 9.970 635 | .82 | 9.580 389 | 6.33 | 0.419 611 | 10 |
| 51 | .551 356 | 5.52 | .970 586 | .80 | .580 769 | 6.33 | .419 231 | 9 |
| 52 | .551 687 | 5.52 | .970 538 | .80 | .581 149 | 6.32 | .418 851 | 8 |
| 53 | .552 018 | 5.52 | .970 490 | .80 | .581 528 | 6.32 | .418 472 | 7 |
| 54 | .552 349 | 5.52 | .970 442 | .80 | .581 907 | 6.32 | .418 093 | 6 |
| 55 | 9.552 680 | 5.50 | 9.970 394 | .82 | 9.582 286 | 6.32 | 0.417 714 | 5 |
| 56 | .553 010 | 5.52 | .970 345 | .80 | .582 665 | 6.32 | .417 335 | 4 |
| 57 | .553 341 | 5.48 | .970 297 | .80 | .583 044 | 6.30 | .416 956 | 3 |
| 58 | .553 670 | 5.50 | .970 249 | .82 | .583 422 | 6.30 | .416 578 | 2 |
| 59 | .554 000 | 5.48 | .970 200 | .80 | .583 800 | 6.28 | .416 200 | 1 |
| 60 | 9.554 329 | | 9.970 152 | | 9.584 177 | | 0.415 823 | 0 |
| | Cos. | D. 1". | Sin. | D. 1". | Cot. | D. 1". | Tan. | M. |

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.554 329 | | 9.970 152 | .82 | 9.584 177 | 6.30 | 0.415 823 | 60 |
| 1 | .554 658 | 5.48 | .970 103 | .80 | .584 555 | 6.28 | .415 445 | 59 |
| 2 | .554 987 | 5.48 | .970 055 | .82 | .584 932 | 6.28 | .415 068 | 58 |
| 3 | .555 315 | 5.47 | .970 006 | .82 | .585 309 | 6.28 | .414 691 | 57 |
| 4 | .555 643 | 5.47 | .969 957 | .80 | .585 686 | 6.27 | .414 314 | 56 |
| 5 | 9.555 971 | | 9.969 909 | .82 | 9.586 062 | 6.28 | 0.413 938 | 55 |
| 6 | .556 299 | 5.47 | .969 860 | .82 | .586 439 | 6.27 | .413 561 | 54 |
| 7 | .556 626 | 5.45 | .969 811 | .82 | .586 815 | 6.25 | .413 185 | 53 |
| 8 | .556 953 | 5.45 | .969 762 | .80 | .587 190 | 6.27 | .412 810 | 52 |
| 9 | .557 280 | 5.45 | .969 714 | .82 | .587 566 | 6.25 | .412 434 | 51 |
| 10 | 9.557 606 | | 9.969 665 | .82 | 9.587 941 | 6.25 | 0.412 059 | 50 |
| 11 | .557 932 | 5.43 | .969 616 | .82 | .588 316 | 6.25 | .411 684 | 49 |
| 12 | .558 258 | 5.43 | .969 567 | .82 | .588 691 | 6.25 | .411 309 | 48 |
| 13 | .558 583 | 5.42 | .969 518 | .82 | .589 066 | 6.23 | .410 934 | 47 |
| 14 | .558 909 | 5.42 | .969 469 | .82 | .589 440 | 6.23 | .410 560 | 46 |
| 15 | 9.559 234 | | 9.969 420 | .83 | 9.589 814 | 6.23 | 0.410 186 | 45 |
| 16 | .559 558 | 5.40 | .969 370 | .82 | .590 188 | 6.23 | .409 812 | 44 |
| 17 | .559 883 | 5.42 | .969 321 | .82 | .590 562 | 6.22 | .409 438 | 43 |
| 18 | .560 207 | 5.40 | .969 272 | .82 | .590 935 | 6.22 | .409 065 | 42 |
| 19 | .560 531 | 5.40 | .969 223 | .83 | .591 308 | 6.22 | .408 692 | 41 |
| 20 | 9.560 855 | | 9.969 173 | .82 | 9.591 681 | 6.22 | 0.408 319 | 40 |
| 21 | .561 178 | 5.38 | .969 124 | .82 | .592 054 | 6.20 | .407 946 | 39 |
| 22 | .561 501 | 5.38 | .969 075 | .83 | .592 426 | 6.22 | .407 574 | 38 |
| 23 | .561 824 | 5.38 | .969 025 | .82 | .592 799 | 6.20 | .407 201 | 37 |
| 24 | .562 146 | 5.37 | .968 976 | .83 | .593 171 | 6.18 | .406 829 | 36 |
| 25 | 9.562 468 | | 9.968 926 | .82 | 9.593 542 | 6.20 | 0.406 458 | 35 |
| 26 | .562 790 | 5.37 | .968 877 | .83 | .593 914 | 6.18 | .406 086 | 34 |
| 27 | .563 112 | 5.37 | .968 827 | .83 | .594 285 | 6.18 | .405 715 | 33 |
| 28 | .563 433 | 5.35 | .968 777 | .82 | .594 656 | 6.18 | .405 344 | 32 |
| 29 | .563 755 | 5.37 | .968 728 | .83 | .595 027 | 6.18 | .404 973 | 31 |
| 30 | 9.564 075 | | 9.968 678 | .83 | 9.595 398 | 6.17 | 0.404 602 | 30 |
| 31 | .564 396 | 5.35 | .968 628 | .83 | .595 768 | 6.17 | .404 232 | 29 |
| 32 | .564 716 | 5.33 | .968 578 | .83 | .596 138 | 6.17 | .403 862 | 28 |
| 33 | .565 036 | 5.33 | .968 528 | .83 | .596 508 | 6.17 | .403 492 | 27 |
| 34 | .565 356 | 5.33 | .968 479 | .82 | .596 878 | 6.17 | .403 122 | 26 |
| 35 | 9.565 676 | | 9.968 429 | .83 | 9.597 247 | 6.15 | 0.402 753 | 25 |
| 36 | .565 995 | 5.32 | .968 379 | .83 | .597 616 | 6.15 | .402 384 | 24 |
| 37 | .566 314 | 5.32 | .968 329 | .85 | .597 985 | 6.15 | .402 015 | 23 |
| 38 | .566 632 | 5.30 | .968 278 | .85 | .598 354 | 6.13 | .401 646 | 22 |
| 39 | .566 951 | 5.32 | .968 228 | .83 | .598 722 | 6.15 | .401 278 | 21 |
| 40 | 9.567 269 | | 9.968 178 | .83 | 9.599 091 | 6.13 | 0.400 909 | 20 |
| 41 | .567 587 | 5.30 | .968 128 | .83 | .599 459 | 6.13 | .400 541 | 19 |
| 42 | .567 904 | 5.28 | .968 078 | .85 | .599 827 | 6.12 | .400 173 | 18 |
| 43 | .568 222 | 5.30 | .968 027 | .83 | .600 194 | 6.13 | .399 806 | 17 |
| 44 | .568 539 | 5.28 | .967 977 | .83 | .600 562 | 6.12 | .399 438 | 16 |
| 45 | 9.568 856 | | 9.967 927 | .85 | 9.600 929 | 6.12 | 0.399 071 | 15 |
| 46 | .569 172 | 5.27 | .967 876 | .83 | .601 296 | 6.12 | .398 704 | 14 |
| 47 | .569 488 | 5.27 | .967 826 | .85 | .601 663 | 6.10 | .398 337 | 13 |
| 48 | .569 804 | 5.27 | .967 775 | .83 | .602 029 | 6.10 | .397 971 | 12 |
| 49 | .570 120 | 5.25 | .967 725 | .85 | .602 395 | 6.10 | .397 605 | 11 |
| 50 | 9.570 435 | | 9.967 674 | .83 | 9.602 761 | 6.10 | 0.397 239 | 10 |
| 51 | .570 751 | 5.27 | .967 624 | .85 | .603 127 | 6.10 | .396 873 | 9 |
| 52 | .571 066 | 5.25 | .967 573 | .85 | .603 493 | 6.08 | .396 507 | 8 |
| 53 | .571 380 | 5.23 | .967 522 | .85 | .603 858 | 6.08 | .396 142 | 7 |
| 54 | .571 695 | 5.25 | .967 471 | .83 | .604 223 | 6.08 | .395 777 | 6 |
| 55 | 9.572 009 | | 9.967 421 | .85 | 9.604 588 | 6.08 | 0.395 412 | 5 |
| 56 | .572 323 | 5.23 | .967 370 | .85 | .604 953 | 6.07 | .395 047 | 4 |
| 57 | .572 636 | 5.22 | .967 319 | .85 | .605 317 | 6.07 | .394 683 | 3 |
| 58 | .572 950 | 5.23 | .967 268 | .85 | .605 682 | 6.08 | .394 318 | 2 |
| 59 | .573 263 | 5.22 | .967 217 | .85 | .606 046 | 6.07 | .393 954 | 1 |
| 60 | 9.573 575 | | 9.967 166 | | 9.606 410 | 6.07 | 0.393 590 | 0 |

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.573 575 | | 9.967 166 | .85 | 9.606 410 | 6.05 | 0.393 590 | 60 |
| 1 | .573 888 | 5.22 | .967 115 | .85 | .606 773 | 6.07 | .393 227 | 59 |
| 2 | .574 200 | 5.20 | .967 064 | .85 | .607 137 | 6.05 | .392 863 | 58 |
| 3 | .574 512 | 5.20 | .967 013 | .87 | .607 500 | 6.05 | .392 500 | 57 |
| 4 | .574 824 | 5.20 | .966 961 | .85 | .607 863 | 6.03 | .392 137 | 56 |
| 5 | 9.575 136 | 5.18 | 9.966 910 | .85 | 9.608 225 | 6.05 | 0.391 775 | 55 |
| 6 | .575 447 | 5.18 | .966 859 | .85 | .608 588 | 6.03 | .391 412 | 54 |
| 7 | .575 758 | 5.18 | .966 808 | .87 | .608 950 | 6.03 | .391 050 | 53 |
| 8 | .576 069 | 5.17 | .966 756 | .85 | .609 312 | 6.03 | .390 688 | 52 |
| 9 | .576 379 | 5.17 | .966 705 | .87 | .609 674 | 6.03 | .390 326 | 51 |
| 10 | 9.576 689 | 5.17 | 9.966 653 | .85 | 9.610 036 | 6.02 | 0.389 964 | 50 |
| 11 | .576 999 | 5.17 | .966 602 | .87 | .610 397 | 6.03 | .389 603 | 49 |
| 12 | .577 309 | 5.15 | .966 550 | .85 | .610 759 | 6.02 | .389 241 | 48 |
| 13 | .577 618 | 5.15 | .966 499 | .87 | .611 120 | 6.00 | .388 880 | 47 |
| 14 | .577 927 | 5.15 | .966 447 | .87 | .611 480 | 6.02 | .388 520 | 46 |
| 15 | 9.578 236 | 5.15 | 9.966 395 | .85 | 9.611 841 | 6.00 | 0.388 159 | 45 |
| 16 | .578 545 | 5.13 | .966 344 | .87 | .612 201 | 6.00 | .387 799 | 44 |
| 17 | .578 853 | 5.13 | .966 292 | .87 | .612 561 | 6.00 | .387 439 | 43 |
| 18 | .579 162 | 5.13 | .966 240 | .87 | .612 921 | 6.00 | .387 079 | 42 |
| 19 | .579 470 | 5.12 | .966 188 | .87 | .613 281 | 6.00 | .386 719 | 41 |
| 20 | 9.579 777 | 5.13 | 9.966 136 | .85 | 9.613 641 | 5.98 | 0.386 359 | 40 |
| 21 | .580 085 | 5.12 | .966 085 | .87 | .614 000 | 5.98 | .386 000 | 39 |
| 22 | .580 392 | 5.12 | .966 033 | .87 | .614 359 | 5.98 | .385 641 | 38 |
| 23 | .580 699 | 5.10 | .965 981 | .87 | .614 718 | 5.98 | .385 282 | 37 |
| 24 | .581 005 | 5.12 | .965 929 | .88 | .615 077 | 5.97 | .384 923 | 36 |
| 25 | 9.581 312 | 5.10 | 9.965 876 | .87 | 9.615 435 | 5.97 | 0.384 565 | 35 |
| 26 | .581 618 | 5.10 | .965 824 | .87 | .615 793 | 5.97 | .384 207 | 34 |
| 27 | .581 924 | 5.08 | .965 772 | .87 | .616 151 | 5.97 | .383 849 | 33 |
| 28 | .582 229 | 5.10 | .965 720 | .87 | .616 509 | 5.97 | .383 491 | 32 |
| 29 | .582 535 | 5.08 | .965 668 | .88 | .616 867 | 5.95 | .383 133 | 31 |
| 30 | 9.582 840 | 5.08 | 9.965 615 | .87 | 9.617 224 | 5.97 | 0.382 776 | 30 |
| 31 | .583 145 | 5.07 | .965 563 | .87 | .617 582 | 5.95 | .382 418 | 29 |
| 32 | .583 449 | 5.08 | .965 511 | .88 | .617 939 | 5.93 | .382 061 | 28 |
| 33 | .583 754 | 5.07 | .965 458 | .87 | .618 295 | 5.95 | .381 705 | 27 |
| 34 | .584 058 | 5.05 | .965 406 | .88 | .618 652 | 5.93 | .381 348 | 26 |
| 35 | 9.584 361 | 5.07 | 9.965 353 | .87 | 9.619 008 | 5.93 | 0.380 992 | 25 |
| 36 | .584 665 | 5.05 | .965 301 | .88 | .619 364 | 5.93 | .380 636 | 24 |
| 37 | .584 968 | 5.07 | .965 248 | .88 | .619 720 | 5.93 | .380 280 | 23 |
| 38 | .585 272 | 5.03 | .965 195 | .87 | .620 076 | 5.93 | .379 924 | 22 |
| 39 | .585 574 | 5.05 | .965 143 | .88 | .620 432 | 5.92 | .379 568 | 21 |
| 40 | 9.585 877 | 5.03 | 9.965 090 | .88 | 9.620 787 | 5.92 | 0.379 213 | 20 |
| 41 | .586 179 | 5.05 | .965 037 | .88 | .621 142 | 5.92 | .378 858 | 19 |
| 42 | .586 482 | 5.02 | .964 984 | .88 | .621 497 | 5.92 | .378 503 | 18 |
| 43 | .586 783 | 5.03 | .964 931 | .87 | .621 852 | 5.92 | .378 148 | 17 |
| 44 | .587 085 | 5.02 | .964 879 | .88 | .622 207 | 5.90 | .377 793 | 16 |
| 45 | 9.587 386 | 5.03 | 9.964 826 | .88 | 9.622 561 | 5.90 | 0.377 439 | 15 |
| 46 | .587 688 | 5.02 | .964 773 | .88 | .622 915 | 5.90 | .377 085 | 14 |
| 47 | .587 989 | 5.00 | .964 720 | .90 | .623 269 | 5.90 | .376 731 | 13 |
| 48 | .588 289 | 5.02 | .964 666 | .88 | .623 623 | 5.88 | .376 377 | 12 |
| 49 | .588 590 | 5.00 | .964 613 | .88 | .623 976 | 5.90 | .376 024 | 11 |
| 50 | 9.588 890 | 5.00 | 9.964 560 | .88 | 9.624 330 | 5.88 | 0.375 670 | 10 |
| 51 | .589 190 | 4.98 | .964 507 | .88 | .624 683 | 5.88 | .375 317 | 9 |
| 52 | .589 489 | 5.00 | .964 454 | .90 | .625 036 | 5.87 | .374 964 | 8 |
| 53 | .589 789 | 4.98 | .964 400 | .88 | .625 388 | 5.88 | .374 612 | 7 |
| 54 | .590 088 | 4.98 | .964 347 | .88 | .625 741 | 5.87 | .374 259 | 6 |
| 55 | 9.590 387 | 4.98 | 9.964 294 | .90 | 9.626 093 | 5.87 | 0.373 907 | 5 |
| 56 | .590 686 | 4.97 | .964 240 | .88 | .626 445 | 5.87 | .373 555 | 4 |
| 57 | .590 984 | 4.97 | .964 187 | .90 | .626 797 | 5.87 | .373 203 | 3 |
| 58 | .591 282 | 4.97 | .964 133 | .88 | .627 149 | 5.87 | .372 851 | 2 |
| 59 | .591 580 | 4.97 | .964 080 | .90 | .627 501 | 5.85 | .372 499 | 1 |
| 60 | 9.591 878 | 4.97 | 9.964 026 | | 9.627 852 | | 0.372 148 | 0 |

Cos. D. 1". Sin. D. 1". Cot. D. 1". Tan. M.

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.591 878 | 4.97 | 9.964 026 | .90 | 9.627 852 | 5.85 | 0.372 148 | 60 |
| 1 | .592 176 | 4.95 | .963 972 | .88 | .628 203 | 5.85 | .371 797 | 59 |
| 2 | .592 473 | 4.95 | .963 919 | .90 | .628 554 | 5.85 | .371 446 | 58 |
| 3 | .592 770 | 4.95 | .963 865 | .90 | .628 905 | 5.85 | .371 095 | 57 |
| 4 | .593 067 | 4.93 | .963 811 | .90 | .629 255 | 5.83 | .370 745 | 56 |
| 5 | 9.593 363 | 4.93 | 9.963 757 | .88 | 9.629 606 | 5.83 | 0.370 394 | 55 |
| 6 | .593 659 | 4.93 | .963 704 | .90 | .629 956 | 5.83 | .370 044 | 54 |
| 7 | .593 955 | 4.93 | .963 650 | .90 | .630 306 | 5.83 | .369 694 | 53 |
| 8 | .594 251 | 4.93 | .963 596 | .90 | .630 656 | 5.82 | .369 344 | 52 |
| 9 | .594 547 | 4.92 | .963 542 | .90 | .631 005 | 5.83 | .368 995 | 51 |
| 10 | 9.594 842 | 4.92 | 9.963 488 | .90 | 9.631 355 | 5.82 | 0.368 645 | 50 |
| 11 | .595 137 | 4.92 | .963 434 | .92 | .631 704 | 5.82 | .368 296 | 49 |
| 12 | .595 432 | 4.92 | .963 379 | .90 | .632 053 | 5.82 | .367 947 | 48 |
| 13 | .595 727 | 4.90 | .963 325 | .90 | .632 402 | 5.80 | .367 598 | 47 |
| 14 | .596 021 | 4.90 | .963 271 | .90 | .632 750 | 5.82 | .367 250 | 46 |
| 15 | 9.596 315 | 4.90 | 9.963 217 | .90 | 9.633 099 | 5.80 | 0.366 901 | 45 |
| 16 | .596 609 | 4.90 | .963 163 | .92 | .633 447 | 5.80 | .366 553 | 44 |
| 17 | .596 903 | 4.88 | .963 108 | .90 | .633 795 | 5.80 | .366 205 | 43 |
| 18 | .597 196 | 4.90 | .963 054 | .92 | .634 143 | 5.78 | .365 857 | 42 |
| 19 | .597 490 | 4.88 | .962 999 | .90 | .634 490 | 5.80 | .365 510 | 41 |
| 20 | 9.597 783 | 4.87 | 9.962 945 | .92 | 9.634 838 | 5.78 | 0.365 162 | 40 |
| 21 | .598 075 | 4.88 | .962 890 | .90 | .635 185 | 5.78 | .364 815 | 39 |
| 22 | .598 368 | 4.87 | .962 836 | .92 | .635 532 | 5.78 | .364 468 | 38 |
| 23 | .598 660 | 4.87 | .962 781 | .90 | .635 879 | 5.78 | .364 121 | 37 |
| 24 | .598 952 | 4.87 | .962 727 | .92 | .636 226 | 5.77 | .363 774 | 36 |
| 25 | 9.599 244 | 4.87 | 9.962 672 | .92 | 9.636 572 | 5.78 | 0.363 428 | 35 |
| 26 | .599 536 | 4.85 | .962 617 | .92 | .636 919 | 5.77 | .363 081 | 34 |
| 27 | .599 827 | 4.85 | .962 562 | .92 | .637 265 | 5.77 | .362 735 | 33 |
| 28 | .600 118 | 4.85 | .962 508 | .92 | .637 611 | 5.77 | .362 389 | 32 |
| 29 | .600 409 | 4.85 | .962 453 | .92 | .637 956 | 5.75 | .362 044 | 31 |
| 30 | 9.600 700 | 4.83 | 9.962 398 | .92 | 9.638 302 | 5.75 | 0.361 698 | 30 |
| 31 | .600 990 | 4.83 | .962 343 | .92 | .638 647 | 5.75 | .361 353 | 29 |
| 32 | .601 280 | 4.83 | .962 288 | .92 | .638 992 | 5.75 | .361 008 | 28 |
| 33 | .601 570 | 4.83 | .962 233 | .92 | .639 337 | 5.75 | .360 663 | 27 |
| 34 | .601 860 | 4.83 | .962 178 | .92 | .639 682 | 5.75 | .360 318 | 26 |
| 35 | 9.602 150 | 4.82 | 9.962 123 | .93 | 9.640 027 | 5.73 | 0.359 973 | 25 |
| 36 | .602 439 | 4.82 | .962 067 | .92 | .640 371 | 5.75 | .359 629 | 24 |
| 37 | .602 728 | 4.82 | .962 012 | .92 | .640 716 | 5.73 | .359 284 | 23 |
| 38 | .603 017 | 4.80 | .961 957 | .92 | .641 060 | 5.73 | .358 940 | 22 |
| 39 | .603 305 | 4.82 | .961 902 | .93 | .641 404 | 5.72 | .358 596 | 21 |
| 40 | 9.603 594 | 4.80 | 9.961 846 | .92 | 9.641 747 | 5.73 | 0.358 253 | 20 |
| 41 | .603 882 | 4.80 | .961 791 | .92 | .642 091 | 5.72 | .357 909 | 19 |
| 42 | .604 170 | 4.78 | .961 735 | .93 | .642 434 | 5.72 | .357 566 | 18 |
| 43 | .604 457 | 4.80 | .961 680 | .93 | .642 777 | 5.72 | .357 223 | 17 |
| 44 | .604 745 | 4.78 | .961 624 | .92 | .643 120 | 5.72 | .356 880 | 16 |
| 45 | 9.605 032 | 4.78 | 9.961 569 | .93 | 9.643 463 | 5.72 | 0.356 537 | 15 |
| 46 | .605 319 | 4.78 | .961 513 | .92 | .643 806 | 5.70 | .356 194 | 14 |
| 47 | .605 606 | 4.77 | .961 458 | .92 | .644 148 | 5.70 | .355 852 | 13 |
| 48 | .605 892 | 4.78 | .961 402 | .93 | .644 490 | 5.70 | .355 510 | 12 |
| 49 | .606 179 | 4.77 | .961 346 | .93 | .644 832 | 5.70 | .355 168 | 11 |
| 50 | 9.606 465 | 4.77 | 9.961 290 | .92 | 9.645 174 | 5.70 | 0.354 826 | 10 |
| 51 | .606 751 | 4.75 | .961 235 | .93 | .645 516 | 5.68 | .354 484 | 9 |
| 52 | .607 036 | 4.77 | .961 179 | .93 | .645 857 | 5.70 | .354 143 | 8 |
| 53 | .607 322 | 4.75 | .961 123 | .93 | .646 199 | 5.68 | .353 801 | 7 |
| 54 | .607 607 | 4.75 | .961 067 | .93 | .646 540 | 5.68 | .353 460 | 6 |
| 55 | 9.607 892 | 4.75 | 9.961 011 | .93 | 9.646 881 | 5.68 | 0.353 119 | 5 |
| 56 | .608 177 | 4.73 | .960 955 | .93 | .647 222 | 5.67 | .352 778 | 4 |
| 57 | .608 461 | 4.73 | .960 899 | .93 | .647 562 | 5.68 | .352 438 | 3 |
| 58 | .608 745 | 4.73 | .960 843 | .93 | .647 903 | 5.67 | .352 097 | 2 |
| 59 | .609 029 | 4.73 | .960 786 | .95 | .648 243 | 5.67 | .351 757 | 1 |
| 60 | 9.609 313 | 4.73 | 9.960 730 | .93 | 9.648 583 | 5.67 | 0.351 417 | 0 |

| M. | Sin. | D. 1''. | Cos. | D. 1''. | Tan. | D. 1''. | Cot. | M. |
|----|-----------|---------|-----------|---------|-----------|---------|-----------|----|
| 0 | 9.609 313 | | 9.960 730 | | 9.648 583 | | 0.351 417 | 60 |
| 1 | .609 597 | 4.73 | .960 674 | .93 | .648 923 | 5.67 | .351 077 | 59 |
| 2 | .609 880 | 4.72 | .960 618 | .93 | .649 263 | 5.67 | .350 737 | 58 |
| 3 | .610 164 | 4.73 | .960 561 | .95 | .649 602 | 5.65 | .350 398 | 57 |
| 4 | .610 447 | 4.72 | .960 505 | .93 | .649 942 | 5.67 | .350 058 | 56 |
| 5 | 9.610 729 | 4.70 | 9.960 448 | .95 | 9.650 281 | 5.65 | 0.349 719 | 55 |
| 6 | .611 012 | 4.72 | .960 392 | .93 | .650 620 | 5.65 | .349 380 | 54 |
| 7 | .611 294 | 4.70 | .960 335 | .95 | .650 959 | 5.65 | .349 041 | 53 |
| 8 | .611 576 | 4.70 | .960 279 | .93 | .651 297 | 5.63 | .348 703 | 52 |
| 9 | .611 858 | 4.70 | .960 222 | .95 | .651 636 | 5.65 | .348 364 | 51 |
| 10 | 9.612 140 | 4.68 | 9.960 165 | .95 | 9.651 974 | 5.63 | 0.348 026 | 50 |
| 11 | .612 421 | 4.68 | .960 109 | .93 | .652 312 | 5.63 | .347 688 | 49 |
| 12 | .612 702 | 4.68 | .960 052 | .95 | .652 650 | 5.63 | .347 350 | 48 |
| 13 | .612 983 | 4.68 | .959 995 | .95 | .652 988 | 5.63 | .347 012 | 47 |
| 14 | .613 264 | 4.68 | .959 938 | .93 | .653 326 | 5.63 | .346 674 | 46 |
| 15 | 9.613 545 | 4.67 | 9.959 882 | .95 | 9.653 663 | 5.62 | 0.346 337 | 45 |
| 16 | .613 825 | 4.67 | .959 825 | .95 | .654 000 | 5.62 | .346 000 | 44 |
| 17 | .614 105 | 4.67 | .959 768 | .95 | .654 337 | 5.62 | .345 663 | 43 |
| 18 | .614 385 | 4.67 | .959 711 | .95 | .654 674 | 5.62 | .345 326 | 42 |
| 19 | .614 665 | 4.65 | .959 654 | .95 | .655 011 | 5.62 | .344 989 | 41 |
| 20 | 9.614 944 | 4.65 | 9.959 596 | .95 | 9.655 348 | 5.60 | 0.344 652 | 40 |
| 21 | .615 223 | 4.65 | .959 539 | .95 | .655 684 | 5.60 | .344 316 | 39 |
| 22 | .615 502 | 4.65 | .959 482 | .95 | .656 020 | 5.60 | .343 980 | 38 |
| 23 | .615 781 | 4.65 | .959 425 | .95 | .656 356 | 5.60 | .343 644 | 37 |
| 24 | .616 060 | 4.63 | .959 368 | .97 | .656 692 | 5.60 | .343 308 | 36 |
| 25 | 9.616 338 | 4.63 | 9.959 310 | .95 | 9.657 028 | 5.60 | 0.342 972 | 35 |
| 26 | .616 616 | 4.63 | .959 253 | .95 | .657 364 | 5.58 | .342 636 | 34 |
| 27 | .616 894 | 4.63 | .959 195 | .97 | .657 699 | 5.58 | .342 301 | 33 |
| 28 | .617 172 | 4.63 | .959 138 | .95 | .658 034 | 5.58 | .341 966 | 32 |
| 29 | .617 450 | 4.62 | .959 080 | .97 | .658 369 | 5.58 | .341 631 | 31 |
| 30 | 9.617 727 | 4.62 | 9.959 023 | .95 | 9.658 704 | 5.58 | 0.341 296 | 30 |
| 31 | .618 004 | 4.62 | .958 965 | .97 | .659 039 | 5.58 | .340 961 | 29 |
| 32 | .618 281 | 4.62 | .958 908 | .95 | .659 373 | 5.57 | .340 627 | 28 |
| 33 | .618 558 | 4.60 | .958 850 | .97 | .659 708 | 5.57 | .340 292 | 27 |
| 34 | .618 834 | 4.60 | .958 792 | .97 | .660 042 | 5.57 | .339 958 | 26 |
| 35 | 9.619 110 | 4.60 | 9.958 734 | .95 | 9.660 376 | 5.57 | 0.339 624 | 25 |
| 36 | .619 386 | 4.60 | .958 677 | .97 | .660 710 | 5.55 | .339 290 | 24 |
| 37 | .619 662 | 4.60 | .958 619 | .97 | .661 043 | 5.55 | .338 957 | 23 |
| 38 | .619 938 | 4.58 | .958 561 | .97 | .661 377 | 5.55 | .338 623 | 22 |
| 39 | .620 213 | 4.58 | .958 503 | .97 | .661 710 | 5.55 | .338 290 | 21 |
| 40 | 9.620 488 | 4.58 | 9.958 445 | .97 | 9.662 043 | 5.55 | 0.337 957 | 20 |
| 41 | .620 763 | 4.58 | .958 387 | .97 | .662 376 | 5.55 | .337 624 | 19 |
| 42 | .621 038 | 4.58 | .958 329 | .97 | .662 709 | 5.55 | .337 291 | 18 |
| 43 | .621 313 | 4.58 | .958 271 | .97 | .663 042 | 5.55 | .336 958 | 17 |
| 44 | .621 587 | 4.57 | .958 213 | .97 | .663 375 | 5.55 | .336 625 | 16 |
| 45 | 9.621 861 | 4.57 | 9.958 154 | .97 | 9.663 707 | 5.53 | 0.336 293 | 15 |
| 46 | .622 135 | 4.57 | .958 096 | .97 | .664 039 | 5.53 | .335 961 | 14 |
| 47 | .622 409 | 4.55 | .958 038 | .98 | .664 371 | 5.53 | .335 629 | 13 |
| 48 | .622 682 | 4.55 | .957 979 | .98 | .664 703 | 5.53 | .335 297 | 12 |
| 49 | .622 956 | 4.57 | .957 921 | .97 | .665 035 | 5.53 | .334 965 | 11 |
| 50 | 9.623 229 | 4.55 | 9.957 863 | .97 | 9.665 366 | 5.52 | 0.334 634 | 10 |
| 51 | .623 502 | 4.53 | .957 804 | .98 | .665 698 | 5.52 | .334 302 | 9 |
| 52 | .623 774 | 4.55 | .957 746 | .98 | .666 029 | 5.52 | .333 971 | 8 |
| 53 | .624 047 | 4.53 | .957 687 | .98 | .666 360 | 5.52 | .333 640 | 7 |
| 54 | .624 319 | 4.53 | .957 628 | .97 | .666 691 | 5.50 | .333 309 | 6 |
| 55 | 9.624 591 | 4.53 | 9.957 570 | .98 | 9.667 021 | 5.52 | 0.332 979 | 5 |
| 56 | .624 863 | 4.53 | .957 511 | .98 | .667 352 | 5.50 | .332 648 | 4 |
| 57 | .625 135 | 4.52 | .957 452 | .98 | .667 682 | 5.52 | .332 318 | 3 |
| 58 | .625 406 | 4.52 | .957 393 | .97 | .668 013 | 5.50 | .331 987 | 2 |
| 59 | .625 677 | 4.52 | .957 335 | .98 | .668 343 | 5.50 | .331 657 | 1 |
| 60 | 9.625 948 | 4.52 | 9.957 276 | .97 | 9.668 673 | 5.50 | 0.331 327 | 0 |

Cos. D. 1''. Sin. D. 1''. Cot. D. 1''. Tan. M.

25°

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.625 948 | | 9.957 276 | | 9.668 673 | | 0.331 327 | 60 |
| 1 | .626 219 | 4.52 | .957 217 | .98 | .669 002 | 5.48 | .330 998 | 59 |
| 2 | .626 490 | 4.52 | .957 158 | .98 | .669 332 | 5.50 | .330 668 | 58 |
| 3 | .626 760 | 4.50 | .957 099 | .98 | .669 661 | 5.48 | .330 339 | 57 |
| 4 | .627 030 | 4.50 | .957 040 | .98 | .669 991 | 5.50 | .330 009 | 56 |
| 5 | 9.627 300 | | 9.956 981 | 1.00 | 9.670 320 | | 0.329 680 | 55 |
| 6 | .627 570 | 4.50 | .956 921 | .98 | .670 649 | 5.48 | .329 351 | 54 |
| 7 | .627 840 | 4.50 | .956 862 | .98 | .670 977 | 5.47 | .329 023 | 53 |
| 8 | .628 109 | 4.48 | .956 803 | .98 | .671 306 | 5.48 | .328 694 | 52 |
| 9 | .628 378 | 4.48 | .956 744 | .98 | .671 635 | 5.48 | .328 365 | 51 |
| 10 | 9.628 647 | | 9.956 684 | 1.00 | 9.671 963 | | 0.328 037 | 50 |
| 11 | .628 916 | 4.48 | .956 625 | .98 | .672 291 | 5.47 | .327 709 | 49 |
| 12 | .629 185 | 4.48 | .956 566 | .98 | .672 619 | 5.47 | .327 381 | 48 |
| 13 | .629 453 | 4.47 | .956 506 | 1.00 | .672 947 | 5.47 | .327 053 | 47 |
| 14 | .629 721 | 4.47 | .956 447 | .98 | .673 274 | 5.45 | .326 726 | 46 |
| 15 | 9.629 989 | | 9.956 387 | 1.00 | 9.673 602 | | 0.326 398 | 45 |
| 16 | .630 257 | 4.47 | .956 327 | .98 | .673 929 | 5.45 | .326 071 | 44 |
| 17 | .630 524 | 4.45 | .956 268 | .98 | .674 257 | 5.47 | .325 743 | 43 |
| 18 | .630 792 | 4.47 | .956 208 | 1.00 | .674 584 | 5.45 | .325 416 | 42 |
| 19 | .631 059 | 4.45 | .956 148 | .98 | .674 911 | 5.45 | .325 089 | 41 |
| 20 | 9.631 326 | | 9.956 089 | 1.00 | 9.675 237 | | 0.324 763 | 40 |
| 21 | .631 593 | 4.45 | .956 029 | 1.00 | .675 564 | 5.45 | .324 436 | 39 |
| 22 | .631 859 | 4.43 | .955 969 | 1.00 | .675 890 | 5.43 | .324 110 | 38 |
| 23 | .632 125 | 4.43 | .955 909 | 1.00 | .676 217 | 5.45 | .323 783 | 37 |
| 24 | .632 392 | 4.45 | .955 849 | 1.00 | .676 543 | 5.43 | .323 457 | 36 |
| 25 | 9.632 658 | | 9.955 789 | 1.00 | 9.676 869 | | 0.323 131 | 35 |
| 26 | .632 923 | 4.42 | .955 729 | 1.00 | .677 194 | 5.42 | .322 806 | 34 |
| 27 | .633 189 | 4.43 | .955 669 | 1.00 | .677 520 | 5.43 | .322 480 | 33 |
| 28 | .633 454 | 4.42 | .955 609 | 1.00 | .677 846 | 5.43 | .322 154 | 32 |
| 29 | .633 719 | 4.42 | .955 548 | 1.02 | .678 171 | 5.42 | .321 829 | 31 |
| 30 | 9.633 984 | | 9.955 488 | 1.00 | 9.678 496 | | 0.321 504 | 30 |
| 31 | .634 249 | 4.42 | .955 428 | 1.00 | .678 821 | 5.42 | .321 179 | 29 |
| 32 | .634 514 | 4.42 | .955 368 | 1.00 | .679 146 | 5.42 | .320 854 | 28 |
| 33 | .634 778 | 4.40 | .955 307 | 1.02 | .679 471 | 5.42 | .320 529 | 27 |
| 34 | .635 042 | 4.40 | .955 247 | 1.02 | .679 795 | 5.40 | .320 205 | 26 |
| 35 | 9.635 306 | | 9.955 186 | 1.00 | 9.680 120 | | 0.319 880 | 25 |
| 36 | .635 570 | 4.40 | .955 126 | 1.00 | .680 444 | 5.40 | .319 556 | 24 |
| 37 | .635 834 | 4.40 | .955 065 | 1.02 | .680 768 | 5.40 | .319 232 | 23 |
| 38 | .636 097 | 4.38 | .955 005 | 1.00 | .681 092 | 5.40 | .318 908 | 22 |
| 39 | .636 360 | 4.38 | .954 944 | 1.02 | .681 416 | 5.40 | .318 584 | 21 |
| 40 | 9.636 623 | | 9.954 883 | 1.00 | 9.681 740 | | 0.318 260 | 20 |
| 41 | .636 886 | 4.38 | .954 823 | 1.00 | .682 063 | 5.38 | .317 937 | 19 |
| 42 | .637 148 | 4.37 | .954 762 | 1.02 | .682 387 | 5.40 | .317 613 | 18 |
| 43 | .637 411 | 4.38 | .954 701 | 1.02 | .682 710 | 5.38 | .317 290 | 17 |
| 44 | .637 673 | 4.37 | .954 640 | 1.02 | .683 033 | 5.38 | .316 967 | 16 |
| 45 | 9.637 935 | | 9.954 579 | 1.00 | 9.683 356 | | 0.316 644 | 15 |
| 46 | .638 197 | 4.37 | .954 518 | 1.02 | .683 679 | 5.38 | .316 321 | 14 |
| 47 | .638 458 | 4.35 | .954 457 | 1.02 | .684 001 | 5.37 | .315 999 | 13 |
| 48 | .638 720 | 4.37 | .954 396 | 1.02 | .684 324 | 5.38 | .315 676 | 12 |
| 49 | .638 981 | 4.35 | .954 335 | 1.02 | .684 646 | 5.37 | .315 354 | 11 |
| 50 | 9.639 242 | | 9.954 274 | 1.00 | 9.684 968 | | 0.315 032 | 10 |
| 51 | .639 503 | 4.35 | .954 213 | 1.02 | .685 290 | 5.37 | .314 710 | 9 |
| 52 | .639 764 | 4.35 | .954 152 | 1.02 | .685 612 | 5.37 | .314 388 | 8 |
| 53 | .640 024 | 4.33 | .954 090 | 1.03 | .685 934 | 5.37 | .314 066 | 7 |
| 54 | .640 284 | 4.33 | .954 029 | 1.02 | .686 255 | 5.35 | .313 745 | 6 |
| 55 | 9.640 544 | | 9.953 968 | 1.00 | 9.686 577 | | 0.313 423 | 5 |
| 56 | .640 804 | 4.33 | .953 906 | 1.03 | .686 898 | 5.35 | .313 102 | 4 |
| 57 | .641 064 | 4.33 | .953 845 | 1.02 | .687 219 | 5.35 | .312 781 | 3 |
| 58 | .641 324 | 4.33 | .953 783 | 1.03 | .687 540 | 5.35 | .312 460 | 2 |
| 59 | .641 583 | 4.32 | .953 722 | 1.02 | .687 861 | 5.35 | .312 139 | 1 |
| 60 | 9.641 842 | | 9.953 660 | 1.03 | 9.688 182 | | 0.311 818 | 0 |

