



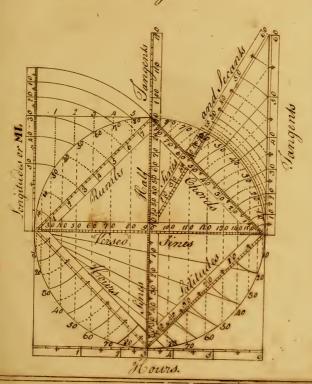
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T R E A T I S E

SHIP-BUILDING

AND

NAVIGATION.

IN THREE PARTS

WHEREIN

The Theory, Practice, and Application of all the necessary instruments are perspicuously handled.

WITH

The Construction and Use of a new invented Shipwright's Sector, for readily laying down and delineating Ships, whether of similar or diffimilar Forms.

ALSO

Tables of the Sun's Declination, of Meridional Parts, of difference of Latitude and Departure, of Logarithms, and of artificial Sines, Tangents and Secants.

By MUNGO MURRAY.

Shipwright, in his Majesty's Yard, DEPTFORD.

To which is added by way of Appendix,

An English Abridgment of another Treatise on Naval Architecture, lately published at Paris by M. Duhamel, Mem. of the R. Acad. of Sciences, Fellow of the Royal Society of London, and Surveyor General of the French Marine.

The whole illustrated with eighteen COPPER PLATES.

L O N D O N:

Printed by D. HENRY and R. CAVE, for the AUTHOR; and Sold by A. MILLAR, in the Strand; J. Scott, in Exchange-Alley; T. Jefferys, at the Corner of St Martin's Lane, Charing-crofs; Meff. Greid and Campbell, at Union-Stairs, and by the Author, at his Houle at Depiford.

M,DCC,LJV.

S DELIVER WELLIAMS

ADVERTISEMENT.

HE several Branches of Mathematicks treated of in this Book are expeditiously taught by the Author, at his House in *Deptford*; where may be had all Sorts of Sliding Rules and Scales: As also Sectors for delineating Ships, Diagonal Scales, &c. on Brass, Wood, or Paste-board. Attendance from fix to eight every Evening, except *Wednesdays* and *Saturdays*.

To the right Honourable the

LORDS COMMISSIONERS,

For executing the Office of

Lord HIGH ADMIRAL

O F

GREAT BRITAIN and IRELAND,

And of his Majesty's

PLANTATIONS ABROAD, &c.
THIS TREATISE

ON

SHIP-BUILDING AND NAVIGATION

Is with the utmost Submission, inscribed

By their Lordships

Most dutiful,

Most humble, and

Most obedient Servant

MUNGO MURRAY.

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PREFACE.

THOUGH the art of Ship-building is of the utmost consequence to the trade and security of this nation, and a competent knowledge of the theory of it necessary for every Shipwright, yet I cannot think of a subject which

has been so little treated of in our language.

This confideration induced me to offer the following sheets to the publick, which are calculated for the instruction and improvement of shipwrights in the art of delineating or drawing of ships, being fully persuaded that any thing which may be conducive to this end must be of great service to the publick in general. I therefore flatter myself that this attempt will meet with a favourable reception, though it were to be wished it had been undertaken by some person of abilities greatly superior to mine.

In order to make this treatife as ufeful as possible, I have briefly explained the nature of proportion, the principles of geometry, the invention of logarithms, and their use in the construction of the line of numbers, by which, I presume, any person that is acquainted with common arithmetick, may, with a little application, be able to construct the lines himfelf, and have a clear idea of all the operations by the sliding rule, in measuring surfaces and solids; a method so expedient and useful, that it is universally practised in measuring all the plank

plank and timber received into his majesty's yards, and used not only by shipwrights, but by many other artificers, as

joiners, painters, &c.

The divisions on the line of numbers, in plate No. II. are taken from the scale of equal parts in the same plate, which is divided in the exactest manner, and may be of great use to the reader, not only in comparing the distances measured on the scale with the table of logarithms, in order to examine how the lines have been graduated, but also in the construction of geometrical figures, as any given or required distances may

be measured by it to a very great accuracy.

Tho' it must be allowed that the principles of geometry, trigonometry, logarithms, and their various uses, have been sufficiently explained by many eminent authors who have wrote on these subjects, yet I thought it requisite to treat concisely of them here, as introductory to the main design, which is to instruct the Shipwright to form all his work by mathematical rules; and, as he is surnished with every thing that is necessary in this treatise, I have no occasion to refer him to other books, with which perhaps he might not be furnished if I did.

In the fecond part, I have endeavoured to explain the method of representing solids upon a plane, with the application thereof to the delineating of ships, in which I have given definitions of all the terms and lines made use of in drawing; I have also shewn the methods that are generally practised, and the difficulties and inconveniences attending them, which I have endeavoured to facilitate by a sector of my own invention, constructed for that purpose; a method entirely new, and, though deduced from mathematical principles, does not restrain the artist from displaying all the skill and judg-

judgment he is mafter of in varying the form of the curves so as to be most suitable for the service for which the ship is

designed.

The third part contains land furveying, geography and navigation, with an analemma divided in so curious and accurate a manner, that by a nonnius division the pole may be set to any latitude, even to three minutes, and all the problems that are usually solved by the globe may be performed with greater exactness by this instrument. I have also shewn the method of constructing the plain and Mercator's charts, the manner of keeping a reckoning, and of finding the latitude and variation of the compass by coelestial observation; to which I have added tables of the sun's declination, of difference of latitude and departure, of meridional parts, of logarithms, and of artificial sines, tangents, and secants.

Tho' it may be the opinion of many that this 3d part, with the tables, might have been omitted, as having no necessary connection with the theory of Ship building, yet, as I was defirous of making this treatise universally useful, I thought it requisite it should contain them, though it would have been

my interest to have done otherwise.

Some time after the first, and most of the second part had been in the press, a treatise in French on the same subject, by the ingenious M. du Hamel du Monceau, Member of the Royal Academy of Sciences at Paris, and Fellow of the Royal Society at London, sell into my hands, and, as I imagined that every body would be desirous of seeing what has been wrote on Ship building, by a foreign author of such distinction, I have added, by way of appendix, an abridgment of that work, which I doubt not will be agreeable to such as are not acquainted with the French language, or have no opportunity of perusing the original.

I flatter myfelf, from the high repute Mons. Du Hamel's writings have every where justly acquir'd, that the additional price of 2s. 6d. for the English abridgment of his book on Ship-building, annexed to mine, will not be thought much of, when it is considered that the original fells for 18 s.

I cannot conclude this preface, without acknowledging the great obligation I am under to the principal officers and gentlemen in his majefty's fervice, not only in the yard where I have the happiness to be employed, but in several others, as well as in the navy, for their kindness in encouraging this work, several of them persons, whose abilities are such, that it would be the greatest vanity in me to imagine they would countenance the undertaking on account of any information they could expect to derive from it themselves; their true motives were doubtless a consciousness of the important service of such a piece to young shipwrights, and a generous disposition to encourage industry.

I believe it will appear very obvious to every body, that I have fpared no pains or cost in endeavouring to render this work as compleat as possible, to which end I have submitted the mathematical part thereof to the perusal and amendment of a gentleman whose abilities in these matters would be indisputable with the publick, were I permitted to name him.

The fuccess of my labour I rest entirely on the judgment and candour of my readers, by which I must stand or fall; whatever may be the event, I shall always have the secret satisfaction of ressecting, that I have sincerely aimed at what is useful, and very much wanted in the English language.

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THE THEORY OF

SHIPBUILDING and NAVIGATION.

PART I.

CHAP. I. SECT. I. Samuel Child Of Involution and Evolution of Quantities.

F a number be multiplied by itself, and the product by the same number, and the new product again by the same, and so on, it is said to be involved into itself so many times, and the several products are distinguished into powers of different denominations, of all which the original number is called the root; the first product being its second power or square; the second the third power, or cube; the third the sourth power, or biquadrate, &c. These powers are usually denoted by a small sigure annexed above the last digit of the root. Thus 12° signifies the second power or square of the root 12, being equal to 144; 12° the third power, or cube thereof, equal to 1728, &c. and so the several powers may be orderly expressed thus, 12,12°, 12°, 12°, &c. that is, 12 root, 12×12=144 square, 12×12×12=1728 cube, 12×12×12 ×12=20736, biquadrate, &c.

Square and cube numbers have borrowed their denominations from geometrical figures or extensions, the root being represented by a right line, which has but one dimension, viz, lengh; the square by a plane, or right lined figure of two dimensions, having equal length and breadth; and the cube by a right lined solid of three dimensions, having equal

length, breadth, and thickness.

The nature of space admits of no other modes of extension, than length, breadth, and thickness, neither is it possible to conceive any body otherwise to exist than under these limitations.

That the reader may have a distinct idea of the method of extracting

gú

the square and cube roots, we think it necessary to make the following remarks on multiplication, and to shew how any root, by being divided into two parts (or made a binomial) may be raifed to the fecond or third

power, &cc.

Since multiplication may be confidered as a manifold addition, it is certain that if either or both multiplicand and multiplier be divided into parts, and all the parts of the one be multiplied by all the parts of the other, the fum of all the products will be equal to the product of the whole multiplicand multiplied by the whole multiplier, and this method is what is in effect performed by the common rule, when either or both confift of more than one fignificant figure, as will appear by the following examples, viz.

EXAMPLE

Let the number 24 be divided into two parts, viz. 20 and 4, and multiplied by 4.

20 + 4 = 24 By the common rule
4 4 4 16
$$80 + 16 = 96$$
 4 × 20 = 80
 96

EXAMPLE II.

Let the number 248 be divided into three parts, viz. 200, 40, and 8, and multiplied by 24 or 20-4.

$$\begin{array}{rcl}
200 + 40 + 8 & = & 248 \\
20 + 4 & = & 24 \\
4 \times 200 + 4 \times 40 + 4 \times 8 \\
20 \times 200 + 20 \times 40 + 20 \times 8 & 496 \\
20 \times 200 + 20 \times 40 + 4 \times 40 + 4 \times 8 & = 5952
\end{array}$$

By the common rule.

$$4 \times 8 = 32
4 \times 40 = 160
4 \times 200 = 800
20 \times 8 = 160
20 \times 40 = 800
20 \times 200 = 4000
5952$$

Though there is no occasion to fet down the several products, as in the above examples, because the excess above the tens may be retained in the memory, and added to the next place, which is always the method observed in practice; yet this will very much affift us in perceiving the reason of the rules for extracting the square and cube roots of any numbers, by carefully observing the steps by which any root is raised to those powers, as in the following example, viz.

Let the root be 24 = 20 + 4.

Square, or fecond power,
$$\frac{20 + 4}{4 \times 20 + 4 \times 4}$$

or $20 \times 20 + 4 \times 20$
 $20 \times 20 + 4 \times 20 + 4 \times 20$
or $20^2 + 2 \times 4 \times 20 + 4^2$
 $= 576$
 $= 24$
 $= 4 \times 4 = 16$
 $= 4 \times 20 = 80$
 $= 4 \times 20 = 80$
 $= 4 \times 20 = 80$
 $= 20 \times 20 = 400$
 $= 576$

It is evident from this operation, that any fquare number whose root is divided into two parts, is equal to the sum of the squares of those parts, and double their product added together.

This observation will hold equally true when the root consists of more than two figures, by repeating the process for every fignificant figure, as in the following example, viz.

Let the root be 2435, or 2000 + 400 + 30 + 5

		2 x 2000 x 400 = 1600000
ift, suppose the	root 2400	400° = 160000
binomial parts	2000 + 400	$2400^2 = 5760000$
2d, root	2430	2 x 2400 x 30 = 144000
binomial parts	2400 + 30	30° = 900
gd, root	2435	2430° = 5904900
binomial parts	2430 + 5	$2 \times 2430 \times 5 = 24300$
The Parts	-15-15	$5^2 = 25$
		$2435^2 = 5020235$

By this method it is plain, that we find a fquare for every figure in the root, and that in finding the fquare of the first figures, we suppose all the rest to be cyphers, and so on till the whole square is composed by the addition of one significant figure after each operation.

B 2

20002 = 4000000

Note, That for every figure that is annexed to the first figure in the root, there will be two in the square; thus, 2' is 4, 20' is 400, 200' is 400000, 2000' is 4000000, &c.

In like manner the cube of any number may be found, by dividing

the root into parts, as in the following example, viz.

Let the root be 24, or 20+4, as before.

Then the fquare will be
$$20^{2} + 2 \times 20 \times 4 + 4^{2}$$
 $20 + 4 \text{ root}$ $20 \times 4 + 2 \times 20 \times 4^{2} + 4^{2}$ $20 \times 4^{2} + 2 \times 20^{2} \times 4 + 20 \times 4^{2}$ $20 \times 4^{2} + 20 \times 4^{2} + 20 \times 4^{2}$ $20 \times 4^{2} + 20 \times 4^{$

Cube, or third power $20^3 + 3 \times 20^2 \times 4 + 3 \times 20 \times 4^2 + 4^3 = \text{cube of } 24 = 13824$

Hence it appears, that if any root be divided into two parts, the cube will be composed of the four following sums, viz.

1/1, The cube of the first part.

2d, Three times the square of the first part multiplied, by the second part.

3d, Three times the first part, multiplied by the square of the second part.

4th, The cube of the second part.

If the root confifts of more than two figures, the same method may be observed as in composing the square, by taking the two first figures for one part, and the next figure for the other part, and so on till all the significant figures are brought in. This is so plain, that we think it needless to give any example here; and as the only use we shall make of it will be to shew how to extract the cube root, we shall just observe under this head, that for every figure annexed to the first figure in the root, there will be three in the cube, besides the cube of the first figure; thus, 2¹ is 8, 20³ is 8000, 200³ is 800000, &c.

S E C T. II.

Evolution of Quantities.

Volution is the unfolding, or refolving of any number into the parts of which it is composed, and is called the extraction of the root of any given power; by means of which, we find a number, that being multiplied by itself as many times less one, as the index of the power contains units, will produce the given number.

In order to this, the method already observed, and the steps taken in the involution of the binomial root must be carefully attended to, in which it will not be difficult to discern how each part of the root is concerned in the power.

To Extract the SQUARE ROOT.

As the fquare was composed by multiplication and addition, the root

must be found by division and subtraction.

When the root of any number is required, the first thing to be done is to prepare it, by points set over such places as the index of the power directs, always beginning at unity, and proceeding towards the left hand, if the given number (which we shall call the resolvend) be integers, and towards the right hand, in decimal parts; now the index of the square being 2, there must be a point over every second signre, as in the following example, viz.

Let the given number be 5929225

Having pointed the given resolvend as above, to find the first figure take the greatest root that is contained in the first period, which in this case is 2000, the square of which is 4000000. Subtract this from the resolvend 5929225, and there will remain 1929225, which is called the first dividend.

Now this number contains double the product of the first figure multiplied by the second figure, and the square of the second figure, as is

evident from the method we used in composing the square.

Divide this dividend, therefore, by double the first figure, and the quotient will be the second figure, provided that when it is multiplied by double the first figure, and the product added to the square of the second figure, the sum does not exceed the dividend. In this example 4000 is double the first figure in the root, and when this is made a divisor to the dividend, the quotient will be 400.

In the next place, multiply this fecond figure by double the first, or which is the same thing, by the divisor, and add the square thereof to the product, and their sum will be 1760000; subtract this from the di-

vidend, the remainder will be 169225, the fecond dividend.

And now we have in effect subtracted the square of the first two figures; for in the first step we subtracted 2000, and in the next 2×2000 ×400+400, all which make 2400. The second dividend will therefore contain double the product of the first two sigures multiplied by the third, and the square of the same third sigure. Therefore,

To find the third figure, double the first two figures for a divisor to

this dividend, and the quotient will be 30; multiply this by the divifor, and add the square of the quotient to the product; the sum will be 144900. When this is subtracted from the dividend, the remainder will be 24325, the third dividend; to which there must be a new divifor found by doubling the figures already found in the root, and the quotient will be 5, the fourth figure. And by observing the same method as before in the operation, there will be no remainder, so that 2435 will be the true root required.

Refolvend 5929225
$$2000^{2} = 4000000$$
1/f divifor $2000 \times 2 = 4000)1929225$

$$4000 \times 400 = 1600000$$

$$400^{2} = 160000$$

$$400^{2} = 160000$$
2d divifor $2400 \times 2 = 4800$) 169225

$$4800 \times 30 = 144000$$

$$30^{2} = 900$$

$$3d \text{ divifor } 2430 \times 2 = 4860$$
) 24325

$$3d \text{ dividend}$$

$$4860 \times 5 = 24300$$

$$5^{2} = 25$$

$$24325$$

By comparing this operation with that by which the square number 5929225 was composed as above, the reader will observe, that the same numbers that were there added together to make up that sum, are hereby regularly subtracted from it. So that this method of discovering the root is only the reverse of that by which it was raised.

We shall conclude this head with observing, that there is no necessity in practice for annexing all the cyphers to the divisors and dividends, nor of subtracting the square of the first figure from the whole resolvend; but the several periods which it consists of, may be brought down one at a time, as in the following example, viz.

Refolvend
$$179409850624(423568 \text{ root} \frac{16}{16} = \text{greateft fiquare in } 17$$

1st divifor 82) 194

2 $164 = 82 \times 2$

2d divifor 843) 3009

3 $2529 = 843 \times 3$

3d divifor 8465) 48085

42325 8465×5

41b divifor 84706) 576006

6 6

508236 $= 84706 \times 6$

51b divifor 847128) 6777024

8 6777024

8 6777024

8 6777024

Observe always, that after having doubled the root in the quotient for a divisor, we are to enquire how oft it may be had in the dividend; so as when the quotient figure is annexed to the divisor, and that increased divisor multiplied by the same quotient figure, the product may be the greatest number that can be had in the dividend: And so proceed from period to period till the whole is finished.

By pursuing this method in extracting the root of the square number 5020225, the reader will observe that the operation is exactly the same

as before, omitting the cyphers.

To Extract the Cube ROOT.

We shall observe the same method in extracting the cube root, as we have done already in the square root; that is, by considering it as divided into two parts in different operations, till we have discovered all the fignificant figures thereof.

Let the number, or resolvend, whose cube root is required be

13824.

When it is properly pointed as above, it appears that the root will con-

fift of two figures.

The first figure in the root will be the greatest root that can be had in the first period 13000, which is 20; the cube of which 8000, must be subtracted from the resolvend, and the remainder will be 5824, for a dividend.

As we have already fubtracted the cube of the first part 20, this number must contain three times the square of that first part multiplied by the second part, three times the first part multiplied by the square of the second, and the cube of the second part, added together.

ther. Therefore, if this dividend be divided by three times the square of the first part = 1200, the quetient will be 4, the second figure required: Then 3 times $20^{\circ} \times 4$, 3 times $20 \times 4^{\circ}$, and 4° must be added together, and the sum subtracted from the dividend, as in the following example, viz.

Refolvend
$$13824$$
 (24 root $20^3 = 8000$
Divifor $3 \times 20^3 = 1200$) 5824
 $3 \times 20^3 \times 4 = 4800$
 $3 \times 20 \times 4^2 = 960$
 $4^3 = 64$
 64

By comparing this example with that which we have given before, where the binomial root 20 + 4 is cubed, the reader will observe, that the very same numbers which compose the cube 13824, and are there added together, are here regularly subtracted from it. This method of extracting the cube root, is, therefore, only the reverse of that by which it was raised.

We shall give one example more, without annexing cyphers to the divisors and dividends.

Let it be required to extract the cube root of 94818816

It is here to be noted, that the two last figures in the dividend must be excluded, before we enquire how often the divisor (which wants two cyphers) is contained in it, because when we proceed to find the second figure in the root, the first must be considered in the place of tens; and when we are to find the third figure, it must be considered in the place of hundreds, this will appear very plain by annexing the cyphers in the

operation.

As the divifor found by this rule, multiplied by the new figure in the root, is not all that is to be substracted from the dividend, but also three times the first part multiplied by the square of the second, and the cube of the second, as in the foregoing example; it will sometimes happen that the quotient must not be taken for the next figure in the root, thus, if the dividend 30818 be divided by 4800, the quotient will be 6, but $3\times40^5\times6+3^5\times40\times6^5+6^5=33336$ which exceeds the dividend, therefore it will be necessary formetimes to try how much the number to be substracted will amount to by the foregoing rule, before we can determine upon the new figure in the root.

If, as it often happens, a number has not a root that can be expressed by a rational number, place as many pairs of cyphers in the square, and ternaries of cyphers in the cube, on the right hand of the remainder, as you would have decimal places in the root, and work as before, distinguishing them from the integers by a comma between; and

thus you may approach infinitely near the exact root.

Mathematicians have proceeded further in the involution and evolution of quantities, viz. to the 4th, 5th, 6th, 7th, 8th, and 9th powers, called biquadrat, furfolid, square cubed, second surfolid, and biquadrat squared, but as we shall not have occasion to apply these in practice, it is sufficient barely to mention them.

How to raise a given root to any power, or to extract the root out of any given power, by the help of logarithms, shall be shewn when

we come to treat of logarithms, and their various uses.

-11-

CHAP

CHAP. II. SECT. I.

Of PROPORTION.

HE whole body of the mathematicks is chiefly concerned in comparing quantities one with another; their mutual relation is what is called proportion, which is either arithmetical or geometrical; and as quantities may be represented by numbers, or lines, we shall first con-

fider proportion with respect to numbers.

Arithmetical proportion is, when in comparing two or more numbers, the lesser is subtracted from the greater, the remainder is called the difference; and when several differences are equal, those numbers are said to be in an arithmetical proportion to one another. As if we compare 2 to 4, and 4 to 6, and 6 to 8; the difference between 2 and 4 is 2, equal to the difference between 4 and 6, and to that of 6 and 8; therefore, 2, 4, 6, 8, or 8, 6, 4, 2, or 2, 5, 8, 11, 14, or 14, 11, 8, 5, 2, are all ranks of numbers in arithmetical proportion, or in arithmetical progression continued. 2, 5, 7, 10, are also proportionals, for the difference between 5 and 2 is the same as between 10 and 7, but then, because it is not the same with the difference betwixt 7 and 5, these four numbers are said to be in a discontinued, as the former ranks are faid to be in a continued arithmetical proportion. Hence the following inferences.

1. If three quantities are in arithmetical proportion continued, the fum of the extremes is equal to the double of the mean, as in this, 8, 10, 12, where 20, the fum of the extremes 8 and 12, is equal to double of

the mean 10.

2. If four quantities are fo, the fum of the extremes is equal to the fum of the means.

as 3, 5, 7, 9, here,
$$3 + 9 = 12$$
 and $5 + 7 = 12$.

3. If never so many quantities are so proportional, the sum of the extremes is always equal to the double of the middle term, if the number of the terms be odd, or to the sum of any two terms equally distant from the extremes, as in the following series.

2, 4, 6, 8, 10, 12, 14.

$$2 + 14 = 8 \times 2 = 16$$
.
or $4 + 12 = 8 \times 2 = 16$, &c.

And this must always hold good, because the last term comprehends

the first, together with the common difference superadded, as often as the number of its place is distant from the first term: But the first term has no addition of the difference at all; and as the second term has one difference or ratio more than the first; the third one more than the second, &cc. so the last but one has one less than the last of all; the last but two one less than the last but one, &cc. whence the sum of any two of these equally distant from the extremes must be equal to the sum of the extremes, because one increases as much as the other decreases.

Therefore, the fum of any number of terms in fuch a progreffion may be had, by multiplying the fum of the extremes by half the number

of the terms.

To find the fum of never so many quantities in this progression, it is only necessary that the extremes and the number of terms be given: so that if by having the first term and the common excess you would find the last, it might be done with great dispatch, by multiplying the number of terms, lessened by unity, into the common excess, and then adding the first term to the product.

Thus, if the last term of a progression of 73 places were required, and the common difference were 4, and the first term 3; you need only multiply 72 by 4, and to the product 288 add 3, and you have 291 for the

last term in the progression.

So that if the progression begins with a cypher, which is the most natural and simple of all, then the sum of all the terms will be equal to the sum of the extremes multiplied by half the number of the terms. Thus suppose

0, 3, 6, 9, 12, 15, 18, 21, 24, 27, 30, 33, 36, 39.

The last term 39, multiplied by 14, the whole number of terms, gives 546; the half of which 273, is the sum of all the terms.

From whence it will follow, that the fum of all the terms in any fuch progression beginning from o, is half the sum of so many terms, all equal to the greatest.

S E C T. II.

Of GEOMETRICAL PROPORTION.

Eometrical proportion is when in comparing two or more numbers, one is divided by the other, the quotient is called the ratio; and when feveral ratio's are equal, the numbers are faid to be in a geometrical

pro-

proportion; thus, 2:6::5:15 are proportionals; for 6 divided by 2 is 3, and 15 divided by 5 is 3, and fo the ratio's are equal. When two numbers are compared, the former is called the antecedent, and the latter the confequent; but when more than two are compared, they are called terms, of which the first and last are called extremes, and all the intermediate ones, means. In order to know whether numbers be proportionals, it is only sinding the ratio of each pair, and here it will be indifferent whether the antecedents or consequents of every pair be made divisors, as in the preceding numbers 2:6::5:15, if 2 the antecedent be divided by 6, the consequent, the quotient is $\frac{1}{2}$, and if 5 be divided by 15, the quotient is $\frac{1}{2}$, so the ratio's are equal, as before when the antecedents were made divisors.

When in a rank of numbers they increase in a geometrical proportion, the ratio will be a common multiplier, and is found by dividing any one of the consequent terms by its antecedent, for so the quotient will be the ratio.

As { 3, 9, 27, 81, 243, &c. Here the common multiplier is 3. 2, 4, 8, 16, 32, &c. Here the common multiplier is 2.

It is plain that if either of these antecedent terms be multiplied by the

ratio, the product will be its confequent.

When a in rank of numbers they decrease in a geometrical proportion, the ratio will be a common divisor, and is found by dividing any one of the antecedent terms by its consequent.

As \ 243, 81, 27, 9, 3, &cc. Here the common divisor is 3. 32, 16, 8, 4, 2, &cc. Here the common divisor is 2.

In like manner, if either of these terms is divided by the ratio, the

quotient will be the next term in the progression.

If in comparing feveral numbers together, we find the ratio of the first and second, to be the same with the ratio of the second and third, third and sourth, fourth and fifth, and so on; those numbers are in a geometrical proportion continued.

If in comparing four numbers together, we find the ratio of the first and second to be the same as the ratio of the third and fourth, but that the ratio of the second and third is not the same; those numbers are called discontinued proportionals, as 2:4::6:12, for the progression

itops here at 4.

The manner of expressing continued proportionals is by separating the terms by two points, as 2:4:8:16:32, &c. but in discontinued proportionals the terms where the progression stops are separated by sour points, as

PROPOSITION 1.

If three numbers are in a geometrical proportion, the product of the extremes will be equal to the product of the middle term multiplied into itself, or which is the same thing, to the square of the middle term.

As in these numbers 2, 6, 18. $2 \times 18 = 6 \times 6 = 36$.

PROPOSITION II.

If four numbers are in geometrical proportion, (whether continued or discontinued) the product of the extremes will be equal to the product of the z means,

Let the numbers be 5:10:6:12 $5 \times 12 = 10 \times 6 = 60$ or 5:10:20:40 $5 \times 40 = 10 \times 20 = 200$

From these two propositions the following inferences may be drawn, viz. 1st, If the product of any two numbers is equal to the square of a third, those three numbers are in geometrical proportion continued.

2d, If the product of any two numbers is equal to the product of any other two, those four numbers are proportionals, and the numbers multiplied into each other will be either 2 means, or 2 extremes, as in the following examples, viz.

 $2 \times 16 = 4 \times 8 = 32$ 16:4 :: 8: 2 4:16:: 2: 8. &c.or $8 \times 12 = 6 \times 16 = 96$ 8:6::16:126:12::8:16, &c.

PROBLEM I.

To find a mean proportional between any two given numbers,

Note, By a mean proportional we are to understand such a number as if multiplied by itself, the product will be equal to the product of the two given numbers.

Rule, Multiply the given numbers by one another, and extract the fquare root of the product, that root will be the mean required.

Ex-

Example, Let the given numbers be 3 and 27.

 $3 \times 27 = 81$ the square root of which is 9 the mean required.

PROBLEM II.

To find a fourth proportional to the three given numbers, so that the ratio of the third and fourth may be equal to the ratio of the first and second.

Rule, Multiply the fecond number by the third, and divide the product by the first, the quotient will be the fourth number required.

Example, Let the given numbers be 2:6::7.

 $6 \times 7 = 42$, and $42 \div 2 = 21$, the fourth number required.

The reason of both these rules is evident from the two foregoing propositions, for where there are three numbers given to find a fourth, though the fourth is not known, we know that the product of it when multiplied by the first will be equal to the product of the second and third numbers, (per prop. II.) therefore, if that product is divided by the first term, the quotient will be the fourth number required. This is the foundation of the rule of three, which we suppose the reader acquainted with already.

In finding a fourth proportional where three numbers are given, the two first give the ratio, and the question as to the fourth proportional

concerns the third number.

Direct proportion is, when the greater the term is by which the question is made, the fourth term will be also the greater; and the leffer that term is, the fourth will also be the leffer.

Reciprocal, or inverse proportion is, when the greater the term is by which the question is made, the fourth will be lesser, and the lesser that

term is, the greater the fourth.

Continual proportion, thus expressed, ::, is, when all the terms between the first and the last are both antecedents and consequents in the same proportion.

Example, 8, 12, 18, 27, are :; for 8:12::12::18::18::27. Wherefore in such series, the last term subtracted from the sum of all the terms will give the sum of all the antecedents, and the first term subtracted from the said sum will give the sum of all the consequents.

If four quantities be proportional, they will also be so alternately, in-

versely, in composition, in division, conversely, and mixtly.

Example			A: B:: C: D
	A : B : : C :	D in numbers	
2, alternately	A : C :: B : 1	D.	12:8::9:6
3, inverfely	B : C :: D :		9:8::6:12
	$\{A + B : B : :$		21:9::14:6
	lA+C:C::		20:8::15:6
5, in divi-	A - B : B : :	C-D:D.	3:9::2:6
fion L	A-C:C::	B-D:D.	4:8:: 3:6
	A:A+B::	C:C+D.	12:21::8:14
6, converie-		\	12:3::8:2
ly	A : A + B : : C $A : A + C : : A$	B : B + D. {	12:20::9:15
			12:4::9:3
	+ B: A - B:: C -		21:3::14:2
ly (A-	+C:A-C::B-	+D:B-D.	20:4::15:3

All these are evidently proportionals, the product of the extremes being equal to that of the means, excepting the inverted, wherein the product of the first and second term is equal to that of the third and sourth, which is a property peculiar to that kind of proportion.

PROPOSITION III.

If the product of any two numbers is divided by a third, the quotient will be a fourth proportional, the divifor will be the first, and the numbers multiplied into each other the second and third terms in the progression.

Example, Let the given numbers be 5 and 8, and their product be di-

vided by 10, a third number:

$$5 \times 8 = 40 \div 10 = 4$$

Therefore, 10:5::8:4 (by inference 2d) for the product of the means is equal to the product of the extremes.

PROPOSITION IV.

When two numbers are multiplied into one another, they may be made mean proportionals to other two numbers, of which I must be the first, and the product of the two numbers will be the last or fourth term.

Example, Let the given numbers be 6 and 8.

It will be $1:6::8:48 = 6 \times 8 = 1 \times 48$. Hence in multiplication,

As 1 is to the multiplier, so is the multiplicand to the product; and in division, as the divisor is to 1, so is the dividend to the quotient.

PROPOSITION. V.

If any two numbers be multiplied, or divided by any same third number, the products or quotients will be proportional to the numbers so multiplied or divided. Let the numbers be 2 and 4, each to be multiplied by 3; then 3 × 2 = 6, and 3 × 4 = 12, and 2 : 4 :: 6 : 12; or if 18 and 15 be divided each by 3, the quotients will be 6 and 5, and 18 : 15 :: 6 : 5.

The powers or roots of proportionals will likewise be proportionals.

2:4::3:6 root 4:16::9:36 fquare 8:64::27:216 cube

Hitherto we have confidered the doctrine of proportion, only with refpect to numbers; but as any quantity may be represented by numbers, all that has been said with regard to them may likewise be applied to any thing that can be augmented or diminished. A line of 2 feet long has the same proportion to a line of 6 feet long that the number 2 has to 6, but the method of finding the proportions of lines, &cc. to one another requires the knowledge of the principles of geometry, which shall be the subject of the next chapter.

CHAP.

CHAP. III. SECT. II

Of GEOMETRY.

As in arithmetick we treat of numbers by comparing them to one another, without confidering their relation to any particular quantity, to in geometry we show to compare quantities to one another, and find their proportions without arithmetical calculation.

Geometry may therefore be fitly called, The science of extension abstractedly considered, without any regard to matter.

GEOMETRICAL DEFINITIONS.

Def. 1. Quantity is any thing that can be augmented or diminished, and may comprehend extension, weight, motion, &c. for one may be taken as greater or lesser, heavier, or lighter, swifter, or slower, in relation to another, of things of the same kind; but there can be no comparison between quantities of different kinds; as hours and miles; for an hour is neither greater nor less, heavier nor lighter, &c. than a mile.

Def. 2. All things that are capable of extension are to be con-

fidered either as lines, furfaces, or folids.

Def. 3. A line is a quantity of one dimension, where the length only is considered.

Def. 4. A surface is a quantity considered under two dimen-

fions, viz length and breadth.

Def. 5. A folid is that which has three dimensions, viz. length, breadth, and thickness, these two last are sometimes called height

and depth.

1 1

Def. 6. A point, in the mathematical fense, and in respect of continual quantity, is that wherein neither of the foregoing dimensions are considered. It therefore consists of no parts; for then it would be a folid, surface, or line. It is analogous to an inflant in time, which partakes neither of the past or the future. The centers of circles, &c. in diagrams are not mathematical points, but sensible objects whereby the understanding, considering them abstractedly, is affished in mathematical speculations.

D Def.

Def.

PLATE Def. 7. Parallel lines are fuch as are every where equally difl. tant from one another, as A B, and C D; for if the lines A C,

tant from one another, as AB, and CB; for it the lines AB, and BD, are equal, and are the shortest that can be drawn from the points A and B, to the line CD, the right lines AB, and CD, if infinitely produced, would be always equidistant, and confequently would never meet; but if BD were shorter or longer than AC, the lines if produced would meet.

Fig. 2. • Def. 8. An angle is the inclination of two lines that meet in a point, so as not to conflitute one strait line, and this will be the case of all strait lines that are not parallel, as the lines A B, and C D, if they are produced; they will meet in the point O, which is called the angular point; the lines that form the angle

are called the legs of the angle.

The quantity of any angle is not determined by the length of the legs that form it, but by the distance of any two points, one of them in one leg, and the other in the other, both equally remote from the angular point; now the greater this distance is, the greater will be the angle, and if there are two angles, as A O C, and $a \circ c$, and if O B, O D, $o \circ b$, $o \circ d$, are all equal to one another, then the angle A O C will be greater than the angle $a \circ c$, because the line $b \circ d$ is shorter than the line B D, and when these distances are equal, the angles will be equal.

All firait lines are measured by a rule, staff, or scale of equal parts, as inches, feet, yards, &c. but angles are measured

by arches of circles.

Fig. 3. Def. 9. Angles that are form'd by any line drawn from any point obliquely to another line, are called oblique angles; and those angles that are form'd by drawing a line from any point directly the shortest way till it meets any right line, are called

right angles.

Fig. 4. Def. 10. A perpendicular line is the shortest that can be drawn from a given point to any given line, that is, when the right line A C, standing upon the right one B D, leans unto neither part, and makes the angles A C D, A C B on both sides equal; those angles are called right ones, and the line A C is perpendicular to D B.

Hence it is evident, that if in the line D B any two points, s, t, be taken equally distant from C, and any point, f, in the line A C, be equally distant from these two points, s, t, then will

the line A C be perpendicular to D B.

Def. 11. A circle is a plain furface contained within one continued PLATE curve line, called the periphery, or circumference; and is drawn I. by fixing the point of one leg of a pair of compafes in any af- Fig. 5- fignable part of a furface, and carrying the point of the other leg round till it arrives again at the place from whence it began to move: The fixed point is called the center, and is equally diffant from all points in the circumference described by the other leg.

Def. 12. The radius or femi-diameter is a strait line drawn from the center to any part of the circumference, of which there

may be an infinite number all equal to one another.

Def. 13. The diameter is a line drawn through the center till it meets the circumference both ways, and is therefore always double the radius; there may be an infinite number of diameters all equal, they all interfect one another in one point, which is the center; so that when the intersection of any two diameters is found, the center of the circle is likewise found. The diameter is the longest strait line that can be drawn within the circle.

Def. 14. A chord is a ftrait line less than a diameter, drawn within the circle from any one point to another, both in the circumference, and cuts the circle into two unequal parts, called fegments.

Def. 15. An arch is any part of the circumference:

If a circle be cut by a diameter, the fegments are equal, and are called femicircles; and if a radius be drawn perpendicular to a diameter, it will divide the femicircle into two equal parts, called quadrants, each containing one quarter part of the whole circle. The space contained between two radii and an arch, is called a sector.

What an arch wants of a femicircle is called the fupplement of that arch, and what it wants of a quadrant is called the com-

plement thereof.

Def. 16. When an arch is the 360th part of the circumference it is called a degree; the 60th part of a degree is called a minute; the 60th part of a minute is called a fecond; and the 60th part of a fecond is called a third, &c.

It is by these degrees and minutes that all angles or arches are measured, in order to which it must be observed, that the circumference of every circle, whether great or small, is supposed

D 2

PLATE to be divided into 360 degrees; but the length of the degrees

I. of a small circle will always be less than the degrees of a large
Fig. 55 one in proportion as the radius of the one is less than the radius of the other.

To illustrate this, draw four semicircles from the center C; divide the outer one into 180 equal parts; now it is very plain that if strait lines are drawn from each of these divisions to meet all at the center, they will pass through all the inner semicircles, and

fo divide them into the same number of degrees.

A circle may be conceived to be formed by the motion of a strait line, for if one end be fastened at the center, the other end carried round till it returns to the same point where the motion began will describe the circumference; and if several points are taken in the line, as at a, b, d, f, they will each describe circumferences of circles, and C a, C b, C d, C f, will be the several semidiameters: this line is represented by a thread fastened at the center; draw the diameter A C B, this thread by its motion from the point A to the point 180 will form all the various angles that can be made by two strait lines, and will always make two angles with the diameter; from this description

the following inferences may be deduced, viz.

Inf. 1. The greatest angle that can be made by two right lines will be less than 180 degrees, for if the thread be drawn through the point A, it will then lie upon the diameter AB, and make no angle with it, but if carried to 20, the angle from A will be 20 degrees, and the angle from B will be so much less than 180 degrees, viz, 180—20=160; and as it is carried through the points 30, 40, 50, 60, 70, 80, the angle from A increases, and that from B decreases; when it comes to 90, both angles will be equal to 90 degrees, and in this position the thread will be perpendicular to the diameter; after it passes 90, the angle from A will still be increasing, and the other decreasing till the thread comes to the point B, where it again falls in with the diameter, and makes no angle; and as the arch from A to B is a semicrele, and contains 180 degrees, it is impossible to make an angle of 180 degrees by two strait lines.

Inf. 2. A right angle contains 90 degrees, and the two lines that form it are perpendicular to each other; if these lines are

produced they will make 4 angles, each 90 degrees,

Inf. 3.

inf. 3. If a right line stands upon another right line, and PLATE makes two angles with it, those two angles will be equal to two I. right ones, or 180 degrees: For if the line is perpendicular, they Fig. 55-will be equal, by the preceding; if the line is oblique, as from any point in the circumference to the center, except the point 90, suppose from 40; then from A to 40 is the measure of one angle, and from B to 40 is the measure of the other angle, but the sum of these two is 180; the angle from A to 40 is as much less as that from B is more than 90 degrees; the first is called an acute, and the last an obtuse angle.

Inf. 4. If one of the two angles formed by the meeting of two lines is known, the other may be found by fubtracting the known angle from 180 degrees, the remainder being

the other angle.

Inf. 5. If feveral right lines are drawn so as to meet in one point in another right line, the sum of all the angles will be 180 degrees, and the sum of all the angles that can be made round a point will be 360 degrees.

Inf: 6. If there are feveral equal chords in the same circle, the

arches subtended by these chords will be equal.

Def. 17. A triangle is a space contained within three lines, Fig. 6, which by their meeting form three angles: When the three lines 7.8 are strait, it is called a rectilineal triangle; when they are arches of the same circle, it is called a spherical triangle; when the three sides are equal, the triangle is called equilateral; when only two are equal, it is called isosceles; and when all the three sides are unequal, it is called scalene.

Def. 18. Quadrilateral, or four fided figures are fuch as are limited by four lines forming four angles. Such as are rectilineal

are either parallelograms or trapezia.

Def. 19. A parallelogram is a figure whose opposite sides are equal and parallel, of which there are four kinds, viz. a square,

a rectangle, a rhombus, and rhomboides.

Def. 20. A square is a figure limited by sour equal sides, all Fig. 9. perpendicular one (a) another, as ABCD; that is, a quadrilateral sigure, whose sides and angles are all equal, is called a geometrical square.

Def. 21. A rhombus is a figure that hath four equal fides, but Fig. 10. no right angle, the opposite angles being equal, viz. EGH=EFH,

and GEF = GHF, but all oblique.

Def. 22:

PLATE Def. 22. A rectangle, or a right angled parallelogram, hath four I. right angles, and its opposite sides equal and parallel, we. Fig. 11. I M = K L, and I K = M L; this figure is often called an oblong, or long square.

ig. 12. Def. 23. A rhomboides is an oblique-angled parallelogram,

and the fides that form the angles are unequal.

Fig. 13. Def. 24. Every quadrilateral figure that has neither opposite

fides, nor opposite angles equal, is called a trapezium.

A right line drawn from any angle (as D) in a four fided figure to its opposite angle (B), is called a diagonal, and divides the figure into two triangles (ABD and BCD).

Def. 25. A polygon is a figure that hath more than four fides.

and may be either regular or irregular.

Fig. 14. Def. 26. A regular polygon has all its fides and angles equal, and may be inferibed in a circle, and all the angular points (a,

b, c, d, e, f) will touch the circumference.

Regular polygons derive their names from the number of their fides or angles at the center of the circle they are inscribed in; thus a polygon of 5 sides is called a pentagon, of 6 sides a hexagon, of 7 sides a heptagon, of 8 sides an octagon, &c.

Fig. 15. Def. 27. An irregular polygon has many unequal fides, stand-

ing at unequal angles, as ABCDEFG.

All irregular polygons may be reduced to regular figures, by drawing diagonal lines in them; thus the polygon ABCDEFG, the diagonals GB, BF, FC, and CE being drawn, will be reduced to five triangles, viz. ABG, GBF, BFC, FCE, and CDE.

S E C T. II.

GEOMETRICAL PROPOSITIONS:

PROPOSITION I. PROBLEM.

Fig. 16. A T a given point in a right line, (as o), to make an angle equal to a given one, (ABC.)

Open your compasses to any convenient distance, and from B

as a center, describe an arch, as st; with the same extent de-PLATE scribe the arch fg, from the center o; then take the chord st in I. your compasses, and set it off from f to k in the arch fg, and draw the line ok, and so the angles ABC, and k of, will be

equal.

Hence an angle of any number of degrees may be made, for if with the radius of any divided circle we describe an arch (as lm) from the point C, as center, in a right line, as C B, and then take the quantity of the given angle (suppose 20 degrees) from the divided circumference of that circle by whose radius the arch was described, and set that off upon the arch from l to m, and draw the line Cm, m Cl will be the angle required; this in effect is making one angle equal to another given one, for any angle may be sound in the divided circle by drawing two semidiameters to two points of division, including the measure thereof in the circumference.

If the angle is already made, describe an arch as before to meet both fides of the angle, the extent of this arch measured upon the divided circumference will give the quantity of the

angle.

PROPOSITION II. THEOREM.

If two right lines interfect or cut one another, the opposite Fig. 17; angles will be equal; the contiguous angles, as a and c, taken together will make 180 degrees (by Inf. 3, Def. 16), but if instead of c we take d, the sum of the angles a and d will likewise be 180 degrees, therefore c and d must be equal; for the same reason, as the angles c or d, added to the angles a or b, will make 180 degrees, it will appear that those opposite angles are likewise equal.

To illustrate this by numbers, let the angle a be 30 degrees, this subtracted from 180 will leave 150, for the angle c, and the angle d will likewise by the same method be found 150, then

150 fubtracted from 180 will leave 30 for the angle b.

PROPOSITION III. THEOREM.

If a right line G H intersects two parallels, A B and CD, the Fig. 18,

opposite angles G E B, C F H, will be equal.

To prove this, as the lines AB, and CD, are parallel by conftruction, they may be confidered as one broad line, croffed by

PLATE the line G II, then the Angles G E B, and C F H, will be eL qual by the preceding, and if the angles are equal, the lines will be parallel; for fupposing A B not parallel to C D, let the line L M be drawn, and supposed parallel to C D, then will the angle G E M be equal to C F H; but this was supposed equal to G E B, therefore G E M = G E B, which is impossible.

Fig. 19. Inf. 1. If a right line, G H, cuts feveral parallels, A B, C D, E F, I K, it will make all the inward angles on the fame fide of the line equal, that is, the angles 1, 2, 3, will all be equal to the angle G R B, and therefore will be equal to one another; this will likewife hold true with regard to the angles 4, 5, 6, for they will all be equal to the angle A R G.

Fig. 18. Inf. 2. The alternate opposite angles will likewise be equal, that is, the angle AEH will be equal to DFG, which may be thus proved, GEB is equal to CFH, by this proposition; it is also equal to AEH, by prop. II. therefore AEH is equal to CFH, and CFH equal to DFG.

PROPOSITION IV. THEOREM.

Fig. 20. If the diameter or radius of a circle cuts any chord into two equal parts, it will be perpendicular thereto, and a perpendicular cutting a chord into two equal parts will pass through the center.

Let b be the middle of the chord AB, through which draw the radius CD, draw also the dotted lines CA and CB, those lines (by Def. 12.) will be equal, the points A and B are equally remote from b by supposition, and therefore the line Cb is perpendicular to AB (by Def. 10.)

Let b be the middle of the chord, and C b perpendicular to it; I say it must pass through the center, for suppose it passes through the point f, then the lines f A, and f B, would not be equal, therefore the line f B would not be perpendicular to A B, which is contrary to the supposition.

 $\bar{h}y_{i-1}^{\mu}$. The perpendicular that divides the chord into two equal parts, also divides the arch into two equal parts, for the line D b being supposed perpendicular to A B, the chords D A and D B will be equal, and therefore the arches will be equal.

Inf. 2 If two chords are biffected by two perpendiculars, those perpendiculars will intersect one another in the center of the circle.

PROP.

PROP. V. THEOREM.

PLATE

If a right line AD be drawn to touch the circumference in I. the point B, and from that point the chord BF be drawn; the Fig. 21. angle ABF, made by the chord and tangent AD, is measured by half the arch FEB, of which BF is the chord.

To demonstrate this, draw the radius CE perpendicular to the chord BF; this will biffect the chord and arch (by the preceding); fo BE is half the arch FEB, and is the measure of the angle BCE; all that remains to be proved then is, that the

angles ABF and BCE are equal.

Draw the radius C B to the point B, which will be perpendicular to the line A D, because the radius is the shortest line that can be drawn from the center to the circumference; therefore the angle A B F, together with the angle F B C, will be 90 degrees: Draw the diameter L G parallel to the chord F B, which will be perpendicular to E C; therefore the angles E C B, and B C L, taken together, will also make 90; but the angles B C L and F B C are equal, being alternate to the parallels B F and G L; and if each be subtracted from 90 degrees, the remainders E C B and A B F will be equal.

To illustrate this by numbers, let the arch FEB be 80 degrees; then the arch EB will be 40 degrees = the angle at the center (r); and because the angle ECL is 90 degrees, the angle a must be 50 degrees; again, the lines FB and GL being parallels, and the line CB crossing them, the angles a and d are alternate; the angle d must therefore be 50 degrees = a; now at the angle ABC is 90 degrees, the angle ABF must be 40,

which is half the arch F E B.

In like manner the angle FBD will be measured by half the arch FGHLB; for the line FB makes two angles with the line AD, therefore (by Inf. 3. Def. 16.) the angle FBD will be 140 degrees, which is half the arch FGHLB, for the arch FEB is 80 degrees by supposition, which subtracted from 360, the whole number of degrees in a circle, there remains 280 for the arch FGHLB, the half of which is 140.

This proposition ought to be well attended to, for the follow-

E

ing propositions will be clearly demonstrated by it.

PROP. VI. THEOREM.

PLATE An angle at the circumference of a circle is measured by half I. the opposite arch; that is, the angle BAC is measured by half

Fig. 22. the arch B D C.

To demonstrate this, draw the line GF to touch the circle at the point A, then the three angles GAB, BAC, CAF, taken together will make 180 degrees (by Inf. 5. Def. 16.); the three lines BA, AC, CB, divide the whole circumference into three arches, BEA, AIC, CDB; therefore the halves of those arches added together will make 180 degrees; but BAG is measured by half the arch BEA, and the angle FAC is measured by half the arch AIC (by the preced.) and what remains to compleat the 180 degrees is half of the arch CDB, which must therefore be the measure of the angle BAC.

Inf. 1. The three angles of any rectilineal triangle added together will make 180 degrees; for being inferibed in a circle, the fides will be chords, and will cut the whole circumference into three arches, the halves of which arches are the measures of their opposite angles; the angle at A is measured by half the arch B D C, the angle at B by half the arch A I C, and the angle

at C by half the arch A E B.

Inf. 2. The angle at the center is double the angle at the circumference, if they stand upon the same arch; the angle at the center O is measured by the whole arch B E A, and is therefore double the angle at the circumference at C, which is measured by half the same arch.

Fig. 23. Inf. 3. If feveral angles are made at different points of the circumference, and all fland upon the same arch, they will all be equal; and if the arch is a semicircle, they will all be right

angles.

The angles at the points $q \not p m$ are all equal, because they stand upon the same arch A E B D C; and the angles at the points 3, 4, 5, 6, are all 90 degrees, because they all stand upon the diameter A D, which divides the circumference into two equal parts, and therefore 180 degrees each.

Fig. 7. Inf. 4. In an Isosceles triangle, the angles at the base are e-

qual, that is, the angle at B is equal to the angle at C.

N. B. By the base of an isosceles triangle is meant the side which joins the two equal sides.

Inf.

In an equilateral triangle all the three angles are equal. PLATE Inf. 5. If in two triangles two fides of the one be equal to I. two fides of the other, each to each respectively; and if the an-Fig. 24-gle formed by those two fides be also equal, their bases and the

other two angles will likewife be equal.

In the triangles ABC, and DEF, let the fide AC be equal to DF, the fide AB equal to DE, and the angle at A equal to the angle at D; then the angle at E will be equal to the angle at B, and the angle at F equal to the angle at C, and the fide FE equal to the fide CB; for let each be inscribed in a circle; because the angles at D and A are equal, the arches on which they stand will be equal, of which FE and CB are the chords, and therefore they must be equal; and the chords DF and AC, being equal, the angles E and B must be equal; and the same may be said of the angles at F and C.

This demonstration supposes the circles to be equal, which may be thus proved: The arch subtended by the chord BC, and that subtended by the chord EF, contain the same number of degrees, because the angles at A and D are equal; the other two arches subtended by the chords AB and AC, will contain as many degrees as those subtended by the chords DE and DF; but these chords are equal; therefore, the arches, and of conse-

quence the circles, are equal.

Inf. 6. If in two triangles two angles of the one be equal to two angles of the other, each to each refpectively, and a fide of each opposite to the fame angle be also equal, the triangles will be equal all respects; and if all the respective fides of any two triangles are equal, their angles, and consequently all their parts, will be equal.

PROP. VII. THEOREM.

If between two parallel lines A B and C D, any two lines, as Fig. 1. l m, r s, are parallel to each other, those lines will be equal, and the distances between the points of intersection r l, f m, will like-

wife be equal.

To demonstrate this, draw the perpendiculars l, n, r, t, which (by Def. 7.) will be equal; the angles at n and t being both right, are likewise equal; the angles at f and m are also equal (by Inf. 1. Prop. 3.) therefore the triangles r s t, and l m n, will be equal in every respect, (by Inf. 6. of the preceding) the sides, E 2.

CHAP. III.

30

PLATE therefore, I m and r s will be equal; and if to the equal fides I. mn, st, be added the line ns, sm and tn will be equal; but Fig. 25. tn is equal to 1r; therefore 1r and sm will be equal.

PROP. VIII.

In any triangle as A B C, if the fide A B be produced to D, and A D is double of A B; if the line D E is drawn parallel to to B C, then will A E be equal to twice A C, and D E equal to twice B C.

To demonstrate this, draw the line CF parallel to AD; then CF will be equal to BD (by Prop. 7.) = AB by supposition; the angle CFE is equal to the angle ABC; for the angle at D is equal to either of them (by Inf. 1. Prop. 2.) and the angle at A is equal to that at C; therefore the triangles A B C and C F E will be equal in all respects, viz. CE = AC, FE = BC = D F, and C F = AB.

After the fame manner it may be proved, that if A D contain AB any number of times, AE will contain AC, and DE

will contain B C the same number of times.

Inf. 1. In any triangle, as ABC, if a line DE is drawn parallel to any fide, as BC; then AB will be to AD as AC is to AE, and as BC to DE.

To demonstrate this, let the line A D be \(\frac{1}{2} \) of A B, then DE

will be \(\frac{3}{4}\) of BC, and AE \(\frac{3}{4}\) of AC.

Divide the line A Binto four equal parts in the points 1, 2, D, through which draw lines parallel to AC to meet the line CB in the points feb; through these draw lines parallel to A B to meet the line A C in the points E, 7, 8; these lines will form ro equal triangles; for the lines E f, 7 e, 8 b, being parallels, the angles B b D, b e c, e f a, f C E, will be equal, and the angles C f e, f e a, e b c, b B D, will likewise be equal; the bases DB, cb, ae, Ef, being between the same parallels, are also equal; therefore the triangles are equal in all respects, and C f, fe, eb, and bB, will be all equal; but Cf is equal to Ea = a c = c D; now C B contains C f four times, and D E contains its equal E a only three times; therefore D E is $\frac{3}{4}$ of B C; again, A C contains C E four times, and A E contains its equal E 7 three times; therefore A E is \frac{3}{4} of A C.

To illustrate this by numbers, let the fide A C be 40, the fide AB AB 32, and the fide BC 52, and let the line DE be drawn PLATE parallel to BC; if any one of the fides of the triangle EAD I. be given, the other two may be found by the rule of three, Fig. 25. For AD (being \(\frac{1}{2}\) of AB) == 24 by fupposition, it will be

 $\left\{ \begin{array}{l} A \ B : A \ D : : A \ C : A \ E \\ 3^2 : 2^4 : : 4^0 : 3^0 \\ A \ B : A \ D : : B \ C : D \ E \\ 3^2 : 2^4 : : 5^2 : 3^9 \end{array} \right.$

If the fide DE (= \frac{1}{2} BC=) 39 by supposition be given, Then \(BC: BA:: DE: DA \)

And S BC: CA:: DE: EA

52: 40:: 39: 30

And A C: CB:: A E: ED

40: 52: 30: 39

Inf. 2. As the radius AD is to the radius AB, so is the chord DE to the chord BC; for the lines DE and BC are parallel, Fig. 26.

which may be thus proved.

In the triangle ABC let the angle at A be 40 degrees, then the angles at B and C will be 70 degrees each; and as the angle at A is common to both triangles, the angles at D and E will likewife be 70 degrees each; therefore the lines BC and D E will make equal angles with the line AB, and consequently will

be parallel.

Hence, as the radius of any circle is to the radius of another circle, so is a chord of the first circle to the chord of the same number of degrees of the second circle; and if two triangles are similar, that is, the angles of one equal to those of the other respectively; then the sides about or opposite to the equal angles will be proportional; for being inscribed in a circle, their respective sides will be chords of arches of an equal number of degrees.

PROP. IX. PROBLEM.

To make a triangle whose sides shall be three given lines (of PLATE which any two put together must be greater than the third.)

Fig. 27. Let the given lines be A B, C D, E F.

Make the line G H equal to any of the given lines, suppose EF; then take either of the other two lines, as CD, and from the point G, as a center with that extent, describe an arch, and with the extent A B from the point H, as a center, describe another arch to cut the former in L; draw the lines G L and H L and the triangle G H L will be the triangle required.

PROP. X. PROBLEM.

Fig. 6. To make an equilateral triangle upon any given line, as A B. Take the line A B in the compasses, with that extent describe an arch from the point A as a center, and with the same extent from the point B, as a center, describe another arch to cut the former in the point C; draw the lines A C, and B C; then will the triangle ABC be equilateral, and each fide equal to the given line A B.

The demonstration of both these propositions is manifest from

the construction of the triangles.

PROP. XI. PROBLEM.

Fig. 28. To raise a perpendicular from any given point D, of a given line AB.

Take any point C, at pleasure; from this as a center describe a circle to pass through the point D, and to cut the line A B in E; through the center C, from E, draw a line to cut the arch in F, and E F, will be the diameter of the semicircle E D F; draw the line DF and it will be the perpendicular required.

· P R O P. XII. PROBLEM.

From any given point F to let fall a perpendicular to a given line, as A B.

Draw a line at pleasure from F to cut the line A B any where, as at E; biffect the line FE; upon C, the middle of the line, as a center, with the extent CE = CF, describe an arch to cut the line line AB in D; draw the line FD and it will be the perpendi-PLATE cular required.

This is only the reverse of Prop. 11.

. All that is necessary to illustrate these two propositions is to prove that in the triangle E D F the angle at D is a right one; this is evident from Inf. 3. Prop. 6. for the line E F being a diameter, and the angle at D being at the circumference, it is therefore a right one.

In practice there is no occasion to describe the whole circle; it will fuffice to interfect the line A B in E, and draw a small

arch, as I g, opposite to the points E and C.

When the point D is not near the end of the line, the perpendicular may be raifed thus; from D fet off two points L M equally remote from D; from M as a center, and with any convenient extent of the compasses exceeding M D, describe an arch, and with the same extent from L, as a center, describe another arch to cut the former in F; the line F D being drawn, will be the perpendicular required.

But if the point F be given; from F, as a center, describe an arch to cut the line A B in L and M; from which points, as centers, describe two arches to intersect each other in N; draw the line FN, which will cut the line BA in D; then will FD be

perpendicular to A B.

PROP. XIII. PROBLEM.

To divide any given right line (A B) into two equal parts. Fig. 29. From the points A and B, as centers, describe two arches to intersect each other in D; and with the same extent describe two arches to interfect each other in C; the line D C being drawn will cut the line A B into two equal parts in G.

PROP. XIV. PROBLEM.

Thro' any three given points, as A, B, D, not lying in a right Fig. 30-

line, to draw a circle.

Join the points AB, BD with right lines; divide those lines into two equal parts; draw the perpendiculars F m, G n, and let them be produced till they interfect each other; the point of interfection C will be the center of the circle required; for as the circumference is to pass thro' the points A, B, D, the lines A B, B D

must

PLATE must be chords; and if any two chords are bissected by two I. perpendiculars, they will, if produced, meet at the center, by Inf.

2. Prop. 4.

By this problem it is evident, that if any three points are taken in the circumference of a given circle, the center may be eafily found; and if the fegment of any circle is given, the circle may be compleated, by taking any three points in the given fegment, and then proceeding as before.

PROP. XV. PROBLEM.

Fig. 31. Thro' a given point F to draw a line parallel to a given line A B.

Draw the line F G at pleasure; at the point F make the angle D F G equal to F G B, the line D F being drawn, will be parallel to the line A B; because the alternate angles are equal, by

Prop. 3.

This may be done without drawing the line F G, thus; open the compasses till with one foot fixed in F, the other may cut the line any where, as in B; then with the same extent, from any other point in the line, as G, describe an arch; and with the extent G B from F, as a center, describe an arch to cut the former in D; the line F D will be the parallel required.

DEMONSTRATION.

In the triangles DGF and BGF, the fide GB is \equiv DF, and FB \equiv DG, and FG common to both. Therefore the triangles are fimilar, and the alternate angles GFB and FGD are equal; and therefore the lines GB and DF are parallels, by *Prop.* 3.

PROP. XVI. PROBLEM.

Fig. 32. To find a line which shall be a fourth proportional to three

given lines as AB, CD, EF.

Upon the line L M take L g = A B, and draw the line g b, making any angle at pleafure with the line L M, and make g b = D C. Set off E F from L to N, and from the point N draw a line parallel to b g; thro' the point b draw the line L O, then will O N be the fourth proportional required.

For

For in the triangle L N O, g b is parallel to N O by confirmed PLATE tion, therefore L g (= A B): g b (= C D):: L N (= E F): I. N O. (by Inf. 1. Prop. 8.).

If it was required to find a third proportional to two given lines (as AB and CD), proceed in the same manner, only take L I \Rightarrow gb, and draw the line I K parallel to gb, then it will be

Lg:gb::LI:IK the third proportional required.

PROP. XVII. PROBLEM.

To find a mean proportional betwixt two given lines as AB, Fig. 33: CD.

Upon the line L M fet off L N = A B and N O = C D, bifect the line L O in C, upon which, as a center, with the extent CO = CL, describe a semicircle from the point N, $\mathcal{C}c$.

From the point N erect a perpendicular, this will interfect the femicircle in the point E; the line E N being drawn, will be a proportional to the lines L N = A B, and N O = C D.

DEMONSTRATION.

The triangles LEO and LEN are fimilar, for the angle LEO is a right one (by Inf. 3. Prop. 6), the angle LNE is also right by construction; and the angle at L is common to both, therefore the angle LEN is equal to the angle at O, the triangles LEN and ENO are also similar, for they have each a right angle at N, and the angle at O in the one is equal to the angle LEN in the other; therefore the angle at L will be equal to the angle NEO; therefore LN:NE:NE:NO by Inf. 2. Prop. 8.

PROP. XVIII. THEOREM.

The radius of any circle, is equal to the chord of 60 degrees of the fame circle.

DEMONSTRATION.

Upon the radius A C make an equilateral triangle A B C, then Fig. 34 (by Inf. 4. Prop. 6.) the angles at A, B, and C will be all equal, consequently 60 degrees each, but A B is a chord of the arch that

PLATE measures the angle at C, which is 60 degrees; therefore the chord 1. A B of 60 degrees, is equal to the radius A C or B C. Fig. 35.

PROP. XIX. THEOREM.

Parallelograms or triangles, having the fame or equal bases, and being between the same parallels, are equal.

DEMONSTRATION.

Let the parallelograms be ABCD, and CEDF.
Because the sides CE and DF are equal, and parallel by confurction; the angles AEC and BFD are equal (by Prop. 3.), and because AB and EF are also equal, if BE is added to each, then AE must be equal to BF, and as AC is equal to BD, therefore the triangles AEC and BFD are equal in every respect, and if the common triangle BEO is taken away from each, the planes

if we add the triangle C O D, the parallelograms A B C D, and C E D F become equal.

Hence it appears that any two triangles (as CDA,CDE) flanding upon the same base (CD), and between the same parallels (AF, CG) are equal; for they are halves of parallelograms of the

ABCO and EFDO will remain equal; to each of which planes,

fame base and altitude (as ABCD and CDEF).

It is evident from this proposition, that we may make a right angled triangle equal to any given oblique one, for if we draw a line, as AF parallel, to either of the given sides, as CD, through the opposite angular point E, and erect a perpendicular at either end of the same side C or D, to meet the parallel in A or B; then will the right angled triangle C B D = C A D, be equal to the oblique one CD E.

Fig. 10. It is likewife evident from hence, that the rhombus E F G H, 12. is equal to the rectangle E F x z, and that the rhomboides N O P Q, is equal to the rectangle N n P p; and confequently that, by the fame method we may make a rectangle equal to any given parallelogram.

PROP. XX. THEOREM.

Fig. 36. In a right angled triangle ABC, the square of the longest fide AC (called the hypothenuse) is equal to the squares of both the

the other fides A B, B C (called the base and perpendicular) taken together.

DEMONSTRATION.

The square ACHI, whose side is the hypothenuse AC, is equal to the rectangles A H F G, and F G I C taken together; therefore all that we have to prove is, that the square BCDE is equal to the rectangle FGIC, and the fquare A BKL to the rectangle AHFG.

First it is evident, that the triangle BC I is one half of the rectangle FGIC, it is also equal to the triangle BCD, because it stands upon the same base B C, and between the same parallels BC, ED; now the triangle BCD = BCI, is one half of the square BCDE, therefore the whole square BCDE, is equal to the whole rectangle F G I C, each being double the equal triangles BCI, BCD.

In like manner, the triangle ABH = half the rectangle AGHF, standing upon the same base A B and between the same parallels A B, L H, is equal to the triangle A K B, which is one half of the square ABKL; therefore the square ABKL, and the rectangle AHFG being double of the equal triangles ABK, A BH, are equal betwixt themselves.

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F₂ CHAP.

C H A P. IV.

Of the Construction and Mensuration of Geometrical Figures.

Aving explained the principles of geometry, we come now to shew their use in the construction, and mensuration of all plain figures, which we shall reduce to three classes, viz.

1. Those that are limited by three right lines, called triangles.
2. Those that are limited by four right lines, called quadrilaterals.

3. Those that are limited by many right lines, called polygons. Mathematicians suppose all plain figures that inclose any part of space, to be comprehended under one of these denominations, for curvilineal figures are supposed to be limited by an infinite number of right lines; we shall begin with triangles, as no singure or space bounded by right lines, can have sewer than three sides.

SECT. I.

Restilineal Trigonometry, or the Construction of Right lined Triangles.

Rigonometry is that science by which we learn to measure the sides and angles of triangles, and is one of the most useful branches of the mathematicks; for as every triangle consists of fix parts, viz. Three sides and three angles, and it often happens that some of them are unknown, yet if any three of them, provided one be a side, be known, the other three may be sound by this art, either geometrically by scale and compasses, or by an arithmetical calculation. It is either rectilineal or spherical, we shall only treat of the first.

Fig. 5.

In order to delineate any triangle, it is abfolutely necessary to have a scale of equal parts to measure the sides by, and a line of chords for measuring the angles, these and the lines of sines, tangents, and secants, and several others, are laid down upon the plain scale, we shall first explain these terms, and then shew how to construct the lines.

1. The RIGHT SINE of any arch, is a perpendicular line drawn Fig. 37. from one end of it, to a radius or diameter drawn to the other end; AD is the right fine of the arch AB, or it is half the chord of double that arch; for taking the arch B J equal to A B, A J will be the chord of the arch ABJ; of which the fine AD is one half.

2. The SINE COMPLEMENT of an arch, is that part of the radius intercepted betwixt the right fine and the center; thus, C D is the fine-complement of the arch A B, for it is equal to F A; the right fine of the arch E A, which is the complement of the

arch A B.

3. The VERSED SINE, is that part of the radius, intercepted between the right fine and the circumference; DB is the versed

fine of the arch A B.

4. A TANGENT to a circle, is any right line fo drawn as to touch the circumference in any point (B), and if to this point be drawn a radius, it will be perpendicular to the tangent; thus BM is a tangent to the circle in the point B, and the tangent of any arch, as A B, is that part of the line B M, intercepted between the point B; at that end of the arch to which the radius is drawn, and the point H, where a line drawn from the center C, thro' A at the other end of the arch, interfects the tangent line BM; therefore HB is the tangent of the arch AB.

5. The SECANT of an arch, is a streight line drawn from the center thro' one end of the arch, produced till it meet a tangent drawn from the point B at the other end of the arch; fo H C is

the fecant of the arch A B.

The fine, tangent, and fecant of the complement of an arch, are called the fine-complement, tangent-complement, fecantcomplement, or co-fine, co-tangent, co-fecant; CR is the cofecant; ER is the co-tangent; AF the co-fine of the arch AB, and the fine, tangent, and fecant of the supplement of an arch, are the same with those of the arch, for being drawn according to the definitions, there refults the fame line.

Hence the fine of 90 degrees is equal to the radius, for it is half the diameter by the definition of a fine, and is the greatest of all the fines; the fine of 30 degrees is half the radius, for it is half the chord of 60 degrees, which was proved to be equal to

the

PLATE the radius; the tangent of 45 degrees is equal to the radius, for let the angle NCE, or NCK be 45 degrees, NK the tangent, and EC the radius, are parallel, being both perpendicular to the diameter KB; but NE and KC are also parallel, being both perpendicular to the diameter EC; and therefore the tangents NK and NE are equal to the radius.

Construction of the Lines on the plain Scale.

I. THE LINE OF EQUAL PARTS.

Fig. 1. This may be made of any length, as A B, and divided first into ten equal parts destinguished by the figures 1, 2, 3, &c. Then each of those divisions must be subdivided into 10 equal parts, so the whole line will be divided into 100 equal parts; the figures 1, 2, 3, &c. denoting 10, 20, 30, &c. of those parts, there will be none cessive for numbering the small divisions betwixt the figures; but for the better illustration of the scale, we shall distinguish those between A and 1, by the letters of the alphabet. Any number less than 100 may be readily found on this line, for if it be less than 10, count as many small divisions beyond the beginning of the line or point A, as there are units in the number, as, if 6 were required, it will be at the point f; if 60, at the figure 6; if 66, count 6 small divisions beyond the figure 6, and you will have the point required.

If the number exceed 100, the small divisions must be subdivided again each into 10, but the length of our line will not admit of these; we shall therefore make use of diagonals, by which means any number under 10,000 may be had with as great certainty, as if the line AB were actually divided into 10,000 equal parts.

To perform this, let there be 50 lines at equal distances from one another, drawn parallel to AB, and having compleated the parallelogram ABCD, let the lower line CD be divided exactly like the upper line AB, into 100 equal parts, and numbered

1, 2, 3, &c. and draw the diagonal A a.

Now the portions of the parallels, 10, 20, 30, &c. intercepted betwirt this diagonal and the perpendicular $A \, C$, will be 1 tenth, 2 tenths, 3 tenths, &c. of the line $C \, a_3$ for in the triangle $A \, C \, a_3$, let $C \, a_4$ be the base, then the portions of the parallels 10, 20, &c. will be bases of as many triangles, similar to the triangle $A \, C \, a_3$, therefore $A \, C \, C \, C \, a_4 \, C \, A_4 \, C_4$ the portion of the parallel 10,

inter-

intercepted betwixt the diagonal A a and perpendicular A C, but PLATE A 10 is the tenth part of A C by conftruction, therefore the portion of the parallel 10, is the tenth part of C a, or the thou-fig. 1. fandth part of the whole line C D or A B; the figures 1, 2, 3, &c. denote 100, 200, 300, &c. and a, b, c, 10, 20, 30, &c. of

those parts.

Again, if there were 9 parallels drawn betwixt the line A B and the parallel 10, it is plain the portion of that next to the line A B, intercepted betwixt the diagonal C a, and perpendicular A C, would be the tenth part of the portion of the parallel 10, intercepted betwixt the fame lines, or the 10000th part of the whole line C D or A B. In the plate we have only four intermediate parallels numbered 2, 4, 6, 8; fo their portions intercepted betwixt the diagonal C a, and perpendicular A C, will be 2,

4, 6, 8, of those parts.

By these means the lines A B and C D, are in effect, divided into 10,000 equal parts; the figures 1, 2, 3, &c. denote 1000, 2000, 3000, &c. the small divisions on the lines A B and C D, betwirt those figures will be hundreds; the tens are not transfered to the lines A B and C D, but may be had at the intersections of the parallels 10, 20, 30, &c. with the diagonals. If the units Fig. 6, are even, they may be found at the intersection of the diagonals, 7.8. and the intermediate parallels, but if they are odd, as 1, 3, 5, &c. half the distance in the diagonal, must be taken betwirt those parallels. To compleat the scale, there must be diagonals drawn from all the divisions in the line A B to the line C D, parallel to that drawn from the point A in the line A B, to the point a in the line C D.

It will be very easy to find any number under 10,000 upon this

fcale, as in the following example, viz.

For units, look for the parallel below the line A B, betwixt the point A and the parallel 10; thus, to find 6, look for the third parallel, its interfection with the diagonal A a (which is the first of all the diagonals) will be the point required; this parallel in Fig. 9, the plate is numbered 6, but the odd numbers must be found betwixt the parallels; for instance, the number 7 will be in the same diagonal A a, between the parallel 6 and the parallel 8.

If 10, 20, 30, &c. be required, look for the interfections of Fig. 10, the parallels so numbered, with the first diagonal A a, and you will have the point required. If the given number is 12, first

and

PLATE find 10, and the intersection of the parallel next below that, with the same diagonal will be 12; the number 25 will be in the Fig. 1. middle of that part of the diagonal betwixt the second and third parallel below the parallel 20; so that if the number be less than 100, it will be in the first diagonal; if it exceeds 100, and is less than 200, it will be in the second diagonal; and if less than 1000, it will be in some of the diagonals, drawn from the several points a, b, c, d, &c. between A and I, in the line A B to the line C D, thus the number 600 will be the fixth small division from A towards 1; but if 606 is required, it will be found at the intersection of the third parallel (numbered 6) with the diagonal fg; and where the same diagonal intersects the parallel, 60 will be the point for 660; and the middle of that part of the same diagonal, betwixt the third and sourth parallel below that of 60, will be the point for 667.

The number 6000 will be at Fig. 6. in the line AB; 6700 at the feventh small division beyond Fig. 6. in the same line; the number 6750 will be at the point where the diagonal drawn from the point 6700 in the line AB, interfects the parallel 50; and where the same diagonal cuts the third parallel below the parallel

50, will be the point for 6756.

The diagonals upon Gunter's scales, confift only of eleven parallels; the upper and lower are graduated, the one into inches. numbered 1, 2, 3, &c. to 9; the other into half inches, numbered 1, 2, 3, &c. to 18; fo there are no small divisions betwixt the figures, but there is an inch before the beginning of one line, and half an inch before the beginning of the other line, divided into ten equal parts in the upper and lower lines; and diagonals drawn as in that, in the plate, which will divide the inch and half inch each into 100 equal parts; fo that if the spaces betwixt the figures be 100, those betwixt the diagonals will be tens, and the units will be at the intersection of the diagonals and intermediate parallels; one example will fuffice to shew how to take off any number by this fcale: fuppose 748, first find the figure 7, and observe where the perpendicular, from that point, intersects the eighth parallel from it, there fix one foot of the compasses, extend the other to the intersection of that parallel with the fourth diagonal, and you will have the extent for 748.

There are feveral other lines of equal parts which are graduated, and numbered exactly as the upper or lower line of the dia-

gonal

gonal scale, and the divisions and subdivisions are in tens; but as PLATE one inch is the twelfth part of a foot, the diagonal scales for feet II. and inches, confift of feven parallels, the upper and lower lines Fig. 4. are numbered as in the other diagonals; the spaces betwixt the figures are to reprefent feet, which suppose one inch in the upper line S T, and half an inch in the lower line NO: They are numbered 1, 2, &c. the one contrary to the other, as upon most of the shipwrights rules. Set off half an inch to the right from O, at the beginning of the lower line to o; and one inch to the left from S, at the beginning of the upper line to m; then draw two diagonals, to be distant from one another one inch on the upper line, and to meet in the lower line at the middle of the inch; and at the other end draw two diagonals, to be at the distance of half an inch from one another in the lower, and to meet at the middle of the half inch in the upper line. It is evident the intersections of these diagonals will represent inches.

The other lines on the scale are taken from the equal divisions Fig. 5. of a circle, and are constructed in the following manner, viz.

1. With the radius you intend for your scale at C as a center, describe a semicircle, ADB; then upon the center C erect the perpendicular CS, which will divide the semicircle into two quadrants AD, DB, and draw the right lines AD, DB.

2. Divide the quadrant B D into 9 equal parts; each of those divisions will contain 10 degrees, as a quadrant or fourth part of a circle contains 90 degrees; place one foot of the compasses in B, and with the other transfer the several divisions from the circumference to the right line B D, then will B D be a line of CHORDS.

3. Upon the point B erect the perpendicular BT; then draw lines from the center C through the several divisions 10,20, 30, &c. of the arch BD to meet the line BT, and number the several points of intersection 10, 20, 30, &c. the same as the arches;

then will B T be a line of TANGENTS.

4. From the points 10, 20, 30, &c. in the arch B D, let fall perpendiculars to the radius CB; those several perpendiculars will Fig. 30. be the sines of those arches, and will divide the radius CB into a line of sines, which must be numbered 10, 20, &c. from C towards B; for since the perpendicular let fall from the point 80, to the radius CB, is the sine of 80 degrees; C 10 will be the sine of 10 degrees (by Def. 2. of this.)

G. It

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5. If the same line be numbered from B towards C, it will become a line of VERSED SINES.

Fig. 5. 6. With one foot of the compasses in C, extend the other to the feveral divisions of the tangent line B T, and transfer those extents to the line CS; then will CS be a line of SECANTS.

> As the shortest secant that can be drawn, is longer than the radius, and the longest fine is equal to the radius; the line of

fecants on the scale, is on the same line with the sines.

7. As the angle, which the diameter A B makes with any line drawn from the point A, to any point in the circumference, is one half of the angle, that the radius B C makes with a line drawn from the center C to the same point (by Prop. 6. Chap. 3.). Right lines drawn from the point A to the feveral points 10, 20, &c. in the arch B D, will divide the radius C D into a line of SEMI-TANGENTS, or tangents of half those arches.

8. Divide the quadrant A D into 8 equal parts, and with one foot of your compasses in A, transfer the several divisions to the right line A D, then will A D be a line of rumbs hereafter to be

fpoken of.

PLATE II.

All these lines are transferred from the semicircle to the scale Fig. 6. where they are drawn parallel to one another, and diffinguished by the initial letters of their proper names, being what is called a plain fcale.

> The line of equal parts, and the line of chords, will be fufficient for the construction of any rectilineal triangle, but we think it necessary here to shew the uses of the other lines.

PROB. I.

PLATE To make or measure any Angle by the Line of Chords I.

1. From the point C, let it be required to draw a line that Fig. 39.

shall make an angle of 40 degrees with the line C G.

With the extent of 60 degrees taken from the line of chords (which is always equal to the radius by Prop. 18. Chap. 2.) defcribe an arch; then take the extent of 40 degrees from the fame line, and fet it off upon the arch from A to D, and the angle A C D will be 40 degrees.

2. When an angle is given to be measured with the same extent, viz. 60 degrees of chords; from the angular point describe an arch as before, to interfect the lines that form the angle; the

length

length of the chord of that arch intercepted between the lines, PLATE measured on the line of chords, will give the number of degrees Fig. 37.

that the angle contains.

If the given angle is greater than 90 degrees, it may be made or measured at twice. Thus, suppose the angle 130 degrees; first take the chord of 90, and fet it off from K to E, then take the chord of 40 degrees, (the remainder) and fet it off from E to A, then will the angle A C K be 130 degrees: Any other two chords whose fum is 130 degrees, would have answered the same purpose. But as every semicircle contains 180 degrees; when the given angle exceeds go degrees, it may be very readily made, by fetting off its complement to 180 degrees, from the extremity of the diameter: Thus, if we let off 50 degrees of chords, from B to A, and draw the line A C, we have the angle A C K = 130 degrees as before. When fuch an angle is given to be measured, if that extent is taken, and substracted from 180 degrees, the remainder will be the quantity of the arch.

R O B.

To find the Sine, Tangent, or Secant of any Arch; the quantity of the Arch, and the length of the Radius being given. Fig. 38.

Let the angle be 40 degrees, and the radius 100.

Now as this is the length of the radius, by which those lines on the scale were constructed; take 40 from the line of fines, that extent measured on the line of equal parts, into which the radius is divided, will give the length in numbers, of the fine of 40 degrees; and by the fame method, we have the tangents and fecants of any arch; but when the radius is not the same, observe the following method.

Suppose the angle 40 degrees, as before, and the radius 88

inches.

Make D C A an angle of 40 degrees by the preceding, and produce the lines C D and C A; then take 88 from any scale of equal parts, and with that extent from the angular point C, defcribe an arch, as L B; from L let fall the perpendicular L M, which will be the fine; the perpendicular B T will be the tangent, and C T the fecant of the arch L B; each of which measured upon the same scale of equal parts as the radius was taken from, will give the fine, tangent, and fecant of the arch in numbers.

PROB. G 2

PROB. III.

PLATE
I. The Length of the Sine, Tangent, or Secant; and the Quantity of Fig. 38.

an Arch given to find the Length of the Radius.

Let the angle be 40 degrees as before.

If the fine is given; at any point as M, of a right line, as C N; erect a perpendicular, and make M L equal to the given fine; then at L make an angle of 50 degrees, the complement of the given angle, and draw the line L C, which will be the radius required.

If the tangent is given, make B T equal to it, and make the complement angle 50 at T; so the line B C will be the radius.

If the fecant is given, make C T equal to it, and make an angle of 40 degrees at C, and one of 50 at T, the line T B will interfect the line C N in B; then will C B be the radius required.

PROB. IV.

The Length of the Sine, Tangent, or Secant; and the Length of the Radius given; to find the Quantity of an Arch.

Let the radius be 88.

If the fine is given, at any point, as M, of a right line, as C N, erect a perpendicular, make M L equal to the given fine; with the given radius 88, from L, as a center, describe an arch to intersect the line C N in C, and draw the line C L; then will L C M be the angle required.

If the tangent is given, erect a perpendicular at any point, as B, of the line CN; make TB equal to the given tangent; from B, as a center with the given radius, describe an arch to intersect the line CN in C; draw the line CT; then will TCB be the

angle required.

If the secant is given, set off the given radius from C to B, at which point erect a perpendicular; then with the extent of the given secant, from C as a center, describe an arch to intersect the perpendicular in T; draw the line C T; then will T C B be the angle required.

DEMONSTRATION.

Draw the perpendiculars D E and G A, the one will be the fine,

fine, and the other the tangent of the arch A D, (by Def. 1 and 4, $PLA^{\dagger}L$ of this.) and C G the fecant of the fame arch; for CA = CDis the ra dius of the circle from which those lines are constructed. Fig. 33.

CD: DE::CL:LM, CA: AG::CB: TB, and

CA: CG:: CB: CT by Prop. 8. Chap. 3.

But C D and C A, are radii of the arch A D; and D E the fine, G A the tangent, and G C the fecant of the fame arch; therefore L M will be the fine, T B the tangent, and C T the fecant of the arch B L, of which C B is the radius.

PROB. V.

To construct a right lined Triangle, three things being known, one of which must always be a Side.

This will admit of four different Cases.

Ist. When the three fides are given, the triangle may be constructed, as already shewn Chap. 3. Prop. 9.

2d. Given two fides, (C A and C F) and the angle (C) includ-

ed by those sides, to delineate a triangle (AFC).

First make the given angle at C; then set off CA and CF the Fig. 48. given sides from the angular point, and draw the line AF.

3d. Given two fides AF and CF, and the angle (C) opposite

to one of them.

Make the angle; as before, then from the angular point C fet off one fide C F, from F as a center; with the extent F A, the other given fide, describe an arch to intersect the line C G, which will be in A or B, and C F A or C F B, will be the triangle required. So that as this case will admit oftwo folutions; we must know whether the angle opposite to the other given side is acute or obtuse, before the answer can be determined; for if obtuse, the least, if acute, the greatest will be the required triangle.

4th. Given one fide (AC), and two angles (A and C).

Draw the given fide AC; make one of the given angles at A,

and the other at C, and produce the lines that form those angles, till they meet in F; then will A F C be the triangle required.

After the triangles are thus constructed, the unknown sides may be measured by the same line of equal parts, by which they were constructed, and the angles by the same line of chords; and although all triangles may be measured and delineated, as we have shewn in the solution of this problem, yet it is usual to divide PLATE them into two classes, viz. right and oblique angled triangles,
I. from whence arises the division of trigonometry, into two parts,
viz. right and oblique; the last of which contains only the foregoing four cases.

PROB., VI.

To construct a right angled Triangle.

Fig. 42. This will admit of fix cases, occasioned by the different names, by which the sides are distinguished, viz. The hypothenuse, which is the side opposite to the right angle, as (AC). The perpendicular (CF) is one side, and the base (AF) the other side, meeting at the right angle. To distinguish one from the other, we shall draw the perpendicular up and down, and the base across the paper; the angle opposite to the base we shall call (simply) the angle, and that opposite to the perpendicular we shall call the complement angle.

Hence, as in a right angled triangle, one angle is always the same, being equal to 90 degrees; it may be said to consist of four variable parts, viz. the three sides, and an oblique angle; any two of which being given, by them the triangle may be con-

ftructed.

Fig. 41. Case 1. Given the hypothenuse AC, and the angle at C 50 de-

grees, to find the base and perpendicular.

Draw the line C G up and down the paper; then with 60 degrees of chords from the point C, describe an arch; make the angle at C 50 degrees, and set off the given hypothenuse from C to A; from the point A let fall the perpendicular A F, then will A F be the base, and CF the perpendicular of the triangle A F C,

right angled at F.

Hence, if the hypothenuse of a right angled triangle be made the radius of a circle, by which the angles are to be measured, the base and perpendicular will become sines of their opposite angles; A F is the sine of the angle at C, and CF the sine of the angle at A, by the definition of a sine; and because the sine of an angle is the same with the sine of that arch, which is the measure of the angle; its length cannot be determined till the length of the radius is known; for which reason the same angle may bave sines, differing infinitely in length from one another in proportion to the radii by which they are measured; so that this case

is the very same with *Prob.* 2. of this; for making the hypothe-PLATE nuse the radius of a circle, we can find the sine of any arch in I. the same manner as we have shewn in that problem.

Case 2. Given the base A F, and the angle at C 40 degrees, Fig. 42.

required the perpendicular CF, and the hypothenuse AC.

This may be done by *Prob.* 2. of this; for if the base of a right angled triangle be made the radius of a circle, the hypothenuse will be the secant, and the perpendicular the tangent of the angle at the base A, which being the complement of the given angle will be 50 degrees; this is also the same as *Case 4. Prob.* 5. of this for here is one side, and the angles given. Therefore draw the line AF across the paper, and make a right angle at F; from F to A set off the given base at A; make an angle of 50 degrees, and draw the line AC; then will ACF be the triangle required.

Case 3. Given the perpendicular C F, and the angle at C 50 Fig. 43.

degrees.

This in effect, is the same with the preceding, and may be constructed as in *Prob.* 2. or *Case* 4. *Prob.* 5. of this; for if the perpendicular be made the radius of a circle, the base will be the tangent, and the hypothenuse the secant of the angle C. Therefore having set off the given perpendicular CF, make a right angle at F; at C make the given angle 50 degrees; draw the line AC; then will ACF be the triangle required.

Case 4. Given the base AF, and the hypothenuse AC, to find

the perpendicular and the angles.

This and the two following cases may be done as in *Prob. 4*. of this; for either of the given sides may be made the radius of a circle, and the other sides will be sines, tangents, or secants; they may likewise be done as in *Case* 2, or 3, of *Prob. 5*. of this; for we have two sides, and either the included angle, or the angle opposite to one of the sides given; in this case the opposite, angle is given. Therefore draw a line across the paper, and set off the given base from A to F; at the point Fercet a perpendicular, then take the given hypothenuse A C with a pair of compasses, and from the point A, as a center, describe an arch to intersect the perpendicular in C; draw the line A C, and the triangle will be constructed.

Case 5. Given the perpendicular C F, and the hypothenuse

AC, to find the base AF, and the angles.

This is exactly the fame with the preceding, only calling what was then the bale, now the perpendicular; for making the right

PLATE angle at F as before, if we fet off the perpendicular from F to C,

I. and with the extent of the given hypothenuse A C, upon C as a

Fig. 43 center, describe an arch; it will intersect the line drawn perpendicular to CF in the point A, then will A CF be the triangle required.

Case 6. Given the base A F, and the perpendicular C F, to

find the hypothenuse and the angles.

Here we have two fides, and the included angle given; therefore by Case 2. Prob. 5. make a right angle as at F; then set off the given base from F to A, and perpendicular from F. to C; draw the line A C, and the triangle will be compleated.

It may now be prefumed, that the reader, by a due attention to what has been faid, may be able to conftruct any triangle when one fide, and any other two parts are given; and it would be needless to give any more examples, as we shall have occasion to shew in another place, how to perform what has been done here geometrically, by arithmetical calculation: We shall therefore under this head only subjoin the following theorem, which should be well understood, and carefully attended to, viz.

THEOREM.

In a right angled triangle, any fide may be made the radius of a circle, and the other fides may be found, by being confidered as fines, tangents, or fecants of the oblique angles.

Fig. 41. Case 1. If the hypothenuse A C is made radius, the base A F will be the fine, and the perpendicular CF the fine complement

of the angle at C.

Fig. 42. Case 2. If the base A F is made radius, the hypothenuse will be the fecant complement; and the perpendicular the tangent complement of the angle at C.

Fig. 43. If the perpendicular CF is made radius, the hypothenuse will be the secant, and the base the tangent of the angle at C.

S E C T. II.

Construction of Quadrilateral Figures, &c.

PROB. I.

To make a Square whose Side shall be the given Line CD.

PLATE
I.

PON one end of the line as D, erect a perpendicular; fet Fig. 9. off the given fide C D from D to B; upon B and C, as centers; with the fame extent, deferibe two arches, interfecting each other in A; and draw the lines A C, A B; then will A B C D be a geometrical fquare, all the fides and angles being equal.

PROB. II.

To make a Rhombus whose Side shall be the given Line E F, and the Angle E 50 Degrees.

First make the angle at E 50 degrees; make E G and E F e-Fig. 10. qual; then with the extent E F, describe an arch from the center F, and another from the center G, intersecting the former in H, and draw the lines G H, H F; then will E F H G be the rhombus required.

PROB. III.

With two given Sides, as I K and K L, to make a Rectangle.

Erect a perpendicular at K, and set off the two given sides to Fig. 11. I and L; from I, as a center, with the extent K L, describe an arch; and with the extent I K, from L as a center, describe another arch to intersect the former in M; draw the lines I M, L M, and the rectangle will be compleated.

PROB. IV.

To Make a Rhomboides whose Sides N O, O 2, and the Angle at O are given.

Make the angle at O, and fet off the given fides to N and Q; Fig. 12. H with

PLATE with the radius O Q, from N as a center, describe an arch; then I. with the extent O N, from Q as a center, describe another arch Fig. 12. to intersect the former in P; draw the lines N P, P Q, and the rhomboides will be made; and if from the points N and P, be let fall perpendiculars to the points n and P; the rectangle N n P p will be equal to the rhomboides N O P Q.

PROB. V.

To describe a regular Polygon, having the Length and Number of Sides given.

This is in effect, the fame with Case 4. Prob. 5. of the preceding section, for every regular polygon may be inscribed in a circle, and if there be a radius drawn to every angle of the polygon, it will contain as many triangles as it has sides; so that if 360, the number of degrees in a circle, be divided by the aumber of sides, the quotient will be the angle at the center; and if that is subtracted from 180 degrees, the remainder will be the sum of both the angles at the base, which is the side of the polygon; and because the triangles have two of their sides equal, the angles at the base will also be equal; so that in every triangle

we have one fide, and all the angles given.

Fig. 14.. Let a b be the fide of a hexagon, then $360 \div 6 = 60$, and 180-60=120, the fum of the angles at a and b, therefore each angle will be 60 degrees: Make therefore at a and at b an angle of 60 degrees, and produce the lines till they meet; from the point of their intersection describe a circle thro' a and b; the distance from a to b will divide the circumference into fix equal parts, and when the chords are drawn to these points, we shall have the hexagon required. Here the angles at the base are the fame with the angle at the center; consequently a polygon of 6 fides confifts of as many equilateral triangles; but as all other polygons confift of as many isosceles triangles as they have fides; and the angles at the center, and circumfereuce may be easily found by the foregoing method; there can be no difficulty in constructing them, as there is no more required, but to find the center of a circle which shall pass thro' the extremities of the given fide:

PHATL

PROB. VI

To describe an Ellipsis.

An ellipsi is a figure contained under one curve line, called the periphery, but differs from a circle; for if there be two diameters drawn in a circle at right angles to one another, they must be of equal lengths, and all points in the circumference are equally distant from the center; but the ellipsis has two diameters of different lengths, at right angles to each other, T S the longeit, is called the transverse diameter, and CE the shortest, the conjugate diameter; fo that the circle is, as it were, flattened one way, the femicircle are shortened in the same proportion, they will give the points through which the femi-periphery of the ellipsis must pass: In order to perform this, make the radius, or half the transverse diameter T x = x E, a fide, and x E half the conjugate diameter = F G the base of a triangle x F G; from the circumference of the circumferibing circle, draw feveral lines, as m, s, n, t, perpendicular to the transverse diameter; transfer those fines to the fide x F of the triangle, viz. make xz = nt, xy = ms, &c. draw z b and y g parallel to the bate FG, transfer the extent zb from n to p, and the extent yg from m to o, then will p and o in the lines n t, m s, be two points thro' which the femi-periphery must pass; and if more lines are transferred from the femicircle to the fide x F, we may by the foregoing method find a fufficient number of points, thro' which the semi-periphery may easily be drawn.

If with the extent Tx = Sx, half the transverse diameter, and from the centers C or E, the extremities of the conjugate diameter, two arches are described, they will intersect the transverse diameter in the points F, f, each of which is called the socus of the ellipsis; and if from any point in the periphery a line be drawn to each of these points, the sum of those lines will always be equal to the transverse diameter, viz. Fa + fa = Fb + fb = FC + fC = FD + fd = Fe + fe = TS; and this being the peculiar property of the ellipsis, any number of points may

be found by the following method.

Having found the two focal points F, f, as before, with any extent of the compasses, so it be less than the transverse diameter,

Fig. 45

PLATE as T i, from the focus F describe an arch; and with the extent
I. S i, the remaining part of the transverse diameter, describe ano-

Fig. 45: ther arch to interfect the former in the point a, which will be in the periphery of the ellipsi; in the same manner you may find as

many points as you pleafe.

From what has been faid it is plain, that if there be a thread equal in length to the transverse diameter, fastened to two pins one in each focus; and if a pencil, or any other convenient instrument be moved round within the thread, so as to keep it at its full extent, it will describe the true periphery of the ellipsis; and if both ends of the thread be fastened at the center, it will describe a circle; so that this figure may properly be said to have two centers, whereas a circle has but one.

PROB. VII.

To make a Circle equal to a given Ellipsis.

Find a mean proportional between the transverse, and conjugate diameters by Prop. 17. Chap. 3. and this will be the diameter of the circle required.

S E C T. III.

Of Mensuration of plain Surfaces.

AV NIG in the preceding sections shewn the construction of plain geometrical figures, and the method of reducing those that are oblique angled, to right angled ones of equal surfaces; we shall now briefly shew how to measure those surfaces, or the whole spaces contained within the circumscribing sides.

These spaces are always estimated, in squares of some affigned dimensions, as inches, seet, yards, &c. and the number of such squares contained in any figure, is called its area or superficial

content.

Now as a fquare has four right angles it will necessarily follow, that all figures must be reduced to right angled ones before they can be measured geometrically, so that the whole of superfuperficial measure may be said to consist in finding the area of Plate a square or rectangle; in order to which, let us suppose a rectangle; angle as a b c d, to be one inch broad; it is plain it will con-Fig. 44-tain as many square inches as it is inches in length, which in this case is 12, and the rectangle may be cut in 12 square inches, but if it were any broader, and of the same length, it would contain 12 times as many square inches as there are inches in breadth; so the square ABCD, of 12 inches long, and 12 inches broad, will contain 144 square inches, which is the area of a superficial foot, or square whose side is one soot; hence the following rules will appear very plain.

PROB. I.

To find the Area of a Square or Rectangle, the Length and Breadth.
being given.

Rule. Multiply the length by the breadth, the product is the

area; this will admit of two cases.

Case 1. If the length and breadth are taken by one kind of measure; as if there is a rectangle 48 inches long, and 24 inches broad; then $48 \times 24 = 1152$ the area in square inches. If the length and breadth are taken in seet, the area will likewise be in seet; the like may be said of yards, rods, &c.

Case 2. If the length is taken in one kind, and the breadth in another kind of measure; as suppose a plank 20 feet long, and

9 inches broad whose area is required.

Rule. Multiply the length by the breadth, and divide the product by 12; the quotient will be the area. $20 \times 9 = 180$; and

180 - 12 = 15 feet the area required.

The reason of dividing the product by 12 is obvious, for if the breadth were 9 feet, the area would be 180 feet; in this case the multiplier (9) is feet, whereas in the other it is but the 12th part of 9 feet, and of consequence the first product will be but the 12th part of the last, and therefore must be divided by 12, and the quotient will be the true product, which in this case will be less than the multiplicand, because the multiplier is a fraction, viz. viz and $zo \times viz = viz = viz = 15$. We have been the longer upon this head, because we shall have occasion in another place to mention the measuring of plank; for it is always accounted as an oblong square, the it generally tapers, the breadth is taken

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PLATE in the middle, which will be exactly true when both edges of 1. the plank are streight, as in Fig_{11} . Plate 1. the trapezium $n \circ p \cdot t$. Fig. 11. = the parallelogram I K M L, for the triangle $r \cdot n \cdot M =$ triangle

r Io; hence in measuring plank.

1 : length in feet : : breadth in feet

12 : length in feet :: breadth in inches : area in feet.

144: length in inches:: breadth in inches:

This may be easily applied to all artificers works, as wainscoting, paving, &c. 9: length in feet: breadth in feet: area in yards.

PROB. II.

. To find the Area of a Triangle.

Rule. Multiply the base by half the perpendicular, (let fall Fig. 35. from one one of the angles to the opposite side) the product will be the area required, as in the triangle D E F, let D F be 40 feet, and the perpendicular E M be 18 feet; the half of which is 9, the $40 \times 9 = 360$ the area in feet $= 20 \times 18$, and $360 \div 9 = 40$ the area in yards.

PROB. III

To find the Area of a Trapezium.

Fig. 45. 1. If the trapezium has two fides parallel; as m n, s t, let fall the perpendicular t r, and multiply it by half the fum of both the parallel fides; the product will be the area.

Note. We suppose the arch st to be so small, that it may be accounted a right line; then the parallelogram mnrt + triangle

s r t = trapezium m n s t, and the parallelogram's area $= r t \times (n t)$ half the fum of n t + m r, and the triangular area $= r t \frac{1}{2} r s$.

2. If none of the fides are parallels, as B C, D A, divide the

Fig. 13. given trapezium into two triangles, by drawing the diagonal B D, and draw the perpendiculars A x, and C z; then multiply the diagonal by half the fum of the two perpendiculars; the product will be the area required

PROB. IV.

To find the Area of an irregular Polygon.

Fig. 15. Rule. Reduce the polygon (as ABCDEFG) into triangles

(as ABG, BGF, BFC, FCE, and CDE); find the areas of those triangles, and add them together; the sum will be the area of the whole trapezium.

PROB. V.

To find the Area of a regular Polygon.

It is evident that the area of every regular polygon is equal to the fum of the areas, of as many isosceles triangles as it contains fides, and that a perpendicular let fall from the center to any fide, would be the radius of the inscrib'd circle; the area of the whole polygon may therefore be found by the following rule, viz.

Multiply the fum of all the fides by half the radius of the inferibed circle, or the radius by half the fum of the fides; the

product will be the area required.

By this rule, it will be easy to find the area of any regular polygon, when the side, and the radius of the inscribed circle are both given: But as it sometimes happens that only the side, and sometimes only the radius of the circle can be practically measured, we shall lay down the proportions they bear to one another in most of the figures that occur in practice, which are calculated to a sufficient exactness in most cases, vix.

The Proportion that the Sides bear to the Radii of the inscribed Circles.

Equilateral triangle	as 1 to 0.288
Pentagon or polygon of 5 fides	0.688
Hexagon 6	0.866
Heptagon 7	1.038
Octagon 8	I . 207
Nonagon 9	ı . 378
Decagon 10	1.538
Undecagon 11	1.703
Duodecagon 12	ı. 866

We shall give one example under this head, which we think will be sufficient.

Required the Area of an Octagon whose Side is 24.

As 1:1.207:24:28, 968, the radius of the inferibed circle. $24 \times 8 = 192 = 100$ of the fides.

Then

PLATE Then multiply 28.968 by 96 = half the fum of the fides; I. and the product will be 1780, 928 the area required.

PROB.

To find the Area of a Circle.

As mathematicians confider a circle as a polygon of an infinite number of equal fides, the circumference will be equal to the fum of all the fides: If this then be multiplied by half the radius, the product will be the area, the same as if it were a polygon; but before this can be done, the circumference must be found, by investigating the proportion it bears to the diameter, which has been calculated to great exactness by several eminent mathematicians, and is univerfally allowed to be as 1 is to 1.141592, &c. in practice, as 1 to 3.1416; hence the area of a circle may be found by the following rule, viz.

Multiply the diameter by 3.1416, and the product will be the circumference; this again multiplied by to of the diameter (which is the fame as half the radius) will give the area, which will be the same as if the diameter be squared, and the i of the product

multiplied by 3.1416, as will appear by the following:

EXAMPLE.

What is the Area of a Circle whose Diameter is 128.

 $128 \times 3.1416 = 402.1248$; then \(\frac{1}{4}\) diameter 32 \times 402.1248 = 12867.9936; the area required: $= 128 \times 32 \times 3.1416$; for when feveral numbers are to be multiplied into one another, it will be indifferent in what order the operations are performed; but if instead of 32 we take 128, which is equal to it, and multiply the diameter by this fraction, it will be $\frac{128 \times 128}{128}$

the square of the diameter 16384 divided by 4 = 4096, alfo $128 \times 32 = 4096$, and $4096 \times 3.1416 = 12867.9936$, the area as before; now because 4 will always be a divisor, and 3.1416 a multiplier; we may take + of 3.1416, which is 7854, for a multiplier, and then there will be no occasion for a divisor; and the area of any circle will be found by multiplying the square of

the

the diameter by .7854, and the product will be the area $128 \times 128 P_{\text{LATB}} = 16384$ the square of the diameter, and $16384 \times .7854 = I$.

12867.9936 the area as before: Hence the areas of circles will be in the same proportion as the squares of their diameters: And because the square of 1 is 1, the area of a circle whose diamewill be .7854; or, if the circumference, which is 3.1416, be multiplied by a $\frac{1}{2}$ of the diameter (1) or .25, it will give .7854 the area as before.

PROB. VII.

To find the Area of a Sector.

Rule. Find the area of the whole circle; then fay, as 360, the degrees contained in the whole circumference; are to the area of the whole circle; so is the number of degrees contained in any Fig. 20. arch, as ADB to the area of the sector ACBD.

PROB. VIII.

To find the Area of the Segment of a Circle, as A b B D.

Rule. Find the area of the triangle made by the radii A C, B C, and the chord A B, which subtract from the area of the sector A C B D; the remainder will be the area of the segment A b B D.

But it often happens that we have the fegment of fo large a circle, that a fmall part of the circumference may be taken for a right line; and when the plane will not contain the radius, it will be difficult to know whether the curve be an arch of a circle, or of an ellipfis, or it may be neither; for as the periphery of the ellipfis falls within that of the circle, fo there may feveral curves fall between them, or within the ellipfis, which mathematicians have given no rules to inveftigate. In fuch cases, we presume the following method may do for practice, and be pretty near the truth in most cases.

Draw feveral lines perpendicular to the chord, or right line, as T S, at equal diffances from one another; suppose 1 foot. These will divide the whole surface, whether it be the segment of a cir-Fig. 45-cle, or of any other curve, into as many trapezia, less one, as there are perpendiculars, and two right angled triangles besides; now the areas of all these added together, will give the area of

PLATE the whole fegment; and as every one of the trapezia have two I. parallel fides, and every perpendicular is a fide to two trapezia, or to a trapezium and a triangle; the sum of all the perpendiculars multiplied by the distance between each, will be the area of the whole; and if the distance be I foot, the sum of all the per-

Fig. 45. pendiculars measured in feet, will be the area in feet of the whole

space contained within the right line and curve.

But as one fide of every trapezium is a curve; if this fide should differ perceptibly from a right line, draw a chord to it, which will cut off a small segment; in which, if there be drawn other two chords to meet at the middle of the arch, we shall have a triangle, the area of which must be added to that of the trapezium; these segments will be greatest at each end, if it be an arch of a circle, which may be reduced to two or more triangles; but there are some curves that approach so near a right line at each end, that a small part may be taken for such, without any sensible error.

PROB. IX.

To find the Area of an Ellipsis.

As every ellipsis is equal to a circle, whose diameter is a mean proportional betwixt the transverse and conjugate diameters, and this is sound by multiplying the transverse diameter by the conjugate, and extracting the square root of the product; the square of this mean diameter multiplied by .7854, will be the area of the ellipsis; hence the following rule:

Multiply the transverse diameter by the conjugate, and that product by .7854; the last product will be the area required.

E X A M P L E.

Let the transverse diameter be 48, and the conjugate 32.

Then $48 \times 32 = 1536$, and $1536 \times .7854$ = 1206.3744, area required.

It remains to be proved, that the mean proportional to the transverse, and conjugate diameters, will be the diameter of a circle equal to the ellipsis; for which take the following.

DEMONSTRATION.

PLATE I.

Let the ellipsis T C S E, be inscribed in a circle whose diameter is T S; then the area of the semicircle will be equal to the sum of the areas of all the trapezia contained in it; now the ellipsis contains the same number, but smaller trapezia, and the sum of their areas is the area of the semi-ellipsis; therefore the area of a circle, is to the area of the ellipsis; as a trapezium in the semi-ellipsis; but a trapezium in the semi-ellipsis; but

S E C T. IV.

Of Mensuration of Solids.

A Solid is that which has three dimensions, viz. length, breadth, and thickness; and as the areas of all surfaces are estimated in squares, so are the contents of any solid estimated in cubes.

A cube is a folid limited by 6 equal square surfaces, like a die. If the side of the square be 1 inch, soot, yard, &c. the side of the Fig. 46; cube will be the same; and the solid is said to be a cubic inch,

foot, or yard.

A parallelopipedon is limited by two parallel and equal fquares, called its bases, and four rectangles for its sides, which may be called the heighth or length, and if they are perpendicular to the bases it is a right one; but when the sides are oblique to the bases, then it is an oblique parallelopipedon; the like may be said of the following figures.

A prism is limited by two parallel and equal polygons for its Fig. 47. bases, and as many rectangles as the polygon has sides; if the bases be triangles, it is called a triangular prism, but if squares, it is a parallelopipedon, &c.

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A pyramid is a prism, taper'd to a point at the top; it has but one base, which is a polygon, and as many isosceles triangles as Fig. 48. the polygon has fides, meeting at the top, which is called the vertex; it is exactly one third part of a prism of the same base and altitude.

A cylinder has two equal and parallel circles for its bases, and Fig. 49 the space betwixt them is limited by one curve surface. It one fide of a rectangle be fixed as an axis, the opposite fide moved round, will describe the curve superficies, and the other two sides will describe the bases; of this form is a rolling stone.

Fig. 50. A cone is, in respect of a cylinder, what a pyramid is in respect of a prism, and is exactly one third of a cylinder of the same base and altitude; it has but one base, which is a circle, and tapers to a point at the top, called its vertex, like a fugar loaf. If the perrendicular of a right angled triangle be fixed immoveably as an axis, the hypothenuse, turned round, will describe the curve surface, and the base of the triangle will describe the circular base of a cone.

> A fphere or globe, is a folid contained under one curve furface, every part of which is equally distant from one point, called its center, and may be formed by the revolution of a femicircle round the diameter. It is exactly two thirds of a cylinder, whose altitude and diameter of its base are equal to that of the globe.

> In order to find the contents of these regular solids, let us examine how they may be composed; and if we may not be allowed to fay, that a great many plain furfaces of one inch fquare, and infinitely thin, laid upon one another, will constitute a cubic inch, because the sum of ever so many cyphers will not make one unit, yet it is very plain, that if feveral dies, or cubes of one inch, be laid upon one another, they will compose a parallelopipedon, containing as many cubic inches as it is inches in heighth; but if the heighth be only one inch, the folid will contain just as many cubic inches as the base contains superficial. If the side of the base be 12 inches, the area will be 144, and it is plain it will take 144 cubic inches to cover this base. It will require 12 such fquares of one inch high to compleat the cube, fo that a cubic foot will contain 1728 cubic inches, that is 144 x 12; hence the following rules may be deduced.

To find the folid Content of a Cube, Parallelopipedon, Prifm, or Cylinder.

Rule. Find the area of the base by the problems in the preceding section, which multiplied by the perpendicular distance betwixt the bases, gives the solid content in the same kind of measure as the dimensions are taken. Or multiply the length, breadth and thickness (all taken by one kind of measure) into one another; the product is the content in cubes of the same measure; hence I : area base: length: content, or I: length: depth x breadth: content,

PROB. II.

To find the folid Content of a Pyramid or Cone.

Rule. Multiply the area of the base by $\frac{1}{3}$ of the height; the product is the content 3: area base:: heighth: content.

PROB. III.

To find the folid Contents of a Globe.

Rule 1. Find the area of a circle whose diameter is equal to that of the globe.

Rule 2. Multiply the area by double the diameter, and divide the product by 3; the quotient is the content of the globe. 3: area circle × 2:: diameter of the globe: content.

PROB. IV.

To find the folid Content of the Frustum of a Pyramid or Cone.

Note. If either of these be cut, by a plane, parallel to the base, the top cut off, will be a pyramid or cone, and the remaining part its frustum, which will have two bases; the small one is that of the cone or pyramid cut off; the great one, is the base of the whole cone or pyramid before it is cut: Hence, if we can find the content of each, and subtract the lesser from the greater, the remainder is the content of the frustum; so all that is wanting is to find the heighth of each, and to do this:

· 1/t. Sub-

64 1/t. Subtract 1 the diameter of the least from 1 the diameter PLATE of the greatest base: then

2dly. Multiply the perpendicular distance betwixt the bases by

the diameter of the greatest base.

adly. Divide this product by the difference of half the bases. and the quotient is the heighth of the whole cone before it is cut, and fubtracting the distance betwixt the bases from this, we have the heighth of the cone cut off.

DEMONSTRATION.

Fig. 50. Let n m A C be the frustum; draw the perpendicular s m; the line Cm is the difference of half the bases, and the triangles mCs, and

t C x are fimilar; therefore C s: ms:: C t: tx, and $\frac{ms \times C +}{C t} = tx$,

but t x is the heighth of the cone; therefore m s the heighth of the frustum.

PROB. V.

To find the folid Content of irregular Solids, which are limited by feveral curve and plain Surfaces.

To do this, let the folid be supposed to be cut by several planes, parallel to the base, and at one foot, or inch distance from one another. Every fection will form two equal plain furfaces. Half the fum of all the areas, including the areas of both bases, will nearly be the content in feet or inches; but if the folid has no plain furfaces parallel to one another, let two finall parts be cut off, which may be measured as parts of a globe, cone or pyramid.

In all the foregoing problems it will be convenient to take the length, breadth and thickness, in the same kind of measure in which the content is required; but very often it happens that the content is required in feet, and the length given in feet; but the breadth and thickness in inches, or partly in feet, and partly in inches; as in, timber, bales, cases, &c. The value of timber is estimated by the load of 50 feet, and the freight of bales, &c. is by the tun of 40 feet. Such of our readers as are not well acquainted in decimals or cross multiplication, may reduce the feet into inches, so first find the content in inches, this divided by 1728, gives the content in feet; and to render this method as useful and expeditious as possible, we have subjoined three tables:

the first is for dividing a number by 1728; the other two for finding the value of a remainder, and, may be of use in dividing by 144, or by 12; and tho' most of our readers may be presumed to have the last table by heart, yet as all may not, we choose to insert it.

TABLE I.	TABLE 2.	TABLE 3.
1 - 1728	1 - 144	
2 - 3456	2 - 288	
3 - 5184	3 - 432	
4 - 6912	4 576	
5 - 8640	5 - 720	5 - 60
6 - 10368	6 - 864	6 - 72
7 - 12096	7 - 1008	7 - 84
8 - 13824	8 - 1152	8 - 96
9 - 15552	9 - 1296	9 - 108
- "	10 - 1440	10 - 120
	11 - 1584	11 - 132
201 1	12 - 1728	12 - 144

EXAMPLE.

Required the content of a case:

Length 7 feet 5 inches, or 89 inches; breadth 3 feet 5 inches,

or 41 inches; 2 feet 5 inches, or 29-inches depth.

Now $89 \times 41 \times 29 = 105821$, and when this is divided by 1728, the quotient will be 61 feet, and 413 remaining; to find the value of this, look for it, or the number next less in the second table, which is 288; against which is 2, that is $\frac{7}{12}$ of a cubic foot, which are called inches; again there will be a remainder of 125; the next number less in the third table is 120, against which is 10, that is $\frac{1}{12}$ of an inch, and a remainder of 5, which is $\frac{7}{12}$ of an inch; so the content is 61 feet, 2 inches, 10 primary parts, and 5 secondary parts; all concisely express'd thus, 61.2.10.5.

It must be observed, that by one inch is understood 144 cubic inches, being the 12th part of a cubic foot; by one of the first parts 12 cubic inches, and by one in the last part is understood 1

cubic inch.

But when the length is given in feet without any odd inches, and the other two dimensions in inches, the operation may be performed without reducing the feet to inches; only dividing by 144.

EXAMPLE.

What is the content of a piece of timber 24 feet long, 18 inches broad, and 14 inches deep; $24 \times 18 \times 14 = 6048$, and 6048 - 144 = 42, the content in feet; after the fame manner any other piece of fquare timber may be measured; but in practice it is not always required to find the exact contents of timber, for fometimes the computed is less, and sometimes more than the real content.

It would be very difficult to find the exact contents of a tree, but as it generally grows pretty near round and tapering, it will be fomewhat like a fruftum of a-cone; notwithfunding which, it is measured as if it were a parallelopipedon, and to find the square base in some places, the circumference of the tree is taken by girting it with a line pretty near the middle, and \(\frac{1}{2}\) of this is accounted the side of the square 3-now it is plain that the area of such a square will be above \(\frac{1}{2}\) less than the area of the circle, and

the tree measures so much less than the true contents.

In other places the tree is hewed fomewhat in the form of an irregular prism of four flat fides and four round; the base will be an octagon, contained under four equal chords, and four arches of circles, but in measuring the tree the chords are supposed to be produced till they meet, and form a fquare; the area of this, multiplied by the length, is accounted the content, tho' it is plain, the tree thus hewed, does not contain near fo much, because there is wood wanting at the corners, these are called wanes, and the flat fides are called fquares; befides the tree may be hewed in fuch a manner as to make it contain more than the real contents of the tree, even if it were allowed to be a cylinder, fo that there may be very great impositions on the purchasers; to prevent which, the government contract, that the tree shall be hewed in such a manner, that what is to be called the fide of the square shall bear a certain proportion to the diameter of the tree, which may be eafily discovered by the callipers; for if they be applied to the wanes, we have the diameter of the tree, and if to the flats, the fide of the square, or the thickness; now because the larger the wanes are, so much more will the tree measure; it must be hewed so that two wanes shall not exceed one square. What is meant by a wane should likewise be expressed, for it is generally allowed to be the round . part part of the tree where the wood is wanting to compleat the fquere, Priess or the chord of it, which may be taken with a pair of compaffee, as in Fig. 53. BE is the wane, and is exactly half the fquere TB; but in fome contracts the portions of the chords, which are produced without the circle to compleat the fquare, are called wanes,

as in Fig 52. DT = half TE.

It is very difficult to hew a tree exactly to this standard, and very often the wanes are as big as the squares, as in Fig. 54. where the fquares divide the circumference into 8 equal parts; by which means the content of the tree, measured as a parallelopipedon, would be to the real content measured as a cylinder, nearly as 34142 to 31416; for which reason, before it is meafured, it must be reduced to its proper thickness at the measuring place, which is nearly the middle of the tree: For tho 'all trees taper, and consequently are greater at the butt than the top end, yet they are allowed to be cylinders, the diameters of which are taken at the middle. But there will be no occasion to hew the tree, as the proportion is known, which the thickness of the tree, when properly hewed, shall bear to the whole diameter. All that is necessary, is only to construct a line of equal parts, which shall have the same proportion to a line of inches, that the diameter of the tree has to this thickness. If the tree happens to be thicker one way than the other, a mean proportional must be found for the diameter.

The construction of a line of equal parts, that shall have the same proportion to a line of inches, that the diameter shall have to the thickness when the tree is hewed so that the flat shall be double

the wane, will admit of two cases.

Case 1. When by the wanes are understood the portions of the chords, produced without the circle to compleat the square.

1/f. Erect a perpendicular at K, and from K to C fet off any number of inches, and from K to O double the line K C; then Fig. 52. draw the line C O, with which as radius, from the center O, deferibe a circle.

2d. Divide the line C O into the same number of equal parts as the line O K contains inches; then will 21½ of those divisions be equal to 24 inches very nearly; that is a tree whose diameter is 24 inches, will be 21½ inches thick when hewed.

Now if the chords be produced till they meet, they will form

PLATE a fquare: And it is very plain that CO is half the diameter of the I. tree, and KO half the thickness; and because the wane CD, or Fig. 52. its equal CK, is half the flat CB, the tree is properly hewed according to the contract. Hence it is evident, that when the tree is fo hewed, the diameter will contain as many equal parts of the line CO, as the thickness taken upon the flat will contain inches.

Cafe 2. When by the wanes are understood the chords of the arches, or the round parts of the tree, where there is no wood taken off, as B E, D N, I G, F T; and it be required to hew the tree; fo that the slats T B, F I, G N, D E be double those

wancs.

1st. Make an angle of 45 degrees, at the point B, or which is the fame thing, an angle of 90 degrees at M; and taking the points B and E, equally remote from M; draw the line B E, and make B A and A T each equal to B E; so shall B T be double of B E.

2d. Thro' the points T, B, E, describe a circle; and thro' the center C draw C A perpendicular to T B; so will the star T B be double the wane B E, the line C B half the diameter of the tree, and the line C A half the thickness: And if the line C B be divided into the same number of equal parts, as the line C A contains inches; it is plain the diameter, when measured on this line, will contain as many equal parts of this, as the thickness contains inches. The following example will suffice to illustrate what has been said on this head.

E X A M P L E.

Fig. 52. Let there be a piece of timber 20 feet long, and 24 inches diameter, to be hewed to as to make the flats, according to Cafe 1. and let us suppose that when the timber is served in for measurement, it is found, by applying the callipers to the flats, to be 22½ inches thick. Now to know if it be properly hewed, measure the diameter by a line graduated, as CO, which will be found to be nearly 21½; which shews there should be one inch more hewed off; and therefore 21½ must be taken for the side of the square base, which will make the content in feet 64; for the thickness is not quite 21½, it being only 21.466.

Now 144 : square of the thickness in inches :: length in feet :

content in feet: That is, 144:460.789156:: 20:64.

The content may be found by measuring the diameter by a line

line of inches, for which the following proportion must be ta-PLATE ken; as 180 is to the square of the diameter in inches so is the length in feet to the contents in feet; for 144 is to 180 as the square of the thickness to the square of the diameter, which may be thus proved: $144 \div 4 = 36$, and $36 \times 5 = 180$, now $\frac{1}{4}$ of Fig. 52. the fquare of the thickness taken upon the flat, multiplied by 5 will be the square of the diameter; for the squares of KO, and KC both together, are equal to the square of OC, by Prop. 20. Chap. 3. but the square of K C is + of the square KO; therefore five times the square of K C will be equal to the square of O C. In this example the square of the thickness is 460.789156, which is the fecond term in the proportion, when 144 is the first: But if + of the fecond term be multiplied by 5, and that product taken for the fecond term, it is certain, to preferve the fame proportion; that + of the first term must likewise be multiplied by 5, and the product made the first term. Now this is the very case here, when the square of the diameter is taken for the second term; $460.789156 \div 4 = 115,197289$; this x 5 = 575.986445; and 24 × 24 = 576; then 180: 576:: 20: 64 the content as before; tho' it is plain this exceeds the real content, because of the wood that is wanting at the corners. It is even more than the whole tree would measure, allowing it to be a cylinder of 24. inches diameter; for the square of the diameter 576 x .7854 = 452.3004 the area of the base in inches. Again, 144: 452.3004 :: 20:62.8, the content in feet.

If it be contracted that the tree is to be hewed, as in Case 2. when the diameter 24 inches is applied to the line constructed for that purpose; it will measure 20.71. Then 144: 20.71 × 20.7

The works of the feveral artificers relating to building, whether superficial or solid, may be measured by the preceding rules: But as all the operations require multiplication and division; this,

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ilcation and divino.

in some cases, is deemed too tedious for practice, on which account they make use of the sliding rule. But before the lines necessary for that purpose can be constructed, there must be some method found to multiply and divide natural numbers, by adding or subtracting artificial ones: This is most effectually done by the Logarithms; which shall be the subject of the next chapter.

CHAP. V.

Of LOGARITHMS.

T is not our business here to construct tables of these admirable numbers, they being already calculated to great exactness. The learned are obliged for this useful discovery to the indesatigable labour of the noble inventor, Lord Neper. We shall only explain so much of the nature of them, as is necessary for understanding the use and construction of the line of numbers.

LOGARITHMS are artificial numbers adapted to natural numbers, and so contrived, that by adding the logarithms of any two numbers, their sum will be the logarithm of the product of these two numbers, or by subtracting the less from the greater, the remainder will be the logarithm of the quotient of the one divided by the other. From this description, the following inferences will easily be deduced, viz.

1. Every natural number must have a proper logarithm, and .

therefore a table should be made to find it by inspection.

2. If the logarithm of any number be increased, the corres-

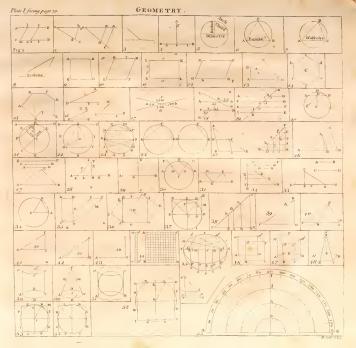
pondent natural number will be increased likewise.

3. If the logarithm of any number be added to itfelf, (or which is the same thing, if it be doubled) the sum will be the

logarithm of the square of the natural number.

4. If the logarithms of any two numbers are known, the logarithm of the product of those two numbers may with certainty be found: For, if the two known logarithms are added together, their sum will be the logarithm of the product.

By a careful attention to these inferences, we may easily make loga-



logarithms to the following rank of natural numbers in a continued geometrical proportion, viz. 1:2:4:8:16:32:64:128, &c. which may be continued to any number of terms. Here 1 is the first term, and 2 the ratio; so every term is the product of the preceding term multiplied by 2, as will appear by bare inspection.

Unity (or 1) is the first natural number, and its logarithm must be a cypher (by Inf. 2.) for unity neither multiplies nor divides any number; so its logarithm must neither increase nor diminish

any other logarithm.

The logarithm of 2 may be assumed at pleasure, but this will determine the logarithm of all the rest: Suppose it 10; the next natural number is $4 \cdot \text{Now } 4$ is equal to 2×2 , therefore its logarithm will be 10 + 10 = 20, which must be the logarithm of $20 \cdot 10 = 20$. Add therefore the logarithms of these two numbers, viz. 20 and 10, and their sum 30 will be the logarithm of 8 (by Inf. 3 and 4.).

It is easy to observe, that as the rank of natural numbers is formed by a continual multiplication of each preceding term by the ratio; so their logarithms are formed by a continual addition of the logarithm of the ratio: And as this logarithm may be assumed at pleasure, so there may be different forts of logarithms, as

in the following, viz.

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1: 2: 4: 8: 16: 32: 64: 128: 256: 512: 1024 Numbers.
0: 10: 20: 30: 40: 50: 60: 70: 80: 90: 100 Logarithms.
0: 15: 30: 45: 60: 75: 90: 105: 120: 135: 150 Logarithms.
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It is evident, that either of these ranks of logarithms will answer the proposed end: For if it were required to multiply 32 by 8, the logarithm of 32 is 50, the logarithm of 8 is 30, and 30 +

50 = 80, which is the logarithm of $256 = 32 \times 8$.

This may fuffice to shew, that if there were a table of logarithms to all the natural numbers we should have occasion for, there would be no need of multiplication or division. The difficulty will be, to make such a table for all the intermediate numbers, which I presume the inventor might effect in the following manager.

Inftead of affurning the logarithm of 2, he might chuse 1.0000000 for the logarithm of the natural number 10, the double of which would be 2.000000; for the logarithm of 100,

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and the treble 3.0000000; for the logarithm of 1000, and so on, as in the following table.

Natural Numbers.	Logarithms.
1	0.0000000
10	1.00000000
100	2.0000000
1000	3.0000000
10000	4.0000000
100000	5.0000000

It is evident from the foregoing table, that the logarithms of all the natural numbers between 10 and 100 would begin with 1; between 100 and 1000 with 2; and between 1000 and 10000 with 3, &c. these initial figures are called characteristicks, and denote how many places the first figure of the natural number stands from unity: It is also evident, that the logarithm of any natural number under 10, would be less than 1, with 7 cyphers annexed, and therefore would begin with 2, 3, &c. with 6 figures more annexed. But to make it contain the same number of sigures as the logarithms of the numbers above 10, he prefixed a cypher to it, which is the characteristick of all the natural numbers under 10.

Having thus assumed 1.000000 for the logarithm of 10, the half of it 0.5000000 would certainly be the logarithm of the square root of 10, which the inventor with great care and pains must have extracted to 7 decimal places. If this root were multiplied by 10, the logarithm of the product would be 1.5000000, the half of which 0.7500000, would certainly be the logarithm of the square root of that product. In this manner, I presume, he proceeded to find the proportionals between 1 and 10, till the root came to more than 9, and then sound mean proportionals betwixt that and the next root less than 9, till at last, after a great number of trials, he came to the root, or absolute number 8.9999999, which is so very near 9, that it may be taken for the same, the logarithm of which he found, by the same number of additions and halvings, to be 0.9542420.

In the fame manner he might proceed to find the logarithms of 5 and 7, and having found these, the logarithms of 2, 3, 4, 6, 8, might easily be found, for half the logarithm of 9 would be the logarithm of 3, and if the logarithm of 5 is subtracted from the

loga-

logarithm of 10, the remainder will be the logarithm of 2, the double of which is the logarithm of 4, and that doubled again will be the logarithm of 8; and if the logarithm of 2 is added to the logarithm of 3, the fum will be the logarithm of 6.

By these means, I presume, after a great deal of indefatigable pains, and an uncommon application, he at last sinished his table, which was justly esteemed one of the most useful discoveries in the art of numbers, and has accordingly been universally received by all mathematicians, and the lord Neper is allowed the whole honour of the invention without any rival.

Other methods have been proposed by authors who have wrote on this subject, whereby the operations may be shortened in the construction of the table; but, as our design in this place is only to make the reader acquainted with the coherence of the logarithms and natural numbers, being the same with that of numbers in arithmetical and geometrical progression; I think the preceding method the most likely to answer that purpose, as being the most intelligible, and the fundamental principle, upon which those methods that have been found to shorten the work must be grounded. Tables being already calculated by the inventor, as well as by several succeeding mathematicians, to a great exactness, there is now no necessity for that trouble, we shall therefore, in the following propositions, shew the manner of finding logarithms in the tables, and some of their various uses in arithmetical operations.

PROP. I.

To find the logarithm of any given number.

Rule, Look for the number in the first column, (under N°) and if it consists of less than 3 figures, its logarithm will be found in the first page, with its proper characteristick. If it consists of 3 figures, it will be found in the following pages in the first column, and right against it in the column under 0, you will find its logarithm, with a proper characteristick.

If the given number confifts of 4 places, find the first three as before, and look for the last figure at top, and in the column under that, right against the three first figures, you will find the proper logarithm: Only you are to observe, that in this case the characteristick will be 3: For the absolute number must always contain

contain one place of integers more than the characteristick does of units. If one, or more, of the last figures are decimals, the logarithm will be the same: The difference will be only in the characteristick, which, as we have observed before, always denotes how many places the first figure of integers stands from unity; the following examples will be sufficient under this head.

Num.	Logar.	Num.	Logar.
8	0.903090		3.879038
88	1.944483	756.9	2.879038
699	2.844477	75.69	1.879038
5463	3.737431	7.569	0.879038

PROB. II.

To find the absolute number corresponding to any given Logarithm.

Rule, Without regarding the characteristick, look for the given logarithm in the table; and right against it, in the first column, under N°, you will find the three first figures, and at top, the fourth figure of the number required. But, if the number thus found should consist of fewer places than is expressed by the characteristick, the deficiency must be made up by annexing cyphers: And if it consists of more places, one or more of the last figures must be decimals, as in the following examples.

EXAMPLE I.

Let the given logarithm be 3.914872. Againft .914872; in the table you will find 822, in the first column under N°; so that, as the characteristick is 3, and the logarithm is sound in the column under 0 at top, the number sought will be 8220. But if the characteristick had been 2, the number would have been 822; and if it had been 1, the last figure would have been a decimal, and only the two first figures integers, viz. 82.2.

If the above logarithm .914872 had not been found under o, in the table, the fourth figure would not have been a cypher, but one of those at top of the table under which it had been

found.

EXAMPLE II.

Let the given logarithm without the characteristick be .018345. This will be found in the column which has the figure 6 at top;

the absolute numbers must therefore be taken to 4 places of figures at least, the characteristick always denoting how many of those figures must be reckoned as integers, as in the following, viz.

Logarithms	Numbers
5.918345	828600
4.918345	82860
3.918345	8286
2.918345	828.6
1.918345	82.86
0.918345	8.286

If the given logarithm cannot be had exactly in the tables, we must take the nearest to it; suppose it 3.86 to 80; the natural number corresponding thereto will be more than 7262, but less than 7263. But because the given logarithm is nearer to that of 7262, that may be taken for the required number: Those who incline to more exactness may find a figure of decimals by the following method.

From the given logarithm
Subtract the next lefs — 3.861080 difference
3.861056 is 24

From the next greater log.
Subtract the next lefs — 3.861116 difference
Subtract the next lefs — 3.861056 is 60

Then fay, as 60 (the difference betwixt the two nearest logarithms to the given one) is to 10 so is 24 (the difference betwixt the given and next less) to 4, the decimal required: So 7262.4 is the natural number corresponding to 3.861080.

That the natural number is by this method found to great exactness, may be proved by adding the logarithms of any two

numbers together whose product is equal to it.

The reason of this is plain, for if to the logarithm of 7262, be added 60, the natural number will be increased a whole unit; but if only 1 tenth, 2 tenths, &c. of 60 be added to it, the natural number will be increased only 1 tenth, 2 tenths, &c. of an unit.

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Hence,

Hence, by the reverse of this method we may find the logarithm of a number of five figures; for, after finding the logarithm of the first four figures, subtract that from the next greater logarithm in the tables; then say, as 10 is to the difference betwixt the logarithms so is the fifth figure in the natural number to the number to be added to the logarithm of the first four figures.

Let the number whose logarithm is required be 72624.

7263 3.861116 10:60::4:24, and
$$\frac{3.861056}{\text{difference 6o}}$$
 24 + 3.861056 = 3.861080

But because the natural number has five figures, the characteristick must be 4.

PROP. III.

Multiplication and Division by Logarithms.

