

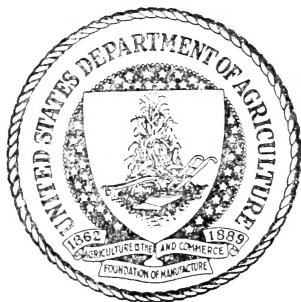


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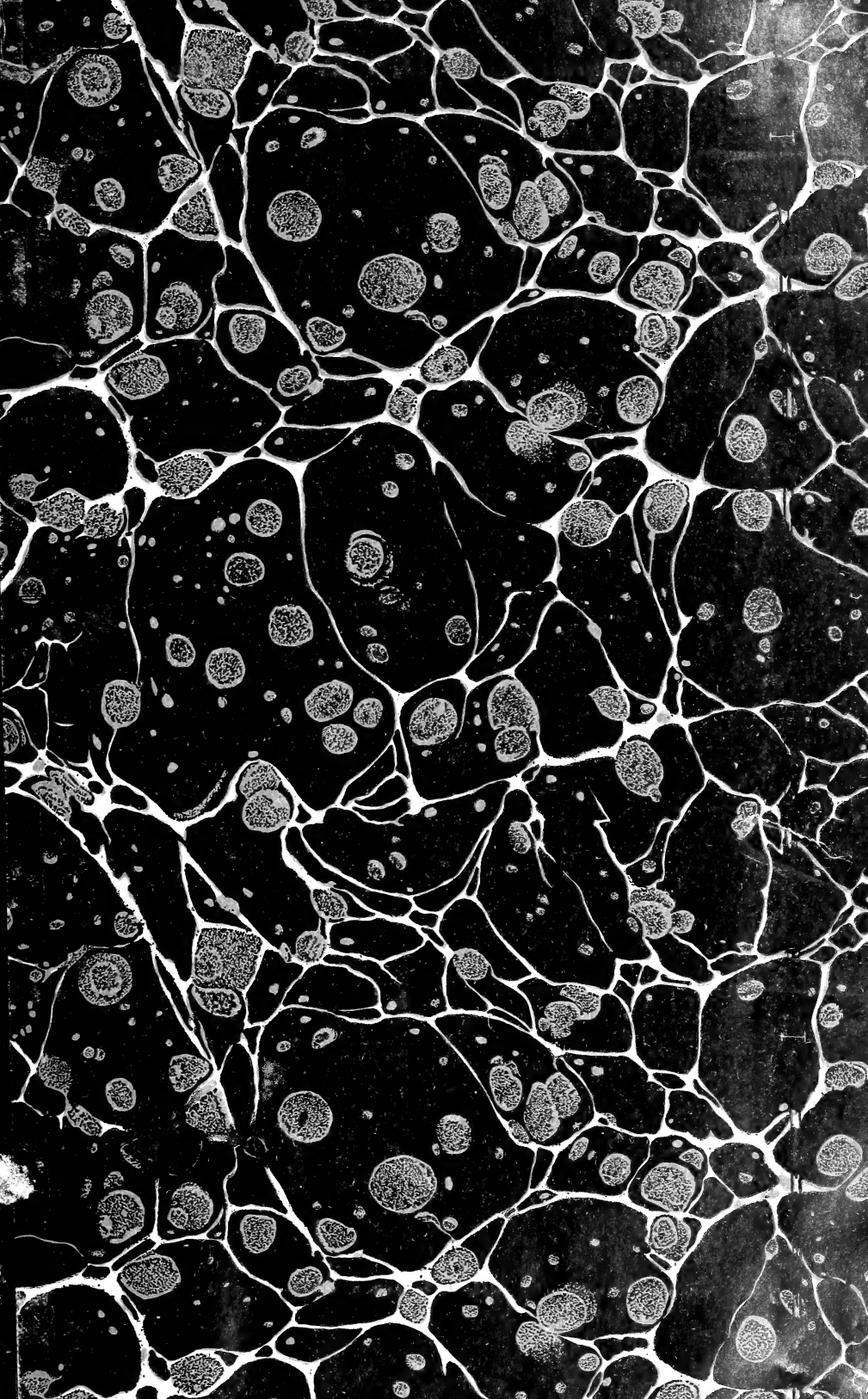
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UNITED STATES DEPARTMENT OF AGRICULTURE

BULLETIN No. 676

Contribution from the Forest Service
HENRY S. GRAVES, Forester

FOREST PRODUCTS LABORATORY, Madison, Wisconsin
In Cooperation with the University of Wisconsin

Washington, D. C.

PROFESSIONAL PAPER

July 16, 1919

THE RELATION OF THE SHRINKAGE
AND STRENGTH PROPERTIES OF
WOOD TO ITS SPECIFIC GRAVITY

By

J. A. NEWLIN, in Charge, Section of Timber
Mechanics, and T. R. C. WILSON, Engineer in
Forest Products

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Species-Locality Averages	6
Determination of Specific Gravity	6
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PURPOSE.

It has long been recognized that there are direct relations between the specific gravity, or density, of a wood and its strength properties.¹ By the analysis of over 200,000 tests, the Forest Products Laboratory, conducted in cooperation with the University of Wisconsin, Madison, Wis., has now definitely established these relations. It is the purpose of this bulletin to state these relations and to put the expression of them in such form as to render them easily useful (1) for estimating the properties of any particular timber; (2) for selecting timber for any given purpose; (3) for comparing the various species; and (4) for determining in what way the species are exceptional and to what uses they are best adapted.

It has usually been assumed that the strength of wood varies directly with the first power of its density; i.e., that the respective strengths of two sticks would differ in the same proportion as the densities. It was recognized that fiber stress at elastic limit in compression perpendicular to the grain, or bearing strength on side

¹ Accurate determinations made at the Forest Products Laboratory on seven species of wood, including both hardwood and coniferous species, showed a range of only about 4½ per cent in the density of the wood substance, or material of which the cell walls are composed. Since the density of wood substance is so nearly constant, it may be said that the density or specific gravity of a given piece of wood is a measure of the amount of wood substance contained in it.

surface, and work values in static bending or toughness, deviate very erratically from this relation; but the relation was supposed to hold especially true in the case of such properties as modulus of rupture, or maximum bending strength, and strength in compression parallel

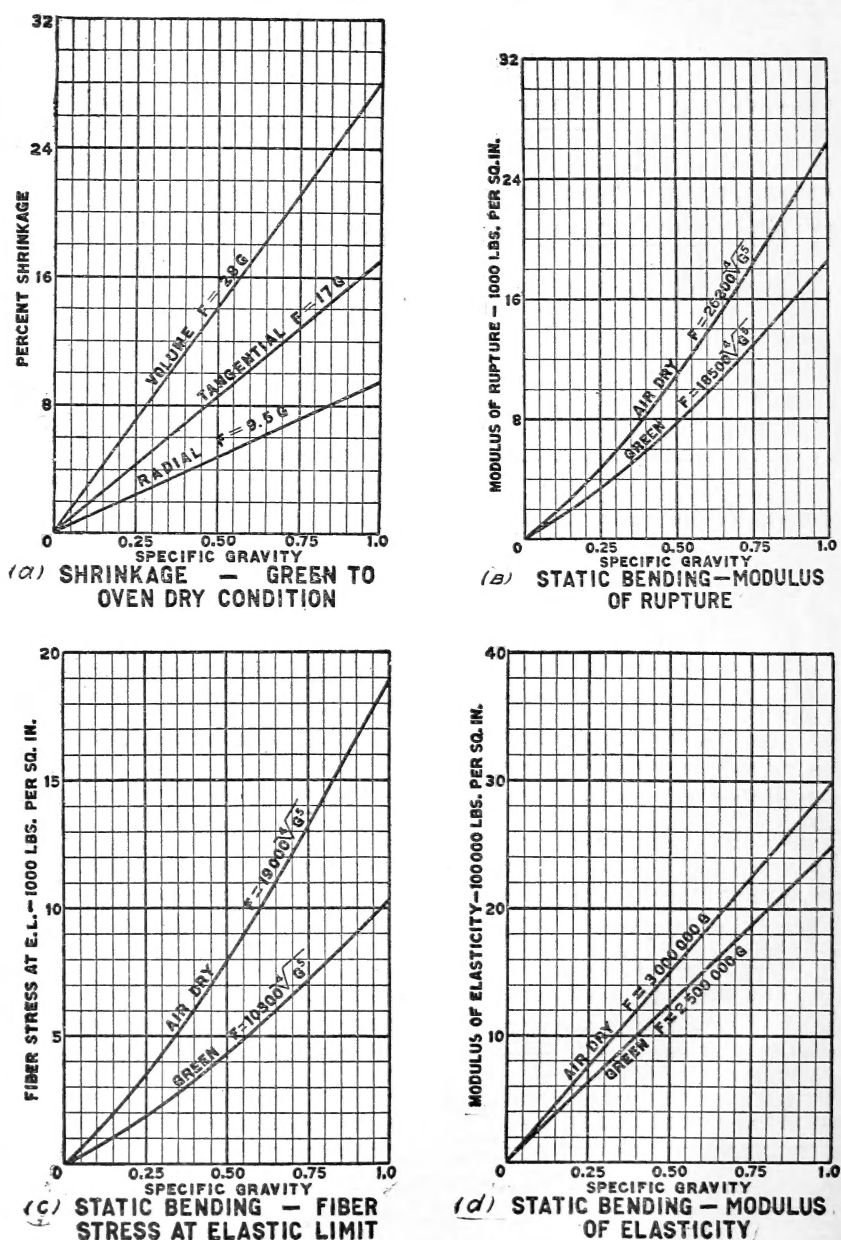


FIG. 1.

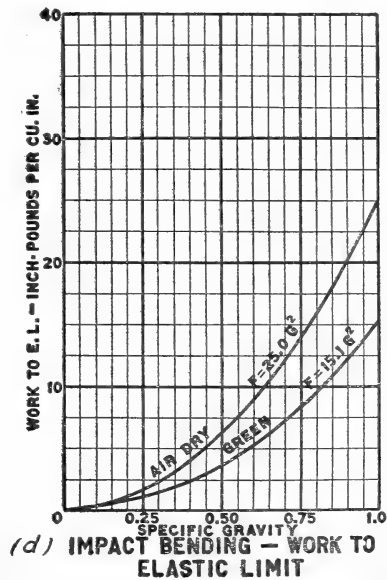
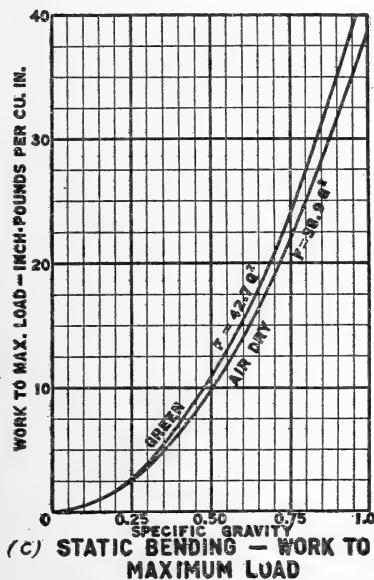
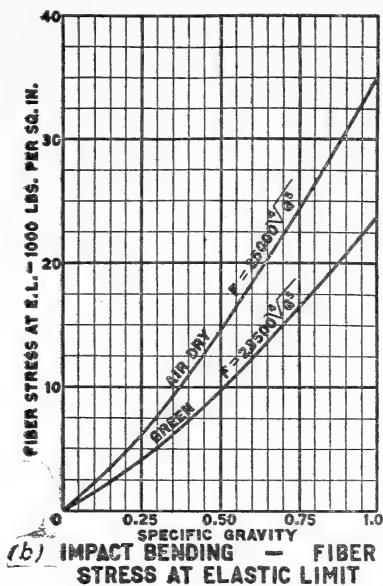
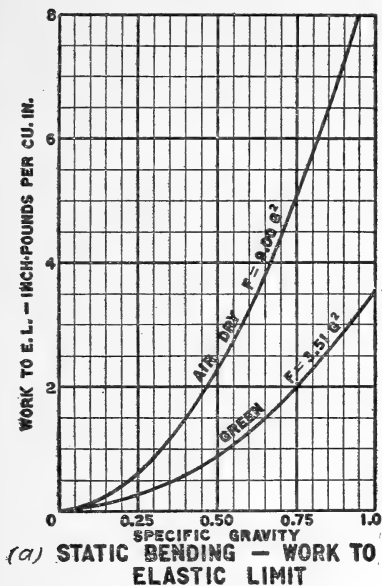
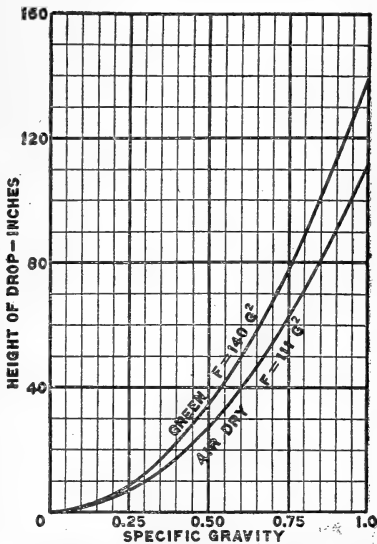