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.641 842 | 4.32 | 9.953 660 | 1.02 | 9.688 182 | 5.33 | 0.311 818 | 60 |
| 1 | .642 101 | 4.32 | .953 599 | 1.03 | .688 502 | 5.35 | .311 498 | 59 |
| 2 | .642 360 | 4.30 | .953 537 | 1.03 | .688 823 | 5.33 | .311 177 | 58 |
| 3 | .642 618 | 4.32 | .953 475 | 1.03 | .689 143 | 5.33 | .310 857 | 57 |
| 4 | .642 877 | 4.30 | .953 413 | 1.02 | .689 463 | 5.33 | .310 537 | 56 |
| 5 | 9.643 135 | 4.30 | 9.953 352 | 1.03 | 9.689 783 | 5.33 | 0.310 217 | 55 |
| 6 | .643 393 | 4.28 | .953 290 | 1.03 | .690 103 | 5.33 | .309 897 | 54 |
| 7 | .643 650 | 4.30 | .953 228 | 1.03 | .690 423 | 5.33 | .309 577 | 53 |
| 8 | .643 908 | 4.28 | .953 166 | 1.03 | .690 742 | 5.32 | .309 258 | 52 |
| 9 | .644 165 | 4.30 | .953 104 | 1.03 | .691 062 | 5.33 | .308 938 | 51 |
| 10 | 9.644 423 | 4.28 | 9.953 042 | 1.03 | 9.691 381 | 5.32 | 0.308 619 | 50 |
| 11 | .644 680 | 4.27 | .952 980 | 1.03 | .691 700 | 5.32 | .308 300 | 49 |
| 12 | .644 936 | 4.28 | .952 918 | 1.05 | .692 019 | 5.32 | .307 981 | 48 |
| 13 | .645 193 | 4.28 | .952 855 | 1.03 | .692 338 | 5.32 | .307 662 | 47 |
| 14 | .645 450 | 4.27 | .952 793 | 1.03 | .692 656 | 5.30 | .307 344 | 46 |
| 15 | 9.645 706 | 4.27 | 9.952 731 | 1.03 | 9.692 975 | 5.30 | 0.307 025 | 45 |
| 16 | .645 962 | 4.27 | .952 669 | 1.05 | .693 293 | 5.32 | .306 707 | 44 |
| 17 | .646 218 | 4.27 | .952 606 | 1.03 | .693 612 | 5.30 | .306 388 | 43 |
| 18 | .646 474 | 4.25 | .952 544 | 1.05 | .693 930 | 5.30 | .306 070 | 42 |
| 19 | .646 729 | 4.25 | .952 481 | 1.03 | .694 248 | 5.30 | .305 752 | 41 |
| 20 | 9.646 984 | 4.27 | 9.952 419 | 1.05 | 9.694 566 | 5.28 | 0.305 434 | 40 |
| 21 | .647 240 | 4.23 | .952 356 | 1.03 | .694 883 | 5.30 | .305 117 | 39 |
| 22 | .647 494 | 4.25 | .952 294 | 1.05 | .695 201 | 5.28 | .304 799 | 38 |
| 23 | .647 749 | 4.25 | .952 231 | 1.05 | .695 518 | 5.30 | .304 482 | 37 |
| 24 | .648 004 | 4.23 | .952 168 | 1.03 | .695 836 | 5.28 | .304 164 | 36 |
| 25 | 9.648 258 | 4.23 | 9.952 106 | 1.05 | 9.696 153 | 5.28 | 0.303 847 | 35 |
| 26 | .648 512 | 4.23 | .952 043 | 1.05 | .696 470 | 5.28 | .303 530 | 34 |
| 27 | .648 766 | 4.23 | .951 980 | 1.05 | .696 787 | 5.27 | .303 213 | 33 |
| 28 | .649 020 | 4.23 | .951 917 | 1.05 | .697 103 | 5.28 | .302 897 | 32 |
| 29 | .649 274 | 4.22 | .951 854 | 1.05 | .697 420 | 5.27 | .302 580 | 31 |
| 30 | 9.649 527 | 4.23 | 9.951 791 | 1.05 | 9.697 736 | 5.28 | 0.302 264 | 30 |
| 31 | .649 781 | 4.22 | .951 728 | 1.05 | .698 053 | 5.27 | .301 947 | 29 |
| 32 | .650 034 | 4.22 | .951 665 | 1.05 | .698 369 | 5.27 | .301 631 | 28 |
| 33 | .650 287 | 4.20 | .951 602 | 1.05 | .698 685 | 5.27 | .301 315 | 27 |
| 34 | .650 539 | 4.22 | .951 539 | 1.05 | .699 001 | 5.25 | .300 999 | 26 |
| 35 | 9.650 792 | 4.20 | 9.951 476 | 1.07 | 9.699 316 | 5.27 | 0.300 684 | 25 |
| 36 | .651 044 | 4.22 | .951 412 | 1.05 | .699 632 | 5.25 | .300 368 | 24 |
| 37 | .651 297 | 4.20 | .951 349 | 1.05 | .699 947 | 5.25 | .300 053 | 23 |
| 38 | .651 549 | 4.18 | .951 286 | 1.05 | .700 263 | 5.27 | .299 737 | 22 |
| 39 | .651 800 | 4.20 | .951 222 | 1.05 | .700 578 | 5.25 | .299 422 | 21 |
| 40 | 9.652 052 | 4.20 | 9.951 159 | 1.05 | 9.700 893 | 5.25 | 0.299 107 | 20 |
| 41 | .652 304 | 4.18 | .951 096 | 1.07 | .701 208 | 5.25 | .298 792 | 19 |
| 42 | .652 555 | 4.18 | .951 032 | 1.07 | .701 523 | 5.23 | .298 477 | 18 |
| 43 | .652 806 | 4.18 | .950 968 | 1.07 | .701 837 | 5.23 | .298 163 | 17 |
| 44 | .653 057 | 4.18 | .950 905 | 1.05 | .702 152 | 5.23 | .297 848 | 16 |
| 45 | 9.653 308 | 4.17 | 9.950 841 | 1.05 | 9.702 466 | 5.25 | 0.297 534 | 15 |
| 46 | .653 558 | 4.17 | .950 778 | 1.07 | .702 781 | 5.23 | .297 219 | 14 |
| 47 | .653 808 | 4.18 | .950 714 | 1.07 | .703 095 | 5.23 | .296 905 | 13 |
| 48 | .654 059 | 4.17 | .950 650 | 1.07 | .703 409 | 5.22 | .296 591 | 12 |
| 49 | .654 309 | 4.15 | .950 586 | 1.07 | .703 722 | 5.23 | .296 278 | 11 |
| 50 | 9.654 558 | 4.17 | 9.950 522 | 1.07 | 9.704 036 | 5.23 | 0.295 964 | 10 |
| 51 | .654 808 | 4.17 | .950 458 | 1.07 | .704 350 | 5.22 | .295 650 | 9 |
| 52 | .655 058 | 4.15 | .950 394 | 1.07 | .704 663 | 5.22 | .295 337 | 8 |
| 53 | .655 307 | 4.15 | .950 330 | 1.07 | .704 976 | 5.22 | .295 024 | 7 |
| 54 | .655 556 | 4.15 | .950 266 | 1.07 | .705 290 | 5.22 | .294 710 | 6 |
| 55 | 9.655 805 | 4.15 | 9.950 202 | 1.07 | 9.705 603 | 5.22 | 0.294 397 | 5 |
| 56 | .656 054 | 4.13 | .950 138 | 1.07 | .705 916 | 5.20 | .294 084 | 4 |
| 57 | .656 302 | 4.15 | .950 074 | 1.07 | .706 228 | 5.22 | .293 772 | 3 |
| 58 | .656 551 | 4.13 | .950 010 | 1.08 | .706 541 | 5.22 | .293 459 | 2 |
| 59 | .656 799 | 4.13 | .949 945 | 1.07 | .706 854 | 5.20 | .293 146 | 1 |
| 60 | 9.657 047 | | 9.949 881 | | 9.707 166 | | 0.292 834 | 0 |

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.657 047 | | 9.949 881 | 1.08 | 9.707 166 | | 0.292 834 | 60 |
| 1 | .657 295 | 4.13 | .949 816 | 1.07 | .707 478 | 5.20 | .292 522 | 59 |
| 2 | .657 542 | 4.12 | .949 752 | 1.07 | .707 790 | 5.20 | .292 210 | 58 |
| 3 | .657 790 | 4.13 | .949 688 | 1.07 | .708 102 | 5.20 | .291 898 | 57 |
| 4 | .658 037 | 4.12 | .949 623 | 1.08 | .708 414 | 5.20 | .291 586 | 56 |
| 5 | 9.658 284 | | 9.949 558 | 1.07 | 9.708 726 | 5.18 | 0.291 274 | 55 |
| 6 | .658 531 | 4.12 | .949 494 | 1.08 | .709 037 | 5.20 | .290 963 | 54 |
| 7 | .658 778 | 4.12 | .949 429 | 1.08 | .709 349 | 5.18 | .290 651 | 53 |
| 8 | .659 025 | 4.12 | .949 364 | 1.08 | .709 660 | 5.18 | .290 340 | 52 |
| 9 | .659 271 | 4.10 | .949 300 | 1.07 | .709 971 | 5.18 | .290 029 | 51 |
| 10 | 9.659 517 | | 9.949 235 | 1.08 | 9.710 282 | 5.18 | 0.289 718 | 50 |
| 11 | .659 763 | 4.10 | .949 170 | 1.08 | .710 593 | 5.18 | .289 407 | 49 |
| 12 | .660 009 | 4.10 | .949 105 | 1.08 | .710 904 | 5.18 | .289 096 | 48 |
| 13 | .660 255 | 4.10 | .949 040 | 1.08 | .711 215 | 5.17 | .288 785 | 47 |
| 14 | .660 501 | 4.08 | .948 975 | 1.08 | .711 525 | 5.18 | .288 475 | 46 |
| 15 | 9.660 746 | | 9.948 910 | 1.08 | 9.711 836 | 5.17 | 0.288 164 | 45 |
| 16 | .660 991 | 4.08 | .948 845 | 1.08 | .712 146 | 5.17 | .287 854 | 44 |
| 17 | .661 236 | 4.08 | .948 780 | 1.08 | .712 456 | 5.17 | .287 544 | 43 |
| 18 | .661 481 | 4.08 | .948 715 | 1.08 | .712 766 | 5.17 | .287 234 | 42 |
| 19 | .661 726 | 4.07 | .948 650 | 1.10 | .713 076 | 5.17 | .286 924 | 41 |
| 20 | 9.661 970 | | 9.948 584 | 1.08 | 9.713 386 | 5.17 | 0.286 614 | 40 |
| 21 | .662 214 | 4.07 | .948 519 | 1.08 | .713 696 | 5.15 | .286 304 | 39 |
| 22 | .662 459 | 4.08 | .948 454 | 1.10 | .714 005 | 5.15 | .285 995 | 38 |
| 23 | .662 703 | 4.07 | .948 388 | 1.08 | .714 314 | 5.15 | .285 686 | 37 |
| 24 | .662 946 | 4.05 | .948 323 | 1.10 | .714 624 | 5.17 | .285 376 | 36 |
| 25 | 9.663 190 | | 9.948 257 | 1.08 | 9.714 933 | 5.15 | 0.285 067 | 35 |
| 26 | .663 433 | 4.05 | .948 192 | 1.10 | .715 242 | 5.15 | .284 758 | 34 |
| 27 | .663 677 | 4.07 | .948 126 | 1.10 | .715 551 | 5.15 | .284 449 | 33 |
| 28 | .663 920 | 4.05 | .948 060 | 1.10 | .715 860 | 5.15 | .284 140 | 32 |
| 29 | .664 163 | 4.05 | .947 995 | 1.08 | .716 168 | 5.13 | .283 832 | 31 |
| 30 | 9.664 406 | | 9.947 929 | 1.10 | 9.716 477 | 5.15 | 0.283 523 | 30 |
| 31 | .664 648 | 4.03 | .947 863 | 1.10 | .716 785 | 5.13 | .283 215 | 29 |
| 32 | .664 891 | 4.05 | .947 797 | 1.10 | .717 093 | 5.13 | .282 907 | 28 |
| 33 | .665 133 | 4.03 | .947 731 | 1.10 | .717 401 | 5.13 | .282 599 | 27 |
| 34 | .665 375 | 4.03 | .947 665 | 1.08 | .717 709 | 5.13 | .282 291 | 26 |
| 35 | 9.665 617 | | 9.947 600 | 1.12 | 9.718 017 | 5.13 | 0.281 983 | 25 |
| 36 | .665 859 | 4.03 | .947 533 | 1.10 | .718 325 | 5.13 | .281 675 | 24 |
| 37 | .666 100 | 4.02 | .947 467 | 1.10 | .718 633 | 5.12 | .281 367 | 23 |
| 38 | .666 342 | 4.03 | .947 401 | 1.10 | .718 940 | 5.12 | .281 060 | 22 |
| 39 | .666 583 | 4.02 | .947 335 | 1.10 | .719 248 | 5.13 | .280 752 | 21 |
| 40 | 9.666 824 | | 9.947 269 | 1.10 | 9.719 555 | 5.12 | 0.280 445 | 20 |
| 41 | .667 065 | 4.02 | .947 203 | 1.12 | .719 862 | 5.12 | .280 138 | 19 |
| 42 | .667 305 | 4.00 | .947 136 | 1.10 | .720 169 | 5.12 | .279 831 | 18 |
| 43 | .667 546 | 4.02 | .947 070 | 1.10 | .720 476 | 5.12 | .279 524 | 17 |
| 44 | .667 786 | 4.02 | .947 004 | 1.12 | .720 783 | 5.10 | .279 217 | 16 |
| 45 | 9.668 027 | | 9.946 937 | 1.10 | 9.721 089 | 5.12 | 0.278 911 | 15 |
| 46 | .668 267 | 3.98 | .946 871 | 1.12 | .721 396 | 5.12 | .278 604 | 14 |
| 47 | .668 506 | 3.98 | .946 804 | 1.10 | .721 702 | 5.10 | .278 298 | 13 |
| 48 | .668 746 | 4.00 | .946 738 | 1.12 | .722 009 | 5.12 | .277 991 | 12 |
| 49 | .668 986 | 3.98 | .946 671 | 1.12 | .722 315 | 5.10 | .277 685 | 11 |
| 50 | 9.669 225 | | 9.946 604 | 1.10 | 9.722 621 | 5.10 | 0.277 379 | 10 |
| 51 | .669 464 | 3.98 | .946 538 | 1.12 | .722 927 | 5.08 | .277 073 | 9 |
| 52 | .669 703 | 3.98 | .946 471 | 1.12 | .723 232 | 5.10 | .276 768 | 8 |
| 53 | .669 942 | 3.98 | .946 404 | 1.12 | .723 538 | 5.10 | .276 462 | 7 |
| 54 | .670 181 | 3.98 | .946 337 | 1.12 | .723 843 | 5.10 | .276 156 | 6 |
| 55 | 9.670 419 | | 9.946 270 | 1.12 | 9.724 149 | 5.08 | 0.275 851 | 5 |
| 56 | .670 658 | 3.98 | .946 203 | 1.12 | .724 454 | 5.10 | .275 546 | 4 |
| 57 | .670 896 | 3.97 | .946 136 | 1.12 | .724 760 | 5.08 | .275 240 | 3 |
| 58 | .671 134 | 3.97 | .946 069 | 1.12 | .725 065 | 5.08 | .274 935 | 2 |
| 59 | .671 372 | 3.97 | .946 002 | 1.12 | .725 370 | 5.08 | .274 630 | 1 |
| 60 | 9.671 609 | | 9.945 935 | 1.12 | 9.725 674 | 5.07 | 0.274 326 | 0 |
| | Cos. | D. 1". | Sin. | D. 1". | Cot. | D. 1". | Tan. | M. |

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.671 609 | | 9.945 935 | | 9.725 674 | | 0.274 326 | 60 |
| 1 | .671 847 | 3.97 | .945 868 | 1.12 | .725 979 | 5.08 | .274 021 | 59 |
| 2 | .672 084 | 3.95 | .945 800 | 1.12 | .726 284 | 5.08 | .273 716 | 58 |
| 3 | .672 321 | 3.95 | .945 733 | 1.12 | .726 588 | 5.07 | .273 412 | 57 |
| 4 | .672 558 | 3.95 | .945 666 | 1.13 | .726 892 | 5.07 | .273 108 | 56 |
| 5 | 9.672 795 | | 9.945 598 | | 9.727 197 | | 0.272 803 | 55 |
| 6 | .673 032 | 3.95 | .945 531 | 1.12 | .727 501 | 5.07 | .272 499 | 54 |
| 7 | .673 268 | 3.93 | .945 464 | 1.12 | .727 805 | 5.07 | .272 195 | 53 |
| 8 | .673 505 | 3.95 | .945 396 | 1.13 | .728 109 | 5.07 | .271 891 | 52 |
| 9 | .673 741 | 3.93 | .945 328 | 1.12 | .728 412 | 5.05 | .271 588 | 51 |
| 10 | 9.673 977 | | 9.945 261 | | 9.728 716 | | 0.271 284 | 50 |
| 11 | .674 213 | 3.93 | .945 193 | 1.13 | .729 020 | 5.07 | .270 980 | 49 |
| 12 | .674 448 | 3.92 | .945 125 | 1.13 | .729 323 | 5.05 | .270 677 | 48 |
| 13 | .674 684 | 3.93 | .945 058 | 1.12 | .729 626 | 5.05 | .270 374 | 47 |
| 14 | .674 919 | 3.92 | .944 990 | 1.13 | .729 929 | 5.05 | .270 071 | 46 |
| 15 | 9.675 155 | | 9.944 922 | | 9.730 233 | | 0.269 767 | 45 |
| 16 | .675 390 | 3.92 | .944 854 | 1.13 | .730 535 | 5.03 | .269 465 | 44 |
| 17 | .675 624 | 3.90 | .944 786 | 1.13 | .730 838 | 5.05 | .269 162 | 43 |
| 18 | .675 859 | 3.92 | .944 718 | 1.13 | .731 141 | 5.05 | .268 859 | 42 |
| 19 | .676 094 | 3.92 | .944 650 | 1.13 | .731 444 | 5.05 | .268 556 | 41 |
| 20 | 9.676 328 | | 9.944 582 | | 9.731 746 | | 0.268 254 | 40 |
| 21 | .676 562 | 3.90 | .944 514 | 1.13 | .732 048 | 5.03 | .267 952 | 39 |
| 22 | .676 796 | 3.90 | .944 446 | 1.13 | .732 351 | 5.05 | .267 649 | 38 |
| 23 | .677 030 | 3.90 | .944 377 | 1.15 | .732 653 | 5.03 | .267 347 | 37 |
| 24 | .677 264 | 3.90 | .944 309 | 1.13 | .732 955 | 5.03 | .267 045 | 36 |
| 25 | 9.677 498 | | 9.944 241 | | 9.733 257 | | 0.266 743 | 35 |
| 26 | .677 731 | 3.88 | .944 172 | 1.15 | .733 558 | 5.02 | .266 442 | 34 |
| 27 | .677 964 | 3.88 | .944 104 | 1.13 | .733 860 | 5.03 | .266 140 | 33 |
| 28 | .678 197 | 3.88 | .944 036 | 1.13 | .734 162 | 5.03 | .265 838 | 32 |
| 29 | .678 430 | 3.88 | .943 967 | 1.15 | .734 463 | 5.02 | .265 537 | 31 |
| 30 | 9.678 663 | | 9.943 899 | | 9.734 764 | | 0.265 236 | 30 |
| 31 | .678 895 | 3.87 | .943 830 | 1.15 | .735 066 | 5.03 | .264 934 | 29 |
| 32 | .679 128 | 3.88 | .943 761 | 1.15 | .735 367 | 5.02 | .264 633 | 28 |
| 33 | .679 360 | 3.87 | .943 693 | 1.13 | .735 668 | 5.02 | .264 332 | 27 |
| 34 | .679 592 | 3.87 | .943 624 | 1.15 | .735 969 | 5.02 | .264 031 | 26 |
| 35 | 9.679 824 | | 9.943 555 | | 9.736 269 | | 0.263 731 | 25 |
| 36 | .680 056 | 3.87 | .943 486 | 1.15 | .736 570 | 5.02 | .263 430 | 24 |
| 37 | .680 288 | 3.87 | .943 417 | 1.15 | .736 870 | 5.00 | .263 130 | 23 |
| 38 | .680 519 | 3.85 | .943 348 | 1.15 | .737 171 | 5.02 | .262 829 | 22 |
| 39 | .680 750 | 3.85 | .943 279 | 1.15 | .737 471 | 5.00 | .262 529 | 21 |
| 40 | 9.680 982 | | 9.943 210 | | 9.737 771 | | 0.262 229 | 20 |
| 41 | .681 213 | 3.85 | .943 141 | 1.15 | .738 071 | 5.00 | .261 929 | 19 |
| 42 | .681 443 | 3.83 | .943 072 | 1.15 | .738 371 | 5.00 | .261 629 | 18 |
| 43 | .681 674 | 3.85 | .943 003 | 1.15 | .738 671 | 5.00 | .261 329 | 17 |
| 44 | .681 905 | 3.85 | .942 934 | 1.17 | .738 971 | 5.00 | .261 029 | 16 |
| 45 | 9.682 135 | | 9.942 864 | | 9.739 271 | | 0.260 729 | 15 |
| 46 | .682 365 | 3.83 | .942 795 | 1.15 | .739 570 | 4.98 | .260 430 | 14 |
| 47 | .682 595 | 3.83 | .942 726 | 1.15 | .739 870 | 5.00 | .260 130 | 13 |
| 48 | .682 825 | 3.83 | .942 656 | 1.17 | .740 169 | 4.98 | .259 831 | 12 |
| 49 | .683 055 | 3.83 | .942 587 | 1.15 | .740 468 | 4.98 | .259 532 | 11 |
| 50 | 9.683 284 | | 9.942 517 | | 9.740 767 | | 0.259 233 | 10 |
| 51 | .683 514 | 3.82 | .942 448 | 1.17 | .741 066 | 4.98 | .258 934 | 9 |
| 52 | .683 743 | 3.82 | .942 378 | 1.17 | .741 365 | 4.98 | .258 635 | 8 |
| 53 | .683 972 | 3.82 | .942 308 | 1.17 | .741 664 | 4.98 | .258 336 | 7 |
| 54 | .684 201 | 3.82 | .942 239 | 1.15 | .741 962 | 4.97 | .258 038 | 6 |
| 55 | 9.684 430 | | 9.942 169 | | 9.742 261 | | 0.257 739 | 5 |
| 56 | .684 658 | 3.80 | .942 099 | 1.17 | .742 559 | 4.97 | .257 441 | 4 |
| 57 | .684 887 | 3.82 | .942 029 | 1.17 | .742 858 | 4.98 | .257 142 | 3 |
| 58 | .685 115 | 3.80 | .941 959 | 1.17 | .743 156 | 4.97 | .256 844 | 2 |
| 59 | .685 343 | 3.80 | .941 889 | 1.17 | .743 454 | 4.97 | .256 546 | 1 |
| 60 | 9.685 571 | | 9.941 819 | | 9.743 752 | | 0.256 248 | 0 |

| M. | Sin. | D. 1'' | Cos. | D. 1'' | Tan. | D. 1'' | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.685 571 | 3.80 | 9.941 819 | 1.17 | 9.743 752 | 4.97 | 0.256 248 | 60 |
| 1 | .685 799 | 3.80 | .941 749 | 1.17 | .744 050 | 4.97 | .255 950 | 59 |
| 2 | .686 027 | 3.78 | .941 679 | 1.17 | .744 348 | 4.95 | .255 652 | 58 |
| 3 | .686 254 | 3.78 | .941 609 | 1.17 | .744 645 | 4.97 | .255 355 | 57 |
| 4 | .686 482 | 3.78 | .941 539 | 1.17 | .744 943 | 4.95 | .255 057 | 56 |
| 5 | 9.686 709 | 3.78 | 9.941 469 | 1.18 | 9.745 240 | 4.97 | 0.254 760 | 55 |
| 6 | .686 936 | 3.78 | .941 398 | 1.17 | .745 538 | 4.95 | .254 462 | 54 |
| 7 | .687 163 | 3.77 | .941 328 | 1.17 | .745 835 | 4.95 | .254 165 | 53 |
| 8 | .687 389 | 3.77 | .941 258 | 1.18 | .746 132 | 4.95 | .253 868 | 52 |
| 9 | .687 616 | 3.78 | .941 187 | 1.17 | .746 429 | 4.95 | .253 571 | 51 |
| 10 | 9.687 843 | 3.77 | 9.941 117 | 1.18 | 9.746 726 | 4.95 | 0.253 274 | 50 |
| 11 | .688 069 | 3.77 | .941 046 | 1.18 | .747 023 | 4.93 | .252 977 | 49 |
| 12 | .688 295 | 3.77 | .940 975 | 1.17 | .747 319 | 4.95 | .252 681 | 48 |
| 13 | .688 521 | 3.77 | .940 905 | 1.18 | .747 616 | 4.95 | .252 384 | 47 |
| 14 | .688 747 | 3.75 | .940 834 | 1.18 | .747 913 | 4.93 | .252 087 | 46 |
| 15 | 9.688 972 | 3.77 | 9.940 763 | 1.17 | 9.748 209 | 4.93 | 0.251 791 | 45 |
| 16 | .689 198 | 3.75 | .940 693 | 1.18 | .748 505 | 4.93 | .251 495 | 44 |
| 17 | .689 423 | 3.75 | .940 622 | 1.18 | .748 801 | 4.93 | .251 199 | 43 |
| 18 | .689 648 | 3.75 | .940 551 | 1.18 | .749 097 | 4.93 | .250 903 | 42 |
| 19 | .689 873 | 3.75 | .940 480 | 1.18 | .749 393 | 4.93 | .250 607 | 41 |
| 20 | 9.690 098 | 3.75 | 9.940 409 | 1.18 | 9.749 689 | 4.93 | 0.250 311 | 40 |
| 21 | .690 323 | 3.75 | .940 338 | 1.18 | .749 985 | 4.93 | .250 015 | 39 |
| 22 | .690 548 | 3.73 | .940 267 | 1.18 | .750 281 | 4.92 | .249 719 | 38 |
| 23 | .690 772 | 3.73 | .940 196 | 1.18 | .750 576 | 4.93 | .249 424 | 37 |
| 24 | .690 996 | 3.73 | .940 125 | 1.18 | .750 872 | 4.92 | .249 128 | 36 |
| 25 | 9.691 220 | 3.73 | 9.940 054 | 1.20 | 9.751 167 | 4.92 | 0.248 833 | 35 |
| 26 | .691 444 | 3.73 | .939 982 | 1.18 | .751 461 | 4.92 | .248 538 | 34 |
| 27 | .691 668 | 3.73 | .939 911 | 1.18 | .751 757 | 4.92 | .248 243 | 33 |
| 28 | .691 892 | 3.72 | .939 840 | 1.20 | .752 052 | 4.92 | .247 948 | 32 |
| 29 | .692 115 | 3.73 | .939 768 | 1.18 | .752 347 | 4.92 | .247 653 | 31 |
| 30 | 9.692 339 | 3.72 | 9.939 697 | 1.20 | 9.752 642 | 4.92 | 0.247 358 | 30 |
| 31 | .692 562 | 3.72 | .939 625 | 1.18 | .752 937 | 4.90 | .247 063 | 29 |
| 32 | .692 785 | 3.72 | .939 554 | 1.20 | .753 231 | 4.92 | .246 769 | 28 |
| 33 | .693 008 | 3.72 | .939 482 | 1.20 | .753 526 | 4.90 | .246 474 | 27 |
| 34 | .693 231 | 3.70 | .939 410 | 1.18 | .753 820 | 4.92 | .246 180 | 26 |
| 35 | 9.693 453 | 3.72 | 9.939 339 | 1.20 | 9.754 115 | 4.90 | 0.245 885 | 25 |
| 36 | .693 676 | 3.70 | .939 267 | 1.20 | .754 409 | 4.90 | .245 591 | 24 |
| 37 | .693 898 | 3.70 | .939 195 | 1.20 | .754 703 | 4.90 | .245 297 | 23 |
| 38 | .694 120 | 3.70 | .939 123 | 1.18 | .754 997 | 4.90 | .245 003 | 22 |
| 39 | .694 342 | 3.70 | .939 052 | 1.20 | .755 291 | 4.90 | .244 709 | 21 |
| 40 | 9.694 564 | 3.70 | 9.938 980 | 1.20 | 9.755 585 | 4.88 | 0.244 415 | 20 |
| 41 | .694 786 | 3.68 | .938 908 | 1.20 | .755 878 | 4.90 | .244 122 | 19 |
| 42 | .695 007 | 3.70 | .938 836 | 1.22 | .756 172 | 4.88 | .243 828 | 18 |
| 43 | .695 229 | 3.68 | .938 763 | 1.20 | .756 465 | 4.90 | .243 535 | 17 |
| 44 | .695 450 | 3.68 | .938 691 | 1.20 | .756 759 | 4.88 | .243 241 | 16 |
| 45 | 9.695 671 | 3.68 | 9.938 619 | 1.20 | 9.757 052 | 4.88 | 0.242 948 | 15 |
| 46 | .695 892 | 3.68 | .938 547 | 1.20 | .757 345 | 4.88 | .242 655 | 14 |
| 47 | .696 113 | 3.68 | .938 475 | 1.22 | .757 638 | 4.88 | .242 362 | 13 |
| 48 | .696 334 | 3.67 | .938 402 | 1.20 | .757 931 | 4.88 | .242 069 | 12 |
| 49 | .696 554 | 3.68 | .938 330 | 1.20 | .758 224 | 4.88 | .241 776 | 11 |
| 50 | 9.696 775 | 3.67 | 9.938 258 | 1.22 | 9.758 517 | 4.88 | 0.241 483 | 10 |
| 51 | .696 995 | 3.67 | .938 185 | 1.20 | .758 810 | 4.87 | .241 190 | 9 |
| 52 | .697 215 | 3.67 | .938 113 | 1.22 | .759 102 | 4.88 | .240 898 | 8 |
| 53 | .697 435 | 3.65 | .938 040 | 1.22 | .759 395 | 4.87 | .240 605 | 7 |
| 54 | .697 654 | 3.67 | .937 967 | 1.20 | .759 687 | 4.87 | .240 313 | 6 |
| 55 | 9.697 874 | 3.67 | 9.937 895 | 1.22 | 9.759 979 | 4.88 | 0.240 021 | 5 |
| 56 | .698 094 | 3.65 | .937 822 | 1.22 | .760 272 | 4.87 | .239 728 | 4 |
| 57 | .698 313 | 3.65 | .937 749 | 1.22 | .760 564 | 4.87 | .239 436 | 3 |
| 58 | .698 532 | 3.65 | .937 676 | 1.20 | .760 856 | 4.87 | .239 144 | 2 |
| 59 | .698 751 | 3.65 | .937 604 | 1.22 | .761 148 | 4.85 | .238 852 | 1 |
| 60 | 9.698 970 | 3.65 | 9.937 531 | 1.22 | 9.761 439 | 4.85 | 0.238 561 | 0 |

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.698 970 | 3.65 | 9.937 531 | 1.22 | 9.761 439 | 4.87 | 0.238 561 | 60 |
| 1 | .699 189 | 3.63 | .937 458 | 1.22 | .761 731 | 4.87 | .238 269 | 59 |
| 2 | .699 407 | 3.65 | .937 385 | 1.22 | .762 023 | 4.85 | .237 977 | 58 |
| 3 | .699 626 | 3.63 | .937 312 | 1.23 | .762 314 | 4.87 | .237 686 | 57 |
| 4 | .699 844 | 3.63 | .937 238 | 1.22 | .762 606 | 4.85 | .237 394 | 56 |
| 5 | 9.700 062 | 3.63 | 9.937 165 | 1.22 | 9.762 897 | 4.85 | 0.237 103 | 55 |
| 6 | .700 280 | 3.63 | .937 092 | 1.22 | .763 188 | 4.85 | .236 812 | 54 |
| 7 | .700 498 | 3.63 | .937 019 | 1.22 | .763 479 | 4.85 | .236 521 | 53 |
| 8 | .700 716 | 3.62 | .936 946 | 1.23 | .763 770 | 4.85 | .236 230 | 52 |
| 9 | .700 933 | 3.63 | .936 872 | 1.22 | .764 061 | 4.85 | .235 939 | 51 |
| 10 | 9.701 151 | 3.62 | 9.936 799 | 1.23 | 9.764 352 | 4.85 | 0.235 648 | 50 |
| 11 | .701 368 | 3.62 | .936 725 | 1.22 | .764 643 | 4.83 | .235 357 | 49 |
| 12 | .701 585 | 3.62 | .936 652 | 1.23 | .764 933 | 4.85 | .235 067 | 48 |
| 13 | .701 802 | 3.62 | .936 578 | 1.22 | .765 224 | 4.83 | .234 776 | 47 |
| 14 | .702 019 | 3.62 | .936 505 | 1.23 | .765 514 | 4.85 | .234 486 | 46 |
| 15 | 9.702 236 | 3.60 | 9.936 431 | 1.23 | 9.765 805 | 4.83 | 0.234 195 | 45 |
| 16 | .702 452 | 3.62 | .936 357 | 1.22 | .766 095 | 4.83 | .233 905 | 44 |
| 17 | .702 669 | 3.60 | .936 284 | 1.23 | .766 385 | 4.83 | .233 615 | 43 |
| 18 | .702 885 | 3.60 | .936 210 | 1.23 | .766 675 | 4.83 | .233 325 | 42 |
| 19 | .703 101 | 3.60 | .936 136 | 1.23 | .766 965 | 4.83 | .233 035 | 41 |
| 20 | 9.703 317 | 3.60 | 9.936 062 | 1.23 | 9.767 255 | 4.83 | 0.232 745 | 40 |
| 21 | .703 533 | 3.60 | .935 988 | 1.23 | .767 545 | 4.82 | .232 455 | 39 |
| 22 | .703 749 | 3.58 | .935 914 | 1.23 | .767 834 | 4.83 | .232 166 | 38 |
| 23 | .703 964 | 3.58 | .935 840 | 1.23 | .768 124 | 4.83 | .231 876 | 37 |
| 24 | .704 179 | 3.60 | .935 766 | 1.23 | .768 414 | 4.82 | .231 586 | 36 |
| 25 | 9.704 395 | 3.58 | 9.935 692 | 1.23 | 9.768 703 | 4.82 | 0.231 297 | 35 |
| 26 | .704 610 | 3.58 | .935 618 | 1.25 | .768 992 | 4.82 | .231 008 | 34 |
| 27 | .704 825 | 3.58 | .935 543 | 1.23 | .769 281 | 4.83 | .230 719 | 33 |
| 28 | .705 040 | 3.57 | .935 469 | 1.23 | .769 571 | 4.82 | .230 429 | 32 |
| 29 | .705 254 | 3.58 | .935 395 | 1.25 | .769 860 | 4.80 | .230 140 | 31 |
| 30 | 9.705 469 | 3.57 | 9.935 320 | 1.23 | 9.770 148 | 4.82 | 0.229 852 | 30 |
| 31 | .705 683 | 3.58 | .935 246 | 1.25 | .770 437 | 4.82 | .229 563 | 29 |
| 32 | .705 898 | 3.57 | .935 171 | 1.23 | .770 726 | 4.82 | .229 274 | 28 |
| 33 | .706 112 | 3.57 | .935 097 | 1.25 | .771 015 | 4.80 | .228 985 | 27 |
| 34 | .706 326 | 3.55 | .935 022 | 1.23 | .771 303 | 4.82 | .228 697 | 26 |
| 35 | 9.706 539 | 3.57 | 9.934 948 | 1.25 | 9.771 592 | 4.80 | 0.228 408 | 25 |
| 36 | .706 753 | 3.57 | .934 873 | 1.25 | .771 880 | 4.80 | .228 120 | 24 |
| 37 | .706 967 | 3.55 | .934 798 | 1.25 | .772 168 | 4.82 | .227 832 | 23 |
| 38 | .707 180 | 3.55 | .934 723 | 1.23 | .772 457 | 4.80 | .227 543 | 22 |
| 39 | .707 393 | 3.55 | .934 649 | 1.25 | .772 745 | 4.80 | .227 255 | 21 |
| 40 | 9.707 606 | 3.55 | 9.934 574 | 1.25 | 9.773 033 | 4.80 | 0.226 967 | 20 |
| 41 | .707 819 | 3.55 | .934 499 | 1.25 | .773 321 | 4.78 | .226 679 | 19 |
| 42 | .708 032 | 3.55 | .934 424 | 1.25 | .773 608 | 4.80 | .226 392 | 18 |
| 43 | .708 245 | 3.55 | .934 349 | 1.25 | .773 896 | 4.80 | .226 104 | 17 |
| 44 | .708 458 | 3.53 | .934 274 | 1.25 | .774 184 | 4.78 | .225 816 | 16 |
| 45 | 9.708 670 | 3.53 | 9.934 199 | 1.27 | 9.774 471 | 4.80 | 0.225 529 | 15 |
| 46 | .708 882 | 3.53 | .934 123 | 1.25 | .774 759 | 4.78 | .225 241 | 14 |
| 47 | .709 094 | 3.53 | .934 048 | 1.25 | .775 046 | 4.78 | .224 954 | 13 |
| 48 | .709 306 | 3.53 | .933 973 | 1.25 | .775 333 | 4.80 | .224 667 | 12 |
| 49 | .709 518 | 3.53 | .933 898 | 1.27 | .775 621 | 4.78 | .224 379 | 11 |
| 50 | 9.709 730 | 3.52 | 9.933 822 | 1.25 | 9.775 908 | 4.78 | 0.224 092 | 10 |
| 51 | .709 941 | 3.53 | .933 747 | 1.27 | .776 195 | 4.78 | .223 805 | 9 |
| 52 | .710 153 | 3.52 | .933 671 | 1.25 | .776 482 | 4.77 | .223 518 | 8 |
| 53 | .710 364 | 3.52 | .933 596 | 1.27 | .776 768 | 4.78 | .223 232 | 7 |
| 54 | .710 575 | 3.52 | .933 520 | 1.25 | .777 055 | 4.78 | .222 945 | 6 |
| 55 | 9.710 786 | 3.52 | 9.933 445 | 1.27 | 9.777 342 | 4.77 | 0.222 658 | 5 |
| 56 | .710 997 | 3.52 | .933 369 | 1.27 | .777 628 | 4.78 | .222 372 | 4 |
| 57 | .711 208 | 3.52 | .933 293 | 1.27 | .777 915 | 4.78 | .222 085 | 3 |
| 58 | .711 419 | 3.50 | .933 217 | 1.27 | .778 201 | 4.77 | .221 799 | 2 |
| 59 | .711 629 | 3.50 | .933 141 | 1.25 | .778 488 | 4.78 | .221 512 | 1 |
| 60 | 9.711 839 | | 9.933 066 | | 9.778 774 | 4.77 | 0.221 226 | 0 |

Cos. D. 1". Sin. D. 1". Cot. D. 1". Tan. M.

LOGARITHMIC SINES, COSINES, TANGENTS, AND COTANGENTS. 49

31°

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.711 839 | 3.52 | 9.933 066 | 1.27 | 9.778 774 | 4.77 | 0.221 226 | 60 |
| 1 | .712 050 | 3.50 | .932 990 | 1.27 | .779 060 | 4.77 | .220 940 | 59 |
| 2 | .712 260 | 3.48 | .932 914 | 1.27 | .779 346 | 4.77 | .220 654 | 58 |
| 3 | .712 469 | 3.50 | .932 838 | 1.27 | .779 632 | 4.77 | .220 368 | 57 |
| 4 | .712 679 | 3.50 | .932 762 | 1.28 | .779 918 | 4.75 | .220 082 | 56 |
| 5 | 9.712 889 | 3.48 | 9.932 685 | 1.27 | 9.780 203 | 4.77 | 0.219 797 | 55 |
| 6 | .713 098 | 3.50 | .932 609 | 1.27 | .780 489 | 4.77 | .219 511 | 54 |
| 7 | .713 308 | 3.48 | .932 533 | 1.27 | .780 775 | 4.75 | .219 225 | 53 |
| 8 | .713 517 | 3.48 | .932 457 | 1.28 | .781 060 | 4.77 | .218 940 | 52 |
| 9 | .713 726 | 3.48 | .932 380 | 1.27 | .781 346 | 4.75 | .218 654 | 51 |
| 10 | 9.713 935 | 3.48 | 9.932 304 | 1.27 | 9.781 631 | 4.75 | 0.218 369 | 50 |
| 11 | .714 144 | 3.47 | .932 228 | 1.28 | .781 916 | 4.75 | .218 084 | 49 |
| 12 | .714 352 | 3.48 | .932 151 | 1.27 | .782 201 | 4.75 | .217 799 | 48 |
| 13 | .714 561 | 3.47 | .932 075 | 1.28 | .782 486 | 4.75 | .217 514 | 47 |
| 14 | .714 769 | 3.48 | .931 998 | 1.28 | .782 771 | 4.75 | .217 229 | 46 |
| 15 | 9.714 978 | 3.47 | 9.931 921 | 1.27 | 9.783 056 | 4.75 | 0.216 944 | 45 |
| 16 | .715 186 | 3.47 | .931 845 | 1.28 | .783 341 | 4.75 | .216 659 | 44 |
| 17 | .715 394 | 3.47 | .931 768 | 1.28 | .783 626 | 4.73 | .216 374 | 43 |
| 18 | .715 602 | 3.45 | .931 691 | 1.28 | .783 910 | 4.75 | .216 090 | 42 |
| 19 | .715 809 | 3.47 | .931 614 | 1.28 | .784 195 | 4.73 | .215 805 | 41 |
| 20 | 9.716 017 | 3.45 | 9.931 537 | 1.28 | 9.784 479 | 4.75 | 0.215 521 | 40 |
| 21 | .716 224 | 3.47 | .931 460 | 1.28 | .784 764 | 4.73 | .215 236 | 39 |
| 22 | .716 432 | 3.45 | .931 383 | 1.28 | .785 048 | 4.73 | .214 952 | 38 |
| 23 | .716 639 | 3.45 | .931 306 | 1.28 | .785 332 | 4.73 | .214 668 | 37 |
| 24 | .716 846 | 3.45 | .931 229 | 1.28 | .785 616 | 4.73 | .214 384 | 36 |
| 25 | 9.717 053 | 3.43 | 9.931 152 | 1.28 | 9.785 900 | 4.73 | 0.214 100 | 35 |
| 26 | .717 259 | 3.45 | .931 075 | 1.28 | .786 184 | 4.73 | .213 816 | 34 |
| 27 | .717 466 | 3.45 | .930 998 | 1.28 | .786 468 | 4.73 | .213 532 | 33 |
| 28 | .717 673 | 3.45 | .930 921 | 1.30 | .786 752 | 4.73 | .213 248 | 32 |
| 29 | .717 879 | 3.43 | .930 843 | 1.28 | .787 036 | 4.72 | .212 964 | 31 |
| 30 | 9.718 085 | 3.43 | 9.930 766 | 1.30 | 9.787 319 | 4.73 | 0.212 681 | 30 |
| 31 | .718 291 | 3.43 | .930 688 | 1.28 | .787 603 | 4.72 | .212 397 | 29 |
| 32 | .718 497 | 3.43 | .930 611 | 1.30 | .787 886 | 4.73 | .212 114 | 28 |
| 33 | .718 703 | 3.43 | .930 533 | 1.28 | .788 170 | 4.72 | .211 830 | 27 |
| 34 | .718 909 | 3.42 | .930 456 | 1.30 | .788 453 | 4.72 | .211 547 | 26 |
| 35 | 9.719 114 | 3.43 | 9.930 378 | 1.30 | 9.788 736 | 4.72 | 0.211 264 | 25 |
| 36 | .719 320 | 3.42 | .930 300 | 1.28 | .789 019 | 4.72 | .210 981 | 24 |
| 37 | .719 525 | 3.42 | .930 223 | 1.30 | .789 302 | 4.72 | .210 698 | 23 |
| 38 | .719 730 | 3.42 | .930 145 | 1.30 | .789 585 | 4.72 | .210 415 | 22 |
| 39 | .719 935 | 3.42 | .930 067 | 1.30 | .789 868 | 4.72 | .210 132 | 21 |
| 40 | 9.720 140 | 3.42 | 9.929 989 | 1.30 | 9.790 151 | 4.72 | 0.209 849 | 20 |
| 41 | .720 345 | 3.40 | .929 911 | 1.30 | .790 434 | 4.70 | .209 566 | 19 |
| 42 | .720 549 | 3.42 | .929 833 | 1.30 | .790 716 | 4.72 | .209 284 | 18 |
| 43 | .720 754 | 3.40 | .929 755 | 1.30 | .790 999 | 4.70 | .209 001 | 17 |
| 44 | .720 958 | 3.40 | .929 677 | 1.30 | .791 281 | 4.70 | .208 719 | 16 |
| 45 | 9.721 162 | 3.40 | 9.929 599 | 1.30 | 9.791 563 | 4.72 | 0.208 437 | 15 |
| 46 | .721 366 | 3.40 | .929 521 | 1.32 | .791 846 | 4.70 | .208 154 | 14 |
| 47 | .721 570 | 3.40 | .929 442 | 1.30 | .792 128 | 4.70 | .207 872 | 13 |
| 48 | .721 774 | 3.40 | .929 364 | 1.30 | .792 410 | 4.70 | .207 590 | 12 |
| 49 | .721 978 | 3.38 | .929 286 | 1.32 | .792 692 | 4.70 | .207 308 | 11 |
| 50 | 9.722 181 | 3.40 | 9.929 207 | 1.30 | 9.792 974 | 4.70 | 0.207 026 | 10 |
| 51 | .722 385 | 3.38 | .929 129 | 1.32 | .793 256 | 4.70 | .206 744 | 9 |
| 52 | .722 588 | 3.38 | .929 050 | 1.30 | .793 538 | 4.68 | .206 462 | 8 |
| 53 | .722 791 | 3.38 | .928 972 | 1.32 | .793 819 | 4.70 | .206 181 | 7 |
| 54 | .722 994 | 3.38 | .928 893 | 1.30 | .794 101 | 4.70 | .205 899 | 6 |
| 55 | 9.723 197 | 3.38 | 9.928 815 | 1.32 | 9.794 383 | 4.68 | 0.205 617 | 5 |
| 56 | .723 400 | 3.38 | .928 736 | 1.32 | .794 664 | 4.70 | .205 336 | 4 |
| 57 | .723 603 | 3.37 | .928 657 | 1.32 | .794 946 | 4.68 | .205 054 | 3 |
| 58 | .723 805 | 3.37 | .928 578 | 1.32 | .795 227 | 4.68 | .204 773 | 2 |
| 59 | .724 007 | 3.38 | .928 499 | 1.32 | .795 508 | 4.68 | .204 492 | 1 |
| 60 | 9.724 210 | | 9.928 420 | | 9.795 789 | | 0.204 211 | 0 |

Cos. D. 1". Sin. D. 1". Cot. D. 1". Tan. M.