Rule, Add or fubtract the logarithms of the natural numbers, their fums will be the logarithms of the products, and their remainders the logarithms of the quotients; and as the rule of Three requires both these operations, we shall refer thereto for examples.

PROP. IV.

The Rule of Three, by Logarithms.

Rule, Add the logarithms of the second and third terms together, and from the sum subtract the logarithm of the first term; the remainder will be the logarithm of the source required.

EXAMPLE. I.

1f 64 give 21, what will 72 give?

fecond term 21 1,322219.
third term 72 1.857332

product 1512 fum 3.179551
first term 64 1.806180

fourth term 23.62 1.373371

As the last logarithm cannot be had exactly in the tables, we must (as already observed) take the nearest to it, which is, 373280. against which, in the column under number, is 236, and the squre at the top is 2; so that 23.62 will be the nearest, for the characteristick being 1, the two last figures will be decimals.

We shall in the next examples show the use of the logarithms, when any of the terms are mixed numbers, or decimal fractions; and here we think it needless to perplex our readers with negative signs, as the whole business may be done by using the same process as if they were all integers; for then the characteristicks will all be positive, and denote how many places of sigures are contained in the product, or quotient; and we may find how many are decimals, by the very same rule that is made use of when the operations are performed by multiplication and division of the natural numbers.

EXAMPLE II.

If 16.5 give 3.75, what will 49.5 give?

We shall work this as if the terms were all integers, and likewise as mixt numbers; the difference will be only in the characteristick.

3·75 49·5	Log.	2.574031 2.694605		0.574031
185.625		5.268636 2.217484	or	2.268636 1.217484
11.25		3.051152		1.051152

In the first operation, when the logarithms of the second and third terms are added together, the characteristick is 5: This shews there will be fix figures in the product: But then, because there is one place of decimals in the multiplicand, and two in the multiplier, there must be three places of decimals in the product, and only the first three figures are integers. And this is agreeable to the characteristick, in the second operation; which being 2, shews there will be three places of integers; but this does not determine how many places of decimals will be requifite to compleat the product. Again, when the logarithm of the first, is subtracted from the sum of the other two, in the first o-

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CHAP. V.

peration the characteristick is 3, which shows there will be four figures in the quotient. But because there are three decimal places in the dividend, and but one in the divisor, there must be two decimals in the quotient. So the first two figures will be integers, and the last two decimals: It is the same by the second operation; where the characteristick is 1. The first operation seems to have the advantage of the second, because it discovers how many decimals will be in the product or quotient.

EXAMPLE III.

If 165 give ,375, what will ,495 give?

The figures in this being the same with the former, the operation will also be the same; the difference will be only in the value of the figures in the product, and quotient. The fecond and third terms being decimals, their product will likewife be decimals; and the characteristick being 5, it will confift of fix places: But when this comes to be divided by the first term, which is 165, all integers, the dividend will contain fix places of decimals more than the divifor, and therefore the quotient must likewise have fix decimal places; whereas, by the preceding operation, the characteristick of the logarithm of the quotient is three, which shows it will contain only four fignificant figures; to which there must be two cyphers prefixed, to make up the deficiency, and then it will be the same as if the operation was performed by natural numbers; .375 × .495 = .185625, and .185625 - 165 = 001125: But if the divisor is a fraction, as , 165, and the dividend the fame as before, then it will contain only three decimal places more than the divifor; fo the quotient must have three decimal places, .185625 ÷ ,165 = 1.125.

PROP. V.

Extraction of Roots, by Logarithms.

Rule, Divide the logarithm of the power by the index of the power, the quotient will be the logarithm of the root; but if the root be given, and the power required, multiply the logarithm of the root by the index of the power; the product will be the logarithm of the power.

NB. The index of the square is 2, of the cube 3, &c. See Chap. 1. Sect. 1.

EXAMPLE I.

What is the square root of 576?

Log. Index Log.

Power 576 2.760422 ÷ 2 = 1.380211, the natural number corresponding to which is 24, the root required.

EXAMPLE II.

What is the cube root of 13824?

This number, confisting of five figures, cannot be found in the tables, therefore we must make use of the method in Example 2. Prop. 2. of this Chap. viz. find the logarithms of 1382, and of 1383, their difference will be 314; then 10: 314::4: 125.6

Log. Log. Log. 1383 140822 Dif 1382 140508 Log. of 13824 is 1382 140508 3144 140508 $314 \times 4 = 1256 \div 10 = 125.6$ 125 1380211, and

the natural number corresponding to this last logarithm is 24, which is the cube root of 13824.

EXAMPLE III.

Admit two cylinders of equal length; the diameter of the one 32 inches, and its content 4096 cubic inches, the diameter of the other 16 inches, required the content in cubic inches?

Here, as the lengths are equal, the contents will have the fame proportion to one another, as the areas of their bases, which being circles, it will be as the squares of their diameters; that is,

As the fquare of 32 (whose Log. 1.505150×2 is =3.010300) Is to the contents 4096 (whose Logarithm is = 3.612360) So is the fquare of 16 (whose Log. 1.204120×2 is = 2.408240) fum 6.020600

To the required contents 1025 (whose Logarithm is = 3.010300)

EXAMPLE IV.

Admit 93 feet to be the length of the keel of a ship of 508 tons, and a ship of 400 tons to be built, exactly similar to the

other; required, the length of her keel?

In order to folve this is must be observed, that the contents of similar solids have the same proportion to one another, that the cubes of their similar sides have, therefore, the following will be a general proportion in all cases where the dimensions are similar, viz.

As the tonnage of any ship, or the solid contents of any body, is to the cube of the keel, or any other part; so is the tonnage of any other similar ship, or the contents of any other similar body, to the cube of her keel, or any other similar part. Hence, 508: cube of 93:: 400: cube of the required keel, the cube root of the south term must be extracted, for the length of the keel: First, to cube 93, by the logarithms.

93 1.968483 × 3 =	5.905449 Log. of the cube of 93
400 its Log. is	2.602060
fum of 2d and 3d terms	8.507500
508 first term, its Log.	2.705864
Log. of the cube, divide by 33 85.88 the required keel (or 86 nearly)	5.801636 1.933878

Here the usefulness of logarithms is very evident, for the cube of 93 would consist of 6 places, as appears by the characteristick; and this again being multiplied by 400, the product would consist of 9 places; and when this product is divided by 508, the quotient will have 6 places; and the cube root of this must be extracted to four places at least; for 85.88 is the length of the keel required, being the nearest natural number to the Log. 1.933878.

What has been already faid, we prefume, is fufficient to recommend the practice of these admirable numbers to our readers, though they may be extended to the solution of most questions which require an arithmetical calculation. But they do not stop here; for they discover a method of performing the foregoing o-

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perations, even without the help of numbers: This is effected by the line of numbers invented by Mr Gunter, which we shall treat of in the next chapter, and shall only here remark, that numbers may be added or subtracted, by a scale of equal parts and a pair of compasses, as in the following examples, where we shall make use of the same scale of equal parts before described, as in Plate 2. Fig. 1.

EXAMPLE I.

Let the two given numbers be 36 and 48.

Rule, Extend from the point A (where the line A B begins) to either of the given numbers, suppose 36; set the same extent forwards from the other given number 48, and it will reach to 84, the sum required in the same line A B.

EXAMPLE II.

Let it be required to find the fum of 3010 and 4771. As these numbers cannot be had on the line AB, find them in the diagonals, and transfer them to the line AB, in the points x, z; the extent from A to x will reach from z to y. Now, to find the value of y, take the distance of the point y from figure z, in the line AB, and set it off from figure z, in the line AB, will intersect the diagonal next before z, in the required point, which will be found to be z.

As fubtraction is only the reverse of addition, it will be needless to give any examples, this being not intended for practice.

The reason of the operation is so plain, as to require no demonstration: For if two rulers, one of ten inches, and another of sourteen, be laid so as to make one strait edge when joined to one another, they will make 24 inches; and if there be six inches cut off from a ruler of 24 inches, there will remain only 18 inches.

CHAP. VI. SECT. I.

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Construction of the Line of Numbers.

PLATE HIS line may be of any length, but as there must be a particular scale adapted to it, we shall fix upon the line Fig. 1. A B, which being divided into 10,000 equal parts, will answer our purpose.

The intent of the line of numbers is only to add or fubtract logarithms, fo that all that is necessary to this end is to place the

logarithms properly upon the line.

The logarithm of 10, by the table at the end of the book, is 1.00000. But because our scale contains only 10,000, we shall fix upon that number for the logarithm of 10, and

all those under 10 will be as in the margin. Find 1-0000 them all amongst the diagonals, and transfer them to 2-3010 the line A B in the points x, z, t, p, y, s, r, n. 3-4771 · Draw the line G H, parallel and equal to the line 4-6020

A B, and transfer the points x, z, t, &c. to this line 5-9990 6-7781 from the line A B.

We have now the logarithms of all the numbers 7-8451 from 1 to 10 upon the line GH; and if to the end 8-9030 of it be joined another line, of the same length, 9-9542 and graduated and numbered properly, we shall 10-1000 have all the numbers from 1 to 100. But as our

scale will not admit of these; draw the line EF parallel and equal to G H; and instead of doubling the line G H, take E N, (half the line E F) and make it the length of a line of numbers, by transferring the logarithms, as was done on the line G H, but there must be a scale of equal parts adapted to the line EN, which must contain 10000 equal parts, if we make use of the fame table of logarithms as before. And by this means the line A B would contain 20000 equal parts, which would require double the number of parallels. Instead then of making a new scale, we may make the fame diagonals answer our end: For it is only taking taking half the logarithms. We shall therefore accommodate the PLATE logarithms to our scale, as in the margin; transfer all these from the diagonals to the line E N in the points 2, 3, 4, 5, 6, 7, 8, 9, 1; Fig. 1.

then graduate and number the line N F, the other half of the line EF, exactly as the line EN. These 1-0000 last will be the logarithms of 20, 30, &c. for the lo-2-1505 garithms of 20, 30, &c. are the logarithms of 2, 3, 2-2385 &c. added to the logarithm of 10; but EN is the 4-3010 5-3495 logarithm of 10; E2, E3, the logarithms of 2, 3, &c. therefore, if N 2, N 3, &c. be made equal to E 2, E 3, &c. E N 2, E N 3, &c. must be the loga-6-3890 7-4225 8-4815 rithms of 20, 30, &c. They may be transferred to the line N F from the diagonals, if to each of the lo-9-4771 garithms in the margin we add 5000. So the loga-10-5000

rithm of 20, will be 6505, the half what it is in the tables. Now to find the units, or intermediate points betwixt 10 and 20, 20 and 30, &c. find in the tables, the logarithms of 11, 12, 13, &c. to 20, and the logarithms of 21, 22, &c. these must be divided into two equal parts, to accommodate them to our scale; and being found in the diagonals, they may from thence

be transferred to the line NF.

We have now the whole line E F divided into 18 unequal parts; 1 at E, and the figures 2, 3, &c. denote so many units; I at N, and the figures 2, 3, &c. to F, denote so many tens; I at F 100: The intermediate divisions betwixt the figures in the line NF are units; fo the 6th division betwixt the figures 2 and 3 is 26; the first betwixt figure 1 and 2 is 11, and so of all the reft.

If the spaces betwixt the figures in the line E N be graduated, as those in the line N F, they will be tenths of units: And because the difference betwixt the logarithms of 1 and 10, the logarithms of 10 and 100, and of 100 and 1000 are all equal; 1 at the point E may be accounted 10, and 1 at N 100, at F 1000. The figures in the line EN will now be tens, and those in the line NF hundreds. The intermediate divisions betwixt the figures in the line E N will now be units, and those in the line N F will be tens. So 3 in the line EN will be 30, and in the line NF 300. The divisions in the line EN betwixt 5 and 6, will be 51, 52, &c. in the line NF 510, 520, &c.

In order to find the points for 101, 102, 121, 122, &c. we M must PLATE must find the logarithms of those numbers, and transfer them from II. the diagonals as before directed; which would require the spaces Fig. 1. betwixt the figures to be divided into 100 equal parts; but the length of our scale will not admit of this. The divisions betwixt the figures 1 and 2 are sub-divided into five, by transferring the logarithms of 102, 104, 122, 124, &c. and the divisions betwixt 2 and 3 are only sub-divided into two, by transferring the logarithms of 205, 215, 235, &c. The spaces betwixt the other figures are only divided into ten; so the units can only be had by

taking $\frac{1}{4}$, $\frac{1}{4}$, $\frac{1}{3}$, &c. as near as the judgment can direct.

The line being thus constructed, it will be easy to find any number upon it: And that this may be done with all possible expidition, where the spaces are divided into ten parts betwixt the figures, every fifth is distinguished by longer strokes than the tens. Again, where the spaces can admit of being divided into more than ten parts, the fub-divisions are distinguished by shorter strokes than the tens. Now the value of these strokes are determined by the value of the figures, which being arbitrary, they must be determined before we can find any number upon the line. If the number be less than 100, 1 at E may be unity; then 1 at N will be ten, 1 at F 100. The strokes representing the tens in the line E N, will be tenths of units, and those in the line NF will be units. The short strokes betwixt the tensare estimated according to their number, for if there were 9 intermediates, each would be rooth part of an unit in the line E N, and tenths of units in the line N F. If there be only 4 intermediate strokes. each will be 200th parts, or two tenth parts of unity: And if there be but one stroke, it will be 500th, or 5 tenths.

If 2 were required, look for that figure in the line E N; if 20, it will be at 2 in the line N F; if 35, or 3.5, count five ftrokes beyond the figure 3 in the line E N; this, as was before observed, will always be longer than any of the others. If 400 were required, 1 at E must be accounted ten, 1 at N 100: So figure 4 in the line N F will be 400; 470 will be 7 strokes beyond figure 4; 475 will be in the middle betwixt the 7th and 8th stroke beyond figure 4; if 473, we must take little more than \$\frac{1}{2}\$ of the space betwixt the 7th and 8th stroke, but this cannot be had to a great

niceity.

The line G H is called a fingle line of numbers, and the line EF a double one: This last containing double the numbers that

the former does; and it is only two lines of numbers joined to PLATE one another, both graduated and numbered alike.

It is very plain that the figures 2, 3, &c. in the line G H Fig. 1, 2. are double the distance from one another, that the same figures are in the line E N or NF; so that we may, by inspection, find either the square or root of any number on these lines. A few

examples will illustrate this.

Let it be required to find the fquare of 6. To do this, is to multiply it by itself, or to double its logarithm. Now this is at the point 6 on the line E N, extend therefore from E to figure 6. the same extent will reach from 6 to $36 = 6 \times 6$: But 36 is double the distance from E that 6 is; and 6 in the line GH is likewise double the distance from G that 6 in the line E N is from E: So we shall have no occasion for compasses; we need only look for the root on the line GH, and the square will be on the line EF right against the root: If the root be less than 10, 1 at G and at E may be units; but if it exceed 10, 1 at G must be 10, and 1 at E 100: If the fquare be given, and the root required; look for the square on the line E F, and the root will be against it on the line GH. Let the fquare root of 81 be required. 81 will be found in the line NF, and will be double the distance from E, that the root is from E. We must therefore find, by compasses, half the distance from E to 81, and whatsoever figure or point is at this middle point in the line EF; the figure of the fame name, or point of the same value in the line G H, will be double that distance from G, and therefore must be against 81; and in this case o is the fquare root of 81.

As the square of any number is double the distance of the root Fig. 2, 3, from E; so is the cube of any number triple the distance of its reot from the point E. And in order to find the cubes or roots of numbers by inspection; draw the line I K equal, and parallel to the lines E F, and G H. Divide it into three equal parts in the points L, M. Make each of these a line of numbers, either by adapting a scale of equal parts to it, or taking one third of the logarithms, and making use of the same diagonals as before. This line is called a triple line of numbers. Now if the cube root of any number be required; look for the cube on this line, and its root will be right against it on the line G H; for the same reafons, that the square is on the line E F. If the root be given, and

the cube required; look for the root on the line G H, and its

cube will be on the line I K, right against the root.

Note. Because the lines GH, EF and IK, are at too great a distance from one another to find the cubes, squares and roots, without a pair of compasses; there is a double line drawn close to the single line, as in Fig. 2. and a single line drawn close to the triple line, as in Fig. 3. so that they may serve for a table of cubes and squares.

S E C T. II.

Of the Use of the double Line of Numbers:

It is evident from the construction of the line of numbers, that the logarithm of any number may be had by a pair of compasses: Thus, extend from the beginning of the line to the number whose logarithm is sought; that extent measured on the scale of equal parts, will give the logarithm required.

EXAMPLE.

Let it be required to find the logarithm of 4.

Extend from the beginning of the line to 4; that extent meafured on the scale of equal parts will give 6021, which is the logarithm of 4. The like may be said of any other number; which is very plain, being only the reverse of the method by which the line was constructed.

The intent of finding the logarithms of any numbers in this manner, is in order to add, or fubtract them. But if this can be done by the line of numbers only, we shall have no occasion for

the scale of equal parts.

We have already shewn how to add any two numbers by the scale of equal parts; therefore we may add the logarithms of any two numbers in the same manner; and the sum will be the logarithm of their product.

E X A M P L E.

Let it be required to add the logarithm of 3 to the logarithm of 41.

This

This cannot be done by the scale of equal parts without having a table of logarithms; but this defect is supplied by the line of numbers. The logarithm of 3, by the table, is 4771, and the logarithm of 4 is 6021. Now the points 3 and 4 upon the line of numbers, are the same distance from the beginning of that line, that the numbers 4771 and 6021, are from the beginning of the scale of equal parts: So that it will be the same thing to extend from the beginning of the line of numbers to 3, that it would be to extend from the beginning of the scale of equal parts to 4771, and when this extent from 1 to 3 is set forward from 4, it will reach to 12, which point is 10792 equal parts from the beginning of the line of numbers; and that number being the sum of 4771 and 6021 (the logarithms of 3 and 4) it is the logarithm of 12, as appears by the table.

Multiplication by the Line of Numbers.

Rule. Extend from 1 to either of the given numbers, that extent will reach from the other given number to the product: A few examples will suffice to illustrate this.

EXAMPLE I.

Let it be required to multiply 8 by 6.

1:6::8:48.

The extent from 1 to 6 will reach from 8 to 48.

EXAMPLE II.

Let it be required to multiply 98 by 8.

Here the distance from 1 to 8, when set forward from 98, will go beyond the end of the line; for, if 1 at the beginning of the line be unity, all the figures on the first part will be units, and those on the second, tens, and 98 will be within two divisions of the end of the line. In this case, 1 at the beginning of the line must be accounted 10, so 98 will be sound on the first part of the line; and because the extent from 1 to 8 is the same as from 10 to 80; when this is set forward from 98, it will reach to 784, the product required.

1: 8:: } 98:784.

A flider having a line of numbers upon it, exactly the fame with that on the rule, will perform the office of a pair of compaffes; and being readier for practice, we shall shew how to

work by it.

As in the first example, let it be required to multiply 6 by 8. Set I upon the slider, against 6 upon the rule, look for 8 upon the slider, and against it, is 48 upon the rule; and when the slider is thus set, we have the product of any number multiplied by 6; for against 2 is 12, against 6 is 36, against 10 is 60, against 16 is 96; but 17 on the slider goes beyond the end of the line upon the rule. In this, and in such like cases, the value of the figures must be alter'd, as observed before; and I at the beginning must be 10, and 17 will be found in the first part of the line upon the slider, and against it you will find 102 upon the rule. If the number had been 170, the operation would have been exactly the same; it would be only calling the 1, 100, and adding a cypher to the product 102, which would make it 1020.

Division by the Line of Numbers.

This is only the reverse of multiplication, for the extent from the divifor to the beginning of the line, fet back from the dividend, will reach to the quotient. Or by the slider; fet the divisor on the slider against 1 on the rule, and against the dividend on the slider, you will find the quotient on the rule.

E X A M P L E.

Let 48 be divided by 8.

8:1::48:6.

Set 8 on the flider, against 1 on the rule; and against 48 on the flider is 6 on the rule; and, without moving the flider, we have the quotient of any number divided by 8, by inspection; as the reader

will eafily perceive upon examination.

Hence, to reduce a vulgar fraction into a decimal, add a cypher to each part of the fraction; and if the denominator upon the flider is fet against 10 on the rule; then against the numerator you will find the decimal fraction upon the rule. Thus, the vulgar fraction of or or or will be found .75 in decimals.

The Rule of Three by the Line of Numbers.

This is only to find a fourth proportional to three given numbers. Rule. Place the numbers, or suppose them to be placed, as in the rule of three direct; then extend from the first to the second; that extent set the same way from the third, will reach to the fourth number required.

By the flider, fet the first term upon the flider against the second term upon the rule; and against the third term upon the

flider you will find the 4th term required upon the rule.

EXAMPLE.

Let the given numbers be 12:20::27, to which a fourth is required that shall bear the same proportion to 27, that 20 does to 12.

Set 12 upon the flider against 20 on the rule; and against 27 upon the flider, you will find 45 upon the rule, which is the fourth term required; for 12:20::27:45, the product of the extremes ($12 \times 45 = 540$) being equal to the product of the means ($20 \times 27 = 540$).

In order to demonstrate the reason of this rule, it will be proper to observe; that to perform the operation by figures, 20 must

be multiplied by 27, and the product divided by 12.

By the method already shewn for multiplication by the line of numbers, the extent from 1 to 20, set forward from 27, will reach to 540, the product; but then, as this product is to be divided by 12, the extent from 12 to 1 must be set back from this product 540. Now it is very plain, that in effect, we only set the distance between 12 and 20 forward from 27: For as we are obliged after we have set forward the distance between 1 and 20; to set back the distance between 1 and 12; it is plain, that betwist this last point and 27, there will be exactly the same distance as there is between 12 and 20.

It must be observed, that in extending, if the second term is greater than the first, the sourth term will be to the right hand of the third; but if it be less, it will be to the lest hand of the third. When we use the slider, it is indifferent whether the first term be taken on the slider, or on the rule, provided the third term be taken on the same line as the first is. Neither is it material which

of the means is taken for the second term; for 12:20::27:45;

and 12:27::20:45.

Having now fully explained the confiruction and use of the line of numbers, we shall give some examples in cases that most commonly occur to the shipwrights. And as the slider is most expeditious, we shall always make use of it.

EXAMPLE I.

Suppose it were required to know how much an artificer would

gain in 30 days, at the rate of 3 shillings per day?

To reduce this to the rule of three, it will be 1:3::3::90, and when the slider is so set, that is 1 against 3, then will 90 be against 30. But as the answer to these, and such like questions, is sometimes required in pounds, this must again be divided by 20; and the operation by the pen would be $3 \times 30 \div 20 = 4.5$. Now, here are two numbers to be multiplied by one another, and divided by a third, therefore it will be 20:3::30:4.5: And instead of setting 1, set 20 against 3, and against 30 you will find 4, and 5 of the small divisions, which are tenths; each of which, in this case, must be reckoned 2s. so that, 4 and 5 tenths will be 4l. 10s. od.

EXAMPLE II.

What is the 3 fifths of 45?

As the 3/5 ths of 5 is 3, fay by the rule of three.

If 5 gives 3, what will 45 give? The answer will be 27, for

5:3::45:27.

From this example, take the following rule for finding the quarters of masts and yards, having the partners and slings given; and also the fraction, that the quarters must be of the partners, or slings.

Rule. Set the denominator of the fraction against the nume-

rator, and against the slings; will be the quarter required.

EXAMPLE III.

If a yard is 25 inches at the slings, what will it be at the yard arm, the proportion being this of the slings?

Set 5 against 2, and against 25 you will find 10. 5:2::25 10. EX-

EXAMPLE IV.

If a ship of 69 feet by the keel, be 23 feet broad; how broad will a ship of 75 feet be, that is built in the same proportion?

Set 69 against 23, and against 75, you will find 25; and the flider being thus set, we have by inspection, the breadth of any hip, if the length of the keel is known, and the proportion, the same as above. If the keel is in set and inches, it will be proper first to work for the seet, and then for the inches.

EXAMPLE V.

What will be the breadth of a ship whose keel is 75 feet 9

inches, the proportion being as 3 to 1?

Set 3 against 1, and against 75 you will find 25; and without moving the slider, against 9 (inches) you will find 3; so the breadth required is 25 feet 3 inches.

EXAMPLE VI.

Suppose a ship to be of the following dimensions, viz.

Length of the keel — — 93 feet 4 inches.

Extream breadth — — 32 0

Breadth at the transom — 18 4

Breadth at the top timber line — 26 0

And suppose several other ships are to be built in the same proportion, and the lengths of the keels are given, as follows; the other dimensions will, by the foregoing method, be found to be as in the columns, viz.

the keels.		Break	ths.	thet	ran.	Bre. at the		
f.	in.	f.	in.	f.	in.	f.	in.	
308	IO	37	4:	21	43	30	3	
				23			7	
123	0	42	0	24	01	34	o	

What has been faid in Example 4, will suffice for finding all these dimensions.

EXAMPLE VII.

The length of the keel, and extreme breadth, being given;

to find the tunnage.

The general method is to multiply the length of the keel by the breadth, and that product by the half breadth; then divide by 94; and the quotient will be the tunnage required: Or, which is the fame thing, multiply the breadth by the is breadth; then fay as 94: is to this product: fo is the length of the keel: to the tunnage.

Let the length of the keel be 93 feet 4 inches, and the breadth

32 feet.

The operation by the pen will be 93 feet 4 inches x 32 =

 $2986.8 \times 16 = 47786.8 - 94 = 508\frac{3}{24}$

The first step by the slider will be, set 1 against 93.4 (or 93 seet $\stackrel{\leftarrow}{\leftrightarrow} = 93.33$), and against 32 will be 2986.8. Now as this product is to be multiplied by 16, and divided by 94, it will be 94:2986.8::16:508 $\stackrel{\leftarrow}{\leftrightarrow}$; therefore, if you move the slider till 94 is against 2986.8, the tunnage 508 nearly, will be against 16. In finding the first product, there is no occasion for estimating the number, only let it be marked, so that 94 may be moved ti; we shall shew in another place how this may be done at once by the slider.

By a careful attention to the manner of folving these questions, it will be easy to apply the slider to any other question in the rule of three, whether direct or inverse; or any thing else that is per-

formed by multiplication or division.

We shall only add a few examples in measuring plank and timber.

Of measuring Plank.

We observed in Chap. 4. Sect. 3. that all plank is considered as an oblong square, and measured as a plain surface, without any regard to the thickness; and that all the varieties thereof may be reduced to the rule of three by the following proportions.

1: length in feet:: breadth in feet:
12: length in feet:: breadth in inches: } area in feet.

144: length in inches:: breadth in inches: J.

EXAMPLES.

Let there be 5 planks of the following dimensions.

L.	B.	L.	B.	Area.	L.	B. Area.	- v L. B.Area.
£.	in.	f.	· f	-f	00 f.	in. f.	in. in. f.
							or 144:240:: 9:15
		1:40::					or 144:480:: 6:20
36	12 >	1:36::	I:	36; or	12:36:	12: 36;	or 144:432:.12:36
30	15	1:30::	1.25:	37.5; or	12:30::	15:372;	or 144: 360::15:37
15	187	1:15::	1.5:	22.5; or	12:15::	18:221;	or 144:180::18:22;

Here every example is done 3 different ways; which method may be very useful for proving the examples, of which our readers may furnish themselves for practice with as many as they please, the above containing 15 different questions in the rule of three, which we presume sufficient for our purpose: Their solutions will be found as before directed: For if 1 at the beginning of the slider be accounted 1 tenth, 1 in the middle will be unity. If then this 1, in the middle of the slider, be set against 20, on the rule; then will 15 on the rule be against 75 on the slider: Or, if 12 be set against 20; then 15 will be against 9: And if 144 be set against 240, 15 will likewise be against 9. The like may be said of all the rest.

Of measuring Timber.

We have shewn before how this may be done by the pen, viz. by finding the superficial content, as if it was plank. This multiplied by the thickness in inches, and the product divided by 12, the quotient will be the content in feet. So that here there will be two operations: The proportions are,

1st. 12: length in feet:: breadth in inches: area in feet.
2d. 12: area in feet:: thickness in inches: contents in feet.
Or, 1: breadth in inches:: thickness in inches: a fourth number.
And 144: fourth number: length in feet: contents in feet.

That is, multiply the breadth by the thickness, if both be inches, and this product by the length in feet; divide the last product by 144, the quotient will be the content in feet.

Required the content of a piece of timber 20 feet long, 18 inches broad, and 15 inches thick.

1ft. 12:20::15:25 Then 12:25::18:37 Or, 144:270::20: 37 Tr

Here we must draw out the slider twice; first 12 against 20, then 25 will be against 15; secondly 12 against 25, and 37 ± will be against 20, or 1 against 18; 270 will be against 15, and if 144 be set against 270, 37 ± will be against 20 as before. There will be no occasion to estimate the value of the fourth proportional to the three first numbers; it will be sufficient to mark it so as that the slider may be moved till 12 or 144 be against this point: But as this will be attended with some inconveniency, it will be best to make use of the inverted line, which performs it at once without moving the slider twice.

Description and Use of the inverted Line.

The flider is fitted betwixt two double lines of numbers, of which the lower one is inverted, in fuch a manner, that 12 upon the inverted line; is exactly againft 12 upon the upper line; fo 20, 30, &c. upon the inverted line, are as much to the left hand of the point 12, as 20, 30, &c. are to the right hand of the point 12 upon the upper line. In reading the inverted line, we begin at the right; and because the distance betwixt 1 and 12 is more than that betwixt 12 and 100, the inverted line begins at 1.4, for 1 would extend beyond the end of the ruler.

Now the slider having two double lines of numbers, graduated exactly as the upper line, it will follow that whatever way the slider be moved, the point 12 upon the upper line on the rule, and the point 12 upon the lower line on the slider, will be both

against the same number.

To measure Timber by this Line, when the Breadth is not the same with the Thickness, and both given in Inches, and the Length in Feet.

Rule. First find any of the three given numbers upon the inverted line; then as this number upon the inverted line: is to either of the two given numbers upon the slider: fo is the third given

given number upon the upper line: to the content in feet upon the slider; observing that the upper line upon the slider, compares with the upper line upon the rule, and the lower line upon the slider with the inverted line.

As in the foregoing example; suppose a piece of timber 20 feet long; is inches broad, and 15 inches thick; set 15 on the inverted line, against 18 on the slider, and against 20 on the upper line, you'll find 37 1 upon the slider; the content the same as by the

two operations.

The reason of this will appear very plain, only by considering in what manner it is performed by two operations, and making use of the same slider, and the upper line with which it compares: For first, to find the fourth proportional to 12:15::18, we draw the flider out till 15 upon it is against 12 upon the upper line; and when in this position, 12 upon the slider will be against 15 upon the inverted line. Now the fourth number willbe on the flider against 18 upon the upper line, which will be 22: And because 18 on the upper line, is the same distance from 12 upon the same line, that 18 is from 12 upon the slider: or which is the same thing, that 18 upon the slider is from 15 upon the inverted line; when we draw the flider to the left hand, to bring 22 1, the fourth number, to 12 upon the upper line; the point 18 upon the flider will likewife come as far to the left, and therefore will be against 1 ; upon the inverted line; which is the very thing we are directed to do by the rule; and when it is thus fet, 12 upon the upper line will be against the fourth number on the flider; and the content, without moving the flider, will be found upon it against 20 upon the upper line.

The all plank is measured as a surface; the value is estimated by the load, which is 50 solid seet: The sollowing proportion will serve to find how many superficial seet of plank will make a load, viz. As the inches thick: is to 12:: so is 50 the solid seet.

in a load : to the superficial feet.

EXAMPLES,

How many superficial feet of 2, 3, 4, inches plank will make a load,

2:12::50:300

2: 12:: 50: 300 3: 12:: 50: 200 4:12:: 50: 150

SECT.

SECT. III.

Of the fingle Line commonly called the girt Line.

I T was observed before in the construction of this line, that the figures upon it are double the distance from one another, that the same figures are upon the double, and triple the distance that they are upon the triple line: Also that the cube and square roots were had by inspection. We shall now show the use of it in measuring timber: And sirst,

Case 1. When the timber is square, that is, when the breadth and thickness are both alike, and given in inches, and the length

in feet; to find the content in feet.

Rule. Set 12 upon the girt against the length on the double line, and the content will be on the double line, against the thickness on the girt.

E X A M P L E.

Required the content of a piece of timber 8 inches thick, and 9 feet long. Set 12 upon the girt, against 9 upon the double line; and against 8 upon the girt will be 4 upon the double line; the required content in feet. The reason of this will appear very plain. If we work it by the double line, the proportion will be 144: (8×8) 64::9:4; so the extent from 144 to 64 will reach from 9 to 4; and if we move the slider till 144 upon it, be against 9 upon the double line, then will 4 be against 64. Now, if instead of 144 and 64 upon the double line on the slider, we take 12 and 8, the roots of these numbers upon the girt line; they being the same distance from one another, they will perform the same office; and because 144 is always the first term, and the square of the thickness the second term, the rule will be general.

This might likewise be performed by the double line without moving the slider twice: The proportions will be 12:8::9:6. Now when 12 is set against 8, then will 6 be the sourch proportional to the three first numbers; and in the next three numbers, the first and second terms being the same as before, there will be no occasion to move the slider; only look for 6, the sourch numbers.

ber

ber before found upon the same line with the 12, and against it you'll find 4, the content, upon the same line with the 8.

Case 2. When the breadth and thickness are unequal, to find

the contents by the girt line.

First find a mean proportional between the breadth and thickness, in inches; then set 12 upon the girt, against the length in feet upon the double line and against the mean upon the girt; will be the contents in seet upon the double line.

EXAMPLE.

Required the contents of a piece of timber 20 feet long, 18 inches broad, and 15 inches thick. Before this can be done we must find the mean thus.

Look for either of the given numbers, suppose 18, upon the double line, and move the slider till this number is opposite to 18, the same number, upon the girt line; then look for 15, the other given number, upon the double line; and against it you'll find the mean required upon the girt line, which will be a little more than 16.4; and when 12 upon the girt is set against 20 on the double line; against the mean on the girt is 37 ½, the content on the double line.

But it is plain that this method requires two operations; one to find the mean, and the other to fet 12 to the length; fo that it

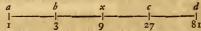
will be better to use the inverted line, as before directed.

To demonstrate the reason of this method of finding the mean, it must be observed, that to do it by the pen, the two] numbers must first be multiplied into one another, and then the square root of the product will be the mean required. Let the two numbers be 3 and 27; their product is 81, the square root of which

is 9, the mean required; for $3 \times 27 = 81 = 9 \times 9$.

Now to do this by the line of numbers, we must first extend from 1 to 3; that from 27 will reach to 81: And to find the square root of 81, we must find the middle point betwixt 81 and the beginning of the line; but this will be exactly in the middle betwixt 3 and 27; for let the extent from 1 to 3 upon the line of numbers, be represented by the line ab; and let c be the point 27; the extent ab set forward from c, will reach to the product 81 at d. Now to find x, the middle of the line ad, divide bc into two equal parts, which will give the point required: For

a b, and c d, being equal by construction, they will be equally distant from the point x, the middle of the line.



The figures on the girt line, as was observed before, are double the distance from one another, that the same figures are upon the double: Therefore when 27 on the double line, is set against 27 on the girt, 3 on the double line, which then will be against 9 on the girt, must be the middle point betwixt 3 and 27 upon the girt, must be proved by a pair of compasses; though these two numbers 3 and 27, are not to be sound upon the girt line, which begins on most of the sliding rules at 4, and ends at 40: Now it is very plain, that if the line was produced to the left, of a sufficient length to begin with 1, that point would be as far to the left of 4, as 10 is to the left of 40; and 2 and 3 would likewise be as far to the left of 4, as 20 and 30 are to the left of 40; and if the extent from 40 to 30 be added to that betwixt 9 and 4, these two will be found equal to the extent betwixt 27 and 9.

The reason I presume, for calling the single line the girt line, is, because when the quarter of the circumference is taken for the side of the square, the tree is girted with a line, and the breadth and thickness being supposed equal, the content will be readily found by this line; and the reason for beginning at 4 will appear by the following examples.

EXAMPLES.

Let there be 3 pieces of timber of 30 feet each, their breadth and thickness equal as below.

Long.	Thick.	Contents.
30	8	13.3
30	9	
30	23	100

If the girt line begins at 1, when 12 upon it is fet against 30 upon the double line, then 8 and 9 will be beyond the end of the double line; so the content cannot be had, unless we observe what point of the girt line is against 1 at the end of the double line, and then bring 1 at the beginning of the double line against the

the fame point; whereas by beginning at 4, we can have the content for any thickness from 4 to 40.

But this line may be adapted to feveral other uses: We shall only men-

tion the three following, viz.

1st. The length and breadth of a ship being given; to find the tonnage. It was observed in Exam. 7. Sect. 2. that the method of doing this required two operations, viz. First to multiply half the breadth by the breadth; then, as 94 is to this product; fo is the length of the keel to the tonnage. Now if we double the first and second terms, their products will be proportional to the third and fourth terms as before; the double of the second term is equal to the square of the breadth, and 188 is the double of 94; therefore 188 is to the square of the breadth; as the length of the keel, is to the tonnage. So that if 188 upon the double line of numbers on the slider, be fet against the length of the keel upon the double line on the rule; then will the tonnage be upon the rule, against the square of the breadth upon the slider. But if, instead of the first and second terms upon the double line, we take their roots upon the girt line, because they are the same distance from one another; the tonnage may be found without moving the flider twice, as in the following example, where we shall take the same dimensions as before,

EXAMPLE.

Length of the keel 93 feet 4 inches, breadth 32 feet; required the tonnage.

Rule. Set the tonnage point upon the girt against 93 feet 4 inches, upon the double line; then against 32, the breadth upon the girt, is 508

upon the double line; the required tonnage.

Note. The tonnage point upon the girt may be found by fetting 10 upon the girt, againft 10 upon the double line; then againft 188 upon the double line, make a mark upon the girt, which will be the tonnage point. Hence, if the length and tonnage be given, and the breadth required; fet the tonnage point againft the length upon the double line; then the breadth will be on the girt, againft the tonnage on the double line. But if the tonnage and breadth are given, and the length required; fet the tonnage upon the double line, againft the breadth on the girt; then will the length be on the double line, againft the tonnage point upon the girt line. As if it were required to find the breadth of a fhip of 300 tons, the length of the keel being 78 feet: When the tonnage point is let againft 78, then will 27, the required breadth upon the girt, be againft 300 upon the double

line: Or suppose the breadth 26 feet, and tonnage 280; required the length of the keel. Set 280 upon the double, against 26 on the girt line; then against the tonnage point is 78 on the double line, the required length of the keel. So in this case, one foot in breadth will increase the tonnage 20 feet, which may be seen without moving the slider.

2d. To find the content of a tree by the girt line, the diameter and length being given, and supposing it to be hewed so as that the two wanes

shall be equal to one square.

We observed before, that if by the wanes be understood, what the slat wants to compleat the side of the square, the proportion would be, as 180, is to the square of the diameter in inches; so is the length in feet, to the contents in feet. Instead of the two first terms upon the double line, take their square roots upon the girt: The root of 180 will be found nearly 13.4, but there is no occasion to estimate the value, but only to find the point, which will be done by setting 10 on the girt against 10 on the double line, and the point will be upon the girt line against 180 upon double line.

E X A M P L E.

Suppose a tree 20 feet long, and 30 inches diameter: Required what the content will be when hewed, so as that the flat shall be equal to half the thickness?

Set the point upon the girt, found as now directed, against 20 on the double line; and against 30 on the girt, is 100 upon the double line; the

required content in feet.

But if by the wanes, be understood the round parts of the tree where there is no wood taken off; the proportion, as was before observed, will be, as 193 nearly, is to the square of the diameter; so is the length to the content. In this case we must make use of the square root of 193; for which purpose we may find a point upon the girt, in the same manner as the point for the root of 180 was sound. Now if the point for 193 be set against 20; then against 30 upon the girt, will be 93 on the double line; which is 7 per Cent. less than the former: A cylinder of such dimensions would measure only 98.17; so that by hewing the tree till the squares are half the thickness, it will measure near 2 per Cent. more than the full contents of the tree, if there had been no wood taken off.

3d. There are two points generally marked on this line; one W G, the other A G, for wine and ale gallons, their use is in gauging; for a wine gallon containing 231 cubic inches, and a circle whose area is 231, having for its diameter 17.14 inches: It is plain a cylinder of that dia-

meter

meter will contain as many wine gallons as it is inches in height; therefore if the length and mean diameter of any cask be given, the wine gallons that it will contain, may be found by the following proportion.

As the square of 17.14 is to the square of the mean diameter; so is the

length, to the content in wine gallons.

Hence if the gauge point W G upon the girt line, (which is the square root of the first term) be set against the length on the double line; then the contents in wine gallons will be found on the double line, against the diameter of a cylinder, or the mean diameter of any cask upon the girt line; but if ale gallons be required, we must make use of the point A G, which should be exactly at 18.94, the diameter in inches of a circle, whose area is 282, the cubic inches in an ale gallon.

S E C T. IV.

Of the triple Line of Numbers.

T was shewn in the construction of this line how to find the cubes, and their roots by inspection. We shall now shew how to find the dimensions of similar solids of different contents, as for instance: Suppose a ship of 508 tons to be 93 feet 4 inches by the keel, and 32 feet broad, and it be required to find the length of the keel, and extreme breadth of

a ship of 400 tons.

This was performed by the logarithms in Chap. 5. Ex. 4. where it was observed that the proportion is, as the tonnage of one ship, or the content of any folid, is to the cube of the keel, or of any other part; fo is the tonnage, or the content of any other fimilar folid, to the cube of the required keel, or any other fimilar part: Hence 508:400:: cube of 93.4 to the cube of the required keel; and the extent from 508 to 400 upon any line of numbers, will reach from the cube of 93.4 to the cube of 86, the length of the required keel. But there will be no need of finding the cube, (which is the fourth proportional to the three given numbers) if the root can be found: Now the cubes of any two numbers are three times the distance from one another that the roots are upon the same line: and because the two tonnages are the first and second terms, they will be the fame distance from one another that the cubes of the keels are, which are the third and fourth terms, and therefore their roots will be one third of the distance from one another that the tonnages are; which in this case are 508 and 400. Let the distance then betwixt these two numbers 02 be be divided into three equal parts, one of which being fet back from 93.4, will reach to 86, the length of the keel required.

Now, as the roots are the same distance from one another upon the single line, that the cubes are upon the triple line; the keels will be the same distance from one another upon the single line, that the tonnages are upon the triple line. Therefore the following method may be used where there is a cube line adapted to the single line.

Rule. Set 94 feet 4 inches, or 93.33, the length of the given keel, upon the fingle line, against 508, the tonnage upon the triple line; then against 400 upon the triple line, is 86 upon the single line, which is the length of the keel required. And when the slider is thus set, we have, by inspection, the lengths of the keels of all ships that are similar to this, be the tonnage what it will: For if the tons are found on the triple line, the lengths of their corresponding keels will be against them on the single line,

The like method may be used in finding the other dimensions, as in the followings table, where the dimensions of a ship of 508 tons are supposed to be as in the columns in the upper line, and are pretty near to those of a ship of 20 guns; the other tonnages are nearly those of 40, 50, &c. guns. We have in each column set down the real dimensions in set and inches, below those sound by the rule, which are in decimals, that our readers may see that some dimensions are pretty near similar in all ships, and others arbitrary.

Guns.	Tons.	Keels.	Extreme Breadth.	Heighth of the Breadth	Tranf. Breacth	Tranf. Heigh.	Length in Held.	Length of gun Decks
20	508 real	93: 4		13: 8			It: 0	
40	814{rule real	109, 0	37, 5 37: 6	16, 0		19,3 22:0	12, 9 16: 0	132, 0
50.	1052 real	118, 5						144, 0
.60	1191 {rule real.	123, 5 123: 0 ¹ / ₂	41,49 42: 8	18, 2	24,4	22,0	14,65	150: 0 150: 0
70	1414{real	131, 4	45, 0 45, 0	19, 2	25,7	23,2	15, 4	159, 0 160: 0:
80	1585 rule real	136, 0					20: 0	165 OF
90		138: 4	48: 6	2.1: 9	31:5	27.9	20: 6	170, 0
100	2000 {rule real	147, 0	50, 5					178, 0.

It must be observed, that as every figure is three times placed upon the triple line, it will be indifferent in what part of the line the tonnages are taken. The only thing to be regarded is, that the slider must be so-placed, that all the tonnages whose dimensions are required, be against some parts

of the fingle line.

Now, if the first 5 on the triple line be accounted 500; when 93.4 is fet to 508; 40 on the fingle line, which is now 400, will be against 40000 on the triple line; and 64, which is at the beginning of the triple line, will be against 46.6 on the fingle. So that in this position, the numbers upon the triple line betwixt 64 and 40, will not be against any part of the fingle line; for there will be no numbers less than 64 upon the triple line, without altering the value of the figures; but 4 at the beginning of the fingle line, will always be the fame distance from 64, the beginning of the. triple line, that 40 at the end of the fingle line, is from 64000 at the end. of the triple line. As the slider is now set, 4 at the beginning of the single: line is accounted 40; and because the distance betwixt 64000 and 40000, is the fame with that betwixt 64 and 40; the value of the figures may be alter'd, and 64000 at the end of the triple line may be called 64, and 40000 will be 40. But we must likewise alter the value of the figures on the fingle line; and 4 at the beginning of the line must be four units, and 40 on the triple, will be against 40 on the fingle line; 20 on the triple. against 31.7 upon the fingle, &c. as in the columns: To find the figures betwixt 64 and 40, let the fecond 5 upon the triple line be 500, and the flider fet as before directed; then will 40 on the triple be against 4, which is at the beginning of the fingle line, but is now accounted 40; against 50 on the triple, is 43 on the single; against 60 on the triple, is 45.75 on the fingle, &c.

In the same manner the extreme breadths to any assigned tonnage may be found, supposing 32 seet to be the extreme breadth of a ship of 508 tons: Let the third 5 on the triple line be 500, and when 32 on the single is against 508 upon the triple, then we have all the numbers below 640 upon the triple line; and 1 upon the triple will be against 4 on the single. But if the second 5 be 500, and the slider properly set, 990 on the triple line, will be against 40 on the single; and as in this position we cannot find the dimensions corresponding to 1000, and the numbers above it; we must in these, and such like cases, observe what point of the triple line is against 40 at the end of the single line; and draw out the slider till 4 at the beginning of the single be against the same point, which in this example is 990: And as the value of the figures upon the triple line are not altered, 4 upon the single line must be accounted 40; and then

against 1000 is 40,1, against 2000 is 50,5, &c. the breadths corresponding to those tunnages. Again, let 5 be some given dimension of a ship of 508 ton; if the flider is properly fet, 260 on the triple, is against 4, the beginning of the fingle line; and when 40 at the end of the fingle line is accounted 4, and brought against 260 on the triple; then against 100 on the triple, is 2,01 on the fingle, against 10 on the triple, is 1,25, against 1 on the triple, is 6,25 on the single. All the other dimensions in the columns are found by the same method, viz. by setting the given dimension to its proper tonnage; and to prove the work, after the length of the keels are found, we may use the double lines of numbers as before directed in Ex. 6. Sect. 2. of this Chap. Here the keel of a ship of 400 tons is found to be 86; when this is fet against 93.4, the keel of 508 tons, against 32, the breadth of 508, is 29.6, the breadth of a ship of 400 tons: And as all the dimensions in the columns for a ship of 508 are known, look for them on the same line that her keel is taken, and against them will be found the corresponding dimensions for a ship of 400 tons.

The Tonnage of a Ship being given to find the Length of the keel, and extreme Breadth.

Before this can be done, the proportion that the length of the keel bears to the extreme breadth must be determined; which suppose as 3 to 1, and then six times the half breadth will be the required length of the keel. Now, because in finding the tonnage, when the length and breadth are given, we are directed to multiply the length by the breadth, and that product by the half breadth, and then divide this last product by 94, and the quotient will be the tonnage; it is certain, if the tonnage be multiplied by 94, the product will be the same as if the length, breadth, and half breadth, were multiplied into one another; and if any of these three be given, the others are found by the given proportion they bear to one another. We shall therefore work for the half breadth, which may be found by the following rule, viz.

First multiply the given tonnage by 94; then divide that product by 12, and lastly extract the square root of the quotient; and that root will

be the half breadth required.

EXAMPLE.

Let the given tonnage be $127\frac{62}{54}$; then $127\frac{62}{54} \times 94 = 12000$, and $12000 \div 12 = 1000$, the cube root of which is 10, the half breadth; so 20 will be the extreme breadth, and 60 the length.

The reason of dividing the product by 12, is because 12 times the cube of the half broadth, is always equal to the product of the heighth of the keel, breadth, and half breadth multiplied into one another, when the length is three times the breadth, as will appear by the following process.

The half breadth 10.

The breadth will be $10 \times 2 = 20$.

The length of the keel will be $10 \times 2 \times 3 = 60$.

Now, as in multiplication, when feveral numbers are to be multiplied into one another, it is indifferent in what order the operations are performed; so it is evident that $10 \times 10 \times 10 \times 2 \times 2 \times 3 = 10 \times 20 \times 60 = 12000$, but $10 \times 10 \times 10$, is the cube of the half breadth, and $2 \times 2 \times 3$ is 12; therefore 12 times the cube of the half breadth will be equal to the product of the length, breadth, and half breadth, multiplied into one another.

By the sliding rule, set 12 upon the double line on the slider, against 94 upon the double line; on the rule look for the tonnage 127 62, or 127,66 upon the slider, against which is 1000. Then to find the cube root of this, set the slider so that 64 upon the triple, is against 4 on the single; then against 1000 on the triple, is 10 on the single; the half breadth.

But as the length does not bear any constant proportion to the breadth; after finding the dimensions by this rule, the breadth may be altered, and the length of the keel can be had by the tonnage point. There is no invariable rule to determine the breadth, but in ships under 500 tons, this method will always bring it to less than a foot, and therefore may be very useful in determining proper dimensions for a ship of any number of tons.

CHAP. VII. SECT. I.

Of the Construction and Use of several Lines on the Shipwright's Rule.

Of SECTOR LINES.

THE inftrument called a fector, is only a rule with a good joint, containing feveral different lines, each divided into some given proportion; as sines, chords, equal parts, &c. Every line upon one leg has a corresponding one upon the other leg, both exactly of the same length, and divided in the same manner; and all the lines on both legs meet at

the center of the joint.

It is very useful in all the practical parts of the mathematicks, especially in dividing a line into any number of equal parts, or into any given proportion. As for instance, if it was required to divide a line, as AB, into any number of equal parts, suppose 9, (See Plate 3. Fig. 1, 5.) it is only opening the rule till the distance betwix 9 and 9, in the line of equal parts, be equal to the line to be divided; and then the extent from 1 to 1, from 2 to 2, &c. in the same lines will be one ninth, two ninths, &c. parts of the line AB; for by opening the rule, the point 9, and every other point in the lines E, P, in effect, describe arches of circles; and if chords be drawn to these arches, they will form so many isosceles triangles, whose bases will be parallels to one another: Therefore C 9 is to 99, as C 1 is to 11, but C 1 is the ninth part of the line C 9; therefore 11 is the ninth part of the line 99.

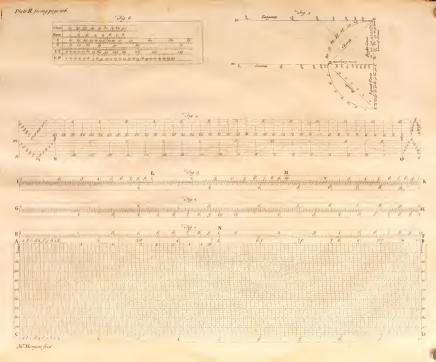
In like manner, if it were required to make the line DF a line of numbers, when the rule is opened till the distance betwixt the extremities of the lines of numbers be equal to the line DF; then if the several distances from 1 to 1, from 2 to 2, &c. be set off from D towards F, the

line DF will be a line of numbers.

Another method of dividing a line, as B D (See Plate 3. Fig. 4.) in the same proportion as the line A B is this. At the point B, the end of the divided line, make an angle, and set off the line to be divided from B to D; then draw the line A C parallel to A B, making D 3 equal A 3,

12





D 2 equal to A 2; D 1 equal to A 1: Draw the lines AD, 33, 22, 11: Then the triangles B 1 a, B 2 b, B 3 c, B A D, being fimilar, B A: B D: B 3: B a: B 2: B a: B 1: B a.

But before any of these methods can be used, the lines on the rule must be divided by some proportion given in numbers, or from the equal

divisions of the arch of a circle.

The fector lines on the shipwrights rules, are for making masts and yards, of which there are four on each leg, divided into the same proportion, that the diameters at the several quarters bear to that at the slings; which being given in numbers, and expressed by the fraction, each quarter is of the slings, they may be constructed in the following manner:

Make an equilateral triangle A B C. (Plate 3. Fig. 6.) From the point A fet off, on the lines A B, and A C, the equal parts expressed by the several denominators of the fractions, and draw lines across at these divisions. Then set off, on these lines, the equal parts expressed by the respective numerators of the fractions, and draw lines from A thro' these points to intersect the line B C. So if the side of the triangle be supposed to be the diameter at the slings, the several divisions of the line B C, from the point B, will be the diameters at the quarters. It will be proper to raise the fractions, so their denominators do not exceed 100.

E X A M P L E.

Let it be required to conftruct the line for yards, the quarters being the following fractions of the slings.

1/t. \$\frac{2}{1}\$5, or \$\frac{81}{84}\$. 2d. \$\frac{9}{10}\$, or \$\frac{90}{100}\$. 3d. \$\frac{7}{10}\$, or \$\frac{70}{100}\$. Yard arm \$\frac{2}{3}\$, or \$\frac{40}{100}\$.

Having constructed the triangle A B C, set off 84 equal parts, the denominator of the first quarter, from A to a; and from A to b draw the line ab, which will be parallel to B C. Upon the line ab set off 81 equal parts, the numerator of the first quarter, from a to c; and draw the line A c to intersect the line B C in the first quarter. Again, for the second quarter, its denominator is 100; therefore set off 100 equal parts from A to B, and from A to C, which in this case is already done, because the side of the equilateral triangle was made 100 equal parts: It remains only to set 90 equal parts from B to the second quarter, and draw a line from A to this point. The denominators of the third quarter and yard arm, are likewise 100; the numerator for the third quarter is 70, which set off from B to the third quarter, and draw a line from A to this point.

The numerator for the yard arm is 40, which fet off from B to y A, and draw a line from A to this point; by this means, if B C be supposed the diameter of a yard at the slings, B y A will be that at the yard arm; B 3 qr. that at the third quarter; B 2 qr. that at the second; and B 1 qr. that at the first quarter; they being by construction $\frac{2}{5}$, $\frac{2}{10}$, $\frac{2}{10}$, $\frac{2}{10}$, of the line B C.

The line being thus divided, may be transferred to each leg of the rule: But if the rule will not contain the length of the line, take such a length as may suit the rule, and with a pair of compasses, set off that length from A to G, and from A to F; and draw the line G F, which being parallel to B C, will be divided in the same proportion, and may be transferred to the rule. In the plate (Fig. 7.) the lines are only drawn to yA, but if continued, would meet in the center of the joint.

The line being thus conftructed, and transferred to the rule, we shall shew the use of it in making a yard; (Plate 3. Fig. 8.) which suppose 71 feet long, of which A B is one half, and S 8, the diameter at the slings 17 inches: Having divided the line A B into four equal parts at the points 1 qr. 2 qr. 3 qr. open the rule till the distance betwixt S and S at the extremities of the lines on the rule, be equal to 17 inches, the diameter of the yard at the slings; then the extent from the dots on the one leg, to those corresponding on the other leg, will give the diameters at those quarters, and at the yard arm, from which they may be set off upon the yard. But it must be observed, that only the half of each of those diameters thus sound, must be taken, and that set off on each side of the middle line upon the yard; for which reason, in practice, it will do better to take half the diameter at the slings, and set the rule by that; and then we have half the diameters at the quarters by the rule.

The lines A B, and A C, (Fig. 6.) and the lines drawn from the point A for the quarters, may be produced to any length, and drawn upon a board. If then the lines A B, and A C, be divided into inches, halfs, and quarters, there will be no occasion to transfer them to the rule: For suppose the diameter at the slings 21 inches, the half is 10 \(\frac{1}{2}\); lay a ruler, or strait edged batten across the board, from 10 \(\frac{1}{2}\) in the line A B, to 10 \(\frac{1}{2}\) in the line A C, and make a mark upon the batten at each intersection with the lines drawn from A for the quarters. By this means we have, upon the batten, half the diameter at each quarter and yard arm; and these being set off on each side of the middle line upon the yard, in their proper places, will give the whole diameter at those places.

After the same manner are the lines for masts, bowsprits, and mizen yards constructed, by an equilateral triangle, and from thence transferred-

to the rules; the proportions, or fractional parts, by which the lines are conftructed, are as follows:

Quarters Mafts Bowfprits lower Mizen Yard Arm	1 60 61 30 37 21 22	2 14 13 9 10 11 12	अर्थभार श्र	Hounds.	Head.	Heel.	Cape,	Yard Atm,
upper 🕽	14	13	2.					1

Another method of proportioning the quarters to the slings, is taken from the divisions of the quarter of a circle, but the diameter at the yard arm must be first determined; which suppose † of the slings, as before, and let G F (Plate 3. Fig. 3.) represent the diameter at the slings. Now to find the diameter at the quarters, take the following rule.

Ist. With the radius GF, describe the quadrant GFE.

2d. Upon the line G E, fet off $\frac{2}{3}$ of the diameter at the flings, from G to e, and thro' e draw a line parallel to G F, to interfect the arch in a; from a draw a line parallel to G E, to interfect the line G F in y; then will y a be the diameter at the yard arm.

3d. Divide the line G y into four equal parts, in the points 1, 2, 3, and draw the lines 1 qr. 2 qr. 3 qr. parallel to G E, which will be the di-

ameters at those quarters.

There is also another line on each leg; these meet at the center of the joint, from whence they are numbered 1, 2, &c. to 12; the space betwixt the figures is nearly \(\frac{1}{2}\) of an inch, each divided into 12 equal parts: So the spaces betwixt the figures may represent seet, and the intermediate divisions inches. But if it was required to make a scale of sect and inches, where one quarter of an inch, one eighth of an inch, or any other space shall represent one foot; it may be done by the same lines, as before directed. Thus, take with the compasses 12 times the space intended to represent one foot, and open the rule till that reaches from 12 upon one leg to 12 upon the other leg. Now, whereas the feet and inches of the scale on the rule, are taken from the center of the joint; those of the other scale, must be taken across at those points.

SECT. II.

Of the Construction of the Ten, Twelve, and Eight Square Lines.

HE use of these lines, is in order to hew a piece of timber so that it shall be a prism contained under 10, 12, or 8 equal planes, which are called squares; their bases will be polygons of the same number of equal sides.

The first thing to be done, is to hew the piece four square; the four sides for a ten square will not be equal, for its base will be a rectangle; whereas the bases for a twelve and eight square will be squares; so they

must first be hewed into parallelopipedons.

There are three lines necessary for making a ten square, viz. The first for determining the longest side of the restangle; the second for determining the side of the polygon; and the third for determining how much wood must be taken off the corners to reduce the restangle to a polygon. Their chief use is for making barrels of capstans.

To Construct the Ten Square Lines.

Upon the line AB (Plate 3. Fig. 9.) erect a perpendicular CF, which make any number of inches, suppose one and a half. Thro' F draw the line DG parallel to AB: From C draw the lines Cm and Cn, making each an angle of 18 degrees with the line CF, fo thall mn be the fide of a polygon of ten equal fides; for the angle at the center is 36 degrees, the tenth part of 360. With the radius C m (equal to C n,) describe the femi-circle Amn B, and erect the perpendiculars AD, BG; fo shall the rectangle A D G B, be half the base of the piece when hewed into sour squares. Now it is plain, that the piece will be thicker one way than the other; for CF is one half of one of the diameters, and CB half the other; and F m half the fide of one of the ten squares: To reduce this rectangle to a polygon, make ms, sA, nt, tB, equal to mn, and produce the lines ms and nt, to b and o, and cut off the triangles D mb and G no; cut off alto the triangles b s A and f o B, fo shall A s m n t B, be half the barrel of a capstan of three inches diameter. If F m be divided into three equal parts, we shall have the divisions of the line marked BS, (Fig. 2.) which may be continued to any length. The use of this, is to find the side of the ten square, which is done by setting off as many divisions of this line as the barrel is inches thick on each side of the middle line on the two

big fides.

If the line A b (Plate 3. Fig. 2.) be divided into three equal parts, we shall have the divisions of the line marked S S, which serves to shew how much must be set off from the middle line on the two small sides, viz. one of these divisions, for every inch of the thickness of the barrel, which in this case will be to b and o; and when the wood is taken off from m to b, and from n to o, we may make m s and n t, each equal to m n, also equal to S A and t B.

If the line AB be divided into three equal parts, it will give the divifions of the line LD, (Fig. 2.) which ferves to shew how much the barrel

must be the biggest way.

In making the barrel, the first thing to be done, is to hew it to the defigned thickness in inches; which is what is called sideing of it, and afterwards to square it; that is to hew it the other way. In order to do this, we must take as many divisions of the line LD, as the barrel is to be inches thick, so when it is thus hewn, it will have two big, and two small sides: There must be a middle line struck on each side, and then proceed as directed, by setting off the proper distances from the middle lines; and when all the wood is taken off, there will remain nothing of the small sides but the middle line; but of the two big sides there will remain the side of the ten square.

In constructing these lines it will be proper to produce the lines CF and Cm, till CF is fix inches or more; then will Fm be half the side of the ten square of a barrel of 12 inches thick, which may be divided into 12 equal parts; the same must be done with the lines S S and L D.

To Construct the Lines for a 12 Square.

These are likewise chiefly for making barrels of capstans, (Plate 3. Fig. 10.) but here the piece must be hewed exactly 4 square; for when all the wood is taken off, the whole side of the 12 square will remain on all the four sides.

There are only two lines necessary for reducing the 4 square to a 12, and formed after the same manner as those for a 10 square; for since the angle at the center of a polygon of 12 equal sides is 30 degrees, if at C two angles of 15 degrees each be made, and the lines Cr and Cs be drawn, it is plain rs will be the side of the 12 square, of which Fr is one half; which being divided into 3 equal parts, will give the divisions of the line 4 S: (Fig. 2.) There must be as many of these divisions set off from

To Construct the Eight Square Lines.

These are on most of the shipwright's rules. Their use is in making masts and yards, and so well known, that we need give no directions how to apply them; and shall only remark, that tho' masts and yards are round, they must be first hewed four square, each side being equal to the diameter of the mast or yard; which, suppose A B, (Plate 3. Fig. 11.) then will the rectangle A G D B, be half a four square, in which a femi-circle may be inferibed of the fame diameter with the mast or yard. If from the center C be drawn the lines C m and C n, making each an angle of 22 a degrees with the line CF, we shall have mn the side of a polygon of eight equal fides, of which F n is one half; and if this is divided into as many equal parts as the diameter has inches, it will give the divisions of the 8 square line; one of which for every inch diameter must be set off from the middle line on all 4 sides: And because the diameter is supposed 3, when that number is set off from the points A, B and F. we shall have the points r, m, n, b: But these points may be found by fetting off their distance from D and G, the side of the square; for which purpose the line n G or m D, must be divided into a equal parts; so either of the lines may be used.

These lines are on foot rules; but there are two lines on the slider of the two foot rules; the one for finding the diameter at the quarters; the other for finding the length and diameter at the slings of masts and yards. We have already shown how to find the quarters by the sliding rule, which requires an operation for every quarter; but this line shows them all at once, only by setting a point in the slider to the given diameter of the

flings;

flings. It is the upper line upon the flider, and has a fpace for mafts, one for yards, one for bowsprits, and one for each arm of a mizen yard.

To find the Quarters by this Line.

For masts, set P on the slider against the diameter at the partners, and against the figures 1, 2, 3, you will find the diameters of the 1st, 2d, and 3d quarters; against HS will be the diameter at the hounds, and against mb the diameter of the lower mast head, but if it is a top mast, the diameter will be against T m.

After the same manner the quarters of the yards may be found, by setting S against the diameter at the slings; and against the sigures 1, 2, 3, will be found the diameters of 1st, 2d, and 3d, quarters; and against YA, the diameter at the yard arm. The same may be said of the bowsprit and mizen yard: One example will be sufficient to illustrate the whole.

Required the bigness at the Quarters, and Yard Arm, of a Main Yard 30 Inches at the Slings.

Set S against 30, then against 1 will be 29, nearest, for the first quarter; against 2 will be 27, for the second; against 3 will be 21 for the third; and against Y A will be 12 for the yard arm.

Note. The slider must be applied to a double line of numbers.

Before this line can be constructed, the proportion that the quarters bear to the slings must be determined, which suppose to be as before.

First quarter	27	In decimals
Second quarter	9	.9
Third quarter Yard arm	3.0	•7
Laiu ailli	7	.4

At any convenient place upon the slider assign a point for S, and draw a score at that point for the slings; set that point or score against 28, and against 27 draw a score upon the slider for 1; then move the slider till S is against 10, and against 9 draw a score upon the slider, for 2 against 7 draw a score for 3; then move S to 5, and against 2 draw a score for the yard arm.

The reason of this will appear very plain, if we find the quarters by a pair of compasses; for then we take the distance betwixt 28 and 27, (which will always be equal to the distance betwixt the diameter at the slings, and that at the first quarter) but this is equal to the distance be-

twixt

twixt S and I upon the slider; therefore if S be set against the diameter at the slings, I will be against that at the first quarter; the like may be

faid of the reft.

If the fractions are all reduced to decimals, the strokes for the quarters, &c. may be remarked, without moving the slider after S is set to 1, as will be found upon examination; and the construction of the line will appear plainer by the decimals; for the points 1, 2, 3 and Y, are exactly the same distance from S, that the numbers .964, .9, .7, .4 are from 1 on the line of numbers. There is no difference therefore between the line on the slider, and the line of numbers, only when the proportion of the quarters, &c. is determined by numbers; as the distances properly set off from 1, to decimal parts, will reach from S to the points 1, 2, 3 and Y A; these points are used instead of the numbers .364, .9, .7, .4.

The lower line on the flider, is for finding the lengths of masts and yards, but before this can be done, there must be a given proportion; the following is generally allowed for masts, viz. As 100 is to 76, so is the extreme breadth in feet, to the length of the main mast in yards.

The lengths of the other masts are proportioned to the main mast, and the points or strokes upon the slider, are laid down from Brb, by those established proportions, in the same manner as the diameters at the

quarters of the yards are proportioned to that of the slings.

The main mast is allowed to be in proportion to the fore mast, as 100 to 89; in like manner there must be proportions for the mizen mast, bowsprit, main, fore and mizen top masts, topgallant mast and sprit sail top mast; by these proportions, the points or strokes, are set off for the different masts at proper distances from B r b.

To find the Lengths of the Masts by the Line.

Set Brb against the extreme breadth in feet; then the lengths of all the masts will be against their respective divisions, which are all distinguished by letters peculiar to each; and at the same time, the lengths of their heads and hounds may be found, there being peculiar letters for that purpose, and those for distinction's sake are across the slider.

Thus \(\frac{2}{N} \) For main mast head. \(\frac{2}{N} \) For main mast hounds.

EXAMPLE.

Required the lengths of the masts of a ship whose extreme breadth is 50 feet.

Set B r b against 50; then the lengths of all the masts, mast heads and hounds, will be sound against their respective divisions, distinguished by letters as follows, viz.

		Leng	ths,	H	ead,	He	ounds,
		Yar	ds.	Fe	et.		Peet.
M	Main mast	38	,0	15	.8	6	.6
F	Fore mast	33	3	11	г		
Z	Mizen mast	32	1 4	12		5	.3
В	Bowfprit	_	¥.	12	.2	4	.85
	Main top mast	24	# 3 #	-		_	-
	Fore top mast	22	7	. 6	.75	2	.7
		20	3	6	• I	2	•4
	Mizen top mast	16	, I	4	.75	1	.9
	Main top gallant mast	11	,0	23	.25	1	.28
F g	Fore top gallant mast	9	,9	2	.9	1	.26
Si	Spritsail top mast	9	,6		<u> </u>	-	

The lengths of the yards are proportioned to the length of the gun deck, and estimated in the same measure that the gun deck is, and are found in the same manner as the masts are.

Set GD against the length of the gun deck, and the lengths of all the yards will be found against their proper letters, as in the following examples, viz.

Admit the gun deck to be 174 feet; required the lengths of all the yards.

Set G D against 174; then the several lengths will be found as follows, viz.

	Feet.
M The main yard	103
F The fore yard	90 1
Z The mizen yard	82
Mt The main top fail yard	71
F t The fore top fail yard	62 +
Mg The main top gallant yar	d 49
Zt The mizen top fail yard	47
Fg The fore top gallant yard	43 *
9 tol Burner lance	43 7

To find the diameter of any mast or yard, first find the length in seet. Set F L against that length, and you will find the diameter in inches against

gainft the letters, reprefenting the maft or yard, whose diameter is required as in the following, viz.

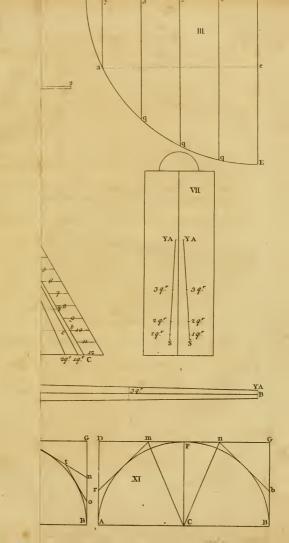
	Feet.		Diameter.
Main maft	114	Lm	38
Fore maft	102	ditto	34
Bowsprit	97 =	В	48 3
Main top maft	69	T m	20 1
Fore top maft	62 1	ditto	18 3
Mizen top mast	48	ditto	14 .4
Main top gallant mast	33	_	9 .9
Fore top gallant mast	30		9.0

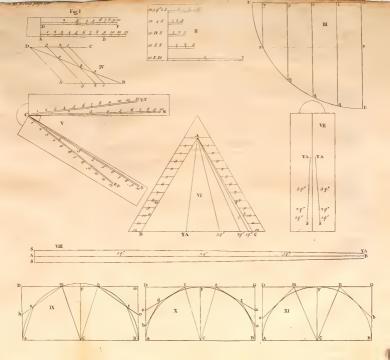
The letters L m fignify all lower masts. B the bowsprit. T m all top

masts, and top gallant masts.

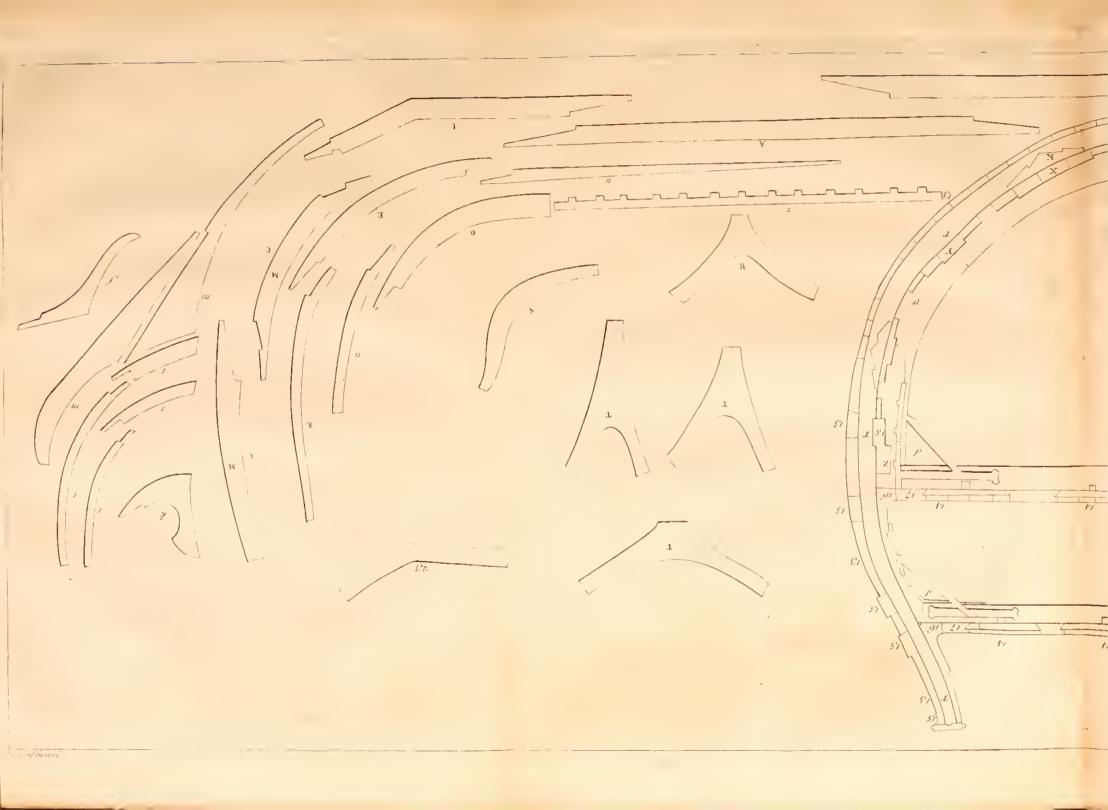
The line for finding the lengths and diameters of masts and yards, is put upon the inside of the slider on the foot rules.

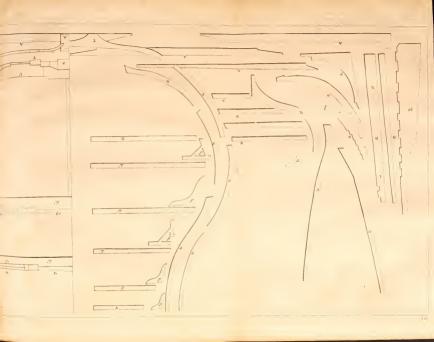
The End of the First Part.













THE THEORY OF

SHIPBUILDING and NAVIGATION.

PART II.

C H A P. I.

Of the Orthographick projection of Solids on a Plane.

HE chief defign of delineating a house, ship, or any other folid upon a plane, is to settle the just dimensions, and symetry of its parts according to the scheme of the builder. When this is done by mathematical rules, we can find the exact length, breadth and heighth, not only of the whole, but also of any particular apartment on a sheet of paper. However, as a plane has but two dimensions, viz. length and breadth, and a solid three; they cannot all be represented by only one projection on the same plane.

A plane is an even furface, to which a right line may be every way applied, and upon which there are feveral ways of projecting folids. We shall only treat of the orthographic projection, as best suited to our

purpose.

Before any solid can be represented by this way of projection upon a plane, it must be supposed to be cut by several planes: These are called plain sections, and will form even surfaces, which having but two dimentions, may be delineated upon a plane: And when the solid is cut so as to form an uneven surface, it is always supposed to be covered with an even one before it can be represented upon a plane; so that in effect, we only represent one plane upon another.

The thing to be represented is called the original, and the plane upon

which it is to be represented, the plane of the projection,

When

When feveral lines parallel to one another, are drawn from all the parts of an original, to cut the plane of the projection; they will upon it describe a figure, which is called the projection of that original. The lines producing this figure, are called the projecting lines or rays; and this manner of representing any object, is called the orthographick pro-

jection of that object.

This parallelism of rays is the effential property which diftinguishes the orthographick from all other kinds of projection: And tho' it is indifferent in what direction the projecting lines are drawn; it will be more convenient to make them perpendicular to the plane of the projection, and when this is parallel to the horizon, the length and breadth of any folid can be found by a plummet carried round it with a thread, fo as to touch all the parts of it; but the heighth cannot be reprefented by this operation. This is what is called a plan of a building.

If another plane be crected perpendicular to the horizon, and the folid in the same position, supposed to be cut length ways by several planes parallel to one another, and perpendicular to the horizon; we can upon it, represent the true lengths and heighths of all these sections, but instead of a plummet, we must make use of a square. This is what is

called the plane of elevation, or fide view of a building.

If another plane be erected perpendicular to the two former, we can upon it, represent the heighth and breadth of any section, cutting the solid right across, perpendicular to the horizontal and side planes. This, in a building, is called the profile, being an end view; in a ship, the head or stern view. By these three planes all the parts of a solid may be represented; and if two of the planes be known, the third may be found

without having recourfe to the folid.

By this description, it may feem that a house or ship, cannot be thus delineated till actually built. But it must be observed, that the extreme length, breadth and heighth, must be determined; by which the three planes aforesaid may be delineated. These may be called the out lines. The several parts contained within them may be delineated so as to answer the intended use; by which means we shall have a distinct view of the whole design, and may discover any inconveniencies that may attend such a disposition of the parts, which may be easily remedied upon paper; and the true dimensions of every particular may then be had upon the draught: Whereas, if we go to creek the structure without a draught, we run the hazard of pulling down several parts in order to make them uniform and convenient for the rest.

The

The delineating a ship upon a plane is called drawing, and the reprefentation is called a draught.

Properties of the Orthographick projection.

1. All right lines upon an original plane, that are perpendicular to the

plane of the projection, will be represented by points.

2. All lines on an original plane, that is inclined to the plane of the projection, will be reprefented by shorter ones, but if they be parallel on the original, they will be so when projected; and when the original is parallel to the plane of the projection, they will be exactly of the same length in both.

3. All planes, whether limited by right or curve lines, when perpendicular to the plane of the projection, will be reprefented by right lines.

4. All planes parallel to the plane of the projection, will be represented by equal and similar planes; but if they be inclined, their represented

tations will be less than their originals.

5. The mutual interfection of two planes, is a right line common toboth planes, and is called their common fection; and if feveral planes interfect one another in the same line, it will be common to all the planes.

6. In the orthographick projection, the distance of the original from the plane of the projection, makes no alteration in its representation.

7. Before any plane can be represented upon another, its position with

respect to the plane of the projection, must be determined.

8. The inclination of one plane to another, is the angle formed by two lines, one in each plane, both drawn perpendicular to the common

fection; where they meet at the same point.

In order to illustrate and demonstrate these properties, we shall in the following problems, shew the different representations of a plane according to its position, in respect of the plane of the projection; and to assist the imagination in conceiving why the same plane will have different representations; the figures are so contrived that they may be cut, and erected to any required angle with the plane of the projection.

PROB. I.

Given, the plane A r d a B C; (Fig. 5.) upon which are drawn the lines r1, d2, a3, parallel to A C, and perpendicular to B C; required, its projection upon the plane B M N T, to which it is supposed perpendicular; so that a C G shall be a right angle.

Drava

Draw the line Cg perpendicular to CG, and make it equal to CB; (Plate 4. Fig. 5.) then will C g be the projection of the plane Ard a B C. But if it were required to project it so that A C D shall be a right angle; draw the line C B perpendicular to C D, and B C will be the required projection of the plane ArdaBC: This will be manifest when the plane is erected, till the point A is perpendicular to the point C; for then parallel lines drawn from the points r, d, a, will fall upon the line C B, and be represented by the points 1, 2, 3; and the whole plane ArdaBC, will be represented by the right line B C, as by properties 1 and 3: For A C and C D being perpendiculars to C B, the common fection of the two planes, will form a right angle at C, when the plane ArdaBC, is turned upon the axis B C till the point A is perpendicular to C; and if then a thread be stretched through the points A and D, we shall have a right angled triangle, of which the thread is the hypothenuse, AC the perpendicular, CD the base, and ACD the right angle; tho' it was a right line before the plane was erected.

Note. The arch BadrA, and the radius AC, are to be cut through,

and then the plane may be turned upon the axis B C.

PROB. II.

Given the plane A r d a B C, to find its representation on the plane

BMNT, to which it is supposed parallel.

This is only making a plane equal and fimilar to the given one. Therefore produce the lines AC, r1, d2, a3, to D, t, f, c; make CD equal AC, It equal r 1, 2 f equal d 2, and 3 c equal a 3; so shall CB cft D be the plane required. For if the plane ArdaBC, be turned round upon the axis B C, till it is parallel to the plane; the point A will come to the point D, r to t, &c. and the parallels r 1, d 2, a 3, will be projected into equal and parallel lines, as by properties 2 and 4. And the projection will be the same, if the original is lifted up to any distance above the plane of the projection, fo it be parallel to it, tho' the projecting lines be oblique to the plane: As if it were required to project the plane ArdaBC upon the plane RPOS, so that the point H shall represent the point B. Draw the line BH, and parallel to it, lines from the points A, r, d, a, 3, 2, 1, C. Make these lines each equal to the line B H; so shall H 6 5 4 k K, be the plane required, equal and similar to the plane ArdaBC; we have omitted drawing the lines from 3, 2, 1 and C to avoid confusion.

If the original is inclined to the plane of the projection, its reprefentation will be less than the original, but its true dimensions may be found found by the following problem; provided its inclination and representation be known, and the direction of the projecting lines.

PROB. III.

Let the angle GCE be the inclination, and B best C, the representation of a plane, and the projecting lines perpendicular to the plane

BbesE; required ArdaBC, the original plane.

It is evident by the properties before described, that when the original is inclined according to the given angle, the projecting lines let full from A, r, d, s, will fall in the points E, s, e, b, to which they are supposed perpendicular; and of consequence E C, s 1, e 2, b 3, will the bases, and r 1, d 2, a 3, hypothenuses of right angled triangles; of which the angles and bases being given, the hypothenuses may be found by constructing the triangles; or if the base and hypothenuse is given, the angle of inclinations

tion may be had in the triangle.

At the point E erect the perpendicular E G; at C make the given angle, and draw the line C G to interfect the perpendicular in G; then will the hypothenuse C G be equal to A C. This will easily be conceived erecting the triangle G C E, till it is perpendicular to the plane B b e b E; and when the plane A r d a B C is inclined to it, according to the given angle, the lines A C and C G will coincide: In like manner the lines r 1, d 2, a 3, may be found, by erecting perpendiculars at the points s, e, b, and drawing lines parallel to C G, from the points s, s, s, to intersect these perpendiculars, which will form so many right angled triangles: Their hypothenuses will be equal to the lines r 1, d 2, a 3.

Note. The lines C G and G E, in the triangle are to be cut through,

PROB. IV.

Given, the plane ArdaBC, and its inclination (the angle GCE) to

the plane BMNT, to project it upon that plane.

This is only the reverse of the former, for here the hypothenuses and angles, are given to find the bases. Make therefore the given angle at C, and C G equal A C, from G let fall the perpendicular G E; so shall the point E be the representation of the point A. Having thus constructed the triangle G C E, right angled at E; the base C E will be the projection of the line A C. In like manner, the bases 1 s, 2 e, 3 b, may be sound; by making G 1, G 2, G 3, in the triangle, equal r 1, d 2, a 3, in the plane A r d a B C: Then draw the lines 1 s, 2 e, 3 b, parallel to C E: These set of from the points 1, 2, 3, in the line B C, upon perpendiculars drawn to those points on the plane B M N T, will give the

lines t s, 2 c, 3 b; fo that B $b e \to C$, will be the projection of the plane $A r d a \to C$.

Our readers should be well acquainted with these problems: For we shall have frequent occasion to find the inclination of one plane to another. The next thing necessary to be understood is, when several planes are given, and their inclinations to one another, to find the dimensions of

another plane which will interfect them in any affign'd polition.

This will admit of feveral varieties; in order to explain which, we shall shew how to lay down a folid upon a plane. For this purpose we shall chuse one limited by fix planes, like a chest, as being the simplest, and easiest to be represented of all folids; for if the ends be two equal right angled parallelograms, supposed to be parallel to one another, and perpendicular to the bottom; the sides will be equal, and parallel planes; the top and bottom will also be equal. But in order to make all the planes different, we shall suppose it broader at one end than the other,

and the top floping.

Let then C s u A, be the narrow, and D t b B, (Plate 4. Fig. 1, 4.) the broad end, right angled at u and A, also at b and B; their heighth at the back fide B D and A C equal. The ends being supposed perpendicular to the bottom and back fide, will occasion the fides likewise to be perpendicular to the bottom, tho' not parallel to one another; the angle T D t, or its equal s C S, will give the flope of the top; or its inclination to the back fide. Now all the planes are different, and before their dimensions can be determined, the length of the chest must be given; which suppose the line A B. This will determine the dimensions of all the planes. And first to find the bottom. At the points A and B, draw the perpendiculars A E and BF; make BF equal Bb, and A E equal Au, and draw the line EF; fo the plane ABFE, will be the bottom. Secondly, to find the back fide, produce the perpendiculars E A and F B, to C and D; making A C and B D, equal the given heighth of the ends, and draw the line CD; fo shall the plane ACDB, be the back side. The bottom is the horizontal plane, and the back fide, the plane of the elevation; and when this is erected perpendicular to that, the angles DBF and GAE, will be right. And if the plane DtbB be turned about upon D B as an axis; and the plane C suA, turned round upon the axis C A, till they are perpendiclar to the horizontal and elevation planes: Then perpendicular lines drawn from the points D and t, will fall in the points B and F, and from C and s in the points A and E; fo that the plane AEFB, will be the projection of the top on the horizontal plane; which will be less than the original, because it is not parallel to the plane upon which which it is projected. But as its inclination is given, the true dimensions may be had by *Prob.* 3. The triangles being constructed, produce the perpendiculars B D and A C, to K and I, making D K equal to the hypothenuse D t, and C I equal to the hypothenuse C s; and draw the line

IK; fo shall the plane CIKD be the top.

In like manner, the forefide may be projected upon the plane of elevation, which will be the plane ASTB: But this will be too short. Therefore from the points F and E, draw the perpendiculars E G and F H: making F H equal to t b, and E G equal to s u, and draw the line G H; fo shall the plane EFHG, be the foreside. The planes being thus found, they may be cut by the dotted lines, and erected to their proper position; and when the line I K, and the dotted perpendiculars are cut, the top may then be turned round upon the line C D, till it lies flat upon the plane A C D B, where it may be preffed down; by which means the line CD will remain immoveable, and acquire fuch a crease or fold, that the plane I K D C, may be turned round upon it as upon a hinge. In like manner, the dotted lines C s, s u, u A, (Fig. 1.) and the dotted lines D t, t b, B b, (Fig. 4.) may be cut; and the ends turned round upon the lines CA and DB, till they are laid flat upon the plane ACDB. And when the top is likewise laid flat upon these, the plane A C D B, may (together with the ends and top) be turned round upon the line A B, till it lies flat upon the plane A G H B; after which all the planes may be turned round, and laid in their first situation; and so they will all lie in one plane. We may now easily erect the chest; and first erect the ends till they are perpendicular to the back fide; and the top may be turned round till it lays upon the lines Cs and Dt. And if the tongue x (Fig. 1.) be put in the slit x in the top, near I; and the tongue a (Fig. 4.) in the slit a in the top near K; then the backfide, together with the ends and top, may be turned round upon the line A B, till it comes to be perpendicular to the bottom; and the point u (Fig. 1.) will be in the point E: And to keep it fast, the tongue y may be put in the slit y. In like manner, the point b (Fig. 4.) will be in the point F, and the tongue e may be put into the flite; fo we have now the ends, top and backfide fastened to the bottom: And if the dotted lines EG, GH, HF be cut, the plane EGHF may be erected perpendicular to the bottom. The point G will be in the point s, and the point H in the point t; and the tongue L, which may represent the hasp of a lock, may be put into the slit L in the forefide.

The cheft being thus erected, it will be easy to make any partitions within it. But if the position of these partitions be known, their true di-R

off

mensions, form and inclination may be found before the planes are erected; provided the dimensions and inclination of these planes to one another be given.

The horizontal and elevation planes are always perpendicular to one another. Now a plane may interfect these two in three different positions.

1/f, When perpendicular to both. Its interfection in both planes will then be in a right line perpendicular to the line AB, the common fection of the two planes, as Fig. 1. which interfects the elevation plane in the line CA, and the horizontal in the line AE. This is what the shipwrights

call a square plane.

2dly, When inclined to the plane of elevation, but perpendicular to the horizontal, as $Fig.\ 2$. which interfects the plane of elevation in the line GH perpendicular to AB, and the horizontal in the line $Hb:\ So$ its inclination to the plane of elevation, will be the angle nHb. This the shipwrights call a canted plane. But if the plane $A \to FB$, be the plane of elevation, and the plane $A \to BB$, the horizontal; the plane interfecting them in the lines GH and Hb, would then be called a raking plane.

3dly, A plane may be inclined to both, as Fig. 3. intersecting the plane of elevation in the line M N, and the horizontal in the line N q. This plane is said to cant and rake. Their positions being thus determined,

their dimensions are likewise determined.

PROB. V.

To find the Dimensions of a square Plane, intersecting the common Section of the Horizontal and Elevation Planes in the Point A.

Through A draw the perpendicular I E, intersecting the common section of the top and backside in the point C, and the common section of the bottom and foreside in the point E. Make a right angle at A, because the required plane is supposed perpendicular to the horizontal; and make A u equal to A E, the breadth of the bottom at that place. Again, because the foreside is perpendicular to the bottom, make a right angle at u, and u s equal to E G, which is the breadth of the foreside at that place: Lastly, draw the line s C; so shall C s be equal to C I, the breadth of the top at that place; and C s u A the required plane, the angle S C s, being the inclination of the top.

The profile, is the proper plane to project all fquare planes upon, as being parallel to it. Now the plane D t b B, is the profile: And if it were required to find the dimensions of a plane, intersecting the horizontal in the line A E, and the elevation in the line A C; it is only setting

off A E from B to p, and drawing p o parallel to BD; then will D o p B, be the plane required, equal to C s u A; and r o equal to S s. For B D and C A, are equal by supposition.

PROB. VI.

To find the Dimensions of a Cant Plane, intersecting the Herizontal Plane in the Line H b, and the Elevation in the Perpendicular G H.

From the point b let fall the perpendicular b w, and produce it to interfect the line S T in W, and draw the line G W; then will G W w H, be the projection of it upon the plane of elevation. Which will be lets than the original, because it is inclined to it; but its true dimensions may be found by Prob. 3. Thus, make H n equal to H b, and raise a perpendicular at n: Make n m equal to w W, and draw the line G m; so shall G m n H, be the required plane. The angle n H b, its inclination to the backsside; and the angle H b E, the inclination to the foreside. The inclination of the top will be the same as that of the bottom, which in this is a right angle.

P R O B. VII.

To find the Dimensions of a Plane that Rakes and Cants; intersecting the Horizontal in the Line N q, and the Elevation in the Line M N.

1/k. From q let fall the perpendicular q z; thro' z draw the line P f, perpendicular to M N, produced to f. From the center N, with the radius N g, interfect the perpendicular f p in P; and draw the dotted line N P. Again, thro' M draw the line M R parallel, and equal to N P, and draw the line P R; fo M N P R, would be the required plane, if the bottom were as broad at the point v, as it is at the point z, and the top parallel to the bottom. But as this is not the case here, the required plane will be narrower at the top than at the bottom.

2d. From M let fall the perpendicular M v, and draw the line v V, parallel to N q; make M m equal to v V, and draw the line P m. So M N P m, would be the required plane, if the top was parallel to the

bottom.

3d. Make NP in the line Nq, equal to v V, and draw the perpendicular Pr, and make Mn equal to Nr, So a line drawn from r to n, would be parallel to MN, and would interfect the line ST fomewhere; and a line drawn from that point of interfection to M, would be the projection of a plane interfecting the plane of elevation in the line MN; and the hori-

R 2 zontal

zontal plane in the line NP. But there will be no occasion to draw this line, because N q is the length of the line of intersection of the required plane; and z the projection of the point q. Therefore a line must be drawn from z to n, which will interfect the line S T in x; fo shall M N z x, be the projection of the required plane, upon the plane of elevation, which will be less than the original. To find which, thro' x draw a perpendicular to the line M N, to interfect the line P m in the point d; fo shall M d P N, be the plane required. And to find its inclination to the plane of elevation, draw the line Z z parallel to f M. and produce it to t: Make f t equal to f p; fo shall z f t, be a right angled triangle; and the angle z f t, the inclination to the backfide. For if the triangle be erected perpendicular to the plane, as mentioned in Prob. 3. the lines ft and fp, will coincide. To find the inclination to the forefide, make the angle & No, equal to the angle & ft; fo shall NoV, be the required angle. For if the lines A B and E F were parallel; the inclination to the backfide and forefide, would be equal. Laftly, to find its inclination to the bottom; thro' the point v draw a perpendicular a b to N q, produced to a. From N, with the radius N'M, intersect the perpendicular in the point b. With the radius a b interfect the line v V. produced in the point c; fo shall a v c, be a right angled triangle, and the angle c a v, the inclination to the bottom. For if the plane MNPR, was projected upon the horizontal plane, the point M would be elevated till a perpendicular from it would fall upon the point v; so a v would be the base, and a b the hypothenuse of the right angled triangle a v c.

DEMONSTRATION.

At N erect the perpendicular NX, make Ns equal to Nq; then will NsYX, be the true dimensions of a plane intersecting the elevation in the line X N, and the horizontal in the line Nq, by the preceding problem; and the angle X Nq a right angle. For when the plane ABCD, is erected perpendicular to the plane ABFE; if the plane XNsY, be turned round upon the axis XN, the point s will describe the semicircles qcb, as if a door be opened, and turned upon the hinges till it lies against a partition or wall, the bottom of it will describe a semicircle upthe floor. But if the upper hinge, suppose at X, be moved to M, it is plain the point q in the bottom of the door will not touch the floor.

And if the door be turned round upon the axis M N, till it lies flat upon the partition, or plane X N s Y; the line N q will lie upon the perpendicular N e; the angle M N q being always a right one; for the bottom

tom of the door is square. But the required plane must touch the floor when it is in the direction of the line Nq; therefore it cannot be fquare: And because the extremity of the bottom, when the plane is in its proper position, will be so far elevated above the plane MNsR, that a perpendicular from it will fall in the point z; it is obvious, that in turning the door upon the axis M N, a perpendicular let fall from the extreme point of the bottom, will always meet the plane M f P R, somewhere in the perpendicular f z produced; and therefore when the door is laid flat upon the partition, or plane M N P R, that extreme point must lie upon the point P, because the dotted line N P, is made equal to N q; and when PR is drawn parallel to MN, and MR parallel, and equal to NP, we shall have the plane MNPR; fo the angle MNP, will be that which the bottom makes with the fide of the door. By which means the triangle N k P, will be added to the fquare bottom; and when the door is turned upon the axis M N, till it is in the direction of the line Na: the dotted line N P will lie close upon the floor on the line Na: When the door is in this position, if the stock of a square be laid upon the plane MNsy, which may represent the partition of a room, and the tongue erected perpendicular to the plane, we may describe the line z n, by keeping the stock of the square perpendicular to the line MN; and moving it along the plane in that direction, the tongue always touching the fide of the door. All which will appear very plain when the planes are cut by the dotted lines, and erected to their proper positions.

Thus I have endeavoured to explain the principles of the orthographick projection, by laying down the fimplest solid that can well be thought of, or conceived: And if I have not done it in such a manner as to make it intelligible to all capacities, it may be owing to their want of a sufficient

knowledge of the principles of geometry and trigonometry.

If they cannot attain this by what has been faid on those subjects in the first part, I would advise such to have recourse to a master for instruction. If they are at a loss how to lay down a solid limited by fix planes, which requires no curves, it will be in vain for them to proceed any farther. For it will be impossible for them to comprehend the reason of the methods used in laying down irregular solids limited by various surfaces, some of which are plain, and others very irregular curves.

In laying down any irregular folid, we may suppose it to be inclosed within fix planes, the opposites of which may be equal and parallel, and all the planes right angled; so we may then proceed upon the same principles as before, for we shall have the dimensions of the three necessary

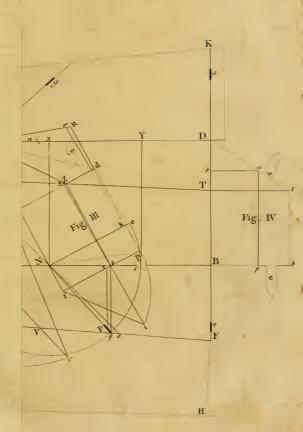
planes

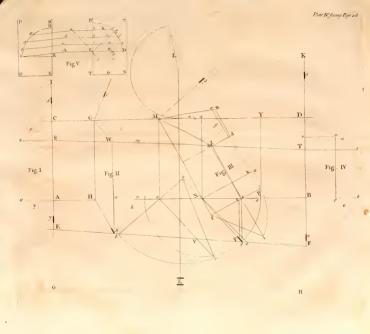
planes, viz. horizontal, elevation and profile. And if the true form and dimensions of two planes parallel to the profile, and likewise their distance from one another be given; we may find the true form and dimensions of any intermediate planes between them, in the same manner as we have done in that already laid down. But it must be observed, that the form of the surface, which limits that part of the solid intercepted betwixt the two given planes, must likewise be given; which shall be shewn plainly when we come to apply what has been now said to the actual laying down of ships on a plane.

CHAP. II. SECT. I.

Explication of the Terms and Names of the Lines used in drawing Ships.

WHAT is chiefly intended in drawing of ships, is to find the form of all the timbers. Now if a ship's side were strait fore and aft, this could be done with as much certainty, as in the folid laid down in the preceding chapter. In that case we need only determine the form of the foremost and aftermost timbers, and then all the sections, either parallel or inclined to the horizontal, cutting the ship lengthwise, would be limited by strait lines; any two points of which being given, a ruler or ftrait edged batten would find the whole line. And tho' all fections parallel to the profile may be limited by curves, and these very irregular, yet if a fufficient number of points be found in each, a thin batten of pliable wood may be bent fo as to touch all the points; and fo describe what is called a fair curve. Now we may have as many points as we please, only by forming as many sections, either parallel or inclined to the horizontal, as shall be thought necessary to have points: For upon supposition that the side is strait fore and ast, these sections will all be limited by strait lines, their lengths will be the given distance betwixt the two parallel planes, and their breadths will be determined by the direction in which they cut the profile. This is fo plain that it needs no example,





ample, and a case that cannot happen in laying down a ship; which being broader near the middle than at either end, cannot have a strait side, And therefore there will be a necessity of determining the form of the profile, by a section at the broadest place of the ship; and also the form

of a fection near each end parallel to the profile.

There can be no invariable rule given to determine the form of these three sections, because they must be conformable to the service the ship is designed for: However, determined they must be, before we can begin to find the form of the intermediates; if by no other means, by repeated trials, till they please the fancy of the artist, affished by his judgment in discerning what form will best answer the proposed design. The next thing to be determined, is the form and dimensions of several sections, either parallel or inclined to the horizontal. They will all be limited by curves, some of which will be very irregular. However there will be three points in each section given, by the direction in which they cut

the given planes.

Here we think it necessary to explain what is to be understood by a fair curve; a term frequently used in drawing: In order to which it must be observed, that the circumference of a circle seems to be the only curve that can with certainty be drawn; for this requires no art. But in defcribing an ellipfis we must find several points, thro' which the curve must pass according to the established properties of that curve; and then these points may be joined by a steady hand, which may be assisted by a mould or pattern, of which the artist should be provided with a variety of different forts made of pear-tree, box, or some other wood proper for that purpose. Now if one that is not very well acquainted with drawing, should attempt to join these points without some such affistance, he would make rather a polygon, confifting of feveral very obtuse angles, than a curve; whereas a mould that will just touch three, four, or more of the points, will cut off all these angles and irregularities, by which means the curve will be clear of all breaches, or fudden turnings and deviations; and this is what is called a fair curve. From this description of it, we may plainly see that, if there be only three points of the curve given, there may be feveral curves drawn thro' them, and all very fair.

In forming an ellipsis, if the transverse and conjugate diameters be given, we may with certainty, find any number of points, thro' which the curve must pass. But the curves that are formed by the several sections of a ship, are very irregular; and as they have no properties peculiar to themselves, except that of being fair, there can be no invariable rule for describing them. We shall therefore attempt to do it by sector

lines

lines taken from an approved body. This will undoubtedly form lines fimilar to the original; and the fector is fo contrived, that it will form very fair lines quite different from the original. It is prefumed this will be very useful to those that are not well acquainted with drawing, for whose use it is chiefly intended. However, before we describe it, we shall shew the methods generally used to regulate the form of all the curves that are necessary in drawing of ships; and in the first place shall explain their names in the following definitions. We shall make use of three planes, as described in the preceding chapter, but give them different names.

FINITION

1. The sheer plane is the same with that of elevation, and is a section of a ship supposed to be cut, by a plane passing thro' the middle line of the keel, stem and stern-post.

2. The floor plane is the fame with the horizontal, and is that on which the whole frame is erected: The upper fide of the keel is in this

plane.

3. The body is the same with the profile. It is a section, supposed to cut the ship thro' the broadest place, and is perpendicular to the sheer

and floor planes.

4. Water lines are supposed to be drawn on the surface of a ship, by the upper part of the water into which the swims, and are formed by the section of a plane cutting the whole body lengthways, perpendicular to the sheer plane, where they will always be represented by strait lines: and if these are parallel to the keel, they will be represented by strait lines on the body plane, called level lines. But these planes will be limited by curve lines on the floor plane, which in some cases will be inverted at the after end, and also at the fore end; but this last is avoided as much as possible. These curves limit the breadth of the ship at certain heighths, expressed by lines drawn on the sheer plane for that purpose. But as the theer plane cuts the ship exactly in two equal and fimilar parts, only one half of these sections are laid down; so that one side will always be represented by a strait line.

5. The heighths of the breadth lines are described on the sheer plane, to determine the heighths at which the half breadth of the planes of the timbers are to be fet off; in which respect, the water lines on the sheer plane may be called the heighths of the breadth lines. But because the extreme breadth of the plane of each timber rifes gradually from the midships fore and aft; the lines representing their heighths will be curves.

Such

Such are the main, and top timber heighths of breadth lines, which are the principal ones that go by that name; but there may be as many more as shall be judged necessary to determine the form of all the timbers.

6. Half breadth lines are described on the floor plane, and are curves limiting the \$\pm\$ breadths of the planes of the timbers, at the heighths expressed by the corresponding heighth of breadth on the sheer plane, in which respect the water lines may be called \$\pm\$ breadth lines; but that name is generally given only to such whose heighths are expressed by curves on the sheer plane. They are formed by supposing the ship to be cut length ways, in a perpendicular direction to the sheer plane, thro' a curve heighth of breadth line. This will form an uneven surface; so the true length of it is not represented on the floor plane.

7. Ribband lines are either square or canted.

The square which is often called the horizontal ribband line, is in all respects the same with the above described the breadth lines: The use of the ribband lines, is to fasten the timbers before the plank is brought on; for which purpose, they must be of a sufficient substance, and formed in such a manner, that they may fit the timbers without forcing or penning them. It would be very difficult to make a square one, because it rounds two ways; for when the ship is cut upon a level by this ribband, the surface produced, will be an uneven one. Upon this account, a plane must be so inclined to the sheer plane, that it shall interfect the timbers at the same points with the square ribband.

The cant or diagonal ribband, so called, because it cuts the body plane in a diagonal, is formed by a plane inclined to the sheer plane; and cutting the ship length ways in that direction, in such a manner, that it will intersect the timbers in the same points that the square ribband does. It will intersect the sheer plane in a strait line parallel to the keel, at the same heighth at the stem and post, with that of the square ribband. Its representation on the floor plane, will be the same as that of the square ribband. But because the plane of it is not parallel to the floor plane; this will not be the true breadth of it. This may be found by Prob. 3. of the preceding chapter, by which means we shall obtain the exact length and breadth of it; and being a plane, it will only round one way, and so a ribband may easily be made by it.

8. Sweeps, are arches of circles, described in the body plane to form

the timbers, and are generally four.

1st. The floor sweep, which is limited by a line drawn in the body plane, perpendicular to the middle line, a little above the keel. The distance of this line above the keel at the midship timber, is called the dead rising; the upper part of this arch forms the head of the sloor timber.

2d. The under breadth (weep; the center of which is in the line that represents the heighth of the extreme breadth of the timber. If there is a part of the timber strait, the center of the sweep will be in the lower line. From this center extend to the point that limits the + breadth of the timber in the same line, and with that radius describe a circle downwards, till it comes near to the floor sweep.

3d. The reconciling fweep, which joins the two former in fuch a manner as to interfect neither; by which means we shall have a fair curve from the heighth of the breadth to the rising line: And if a strait line is drawn from the side of the keel at the upper edge, to touch the back of the floor sweep, we shall have the form of the midship timber below

the breadth.

4th. The upper breadth sweep; the center of which is in the line that represents the extreme upper heighth of the breadth of the timber; from which a circle must be described to pass thro' the point that limits the breadth of the timber in the fame line, and produced upwards discretionally to form the top timber. To these four some add a fifth, to form the hollow of the top timber; but this is generally done by a mould for placed as just to touch the above breadth fweep, and pass thro' the point that limits the 's breadth of the top timber: So that now the form of the midship timber is determined from the keel to the top of the side. The radius of the underneath iweep decreases, the farther the timber is from the midships; but the other sweeps have generally the same radius for all the timbers. There is no certain rule to determine the radii of these fweeps. Some do it by proportioning them to the extreme breadth of the ship, according to some given ratio. But there are various ways of forming this midship timber; sometimes by two arches, and instead of having a strait line from the edge of the keel to touch the back of the floor fweep in some ships it is made a hollow.

9. Half breadth of the floor is the distance of the center of the floor sweep from the middle line in the body plane, at the midflip timber, which will always be less than the distance betwixt the point where the strait line drawn from the fide of the keel to touch the back of the floor sweep is from the middle line. This last may be called the true! breadth

of the floor, and in sharp ships will be above the rising line.

to. Rifing of the floor, is a curve drawn on the sheer plane, limited at the midships by the dead rifing; and in flat ships it runs nearly parallel to the keel for some timbers before and abast the midship, for which reason these timbers are called flats; but in sharp ships it rifes gradually from the midship till it ends on the stem and post. To this line is some-

times adapted an ! breadth of the floor line. The use of these two lines is

to find the centers of the floor fweeps.

11. Cutting down line, is drawn on the sheer plane. It is limited in the midships by the thickness of the shoot timber, and abase by the breadth of the kelson; for it must be carried so high abase as to leave room for the kelson, for which purpose the thickness of the timbers must be known. It must be carried up so high upon the stem as to leave sufficient substance for the breeches of the riling timbers. The lower edge of the kelson is in this line; so it limits the thickness of all the shoot timbers, and likewise the heighth of the dead wood afore and abase.

12. Timber and room, or room and space, is the distance betwixt the moulding edges of two timbers, which must always contain the breadth of two timbers, and sometimes two or three inches between them. It must be observed, that one mould serves for two timbers; the foresside of the one being supposed to unite with the aftside of the other, and so make only one line, which is actually the case in all the frames, which in some ships are every third, in others every fourth timber. The frames are first put up, and saftened to the ribbands, and afterwards the others are put up, which are called filling timbers. The midship timber is called dead-stand distinguished by this character \bigoplus ; the timbers abase the midship are distinguished by the figures 1, 2, 3, &c. and those before the midship by the letters of the alphabet A, B, C, &c.

S E C T. II.

Of WHOLE MOULDING.

HE length of the keel, extreme breadth, depth in the hold, heighth between decks, and in the waste; and sometimes the heighth and breadth of the wing transom are agreed on by contract in the merchant's service: From which dimensions the builder is to form a draught suita-

ble to the trade the ship is designed for.

The first thing that is generally done, is to lay down the keel, stem and post, upon the sheer planes: Then to determine the proper station of the midship timber, where a perpendicular is erected: It is generally about \$\frac{1}{2}\$ of the keel before the post. On this line the given depth of the hold is set off from the upper side of the keel; to obtain which point, the thickness of the timber and plank must be added to that agreed on

bv

by contract. This being fixed, will enable us to determine the upper heighth of the extreme breadth at that place, which fometimes is the very point itself. The lower heighth of the breadth must likewise be determined at this place. Then we may form the two main heighths of the breadth lines which nearly unite abaft and afore. Abaft, these curves end at the wing transom, or above it; and afore, they are carried up sometimes as high as the hawse holes. The heighth of the breadth line of the top timber must likewise be formed. This is generally done by a bow, which makes nearly an arch of a circle. It is limited in midships by contract, afore and abaft only by the fancy and judgment of the artift, according to what sheer he designs: We must also form a line for the rifing of the floor; for which purpose we must determine the dead rising, which is that of the midship timber. This limits it at that place, and in the whole moulding it is pretty near parallel to the lower heighth of the breadth line. These lines must absolutely be drawn on the sheer plane; and corresponding to the main and top timber heighth of breadth lines: there must be two half breadth lines formed on the floor plane.

The main half breadth at the midship timber is agreed on by contract, only observing that the thickness of the timber and plank must be deducted out of it, because it is the extreme breadth from outside to outfide of the plank that is contracted for. Those in the draughts are called moulded half breadths: Then the breadth at the wing transom, if a square stern, is limited: It is generally about two thirds of the extreme breadth, but this is just as the artist shall think proper. He also fixes the breadth of the top timber, and then describes the two half breadth lines. In the due formation of these curves on the sheer and sloor plane. the whole art of drawing chiefly confifts; which must be acquired by practice, fo that it will be fearce possible for one that is not very well acquainted with drawing, to form them, without having recourse to some other draughts. After these are formed, the stations of the timbers are fixed, if the room and space, and the breadth of the midship timber is agreed on by contract, this will determine the station of all the stimbers; observing that the timbers abaft the midships must be set off from the forefide of the midship timber; and the timbers before the midship from the aft fide of it. At every third or fourth timber there must be perpendiculars drawn on the sheer and floor planes, to the line that represents the lower edge of the keel, which is the common fection of these two planes; tho' fometimes the half breadth lines are described on the sheer plane, when there is not space to produce the perpendiculars till they be of sufficient length to contain the heighth of the breadth and half breadth. After

After the timbers are stationed, and the perpendiculars for the frames drawn on the sheer and floor planes; we proceed to the body plane, and draw a line equal in length to the whole breadth moulded. This line may be called the base of the hody plane. A perpendicular is erected at each end of it, and one in the middle, which may be produced at pleasure. The next thing to be done, is to form the midship frame: The limits of it are had from the sheer and sloor planes; the lower, upper and top timber heighths of the breadth are taken from the theer plane at the perpendicular, representing the midthip frame, and fet off on the middle line of the body plane from the base. Thro' these points, lines are drawn parallel to the base, and the respective half breadths corresponding to each, are set off on these lines, from the middle line in the body plane. The lower and upper main half breadths are limited by the perpendiculars already drawn at each end of the base. The half breadth of the top timber, is had from the floor plane on the perpendiculars reprefenting the midship frame. The heighth of the dead rifing is likewise taken from the sheer plane, and set up from the base upon the middle line in the body plane, thro' which point a line parallel to the base must be drawn; and upon this line the half breadth of the floor, is fet off from the middle line, at which point a perpendicular is erected. The center of the floor sweep is in this line, from which a circle must be described that shall just touch the rising line. A proper radius for the under breadth sweep is next to be found: The center of it is in the lower breadth line, from which it is described to pass thro' the point which limits the half breadth. After which the radius, and center of a reconcileing sweep to join the floor, and under breadth sweeps is found, and the circle described; and to compleat the frame below the breadth, the half breadth of the keel is fet off from the middle line on the base; from which point, a strait line is drawn to touch the back of the floor sweep.

By this way of forming the frame, it is plain the centers and radii of the fweeps are arbitrary, but they must be determined before any of the enter timbers can be formed; if by no other means, by repeated trials, till they are made to please the fancy and judgment of the artist. But there are various other ways of forming this frame; fo that, the' feveral ships may be of the fance breadth, depth in the hold, and dead rising; they may all differ in the form of their timbers. After this midship timber is formed, a pattern or mould is made to fit exactly to the curve, and the dead rising line. By this, and a hollow mould, all the timbers are formed for as the rising line, and lower heighth of the breadth line are parallel to one another in the sheer plane: This is what is called whole

moulding, which we shall illustrate by laying down a long boat. And because in several mould lost there is not sufficient length for the sheer plane, it is often haid down as if it were cut by the midship frame, and one part laid upon the other in such a manner, that the midship timber of the after part shall coincide with a perpendicular let fall from the fore part of the sem.

To lay down a Long-Boat 29 Feet 1 Inch long, and Breadth Moulded 9 Feet. (See Plate 5.) 8172.

1/l. Draw the strait line P ①, and erect the perpendicular P T. From the point P set off 29-1, the given length of the keel. But because the plate will not admit of the whole length, let the station of the midship timber be assigned; at which point erect the perpendicular ① M. Let M be the upper, and N the lower heighth of breadth, at that place; T the heighth of breadth at the transom, and draw the curve T M to represent the sheer, or extreme heighth of the side. This in a ship would be called either the upper heighth of breadth line, or the upper edge of the wale. Draw also a curve thro' the point N, parallel to T M, to represent the breadth of the upper strake in a boat, or lower edge of the wale, if in a ship. The dotted line T N may also be drawn to represent the lower heighth of breadth.

2d. Set off the rake of the post from P to p, and draw the line p t to represent the aft side of the post; so shall T t represent the round up of the transom. Set off the breadth of the post from p to r, and from T to s, and draw the line r s to represent the fore side of the post, which may either be a curve or a strait line at pleasure. Set up the heighth of the tuck from p to k. Let k x be the thickness of the transom, and draw the

line zx to represent the forc side of the transom.

3d. Set up the dead rifing from \bigoplus to d, and form the rifing line ris. We may then draw the line K L parallel to $P \bigoplus$, to reprefent the lower edge of the keel, and another to reprefent the thickness of the plank or the rabit. The rabit on the post may likewise be represented, and the stations of the timbers assigned; distinguished in the plate by their pro-

per names, viz. 1, 1, 2, 3, 4, 5, 6, 7, 8, 9.

Thus have we compleated the sheer plane, or side draught for the after body; and in like manner is that for the fore body to be done. First produce the line \bigoplus M to y the heighth of the fore part of the stem, and form the stem either by sweeps or some other contrivance. The breadth of the stem must be known, and the aft side likewise formed. The stem being formed, we may set off from the fore part of it as much as the line

P \bigoplus wanted of the whole length of the boat, which suppose \bigoplus \bigoplus . Erect the perpendicular \bigoplus F, and make it equal to \bigoplus M, the heighth of the sheer, and form the curve F S, which will represent the sheer or heighth of the side in the fore body. We may likewise draw a line to represent the lower part of the upper strake, and one for the lower heighth of the breadth. The rising line must also be formed, and the timbers stationed and distinguished by their proper names \bigoplus , \bigoplus , A, B, C, D, E, F, G, H. Now the whole sheer plane is compleated; for if the line S T was drawn assumed, till the point F came to the point M, we should have the whole length of the boat.

the defigned round of the harpin.

We must in the next place form the midship timber, either by twoor three sweeps, or some other contrivance which must be left entirely to the sarcy and judgment of the artist: If he uses three sweeps, a proper center of each must be sound. That of the under breadth must always be in the breadth line, as in this case at a. The center of the sloor sweep, suppose at C, must be so, that when it is described, the back of the sweep may just touch the rising line. These two centers being sound, and the arches described, we may with certainty find the center of the reconciling sweep, provided the radius be known, thus: Set off the given radins upon any strait line, as from A upon the base line to R; then take the radius of the lower breadth fweep, which fet off from A to a; take alfo the radius of the floor fweep, and fet off from A to c: Then with the radius a R, from the center of the under breadth fweep, deferibe an arch; and with the radius c R, from the center of the floor fweep, describe another arch to interfect the former in r, which will be the center of the reconciling fweep: For if with the radius A R, from the center r, we describe an arch, it will just touch the under breadth, and floor sweeps in the points t and s. A line drawn from r to t will pass through the center of the underbreadth sweep, and a line drawn from r to s will pass through the center of the floor fweep; fo that it will be impossible for the reconciling to interfect either of the other two arches. The curve part of the timber being formed, a strait line must be drawn from the fide of the keel to touch the back of the floor sweep; for which purpose the half breadth of the keel must be set off on each side of the point C, upon the base line. The form of the midship frame being determined, will in some measure determine the form of all the rest. For if a mould be made on any fide of the middle line to fit the curve part of it; and the rifing line, as that marked B E N D, and laid in fuch a manner that the lower part of it, which is strait, may be set upon the several risfing lines, and the upper part just touch the point of the half breadth in the breadth line, corresponding to that rifing upon which the mould is placed; a curve may then be drawn by the mould to the rifing line. In this manner we may proceed fo far as the rifing line is parallel to the lower heighth of the breadth line. Then a hollow mould must be made. the upper end of which is left strait, as that marked H l w. This is applied in fuch a manner, that some part of the hollow may touch the fide of the keel, and the strait part touch the back of the curve before described by the bend mould; and, beginning abaft, the strait part will always come lower on every timber till we come to the midship timber, where it comes to the fide of the keel. Having thus formed the timbers, fo far as the whole moulding will ferve; the timbers abaft them are next formed. Their half breadths are determined by the sheer and floor planes, which is the only fixed point thro' which the curve of these timbers must país. Some form these after timbers before the whole is moulded, and then make the hollow mould, which will be straiter than the hollow of either of these timbers. It is indifferent which are first formed, or what methods are used; for after the timbers are all formed, tho' every timber may appear very fair, when confidered by itself, it is uncertain, what the form of the fide will be. In order to find which, we must form several ribband

band and water lines; and if these do not make fair curves, they must be rectified, and the timbers formed from these ribband and water in using the hollow mould, when it is applied to the curve of each timber, if the strait part is produced to the middle line, we shall have as many points of interfection as there are timbers: And if their heighths above the base be transferred to the corresponding timbers in the sheer plane, a curve passing thro' these points is what is called a rising strait. This may be formed by fixing a point for the aftermost timber that is whole moulded, and transferring that heighth to the sheer plane. The curve must pass thro' this point, and fall in with the rising line, somewhere abast (1): And if the several heighths of this line be transferred from the sheer. to the middle line in the body plane; these points will regulate what is called the hawling down of the hollow mould. The timbers being thus formed, and proved by ribband and water lines; we may then form the transom. This may be done either by ribband or water lines. Here it is by water lines, of which there are three, formed in the following manner. (Plate 5.)

1/l. Draw three lines in the body plane parallel to the base: These are called level lines, and may be equally spaced betwirt the tuck, and heighth of the sheer, taken upon a perpendicular to the keel. They may be likewise drawn on the sheer plane at the same heighths, so they will be parallel to the keel. They are distinguished by 1/s. 2d. and 3d. W.

2dly. To form them on the floor plane. Take the distance betwixt the middle line in the body plane, and the several intersections of the level lines with the timbers: Transfer these to the corresponding timbers in the floor plane, which will give the points thro' which the curves will pass: So the portion of the first level line in the body plane, intercepted betwixt the middle line and timber 9, will be equal to the distance taken upon the perpendicular in the floor plane, drawn from the point 9, to intersect the curve of the first water line. The like may be said of all the rest.

The water lines being thus formed; the next thing to be determined, is the round aft of the transom, if any; if none, produce the line $T \not o$ to b, then will $K \not o$ be the half breadth of the transom at the heighth of the theer: So the heighth P T in the sheer plane, must be transferred to the middle line in the body plane. Thro' this point a line $K \not o$, must be drawn parallel to the base A C, upon which the half breadth $K \not o$ being set off, we shall have one point thro' which the curve must pass. In like manner there must be perpendiculars let fall from the several intersections of the water lines, and aft side of the post in the sheer plane, and produ-

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ced to interfect their corresponding water lines in the floor plane; which will give their half breadths. These again being transferred, to their corresponding level lines in the body plane, we shall have the points through which the curve of the transom must pass; observing at the tuck to set off the half breadth of the post; or the depth of the rabbet may be deducted out of it. The transom being thus formed, it is plain it will be too short, by reason of the raking of the post: We must therefore take the heighth of the transom upon the rake, which will be the line p T in the sheer plane; and set up this on the middle line in the body plane. In like manner we must fet up on the middle line in the body plane, the several distances of the water lines, from the point p in the sheer plane; and thro' these points draw the several dotted lines, upon which must be set off the half breadths as before: Then a curve passing thro' these points, will give the true form and dimensions of the transom, as is expressed by the dotted curve.

If the transom is to round aft, as the curve K n G on the floor plane, it may be formed after the same manner without regarding the round; and after it is properly trimmed the round may be worked out: But as this will require very thick plank; in fuch cases it will be proper to make use of a fashion piece, and wing transom: This fashion piece will be formed in the same manner as that for a ship which has a square tuck,

fo the fame operation will ferve for both.

Now the fashion pieces being always sided strait, their planes will intersect the sheer and sloor planes in a strait line. In this case, it will be in the line G g on the floor plane, which touches the transom in the point n; G n being supposed the thickness of the fashion piece. Having thus determined its direction on the floor plane, this will likewise determine its direction on the sheer plane. If the transom had no round, only what is called a flight or rifing like a floor timber, the plane of the fashion piece would intersect the sheer plane in the rabbet of the stern post; and the floor plane in a strait line drawn from G to K. But here it is supposed to be in the line G g, which will throw the head of the fashion piece aft to W on the sheer plane; the point where a perpendicular erected from g interfects the sheer line or breadth line produced. Now k being the heighth of the tuck, the line k W will be that in which the fashion piece interfects the sheer plane.

Having thus found the interfection of the plane of the fashion piece, both on the sheer and sloor planes, it is evident it will rake aft and cant forward; fo the true dimensions and form of it may be found by Prob.

6. Chap, 1, in the following manner.

is. Produce all the water lines in the sheer plane, to the line k W in the points a, s, b,; and let fall the perpendiculars a e, s o, b u.

adly. From the points e, o, u, draw lines parallel to G g, to interfect each corresponding water line on the floor plane in the points 3, 2, 1.

3dly. Transfer the several points G, 3, 2, 1, on the floor plane, to the points G, 3, 2, 1, on the sheer plane, in such a manner, that lines drawn from G to G, from 3 to 3, &c. may be perpendicular to g L; and let the point G be in the breadth line, the point 3 in the third water line, &c. on the sheer plane; so the plane W G 3 2 1 k will be the projection of the plane of the fashion piece on the sheer plane. But it will be less than the plane of the fashion piece, because it is not parallel to the sheer plane. Therefore,

4thly. Thro' the points G, 3, 2, 1, in the sheer plane, draw the dotted

perpendiculars GF, 3A, 2S, 1H, to the line Wk.

5thly. Make the lines W F, a A, s S, b H, in the sheer plane, equal to the lines g G, e 3, o 2, u 1, in the shoor plane; so that they may intersect the dotted perpendiculars in the points F, A, S and H: So shall W FAS H k be the true form and dimensions of the plane of the aft side of the sashin piece. When it is in its proper position, the line W F will be in the same plane with the sheer line; the line a A in the same plane with the water line a 3; the line a S in the same plane with the water line a 3; and the line a H in the same plane with the water line a 1.

We have now formed all the timbers in the after body. Those for the fore body are formed in the same manner, by transferring the several heighths of the rising and breadth lines from the sheer to the body plane; the half breadths corresponding to each heighth, must also be transferred from the floor to the body plane. The same hollow mould will serve both for the fore and after body; and the level lines by which the water lines, to prove the after body, were formed, may be produced into the fore body, and by them the water lines to prove the fore body may be described.

Another method of proving the body, is by ribband lines, which are formed by fections of planes inclined to the sheer plane, and intersecting the body plane diagonally, as before observed; of which there may be

as many as we shall judge needful.

Here we think it sufficient to lay down one, represented in the body plane by the lines marked dia. These are drawn in such a manner, as to be perpendicular to as many timbers as conveniently may be. After they are drawn in the body plane, the several portions of the diagonal, intercepted betwixt the middle line and each timber, must be transferred

T₂ to

to the floor plane: Thus, fix one foot of the compasses in the point where the diagonal interfects the middle line in the body plane; extend the other foot to the point where the diagonal interfects the timber, suppose timber of fet off the same extent upon the perpendicular representing the plane of timber 9, from the point where it interfects the line K L, on the floor plane; do the fame by all the other timbers both in the fore and after body; and we shall have the points thro' which the curve must pass. And if this should not prove a fair curve, it must be altered, obferving to conform to the points as nearly as the nature of the curve will admit: So it may be carried within one point, and without another, according as we find the timbers will allow: For after all the ribband lines are formed, the timbers must, if needful, be altered by the ribband lines, this is only the reverse of forming the ribband lines; for taking the portions of the feveral perpendiculars intercepted betwixt the line K L, and the curve of the ribband line in the floor plane, and fetting them off upon the diagonal, from the point where it interfects the middle line; we shall have the points in the diagonal, thro' which the curves of the timbers must pass: So the distance betwixt the line K L, and the ribband at timber 3 on the floor plane, when transferred to the body plane, will extend on the diagonal, from the middle line, to the point where the curve of timber 3 interfects that diagonal. The like may be faid of all the other timbers; and if feveral ribband lines be formed, they may be fo contrived, that their diagonals in the body plane shall be at such distances, that a point for every timber being given in each diagonal, will be fufficient to determine the form of all the timbers.

In stationing the timbers upon the keel, for a boat, there must be room for two futtocks in the space before, or abast \bigoplus ; for which reason, the distance betwixt those two timbers will be as much more, than that betwixt the other, as the simber is broad. Here it is betwixt \bigoplus and \bigotimes ; which contains the distance betwixt \bigoplus and \bigotimes , and the breadth of the

timber besides.

This method of whole moulding will not answer for the long timbers afore and abaft: They are generally canted in the same manner as those for a ship, of which we shall treat in their proper place; and here shew in what manner the timbers are moulded after they are laid down in the

mould loft, by a rifing fquare, bend, and hollow mould.

It was shewn before how to form the timbers by the bend and hollow moulds, on the draught. The same method must be used in the lost, but the moulds must be made to their proper scantlings in real seet and inches. Now when they are set, as before directed, for moulding each timber,

timber; let the middle line in the body plane be drawn across the bend mould, and draw a line across the hollow mould at the point where it touches the upper edge of the keel; and let them be marked with the proper name of the timber, as in the figure (Pate 5.): So the graduations of the bend mould will be exactly the same as the narrowing of the breadth; for the distance betwixt \bigoplus and 7, on the bend mould, is equal to the difference betwixt the half breadth of timber 7, and that of \bigoplus . The heighth of the head of each timber is likewise marked on the bend mould, and also the floor and breadth sirmarks. The floor sirmark is in that point where a strait edged batten touches the back of the bend mould, the batten being so placed as to touch the lower edge of the keel at the same time. The several risings of the floor, and heighth of the cutting down line, are marked on the rising square, and the half breadth of the keel set off from the side of it, as in the figure.

Note. The cutting down is omitted in the plate to avoid confusion. The moulds being thus prepared, let it be required by them to mould

timber 7.

The timber being first properly sided to its breadth, lay the bend mould upon it, so as may best answer the round according to the grain of the wood: Then lay the rifing square to the bottom of the bend mould, so that the line drawn across the bend mould at timber 7, may coincide with the line representing the middle of the keel upon the rifing square; and draw a line upon the timber by the fide of the square, or let the line be scored, or cut by a tool made for that purpose, called a raseing knife. The term rafeing is used when any line is drawn by such an instrument instead of a pencil. This line so rased will be the side of the keel. Then the square must be moved till the side of it comes to 7 on the bend mould. and another line must be rased in by the side of it, to represent the middle of the keel. The other fide of the keel must likewise be rased after the fame manner, and the point 7 on the rifing square be marked on each fide of the keel, and a line rased across at these points, to represent the upper edge of the keel. From this line the heighth of the cutting down line at 7 must be set up, and then the rising square may be taken away, and the timber may be rased by the bend mould, both inside and outside, from the head to the floor firmark: Or it may be carried lower if needful. After the firmarks, and head of the timber are marked, the bend mould may likewise be taken away; and then the hollow mould applied to the back of the fweep in fuch a manner, that the point 7 upon it may interfect the upper side of the keel, before set off by the rising square: And when in this polition, the timber may be rafed by it, which will compleat the outfide

SECT

fide of the timbers. The infide of the timbers may likewise be formed by the hollow mould. The scantling at the keel is given by the cutting down before set off. The mould must be so placed, as to touch the sweep of the infide of the timber formed before by the bend mould, and pass thro' the cutting down point.

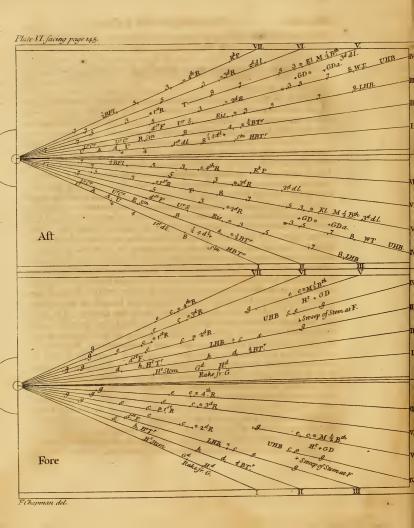
The use of the firmarks, is to find the true places of the futtocks; for as they are cut off 3 or 4 inches short of the keel; they must be so placed, that the futtock and floor firmarks may compare, or coincide: Notwithstanding which, if the timbers are not very carefully trimmed, the head of the futtock may be either within or without its proper half breadth;

to prevent which a half breadth staff is made use of.

The half breadth staff may be one inch square, and of any convenient length. Upon one side of it are set off, from one end, the several half breadths of all the timbers in the after body; and those of the fore body upon the opposite side. On the other two sides are set off the several heighths of the sheer; the after body on one side, and the fore body on its opposite. Two sides of the staff are marked half breadths, and the other two sides, heighth of the sheer, as in the sigure. (Plate 5.)

The staff being thus prepared, and the sloor timbers fastened on the keel, and levelled acros; the futtocks must next be fastened to the floor; but they must be set first to their proper half breadth and heighth: The half breadth staff, serves to set them to the half breadth; for which purpose a small line, called a ram line, is stretched from the middle line of the stem, to that of the transom or post; to which a plummet is hung by a line, fo tied round the ram line, that it may flip eafily along upon it, and may be moved to the plane of any timber, and as the plummet will occasion this line to be always perpendicular to the keel, which in a boat is generally parallel to the plane of the horizon: We may, by it, likewise set the timbers perpendicular to the keel, and then set them to their proper half breadth by the staff; and when the two firmarks coincide, the futtock will be at its proper heighth, and may be nailed to the floor timbers, and likewife to the breadth ribband; which may be fet to the heighth of the sheer by a level laid across, taking the heighth of the sheer by the staff from the upper side of the keel; by which means we shall discover if the ribband is exactly the heighth of the sheer; and if not, the true heighth may be fet off by a pair of compaffes from the level, and marked on the timbers. The next thing to be explained, is the construction and use of the bevelling board; but we shall first shew how to form the timbers by fweeps, because the same method for bevelling serves for both.





SECT. III.

Of forming the Body by Sweeps. (Plate 7.)

N thips of war the general dimensions are established by the authority of those appointed by the government for that purpose, which I have collected into a table, together with the principal dimensions of ships for

the merchant fervice, to which we refer our readers.