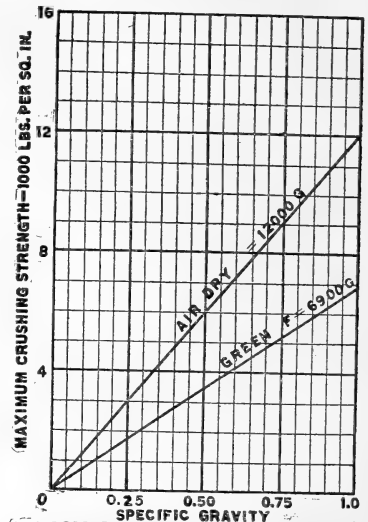
FIG. 2.

to the grain, or strength as a column. It has also been supposed that the relation applied between pieces of the same species, between pieces of different species, and between average results of strength tests on different species. A study of the data at present available, which are derived from a much larger number of tests and which cover a greater

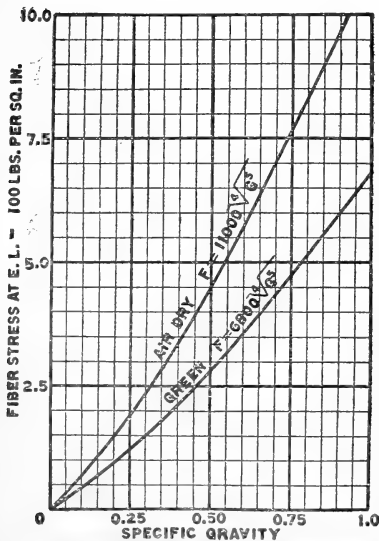
range in specific gravity and strength values than was true of the data available heretofore, made it evident that these assumptions were inaccurate and that there was a better and more correct method expressing the actual relations between specific gravity and strength.



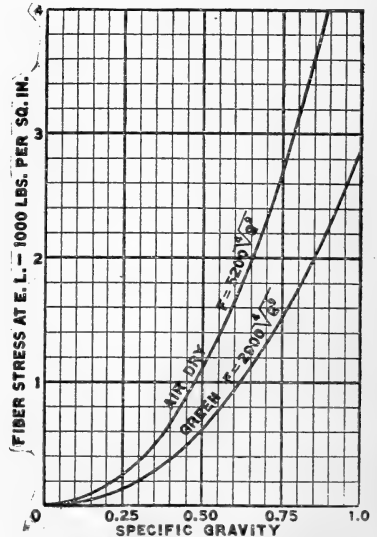
(a) IMPACT BENDING — HEIGHT OF DROP CAUSING COMPLETE FAILURE



(b) COMPRESSION II TO GRAIN
MAXIMUM CRUSHING STRENGTH

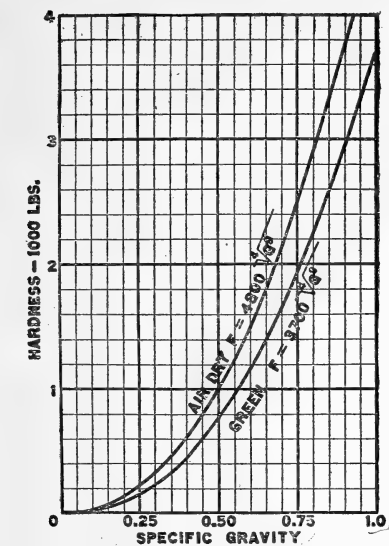


(c) COMPRESSION II TO GRAIN
FIBER STRESS AT ELASTIC LIMIT

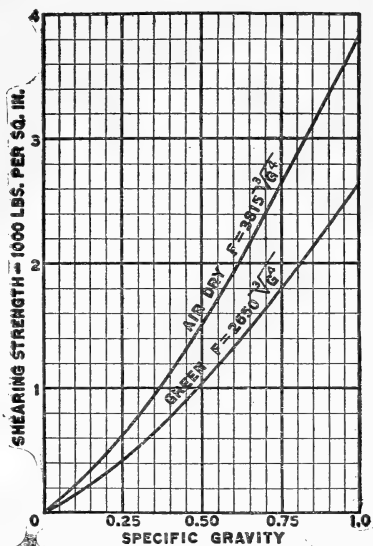


(d) COMPRESSION I TO GRAIN
FIBER STRESS AT ELASTIC LIMIT

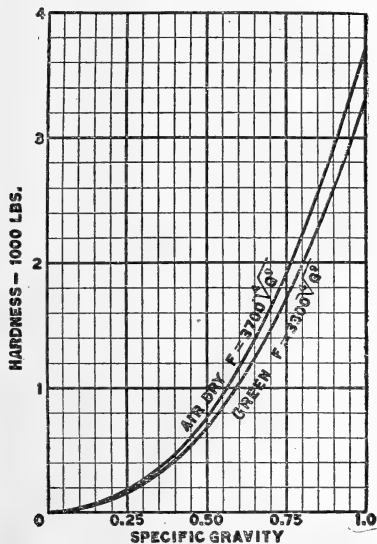
FIG. 3.



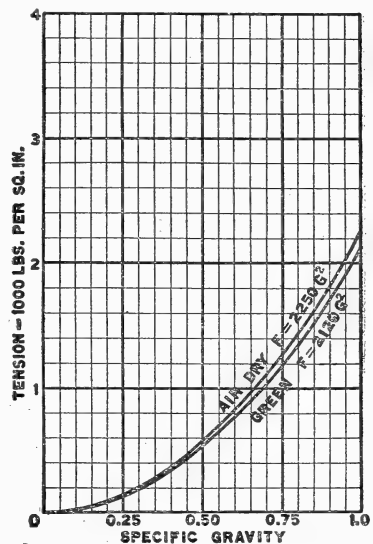
(a) HARDNESS - END SURFACE



(b) SHEARING STRENGTH || TO GRAIN



(c) HARDNESS - SIDE SURFACE



(d) TENSION I TO GRAIN

FIG. 4.

In order that the relation between specific gravity and each of the various mechanical properties of wood may be easily put to practical use, the relation, both for green and for air-dry material, is given in the form of an equation (Table 1) and, in addition, in the form of a curve (figs. 1 to 4).

SPECIES-LOCALITY AVERAGES.

The specific-gravity relations given in this bulletin are derived from a study of what may be called "species-locality" averages; that is, each average represents tests of material of one species from one locality.

There are two principal reasons for using "species-locality" averages in preference to the results of individual tests. First, the number of individual tests is quite large, amounting in some instances to as many as 900 from a single "species-locality", so that an immense amount of work is saved by the use of the "species-locality" averages; second, if individual tests were used, the "species-localities" having larger trees or a larger number of trees would include a larger number of tests and would have undue weight in determining the relations.

The method of analysis used is applicable also to individual tests from a single species to determine the specific gravity relations within that species. It has been applied to a few of the properties of some of the more important species which are used for structural timbers where there was a rather large number of test pieces and a considerable range in specific gravity.

DETERMINATION OF SPECIFIC GRAVITY.

Specific gravity of wood, as used herein, is based on the volume of the specimens when tested (green or air-dry) and their weight when in an oven-dry condition; that is, it is the ratio of the weight of the specimen of wood, *oven-dry*, to the weight of a volume of water equal to the *volume of the specimen at the time of test*. Because of the shrinkage which takes place in wood when it is dried, this figure is not the true specific gravity of a piece of oven-dry wood. The method, however, is easily applied to each specimen tested, and is the standard method of the Forest Service for the determination of a specific-gravity figure for use in studying the properties of wood.

MOISTURE CONTENT OF TEST SPECIMENS.

Both green and air-dry specimens were used in the tests, and the relations between specific gravity and strength were determined separately for green and air-dry wood. Variations in the moisture content of wood have no effect on its mechanical properties so long as the wood is thoroughly green; they have considerable influence on these properties, however, as soon as the wood becomes air-dry, or partially air-dry. Accurate comparisons can not be made between the properties of two lots of air-dry specimens unless they were tested at the same moisture content or adjustments made in the strength figures for difference in moisture content.

The moisture content of the air-dry material at the time of test varied from 8 to 18 per cent. Modulus of rupture and maximum strength in compression parallel to the grain were adjusted to a moisture content of 12 per cent before determinations of the relation of these properties to the specific gravity was made. This adjustment was possible because the laws governing the variation of these properties with varying moisture content are fairly well established. However, in the case of the other strength functions their variation with varying moisture content has not been studied in detail and no such adjustment is possible with any very great degree of accuracy. Consequently, the actual moisture content values as obtained from tests have been used in the determination of the relation of these properties to specific gravity.

THE EQUATIONS.

Table 1 and figures 1 to 4 give equations which represent the average relations between specific gravity and each of the mechanical properties. All the "species-locality" averages available on any particular property were considered in deriving the equations for that property. The number of "species-locality" averages from which an equation is derived varies from 84 to 178. This variation is due to the fact that several of the tests were not used in some of the earlier testing work and to the fact that tests have not yet been completed on air-dry material for all of the "species-localities" listed.

Table 1 gives first the equations for shrinkage and for each of the strength properties of green and air-dry wood in terms of the specific gravity. These equations, as explained in the appendix, are reduced to a simple form; and the powers of gravity used are such that the equations may be solved by arithmetical operations and without the use of higher mathematics. However, to simplify even further the use of the equations, figures 1 to 4 have been prepared for their solution. Each of the curves shown in these diagrams represents the equation connecting specific gravity and one of the properties of wood. The curves representing the equations for radial, tangential, and volumetric shrinkage appear in figure 1(a). In each of the other figures, 1(b) to 4(d), appear two curves for some one mechanical property. One of these curves is for green and the other for air-dry material. If the specific gravity is known, the equation value for any one or all of the properties of the wood in question may be readily determined from the curves without computation.