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.724 210 | | 9.928 420 | 1.30 | 9.795 789 | 4.68 | 0.204 211 | 60 |
| 1 | .724 412 | 3.37 | .928 342 | 1.32 | .796 070 | 4.68 | .203 930 | 59 |
| 2 | .724 614 | 3.37 | .928 263 | 1.33 | .796 351 | 4.68 | .203 649 | 58 |
| 3 | .724 816 | 3.37 | .928 183 | 1.32 | .796 632 | 4.68 | .203 368 | 57 |
| 4 | .725 017 | 3.35 | .928 104 | 1.32 | .796 913 | 4.68 | .203 087 | 56 |
| 5 | 9.725 219 | 3.35 | 9.928 025 | 1.32 | 9.797 194 | 4.67 | 0.202 806 | 55 |
| 6 | .725 420 | 3.37 | .927 946 | 1.32 | .797 474 | 4.68 | .202 526 | 54 |
| 7 | .725 622 | 3.35 | .927 867 | 1.33 | .797 755 | 4.68 | .202 245 | 53 |
| 8 | .725 823 | 3.35 | .927 787 | 1.32 | .798 036 | 4.67 | .201 964 | 52 |
| 9 | .726 024 | 3.35 | .927 708 | 1.32 | .798 316 | 4.67 | .201 684 | 51 |
| 10 | 9.726 225 | 3.35 | 9.927 629 | 1.33 | 9.798 596 | 4.68 | 0.201 404 | 50 |
| 11 | .726 426 | 3.33 | .927 549 | 1.32 | .798 877 | 4.67 | .201 123 | 49 |
| 12 | .726 626 | 3.33 | .927 470 | 1.33 | .799 157 | 4.67 | .200 843 | 48 |
| 13 | .726 827 | 3.35 | .927 390 | 1.33 | .799 437 | 4.67 | .200 563 | 47 |
| 14 | .727 027 | 3.33 | .927 310 | 1.32 | .799 717 | 4.67 | .200 283 | 46 |
| 15 | 9.727 228 | 3.33 | 9.927 231 | 1.33 | 9.799 997 | 4.67 | 0.200 003 | 45 |
| 16 | .727 428 | 3.33 | .927 151 | 1.33 | .800 277 | 4.67 | .199 723 | 44 |
| 17 | .727 628 | 3.33 | .927 071 | 1.33 | .800 557 | 4.65 | .199 443 | 43 |
| 18 | .727 828 | 3.32 | .926 991 | 1.33 | .800 836 | 4.67 | .199 164 | 42 |
| 19 | .728 027 | 3.33 | .926 911 | 1.33 | .801 116 | 4.67 | .198 884 | 41 |
| 20 | 9.728 227 | 3.33 | 9.926 831 | 1.33 | 9.801 396 | 4.65 | 0.198 604 | 40 |
| 21 | .728 427 | 3.32 | .926 751 | 1.33 | .801 675 | 4.67 | .198 325 | 39 |
| 22 | .728 626 | 3.32 | .926 671 | 1.33 | .801 955 | 4.65 | .198 045 | 38 |
| 23 | .728 825 | 3.32 | .926 591 | 1.33 | .802 234 | 4.65 | .197 766 | 37 |
| 24 | .729 024 | 3.32 | .926 511 | 1.33 | .802 513 | 4.65 | .197 487 | 36 |
| 25 | 9.729 223 | 3.32 | 9.926 431 | 1.33 | 9.802 792 | 4.67 | 0.197 208 | 35 |
| 26 | .729 422 | 3.32 | .926 351 | 1.35 | .803 072 | 4.65 | .196 928 | 34 |
| 27 | .729 621 | 3.32 | .926 270 | 1.33 | .803 351 | 4.65 | .196 649 | 33 |
| 28 | .729 820 | 3.32 | .926 190 | 1.33 | .803 630 | 4.65 | .196 370 | 32 |
| 29 | .730 018 | 3.32 | .926 110 | 1.35 | .803 909 | 4.63 | .196 091 | 31 |
| 30 | 9.730 217 | 3.30 | 9.926 029 | 1.33 | 9.804 187 | 4.65 | 0.195 813 | 30 |
| 31 | .730 415 | 3.30 | .925 949 | 1.35 | .804 466 | 4.65 | .195 534 | 29 |
| 32 | .730 613 | 3.30 | .925 868 | 1.33 | .804 745 | 4.63 | .195 255 | 28 |
| 33 | .730 811 | 3.30 | .925 788 | 1.35 | .805 023 | 4.65 | .194 977 | 27 |
| 34 | .731 009 | 3.28 | .925 707 | 1.35 | .805 302 | 4.63 | .194 698 | 26 |
| 35 | 9.731 206 | 3.30 | 9.925 626 | 1.35 | 9.805 580 | 4.65 | 0.194 420 | 25 |
| 36 | .731 404 | 3.30 | .925 545 | 1.33 | .805 859 | 4.63 | .194 141 | 24 |
| 37 | .731 602 | 3.28 | .925 465 | 1.35 | .806 137 | 4.63 | .193 863 | 23 |
| 38 | .731 799 | 3.28 | .925 384 | 1.35 | .806 415 | 4.63 | .193 585 | 22 |
| 39 | .731 996 | 3.28 | .925 303 | 1.35 | .806 693 | 4.63 | .193 307 | 21 |
| 40 | 9.732 193 | 3.28 | 9.925 222 | 1.35 | 9.806 971 | 4.63 | 0.193 029 | 20 |
| 41 | .732 390 | 3.28 | .925 141 | 1.35 | .807 249 | 4.63 | .192 751 | 19 |
| 42 | .732 587 | 3.28 | .925 060 | 1.35 | .807 527 | 4.63 | .192 473 | 18 |
| 43 | .732 784 | 3.27 | .924 979 | 1.37 | .807 805 | 4.63 | .192 195 | 17 |
| 44 | .732 980 | 3.28 | .924 897 | 1.35 | .808 083 | 4.63 | .191 917 | 16 |
| 45 | 9.733 177 | 3.27 | 9.924 816 | 1.35 | 9.808 361 | 4.62 | 0.191 639 | 15 |
| 46 | .733 373 | 3.27 | .924 735 | 1.35 | .808 638 | 4.63 | .191 362 | 14 |
| 47 | .733 569 | 3.27 | .924 654 | 1.37 | .808 916 | 4.62 | .191 084 | 13 |
| 48 | .733 765 | 3.27 | .924 572 | 1.35 | .809 193 | 4.63 | .190 807 | 12 |
| 49 | .733 961 | 3.27 | .924 491 | 1.37 | .809 471 | 4.62 | .190 529 | 11 |
| 50 | 9.734 157 | 3.27 | 9.924 409 | 1.35 | 9.809 748 | 4.62 | 0.190 252 | 10 |
| 51 | .734 353 | 3.27 | .924 328 | 1.37 | .810 025 | 4.62 | .189 975 | 9 |
| 52 | .734 549 | 3.25 | .924 246 | 1.37 | .810 302 | 4.63 | .189 698 | 8 |
| 53 | .734 744 | 3.25 | .924 164 | 1.35 | .810 580 | 4.62 | .189 420 | 7 |
| 54 | .734 939 | 3.27 | .924 083 | 1.37 | .810 857 | 4.62 | .189 143 | 6 |
| 55 | 9.735 135 | 3.25 | 9.924 001 | 1.37 | 9.811 134 | 4.60 | 0.188 866 | 5 |
| 56 | .735 330 | 3.25 | .923 919 | 1.37 | .811 410 | 4.62 | .188 590 | 4 |
| 57 | .735 525 | 3.23 | .923 837 | 1.37 | .811 687 | 4.62 | .188 313 | 3 |
| 58 | .735 719 | 3.25 | .923 755 | 1.37 | .811 964 | 4.62 | .188 036 | 2 |
| 59 | .735 914 | 3.25 | .923 673 | 1.37 | .812 241 | 4.60 | .187 759 | 1 |
| 60 | 9.736 109 | | 9.923 591 | | 9.812 517 | | 0.187 483 | 0 |

Cos. D. 1". Sin. D. 1". Cot. D. 1". Tan. M.

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.736 109 | | 9.923 591 | 1.37 | 9.812 517 | 4.62 | 0.187 483 | 60 |
| 1 | .736 303 | 3.23 | .923 599 | 1.37 | .812 794 | 4.60 | .187 206 | 59 |
| 2 | .736 498 | 3.25 | .923 427 | 1.37 | .813 070 | 4.62 | .186 930 | 58 |
| 3 | .736 692 | 3.23 | .923 345 | 1.37 | .813 347 | 4.60 | .186 653 | 57 |
| 4 | .736 886 | 3.23 | .923 263 | 1.37 | .813 623 | 4.60 | .186 377 | 56 |
| 5 | 9.737 080 | | 9.923 181 | 1.38 | 9.813 899 | 4.62 | 0.186 101 | 55 |
| 6 | .737 274 | 3.22 | .923 098 | 1.37 | .814 176 | 4.60 | .185 824 | 54 |
| 7 | .737 467 | 3.22 | .923 016 | 1.37 | .814 452 | 4.60 | .185 548 | 53 |
| 8 | .737 661 | 3.23 | .922 933 | 1.38 | .814 728 | 4.60 | .185 272 | 52 |
| 9 | .737 855 | 3.23 | .922 851 | 1.37 | .815 004 | 4.60 | .184 996 | 51 |
| 10 | 9.738 048 | | 9.922 768 | 1.38 | 9.815 280 | 4.58 | 0.184 720 | 50 |
| 11 | .738 241 | 3.22 | .922 686 | 1.38 | .815 555 | 4.60 | .184 445 | 49 |
| 12 | .738 434 | 3.22 | .922 603 | 1.38 | .815 831 | 4.60 | .184 169 | 48 |
| 13 | .738 627 | 3.22 | .922 520 | 1.38 | .816 107 | 4.60 | .183 893 | 47 |
| 14 | .738 820 | 3.22 | .922 438 | 1.37 | .816 382 | 4.58 | .183 618 | 46 |
| 15 | 9.739 013 | | 9.922 355 | 1.38 | 9.816 658 | 4.58 | 0.183 342 | 45 |
| 16 | .739 206 | 3.20 | .922 272 | 1.38 | .816 933 | 4.60 | .183 067 | 44 |
| 17 | .739 398 | 3.20 | .922 189 | 1.38 | .817 209 | 4.58 | .182 791 | 43 |
| 18 | .739 590 | 3.22 | .922 106 | 1.38 | .817 484 | 4.58 | .182 516 | 42 |
| 19 | .739 783 | 3.20 | .922 023 | 1.38 | .817 759 | 4.60 | .182 241 | 41 |
| 20 | 9.739 975 | | 9.921 940 | 1.38 | 9.818 035 | 4.58 | 0.181 965 | 40 |
| 21 | .740 167 | 3.20 | .921 857 | 1.38 | .818 310 | 4.58 | .181 690 | 39 |
| 22 | .740 359 | 3.18 | .921 774 | 1.38 | .818 585 | 4.58 | .181 415 | 38 |
| 23 | .740 550 | 3.20 | .921 691 | 1.40 | .818 860 | 4.58 | .181 140 | 37 |
| 24 | .740 742 | 3.20 | .921 607 | 1.38 | .819 135 | 4.58 | .180 865 | 36 |
| 25 | 9.740 934 | | 9.921 524 | 1.38 | 9.819 410 | 4.57 | 0.180 590 | 35 |
| 26 | .741 125 | 3.18 | .921 441 | 1.40 | .819 684 | 4.58 | .180 316 | 34 |
| 27 | .741 316 | 3.18 | .921 357 | 1.38 | .819 959 | 4.58 | .180 041 | 33 |
| 28 | .741 508 | 3.18 | .921 274 | 1.40 | .820 234 | 4.57 | .179 766 | 32 |
| 29 | .741 699 | 3.17 | .921 190 | 1.38 | .820 508 | 4.58 | .179 492 | 31 |
| 30 | 9.741 889 | | 9.921 107 | 1.40 | 9.820 783 | 4.57 | 0.179 217 | 30 |
| 31 | .742 080 | 3.18 | .921 023 | 1.40 | .821 057 | 4.58 | .178 943 | 29 |
| 32 | .742 271 | 3.18 | .920 939 | 1.38 | .821 332 | 4.57 | .178 668 | 28 |
| 33 | .742 462 | 3.17 | .920 856 | 1.40 | .821 606 | 4.57 | .178 394 | 27 |
| 34 | .742 652 | 3.17 | .920 772 | 1.40 | .821 880 | 4.57 | .178 120 | 26 |
| 35 | 9.742 842 | | 9.920 688 | 1.40 | 9.822 154 | 4.58 | 0.177 846 | 25 |
| 36 | .743 033 | 3.18 | .920 604 | 1.40 | .822 429 | 4.57 | .177 571 | 24 |
| 37 | .743 223 | 3.17 | .920 520 | 1.40 | .822 703 | 4.57 | .177 297 | 23 |
| 38 | .743 413 | 3.17 | .920 436 | 1.40 | .822 977 | 4.57 | .177 023 | 22 |
| 39 | .743 602 | 3.15 | .920 352 | 1.40 | .823 251 | 4.55 | .176 749 | 21 |
| 40 | 9.743 792 | | 9.920 268 | 1.40 | 9.823 524 | 4.57 | 0.176 476 | 20 |
| 41 | .743 982 | 3.15 | .920 184 | 1.42 | .823 798 | 4.57 | .176 202 | 19 |
| 42 | .744 171 | 3.17 | .920 099 | 1.40 | .824 072 | 4.55 | .175 928 | 18 |
| 43 | .744 361 | 3.15 | .920 015 | 1.40 | .824 345 | 4.57 | .175 655 | 17 |
| 44 | .744 550 | 3.15 | .919 931 | 1.42 | .824 619 | 4.57 | .175 381 | 16 |
| 45 | 9.744 739 | | 9.919 846 | 1.40 | 9.824 893 | 4.55 | 0.175 107 | 15 |
| 46 | .744 928 | 3.15 | .919 762 | 1.42 | .825 166 | 4.55 | .174 834 | 14 |
| 47 | .745 117 | 3.15 | .919 677 | 1.40 | .825 439 | 4.57 | .174 561 | 13 |
| 48 | .745 306 | 3.13 | .919 593 | 1.42 | .825 713 | 4.55 | .174 287 | 12 |
| 49 | .745 494 | 3.15 | .919 508 | 1.40 | .825 986 | 4.55 | .174 014 | 11 |
| 50 | 9.745 683 | | 9.919 424 | 1.42 | 9.826 259 | 4.55 | 0.173 741 | 10 |
| 51 | .745 871 | 3.15 | .919 339 | 1.42 | .826 532 | 4.55 | .173 468 | 9 |
| 52 | .746 060 | 3.13 | .919 254 | 1.42 | .826 805 | 4.55 | .173 195 | 8 |
| 53 | .746 248 | 3.13 | .919 169 | 1.40 | .827 078 | 4.55 | .172 922 | 7 |
| 54 | .746 436 | 3.13 | .919 085 | 1.42 | .827 351 | 4.55 | .172 649 | 6 |
| 55 | 9.746 624 | | 9.919 000 | 1.42 | 9.827 624 | 4.55 | 0.172 376 | 5 |
| 56 | .746 812 | 3.12 | .918 915 | 1.42 | .827 897 | 4.55 | .172 103 | 4 |
| 57 | .746 999 | 3.12 | .918 830 | 1.42 | .828 170 | 4.53 | .171 830 | 3 |
| 58 | .747 187 | 3.13 | .918 745 | 1.42 | .828 442 | 4.55 | .171 558 | 2 |
| 59 | .747 374 | 3.12 | .918 659 | 1.43 | .828 715 | 4.55 | .171 285 | 1 |
| 60 | 9.747 562 | | 9.918 574 | 1.42 | 9.828 987 | 4.53 | 0.171 013 | 0 |
| | Cos. | D. 1". | Sin. | D. 1". | Cot. | D. 1". | Tan. | M. |

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.747 562 | | 9.918 574 | | 9.828 987 | | 0.171 013 | 60 |
| 1 | .747 749 | 3.12 | .918 489 | 1.42 | .829 260 | 4.55 | .170 740 | 59 |
| 2 | .747 936 | 3.12 | .918 404 | 1.42 | .829 532 | 4.53 | .170 468 | 58 |
| 3 | .748 123 | 3.12 | .918 318 | 1.43 | .829 805 | 4.55 | .170 195 | 57 |
| 4 | .748 310 | 3.12 | .918 233 | 1.42 | .830 077 | 4.53 | .169 923 | 56 |
| 5 | 9.748 497 | | 9.918 147 | | 9.830 349 | | 0.169 651 | 55 |
| 6 | .748 683 | 3.10 | .918 062 | 1.42 | .830 621 | 4.53 | .169 379 | 54 |
| 7 | .748 870 | 3.12 | .917 976 | 1.43 | .830 893 | 4.53 | .169 107 | 53 |
| 8 | .749 056 | 3.10 | .917 891 | 1.42 | .831 165 | 4.53 | .168 835 | 52 |
| 9 | .749 243 | 3.10 | .917 805 | 1.43 | .831 437 | 4.53 | .168 563 | 51 |
| 10 | 9.749 429 | | 9.917 719 | | 9.831 709 | | 0.168 291 | 50 |
| 11 | .749 615 | 3.10 | .917 634 | 1.42 | .831 981 | 4.53 | .168 019 | 49 |
| 12 | .749 801 | 3.10 | .917 548 | 1.43 | .832 253 | 4.53 | .167 747 | 48 |
| 13 | .749 987 | 3.10 | .917 462 | 1.43 | .832 525 | 4.53 | .167 475 | 47 |
| 14 | .750 172 | 3.08 | .917 376 | 1.43 | .832 796 | 4.52 | .167 204 | 46 |
| 15 | 9.750 358 | | 9.917 290 | | 9.833 068 | | 0.166 932 | 45 |
| 16 | .750 543 | 3.08 | .917 204 | 1.43 | .833 339 | 4.52 | .166 661 | 44 |
| 17 | .750 729 | 3.10 | .917 118 | 1.43 | .833 611 | 4.53 | .166 389 | 43 |
| 18 | .750 914 | 3.08 | .917 032 | 1.43 | .833 882 | 4.52 | .166 118 | 42 |
| 19 | .751 099 | 3.08 | .916 946 | 1.43 | .834 154 | 4.53 | .165 846 | 41 |
| 20 | 9.751 284 | | 9.916 859 | | 9.834 425 | | 0.165 575 | 40 |
| 21 | .751 469 | 3.08 | .916 773 | 1.43 | .834 696 | 4.52 | .165 304 | 39 |
| 22 | .751 654 | 3.08 | .916 687 | 1.43 | .834 967 | 4.52 | .165 033 | 38 |
| 23 | .751 839 | 3.08 | .916 600 | 1.45 | .835 238 | 4.52 | .164 762 | 37 |
| 24 | .752 023 | 3.07 | .916 514 | 1.43 | .835 509 | 4.52 | .164 491 | 36 |
| 25 | 9.752 208 | | 9.916 427 | | 9.835 780 | | 0.164 220 | 35 |
| 26 | .752 392 | 3.07 | .916 341 | 1.43 | .836 051 | 4.52 | .163 949 | 34 |
| 27 | .752 576 | 3.07 | .916 254 | 1.45 | .836 322 | 4.52 | .163 678 | 33 |
| 28 | .752 760 | 3.07 | .916 167 | 1.45 | .836 593 | 4.52 | .163 407 | 32 |
| 29 | .752 944 | 3.07 | .916 081 | 1.43 | .836 864 | 4.52 | .163 136 | 31 |
| 30 | 9.753 128 | | 9.915 994 | | 9.837 134 | | 0.162 866 | 30 |
| 31 | .753 312 | 3.07 | .915 907 | 1.45 | .837 405 | 4.52 | .162 595 | 29 |
| 32 | .753 495 | 3.05 | .915 820 | 1.45 | .837 675 | 4.50 | .162 325 | 28 |
| 33 | .753 679 | 3.07 | .915 733 | 1.45 | .837 946 | 4.52 | .162 054 | 27 |
| 34 | .753 862 | 3.05 | .915 646 | 1.45 | .838 216 | 4.50 | .161 784 | 26 |
| 35 | 9.754 046 | | 9.915 559 | | 9.838 487 | | 0.161 513 | 25 |
| 36 | .754 229 | 3.05 | .915 472 | 1.45 | .838 757 | 4.50 | .161 243 | 24 |
| 37 | .754 412 | 3.05 | .915 385 | 1.45 | .839 027 | 4.50 | .160 973 | 23 |
| 38 | .754 595 | 3.05 | .915 297 | 1.47 | .839 297 | 4.50 | .160 703 | 22 |
| 39 | .754 778 | 3.05 | .915 210 | 1.45 | .839 568 | 4.52 | .160 432 | 21 |
| 40 | 9.754 960 | | 9.915 123 | | 9.839 838 | | 0.160 162 | 20 |
| 41 | .755 143 | 3.05 | .915 035 | 1.47 | .840 108 | 4.50 | .159 892 | 19 |
| 42 | .755 326 | 3.05 | .914 948 | 1.45 | .840 378 | 4.50 | .159 622 | 18 |
| 43 | .755 508 | 3.03 | .914 860 | 1.47 | .840 648 | 4.50 | .159 352 | 17 |
| 44 | .755 690 | 3.03 | .914 773 | 1.45 | .840 917 | 4.48 | .159 083 | 16 |
| 45 | 9.755 872 | | 9.914 685 | | 9.841 187 | | 0.158 813 | 15 |
| 46 | .756 054 | 3.03 | .914 598 | 1.45 | .841 457 | 4.50 | .158 543 | 14 |
| 47 | .756 236 | 3.03 | .914 510 | 1.47 | .841 727 | 4.50 | .158 273 | 13 |
| 48 | .756 418 | 3.03 | .914 422 | 1.47 | .841 996 | 4.48 | .158 004 | 12 |
| 49 | .756 600 | 3.03 | .914 334 | 1.47 | .842 266 | 4.50 | .157 734 | 11 |
| 50 | 9.756 782 | | 9.914 246 | | 9.842 535 | | 0.157 465 | 10 |
| 51 | .756 963 | 3.02 | .914 158 | 1.47 | .842 805 | 4.50 | .157 195 | 9 |
| 52 | .757 144 | 3.02 | .914 070 | 1.47 | .843 074 | 4.48 | .156 926 | 8 |
| 53 | .757 326 | 3.03 | .913 982 | 1.47 | .843 343 | 4.48 | .156 657 | 7 |
| 54 | .757 507 | 3.02 | .913 894 | 1.47 | .843 612 | 4.48 | .156 388 | 6 |
| 55 | 9.757 688 | | 9.913 806 | | 9.843 882 | | 0.156 118 | 5 |
| 56 | .757 869 | 3.02 | .913 718 | 1.47 | .844 151 | 4.48 | .155 849 | 4 |
| 57 | .758 050 | 3.00 | .913 630 | 1.47 | .844 420 | 4.48 | .155 580 | 3 |
| 58 | .758 230 | 3.00 | .913 541 | 1.48 | .844 689 | 4.48 | .155 311 | 2 |
| 59 | .758 411 | 3.02 | .913 453 | 1.47 | .844 958 | 4.48 | .155 042 | 1 |
| 60 | 9.758 591 | | 9.913 365 | | 9.845 227 | | 0.154 773 | 0 |

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.758 591 | 3.02 | 9.913 365 | 1.48 | 9.845 227 | 4.48 | 0.154 773 | 60 |
| 1 | .758 772 | 3.00 | .913 276 | 1.48 | .845 496 | 4.47 | .154 504 | 59 |
| 2 | .758 952 | 3.00 | .913 187 | 1.47 | .845 764 | 4.48 | .154 236 | 58 |
| 3 | .759 132 | 3.00 | .913 099 | 1.48 | .846 033 | 4.48 | .153 967 | 57 |
| 4 | .759 312 | 3.00 | .913 010 | 1.47 | .846 302 | 4.47 | .153 698 | 56 |
| 5 | 9.759 492 | 3.00 | 9.912 922 | 1.48 | 9.846 570 | 4.48 | 0.153 430 | 55 |
| 6 | .759 672 | 3.00 | .912 833 | 1.48 | .846 839 | 4.48 | .153 161 | 54 |
| 7 | .759 852 | 2.98 | .912 744 | 1.48 | .847 108 | 4.47 | .152 892 | 53 |
| 8 | .760 031 | 3.00 | .912 655 | 1.48 | .847 376 | 4.47 | .152 624 | 52 |
| 9 | .760 211 | 2.98 | .912 566 | 1.48 | .847 644 | 4.48 | .152 356 | 51 |
| 10 | 9.760 390 | 2.98 | 9.912 477 | 1.48 | 9.847 913 | 4.47 | 0.152 087 | 50 |
| 11 | .760 569 | 2.98 | .912 388 | 1.48 | .848 181 | 4.47 | .151 819 | 49 |
| 12 | .760 748 | 2.98 | .912 299 | 1.48 | .848 449 | 4.47 | .151 551 | 48 |
| 13 | .760 927 | 2.98 | .912 210 | 1.48 | .848 717 | 4.48 | .151 283 | 47 |
| 14 | .761 106 | 2.98 | .912 121 | 1.50 | .848 986 | 4.47 | .151 014 | 46 |
| 15 | 9.761 285 | 2.98 | 9.912 031 | 1.48 | 9.849 254 | 4.47 | 0.150 746 | 45 |
| 16 | .761 464 | 2.97 | .911 942 | 1.48 | .849 522 | 4.47 | .150 478 | 44 |
| 17 | .761 642 | 2.98 | .911 853 | 1.50 | .849 790 | 4.47 | .150 210 | 43 |
| 18 | .761 821 | 2.97 | .911 763 | 1.48 | .850 057 | 4.47 | .149 943 | 42 |
| 19 | .761 999 | 2.97 | .911 674 | 1.50 | .850 325 | 4.47 | .149 675 | 41 |
| 20 | 9.762 177 | 2.98 | 9.911 584 | 1.48 | 9.850 593 | 4.47 | 0.149 407 | 40 |
| 21 | .762 356 | 2.97 | .911 495 | 1.50 | .850 861 | 4.47 | .149 139 | 39 |
| 22 | .762 534 | 2.97 | .911 405 | 1.50 | .851 129 | 4.47 | .148 871 | 38 |
| 23 | .762 712 | 2.95 | .911 315 | 1.48 | .851 396 | 4.47 | .148 604 | 37 |
| 24 | .762 889 | 2.97 | .911 226 | 1.50 | .851 664 | 4.47 | .148 336 | 36 |
| 25 | 9.763 067 | 2.97 | 9.911 136 | 1.50 | 9.851 931 | 4.47 | 0.148 069 | 35 |
| 26 | .763 245 | 2.95 | .911 046 | 1.50 | .852 199 | 4.47 | .147 801 | 34 |
| 27 | .763 422 | 2.97 | .910 956 | 1.50 | .852 466 | 4.47 | .147 534 | 33 |
| 28 | .763 600 | 2.95 | .910 866 | 1.50 | .852 733 | 4.47 | .147 267 | 32 |
| 29 | .763 777 | 2.95 | .910 776 | 1.50 | .853 001 | 4.47 | .146 999 | 31 |
| 30 | 9.763 954 | 2.95 | 9.910 686 | 1.50 | 9.853 268 | 4.47 | 0.146 732 | 30 |
| 31 | .764 131 | 2.95 | .910 596 | 1.50 | .853 535 | 4.47 | .146 465 | 29 |
| 32 | .764 308 | 2.95 | .910 506 | 1.52 | .853 802 | 4.47 | .146 198 | 28 |
| 33 | .764 485 | 2.95 | .910 415 | 1.50 | .854 069 | 4.47 | .145 931 | 27 |
| 34 | .764 662 | 2.93 | .910 325 | 1.50 | .854 336 | 4.47 | .145 664 | 26 |
| 35 | 9.764 838 | 2.95 | 9.910 235 | 1.52 | 9.854 603 | 4.47 | 0.145 397 | 25 |
| 36 | .765 015 | 2.93 | .910 144 | 1.50 | .854 870 | 4.47 | .145 130 | 24 |
| 37 | .765 191 | 2.93 | .910 054 | 1.52 | .855 137 | 4.47 | .144 863 | 23 |
| 38 | .765 367 | 2.95 | .909 963 | 1.50 | .855 404 | 4.47 | .144 596 | 22 |
| 39 | .765 544 | 2.93 | .909 873 | 1.52 | .855 671 | 4.47 | .144 329 | 21 |
| 40 | 9.765 720 | 2.93 | 9.909 782 | 1.52 | 9.855 938 | 4.47 | 0.144 062 | 20 |
| 41 | .765 896 | 2.93 | .909 691 | 1.50 | .856 204 | 4.47 | .143 796 | 19 |
| 42 | .766 072 | 2.92 | .909 601 | 1.52 | .856 471 | 4.47 | .143 529 | 18 |
| 43 | .766 247 | 2.93 | .909 510 | 1.52 | .856 737 | 4.47 | .143 263 | 17 |
| 44 | .766 423 | 2.92 | .909 419 | 1.52 | .857 004 | 4.47 | .142 996 | 16 |
| 45 | 9.766 598 | 2.93 | 9.909 328 | 1.52 | 9.857 270 | 4.47 | 0.142 730 | 15 |
| 46 | .766 774 | 2.92 | .909 237 | 1.52 | .857 537 | 4.47 | .142 463 | 14 |
| 47 | .766 949 | 2.92 | .909 146 | 1.52 | .857 803 | 4.47 | .142 197 | 13 |
| 48 | .767 124 | 2.93 | .909 055 | 1.52 | .858 069 | 4.47 | .141 931 | 12 |
| 49 | .767 300 | 2.92 | .908 964 | 1.52 | .858 336 | 4.47 | .141 664 | 11 |
| 50 | 9.767 475 | 2.90 | 9.908 873 | 1.53 | 9.858 602 | 4.47 | 0.141 398 | 10 |
| 51 | .767 649 | 2.92 | .908 781 | 1.52 | .858 868 | 4.47 | .141 132 | 9 |
| 52 | .767 824 | 2.92 | .908 690 | 1.52 | .859 134 | 4.47 | .140 866 | 8 |
| 53 | .767 999 | 2.90 | .908 599 | 1.53 | .859 400 | 4.47 | .140 600 | 7 |
| 54 | .768 173 | 2.92 | .908 507 | 1.52 | .859 666 | 4.47 | .140 334 | 6 |
| 55 | 9.768 348 | 2.90 | 9.908 416 | 1.53 | 9.859 932 | 4.47 | 0.140 068 | 5 |
| 56 | .768 522 | 2.92 | .908 324 | 1.52 | .860 198 | 4.47 | .139 802 | 4 |
| 57 | .768 697 | 2.90 | .908 233 | 1.53 | .860 464 | 4.47 | .139 536 | 3 |
| 58 | .768 871 | 2.90 | .908 141 | 1.53 | .860 730 | 4.47 | .139 270 | 2 |
| 59 | .769 045 | 2.90 | .908 049 | 1.52 | .860 995 | 4.47 | .139 005 | 1 |
| 60 | 9.769 219 | | 9.907 958 | | 9.861 261 | | 0.138 739 | 0 |

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.769 219 | | 9.907 958 | | 9.861 261 | | 0.138 739 | 60 |
| 1 | .769 393 | 2.90 | .907 866 | 1.53 | .861 527 | 4.43 | .138 473 | 59 |
| 2 | .769 566 | 2.88 | .907 774 | 1.53 | .861 792 | 4.42 | .138 208 | 58 |
| 3 | .769 740 | 2.90 | .907 682 | 1.53 | .862 058 | 4.43 | .137 942 | 57 |
| 4 | .769 913 | 2.88 | .907 590 | 1.53 | .862 323 | 4.42 | .137 677 | 56 |
| 5 | 9.770 087 | 2.90 | 9.907 498 | | 9.862 589 | | 0.137 411 | 55 |
| 6 | .770 260 | 2.88 | .907 406 | 1.53 | .862 854 | 4.42 | .137 146 | 54 |
| 7 | .770 433 | 2.88 | .907 314 | 1.53 | .863 119 | 4.42 | .136 881 | 53 |
| 8 | .770 606 | 2.88 | .907 222 | 1.53 | .863 385 | 4.43 | .136 615 | 52 |
| 9 | .770 779 | 2.88 | .907 129 | 1.55 | .863 650 | 4.42 | .136 350 | 51 |
| 10 | 9.770 952 | 2.88 | 9.907 037 | | 9.863 915 | | 0.136 085 | 50 |
| 11 | .771 125 | 2.88 | .906 945 | 1.53 | .864 180 | 4.42 | .135 820 | 49 |
| 12 | .771 298 | 2.87 | .906 852 | 1.55 | .864 445 | 4.42 | .135 555 | 48 |
| 13 | .771 470 | 2.88 | .906 760 | 1.53 | .864 710 | 4.42 | .135 290 | 47 |
| 14 | .771 643 | 2.87 | .906 667 | 1.55 | .864 975 | 4.42 | .135 025 | 46 |
| 15 | 9.771 815 | 2.87 | 9.906 575 | | 9.865 240 | | 0.134 760 | 45 |
| 16 | .771 987 | 2.87 | .906 482 | 1.55 | .865 505 | 4.42 | .134 495 | 44 |
| 17 | .772 159 | 2.87 | .906 389 | 1.55 | .865 770 | 4.42 | .134 230 | 43 |
| 18 | .772 331 | 2.87 | .906 296 | 1.55 | .866 035 | 4.42 | .133 965 | 42 |
| 19 | .772 503 | 2.87 | .906 204 | 1.53 | .866 300 | 4.40 | .133 700 | 41 |
| 20 | 9.772 675 | 2.87 | 9.906 111 | | 9.866 564 | | 0.133 436 | 40 |
| 21 | .772 847 | 2.85 | .906 018 | 1.55 | .866 829 | 4.42 | .133 171 | 39 |
| 22 | .773 018 | 2.87 | .905 925 | 1.55 | .867 094 | 4.42 | .132 906 | 38 |
| 23 | .773 190 | 2.85 | .905 832 | 1.55 | .867 358 | 4.40 | .132 642 | 37 |
| 24 | .773 361 | 2.87 | .905 739 | 1.55 | .867 623 | 4.42 | .132 377 | 36 |
| 25 | 9.773 533 | 2.85 | 9.905 645 | | 9.867 887 | | 0.132 113 | 35 |
| 26 | .773 704 | 2.85 | .905 552 | 1.55 | .868 152 | 4.42 | .131 848 | 34 |
| 27 | .773 875 | 2.85 | .905 459 | 1.55 | .868 416 | 4.40 | .131 583 | 33 |
| 28 | .774 046 | 2.85 | .905 366 | 1.55 | .868 680 | 4.40 | .131 320 | 32 |
| 29 | .774 217 | 2.85 | .905 272 | 1.57 | .868 945 | 4.42 | .131 055 | 31 |
| 30 | 9.774 388 | 2.83 | 9.905 179 | | 9.869 209 | | 0.130 791 | 30 |
| 31 | .774 558 | 2.85 | .905 085 | 1.57 | .869 473 | 4.40 | .130 527 | 29 |
| 32 | .774 729 | 2.83 | .904 992 | 1.55 | .869 737 | 4.40 | .130 263 | 28 |
| 33 | .774 899 | 2.85 | .904 898 | 1.57 | .870 001 | 4.40 | .129 999 | 27 |
| 34 | .775 070 | 2.83 | .904 804 | 1.55 | .870 265 | 4.40 | .129 735 | 26 |
| 35 | 9.775 240 | 2.83 | 9.904 711 | | 9.870 529 | | 0.129 471 | 25 |
| 36 | .775 410 | 2.83 | .904 617 | 1.57 | .870 793 | 4.40 | .129 207 | 24 |
| 37 | .775 580 | 2.83 | .904 523 | 1.57 | .871 057 | 4.40 | .128 943 | 23 |
| 38 | .775 750 | 2.83 | .904 429 | 1.57 | .871 321 | 4.40 | .128 679 | 22 |
| 39 | .775 920 | 2.83 | .904 335 | 1.57 | .871 585 | 4.40 | .128 415 | 21 |
| 40 | 9.776 090 | 2.82 | 9.904 241 | | 9.871 849 | | 0.128 151 | 20 |
| 41 | .776 259 | 2.83 | .904 147 | 1.57 | .872 112 | 4.38 | .127 888 | 19 |
| 42 | .776 429 | 2.82 | .904 053 | 1.57 | .872 376 | 4.40 | .127 624 | 18 |
| 43 | .776 598 | 2.82 | .903 959 | 1.57 | .872 640 | 4.40 | .127 360 | 17 |
| 44 | .776 768 | 2.82 | .903 864 | 1.58 | .872 903 | 4.38 | .127 097 | 16 |
| 45 | 9.776 937 | 2.82 | 9.903 770 | | 9.873 167 | | 0.126 833 | 15 |
| 46 | .777 106 | 2.82 | .903 676 | 1.57 | .873 430 | 4.38 | .126 570 | 14 |
| 47 | .777 275 | 2.82 | .903 581 | 1.58 | .873 694 | 4.40 | .126 306 | 13 |
| 48 | .777 444 | 2.82 | .903 487 | 1.57 | .873 957 | 4.38 | .126 043 | 12 |
| 49 | .777 613 | 2.80 | .903 392 | 1.58 | .874 220 | 4.38 | .125 780 | 11 |
| 50 | 9.777 781 | 2.82 | 9.903 298 | | 9.874 484 | | 0.125 516 | 10 |
| 51 | .777 950 | 2.82 | .903 203 | 1.58 | .874 747 | 4.38 | .125 253 | 9 |
| 52 | .778 119 | 2.80 | .903 108 | 1.58 | .875 010 | 4.38 | .124 990 | 8 |
| 53 | .778 287 | 2.80 | .903 014 | 1.57 | .875 273 | 4.38 | .124 727 | 7 |
| 54 | .778 455 | 2.82 | .902 919 | 1.58 | .875 537 | 4.40 | .124 463 | 6 |
| 55 | 9.778 624 | 2.80 | 9.902 824 | | 9.875 800 | | 0.124 200 | 5 |
| 56 | .778 792 | 2.80 | .902 729 | 1.58 | .876 063 | 4.38 | .123 937 | 4 |
| 57 | .778 960 | 2.80 | .902 634 | 1.58 | .876 326 | 4.38 | .123 674 | 3 |
| 58 | .779 128 | 2.78 | .902 539 | 1.58 | .876 589 | 4.38 | .123 411 | 2 |
| 59 | .779 295 | 2.80 | .902 444 | 1.58 | .876 852 | 4.38 | .123 148 | 1 |
| 60 | 9.779 463 | | 9.902 349 | | 9.877 114 | | 0.122 886 | 0 |

Cos. D. 1". Sin. D. 1". Cot. D. 1". Tan. M.