The sheer and floor planes are laid down in this, exactly in the same manner as in that of whole moulding. We may have a fufficient number of points from the tables, to determine the heighths of the breadth, and half breadth lines. A rifing of the floor line must likewise be formed on the sheer draught. We may then go to the body plane, and form the midship bend or frame timber; the limits of which, we have from the sheer and floor planes, and it must be formed in the same manner as before directed in whole moulding, either by two, three, or more fweeps, as the artist shall think most suitable to the service the ship is designed for. The lower, upper, and top timber heighths of breadth, and rifings of the floor, are fet up on the middle line in the body plane, as in whole moulding, and lines drawn thro' these points parallel to the base upon which the half breadths are set off. A mould may then be made for the midship frame as before, and laid upon the feveral rifings in the fame manner as in whole moulding, with this difference; that here an under breadth sweep is defcribed to pass thro' the point which limits the half breadth of the timber; the center of which will be in the breadth line of that timber. The proper centers for all the frames being found, and the arches described, the bend mould must be so placed on the rising line of the sloor, that the back of it may touch the back of the under breadth sweep. But the general practice is to describe all the floor sweeps with compasses as well as the under breadth fweeps, and to reconcile these two by a mould which is an arch of a circle; its radius being the same with that of the reconciling sweep, by which the midship frame was formed. It is usual for all the floor sweeps to be of one radius; and in order to find their centers, a line is formed on the floor plane for the half breadth of the floor: This, as was before observed, is only an imaginary one; for it cannot be described on the surface of the ship: Instead of it some make use of a diagonal in the body plane, to limit the half breadth of the floor upon every rifing line, and erect perpendiculars at the feveral interfections in the

the fame manner as for the midship frame, as in the draught; where it is very plain the sloor sweep constitutes no part of the after timbers abast

the fquare body.

After the sweeps are all described, we must have recourse to moulds, or some such contrivance, to form the hollow of the timbers, much in the same manner, as in whole moulding; and when we have thus formed all the timbers, they must be proved by ribband and water lines, as before directed; and altered, if needful, to make these lines fair. Hence it is obvious, that the form of the ribband lines must be determined, before we can with certainty have the true form of the timbers. But there will be a necessity of determining, at least, the form of three timbers, viz., the midship, foremost and astermost, before we can form a ribband line. These will give three points, thro' which the curve of each ribband must pass. The points in the intermediate timbers may be found by forming timbers as before directed; and by repeated trials, altering them till they make sair ribbands; for it is by them that the whole structure is regulated, when every frame is erected into its proper place.

S E C T. IV.

Description and Use of the Sector in forming the Body.

HE fector has feven lines on each leg, meeting at the center of the joint, numbered I, II, III, IV, &c. fo that every line upon one leg has a corresponding one upon the other leg, both divided and numbered alike. The after body is upon one fide, and the fore body on the other.

(Plate 6.) The Lines for the after Body are as follows.

I. Has five divisions, viz. \bigoplus , 4, 1th dl, 8, ftⁿ; and marked at the end HBT', denoting the heighth of the top timber breadth line at four timbers; ftⁿ is the ftern timber, and 1th dl, the first diagonal in the body plane.

II. Has eight divisions, viz. L'C, U, C, S, 8, 4, ⊕, and marked at the end 'BT', denoting the half breadth of the top timber at three timbers. L'C fignifies the lower counter, and U'C, the upper counter; to denotes

denotes the heighth, and A the rake of the counters, both taken from the wing transom; S' is the rake of the stern timber, which is likewise taken

from the wing transom at the heighth of the sheer rail.

III. Has eight divisions, viz. d^a, u'S. R 1 s, \bigoplus , 3, 5, 7, 8: It is marked at the end L H B, for the heighth of the lower breadth line for sive timbers: d^a is for the distance betwixt the frames, and R 1 s, for the distance betwixt the lower breadth line, and the dead tising in the body plane: u'S. is the radius of the upper breadth sweep.

IV. Is in two parts. The innermost has four divisions, viz. 7, 5, 3, ph. expressing the points where these timbers intersect the second diagonal in the body plane: It is marked at the end 2 R for the second ribband.

The outermost part has fix divisions, viz. \bigoplus , 3, 5, 7, 8, W T, and marked at the end U H B for the heighth of the upper breadth line at five

timbers, and at the wing transom denoted by W T.

V. Is likewise in two parts. The innermost has four divisions, viz. 7, 5, 3, \bigoplus , expressing the points where these timbers intersect the first

diagonal: It is marked 1 R for the first ribband.

The outermost part has eight divisions, viz. T, 8, 7, 5, 3, \bigoplus , kl, and then marked $M : \mathbb{R}^n$, for the main half breadth of five timbers; T for that at the wing transom, and kl for the half breadth of the keel in midhlips; without which there is another division marked 3^d d l for the third diagonal.

VI. Has four divisions, viz. 7, 5, 3, \(\oplus \); for the points where those timbers interfect the third diagonal, it is marked 3d R, denoting the third ribband; without which, there is another division marked 2d d l, for

the fecond diagonal.

VII. Has five divisions, viz. 7, ½ BF 1, 5, 3, ⊕. ½ BF 1, denotes the half breadth of the floor: The other four are for the points where those timbers intersect the fourth diagonal: It is marked 4 R, denoting the fourth ribband; without which there is another division for the rake of

the post marked R * P.

The heighth of the gun-deck is betwixt N° IV and V. G D \oplus for that in midthips, and G D a for that at the poft. There is likewise another division betwixt N° I and II for the fourth diagonal: It is marked $\frac{1}{4}$ 4"dl, which must be doubled, because the length of the sector will not contain the whole.

INDEX to the AFTER BODY.

	N°	N°
Heighth of breadth	$ \left\{ \begin{array}{l} \text{lower} \\ \text{upper} \\ \text{top timber} \end{array} \right\} \begin{array}{l} \text{III} \\ \text{IV} \\ \text{III} \end{array} $	$ \begin{cases} I \\ 2 \\ 3 \\ 4 \end{cases} $ $ \begin{cases} V \\ I V \\ VI \\ VII \end{cases} $
Half breadth Counter and stern to	{ main top timber } II VIII imber, heighth	Diagonals \[\begin{pmatrix} \begin{pmatrix} 1 & V & V & V & V & V & V & V & V & V &
and rake Rake of the post Upper breadth swee	VII	Distance betwixt the frames III

The Lines for the FORE BODY are.

I. Has three divisions, viz. H. stem, $\frac{G^4}{\text{rake f'}G}$ denoting the heighth of

the stem; and its rake from timber G at the gun-deck and head.

II. Has four divisions, viz. d, b, and these marked H, T, for the heighth of the top timber line at these timbers; and again d, b, for the $\frac{1}{2}$ breadth of those timbers; and the line marked $\frac{1}{2}$ B T.

III. Has four divisions, viz. d^{μ} F for distance betwixt the frames, and c, e, g; it is marked L H B, denoting the heighth of the lower breadth

line at these timbers.

IV. Is in two parts. The innermost has four division, viz, g, e, c, \oplus ; for the points of intersection of these timbers, with the second diagonal, is marked 2^4 R, for the second ribband.

The outermost part has three division, viz. c, e, g: It is marked UHB,

denoting the heighth of the upper breadth line at these timbers.

V. Is in two parts. The innermost has four divisions, $viz. g, e, c, \oplus$; for the points of intersection of these timbers, with the first diagonal: It is marked 1ⁿ R for the first ribband.

The outermost part has four divisions, viz. g, e, c, \(\phi\): It is marked

M & Bth for the main half breadth at these timbers.

VI. Has four divisions, viz, g, e, c, \bigoplus , for the points of intersection of these timbers with the third diagonal: It is marked 3^4R for the third ribband.

VII. Has four divisions, viz. g, e, e, \oplus , for the points of intersection of these timbers, with the sourth diagonal: It is marked 4^{th} R, for the sourth ribband. The sweep of the stem is betwixt N° III and IV; and the heighth of the gun deck betwixt IV and V.

IN-

INDEX to the FORE BODY.

Heighth of breadth	lower upper III IV II	Ribbands	$\left\{ \begin{array}{c} 1\\2\\3\\3 \end{array} \right\}$) V) V V V
Half breadth { main top tin Stem heighth and rak		Distance of frames Sweep of the stem		VII III I.I and IV

Having thus described the lines, we shall now shew their use in laying

down a ship. (Plate 7.)

The general dimensions being determined, and a scale adapted to the draught, take the half breadth with a pair of compasses, and placing one soot in the proper point for the half breadth of \bigoplus , which will be sound in N° V. open the sector till the other soot reaches to the same point in the corresponding line on the other leg.

The sector being thus set, it will be indifferent whether we begin with

the body or sheer plane: Let it then be the sheer.

L/l. Draw the line X Z to represent the upper edge of the keel, and length of the gun deck; but it may be produced to the aft side of the wing transom, and fore part of the stem.

2d. Erect a perpendicular to the line X Z, upon which fet up the heighth of the wing transom to W; taken from N° IV. on the sector.

3d. Take the rake of the post from N° VII. on the sector, and set it forward from the perpendicular of the wing transom to the point 7, where a perpendicular must be erected, which will be the station of that timber.

4th. Take the distance of the frames from No III. on the sector, and set it off from 7 to 8; and erect a perpendicular at that point for timber 8. Draw also a line from 8 to the wing transform, to represent the fore part of the post.

5th. Take the heighth and rake of both counters, also the rake of the stern timber from No II. The heighth of the stern timber is on No I.

and by these form the counters, and upright of the stern.

6tb. Station the timbers, by taking the distance betwirt the perpendiculars at 7 and 8; which at eight times will reach to \bigoplus ; and erect perpendiculars at 5, 3 and \bigoplus . Then for stationing the timbers in the fore body, we must turn the sector, and take the distance of the stames from N° III. which, see eight times from \bigoplus , will reach to H. Erect perpendiculars at C, E, G and H; and from G set off the distance of the guarantees.

deck before G. It is in \mathbb{N}° I, on the fector; which will reach to \mathbb{Z} ; at which point creek a perpendicular, and fet off the heighth of the gundeck, taken from the fector; and from the gundeck fet up the heighth of the head of the ftem, also its distance before G; both taken from \mathbb{N}° I. We may then form the stem. The center of the sweep is in the perpendicular of timber F, and the radius of the sweep is upon the sector betwixt \mathbb{N}° III and IV, which set up from the point F, will give the center: So the sweep will not reach to the gundeck, we must make use of a mould to break in fair with the back of the fweep.

CHAP. II.

7th. Set up the heighths of the lower, upper, and top timber breadth lifes upon the perpendiculars erected for the stations of the several timbers. The points corresponding to each, are on their proper lines on the

fector.

Having thus finished the sheer plane, we may then go to the shoor plane; and producing all the perpendiculars for the timbers, we may upon them set off the main, and top timber half breadths. The points corresponding to each, are on their proper lines upon the sector; which must be set off from the line W K, representing the lower side of the keel, and may be produced both ways, as sar as shall be needful. We must in the next place form all the ribband lines, which are the dotted ones in the draught; beginning with the fourth ribband. But it will be more expeditious, first to draw all the diagonals in the body plane.

Let AB be the whole breadth, on the middle of which erect the perpendicular KO; fo shall AK, or KB, be the half breadth. Upon the line KO, fet up the several heighths of the breadth lines, taken from the sheer plane, and draw lines parallel to the base, as directed in the preceding fections; and likewife fet off the half breadths, corresponding to each, taken from the floor plane. We may also set off the heighth and half breadth of the wing transom; all which may be done without the fector, but we must have recourse to it for the dead rising. This is in No III. in the after body, and must be set off upon the line K O, from the lower heighth of breadth to i. Thro' i draw the line r is, parallel to the base, and set off the $\frac{1}{2}$ breadth of the sloor from i to r, and from i to s: It is upon No VII. on the fector. Then taking ri, fet it up from i upon the line KO, to which point draw the dotted diagonal marked 1ª R4. This regulates all the other diagonals: For if one line be drawn from the point of its intersection, with the middle line, to the half breadth of the wing transom; and another from the point r, its interfection with the rifing line, to the point @ at the lower heighth of breadth:

breadth; each of these may be divided into sour equal parts by the dotted

diagonals 24 R4 34 R4 44 R4.

Note. The lines from the ends of the first diagonal to the lower heighth of breadth, and to the wing transom, were drawn only with a black lead pencil, and wiped out after the diagonals were drawn. The diagonals being thus drawn, we may form the midship frame, for which purpose we must find a point in each diagonal, thro' which the curve of the timber must pass. These points we have from the sector; which must be set off from the interfections of the diagonals with the line KO. That in the first diagonal is in No I. The point in the second diagonal, is in No VI. The point in the third diagonal, is in No V. And the point in the fourth diagonal, is betwixt No I, and II. This last must be doubled, because the sector will not contain the whole length. The midship frame being formed, we must in the next place form the after and foremoth timber; which the fector does, by giving the distance on every diagonal betwixt these timbers, and the midship frame now formed: So that we shall have a point in each diagonal, thro which the curve of the timber must pass. To find the point in the first diagonal for the after timber; extend from \(\mathre{O} \) 1 R in N\(^6\) V, to the corresponding point on the other leg. Set off this distance from non the first diagonal: Do the same upon the fecond, third and fourth diagonals. The point on the fecond diagonal, is in No IV. That on the third, in No VI. And that on the fourth in No VII. The curve must pass thro' these points, and likewise thro' the point for the half breadth, which was before fet off from the sheer and floor planes; by which means we have determined the form of the after timber; and the foremost timber is to be formed by the same method. These two timbers being formed, we may find points in the diagonals for all the intermediate timbers. Thus, to find the point for timber 3 in the first diagonal; extend from the point 3 in the inner part of the line No V, to its corresponding point on the other leg. Set off this in the first diagonal from the after timber, already formed; which will give the point thro' which timber 3 must pass; and to find the point in the second diagonal, we must extend from 3 in the inner part of the line No IV: and fet off this diffance in the fecond diagonal from the after timber. The fame method must be used to find the points in the third and fourth diagonals. In like manner we may find a point in each diagonal for the timbers 5 and 7, which will be sufficient for the after body: And the same process must be used to find points in each diagonal for the timbers in the fore body.

Having now found the points, before we form the timbers, it may be proper, by them, to form the ribbands: For now we may take the diffance

CHAP. II.

of each point in the diagonal, from its intersection with the middle line KO, and transfer it to the floor plane upon the perpendiculars that reprefent the planes of the timbers, as directed in Sect. 2. In order to limit the ends of the ribband lines in the floor plane; we must set off half the thickness of the post, on one side of the middle line K O, and half the thickness of the stem on the other side of it, in the body plane; first deducting the depth of the rabbet out of it. We must likewise determine the inner part of the rabbet on the stem, and upon the post in the sheer plane. In the stem, it is generally in the middle betwixt the lines that represent the outside of the rabbet. It may be also so on the post, from the wing to the lower transom; and from thence the line may be continued fair to interfect the line that represents the after side of the rabbet, at the upper edge of the keel; for there the rabbet is cut square into the post.

Now, it is obvious that when the plane of any diagonal ribband is in its proper place and position, the line W K will be in the sheer plane, parallel to the upper fide of the keel; and its heighth will be the same with that of the point where the diagonal interfects the middle line in the body plane, But by reason of its inclination, and of the half thickness of the ftem and post; the heighth of the plane of the ribband upon the post and stem, will be in the point where the diagonal intersects the line that represents the rabbet in the body plane. This then must be transferred from the body to the sheer plane, and set up from the upper edge of the keel upon a perpendicular that will interfect the line that represents the infide of the rabbet at that heighth. This perpendicular may be produced into the floor plane; and if that part of the diagonal intercepted betwixt the middle line, and the line that represents the infide of the rabbet, in the body plane, be fet off upon the perpendicular, it will give the proper point for the end of the ribband line, as may be feen in the plate; where all the ribbands are dotted lines, and they are marked 1ª DR, 2 DR, &c.

Note. The scale in the plate is so small, that we have taken the out-

fide of the rabbet to limit the end of the ribband.

The ribbands being thus formed, we may from them form all the tim-

bers below the breadth.

The next thing to be done, is to form the top timbers. We have the heighth and half breadth of each from the sheer and floor planes; and the timbers below the breadth, are carried up by a fweep, which forms the lower part of the top timber. The center of this sweep is in the upper heighth of the breadth line of the timber, and may be taken from the fector: It is on No III. after body. The midfhip top timber has generally a hollow, which is left intirely to the artist; for some, especially fmall

fmall ships, have none. The general practice is to make a mould for this hollow, either by a sweep, or some other contrivance, and produce it considerably above the heighth of the top timber in a strait line, or very near one. The midship timber is formed by this mould, and so placed, that it breaks in fair with the back of the upper breadth sweep. All the other timbers are likewise formed by the same mould; observing to place it so that the strait part of it may be parallel to the strait part of the midship timber; and moved up or down in that direction till it just touches the back of the upper breadth sweep. Some begin at the after timber after the mould is made for the midship one, because they think it easier keeping the strait part of the mould parallel to this; than to the midship timber; and by this means the top side is kept from winding.

Others again, make a mark upon the mould where the breadth line of the midthip timber croffes it; and with the same mould they form the atter timber. This will occasion the mark that was made on the mould, when in midships, to fall below the breadth line of the after timber; and so another mark is made at the heighth of the breadth of the after timber. The next thing to be done, is to lay the strait part of the mould obliquely across the breadth lines of the top timbers, in such a manner that it may interfect the breadth line of the midship timber at one of these marks, and the breadth line of the after timber at the other mark. Then the feveral interfections of the breadth lines of the timbers, are marked upon the mould, The mould being thus marked, must be so placed in forming each timber, that the proper mark may be applied to its proper breadth; and the mould be turned about so as just to touch the upper breadth sweep. Any of these methods may make a fair side; but it may be easily proved by forming another half breadth line. The same of the sa

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CHAP. III. SECT. I.

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Of the CANT TIMBERS.

Itherto we have confidered the timbers, as having their planes perpendicular both to the sheer and floor planes. These are called iquare timbers; and when they are all formed, we may from them form as many ribband and water lines as shall be necessary to form the cant timbers. Their planes are inclined to the sheer, but perpendicular to the floor planes. The reason of canting these timbers, is that they may nearly be equally spaced at the breadth ribband: For if the post has a considerable rake, and the timbers all square, there will be a great space at the breadth ribband, betwirt timber 8 and the wing transom: Besides the timber may be so canted, that it may be square to some of the ribbands; whereas, if they were perpendicular to the sheer plane, they would interfect the ribband lines so as to form very oblique angles; which would occasion a very great bevelling. Another advantage that attends canting the timbers, is that they will not require such compass timber.

It is usual to begin the cant timbers from the aftermost short timber; and space them near equally on the breadth line, to the wing transom: And in order to space them upon the keel, the cant of the sashion piece must be determined. Now if we suppose the plane of the sashion piece to intersect the sheer and short planes in the point F, it must intersect the short plane in the line F P, because the point P is supposed to be the end of the wing transom. So the angle of F P will be its inclination to the sheer plane. It will intersect the sheer plane in a perpendicular erected from the point F; and if the space betwixt the point F, and the foremost cant timber upon the keel, be divided into the same number of equal parts, that the space betwixt the same timber, and the wing transom upon the breadth line, is divided into; this will determine the cant of all the timbers only by drawing lines from all points in the line W K, to the corresponding points in the breadth line, in the same manner as the line F P, determines the cant of the sashion piece.

It would be needless to draw all these lines in the plate; the only intent of drawing them being to shew how to form the timbers by them: And as one method serves for all the cant timbers, which are supposed perpen-

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dicular to the floor plane; it will be fufficient to shew the formation of

the fashion piece.

Before any of the cant timbers can be formed, there must be a fuslicient number of water lines, or diagonal and horizontal ribband lines formed from the square timbers; and when these are absolutely determined, we may, with certainty, form all the cant timbers, either by water, or ribband lines.

If we make use of the diagonal ribbands, which are distinguished by the dotted curves in the floor plane, we must form an horizontal ribband corresponding to each. We have only laid down one of these horizontals in the plate, viz. that corresponding to the third diagonal: It is marked 3⁴ H R. To form this ribband, fix one soot of the compasses in the point where the third diagonal intersects the midship frame in the body plane; and extend the other soot to touch the middle line KO; so that if a line were drawn from one soot of the compasses to the other, it would be perpendicular to the line KO: This distance set off from the line WK, upon the perpendicular that represents \bigoplus in the floor plane, will give the point thro' which the curve must pass at that place. The same method must be used for finding the points on all the other timbers.

Now, tho' the diagonal and horizontal ribbands feem to be quite different curves in the plate, they will make but one line upon the timbers; for the one interfects them in a direction perpendicular to the sheer plane, and the other is fo inclined as to interfect the timbers in the very same points. The horizontal one is too short upon the plate, but the true length of it might eafily be had by transferring to the sheer plane, the several heighths at which the diagonal interfects the timbers in the body plane. By there we might form a heighth of breadth line to correspond to this horizontal ribband, which is only a half breadth line; and the length of this heighth of breadth line may be taken by a penning batten, and all the timbers marked upon it. Now when the batten is applied to a strait line, and all the timbers transferred to this line from the batten, we may erect perpendiculars at each, and fet off the fame half breadths as before; by which means we may have the true length of the horizontal ribband: But as this will be of no manner of fervice, we shall omit forming it. We only mention it, because several imagine these two curves to be as different on the furface of the ship as they are upon the draught. The horizontal ribband corresponding to the first diagonal one, is formed to timber 7, and marked 1th HR; but the horizontals for the fecond and fourth diagonals were formed by a black-lead pencil, and only the point in which they interfect the line F P, is in the plate; which is fullicient for our purpole.

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There are likewise five water lines formed, four of which are reprefented by level lines in the body plane; and by lines parallel to the keel in the sheer plane: Three of them represent the planes of the transoms in the sheer plane, viz. Dk, IA, 2d: But the plane of the third transom is perpendicular to the post, The lower water line is drawn parallel to the keel from the stem to the post, and produced into the body plane, as in the plate, where it is marked M N: The plane of the third transom interfects the timbers at different heighths, which are transferred from the

theer to the body plane, where it forms a curve.

The water lines being now drawn in the sheer and body plane; our next business is to form them in the floor plane, where they will be curves. The points thro' which the curve of the lower water line is to pass, are had by transferring the feveral portions of the level line, intercepted betwixt the line KO, and the curve of each timber, from the body plane to the corresponding perpendiculars in the floor plane, where it is marked Wat'L. It must be observed that the line KO, in the body plane, represents the several perpendiculars that are drawn in the sheer plane to represent the planes of the timbers: For the spaces in the body plane, contained betwixt the line K O, and the curves of each timber, are fo many different planes; and when in their proper places, they will be parallel to one another, if perpendicular to the sheer and floor planes. Thus the plane contained betwixt the line KO, and the curve of timber (1), is (when in its proper place) supposed to be erected perpendicular to the theer plane, in the line which represents the plane of ; and the like may be faid of all the rest. The planes of the cant timbers will not be parallel to one another, because they are differently inclined to the sheer plane; but as they are perpendicular to the floor plane, they will intertect the sheer plane in a line perpendicular to the keel: So the plane of the fashion piece intersects the sheer plane in the dotted perpendicular erected from the point F, which is the same with the line K O, in the body plane. We thought it necessary to take notice of this, because some who are learning to draw, mistake the line KO; for they imagine it only represents the post or stem.

Another error which they frequently fall into, is about forming the water lines when their planes are not parallel to the keel. They imagine that the half breadths must be set off from the line WK, which reprefents the lower edge of the keel; whereas it is indifferent what strait line they are fet off from, fo the timbers be exactly spaced, and perpendiculars drawn to reprefent their planes. Now when the water lines are supposed parallel to the keel, all the timbers are properly spaced, and the per-

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pendiculars ready drawn to the line W K; which is the reason it is used in fuch cases: Tho' when the plane is in its true place, the line WK. will be in the line M N. But the cafe will be quite different when the water lines are not parallel to the keel; for then their planes will interfect the sheer plane in a strait line, forming oblique angles with the planes of the timbers; this is the case in the plane of the third transform. The distances betwixt the timbers will be more in this line than in the line WK; fo the half breadths cannot be fet off from the line WK, upon the perpendiculars that represent the planes of the timbers unless they be properly spaced at the same distance they are upon the line that represents the plane of the third transom in the sheer plane; upon which account we have made use of that line to set off the half breadths from, and drawn the dotted perpendiculars at the points where it interfects the planes of the timbers 8, 7, and at the point where it interfects the lower heighth of breadth line. The heighths of the points of intersection are transferred from the sheer to the body plane; and the half breadths at these heighths, transferred from the body plane to the dotted perpendiculars before drawn: The half breadth to be fet off upon the perpendicular where it interfects the lower heighth of breadth line, is had from the floor plane, and the dotted perpendicular a a, will shew the place where the half breadth must be taken: This perpendicular, if produced, will interfect the plane of the third transom in the lower heighth of breadth.

Having now formed four diagonal ribbands with their corresponding horizontals, and also two water lines; we may by these, form the fashion piece, either upon the body plane or sheer plane: But as the plane of the fashion piece is parallel to neither of these, it will require two ope-

rations.

Now the line F P, will interfect all the ribband and water lines; but because the diagonal ribbands are not in their proper position, the line F P will not interfect them in the point where the plane of the fathion piece interfects them. The first thing then to be done, is to find the true place of the fashion piece on each diagonal ribband: And first, to find its place upon the fourth diagonal ribband, from the point t, where the fourth horizontal ribband interfects the line FP, let fall a perpendicular to the point s, and produce it to interfect the diagonal ribband in r; fo shall r be the true place of the fathion piece upon that ribband; that part of the perpendicular betwixt t and s is not drawn in the plate to avoid the confufion of too many lines. The reason of this will be very evident, if we suppose the whole plane of the ribband to be turned round upon the axis WK; for then the point r will always be right over some point of the X 2

perpendicular rts; and when the ribband is in its proper inclination, a perpendicular from r will fall into the point t, and the plane of the fashion piece will intersect the floor plane in the line t F, and the plane of the diagonal ribband in a strait line drawn from r to F: For it must be observed that when the ribband is in its proper place, the line W K will be in the sheer plane, in a line parallel to the keel; the heighth of which may be had from the body plane. In this case it will be the distance betwikt K and r, but it will be needless to draw this line in the plate.

Having now found the place of the fashion piece on the fourth diagonal ribband, we must by the same method find its place on the other diagonals, as in the plate, where lines perpendicular to W K, are drawn to the points o, o, o, in the diagonal ribbands, from the points where the line

F P interfects the corresponding horizontal ribbands.

These points being now found, we may take the nearest distance of each point to the line W K, and set off those distances on the proper diagonals in the body plane. Thus, for the fourth ribband, place one foot of the compasses in the point r, and the other in the point s in the floor plane; and set off that distance from r to S, on the fourth diagonal in the body plane: Do the same by all the rest of the diagonals; and a curve intersecting the diagonals in these points would be the projection of the sufficient piece in the body plane, but we have not drawn this in the plate; for as the plane of the sufficient piece is not parallel to that of the body plane, its projection will be less than the original: However this may be found by Prob, 6, Cbap, 1, Part 2, by the following method.

1/f. Draw a perpendicular to the line KO, in the body plane, to pass

thro' the point S to F.

2d. Take the distance from r to F, in the floor plane, and set it off from r to F, in the body plane. In like manner draw perpendiculars to the line K O, in the body plane, thro' the points before found on the diagonals, as in the plate, where only that part of the perpendicular is drawn which lies without the diagonal; and take the several distances betwixt the points o and F, in the floor plane, and set them off from the intersections of their corresponding diagonals, with the line K O, to the points o, o, in the body plane: So we have the points o, o, F, thro' which the curve must pass.

3d. To find the point P in the body plane, thro' which the curve must pass. Transfer the point P in the floor plane, to the point P, in the sheer plane, by a perpendicular to the line W K, to intersect the heighth of breadth line in the point P; and set off this heighth upon the line W O, in the body plane, which will be a little above W, the heighth of

the wing transom: Draw a perpendicular at this point, to the line KO; take the line FP, in the floor plane, and set it off upon this perpendicular, from the line KO, to the point P: So shall the curve VP 00, he

the form of the fashion piece.

There points may all be found without the diagonal ribbands, by half breadth lines and water lines, formed on the floor plane, as for infrance: To find the point F; place one foot of the compasses in t, the point where the horizontal ribband interfects the plane of the fathion piece, and the other in s; ts being perpendicular to WK: With that extent, move the compasses with one point in the line KO, and the other point perpendicular to it, till it interfect the fourth diagonal, in the point S; thro' which draw the perpendicular t F. Then take the distance from t to F, in the the floor plane, which fet off from t to F, in the body plane; fo shall F be the point required, as before: In like manner the points o, o, may be found: But this, as well as the other method, requires two operations; whereas, if feveral water lines were formed, with their planes parallel to the keel, we might find the points by one operation. Thus, suppose it was required to find a point in the level line, that represents the plane of the water line formed in the floor plane, which is marked Wat L. Fix one foot of the compasses in the point f, where the line F P interiects the water line in the floor plane, and the other foot in the point F. Set off this upon the level line in the body plane, from the line KO to f, which will be the point required. All the other cant timbers, both in the fore and after body, are formed after the same manner as the fashion piece. We have formed but one more in the plate, which is abaft the fashion piece, to affift us in forming the transoms.

S E C T. II.

Of the TRANSOMS.

THE transoms are fastened to the stern post, in the same manner that the sloor timbers are to the keel; and as the sloor timbers have a rising, so likewise have the transoms, which is called the slight; and besides this slight, the wing transom has a round ast, and a round up, both which are arbitrary: The deck transom has a round up, the same with that of the beams: But in forming the transoms, there is no regard

had to the round up; for that may be done by the beam mould, after the

transom is properly hewed the moulding way.

In forming the transoms, the first thing to be done, is to assign each its proper place upon the post, and then to determine the position of their planes with respect to the floor plane; for their planes are always perpendicular to the sheer plane. In the plate there are five transforms: Their upper sides upon the post are in the points W, D⁶, 1^a, 2^a, and 3^a: The planes of the wing, deck, first and second transoms, are supposed parallel to the floor plane, and represented in the sheer plane by lines drawn parallel to the keel from the post, till they intersect the lower heighth of breadth line; and the plane of the third is represented by a line perpendicular to the post, as in the plate, So it will not be parallel to the floor plane.

The heighth and position of the transoms being determined, we have no more to do, but to form water lines for each. That for the third we have already formed: The rest being supposed parallel to the sloor plane, may be formed in the same manner as the water line there laid down: The only difficulty will be to find a sufficient number of points to determine their forms; because in the deck and first transoms, their planes intersect the breadth; so that we could only have a point in timber 8, if the sufficient planes, there are some they are formed, we may have likewise a point in each of their planes, thro' which the curves of the water lines shall pass.

We shall begin with the wing transom. First determine the round aft which suppose the line W T, in the floor plane: Take its heighth from the sheer plane, and set it up in the body plane from K to W, and draw the line WT: Then take this line WT, and fet it off on the floor plane, on the line F P, which will reach to the point n. A curve drawn thro' the point n, to break in fair with the breadth line, as in the plate, will interfect the line WT in T; fo shall WTn, be the aft side of the wing transom. Next for the deck transom, draw a level line in the body plane at the point D' to timber 8. Set off this distance upon timber 8, in the floor plane, from the line W K; which will give us a point thro' which the curve must pass: Then take the distance in the level line, betwixt the line KO, and the curve of the fashion piece; which set off from the point F, upon the line FP, in the floor plane; and this will give another point thro' which the curve must pass: Again, take the distance in the fame level line, betwixt the line KO, and the curve of the timber abaft the fashion piece; which set off from the point G upon the line Gg, in the floor plane; and we shall have a third point thro' which the curve

must pass. Lastly, let fall a perpendicular to the line W K, from the point D^k upon the post, and produce it into the sloor plane, upon which set off half the thickness of the post, allowing for the rabbet, which will limit the end of the water line that forms the deck transfom. After the same manner are the first and second transfoms formed, by drawing level lines in the body plane, at their heighths upon the line K O.

Now some are apt to mistake these level lines for the lengths of the transoms: The reason, as was before observed, is because they inagine the line K O to be the stern post; whereas it is the perpendicular in which the plane of the sashion piece intersects the sheer plane; and so these lines

are drawn upon the plane of the fashion piece,

All that now remains, is to determine the length of each transom; and this is done by the line F P, in the floor plane, which interfects the wing, deck, first and second transoms, to their proper lengths. But before we can find the length of the third, the plane of the fathion piece must be projected upon the sheer plane: Thus, take the nearest distance betwixt any perpendicular in the floor plane, and the point where the line F P interfects the water line; and fet that off from the fame perpendicular upon the line that represents the same water line in the sheer plane. Now the curve P F will be found to be the projection of the aft fide of the fashion piece upon the sheer plane: For the distance betwixt the perpendicular of timber 8, and the point f, where the line F P interfects the lower water line in the floor plane, is equal to the distance betwixt the fame perpendicular and the curve PF, taken in the line MN. The distance betwixt the perpendicular of timber 8, and the point where the line F P intersects the second water line in the floor plane, is equal to the distance betwixt the same perpendicular and the curve P F, taken in the line that reprefents the fecond transom in the sheer plane. And by the fame method, we find points in the lines that represent the deck and first transforms. The point P is transferred from the half breadth line in the floor plane plane, to the heighth of breadth line in the sheer plane. The curve being thus drawn, will interfect the line that represents the plane of the third transom, in the point z: From which point draw the perpendicular z F, to the curve of the dotted water line; fo shall 34 z, F, be the true form of the third transom; and a line drawn from F to P, will be the plane of the fashion piece. It must be observed that the ends of the transoms are let into the fashion piece; for which there must be a proper allowance left without the lengths found by the line F.P. We have in the plate only laid down the half of each transom. Those who incline

incline to lay down the whole transoms, may easily transfer the halfs al-

ready described to the other side of the line WF.

Having now formed all the timbers, both square and cant, in the after body; we shall proceed to the fore body. The cant timbers are laid down in the same manner as those in the after body, by the diagonal and horizontal ribbands; where the dotted line K T represents the plane of the knuckle timber, canted upon the floor plane; from whence it is transferred to the body plane, and represented by the dotted curve betwixt timber H and G.

The hawfe pieces are feldom laid down in the loft; it being the general practice to make moulds for them after the other timbers are put up, and the harpins are brought about; but they may be formed in the fol-

lowing manner.

Let P H represent the plane of the hawse piece on the floor plane, which may be produced to K T, the plane of the knuckle timber: In the plate let H be supposed the heel of the hawse piece; from which point erect the dotted perpendicular b / into the sheer plane, and draw the dotted level lines a l, c l, in the body plane; by which, form the water lines a l, c l, in the floor plane, and draw the dotted lines a l, c l. perpendicular to the line bl, in the sheer plane; which will represent the planes of the water lines. Draw also the dotted perpendicular b l, to the point where the line b l interfects the upper heighth of breadth line. Upon the line cl in the sheer plane, set off the distance HP, taken from the floor plane, P being the point where the plane of the hawse piece interfects the water line cl. Then take the distance from H, to the point where the line H P interfects the M & Bth line, and fet it off upon the line b l to t; or, rather find the point upon the lower heighth of breadth line, where the hawfe piece comes to; from which draw a perpendicular to the line b l, and upon this fet off the distance, as before: Then take the distance from H to the point where the line H P interfests the water line a l in the floor plane, and fet it off upon the line a l, in the theer plane to p. Lastly, to find the heighth of the heel, because we have not formed a timber at the point H, produce the line H P, to interfect the plane of the knuckle timber K T, in the floor plane, at the point r: Take r K, with a pair of compasses, and placing one foot in the curve of the knuckle timber in the body plane; fo as that the other foot touch the line K O, or rather set off r K from the line K O to k upon the base line; at which point erect a perpendicular to intersect the curve of the knuckle timber in the point k; fo shall k k be the heighth of the heel, if the plane of the hawfe be produced to interfect the plane of knuckle

knuckle timber: But in the plate the heel of the plane of the hawse piece is supposed to be at the point H: Therefore a perpendicular must be erected from the point r, into the sheer plane, upon which setting up the heighth kk, we shall have the point k. We may by the same method find a point in the plane of timber H, in the sheer plane; through which the curve of the hawse piece must pass; and if produced to k, it will intersect the perpedicular k, in the point k; which is the heighth of the heel.

Tho' the hawse pieces are seldom laid down, yet by forming them on the sheer plane, we shall thereby discover if there be any faults in the half breadth lines or water lines: For if the timbers that are formed by these lines are not fair, some of those lines from which they are formed must certainly be the occasion of it; which therefore must be rectified before we can find the true form of the harpins; which is the next thing to be done.

S E C T. III.

To form the Harpins and Rails of the Head.

As the harpins are level'd across, they will be formed by the section of a plane perpendicular to the sheer plane: But there is no necessity for these sections to be parallel to the keel. In the plate we have drawn only a strait line to represent the plane of the harpin above the wale. It is drawn from the stem to timber E, and marked harpin. Now in order to form the curve of this harpin, it would be proper to form timber F, in the body plane: Also to draw perpendiculars to the several points where the plane of the harpin intersects the planes of the timbers E, F, G and H, in the sheer plane; and upon these to fet off the half breadths corresponding to each, taken from the body plane. This would give us the points thro' which the curve must pass, which would be a water line. But as this is performed exactly in the same manner as the water line that represents the third transom, we judge it unnecessary to form it in the plate.

The rails of the head are projected on the sheer plane, according to their true hangings; and in order to find their true lengths, draw the dotted line S T, parallel to the keel at the heighth of the rails, upon the head. We must then determine the station of the cat-head upon the Y

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floor plane; and likewise the thickness of the head at the rail: and let fall a perpendicular from the point T, where the line ST interfects the cat-head in the sheer plane, to the point T in the floor plane; and likewife a perpendicular from S in the sheer, to S in the floor plane; and draw the line TS: sS in the floor plane being half the thickness of the head of the figure at the rail; fo shall T S, in the floor plane, be the true length of the rail. Let the line T S, in the sheer plane, be divided into any number of equal parts: Suppose into the points x, y, z; from which points draw perpendiculars to the line TS, to be limited by the rail. Divide the line TS, in the floor plane, into the fame number of equal parts, in the points x, y, z. Draw perpendiculars to these points, and make them

equal to the corresponding ones in the sheer plane; so we shall have the points thro' which the curve of the rail must pass.

We have now shewn different ways of forming all the timbers: where it must be observed that we have always supposed every timber to be one intire piece of wood from the keel to the top of the fide; whereas in reality, they are in feveral different pieces; the head of the lower piece being cut square to join to the heel of the next above it: And in order to support these joinings, another sett of pieces are cut, and joined together in such a manner, that if both the setts were fastened together, the joinings in one fett, would be nearly against the middle of the pieces in the other fett. In this manner are all the frames fastened and erected, as if each was one piece of wood. The pieces laid across the keel, to which they are fastened, are called floor timbers: The other pieces are called futtocks, except that which goes to the top of the fide, which is called a top timber. Hence it is plain that the mould which ferves for the floor timber, will ferve for the lower part of the corresponding futtock. The mould for the upper part of the first futtock, will be the same with that for the lower part of the fecond; and the mould for the lower part of the top timber will be the same with that of the upper part of the corresponding suttock. It is of great importance in building, to give proper fearph to the timbers; for which we refer our readers to the table of icantlings at the end of this part.

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CHAP. IV. SECT. I.

Of Bevelling the TIMBERS.

In the preceding chapters we have confidered the timbers as plain furfaces, without any regard to their thickness or breadth; whereas every timber confists of two planes, and the space contained betwixt them is the breadth of the timber. We have already shewn how to find the form of one of these planes, which is called the moulding side of the timber. The form of the other side will be different from the moulding side, except in midships. Now if the timber be properly hewed from the moulded side, we shall have the form of the other side: This is what is called bevelling the timbers; a term so well known that it needs no explication. We shall only remark that the bevelling is the angle made by the meeting of two planes limiting a solid; and as this angle cannot be measured by scale and compasses, without cutting the folid by another plane perpendicular to both; it is done by an instrument called a bevel. When the angle is a right one, the timber is said to be square, and is

measured by an instrument of that name.

In order to hew any piece of timber to its proper bevel, it will be very proper first to make one fide fair, and out of winding; a term used to fignify that the fide of the timber should be a plane. Now if this side be uppermost, and placed horizontally, or upon a level; it is plain if the timber is to be hewed square, it may be done by a plummet and line; but if the timber is not hewed fquare, the line will not touch both the upper and lower edge of the piece; or if a fquare be applied to it, there will be wood wanting either at the upper or lower fide. This is called within or without a fquare. When the wood is deficient at the under fide, it is called under bevelling; and when it is deficient in the upper fide, it is called standing bevelling; and this deficiency will be more or less, according to the depth of the piece; fo that before the proper bevellings of the timbers are found, it will be fometimes very convenient to affign the breadth of the timber; nay in most cases it will be absolutely necessary, especially afore and abast; tho' the breadth of two timbers, or the timber and room, which, as was before observed, includes the two timbers, and the space betwixt them, may be taken without any sensible error; as far as the fquare body goes. For as one line reprefents the Y 2 moulding

moulding fide of two timbers, the forefide of the one being supposed to unite with the aft side of the other; the two may be considered as one

intire piece of timber.

Notwithstanding it is usual in draughts to lay down only every third or fourth timber; yet in the loft it will be necessary to lay down all the timbers: But as our plate will not admit of this, let us suppose the line a a e, betwixt the timbers 5 and 7, in the floor plane, to represent the moulding fide of two timbers; and the lines m n and r s, the moulding fides of other two timbers. Draw the lines bc and kl, the one in the middle betwixt e a and mn, and the other in the middle betwixt e a and rs: fo shall the distance betwixt the lines bc and kl, be the breadth of two timbers, together with the space betwixt them: The portion b k of the ribband may be taken for a strait line, and then the angle that is made by the line b c and b k, or the angle made by the line k l and k b, will be the bevelling according to the fide on which the timber is moulded; the one being as much standing as the other is under bevelling. In order to find how much this is from a square, draw the lines 1, 2, 3, 4, perpendicular to the lines b c and k l; and the portions of the line e a intercepted betwixt the ribbands, and these perpendiculars will be what the timber is either within or without a square; so 4 e will be that at the fourth ribband: And because the line ea represents the moulding side of both timbers, the timber before it will be standing, and the timber abast it, under bevelling.

It is very necessary to observe that the planes of the ribbands should be perpendicular to the planes of the timbers, which is the case in all the iquare timbers; But the planes of the cant timbers are inclined to the planes of the ribbands; therefore their bevelling cannot be had by the ribband lines in the same manner as these of the square, because when the stock of the bevel is laid upon the moulding side of the timber, the

tongue of the bevel will be out of the plane of the ribband.

Another thing to be carefully observed, is in what direction the stock of the bevel is to be laid upon the moulding side of the timber. This is found in the body plane: If we bevel by ribband lines, the diagonals will give the line of direction; but if the bevellings are taken by water lines, the level lines in the body plane will give the direction m which the slock of the bevel is to be laid upon the timber: When these lines in the body plane are very oblique to the curves of the timbers, if the bevel is not kept exactly in the same direction, it will occasion a very great error; and only the very sharp edge of the tongue will touch the timber. For this reason, the best way to take the bevellings will be, so

that both stock and tongue may be square to the timber; but this will alter the bevelling, and bring it likewise nearer to a square, which is another advantage we shall gain by altering the direction of the stock; and

the true bevelling may be found by the following method.

Let the distance betwixt timber 7 and timber 8, in the sloor plane, he supposed the breadth of a timber; then the perpendicular at 8 will represent the plane of the aft side; and the perpendicular at 7, the plane of the fore side of the timber in the sloor plane: The curve of timber 8 in the body plane, will be the form of the aft side; and the curve of timber 7, the form of the fore side of the timber: So that the nearest distance betwixt these two curves, will certainly be what the bevelling differs from a square; for if the timber were square, the same curve would

represent both fides of it.

Now if it were required to find the bevelling of this timber by the water line, (Wat'L in the floor plane) it is evident it will be the angle 8 i u, if the moulded fide be aft; and x u will be what it is without a fquare. This will be in the direction of the level line in the body plane, where it is x u; but x v being the nearest distance betwixt the curves taken from the point x, that must be set off from x to v, on the sloor plane; fo shall 8 i v, be the true bevelling, when the bevel is set square to the timber at the point v, where the firmark must be placed. But if the moulded fide be forward, the angle x u i, will be the bevelling, and x uwhat it is within a square; the same as that which was without a square when the moulding fide was aft. Here uz is the nearest distance betwixt the curves, taken from the point u; and when this is fet off from x to z, in the floor plane, the angle $x \approx i$, will be the true bevelling at the point z, in the body plane, where the firmark must be placed. This method will be very useful for the cant timbers, when they are bevelled by water lines, and may be done by the workman, if the bevelling is given in the direction of the plane of the water line, by observing the following directions, which are in effect the same with these now prescribed.

1st. Apply a square to the bevelling board, at the point where the line that determines the bevelling of the timber interfects the side of the board; and the distance of the other end of the line from the square upon the opposite side of the board, will be what it is within or without a square,

2d. If the timber has an under bevelling, take the quantity of it, found by the square, with a pair of compasses, and set it off upon the line of direction, on the timber, from the point where the line intersects the moulded side, which is rased in upon the timber: One foot of the compasses being fixed in this point, let the other foot rest in a point in the

line of direction: From this last point take the nearest distance to the outside of the timber, and mark the sirmark at that place.

3d. Take the nearest distance sound on the timber, and set it off from the square upon the same side of the bevelling board, from which the distance set off upon the line of direction, was taken; and mark that place upon the board. A line drawn from that point, to the point where the square was applied on the opposite side of the board, will give the true bevelling, to be taken square to the timber, observing to set it to the proper firmark.

If the timber has a standing bevelling, we must apply a strait edged batten to the line of direction upon the timber, upon which we must set off what the bevelling is, without a square; and proceed in the same

manner as before.

Note. If the bevelling board is not exactly the breadth of the timber, the bevelling must be transferred from the board to two parallel lines,

the breadth of the timber being the distance betwixt them.

But if it be required to bevel the cant timbers by the diagonal ribbands, the angle $F \circ b$, will be that which the fashion piece will then make with the third ribband: For δ being the point where the plane of the fashion piece intersects the third ribband; a line drawn from δ to F, will be that in which the plane of the timber intersects the plane of the ribband: But then as these planes are not perpendicular to one another, the angle $F \circ \delta$ will not be the true bevelling, unless the bevel be so applied that the tongue may be in the direction of the ribband, and then the stock cannot lay slat upon the side of the timber: For which reason this method will not do for practice; for the surest way to take any bevelling, is when both the stock and the tongue of the bevel are square to the timber.

In order then to find the true bevelling upon a fquare, the direction in which the ribband interfects the timber must be given, as well as the angle $F \circ b$; and likewise the breadth of the timber: Now if these three be given, the angle upon the square may with certainty be found by the following method.

Let the diffance betwixt the parallel lines A B and E F, be the breadth of the timber; B a the direction of the ribband; and a b what the bevelling is without a square. (See the Fig. under the Scale, Plate 7.)

Now, that we may the easier conceive how this bevelling may be found, let us suppose the timber to be quite strait, and first trimmed square. Then, because ab is what it is without a square, it is plain there must be so much lined off the aft side of the timber, and when this is

hewed off; the line a B will be the breadth of the outfide of the timber; and if B D be made equal to B a, and D d equal to a b, and the angle at D a right one; then it is plain the angle A B d, will be the beveling, if the tongue of the bevel can be kept in the direction of the line B a: But when the flock of the bevel is laid flat on the fide of the timber, the tongue will naturally be perpendicular to the plane of the timber, which will be in the line B F; and if F f be made equal and parallel to D d; then will the angle A B f; be the true bevelling upon a fquare: But if the outfide of the timber is a curve, the flock must be placed at the point t, and t B made equal to F a; and the tongue

will come to the point a.

To apply this to find the bevelling of the fashion piece at the third ribband, the angle $F \circ b$, is given in the floor plane; and to find the direction in which the plane of the ribband intersects the plane of the timber; we must find the angle, or the inclination of these two planes to one another: For tho' the plane of the timber is perpendicular to the plane of the water lines; it will not be so to the planes of the ribbands: And what was afferted in Prob. 7. in regard to the angle at the top and bottom of the chest, viz. that they would be equal, must be understood so, as that both the stock and tongue of the bevel be kept parallel to the back side of the chest; which might be easily done, when the partition is properly bevelled to the backside of the chest: But here the case is different, therefore we must find it by the following method.

is in which the point o draw the line e o perpendicular to F o; the line in which the plane of the timber interfects the plane of the ribband on

the floor plane.

2d. Thro' the point o in the body plane, draw the line e o perpendicular to K O, o being the point where the ribband interfects the fashion piece.

3d. Take the line e from the floor plane, and fet it off from the point 3, where the third diagonal interfects the line K O in the body plane to the point e in the line e.

And lastly draw the line 3 e; so shall O 3 e, be the angle the plane of

the ribband makes with the plane of the fashion piece.

Now let the distance betwixt the line K O and pf, be supposed the breadth of the timber; then will 3 q be the breadth of it upon the plane of the ribband; which set off upon the floor plane from o to m, and draw the line b m B, parallel to F o; so b m will be what the bevelling is without a square, when taken in the direction of the ribband; and the angle F o b, the bevelling. In order to find the bevelling upon a square,

lct

fet off the breadth of the timber from o to l, and make l 2 equal to mb; fo shall F o 2, be the true bevelling on a square. The line 2 o is omitted in the plate, because it would be too near to the ribband line b o.

We have now shewn how to bevel the cant timbers either by water or ribband lines; and much after the same method, may the fashion piece of a square tuck be bevelled. It both rakes and cants, and of consequence will be inclined to the planes of the water lines, if they are parallel to

the keel; as that of the long-boat. (See Plate 5.)

Now, in a ship the planes of the water lines may be represented by lines perpendicular to the plane of the sashion piece, in the sheer plane; and formed in the same manner as that of the third transom in the ship (Plate 7.): And then we shall have the true bevelling in the same manner as that of the cant timbers. It may likewise be done by water lines parallel to the keel, as in the long-boat; where we cannot form all the necessary water lines perpendicular to the plane of the sashion piece, because there are no top timbers. We may therefore find the angle the planes of the water lines make with the plane of the fashion piece; and from thence find the true bevellings, by the method directed for sinding the bevellings by the ribband lines, when the plane of the fashion piece is perpendicular to the floor plane: So that all that seems now necessary, is to shew how to find the angle the plane of the sashion piece makes with the floor plane, to which the planes of the water lines are supposed parallel; in order to which;

1/l. Produce the line W k to the point m, in the line g L, the common

fection of the sheer and floor planes.

2d. Thro' the point m draw the line d n parallel to g G.

3d. Let fall the perpendicular k y, and thro' the point y draw the line ln perpendicular to dn. Draw also the line y v perpendicular to ln.

Note. The point k may be affured at pleasure.

4th. From the center m, with the radius m k, interfect the line l n in the point l. We may also draw the line m l; so k m l, will be the angle formed upon the plane of the fashion piece by its intersection with the sheer and floor planes.

Laftly. With the radius n l, from the center n, interfect the line y v in v; so shall l n v, be the angle which the plane of the sashion piece makes with the plane of the water lines; as in *Prob.* 7. Chap. 1. Part 2.

Having thus found the angle, let dm be the breadth of the fashion piece: Thro' d draw a line parallel to nl, to intersect the line nv in the point c; so shall cn be the breadth of the fashion piece upon the plane of the ribband. If then lines be drawn on the floor plane, parallel to

gG, eg, eg, ug; as xf parallel to gG, and if xG be equal to ng, and perpendicular to gG; then the angle gGf, will be the bevelling upon the plane of the ribband, and xf what it is without a fquare. Again, if from the point G we set off dn, the breadth of the timber, and draw the dotted line ii, equal and parallel to xf; we shall have the angle

g Gi, the true bevelling upon a square.

After the bevellings of the timbers are found, they are put on a board provided for that purpose, called a bevelling board. This board should be made the exact breadth of the timber, which suppose x, z,s, t, in the figure bevel (Plate 5.). If upon one edge of the board we fet off as many points, as we intend it shall contain timbers, and place them at any convenient distance from one another, whether equal or unequal is indifferent, and diflinguish them all by their proper names; we may then lay the graduated edge of the board to the line that represents the moulding fide of the timber, so that the proper point be at the intersection of the plane of the ribband, and the plane of the timber; and when in this polition, if we mark the other edge of the board where it crosses the ribband; a line drawn across the board from these two points, will be the true bevelling of the timber at that place. So when the board is applied to timber 7 in. the floor plane, we shall find the bevelling to be as much from a square as isexpressed by the dotted square line drawn across the board at that place. It must be observed that the perpendicular at timber 7. represents the forefide of the floor timber, and aftfide of its corresponding futtock: So that the floors will be under, and the futtocks standing bevellings, and where the space of the ribband, containing these two timbers, is strait, the one will be as much standing as the other is under bevelling; as in the plate, where the perpendiculars drawn to timber 7, from the points in which the aftfide of the floor, and forefide of the futtock interfect the ribband, are parallel to that drawn thro' the point, where the line that represents the moulding fide of both timbers, interfects the ribband: This method will answer for all the timbers, whether we bevel by half breadth lines. water lines, or ribbands, only observing the directions given before, to transfer oblique to square bevellings. We shall likewise hereby find, that in some cases, where the ribbands are very round, one bevelling will not do for two timbers, and even when it is only taken for one timber an ailowance ought to be made for the round of the timber; for which purpose it will be necessary in some cases to make a mould to set the round or hollow, and fasten this to a strait edged batten in the proper direction.

Another method practifed to find the bevellings for the fquare timbers

hers, is by the diagonals in the body plane; without regarding the curves of the ribbands in the floor plane: But this cannot be used, unless we

first form all the timbers in the body plane.

Let then the diffance betwixt the parallel lines AB and CD, be the timber and room, that is, as before observed, the breadth of two timbers, and the space betwixt them, and if this be equal to the distance betwixt the perpendiculars representing the planes of the timbers, we have all the timbers ready formed in the body plane in *Plate* 5. and may

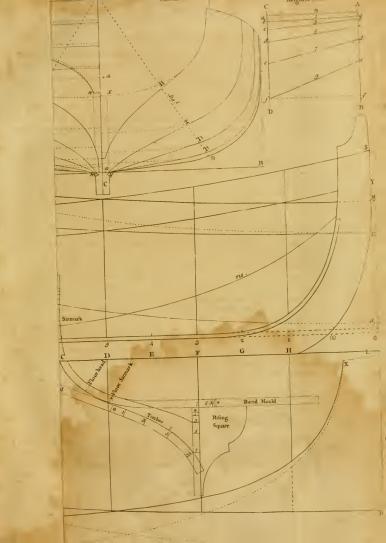
find the bevellings in the following manner.

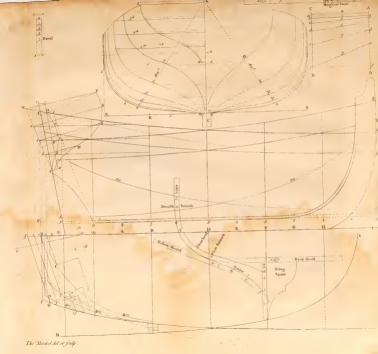
Draw the line A C, perpendicular to A B and C D, for the bevelling of : Then take the feveral distances in the diagonal, from (1) to the points where it interfects the timbers 1, 3, 5, 7 and 9, and fet them off from the point a, to the points b, c, d, e and f, in the lines A B and C D; fo that lines drawn from f to f, from e to e, &c. would be parallel to A C. Then draw the lines a b, b c, c d, de, ef; which will give the bevellings of the timbers 1, 3, 5, 7 and 9: That is to fay, of two timbers, viz. a floor timber and a futtock. So fe will be what the bevelling of timber o is within a square, as may be seen in the floor plane, by producing the line that represents the plane of timber 9, till it is equal in length to that which represents the plane of timber 7: But it must be observed that the perpendicular at 9, represents the foreside of the sloor timber; therefore the futtock corresponding to it, is before the perpendicular at 9; the futtock corresponding to timber 7, will likewise be before its perpendicular: So that the this method may give us nearly the bevellings of two timbers, yet these are not the two that are to be fastened together. Therefore this method ought to be rejected, unless we set off the breadth of the timbers on each fide of the line that represents the moulding edge, and draw perpendiculars betwixt each on the floor plane. We might then indeed find points in the diagonal, betwixt the timbers formed, which would give the bevellings of each floor timber with its correfponding futtock.

SECT. II.

To find the Bevellings of the Transoms. (Plate 7.)

Here are two ways of doing this. One is by forming curves on the sheer plane, by sections of planes cutting the ship fore and aft, parallel to the sheer plane. These planes will be represented by strait lines in the





the floor plane, parallel to WK; and in the body plane, by ftrait lines parallel to KO. In the plate we have only formed the two dotted curves in the sheer plane, to timber 7; the intersections of these with the planes of the transoms, which in the sheer plane are represented by strait lines, will give the bevellings; fo that all that is now necessary, is to shew how these curves are formed, and in what direction the stock of the bevel is to be placed upon the transom. In order to this, first draw the two dotted lines in the body plane, parallel to KO, to interfect the timbers. Transfer the heighths of these intersections to their corresponding timbers on the sheer plane; which will give the points thro' which there curves must pass. Secondly draw two dotted lines parallel to WK in the floor plane, to interfect all the transforms: These transferred to the planes of the transoms in the sheer plane, will give the points where the curves interfect these planes. These dotted lines in the sloor plane, must be the fame distance from the line W K, that the corresponding ones are from the line KO, in the body plane. They will interfect the transoms in the direction in which the stock of the bevel is to be laid upon the transoms; and if this should be judged too oblique, it may be transferred to a square one, as before directed. As the third transom is not formed in the floor plane, a line must be drawn parallel to the plane of it, where it is formed, to find the proper place and direction of the bevel-

The other method is by forming more timbers abaft the f. shion piece. Their planes will be represented by strait lines in the floor plane, where they will intersect all the transoms already formed. In the plate we have only drawn one G g, by which we have formed another cant timber in the body plane, in the same manner as the sashion piece was formed. The angle formed by the curve of this timber, and the level lines that are drawn at the heighth of each transom in the body plane, will be the bevelling; and the strait line which represents the plane of the timber, will give the direction in which the bevel is to be placed upon the transforms. This may likewise be transferred from an oblique to a square bevelling; and if needful, a mould made for the hollow of the transform.

The only thing that remains in regard to bevellings, is to shew how the ribbands are bevelled. Now as their planes are represented by diagonals in the body plane, the angles that are formed by the diagonals, and the timbers in the body plane, will be the bevellings; and the prependiculars representing the planes of the timbers in the floor plane, will give the direction for the bevel. The harpins are bevelled by level lines in the body plane; but as they are not parallel to the keel, when the stock is laid stat upon the upper side of the harpin, the tongue will not be in

Z 2

the direction of the timber; yet as the harpins are not above four or five inches broad, this need not be regarded. Those who incline to greater exactness may use the same method as in finding the bevellings of the sufficient piece for a square tuck, or form the harpins by diagonals in the body plane, which may be so contrived as to intersect the timbers nearly in the same points with the sheer.

C H A P. V.

Of forming Bodies not similar to that by which the Lines on the Sector were constructed.

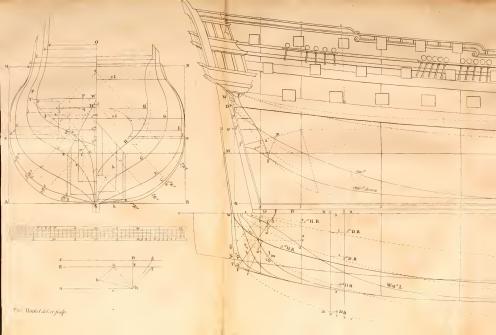
E have, as was proposed in this second part, shewn the general methods used in drawing of ships, and how to lay down a ship by the sector, if similar to that from which the lines were constructed. We shall now shew the use of the sector in forming bodies that are not

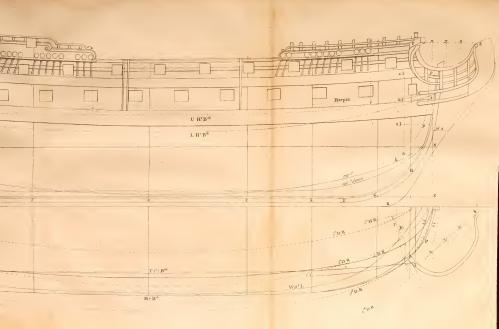
fimilar to one another.

The first thing to be done, is to set the sector by the proposed half breadth, and draw the diagonals as before directed. Then we must form the midship frame by the points, as in Plate 7. By this we shall discover, that it will be either too full or too sharp; and therefore must be altered by the artift, according to the service the ship is designed for. The foremost and aftermost timber must likewise be formed by the artist; and then the portions of the diagonals intercepted betwixt these timbers and the midship, will not be the same as that given by the sector, when fet to the half breadth. In order then to find the points in the diagonals for the intermediate timbers, the fector must be set to each seperately. Thus, take with a pair of compasses, the portions of the diagonals intercepted betwixt the midship and aftermost timber, now made conformable to the fervice for which the ship is designed; and by these set the fector feparately for each, till the diftance taken by the compaffes reach from the proper points in one leg, to the corresponding points in the other leg; and being thus fet, we may find the proper points in that diagonal; and then fet the fector for the next diagonal.

In order to illustrate this, we have in *Plate* §, laid down the midship, foremost and afternost timbers of two ships; the one an *East India* ship, the other a *French* privateer. Their bodies are very different from one another, and likewise from that by which the sector was formed; and if the intermediate timbers formed by the sector in both ships, will produce









fair ribbands, it may be prefumed that it may be very nfeful in and other cases.

Now because we cannot open the sector in the plate, we have taken the feveral divisions of the four ribband lines upon the after body of the fector, and fet them off from the point C, upon the four lines C 1 R, C 2 R, &c. intersecting one another in the point C: So that the point C is the same distance from the points 7, 5, 3 and \$\oplus\$, upon these lines, that the same points are from the center of the joint upon the sector. We have likewise drawn four other lines to intersect the former in the point C. But the angle formed by the two lines marked 1" R, is not equal to the angle formed by the two lines marked 2dR; nor to that formed by the two lines marked 34 R, or by those marked 4th R. The angle formed by each two lines of the fame name, is determined in the following mauner. From the center C, an arch of a circle is described to intersect the line 1 R in the point . From this point, the distance betwixt the midship and aftermost timber now formed, taken upon the first diagonal, is set off upon the arch; and the other line C 1ª R is drawn thro' this point. In like manner the other three lines are drawn, by describing arches of circles from the center C, to meet each line in the point \(\operatorname{O} \), and fetting off upon each arch the distance betwixt the midship, and aftermost timber, taken upon the diagonal corresponding to each line. So the distance betwixt the points (and (), in the two lines marked 1 R, is equal to the portion of the first diagonal intercepted betwixt the midship and aftermost timber; the distance betwixt these points in the lines marked 2d R. is equal to the portion of the second diagonal intercepted betwixt the aforefaid two timbers, &c. The lines being thus drawn, and each divided in the same proportion as its corresponding one of the same name is, the points on each diagonal for the timbers 3, 5 and 7, will be found upon examination to be at the same distance from the after timber, that these points are from one another, in the two lines corresponding to each diagonal.

The like process may be used for forming the intermediate timbers in the fore-body: But it must be observed, that in forming the ribbands from these timbers, their stations in the sheer plane must be determined by the sector, as in *Plate* 7. and after the ribbands are all formed, the

proper stations of the timbers may be affigned.

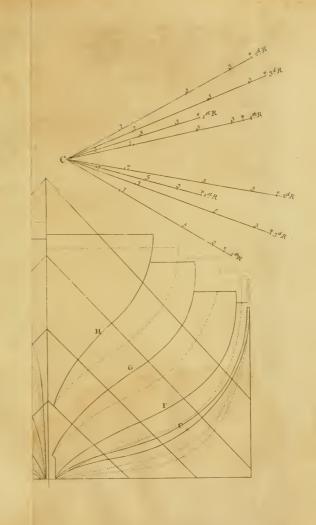
Now tho', both the ribbands and timbers thus formed may prove fair, yet neither this method by the fector, nor any other method, which has been published, can be established as a certain invariable rule; because the curves by which they are formed have no properties peculiar to themselves to distinguish them from all other curves, as was before observed.

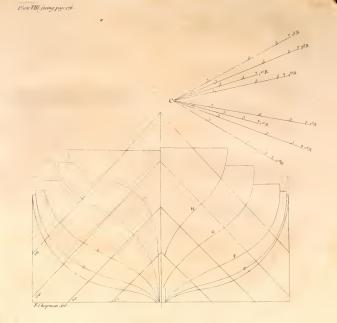
The only way to make any confiderable improvements in this art, we presume, will be, by carefully examining the different bodies of several ships that have been actually built, and whose good or bad qualities have been discovered by experience. We have therefore, for the sake of such of our readers as are not surnished with a sufficient number of draughts for that purpose, collected into the following table all the dimensions that are necessary to determine the form of source different ships; and we may venture to affirm, that the youth will receive more benefit by delineating these from the dimensions, and thereby sooner acquire the art of drawing, than by all the rules and directions that have been hitherto published on that subject.

The dimensions in the following tables are taken from the diagonal scale, Plate 2, and the number of equal parts contained in twelve feet, is

specified at each ship.

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Jitto to the touch of the stem	11195	2105	96011	9880	8616		4024	7756	6820	6808		4580		5426
Jitto to afflide of item on the J. deck	17446 17413 16458 14270 12844 11945	7413	16458	142701	12844		6474 11710 1015c	1710	10150				5148	
Oitto to the knuckle	175551799516458142801284412097	75501799516458	16458	1428cm	2844		6634	1730	10266	9762	9108			8494
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Ditto to the fecond counter	3950	3410		3164	2688		5	3010						
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racigntin or the item	7750		8000	6568	6130		3472	2900			- 1		3950	4893
do of the lower duct.	2408		5458	4756			1	4030						I
The sound and some services	4940	5,30	4939	4278		2930	2130	3500				2541		1
Chem	5150	5041	5304	4342	4200	3200	2600	3766				2770	3000	
edge >	5230	5840	5574	4084	4127	3371	2078				2966		1830	
of the lower wale	3510	4190	4080		3250	2630	1075		2490				1730	2236
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DIMENSIONS for forming the BODIES. A first RATE 100 Guns. 2262=12 Feet.

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	Timbers	D	iagona	ls.		Heigh		bread.		brea.	frames.
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	⊕	1620 3114									
	. 8	1460 2790									7232
	16	1186 2212									11862
	54	0766 1532									
	30	0311057									
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bei	hat of the diagonals?	1178 228					557.0	10325	3924	3052	1 5006
D,6:	ance from ditto on a	1184230		5044	7904						
411	e bufe produced }	11041230	14120	12744	1//00			1			-

Nº 2. A iecond RATE 90 Guns. 2731=12 Feet.

Timbers		Diag	gonals			Heigh	ith of	bread.	Half	brea.	f ames.
names.	ıít.	2d.	3d.	4th.	5th.	low.	upp.	top. ti.	main	top.	fro. 🕀
A								9750			0000
9	1410 2	728	4700	6008	7051	4416	5130	10041	5366	3830	6820
18											11914
27											17014
32											19842
I											6556
S											11645
W											13345
Z.							6018	10272	4116	3012	15045
Heighth of the diagonals an the middle line	11642						1	-			
the bair produced	11642	2214	4084	5944	17823			-			

No 2. A third RATE 74 Guns. 2730=12 Feet.

Timbers	D	iagonals.				bread.			frames
names.	1ft. 2d.	3d. 4th.	5th.	low.	upp.	top ti.	main	top.	tro. 🕀
(1533 2877	4658 5923	6864	4069	4632	7920	5166	4.064	
9	1462 2729	4533 5806	6.743	4199	4717		5103		
* 8		3922 5241							1.1962
27		2500 3956							17083
33		1156 2512							20499
F		4547 5834					5140		
M		4206 5504					4926		
S		3267 4660							14468
Her thin of the diagonals?		1932 3210			5400	0400	314/	3.97	14400
Dirance from ditto en ?	- 1	3942 6713	1 0	8					
Bu hide produced }	114410172	1394-10/14	7404	•	'	٠	ı	k.	No 1

DIMENSIONS for forming the BODIES. 179 A fourth RATE 50 Guns, 1034 Tons, 2722=12 Feet.

- 1 - 1 - 1 - 1	ditti 1								-		
Timbers		Di	agona	ls.		Heig	hth of	brea.	Half	brea.	f nrs.
names.	11.	2d.	3d.	4th.	5th.	low.	upp.	top.	main	top.	tro.
A	1406	2600	4154	5216	6000	3444	3950	7010	1496	3400	0000
9							3968				
18											10993
2.4											14559
29											17505
1											5342
P											8898
S											10688
W								7512	2690	2540	12460
Heighth of diagonal on the middle line D.flance from ditto on 7	1058										
the bate produced },	1071	1984	3482	14976	10480	-					-

No 5. A fifth RATE 40 Guns, 706 Tons, 2736=12 Feet.

			1				0110,				
Timbers		Di	agona	ıls.		Heig	hth of	brea.	Half	brea.	framer.
names.	ist.	2d.	3d.	4th.	5th.	low.	upp.	top.	main	top.	tro.
\oplus							3766				
10	1098	1818	3136	4230	5030	3254	3778	6570	4006	3027	5954
19	0680	1218	2346	3500	4416	3628	3960	6850	3712	2828	10424
25	0339	0600	1448	2558	3560	4220	4398	7114	3198	2511	13400
28	0128	0216	0761	1796	2864	4708	4760	7262	2950	2376	14888
G	1175	1958	3300	1360	5040	3290	3778	6436	3990	3027	4210
N	0911	1534	2764	3880	4682	3514	3862	6544	3762	2998	7178
T											10156
Y											11676
Heighth of diagonal on }	1020							- / /			
Disance f om ditto oo the base produced				4634							

Nº 6 A fixth RATE 20 Guns 508 Tons 2744=12 Feet

11 0. 11.	DACII ICII	1 10 2	.0 04							
Timbers	I	Diagona	ıls.		Heig	hth of	brea.	Half	brea.	Diffance of frames
names.	1st. 2d.									fro.
0	1064 187									
9	0939 164									
18	0610 110									
24	0290 053									
26	0119 022									
I	0922 162									
P	0642 115									
S	0432 082									
U	0000 037							1764	2180	11136
Haighth of diagonal on the middle line	0848 150									
the base produced	0860 151	42720	4106	1560c	-					
				Aa						Nº 7

N 7.	R SLUU.	r or 150 r	ons, 2090:	= 12	T. CCF	
Timbers	Diago	nais.	Heighth of	brea.	Half brea	Daitance of frames.
names.	1ft. 2d. 30		low. upp.			
0	0754 1262 18	30 2290 257	1448 1622	2510	2078 1976	5
4	0678 1145 17	12 2168 251	2 1 500 1 66 5	2550	2062 1900	2000
8	0518 0899 14	05 1898 231	5 1632 1758	2654	1939 1830	4150
12	0254047609	10 1403 189	8 1895 1939	2819	1704 1600	6268
14	0115022005	38 1057 159	2074 2090	2920	1446 136	2 7334
Ď	0714119417	66 2217 253	8 1 500 1 6 5 6	2538	2078 196	1 1999
F	0616 1072 16	51 2134 248	115971717	2608	2048 191	8 3070
H	0449 0836 13	76 1872 225	7 1793 1848	2702	1930 184	8 4144
K	0110 0412 08	70 1351 177	3 2106 2106	2856	1586 166	8 5212
II sighth of the diagonals }	0614 1066 16			-		-
Diffance from ditto on the base produced	0614104617	00 2378 310	1	-	ļ	

The LONDON EAST INDIA Ship 630 Tons, 2730=12 Feet.

Timbers	Diagonals.	Heighth of brea. Half brea.	mes.
names.	1ft. 2d. 3d. 4th. 5th.	low. upp. top. main top. tro	· (D)
A	1430 2588 3886 4720 521	3230 3654 6014 3674 2980 -	
4	1374 2476 3790 4636 513	3 3754 6126 3623 2966 4	152
12	1140 2040 3306 4252 481	12-2-1-7: 2:	296
20	0560 1148 2182 3270 411		
24	0228 0546 1372 2430 352		526
D	1376 2485 3784 4632 514	200 000	894
H	1264 2276 3586 4481 502	0 0 0 0	978
M	1012 1886 3120 4116 471	33 77 7 3 70	060
0	0578 1340 2577 3652 434		404
Heighth of the diagonals }	1110 2020 3330 4640 595		
Diffance from date on }	1106 2020 3226 4407 557	1	

The RONETTA 208 Tons, 2727=12 Feet.

N 0.	THE POL	TI	1 1							
Timbers	Di	agonal	s.	1	Heigl	nth of	brea.	Half	brea.	frames.
names.	Ift. 2d.	3d.	4th.	5th.	low.	upp.	top.	main	top.	tro.
A	09151707	29353	3934	4616	2704	3026	5232	3260	2521	
9	084211548	2797	2775	4462	2790	3084	5308	3140	2474	4599
18	05160956	1900	2898	3690	3410	3000	5508	2733	1606	9198
24	02060354	0890	1000	2422	4150	4330	6822	1244	1242	122.54
1 26	08101524	2766	2756	1160	2820	2136	5320	3142	514	4364
p	0539 1044	2047	3060	3786	3292	3580	5550	2708	2330	
Ř	0220 0640	1550	25:0	3220	3522	3800	5678	2290	2040	8470
S	0362	1174	2090	2756	3677	3956	5764	1942	1748	9000
Heighth of the diagonals	07101320							1		
D stance from ditto on } the base produced	0706 1315	23611	3400	14393	-					Nº 10.

No 10. The THAMES 240 Tons, 2745=12 Feet.

N. 10.	The II	1 77 :A1	I E O							
Timbers	D	agona	ls.		Heig	hth of	brea.	Hair	brea.	1 182 - 1 of
names.	1ft. 2d.	3d.	4th.	5th.	low.	upp.	top.	main	top.	tro 🕀
\oplus	1024 1731									
3	0845 1441									4791
5	0510 0913									7966
7	01930334									
8	0106 0155									11952
В	0970 1647									319
D	0722 1240									
E	0532 0951									
F	0345 0699					3622	5398	2310	2055	7950
Heighth of the diagonals }	0824 1434	2682	4068	5581						
Diffance from ditto on }	0858 1439	2419	3317	4110						

Nº 11. A FRENCH Privateer of 372 Tons, 2730=12 Feet.

Timbers		Di	agona	ls.		Heig	hth of	brea.	Half	brea	frames.
names.	ıit.	2d.	3d.	4th.	5th.	low.		top.	main	top.	fr.
(1)						2762			3242	/ 0 .	
8	0700	1536	2480	3174	3578	2830		4536	3216	2711	3948
16	0450	1010	1790	2530	3134	3082				2584	
24	0164	0370	1754	1300	2040	3608		5062	2600	2280	11812
27	0073	0116	0279	0598	1330	3907		5260	2364	2110	13294
Ĥ	0750	1544	2449	3114	3464	2874		4600	3096	2660	3700
M	0625	1238	1990	2628	3056	3122	-	4700	2810	2548	5674
0						3354		4752	2526	2486	6670
0	0106	0518	1088	1672	2146	3711		4834	2084	2398	7648
Heighth of the diagonals }	0800	1611	2472	3232	3900						
Diffance from ditto on the base produced			2880						-	-	

No 12. A SHIP of 162 Tons. 2702=12 Feet.

Timbers	Diago	nals.	Heighth of	brea Ha	f brea.	Distance of frames.
names.	Ift. 2d. 3d	. 4th. 5th.	low. upp.	top. mai	n top.	fro. 🕀
A	0914 1652 250			3838 249	4 2136	
4	0814 1486 234			3926 243		3520
12	0535 0962 159			4170 222		
16	0260 0504 095			4340 202	8 1 682	
18	0800 1458 233			3898 240		20
11	0630 1140 186			3974 231	-	000
K	0298 0776 14			4026 200	1848	6014
M	010007			4090130	1 1 287	6912
Heighth of the diagonals }	0716 1300 21		2		_	
Diffance from ditto on }	0712 1300 21	87 3132 4160			-	NTO -
		A a 2				IN- 13

A Fishing S M A C K. 114 Tons, 2723=12 Feet.

Timbers		Di	agona	ils.		Heig	hth of	brea.	Half	brea	frames.
names.	1ft.	2d.	3d.	4th	5th.	low.	upp.	top.	main	top.	fro.
A	0681	1316	2100	2672	3143	1920		3310	2400	2051	
6	0554	1101	1916	2500	2988	2042		3186	2361	2000	2142
12	0321							3200		1800	
15	0186							3278	, , ,	1608	20, 1
18	0098								1552	J .	6440
C	0628							J 1		2024	6 1
F					2918			00	2	1930	
1		1	1 -	1	2580	- '		J .	1968	_	3240
.Heighth-of the diagonals?	0500				1814	2000		3000	1330	1000	4312
on middle line S				2644							
the base produced	0500	11000	11020	12044	3450	-	-		-		,

No 14. A SLOOP of 50 Tons, 5462=12 Feet.

Timbers	D	iagonals.		Heighth	of brea.	Half I	brea.	frames.
names.	11t. 2d.	3d. 4th.	5th.	low. up	p. top.	main	top.	11.0 (D
0	1422 2547	36844724	5698	1956 27	70 4190	3570	3303	
4	1400 2518	3657 4710	5676	2028 27	82 4164	35703	3303	2968
8		3354 4452						5984
12		2665 3808						
14		2112 3244						
В		3598 4670						2662
D		3400 4484						4154
F		3001 4045						5624
Heighth of the diagonals?		2264 3214			32 4790	2388	2200	7120
on the middle live		3110 +352			1.			
the base produced	1120 2020	2838 3583	14250			-		

These tables of dimensions are so particular that one example will be sufficient to illustrate their use in laying down any of the ships.

Let it then be required to lay down the Bonetta pink, which in the ta-

bles is No 9. 398 Tons.

1st. Draw the line AB, upon which erect the perpendicular CD; and because the main half breadth in the column is 3268, take that from the scale, and lay it off from C to A, and from C to B, and erect perpendiculars at A and B.

2d. Look for the lower heighth of breadth, in the column; which will be found to be 2704. Set up this from A to L, and from B to L, and draw the line L L, which will be parallel to AB. Set up also the upper heighth 3026, from A to V, and from B to V; and lay off 2354, which

by

by the tables is the radius of the upper breadth fweep, from the points

V and V; which will give us the center of the fweep.

3d. Set up 5232, the heighth of the top timber line, from C upon the line CD; thro' which point draw a line parallel to AB, and lay off 2521. the half breadth of the top timber, both ways upon it, from the line CD; and form the top timber by a mould, to break in fair with the back of the upper breadth fweep. This compleats the upper part of the midship frame.

4th. To form the lower part of the midship frame, draw the five diagonals; their heighths from the point C, upon the line C D, and their distance from C, upon the line AB produced, is given in the proper columns. The heighth of the fifth diagonal is 5000, which fet up from C to 5: The distance from the middle line upon the base is 4393, which lay off from C, upon the base produced; and draw a line to this point from 5; which will be the upper or fifth diagonal. In the same manner are the other diagonals drawn, by taking the numbers from the proper columns.

5th. Lay off 4616 from 5 upon the fifth diagonal, 3934 from 4 upon the fourth, 2935 from 3 upon the third, 1707 from 2 upon the second, and 915 from 1 upon the first diagonal: A curve passing thro' these points, and the main breadth at the lower heighth will form the midship frame to the floor head. A firait line to touch the curve in this point, drawn to the upper edge of the keel, compleats the whole midship frame. The points in the diagonals are in the column corresponding

to (H)

In like manner we may find points in the diagonals, for all the other timbers, and also for their lower, upper, and top timber heighths of breadths and half breadths, from the dimensions in the proper columns corresponding to each; and by these form the timbers. We may likewife station the timbers in the sheer and sloor planes, the distances of each from (1) being in the proper columns, and also form all the curves that are necessary upon these planes. But as our plate will not contain this,

we shall only lay down the stem, post, counter and stern.

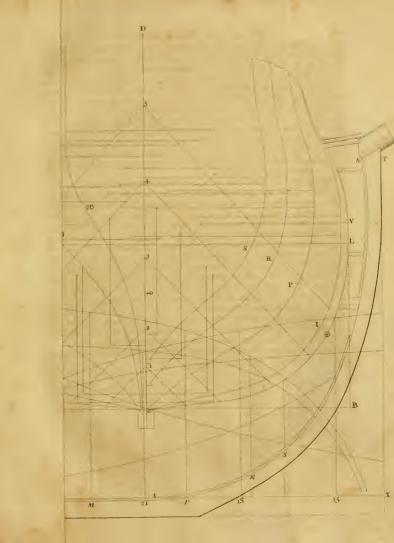
In order to do this, draw the line Z X, to represent the upper fide of the keel; and at any convenient place erect a perpendicular for the after timber 26: The diftance of this timber from (+), is 13254; and the wing transom from (1), is 14744; which therefore is 1490, abaft timber 26. The heighth of the wing transom is 5440. Set up this from the line Z X, upon a perpendicular erected to the point W 1490, abast timber 26. The distance of ⊕ from the fore part of the post is 12994, which subtracted from 13254, remains 260. Lay this off from 26 to P, and draw draw the line P W for the fore fide of the post. The counter is 2250 abast 26, which lay off on the line Z X, and erect a perpendicular, upon which set up 5680 to c, which is the heighth of the counter. The upright of the stern at the sheer rail, is 2370 abast timber 26, which set off from timber 26 upon the line Z X, at that point erect a perpendicular to s, and draw the line c s, which may be produced to the heighth of the stern, as in the plate. We may then form the counter; where it must be observed that a pink has no transom. We have only assumed the point W to determine the rake of the post. Timber 26 is 13254 from \bigoplus , and timber 24 is 12264 from \bigoplus . Therefore the distance betwixt them is 990, which set off from 26 to 24, gives the station of that timber; and by the same manner, the stations of the

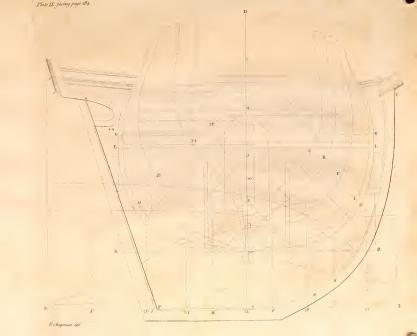
other timbers may be found.

Having thus laid down the stern, we shall in the next place lay down the stem. Erect the perpendicular X T, to limit the fore part of the stem; upon which set up 5526, the heighth of the aft side of the stem from X to T, and let b be the aft fide of the head. The head of the stem is 10266, and the touch of the stem is 6826 before (, therefore the distance betwixt them is 3440, which set off upon the line Z X, from a perpendicular let fall from b; this will give the point t, the touch of the stem, where erect a perpendicular, and set up 3296 to 0; which will give the center of the lower sweep of the stem. The radius of the upper fweep is 7080, and n the center; and these two sweeps will form the stem. We may now station the timbers F, I, M, P, R and S, as in the plate: for as the touch of the stem is 6826, and timber P 7430 before (1); P will be 604 before the touch of the stem. We have in the plate laid down the main and top timber half breadth lines, also the rifing and narrowing of the floor and floor sweeps. After the same manner any of the other ships may be laid down from the tables.

Having now given the principal dimensions, we shall in the next place

give the scantlings.





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N. B. The stern post is the same thwartships with the keel below, and the head square, it to be had.

Of the ROTHER.

HE general method is to make the breath of the rother, at the lower end in large flips $\frac{1}{3}$ or $\frac{1}{3}$, and in fmall flips $\frac{1}{3}$ of the extreme breadth of the flip; but this cannot be effa-billhed as an invariable rule, for a full built will require more rother than a fharp-built flip, and it will be neceffary fornetimes

to have a piece, fayed to the affide of the rother, called a back. As to the feandings, the head of the rother, if it can be had, may be 3 or 4 inches bigger than the head of the fern poth thwarthins, and two inches bigger afore and aft than thwardhips. For the fake of fuch of our readers as are not acquainted with

For the take of fuch of our readers as are not acquainted with the terms relating to shipbuilding, we shall conclude this fecord part with the following gloslary.

GLOSSARY,

OR

EXPLICATION,

Of TERMS relating to

SHIPBUILDING.

BEAMS, are the large pieces of timber, which are laid across the ship; their ends are lodged on the clamps, and being bound by knees to the side, keep the ship to her breadth.

Bow, is the round part of the ship, forward. That on the right hand, with one's face forward, is called the Starboard, and that on the lest the Larboard-bow; they both unite at the stem.

BREAST-HOOKS, are large knees fayed across the stem to both bows, into which they are bolted.

Carlings, are square pieces of timber, lying fore and aft from one beam to another, into which they are scored.

CATHEAD, is a large square piece of timber; one end of it is fastened upon the forecastle, the other end projects without the bow so faras to keep the anchor clear of the ship when it is heaving up by a tackle, the block of which is called the Cat-block: The rope which passes thro' the several shivers of the block, and extremity of the cathead, is called the Cat-fall.

Bb

CLAMPS,

- CLAMPS, are thick planks, which support the ends of the beams.
- COUNTER. The hollow part of the stern above the wing-transom is caled the lower, and that part betwixt it and the lower part of the cabbin-lights is called the upper or second Counter.
- DEAD WOOD, confifts of large pieces of timber laid one upon another, upon the keel, afore and abaft, where the ship is so thin as not to admit of sufficient substance for the two half timbers, which are therefore scored into this dead wood. The half timbers are used when, by reason of the sharpness of the floor, one piece of timber cannot be had which will make a floor-timber.
- Decks, are the same in a ship that floors are in a house, and are denominated, according to their heighth, lower, middle, and upper: Besides which, there is a deck which covers the cabbin, and reaches from the stern near to the main-mast; this is called the Quarter-deck. In some ships there is an apartment above the great cabbin, called the Roundhouse; the deck which covers it is called the Poop. Another deck covers the forecastle, which is an apartment in the fore-part of the ship, in which is the cook-room.
- FAY, is to fitt two pieces of wood so as to join close together. The plank is said to say to the timbers when it bears, or lies close to all the timbers.
- HARPINS, are the fore-part of the wales which go round the bow and are fastened to the stem.
- HAWSE-PIECES, are broad timbers in the bow of the ship, thro' which there are holes cut for the cables to pass.
- Head, is some figure, often that of a lion, carved as an ornament for the fore-part of the ship. There is a large piece of timber sayed to the stem upon which the figure rests; this is called the Knee of the head, and by reason of the great breadth at the the upper part, it is composed of several pieces: It is let into the head, and sastened to the bow on each side by knees, called the Cheeks of the head. The head is supported by rails, which extend from the crown of the figure to the cathead.
- HEEL. The lower part of a mast, or any timber, is called the heel, and the upper part the head.

 KEEL

- KEEL, is the principal piece of timber first laid upon the blocks, which supports the whole structure. When this cannot be had of a sufficient depth in one piece, there is a plank sastened to the bottom, called the False Keel, which serves likewise to save the bottom of the main keel.
- KEELSON, is fayed over the floor-timbers, and bolted thro' them into the keel.
- KNERS, are crooked pieces of timber. One leg or arm is bolted to the beams, and the other to the ship's side. They are either lodging or hanging. The hanging knees are fayed up and down, and the others fore and aft the side, and rest upon the clamps.
- LIMBER-BOARDS, are short pieces of plank, fayed next to the keelson, which may be taken out to clear the limber-holes, that are left either below or above the floor-timbers, for a passage for the water to the pump.
- RABBET. When a plank is to be fastened to any piece of timber, such as the stem or post, there is so much wood cut out of the piece as the plank is thick, which is called the Rabbet; and when the plank is let into this rabbet, it will be even with the outside of the piece, as at the after-end of the keel, and lower end of the stern-post.
- Rails, are narrow planks, generally of fir, upon which there is a moulding fluck. They are for ornament, and nailed across the stern above the wing-transom and counters, &c. They are likewise nailed upon several planks along the sides; one in particular is called the Sheer-rail, which limits the heighth of the side from the forecastle to the quarter-deck, and runs aft to the stern and forward to the cathead. The wales are nearly parallel to this.
- ROTHER, is a piece of timber, or several pieces fastened together, and fitted to the stern-post, to which it is hung by irons, whereon it moves, and thereby the ship is steered.
- SCANTLING, is the breadth or thickness of a piece of timber.
- SCARPHS. When two pieces of timber are joined together, fo that the end of the one goes over the end of the other, being tapered so that the one may be let into the other and become even, they are said to be scarphed; such are the keel-pieces. But when the ends of the two Bb 2

pieces are cut square and put together, they are said to butt to one another; and when another piece is laid upon, and sastened to both, as is the case in all the frame-timbers, this is called scarphing the timbers; and half the piece which sastens the two timbers together is reckoned the length of the scarph.

- SPEM, is that circular piece of timber where both the fides of the ship unite forward. The lower end of it is scarphed into the keel, and the bowsprit rests upon the upper end of it.
- STEPS, are large pieces of timber fayed across the keelson, into which the heels of the masts are fitted.
- STERN, is the after-part of the ship, in which are all the cabbin-lights. It likewise includes the stern-frame, which consists of the stern-post, transoms, and fashion-pieces, all sastened together.
- STERN-POST, is that firait piece of timber at the after-end of the ship, which unites both the sides. The heel of it is tenanted into the keel, and the wing-transom sastened at the head of it.
- TIMBERS, in a ship, are as the ribs in the body, and serve to support the sides, the planks being all sastened to them; the two aftermost are called Fashion-pieces; they support the ends of transoms. The two timbers, forward, at the cathead, are called Knuckle-timbers. [For the names of the other timbers, see Chap. III.. Sect. 3. Part II.
- TUCK-square, is, when the heels of the sashion-pieces are let in upon the post, at which place the heighth of the tuck is fixed.
- WALES, are planks, thicker than the rest, brought about the outside of the ship, in the wake of the decks.

THE THEORY OF

SHIPBUILDING and NAVIGATION.

PART III.

Of NAVIGATION.

CHAP. L SECT. I.

Of Trigonometry by tabular Calculation from a Table of natural Sines. Tangents and Secants.

E have in the first part explained the doctrine of trigonometry, so far as to give a solution to all the varieties geometrically by scale and compasses. We come now to shew how to perform the same arithmetically by a table of natural fines, tangents and fecants; in order to which, it will be abfolutely necessary to shew how this table may be constructed.

To Construct a Table of natural Sines, Tangents and Secants, to a Radius of 10000 equal Parts.

Describe a quarter of a circle, and let the radius be 10000 equal parts. Divide the arch into 90 degrees, and draw fines, tangents and fecants to every degree, as directed in making the plain scale. Measure each off these seperately, by the same line of equal parts that the radius was taken from, and fet down the numbers contained in each, in proper columns corresponding to every degree in the quadrant, as in the following table, where it is done only to every fifth degree, being fufficient to shew the nature of the table, which has been calculated to great exactness, by numbers for 192

for every minute to a radius of 100,000; but in practice the logarithms of those fines, tangents and secants are used.

A Table of natural SINES, TANGENTS and SECANTS.

Deg.	Sines.		Tang.		Seca.		
5	871	9962	875	11430	10038	11473	85
10	1736	9848	1763	56713	10154	57588	80
15	2588	9659	2679	37320	10353	38637	75
20	3420	9397	3639	27474	10642	29238	70
25	4226	9063	4663	21445	11034	23662	65
30	5000	8660	5773	17320	11547	20000	60
35	5735	8191	7002	14281	12208	17434	55
40	6427	7660	8390	11917	13054	15557	50
45	7071	7071	10000	10000		14142	45
		Sines.		Tang.		Seca.	Deg.

This table gives by inspection, the sine, tangent, or secant of any arch, or number of degrees therein expressed, if the radius of the circle be 10000; and because, as the radius of a circle is to the sine, tangent, or secant of any arch of the same circle, so is the radius of any other circle; to the sine, tangent, or secant of a similar arch of this other circle, as proved in Prop. 8. Chap. 3. Sect. 2. Part 1.

Therefore we may find the fine, tangent, or fecant of any arch, in any circle, provided the radius be known, by the following proportion.

As the radius in the table.

Is to the fine, tangent, or fecant of any arch in the table.

So is the radius of any other circle.

To the fine, tangent, or fecant of a fimilar arch of this other circle.

E X A M P L E.

Required how many feet in length is the fine of 35 degrees, supposing the radius to be 130 feet.

The tabular radius is 10000, the fine of 35 degrees in the table is 5735; therefore by the rule of three.

10000 : 5735 :: 130 : 74 7550, or 74 ,555 130 172050, 5735 1|000|74|550

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If the length of the radius of any circle, and the length of a fine, tangent, or fecant of the fame circle be given, and it be required to find the arch; the proportion will be,

As the given radius of any circle

Is to the given fine, tangent, or fecant of the fame circle:

So is the radius in the table

To a fine, tangent, or fecant in the table;

which must be found in the table; and corresponding thereto in the column of degrees, is the quantity of the arch required.

EXAMPLE.

Let the radius be 500, and the given fine 383; then

500:383::10000:7600

 $\frac{383}{3830000(7660)}$, and this found in the column of

fines in the table, corresponding thereto, is 50 degrees the quantity of the arch required.

It will be needless to give any more examples, as in practice we shall use the table of logarithms.

SECT. II.

Of artificial SINES, TANGENTS and SECANTS.

WE observed in the first part, that the sides of a right angled triangle were distinguished by different names, viz. hypothenuse, perpendicular and base; and that by the angle, is understood that opposite to the base, which is supposed to be drawn across the paper; and the perpendicular up and down, making a right angle with the base, to which angle the hypothenuse is always opposite.

The fides may be confidered likewise as fines, tangents, or secants, by which means, besides the aforesaid proper names, they will acquire another, which we shall call their sirnames; and these will vary according

to the fide made radius.

If the hypothenuse be radius, the base will be the sine; and the perpendicular, the sine complement of the angle.

If the base be made the radius, the hypothenuse will be the secant complement; and the perpendicular, the tangent complement of the same angle as above.

If the perpendicular be made the radius, the base will be the tangent, and the hypothenuse the secant of the angle; all which has been demon-

strated in the first part.

Hence, the whole business of trigonometry, may be said to consist, either in finding a fine, tangent, or secant, to a given arch, the radius being known; or if the radius, and either the sine, tangent, or secant be known, to find the arch; both which may be performed by a due attention to the two foregoing proportions: And as any side may be made radius, there may be different operations for each case.

All the various cases of right angled triangles, are express'd in the fol-

lowing table.

The Proportions for the feveral Solutions of the fex Cafes of Plane rightangled Triangles.

Given	Requir.		Radius.	Cates.
Нуро.	Bafe	R: fine of the angle :: H : B R: fine comp. of the angle :: H : P	Hypo.	
and	and	Sec. comp. of the angle : $R:H:B$ Sec. co. of the angle : $tan.$ co. of the ang. : $tH:P$	Base.	1/1.
Angle	Perpen.	Sec. of the angle : tang. of the angle : : H : B Sec. of the angle : R : : H : P	Perpen.	
Base	Нуро.	Sine of the angle : $R::B:H$ Sine of the ang.: fine comp. of the ang:: $B:P$	l-lypo.	
and	and	R: fec. comp. of the angle::B:HR: tang. comp. of the angle::B:P	Bafe.	2 <i>d</i> .
Angle	Perpen.	Tang. of the angle : fec. of the angle : : B : H Tang. of the angle : R : : B : P	Perpen	
Perpen.		Sine comp. of the angle: K::P:Fl Sine comp. of the angle: fine of the angle::P:B	Нуро	
and	and	Tan. co. of the ang. : fec. co. of the ang. : : P : H Tang. comp. of the angle : R : P : B	Base.	3d.
Angle	Base	R : fec. of the angle : : P : H R : tang, of the angle : : P : B	Perpen	
Hypo.	Angle	H: B:: R: fine of the angle required	Hypo.	
and	and	B:H::R: fec. comp. of the angle required	Bafe.	
Bafe.	Perpen.	After finding the angles the perpendicular is found by case 1st. or 2d.		41h.
Bate	Angle	B: P:: R: tang. comp. of the angle required	Bale.	
and	and	P:B::R:tang. of the angle required	rerpen	
Perpen.	Нуро.	After finding the angles the hypothenule is found by case the $2d$, or $3d$.		51b.
Perpen.	Angle	P:H::R:lec. of the angle required	Perpen.	
and	and	H: P:: R: fine comp. of the angle required	Hypo.	()
Нуро.	Bafe.	After finding the angles the base is found by case 1st. or 3d.		61b.

It is evident from what has been faid, that the first thing to be done, in order to give a solution to any of the cases, is, to make one of the sides radius; now if the thing required be a side, any of the three may be made radius; for there is no necessity, for making the given side radius, but after the radius is fixed, then both the given and required sides, will have particular sirnames; the proportion for sinding a side will always be,

As the sirname of the given side, Is to the sirname of the required side:

So is the given fide. To the required fide.

If the thing required be an angle, one of the given sides must be made radius, which will determine the firname of the other side; and the proportion will be

As one of the given fides, viz. that made radius

Is to the other given fide:

So is the radius

To the firname of the fecond fide.

And when this is found in the table, the quantity of the requir'd angle

will be found in degrees and minutes in their proper columns.

Note. If the thing requir'd be a fide, the two first terms will be either fines, tangents, or secants, to be taken out of the logarithmick table of sines, tangents and secants; the third term will be a natural number, as miles, yards, or any other measure, the logarithm of which, must be taken out of the table of logarithms; and, when the logarithms of the second and third terms are added together, if from this sum be subtracted the logarithms of the first term, look for the remainder in the table of logarithms; and corresponding thereto in the proper column, will be the natural number, expressing the length of the required side, taken by the same measure with the given side.

When an angle is required, we must not work for the angle itself, but for the sine, tangent, or secant of it; the two first terms of the proportion will be natural numbers, and their logarithms must be taken out of the table of logarithms; the third term will be a fine, tangent, or secant, and its logarithm must be taken out of the table of artificial sines, tangents and secants; and then the second and third terms must be added, and the first subtracted from their sum as before; the remainder must be found in the table of artificial sines, tangents and secants; and the quantity of the angle required will be found in degrees and minutes corresponding thereto.

We shall illustrate the whole by an example in each case, by the tables,

and also by Gunter's scale.

The general rule by the pen, is the fame as in any other question in the rule of three; and if we use the natural sines, it will be performed, by multiplying the second term by the third, and dividing the product by the first term, the quotient will be the fourth term required; observing to make the first term according to the aforesaid proportions, but it will be indif-

indifferent which of the other two is made the fecond term, as they are

to be multiplied into each other.

But as the natural fines, \mathcal{C}_c are calculated to feven places, this would make the operations very tedious, upon which account their logarithms are used, and are had by the table of artificial fines, tangents and secants; if the table of logarithms, was made for natural numbers to seven places, we could find the logarithms of natural fines, \mathcal{C}_c as easily as of any other number; but even in that case, we must have a table of natural sines, \mathcal{C}_c and afterwards have recourse to the table of logarithms, whereas by the table of artificial sines, \mathcal{C}_c we have the logarithm at once.

This table contains every degree, and minute, of the quadrant; if the number of degrees be less than 45, look for it at the head of the table; and for the minutes under Min. increasing downwards on the less than 6 the page; but if the degrees exceed 45, look for them at the bottom of the page, and the minutes in the right hand column above M, increasing upwards; and when the degrees and minutes are thus found, the logarithmick fine, tangent, or secant, will be found in its proper column; observing if the degrees be found at the top, the word sine, tangent, or secant, must be found at the top, underneath which, right against the minutes, which must be found under Min. is the thing requir'd; but if the degrees are at bottom, these words must be found at the bottom, above which, and right against the minutes, which must be also found above M; is the thing required.

E X A M P L E.

Let it be required, to find the fine, tangent and secant of an arch, or angle of 33° 45'. Here the degrees are less than 45; therefore look for them at the top, and the minutes under M; right against which, and under the word fine, is 9.744739; under tangent, is 9.824893; under secant, is 10.080154; but if the fine, tangent and secant of 56° 15' were required, look for 56 degrees at the bottom, and 15 minutes over M; right against which, and above the word sine, is 9.919846; above tangent, is 10.175107; above secant 10.255261.

The degrees at the top begin at o, and increase to 44; the degrees at the bottom, in the first page, are 89, and decrease to 45; the one including the minutes, is always the complement of the other; so that if it was required to find the sine complement of any arch, look for the sine, and

in the fame line, you'll find the fine of the complement.

Cc2

Thus

Thus to find the fine complement of 33°, 45'; look for the degrees 33° at the top, and 45' in the left hand column under Min, the fine will be under the word fine as before, 9.744739, and the fine complement 9.919846 in the fame line above the word Sine; the like may be faid of the tangent complement and the fecant complement.

Having the logarithmick fine, tangent, or fecant, to find the degrees

and minutes corresponding thereto.

This is only the reverse of the former, for you must look over the table, till it is found, and if in a column that has the word sine, tangent, or secant, at the top; the degrees are at the top; and the minutes in the left hand column under Min. but if it is in a column, which has these words at the bottom, the degrees are at the bottom, and the minutes above M in the right hand column.

EXAMPLE.

Let it be required to find the degrees and minutes, answering to the tangent, 10,346337; this will be found over the word tangent, therefore the degrees must be at the bottom, viz. 65, and right against it above M, is 45; so 65° , 45° , is the arch required: But if the complement was required, the degrees would be at the top, and the minutes under Min. viz. 24° , 15° . Sometimes the exact number cannot be found in the table, in which case, all that can be done, is, to take the nearest to it; so we can never err a whole minute.

To work these by scale and compasses, there is a line of logarithmick sines, and a line of logarithmick tangents, upon Gunter's scales, constructed in the same manner as the line of numbers; for against 30 degrees, in the line of sines, is 5000 in the line of numbers, the natural sine corresponding thereto; and against 30 degrees, in the tangents, is 5773, the natural tangent; the line of sines is continued to 90 degrees, but the tangents to 45 degrees; the tangents above 45 degrees, are the same with their complements, for the radius, which is equal to the tangent of 45 degrees, is a mean proportional betwixt the tangent of any arch, and the tangent of its complement to 90 degrees, which is the reason, that the line of tangents is numbered 1 and 89, 5 and 85, 10 and 80, &c.

The tables being thus explained, we shall in the next place shew their

use in the resolution of the fix cases, of right angled triangles.

CASE I.

Given the hypothenuse 60 miles, the angle 56°, 15'; required the base, and perpendicular.

For the BASE.

As the radius, or fine of 90° o	-	-	-	10.000000
Is to the fine of 56° 15' -		-	-	9.919846
So is the hypoth-nuse 60 miles	- 11-	-	-	1.778151
To the base 49.9 miles -		-	-1	+.697997

For the PERPENDICULAR.

As the radius, or fine of 90°	-	-		10.000000
Is to the fine complement of the	angle,	or fine	of 33°	45' 9.744739
So is the hypothenuse 60 miles	-	-		1.778151
To the perpendicular 33.3	-		-	+1.522890

By GUNTER's Scale.

Extend the compasses from 90 on the line of sines, to 56° 15'; the same extent will reach in the line of numbers, from 60 to 50 nearly, for the base; and the extent from 90 to 33° 45' on the line of sines, will reach in the line of numbers, from 60 to 33 \frac{1}{2} nearly for the perpendicular.

CASE II.

Given the perpendicular 33.3 miles, and the angle 56°, 15'; required the hypothenufe, and base.

To avoid working by the fecants, let the hypothenuse be radius, and it

will be,

For the HYPOTHENUSE.

As the fine complement of the angle,	or fine o	of 33° 45	com. a	rith. 0.255261
Is to the radius, or fine of 90° 0'	-	-		10.000000
So is the perpendicular 33.3 miles		-	-	1.522890
To the hypothenuse 60 miles	-		-	+1.778151

In this, and fuch like cases, where the first term is not radius, instead of the logarithm of the first term, use the complement arithmetical of it, which is, what any logarithm wants of the logarithm of the radius; now this being always 10,000000, the complement arithmetical, will be found, by subtracting each figure in the logarithm, from 9 excepting, the first

first towards the right hand, which must be subtracted from 10; as in this example, the logarithm of the sine of 33° 45′, by the table, is 9.744739, and by subtracting, as above directed, the complement arithmetical will be 255261; this is so plain and easy, that by a little practice, the complement arithmetical, will be as readily taken out of the table, as the logarithm itself, and then it must be added to the other two logarithms; and when the logarithm of the radius is subtracted from this sum, the remainder will be the logarithm of the fourth term required; and this will be the same thing, as if the operation was performed by the common method, viz. by subtracting the logarithm of the first term, from the sum of the logarithms of the second and third terms; in this example the sum of the two is - - - 111.522890.

Logar, of the first is 9.744739

Sine 33° 45' 9.744739
Radius
Perpen. 33.3 miles 1.522890
1.522890
9.744739
1.778151

Remainder 1.778151

Now in subtraction as a lesser number is taken from a greater; it is plain if any number be added to both, and then the lesser subtracted from the greater, it will make no alteration in the remainder; and this is the very case here, for 9.744739, is to be subtracted from 11.522890; if to each of these be added the complement arithmetical, viz. 0.255261; the sum of the greatest will be 11.778151; the sum of the least will be 10.00000; and as all the figures in the lesser number are cyphers, except the first to the less hand; the subtraction is performed, only by cancelling the first figure to the less hand in the greatest number.

For the BASE.

As the fine complement of the angle or fine of 33° 45' com. arith. 0.255261 Is to the fine of the angle 56° 15' - - - 9.919846 So is the perpendicular 33.3 miles - - - 1.522890 To the bafe 49.9 miles - - - + 1 697997

By the GUNTER's Scale.

The extent from 33° 45′ to 90° in the line of fines, will reach in the line of numbers from 33.3 to 60, for the hypothenufe; and the extent from 56° 15′ to 33° 45′ in the line of fines, will reach in the line of numbers, from 33.3 to 49.9 for the base.

CASE III.

CASE III.

Given the base 49.9 miles, and the angle 56° 15' required the hypothenuse, and perpendicular making the hypothenuse radius.

For the HYPOTHENUSE.

As fine of the angle 56° 15'	comp.	arith.	-	-		0.080154
Is to the radius	-	-	-	-	-	10.000000
So is the base 49.9 miles	-	-	-	-	-	1.697997
To the hypothenuse 60 miles	. •	-	-			+1.778151

For the PERPENDICULAR.

As the fine of the angle 56° 1	5' comp	. arith.	-		0.080154
Is to the fine complement 33°	45	-	-	-	9.744739
So is the base 49.9 miles	-	-	-	-	1.697997
To the perpendicular 33.3	-	- -			+1.522890

By GUNTER's Scale.

The extent from 56° 15' to 90 in the line of fines, will reach from 49.9 to 60 on the line of numbers; for the hypothenuse, and the extent from 56° 15', in the line of sines, will reach from 49.9 to 33.3 on the line of numbers for the perpendicular.

C.A S E IV. and V.

Are exactly the same, only changing the names of the base and perpendicular.

Given the hypothenuse 60 miles, and base 49.9 miles; required the angles and perpendicular.

As the hypothenuse			comp	lement	arithn	netick		8.221849
Is to the base 49.9	miles		-	-	-	-	-	1.697997
So is the radius	-	-	-	-	-	- 1		10.000000
To the fine of the	angle	56°	151	-	-	-		+9.919846

By GUNTER's Scale.

The extent in the line of numbers from 60, to 49.9, will reach in the line of fines, from 90° to 56°, 15'; and when the angle is found, the other fide, may be found by Cafe 1. or 3.

CASE

CASE VI.

Given the base 49.9 miles, and perpendicular 33.3; required the angles and hypothenuse:

Making the perpendicular radius, the base will be the tangent, and the

proportion will be,

As the perpendicular 33.3 miles compl	ement	arithn	netical	8.477110
Is to the base 49.9	-	-	-	1.697997
So is the radius, or tangent of 45°	-	-	-	10.000000
To the tangent of the angle 56°, 15'	-	1	-	20.175107

In this case, the first figure in the logarithm of 33.3 is a cypher; therefore the next to it must be subtracted from 10, and all the rest from 9 as before, to find the complement arithmetical; and when the three are added, the characteristick will be 20, the characteristick of the radius being subtracted, there will remain 10; and this found in the table of artificial sines, tangents and secants, against it is 56° 15′ the tangent of the angle required.

By GUNTER's Scale.

The extent in the line of numbers from 33.3 to 49.9; will reach in the line of tangents, from 45° to a point in the same line, which is either 33° , 45^{\prime} or 56° , 15^{\prime} ; and to know which of the two it is; I find the extent in the line of numbers, is from a less to a greater, and therefore it must be so in the line of tangents; so the point must be more than 45° o', and of consequence must be 56° , 15^{\prime} .

These are all the cases in right angled triangles. We might here likewise shew how to solve all the cases in oblique triangles, but as the whole business of navigation may be performed without them, we shall apply

the doctrine of right angled triangles to navigation.

Now as navigation is a science which teaches us how to direct a ship's way from one port to another; it will from thence follow, that the situation, and distances of the places must be known. Our first business then shall be to shew how this may be attained. In order to this, it will be absolutely necessary to understand the principles of geography, which shall be the subject of the next chapter.

CHAP. II. Of GEOGRAPHY.

SECT. I. Of SURVEYING of LAND.

Eography is that science by which we learn how to lay down, either all the places in any particular country, called a chart, or map; or all the habitable parts of the world upon a globe. The first is commonly called surveying of land, and the latter is what is generally understood by geography; we shall explain both.

The chief defign of furveying, is to lay down all the places, in any particular piece of ground, upon paper; by which means, their diffances, and positions, from one another, may be had, with as much certainty, as if they were to be measured on the very spot of ground where they are

situated.

Let it be required to lay down all the places in the plane ABDE, viz. F, G, H, I, K, L, M.

The instruments necessary for this purpose, are, a well graduated circle, with an index, and fights, to take angles by; and a chain, line, or

staff, to measure distances by.

Assume, (See Plate 10.) at any convenient distance from one another, any two points B and D, from whence, all the points in the plane, may be seen, place the circle with its center over the point B, and the index right over the diameter; move the circle, upon a pin provided for that purpose, till the point D may be seen thro' the sights, and fasten the circle in that position; then move the index, till all the points, may be seen successively, thro' the sights, noting the degrees cut by the index, corresponding to each point; then move the instrument, from the point B, to the point D, placing it so, that the index being laid upon the diameter, the point B may be seen thro' the sights; and then safen the instrument, with its center right over the point D; move the index, till all the points, successively, may be seen thro' the sights, noting the degrees cut by the index, as before; then measure the distance betwixt B and D, which suppose 40 fathoms, or yards, Sec.

To lay this down upon paper, take 40 from any scale of equal parts, which lay off upon any strait line from b to d, at the point b, make the same number of angles, equal to those taken in the field; do the same at the point d, the intersections of the lines drawn from b, with their

D d corre

corresponding lines drawn from d, will give the points f, g, b, i, k, l, m; and if we measure their distances from one another, by the same scale that the distance of the points b and d was taken from, we shall have the true stance of the points in the field.

For the triangles DFB, and dfb, are equiangular, by conftruction; therefore bd:bf::BD:BF, but bd contains as many equal parts of the scale, as BD does fathoms; therefore bf must contain as many e-

qual parts of the scale as BF does fathoms.

As these are all the places that are supposed can be seen from the points B and D, the adjacent places cannot be laid down without altering the two stations: Let the next two stations be K and M, from whence taking the angles as before; all the places that can be seen from K and M, may be laid down in the same manner as those seen from B and D. We may proceed in the same manner to lay down all the places in an island, or country, by continuing to alter our station to places already laid down, till we have gone over the whole; this gives us the nearest distance betwixt any two places, but by the intervention of valleys, it will be im-

possible to go the nearest way in a mountainous country.

Another method is by actually travelling over the country, in a direct line, and measuring the distances by a wheel provided for that purpose. There must also be a contrivance to keep in a direct line, which may be done by fetting a flake, at fuch a distance from the place we set out from, that it may from thence be distinctly seen; we may then, by the help of the fights, fet several intermediate stakes in a strait line between them. After we have travelled to the farthest stake, we may then place another stake at such a distance, that from it, at least two of the former stakes may be seen, by which it may be set in a direct line with them: and placing feveral intermediate stakes betwixt these two last ones, we may by them, produce the line to another flake, and proceed thro' the whole extent of the country. We may likewise keep in a direct line by the mariner's compass, of which, we shall only here remark, that wherever it is carried to, the needle will always point to the north, or its variation may be found. We do not propose this method as the most expeditious, neither is it strictly true, or practicable, unless upon a plane; but as it agrees exactly with the plain fea chart, we shall infert it.

Being now provided with a wheel, and mariner's compass, with fights properly fitted to it, let us set out from the point C, directly as the needle points, setting a stake at every mile, till we arrive at the point A, so from C to A, is due north: in travelling along, if we see any places either to the right or lest, thro' the sights placed at angles to the needle, they

will

will be either due east, or due west of us; we must measure their distance from the line CA, and also the distance we are then from the point C. both which must be noted in a book provided for that purpose. When we arrive at A, the fights being at right angles with the needle, we may fet a stake at X, and move directly to it, setting stakes at every mile as we go, and when we arrive at X, we may travel directly fouth again to S, measuring the distances of all the places from the line X S, as soon as they can be feen thro' the fights; we may proceed in the fame manner, first going north or south, then east or west, till we have gone over the whole country to be laid down. The lines A C and X S, will be fo nearly parallel to each other, that they may without any fensible error be taken as fuch.

Now in order to lay down this in a map (See Plate 10.) let the extent from fouth to north be 90 miles, and likewise that from east to west 90 miles; draw the line A C, and perpendicular to it, the lines A E and CF; draw also the line EF parallel to AC; so these four lines will limit the map, let each be graduated into go equal parts, and at every tenth draw lines parallel to A C, and also to E F; so the whole map will be divided into nine equal fquares.

We may now lay down all the places in the map from the notes taken off in the field, as for instance, if it were required to lay down the point Y. I find by my notes, I travelled 28 i miles due north from C. and 14 i miles due east before I arrived at Y; therefore lay a ruler across from 28 2 upon the line AC, to 28 3 on the line EF; and take 14 3 with a pair of compasses, which lay off by the edge of the ruler, from the

line A C, and this will give the point Y.

It is very plain that no place can be laid down in the map, unless the distance and position of it, with respect to some other place be known; and when this cannot be measured by reason of its being inaccessible by the intervention of seas, or otherwise we must have recourse to colostial observation; and tho' two places be so remote, that they cannot be seen from one another; yet we may by observing the sun, or some star, at both places, find how far the one is to the northward, or fouthward of the other; we must also find some way to know how far the one is to the eastward, or westward of the other, and when those two are found, their distances and situation may with certainty be found by trigonometry.

That we may comprehend, the manner, by which the fituation, and distances of places, have been found, we must explain some principles of geography, which science, consists, in giving a true description, of all the habitable parts of the whole world, as was before observed.

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SECT.

SECT. II.

Of the G L O B E.

HE first thing we shall observe is, that this earth, and sea together, is supposed to compose a globe; the first geographers found out this, by observing, that in whatsoever place of the earth, they were; their fight was always terminated, by a circle, unless intercepted by hills or otherwife, and the observer in the center of it; the firmament at the fame time, forming the half of a concave fphere over his head, and tho' he moved his fituation, for thousands of miles, he still found himself in the center of a circle, and the point over his head continue at the fame distance, which could not be, if the earth was flat; for supposing the observer placed at C, in the center of the circle H Z O N; (Plate 11.) then Z would be the point in the firmament over his head, but if he moved upon the diameter, from O to G, he would then be under the point D, which is much nearer to him, than the point Z was, when in C: but if the earth be allowed to be round, and the observer at l: Z will be the point over his head, but when he has moved to G, the point H will be over him, and at the same distance from him, that the point Z was, when in C: Upon this account, they refolved, to defcribe the earth, not upon a plane, but upon a globe: For which purpose, an artificial one was made, to represent the natural one. As the earth, was supposed a folid globe, the firmament, which every where furrounded it, was supposed to be a concave sphere, in which the sun and ftars feemed to move, for they were continually shifting their situation with respect to us, so that either the sun and stars, or the earth must be in a continual motion, and tho' it is certain that the earth has the motion, we shall suppose the sun, moon and stars to move round, and the earth immoveable in the center, being apparently fo to our fenses.

They likewise found, that the sun, by his daily motion from east to west, described an arch of a circle, ascending one half, and descending the other, the stars, also describing arches by their motion; amongst them, they observed one, seemingly not to change its situation, but always at or near the same distance, from the point over the observer's head, while he continued his station, or moved either east or west: But when he moved, either south, or north, the star appeared either nearer

to, or further from, that point.

They likewise found that the observer might move so far to the southward till the star would just disappear, and the sun, which at his first setting out, was a great distance from the point over his head at noon, was now right over him; from thence, they supposed the heavens, with all the stars, sun and moon, to be carried round the earth once in 24 hours, two points only being immoveable, one near the aforesaid star, and the other diametrically opposite to it; by which motion, every point in the heavens, excepting those two, would by every revolution, describe a circle.

GEOGRAPHICAL DEFINITIONS.

Def. 1. A globe, or sphere, is a solid body, which has a point within it, equally distant from every point of its surface; and may be conceived to be formed by the revolution of a semi-circle, round the diameter, which is supposed to continue immoveable. (As was observed in the first part).

Def. 2. The axis of the globe, is that line passing thro' the center, round which the whole globe is moved, and may be termed a diameter. Def. 3. The poles, are the two points in the globe's surface, through

which the axis is supposed to pass; these have no motion, one is called

the north, and the other the fouth pole.

There are two globes used; upon one, all the kingdoms of the earth are described, this is called the terrestrial, or terraqueous globe, containing all the land, and water: The other is called the celestial, containing all the constellations; and tho' the firmament be supposed a concave, they may be duly represented on the convex superficies of a globe; and supposing it transparent, and the observer in the center, they would appear to him, in the same manner as they really are in the heavens; the same circles are described upon both, and are either great, or small; the planes of the great circles go thro' the center of the earth, and their diameters are the same with the diameter of the globe; the planes of the small circles do not pass thro' the center, they are parallel to the plane of some great circle, their diameters are less than the diameter of the globe, and continually decrease, according to their distance from the plane of the great circle, to which they are parallel.

Def. 4. Meridians, are great circles, interfecting one another in both

poles, of which there may be an infinite number.

Def. 5. The equator, or equinoctial line, is a great circle, cutting all the meridians at right angles exactly in the middle, being equally diftant from both poles.

Def. 6. The ecliptick, is a great circle croffing the equinoctial in two opposite

opposite points in such a manner, that the planes of those circles form

an angle of 23° 30'.

Def. 7. The horizon, is that circle which terminates the fight; supposing the observer at sea, he finds himself in the center, and the sea and sky uniting: It is plain, if he alters his station, this circle will change likewise; so that it cannot be described upon the superficies of the globe; it is called the visible, or sensible horizon.

Def. 8. The zenith, is that point in the heavens, which is right over the observer's head; the opposite point in the other hemisphere, is called the nadir; these two points vary continually as the observer changes his station.

In order to represent the horizon, and zenith by the globe, the axis is fitted in a brass circle, in which the axis turns round, this circle then will represent any meridian, because any place upon the superficies of the globe, may be brought right under it; this, with the globe within it, is placed in a broad wooden circle, the infide of it is the fame diameter. with the infide of the brazen meridian; fo the half of the globe will always be under, and the other half over this circle; and the meridian may be so moved in the notches, as to bring any part of it to this wooden circle; which is therefore called the real, or rational horizon, and is always parallel to the visible, before described, as in the artificial globes they are both the fame, because the eye may be so placed as to see the whole half of the globe at one view; by the help of this circle, we may reprefent the horizon of any place, for it is only turning the globe upon its axis, 'till the place is under the brazen meridian; and then moving the meridian in the notches, 'till the point is go degrees distant from the horizon; for that point will be the zenith, and is equally diffant from every point in the horizon.

Def. 9. Azimuth circles, are supposed to pass thro' the zenith, and nadir points, all divided into two equal parts by the horizon; these cannot be described upon the globe, but are represented by a quadrant of altitude, which is a thin piece of brass, that may be screwed to any part of the brazen meridian; and when this is brought to the zenith, the other end will move round upon the horizon; all these five circles, here de-

fined, bisect each other, and the globe into two equal parts.

Def. 10. Parallel circles, are fuch as divide the globe into two unequal parts, and are drawn parallel to fome great circle; those parallel to the horizon are called parallels of altitude or almicanters, but are not described on the globe: Those parallel to the equator, on the terrestrial globe, are called parallels of latitude, and are actually drawn thro' every tenth degree of the meridian.

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The equinoctial is divided into 360 degrees, and a meridian drawn thro' every tenth: One of these meridians is graduated, every quarter of it into 90 degrees; beginning at the equinoctial, and ending at each pole, each

pole being 90 degrees distant from the equinoctial.

Tho' there are no more meridians, nor parallels, actually drawn upon the globe; there may be an infinite number of both; for every place on the earth's furface, is supposed to be at the intersection of a meridian, and a parallel of latitude, which point may be found by the brazen meridian; it is by these intersections, that the situations of places are determined.

Def. 11. Latitude of a place, is an arch of the meridian, intercepted between the place, and the equinoctial; and is either fouth, or north, according as it lies to the fouthward or northward of the equinoctial.

Difference of latitude, is an arch of the meridian, intercepted between

the parallels of two places.

Def. 12. Longitude of a place, is an arch of the equinoctial, intercepted betwirt the graduated meridian, and a meridian drawn thro' the place, and fometimes is accounted quite round the globe, and at other times it is accounted both ways, east and west.

Difference of longitude, is an arch of the equinoctial, intercepted be-

twixt the meridians, of two places.

Def. 13 Departure, is the distance of any place from the meridian, taken upon the parallel of latitude of the place, and therefore is always less than the difference of longitude; it is sometimes called the meridional distance; of which in another place.

Def. 14. Declination, is an arch of the meridian, intercepted betwixt

the fun, or star, and the equinoxial.

Def. 15. Tropicks, are two circles, parallel to the equinoctial 23° 30' distant from it; that to the northward, is called the tropick of cancer; that to the southward, the tropick of capricorn, these two limit the ecliptick.

Def. 16. Polar circles, are 23° 30' distant from the pole, that at the

north, is called the artick, and that at the fouth antartick.

From these definitions, the following inferences may be deduced.

Inf. 1. Every point on the earth's furface, has a corresponding point in the heavens for its zenith, from which, if a line be drawn thro' the point affumed on the earth's furface, it will pass to the earth's center: And the latitude of any place, is always equal to the distance of the zenith from the equinoctial.

Inf. 2. Those inhabitants of the earth, who have the pole in their zenith, have the equinoctial in their horizon, and are in 90 degrees of la-

titude;

titude; and those who have the poles in the horizon, have the equinoctial in their zenith, and are in no latitude.

Inf. 3. The elevation of the pole, above the horizon, is equal to the

latitude of the place. (Plate 11. Fig. 1.)

DEMONSTRATION.

Let P represent the pole, Z the zenith, \mathbb{E} Q the equinoctial, H O the horizon; the arch \mathbb{E} Z, is the latitude of the place by Inf. 1. if to the arch \mathbb{Z} P, be added the arch \mathbb{Z} \mathbb{E} , their sum will be 90 degrees, because the pole is 90 degrees from the equinoctial; but if to the same arch \mathbb{Z} P, be added the arch PO; their sum will also be 90 degrees, because the zenith is 90 degrees from the horizon; therefore the arch PO, is equal to the arch \mathbb{E} Z.

The globe being thus prepared, with the aforefaid circles delineated upon it, their next bufiness was to find the latitudes and longitudes of places which they effected in the following manner, by celestial observations.

As to the latitude, it is plain, that if there was a star in the pole, there would be no more required, but to take its altitude or heighth above the horizon, with a good instrument, which would be the latitude of the place: But as there is no star in the pole, they were forced to take the least and greatest altitude of any star near the pole, which by making an entire revolution round the pole in 24 hours, would be twice in the observer's meridian: Suppose then its least altitude 48 degrees, and greatest 52 degrees, the difference betwixt these is 4 degrees, the half of which must be the star's distance from the pole; and this being added to the leaft, or subtracted from the greatest, gives the latitude; for in the first, the pole is 2 degrees higher above the horizon than the star, which must therefore be added to the altitude 48, which gives 50 the latitude, but when the star is 52 degrees of altitude, it will then be elevated 2 degrees above the pole; which being subtracted from the altitude, there remains 50, the latitude as before. This way of finding the latitude would require 12 hours difference betwixt the two observations, which therefore cannot be done at fea, because a ship in that time, may alter her latitude confiderably; neither is it practicable when the pole is near the horizon: But after they had found the declination of fome stars, or their distances from the pole; it was then enough to find one of the altitudes, and when below the pole, the distance of the star from the pole. added to the altitude, gives the latitude; but if above the pole, it must be subtracted from the altitude, the remainder is the latitude; one example will be sufficient to illustrate this: Let the star be at 10 degrees from the pole, and b O, the altitude, 40 degrees; the arch l' O is the latitude by Inf. 3. but this is the sum of the star's altitude, and distance from the pole, which must therefore be 50 degrees the latitude of the place.

But if the flar is in r, then r O, the altitude, is 60 degrees, and P O the latitude as before; therefore subtracting the stars distance from the pole, viz. 10 degrees, from the altitude 60, there will remain 50, the latitude as before. But as these observations are made in the night, they cannot be depended upon at sea; we shall therefore shew how to find the latitude by the sun's zenith distance, or altitude when in the meridian of the observer.

If the sun was always in the equinoctial, his distance from the zenith, would be the latitude of the place, by Inf. 1. but that it is not so, is evident, because then the sun would always rise and set in the same points of the horizon, and his meridian altitude, would be the same every day to an observer while he continues in the same place; therefore we must likewise know the declination at the same time that we have

the zenith distance.

The geographers, by a daily observation of the sun's greatest altitude, which always happens when he is upon the meridian of the place, that is at mid-day, found that an observer, who was above 23° 30' distant from the line, had the sun approaching his zenith, for one half of the year, and the other half receding from it, and after his nearest approach, it was a whole year before he came back to the same place; they likewise found the greatest distance from the zenith was just 47 degrees, more than the nearest approach; and from thence his greatest distance from the line was 23° 30', and by keeping an exast account of his zenith distance every day, they formed tables of his daily declination, or distance from the line; so that we have now by inspection, the sun's declination on any day of the month.

The table being thus made, the latitude will always be found, either by adding the zenith distance and declination together, or subtracting the one from the other, all the various cases that can happen, shall be explained in the next section; and we shall now proceed to shew how they

found the longitude.

To attain this, they confidered that the fun, and stars in the space of 24 hours, return'd near to the same points in the heavens, in which they were at that time the day before, and consequently moved 360 degrees in the 24 hours, which in one hour would make 15 degrees; so that if two places were 15 degrees to the eastward or westward of one

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another, those in the eastermost place, would see the sun, a whole hour before those in the westermost place; and these last would see the sun an

hour after it disappeared to the others.

Now if the whole earth, should be, at the same instant of time, deprived of the light of the fun, by the intervention of fome opake body, it would happen just at the sun's rising in some places, whereas in other places the fun would be upon the meridian, and in other places 15 degrees from the meridian; in short it would happen at different times of the day, to all the inhabitants of the enlightened hemisphere, that lie under different meridians; and therefore, if the hour were exactly known at all those places, from thence their difference of longitude might with certainty be found, for the difference of the hours multiplied by 15, will give the degrees; as supposing three places C, B, A, to those at B, let it be noon; to those at A, let it be 10 in the forenoon; and at C, 3 in the afternoon; C would be the eastermost, for the sun passed the meridian of that place, and got to the meridian of B, in three hours, which makes 45 degrees difference of longitude that B is to the westward of C, but then the sun must move two hours more to come to the meridian of A, it being only to in the forenoon at that place, which makes 30 degrees difference of longitude, A is to the westward of B, and 75 degrees to the westward of C.

As such cases of total darkness seldom happen, the longitudes of places are not much to be depended upon except where good observations, of the sun, moon, or other heavenly bodies, have been made; sometimes the longitude has been found by actual mensuration, or by good sea journals; and by frequently going to the same ports at last, tables of the latitudes and longitudes of the most remarkable places in the whole habitable world have been made; and by these tables, all the places may be laid down, according to their latitudes and longitudes upon the globe; as suppose it were required to lay down a place in 10 degrees east longitude, and 20 degrees north latitude, or which is the same thing, to find a place upon the globe, in that latitude and longitude. Move the globe upon its axis till the brazen meridian cuts the 10th degree upon the equator, on the east side of the first meridian; then look for the 20th degree upon the brazen meridian, and right under that is the place required.

S E C T. III.

The Description and Use of the ANALEMMA.

T would be foreign to our defign to flew how to folve all the geographical problems by the globe; it will be of greater use in navigation, to shew how to delineate all the circles of the sphere upon a plane, which may be done several ways; but as we have already explained the principles of the orthographick projection of solids, we shall now make use of

that way. (Plate 12.)

It will be very easy to conceive that if the globe were cut by a plane passing thro' the center; the section would be a circle, and when this plane passes thro' the poles, the circle will be a meridian, as in the plate; PÆSQ, may represent the meridian of the place, P the north, and S the fouth pole; P S the axis; Æ Q the equinoctial; for tho' this is only the diameter of it, yet because the plane of the equinoctial is perpendicular to the plane of the meridian, it will be represented by its diameter, and for the same reason all the parallels of latitude, which upon the globe, are circles parallel to the equinoctial, will in this projection, be represented by their respective diameters, and drawn parallel to the line ÆQ; each quarter of the meridian is divided into go degrees, beginning at the equinoctial, which will be all equal; but the degrees of the equinoctial, tho' upon the globe they are all equal, will here be unequal, and are represented by their respective sines, beginning at the center: P S will represent a meridian described upon the globe, at right angles to the meridian, thro' which the globe is supposed to be cut; every other meridian will be represented by an elipsis, and may be drawn thro' every 10th degree of the equinoctial. The most expeditious way of describing them, is by finding the points in every parallel of latitude, thro' which the meridians will pass, which may be done by a fector, or as readily without it; thus, First divide the equinoctial into degrees, which being only a line of fines, will be the fame as the construction of the line of fines on the plain scale; and because there are as many degrees in every parallel, as in the equinoctial, they must likewife be divided into the fame number of parts; and in the fame proportion that the line Æ Q is divided into: Now let it be required to divide the parallel of 23° 30': Draw the line E C K, which will represent the ecliptick, divide it into degrees, by fixing one point of the compasses in

C, and with the other transfer all the divisions of the equinoctial to this line, and thro' each division, draw a line parallel to the line P S, to interfect the parallel of 23° 301, which will divide it into the same number of parts, and in the fame proportion with the equinoctial; for ECm, is a right angled triangle, of which E C, the radius, or femi-diameter of the globe, is the hypothenuse; Em the radius of the parallel, or fine complement of the latitude, is the base; and C m, the fine of the latitude, is the perpendicular. Now the lines drawn thro' the feveral divisions of the line EC, will all be parallel to the perpendicular C m; and therefore constitute so many right angled triangles, all similar to E C m. There-latitude, fo is a degree, or any part of the equinoctial, to a degree, or proportional part of the parallel. After the same manner all the other parallels may be divided: and the meridians drawn as in the plate; there will be no occasion to draw lines from the divisions of E C to the parallel. only lay a ruler parallel to P S, and mark its interfection with the parallel. After the meridians and parallels are all drawn, the places may be laid down according to their latitudes and longitudes, in the same manner as on the globe, but their distances cannot be measured so easily; we shall therefore shew how to do this without laying down the places, and also how to folve all the geographical problems necessary in navigation, by fcale and compaffes; and by this plate, with as much certainty as with the globe itself.