The second portion of Table 1 gives what may be termed a measure of the accuracy of the respective equations. It is not to be expected that all the "species-locality" averages will satisfy the equation exactly or even very closely. Some of the properties are more erratic than others, so that one "species-locality" may far exceed

the equation values and another "species-locality" fall far below them.

In figure 5 are plotted the curves of the equation for modulus of rupture in static bending in green material, $M=18500 \sqrt[4]{g^5}$, and of the equation for the same property in air-dry material, $M=26200 \sqrt[4]{g^5}$. In order to give a graphical idea as to the reliability of these equations, the specific gravity and the modulus of rupture of each "species-locality" have been plotted as a point. The reference number placed near each plotted point is assigned to the "species-locality" in the order of its respective specific gravity as determined from compression parallel to grain specimens of green wood. In figures 6, 7, and 8 the data are given for the curves on shrinkage in volume from green to oven-dry condition, maximum crushing strength in compression parallel to grain, and fiber strength at elastic limit in compression perpendicular to grain.

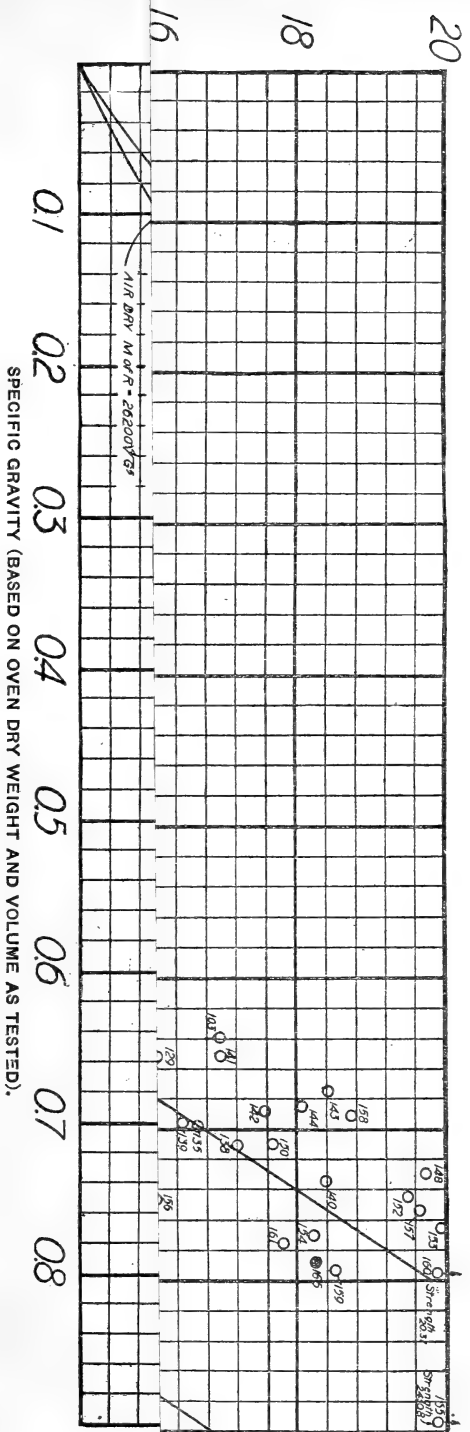
Under each property is listed in this second portion of Table 1, for both green and air-dry conditions, those percentages of the equation value above which were one-tenth of the "species-localities." Similarly, there are listed those percentages above which were one-fourth of the "species-localities," those below which were one-fourth, and those below which were one-tenth. For instance, in static bending (green), one-tenth of the "species-localities" tested had a modulus of rupture of more than 114 per cent of what the specific gravity equation indicated they should have had; one-fourth of them had a modulus of rupture greater than 108 per cent of the equation value; one-fourth of them less than 91 per cent of the equation value; and the lowest one-tenth had a modulus of rupture less than 84 per cent of what the equation indicated they should have had. It follows from these figures that one-half of the "species-localities" had a modulus of rupture of between 91 per cent and 108 per cent of the value given by the equation, and that the other one-half were evenly divided between those that were more than 108 per cent and those that were less than 91 per cent.

The third portion of Table 1 gives the actual value of each property for each "species-locality" as determined by the tests, expressed as a percentage of the value computed from the specific gravity by the use of the equation at the head of the column. For instance, it is found from the table that air-dry Biltmore ash has a modulus of rupture 98 per cent as great as that of the average wood of its specific gravity, the modulus of rupture of the average wood of this specific gravity being the figure given by the equation. These percentages are given for both green and air-dry wood.

Big sheoak.....	Mississippi.....	135	Sumac, staghorn.....	Wisconsin.....	61
Do.....	Ohio.....	154	Sycamore.....	Indiana.....	63
Bitternut.....	do.....	139	Do.....	Tennessee.....	65
Mockernut.....	Mississippi.....	144	Umbrella, Fraser.....	do.....	45
Do.....	Pennsylvania.....	159	Willow:		
Do.....	West Virginia.....	155	Black.....	Wisconsin.....	11
Nutmeg.....	Mississippi.....	112	Western black.....	Oregon.....	43a
Pignut.....	do.....	148	Witch hazel.....	Tennessee.....	114
Do.....	Ohio.....	157			
Do.....	Pennsylvania.....	160			
Do.....	West Virginia.....	161			

CONIFERS.

Cedar:			Pine—Continued.		
Incense.....	California.....	26	Lodgepole.....	Montana, Granite County.....	41a
Western red.....	Montana.....	2	Do.....	Montana, Jefferson County.....	40a
Do.....	Washington.....	10	Do.....	Wyoming.....	34
White.....	Wisconsin.....	1	Longleaf.....	Florida.....	123
Cypress, bald.....	Louisiana.....	62	Do.....	Louisiana, Lake Charles.....	113
Douglas fir.....	California.....	45a	Do.....	Louisiana, Tangipa- hoia Parish.....	96
Do.....	Oregon.....	67a	Do.....	Mississippi.....	95
Do.....	Washington, Che- halis County.....	46a	Norway.....	Wisconsin.....	57
Do.....	Washington, Lewis County.....	75	Pitch.....	Tennessee.....	71
Do.....	Washington and Oregon.....	67	Pond.....	Florida.....	86
Do.....	Wyoming.....	48	Shortleaf.....	Arkansas.....	77
Fir:			Sugar.....	California.....	22
Alpine.....	Colorado.....	4	Table Mountain.....	Tennessee.....	82
Amabilis.....	Oregon.....	39	Western white.....	Montana.....	42
Do.....	Washington.....	18	Western yellow.....	Arizona.....	19
Balsam.....	Wisconsin.....	14	Western.....	California.....	37
Grand.....	Montana.....	36	Do.....	Colorado.....	41
Noble.....	Oregon.....	16	Do.....	Montana.....	32
White.....	California.....	17	White.....	Wisconsin.....	25
Hemlock:			Redwood.....	California, Albion.....	28
Black.....	Montana.....	47	Do.....	California, Korb.....	13
Eastern.....	Tennessee.....	52	Spruce:		
Do.....	Wisconsin.....	15	Engelmann.....	Colorado, Grand County.....	8
Western.....	Washington.....	50	Do.....	Colorado, San Miguel County.....	3
Larch, western.....	Montana.....	84	Red.....	New Hampshire.....	44
Do.....	Washington.....	64	Do.....	Tennessee.....	29
Pine:			White.....	New Hampshire.....	7
Cuban.....	Florida.....	127	Do.....	Wisconsin.....	38
Jack.....	Wisconsin.....	43	Tamarack.....	do.....	81
Jeffrey.....	California.....	33	Yew, western.....	Washington.....	134
Loblolly.....	Florida.....	88			
Lodgepole.....	Colorado.....	31			
Do.....	Montana, Gallatin County.....	35a			



LIST OF SPECIES AND REFERENCE NUMBERS FOR FIGURES 5 TO 9.

HARDWOODS.

Species.	Locality.	Reference No.	Species.	Locality.	Reference No.
Alder, red	Washington	30	Hickory—Continued.		
Ash:			Shagbark	Mississippi	140
Biltmore	Tennessee	91	Do	Ohio	152
Black	Michigan	60	Do	Pennsylvania	143
Do	Wisconsin	70	Do	West Virginia	153
Blue	Kentucky	90	Water	Mississippi	141
Green	Louisiana	93	Holly, American	Tennessee	87
Do	Missouri	100	Hornbeam	do	149
Pumpkin	do	79	Laurel, mountain	do	145
White	Arkansas	106	Locust:		
Do	New York	128	Black	do	158
Do	West Virginia	83	Honey	Indiana	162
Aspen	Wisconsin	23	Madrona	California	101
Largetooth	do	20	Do	Oregon	125a
Basswood	Pennsylvania	12	Magnolia	Louisiana	66
Do	Wisconsin	5	Maple:		
Beech	Indiana	110	Oregon	Washington	58
Do	Pennsylvania	98	Red	Pennsylvania	69
Birch:			Do	Wisconsin	92
Paper	Wisconsin	73	Silver	do	56
Sweet	Pennsylvania	129	Sugar	Indiana	104
Do	do	107	Do	Pennsylvania	108
Yellow	Wisconsin	103	Do	Wisconsin	124
Do	Tennessee	9	Oak:		
Buckeye, yellow	Oregon	81a	Bur	do	125
Buckthorn, cascara	Tennessee	27	California black	California	80
Butternut	Wisconsin	21	Canyon live	do	163
Do	do	46b	Chestnut	Tennessee	121
Chinquapin, western	Oregon	46b	Cow	Louisiana	133
Cherry:			Laurel	do	116
Black	Pennsylvania	72	Post	Arkansas	130
Wild red	Tennessee	24	Do	Louisiana	137
Chestnut	Maryland	46	Red	Arkansas	119
Do	Tennessee	40	Do	Indiana	118
Cottonwood, black	Washington	6	Do	Louisiana	117
Cucumber tree	Tennessee	59	Do	Tennessee	97
Dogwood:			Highland Spanish	Louisiana	94
Flowering	do	151	ish		
Western	Oregon	125a	Lowland Spanish	do	142
Elder, pale	do	69a	Swamp white	Indiana	150
Elm:			Tanbark	California	115
Cork	Wisconsin, Marathon County	126	Water	Louisiana	111
Do	Wisconsin, Rusk County	120	White	Arkansas	132
Slippery	Indiana	102	Do	Indiana	138
Do	Wisconsin	74	Do	Louisiana, Richland Parish	136
White	Pennsylvania	55	Do	Louisiana, Winn Parish	131
Do	Wisconsin	53	Willow	Louisiana	109
Greenheart		165	Yellow	Arkansas	122
Gum:			Do	Wisconsin	105
Black	Tennessee	68	Osage orange	Indiana	184
Blue (Eucalyptus)	California	147	Poplar, yellow (tulip tree)	Tennessee	35
Cotton	Louisiana	76	Rhododendron, great	do	85
Red	Missouri	54	Sassafras	do	51
Hackberry	Indiana	90	Serviceberry	do	156
Do	Wisconsin	78	Silverbell tree	do	49
Haw, pear	do	146	Sourwood	do	89
Hickory:			Sumac, staghorn	Wisconsin	61
Big shellbark	Mississippi	135	Sycamore	Indiana	63
Do	Ohio	154	Do	Tennessee	65
Bitternut	do	139	Umbrella, Fraser	do	45
Mockernut	Mississippi	144	Willow:		
Do	Pennsylvania	159	Black	Wisconsin	11
Do	West Virginia	155	Western black	Oregon	43a
Nutmeg	Mississippi	112	Witch hazel	Tennessee	114
Pignu	do	148			
Do	Ohio	157			
Do	Pennsylvania	160			
Do	West Virginia	161			