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.779 463 | 2.80 | 9.902 349 | 1.60 | 9.877 114 | 4.38 | 0.122 886 | 60 |
| 1 | .779 631 | 2.78 | .902 253 | 1.58 | .877 377 | 4.38 | .122 623 | 59 |
| 2 | .779 798 | 2.80 | .902 158 | 1.58 | .877 640 | 4.38 | .122 360 | 58 |
| 3 | .779 966 | 2.78 | .902 063 | 1.60 | .877 903 | 4.37 | .122 097 | 57 |
| 4 | .780 133 | 2.78 | .901 967 | 1.58 | .878 165 | 4.38 | .121 835 | 56 |
| 5 | 9.780 300 | 2.78 | 9.901 872 | 1.60 | 9.878 428 | 4.38 | 0.121 572 | 55 |
| 6 | .780 467 | 2.78 | .901 776 | 1.58 | .878 691 | 4.37 | .121 309 | 54 |
| 7 | .780 634 | 2.78 | .901 681 | 1.60 | .878 953 | 4.37 | .121 047 | 53 |
| 8 | .780 801 | 2.78 | .901 585 | 1.60 | .879 216 | 4.37 | .120 784 | 52 |
| 9 | .780 968 | 2.77 | .901 490 | 1.60 | .879 478 | 4.38 | .120 522 | 51 |
| 10 | 9.781 134 | 2.78 | 9.901 394 | 1.60 | 9.879 741 | 4.37 | 0.120 259 | 50 |
| 11 | .781 301 | 2.78 | .901 298 | 1.60 | .880 003 | 4.37 | .119 997 | 49 |
| 12 | .781 468 | 2.77 | .901 202 | 1.60 | .880 265 | 4.38 | .119 735 | 48 |
| 13 | .781 634 | 2.77 | .901 106 | 1.60 | .880 528 | 4.37 | .119 472 | 47 |
| 14 | .781 800 | 2.77 | .901 010 | 1.60 | .880 790 | 4.37 | .119 210 | 46 |
| 15 | 9.781 966 | 2.77 | 9.900 914 | 1.60 | 9.881 052 | 4.37 | 0.118 948 | 45 |
| 16 | .782 132 | 2.77 | .900 818 | 1.60 | .881 314 | 4.38 | .118 686 | 44 |
| 17 | .782 298 | 2.77 | .900 722 | 1.60 | .881 577 | 4.37 | .118 423 | 43 |
| 18 | .782 464 | 2.77 | .900 626 | 1.62 | .881 839 | 4.37 | .118 161 | 42 |
| 19 | .782 630 | 2.77 | .900 529 | 1.60 | .882 101 | 4.37 | .117 899 | 41 |
| 20 | 9.782 796 | 2.75 | 9.900 433 | 1.60 | 9.882 363 | 4.37 | 0.117 637 | 40 |
| 21 | .782 961 | 2.77 | .900 337 | 1.62 | .882 625 | 4.37 | .117 375 | 39 |
| 22 | .783 127 | 2.75 | .900 240 | 1.60 | .882 887 | 4.35 | .117 113 | 38 |
| 23 | .783 292 | 2.77 | .900 144 | 1.62 | .883 148 | 4.37 | .116 852 | 37 |
| 24 | .783 458 | 2.75 | .900 047 | 1.60 | .883 410 | 4.37 | .116 590 | 36 |
| 25 | 9.783 623 | 2.75 | 9.899 951 | 1.62 | 9.883 672 | 4.37 | 0.116 328 | 35 |
| 26 | .783 788 | 2.75 | .899 854 | 1.62 | .883 934 | 4.37 | .116 066 | 34 |
| 27 | .783 953 | 2.75 | .899 757 | 1.62 | .884 196 | 4.35 | .115 804 | 33 |
| 28 | .784 118 | 2.73 | .899 660 | 1.60 | .884 457 | 4.37 | .115 543 | 32 |
| 29 | .784 282 | 2.75 | .899 564 | 1.62 | .884 719 | 4.35 | .115 281 | 31 |
| 30 | 9.784 447 | 2.75 | 9.899 467 | 1.62 | 9.884 980 | 4.37 | 0.115 020 | 30 |
| 31 | .784 612 | 2.73 | .899 370 | 1.62 | .885 242 | 4.37 | .114 758 | 29 |
| 32 | .784 776 | 2.75 | .899 273 | 1.62 | .885 504 | 4.35 | .114 496 | 28 |
| 33 | .784 941 | 2.73 | .899 176 | 1.63 | .885 765 | 4.35 | .114 235 | 27 |
| 34 | .785 105 | 2.73 | .899 078 | 1.62 | .886 026 | 4.37 | .113 974 | 26 |
| 35 | 9.785 269 | 2.73 | 9.898 981 | 1.62 | 9.886 288 | 4.35 | 0.113 712 | 25 |
| 36 | .785 433 | 2.73 | .898 884 | 1.62 | .886 549 | 4.37 | .113 451 | 24 |
| 37 | .785 597 | 2.73 | .898 787 | 1.63 | .886 811 | 4.35 | .113 189 | 23 |
| 38 | .785 761 | 2.73 | .898 689 | 1.62 | .887 072 | 4.35 | .112 928 | 22 |
| 39 | .785 925 | 2.73 | .898 592 | 1.63 | .887 333 | 4.35 | .112 667 | 21 |
| 40 | 9.786 089 | 2.72 | 9.898 494 | 1.62 | 9.887 594 | 4.35 | 0.112 406 | 20 |
| 41 | .786 252 | 2.73 | .898 397 | 1.63 | .887 855 | 4.35 | .112 145 | 19 |
| 42 | .786 416 | 2.72 | .898 299 | 1.62 | .888 116 | 4.37 | .111 884 | 18 |
| 43 | .786 579 | 2.72 | .898 202 | 1.63 | .888 378 | 4.35 | .111 622 | 17 |
| 44 | .786 742 | 2.73 | .898 104 | 1.63 | .888 639 | 4.35 | .111 361 | 16 |
| 45 | 9.786 906 | 2.72 | 9.898 006 | 1.63 | 9.888 900 | 4.35 | 0.111 100 | 15 |
| 46 | .787 069 | 2.72 | .897 908 | 1.63 | .889 161 | 4.33 | .110 839 | 14 |
| 47 | .787 232 | 2.72 | .897 810 | 1.63 | .889 421 | 4.35 | .110 579 | 13 |
| 48 | .787 395 | 2.70 | .897 712 | 1.63 | .889 682 | 4.35 | .110 318 | 12 |
| 49 | .787 557 | 2.72 | .897 614 | 1.63 | .889 943 | 4.35 | .110 057 | 11 |
| 50 | 9.787 720 | 2.72 | 9.897 516 | 1.63 | 9.890 204 | 4.35 | 0.109 796 | 10 |
| 51 | .787 883 | 2.70 | .897 418 | 1.63 | .890 465 | 4.33 | .109 535 | 9 |
| 52 | .788 045 | 2.72 | .897 320 | 1.63 | .890 725 | 4.35 | .109 275 | 8 |
| 53 | .788 208 | 2.70 | .897 222 | 1.65 | .890 986 | 4.35 | .109 014 | 7 |
| 54 | .788 370 | 2.70 | .897 123 | 1.63 | .891 247 | 4.33 | .108 753 | 6 |
| 55 | 9.788 532 | 2.70 | 9.897 025 | 1.65 | 9.891 507 | 4.35 | 0.108 493 | 5 |
| 56 | .788 694 | 2.70 | .896 926 | 1.63 | .891 768 | 4.33 | .108 232 | 4 |
| 57 | .788 856 | 2.70 | .896 828 | 1.65 | .892 028 | 4.35 | .107 972 | 3 |
| 58 | .789 018 | 2.70 | .896 729 | 1.63 | .892 289 | 4.33 | .107 711 | 2 |
| 59 | .789 180 | 2.70 | .896 631 | 1.65 | .892 549 | 4.35 | .107 451 | 1 |
| 60 | 9.789 342 | | 9.896 532 | | 9.892 810 | | 0.107 190 | 0 |

| M. | Sin. | D. 1''. | Cos. | D. 1''. | Tan. | D. 1''. | Cot. | M. |
|----|-----------|---------|-----------|---------|-----------|---------|-----------|----|
| 0 | 9.789 342 | | 9.896 532 | 1.65 | 9.892 810 | | 0.107 190 | 60 |
| 1 | .789 504 | 2.70 | .896 433 | 1.63 | .893 070 | 4.33 | .106 930 | 59 |
| 2 | .789 665 | 2.68 | .896 335 | 1.63 | .893 331 | 4.35 | .106 669 | 58 |
| 3 | .789 827 | 2.70 | .896 236 | 1.65 | .893 591 | 4.33 | .106 409 | 57 |
| 4 | .789 988 | 2.68 | .896 137 | 1.65 | .893 851 | 4.33 | .106 149 | 56 |
| 5 | 9.790 149 | 2.68 | 9.896 038 | 1.65 | 9.894 111 | | 0.105 889 | 55 |
| 6 | .790 310 | 2.68 | .895 939 | 1.65 | .894 372 | 4.35 | .105 628 | 54 |
| 7 | .790 471 | 2.68 | .895 840 | 1.65 | .894 632 | 4.33 | .105 368 | 53 |
| 8 | .790 632 | 2.68 | .895 741 | 1.67 | .894 892 | 4.33 | .105 108 | 52 |
| 9 | .790 793 | 2.68 | .895 641 | 1.65 | .895 152 | 4.33 | .104 848 | 51 |
| 10 | 9.790 954 | 2.68 | 9.895 542 | 1.65 | 9.895 412 | | 0.104 588 | 50 |
| 11 | .791 115 | 2.67 | .895 443 | 1.67 | .895 672 | 4.33 | .104 328 | 49 |
| 12 | .791 275 | 2.68 | .895 343 | 1.65 | .895 932 | 4.33 | .104 068 | 48 |
| 13 | .791 436 | 2.67 | .895 244 | 1.65 | .896 192 | 4.33 | .103 808 | 47 |
| 14 | .791 596 | 2.68 | .895 145 | 1.67 | .896 452 | 4.33 | .103 548 | 46 |
| 15 | 9.791 757 | 2.67 | 9.895 045 | 1.67 | 9.896 712 | | 0.103 288 | 45 |
| 16 | .791 917 | 2.67 | .894 945 | 1.65 | .896 971 | 4.32 | .103 029 | 44 |
| 17 | .792 077 | 2.67 | .894 846 | 1.65 | .897 231 | 4.33 | .102 769 | 43 |
| 18 | .792 237 | 2.67 | .894 746 | 1.67 | .897 491 | 4.33 | .102 509 | 42 |
| 19 | .792 397 | 2.67 | .894 646 | 1.67 | .897 751 | 4.32 | .102 249 | 41 |
| 20 | 9.792 557 | 2.65 | 9.894 546 | 1.67 | 9.898 010 | | 0.101 990 | 40 |
| 21 | .792 716 | 2.67 | .894 446 | 1.67 | .898 270 | 4.33 | .101 730 | 39 |
| 22 | .792 876 | 2.65 | .894 346 | 1.67 | .898 530 | 4.33 | .101 470 | 38 |
| 23 | .793 035 | 2.65 | .894 246 | 1.67 | .898 789 | 4.32 | .101 211 | 37 |
| 24 | .793 195 | 2.65 | .894 146 | 1.67 | .899 049 | 4.32 | .100 951 | 36 |
| 25 | 9.793 354 | 2.67 | 9.894 046 | 1.67 | 9.899 308 | | 0.100 692 | 35 |
| 26 | .793 514 | 2.65 | .893 946 | 1.67 | .899 568 | 4.33 | .100 432 | 34 |
| 27 | .793 673 | 2.65 | .893 846 | 1.68 | .899 827 | 4.32 | .100 173 | 33 |
| 28 | .793 832 | 2.65 | .893 745 | 1.67 | .900 087 | 4.33 | .099 913 | 32 |
| 29 | .793 991 | 2.65 | .893 645 | 1.68 | .900 346 | 4.32 | .099 654 | 31 |
| 30 | 9.794 150 | 2.63 | 9.893 544 | 1.67 | 9.900 605 | | 0.099 395 | 30 |
| 31 | .794 308 | 2.65 | .893 444 | 1.68 | .900 864 | 4.32 | .099 136 | 29 |
| 32 | .794 467 | 2.65 | .893 343 | 1.67 | .901 124 | 4.33 | .098 876 | 28 |
| 33 | .794 626 | 2.63 | .893 243 | 1.68 | .901 383 | 4.32 | .098 617 | 27 |
| 34 | .794 784 | 2.63 | .893 142 | 1.68 | .901 642 | 4.32 | .098 358 | 26 |
| 35 | 9.794 942 | 2.65 | 9.893 041 | 1.68 | 9.901 901 | | 0.098 099 | 25 |
| 36 | .795 101 | 2.63 | .892 940 | 1.68 | .902 160 | 4.32 | .097 840 | 24 |
| 37 | .795 259 | 2.63 | .892 839 | 1.67 | .902 420 | 4.33 | .097 580 | 23 |
| 38 | .795 417 | 2.63 | .892 739 | 1.68 | .902 679 | 4.32 | .097 321 | 22 |
| 39 | .795 575 | 2.63 | .892 638 | 1.70 | .902 938 | 4.32 | .097 062 | 21 |
| 40 | 9.795 733 | 2.63 | 9.892 536 | 1.68 | 9.903 197 | | 0.096 803 | 20 |
| 41 | .795 891 | 2.63 | .892 435 | 1.68 | .903 456 | 4.32 | .096 544 | 19 |
| 42 | .796 049 | 2.62 | .892 334 | 1.68 | .903 714 | 4.30 | .096 286 | 18 |
| 43 | .796 206 | 2.63 | .892 233 | 1.68 | .903 973 | 4.32 | .096 027 | 17 |
| 44 | .796 364 | 2.62 | .892 132 | 1.70 | .904 232 | 4.32 | .095 768 | 16 |
| 45 | 9.796 521 | 2.63 | 9.892 030 | 1.68 | 9.904 491 | | 0.095 509 | 15 |
| 46 | .796 679 | 2.62 | .891 929 | 1.70 | .904 750 | 4.32 | .095 250 | 14 |
| 47 | .796 836 | 2.62 | .891 827 | 1.68 | .905 008 | 4.30 | .094 992 | 13 |
| 48 | .796 993 | 2.62 | .891 726 | 1.68 | .905 267 | 4.32 | .094 733 | 12 |
| 49 | .797 150 | 2.62 | .891 624 | 1.70 | .905 526 | 4.32 | .094 474 | 11 |
| 50 | 9.797 307 | 2.62 | 9.891 523 | 1.68 | 9.905 785 | | 0.094 215 | 10 |
| 51 | .797 464 | 2.62 | .891 421 | 1.70 | .906 043 | 4.30 | .093 957 | 9 |
| 52 | .797 621 | 2.60 | .891 319 | 1.70 | .906 302 | 4.32 | .093 698 | 8 |
| 53 | .797 777 | 2.62 | .891 217 | 1.70 | .906 560 | 4.30 | .093 440 | 7 |
| 54 | .797 934 | 2.62 | .891 115 | 1.70 | .906 819 | 4.32 | .093 181 | 6 |
| 55 | 9.798 091 | 2.60 | 9.891 013 | 1.70 | 9.907 077 | | 0.092 923 | 5 |
| 56 | .798 247 | 2.60 | .890 911 | 1.70 | .907 336 | 4.32 | .092 664 | 4 |
| 57 | .798 403 | 2.62 | .890 809 | 1.70 | .907 594 | 4.30 | .092 406 | 3 |
| 58 | .798 560 | 2.62 | .890 707 | 1.70 | .907 853 | 4.32 | .092 147 | 2 |
| 59 | .798 716 | 2.60 | .890 605 | 1.70 | .908 111 | 4.30 | .091 889 | 1 |
| 60 | 9.798 872 | 2.60 | 9.890 503 | 1.70 | 9.908 369 | | 0.091 631 | 0 |
| | Cos. | D. 1''. | Sin. | D. 1''. | Cot. | D. 1''. | Tan. | M. |

LOGARITHMIC SINES, COSINES, TANGENTS, AND COTANGENTS. 57

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| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.798 872 | 2.60 | 9.890 503 | 1.72 | 9.908 369 | 4.32 | 0.091 631 | 60 |
| 1 | .799 028 | 2.60 | .890 400 | 1.70 | .908 628 | 4.30 | .091 372 | 59 |
| 2 | .799 184 | 2.58 | .890 298 | 1.72 | .908 886 | 4.30 | .091 114 | 58 |
| 3 | .799 339 | 2.60 | .890 195 | 1.70 | .909 144 | 4.30 | .090 856 | 57 |
| 4 | .799 495 | 2.60 | .890 093 | 1.72 | .909 402 | 4.30 | .090 598 | 56 |
| 5 | 9.799 651 | 2.58 | 9.889 990 | 1.70 | 9.909 660 | 4.30 | 0.090 340 | 55 |
| 6 | .799 806 | 2.60 | .889 888 | 1.72 | .909 918 | 4.32 | .090 082 | 54 |
| 7 | .799 962 | 2.58 | .889 785 | 1.72 | .910 177 | 4.30 | .089 823 | 53 |
| 8 | .800 117 | 2.58 | .889 682 | 1.72 | .910 435 | 4.30 | .089 565 | 52 |
| 9 | .800 272 | 2.58 | .889 579 | 1.70 | .910 693 | 4.30 | .089 307 | 51 |
| 10 | 9.800 427 | 2.58 | 9.889 477 | 1.72 | 9.910 951 | 4.30 | 0.089 049 | 50 |
| 11 | .800 582 | 2.58 | .889 374 | 1.72 | .911 209 | 4.30 | .088 791 | 49 |
| 12 | .800 737 | 2.58 | .889 271 | 1.72 | .911 467 | 4.30 | .088 533 | 48 |
| 13 | .800 892 | 2.58 | .889 168 | 1.72 | .911 725 | 4.30 | .088 275 | 47 |
| 14 | .801 047 | 2.57 | .889 064 | 1.73 | .911 982 | 4.28 | .088 018 | 46 |
| 15 | 9.801 201 | 2.58 | 9.888 961 | 1.72 | 9.912 240 | 4.30 | 0.087 760 | 45 |
| 16 | .801 356 | 2.58 | .888 858 | 1.72 | .912 498 | 4.30 | .087 502 | 44 |
| 17 | .801 511 | 2.57 | .888 755 | 1.73 | .912 756 | 4.30 | .087 244 | 43 |
| 18 | .801 665 | 2.57 | .888 651 | 1.72 | .913 014 | 4.28 | .086 986 | 42 |
| 19 | .801 819 | 2.57 | .888 548 | 1.73 | .913 271 | 4.30 | .086 729 | 41 |
| 20 | 9.801 973 | 2.58 | 9.888 444 | 1.72 | 9.913 529 | 4.30 | 0.086 471 | 40 |
| 21 | .802 128 | 2.57 | .888 341 | 1.73 | .913 787 | 4.28 | .086 213 | 39 |
| 22 | .802 282 | 2.57 | .888 237 | 1.72 | .914 044 | 4.30 | .085 956 | 38 |
| 23 | .802 436 | 2.55 | .888 134 | 1.73 | .914 302 | 4.30 | .085 698 | 37 |
| 24 | .802 589 | 2.57 | .888 030 | 1.73 | .914 560 | 4.28 | .085 440 | 36 |
| 25 | 9.802 743 | 2.57 | 9.887 926 | 1.73 | 9.914 817 | 4.30 | 0.085 183 | 35 |
| 26 | .802 897 | 2.55 | .887 822 | 1.73 | .915 075 | 4.28 | .084 925 | 34 |
| 27 | .803 050 | 2.57 | .887 718 | 1.73 | .915 332 | 4.30 | .084 668 | 33 |
| 28 | .803 204 | 2.55 | .887 614 | 1.73 | .915 590 | 4.28 | .084 410 | 32 |
| 29 | .803 357 | 2.57 | .887 510 | 1.73 | .915 847 | 4.28 | .084 153 | 31 |
| 30 | 9.803 511 | 2.55 | 9.887 406 | 1.73 | 9.916 104 | 4.30 | 0.083 896 | 30 |
| 31 | .803 664 | 2.55 | .887 302 | 1.73 | .916 362 | 4.28 | .083 638 | 29 |
| 32 | .803 817 | 2.55 | .887 198 | 1.75 | .916 619 | 4.28 | .083 381 | 28 |
| 33 | .803 970 | 2.55 | .887 093 | 1.73 | .916 877 | 4.30 | .083 123 | 27 |
| 34 | .804 123 | 2.55 | .886 989 | 1.73 | .917 134 | 4.28 | .082 866 | 26 |
| 35 | 9.804 276 | 2.53 | 9.886 885 | 1.75 | 9.917 391 | 4.28 | 0.082 609 | 25 |
| 36 | .804 428 | 2.55 | .886 780 | 1.73 | .917 648 | 4.30 | .082 352 | 24 |
| 37 | .804 581 | 2.55 | .886 676 | 1.75 | .917 906 | 4.28 | .082 094 | 23 |
| 38 | .804 734 | 2.53 | .886 571 | 1.75 | .918 163 | 4.28 | .081 837 | 22 |
| 39 | .804 886 | 2.55 | .886 466 | 1.73 | .918 420 | 4.28 | .081 580 | 21 |
| 40 | 9.805 039 | 2.53 | 9.886 362 | 1.75 | 9.918 677 | 4.28 | 0.081 323 | 20 |
| 41 | .805 191 | 2.53 | .886 257 | 1.75 | .918 934 | 4.28 | .081 066 | 19 |
| 42 | .805 343 | 2.53 | .886 152 | 1.75 | .919 191 | 4.28 | .080 809 | 18 |
| 43 | .805 495 | 2.53 | .886 047 | 1.75 | .919 448 | 4.28 | .080 552 | 17 |
| 44 | .805 647 | 2.53 | .885 942 | 1.75 | .919 705 | 4.28 | .080 295 | 16 |
| 45 | 9.805 799 | 2.53 | 9.885 837 | 1.75 | 9.919 962 | 4.28 | 0.080 038 | 15 |
| 46 | .805 951 | 2.53 | .885 732 | 1.75 | .920 219 | 4.28 | .079 781 | 14 |
| 47 | .806 103 | 2.52 | .885 627 | 1.75 | .920 476 | 4.28 | .079 524 | 13 |
| 48 | .806 254 | 2.53 | .885 522 | 1.77 | .920 733 | 4.28 | .079 267 | 12 |
| 49 | .806 406 | 2.52 | .885 416 | 1.75 | .920 990 | 4.28 | .079 010 | 11 |
| 50 | 9.806 557 | 2.53 | 9.885 311 | 1.77 | 9.921 247 | 4.27 | 0.078 753 | 10 |
| 51 | .806 709 | 2.52 | .885 205 | 1.75 | .921 503 | 4.28 | .078 497 | 9 |
| 52 | .806 860 | 2.52 | .885 100 | 1.77 | .921 760 | 4.28 | .078 240 | 8 |
| 53 | .807 011 | 2.53 | .884 994 | 1.75 | .922 017 | 4.28 | .077 983 | 7 |
| 54 | .807 163 | 2.52 | .884 889 | 1.77 | .922 274 | 4.27 | .077 726 | 6 |
| 55 | 9.807 314 | 2.52 | 9.884 783 | 1.77 | 9.922 530 | 4.28 | 0.077 470 | 5 |
| 56 | .807 465 | 2.50 | .884 677 | 1.75 | .922 787 | 4.28 | .077 213 | 4 |
| 57 | .807 615 | 2.52 | .884 572 | 1.77 | .923 044 | 4.27 | .076 956 | 3 |
| 58 | .807 766 | 2.52 | .884 466 | 1.77 | .923 300 | 4.27 | .076 700 | 2 |
| 59 | .807 917 | 2.50 | .884 360 | 1.77 | .923 557 | 4.28 | .076 443 | 1 |
| 60 | 9.808 067 | | 9.884 254 | 1.77 | 9.923 814 | | 0.076 186 | 0 |
| | Cos. | D. 1". | Sin. | D. 1". | Cot. | D. 1". | Tan. | M. |

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.808 067 | 2.52 | 9.884 254 | 1.77 | 9.923 814 | 4.27 | 0.076 186 | 60 |
| 1 | .808 218 | 2.50 | .884 148 | 1.77 | .924 070 | 4.28 | .075 930 | 59 |
| 2 | .808 368 | 2.52 | .884 042 | 1.77 | .924 327 | 4.27 | .075 673 | 58 |
| 3 | .808 519 | 2.50 | .883 936 | 1.78 | .924 583 | 4.28 | .075 417 | 57 |
| 4 | .808 669 | 2.50 | .883 829 | 1.77 | .924 840 | 4.27 | .075 160 | 56 |
| 5 | 9.808 819 | 2.50 | 9.883 723 | 1.77 | 9.925 096 | 4.27 | 0.074 904 | 55 |
| 6 | .808 969 | 2.50 | .883 617 | 1.78 | .925 352 | 4.28 | .074 648 | 54 |
| 7 | .809 119 | 2.50 | .883 510 | 1.77 | .925 609 | 4.27 | .074 391 | 53 |
| 8 | .809 269 | 2.50 | .883 404 | 1.78 | .925 865 | 4.28 | .074 135 | 52 |
| 9 | .809 419 | 2.50 | .883 297 | 1.77 | .926 122 | 4.27 | .073 878 | 51 |
| 10 | 9.809 569 | 2.48 | 9.883 191 | 1.78 | 9.926 378 | 4.27 | 0.073 622 | 50 |
| 11 | .809 718 | 2.50 | .883 084 | 1.78 | .926 634 | 4.27 | .073 366 | 49 |
| 12 | .809 868 | 2.48 | .882 977 | 1.77 | .926 890 | 4.28 | .073 110 | 48 |
| 13 | .810 017 | 2.50 | .882 871 | 1.78 | .927 147 | 4.27 | .072 853 | 47 |
| 14 | .810 167 | 2.48 | .882 764 | 1.78 | .927 403 | 4.27 | .072 597 | 46 |
| 15 | 9.810 316 | 2.48 | 9.882 657 | 1.78 | 9.927 659 | 4.27 | 0.072 341 | 45 |
| 16 | .810 465 | 2.48 | .882 550 | 1.78 | .927 915 | 4.27 | .072 085 | 44 |
| 17 | .810 614 | 2.48 | .882 443 | 1.78 | .928 171 | 4.27 | .071 829 | 43 |
| 18 | .810 763 | 2.48 | .882 336 | 1.78 | .928 427 | 4.28 | .071 573 | 42 |
| 19 | .810 912 | 2.48 | .882 229 | 1.80 | .928 684 | 4.27 | .071 316 | 41 |
| 20 | 9.811 061 | 2.48 | 9.882 121 | 1.78 | 9.928 940 | 4.27 | 0.071 060 | 40 |
| 21 | .811 210 | 2.47 | .882 014 | 1.78 | .929 196 | 4.27 | .070 804 | 39 |
| 22 | .811 358 | 2.48 | .881 907 | 1.80 | .929 452 | 4.27 | .070 548 | 38 |
| 23 | .811 507 | 2.47 | .881 799 | 1.78 | .929 708 | 4.27 | .070 292 | 37 |
| 24 | .811 655 | 2.48 | .881 692 | 1.80 | .929 964 | 4.27 | .070 036 | 36 |
| 25 | 9.811 804 | 2.47 | 9.881 584 | 1.78 | 9.930 220 | 4.25 | 0.069 780 | 35 |
| 26 | .811 952 | 2.47 | .881 477 | 1.80 | .930 475 | 4.27 | .069 525 | 34 |
| 27 | .812 100 | 2.47 | .881 369 | 1.80 | .930 731 | 4.27 | .069 269 | 33 |
| 28 | .812 248 | 2.47 | .881 261 | 1.80 | .930 987 | 4.27 | .069 013 | 32 |
| 29 | .812 396 | 2.47 | .881 153 | 1.78 | .931 243 | 4.27 | .068 757 | 31 |
| 30 | 9.812 544 | 2.47 | 9.881 046 | 1.80 | 9.931 499 | 4.27 | 0.068 501 | 30 |
| 31 | .812 692 | 2.47 | .880 938 | 1.80 | .931 755 | 4.25 | .068 245 | 29 |
| 32 | .812 840 | 2.47 | .880 830 | 1.80 | .932 010 | 4.27 | .067 990 | 28 |
| 33 | .812 988 | 2.45 | .880 722 | 1.82 | .932 266 | 4.27 | .067 734 | 27 |
| 34 | .813 135 | 2.47 | .880 613 | 1.80 | .932 522 | 4.27 | .067 478 | 26 |
| 35 | 9.813 283 | 2.45 | 9.880 505 | 1.80 | 9.932 778 | 4.25 | 0.067 222 | 25 |
| 36 | .813 430 | 2.47 | .880 397 | 1.80 | .933 033 | 4.27 | .066 967 | 24 |
| 37 | .813 578 | 2.45 | .880 289 | 1.82 | .933 289 | 4.27 | .066 711 | 23 |
| 38 | .813 725 | 2.45 | .880 180 | 1.80 | .933 545 | 4.25 | .066 455 | 22 |
| 39 | .813 872 | 2.45 | .880 072 | 1.82 | .933 800 | 4.27 | .066 200 | 21 |
| 40 | 9.814 019 | 2.45 | 9.879 963 | 1.80 | 9.934 056 | 4.25 | 0.065 944 | 20 |
| 41 | .814 166 | 2.45 | .879 855 | 1.82 | .934 311 | 4.27 | .065 689 | 19 |
| 42 | .814 313 | 2.45 | .879 746 | 1.82 | .934 567 | 4.25 | .065 433 | 18 |
| 43 | .814 460 | 2.45 | .879 637 | 1.80 | .934 822 | 4.27 | .065 178 | 17 |
| 44 | .814 607 | 2.43 | .879 529 | 1.82 | .935 078 | 4.25 | .064 922 | 16 |
| 45 | 9.814 753 | 2.45 | 9.879 420 | 1.82 | 9.935 333 | 4.27 | 0.064 667 | 15 |
| 46 | .814 900 | 2.43 | .879 311 | 1.82 | .935 589 | 4.25 | .064 411 | 14 |
| 47 | .815 046 | 2.45 | .879 202 | 1.82 | .935 844 | 4.27 | .064 156 | 13 |
| 48 | .815 193 | 2.43 | .879 093 | 1.82 | .936 100 | 4.25 | .063 900 | 12 |
| 49 | .815 339 | 2.43 | .878 984 | 1.82 | .936 355 | 4.27 | .063 645 | 11 |
| 50 | 9.815 485 | 2.45 | 9.878 875 | 1.82 | 9.936 611 | 4.25 | 0.063 389 | 10 |
| 51 | .815 632 | 2.43 | .878 766 | 1.83 | .936 866 | 4.25 | .063 134 | 9 |
| 52 | .815 778 | 2.43 | .878 656 | 1.82 | .937 121 | 4.27 | .062 879 | 8 |
| 53 | .815 924 | 2.42 | .878 547 | 1.82 | .937 377 | 4.25 | .062 623 | 7 |
| 54 | .816 069 | 2.43 | .878 438 | 1.83 | .937 632 | 4.25 | .062 368 | 6 |
| 55 | 9.816 215 | 2.43 | 9.878 328 | 1.82 | 9.937 887 | 4.25 | 0.062 113 | 5 |
| 56 | .816 361 | 2.43 | .878 219 | 1.83 | .938 142 | 4.27 | .061 858 | 4 |
| 57 | .816 507 | 2.42 | .878 109 | 1.83 | .938 398 | 4.25 | .061 602 | 3 |
| 58 | .816 652 | 2.43 | .877 999 | 1.82 | .938 653 | 4.25 | .061 347 | 2 |
| 59 | .816 798 | 2.42 | .877 890 | 1.83 | .938 908 | 4.25 | .061 092 | 1 |
| 60 | 9.816 943 | | 9.877 780 | | 9.939 163 | | 0.060 837 | 0 |

41°

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.816 943 | 2.42 | 9.877 780 | 1.83 | 9.939 163 | 4.25 | 0.060 837 | 60 |
| 1 | .817 088 | 2.42 | .877 670 | 1.83 | .939 418 | 4.25 | .060 582 | 59 |
| 2 | .817 233 | 2.43 | .877 560 | 1.83 | .939 673 | 4.25 | .060 327 | 58 |
| 3 | .817 379 | 2.42 | .877 450 | 1.83 | .939 928 | 4.25 | .060 072 | 57 |
| 4 | .817 524 | 2.40 | .877 340 | 1.83 | .940 183 | 4.27 | .059 817 | 56 |
| 5 | 9.817 668 | 2.42 | 9.877 230 | 1.83 | 9.940 439 | 4.25 | 0.059 561 | 55 |
| 6 | .817 813 | 2.42 | .877 120 | 1.83 | .940 694 | 4.25 | .059 306 | 54 |
| 7 | .817 958 | 2.42 | .877 010 | 1.83 | .940 949 | 4.25 | .059 051 | 53 |
| 8 | .818 103 | 2.42 | .876 899 | 1.85 | .941 204 | 4.25 | .058 796 | 52 |
| 9 | .818 247 | 2.40 | .876 789 | 1.83 | .941 459 | 4.25 | .058 541 | 51 |
| 10 | 9.818 392 | 2.42 | 9.876 678 | 1.83 | 9.941 713 | 4.25 | 0.058 287 | 50 |
| 11 | .818 536 | 2.42 | .876 568 | 1.85 | .941 968 | 4.25 | .058 032 | 49 |
| 12 | .818 681 | 2.40 | .876 457 | 1.85 | .942 223 | 4.25 | .057 777 | 48 |
| 13 | .818 825 | 2.40 | .876 347 | 1.83 | .942 478 | 4.25 | .057 522 | 47 |
| 14 | .818 969 | 2.40 | .876 236 | 1.85 | .942 733 | 4.25 | .057 267 | 46 |
| 15 | 9.819 113 | 2.40 | 9.876 125 | 1.85 | 9.942 988 | 4.25 | 0.057 012 | 45 |
| 16 | .819 257 | 2.40 | .876 014 | 1.83 | .943 243 | 4.25 | .056 757 | 44 |
| 17 | .819 401 | 2.40 | .875 904 | 1.85 | .943 498 | 4.23 | .056 502 | 43 |
| 18 | .819 545 | 2.40 | .875 793 | 1.85 | .943 752 | 4.23 | .056 248 | 42 |
| 19 | .819 689 | 2.38 | .875 682 | 1.85 | .944 007 | 4.25 | .055 993 | 41 |
| 20 | 9.819 832 | 2.40 | 9.875 571 | 1.87 | 9.944 262 | 4.25 | 0.055 738 | 40 |
| 21 | .819 976 | 2.40 | .875 459 | 1.85 | .944 517 | 4.23 | .055 483 | 39 |
| 22 | .820 120 | 2.38 | .875 348 | 1.85 | .944 771 | 4.25 | .055 229 | 38 |
| 23 | .820 263 | 2.38 | .875 237 | 1.85 | .945 026 | 4.25 | .054 974 | 37 |
| 24 | .820 406 | 2.40 | .875 126 | 1.87 | .945 281 | 4.23 | .054 719 | 36 |
| 25 | 9.820 550 | 2.38 | 9.875 014 | 1.85 | 9.945 535 | 4.25 | 0.054 465 | 35 |
| 26 | .820 693 | 2.38 | .874 903 | 1.87 | .945 790 | 4.25 | .054 210 | 34 |
| 27 | .820 836 | 2.38 | .874 791 | 1.85 | .946 045 | 4.23 | .053 955 | 33 |
| 28 | .820 979 | 2.38 | .874 680 | 1.87 | .946 299 | 4.25 | .053 701 | 32 |
| 29 | .821 122 | 2.38 | .874 568 | 1.87 | .946 554 | 4.23 | .053 446 | 31 |
| 30 | 9.821 265 | 2.37 | 9.874 456 | 1.87 | 9.946 808 | 4.25 | 0.053 192 | 30 |
| 31 | .821 407 | 2.38 | .874 344 | 1.87 | .947 063 | 4.25 | .052 937 | 29 |
| 32 | .821 550 | 2.38 | .874 232 | 1.85 | .947 318 | 4.23 | .052 682 | 28 |
| 33 | .821 693 | 2.37 | .874 121 | 1.87 | .947 572 | 4.23 | .052 428 | 27 |
| 34 | .821 835 | 2.37 | .874 009 | 1.88 | .947 827 | 4.23 | .052 173 | 26 |
| 35 | 9.821 977 | 2.38 | 9.873 896 | 1.87 | 9.948 081 | 4.23 | 0.051 919 | 25 |
| 36 | .822 120 | 2.37 | .873 784 | 1.87 | .948 335 | 4.25 | .051 665 | 24 |
| 37 | .822 262 | 2.37 | .873 672 | 1.87 | .948 590 | 4.23 | .051 410 | 23 |
| 38 | .822 404 | 2.37 | .873 560 | 1.87 | .948 844 | 4.25 | .051 156 | 22 |
| 39 | .822 546 | 2.37 | .873 448 | 1.88 | .949 099 | 4.23 | .050 901 | 21 |
| 40 | 9.822 688 | 2.37 | 9.873 335 | 1.87 | 9.949 353 | 4.25 | 0.050 647 | 20 |
| 41 | .822 830 | 2.37 | .873 223 | 1.88 | .949 608 | 4.23 | .050 392 | 19 |
| 42 | .822 972 | 2.37 | .873 110 | 1.87 | .949 862 | 4.23 | .050 138 | 18 |
| 43 | .823 114 | 2.35 | .872 998 | 1.88 | .950 116 | 4.25 | .049 884 | 17 |
| 44 | .823 255 | 2.37 | .872 885 | 1.88 | .950 371 | 4.23 | .049 629 | 16 |
| 45 | 9.823 397 | 2.37 | 9.872 772 | 1.88 | 9.950 625 | 4.23 | 0.049 375 | 15 |
| 46 | .823 539 | 2.35 | .872 659 | 1.87 | .950 879 | 4.23 | .049 121 | 14 |
| 47 | .823 680 | 2.35 | .872 547 | 1.88 | .951 133 | 4.25 | .048 867 | 13 |
| 48 | .823 821 | 2.35 | .872 434 | 1.88 | .951 388 | 4.23 | .048 612 | 12 |
| 49 | .823 963 | 2.35 | .872 321 | 1.88 | .951 642 | 4.23 | .048 358 | 11 |
| 50 | 9.824 104 | 2.35 | 9.872 208 | 1.88 | 9.951 896 | 4.23 | 0.048 104 | 10 |
| 51 | .824 245 | 2.35 | .872 095 | 1.90 | .952 150 | 4.25 | .047 850 | 9 |
| 52 | .824 386 | 2.35 | .871 981 | 1.88 | .952 405 | 4.23 | .047 595 | 8 |
| 53 | .824 527 | 2.35 | .871 868 | 1.88 | .952 659 | 4.23 | .047 341 | 7 |
| 54 | .824 668 | 2.33 | .871 755 | 1.90 | .952 913 | 4.23 | .047 087 | 6 |
| 55 | 9.824 808 | 2.35 | 9.871 641 | 1.88 | 9.953 167 | 4.23 | 0.046 833 | 5 |
| 56 | .824 949 | 2.35 | .871 528 | 1.90 | .953 421 | 4.23 | .046 579 | 4 |
| 57 | .825 090 | 2.33 | .871 414 | 1.88 | .953 675 | 4.23 | .046 325 | 3 |
| 58 | .825 230 | 2.35 | .871 301 | 1.90 | .953 929 | 4.23 | .046 071 | 2 |
| 59 | .825 371 | 2.33 | .871 187 | 1.90 | .954 183 | 4.23 | .045 817 | 1 |
| 60 | 9.825 511 | . | 9.871 073 | 1.90 | 9.954 437 | . | 0.045 563 | 0 |

Cos. D. 1". Sin. D. 1". Cot. D. 1". Tan. M.

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------------|--------|-----------|--------|-----------|----|
| 0 | .9825 511 | 2.33 | .9871 073 | 1.88 | 9.954 437 | 4.23 | 0.045 563 | 60 |
| 1 | .825 651 | 2.33 | .870 960 | 1.90 | .954 691 | 4.25 | .045 309 | 59 |
| 2 | .825 791 | 2.33 | .870 846 | 1.90 | .954 946 | 4.23 | .045 054 | 58 |
| 3 | .825 931 | 2.33 | .870 732 | 1.90 | .955 200 | 4.23 | .044 800 | 57 |
| 4 | .826 071 | 2.33 | <u>.870 618</u> | 1.90 | .955 454 | 4.23 | .044 546 | 56 |
| 5 | 9.826 211 | 2.33 | 9.870 504 | 1.90 | 9.955 708 | 4.22 | 0.044 292 | 55 |
| 6 | .826 351 | 2.33 | .870 390 | 1.90 | .955 961 | 4.23 | .044 039 | 54 |
| 7 | .826 491 | 2.33 | .870 276 | 1.92 | .950 215 | 4.23 | .043 785 | 53 |
| 8 | .826 631 | 2.32 | .870 161 | 1.90 | .956 469 | 4.23 | .043 531 | 52 |
| 9 | .826 770 | 2.33 | .870 047 | 1.90 | .956 723 | 4.23 | .043 277 | 51 |
| 10 | 9.826 910 | 2.32 | 9.869 933 | 1.92 | 9.956 977 | 4.23 | 0.043 023 | 50 |
| 11 | .827 049 | 2.33 | .869 818 | 1.90 | .957 231 | 4.23 | .042 769 | 49 |
| 12 | .827 189 | 2.32 | .869 704 | 1.92 | .957 485 | 4.23 | .042 515 | 48 |
| 13 | .827 328 | 2.32 | .869 589 | 1.92 | .957 739 | 4.23 | .042 261 | 47 |
| 14 | .827 467 | 2.32 | .869 474 | 1.90 | .957 993 | 4.23 | .042 007 | 46 |
| 15 | 9.827 606 | 2.32 | 9.869 360 | 1.92 | 9.958 247 | 4.22 | 0.041 753 | 45 |
| 16 | .827 745 | 2.32 | .869 245 | 1.92 | .958 500 | 4.23 | .041 500 | 44 |
| 17 | .827 884 | 2.32 | .869 130 | 1.92 | .958 754 | 4.23 | .041 246 | 43 |
| 18 | .828 023 | 2.32 | .869 015 | 1.92 | .959 008 | 4.23 | .040 992 | 42 |
| 19 | .828 162 | 2.32 | .868 900 | 1.92 | .959 262 | 4.23 | .040 738 | 41 |
| 20 | 9.828 301 | 2.30 | 9.868 785 | 1.92 | 9.959 516 | 4.22 | 0.040 484 | 40 |
| 21 | .828 439 | 2.32 | .868 670 | 1.92 | .959 769 | 4.23 | .040 231 | 39 |
| 22 | .828 578 | 2.30 | .868 555 | 1.92 | .960 023 | 4.23 | .039 977 | 38 |
| 23 | .828 716 | 2.32 | .868 440 | 1.93 | .960 277 | 4.22 | .039 723 | 37 |
| 24 | .828 855 | 2.30 | .868 324 | 1.92 | .960 530 | 4.23 | .039 470 | 36 |
| 25 | 9.828 993 | 2.30 | 9.868 209 | 1.93 | 9.960 784 | 4.23 | 0.039 216 | 35 |
| 26 | .829 131 | 2.30 | .868 093 | 1.92 | .961 038 | 4.23 | .038 962 | 34 |
| 27 | .829 269 | 2.30 | .867 978 | 1.93 | .961 292 | 4.22 | .038 708 | 33 |
| 28 | .829 407 | 2.30 | .867 862 | 1.92 | .961 545 | 4.23 | .038 455 | 32 |
| 29 | .829 545 | 2.30 | .867 747 | 1.93 | .961 799 | 4.22 | .038 201 | 31 |
| 30 | 9.829 683 | 2.30 | 9.867 631 | 1.93 | 9.962 052 | 4.23 | 0.037 948 | 30 |
| 31 | .829 821 | 2.30 | .867 515 | 1.93 | .962 306 | 4.23 | .037 694 | 29 |
| 32 | .829 959 | 2.30 | .867 399 | 1.93 | .962 560 | 4.22 | .037 440 | 28 |
| 33 | .830 097 | 2.28 | .867 283 | 1.93 | .962 813 | 4.23 | .037 187 | 27 |
| 34 | .830 234 | 2.30 | .867 167 | 1.93 | .963 067 | 4.22 | .036 933 | 26 |
| 35 | 9.830 372 | 2.28 | 9.867 051 | 1.93 | 9.963 320 | 4.23 | 0.036 680 | 25 |
| 36 | .830 509 | 2.28 | .866 935 | 1.93 | .963 574 | 4.23 | .036 426 | 24 |
| 37 | .830 646 | 2.30 | .866 819 | 1.93 | .963 828 | 4.22 | .036 172 | 23 |
| 38 | .830 784 | 2.28 | .866 703 | 1.95 | .964 081 | 4.23 | .035 919 | 22 |
| 39 | .830 921 | 2.28 | .866 586 | 1.93 | .964 335 | 4.22 | .035 665 | 21 |
| 40 | 9.831 058 | 2.28 | 9.866 470 | 1.95 | 9.964 588 | 4.23 | 0.035 412 | 20 |
| 41 | .831 195 | 2.28 | .866 353 | 1.93 | .964 842 | 4.22 | .035 158 | 19 |
| 42 | .831 332 | 2.28 | .866 237 | 1.95 | .965 095 | 4.23 | .034 905 | 18 |
| 43 | .831 469 | 2.28 | .866 120 | 1.93 | .965 349 | 4.22 | .034 651 | 17 |
| 44 | .831 606 | 2.27 | .866 004 | 1.95 | .965 602 | 4.22 | .034 398 | 16 |
| 45 | 9.831 742 | 2.28 | 9.865 887 | 1.95 | 9.965 855 | 4.23 | 0.034 145 | 15 |
| 46 | .831 879 | 2.27 | .865 770 | 1.95 | .966 109 | 4.22 | .033 891 | 14 |
| 47 | .832 015 | 2.28 | .865 653 | 1.95 | .966 362 | 4.23 | .033 638 | 13 |
| 48 | .832 152 | 2.27 | .865 536 | 1.95 | .966 616 | 4.22 | .033 384 | 12 |
| 49 | .832 288 | 2.28 | .865 419 | 1.95 | .966 869 | 4.23 | .033 131 | 11 |
| 50 | 9.832 425 | 2.27 | 9.865 302 | 1.95 | 9.967 123 | 4.22 | 0.032 877 | 10 |
| 51 | .832 561 | 2.27 | .865 185 | 1.95 | .967 376 | 4.22 | .032 624 | 9 |
| 52 | .832 697 | 2.27 | .865 068 | 1.97 | .967 629 | 4.23 | .032 371 | 8 |
| 53 | .832 833 | 2.27 | .864 950 | 1.95 | .967 883 | 4.22 | .032 117 | 7 |
| 54 | .832 969 | 2.27 | .864 833 | 1.95 | .968 136 | 4.22 | .031 864 | 6 |
| 55 | 9.833 105 | 2.27 | 9.864 716 | 1.97 | 9.968 389 | 4.23 | 0.031 611 | 5 |
| 56 | .833 241 | 2.27 | .864 598 | 1.95 | .968 643 | 4.22 | .031 357 | 4 |
| 57 | .833 377 | 2.25 | .864 481 | 1.97 | .968 896 | 4.22 | .031 104 | 3 |
| 58 | .833 512 | 2.27 | .864 363 | 1.97 | .969 149 | 4.23 | .030 851 | 2 |
| 59 | .833 648 | 2.25 | .864 245 | 1.97 | .969 403 | 4.22 | .030 597 | 1 |
| 60 | 9.833 783 | | 9.864 127 | | 9.969 656 | | 0.030 344 | 0 |
| | Cos. | D. 1". | Sin. | D. 1". | Cot. | D. 1". | Tan. | M. |