The meridians, the equinoctial, with its parallels, and the ecliptick being thus delineated upon brass, wood, or pasteboard, are made to move about the center, within the circle Z H N O, which may represent a meridian in the heavens; Z is the zenith, and because the meridian Z H N O, passes thro' the zenith, Z H, and Z O will be azimuth circles of 90 degrees each; they are graduated both ways, to shew the altitude and zenith distance. H O is the horizon, the meridian's drawn thro' each 15th degree, are the hour circles, and because the sun is the same distance from the meridian of the place at any hour in the afternoon, that he is in the forenoon, at the hour which is as much before as the other is after 12; the meridian of 11 in the forenoon, will be that of 1 in the afternoon, as they are numbered in the plate. When the pole is in the zenith, the meridians will all be azimuths, and the equinoctial will be the

horizon.

The observer is always in that point of the circle PÆS Q, which is directly under Z, the points of the compass are marked on the horizon; and the sun's place in the ecliptick to every fifth day of the month,

is marked on the line E K: This projection is called the analemna; when the north pole is above the horizon, the right hand quarter, viz. Z C O, will be eaft, and the hours before fix in the morning, and after fix in the evening, will be on the right hand fide of the meridian of fix, which will always be represented by the line P S; the hours from fix in the morning to noon, and from noon to fix in the evening, will be in the left hand quarter, viz. Z C H, which is the west: When the fouth pole is elevated above the horizon, that which was east, will now be weit, and the forenoon hours, will be the afternoon hours; the sum will rise in the left, and set in the right hand quarters. Tho' in this plate, the heaven's and earth coincide, yet in reality, they are at such a distance, that the earth is accounted only a point; so that in all observations, the observer is supposed at the center of the earth.

Geographical Problems folved by the Analemma, and by Scale and Compasses.

PROB. I.

Given the fun's declination and zenith distance at mid-day, or meridian altitude; to find the latitude of the place.

This admits of three varieties.

CASE I.

The latitude and declination both north, and the fun to the northward of the observer, or both fouth, and the fun to the southward of the observer.

Note. This can only happen to those within the tropicks.

Rule. Subtract the zenith distance from the declination, the remainder will be the latitude.

E X A M P L E.

Declination 20° 00' north Latitude north. Zenith distance 10° 00' north 10° 00'

But if the declination and latitude were both fouth, and the fun to the fouthward of the observer, the latitude would be ro degrees south.

To delineate this by scale and compasses.

Describe the circle ZHNO, from Z set off towards O, the given zenith distance 10° 0' to , and from fet off 20° 0' the given declination to

 α , then α Z is the latitude, by Inf 1. or from \bigoplus fet off the complement of the declination 70° o' to p, then p O is the latitude by Inf. 3. By the analemma, fet 20° o' from \cancel{E} towards P, to 10° o' from Z counted towards O, then P will be againft 10° o' from O, the required latitude.

CASE II.

The latitude and declination both north, and fun fouth, or both fouth, and fun north.

Rule. Add the declination to the zenith distance; their sum will be the latitude of the place.

E X A M P L E.

Declination 20' 00° north Latitude. Zenith distance 30' 00° south 50' 00°

But if the declination were fouth, and the fun north, the latitude would

be 50° 00 fouth.

By scale and compasses, set off the given zenith distance 30° 00' from Z to 30 towards H, and the given declination from 30 to Æ; ZÆ will be the latitude.

By the analemma, fet 20° 00′ counted from Æ towards P, to 30° 00′ counted from Z towards H; P will be against 50° 00′ accounted from O, the required latitude.

CASE III.

The latitude and declination of different names, that is the one north, and the other fouth.

Rule. Subtract the declination (which in this case, will always be the least) from the zenith distance; the remainder will be the latitude.

E X A M P L E.

Declination 15° 00' fouth Latitude. Zenith distance 65 00 fouth 50° 00'

But if the declination was north, the latitude would be fouth.

By scale and compasses, describe the circle ZHNO, from Ziset off the given zenith distance 65 degrees towards H, if in the north latitude, but towards O, if in south latitude, from 65, set off the given declination 15 to Æ; then ÆZ is the required latitude.

By

By the analemma, set 50° 00' counted from Æ towards S, to 65° 00'

from Z towards H, and P will be against 50° the latitude.

It is by this problem, that the latitude is found at fea, when the fun's zenith diffance is taken at noon; for which we may take the following general rule. If the fun and the equinoctial be both on the fame fide of the observer, consider which is nearest the zenith; and if it be the fun, no dial, the declination and zenith distance must be added; but if it be the equinoctial, the declination must be subtracted from the zenith distance.

Those that live within the tropicks, will sometimes have the sun on one side, and the equinoctial on the other side of their zenith, and then

the zenith distance must be subtracted from the declination.

Those that are so remote from the equinoctial, that the sun performs the diurnal revolution above the horizon, will have him twice in their meridian every 24 hours: In this case, instead of the declination, take the complement of it, or the sun's distance from the pole; when the observation is at 12 at night, or more properly when the sun is nearest the horizon, the latitude will be found in the same manner, as if the altitude of a star was taken, which was sufficiently explained in the last section: But when the observation is made at noon, it will be the same as in the second case of this problem.

PROB. II.

Given the latitude and declination, to find the fun's amplitude, and the bour of his rifing or fetting.

CASE I.

In order to folve this, it must be observed, that the sun by his apparent diurnal motion, describes circles nearly parallel to the equinoctial, which may be called parallels of declination, being the same as the parallels of latitude betwixt the two tropicks. The sun performs his revolution in 24 hours thro' all the meridians, and when in the meridian of the place, it is either mid-day, or mid-night; in the analemma, this meridian is that which limits the projection; the sun will be all that day somewhere in the parallel of declination, and if a meridian he drawn thro' the point where the parallel of declination intersects the horizon, it will give the hour of his rising or setting, and the degrees of the horizon intercepted between the sun, and east or west point of the horizon, is the sun's amplitude.

This being premifed, the following general rule will folve all the varieties of this problem by the analemma.

Rule. Set the pole to the given latitude, and we have the amplitudes, and hour of the fun's rifing and fetting, for any day in the year in that

latitude, by inspection.

For the day of the month being given, the declination may be found by the table, or by looking for the sun's place in the ecliptick, on the analemma; the degree of the horizon cut by the parallel of declination is the required amplitude, and the meridian passing thro' the sun, when in the

horizon, gives the hour.

By scale and compasses, describe the circle Z H N O as before, Let the given latitude be 50° oo' north, and declination 23° 30' north. Set off by the line of chords 50° oo' from O to P, and draw the line P S, and at right angles to it, the line E A C, which will represent the equinoctial; draw the parallel of latitude 23° 30', to intersect the horizon in x; thro' x draw a meridian, to intersect the equinoctial in y. Cx is the amplitude measured on the line of sines, and Cy measured on the same line, gives the degrees and minutes of the equinoctial before or after fix, which converted into time, gives the hour of the sun's rising or setting.

E X A M P L E.

In 50° 00' north latitude.

Decl. north.	Amp.	Sun rife.	Sun fet.
Deg.	Deg. M.	н. м.	н. м.
5	7 48	5 36	6 24
10	15 40	5 I t	6 49
15	23 45	4 46	7 14
20	32 08	4 17	7 43
33 30	38 20	3 55	8 05

The amplitudes will be the fame in fouth declination, but the hours of the fun's rifing, will be the fame with the hours of his fetting, when the declination was north.

PROB. III.

Given the latitude, fun's altitude and declination, to find the azimuth and hour.

By the analemma, fet the pole to the latitude, lay a ruler, or strait slip of paper, across the given altitude; this will intersect the given parallel of declination. The meridian passing thro' this point of intersection,

gives

gives the hour; at this point make a mark with a pencil upon the ruler, then move the pole to the zenith, so as not to move the ruler; the meredian that passes thro' the pencil mark, will be the azimuth circle passing thro' the sun, and it will cut the horizon in the degrees and minutes of the required azimuth. It will be proper to take the distance with a pair of compasses, between the sun, and the line TO, or TH;

in case, the ruler should slip by moving the pole to the zenith.

By scale and compasses; let the given latitude be 50° o', declination 23° 30' both north, and altitude 20° 0'. Describe the circle ZHNO. and draw the equinoctial parallel of declination, and axis as before. Draw also the parallel of altitude alt q by setting off 20° o' of the line of chords from O to q, and from H to a; this will interfect the parallel of declination in t, thro' which draw an azimuth circle, and a meridian, and these two will give the things required. There will be no occasion to draw the whole circles, only to find the interfection of the azimuth circle with the horizon, and of the meridian with the equinoctial, which is only dividing the horizon in the fame proportion with the parallel of altitude; and the equinoctial in the same proportion with the parallel of declination: Thus, for the azimuth, draw the radius Cq, and Clq. will be a right angled triangle; thro' t draw t f parallel to C l; transfer Cf to the horizon in s, and draw s v parallel to CN; fo v O will be the azimuth. Or it may be done thus, with I q, the radius of the parallel of altitude, describe from the center C, an arch, i g produce the line t f to g; thro' g draw a line from C, which will give the point v as before. For the hour, draw the line t I parallel to P S, to intersect CE in 1, transfer C 1 to the equinoctial in 2; so shall C 2, measured on the line of fines, and converted into time, give the hour after 6.

Those are the problems that are absolutely necessary to be known at sea; the first for finding the latitude, the last two for finding the varia-

tion of the compass, of which in its proper place.

PRORIV

Given the latitude and longitude of two places; to find their distance and

angle of position.

The nearest distance between any two places will be in a plane passing thro' the two places, and the center of the earth, which upon the surface of the earth, will be an arch of a great circle; and the angle which this circle makes with the meridian of each place, is the angle of position, which will not be the same in both places.

By the analemma. Let the two places be A and B; A in 50° 0', B

F f

in 13° 30′, both north latitude; their difference of longitude 52° 58′s. B the westmost: First set the pole to the latitude of A, then look for 37° 2′ (the complement of the difference of longitude) upon the equinoctial; the meridian passing thro' that point, will intersect the parallel of latitude of 13° 30′ in the point B; thro' B lay a ruler across parallel to the horizon; its intersection with the graduated meridian, will give the distance of B from A, counting the degrees from the zenith, and will be about 56° 15′.

For the angle of polition from A to B. The ruler being laid across asbefore, mark the point B upon it; move the pole to the zenith, the meridian passing thro' the point, will be the azimuth circle required; but if it were required to find the angle of position from B to A, set the pole

to the latitude of B, and proceed as before.

By scale and compasses describe the circle, and quarter it as before. Draw the axis and equinoctial to the latitude of A, also the parallel of latitude of 13° 30': Now to find the point B in this parallel, it is only to draw a meridian, which shall make an angle of 52° 58', with the meridian of A. To do this by the line of chords, fet off 52° 581 from Æ both ways to d and d, from which two points, lay a ruler across to interfect the equinoctial in b, which will be the point in the equinoctial, thro' which the meridian of B must pass; or by the line of sines, take the complement of the difference of longitude 37° 2', which fet off from the center \mathbb{C} , and this will give the point b; thro' which draw a meridian as before directed, to interfect the parallel of latitude of 13° 30' in the point B, and thro' this point draw L T, parallel to the horizon; ZL or ZT, measured on the line of chords, will give the distance nearly 56° 15': Draw also the azimuth circle ZBG; CG measured on the line of sines, nearly 21 degrees, will give the complement of the angle of polition with the meridian of A; or thro' G, draw a line parallel to ZCN, to interfect the circle in D'and F; HD or HF, measured on the line of chords, will be the angle of position, that the meridian of A makes with the great ci cle passing thro' A and B, and will be nearly 60 degrees; but to find the angle it makes with the meridian of B, we must draw the equinoctial and axis to the latitude of B, and proceed as before.

This problem can be of little use to the mariner, because it gives the nearest distance betwixt two places, and the compass, which is the only guide he has to condust him from one port to another, leads him out of the direct road; for the path which the ship describes, will be a curve, making equal angles with all the meridians she crosses; whereas the arch of the great circle, which is the nearest distance, makes unequal angles with all the meridians; and therefore in practice, we cannot go the nearest

way, by the compass, unless the places lie under the same meridian, or

under the equinoctal.

The compass is so well known that it needs no description, being only a card, upon which a circle is described; it is divided into 32 equal parts called points, each confissing of 11° 15'; these are subdivided into quarters, without which there is another circle divided into 360 degrees; a needle, touch'd with the load-stone, by which it acquires that surprising quality of pointing to the north pole, is fixed under the card, upon which there is a flour de luce, which will point out the meridian; for though it sometimes varies from it, we may discover the quantity by celestial observation of which in another place: The lines that the ship forms in steering by the compass, are called rumbs; and that these make equal angles with all the meridians is evident, because the needle always lies in the meridian of the place, and the rumbs all meet at the center of the circle upon the card. The needle is the diameter of this circle, so that moving the card can never alter any angles, that are made by the intersection of any two lines upon it.

It will be very difficult, if not impossible, to describe the rumb lines, either upon the globe, or upon any plane, where the meridians intersect in the pole, for they must be so described, that if a ship sail upon any rumb to any port, and then sail back the same distance upon the opposite rumb, she will then return back to the same port from which she fuil'd; and that this is really true, where there is no variation or currents, or the ship is not forced out of her direct course by the sea, wind, or bad sheerage, must be allowed; and agreeable to the nature of the triangle, formed by the rumb lines, meridians, and parallels of latitude upon the globe; tho' strictly speaking, they cannot be called triangles, for the mathematicians have reduced all triangles either to plane or spherick, but the properties of neither agree to these. However as they have three fides, and three angles, a small distance may be allowed to be a strait line; we shall therefore consider them as right angled triangles.

Let there be two ports A and B, A in 50° o', B in 13° 30', and the difference of longitude 52° 58' as before, that is the diffance of the two meridians upon the equinoctial in miles, will be 3178; but in the parallel of latitude of B, the diffance of the meridians will be 3090 miles, and in the parallel of A 2043 miles; the difference of latitude betwixt A and

B, is 36° 30', or 2190 miles.

Now if a thip fail directly fouth 2190 miles from A, and then 3090 directly west, she will certainly arrive at B; and if she fails back again the same distance upon the opposite rumbs, that is first 3090 miles east,

Ff2 and

and then 2190 miles north, she will certainly arrive at A; this would make the whole diffance failed 5280 miles. But if in failing from A, she first fails 2043 miles west, and then 2190 miles south, she would likewife arrive at B; and by failing the fame distances upon the opposite rumbs. The would return back to A. Her distance sailed would be 4233 miles, but the nearest distance is 3376; supposing it possible to steer upon the arch of a great circle. The direct course by the compass from A to B, will be fouth 50° 6' west, and the distance to be failed in that course, will be 3414 miles, as shall be shewn in Mercator's failing; what we are here to prove is, that if a ship sails from B, north 50° 6' east 3414 miles, the will arrive at A. The only difficulty will be to reconcile this to the properties of a right angled triangle; for in failing from B to A, the distance 3414, is the hypothenuse; the difference of latitude 2100, is the perpendicular; and the meridian distance in the parallel of latitude of A, viz. 2043 will be the base. Now in sailing back from A to B, upon the opposite rumb, the distance, difference of latitude, and angle, will be the same as before, from whence it may be argued, that the base will be the same as before, viz. 2043; so that when the ship arrives in the parallel of latitude of B, she will be 1047 miles to the eastward of it.

But it must be considered that the whole difference of longitude to be run down from B to A, is 52° 58', which cannot be done by failing only 2043 east, unless it be all in the parallel of A. Now in failing directly upon one rumb, there is no eafting made in the parallel of A, and of confequence, all the easting that is necessary to be made, in order to run down the logitude, must be made before she arrives at the parallel of latitude of A; and the nearer to B the eafting is made, the more it will require to run down the longitude: Again, neither the whole easting, nor strictly speaking, any part of it, can be said to be run down in any parallel of latitude betwixt B and A; for if the fail from B, in the direct course towards A any assignable distance, she must make a small part of it northing, and a small part of it easting; and if she sail back upon the opposite rumb, she will make the same westings, betwixt the same parallels she made the eastings in; and because the same eastings, are made in the fame parallels of latitude that the westings are made; the difference of longitude in both, will be the fame; and the ship in failing back upon

the opposite rumb, will certainly arrive at B.

Or let us suppose 2190 parallels of latitude actually described betwixt A and B, likewise 2190 meridians. Now in failing from B to A, instead of failing the direct course, let us fail first directly east till we come to the first of these meridians; then due north again to the first parallel, and due

east to the second meridian; and so proceed failing, first north, and then east, till the last north course brings us to the parallel of A, and then an east course will bring us to A. By this means she forms 2190 small right angled triangles; the perpendiculars will all be equal, viz, one mile each, but the bases will all be unequal, still decreasing the nearer we come to A. In failing back, if we go upon the opposite rumbs, we must first sail as much west in the parallel of A, as we did east before; and then fouth to the next parallel, in which we must sail as much west as we did east before to come at the next meridian, and so proceed failing first fouth and then west, till we come to B; where it must be obferved, that in every parallel of latitude, we make as much eafling as we did westing, which will infallibly bring us back to the same port.

Now let us suppose an infinite number of parallels of latitude, and an infinite number of meridians; and let us freer an infinite number of courses, first north, and then east, we shall have an infinite number of fmall triangles, and their perpendiculars and bases being infinitely small, both may be faid to vanish, and leave nothing but the hypothenuse, which upon the globe, is represented by a curve, making equal angles with all the meridians, being the path a ship describes, which is led by the direction of the compass from B to A; and in failing back from A to B, the triangles will be the same as before, and so quite vanish, leaving only the distance, which will certainly bring the ship back to B.

We shall not here examine how these rumb lines are described upon the globe, for as we observed before, though in theory they may be conceived to be drawn, yet it will be scarce possible to draw them true, with inclin'd meridians; this shews the necessity of a projection of the fphere upon a plane, where all the meridians may be parallel to each other; in this case the rumbs will all be strait lines. How to construct

fuch a projection, shall be the subject of the next chapter.

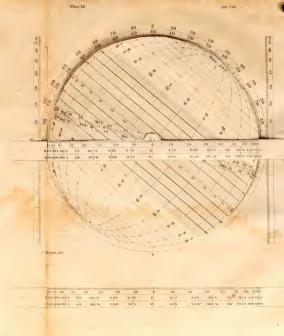
We shall only here remark that in navigation, the departure, and meridian distance, may be considered as one thing, viz. The whole easting, or westing that a ship must make in steering upon a direct course from one port to another; and this will always be equal to the fum of all the departures made every 24 hours, but will not agree with the common definition of departure and meridian distance, as in Def. 10. for by that, we can affign no proper departure betwixt any two places, that are not in the fame parallel of latitude; for let the two places be A and B, the distance betwixt their meridians, in the parallel of A will be 2043 miles, and in the parallel of B 3000 fo that neither of these can properly be called the meridian distance, or departure betwixt these two places; but if we sail

in a direct course, viz. south 50° 6' west from A 3414 miles; we shall make 2619 westing when we arrive at A, which we shall call the departure, or meridian distance betwixt A and B, and in sailing back from B, the course will be north 50° 6' east; the distance 3414, and the east-

ing 2610, the same as the westing before.

From this we may infer that the same course and distance, whether we steer from or towards the equator, will always give the same difference of latitude and departure; which is the reason that several experienced artists keep their account by their meridian distance, without regarding their longitude; for we must not suppose, as some have alledged, that they are ignorant of the cause why they make more westing in going towards the equator, than they make eafting in returning back, for they well know that (outward bound) they get into the parallel of their port, long before they run down their difference of longitude, which therefore must require more departure than in coming home; because that it is possible they may have 6 or 8 degrees of longitude to run down in the parallel of 13° 30' when failing to B; and the fame number of degrees of longitude to run down in the parallel of 50° o', when failing from B to A. So they do not return near the opposite rumb to that on which they failed out; but as they constantly steer the same courses out every voyage, as near as the wind will permit, in the course of many voyages, they find the meridian distance nearly the same every voyage outward bound; and if in feveral voyages they can fleer the fame courses home, that they steered home the preceding voyages, they will find their departures nearly the same as in their former voyages, tho' always less than the departures out, for the reasons before affigned: But it happens fo rarely, that they can keep the fame courses two voyages; that very few have any regard to the meridian distance, but keep their account by the difference of longitude, which will always be the fame out and home, whatever courses they steer.





C H A P. III.

Of PLAIN SAILING.

S E C T. I.

The CONSTRUCTION and USE of SEACHARTS.

The LONG-LINE, and HALF MINUTE GLASS.

LAIN failing is that where the plain chart is used, all the various cases of which will be exactly the same with those of right angled triangles; so that we are only to shew how those triangles are formed upon

the chart; and the names of the fides.

In this chart the meridians are strait lines drawn parallel to one another; the equinoctial, and all the parallels of latitude are likewise strait lines parallel to one another; by this means the rumbs will be strait lines, and make equal angles with all the meridians, but then all the parallels of latitude will be equal to the equinoctial, which is a very great error, at any constructed in the same manner as that of surveying land inchart, and constructed in the same manner as that of surveying land inchart, and constructed in the same manner as that of surveying land inchart, and constructed in the same manner as that of surveying land inchart, and constructed in the same manner as that of surveying land inchart, and those parallel to B E, parallels of latitude; which being all equal to the equinoctial, will make the departure and difference of longitude the very same thing, though in the parallel of latitude of 60 degrees, it is only one half of the difference of longitude; and if nearer the pole, the error will still be greater, so that this chart must be very erroncous.

The only true fea chart is *Mercator's*, which retaining the parallelism of the meridians, will occasion the degrees of longitude in any parallel, to be equal to the same degrees in the equinoctial, as in the plain chart; but to remedy this, the degrees of the meridian in this chart, are enlarged in the same proportion that the degrees of the parallels of latitude are. Before we shew the construction of this chart, we shall shew all the uses of the plain chart; for as there are two sea charts, from hence arises the division of navigation in two parts, viz. plain, and *Mercator's* failing;

we shall here treat of the first.

Every place is supposed to have a meridian, and parallel of latitude, and if actually drawn, and likewise a strait line from any place to another, that differ both in latitude and longitude; we shall then have a roll of a roll of the strain and the strain and the strain are later to the strain and the strain are later to the strain are strain as a stra

angled triangle, whereof the meridian will be the perpendicular, the departure the base; and the distance the hypothenuse: Let the two places be A and Z, A a or Z z, will be the perpendicular; a Z or A z, the base; and A Z, the distance upon the rumb line; and that A a is the difference of latitude, and a Z the departure; betwixt A and Z, is evident by the definition of those terms: The angle that is formed by the rumb line, and the meridian, is called the course, which corresponds to the angle opposite to the base in trigonometry.

As in trigonometry there are fix cases, so there are the same in plain sailing, and the solutions the same in both, only changing the names of the parts. The hypothenuse, is called the distance; the perpendicular is called the difference of latitude; the base is called the departure; and

the angle opposite to the base, is called the course.

Now here, as in trigonometry, there are four things, any two of which

being given, the other two may be found.

The mariner has two things given, viz. the course and distance; the former by the compass, and the latter by the log-line and half minute

glafs.

To the end of this line there is fastened a piece of wood, with as much lead at the lower end as will ferve to make it swim upright in the water: It is divided into knots, the distance betwixt the knots must be exactly the 120th part of a mile; and there must be a sufficient quantity of line betwixt the log, and the mark from which the line begins to be diveded; fo that when the mark is at the ship's stern, the log may be clear of the eddy of the ship; and then the half minute glass is turned, and the line vereed of the reel, which is stopped as soon as the glass is out: this will give the exact distance the ship has sailed in the half minute; and if she continues at the same rate for a whole hour, her distance run in the hour is also known; for she will go as many miles in the hour, as there are knots run out in the half minute; this is the only method they have to measure the distance, and may be liable to great errors unless the line be very carefully divided, and the glass actually half a minute.

SECT. II.

The Resolution of the fix Cases of PLAIN SAILING.

HE most expeditious way, and which is always used in practice. is by the table of difference of latitude and departure.

This table gives, by inspection, the difference of latitude, and depar-

ture, to any course, for any distance less than 100 miles.

In the uppermost rank, are placed the courses from 1 degree to 45, including points and quarter points; and in the lower rank, the courfes from 45 to 90; each course is divided into two columns; under lat, is the difference of latitude; and under dep. is the departure; and under dift, is the diftance corresponding to them; but when the course is more than 45 degrees, it will be found in the lower rank; and the difference of latitude over lat. and the departure over dep.

We shall work an example in each case, by the logarithms, by scale and compasses, and by these tables which will sufficiently explain their nature: We shall likewise shew how to delineate them by the line

of rumbs.

CASE I.

Given the course and distance, to find the difference of latitude and departure.

XAMPLE.

A ship fails SWbW 60 miles. I demand the latitude come to, and departure.

This is exactly the same with the first case of trigonometry, and the triangle delineated in the same manner, only we make use of the line of

rumbs to fet off the angle by.

The line of rumbs is constructed in the same manner as the line of chords, from a quarter of a circle, divided into 8 equal parts, for points of the compass, and those sub-divided into quarters; the use of this line is to fct off the course, which is always given in points of the compass, and not in degrees; as in this example the course is five points from the meridian; therefore upon the line R T, from the point R, describe an arch with the chord of 60 degrees, upon which fet off five points taken

from the line of rumbs; this might be taken off the line of chords, tho' not so exactly, because of the odd minutes; being 56° 15', so that in all the cases in navigation, we shall make use of the line of rumbs, observing that the arch must be described by the chord of so degrees, to which that line of rumbs is adapted. We shall give no further directions for delineating the following examples, only refer to the like cases in trigonometry. In order to work them by the logarithms, the points must be turned into degrees, for which there is a table to find them by inspection; 5 points is 56° 15', then it will be,

As the radius or fine of 90		-	10.000000
Is to the distance 60 miles			1.778151
So is the fine of the course 560	15,	-	9.919846
To the departure 49.9 miles	-	•	+1.697997
As radius	-		10.000000
Is to the distance 60 miles-		-	1.778151
So is S. C. of the course 33° 4			9.744739
To difference of latitude 3.3.3:	miles	-	+1.522880

By the table of difference of latitude and departure, the course is more than four points, therefore it will be sound in the bottom, that is 5 points; and in the column over lat. is 33.3, for the difference of latitude; and 49.9 in the column over dep. for the departure, both right against 60 in the column dift.

By extending on Gunter's scale, if the course be turned into degrees,

it will be just the same as was in right angled triangles.

But there are two lines on Gunter's scale by which it may be done, one is marked SR, and the other TR; that is the fines and tangents of the rumbs; and as the sine of 90 degrees, and the tangent of 45 degrees are equal to the radius, so 8 points is for the radius on the line sine rumb, and 4 points for the radius on the line tangent rumb.

For the departure R: S 5 points: 60: 50 nearly. For the difference of R: S 3 points: 60: 33.3.

The extent from 8 points to 5 points on the line 8 R, will be the same as from 90 to 56° 15′ on the logarithmick line of sines, and will reach from 60 to 50, on the line of numbers for the departure; the extent from 8 points to 3 points, will be the same as from 90 to 33° 45′ on the logarithmick sines, and will reach from 60 to 33.3 on the line of numbers for the difference of latitude.

CASE II.

Given course and difference of latitude, to find the distance and departure,

EXAMPLE.

A ship sails SEbS, till she alters her latitude 50 miles; I demand her distance and departure.

This is exactly the same triangle with the preceding, but what was the difference latitude before, is now the departure; the proportion will be,

As line comp. of the course, viz. 56° 151	9.919846
Is to the difference of latitude 50 miles	1.697997
So is the radius or fine of 90	10.000000
To the distance 60 miles	1.778151
As fine comp. of course or of 56° 15'	9.919846
Is to the difference of latitude 50 miles	1.697997 11.442736
So is the fine of the course 33° 45'	9.744739 \$ 9.919846
To the departure 33.3 miles	1.522800 1.522800

By the table of difference of latitude and departure, the course is now three points, find it in the upper rank, and under lat. find 50 the given difference of latitude; corresponding thereto under dist. is 60, and under dep. is 33.3.

By Gunter's scale, S of 5 points: fine of 8 points:: 50:60; the extent from 5 points to 8 points, on the line S R, will reach from 50 to 60 on the line of numbers and gives the distance.

For the departure S of 5 points: fine 3 points:: 50:53.3.

CASE III.

Given course and departure to find the difference of latitude and distance.

EXAMPLE.

A ship sails N W by W till she gets 50 miles to the westward; I demand the distance and difference of latitude; this is a case that can scarce ever happen, and is the same with the preceding, only calling what was difference of latitude in the former, in this the departure, and what was departure in the former, is now difference of latitude; and then the operations will, in all repects, be the same as before.

Gg2

CASE IV.

Given the distance and difference of latitude; I demand the course and departure.

E X A M P L E.

A ship sails betwixt the south and west 60 miles, and finds by a good observation, she has made 50 miles southing; I demand the course and departure, delineate the triangle as in Case 4. right angled triangles; the proportion is

As the distance 60 miles	~	-	_		1.778151
Is to difference of latitude	50 miles		-	-	1.697997
So is radius or fine of 90	•	-	- ::		10.000000
					11.697997
To the S. C. of the course	56° 15'				9.919846

So the course will be S. W. b S. the departure will be found by

Case 1. or 2.

By the table of difference of latitude and departure, turn over till you find 50 in the difference of latitude column, and 60 in the diffance column; and because I find 50 in the column that has lat. at the top, the course will be there also, viz. 3 points, that is S. W. b S. and in the departure column I find 33.3 westing.

By Gunter's scale; the extent from 60 to 50, on the line of numbers,

will reach from 8 points to 5 points on the line S R.

CASE V.

Given distance and departure, to find the course and difference of latitude.

EXAMPLE.

A ship sails betwixt the north and east 60 miles, till her departure is 50 miles; I demand her course and difference of latitude. This is exactly the same with the preceding, and scarce can happen, so we shall proceed to the next.

CASE. VI.

Given difference of latitude and departure, to find the course and distance.

E X A M P L E.

Two iflands P and T, T in 32° 41', and P in 20° 53' both north latitude;

titude; P lieth to the westward of T 6° 45'. I demand their bearing and distance, or which is the same thing, what course must be steer'd from P to T, and how many leagues distant; delineate the triangle as in Case 6 trigonometry, and find the difference of latitude by subtraction, which turn to leagues off 20 to one degree, as in the operation.

A	32	41			Departur
В	20	53			20
	11	48			120
	20				15
	220 1	eagues			135 depart
	16 f	or 48 mi	les		
	236 0	liffe. of l	ati. in lea	gues	

The proportion is,

As the difference of latitude 236 miles	2.372912
Is to the departure 135 miles	2.13.334
	10.00000
So is the radius or tangent of 45	12.130334
To the tangent of the course 29° 461	9.757422

By the table of difference of latitude and departure, these numbers are too large to be found in the table, therefore take the quarter of each, so 59 will be for the difference of latitude, and 33 \frac{1}{4}, the departure; find these in their proper columns, and corresponding thereto in the distance column, will be 68 or 69, which multiplied by 4, will give the whole distance; and because the difference of latitude is greater than the departure, the course will be found to be near 30 degrees, and taking 68.5, which is the nearest distance corresponding to the difference of latitude and departure; in the tables, the whole distance will be 274 leagues, and the course from P to T, will be S, S, W. \(\frac{1}{2}\) W 2 degrees westerly.

By Gunter's scale; the extent on the line of numbers from 236 to 135, will reach from the tangent of 45 to 30, or 60 degrees on the line of tangents: Now to know which of these two will be the angle, observe which is greatest, the difference of latitude or departure; for if the difference of latitude be greatest, as in this example, the angle will be less than 45 degrees, but if the departure be greatest, the angle will be more

than 45 degrees.

There are all various cases in plain failing, which being well understood, it will be easy to give a true solution to the following questions, by the table of difference of latitude and departure: For it will be too tedious to work them by the logarithms, or conftruct them geometrically; therefore in practice we always use the tables, and for the proof, let them be performed by *Gunter*'s scale.

A ship in 22° 51' north latitude, sails N. N. & W. 83 leagues the lati-

tude come to, and departure from the meridian is required.

A ship in 0° 56' north latitude, sails S b W \ W, till by a good observation she is 1.13 south latitude; her distance and departure is required.

A fhip in 36° 40' fouth latitude, fails betwixt the N and E, till fhe gets into 34° 50' fouth latitude, and finds by the log, she has run 63

leagues; the course and departure is required.

Two islands A and B, A in 2° 2' north latitude; B in 5° 16' fouth latitude; B lies 250 leagues to the westward of A; the course and distance is required.

S E C T. III.

Of working a Traverse, or reducing various Courses into One.

Being now provided with a good fea chart, to find the bearing and distance of any two places and with alto with a log line, and half minute glass, to know how far we have advanced towards our port; we need only keep an exact account of the distances, by fetting down every day at noon, the number of miles failed the preceding 24 hours, in a book provided for that purpose: Now if at any time we want to know our distance from the port we are bound to, it is only collecting the feveral distances we have failed every 24 hours, and fubtracting the fum from the whole distance: the remainder will be the distance we are from our port: But as it is impossible to keep a ship in her direct course, by reason of contrary winds, the intervention of lands, or various other accidents, which forces her out of the direct course; it will be absolutely necessary to keep an exact account of every particular course and distance, failed in 24 hours; and then reduce all these different courses and distances into one: This is what is called a traverse, and is only so many different questions of the first case of plain failing; for after we find the differences of latitude and departure, to every particular course, if they are in the same quarter of the compass, we may collect all the differences of latitude into one; which will be the whole difference of latitude, from the first port sailed from, and the sum of all the departures will be the whole departure; and having the difference of latitude and departure, the course and distance is found by the last case of plain sailing. If some of the differences of latitude be northerly, and some southerly, add the several northings together, and also the several southings; if they are equal, the ship has not altered her latitude, if unequal, subtract the less from the greater, the remainder will be the whole difference of latitude; do the same by the departure when there are eastings and westings. The whole art of navigation depends upon keeping a correct and distinct account of these various courses, and reducing them to one: For which purpose it will be proper to make a table of fix columns, as the following:

Courfe.	Distance.	North.	South,	East.	Weft.
S. E.	38	0.0	26.9	26.9	0.0
S. E. b E.	42	0.0	23.3	34.9	0.0
E. S. E.	25	0.0	9.6	23.1	00
E.	30	0.0	0.0	30.0	0.0
E. N. E.	15	5.7	0.0	13.9	0.0
N. W.	24	17.0	0.0	0.0	17.0
W. S. W.	17.	0.0	6.5	0.0:	15.7
		22.7	66 3	128.8	32.7
Courfe good:	Distance.		22.7	32.7	
S. 66° E.	106		43.6	96.1	},

In the first are the several courses; in the second their corresponding distances; then by the table of difference of latitude and departure, find a difference of latitude and departure to every course and distance, and set them down in their proper columns, sum up all the northings, is 22.7, which subtract from 66.3, the sum of the southings; there remains 43.6 miles of south difference of latitude; the sum of the eastings is 128.8, from which subtract 32.7, the sum of the westings; there remains 96.1 miles east departure. As this number exceeds the limits of the table, take half of it 48; take also half the difference of latitude 21.8; the nearest I can find to these two in the tables, is 21.6 and 48.4 in the column over 66 degrees, and in the distance column is 53, which doubled, makes 106 for the whole distance.

By this way of keeping an account, we may at any time, know the course and distance to the port sailed from, which suppose in 30° 30′ north latitude, and likewise the course and distance to the port bound toy which suppose in 20° 18′ north latitude, and 72 leagues to the eastwards. Let the port sailed from be A, and the port bound to B; the difference

of latitude will be 24 leagues, and the departure 72; the course will be nearly E. S. E. ‡ E. about 77 leagues distant; but after steering the several courses, as in the table, the ship arrives at C. I find by the preceding calculation, the whole difference of latitude made from A to C, is 43.6 miles southing; and the whole departure 96.1 miles easting; therefore subtracting the difference of latitude made from A to C, from the whole that was to be made from A to B; the remainder will be the difference of latitude yet to be made, and subtracting the departure made, from the whole that was to be made at first setting out, the remainder will be what is yet to be made: And so having the difference of latitude and departure given, by them the course and distance is found. See the operation.

Difference of latitude from A to B

72 miles

72 miles

43.6 miles.

Difference of latitude from C to B 28.4 miles is 9 ½ leagues.

Departure from A to B
Departure from A to C
Departure to be made from C to B
Departure to be made from C to B

The nearest I find to those two in the table of difference of latitude and departure are 39.9, and 9.2; so the course will be S. 77° W. 41

leagues distant.

By this it is evident, that it is first absolutely necessary to know the whole difference of latitude and departure, that is to be made before we set out. Secondly, we must keep an exact account of the various courses and distances seered, by which we may at any time know how much of our difference of latitude is made, and consequently by subtraction, we may always tell what difference of latitude and departure we have to make; all this may be done without a chart, by a table of latitude and longitude of places.

The geometrical conftruction of a traverse would be too tedious for practice, but as there are several small islands, rocks, and lands, laid down in a chart, that are not in the tables of latitude and longitude; it will not be improper, every day at noon, to mark the place the ship is in upon the chart; by this means we may have a view, not only of our port, but also of any rocks or sands; this is especially necessary when we come near to

the land, we shall therefore shew how this is to be done.

S E C T. IV.

To prick the PLAIN CHART. (Plate X).

HIS is to lay down the place the ship is in at any time, or to find the bearing and distance of any two places upon the chart.

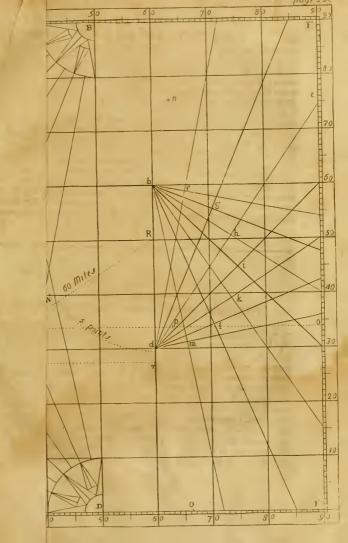
Suppose a ship bound from A to O; required the course and distance. There are feveral compasses, or rumb lines upon the chart, by which the course may be readily found; thus, lay the strait edge of a ruler so that it may touch the two places A and O, then take a pair of compasses, and placing one foot in the center of any compass, open the compasses till the other foot touches the edge of the ruler; then fliding the compasses with one foot by the edge of the ruler, the other foot being perpendicular to it, will trace out the rumb line on which the ship must steer: Now as the rumbs are only drawn to the whole points, it may happen, as in this case, that the foot of the compasses will not fall exactly in the rumb. but we may eafily estimate the quarters; so the course from A to O, will be S. E. b S & E. A C, is the whole difference of latitude; suppose oo leagues, CO the whole departure 66 ½ leagues. Now it is certain if we fail oo leagues fouth, and then 66 1 leagues east, we shall arrive at O; but I find by my account, that I have made only 14 leagues fouthing, and 35 leagues easting: Now I want to know what place I am in, that I may steer a direct course for O. To find this, provide two pair of compasses: In one take the difference of latitude 14 leagues, which fet off in the line A C from A to e; with the other pair take the departure 35, which fet off from C to r in the line C F; from r with the difference of latitude, describe an arch, and from e, with the departure describe another arch, to cut the former in s, which is the point the ship is in at the time the calculation is made, and may be done every day at noon, or if need be at any other time. The next day at noon, after reducing the various courses to one, I find I have made, in that time, 42 leagues fouthing, and 28 leagues eafting; I want to know the place the ship is in: If the points, where the thip was the day before, be at the interfection of a meridian, and parallel, we may find it by the same method we found the point s the day before; if it is not, take with one pair of compasses, the nearest distance of the point s, to any parallel; with another pair of compasses take the departure 28, with which describe an arch from s as center; then slide the first pair of Hh com-

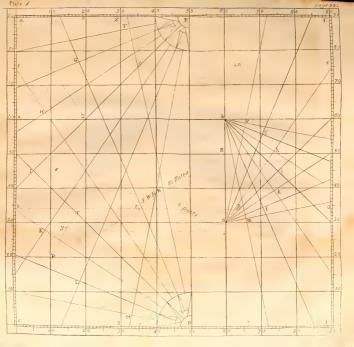
compasses with one foot in the parallel, and the other perpendicular to it. till it cut the arch in n; again with one pair of compasses, take the nearest distance of the point n to a meridian, and with the other pair take the difference of latitude 42, and describe an arch from the point n as center, and move the first pair upon the meridian, till it cut the arch in p, which is the place the ship is in. After the same manner we may find the place the ship is in every day at noon: When the chart is not very large, it may be done thus; let the ship be in s as before; first lay a ruler across the chart. let the edge be parallel to some east or west line, and passing through s, mark the two points e e, where the ruler cuts the two lines that limit the chart, then take the difference of latitude 42, and fet it from e and e to o and o, and lay the ruler across by these two points. It is plain the thip must be some where in the line oo; to find which, take with a pair of compasses, the nearest distance of the point s, to any meridian; obferve where that meridian cuts the edge of the ruler; from this fet off the distance in the compasses by the edge of the ruler to t; then taking the easting 28, it will reach from t to p, which is the place the ship is in.

C H A P. IV.

Of Mercator, middle Latitude, and parallel Sailing.

E have now fully explained all the varieties of failing by the plain chart, but it is subject to very great errors, for by making all the parallels of latitude equal to the equinoctial; the difference of longitude betwixt any two places will always be equal to the departure, whereas in fact the difference of longitude, may be sometimes double, or treble, and always more than the departure, except when the two places are upon the equinoctial. To illustrate this, let there be two islands A in 32° 41′, and B in 20° 53′, both north latitude, and let their difference of longitude be 7.15, or 145 leagues, that is to say, if there be a meridian drawn thro' A, and one thro' B; their greatest distance will be upon the equinoctial, viz. 145 leagues, but these meridians continually approach one another, till at last they meet in the pole, therefore their distance in the parallel of 20° 53′, will be less than 145 leagues; let it then be 135 leagues, and their diffance





stance in the parallel of 32° 41', will be still less than their distance in the parallel of 20° 53', which suppose 121 leagues; the disserence of latitude from A to B, is 236 leagues, so if a ship at A sails 236 leagues due north, and then 135 leagues due east, she will certainly arrive at B; again if the sails from B 236 leagues due north, and then 121 leagues due west, she will arrive at A, but by the principles of the plain chart, she must sail 135 leagues, which makes an error of 14 leagues; and if the two places were more to the northward, the error would still be greater.

SECT. I.

Of the Principles of MERCATOR's Chart.

O remedy this error, a new chart must be made, in which the degrees of any parallel, shall have the same proportion to the degrees of the meridian, that they actually have upon the globe; but this must not be, by inclining the meridians, because the rumb lines would make unequal angles with them: The meridians then must continue parallel to one another; this will make a degree in any parallel, equal to a degree in the equinoctial, which is a monstrous error; for a degree in the parallel of 60, is but half a degree in the equinoctial: Therefore in this chart, the degree of the meridian that lies betwixt 59° 30′, and 60° 30′, must be double the degree that lies betwixt the equinoctial, and the first degree upon the meridian, that is supposing the parallel of latitude of one degree to be 60 miles distant from the equinoctial; then the distance betwixt the parallel of 59° 30', and the parallel of 60° 30' must be 120 miles: This will occasion the meridian to be unequally graduated, and suppose a parallel of latitude be drawn thro' every degree of the meridian, the distances betwixt these parallels will be unequal; that betwixt the first and the equinoctial will be the leaft, but it increaseth the further the parallel is removed from the equinoctial, in the fame proportion that the parallel is less than the equinoctial.

In order then to graduate the meridian, let us suppose a degree of the equinoctial, or of the meridian, which are both great circles, to be 60 miles; the parallel of 1 degree of latitude, is very near as great as the equinoctial, and so the first degree of the meridian will be 60 miles; in like manner the parallels of 2, of 3, of 4, of 5, are so near the equinoc-

Hh2

tial, that the distances betwixt them may be all equal, that is 60 miles; but then the parallels begin to decrease very perceptibly, and therefore the distance betwixt the parallel of 5 and 6 will be 61, and the distance betwixt the parallel of 6 and 7, will be a little more, and still increasing; fo the only difficulty will be to graduate the meridian. The first thing to be done, is to calculate how many miles will make one degree in any parallel of latitude, for which take this proportion:

As the radius, is to the fine complement of the latitude, -fo is 60 the miles in a degree upon the equinoctial, to the number of miles that will be contained in a degree in that parallel, or which is the same thing.

R: S. C. latitude: : difference of longitude: departure.

DEMONSTRATION. (Plate 11. Fig. 1.)

Let Æ Z be the latitude, then will Z P be the complement; Z z the radius of the parallel is the fine of the complement angle P C Z. Now the degrees of one circle are to the degrees of another, as the radius of the one is to the radius of the other, as was proved in part first. Therefore Æ C, the radius of the equinoctial is to Z z, the radius of the parallel, or fine complement of the latitude, as a degree of the equinoctial, or difference of longitude, is to a degree of the parallel or departure.

By this calculation it will be found that a degree upon the parallel of 60 degrees, will contain but 30 miles; for the complement of 60 is 30, and the fine of 30 degrees, is half the chord of 60 degrees, or half the radius; so the diameter of the parallel of 60, is half the diameter of the

equinoctial.

Tho' this proportion be true, it would be a great labour to make tables by it, which Mr Wright has effected by another method; for he confidering that the radius is to the fine complement as the fecant is to the radius, calculated a table of meridional parts, by a continual addition of the secants. In this chart the fine complement is equal to the radius, because the meridians are parallel to each other; so the degrees of the parallel are all enlarged beyond their due measure, and therefore the degrees of the meridian must be enlarged in the same proportion, which will be as the secant of the parallel is to the radius; to prove this, let CB be 60 miles, equal a degree of the equinoctial (Plate 11. Fig. 3.) with this, as radius, describe a circle, and draw the parallel FE; it is plain DE would be a degree in that parallel; but upon the chart it is DG. In the triangles DEC, and ACB, the angles ACB, and DEC, are equal being alternates, to the two parallels DG, and CB; the angles at D and B, are right, therefore the triangles are fimilar, and CE: DE:: CA: CB, but in Mercator's chart D E'is enlarged till it is equal to C E; therefore to keep the same proportion, CB must be enlarged till it is equal to CA, that is if CB be a degree of the meridian at the equinoctial, CA must be a degree of the meridian at the parallel FE; by this means, it will be enlarged in the same proportion that a degree of a parallel is enlarged: Now let DE be the parallel of 30°, if 60 miles be a degree of the equinoctial; then 51.96 should be a degree in this parallel, as in the following operation; but it is enlarged to 60, therefore the degree of the meridian, that lies betwixt the parallel of 29° 30', and the parallel of 30° 30', must be enlarged in the same proportion; that is 51.96:60::60:69.28; for 60 x 60-51.96=69.28. (See the operation by the logarithms). The complement of the parallels is 60 degrees; therefore

As radius!	10.0000000		1.778151
Is to fine of 60°	9.937531 1.778151	>	3 556302
So is 60 miles in the equator To 52 miles in the par.	+1.715082-		1.715682
10 52 miles in the puss	1 - 7 - 3	69.23	1.840620

So a degree in the meridian at the parallel of 30 degrees of latitude must be 69.28 miles, and that this is equal to the secant of 30 degrees, will appear by the following operation.

As radius	10.0000000
Is to the fecant of 30°	10.062469.
So is 60 miles	1.778151
To 60.28 miles	+1.840620

By the same manner, we may find the number of miles that will make a degree of the meridian in any latitude; but Mr Wright has constructed tables of meridional parts in fuch an excellent manner, that the meridian.

by them may be very eafily graduated.

In this table, we find by inspection, the number of miles that any parallel of latitude is distant from the equinoctial; fo the parallel of 290 30', will be 1854 miles from the equinoctial, and the parallel of 30° 30' will be 1923; the difference is 69, which must therefore be a degree of the meridian at that parallel.

The manner Mr Wright calculated this table, was by a continual addition of the fecants, which he calculated even to minutes, with the utmost care and exactness; he assumed 60 equal parts for a degree of the equinoctial, and therefore the first five degrees of the meridian would be OHC:

one of those equal parts each, because if the radius of a circle be 60 equal parts, the sccants of 1, 2, 3, 4, 5 degrees, will be 60 near equal to the radius, that they may be accounted 60 each, so the sum of those sccants will be 300 equal parts; these are called meridional parts, and shew the distance of the parallel of 5 degrees from the equinoctial: The sum of all the sccants from the equinoctial to the parallel of 29° 30′, is 1854, which is the distance of that parallel from the equinoctial: Now if it be required to find the distance of the parallel of 30° 30′ from the equinoctial; find the sccant of 30°, which will be 69, and this added to 1854, makes 1923, which exactly agrees with the meridional parts in the tables, corresponding to 30° 30′ latitude. Having thus shewn the construction of the table of meridional parts, we shall now shew its use in making Mercator's chart.

SECT. II.

To make MERCATOR's Chart. (Plate 13).

HIS may be made to contain all the known parts of the whole world, which is called a general chart, or to contain only a part of it, which is called a particular chart; and as they are both projected in the fame manner, we shall only shew how to make one from the latitude of 30 degrees to the latitude of 60 degrees, and to contain 44 degrees of longitude. Draw the line AB, to represent the parallel of 30 degrees, which make 2640 equal parts, being the miles in 44 degrees, upon the equinoctial, or in any parallel of latitude; then draw the perpendiculars CA and DB, to represent two meridians; and to find the parallel of 60, look for it in the table of meridional parts, from which subtract the meridional parts of the parallel of 30; the remainder will give the distance betwixt these two parallels, as in the following operation it is 2640, which set off by the same scale of equal parts,

60-4528 30-1888 2640

from A to C, and from B to D, and draw the line C D, to represent the parallel of 60 degrees, thus the chart is limited; then draw another meridian any where at pleasure, to meet the parallels A B and C D.

This

This is called the first meridian, where the longitude is supposed to begin; from which graduate the parallel into degrees both ways, and at every tenth draw a meridian, as in the draught where they are numbered 10° 20′, &c. on each side of the first meridian; then graduate the first meridian into degrees; and at every tenth draw a parallel numbered 30, 40, 50, 60. Now to find the number of equal parts, or which is the same thing of equinoctial miles betwixt these parallels, proceed thus:

	Mer. parts.	Diff.
60	4528 1888	2640
30	1888	5 2040
50	3475 188	1587
30	188	5 1507
40	2623	1
30	1888	735

In the first column are the degrees of latitude; in the second, the corresponding meridional parts; and in the third, the distance of each parallel from the parallel of 30 degrees. We must proceed in the same manner, to find the distance of each degree from the parallel of 30, or from one another, and where the scale will permit, the degrees may be divided into minutes; the meridians A C, and B D, may be graduated, also the parallels A B, and C D, and the places laid down according to their true latitudes and longitudes; or if the places be actually laid down their true latitudes and longitudes may be found, and also their bearings and distances by the following problems.

PROB. I.

Having the latitude and longitude of a place; to find it upon the chart.

EXAMPLE I.

I want to find the lizard, which by the tables, is in 50 degrees north

latitude, and in o longitude.

Look on the graduated meridian for 50 degrees of latitude, where in this chart, there is actually a parallel drawn, and because the lizard has no longitude, it will be at the intersection of the first meridian with that parallel.

EXAMPLE II.

I want to find the island of *Madeira* in the chart, whose latitude is 32° 17' north, and longitude 12° 8' west.

Look on the graduated meridian for 32° 17'; then with a pair of com-

passes take the nearest distance of that point to any parallel of latitude; find upon the graduated parallel 12° 8', on the west side of the first meridian, and with another pair of compasses take its nearest distance from any meridian; move both compasses, keeping the foot of the first in the parallel of latitude, and the other in the meridian, till the other two seet of the compasses meet, which will be the place required; observing to move the compasses fo that their points be parallel either to a meridian or parallel. Or it may be done as in the plain chart, by laying the strait edge of a ruler across the chart, parallel to some east and west line, to interfect the meridian in 32° 17', the given latitude; then with a pair of compasses, take 12° 8', the given longitude, which set off by the edge of the ruler, from the point where the ruler intersects the first meridian, this will give the place required.

PROB. II.

To find the latitude and longitude of any place in the chart: This is only the reverse of the former.

Let the latitude and longitude of Madeira be required.

With a pair of compasses take its nearest distance to any parallel of latitude, which set off from the intersection of that parallel, with the graduated meridian and it will be found to be 32° 17'.

For the longitude, take its nearest distance from any meridian, which set off from that meridian upon the graduated parallel, and it will give 12° 8'.

PROB. III.

To find the bearing and distance of any two places upon the chart. The course is found in the same manner as upon the plain chart.

The distances in this chart cannot be measured, as on the plain chart, at once, by a scale of equal parts; for a degree of the meridian upon the globe, is at all places equal to a degree upon the equinoctial; and therefore if two places lie in the same meridian, their proper difference of latitude will be their true distance, as in the following.

EXAMPLE.

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Now tho' the real distance betwixt these two parallels upon the earth be 1063 miles, yet upon the chart it is 1427; so in this chart the distances are not truly set down, except the places lie under the equinoctial, but there is a certain method of finding the true distances, by these laid down in the chart; which admits of sour different cases.

CASE I.

If the two places lie under the fame meridian, then the proper difference of latitude turned into miles, is the real distance, as in the afore-faid example.

CASE II.

If both places lie under the equinoctial, then the distance is truly meafured upon the equinoctial.

CASE III.

To find the distance of two places lying in the same parallel of latitude.

In all *Mercator*'s charts there is a direction how this is to be found, but when the places are at any confiderable diffance, it will be very erroneous, as will appear in the following example.

EXAMPLE.

Let the two places be in the parallel of 50° 0′, and their difference of longitude 42 degrees, which is 2520 miles, and is the real diffance betwixt them upon the chart, when measured upon the equinoctial, or graduated parallel; but their true diffance upon the parallel, is 1620 miles, which will make 42 degrees of the parallel of 50° 0′, tho' it will take 2520 miles to make 42 degrees upon the equinoctial, for R: sine of 40: 2520: 1620; so the true diffance in the parallel is 27 equinoctial degrees.

The chart directs to take the distance betwixt the two places with a pair of compasses, and apply it to the graduated meridian, in such a manner, that one foot may be as many degrees above, as the other is below the parallel; the degrees intercepted between the feet of the compasses, allowing 60 miles to one degree, will, according to their direction be the true distance in the parallel; so that 2520 miles taken upon the equinoctial, which is the real distance upon the chart, should reach in the graduated meridian from 36° 30', to 63° 30', the one being as much

above

above, as the other is below the parallel of 50° o'; for the true diffance in the parallel is 27 degrees, the half of which, 13° 30', being added to 50, gives 63° 30', and subtracted from 50, gives 36° 30'; but the diffance betwirt these parallels upon the chart is 2617 equinoctial miles, as by the operation, which will occasion an error of 997 miles.

63° 30' 4972 meridional parts 36° 30' 2355 2617 difference.

To remedy this, instead of the former take the following method. Rule. Open the compasses till one foot is half a degree upon the meridian below, and the other foot half a degree above the parallel of latitude; count how many times that extent is contained betwixt the two places, which will give the number of equinostial degrees betwixt them, and multiplied by 60, it will give the true distance in miles betwixt these two places upon the earth, if taken in the parallel; which the not the nearest, as was before observed, yet is the shortest that can be made by steering upon one point of the compass: In the following operation we shall see how near this comes to the truth. A degree upon the graduated meridian at the parallel of 50° 0', should be equal to the scant of 50 degrees, supposing the radius to be 60 miles; then R: sec. 50°: :60: 93.34.

	Logarithm.	93.34
Sec. 500	10.191932	65338
60 miles	1.778151	18668
93.34 miles	+1.970083	2520.18

CASE IV.

When the two places differ both in latitude and longitude, to find their diffance.

Rule. 1st. Lay the edge of a ruler to touch the two places.

2d. Take their proper diff. of latitude, with a pair of compasses, upon the equinoctial, apply this distance to the edge of the ruler, so that when one foot is placed close to the ruler, the other foot may just touch some east and west line, crossed by that edge of the ruler; and there stay the compasses, the distance by the ruler's edge, from the place where the compasses rested; to that place where the ruler crosses the aforesaid east and west line measured on the equinoctial, gives the true distance.

E X A M. P L E. (Plate XIII.)

Let the two places be the Lizard and Madeira.

Lizard 50° 0'
Madeira 32° 17'

Difference of latitude 17° 43'

The ruler being laid upon the two places, take the difference of latitude 17° 43' from the equinoctial, and when applied to the ruler as before directed, one foot of the compasses will be in the point b, when the other will just touch the parallel of 50 in the point c; so the distance from b to the Lizard, measured on the equinoctial, will be near 20 degrees, is 400 leagues, the true distance from the Lizard to Madeira; and the course S. S. W. almost half W; the distance would be the same, if the difference of latitude were taken from the point L, to touch the parallel of 60 in H; for then L M would be the distance.

It must be observed that by the distance is meant, that which is made on the rumb line from one place to another, which will not be the nearest.

PROB. IV. (Plate XIII).

The course and distance given, also the latitude sailed from, to find the difference of latitude, departure, and difference of longitude.

The difference of latitude and departure are found exactly as in the plain chart, which we omitted there, judging it properer to infert it here. Let the place failed from be A, in the latitude of 30° o' north, and the

course N. E. b N. 192 leagues.

Rule. First thro' A, draw a meridian and parallel of latitude. Secondly, With the chord of 60 degrees, descaibe an arch, on which set off three points, the given course; and draw the line A H, which make 192 leagues, the given distance. Thirdly, From H let fall to the line A C, the perpendicular HF. A F measured on the equinocital, or graduated parallel, will be 160 leagues, the difference of latitude; and H F measured on the same, will be nearly 107 leagues, the departure.

This may be done without delineating the triangle thus: First, lay a ruler thro' the given place A, parallel to some N. E. b. N line. Secondly, Lay off 192 leagues by the edge of the ruler from A to H. Thirdly, Thro' H lay the ruler parallel to an east and west line to intersect the graduated meridian; the distance from the ruler to 30° in the graduated meridian, will be the difference of latitude, observing to measure it upon

the equinoctial, the distance must likewise be set off from A to H, in equinoctial leagues. To find the departure. First, With a pair of compasses take the nearest distance of the point A, to any meridian. Secondly, set off that distance by the edge of the ruler, (now passing thro' H, and parallel to an east and west line); from the point where the ruler interfects that meridian; the distance of that point from H, measured on the equinoctial, will be the departure.

To find the difference of longitude, it will necessary again to remark, that if a ship sail any determinate distance upon any particular rumb, the difference of latitude and departure, will always be the same in whatever latitude she is in; for if the place sailed from were in the parallel of 38°, or 46°, the course and distance the same as before; the difference of latitude would still be 160, and departure 107, as in the triangle KLM,

or OPR.

Now tho' she alters her latitude equally in both places, it will not be

fo in respect of the longitude.

By the plain chart, when she fails from 30°, the point Hat which she arrives, will be in 38°; and when the fails from 38°, the point M at which the arrives, will be in the parallel of 46° But in Mercator's chart. the point H is in the latitude 36° 41', and the point M in the latitude of 44° 01; fo that neither of these points is the true place upon Mercator's chart that the ship arrives at. In order to find the true place, produce the line A H, to interfect the parallel of 38° in the point K, produce also the line AF to G; K will be the place come to; KG, the difference of longitude; HF, the departure; AF, the proper difference of latitude; A G, the meridian difference of latitude: But tho' K be the place the ship is in, AK is not the true distance, but it may be found by the preceding problem: When she sails from the parallel of 38°, the true place O, at which the arrives, is found by producing the line K M to O, in the parallel of 46° o': Produce also the line K L to N, then will N O be the difference of longitude; L M, the departure; L K, the proper difference of latitude; KN, the meridian difference of latitude. The difference of longitude in the first, will be 388 miles; in the last it will be 433, being both measured upon the equinoctial; this shews the neceffity of knowing betwixt what latitudes any departure is made, before the difference of longitude can be found; and that in order thereto the first thing to be done, is to find the departure, as directed in plain failing, and then the difference of longitude may be found as here directed; the reason of which will appear by carefully examining the principles by which Mercator's chart is constructed. For tho' in this chart, the degrees of the parallels of latitude are apparently equal to the degrees of the equinoctial. Yet if they be measured as directed in Caje 3. of the preceding problem, they will be found to retain the same proportion to the degrees of the equinoctial in this chart, that they actually do upon the globe. Now the distance of any two places in any parallel is their departure, and the distance of their meridians on the equinoctial, is their difference of longitude equal to their apparent distance in the parallel on the chart; but when a ship alters both her latitude and longitude, the departure cannot be said to be made either in the latitude failed from, nor in that come, at was observed before.

Let us then suppose the departure to be made in that parallel of latitude that lies in the middle between the two, viz. in 34°. Now a degree of the enlarged meridian at this parallel is 72.4; for 2207.8 is the meridional parts to 34° 30′, and 2135.4, the meridional parts for 33° 30′; the difference is 72° 4′, which multiplied by 5° 21′ (the degrees in the departure) gives 387 miles, or 129 leagues, the difference of longitude.

This is what is called middle latitude failing, which tho' not frictly true, because the distances betwire the parallels of latitude on the meridian are not in a continued geometrical proportion, yet in a short run there can be no considerable error; we shall therefore in the next section work the problems of Mercator's sailing both by the meridional parts, and middle latitude.

There are two lines on Gunter's scale, one of equal parts marked E P, which may serve to graduate the equinoctial; to this is adapted another line marked Mer. which serves to graduate the meridian; and by these Mercator's chart may be constructed. Now to find the distance betwixt any two parallels by these two lines; as for instance, betwixt the parallel of 30, and the parallel of 60, extend from 30 to 60 on the line Mer. measure this on the line E P, is 44 degrees; makes 2640 miles.

SECT. III.

CONTAINING THE VARIOUS CASES.

Of MERCATOR'S SAILING. (Plate XIII.)

Aving in the former section show to construct Mercator's chart, and the use of it in navigation; we shall now show to find all that is necessary for the mariner to know without the chart; this is what is called Mercator's sailing, which presupposeth the knowledge

248 MERCATOR'S SAILING. CHAP. IV. of plain failing: The only defect of which, is that by the plain chart, the difference of longitude cannot be found, and tho' Mercator's chart gives the difference of longitude; the departure must be first found by the plain chart.

PROB. I.

The latitude and longitude of two places being given to find their beatrance and diffance.

F. X A M P L E. (Plate XIII.)

I demand the course and distance from the Lizard to Madeira.

To delineate this. 1st. Find by the table of meridional parts the meridional difference of latitude 1427, which set off from L to l. 2d. At l draw a perpendicular to L m, on which set off the difference of longitude 728, and draw the line l m. 3d. Set off the proper difference of latitude 1063, from L to b. 4th. Draw the line b b parallel to m l; b b will be the departure; L m the distance; the angle l L m, the course,

The triangles L l m, and L b b, are fimilar; therefore L l : l m :: L b: b b, that is the meridional difference of latitude is to the difference of longitude, as the proper difference of latitude is to the departure.

As the meridional difference of latitude 1427 3.154424
Is to the proper difference of latitude 1063 3.026533
So is the difference of longitude 728 2.862131
5.888664
To the departure 542.3 2.734240

By Gunter's scale, the extent from 1427 to 1063, will reach from 728

to 542 on the line of numbers.

The departure being thus found, the course and distance may be found by the 6th case of plain sailing; or without the departure, the course may be found by this proportion, as the meridional difference of latitude is to the difference of longitude, so is the radius to the tangent of the course. The extent from 1427 to 728, or from 1063 to 542.3; if taken on the line of numbers, will reach on the tangent line from 45 to 27° 2′. See the Operation.

As

As meridional diff. of latitude 14727 3.154424 Prop. diff. of lat. 3.026533 ls to the radius or tangent of 45 10.000000 Radius 10.000000 So is the difference of longitude 728 2.862131 Departure 12.734240 To tang. of course 27° 2′ S.S.W. ½W. 9.797797 Tangent 27° 2′ 9.797797

The course being thus sound, the distance may be sound by Case 2. of Plain Sailing. Thus S. C. of 27° 2'R: difference of latitude 1063: distance: 1191.

To find the departure by the middle latitude, add the two latitudes, the half of which subtract from 90, gives the complement of the middle latitude; then R: S. C. latitude: difference of longitude: departure.

Lizard	50.0	As radius ·	10.000000
Maderia	32.17	Is to fine 48.52	9.876899
Sum	82-17	Diff. of long. 728	2.862131
Half		Departure 548.2	2.738920
Complement	48.52	mental begins a mark	40.00

By Gunter's scale; the extend from 90 to 49 on the line of sines, will reach from 728 to 548 on the line of numbers.

The difference betwixt the departure, by this and the preceding, is only 6 miles, which is fo fmall, that it will make no difference in the dif-

tance and bearings.

The departure may be found in the table of difference of latitude and departure: Thus look for the complement of the middle latitude as if it were a given course, and for the difference of longitude as if it were the distance failed on that course; the departure corresponding to that course and distance, will be the true departure required. Here the complement of the latitude is 49 nearest, which find in the table. But the difference of longitude exceeds the distance in the tables, therefore take 100 seven times, and then 28; now against 100 in distance column, is 75.7 in the departure column, which multiplied by 7, is 528.5; to which add 18.4, the departure corresponding to the distance 28, makes 546.9 for the whole departure.

The reason of this is, because, if in a right angled triangle, if the angle be made the complement of the latitude, the hypothenuse will be the radius, and the base the sine of the angle; but the hypothenuse may be

called the distance, and the base the departure.

PROB. II.

Both latitudes and departure given, to find the difference of longitude.

Rule.

Rule. Find the proper and meridional difference of latitude, as in the former, and the proportion will be, as the proper difference of latitude is to the meridional difference of latitude, so is the departure to the difference of longitude.

E X A M P L E. (Plate XIII.)

A ship in latitude N. 49° 10′, and 15° 22′ W. longitude, fails N. N. E. ½ E. till by a good observation she is in the latitude of 52° 40′. I demand the longitude come to.

Latitude come to 52.40 3731 meridional parts
Latitude failed from 49.10 3397

Prop. diff. of lat. 70 lea. 3.30 334 merid. dift. of lat. 111 leagues

The departure by the tables will be found to be nearly 42 leagues.

To delineate this. Ift. Make the line $a \ d \ 70$, and $a \ b \ 111$, by any feale of equal parts, and draw the perpendiculars $b \ c$, and $d \ e$. 2d. Make $d \ e \ 42$, and draw the line $a \ e$, which produce to c; then $a \ e$ will be the diffance; $d \ e$ the departure; $b \ c$ the difference of longitude; $a \ d$ the proper difference of latitude; $a \ b$ the meridional difference of latitude.

Note. This is by a larger scale than that by which the chart is made.

As 70 proper difference of latitude
1.845098
1s to 111 meridional diffance of latitude
2.045323
So is the departure 42
1.623249
3.668572
To difference of longitude 66.6 leagues
1.823474

By Gunter's scale; extend from 49° 10′ to 52 40′ upon the meridional line: This upon the line E P, will be 5 degrees, and something more than a half, makes 334 miles, the meridian difference of latitude: The proper difference of latitude is 210; the departure is 126. Then Prop. di. lar. Depar. Mer. di. lat. Dif. long.

210: 126:: 334: 200 nearly.

By the middle latitude S C mid.: lat.: R:: dep.: D longitude.

52° 40'
49 10
101 50 fum
50 55 middle latitude
39 5 comp. middle latitude
30 5 45 fundle latitude
30 5 65 middle latitude
30 5 65 middle latitude
30 5 65 middle latitude

By Gunter's scale; the extent from the side of 39 to 90, will reach from 42, on the line of numbers, to 66 .

Ву

By the table of difference of latitude and departure find 39 degrees, and in the departure column look for 42.2, against which in the dif-

tance column is 67.

There are several other problems commonly inserted in *Mercator*'s sailing, which we shall omit; for all that is necessary to be known, is the latitude and longitude of the place, which may be had every day at noon; the latitude sailed from the day before, the latitude come to at noon, and the departure made the last 24 hours, are found as directed in plain sailing, and the difference of longitude by *Prob.* 2. of this; and the latitude and longitude being sound, the course and distance to the port bound to, are sound by *Prob.* 1.

And as to what is called parallel failing, it is in effect the same as middle latitude; for when a ship sails in any parallel of latitude, the latitude sailed from, and that come to, are the same, and of consequence, the parallel the ship sails in may be called the middle latitude, and the distance sailed may be called the departure, by which the difference of longitude may be found as in the preceding problem; one example will be

fufficient to illustrate this.

- Suppose two islands in the parallel of 50° 55', and their distance in

that parallel 42 leagues; required the difference of longitude.

It is plain that the diffance here is the departure, which being the fame as in the last problem, the operation will be exactly the same as in that; and if the difference of longitude were given, suppose 3° 20', their

distance in the parallel may be found by Prob. I.

In order to construct this geometrically, let the globe be supposed to be cut thro' the plane of the equinoctial, and the meridians and parallels of latitude projected orthographically upon this plane; the equinoctial and parallels would be concentrick circles, of which the pole would be the center; the meridians would all be strait lines intersecting one another in the center, and so the radius of the equinoctial would be one quarter of the meridian. The radius of any parallel of latitude would be the fine of the complement of that parallel, or its distance from the pole, and the fine of the parallel would be that part of the meridian intercepted betwixt the parallel circle and the equinoctial; this being premifed. 1st. With the chord of 60, or fine of 30, describe an arch, or circle as in (Plate XI. Fig. II.) 2d. From any point H, fet off the given difference of longitude 67 leagues, to F, and draw the chord H F, and radii C F and CH. 3d. With the fine complement of the latitude, viz 30 degrees from the center C, describe the arch R M; the chord R M will be the departure required. For the triangles C H F and C R M are fimilar. Kk thereOF MERCATOR'S SAILING. CHAP. IV.

therefore C H, the radius, is to H F, the difference of longitude, as C R, the fine complement, is to R M, the departure. If you have no line of fines, lay off 50° 55', the given latitude, by the chords from H, both ways upon the equinoctial, a ruler laid across by these two points, will intersect the meridian C H in R, and C R will be the radius of the parallel.

Having the distance in the parallel to find the difference of longitude. To delineate this, is only the reverse of the former. 1st. With the sine complement of the latitude from the center C, describe the arch R M, making the chord R M equal 42 leagues, their given distance in the parallel. 2d. With the sine of 90, or chord of 60, describe from the center C another arch, and produce the lines C R and C M to intersect that arch in the points H and F, so shall H F be the difference of

longitude.

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We have now explained the fundamental principles of navigation, and shewn how to solve all the problems, and various cases of plain, Mercator, middle latitude, and parallel failing, that are necessary for keeping a reckoning; and as to great circle sailing, it may be said to be impracticable, at least by any sea chart; for the arch of a great circle makes unequal angles with all the meridians; and how to describe such a curve upon a chart, wherein all the meridians are parallel to each other, seems if not impossible, at least so difficult, that the benefit arising from thence would not compensate the labour; for, supposing it actually described, there must be a new invention to direct a ship in that curve, for it cannot well be affirmed that it could be done by the compass. We shall therefore omit this, and proceed to the application of what has been said to the actual keeping of a reckoning, which shall be shewn in the next chapter.

CHAP. V.

To find the Latitude and Variation of the Compass by celestial Observation, and how to keep a Reckoning at Sea.

SECT. I.

To work an Observation, and how to find the Zenith distance by DAVIS'S Quadrant. (Plate XI. Fig. IV. and V.)

THIS inftrument confifts of two arches both drawn from one center H; to conftruct which, upon the point H raise H Z perpendicular to HO; with the radius HS describe an arch SF, which make 30 degrees; with the radius HG, describe another arch GK, which make 60 degrees; number the great arch, beginning at its intersection with the line HO, to 30 upwards; number the little arch from its intersection with the line Z H, increasing down to 60; so that both toge-

ther make 90 degrees.

It has three vanes, one fixed immoveably at H, with a slit in it, this is called the horizon vane; another is fitted to move upon the great arch, with a hole, which must be put to the observer's eye, thro' which, and the slit in the horizon vane, the horizon must be seen; this is called the fight vane; the third is fitted to move upon the small arch, it is called the shade vane, because the sun throws its shadow upon the horizon vane: These two vanes must be so placed, that the observer may see the shade exactly upon the upper side of the slit, at the same time that he sees the horizon thro' the slit, and counting the degrees upon both arches, their sum will be the zenith distance.

To prove this; from the center H describe the semi-circle AZM \oplus O to represent an azimuth circle; A the horizon; Z the zenith; \oplus the sun.

Place the fight vane at o degrees, on the great arch, and when the horizon A is feen thro' the slit at H, the perpendicular Z H, from the zenith, will cut the little arch at o degrees: Let the sun be at \bigoplus ; it is plain the angle Z H \bigoplus , is his zenith distance, which measured by the little arch, is 40 degrees, being the place where the shade vane is placed: But because the arch will not admit of being divided into minutes, let the shade vane be placed at 25 degrees, the instrument must be moved till the line

Kk2

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H \oplus ; cut the little arch at 25 degrees, and then the line H O will cut the great arch at 15 degrees: Produce the line H S to M; it is plain the angle Z H M, added to the angle M H \oplus , will be the fun's zenith distance; to measure the angle Z H M, draw the line H G perpendicular to H S, it will cut the great arch at 0 degrees; the fight vane must be placed at K, to see the horizon A, thro' the slit which will be 15 degrees on the great arch, but the angle G H O is equal to the angle Z H M, for the angles M H G and Z H O are equal, being both right. Therefore taking the angle M H O from both, the remainings Z H M and G H O will be equal; therefore the degrees on both arches being added together, will be the zenith distance, which being had, the latitude will be found by Chap. II. Sett. III. Prob. I.

The best instrument for taking the altitude at sea is *Hadley*'s quadrant, but as there is a small pamphlet explaining the nature, use, and the theory on which that curious and useful instrument is sounded, given gratis with it wherever it is fold; it will be needless to give a description of it here.

After the latitude is thus found by a good observation, if it agrees with the latitude by the account, it may be prefumed that your longitude by account is true; but if there be any confiderable difference, it may be feared there will likewife be an error in the longitude; to correct which there can be no certain rule, because it is uncertain whether the error is in the course or distance; for it must always be supposed, that the artist has given all the proper allowances in casting up the day's work, and frequently examined the log line and glasses, and likewise taken all opportunities of examining the current, and comparing this with his former journals: If after all this the observed latitude, and that by account do not agree, the only thing that can be done, is to let the longitude go as by his account, or make a remark what the longitude would have been, provided the error was in the course, and supposing the distance true; and likewise what the longitude would have been, were the error in the distance, and the course true; so that it may be presumed one of these three may chance to hit.

If a ship be sailing due north or south, her difference of latitude, and distance, will be the same; and if they differ by observation, it is likely the error is in the half minute glass, or log line, but if she sails due east, or due west, she does not alter her latitude, but if by the observation it is sound she has made any difference of latitude, there certainly must be error in the course, which may be owing to the steerage, or the compass, for the needle does not always point out the meridian, but varies sometimes to the eastward, and sometimes to the westward of it; and this is what is called the variation of the compass, and must be found before the course can be corrected.

SECT.

S E C T. II.

To find the Variation of the COMPASS.

HEN any heavenly object, as a star, or the sun, is in the horizon, the point of the compass that it bears upon may be had by fights fitted to the common compass, and by an azimuth compass the degrees may be found, that the object is distant from the east, or west points of the horizon; this is called the magnetick amplitude, and if this agrees with the true amplitude, there is no variation; so the true amplitude must be sound either geometrically, or by calculation.

It was shewn in Chap. II. how to do this geometrically; and to do this

by calculation, the following problem will ferve.

PROB. I.

The latitude of the place, and the fun's declination given to find the amplitude.

E X A M P L E.

Given

The proportion is

As the fine of 61° 44' the comp. of the latitude

1s to the radius

So is the fine of 15° 24' the declination

To the fine of the amplitude 17° 33'

9.479302

Latitude

Declination

28° 16' N.

15 24 N.

By this it appears that the fun then rifes E. b N. A. N. nearly, but if by the compass it bears E. A. N. there will be a point variation to know whe-

ther the variation be easterly or westerly, take this general rule.

When you are looking to the sun to take the amplitude, if the magnetick be to the right hand of the true, the variation is westerly, as in this case; and to rectify the course steered, there must be one point taken to the lest hand, if the course steered be N. b E. the true course will be N. which shews that the north point of the compass is a point to the westward of the true north, but if the magnetick amplitude be to the lest hand of the true, then is the variation easterly; and in correcting the course, the variation must be allowed to the right hand of the course steered.

DEMONSTRATION.

Of the proportion for finding the true amplitude see Plate XI. Fig. I. Let P O be the given latitude, P Z is the complement; thro' P draw P p, parallel to the horizon H O, draw the parallel of declination E X, to intersect the horizon in X: C X, will be the sine of the amplitude; C x the sine of the declination, and P p the sine complement of the latitude; the triangles P p C, and C x X, are similar, for the angles at p and x are both right; the angle at X is equal to the angle P C p, being each of them the complement of the latitude; therefore P p the sine complement of the latitude, is to P C the radius, as C x the sine of the declination, is to C X the sine of the amplitude.

When the fun is rifen any confiderable heighth above the horizon, it will not be eafy to find its true bearance by the compass, but, if it is within 10 or 12 degrees of the horizon, it may be had by an azimuth compass.

The fun's azimuth is an arch of the horizon, contained between the fouth or north points of the horizon; and an azimuth circle paffing thro' the center of the fun to find this geometrically was shewn in *Chap*. II.

And to do it by calculation the following problem will ferve.

PROB. II.

The latitude of the place, the fun's declination, and altitude being given, to find the azimuth.

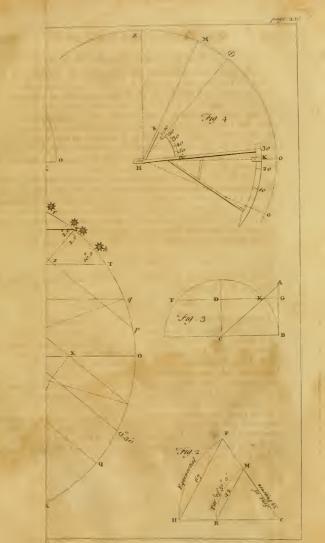
E X A M P L E.

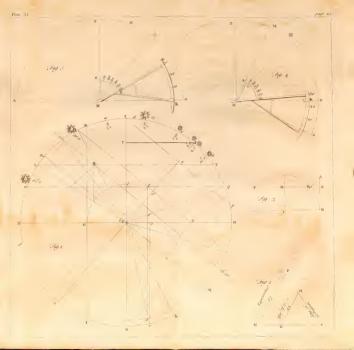
Latitude 28° 16' N. declination 15° 24' N. altitude 9° 3'.

Rule. 1st, Take the complement of the altitude; the complement of the latitude; the complement of the declination; and add these three together. 2dly, Take half this sum, from which subtract the complement of the declination. 3dly, Take the sine of this remainder, and the sine of the half sum from the logarithms. 4thly, Take the sines of the complement of the altitude, and the complement of the latitude from logarithms, and subtract each of them from the logarithm of the radius; the remainders will be the complements arithmetical of those sines.

Now these four must be added together, viz. the complement arithmetical of the sines of the complement of the altitude, and of the complement of lattitude, and the sines of the half sum, and remainder. Half the sum of these four logarithms is the logarithm of the sine complement

of half the azimuth required.





80° 30' Comp. altitude comp. arithmetical of the fine 0.005997
61 44 Comp. latitude, comp. arithmetical of the fine 0.055146

216 50 Sum of the three

108 25 Half sum; from 180 remains 71° 35'. Sine 9.977167

74 36 Complement declination

33 49 Remainder Sum of the four 19.78 3804

Sum of the four 19.78 3804

38° 46' Is the comp. of 51°14', of which the fine is 't the fum 9.891902

38 46 77 32 The fun's azimuth from the north

Note. If the declination be fouth, and latitude north, and the contrary, inftead of taking the complement of the declination you must add 90

thereto, and proceed as before.

The demonstration of this problem depends upon the doctrine of spherick trigonometry; for here are three sides given, viz. the complement of the altitude, the complement of the latitude, and the sun's distance from the elevated pole; this last will be the complement of the declination, when the latitude and declination are both north, or both south; but if one be north, and the other south, 90 must be added to the declination; the three sides being given, the angles are found as in the preceding operation.

Having thus found the true azimuth, the magnetick is found by obfervation; the same directions as were given in the amplitudes, will serve

to know whether the variation be easterly or westerly,

SECT. III.

How to keep a Reckoning at Sea in order to know at any time the Latitude and Longitude the Ship is in, and the Course and Distance to any Port.

THE regular method of doing this, is by keeping an exact account of the various courses, and distances sailed in 24 hours; for which reason the log is hove every hour, and the distance and course set down in proper columns, in a book provided for that purpose, which is called the log-book, ruled and column'd as explained in the following pages.

In the first column, at the head, is H for hours, under which are set down the hours; the second has K at the head, in which are set down the knots run out at every hour; the third column has F at the head, in which are set down the odd fathoms at every hour; the fourth has course at the head, in which are set down the courses corresponding to the hours; the fifth has winds at the head, in which are set down the shiftings of the winds; the fixth has remarks at the head, in which is set down what sail is carried, and the weather, which are two things very necessary to be observed; for if it blows hard a ship cannot make good the course steered by the compass.

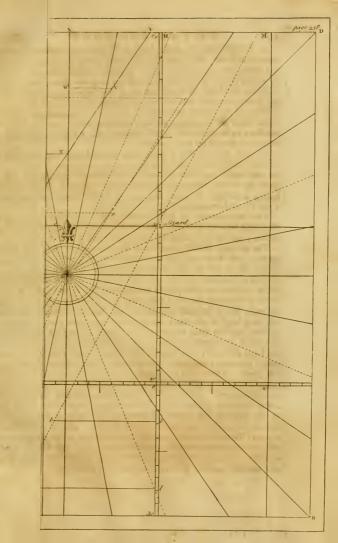
In fome ships the log is hove once in two hours, and set down upon a board, from which every one that keeps an account, transcribe it into his own book, and then reduces all the different courses into one, and finds the whole difference of latitude and departure made the last 24 hours, as directed in plain sailing, and the difference of longitude by

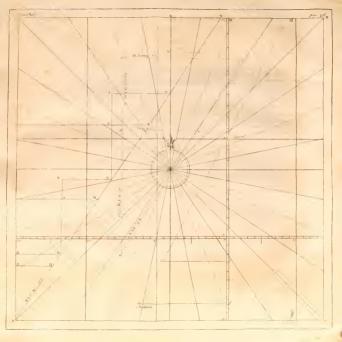
Prob. II. of Mercator's.

The this account be kept by the greatest care and exactness, there will often be very great errors discovered in the latitude, by good observations; and in the longitude when any known land is made.

The occasion of these errors may be attributed to these four following causes. 1st. If the log line and glass be not duly proportioned to one another, there will be an error in the distance; for admitting the glass to be only 29 feconds, and the line right divided, the ship would be a head of the account the 30th part of the distance; for there is only an account taken of what she runs in 29 seconds, and what she runs in the 30th is omitted; but if the glass be true, and the line short divided, the account will be a head of the ship; for supposing the 120th part of a mile to be 50 foot, and the space between the knots to be only 45 foot, it is plain that every 50 leagues run by the account, is only 45; fo that the ship must run the 10th part of the whole distance, more than by the account, . before the makes the land. 2d. Is owing to the variation of the magnetick needle, which does not always point out the meridian; this will occasion a great error in the course, if the variation is not known, and allowed in the course. 3d. Is owing to the lee-way a ship make; for when a thip fails close by the wind, the does not make good the course steered by the compass, but falls to the leeward of it, more or less according to the fail the carries, and the heighth of the fea. 4th. Is when there is a current; for when that fets upon the fame rumb on which the ship is steered, her real distance will be more than by the log; and if it sets upon the opposite rumb, it will be less; and if it sets athwart the ship's way, it will occasion an error both in the course and distance.

LOG-





SEC	SECT. III. Log on board the SEA-Horse, Anno Dom. 1738. 259						
H.	K.	F.	Courses.	Winds.	REMARKS, Saturday, May 27, 1738.		
1	7			1 1 1	Lizard 50° o' north latitude, and 0° o		
2			To all Ton		longitude.		
3			- 1	10.11	Lizard N. W. 4 leagues distance, fine		
4	5	3	S. W.	N. b E.	moderate gale, and pleasant fair wea-		
5	6	4		N.	ther.		
6	7 8			fresh gale	Handed all our small sails, and reeft		
- 7			1 00	N. b W.	both top-fails.		
	7	10.0	- 10	N. N. W.	A great sea from the N. W.		
9		3		N. W.	Double reef M.T.S. and handed. F.TS.		
10	5	4		N.W.bW.			
11	5		4.1	W. N. W.			
12	4	3		337	Dat Barret		
1	- 4	4	CCXX	W.	Drizling rain.		
- 2	4		S. S. W.	1.1	Che form son Gift		
3	5		S. W. b S.	W.bN.	Set fore top-fail. Fine clear weather, out all reels, and		
4	5	4	3. 11. 03.	N·W.bN.	fet the finall fails.		
- 5	5	3		IN W. DIV.	let the illian fails.		
-	5 6				At noon clear weather, had a good ob-		
7 8			700 ()		fervation.		
9	7	3	4.1		Zenith diftance 25° 0°		
10	6	4		The same	D. P. Standard		
11	6	-		-1,-1	Latitude come to 47 56		
12	5		0.00				
Cour	fe. (I)	ict s	. IW: II ati. I	vII ati, by Di	ff. of Longi. Varia- Weridio. distance.		
-			accou	nt observa. lo	ngi. come to tion 33 miles from the		
S.16	W. I	24 11			51' 0° 51' 1 point Lizard		
Cour					Latitude by observation 47° 567		
S. E.				2 10.3 0	Latitude failed from 50 00		
S. S.			46 39.		-		
S. b	V 3	W.	62 58.2		97 56		
S. 11			14 14.1		Middle latitude 48 58		
118.2 11.0 44.5 C. middle latitude 41 02							
			1.012	11.0			
100				-	Degrees. Dep. Dif. of long.		
Lasi	Lati. failed from 50.00						
	Difference of lat. 1 58						
Latitude come to 48 o2							

AFTER the log-book is thus copied, the next thing to be done is to reduce all the various courses into one, so that the whole difference of latitude, and the whole departure may be found; this is what

TO WORK A DAY'S WORK. CHAP. V.

is called working a day's work. In order to which, it will be proper to make a traverse table, upon a slate or waste paper, as directed in plain failing. But it must be observed the courses must be corrected, by allowing for variation and lee-way. Now, as our account is to begin from the Lizard, we must suppose the ship to sail S. E. from it, to the place the was in at 3, when it bore N. W. and because there is one point, and variation, the course corrected will be S. E. b E. + E. The next course steered is S. W. allowing variation, makes S. S. W. 3 W. but when the wind came to W. N. W. I allow 1 point lee-way, makes it S. b W. 3 W. when the wind comes to west, she lies only S. S. W. and allowing for variation and lee-way, the makes only S. + E. course; the last course steered is S. W. b S. the wind being large, makes no lee-way, allowing the variation; true course is S. b W. 3 W. The courses being thus corrected, against the first set down 12 miles, the distance from the Lizard; against the next is 46, being what the ship has run by the log from 3 to 41; against the next is 62, being what she has run from 11 to 2; and from 5 to noon; against S. + E. is 14 miles, what she failed from 2 to 5: We may then find the proper difference of latitude and departure to each courfe, by the table; the fum of the fouthings is 118 miles, that is 1° 58', and because the latitude is decreasing, this must be subtracted from the latitude of the Lizard, which makes the latitude by account 48° 2', but by observation 47°, 56'; the whole westing is 44.5, and easting is 11, so the departure is 33.5 west. And by this, to find the difference of longitude, add the latitude failed from, and that come to, into one, and fubtract half that fum from 90, the remainder is 410 21, the complement of the middle latitude. Again look in the table of difference of latitude and departure for 41°, and look for the departure 33.5, in the proper column, against which, in the distance column, is 51, the difference of longitude. To find the latitude by the observation, look for the declination corresponding to the day of the month, which is 220 47', added to the zenith distance 25° 9', makes 47° 56'. After finding the whole difference of latitude and departure, because the numbers exceed those in the tables, I take half of each, which I find in the column corresponding to 16° against 62 distance, which doubled, makes 124, as in the operation under the log; the like process must be used every day at noon. H.

SECT. III.	Log on be	ard the SE.	A-Horse, Anno Dom. 1733. 261		
H. K. F.	Courses.	Winds	REMARKS, Sunday, May 28, 1738.		
1 7	S.W.bW.	N. E.	Moderate gales and fine pleafant wea-		
2 6.	all arrows and	a Cod Mar. March	ther.		
3 5	Il mon 3	E (a) 10 E	of any margin round and hands are		
4 5	s. w.	Description.			
5 4	5. W.	4 7 2	Little wind with fmall drizling rain.		
6 3 2	19 2 W	2.0	Found it S. S. W. one mile in an		
8 1	1 11	This	hour.		
9. 111	the how W.	13 av	Fresh gales, handed all our small fails.		
10	Angenth .	Calm	At noon clear, zenith distance 22° 48'		
11	relatively	C.F.	Declination 22 53		
12 I	O SAME I	S. E. S. S. E.	Latitude by observation 45 41		
2 4	S. S. W.	3. 3. E.	At fun rifing, by a good observation,		
	3.3.17	A DESTRUCT	amplitude 23° 23's in order to find		
3 5 3	01 16 10	1 1-7 11 =	the true amplitude, find what diffe-		
5 8 7 =	med late.	od ton :	rence of latitude the ship made from		
5 8 6 9	-7-2 1001	Series Plan	fun rifing till noon.		
7 9	milde,	tel typical	Course corrected S. b W. distance 70,		
	vice following	Color record	difference of latitude 68.7. Latitude at noon		
9 9	WOODER VILL	million of	Diffe, of lati, fince fun rifing to 11 110		
The same time	to but a	L TOP I	Latitude at fun rifing 46 50		
11 9	of the breaks	mil re , all	Complement of the latitude 43 10		
Courte Dif 1 S	i. IW.II.ati.	v Lati, by Di	ffe. of Longi. Variati-Meridio. distance		
1			ngi. come to on from the Lizard		
S18°W 144 1	36 45 45° 4	0 450 41 1	2' 1° 53' 1 point 1° 18' 10		
Courfes co	rected. Dif.	S. W.	Sine of 43° 10' comp. lati. 9.83513		
	. W. 23	16.3 16.3	Is to radius - 10.00000		
	W. b S. 13	_	Sine of declination 22° 53' 9.58979		
	b W. 87	85.3 17.0	Sine of amplitude 34 38 9.75460		
	. b.W24	23-5 4.7	Magnetick 23 23		
Cour. good S.		135.9 45.2	Variation 110151 ' on many		
Latitude yester	rday at noon	479 561	I dans nie beiter beiter beiter		
This day		45 41	not a the man to broth one		
4 000	on it the Ka	93 37	the last and a particular		
Middle latitud	e	46 48			
Comp. of middle latitude 43 12					
-		f. of long.			
43	45.3	62	**		
		Ll2	H.		

TO WOOD A DATE WORK DONE OF .

262		T.o.	on board t	he SEATHO	RSE, Anno Dom. 1738. CHAP. V.		
Н.	K.	F.	Courfes.	Winds.	REMARKS, Monday, May 29, 1738.		
-	-8		5. W.	N. b.E.	Fresh gales and cloudy most part of		
2	7.	3	m - 1 - 1 1	Cr 0.7	these 24 hours.		
3		4	1 70	55 m 990-7	Found the fun's azimuth by a good		
1114	6	000	0000.00	0.000	observation 75° 30' after the sun's ri- sing; his altitude was then 9° 30';		
5	5 5 6	. 4	0 0 0 0	N.	the true amplitude is 67° 4', which		
7 8		3	MARGE	- 17-	makes the variation 8° 26', as by the		
	6		S.W.bW.	N. N. W.	following operation.		
9.	6		make all as	Landa Dall	Com. alti. 80° 207 Ar. com. 0.005007		
10	5.56	3		1 F-4	Com. alti. 80° 307 Ar. com. 0.005997 Com. lat. 45 34 Of fines 0.146262		
12	6	3	The lati-		Com. dec.67 2		
I	6.	4	tude at the	2 730	Sum 193 6 0.152259		
2	8		time of ob-		Half fum 96 33		
3 4 5 6	-7·	4	of the azi	- fum less	Supple. 83 27 their fines \ 9.997156 Com.dec. 29 31 their fines \ 9.692562		
5	7	3	muth	2	Sum of the logarithms 19,841977		
6	8		449 26!	1, 1, 100	Half 9.920988		
7 8	9	7.	1001	9	Sine com. half azim. 56° 28'		
2.9	8	3	1	1	Complement 33 32		
10	.8	- 1	00 1	1	True azimuth from the N. 67 4		
11	8:	(a)	Cloudy,no	of ghi li	West variation 8 26		
12	8	-4	observati.		Magnetick azimuth 75 30		
Çou	rfe. L	oif. S	. W. Lati.	by Lati. by D	iffe. of Longi. Variati- Weridio. diftance, ngi. come to on. from the Lizard.		
6	W.	68	18 1 18 43° 4		19 46 48 39 1 point. 3° 16'.		
	rfes c			S. W.			
S. V	V. 6	S. 1 7	W. 45		Points. Depar. Dif. of long.		
	V. 🚁		123		.4 590 %. 7 83		
S. I	V. dif	t.	168 1	18.7 118.0	Dif. of long. 166		
T	d o	O-	rday at noon	45° 41.	DIL 01 1018 109		
					(2° 46)		
	Diffe. of lati, these 24 hours 1 58 2° 46. Latitude come to 43 43						
			from	45 41	C F 14		
	0.095	1 od	1 191111	89 24	male non-		
Middle latitude 44 42							
Comp. of middle latitude 45 18							
-0.					The state of the s		

ě.

The preceding three days will be fufficient to shew the manner of taking off and working the log, as the operations for finding the latitude by the zenith distance, and the variation of the compass by an amplitude and azimuth, are there set down at large. We have also show to correct the course, by allowing for lee-way and variation, and how to account for a current. After working each day's work in the log-book, they may from thence be transferred into a journal; the form of which is hereunto annexed.

Journal of a Voyage, intended by God's affifiance, in the Ship Sea-Horfe, from London to Jamaica, under the Command of A. B. in the Year 1738.

Weeks day.	Months day.	Courfe made good.	Dift.in miles.	Latitude by account.	Latitude by observation.	Longitude.	Meridional distance from the Lizard.	Variation.	Winds.
ħ	<i>May</i>	S. 16° W.	124	48° 2°	47°,56°	0° 51	o° 33	1‡point	Yesterday at 3 P. W. Lizard, N. W. 4 leagues, the first part fresh gales and a great sea, the latter moderate and clear, N. to W.
,0	28	S. 18º W.	144	45° 40'	45° 41′	1° 53	1° 18!	By ani.	N. E. to S. E. fresh gales, and clear the latter part.
. >	29	s. w.	168	43° 43	To the	4° 39	3° 16'	By azi. 8° 26'	N. E. E. to N. N.W.freshgales and cloudy.

The following characters are generally used to express the days of the week.

O Sunday; D Monday; & Tuesday; & Wednesday; 4 Thursday; 2 Friday; 5 Saturday.

264 ChAP. V.

OF THE MOON AF

tecon i year of of the Moon's Age, and Time of High Water to a year stace our Savious of the Moon's Age, and Time of High Water to a year stace our Savious of the Moon's Age, and Time of High Water to a year stace our savious of the Moon's Age, and Time of High Water to a year of the Moon's Age, and Time of High Water to a year of the Moon's Age, and Time of High Water to a year of the Moon's Age, and Time of High Water to a year of the Moon's Age, and Time of High Water to a year of the Moon's Age, and Time of High Water to a year of the Moon's Age, and Time of High Water to a year of the Moon's Age, and Time of High Water to a year of the Moon's Age, and Time of High Water to a year of the year of the Moon's Age, and Time of High Water to a year of the year of t

IN ROM what has been faid, it is plain, that if the account of the journal be true, the ship will arrive at her designed port, by steering fuch a course as the journal directs, and in order to fail into the harbour, if in a tide way, the mariner should know what time it will be high water; but as this is governed by the moon, it follows, that to attain this:

the first thing to be done is, to find her age! I way fluit it to flug

If the months all contained an equal number of days, and the change of the moon was always on the last day of every month, the day of the moon would then be the same with the day of the month, and we should have exactly twelve compleat moons every year; but it has been found: by a long feries of good observations, that every year contains twelve compleat moons and eleven days more, very nearly, so that if the moon happens to change any year the last day of December, ait will be eleven days past the change on the last day of the December following; and twenty-two days after the change, the succeeding year, and the third year it will be thirty-three days; but as there are but 29; days from the change of the moon till it changes again, it is plain that in three years time, which contain 36 months, we shall have 37 compleat moons, and three days more; fo that the moon will be, on the last day of December, in the third year, 3 days after the change; and on the fourth it will be 11 days more, that is, the last day of December will be 14 days after the change. Now it will be very easy to find the moon's age any day of the month provided the moon's age be known the last day of the preceding year, our first business then shall be to shew how this is found.

As every year contains 12 moons and 11 days, every three years will contain one whole moon more than months, and three days more, fo that 18 years will contain fix whole moons more than months, and 18 days more; that is to fay, if the moon changes on the last day of December, it will be in 18 years afterwards, 18 days past the change on the last day of December; and the year following, viz. the 19th year, it will be 11 days more, which makes 29 days, and this being a whole moon except half a day, we shall have new moon some time of the last day of December; fo that at the expiration of 19 years the new and full moons happen on the same day of the same month they did 19 years before that.

This revolution of 19 years is called the lunar cycle, or the Metonic cycle, from its author Meton the Athenian. The new moon, or the change,

was on the last day of December, two years before the birth of our Saviour, so that every nineteenth year from that time the moon changed on the last day of December, and the year of our Saviour's birth was the second year of the cycle. Hence it is manifest, that if we add I to any year fince our Saviour's birth, and divide the fum by 19, the quotient will shew how many cycles have past since its first commencement, and the remainder will shew what year of the cycle that is, which is called the golden number, or prime for that year; it finds the the age of the moon on the last day of the preceding year, or the number of days past fince the new moon; this number is called the epact, and fince the epact of the first year is 11, of the second 22, of the thire 3, and so on constantly increasing by 11; as was before observed, it is evident that to find the epact for any year we must multiply the golden number by 11, the product if less than 30 will be the epact for that year, if it exceed 30 divide it by 30, and the remainder will be the epact.

EXAMPLEL

Required the Epatt for the Year 1730.

First find the golden number by the preceding rule. irst find the golden number by the precently

To the year 1730 golden number 102 2 101 d first add 1 multiplied by 11 1 1 1 d first add 1 product is the epact 22 golden number

EXAMPLE IL

to any time to excell a deposit a Required the Epact for the Year 1744.

30)176(5 19)1745(91 16 golden number 20 epact

Now as the epact expresses the age of the moon on the last day of December, it is plain that if the moon changes on that day in any year, it will change on the 20th of December the next year, because on the last day of December it will be 11 days past the change; but if this 20th day be called the 31st, as was the case in the year 1753, when the style was altered, it will make an alteration in the epact of 11 days: Therefore to find the epact fince the commencement of the new flyle, we must divide

divide the year without adding 1 to it, by 19, the remainder will be the golden number, which multiplied by 11 will give the epact as before.

EXAMPLE III.

 Required the Epatt for the Year 1754.

 19)1754(92
 golden number | 6.

 1171;
 multiplied by 11

 44
 product. 30)b6(2...

 38
 60

 6 golden number
 epa&t 6

It is plain if the moon changes on the last day of any year, the day of the moon will be the same with the day of the month in January following till the change; and because the time betwixt one new moon and the next is 29 days and an half, the 30th day of January will be the first day of the next moon, and the first day of February will be the third day of the moon, and consequently if we add two to any day of the month in February that year, it will give us the day of the moon; now as in common years. February has but 28 days, if to this, 2 be added, it will make 30, which is half a day more than the moon contains; so that it will change on the last day of February, and therefore the first day of March will always be the same day of the moon that the first day of January is, and the first day of April, the same as the first day of February (except in leap years, when one day more must be added to the first day of March), for if the moon changes on the last day of February, it will change again before the 30th of March, and fo the first day of April will be the 3d day of the moon, and the 27th day of April the 20th day of the moon; fo the 28th day of April will be the first day of the moon, and the first day of May will be the 4th day of the moon.

Now, though the moon does not change the last day of December, the epact gives the age of it on that day, and therefore if the epact be added to the day of the month in January, the sum will be moon's age; but in February we must add 2 to the epact and day of the month, to find the moon's age; in March again, except in leap years, the epact and day of the month will give the moon's age. Hence this general rule will serve

to find the moon's age on any day of the month.

Rule, Add the epact to the day of the month, and the number for that month, the fum if less than 30 is the moon's age, if it exceeds 30 take 30 from it, and the remainder will give the moon's age.

The following numbers must be added in the months to which they correspond.

'January April October February 2 May August 6 November 10 March June December 10

XAMPLE

Required the moon's age the 24th day of January 1754.

The epact by the preceeding rules will be found to be 6, the number for the month is o, now we have only 6 to add to the 24, which makes 30, which being half a day more than a whole moon, the moon changes some time that day.

XAMPLE

Required the moon's age the 26th of April 1754, to 26 add 2 for the month, and the epact 6, the fum is 34, from which substracting 30, the remainder is 4, the moon's age.

After finding the moon's age we may thereby find the time of high

water from the following principles.

It has been observed that when it is high water in any port, the moon will always be on the same point of the compass; and as the moon in 24 hours moves through all the points of the compass, it is plain she must take 45 minutes in moving from any point to the next; for 32, the points of the compass, multiplied by 45, gives 1440, the minutes in 24 hours; hence, if it is high water in one port at 12, and the moon then on the fouth point of the compais, and high water in another port, when the moon is on the S. S.W. point, it will be I hour and 30 minutes

after 12 when it is high water at this last place.

Now, if the moon and the fun were always on the meridian at the fame time, the moon would always come to the same point of the compass at the same hour of the day, and of consequence it would be always high water at the same hour; but since the moon comes to the meridian with the fun only on the day of the change, which happening only once in 30 days, it will from thence follow that the difference of the time of her coming to the meridian from the day of the change, or any day of her age, to the next day, will be 48 minutes; for, 30 the days in the moon, multiplied by 48 gives 1440, the minutes in 24 hours, at which time the moon will again come to the meridian with the fun, and will then be on the fouth fide of the compass; the first day after the change it will be48 minutes after 12, before the moon comes to the meridian, or fouth

point

point of the compass; the second day 1 hour 36 minutes; and as it is thus 48 minutes every day later in coming to the south point of the compass, it will be so with respect to any other point, which is the reason that it is high water in any port 48 minutes later every day

than it was the preceding.

From what has been faid, it is manifelt, that before the time of high water can be found on any day of the moon, two things must be known; first, on what point of the compass the moon will be every day at high water; secondly, at what time the moon will come to the meridian on that day. As for the first, which is called the flowing, it must only be had by experience, and for the second, which is called the moon's southing, it will always be found by multiplying the moon's age by 48, and dividing the product by 60, the quotient will give the hour, and the remainder the minutes the moon is on that day later of coming to the meridian than the sun. Now these two being given, if to the hours and minutes of southing we add the hours and minutes corresponding to the flowing, that is, to the point of compass on which the moon is at high water, the sum is the time of high water on that day.

EXAMPLE.

Required the time of high water at London-Bridge, Feb. 27, 1754, the flowing S. W.

Because when the sun is on the south point of the compass it will be 12 hours, that is, either noon or midnight, it will be 3 hours after noon when the moon is on the S.W. point of the compass; for in 45 minutes she moves from one point to the next; S.W. is 4 points from the south, and 4 times 45 is 180 minutes, which is three hours. The age of the moon on that is, 3 multiplied by 48 is 144, divided by 60 is 2 hours and 24 minutes, the moon's southing that day, to which adding 3 hours the stowing, the sum will be 5 hours and 24 minutes, the time of high water required.

F I N I S.

THE

ELEMENTS

OF

NAVAL ARCHITECTURE:

OR, A

PRACTICAL TREATISE

ON

SHIP-BUILDING.

LATELY PUBLISHED AT PARIS.

By M. DUHAMEL du MONCEAU,

Inspector General of the Marine to his most Christian Majesty, Member of the Royal Academy of Sciences at Paris, and Fellow of the Royal Society at London.

CAREFULLY ABRIDGED

By MUNGO MURRAY.

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PRACTICAL TREATISE

ON

SHIP-BUILDING.

CHAP. I.

General Proportions for Building:

AVAL Architecture may be divided into three principal parts.

I. To give the ship such a figure or exterior form, as may suit the service she is designed for.

II. To find the true form of all the pieces of timber that

shall be necessary to compose such a solid.

III. To make proper accommodations for guns, ammunition, provifions, and apartments for all the officers, and likewife for the cargo.

We shall at present only treat of the first of these, namely the exterior figure, and consider it first, as it regards the bottom, that is, the part which lies under water, and may be called the quick-work; or secondly, the part which is above water, and may be called the dead-work.

In order to give a proper figure to the bottom, all the qualities which are neceffary to make a fhip answer the service for which she is design'd, should be considered. A ship of war should carry her lower tier of guns four or five seet out of the water. A ship for the merchants service should show the cargo well, and both of them should be made to go well, carry a good sail, steer well, and lie too easily in the sea.

Some

Some eminent geometricians have endeavoured to find the form of a folid which may beft answer all these qualities, and meet with the least resistance in dividing the sluid through which it is to pass; but have not been able to reduce their theory to practice by reason of the different positions a ship is obliged to be in when under fail. The ship-builders despairing to establish this point by mathematical rules, have applied themselves wholly to their own observations and experience, which may indeed supply the desciencies of art, but though they may thereby discover that a ship has several bad qualities, it will not be easy to determine where the fault lies; for it may be owing to the rigging; and though the fault be not there, yet they cannot be certain in what particular part of the body it is. If their observations be assisted by principles drawn

from theory, it will conduce very much to attain their end.

As there have been feveral ships built which have seemed to answer all the fervices for which they have been defigned, fome builders have made it their principal study to copy ships which have gained the applause of the feamen. This method they very improperly call the principal rule which should be observed in building. Now, as the bodies of ships are very different from one another, so there are, by this means, as many different methods used; some chusing one, and some another for a standard. But it must be observed, that even though it were possible to find such a body as should give intire satisfaction, and have all the good qualities that should be necessary to answer the services proposed, yet this could by no means be established as a standard by which other ships of different dimensions may be built. For admitting we have a first rate of 100 guns, which by experience has been found to be a very good ship in all respects, vet we should find ourselves very much deceived, if we should build a thip of 20 guns by making all the parts have the fame proportion to one another that they have in that of 100 guns.

The first thing to be done in order to lay down the draught of a ship is to determine the length, which should be either on the lower gun deck, or at the load-water line; for there must be great care taken that there is a sufficient space betwixt the ports. This will oblige us sirst to fix the number and dimensions of the ports, the distance of the aftermost port from the transom, and of the foremost from the stem, and the distance betwixt the ports. This article may be determined by the sol-

lowing tables:

A Table of the Number of Ports on each Side of a Ship, according to the Number of Guns, and the Weight of the Shot:

A Ship o	of rea	Guno	A Ship o	£ 200 (inne	A Ship	of 74 (ins.
Decks	Ports	Shot	Decks	Ports	Shot	Decks	Ports	
						Decks		Shot
I	16	48 or 36	1	14	36	I	13	36
2	15	12	2	15	18	1	14	3
Quarter		8	Quarter	14	12	2		18
Forecaftle	5 3 2	8	Forecastle	13	6	Ouarter .	8	
Poop	2	4	Poop	1 -3		Forecastle	8 8	8
1						Poop	2	4
A Ship	of 64 (Guns.	A Ship o	of 58 C	iuns.	The	Tiger.	
Decks	Ports	Shot	Decks	Ports		Decks	Ports	Shot
	12	7	1	12	18	I	I I	18
1 {	13	24	2	13	12	2	12	8
2	13	12	Quarter	} 4		Quarter	3	6
- (14	5 11	Forecastle	S 4	4	Forecastle	2	4
Quarter	7	} 6						
Forecastle						-		
A Ship			A Frigate			A Frigate		Guns
Decks	Ports	Shot	Decks	Ports	Shot	Decks	Ports	Shot
1	11	18	1	11	12	I	10	6
2	12	12	2	12	8	Quarter	6	4
Quarter	2	4				Forecastle		
A Frigate	of 32		A Frigate	of 32 (A Frigate		
Decks	Ports	Shot	Decks	Ports	Shot	Decks	Ports	Shot
I	4	8	I	10	8	1	3	8
2	10	6	2	6	6	2	10	4
Quarter	2	4				Quarter	1	4
Forecastle								
A Frigate of 24 Guns.			A Frigate			Frigates of	20 Gun	s have
Decks	Ports	Shot	Decks	Ports	Shot	10 Ports		
1	10	6	1	9	6	on one D	eck. Sho	ot 6 lb.
Quarter	2	4	Quarter	2	4			

Veffels of 16 guns have 8 ports on one deck, the guns to carry 4 lb. flot. Veffels of 12 guns have 6 ports on one deck, the guns to carry 4 lb. flot.

A Table of the Dimensions of the Ports and Height of their Sells, according to the Weight of the Shot.

	Sho	ot	H	ci.								ight of					
	lb.		f.	in		f.	in.		f.	in.	ıst	Deck	2d	Deck	3d	Deck	Quarter-
	48		2	9		3	O	or	3	2	f.	in.	f.	in.	Ĭ		Deck and
ı	36		2	8		3		or	3	1	2	2					Forecastle
8	24	- 1	2	.5		2	8	or	2	10	2	1	2	0			
ı	18	ı	2	4		2	7	or	2	8	1	ΙI	I	9			
ı	12		2	2	2	2	4	or	2	6	1	10	I	8	1	7	
ı	8	1	1	9		I	11	or	2	3	1	8	1	6			1 5
ı	6	-	I	6		I	8	or	I	11	I	7	1	6			1 5
	4	- 1:	I	.14		I	6	or	I	9	1	5					1 3

A Table of the Number, Dimensions and Distances betwixt the Ports on the lower Deck; also the Distance betwixt the foremost Port and the Stem, betwixt the Aftmost and the Sternpost.

Ships Names.	Noof	Brea	idth	Dist.	betw.	Fore	most	Aftı	nost	Leng	th on
	Ports	of P	orts	Po	rts	from	Stem	from	Post	L. I	Deck
Amiable	13	2	8	7	6	13	4	9	0	147	
Invincible	13	2	8	7	4	12	4	9	0	144	
Achilles	I 2	2	8	7	8	18	2	10	6	145	
Touloufe	12	2	8	7	6	17	4	9	2	141	
Ardent, 64 guns	12	2	8	7	6	17	0	9	2	140	8
Fleuron, 64 guns	12	2	8	7	8	18	10	10	6.	145	8
Dauphin Royal 74 guns	13	2	10	7	7	18	2	10	0	156	

Note, An inch French measure is equal to 11 to twelve parts called lines, which are divided into twelve parts, called points.

The next thing to be done is to establish the breadth by the midship beam; the builders are pretty much divided in proportioning this to the length. Most of them conform to dimensions taken from ships of the same burthen, and designed for the same service.

After these two dimensions are determined, the depth of the hold must be fixed, which in most ships is half the breadth; but the form of the body should be considered; for a flat floor will require less hold than a sharp one. The distances likewise between the decks must be determined. The following table may be very useful towards ascertaining the three aforesaid dimensions.

A Table of the Length, Breadth, and Depth in Hold of the following Ships.

Ships Names	Guns	Length at	Breadth	Depth in		
Ships Ivanies	Guns	load-water	breadth	the Hold		
	-	feet in.	f. in.	f. in.		
Monarque	- ·					
Intrepide	74	165	43			
Alcide	74 64	165	43			
Renommée		149		19 4		
Palme	30	120		15 7		
Soleil Royal	80	85 182		10 5		
Formidable	80		48	23		
Tonnant	80	178	46	21 10		
Sceptre		165		23		
Superbe	74 74		43			
Esperance		1 23		21		
Magnifique	74	154	42	20 6		
Northumberland	74 68	165	43			
Lis	64	149	40	20		
Hercule	64	149	40 6	19		
Protee	64	149	40 6	19 4		
Illustre	64	150		19 4		
Opinatre	64	150		20		
Dragon	64	150		19 5		
Leopard	64	149	30 6	18 6		
St Laurent	60	146	33	18 8		
Amphion	50	145		18		
Amazon •		145	39	10		
Brillant	44 50		25			
Arc-en-Ciel	50	135	35	17 0		
Tigre		135	37	17 9		
Alcion	5 ² 5 ⁰	131	37	17		
Aquilon	46	132	35 4			
Junon	46	136	34 36 6	16 6		
Favorite	36	127	,	14		
Anglesea	32	121 8	33 6	16		
Serenne	30	118	50			
Emeraude	28	118	31 8	15 9		
Galatée	24	110	29	14 6		
Mutine	24	110	29	14 6		
Cumberland	24	102	26	13		
Marshal Saxe	22	100	27	14		
Anemone	12	84	22	9		
	1	1 04	1	1 9		

Ships Names	Guns	Length	Breadth	Depth
		feet	f. in.	f. in.
Amarante	12	84	22	9
Elizabeth	64	143	38 4	9 18
Brave	80	172	44	2 I
Florissant	74	165	45	22 6
Couronne		167	44	22 7
Hardi	74 64	149	40 6	20 9 10 6
Aigle	50	144	39	
Hermione	26	126	39 33 8	. 13 8
Juste	70	151	42	21
Triponne	26	114	31 8	
Panthere	20	108	28 6	
Badine	6	66	18 4	

We may then proceed to fix the length of the keel, which will oblige us to determine the rake of the stem and post, for which the builders have given us no invariable rule, they being very much divided in their opinions; for where some have given a rake of 18 or 20 feet, others have given none at all. The height of the stem and wing-transom must also be determined, which may be regulated by the decks.

The difference betwixt the draught of water abaft and that afore, should likewife be considered; for though some imagine that when a ship is loaded her keel should be parallel to the surface of the water, yet in many cases it will be found necessary that the keel abaft should be deeper in the water than it is assore. This will give the rudder more power, and thereby contribute to make a ship steer well; but this difference of the draught of water is intirely arbitrary; for in large ships some have given shive, whereas others have given but three, or even two feet of difference. Though I could not procure the true difference of the draught of water of many shipsof war, yet I am assured that the following are pretty exact.

The Difference of the Draught of Water in the following Ships.

	feet	in.	11	feet	in.
Northumberland	1	2	Panthere	1	4
Auguste	1	6	Couronne	2	I
Aloze	1	0	Triponne	2	
Hermione	2	0	Renommêe	1	4
Amazone	1	6 .	Tigre	3	2
Badine	0	10	Intrepide	2	3
Palme	I	4	Alcide	2	0

The

The length of the wing transom must also be determined; some make it $\frac{1}{2}$ of the main breadth; but this is likewise arbitrary, the broader a ship is abast, the more room there will be for accommodations for the officers; but this will be disadvantageous to her sailing upon a wind.

The following Examples will be fufficient to fix the Length of the Wing transom for any Ship,

For a ship of 110 guns, $\frac{a}{3}$ of the main breadth, and 3 lines more to every foot-102 guns, $\frac{a}{3}$ of the main breadth, and 8 inches more.

82 guns, 3 of ditto.

74 guns, 7 inches, 9 lines for every foot in breadth.

62 guns, 7 inches, 8 lines for ditto.

56 guns, 7 inches, 7 lines, 3 points for ditto. 50 guns, 7 inches, 6 lines, 6 points for ditto.

46 guns, 7 inches, 6 lines for ditto.

32 guns, 7 inches, 51 lines for ditto.

For a frigate of 22 guns, 7 inches 4 lines.

12 guns, 7 inches.

Some, without regarding these proportions, make the wing transoms of the first and second rates two thirds of the breadth, and for all the rest one foot less.

After these dimensions are determined, the timbers may be considered which form the sides of the ship. A frame of timbers is composed of one short timber, two or three suttocks and a top timber on each side: All these being united together, and secured by cross-bars, form a circular inclosure, that which incloses the greatest space is called the midship frame: The curve of this frame is inverted at the lower part, so that the floor timber will be somewhat hollow in the midsle, whereby the ends will form a very obtuse angle; but this angle decreases the farther the frames are removed from the midships, in such a manner, that the foremost and aftermost will become very sharp, and form a very acute angle. These floor timbers are called crutches.

The builders feem to agree nearly as to the length of the midship floor timber, making it generally half the length of the main beam; but they differ very much about the rising of it, some chusing a flat and others a sharp floor. And if we consider the advantages and disadvantages that attend the one and the other, we shall not be much surprized to find them so much divided upon this article; for it is certain, the more rising a ship has, she will hold the better wind, but then this will occasion her to draw more water, which will be sometimes attended with very

great inconveniencies.

A Table of the rising of the Midship Floor Timbers.

Guns	f.	in.	lines	1	Guns	f.	in.	lines >	
110	0	0	10		56	0	1	4	2
102	0	0	101	to every foot in length.	32	0	I	4	to every foot
86	0	1	0	in length.	28	0	1	4	in length.
74	0	I	0		22	0	I	6	
62	0	I	0 1 J		16	0	1	6.)

Note, What we have here rendered the rifing of the floor timbers, the author calls the Aculement, and makes a diffinction betwixt it and the

rising, which we shall see when we come to form the frames.

They differ as much in determining the flation of the midship frame, some placing it before, others at the middle of the ship; others again have two shoor timbers of equal length, and rising, one of which is placed exactly in the middle, or the breadth of the timber before the middle, and the other at a proper distance before it. Those who place it before alledge that if a ship is full forward, after she has once opened a column of water, she will afterwards meet with no resistance, and the water will easily unite abast, and by that means force the ship a-head, and have more power on the rudder the farther it is from the centre of gravity; and besides this comes nearest the form of sithes, which should seem to be the most advantageous for dividing sluids.

Those who would have it placed in midships say, that by that means the water-lines forward will be easier, and of consequence properer for dividing shuids; and that there will be space enough betwixt it and the rudder for forming very sair water-lines, so that the water will easily unite at the rudder; and besides it will be easier by this means to balance the sore body and after body; and in general the building will by this means be very much sacilitated: so that, in my opinion, it will be properest to place it very near the middle, though it is the general

practice to place it before it.

After the rifing of the midship floor timber is determined, we may then proceed to fix the height of the rifing line of the floor abaft on

the post, and afore upon the stem.

Now, as all ships are narrower abaft and afore, than in midships, the other floor timbers will of consequence be shorter and have a greater rising, which will be still increasing till it ends on the post and stem. There are several different methods used by the builders to settle the height of this line. Some imagine, that by narrowing the floor abaft, which will occasion the rising line to be high upon the post, the ship will

will thereby steer better, and besides, the water which is opened by the midship frame will then have a greater pressure upon the after part of the ship, and thereby contribute to her failing: Yet these arguments are of very little weight; for if we only confider the steerage, it is certain, that the higher the rifing line is carried abaft, and the narrower a ship is, the water will have the easier passage, and more power upon the rudder. But then we shall thereby run the risk of falling into two great inconveniencies; for by this means we take away the buttock, which is the only thing we have to support all the weight of the after part of the ship; neither shall we be able to give a proper balance betwixt the fore and after part, and when the fore and after parts are not duly balanced, it will occasion a ship to pitch very hard, and be in danger of being frequently pooped by the fea when it runs high. To prevent these inconveniencies it will be proper to give all ships, especially the large fort, a full buttock. As to the height of the rifing line afore, it should be determined by the form of the water lines; but before this can be done, the timbers must be formed.

Note, What we have rendered the rifing line of the floor, our author calls les façons, which, he fays, is the increase of the acculement, the extreme points of which upon the perpendicular of the flem and post, are now to

be determined.

The height of the lower deck is the next thing to be confidered: It is determined in midfhips by the depth of the hold, and fome builders make it no higher at the ftem; but they raife it abaft more than it is in midfhips, as much as the load-water mark abaft exceeds that afore. As to the height betwixt decks, it is altogether arbitrary, and must be determined by the rate of the ship, and the service that she is designed for.

We come now to confider the upper works, or all that is above water, called the dead-work: And here the ship must be narrower, so that all the weight that lies above the load-water line will thereby be brought nearer the middle of the ship; by which means she will strain less by working the guns, and the main sail will be easier trimmed when the shrouds do not spread so much. But though these advantages are gained by narrowing a ship above water, great care must be taken not to narrow her too much, for there must be sufficient room upon the upper deck for the guns to recoil. The security of the masts should likewise be considered, which requires sufficient breadth to spread the shrouds, though this may be affished by enlarging the breadth of the channels.

C H A P. II.

Of the Scantlings and Dimensions of the principal Pieces of Timber in a Ship.

A LTHOUGH it is not my intention, as I observed in the beginning of the last chapter, to treat of all the pieces that compose the ship, yet I think it necessary to say something of the principal pieces. I shall therefore in the following plate lay down each piece by itself, by which means we shall see the length of the scarphs, and in what manner they are to be joined together.

Explanation of Plate I.

I.

A. The keel in four pieces, to be well bolted together, and clinched.

II.

I. The fore foot, one end of which is fcarphed to the fore end of the keel, of which it is a part, and the other end makes a part of the stem, to which it is scarphed.

III.

u u. Two pieces of dead wood, one afore and the other abaft, fayed upon the keel.

IV.

C C. The stem in two pieces, to be scarphed together.

V.

E.E. The apron in two pieces, to be scarphed together, and fayed on the inside of the stem, to support the scarph of the stem; for which purpose the scarph of the apron must be clear from that of the stem.

VI.

o. The stemson in two pieces, to support the scarph of the apron. o. The false post, which is sayed to the fore part of the post.

VII.

B. The stern post: It is tenanted into the keel, to which it is fastened with a knee.

D. The

VIII.

D. The back of the post, which is likewise tenanted into the keel and well bolted to the post; the design of it is to give sufficient breadth to the post, which seldom can be got broad enough in one piece.

IX.

F. The knee which fasteneth the post to the keel.

X.

N. The wing transom. It is fayed across the stern post, and bolted to the head of it: The fashion pieces are fastened to the ends of it; underneath this and parallel to it is the deck transom.

XI.

OO. Two transoms fastened to the stern post and fashion pieces, in the same manner as the wing transom.

XII.

P. The transom knee, which fasteneth it to the ship's side.

XIII.

Q. The fashion piece, of which there is one on each side: Their heels are fastened to the stern post at the height of the sloor ribbands, and their heads are fastened to the wing transom.

XIV.

T. A floor timber. It is laid across the keel, to which it it sastened by a bolt through the middle.

XV.

K. The lower futtock,

XVI.

TTTTT. 2d, 3d, 4th futtocks and top timbers. These shew the proper length and scarph of the timbers in midships frame.

XVII.

U U. Riders. These are fayed in the inside of the ship, and consist of floor and futtock riders,

C 2

Z. The

XVIII.

Z. The keelfon. This is made of two or three large pieces of timber fearphed together in the fame manner as the keel. It is placed over the middle of the floor timbers, and fcored about an inch and a half down upon each of them.

XIX,

R, S. Breast-hooks. These are sayed in the inside to the stem, and to the bow on each side of it, to which they are fastened with proper bolts. There are generally four or five in the form of R in the hold, one in the form of S into which the lower deck planks are rabbited; there is one right under the hawse holes, and another under the second deck.

XX.

X, Y, Z. are thick planks which are fayed in the infide, and ftretch fore and aft to strengthen the scarphings of the timbers.

XXI.

Z. are thick planks in the infide, called clamps, which support the ends of the beams.

XXII.

15, 15, 15, 15, 15, are the wales. They are planks broader and thicker than the reft, which are faftened to the outfide of the ship in the wake of the decks. We shall have occasion in another place to show how they are laid down in a draught. As to the plank below the wale to the keel, and above it to the top of the side, we refer to the section of one half of the midship frame, as laid down in the plate.

XXIII.

d, d, d, d, d, d, d, are knees. These are crooked pieces of timber confishing of two arms which form an angle, either within or without a square, or exactly square; their use is to fasten any two pieces together, as the beams to the ship sides.

XXIV.

19. The rudder. This is joined to the stern post by the rudder irons, upon which it turns round in the googings which are sastened upon the stern post for that purpose. There is a mortise cut out of the head of

it, into which a long bar is fitted, called the tiller, by which the rudder is turned from one fide to the other.

XXV

23. The cat heads. These are two large pieces of square timber, one on each side of the bowsprit. They project out before the bow, in order to keep the anchor clear of the ship, which is hove up by a rope called the cat fall, that passes through shivers in the outer end of the cat-head: Their inner ends are fastened upon the forecastle.

XXVI.

m, m, i, i, i, are the several pieces which compose the knee of the head; the lower part m is fayed to the sten, the heel of it is scarphed to the head of the foresoot; it is fasten'd to the bows by two knees called cheeks, in the form of f, and to the stem by a knee call'd a standard, in the form of f.

XXVII.

Beams &, a, X Y, are large pieces of timber which support the planks of each deck.

Having thus explained all the pieces in the plate, we shall in the following table give their scantlings.

SCANTLINGS of the principal Pieces of Timber in a SHIP.

	Taansoms Wasses (TIMBERS	Planchere thick Thwa STEM {Fore; Ditto, false or STERN-POST:	KNEES	BREAST F	
	Deck fecond fecond iff and 20 gd and 4t gth and 60	Floor Spece	arthips and aft, apron thic Thick	rst deck cond deck parter decl op {Si op {M		BREADTH LENGTH I
	Sided Sided Sided Thick Sided Start St	Above al on the key and in at the and in at the Broad Out and in Out and in Out and in	k Below	'.ı 🖹	d d forecafile { Sic	5 5 T
Now, The		keel keel keel keel keel keel keel keel werdeck the lower deck in at the lower deck in at the head knd in { Aloft kloft		Side Moulded	as thick as the rim	CANTLINGS OF the SHIPS of SHIPS of SHIPS
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C H A P. III.

A Method to lay down a 70 Gun Ship upon the Plane of Elevation.

THE Dimensions we have given of the principal parts of a ship of each class collected from the practice of different builders, which many have so great a regard to, as not to vary from them in the minutest article, we think only to be so far observed, as they shall produce such a form as the service the ship is designed for, shall require, agreeable

to mathematical principles.

We shall now illustrate what has been said on that head by drawing a ship from these dimensions. But it will be first necessary to observe, that the builders make use of three different planes for one ship; sit, the plane of elevation, in which the whole length is laid down according to a side view; 2d, The plane of the projection, which some call a vertical plane of the timbers, because it gives us an end view of the form of all the timbers, before the plank is put on. 3d, The horizontal plane, upon which are described all the curves that are formed by sections of the body parallel to the horizon, which must be considered as well as those vertical sections which form the curves of the timbers. We may likewise form the curves of the ribbands upon this plane, which will be of great use in proving whether the form we give the timbers will produce a fair side.

It is indifferent with which of these we begin, though that of the elevation seems most commodious. But first of all it will be very proper to draw out a list of all the dimensions of the vessel we are to build, so that we may have a view of the whole design.

This ship then is to have two tier of guns, so there must be two decks quite fore and ast, likewise a quarter deck as far as the main mast, a fore-

castle 33 feet long, and a poop to the mizen mast.

There are to be 13 ports of a fide on the lower deck, the guns to carry 24 lb. shot; 14 ports on each fide upon the upper deck, the guns to carry 18 lb shot; on the quarter deck 4 guns, and on the forecastle 2 guns of 8 lb. shot on each fide, and 2 of 4 lb. on each fide on the poop.

of the Plane of Elevation.	CHAP. III.
and the second second second second	feet in l.
Ports on the lower deck fore and aft	2 10
Distance betwixt the ports	7 9
Aftermost port from the post	9 3
Foremost from the stem	· 17 2
Height of the fells, including the lower deck planks	2 5
Ports up and down on the lower deck	2 7
Distance from the upper side of the lower deck bear	n to the ?
upper fide of the upper deck beams	6 11 -
Rifing of the fecond deck abaft -	
Second deck ports up and down	2 4
Second deck ports fore and aft -	2 6
Height of the fells from the deck line -	I II 6
Distance betwixt the second deck and quarter de-	ck from)
plank to plank	6 6
Quarter deck ports up and down	I 10
Quarter deck ports fore and aft -	- 2
Height of the fells —	<u> </u>
Distance betwixt the quarter deck and poop -	<u> </u>
Ports on the poop fore and aft	1 10
Height of the fells — —	I O
Length from rabbit to rabbit on the gun deck	 156 3
Extreme breadth	42
Depth in the hold below the plank	21 0 0
Rifing of the lower deck abaft, not including the di	ifference 7
of the draught of water	fference \{ 2 \text{II} 6
Height of the stem	31 9 3
Height of the post	31 7 9
Rake of the stem	15 7 2
Rake of the post	3 I 5
Length by the keel -	 139 6 10
Depth of the keel	- I 7 3
Length of the wing transom	27
Length of the midship floor timber	21
Rifing of ditto	1 9
Difference of the draught of water abaft more than	afore 3 2 0
Height of the rifing line of the floor abaft -	- 13 6 0
Height of the rifing line of the floor afore	5 7 5

I would advise young beginners in the art of drawing to conform exactly to these dimensions, which we have here given for an example, and

and observe all the particular directions which we shall give in laying down a ship of 70 guns; for they much begin by making themselves acquainted with the terms, and thereby gain a general idea of the whole defig. After finishing this draught, they may then proceed to another of a different rate, and as we have given the principal dimensions of several good ships, they may chuse such a one as will best answer their defign.

Plate II. Fig I.] 1st. Provide a scale of equal parts properly divided into feet and inches, adapted to the intended length of the draught, and draw the line A B, which make 156 feet 3 inches for the length of the gun

deck, from the rabbit of the stem to that of the post.

To find the length on the gun deck, multiply 13, the number of ports, by 2 f. 10 in. the dimensions of each port 36 10 0 forc and aft, the product is

Again multiply 7 f. 9 in. the distance betwixt the ports, by }

Aftmost port before the post
Foremost abase the ftem
Length on the gun deck

12, the number of spaces, the product is

9 3 0
17 2 0
156 3 0

adly, Draw the line CD equal and parallel to AB, let 21 feet, the half of the main breadth, be the distance betwixt them, and erect the perpen-

diculars CF and DZ.

3dly. Set off 3 feet 2 inches, the difference of the draught of water, from B to G, and draw the line AG, which will give the position of the lower side of the keel. From A set off 1 foot 7 inches 3 lines, the depth of the keel, as in the table of scantlings, to K, and draw the line KI parallel to AG, which will be the upper side of the keel.

4thly, Set off 1 foot 3 inches 3 lines, the breadth of the stem from G to M, and draw the dotted line M N parallel to G Z. From G set off

15 feet 7 inches 2 lines, the rake of the stem, to O.