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Cedar:			Pine—Continued.		
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Douglas fir	California	45a	Do	Louisiana, Tangipahoa Parish	96
Do	Oregon	67a	Do	Mississippi	95
Do	Washington, Chehalis County	46a	Norway	Wisconsin	57
Do	Washington, Lewis County	75	Pitch	Tennessee	71
Do	Washington and Oregon	67	Pond	Florida	80
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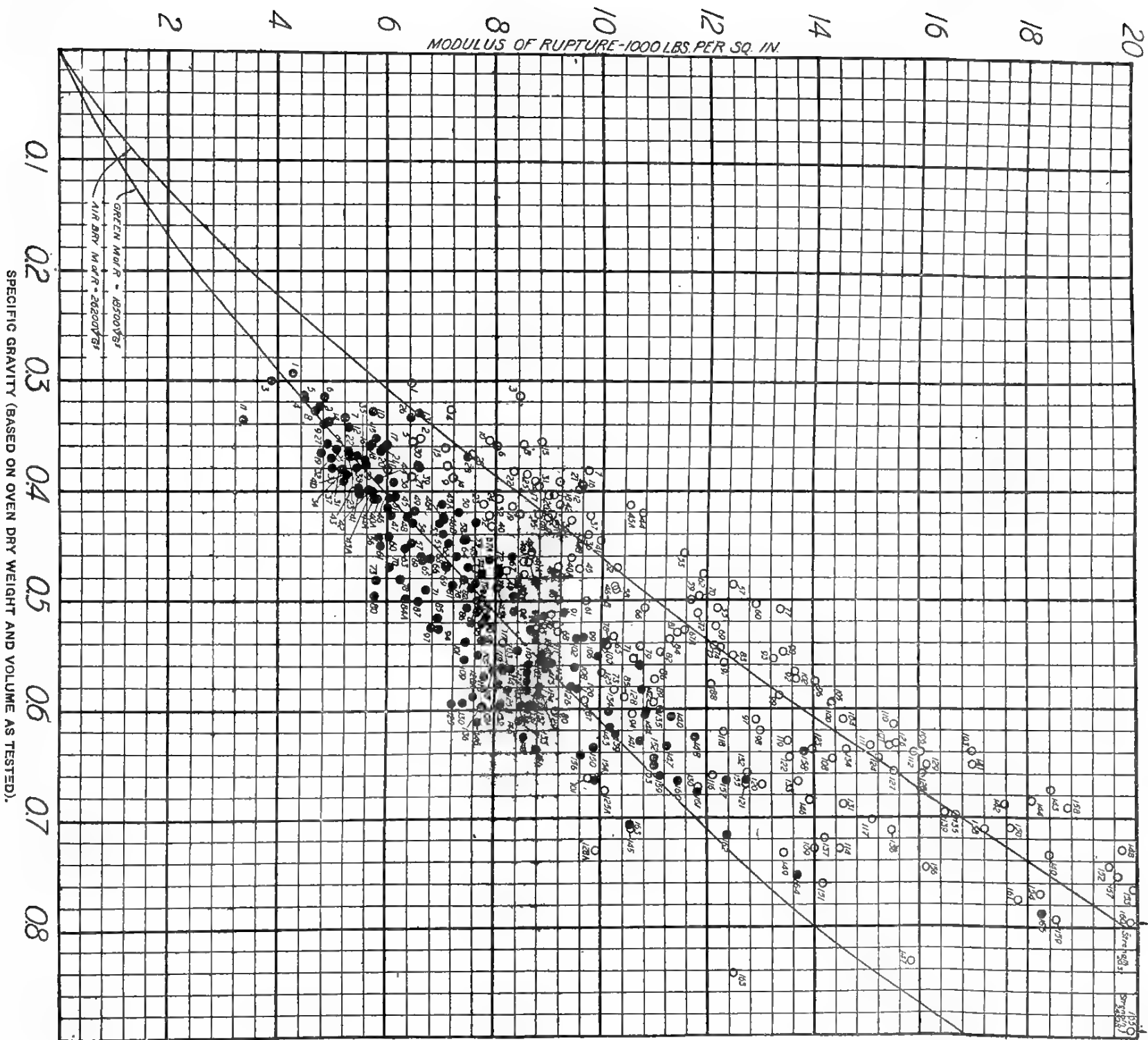


Fig. 5.—Relation of modulus of rupture in static bending to specific gravity.

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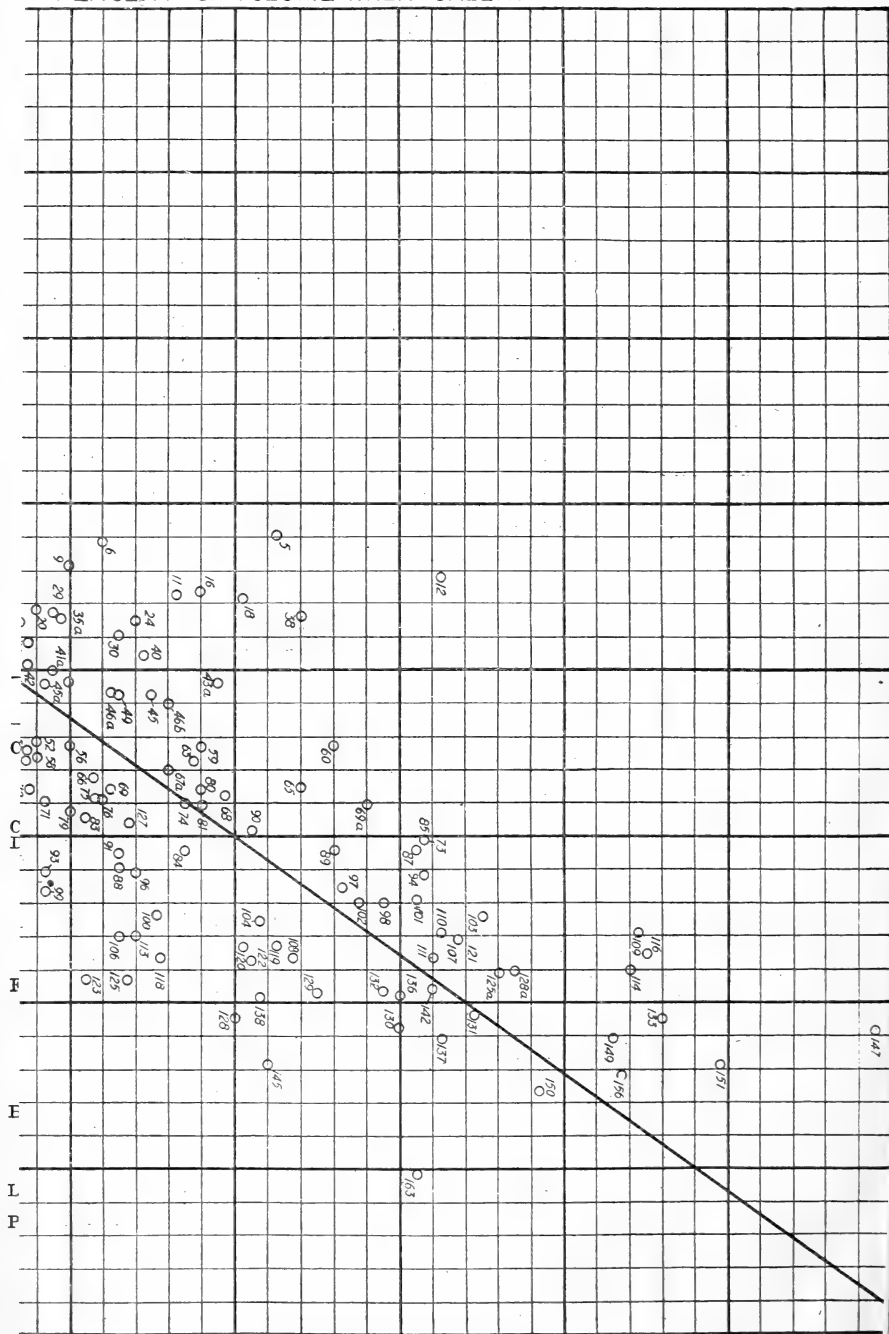
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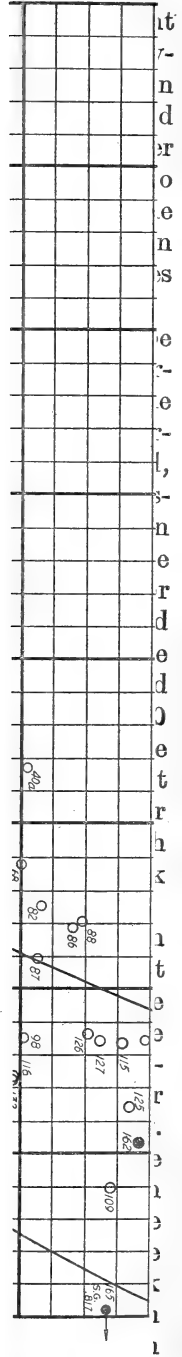
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PERCENT OF VOLUME WHEN GREEN.

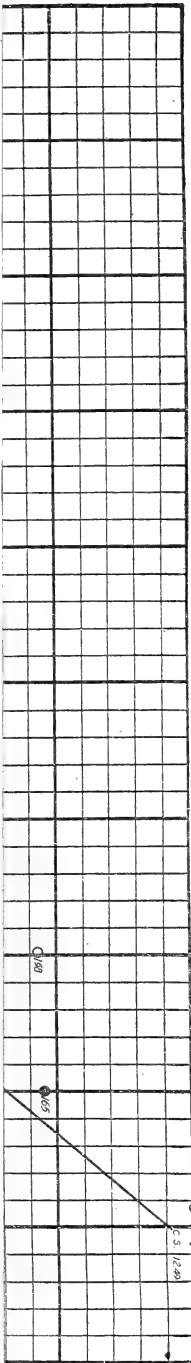


dry conditions to specific gravity.