| M. | Sin. | D. 1". | Cos. | D. 1". | Tan. | D. 1". | Cot. | M. |
|----|-----------|--------|-----------|--------|-----------|--------|-----------|----|
| 0 | 9.833 783 | | 9.864 127 | | 9.969 656 | | 0.030 344 | 60 |
| 1 | .833 919 | 2.27 | .864 010 | 1.95 | .969 909 | 4.22 | .030 091 | 59 |
| 2 | .834 054 | 2.25 | .863 892 | 1.97 | .970 162 | 4.22 | .029 838 | 58 |
| 3 | .834 189 | 2.25 | .863 774 | 1.97 | .970 416 | 4.23 | .029 584 | 57 |
| 4 | .834 325 | 2.27 | .863 656 | 1.97 | .970 669 | 4.22 | .029 331 | 56 |
| 5 | 9.834 460 | | 9.863 538 | | 9.970 922 | | 0.029 078 | 55 |
| 6 | .834 595 | 2.25 | .863 419 | 1.98 | .971 175 | 4.22 | .028 825 | 54 |
| 7 | .834 730 | 2.25 | .863 301 | 1.97 | .971 429 | 4.23 | .028 571 | 53 |
| 8 | .834 865 | 2.25 | .863 183 | 1.97 | .971 682 | 4.22 | .028 318 | 52 |
| 9 | .834 999 | 2.23 | .863 064 | 1.98 | .971 935 | 4.22 | .028 065 | 51 |
| 10 | 9.835 134 | | 9.862 946 | | 9.972 188 | | 0.027 812 | 50 |
| 11 | .835 269 | 2.25 | .862 827 | 1.98 | .972 441 | 4.22 | .027 559 | 49 |
| 12 | .835 403 | 2.23 | .862 709 | 1.97 | .972 695 | 4.23 | .027 305 | 48 |
| 13 | .835 538 | 2.25 | .862 590 | 1.98 | .972 948 | 4.22 | .027 052 | 47 |
| 14 | .835 672 | 2.23 | .862 471 | 1.98 | .973 201 | 4.22 | .026 799 | 46 |
| 15 | 9.835 807 | | 9.862 353 | | 9.973 454 | | 0.026 546 | 45 |
| 16 | .835 941 | 2.23 | .862 234 | 1.98 | .973 707 | 4.22 | .026 293 | 44 |
| 17 | .836 075 | 2.23 | .862 115 | 1.98 | .973 960 | 4.22 | .026 040 | 43 |
| 18 | .836 209 | 2.23 | .861 997 | 1.98 | .974 213 | 4.22 | .025 787 | 42 |
| 19 | .836 343 | 2.23 | .861 877 | 1.98 | .974 466 | 4.23 | .025 534 | 41 |
| 20 | 9.836 477 | | 9.861 758 | | 9.974 720 | | 0.025 280 | 40 |
| 21 | .836 611 | 2.23 | .861 638 | 2.00 | .974 973 | 4.22 | .025 027 | 39 |
| 22 | .836 745 | 2.23 | .861 519 | 1.98 | .975 226 | 4.22 | .024 774 | 38 |
| 23 | .836 878 | 2.22 | .861 400 | 1.98 | .975 479 | 4.22 | .024 521 | 37 |
| 24 | .837 012 | 2.23 | .861 280 | 2.00 | .975 732 | 4.22 | .024 268 | 36 |
| 25 | 9.837 146 | | 9.861 161 | | 9.975 985 | | 0.024 015 | 35 |
| 26 | .837 279 | 2.22 | .861 041 | 2.00 | .976 238 | 4.22 | .023 762 | 34 |
| 27 | .837 412 | 2.22 | .860 922 | 1.98 | .976 491 | 4.22 | .023 509 | 33 |
| 28 | .837 546 | 2.23 | .860 802 | 2.00 | .976 744 | 4.22 | .023 256 | 32 |
| 29 | .837 679 | 2.22 | .860 682 | 2.00 | .976 997 | 4.22 | .023 003 | 31 |
| 30 | 9.837 812 | | 9.860 562 | | 9.977 250 | | 0.022 750 | 30 |
| 31 | .837 945 | 2.22 | .860 442 | 2.00 | .977 503 | 4.22 | .022 497 | 29 |
| 32 | .838 078 | 2.22 | .860 322 | 2.00 | .977 756 | 4.22 | .022 244 | 28 |
| 33 | .838 211 | 2.22 | .860 202 | 2.00 | .978 009 | 4.22 | .021 991 | 27 |
| 34 | .838 344 | 2.22 | .860 082 | 2.00 | .978 262 | 4.22 | .021 738 | 26 |
| 35 | 9.838 477 | | 9.859 962 | | 9.978 515 | | 0.021 485 | 25 |
| 36 | .838 610 | 2.22 | .859 842 | 2.00 | .978 768 | 4.22 | .021 232 | 24 |
| 37 | .838 742 | 2.20 | .859 721 | 2.02 | .979 021 | 4.22 | .020 979 | 23 |
| 38 | .838 875 | 2.22 | .859 601 | 2.00 | .979 274 | 4.22 | .020 726 | 22 |
| 39 | .839 007 | 2.22 | .859 480 | 2.02 | .979 527 | 4.22 | .020 473 | 21 |
| 40 | 9.839 140 | | 9.859 360 | | 9.979 780 | | 0.020 220 | 20 |
| 41 | .839 272 | 2.20 | .859 239 | 2.02 | .980 033 | 4.22 | .019 967 | 19 |
| 42 | .839 404 | 2.20 | .859 119 | 2.00 | .980 286 | 4.22 | .019 714 | 18 |
| 43 | .839 536 | 2.20 | .858 998 | 2.02 | .980 538 | 4.20 | .019 462 | 17 |
| 44 | .839 668 | 2.20 | .858 877 | 2.02 | .980 791 | 4.22 | .019 209 | 16 |
| 45 | 9.839 800 | | 9.858 756 | | 9.981 044 | | 0.018 956 | 15 |
| 46 | .839 932 | 2.20 | .858 635 | 2.02 | .981 297 | 4.22 | .018 703 | 14 |
| 47 | .840 064 | 2.20 | .858 514 | 2.02 | .981 550 | 4.22 | .018 450 | 13 |
| 48 | .840 196 | 2.20 | .858 393 | 2.02 | .981 803 | 4.22 | .018 197 | 12 |
| 49 | .840 328 | 2.18 | .858 272 | 2.02 | .982 056 | 4.22 | .017 944 | 11 |
| 50 | 9.840 459 | | 9.858 151 | | 9.982 309 | | 0.017 691 | 10 |
| 51 | .840 591 | 2.20 | .858 029 | 2.03 | .982 562 | 4.22 | .017 438 | 9 |
| 52 | .840 722 | 2.18 | .857 908 | 2.02 | .982 814 | 4.20 | .017 186 | 8 |
| 53 | .840 854 | 2.20 | .857 786 | 2.03 | .983 067 | 4.22 | .016 933 | 7 |
| 54 | .840 985 | 2.18 | .857 665 | 2.02 | .983 320 | 4.22 | .016 680 | 6 |
| 55 | 9.841 116 | | 9.857 543 | | 9.983 573 | | 0.016 427 | 5 |
| 56 | .841 247 | 2.18 | .857 422 | 2.02 | .983 826 | 4.22 | .016 174 | 4 |
| 57 | .841 378 | 2.18 | .857 300 | 2.03 | .984 079 | 4.22 | .015 921 | 3 |
| 58 | .841 509 | 2.18 | .857 178 | 2.03 | .984 332 | 4.22 | .015 668 | 2 |
| 59 | .841 640 | 2.18 | .857 056 | 2.03 | .984 584 | 4.20 | .015 416 | 1 |
| 60 | 9.841 771 | | 9.856 934 | | 9.984 837 | | 0.015 163 | 0 |

| M. | Sin. | D. 1''. | Cos. | D. 1''. | Tan. | D. 1''. | Cot. | |
|----|-----------|---------|-----------|---------|-----------|---------|-----------|----|
| 0 | 9.841 771 | 2.18 | 9.856 934 | 2.03 | 9.984 837 | 4.22 | 0.015 163 | 60 |
| 1 | .841 902 | 2.18 | .856 812 | 2.03 | .985 090 | 4.22 | .014 910 | 59 |
| 2 | .842 033 | 2.17 | .856 690 | 2.03 | .985 343 | 4.22 | .014 657 | 58 |
| 3 | .842 163 | 2.18 | .856 568 | 2.03 | .985 596 | 4.20 | .014 404 | 57 |
| 4 | .842 294 | 2.17 | .856 446 | 2.05 | .985 848 | 4.22 | .014 152 | 56 |
| 5 | 9.842 424 | 2.18 | 9.856 323 | 2.03 | 9.986 101 | 4.22 | 0.013 899 | 55 |
| 6 | .842 555 | 2.17 | .856 201 | 2.05 | .986 354 | 4.22 | .013 646 | 54 |
| 7 | .842 685 | 2.17 | .856 078 | 2.03 | .986 607 | 4.22 | .013 393 | 53 |
| 8 | .842 815 | 2.18 | .855 956 | 2.05 | .986 860 | 4.20 | .013 140 | 52 |
| 9 | .842 946 | 2.17 | .855 833 | 2.03 | .987 112 | 4.22 | .012 888 | 51 |
| 10 | 9.843 076 | 2.17 | 9.855 711 | 2.05 | 9.987 365 | 4.22 | 0.012 635 | 50 |
| 11 | .843 206 | 2.17 | .855 588 | 2.05 | .987 618 | 4.22 | .012 382 | 49 |
| 12 | .843 336 | 2.17 | .855 465 | 2.05 | .987 871 | 4.20 | .012 129 | 48 |
| 13 | .843 466 | 2.15 | .855 342 | 2.05 | .988 123 | 4.22 | .011 877 | 47 |
| 14 | .843 595 | 2.17 | .855 219 | 2.05 | .988 376 | 4.22 | .011 624 | 46 |
| 15 | 9.843 725 | 2.17 | 9.855 096 | 2.05 | 9.988 629 | 4.22 | 0.011 371 | 45 |
| 16 | .843 855 | 2.15 | .854 973 | 2.05 | .988 882 | 4.20 | .011 118 | 44 |
| 17 | .843 984 | 2.17 | .854 850 | 2.05 | .989 134 | 4.22 | .010 866 | 43 |
| 18 | .844 114 | 2.15 | .854 727 | 2.07 | .989 387 | 4.22 | .010 613 | 42 |
| 19 | .844 243 | 2.15 | .854 603 | 2.05 | .989 640 | 4.22 | .010 360 | 41 |
| 20 | 9.844 372 | 2.17 | 9.854 480 | 2.07 | 9.989 893 | 4.20 | 0.010 107 | 40 |
| 21 | .844 502 | 2.15 | .854 356 | 2.05 | .990 145 | 4.22 | .009 855 | 39 |
| 22 | .844 631 | 2.15 | .854 233 | 2.07 | .990 398 | 4.22 | .009 602 | 38 |
| 23 | .844 760 | 2.15 | .854 109 | 2.05 | .990 651 | 4.20 | .009 349 | 37 |
| 24 | .844 889 | 2.15 | .853 986 | 2.07 | .990 903 | 4.22 | .009 097 | 36 |
| 25 | 9.845 018 | 2.15 | 9.853 862 | 2.07 | 9.991 156 | 4.22 | 0.008 844 | 35 |
| 26 | .845 147 | 2.15 | .853 738 | 2.07 | .991 409 | 4.22 | .008 591 | 34 |
| 27 | .845 276 | 2.15 | .853 614 | 2.07 | .991 662 | 4.20 | .008 338 | 33 |
| 28 | .845 405 | 2.13 | .853 490 | 2.07 | .991 914 | 4.22 | .008 086 | 32 |
| 29 | .845 533 | 2.15 | .853 366 | 2.07 | .992 167 | 4.22 | .007 833 | 31 |
| 30 | 9.845 662 | 2.13 | 9.853 242 | 2.07 | 9.992 420 | 4.20 | 0.007 580 | 30 |
| 31 | .845 790 | 2.15 | .853 118 | 2.07 | .992 672 | 4.22 | .007 328 | 29 |
| 32 | .845 919 | 2.13 | .852 994 | 2.08 | .992 925 | 4.22 | .007 075 | 28 |
| 33 | .846 047 | 2.13 | .852 869 | 2.07 | .993 178 | 4.22 | .006 822 | 27 |
| 34 | .846 175 | 2.15 | .852 745 | 2.08 | .993 431 | 4.20 | .006 569 | 26 |
| 35 | 9.846 304 | 2.13 | 9.852 620 | 2.07 | 9.993 683 | 4.22 | 0.006 317 | 25 |
| 36 | .846 432 | 2.13 | .852 496 | 2.08 | .993 936 | 4.22 | .006 064 | 24 |
| 37 | .846 560 | 2.13 | .852 371 | 2.07 | .994 189 | 4.20 | .005 811 | 23 |
| 38 | .846 688 | 2.13 | .852 247 | 2.08 | .994 441 | 4.22 | .005 559 | 22 |
| 39 | .846 816 | 2.13 | .852 122 | 2.08 | .994 694 | 4.22 | .005 306 | 21 |
| 40 | 9.846 944 | 2.12 | 9.851 997 | 2.08 | 9.994 947 | 4.20 | 0.005 053 | 20 |
| 41 | .847 071 | 2.13 | .851 872 | 2.08 | .995 199 | 4.22 | .004 801 | 19 |
| 42 | .847 199 | 2.13 | .851 747 | 2.08 | .995 452 | 4.22 | .004 548 | 18 |
| 43 | .847 327 | 2.12 | .851 622 | 2.08 | .995 705 | 4.20 | .004 295 | 17 |
| 44 | .847 454 | 2.13 | .851 497 | 2.08 | .995 957 | 4.22 | .004 043 | 16 |
| 45 | 9.847 582 | 2.12 | 9.851 372 | 2.10 | 9.996 210 | 4.22 | 0.003 790 | 15 |
| 46 | .847 709 | 2.12 | .851 246 | 2.08 | .996 463 | 4.20 | .003 537 | 14 |
| 47 | .847 836 | 2.13 | .851 121 | 2.08 | .996 715 | 4.22 | .003 285 | 13 |
| 48 | .847 964 | 2.12 | .850 996 | 2.10 | .996 968 | 4.22 | .003 032 | 12 |
| 49 | .848 091 | 2.12 | .850 870 | 2.08 | .997 221 | 4.20 | .002 779 | 11 |
| 50 | 9.848 218 | 2.12 | 9.850 745 | 2.10 | 9.997 473 | 4.22 | 0.002 527 | 10 |
| 51 | .848 345 | 2.12 | .850 619 | 2.10 | .997 726 | 4.22 | .002 274 | 9 |
| 52 | .848 472 | 2.12 | .850 493 | 2.08 | .997 979 | 4.20 | .002 021 | 8 |
| 53 | .848 599 | 2.12 | .850 368 | 2.10 | .998 231 | 4.22 | .001 769 | 7 |
| 54 | .848 726 | 2.10 | .850 242 | 2.10 | .998 484 | 4.22 | .001 516 | 6 |
| 55 | 9.848 852 | 2.12 | 9.850 116 | 2.10 | 9.998 737 | 4.20 | 0.001 263 | 5 |
| 56 | .848 979 | 2.12 | .849 990 | 2.10 | .998 989 | 4.22 | .001 011 | 4 |
| 57 | .849 106 | 2.10 | .849 864 | 2.10 | .999 242 | 4.22 | .000 758 | 3 |
| 58 | .849 232 | 2.12 | .849 738 | 2.12 | .999 495 | 4.20 | .000 505 | 2 |
| 59 | .849 359 | 2.10 | .849 611 | 2.10 | .999 747 | 4.22 | .000 253 | 1 |
| 60 | 9.849 485 | | 9.849 485 | | 0.000 000 | | 0.000 000 | 0 |

| | Cos. | D. 1''. | Sin. | D. 1''. | Cot. | D. 1''. | Tan. | M. |
|--|------|---------|------|---------|------|---------|------|----|
|--|------|---------|------|---------|------|---------|------|----|

A TABLE
OF THE
NATURAL SINES, COSINES, TANGENTS,
AND COTANGENTS,
FOR EVERY
DEGREE AND MINUTE FROM 0° TO 90° .

0°

1°

2°

| M. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | M. |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0 | .00000 | 1.0000 | .00000 | ∞ | .01745 | .99985 | .01746 | 57.290 | .03490 | .99939 | .03492 | 28.636 | 60 |
| 1 | 029 | 000 | 029 | 3437.7 | 774 | 984 | 775 | 56.351 | 519 | 938 | 521 | .399 | 59 |
| 2 | 058 | 000 | 058 | 1718.9 | 803 | 984 | 804 | 55.442 | 548 | 937 | 550 | .166 | 58 |
| 3 | 087 | 000 | 087 | 1145.9 | 832 | 983 | 833 | 54.561 | 577 | 936 | 579 | 27.937 | 57 |
| 4 | 116 | 000 | 116 | 859.44 | 862 | 983 | 862 | 53.709 | 606 | 935 | 609 | .712 | 56 |
| 5 | .00145 | 1.0000 | .00145 | 687.55 | .01891 | .99982 | .01891 | 52.882 | .03635 | .99934 | .03638 | 27.490 | 55 |
| 6 | 175 | 000 | 175 | 572.96 | 920 | 982 | 920 | .081 | 664 | 933 | 667 | .271 | 54 |
| 7 | 204 | 000 | 204 | 491.11 | 949 | 981 | 949 | 51.303 | 693 | 932 | 696 | .057 | 53 |
| 8 | 233 | 000 | 233 | 429.72 | 978 | 980 | 978 | 50.549 | 723 | 931 | 725 | 26.845 | 52 |
| 9 | 262 | 000 | 262 | 381.97 | .02007 | 980 | .02007 | 49.816 | 752 | 930 | 754 | .637 | 51 |
| 10 | .00291 | 1.0000 | .00291 | 343.77 | .02036 | .99979 | .02036 | 49.104 | .03785 | .99929 | .03783 | 26.432 | 50 |
| 11 | 320 | .99999 | 320 | 312.52 | 065 | 979 | 066 | 48.412 | 810 | 927 | 812 | .230 | 49 |
| 12 | 349 | .999 | 349 | 286.48 | 094 | 978 | 095 | 47.740 | 839 | 926 | 842 | .031 | 48 |
| 13 | 378 | .999 | 378 | 264.44 | 123 | 977 | 124 | .085 | 868 | 925 | 871 | 25.835 | 47 |
| 14 | 407 | .999 | 407 | 245.55 | 152 | 977 | 153 | 46.449 | 897 | 924 | 900 | .642 | 46 |
| 15 | .00436 | .99999 | .00436 | 229.18 | .02181 | .99976 | .02182 | 45.829 | .03926 | .99923 | .03929 | 25.452 | 45 |
| 16 | 465 | .999 | 465 | 214.86 | 211 | 976 | 211 | .226 | 955 | 922 | 958 | .264 | 44 |
| 17 | 495 | .999 | 495 | 202.22 | 240 | 975 | 240 | 44.639 | 984 | 921 | 987 | .080 | 43 |
| 18 | 524 | .999 | 524 | 190.98 | 269 | 974 | 269 | .066 | .04013 | 919 | .04016 | 24.898 | 42 |
| 19 | 553 | .998 | 553 | 180.93 | 298 | 974 | 298 | 43.508 | 042 | 918 | 046 | .719 | 41 |
| 20 | .00582 | .99998 | .00582 | 171.89 | .02327 | .99973 | .02328 | 42.964 | .04071 | .99917 | .04075 | 24.542 | 40 |
| 21 | 611 | .998 | 611 | 163.70 | 356 | 972 | 357 | .433 | 100 | 916 | 104 | .368 | 39 |
| 22 | 640 | .998 | 640 | 156.26 | 385 | 972 | 386 | 41.916 | 129 | 915 | 133 | .196 | 38 |
| 23 | 669 | .998 | 669 | 149.47 | 414 | 971 | 415 | .411 | 159 | 913 | 162 | .026 | 37 |
| 24 | 698 | .998 | 698 | 143.24 | 443 | 970 | 444 | 40.917 | 188 | 912 | 191 | 23.859 | 36 |
| 25 | .00727 | .99997 | .00727 | 137.51 | .02472 | .99969 | .02473 | 40.436 | .04217 | .99911 | .04220 | 23.695 | 35 |
| 25 | 756 | .997 | 756 | 132.22 | 501 | 969 | 502 | 39.965 | 246 | 910 | 250 | .532 | 34 |
| 27 | 785 | .997 | 785 | 127.32 | 530 | 968 | 531 | .506 | 275 | 909 | 279 | .372 | 33 |
| 28 | 814 | .997 | 815 | 122.77 | 560 | 967 | 560 | .057 | 304 | 907 | 308 | .214 | 32 |
| 29 | 844 | .996 | 844 | 118.54 | 589 | 966 | 589 | 38.618 | 333 | 906 | 337 | .058 | 31 |
| 30 | .00873 | .99996 | .00873 | 114.59 | .02618 | .99966 | .02619 | 38.188 | .04362 | .99905 | .04366 | 22.904 | 30 |
| 31 | 902 | .996 | 902 | 110.89 | 647 | 965 | 648 | 37.769 | 391 | 904 | 395 | .752 | 29 |
| 32 | 931 | .996 | 931 | 107.43 | 676 | 964 | 677 | .358 | 420 | 902 | 424 | .602 | 28 |
| 33 | 960 | .995 | 960 | 104.17 | 705 | 963 | 706 | 36.956 | 449 | 901 | 454 | .454 | 27 |
| 34 | 989 | .995 | 989 | 101.11 | 734 | 963 | 735 | .563 | 478 | 900 | 483 | .308 | 26 |
| 35 | .01018 | .99995 | .01018 | 98.218 | .02763 | .99962 | .02764 | 36.178 | .04507 | .99898 | .04512 | 22.164 | 25 |
| 36 | 047 | .995 | 047 | 95.483 | 792 | 961 | 793 | 35.801 | 536 | 897 | 541 | .022 | 24 |
| 37 | 076 | .994 | 076 | 92.908 | 821 | 960 | 822 | .431 | 565 | 896 | 570 | 21.881 | 23 |
| 38 | 105 | .994 | 105 | 90.463 | 850 | 959 | 851 | .070 | 594 | 894 | 599 | .743 | 22 |
| 39 | 134 | .994 | 135 | 88.144 | 879 | 959 | 881 | 34.715 | 623 | 893 | 628 | .606 | 21 |
| 40 | .01164 | .99993 | .01164 | 85.940 | .02908 | .99958 | .02910 | 34.368 | .04653 | .99892 | .04658 | 21.470 | 20 |
| 41 | 193 | .993 | 193 | 83.844 | 938 | 957 | 939 | .027 | 682 | 890 | 687 | .337 | 19 |
| 42 | 222 | .993 | 222 | 81.847 | 967 | 956 | 968 | 33.604 | 711 | 889 | 716 | .205 | 18 |
| 43 | 251 | .992 | 251 | 79.943 | 996 | 955 | 997 | .366 | 740 | 888 | 745 | .075 | 17 |
| 44 | 280 | .992 | 280 | 78.126 | .03025 | 954 | .03026 | .045 | 769 | 886 | 774 | 20.046 | 16 |
| 45 | .01309 | .99991 | .01309 | 76.390 | .03054 | .99953 | .03055 | 32.730 | .04798 | .99885 | .04803 | 20.819 | 15 |
| 46 | 338 | .991 | 338 | 74.729 | 083 | 952 | 084 | .421 | 827 | 883 | 833 | .693 | 14 |
| 47 | 367 | .991 | 367 | 73.139 | 112 | 952 | 114 | .118 | 856 | 882 | 862 | .569 | 13 |
| 48 | 396 | .990 | 396 | 71.615 | 141 | 951 | 143 | 31.821 | 885 | 881 | 891 | .446 | 12 |
| 49 | 425 | .990 | 425 | 70.153 | 170 | 950 | 172 | .528 | 914 | 879 | 920 | .325 | 11 |
| 50 | .01454 | .99989 | .01455 | 68.750 | .03199 | .99949 | .03201 | 31.242 | .04943 | .99878 | .04949 | 20.206 | 10 |
| 51 | 483 | .989 | 484 | 67.402 | 228 | 948 | 230 | 30.960 | 972 | 876 | 978 | .087 | 9 |
| 52 | 513 | .989 | 513 | 66.105 | 257 | 947 | 259 | .683 | .05001 | 875 | .05007 | 19.970 | 8 |
| 53 | 542 | .988 | 542 | 64.858 | 286 | 946 | 288 | .412 | 030 | 873 | 037 | .855 | 7 |
| 54 | 571 | .988 | 571 | 63.657 | 316 | 945 | 317 | .145 | 059 | 872 | 066 | .740 | 6 |
| 55 | .01600 | .99987 | .01600 | 62.499 | .03345 | .99944 | .03346 | 29.882 | .05088 | .99870 | .05095 | 19.627 | 5 |
| 56 | 629 | .987 | 629 | 61.383 | 374 | 943 | 376 | .624 | 117 | 869 | 124 | .516 | 4 |
| 57 | 658 | .986 | 658 | 60.306 | 403 | 942 | 405 | .371 | 146 | 867 | 153 | .405 | 3 |
| 58 | 687 | .986 | 687 | 59.266 | 432 | 941 | 434 | .121 | 175 | 866 | 182 | .296 | 2 |
| 59 | 716 | .985 | 716 | 58.261 | 461 | 940 | 463 | 28.877 | 205 | 864 | 212 | .188 | 1 |
| 60 | .01745 | .99985 | .01746 | 57.290 | .03490 | .99939 | .03492 | 28.636 | .05234 | .99863 | .05241 | 19.081 | 0 |

Cos. Sin. Cot. Tan.

Cos. Sin. Cot. Tan.

Cos. Sin. Cot. Tan.

M.

NATURAL SINES, COSINES, TANGENTS, AND COTANGENTS.

3°

4°

5°

| M. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | M. |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0 | .05234 | .99863 | .05241 | 19.081 | .06976 | .99756 | .06993 | 14.301 | .08716 | .99619 | .08749 | 11.430 | 60 |
| 1 | 263 | 861 | 270 | 18.976 | .07005 | 754 | .07022 | .241 | 745 | 617 | 778 | .392 | 59 |
| 2 | 292 | 860 | 299 | .871 | 034 | 752 | 051 | .182 | 774 | 614 | 807 | .354 | 58 |
| 3 | 321 | 858 | 328 | .768 | 063 | 750 | 080 | .124 | 803 | 612 | 837 | .316 | 57 |
| 4 | 350 | 857 | 357 | .666 | 092 | 748 | 110 | .065 | 831 | 609 | 866 | .279 | 56 |
| 5 | .05379 | .99855 | .05387 | 18.564 | .07121 | .99746 | .07139 | 14.008 | .08860 | .99607 | .08895 | 11.242 | 55 |
| 6 | 408 | 854 | 416 | .464 | 150 | 744 | 168 | 13.951 | 889 | 604 | 925 | .205 | 54 |
| 7 | 437 | 852 | 445 | .366 | 179 | 742 | 197 | .894 | 918 | 602 | 954 | .168 | 53 |
| 8 | 466 | 851 | 474 | .268 | 208 | 740 | 227 | .838 | 947 | 599 | 983 | .132 | 52 |
| 9 | 495 | 849 | 503 | .171 | 237 | 738 | 256 | .782 | 976 | 596 | .09013 | .095 | 51 |
| 10 | .05524 | .99847 | .05533 | 18.075 | .07266 | .99736 | .07285 | 13.727 | .09005 | .99594 | .09042 | 11.059 | 50 |
| 11 | 553 | 846 | 562 | 17.980 | 295 | 734 | 314 | .672 | 034 | 591 | 071 | .024 | 49 |
| 12 | 582 | 844 | 591 | .886 | 324 | 731 | 344 | .617 | 063 | 588 | 101 | 10.988 | 48 |
| 13 | 611 | 842 | 620 | .793 | 353 | 729 | 373 | .563 | 092 | 586 | 130 | .953 | 47 |
| 14 | 640 | 841 | 649 | .702 | 382 | 727 | 402 | .510 | 121 | 583 | 159 | .918 | 46 |
| 15 | .05669 | .99839 | .05678 | 17.611 | .07411 | .99725 | .07431 | 13.457 | .09150 | .99580 | .09189 | 10.883 | 45 |
| 16 | 698 | 838 | 708 | .521 | 440 | 723 | 461 | .404 | 179 | 578 | 218 | .848 | 44 |
| 17 | 727 | 836 | 737 | .431 | 469 | 721 | 490 | .352 | 208 | 575 | 247 | .814 | 43 |
| 18 | 756 | 834 | 766 | .343 | 498 | 719 | 519 | .300 | 237 | 572 | 277 | .780 | 42 |
| 19 | 785 | 833 | 795 | .256 | 527 | 716 | 548 | .248 | 266 | 570 | 306 | .746 | 41 |
| 20 | .05814 | .99831 | .05824 | 17.109 | .07556 | .99714 | .07578 | 13.197 | .09295 | .99567 | .09335 | 10.712 | 40 |
| 21 | 844 | 829 | 854 | .084 | 585 | 712 | 607 | .146 | 324 | 564 | 335 | .678 | 39 |
| 22 | 873 | 827 | 883 | 16.999 | 614 | 710 | 636 | .096 | 353 | 562 | 394 | .645 | 38 |
| 23 | 902 | 826 | 912 | .915 | 643 | 708 | 665 | .046 | 382 | 559 | 423 | .612 | 37 |
| 24 | 931 | 824 | 941 | .832 | 672 | 705 | 695 | 12.996 | 411 | 556 | 453 | .579 | 36 |
| 25 | .05960 | .99822 | .05970 | 16.750 | .07701 | .99703 | .07724 | 12.947 | .09440 | .99553 | .09482 | 10.546 | 35 |
| 26 | 989 | 821 | 999 | .668 | 730 | 701 | 753 | .898 | 469 | 551 | 511 | .514 | 34 |
| 27 | .06018 | .99819 | .06029 | .587 | 759 | 699 | 782 | .850 | 498 | 548 | 541 | .481 | 33 |
| 28 | 047 | 817 | 058 | .507 | 788 | 696 | 812 | .801 | 527 | 545 | 570 | .449 | 32 |
| 29 | 076 | 815 | 087 | .428 | 817 | 694 | 841 | .754 | 556 | 542 | 600 | .417 | 31 |
| 30 | .06105 | .99813 | .06116 | 16.350 | .07846 | .99692 | .07870 | 12.706 | .09585 | .99540 | .09629 | 10.385 | 30 |
| 31 | 134 | 812 | 145 | .272 | 875 | 689 | 899 | .659 | 614 | 537 | 658 | .354 | 29 |
| 32 | 163 | 810 | 175 | .195 | 904 | 687 | 929 | .612 | 642 | 534 | 688 | .322 | 28 |
| 33 | 192 | 808 | 204 | .119 | 933 | 685 | 958 | .566 | 671 | 531 | 717 | .291 | 27 |
| 34 | 221 | 806 | 233 | .043 | 962 | 683 | 987 | .520 | 700 | 528 | 746 | .260 | 26 |
| 35 | .06250 | .99804 | .06262 | 15.969 | .07991 | .99680 | .08017 | 12.474 | .09729 | .99526 | .09776 | 10.229 | 25 |
| 36 | 279 | 803 | 291 | .895 | .08020 | 678 | 046 | .429 | 758 | 523 | 805 | .199 | 24 |
| 37 | 308 | 801 | 321 | .821 | 049 | 676 | 075 | .384 | 787 | 520 | 834 | .168 | 23 |
| 38 | 337 | 799 | 350 | .748 | 078 | 673 | 104 | .339 | 816 | 517 | 864 | .138 | 22 |
| 39 | 366 | 797 | 379 | .676 | 107 | 671 | 134 | .295 | 845 | 514 | 893 | .108 | 21 |
| 40 | .06395 | .99795 | .06408 | 15.605 | .08136 | .99668 | .08163 | 12.251 | .09874 | .99511 | .09923 | 10.078 | 20 |
| 41 | 424 | 793 | 438 | .534 | 165 | 666 | 192 | .297 | 903 | 508 | 952 | .048 | 19 |
| 42 | 453 | 792 | 467 | .464 | 194 | 664 | 221 | .163 | 932 | 506 | 981 | .019 | 18 |
| 43 | 482 | 790 | 496 | .394 | 223 | 661 | 251 | .120 | 961 | 503 | 10011 | 9.9893 | 17 |
| 44 | 511 | 788 | 525 | .325 | 252 | 659 | 280 | .077 | 990 | 500 | 040 | .9601 | 16 |
| 45 | .06540 | .99786 | .06554 | 15.257 | .08281 | .99657 | .08309 | 12.035 | .10019 | .99497 | .10069 | 9.9310 | 15 |
| 46 | 569 | 784 | 584 | .189 | 310 | 654 | 339 | 11.992 | 048 | 494 | 099 | .9021 | 14 |
| 47 | 598 | 782 | 613 | .122 | 339 | 652 | 368 | .950 | 077 | 491 | 128 | .8734 | 13 |
| 48 | 627 | 780 | 642 | .056 | 368 | 649 | 397 | .909 | 106 | 488 | 158 | .8448 | 12 |
| 49 | 656 | 778 | 671 | 14.990 | 397 | 647 | 427 | .867 | 135 | 485 | 187 | .8164 | 11 |
| 50 | .06685 | .99776 | .06700 | 14.924 | .08426 | .99644 | .08456 | 11.826 | .10164 | .99482 | .10216 | 9.7882 | 10 |
| 51 | 714 | 774 | 730 | .860 | 455 | 642 | 485 | .785 | 192 | 479 | 246 | .7601 | 9 |
| 52 | 743 | 772 | 759 | .795 | 484 | 639 | 514 | .745 | 221 | 476 | 275 | .7322 | 8 |
| 53 | 773 | 770 | 788 | .732 | 513 | 637 | 544 | .705 | 250 | 473 | 305 | .7044 | 7 |
| 54 | 802 | 768 | 817 | .669 | 542 | 635 | 573 | .664 | 279 | 470 | 334 | .6768 | 6 |
| 55 | .06831 | .99766 | .06847 | 14.666 | .08571 | .99632 | .08602 | 11.625 | .10308 | .99467 | .10363 | 9.6493 | 5 |
| 56 | 860 | 764 | 876 | .544 | 600 | 630 | 632 | .585 | 337 | 464 | 393 | .6220 | 4 |
| 57 | 889 | 762 | 905 | .482 | 629 | 627 | 661 | .546 | 366 | 461 | 422 | .5949 | 3 |
| 58 | 918 | 760 | 934 | .421 | 658 | 625 | 690 | .507 | 395 | 458 | 452 | .5679 | 2 |
| 59 | 947 | 758 | 963 | .361 | 687 | 622 | 720 | .468 | 424 | 455 | 481 | .5411 | 1 |
| 60 | .06976 | .99756 | .06993 | 14.301 | .08716 | .99619 | .08749 | 11.430 | .10453 | .99452 | .10510 | 9.5144 | 0 |

6°

7°

8°

| M. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | M. |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0 | .10453 | .99452 | .10510 | 9.5144 | .12187 | .99255 | .12278 | 8.1443 | .13917 | .99027 | .14054 | 7.1154 | 60 |
| 1 | 482 | 449 | 540 | .4878 | 216 | 251 | 308 | .1248 | 946 | 023 | 084 | .1004 | 59 |
| 2 | 511 | 446 | 569 | .4614 | 245 | 248 | 338 | .1054 | 975 | 019 | 113 | .0855 | 58 |
| 3 | 540 | 443 | 599 | .4352 | 274 | 244 | 367 | .0860 | .14004 | 015 | 143 | .0706 | 57 |
| 4 | 569 | 440 | 628 | .4090 | 302 | 240 | 397 | .0667 | 033 | 011 | 173 | .0558 | 56 |
| 5 | .10597 | .99437 | .10657 | 9.3831 | .12331 | .99237 | .12426 | 8.0476 | .14061 | .99006 | .14202 | 7.0410 | 55 |
| 6 | 626 | 434 | 687 | .3572 | 360 | 233 | 456 | .0285 | 090 | 002 | 232 | .0264 | 54 |
| 7 | 655 | 431 | 716 | .3315 | 389 | 230 | 485 | .0095 | 119 | .98998 | 262 | .0117 | 53 |
| 8 | 684 | 428 | 746 | .3060 | 418 | 226 | 515 | .79906 | 148 | 994 | 291 | 6.9972 | 52 |
| 9 | 713 | 424 | 775 | .2806 | 447 | 222 | 544 | .9718 | 177 | 990 | 321 | .9827 | 51 |
| 10 | .10742 | .99421 | .10805 | 9.2553 | .12476 | .99219 | .12574 | 7.9530 | .14205 | .98986 | .14351 | 6.9682 | 50 |
| 11 | 771 | 418 | 834 | .2302 | 504 | 215 | 603 | .9344 | 231 | 982 | 381 | .9538 | 49 |
| 12 | 800 | 415 | 863 | .2052 | 533 | 211 | 633 | .9158 | 263 | 978 | 410 | .9395 | 48 |
| 13 | 829 | 412 | 893 | .1803 | 562 | 208 | 662 | .8973 | 292 | 973 | 440 | .9242 | 47 |
| 14 | 858 | 409 | 922 | .1555 | 591 | 204 | 692 | .8789 | 320 | 969 | 470 | .9110 | 46 |
| 15 | .10887 | .99406 | .10952 | 9.1309 | .12620 | .99200 | .12722 | 7.8606 | .14349 | .98965 | .14499 | 6.8969 | 45 |
| 16 | 916 | 402 | 981 | .1065 | 649 | 197 | 751 | .8424 | 378 | 961 | 529 | .8828 | 44 |
| 17 | 945 | 399 | .11011 | .0821 | 678 | 193 | 781 | .8243 | 407 | 957 | 559 | .8687 | 43 |
| 18 | 973 | 396 | 040 | .0579 | 706 | 189 | 810 | .8062 | 436 | 953 | 588 | .8548 | 42 |
| 19 | .11002 | 393 | 070 | .0338 | 735 | 186 | 840 | .7882 | 464 | 948 | 618 | .8408 | 41 |
| 20 | .11031 | .99390 | .11099 | 9.0098 | .12764 | .99182 | .12869 | 7.7704 | .14493 | .98944 | .14648 | 6.8269 | 40 |
| 21 | 060 | 386 | 128 | 8.9860 | 793 | 178 | 899 | .7525 | 522 | 940 | 678 | .8131 | 39 |
| 22 | 089 | 383 | 158 | .9623 | 822 | 175 | 929 | .7348 | 551 | 936 | 707 | .7994 | 38 |
| 23 | 118 | 380 | 187 | .9387 | 851 | 171 | 958 | .7171 | 580 | 931 | 737 | .7856 | 37 |
| 24 | 147 | 377 | 217 | .9152 | 880 | 167 | 988 | .6996 | 608 | 927 | 767 | .7720 | 36 |
| 25 | .11176 | .99374 | .11246 | 8.8019 | .12908 | .99163 | .13017 | 7.6821 | .14637 | .98923 | .14796 | 6.7584 | 35 |
| 26 | 205 | 370 | 276 | .8686 | 937 | 160 | 047 | .6647 | 666 | 919 | 826 | .7448 | 34 |
| 27 | 234 | 367 | 305 | .8455 | 966 | 156 | 076 | .6473 | 695 | 914 | 856 | .7313 | 33 |
| 28 | 263 | 364 | 335 | .8225 | 995 | 152 | 106 | .6301 | 723 | 910 | 886 | .7179 | 32 |
| 29 | 291 | 360 | 364 | .7996 | .13024 | 148 | 136 | .6129 | 752 | 906 | 915 | .7045 | 31 |
| 30 | .11320 | .99357 | .11394 | 8.7769 | .13053 | .99144 | .13165 | 7.5958 | .14781 | .98902 | .14945 | 6.6912 | 30 |
| 31 | 349 | 354 | 423 | .7542 | 081 | 141 | 195 | .5787 | 810 | 897 | 975 | .6779 | 29 |
| 32 | 378 | 351 | 452 | .7317 | 110 | 137 | 224 | .5618 | 838 | 893 | .15005 | .6646 | 28 |
| 33 | 407 | 347 | 482 | .7093 | 139 | 133 | 254 | .5449 | 867 | 889 | 034 | .6514 | 27 |
| 34 | 436 | 344 | 511 | .6870 | 168 | 129 | 284 | .5281 | 896 | 884 | 064 | .6383 | 26 |
| 35 | .11465 | .99341 | .11541 | 8.6648 | .13197 | .99125 | .13313 | 7.5113 | .14925 | .98880 | .15094 | 6.6252 | 25 |
| 36 | 494 | 337 | 570 | .6427 | 226 | 122 | 343 | .4947 | 954 | 876 | 124 | .6122 | 24 |
| 37 | 523 | 334 | 600 | .6208 | 254 | 118 | 372 | .4781 | 982 | 871 | 153 | .5992 | 23 |
| 38 | 552 | 331 | 629 | .5989 | 283 | 114 | 402 | .4615 | .15011 | 867 | 183 | .5863 | 22 |
| 39 | 580 | 327 | 659 | .5772 | 312 | 110 | 432 | .4451 | 040 | 863 | 213 | .5734 | 21 |
| 40 | .11609 | .99324 | .11688 | 8.5555 | .13341 | .99106 | .13461 | 7.4287 | .15069 | .98858 | .15243 | 6.5606 | 20 |
| 41 | 638 | 320 | 718 | .5340 | 370 | 102 | 491 | .4124 | 097 | 854 | 272 | .5478 | 19 |
| 42 | 667 | 317 | 747 | .5126 | 399 | 098 | 521 | .3962 | 126 | 849 | 302 | .5350 | 18 |
| 43 | 696 | 314 | 777 | .4913 | 427 | 094 | 550 | .3800 | 155 | 845 | 332 | .5223 | 17 |
| 44 | 725 | 310 | 806 | .4701 | 456 | 091 | 580 | .3639 | 184 | 841 | 362 | .5097 | 16 |
| 45 | .11754 | .99307 | .11836 | 8.4490 | .13485 | .99087 | .13609 | 7.3479 | .15212 | .98836 | .15391 | 6.4971 | 15 |
| 46 | 783 | 303 | 865 | .4280 | 514 | 083 | 639 | .3319 | 241 | 832 | 421 | .4846 | 14 |
| 47 | 812 | 300 | 895 | .4071 | 543 | 079 | 669 | .3160 | 270 | 827 | 451 | .4721 | 13 |
| 48 | 840 | 297 | 924 | .3863 | 572 | 075 | 698 | .3002 | 299 | 823 | 481 | .4596 | 12 |
| 49 | 869 | 293 | 954 | .3656 | 600 | 071 | 728 | .2844 | 327 | 818 | 511 | .4472 | 11 |
| 50 | .11898 | .99290 | .11983 | 8.3450 | .13629 | .99067 | .13758 | 7.2687 | .15356 | .98814 | .15540 | 6.4348 | 10 |
| 51 | 927 | 286 | .12013 | .3245 | 658 | 063 | 787 | .2531 | 385 | 809 | 570 | .4225 | 9 |
| 52 | 956 | 283 | 042 | .3041 | 687 | 059 | 817 | .2375 | 414 | 805 | 600 | .4103 | 8 |
| 53 | 985 | 279 | 072 | .2838 | 716 | 055 | 846 | .2220 | 442 | 800 | 630 | .3980 | 7 |
| 54 | .12014 | 276 | 101 | .2636 | 744 | 051 | 876 | .2066 | 471 | 796 | 660 | .3859 | 6 |
| 55 | .12043 | .99272 | .12131 | 8.2434 | .13773 | .99047 | .13906 | 7.1912 | .15500 | .98791 | .15689 | 6.3737 | 5 |
| 56 | 071 | 269 | 160 | .2234 | 802 | 043 | 935 | .1759 | 529 | 787 | 719 | .3614 | 4 |
| 57 | 100 | 265 | 190 | .2035 | 831 | 039 | 965 | .1607 | 557 | 782 | 749 | .3496 | 3 |
| 58 | 129 | 262 | 219 | .1837 | 860 | 035 | 995 | .1455 | 586 | 778 | 779 | .3376 | 2 |
| 59 | 158 | 258 | 249 | .1640 | 889 | 031 | .14024 | .1304 | 615 | 773 | 809 | .3257 | 1 |
| 60 | .12187 | .99255 | .12278 | 8.1443 | .13917 | .99027 | .14054 | 7.1154 | .15643 | .98769 | .15838 | 6.3138 | 0 |
| | Cos. | Sin. | Cot. | Tan. | Cos. | Sin. | Cot. | Tan. | Cos. | Sin. | Cot. | Tan. | M. |

83°

82°

81°

NATURAL SINES, COSINES, TANGENTS, AND COTANGENTS.