5thly, Set up 31 feet 9 inches 3 lines, the height of the stem from G to P. With the radius I P describe the arch P O, which will be the fore side of the stem, and from the same center describe another arch within the former, which will give the inside of the stem, and another arch for the rabbit may be described four inches before the inside of the stem.

6tly, Set up 25 feet 1 inch from K to L for the height of the gun

deck abast, and 21 feet 6 inches from I to e, for the height afore.

7thly, Set up 2 feet 5 inches, the height of the port-fells from L to a, which will give the upper fide of the wing transom; from which fet up

D
2 feet

2 feet 7 inches, the height of the ports; also 1 foot for the depth, and 6 inches 9 lines for the round of the helm port transom, to the point F. which will be the height of the post; so KF will be 31 feet 7 inches 9 lines. From K fet off 3 feet 1 inch 5 lines to f, for the rake of the post, and draw the line Ff for the ast side of the post. From f to b fet off the depth of the keel, and draw the line bd for the fore fide of the post, making $F d^{\frac{3}{4}}$ of fb, so shall f O be the whole length of the keel.

The builders are very much divided about affigning a proper place for

the midship frame, for which the following method may be used:

Divide the line CD into two equal parts, then take 5 feet 6 inches 10 lines, that is is part of 156 feet 3 inches, the length of the gun deck: Set off this before the middle of the line CD, which will give the point F the station of the midship frame. Set up 21 feet from F to Z, which will give the height of the gun deck at the midship frame. From the point Z fet off 2 feet 7 inches 6 lines (the * of the height of the gun deck at the midship frame,) through which point draw a line VT. parallel to CD, which will be the load-water line. Through the point F draw the line Gg, parallel and equal to the load-water line, which will shew how much water the ship will draw abast more than afore.

One of the frames is placed pretty near the chefs tree, which is called the loof frame; to find its place, from the point of D fet off i of the line D.C, and there draw a dotted line perpendicular to A B. Again divide the line FG into nine equal parts, and draw eight lines perpendicular to A B, which will station eight frames in the fore-body besides that of

the loof.

There is in the after-body a frame to balance that of the loof in the fore-body; these two are of equal breadth in some points, and this will occasion the center of gravity of that part contained betwixt these two frames to be near the plane of the midship frame, which will keep the fore part and after part upon a balance. It must be as far abaft the middle of the line CD as that of the loof is before it.

The frames in the after-body are the same distance from one another as they are in the fore, which will occasion one more abaft than before;

so there are nine abast, besides that of the balance.

We shall in the next place lay down the deck lines, and first for the lower deck draw a fair curve through the points L Z e, and parallel to it draw another curve for the port-fells, which are 2 feet 5 inches above the deck line. The sound of the sound of the state of the The

and an make that is it is upon as may be discussed

The aftermost port is 9 feet 3 inches before the post, which set off to u, and the ports are 2 feet 10 inches fore and ast; which set off from u to x, the distance betwixt the ports is 7 feet 9 inches, which set off from x to Y for the aft side of the second port; from Y again set off 2 feet 10 inches, which will give the soreside of the next. Proceed in the same manner till all the ports are spaced; so shall the foremost port be 17 feet 2 inches abast the rabbit of the stem. The height of the ports is 2 feet 7 inches; which set up from u, draw a curve parallel to the deck line, which will give the upper part of all the ports; after which these two lines may be wiped off the draught, which must be therefore drawn with a black lead pencil, and only the ports inked in.

Draw a line for the upper deck, which is 6 feet 11 inches above the lower from the midfhip frame forward, and 6 inches more abaft. We may then draw a line for the port-fells, and one for their height parallel to the deck line, and space the ports so that they may be exactly over the mid-

dle of the distance betwixt the lower deck ports.

Before we can fet off the height of the Quarter deck we must find the true place of the main mast. The general rule is to take 4 lines for every foot the gun deck is in length, and fet it off abaft the middle, which will give the fore fide of the mast: now the length 156 feet 3 inches × 4 lines = 625=4 feet 2 inches 1 line, which fet off abaft the middle of the line CD, and there erect a line perpendicular to the water-line, which will be the fore fide of the malt, and parallel to it draw a line for the middle, and one for the aft fide of the mast, the diameter of which is 35 inches. Set off 6 feet 6 inches on the aft fide of the main mast, for the height of the quarter deck afore, and 6 feet 10 inches for the height abaft; and draw a line nearly parallel to that of the upper deck, which will be the line for the quarter deck. We may then space the ports. fo that they may be exactly over those of the lower deck. The forecastle is 6 feet 6 inches high, at which distance draw a line parallel to the upper deck line, which will give the line for the forecastle deck. As to the length of this deck, it ends forward at the beak head, and is carried aft diferetionally, observing to leave room for the capstan bars. In spacing the ports upon the forecastle, care must be taken that none be oppolite to the fore mast. Now to find the center of this mast, take 15 feet 7 inches 2 lines, the tenth part of the whole length, which fet off from the rabbit of the stem upon the lower deck abast, from which point set off 32 inches and 1 line, being the diameter of the mast, through the middle in of this draw a perpendicular line, as in the plate. The boltfprit generally makes an angle of 34 or 35 degrees with the load-water line.

The poop is pretty near parallel to the quarter deck; the distance betwixt them forward is 6 feet, an abast 6 feet 3 inches. It ends about 18 inches before the mizen mast, the ast side of which is $\frac{2}{3}$ of the main

breadth before the rabbit of the post upon the gun deck.

The counter is generally an arch paffing from the upper fide of the wing-transom to the lower fide of the beam of the second deck. The rake of the lower counter is $\frac{2}{3}$ of an inch for every foot of the main breadth. The rake of the second counter is $\frac{2}{3}$ of the lower; its height above the deck is 3 feet 5 inches. The hollow of the counters is altogether arbitrary, infomuch that some give none to the lower. The upright

of the stern rakes 2 inches in a foot, as in the plate.

The beauty of a ship depends much upon giving the wales a proper hanging; for by them the sheer and drift rails are regulated, being all nearly parallel to one another, though they generally rife a little more abaft on account of the accommodations for the officers. It is this which makes a ship look airy and graceful in the water. There is no certain rule for laying them down; this is left entirely to the fancy and taste of the artist; but in placing the wales great care must be taken that they be wounded as little as possible by the ports; the foremost port on the gun deck must be 11 or 2 inches above, and the third port from abaft just touch the upper side of the upper strake of the main wales. The lower edge of the lower strake may glance with the edge of the water when loaded. There are two firakes of wales, and one firake between them of 15 inches broad each. The range of the deck should be considered in placing the wales, so that the scuppers may be in the strake betwixt the wales. The like caution must be used for the channel wales as may be feen in the plate, where they are all laid down, together with the sheer and drift rails; the rails, cheeks, and knee of the head are likewife laid down in the plate, and being for an ornament to the ship, are left to the fancy and taste of the builder. Though the knee may help a thip to hold a good wind, the fore part of it is generally one twelfth. part of the length before the stem. record with the control of the control of the

C H A P. IV.

To lay down the Frames upon the Plane of Projection.

upon the plane of elevation, the next thing to be delineated upon the plane of elevation, the next thing to be determined is the different breadths of the flip at any affigured points of the length, whereby we shall gain the forms of all the planes that are made by sections, perpendicular to the load-water line. The timbers that compose the body of a ship are supposed to have their planes in that position, and may be all delineated upon the plane of the projection; but as both sides of a ship are exactly the same, it will suffice to lay down the half of each, those of the fore-body on the right, and those of the after-body on the left hand. And whereas these planes diminish afore and aft, the planes of all the frames may be all delineated upon the plane of the mid-ship one, which may be called the master frame. The first thing then necessary to be known is how to form this frame.

The mid-ship frame is that which is at the broadest part of the ship. The builders differ about the form of this frame, but there are several preliminary operations which are necessary to be observed in all the dif-

ferent methods used in forming it.

Preliminary Operations for forming the Midship Frame,

Plate III, Fig. I. and II.] 1ft. Draw the line AB to represent the upper side of the keel; it must be at least as long as the ship is broad. This line our author calls the line of aculement, because upon it the aculement of the midship shoot timber terminates.

adly, Draw the line CD parallel and equal to AB, so that AC and BD may be equal to the rising of the midship floor timber. This line may be called the rising line, because it limits the height of the ends of

the midship floor timber above the keel.

3dly, Draw the line G H for the height of the lower deck parallel to the former, and below this draw a line to reprefent the load-water line, taking its diffance below the deck line from the plane of elevation at the midfhip frame. Draw alfo the lines I K and L M, the one for the fecond deck, and the other for the finer rail or top of the fide in midfhips. The height of both are to be taken from the plane of elevation.

4thly, Draw the line NO perpendicular to AB; this is called the middle line, and represents the middle line of the stem and post, dividing the whole ship into two equal parts; and parallel to NO draw the lines AL and BM, to limit the breadth; also a line for half the thickness of the stem, and one for half the thickness of the post. Draw the lines at parallel to NO, dividing the lines OA and OB into two equal parts. Draw also the diagonal GB. These lines being drawn, we may proceed to form the midship frame by some of the following methods.

METHODI.

To form a Midship Frame that shall be neither too sharp nor too stat.

Plate III. Fig. I.] 1st, Divide the line ax, which marks the head of the

floor timber into three equal parts; fet off one from a to b.

2d, Divide the line dB, the diffance betwirt the load-water line and the upper fide of the keel, into feven equal parts; fet off one of thefe from d to e, and from e to m, and draw the diagonal a V, which divide into two equal parts in the point m. Note, the diagonal a V is wiped

out after finding the point n.

3d. Describe an arch of a circle to pass through the points b and e, make the radius the whole length and half the length of the line Be, so the center A may be found by describing an arch with that radius from e, and one from b to intersect one another in A, we shall only make use of that part of this arch betwixt l and m. Now, to find the other arches m d, la, au, nV, it must be observed, that in order to reconcile two arches, so as to make a fair curve, a strait line must past through the centers of both, and through the points where they unite or touch one another; draw therefore the lines Am and Al, so shall k be the center of the arch md, and o the center of the arch la. Again through the center o draw the line ao, produce it to P, which will be the center of the arch an. Lastly, from P thro'n draw the line Ps, s will be the center of the inverted arch n V. Note, the center s will be without the Plate.

4th. To form the top timber fet back the tenth part of the half breadth from K to S, upon the line of the fecond deck; describe an arch of a circle thro' the points d and K, taking $\frac{1}{7}$ of the whole breadth for the radius: Again, from the point M, upon the line LM, fet back the fifth part of the whole breadth to g. Describe an arch of a circle through the points S and I, taking the diagonal GB for the radius. As this arch is inverted in respect of the arch dS, the center will be without the figure. This compleats the form of half the midship frame, and by the same ope-

rations we may find the other half.

It must be observed that there is no regard had to the round of the beam in setting off the deck line or depth of the hold.

M E-

METHOD II.

To describe a Midship Frame of a circular Floor.

Plate III. Fig. II.] From the center G, the point where the middle line interfects the deck line, making the half breadth the radius describe the arch b, G, c, O: Let d be the head of the floor timber, and $d \times$ the rising. Assume the point f, according to what round you propose to give to the second futtock, and describe the arch df; the center may be sound as directed in the preceding method. Divide the arch c O into three equal parts; set off one from c to g, and from the center h; describe the arch dg: there remains only the inverted arch g Y to be described; the center may be sound as before directed.

METHOD III.

To draw a Midship Frame which shall be very full.

Plate III. Fig. III.] 1ft. Draw the rifing and deck lines as before; let dx be the rifing.

2d. Make db the fide of the fquare dbac equal to Cb the + of the breadth.

3d. Inscribe the two quadrants ceb, and cfb into the square.

4th. Divide the fide ca into a certain number of equal parts in the points O, N, M, La; draw the lines i L, h M, &c. perpendicular to ac.

5. Divide the line CG, the depth of the hold after deducting the rifing, into the same number of equal parts in the points E, F, I, K, and make the lines Ep, Fq, Ir, Ks, in the frame, equal to the lines Ot, Nn, Me, Lm in the square, describe a curve through the points G, P, q, r, s, b, and the remaining part of the frame may be described by the preceding methods.

METHOD IV.

To describe a Midship Frame for a very sharp Ship.

Plate III. Fig. 1V.] Let the length of the floor timber be half the breadth as before, and the rifing one fifth or one fixth of the whole length of the floor timber; lay this off from x to E, and deferibe a parabola through the points G, P, Q, E, of which the point G is the vertex, and GC the axis. This method is extracted from M. Bouguer. The parabola may be formed by the following method: 1. Through the point E draw the line Tx perpendicular to GC, and the line dE perpendicular to AG, and produce

produce the line GG to D. 2dly, Upon the line GD find the center of a femicircle that shall pass through the points T, d, and D, so shall GD be the parameter of the parabola, by which we may find any number of points through which the curve must pass: for instance, suppose, it were required to find a point in the post-cocicular XP, through which the curve must pass; upon the line GD find the center of a semicircle which shall pass through the points D and X; this will intersect the line AG in b, make b P equal and parallel to GX, so shall P be the point required; in like manner the points a Q f may be found. The remainder of the curve from E to g will be composed of two arches, the one to reconcile with the parabola in the point E, and the other inverted to pass through the point g; the center of which may be found by any of the preceding methods. In order to find the center of that which joins with the parabola make T R equal to half the parameter G D, and draw the line E R, upon which find a point S for the center of the arch.

We might shew a great many more methods of describing this midship frame. It is very true that great care ought to be had in forming this frame, because upon it chiefly depends the form of all the other timbers; I say chiefly, but not altogether; for two ships may be similar as to their midship frames, and yet very different afore and abaft; and though the artists should make themselves acquainted with all the different ways of forming this frame, I should recommend that method to them which is the simplest and which gives them the most liberty to vary the form of it, according to every one's particular taste or fancy; and it is very possible there may be several other methods as easy and plain as those we have described. This frame being once formed, we may form all the rest upon the same plane. We shall in the next place shew the different methods

used by the builders for that purpose.

The ancient builders not being acquainted with the methods of laying, down their defigns in a draught, found out a mechanic way of doing this only by help of the midfhip frame, which they might have formed by fome of the preceding methods or any other contrivance of their own; and though this method is defective in feveral points, yet as it is an ingenious contrivance, we shall give it a place here.

METHOD I.

Of forming the Timbers by a Mould made to the Midship Frame; a rising Staff and overcast Staff (*

Plate III. Fig. VII.] 1st. Having formed the midship frame and set off its scantlings, make a mould to sit both outside and inside, which may be called the bend mould

2d.

2d. Draw the line $Z \mid x$ to limit the head of the floor timber at d; let $d \mid u$ be the rifing, and draw the line $a \mid u$; let t be the height of the rifing line abaft, and draw the line $d \mid t$ to represent the floor heads, or floor ribband. Set off $d \mid x$ from d to H; and from e, the head of the first suttect, to e, and divide each into six equal parts, being the number of frames from midships to the balance frame.

3d. Divide the line au into five equal parts, and set off two of them from a to S; divide the line a S into the same proportion, that the part A δ of the base A C of the right angled triangle $(\beta g. 5.)$ is divided into, and transfer these divisions to the bend mould, and let them be numbered o, 1, 2, 3, 4, 5, 6, which points will give the narrowing of the floor, as we shall show, after constructing the triangle. We shall only remark, that the line a S, which is $\frac{1}{3}$ of au, is nearly the difference betwixt half the length of the midship floor timber, and half the length of the floor timber at the balance frame. But as this appears to be too much, we may take $\frac{1}{6}$ as in the figure, or any other quantity which shall be thought most convenient.

To construct the Triangle, Fig. 5.

Upon the line A C, drawn at pleasure, set off any distance from A to 1, and double that distance from 1 to 2, treble from 2 to 3, and so on in the same progression till we have as many divisions on the line A C as we propose to have frames abast the midship. Erect a perpendicular at A, which may be produced at pleasure, and from any point B draw lines to all the divisions of the base A C. Observe that though in the triangle we have drawn a line for every frame to the saline frame. The triangle being thus constructed, apply the line a S to it, in such a manner, that it may be parallel to A C, and be contained betwixt the lines B A and B 6, the lines drawn from the point B to the points 1, 2, &c. will divide it into the required proportion.

To coustruct the Rising Staff, Fig. 5.

This staff K may be of the same breadth with the keel, and a little longer than at, the height of the rising of the floor. In order to graduate that staff, set off xu, the rising of the midship floor from K to o, and make oL equal to at; apply the line oL to the triangle, so that it may be parallel to the base, and contained betwirt the lines AB and BC the

E lines

lines from the point B to the feveral points in the base will divide it into the required proportion, which will give the rifing of the floor.

Note, Our author calls x u the acculement, and u d the rifing ; the line u a will pass through the point where the inverted arch joins the floor sweep.

To construct the over cast Staff, Fig. 5.

That we may have a clear understanding of what is meant by overcast, it will be proper to observe, that in forming the frames by the bend mould, when it is fet to the narrowing of the floor, the head of the mould will come too far in at the deck; the mould must therefore be moved round upon the point which represents the floor ribband, till the head goes out to the proper breadth; this will occasion the lower part of the mould to rife a certain quantity, which is called the over-cast. In order to graduate this staff we must determine the difference betwixt the main breadth at the midship frame, and at the balance frame, which suppose DF, let this be placed parallel to the base, and contained betwixt the line BA and B6; fo shall the lines B6, B5, &c. divide it into the required proportion.

These are the instruments that are necessary for forming the after frames, those for the fore part are constructed in the same manner, only the graduations for these are but half the graduations of the former, for which reason there must be another bend mould graduated for the

fore body.

Now, in order to form the frames by these instruments, place the bend mould upon the rifing staff in such a manner that the middle line of the staff produced may pass through the narrowing of the floor upon the bend mould, expressed by the division corresponding to the frame to be formed; suppose frame 6, (Fig. 7.) the lower or strait part of it expressed by the dotted line in the figure being applied to the rifing staff, till the middle line B a pass through the division 6 on the bend mould: mark by the edge of the rifing staff the point 6, which expresses the rifing of the floor at that frame. Set up the over cast (expressed by the space contained betwixt the points 5 and 6 upon the over cast staff) from the lower part of the bend mould to the point 6 upon the line Ba; then keeping the point d immoveable, turn the bend mould upon this point till the lower part rife to the overcast at the point 6 upon the line Ba, and when in this position we may describe the curve to the floor head, and then invert the bend mould, and placing the point 6 (betwixt d and H) to the point set off before to express the rising, turn the mould till the strait part touch the curve before described, and then draw the

lower part, which compleats the frame.

This is the method that is used when they mould the timbers, and it may likewise be used to lay them down upon a draught; for if the line au of the bend mould (Fig. 8.) be laid upon the line A V, we may, when in that polition, describe the midship frame from the point d to the point X. In like manner we may describe all the rest of the frames, by giving each its proper over-cast and rising; as for instance, if it were required to describe frame 6, take the rising K 6 upon the rising staff, and set it off from the point B to the point a upon the line BG, and draw a line through the point a parallel to AV, upon which laving the bend mould in fuch a manner that the point 6 which expresses the narrowing of the floor, shall be upon the point a; then will the point d be upon the point RS: fet up the proper over-cast from a to 6, and keeping the point dimmoveable, push up the bend-mould which at first was placed at the point a, till it be raised to the point 6, which will throw out the point X to the proper breadth at the deck. But because the deck is higher at timber 6 than at the midship frame. Take the distance betwixt e and 6, at the head of the futtock on the bend mould, and fet it up from x to 6, and then inverting the bend mould, fo that the point 6 betwixt d and H be at the point X, and the strait part of the mould touch the curve before described: we may then describe the lower part to the point X, which compleats the whole frame. The timbers for the fore body may be described by the same process as those of the after body, only making use of the bend mould, rifing and overcast staff graduated for that purpose; but as we observed before, we cannot lay down any timbers by this method but those betwixt the midship and ballance frame.

The builders finding how very advantageous it would be for them to form all the timbers upon the plane of the projection, because they could then at one view see how they would compare one with another, have tried several expedients to perform this, of which I might instance ten or twelve, but shall content myself with explaining three, which may be sufficient for those purposes, in order to which I shall first shew another method of forming the midship frame, different from those we have shewn before.

Plate III. Fig. 6. 1st. Draw the rifing deck and load-water lines, and set off the length of the floor timber as before.

2d. Take one fourth of the length of the floor timber, and set it off from O to d, upon which erect the perpendicular dc, and divide it into two equal parts in the point e.

3d. Describe an arch through the point a, the head of the floor timber, and the point e, taking for the radius the distance from the upper edge of the keel to the port-fells, or a little more or less, according to what round you propose to the floor head. This determines the rising of the floor timber, and with the radius O, half the length of the floor timber, describe the arch e Y, which determines the acutement of the floor timber.

4th. At the point l, the middle of the line AO, erect the perpendicular lm; and at the point n, the middle of the line Al, erect the perpendicular no; erect also the perpendicular pq at the middle of the line An; and another no, at the middle of the line An; and lastly, another

t u, at the middle of the line Ar.

5th. Take the distance ln, which set off on the line no from n to z; and on the line pg, from p to g; then taking the distance from a to g set that off from p to y; again take the distance py, which set off from r to b, and the distance ba from r to F; and lastly take the distance rF, which set off from t to E, and then the distance E a from t to x, a curve passing through the point a, z, y, F, x, T, will form the midship frame under water. We may then set off half the thickness of the post and stem on each side of the midshe line, and form the rest of the timbers; those for the fore body on the right, and for the after body to the left of the midshe line.

Plate II. If. To lay down the post upon the plane of projection, take the difference of the draught of water abase more than in midships, as marked on the plane of elevation (Fig. 2.) fet off this from F to d (Fig. 3.) and draw the line de parallel to AB; take also KF, the height from the plane of elevation, which set off from e to r, so shall the point r

be the head of the post.

2d, to lay down the wing transom, take its height from the plane of elevation, which set up on the plane of projection to f, and draw the line gf perpendicular to the middle line, so gf represents the upper side of the wing transom without regarding the round up or the round aft. Take also the height of the rising line upon the post from the plane of elevation.

which fet off from e to G.

3d. To form the fashion piece; take upon the plane of the projection n G the height of the load-water line, above the rising line upon the post, which set off from n to o upon the water line; take also GP, the distance betwirt the rising line and lower deck, which set off from p to q upon the deck line, and describe a circle through the points f, q, o. There is a problem in geometry to find the center of this arch. Note, the point q may be taken surther out or in, as you design a lank or full fashion piece.

Lastly,

Lastly, describe the arch o G; the radius of this arch may be the main half breadth; so shall f, q, o, G be the form of the sashion piece, which may be varied according to the sancy of the artist, by altering the centers.

Having thus formed the midship and after frames, we shall in the next place thew how to space the ribband lines, which are represented by the diagonals in the figure, but it will be proper to remark, that the ribbands are thin narrow planks which are made so, that they may easily be bent to the timbers. That which is nailed to the post at the height of the rising line, and to the midship frame, at the end of the rising of the floor timber, is called the floor ribband. That which answers to the wing transom and to the height of the lower deck, on the midship frame, is called the breadth ribband; all the rest betwixt these two are called intermediates.

From the Point H draw the line H G for the floor ribband, and from the point T draw the curve T, E, q, p for the breadth ribband, and draw the two intermediates betwixt them, so that by them the curve of the midthip frame and fashion piece may be divided into three equal parts.

Now, it is very plain, that if the ribbands had a proper form, and nail'd at the proper heights and politions, they would compose a kind of a model, by which the circular form of every timber might easily be discovered; but as we have only the extreme points of each given, we cannot from thence form such a curve as shall be necessary. We must therefore find a method to form some intermediate timbers betwixt the midship and after one, and thereby form the ribbands so that they shall make fair curves. There are some preliminary operations which are necessary towards performing this.

1st. To construct an equilateral Triangle for the Progression of the Frames in the Aster-Body.

Plate IV. Fig. 1. From the point M set off any distance to 1, upon any strait line, and from 1 to 2 treble that distance, from 2 to 3 five times that distance, from 3 to 4 seven times that distance, and proceed in that progression, increasing the spaces betwixt the figures by equal differences, viz. double the distance betwixt M and 1, till we have as many divisions less one as there are frames betwixt the midship and post, including that of the midship and post; and because there are nine frames the line must consist of ten divisions, from the point M to the point E. Let them be numbered 1, 2, 3, &c. make M E the base of an equilateral triangle S M E, and draw the lines S 1, S 2, &c. observing to produce them all till the distance betwixt the lines S E and S 9, upon a line parallel to the base, be at least equal to the distance betwixt the frames in the plane

of elevation. The line S M represents the midship frame, and the line S E, the post, and the nine intermediates, represent the nine frames be-

twixt the midship and post.

In order to give us a clear understanding of the use of this triangle, it will be necessary to remark, that the midship frame being that which incloseth the greatest space, and the aftermost that which incloseth the least, it will follow, that the intermediate frames will partake of the form of each; but mostly of that to which they are nearest; yet they will still retain a little of the form of each. Hence, when the intermediate frames are all formed, their curves will divide all the diagonals. drawn in the plane of projection, into as many parts as there are frames; and all the methods the builders have invented ferve only to divide them

into fuch a proportion as shall produce the fairest curves.

Now, if the proportion pitched upon for that purpose, be as 1, 3, 5, 7, 9, &c. then they must all be divided into the same proportions as the base of the triangle is divided into; and this may be performed very readily, only by taking the length of each diagonal from the plane of the projection, and applying it to the triangle in fuch a manner that it shall become the base of an equilateral triangle; as for instance, to divide the first intermediate diagonal; take the length of it in the plane of projection. (Plate II. Fig. 3) and fet it off from the point S to m and k on the fides of the triangle SM and SE; and draw the line mk, which being parallel to the base of the triangle, will be divided into the same proportion. In like manner all the rest of the diagonals may be divided; but as the builders are not agreed as to the precise form of a ship's bottom, some chuse to divide the base of the triangle into another proportion; others again in applying the diagonals to the triangle give them different inclinations to the line MS. It would be very proper to try feveral of these methods, by which means we might discover which would be most convenient; and after all the diagonals are divided into as many points as there are frames, curves passing through these points will determine the form of all the frames from the midship to the post. It only remains to shew how to end each frame upon the post. It was before observed that the keel is not parallel to the furface of the water, fo that it will be very eafy to conceive that the height of each frame taken from the upper fide of the keel, upon a perpendicular to the furface of the water, will always increase, the nearer the frame is to the stern post. Now g K is what the keel is deeper abaft than at the midship frame; and to find how much any frame abaft exceeds that of the midship, suppose the first; take the distance betwixt the line g G and K I at that frame, from the plane

of elevation, (Plate II.) which fet off from F towards d, (Fig. 3.) and at that point draw a line parallel to de, which will be the first frame upon the keel. In like manner we may draw lines parallel to de, for all the rest, as in the figure, which will determine their heights from the upper side of

the keel to the furface of the water.

It must be observed, that the diagonals in the plane of the projection. which end on the fashion piece, must likewise end on the fashion piece on the plane of elevation; we must therefore draw the fashion piece on the plane of elevation. Thus, take the distance of the point G, in the plane of the projection, from the upper fide of the keel, which fet off upon the stern post in the plane of elevation to the point b; through n, the rabbit of the wing transom, draw the strait line bn, which will represent the fashion piece on the plane of elevation. Now as only the lowest diagonal ends upon the post, in the plane of projection, which in the plane of elevation ends at b, fo the other diagonals that end upon the fashion piece, must likewise end on the fashion piece in the plane of elevation. Their height must therefore be transferred from the plane of the projection to that of the elevation; so the second diagonal will end at the point P. upon the fathion piece in the plane of elevation. In like manner all the rest may be transferred to the plane of elevation; and as the line that represents the fashion piece upon the plane of elevation rakes aft, this will occasion the line PS, which is perpendicular to the line that represents frame q, to exceed the line b.M. In the triangle, the line SM represents the midship frame and the line SE the post; that is, if the point where the ribband ends on the post, be equally distant from frame o, that frame o is from frame 8. Now as M b is longer than M L, we must draw the line S D without the triangle, which is to be used instead of the line S E. when we come to apply the diagonal HG to the triangle; for the point H must touch the line SM, and the point G the line SE. To find the point D, take M L from the plane of elevation, and apply it to the triangle, to that BC shall be equal to it; and parallel to ME; it must also be contained betwixt the line So and SE. Then take b M and set off from B, which will give the point D. In like manner the line SF must be used when we divide the diagonal MK; and to find the point F fet off PS in the plane of elevation, from B to F in the triangle; and draw the line SF. In the fame manner there must be lines drawn for every Plate IV. Fig. 1.1 diagonal without the line SE; fo the line SE is not used in dividing the diagonals. Let it be further observed, that in applying each diagonal to the triangle, it must not only be contained betwixt the line SM and the line corresponding to the diagonal, which is to be divided, but it must likewise form a certain angle with the line MS,

that

that is, with that part of it which is intercepted betwixt the diagonal and the point S. These which appear to me to be properest for that purpose are as follows: The first diagonal to make an angle of 60 degrees; the second 62;, the third 68, the fourth 86, the fisth 65, the sixth 60 degrees; but the artists vary these angles according to the form they design to give to the timbers; nay, some draw them always parallel to the base

of the triangle.

Our author then proceeds to the forebody, and forms a triangle, the base of which he divides in the same manner as that already described, by which he divides each diagonal. He likewise show to space the diagonals upon the step is ut as the artists leave us so much undetermined as to the angles that each diagonal is to make with the line SM, when they are applied to the triangle, it will be very difficult to apply this method to practice. So we presume it will be needless to say any more on that head, judging what has been already said sufficient to give our readers an idea of the principles on which the method is grounded; we skall proceed therefore to the next method he proposes.

To form the Timbers by a Quarter of a Circle, Plate IV. Fig. 2. 3.

1st. Form the midship frame, the fashion piece, the foremost timber, also the two balance frames, by some of the preceding methods. Note, Those who make use of the following method of forming the rest of the timbers are supposed to be previously acquainted with the manner of forming the midship frame, &c.

2d. Space all the diagonals for the ribbands as directed in the pre-

ceding method.

3d. From the center A with any radius describe a quarter of a circle, and divide it into so many equal parts, that there may be a point for each timber to be formed, and draw the radii A 1, A 2, &c. to A 9, so we shall have one for each frame.

4th. Take ab the first diagonal, which set off from the point A

upon the line A C, to 1.

5th, Take ac, the distance upon the lower ribband, betwixt the post and balance frame, which in the plane of projection is the 6th frame, set off this distance upon a perpendicular erected upon the line AB, to intersect the radius A 6, in such a manner that the perpendicular G I shall

be equal to ac.

6th. Produce the line C A to F, and upon this line find a point, which shall be the center of a circle whose circumference shall pass through the point 1, before marked upon the line A C, and the point 1, now marked upon the radius A 6; describe the arch through these two points to the point 1 on the line A B.

7th,

7th. Let fall perpendiculars to the line A B from the points where the arch 1, 1, 1 interfects the feveral radii. Transfer these perpendiculars to the line a b, which will divide the lower diagonal into the points through which the curves of the frames must pass. Note, the perpendiculars are

not drawn to avoid contusion.

After the same manner all the other diagonals are graduated, first by taking the whole length of each diagonal, and setting them up on the line A C, from the point A to the points 5, 4, 3, 1, 2, and secondly, by taking the several distances upon each diagonal intercepted betwixt the after frame and the balance frame, and applying them severally to the radius A6, in such a manner that they shall be contained betwixt the radius A6 and the line AB, upon the perpendiculars let sall from the points 5, 4, 3, 1, 2. And thirdly by describing arches through the points in the line A C, to pass through the points of the same number upon the radius A6, whose centers are in the line AF; the arches to be produced to intersect the line AB in the points 5, 4, 3, 1, 2, will intersect all the radii; the perpendiculars let sall from the intersections of the radii with the arch corresponding to each diagonal, will divide that diagonal into the points through which the curves of the frames must pass.

The diagonals for forming the frames in the fore body are divided into the points through which the curves must pass by the same operations, only observing that frame 4 is the balance frame for the fore body.

CHAP. V.

Of the Projections on the horizontal Planes, and of the Water and Ribband Lines on the Plane of Elevation, and that of the Trojection.

ATER Lines are described upon a ship's bottom by the surface of the water into which she swims; that which determines how much is under water when she is loaded is called the load-water line. Now it is plain, that it a ship is lightened, she will sufe higher out of the water; and if she be lightened so as to rise equally afore and abast, the surface of the water will then form another water-line parallel to the loadwater line. Again, if the ship is lightened more she will still rise higher, and if the same difference still continues betwixt the draught of water abast and afore, we shall have another water line parallel to the two sormer;

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so that by this means we may describe as many water lines as we please,

all parallel to one another.

In order to form an idea how these lines are represented on the different planes, let us suppose a ship upon the stocks upon a level ground, and her keel in the same position, with respect to the horizon, that it is to be in the water when loaded; we may then describe several black lines upon the ship's bottom, which may be whitened for that purpose, all parallel to the horizon: These will all be water lines.

Now, if a spectator be removed at any considerable distance from the ship upon a line in the same direction with the keel, all these black lines which were drawn upon the ship's bottom, parallel to the horizon, and which are actually curves, will appear to him all strait lines, because he sees them all upon a plane formed by a section passing through the mid-ship frame perpendicular to the keel. Hence the water lines will be re-

presented by strait lines upon the plane of the projection.

Again, if a spectator is removed at any considerable distance from the ship upon a line perpendicular to the keel, so as to see the whole length of the ship at one view, the water lines will then appear to him strait lines, because he sees them upon a plane erected perpendicular to the horizon upon the middle line of the keel. Hence the water lines will be repre-

fented by strait lines upon the plane of elevation.

But if the spectator be supposed to be placed underneath the middle of the ship at any considerable depth, in a line perpendicular to the level ground, he will then, viewing the ship's bottom upwards, discover the curvings of all the water lines. These curves are all projected upon a plane, which we must imagine to be formed by a section of the ship through the load-water line, and we are now to shew how these are formed:

To form the Water Lines upon the Horizontal Plane.

Let the water lines to be formed be represented in the plane of the projection by strait lines all parallel to one another. These will be represented by the strait lines in the plane of elevation. Suppose qr, st bx, and TV, all parallel to one another, and the same distance from the load-water line TV that the lines which represent them in the plane of the projection are from it. In order to form these upon the horizontal plane,

rst, Take half the thickness of the post from the plane of the projection, and lay it off on the horizontal plane from A to E, and through the point E draw the line Es parallel to AB, five or fix feet long; lay off the fame distance from B to F, and thro' the point F draw a line F R parallel to AB, five or fix feet long.

2d. From the points where the water lines interfect the stern post upon the plane of elevation, let fall perpendiculars. In like manner let fall perpendiculars from the points where the water lines interfect the stern.

3d. Take upon the water lines, in the plane of the projection, the feveral distances intercepted betwixt the middle line and the curve of the midship frame, and lay them off from the line A B in the horizontal plane. upon the perpendicular that represents the midship frame. Take also from the plane of projection the feveral distances intercepted betwixt the middle line and the curvings of the other frames, and lay them off in the horizontal plane from the line AB upon the perpendiculars corresponding to their respective frames, both in the fore body and after body, and curves palling through all these points will give the true form of all the water lines. They end forward at the points where the perpendiculars interfect the line F R. The water lines abast which end upon the post in the plane of elevation, will end where the perpendiculars interiect the line Es upon the horizontal plane. But the 3d and 4th water lines cannot end upon the post, by reason of the fashion pieces; and in order to find the points where these shall end, we must proceed in the following manner.

To find the point where the load-water line ends, let fall a perpendicular from the point k, where it interfects the fashion piece on the plane of elevation, to N. Take from the plane of the projection upon the line that represents the load-water lines, the distance betwixt the fashion piece and the mid-line; lay this off upon the horizontal plane from the line A B to the point N, which will end the load-water line upon the horizontal plane, from whence it may be drawn to g; so g N will be the flat of the Tuck; and to find the point g draw a line parallel to k N thro' the point where the line T V cuts the rabbit of the post, which will give the point g. We may after the same manner find the ends of the other water lines that do not go the stern post for a square tuck.

To form the Ribbands upon the Horizontal Plane.

We observed before, that the ribbands were thin planks nailed to all the frames from the post to the stem; and that when they are carried round, so as to make fair curves, the form of all the filling timbers may be by them determined. These filling timbers are to be placed betwixt

the frames, which were methodically laid down in the draught. We shall here further observe, that these ribbands will round two ways, one in a vertical, and one in an horizontal fente, occasioned by the nature of the form of the ship's body; for they will, in carrying them about, naturally fly higher abaft and before than they are in midships, which gives them a vertical curve, and the narrowing of the ship's breadth from the midships both ways gives them the horizontal curve; thence they will be reprefented by different lines on all the planes.

They are represented upon the plane of the projection by streight lines, all but the breadth ribband, which is usually represented by a curve; but upon the plane of elevation, and that of the horizon they will be reprefented by curves. The reason of these different appearances, arises from the different situations in which they are supposed to be viewed, as was

observed in respect of the water lines.

Now in order to comprehend the relation betwixt these horizontal curves, and the lines that represent them upon the plane of the projection, it will be fufficient to remark, that these horizontal curves result from the different lengths of the perpendiculars that are supposed to be drawn in the plane of the projection, from the points where the lines that represent the ribbands interfect the frames, to the middle line. Hence, if the lengths of these perpendiculars are transferred to the lines corresponding to each frame in the horizontal plane, we shall have the points thro' which the curve that forms the ribband must pass.

But if these ribbands are to be represented upon a plane placed in an oblique polition to the horizon, that is to fay, a plane that has the fame inclination to another plane erected perpendicularly upon the middle line of the keel, that the line that represents that ribband, has to the middle line in the plane of the projection; in that case, they will have a quite different form from what they have upon the plane of the horizon.

Now, to conceive the relation betwixt these and the lines that represent them upon the plane of the projection, it will be sufficient to remark, that if the teveral distances taken upon each diagonal intercepted betwixt the middle line and the points where these diagonals intersect the curves of the timbers in the plane of the projection; I fay, if these be transferred to the lines that represent those timbers, we shall have the points thro' which the curves that form the ribbands must pass.

Again, if these ribbands are to be represented upon the plane of elevation, they will have a different form from any of the former; to find which we need only take the perpendicular diffances from the points where the diagonals interfect the curves of the timbers in the plane

of the projection to the line that represents the upper side of the keel, and transfer them to the plane of elevation, setting them up from the upper side of the keel upon the line corresponding to the timber, from which they were taken upon the plane of the projection. This will give us the points thro' which their curves must pass.

Having thus given a general description of these curves, we shall

now proceed to describe them upon the different planes.

To describe the Floor Ribband upon the Plane of Elevation.

1st. Take the perpendicular distance betwixt the point a, where the diagonal interfects frame 9, and the lower water line in the plane of the projection.

2d. Set up this diffance from the point S, where the lower water line interlects frame 9 in the plane of elevation, and we shall have a point G.

thro' which the curve must pass.

Now, it is plain, that we may, by repeating the fame operations, have a point in each frame, thro' which the curve of the ribband must pass upon the plane of elevation. After the same manner are all the other ribbands formed.

To describe Ribbands upon the Horizontal Plane.

The breadth ribband is formed by transferring the lengths of all the perpendiculars that are supposed to be drawn from the points where the curve that represents this ribband intersects the timbers, to the middle line in the plane of the projection: This curve, in the plane of the projection, is drawn from the breadth in midships to the extremity of the wing transom.

1st. Lay off the length of the wing transon upon the perpendicular "L.

ad. Take the length of the perpendicular drawn, from the point where the curve that represents the breadth interfects frame 9, to the mid-line in the plane of the projection; lay off this from the line A B upon the perpendicular representing frame 9 in the horizontal plane, to the point S, which will be one of the points thro' which the curve of the ribband must pass. We may proceed in the same manner to find points upon all the perpendiculars, both afore and abast, so shall the curve L, S, Q, t, be the form of the breadth ribband. But to compleat this ribband, the round ast of the wing transom must be set off.

To form the Oblique or Gant Ribbands.

We observed before, that these ribbands could not be formed either upon the horizontal plane or that of elevation, upon which account they were seldom drawn, because each must be drawn upon a separate plane. However, those who incline to draw them may use the following method:

Let it then be required to form the first ribband represented in the

plane of the projection, by the diagonal H G.

1st. Produce line HG to the point p in the middle line upon the

plane of the projection.

2d. Take the height of the point p above the line that represents the upper side of the keel in midships, in the plane of the projection; set up this from the same line in the plane of elevation, on a perpendicular, upon the post, from which point let sall a perpendicular to the point F in the line CD, and produce all the perpendiculars that represent the frames to the line CD; so F, Q will be the axis of the ribband from the post to the midships.

3d. Take upon the plane of the projection in the line HP, the distance

pG, which fet off upon the perpendicular from the point F to f.

4th. Take the distance on the diagonal from the point p in the middle line to its intersection with the frame 9. Set off this from the line CD upon the perpendicular corresponding to frame 9; this will give us a point thro' which the curve must pass. Do the same for all the other

frames to the midship.

In like manner the curve for the fore part of the ribband is formed from the interfections of the diagonal 4, 5, with the curves of the frames in the plane of the projection; but it is evident, this is a different plane from that of the line Hp; therefore we must have a different axis for the curve of the fore part of the ribband. In order to which, take from the plane of the projection the diagonal 4, 5; fet off this from the point O to Z, and draw the line Z X parallel to C D. We must likewise take the height of the point 4 in the plane of the projection, and set it up on the stem; from which point letting fall a perpendicular to the line Z X, we shall limit the fore end of the ribband. The points thro' which the curve must pass will be found in the same manner as those for the after-body.

The builders make use of the cant ribbands to find the bevellings of the timbers; For we must represent each frame as one intire piece of circular timber, and being all fastened to the keel they form the side of the ship. They are square upon the upper side of the keel; but because

both

both the outfide and infide of the ship's sides, length-ways, form curves, it is plain, that the fections of any of the frames, the midship only excepted, will produce a furface in the form of a lozenge or rhombus; the angles which are formed by these sections are what are called the bevellings of the timbers.

The ship-wrights take these angles mechanically by an instrument call'd a bevel; thus they draw, upon the plane of the ribband, a line parallel to that which represents the frame, and distant from it the whole breadth of the timber; and applying the flock of the bevel to the line that represents the frame, and the tongue to the ribband, they have the quantity of the angle which forms the bevelling of the timber at that place.

It is plain the angle b, a, c, which points to the midship frame, will be obtule, whereas the angle b, a, d, which points to the post, will be acute.

Now, as every timber has two planes, that which points to the midships will have what they call a standing bevelling, and that which points either to the post or stem will be under bevelling.

We shall shew in another place how the modern builders, by putting the frames in an oblique position to the keel afore and abaft, lessen the bevellings.

CHAP. VI.

Another Method of laying down the Horizontal Plane, and the Plane of Projection.

HOSE who are well versed in the art of drawing have taken a method quite different from any of those we have described, which shall be the subject of this chapter.

After forming the plane of elevation, and drawing all the perpendiculars for the frames, as before, the following method must be observed:

To lay down the Breadth Ribband on the Horizontal Plane.

The extremities of it on the stem and post, and the point thro' which it is to pass on the midship frame are found as directed in the preceeding chapter. It remains now to find the points in the balance frames, thro' which it is to pass.

To find the point in the fore balance frame take 112 parts of half the main 40 Of the Formation of Water Lines and Ribbands. CHAP. VI. main beadth, which fet off on the line that represents that frame in the horizontal plane from K to L.

To find the point in the balance frame abaft, take 1504 parts of the half of the main breadth from M to N. It will be necessary to have another point in the fore-body, thro' which the curve must pass; for which pur-

pose use the following method:

Divide the space contained betwixt the line that represents the balance frame afore and the rabbit of the stem, into two equal parts, and draw the line OP, on which set off the 160th part of the main breadth, which will give the point P, thro' which the curve is to pass. It must be observed, that the proportions for finding these points may be varied according to the form we propose to give to the ribband. After the points H, N, Q, L, P, I are thus set off, we may describe the curve either by moulds or penning battens.

II.

To lay down the Floor Ribband on the Horizontal Plane.

1st. The height of this ribband must be determined both upon the post and stem, from which points letting fall perpendiculars, we shall have the extremities of it on the horizontal plane, observing to allow for the rabbit.

2d. Take half the length of the midship floor timber, and set off on the line that represents the midship frame on the horizontal plane from a

to S, which will be the point thro' which the curve must pais.

3d. Take $\frac{1}{2}\frac{4}{3}$ of the line a s, the breadth at the midship frame, and set it off on the balance timber afore, from K to T, and set off $\frac{1}{2}\frac{4}{3}\frac{6}{9}$ of the same line, upon the balance timber abast to V, and draw the curve thro' the points G, V, S, T, R.

III.

To lay down the after Balance Timber upon the Plane of Projection.

1st. Produce the line which represents it on the horizontal plane to the sheer rail, on the plane of elevation, and take the distance upon this line betwixt the upper side of the keel, and the lower edge of the second wale, which here represents the breadth ribband; set up this from A to C on the plane of the projection, from which point draw the line C D, perpendicular to the middle line. (Plate II. Fig. 1, 2, 3.)

2d. Take the line M N in the horizontal plane, and fet off from D to E, which will give one point, through which the curve of the timber

must pass.

3d. Take

3d, Take the height of the floor ribband, in the plane of clevation, and fet it up on the plane of the projection to G; from the point H, at the end of the floor timber, draw the line H G which will represent the floor ribband on the plane of the projection. (Plate II, fig. 1, 2, 3.)

4th, Take the distance M V, in the horizontal plane, with a pair of compasses, and move the compasses with one foot, in the middle line, and the other in a line perpendicular to it, till it intersect the diagonal in the point L, thro' which the curve of the frame must pass. To those who are acquainted with drawing, the three points E, L, F, will be sufficient to form the timber; they who incline to have another point may divide the line A C into two equal parts by a perpendicular M K drawn to the middle line, from which setting off "the of the line M K we shall have another point thro' which the curve must pass.

IV.

To lay down the ninth Frame abaft on the Plane of the Projection.

Take the height of the breadth ribband at this frame, in the plane of elevation, and fet it up on the plane of the projection from F to O, and draw the line OP perpendicular to the middle line. (Plate II. fig. 1.2.3.)

2d, Take the distance X S in the horizontal plane, and set off from O

to P, which will be the point thro' which the curve must pass.

3d, Take the distance X Z in the horizontal plane, which set off from the middle line, to intersect the diagonal that represents the floor ribband, in the plane of projection in Q, observing to keep the compasses as before directed.

4th, Divide the line KO in two equal parts, and draw the line RS perpendicular to the middle line, on which fet off 100 of the line PO, from R to S, and draw the curve thro' the points P, S, Q, F, which will be the form of the ninth frame.

v

To lay down the intermediate Ribbands abaft on the Plane of the Projection.

1st, Take the distance betwixt the upper side of the keel and the breadth, upon the line that represents the midship frame, in the plane of elevation, and set it up from A to T, and from B to T, in the plane of the projection, so shall the line T T give the height of the breadth ribband in midships.

2d, Divide the curve H M T into as many equal parts as there are to be intermediate ribbands; divide also the curve of the ninth frame QSP into the same number, and, thro' these divisions, draw the diagonals

which will represent the ribbands as in the plate,

C

To lay down the first intermediate Ribband upon the Horizontal Plane.

1st, Take the nearest distance of the point V (which is the extremity of the diagonal in the plane of the projection) to the middle line OF, set off this on the line which represents the midship frame in the horizontal plane, which will give the point thro' which the curve must pass at that place. After the same manner we may find the points in the lines that represent the balance and ninth frames in the horizontal plane.

2d, Take FZ, the height of the ribband upon the rabbit of the post, in the plane of the projection, and set it up on a perpendicular, from N to the point k on the line that represents the rabbit of the post in the plane of elevation; take the nearest distance of the point k to the perpendicular of the post, which set off from E to e, and this will be the end of the ribband; so a curve passing thro the points e, d, c, b, will be the form of the ribband.

VII.

To lay down the Wing Transom upon the Plane of the Projection, and on the Horizontal Plane.

1st, Take the height of the upper fide of the wing transom (including the round up) in the plane of elevation, and set it up in the plane of the

projection to the point e.

2d, Take the height in the plane of elevation, without regarding the round up, and fet off from F to f; and draw the line f g perpendicular to the middle line, on which fet off the length of the transom from f to g, this is equal to the line G H in the horizontal plane. The curve g e represents the upper side of the wing transom.

The round aft of the transom is represented upon the horizontal plane

by the curve L ke; HL is the square end of it.

VIII.

To lay down all the Frames in the after Body.

All these are laid down in the same manner as the ninth and balance frames before described, that is, by taking the half breadth of the ribbands at each frame in the horizontal plane, and setting them off from the middle line in the plane of the projection to intersect the diagonal corresponding to the ribband, as directed in forming the balance frame, by this means we shall divide each into as many points as there are frames: the curves drawn thro' these points will give the form of all the frames in the after body.

IX. To

IX.

To lay down the Position of the Fashion Piece on the Horizontal Plane.

Let fall the perpendicular GH, from the end of the wing transom, and draw the line H l, which will represent the plane of the sashion piece upon the horizontal plane, observing to make the angle GH l, about 25 degrees.

. X.

To form the Fashion Piece in the same Manner it is to be, when put into its proper place in the Ship.

The fashion piece laid down in the plane of the projection, regards that frame as it would appear when viewed from abast; but as the fashion pieces on each side are not in one plane, as all the rest of the frames are, we shall be much deceived, if we imagine that the fashion piece laid down in the plain of projection, will give the true form of that which is to be put in the ship. We must therefore lay it down upon another plane, and, to avoid consusting, we shall separate it from the plane of projection.

Note, The fashion piece, mention'd by our author, described in the plane of the projection, is that betwist the ninth frame, and the curve fq o G, which represents the fashion piece of a square tuck; it is formed in the same manner as the rest of the frames, by transferring the lines n m, p o, &c. in the borizontal plane, to the plane of projection, to intersect the diagonals coresponding to these ribbands in the points i, l, &c:

1st, Draw the line f G, to represent the middle line of the plane of

projection. (Fig. 4.)

2d, Draw the line fg perpendicular to Gf, to represent the wing transom.

3d, From l, the point where the fashion piece interfects the floor ribband in the plane of the projection, take the nearest distance to the line fg, which represents the wing transom, and set off this distance in Fig. 4. from f to b, and draw the line $b \, l$ parallel to fg.

4th, From the point l, where the fashion piece intersects the first intermediate diagonal, in the plane of projection take the nearest distance to the line fg, set it off from f to k, in Fig. 4, and draw the line km, paral-

lel to fg.

5th, In like manner, the points where the fashion piece intersects the second and third diagonals in the plane of projection, are to be transferr'd to the points q and n, Fig. 4. and the lines p q, n o drawn parallel to f g.

6th, To find the points through which the curve must pass: Take the line l H, which represents the position of the fashion piece upon the horizontal plane; lay this off from f to g: Again, take the distance ly in the horizontal plane, which lay off from q to p, in like manner set off the distance lx, from n to o; and the distance lp from k to m, and lastly, the distance ln, from b to l; so a curve drawn through the points g, p, o, m, l, will give the true form of the fashion piece.

.XI.

To lay down the Fashion Piece upon the Plane of Elevation.

1st, Take the several heights above the keel, of the points where the fashion piece intersects the diagonals in the plane of projection, and transferr them to the lines s, p, q z, y, in the plane of elevation, drawn parallel to the keel, and the same height above it, that their coresponding points are in the plane of projection.

2d, Take the nearest distance of the point n, in the plane of elevation, to the line CF, the perpendicular from the head of the post, set off this from the same line in the plane of elevation upon the line p; which will

be the point through which the curve must past.

3d, In like manner the points z, y, must be transferr'd from the horizontal plane, to the plane of elevation in the points z, x, a curve passing through these points will be the projection of the fashion piece

on the plane of elevation.

We shall hear remark, that some builders to avoid giving a great bevelling to the timbers, and likewise that they may not require such compass timber, do change the direction of all the frames in the fore-body before that of the loof; that is, the lines that represent them in the horizontal plane make an acute angle with the line that represents the keel; these are called cant timbers, and may be formed in the same manner as the sashion piece, which we have now described. Tho' several builders form all the frames perpendicular to the keel, to have the floor timbers in one piece, which will be much stronger than when in two pieces, and this will inevitably be the case when the timbers are canted.

We might here shew how to lay down the top timbers, but as that part under water is the most material, we shall proceed to form the timbers

afore.

XII.

To lay down the Frames for the Fore-body.

The balance and the eighth frame must first be formed in the same manner as the balance and ninth frame abast: In order to which the curve that

that represents the breadth ribband must be laid down in the plane of the projection afore. The diagonal, which represents the sloor ribband must likewise be laid down in the plane of the projection, for which purpose we must take the height of the ribband above the keel upon the rabbit of the stem, and set it upon the line that represents the rabbit of the post in the plane of the projection, to the point 4; from which draw a line to the floor head, so 4 5 will represent the floor ribband.

XII.

To space the Diagonals that represent the Ribbands afore, in the Plane of the Projection.

1st. As the points of their intersection at the midship frame are the same afore that they are abast, we need only transfer them from abast to the fore body.

2d. Take the height of the breadth ribband upon the stem in the plane of elevation, and set it up from F to 17 in the plane of projection.

3d. Divide the distance betwixt 4 and 17 into four equal parts, which will give the points in the plane of projection, where the intermediate dia-

gonals end on the stem.

After the diagonals are drawn in the plane of the projection, the ribbands may be laid down in the horizontal plane, and from thence all the other frames may be laid down in the plane of projection, in the very fame manner that the horizontal ribbands and the frames for the afterbody were laid down.

CHAP.

General Remarks on Ship Building.

A LL the rules we have hitherto laid down, collected from the principal dimensions of ships built by the most eminent masters, should only be so far regarded as they may affift the artist in forming the body in such a manner as to produce effects answerable to the service for which the vessel is designed.

In order to qualify a builder for fuch an undertaking, it is necessary he should understand the nature of sluids, and of such bodies as will float in the water; when he has made himself acquainted with these, I

would recommend him to Mr Bouguer's treatife on ship-building.

The principal Qualities belonging to Ships.

1st. To be able to carry a good fail, not only because in forming the body, the water lines are all supposed to be described when a ship is upright in the water, but likewise for doubling a cape, or getting off a lee shore, which will be impossible to be done when a ship lies over in the water, this will likewise render her lower tier, if not all her guns useless.

2d. A ship should steer well, and feel the least motion of the helm.

3d. A ship should carry her lower tier of guns four feet and a half, or five feet out of the water, otherwise a great ship that cannot open her ports upon a wind, but in smooth water, may be taken by a small one, that can make use of her guns, or she must bare away before the wind, to have the use of her guns; on which account it will be proper to raise the ports higher before than in midships, because the fore part of the ship is often pressed into the water by carrying sail.

4th. A ship should be duly possed, so as not to dive or pitch hard, but go smooth and easy through the water, rising to the sea when it runs high, and the ship under her courses, or lying to under a mainfail, other-

wife the will be in danger of carrying away her mafts.

5th. A ship should fail well before the wind, large, but chiefly close

hawled, keep a good wind, not fall off to the leeward.

Now the great difficulty confifts in uniting fo many different qualities in one ship, which seems indeed to be impossible; the whole art therefore confists in forming the body in such a manner, that none of these qualities shall be entirely destroyed, and in giving the preference to that which is most required in the particular service for which the vessel is built; in order to

which

which it will be necessary to know, at least nearly, what form will give a vessel noe of these qualities, considered abstractly from the rest.

To make a Ship carry a good Sail.

A flat floor timber, and fomewhat long, or the lower futtock pretty round, a streight upper futtock, the top timber to throw the breadth out aloft; at any rate to carry her main breadth as high as the lower deck; now, if the rigging be well adapted to such a body, and the upper works lightened as much as possible so that they all concurr to lower the center of gravity, there will be no room to doubt of her carrying a good sail.

To make a Ship Steer well, and quickly Answer the Helm.

If the fashion pieces be well formed, and the tuck carried pretty high; the midship frame carried pretty forward; a considerable difference of the draught of water abast more than afore, a great rake forward and none abast, a snug quarer deck and forecastle, all these will make a ship steer well; but to make her seel the least motion of her helm, it will be neessary to regard her masts. There is one thing not to be forgot, that a ship which goes well will certainly steer well.

To make a Ship carry ber Guns well out of the Water.

It is plain that a long floor timber, and not of a great rifing, a very full midthip frame, and low tuck with light upper works will make a ship carry her guns high.

To make a Ship go smoothly through the Water without pitching hard.

A long keel, a long floor not to rife to high afore and abaft, the area or fpace contained in the fore body, duly proportioned to that of the after body, according to the respective weights they are to carry; all these are necessary to make a ship go smoothly through the water.

To make a Ship keep a good Wind.

A good length by the keel, not too broad, but pretty deep in the hold, which will occasion her to have a short floor timber, and great rising.

As fuch a ship will meet with great refissance in the water going over the broad side, and little when going a head, she will not fall much to the leeward.

Now some builders imagine that it is not possible to make a ship carry her guns well; carry a good sail; and to be a prime sailer, because it

woul:

would require a very full bottom to gain the first two qualities, whereas a sharp ship will best answer for the latter; but when it is considered that a sull ship will carry a great deal more sail than a sharp one, a good artist may so form the body as to have all these three good qualities, and likewise steer well, for which purpose I would recommend somewhat in length more than has been formerly practised.

After what has been faid upon this head, I believe it will not be thought impossible to unite all these different qualities in one ship, so that all of them may be discerned in some degree of eminence, but when it happens otherwise, the sault must be owing to the builder, who has not applyed

himself to study the fundamental rules and principles of his art.

Excepting fome antient builders, who were happily born with a natural genius, and our moderns, who being inftructed in the principles of the mathematics, have truly laboured very hard to make a progrefs in the art of fhipbuilding, one may, without violating the truth, affirm that the greatest part satisfy themselves with copying such ships as they efterm good sailors, and it is these service mechanick methods, which to the great reproach of the art, are but too common, that have produced all these pretended rules of proportion, all these methods of describing the mid-ship frame, and forming the rest of the timbers, which every builder endeavours if possible to conceal and keep wholly in his own family.

How low and mean is this? it is as if a great architect should endeavour to conceal the proportions of the different orders of architecture, whereas they are published every where, and so well known that many can raise a very beautifull porch or triumphal arch; but tho' the methods of describing the midship frame and forming the rest of the timbers be known to most apprentices, yet we have but sew good master builders: This requires more than those mechanick rules, they should at least have such a knowledge of the mathematics, physicks, mechanicks, of the nature of solids and sluids, as to be able to discover what sigure would procure some good quality without hazarding or putting a bad one in its place,

Let us suppose one to have a collection of draughts of a vast number of ships, and whose good and bad qualities have been remarked with all possible exactness, such a valuable treasure would be of great service to a person who could calculate precisely by the draughts where the sault lay, and how it might be rectified. For instance, suppose a ship sails well, but carries her guns too low, a builder who is not acquainted with these principles would raise her deck, in consequence of which she would not sail well; whereas one that could exactly calculate how much the resistance of the sluid is diminished upon the prow, would take great care

to add no more to any of the other parts than he could find by an exact calculation might be done without augmenting the refiftance in the fluids.

M. Bouguer has published several useful problems for making these calculations, to which we refer the reader, and only explain what regards the height of the gun deck, and the resistance of the fluid, in one example of a 70 gun ship.

C H A P. VIII.

To know by the Draught how high a Ship will carry her Guns out of the Water.

THIS is only to know if, when a ship is loaded with all her ammunitions and provisions on board, and ready to fail, her seat in the water will then agree exactly with the load water line in the draught.

It may be demonstrated by several experiments, that any floating body of whatsoever figure will just fink so far in the water as to displace a

bulk of water of equal weight with itself.

Hence it will be necessary, first to find a method of calculating the exact weight of a ship ready equipt for sea, and, secondly, to know the exact weight of the water the ship displaces, when loaded to the water line in the draught.

In order to the first, the exact weight of all the timber, iron, lead, masts, fails, rigging, and in short of all the materials, men, provisions,

and every thing else on board the ship must be known.

It must be confessed that this is a very laborious task, yet the zeal of our modern builders has surmounted all these difficulties, and got the exact weight of a ship of each class with all its surniture, and six months provisions on board. It will be sufficient for our purpose to give the particulars, of the two followings, one of 30 and another of 50 guns, both ready equipt for sea, with six months provisions on board.

An Estimate of the Weight of the RENOMEE Frigate of Thirty Guns, with Six Months Provisions.

WFIGHT of the HULL.

	Cubic	Under	Above	T	Total	
	feeet	water	water		Cuns.	
01 4 6 1 . 7 6		Pounds.	Pounds.	Tons	Pounds	
Oak tim- under w. at 72 lb. per f. above w. at 66 lb.	5640	406080		299	800	
ber above w. at 66 lb.	2920		192720	-99	000	
Fir at 50 lb. per foot above water	600	30000	01	20	000	
	560	10 1	28000	29	000	
Carved work ——			2200	I	200	
Iron knees and standards		4200	7010	- 5	1210	
Bolts, rudder irons, chain plates, nails		11650	6558	9	208	
Lead for the hause holes & scuppers	-	250	430	ó	680	
Locks —			170	0	170	
Oakum -		1200	1830	I	1030	
Pitch and Tar			650	0	650	
Paint			440	0	440	
In the Cook room	-	1	8000	4.	000	
Total		453380	248008	350	1388	

WEIGHT of the FURNITURE.

	Pounds.	Pounds.	Tons	Pds
Masts compleat set and spare	3000	37000	20	00
Blocks —	1000	5444	2	444
Pumps — —	1734	670	I	404
Cables and Hawfers	24444		· I 2	444
Sails and their Cases	4222	377.8	4	000
Anchors and their Stocks	2611	6944	4	1555
Cordage for the rigging		17282	8	1282
The master's Stores	3333	117	1	1333
Boats	1	6666	3	666
	40344	75784	58	128

WEIGHT of the Provisions, &c.

	Under	Above		otal -
	water	water		Γuns.
Described for Consult Consult	Pounds.	Pounds.	Tons	Pounds
Provisions for 6 months for 200 men with all their equipage	245420		122	1420
Water for two months and a half	100000		50	000
Cafks ———	32800		16	800
The Captain's table	15000	5000	10	000
Total	393220	5000	199	220

WEIGHT of the OFFICERS STORES.

The Carpenter's Stores
The Caulker's Stores
The Surgeon's Effects
The Pilot's I ffects
The Chaplain's Effects

Under	Above	Total
water	water	in Tons
Pounds.	· Pounds.	Tons Pds
3000	-1000	2 00
1000 -	_	0 1000
2400		1 400
740	_ 360	0 1100
	100	0 100
7140	1460	4 600

WEIGHT of the Guns and Ammunition.

Iron Guns ——
Carriages fitted
Balls round and crofs bar
Balls of one pound ——
Powder and Powder Barrels
Implements for the powder
Crows, Handspikes, Gunners Uten-
fils, and Stores
Musquets, Cutlasses, and Pole Axes

Under	Above	Total			
water	water	in 7	Fons		
Pounds.	Punds.	Tons	Pds		
	60300	30	300		
	14000	7	00		
11570	2430	7	00		
600	- 11	0	600		
7108	112	3	1220		
1368	132	0	1500		
3200	1500	2	700		
	900	0	900		
23846	79374	51	1220		

WEIGHT of the MEN and their EQUIPAGE.

8 principal Officers and their Effect 200 Men and their Effects To		Above water Pounds. 4000	in '	Tons. Pounds 00 00
BALLAST	200000	74000	100	00

RECAPITULATION.

and the last of th	Under	Above		
A STATE OF THE STA	water	water		ons.
The Huil	Pounds.	Pounds.		Pounda
	453380	248008	350	1388
The Furniture	40344	75784	58	128
The Provisions	393220	5000	199	220
Officers Stores	7140	1460	12	600
Guns and Ammunition	23846	79374	51	1220
Weight of the Men		44000	22	00
Ballaft —	200000	2.0	100	00
Total	1117930	453626	785	1556

An Estimate of the Weight of a Frigate of Fifty Guns, with Six Months
Provisions.

The state of the s	Under	Above	To	tal
Deport - may be a first	water	water	I ni	ons.
man half and delivered to the	Pounds.	Pounds.	Tons	Pounds
The Hull	774270	769134	771	1404
The Furniture	98237	163184	130	1421
Ballast	300000		150	0.00
Guns and Ammunition	67960	199320	133	1280
Provisions	659400	8000	383	1400
Stores	9800	2800	6	600
Men and their Equipage		77000	38	1000
matter than the state of the state of	1909667	1219438	1564	1105

But as all ships of the same class are pretty near the same dimensions, and have the same number of guns, &c. we may have the exact weight of each only by examining the draught of water, and computing the weight

of that column of water which is displaced by the ship.

and the state of t

Now if the *Intrepide* weighs 2718 tuns, the must fink fo far into the water till the has displaced a column of water containing 73459 ½ cubick feet, for a cubiek foot of salt water being supposed to weigh 74 lb. the 73459 ½ will weigh 5436000 lb. or 2718 tuns, or if the displaces 73459 ½ cubick feet of salt water, we may thence conclude that the weighs 2718 tuns.

In like manner, if the weight of the ship which is to be laid down in

the draught be known; as, for instance, that of a ship of 78 guns, is 2350 tuns, we may with certainty know if the water line in the draught be properly placed, only by reducing the bottom into cubick feet.

The antient builders were unacquainted with the manner of performing this, but our moderns make an exact calculation of the contents of the bottom before they begin to build, whereby they will be fure to

keep the lower tier of guns well out of the water.

If a ship's body were any regular figure, the solid contents of it could eafily be found geometrically, but as the case is quite otherwise, we must be fatisfyed with dividing it into feveral parts, of which we may have a great number, and they will thereby become so small, that they may, without any sensible error, be esteemed as regular figures, limited by streight

lines, tho' some of them are actually curves.

In the draught of the 70 gun ship which we have laid down, the bottom is divided on the plain of elevation into feveral parts, in a vertical way by the lines that represent the frames; and in an horizontal way by the water lines, fo that the whole may be faid to be divided into fo many parallelopipedons, A, B, C, D, or a, b, c, d, contained betwixt the two frames 6 and 7, and limited on the fide AB by a plain supposed to be erected vertically upon the keel, and on the other fide by the round of the outside of the ship, at the height of the breadth water line, or a c. Now it is very plain that the area of the furface, which limits the lower part of this folid, is less than the area of the surface, which limits the upper part: But if we increase the water lines, and frames we may find the solid contents to a sufficient exactness for our purpose.

Now, in order to find the area of the upper furface ABDC, let AC be 16 feet 11 inches, and BD 13 feet 6 inches; add these two, the fum is 30 feet 5 inches, the half of which is 15 feet two inches and a half. and this fum multiplyed by A B, which suppose 8 feet, the distance betwit the frames, the product is 121 feet 8 inches, the area of the upper

furface of the parallelopipedon.

The area of the lower furface of the parallelopipedon may be found after the same manner, which suppose 97 feet 4 inches. Now, if these two areas be added together their fum will be 219 feet, the half of which is 100 feet 6 inches for the mean area, and this multiplied by a b, the distance betwixt the water lines, which suppose 4 feet 4 inches, produces 474 feet 6 inches cubick.

By the same process we may find the solid contents of the other parallopipeds, and adding them together, and doubling that fum we shall have

the folid content of the whole bottom of the ship in cubick feet to a

fufficient degree of exactnefs.

I made use of this method before Mr Bouguer's treatise was published, where there is one which is more convenient and expeditious, for inflead of finding the area of every single surface contained betwixt the frames upon the section of a water line, he finds by one operation the area of the whole surface formed by the horizontal section or water line, except that part intercepted betwixt the aftermost frame and the post, and the part contained betwixt the the foremost frame and the sem, which upon account of the rake must be measured separately, as also all that lies betwixt the upperside of the keel and the first water line. His method is as follows:

Take the lengths of all the lines that represent the frames on the horizontal plane, add all these together, excepting the foremost and aftermost, of which take only one half of each, so if it were required to find the area of the surface formed by a horizontal section in the plane of the load water line, it will be $\stackrel{\cdot}{Z}Z+BD+AC+IH+LK$, &c. $+\stackrel{\cdot}{Z}X+AB$, supposing AB to be the distance betwixt the frames equally spaced betwixt

ZZ and NO.

To demonstrate this, let it be considered by what operation the two trapezia ABDC and HIAC are measured. We observed in the preceeding article that this was performed by adding the length of the lines BD and AC together, and then taking half that sum; the length of the lines AC and HI, must likewise be added together, and the half of that sum taken; now, it is evident that it will be same thing to take half the line BD, and half the line HI, and the whole line AC, and add all these three together.

because the line AC, is common to both the trapezia.

After the areas of all the water lines are thus found, the folid content of the space contained betwixt the water lines may be had by multiplying the area by the distance between the water lines: But because the area sof the two surfaces which limit this part are unequal, a mean area must be found; this is half the sum of the two areas, so that all that is now to be done, is to add the areas of the water lines into one sum, excepting that of the upermost and lowermost, of which only one half of each must be taken, and if this sum is multiplied by the distance betwixt the water lines, the product will give half the solid content of the bottom, observing that the water lines in the plain of elevation be equally distant from one another.

The application of this method in finding the cubick feet contained in

a 70 gun thip laid down in the draught.

The forepart is divided into eight, and the after into nine equal parts, besides that betwixt the aftermost timber and the post, and that betwixt the foremost timber and the stem.

The bottom is likewise divided into four equal parts by water lines drawn parallel to the load water line, all which are formed upon the horizontal plane, for it will be very useful to know the solid content of each particular part contained betwixt the water lines, also to distinguish that of the fore body from the after body, whereby we may be enabled to know if the weight be duly poised. We shall consider all this in the following

calculation.

Note, there must be four inches added to each line that represents the frames in the horizontal plane for the thickness of the plank, that being nearly a mean hetwixt the thickness of the plank next the wale, and that next the keel.

The Area of the Upper Water Line abaft.

The breadth of the furface at the load water line, upon the midship frame a Q is 21 feet 2 inches, feet. one half is 10 1st Frame 21 2d Frame I 3d Frame 9 4th Frame 20 Breadth at 5th Frame II 6th Frame 7th Frame 8th Frame 7 The 9th Frame X S is 12 feet 9 inches, one half of which is 6 171

which total doubled is 343 feet 11 inches, and multiplied by 8, the diffance betwixt the frames, is the whole area of the water 2751 4 line from the midthip to the after frame, in cubick feet

To this must be added the area of the trapezium XSLe Now half of the lines XS and Le is 10 Feet o Inches Distance betwixt them is 9

Product is 97 6
which being doubled is ______ 195
The whole area in cubick feet 2946

By using the same process we may find the areas of all the other water lines, and adding all these areas together, excepting that of the first and fifth, of which taking only one half, multiply this sum by 4 feet 5 inches, which which is the diftance betwixt them, we shall have the area in cubick feet of that part of the ship abast the midship frame, contained betwixt the lower water line, and load water line.

	feet	inch.	1.	p.	
Half the area of the load water line	1473	2	0	0	
Whole area of the 4th water line	2516	1	4	0	
Whole area of the 3d water line	2052	0	4	0	
Whole area of the 2d water line	1452	10	7	6	
Half the area of the 1st water line	144	3	2	0	
Total	7638	5	5	6	
Multiplied by the distance betwixt the water lines	4	5	0	0	
Productin cubick feet betwixt the lower, and load water line	33736	6	1	3	6.
Betwixt the lower water line and keel	333	6	3	0	0
Keel and post	101	8	o	0	0
Cubick feet abaft the midship frame underwater, when loaded	34171	8	4	3	6
Cubick ft. before the midship frame under water, when loaded	28928	6	1	0	0
	63100	2	5	3	6
Multiply by the weight of a cubick foot of falt water		po	ound	ls	74
pound	ls	tuns.			Ď.
Weight of the whole ship with all her furniture } 46614	.98	2334		14	.98

We have omitted the operation for the fore part, because it is per-

formed exactly by the same method with the after part.

It must be observed that in finding the cubick feet of that part contained betwirt the lower water line and upper side of the keel, we must take the heights of all the frames intercepted betwirt these two lines, and divide their sum by the number of frames abast the midship, the quotient will be 1 soot o inches o lines.

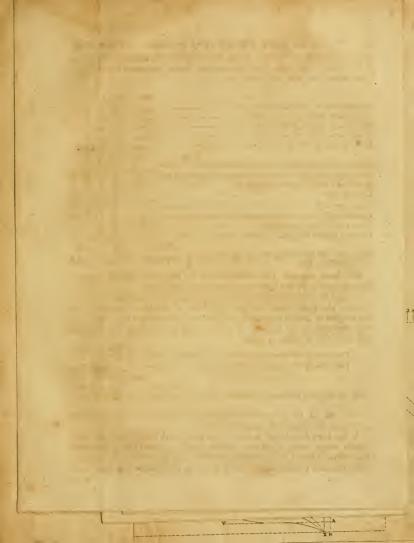
The area of the lower water line is	Feet 288		Lines 4	
The area of the upper fide of the keel	_79	6	0	
Total	368	0	4	
one half is	184	0	2	
Area of that part contained betwirt the lower water line and keel	222	6	2	

The use of the preceeding calculation is to know if the load water

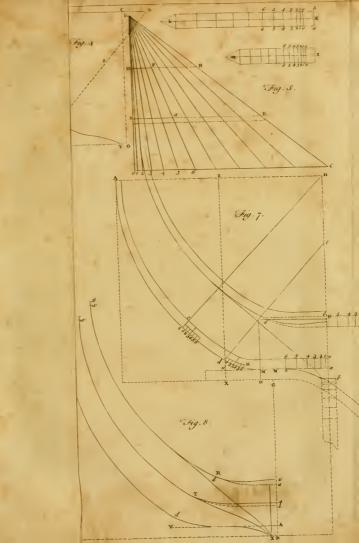
line upon the draught be properly placed.

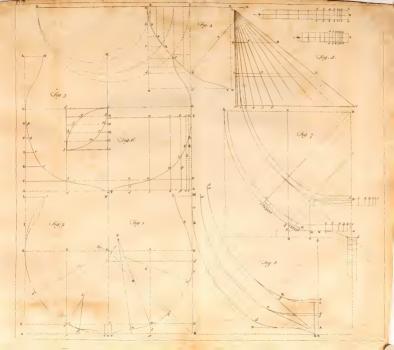
It has been found that a ship of 70 guns, with every thing on board, should weigh nearly 2350 tons, which is only 15 tons 1297 pound more than what is found by calculating from the load water line in the draught, this difference would occasion the ship not to draw above one inch more

water









water it is not worth the regarding. But then by this calculation we diffeover that the ship is too lean before; for whereas the fore part should exceed the after part by 30 tuns, we find, by this calculation, that the after

part exceeds the fore part by 193 tuns 1995 pounds.

Upon this account we must consider carefully if the midship frame is properly placed; it is here 5 seet before the middle. If the midship frame was exactly in the middle it would augment the weight of the fore part 102 tuns 307 pounds, and diminish that of the after part exactly the same quantity, by which means the fore part would be 1172 tuns 1014 pounds, and the after part 1162 tuns. Now we may fill out the fore part, so as to gain 15 tuns 636 pounds, which was deficient, to make the calculation taken from the draught agree with the real weight proposed for a ship of 70 guns sitted out for sea, with fix months provision on board; and the fore-body will weigh 25 tuns 1255 pounds more than the after part, which may be judged sufficient.

C H A P. IX.

A method to calculate the Resistance of the Water upon the fore Part of the Ship.

AILY Experience sufficiently proves that the sluids, by their motion, attack the solids that oppose them, as bridges, mills, &c. with such violence as to carry all before them; and this is agreeable to

the very nature of fluids.

For all fluids are an affemblage of a prodigious number of small solid bodies of a globular form, each of which being easily put in motion will ask upon any surface with the same force that any other solid body of the like mass would do. But as these particles have but a very small cohefion with each other, sluids cannot ask with the same force as solids which

have their parts united.

A mass of water of 20 cubical sect will not act with the same force upon the pier of a bridge which opposes it, as a mass of ice of the same dimensions; because the whole mass of ice having its parts so united together, that one cannot advance without the other, it gives the blow with the united force of all the parts at once, whereas the parts that compose the mass of water, being but slightly united, they cannot act jointly or in concert, and they exert their force one after another; they indeed succeed one another immediately, and are a little united by their reciprocal prefixer:

fure; but as every part has its own peculiar velocity, so it makes its effort fingly by itself, and, being easily put in motion, it will be as easily turned out of its direction, the parts being only retained together by the weight of those that come next them.

Fluids have a continual effort, because when a certain number have produced their effect they are succeeded by others as long as the cur-

rent lasts.

Hence it will follow, that when a vessel is lest to a current of the river, it can receive no more velocity than the current has, and its velocity will be accelerated till it is equal to that of the current.

If, on the contrary, any floating body receives a motion in a contrary direction to that of the current, it will be continually retarded, till it has none, and then it will change its direction to follow that of the current.

We shall here remark, that it is indifferent whether we ascribe the motion to the solid or to the suid; for the impression of the water upon the ship's stem is the same when under sail, as when at an anchor, provided the motion of the current be equal to that which the ship acquires by sailing.

The effort of fluids is as the square of the velocity of the current.

It is very plain that the more rapid the current is, the greater will the impression of the sluid be; for the parts will then shock the solid with greater force than when it runs slowly; so that the force is augmented in proportion to the velocity. Again, the number of the parts of the sluid that strike the solid in any space of time, is in proportion to the velocity of the current; for the saster it runs the greater will be the number of the parts that strike the solid in a space of time; so that not only the effort of the fluid, but likewise the number of parts that attack the solid, is augmented in proportion to the velocity of the current, and when these two are united, the effort of the sluid will be in a duplicate ratio of the velocity; so that if the velocity be doubled, the shock will be quadrupled.

Hence, the faster a ship goes through the water, the greater will be the resistance she meets with, and this will be augmented in a duplicate ratio

of the velocity with which she sails.

The impression of a fluid increases as the surfaces which oppose its

It is very plain, that if one surface is double another it will receive double the number of the parts of the sluid, and of consequence the impression will be double upon a surface, whose area is double the area of another surface. Hence those ships whose midship frames have the greatest capacity meet with most resistance.

The efforts of fluids will be less when the surfaces are in an oblique

polition to the current, than when in a perpendicular polition.

Plate IV. Fig. 7.] Let E A represent the course of the fluid setting perpendicularly on any body AB; it is plain, that it receives the impression of all the parts of the fluid contained between A and B; whereas, if the point B be moved to D, the parts of the water contained betwixt B and G will have no impression upon A D. Hence the quantity of the sluid which attacks AB is to that which attacks AD as AB is to AG; that is, as the radius is to the fine of the angle of incidence E A D. But if there were no other advantage gained by this oblique position, than being exposed to sewer parts of the fluid, it would be of very little fervice to a ship which must have a sufficient breadth, suppose A B; it is plain, the number of the parts of the fluid which give the impression will be the fame, when the fore part of the ship is in the form of ADB, as when it is flat in the form of AB; but the fluid which exerts its force on the furface ADB does not produce the fame impression as when it exerts its force on AB, because the direction of each particle of water, which strikes any surface obliquely, may be resolved into two directions. one perpendicular, and the other parallel to the plane.

In order to give us an idea of compound motions, and of the resolution of their forces, let us suppose two rulers A A and B B, (Plate IV. Fig. 5.) placed upon a plane at right angles to one another, and a small ball C placed at the angle of their meeting, it is plain, if we slide the ruler B B in a parallel position to itself, it will carry the ball C along the edge of the ruler A A; but if both the rulers be made to slide together, so that they still preserve the same angle, in such a manner that when the ruler A A arrives at the line VII, VII, the ruler B B arrives only at the line 3, 3. It is plain, the ball will describe the diagonal of the parallelogram C, VII, D, 3. the sides of which will be proportional to the distance the rulers have moved, that is, D VII is to D 3 as 3 to 7; but if the rulers be supposed to be moved equally, so that when A A arrives at the line VII, VII, B B shall arrive at the line 77, the ball will describe the

diagonal CF of the square C VII, F 7.

Now, if we substitute any other two agents in the place of the rulers, such as two hammers, and both be supposed to strike the ball with equal force at the same time, it is plain, the ball will go in the direction of the diagonal CF; but if the force with which one hammer strikes the ball be to that by which the other hammer strikes the ball, as 7 to 3, then

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- 1 th die the state of the sta

the ball will move in the direction of the line CD.

The principal Effects of Compound Motions. (Plate IV. Fig. 6.)

If two powers C and B act with equal force on the body A, but in the contrary directions of the lines C A and B A, the body A will remain at reft; but if one of the powers acts with greater force than the other, the body will follow the direction of that which predominates, diminished by the quantity of the smaller force.

2d, If two powers D and E act upon the body A in the same direction, viz. in the lines D A and E A, the body A will sollow the direction of both, and pass through the point F, with this only difference, that it will go with greater velocity when impelled by both powers than with one.

3d. Let the two powers G and H strike the solid A, in the direction of the lines G A and H A, it will thereby receive a compound motion, the force and direction of which may be expressed by the diagonal of a

parallelogram, as was before observed.

In order to confruct this parallelogram, which is called the refolution of the forces, let the two powers G and H be fupposed equal and expressed by the lines H A and G A; from the point G draw the line E G equal and parallel to H A, and the diagonal E A (the result of the two powers represented by the sides of the parallelogram H A and GA) shall express the velocity and direction of the compound motion; the effect of which will be, that the body A will be carried to the point F. But supposing the forces unequal, and let that of H, (Fig. 9) represented by the line H A, be double that of G, represented by the line R A; then from the point R draw the line R S equal and parallel to H A, which shall express the force and direction of the power H; and from the point H draw the line H S parallel to R A, which will express the force and direction of the power G; the diagonal S A expresses the velocity and direction of the body A, which will pass through the point T, whereas, if the powers were equal, it would pass through the point F.

It may be remarked, that two attractive powers placed at P and Q, would produce the same effect as two impulsive powers at G and H, and that the parallelogram may be constructed on the lines AQ and AP.

CONSEQUENCES.

1st. The acuter the angle of the direction of the power is, the nearer will they approach to one direction, and act with greater force; so the result of G and H is greater than that of K and I, supposing the powers to be equal.

2d. The greatest effect of two powers is, when they both act in the

same direction, and the least when they act in contrary directions.

3d. When two equal powers act in such a direction that they form an angle of 120 degrees, as A K and A I; in this and in no other case, the result will be equal to the single force of A I or A K; it only changes the direction; for when the two powers act jointly, A will be carried to F, whereas if K only acted, it would be carried to T; or if I only acted, A would be carried to V.

4th. If the direction of two powers make an angle less than 120 degrees, as G A and H A, they will assist one another; but if they form an angle greater than 120 degrees, as L A and A M, they will be recipro-

cally diminished.

The Refults of a Motion impressed upon a Body A, in Relation to a Surface a b, which opposes its Motion. (Plate IV. Fig. 6.)

1st. When a body strikes a surface obliquely it will be with less force than when it strikes it perpendicularly; for it may strike it so obliquely as only to graze along it; between the perpendicular shock, which is the greatest, and the oblique, which approaches nearest to a parallel to the surface, there may be an infinite number of directions, less or more oblique, and the surface will be struck with more or less force.

2d. If the two powers are united in D, they will act, in the direction DF, with great force upon ab, because they not only act jointly, but

likewise in a perpendicular direction upon the surface ab.

3d, If the two powers be equal in force, and act in the direction of the lines GA and HA, the body A will also fall perpendicularly on the furface ah, but with less force than in the first case, because of the obli-

quity of the directions.

4th, If the power H have double the force of the power G, then the direction will be changed into the line SA, (Fig. 9.) and the body will strike the surface obliquely in the direction of the line ST, but with less force than in the second case, not only on account of the diminution of the force of the power G, but also on account of the obliquity of the shock.

5th. It will be indifferent whether the body A receives its impulse from one single power, or from two, so that it strikes the surface ab in the same direction. Hence we shall have no occasion to consider the powers which give the motion, but only the velocity and the direction in which they strike the surface.

6th. It will produce the same effect, whether we change the line of direction

direction, in which the body A strikes the surface ab, or change the po-

fition of the surface ab in respect of the line of direction.

From what has been faid, it will follow, that if the common effect of two powers acting upon the same body be known, and also the direction and sorce of one of them, then the direction and sorce of the other may be found; for let the body G (Fig. 5.) be carried to the point D by the action of two powers, and one represented by the line G, VII; draw the line D 3 equal and parallel to C, VII, and compleat the parallelogram, so shall G 3 express the sorce of the other power.

The Application of what has been said to the Shock of Fluids.

We have hitherto considered the shock of a solid body in different directions upon the surface of another solid, but we will readily grant that sluids do not act in the shock in the same manner that solids do. It is very probable, that when a sluid salls perpendicularly upon a surface, there is a mass of water that rests immoveable before the surface, which occupies the place of a solid body, and has nearly the same effect as if the surface was round, so that the sluid does not attack the body that opposes it in a direction perpendicular to its course; besides, the particles of water which attack a surface, whether obliquely or not, may rebound and change their direction, so that the laws of sluids are quite different from the laws of solids in the shock.

The oblique direction of a particle of water may be refolved into one that is perpendicular to the body which opposes its course, and one that

is parallel to it.

In order to conftruct this resolution, (Plate IV. Fig. II.) upon the line AC inclined to the current, form the parallelogram AHEF (AE representing the velocity and direction of the current) making EF parallel to CA and EH perpendicular to CA. The diagonal EA, which represents a particle of water and its velocity, will be the result of a motion supposed to be produced by two powers, one parallel to AC, whose force and direction is represented by EF, the side of the parallelogram.

Hence it will follow, that when a surface is exposed to the shock of a current, in different oblique directions, the force of the direct shock is to that of the oblique, as the square of the radius is to the square of the fine of the oblique angle of incidence; for the effort of the particle E.A, which strikes the body A.B, in a perpendicular direction, is to the effort of the same particle of E.A, which strikes the body A.C in an oblique direction, as E.A is to E.H.; but E.A is to E.H. as A.B, the sine of the right angle,

angle, is to AG, the fine of the oblique angle of incidence. But it was before observed, that the sum of the particles that strike AB is to the sum of the particles that strike AC as the radius is to the fine of the angle of incidence. Hence, by multiplying the effort of one particle, by the number of particles that strike AB; (that is, the effort of the whole water upon AB) and multiplying the effort of one particle, by the number of particles that fall upon AC, (that is, the effort of the whole sluid upon CA) we shall have the following proportion: The effort of the whole sluid upon AB is to its effort upon AC as the square of the radius is to the square of the angle of incidence.

When the surfaces A B and A D, which oppose the current A E, are unequal (Plate IV. Fig. 10.) the quantities of water which strike these surfaces are as the product of the surfaces by the sines of the angles of incidence; from whence we shall have the following proportion: The effort of the sluid upon A D is to that upon A B as the square of A G, the sine of the angle of incidence multiplied by the surface A D, is to the

square of A B the radius, multiplied by the surface A B.

CONSEQUENCES.

ift, If two equal furfaces, exposed to the same current, receive its shock in different obliquities, the impressions will be to one another as the squares of the sines of the angle of incidence.

ad. A turface parallel to the current can receive no shock, because there

is no angle of incidence.

3d, If two unequal furfaces are exposed to the same current, the impressions they receive by the shock in different obliquities, are to one another as the products of the squares of the sines of the angles of incidence, and of the surfaces that receive the shock.

4th. If two equal furfaces receive the shock of two unequal currents, the impressions will be to one another as the products of the squares of

the velocities, and of the squares of the angles of incidence.

5th. If two unequal furfaces are exposed to two unequal currents, which strike them with different obliquities, the impressions will be to one another as the products of the squares of their velocities; of the squares of the surfaces.

All these consequences may be deduced from the preceding principles;

it only remains to apply them.

Let AB (Plate V. Fig. 4) represent the extreme breadth of a vessel, and let the fore part be formed according to the angles ACB, or AFB, or ALB. In order to find the efforts of the fluid, suppose

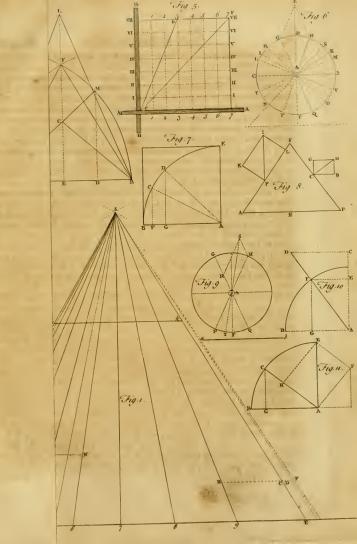
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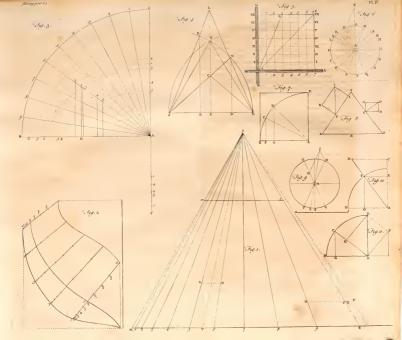
fing the velocity and direction to be the same, and parallel to the keel, in the three cases; upon the middle of the line AB, erect the perpendicular EL, which will pass through the tops of all the triangles; then to find the sines of the angles of incidence, with the radius AB describe two arches AF and BF to interfect one another in the vertex of the equilateral triangle; the arches will interfect the sides of the angle, that is less than 60 degrees; but not the sides of that which is more than 60 degrees, produce one of the sides from C to M (Plate IV. Fig. 4.) Lastly, let sail the perpendiculars MD, FE, PK, upon the line AB, from all the points where the arches interfect, either the sides of the triangles, or the sides that are produced. So shall AE, AD, and AK, represent the sines of the angles of incidence upon the different triangles AFB, ACB, and ALB.

It will be easier to observe, that the effort of the fluid upon the intire fore parts ACB, AFB, or ALB, is to the effort upon the extreme breadth, as the effort upon AC, AF, or AL, is to the effort upon AE; but it was proved before, that the impressions received by two unequal surfaces, opposed to the direction of a current, are as the squares of the sines of the angles of incidence multiplied by the surfaces, so, in this case, the impression on AC will be to that on AE, or (which is the same thing) the impression on ACB will be to that on AB, as the square of AD, the sine of the angle of incidence multiplied by ACB, is to the

square of the radius multiplied by AB.

We have also the effort on AFB to the effort on AB; as AFB. multiplied by the square of AE, the fine of the angle of incidence, is to A B, multiplied by the square of A B the radius. This proportion would shew the effort of the fluid upon the prow AFB, in a perpendicular direction to the fides AF and BF, which would be very useful, if it were required to determine the dimensions of the timber, that is, to relist that pressure of water; but in the present case, where only the relative effort upon the prow is confidered in the direction of the keel, we must form another resolution. Let then CD (Fig. 8) represent the effort upon FB, perpendicular to that furface, if from the point F we let fall the perpendicular DH, and compleat the parallelogram GCDH, CG fhall represent the relative effort upon the prow in the direction of the keel, so the whole effort upon FB, may be represented by FB multiplied by the square of the angle of incidence, which is to the relative effort as FB is to EB: The relative effort then is equal to the square of the fine of the angle of incidence multiplied by EB, or by the fum of the particles which fall upon FB; fo to find the relative effort on FB, we must multiply





multiply the square of the angle of incidence by the projection of the

plane FB upon the beam EB.

The this method cannot be truly applied but to rectilineal triangles, yet, by dividing curves into a number of small parts, each may be considered, without any sensible error, as a strait line. M. Bouguer makes use of this method of approximation to a sufficient degree of exactness. What we have already said upon that head, it is to be hoped, will facilitate this description to such as have only a slight knowledge of the mathematics; so that all that remains now is to apply this to the draught of a ship of 70 guns, which has been already laid down.

A Calculation of the Refislance of a Fluid upon the Prow of the ship of 70 Guns, which we have laid down in a draught compared with the Effort of the same Fluid upon the Area of the Midship Frame,

As the operations are to be performed upon the plane of projection before laid down, all the frames in the fore part must be exactly formed as before in *Plate* II. in order to which it will be necessary to make use of a larger scale, as in *Plate* V:

It will be very convenient to draw the water lines I, II, III, &c. and the frames 1, 2, 3, &c. to the midship frame at equal distances from one

another.

It is plain, that the water lines and frames divide the prow into trapezia, such as ra, 8b, 7c, &c. corresponding to the trapezium ab, and parallelogram ad in the plane of elevation Plate II.

It will be necessary to observe, that there must be so many water lines and frames that the lines 8 a, 7 b, 6 c, 3 cc, which are curves, may be

esteemed strait lines.

We must draw the diagonals r a, 86, 7c, &c. through the trapezia; but we may take two trapezia at once near to the midships, because the

ships fides are there nearly parallel to the current.

It will likewise be proper to observe that these diagonals are the projections of the diagonals of the parallelograms represented upon the plane of elevation, at least, on the surface of the ship; as for instance, the diagonal 8 b, on the plane of the projection, is the projection of the diagonal 8 d drawn on the plane of elevation.

These diagonals divide the prow into the triangles 1, 2, 3, 4, &c. which

strike the fluid with different degrees of obliquity.

We have not the entire areas of these triangles, by reason of the curving of the prow, but only their projection on the midship frame; but this is all we want, for the sum of all the particles of water that strike the tri-

K angle

angles are proportioned to the triangle projected on the midship frame, since the water that ranges along each triangle may be considered as a triangular prism, the base of which is equal to the triangle ra8, Fig. 1, Plate V. and this was the thing in question. Mr. Bouguer proposes to calculate the effort of the sluid on each triangle, their sum will give the shock of the water upon the whole prow, and compare this to the shock of the sluid upon a surface parallel to the area of the midship frame.

To attain this Mr. Bouguer lets fall perpendiculars to every frame, from the angles formed at the interfection of the water lines and the diagonals that were drawn to form the triangle; for inftance, upon the frame 8, the perpendicular lb and rp; upon the frame 78, the perpendicular lb on one fide, and the perpendicular nc on the other fide: Cc.

This method requires that there be as many right angled triangles formed as there are triangles on the prow, and as there must be a great number of them, it will be necessary to find some method of forming them. The following seems to me to be the most expeditious.

Draw two parallel lines BD and CR; let the diffance betwixt them be equal to that betwixt the frames on the plane of elevation, and by this one operation we have the height of all the triangles that are contained

betwixt the parallels.

As the base of all the rectangles should be equal to the perpendicular of the corresponding triangle of the prow, we may set off the length of each perpendicular upon the parallel CR; so shall CH Fig. 2, be equal to rp, Fig. 1; HL, Fig. 2, equal to sa, Fig. 1; LE equal to 8 M, &c. to compleat the triangles, draw the perpendiculars HN, LM, and the hypothenuses DH, NL, &c.

If one of these rectangles be considered singly, DH may represent the

radius, and CH will be the fine of the angle of incidence.

All these triangles being described, we may begin to find their areas on the plane of the projection, because it is upon this that the relative impulse in the direction of the keel depends, which is the thing now required, as

was before observed.

The furface of a triangle is found by multiplying half the base by the perpendicular, so the surface of the triangle r, a, 8, will be the product of the perpendicular r, p, (equal to C H) multiplied by half the base a 8, and this will be the sum of all the particles which strike the triangle r, a, 8, which is an element of the prow of the ship.

In order to find the relative force of the fluid in the direction of the keel on that part of the bottom corresponding to the triangle r, a, 8, it is

onij

only multiplying the surface of the triangle by the square of the sine of the incidence; in place of multiplying it by the square of the radius, which would give the impulse the triangle would receive from the water in a perpendicular direction; now if we divide this impulse by the oblique one, the quotient will give the quantity that the impulse is diminished by the obliquity of the prow; but there will be no occasion for this last step, for as the sum of all the products of the triangles multiplied by the square of the radius, gives the effort of the sluid upon the midship frame; the direct effort may be found by multiplying the area of the midship frame by the square of the radius, and if this be divided by the sum of the products of all the triangles multiplied by the squares of the sines of the angles of incidence on each triangle, we shall know the diminution of the resistance which the prow meets with in proportion to that of the midship frame.

It would be almost impracticable to multiply the surface of each triangle by the square of the sine of the angle of incidence, upon which account Mr Bonguer substituted proportional lines in place of the squares of the sines, which we shall now explain.

It was before observed, that if D H be the radius, C H will be the

fine of the angle of incidence.

If we let fall the perpendicular CO upon the line DH, we shall have the triangle DCH similar to DOC; so taking the equal lines CD, and NH for the radius, CO will be the fine of the angle of incidence.

If we draw OP perpendicular to DC, the triangles DOC and COP will be fimilar, therefore the triangles DCH and COP will be fimilar, and DH is to CH as OC to CP; but DH is to CH as DC to CO, and by multiplying these two proportions, the square of DH will be to the square CH as DC is to PC; that is, if DC represent the square of the radius, PC will be the square of the sine of the angle of incidence CDH. So the lines CP, HQ, LG, &c, give the squares of the sines of the angles of incidence in the triangles 1, 2, 3, &c, which are to be multiplied by the surfaces of the triangles; and the parallels DC, NH, &c. always represent the radius.

A Calculation of the Refislance of the Fluid upon the Prow of a Ship of 70 Guns, compared with that upon the Midship Frame.

Sind, compared and their upon the Little property														_ = 0.0			
اند.	10	0.00		A11			- [1				Multiply-			Product gives			
3.	Perpendi- cular.			Multiply- ed by half			Product.				ed by the			the effort of			
an											fquare of			the water up-			
316	cular.			the bafe.			0 - 20 00 000				the fine of			on the trian-			
S				Harry Market			101101				the angle of			gle.			
W 9	0.073			7 - 4 - 40			more and the late of				incidence.			h ₁ 4			
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12	0	10	0	1	7	6	1	4	3	0	0	2	0	0	2	8	6
13	0	2	6	1	76	6	0		10	3	0	0	8	0	0	2	6
14	0	4	0		6	6	0	36	2	0	0	mg I	2	0	0	7	2
15	0	i	0	1	6	6	0	Í	6	6	0	0	3	0	" 0	0	4
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The total effort of the first piece r V														104	2	8	8
Of the fecond														57	10		2
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1	Of the fourth														0	6 8	10
1000	Of the fifth													12	9	8	7
107	1		MIN.			he fi						-7		3	2	8	II
10				83			11-65								W.	1	

Total 249 10 11 7

We must in the next place find the direct effort of the water upon the area of the midship frame, by multiplying the area by the square of the radius.

minimum and a second of the se

OPERATION.

Half the 6th water line r VI	10	2	0	
The whole 5th water line V	20	0	o	
The 4th water line	19	5	0	
The 3d water line	18	I	0	
The 2d water line	15	II	6	
The 1st water line	12	0	0	
The breadth of the keel	0	0	0	
Total	95	9	6	
Multiplied by the diffance betwixt the water lines, which is	3	2	0	
Product is the area of the midship frame	303	4	I	
Multiplied by the distance betwixt the frames	8	0	0	
Product	2426	Q	Q	

This being divided by 249:10:11, the sum of the efforts of the fluid upon the triangles of the prow; the quotient is $9\frac{7}{10}$, which shews that the effort of the fluid upon the prow is to that upon the midship frame as 1 is to $9\frac{7}{10}$, which is a sufficient diminution of the resistance for a ship of this force. Hence we may conclude that the water lines in the fore-body are well formed, but a frigate will require more diminution, as will appear by the following examples.

The Brillant, as 3 to 1, a very bad failer. The Tigre, as 5 to 1, a company keeper.

A flip of 50 guns, defigned by M. Boyer, but not built, as 8 to 1.

The Monarque, of 74 guns, built by M. Ollivier in 1745, as 9 ½ to 1. The Palme, of 12 guns, 4 lb. shot, built by M. Ollivier in 1744, as

13 to 1.
The Aleid, of 64 guns, by Mr Ollivier, at Brest 1741, as 6 to 1.

The Renomne, built at Breft by Mr Defalieurs 1744, as 10 to 1.—this ship, by the account of the captians, was a very fine failer.

The Badine, 6 guns of 3 lb. shot, as 7 1 to 1.

The Panthere, of 20 guns, 6lb. shot, as 10 to 1.

The Amazon, of 44 guns, built by M. Blaife Pengalit, as 8 3 to 1.

The Superbe, built by M. Helie, as 5 20 to 1.

The Mutine, of 24 guns, built by M. Geffroi, senior, as 10 3 to 1.

We have compared the efforts of the fluid upon the prow of each thip, with that upon a plane, equal to the area of the midship frame.

It will be proper also to examine if the resistance in those be less than in ships which are known to be good failers; but it may happen that a

thip,

fhip, whose midship frame has a small area, may meet with little resistance, tho' her prow be not diminished in proportion to that of her midship frame; so it will not be sufficient to know this proportion only, to be affured whether or not the ship will be a fine sailer. We must also compare the areas of the midship frames, and not rest satisfied with comparing the efforts of the sluid; upon the prow of the ship we have laid down, with that upon the prow of a ship of the same rate, which has gained a good character.

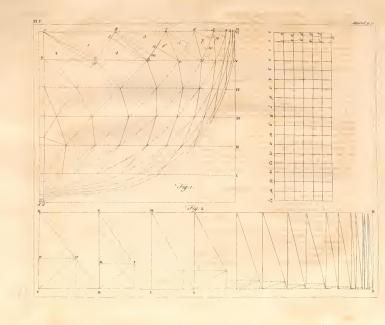
The first Example of Comparison.

We know that the area of the midship frame of the 70 gun ship, we have laid down, is 606:8:2, and that the effort of the stuid upon the prow is to that on the midship frame as 1 is to 9 \(\frac{7}{20}\). Now if another ship of the same rate has the area of her midship frame 7 or 800 seet, supposing the sails, and every thing that may contribute to sailing, to be alike in both; it is plain this last cannot sail so well as that we have laid down, and by this example, it is very plain, that if we would calculate which of two ships would sail best, we must, after finding how much the resistance of the fluid upon the midship frame of each is diminished by the form of their prows; also compare the areas of their midship frames, that we may know which of the two has the greatest mass of water to displace; but if it was only required to know, which of two ships of the same rate would sail best, it would be sufficient to compare the efforts of sluids upon their prows.

The fecond Example of Comparison.

We have found by the calculation, that the effort of the fluid upon the prow of our fhip of 70 guns, is 249:10:11:7; but if by a like calculation we find the refiftance upon the prow of a ship of the same force, and carrying the same quantity of sail, to be 300 feet, we may thence conclude that ours will sail best.

It will be proper to examine, by the fame calculation, whether the ship we have laid down, can carry a good sail, drive but little to the leeward, and streer well; but as this treatife has already exceeded the bounds I proposed, I am forced to confine myself to the two preceding conditions, which are the most important. The methods to find the other qualities of the ships we lay down, may be sound in Mr Bouguer's treatife.







An Explication of the Signs or Characters made use of in this TREATISE.

SIGNS. NAMES. SIGNIFICATIONS.

Plus, or more. The fign of addition, as 3 + 5, is 3 more 5, that is, the character + placed between any two or more figures, fignifies that they are to be added into one fum.

Minus, or less and fignifies that 3 is to be taken from 5.

Multiplied by $\begin{cases} & \text{The fign of multiplication, as } 5 \times 3, \text{ fignifies} \\ & & \text{5 multiplied by } 3. \end{cases}$

Divided by $\begin{cases} \text{The fign of division, as } 8 \div 4, \text{ fignifies } 8 \text{ divided by } 4. \end{cases}$

The fign of equality, that is when this is placed betwixt numbers or quantities, it fignifies that they are equal. as 5+3=8, or 10-2=5+3, that is, 5 more 3, is equal to 8, and 10 lefs 2, is Lequal to 5 more 3.

So is The fign fimularity of ratio. It is always placed betwixt the two middle terms or numbers in proportion, thus 3:9::8:24, that is, as 3 is to 9, fo is 8 to 24.

R. Radius.

S. Sine.

T. Tangent,

Sec. Secant.

S. c. Sine complement.

T. c. tangent complement. Sec. c. Secant complement.

H. Hypothenuse.

B. Base.

P. Perpendicular.

ERRATA.

Page	Line	for	read
14	19	a în	in a
25	15	of division	in the divisions
26	31	f B	fb
30	Margin	Fig. 25	Fig. 25 at Prop. VIII-
- 30	30	Cfe	CfE
	13	from the point N, &c.	cancel
35 - 38	Margin	Fig. 5.	cancel
- 30	Margin	Plate II.	Plate I. Fig. 37.
40		Fig 1.	Plate II. Fig. 1.
40	Margin	Fig 6, 7, 8, 9, 10.	cancel
41	Margin	Example	Examples
41	30		cancel
43	Margin	Fig. 30.	
49	4	40	50
49	10	50	40
49	13	base at A also for 50	base; at A read 40
53	15	Tx = xE	Tx = xF
53	18	m, s, n, t,	ms, nt,
53	34	FD	F d
56	17	the	then
56	27	$rt\frac{\tau}{2}rs$	$rt \times \frac{1}{2} rs$
58	12	1.14592	3.14592
58	31	785	.785
59	5	whose diame-	whose diameter is 1.
59	30	line, as	line
04	II ,	C m	Cs
64	12	ms×C+	$ms \times Ct$
		Cs	Cs =
64	21	including the areas	including half the areas
68	Margin	731 7	before Case 2d. prefix Fig. 53
82	Margin	Plate I.	Plate II.
82	0 17	5.9990	5.6990
102	Column 8	Length	Depth
103	22	as in the columns	cancel
104	7	6.25	625
105	2	height	length
105	16	double line; on the rule	double line on the rule; look
106	21	11,	1, 1,
106	22	11,	I, I,
106	last line	AC	AD
110	31	fo B	t o B
111	4	Fig. 2.	Fig. 9.
111	5	SS	SS Fig. 2.
114	5	remarked	marked
121	36	15, 26, 36,	1r, 2d, 3a.
122	34	GAE	CAE
		provided the dimensions	
124	2 and 3	and inclination of these	cancel "
		planes to one another be	
,		given,	
126	32	sqcb	5 9 7

ERRATA:

Page	Line	for	read =
130	18	the body	the body plane
131	16	ribband lines	ribbands
			See Plate VII. where the curves
133	after line 22	add	here defined are distinguished
			by their initial letters.
136	36	M to y	M to S
137	37	C	C
138	19	BEND	Bend Mould
138	26	H lw	Hollow mould
144	20	floor	floor timbers
152	10	50	fo
162	29	61	b l
168	40	when this is	cancel
169	t	hewed of	cancel
169	1	of the outside	(in that direction)
199	8	+.697997	+1.697997
201	17	56° 15'	56 15' to 33° 45'
204	4	ftance	distance
214	ri	Eo: En	En: Eo
217	1	50	15
218	16	Cx	CX
225	5	Long line	Log line
225	17	A B	AC
225	18	BE	AE
228	31	difference of R	difference of latitude; R.
231	7	by 3 15	cancel
237	4	north	fouth
244	24	65338	65338
-74	25	18668	18688
249	6	27°. 2' R: differenece of	
		latitude	tude 1063:
249	7	distance: 1191	distance 1191
249	14	2.738920	2.739030
249	28	75.7	75.5
249	29	18.4	21.1
249	30	546.9	549.6
250	35	fide	fine
253	10	30	60
253	11	60	30
253	33	25	15
254	1	25	15
254	2	15	25
254	6	15	25 P P
256	4	Pp	
256	6	P'p	PP
258	12	transcribe	transcribes
258	34	make	makes

ERRATA to the APPENDIX.

Page	Line	for	read
18	22	of D	D
22	33	d and K	d and S
22	35	to g	to l
22	35 36	s and I	s and l
23	5 6	d also for dx	b read bx
27	5 7	point X	point #
27	14	ŔS	Ŕ
27	17	point X	point #
35	26	lines	line
37	26	n L	NL
35 37 38 40	17	HP	Нр
40	23	S	5
42	10	from N	firike it out
43	27	3d from l	3d from i
44 54 62	20	zx	z y
54	17	&c. + 2 X S + A B	&c. + XSXAB
62	25	Plate IV. Fig II.	Plate IV. Fig. 11.
			and the other perpendicular to
62	line 32	add	it whose force and direction is represented by the line EH.

Where the References to the Plates are omitted in Part II. See Plate VII. and in the Appendix, See Plate 2.

TABLES of the Sun's Declination: Adapted to the New Style.

First after Leop Tear. Sun's Declination 1753, 1757, 1761, 1765, 1769.

17	7.30	100	80		1110	co I	186	7.1/	M	10	7.	re 1	7.	W 1	du.	40 1	Seet	an I	UA	6 1	λ.	v. 1	Die	7700	6 1
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6	22	28	15	23	05	20	c6	37	16	40	22	43		42	16	39	.6	20	05	17	16	09	. 2	36	6
7	22	30	15	10	05	06	97	00	16	56	22	49	22	36	16	21	06	57	05	40	16	30	22	43	
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9	22	07	14	31	04	10	07	45	17	29	23	00	22	22	15	48	05	12	06	26	17	CI	13	55	
10	2.8	55	174	12	02	55	08	07	17	44	23	05	22	15	15	31		40		48	17	18	23	00	1
11	31	46	13	52	02	32	08	29	13	00	21	00	23	07	15	13	(4	26	67	11	17	25	2.2	05	11
12	21	35	13	32	03	03	c8	51	18	15	23	13	21	58	14	55	04	03	67	34	17	51	23	10	1
113	21	25	13	12	02	44	cq	13	18	39	23	16	21	50	14	36	03	40	C7	46	18	07	23	14	13
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111	21	0.1	12	31	OI	57	00	55	18	59	2.2	22	31	3.1	13	50	62	54	68	41	18	38	2.3	20	1.0
16	20	52	12	10	CI	33	10	17	19	11	23	24	21	22	13	40	02	31	09	03	18	54	22	23	16
17	20	40	11	49	OI	10	19	28	19	26	23	26	21	11	13	21	02	80	0.0	25	10	08	23	25	10
18	20	28	11	28	00	46	10	59	12	39	23	27	2.1	OI	13	02	01	44	cq	47	19	23	23	27	18
10	20	3.5	11	06	co	22	11	20	19	52	22	28	20	50	12	42	CI	21	10	00	19	37	2.3	28	10
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22	In	35	10	01	co	49	12	21	20	29	23	20	20	15	11	42	00	11	41	11	20	17	23	29	21
22	10	21	CQ	39	01	12	12	41	20	41	22	28	20	03	11	22	Sou	. 13	11	34	20	29	21	28	81
24	19	06	09	17	21	36	13	OI	10	52	23	27	10	SI	11	10	00	36	11	55	20	41	22	27	14
25	13	51	08	55	02	00	13	20	3.5	03	23	20	10	38	10	40	OI	00	12	. 16	20	53	23	25	35
26	18	36	c8	32	02	22	13	39	2.1	12	23	24	10	25	10	20	10	23	12	37	21	04	23	23	26
27	13	21	08	10	03	47	13	59	21	21	23	21	10	II	00	58	01	47	12	57	21	15	23	21	37
28	18	05	07	47	02	10	14	18	11	33	23	19	18	57	00	37	02	10	13	17	21	26	123	18	28
29	17	49	1	.,	03	33	14	36	21	42	23	15	18	43	00	16	03	34	113	37	31	36	23	14	29
39	17	12			03	57	14	55	21	51	23	12	18	20	08	54	C2	57	13	57	21	46	23	10	30
17	17	15			04	20	1	-	22	08	1		18	14	08	33	1	31	14	17	1		23	06	31
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Second after Leap-Year. Sun's Declination, 1754, 1758, 1762, 1766, 1770.

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3		0 16		00	44	05	23	15	44	22	22	22	59	17	31	97	32	04	02	15	09	22	12	3
4		13 10		06	21	05	46	16	01	22	29	22	54	17	15	97	10	94	.25	15	28	2.2	20	4
5		37 19		05	58	06	09	16	18	22	36	22	49	16	59	06	47	04	48	15	47	22	27	5
6		C 1		05	35	c6	32	16	35	22	43	22	43	16	43	06	25	05	11	16	05	22	34	0
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13		18 1		01	14	c8	45	18	11	23	11	22	00	14	59	0.4	32	07	28	17	31 48	23	10	111
13		28 1		C2	51	00	07	18	16	23	15	21	52	14	41	03	46	07	50	13	04	23	14	10
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15		06 1:		CZ	03	00	50	13	56	23	2.1	21	34	13	04	02	00	08	35	18	35	23	20	
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21		52 1	0 28	No	1.19	11	55	20	14	23	29	20	30	12	07	co	39	10	47	20	00	23	29	21
22	19	38 1	0 07	co	43	12	15	20	26	13	29	20	18	11	47	00	16	21	08	20	13	23	29	2.
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24		10 6		01	30	12	55	20	50	23	27	19	54	11	o6	00	31	11	50	20	38	-3	27	24
25		55 C		01	53	13	15	21	01	23	26	19	41	10	45	00	54	12	11	20	50	23	26	25
26		40 0		02	17	13	34	31	3 1	23	24	19	29	10	24	10	17	12	32	2.1	02	23	24	26
27		25 0		02	40	13	53	21	31	23	21	19	15	10	03	CI	40	12	51	11	13	23	21	27
		09 0	7 53	03	04	14	12	21	31	23	18	19	10	c9	42	02	04	13	11	2.2	24	23	18	28
19		53		103	27	14	31	21	40	23	15	18	47	cg	20	02	28	13	32	2.1	34	23	15	24
10		37		03	25	14	50	21	49	23	12	18	33	02	58	02	52	13	2	2.1	44	23	11	30
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TABLES of the Sun's Declination. Adapted to the New Stile.

Third after Leap-Year. Sun's Declination 1755, 1759, 1763, 1767, 1771.

179	-	-		-	-	-	1 1 22	-	-	-	-	-	-		_		_	_							
2	1.7	onu.	1 8		IM.	rco	d	bril	1 Di	lay	1 7	unc	1	uly	1 Au	gujt	1 Sep	tem.	10	čt.	1 N	ov.	Des	cem.	TE
5	S.	outh	So	uth	15,	uth	N.	orth	No	orth	No	orth	N.	orth	No	orth	1 No	orth	So	uth	Sa	uth	So	uth	y's
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3	2.2	51	16	31	105	50	105	17	15	40	22	20	23	01	17	35	07	38	03				22		1 2
4	22	45	16	14	06	27	0.5	40	115	58	22	27	22	56	117	10	07	16		55	1 15	05		09	3
6	22	39	15	56	06	03	06	02	16	15	22	34	22		17	04	06		04		15	24	22	17	4
6	2.2	32	115	33	05	40	06	26	16	32	22	40	22	50	16		06	54		41	16	42	22	25	5
7	22	24	15	19	05	17	06	48	16			46		38	16	48		32	05	04		00	22	32	6
8	22	16	15	00	04		07	10		49	22		22			31	06	09	05	27	16	18	22	39	7
	22	08				54			17	05	22	52	22	32	16	14	05	46	05	50	16	36	22	45	8
9	21		14	4I 22	04	97	07	31	17	22	22	57	22	25	15	57	05	23	06	13	16	54	22	51	9
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11	119	56	10	34	No	.14	11	50	20	12	23	29	20	33	12	12	00	45	10	42	19	57	23	20	21
12	19	42	10	11	00	37	12	10	20	24	23	20	20	23	11	52	00	22	11	04	20	10	21	20	22
-3	19	28	00	50	OI	OI	12	30	20	36	23	28	20	11	11	32	Sou	.01	11	25	20	23	23	20	23
24	19	14	09	38	OI	24	12	50	20	47	23	28	Iq	58	II	12	00	25	11	45	20	35	23	28	24
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27	18	20	08	21	C2	35	13	48	21	IQ	23	22	Io	18	10	00	OI	35	12	47	21	10	23	22	27
.8	18	11	07	58	02	58	14	07	21	20	23	20	Iq	04	00	48	01	59	13	07	21	21	23	19	28
20	17	56	l '		02	22	14	26	2.1	38	23	17	18	50	00	27	02	22	13	27	21	31		16	20
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167	17	22			04	68	-4	73	21	-6	-3	-4	18	21	08	44		45	14	07	-1	42	23	00	30
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Leap-Year. Sun's Declination, 1756, 1760, 1764, 1768, 1772.

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Н	Da		nu.		ru.		ar.	A			lay		une	1.5	uly		gust		tem.		3.		9 v ,		em.	D
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и	7	22	40	16	00	05	46	06	20	16	27	22	39	22	47	16	52	06	37	04	59	15	55	22	30	4
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ı	7	22	26	15	24	04	59	07	05	17	00	22	51	22	34	16	18	05	52	05	45	16	31	22	44	7
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и	9	22	10	14	46	01	13	07	50	17	33	23	01	23	20	15	44	05	06	06	31	17	06	22	56	9
	10	22	01	14	27	03	49	08	12	17	48	23	06	22	13	15	26	04	44	06	54	17	23	23	OI	10
	11	21	52	14	07	03	26	08	34	18	04	23	10	22	oş	12	08	04	21	07	17	17	39	23	06	II
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и	17	20	49	12	05	OI	04	10	42	19	29	23	26	21	00	13	16	OZ	02	09	31	19	12	23	25	17
н	18	20	37	11	43	00	40	11	03	19	42	23	28	20	58	12	57	01	48	09	53	19	26	23	27	18
н	19	20	25	11	22	00	16	11	24	19	55	23	28	20	47	12	37	01	15	10	14	19	40	23	28	19
	20	20	12	II	Oï	No	1.07	11	45	20	08	23	29	20	36	12	17	00	52	10	36	19	54	23	29	20
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	22	19	45	10	18	00	55	12	26	20	32	23	28	20	13	11	37	90	05	11	19	20	20	23	29	22
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	25	19	03	09	34	02	41	12	25	21	54	23	25	19	35	10	35	OI	06	12	21	20	44	23	25	25
	26	18	48	08	40	02	20	13	44	21	15	23	23	19	21	10	14	OI	29	12	42	21	07	22	22	26
	27	18	32	08	27	02	52	14	03	21	25	23	20	10	08	00	53	01	53	13	02	21	18	23	10	27
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2 :	19	18	OI.	07	41	03	39	14	41	21	44	23	15	18	40	09	11	OZ	39	13	42	21	39	23	13	29
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A Large and very Useful

TABLE OF DIFFERENCE

OF

LATITUDE and DEPARTURE

IN

MINUTES and TENTH PARTS

TO

Every DEGREE and QUARTER-POINT

OF THE

COMPASS,

For the exact Working of a

TRAVERSE.

4	AND DESCRIPTION OF				A T	ABL	e of	Dr	FFER	ENC	E				
O	ΙL	Jeg.	2 1	eg.	‡ Po	oint.	31	Deg.	4 I	Deg.	5 I	Deg.	Po	int.	Dift.
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1	01.0	00.0	01.0	00.0	01.0	00.0	01.0	00.1	01.0	00.1	01.0	00.1	01.0	00.1	I
2	02.0	0.00	02.0	00.1	02.0	00.1	02.0	1.00	02.0	00.1	02.0	00.2	02.0	00.2	2
3	03.0	00.1	03.0	00.1	03.0	00.1	03.0	00.2	03.0	00.2	03.0	00.3	03.0	00.3	3
4	04.0	00.1	04.0	1.00	04.0	00.2	04.0	00.2	04.0	00.3	04.0	00.3	04.0	00.4	4
_5,	05.0	00.1	05.0	00.2	05.0	00.2	05.0	00.3	05.0	00.3	05.0	00.4	05.0	00.5	5
6	16.0	00.1	06.0	00.2	06.0	00.3	06.0	00.3	06.0	00.4	06.0	00.5	06.0	00.6	6
7 8	07.0	00.1	07.0	00.2	07.0	00.3	07.0	00.4	07.0	00.5	07.0	00.6	07.0	00.7	7
	08.0	00.1	08.0	00.3	09.0	00.4	09.0	00.4	09.0	00.6	09.0	00.7	09.0	00.0	9
10	10.0	00.2	10.0	00.4	10.0	00.5	10.0	00.5	10.0	00.7	10.0	00.0	10.0	01.0	10
	11.0	00.2	11.0	00.4	11.0		11.0	00.6	11.0	00.8	11.0	01.0	10.0	01.1	11
11	12.0	00.2	12.0	00.4	12.0	00.5	12.0	00.6	12.0	00.8	12.0	01.0	11.9	01.1	12
13	13.0	00.2	13.0	00.4	13.0	.00,6	13.0	00.7	13.0	99.9.	12.0	01,1	12.9	01.3	13
14	14.0	00.2	14.0	00.5	14.0	.00.7	14.0	.00.7	14.0	01.0		01.2	13.9	01.4	14
15	15.0	00.3	15.0	00.5	15.0	00.7	15.0	00.8	15.0	01.0	14.9	01.3	14.9	01.5	15
16	16.0	00.3	16.0	00.6	16.0	00.8	16.0	00.8	16.0	01.1	15.9	01.4	15.9	01.6	16
	17.0	00.3	17.0	00.6	17.0	00.8	17.0	00.9	17.0	01.2	16.9	01.5	16.9	01.7	
17	18.0	00.3	18.0	00.6	18.0	00.9	18.0	00.9	18.0	01.3	17.9	01.6	17.9	01.8	17 18
19	19.0	00.3	19.0	00.7	19.0	00.9	19.0	01.0	19.0	01.3	18.9	01.7	18.9	01.9	19
20	20.0	00.4	20.0	00.7	20.0	0.10	20.0	01.0	20.0	01.4	19.9	01.7	19.9	02.0	20
21	21.0	00.4	21.0	00.7.	21.0	01.0	21.0	01.1	20.9	01:3	20.9	01.8	20.9	02.I	21
22	22.0	00.4	22.0	00.8	22.0	01.1	22.0	01.1	21.9	01.5	21.9	01.9	21.9	02.2	22
23	23.0	00.4	23.0	00.8	23.0	01.1	23.0	01.2	22.9	01.6	22.9	02.0	22.9	02.3	23
24	24.0	00.4	24.0	00.8	24.0	01.2	24:0	01.3	23.9	01.7	23.9	02.1	23.9	02.4	24
25	25.0	00.4	25.0	00.9	25.0	01.2	25.0	01.3	24.9	01.7	24.9	02.2	24.9	02.4	25
26	26.0	00.5	26.0	00.9	26.0	01.3	26.0	01.4	25.9	01.8	25.9	02.3	25.9	02.5	26
27 28	27.0	00.5	27.0	00.9	27.0	01.3	27.0	01.4	26.9	01.9	26.9	02.4	26.9	02.6	27 28
20	29.0	00.5	29.0	01.0	29.0	01.4	29.0	01.5	28.9	02.0	28.9	02.5	28.9	02.9	29
30	30.0	00.5	30.0	01.1	30.0	01.5	30.0	01.6	29.9	02.1	29.9	02.6	29.9	02.9	30
-	31.0	00.5	31.0	OI.I	31.0	01.5	31.0	01.6	30.9	02.2	30.9	02.7	30.8	03.0	31
31	32.0	00.6	32.0	01.1	32.0	01.6	32.0	01.7	31.9	02.2	31.9	02.8	31.8	03.1	32
33	33.0	00.6	33.0	01.2	33.0	01.6	33.0	01.7	32.9	02.3	32.9	02.9	32.8	03.2	33
34	34.0	00.6	34.0	01.2	34.0	01.7	34.0	01.8	33.9	02.4	33.9	03.0	33.8	03.3	34
35	35.0	00.6	35.0	01.2	35.0	01.7	35.0	01.8	34.9	02.4	34.9	03.1	34.8	Þ3.4	35
36	36.0	00.6	€6.0	01.3	36.0	01.8	35.9	01.9	35-9	02.5	35.9	03.1	35.8	03.5	36
37	37.0	00.6	37.0	01.3	37.0	01.8	36.9	01.9	36.9	02.6	36.9	03.2	36.8	03.6	37
37 38	38.0	00.7	38.0	01.3	38.0	01.9	37.9	02.0	37.9	02.7	37.9	03.3	37.8	03.7	38
39	39.0	00.7	39.0	01.4	39-0	01.9	38,9	02.0	38.9	02.7	38.9	03.4	38.8	03.8	39
40	40.0	00.7	40.0	01.4	40.0	02.0	49.9	02.1	39.9	02.8	39.8	03.5	39.8	03.9	40
41	41.0	00.7	41.0	01.4	41.0	02.0	40.9	02.1	40.9	02.9	40.8	03.6	40.8	04.0	41
42	42.0	00.7	42.0	01.5	41.9	02.1	41.9	02.2	41.9	02.9	41.8	03.7	41.8	04.1	42
43	43.0	00.8	43.0	01.5	42.9	02:1	42.9	02.2	42.9	03.0	42.8	03.8	42.8	04.2	43
44	44.0	00.8	44.0	01.5	43.9	02.2	43.9	02.4		03.1	43.8	03.8	43.8	04.4	44
45	45.0	00.8	45.0	01.6	44.9	1	1		1						45
46	46.0	00.8	47.0	01.6	45.9	02.3	45.9	02.4		03.2	45.8	04.0	45.8	04.5	46
47 48	48.0	00.8	48.0	01.7	47.9		47.9					04.1	47.8	04.7	47
49	49.0	1		01.7	48.9							04.3	48.8	04.8	49
50	50.0			01.7	49.9		49.9					04.4	49.8	04.9	50
		Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	10
Dift.	1 89	Deg.		Deg.		Point.		Deg.		Deg.		Deg.	711	oint.	1
Busin	-	OR STATE OF	L. HISTORY	B. STREET, STR	-	-	-	THE OWNER OF THE OWNER,	-		-	-	-	-	-

		(of L	АΓΙ	rup	E an	d D	EPAI	RTUF					5
Dift	1 Deg.	2 D	eg.	¿Po	int.	3 I	Jeg.	4.	Dez.	51	Deg.	1 Pc	int.	5 Ditt.
7	Lat. Dep.	L.it.	Dip.	Lit.	Dep.	Lut.	Dep.	Lat	Dip	Lat	D.p	Lat.	Dep.	8
51	51.0:00.9		8.10	50.9	2.5	50.9	02.7	50.9	036	50.8	04.4	50.8	050	51
52	52.0 00.9	52.0	8.10	51.9	02.6	51.9	02.7	51.9	3.6	51.8	4.5	51.7	05.1	52
53	53.0 00.9		8.10	52.9	02.6	52.9	02.8	52.9	03.7	52.8	04.6	52.7	05.2	53
54	54.0 00.9		01.9	53.9	02.7	53.9	C2.8	53.9	3.8	53.8	04 7	53.7	05.3	54
55	55.0 01.0	55.0	01.9	54 9	2.7	54.9	02.8	54.9	03.8	54.8	C4.8	54.7	05.4	55
56	56.0 01.0	56.0	02.0	55.9	02.7	55.9	C2.9	55.9	03.9	55.8	04.9	55.7	05.5	56
57	57.0 01.0		02.0	56.9	02.8	56.9	03.0	56.9	C4.C	56.8	05.0	56.7	05.6	57
58	58.0 01.0		02.0	57.9	02.8	57.9	03.0	57.9	04.0	57.8	05.1	57.7	05.7	58
59	59.0 01.0		02.1	58.9	02.9	58.9	03.1	58.9	04.1	58.8	05.1	58.7	05.8	59
60	60.0 01.1	- mounts	C2.1	59.9	2.9	59.9	03.1	59.9	C4.2	59.8	05-2	59.7	05.9	60
61	61.0 01.1		02.1	60.9	03.0	60.9	03.2	60.9	04.3	60.8	05.3	60.7	06.0	61
62	62.0 01.1		02.2	61.9	03.0	61.9	03.2	61.9	C4.3	61.8	05.4	61.7	06.1	62
63	63.0 01.1		02.2	62.9	03.1	62.9	03.3	62.8	04.4	62.8	05.5	62.7	c6.2	63
64	64.0 01.1		02.3	63.9	03.1	63.9	03.3	63.8	04.5	63.8	05.6	63.7	06.3	64
65	65.0 01.1	1	02.3	64.9	03.2	64.9	03.4	64.8	04.5	64.8	05.7	64.7	c6.4	65
66	66.0 01.2		02.3	65.9	03.2	65.9	03.5	65.8	04.6	65.7	05.8	65.7	c6.5	66
67	67.0 01.2		02.3	66.9	03.3	66.9	03.5	66.8	04.7	66.7	05.8	66.7	c6.6	67
68	68.0 01.2		02.4	67.9	03.3	67.9	03.6	67.8	04.7	67.7	05.9	67.7	06.7	68 69
69	70.0 01.2		02.4	68.9	03.4	68.9	03.6	68.8		68.7	06.0	68.7	o6.8	
70		·		HONOUS.	03.4		03.7	69.8	04.9	69.7		69.7	-	70
71	71.0 01.2	71.0	02.5	70.9	03.5	70.9	03.7	70.8	05.0	70.7	06.2	70.7	07.0	71
72	72.0 01.3	72.0	C2.5	71.9	03.5	71.9		71.8	05.0	71.7	06.3	71.7	07.1	72
73	73.0 01.3		02.5	72.9	03.6	72.9	03.8	72.8	05.1	72.7	6.4	72.6	07.2	73
74	74.0 01.3	74.0	02.6	73.9	03.6	73.9	03.9	73.8	05.2	73.7	06.5	73.6	07.3	74
75	75.0 C1.3	75.0		74.9	03.7	74.9	03.9	74.8	05.2	7.4.7	06.5	74.6	c7.3	75
76	76.0 01.3		02.7	75.9	03.7	75.9	04.0	75.8	05.3	75.7	06.6	75.6	07.4	76
77 78	77.0 01.3	77.0	02.7	76.9	03.8	76.9	04.0	76.8	05.4	76.7	06.7	76.6	07.5	77 78
70	79.0 01.4	-9.0	02.8	77·9 78.9	03.9	77.9	04.1	78.8	05.4	77·7 78-7	06.9	77.6	07.7	70
79	80.0 01.4		02.8	79.9	03.9	79.9	04.2	79.8	05.6	79.7	07.0	79.6	07.8	79 80
81	81.0 01.4		.2.8	80.9		80.9		80.8	-	80.7		80.6	07.9	81
82	82.0 01.4		02.9	81.9	04.0	81.9	04.2	81.8	05.7	81.7	07.1	31.6	08.0	82
83	83.0 01.5		02.9	82.9	04.1	82.9	04.3	82.8	05.8	82.7	07.2	32.6	08.1	83
84	84.0 01.5	83.9	02.9	83.9	04.1	83.9	04.4	83.8	05.0	83.7	07.3	83.6	c8.2	84
85	85.0 01.5	84.9	03.0	84.9	04.2	84.9	04.4	84.8	05.9	84.7	07.4	84.6	08.3	85
86	86.0 01.5	85.9	03.0	85.9	04.2	85.9	04.5	85.8	66.0	85.7	07.5	35.6	08.4	86
87	87.0 01.9		03.0	86.9	04.3	86.9	04.6	16.8	66.1	86.7	07.6	86.6	08.5	87
88	88.0 01.9		03.1	87.9	04.3	87.9	04.6	87.8	c6.1	87.7	07.7	87.6	08.6	88
89	89.0 01.6		23.1	88.9	04.4	88.9	04.7	83.8	c6.2	88.7	07.8	88.6	08.7	89
90	90.0 01.6		03.1	89.9	04.4	89.9	04.7	89.8	06.3	89.7	07.8	19.6	08.8	90
191	91.0 01.6	90.9	03.2	90.9	04.5	90.9	04.8	90.8	6.4	90.7	07.9	90.6	08.0	91
92	92.0 01.6		03.2	91.9	0.4.5	91.9	04.8	91.8	c6.4	91.6	118.0	91.6	09.0	92
93	93.0 01.6		03.2	92.9	04.6	92.9	049	92.8	c6.5	92.6	1.80	2.6	09.1	93
94	94.0 01.6	93.9	03.3	93.9	04.6	93.9	04.9	93.8	c6.6	93.6	08.2	93.5	09.2	94
95	95.0 01.7	94.9	03.3	94.9	04.7	94.9	05.0	94.8	06.6	94.6	58.3	94.5	09.3	95
96	96.0 01.7	95.9	03.4	95.9	04.7	95.9	05.0	95.8	106.7	95 8	c8.4	95.5	09.4	96
97	97.0 01.7		03.4	96.9	04.8	96.0	05.1	6.8	06.8	96.6	08.5	90.5	79.5	97
98	98.0 01.7		73.4	97.9	04.8	97.9	05.1	97.8	06.8	197.6	08.5	97.5	19.6	98
99	99.0 01.7		03.5	98.9	04.9	98.9	05.2	98.8		98.6	c8.6	98.5	9.7	99
100	100.0 01.7	99.9	03.5	99.9	04.9	99.9	05.2	99.8	07.0		08.7	99.5	c9.8	100
Dift	Dep. Lat.	Det.	Lat.	Do	1 at.	Dep	lat.	Dep	Lest.	Dip.	17.	Dep	1,41	Diff
7	89 Deg.	88 1	Deg.	7 1	oint.	87	Dig.	86	Deg.	1 85.	1).	17:1	omt.	13
Street, Square,	-	-	-	-	STATE OF THE PERSON.	STREET, SQUARE,	STATE OF THE PARTY.	THE PERSON NAMED IN	MANAGE AND	MATORIA PROPERTY.	SALA SER	- GEORGE	-	STATE OF THE PARTY.