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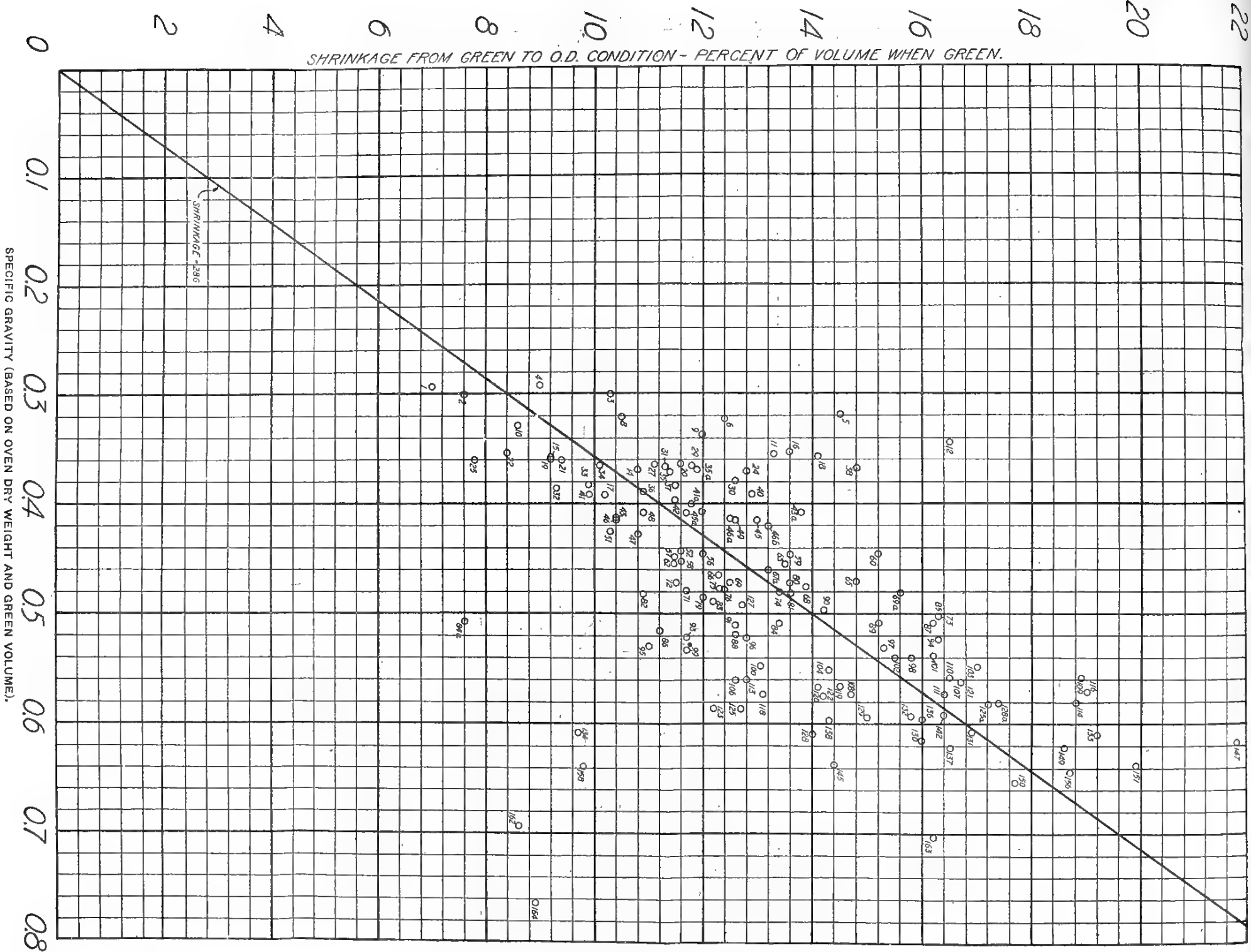


Fig. 6.—Relation of shrinkage from green to oven dry conditions to specific gravity.

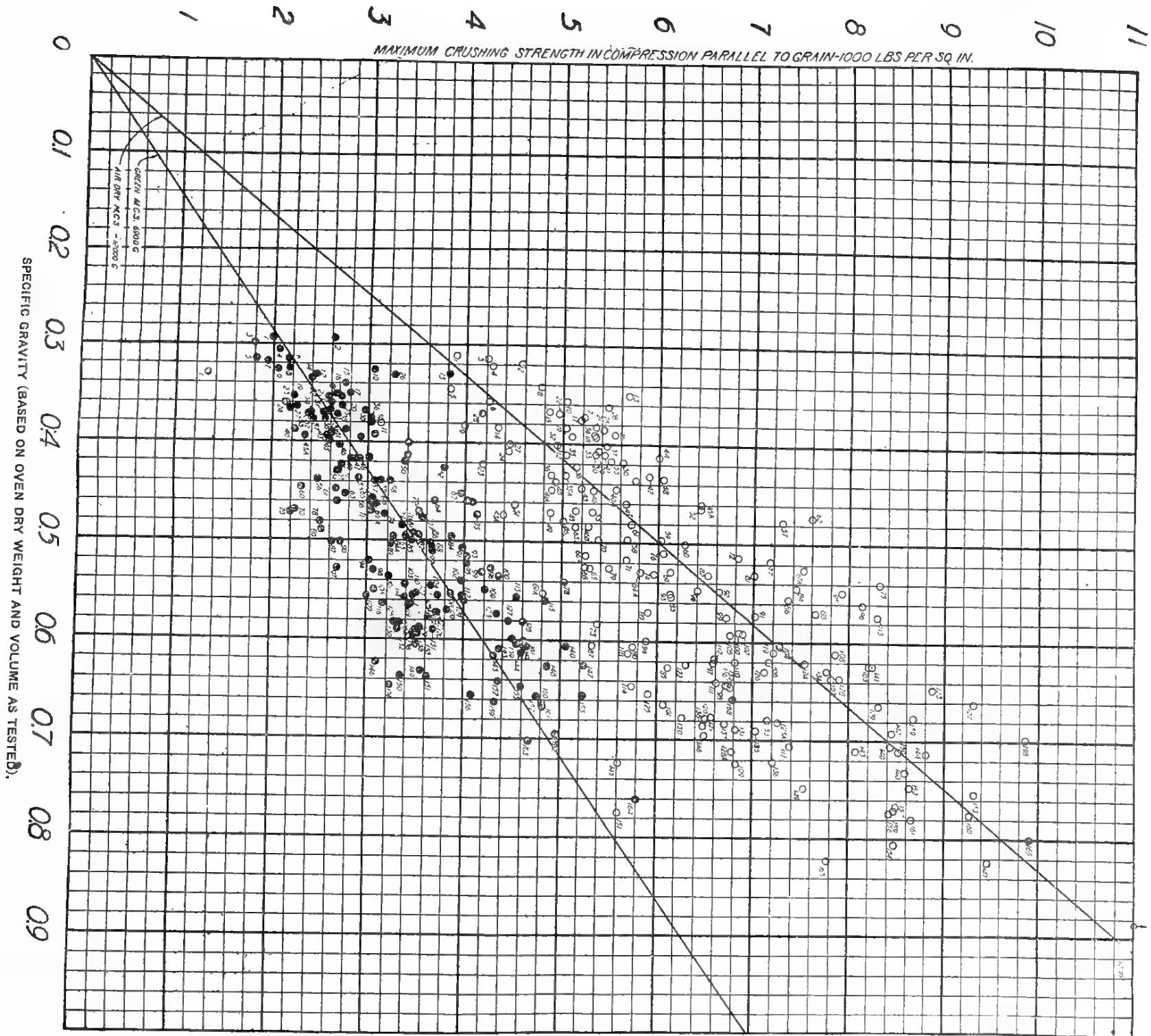
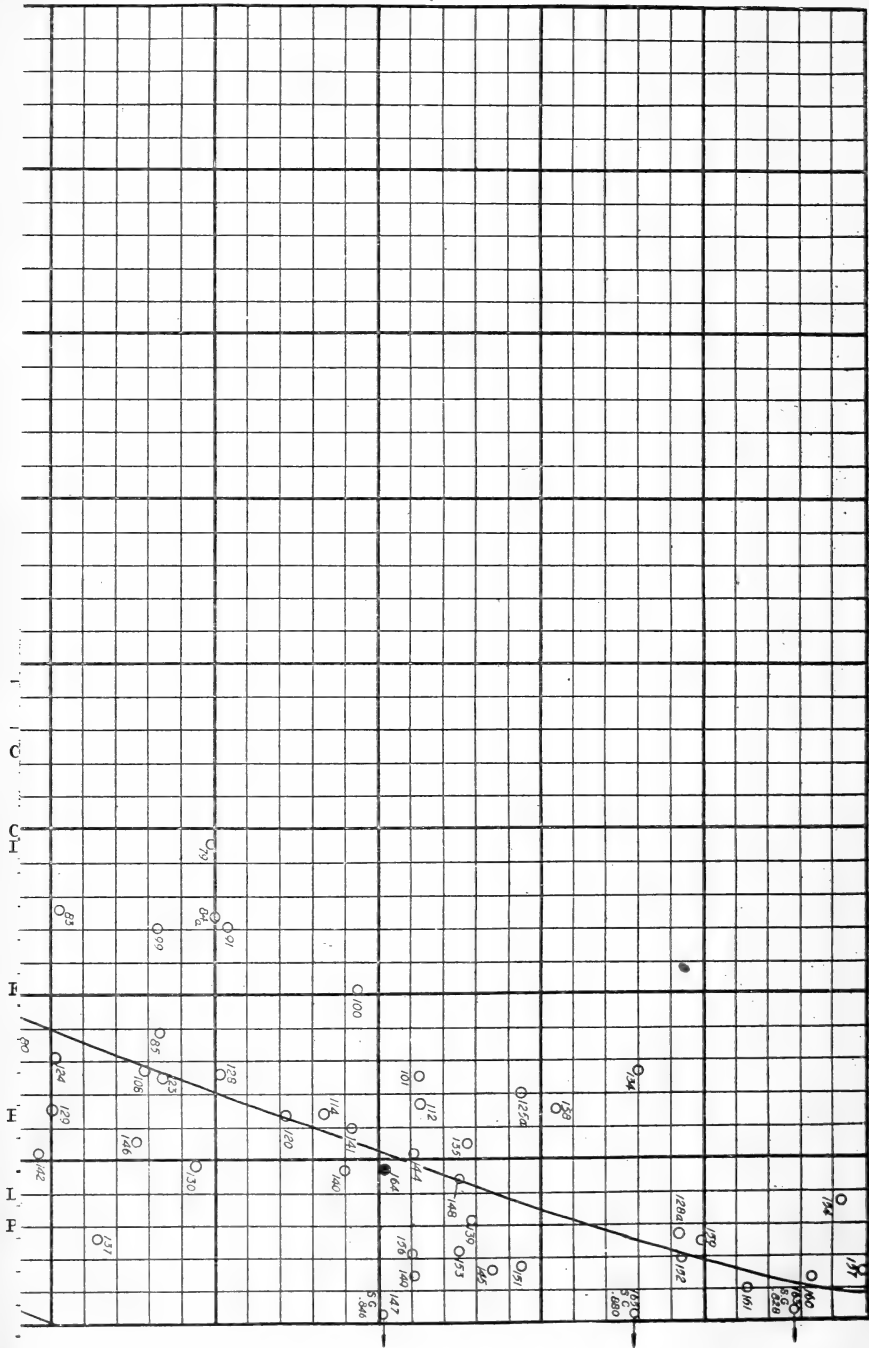
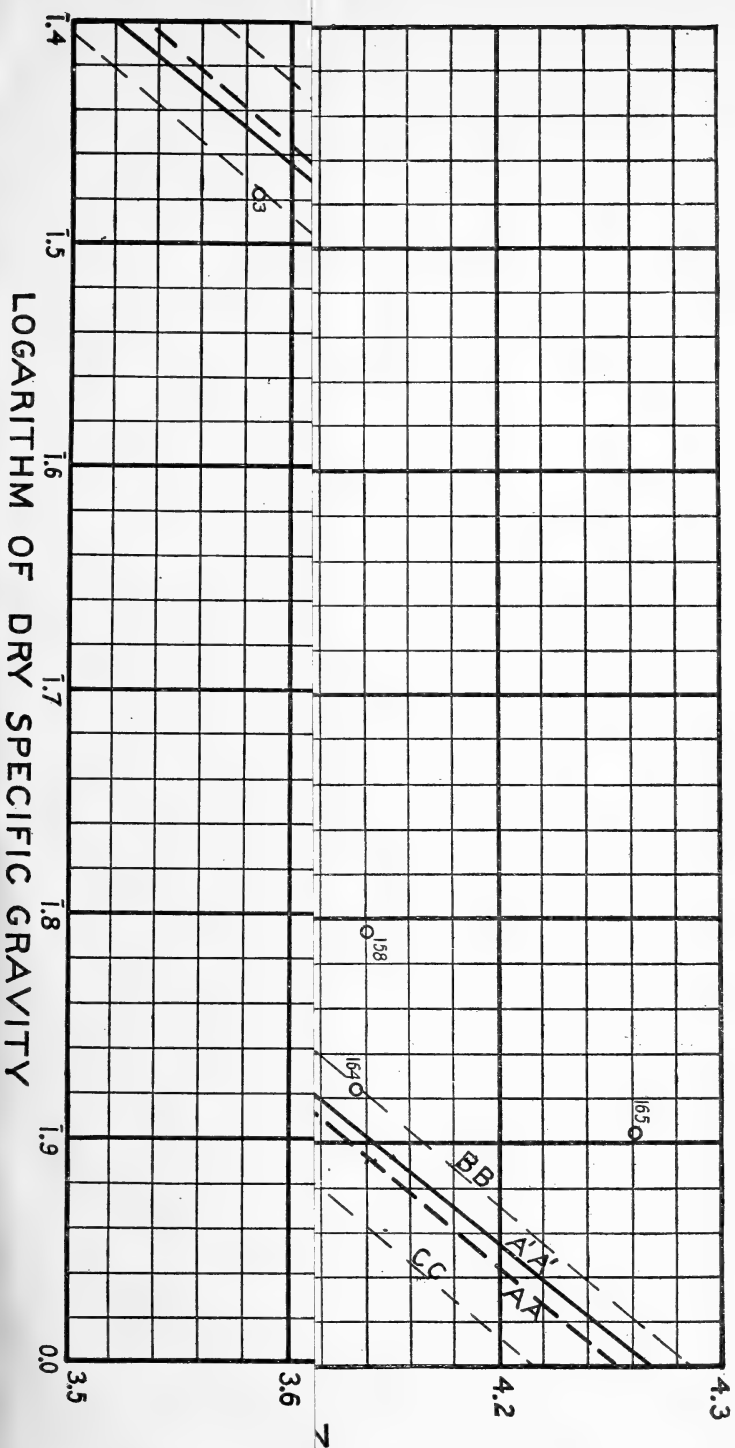