9°

10°

11°

| M. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | M. |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0 | .15643 | .98769 | .15838 | 6.3138 | .17365 | .98481 | .17633 | 5.6713 | .19081 | .98163 | .19438 | 5.1446 | 60 |
| 1 | 672 | 764 | 868 | .3019 | 393 | 476 | 663 | .6617 | 109 | 157 | 468 | .1366 | 59 |
| 2 | 701 | 760 | 898 | .2901 | 422 | 471 | 693 | .6521 | 138 | 152 | 498 | .1286 | 58 |
| 3 | 730 | 755 | 928 | .2783 | 451 | 466 | 723 | .6425 | 167 | 146 | 529 | .1207 | 57 |
| 4 | 758 | 751 | 958 | .2666 | 479 | 461 | 753 | .6329 | 195 | 140 | 559 | .1128 | 56 |
| 5 | .15787 | .98746 | .15988 | 6.2549 | .17508 | .98455 | .17780 | 5.6234 | .19224 | .98135 | .19589 | 5.1049 | 55 |
| 6 | 816 | 741 | .16017 | .2432 | 537 | 450 | 813 | .6140 | 252 | 129 | 619 | .0970 | 54 |
| 7 | 845 | 737 | 047 | .2316 | 565 | 445 | 843 | .6045 | 281 | 124 | 649 | .0892 | 53 |
| 8 | 873 | 732 | 077 | .2200 | 594 | 440 | 873 | .5951 | 309 | 118 | 680 | .0814 | 52 |
| 9 | 902 | 728 | 107 | .2085 | 623 | 435 | 903 | .5857 | 338 | 112 | 710 | .0736 | 51 |
| 10 | .15931 | .98723 | .16137 | 6.1970 | .17651 | .98430 | .17933 | 5.5764 | .19366 | .98107 | .19740 | 5.0658 | 50 |
| 11 | 959 | 718 | 167 | .1856 | 680 | 425 | 963 | .5671 | 395 | 101 | 770 | .0581 | 49 |
| 12 | 988 | 714 | 196 | .1742 | 708 | 420 | 993 | .5578 | 423 | 096 | 801 | .0504 | 48 |
| 13 | .16017 | 709 | 226 | .1628 | 737 | 414 | .18023 | .5485 | 452 | 090 | 831 | .0427 | 47 |
| 14 | 046 | 704 | 256 | .1515 | 766 | 409 | 053 | .5393 | 481 | 084 | 861 | .0350 | 46 |
| 15 | .16074 | .98700 | .16286 | 6.1402 | .17794 | .98404 | .18083 | 5.5301 | .19509 | .98079 | .19891 | 5.0273 | 45 |
| 16 | 103 | 695 | 316 | .1290 | 823 | 399 | 113 | .5209 | 538 | 073 | 921 | .0197 | 44 |
| 17 | 132 | 690 | 346 | .1178 | 852 | 394 | 143 | .5118 | 566 | 067 | 952 | .0121 | 43 |
| 18 | 160 | 686 | 376 | .1066 | 880 | 389 | 173 | .5026 | 595 | 061 | 982 | .0045 | 42 |
| 19 | 189 | 681 | 405 | .0955 | 909 | 383 | 203 | .4936 | 623 | 056 | .20012 | 4.9969 | 41 |
| 20 | .16218 | .98676 | .16435 | 6.0844 | .17937 | .98378 | .18233 | 5.4845 | .19652 | .98050 | .20042 | 4.9894 | 40 |
| 21 | 246 | 671 | 465 | .0734 | 966 | 373 | 263 | .4755 | 680 | 044 | 073 | .9819 | 39 |
| 22 | 275 | 667 | 495 | .0624 | 995 | 368 | 293 | .4665 | 709 | 039 | 103 | .9744 | 38 |
| 23 | 304 | 662 | 525 | .0514 | .18023 | 362 | 323 | .4575 | 737 | 033 | 133 | .9669 | 37 |
| 24 | 333 | 657 | 555 | .0405 | 052 | 357 | 353 | .4486 | 766 | 027 | 164 | .9594 | 36 |
| 25 | .16361 | .98652 | .16585 | 6.0206 | .18081 | .98352 | .18384 | 5.4397 | .19794 | .98021 | .20194 | 4.9520 | 35 |
| 26 | 390 | 648 | 615 | .0188 | 109 | 347 | 414 | .4398 | 823 | 016 | 224 | .9446 | 34 |
| 27 | 419 | 643 | 645 | .0080 | 138 | 341 | 444 | .4219 | 851 | 010 | 254 | .9372 | 33 |
| 28 | 447 | 638 | 674 | .9972 | 166 | 336 | 474 | .4131 | 880 | 004 | 285 | .9298 | 32 |
| 29 | 476 | 633 | 704 | .9865 | 195 | 331 | 504 | .4043 | 908 | .97998 | 315 | .9225 | 31 |
| 30 | .16505 | .98629 | .16734 | 5.9758 | .18224 | .98325 | .18534 | 5.3955 | .19937 | .97992 | .20345 | 4.9152 | 30 |
| 31 | 533 | 624 | 764 | .9651 | 252 | 320 | 564 | .3868 | 965 | 987 | 376 | .9078 | 29 |
| 32 | 562 | 619 | 794 | .9545 | 281 | 315 | 594 | .3781 | 994 | 981 | 406 | .9006 | 28 |
| 33 | 591 | 614 | 824 | .9439 | 309 | 310 | 624 | .3694 | .20022 | 975 | 436 | .8933 | 27 |
| 34 | 620 | 609 | 854 | .9333 | 338 | 304 | 654 | .3607 | 051 | 969 | 466 | .8860 | 26 |
| 35 | .16648 | .98604 | .16884 | 5.9228 | .18367 | .98299 | .18684 | 5.3521 | .20079 | .97963 | .20497 | 4.8788 | 25 |
| 36 | 677 | 600 | 914 | .9124 | 395 | 294 | 714 | .3435 | 108 | 958 | 527 | .8716 | 24 |
| 37 | 706 | 595 | 944 | .9019 | 424 | 288 | 745 | .3349 | 136 | 952 | 557 | .8644 | 23 |
| 38 | 734 | 590 | 974 | .8915 | 452 | 283 | 775 | .3263 | 165 | 946 | 588 | .8573 | 22 |
| 39 | 763 | 585 | .17004 | .8811 | 481 | 277 | 805 | .3178 | 193 | 940 | 618 | .8501 | 21 |
| 40 | .16792 | .98580 | .17033 | 5.8708 | .18509 | .98272 | .18835 | 5.3093 | .20222 | .97934 | .20648 | 4.8430 | 20 |
| 41 | 820 | 575 | 063 | .8605 | 538 | 267 | 865 | .3008 | 250 | 928 | 679 | .8359 | 19 |
| 42 | 849 | 570 | 093 | .8502 | 567 | 261 | 895 | .2924 | 279 | 922 | 709 | .8288 | 18 |
| 43 | 878 | 565 | 123 | .8400 | 595 | 256 | 925 | .2839 | 307 | 916 | 739 | .8218 | 17 |
| 44 | 906 | 561 | 153 | .8298 | 624 | 250 | 955 | .2755 | 336 | 910 | 770 | .8147 | 16 |
| 45 | .16935 | .98556 | .17183 | 5.8197 | .18652 | .98245 | .18986 | 5.2672 | .20364 | .97905 | .20800 | 4.8077 | 15 |
| 46 | 964 | 551 | 213 | .8095 | 681 | 240 | .19016 | .2588 | 393 | 899 | 830 | .8007 | 14 |
| 47 | 992 | 546 | 243 | .7994 | 710 | 234 | 046 | .2505 | 421 | 893 | 861 | .7937 | 13 |
| 48 | .17021 | 541 | 273 | .7894 | 738 | 229 | 076 | .2422 | 450 | 887 | 891 | .7867 | 12 |
| 49 | 050 | 536 | 303 | .7794 | 767 | 223 | 106 | .2339 | 478 | 881 | 921 | .7798 | 11 |
| 50 | .17078 | .98531 | .17333 | 5.7694 | .18795 | .98218 | .19136 | 5.2257 | .20507 | .97875 | .20952 | 4.7729 | 10 |
| 51 | 107 | 526 | 393 | .7594 | 824 | 212 | 166 | .2174 | 535 | 869 | 982 | .7659 | 9 |
| 52 | 136 | 521 | 393 | .7495 | 852 | 207 | 197 | .2092 | 563 | 863 | .21013 | .7591 | 8 |
| 53 | 164 | 516 | 423 | .7396 | 881 | 201 | 227 | .2011 | 592 | 857 | 043 | .7522 | 7 |
| 54 | 193 | 511 | 453 | .7297 | 910 | 196 | 257 | .1929 | 620 | 851 | 073 | .7453 | 6 |
| 55 | .17222 | .98506 | .17483 | 5.7199 | .18938 | .98190 | .19287 | 5.1848 | .20649 | .97845 | .21104 | 4.7385 | 5 |
| 56 | 250 | 501 | 513 | .7101 | 967 | 185 | 317 | .1767 | 677 | 839 | 134 | .7317 | 4 |
| 57 | 279 | 496 | 543 | .7004 | 995 | 179 | 347 | .1686 | 706 | 833 | 164 | .7249 | 3 |
| 58 | 308 | 491 | 573 | .6906 | .19024 | 174 | 378 | .1606 | 734 | 827 | 195 | .7181 | 2 |
| 59 | 336 | 486 | 603 | .6809 | 052 | 168 | 408 | .1526 | 763 | 821 | 225 | .7114 | 1 |
| 60 | .17365 | .98481 | .17633 | 5.6713 | .19081 | .98163 | .19438 | 5.1446 | .20791 | .97815 | .21256 | 4.7046 | 0 |

80°

79°

78°

Cos. Sin. Cot. Tan. Cos. Sin. Cot. Tan. Cos. Sin. Cot. Tan. M.

12°

13°

14°

| M. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | M. |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0 | .20791 | .97815 | .21256 | 4.7046 | .22495 | .97437 | .23087 | 4.3315 | .24192 | .97030 | .24933 | 4.0108 | 60 |
| 1 | 820 | 809 | 286 | .6979 | 523 | 430 | 117 | .3257 | 220 | 023 | 904 | .0058 | 59 |
| 2 | 848 | 803 | 316 | .6912 | 552 | 424 | 148 | .3200 | 249 | 015 | 995 | .0009 | 58 |
| 3 | 877 | 797 | 347 | .6845 | 580 | 417 | 179 | .3143 | 277 | 008 | .25026 | 3.9959 | 57 |
| 4 | 905 | 791 | 377 | .6779 | 608 | 411 | 209 | .3086 | 305 | 001 | 056 | .9910 | 56 |
| 5 | .20933 | .97784 | .21408 | 4.6712 | .22637 | .97404 | .23240 | 4.3029 | .24333 | .96994 | .25087 | 3.9861 | 55 |
| 6 | 962 | 778 | 438 | .6646 | 665 | 398 | 271 | .2972 | 362 | 987 | 118 | .9812 | 54 |
| 7 | 990 | 772 | 469 | .6580 | 693 | 391 | 301 | .2916 | 390 | 980 | 149 | .9763 | 53 |
| 8 | .21019 | .9766 | .499 | .6514 | 722 | 384 | 332 | .2859 | 418 | 973 | 180 | .9714 | 52 |
| 9 | 047 | 760 | 529 | .6448 | 750 | 378 | 363 | .2803 | 446 | 966 | 211 | .9665 | 51 |
| 10 | .21076 | .97754 | .21560 | 4.6382 | .22778 | .97371 | .23393 | 4.2747 | .24474 | .96959 | .25242 | 3.9617 | 50 |
| 11 | 104 | 748 | 590 | .6317 | 807 | 365 | 424 | .2691 | 503 | 952 | 273 | .9568 | 49 |
| 12 | 132 | 742 | 621 | .6252 | 835 | 358 | 455 | .2635 | 531 | 945 | 304 | .9520 | 48 |
| 13 | 161 | 735 | 651 | .6187 | 863 | 351 | 485 | .2580 | 559 | 937 | 335 | .9471 | 47 |
| 14 | 189 | 729 | 682 | .6122 | 892 | 345 | 516 | .2524 | 587 | 930 | 366 | .9423 | 46 |
| 15 | .21218 | .97723 | .21712 | 4.6057 | .22920 | .97338 | .23547 | 4.2468 | .24615 | .96923 | .25397 | 3.9375 | 45 |
| 16 | 246 | 717 | 743 | .5993 | 948 | 331 | 578 | .2413 | 644 | 916 | 428 | .9327 | 44 |
| 17 | 275 | 711 | 773 | .5928 | 977 | 325 | 608 | .2358 | 672 | 909 | 459 | .9279 | 43 |
| 18 | 303 | 705 | 804 | .5864 | .23005 | 318 | 639 | .2303 | 700 | 902 | 490 | .9232 | 42 |
| 19 | 331 | 698 | 834 | .5800 | 033 | 311 | 670 | .2248 | 728 | 894 | 521 | .9184 | 41 |
| 20 | .21360 | .97692 | .21864 | 4.5736 | .23062 | .97304 | .23700 | 4.2193 | .24756 | .96887 | .25552 | 3.9136 | 40 |
| 21 | 388 | 686 | 895 | .5673 | 090 | 298 | 731 | .2139 | 784 | 880 | 583 | .9089 | 39 |
| 22 | 417 | 680 | 925 | .5609 | 118 | 291 | 762 | .2084 | 813 | 873 | 614 | .9042 | 38 |
| 23 | 445 | 673 | 956 | .5546 | 146 | 284 | 793 | .2030 | 841 | 866 | 645 | .8995 | 37 |
| 24 | 474 | 667 | 986 | .5483 | 175 | 278 | 823 | .1976 | 869 | 858 | 676 | .8947 | 36 |
| 25 | .21502 | .97661 | .22017 | 4.5420 | .23203 | .97271 | .23854 | 4.1922 | .24897 | .96851 | .25707 | 3.8900 | 35 |
| 26 | 530 | 655 | 047 | .5357 | 231 | 264 | 885 | .1868 | 925 | 844 | 738 | .8854 | 34 |
| 27 | 559 | 648 | 078 | .5294 | 260 | 257 | 916 | .1814 | 954 | 837 | 769 | .8807 | 33 |
| 28 | 587 | 642 | 108 | .5232 | 288 | 251 | 946 | .1760 | 982 | 829 | 800 | .8760 | 32 |
| 29 | 616 | 636 | 139 | .5169 | 316 | 244 | 977 | .1706 | .25010 | 822 | 831 | .8714 | 31 |
| 30 | .21644 | .97630 | .22169 | 4.5107 | .23345 | .97237 | .24008 | 4.1653 | .25038 | .96815 | .25862 | 3.8667 | 30 |
| 31 | 672 | 623 | 200 | .5045 | 373 | 230 | 039 | .1600 | 066 | 807 | 893 | .8621 | 29 |
| 32 | 701 | 617 | 231 | .4983 | 401 | 223 | 069 | .1547 | 094 | 800 | 924 | .8575 | 28 |
| 33 | 729 | 611 | 261 | .4922 | 429 | 217 | 100 | .1493 | 122 | 793 | 955 | .8528 | 27 |
| 34 | 758 | 604 | 292 | .4860 | 458 | 210 | 131 | .1441 | 151 | 786 | 986 | .8482 | 26 |
| 35 | .21786 | .97598 | .22322 | 4.4799 | .23486 | .97203 | .24162 | 4.1388 | .25179 | .96778 | .26017 | 3.8436 | 25 |
| 36 | 814 | 592 | 353 | .4737 | 514 | 196 | 193 | .1335 | 207 | 771 | 048 | .8391 | 24 |
| 37 | 843 | 585 | 383 | .4676 | 542 | 189 | 223 | .1282 | 235 | 764 | 079 | .8345 | 23 |
| 38 | 871 | 579 | 414 | .4615 | 571 | 182 | 254 | .1230 | 263 | 756 | 110 | .8299 | 22 |
| 39 | 899 | 573 | 444 | .4555 | 599 | 176 | 285 | .1178 | 291 | 749 | 141 | .8254 | 21 |
| 40 | .21928 | .97566 | .22475 | 4.4494 | .23627 | .97169 | .24316 | 4.1126 | .25320 | .96742 | .26172 | 3.8208 | 20 |
| 41 | 956 | 560 | 505 | .4434 | 656 | 162 | 347 | .1074 | 348 | 734 | 293 | .8163 | 19 |
| 42 | 985 | 553 | 536 | .4373 | 684 | 155 | 377 | .1022 | 376 | 727 | 325 | .8118 | 18 |
| 43 | .22013 | .97547 | .22567 | 4.4313 | 712 | 148 | 408 | .0970 | 404 | 719 | 356 | .8073 | 17 |
| 44 | 041 | 541 | 597 | .4253 | 740 | 141 | 439 | .0918 | 432 | 712 | 387 | .8028 | 16 |
| 45 | .22070 | .97534 | .22628 | 4.4194 | .23769 | .97134 | .24470 | 4.0867 | .25460 | .96705 | .26328 | 3.7983 | 15 |
| 46 | 098 | 528 | 658 | .4134 | 797 | 127 | 501 | .0815 | 488 | 697 | 359 | .7938 | 14 |
| 47 | 126 | 521 | 689 | .4075 | 825 | 120 | 532 | .0764 | 516 | 690 | 390 | .7893 | 13 |
| 48 | 155 | 515 | 719 | .4015 | 853 | 113 | 562 | .0713 | 545 | 682 | 421 | .7848 | 12 |
| 49 | 183 | 508 | 750 | .3956 | 882 | 106 | 593 | .0662 | 573 | 675 | 452 | .7804 | 11 |
| 50 | .22212 | .97502 | .22781 | 4.3897 | .23910 | .97100 | .24624 | 4.0611 | .25601 | .96667 | .26483 | 3.7760 | 10 |
| 51 | 240 | 496 | 811 | .3838 | 938 | 093 | 655 | .0560 | 629 | 660 | 515 | .7715 | 9 |
| 52 | 268 | 489 | 842 | .3779 | 966 | 086 | 686 | .0509 | 657 | 653 | 546 | .7671 | 8 |
| 53 | 297 | 483 | 872 | .3721 | 995 | 079 | 717 | .0459 | 685 | 645 | 577 | .7627 | 7 |
| 54 | 325 | 476 | 903 | .3662 | .24023 | 072 | 747 | .0408 | 713 | 638 | 608 | .7583 | 6 |
| 55 | .22353 | .97470 | .22934 | 4.3604 | .24051 | .97065 | .24778 | 4.0358 | .25741 | .96630 | .26639 | 3.7539 | 5 |
| 56 | 382 | 463 | 964 | .3546 | 079 | 058 | 809 | .0308 | 769 | 623 | 670 | .7495 | 4 |
| 57 | 410 | 457 | 995 | .3488 | 108 | 051 | 840 | .0257 | 798 | 615 | 701 | .7451 | 3 |
| 58 | 438 | 450 | .23026 | .3430 | 136 | 044 | 871 | .0207 | 826 | 608 | 733 | .7408 | 2 |
| 59 | 467 | 444 | 056 | .3372 | 164 | 037 | 902 | .0158 | 854 | 600 | 764 | .7364 | 1 |
| 60 | .22495 | .97437 | .23087 | 4.3315 | .24192 | .97030 | .24933 | 4.0108 | .25882 | .96593 | .26795 | 3.7321 | 0 |
| | Cos. | Sin. | Cot. | Tan. | Cos. | Sin. | Cot. | Tan. | Cos. | Sin. | Cot. | Tan. | M. |

77°

76°

75°

15°

16°

17°

| M. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | M. |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0 | .25882 | .96593 | .26795 | 3.7321 | .27564 | .96126 | .28675 | 3.4874 | .29237 | .95630 | .30573 | 3.2709 | 60 |
| 1 | 910 | 585 | 826 | .7277 | 592 | 118 | 706 | .4836 | 265 | 622 | 605 | .2675 | 59 |
| 2 | 938 | 578 | 857 | .7234 | 620 | 110 | 738 | .4798 | 293 | 613 | 637 | .2641 | 58 |
| 3 | 966 | 570 | 888 | .7191 | 648 | 102 | 769 | .4760 | 321 | 605 | 669 | .2607 | 57 |
| 4 | 994 | 562 | 920 | .7148 | 676 | 094 | 801 | .4722 | 348 | 596 | 700 | .2573 | 56 |
| 5 | .26022 | .96555 | .26951 | 3.7105 | .27704 | .96086 | .28832 | 3.4684 | .29376 | .95588 | .30732 | 3.2539 | 55 |
| 6 | 050 | 547 | 982 | .7062 | 731 | 078 | 864 | .4646 | 404 | 579 | 764 | .2506 | 54 |
| 7 | 079 | 540 | .27013 | .7019 | 759 | 070 | 895 | .4608 | 432 | 571 | 796 | .2472 | 53 |
| 8 | 107 | 532 | 044 | .6976 | 787 | 062 | 927 | .4570 | 460 | 562 | 828 | .2438 | 52 |
| 9 | 135 | 524 | 076 | .6933 | 815 | 054 | 958 | .4533 | 487 | 554 | 860 | .2405 | 51 |
| 10 | .26163 | .96517 | .27107 | 3.6891 | .27843 | .96046 | .28990 | 3.4495 | .29515 | .95545 | .30891 | 3.2371 | 50 |
| 11 | 191 | 509 | 138 | .6848 | 871 | 037 | .29021 | .4458 | 543 | 536 | 923 | .2338 | 49 |
| 12 | 219 | 502 | 169 | .6806 | 899 | 029 | 053 | .4420 | 571 | 528 | 955 | .2305 | 48 |
| 13 | 247 | 494 | 201 | .6764 | 927 | 021 | 084 | .4383 | 599 | 519 | 987 | .2272 | 47 |
| 14 | 275 | 486 | 232 | .6722 | 955 | 013 | 116 | .4346 | 626 | 511 | .31019 | .2238 | 46 |
| 15 | .26303 | .96479 | .27263 | 3.6680 | .27983 | .96005 | .29147 | 3.4308 | .29654 | .95502 | .31051 | 3.2205 | 45 |
| 16 | 331 | 471 | 294 | .6638 | .28011 | .95997 | 179 | .4271 | 682 | 493 | 083 | .2172 | 44 |
| 17 | 359 | 463 | 326 | .6596 | 039 | 989 | 210 | .4234 | 710 | 485 | 115 | .2139 | 43 |
| 18 | 387 | 456 | 357 | .6554 | 067 | 981 | 242 | .4197 | 737 | 476 | 147 | .2106 | 42 |
| 19 | 415 | 448 | 388 | .6512 | 095 | 972 | 274 | .4160 | 765 | 467 | 178 | .2073 | 41 |
| 20 | .26443 | .96440 | .27419 | 3.6470 | .28123 | .95964 | .29305 | 3.4124 | .29793 | .95459 | .31210 | 3.2041 | 40 |
| 21 | 471 | 433 | 451 | .6429 | 150 | 956 | 337 | .4087 | 821 | 450 | 242 | .2008 | 39 |
| 22 | 500 | 425 | 482 | .6387 | 178 | 948 | 368 | .4050 | 849 | 441 | 274 | .1975 | 38 |
| 23 | 528 | 417 | 513 | .6346 | 206 | 940 | 400 | .4014 | 876 | 433 | 306 | .1943 | 37 |
| 24 | 556 | 410 | 545 | .6305 | 234 | 931 | 432 | .3977 | 904 | 424 | 338 | .1910 | 36 |
| 25 | .26584 | .96402 | .27576 | 3.6264 | .28262 | .95923 | .29463 | 3.3941 | .29932 | .95415 | .31370 | 3.1878 | 35 |
| 26 | 612 | 394 | 607 | .6222 | 290 | 915 | 495 | .3904 | 960 | 407 | 402 | .1845 | 34 |
| 27 | 640 | 386 | 638 | .6181 | 318 | 907 | 526 | .3868 | 987 | 398 | 434 | .1813 | 33 |
| 28 | 668 | 379 | 670 | .6140 | 346 | 898 | 558 | .3832 | .30015 | 389 | 466 | .1780 | 32 |
| 29 | 696 | 371 | 701 | .6100 | 374 | 890 | 590 | .3796 | 043 | 380 | 498 | .1748 | 31 |
| 30 | .26724 | .96363 | .27732 | 3.6059 | .28402 | .95882 | .29621 | 3.3759 | .30071 | .95372 | .31530 | 3.1716 | 30 |
| 31 | 752 | 355 | 764 | .6018 | 429 | 874 | 653 | .3723 | 098 | 363 | 562 | .1684 | 29 |
| 32 | 780 | 347 | 795 | .5978 | 457 | 865 | 685 | .3687 | 126 | 354 | 594 | .1652 | 28 |
| 33 | 808 | 340 | 826 | .5937 | 485 | 857 | 716 | .3652 | 154 | 345 | 626 | .1620 | 27 |
| 34 | 836 | 332 | 858 | .5897 | 513 | 849 | 748 | .3616 | 182 | 337 | 658 | .1588 | 26 |
| 35 | .26864 | .96324 | .27889 | 3.5856 | .28541 | .95841 | .29780 | 3.3580 | .30209 | .95328 | .31690 | 3.1556 | 25 |
| 36 | 892 | 316 | 921 | .5816 | 569 | 832 | 811 | .3544 | 237 | 319 | 722 | .1524 | 24 |
| 37 | 920 | 308 | 952 | .5776 | 597 | 824 | 843 | .3509 | 265 | 310 | 754 | .1492 | 23 |
| 38 | 948 | 301 | 983 | .5736 | 625 | 816 | 875 | .3473 | 292 | 301 | 786 | .1460 | 22 |
| 39 | 976 | 293 | .28015 | .5696 | 652 | 807 | 906 | .3438 | 320 | 293 | 818 | .1429 | 21 |
| 40 | .27004 | .96285 | .28046 | 3.5656 | .28680 | .95799 | .29938 | 3.3402 | .30348 | .95284 | .31850 | 3.1397 | 20 |
| 41 | 032 | 277 | 077 | .5616 | 708 | 791 | 970 | .3367 | 376 | 275 | 882 | .1366 | 19 |
| 42 | 060 | 269 | 109 | .5576 | 736 | 782 | .30001 | .3332 | 403 | 266 | 914 | .1334 | 18 |
| 43 | 088 | 261 | 140 | .5536 | 764 | 774 | 033 | .3297 | 431 | 257 | 946 | .1303 | 17 |
| 44 | 116 | 253 | 172 | .5497 | 792 | 766 | 065 | .3261 | 459 | 248 | 978 | .1271 | 16 |
| 45 | .27144 | .96246 | .28203 | 3.5457 | .28820 | .95757 | .30097 | 3.3226 | .30486 | .95240 | .32010 | 3.1240 | 15 |
| 46 | 172 | 238 | 234 | .5418 | 847 | 749 | 128 | .3191 | 514 | 231 | 042 | .1209 | 14 |
| 47 | 200 | 230 | 266 | .5379 | 875 | 740 | 160 | .3156 | 542 | 222 | 074 | .1178 | 13 |
| 48 | 228 | 222 | 297 | .5339 | 903 | 732 | 192 | .3122 | 570 | 213 | 106 | .1146 | 12 |
| 49 | 256 | 214 | 329 | .5300 | 931 | 724 | 224 | .3087 | 597 | 204 | 139 | .1115 | 11 |
| 50 | .27284 | .96206 | .28360 | 3.5261 | .28959 | .95715 | .30255 | 3.3052 | .30625 | .95195 | .32171 | 3.1084 | 10 |
| 51 | 312 | 198 | 391 | .5222 | 987 | 707 | 287 | .3017 | 653 | 186 | 203 | .1053 | 9 |
| 52 | 340 | 190 | 423 | .5183 | .29015 | 698 | 319 | .2983 | 680 | 177 | 235 | .1022 | 8 |
| 53 | 368 | 182 | 454 | .5144 | 042 | 690 | 351 | .2948 | 708 | 168 | 267 | .0991 | 7 |
| 54 | 396 | 174 | 486 | .5105 | 070 | 681 | 382 | .2914 | 736 | 159 | 299 | .0961 | 6 |
| 55 | .27424 | .96166 | .28517 | 3.5067 | .29098 | .95673 | .30414 | 3.2879 | .30763 | .95150 | .32331 | 3.0930 | 5 |
| 56 | 452 | 158 | 549 | .5028 | 126 | 664 | 446 | .2845 | 791 | 142 | 363 | .0899 | 4 |
| 57 | 480 | 150 | 580 | .4989 | 154 | 656 | 478 | .2811 | 819 | 133 | 396 | .0868 | 3 |
| 58 | 508 | 142 | 612 | .4951 | 182 | 647 | 509 | .2777 | 846 | 124 | 428 | .0838 | 2 |
| 59 | 536 | 134 | 643 | .4912 | 209 | 639 | 541 | .2743 | 874 | 115 | 460 | .0807 | 1 |
| 60 | .27564 | .96126 | .28675 | 3.4874 | .29237 | .95630 | .30573 | 3.2709 | .30902 | .95106 | .32492 | 3.0777 | 0 |

74°

73°

72°

| M. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | M. |
|----|------|------|------|------|------|------|------|------|------|------|------|------|----|
|----|------|------|------|------|------|------|------|------|------|------|------|------|----|

| M. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | M. |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0 | .30902 | .95106 | .32492 | 3.0777 | .32557 | .94552 | .34433 | 2.9042 | .34202 | .93969 | .36397 | 2.7475 | 60 |
| 1 | 929 | 097 | 524 | .0746 | 584 | 542 | 465 | .9015 | 229 | 959 | 430 | .7450 | 59 |
| 2 | 957 | 088 | 556 | .0716 | 612 | 533 | 498 | .8987 | 257 | 949 | 463 | .7425 | 58 |
| 3 | 985 | 079 | 588 | .0686 | 639 | 523 | 530 | .8960 | 284 | 939 | 496 | .7400 | 57 |
| 4 | .31012 | 070 | 621 | .0655 | 667 | 514 | 563 | .8933 | 311 | 929 | 529 | .7376 | 56 |
| 5 | .31040 | .95061 | .32653 | 3.0625 | .32694 | .94504 | .34596 | 2.8905 | .34339 | .93919 | .36562 | 2.7351 | 55 |
| 6 | 068 | 052 | 685 | .0595 | 722 | 495 | 628 | .8878 | 366 | 909 | 595 | .7326 | 54 |
| 7 | 095 | 043 | 717 | .0565 | 749 | 485 | 661 | .8851 | 393 | 899 | 628 | .7302 | 53 |
| 8 | 123 | 033 | 749 | .0535 | 777 | 476 | 693 | .8824 | 421 | 889 | 661 | .7277 | 52 |
| 9 | 151 | 024 | 782 | .0505 | 804 | 466 | 726 | .8797 | 448 | 879 | 694 | .7253 | 51 |
| 10 | .31178 | .95015 | .32814 | 3.0475 | .32832 | .94457 | .34758 | 2.8770 | .34475 | .93869 | .36727 | 2.7228 | 50 |
| 11 | 206 | 006 | 846 | .0445 | 859 | 447 | 791 | .8743 | 503 | 859 | 760 | .7204 | 49 |
| 12 | 233 | .94997 | 878 | .0415 | 887 | 438 | 824 | .8716 | 530 | 849 | 793 | .7179 | 48 |
| 13 | 261 | 988 | 911 | .0385 | 914 | 428 | 856 | .8689 | 557 | 839 | 826 | .7155 | 47 |
| 14 | 289 | 979 | 943 | .0356 | 942 | 418 | 889 | .8662 | 584 | 829 | 859 | .7130 | 46 |
| 15 | .31316 | .94970 | .32975 | 3.0326 | .32969 | .94409 | .34922 | 2.8636 | .34612 | .93819 | .36892 | 2.7106 | 45 |
| 16 | 344 | 961 | .33007 | .0296 | 997 | 399 | 954 | .8609 | 639 | 809 | 925 | .7082 | 44 |
| 17 | 372 | 952 | 040 | .0267 | .33024 | 390 | 987 | .8582 | 666 | 799 | 958 | .7058 | 43 |
| 18 | 399 | 943 | 072 | .0237 | 051 | 380 | .35020 | .8556 | 694 | 789 | 991 | .7034 | 42 |
| 19 | 427 | 933 | 104 | .0208 | 079 | 370 | 052 | .8529 | 721 | 779 | .37024 | .7009 | 41 |
| 20 | .31454 | .94924 | .33136 | 3.0178 | .33106 | .94361 | .35085 | 2.8502 | .34748 | .93769 | .37057 | 2.6985 | 40 |
| 21 | 482 | 915 | 169 | .0149 | 134 | 351 | 118 | .8476 | 775 | 759 | 090 | .6961 | 39 |
| 22 | 510 | 906 | 201 | .0120 | 161 | 342 | 150 | .8449 | 803 | 748 | 123 | .6937 | 38 |
| 23 | 537 | 897 | 233 | .0090 | 189 | 332 | 183 | .8423 | 830 | 738 | 157 | .6913 | 37 |
| 24 | 565 | 888 | 266 | .0061 | 216 | 322 | 216 | .8397 | 857 | 728 | 190 | .6889 | 36 |
| 25 | .31593 | .94878 | .33298 | 3.0032 | .33244 | .94313 | .35248 | 2.8370 | .34884 | .93718 | .37223 | 2.6865 | 35 |
| 26 | 620 | 869 | 330 | .0003 | 271 | 303 | 281 | .8344 | 912 | 708 | 256 | .6841 | 34 |
| 27 | 648 | 860 | 363 | .29974 | 298 | 293 | 314 | .8318 | 939 | 698 | 289 | .6818 | 33 |
| 28 | 675 | 851 | 395 | .9945 | 326 | 284 | 346 | .8291 | 966 | 688 | 322 | .6794 | 32 |
| 29 | 703 | 842 | 427 | .9916 | 353 | 274 | 379 | .8265 | 993 | 677 | 355 | .6770 | 31 |
| 30 | .31730 | .94832 | .33460 | 2.9887 | .33381 | .94264 | .35412 | 2.8239 | .35021 | .93667 | .37388 | 2.6746 | 30 |
| 31 | 758 | 823 | 492 | .9858 | 408 | 254 | 445 | .8213 | 048 | 657 | 422 | .6723 | 29 |
| 32 | 786 | 814 | 524 | .9829 | 436 | 245 | 477 | .8187 | 075 | 647 | 455 | .6699 | 28 |
| 33 | 813 | 805 | 557 | .9800 | 463 | 235 | 510 | .8161 | 102 | 637 | 488 | .6675 | 27 |
| 34 | 841 | 795 | 589 | .9772 | 490 | 225 | 543 | .8135 | 130 | 626 | 521 | .6652 | 26 |
| 35 | .31868 | .94786 | .33621 | 2.9743 | .33518 | .94215 | .35576 | 2.8109 | .35157 | .93616 | .37554 | 2.6628 | 25 |
| 36 | 896 | 777 | 654 | .9714 | 545 | 206 | 608 | .8083 | 184 | 606 | 588 | .6605 | 24 |
| 37 | 923 | 768 | 686 | .9686 | 573 | 196 | 641 | .8057 | 211 | 596 | 621 | .6581 | 23 |
| 38 | 951 | 758 | 718 | .9657 | 600 | 186 | 674 | .8032 | 239 | 585 | 654 | .6558 | 22 |
| 39 | 979 | 749 | 751 | .9629 | 627 | 176 | 707 | .8006 | 266 | 575 | 687 | .6534 | 21 |
| 40 | .32006 | .94740 | .33783 | 2.9600 | .33655 | .94167 | .35740 | 2.7980 | .35293 | .93565 | .37720 | 2.6511 | 20 |
| 41 | 034 | 730 | 816 | .9572 | 682 | 157 | 772 | .7955 | 320 | 555 | 754 | .6488 | 19 |
| 42 | 061 | 721 | 848 | .9544 | 710 | 147 | 805 | .7929 | 347 | 544 | 787 | .6464 | 18 |
| 43 | 089 | 712 | 881 | .9515 | 737 | 137 | 838 | .7903 | 375 | 534 | 820 | .6441 | 17 |
| 44 | 116 | 702 | 913 | .9487 | 764 | 127 | 871 | .7878 | 402 | 524 | 853 | .6418 | 16 |
| 45 | .32144 | .94693 | .33945 | 2.9459 | .33792 | .94118 | .35904 | 2.7852 | .35429 | .93514 | .37887 | 2.6395 | 15 |
| 46 | 171 | 684 | 978 | .9431 | 819 | 108 | 937 | .7827 | 456 | 503 | 920 | .6371 | 14 |
| 47 | 199 | 674 | .34010 | .9403 | 846 | 098 | 969 | .7801 | 484 | 493 | 953 | .6348 | 13 |
| 48 | 227 | 665 | 043 | .9375 | 874 | 088 | .36002 | .7776 | 511 | 483 | 986 | .6325 | 12 |
| 49 | 254 | 656 | 075 | .9347 | 901 | 078 | 035 | .7751 | 538 | 472 | .38020 | .6302 | 11 |
| 50 | .32282 | .94646 | .34108 | 2.9319 | .33929 | .94068 | .36068 | 2.7725 | .35565 | .93462 | .38053 | 2.6279 | 10 |
| 51 | 309 | 637 | 140 | .9291 | 956 | 058 | 101 | .7700 | 592 | 452 | 086 | .6256 | 9 |
| 52 | 337 | 627 | 173 | .9263 | 983 | 049 | 134 | .7675 | 619 | 441 | 120 | .6233 | 8 |
| 53 | 364 | 618 | 205 | .9235 | .34011 | 039 | 167 | .7650 | 647 | 431 | 153 | .6210 | 7 |
| 54 | 392 | 609 | 238 | .9208 | 038 | 029 | 199 | .7625 | 674 | 420 | 186 | .6187 | 6 |
| 55 | .32419 | .94599 | .34270 | 2.9180 | .34065 | .94019 | .36232 | 2.7600 | .35701 | .93410 | .38220 | 2.6165 | 5 |
| 56 | 447 | 590 | 303 | .9152 | 093 | 009 | 265 | .7575 | 728 | 400 | 253 | .6142 | 4 |
| 57 | 474 | 580 | 335 | .9125 | 120 | .93999 | 298 | .7550 | 755 | 389 | 286 | .6119 | 3 |
| 58 | 502 | 571 | 368 | .9097 | 147 | 980 | 331 | .7525 | 782 | 379 | 320 | .6096 | 2 |
| 59 | 529 | 561 | 400 | .9070 | 175 | 979 | 364 | .7500 | 810 | 368 | 353 | .6074 | 1 |
| 60 | .32557 | .94552 | .34433 | 2.9042 | .34202 | .93969 | .36397 | 2.7475 | .35837 | .93358 | .38386 | 2.6051 | 0 |
| | Cos. | Sin. | Cot. | Tan. | Cos. | Sin. | Cot. | Tan. | Cos. | Sin. | Cot. | Tan. | M. |