S. Carrie	6	PROPERTY	-	o minerada	product .	AT	ABL	E of	Ďī	FFE	ENC	E				
3-	UI	6 L	eg.	7 L	eg.	8 1	eg.	3 Po	int.	91	Deg.	10 I	eg.	II	Deg.	C
1	Dift.	Lat.	Dip.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	ift.
Ĭ	-1	01.0	00.1	01.0	00.1	01.0	00.1	01.0	00.1	01.0	00.2	01.0	00.2	01.0	00.2	1
ı	2	02.0	00.2	02.0	00.2	02.0	00.3	02.0	00.3	02.0	00.3	02.0	00.3	02.0	00.4	2
H	3	03.0	00.3	03-0	00.4	03.0	00.4	03.0	00.4	03.0	00.5	03.0	00.5	02.9	00.6	3
ı	4	04.0	00.4	04.0	00.5	04.0	00.6	04.0	00.6	03.9	00.6	03.9	00.7	03.9	00.8	4
H	.5	05.0	00.5	05.0	00.6	05.0	00.7	04.9	00.7	04.9	00.8	04.9	00.9	04.9	01.0	_5
No.	6	06.0	00.6	06.0	00.7	05.9	00.8	05.9	00.9	05.9	00.9	05.9	01.0	05.9	01.1	6
Ħ	7 8	07.0	00.7	c6.9	00.9	06.9	01.0	06.9	01.0	06.9	01.1	06.9	01.2	06.9	01.3	7 8
3		c8.o	00.8	07.9	01.0	07.9	01.1	07.9	01.2	07.9	01.3	07.9	01.4	07.9	01.5	
1	9	08.9	00.9	08.9	01.1	08.9	01.2	08.9	01.3	08.9	01.4		01.6		01.7	9
н	10	09.9	01.0	09.9	01.2	09.9	01.4	09.9	01.5	09.9		09.8	01.7	09.8	01.9	10
1	II	10.9	01.1	10.9	01.3	10.9	01.5	10.9	01.6	10.9	01.7	10.8	01.9	10.8	02.1	II
Н	12	11.9	01.3	11.9	01.5	11.9	01.7	11.9	01.8	11.9	01.9	11.8	02.1	11.8	02.3	12
ı	13	12.9	01.4	12.9	01.6	12.9	01.8	12.9	01.9	13.8	02.0	13.8	02.3	13.7	02.5	13
-	14	13.9	01.5	13.9	01.7	13.9	01.9	14.8	02.1	14.8	02.3	14.8	02.6	14.7	02.9	14 15
1	15	14.9		14.9			_	15.8		15.8	02.5	15.8	02.8	15.7	03.1	16
740	16	15.9	01.7	15.9	01.9	15.8	02.2	16.8	02.3	16.8	02.5	16.7	03.0	16.7	03.2	
-	17	16.9	01.0	17.9	02.1	17.8	02.4	17.8	02.6	17.8	02.8	17.7	03.1	17.7	03.4	17 18
100	19	18.9	02.0	18.9	02.3	18.8	02.6	18.8	02.8	18.8	03.0	18.7	03.3	18.6	03.6	19
200	20	19.9	02.1	19.8	02.4	19.8	02.8	19.8	02.0	19.8	03.1	19.7	03.5	19.6	03.8	20
-	21	20.0	02.2	20.8	02.6	20.8	02.0	20.8	03.1	20.7	03.3	20.7	03.6	20.6	04.0	21
ě	22	21.9	02.3	21.8	02.7	21.8	03.1	21.8	03.2	21.7	03.4	21.7	03.8	21.6	04.2	22
ı	23	22.9	02.4	22.8	02.8	22.8	03.2	22.8	03.4	22.7	03.6	22.6	04.0	22.6	04.4	23
1	24	23.9	02.5	23.8	02.9	23.8	03.3	23.7	03.5	23.7	03.8	23.6	04.2	23.6	04.6	24
ı	25	24.9	02.6	24.8	03.0	24.8	03.5	24.7	03.7	24.7	03.9	24.6	04.3	24.5	04.8	25
ı	26	25.9	02.7	25.8	03.2	25.7	03.6	25.7	c3.8	25.7	04.1	25.6	04.5	25.5	05.0	26
ŧ		26.9	02.8	26.8	03.3	26.7	03.8	26.7	04.0	26.7	04.2	26.6	04.7	26.5	05.2	27
ı	27 28	27.8	02.9	27.8	03.4	27.7	03.9	27.7	04.1	27.7	04.4	27.6	04.9	27.5	05.3	28
ı	29	28.8	03.0	28.8	03.5	28.7	04.0	28.7	04.3	28.6	04.5	28.6	05.0	28.5	05.5	29
ı	30	29.8	03.1	29.8	03.7	29.7	04.2	29.7	04.4	29.6	04.7	29.5	05.2	29.4	05.7	30
1	31	30.8	03.2	30.8	03.8	30.7	04.3	30.7	04.5	30.6	04.9	30.5	05.4	30.4	05.9	31
	32	31.8	03.3	31.8	03.9	31.7	04.5	31.7	04.7	31.6	05.1	31.5	05.6	31.4	06.1	32 .
Į,	33	32.8	03.4	32.8	04.0	32.7	04.6	32.6	04.8	32.6	05.2	32.5	05-7	32.4	06.3	33
ı	34	33.8	03.6	33.7	04.1	33.7	04.7	33.6	05.0	33.6	05.4	33.5	05.9	33.4	06.5	34
ı	35	34.8	03.7	34.7	04.3	34.7	04.9	34.6	05.1	34.6	05.5	<u>34·5</u>	06.1	34.4	06.7	35
I	36	35.8	03.8	35.7	04.4	35.6	05.0	35.6	05.3	35.6	05.6	35.4	06.2	35.3	06.9	36
1	37 38	36.8	03.9	36.7	04.5	36.6	05.1	36.6	05.4	36.5	05.8	36.4	06.6	36.3	07.1	37 38
-		37.8 38.8	04.0	37.7	04.6	37.6 38.6	05.3	37.6 38.6	05.0	37.5	06.1	37·4 38·4	06.8	37·3 38·3	07.4	39
ı	39 40	39.8	04.1	39.7	04.9	39.6	05.6	39.6	05.9	39.5	06.3	39.4	06.9	39.3	07.6	39 40
		40.8	04.3		05.0	40.6	05.7	40.6	06.0	40.5	06.4	40.4	07.1	40.2	07.8	41
B	41 42	41.8	04.4	40.7	05.1	41.6	05.8	41.5	06.2	41.5	06.6	41.4	07.3	41.2	08.c	42
1	43	42.8	04.5	42.7	05.2	42.6	06.0	42.5	06.3	42.5	06.7	42.3	07.5	42.2	08.2	43
1	44	43.8	04.6		05.4	43.6	06.1	43.5	06.5	43.5	06.9	43.3	07.6	43.2	08.4	44
ı	45	44.8	04.7	44.7	05.5	44.6	06.3	44.5	06.6	44.4	07.0	44.3	07.8	44.2	08.6	45
1	46	45.7	04.8	45.7	05.6	45.6	06.4	45.5	06.7	45.4	07.2	45.3	08.0	45.2	68.8	46
1	47	46.7	04.9	46.6	05.7	46.5	06.6	46.5	06.9	46.4	07.3	46.3	08.2	46.1	09.0	47
I	48	47.7	05.0	47.6	05.9	47.5	06.7	47.5	07.0	47-4	07.5	47.3	08.3	47.1	09.2	47 48
ı	49	48.7	05.1	48.6	06.0	48.5	06.8	48.5	07.2	48.4	07.7	48.3	08.5	48.1	09.3	49
ı	50	49.7	05.2	49.6	06.1	49.5	07.0	49.5	07.3	49.4	07.8	49.2	08.7	49.1	09.5	50
ı	Dift	Dep.	Lot.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dop.	Lat.	Dep.	Lat.	Dep.	Lat.	Ü
1	u.	84	Deg.	831	eg.	82	Deg.	7. F	oint.	81	Deg.	80.	Deg.	79	Deg.	.A.
5	-	THE REAL PROPERTY.	TRUE W	THE OWNER OF THE OWNER,	STATE OF THE PARTY OF		-	OR RESERVE	-	Name of Street,	COLUMN TWO	-	-	ALC: UNKNOWN	STATE OF THE PERSON.	_

	_	_		Of	LA:	TITU	DE .	and	DEP	ART	URE.			-	7
D	1 6	Deg.	7	Deg.	8.	Deg.	1 3 P	oint.	9	Deg.	10	Deg.	1 11	Deg.	D.A.
7	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	1 Dip.	Lat.	Dip.	Lit.	Dip	7
51	50.7	05.3	50.6	06.2	50.5	07.1	50.4	07.5	50.4	08.0	50.2	08.9	50.1	09.7	51
52	51.7	05.4	51.6	06 3	51.5	07.2	51.4	07.6	51.4	08.1	51.2	09.0	51.0	09.9	52
53	52.7	05.5	52.6	06.5	52.5	07.4	52.4	07.8	52.3	8.3	52.2	09.2	52.0	10.1	53
54	53.7	05.6	53.6	06.6	53.5	07.5	53.4	07.9	53.3	08.4	53.2	09.4	53.0	10.3	54
55	54.7	05.7	54.6	06.7	54.5	97.7	54.4	08.1	54.3	08.6	54.2	09.5	54.0	10.5	55
56	55.7	05.9	55.6	06.8	55.5	07.8	55.4	08.2	55.3	08.8	55.1	09.7	55.0	10.7	56
57	56.7	06.0	56.6	06.9	56.4	07.9	56.4	08.4	56.3	08.9	56.1	09.9	56.0	10.9	57
58	57.7	06.1	57.6 58.6	07.1	57·4 58.4	08.2	57.4	08.5	57.3	09.1	57.1	10.1	56.9	11.1	58
59 60	59.7	06.3	59.5	07.3	59.4	08.4	58.4 59.4	08.8	58.3 59.3	09.2	58.1	10.2	57·9 58.9	11.3	59
61	60.7	06.4	60.5	07.4	60.4	08.5	60.3	08.9	60.2		59.1	10.6		11.6	61
62	61.7	06.5	61.5	07.6	61.4	08.6	61.3	09.1	61.2	09.5	61.1	10.8	59.9	11.8	62
63	62.7	06.6	62.5	07.7	62.4	08.8	62.3	09.1	62.2	09.9	62.0	10.0	61.8	12.0	63
64	63.6	06.7	63.5	07.8	63.4	08.9	63.3	09.4	63.2	10.0	63.0	11.1	62.8	12.2	64
65	64.6	06.8	64.5	07.9	64.4	09.0	64.3	09.5	64.2	10.2	64.0	11.3	63.8	12.4	65
66	65.6	06.9	65.5	08.0	65.4	09.2	65.3	09.7	65.2	10.3	65.0	11.5	64.8	126	66
67	66.6	07.0	66.5	08.2	66.3	09.3	66.3	09.8	66.2	10.5	66.0	11.6	65.8	12.8	67
68	67.6	07.1	67.5	08.3	67.3	09.5	67.3	10.0	67.2	10.6	67.0	8.11	66.7	13.0	68
69	68.6	07.2	68.5	08.4	68.3	09.6	68.3	1.01	68.2	10.8	68.0	12.0	67.7	13.2	69
70	69.6	07.3	69.5	08.5	69.3	09.7	69.2	10.3	69.1	10.9	68.9	12.2	68.7	13.4	70
71	70.6	07.4	70.5	08.7	70.3	09.9	70.2	10.4	70.1	11.1	69.9	12.3	64.7	13.5	71
72	71.6	07.5	71.5	08.8	71.3	10.0	71.2	10.6	71.1	11.3	70.9	12.5	70.7	13.7	72
73	72.6	07.6	72.5	08.9	72.3	10.2	72.2	10.7	72.1	11.4	71.9	12.7	71.7	13.9	73
74	73.6	07.7	73.4	09.0	73.3	10.3	73.2	10.9	73.1	11.6	72.9	12.8	72.6	14.1	74
7.5	74.6	07.8	74.4	09.1	74.3	10.4	74.2	11.0	74-1	11.7	73.9	13.0	73.6	14-3	75
76	75.6	07.9	75.4	09.3	75.3	10.6	75.2	11.1	75.1	11.9	74-8	13.2	74.6	14.5	76
77	76.6 77.6	08.1	76.4	09.4	76.3	10.7	76.2	11.3	76.1	12.0	75.8	13.4	75.6	14.7	77 78
70	78.6	08.3	77.4	09.5	77.2	11.0	77.2 78.1	11.4	77.0	12.2	76.8 77.8	13.5	76.6 77.5	14.9	70
79 80	79.6	08.4	79.4	09.8	79.2	11.1	79.1	11.7	79.0	12.5	78.8	13.7	78.5	15.3	79 80
81	80.6	08.5	80.4	09.9	80.2	11.3	80.1	11.9	80.0	12.7	70.8	14.1	79.5	15.5	81
82	81.5	08.6	81.4	10.0	81.2	11.4	81.1	12.0	0.18	12.8	79.8 80.8	14.1	80.5	15.6	82
83	82.5	08.7	82.4	10.1	82.2	11.6	82.1	12.2	82.0	13.0	81.7	14.4	81.5	15.8	83
84	83.5	08.8	83.4	10.2	83.2	11.7	83.1	12.3	83.0	13.1	82.7	14.6	82.5	16.0	84
85	84.5	08.9	84.4	10.4	84.2	11.8	84.1	12.5	84.0	13.3	83.7	14.8	83.4	16.2	85
86	85.5	09.0	85.4	10.5	85.2	12.0	85.1	12.6	84.9	13.4	84.7	14.9	84.4	16 4	86
87	86.5	09.1	86.3	10.t	86.2	12.1	86.0	12.8	85.9	13.6	85.7	15.1	85.4	16.6	87
88	87.5	09.2	87.3	10.7	87.1	12.2	87.0	12.9	86.9	13.8	86.7	15.3	86.4	16.8	88
89	88.5	09.3	88.3	3.01	88.1	12.4	88.0	13.1	87.9	13.9	87.6	15.4	87.4	17.0	89
90	89.5	09.4	89.3	11.0	89.1	12.5	89.0	13.2	88.9	14.1	88.6	15.6	88.3	17.2	20
91	90.5	09.5	90.3	11.1	90.1	12.7	90.0	13.3	89.9	14.2	89.6	15.8	89.3	17.4	91
92	91.5	09.6	91.3	11.2	91.1	12.8	0.10	13.5	90.9	14.4	90.6	16.0	90.3	17.6	92
93	93.5	09.7	93.3	11.3	92.1	12.9	92.0	13.6	91.9	14.5	91.6	16.1	91.3	17.7	93
95	94.5	09.9	94.3	11.6	94.1	13.2	94.0	13.0	92.8	14.7	93.6	16.3	92.3	18.1	94
96	95.5	10.0	95.3	11.7	95.1	13.4	95.0	14.1	94.8	15.0		16.7	93.3	18.3	96
97	96.5	10.1	96.3	11.8	96.1	13.5	95.0	14.1	95.8	15.2	94·5 95·5	16.8	94.2	18.5	97
98	97.5	10.2	97.3	11.9	97.0	13.6	96.9	14.4	96.8	15.3	96.5	17.0	90.2	13.7	98
99	98.5	10.3	98.3	12.1	98.0	13.8	97.9	14.5	07.8	15.5	97.5	17.2	97.2	18.9	99
100	99.4	10.4	99.2	12.2	99.0	13.9	98.9	14.7	98.8	15.6	98.5	17.4	98.2	19.1	100
Dift	Dep	Lat.	Dif	Lat.	Dep.	Lat.	Dep.	Lat	Dep.	Lat.	Dep.	Lat.	Dep.	Late	Dift
7	84 1	Ocg.	83 1	Deg.	82 1	Deg.	7 t P	omt.	81 I	Deg.	80 I	Deg.	79 1	Jeg.	7
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$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	4	-		-	-	AT	ABL	E of	DI	FFER	ENC	Е				
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1 01.0 00.2 01.0 00.2 01.0 00.2 01.0 00.2 01.0 00.3 01.0 00.3 1 2 2 2 2 00.6 02.0 00.6 02.0 00.6 02.0 00.6 02.0 00.6 02.0 00.6 02.0 00.8 03.9 00.6 02.0 00.8 03.9 00.6 02.0 00.8 03.9 00.6 02.0 00.8 03.9 00.6 02.0 00.8 03.9 00.6 02.0 00.8 03.9 00.6 02.0 00.8 03.9 00.6 02.0 00.8 03.9 00.6 02.0 00.8 03.9 00.6 02.0 00.8 03.9 00.6 02.0 00.8 03.8 01.1 02.0 00.8 03.8 01.1 02.0 00.8 03.8 01.1 02.0 00.8 03.8 01.1 02.0 00.8 03.8 01.1 02.0 00.8 03.8 01.1 02.0 00.8 03.8 01.1 02.0 00.8 03.8 01.1 02.0 00.8 03.8 03.1 02.0	ii.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.									5
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4	2	02.0	00.4	02.0	00.4	01.9		01.9	00.5	01.9	00.5	01.9	00.5	01.9		2
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$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	17		03.3	16.6	03.5	16.6	03.8	16.5	04.1	16.5	04.1	16.4	04.4	16.3	04.7	17
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$\begin{array}{cccccccccccccccccccccccccccccccccccc$	_	30.4	06.0	-	06.4	30.2	07.0					29.9		29.8	08.5	
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$\begin{array}{cccccccccccccccccccccccccccccccccccc$														34.6		
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	37															37
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U Dep. Lat. Dep Lat. Dep. Lat.						47.7	4							47.1		
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	Ø1	1 Po	int.	121.	eg.	13 L	eg.	14 I	eg.	1 1 Pc	int.	15 1	Deg.	16 1	Deg.	9
	Din.	Lat.	Dep.	Lat.	Des.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lut.	Dep	5
3	51	50.0	10.0	49.9	10.6	49-7	11.5	49.5	12.3	49.5	12.4	49.3	13.2	49.C	14.1	51
	52	51.0	10.1	50.9	10.8	50.7	11.7	50.5	12.6	50.4	12.6	50.2	13.5	50.C	14.3	52
	53	52.0	10.3	51.8	0.11	51.6	11.9	51.4	12.8	51.4	12.9	51.2	13.7	50.9	14.6	53
	54	53.0	10.5	52.8	11.2	52.6	12.1	52.4	13.1	52.4	13.1	52.2	14.0	51.9	14.9	54
	55	53.9	10.7	53.8	11.4	53.6	12.4	53.4	13.3	533	13.4	53.1	14.2	52.9	15.2	55
	56	54.9	10.9	54.8	11.6	54.6	12.6	54.3	13.5	54.3	13.6	54.1	14.5	53.8	15.4	56
	57	55.9	11.1	55.8	8.11	55.5	12.8	55.3	13.8	55.3	13.9	55.1	14.8	54.8	15.7	57
	58	56.9	11.3	56.7	12.1	56.5	13.0	56.3	14.0	56.3	14.1	56.0	15.0	55.8	16.0	50
	59	57.9	11.5	57·7 58.7	12.3	57·5 58.5	13.3	57.2	14.3	57.2	14.3	57.0	15.3	56.7	16.3	59 60
	50	58.8	11.7		12.5		13.5	58.2	14.5	58.2	14.6	58.0	15.5	57.7	16.5	_
	61	59.8	11.9	59.7	12.7	59.4	13.7	59.2	14.8	59.2	14.8	58.9	15.8	58.6	16.8	61
	52	60.8	12.1	60.6	12.9	60.4	13.9	60.2	15.0	60.1	15.1	59.9	16.0	59.6	17.1	
	63	61.8	12.3	61.6	13.1	61.4	14.2	61.1	15.2	61.1	15.3	60.9	16.3	61.5	17.4	64
	64	62.8	12.5	62.6	13.3	62.4	14.4	62.1	15.5	63.0	15.8	61.8	16.8	62.5	17.6	65
		-	12.7		13.5	63.3	14.6		15.7				-		18.2	66
	66	64.7	12.9	64.6	13.7	64.3	14.8	65.0	16.0	64.0	16.0	63.7	17.1	63.4	18.5	67
	63	65.7	13.1	65.5	13.9	65.3	15.1	66.0	16.4	66.0	16.3	64.7	17.3	64.4	18.7	68
	69	67.7	13.3	66.5	14.1	67.2	15.3	66.9	16.7	66.9	16.8	65.7	17.6	66.3	19.0	69
	70	68.7	13.7	68.5	14.6	68.2	15.7	67.9	16.9	67.9	17.0	67.6	18.1	67.3	19.3	70
		69.6			14.8	69.2	16.0	68.9		68.9		68.6	18.4	68.2	19.6	71
	71	70.6	13.9	70.4	15.0	70.2	16.2	69.9	17.2	69.8	17-3	69.5	18.6	69.2	19.8	72
	72	71.6	14.0	71.4	15.2	71.1	16.4	70.8	17.7	70.8	17.5	70.5	18.9	70.2	20.1	73
	73	72.6	14.4	72.4	15.4	72.1	16.6	71.8	17.9	71.8	18.0	71.5	19.2	71.1	20.4	74
	75	73.6	14.6	73.4	15.6	73.1	16.9	72.8	18.1	72.7	18.2	72.4	19.4	72.1	20.7	75
	/3 76		14.8	74-3	15.8	74.1	17.1	_	18.4	73.7	18.5	73.4	19.7	73.1	20.9	76
		74.5	15.0	75-3	16.0	75.0	17.3	73.7	18.6	74.7	18.7	74.4	19.9	74.0	21.2	77
п	77 78	76.5	15.2	76.3	16.2	76.0		75.7	18.9	75.7	18.9	75.3	20.2	75.0	21.5	78
		77-5	15.4	77.3	16.4	77.0	17.5	76.7	19.1	76.6	19.2		20.4	75.9	21.8	79
ш	79 80	78.5	15.6	78.2	16.6	78.0	18.0	77.6	19.4	77.6	19.4	77.3	20.7	76.9	22.0	79 80
	81	79.4	15.8	79.2	16.8	78.9	18.2	78.6	19.6	78.6	19.7	78.2	21.0	·	22.3	81
	82	80.4	16.0	80.2	17.0	79.9	18.4		19.8	79.5	19.9	79.2	21.2	77·9 78.8	22.6	82
	83	81.4	16.2	81.2	17.3	80.9	18.7	79.6	20.1	80.5	20.2		21.5	79.8	22.9	83
ш	84	82.4	16.4	82.2	17.5	81.8	18.9	81.5	20.3	81.5	20.4	81.1	21.7	80.7	23.1	84
п	85	83.4	16.6	83.1	17.7	82.8	19.1	82.5	20.6	82.4	20.7	82.1	22.0	81.7	23.4	85
	86	84.3	16.8	84.1	17.9	83.8	19.3	83.4	20.8	83.4	20.9	83.1	22.3	82.7	23.7	86
	87	85.3	17.0	85.1	18.1	84.8	19.6	84.4	21.0	84.4	21.1	84.0	22.5	83.6	24.0	87
	88	86.3	17.2	86.1	18.3	85.7	19.8	85.4	21.3	85.4	21.4	85.0	22.8	84.6	24.3	88
1	89	87.3	17.4	87.1	18.5	86.7	20.0	86.4	21.5	86.3	21.6	86.0	23.0	85.6	24.5	89
	90	88.3	17.6	88.0	18.7	87.7	20.2	87.3	21.8	87.3	21.9	86.9	23.3	86.5	24.8	90
	91	89.3	17.8	89.0	18.9	88.7	20.5	88.3	22.0	88.3	22.1	87.9	23.5	87.5	25.1	91
	92	90.2	17.9		19.1	89.6	20.7	89.3	22.3		22.4	88.9	23.8	88.4	25.4	92
	93	91.2		91.0	19.3	90.6	20.9	90.2	22.5	90.2	22.6	89.8	24.1	89.4	25.6	93
	94	92.2			19.5	91.6	21.1	91.2	22.7	91.2	22.8	90.8	24.3	90.4	25.9	94
1	95	93.2		92.9	19.7	92.6	21.4	92.2	23.0	92.1	23.1	91.8	24.6	91.3	26.2	95
1	96	94.2	18.7	93.9	20.0	93.5	21.6	93.1	23.2	93.1	23.3	92.7	24.8	92.3	26.5	96
	97	95.1	18.9	94.9	20.2	94.5	21.8	94.1	23.5	94.1	23.6	93.7	25.1	93.2	26.7	97 98
1	98	96.1	19.1	95.9	20.4	95.5	22.0	95.1	23.7	95.1	23.8	94.7	25.4	94.2	27.0	
	99	97.1	19.3		20.6	96.5	22.3	96.1	23.9			95.6		95.2	27.3	99
1	00	98.1	19.5		20.8	97.4	22.5	97.0	24.2		24.3			96.1	27.6	100
1	Dift	Det.	Lat	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Det	Lat.	Dep.	Tat.	Dep.	Lat	Diff
	7	7 1	oint.	78	Deg.	77	Deg.	76	Deg.	1 91	Point.	1 75	Deg.	1 74	Deg.	1 7
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10			4		A T	ABL	E of	Dı	FFE	RENC	E*				
Dift.	11	Point.	17	Deg.	18.	Deg.	19.	Deg.	13 1	oint.	20	Deg.	21	Deg.	TO
F.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Dift.
1	01.0	00.3	01.0	00.3	01.0	00.3	00.9	00.3	00.9	00.3	00.9	00.3	00.9	00.4	I
2	01.9	00.6	01.9	00.6	01.9	00.6	01.9	00.7	01.9	00.7	01.9	00.7	01.9	00.7	2
3	02.9	00.9	02.9	00.9	02.9	00.9	02.8	01.0	02.8	01.0	02.8	01.0	02.8	01.1	3
4	03.8	01.2	03.8	01.2	03.8	01.2	03.8	01.3	03.8	01.3	03.8	01.4	03.7	01.4	4
_5	04.8	01.5	04.8	01.5	04.8	01.5	04.7	01.6	04.7	01.7	04.7	01.7	04.7	01.8	5
6	05.7	01.7	05.7	8.10	05.7 06.7	01.9	05.7	02.0	05.6	02.0	05.6	02.1	05.6	02.1	6
7 8	07.7	02.0	07.6	02.0	07.6	02.2	07.6	02.3	07.5	02.4	07.5	02.4	06.5	02.5	8
9	08.6	02.6	08.6	02.6	08.6	02.8	08.5	02.9	08.5	03.0	08.5	03.1	08.4	03.2	9
10	09.6	02.9	09.6	02.9	09.5	03.1	09.5	03.3	09.4	03.4	09.4	03.4	09.3	03.6	10
11	10.5	03.2	10.5	03.2	10.5	03.4	10.4	03.6	10.4	03.7	10.3	03.8	10.3	03.9	II
12	11.5	03.5	11.5	03.5	11.4	03.7	11.3	03.9	11.3	04.0	11.3	04.1	11.2	04.3	12
13	12.4	03.8	12.4	03.8	12.4	04.0	12.3	04.2	12.2	04.4	12.2	04.4	12.1	04.7	13
14	13.4	04.1	13.4	04.1	13.3	04.3	13.2	04.6	13.2	04.7	13.2	04.8	13.1	05.0	14
15	14.4	04.4	14.3	04.4	14.3	04.6	14.2	04.9	14.1	05.1	14.1	05.1	14.0	05.4	15
16	15.3	04.6	15.3	04.7	15.2	04.9	15.1	05.2	15.1	05.4	15.0	05.5	14.9	05.7	16
17	16.3	04.9	16.3	05.0	16.2	05.3	16.1	05.5	16.0	05.7	16.0	05.8	15.9	06.1	17
	17.2	05.2	17.2	05.3	17.1	05.6	17.0	05.9	16.9	06.1	16.9	06.2	16.8	06.4	18
19	19.1	05.8	19.1	05.8	19.0	06.2	18.9	06.5	18.8	06.7	18.8	06.8	18.7	07.2	19
21	20.1	06.1	20.1	06.1	20.0	06.5	19.9	06.8	19.8	07.1	19.7	07.2	19.6	07.5	21
22	21.1	06.4	21.0	06.4	20.9	06.8	20.8	07.2	20.7	07.4	20.7	07.5	20.5	07.9	22
23	22.0	06.7	22.0	06.7	21.0	07.1	21.7	07.5	21.7	07.7	21.6	07.9	21.5	08.2	23
24	23.0	07.0	22.9	07.0	22.8	07.4	22.7	07.8	22.6	08.1	22.6	08.2	22.4	08.6	24
25	23.9	07.3	23.9	07.3	23.8	07.7	23.6	08.1	23.5	08.4	23.5	08.5	23.3	09.0	25
26	24.9	07.5	24.9	07.6	24.7	08.0	24.6	08.5	24.5	08.8	24.4	08.9	24.3	09.3	26
27	25.8	07.8	25.8	07.9	25.7	08.3	25.5	08.8	25.4	09.1	25.4	09.2	25.2	09.7	27
28	26.8	08.1	26.8	08.2	26.6	08.7	26.5	09.1	26.4	09.4	26.3	09.6	26.1	10.0	28
29	27.8	08.4	27.7	08.5	27.6	09.0	27.4	09.4	27.3	09.8	27.3	09.9	27.1	10.4	29
30	28.7	08.7	28.7	08.8	28.5	09.3	28.4	09.8	28.2	10.1	28.2	10.3	28.0	10.8	30
31	29.7 30.6	09.0	29.6	09.1	29.5	09.6	29.3	10.1	29.2	10.4	29.1	10.6	28.9	11.1	31
32 33	31.6	09.3	30.6	09.4	30.4	10.0	30.3	10.4	30.1	11.1	30.1	10.9	29.9 30.8	11.5	32
34	32.5	09.9	32.5	09.9	32.3	10.5	32.1	11.1	32.0	11.5	31.9	11.6	31.7	12.2	33 34
35	33.5	10.2	33.5	10.2	33.3	10.8	33.1	11.4	33.0	8.11	32.9	12.0	32.7	12.5	35
36	34.4	10.4	34.4	10.5	34.2	11.1	34.0	11.7	33.9	12.1	33.8	12.3	33.6	12.9	36
	35.4	10.7	35.4	10.8	35.2	11.2	35.0	12.0	34.8	12.5	34.8	12.7	34.5	13.3	
37 38	36.4	11.0	36.3	11.1	36.1	11.7	35.9	12.4	35.8	12.8	35.7	13.0	35.5	13.6	37 38
39	37.3	11.3	37.3	11.4	37.1	12.0	36.9	12.7	36.7	13.1	36.6	13.3	36.4	14.0	39
40	38.3	11.6	38.3	11.7	38.0	12.4	37.8	13.0	37.7	13.5	37.6	13.7	37.3	14.3	40
41	39.2	11.9	39.2	12.0	39.0	12.7	38.8	13.3	38.6	13.8	38.5	14.0	38.3	14.7	41
42	40.2	12.2	40.2	12.3	39.9	13.0	39.7	13.7	39.5	14.1	39-5	14-4	39.2	15.1	42
43 44	42.1	12.5	41.I 42.I	12.0	40.9	13.3	40.7	14.0	40.5	14.5	40.4	14.7	40.1	15.4	43
45	43.I	13.1	43.0	13.1	42.8	13.9	42.5	14.7	42.4	15.2	42.3	15.4	42.0	16.1	44
46	44.0	13.4	44.0	13.4	43.7	14.2	43.5	15.0	43.3	15.5	43.2	15.7	42.9	16.5	#3 46
47	45.0	13.6	44.9	13.7	44.7	14.5	44.4	15.3	44.2	15.8	44.2	16.1	43.9	16.8	47
48	45.9	13.9	45.9	14.0	45.7	14.8	45.4	15.6	45.2	16.2	45.1	16.4	44.8	17.2	48
49	46.9	14.2	46.9	14.3	46.6	15.1	46.3	16.0	46.1	16.5	46.0	16.8	45.7	17.6	49
50	47.8	14.5	47.8	14.6	47.6	15.4	47.3	16.3	47-1	16.8	47.0	17.1	46.7	17.9	50
Dift.	Dep.	Lat.	Dep	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dift.
7	61 P	oint.	73 L	eg.	72 L	eg.	71 L	eg.	6 P	oint.	70 L	eg.	69 L	eg.	₹
															- 6

				Of:	LAT	TITU	DE .	and	DEP	ART	URE.				11
D	1 1 P	oint.	17	Deg.	18	Deg.	19	Deg.	13 P	oint.	20	Deg.	1 21	Deg.	Dift.
₹.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dop.	Lat.	Dep	7
51	48.8	14.8	48.8	14.9	48.5	15.8	48.2	16.6	48.0	17.2	47.9	17.4	47.6	18.3	51
52	49.7	15.1	49.7	15.2	49.4	16.1	49.2	16.9	49.0	17.5	48.9	17.8	48.5	18.6	52
53	50.7	15.3	50.7	15.5	50.4	16.4	50.1	17.3	49.9	17.9	49.8	18.1	49.5	19.0	53
54	51.7	15.7	51.6	15.8	51.3	16.7	51.0	17.6	50.8	18.2	50-7	18.5	50.4	19.4	54
55	52.6	16.0	52.6	16.1	52.3	17.0	52.0	17.9	51.8	18.5	51.7	18.8	51.3	19.7	55
56	53.6	16.2	53-5	16.4	53.3	17.3	52.9	18.2	52.7	18.9	52.6	19.2	52.3	20.1	56
57 58	54-5	16.5	54.5	16.7	54.2	17.6	53.9	18.6	53.7	19.2	53.6	19.5	53.2	20.4	57 58
58	55.5	16.8	55.5	17.0	55.2	17.9	54.8	18.9	54.6	19.5	54-5	19.8	54.1	20.8	58
59 60	56.5	17.1	56.4	17.3	56.1	18.5	55.8	19.2	55.5 56.5	19.9	55.4 56.4	20.2	55.1 56.0	21.1	59
61	57.4	17.4	57.4	17.5	57-1	18.8	_	19.5			_			-	
62	58.4	17.7	58.3	17.8	58.0		57.7	19.9	57.4	20.6	57.3	20.9	56.9	21.9	61
63	59.3	18.3	59·3 60.2	18.4	59.0	19.2	58.6	20.2	58.4	20.9	58.3	21.2	57·9 58·8	22.6	63
64	61.2	18.6	61.2	18.7	60.9	19.5	60.5	20.8	60.3	21.6	60.1	21.0	59.7	22.9	64
65	62.2	18.9	62.2	19.0	61.8	20.1	61.5	21.2	61.2	21.9	61.1	22.2	60.7	23.3	65
66	63.2	19.2	63.1	19.3	62.8	20.4	62.4	21.5	62.1	22.2	62.0	22.6	61.6	23.7	66
67	64.1	19.4	64.1	19.5	63.7	20.7	63.3	21.8	63.1	22.6	63.0	22.9	62.6	24.0	60
68	65.1	19.7	65.0	19.9	64.7	21.0	64.3	22.1	64.0	22.9	63.9	23.3	63.5	24.4	67
69	66.0	20.0	66.0	20.2	65.6	21.3	65.2	22.5	65.0	23.2	64.8	23.6	64.4	24.7	69
70	67.0	20.3	66.9	20.5	66.6	21.6	66.2	22.8	65.9	23.6	65.8	23.9	65.4	25.1	70
71	67.9	20.6	67.0	20.8	67.5	21.9	67.1	23.1	66.8	23.9	66.7	24.3	66.3	25-4	71
72	68.9	20.9	68.8	21.1	68.5	22.2	68.1	23.4	67.8	24.3	67.7	24.6	67.2	25.8	72
73	69.9	21.2	69.8	21.3	69.4	22.6	69.0	23.8	68.7	24.6	68.6	25.0	68.2	26.2	73
74	70.8	21.5	70.8	21.6	70.4	22.9	70.0	24.1	69.7	24.9	69.5	25.3	69.1	26.5	74
75	71.8	21.8	71.7	21.9	71.3	23.2	70.9	24.4	70.6	25.3	70.5	25.6	70.0	26.9	75
76	72.7	22.I	72.7	22.2	72.3	23.5	71.9	24.7	71.6	25.6	71.4	26.0	71.0	27.2	76
	73-7	22.4	73.6	22.5	73.2	23.8	72.8	25.1	72.5	25.9	72.4	26.3	71.9	27.6	77
77	74.6	22.6	74.6	22.8	74-2	24.1	73.7	25.4	73.4	26.3	73.3	26.7	72.8	28.0	77
79 80	75.6	22.9	75.5	23.1	75.1	24.4	74.7	25.7	74.4	26.6	74.2	27.0	73.8	28.3	79 80
	76.6	23.2	76.5	23.4	76.1	24.7	75.6	26.0	75.3	27.0	75.2	27.4	74.7	28.7	
81	77.5 78.5	23.5	77.5	23.7	77.0	25.0	76.6	26.4	76.3	27.3	76.1	27.7	75.6	29.0	81
82	78.5	23.8	78.4	24.0	78.0	25.3	77.5	26.7	77.2	27.6	77.1	28.0	76.6	29.4	82
83	79·4 80.4	24.1	79.4	24.3	78.9	25.6	78.5	27.0	78.1	28.0	78.0	28.4	77.5	29.7	83
84	80.4	24.4	86.3	24-5	79.9	26.0	79.4	27.3	79.1 80.0	28.3	78.9	28.7	78.4	30.1	84
85	81.3	24.7	81.3	24.8	80.8	26.3	80.4	27.7		28.6	79.9	29.1	79.4	30.5	85
86	82.3	25.0	82.2	25.1	81.8	26.6	81.3	28.0	81.0	29.0	80.8	29.4	80.3	30.8	86
87	83.3	25.3	83.2	25.4	82.7	26.9	82.3	28.3	81.9	29.3	81.8	29.8	81.2	31.2	8 ₇ 88
89	84.2	25.5	84.2	25.7 26.0	83.7	27.2	83.2 84.1	28.7	82.9	29.6	82.7	30.1	82.2	31.5	89
90	85.2	25.8	85.1 86.1	26.3	84.6 85.6	27.5 27.8	85.1	29.0	83.8	30.3	83.6 84.6	30.4	84.0	32.3	90
-	_	_							04.7						
91	87.1	26.4	87.0 88.0	26.6 26.9	86.5 87.5	28.1	86.0 87.0	29.6	85.7 86.6	30.7	85.5 86.5	31.1	85.0 85.9	32 6	91
93	89.0	20.7	88.9	27.2	88.4	28.7	87.9	30.3	87.6	31.3	87.4	31.5	86.8	33.3	93
93	90.0	27.3	89.9		89.4	29.0	88.9	30.6	88.5	31.7	88.3	32.1	87.8	33.7	94
95	90.0	27.6	90.8	27.5 27.8	90.4	29.4	89.8	30.9	89.4	32.0	89.3	32.5	88.7	34.0	95
96	91.9	27.9	91.8	28.1	91.3	29.7	90.8	31.3	90.4	32.3	90.2	32.8	89.6	34.4	96
97	92.8	28.2	92.8	28.4	92.3	30.0	91.7	31.6	91.3	32.7	91.1	33.2	90.6	34.8	
98	93.8	28.4	93.7	28.7	93.2	30.3	92.7	31.9	92.3	33.0	92.1	33.5	91.5	35.1	97 98
99	94.7	28.7	94.7	28.9	94.2	30.6	93.6	32.2	93.2	33.4	93.0	33.9	92.4	35.5	99
100	95.7	29.0	95.6	29.2	95.1	30.9	94-5	32.6	94.2	33.7	94.0	34.2	93.4	35.8	100
Dift	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lot	Dep.	Lat.	Dep	Lat.	Dep.	Lat.	Dia
if.	61 P	oint.	73	Deg.	72	Deg.	711	Jeg.	6; P	oint.	70 I	Ocg.	69 I	Deg.	3
_	_	-		-	_		_		_	-		-	_	-	-

12						A T	ABL	E of	Dr	FFER	ENC	E				
7	7 2	2 D	eg.	2 Po	ints	23 I	eg.	24 I	eg.	25 I		2 Po		26 I		יות.
DIII.	L	at.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	
			00.4	00.9	00.4	00.9	00.4	00.9	00.4	00.9	00.4	00:0	00.4	00.9	00.4	1
			00.7	01.8	00.8	01.8	00.8	01.8	00.8	01.8	00.8	01.8	00.9	01.8	00.9	2
	_		01.1	02.8	01.5	03.7	01.6	03.6	01.6	03.6	01.7	03.6	01.7	03.6	01.8	3 4
			01.9	04.6	01.9	04.6	02.0	04.6	02.0	04.5	02.1	04.5	02.1	04.5	02.2	5
			02.2	05.5	02.3	05.5	02.3	05.5	02.4	05.4	02.5	05:4	02.6	05.4	02.6	6
			02.6	06.5	02.7	06.4	02.7	06.4	02.8	06.3	03.0	06.3	03.0	06.3	03.1	
			03.0	07.4	03.1	07.4	03.1	07.3	03.2	07.2	03.4	07.2	03.4	07.2	03.5	7 8
			03.4	08.3	03.4	08.3	03.5	08.2	03.7	08.2	03.8	08.1	03.8	08.1	03.9	9
1		9.3	03.7	09.2	03.8	09.2	03.9	09.1	04. I	09.1	04.2	09.0	04.3	09.0	04.4	10
1		0.2	04.1	10.2	04.2	10.1	04.3	10.0	04.5	10.0	04.6	09.9	04-7	10.8	04.8	II
I		1.1	04.5	11.1	04.6	11.0	04.7	11.0	04.9	10.9	05.1	10.8	05.1	11.7	05.3	12
I		3.0	04.9	12.0	05.0	12.9	05.5	12.8	05.7	12.7	05.9	12.7	06.0	12.6	06.1	14
ī		3.9	05.6	13.9	05.7	13.8	05.9	13.7	06.1	13.6	06.3	13.6	06.4	13.5	06.6	15
1		4.8	06.0	14.8	06.1	14.7	06.2	14.6	06.5	14.5	06.8	14.5	06.8	14.4	06.0	16
1		5.8	06.4	15.7	06.5	15.6	06.6	15.5	06.9	15.4	07.2	15.4	07.3	15.3	07.5	17
1		6.7	06.7	16.6	06.9	16.6	07.0	16.4	07.3	16.3	07.6	16.3	07.7	16.2	07.9	18
1		7:6	07.1	17.6	07.3	17.5	07.4	17.4	07.7	17.2	08.0	17.2	08.1	17.1	08.3	19
2	0 1	8.5	07.5	18.5	07.7	18.4	07.8	18.3	08.1	18.1	08.5	18.1	08.6	18.0	08.8	20
		9.5	07.9	19.4	08.0	19.3	08.2	19.2	08.5	19.0	08.9	19.0	09.0	18.9	09.2	21
	_	0.4	08.2	20.3	08.4	20.3	08.6	20.1	08.9	19.9	09.3	19.9	09.4	19.8	09.6	22
		1.3	08.6	21.2	08.8	2I.2 22.I	09.0	21.0	09.4	20.8	10.1	21.7	10.3	20.7	10.5	23
		2·3 3·2	09.0	23.1	09.2		09.8	22.8	10.2	22.7	10.6	22.6	10.7	22.5	11.0	25
		4.1	09.7	24.0	09.9	-	10.2	23.8	10.6	23.6	11.0	23.5	II.I	23.4	11.4	26
		5.0	10.1	24.9	10.2		10.5	24.7	11.0	24.5	11.4	24.4	11.5	24.3	11.8	27
		6.0	10.5		10.7		10.9	25.6	11.4	25.4	11.8	25.3	12.0	25.2	12.3	28
		6.9	10.9	26.8	11.1		11.3	26.5	11.8	26.3	12.3	26.2	12.4	26.1	12.7	29
3	0 2	7.8	11.2	1	11.5		11.7	27.4	12.2	27.2	12.7	27.1	12.8	27.0	13.2	30
		8.7	11.6		11.9		12.1	28.3	12.6	28.1	13.1	28.0	13.3	27.9	13.6	31
		9.7	12.0	1 /			12.5	29.2	13.0		13.5	28.9	13.7	28.8	14.0	32
		0.6	12.4		12.0		12.9	30.1	13.4	30.8	13.9	30.7	14.1	30.6	14.5	33
		2.5	13.1					32.0	14.2	31.7	14.8	31.6	15.1	31.5	15.3	35
	7 -	3.4	13.5				14.1	32.9	14.6	32.6	15.2	32.5	15.4	32.4	15.8	36
		3.4	13.0				14.4		15.0		15.6	33.4	15.8	33.3	16.2	37
1		5.2	14.2						15.5		16.1	34.3	16.2	34.2	16.7	38
	39 3	6.2	14.6	36.0	14.9	35.9	15.2	35.6	15.9		16.5	35.3	16.7	35.1	17.1	39
		7.1	15.0	37.0				100	16.3	-	16.9		17.1	36.0	17.5	40
		8.0	15-4		15.7	37.7	16.0		16.7	37.2	17.3		17.5	35.8	18.0	41
		8.9	15.7						17.1	38.1	17.7	38.0	18.0	37.7	18.4	42
		9.9	16.1						17.5		1 0 0	39.8	18.8	39.5	19.3	43
		11.7	16.0						18.3				19.2	40.4	19.7	45.
		2.7	17.2						-		19.4	41.6	19.7	41.3	20.2	46
		3.6	17.6										20.1	42.2	20.6	47
		4.5	18.0					43.8	19.5					43.1	21.0	48
8 -	19 4	5.4	18.4	45.3	18.8	45.1	19.2	44.8	19.9				20.9	44.0		49
		6.4	18.7	- 1					20.3			45.2			21.9	50
1	Dia	Dep.	Lat.	Dep.	Lat.	-		Dep.	Lat.	Dep.	Dog.	Dep.	Point.	Dep.	Deg.	Diff
1		68	Deg.	101	oints	1 07	Deg.	1 00	Deg.	65	Deg.	1 53	OHIL.	1 04	Deg.	1

			Of 1.	ATI	TUD	E an	d D	EPAR	RTUF					13 Uiit.
0	22 Deg.	1 2 Po	ints	231	eg.	24 1.	eg.	25 L	eg.	21 Pc	int.	26]		Ę.
Dift.	Lat. D.p.	Lat.	Dep.	Lat.	Dep.	Lat.	Dp.	Lat_	Dep	Lat.	usp.	Last.	Dep	
51	47.3 19.1	47.1	19.5	46.9	19.9	46.6	20.7	46.2	21.6	46.1	21.8	45.8	22.4	51
52	48.2 19.5	48.0	19.9	47.9	20.3	47.5	21.1	47.1	22.0	47.0	22.2	46.7	22.8	52
53	49:1 19.9	19.0	20.3	48.8	20.7	48.4	21.6	48.0	22.4	47.9	22.7	48.5	23.2	53 54
54	50.1 20.2	49.9	20.7	49.7	21.1	49.3	22.0	48.9	23.2	49.7	23.5	49 4	24.1	559
55	51.0 20.6	50.8	21.0	50.6	21.5				-	50.6	23.9	50.3	24.5	56
56	51.9 21.0 52.8 21.4	51.7	21.4	51.5	21.9	51.2 52.1	22.8	50.8	23.7	51.5	24.4	51.2	25.0	57
57 58	52.8 21.4	52.7	22.2	52.5	22.7	53.0	23.6	52.6	24.5	52.4	24.8	52.1	25.4	58
59	54.7 22.1	54.5	22.6	54.3	23.1	53.9	24.0	53.5	24.9	53.3	25.2	53.0	25.9	59
60	55.6 22.5	55.4	23.0	55.2	23.4	54.8	24.4	54.4	25.4	5412	25.7	53.9	26.3	60
61	56.5 22.8	56.4	23.3	56.1	23.8	55.7	24.8	55.3	25.8	55.1	26.1	54.8	26.7	61
62	57.5 23.2	57.3	23.7	57.1	24.2	56.6	25.2	56.2	26.2	56.0	26.5	55.7	27.2	62
63	58.4 23.6	58.2	24.1	58.0	24.6	57.5	25.6	57.1	26.6	57.0	26.9	56.6	27.6	63
64	59.3 24.0	59.1	24.5	58.9	25.0	58.5	26.0	58.0	27.0	57.9	27.4	57.5	28.0	64
65	60.3 24.3	60.1	24.9	59.8	25.4	59-4	26.4	58.9	27.5	58.8	27.8	58.4	28.5	65
66	61.2 24.7	61.0	25.3	60.8	25.8	60.3	26.8	59.8	27.9	59.7	28.2	59.3	28.9	66 6-
67	62.1 25.1	61.9	25.6	61.7	26.2	61.2	27.2	60.7	28.3	60.6	20.0	60.2	29.4	68
68	63.0 25.5	62.8	26.0	62.6	26.6	62.1	27.7 28.1	61.6	28.7	62.4	29.5	62.0	30.2	69
69	64.0 25.8	63.7	26.4	63.5	27.0	63.9	28.5	63.4	29.6	63.3	29.9	62.9	30.7	70
70	64.9 26.2	64.7	-		27.7	64.9	28.9	64.3	30.0	64.2	30.4	63.8	31.1	71
71	65.8 26.6	66.5	27.2	65.4	28.1	65.8	29.3	65.2	30.4	65.1	30.8	64.7	31.6	72
72	66.8 27.0	67.4	27.9	67.2	28.5	66.7	29.7	66.2	30.8	66.0	31.2	65.6	32.0	73
73 74	68.6 27.7	68.4	28.3	68.1	28.9	67.6	30.1	67.1	31.3	66.9	31.6	66.5	32.4	74
75	69.5 28.1	69.3	28.7	69.0	29.3	68.5	30.5	68.0	31.7	67.8	32.1	67.4	32.9	75
76	70.5 28.5		29.1	70.0	29.7	69.4	30.9	68.9	32.1	68.7	32.5	68.3	33-3	76
77	71.4 28.8		29.5	70.9	30.1	70.3	31.3	69.8	32.5	69.6	32.9	69.2	33.8	77
78	72.3 29.2		29.8	71.8	30.5	71.3	31.7	70.7	33.0	70.5	33.3	70.1	34.2	78
79	73.2 29.6	73.0	30.2	72.7	30.9	72.2	32.1	71.6	33.4	71.4	33.8	71.0	34.6	79 85
80	74.2 30.0		30.6	73.6	31.3	73.1	32.5	72.5	33.8	72.3	34.2	71.9	35.1	
81	75.1 30.3		31.0	74.6	31.6	74.0	32.9	73-4	34.2	73.2	34.6	72.8	3 5 ·5	81
82	76.0 30.7	75.8	31.4	75.5	32.0	74.9	33.3	74.3	34.7	74-1	35.1	73.7	35.9	83
83		76.7	31.8	76.4	32.4	75.8	33.7	75.2 76.1	35.1 35.5	75.0	35·5 35·9	74.6 75.5	36.4 36.8	84
84	77.9 31.5		32.1	77.3	32.8	77.6	34.1	77.0	35.9	76.8	36.3	76.4	37.3	85
	1	-		_	33.2	78.6		77.9	36.3	77.7	36.8	77.3	37.7	86
86 87	79.7 32.2		32.9	79.2	33.6	79.5	35.c 35.4	78.8	36.8	78.6	37.2	78.2	38.1	87
88	81.6 33.0		33.7	81.0	34.4	80.4	35.8	79.8	37.2	79.6	37.6	79.1	38.6	88
89			34.1	81.9	34.8	81.3	36.2	80.7	37.6	80.5	38.1	80.0	39.0	89
90		' ^	34.4	82.8	35.2	82.2	36.6	81.6	38.0	81.4	38.5	80.9	39.5	90
91	0		34.8	83.8	35.6	83.1	37.0	82.5	38.5	82.3	38.9	81.8	39.9	91
92		85.0	35.2	84.7	35.9	84.0	37.4	83.4	38.9	83.2	39.3	82.7	10.3	92
93	86.2 34.8	85.9	35.6	85.6	36.3	85.0	37.8	84.3	39.3	84.1	39.8	83.6	40.8	93
94			36.0	86.5	36.7	85.9	38.2	85.2	39.7	85.0	40.2	84.5	41.2	94
95			36.4	87-4	37.1	86.8	38.6	86.1	40.1	85.9	40.6	85.4	41.6	95
95	89.0 36.0		36.7	88.3	37.5	87.7	39.0	87.0	40.6	86.8	41.0	86.3	42.1	96
97	89.9 36.			89.3	37.9	88.6	39.4	87.9 88.8	41.0	87.7	41.9	87.2	42.5	97 98
98				90.2	38.4	89.5	39.9	89.7	41.4	89.5	42.3	89.0	43.4	99
1.99				91.1	39.1	91.4	40.7	90.6	42.3	90.4	42.8	89.9	43.8	100
100	92.7 37.5	Det.	Lat.	Dep.	Lat.	Dep.	Lat.	Den.	Lat.	Der.	Lot.	Dep	Lat	
Diff	68 Deg.		oints		Deg.		Deg.	-	Deg.		oint.		Deg.	Dist.
1	1 00 17-6.			-	- 6	-	- 0		-			_		_

14					A T	ABL	E of	Dı	FFEI	RENC	E				
U	27 I	Deg.	28 I	Deg.	2 1 P	oint.	29 I	Deg.	30]	Deg.	23 P	oint.	31	Deg.	Dift.
æ.	Lat.	Dep.	Lat:	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dip.	Lat.	Dep.	Lat.	Dep.	7
I	00.9	00.5	00.9	00.5	00.9	00.5	00.9	00.5	00.9	00.5	00.9	00.5	00.9	00.5	1
2	01.8	00.9	01.8	00.9	01.8	00.9	01.7	01.0	01.7	01.0	01.7	01.0	01.7	01.0	2
3	02.7	01.4	02.6	01.4	02.6	01.4	02.6	01.5	02.6	01.5	02.6	01.5	02.6	01.5	3
4	03.6	01.8	03.5	01.9	03.5	01.9	03.5	01.9	03.5	02.0	03.4	02.1	03.4	02.1	4
_3	04.5	02.3	04.4	02.3	04.4	02.4	04.4	02.4	04.3	02.5	04.3	02.6	04.3	02.6	5
6	05.3	02.7	05.3	02.8	05.3	02.8	05.2	02.9	05.2	03.0	05.1	03.1	05.1	.03.1	6
* 7	06.2	03.2	06.2	03.3	06.2	03.3	06.1	03.4	06.1	03.5	06.0	03.6	06.0	03.6	7 8
	07.1	03.6	07.1	03.8	07.1	03.8	07.0	03.9	06.9	04.0	06.9	04.1	06.9	04.1	1 18
9	08.0	04.1	07.9	04.2	07.9	04.2	07.9	04.4	07.8	04.5	07.7	04.6	07.7	04.6	9
10	08.9	04.5	08.8	04.7		04.7		04.8		05.0		05.1		05.1	10
II	09.8	05.0	09.7	05.2	09.7	05.2	09.6	05.3	09.5	05.5	09.4	05.7	09.4	05.7	11
12	10.7	05.4	10.6	05.6	10.6	05.7	10.5	05.8	10.4	06.0	10.3	06.2	10.3	06.2	12
13	11.6	05.9	11.5	06.1	11.5	06.1	11.4	06.3	11.3	06.5	11.1	07.2	11.1	06.7	13
:14	12.5	06.4	12.4	06.6	13.2	07.1			13.0		12.9	07.7	12.0	07.2	14
15	13.4		13.2	07.0			13.1	07.3	_	07.5		08.2		07.7	15
16	14.3	07.3	14.1	07.5	14.1	07.5	14.0	07.8	13.9	08.0	13.7		13.7	08.8	16
17 18	15.1	07.7	15.0	08.0	15.0	08.0	14.9	08.7	14.7		14.6	08.7	14.6		17
19	16.0	08.2	15.9	08.5	16.8	08.5	15.7	09.2	16.5	09.0	16.3	09.3	16.3	09.3	10
20	17.8	09.1	17.7	09.4	17.6	09.4	17.5	09.7	17.3	10.0	17.2	10.3	17.1	10.3	20
21	18.7			-	18.5		18.4	10.2	18.2	10.5	18.0	10.8	18.0	10.8	
22	/.	09.5	18.5	09.9	19.4	10.4	19.2	10.2	19.1	11.0	18.9	11.3	18.9	11.3	21
23	19.6	10.0	20.3	10.3	20.3	10.8	20.1	11.1	19.9	11.5	19.7	11.8	19.7	11.8	23
24	21.4	10.4	21.2	11.3	21.2	11.3	21.0	11.6	20.8	12.0	20.6	12.3	20.6	12.3	24
25	22.3	11.3	22.1	11.7	22.0	11.8	21.9	12.1	21.6	12.5	21.4	12.0	21.4	12.9	25
26	23.2	11.8	23.0	12.2	22.9	12.3	22.7	12.6	22.5	13.0	22.3	13.4	22.3	13.4	26
27	24.I	12.3	23.8	12.7	23.8	12.7	23.6	13.1	23.4	13.5	23.2	13.9	23.1	13.9	27
28	24.9	12.7	24.7	13.1	24.7	13.2	24.5	13.6	24.2	14.0	24.0	14.4	24.0	14.4	28
20	25.8	13.2	25.6	13.6	25.6	13.7	25.4	14.1	25.1	14.5	24.9	14.9	24.9	14.9	20
30	26.7	13.6	26.5	14.1	26.5	14.1	26.2	14.5	26.0	15.0	25.7	15.4	25.7	15.4	30
31	27.6	14.1	27.4	14.6	27.3	14.6	27.1	15.0	26.8	15.5	26.6	15.9	26.6	16.0	31
32	28.5	14.5	28.3	15.0	28.2	15.1	28.0	15.5	27.7	16.0	27.4	16.4	27.4	16.5	32
.33	29.4	15.0	29.1	15.5	29.1	15.6	28.9	16.0	28.6	16.5	28.3	17.0	28.3	17.0	33
34	30.3	15.4	30.0	16.0	30.0	16.0	29.7	16.5	29.4	17.0	29.2	17.5	29.1	17.5	34
35	31.2	15.9	30.9	16.4	30.9	16.5	30.6	17.0	30.3	17.5	30:0	18.0	30.0	18.0	35
36	32.1	16.3	31.8	16.9	31.7	17.0	31.5	17.5	31.2	18.0	30.9	18.5	30.9	18.5	36
27	33.0	16.8	32.7	17.4	32.6	17.4	32.4	17.9	32.0	18.5	31.7	19.0	31.7	19.1	
38	33.9	17.3	33.5	17.8	33.5	17.9	33.2	18.4	32.9	19.0	32.6	19.5	32.6	19.6	37 38
39	34.7	17.7	34.4	18.3	34.4	18.4	34.1	18.9	33.8	19.5	33.4	20.0	33.4	20.1	39
40	35.6	18.2	35.3	18.8	35.3	18.9	35.0	19.4	34.6	20.0	34.3	20.6	34.3	20.6	40
41	36.5	18.6	36.2	19.2	36.2	19.3	35.9	19.9	35.5	20.5	35.2	21.1	35.1	21.1	41
42	37.4	19.1	37.1	19.7	37.0	19.8	36.7	20.4	36.4	21.0	36.0	21.6	36.0	21.6	42
43	38.3	19.5	38.0	20.2	37.9	20.3	37.6	20.8	37.2	21.5	36.9	22.1	36.9	22.I	43
44	39.2	20.0	38.8	20.7	38.8	20.7	38.5	21.3	38.1	22.0	37.7	22.6	37.7	22.7	44
45	40.1	20.4	39.7	21.1	39.7	21.2	39.4	21.8	39.0	22.5	38.6	23.1	38.6	23.2	45
46	41.0	20.9	40.6	21.6	40.6	21.7	40.2	22.3	39.8	23.0	39.5	23.6	39.4	23.7	46
47	41.9	21.3	41.5	22.I	41.4	22.2	41.1	22.8	40.7	23.5	40.3	24.2	40.3	24.2	47
48	42.8	21.8	42.4	22.5	42.3	22.6	42.0	23.3	41.6	24.0	41.2	24.7	41.1	24.7	48
49	43.7	22.2	43.3	23.0	43.2	23.1	42.9	23.8	42.4	24.5	42.0	25.2	42.0	25.2	49
50	44.5	22.7	44.1	23.5	44.1	23.6	43.7	24.2	43.3	25.0	42.9	25.7	42.9	25.7	.50
D	Dep.	Lat.	Dirp	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dift
ابن	63 L).eg.	62 1	Jeg,	52 P	oint.	611.	reg.	60 I	Jeg.	5 + P	oint.	59 I	eg,	.41
2													1		

Г				Of	LA	TIT	UDE	and	DE:	PART	TURE				1
-	2 27	D-g.	28	Deg.	21	Point.	1 20	Deg.	30	Deg.	1211	Point,	1 21	Deg.	
1 5	Litt.	Dep.	Lat.	Dep	1,26.	Dep	Lat.	Dip.	Lat.		Lit.	Dep	1 411	IDIP.	- Dim.
5	1 45.4	23.2	45.0	23.0	45.0	24.0			-		-	26.2	-1		3 5
5.	2 46.3	23.6	45.9	24.											
5.			46.8	24.0											
5-	48.1	24.5		25.4	1 47.6	25.	47.2								
5.		25.0	48.6	25.8	48.5	25.9	48.1	26.7	47.6			28.3			3 5
50	49.9	25.4	49.4	26.3	49.4	26.	49.0	27.1	48.5	28.0	48.0	28.8	48.0		
5	50.8			26.8	50.3	26.0						29.3			
58				27.2				28.1	50.2			29.8			
59			1 -	27.7							50.6	30.3		30.2	
60	20 7	27.2	53.0		-			29.1	52.0	30.0	51.5	30.8	51.4	30.0	
61	JULIA		53.9	28.6		28.8	53.3	29.6	52.8	30.5	52.3	31.4	52.	31.4	61
62		28.1	54.7	29.1	54.7	29.2		30.1	53.7	31.0		31.9			
63		28.6	55.6	29.6		29.7		30.5		31.5	54.0	32.4	54.0	32.4	
64		29.1	50.5	30.0		30.2				32.0	54.9	32.9	54.9	33.0	
65		29.5	57.4	30.5		30.6	1	31.5	56.3	32.5	55.7	33.4		33.5	65
66	1 3	30.0	58.3	31.0		31.1	57.7	32.0		33.0	56.6	33.9	56.6	34.0	
67	59.7	30.4	59.2	31.5		31.6		32.5	58.0	33.5	57·5 58·3	34-4			68
60	61.5	30.9	60.0	31.9		32.1	59.5	33.0		34.0		35.0	58.3		
70	62.4	31.3	61.8	. 2.4	60.9	32.5	60.3	33.5	59.8	34.5	59.2	35.5	59.1	35.5	
	-	-		32.9	_	33.0	61.2	33.9	60.6	35.0	60.0	36.0	60.0		
71 72	63.3	32.2	62.7	33.3	62.6	33-5	62.1	34.4	61.5	35.5	60.9	36.5	60.9	36.6	71
7.3	65.0	32.7	63.6	33.8	63.5	33.9	63.0	34.9	62.4	36.0	61.8	37.0	61.7	37.2	
74	65.9	33.6	65.3	34.3	65.3	34.4	63.8	35.4	63.2	36.5	62.6	37.5	62.6	37.6	
75	66.8	34.1	66.2	34·7 35·2	66.1	34·9 35·4	64.7	35.9	64.1	37.0	63.5	38.0	63.4	38.1	74
76	67.7	34.5	67.1		67.0		66.5	-	64.9	37.5	64.3	38.6	64.3	38.6	75
77	68.6	35.0	68.0	35·7 36.2	67.9	35.8 36.3		36.8	65.8	38.0	65.2	39.1	65.1	39.1	76
78	69.5	35.4	68.9	36.6	68.8	36.8	67.3	37·3 37·8	66.7	38.5	66.0	39.6	66.0	39.7	77
	70.4	35.9	69.7	37.1	69.7	37.2	69.1	38.3	67.5	39.0	67.8	40.1	66.9	40.2	70
79 80	71.3	36.3	70.6	37.6	70.6	37.7	70.0	38.8	69.3	39.5	68.6	41.1	68.6	40.7	79 80
81	72.2	36.8	71.5	38.0	71.4	38.2	70.8	-	70.1	-					81
82	73.1	37.2	72.4	38.5	72.3	38.7	71.7	39.3	71.0	40.5	69.5	41.6	70.3	41.7	82
83	74.0	37.7	73.3	39.0	73.2	39.1	72.6	40.2	71.9	41.0		42.7	71.1	42.7	83
84	74.8	38.1	74.2	39.4	74.1	39.6	73.5	40.7	72.7	42.0		43.2	72.0	43.3	84
85	75.7	38.6	75.0	39.9	75.0	40.1	74.3	41.2	73.6	42.5		43.7	72.9	43.8	85
86	76.6	39.0	75.9	40.4	75.8	40.5	75.2	41.7	74.5	43.0	_	44.2	73.7	44.3	86
87	77.5	39.5		40 8	76.7	41.0	76.1	42.2	75.3	43.5		44.7	74.6	44.8	87
88	78.4	40.0	77-7	41.3		41.5	77.0	42.7	76.2	44.0		45.2		45.3	88
89	79.3	40.4	78.6	41.8	77.6	42.0	77.8	43.1	77.1					45.8	89
90	80.2	40.9	79.5	42.3	79.4	42.4	78.7	43.6	77.9	45.0				46.3	90
91	81.1	41.3	80.3	42.7	80.3	42.9	79.6	44.1	78.8					46.9	91
92	82.0	41.8		43.2	81.1	43.4	80.5	44.6						47.4	92
93	82.9	42.2		43.7	82.0	43.8	81.3	45.1		46.5	79.8			47.9	93
94	83.8	42.7		44.1	82.9	44.3	82.2	45.6	81.4	47.0				48.4	94
95	84.6	43.1		44.6		44.8		46.1				18.8	81.4	18.9	95
96	85.5	43.6		45.1		45.3		46.5	83.1	48.0	82.3	19.4	82.3	49.4	96
97	86.4		85.6	45.5	85.5	45.7	84.8	47.0		48.5	83.2			50.0	97
-98	87.3			46.0		46.2	85.7		84 91			50.41		50.5	98
100	88.2					46.7		48.0				50.9		51.0	99
	89.1					47.1						51.4		51.5	100
Dift.	Dep		Dep.	Lat.	Dep	L		Lat	Dep.	-	-		-	Lat.	Diff
:-1	63 I	eg.	62 1	eg.	5 2 Pc	int.	01 L	eg.	60 D	leg.	5 Po	int.	59 D	eg.	=
													-	ALC: UNITED BY	-

	16					AT	ABL	E of	Di	FFER	ENC	Е				-	
-	رت	32 1	J.g. 1	33 L	leg.	3 Po	ints	34 1	Deg.	35 1	Jeg.	36 1	Jeg.	3: 1	oint.	U	ĺ
1	5	Lit.	Dep.	Lit.	Dip.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lut.	Dip.	Lat.	Dep.	.÷	İ
	I	8.00	00.9	oc.8,	00.5	8.00	00.6	00.8	00.6	00.8	00.6	00.8	00.6	00.8	00.6		ı
T T	2	01.71	01.1		01.1	01.7	1.10	01.6	01.1	01.6	01.1	01.6	01.2	01.6	01.2	2	ı
i i	3	02.5	01.6		01.6	02.5	01.7	02.5	01.7	02.5	01.7	02.4	01.8	02.4	01.8	3	ı
ă	4	C3.4	02.1		02.2	03.3	02.2	03.3	02,2	03.3	02.3	03.2	02.4	03.2	02.4	4	ı
1 .	5	04.2	02.6	04.2	02.7	04.2	02.8	04.1	02.8	04.1	02.9	04.0	02.9	04.0	03.0	_5	ı
2	6	05.1	03.2	05.0	03.3	05.0	03.3	05.0	03.3	04.9	03.4	04.8	03.5	04.8	03.6	6	ı
1	7 8	05.9	03.7		03.8.	05.8	03.9	05.8	03.9	05.7	04.0	05.7	04.1	05.6	04.2	7 8	ı
		06.8	04.2		04.4	06.6	04.4	06.6	04.5	06.6	04.6	06.5	04.7	06.4	04.8		ı
١.	9	07.6	04.8		04.9	07.5	05.0	07.5	05.0	07.4	05.2	07.3	05.3	07.2	05.4	9	ı
8 -		08.5	05.3	_	05.4	_	05.6	08.3	05.6	08.2	03.7	08.1	05.9	08.0	06.0	10	ı
•	11	09.3	05.8		06.0	09.1	06.1	09.1	06.2	09.0	c6.3	08.9	06.5	08.8	06.6	11	
	2	11.0	06.4		06.5	10.0	06.7	09.9	06.7	09.8	06.9	09.7	07.0	09.6	07.1	12	ı
	13	11.9	07.4	10.9	07.1	11.6	07.2	10.8	07.3	11.5	07.5	11.3	07.6	10.4	07.7	13	ı
	15	12.7	07.9	12.6	08.2	12.5	08.3	12.4	08.3	12.3	08.6	12.1	08.8	12.0	08.9	14	ı
	16	13.6	08.5	13.4	08.7	13.3	08.9	13.3	08.9	13.1	00.2	12.0	09.4	12.0		15	l
	7	14.4	09.0	14.3	09.3	14.1	09.4	14.1	09.5	13.9	09.2	13.8	10.0	13.7	10.1		ı
	8	15.3	09.5	15.1	09.8	15.0	10.0	14.9	10.1	14.7	10.3	14.6	10.6	14.5	10.7	17 18	ı
	19	16.1	10.1	15.9	10.3	15.8	10.6	15.8	10.6	15.6	10.9	15.4	11.2	15.3	11.3	19	ı
	20	17.0	10.6	16.8	10.9	16.6	11.1	16.6	11.2	16.4	11.5	16.2	11.8	16.1	11.9	20	ı
	21	17.8	11.1	17.6	11.4	17.5	11.7	17.4	11.7	17.2	12.0	17.0	12.3	16.9	12.5	21	ı
1	22	18.7	11.7	18.5	12.0	18.3	12.2	18.2	12.3	18.0	12.6	17.8	12.9	17.7	13.1	22	ı
1:	23]	19.5	12.2	19.3	12.5	19.1	12.8	19.1	12.9	18.8	13.2	18.6	13.5	18.5	13.7	23	ı
4 :	24	20.4	12.7	20.1	13.1	20.0	13.3	19.9	13.4	19.7	13.8	19.4	14.1	19.3	14.3	24	ı
1:	25	21.2	13.2	21.0	13.6	20.8	13.9	20.7	14.0	20.5	14.3	20.2	14.7	20.1	14.9	25	
	26	22.0	13.9	21.8	14.2	21.6	14.4	21.6	14.5	21.3	14.9	21.0	15.3	20.9	15.5	26	ı
1	27	22.9	14.3	22.6	14.7	22.4	15.0	22.4	15.1	22.1	15.5	21.8	15.9	21.7	16.1	27	ı
	28	23.7	14.8	23.5	15.2	23.3	15.6	23.2	15.6	22.9	16.1	22.7	16.5	22.5	16.7	28	ı
	29	24.6	15.4	24.3	15.8	24. I	16.1	24.0	16.2	23.8	16.6	23.5	17.0	23.3	17.3	29	ı
	30	25.4	15.9	25.2	16.3	24.9	16.7	24.9	16.8	24.6	17.2	24.3	17.6	24.1	17.9	30	
	31	26.3	16.4	26.0	16.9	25.8	17.2	25.7	17.3	25.4	17.8	25.1	18.2	24.9	18.5	31	ı
	32	27.1	17.0	26.8	17.4	26.6	17.8	26.5	17.9	26.2	18.4	25.9	18.8	25.7	19.1	32	ı
	33	28.8	17.5	27.7	18.0	27.4	18.3	27.4	18.5	27.0	18.9	26.7	19.4	26.5	19.7	33	ı
	34	29.7	18.5	29.4	18.5	28.3	18.9	29.0	19.0	27.9	19.5	27.5	20.6	27.3	20.3	34	į
	35						19.4	1			20.6			28.0		35	ı
	36	30.5	19.1	30.2	19.6	30.8	20.0	29.8	20.1	29.5	21.2	29.1	21.2	29.7	21.4	36	
	37 38	32.2	20.1	31.9	20.7	31.6	21.1	30.7	21.2	31.1	21.8	30.7	22.3	30.5	22.6	37 38	l
	39	33.1	20.7	32.7	21.2	32.4	21.7	32.3	21.8	32.0	22.4	31.6	22.9	31.3	23.2	39	ı
	40	33.9	21.2	33.6	21.8	33-3	22.2	33.2	22.4	32.8	22.9	32.4	23.5	32.1	23.8	40	ı
- 1	41	34.8	21.7	34.4	22.3	34.1	22.8	34.0	22.0	33.6	23.5	33.2	24.1	32.9	24.4	4I	I
	42	35.6	22.3	35.2	22.9	34.9	23.3	34.8	23.5	34.4	24.1	34.0	24.7	33.7	25.0	42	ı
1	43	36.5	22.8	36.1	23.4	35.8	23.9	35.6	24.0	35.2	24.7	34.8	25.3	34.5	25.6	43	ı
-	44	37.3	23.3	36.9	24.0	36.6	24.4	36.5	24.6	36.0	25.2	35.6	25.9	35.3	26.2	44	ı
Total Section	45	38.2	23.8	137.7	24.5	37.4	25.0	37.3	25.2	36.9	25.8	36.4	26.5	36.1	26.8	45	ı
-	46	39.0	24.4	38.6	25.1	38.2	25.5	38.1	25.7	37.7	26.4	37.2	27.0	36.9	27.4	46	ı
1	47	39.9	24.9	39.4	25.6	39.1	26.1	39.0	26.3	38.5	27.0	38.0	27.6	37.7	28.0	47	ı
1	48	40.7	25.4		26.1	39.9	26.7	39.8	26.8	39.3	27.5	38.8	28.2	38.6	28.6	48	ì
1	49	41.6	26 0		26.7	40.7	27.2	40.6	27.4	40. I	28.1	39.6	28.8	39.4	29.2	49	ı
	50	42.4	26.5		27.2	41.6	27.8	41.4	28.0	41.0	28.7	40.4	29.4	40.2	29.8	50	ı
	Dif	Dep.	Lat.	Dep	Lat.	Dep.	Lat.	Dep	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dift.	١
ķ		58	Deg.	57	Deg.	1 5 P	oints	1 50	Deg.	55	Deg.	1 54	Deg.	43 F	oint.	1 7	l

					Of I	ATI	TUD	E di	id D	EPA	RTUI	RE.				17
1	Dift.	32	Deg.	331	Deg.	3 Po	ints	34	Deg.	35 1	Jeg.	36 I	Deg.	31 Pc	oint.	Diff.
ı	7	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dip.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	7
ı	51	43.2	27.0	42.8	27.8	42.4	28.3	42.3	28.5	41.8	29.3	41.3	30.0	41.0	30.4	51
ı	52	44.1	27.6	43.6	28.3	43.2	28.9	43.1	29.1	42.6	29.8	42.1	30.6	41.8	31.0	52
ı	53	44.9	28.1	44.5	28.9	44.1	29.4	43.9	29.6	43.4	30.4	42.9	31.2	42.6	31.6	53
ı	54	45.8	28.6	45.3	29.4	44.9	30.0	44-8	30.2	44.2	31.0	43.7	31.7	43.4	32.2	54
ı	55	46.6	29.1	46.1	30.0	45.7	30.6	45.6	30.8	45.1	31.5	44.5	32.3	44.2	32.8	55
ı	56	47.5	29.7	47.0	30.5	46.6	31.1	46.4	31.3	45.9	32.1	45.3	32.9	45.0	33.4	56
R	57	48.3	30.2	47.8	31.0	47.4	31.7	47.3	31.9	46.7	32.7	46.1	33.5	45.8	34.0	57
	58	49.2	30.7	48.6	31.6	48.2	32.2	48.1	32.4	47.5	33.3	46.9	34.1	46.6	34.5	58
ı	59	50.0	31.3	49.5	32.1	49.1	32.8	48.9	33.0	48.3	33.8	47.7	34-7	47.4	35.1	59
ı	60	50.9	31.8	50.3	32.7	49.9	33.3	49.7	33.6	49.2	34.4	48.5	35.3	48.2	35.7	60
	61	51.7	32.3	51.2	33.2	50.7	33.9	50.6	34.1	50.0	35.0	49.3	35.9	49.0	36.3	61
	62	52.6	32.8	52.0	33.8	51.6	34.4	51.4	34.7	50.8	35.6	50.2	36.4	49.8	36.9	62
ı	63	53.4	33.4	52.8	34.3	52.4	35.0	52.2	35.2	51.6	36.1	51.0	37.0	50.6	37.5	63
	64	54.3	33.9	53.7	34.9	53.2	35.6	53.1	35.8	52.4	36.7	51.8	37.6	51.4	38.1	64
ı	65	55.1	34.4	54.5	35.4	54.0	36.1	53.9	36.3	53.2	37.3	52.6	38.2	52.2	38.7	65
	66	56.0	35.0	55.4	35.9	54.9	36.7	54.7	36.9	54.1	37.9	53.4	38.8	53.0	39.3	66
	67	56.8	35.5	56.2	36.5	55.7	37.2	55.5	37.5	54.9	38.4	54.2	39.4	53.8	39.9	67
	68	57.7	36.0	57.0	37.0	56.5	37.8 38.3	56.4	38.0	55.7	39.0	55.0	40.0	54.6	40.5	
ı	69	58.5	36.6	57.9	37.6	57.4	38.3	57.2	38.6	56.5	39.6	55.8	40.6	55.4	41.1	- 69
	70	59.4	37.1	58.7	38.1	58.2	38.9	58.0	39.1	57.3	40.2	56.6	41.1	56.2	41.7	70
ı	71	60.2	37.6	59.5	38.7	59.0	39.4	58.9	39.7	58.2	40.7	57.4	41.7	57.0	42.3	71
	72	61.1	38.2	60.4	39.2	59.9	40.0	59.7	40.3	59.0	41.3	58.2	42.3	57.8	42.9	72
	73	61.9	38.7	61.2	39.8	60.7	40.6	60.5	40.8	59.8	41.9	59.1	42.9	58.6	43.5	73
ı	74	62.8	39.2	62.1	40.3	61.5	41.1	61.3	41.4	60.6	42.4	59·9 60.7	43.5	59.4	44.I	74
ı	75	63.6	<u>39·7</u>	62.9	40.8	62.4	41.7	62.2	41.9	61.4	43.0		44.1		44.7	75
	76	64.4	40.3	63.7	41.4	63.2	42.2	63.0	42.5	62.3	43.6	61.5	44.7	61.0	45.3	76
ı	77 78	65.3	40.8	64.6	41.9	64.0	42.8	63.8	43.1	63.1	44.2	62.3	45.3	62.6	45.9	77 78
	70	67.0	41.3	65.4	42.5	64.9	43.3	64.7	43.6	63.9	44.7	63.1	45.8	63.5	46.5	70
ı	79	67.8	41.9	66.3	43.0	65.7	43.9	65.5	44.2	64.7	45·3 45·9	63.9		64.3	47.7	79 80
ı	18	68.7	42.4	67.1	43.6		44.4		44.7	65.5			47.0	65.1	48.3	81
ı	82	69.5	42.9	67.9 68.8	44.1	67.4	45.0	67.1	45.3	67.2	46.5	65.5 66.3	47.6 48.2	05.1 65.9	48.8	82
ı	83	70.4	43.4	69.6	44.7	69.0	45.6 46.1	68.8	45.9	68.0	47.0 47.6	67.1	48.8	66.7	49.4	83
H	84	71.2	44.0	70.5	45.2	69.8	46.7	69.6	47.0	68.8	48.2	68.0	49.4	67.5	50.0	84
ı	85	72.1	45.0	71.3	46.3	70.7	47.2	70.5	47.5	69.6	48.8	68.8	50.0	68.3	50.6	85
ı	86	72.9		-	46.8		47.8		48.1			69.6		69.1	51.2	86
ı	87	73.8	45.6	72.1	47.4	71.5	48.3	71.3	48.6	70.5	49.3	70.4	50. 5	69.9	51.8	
1	88	74.6	46.6	73.8	47.9	73.2	48.9	73.0	49.2	72.1	50.5	71.2	51.7	70.7	52.4	87 88
1	89	75.5	47.2	74.6	48.5	74.0	49.4	73.8	49.8	72.9	51.0	72.0	52.3	71.5	53.0	89
1	90	76.3	47.7	75.5	49.0	74.8	50.0	74.6	50.3	73.7	51.6	72.8	52.9	72.3	53.6	90
1	91	77.2	48.2	76.3	49.6	75.7	50.6	75.4	50.9	74.5	52.2	73.6	53.5	73.I	54.2	91
1	92	78.0	48.7	77.2	50.1	76.5	51.1	76.3	51.4	75.4	52.8	74.4	54.1	73.9	54.8	92
1	93	78.9	49.3	78.0	50.6		51.7	77.1	52.0	76.2	53.3	75.2	54.7	74.7	55.4	93
1	94	79.7	49.8	78.8	51.2	77·3 78.2	52.2	77.9	52.6	77.0	53.9	76.0	55.3	75.5	56.0	94
1	95	80.6	50.3	79.7	51.7	79.0	52.8	78.8	53.1	77.8	54.5	76.9	55.8	76.3	56.6	95
	96	81.4	50.9	80.5	52.3		53.3	79.6	53.7	78.6	55.1		56.4	77.1	57.2	96
1	97	82.3		81.4	52.8	79.8	53.9	80.4	54.2	79.5	55.6	77·7 78.5	57.0		57.8	
ı	98	83.1	51.9	82.2	53.4	81.5	54.4	81.2	54.8	80.3	56.2	79.3	57.6	77·9 78.7	58.4	97 98
1	99	84.0	52.5	83.0	53.9	82.3	55.0	82.1	55-4	81.1	56.8	80.1	58.2	79.5	59.0	99
1	100	84.8	53.0	83.9	54.5	83.1	55.6	82.9	55.9	81.9	57.4	80.9	58.8	86.3	59.6	100
1		Dop.	Lat	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Deb	Lat.	Dep.	Tat.	Dep.	Lat.	Diff.
1	Dift	58 1	Jeg.		Deg.	5 P		56 1			Deg.	54	Deg.	43 P	oint.	P
1			(7-	,,	0	-	-		-	,,,	-			_	_	-

1	8				A T	ABL	E of	DII	FER	ENCI	2				
ŀ	ÜI	37 Deg.	38 D	eg.	39 L	eg.	3 P	oint.	40 L	Jeg.	41 I.	Deg.	42 I	eg.	U
L	اجَ	Lat. Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	in.
ľ	I	00.8 00.6	00.8	00.6	00.8	00.6	00.8	00.6	00.8	00.6	00.8	00.7	00.7	00.7	I
ı	2	01.6, 01.2	01.6	01.2	01.6	01.3	01.5	01.3	01.5	01.3	01.5	01.3	01.5	01.3	2
ı	3	02.4 01.8	02.4	01.8	02.3	01.9	02.3	01.9	02.3	01.9	02.3	02.0	02.2	02.0	3
1	4	03.2 02.4	03.2	02.5	03.1	02.5	03.1	02.5	03.1	02.6	03.0	c2.6	03.0	02.7	4
ı	5	04.0 03.0	03.9	03.1	03.9	03.1	03.9	03.2	03.8	03.2	03.8	03.3	03.7	03.3	.5
1	6	04.8 03.6	04.71	03.7	04.7	03.8	04.6	03.8	04.6	03.9	04.5	03.9	04.5	04.0	.6
1	7 8	05.6 04.2	05.5	04.3	05.4	04.4	05.4	04.4	05.4	04.5	05.3	04.6	05.2	04.7	7 8
Ł	8	06.4 04.8	06.3	04.9	06.2	05.0	06.2	05.1	06.1	05.1	06.0	05.2	05.9	05.4	
ı	9	07.2 05.4	07.1	05.5	07.0	05.7	07.0	05.7	06.9	05.8	06.8	05.9	06.7	06.0	9
ı	10	08.0 06.0	07.9	06.2	07.8	06.3	07.7	06.3	07.7	06.4	<u>07.5</u>	06.6	07.4	06.7	10
	ΙI	08.8 06.6	08.7	06.8	08.5	06.9	08.5	07.0	08.4	07.1	08.3	07.2	08.2	07.4	11
	12	09.6 07.2	09.5	07.4	09.3	07.6	09.3	07.6	09.2	07.7	09.1	07.9	08.9	08.0	12
	13	10.4 07.8	10.2	08.0	10.1	08.2	10.8	08.2	10.0	09.0	10.6	09.2	10.4	08.7	13
	14		11.0	08.6	10.9	09.4	11.6	09.5	11.5	09.6	11.3	09.8	11.1	10.0	14
	15		·	09.2	_						12.1	10.5	11.0	1	15
	16	12.8 09.6	12.6	09.9	12.4	10.7	12.4	10.1	12.3	10.3	12.8	11.2	12.6	10.7	16
	17	13.6 10.2	13.4	10.5	13.2	11.3	13.1	11.4	13.8	11.6	13.6	11.8	13.4	12.0	17
- 8	19	15.2 11.4	15.0	11.7	14.8	12.0	14.7	12.1	14.6	12.2	14.3	12.5	14.1	12.7	19
	20	16.0 12.0	15.8	12.3	15.5	12.6	15.5	12.7	15.3	12.9	15.1	13.1	14.9	13.4	20
2	21	16.8 12.6	16.5	12.0	16.3	13.2	16.2	13.3	16.1	13.5	15.8	13.8	15.6	14.0	21
R	22	17.6 13.2	17.3	13.5	17.1	13.8	17.0	14.0	16.9	14.1	16.6	14.4	16.3	14.7	22
- 23	23	18.4 13.8	18.1	14.2	17.9	14.5	17.8	14.6	17.6	14.8	17.4	15.1	17.1	15.4	23
	24	19.2 14.4	18.9	14.8	18.6	15.1	18.6	15.2	18.4	15.4	18.1	15.7	17.8	16.1	24
	25	20.0 15.0	19.7	15.4	19.4	15.7	19.3	15.9	19.1	16.1	18.9	16.4	18.6	16.7	25
	26	20.8 15.6	20.5	16.0	20.2	16.4	20.1	16.5	19.9	16.7	19.6	17.1	19.3	17.4	26
	27	21.6 16.2	21.3	16.6	21.0	17.0	20.9	17.1	20.7	17.4	20.4	17.7	20.1	18.1	27
I	28	22.4 16.8	22.1	17.2	21.8	17.6	21.6	17.8	21.4	18.0	21.1	18.4	20.8	18.7	28
ı	29	23.2 17.5	22.9	17.9	22.5	18.2	22.4	18.4	22.2	18.6	21.9	19.0	21.5	19.4	29
ı	30	24.0 18.1	23.6	18.5	23.3	18.9	23.2	19.0	23.0	19.3	22.6	19.7	22.3	20.1	30
1	31	24.8 18.7	24.4	19.1	24.1	19.5	24.0	19.7	23.7	19.9	23.4	20.3	23.0	20.7	31
١	32	25.6 19.3	25.2	19.7	24.9	20.1	24.7	20.3	24.5	20.6	24.1	21.0	23.8	21.4	32
1	33	26.4 19.9	26.0	20.3	25.6	20.8	25.5	20.9	25.3	21.2	24.9	21.7	24.5	22.1	33
I	34	27.2 20.5	26.8	20.9	26.4	21.4	26.3	21.6	26.0	21.9	25.7	22.3	25.3	22.7	34
-	35	28.0 21.1	27.6	21.5	27.2	22.0	27.1	22.2	26.8	22.5	26.4	23.0	26.0	23.4	35
E	36	28.7 21.7	28.4	22.2	28.0	22.7	27.8	22.8	27.6	23.1	27.2	23.6	26.8	24.1	36
-	37	29.5 22.3	29.2	22.8	28.8	23.3	28.6	23.5	28.3	23.8	27.9	24.3	27.5	24.8	37
Î	38	30.3 22.9	29.9	23.4	29.5	23.9	29.4	24. I	29.1	24.4	28.7	24.9	28.2	25.4	38
1	39	31.1 23.5	30.7	24.0	30.3	24.5	30.1	24.7	29.9	25.1	30.2	25.6	29.0	26.1	39
-	40	31.9 24.1	31.5	24.6	31.1	25.2	30.9	25.4	30.6	25.7	1-				40
1	41	32.7 24.7	32.3	25.2	31.9	25.8	31.7	26.0	31.4	26.4	30.9	26.9	30.5	27.4	41
-	42	33.5 25.3		25.9	32.6	26.4	32.5	26.6	32.2	27.0	31.7	28.2	32.0	28.8	42
1	43	34.3 25.9 35.1 26.5		26.5	33.4	27.1	33.2	27.3	33.7	28.3		28.9	32.7	29.4	43
-	44 45	35.1 26.5 35.9 27.1	34.7	27.1	34.2	27.7	34.8	28.5	34.5	28.9	34.0	29.5	33.4	30.1	44
ı	_			28.3	35.7	28.0	35.6	29.2	35.2	29.6	34-7	30.2	34.2	30.8	46
	46	36.7 27.7 37.5 28.3	36.2	28.9	35.7	29.6	35.0	29.8	36.0	30.2		30.8	34.9	31.4	
1	47 48	38.3, 28.9		29.6	37.3	30.2	37.1	30.5	36.8	30.9	36.2	31.5	35.7	32.1	47
	49	39.1 29.5	38.6	30.2	38.1	30.8	37.9	31.1	37.5	31.5	37.0	32.1	36.4	32.8	49
	50	39.9 30.1	39.4	30.8	38.9	31.5	38.6	31.7	38.3		37.7	32.8	37.2	33.5	50
		Dep. Lat.	Dep	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lat.	10
	Dift.	53 Deg.		Deg.		Deg.		Point.	50	Deg.	49	Deg.	48	Deg.	#
1	-									-	_	-			-

1					Of:	LA	IITU		and	DEP	ART	URE.				19
ı	Dift.	37	Deg.	38	Deg.		Deg.		Point.		Deg.		Deg.	1 42	Deg.	ייים ליווים בייים
ı	7	Lat.	Dep.	Lat.	Dep.	Lat.	Dep.	Lut.	Dip.	Lal.	Dep.	Lat	D.p.	Leit	Up.	=
ı	51	40-7	30.7	40.2	31.4	39.6	32.1	39.4	32.4	39.1	32.8	38.5	1331	17-0	34.1	SI
ł	52	41.5	31.3	41.0	32.0	40.4	32.7	40.2	33.0	39.8	33.4	39.2	134 I	3 .	34.8	57
ı	53	42.3	31.9	41.8	32.6	41.2	33.4	41.0	33.6	40.6	34.1	40.0	13+	14.4	135.5	573
ı	54	43.I	32.5	42-6	33.2	42.0	34.0	41.7	34.3	41.4	34.7	408	35		30 1	5.
ı	55	43.9	33.1	43-3	33.9	42-7	34.6	42.5	34.9	12.1	35.4	41.5	36.1	4		55 1
ı	56	44.7	33.7	44.I	34.5	43.5	35.2	43.3	35.5	42.9	36.0	42.3	36.7	410	37.5	5.51
ı	57 58	45.5	34.3	44.9	35.1	44.3 45.1	35.9	44.8	36.2	43.7	36.6	43.8	37.4	42.4	33.8	31-1
ı	59	47.1	34·9 35·5	45.7	36.3	45.8	37.1	45.6	37-4	45.2	37.9	44.5	38.7	43 8	30.5	51.
ı	60	47.9	36.1	47.3	36.9	46.6	3718	46.4	38.1	46.0	38.6	45.3	39.4	44.6	40.1	50
ı	61	48.7	36.7	48.1	37.6	47.4	38.4	47.2	38.7	46.7	39.2	46.0	40.0	45.3	40.8	61
ı	62	49.5	37.3	48.9	38.2	48.2	39.0	47.9	39.3	47.5	39.9	46.8	40.7	46.1	41.5	60
1	63	50.3	37.9	49.6	38.8	49.0	39.6	48.7	40.0	48.3	40.5	47.5	41.3	46.8	42.2	631
I	64	51.1	38.5	50.4	39.4	49.7	40.3	49.5	40.6	49.0	41.1	48.3	42.0	47.6	42.8	64
ı	65	51.9	39.1	51.2	40.0	50.5	40.9	50.2	41.2	49.8	41.8	49.1	42.6	48.3	43.5	65
1	66	52.7	39.7	52.0	40.6	51.3	41.5	51.0	41.9	50.6	42.4	49.8	43.3	49.0	44.2	66
П	67	53.5	40.3	52.8	41.3	52.1	42.2	51.8	42.5	51.3	43.1	50.6	44.0	49.8	44.8	68
ı	68	54.3	40.9	53.6	41.9	52.8	42.8	52.6	43.1	52.1	43.7	51.3	44.6	50.5	45.5	66
ı	69	55.1	41.5	54.4	42.5	53.6	43.4	53.3	43.8	52.9 53.6	44.4	52.1 52.8	45.9	51.3	46.2	69
ı	70	55.9	42.1	55.2	43.1	54.4	44.7	54.9	45.0		45.6	53.6	46.6	52.8		75
ı	71 72	56.7	42.7	55.9 56.7	43.7	56.0	45.3	55.7	45.7	54.4	46.3	54.3	47.2	53.5	47.5	72
ı	73	57·5 58.3	43.9	57.5	44.9	56.7	45.9	56.4	46.3	55.9	46.9	55.I	47.9	54.2	48.8	73
ı	74	59.1	44.5	58.3	45.6	57.5	46.6	57.2	46.9	56.7	47.6	55.8	48.6	55.0	49.5	74
ı	75	599	45.1	59.1	46.2	58.3	47.2	58.0	47.6	57.5	48.2	56.6	49.2	55.7	50.2	7.5
ı	76	60.7	45.7	59.9	46.8	59.1	47.8	58.7	48.2	58.2	48.9	57.4	49.9	56.5	50.9	76
ı	77	61.5	46.3	60.7	47·4 48.0	59.8	48.5	59.5.	48.8	59.0	49.5	58.1	50.5	57.2	51.5	7.7
H	78	62.3	46.9	61.5		60.6	49.1	60.3	49.5	59.7	50.1	58.9	51.2	58.0		778
ı	79 80	63.1	47.5	62.3	48.6	61.4	49.7	61.1	50.1	60.5	50.8	59.6	51.8	58.7	52-9	79 80
H		63.9	48.1	63.0	49.3	62.2	50.3	61.8	50.8	61.3	51.4	60.4	52.5	59.4	53.5	
ı	81	64.7	48.7	63.8	49.9	62.9	51.0	62.6	51.4	62.0	52.1	61.1	53.1	60.2	54.2	81
ı	83	65.5	49.3	64.6	50.5	63.7	52.2	64.2	52.7	62.8	52.7	61.9	53.8 54.5	60.9	54.9	82 83
Ł	84	67.1	49.9 50.6	6612	51.7	65.3	52.9	64.9	53.3	64.3	53.4	63.4	55.1	62.4	55.5	84
I	85	67.9	51.2	67.0	52.3	66.1	53.5	65.7	53.9	65.1	54.6	64.1	55.8	63.2	56.9	85
I	86	68.7	51.8	67.8	52.9	66.8	54.1	66.5	54-6	65.9	55-3	54.9	56.4	63.9		86
I	87	69.5	52.4	68.6	53.6	67.6	54.7	67.3	55-2	66.6	55.9	65.7	57.1	64.6	57·5 58.2	87 88
I	88	70.3	53.0	69.3	54.2	68.4	55.4	68.0	55.8	67.4	56.6	66.4	57·7 58·4	65.4	58.9	88
ı	89	71.1	53.6	70.1	54.8	69.2	56.0	68.8	56.5	68.2	57.2	67.2		66.1	59.6	89
I	90	71.9	54.2	70.9	55.4	69.9	56.6	69.6	57-1	68.9	57.9	67.9	59.0	66.9	60.2	90
	91	72.7	54.8	71.7	56.c	70.7	57.3	70.3	57.7	69.7	58.5	68.7	59.7	67.6	60.9	91
ı	92	73.5	55.4	72.5	56.6	71.5	57·9 58.5	71.1	58.4	70.5	59.I	69.4	60.4	68.4 69.1	61.6	92
I	93 94	74.3	56.0 56.6	73·3 74·1	57.3	72.3	50.5	71.9	59.6	71.2	59.8	70.2	61.7	69.0	62.9	93
ı	95	75.1	57.2	74.9	57.9 58.5	73.8	59.8	73.4	60.3	72.8	61.1	71.7	62.3	70.6	63.6	95
I	96	76.7	57.8	75.6	59.1	74.6	60.4	74.2	60.9	73.5	61.7	72.5	63.0	71.3	64.2	96
ı	97	77.5	58.4	76.4	59.7	75.4	61.0	75.0	61.5	74.3	62.4	73.2.	63.6	72.1	64.9	97
ı	98	78.3	59.0	77.2	60.3	76.2	61.7	75.8	62.2	75.1	63.0	74.0	64.3	72.8	65.6	97 98
ı	99	79.1	59.6	78.0	61.0	76.9	62.3	76.5	62.8	75.8	63.6	74.7	65.0	73.6	66.2	99
H	100	79.9	60.2	78.8	61.6	77-7	62.9	77.3	63.4	76.6	64.3	75.5	65.6	74.3	66.9	100
١	Dift.	Dep.	Lat.	Dep.	Lat.	Dr	Lat.	Dep	Lat.	Dep.	Lat.	Dep	Lat.	Dep.	Lat-	Dift.
1	P.	53 l	Ocg.	52	Deg.	. 51	Deg.	4ª F	oint.	501	Jeg.	49	eg.	48]	Ocg.	7
		-	-	-	-		-		-							

		4.	D		_	
20		ABLE of				
<u> </u>	33 Point.	43 Deg.	44 Deg.	4 Points	Dift.]	
Dift.] I	Lat. Dep.	Lat. Dep.	Lat. Dep.	Lat. Dep.	<u> </u>	
	00.7 00.7	00.7 00.7	00.7 00.7	00.7 00.7	1 2	
² 3	02.2 02.0	02.2 02.0	02.2 02.1	02.1 02.1	3	
3 4	03.0 02.7	03.0 02.7	02.9 02.8	02.8 02.8	4	1
	03.7 03.4	03.7 03.4	03.6 03.5	03.5 03.5	5	
<u>5</u>	04.4 04.0	04.4 04.1	04.3 04.2	04.2 04.2	6	
7 8	05.2 04.7	05.1 04.8	05.0 04.9	04.9 04.9	8	-1"
	05.9 05.4		05.8 05.6	05.7 05.7	9	
9	06.7 06.0		07.2 06.9	07.1 07.1	10	
11	08.2 07.4	1-2-1-	07.9 07.6	07.8 07.8	11	
12	1 - 1 - 7 - 1		08.6 08.3	08.5 08.5	12	
13			09.3 09.0	09.2 09.2	13	
14			10.1 09.7	10.6 10.6	14	
15			11.5 11.1		15	200
16	1 31 /		12.2 11.8	11.3 11.3		
18			12.9 12.5	12.7 12.7	17	
19	14.1 12.8		13.7 13.2	13.4 13.4	19	
20		14.6 13.6	14.4 13.9	14.1 14.1	20	
. 21			15.1 14.6	14.8 14.8	21	
2.2			15.8 15.3	15.6 15.6		
23				17.0 17.0		
2	18.5 16.				25	
2			1-0-1-0-			
2		1 19.7 18.4	19.4 18.8			
. 2						
2						
3						
3						
3						
3	4 25.2 22.					
	5 25.9 23.					
3	6 26.7 24.					
3	7 27.4 24 8 28.2 25					
	8 28.2 25				39	
	29.6 26		1001			
	30.4 27					
	12 31.1 28	.2 30.7 28.	6 30.2 29.	2 29.7 29.	7 42	
- 1 - 1 + 1 - 1	43 31.8 28	.9 31.4 29.				
	44 32.6 29					
		32.9 30.				
		.6 34.4 32.			2 47	
A CONTRACTOR		2.2 35.1 32				
	49 36.3 32	.9 35.8 33	4 35.2 34.	0 34.6 34.	6 49	
-2 - 10	50 37.0 33	36.6 34	1 36.0 34.			
	part	at. Dep. La				
	Pl 4 Poin	it. 47 Deg	. 46 Deg	. 4 Point	5 1	

	Out	-	The second of the second	-	
				ARTURE.	21
Diff.	33 Point.	43 Deg.	44 Deg. 1	4 P ints	D::::
51	37.8 34.3		36.7 35.4	36. I 36 I	FT
52	38.5 34.9	38.c 35.5	37.4 36.1	36.8 36.8	52
5 ² 53	39.3 35.6	38.8 36.1	38.1 36.8	37.5 37.5	53
54	40.0 36.3		38.8 37.5	38.2 38.2	54
<u>55</u>	40.8 36.9	40.2 37.5	39.6 38.2	38.9 38.9	55
56	\$1.5 37.6 \$2.2 38.3		40.3 38.9	39.6 39.6	50
57 58	13.0 39.0			41.0 41.0	57 58
59 60	43.7 39.6	43.2 40.2	42.4 41.0	41.7 41.7	59
	44.5 40.3		43.2 41.7	42.4 42.4	60
61	45.2 41.0		43.9 42.4	43.1 43.1	61
62 63	45.9 41.6 46.7 42.3		44.6 43.1 45.3 43.8	43.8 43.8	62 63
64	47.4 43.0	46.8 43.6	45.3 43.6	45.3 45.3	64
65	48.2 43.7	47.5 44.3	46.8 45.2	46.0 46.0	65
66	48.9 44.3	48.3 45.0	47.5 45.8	46.7 46.7	66
6 ₇ 68	49.6 45.0		48.2 46.5	47.4 47.4	67
69	50.4 45.7 51.1 46.3		48.9 47.2	48.1 48.1 48.8	68 69
	51.9 47.0	51.2 47.7	49.6 47.9 50.4 48.6	49.5 49.5	70
70 71	52.6 47.7	51.9 48.4	51.1 49.3	50.2 50.2	71
72	53.4 48.4	52.7 49.1	51.8 50.0	50.9 50.9	72
73 74	54.1 49.0	53.4 49.8	52-5 50-7	51.6 51.6	73
74	54.8 49.7	54.1 50.5	53.2 51.4	52.3 52.3	74
75	55.6 50.4	54.9 51.1	53.9 52.1 54.7 52.8	53.0 53.0	75 76
76 77 78	57.1 51.7	56.3 52.5	54.7 52.8 55.4 53.5	53·7 53·7 54·4 54·4	77
78	57.8 52.4	57.0 53.2	56.1 54.2	55.2 55.2	77 78
79 80	57.8 52.4 58.5 53.1	57.8 53.9	56.8 54.9	55.9 55.9	79 80
	59.3 53.7	58.5 54.6	57.5 55.6	56.6 56.6	
81 82	60.0 54.4	59.2 55.2	58.3 56.3	57·3 57·3 58.0 58.0	81 82
83	60.8 55.1	60.7 56.6	59.0 57.0 59.7 57.7	58.7 58.7	83
84	62.2 56.4	61.4 57.3	59.7 57.7 60.4 58.4	59.4 59.4	84
85	63.0 57.1	62.2 58.0	61.1 59.0	60.1 60.1	85
86	63.7 57.8	62.9 58.7	61.9 59.7	60.8 60.8	86
8 ₇ 88	64.5 58.4	63.6 59.3	62.6 60.4	61.5 61.5	8 ₇ 88
89	65.2 59.1 65.9 59.8	65.1 60.7	63.3 61.1 64.0 61.8	62.9 62.9	89
90	66.7 60.4	65.8 61.4	54.7 62.5	63.6 63.6	90
91	67.4 61.1	66.6 62.1	65.5 63.2	64.3 64.3	91
92	68.2 61.8	67.3 62.7	66.2 63.9	65.1 65.1	92
93	68.9 62.5	68.0 63.4	66.9 64.6	65.8 65.8	93
94 95	69.7 63.1 70.4 63.8	68.8 64.1 69.5 64.8	67.6 65.3 68.3 66.0	66.5 66.5 67.2 67.2	9 1 9 5
96	71.1 64.5	70.2 65.5	69.1 66.7	67.9 67.9	96
97	71.9 65.1	70.9 66.2	69.8 67.4	68.6 68.6	97
97 98	72.6 65.8	71.7 66.8	70.5 68.1	69.3 69.3	97
99	73.4 66.5	72.4 67.5	71.2 68.8	70.0 70.0	100
100	74.1 67.2		71.9 69.5 Dep. Lat	70.7 70.7 Dep. Lat.	H
i di	Dep. Lat	Drp. Lat.	46 Deg.	4 Points	Dia
	1 4, 1 Out.	1 4/ 100%	40 Deg.	4 2 011113	

c



A TABLE of MERIDIONAL PARTS.

																		ı
L.	10	1 1	2	3_	4	_5_	1 6	7	- 8	9	10	111	12	13	14	15	14.	ı
7.1	Min.	Min.	M.n.	Min.	Min.	M.n.	Min.	Alin.	Min.	Min.	Min.	Man.	Min.	Min.	Min.	Min.	A:	ш
10	-0	60.0	130.0	180.1		300.4	360.7	421.1	481.6	542.2	603.1	664.1	725 3	786.8	348.5	910.9	0	I
1	1.0	61.0	111.0	181.1		301.4	361.7	422.1	482.6	543-3	604 1	665.1	726.4	787.9	849.5	911.5	3	ě
2	2.0	62.0	122.0	182.1		302.4	362.7	423.1		544-3	606.1	666.1	727.4	789.9	850.6	912.6		1
3	3 0	63.c	123.0		243.2	301.4	364.7	424.1		545.3	607.1	668.1	729.4	790.9	852.6	914.6		4
4	4.0						-	426.1			608.2	669.2	730.5	392.0	853.7	915.7	5	ı
1 6	6.0	65.0	125.0			306.4	365.7	420.1	487.6	547.3	600.2	670.2	738.5	793.0	854.7	916.7	16	ı
	7.0	67.0	127.0		247.2	307.4	367-7	428,1	488 6	549.3	610.2	671.2	732.5	794.0	855.7	1917-7	1 7	ı
7 8	8.0	68.0	123.0	188.1	248.2	308 4	368.7	429.1	489.6	550.3	611.2	672.2	733-5	795.0	8 56.8	918.8		ı
9	9.0	69.0	129.0	139.1	249.2	309.4	369.7	430.1	490.7	551.4	612.2	673.2	734.6	796.1	857.8	919-8	9	ı
10	10.0	70.0	130.0			310.4	370.7	431.1	491.7	552.4	613.2	674.3	735.6	797.1	858.9	920.8	10	ı
21	11.0	71.0	131.0			311.4	371.7	432.1	492.7	553.4	614.2	675.3	736.6	798.1	859.9	911.9	11	I
12	12.0	72.0	132.0			312.4	372.7	433.1	493-7	554-4	615.3	676.3	737.6	799.1 800.2	862.0	921.9	13	ı
13	13.0	73.0	133.0	193.1		314.4	373-7	434.2		555.4 556.4	617.3	678.3	739-7	801.2	863.0	925.0	14	ı
	15.0		135.0	195.1		315.4	375.8	436.2		557-4	6 18. 2	679.4	740.7	802.2	864.1	916.0	35	ı
16	16.0	75.0	136.0	196.1		316.5	376.8	437.2	497-7	558.4	619.3	680.4	741.7	803.2	865.1	927.0	16	ı
17	17.0	77.0	137.0	197.1	257.2	317.5	377.8	438.2	493.7	559-4	620.3	681.4	742.8	804.3	866. r	928.1	17	ı
18	18.0	78.0	133.0	198.1	258.2	318.5	378.8	439.2	499.8	560.5	621.3	682.4	743.8	805.3	867.2	929.1	18	ı
19	19.0	79.0	139.0	199.1		319.5	379.8	440.2		561.5	622.4	683.4	744.8	806.3	868 2	930.1	19	ı
20	20.0	800	140.0	200.1		320.5	380.8	441.2	501.8	562.5	623.4	684.5	745.8	807.3 808.4	869.2	931.2	20	ı
21	21.0	81.0	141 0	201.1		321.5	381.8	442.2	502.8	563.5 564.5	624.4	686.5	746.9	809.4	870.3	933.2	21	ı
22	22.0	82.0	142.0	203.1	263.3	323.5	383.8	444.2	504.8	565.5	616.4	687.5	747·9 748.9	810.4	872.3	934-3	23	ı
23	24.0	84.0	144.0		264.3	324.5	384.8	445.2	505.8	566.6	627.4	688.5	749.9	811.4	873.4	935.3	24	ı
2 0	24.0	85.0	1450	205.1		325.5	385.8	446.3	506.8	567.6	628.5	689.6	751.0	812.5	874.4	936.3	25	ı
26	16.0	\$6.0	146.0	206.1	266.3	326.5	386.8	447.3	507.8	568.6	629.5	690.6	752.0	813.5	875.4	937-4	26	ı
1 27	27.0	870	147.0	207.1	267.3	327.5	387.8	448.3	508.9	569.6	630.5	691.6	753.0	814.5	876.5	938.4	2.7	ı
28	28.0	88.0	148.1	208.1	268.3	328.5	388.8	449.3	509.9	570.6	631.5	692.6	754.0	815.5	877.5 878. c	939-4	25	ı
29	29.0	89.0	149.1	209.1	269.3	329-5	389.8	450.3	510.9	571.6	632.5	693.6	755-1			940.5	29	ı
30	30.0	90.0	150.1	210.1	270.3	330.5	390.8	451.3	511.9	572.6	633.5	694.7	756.1	817.6	879.6 880.6	941.5	30	ı
31	31.0	91.0	151 1	211.1	271.3	332.5	391.9	452.3	512.9	573·7 574·7	634.6	695.7	757-1	819.6	881.6	941.5	31	
32 33	33.0	92.0	152.1	213.1	273.3	333-5	393.9	454-3	514.9	575.7	636.6	697.7	759-2	810,7	882.7	944.6	33	ı
34	34.0	94.0	154.8	214.1	274.3	334.5	394.9	455.3	515.9	576.7	637.6	698.7	760.2	821.7	883.7	945.6	34	ı
35	35.0	95.0	155.1	215.1	275.3	335-5	395-9	456.3	516.0	577-7	638.6	699.8	761.2	822.7	884.7	946.7	35	
36	36.0	96.0	156.1	216.1	276.3	336.5	396.9	457-3	518.0	578.7	639.6	700.8	762.2	823.7	88:.8	947.7	36	
37	37.0	97.0	157.1	217.1	277.3	337.5	397.9	458.4	519.0	579-7	640.6	701.8	763.3	824.8	886.8	948.7	37	
38	38.0	98.0	158.1	218.2	278.3	338.6	398.9	459-4	520.0	580.8	641.7	702.8	764.3	825.8	887.8 888.q	949.8	38	
39	39.0	99.0	159.1	219.2	279.3	339.6	399.9	460.4	521.0	581.8	642.7	703.8	765.3				39	
40	40.0	100.0	160.1	220.2	280.3	340.6 341.6	400.9	461.4	522.0	581.8	643-7	704.9	767.4	827.9	889.9	951.9	40	
41	41.0	101.0	161.1	327.2	281.3	342.6	402.9	463.4	523.0	583.8	645.7	706 9	768.4	829.9	892.0	953.9	42	
43	43.0	303.0	161.1	223.2	283.3	343.6	403.9	464.4	525.0	585.8	646.7	707 9	769.4	831.0	893.0	955.0	43	
44	44.0	104.0	164.1	224 2	284.3	344.6	404.9	465.4	526.0	586.8	647.7	708.9	770.4	832.0	894.0	956.0	44	
45	45.0	105.0	165.1	225.2	285.7	345.6	405 9	466.4	527.1	487.9	648.8	710.0	771.5	833.0	895.1	957.1	45	
46	46.0	106.0	166.1	226.2	286.2	346.6	407.0	467-4	528.1	588.9	649.8	711.0	772.5	834 1	896.1	958.1	46	
47	47.0	107.0	167.1	227.2	287.3	347.6	408.0	468.4	529.1	589.9	650.8	712.0	773-5	835.1	897.1	959.2	47	
48	48.0	108.0	168.1	228.2	288.3	348.6 349.6	410.0	469.5	530.1	590.9	652.8	713.0	774.5	837.2	809.2	961.7	48 40	
+9	49.0	110.0		-		349 6	411.0	-				715.1	276.6	838.2	QEO.2	962.3	-	
51	50.0	111.0	170.1	230.2	290.3	351.6	412.0	471.5	532.1	592.9	654.9	716.1	777.6	839.2	901.2	961.4	50	
52	52.0	112.0	172.2	2 72.2	202.4	352 6	413.0	473.5	534.1	595.0	655.9	717.2	778.6	840.3	902.3	964.4	52	
53	53.0	113.0	173 1	237.2	203.4	353.6	414.0	474-5	535.1	596.0	656.9	718.2	779-7	3413	903.3	965.5	53	
54	54.0	111.0	1-4.1	234.3	294.4	354.6	415.0	475.5	536.2	597.0	657.9	719.2	780.7	842.3	904.3	966.5	54	
55	55.0	1150	275.2	235.2	295.4	355.6	4160	476.5	537.2	:98.0	659.0	720.2	781 7	343.4	505.4	967.6	55	
56	56.0	116.0	1~6.1	236.2	296.4	3:66	4170	477-5	538.2	509.0	660.0	721.2	782.7	841.4	906.4	968.6	56	
57	57.0	113.0	177.1	237.2	297.4	357.6	418.0	478.5	539.3	600.0	661.0	722.3	793.8	845.4	907.4	969.6	57	
58	58.0	110.0	178.1	238.2	208.4	359.7	419.0	479.6	540.2	602.1	662.0	723.3	785.8	\$47.5	909.5	971.7	59	
32	Min.	Min.	M.7.	Min	Min.	Mir.	Min.	Min.	Min.	Min.	Min.	Min.	Alin.	Min.	Min.	Nin.	岩	
200	-	-	-				6	-	8			-			-	15	岩	
L_{i}	0	-1	2	3	- 4	5 1	-0	-7	0	- 9	-10	-11	12	17	14_	24	Ant	

L_{-}	16	17_	18	_ 19	20	21	22	23	24	25	20	27	20	29	L.
M	Min.	Min.	Min.	Min.	Min.	Min.	Mlin.	Min.	Min.	Min.	Min.	Min.	Min.	Min.	M
0	972.8	1035.3	1098.2	1161.5	1225.1	1289.2	T353-7	1418.7	1484.1	1550.0	1616.0	1683 6	1751.2	1819.5	-0
1 2	973.8 974.8	1036.3	1099.3	1162.5	1226.2	1290,2	1354.8	1419.7	1485.2	1551.1	1617.6	1684.7	1752.3	1820.6	ĭ
3	975 9	1033.4	1101.4	1164.7	1227.3	1291.3	1355.8	1420.8	1486.3	1552.2	1618.7	1685.8	1753.4	1821.7	2
4	976.9	1039.5	1102.4	1165.7	1229.4	1293.5	1358.0	1421.9	1487.3	1553-3	1619.8	1686.g	1754.6	1822.9	3
	978 0	1040.5	1103.5	1166.8	1230.4	1294.5	1359.0	1424.1	1489.5	1555-5	1622.0	1689.1	1755.7	1824.0	4
5 6	979.0	1041.6	1104.5	1167.8	1231.5	1295.6	1360.1	1425.1	1490.6	1536.6	1622.2	1600.3	1756.8	1825.2	5
7 8	980.0	1042,6	1105.6	1168.9	1232.6	1296.7	1361.2	1426.2	1491.7	1567.7	1624.3	1691.4	1750.1	1827.5	
9	982.1	1043.7	1100.0	1170.0	1233.6	1297.8	1362.3	1427.3	1492.8	1558.8	1625.4	1602.5	1760.2	1828.6	7 8
10	983.2	1045.8	1108.7	1172.1	1235.8	1299.9	1303.3		1493.9	1559.9	1626 5	1693.6	1761.4	1829.7	_9
11	984.2	1046.8	1100.8	1173.1	1236.8	1299.9	1365.5	1429.5	1495.0	1561.0	1627.6	1694.8	1762.5	1830.9	10
12	985.2	1047.9	1110.8	1174.2	1237.9	1302.0	1366.6	1431.7	1497.2	1562.1	1629.8	1695.9	1763.6	1832.0 1833.2	11
13	986.3	1048.9	1111.9	1175.2	1239.0	1303.1	1367.6	1432.8	1498.3	1564.3	1631.0	1698.1	1765.9	1834.3	13
14	987.3	1049.9	1112.9	1176.3	1240.0	1304.2	1368.7	1433.9	1499.4	1565.4	1632.0	1699.3	1767.0	1835.5	14
15	988.4 989.4	1051.0	1114.0	1177.4	1241.1	1305.3	1369.8	14.34.9	1500.5	1566.5	1633.2	1700.4	1768.2	1836.6	15
17	990.4	1053.1	1116.1	1179.5	1242.2	1306.3	1370.9	1436.0	1501.6	1567.6	1634.3	1701.5	1769.3	1837.8	16
18	991.5	1054.1	1117.1	1180.5	1244.3	1308.5	1373.1	1438.2	1503.8	1508.7	1635.4	1702.6	1770.5	1838.9	18
19	992.5	1055.2	1118.2	1181.6	1245.4	1309.6	1374.2	1439.3	1504.9	1571.0	1637.7	1703.8	1771.6	1840.1 1841.2	10
20	993.6	1056.2	1119.2	1182.7	1246.4	1310.6	1375-3	1440.4	1506.0	1572.1	16388	1706.0	1773.9	1842.4	20
21	994.6	1057.3	1120.3	1183.7	1247.5	1311.7	1376.4	1441.5	1507.1	1573.2	1639.9	1707.1	1775.0	1843.5	21
22	995.6	1058.3	1121.3	1184.8	1248.6	1312.8	1377.4	1442.6	1508.2	1574.3	1641.0	1708.3	1776.1	1844.6	22
24	997.7	1060.4	1123.4	1186.9	1250.7	1314.9	1370.5	1444.8	1509.3	1575.4	1642.1	1709.4	1777.2	1845.8	23
25	908.8	1061.4	1124.5	1188.0	1251.8	1316.0	1380.7	1445.8	1511.5	1576.5	1643.2	1710.5	1778.4	1846.9	24
26	999.8	1062.5	1125.5	1189.0	1252.8	1317.1	1381.8	1446.0	1511.5	1577.6	1644.3	1711.6	1779.5	1848.1	25
27	1000.8	1063.5	1126.6	1190.1	1253.9	1318.1	1382.8	1448.0	1513.7	1579.8	1646.6	1712.0	1780.6	1849.2	26
28	1001.9	1064.6	1127.6	1191.1	1455.0	1319.2	1383.9	1449.1	1514.1	1580.9	1647.7	1715.0	1783.0	1851.5	28
29	1002.9		1128.7	1192.2	1256.0	1320.3	1385.0	1450.2	1515.9	1582.0	1648.8	1716.1	1784.1	1852.7	29
30	1004.0	1067.7	1129.7	1193.2	1257.1	1321.4	1386.1	1451.3	1517.0	1583.2	1649.9	1717.3	1785.2	1853.8	10
31	1005.0	1068.8	1130.8	1194.3	1258.2	1322.4	1387.2	1452.4	1518.1	1584.3	1651.0	1718.4	1786.4	1855.0	31
33	1007.1	1069.8	1132.0	1196.4	1260.3	1324.6	1389.4	1453.5 1454.6	1519.2	1585.4	1652.2	1719.5	1787.5	1856.1	32
34	1008.1	1070.9	1134.0	1197.5	1261.4	1325.7	1390.4	1455.7	1521.4	1587.6	1654.4	1720.7	1788.6	1857.2 1858.4	33
35	1009.2	1072.0	1135.1	1198.5	1262.4	1326.7	1391.5	1456.8	1522.5	1588.7	1655.5	1722.0	1750.0	1859.6	34
36	1010.2	1073.0	1136.1	1199.6	1263.5	1327.8	1392.6	1457.9	1523.5	1589.8	1656.6	1724.0	1792.1	1860.7	35
37 38	1011.3	1074.1	1137.2	1200.7	1264.6	1328.9	1393.7	1458.9	1524 7	1590.9	1657.8	1725.2	1793.2	1861.9	37
39	1013.4	1076.2	1130.2	1202.8	1265.6	1330.0	1394.8	1460.0	1525.8	1592.0	1658.9	1726.3	1794.3	1863.0	38
40	1014.4	1077.2	1140.3	1203.9	1267.8	1332.1	1395.8	1462.2	1526.9	1593.2	1660.0	1727.4	1795.5	1864.2	39
41	1015.4	1078.3	1141.4	1204.9	1268.8	1333-2	1390.9	1463.3	1528.0	1594-3	1661.1	1728.6	1796.6	1865.3	40
42	1016.5	1079.3	1142.4	1206.0	1269.9	1334.2	1399.1	1464.4	1530.2	1595.4	1663.4	1729.7	1797.8	1866.5	41
43	1017.5	1080.4	1143.5	1207.1	1271.0	1335.2	1400.2	1465.5	1531.3	1597.6	1664.5	1731.9	1800,0	1868.8	42
44	1018.6	1081.4	1144.6	1208.1	1272.1	1336.4	1401.3	1466.6	1532.4	1598.7	1665.6	1733.1	1801.2	1869.9	44
16	1019.6	1082.5	1145.6	1210.2	1273.1	I337.5	1402.4	1467.7	1533-5	1599.8	1666.7	1734.2	1802.3	1871.1	45
17	1020.0	1084.6	1140.7	1211.3	1274.2	1338.6	1403.4	1468.8	1534.6	1600.9	1667.8	1735-3	1803.5	1872.2	46
48	1022.7	1085.6	1148.8	1212.4	1276.3	1339.7	1404.5	1469.8	1535.7	1602.0	1669.0	1736.6	1804.6	1873.4	47
49	1023.8	1086.7	1149.8	1213.4	1277.4	1341.8	1406.7	1472.0	1537.9	1604.3	1671.2	1737.6	1805.7	1874.5	48
\$ 50	1024.8	1087.7	1150.9	1214.5	1278.5	1342.0	1407.8	1473.1	1539.0	1605.4	1672.3	1730.0	1808.0	1876 8	49
51	1025.9	1088.8	1152.0	1215.5	1279.5	1344.0	1408.8	1474.2	1540.1	1606.5	1673.4	1739.9	1800.2	1878.0	50
52	1026.9	1089.8	1153.0	1216.6	1280.6	1345.0	1409.9	1475.3	1541.2	1607.6	1674.6	1742.1	1810.3	1879.2	52
53 54	1020.0	1090.9	1154.1	1217.7	1281.7	1346.1	1411.0	1476.4	1542.3	1608.7	1675.7	1743.2	1811.4	1880.3	53
	1030.1	1093.0	1156.2	1110.8	1283.8	1347.2	1412.1	1477-5	1543.4	1609.8	1676.9	1744-4	1812.6	1381.5	54
. 55 56	1030.1	1094.0	1150.2	1220.0	1283.8	1348.3	1413.2	1478.6	1544.5	1610.9	1678.0	1745.5	1813-7	1882.6	55
57	1032.2	1095.1	1158.3	1221.9	1286.c	1350.4	1415.4	1479-7	1545.6	1612.0	1679.1	1746.6	1814.9	1883.8 1884.9	56
:8	1033 2	1096.1	1159.4	1223.0	1287.0	1351.5	1416.5	1481.0	1547.8	1614.2	1681.3	1747.0	1817.2	1886.1	53 58
59	1034.3	1007.2	1160.4	1224.1	1288.1	1352.6	1417-7	1483.0	1548.9	1615.4	168z.4	1750.c	1818.3	1887.2	59
И	Min.	Min.	Min.	Min.	Min.	Min.	Min.	Min.	Min.	Min.	Min.	Min.	Min.	Min.	M
Ĺ.	16	17	18	19	20	21	22	23	24	25	26	27	28	20	7.
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L.	1 30	31	32	33	34	35	36	37	38	39_	40	41	42	L.
32	Min.	Min.	Min.	Blin.	Min.	Min.	Min.	Nin.	Atin.	Min.	Min.	Alin.	Mun.	B1.
-0	1888.4	1958.1	2028.4	2099.6	2171.5	2244-3	2318.0	2392.7	2468.2	2545,0	26:2.7	2701.6	2781.7	0
	1889.5	1959.2	2029.6	2100.7	2172.7		2319.3	2393.9	2460.6	2546.2	2624.0	2702.0	2783.1	1
2	1890.7	1060.4	2010.7	2101.9	2173.9	2245.5	2320.5	2395.2	2470.8	2547-5	2625.3	2704.3	2784-4	12
3	1891.0	1961.4	2031.9	2103.1	2175.1	2248.0	2321.7	2196.4	2472.1	2548.8	2626.6	2705.6	2785.8	3
	1893.0	2962.7	2013.1	2104.3	2176.3	2240.2	2323.0	2397.7	2473-4	2550.1	2627.0	2700.9	2787.1	4
4	1894.2	1963.9	2034.3	2105.5	2177-5	2250.4	2324.2	2398.9	2474.6	2558.4	2629.2	2708.3	2788.5	5
5		1965.0	2034.3	2106.7	2178.7	2251.6	2325-4	2400.2	2475.9	2552.7	2630,5	2700.6	2780.8	6
	1895.3	1966.2	2036.7	2107.0	2180.0	2252.0	2320.7	2401.4	2477.1	2554.0	2631.9	2710.0	2701.2	
7 8	1897.6	1967.4	2037.8	2100.2	2181.2	2254.1	2327.9	2402.7	2478.5	2555.3	2633.2	2712.2	2792.5	7
	1808.8	1968.5	2019.0	2110.3	2182.4	2255.3	2329.2	2403.9	2479.7	2550.0	2634.5	2713.6	2793.8	9
9					2183.6	2256.5	2330.4		2481.0	_		-		
10	1899.9	1969.7	2040.2	2111.5	2184.8	2250.5	2330.4	2405.2	2482.3	2557.8	2635.8	2714.9	2795.1	10
11	1901.1	1970.9	2041.4	2213.0	2186.0	2250.0	2312.9	2407.7	2483.5	2559.1	2638.4	2717.5	2796.5	22
12	1902.3	1972.0	2042.6	2215.1	2187'2	2250.2	2334.1	2409.0	2484.8	2561.4	2639.7	2718.0	2797-9	12
13	1903.4	2973.2	2043.8	2116.3	2188.4	2261.3	2335-3	24.10.2	2486.1	2563.0	2641.0	2720.2	2799-3	13
14	1904.6	1974-4	2044.9											
15	1905.7	1975.6	2046 2	2117-5	2189.6	2262.7	2336.6	2411.5	2487 4	2564.3	2642.3	2721.5	2802.0	25
16	1906.9	1976.8	2047.3	2118.7	2100.8	2263.9	2337.8	2412.7	2488.6	2565.0	2643.6	2722.9	2803.3	10
17	1908.1	1977.9	2048.5	2119.8	2192.0	2265.1	2339.0	2414.0	2489.9	2566.9	2644.9	2724.2	2804.7	17
18	1909.2	1979-1	2049.7	2121.0		2267.6	2340.3	2415.2	2491.2	2568.2	2646.3	2725.5		18
19	1910.4	1980.3	2050.8		2194.5		2341.5	2410.5	2492.5	2569.5	2647.6	2726.9	2807.4	19
20	1911.5	1981.4	2052.0	2123.4	2195.7	2268.8	2342.8	2417.8	2493.7	2570.7	2648.9	2728.2	2808.7	20
21	1912.7	1982.6	2053.2	2124.6	2196.9	2270.0	2344.0	2419.0	2495.0	2572.0	2650.2	2729.5	2810.1	21
22	1913.8	1983.7	2054.4	2125.8	2198.1	2271.2	2345.3	2420.3	2496.3	2573-3	2651.5	2730.8	2811.4	22
23	1915.0	1984.9	2055.6	2127.0	2199.3	2272.5	2346.5	2421.5	2497.6	2574.6	2652.8	2732.2	2812.8	23
24	1916.2	1986.1	2056.8	2128.2	2200.5	2273-7	2347.8	2422.8	2498.8	2575-9	2654.8	2733'5	2814-1	24
25	1917.3	1987.3	2058.0	2129.4	2201.7	2274.9	2349.0	2424.0	2500.1	2577,2	2655.4	2734.8	2815.5	25
26	1918.5	1988.4	2059.1	2130.6	2203.0	2276.1	2350.2	2425.3	2501.4	2578.5	2656.8	2736.2	2816.8	26
27	1919.6	1989.6	2060.3	2131.8	2204.2	2277.4	2351.5	2426.5	2502.7	2579.8	2658.1	2737-5	2818.2	27
28	1920.8	1990.8	2061.5	2133.0	2205.4	2278.6	2352.7	2427.8	2503.4	2581.1	2659.4	2738.8	2819.5	28
29	1921.9	1992.0	2062.7	2134.2	2206.6	2279 8	2354.0	2429-1	2505.2	2582.4	2660.7	2740.2	1820.9	29
30	1927.1	1993.1	2063.9	2135.4	2207-8	2281.0	2355.2	2430.3	2506,5	2583.7	2662.0	2741.5	2822.3	30
31	1924.3	1994.3	2065 1	2136.6	2209.0	2282.3	2356.5	2431.6	2507.8	2585,0	2663.3	2742.0	2827.6	31
32	1925.4	1995.5	2066.2	2137.8	3210.2	2283.5	2357.7	2432.9	2500.0	2586.3	2664.6	2744.2	2825.0	32
33	1926.6	1996.6	2067.4	2139.0	2211.4	2284.7	2358.9	2434.1	2510.3	2587.6	2666.0	2745-5	2826.3	33
34	1927.8	1997.8	2068.6	2140.2	2212.7	2286.0	2360.2	2435 4	2511.6	2588.9	2667.3	2746.9	2827.7	34
35	1928.0	1999.0	2069.8	2141.4	2213.9	2287.2	2361.4	2436.7	2512.0	2500,2	2663.6	2748.2	2820.0	35
36	1928.9	2000,2	2009.8	2142.6	2215.1	2288.4	2362.7	24 37-9	2514.2	2591.5	2669.9	2749.5	2830 4	35
37	1930.1	2000.2	2071.0	2143.8	2216.3	2289.7	2363.9	2439.2	2525.4	2592.8	2671.2	2750.0	2831.8	37
38	1932.4	2002.5	2073.4	2145.0	2217'5	2290.g	2365.2	2440 4	2516.7	2594.1	2672.5	2752.2	2833.1	38
39	1933.6	2003.7	2074.6	2146.2	2218.7	2292.1	2366.4	2441.7	2518.0	2595.4	2673.9	2753-5	2834.5	39
				2147-4	2219.9		2367.7			2596.7	2675.1			
40	1934.7	2004.9	2075.7 2076.9	2148,6	2221.2	2294.6	2368.0	2444.2	2519.3	2598.0	2676.5	2754-4	2835.8	40
41	2935.9	2000.0	2078.2	2149.8	2222.4	2294.8	2370.2		2521.8	2599.3	2677.8	2750.2	2838.6	41
42	1937.1	2003.4	2079.3	2151.0	2223 6	2207.0	2371.4	2445.5	2523.1	2500.6	2679.1	2757.0	2839.9	42
	1930.4	2003.4 2009.6	2079.3	2152.2	2224.8	2298.2	2372.7	2448.0	2523.1	2601.0	2680.5	2750.9	2841.3	
44	-				2226.0							- A		44
45	1940.5	2010.7	2081.7	2153.4	2227.2	2299.5	2373-9	2449-3	2525.7	2603.2	2681.8	2761.5	2841.6	45
46	1941.7	20119	2082.9	2154.6	1225.5	2300.7	2375.2	2450.6	2527.0	2604.5	2683.2	2762.9		46
47	1942.9	2013.1	2084.1	2155.8	2229.7	2302.0	2370.4	2451.8	2528.3	2605.8	2684.4	2764.3	2845.4	47
48	1944.0	2014 3	2085.3	2157.0	2230.9		2377-7	2453.1	2529.5	2608.4	2685.7	2765.6	2846.7	,48
19	1945.2	2015.4		-		2304.4	2378.9	2454.3	2530.8			2766 9	2848.1	40
50	1946 4	2016.6	2087.7	2159.4	2232.1	2305.7	2380.1	2455.6	2532.1	2609.7	2688.4	2768.3	2849.5	50
52	1947.5	2017 8	2088.9	2160.7	2233.3	2306.9	2381.4	2456.9	2533.4	2611.0	2689.7	2769.6	2850.8	51
52	1948.7	2010.C	1,0001	2161.9	2234.6	2308.1	2 382.6	2458.3	2534.7	2612.3	2691.0	2771.0	2852.2	52
53	1949.9	2020,2	2091.3	2163.1	2235-8	2309.4	2353.9	2459.4	2556.0	2613.6	2692.3	2772.3	2853 6	.53
54	1951 0	2021.3	2092.5	2164.3	2237.0	23106	2385.1	2460.7	2537-2	2614.9	2693.7	2773.7	2854.9	54
155	1952.2	2022.5	1093.7	2165.5	2238.z	2311 8	2386.4	2461.9	2538 5	2616 2	2595.0	2775 0	2856.3	55
56	1953 4	2023.7	2094.9	2166.7	2239 4	2313.1	2387.6	2463.2	2539.8	2617.5	2696.3	2776.4	2857.7	56
155	1954.5	2024.9	2096.1	2167.9	2240.7	2314.3	2388.9	2464.5	2541.1	2618 8	2607.6	27:7-7	28:9.1	57
ς8	1955.7	2026.0	2097.3	2169.1	2241.9	2314.4	2390.2	2465.8	2541.4	2620.1	2599.0	2779-0	2860.5	58
19	1956.9	2027.2	2098.5	2170.3	2247.1	2316 7	2391.4	2467 0	2543.7	2621.4	2700.3	2780.4	2861 8	50
11	Min.	Alin.	Min.	Min.	Min.	Min.	M:n.	Min.	Min.	Min.	Min.	Min.	Afin.	20
1.	30	31	72	33	34	35	36	37	38	39			-	17
	1 30	3.	34	1 55	1 34	33	30	37	30	39	40	41	42	\$ 100