FIG. 7.—Maximum crushing strength in compression parallel to grain to specific gravity.

ULAR TO GRAIN-100 LBS. PER SQ. IN.



ular to grain to specific gravity.



FIBER STRESS AT ELASTIC LIMIT IN COMPRESSION PERPENDICULAR TO GRAIN-100 LBS. PER SQ. IN.

SPECIFIC GRAVITY (BASED ON OVEN DRY WEIGHT AND VOLUME AS TESTED).

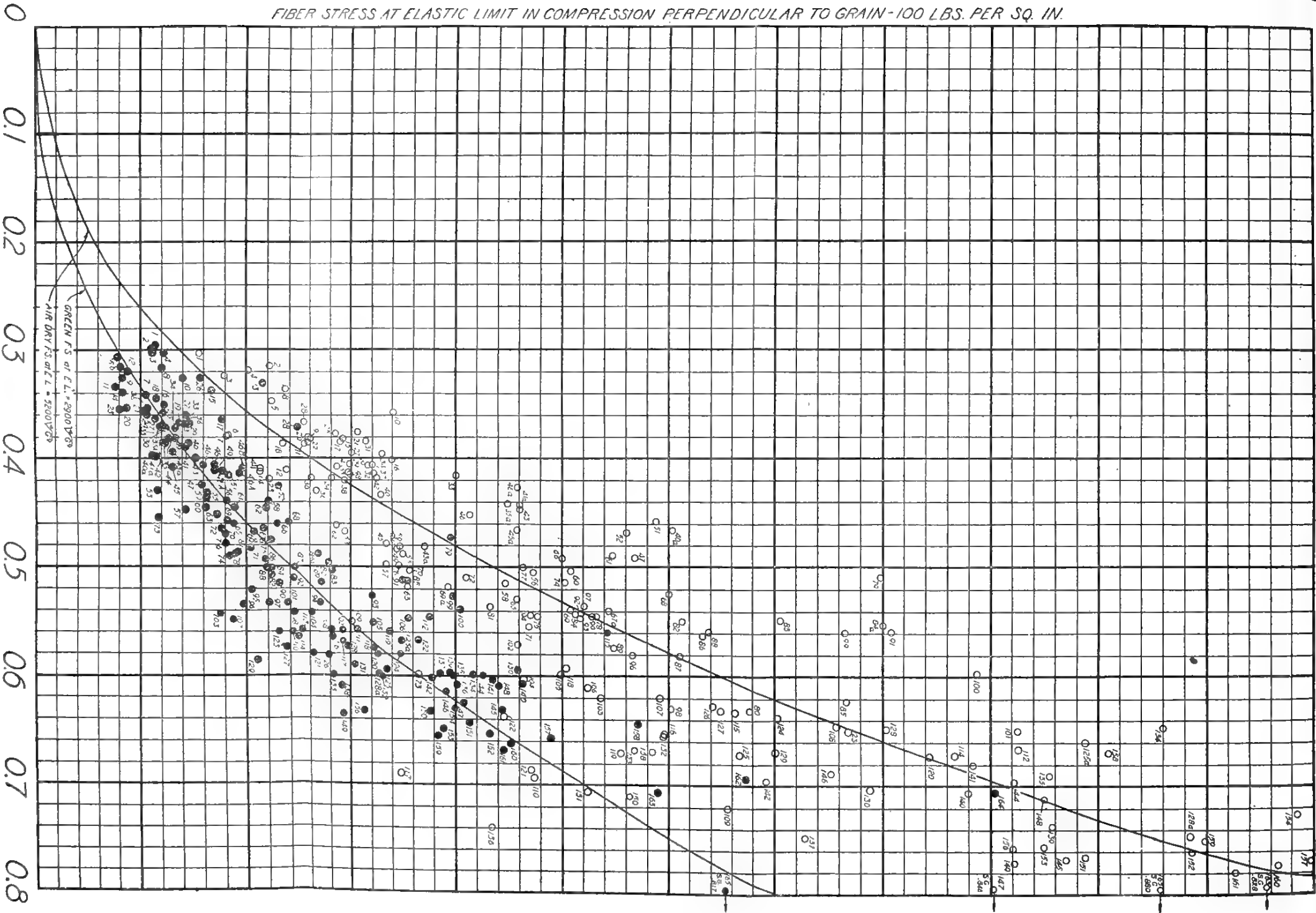


Fig. 8.—Relation of fiber stress at elastic limit in compression perpendicular to grain to specific gravity.

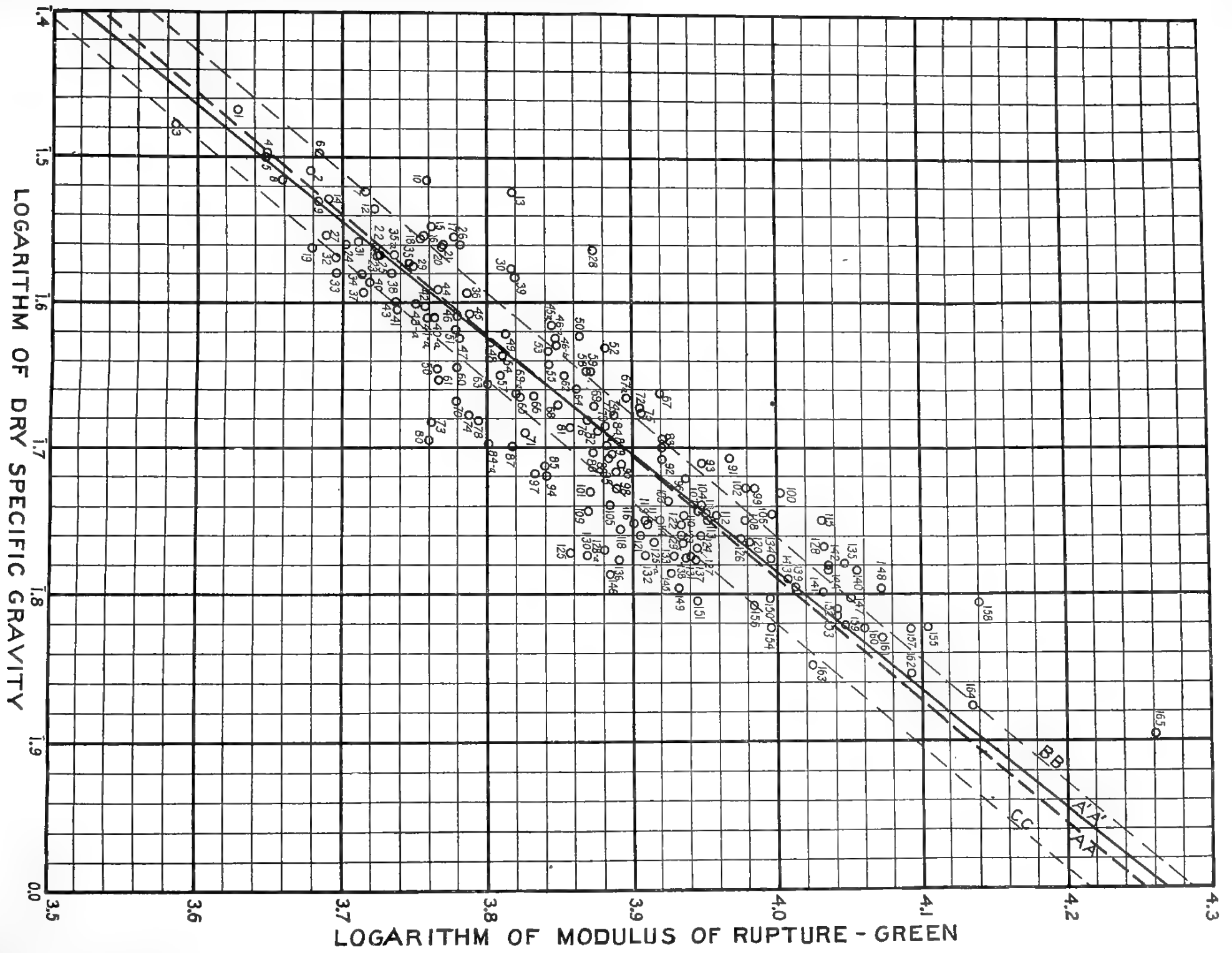


FIG. 9.

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APPLICATION OF THE EQUATIONS.

Additional data may possibly necessitate the making of some slight changes in the equations given in Table 1 and the diagrams. However, for comparing species and for determining the best utilization of timber, the value of the equations as they are now is not affected by this possibility. It is to be expected that among a large number of species of widely different structure many will be found which do not satisfy very accurately the average equations connecting the various properties with specific gravity. It is often this variation from an average relation which determines the usefulness of a species for a special purpose.

As an example of the use to which the table and diagrams may be put, suppose it is desired to obtain the strength in compression parallel to the grain of a piece of green hemlock (eastern) grown in the southern Appalachian region. Its specific gravity may be determined by any one of several means which may readily be devised, and we will say that it is found to be 0.38. In the table, the "species-locality" which is probably most nearly representative of the region in question is the eastern hemlock from Tennessee, and of this the maximum crushing strength is 29 per cent above the average for woods of the same specific gravity. To find what an average wood of a specific gravity of 0.38 will stand in compression parallel to the grain, we solve the equation $C = 6,900 \times 0.38$, or turn to figure 1 and read from the curve a maximum crushing strength of about 2,600 pounds per square inch. But since the compressive strength of the Tennessee hemlock was 29 per cent high, it is reasonable to expect that the timber in question will also run about 29 per cent high, or that the value would be about 3,300 or 3,400 pounds per square inch ($2,600 \times 1.29 = 3,354$). Any of the other properties of the hemlock under consideration may be estimated in a similar manner.