21°

22°

23°

| M. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | M. |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0 | .35837 | .93358 | .38386 | 2.6051 | .37461 | .92718 | .40403 | 2.4751 | .39073 | .92050 | .42447 | 2.3559 | 60 |
| 1 | 864 | 348 | 420 | .6028 | 488 | 707 | 436 | .4730 | 100 | 039 | 482 | .3539 | 59 |
| 2 | 891 | 337 | 453 | .6006 | 515 | 697 | 470 | .4709 | 127 | 028 | 516 | .3520 | 58 |
| 3 | 918 | 327 | 487 | .5983 | 542 | 686 | 504 | .4689 | 153 | 016 | 551 | .3501 | 57 |
| 4 | 945 | 316 | 520 | .5961 | 569 | 675 | 538 | .4668 | 180 | 005 | 585 | .3483 | 56 |
| 5 | .35973 | .93306 | .38553 | 2.5938 | .37595 | .92664 | .40572 | 2.4648 | .39207 | .91994 | .42619 | 2.3464 | 55 |
| 6 | .36000 | .295 | 587 | .5916 | 622 | 653 | 606 | .4627 | 234 | 982 | 654 | .3445 | 54 |
| 7 | 027 | 285 | 620 | .5893 | 649 | 642 | 640 | .4606 | 260 | 971 | 688 | .3426 | 53 |
| 8 | 054 | 274 | 654 | .5871 | 676 | 631 | 674 | .4586 | 287 | 959 | 722 | .3407 | 52 |
| 9 | 081 | 264 | 687 | .5848 | 703 | 620 | 707 | .4566 | 314 | 948 | 757 | .3388 | 51 |
| 10 | .36108 | .93253 | .38721 | 2.5826 | .37730 | .92609 | .40741 | 2.4545 | .39341 | .91936 | .42791 | 2.3369 | 50 |
| 11 | 135 | 243 | 754 | .5804 | 757 | 598 | 775 | .4525 | 367 | 925 | 826 | .3351 | 49 |
| 12 | 162 | 232 | 787 | .5782 | 784 | 587 | 809 | .4504 | 394 | 914 | 860 | .3332 | 48 |
| 13 | 190 | 222 | 821 | .5759 | 811 | 576 | 843 | .4484 | 421 | 902 | 894 | .3313 | 47 |
| 14 | 217 | 211 | 854 | .5737 | 838 | 565 | 877 | .4464 | 448 | 891 | 929 | .3294 | 46 |
| 15 | .36244 | .93201 | .38888 | 2.5715 | .37865 | .92554 | .40911 | 2.4443 | .39474 | .91879 | .42963 | 2.3276 | 45 |
| 16 | 271 | 190 | 921 | .5693 | 892 | 543 | 945 | .4423 | 501 | 868 | 998 | .3257 | 44 |
| 17 | 298 | 180 | 955 | .5671 | 919 | 532 | 979 | .4403 | 528 | 856 | .43032 | .3238 | 43 |
| 18 | 325 | 169 | 988 | .5649 | 946 | 521 | .41013 | .4383 | 555 | 845 | 067 | .3220 | 42 |
| 19 | 352 | 159 | .39022 | .5627 | 973 | 510 | 047 | .4362 | 581 | 833 | 101 | .3201 | 41 |
| 20 | .36379 | .93148 | .39055 | 2.5605 | .37999 | .92499 | .41081 | 2.4342 | .39608 | .91822 | .43136 | 2.3183 | 40 |
| 21 | 406 | 137 | 089 | .5583 | .38026 | 488 | 115 | .4322 | 635 | 810 | 170 | .3164 | 39 |
| 22 | 434 | 127 | 122 | .5561 | 053 | 477 | 149 | .4302 | 661 | 799 | 205 | .3146 | 38 |
| 23 | 461 | 116 | 156 | .5539 | 080 | 466 | 183 | .4282 | 688 | 787 | 239 | .3127 | 37 |
| 24 | 488 | 106 | 190 | .5517 | 107 | 455 | 217 | .4262 | 715 | 775 | 274 | .3109 | 36 |
| 25 | .36515 | .93095 | .39223 | 2.5495 | .38134 | .92444 | .41251 | 2.4242 | .39741 | .91764 | .43308 | 2.3090 | 35 |
| 26 | 542 | 084 | 257 | .5473 | 161 | 432 | 285 | .4222 | 768 | 752 | 343 | .3072 | 34 |
| 27 | 569 | 074 | 290 | .5452 | 188 | 421 | 319 | .4202 | 795 | 741 | 378 | .3053 | 33 |
| 28 | 596 | 063 | 324 | .5430 | 215 | 410 | 353 | .4182 | 822 | 729 | 412 | .3035 | 32 |
| 29 | 623 | 052 | 357 | .5408 | 241 | 399 | 387 | .4162 | 848 | 718 | 447 | .3017 | 31 |
| 30 | .36650 | .93042 | .39391 | 2.5386 | .38268 | .92388 | .41421 | 2.4142 | .39875 | .91706 | .43481 | 2.2998 | 30 |
| 31 | 677 | 031 | 425 | .5365 | 295 | 377 | 455 | .4122 | 902 | 694 | 516 | .2980 | 29 |
| 32 | 704 | 020 | 458 | .5343 | 322 | 366 | 490 | .4102 | 928 | 683 | 550 | .2962 | 28 |
| 33 | 731 | 010 | 492 | .5322 | 349 | 355 | 524 | .4083 | 955 | 671 | 585 | .2944 | 27 |
| 34 | 758 | .92999 | 526 | .5300 | 376 | 343 | 558 | .4063 | 982 | 660 | 620 | .2925 | 26 |
| 35 | .36785 | .92988 | .39559 | 2.5279 | .38403 | .92332 | .41592 | 2.4043 | .40008 | .91648 | .43654 | 2.2907 | 25 |
| 36 | 812 | 978 | 593 | .5257 | 430 | 321 | 626 | .4023 | 035 | 636 | 689 | .2889 | 24 |
| 37 | 839 | 967 | 626 | .5236 | 456 | 310 | 660 | .4004 | 062 | 625 | 724 | .2871 | 23 |
| 38 | 867 | 956 | 660 | .5214 | 483 | 299 | 694 | .3984 | 088 | 613 | 758 | .2853 | 22 |
| 39 | 894 | 945 | 694 | .5193 | 510 | 287 | 728 | .3964 | 115 | 601 | 793 | .2835 | 21 |
| 40 | .36921 | .92935 | .39727 | 2.5172 | .38537 | .92276 | .41763 | 2.3945 | .40141 | .91590 | .43828 | 2.2817 | 20 |
| 41 | 948 | 924 | 761 | .5150 | 564 | 265 | 797 | .3925 | 168 | 578 | 862 | .2799 | 19 |
| 42 | 975 | 913 | 795 | .5129 | 591 | 254 | 831 | .3906 | 195 | 566 | 897 | .2781 | 18 |
| 43 | .37002 | 902 | 829 | .5108 | 617 | 243 | 865 | .3886 | 221 | 555 | 932 | .2763 | 17 |
| 44 | 029 | 892 | 862 | .5086 | 644 | 231 | 899 | .3867 | 248 | 543 | 966 | .2745 | 16 |
| 45 | .37056 | .92881 | .39806 | 2.5065 | .38671 | .92220 | .41933 | 2.3847 | .40275 | .91531 | .44001 | 2.2727 | 15 |
| 46 | 083 | 870 | 930 | .5044 | 698 | 209 | 968 | .3828 | 301 | 519 | 036 | .2709 | 14 |
| 47 | 110 | 859 | 963 | .5023 | 725 | 198 | .42002 | .3808 | 328 | 508 | 071 | .2691 | 13 |
| 48 | 137 | 849 | 997 | .5002 | 752 | 186 | 036 | .3789 | 355 | 496 | 105 | .2673 | 12 |
| 49 | 164 | 838 | .40031 | .4981 | 778 | 175 | 070 | .3770 | 381 | 484 | 140 | .2655 | 11 |
| 50 | .37191 | .92827 | .40065 | 2.4960 | .38865 | .92164 | .42105 | 2.3750 | .40408 | .91472 | .44175 | 2.2637 | 10 |
| 51 | 218 | 816 | 098 | .4939 | 832 | 152 | 139 | .3731 | 434 | 461 | 210 | .2620 | 9 |
| 52 | 245 | 805 | 132 | .4918 | 859 | 141 | 173 | .3712 | 461 | 449 | 244 | .2602 | 8 |
| 53 | 272 | 794 | 166 | .4897 | 886 | 130 | 207 | .3693 | 488 | 437 | 279 | .2584 | 7 |
| 54 | 299 | 784 | 200 | .4876 | 912 | 119 | 242 | .3673 | 514 | 425 | 314 | .2566 | 6 |
| 55 | .37326 | .92773 | .40234 | 2.4855 | .38939 | .92107 | .42276 | 2.3654 | .40541 | .91414 | .44349 | 2.2549 | 5 |
| 56 | 353 | 762 | 267 | .4834 | 966 | 096 | 310 | .3635 | 567 | 402 | 384 | .2531 | 4 |
| 57 | 380 | 751 | 301 | .4813 | 993 | 085 | 345 | .3616 | 594 | 390 | 418 | .2513 | 3 |
| 58 | 407 | 740 | 335 | .4792 | .39020 | 073 | 379 | .3597 | 621 | 378 | 453 | .2496 | 2 |
| 59 | 434 | 729 | 369 | .4772 | 046 | 062 | 413 | .3578 | 647 | 366 | 488 | .2478 | 1 |
| 60 | .37461 | .92718 | .40403 | 2.4751 | .39073 | .92050 | .42447 | 2.3559 | .40674 | .91355 | .44523 | 2.2460 | 0 |
| | Cos. | Sin. | Cot. | Tan. | Cos. | Sin. | Cot. | Tan. | Cos. | Sin. | Cot. | Tan. | M. |

24°

25°

26°

| M. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | M. |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0 | .40674 | .91355 | .44523 | 2.2460 | .42262 | .90631 | .46631 | 2.1445 | .43837 | .89879 | .48773 | 2.0503 | 60 |
| 1 | 700 | 343 | 558 | .2443 | 288 | 618 | 666 | .1429 | 863 | 867 | 809 | .0488 | 59 |
| 2 | 727 | 331 | 593 | .2425 | 315 | 606 | 702 | .1413 | 889 | 854 | 845 | .0473 | 58 |
| 3 | 753 | 319 | 627 | .2408 | 341 | 594 | 737 | .1396 | 916 | 841 | 881 | .0458 | 57 |
| 4 | 780 | 307 | 662 | .2390 | 367 | 582 | 773 | .1380 | 942 | 828 | 917 | .0443 | 56 |
| 5 | .40806 | .91295 | .44697 | 2.2373 | .42394 | .90560 | .46808 | 2.1364 | .43968 | .89816 | .48953 | 2.0428 | 55 |
| 6 | 833 | 283 | 732 | .2355 | 420 | 557 | 843 | .1348 | 994 | 803 | 989 | .0413 | 54 |
| 7 | 860 | 272 | 767 | .2338 | 446 | 545 | 879 | .1332 | .44020 | 790 | .49026 | .0398 | 53 |
| 8 | 886 | 260 | 802 | .2320 | 473 | 532 | 914 | .1315 | 046 | 777 | 062 | .0383 | 52 |
| 9 | 913 | 248 | 837 | .2303 | 499 | 520 | 950 | .1299 | 072 | 704 | 098 | .0368 | 51 |
| 10 | .40939 | .91236 | .44872 | 2.2286 | .42525 | .90507 | .46985 | 2.1283 | .44098 | .89752 | .49134 | 2.0353 | 50 |
| 11 | 966 | 224 | 907 | .2268 | 552 | 495 | .47021 | .1267 | 124 | 739 | 170 | .0338 | 49 |
| 12 | 992 | 212 | 942 | .2251 | 578 | 483 | 056 | .1251 | 151 | 726 | 206 | .0323 | 48 |
| 13 | .41019 | 200 | 977 | .2234 | 604 | 470 | 092 | .1235 | 177 | 713 | 242 | .0308 | 47 |
| 14 | 045 | 188 | .45012 | .2216 | 631 | 458 | 128 | .1219 | 203 | 700 | 278 | .0293 | 46 |
| 15 | .41072 | .91176 | .45047 | 2.2199 | .42657 | .90446 | .47163 | 2.1203 | .44229 | .89687 | .49315 | 2.0278 | 45 |
| 16 | 098 | 164 | 082 | .2182 | 683 | 433 | 199 | .1187 | 255 | 674 | 351 | .0263 | 44 |
| 17 | 125 | 152 | 117 | .2165 | 709 | 421 | 234 | .1171 | 281 | 662 | 387 | .0248 | 43 |
| 18 | 151 | 140 | 152 | .2148 | 736 | 408 | 270 | .1155 | 307 | 649 | 423 | .0233 | 42 |
| 19 | 178 | 128 | 187 | .2130 | 762 | 396 | 305 | .1139 | 333 | 636 | 459 | .0219 | 41 |
| 20 | .41204 | .91116 | .45222 | 2.2113 | .42788 | .90383 | .47341 | 2.1123 | .44359 | .89623 | .49495 | 2.0204 | 40 |
| 21 | 231 | 104 | 257 | .2096 | 815 | 371 | 377 | .1107 | 385 | 610 | 532 | .0189 | 39 |
| 22 | 257 | 092 | 292 | .2079 | 841 | 358 | 412 | .1092 | 411 | 597 | 568 | .0174 | 38 |
| 23 | 284 | 080 | 327 | .2062 | 867 | 346 | 448 | .1076 | 437 | 584 | 604 | .0160 | 37 |
| 24 | 310 | 068 | 362 | .2045 | 894 | 334 | 483 | .1060 | 464 | 571 | 640 | .0145 | 36 |
| 25 | .41337 | .91056 | .45397 | 2.2028 | .42920 | .90321 | .47519 | 2.1044 | .44490 | .89558 | .49677 | 2.0130 | 35 |
| 26 | 363 | 044 | 432 | .2011 | 946 | 309 | 555 | .1028 | 516 | 545 | 713 | .0115 | 34 |
| 27 | 390 | 032 | 467 | .1994 | 972 | 296 | 590 | .1013 | 542 | 532 | 749 | .0101 | 33 |
| 28 | 416 | 020 | 502 | .1977 | 999 | 284 | 626 | .0997 | 568 | 519 | 786 | .0086 | 32 |
| 29 | 443 | 008 | 538 | .1960 | .43025 | 271 | 662 | .0981 | 594 | 506 | 822 | .0072 | 31 |
| 30 | .41469 | .90996 | .45573 | 2.1943 | .43051 | .90259 | .47698 | 2.0965 | .44620 | .89493 | .49858 | 2.0057 | 30 |
| 31 | 496 | 984 | 608 | .1926 | 077 | 246 | 733 | .0950 | 646 | 480 | 804 | .0042 | 29 |
| 32 | 522 | 972 | 643 | .1909 | 104 | 233 | 769 | .0934 | 672 | 467 | 931 | .0028 | 28 |
| 33 | 549 | 960 | 678 | .1892 | 130 | 221 | 805 | .0918 | 698 | 454 | 967 | .0013 | 27 |
| 34 | 575 | 948 | 713 | .1876 | 156 | 208 | 840 | .0903 | 724 | 441 | .50004 | 1.0000 | 26 |
| 35 | .41602 | .90936 | .45748 | 2.1859 | .43182 | .90196 | .47876 | 2.0887 | .44750 | .89428 | .50040 | 1.9984 | 25 |
| 36 | 628 | 924 | 784 | .1842 | 209 | 183 | 912 | .0872 | 776 | 415 | 076 | .9970 | 24 |
| 37 | 655 | 911 | 819 | .1825 | 235 | 171 | 948 | .0856 | 802 | 402 | 113 | .9955 | 23 |
| 38 | 681 | 899 | 854 | .1808 | 261 | 158 | 984 | .0840 | 828 | 389 | 149 | .9942 | 22 |
| 39 | 707 | 887 | 889 | .1792 | 287 | 146 | .48019 | .0825 | 854 | 376 | 185 | .9926 | 21 |
| 40 | .41734 | .90875 | .45924 | 2.1775 | .43313 | .90133 | .48055 | 2.0809 | .44880 | .89363 | .50222 | 1.9912 | 20 |
| 41 | 760 | 863 | 960 | .1758 | 340 | 120 | 091 | .0794 | 906 | 350 | 258 | .9897 | 19 |
| 42 | 787 | 851 | 995 | .1742 | 366 | 108 | 127 | .0778 | 932 | 337 | 295 | .9883 | 18 |
| 43 | 813 | 839 | .46030 | .1725 | 392 | 095 | 163 | .0763 | 958 | 324 | 331 | .9868 | 17 |
| 44 | 840 | 826 | 065 | .1708 | 418 | 082 | 198 | .0748 | 984 | 311 | 368 | .9854 | 16 |
| 45 | .41866 | .90814 | .46101 | 2.1692 | .43445 | .90070 | .48234 | 2.0732 | .45010 | .89298 | .50404 | 1.9840 | 15 |
| 46 | 892 | 802 | 136 | .1675 | 471 | 057 | 270 | .0717 | 036 | 285 | 441 | .9825 | 14 |
| 47 | 919 | 790 | 171 | .1659 | 497 | 045 | 306 | .0701 | 062 | 272 | 477 | .9811 | 13 |
| 48 | 945 | 778 | 206 | .1642 | 523 | 032 | 342 | .0686 | 088 | 259 | 514 | .9797 | 12 |
| 49 | 972 | 766 | 242 | .1625 | 549 | 019 | 378 | .0671 | 114 | 245 | 550 | .9782 | 11 |
| 50 | .41998 | .90753 | .46277 | 2.1609 | .43575 | .90007 | .48414 | 2.0655 | .45140 | .89232 | .50587 | 1.9768 | 10 |
| 51 | .42024 | 741 | 312 | .1592 | 602 | .89994 | 450 | .0640 | 166 | 219 | 623 | .9754 | 9 |
| 52 | 051 | 729 | 348 | .1576 | 628 | 981 | 486 | .0625 | 192 | 206 | 660 | .9740 | 8 |
| 53 | 077 | 717 | 383 | .1560 | 654 | 968 | 521 | .0609 | 218 | 193 | 696 | .9725 | 7 |
| 54 | 104 | 704 | 418 | .1543 | 680 | 956 | 557 | .0594 | 243 | 180 | 733 | .9711 | 6 |
| 55 | .42130 | .90692 | .46454 | 2.1527 | .43706 | .89943 | .48593 | 2.0579 | .45269 | .89167 | .50769 | 1.9697 | 5 |
| 56 | 156 | 680 | 489 | .1510 | 733 | 930 | 629 | .0564 | 295 | 153 | 806 | .9683 | 4 |
| 57 | 183 | 668 | 525 | .1494 | 759 | 918 | 665 | .0549 | 321 | 140 | 843 | .9669 | 3 |
| 58 | 209 | 655 | 560 | .1478 | 785 | 905 | 701 | .0533 | 347 | 127 | 879 | .9654 | 2 |
| 59 | 235 | 643 | 595 | .1461 | 811 | 892 | 737 | .0518 | 373 | 114 | 916 | .9640 | 1 |
| 60 | .42262 | .90631 | .46631 | 2.1445 | .43837 | .89879 | .48773 | 2.0503 | .45399 | .89101 | .50953 | 1.9626 | 0 |

65°

64°

63°

| Cos. | Sin. | Cot. | Tan. | Cos. | Sin. | Cot. | Tan. | Cos. | Sin. | Cot. | Tan. | M. |
|------|------|------|------|------|------|------|------|------|------|------|------|----|
|------|------|------|------|------|------|------|------|------|------|------|------|----|

27°

28°

29°

| M. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0 | .45399 | .89101 | .50953 | 1.9626 | .46947 | .88295 | .53171 | 1.8807 | .48481 | .87462 | .55431 | 1.8040 | 60 |
| 1 | .425 | .879 | .50989 | .9612 | .473 | .881 | .53208 | .8794 | .487 | .875 | .554 | .8028 | 59 |
| 2 | .451 | .874 | .51026 | .9598 | .479 | .880 | .53246 | .8781 | .490 | .876 | .554 | .8016 | 58 |
| 3 | .477 | .861 | .5063 | .9584 | .47024 | .87924 | .53283 | .8768 | .493 | .874 | .554 | .8003 | 57 |
| 4 | .503 | .848 | .5099 | .9570 | .47050 | .87850 | .53320 | .8755 | .496 | .872 | .554 | .7991 | 56 |
| 5 | .45529 | .89035 | .51136 | 1.9556 | .47076 | .88226 | .53358 | 1.8741 | .48608 | .87391 | .55621 | 1.7979 | 55 |
| 6 | .554 | .821 | .173 | .9542 | .47101 | .88158 | .53395 | .8728 | .489 | .872 | .556 | .7966 | 54 |
| 7 | .580 | .808 | .209 | .9528 | .47127 | .88089 | .53432 | .8715 | .492 | .870 | .556 | .7954 | 53 |
| 8 | .606 | .88995 | .246 | .9514 | .47153 | .88020 | .53470 | .8702 | .495 | .868 | .556 | .7942 | 52 |
| 9 | .632 | .881 | .283 | .9500 | .47178 | .87951 | .53507 | .8689 | .498 | .866 | .556 | .7930 | 51 |
| 10 | .45658 | .88968 | .51319 | 1.9486 | .47204 | .88158 | .53545 | 1.8676 | .48735 | .87321 | .55812 | 1.7917 | 50 |
| 11 | .684 | .955 | .356 | .9472 | .47229 | .88089 | .53582 | .8663 | .490 | .871 | .558 | .7905 | 49 |
| 12 | .710 | .942 | .393 | .9458 | .47255 | .88020 | .53620 | .8650 | .493 | .869 | .558 | .7893 | 48 |
| 13 | .736 | .928 | .430 | .9444 | .47281 | .87951 | .53657 | .8637 | .496 | .867 | .558 | .7881 | 47 |
| 14 | .762 | .915 | .467 | .9430 | .47306 | .87882 | .53694 | .8624 | .499 | .865 | .558 | .7868 | 46 |
| 15 | .45787 | .88902 | .51503 | 1.9416 | .47332 | .88089 | .53732 | 1.8611 | .48862 | .87250 | .56003 | 1.7856 | 45 |
| 16 | .813 | .888 | .540 | .9402 | .47358 | .88020 | .53769 | .8598 | .491 | .870 | .560 | .7844 | 44 |
| 17 | .839 | .875 | .577 | .9388 | .47383 | .87951 | .53807 | .8585 | .494 | .868 | .560 | .7832 | 43 |
| 18 | .865 | .862 | .614 | .9375 | .47409 | .87882 | .53844 | .8572 | .497 | .866 | .560 | .7820 | 42 |
| 19 | .891 | .848 | .651 | .9361 | .47434 | .87813 | .53882 | .8559 | .500 | .864 | .560 | .7808 | 41 |
| 20 | .45917 | .88835 | .51688 | 1.9347 | .47460 | .88020 | .53920 | 1.8546 | .48989 | .87178 | .56194 | 1.7796 | 40 |
| 21 | .942 | .822 | .724 | .9333 | .47486 | .88089 | .53957 | .8533 | .492 | .862 | .561 | .7783 | 39 |
| 22 | .968 | .808 | .761 | .9319 | .47511 | .87951 | .53995 | .8520 | .495 | .860 | .561 | .7771 | 38 |
| 23 | .994 | .795 | .798 | .9306 | .47537 | .87882 | .54032 | .8507 | .498 | .858 | .561 | .7759 | 37 |
| 24 | .46020 | .782 | .835 | .9292 | .47562 | .87813 | .54070 | .8495 | .501 | .856 | .561 | .7747 | 36 |
| 25 | .46046 | .88768 | .51872 | 1.9278 | .47588 | .87951 | .54107 | 1.8482 | .49116 | .87107 | .56385 | 1.7735 | 35 |
| 26 | .072 | .755 | .909 | .9265 | .47614 | .88089 | .54145 | .8469 | .494 | .869 | .563 | .7723 | 34 |
| 27 | .097 | .741 | .946 | .9251 | .47639 | .88020 | .54183 | .8456 | .497 | .867 | .563 | .7711 | 33 |
| 28 | .123 | .728 | .983 | .9237 | .47665 | .87951 | .54220 | .8443 | .500 | .865 | .563 | .7699 | 32 |
| 29 | .149 | .715 | .52020 | .9223 | .47690 | .87882 | .54258 | .8430 | .503 | .863 | .563 | .7687 | 31 |
| 30 | .46175 | .88701 | .52057 | 1.9210 | .47716 | .87813 | .54296 | 1.8418 | .49242 | .87036 | .56577 | 1.7675 | 30 |
| 31 | .201 | .688 | .094 | .9196 | .47741 | .88089 | .54333 | .8405 | .495 | .861 | .565 | .7663 | 29 |
| 32 | .226 | .674 | .131 | .9183 | .47767 | .88020 | .54371 | .8392 | .498 | .859 | .565 | .7651 | 28 |
| 33 | .252 | .661 | .168 | .9169 | .47793 | .87951 | .54409 | .8379 | .501 | .857 | .565 | .7639 | 27 |
| 34 | .278 | .647 | .205 | .9155 | .47818 | .87882 | .54446 | .8367 | .504 | .855 | .565 | .7627 | 26 |
| 35 | .46304 | .88634 | .52242 | 1.9142 | .47844 | .87813 | .54484 | 1.8354 | .49369 | .86964 | .56769 | 1.7615 | 25 |
| 36 | .330 | .620 | .279 | .9128 | .47869 | .88089 | .54522 | .8341 | .496 | .853 | .567 | .7603 | 24 |
| 37 | .355 | .607 | .316 | .9115 | .47895 | .88020 | .54560 | .8329 | .499 | .851 | .567 | .7591 | 23 |
| 38 | .381 | .593 | .353 | .9101 | .47920 | .87951 | .54597 | .8316 | .502 | .849 | .567 | .7579 | 22 |
| 39 | .407 | .580 | .390 | .9088 | .47946 | .87882 | .54635 | .8303 | .505 | .847 | .567 | .7567 | 21 |
| 40 | .46433 | .88566 | .52427 | 1.9074 | .47971 | .87813 | .54673 | 1.8291 | .49495 | .86892 | .56962 | 1.7556 | 20 |
| 41 | .458 | .553 | .464 | .9061 | .47997 | .88089 | .54711 | .8278 | .497 | .851 | .569 | .7544 | 19 |
| 42 | .484 | .539 | .501 | .9047 | .48022 | .88020 | .54748 | .8265 | .500 | .849 | .569 | .7532 | 18 |
| 43 | .510 | .526 | .538 | .9034 | .48048 | .87951 | .54786 | .8253 | .503 | .847 | .569 | .7520 | 17 |
| 44 | .536 | .512 | .575 | .9020 | .48073 | .87882 | .54824 | .8240 | .506 | .845 | .569 | .7508 | 16 |
| 45 | .46561 | .88499 | .52613 | 1.9007 | .48099 | .87813 | .54862 | 1.8228 | .49622 | .86820 | .57155 | 1.7496 | 15 |
| 46 | .587 | .485 | .650 | .8993 | .48124 | .88089 | .54900 | .8215 | .509 | .843 | .569 | .7485 | 14 |
| 47 | .613 | .472 | .687 | .8980 | .48150 | .88020 | .54938 | .8202 | .512 | .841 | .569 | .7473 | 13 |
| 48 | .639 | .458 | .724 | .8967 | .48175 | .87951 | .54975 | .8190 | .515 | .839 | .569 | .7461 | 12 |
| 49 | .664 | .445 | .761 | .8953 | .48201 | .87882 | .55013 | .8177 | .518 | .837 | .569 | .7449 | 11 |
| 50 | .46690 | .88431 | .52798 | 1.8940 | .48226 | .87813 | .55051 | 1.8165 | .49748 | .86748 | .57348 | 1.7437 | 10 |
| 51 | .716 | .417 | .836 | .8927 | .48252 | .88089 | .55089 | .8152 | .521 | .835 | .569 | .7426 | 9 |
| 52 | .742 | .404 | .873 | .8913 | .48277 | .88020 | .55127 | .8140 | .524 | .833 | .569 | .7414 | 8 |
| 53 | .767 | .390 | .910 | .8900 | .48303 | .87951 | .55165 | .8127 | .527 | .831 | .569 | .7402 | 7 |
| 54 | .793 | .377 | .947 | .8887 | .48328 | .87882 | .55203 | .8115 | .530 | .829 | .569 | .7391 | 6 |
| 55 | .46819 | .88363 | .52985 | 1.8873 | .48354 | .87813 | .55241 | 1.8103 | .49874 | .86675 | .57541 | 1.7379 | 5 |
| 56 | .844 | .349 | .53022 | .8860 | .48379 | .88089 | .55279 | .8090 | .533 | .827 | .569 | .7367 | 4 |
| 57 | .870 | .336 | .569 | .8847 | .48405 | .88020 | .55317 | .8078 | .536 | .825 | .569 | .7355 | 3 |
| 58 | .896 | .322 | .606 | .8834 | .48430 | .87951 | .55355 | .8065 | .539 | .823 | .569 | .7343 | 2 |
| 59 | .921 | .308 | .643 | .8820 | .48456 | .87882 | .55393 | .8053 | .542 | .821 | .569 | .7332 | 1 |
| 60 | .46947 | .88295 | .53171 | 1.8807 | .48481 | .87462 | .55431 | 1.8040 | .50000 | .86603 | .57735 | 1.7321 | 0 |
| | Cos. | Sin. | Cot. | Tan. | Cos. | Sin. | Cot. | Tan. | Cos. | Sin. | Cot. | Tan. | M. |

62°

61°

60°

30°

31°

32°

| M. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | M. |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0 | .50000 | .86603 | .57735 | 1.7321 | .51504 | .85717 | .60086 | 1.6643 | .52992 | .84805 | .62487 | 1.6003 | 60 |
| 1 | 025 | 588 | 774 | .7309 | 529 | 702 | 126 | .6632 | .53017 | 789 | 527 | .5993 | 59 |
| 2 | 050 | 573 | 813 | .7297 | 554 | 687 | 165 | .6621 | 041 | 774 | 568 | .5983 | 58 |
| 3 | 076 | 559 | 851 | .7286 | 579 | 672 | 205 | .6610 | 066 | 759 | 608 | .5972 | 57 |
| 4 | 101 | 544 | 890 | .7274 | 604 | 657 | 245 | .6599 | 091 | 743 | 649 | .5962 | 56 |
| 5 | .50126 | .86530 | .57929 | 1.7262 | .51628 | .85642 | .60284 | 1.6588 | .53115 | .84728 | .62689 | 1.5952 | 55 |
| 6 | 151 | 515 | 968 | .7251 | 653 | 627 | 324 | .6577 | 140 | 712 | 730 | .5941 | 54 |
| 7 | 176 | 501 | .58007 | .7239 | 678 | 612 | 364 | .6566 | 164 | 697 | 770 | .5931 | 53 |
| 8 | 201 | 486 | 046 | .7228 | 703 | 597 | 403 | .6555 | 189 | 681 | 811 | .5921 | 52 |
| 9 | 227 | 471 | 085 | .7216 | 728 | 582 | 443 | .6545 | 214 | 666 | 852 | .5911 | 51 |
| 10 | .50252 | .86457 | .58124 | 1.7205 | .51753 | .85567 | .60483 | 1.6534 | .53238 | .84650 | .62892 | 1.5900 | 50 |
| 11 | 277 | 442 | 162 | .7193 | 778 | 551 | 522 | .6523 | 263 | 635 | 933 | .5890 | 49 |
| 12 | 302 | 427 | 201 | .7182 | 803 | 536 | 562 | .6512 | 288 | 619 | 973 | .5880 | 48 |
| 13 | 327 | 413 | 240 | .7170 | 828 | 521 | 602 | .6501 | 312 | 604 | .63014 | .5869 | 47 |
| 14 | 352 | 398 | 279 | .7159 | 852 | 506 | 642 | .6490 | 337 | 588 | 055 | .5859 | 46 |
| 15 | .50377 | .86384 | .58318 | 1.7147 | .51877 | .85491 | .60681 | 1.6479 | .53361 | .84573 | .63095 | 1.5849 | 45 |
| 16 | 403 | 369 | 357 | .7136 | 902 | 476 | 721 | .6469 | 386 | 557 | 136 | .5839 | 44 |
| 17 | 428 | 354 | 396 | .7124 | 927 | 461 | 761 | .6458 | 411 | 542 | 177 | .5829 | 43 |
| 18 | 453 | 340 | 435 | .7113 | 952 | 446 | 801 | .6447 | 435 | 526 | 217 | .5818 | 42 |
| 19 | 478 | 325 | 474 | .7102 | 977 | 431 | 841 | .6436 | 460 | 511 | 258 | .5808 | 41 |
| 20 | .50503 | .86310 | .58513 | 1.7090 | .52002 | .85416 | .60881 | 1.6426 | .53484 | .84495 | .63299 | 1.5798 | 40 |
| 21 | 528 | 295 | 552 | .7079 | 026 | 401 | 921 | .6415 | 509 | 480 | 340 | .5788 | 39 |
| 22 | 553 | 281 | 591 | .7067 | 051 | 385 | 960 | .6404 | 534 | 464 | 380 | .5778 | 38 |
| 23 | 578 | 266 | 631 | .7056 | 076 | 370 | .61000 | .6393 | 558 | 448 | 421 | .5768 | 37 |
| 24 | 603 | 251 | 670 | .7045 | 101 | 355 | 040 | .6383 | 583 | 433 | 462 | .5757 | 36 |
| 25 | .50628 | .86237 | .58709 | 1.7033 | .52126 | .85340 | .61080 | 1.6372 | .53607 | .84417 | .63503 | 1.5747 | 35 |
| 26 | 654 | 222 | 748 | .7022 | 151 | 325 | 120 | .6361 | 632 | 402 | 544 | .5737 | 34 |
| 27 | 679 | 207 | 787 | .7011 | 175 | 310 | 160 | .6351 | 656 | 386 | 584 | .5727 | 33 |
| 28 | 704 | 192 | 826 | .6999 | 200 | 294 | 200 | .6340 | 681 | 370 | 625 | .5717 | 32 |
| 29 | 729 | 178 | 865 | .6988 | 225 | 279 | 240 | .6329 | 705 | 355 | 666 | .5707 | 31 |
| 30 | .50754 | .86163 | .58905 | 1.6977 | .52250 | .85264 | .61280 | 1.6319 | .53730 | .84339 | .63707 | 1.5697 | 30 |
| 31 | 779 | 148 | 944 | .6965 | 275 | 249 | 320 | .6308 | 754 | 324 | 748 | .5687 | 29 |
| 32 | 804 | 133 | 983 | .6954 | 299 | 234 | 360 | .6297 | 779 | 308 | 789 | .5677 | 28 |
| 33 | 829 | 119 | .59022 | .6943 | 324 | 218 | 400 | .6287 | 804 | 292 | 830 | .5667 | 27 |
| 34 | 854 | 104 | 061 | .6932 | 349 | 203 | 440 | .6276 | 828 | 277 | 871 | .5657 | 26 |
| 35 | .50879 | .86089 | .59101 | 1.6920 | .52374 | .85188 | .61480 | 1.6265 | .53853 | .84261 | .63912 | 1.5647 | 25 |
| 36 | 904 | 074 | 140 | .6909 | 399 | 173 | 520 | .6255 | 877 | 245 | 953 | .5637 | 24 |
| 37 | 929 | 059 | 179 | .6898 | 423 | 157 | 561 | .6244 | 902 | 230 | 994 | .5627 | 23 |
| 38 | 954 | 045 | 218 | .6887 | 448 | 142 | 601 | .6234 | 926 | 214 | .64035 | .5617 | 22 |
| 39 | 979 | 030 | 258 | .6875 | 473 | 127 | 641 | .6223 | 951 | 198 | 076 | .5607 | 21 |
| 40 | .51004 | .86015 | .59297 | 1.6864 | .52498 | .85112 | .61681 | 1.6212 | .53975 | .84182 | .64117 | 1.5597 | 20 |
| 41 | 029 | 000 | 336 | .6853 | 522 | 096 | 721 | .6202 | .54000 | 167 | 158 | .5587 | 19 |
| 42 | 054 | .85985 | 376 | .6842 | 547 | 081 | 761 | .6191 | 024 | 151 | 199 | .5577 | 18 |
| 43 | 079 | 970 | 415 | .6831 | 572 | 066 | 801 | .6181 | 049 | 135 | 240 | .5567 | 17 |
| 44 | 104 | 956 | 454 | .6820 | 597 | 051 | 842 | .6170 | 073 | 120 | 281 | .5557 | 16 |
| 45 | .51129 | .85941 | .59494 | 1.6808 | .52621 | .85035 | .61882 | 1.6160 | .54097 | .84104 | .64322 | 1.5547 | 15 |
| 46 | 154 | 926 | 533 | .6797 | 646 | 020 | 922 | .6149 | 122 | 088 | 363 | .5537 | 14 |
| 47 | 179 | 911 | 573 | .6786 | 671 | 005 | 962 | .6139 | 146 | 072 | 404 | .5527 | 13 |
| 48 | 204 | 896 | 612 | .6775 | 696 | .84989 | .62003 | .6128 | 171 | 057 | 446 | .5517 | 12 |
| 49 | 229 | 881 | 651 | .6764 | 720 | 974 | 043 | .6118 | 195 | 041 | 487 | .5507 | 11 |
| 50 | .51254 | .85866 | .59691 | 1.6753 | .52745 | .84959 | .62083 | 1.6107 | .54220 | .84025 | .64528 | 1.5497 | 10 |
| 51 | 279 | 851 | 730 | .6742 | 770 | 943 | 124 | .6097 | 244 | 009 | 569 | .5487 | 9 |
| 52 | 304 | 836 | 770 | .6731 | 794 | 928 | 164 | .6087 | 269 | .83994 | 610 | .5477 | 8 |
| 53 | 329 | 821 | 809 | .6720 | 819 | 913 | 204 | .6076 | 293 | 978 | 652 | .5468 | 7 |
| 54 | 354 | 806 | 849 | .6709 | 844 | 897 | 245 | .6066 | 317 | 962 | 693 | .5458 | 6 |
| 55 | .51379 | .85792 | .59888 | 1.6698 | .52869 | .84882 | .62285 | 1.6055 | .54342 | .83946 | .64734 | 1.5448 | 5 |
| 56 | 404 | 777 | 928 | .6687 | 893 | 866 | 325 | .6045 | 366 | 930 | 775 | .5438 | 4 |
| 57 | 429 | 762 | 967 | .6676 | 918 | 851 | 366 | .6034 | 391 | 915 | 817 | .5428 | 3 |
| 58 | 454 | 747 | .60007 | .6665 | 943 | 836 | 406 | .6024 | 415 | 899 | 858 | .5418 | 2 |
| 59 | 479 | 732 | 046 | .6654 | 967 | 820 | 446 | .6014 | 440 | 883 | 899 | .5408 | 1 |
| 60 | .51504 | .85717 | .60086 | 1.6643 | .52992 | .84805 | .62487 | 1.6003 | .54464 | .83867 | .64941 | 1.5399 | 0 |
| | Cos. | Sin. | Cot. | Tan. | Cos. | Sin. | Cot. | Tan. | Cos. | Sin. | Cot. | Tan. | M. |

59°

58°

57°

33°

34°

35°

| M. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | M. |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0 | .54404 | .83867 | .64941 | 1.5399 | .55919 | .82904 | .67451 | 1.4826 | .57358 | .81915 | .70021 | 1.4281 | 60 |
| 1 | .488 | .851 | .982 | .5389 | .943 | .887 | .493 | .4816 | .381 | .899 | .064 | .4273 | 59 |
| 2 | .513 | .835 | .65024 | .5379 | .968 | .871 | .536 | .4807 | .405 | .882 | .107 | .4204 | 58 |
| 3 | .537 | .819 | .065 | .5369 | .992 | .855 | .578 | .4798 | .429 | .865 | .151 | .4255 | 57 |
| 4 | .561 | .804 | .106 | .5359 | .56016 | .839 | .620 | .4788 | .453 | .848 | .194 | .4240 | 56 |
| 5 | .54586 | .83788 | .65148 | 1.5350 | .56040 | .82822 | .67663 | 1.4779 | .57477 | .81832 | .70238 | 1.4237 | 55 |
| 6 | .610 | .772 | .189 | .5340 | .064 | .806 | .705 | .4770 | .501 | .815 | .281 | .4229 | 54 |
| 7 | .635 | .756 | .231 | .5330 | .088 | .790 | .748 | .4761 | .524 | .798 | .325 | .4220 | 53 |
| 8 | .659 | .740 | .272 | .5320 | .112 | .773 | .790 | .4751 | .548 | .782 | .368 | .4211 | 52 |
| 9 | .683 | .724 | .314 | .5311 | .136 | .757 | .832 | .4742 | .572 | .765 | .412 | .4202 | 51 |
| 10 | .54708 | .83708 | .65355 | 1.5301 | .56160 | .82741 | .67875 | 1.4733 | .57596 | .81748 | .70455 | 1.4193 | 50 |
| 11 | .732 | .692 | .397 | .5291 | .184 | .724 | .917 | .4724 | .619 | .731 | .499 | .4185 | 49 |
| 12 | .756 | .676 | .438 | .5282 | .208 | .708 | .960 | .4715 | .643 | .714 | .542 | .4176 | 48 |
| 13 | .781 | .660 | .480 | .5272 | .232 | .692 | .68002 | .4705 | .667 | .698 | .586 | .4167 | 47 |
| 14 | .805 | .645 | .521 | .5262 | .256 | .675 | .045 | .4696 | .691 | .681 | .629 | .4158 | 46 |
| 15 | .54829 | .83629 | .65563 | 1.5253 | .56280 | .82659 | .68088 | 1.4687 | .57715 | .81664 | .70673 | 1.4150 | 45 |
| 16 | .854 | .613 | .604 | .5243 | .305 | .643 | .130 | .4678 | .738 | .647 | .717 | .4141 | 44 |
| 17 | .878 | .597 | .646 | .5233 | .329 | .626 | .173 | .4669 | .762 | .631 | .760 | .4132 | 43 |
| 18 | .902 | .581 | .688 | .5224 | .353 | .610 | .215 | .4659 | .786 | .614 | .804 | .4124 | 42 |
| 19 | .927 | .565 | .729 | .5214 | .377 | .593 | .258 | .4650 | .810 | .597 | .848 | .4115 | 41 |
| 20 | .54951 | .83549 | .65771 | 1.5204 | .56401 | .82577 | .68301 | 1.4641 | .57833 | .81580 | .70891 | 1.4106 | 40 |
| 21 | .975 | .533 | .813 | .5195 | .425 | .561 | .343 | .4632 | .857 | .563 | .935 | .4097 | 39 |
| 22 | .999 | .517 | .854 | .5185 | .449 | .544 | .386 | .4623 | .881 | .546 | .979 | .4089 | 38 |
| 23 | .55024 | .501 | .896 | .5175 | .473 | .528 | .429 | .4614 | .904 | .530 | .71023 | .4080 | 37 |
| 24 | .048 | .485 | .938 | .5166 | .497 | .511 | .471 | .4605 | .928 | .513 | .066 | .4071 | 36 |
| 25 | .55072 | .83469 | .65980 | 1.5156 | .56521 | .82495 | .68514 | 1.4596 | .57952 | .81496 | .71110 | 1.4063 | 35 |
| 26 | .097 | .453 | .66021 | .5147 | .545 | .478 | .557 | .4586 | .976 | .479 | .154 | .4054 | 34 |
| 27 | .121 | .437 | .063 | .5137 | .569 | .462 | .600 | .4577 | .999 | .462 | .198 | .4045 | 33 |
| 28 | .145 | .421 | .105 | .5127 | .593 | .446 | .642 | .4568 | .58023 | .445 | .242 | .4037 | 32 |
| 29 | .169 | .405 | .147 | .5118 | .617 | .429 | .685 | .4559 | .047 | .428 | .285 | .4028 | 31 |
| 30 | .55194 | .83389 | .66189 | 1.5108 | .56641 | .82413 | .68728 | 1.4550 | .58070 | .81412 | .71329 | 1.4019 | 30 |
| 31 | .218 | .373 | .230 | .5099 | .665 | .396 | .771 | .4541 | .094 | .395 | .373 | .4011 | 29 |
| 32 | .242 | .357 | .272 | .5089 | .689 | .380 | .814 | .4532 | .118 | .378 | .417 | .4002 | 28 |
| 33 | .266 | .340 | .314 | .5080 | .713 | .363 | .857 | .4523 | .141 | .361 | .461 | .3994 | 27 |
| 34 | .291 | .324 | .356 | .5070 | .736 | .347 | .900 | .4514 | .165 | .344 | .505 | .3985 | 26 |
| 35 | .55315 | .83308 | .66398 | 1.5061 | .56760 | .82330 | .68942 | 1.4505 | .58189 | .81327 | .71549 | 1.3976 | 25 |
| 36 | .339 | .292 | .440 | .5051 | .784 | .314 | .985 | .4496 | .212 | .310 | .593 | .3968 | 24 |
| 37 | .363 | .276 | .482 | .5042 | .808 | .297 | .69028 | .4487 | .236 | .293 | .637 | .3959 | 23 |
| 38 | .388 | .260 | .524 | .5032 | .832 | .281 | .071 | .4478 | .260 | .276 | .681 | .3951 | 22 |
| 39 | .412 | .244 | .566 | .5023 | .856 | .264 | .114 | .4469 | .283 | .259 | .725 | .3942 | 21 |
| 40 | .55436 | .83228 | .66608 | 1.5013 | .56880 | .82248 | .69157 | 1.4460 | .58307 | .81242 | .71769 | 1.3934 | 20 |
| 41 | .460 | .212 | .650 | .5004 | .904 | .231 | .200 | .4451 | .330 | .225 | .813 | .3925 | 19 |
| 42 | .484 | .195 | .692 | .4994 | .928 | .214 | .243 | .4442 | .354 | .208 | .857 | .3916 | 18 |
| 43 | .509 | .179 | .734 | .4985 | .952 | .198 | .286 | .4433 | .378 | .191 | .901 | .3908 | 17 |
| 44 | .533 | .163 | .776 | .4975 | .976 | .181 | .329 | .4424 | .401 | .174 | .946 | .3899 | 16 |
| 45 | .55557 | .83147 | .66818 | 1.4966 | .57000 | .82165 | .69372 | 1.4415 | .58425 | .81157 | .71990 | 1.3891 | 15 |
| 46 | .581 | .131 | .860 | .4957 | .024 | .148 | .416 | .4406 | .449 | .140 | .72034 | .3882 | 14 |
| 47 | .605 | .115 | .902 | .4947 | .047 | .132 | .459 | .4397 | .472 | .123 | .078 | .3874 | 13 |
| 48 | .630 | .098 | .944 | .4938 | .071 | .115 | .502 | .4388 | .496 | .106 | .122 | .3865 | 12 |
| 49 | .654 | .082 | .986 | .4928 | .095 | .098 | .545 | .4379 | .519 | .089 | .167 | .3857 | 11 |
| 50 | .55678 | .83066 | .67028 | 1.4919 | .57119 | .82082 | .69588 | 1.4370 | .58543 | .81072 | .72211 | 1.3848 | 10 |
| 51 | .702 | .050 | .071 | .4910 | .143 | .065 | .631 | .4361 | .567 | .055 | .255 | .3840 | 9 |
| 52 | .726 | .034 | .113 | .4900 | .167 | .048 | .675 | .4352 | .590 | .038 | .299 | .3831 | 8 |
| 53 | .750 | .017 | .155 | .4891 | .191 | .032 | .718 | .4344 | .614 | .021 | .344 | .3823 | 7 |
| 54 | .775 | .001 | .197 | .4882 | .215 | .015 | .761 | .4335 | .637 | .004 | .388 | .3814 | 6 |
| 55 | .55799 | .82985 | .67239 | 1.4872 | .57238 | .81999 | .69804 | 1.4326 | .58661 | .80987 | .72432 | 1.3806 | 5 |
| 56 | .823 | .969 | .282 | .4863 | .262 | .982 | .847 | .4317 | .684 | .970 | .477 | .3798 | 4 |
| 57 | .847 | .953 | .324 | .4854 | .286 | .965 | .891 | .4308 | .708 | .953 | .521 | .3789 | 3 |
| 58 | .871 | .936 | .366 | .4844 | .310 | .949 | .934 | .4299 | .731 | .936 | .565 | .3781 | 2 |
| 59 | .895 | .920 | .409 | .4835 | .334 | .932 | .977 | .4290 | .755 | .919 | .610 | .3772 | 1 |
| 60 | .55919 | .82904 | .67451 | 1.4826 | .57358 | .81915 | .70021 | 1.4281 | .58779 | .80902 | .72654 | 1.3764 | 0 |
| | Cos. | Sin. | Cot. | Tan. | Cos. | Sin. | Cot. | Tan. | Cos. | Sin. | Cot. | Tan. | M. |