26	5.			A	Tab	le of.	Mer	idiona	l Pa	erts.				
L.	43	. 44	. 45	46	47	48	49	50	51.	52	53	54	1 55	L.
M	Min.	Min.	Min.	Min.	Min.	Min.	Min.	Min.	Min.	Min.	Min.	Min,	Min.	in
0	2863.1	2945.7	3030.0	3115.6	3202.8	3291 6	3382.1	3474-5	3568.8	3665.2	3763.8	3864.7	3968.0	-c
1 2	2864.5 2865.8	2947.2	3031.4	3117.0	3204.2	3294.6	3383.6 3385.2	3476.1	3570.4	3666.9	3765.5	3866.4 3868.1	3969.7	1
3	2867.2	2950.0	3034 2	3119.9	3207.2	3296.1	3386.7	3477.6	3572.0 3573.6	3670.1	3768.8	3869.8	3971.5	2
4	z868.5	2951.4	3035 6	3121.4	3208.6	3297-5	3388.2	3479.2 3480.7	3575.2	3671.7	3770.4	3871.5	3975.0	3
5	2871.3	2954.2	3037.0	3122.8	3210.1	3299.0	3389.7	3482.3	3576.8	3673-4	3772.1	3873.2	3976.7	1 5
	2872.7	2955.6	3039.8	3125.7	3213.0	3300.5	3391.3	3483.9 3485.4	3578.4 3580.0	3675.0	3773.8	1874.9 3876 6	3978-5	6
8	2874-1	2957.0	3041.3	3127.1	32 14.5	3303-5	3394-3	3487.0	3.81.6	3678.2	3777.1	3878.3	3982.0	8
9	2875.4	2958.4	3042.7	3128.6	3216.0	3305.0	3395-9	3488.5	3583.2	3679.9	3778.8	3980.0	3983.7	2
11	2878.2	2959.0	3044.1	3130.0	3217.4	3308.0	3397·4 3398.9	3490.1	3584.8 3586.4	3681.5	3780.4	3882.7 3883.4	3985.5	11
12	2879.5	2962.5	3047.0	3132.9	3220.4	3399.5	3400.4	3493.2	3588.0	3684.8	3783.8	3885.1	3989.0	12
13	2880.9	2963.9	3048.4	3134-3	3223.3	3311.0	3402.0	3494.8	3589.5	3686.4	3785.5	3886.8 3888.6	3990.7	33
15	2883.7	2966.7	3051.2	3137.2	3224.8	3314.0	3405.0	3497.9	3598.7	3689.7	3788.8	3890.3	3992.5	14
716	2885.0	29.68.1	3052.6	3138.7	3226.3	3315-5	3406.6	3499.5	3594-3	3691.3	3790.5	3802.0	3994-2	16
18	2886.4	2969.5	3054-1	3140,1	3227.7	3317.0	3408 I	3501.0	3595-9	3692.9	37.92.1	3893.7 3895.8	3997-7	17
19	2889.2	2972.3	3056.0	3143.0	3230.7	3320.0	3411.2	3502.6	1597·5 3599·1	3694.6 3696.2	3793.8 3795.5	3897.1	3999.5 4001.3	10
20	2890.5	2973.7	3058.3	3144-5	3232.2	3321.5	3412.7	3505-7	3600.7	3697.8	37.97.2	3898.8	4003.0	20
21	2891.9	2975-1	3059-7	3145.9	3233.6	3323.1	3414.2	3507.3	3602.3	3699.5	3798.8	3900.5	4004 8	23
23	2894.7	2977.9	3061.2	3147.4	3235.1 3236.6	3324.6 3326.1	3415.8	3510.5	3603.9	3701.1	3800.5	3904.0	4006.5	22 23
24	2896.0	2979.3	3064.0	3150.3	3238.1	3727.6	3418.8	3512.0	3607.1	3704.4	3803.9	3905.7	4010.0	24
25	2897.4	2980.7	3065.4	3151.7	3239.5	3329.1	3420:4	3513 6	3608.7	3706.0	3805.5	3907.4	4011.8	25
26:	2898.8	2982.1	3066.9	3153.2 3154.6	3241.0	3330.6	3421.9	3515.1	3610.3	3707-7	3807.2 3808.9	3909.1	4013.6	26
28	2901.5	2984.0	3069.7	3156.1	3244.0	3333.6	3425.0	3518.3	3613.6	3710.9	3810.6	3910.9	4015.3	27
29	2902.9	2986.3	3071.1	3157.5	3745.5	3335.1	3426.5	3519.8	\$615.2	3712.6	3812.3	3914-3	4018.9	20
30	2904.3	2987.7	3072.6	3159.0	3246.9 3248.4	3336.6 3338.1	3428.1	3521-4	3616.8	3714.2	3813.9	3916.0	4020.6	30
32	2907.1	2990.5	3075.4	3161.9	3249.9	3339.6	3431.2	3523.0	3620.0	3715.9	3815.6	3917-7	4022.4	31
33	2908.4	2991.9	3076.9	3163.3	3251.4	3341.1	3432.7	3526.1	3621.6	3719.2	3819.0	3921.2	4025.9	33.
34 35	2911.2	2993-3	3078.3	3166,2	3252.9	3342.7	3434.2	3527.7	3623.2	3720.8	3820.7	3922.5	4027.7	34
36	2912.6	2996.1	3081.1	3167.7	3255.8	3344.2	3435.8 3437+3	3529.3	3624.8	372244	3822.3	3924.6	4029.5	35 36
37 38	2914.0	2997-5	3082.6	3169.1	3257·3 3258.8	3347-2	3438.9	3532.4	3628.0	3725.7	3825-7	3928.1	4033.0	37
39	2915.3	3000.3	3084.0	3170.6	3258.8	3348.7	3440.4	3534.0	3629.6	3727.4	3827.4 3829.1	3929.8	4036.6	38
40	2918.1	3001.8	3086.0	3173-5	3261.8	3351.7	3443-5	3537.2	3672.9	3730-7	3830.8	3933-3	4038.3	39 40
41	2919-5	3003.2	3088.3	3175-0	3263.3	3353.2	3445.0	3538.8	3634.5	3732-3	3832.5	3935.0	4040.1	41
42 43	2920-9	3004.6	3089.7	3176.4	3264.7	3354.8	3446.6 3448.1	3540.3	3636.1 3637.7	3734.0	3834.2	3936.7	4041.9	42
44	2923.6	3007.4	3092.6	3179-3	3267.7	3357.8	3449.7	3542.5	3639.3	3735.6 3737-3	3835.8 3837.5	3938.5	4043.6	43 44
45	2925.0	3008.8	3094.0	3180.8	3269.2	3359-3	3451.2	3545.X	3640.9	3738.9	3839.2	3941.9	4047.2	4.5
46	2926.4	3010.2	3095.5	3182.3	3270.7	3360.8	3452.8	3546.7 3548.2	3642.5 3644.2	3740.6	3840.9 3842.6	3943-7	4049.0	46
48	2929.2	3013.	3098.3	2185.2	3273.7	3363.9	3454-3	3548.2	3645.8	3742.2	3844.3	3945.4	4050 8	47 48
40	2930.6	3014 4	3009.8	3186.6	3275.2	3365.4	3457-4	3551.4	3647.4	3745.6	3846.0	3948.9	4054.3	49
5C	2932.0	3015 8	3101.2	3188.1	3276.6	3366.9	3459 0	3553.0	3649.0	3747.2	3847.7	3950.6	4056.1	50
52	2014.7	3018.7	3104.1	3191.0	3279 6 3281.1	3369.9	3462.1	3554.6 3556.1	3652.3	3748.9	3849.4	3952.3	4057.9	51 52
53	2936.1	3026.1	3105.6	3192.5	3281.1	3371.5	3463.6	3557-7	3653.9	3752.2	3852.8	3955.8	4061.4	52
54	2937.5	3021.5	3107.0	3194.0	3282.6	3373.0	3465.2	3559-3	3655.5	3753.8	3854.5	3957.6	4063.2	54
5¢	2930.9	3021.9	3100.8	3196.4	3284.1	3374·5 3376.0	3468.3	3560.9	3657.1	3755-5 3757-2	3856.2 3857.9	3959.3	4065.8	55 56
51	2941-7	3025.7	3111.2	3198.4	3287.1	3377.6	3469.8	3564.1	3660.4	3758.8	3859.6	3962.8	4068.6	57
58	2944-4	3027.1	3112.7	3199.8	3288.6	3379.1 3380.6	3471.4	3565.7	3662.0 3663.6	3760.5	3861.3 3863.0	3964.5	4070.4	58
N	Min.	Min.	Min.	Min.	Min.	Min.	Min.	Min.	Min.	Min.	Min.	Min .	Min.	59 M
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M	Min.	Min.	Miny	Min.	Min.	Min.	Min.	Min.	Min.	Min	B21 .	Blue.	Bain.	M	ł
-0		4182.7	4294 3	4409.2	4527 4	4649.3	-	4905.0	-	5178.8		-			ı
	4073.9	4184.5	4294 3	4411.1	4529 4	4651.3	4775.0		5039 5	5170.8	5123.6	5474 0	5630.9	10	ı
1	4075.7	4186.3	4298.1	4413.1		46 46 4	4777.1	4907.2	5041.7	5183.6	5320.0	5476.6	5633.5	1	ı
2	4077.5	4133.2	4300.0	4415.0	4531.4	4655.5	4779-3 4781-4	4909.4	5044.0	5186.0	5328 5	5486.7	5636.2 5638.0	2	ı
3	4081.1	5100.0	4301.9	4417.0	4533-4	4657.5	4783.5	4912.6	5046.3		5330.9	5484 3	5030.0	3	Л
4		-	-	-	4535-4			4913.8		5188.3	5333-4		5641.5	1 4	ı
5	4082.9	4191.8	4303.8	4418.9	4537-4	4659.6	4785.7	4916.0	5050.9	5190.7	5335-9	5486.9	56.14.2	5	ı
	4084.7	4193.7	4305.7	4420.8	4539.4	4661.7	4787.8	4918.2	5053.2	5193.1	5338.3	54854	56.16.9	6	ı
7 8	4086.5	4195.5	4307.6	4422.8	4541 4	4663.7	4790.0	4920 4	5055-5	5195.4	5340.8	5402.0	5649.0	1 2	ı
	4088.3	4197-4	430) 5	4424.7	4343-4	4665.8	4792.1	4922.6	5057.7	5197.8	5343-3	5454 6	5652.3	8	ı
9	4090.1	4199.2	4311.4	4426.7	4545-4	4667 9	4794.2	4924.8	5060.c	5200.2	5345.7	5497-1	5655.0	0	ı
10	4091.9	4101.1	4313 2	4428.6	4547-5	4669 9	4796.4	4927.1	5062.3	5202.6	5348.2	5490.7	\$657.6	10	ı
2.7	4093.7	4202.9	4315.1	4430.6	4549-5	4672.0	4798.5	4929-3	5064.6	5205.0	5350.7	5502.3	5660.3	11	1
12	4093.5	4204.7	4317.0	4432.5	4551.5	4674.1	4800.7	4931.5	5066.9	5:07.3	5353.2	5504.9	5663.0	12	1
13	4097.3	4206.6	4318.9	4434.5	4553-5	4676.2	4302.8	4933-7	5069.2	5209.7	5355.6	5505	5665-7	13	t
14	4099.1	4208.4	4320.8	4436.4	4555.5	4678.2	4804.9	4935-9	5071.5	5212.1	5358.1	5510.0	5668.4	14	ı
15	4100.9	4310.3	4322.7	4438.4	4557-5	4680.3	4807.1	4938.1	5073 8	5284.5	5360.6	5512 6	\$677.1	15	1
16	4101.7	4212.1	4324.6	4440.4	4559-5	4682.4	4809.2	4040.4	5076.1	5216.9	5363-1	5515.2	5673.8	16	ı
17	4104.5	4214.0	4346.5	4442.3	4561.5	4684.5	4811.4	4942.6	5078.4	5219.3	5365.6	5517.8	5676.5	17	1
18	4106.3	4215.8	4328.4	4444.3	4563.6	4686.6	4813.5	4944.8	5080.7	5221.7	5368.1	5520.4	5679.2	18	i
19	4108.1	4217 7	4330.3	4446.2	4565.6	4688.6	4815.7	4947-0	5083.0	5224.1	5370.5	5523-0	9681.9	19	ı
20	4100.0	4219.5	4332.2	4448.2	4507.6	4690.7	4817 8	4949.3	5083.3	5226.5	5373.0	5525.6	5684.6	20	í
21	4111.7	4221.4	4334.2	4450.2	4569.6	4602.8	4820.0	4951.5	5087.7	5228.0	\$275.5	5528.2	9687.3	21	i
22	4113.5	432 3.2	4336.1	4452 1	4571.6	4694.9	4822.2	4953-7	5090.0	5231.3	5378.0	5530.8	5640.0	82	í
23	4115.3	4225.1	4338.0	4454.1	4573-7	4697.0	4824.3	4956.0	5092.3	5233.7	\$ 280. g	5533-4	5692.8	23	ı
24	4117.1	4227.0	4339.9	4456.0	4575-7	4699.1	4826.5	4958.2	5094.6	5236.1	5383.0	5536.0	5695.5	34	ı
25	4118.0	4228.8	4341.8	4458.0	4577-7	4701.2	4828.6	4960.4	5099.9	5238.5	5385.5	5538.6	5608.2	15	ı
26	4120.7	4210.7	4343.7	4460.0	4579-7	4703.2	4810.8	4962.7	5096.2	5240 9	5388.0	5541-2	5700-0	26	ı
27	4122.5	4232.5	4345.6	4461.9	4581.8	4705.3	4831.9	4964.9	5101 5	5243 3	5399-5	5543.8	5703.6	27	ı
28	4124.3	4234-4	+347-5	4463.9	4583.8	4707.4	4835.1	4567.1	\$103.0	5245.7	5393.0	5546.4	5706.9	28	۰
29	4126.1	4236.2	4349-4	4466.0	4585.8	4709.5	4837-3	4969.4	\$106.2	5248.1	5395.5	5549.0	5,00.1	29	ı
30	4127.9	4238.1	4351-3	4467.8	4587.8	4711.6	4819.4	4971.6	\$108.5	5250-5	5398.0	5551.6	5731.8	30	F
31	4129.7	4140.0	4353-3	4469.8	4589.9	4723.7	4841.6	4973-9	5110.8	52 52.0	5400.5	5554.2	5714.5	31	L
32	4131.6	4241.8	4355.2	4471.8	4591.0	4715.8	4843.8	4976.1	5113.1	5255.3	5403.0	5556.8	5717-3	32	ı
33	4133-4	4243-7	4357.1	4473.8	4593-9	4717.9	4845.9	4978.3	5115.5	5257.7	5404.6	\$559 C	5720.0	33	ſ
34	4135.2	4245.6	4359.0	4475-7	4596.0	4720 0	4848.1	4980.6	5117.8	5260.1	5408.1	5562.1	5722.7	34	ı
35	4137.0	4247-4	4360.0	4477.7	4598.0	4722.6	4850.3	4982.8	5120.1	5262.6	5410.6	5564.7	5725 5	35	r
36	4138.8	4249.3	4162.8	4479'7	46co.1	4724.2	4852.5	4985.1	5122.5	526 5.0	5413.1	5567.3	5728.2	36	П
37	4140.6	4351.2	4364.8	4481.7	4602.1	4726.3	4854.6	4987.3	5124.8	5267.4	5415.6	5569.9	5732.0	37	
38	4142.5	4253.0	4366.7	4483.6	4604.1	4728.4	4856.8	4989.6	5227.3	5260.8	5418.1	5572.6	5733-7	38	1
39	4144.3	4254-9	4368.6	4485.6	4606.2	4730.5	4859.0	4991.8	5129.5	5372.3	5420.7	5575-2	5736.4	39	ı
40	4146.1	4256.8	4370-5	4487.6	4608.2	4732.6	4861 2	4994.1	5131.8	5274.7	5423.2	5577.8	5739.2	40	
41	4147-9	4258.6	4372.5	4489 6	4610.3	4734-7	4863.3	4996.3	5134-1	5277.8	5425.7	5580.5		41	ſ
42	4149.7	4260.5	4374-4	4491.6	4612.3	4736.9	4865.5	4998.6	5136.5	5279.5	5428.2	5583.1	5744-7	42	Ĺ
43	4151.6	4262.4	4376.3	4493-5	4614 3	4739.0	4867.7	5000.0	5138.8	5282.0	5430.8	5585.7		43	
44	4153-4	4264.3	4378.2	4495.5	4616.4	4741.1	4869.9	5003.1	5141.2	5284.4	5433-3	5 588.4		44	
45	4155.2	4266	4380.2	4497.5	4618.4	4743-2	4872.3	5005.4	5143-5	5286.8	5435 8	5591.0			
46		4268.0	4382.1	4499-5	4620.5	4745-3	4874.3	5007.6	5145.9	5289.3	5438.4	5591.0	5755-7	45	
47	4157.0	4269.0	4384.0	4501.5	4622.5	4747.4	48-6.4	5000.9	5148.2	5291.7	5440.9	5596.3		47	
48	4160.7	4271.8	4385.9	4503.5	4624.6	4749.5	4878 6	5012.2	5150.6	5294.2	5447-5	5590.3	5761 3	48	
49	4162.5	4273.6	4387.9	4505.5	4626.6	4751.7	4380.8	5014.4	5152.9	5296.6	5446.0	5601.6		49	
		4275.5	4189.8	4507.5	4628.7	4753.8	4882 0	5016.7	5155.3	5200.0	5448.5	5604.3	5"66.8		
50	4164.3	4275.5	4391.7	4509.4	4630.7	4755-9	4886.2	5010.7	5157.6	5301.5	5457.8	5606.0	5760.6	50	
51 52	4168.0	4279.3	4393-7	4522.4	4632.8	4758.0	4887.4	5019.0	\$160.0	5303.9	5457.6	5600.6	5772.3	П	
53	4169.8	4282.1	4395.6	4513.4	4634.8	4760.1	4889.6	5023.5	\$162.3	5303.9	5456.2	5612.2	5775.3	52 53	
	4171.7	4287.0	4397-5	4515.4	4636.0	4762.3	4891.8	5025.8	5164.7	5303.8	5450.2	5614.9	5777-9	53 54	
54	-	4284.0	4199 5	4517-4	4619.0	4764.4	4894.0	5028.1	5167.0				5780.7		
55	4173-5	4286,8	4401.4	4517-4	4641.0	4766.5	4896.2	5028.1	5169.4	5311-3	5461.2	5617.5		55	1
56	4175-3	4288.7	4401.4	4519.4	4643.1	4768.6	4998.4	5030.3	5171.8	5313.7	5466.4	5020.2	5786.2	56	
57	4177.2	4290.6	4405.3	4523.4	4645.1	4770.8	4900.6	5034-9	5174.1	5318.6	5468.0	5625.5	5789.0	58	
59	4180.8	4202.5	4107.2	4525-4	4647.2	4772.9	4902.8	5037.2	5176.5	5321.1	5471.5	5628.2	5791.8	59	
M	Min.	Min.	Min.	Min.	Min.	Min.	Min.	Min.	Min.	Min.	Min.	Min.	Min	71 71	
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2 280.0. 2971.8 2814.9 2941.4 6744.7 675.0 680.0 297.1 2818.2 297.6 297.7 675.0 297.8 287.				6145.7	6334.9							8045.7	8375-3			i i
1		5800.2		61 51.0	6241.4	6547.2		6078.1	7214.2				8-86 8	8745.5		1
1		5803.0		6155.0	6344.6	6544.7	6756.6	6980.9	7222.5	7480.6		8061.6		8758.2		ł
\$ 88.6.6 \$38.6.6 \$39.5.6 \$10.1.6 \$351.1 \$635.1.6 \$679.0 \$699.0 \$7.20.0						6548.2			7226.6	7485.0		8066.8	8398.3	8764.8		ł
8 887-0 599-4 617-04 619-3 619-5 6	5					6551.6								8771.2		ı
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9 \$89.8 999.4 977.3 5 954.1 6 954.2 978.2 999.5 978.2 999.4 978.2 999.4 978.2 999.4 978.2 999.5 978.2 999.5 978.2 999.5 978.2 999.5 978.2 999.5 978.2 999.5 978.2 999.5 978.2 999.5 978.2 999.5 978.2 999.5 978.2 999.5 978.2 999.5 978.2 999.5 978.2 999.5 978.2 999.5 978.2 999.5 978.2 999.5 978.2 999.5 978.2 999.5 978.2 978.2 999.5 978.2 979.5 979.5 979.5 979.5 979.5	8	5817.0			6360.0	6561.0			7243.1		7782-2		8421.6	8700.6	8	ı
10 882.4.6 999.5.3 617.6.6 697.4.6 698.8.7 698.8.7 698.8.7 619.8.8 6				6173 5	6364.1	6565.4	6778.5				7788.1	8093.2	8427.4			ı
11 58.24. 998.3 10.77 970.6 974.3 978.5 701.7 725.8 736.4 779.5 829.3 849.0 881.0 11 12 58.25. 58.24. 998.5 979.										7511.9	7793 0	8098.5	8433-3	8803.6		ı
12 \$33.9 \$60.4.2 \$613.9 \$617.2 \$675.2 \$695.		5825.4				6572.3	6785.8	7013.1	7255.8	7516.4	7797.8		8439.1	8810.1		ı
12 583.9 600-11 619-02				6185.0	6277.2	6570.2	6702.2				7807.6		8450.0			ı
12 \$89.5 601.0 \$69.2 \$99.0 \$69.0 \$60.2 \$70.2 \$70.5 \$79.0 \$		5833.9	6007.1	6189.0	6380.5	6532.6	6796.9		7268.4		7812.5	8119.8	8456.8	8829.7		ı
10		5836.7			6383.7		6800.5	7028.7	7272.6		7817.4		8462.6	8836.2		ı
18		5839.5	6013.0	6195.2	6387.0	6589.5	6804.2		7276.8		7822.3	8130.6	8468.6	8842.8	16	ı
10 828.5.0 601.9 620.4.6 619.6.9 660.0 681.8 70.4.5.1 789.4. 785.7. 785.7. 182.6.7 828.6.1 19 826.5	17	5842.3			6202.6	6593.0	6811.6	7030.6		7543.6	7827.2	8135.9	84804	8876.0		ı
20 \$80.38 603.49 602.77 602.01 602.40 603.77 602.41 792.79 795.61 784.70 872.70 795.81 872.70 872.70 795.81 872.70 872.70 795.81 872.70 872.70 795.81 872.70 872.70 795.81 872.70 872.70 795.81 872.70 872.70 795.81 872.70 872.70 795.81 872.70 872.70 795.81 872.70 872.70 795.81 872.70 872.70 795.81 872.70 872.70 795.81 872.70 872.70 795.81 872.70		5848.0			6396.9	6600.0		7044.5	7289.4		7837.1	8146.2				ı
21 \$83,77 6027-9 6210.8 6219.9 600.9 6829.7 7959.9	100	5850.8	6024.9	6207.7	6400,2	6603 4								8860.2		ı
23 889.3 603.8 631.7 641.7 615.9 630.1 760.3 730.6 757.0 786.6 787.0 786.6 830.0 2.1 2.1 585.0 603.8 631.3 641.4 6617.6 660.0 683.8 70.0 70.5 780.1 78		5853.7			6403.5	6606.9	6822.7	7052.4	7297.9	7561.8	7847.0	8157.5	8498.2	8875.9		ı
24 580.2 051.6 051.6 051.7 051.6 051.7 051.6 051.7 051.7 051.7 051.6 051.7 0		5850.5			6470.7		6820.4	7050.3			7851.9	8162.9	8504.2	8882.6		ı.
12 2850.0 6094.8 6024.7		5862.2	6036.8			6617.4	6333.8		7310.6		7861.0	8173.7	8516.2	8305.0		ı
a6 587-9 604.7 62			6039.8	6221.3				-								ľ
28 287-35 6048-7 623-7 623-6 663-6 663-7 624-7 733-7 733-7 735-7	26	5867.9	6042.7	6226.7		6624.4	6841.2			7584.7	7871.8	8184.6	8528.2	8909.3	26	١
30 5870.4 9041.7 033.0 0340.9 1053.0 034.1 7 035.0 1054.1 7 035.1 7 034.1 7 035.1 7 034.1 7 035.1 7 034.1 7 035.1 7 034.1 7 035.1 7 034.1 7 035.1 7 034.1 7 035.1 7 034.1 7 035.1 7 034.1 7 035.1 7 034.1 7 035.1 7 034.1 7 035.1 7 034.1 7 035.1 7 034.1 7 035.1 7 034.1 7 035.1 7 03	27	5870.7	6045.7		6423.3	6627.9	6845.0	7076.2			7876.8	8190 I	8534-2	8916.0		ı
10 150-24 150-2						6625.0	6852.5			7508.3		8195.5	8546.2	8020.5		P
13 \$883.5 667.7 654.3 649.9 666.5 668.0 769.1 739.0 739.0 790.5 821.0 839.3 31 839.7 666.7 764.5 766.7 766.5 769.7 790.6 821.0 829	-															ı
32 838.6 660.7 624.3 64.3 64.3 64.5 665.7 655.7 670.1 735.4 735.4 750.6 750.8 870.4 894.8 33 3 837.6 860.7 624.3 64.5 655.2 657.5 760.1 735.4 735.4 750.6 750.8 870.5 860.6 83.8 870.7 660.7 624.8 650	31	5882.1	6057-7	6243.2	6436.6	6642.0	6860.0		7340.5	7607.7	7896.8	8212.0	8558.4	8943.0	31	ı
14 880.7 606.7 632.8 752.7 646.6 662.6 687.2 100.1 353.4 691.6 791.6 828.8 896.6 696.4 34.2 36.3 369.4 607.7 661.6 666.7 687.6 711.1 715.0 791.7 828.3 893.6 898.8 898.8 898.8 897.7 765.0 791.7 828.1 898.7 766.0 793.0 799.1 829.6 838.8 897.1 799.0 799.1 829.6 838.8 897.1 799.0 799.1 829.6 838.8 899.7 796.0 799.1 829.6 838.8 899.7 790.0 799.1 829.6 838.8 899.7 790.0 799.1 829.7 899.7 899.7 899.7 899.7 799.0 799.7 829.7 899.8 899.8 899.1 712.3 737.0 794.9 799.7 820.3 899.7 713.0 794.9 799.7 820.3 899.7 713.0 794.9 799.7 820.	32	5885.0	6060.7	6245.3	6439.9	6645.5	6863.7		7344.8	7612.3	7901.9	8217.5	8564.4	8949.8	32	ı
1	33				6446.6	6652.6	6871.2			7621.6		8223.0	8570.5			
36 389.6.4 for2.7 for4.8.0 for4.5.7 for5.8.0 for5.7 for5.7 for5.8.0 for5.7 for5.8.0 for5.7 for5.8.0 for5.8																ı
37 S99.3 607.7 666.12 64.6.6 666.2 688.2 710.2 730.7 74.0 79.2 79.2 79.2 79.2 79.2 79.2 79.2 79.2	36	5896.4	6072.7	6258.0	6453.3	6650.7	6878.7	7112.2	7362.0	7630.9			8588.9	8977.1	36	ı
393 959.1 561.8 5627.5 6627.3 6627.3 6627.3 689.3 718.3 737.6 763.4 7927.3 82.6 3 867.3 897.7 34 14 1970.8 687.8 627.9 627.4 685.0 697.5 687.8 627.9 627.4 685.0 697.5 718.5 7	37	5899.3			1 0456.6	6663.2	6382.5		7366.4			8245.1	8595.0	8983.9	37	
40 507.0 608.48 677.0 677.0 677.0 687.1			6078.8							7644.0		8250.7				ı
41 5910.8 6687.8 6277.9 6270.6 6677.4 6887.6 690.1 7134.7 7188.6 7679.0 790.7 8278.6 8619.6 6901.5 44 43 5913.7 660.9 6287.5 6277.4 6887.6 690.1 7134.7 7188.6 7679.0 790.6 8278.0 8857.8 9888.7 890.8 44 45 5913.6 660.9 6283.5 6381.6 6688.1 690.9 7144.9 7398.7 7698.0 7937.8 7288.6 6621.0 903.4 43 45 5924.4 690.9 6288.6 6487.5 6917.7 6918.7 714.6 714.5 71																
42 5313,7 600.8 627.1 647.4 6381.0 650.4 7156.4 7385.0 795.0 795.0 827.0 835.3 8018.4 43 43 537.6 630.9 638.6 638.1 6500.3 7144.5 7358.4 7657.7 757.8 86.2 652.0 935.4 43 44 43 44 44 44 44 44 45 362.4 630.9 638.6 638.1 6500.3 7144.5 7358.4 7657.7 757.8 86.2 652.0 935.4 44 44 44 45 362.4 632.0 935.4 638.1 6500.3 7144.5 7358.4 765.4 756.4 756.1 632.0 935.4 632.0 935.4 44 45 45 362.4 760.5 756.4 756.4 756.4 756.4 756.1 7		5910.8		6273.9		6677-4	6897.6		7282.7	7654.3		8267.4	8619.6		41	
44 590.5 66.6 683.5 683.5 683.1 695.1 690.0 744.5 736.8 765.4 796.8 824.8 863.8 692.3 44 4 4 4 502.4 690.9 628.6 684.5 690.7 691.8 745.8 7		5913.7		6277.1	6473-4	16681.0	6901.4	7136.4	7388.0	7650.0		8273.0	8625.8		42	
14 15 15 15 15 15 15 15			6006.0	6282.5		6688 T			7392.4	7668.4			8628.2			
46 998.4.2 613.0 628.8.3 638.6.9 698.1 698.2 910.4 716.7 710.9 762.6 77.8 797.1 180.5 180.0 7 90.6.3 14 67 998.1 10.0 629.2 910.0 629.2 910.4 1698.3 910.4 716.7 710.9 762.6 77.8 797.1 180.5 180.0 7 90.6.3 14 67 90.9 17.8 180.1 180.0 90.3 17.8 17.8 17.8 17.8 17.8 17.8 17.8 17.8			1													
4.7 g88.1 100.0 103.0 109.0 10	46	5925.2	6103.0	6289.8	6486.9	6695.3				7677.8	7973.1	8205.5	8650.7		46	
49 593.9 512.1 520.4 527.0 570.5 628.1 716.9 716.9 718.2 520.2 728.8 5312.4 550.9 507.3 49 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	47	5928.1	6106.0	6293.0		6698.9		7156.7	7409.9	7682.6	79 8.2	8201.1	8656.9	9053.3	Mark.	
$\begin{array}{c} \mathbf{g} \\ $					6493.6		6028.7		7414.2		7988.5		8660.5	0067.2	43	
\$\ \text{915,07} \ \text{118.2} \ \ \text{670.5} \										ALCOHOLD 1						
\$\frac{1}{5}\$ 23 \text{92.6.6}\$ 6 \text{11.2}\$ \(\frac{1}{5}\$ \text{90.9.1}\$ \) \(\frac{1}{5}\$ \text{0.7.6.8}\$ \) \(\frac{1}{5}\$ \text{90.9.1.7}\$ \) \(\frac{1}{5}\$ \text{0.7.6.7}\$ \) \(\frac{1}\$ \text{0.7.6.7}\$ \) \(\frac{1}{5}\$ \text{0.7.6.7}\$ \) \(\fra	51		6118.2	6305.9	6503.8	6713.2	6935.7		7427.4	7701.5	7998.9	8323.8	8682.0	9081.4		
\$\frac{4}{5}\frac{930.8}{5}\frac{6}{177.4}\frac{6}{171.5}\frac{1}{6}\frac{1}{1671.6}\frac{6}{1671.6}\frac{6}{6}\frac{6}{951.1}\frac{7}{1750.7}\frac{7}{451.0}\frac{7}{773.0}\frac{7}{175.0}\frac{8}{104.6}\frac{8}{1701.8}\frac{8}{1701.0}\frac{1}{100.7}\frac{5}{5}\frac{1}{5}\fra	52	5942.6		6309.1	6507.2	6716.8	6939.5	7177.1	7431.8	7706.3		8329.4			52	
\$\frac{1}{2}\frac{1}\frac{1}{2}\f	53		6124.3			6720.4	6943.4		7436.2							
66 5954.3 6134.5 6132.0 6132.8 673.14 6954.0 7193.6 7449.5 77254.8 8024.8 8,3 14.3 8713.6 8175.0 56 17 5957.2 61 77 5957.2 6136.5 6324.0 5134.0 7532.6 615.3 710.0 7532.0												THE R. P. LEWIS CO., LANSING				
cy goyr.2 \$1,95.6 \$1.24.2 \$6.34.9 \$6.38.3 \$1.99.7 \$7.84.9 \$7.30.0 \$0.90.0 \$8.58.0 \$2.30.0 \$1.92.4 \$2.58.2 \$3.90.0 \$1.90.0 \$2.82.4 \$2.75.6 \$3.91.2 \$3.25.2 \$3.90.0 \$3.9	156		6133.5		6520.8	6731.2	6954.9			7725-4	8024.8	83;2.3	8713.6		56	
59 5963.0 6142.7 6331.7 6531.0 6742.1 6966.5 7205.9 7462.8 7739.8 8040.5 8369.5 8732.7 9138.4 59 Min. Min. Min. Min. Min. Min. Min. Min.	57	5957.2	6136.5	6325.2	6524.2	6724.0	6958.8	7197.7	7452.0	7730.2	8030.0	8358.0	8;20.0	9124.0	677	
M Min. Min. Min. Min. Min. Min. Min. Min		5000.1	6149.5			6748.5			7458.3	7735.0	8040.5					
24 04 7 70 7 71 7 72 1 73 1 74 1 75 1 77 1 79 1 79 1 70 1 71 1 72 1 73				-		-		-								
	201	00	/0	1	/2	- 1	/4	-	,,,	- //	100	, , 9	-	-	-	

1	L. 1	81	83	- 84	85	- 68	_ 8;_ !	- 33	39	**	
1 "	N1	Min.	Min.	Afrin.	Mia.	Alin.	Afin.	Min	Min.	M	
1	0	9145.6	9605.9	10137.0	10764.7	11540	12521.3	11945 1	10249.8	0	
1	1 2	9152.7	9622.4	10156.2	10787.7	11561.;	12560.7	1397-4	16.,10.3	2	
1	3	9167.2	9630.6	10165 8	10794 3	115-5-0	12580 €	4003.1	16.175.1	3	
	4	9174-4	96;8 9	10175-4	10810	11500.5	12 ;99.5	14453-2	165770	4	
	5	9181.6	9647.2	10185.1	10812.5	11605.8	12618.0	14 61.0	16,61.0	5	
		9100.9	9655.5	10204.6	10845 9	11634.5	12658.6	14123-3	11- 26.2	7	
4 4 1	7 8	9203.5	0672 2	10214-4	10857	11639.3	126 8.6	14163.9	16701.7	8	
-	9	9210.8	9630.6	10224-1	10009 6	11564.1	12608 6	14114	168 28.5	9	
1	10	9218.1	9689.0	10234.0	10893 3	116,4.0	12718.8	1421,.8	16900 6	10	
	12	9232.8	9705.8	10253.7	10905.2	11709.1	12750.5	14278.9	1-166 0	12	
8	13	9240.2	9714.2	10:63.6	10917-2	11724.2	12780.0	14310.9	17130.5	13	
1	14	9247.6	9722.7	10273.9	10920 1	11739 4	12800.7	14313 2	17213.2	14	
1	15	9255.0	9731-2	10293.5	10041.2	11754-7	11821.5	14375.3	17388.7 17366 c	15	
	17	9269.9	9748.3	10303.5	15965.5	11785.4	12863.5	14441.9	17445.0	17	
	18	9277-3	9756 8	10313.6	10977.7	11800.9	12581.7	14475.4	1-525.9	13	
	19	9281.8	9765 4	10323.7	10989 9	11816.4	17906.C	14500-3	17608.7	19	
	20	9292.3	97-4 0	10334.8	11002.2	11832.0	12927.4	14543	17693 6	20	
1	21	9399.3	9702.7	10374.1	11016.9	11863.4	12970.6	14613.0	17569.9	:2	
	23	9314.8	9800.0	10364.3	11039.3	11879.2	12992.5	14648 3	17961.6	23	
	24	9322.4	9308.6	10374.5	11051.7	11895.1	13014-4	14683.9	.8055.8	24	
	25	9330.0	9817.3	10384.8	11064 2	11911 0	13056.6	14719-9	18152.6	25	
	27	9337-5	9834.8	10405.4	11089.3	11947.1	13081.2	14703.0	18354.9	27	
	28	9352.8	9843.6	10415.8	11102.0	11959.4	13103.8	1483C.2	18.160.7	28	
1	29	9360 4	9852.4	10426.2	11114.6	119-5.6	13126.5	14867.8	18569.8	29	
	32	9368.1	9861.3	10436.6	11127.4	11992.0	13149.3	14505.8	18682.5	30	
-	31	9375-8	9879.0	10457-5	11152.9	12024.9	13195.5	14983.0	18919.7	33	
1	3 3	9391.2	9887.8	10468 0	1116:.8	12041.5	13218.8	15012.3	19044.7	33	
1	34	9308-9	9896.7	10478.5	11178.7	12058.2	13242.3	1 5062.1	19174-4	34	
1	35	9406.6	9905.7	10489 1	11191.7	12074-9	13289.7	15143.0	19309.2	35	
1 -	36 37	9414-4	9914 6	10510 4	11204.7	121091.7	13313.7	15184.2	10595.8	37	
1	38	9429.9	9932.7	10521.1	11230.9	12125.6	13337.8	15225.8	19748 6	38	
	39	9437.8	9941-7	10531.8	11244.0	12142.7	13362.1	15268.0	19008 5	32	
	40	9445.6	9950 8	10542.6	11257.2	12179 9	13386.6	15310.7	20252 5	40	
1	42	9453.4	9968.9	10564.1	11283.8	12194.4	13436.1	15397.8	20438.3	42	
1	43	9469.1	9978.0	10574.9	11297.1	12211.8	13461.1	15441.1	20634.8	43	
1	44	9477.0	9987.2	10585.8	11310.6	12239.3	13486.3	15487 0	10843.1	44	
	45	9492.9	9996.3	10596.7	11324.0	12246.9	13511.6	15532 6	21064.9	45	
	47	9492.9	10014.8	10618.7	11337.0	12282.4	13563.0	115625.5	21556.6	47	
	48	9 508.8	10024.0	10629.7	11364.8	12300 2	13588.9	15673 0	21831.7	48	
	49	9516 8	10033 3	10640.8	11378.4	12318.2		15721 0	22130.6		
	50 51	9524.8	10041.6	10661.0	11392.2	12736.3		15769.8	224 58.0 22819 9		
1	52	9532 9	10051.9	10674-1	11419.8	12354.4	13694.7	15869.5	23224.3	52	
1	53	9518 9	10070.6	10685.3	11433.7	12391.0	13721.7	11920 4	23682.9	53	
-	54	9557.0	10080.0	10696.5	18447.7	12409.5		15072.1	24211.8	1	
	55	9565.1	10098.9	10707.7	11461.7	12428.0		16024 6	24836.0		
	52	9573.2	10108.4	10719.1	11489.9	12465.3	13831.7	16132.0	126582 9		
1	58	9589.5	10117.9	10741.8	11504.1	12484.2	113859.8	16187.0	27918 0	58	
	59		10127.4	107(3.3	11518.3	11543.1		16242.0		59 M	
1	R1		Min.	Min.	Min.	Min. 86	Min.	Min. 88	Min.	In I	
-	L.	82	83	84	85	80	1 87	1 22	70	1 2	 -

T A B L E

LOGARITHMS

For Numbers increasing in their Natural Order from Unite to 10000.

Num	Logarith.		Num.	Logarith.		Num.	Logarith.
I	0.000000		34	1.531479		67	1.826075
2	0.301030		35	1.544068		68	1.832509
3	0.477121		36	1.556302		69	1.838849
3 4	0.602060		37	1.568202		70	1.845098
5 6	0.698970		38	1.579784		71	1.851258
6	0.778151		39	1.591065		72	1.857332
7 8	0.845098		40	1.602060		73	1.863323
8	0.903090		41	1.612784		74	1.869232
9	0.954242		42	1.623249		75	1.875061
10	1.0000000		43	1.633468		75 76	1.880814
11	1.041393		44	1.643453		77	1.886491
12	1.079181		45	1.653212		78	1.892095
13	1.113943		46	1.662758		79	1.897627
14	1.146128		47	1.672098		80	1.903090
15	1.176091		48	1.681241		81	1.908485
16	1.204120		49	1.690196		82	1.913814
17	1.230449		50	1.698970		83	1.919078
18	1.255272		51	1.707570		84	1.924279
19	1.255272		52	1.716003		85	1.929419
20	1.301030		53	1.724276		86	1.934498
21	1.322219		54	1.732394		87	1.939519
22	1.342423		55	1.740363		88	1.944483
23	1.361728		56	1.748188		89	1.949390
24	1.380211		57	1.755875		90	1.954242
25 26	1.397940		58	1.763428		91	1.959041
26	1.414973		59_	1.770852		92	1.963788
27	1.431364	н	60	1.778151		93	1.968483
	1.447158	н	61	1.785330		94	1.973128
29	1.462398		62	1.792392		95	1.977724
.30	1.477121		63	1.799340		96	1.982271
31	1.491362		64	1.806180		97	1.986772
32	1.505150		6 ₅	1.812913		98	1:991226
_ 33	1.518514		66	1.819544		99	1.995635
					-		

No.	1 0	1 I	1 2	1 3	4	1 5	1 6	-	1 8	1 9
100	-		0 - 58	001301	001734	002166		0, 29	003460	1 '
101	004321	004751	005130	005609	006038	006465	006394	0_7321	007748	
102			0=9451	009876	010300	010721	011147	11570		
103		013259	01,630	014100	014520	014910	015350	015770		01661
104			017 68	13284	015700	019947	31):32	019947	020361	102057
Inc	021189		022015	02242				7.11		STREET, ST.
106	025306	025715	026124	026533	0_5942	023252	02505	024075	024486	02489
107	029384	029789	030195	030600	031004	027350	027757	032216	028571	C28978
108	033424	033826	034227	034628	35020	035.130	035830	036229	036629	037021
109	037426	037825	038223	038620	039017	039+14	039811	040207	040602	140998
110		041787	042182				-	1	THE SECTION	
111	041393	045714	046105	042575	042959	043362	043755	044148	044540	344931
112	049218	249606	049993	050380		047275	047664	048053	048442	548835
113		053463	053346	054230	050766	051152	051538	051924	052309	052694
114	056905	057286	057666	058046	058426	058805	059185		056142	055524
115	060608	061072	061452	061820	062206			059563	059942	000320
116	064458	064832	065266	065580	065953	062582	062958	063333	063708	064083
117	068186	068557	068928	069298	069668	006326	066698	067071	067443	067814
118	071882	072250	072617	072985	973352	073718	074085		071145	071514
119	075547	075912	076276	076640	077004	077368	077731	074451	074816	075182
120	079181	079543	079904	080266	080626	08:087	081347			
121	082785	083144	083503	083861	084219	084576	084934	081707	082067	082426
122	086360	086716	087071	087426	087781	088136	088490	085291	085647	086004
123	089905	090258	090611	090963	091315	091667	092018		092721	089552
124	093422	093772	094122	094471	094820	095169	095518	092370	096215	093071
125	096910	097257	097604	097951	098297	098644	098990		Transmission of Street	
126	100370	100715	101059	101403	101747	102090	102434	099335	099681	100026
127	103804	104145	104487	104828	105169	105510	105851	102777	103119	103462
128	107210	107549	107888	108227	108565	108903	109241	109578	109916	106870
129	110590	110926	111262	111598	111934	112270	112605	112940	113275	113609
130	113943	114277	114611	114944	115278	11561	115943	116276	116608	
131	117271	117603	117934	118265	118505	118926	119256	119586	119915	116940
132	120574	120903	121231	121560	121888	122216	122543	122871	123198	120245
133	123852	124178	124504	124830	125156	125481	125806	126131	126456	126781
134	127105	127429	127752	128076	128399	128722	129045	129368	129690	130012
135	130334	130655	130977	131298	131619	131939	132200	132880	I 32900	133219
136	133539	133858	134177	134496	134814	135133	135451	135768	136086	130403
137	136721	137037	137354	137670	137987	138303	138618	138934	139249	139564
138	139879	140194	140508	140822	141136	141450	141763	142076	142389	142702
139	143015	143327	143639	143951	144263	144574	144885	145196	145507	145818
140	146128	146438	146748	147058	147367	147676	147985	148294	148603	148911
141	149219	149527	149835	150142	150449	150756	151063	151370	151676	141982
142	152288	152594	152900	153205	153510	153815	154119	154424	154728	155032
143	155336	155640	155943	156246	150549	156852	157154	157457	157750	153061
144	158362	158664	158965	159266	159567	159868	160168	160468	160769	161068
	0	I	12	3	4	5	6	7	8	9
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L	0	G	A	R	ſ	T	H	M	S

No	0	1	2	_ 3	4	5	6	7	8	9
145	161368	161667	161967	162266	162564	162863	163161	163459	163757	164055
146	164353	164650	1649:7	165244	165541	165838	166134	166430	166726	167022
147	167317	167613	167908	168203	168497	168792	169086	169380	169674	169968
148	170262	170555	170848	171141	171434	171726	172019	172311	172603	172895
149	173:86	173478	173769	174060	174351	174641	174932	175222	175512	175802
150	176091	176381	176670	176959	177248	177536	177825	178113	178401	178689
151	178977	179264	179552	179839	180126	180413	180699	180986	181272	181558
152	181844	182129	182415	182700	182985	183270	183554	183839	184123	184407
153	184691	184975	185259	185542	185825	186108	186391	186674	186956	187239
154	187521	187803	188084	188366	188647	188928	189209	189490	189771	190051
155	190332	190612	190892	191171	191451	191730	192010	192289	192567	192846
156	193125	193403	193681	193959	194237	194514	194792	195069	195346	195623
157	195900	196176	196452	196729	197005	197281	197556	197832	198107	198382
158	198657	198932	199206	199481	199755	200029	200303	200577	200850	201124
159	201397	201670	201943	202216	202488	202761	203033	203305	203577	203848
160	204120	204391	204662	204933	205204	205475	205745	206016	206286	206556
161	206826	207095	207365	207634	207903	208172	208441	208710	208978	209247
162	209515	209783	210051	210318	210586	210853	211120	211388	211654	211921
163	212188	212454	212720	212986	213252	213518	213783	214049	214314	214579
164	214844	215100	215373	215638	215902	216166	216430	216694	216957	217221
165	217484	217747	218010	218273	218535	218798	219060	219322	219584	219846
166	220108	220370	220631	220892	221153	221414	221675	221936	222196	222456
167	222716	222976	223236	223496	223755	224015	224274	224533	224792	225051
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23			365862	366049	366236	366423		366796	366983	367169
23	10,00			367915		368287		368659	368844	369030
23		369401		369772		370143		370513	370698	370883
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238	376577	376759	376942			377488		377852	378034			
239	378398	378580		378943				379668	379849	380030		
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3	84	584331	584444	584557	584670	584783	584896	585009	585122	585235	585348
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3	86	586587	586700	586812	586925	587037	587149	587262	587374	587486	587599
3	87	587711	587823	587935	588047	588160	588272	588384	588496	588608	588729
3	88	588832	588944	589055	589167	589279	589391	589503	589614	589726	589838
3	89	589950	590061	590173	590284	590396	590507	590619	590730	590842	590953
	30	591065	591176	591287	591398	591510	591621		591843		592066
			592288	592399		592621	37	591732		591955	
	91	593286	593397	593508	592510		592732	592843	592954	593064	593175
	92					593729	593840	593950	594061	594171	594282
	93	594392	594503	594613	594724	594834	594945	595055	595165	595276	595386
	94	595496	595606	595717	595827	595937	596047	596157	596267	596377	596487
	95	596597	596707	596817	596927	597037	597146	597256	597366	597476	597585
	96	597695	597805	597914	598024		598243	598353	598462		598681
	97	598790	598900	599009	599119	599228	599337	599446	599556	599665	599774
	98	599883	599992	600101	600210	600319	600428	600537	600646	600755	600864
	99	600973	601082	601190	601299	601408	601517	601625	601734	601843	601951
	00	602060	602168	602277	602386	602494	602602	602711	602819	602928	60303f
	01	603144	603253	603361	603469	603577	603685	603794	603902	604010	604118
	C 2	604226	604334	604442	604550	604658	604766	604874	004982		60519-
	.03	605305	605413	605520	605628	605736	605843	605951	606059	606166	606274
4	.04	606381	606489	606596	606704	606811	606918	607026	607133	607240	60734
4	.05	607455	607562	607669	607777	607884	607991	608098	608205	608312	608410
	.06	608526	608633	608740	608847	608954	603060	609176	600381	609274	609488
4	.07	609594	609701	609808	609914	610021	610128	610234	610447		610554
A	.08	610660	610767	510873	610979	611086	611192	611298	611511	611405	61161-
4	.09	611723	611829	611936	612042	612148	612254	612360	612572	612466	612675
1	10	612784	612890		613102	613207	613313	613419	613630	613525	613736
	11	613842	613947	614053	614159	614264	614370	614475	614606		614792
	12	614897	615003		615213	615319	615424	615520	615740		615845
	13	615950	616055		616265		616475	616580	616790		616895
	14		617105		617315		617524	617629	617839	617734	617943
-		0	1	2	3	4	5	-6-		- 8 -	9
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38			L	0 G.	AR I	TH	M S.			
No.	0	I	2	3	4	1 5	6	7	1 8	9
415	618048	618153	618257	618362	618466	618571	618675	618780	618884	618989
416	619093	619198	619302	619406	619511	619615	619719	619823	619928	620032
417	620136	620240	620344	620448	620552	620656	620760	620864	620968	621072
+18	621176	621280	621384	621488	621592	621695	621799	621903	622007	622110
419	022214	622318	622421	622525	622628	622732	622835	622939	623042	623146
-20	623249	623353	623456	623559	623663	623766	623869	623972	624076	624179
42.1	624282	624385	624488	624591	624694	624798	624901	625004	625107	625209
422	625312	625415	625518	625621	625724	625827	625929	626032	626135	626238
+23	626340	626443	626546	626648	626751	626853	626956	627058	627161	627263
424	627366	627468	627571	627673	627775	627878	627980	628082	628184	628287
425	628389	628491	628593	628695	628797	628900	6290C2	629104	629206	629308
426	629410	629511	629613	629715	629817	629919	630021	630123	630224	630326
427	630428	630529	630631	630733	630834	630936	631038	631139	631241	631342
428	631444	631545	631647	631748	631849	631951	632052	632153	632255	632356
429	632457	632558	632660	632761	632862	632963	633064	633165	633266	633367
+30	633468	633569	633670	633771	633872	633973	634074	634175	634276	634376
431	634477	634578	634679	634779 635785	634880	634981	635081	635182	635283	635383
432	635484	635584	635685	635785	635886	635986	636086	636187		636388
433	636488	636588	636688	636789	636889	636989	637089	637189	637289	63739c
434	637490	637590	637690	637790	637890	637990	638090	638190	638289	638389
435	638489	638589	638689	638789	638888	638988	639088	639188	639287	639387
436	639486	639586	639686	639785	639885	639984	640084	640183	640283	640382
437	640481	640581	640680	640779	640879	640978	641077	641176	641276	941375
438	641474	641573	641672	641771	641870	641970	642069	642168	642267	652366
439	642464	642563	642662	642761	642860	642959	643058	643156	643255	643354
440	643453	643551	643650	643749	643847	643946	644044	644143	644242	644340
441	644439	644537	644635	644734	644832	644931	645029	645127	645226	645324
442	645422	645520	645619	645717	645815	645913	646011	646109	646208	646306
443	646;04	646502		646698	646796	646894	646991	647089	648165	647285
144	647383	647481	647578	647676	647774		647969			
145	648360	648458	648555	648653	648750	648848	648945	649043	649140	649237
446	649335	649432	650502	649627	649724	649821	650890		651084	651181
447	650307	650405	651472	650599	651666	651762	651859	651956	652053	652150
448	652246	652343	652440	652536	652633	652730	652826		653019	653116
20 ma			7		653598	653695	653791		653984	654080
450	653212	6533c9	653405 654369	653502	654562	654658	654754		654946	655042
451 452	655133	655234	655331	655427	655523	655619	655714	655810		656002
452 453	656098	656194	65£290	656386	656481	656577	656673		656864	65696c
454	657056	657151	657247	657343	657438	657534	657629		657820	657916
	658011	658107	658202		658393	658488	658584	658679	Married Committeed	658870
45 5	658955	659000	659155		650346	659441	659536	659631		659821
157	650916	660011	660106		660296	660391	660486	660581		660771
.58	660865	660960	661055		661245	661339	661434	661529		66171
-59	661813	661907	662002	662096	662191	662285	662380	662474	662569	66266
.32	0	I	2	3	4	5	6	7	8	9
-		OCTUGE DE LA CONTRA DE	THE RESIDENCE	Sa Printer March	A PARTE NAME OF THE PARTY OF TH	THE PARTY OF	ARREST DESCRIPTION	DATE OF THE PERSON	THE PARTY OF	NAME OF TAXABLE

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No.		1	2	3_	4	_ 5	6	7_	8	9_
	662758	662852	052947	663041	663135	663230	66 324	663418	663512	663607
461		663795	663889	663983	664078	664172	664266	664365	664454	664.54
162			664835	664924	665018	665112	605206	655299	665393	665487
163		665675	365763	665862	665956	666050	666143	656237	666331	666424
464		666612	666705	666799	666892	666986	667079	667173	667266	667359
1.165		667546	667640	667733	667826	657920	668013	658106	668197	668293
196		668479	668572	668665	668758	668852	668945	659038	669131	669224
457	669317	669410	669503	669596	669689	669782	669874	669967	670060	670153
468		670339	670431	670524	670617	670710	670802	670895	670988	67108c
+69	1,	671265	671358	671451	671543	671636	671728	671821	671913	672005
470		672190	672283	672375	672467	672560	672652	672744	672836	672929
471		673113	673205	673297	673390	673482	673574	673666	673758	673850
472		674034	674126	674218	675228	674402	674494 675412	674586	674677	674769
473		675870	675961	676053	676145	676236	676328	676419	675575	675687
474	777	676785	676876	676968		Committee to	Continue Ann			
475		677698	6-7780		677972	678063	677242	677333	677424	677516
476	678518	678609	677789 678700	677881	678882	678973	678154	679155	678336	678427
477 478		679519	679610	679700	679791	679882	679973	680063	680154	679337
479	680335	680426	680517	630607	680698	680789	680879	680970	681060	681151
480	681241	681332	681422	681513	631603	681693	681784	681874	681964	682055
481	682145	682235	682326	682416	632506	682596	682686	682777	682867	682957
482	683047	683137	683227	683317	683407	683497	683587	683677	683767	683857
483	683947	684037	684127	684217	684307	684396	684486	684576	684666	684756
484	684845	684935	685025	685114	685204	685294	685383	685473	685563	685552
485	685742	685831	685921	686010	686100	686189	686279	686368	686457	686547
486	686636	686726	686815	686904	686994	687083	687172	687261	687351	687440
487	687529	687618	687707	687796	687885	687975	688c6+	688153	688242	638331
188	688 120	688509	688598	688687	688776	688865	688953	689042	689131	639220
189	689309	689398	689486	689575	689664	680753	689841	689930	690019	690107
490	690196	690285	690373	690462	690550	690639	690727	690816	690905	690993
491	691081	691170	691258	691347	691435	691523	691612	691700	691788	491877
492	691965	692053	692142	692230	692318	692406	692494	692583	692671	692759
493	692847	692935	693023	693111	693199	693287	693375	603463	603551	693639
194	693727	693815	693903	693991	694078		604254	694342	69443C	6945175
+95	694605	694693	694,81	694368	694956			695219	695306	695394
196	695482	695569	695657	695744	695832	695919	696007		695182	6962663
197	696356	696444	696531	696618	696706		696880	696968	69-055	697142
498	697229	6973.6	697404	697491	697578	697655	677752	697839	637925	698013
199	1		698275	698352	608448	698575	698622	698709	6,8796	698883
500	698970	699057	693144	699230	699317	699404	690491		699664	099751
501	699838	699924	700011	700008	700184	700271	700357	700444	700531	700017
502	700704	700790	700877	700963	701050	7 11136	701222	701,09	701395	701.15
503	701568	702517	701741	702689	701913	7019191	702947	702172	702258	702314
	702430	''-	2	7	124/13		6	703033	703119	703205
-	-	CHARLES STORY	ALPAE DE DE	DE TRAL BUILDING	4	5		7	O I	9

40			L	0 G A	RIS	THA	1 S.			
No.	1 0	I	2	3	4	5	6	7 1	8	9
505	703291	703377	703463	703549	703635	703721		703893	703979	704065
506	704150	704236	704322	704408	704494	704579	704665	704751	704837	704922
507	705008	705094	705179	705265	705350	705436	505522	705607	705693	705778
508		705949	706035	706120	706205	706291		706462	706547	706632
500		706803	706888	706974	707059	707144	707229	707315	708251	708336
510		707655	707740	707826	707911	707996	708931	709015	709100	709185
511		708506	708591	708676	709609	709694	709779	709863	709948	710033
51:		709355	710287	710371	710456	710540	710625	710710	710794	710879
51			711132	711216	711301	711385	711470	711554	711638	711723
			711976	712060	712144	712229	712313	712397	712481	712565
51			712818	712902	712986	713070	713154	713238	713322	713406
51			713658	813742	713826	703910	713994	714078	714162	714246
51	8 714330		714497	714581	714665	714749	714832	714916	715000	715084
51			715335	715418	715502	715586	715669	715753	715836	715920
52	0 71600	716087	716170	716254	716337	716421	716504	716588	716671	716754
52		716921	717004	717088	717171	717254	717338	717421	717504	717587
52	2 717670		717837	717920	718003	718086		718253	718336	718419
52				718751	718834	718917	719000	719083	719103	720077
52				719580	-		1	720738	720821	720003
52	5 72015			720407	720490	720573		721563	721646	721728
52				721233	722140	722222		722387	722469	722552
52				722881	722963	723045		723209	723291	723374
52				723702	723784	723866		724030	724112	724194
-		-		724522				724849	724931	725013
5.			725258	725340	1,	725503		725667	725;48	725830
5.						726320	726401	726483	726564	726646
5			726890			727134			727379	727460
	34 72754		3 727704						728192	728273
	35 72835	4 72843	5 728516	728597				728922		
	36 72916							729732		729893
5	37 72997	4 73005						730540		731508
	38 73078	2 73086	31730944							
-	39 73158		- 1							
	40 73239					73359				
	41 73319						0 734480			
	42 73399	0.0	0 73496				0 735279	735359	735439	735519
	43 734.80		9 73575		8 73591			73615	736237	736317
3	45 7363					5 7:679				737113
	46 7371	93 73727	2 73735	2 73743	1 73751	1 73759		73774		737908
	47 7379	87 73806	7 73814	6 73822	5 73830	5 73838				
1	48 7387	81 73886	0 73893	9 73901	8 73909		7 73925			
	49 7395	72 73965					74004		8	740204
	0	1	2	3	4	5		. 7	-	9

No.	0	1	2	3	4	_ 5	6	7_	_ 8_	9 -
550	740363	740442	740521	740599	740678	740757	740836	740915	740994	741073
551	741152	741230	741309	741388	741467	741546	741624	741703	741782	741860
552	741939	742018	742095	742175	742254	742332	742411	742489	742568	742647
553	742725	742804	742882	742961	743239	743118	743196	743275	743353	743431
554	743510	743588	743666	743745	743823	743902	743480	744058	744136	74-215
555	744493	744371	744449	744528	741606	744684	744762	744840	744919	744 397
556	745075	745153	745231	745309	745387	745465	745543	745621	745699	745777
557	745855	745933	746011	746089	746167	746245	746323	746401	7 6479	7.6550
558	746034	746712	746790	746868	746945	747023	747101	747179	747256	747334
559	747412	747489	747567	747645	747722	747800	747878	747955	74803	
560	748188	748266	748343	748421	748498	748576	748653	748731	748808	748885
561	748963	749040	749118	749195	749272	749350	749127	749504	749582	749659
562	749736	749814	749891	749968	750045	750123	750200	750277 751048	75035	750431
563	750508	750586	750663	750740	750817	75089+		751040	751124 751895	751202
564	751279	751356	751433	751510	751587	751664	751741	751818		75197
565	752048	752125	752202	752279	752356	752433	752509	752586	752663	752740
566	752816	752893	752970	753047	753123	753200	753277	753353	753430	
567	753583	753660	753736	753813	753889	753966	754042	754119	754195	754272
568	754348	754425	754501	754578	754654	754730	754807	755646	751950	755799
569	755112	755189	755265	755341	755417	75549	755570	756408	755722	7565 0
570	755875	755951	756027	756103	756180	756256	756332	757163		
571	756636	756712				757016	757092	757927	757244	7573
572	757396	757472 758230	757548	757624	757700 7584 5 8	757775 758533	758609	758685	758761	750836
573	758912	758988	759063	759139	759214	759290	759366	759 41	759517	759=92
574	759668	759743	759819	759894	759970	760045	760121	760196	760272	76034"
575	760422	760498	760573	760649	760724	760799	760875	760050	761025	611 1
576	761176	761251	761326	761402	761477	761552		761702	761778	-61852
577 578	761928	762003		762153	762228	762303	762378	762453	762529	76260
579	762679	762754	762829	762904	762978	763053	,763128	763203	763278	,5335
580	763428	763503	-	763653	763727	763802	7638,7	763952	764027	764102
581	764176	764251	764326	764400	764475	764550	764624	76,699	764774	764848
582	764923	764998	765072	765147	765221	765296	765370	765445	765520	765594
583	795669	765743		765892	765966	766041	765115	766190	76626.1	766 38
584	766413	766487	766562	766636	766710	766785	766859	766933	767007	767082
585	767156	767230	767304	767379	767453	767527	767601	767675	767749	6-82
586	767898	767972		768120	768194	768268	768 342	768416	768490	76855
587	768638	768712		768860	768934	769008	769082	769156	769230	7693
588	769377	769451	769525	769599	769673	769746	769820	059894	769968	77004
589		770189	770263	770336	770410	770484	770557	770631	770705	7707-8
590		770926	770999		771146	771220	771293	771367	771440	775 14
591		771661	771734	771808	771881	771955	772028	772102	772175	77224
592		772395	772468	772542	772615	772688	772762	772835	7-2008	772981
593	773055	773128		773274	773348	773421	773494	773567	773640	77371
594	773786	773860	773933	774006	774079	774152	774225	774298	77+37I	77+1-
	0	1	2	3	4	5	6	7	8	9
-	-		-	No. of Concession, Name of Street, or other Designation, or other	-	THE OWNER WHEN	THE RESERVE	-		THE RESIDENCE

42	,		L	0 G.	A R 1	TH	M S.			
No.	0	I	2	3	4	5	6	7	ď	9
595	774517	774590	774663	774736	774809	774882	774955	775028	775100	775173
596	775246	775319	775392	775465	775538	775610	775683	775756	775829	775902
597	775974	776047	776120	776193	776265	779338	776411	770483	776556	776629
598	776701	776774	776846	776919	776992	777064	777137	777209	777282	777354
599	777427	777499	777572	777644	777717	777789	777862	777934	778006	778079
500	778151	778224	778296	778368	778441	778513	778585	778658	778730	778802
501	778874	778947	779019	779091	779163	779236	779308	779380	779452	779524
602	779596	779669	779741	779813	780605	779957 780677	780749	780101	780893	780245 780065
603	781037	781109	781181	781253	781324	781396	781468	781540	781612	781684
605	781755	781827	781899	781971	782042	782114	78 2186	782258	782329	782401
606	782473	782544	782616	782688	782759	782831	782902	782974	783046	783117
607	783189	793260	783332	783403	783475	783546	783618	783689	783761	783832
608	783904	783975	784046	784118	784189	784261	784332	784403	784475	784546
600	784617	794689	784760	784831	784902	784974	785045	785116	785187	785259
610	785330	785401	785427	785543	785615	785686	785757	785828	785899	785970
611	786041	786112	786183	786254	786325	786396	686467	786 538	786609	786680
612	786751	786822	786893	786964	787035	737106	787177	787248	787319	787390
613	787460	787531	787602	787673	787744	787815	787885	787956	788027	788098
614	788168	788239	788310	788381	788451	788522	783593		788734	783804
615	788875	788946	789016	789087	789157	789228	789299		789140	789510
616	789581	789651	789722	789792	789863	789933	79000 4	790074	790144	790215
617	790285	790356	790426	790496	790567	790637	792707	790778	790843	790918
618	790988	791059	791129	791199	791269	791340	791410	791480	791550	791620
619	791691	791761		791901	791971	* *		Commence was		792322
620	792392	792462	792532	792602	792672	792742	792812	792882	792952	793022
621	793092	793162	793231	793301	79337 I 794070	793441 794139	794209	794279	794349	793721 794418
622 623	793790 794488	794558	794627	794697	794767	794836	794906	794976	795045	795115
624	795185	79525+	795324	795393	795463	795532	795602	795671	795641	79581
	795880	795949	796019	796088	796158	796227	796297	796366	796436	796505
625 626	796574	796644	796713	796782	796852	796921	796990	797060	797129	797198
627	797268	797337	797406	797475	797545	795614	797683	797752	797821	797890
628	797960	798029	798298	798167	798236	798305	798374	798+43	798512	7985 2
629	798651	798720	798789	798858	798927	798996	799065	799134	799203	799272
630	799341	799409	799478	799547	799616	799685	739754	799823	799892	79956:
631	800029	800098	800167	800236	800305	800373	800442	800511	800580	800648
632	800717	800786	800854	800923	800992	801060	801129	801108	801267	801335
633	801404	801472	801541	801609	801678	801747	802500	801884	801952	802021
634	802089	802158	802225	802295	802363	802432				803384
635	802774	802342	802910	802979	8030+7	803116	803184	803252	803321	804071
636	803457	803525	803591	803662	803730	803798	804548	804616	804685	804753
537	804139	804208	804276	804344	805093	805161	305229	805297	805365	805433
638	805501	805569	805637	805705	805773	805840	805908	805976	806044	806112
639	005501	003309	2	3	4	5	6	7	8	9
-	D.	Name of Street		- 3	4	, ,				المشسا

No. 040 041 042 043	805180 805859 807535 808886 808886	806248 806926 807603 808279	800316 800394 807670	800383	805451	836519	806587	806655	806723	806790
641 642 643	805859 807535 808886	806926 807603 808279	806994							
043	807535 808836	807603 808279			807120	807197	807264	807332	807400	80746;
043	808886	808279		807738	807806	807873	807941	308 08	808076	808142
	808886		808346	808414	803481	30854	308616	808683	808751	808315
-	809560	808953	809021	820088	859155	809223	809290	807358	809425	809:92
-45		839627	809594	800762	800820	800806	809963	Sicosi	810098	81016:
040	810232	810300	810367	810434		810568	810536	810703	810770	51033
047	810004	810971	811038	811105	811173	811240	811307	811374	811441	811505
1545	811575	811642	811709	811776	811843	811910	811977	812044	812111	812176
649	812245	812312	812378	812445	812512	822579	8126,6	812713	812780	812346
550	812913	812080	813047	813114	813180	813247	813314	813381	813447	813514
651	813581	813548	813714	813781	813848	813914	813981	814048	814114	814181
052	814248	814314	814381	814447	814514	814580	814647	814714	814780	814847
653	814913	814980	815046	815113	815179	815246	815312	815378	815445	S15511
55+	815578	815644	815710	815777	815843	815010	815976	816042	816109	516175
555	816241	816308	816374	816440	816506	816573	816639	816705	316771	816838
056	816904	816970	817036	817102	817169	817235	817301	817367	817433	817499
657	817565	817631	817698	817764		817896	817962	818028	\$18094	819160
658	818226	818292	818358	818424	818490	818556	818622	818638	818754	818819
659	818885	818951	819017	819083	819149	819215	819281	819346	819412	819478
660	819544	819610	819575	819741	819807	819873	819939	820-04	820070	820136
661	820201	820267	820333	820398	820464	820530	820595	820661	820727	820792
	820858	820924	820989	821055	821120	821186	821251	821317	821 82	821448
	821513	821579	821644	821710	821775	821841	821506	821972	822037	822102
664	822168	822233	822299	822364	822430	822495	822560	822626	822691	822756
	822822	822887	822952	823017	823083	823148	823213	823279	823344	\$23409
	823474	823539	823605	823670	823735	823800	823865	823930	823996	824061
	824126	824191	824256	824321	824386	824451	824516	824581	824646	825361
	825426	825491	825556	825621	825686	825751	825815	825880	825045	826010
	826075	826140	826204	826269		826399	826464	826528	826593	825658
	826722	826787		826917	826981	827046	827111	827175	827230	827305
	827369	827434	827498	827563	827628	827692	827757	827821	827886	827950
	828015	828080		828209	828273	828338	828402	828456	828531	828595
	828660	828724	828789	828853	828918	828982	829046	829111	829175	829230
7.7	829304	829368	829432	829497	829561	829625	829690	829754	829818	829882
	829947	830011	830075	830139	830204	830268	830332	830396	830460	830524
	830589	930653	830717	830781	830845	830909	830973	83103"	881102	831166
	831230	831294	831358	831422	831486	831550	831614	831678	831742	831856
	831870	831934	831998	832062	832125	832189	832253	832317	832381	8 32 145
	8 32 500	832573	832637	832700	832764	832828	832892	832956	833019	83328;
	833147		833275	833338	833402	833466	833530	833593	833057	833721
182	833784	833848	833912	833975	834039	834103	834166	834230	834293	8 34357
	834421	834484	834548	834611	834675	834738	834802	834866	834929	834993
584	835056	835120	835183	835246	835310	835373	8 35 4 37	835500	83-504	835527
	0	I	1/2	3	4	15	6	7	8	9

44			L	0 G 2	4 R I	TH	M S.		-	
No	0	I	2	3	4	5	6	7 1	8	9
685	835691	835754	835817	8 5881	835944	836007	836071	836134	836197	836261
686	836324	836387	836451	836514	836577	836640	836704	836767	836830	836893
687	336957	837020	837083	837146	837209	837273	837336	837399	837462	937525
688	837585	837652	837715	837778	837841	837904	837967	838030	838093	838156
689	838219	838282	838345	838408	838471	838534	838597	838660	83 723	838786
690	838849	838912	838975	839038	839101	839164	839227	839289	839352	839415
691	839478	839541	839604	839667	839729	839792	839855	839918	839981	8-0043
692	840106	840169	840232	840294	840357		840482	840545	840608	840671
693	840733	840796	840859	840921	840984	841046	841109	841172	8:1234	841297
694	841359	841422	841485	841547	841610	841672	841735	841797	841860	841922
695	841985	842047	842110	842172	842235	842297	842360	842422	842484	842547
696	842609	842672	842734	842796	842859	842921	842983	843046	843108	843170
697	843233	843295	843357	843420	843482	843544	843606	843669	843731	843793
698	843855	843918	843980	844042	844104	844166	844229	844291	844353	844415
699	844477	844539	844601	844663	844726	844788	844850	844912	844974	845036
700	845098	845160	845222	845284	845346	845408	845470	845532	845594	845656
701	845718	845780	845842	845904	845966	846028	846090	846151	846832	846275 846893
702	846337	846399	846461	846523	846585	846646	847326	846770	847449	847511
703	846955	847017	847079 847696	847141	847819	847881	847943	848004	848066	848127
704	847573	847634					848559	848620	848682	848743
705	848189	848251	848312	848374	848435	848497	849174	849235	849296	849358
706	848805	848866	848928	848989 849604	849051	849726	849788	859849	849911	849972
707	849419 850033	849481	850156	850217	850279	850340	850401	850462	850524	850585
708	850646	850707	850769	850830	850891	850952	851014	851075	851136	851197
709		851319	851381	851442	831503	851564	851625	851686	851747	851808
710	851258 851870	851931	851992	852053	852114	852175	852236	852297	852358	852419
711	852480	852541	852602	852663	852724	852785	852845	852907	852968	853029
712 713	853089	853150	853211	853272	853333	853394		853516	853576	853637
714	853698	853759	853820	853881	853941	854002	854063	854124	854184	854245
	854306	854367	854427	854488	854549	854610	854670	854731	854792	854852
715 716	854913	854974	855034	855095		855216	855277	855337	855398	855459
717	855519		855640	855701	855761	855822	855882	855943	856003	856064
718	856124		856245	856306	856366	856427	856487	856548	856608	856668
719	856729		856850	856910	856970	857031		859151	857212	857272
720	857332	857393	857453	857513	857574	857634		857754	857815	857875
721	857935	857995	858056	858116	858176	858236	858296	858357	858417	858477
722	858537	858597	858657	858718		858838		858958	859018	859078
723			859258	859318		859438		859559	859619	859679
724	859739	859798	859858	859918		860038		860158	860218	860278
725	860338		860458	860518		860637			860817	860877
726	860937	860996	861056	861116		861236	361295		861415	
72.7	851534		861654	861714					862608	
728	862131		862251	862310		862430			863204	
729	862727	862787	862847	862906			6		8	-
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No.	0	1	2	3	4	55_	6	7_7_	8	1 9
730	863323	863382	863442	863501	863561	863620		363739	863798	
731	863917	863977 864 5 70	864036	864096	864155	864214		864333		
732	865104	865163	865222	865282	864748	864808		864925		
733 734	865696	865755	865814	865873	865933	865992	865459	865518	1865578	865637
	866287	866346	866405	866465	866524	866583			1	665218
735 736	866878	866937	866996	367055	867114	867173		866701	866760	
737	867467	867526	867585	867644	867703	867762	867821	867880		867409
738	868056	868115	868174	868233	868292	868350	868409	868468	868527	868586
739	868644	868703	868762	868821	868879	868938	868997	869056	869114	869173
740	869232	869290	869349	869408	869466	869525	869584	869642	869701	869760
741	818698	869877	869935	869994	870053	870111	870170	870228	870287	870345
742	870404	870462	870521	870579	870638	870696	870755	870813	870872	870930
743	870989	871047	871106	871164	871223	871281	871339	871398	1871456	871515
744	871573	871631	871690	871748	871806	871865	871923	871981	872040	872098
745	872156	872215	872273	872331	872389	872448	872506	872564	872622	872681
746	872739 873321	872797 873379	872855	872913	872972	873030	873088	873146	873204	873262
747 748	873902	873960	873437 874018	873495 874076	873553 874134	873611 874192	873669	873727	873785	873843
749	874482	874540	874598	874656	874714	874772	874830	874308 874887	874366	874424
	875061	875119	875177	875235	875293	875351	875409	875466	874945	875003
750 751	875640	875698	875756	875813	875871	875929	875987	876044	875524 876102	875582 876160
752	876218	876276	876333	876391	876449	876506	876564	876622	876680	876737
753	876795	876853	876910	876968	877026	877083	877141	877198	877256	877314
754	877371	877429	877486	877544	877602	877659	877717	877774	877832	877889
755	877947	878004	878062	878119	878177	878234	878292	878349	878407	878464
756	878522	878579	878637	878694	878751	878809	878866	878924	878981	879038
757	879096	879153	879211	879268	879325	879383	879440	879497	879555	879612
758	879669	879726	879784 880356	879841 880413	879898	879956	880013	880070	880127	886185
7 <u>59</u> 760	880814		880928	880985	880471	880528	880585	880642	880699	880756
761	881385	881442	881499	881556	881613	S81099 881670	881156	881213	881270	881328
762	881955	882012	882069	882126	882183	882240	881727	881784	881841	881898
763	882524	882581	882638	882695	882752	882809	882866	882923	882980	882468 883036
764	883093	883150	883207	883264	883321	883377	883434	883491	883548	\$83605
765	883661	883718	883775	883832	883889	883945	884002	884059	884115	884172
766	884229	884285	884342	884399	884455	884512	884569	884625	884682	884739
767	884795	884852	884909	884965	885022	885078	885135	885191	885248	885305
768	885361	885418	885474	885531	885587	885644	885700	885757	885813	885870
769	885926	885983	886039	886096	886152	886209	886265	886321	886378	886434
770	886491	886547	886603	886660	886716	886773	886829	886885	886942	886998
771	887054	887673	887167	887223	887280	887336	887392	887448	887505	887561
772	887617	888236	887730	887786 888348	887842	887898 888460	887955	888011	888067	888123
773 774	888741	888797	888853	888909	888965	889021	888516	888573	888629	888685
1/4	0	1	2	-				889133	889190	889246
	1	-	-	3 1	4	5	6	7 1	8	9

46			L	0 G 2	4 R I	THI	M S.			
No.	0	I	2	3	4	5	6	7 1	8	9
775	889302	88 358	889414	889470	889526	889528	889638	889694	889750	889806
7,6	889862	886918	889974	890030	890086	890141	890197	890253	890309	890365
777	890421	890477	890533	890589	890644	890700	890756	890812	890868	890924
778	890980	891035	891091	891147	891203	891259	891314	891370	891426	891482
779	91537	891593	891649	891705	891760	891816	891872	891927	891983	892039
780	892095	892150	892206	892262	892317	892373	892428	892484	892540	892595
781	892651	892707	892762	892818	892873 893429	892929 893484	89298 5 893540	893040 893595	893096	89 3151 893706
782 783	893207	893262	893873	893928	893984	894039	894094	894150	894205	894261
784	894316	894371	894427	894482	894538	894593	894648	894701	894759	894814
785	894870	894925	894980	895036	895091	895146	895201	895257	895312	895367
786	895422	895478	895533	895588	895643	895699	895754	895809	895864	895919
787	895975	896030	896085	896140	896195	896251	896306	896361	896416	896471
788	896526	896581	896636	896691	896747	896802	896857	896912	896967	897022
789	897077	897132	897187	897242	897297	897352	897407	897462	897517	897572
790	897627	897682	897737 898286	897792	897847	897902	897957	898012	898067	898122
791	898176	898231	898286	898341	898396	898451	898506	898561	898615	898670
792	898725	898780	898835	898890	898944	898999	899054	899109	899164	899218
793	899273	899328	899383	899437	899492	899547	899602	899656	899711	899766
794	899820	899875	899930	899985	900039	900094	900149	900203	900258	900312
795	900367	900422	900476	900531	900586	900640	900695	900749	900804	900858
796	900913	900968	901022	901077	901131	901186	901240	901295	901349	901404
797	901458	901513	901567	901022	902220	901/31	901/05	902384	902438	902492
798	902547	902601	902655	902710	902764	902818	902873	902927	902981	903036
799 800	903090	903144	903198	903253	903307	903361	903416	903470	903524	903578
801	903632	903687	903741	903795	903849	903903	903958	904012	904066	904120
802	904174	904228	904283	904337	904391	904445	904499	904553	904607	904661
803	904715	904770	904824	904878	904932	904986	905040	905094	905148	905202
804	905256	905310	905364	905418	905472	905526	905580	905634	905688	905742
805	905796	905850	905904	905958	906012	906065	906119	906173	906227	906281
806	906335	906389	906443	906497	906550	906604	906658	906712	606766	906820
807	906873	906927	906981	907035	907089	907142	907196	907250	907304	907358
808	907411	907465	907519	907573	907626	907680	907734	907787	907841	907895
809	907948	908002	908056	908109			-	908324	908914	908967
810	908485	908539	908592	908646	908699	908753	908807		900914	900907
811	909021	909074	909128	909181	909235	909288	909342	909395	909449	910037
812	909556	910144	910197	910251	910304	910358	910411	910.164	910518	910571
814	910624	910678	910731	910784	910838	910891	910944	910998	911051	911104
815	911158	911211	911264	911317	911371	911424	911477	911530	911584	911637
816	911150	911743	911797	911850	911903	911956	912009	912063	912116	12169
817	912222	912275	912328	912381	912435	912488	912541	912594	912647	91270C
818	912753	912806	912859	912912	912966	913019	913072	913125	913178	913231
819	913284	913337	913390	913443	913496	913549	913602	913655	913708	913701
-	0	I	2	3	4	5	6	7	8	9

1										
No.		1	2	3	4	5	6	7	0	9
12	913 14	913867	913920	913973	914026	914079	914131	914184	914237	914200
521	914343	914396	914449	914502	914555	914608	914560	914713	914706	914819
822	914872	914925	914977	915030	915083	915136	915189	915241	915294	915347
823	915400		915505	915558	915611	915664	915716	915769	915822	915874
824	915927	915980	916033:	916085	916138.	916191	916243	916296	916349	910471
325	916454	91650	916550	916612	916664	916717	910770	910822	916875	915627
826	916980	917033	917085	917138	917190	917243	917295	917348	917400	917453
827	917505	917558	917610	917663	917715	917768	917820	917873	917925	917978
828	918030	918083	918135	918188	918240	918292	918345	918397	918450	918502
829	918554	918607	918659	918712	918764	918816	918869	918921	918973	919026
830	919078	919130	919183	919235	919287	919340	919392	919444	919496	919549
831	919601	919653		919758	919810	919862	919914	919967	920019	
832	920123	920175	920228	920280	920332	920384	920436	920489		9 0593
833	920645	920697	920749	920801	920853	920900	920958	921010	921062	921114
834	921166	921218	921270	921322	921374	921426	921478	921530	921582	921634
835	921686	921738	-	921842	921894	921940	921998	922050	922102	922154
336	922206	922258	922310	922362	922414	922466	922518	922570	922622	922674
837	922725	922777	922829	922881	922933	922985	923037	923088	923140	923192
838	923244	923296	923348	923309	923451	923503	923555	923507	923658	923710
839	923762	923814	923865	923917	923969	924021	924072	924124	924176	924228
840	924279	924331	924383	924434	924486	924538	924589	924641	924693	924744
841	924796	924878	924899	924951	925002	925054	925106	925157	925209	925260
842	925312	925364	925415	925467	925518	925570	925621	925673	92572+	925776
843	925828	925879	9259 (1	925982	926034	926085	926137	926188	926239	926201
844	926342	926394	926445	926497	926548	926600	926651	926702	926754	926805
845	926857	926908	926959	927011	927062	927114	927165	927216	927268	927319
846	927370	927422	1	927524	927576	927627	927678	927730	927781	927832
847	927883	927935		928037	928088	928140	928191	928242	928293	928345
848	928396	928447	928498	928549	928601	928652	928703	928754	928805	928856
849	928908	928959	929010	929061	929112	929163	929214	929266	929317	929368
850	929419	929470	929521	929572	929623	929674	929725	929776	929827	929878
851	929930	929981		930083	930134	930185	930236	930287	93=338	930389
852	930440	930491	930541	930592	930643	930694	930745	930796	930847	930898
853	930949	931000		931102	931153	931203	931254	931305	931356	93140
854	931458	931509	931560	931610	931661	931712	931763	931814	931864	931915
855	931966	932017	932068	632118	932169	932220	932271	932321	932372	932423
856	932474	932524	1.0	932626	932677	932727		932 29	932879	
857	932981	933031	933082	933133	933183	933234		933335	933386	93343
858	933487	933538	933588	933639	933690	933740	933791	933841	9 13892	
859	933993	934044	93+094	934145	934195	934246	934296	934347	934307	9 1 1448
860	934498	934549	934500	934650	93 700	934751	934801	234852	934 2	9319-1
861	935003	935054		935154	935205	935255	935306	935 156	9354	13,45
862	935507	935558		035658	135,09	935759	935809	935860	935910	3596
863	936011	930061	936111	036162	93/12/2	1,6262	936 13		926413	9364 .
864	936514	93 564	93661	936664	936-15	936765	936815		9 0016	= 3011/6
1	0	1	2	3	4	5	6	7	8	9
Common	-		DESCRIPTION OF THE PARTY NAMED IN	-	-	-	-	Line and the last	ACCRECATE VALUE	C)

‡8			L	O G	A R 1	THI	M S.			
No.		I	2	3	4	5	6	_ 7	8	9
365			937116	937167	937217	937267	937317	937367	937418	937468
366	937518		937618	937668	937718	937769	937819	937869	937919	937969
867	938019	938069	938119	938169	938219	938269	938319	938370	938420	938470
368 869	938520	938570	938620	938670	938720	938770	938820	938870	938920	938970
870	939020	939070	939120		939220	939270	939319	939369	939419	939469
871	939519	939569	939619	939669	939719	939769	939819	939868	939918	939968
872		940566	940616	940666	940716	940765		940865	940417	940964
873	941014	941064	941114	941163	941213	941263	941313	941362	941412	941462
874	941511	941561	941611	941660	941710	941760	941809	941859	941909	941958
875		942058	942107	942157	942206	942256	942366	942355	942405	942454
876	942504	942554	942603	942653	942702	942752	942801	942851	942900	942950
877	943000	943049	943099	943148	943198	943247	943297	943346	943396	943445
878	943494	943544	943593	943643	943692	943742	943791	943841	943890	943939
879		944038	944088	944137	944186	944236	944285	944335	944384	944433
880		944532	944581	944631	944680	944729	944779	944828	944877	944927
881		945025	945074	945124	945173	945222	945272	945321	945370	945419
883		945518	945567	945616	945005	945715	945764	945813	945862	945911
882	946452	946501	946550	946600	946649	946698	946747	946796	496845	946894
88		946992	947041	947090	947139	047189	947238	947287	947336	947385
888	947434	947483	947532	947581	947630	947679	947728	947777	947826	947875
882		947973	948021	948070	948119	948168	948217	948266	948315	948364
888	948413	948462	948511	948560	948608	948657	948706	948755	948804	948853
886		948951	948999	949048	949097	949146	949195	949244	949292	949341
890	949390	949439	949488	949536	949585	949633	949683	949731	949780	949829
89:	949878	949926	949975	950024	950073	950121	950170	950219	950267	950316
89:		950413	950462	950511	950560	950608	950657	950705	950754	950803
-89	3 950851	950900	950949	950997	951046	951095	951143	951192	951240	951289
89.	951337	951386	951435	951483	951532	951580	951629	951677	951726	951774
89		951872	951920	951969	952017	952066	952114	952163	952211	952259
89		952356	952405	952453	952502	952550	952599	953131	953180	952744
89		953325	953373	953421	953470	953518	953566	953615	953663	953711
89		953808	953856	953905	953953	954001	954049	954098	954146	954194
90		954291	954339	954387	954435	954484	954532	954580	954628	954677
90		954773	954821	954869	954918	954966	955014	955062		955158
90	2 955206	955255	955303	955351	955399	955447	955495	955543	955591	955640
90	3 955688	955736	955784	955832	955880	955928	955976	956024	956072	956120
90			956264		956360	956409	956457	956505	956553	956601
90		956697	956744			956888	956936	956984	957032	957080
90		957176	957224		957320	957368	957416	957464	957511	957559
30	7 957607	957655			957799	957847	957894	957942		958038 958516
90				958229	958277	958325		958420	958468	958994
90	330304	950012	2	3	930/33	5	930030	7	1 8	930994
-		i i	1 4	1 3	-	1)				CONTRACTOR OF THE PARTY OF THE

ł											77
1	No.	0	I	2	_ 3	4	_ 5	6	7	8	9
ı	910	959041	959089	959137	959184	959232	959280	959328	959375	959423	959471
1	911	959518	959566	959614	959661	959709	959757	959804	959852	959900	957947
	912	959995	960042	960090	960138		960233	960280	9611328	960376	960423
ı	913	960946	960518	960566	960613		960708	960756	960804	960851	96089
	914	-	960994	961041	961089		961184	961231	161279	961326	961374
	915	961421	961468	961516	961563		961658	961706	961753	961801	961848
ı	917	962369	961943	962464	962038	962085	962132	962180	962227	962275	962322
п	918	962843	962890	962937	962985	963032	953079	963126	963174	963221	963261
	919	963315	963363	963410	963457	963504	963552	963599	903646	963693	263741
	020	963788	963835	963882	963929		964024	964071	964118	964165	951212
	221	961260	964307	964354	964.101	964448	964495	964542	964590		96,684
	922	964731	964778	954825	964872	964919	964966	965013	965060	965108	965155
	923	965202	965249	965296	965343	965390	965437	965484	965531	965578	965625
	924	965672	965719	965766	965813	965860	965907	965954	966001	966048	966095
	925	966142	966189	966235	966283	966329	966376	966423	966470	966517	966564
ı	926	966611	966658	956705		966798	966845	966892	966939	966986	167033
	927	967080	967127	967173	957220	967267	957314	967361	967408	967454	967501
ı	928	967548	967595	967642	967688	967735	967782	967829	967875	967922	967969
	929	963016	968062	968109	968156		968249	968296	968343	968389	
	930	968483	968530	968576	968623		968716	968763	968810	968856	968903
ı	931	968950	968996	969043	969090		969183	969229	969276	969323	969369
ı	932	969416	969462	969509	969556	969602	969649	969695	969742	969788	969835
	934	970347	979393	970440	970486		970114	970161	970207	970254	970300
	935	970812	970858	970904	970951	970997	Andrew Commercial	STREET STREET,			
	935	971276	971322	971369	971415		971044	971090	971137	971183	971229
	937	971740	971786	971832	971879		971971	972018	972064	972110	972156
	938	972203	972249	972295	972342	972388	972434	972480	972527	972573	972619
	939	972666	972712	972758	972804	972851	972897	972943	972989	973035	973082
	940	973128	973174	973220	973266	973313	973359	973405	973451	973497	973543
	941	973590	973636	973682	973728	973774	973820	973866	973913	973959	974005
	942	974051	974097	974143	974189	974235	974281	974327	974373	974420	974466
	943	974512	974558	974604	994650		974742	974788	974834	974880	974926
	944	974972	975018	975064	975110	975156	975202	975248	975294	97534¢	.)753861
	945	975432	975478	975524	975570	975616	975661	975707	975753	975799	97584=
	946	975891	975937	975983	976029		976121	976166	976212	976258	
	247	976350	976396	976442	976487		976579	976625	976571	9,6717	97676.
	948	976808	976854	976,00	976946		977037	977683	977129		977220
	949		977769	977815	977403		977495	977541	977586	977672	977678
	950 951	977724	978226	977015	977861	977906	977952	977908	978043	978089	9,8135
	952	97863	978683	978728	978774	978819	978365	978454	978550	979602	978591
	953	979093	979138	979184	979230	9-9275	979321	979366	979412	979457	979047
	954	979548	979594	979639	979685		979776	979821	979867	979912	979958
		0	1	2	3	-4	5	6	7	- 8	9
ı	-	-	-	APPENDANCE OF THE PERSON NAMED IN	Name and Address of the Owner, where the Owner, which is t	The same of the sa	MINISTER PROPERTY.	-	Sufficient and Street	CONTRACTOR OF THE PERSON NAMED IN	STATE OF THE PARTY

D.C. Bar				,			1	7	,		
There	No.	The same of the sa	1	2	3_	4	5	6	7_	8	9
- Falls	955		980049	980094	980140	980185	980231	980276	680322	980367	980412
ı	956		980503		980594		980685		1980776	1980821	930867
1	257	980912	980957	981003		981093	981139			981275	981320
1	958	981365	981411	1981456	981501		981592	981637	931683	981728	981773
1	959	981819	981864		981954	982000	982045	982090		982181	982226
1	960	982271	982316	982362	982407	982452	982497	982543		982633	982678
200	961	982723	982769		982859	982904	982949	982994	983040	983085	983130
ĕ	962	983175	983220	983265	983310	983356	983401	983446	983491	983536	983581
ı	963	983626	983671	983716	983762	983807	983852	983897	983942	983987	984032
ă	964	984077	984122	984167	984212	984257	984302	984347	984392	984437	984482
	965	984527	984572	984617	984662	984707	984752	984797	984842	984887	984932
1	966	984977	985022	985067	985112	985157	985202	985247	985292	985337	985382
1	467	985426	985471	985516	985561	985606	985651	1985696	985741	985786	985830
	958	985875	985920	985965	986010	986055	986100	986144	986189	986234	986279
	969	986324	986369		986458	986503	986548	986593	986637	986682	986727
1	970	986772	986816	986861	986906	936951	986995	987040	987085	987130	987174
	971	987219	987264	987309	987353	987398	987443	987587	987532	987577	987622
	972	987656	987711	987756	987800	987845	987890	987934	987979	988024	988068
	973	988113	988157	988202	988247	988291	988336	988381	988425	988470	988514
Į.	974	983559	988603	988648	983693	988737	988782	988826	988871	988915	988950
	975	989005	989049	989094	989138	989183	989227	989272	989316	989361	989405
	976	989450	989494	989539	989583	989628	989672	989717	989761	989806	989850
	977	989895	989939	989983	990028	990072	990117	990161	990206		990294
	978	990339	990383	990428	990472	990516	990561	990605	990650	990694	990738
	979	990783	990827	990871	990916	990960	991004	991049	991093	991137	991182
19	980	991226	991270	991315	991359	991403	991448	991492	991536	991580	991625
1	186	991669	991713	991757	991802	991846	991890	991934	991979	992023	992067
15	82	992111	992156	992200	992244	992288	992333	992377	992421	992465	992509
9	83	992553	992598	992642	992686	992730	992774	992818	992863	992907	992951
	984		993039	993083	993127	993172	993216	993260	993304	993348	993392
	85		973480	993524	993568	993613	993657	993701	993745	993789	993833
	86		993921	993965	994009	994053	994097.	994141	994185	994229	994273
1	87		994361	994405	994449	994493	994537	994581	994625	994669	994713
	88		994801	994845	994889	994933	994977	995021	995064	995108	995152
ш	989		995240	995284	995328	995372	995416	995450	995504	995547	995591
	990		995679	995723	995767	995811	995854	995898	995942	995986	996030
	991		996117	996161	996205	996249	996293	996336	996380	996424	996468
	92		996555	996599	996643	996687	996730	996774	996818	996862	996905
	93		996993	997037	997080	997124	997168	997212	997255	997299	997343
36	194		997430	997474	997517	997561	997605	997648	997692	997736	997779
	195		997867	997910	997954	997998	998041	998085	993128	998172	998216
	196		998303	998346	998390	998434	998477	998521	998564	998608	998652
	97		998739	998782	998826	998869	998913	998956	999000	999¢43	999087
	98		999174	999218	999261	999305	999748	999392	999435	999478	999522
	99	-				999739	999783	999826	999870	999913	999957
The same		0	1	2	3 1	4	5	6	7	8 1	9

A TRIANGULAR CANON LOG CULTIMICAL: or, A TABLE of Artificial size, Takes GENTS and SECANTS, the Radius 10.000000; and to every Degree of the Quantum.

			0 1	Jorna.							1 1	J. Peris			
Z	S no		Tang.		Sec nt.			2	Sac		Taoj.		- 011		
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C	6.463726	10.0001	6.463	. 3027	10.00	13 5362-4	59	0	8.241 5	97	Capital	1 7			1
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3	6.94084-		69147	1 5 1 2	1 .00	13.059153	100	3	2 111 3	9- 19-1	61111		access)	11211	170
4	7.061786		7.5657 0	11 83-14	10, 00 0	1 - 34214	56	4	8.26 1	4. 9=5	c 1	110		March 1975	
5	7.1 260	9 9 11 9	7,2118-	11.7 81.2	10. 00 0	12. 3 3 4	55	6	6.28624	9. 9 2.		3 7			
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9	7.41796		7.41-97		10,000002	12.5162-4	152		8.7C1 4	90 11		11.6 11.6			All I
11	7.463725	9.919 8	7 503120		1 .000002	12.494882			8. 114454			11.f8 5			All I
12	7.542006	0.9 9 07	7.112909	12 45 008	10,000003	12.45-093	48	12	8.321 27	9.99 90	1. 2 122	116-1-		11 - 111	Sing.
13	7-5-766		7.177673	12 425 3:8	10 000003	12.422732	47	13	8.327010	9.9 902	8.327114	11. 72	1	316	474
14		1.9 9 6	1.6 857	12 360143	10,0000 4	12.390147	40	14	8.332924	9. 59839		11. 4 5	1	116.1 -	1
16		9. 69995		12.300150	10.000000	12.332155	34	16	8.344 (C4	9.999999	8,34 610	11.6:0 4		11 6	174
17	6041-7	9.0100 5	7.6 4179	12.305821	10.000005	12.30 (827	43	17	8.350180	9-999891	8.350229	11.649710	1 000100	116	3 3
18	7-71 '99-	9.99994	7.78 003	12.280997	10,0000000	12.281003	42	18	8.355783	9.99 888	8.3:5505	11.644105	1 000115	11 6 40:	45.9
10	7.742477	9.515963	.7 4761	12.2:7516	10,000007	12.237522	41		8.761315	9.999835		11.6331 5	1 0 11		12.
20	78 5047	9.990093	7 78 - 51	12.114049	10.000008	12.334017	20	20	8.373171	9.999988 A	8.372201	11.627- 8	10.00-12		150
22	8-6145	9.90 01	7.806155	12,193845	10 000000	12.193854		22	8.3714 9	7.990876	8.377622	11.6223		11 6121L1	12
23	7.825451		7.82 0460		10.000010	12.174549		23	8.382-62	9.969873	8.3 . 809	11.617111 11.6119ch	12. 0019		13.5
24		9 999 59	- 843 44	12.118326	10,000011	12.138:38	36	24	8.393101		-	11.66-16			1304
26		9.990938	7 8-8708		10 000011	12.130530		25	8.398170			11.6.1685	1=,600136	11.6 1 21	131
27	7.895085	9 950987	7.895000	12.104001	10.000013	12.104915	32	27	8.403190	9.999361	8.40 338	11.596662	1 0130	11.196801	
28	7.910879	9.009986	7-91 14	12.071866	10 000014	12.C801 1	32	18	8 408161	9.094858		11.50166		11.5 18:0	100
29	7.926119	9.916984		-	10.000016	12.073581		29	8-417010	9.999854		11.481012		11. (52 81	120
30		9 900082		12.044900		12.050158		30 11	8.4217919			11.5771.1		11.5-2 7	20
30	7.068870	9.500081	- 96888a	12 031111	10.000019	12.031130	28	32	8.4.7462	0.900844	8.427618	11.5727 2		11.12538	
33		9.90.0080		12.004781	10,000020	12.004802	2-	33	8-471156			11.56,038	10 (00162		16
34	8.007-87	9-999979	8.00-800	11 992 191	10.000021	11.992213		34	8.441304	9.999836		11.508440		11.358666	12
36	8.020028	9.969976	8.0.0044	11.97995:	10.000022	11.992213	24	35	8.41 (541	9.900831	8.446110	11.5:3840	10.ccosto	11.45404	
37	8.031919	9-990975	8.011066	11.0680;5	\$10,0000a5	11.968080		37	8.450440	9.990827	3.450613	TI \$4038-	10-10-10-9	11.54 560	
33	8.043501		8.043517	11.956423	10.000 26	11 956499		38	8.459301	9-999810		11.514.30	10 000176		12
30 40	8.06 27-6		8 06 3 6	11.934194	10.000010	11.934224		39		9.996816		11.536151	10 000194	11.536325	20
41		9.999960	8.0-6 533	11 9 . 3460	10.000031	11.923500		18	4.4679Sc	9.999812	8.4681-2	11 551827	1 .0001	11 532014	
42	18.0S6g6=	9.900068	8.086967	11. 13003	10,000 32	11.913035		42		9.909839		11.52-546	1 .0.01 1	11 52"73	13
43	8.107163	9.999966	8.10-262	11.502783	10.000034		17	43	3.4 6604	9.005801	8-276603 3 48 892	11 523300	10.000104	11.51000	16
14		9.990963			10 000037	11.883074	7.	4-		9.909767		17 011940	102 3	11.01 1 2	10
46	8.126471	9.999961	8.126510	11.8-3490	10.00030	11.8-3529	14	16	3.488667	9.909793	8.4801-0	11 51 8;0	doctors. 1	11.011 9"	14
47	8.135810	9.999939	8.13:851	11.864140	10 000041	11.864190	23	47	3.403040	9.90070	8.403250	11 406700		11.506-6	13
48 49	8.153907	9.909058	8.144996	11.826048	10.0000/2	11.846047	12	\$2 40	\$.4070-8	7 5 9786	8. 01248	11.4 870-		11 498910	
5		9.990054		11.837273	12 ccc 46	11.837319	10	100		9.9007~5	8 5 126-	TE 404733	10.0 172	11.4 4055	
51	8.171280	9-909952	8.1-1728	11.828672	10.ccne48	11.828720	0	12	9.5 8074	9.9:0 74	P. 500 100	11 4cc o		11.4 10:6	1.3
52	9.179713	9.9999950	8 17076;	11.810337	10.000010	11.920287	8	12	8. 41-867	9 01 076:		11.486 CZ	10, 07 6	18 ,83-74	
51 54	8,106102	9.999946	8 156156	11.50 844		11 801898	6	73 74	3.5 551	9.000761		11 47021	10. 01239		13
1 ::				11.7 5 74		11.70500	-	55	8.51.343	0.00 757	3.504:36	11 4"-414	7 01 7-3	11. 2. 12	1
56	8.211805	9.99904:	8 211053	11." 04"	10.00000	1193105	4	;6	8 5281 2	9.009754	3. 1.3.	1 171611	District of the last	11.1" . 5	1
5 S	8.219581	9.999040	8.219641	11.7 280;		11.78 A10	1 3	17	8	9.4009-48	8 1200 0	11 46- 1	British	11 464177	
50	9 234557	0.999936	8 274611	11.765329			1 2	150	8 52 1 6	19.00074	3 539042	11-4-5	200	11 6 1	1
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5	8.5428 9	9-999735	8.543084	11.456916	10.000265	11.457181	60	0	8.718800	9.999404	8.719396	11.380604	10.000596	11.281200	6
1	8.546422	9-991731	8.546661	11.453309	10.000269	11.453578	59	I 2	8.721204	9.999398	7.724203	11.278194	10.0006c2	11.278796	5
1	8.549995	9.999726	8.550268	11.446183	10.000273	11.450005	58 57	3	8.725972	9.999391	8.726588	11.273412	10.000616	11.274028	5
I	8 557054	9-969717	8.557336	11.442664	10.000283	11.442946	56	4	8.728337	9-999378	8.728959	11.271041	10.000622	11.271663	I
l	8 :60540	9 69:713	8.560828	11.439172	10.000287	11.439460	55	5	8.730688	9.999371	8.731317	11.268683	10 000629	11.269312	li
1	8. 563099		8 564201		10.000202	11.436001	54	6	8.733027	9.999364	8.733663	11.266337	IC-COC636	11.266973	I
1	8.567431	9.505744	8.571137	11.432272	10.000296	11.432569	53	3	8.735353	9.999357	8.735996 2.738317	11.264004	10.000643	11 264646	ŀ
ı	8.570836	9.999664	8.574520	11.425480	10.000306	11.425786	51	9	8.739969	9.999330	8.740626	11.259374	10.000657	11.260031	ł
U	8.577566	9.999689	8.577877	11.422123	10,000111	11.422434	50	10	8.742250	9-999336	8.742922	11.257078	10.000664	11.25 741	ľ
ì	8. 180892	9.0996851	8.681208	11.418792	20.000315	11.419108	49	H	8.744536	9.999329	8.745207	11.254793	10.000671	11.255464	۱
l	8.584193	9 959680	8.5845 4	11.415486	10.000320	11.415807	48	12	8.746801	9.999322	8.747479	11.252521	10.000686	11.253198	ŀ
ı	8.5957469	9.999675	8.587794	11.412206	10.000325	11.400270	47 46	13 14	8.751297	9 999308	8.751989	11.248011	10.000692	11.248703	l
١	8.5030.8	9.996665	8.554283	11 405717	10 000335	11.406052	45	扁	8.753528	9.099301	8.754227	11.245773	10.000600	11 246472	I
ı	8.597153	c.909660	8,597492	11-402508	10.000340	21.402848	44	16	8.755747	9 999204	8.756462	11.243547	10 000766	11.244253	ŧ
I	8.600332	9.999655	8.600677	11.399323	10.000345	11.399668	43	17	8.757955	9.999286	8.758668 8 76c872	11.241332	19.000713	11.239849	Ì
l	8.606633	9 999645	8.603839	11.396161	10.000350	11.396511	41	19	8.762337	9-999279	8.761065	11.239128	10.000728	11.239049	١
l	8.6:9734		8.6 0004	11.380cc6	10.000360	11.300266	40	20	8.764;11	9.999265	8.765246	11.234753	10.000735	11.235489	1
	8.612823	9.999635	8.617180	11.386811	10.000365	11.387176	39	21	8.766675	9.599257	8.767417	11 232582	10.000743	11.233325	1
I	8.61 (891	9.995620	8.616262	11.383738	10.000371	11 384109	38	22	8.768827	9.999250	8.769578	11.230422	10.000750	11.231172	ı
1	8.618937	9.559624	8.622243	11.380687	10.000376	11.381063	37 36	23	8.773101	9.999242	8.771727	11.226133	10.000758	11.226899	
I	8.624965		8.625352	11.374648	20,000386	11.375035	35	2.5	8.775223	9.000227	8.775995	11.224005	10.000773	11.224777	ı
1	8.627948	0.060608	8.628340	11.371660	10.000302	11.372052	34	25	8.777333	9 999220	8.778114	11.221386	10-000780	11.222667	1
1	8 630011	9.999603	9 631308	11.368692	10.000307	11.369089	33	27	8.779434	9.999212	8.780222	11.219778	10.000788	11.220566	
3	8.633851		8.634256	11.365744	10.000403	11 356146	32	28	8.781524	9-999205	8.782320	11.217680	10.000863	11.218476	
9	8.636776		8 637184		10.600408	11.160120	31	30	8.785675	0.909180	8.786486	11.213514	10.000311	11.214325	
2	8.639680	9.559586	8.642682	11.359907	10.000419	11.357437	30	31	8.787736	9.999134	8.788554	11.211446	10.000818	11.212264	1
3	8.645428	9.999575	8.644853	11.354147	10.000425	11.354572	28	32	18.739787	9.999174	8.790613	11.209387	10.000826	11.210213	
î	8.648274	9.999570	8.648704	11.351206	10.000430	11.348898	27	33	8.791828	9.999156	8.792662 8.794701	11.207338	10.000834	11.206141	
1	8.651102	9.909564	8.651537	11.348462	10.000430	11.346089	25	34	8-795881	9.999150	8.796712	11.201260	10.000850	11.204110	
6	8.653921		8.654532	11.342851	10.000442	11.343298	24	36	8.797804	9.999130	8.798752	11.201248	10.000858	11.202106	ı
7	8.659475	9.095547	8.659928	11.340072	10.000453	11.340525		37	8.799897	9.999134	8 8cc763	11.199237	10.000866	11.108108	I
8	8.662230	9-999541	8.662689	11.337311	10.000459	11.337770	22	38 39	8.801891	9.999118	8.802765	11.19/235	10 000882	31 1:6124	
9	8.667689	9.999535	8.658160	11.334567	10,000471	11.332311	20	39	8.805852	0.000110	8.806742	11.193258	10.000800	11.1041.8	1
C	8.670303	9.999524	8 670870	11.329130	10.000476	11.329607	10	41	8.807819	9.909102	8.808717	11.161283	10.000868	11.192181	
2	8.673080	9.999518	8.673563	11.326437	10.000482			42	8.809777	9.999104	8.81c683 8.812641	11.189317	10.000014	11.190223	
3	3.678405	9.599512	8.676239	11.323761	10.000494	11.324249	17	43 44	8.811726	9.999056	8.814589	13.185411	10.000914	11.186233	d
4	8.681043	9.599500	8.681544	11.318456	10.000500		15	45	8.815598	9.999069	8.816520	11.181471	10.000031	11.184401	4
ŝ	2.18:665		8.684172	11.315828	10.000506	11.316338	14	46	8.817522	9.999061	8.818461	11.181530	10.000939	11.182478	
7	8.686272	9.90048-	8.686784	11.313216	10 000513	31.313727	13	47	8.81c436 8.821342	9.999052	8.822298	11 179616	10.000947	11.17864	
3	8 (88863 S.601438	9-955481	8.689381	11.310619	10.000519	11.311135	12	43 49	S.S23240	9.999041	8.824205	11.175795	10.00064	11.176760	
9	8.602008	9.900460	8 694 529	11.305471	10.000531	11,306002	10	50	8.825130		8.826103	11.17:897	10.000073	31 174870	ı
	8.606543	19.099462	18.697081	11.302010	10.000537	11.303457	9	51	8.827011	9 999019	8.827092	11.172008	10.000981	11.172980	
2	8 699073	9.9194:6	18:695617	11.300283	10.000544		8	52	8.830740		8.829874	11.176 126	10.000990	11.171116	
3	8 - 015°9 S.704090	9.599450		11.297861 11.295353	10.000550	11.298417 17.295910	6	53 54	8.832607		8.833613	11.166387	10.001007	11.167393	
+	3.706577	9-999437		11.292860			1-	50	8.834456		8.833471	11.164529	10.001015	11.165544	
6	3,709049	9.990431	8-700618	11.250381	10.000560	11.200951	1 4	56	8.836297	9.998076	8.837321	11.162679		11.1613703	
-	3.711527			17.287917	10.000576		3	57	8.838130			11.160837			
3	3.7110 2	9.000411	8.714534	11.285465	10.000 82		1 2	50		0.998050	8.842824	11.15-179	10.001050	11.1583 6	5
	1 2 20 3	0 900404		11 280604			10	60					10.001059		S
	1.7:3800	Sine.	1 1.1.9350	Ta.g.		Se.ant.	M			Sinc.		Tang.		Secant.	

-	-			4 1	legrees.			-	-			5 /	leves.			-
	N	Sac	-	Tang.	1	Secant.		1	=	Sice		Targ	1	Sector.	1	-
	7. 10		9,41 8041	8 844644		10,0,1000		=	7.1		-					
	1	8.243534 8.845387 8.817181	9.948932	8.346455	11.153545	10.001033	11.150415	59	ı	8 94 5 2 5 6	9.0 8344	3.941952	11.05 (48	0 1	11.	line.
	3	8.843971	9.908414	8 3 : 056	11.14174	10.001086	11.152817	50	3	8.9431 4	90 31	3.9462	11.055148	10.0 16.	1. 6 6	
	4	8.850751	9.908396	8.8;123	11 148154	10. 01 95	11 149-49	56	4	8 946033	9.99 ,	8.949168	11.050832	10 17	1. 60 000	16
Н	6	8.8542,0	9.948878	8.855403	11.144597	10.001113	11.145,09	4	6	18.948874	9.59 272	13 950597	11.049.03	10.001727	11 (1 26	5
	8	8.8;7901	9.998869	8.558932	11.141068	10.001131	11.143951	53	7 8	8.950187	9.998266	3.952021	11.04797	10.001 34	11. 71	5 11 1
	9	8.8 59946	9.998860	8.862433	11.130314	10.00 140	11.140554	51	9	8.953100	9-498243	8.954856	11 043733	10.0 757	1 0 55 1	51
н	11	8,863-14	9.998811		11.135827	10.001168	11.136986	49	11	8.955896	9.998220	8.957677	11 041326	10.001780	11.0441 6	1
ı	13	8.56 454	5.998823	8.867632	11.132:68	10.001177	11.133545	48	13 13	3.9586-0	9.998197	8.960473	11.040925 11.030527	10.001791	11.042716	479
Н	14	8.868165	9.998813	8.869357	11.131649	10.001186	11.131835	46	14	8.960052	9 9981 4	8.963254	11.038134	10.001326	11.039048	4
н	16	8 871565	9-993-95	8.871770	11 127230	10.001205	11.128435	44	16	8.962801	9.998163	8.964679	11.035,61	10.00183	11.037199	44
	18	8.874918	9.998766	8.377849	11.123838	10.001224	11.125062	42	18	8.065534	9.008139	S.06-204	11.032606	1010 861	11.031330	1
	20	8.878185	9.998757	8.879919	11.122152	10.001234	11.123385	41 40	19	8.96 893 S 963249	9 998127	8.568-66	11.031234	10.001872	11.033107	4 t
	21	8.879949	9.998747	8 8812c2 8.881860	11.118798	10.001263	11.116051	39	2 E 2 E	8.969600	9.998092	8 9714 6	11.028504	10 001806	11.030,00	3
п	23	8.883258	9.998728	8.884530	11.115470	10.001272	11.116742	31	23	8.971618	9.998080	8.975660	11.025-91	10.001920	11 027-1	37
п	25	8,386542	9.998708	8.887833	11.112167	10.001292	11.1134.8	35	25	8.974962	9.948056	8.9-6406	11.023440	10.001932	11. 25 73	36
ı	26	8 888 174	9.998669	8.889476	11.110524	10.001301	11.111826	34	26 27	8 976293	9.998044	8.978248	11.021752	10.001968	11.023707	
- 1	28 29	8.893035	9.998679	8.891742	11.107258	10.001321	11.108 (79	32	28 29	8.978941 8.980259	9.998020	8.982251	11.019079	10.001980	11.011059	32
	30	8.894643	9.998659	8.895984	11.104016	10.001341	11.105357	30	30	8.981573	9.9 /- 906	8.983577	11.016423	10.002004	11.018427	3.
1	31	8.896245	9.998649	8.897596	11.102404	10.001361	11.103754 11.1021 8	28	33 12	8 982883	9-997984	8.984899	11.013783	10.002016	11.017117	29
ł	4	8.899432	9.998629	8.900803	11.099197	10.001381	11.100,68	27 26	33 24	8.986491	9-997947	8.987531	11.011158	10.002041	11.014500	27
1	35	8.902505	9.998609	8.903987	11.096013	10.001301	11.097404	25	35	8.985083	9-997935	8,990149	11.009851	10.002065	11.011917	25
1	36 37	8.904168 8.905736	9.998589	8.905570	11.094430	10.001401	11.095831	24	36 37	8.989374 8.990660	9.997910	8.991451	11.008549	10.002078	11.010626	24
1	38	8.9c7297 8.9c8853	9.098578	8.908719	11.091281 11.089715	10.001422	11.092702	22 21	38 39	8.691943	9.997885	8 994045	11.004663	10.002102	11.00905*	22
1	40	8.910404	9.998558	8.911846	11.088154	10.001442	11.089596	20	40	8 994497	9-997872	8 996624	11.003376	10.002127	11.005503	20
н	41	8.913488	9.698537	8.914951	11.:85040	10.001463	11.086512	18 10	41 42	8.995768	9.997847	8.997908	11.000812	10.002153	11.002964	19 13
	43	8.915022	9.998527	8.916495	11.083505	10.001473	11.083450	17 16	43 44	8.999559	9.997835	9.000465	10.998262	10.001178	11.000440	17 16
п	45	8.918073	9.998506	8.621096	11.080432	10.001494	11.081927	15	45 46	9.002660	9.997869	9.003007	10.996993	10.001191	10.999184	豆
	47	8.921103	9.998485	8.924136	11.077381	10.001515	11.078807	13	47 48	9.003318	9.997784	9.005734	10.594,66	10.002216	10.996682	Ħ
п	48 49	8,024112	9.998464	8.925649	11.074351	10.001536	11.07 (885	11	49	9.005805	9.997758	9.008047	10.001053	10.003842	10-004195	ш
	50 51	8.925609	9.998453	8.917156	11.071341	10.001547	11.074391	10	51	9.007044	9.997745	9.010346	10 950702	10.002257	10.992956	10
ı	52	8.928587	9.998431	8.930155	11.060845	10.001568	11.071413 11.060932	8	53	9.009510		9.011790	10.988210	10021\$1	10.950490	1
ı	54	8.931544	9.998410	8.933134	11.066866	10.001590	11.068456	6	14	9.011962	9.997693	9.014268	10.985732	10 002 3=7	10 988038	6
	55	8.933-15	9.9¢8399 9.9£8388	8.934616	11.063907	10.001613	11.065519	5	56	9.013182	9.597680	9.015502	10.983267	10,002324	10.08,600	5
	57	8.935942	9.998377	8.937565	11.062475	10.001623	11.c64058	3	57	9.016824	9-997654	9.017959	10.982041	10.002346	10. 386	3 2
	59	8.938850	9.998355	8.940494	11.050506	10.001645	11.061150	1	50	9.018031	9.997618	9.020403	10.979597	10,602372	10.981960	1
	=	34 200	Sine	34.42.	Tang.		Secant.	М			Sine	,	Tang.		Secant.	M
N				85 1	Degrees.							84	Degrees.			