Again, suppose it is desired to obtain a wood for a use which requires that it be very strong for its weight in its ability to resist a splitting force. Tension perpendicular to grain is the best measure of this. By looking down the column, "Tension, surface of failure radial," it is found that in ability to resist such a force, yellow buckeye is 17 per cent stronger when green and 120 per cent stronger when air-dry than is the average wood of the same specific gravity. It would appear at first that yellow buckeye is the most desirable wood for the purpose, but there is another consideration to be taken into account. Tension perpendicular to the grain varies with the square of the specific gravity; and it must be remembered that those properties (such as tension perpendicular to grain, hardness, work values, and compression perpendicular to the grain) which vary with the higher powers of specific gravity show a large increase in strength

with a comparatively small increase in specific gravity. For instance, a wood with twice the specific gravity of another would be expected to have four times as much strength in tension. Yellow buckeye is a very light wood and woods of more than double its specific gravity may easily be found. Such woods, even though they may run somewhat less in tension strength than the average wood of their weight, may have a tension strength considerably in excess of that of yellow buckeye. Thus, the red oaks, having a specific gravity of about twice that of yellow buckeye, are several times as strong in tension perpendicular to the grain, although they are very little above the average wood of their weight in this respect.

It may be seen from these examples that in comparing different timbers or species, in estimating their various properties, and in finding species with exceptional strength in some properties which may render them valuable for special uses, a knowledge of the specific-gravity strength relations is a valuable aid. It must be borne in mind, however, that such equations can never take the place of tests of species whose properties are unknown. If any particular mechanical property is known, the specific gravity may be approximated and the other properties estimated; even the properties of woods upon which no test data are available can be estimated with a fair degree of accuracy from the results of specific gravity determinations. Nevertheless, it is apparent from a study of the table and diagrams that no one kind of test can replace a complete series of tests.

APPENDIX.

METHOD OF DERIVING EQUATIONS.

In plotting the various points to a natural scale (i. e., the shrinkage or a given mechanical property vs. specific gravity) it was found that in many cases they arranged themselves in the form of a curve, or if their trend was along a straight line, this line would not pass through the origin. Assuming that the function should pass through the origin, i. e., that a piece of wood of zero weight or specific gravity should have zero strength, it was found that in practically every case a curve of the form $f=pG^n$ (where f is the strength value, G the specific gravity, and p and n are constants) would fit the points quite well. This equation is the general equation of the parabola of the n th degree passing through the origin.

In order to simplify the determination of the proper values for the constants p and n the equation was transformed into the logarithmic form, $\log f = \log p + n \log G$. This equation represents a straight line having its slope equal to n and its intercept on the y axis equal to $\log p$. Consequently, to find the constants p and n it is only necessary to plot $\log f$ against $\log G$ on ordinary cross-section paper and find the straight line which best averages the points; then n and $\log p$ are determined from the slope and intercept of this line.

To find the straight line which best averages the points in the logarithmic plot the following plan was adopted:

By successive trials the parallel lines BB and CC (see fig. 9) were so located that 25 per cent of the points were above BB and 25 per cent were below CC and at the same time the vertical distance between the two was a minimum. Two lines (not shown on the figure) were then drawn as follows: Both parallel to BB and CC, one bisecting the distance between them and the other in such a position that 50 per cent of the points were on each side of it. AA was then drawn midway between these two lines and assumed to be the line which best averages the points and best represents the relation between specific gravity and the strength property in question. This method, as can readily be seen, is very likely to produce values of n such that the resulting equations can not be handled without the use of logarithms. As the slope of the lines could in most cases be varied through a considerable angle without appreciably affecting the distance between the lines BB and CC, the slope was so taken that n would be a fraction with the denominator 1, 2, 3, or 4. The solution of the equation is then possible by using the rules for the extraction of square and cube roots. Whenever it happened that more than one direction of the lines BB and CC fulfilled the conditions outlined above, preference was given to that slope which would simplify the form of the equation. The constant p was changed at the same time, so that the new line A'A' passed as nearly through the center of gravity of the points as possible.

The analytical process known as the "method of least squares" can be applied to determining the mathematical relations between two properties of a substance as ascertained from experimental results. This method was used in one or two instances to determine the specific gravity strength relations; but it was found that the long and refined computations essential to the application of this method to so large a number of tests was not justified by the added accuracy of the final determinations. Especially is this true since it is desirable to obtain n to the nearest 0.125 only, and since undue refinement in the value of the constant p is unnecessary in view of the fact that there is a considerable variation of actual results from the values given by any equation which may be derived.

II.—MEASURE OF ACCURACY OF RESPECTIVE EQUATIONS.

Proportion of species-locality.	Percentage of equation value.																									
	119	128	127	123	114	127	139	149	148	118	122	135	142	130	119	133	136	121	121	120	119	117	130	134	135	140
10 per cent above, per cent.	119	128	127	123	114	127	139	149	148	118	122	135	142	130	119	133	136	121	121	120	119	117	130	134	135	140
25 per cent above, per cent.	110	116	109	112	108	113	117	123	123	110	109	121	118	115	111	117	115	110	111	111	109	109	118	116	118	127
25 per cent below, per cent.	90	88	89	91	91	89	86	83	75	90	90	85	86	86	90	86	88	87	88	90	83	89	83	81	80	74
10 per cent below, per cent.	80	77	79	79	84	76	72	70	60	84	86	71	76	73	83	72	77	70	78	81	89	83	68	58	55	51
10 per cent above, per cent.	126	113	122	164	139	167	130	120	143	145	145	116	142	133	131	124	120	125	122	144	141	139	141	139	141	
25 per cent above, per cent.	111	106	110	135	117	130	112	110	125	120	127	108	120	118	115	111	112	110	126	121	127	122	127	127	122	
25 per cent below, per cent.	85	89	90	75	83	72	85	89	78	83	82	88	86	86	83	85	83	85	94	91	90	88	78	79	69	85
10 per cent below, per cent.	75	80	81	60	66	58	73	81	63	70	68	81	67	74	79	83	83	79	83	83	79	78	56	64	54	

III.—ACTUAL VALUE OF EACH PROPERTY FOR EACH "SPECIES-LOCALITY" AS DETERMINED BY TESTS—EXPRESSED IN PERCENTAGE OF EQUATION VALUE.

Alder, red (Washington); Green; Air-dry.	30	119	125	117	122	119	123	139	131	102	119	127	128	117	136	117	138	98	137	119	128	108	110	125	138	139	137
Ash, Baltimore (Tennessee); Green; Air-dry.	91	88	87	80	124	116	104	142	104	88	120	110	130	86	123	114	103	135	121	121	125	124	110	119	109	106	98
Ash, black (Michigan); Green; Air-dry.	60	122	118	103	70	90	100	61	139	144	82	88	81	123	66	76	88	86	100	101	103	100	88	132	86	131	98
Ash, black (Wisconsin); Green; Air-dry.	70	80	84	82	128	117	131	92	130	229	87	69	114	99	174	136	105	115	114	130	114	132	148	106	144	124	169
Ash, blue (Kentucky); Green; Air-dry.	99	84	77	72	120	113	92	146	121	117	102	87	117	108	115	114	86	144	135	135	138	141	128	96	108	92	101

TABLE 1.—Equations and variations—specific gravity, shrinkage, and strength relations based on tests of small clear pieces, green and air-dry—Con.

Species and locality.	Reference number.	Specific gravity, oven-dry, based on		Moisture content.	Shrinkage from green to oven-dry condition.	Static bending.								Impact bending, 50-pound hammer.				Compression parallel to grain.			Hardness: load required to embed a 0.444-inch ball one-half its diameter.		Shear.		Cleavage.		Tension.															
		Per cent.	Per cent of dimensions when green.			Lbs. per sq. in.	Fiber stress at elastic limit.	Lbs. per sq. in.	Modulus of rupture.	Modulus of elasticity.	Lbs. per sq. in.	Fiber stress at elastic limit.	Modulus of elasticity.	Inch lbs. per cu. in.	Work to maximum load.	Total work.	Inch lbs. per cu. in.	Work to elastic limit.	Modulus of elasticity.	Work to elastic limit.	Inches.	Height of drop causing complete failure.	Fiber stress at elastic limit.	Lbs. per sq. in.	Maximum strength.	Modulus of elasticity.	Lbs. per sq. in.	Compression perpendicular to grain.	Lbs. per sq. in.	Fiber stress at elastic limit.	Lbs. per sq. in.	Fiber stress at elastic limit.	Modulus of elasticity.	Lbs. per sq. in.	Surface of failure.	End surface.	Radial surface.	Tangential surface.	Lbs. per sq. in.	Surface of failure.	Lbs. per sq. in.	Surface of failure.

III.—ACTUAL VALUE OF EACH PROPERTY FOR EACH "SPECIES-LOCALITY" AS DETERMINED BY TESTS—EXPRESSED IN PERCENTAGE OF EQUATION VALUE—Continued.

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30						
Ash, green (Louisiana):																																				
Green:																																				
Air-dry:	93				80																															
Ash, pumpkin (Missouri):																																				
Green:																																				
Air-dry:	100				87	90	78	128	118	110	139	104	92	103	102	108	83	105	97	104	135	125	130	112	124	120	109	103	98	100	87	87	87			
Ash, white (Missouri):																																				
Green:																																				
Air-dry:	79				88	80	77	107	101	86	130	94	69	90	101	117	92	103	100	89	180	121	119	112	124	112	124	121	125	101	101	98	98	101	101	101