56°

55°

54°

36°

37°

38°

| M. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | M. |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0 | .58779 | .80902 | .72654 | 1.3764 | .60182 | .79864 | .75355 | 1.3270 | .61566 | .78801 | .78129 | 1.2799 | 60 |
| 1 | 802 | 885 | 699 | .3755 | 205 | 846 | 401 | .3262 | 589 | 783 | 175 | .2792 | 59 |
| 2 | 826 | 867 | 743 | .3747 | 228 | 829 | 447 | .3254 | 612 | 765 | 222 | .2784 | 58 |
| 3 | 849 | 850 | 788 | .3739 | 251 | 811 | 492 | .3246 | 635 | 747 | 269 | .2776 | 57 |
| 4 | 873 | 833 | 832 | .3730 | 274 | 793 | 538 | .3238 | 658 | 729 | 316 | .2769 | 56 |
| 5 | .58896 | .80816 | .72877 | 1.3722 | .60298 | .79776 | .75584 | 1.3230 | .61681 | .78711 | .78363 | 1.2761 | 55 |
| 6 | 920 | 799 | 921 | .3713 | 321 | 758 | 629 | .3222 | 704 | 694 | 410 | .2753 | 54 |
| 7 | 943 | 782 | 966 | .3705 | 344 | 741 | 675 | .3214 | 726 | 676 | 457 | .2746 | 53 |
| 8 | 967 | 765 | .73010 | .3697 | 367 | 723 | 721 | .3206 | 749 | 658 | 504 | .2738 | 52 |
| 9 | 990 | 748 | 055 | .3688 | 390 | 706 | 767 | .3198 | 772 | 640 | 551 | .2731 | 51 |
| 10 | .59014 | .80730 | .73100 | 1.3680 | .60414 | .79688 | .75812 | 1.3190 | .61795 | .78622 | .78598 | 1.2723 | 50 |
| 11 | 037 | 713 | 144 | .3672 | 437 | 671 | 858 | .3182 | 818 | 604 | 645 | .2715 | 49 |
| 12 | 061 | 696 | 189 | .3663 | 460 | 653 | 904 | .3175 | 841 | 586 | 692 | .2708 | 48 |
| 13 | 084 | 679 | 234 | .3655 | 483 | 635 | 950 | .3167 | 864 | 568 | 739 | .2700 | 47 |
| 14 | 108 | 662 | 278 | .3647 | 506 | 618 | 996 | .3159 | 887 | 550 | 786 | .2693 | 46 |
| 15 | .59131 | .80644 | .73323 | 1.3638 | .60529 | .79600 | .76042 | 1.3151 | .61909 | .78532 | .78834 | 1.2685 | 45 |
| 16 | 154 | 627 | 368 | .3630 | 553 | 583 | 088 | .3143 | 932 | 514 | 881 | .2677 | 44 |
| 17 | 178 | 610 | 413 | .3622 | 576 | 565 | 134 | .3135 | 955 | 496 | 928 | .2670 | 43 |
| 18 | 201 | 593 | 457 | .3613 | 599 | 547 | 180 | .3127 | 978 | 478 | 975 | .2662 | 42 |
| 19 | 225 | 576 | 502 | .3605 | 622 | 530 | 226 | .3119 | .62001 | 460 | .79022 | .2655 | 41 |
| 20 | .59248 | .80558 | .73547 | 1.3597 | .60645 | .79512 | .76272 | 1.3111 | .62024 | .78442 | .79070 | 1.2647 | 40 |
| 21 | 272 | 541 | 592 | .3588 | 668 | 494 | 318 | .3103 | 046 | 424 | 117 | .2640 | 39 |
| 22 | 295 | 524 | 637 | .3580 | 691 | 477 | 364 | .3095 | 069 | 405 | 164 | .2632 | 38 |
| 23 | 318 | 507 | 681 | .3572 | 714 | 459 | 410 | .3087 | 092 | 387 | 212 | .2624 | 37 |
| 24 | 342 | 489 | 726 | .3564 | 738 | 441 | 456 | .3079 | 115 | 369 | 259 | .2617 | 36 |
| 25 | .59365 | .80472 | .73771 | 1.3555 | .60761 | .79424 | .76502 | 1.3072 | .62138 | .78351 | .79306 | 1.2609 | 35 |
| 26 | 389 | 455 | 816 | .3547 | 784 | 406 | 548 | .3064 | 160 | 333 | 354 | .2602 | 34 |
| 27 | 412 | 438 | 861 | .3539 | 807 | 388 | 594 | .3056 | 183 | 315 | 401 | .2594 | 33 |
| 28 | 436 | 420 | 906 | .3531 | 830 | 371 | 640 | .3048 | 206 | 297 | 449 | .2587 | 32 |
| 29 | 459 | 403 | 951 | .3522 | 853 | 353 | 686 | .3040 | 229 | 279 | 496 | .2579 | 31 |
| 30 | .59482 | .80386 | .73996 | 1.3514 | .60876 | .79335 | .76733 | 1.3032 | .62251 | .78261 | .79544 | 1.2572 | 30 |
| 31 | 506 | 368 | .74041 | .3506 | 899 | 318 | 779 | .3024 | 274 | 243 | 591 | .2564 | 29 |
| 32 | 529 | 351 | 086 | .3498 | 922 | 300 | 825 | .3017 | 297 | 225 | 639 | .2557 | 28 |
| 33 | 552 | 334 | 131 | .3490 | 945 | 282 | 871 | .3009 | 320 | 206 | 686 | .2549 | 27 |
| 34 | 576 | 316 | 176 | .3481 | 968 | 264 | 918 | .3001 | 342 | 188 | 734 | .2542 | 26 |
| 35 | .59599 | .80299 | .74221 | 1.3473 | .60991 | .79247 | .76964 | 1.2993 | .62365 | .78170 | .79781 | 1.2534 | 25 |
| 36 | 622 | 282 | 267 | .3465 | .61015 | 229 | .77010 | .2985 | 388 | 152 | 829 | .2527 | 24 |
| 37 | 646 | 264 | 312 | .3457 | 038 | 211 | 057 | .2977 | 411 | 134 | 877 | .2519 | 23 |
| 38 | 669 | 247 | 357 | .3449 | 061 | 193 | 103 | .2970 | 433 | 116 | 924 | .2512 | 22 |
| 39 | 693 | 230 | 402 | .3440 | 084 | 176 | 149 | .2962 | 456 | 098 | 972 | .2504 | 21 |
| 40 | .59716 | .80212 | .74447 | 1.3432 | .61107 | .79158 | .77196 | 1.2954 | .62479 | .78079 | .80020 | 1.2497 | 20 |
| 41 | 739 | 195 | 492 | .3424 | 130 | 140 | 242 | .2946 | 502 | 061 | 067 | .2489 | 19 |
| 42 | 763 | 178 | 538 | .3416 | 153 | 122 | 289 | .2938 | 524 | 043 | 115 | .2482 | 18 |
| 43 | 786 | 160 | 583 | .3408 | 176 | 105 | 335 | .2931 | 547 | 025 | 163 | .2475 | 17 |
| 44 | 809 | 143 | 628 | .3400 | 199 | 087 | 382 | .2923 | 570 | 007 | 211 | .2467 | 16 |
| 45 | .59832 | .80125 | .74674 | 1.3392 | .61222 | .79069 | .77428 | 1.2915 | .62592 | .77988 | .80258 | 1.2460 | 15 |
| 46 | 856 | 108 | 719 | .3384 | 245 | 051 | 475 | .2907 | 615 | 970 | 306 | .2452 | 14 |
| 47 | 879 | 091 | 764 | .3375 | 268 | 033 | 521 | .2900 | 638 | 952 | 354 | .2445 | 13 |
| 48 | 902 | 073 | 810 | .3367 | 291 | 016 | 568 | .2892 | 660 | 934 | 402 | .2437 | 12 |
| 49 | 926 | 056 | 855 | .3359 | 314 | .78998 | 615 | .2884 | 683 | 916 | 450 | .2430 | 11 |
| 50 | .59949 | .80038 | .74900 | 1.3351 | .61337 | .78980 | .77661 | 1.2876 | .62706 | .77897 | .80498 | 1.2423 | 10 |
| 51 | 972 | 021 | 946 | .3343 | 360 | 962 | 708 | .2869 | 728 | 879 | 546 | .2415 | 9 |
| 52 | 995 | 003 | 991 | .3335 | 383 | 944 | 754 | .2861 | 751 | 861 | 594 | .2408 | 8 |
| 53 | .60019 | .79986 | .75037 | .3327 | 406 | 926 | 801 | .2853 | 774 | 843 | 642 | .2401 | 7 |
| 54 | 042 | 968 | 082 | .3319 | 429 | 908 | 848 | .2846 | 796 | 824 | 690 | .2393 | 6 |
| 55 | .60065 | .79951 | .75128 | 1.3311 | .61451 | .78891 | .77895 | 1.2838 | .62819 | .77806 | .80738 | 1.2386 | 5 |
| 56 | 089 | 934 | 173 | .3303 | 474 | 873 | 941 | .2830 | 842 | 788 | 786 | .2378 | 4 |
| 57 | 112 | 916 | 219 | .3295 | 497 | 855 | 988 | .2822 | 864 | 769 | 834 | .2371 | 3 |
| 58 | 135 | 899 | 264 | .3287 | 520 | 837 | .78035 | .2815 | 887 | 751 | 882 | .2364 | 2 |
| 59 | 158 | 881 | 310 | .3278 | 543 | 819 | 082 | .2807 | 909 | 733 | 930 | .2356 | 1 |
| 60 | .60182 | .79864 | .75355 | 1.3270 | .61566 | .78801 | .78129 | 1.2799 | .62932 | .77715 | .80978 | 1.2349 | 0 |
| | Cos. | Sin. | Cot. | Tan. | Cos. | Sin. | Cot. | Tan. | Cos. | Sin. | Cot. | Tan. | M. |

53°

52°

51°

39°

40°

41°

| M. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | M. |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0 | .62932 | .77715 | .80978 | 1.2349 | .64279 | .76604 | .83910 | 1.1918 | .65000 | .75471 | .86929 | 1.1504 | 60 |
| 1 | 955 | 696 | .81027 | .2342 | 301 | 580 | 960 | .1910 | 628 | 452 | 980 | .1497 | 59 |
| 2 | 977 | 678 | 075 | .2334 | 323 | 567 | .84009 | .1903 | 650 | 433 | .87031 | .1490 | 58 |
| 3 | 63000 | 660 | 123 | .2327 | 346 | 548 | 059 | .1896 | 672 | 414 | 082 | .1483 | 57 |
| 4 | 022 | 641 | 171 | .2320 | 368 | 530 | 108 | .1889 | 694 | 395 | 133 | .1477 | 56 |
| 5 | .63045 | .77623 | .81220 | 1.2312 | .64390 | .76511 | .84158 | 1.1882 | .65716 | .75375 | .87184 | 1.1470 | 55 |
| 6 | 068 | 605 | 268 | .2305 | 412 | 492 | 208 | .1875 | 738 | 356 | 236 | .1463 | 54 |
| 7 | 090 | 586 | 316 | .2298 | 435 | 473 | 258 | .1868 | 759 | 337 | 287 | .1456 | 53 |
| 8 | 113 | 568 | 364 | .2290 | 457 | 455 | 307 | .1861 | 781 | 318 | 338 | .1450 | 52 |
| 9 | 135 | 550 | 413 | .2283 | 479 | 436 | 357 | .1854 | 803 | 299 | 389 | .1443 | 51 |
| 10 | .63158 | .77531 | .81461 | 1.2276 | .64501 | .76417 | .84407 | 1.1847 | .65825 | .75280 | .87441 | 1.1436 | 50 |
| 11 | 180 | 513 | 510 | .2268 | 524 | 398 | 457 | .1840 | 847 | 261 | 492 | .1430 | 49 |
| 12 | 203 | 494 | 558 | .2261 | 546 | 380 | 507 | .1833 | 869 | 241 | 543 | .1423 | 48 |
| 13 | 225 | 476 | 606 | .2254 | 568 | 361 | 556 | .1826 | 891 | 222 | 595 | .1416 | 47 |
| 14 | 248 | 458 | 655 | .2247 | 590 | 342 | 606 | .1819 | 913 | 203 | 646 | .1410 | 46 |
| 15 | .63271 | .77439 | .81703 | 1.2239 | .64612 | .76323 | .84656 | 1.1812 | .65935 | .75184 | .87698 | 1.1403 | 45 |
| 16 | 293 | 421 | 752 | .2232 | 635 | 304 | 706 | .1806 | 956 | 165 | 749 | .1396 | 44 |
| 17 | 316 | 402 | 800 | .2225 | 657 | 286 | 756 | .1799 | 978 | 146 | 801 | .1389 | 43 |
| 18 | 338 | 384 | 849 | .2218 | 679 | 267 | 806 | .1792 | .66000 | 126 | 852 | .1383 | 42 |
| 19 | 361 | 366 | 898 | .2210 | 701 | 248 | 856 | .1785 | 022 | 107 | 904 | .1376 | 41 |
| 20 | .63383 | .77347 | .81946 | 1.2203 | .64723 | .76229 | .84906 | 1.1778 | .66044 | .75088 | .87955 | 1.1369 | 40 |
| 21 | 406 | 329 | 995 | .2196 | 746 | 210 | 956 | .1771 | 066 | 069 | .88007 | .1363 | 39 |
| 22 | 428 | 310 | .82044 | .2189 | 768 | 192 | .85006 | .1764 | 088 | 050 | 059 | .1356 | 38 |
| 23 | 451 | 292 | 092 | .2181 | 790 | 173 | 957 | .1757 | 109 | 030 | 110 | .1349 | 37 |
| 24 | 473 | 273 | 141 | .2174 | 812 | 154 | 107 | .1750 | 131 | 011 | 162 | .1343 | 36 |
| 25 | .63496 | .77255 | .82190 | 1.2167 | .64834 | .76135 | .85157 | 1.1743 | .66153 | .74992 | .88214 | 1.1336 | 35 |
| 26 | 518 | 236 | 238 | .2160 | 856 | 116 | 207 | .1736 | 175 | 973 | 265 | .1329 | 34 |
| 27 | 540 | 218 | 287 | .2153 | 878 | 097 | 257 | .1729 | 197 | 953 | 317 | .1323 | 33 |
| 28 | 563 | 199 | 336 | .2145 | 901 | 078 | 308 | .1722 | 218 | 934 | 369 | .1316 | 32 |
| 29 | 585 | 181 | 385 | .2138 | 923 | 059 | 358 | .1715 | 240 | 915 | 421 | .1310 | 31 |
| 30 | .63608 | .77162 | .82434 | 1.2131 | .64945 | .76041 | .85408 | 1.1708 | .66262 | .74896 | .88473 | 1.1303 | 30 |
| 31 | 630 | 144 | 483 | .2124 | 967 | 022 | 458 | .1702 | 284 | 876 | 524 | .1296 | 29 |
| 32 | 653 | 125 | 531 | .2117 | 989 | 003 | 509 | .1695 | 306 | 857 | 576 | .1290 | 28 |
| 33 | 675 | 107 | 580 | .2109 | .65011 | .75984 | 559 | .1688 | 327 | 838 | 628 | .1283 | 27 |
| 34 | 698 | 088 | 629 | .2102 | 033 | 965 | 609 | .1681 | 349 | 818 | 680 | .1276 | 26 |
| 35 | .63720 | .77070 | .82678 | 1.2095 | .65055 | .75946 | .85660 | 1.1674 | .66371 | .74799 | .88732 | 1.1270 | 25 |
| 36 | 742 | 051 | 727 | .2088 | 077 | 927 | 710 | .1667 | 393 | 780 | 784 | .1263 | 24 |
| 37 | 765 | 033 | 776 | .2081 | 100 | 908 | 761 | .1660 | 414 | 760 | 836 | .1257 | 23 |
| 38 | 787 | 014 | 825 | .2074 | 122 | 889 | 811 | .1653 | 436 | 741 | 888 | .1250 | 22 |
| 39 | 810 | .76996 | 874 | .2066 | 144 | 870 | 862 | .1647 | 458 | 722 | 940 | .1243 | 21 |
| 40 | .63832 | .76977 | .82923 | 1.2059 | .65166 | .75851 | .85912 | 1.1640 | .66480 | .74703 | .88992 | 1.1237 | 20 |
| 41 | 854 | 959 | 972 | .2052 | 188 | 832 | 963 | .1633 | 501 | 683 | .89045 | .1230 | 19 |
| 42 | 877 | 940 | .83022 | .2045 | 210 | 813 | .86014 | .1626 | 523 | 664 | 097 | .1224 | 18 |
| 43 | 899 | 921 | 071 | .2038 | 232 | 794 | 064 | .1619 | 545 | 644 | 149 | .1217 | 17 |
| 44 | 922 | 903 | 120 | .2031 | 254 | 775 | 115 | .1612 | 566 | 625 | 201 | .1211 | 16 |
| 45 | .63944 | .76884 | .83169 | 1.2024 | .65276 | .75756 | .86166 | 1.1606 | .66588 | .74606 | .89253 | 1.1204 | 15 |
| 46 | 966 | 866 | 218 | .2017 | 298 | 738 | 216 | .1599 | 610 | 586 | 306 | .1197 | 14 |
| 47 | 989 | 847 | 268 | .2009 | 320 | 719 | 267 | .1592 | 632 | 567 | 358 | .1191 | 13 |
| 48 | 64011 | 828 | 317 | .2002 | 342 | 700 | 318 | .1585 | 653 | 548 | 410 | .1184 | 12 |
| 49 | 033 | 810 | 366 | .1995 | 364 | 680 | 368 | .1578 | 675 | 528 | 463 | .1178 | 11 |
| 50 | .64056 | .76791 | .83415 | 1.1988 | .65386 | .75661 | .86419 | 1.1571 | .66697 | .74509 | .89515 | 1.1171 | 10 |
| 51 | 078 | 772 | 465 | .1981 | 408 | 642 | 470 | .1565 | 718 | 489 | 567 | .1165 | 9 |
| 52 | 100 | 754 | 514 | .1974 | 430 | 623 | 521 | .1558 | 740 | 470 | 620 | .1158 | 8 |
| 53 | 123 | 735 | 564 | .1967 | 452 | 604 | 572 | .1551 | 762 | 451 | 672 | .1152 | 7 |
| 54 | 145 | 717 | 613 | .1960 | 474 | 585 | 623 | .1544 | 783 | 431 | 725 | .1145 | 6 |
| 55 | .64167 | .76698 | .83662 | 1.1953 | .65496 | .75566 | .86674 | 1.1538 | .66805 | .74412 | .89777 | 1.1139 | 5 |
| 56 | 190 | 679 | 712 | .1946 | 518 | 547 | 725 | .1531 | 827 | 392 | 830 | .1132 | 4 |
| 57 | 212 | 661 | 761 | .1939 | 540 | 528 | 776 | .1524 | 848 | 373 | 883 | .1126 | 3 |
| 58 | 234 | 642 | 811 | .1932 | 562 | 509 | 827 | .1517 | 870 | 353 | 935 | .1119 | 2 |
| 59 | 256 | 623 | 860 | .1925 | 584 | 490 | 878 | .1510 | 891 | 334 | 988 | .1113 | 1 |
| 60 | .64279 | .76604 | .83910 | 1.1918 | .65606 | .75471 | .86929 | 1.1504 | .66913 | .74314 | .90040 | 1.1106 | 0 |
| | Cos. | Sin. | Cot. | Tan | Cos | Sin. | Cot. | Tan. | Cos. | Sin. | Cot. | Tan. | M. |

50°

49°

48°

42°

43°

44°

| M. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | Sin. | Cos. | Tan. | Cot. | M. |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|---------|--------|----|
| 0 | .66913 | .74314 | .90040 | 1.1106 | .68200 | .73135 | .93252 | 1.0724 | .69466 | .71934 | .96569 | 1.0355 | 60 |
| 1 | 935 | 295 | 093 | .1100 | 221 | 116 | 306 | .0717 | 487 | 914 | 625 | .0349 | 59 |
| 2 | 956 | 276 | 146 | .1093 | 242 | 096 | 360 | .0711 | 508 | 894 | 681 | .0343 | 58 |
| 3 | 978 | 256 | 199 | .1087 | 264 | 076 | 415 | .0705 | 529 | 873 | 738 | .0337 | 57 |
| 4 | 999 | 237 | 251 | .1080 | 285 | 056 | 469 | .0699 | 549 | 853 | 794 | .0331 | 56 |
| 5 | .67021 | .74217 | .90304 | 1.1074 | .68306 | .73036 | .93524 | 1.0692 | .69570 | .71833 | .96850 | 1.0325 | 55 |
| 6 | 043 | 198 | 357 | .1067 | 327 | 016 | 578 | .0686 | 591 | 813 | 907 | .0319 | 54 |
| 7 | 064 | 178 | 410 | .1061 | 349 | .72996 | 633 | .0680 | 612 | 792 | 963 | .0313 | 53 |
| 8 | 086 | 159 | 463 | .1054 | 370 | 976 | 688 | .0674 | 633 | 772 | .97020 | .0307 | 52 |
| 9 | 107 | 139 | 516 | .1048 | 391 | 957 | 742 | .0668 | 654 | 752 | 076 | .0301 | 51 |
| 10 | .67129 | .74120 | .90569 | 1.1041 | .68412 | .72937 | .93797 | 1.0661 | .69675 | .71732 | .97133 | 1.0295 | 50 |
| 11 | 151 | 100 | 621 | .1035 | 434 | 917 | 852 | .0655 | 696 | 711 | 189 | .0289 | 49 |
| 12 | 172 | 080 | 674 | .1028 | 455 | 897 | 906 | .0649 | 717 | 691 | 246 | .0283 | 48 |
| 13 | 194 | 061 | 727 | .1022 | 476 | 877 | 961 | .0643 | 737 | 671 | 302 | .0277 | 47 |
| 14 | 215 | 041 | 781 | .1016 | 497 | 857 | .94016 | .0637 | 758 | 650 | 359 | .0271 | 46 |
| 15 | .67237 | .74022 | .90834 | 1.1009 | .68518 | .72837 | .94071 | 1.0630 | .69779 | .71630 | .97416 | 1.0265 | 45 |
| 16 | 258 | 002 | 887 | .1003 | 539 | 817 | 125 | .0624 | 800 | 610 | 472 | .0259 | 44 |
| 17 | 280 | .73983 | 940 | .0996 | 561 | 797 | 180 | .0618 | 821 | 590 | 529 | .0253 | 43 |
| 18 | 301 | 963 | 993 | .0990 | 582 | 777 | 235 | .0612 | 842 | 569 | 586 | .0247 | 42 |
| 19 | 323 | 944 | .91046 | .0983 | 603 | 757 | 290 | .0606 | 862 | 549 | 643 | .0241 | 41 |
| 20 | .67344 | .73924 | .91099 | 1.0977 | .68624 | .72737 | .94345 | 1.0599 | .69883 | .71529 | .97700 | 1.0235 | 40 |
| 21 | 366 | 904 | 153 | .0971 | 645 | 717 | 400 | .0593 | 904 | 508 | 756 | .0230 | 39 |
| 22 | 387 | 885 | 206 | .0964 | 666 | 697 | 455 | .0587 | 925 | 488 | 813 | .0224 | 38 |
| 23 | 409 | 865 | 259 | .0958 | 688 | 677 | 510 | .0581 | 946 | 468 | 870 | .0218 | 37 |
| 24 | 430 | 846 | 313 | .0951 | 709 | 657 | 565 | .0575 | 966 | 447 | 927 | .0212 | 36 |
| 25 | .67452 | .73826 | .91366 | 1.0945 | .68730 | .72637 | .94620 | 1.0569 | .69987 | .71427 | .97984 | 1.0206 | 35 |
| 26 | 473 | 806 | 419 | .0939 | 751 | 617 | 676 | .0562 | .70008 | 407 | .98041 | .0200 | 34 |
| 27 | 495 | 787 | 473 | .0932 | 772 | 597 | 731 | .0556 | 029 | 386 | 098 | .0194 | 33 |
| 28 | 516 | 767 | 526 | .0926 | 793 | 577 | 786 | .0550 | 049 | 366 | 155 | .0188 | 32 |
| 29 | 538 | 747 | 580 | .0919 | 814 | 557 | 841 | .0544 | 070 | 345 | 213 | .0182 | 31 |
| 30 | .67559 | .73728 | .91633 | 1.0913 | .68835 | .72537 | .94896 | 1.0538 | .70091 | .71325 | .98270 | 1.0176 | 30 |
| 31 | 580 | 708 | 687 | .0907 | 857 | 517 | 952 | .0532 | 112 | 305 | 327 | .0170 | 29 |
| 32 | 602 | 688 | 740 | .0900 | 878 | 497 | .95007 | .0526 | 132 | 284 | 384 | .0164 | 28 |
| 33 | 623 | 669 | 794 | .0894 | 899 | 477 | 062 | .0519 | 153 | 264 | 441 | .0158 | 27 |
| 34 | 645 | 649 | 847 | .0888 | 920 | 457 | 118 | .0513 | 174 | 243 | 499 | .0152 | 26 |
| 35 | .67666 | .73629 | .91901 | 1.0881 | .68941 | .72437 | .95173 | 1.0507 | .70195 | .71223 | .98556 | 1.0147 | 25 |
| 36 | 688 | 610 | 955 | .0875 | 962 | 417 | 229 | .0501 | 215 | 203 | 613 | .0141 | 24 |
| 37 | 709 | 590 | .92008 | .0869 | 983 | 397 | 284 | .0495 | 236 | 182 | 671 | .0135 | 23 |
| 38 | 730 | 570 | 062 | .0862 | .69004 | 377 | 340 | .0489 | 257 | 162 | 728 | .0129 | 22 |
| 39 | 752 | 551 | 116 | .0856 | 025 | 357 | 395 | .0483 | 277 | 141 | 786 | .0123 | 21 |
| 40 | .67773 | .73531 | .92170 | 1.0850 | .69046 | .72337 | .95451 | 1.0477 | .70298 | .71121 | .98843 | 1.0117 | 20 |
| 41 | 795 | 511 | 224 | .0843 | 067 | 317 | 506 | .0470 | 319 | 100 | 901 | .0111 | 19 |
| 42 | 816 | 491 | 277 | .0837 | 088 | 297 | 562 | .0464 | 339 | 080 | 958 | .0105 | 18 |
| 43 | 837 | 472 | 331 | .0831 | 109 | 277 | 618 | .0458 | 360 | 059 | .99016 | .0099 | 17 |
| 44 | 859 | 452 | 385 | .0824 | 130 | 257 | 673 | .0452 | 381 | 039 | 073 | .0094 | 16 |
| 45 | .67880 | .73432 | .92439 | 1.0818 | .69151 | .72236 | .95729 | 1.0446 | .70401 | .71019 | .99131 | 1.0088 | 15 |
| 46 | 901 | 413 | 493 | .0812 | 172 | 216 | 785 | .0440 | 422 | .70998 | 189 | .0082 | 14 |
| 47 | 923 | 393 | 547 | .0805 | 193 | 196 | 841 | .0434 | 443 | 978 | 247 | .0076 | 13 |
| 48 | 944 | 373 | 601 | .0799 | 214 | 176 | 897 | .0428 | 463 | 957 | 304 | .0070 | 12 |
| 49 | 965 | 353 | 655 | .0793 | 235 | 156 | 952 | .0422 | 484 | 937 | 362 | .0064 | 11 |
| 50 | .67987 | .73333 | .92709 | 1.0786 | .69256 | .72136 | .96008 | 1.0416 | .70505 | .70916 | .99420 | 1.0058 | 10 |
| 51 | .68008 | 314 | 763 | .0780 | 277 | 116 | 064 | .0410 | 525 | 896 | 478 | .0052 | 9 |
| 52 | 029 | 294 | 817 | .0774 | 298 | 095 | 120 | .0404 | 546 | 875 | 536 | .0047 | 8 |
| 53 | 051 | 274 | 872 | .0768 | 319 | 075 | 176 | .0398 | 567 | 855 | 594 | .0041 | 7 |
| 54 | 072 | 254 | 926 | .0761 | 340 | 055 | 232 | .0392 | 587 | 834 | 652 | .0035 | 6 |
| 55 | .68093 | .73234 | .92980 | 1.0755 | .69361 | .72035 | .96288 | 1.0385 | .70608 | .70813 | .99710 | 1.0029 | 5 |
| 56 | 115 | 215 | .93034 | .0749 | 382 | 015 | 344 | .0379 | 628 | 793 | 768 | .0023 | 4 |
| 57 | 136 | 195 | 088 | .0742 | 403 | .71995 | 400 | .0373 | 649 | 772 | 826 | .0017 | 3 |
| 58 | 157 | 175 | 143 | .0736 | 424 | 974 | 457 | .0367 | 670 | 752 | 884 | .0012 | 2 |
| 59 | 179 | 155 | 197 | .0730 | 445 | 954 | 513 | .0361 | 690 | 731 | 942 | .0006 | 1 |
| 60 | .68200 | .73135 | .93252 | 1.0724 | .69466 | .71934 | .96569 | 1.0355 | .70711 | .70711 | 1.00000 | 1.0000 | 0 |
| | Cos. | Sin. | Cot. | Tan. | Cos. | Sin. | Cot. | Tan. | Cos. | Sin. | Cot. | Tan. | M. |

47°

46°

45°

AUXILIARY TABLE FOR SMALL ANGLES.

0°

1°

2°

3°

4°

| M. | Sin. | Tan. | Sin. | Tan. | Sin. | Tan. | Sin. | Tan. | Sin. | Tan. | M. |
|----|------|------|------|------|------|------|------|------|------|------|----|
| | 4.68 | | 4.68 | | 4.68 | | 4.68 | | 4.68 | | |
| 0 | 5575 | 5575 | 5553 | 5619 | 5487 | 5751 | 5376 | 5972 | 5222 | 6281 | 0 |
| 1 | 5575 | 5575 | 5552 | 5620 | 5485 | 5754 | 5374 | 5976 | 5219 | 6287 | 1 |
| 2 | 5575 | 5575 | 5551 | 5622 | 5484 | 5757 | 5372 | 5981 | 5216 | 6293 | 2 |
| 3 | 5575 | 5575 | 5551 | 5623 | 5482 | 5760 | 5370 | 5985 | 5213 | 6299 | 3 |
| 4 | 5575 | 5575 | 5550 | 5625 | 5481 | 5763 | 5367 | 5990 | 5210 | 6305 | 4 |
| 5 | 5575 | 5575 | 5549 | 5627 | 5479 | 5766 | 5365 | 5994 | 5207 | 6311 | 5 |
| 6 | 5575 | 5575 | 5548 | 5628 | 5478 | 5769 | 5363 | 5999 | 5204 | 6317 | 6 |
| 7 | 5575 | 5575 | 5547 | 5630 | 5476 | 5773 | 5361 | 6004 | 5201 | 6323 | 7 |
| 8 | 5574 | 5576 | 5547 | 5632 | 5475 | 5776 | 5358 | 6008 | 5198 | 6329 | 8 |
| 9 | 5574 | 5576 | 5546 | 5633 | 5473 | 5779 | 5356 | 6013 | 5195 | 6335 | 9 |
| 10 | 5574 | 5576 | 5545 | 5635 | 5471 | 5782 | 5354 | 6017 | 5192 | 6341 | 10 |
| 11 | 5574 | 5576 | 5544 | 5637 | 5470 | 5785 | 5351 | 6022 | 5189 | 6348 | 11 |
| 12 | 5574 | 5577 | 5543 | 5638 | 5468 | 5788 | 5349 | 6027 | 5186 | 6354 | 12 |
| 13 | 5574 | 5577 | 5542 | 5640 | 5467 | 5792 | 5347 | 6031 | 5183 | 6360 | 13 |
| 14 | 5574 | 5577 | 5541 | 5642 | 5465 | 5795 | 5344 | 6036 | 5180 | 6366 | 14 |
| 15 | 5573 | 5578 | 5540 | 5644 | 5463 | 5798 | 5342 | 6041 | 5177 | 6372 | 15 |
| 16 | 5573 | 5578 | 5539 | 5646 | 5462 | 5802 | 5340 | 6046 | 5173 | 6379 | 16 |
| 17 | 5573 | 5578 | 5539 | 5648 | 5460 | 5805 | 5337 | 6051 | 5170 | 6385 | 17 |
| 18 | 5573 | 5579 | 5538 | 5649 | 5458 | 5808 | 5335 | 6055 | 5167 | 6391 | 18 |
| 19 | 5573 | 5579 | 5537 | 5651 | 5457 | 5812 | 5332 | 6060 | 5164 | 6398 | 19 |
| 20 | 5572 | 5580 | 5536 | 5653 | 5455 | 5815 | 5330 | 6065 | 5161 | 6404 | 20 |
| 21 | 5572 | 5580 | 5535 | 5655 | 5453 | 5818 | 5327 | 6070 | 5158 | 6410 | 21 |
| 22 | 5572 | 5581 | 5534 | 5657 | 5451 | 5822 | 5325 | 6075 | 5154 | 6417 | 22 |
| 23 | 5572 | 5581 | 5533 | 5659 | 5450 | 5825 | 5322 | 6080 | 5151 | 6423 | 23 |
| 24 | 5571 | 5582 | 5532 | 5661 | 5448 | 5829 | 5320 | 6085 | 5148 | 6430 | 24 |
| 25 | 5571 | 5583 | 5531 | 5663 | 5446 | 5833 | 5317 | 6090 | 5145 | 6436 | 25 |
| 26 | 5571 | 5583 | 5530 | 5665 | 5444 | 5836 | 5315 | 6095 | 5141 | 6443 | 26 |
| 27 | 5570 | 5584 | 5529 | 5668 | 5443 | 5840 | 5312 | 6100 | 5138 | 6449 | 27 |
| 28 | 5570 | 5584 | 5527 | 5670 | 5441 | 5843 | 5310 | 6105 | 5135 | 6456 | 28 |
| 29 | 5570 | 5585 | 5526 | 5672 | 5439 | 5847 | 5307 | 6110 | 5132 | 6462 | 29 |
| 30 | 5569 | 5586 | 5525 | 5674 | 5437 | 5851 | 5305 | 6116 | 5128 | 6469 | 30 |
| 31 | 5569 | 5587 | 5524 | 5676 | 5435 | 5854 | 5302 | 6121 | 5125 | 6476 | 31 |
| 32 | 5569 | 5587 | 5523 | 5679 | 5433 | 5858 | 5300 | 6126 | 5122 | 6482 | 32 |
| 33 | 5568 | 5588 | 5522 | 5681 | 5431 | 5862 | 5297 | 6131 | 5118 | 6489 | 33 |
| 34 | 5568 | 5589 | 5521 | 5683 | 5430 | 5866 | 5294 | 6136 | 5115 | 6496 | 34 |
| 35 | 5567 | 5590 | 5520 | 5685 | 5428 | 5869 | 5292 | 6142 | 5112 | 6503 | 35 |
| 36 | 5567 | 5591 | 5518 | 5688 | 5426 | 5873 | 5289 | 6147 | 5108 | 6509 | 36 |
| 37 | 5566 | 5592 | 5517 | 5690 | 5424 | 5877 | 5286 | 6152 | 5105 | 6516 | 37 |
| 38 | 5566 | 5593 | 5516 | 5693 | 5422 | 5881 | 5284 | 6158 | 5101 | 6523 | 38 |
| 39 | 5566 | 5593 | 5515 | 5695 | 5420 | 5885 | 5281 | 6163 | 5098 | 6530 | 39 |
| 40 | 5565 | 5594 | 5514 | 5697 | 5418 | 5889 | 5278 | 6168 | 5095 | 6537 | 40 |
| 41 | 5565 | 5595 | 5512 | 5700 | 5416 | 5893 | 5276 | 6174 | 5091 | 6544 | 41 |
| 42 | 5564 | 5596 | 5511 | 5702 | 5414 | 5897 | 5273 | 6179 | 5088 | 6551 | 42 |
| 43 | 5564 | 5597 | 5510 | 5705 | 5412 | 5900 | 5270 | 6185 | 5084 | 6557 | 43 |
| 44 | 5563 | 5599 | 5509 | 5707 | 5410 | 5905 | 5266 | 6190 | 5081 | 6564 | 44 |
| 45 | 5562 | 5600 | 5507 | 5710 | 5408 | 5909 | 5265 | 6196 | 5077 | 6571 | 45 |
| 46 | 5562 | 5601 | 5506 | 5713 | 5406 | 5913 | 5262 | 6201 | 5074 | 6578 | 46 |
| 47 | 5561 | 5602 | 5505 | 5715 | 5404 | 5917 | 5259 | 6207 | 5070 | 6585 | 47 |
| 48 | 5561 | 5603 | 5503 | 5718 | 5402 | 5921 | 5256 | 6212 | 5067 | 6593 | 48 |
| 49 | 5560 | 5604 | 5502 | 5720 | 5400 | 5925 | 5254 | 6218 | 5063 | 6600 | 49 |
| 50 | 5560 | 5605 | 5501 | 5723 | 5398 | 5929 | 5251 | 6224 | 5060 | 6607 | 50 |
| 51 | 5559 | 5607 | 5499 | 5726 | 5396 | 5933 | 5248 | 6229 | 5056 | 6614 | 51 |
| 52 | 5558 | 5608 | 5498 | 5729 | 5394 | 5937 | 5245 | 6235 | 5053 | 6621 | 52 |
| 53 | 5558 | 5609 | 5497 | 5731 | 5392 | 5942 | 5242 | 6241 | 5049 | 6628 | 53 |
| 54 | 5557 | 5611 | 5495 | 5734 | 5389 | 5946 | 5239 | 6246 | 5045 | 6635 | 54 |
| 55 | 5556 | 5612 | 5494 | 5737 | 5387 | 5950 | 5237 | 6252 | 5042 | 6643 | 55 |
| 56 | 5556 | 5613 | 5492 | 5740 | 5385 | 5955 | 5234 | 6258 | 5038 | 6650 | 56 |
| 57 | 5555 | 5615 | 5491 | 5743 | 5383 | 5959 | 5231 | 6264 | 5034 | 6657 | 57 |
| 58 | 5554 | 5616 | 5490 | 5745 | 5381 | 5963 | 5228 | 6269 | 5031 | 6665 | 58 |
| 59 | 5554 | 5618 | 5488 | 5748 | 5379 | 5968 | 5225 | 6275 | 5027 | 6672 | 59 |
| M. | Sin. | Tan. | Sin. | Tan. | Sin. | Tan. | Sin. | Tan. | Sin. | Tan. | M. |

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