_			6 L	egrees.							7 1	egrees.			-
Min.	Sine.		Tang.		Secant.			Min.	Sine		Tang.		Secant.		1
0	9.019235	9.997614	9.021620	10.978380	10.002386	10.980765	6c	0	9.085804	9.996751	9.089144	10.910856	10,003249	10.914105	60
1	9.020435	9.997601	9.022834	10.977166	10.002399	10.979565	59 58	1 2	9.086922	9.996735	9.090187	10.909813	10.003265	10.913078	59
3	9.021032	9.997500	0.025251	10.674749	10.002426	10.977175	57	3	9.088970	9.996704	9.092265	10.907734	10.003296	10.911030	58
4	9.024016	2.997561	0.026455	10.973545	10.002439	10.975084	56	4	9.089990	9.996688	9.093302	10,506698	10.003312	10.910010	56
5	9.025203	9-997547	9.027655	10.972345	10.002452	10.974797	55	5	9.091008	9.996673	9.094335	10.905664	10.003327	10.908992	55
0	9.026386	9-997534	9.028852	10.971148	10.002466	10.973613	54	6	9.092024	9-996657	9.095367	10.904633	10.003343	10.907976	54
8	9.028744	9.997507	9.031237	10.968763	10.002403	10.971256	52	8	9.094047	9.996625	9.097422	10.002578	10.003375	10.905953	53 52
9	9 029918	9.997493	9.032425	10.967575	10.002507	10.970082	51	9	9.035056	9.996610	9.098446	10.901554	10.003390	10.904944	51
10	9.031089		9.033609	10.966391	10.002520	10.968911	50	10	9.096061	9.996594	9 099468	10,500532	10,003406	10.903938	50
11	9.032257	9.997466	9.034791	10.065209	10.002548	10.0667743	49	11	9.093065	9 996578	9.100487	10.899513	10.003422	10.902935	49 48
13	9.034582	9.997439	9.037144	10.962856	10.002561	10.665417	47	13	9.099065	9.996546	9.102519	10.897481	10.003454	10,900935	47 8
1.5	9.035741	9.997425	9.038316	10.561684	10.002575	10.964259	46	14	9.100062	9.996530	9.103532	10.896468	10 003470	10.899938	46
15	9.036896	9-997411	9.039485	10.560515	10 002589	10.963104	45	15	9 101056	9.996514	9.104542	10.895458	10.003486	10.898944	45
17	9.038048	9-997397	9.040651	10-959:49	10.002603	10.960802	44	16	0.102048	9.990498	9.105550	10.893444	10.003502	10.897952	1125
18	9 040342	9.007360	9.042973	10.957027	10.002631	10.959658	42	18	9.104025	9.996465	9.107550	10.892441	10.002524	10.80:076	1025
19	9.041485		9.044130	10 955870	10.002645	10.958515	41	19	9.105010	9.996449	9.108563	10.891440	10.003551	10.894990	41
20	9 042625	9-997341	9.04528;	10.954716	10.002659	10.957375	39	20	9.105992	9.996433	9.109559	10,800441	10.003567	10.8:4008	
23	9.044895	9.997327	9.0464.34	10.953500	10.00267	10.955238	38	22	9.107951	9.996400	9.111551	10.888440	10.003600	10.892049	39
23	9-046026	9.9972 9	9.048-27	10.951273	10.002701	10.953474	37	23	9.108927	9.996384	9.112543	10.887457	19:003616	10.801073	37
24	9 047 154	5.997285	9.049869	10.950131	10 002715	10.952846	36	24	9.109901	9.996368	9.113533	10.886467	10.003632	10.890099	36
25	9.048279	9-997271	9.051003	10.948992	10.002729	10.951721	35	25 26	9.110873	9.996351	9.114521	10.885479	10.003649	10.889127	35
27	9 049400	9.597257	9-052144	10.946723	10.002758	10.950599	34	27	9.111042	9.996318	9.116491	10.883500	10.003682	10.887191	34
38	9.051635	9.997228	5.054407	10.045593	10 002772	10 648 365	32	28	9.113774	9.996303	9-117472	10.882528	10.003698	10.886226	32 2
29	9.002748	9-997214	5.5522	10.944465	10.002786	10.947251	31	29	9.114738	9.996285	9 118452	10.581548	10.003715	10.885263	
30	9.053859	9.997189	9.0,66:9	10.943340	10.002801	10 946141	30	30	9.115698	9.996269	9.119429	10.880571	10.003731	10 884302	30
32	9 056071	9.997170	9 053000	10.042219	10.002830	10,945034	28	31	9.117612	9.996235	9.121377	10.878623	10.003745		
33	9.057172	9.997156	9.060016	10.039184	10.0 2 41	10.942828	27	33	9.118567	9.996218	9.122348	10.877652	10.003781	10.881422	27
3+	9 058271	9-997141	9.061130	10.938870	10.002359	10.941729	26	<u>34</u>	9.119519	9.996202	9.123317	10.876683	10.003789	10.380481	
36	9.059367	9.997127	9.062240	10.937760	10.002838	10.930633	25	35	9.120469	9-996188	9.124284	10.875716	10.003815	10.878531	25
37	9.061551	9.997098	9.064453	10.9355:7	10.002302	10 938449	23	37	9.122362	9.996151	9 126201	10.873789	10.003849	10.877628	23
33	052639		9 065:56	10.934444	10.002917	10 937361	22	38	9-123306	9.996134	9.127172	10.872818	10.003866	10.876694	22
39	9.063723	9.997068	9.067655	10.032248	10.002932	10.936276	21	39 40	9.124248	9.996117		10.870913	10.003883	10.875752	
40	9 06 5885	(+397039	9.007752	10.932218	10.002946	10.935194	10	41	0.126125	9.996083	9.129087	10.869950	10.003917	10.874813	19
42	8.066.62	9 997024	9.069038	10.930662	10.002976	10.933038	18	42	9.127060	9.996066	9.130994	10.860co6	10:003934	10.872949	18
43	9.068036	9.997009	9.071027	10.928673	10.002006	10.931964	17	43	9.127093	9-996049	9 131944	10.868056	10.003951	10.872007	17
44	9.070176	9-99(979	9.073197	10.026302	10.003888	10.929824	15	45	-	9.996:15	9.132839	10.866161	10.003985	10.870146	
46	9.071242	9.996964	9 074278	10 925722	10.003036	10.928758	14	46	9.130781	9.995908	9.134783	10.86 5216	10.004002	10.860210	14
47	9-072305	9.996949	9 075356	10 924644	10.003011	10:927694	13	47	9.131706	9.095.80	9.135726	10.864274	10.004020	10.868204	12
48	6 073366	6.996934	9.076.132	10.023568	10.003066	10 926634	11	48	9.132630	9-995963	9.136666	10.863333	10.004037	10.867370	12
50	9.075480		9.078576	10,021424	10.003066	10.924520		50		9.995928	0.138542	10.861458	10.004072	10.865530	
511	9.076523	9.996889	9.079644	10.929356	10.003111	10.923467	900	51	9.135387	9.99:911	9-139476	10.860524	10.004089	10.864612	9
52	9.078611	9.996874	9.080710	10.919290	10.003126	10.922417		52	9.136303	9.995894	9.14-409	10.850501	10.004106	10.863607	
54	9.079676	9.996843	9 082834	10.918327	10.003142	10.921369	6	53 54	8.138127	9.995850		10.857731	10,004194	10.802784	
55	9.082719	9.996828	9.083891	10.916109	10.001172	10.910281	1 6	55	9.139037	9 995841		10.856804	10.004750	10.860062	1 -
56	0.081759	9.996812	9.084047	10.915053	10.003187	10.018241		56	9.139004	9.99 4822	C.144121	10.855879	10.004176		4
57	c. 8:8:2	9.996707	9.086000		10.003203	10.917203	3	57 58	9.141754	9.995788		10.854956	10.004194	10.850150	
31	3.084864	9.996766	9.083098	10.911902	10.001234	10.910108	1	50		9.905700	0.146885	10.857115	10.004212	10.857344	1
to	9.08-891	9,996751		10.010856	10.003249	10.914105	0	60		9-995753	9-147802	10.8;2197	10.004247	10.856445	0
	1 -	Sine.	1	Tang.		·Secant.	M			Sine.	F	Tang.	1	Secant.	M
			8 2	Degrees.		-					82	Degrees.			
com			3	-0								3			

			8 I	egrees.							9 1	erces.			
Min.	Sine		Tang.		Secunt.			Min.	Sine		Tang.		Cant.		
0	9-143555	9-595753	9.14-802	10.852197	10,00; 247		60		9.194332	9,904610	9.100712	1 8 287	1.0 5 0		6
	9-14-14-53	9.995735	9.148718	10.851282	10.004165	10.855547	5	1	9.195129	9.95460	9.201345	10 7 4-1	10 1	10.00 371	52 8
2	9.145349	9.995717	9.149032	10.847456	10.004283	10.853756	57		9.196719	0.994560	9.201345	10 ~67841	1 014	1 3 1	CI
1 4	9.147136		9.151454	10.848546	10.004318	10.8:1364	50	4	9.197511	5.994540		10.797029	1	1 2 1	51
1-2	9.148026			10.847637	10 004336	10.8510"4	55	5	9.198702	9.994519	9.203782	10. (6217	10.005481	1 . 1 8	55
6	9.148915	9.995646	9.153269	10.846731	10.004354	10.851085	54	6	9.199091	9.994459	9.204591	12.795468	10. 5 1	10.8 9	54 2
7	9.149801	9.095628	9-154174	10.845826	10.004372	10.850198	53	7	9.199879	9-994479	9.206207	10.794600	10 - 5521	10 8 21	57
9	9.151569			10.844022	3 .004408	10 848 11	51	9	9.201451	9.994439	9.207-13	10.702 87	1 6 5,62	10.79 5 9	51
10	9.152451	9-995573	9.156887	10.843123	10.004127	10 847559	50	10	9.201214	9.994418	9.207816	10.792181	10.0 5581	10.707766	Su
11		9-595555	9.157775	10.841225	10.004445	10.8466-0	49	11	9.203017	9-994397		10.791381	10 00 (602	10.74 6983	46
12	9.154208	9,995537	9.158671	10.841329		10.845792	48	12	9.203797	9-994377	9.200410	10.780780	1 . 5623	10.797421	48
13	9.155957	9.995519	9.159565	10.840435	10 004481	10.844917	47	13	9.204577	9.994357	9.210220	10.789780 10.78808z	10 00,664	10 7 444	
15		9.995482	9.161347	10 8186 53	10.004518	10.843170	45	붜	9.206171	9.994316		1088185	10. 0:684	10 753 69	15
16		9.995464	9.162236	10.837764	10.004536	10.842700	241	16	9.206006	5-994295	9.212611	10.787389	10 005705	10 74 1094	24
17		9.995445		10.816877	10.004554	10.841431	43	17	9 20 7679	9-994274	9.213405	10.786595	10.001723	10. 02320	-3
18		9-995427	9.164008	10.835992	10.004573	10.840(65	41	18	9.208452	9-994254	9.214138	10.78 (802	1-005746	10.7 0778	42
20		9.995390		10.834226	10.004610	10.8188:6	40	20	9.209092	9.994212	9.215779	10,-84 2-	10.601788	1 700008	40
21		9.995372		10.833346	10.004628	20.827074	30		9,210760	9.994191	9.216;68	20. 8:432	10.000000	1 .7 9240	30
12		9-995353	9.167532	10.832468	10.004647	10.830115	38	22	9.211526	9-994171	9-217356	10.782634	1 0 829	10.788404	3
23	9.163743	9.995334	9.168499	10.831591	10.004665	10.836257	37	23 24	9.212291	9.994129	9.218142	10.781858	10.60 50	10.787709	37 4
12	9.165454		9.170157	10.829843	10.004703	10.834546		25	9,213818	0.994108	9.219710	10.780100	10.00 802	10.58 19:	20
26	9.166307	9.995278		10.828971	10.004721	10.833693	34	26	9.214579	9-994087	9.220192	10.779508	10.0 5 13	10 98 421	34
27	9.567159		9-171899	10.828101	10.004740	10.8 32841	33	27	0.215338	9.994:66	9.221272	10.778728	10.000134	10.784662	30
28	9.168856	9-995141	9.1-2-67	10.827233	10.004759	10.831992	32	28	9-2168-97	9-994045	9.222052	10.777948	10.00 59 55	0 79:146	37 8
29	9.169702			10.526300	10.004778	10.830298	30	30			9 22 16 6		10.006.07	1 . 7 1 1	
30	9-170546			10.82,618	10.004,97	10.820453	20	30	9.217009	9.953 81	9.224318	10.77 (618	10.00 918	10 -316:6	2 4
32	9.171389	9.995165	9.176224	10.8237-6	10.004835	10.818611	28	32	19.219116	5.093660	1.225156	10.774944	10.006010	10.7 3 4	35 4
33	9.171230			1c.S22916	10.004854	10.82:769	27	33	9.219868	9-993939	9.225929	10.774071	10.006 61	10.770192	
34	9-173070		9.177942	10.522047	10.004873	10.826002	25	34	0.221167	9.593896		10.77252	1 061 3	10.77 (12	5
36	9-173508		9.178799	10.820145	10 004011	10.825256	24	35		9.593875	9.218239	10 771 6	10,006125	10.77:886	24
37	9.175578	9.995070	9.180508	10.810442	10,004030	10.824422	23	3"	9.222861	9.993854	9.22 COT	10.270992	1 . 061:6	10.7777	23 4
38	9-176411				10.004949	10.523589	22	38		9.993832	9.229773	10.770226	10.006165	10.776.04	22
39	9.177242			10.817789		10.822-5-	30	39	9-224349	9-993789	(+231302	10.768608	10 0 6211	10.7-4468	
41		9.995013	9.183059	10.816003	10.004987	10.821928	10	40			9.232065	10.76-93	10.006272	10.774167	10
42	9.179726	9-994974	9.184752	10 815247	10.005026		18	12	9.226:7	9.993746	9 232826	10,-6-174	1.006254	10.7"342"	18
143		9.994955			10.005045		15	43	9.1:7311	9-99372	9-233486	1066.1	10. (2-5	10.7"1(80	
144	9.182105	9.904935		10.813561	10.005065		10		9.728048	9.903003	9 234345	10.764807	10.006210	10.771952	
145		9.994896			10.00 034		14	4-	9.229518	9.99 1 6=	9.21 500	10 - 6 11 1	0 006140	1 .7 0.31	14
47	9 183834	0.594877	9.188957	13.811042	10.005123	10.816166	130	47	9.230252	9.993638	9.236614	10.063386	1 06 362	1 7697	13
48		9.90485	9.189795	1 3 8 10206	10 005143		12	48	9.730 43	993616	9 237 368	10.762612	1 6 6	10.26 282	12
49		9.914878			10 000162		111	40	9 231711		Special Contract of the last o	1 2612	1 6418	10.50 205	-
50	0.187002	9-994813		10.808:38	10.005102	10.813720	10	8	9 232414	993572	-2396 2	10 7 0375	10.0 64	10-076 9	
52	9.137903	9.994779	9.103124	10.306876	10.00 211	10.812 0	1	12	0.233 109	0.001-28	9.340371	1 .7 (0629	10 0061-1	1 proper	1 5
53					10.005241	10.811238	1	13	9 234627	9.95	.241115	10.758 81	10.0 6:16	10 -64 1	6
무	-	9-904739			10 00-261	10 810480	-	5/1	9.235349	0.00:46:		17.7-8135	10 0 0 0	1 .762627	
55	9.190313		9.1556.6	10.804374	10.00 ; 280		1	55	9.23679			1 56646			
1	9.191922	19.000630	9.30-2 2	10.802-47	10 005320	10.3 3 17	0	30	9.23-515	9-942418	9 224097	10.751903	10.006;82	10.76248	3
4	0-102754	0. 04660	9 168074	10 801926	10.00 \$140	10.50-256	1 2	98	9 17 237		1.244830		15.0 01	1-61-65	
gr Gc		9.994640	0.190712	10.801 06	10 00 536	10.800668	1 0	60	6.23 52	9 99 3 4	9 24 579	10.753681		10 760110	
T	31.234.214	Sine	1	Tang.		Secant.	RS	-	-	Sinc	1	Tang.		Secant.	M
1-			8.	Degrees.			-	1-		917	8.5	Degrees.			
-		-	01.	ocgites.	THE RESERVE AND ADDRESS OF THE PARTY OF THE	-	-		-		80	ENG.	-	A STATE OF THE PARTY OF THE PAR	-

			10	Degrees.							Ιí	Degrees.			-
Min.	Sine.		Tang.		Secant.			Min.	Sine		Tang.		Secant.		
0.1	9.239670 9.240386	9-993351 9 993329 9-993307	9.246319 9.247057 9.247794	10.753681	10.006548	10.761330	60 59	0 I 2	9.280599 9.281248 9.281897	9 991947 9 991922 9 991897	9 288652 9.289136 9.289999	10.711348	10.0.8:53	10.7194 1 10.718752 10.718103	60 59
4	9.241814	9.993284 9.993262 9.693240	9.248530 9.249264 9.249998	10.751470	10.006715	10.758186	57 56	3 4	9.282544 9.283190	9.991848	9.290671	10.709329	10.008127	10.717456	57 56
5 6 7 8	9.243947 9.244646	9 993217 9-993195 9-993172	9.25073	10.749270	10.006805 10.006828	10.756053	55 54 53 52	5 6 7 8	9.284480 9.285124 9.285766	9.991799 9.991774 9.991749	9.292682	10.707318	10.008201 10.008226 10.008226	10.716164 10.715 (20 10.714876 10.714234	55 54 53 52
10	9.246c69 9.246775 9.247478	9.993149	9.252920 9.253648 9.254374	10.747080	10.006851 10.006873 10.006896	10.753930	51 50 49	9 10	9.286408 9.287048 9.287687	9.991724 9 991699 9.991674	9 254684	10.704651	10.008276	10.713592 10.712952 10.71212	51 50
12 13 14	9.248181 9.248883 9.248883	9.993081 9.993059 9.993036	9.255100	10.744900 10.744176 10.743453	10.006919 10.006941 10.006964	10.751819	48 47 46	12 13 14	9.288326 9.288964 9.289600	9.991649 9.991624 9.991599	9.296677 9.297339 9.298001	10.703323	10.008351	10.711674	49 48 47 46
15 16 17	9.250282 9.250680 9.251577	9-993013 9-992990 9-992967	9.257269 9.257990 9.258710	10.74273 1 10.742010 10.741290	10.006987 10.007010 10.007033	10.749718	45 44 43	15 16 17	9.290336 9.290870 9.291504	9 991574 9 991549 9.991524	9.298662 9.299322 9.299980	10.701338	10.008436 10.008451 10.008476	10.709764 10.7 9130 10.708496	45 44 43
18 19 20	9.253067 9.253067 9.253761	9 992944 9 992921 9.992898	9.259428 9.160146 9.26c862	10.740571 10.739854 1~739137	10.007056	10.747627 10.746932 10.746239	41 40	18 19 20	9.292137 9.292768 9.293399	9.991498 9.991473 9.991448	9.300638	10.699362	10.008502	10.707263	42 41 40
22 23	9 254453 9.255144 9.255834 9.256523	9.992875 9.992852 9.992829 9.992806	9.261578 9.262292 9.263005 9.263717	10.738422 10.737708 10.736995 10.736283	10.007125 10.007143 10.007171	10.745547 10.744856 10.744166	39 38 37	21 22 23	9.294029 9.294658 9.295286	9.99!423 9.99!397 9.99!372	9-303261	10.697393 10.696739 10.696086 10.695433	10.008577 10.008603 10.008628 10.008654	10.705971	39 38 37
24 25 26	9.257211	9.992783	9.264428 9.265138 9.26584	10.735572	10.007194 10.007217 10.007240	10.743477 10.742789 10.742102	35 34	24 25 26	9.295913 9.296539 9.297164	9.991346 9.991321 9.991295	9-304567 9-305218 9-305869	10.694782	10.008679	10.704087	36 35 34
27 28 29	9.258583 9.259263 9.259951 9.260633	9.992736 9.992713 9.992689 9.992666	9.26655	10.734153	10.007264	10.741417	33 32 31	27 28 29	9.297788 9.298412 9.299934	9.991270 9.991244 9.991213	9.306519 9.307167 9.307815 9.308463	10.693481 10.692\$32 10.692184 10.691537	10.008730 10.008756 10.008782	10.7022.2	33 32 31
30 31 32 33	9.261314 9.261994 9.262673	9.992643	9.268671 9.269375 9.27 077	10.732033 10.731329 10.730625 10.729923	10.007334 10.007357 10.007381 10.007404	10.739367 10.738686 10.738006 10.737327	30 29 28 27	30 31 32 33	9 2996 55 9.300267 9.300895 9.301514	9.991193 9.991167 9.991141 9.991115	9.3091c9 9.309754 9.310398	10.690891 10.690246 10.689601	10.008833	10.700345 10.699724 10.699105 10.698486	31 29 28 27
34 35 36	9.263351	9.992572 9.992549 9.992525	9.270779 9.271479 9.272178	10.723221	10.007428	10.735649	26 25 24	34 35 36	9.302132 9.302748 9.303364	9.991090 9 991064 9 991038	9.311042	10.688958	10.008910 10.008936 10.008962	10.697868	26 25 24
37 58 39	9.265377 9.266051 9.266723	9.992501 9.992478 9.992454	9.272876 9.273573 9.274269	10.727:24	10.007499 10.007522 10.007546	10.734622 10.733949 10.733277	23 22 21	37 38 39	9.303979 9.304593 9.305207	9.991012 9.990986 9.990960	9.312967 9.313608 9.314247	10.687032 10.686392 10.685753	10.008588 10.009014 10.009041	10.696021 10.695407 10.694793	23 22 21
40 41 42	9.267304 9.268065 9.268734	9.992406 9.992382	9.274964 9.275658 9.276351	10.725:36	10.007570	10.732605 10.73193 c 10.731266	20 19 18	40 41 42	9.305819 9.306430 9.307041 9.307650	9.99°934 9.99°988 9.99°881	9.314885 9.315523 9.316159	10.685115 10.684477 10.683841	10.00 9066 10.009092 10.009118	10.694181	20 19 18
43 44 45	9.269462	9.992338	9.277043 9.277734 9.278424	10.722957	10.007641	10.730598	16 16 15	43 44 45	9.308259	9.990855 9.990829 9.990803	9.31679; 9.317430 9.318064	10.683205	10.009145	10.692350 10.691741 10.691133	17 16 15
46 47 48	9.271400 9.272063 9.272716 9.273388	9.992287 9.992262 9.992238 9.992214	9 279113 9 279801 9 280488 9 281174	10.720887 10.720199 10.719512 17.718826	10.007713 10.007737 10.007761 10.007786	10.728600 10.727936 10.727274 10.726612	14 13 12	46 47 48	9.309474 9.310080 9.310685 9.311289	9.990777	9.318697 9.319329 9.319961 9.320592	10.681303 10.684670 10.680039 10.679408	10.009223 10.009250 10.009276 10.009303	10.690526 10.689920 10.689315 10.688711	14 13 12
49 50 51 52	9-274049 9-274708 9-275367	9.992214 9.992166 9.992142	9.281174	10.718141	10.007810 10.007834 10.007858	10.725951	10 98	49 50 51 52	9.311289 9.311893 9.312495 9.313097	9.990697 9.990671 9.990644 9.990618	9.321222	10.678778	10.009329 10.009355 10.009382	10.688107	10 9
53 54 55	9.276681	9 992117 9 992293	9 283907 9 284588	10.716c93 10.715412 10.714732	10.007882	10.723975	76 -5	53 <u>54</u>	9.313698 9.314297 9.314896	9.990591	9.323106 9.323733 9.324358	10.677521 10.676894 10.676267 10.675642	10.009409	10.686302	76
56 57 58	9.277001 9.278644 9.279297	9.99.044	9.285947 9.286624	10.714053 10.713375 10.712599	10.007980 10.008004	10.722009	3 2	5.5 56 57 58	9.315495 9.316092 9.316688	9.990511 9.990485 9.990458	9.324983 9.325607 9.326230	10.675017	10.009488	10.684505 10.683908 10.683311	3 2
59 60	9.289948	9.991971 9 991947 Sine.	9.287977	10.712023 10.711348 Tang.	10.008029	10.720052 10.719401 Secant.	0 M	59	9.317284 9.317879	9.990431 9.990404 Sint.	9.326853 9.327474	10.673147 10.672525 Tang.	10.009569	10.632716 10.682121 Secant.	0 M
-			79	Degrees.	λ.	100		0			78 1	Degrees.			-

-			12 /	Degrees.			-	T			13	Degrees.			
Min	Sine		Tang.		Secant.		1	Min.	Sine		Tang.		Secant.		T
-0 =	9.317879	9.990377	9.327474	10.672525	10.009596	10.682121	6.	-0	9.352033	9.988724	9.363364	10 6,5636	10.011276	12.64 9 2	
3	9.319066	9.990351	9.328715	10.671285	10.009649	10.680934	58	2	9.353181	9.988605	9.363943	10.636060 1 .635484 10.634910	10.01133;	10.641361	180
4	9.320149	9.990997	9-329953	10.670047	10.009703	10.679750	56	4	9-354271	9.988607	9.365664	10.634336	10.011364	10.6462-4	150
6	9.321430	9.990243	9.331187	10.668813	10.009757	10.678570	54	56	9-354815	9.988578 9.988548 9.988519	9.366217	10.633763	10.011411	10.645185	54
8	9-322607	9.990161	9.332418	10.667582	10.009812	10.677393	52 51	7 8 9	9.355901 9.356443 9.356984	9.988489	9.367382 9.367953 9.368524	10.632047	10.011481	10.644019	52
10	9-323780	9.990134	9-333646	10.666354	10.009866	10.676220	50	10	9 357524	9.988430	9.369094	10.631476	10.011570	10.643216	G
12	9.324950	9.990079	9.334871	10.665129	10.009931	10.675049	43 43	12	9.358664 9.358603 9.359141	9,988451	9.369663	10.630337	13.011509	10.641916 10.6411 7 10.646 59	43
H	9.326117	9.990025	9.336093	10.663907	10.009975	10.673883	46	14	9.359678	9.988312	9.370799	10.628633	10.011658	10.640 Sgg	47
16	9.327281	9.989970	9.337311	10.662689	10.010003	10.673300	45 44	16	9.360751	9.988182	9-371933	10.618067	10 011718	10.631785	45
81	9.328442	9.989815	9 338527	10 661473	10.010085	10.671558	43 42 41	13	9.361287	9.988222	9.373664	10.626935	10.011777	10.638-23	43
20	9-329599	9.989860	9-339739	10.660261	10.010140	10.670401	40	19	9.362356	9.988163	9-374193	10.625807	10.011337	12.637644	41
12	9.330176	9.939304	9.340344	10.659052	10.010106	10.669824	30	21	9.363422	9.988103	9-375319	10.624681	10.011847	10.63 578	3
23 34	9.331328	9.989749	9.341552	10.657845	10.010151	10.668on6	37 36	23 24	9.364485	9.988043	9.376442	10.623558	10.011937	10.635515	3°
25 26	9-332478	9.989-21	9.342757	10.656642	10.010279	10 667512	35 34	25 :6	9.365546	9.987983	9.377563	19.622437	10.012017	10.634454	35
28	9.333624	9.989665 9.989637 9.989659	9.343958	10.656042 10.655442 10.654843	10.010333	10.666376	33	28	9.366604	91987922 9-981892	9.378681	10.621319	10.012108	10.6353 6	23 32
29 30	9.334766	9.939581	9-345157	10.654245	10.010390	10.665233	31	29 30	9.368185	9.987812	9-379797	10.620203	10.012138	10.631815	31
31 32	9.335906	9.989553	9.346353	10.653647	10.010446	10.664094	29 28		9.368712 9.369236	9.987801	9.380910	10.618534	10.012109	10.631289	20
33 34	9.337043	9.989469	9+347545	10.652455	10.010503	10.662350	27 26	33 34	9 369761	9.987740	9.381020	10.617475	10.012265	10.61 239	2 n
35	9.338176	9.989441	9.348735	10.651265	10.010559	10.661827	25 24	35 36	9.3708c8	9.987679	9.38;128	1 .616218	10.012341	10.6236-	25
37 38	9.339871	9 989384 9.989356 9.989318	9-349912 9-350514 9-351106	10.650078 10.640486 10.643804	10.010615	10.660693	22	37 38	9-3718 42	9.987618	9.384234	1 .615766	10.012382	10.628148	
39 40	9.340434	9.989299	9.351697	10,6483 3	10.010700	10.659004	20	3 <u>9</u> 40	9-372894	9.987557	9.385888 9.385888 9.386438	10.614663	10.012443	10.6271.6	1
41 42	9.341558 9.342119			10.647713	10.010729	10.653442	81	41 42	9·373933 9·374452	9.987465	9.386438	10.613013	10.012504	10.626.67	I G
#3 ##	9.342679	9 989214	9-353465	10.645047	10.010786	10.65-321	17	43 44	9-37497	9.987434	9 387536	10.611464	1d.c12566	1 .604512	16
45 46	9+343797 9-344355	9.989157	9.355227	10.64536	10.010843	10.656203	3 ¢	45 46	9-376519	9.9873-2	9.388631	10.61136	10.012623	10.6231 -	
48	9.345469	9.689100	9.355813 9.356398 9.35682	10 644187 10.643602 10 643018	10.010900	10.655089	13	17 18	9-377549	9.98711	9.38,824	10.6:0276	1 0126,0	10.622451	1 ; 2 2
49 50	9.346579	9 589014	9.317566	10.643414	10.015686	10.653975	11	+)	9.378563 9.378577 9.379633	9.987218	9.391359	10.603640	10-012752	10.621	10
51 52	9-347134	9.98898	9.358119	10.641861	10.011015	10.6 2313	9	\$1 12	9.379603	9 987185	9.391913		10,012814	10.62 1	3
53 54	9.348240	o. 88808	9.35,313	10 640106	10.011073	10.651760	6	53 14	9.380113	9.987124	9.301989		10.012876	10.61, 19	7 6
56	9.31/343	9 (88840)	9,360474 9,361053	10,638947	10.011131	10.6 -0656	5	ςς ;6	9.381643	9,987061	9.394614	10.6. 5356	1 .012939	10.018.	5
58	9-350443 9-35 992	9.588311	9.3622.0	10.637750	10.011218	10.640008	3	8	9.3 20 0	9-9319-8	9.39:114	10.604306	10.013002	10.61-848	3 2
60	9.351540	9.988724 Sine		10 636636	1-011247	1 .6 3450	5	- 0	9.383168	9. 36904	9.396233	10.603 191	10,013 64	10.61.83	6
		Sine 1	77 1	Degrees.		S cant.	W.	E		Sine	76 1	lang.	- 1	Securit.	Al
			11 -								10 1	16816620			

30							-,	_							-1
_			14 D	egrees.			-	Ц.			15 1	egrees.			-1
Min.	Sine.	V	Tang.		Secant.			Min.	Sine		Tang.		Secant.		
0	9.383675	9.986904	9-396771	10.603229	10.013096	10.616325	60 59	0	9.412996	9.984944	9.428052	10.571947	10.0150,6	10.587004	60
2	9.384687	9.986841	9.397846	10.602154	10.013159	10.615313	58	2	9.413938	9.984876	9.429062	10.570938	10.015124	10.586062	59 58
3	9.385192	9.986809 9.986778	9.398383	10.601617	10.013191	10.614808	57 56	3	9.414408	9.984842	9.429566	10.570434	10.015158	10.585592	57
5	9.386201	9.986746	9.399455	10.600545	10.013254	10.613799	55	5	9-415347	9.984774	9.430573	10.569427	10.015226	10.584653	195
6	9.386704	9.986714	9.399990	10.600010	10.013286	10.613296	53	6	9.415815	9.984740	9.431075	10.568925	10.015260	10.584185	54
8	9.387709	9.986651	9.401058	10.598942	10.013349	10.612291	52 51	8	9.416751	9.984672	9.432079	10.567921	10.015328	10.583249	53
9	9.388210	9.986619	9.401591	10 598409	10.013381	10.611289	50	9	9-417217	9 984637	9.432580	10.567420	10.015362	10.582783	51
11	9.389211	9.986555	9.402656	10.597344	10.013445	10.610789	49	11	9.418149	9.934 569	9.433580	10.566410	10.015431	10.581850	50 49
12	9.389711	9.986523	9.403187	10.596813	10.013477	10 610289	47	12	9.418615	9.984535	9-434080	10.565920	10.015465	10.581385	48
34	9 390708	9.586459	9.404249	10.595751	10.013541	10,609292	46	14	9-419544	9.984466	9-435078	10.564922	10.015534	10.580456	46
15	9.341703	9.986427	9.404778	10.595222	10.013573	10.608794	45	15	9.420007	9.984432	9.435576	10.564424	10.015568	10.579993	45
17	9.39:199	9.986363	9.405836	10.594164	10.013637	10.607801	43	17	9.420933	9.984363	9.436570	10.563430	10.015637	10.579067	44
18	9.392695	9-986331	9.406364	10.593636	10.013669	10.607305	42	18	9.421395	9.984328	9-437067	10.562933	10.015 06	10.578605	42
20	9.39368	9.986266	9.407419	10.592581	10.013734	10.606315	40	20	9 422318	9.984259	9.438059	10.561941	10.015741	10.577682	40
21	9 394179		9-407945	10.592055	10.013766	10.605821	39	2 I 2 2	9.422778	9.984224	9.438554	10.561446	10.015776	10.576762	39
23	9.395166	9 986169	9.408996	10.591003	10.013831	10.604834	37	23	9.423697	9.984155	9-439543	10.560457	10.015845	10.576303	37
24	9-395658		9.409521	10.590479	10.013863	10.604342	35	24	9.424615	9.984120	9.440529	10.559964	10.015880	10.575844	36
25	9.396150	9.986072	9.410569	10.589431	10.013928	10.603359	34	26	9.425073	9.984050	9 44 1022	10.558978	10.015950	10.574927	35
27	9-397 31	9.986039	9.411615	10.588968	10.01396	10.602868	33	27 28	9.425530	9.984015	9.441514	10.558485	10.015985	10.574470	33
20		9.985974		10.587863	10.014026	10.601589	31	29		9.983945	9-442497	10.557502	10.016054	10.573557	32
30	9.398600	0 08 5044	9 412658	10.587342	10.014058	10.601400	30	30	9.426899	9.983910	9-442988	10.557012	10.016089	10.573101	30
3 3 3 2	9.399088	9.98 5876	9.413179	10.586301	10.014124	10.600425	28	32	9.427809	9.983840		10.556031	10.016160		28
33	9.400062	9.98 5843	9.414219	10.585781	10.014157	10.599937	27	33	9.428263			10.555542	10.016195	10.571737	27
34	9.400540			10.584743	10.014222	10.598965		34 35	9.429170	9.983739	9-445435	10.554565	10.016265		26
36	9.401 520	9.985740	9.41 577 9	10.584225	10.014255	10.598480		36	9.429623	9.983700	9.445923	10.554077	10.016300	10.570377	24
3	9.40200			10.583707	10.014321	10.597511	22	37	9.430527	9.983629	9.446898	10 553102	10.016371	10.569473	23
39								39				10.552616	10.016406		21
44				10.582157	10.014420	10.596545		41	9.431879	9.983521	9-447870 9-448356 9-448841	10.552130	10.016442	10.568121	10
4:	9.40441	9.985547	9.418873	10.581127	10.01445	10.595580	18	41		9.983487	9.448841	10.551159	10.016513		18
4:			9-419387	10.580099	10.014520	10.594618	16	41		9.983416	9.449810		10.016584		17
4	9.40586	9 985447	9.42041			10.594138		49	9.43367				10.016616		15
4			9.420927	10.579072	10.014586			46	9-434569	9.483300	9.451260	10.549223	10.016691	10.565431	112
4		9.985347	9.421951	10.578048	10.01465			48	9.435016	9.983279			10.016726	10.564984	12
59								50					10.016798		
15	9.40873	9.985247	9.423484	10:576516	10.01475	10.591269	9	51	9.43635	19.983166	9.453187	10.546813	10.016834	10.563647	9
52			9-423993	10.576006		10.590793	1 7	52	9-43724	0.083004	9.454148	10.54.852	10.016900	10.562758	7
54	9.41015	9.985146	9.425011	10.574989	10.014854	10.589842	6	54	9 437080						-
55			9-425519	10.574481		10.589368	5	55 56		9.982986	9.455586	10.544414	10.01701	1 10 561428	
57	9.4 1579	9.985045	9.426534	10.573466	10.014959	10:588421	3	57	9.439014	9.982950	9.45606	10.543936	10.01705	10.560986	6 3
59	9.412052	9.984978	9-427041	10.572959		10.587948	1	58 59	9.439897	9 982878	9.45701	10.542981	10.01712	2 10.56010	3 1
60		9.984944	9.428052	10.571947	10.015056	10.587004	0	60		9.982842 Sine.	9.45749	Tang.	10.01715		
1 -		Sine.		Tang.		Secant.	M	=	·	, Sine.	-			- Secant.	IM
1_			75	Degrees.							74	Degrees.	-		

-			16 I	Degrees.			-				17	Degra				
		1		6			-				1/1	Jegin	2 .			-
Min.	Sine		Tang.	3 -00	Secant.		-	Mi	Sine		Tang.	ш.		S-cant.	1 -	10
5	9-41-335	9.931842	9.457496	10.542504	10,017158	10.559662	60	0	9.465915	9.980596	9.48 5339	10.51		10 0144 -4	1 . 314-05	6.
2	9.441118	9.981805	9 458449	10.542027	10.017195	10.558782	59	2	9.466761	9.980558	9-485791	10.51	1758	10.010181	10 5,3052	98
3	9.441658	9.932733	9.453925	10.541075	10.017267	10.558342	57	3	9.467585	9.980480	9.486693	10.51	1107	10.019;20	10. 31827	134
2	9-441535	9.982660	9 464875	10.540125	10.017340	10.557465	55	-	9.46,990	9.980403	9.487593	10.51		10 014 97	10,51200	10
6	9-442973	9.982623	9.460349	10.539651	10.0173-6	10.557027	54	6	9.468407	9.980364	9.488043	10.51		10.019636	10.5311593	154
8	9-443847	9.98:501	9.461297	10.538703	10.017449	10.556153	52	8	9.469227	9.980286	9.488941	19.51	1959	10,019714	10.530777	42
9	9 4441720	9.982477	9 461770	10.518230	10.017486	10.555716	51	9	9.469637	9.980247	9-489390	10.51	-	10.019793	10 (30363	53
11	9-445155	9 982448	9.461714	10.557285	10.017550	10.554845	49	11	9-470455	9.980169	9-490286	10.50	9714	10,019871	10.539545	46
12	9.445590	9.983367	9.463658	10.536342	10.017596	10.554410	48	12	9-470863	9.980091	9-490733	10.50	9207	10.019870	10.52913	40
14	9.446459	9.982294	9.464128	10.535871	10.017669	10.551541	46	14	9.471678	9.980052	9.491627	10 50	8373	10 019948	10 528271	46
16	9.446893	9.932257	9.464;99	10.535401	10.017743	10.553107	45	16	9-472086	9.979973	9-492673	10.50	7481	10.619988	10.527914	45
18	9-447759	9.982210	9.466003	10.534461	10.017817	10.551841	43	17 18	9-473898		9 491965	10.50		10.020108	10.52 101	43
19	9 448623	9.982146	9.466476	10.333-23	10.017854	10.531377	41	19	9-473710	9.979855	9-493654	10.50	6145	10.010145	10.526290	41
20	9.449054	9.981109	9.466945	10.533055	10.917928	10.550515	40 39	20	9-474315	9.979816	9-494249	10.50	5701	10.030184	10 525885	40
22	9-449915	9.982035	9.467880	19.532120	10.017965	10.550085	38	22	9-474923	9-979737	9-495186	10.50.	1812	10 020263	10 525077	38
23	9.450345	9.981961	9.462814	10.531156	10.018039	10 549215	37	23 24	9-475327	9.979697	9.495630	10.50	4370 3937	10.010303	10.524673	37
25	9.451204	9.981924	9.469280	10.530720	10.018076	10.548796	35	25	9 476133	9.979618	9.496515	10.50		10.020381	10.523507	35
25	9 452660	9 981849	9-470211	10.529789	10.018151	10.547940	34	26	9.476536	9-979578	9-496957	10.50	1601	10.010421	10.523464	34
28	9.452488	9.981812	9.470676	10.516850	10.018188	10.547512	32	28	9-477741	9-979499	9.497841	10.50		10.020501	10.522660	32
30	9-453342	9 981737	9.471605	10.568395	10.018263	10.546658	30	10	9.478142	9-979419	9.498-22	10.50	1278	10.010580	10.521858	30
31	9.453768	9.981699	9.472068	10.527931	10.0183300	10.546133	29	31	9 478541	9-979340	9 499163	10.500	0837	10.020620	10.521458	26
33	9.454619	9.981624	9-472995	10.527005	10.018375	10.545381	27	33	9-479342	9.979300	9.500042	10.49	9958	10.010700	10,520658	2.7 2.6
34	9.455469	9.981549	9-473919	10.526082	10.018421	10 541531	35	34	9 480140	9.979220	9.500920	10.49		10.020780	10 519560	20
36	9 455893	9.981512	9-474381	10.525619	10.018488	10.544107	24	36	9.480538	9.979180	9.501359	10.49	8641	10.010820	10.519461	24
38	9.456739	9.981436	9-475393	10.524697	10.018564	10.543261	22	37	9.481314	9.979100	9.502235	30.497	7765	10.010900	10.518666	23
39	9.457161	9.981399	9-475763	10.524137	10.018601	10.542838	21	39	9.481731	9.979019	9.502672	10.49		10.020941	10.518268	21
41	9.4580:6	9.981323	9.476683	10.523317	10.018677	10.541994	19	41	9 482525	9.978979	9.503546	10.496	6454	10.021021	10.517475	10
42 41	9 458427 9.458848	9.981285	9.477142	10.522858	10.018715	10.541573	38	42 43	9.482921	9.978939	9 503981	10.49	5582	10.021061	10.517079	17
44	9.459268	9.981209	9.478059	10.521947	10.018791	10.540731	16	44	9483712	9.978858	9.504854	20.49		10.021142	10.516288	16
45 46	9.459688	9.981133	9.478975	10.521025	10.018867	10.539892	35 34	4¢	9-484107	0.978777	9-505724	10.49	1276	10.021182	10-515893	14 14
47	9.460527	9.981095	9-479433	10.520;63	10.018905	10.539473	23	47	9.484805	9.978736	9 506159	10.49		10.011263	10.515105	13
49	9.161364	9.981019	9.480345	10.519655	100 8981	10.538636	11	49	9.485682	9 478655	9.50.027	10 44	2973	10.021745	10.514318	31
50	9.461782	9.980980	9.480801	10. 519199	10.019019	10.538218	10	50	9.486075	9.978615	9.507460	10.49		10.021385	10.513925	10
52	9.462616	9.980904	9.481712	10.518188	10.019096	10.537384	g	Ç2	9.486850	9.978533	9.508316	10 49	1674	10 021467	10.513140	8
53 54	9.463032	9.980827	9 482621	10.517833	10.019173	10 136552	6	53	9.487641	9.978452	9.500759	10.49		10 21 (48	10.51-357	6
55	9.463864	9.980789	9.483519	10, 516925	10.019211	10.5;6136	5	55	6.488033	9.978411	9.509622	10.48	c378	10.021589	10. 111906	5
56 57	9.464279	9.980712	9 483982	10.516018	10.01928	10.535306	3	57	9.488814	9.978329	9.580485	10.48	9519	10.023571	10,511186	1
58	9.465108	9.980673	9.48443	10.515164	10.019365	10.534892	2 1	58	9-489504	9.918247	9.510916	10 48	3644	10.021712	10.510796	2
60	9.465935	19.980566	9.485330	10.514661	10 019104	10.434065	0	60	9 409981	9.978206	9.501776	10.48	8224	10.031704	10 61 0 8	c
		Sine.	11	Tang.		Secant.	Z			5 he	1	Tar			2 11	M
			73	Degrees							. 72	Deire	85.			

			18.	Degrees.							19	Degrees.			-1
M a.	Sine.		Tang.		Secant.	-		Min.	Sine.		Tang.		Secant.		
0	9.489982	9.978260	9.511776	10.483224	10.021794	10.510018	60	0	9.512642	9.975670	9.536972	10.463028	10.024330	10.487358	60
1 2	9.490371	9.978165	9.512206	10.487794	10.021835	10.509629	59	2	y-513009 y-513375	9.975626	9-537792	10.462618	10.024373	10.486991	59
3	9.491147	9.978083	9.513064	10.486936	10.021917	10.508853	57	3	9.513741	9-975539	9.538202	10.461798	10,024461	10.486250	58
4	9.491534	9.978042	9.513493	10.486507	10.021958	10.508465	56	4	9.514107	9-975490	9-538611	10.461389	10.024504	10.485893	56
6	9.491922	9.977959	9.514349	10.485651	10.022041	10.507692	55 54	6	9.514837	9-975408	9.589429	10.460571	10.024548	10.485528	55
7	9.492695	9.977918	9.514777	10.485223	10.022082	10.505019	53	7 8	9.515202	9.975365	9.539837	10.459755	10.024635	10.484798	54
9		9.977835	9.515631	10.484369	10.022165	10.506534	52 51	9.	y.515030	9.975321	9.540653	10.459347	10.024679	10.484434	52
10	9.493851	9-977794	9.516057	10.483942	10.022206	10.506149	50	10	9.516294	9-975:33	9-541061	10.458939	10.024767	10.483706	27
11	9.494236		9.516484	10.483516	10.022248	10.505764	49 48	11	9.516657	9-975189	9.541468	10.458532	10.024811	10.483343	49
13	9.495005	9.977609	9.517335	10.482665	10.022331	10.504995	47	13	9.517382	9.975101	9.542281	10.457719	10.024899	10.482618	48
14	9-495388			10.482230	10.022372	10.504612	46	14	9.517745	9-975057	9.542688	10.457312	10.024943	10.482255	46
16	9-495772		9.518610	10.481390	10.022414	10.504228	45	15 16	9.518468	9-975013	9-543094	10.450501	10.524987	10.481893	45
17	9.496537	9.977503	9.519034	10.480966	10.022497	10.503463	43	17	9.518829	9-974925	9.543005	10.456095	10.025075	10.481170	44 4
18	9 496919			10.480542	10.022539	10.50308	42	19	9.519551	9 974880	9.24431.	10.455690	10.025120	10.480810	42
20	9.497682	9-977377	9.520305	10.479595	10.022623	10.502318	40	20	9 519911	9-974792	9-545119	10.454881	10.02 5208	10.480080	년 1 40
1 - I	9.498063	9-977335	9.520728	10.479272	10 022665	10.501936	39 38	21	9.520271	9-974747	9-545524	10.454476	10.025252	10.479729	39
22 23	9.498824	9.977251	9.521573	10.478427	10.022748	10.501175	37	23	9.520490	9-974659	9-546331	10.453669	10.025341	10.479369	33
24	9-499204		9-521995	10.478002	10.022790	10.500795	36	24	9-521349	9 97-1614	9.546735	10.453265	10.025386	10,478651	37 36
2 2 6	9-499584	9.977107		10.477583	10.022833	10.500416	35	25 26	9.521707	9 974 570	9-347540	10.452862	10.025430	10.478293	35
6 2"	9.500342	19.977083	9.523259	10.476741	10.022917	10.499658	34 33	27	9.522423	9.974481	9-547943	10.452057	10.025519	10.477934	34
28	9.500721	9.977041	9.523679	10.476320	10.022959	10.499279	32	28	9.522781	9-974436	9-548345	10.451655	10.025564	10.477219	32
29 30	9.501470	9.976957	9-524520	10.475480	10.023043	10.498524	31	30	9.523495	9.974347	9.549149	10.450851	10.025653	10.476:05	31
31	9.501854	9.976914	9.534939	10.475060	10.022086	10.498146	29	31	9.523852	9.974302	9-549550	10.450450	10.02 1608	10.476148	30
32	9.502231	9.976872	9.525359	10.474641	10.023128	10.497769	28	32	2.524564	9.974257	9.550352	10.450049	10.025743	10.475792	28
34	9.502984	9.976787	9,526197	10.473803	10.023213	10.497016	26	34	9.524-)20	9.974167	9.550752	10.449248	10.025833	10.475080	27
35	9.503360			10.473385	10.02325	10.496640	25	35	9.525275	9-974077	9.551152	10.448847	10.025873	10.474725	25
36	9.504110	9 976660		10.472549	10.023340	10.495889	23	37	9.525984	9.974077	9.551952	10.448048	10.025923	10.474370	24
18	9.504485	9.976617	9.527868	10.472132	10.023383	10.495515	22	58	9.526692	9-973987	9-552351	10.447649	10.026313	10.473661	22
39	9. 105234	9.970574		10.471208	10.023468	10.404766	20	39	9 527046	9.973897	9.553149	10.446851	10.026103	10.473307	21
41	9.505628	9.976489	9.529119	10.470881	10.023511	10.494392	19	41	9-527400	9.973852	9.553548	10.446452	10.026148	10.472600	20 19
42	9.505981	9.976446	9.529535	10.470465	10.023554	10.494019	18	42	9.527753	9.973807	9.553946	10.446054	10.026193	10.472247	18
43	9.506727	9.976361	9.530366	10.469634	10.023639	10.493273	16	44	9.528457	9.973716	9.554741	10.415258	10.026284	10 471542	17
45	9.507099	9.976318	9.530781	10.469219	10.023682	10.492902	15	45	9.528810	9.973671	9.555539	10.444501	10.026329	10.471190	15
46	9.507842	9 976232	9.531611	10.468380	10.023768	10.492157	14	46	9 529161	9.973580	9-555933	10.544.67	10,026420	10.470487	14
48	9.508214	9.976189	9.532025	10.467975	10.023811	10.491786	12	48	9.539864	9-973535	9.556329	10.443671	10.026465	10.470136	12
49	9.508916		9.532853	10.467147	10.023897	10.491044	10	49	9.530565	9.973443	9.557121	10.4.12879	10.026556	10.469435	10
50	9.5093.6	9.976060	19.533266	10.466734	10.023940	10.490674	0	51	9.530915	9-973398	9.557517	10.442483	10.026502	10.469085	9 8
52	9.509696	9.975974	9.533679	10.466321	10.023983	10.490304	8	52 53	9.531265	9.973352	9.557912	10.442087	10.026648	10.468735	- 12
53 54	9.510434	9.975930	9.534504	10.465496	10.024070	10.48 0566	6	54	9.531963	9 973261	9.558702	10.441297	10.026739	10.468036	7
55		9.975887	9.534916	10.465084	10.024113	10.489197	5	55	9.532312	9.973215	9.559097	10.440509	10.026785	10.467688	. 5
56	9.511172	9.975844	9.535328	10.404072	10.024150	10.488460	4		9.532661	9.973169	9.559491	10.440115	10.026376	10.467339	4
58	9.511907	9.975757	9.530150	10.463849	10.024243	10.188093	2	58	9-533357	9.973078	9.560279	10.439721	10.025922	10.466643	2
59 60	9.512275 9.512642	9-975713	9.536561	10.463439	10.024287	10.487725	0	59 60	9.533704	9.973032	9.561066	10.439327	10.020908	10.466296	0
		Sine.		Tang.	-	Secant	M			Sine		· Tang.		Secant.	M
-			71 .	Degrees.							70	Degrees.			
-							-	-	-	-	STATISTICS.		THE RESERVE TO SHARE	-	-

_			20 /	egrees.			_	-			21	Degrees.			_
	1			· Green				-			- 21	orgress.		,	-
Min.	Sine		Tang.		Secant.			Min.	Sine		Tang.		Secunt.		
0	9-534052	9.972986	9.561066	10.438935	10.027014	10.465948	6c	0	9-554329	9.970152	9.581177	10 415823	10 01984	10.44 0 1	éc:
2	9-534745	9.972894	9.562144	10.438146	10.027106	10.465255	58	2	9-554987	9 9700 \$5	9.584932	10.415 68	10 019945	10.445683	58
4	9.535091 9.53543	9.972802	9.562636	10.437756	10.027198	10.264562	56	3	9.555315	9.97:006	9.585300	10 414691	10.029994	10.444685	37
5	9.535783	9.972755	9.563028	10.436972	10.027245	10.464217	55	5	9.555971	9.909909	9.586062	10.413038	10.030000	10.444 14	81
7	9.5364-4	9.972663	9.563811	10.436189	10.027337	10.463526	53	7	9.5566199	9.169860	9.5864-9	10.413181	10-730-89	10.443 74	6
9	9.536818	9.972617	9.564202	10.435798	10.027383	10.463182	52 51	8.	9.556953	9.969762	9.587190	10.412810	10.010286	10.443047	50
10	9-537507	9.072524	9.564983	10.435017	10.027476	10.462493	55	10	9.557606	9.969665	9.58794	10.412059	10.030335	10.442394	
11	9.537851	9-972477	9.565373	10.434627	10.027522	10.462149	45 48	11	9.557932	9.969616	9.588316	10.411684	10.030384	10.442008	45
13 14	9.538537 0.538880	9.972384	9.565153	10.433847	10.027615	10.461462	4- 46	13	9.558583	9.969518	9.589066	10.410933	10.030,82	10.441416	4.
15	9-539223	9-972338	9.566932	10.433068	10,027709	10.460777	45	14	9.558909	9.969420	9.589440	10.410186	10.030580	10.440760	45
16	9.539565	9.972245	9.567709	10.432679	10,02775	10.460435	44	16	9.559558	9.969370	9.5901;8	10.409812	10.030630	10.440441	44
18	9.539907 9.540249	9.972198	9.568097	10.431902	10.027849	10.459751	43 42	17 18	9.559883	9.969321	9.590562	10.409438	10.030718	10.440117	41 42
19 20	9-540590	9.972105	9.568486	10.431514	10.027895	10.459410	41 40	19	9.560855	9.969223	9.591308	10.408692	10.030777	10.439469	40
21	9.541272	9.972011	9.569261	10.430739	10.027989	10.458728	39	21	9.561178	9.969124	9.592054	10.407946	10.030876	10.435822	3
22	9.541613	9.971964	9.569648	10.430352	10.028036	10.458387	38 37	22	9.561401	9.969075	9.591426	10-407574	10.030925	10.43849	38
24	9-542293	9.971870	9.570422	10 429578	10.028130	10.457707	36	24	9.562146	9.968976	9.593170	10.406829	10.031024	10.437854	36
25 26	9-542632	9.971813	9.570809	10.429191	10.028177	10.457368	35	25	9-562795	9.968926	9.593542	10.406458	10.031074	10.437531	3 5 3 4
27	9-543310		9-571581	10.428419	10.028271	10.456690	33	27	9.563112	9.968827	9.554285	10,405715	10.031173	10.436888	33
29	9.543649	9.971635	9.572352	10.427648	10.028365	10.456013	31	28	9.563433	9.968777	9.594656	10-405344	10.031223	10.436566	32 31
30	9.544325	9.971588	9-572738	10.427262	10.028412	10.455675	30 20	30	9.564075	9.968678	9-595397	10.404602	10.03.322	10.435925	3
32	9-544663	9-971540	9-573123	10.426493	10.028507	10.454999	±Š	31	9.564396	9.968628	9.595768	10.404232	10.031372	10.435605	28
33 34	9.545338	9.971446	9.573892	10.426108	10.028554	10.454662	27	33	9.565036	9.968528	9.596808	10 403492	10.031472	10.434644	27
35	9-546011	9-971351	9.574660	10.425340	10.028647	10.453989	25	35	9.565676	9.968429	9-597247	10.402753	10.031571	10.434324	2.5
36	9-546347	9.971303	9.575044	10.424956	10.028696	10.453553	24	36	9-565995	9.968379	9-597616	10.402384	10.031621	10.431000	23
38	9-547019	9.971208	9.575810	10.424190	10.028792	10.452981	22 21	38	9.566632	9.968278	9.598354	10-401646	10.031722	10.433368	22
1 <u>79</u> 40	9.547680	9.971113	9.576576	10.423424	10.028887	10-452311	20	39	9.567269	9.968178	9-598722	10.400909	10.031522	10.433049	21
41	9.548024		9.576958	10.423041	10.028934	10.451641	19	41	9.567587	9.968128	9-599459	10.40 541	10.031872	10.432413 10.4:20cf.	10
43	9-548693	9.970970	9-577723	10.422277	10.029030	10.451307	17	42	9.567904	9.968078	9.599827	10.399803	10.031973	10.431778	15
44	9.549027	9.970922	9 578104	10.421896	10,029078	10.450075	16	44	9.568835	9.967977	9.600562	10.399438	10.032023	10.431.61	16
46	9.545693	9.970826	9.578867	10.421133	10.029173	10.450306	14	46	9.569172	9.967876	9.601296	10.398704	10.033124	10.430828	14
47	9.55026	9.97-779	9.579629	10.420752	10.029221	10.449973	13	47 48	9.569488	9.967826	9.601662	10.398337	10.032174	10.430512	13
49	9. 550692	9.970683	9.580009	10.419991	10.019317	10.449308	ш	49	9.570120	9.967725	9.602 195	139-605	10 031275	10.429880	回
50	9.551024	9.970635	9.580389	10.419611	10.029365	10.448976	9	50	9-570435	9.967674	9.602761	10.397239	10.032326	10.429564	10
52	9.551687	9.970538	9.581149	10.418851	10.029462	10.448313	8	52	9.571066	9.967573	9.603493	10.395507	10.032427	10.428035	900
54	9-552349		9.581907	10.418093	10.039558	10.447982	6	53 54	9.571380	9.967522	9.603858	10.396142	10.0324 8	10.415375	7
55	9.552680	9.970394	9.582286	10-417714	10.029606	10.447320	5	95	9-572009	9.967420	9.604588	10.395412	10.0325-9	10.427991	1
57	9.553341	9-970297	9.583043	10.416956	10.029703	10.446659	3	56 57	9.572323	9.967370	9.604953	10.394683	10 032681	10.427103	3
5S	9.554000	9.970249	9.583422	10.416578	10.029751	10.446330	2	58	9.572949	9.967268	9.605682	10.394318	10.032-31	10.4.70 4	2
60	9.554329	9.970152 Sine	9.584177	Tang.	10.029848	10.445671	о М	6c	9-571575	9.467166	9.606410	10.393590	10 432834	10.426426	o.
-		Sine	60			Secant.	20	L		Sine	-	Tang.		Secan.	M
			09 1	Degrees.		0.000	1				68	Degrees.			- 1

_	22 Degrees.								23 Degrees.							
Min.	Sine.		Tang.		Secant.			Min.	Sine		Tang.		Secant.			
0	9·573575 9·573888	9.967166	9.606410	10.393590	10.032834	10.426425	60	0	9.591878	9.964026	9.627853	10.372148	10,035974	10.408122	60	
2	9-574200	9.967064	9.607137	10.393863	10.032005	10.425800	59 58	2	9.592175	9.963972	9.628203	10.371797	10.036028	10 407824	59	
3	9.574512	9.967012	9.607500	10.392500	10.032087	10.425488	57	3	9.592473	9.963865	9.628554	10.371448	10.036081	10.407527	58	
4	9.574824	9.966961	9.607863	10.392137	10.033039	10.425176	56	4	9.593069	9.963811	.9.629255	10.370745	10.036189	10.406933	56	
5	9.575136	9.966859	9.608225	10.391775	10.033090	10.424864	55	5	9.592363	9.963757	9.629606	10.370394	10.036243	10.406637	55	
7	9-575738	9.966807	9.608950	10.391050	10.033192	10.424242	54		9.593659	9.963704	9.629956	10.370044	10.036296	10.406341	54	
8	9.576068	9.966756	9.609312	10.390688	10.033244	10.423931	52	7 8	9.594251	9.963596	9.630656	10.369694	10.036350	10.406044	53	
9	9.576379	9.966704	9.609674	10 390326	10.033295	10.423621	51	9	9.594547	9.963543	9.631005	10.368995	10.036458	10.405453	51	
11	9.576009	9.966653	9.610039	10.389964	10.033347	10.423311	50 49	10	9.594842	9.963488	9.631354	10.368645	10.036512	10.405158	50	
12.	9-577309	9.966550	9.610759	10.389241	10.033398	10.422691	48	11	9-595137	9.963434	9.631704	10.368296	10.036566	10.404863	49	
13	9.577618	9.966499	9.611120	10.388880	10.033501	10.422382	47	13	9-595727	9.963325	9.632401	10.367947	10.036620	10.404568	48	
14	9-577927	9.966447	9.611480	10.388520	10.033553	10.422072	46	14	9.596021	9.963281	9.632750	10.367250	10.036729	10.403979	46	
16	9-578545	9.966344	9.612001	10.388159	10.033605	10.421764	45 44	15 16	9.596315	9.963217	9.633098	10.366901	10.036783	10.403685	45	
17	9.578853	9.966292	9.612561	10.387438	10.033708	10.421146	43	17	9.596609	9.963162	9.633447	10.366553	10,036837	10.403391	44	
18	9-579162	9.966240	9.612921	10.387079	10.033760	10.420838	42	18	9.597196	9.963054	9.634143	10.365857	10.036892	10.403097	43	
20	9.579469	9.966136	9.613281	10.386719	10.033812	10.420530	41	19	9.597490	9.962999	9.634490	10.365510	10.037001	10.402510	41	
21	9.580084	9.966085	9.614000	10.386000	10.033863	10.420233	40 39	20 21	9-597783	9.962945	9.634838	10.365162	10,037055	10.402217	40	
22	9.580392	9.966033	9.614359	10.385641	10.033967	10.419608	38	22	9.598075	9.962890	9.635185	10.364815	10.037110	10.401925	39	
23	9.580699	9.965981	9.614718	10.385282	10.034019	10.419301	37	23	9.598660	9.962781	9.635879	10.364121	10.037219	10.401632	33	
25	9.581312	9.965876	9.615077	10.384923	10.034071	10.418995	36	24	9-598952	9.962727	9.636226	10.363774	10.037273	10.401048	36	
26	9.581618	9.965824	9.615793	10.384565	10.034124	10.418688	35	25	9.599244	9.962672	9.636572	10.363428	10.037328	10.400755	35	
27	0.581024	9.965772	9.616151	10.383849	10.034228	10.418076	34	27	9.599536	9.962617	9.636918	10.363081	10.037383	10.400464	34	
28 29	9.582229	9.965720	9.616509	10.383491	10.034280	10.417771	32.	28	9.600118	9.962509	9.637611	10.362389	10.037493	10.399882	33	
30	9.582840	9.965615	9.617224	10.383133	10,034332	10.417465	31	29	9.600409	9.962453	9.637956	10.362044	10.037547	10.399591	31	
31	9.583144	9.965563	9.617581	10.382418	10.034385	10.417160	30	30	9.600500	9.962398	9.638302	10.361698	10.037602	10.399300	30	
32	9.583449	9.965511	9.617938	10.382061	10,034489	10.416551	28	31 32	9.601280	9.962288	9.638647	10.361353	10.037657	10.399010	29	
33 34	9.583753	9.965458	9.618295	10.381705	10.034542	10.416246	27	33	9.601570	9.962233	9.639337	10.360662	10.037767	10.398430	27	
35	9.584361	9.965353	9.619008	10.380992	10.034594	10.415942		34	9.501860	9.962178	9.639682	10.360318	10.037822	10.398140	26	
36	9.584665	9.965301	9.619364	10.380635	10.034699	10.415335	25	35 36	9.602149	9.962123	9.640027	10.359973	10.037877	10.397850	25	
37 38	9.584968	9.965248	9.619720	10.380279	10.034752	10.415031	23	37	9.602728	9.962012	9.640716	10.359284	10.037933	10.397561	23	
39	9.585574	9.965195	9.620432	10.379568	10.034805	10.414728	22	38	9.603017	9.961957	9.641060	10.358940	10.038043	10.396983	22	
40	9.585877	9.965090	9.620787	10.379213	10.034910	10.414123	20	39 40	9.603594	9.961902	9.641404	10.358596	10.038098	10.396695	21	
41	9.586179	9.965037	9.621142	10.378858	10.034963	10.413820	19	41	9.603882	9.961791	9.641747	10.358253	10.038154	10.396406	10	
42	9.586482	9.964984	9.621497	10.378503	10.035016	10.413518	18	42	9.604170	9.961735	9.642434	10.357566	10.038264	10.395830	18	
44	9.587085	9.964878	9.622207	10.377793	10.035069	10.413216	17	43	9.604457	9.961680	9.642777	10.357223	10.538320	10.395543	17	
45	9.587386	9.964826	9.622561	10.377439	10.035174	10.412612	15	44 45	9.605032	9.961569	9.643120	10.356880	10.038375	10.395255	16	
4.6	9.587688	9.964773	9.622915	10.377085	10.035227	10.412312	14	46	9.605319	9.961513	9.643806	10.356194	10.038431	10.394968	15	
48	9.588289	9.964719	9.623269	10.376731	10.035280	10.412011	13	47	9.605606	9.961458	9.644148	10.355852	10.038542	10.394394	13	
49	9.588591	9.964613	9.623976	10.376024	10.035333	10.411711	12	48 49	9.605892	9.961402	9.644490	10.355510	10.038598	10.394108	12	
50	9.588890	9.964560	9.624330	10.375670	10.035440	10.411110	10	50	9.606465	9.961290	9.645174	10.354826	10.038654	10.393821	11	
51	9.589190	9.964607	9.624683	10.375317	10.035493	10.410810	9	51	9.606751	9.961235	9.645516	10.354484	10.038765	10.393535	10	
52	9.589489	9.964454	9.625036	10.374964	10.035546	10.410511		52	9.607036	9.961179	9.645857	10.354142	10.038821	10.392964	8	
54	9.590088	9.964347	9.625741	10.374259	10.035659	10.410211	7	53 54	9.607322	9.961123	9.646199	10.353801	10.038877	10.392678	7	
55	9.590387	9.964294	9.626093	10.373907	10.035706	10.409613	5	55	9.607892	9.961011	9.646881	10.353119	10.038989	10.392393	-	
56	9.590686	9.964240	9.626445	10.373555	10.035760	10.409314	4	56	9.608176	9.960955	9.647222	10.352778	10.039945	10.392108	5	
58	9.591282	9.964133	9.627149	10.373203	10.035813	10.409016	3 2	57 58	9.608461	9.960899	9.647562	10.352438	10.039101	10.391539	3	
59	9.591080	9 964080	9.627501	10-372499	10.035920	10.408420	,.I	59	9.609029	9.960786	9.647903	10.352097	10.039157	10.391255	2 I	
00	9.591878	9.964026 Sine.	9.627852	10.372148	.10.035974	10.408122	0	δρ	9.609313	9.960730	9.648583	10.351417	10.039270	10.390687	0	
- Secant. IV									194	Sine.		Tang.		Secant.	M	
67 Degrees.								. 66 Degrees.								

24	Deg	ree.	s.

		-	24 L	egrees.		1100,0					25 L	egrees.			_1
Min.	Sine		Tang.		Secant.		ı	Mis.	Sine	-	Tang.		Secant.		
-	9.609313	9.960730	9.648583	10.351417	10.039270	10.390687	60	-0	6.625948	9.957276	9.668671	10.331327	10.042724	10.3740 2	6
1	9.609597	9.960674	9.648923	10.351077	10.039326	10.390403	59	2	9.626219	9.957217	9.669002	10.330998	10.042783	10.373781	19
2	9.609880	9.960618	9.649263	10.350737	10.039382	10.390120	58	2		9.957158	9.669332	10.330000	10,6429-1	10.373740	57 8
3	9.610446	9.960505	9.649942	10.350058	10.039495	10.389553	57	4		9.957040	9.669991	10.330009	10.042960	10.371070	56
	9.610720	9.060448	9.650281	10.349719	10.039552	10.389271	55	-	9.627300	9.956981	9.670320	10.319680	10,043019	10.372700	55 2
6	9.611012	9.960392	9.6;0620	10.349380	10.039608	10.388988	54	6	9.627570	9.956921		10.329351	10.043078	10.371430	54
1 7	9.611294	9.960335	9.650959	10.349041	10.039665	10.388706	53	7	9.617840	9.956862	9.670977	10.320023	10.043138	10.371160	53
8	9.611876	9.960279	9.651636	10.348764	10.039721	10.358141	51 51	9	9.628378	9.956744	9.671631	10.328365	10.043150	10.371622	51
2	9.612140	9.960165	9.651974	10.348026	10.019814	10.387860	50	10	9.628647	9.956684	9.671063	10.328037	10.643316	10.371353	50
112	9.612421	9.960109	9.652312	10.347688	10.039891	10.387579	49	11	9.628916	9.956625	9.672291	10.327709	10.043375	10.371084	44
12	9.611702	9.960052	9.652650	10.347350	10.039948	10.387198	48	12	9.629184	9.956566	9.672619	10.327381	10.043434	10.370815	42
13	9.612983	9-959995	9.651988	10.347012	10.040005	10.387017	47	13	9.629453	9.956506	9 672947	10.327053	10.043553	10.370179	46
14	9.613545	9.959881	9.651661	10.346337	10.040118	10.386455	45		9.629989	9.956387	9,673602	10.326398	10.043613	10.370011	45
1.2	9.613825	9.959825	9.654000	10.346000	10.040175	10.386175	44	16	9.630151	9.956327	9.673929	10.316071	10 043673	10.369743	44
17	9.614105	9.959768	9.654337	10.345662	10.040131	10.385895	43	17	9.630524	9.956268	9.674257	10.325743	10.043731	10.369476	43
18	9.614385	9.959711	9.654674	10.345326	20.040289	10.385615	42	18	9.630792	9.956208	9.674584	10.315416	10.043751	10.369208	H
19	9.614665	9.959653	9.655011	10.341989	10.040346	10.385056	41	19	9.631326	9.956089	9.675137	10.324763	10.043911	10.768674	
20	9.614944	9.959596	9.655318	10.344652	10.040404	10.305050	40 39	20	9.631591	9.956029	9.675564	10.324436	10.043971	10.36840-	30
22	9.615502	9.959482	9.656010	10.343980	10.040518	10.384498	38	23	9.631859	9.955969	9.675890	10.324110	10.044031	10.308141	100
23	9.615781	9-959425	9.656356	10.343644	10.040575	10.384219	37	23		9.955909	9.676216	10.313783	10 044091	10.361874	37
12	9.616060	9.959367	9.656692	10.343308	10.040533	10.383940	36	24	9.632392	9-955849	9.676543	10.323457	10.044151		14
25	9.616338	9.959310	9.657028	10.341972	10.040690	10.383662	35	25	9.632658	9.955789	9.676869	10.323131	10.044211	10.367341	35
26	9.616616	9.959153	9.657364	10.342636	10.040747	10.383384	34	27		9.955669	9.677520	10.322480	10.044331	10.366811	33
28	9.617172	9.959138	9.658034	10.341966	10.040862	10.382828	32	28	9.633454	9.955609	9.677846	10.322154	10.044391	10.366 46	12
29	9.617450	9.959080	9.658369	10.341631	10.040919	10.382550	31	19		9.955548	9.678171	10.321829	10.044452	10.366281	31
30	9.617727	9.959023	9.658704	10.341296	10.040977	10.382273	30	30			9.678496	10.321504	10.044512	10.366016	3C
31	9.618004	9.958065	9.659039	10.340961	10.041035	10.381996	29	31	9.634514	9.955428	9.678821	10.321179	10.044572	10.367486	28
32	9.618558	9.958850	9.659778	10.340292	10.041150	10.381442	27	32	9.634778	9.955307	9.679471	10.320529	10.044693	10.36;222	27
34	9.618834	9.958792	9.660042	10.339958	10.041208	10.381166	26	34	9.635042	9-955247	9.679795	10.320205	10.044753	10.3640.8	
34	9.619110	9.958734	9.660376	10.339624	10.041265	10.380850	25	35	9.635306	9.955186	9.680120	10.319380	10.044814	10.364694	
36	9.619386	9.958677	9.660710	10.339290	10.041323	10.380614	24	36	9.635570	9.955126	9.680444	10.519556	10.044874	10.364430	
33	9.619662	9.958561	9.661043	10.338927	10.941381	10.380062	22	37	9.635097	9.955005	9.681092	10.318908	10.044995	10.3630-3	
30		9.958503	9.661710	10.338290	10.041497	10.379787	21	39	9.636360	9.954944	9.681416	10.318584	10.045056	10.363640	21
40	9.620488	9.958445	9.662043	10.337957	10.041555	10.379512	20	40	9.636623	9.954883	9.681740	10.318260	10.045117	10.361377	20
41	9.620763	9.958387	9.662376	10.337623	10.941613	10.379237	19	41	9.636886	9.954823	9.682063	10.317937	10.045177	10.363144	10
42	9.621313	9.958329	9.662709	10.337291	10.041671	10.378962	17	43	9.637148	9.954762	9.682386		10.045238	10.362589	
4.	9.621587	9.958212	9.663374	10.336625	10.541787	10.378413	16	43	9.637671	9.954640	9.683033	10 316967	10.045359	10.362327	16
	9.621861		9.663707	10.336293	10.041846	10.178179	15	43	9.637935	9-954579	9.683356	10.316644	10.045421	10.362065	15
40	9.612135	9.958096	9.664039	10.335961	10.041904	10.377865	14	46	9.638197	9.954518	9.683678		10.045482	10.361803	14
4	9.622409	9.958038	9.664371	10.335629	10.041962	10.377591	13	47		9.954457	9.684001	10.315999	10.045643	10.361541	
41	9.622682	9.957979	9.664703	10.335297	10.042021	10.377318	11	48	9.638981		9.684646	10.315354	10.04 566 5	10.361019	8
51		-	9.665366	10.274614	10.041137	10.376771	10	77	9.639242	9.954274	9.684968	10.315032	10.045716	10.360758	10
5			9.665697	10.334302	10.042196		9	51		9.954213	9.68 5290	10.314710	10.04578=	10,360497	0
5:	9.623777	9.957746	9.666029	10.333971	10.042254	10.376226	8	52		9.954152	9.685612		10.045848	10.360136	8
5			9.666601	10.353640	10.042313	10.375953	6	53	9.640024	9.954090	9.685255	10.314066	10.045910	10.359976	6
5				10.333309	10.041430		5	54	9.640544	9.953968	9.686577	10.313423	10.046032	10.359455	1.5
5	5 9.624591 6 9.624861	9-957570	9.667352	10.332979	10.041430		4	55		9.953908			10.046004	10.359196	4
5	9.615135		9.667682	10.332318	10.042548	10.374865	3	57	9.641064	9.953845	9.687219	10.312781	10.046155	10.358936	3
5	8 9.625406	9.957393	9 668013	10.331987	10.042607		12	58		9.953783			10.046217	10.358676	3
5				10.331657	10.042565		0	60	9.641842	9.953722	9.687861	10.313130	10.046340	10.358148	0
1-	9.02 1940	Sine.	7	Tang.		Secunt.	M	-	7.04104.	Sing		Tang.		Secant.	M
1-		, ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,		D			-	-			61	Degrees			-

65 Degrees

64 Degrees.

26 Degrees.

27 Degrees.

<u> </u>			20 4	Degrees.							27	Degrees.	-		
Mun.	Sine.	i e	Tang.		Secant.			Min.	Sine.°		Tang.		Secant.		
0	9.641842	9.953660	9.688182		10.046340	10.358158	60	0	9.657047	9.049881	9.707166	10.292834	10.050119	10.342953	60
1	9.642101	9.953598	9.688822	10.311498	10.046410	10.357899	59	2	9.657295	9.949816	9.707478	10.292522	10.050183	10.342705	59
3	9.642618	9-953537	9.689143	10.310857	10.046525	10.357382		3	9.657790	9.949688	9.708102	10.291898	10.050312	10 342210	57
4	9.642876	9.953412	9.689463	10.310537	10.046587	10.357123	56	4	9.658037	9.949623	9.708414	10.291586	10.050377	10.341963	56
5	9.643135	9-953351	9.689783	10.310217	10.046648	10.356865	55	5	9.658284	9.949558	9.708726	10.291274	10.050441	10.341716	55
6	9.643393	9.953228	9.690103	10.309897	10.046710	10.356607	54	6	9.658531	9.949494	9.709037	10.290963	10.050506	10.341469	54
8	9 643948	9 953 166	9.690742	10.309258	10.046834	10.356092	52	8	9.659024	9-949364	9.709660	10.290340	10.050635	10.340975	52
9	9.644165	9.953104	9.691062	10.308938	10.046896	10.355835	53	_9	9.65,9271	9.949300	9.709971	10.290027	10.050700	10.740729	51
10	9.644423	9.953042	9.691381	10.308619	10.046958	10.355577	50	10	9.659517	9.949235	9.710282	10.289718	10.050765	10.340483	50
11	9.644680 9.643936	9.952980	9.691700	10.308300	10.047020	10.355320	49	11	9.659763	9.949170	9.710593	10.289407	10.050830	10.340237	49
123	9.645193	9 952855	9.692338	10.307662	10.047145	10.354807	47	13	9-660255	9.945040	9.711215	10.288785	10.050960	10.339745	47
14	9 945450	9-952793	9.692656	10.307343	10.047207	10.354550	46	14	9.660500	9.948975	9.711525	10.288475	10.051025	10.339499	46
15	9.645706	9-952731	9.692975	10.307025	10.047269	10.354294	45	15	9.660746	9.948910	9.711836	10.288164	10.051090	10.339254	45
16	9.645962	9.952668	9.693293	10.306707	10.047331	10.354038	44	16	9.661236	9.948845	9.712456	10.287544	10.051155	10.339009	44
18	9 646473	9.952544	9.693930	10.306070	10.047456	10.353526	42	18	9.661481	9.548715	9.712766	10.287234	10.051285	10.338519	42
19	9.646729	9.952481	9.604248	10.305752	10.047519	10.353271	41	19	9.661726	9.948649	9.713076	10.286924	10.051350	10.338274	41
20	9.646984	9.952419	9.694566	10.305434	10.047581	10.353016	40	20	9.661970	9.948584	9.713386	10.286304	10.051416	10.338030	40
71	9.647239	9.952356	9.695201	10.305117	10.047644	10.352,00	39 38	22	9.662459	9.948453	0.714004	10.285995	10.051546	10.337541	39
23	9.647749	9.952231	9.695518	10.304482	10.047769	10.352251	37	23	9.662703	9.948388	9.714314	10.285685	10.051612	10.337297	37
24	9-648004	9.952168	9.695835	10.304164	10 047832	10.351996	36	24	9.662946	9.948323	9.714624	10.285376	10.051677	10:337054	36
2.5	9.648258		9 696153	10.303847	10.047894	10.351742	35	25	9.663190	9.948257	9.714933	10.285067	10.051743	10.336810	35
26	9.648512		9 696786	10.303530	10.047957	10.351488	34	27	9.663433	9.948126	9.715551	10.284449	10.051874	10.336323	34
28	9 649020	9.951917	9.697103	10.302897	10.048083	10.350980	32	28	9.663920	9.948060	9.715859	10 284140	10.051940	10.336080	32
29	9 649274		9.697420	10.302580	10.048146	10.350726	31	29	9.664163	9-947995	9.716168	10.283832	10 052005	10.335837	31
30	9 649527	9.951791	9.697736	10.302264	10.048209	10.350473	30	30	9.664406	9.947929	9.716477	10.283523	10.052071	10.335594	30
31	9.649781		9.698369	10.301947	10.048335	10.349966	28	32	9 664891	9.947797	9.717093	10.282907	10.052203	10.335109	28
33	9.650287	9.951602	9.698685	10.301315	10.048398	10.349713	27	33	9.665133	9-947731	9.717401	10.282509	10.052269	10.334867	27
34	9.650939		9.699001	10.300999	10.048461	10.349460	26	34	9.665375	9.947665	9.717709	10.281983	10.052334	10.334625	26
3 3 5	9.650792		9.699316	10.300684	10.04858	10.349208 10.348956	25	35 36	9.665617	9.947599	0.718325	10.281675	10.052466	10.334303	25
36	9.651297		9.699947	10-300053	10 048651	10.348703	23	37	9.666100	9.947467	9.718633	10.281367	10.052533	10.333900	23
38	9.651549	9.951286	9.700263	10.299737	10.048714	10.348451	22	38	9 666341	9.947401	9.718940	10.281060	10.052599	10.333658	22 -
39	9.651800			10.299422	10.048778	10.348260	21	<u>39</u>	9.666825	9.947335	9.719240	10 280445	10.052005	10.333417	20
40	9.65233		9.700893	10.298792	10.048841	10.347948	19	40 41	0.66706	9.967203	9.719862	10 280138	10.052797	10.333170	19
41	9.652555			10.298477	10.048968	10.347445	18	42	9.667305	9.567136	9.720169	10.279831	10.052864	10.332695	18
43	9.6 52806			10.298163	10.049031	10.347194	16	43	9.667.786	9.967070	9.720476	10.279524	10.052930	10.332454	16
§ 44	9.653057			10.297848	10.049095	10.346692	15	44	9.668026	9.946037	9.721089	10 278911	10.053063	10.332214	15
45	9.6;3307	9.950841	9.702466	10.297534	10.049159	10.346442	14	45	0.668166	9.946871	9.721396	10.278604	10.053129	10.331733	14
1 4-	9.653808	9.950714	9.703095	10.296905	10.049286	10.346192	13	47	9.668506	9.946804	9.721702	10.278298	10.053196	10.331494	13
4.9	9.654050			10.296591	10.049350	10.345941	12	48	9.668746	9.946738	9.722008	10.277685	10.053262	10.331254	11
49	9.6543-9				10.049414	10 345442	10	49 50	0.660225	9.946604	9.722621	10.277379	10.053395	10.330775	10
50	9.654558			10.295904	10.0494/3	10.345442	9	51	9.669464	9.946538	9-722927	10,277072	10.053462	10.330536	9
52	9.655057	9.950364	9.704663	10.295337	10.049606	10.344442	8	5,2	9.669,03	9.946471	9.723232	10.276768	10.053529	10.330297	8
53	9.655307		9.704976	10.295023	10.049670	10.344693	7	53 54	9.66,942	9.946404	9.723538	10.276156	10.053566	10.336050	6
54	9.655556			10.294710	10.049734	10.344195	5	27	0.670419	9,946270	2.724-49	10.275851	10.053730	10.329581	5
55	9.055054	9.950202		10.294084	10.049862	10.343046	4	56	9.670658	9.946203	9.724454	10.275546	10.053797	10.329342	4
57	9.656302	9.950074	9.706228	10.293772	10.045926	10.343698	3	57	9.670896	9.046136	9-724759	10.275240	10.053864	10.329104	3
58	9.65655	9.950000		10.293459	10.050055	10.343449	1	58 59	9.671134	0.946002	9.725369	10 274630	10.053998	10.328628	1
59			9.707166	10.291834	10.051119	10.342953	0	60	9.671609	9.945935	9.725674	10.274326	10.054065	10.328391	0
1 -	1	Sine.		Tang.		Secant.	M		1	Sine	1	Tang.		Secant.	M

63 Degrees.

62 Degrees.

_		1	- 0	D			_		0						3
			28	Degrees.			E			29	Degrees.			_/	
Min.	Sine.		Tang.		Secant.		1	Min.	Sine.	9.0	Ta ·g.		Secant.		
0	9.671609	9-945935	9.725674	10.274326	10.054065	10.328391	60	0	9.6855799	9.941819	9-743752	10.255950	10.0;8181	10.31442 /	60
2	9.672084	9.945800	9.726284	10.273716	10.054199	10.327916	59	2	4.686027	9.9416-9	9 744348	10.2 3652	10.058322	10. 1 973	56
3 4	9.672321	9-945733	9.726892	10.273412	10.054267	10.32767>	57	3 4	9.686234	9.041539	9.744645	10.25,35	10.068-61	10.313740	10
- 5	9.672795	9.945598	9-727197	10.271803	10.054401	10.127105	55	5	9 686709	9.941468	9.745240	10.254700	10.0.8,31	10. 113241	55
	9.673032	9.945531	9.727501	10.272499	10.054469	10.326968	54	6	9.686936	9.941398	9-74-538	10.254:62	10.0;86:2	10.311604	54
7 8	9.673505	9.945396	9.718109	10.271891	10.054604	10.326495	52	8	9.687389	9.941257	9. 46132	10.253868	10.058742	10.312610	SI
9	9.673977	9.945328	9.728716	10.271284	10.054739	10.126021	50	9	0.687842	9-941187	9.746726	10.253571	10.0 (8862	10.312354	(I)
11	9.674213	9 945193	9.729020	10.270,80	10.054807	10.325787	49	11	9.698069	9.941046	9.747023	10.252977	10.058954	10.311931	49
12	9.674448	9.945125	9.729323 9.729626	10.27 3677	10.054874	10.325551	48	12	9.688295	9-940975	9-747319	10.252681	10.039003	10.311705	48
14	9.674919	9-944990	9.729929	10.270070	10.055010	10.325081	46	14	9.688747	9.940834	9.747912	10.252087	10.059166	10.311253	46
16	9.675155	9.944922	9-730232	10.269767	10.055078	10.324845	45	16	0.689198	9.940763	9.748209	10.251791	10.059237	10.311028	45
18	9.675624	9-944786	9.73°535 9.73°838 9.731241	10.269862	10.055214	10.324376	43	17	9.689423	9.940622	9.748801	10.251199	10.059378	10.310577	43
19	9.676094	9-944718	9-731444	10.268556	10.055350	10.324141	42 41	19	9.689648 9.689873	9.940480	9-749097	10.250607	10.059520	10.310117	42
20	9.675318	9-944582	9.731746	10.268254	10.055418	10.323672	40	20	9.690098	9.940409	9.749689	10.250311	10.059591	10.309902	40
21	9.676796	9.944514	9-732351	10.267649	10.055554	10.323438	39	21	9.690323	9.940338	9.749985	10.250015	10.059733	10.309452	39
23 24	9.677030	9.944377	9.732653	10.267347	10.055622	10.322970	37 36	23	9.690772 9.690996	9.940196	9.750576	10.249424	10.059804	10.309228	37
25	9.677497	9.944241	9.733257	10-266743	10.055759	10.322502	35	24	9.691220	9.940053	9.751167	10.248833	10.050946	10, 308 770	35
26 27	9.677738	9-944172	9.733558	10.266442	10.055827	10.322263	34	26	9.691444	9.939982	9.751462	10.248538	10.060018	10.308355	54
28	9.678197	9.944036	9.734162	10.265818	10.055964	10.321803	33 32	28	9.691892	9.939913	9.751757	10-247948	10.060160	10.308108	33
29	9.678430	9.943967	9.734463	10.265537	10.056033	10.321570	31	29	9.692115	9.939768	9-752347	10.247653	10.060232	10.307884	31
30	9.678895	9.943830	9.731764	10.264074	10.056170	10.721104	30 29	30	9.692339	9.939697	9.752642	10.247062	10.060375	10.307338	30
32	9.679128	9.943761	9.735668	10.264633	10.056239	10.320872	28	32	9.692785	9-979554	9-753231	10.246769	10.060446 10.060518	10.307215	28
34	9.679592	9.943614	9.735968	11.264031	10.056376	10.320408	26	33 34	9.693231	9-939410	9-753820	10.246180	10.060589	10.306769	26
3 5 3 6	9.679824	9-943555	9.736269	10.263731	10.056445	10.320176	25 24	35	9.693453	9-939339	9.754115	10.245885	10.060661	10.306 547	25
37	9.680288	9-9+3417	9.736870	10,267120	10.056583	10.319712	23	36 37	9.693898	9.939145	9-754703	10.245297	10.060805	10.306102	23
38	9.680519	9-943348	9.737171	10.262829	10.056652	10.319481	21	38 39	9 694120	9.939123	9.754997	10.245001	10.060877	10.305880	21
40	9.680982	9.943210	9.737772	10.262220	10.056790	10.319013	20	40	9.694564	9.938980	9.755585	10.244415	10.061020	10.302436	20
41	9.681213	9-943141	9.738071	10.261928	10.056859	10.318787	19	41 42	9 695007	9.938008	9.755878	10.244122	10.061092	10.305214	19
43	9.681674	9.943003	9.738671	10.261329	10.056995	10.318326	16	43	9.695229	9.938763	9.756465	10.243535	10.061236	10.304771	17
44	9.682135	9-942933	9.739271	10.260720	10 057136	10.318095	15	45	0.695450	9.938691	9.756759	10 242948	10.061381	10.704230	15
45 46	9.682365	9.942795	9-739570	10.260430	10.057205	10.317635	14	46	9.695892	9.938547	9-757345	10.242655	10.061453	10.304108	14
47	9.682595	9.942725	9.739870	10.259831	10.057274	10.317405	13	47 48	9.696113	9.938475	9.757638	10.242362	10.061508	10.303660	13
49	9.683055	9.942587	9.740468	10.259532	10.057413	10.316145	11	49	9.696554	9.938330	9.757931	10.241481	10.061670	10.303416	11
50 51	9.683284	9.942517	9.740767	10.259233	10.057483	10.316716	9	50	9.696774	9.938258	9.758517	10.24119	10 061815	10 303004	9
ς2 53	9.683743	9.942378	9/741365	10 258635	10.057622	10.316257	8	52	0.697215	9.938113	9.759102	17,240896	10.961887	10.30278	8
13 54	9.684201	9.042139	9.741962	10.258038	10.057-61	10.310013	6	53 54	9.697435	9.938 40	9.759305	10.240713	10.061033	10.30-34 ;	6
55	9.684430	9.942169	9.742261	10 257739	10.05-831	10.315570	5	55	9.6078-4	9.937895	9.759979	10.240021	10.062105	10 302126	5
57	9.684817	9.942029	9.7428 18	10.217142	17.057971	10.315342	3	56	9.648014	9.937811	9.760172	10.239436	10.062251	10.30168-	
58 59	9.685343	9.941959	9.743156	10.256844	1 .058041	10.31488;	1	58 59	9.698532	9.937676	9.760856	10.239144	10.062336	10. 301468	
60	9.685571	9.941819	9.743752	10.256248	10.058181	10.314429	0	60	9.608070	9-937531	9.761419	10.238561	10.062.169	10.701033	0
-		Sine.	'	Tang.	1	Secunte	M	1		Sine		Tang.		Secant,	1.11
1			61.	Degrees.		-				77	60 .	Degrees.			

-			30 I	Degrees.			-	_			21 /	Degrees.			-
-			7					-			31 1	ı gruss			-
Min.	Sine.		Tang.		Secant.		ı	Min.	Sine		Tang.	•	Secant.		
0 1	9.698970	9-937537	9.761439	10.238561	10.062469	10.301030	6c 59	0.	9.711839	9.933066	9.778774	10,221226	10.066934	10.288161	60
2	9.699407	9-937458 9-937 3 85	9.762223	10-227077	10.062615	10.300593	58	2	9.712260	9.932990	9.779060	20.220654	10.067086	10.287950	1 48
3.	9.699626	9-937312	9.762314	10.237686	10.062688	10.300374	57 56	3	9.712469	9.932838	9.779632	10,220368	10.067162	10.287530	57
	9.700062	9.937165	9.762897	10.237103	10.062835	10.299938	55		9.712889	9.932685	9.780203	10.219797	10.067315	10.287111	55
6	9.700280	9.937092	9.763188	10,236812	10.062908	10.299720	54 53	6	9.713098	9.932609	9.780489	10.219511	10.067391	10.286602	54
8	9.700716	9.936,46	9.763770	10.236230	10.063054	10.299284	52	8	9.713517	9-932457	9.781060	10.218940	10.067543	10.286483	52
9	9.700933	9.936872	9.764261	10.235939	10.063138	10.298849	51 50	9	9.713726	9-932380	9.781346	10.218654	10.067620	10.286274	52
11	9.701368	9.936725	9.764643.	10.235357	10.063275	10.298634	49	11	9-714144	9.932228	9.781916	10.218084	10.067772	10.285856	49
12	9.701585	9.936652	9.764933	10.235067	20.063348	10,298415	48 47	12	9.714352	9.932151	9.782201	10.217799	10.067849	10.285648	48
14	9.702019	9.936505	9.765514	10 234486	10.063495	10.297981	46	14	9.714769	9.931998	9.782771	10.217229	10.068002	10.285231	46
15 16	9.702236	9-936431	9.765805	10.234195	10.063569	10.297764	45	15 16	9.714978	9.931921	9.783056	10.216660	10.068079	10,285022	
17	9.702669	9.936284	9.766385	10 233615	10.063716	10.297331	43 42	17	9.715394	9.931768	9.783341 9.783626 9.783910	10.216374	10.068232	10,284598	
19	9.703101	9.936136	9.766965	10.233035	10.063864	10.296899	41	29	9.715809	9.931614	9.784195	10.215805	20.068386	10.284191	41
20	9.703317	9-936062	9.767255	10.232745	10.063938	10.296683	40 39	20	9.716017	9.931537	9.784479	10,215521	10.068463	10.283981	40
22	9-703749	9-935914	9.767834	10.232166	10.064086	10.296251	38	22	9.716432	9.931383	9.78 5048	10.214952	10,068616	10.283568	38
23	9.703964	9.935840	9.768124	10.231876	10.064160	10.296036	37 36	23	9.716639	9.931306	9.785332	10.214668	10.068693	10.283361	37
25	9.704395	9'935692	9.768703	10.231297	20.064308	10.295605	35	25	9.717053	9.031152	9.785900	10,214100	10.068848	10.282947	35
26	9.704610	9.935618	9.768992	10.231008	10.064382	10.295390	34	26	9.717259	9.930998	9.786184	10.213816	10.068925	10.282741	34
28	9.705040	9.935460	9.769860	10.230429	10.064531	10.294960	32	28	9.717672	9.930920	9.786752	10.213248	10.069079	10.282327	32
29 30	9.705254	9-535395	9.770148	10.230140	10.064680	10.294531	31 30	10	9.718085	9.930766	9.787319	10-212681	10.069234	10.281915	30
31 32	9.705683	9.935246	9.770437	10.229563	10.064754	10.294317	29	31	9.718291	9.930688	9-787603	10.212397	10.069312	10.281709	29
33	9.706112	9.935171	9.771015	10.228985	10,064901	10.293888	27	32 33	9.718703	9.930533	9.788170	10,211830	10.060467	10.281297	27
34	9.706326	9.935022	9.771303	10.228697	10.064978	10.293674	26 25	34	9.718909	9.930456	9.788453	10.211547	10.069544	10.281091	26
35	9.706753	9.934873	9.771880	10.228120	10.065127	10.293247	24	35 36	9.719320	9.930300	9.789019	10.210981	20.069700	10.280680	24
37	9.706967	9.934798	9.772168	10.227832	10.065202	10.293033	23	37 38	9.719525	9.930223	9.789302	10.210698	10.069777	10.280475	23
39	9.707393	9.934649	9-772745	10.227255	10.065351	10.291607	21	39	9-719935	9.930067	9.789868	10.210132	10.069933	10.280065	
40 41	9.707666	9.934574	9.773033	10.226967	10.065426	10.292393	20	40 41	9.720140	9.929989	9.790151	10.209849	10.070011	10.279860	
42	9.708032	9.934424	9.773608	10.226392	10.065576	10.291968	18	42	9.720549	9.929833	9.790716	10.209284	10.070167	10.279451	28
43	9.708457	9-934349 9-934274	9.774184	10.225816	10.065726	10.291542	16	43 44	9.720958	9.929755	9-790999	20.208719	10.070323	10.279042	16
45 46	9 708670	9.934199	9.774471	10.225529	10.065801	10,291330	15	45 46	9.721162	9.929599	9.791563	10 208436	10.070401	10.278838	
147	9.709094	9.934048	9.775046	10.224954	10.065952	10.290906	23	47	9.721570	9.929442	9.792128	10.207872	10.070558	10,278430	13
48	9.709306	9.933973 9.933898	9.775621	10.224667	10.066102	10.290694	12	48 49	9.721774	9.929364	9.792410	10.207590	10.070636	10.278226	12
50	9.709730	9.933822	9.775908	10.224092	10.066178	10.290270	10	50	9.722181	9.929207	9-792974	10.207026	10.070793	10.277819	10
52	9.710153	9.933747	9.776482	10.223805	10.066253	10.290058	9	51 52	9.722385	9.929129	9.793256	10.206744	10.070871	10.277615	8
53	9.710364	9.933596	9.776768	10.223231	10.066404	10.289636	7	53	9.722791	9.928972	9.793819	10.206180	10.071028	10.277209	7 6
54. 55	9.710786	9-933520	9-777342	10.222658	10.066555	10,289214	-5	<u>54</u> 55	9-723297	9.928814	9.794101	10.205617	10.071185	20.276805	-5
56	9.710997	9.933369	9.777628	10.222372	10.066631	10.289003	4	56	9.723400	9.928736	9.794664	10.205336	10.071264	10.276603	4
57	9.711419	9.933217	9.778201	10.221799	10.066783	10.288581	3 2	57 58	9.723805	9.928578	9.795227	10.204772	10.071422	10.276295	
60	9.711629	9.933141	9.778487	10.221512	10.066858	10.288371	1	59	9.724007	9.928499	9.795508	10.204492	10.071501	10.275992	0
-		Sine.	1	Tang.		Secant.	M	-		Sine.	[Tang.	1	Secant.	M
			59	Degrees.	1000						58	Degrees.			_

			32 D	egrees.							33 1	Degrees.			
Min.	Sine		Tang.		Secant.			Min.	Sine		Tang.		Secant.		
0	9.724210	9.928420	9.795789	10.204211	10.071579	10.275790	6c	0	9.736103	9.923591	9.812517	10.187481	10.076409	10.161891	60
2	9-734412	9.918262	9.796351	10.203649	10.071737	10.275386	58	2	9.736303	9.923509	9.812794	10.187206	10.076573	10.263697	59
3	9.724816	9.928183	9.796632	10,203368	10.071817	10.275184	57	3	9.736692	9.923345	9.813347	10.186653	10 076655	10.263308	57
4	9-72 5017	9.928104	9-796913	10.203087	10.071996	10.274983	20	4	9.736886	9.923263	9.813613	10.186377	10 076819	10.263114	56
8	9.725219	9.927946	9 797474	10.202525	10.072054	10.274580	54	6	9.737274	9.9232098	9.814175	10.185824	10.076902	10.26292-	55 54
7	9.725622	9.917867	9.797755	10.202245	10.072133	10.274378	53	7 8	9.737467	9.923016	9.814452	10.185548	10.0,6484	10 262532	53
9	9.725823	9.927787	9.798316	10.201684	10.072292	10.274177	51	9	9.737661	9.922851	9.814728	10 185272	10.077667	10.262339	51
10	9.726225	9.927628	9.798596	10.201404	10.072371	10.273775	50	10	9.738048	9.922768	9.815279	10.184720	10.077232	10.261952	50
11	9.726426	9-927549	9.798877	10.201123	10.072451	10.273574	49	н	9.738241	9.922686	9.815555	10.184445	10.07;314	10.261756	44
23	9.716827	9.927390	9.799437	10.200563	10.071610	10.273173	4?	13	9.738627	9.922603	9.821107	10.183893	10.077397	10.261566	48 47
14	9.727027	9.927320	9.799717	10.200283	10.072690		46	14	9.738820	9.922338	9.816382	10 183618	10.077562	10.261180	46
16	9.727128	9.927231	9.799997	10.199723	10.072769	10.172772	45	15	9.739013	9.922355	9.816658	10.183342	10.077645	10.260987	45
17	9.727628	9.927071	9.800557	10.199443	10.072929	10.272372	43	17	9.739398	9.922189	9.817209	10.182791	10.077812	10.260602	44
19	9.727828	9.926991	9.800836	10.198884	10.073009	10.272172	42	18	9.739590	9.922106	9.817484	10.182516	10.077894	10.260410	42
20	0.728227	9.926831	9.801396	10.198604	10.073169	10.271773	40	20	9.739783	9.921040	9.818035	10.181965	10.07/977	10.26002;	41 40
21	9.728427	9.926751	9.801675	10.198325	10.073249	10.271573	39	21	9.740167	9.521857	9.818210	10.181690	10.078143	10.259833	30
22	9.728626	9.926671	9.801955	10.193045	10.073329	10.271374	38	22	9.740359	9.921774	9.818585	10.181415	10.078226	10.259641	38
24	9.729024	9.926511	9.802513	10.197487	10.073489	10.270476	36	24	9.740742	9.921607	9.819135	10.180865	10.078393	10.259449	36
25	9.729223	9.926432	9.802792	10.197207	10.073569	10.270777	35	25	9.740934	9.921524	9.819410	10.180590	10.078476	10.259066	35
27	9.729422	9.926351	9.803072	10.196928	10.073649	10.270578	34	26	9.741125	9.921441	9.819684	10.180316	10.078559	10.258875	34
28	9.719820	9.926190	9 803630	10.196370	10.073810	10.270180	32	28	9.741507	9.921357	9.810234	10.179766	10.078726	10.258492	33
29	9.730018	9.926110	9.803908	10.196091	10.073891	10.269982	31	29	9.741699	9.921190	9.810508	10.179492	10.078310	10.258301	31
30	9.730216	9.925949	9.804187	10.195813	10.073971	10.269783	20	30	9.741889	9.921107	9.820783	10.179217	10.078893	10.258110	39
32	9.730613	9.925868	9.804745	10.195255	10.074132	10.269387	28	31 32	9.742080	9.921023	9.821332	10.178668	10.079061	10.257729	28
33	9.730811	9.925787	9.805023	10.194977	10.074212	10.269189	27	33	9.742462	9.920855	9.821606	10.178394	10.079144	10.257638	27
34	9.731206	9.925626	9.805580	10.194420	10.074374	10.268794	25	34 35	9.742652	9-920688	0.822154	10.177845	10.079223	10.257158	25
36,	9.731404	9.925545	9.805859	10.194141	10.074455	10,268596	24	36	9-743032	9.920604	9.822429	10.177571	10.079306	10 256967	2.4
37	9.731601	9.925465	9.806137	10.193863	10.074535	10.268398	23	37 38	9.743222	9.920520	9.822703	10.177297	10.079480	10.256777	23
39	9.731996	9.925303	9.806693	10.193307	10.074697	10.268004	2.7	39	9.743602	9.920352	9.823250	10.176749	10.079648	10.256398	21
40	9-732193	9.925222	9.806971	10.193029	10.074778	10.267807	20	40	9-743792	9.920268	9.823524	10.176476	10.079731	10.256208	20
42	9-732390	9.925141	9.807249	10.192751	10.074859	10.267601	19	41	9-743982	9.920099	9.823798	10.176202	10.079816	10.256018	19
43	9.732784	9.924979	9.807805	10.192195	10.07;021	10.267216	17	43	9.744361	9.910015	9.824345	10.175654	10.079985	20.255639	17
144	9.732980	9.924857	9.808083	10.101917	10.075103	10.267020	16	44	9.744550	9.919011	9.824619	10.175381	10.080069	20.255540	16
45	9-733177	9.924816	9.808618	10.191639	10.075184	10.266823	14	45	9-744739	9.919846	9.824893	10.175107	10.080154	10.255261	15 14
47	9.733569	9.924653	9.808916	10.191084	10.075346	10.266431	13	47	9.745117	9.919677	9.825439	10.174561	10.080322	10.254883	13
48 49	9.733765	9.924572	9.809193	10.190807	10.075418	10.266235	72	48 49	9-745306	9.919508	9.825713	10.174287	10.080407	10.254694	12
50	9-734157	9-924409	9.809748	10.190252	10.075591	10.265843	10	50	9.74 683	9.919424	9.826259	10-173741	10.080576	10.254317	10
51	9-734353	9.924328	9.810025	10.189975	10.075672	10.265647	9	51	9.74 (871	9.914339	9.826532	10.173468	20,080661	10.2 54 129	2
52	9-734548	9.924246	9.810302	10.189697	10.075754	10.265451	0	52	9.746259	9.919169	9.826805	10.173194	10.080746	10.253940	7
54	9-734939	9.924083	9.810857	10,189143	10.075917	10.165061	8	H	9.746436	9.919084	9.827351	10.172649	10.080915	10.253564	6
55	9-735134	9.924011	9.811134	10.188866	10.07 5909	10.264865	15	55	9.746624	9.919000	9.827624	10.172376	10.081000	10 253376	5
50	9-735330	9.923919	9.811410	10.188589	10.076080	10.264670	4	57	9.746009	9.919915	9.824897	10.172103	10.081085	10.253188	4
58	9-735719	9-923755	9.811964	10.188036	10.076245	10.264280	3	58	9.747187	9.918744	0 828442	10.171458	10 081255	10.252811	2
59	9.735914	9.923673	9.812241	10.187759	10.076327	10.264086		19	9.747374	9-918659	9.818987	10 171285	10.081341	10.252626	1
-	7,3113	Sine	1-3-7	Targ.	1	Secant.	Ñ.	-	9.747562	Sine	22.00	Tang.		Secant.	M
1			57	Degrees.		-	-				56	Degrees.			
-		_									-	0	_	-	-

-			34 D	egrees.				_			35 L	Degrees.			-
Min.	Sine		Tang.		Secant,			Min	Sine	.	Tang.		Secant.		
-0 -	9.747562	9.918574	9.828987	10.171013	10.081426	10.252439	60 59	0 1	9.758591	9.913364	9.845227	10.154773	10.086724	10.241409	60 59
3	9.747936	9.918404	9 829532 9.829805	10.170468	10.081596 10.081682 10.081767	10.252064	58 57 56	3	9.758952 9.759132 9.759312	9.913187 9.913099 9.913010	9.845764 9.846033 9.846302	10.154236	10.086812	10.241048	58 57
4 5	9.748310 9.748497 9.748683	9.918233 9.918147 9.918c62	9.830077 9.830349 9.830621	10.169651	10.081852	10.251503	55 54	4 5	9.759492	9.912921	9.846570	10.153429	10.087078	10.240508	56 55
7 8	9.748870	9.917976	9.830893	10.160107	10.082024	10.251130	53 52	7	9.759851	9.912744	9.847107	10.152892	10.087256	10.240148	53 52
<u>9</u> 10	9-749242	9.917805	9.831437	10.168563	10.081195	10.250757	51 50	9	9.760390	9.912566	9.847644 9.847913 9.848181	10.152356	10.087434	10.239789	51 50
11 13	9.749615 9.749801 9.749987	9.917634 9.917548 9.917462	9.831981 9.832253 9.832525	10.168019	10.082366 10.082452 10.082538	10.250385	49 48 47	11 12 13	9 760749	9 912388 9.912299	9.848449	10.151551	10.087701	10.239431	49 48 47
4	9.750172	9.917376	9.832796	10.167204	10.082624	10.249828	46 45	14	9.761106	9.912121	9.848985	10.151014	10.087879	10.238894	46
16 17	9.750543	9.91720;	9.8333339	10.166661 10.166389 10.166118	10.082796 10.082882 20.082968	10.249457	44	16 17 18	9.761464 9.761642 9.761821	9.911942 9.911853 9.911763	9.849522 9.849790 9.850057	10.150478	10.088058 10.088147 10.088237	10.238536 10.238358 10.238179	44
18 19 20	9.750914 9.751099 9.751284	9.917032 9.916945 9.916859	9.833882 9.834154 9.834425	10.165846	10.083054	10.248901	41	19	9.761999	9-911674	9.850325	10.149675	10.088326	10.238001	42 43 40
21 22	9.751469	9.916773	9.834696	10.165304	10.083227	10.248534	39 38	21 22	9.762356	9.911495	9.850861	10.149139	10.088505	10.237644	39 38
23 24	9.751838	9.916600		10.164762	10.083400	10.248161	37 36 35	23 24 25	9.762712 9.762889	9.911315 9.911226 9.911136	9.851396 9.851664 9.851931	10.148336	10.088774	10.237288	36
25 26 27	9.752207 9.752392 9.752576	9.916427	9.836051	10.163949	10.083659	10.247608	34 33	26 27	9.763245	9.911046	9.852199	10.147801	10.088954	10.236755	35 34 33
28 29	9.752760	9.916167	9.836864	10.163407	10.083833	10.247240	31	28 29	9.763600	9.910866	9.852733 9.853001 9.853268	10.147266	10.089134	10.236400	32 31
31	9.753128 9.753312 9.753495	9.915994	9.837405	10.162866	10.084006	10.246872	30 29 28	30 31 32	9.763954 9.764131 9.764306	9.910686	9.853535	10.146465	10.089314 10.089404 10.089494	10.236046	30 29 28
33 34	9.753679	9.915733	9.837946	10.162054	10.084267	10.246321	27 26	33 34	9.764485	9.910415	9.854069	10.145931	10.089585	10.235515	27 26
35	9.754046	9.915472	9 838757	10.161513 10.161243 10.160973	10.084441	10.245954 10.245771 10.245588	25 24 23	35 36 37	9.764838 9.765015	9.910235	9.854603 9.854870 9.855137	10.145397 10.145130 10.144863	10.089765 10.089856 10.089946	10.235162 10.234985 10.234809	25 24 23
38	9.754412	9.915297	9.839297	10.160702	10.084703	10 245405	22	38 39	9.765367	9.909963	9.855404	10.144596	10.090037	10.234633	21
40	9.754960	9.91503	9 840108	10.160162	10.084877	10.245040	19 18	40 41	9.765720 9.765896 9.766071	9.909782 9.909691 9.909601	9 855938 9.856204 9.856471	10.144062	10.090218 10.090308 10.090399	10.234280	20 19 18
42 43 44	9.755508	9.914860	9.840647	10.159622	10.085052	10.244674 10.244492 10.241310	17 16	42 43 44	9.766247	9,909510	9 8 56737 9.8 57004	10.143263	10.090490	10.233753	17 16
45 46	9.755872	9.91468	9.841187	10.158813	10.085315	10.244128	14	45 46	9.766599 9.766774 9.766949	9.909328 9.909237 9.909146	9.857270 9.857537 9.857803	10.142730 10.142463 10.142197	10.090672	10.233401 10.233226 10.233051	15 14 13
48	9.7 564 18	9.91442	9.841996	10.158273	10.085490	10.243764 10.243582 10.243400	12	47 48 49		9.909055	9.858069	10.141031	10.090945	10.232876	12
50		9.9142	9.842535	10.157465	10.08;754	10.243218	10	50	9.767475	9.908873	9.858602 9.858868	10.141398	10.091127	10.232525	10
53	9.757144	9.91308	9.843343	10.156026	10.08fo18	10.242674	7 6	52 53 54	9.767824 9.767999 9.768173	9.908691 9.908599 9.908507	9.859134	10.140600	10.091310 10.091401 10.091493	10.232176 10.232001 10.231826	7
54	9.757688	9.91350	0.843882 8 0 844151	10.156118	10.085194	10.242312	5 4	55 56	0.768348	0.908416	9.859932		10.091584	10.231652	5 4
17. 77	9.758040	9.91363	9.844420	10.155311	10.08637	10 241950 10 241770 10.241589	3 2 1	57 58	9.768697 9.768871 9.769045	9.908233	9.860464 9.860730 9.860805	10.139270	10.091767	10.231303	3 2 1
66		9.9'345 9.91336 Sine.		10.155042 10.154771 Tang.		10.241400 S ecant,	o M	60		9.907958 Sinc	9.861261	10.138739 Tang.	10.092042	10.230781 Secant.	o M
1	·		55	Degrees	ride or		-	-			54	Degrees.			

-			26 I	Degrees.			-				27	Degrees.			
-			30 1	- Cg. tt.			-	-	1		3/ 4	Degrees.			-
M.n.	Sine		Tang.		Secant.			Min	S.ne		Tang.		Secant.		
0	9 769219	9-907958	9.861261	10.138739	10.092042	10 230, 81	64	0	9-779463	9.902349	9.877114	10.122886	10.097651	10.12053	60
1 2	9.769; 16	9-907774	9.861792	10.118208	10.092226	10 2 30434	59	2	9-779798	9.902158	9.877640	10.1:2360	10.09-842	10 2202 2	59
3	9.769740	9.507682	9.862058	10.137942	10.092318	10.230260	57	3.	9.779965	9.902063	9.878765	10.122097	10.097957	10.220034	57
-2	9-770087	9.907498	9.862589	10.137411	10.092502	10.229913	5.5	-	9.750300	9.9018-:	7 878428	10.121572	10.098128	10.219700	55
6	9.770260	9 907406	9.862854	10.137146	10.092594	10.229740	54	6	9 780467	9.01776	9.378691	10.121309	10.098224	10.219533	¢4 .
8	9.770666	9.907121	9.863385	10.136615	10.092778	10.229394	52	8	9.780801	9.501585	9.879216	10.120784	10.098415	10.210199	53
9	9.770779	9.907017	9.863915	10.136085	10.002961	10 229043	50	9	9.781134	9.901394	9.879741	10.120322	10.098510	10.215032	51
11	9.771125	9.906945	9.864180	10.195820	10.093055	10.228875	49	12	9.281201	9.501298	9.880003	10.119997	20.098702	10.218600	49
12	9.771298	9.906852	9.864710	10.135555	10.093148	10 228702	48	12	9.781467	9.901202	9.880265	10.119735	10.095798 10.098894	10.218532	48
14	9.771642	9.906667	9.864975	10.135024	10.003333	10.228357	46	14	9.781800	9.901010	9.880790	10.119210	10.098,90	10.216190	46
15	9.771815	9.906574	9.865240	10.134760	10.093425	10.228185	45 44	16	9.781966	9.900914	9.881914.	10.118948	10.099086	10.218034	45
17	9.772159	9.906389	9.865770	10.134230	10.093611	10.227841	42	17	9.782298	9.900721	9.881576	10.118423	10.099374	10.217702	43
18	9-772331	9.906204	9.866300	10.133700	10.093796	10.227497	41	19	9.782630	9.900020	9.882101	10.117899	10.099471	10-217530	42
20	9-772675	9.906018	9.866829	10.133436	10.093889	10.227325	4C	20	9.782796	9.900433	9.882363	10.117637	10.099567	10.217204	40
21	9.772847	9.905925	9.867094	10.132906	10.094075	10 226981	39 38	21	9.783127	9.900337	9.882887	10,117113	10.099663	10.217039	39
23	9-773190	9-905832	9.867623	10.132642	10.094167	10.226310	31 36	23	9-783292	9.900144	9.883148	10.116852	10.095856	10.216708	37
24	9-773533	9.905645	9.867887	10.132113	10.094355	10 226467	35	25	9.783623	9.899951	9.883672	10.116328	10.100049	10.216377	36
26	9-773704	9.905552	9.868152	10.131848	10.094448	10.226296	34	26 27	9.783788	9.899854	0.883934	10.116066	10.100146	10.216212	34
27	9.774046	9.905366	9.868680	10.131320	10.094634	10.225954	32	28	9.784118	9.899660	9.884457	10.115543	10.100340	10.215882	33
29	9.774217	9.905272	9.858945	10.131055	10.094821	10.225783	31	29	9.784282	9.899564	9.884719	10.11(28)	10.100436	10.215718	31
30	9.774388	9.905085	9.869473	10.130527	10.094915	10.225442	29	30 31	9.784612	9.899370	9.885242	10.114758	10,100610	10.215553	30
32	9-774729	9.904992	9.869737	10.130263	10.095008	10.225271	28	32 33	9.784776	9.899273	9.885503	10.114496	10-100727	10.215224	28
34	9.775070	2.904804	9.870265	10.129735	10.095196	10.224930	26	34	9.785105	9.899078	9.886026	10-113974	10.100022	10.214895	26
35	9.775240	9.904617	9.870529	10.129471	10.095289	10.22476:	25	35	9.785269	9.898981	9.886288	10.113712	10.101116	10.214731	25
37	9.775580	9.904523	9.871057	10.128943	10.095477	10.224420	23	37	9.785597	9.898787	9.886810	10.113189	10.101213	10.214463	23
38	9.775750	9.904335	9.871321	10.128415	10.095671	10.224280	21	38 39	9.785925	9.898592	9 887072	10.112928	10.101311	10.214239	22
40	9.776090	9.904243	9.871849	10.118151	10.095759	10.223910	20	40	9.736089	9.898494	9.887594	10.112406	10.101506	10.213911	20
41 42	9.776259	9.904147	9.872112	10.127888	10.095853	10.223741	18	42	9.786252	9.898397	9.887855	10.112145	10.101603	10.213748	19
43	9.776598	9.903959	9.872640	10.127360	20.096041	10.123402	17	43	9.786579	9.898201	9.888377	10.111622	10.101798	10.213420	17
44	9-776937	9.903770	9.873167	10.126833	10.096230	10 223063	15	45	9.786905	9.838. 6	9.888900	10-111100	10.101994	20.213094	10
46	9.777106	9.903676	9.873430	10.126570	10.096324	10.222894	14	46	9.787069	9.897908	9.889160	10.110839	10.102042	10.212931	14
47 48	9-777175	9.903487	9.8/3947	10.126042	10.096517	10.221556	12	48	9 787395	9.80-712	9.889682	10.110318	10.102288	10.212604	13
49	9.777613	9.903393	9.874220	10.125780	10.096608	10.222387	11	49 50	9.787557	9.897614	9.839943 0.890204	10.110057	10.102484	10.212443	11
50	9.777731	9.903203	9.874747	10.125253	10.096797	10.222050	9	51	9.787883	9.897418	0.890465	10,109535	10.102 (82	10,212117	10
52 53	9.778119	9.903108	9.875010	10.124990	10.096892	10.221881	7	ς2 51	9.788045	9.897320	9.890725	10.109275	10.102680	10.211955	8
54	9.778455	9.902919	9.875536	10.124463	10.097081	10.222545	6	54	9.788370	9.897123	9.891247	10.108-53	10.102877	10.211630	6
55	9.778623	9.902824	9.875800 n.876063	10.124200	10.097176	10.221376	5	55	9.788531	9.897025	9.891507	10.108493	10.102975	10.211467	5
17	9.778960	9.902634	9.876326	10.123674	10.097366	10 22 1040	3	57	9.788856	9.806828	9.892028	10.107971	10.103172	10.211143	3
58	9.779128	9.902414	9 876589	10.123411	10.097556	10.220705	1	58	9.789018	9.8 66 28	9.892289	10.107711	10.103271	10.210083	2
66 —	9.779463	9.902349 Sine.	9.877134	10.122886	30.097652	Secant.	9	60	9.780342	9.89657	7.892810	10.10,190	10.101468	20.210658	0
1-		Sine.		Tang.		Secant.	173	-		Sine	-	Tang.		Secant.	М
-	100		53	Degrees		See 1	-				52	Degrees.			

			38 L	egrees.							39 1	Degrees.	4.7		
Min.	Sine		Tang.		Secant.		1	Min.	Sine		Tang.	1	Secants		
0	9.789342	9.896532	9.892810	10.107190	10.103468	10.210658	60 59	0	9.798872	9.890503	9.908369	10.091631	10.109497	10.201128	60
2	9.789665	9.896335	9.893331	10.106669	10.103665	10.210335	58	2	9.799184	9.890298	9.908886	10.091114	10.109702	10.2008:6	58
3	9.789827	9.896236	9.893491	10.106409	10.103764	10.210173	57 56	3	9.799339	9.890195	9.909144	10.090856	10.109805	10.200505	57
5	9-790149	9.896038	9.894111	10.105889	10.103962	10.209851	55	_ <u>_</u>	9.799651	9.889990	9.909660	10.090340	10.110010	10.200340	56
6	9.790310	9.895939	9.894371	10.105628	10.104061	10.209690	54	6	9.799806	9.889888	9.909918	10.090081	10.110112	10.200194	54
8	9.790471	9.895840	9.894632	10.105308	10.104100	10.209367	53 52	8	9.799962	9.889682	9.910177	10.089565	10.110215	10.200038	53
9	9-790793	9.895641	9.895152	10-104848	10.104359	10.209207	51	9	9.800272	9.889579	9.910693	10.089307	10.110421	10.199728	51
11	9.790954	9.895542	9.895412	10.104588	10.104458	10.209046	5° 49	II	9.800427	9.889476	9.910951	10.089049	10.110523	10.199573	.50
12	9-791275	9.895343	9.895932	10.104068	10.104656	10.208725	48	12	9.800737	9.889271	9.911467	10.088533	10.110729	10.199262	48
13	9.791436	9.895244	9.896192	10.103808	10.104756	10.208564	47 46	13	9.800892	9.889167	9.911724	10.088275	10-110832	10.198108	47 46
15	9.791757	9.895045	9.896712	10.103288	10.104955	10.208243	45	15	9.801201	9.888961	9.912240	10.087760	10.111039	10.198798	45
16	9.791917	9.894945	9.896971	10.103029	10.105055	10.208083	44	16	9.801356	9.888858	9.912498	10.087502	10.111142	10.198644	44
18	9-792237	9.894746	9.897491	10,102509	10.105254	10.207763	42	18	9.801665	9.888651	9.912/50	10.086986	10.111349	10.198335	43
19	9-792397	9.894646	9.897751	10.102249	10.105354	10.207603		19	9.801819	9.888548	9.913271	10.086729	10.111452	10.198181	41
20 21	9.792557	9.894546	9.898010	10.101990	10.105454	10.207443	39	20	9.801973	9.888444	9.913529	10.086471	10.111556	10.198026	40
22	9.792876	9.894346	9.898530	10.101470	10.105654	10.207124	38	22	9.802282	9.888237	9.914044	10.085956	10.111763	10.197718	39 38
23 24	9.793°35 9.793195	9.894246	9.898789	10.101211	10.105754	10.206964	37 36	23	9.802435	9.8888133	9.914302	10.085698	10.111866	10.197564	37 36
25	9.793354	9.894056	9.899308	10.100692	10.105954	10.206646	35	25	9.802743	9.887926	9.914817	10.085183	10.112074	10,197257	35
26	9.793513	9.893976	9.899568	10.100432	10.106054	10.206486	34	26	9.802897	9.887822	9.915075	10.084925	10.112178	10.197103	34
28	9.793673	9.893745	9.900086	10.099913	10.106255	10.206168	32	28	9.803050	9.887718	9.915332	10.084410	10.112286	10.196796	33
29	9.793991	9.893645	9.900346	10.099654	10.106355	10.206009		29	9.803357	9.887510	9.915847	10.084153	10.112490	10.196643	31
30	9-794150	9-893544	9.900605	10.099395	10.106456	10.205850		30	9.803510	9.887406	9.916104	10.083895	10.112594	10.196489	30
32	9.794467	9.893343	9.901124	10.098876	10.106657	10.205533	28	32	9.803817	9.887198	9.916619	10.083381	10.112802	10.196183	28
33 34	9.794626	9.893243	9.901383	10.098617	10.106757	10.205374	27	33	9.803970	9.887093	9.916876	10.083123	10.112907	10.196030	27
35	9.794942	9.893041	9.901901	10.098099	10.106959	10.205057	25	35	9.804276	9.886885	9-917391	10.082609	10.113115	10.195724	25
36	9.795101	9.892940	9 902160	10.097840	10.107060	10.204899	24	36	9.804428	9.886780	9.917648	10.082352	10.113220	10.195572	24
37	9.795417	9.892738	9.902679	10.097321	10.107160	10.204583	22	38	9.804734	9.886571	9.917903	10.081837	10.113324	10.195419	23
<u>39</u>	9-795575	9.892637	9.902938	10.097062	10.107362	10.204425		<u>39</u>	9.804886	9.886466	9.918420	10.081580	10-113534	10.195114	21
40 41	9.795733	9.892536	9.903197	10.096803	10.107463	10.204267		40 41	9.805038	9.886362	9.918677	10.081323	10.113638	10.194961	10
42	9.796049	9.892335	9.903714	10.096286	10.107666	10.203951	18	42	9.805343	9.886152	9.919191	10.080809	10,113848	10.194657	18
43 44	9.796206	9.892233	9.903973	10.096028	10.107767	10.203794	16	43 44	9.805495	9.886047	9.919448	10.080552	10.113954	10.194505	16
45	9.796521	9.892030	9.904491	10.095509	10.107970	10,203479	15	45	9.805799	9.885837	9.919962	10.080038	10.114163	10.194201	15
46	9.796679	9.891929	9.904750	10.095250	10,108071	10.203321	14	46	9.805951	9.885732	9.920219	10.079781	10-114268	10.194049	14
48	9.796993	9.891726	9.905267	10.094733	10.108274	10 203007	12	48	9.806254	9.885521	9.920733	10.079267	10.114478	10.193746	12
49	9-797150	9.891624	9.905526	10.094474	10.108376	10.202850	TO	49	9.806406	9.885416	9.920990	10.079010	10.114584	10.193594	買
50 51	9.797307	9.891523	9.905784	10.094215	10.108477	10.202692		50. 51	9.806557	9.885311	9.921247	10.078497	10.114089	10.193442	9
52	9.797621	9.891319	9.906302	10.093698	10.108681	10.202379	8	52	9.806860	9.885100	9.921760	10.078240	10.114900	10.193140	8
53	9.797777	9.891217	9.906560	10.093440	10.108885	10.202222	6	53 54	9.807011	9.884994	9.922274	10.077983	10.115005	10.192989	6
55	9.798091	9.891013	9.907077	10.092923	10,108987	10.201909	5	55	9.807314	9.884783	9.922530	10.077470	10.115217	10.192686	5
56	9.798247	9.890911	9.907336	10.092654	10.109089	10.201753	4	56	9.807465	9.884677	9.922787	10.077213	10.115322	10.192535	4
58	9.798560	9.890707	9.907852	,0.092147	10.109293	10.201440	2	58	9.807766	9.884466	9.923300	10.076700	10.115534	10.192234	2
59	9.7988719	9.890605	9.908369	10.091889	10,109395	10.201284	1 0	59 60	9.807917	9.884360	9.923557	10.076443	10.115640	10.192083	0
-	773-72	Sine	7.2-3.9	Tang		Secant.	M		3,00000/	Sine	73-3-13	Tang.	3,1	Secant.	$\overline{\mathbf{M}}$
1			50 1	Degrees.	11-11			-			50 -	Degrees.			-,

			40 L	legrees.			_	_			41 I	derre s.			- 1
Min.	Sine.		Tang.		Secant.			Min.	Sine		Tang.		Secant.		
0 1 2	9.808219	9.884148	9.924070	10. 61.15 10.075030 10. 75673	10.115 6	10. 91781	501	0 - 2	9.81-080	9.877780 9.8776°0 9.8776°0	99 410	10.06 9 2	10.12.1	10.1	,
3	9.808519	9.883936	9.924583	10. 75150	10.1 60 4	1 .191,81	5	th war	3 81-3 8	9.8**450	9 9 99 8	1 4600-1	1 .1225	10.1%2 11	1
6	9.808819	9 883727 9 883617 9 883610	9.925096	1 . "4904 10. 74648 10 C 4191	10.116183	10.191030	53	6	9.2 - 3	9. 7 2 30	9.94 1694	1 .0 95 1	10.112.8	10.1 23*1	C
8 9	9.809269	9.88329	9.924865	10.074135	10.1165.6	10.10 58	52	8	4.818163	9.8-6849	9.941204	10.058796	10.123 1	10.1817 3	3 2
10 11	9.809569 9.809718 9.809368	9.883101	9.9:63-8	10 073612	10.116809	10.1 -431	40 42	11	981 312	9 8 7 6 6 7 8 9 . 5 7 6 5 6 8 9 . 8 7 6 4 5 7	9.941713	10.053032 10.053032	10.123721	10.1 14 4	44
13	9.810017	9.882871	9.927147	10.072507	10.1:7119	10.18993	41	13 1	9.811 2,	9.876345	9.94223	10.0 7512	1 1.36:3	1 1 12 1	4
15 16	9.810465	9.882657 9.882550 9.882441	9.927659	10.012341	10, 17143	10.1.968,	44	11	9.819113	9.87 125	9.942988 9.943743 9.943498	10.056777	1-3 75 1-1-1-0 10.124 6	10.1 43	4 . 4
18 19		9.882336	9.928427	10.071573	10.117664	10.189c88	42		9 819 41	9.87579	9.943712	1 . 56248		10.1 41	
20	9.811210	9.882121 9.882014 9.881907	9.929196	10.071060	10.117879	10.188939	30	11	9 81 832 9.8196	9.8 5578 9.8754 9.8754	9.944 1	10.05,-19	1 -1 442	1 .1.000	7
23 34	9.811507	9.881799	9.929708	10.070292	10.118408	10.188493	37 36	23	9.82 2 3	9.87513-	9.94502	1 .074074	1-1-4-61	10.17 (3)	
25 16 27	9.811804 9.811952 9.812100	9.881584 9.881477 9.881369	9.930219	10.069780 10.069524	10,118416	10.18 196	34	26	9.8205 0	9.875014 9.8749 3 4.874791	9.945*90	10.0 411	1 125797	1	1
28 29	9.812248	9.881261	9.930987	10.069013	10.118-30	10.187752	31	18 29	9.830979	9.874568	0.946554	10.0537.0	10.12110	10 1 9 21	3.
30 31 32	9.812.41 9.812692 9.812840			10.068501	10.118954	10.187456 10.187308 10.187160	20 28	30 31 12	9.821265	9.874344	9.947063	10.053191	10.125656	10.1-8-3	2 95
33 34	9.811988	9.880721	9.932266	10.067734	10.119278	10.187612	20	33 34	9.821693	9.874120	9.947572	1 .057428	10 12 179	10.1 8165	2 6
35 36 37	9.813283	9.880307	9.932778 9.933933 9.933289	10.066967	10.119495	10.1 671	25	35 36 37	9.821977	9.873846	9.9480 1	10.051919	10.126216	10 1 77 18	2
38 39	9.813725	9.880180	9.933800	10.066200	10.119820	10.1 6275 10.186128	21	38 39	9.8.2404	9.8-3560	9.948844	10.051156	1 . 126.14n	10.1775 1	2 -
40 41 42	9.814019	9 879855		10.065944 10.065689 10.065433	10.120037	10.185687	19	41 41	9.822683	9 877213	9.949607	10.050647	10.126777	1 17-12	10
43 44	9.814460	9.879637	9.934822	10.065177	10.120461	10.185540	17	43	9.813114	9.872968	9.950370	10.049884	10,127001	10.1-6 6	116
45 46 47	9.814753 9.814900 9.815046	9.879311	9.935589	10,064156	10 120 180 1 120 680 10 120 748	10 1 5100	13	46 17	9.823397	9.8726 4	9.9508-9	10.0.886	1 121341	10.1-6161	114
48 49	9.815193	9.879093	9.936355	10.063000	10.121016	10 184661	11	100	9.823963	1 S72311		10.0 23 48	10.1 7566	10.1-6 37	11
50 51 52	9.815485	9.878766	9.936866	10.063134	10.121234	10.184212	8		9.824245	0.871081	0495340		10.117005	10 1- 5614	6
53 54	9.815923	9.878547	9.937632	10.062623	10.1214.1		6	53 54 55	9.824663	9.8 1751	1.95291	10.04794	10.17824		16
55 56 57	9.816215	9.878219	9.938142	10.061858	10.121781	10.1.3639	4 3	56 57	9.825 90	9.871528	9.953421	10.046 70	10.128472	10.17401	4 12
58 50 60	9.816652 9.816797 9.816543	9.877999	9.938908	10.061347	10.12.001	10.183348		50	9.82 (230		19.954195	10. 4581	16.32 817	10.17 7	3
1-	3.010543	Sine.		Tang.		Ser nt.	11	1		Sine.	1	Degrees.	1	1 Sc a 1.	
1_		-	40	Degrees				ji.	-		40	Aregrees.		-	

-			42	Degrees.			_	6		-		()			
	,		44	· cgrees.			_	-			43 -	Degrees.			
Min.	Sine.		Tang.		Secant.			Min.	Sine		Tang.		Secant.		
C 1	9.825511	9.871073	9-954437	10.045563	10.128926	10.174489		0	9.833783	9.854127	9.969656	10.030344	10.135872	10.166217	
2	9.823791	9.870846	9-954945	10.045054	10.129154	10.174209	58	2 3	9.834054	9.863892	9.970162	10.029838	10.136108	10.16:046	1 28
4	9.826071	9 870618	9.955453	10.044546	10.129382	10.173928		4	9.834325	9.863774	9.970416	10.029584	10.136226	10.165811	57
5	9 826211	9.870304	9-955707	10.04:292	10.129496	1173789		ş	9.834460	9.863538	9-970922	1 10.029078	10.13646:	10.16 5540	300
7	9.826:91	19.870276	9.955561	10.044038	10.129610	10.173649		7	9.834595	9.863419	9.971175	10.028825	10.136581	10.165405	54
8	9.826631	9.870161	9.956469	10.043531	10.129839	10.173370	52	8	9.834865	9.863183	9-971682	10.028318	10.136817	10.165135	52
10	9.826910	0.86:933	9 956977	10.043023	10.130067	10.173090	51	9	9.835134	9.862946	9.971935	10.028065	10-136936	10.165001	51
11	9.827049	9.869318	9.957231	10.042760	10.130182	10.172951	49	11	9.835269	9.862827	9.972441	10.027550	10.137173	10.164866	150
13	9.827318	19.869589	9-95748	10.042515	10.130296	10.172811	48	12	9.835403	9.862709	9.972694	10.027305	10.137291	10.164597	48
14	9.827467	9 869474	9 957993	10.042007	10.130526	10.172533	46	14	9.835672	9.862471	9.973201	10.026799	10.137529	10.164328	47 46
16	9.827745	9 869245	9.95850	10.041753	10.130640	10.172394	45	15	9.8358:7	9.862353	9.973454	10.026546	10.137647	10,164193	4.5
17	9 827884	0.860130	9.958751	10.041245	10.130870	10,172116	43	17	9.836075	9.862115	9.973960	10.026040	10.137766	10.164059	44
10	9.828162		9.959008	10.040992	10.130985	10.171977	42 41	18	9.836209.	9.861996	9.974213	10.025787	10.138004	10.163791	42
20	9.82.301	9.863785	9.959515	10.040484	10 131215	10.171699		20	9.836477	9.861758	9-974719	10,025280	10.138242	10.163657	
22	9.828439	9.863670	9.959770	10.040231	10.131330	10.171561	39	21	9.836611	9.861638	9-974973	10.025027	10.138362	10. 162280	120
23	9.828716	9.868324	9.960277	10.039723	10.131560	10.171284	37	23	9.836878	9.861400	9.975226	10.024774	10.138481	10.163255	38
24	9. 28003	9.868200	9.960530	10.039470	10.131676	10.171145	36	34	9.837012	9.861280	9.975732	10.024268	10.138720	10,162988	37 36
26	9.829171	9.863093	0.061038	10.038962	10.131791	10.171007	35	25 25	9.837146	9.861161	9.975985	10.024015	10.138839	10.162854	
27	9.829269	9.867978	9.961291	10.038708	10.132022	10.170731	33	27	9.837412	9.860921	9.976491	10.023509	10.139078	10.162 687	34
29	9.829545	9.357747	9.961799	10.038201	10.132138	10.170592	32 31	29	9.837546	9.860802	9-976997	10.023256	10.139198	10.162454	32
30	0.829683	9.857533	9.962052	10.037947	10.132369	10.170317	30	30	9.837812	9.860562	9.977250	10.022750	10.139438	10,162188	31
31	9.829950	9.867399	9 952306	10.037694	10.132485	10.170179	28	31	9.837945	9.860442	9.977503	10.022497	10.139558	10.162055	20
33 34	9.83:097	9.867283	9 962813	10.037187	10.132717	10.169903	27 26	33	9.838211	9.860202	9.978009	10.021991	10.139798	10.161922	28
35	9.830372	9.867051	0.062220	10.036680	10.132833	10.160628	25	34	9.838344	9.86co82	9.978262	10.021738	10.139918	10.161656	26
36	9.830509	0.866035	0.062524	10.036426	10.133065	10.160401	24	36	9.838607	9.859962	9.978515	10.021485	10.140038	10.161323	25
37 38	9.830784	9.866703	9.963827	10.036172	10.133181	10.169354	23	37 38	9.838742	9.859721	9.979021	10.020979	10.140279	10.161248	23
39	9.830921	9.866587	9.964335	10.035665	10.133414	10.169079	21	39	9.839007	9.855480	9.979274	10.020/20	10.140399	10.161125	22
40	9.831058	9.866470	9.964588	10.035412	10.133530	10.168942	20	40	9.839140	9.859360	9.979780	10.020220	10,140640	10.160860	20
42	0.831333	9.866237	9.965095	10.034005	10.133763	10.168668		41	9.839272	9.859239	9.980033	10.019967	10.140761	10.160728	19
43 44	9 831460	9.866004	9.965349	10.034651	10.133880	10.16853	17	43	9.839536	9.858998	9.980538	10.019461	10-141002	10.160464	17
45	9 831742	9.865887	9.965855	10.034144	10.134113	10.168257	15	45	9.839800	9.858756	9.981044	10.018956	10.141123	10.160332	16
46 47	9 831879	9.865770	9.966109	10.033891	10,134230	10.168121	14	46	9.839932	9.858635	9.981297	10.018703	10.141365	10.160068	15
48	9.832152	0 865536	9.966616	10.033384	10,134347	10 167848	13	47 48	9.840064	9.858514	9.981550	10.018450	10.14.486	10.159936	13 12
49 50	9.832288	9.865419	9.966869	10.033131	10.134581	10.167712	11	49	9.840328	9.858272	9.982056	10.017914	10.141728	10.159672	11
51	9 832761	9.865185	9.96712:	10.032877	10.134698	10.167575	10	50	9.840460	9.858150	9.982309	10.017691	10.141849	10.159541	10
53	9.832697	9.865068	9.967630	10.032371	10.134932	10.16730:	8	52	9.840722	9.857908	9.982814	10.017185	10.141971	10.159409	8
54	9.832970	9.864833	9.968136	10.032118	10.135050	10.167167	7	53	9.840854	9.857786	9.983067	10.016933	10.142214	10.159146	7
55 56	9.833105	9.864716	9.968389	10,031611	10.135284	10.16680	-5	55	9.841116	9.857543	9.983573	10.016427	10.142457	10.1 (8884	5
57	0.833377	9.864508	9.968843	10.031357	10,135402	10.166622	4	56	9.841247	9.857421	9.983826	10.016174	10.142579	10.158753	4
581	9.8435121	9.864363	9.969150	10.030851	10.135637	10.166488	2	58	9.841509	9.857178	9.984331	10.015668	10.142700	10.148621	3 2
60	9.833783	9.864127	9.969656	10.030597	10.135755	10.16635	0		9.841640	9.857056	9.984884	10.015416	10.142944	10.158360	1
		Sine		Tang.		Secant.	M	=)	2.24.771	Sine.	5.704037	Tang.	10,143000		o M
			47 L	egrees.	100		- 0				46 D	egrees		-	-

_			44 1.	113168.			
Min.	Sine		Tang.		Secant.		
0	9. 41771	9 8 6 14	9.98483	1 .01.10.	10.143066	10.15 229	59
1 2	9.841902	9.8 56612	9.18 3 3	10.0146 7	10.143310	10.155698	58
3	9.842103	6.8 6:68	1.9850	10 0144 4	10.143432	10.157837	57
4	9.8 194	91 145	9- 3-48	1-014151	10.14 554	J 1577	55
6	84 414	0 8 50201	9.0 01	10.013 39	10.1436 7	10-15 16 10-157 45	54
7 8	842515	9.856 78	19.94 507	1 .01; 93	0.1-3 22	10.15 3 3	53
	0.8429 6	9.855833	9.98 360	10.0131	10.144644	10.157 85	32 38
10	9.843076	9.855711	9 98736	10.012635	10.144280	10.156924	50
11	9.841206	9 855588	0.48 13	10.012382	10.1 4412	10 156794	4.9
12	0 8433 6	9.855465	9. 8 1-1	10.01212	10.14463	10.156664	43
13	9.84346,	9.855219	9. 883	10 -11624	1 1447 1	1 .15640;	46
35	0.8437 5	9.855096	,.988 29	10 0113,1	10.144904	10.1,6275	45
16	9.843855	9 8 4973	9.988882	10.010 66	10.145027	10.156145	44
18	9.844114	9.854850	9 989187	10.010 00	10.145150	10.156010	42
19	9.844243	9.854603	9 989640	10.113	10 145397	10 155757	41
20	9.844372	9.854480	9.989893	10. 101 7	.0.145520	10.155627	40
21	9.8445.2	9.854356	9.990145	10.009815	10.145644	10.155,98	39
23	0.814260	9.854109	9.990651	10 00 349	10.14;801	10.155240	37
24	9.844589	9.853986	8.9900 3	1 .009016	10.146014	10 155111	36
25	9.845018	9.853862	9-0914 9	10.008.44	10.146138	10.154 82	3.5 3.4
27	9.845270	0.855738	9.691662	10.008338	10.146386	10.154724	33
2\$	6.845404	9.853440	9.991914	10.0:8086	10.14651	0.154595	32
29	9.845533	9.853242	9-902420	10.00 7550	10.146634	10.154338	31
30	0.845002	0.853118	9.091672	10.00 7538	10.146882	10.154338	29
32	9.845910	0.842994	9.992925	10.007075	10.147006	10-154081	28
33	9.846174	9.852869	9-993430	10 006822 10 006569	10-14-131	10.153952	26
	9.84 3 4	9.852620	9.093683	10.006317	10.147380	10.1 3696	25
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3"	9.846:60	3.852247	9-954441	10.005559	10.1 7629	10.153440	23
39	9.846816	9.852122	9.994694	10.005306	10.147753	10.143184	2 1
4	9.846944	9.851097	9-9-4947	10.0 5053	10.1480 3	10.1 3056	20
41	9.847074	9.851872	9-995199	10.004548	10.148128	10.152229	13
43	9.84-327	9.8 : 1622	9.995705	10.001295	10.148378	10.15:673	17
44	9.847454	9.851497	9.99595	10.00404;	10 148503	10.1(2(46	16
45	9.847582	9.851372	9.996210	10.003790	10.148628	10.152418	14
47	9.847836	9.851121	9.996715	10.003285	10.148879	10.152163	13
48	1.847964	9.840996	9.996968	10.003032	10.149004	10.152036	12
50	9.848091	9.850870	9.997473	10.002 (27	10.14913	10.1 1 0	11
51	9.848345	9.850619	9.997726		10.149381	10.1 1655	
52	9.848472	9.850493	9-997979	10.002274	10.149507	10.15152	3
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