Ash, white (Arkansas):	106	101	100	101	112	105	95	109	79	109	111	97	119	114	109	117	119	106	100	89	111	98
Green:	111	100	101	112	105	95	109	79	109	111	97	119	114	109	117	119	106	100	89	111	98
Air-dry:	114	102	102	122	78	88	69	81	103	98	88	76	130	128	110	120	101	161	100	100	74
Ash, white (West Virginia):	83	79	107	108	100	102	111	130	115	119	101	140	111	105	92	100	130	140	118	111	117	113
Green:	106	100	102	119	113	120	115	111	120	115	99	145	98	100	126	124	100	118	58	150	117
Air-dry:	87	108	103	111	130	115	119	101	120	115	140	111	105	100	126	124	100	118	58	150	117
Ash, white (New York):	128	82	96	113	111	108	111	130	111	108	111	140	111	105	92	100	130	140	118	111	117	113
Green:	118	105	102	130	104	76	116	108	121	99	137	103	94	106	121	117	126	111	109	80	142
Air-dry:	82	96	88	113	111	92	114	102	115	99	111	103	96	106	112	111	129	119	103	105	112
Aspen (Wisconsin):	23	106	96	113	98	99	90	135	117	125	100	96	121	86	75	92	87	89	72	68	70	55
Green:	106	96	113	98	99	90	135	117	125	100	96	121	86	75	92	87	89	72	68	70	55
Air-dry:	114	92	132	109	111	129	106	106	86	112	107	135	96	115	111	124	120	130	135	135	144
Aspen, largetooth (Wisconsin):	20	114	92	132	109	111	129	106	106	86	112	107	135	96	115	111	124	120	130	135	135	144
Green:	117	107	133	128	104	128	131	122	166	146	143	110	121	106	114	100	121	100	131	101	100
Air-dry:	171	215	176	105	108	133	98	97	108	106	112	120	104	120	107	152	98	106	105	103	123
Basewood (Pennsylvania):	12	171	215	176	105	108	133	98	97	108	106	112	120	104	120	107	152	98	106	105	103	123
Green:	135	115	127	135	115	127	177	177	172	140	136	180	137	165	102	128	85	93	90	97	150
Air-dry:	162	206	156	101	101	106	126	135	102	97	97	122	114	73	84	113	96	103	115	130	132
Basewood (Wisconsin):	5	162	206	156	101	101	106	126	135	102	97	97	122	114	73	84	113	96	103	115	130	132
Green:	113	90	157	108	64	91	62	108	51	55	75	93	185	117	108	123	115	150	159	194	144
Air-dry:	105	87	111	90	96	96	86	106	81	103	90	108	98	107	91	91	104	106	97	130	135
Beech (Indiana):	110	105	87	111	90	96	96	86	106	81	103	90	108	98	107	91	91	104	106	97	130	135
Green:	78	108	99	67	110	123	92	94	87	98	87	98	67	93	97	98	94	98	128	123	140
Air-dry:	105	101	118	95	91	84	100	88	69	83	87	74	92	76	84	80	83	102	117	106	122
Green:	93	90	90	83	104	73	71	105	101	110	73	90	87	84	82	83	97	94	103	101	50
Air-dry:	116	147	109	70	78	84	59	151	146	82	82	77	137	62	68	71	76	78	87	83	66
Birch, paper (Wisconsin):	73	116	147	109	70	78	84	59	151	146	82	82	77	137	62	68	71	76	78	87	83	66
Green:	90	113	76	86	91	102	62	107	86	81	97	62	94	76	88	101	94	98	83	86	73
Air-dry:	119	105	109	121	102	53	132	117	128	106	109	150	150	109	150	150	134	120	96	102	61
Birch, sweet (Pennsylvania):	129	119	105	109	121	102	53	132	117	128	106	109	150	150	109	150	150	134	120	96	102	61
Green:	106	131	94	100	99	107	90	144	125	110	100	115	106	91	92	95	86	93	88	88	74
Air-dry:	105	104	106	102	144	88	119	118	88	119	118	114	142	129	102	82	104	103	118	66	55
Birch, yellow (Pennsylvania):	107	106	131	94	100	99	107	90	144	125	110	100	115	106	91	92	95	86	93	88	88	74
Green:	111	152	97	86	97	117	59	112	85	96	107	80	81	81	90	123	83	86	83	71	72
Air-dry:	127	118	129	127	118	129	123	119	119	97	109	88	130	121	110	108	76	90	104	121	142
Birch, yellow (Wisconsin):	103	111	152	97	86	97	117	59	112	85	96	107	80	81	81	90	123	83	86	83	71	72
Green:	127	118	129	127	118	129	123	119	119	97	109	88	130	121	110	108	76	90	104	121	142
Air-dry:	127	118	129	127	118	129	123	119	119	97	109	88	130	121	110	108	76	90	104	121	142

Butternut (Wisconsin): Green.....	21	93	107	95	108	113	110	130	149	177	107	110	123	121	115	106	123	90	112	121	121	114	119	124	108	110	137	121	115	154	145	159	159	125	116		
Chinquapin, western (Oregon): Green.....	466	112	116	105	119	110	95	169	123	106	110	100	128	126	85	105	128	125	135	137	114	119	124	108	110	137	121	115	154	145	159	159	125	116			
Cherry, black (Pennsylvania): Green.....	72	87	82	89	103	111	111	102	135	125	110	105	123	107	111	109	114	86	117	121	112	115	117	128	114	130	87	115	138	81	92	87	87	87			
Cherry, wild red (Tennessee): Green.....	24	124	81	168	99	96	115	100	110	137	98	107	105	118	96	87	103	90	110	108	112	93	101	109	106	104	106	106	109	106	125	132	87	90	106		
Chestnut (Maryland): Air-dry.....	46	90	86	97	100	112	104	103	142	82	79	90	100	97	85	115	128	102	119	101	108	105	95	85	112	93	113	94	128	125	149	132	149	132	94	132	
Chestnut (Tennessee): Green.....	40	118	92	103	90	93	94	100	106	103	104	98	124	107	91	83	86	107	116	105	110	103	89	130	111	123	112	110	133	111	110	127	110	127	110	127	
Cottonwood, black (Washington): Green.....	6	109	120	161	117	111	135	121	118	149	119	124	144	139	111	99	126	93	101	103	106	100	105	125	146	117	132	125	146	117	132	146	117	132	146	117	
Cucumber tree (Tennessee): Green.....	59	109	124	118	112	110	140	94	119	101	109	127	100	111	114	103	133	90	93	93	90	105	117	110	112	107	106	110	112	107	123	182	182	106	106		
Dogwood, flowering (Tennessee): Green.....	151	111	116	104	82	84	74	77	121	94	52	43	56	99	83	83	67	87	104	118	115	102	103	96	71	101	137	103	103	103	103	103	103	103	103	103	
Dogwood, western (Oregon): Green.....	125a	106	116	97	80	88	75	77	117	89	82	87	71	119	66	91	93	106	112	110	106	98	105	78	86	104	102	102	102	102	102	102	102	102	102	102	
Elder, pale (Oregon): Green.....	69b	116	99	115	87	94	78	96	97	149	85	88	85	120	95	95	111	99	124	135	135	115	105	139	96	126	108	108	108	108	108	108	108	108	108	108	
Elm, cork (Wisconsin, Marathon County): Green.....	126	83	101	85	77	137	111	101	131	113	101	79	128	101	94	94	87	88	83	80	93	94	99	101	76	87	120	103	103	103	103	103	103	103	103	103	
Elm, cork (Wisconsin, Marathon County): Air-dry.....	126	75	105	93	59	131	113	94	94	113	94	94	91	120	79	94	87	88	83	80	93	94	99	101	76	87	120	103	103	103	103	103	103	103	103	103	103

TABLE 1.—Equations and variations—specific gravity, shrinkage, and strength relations based on tests of small clear pieces, green and air-dry—Con.

Species and locality.	Shrinkage from green to oven-dry condition.			Static bending.				Impact bending, 50-pound hammer.				Compression parallel to grain.				Hardness: load required to embed a 0.444-inch ball one-half its diameter.			Shear.		Cleavage.		Tensile.																		
	In volume.	Radial.	Tangential.	Fiber stress at elastic limit.	Lbs. per sq. in.	Modulus of elasticity.	Wk to elastic limit.	Inch lbs. per cu. in.	Wk to maximum load.	Inch lbs. per cu. in.	Total work.	Fiber stress at elastic limit.	Lbs. per sq. in.	Modulus of elasticity.	1,000s of lbs. per sq. in.	Lbs. per sq. in.	Fiber stress at elastic limit.	Height of drop causing complete failure.	Inches.	Lbs. per sq. in.	Maximum crushing strength.	1,000s of lbs. per sq. in.	Modulus of elasticity.	Compression perpendicular to grain.	Lbs. per sq. in.	End surface.	Lbs.	Radial surface.	Lbs.	Tangential surface.	Lbs. per sq. in.	Surface of failure radial.	Lbs. per sq. in.	Surface of failure tangential.	Lbs. per sq. in.	Surface of failure radial.	Lbs. per sq. in.	Surface of failure tangential.			
Reference number.	Per cent.			Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.		
Specific gravity, oven-dry, based on moisture content.	Per cent.			Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.

III.—ACTUAL VALUE OF EACH PROPERTY FOR EACH "SPECIES-LOCALITY" AS DETERMINED BY TESTS—EXPRESSED IN PERCENTAGE OF EQUATION VALUE—Continued.

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
Elm, cork (Wisconsin, Rusk County): Green..... 120 Air-dry.....				89	89	84	93	102	80	100	139	122	90	92	78	108	86	97	84	95	100	108	108	97	97	104	88	97	83
Elm, slippery (Indiana): Green..... 102 Air-dry.....				103	99	107	118	113	98	130	95	126	109	99	115	102	108	106	94	92	112	104	94	110	99	128	115	142	128
Elm, slippery (Wisconsin): Green..... 74 Air-dry.....				100	108	108	92	105	101	90	164	172	94	95	94	156	102	97	95	80	106	108	111	120	106	151	131	143	119
				100	108	108	109	100	95	132	154	207	112	100	135	147	111	94	99	108	101	93	104	110	102	95	83	81	45

TABLE 1.—Equations and variations—specific gravity, shrinkage, and strength relations based on tests of small clear pieces, green and air-dry—Con.

Species and locality.	Shrinkage from green to oven-dry condition.		Static bonding.						Impact bonding, 50-pound hammer.				Compression parallel to grain.			Hardness: load required to embed a 0.444-inch ball one-half its diameter.			Shear.		Cleavage.		Tension.					
	In volume.	Radial.	Tangential.	Lbs. per sq. in. Fiber stress at elastic limit.	Lbs. per sq. in. Modulus of elasticity.	Inch lbs. Work to elastic limit.	Inch lbs. Work to maximum.	Inch lbs. Work load.	Inch lbs. Total work.	Lbs. per sq. in. Fiber stress at elastic limit.	1,000s lbs. Modulus of elasticity.	Inch lbs. Work to elastic limit.	Height of drop causing complete failure.	Inches.	Lbs. per sq. in. Fiber stress at elastic limit.	Lbs. per sq. in. Maximum crushing strength.	1,000s lbs. Modulus of elasticity.	Lbs. per sq. in. Compression perpendicular to grain.	Lbs. End surface.	Lbs. Radial surface.	Lbs. Tangential surface.	Lbs. per sq. in. Surface of failure radial.	Lbs. per sq. in. Surface of failure tangential.	Lbs. per sq. in. Surface of failure radial.	Lbs. per sq. in. Surface of failure tangential.	Lbs. per sq. in. Surface of failure radial.	Lbs. per sq. in. Surface of failure tangential.	

III.—ACTUAL VALUE OF EACH PROPERTY FOR EACH "SPECIES-LOCALITY" AS DETERMINED BY TESTS—EXPRESSED IN PERCENTAGE OF EQUATION VALUE—Continued.

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
Oak, laurel (Louisiana):																														
Green.....		116			119	73	99	89	88	98	76	83	61	90	108	72	89	82	81	94	88	102	110	112	110	96	92	109	104	126
Air-dry.....								77	78	89	64	70	91	78	106	60	91	83	87	117	130	71	95	92	104	95	77	73	83	95
Oak, post (Arkansas):																														
Green.....		130			93	101	105	88	76	61	110	60	38	89	88	79	74	80	82	63	125	97	72	102	104	91	86	101	100	108
Air-dry.....								68	74	66	66	56	45	72	81	59	80	51	77	77	85	72	96	84	83	72	71	76	55	90
Oak, post (Louisiana):																														
Green.....		137			95	91	87	96	90	84	97	86	64	84	95	67	95	81	87	83	106	100	116	112	112	93	89	94	92	102
Air-dry.....								62	81	82	43	83	128	90	83	87	95	66	82	97	132	62	100	81	82	85	55	92	54	85
Oak, red (Arkansas):																														
Green.....		119			91	78	86	77	89	88	63	94	101	93	92	87	94	76	88	82	107	110	114	114	114	101	102	107	106	118
Air-dry.....								96	92	105	92	81	120	92	92	88	93	69	99	128	66	92	110	112	102	102	85	110	108	136

